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Designing superconducting magnets using simple genetic algorithms



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The challenges in designing superconducting magnets

- Magnets for particles detection
- Magnets for particles accelerators

Why AI methods can be useful

Examples of Genetic Algorithms Applications for Superconducting Magnets

- Description
- Ex : how to optimize the conductor cost in a 3D magnet design : the MADMAX dipole
- Ex: how to optimize the magnetic field quality in a 2D magnet design : the F2D2 dipole

Conclusions

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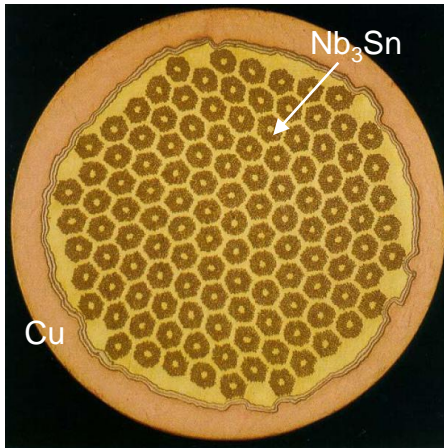


Challenges in Superconducting Magnets Design



9/1/2020

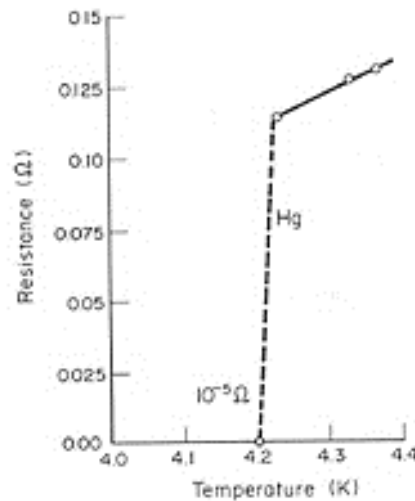
Why superconductivity?



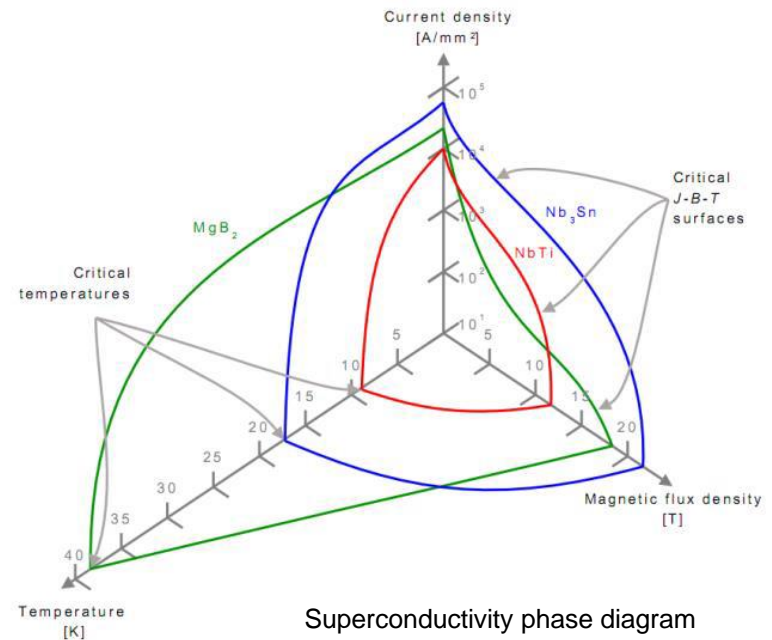
Nb₃Sn bronze-process wire [1]



Superconductive materials show zero electric resistance
→ they can transport a lot of current without heating



Hg resistivity



Superconductivity phase diagram

The superconducting state is limited by

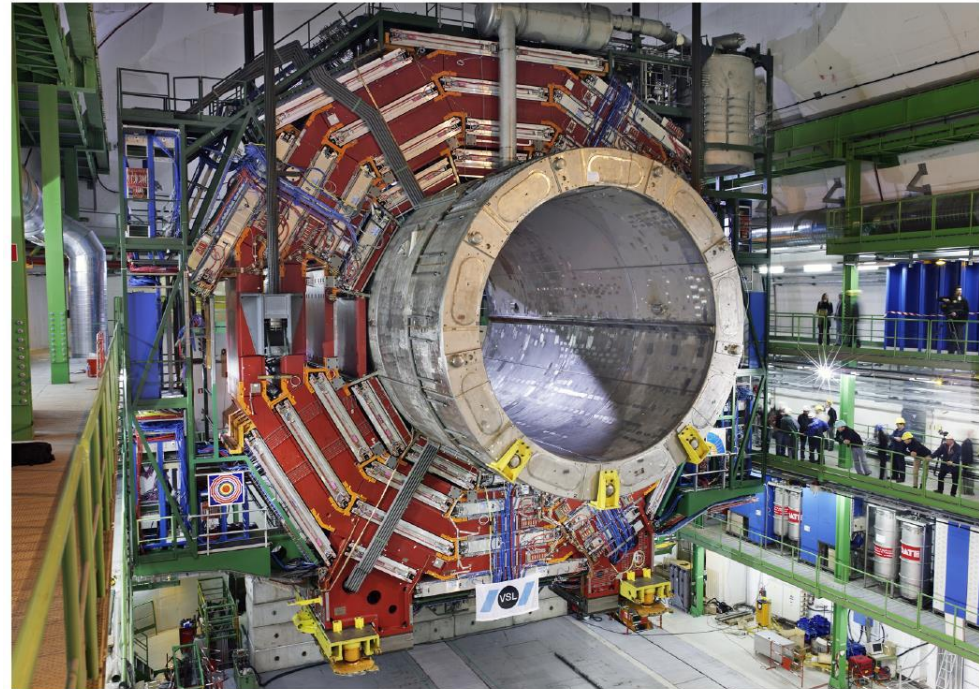
- \vec{B} magnetic field
- \vec{J} current density inside the material
- T temperature

Why superconducting magnets?

The CMS solenoid at CERN

Advantages:

- Very high magnetic field (up to 40T)
- Reduced dimensions (10x compared to copper magnets)
→ scale economy, better quality control in performances
- No ohmic power dissipation → reduced consumptions



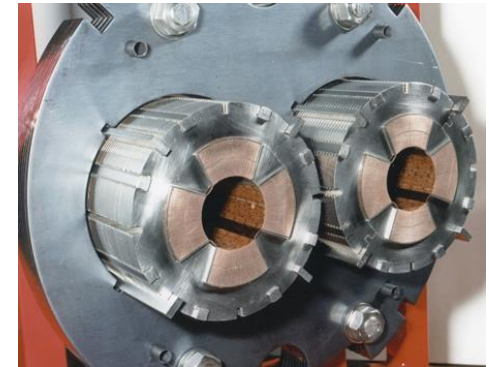
YB0 landing in the CMS experiment hall

Why superconducting magnets?

Drawbacks:

- Must work in cryogenic environment (1.8 K to 70 K)
- The superconducting state is very fragile → even a deposit of few *mJ* can make a magnet transit to the normal state
- High magnetic field + High current → High forces & high energy density in the materials

The Nougat solenoid (32.5 T) @ LCNMI Grenoble



The quadrupoles MQYY for Hi-Lumi LHC, designed and assembled by CEA

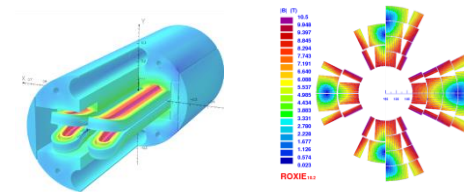


The ISEULT MRI @ Neurospin

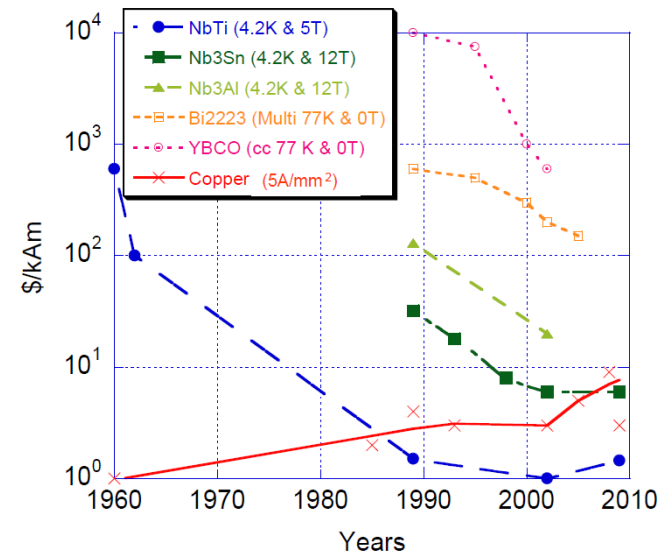
Which challenges?

- **Field quality**
 $\Delta B/B \sim 10^{-4}$ for particle accelerators
 $\Delta B/B \sim 10^{-8}$ for MRI
- **Mechanics**
 Stress can reach 300 MPa on the conductor
- **Cryogenics**
 Must cool down tons of materials
- **Protection**
 Transition to the normal state means 1000s A in
 $\sim \text{mm}^2$ wires (normal Cu wire carries some A)
- **Cost**
 Superconductors can cost up to 1000\$/kAm

FCC Dipole & Quadrupole



US\$ 150/kg \leftrightarrow ~ 1 \$/kAm

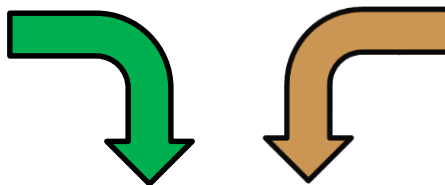


P. Fazilleau – Ecole des accelerateurs 2016

Field Quality

Depends on:

- Position of the coils → linear contribution to B
- Position of the ferromagnetic materials → non linear contribution to B

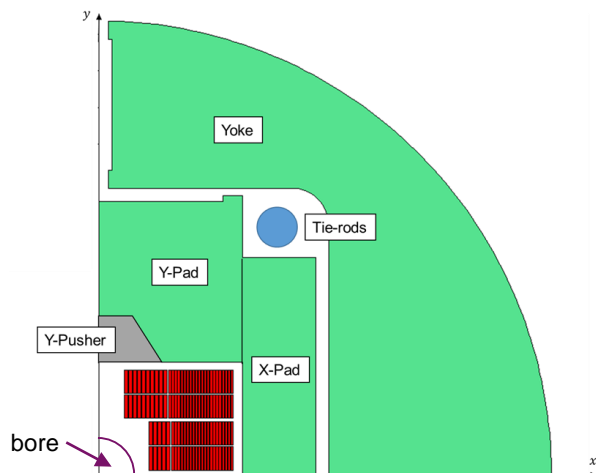


Not possible to write down an analytical function

Cost

Depends on:

- The volume of conductor needed
- The quantity of superconducting material needed in the cable to stand the magnetic field peak



Problem is :

Given a certain B according to specs,

Field Quality

Minimization of the ratio $\Delta B/B$ in the bore region

Cost

Minimization of the ratio $\Delta B/B$ on the conductors

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cea



Examples of Genetic Algorithms Applications for Superconducting Magnets

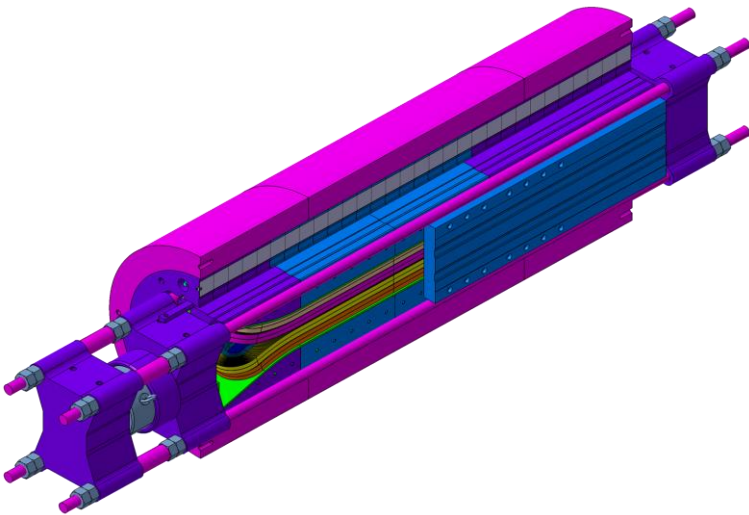


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Field Quality

F2D2

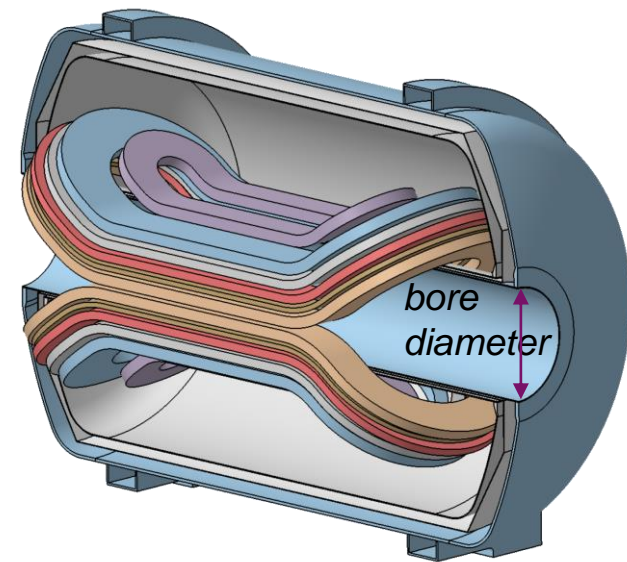
The 16 T graded Nb_3Sn flared ends dipole to prove the feasibility of the Future Circular Collider at CERN.



Cost

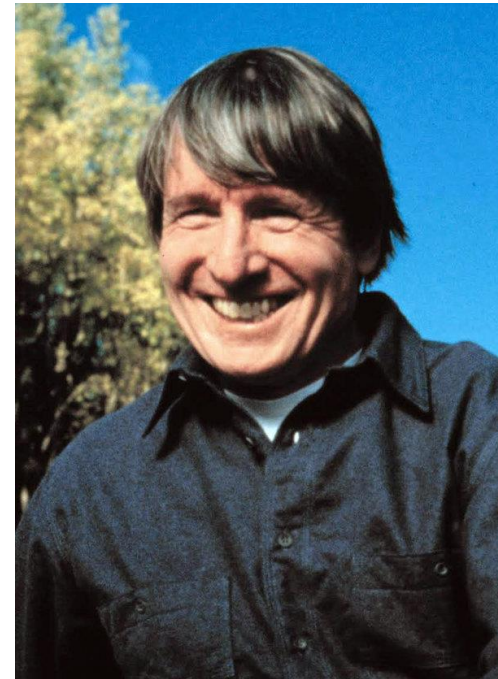
MADMAX

The 9 T NbTi , 1.3 m of useful diameter dipole (the biggest in the world) to find axions-like particles.



One of the first AI methods

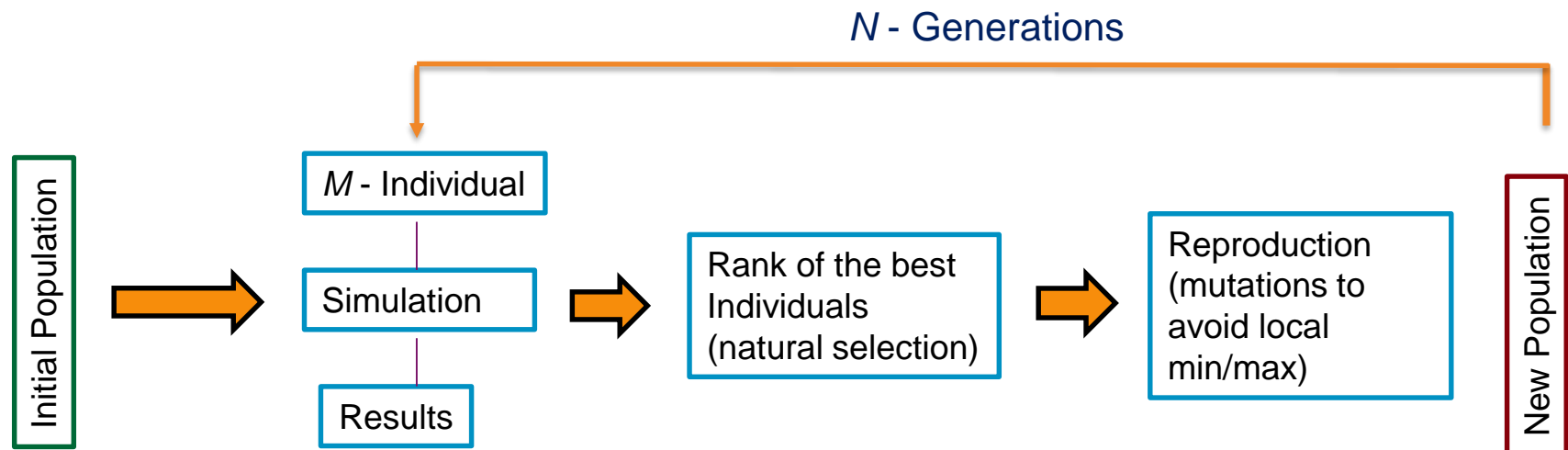
- Invented by *John Henry Holland*, prof. at University of Michigan, in *Adaptation in Natural and Artificial Systems* (1975, MIT Press)
- They mock the darwinian evolution
- Used in physics, engineering, finance... to find maximum/minimum of unknown functions



Concepts:

- Each parameter = GENES
- Set of parameters = INDIVIDUAL
- Set of individuals = POPULATION
- Evolution of the population = GENERATION

Working Principles



Initial Population

Step 1

Choose the parameters (genes) and their range

Ex:

$$L_{xy1} \in [-2,1]$$

$$L_{xy2} \in [-3,4]$$

...

Step 2

Build an individual (by randomic PDF generation). 1 number for each gene

$$L_{x1} = \begin{pmatrix} L_{x11} = 0.5 \\ L_{x12} = 1.2 \\ \dots \end{pmatrix}$$

Step 3

Build a population

$$L_1 = \begin{pmatrix} L_{11} = (L_{111}, L_{112}, \dots) \\ L_{12} = (L_{121}, L_{122}, \dots) \\ \dots \end{pmatrix}$$

How to choose correctly

v number of parameters (degree of freedom) of the problem

$$m \text{ number of individuals} \geq D_{v,2} = \frac{v!}{(v-2)!}$$

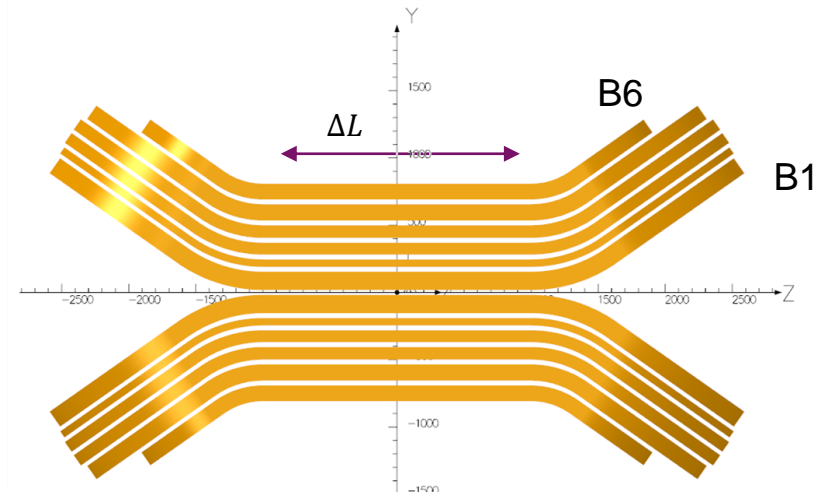
$$n \text{ generations}^* > 2^{v-1}$$

Minimal number of simulations

$$m \times n = 2^{v-1} \frac{v!}{(v-2)!}$$

Limit the number of parameters

*criteria (n actually depends on how fast the function goes to min / max)



GA parameters:

- $0 < \Delta L < 300$ mm B1→B4
- $0 < \Delta L < 400$ mm B5
- $0 < \Delta L < 500$ mm B6



Population = 30 individuals
Generations = 32

Tot forecast 3D simulations = 960

Simulation

Step 1 – Fitness Function

Choose what do you want to evaluate

Ex: Volume – Cost function for the conductor

$$\left\{ \begin{array}{l} C_{cond} = V_{cond} \left(C_{Cu} \left(1 - \frac{J_E}{J(B_{peak})} \right) + C_{NbTi} \left(\frac{J_E}{J(B_{peak})} \right) \right) \\ J(B_{peak}) = (1 - m) J_c \left(\frac{B_{peak}}{1 - m}, T_0 \right) \end{array} \right.$$

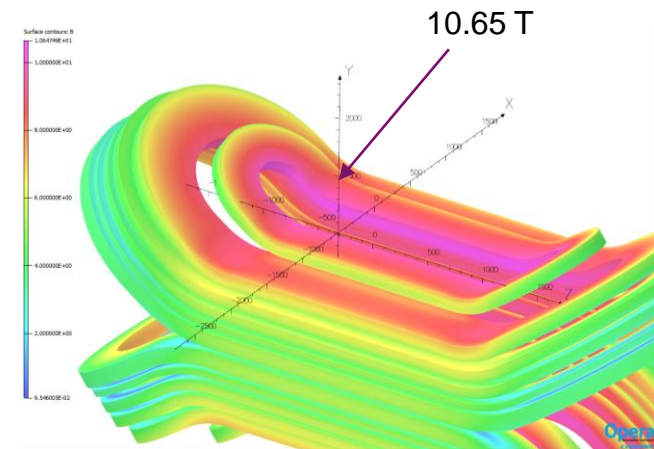
Where:

- V_{tot} conductor volume
- J_E engineering current density
- T_0 operating temperature
- $m = 0.1$ LL margin
- C_{Cu} copper volume cost
- C_{NbTi} NbTi volume cost

Step 2

Evaluate the fitness function (simulations) for each individual

$C_{cond}(L_{11}), C_{cond}(L_{12}), \dots$



Rank of the best individuals

Step 1 – Choose if you want to find *min* or *max* of your fitness function

Ex: min of $C_{cond}(V_{cond}, B_{peak})$

Step 2 - Ranking

Rank the individual according to which one has the minimal value.

Ex:

$L_{11} = 2000$	→	1. $L_{12} = 1500$
$L_{12} = 1500$		2. $L_{15} = 1600$
$L_{13} = 1700$		3. $L_{13} = 1700$
$L_{14} = 1900$		4. $L_{14} = 1900$
$L_{15} = 1600$		5. $L_{11} = 2000$
$L_{16} = 2100$		6. $L_{16} = 2100$

Step 3

Assign a probability of reproduction to the individuals according to the rank

Criteria:

i rank position

$$p_i = \frac{\frac{m-i}{m}}{\sum_{i=1}^m \frac{m-i}{m}}$$

1. $L_{12} \rightarrow p(L_{12}) = 0.333$
 2. $L_{15} \rightarrow p(L_{15}) = 0.267$
 3. $L_{13} \rightarrow p(L_{13}) = 0.200$
 4. $L_{14} \rightarrow p(L_{14}) = 0.133$
 5. $L_{11} \rightarrow p(L_{11}) = 0.067$
 6. $L_{16} \rightarrow p(L_{16}) = 0.000$

Reproduction

Step 1 – Coupling

Random extraction of two numbers x_1, x_2 with an uniform PDF [0,1]

Ex: $x_1 = 0.3, x_2 = 0.7$

Calculate the cumulative function $\int p_i$, assigning the respective parameter

1. $L_{12} \rightarrow [0,0.333]$
2. $L_{15} \rightarrow (0.333,0.6]$
3. $L_{13} \rightarrow (0.6,0.8]$
4. $L_{14} \rightarrow (0.8,0.933]$
5. $L_{11} \rightarrow (0.933,1]$

Where x_1, x_2 falls, you have your couple ;)
No self reproduction allowed.

Step 2 – Cross-over

Random extraction of two numbers c_1, s_2
 c_1 uniform PDF [cross-over,1]
 s_2 uniform PDF [0,1]

Generally, $\text{cross-over} > 0.7$

If $x_1 < c_1$ and $x_2 < c_1$
Reproduction! ;))

$$\begin{aligned} L_{211} &= s_2 \cdot L_{121} + (1 - s_2)L_{131} \\ L_{212} &= s_2 \cdot L_{122} + (1 - s_2)L_{132} \\ L_{213} &= s_2 \cdot L_{123} + (1 - s_2)L_{133} \\ &\dots \end{aligned}$$

For every gene

Else

$$L_{21} = L_{12}$$

Until we replace L_1

Bonus: Mutation

Step 1

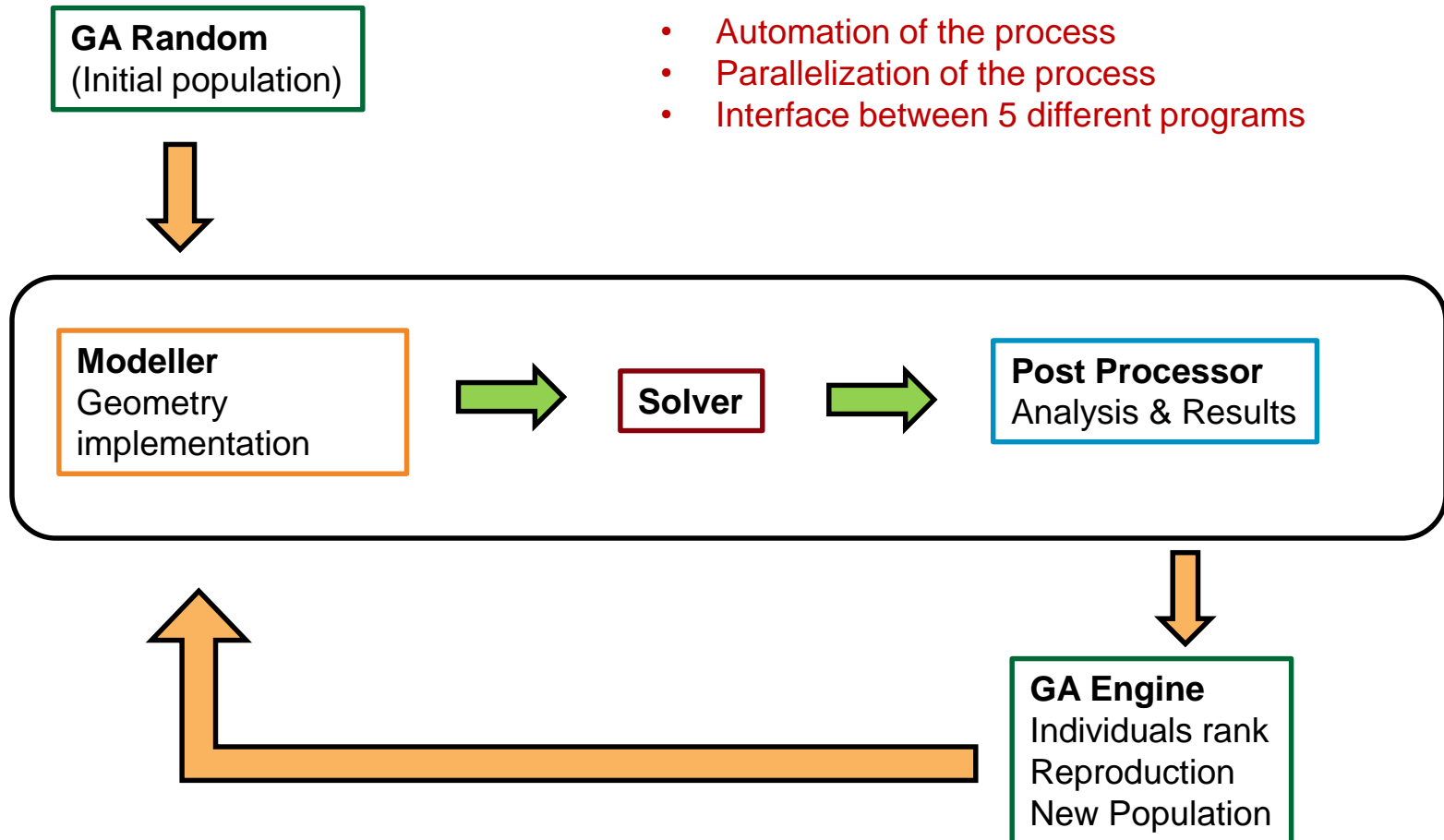
For each gene,
Random extraction of one number
 x_3 uniform PDF [0,1]

If $x_3 < p_{mutation}$
Then rebuild the gene (step 1 Initial population)

Generally $p_{mutation} < 0.1$

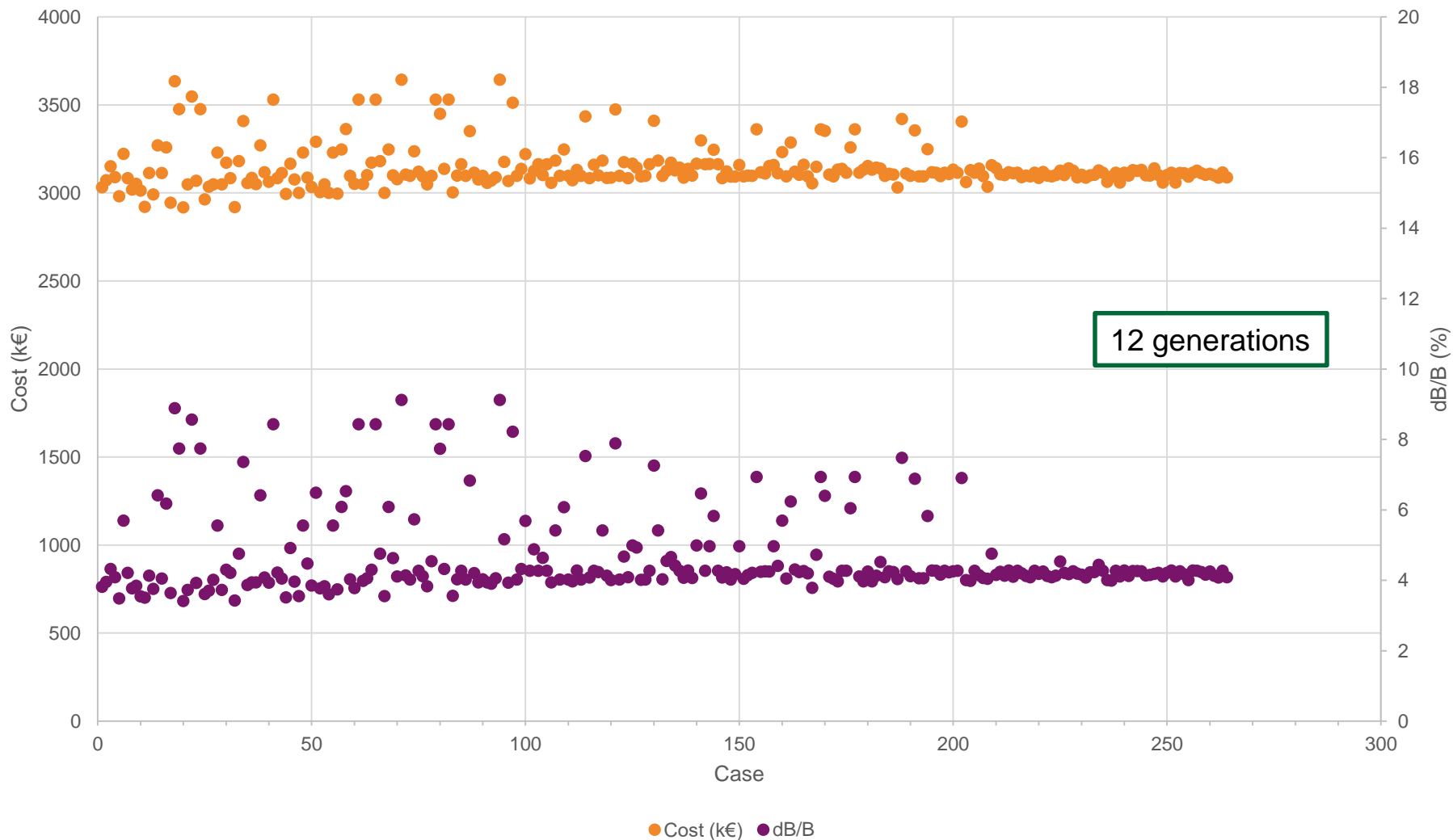
Repeat for each generation

Implementation in OPERA 3D

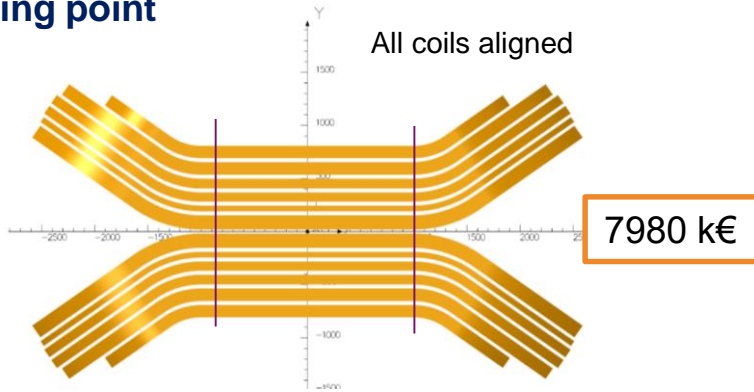


- Automation of the process
- Parallelization of the process
- Interface between 5 different programs

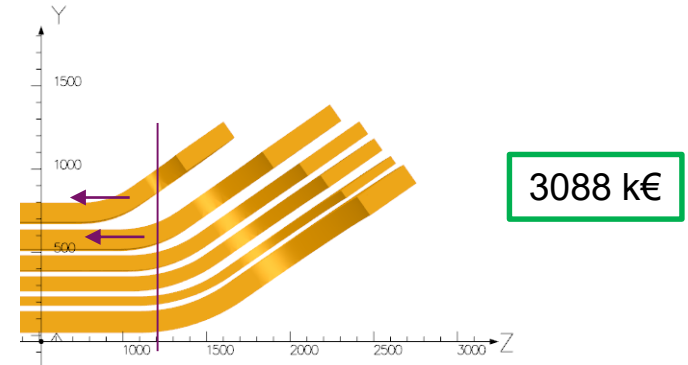
GA v90 Straight Length - Cost and Overfield



Starting point



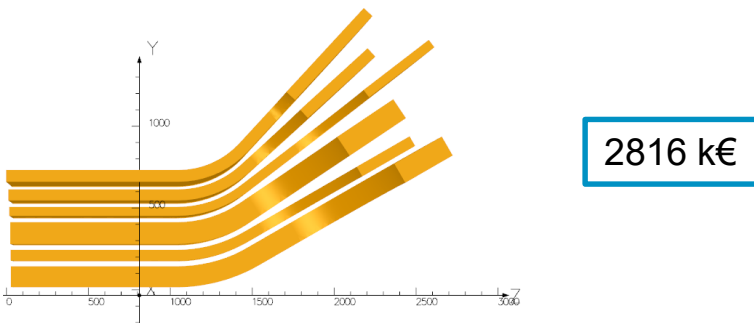
Final solution



GA + parametric study
to understand the sensitivity of parameters

Intermediate solution

GA study varying many parameters

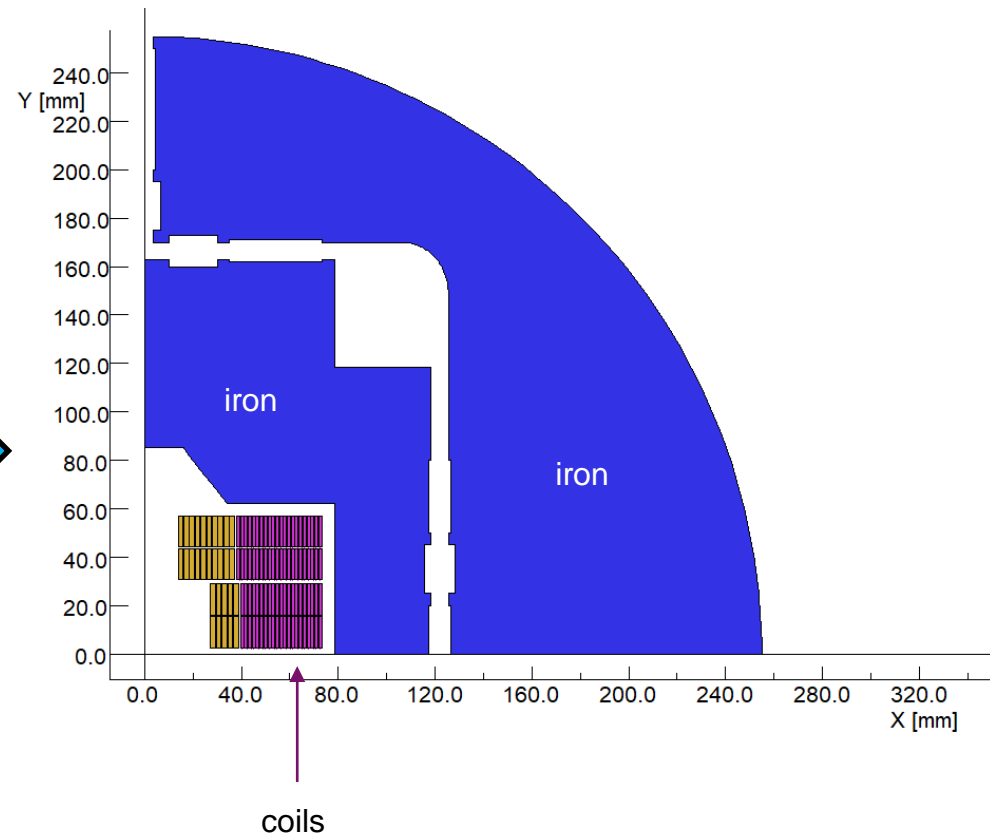
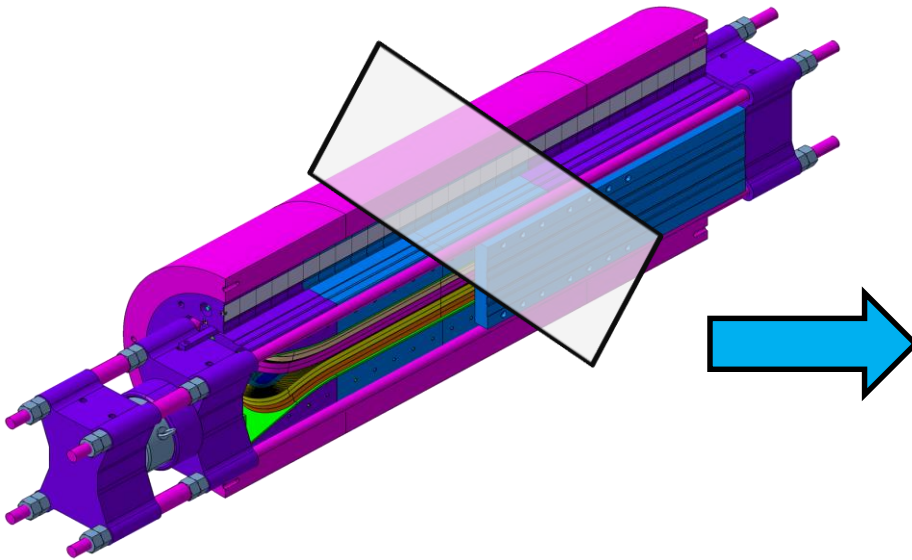


but not feasible for assembly



3D assembly

2D magnetic



Fourier expansion of the magnetic field

$$B_r = \sum_{n=1}^{\infty} \left(\frac{r}{r_{ref}} \right)^{n-1} [B_n \sin(n\theta) + A_n \cos(n\theta)]$$

$$B_\theta = \sum_{n=1}^{\infty} \left(\frac{r}{r_{ref}} \right)^{n-1} [B_n \cos(n\theta) - A_n \sin(n\theta)]$$

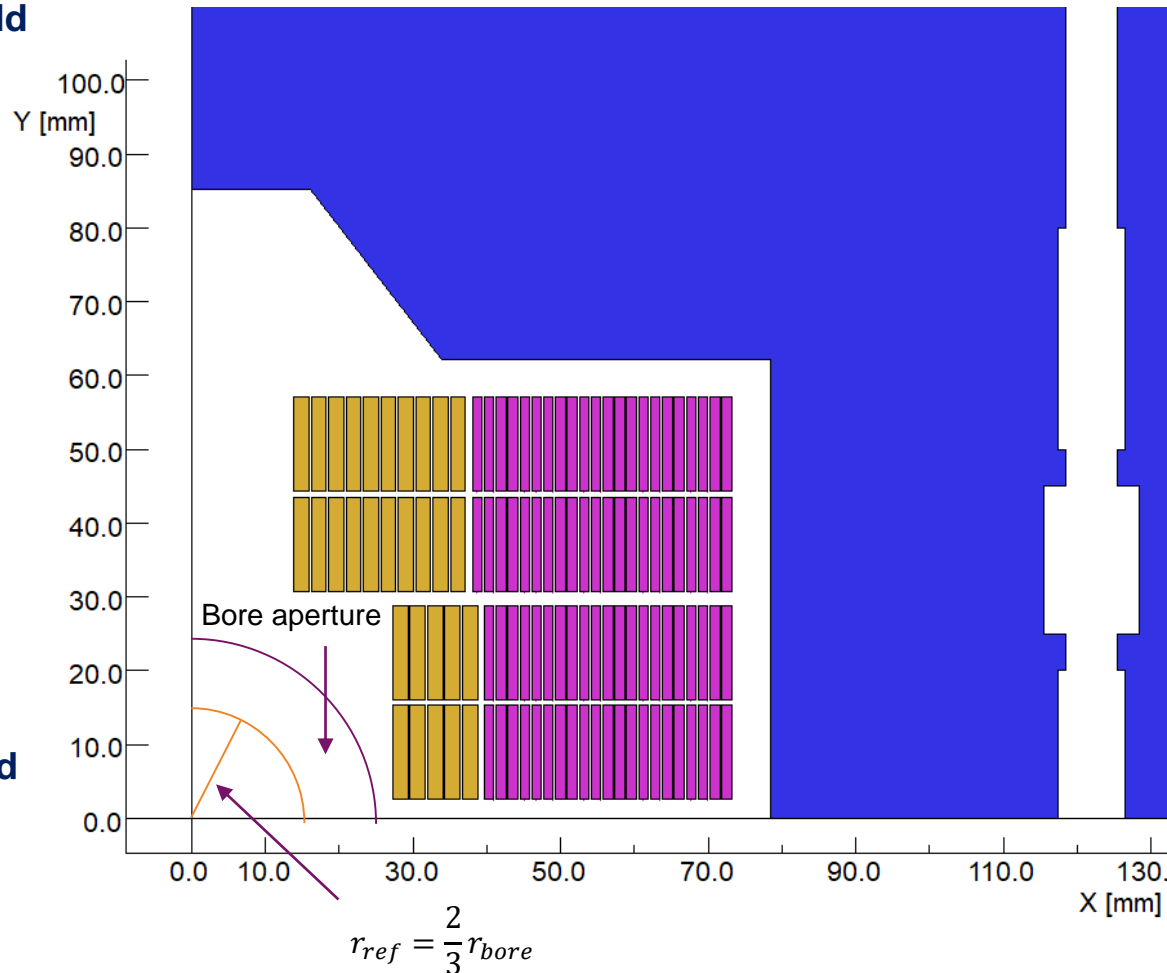
Harmonics

$$b_n = \frac{B_n}{B_{ref}} \cdot 10^4$$

$$a_n = \frac{A_n}{B_{ref}} \cdot 10^4$$

Series expansion of the magnetic field

$$B_y + iB_x = 10^{-4} B_0 \sum_{n=1}^{\infty} (b_n + ia_n) \left(\frac{x + iy}{r_{ref}} \right)^{n-1}$$

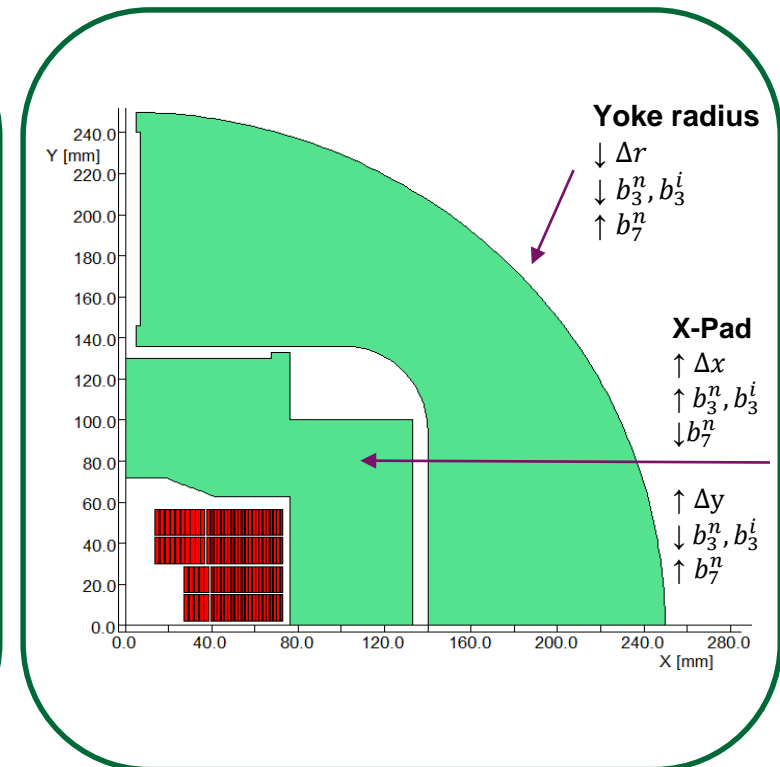
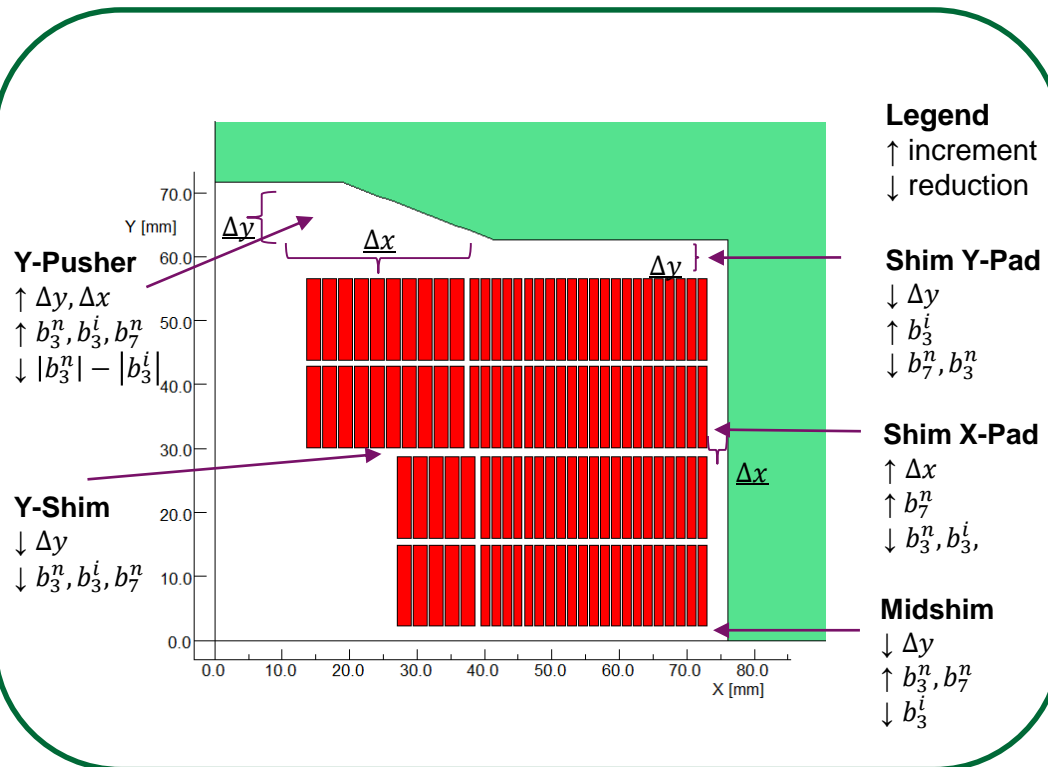


Parameters

- Turns and position of the coil without iron → analytical
- Position of the coils & position of the iron → GA

Criteria

- $-3 \leq b_n \leq 3$ @ 15.5 T
- $-15 < b_3 < 15$ @ 1.04 T (induction)



GA study:

Number of parameters = 9

Forecast number of individuals = 72

Forecast number of generations = 256

Forecast number of simulations = 18432



Time per simulation = 115 s

Total time = 24.5 d

GA study coil + iron:

Number of parameters = 3 (coils) + 6 (iron)

Forecast number of individuals = 3 + 30

Forecast number of generations = 8 + 64

Forecast number of simulations = 1944

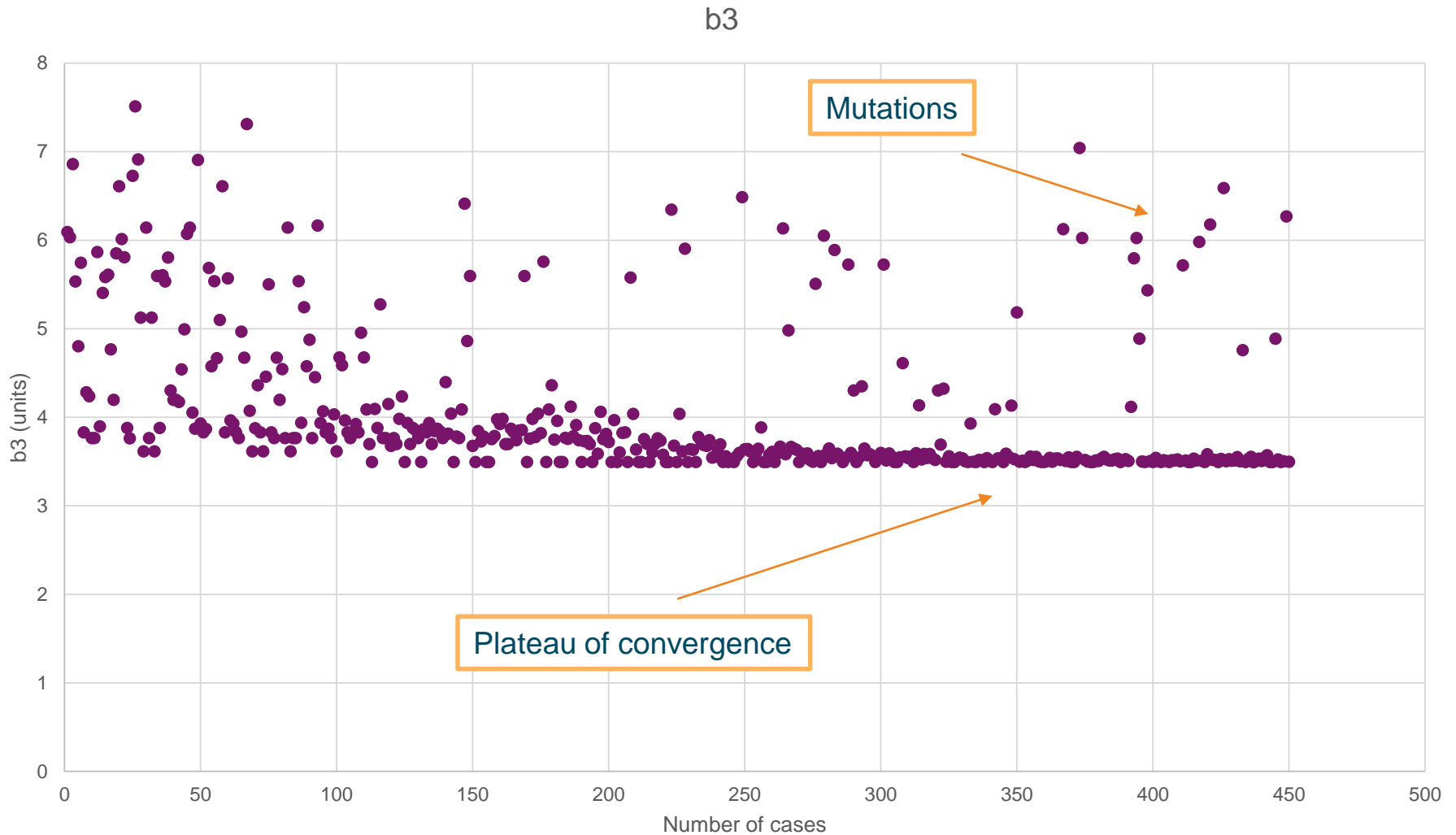


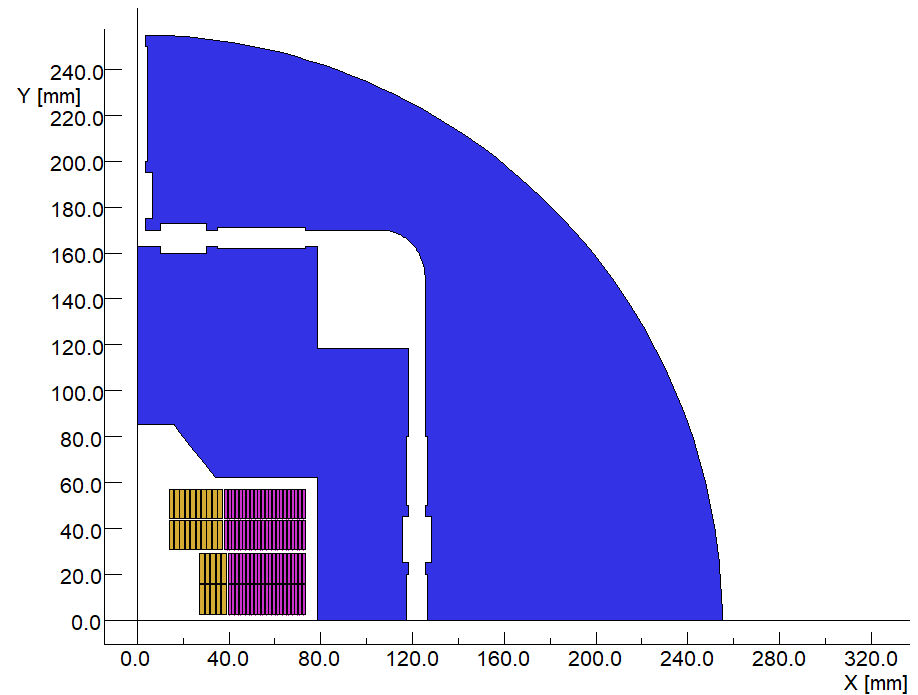
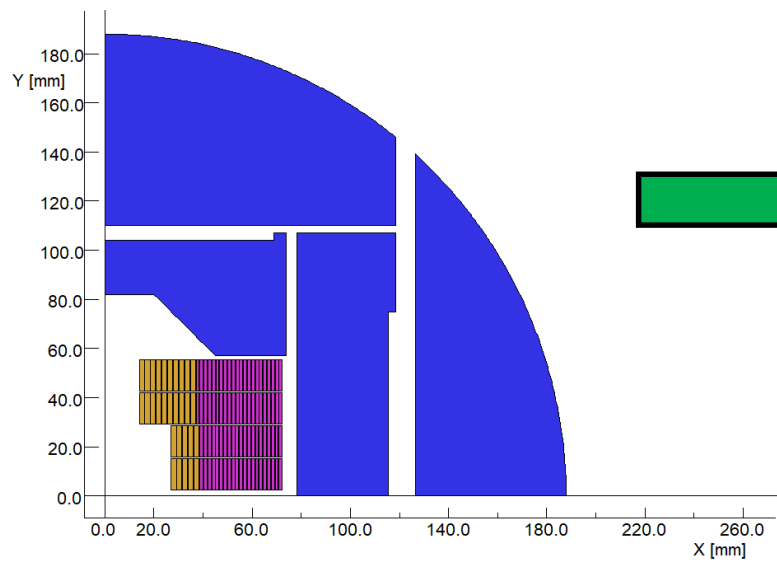
Time per simulation = 45 s

Total time = 2.6 d

Procedure :

- 1) GA for iron
- 2) Adaptation of parameters for coils





GA can be used for :

- Minimization problem
- Maximization problem

When you don't know how to write down a function (or a part of).

Warnings:

- To be used with a limited number of variables (as a function of your resolution time)
- How to rank the individuals is one of the hardest problem if you look for multiple fitness functions (ex: *minimize both Bpeak and Volume*)
- They will always find an approximate solution
- Save all the data and look at them in real time → you can converge faster than you thought



1. A. Devred, (2006) « Practical low-temperature superconductors for electromagnets », CERN-2004-006,
2. R. L. Haupt; et all (2007) « Genetic Algorithms in Electromagnetics », Wiley
3. H. Felice; et all (2019) « F2D2: A Block-Coil Short Model Dipole Towards FCC », *IEEE Transaction on Applied Superconductivity*, vol. 29, Issue: 5
4. E. Rochepault; et all (2020) « 3D Conceptual Design of F2D2, the FCC Block-Coil Short Model Dipole », *IEEE Transaction on Applied Superconductivity*, vol. 30, Issue: 4
5. V. Calvelli; et all (2020) « 2D and 3D Conceptual Design of the MADMAX Dipole », *IEEE Transaction on Applied Superconductivity*, vol. 30, Issue: 4