

DE LA RECHERCHE À L'INDUSTRIE



Beyond mean field : the Bohr Hamiltonian

S. Hilaire
CEA, DAM, DIF

DE LA RECHERCHE À L'INDUSTRIE



What's the point of using it ?

GENERAL MOTIVATION

Providing nuclear reaction models with « **credible and coherent** » microscopic inputs

- makes (really) sense when dealing with unmeasured target
- the sounder the underlying physics the better the predictive power
- no direct link between xs and n-n interaction for **all nuclei**
- **many inputs** needed
 - . Discrete levels properties (masses, J, p, deformation etc ...)
 - . Nuclear level densities up to 200MeV
 - . Gamma strength functions
 - . Fission properties (barriers, broken symmetries, = path)
 - . Optical potential (spherical and deformed)
- all this can be derived from nuclear structure more or less directly
- all this can be used mostly through tables
- robust codes needed
- robust methodology (recipes)
 - . to reduce human intervention while producing tables
 - . to fill gaps (even-even limitation for instance)

GENERAL MOTIVATION

Providing nuclear reaction models with « **credible and coherent** » microscopic inputs

- makes (really) senses when dealing with unmeasured target
- the sounder the underlying physics the better the predictive power

All this has been done with Skm for all nuclei (S. Goriely) !

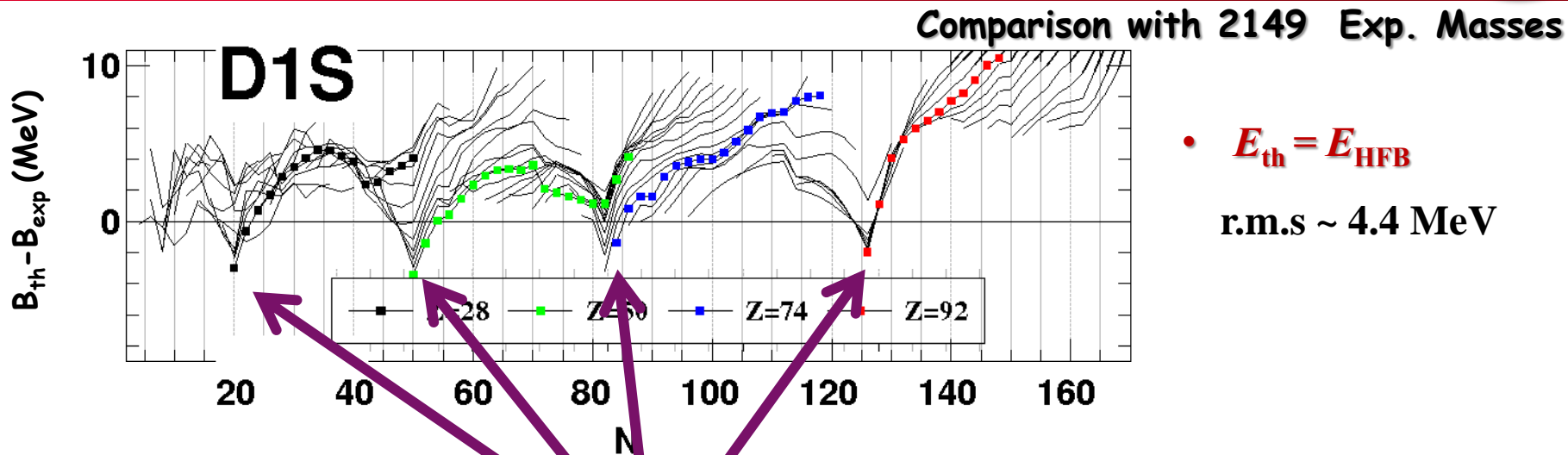
Let's do it with Gogny !

- . Optical potential (spherical and deformed)
- all this can be derived from nuclear structure more or less directly
- all this can be used mostly through tables
- robust codes needed
- robust methodology (recipes)
 - . to reduce human intervention while producing tables
 - . to fill gaps (even-even limitation for instance)

- Motivation
- The starting point : nuclear masses
- Spectroscopy
- Nuclear Reaction inputs
- Conclusions & Perspectives

THE STARTING POINT :

Nuclear masses



- $E_{th} = E_{HFB}$
- r.m.s ~ 4.4 MeV

Discussion with M. Girod :
We forgot to estimate infinite basis effect
⇒ Overbinding of 1-3 MeV

How can we compute binding energies ?

$$B = B(N_0) + \Delta_\infty$$

⇒ Infinite basis correction : code AMEDEC

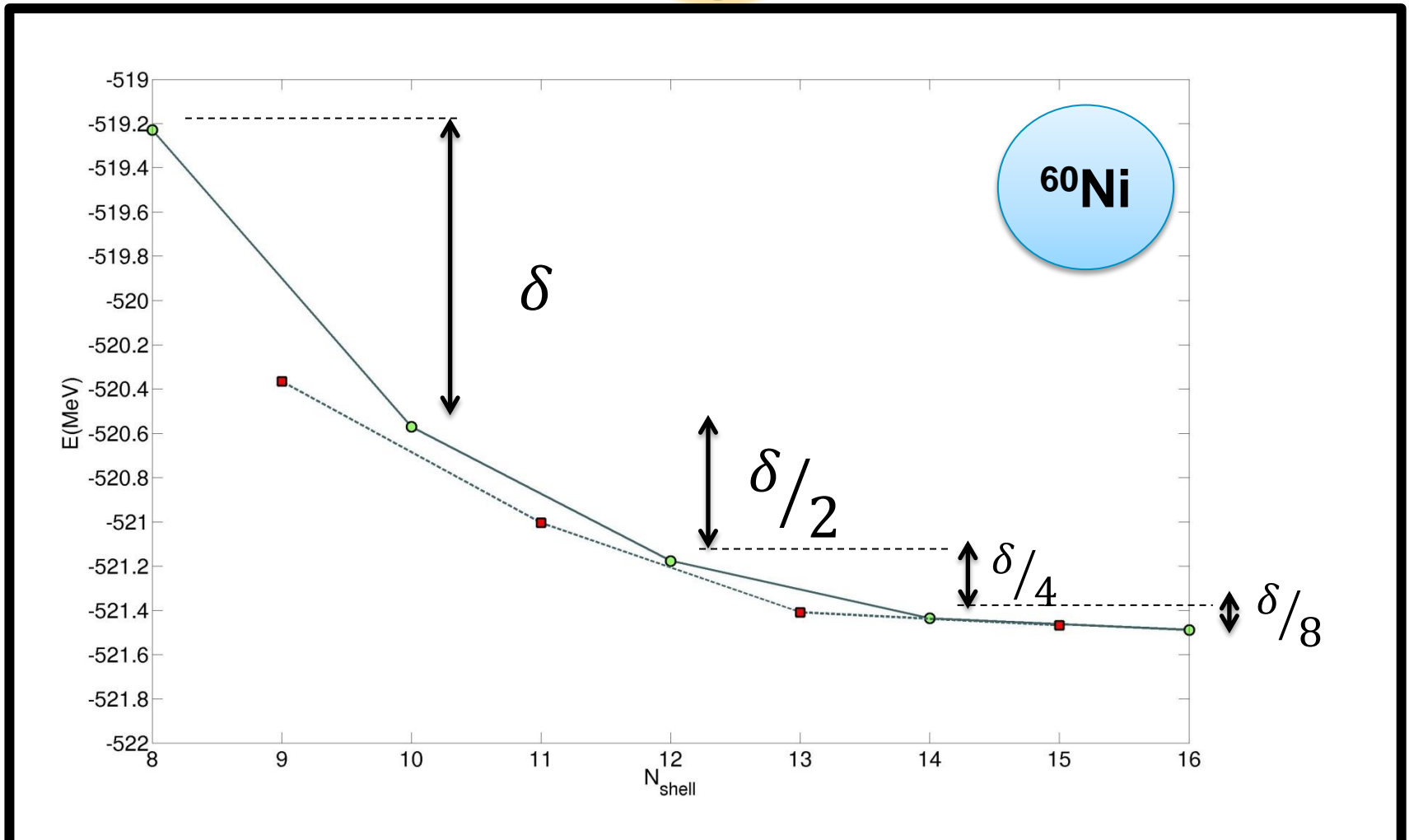
$$\Delta_\infty = E(N_0) - E(N = +\infty)$$

⇒ Assumption

$$\Delta_\infty = 2[E(N_0) - E(N_0 + 2)]$$

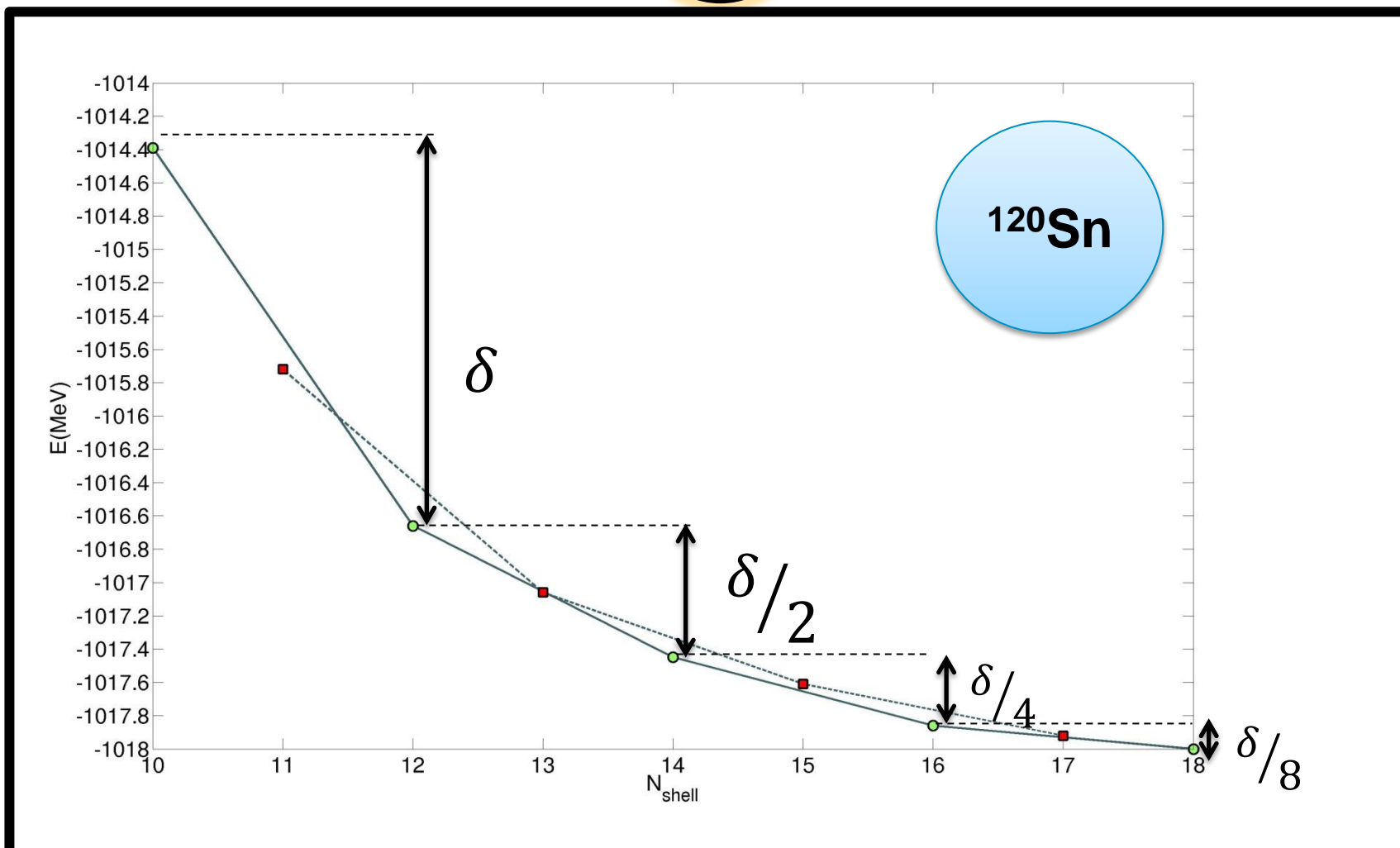
How can we compute binding energies ?

$$B = B(N_0) + \Delta_{\infty}$$

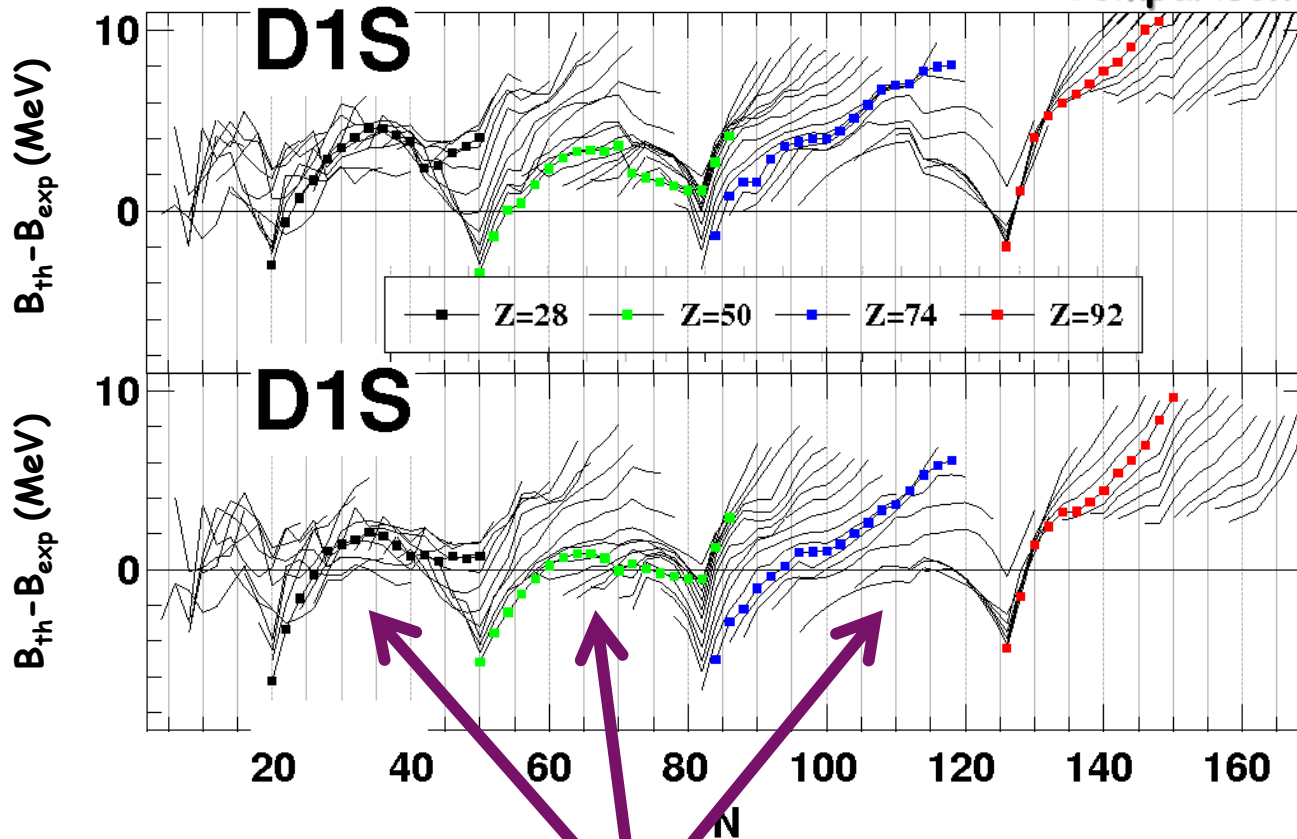


How can we compute binding energies ?

$$B = B(N_0) + \Delta_{\infty}$$



Comparison with 2149 Exp. Masses



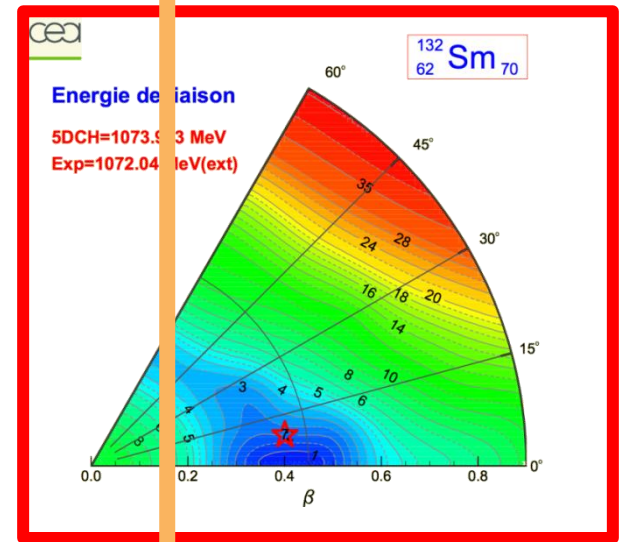
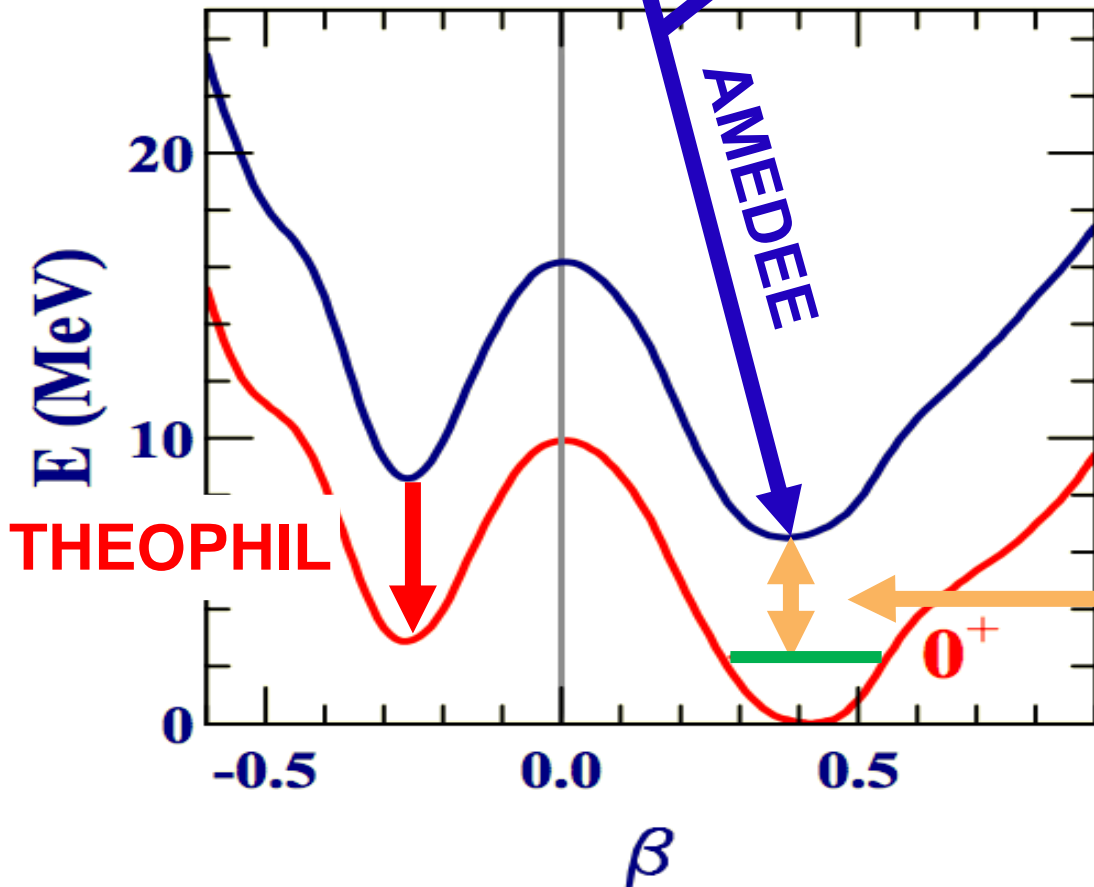
- $E_{th} = E_{HFB}$
r.m.s ~ 4.4 MeV

- $E_{th} = E_{HFB} - \Delta_{\infty}$
r.m.s ~ 2.6 MeV

Discussion with Girod :
You forgot to include bmf (quadrupole) correlations
⇒ Arches between magic nuclei

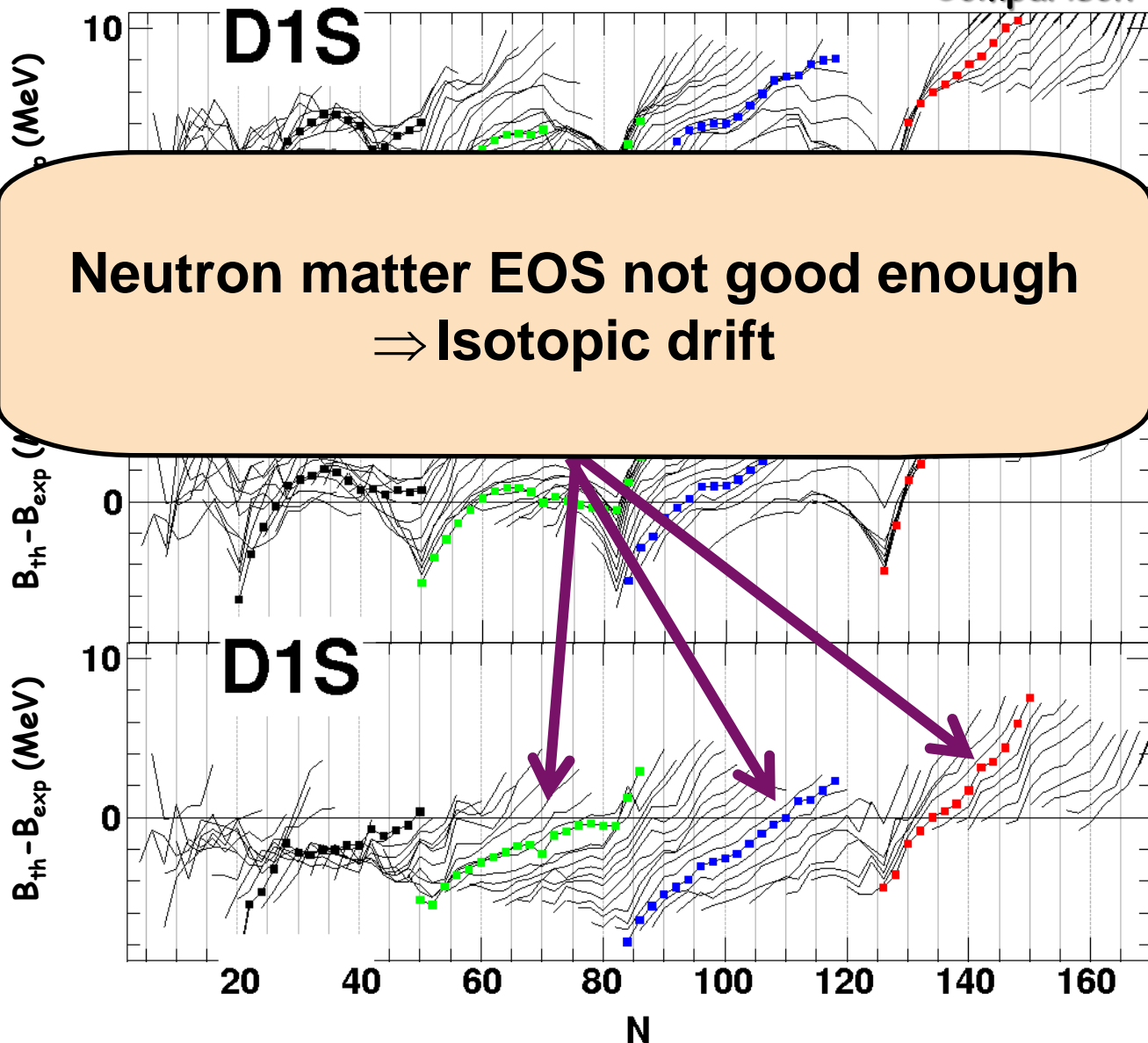
How can we compute binding energies ?

$$B = B(N_0) + \Delta_\infty + \Delta_{\text{quad}}$$



KUMAR

Comparison with 2149 Exp. Masses



Neutron matter EOS not good enough
=> Isotopic drift

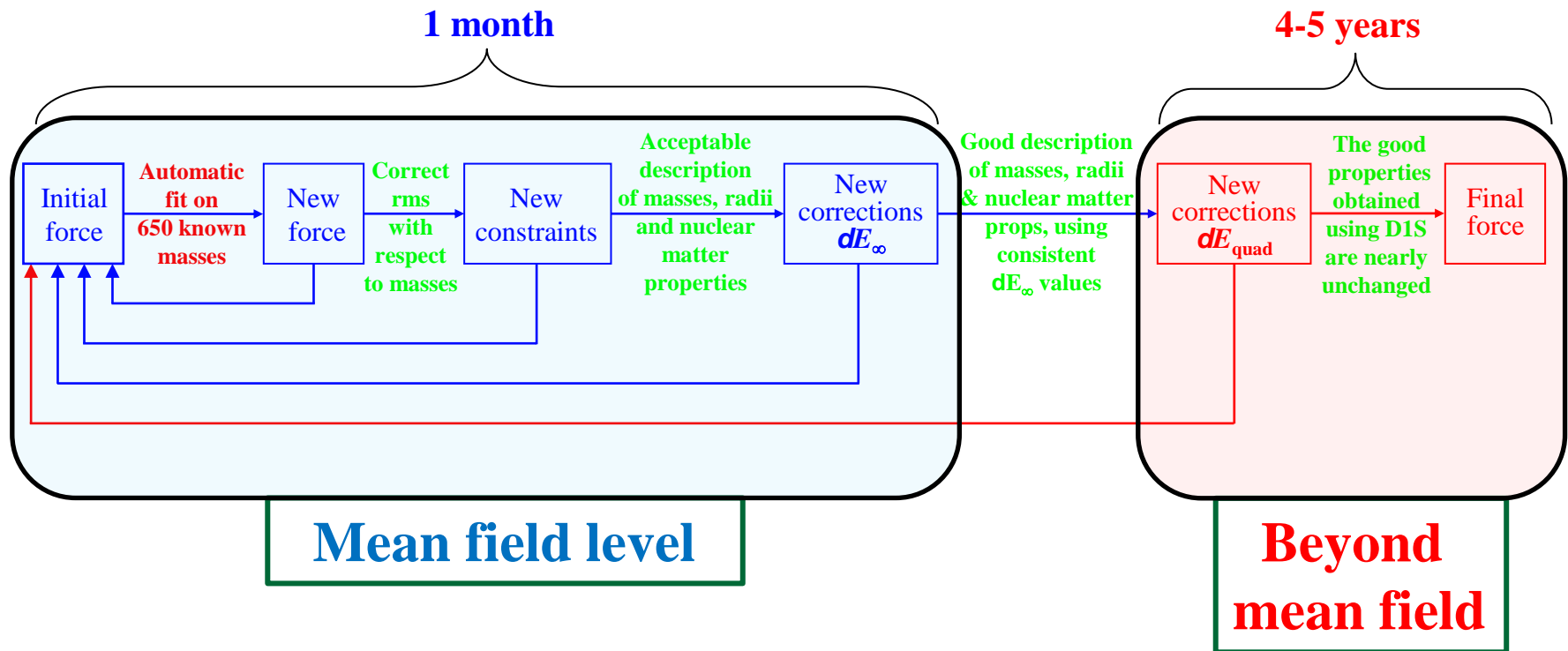
- $E_{th} = E_{HFB}$
r.m.s ~ 4.4 MeV
- $E_{th} = E_{HFB} - \Delta_{\infty}$
r.m.s ~ 2.6 MeV
- $E_{th} = E_{HFB} - \Delta_{\infty} - \Delta_{quad}$
r.m.s ~ 2.9 MeV

BASIC STRUCTURE PROPERTIES

HFB Mass models

Most advanced theoretical approach = multireference level

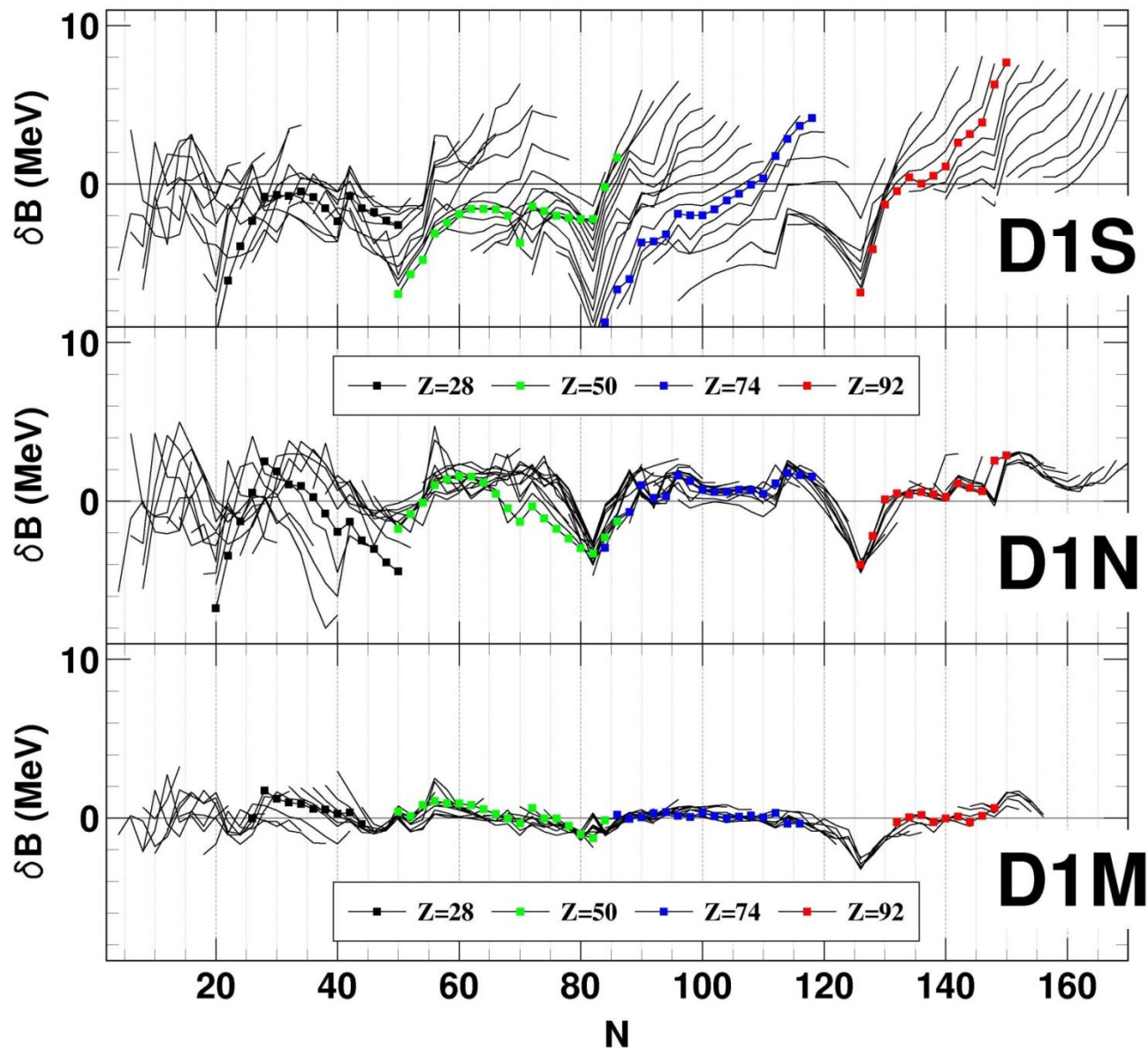
- Methodology : $E = E_{mf} + dE_{\infty} + dE_{quad}$



* Additional filters

- Collective properties ($0^+, 2^+$, BE2), RPA modes, backbending properties, pairing properties, fission properties, gamma strength functions, level densities

Major goal reached : first Gogny mass model !



r.m.s ~ 3 MeV

r.m.s ~ 1 MeV

r.m.s = 0.798 MeV

SPECTROSCOPY

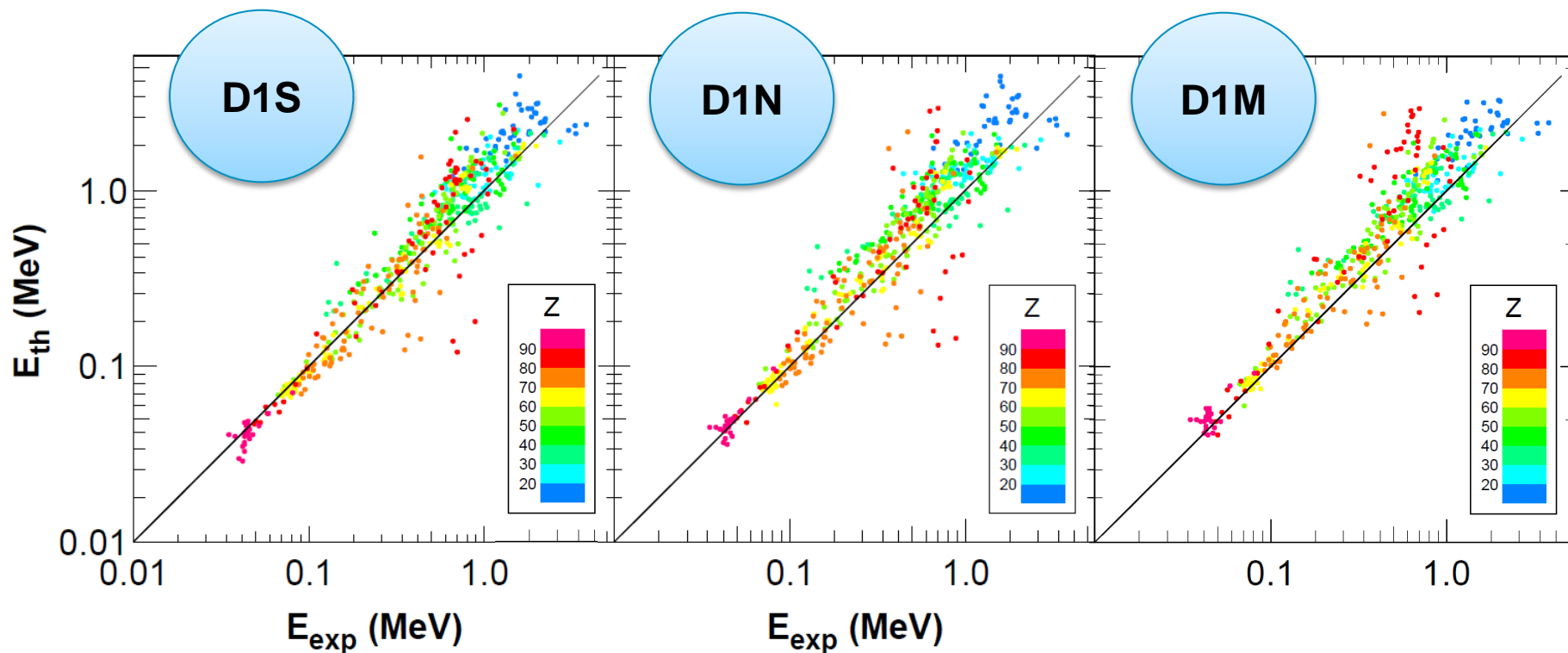
- Several tens of papers with D1S
 - Collective states spectroscopy (rotations and vibrations)
 - Shape coexistence & mixing
 - Transition strengths
 - Drip lines (through mass differences)
 - Improved nuclear deformations (radii, β and γ Bohr parameters)

- ⇒ Showing the predictive power of the D1S effective interaction

- Global systematics published in PRC81 (2010) 014303 with D1S
 - not with Kumar/Girod code but with J. Libert one

- Web site : www.phynu.cea.fr (D1S now, D1M soon)

Excitation energies of the first 2^+ for 519 e-e nuclei



STRUCTURE OF EVEN-EVEN NUCLEI USING A MAPPED ...

PHYSICAL REVIEW C **81**, 014303 (2010)

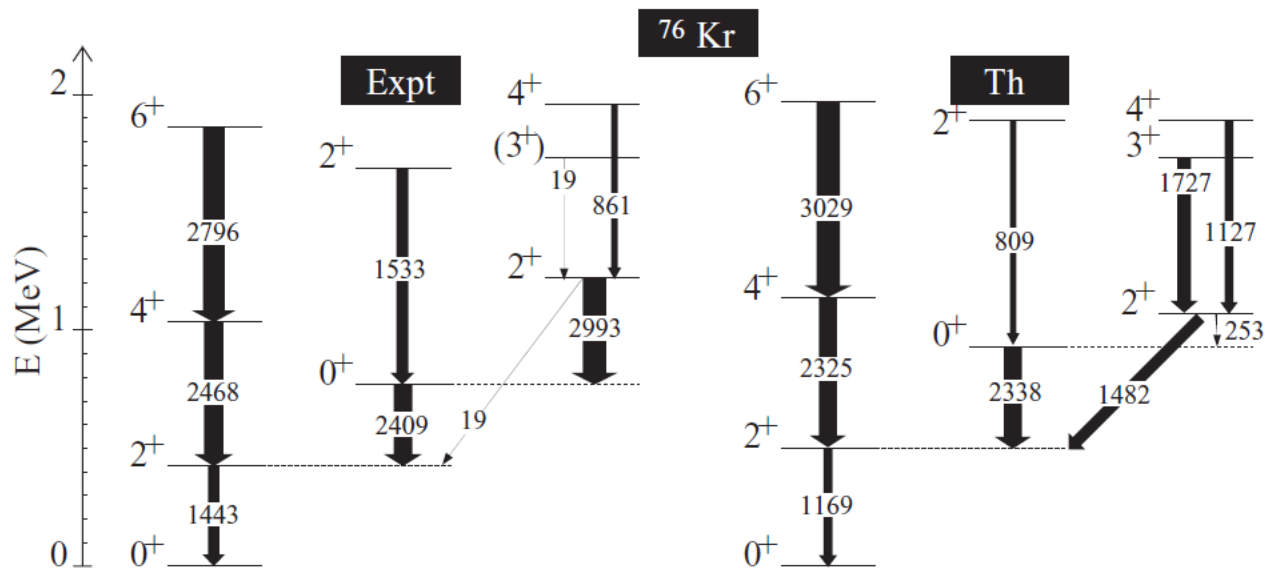
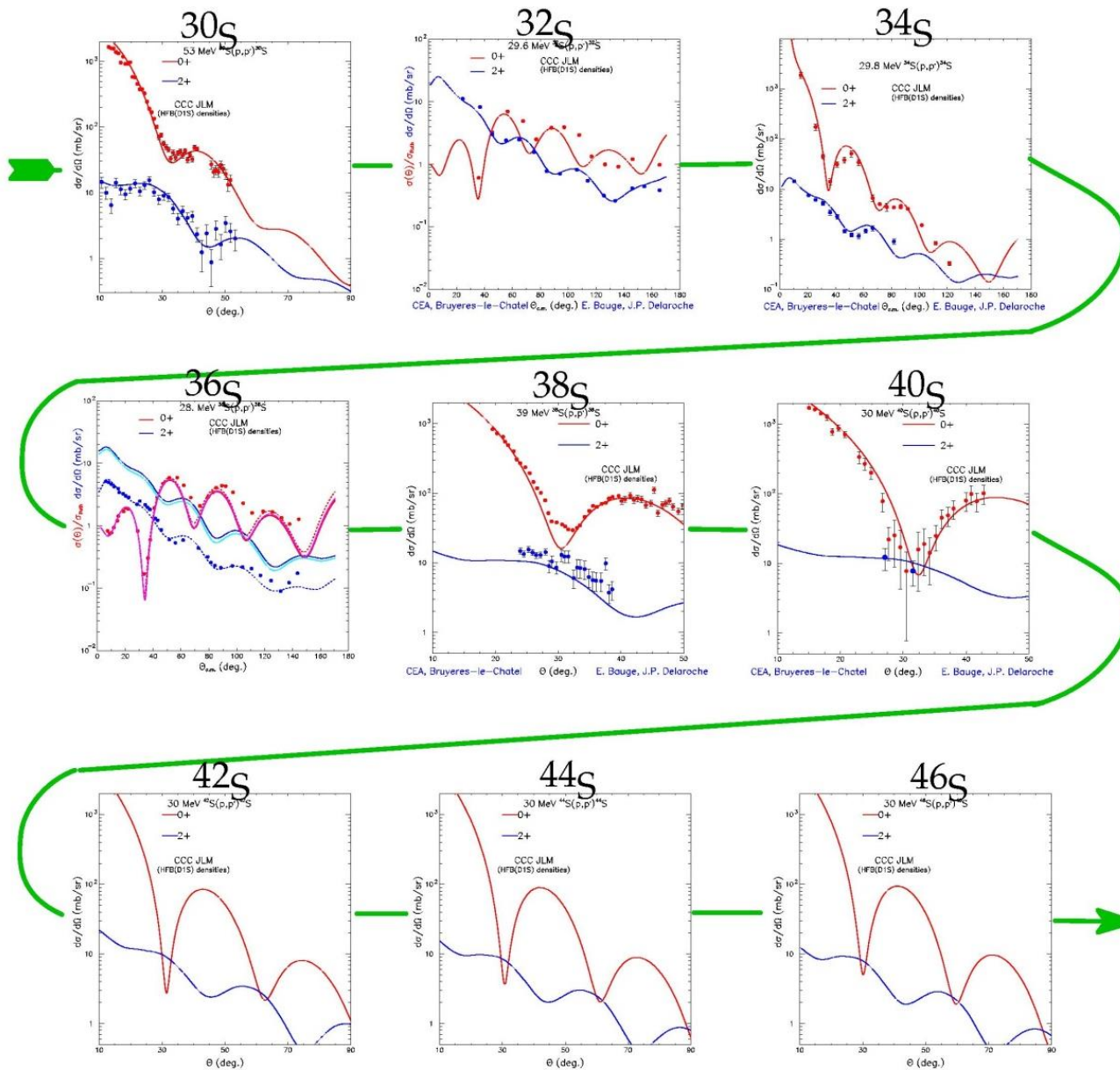
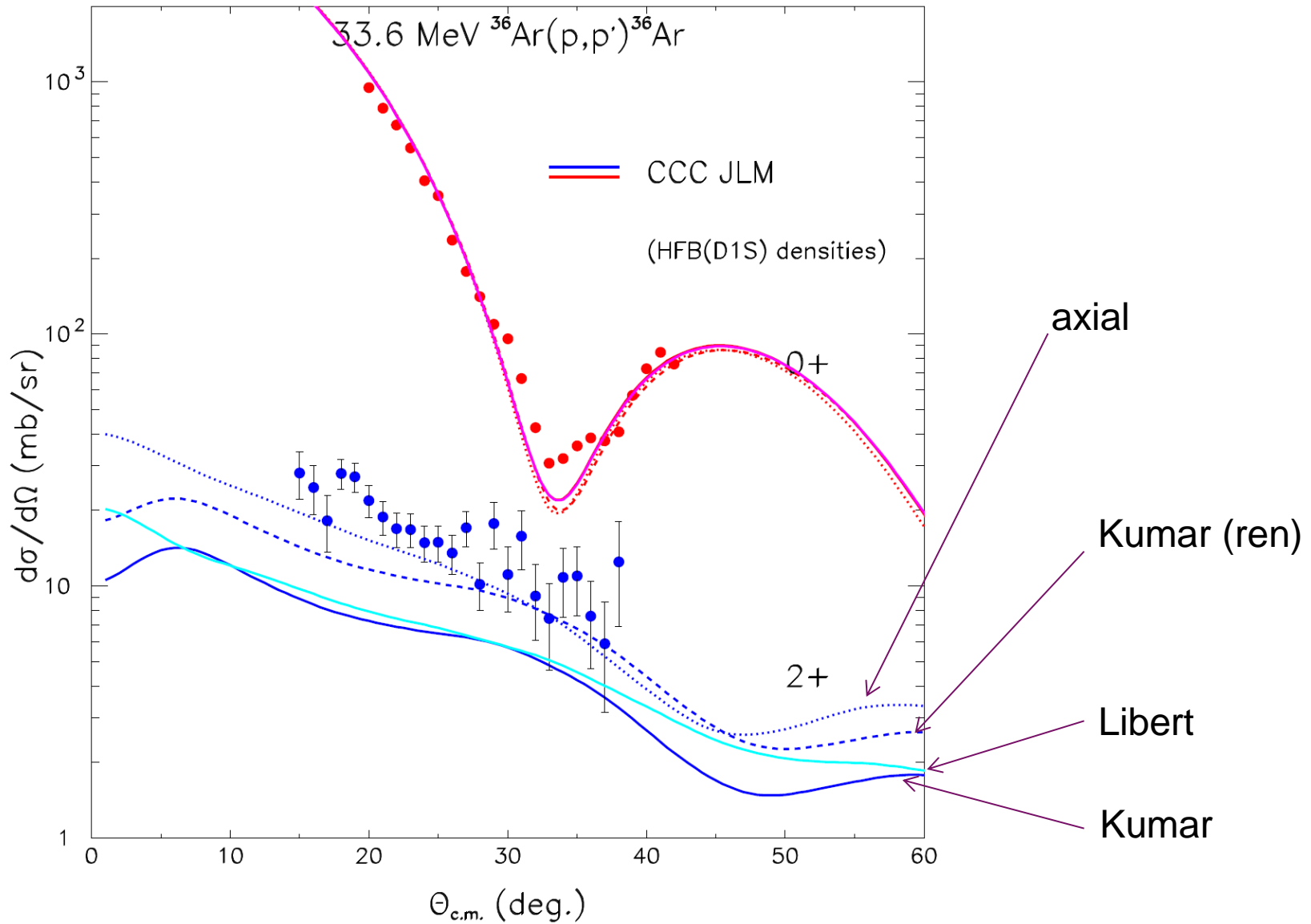


FIG. 1. Experimental and theoretical spectra (MeV) and transition strengths ($e^2 \text{ fm}^4$) of ^{76}Kr showing the excitations that we examine in the present global study. The experimental spectrum, on the left, is from Ref. [23] as well as from data repository for the 3^+ and 4^+ members of the γ band [24]. Calculated values are those from Ref. [23].

NUCLEAR REACTION INPUTS

Optical model





LEVEL DENSITIES (The combinatorial method)

See PRC 78 (2008) 064307 and PRC 86 (2012) 064317 for details

- TDHFB + effective nucleon-nucleon interaction

⇒ temperature (energy) dependent single particle level schemes

- Combinatorial calculation ⇒ intrinsic p-h and total state densities $\omega_{ph}(U, K, \pi)$

- Collective effects ⇒ from state to level densities $\rho(U, J, \pi)$

1) folding of intrinsic states and vibrational states : $\omega = \omega_{ph} * \omega_{vib}$

2) construction of rotational bands for deformed nuclei

$$\rho(U, J, \pi) = \sum_K \omega(U, E_{rot}^{JK}, K, \pi)$$

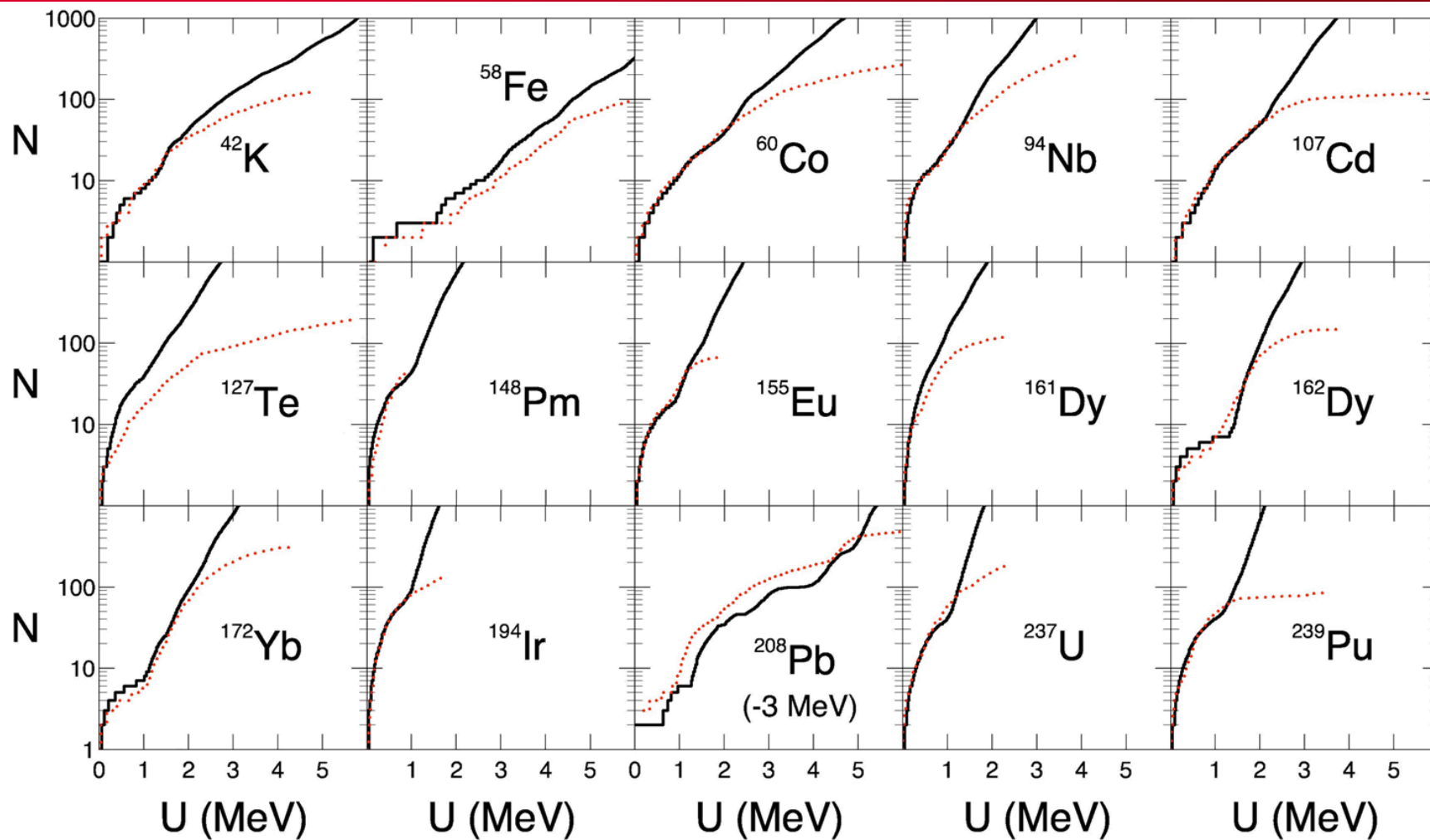
trivial relation for spherical nuclei

$$\rho(U, J, \pi) = \omega(U, K=J, \pi) - \omega(U, K=J+1, \pi)$$

Predicted within the same theoretical framework (coherence)

- Phenomenological mixing of spherical and deformed densities for small deformations

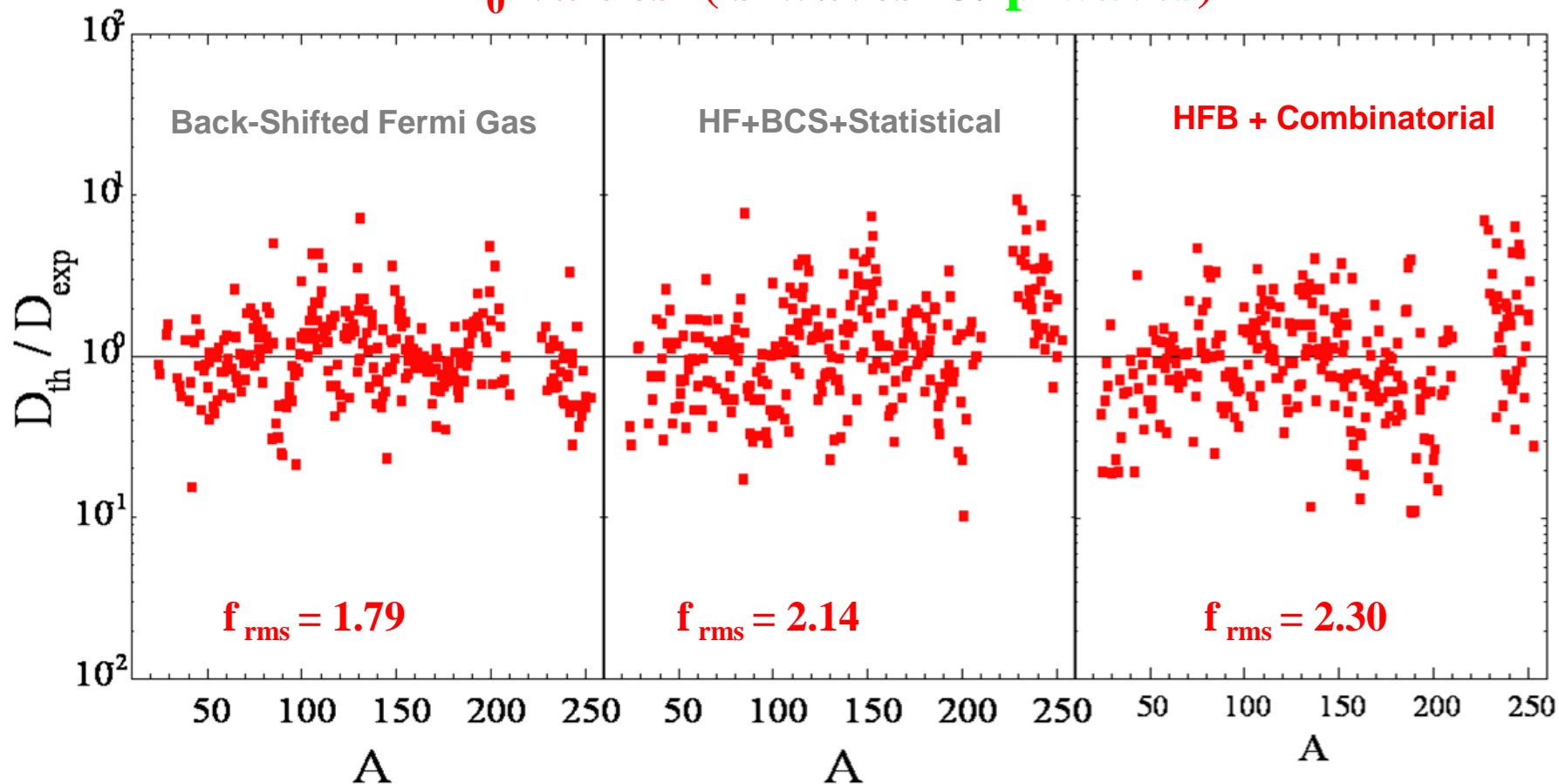
LEVEL DENSITIES (The combinatorial method)



➔ Structures typical of non-statistical feature

LEVEL DENSITIES (The combinatorial method)

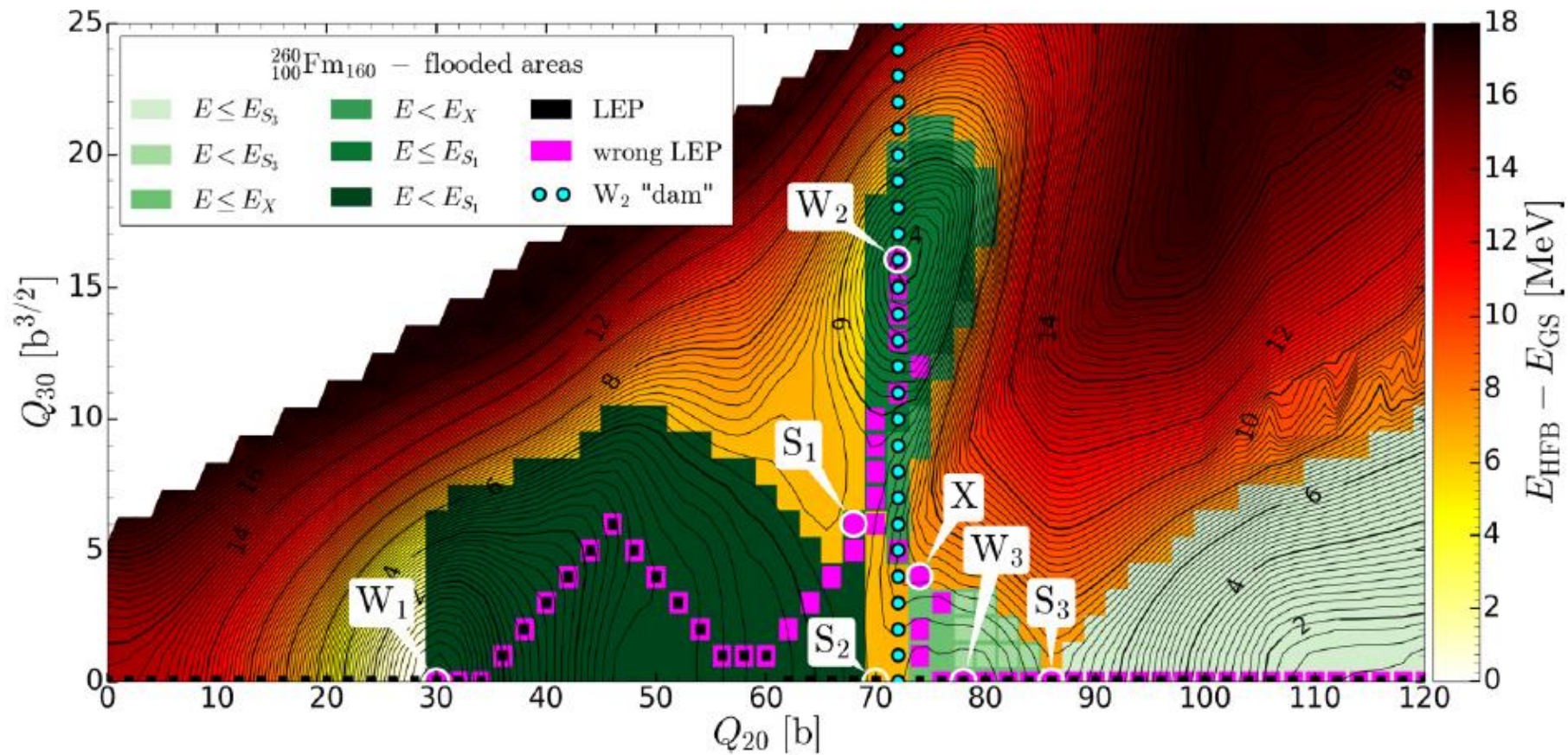
D_0 values (s-waves & p-waves)



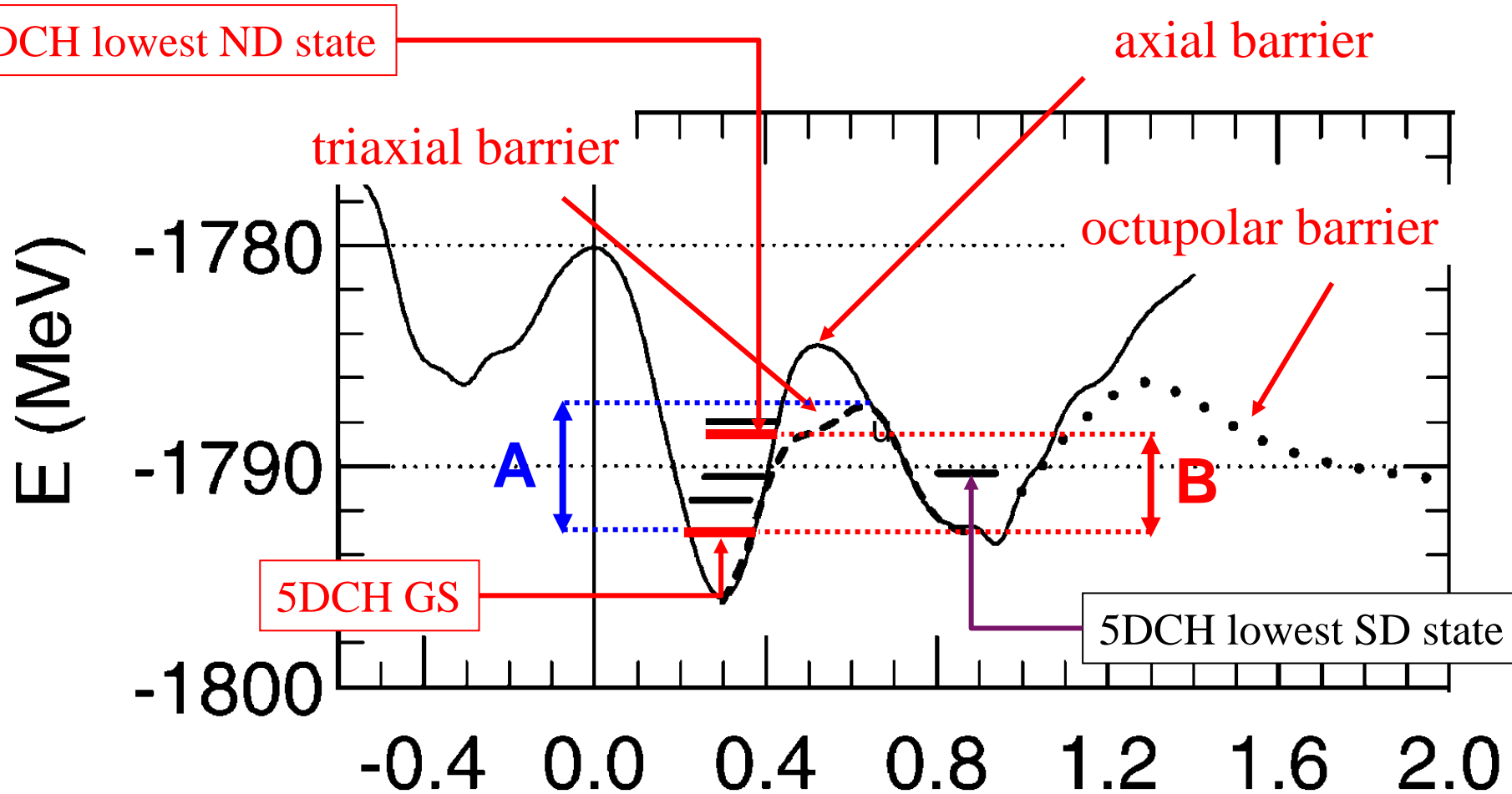
➔ **Descripti**
global a

$$f_{\text{rms}} = \exp \left[\frac{1}{N_e} \sum_{i=1}^{N_e} \ln^2 \frac{D_{\text{th}}^i}{D_{\text{exp}}^i} \right]^{1/2} \text{ with other}$$

Fission paths

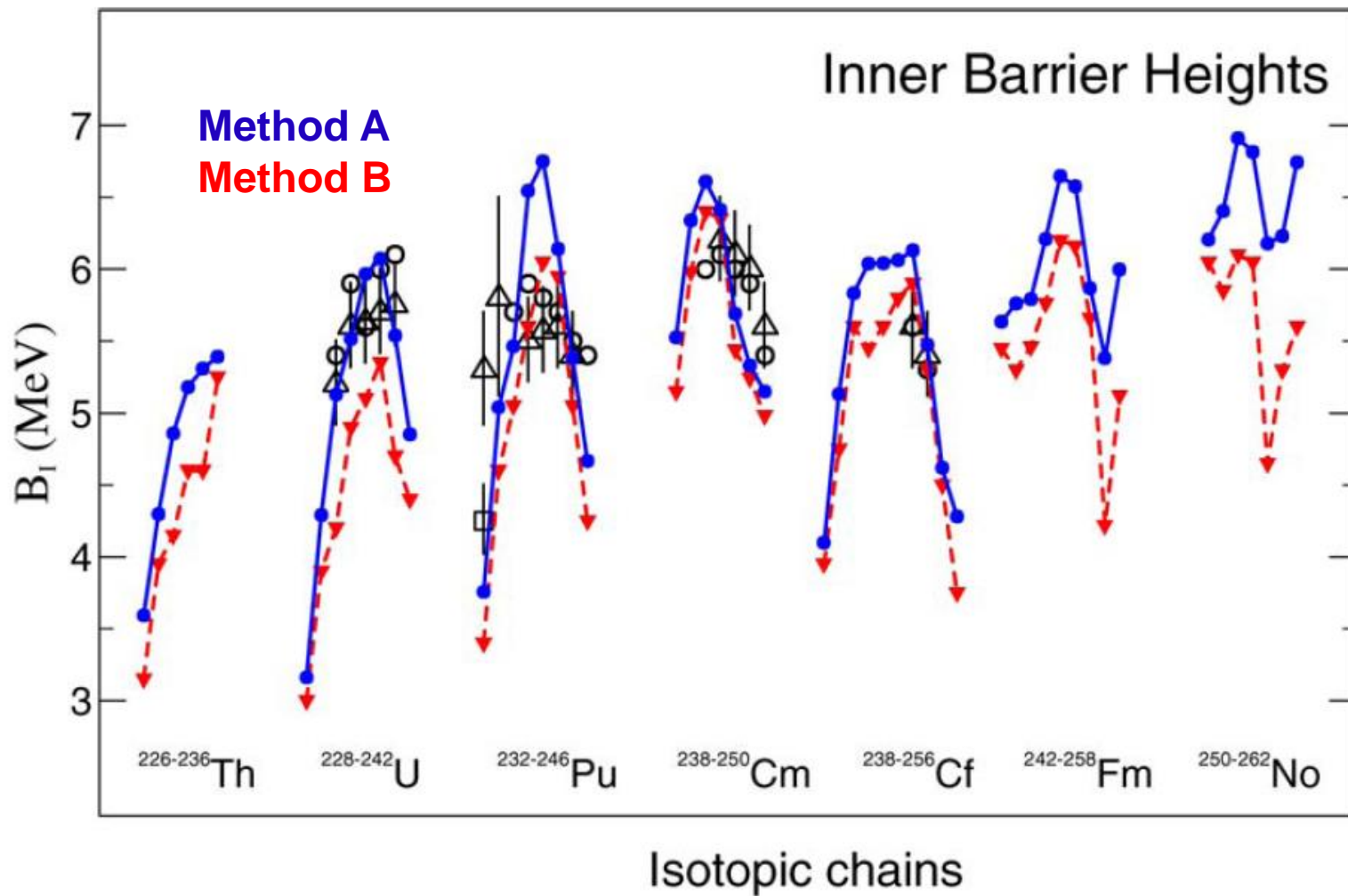


Fission barriers



Determining a fission is a complex task depending on the considered degrees of freedom

Fission barrier heights



CONCLUSIONS & PROSPECTS

5DCH powerfull approach for systematic approach : robust and fast

Provides usefull nuclear reaction input on top of pure structure data

There is a clear need to maintain the know how and even push the approach further

Perspectives :

- Develop new codes with « young » staff members
- HFB3 project started
- Update of FELIX (TDGCM+GOA into GCM+GOA) under consideration