



IFSC UNIVERSIDADE
DE SÃO PAULO
Instituto de Física de São Carlos



Testing fundamental physics with Astrophysical Sources: LIV

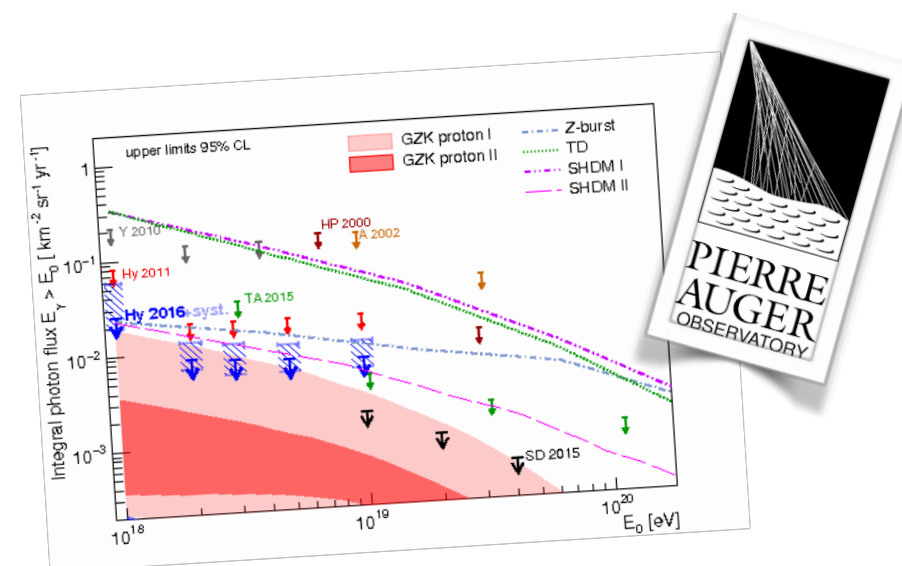
Humberto Martínez-Huerta,
IFSC-USP, Brazil

**Meeting of the Cosmic Rays Section of the Mexican
Physical Society
3-5 Oct 2018**

Index

- I. Lorentz invariance violation (LIV)
- II. Limits: TeV γ -rays
 - i. Time Energy Dependent delay
 - ii. Photon Decay
 - iii. Pair production threshold shifts
- III. UHECR

- i. GZK-photons + LIV
- ii. Limits: UHECR



I. Lorentz invariance violation (LIV)

II. Limits: TeV γ -rays

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iii. Pair production threshold shifts

III. UHECR

i. GZK-photons + LIV

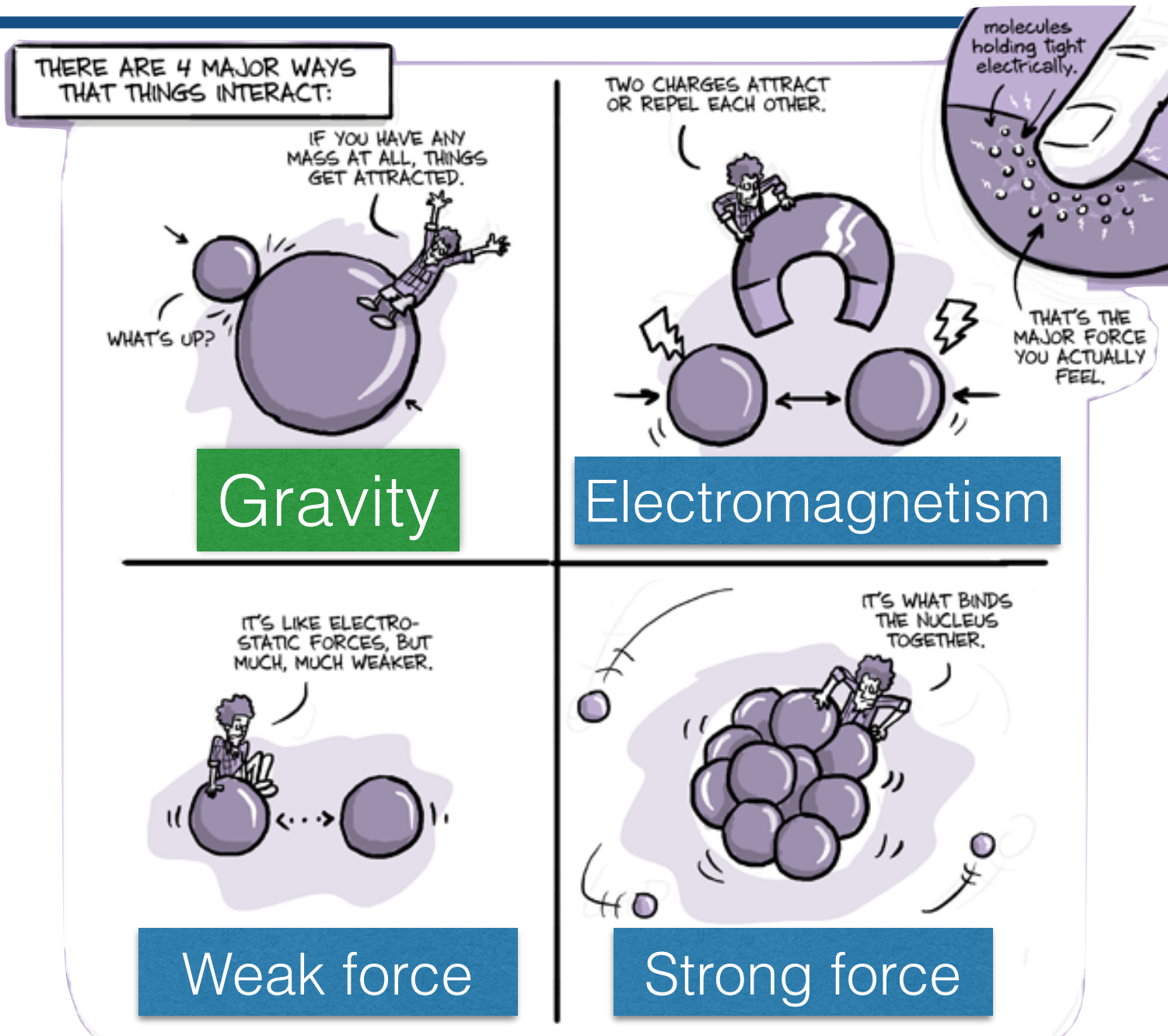
ii. Limits

Fundamental Forces of Nature

General
Relativity



Geometrical
Theory

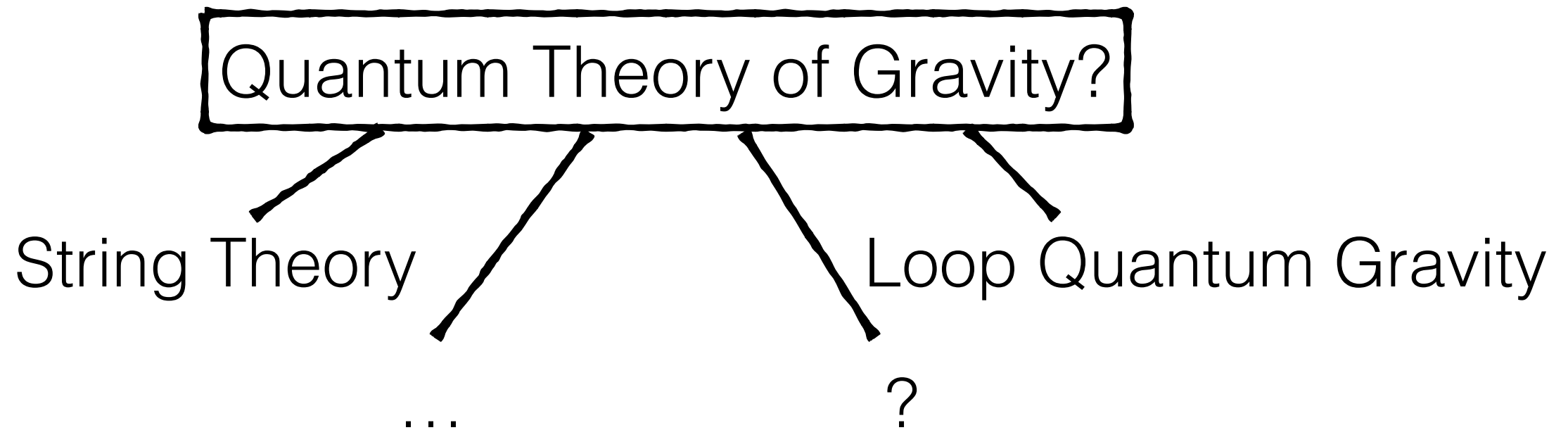


Standard
Model



Quantum
Field
Theory

- SM & GR: the best theories describing the 4-fundamental Forces.
- No conflict with predictions from either of them.
- **They are fundamentally different.**



New Physics involves new features, such as:

- Higher Dimensions of s-t
- Brane World scenarios
- Noncomutative geometries
- ...
- The law of relativity might not hold exactly at all energy scales → **Lorentz Invariance Violation (LIV)**

... **LI may not be an exact symmetry of Nature**

Generic LIV dispersion relation

$$E^2 - p^2 \pm \epsilon A^2 = m^2,$$

$$E \gg m,$$

$$A = \{E, p\}$$

$$\epsilon \rightarrow \epsilon(A)$$

A general modification to the dispersion relation would rather involve a general function of energy and momentum

$$\epsilon(A)A^2 = \epsilon(0)A^2 + \epsilon'(0)A^{(2+1)} + \frac{\epsilon''(0)}{2!}A^{(2+2)} + \frac{\epsilon'''(0)}{3!}A^{(2+3)} + \dots$$

The dispersion relation:

$$E^2 - p^2 \pm \delta_n A^{n+2} = m^2,$$

$$\delta_n \stackrel{n \geq 1}{=} \epsilon^{(n)} / M^n = 1 / (E_{LIV}^{(n)})^n$$

it is not necessarily bound to a particular LIV-model, which allows to generalize to some point the search of LIV-signatures.

LIV negligible at the lower standard energies

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II. Limits: TeV γ -rays

i. Time Energy Dependent delay

ii. Photon Decay

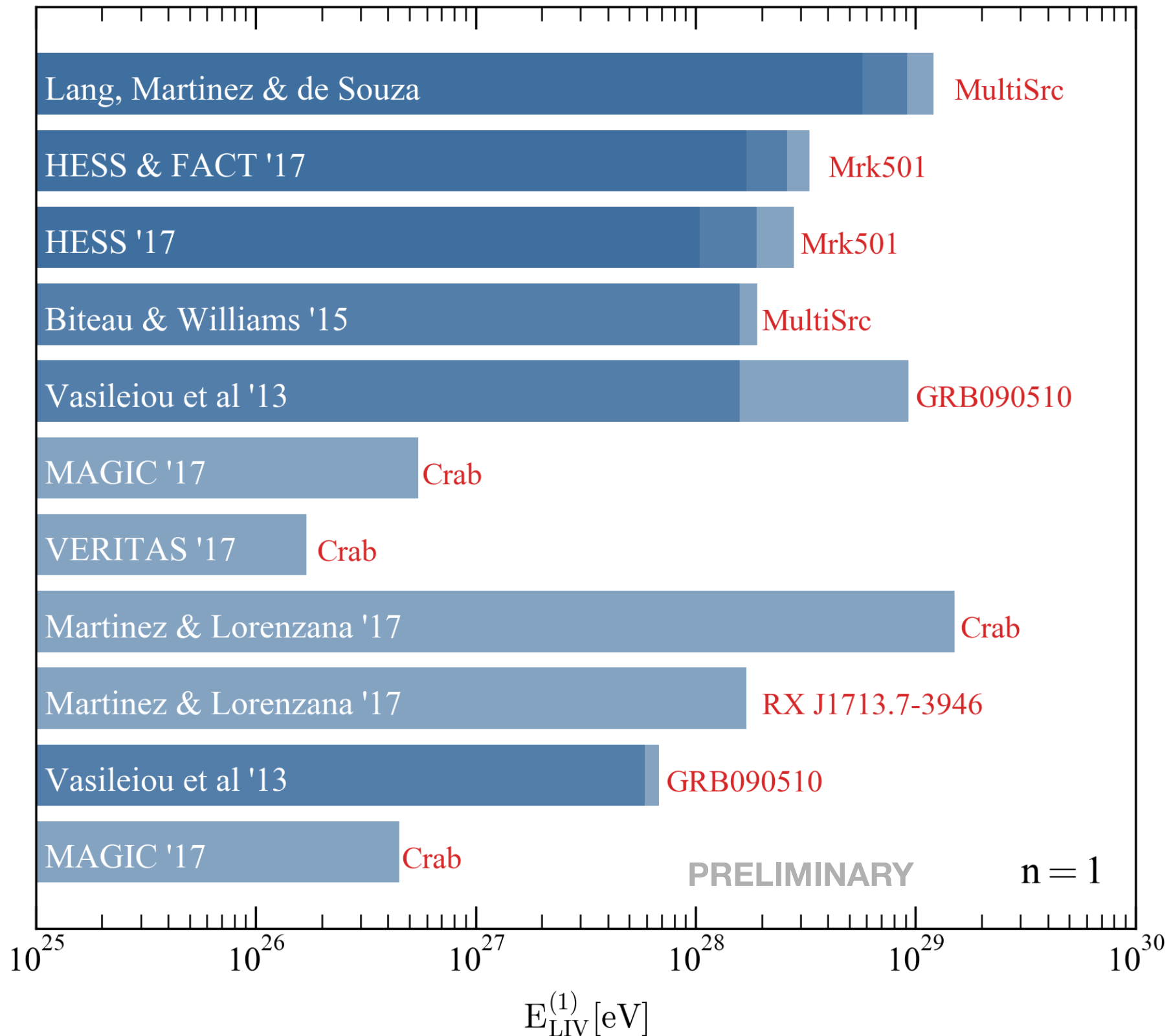
iii. Pair production threshold shifts

III. UHECR

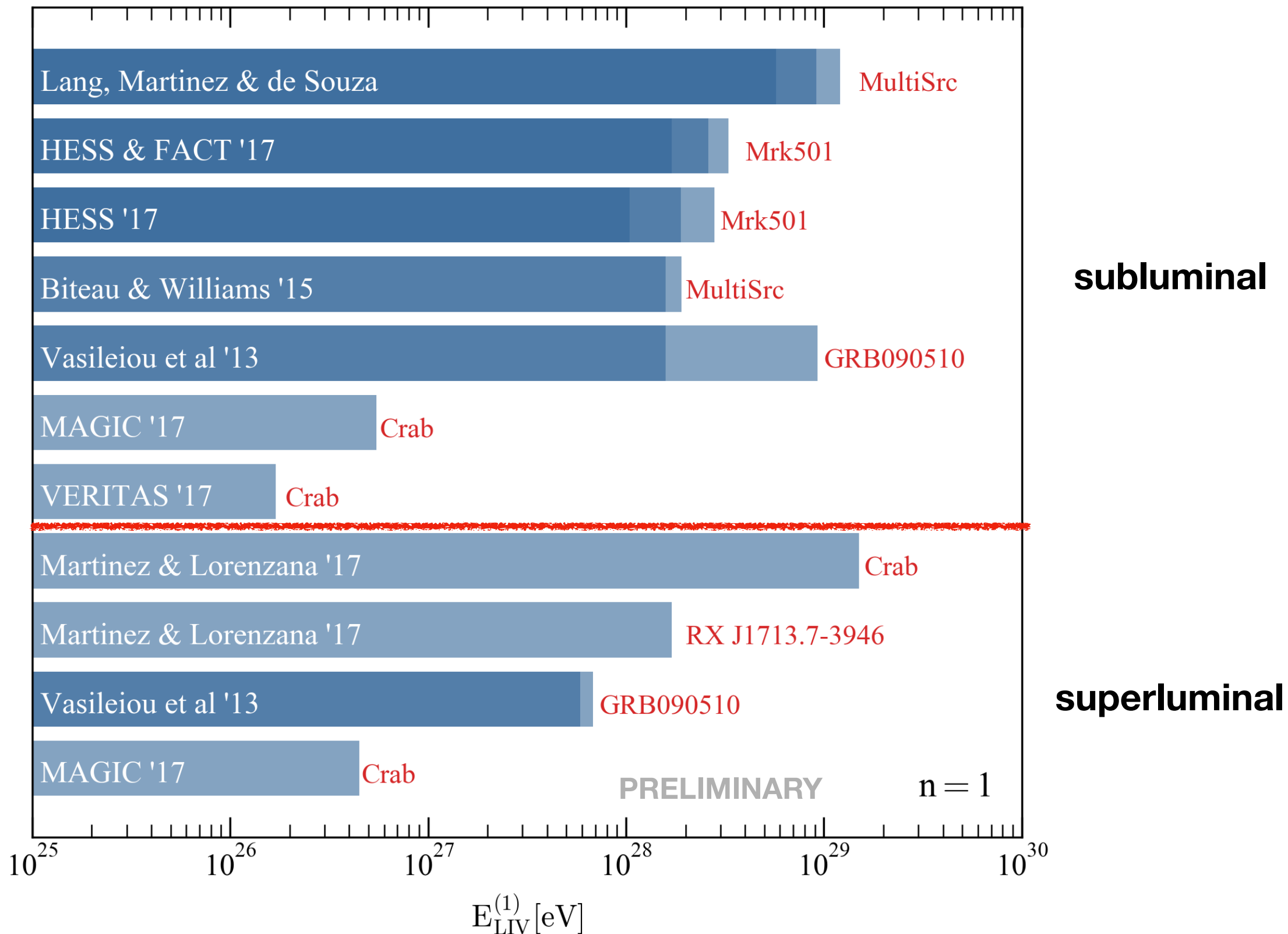
i. GZK-photons + LIV

ii. Limits

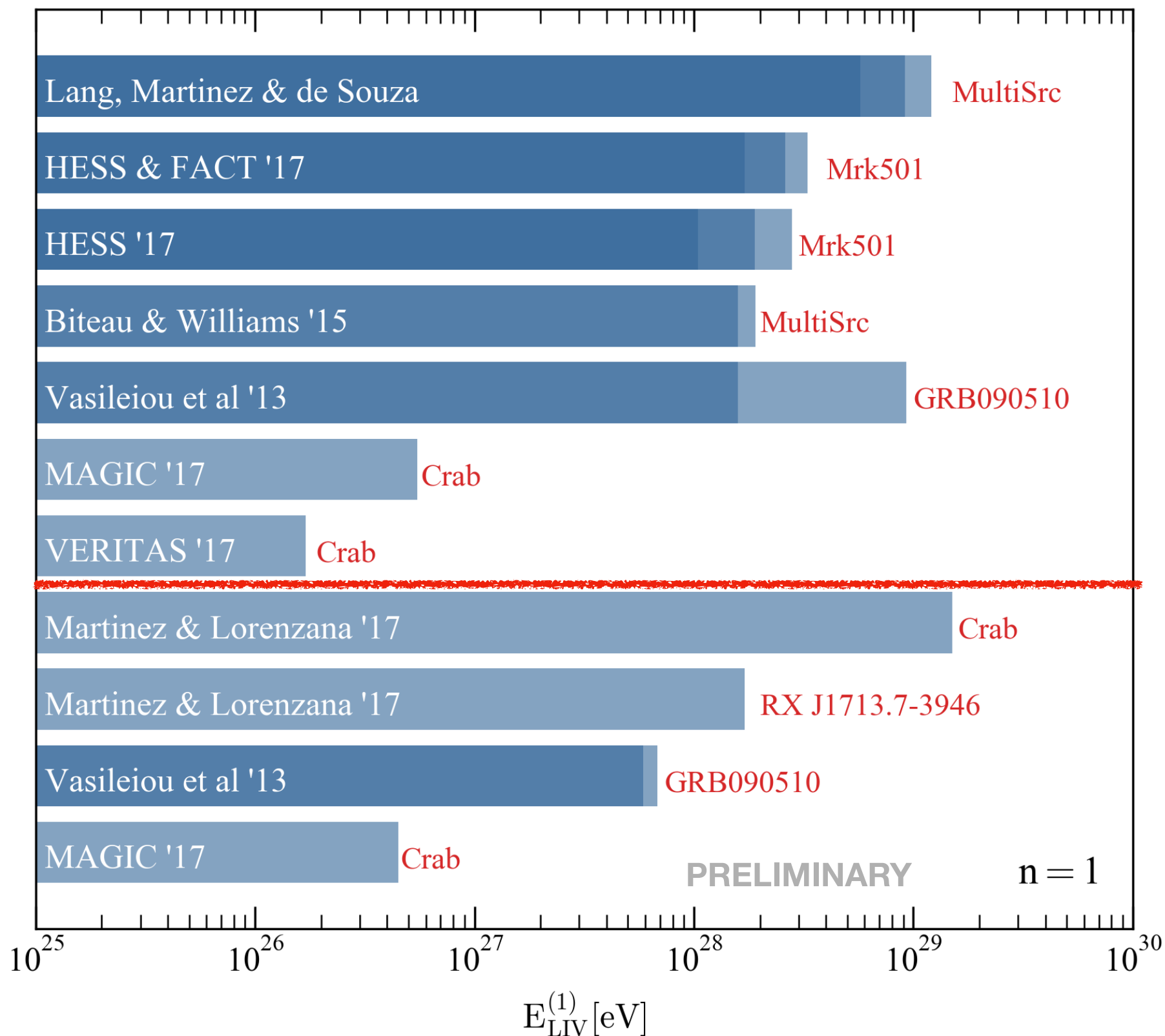
LIV limits by γ -rays



LIV limits by γ -rays



LIV limits by γ -rays



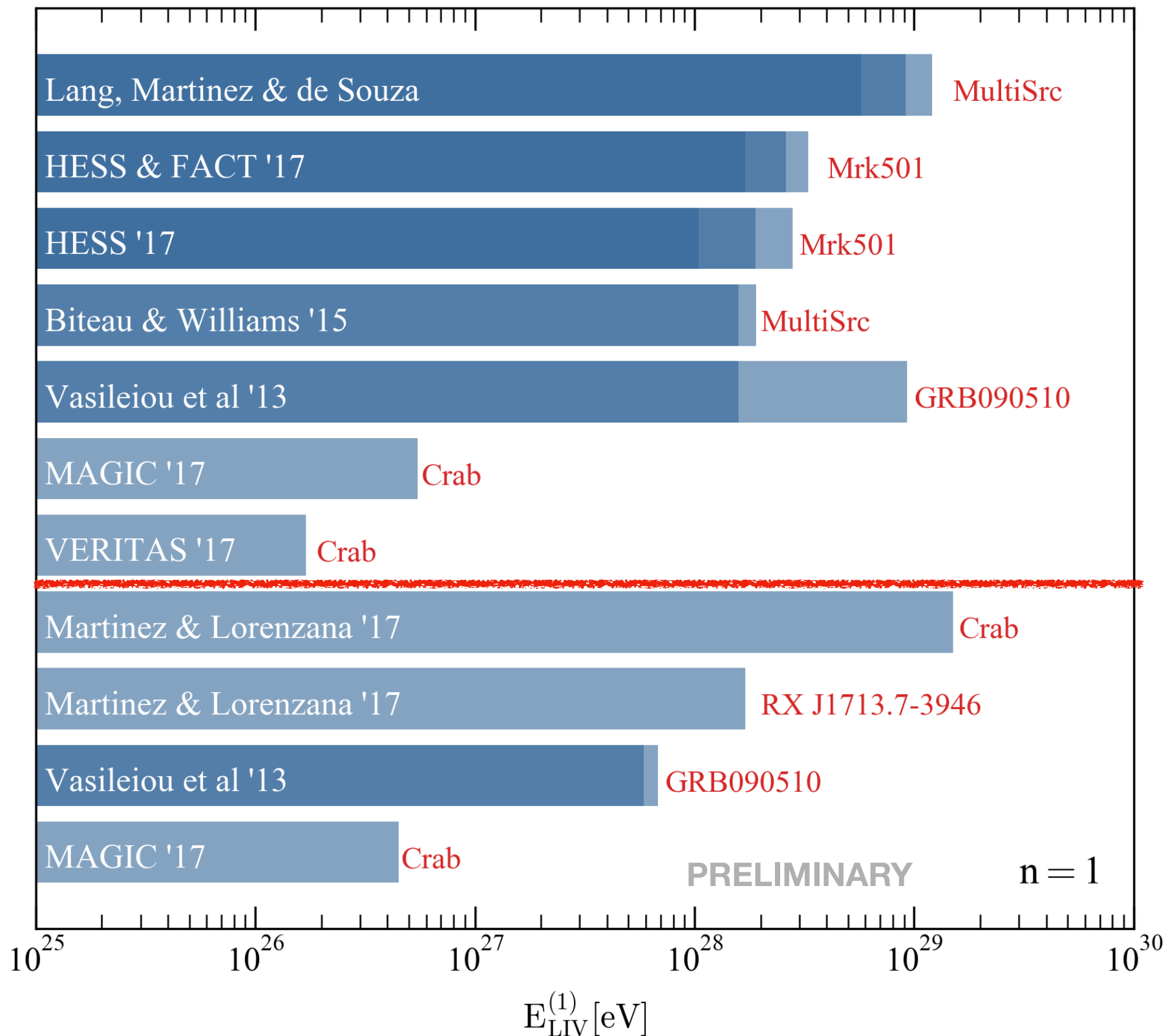
LIV limits by γ -rays

Pair production shift threshold

Time Energy Dependent -delay

Photon decay

Time Energy Dependent -delay



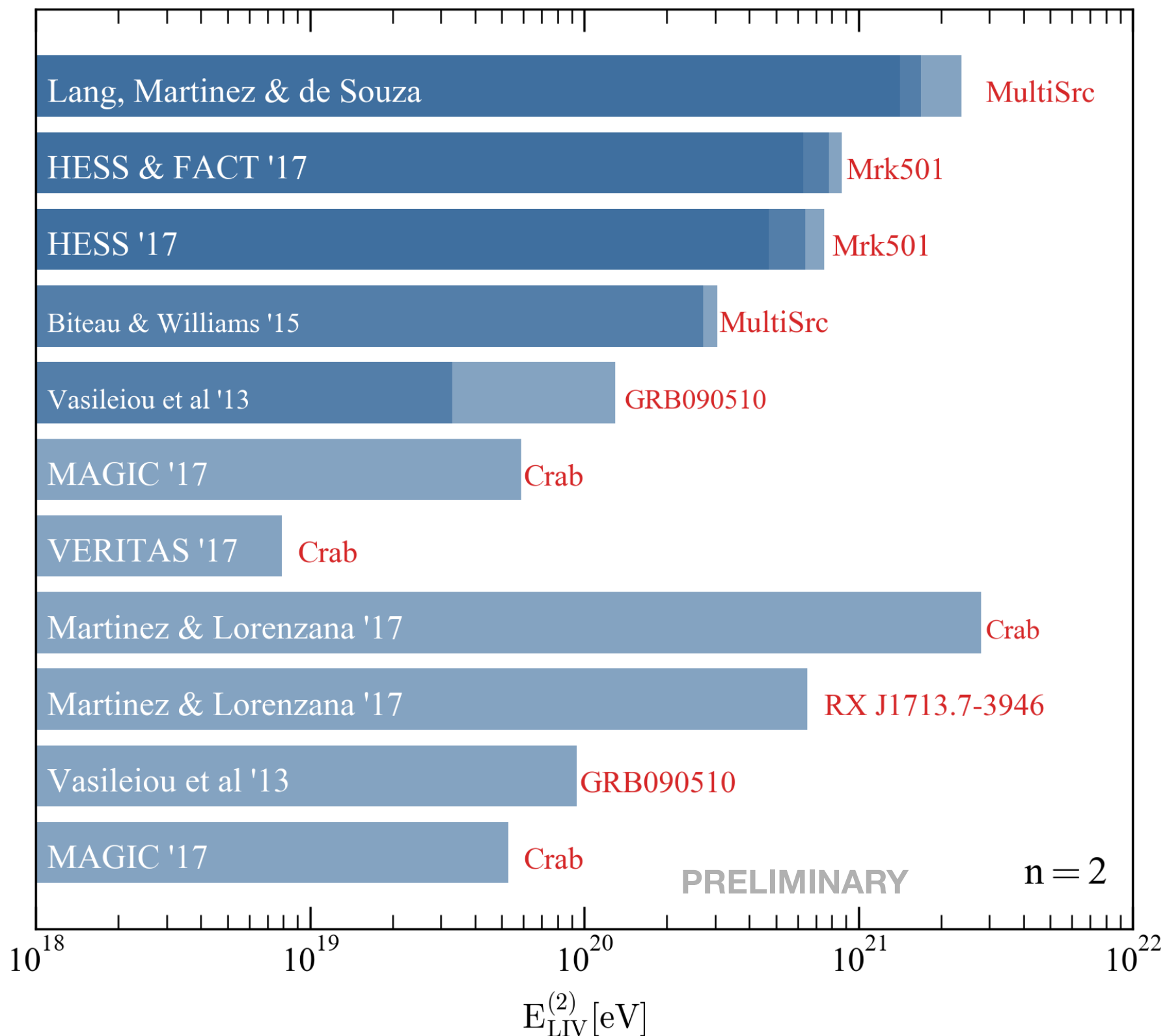
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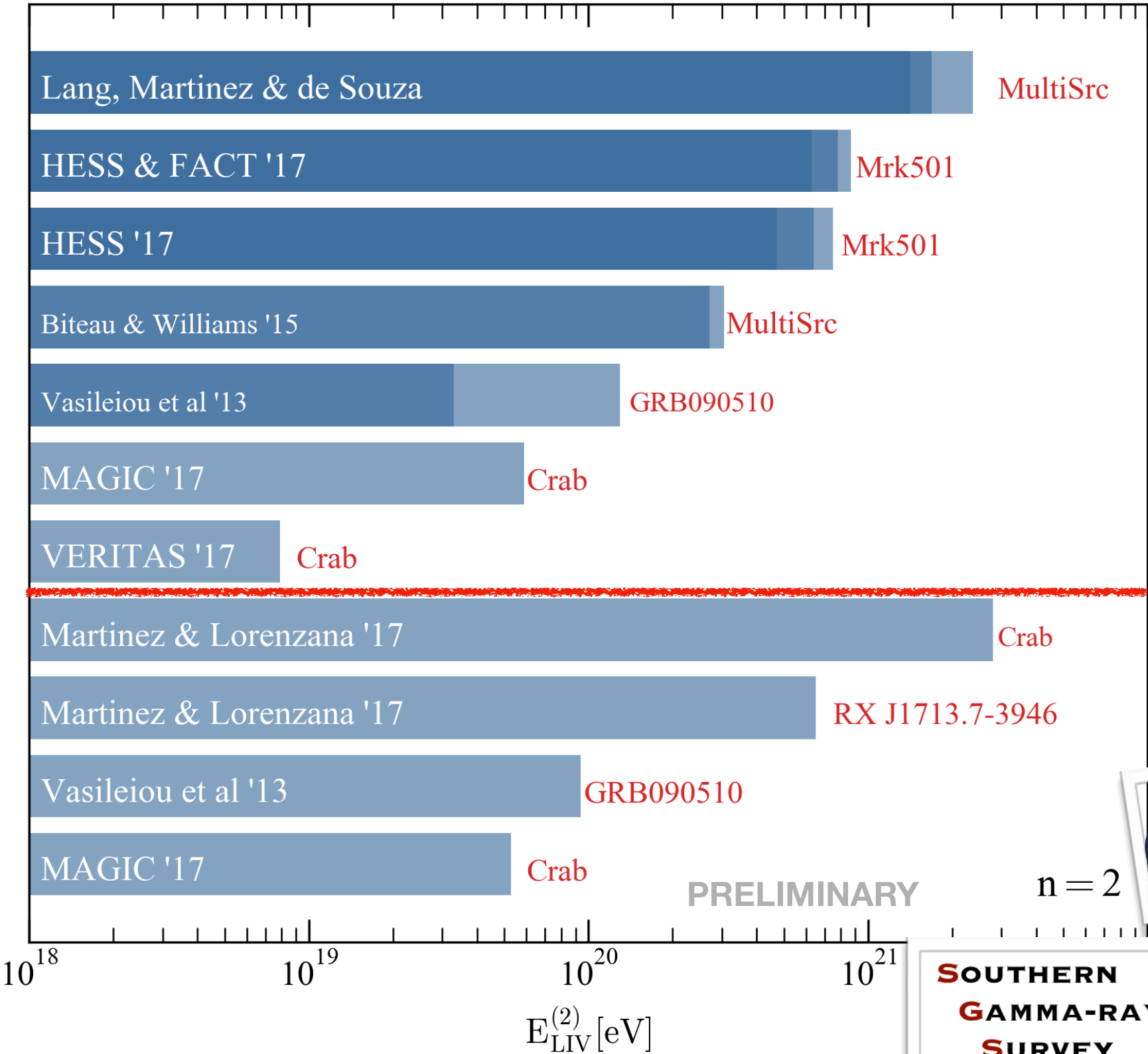
LIV limits by γ -rays

Pair production shift threshold

Time Energy Dependent -delay

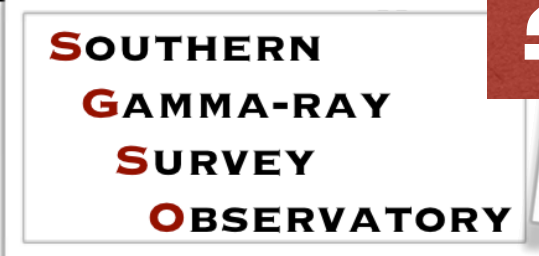
Photon decay

Time Energy Dependent -delay



PRELIMINARY

n = 2



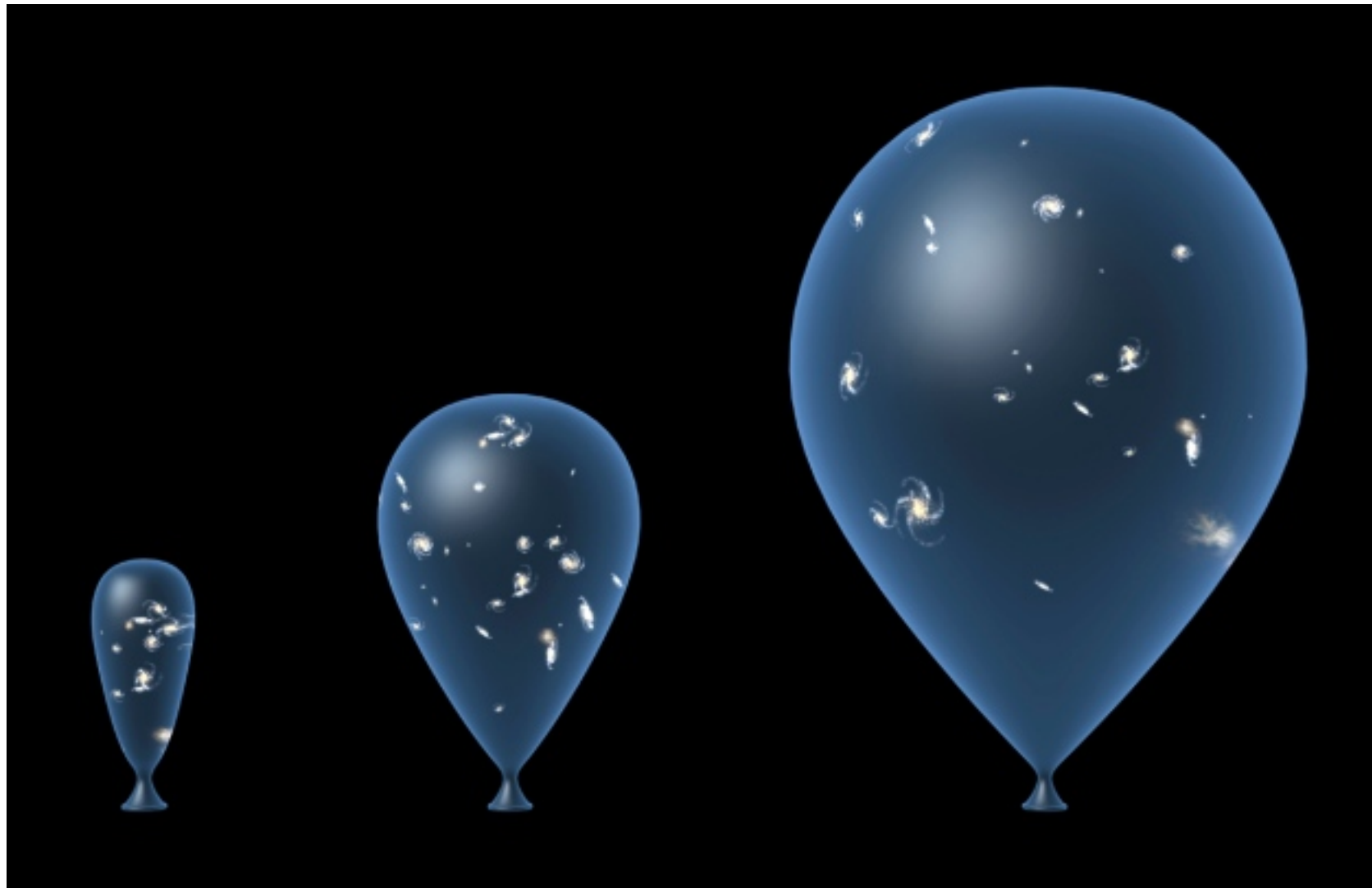
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Time energy dependent delay

The corresponding differential relation between time and redshift is

$$dt = -H_0^{-1} \frac{dz}{(1+z)h(z)} \quad ; \quad h(z) = \sqrt{\Omega_\Lambda + \Omega_m(1+z)^3}$$



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A particle with velocity u travels an elementary distance:

Two particles with velocities differing by Δu

$$u dt = -H_0^{-1} \frac{u dz}{(1+z)h(z)} \quad \longrightarrow \quad \Delta L = H_0^{-1} \int_0^z \frac{\Delta u dz}{(1+z)h(z)}$$

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LIV - energy dependence group velocity

$$E_\gamma^2 = p^2 \pm \left(\frac{E_\gamma^2}{E_{LIV}^{(n)}} \right)^n \quad \rightarrow \quad u = \frac{dE}{dp} \approx 1 + \frac{n+1}{2} \left(\frac{E_\gamma}{E_{LIV}^{(n)}} \right)^n$$

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Time energy dependent delay

Constraints on Lorentz Invariance Violation from *Fermi*-Large Area Telescope Observations of Gamma-Ray Bursts

V. Vasileiou,^{1,*} A. Jacholkowska,^{2,†} F. Piron,¹ J. Bolmont,² C. Couturier,²
J. Granot,³ F. W. Stecker,^{4,5} J. Cohen-Tanugi,¹ and F. Longo^{6,7}

GRB Name	PairView		SMM		Likelihood ^a	
	95%	99.5%	$n=1, s_{\pm}=+1$ (E_{PI} units)		95%	99.5%
080916C	0.11	0.081	95%	99.5%	0.22	0.2
090510	7.6	1.3	0.09	0.067	5.2	4.2
090902B	0.17	0.13	5.9	1.2	0.12	0.074
090926A	–	0.55	0.15	0.11	1.2	0.45
			8	0.35		
			$n=1, s_{\pm}=-1$ (E_{PI} units)			
	95%	99.5%	95%	99.5%	95%	99.5%
080916C	18	0.33	5.4	0.31	0.2	0.18
090510	0.56	0.48	0.57	0.48	11	3.6
090902B	0.38	0.2	0.86	0.28	0.37	0.11
090926A	0.24	0.18	0.2	0.12	0.17	0.15
			$n=2, s_{\pm}=+1$ (10^{10} GeV units)			
	95%	99.5%	95%	99.5%	95%	99.5%
080916C	0.31	0.28	0.24	0.21	0.35	0.33
090510	6.7	3.3	13	3.3	8.6	6.4
090902B	0.8	0.72	0.73	0.64	0.64	0.49
090926A	0.67	0.48	9.1	1.6	0.48	0.47
			$n=2, s_{\pm}=-1$ (10^{10} GeV units)			
	95%	99.5%	95%	99.5%	95%	99.5%
080916C	–	0.69	–	5.2	0.34	0.32
090510	1.9	1.5	1.9	1.5	9.4	5.4
090902B	1.6	0.97	3.5	1.2	0.64	0.46
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Time energy dependent delay



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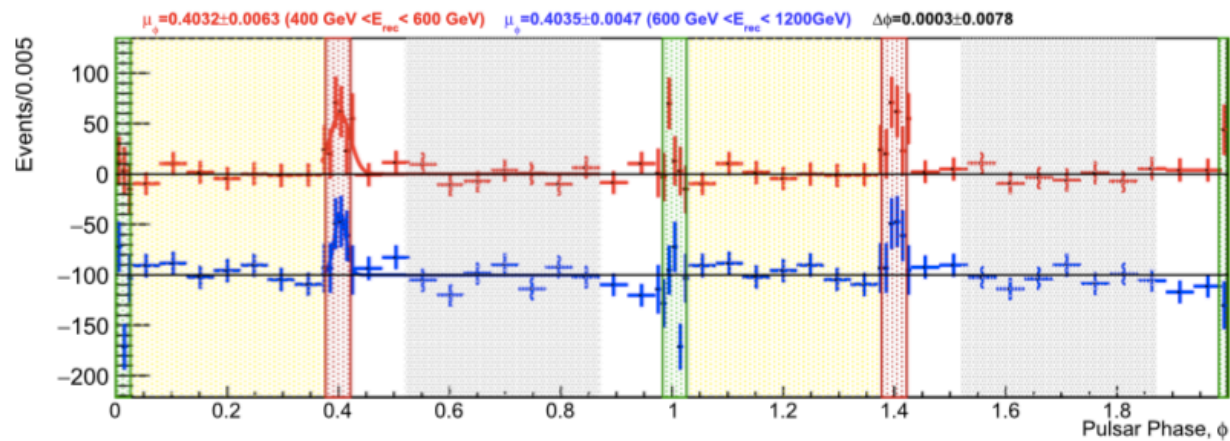
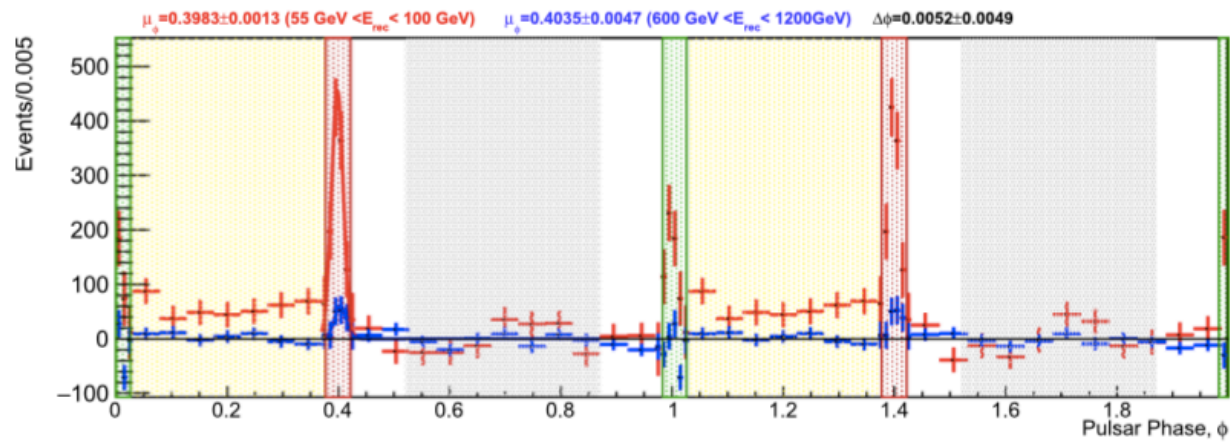


Table 2
Obtained 95%CL Limits from the Peak Comparison Method

Case	55–100 GeV versus 600–1200 GeV	400–600 GeV versus 600–1200 GeV
	E_{QG1} (GeV)	
$\xi_1 = +1$	2.5×10^{17}	1.1×10^{17}
$\xi_1 = -1$	6.7×10^{17}	1.1×10^{17}
	E_{QG2} (GeV)	
$\xi_2 = +1$	1.8×10^{10}	1.4×10^{10}
$\xi_2 = -1$	2.9×10^{10}	1.5×10^{10}

Time energy dependent delay



Source	Experiment	Limit on $E_{QG}^{(1)}$	Limit on $E_{QG}^{(2)}$	Distance	Δt	E_{max}	Ref.
HAWC Pulsar ref.	HAWC	10^{17} GeV	$9 \cdot 10^9$ GeV	2kpc	1 ms	500GeV	
HAWC GRB ref.	HAWC	$4.9 \cdot 10^{19}$ GeV	$1.1 \cdot 10^{11}$ GeV	$z = 1$	1 s	100GeV	

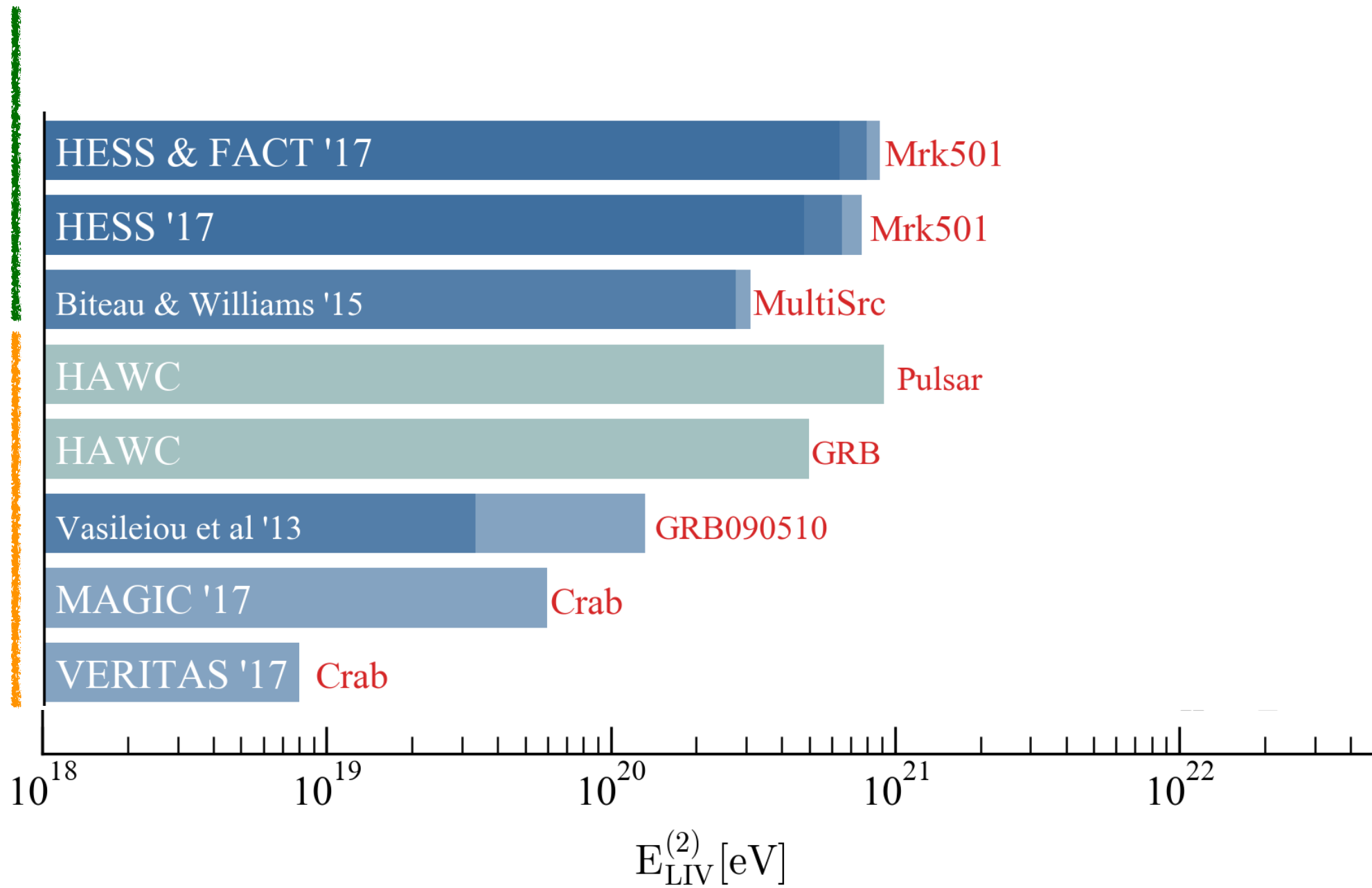
The potential of the HAWC observatory,
based on the reference scenarios

Time energy dependent delay



Pair production shift threshold

Time Energy Dependent



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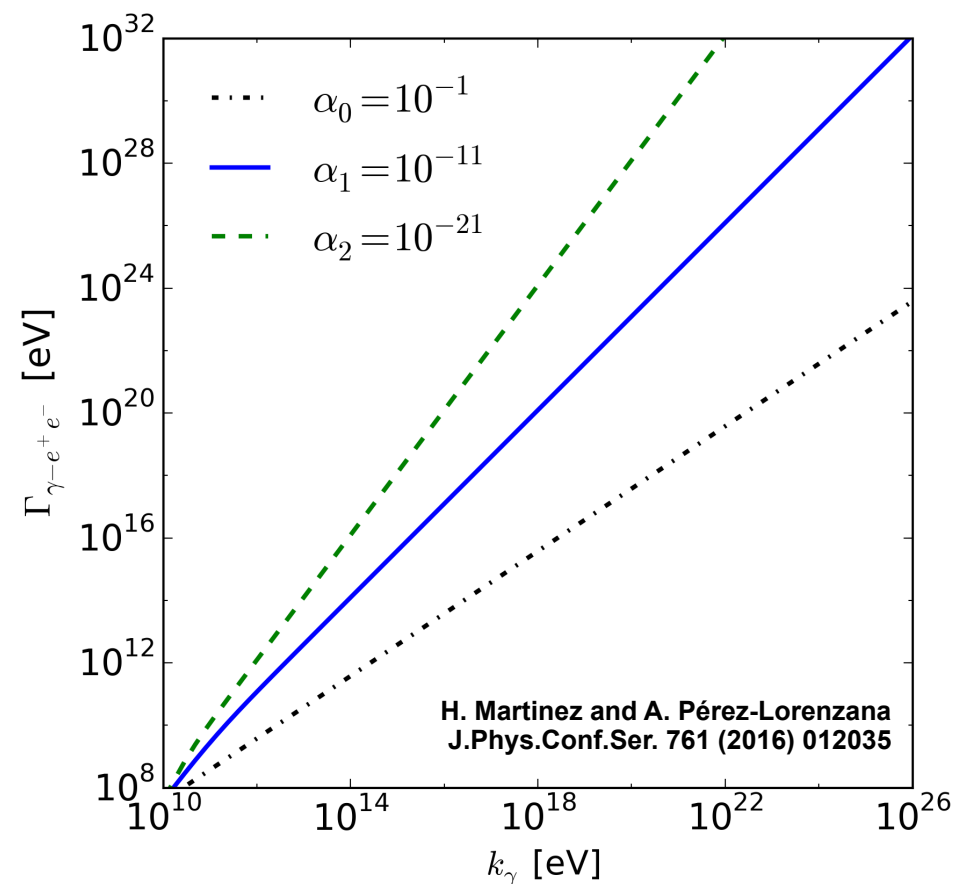
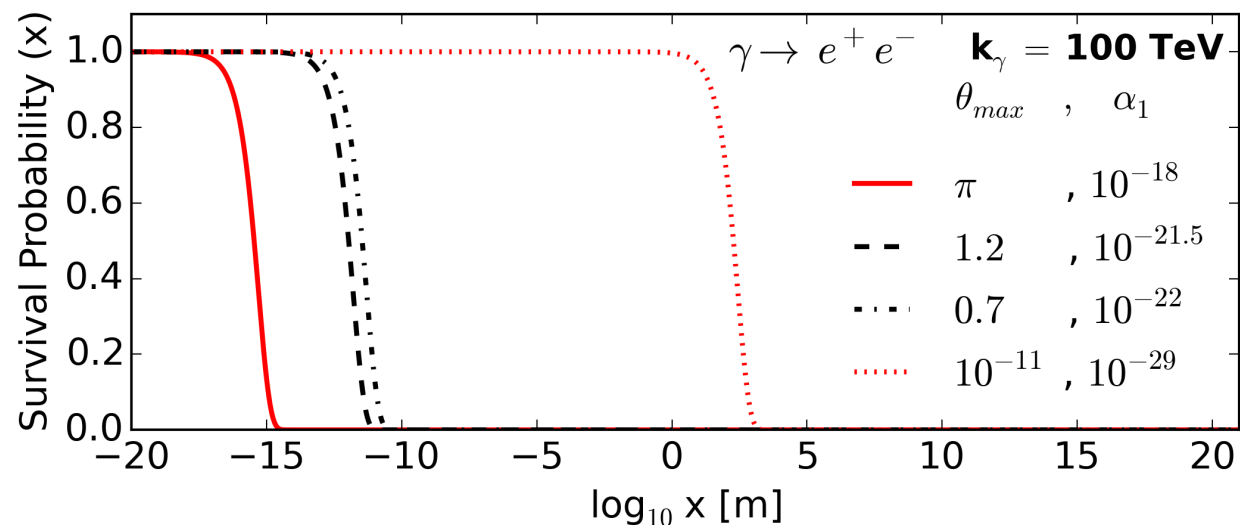
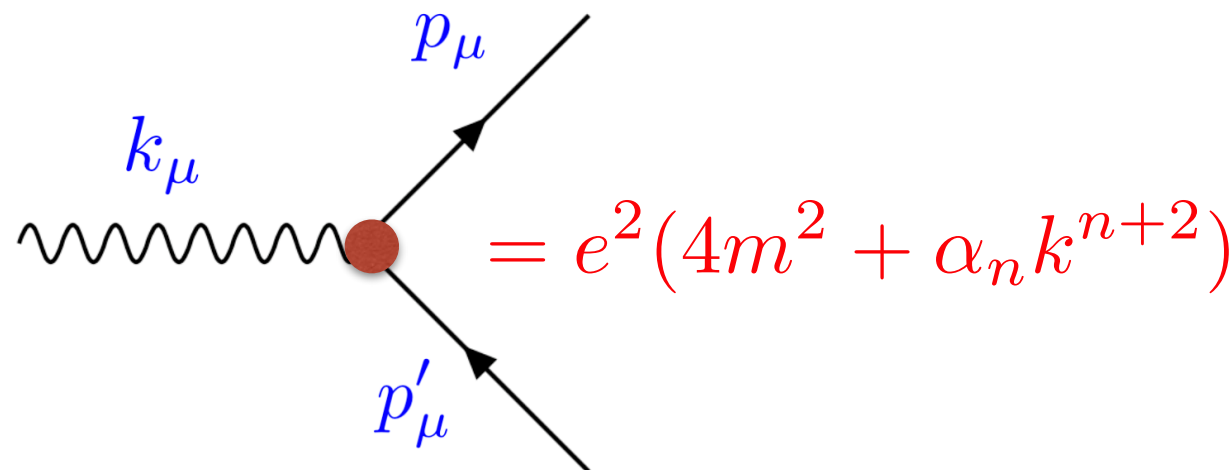
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Photon decay

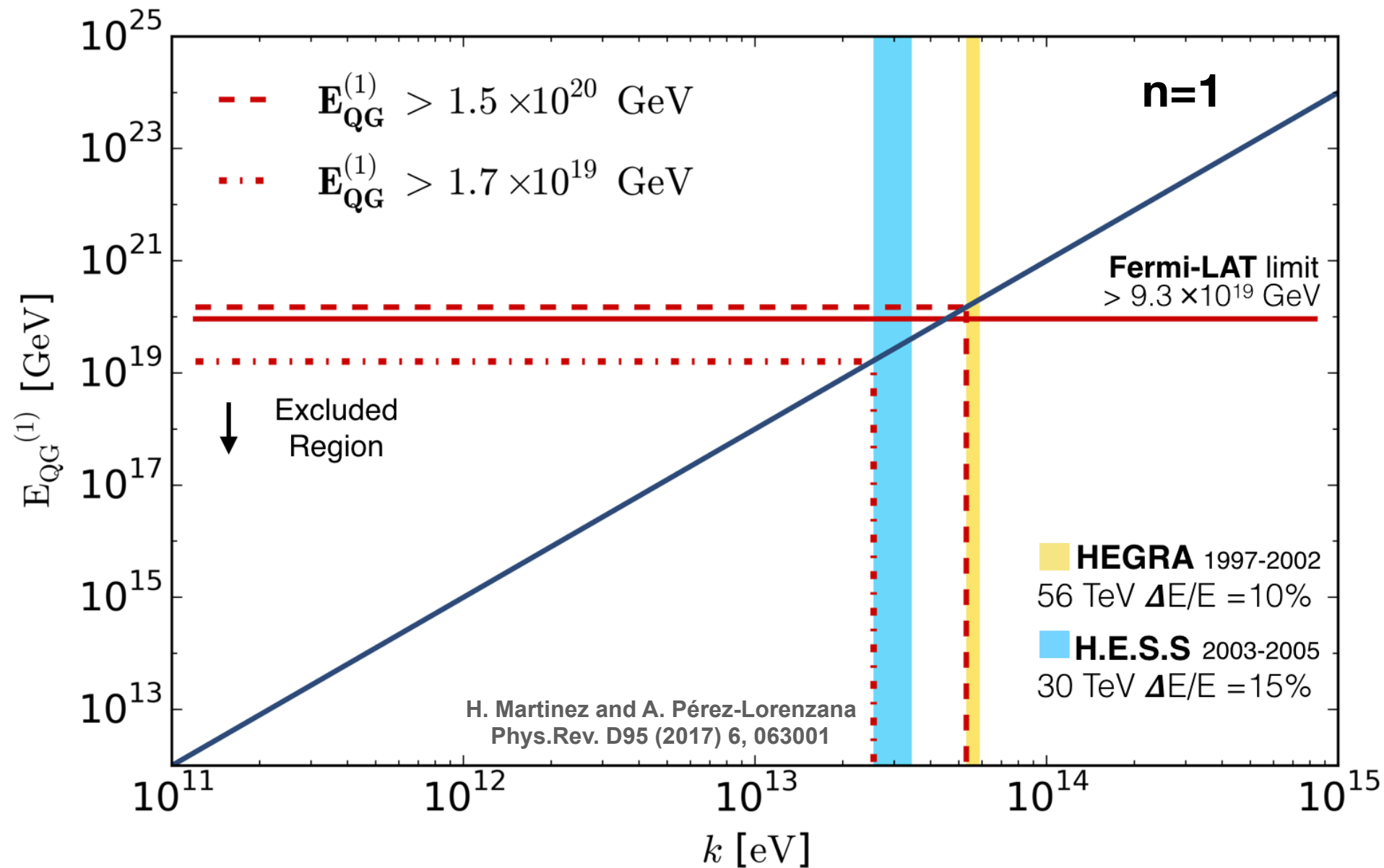


Above this energy threshold, the decay rate is quite efficient that photons should not arrive at Earth from astrophysical distances

$$E_{LIV}^{(n)} > E_\gamma \left[\frac{E_\gamma^2 - 4m_{e^-}^2}{4m_{e^-}^2} \right]^{1/n}$$

If you observe VHE gamma-rays, the LIV process is restricted!!

E_{LIV} excluded region due to $\gamma \rightarrow e^+e^-$



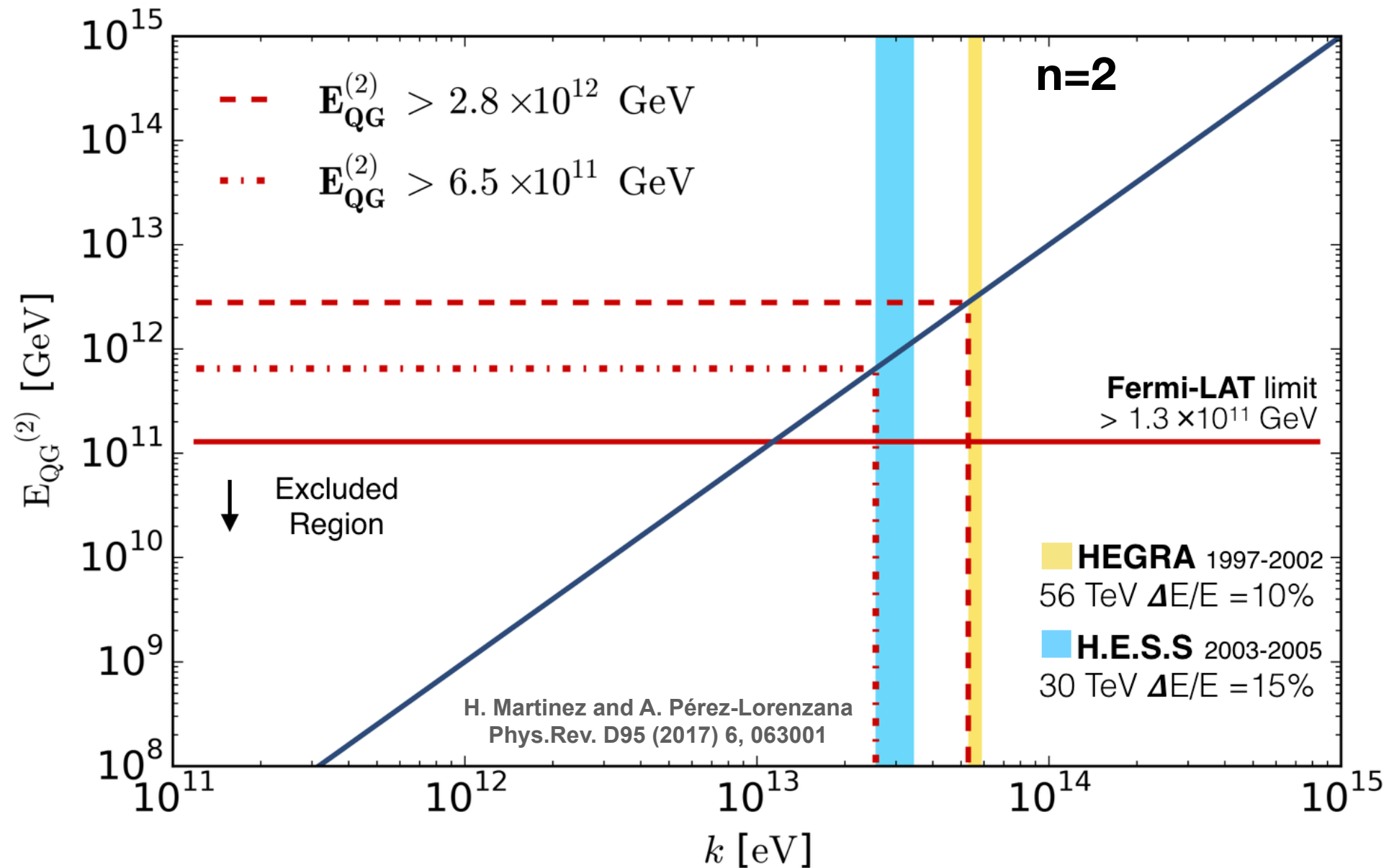
CRAB

HEGRA Collaboration,
 The Astrophysical Journal,
 614:897-913, 2004

SNR RX J1713.7.3946

HESS Collaboration,
 Astron. Astrophys, 449, 223
 (2007)

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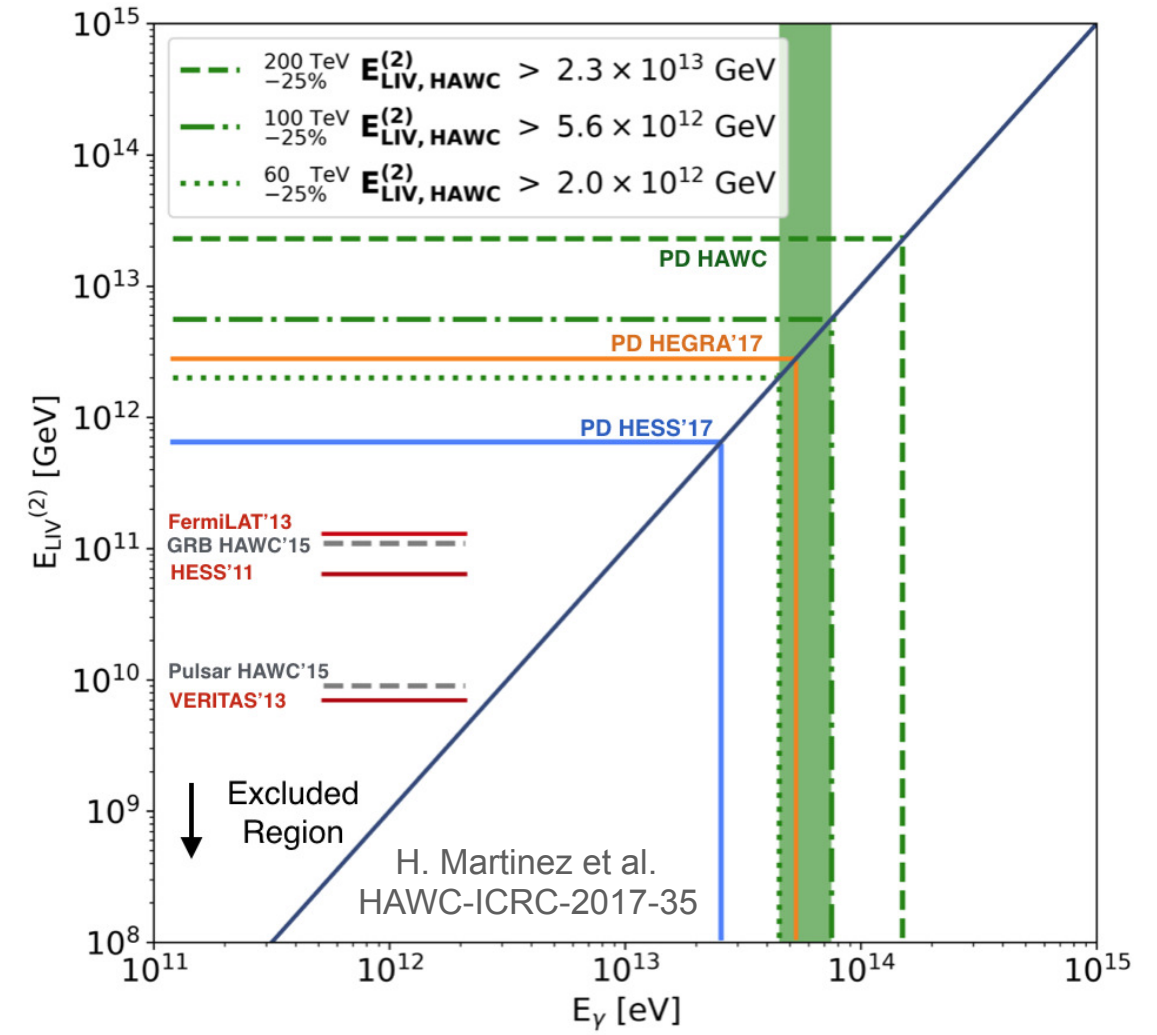
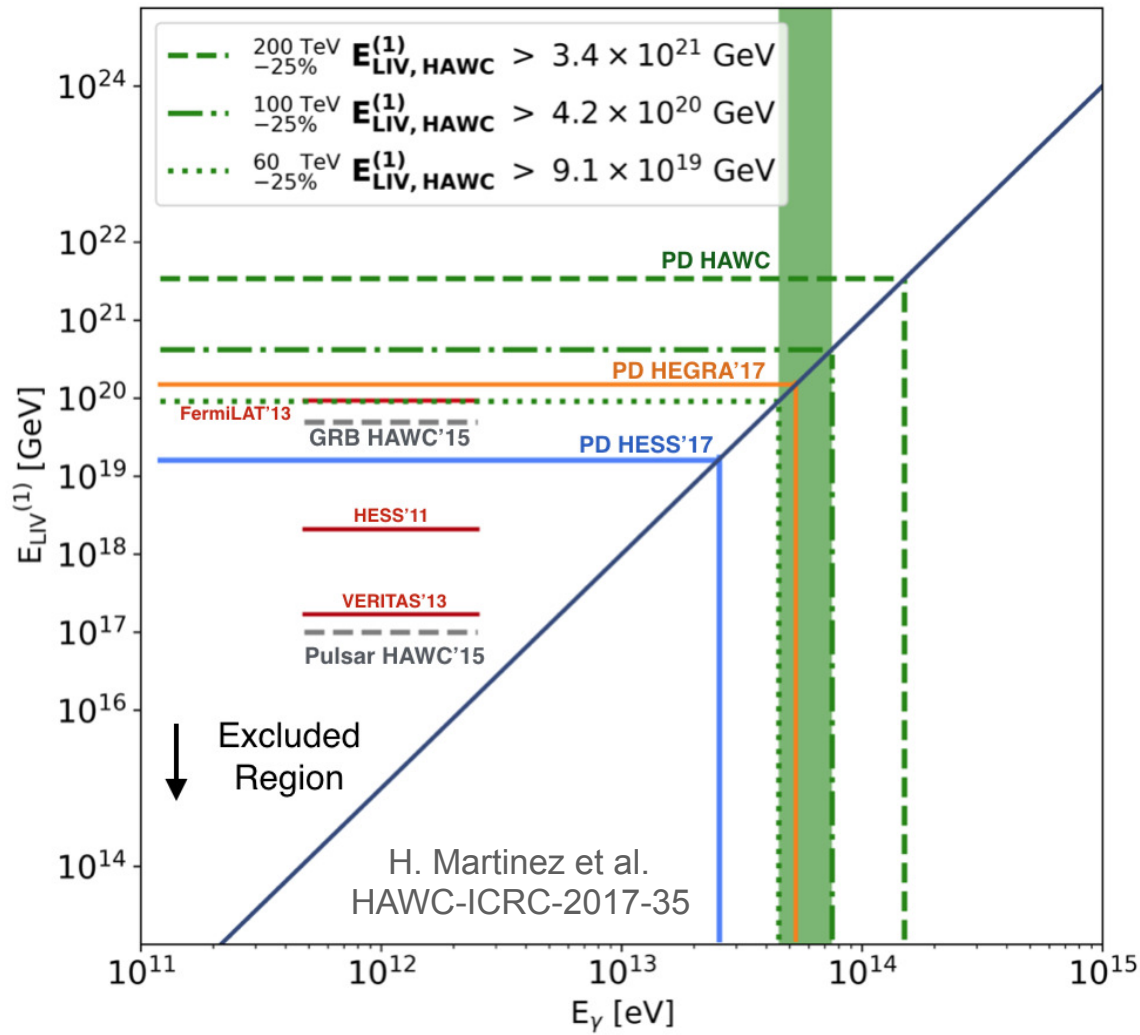


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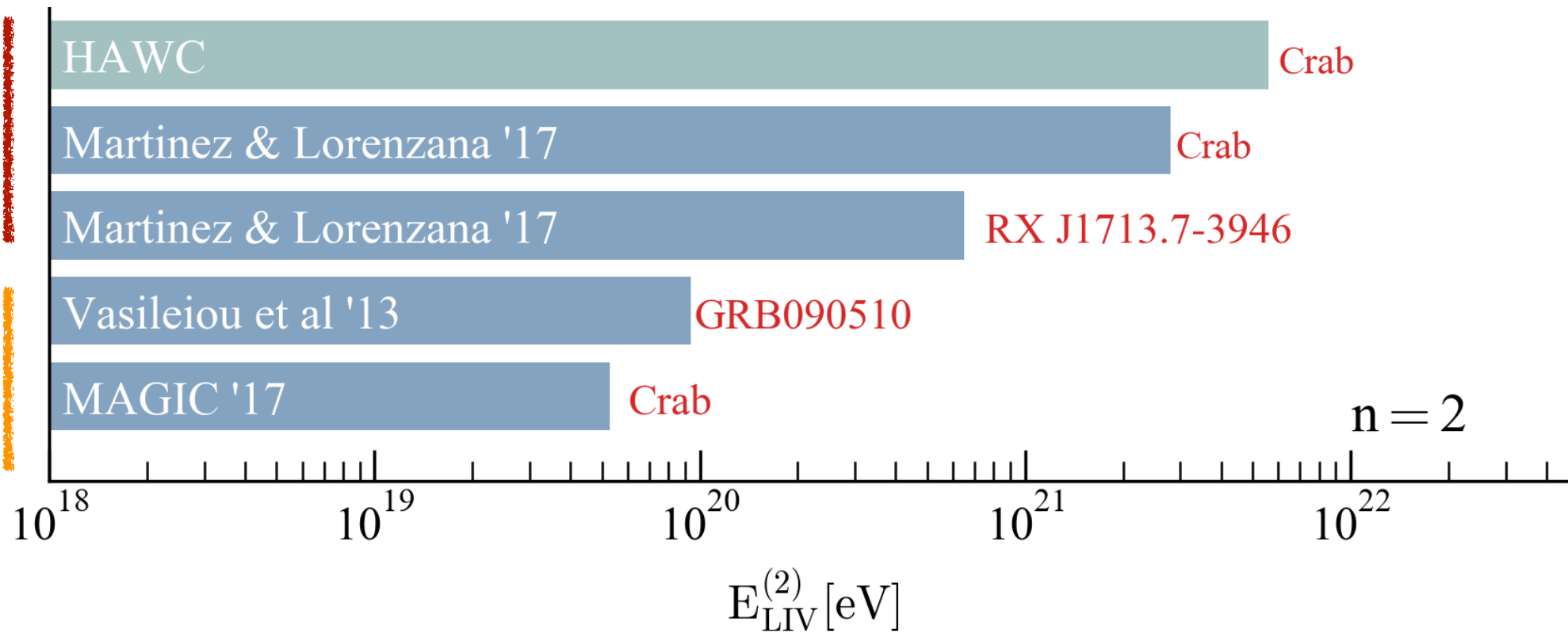


ELIV potential limits from HAWC
 for $n=1$ (left), $n=2$ (right) and energy unc. of 25%.



Photon
decay

Time
Energy
Dependent



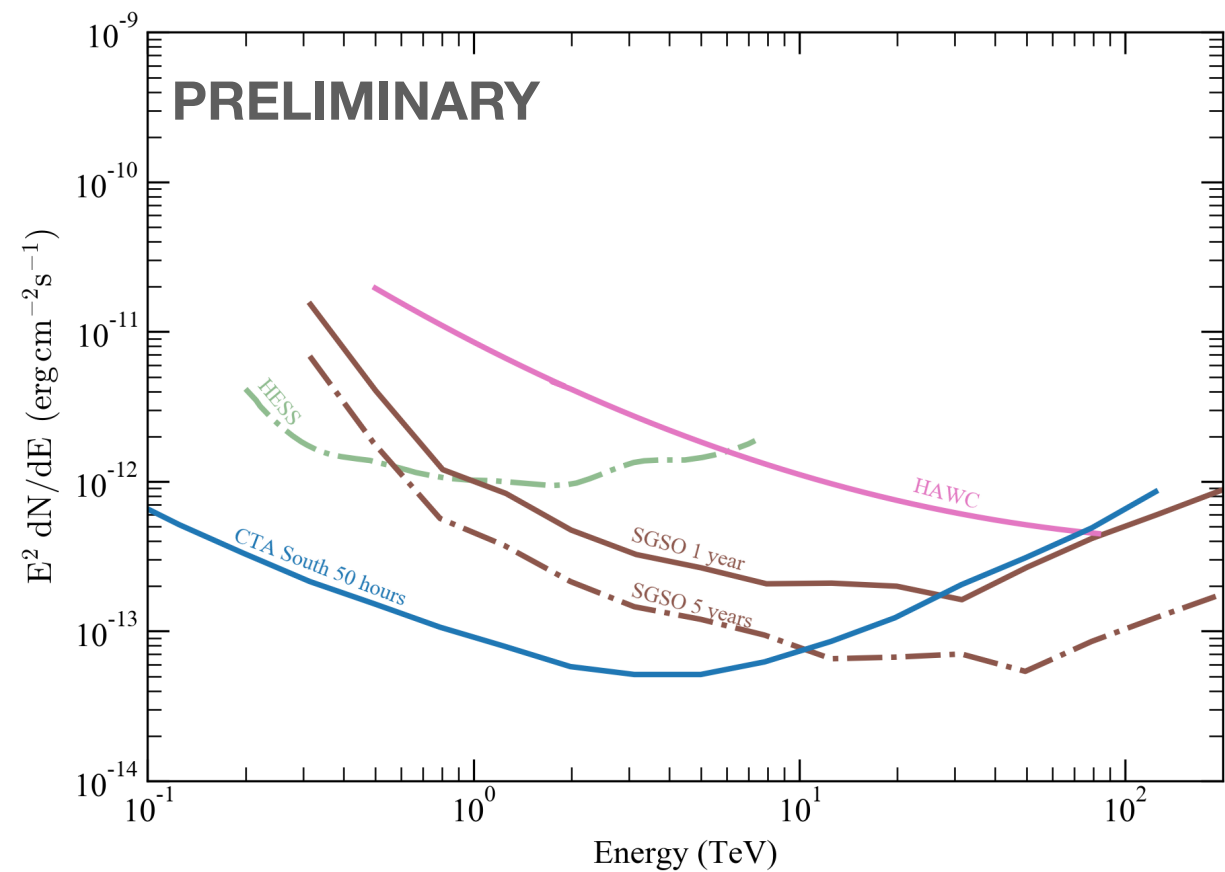
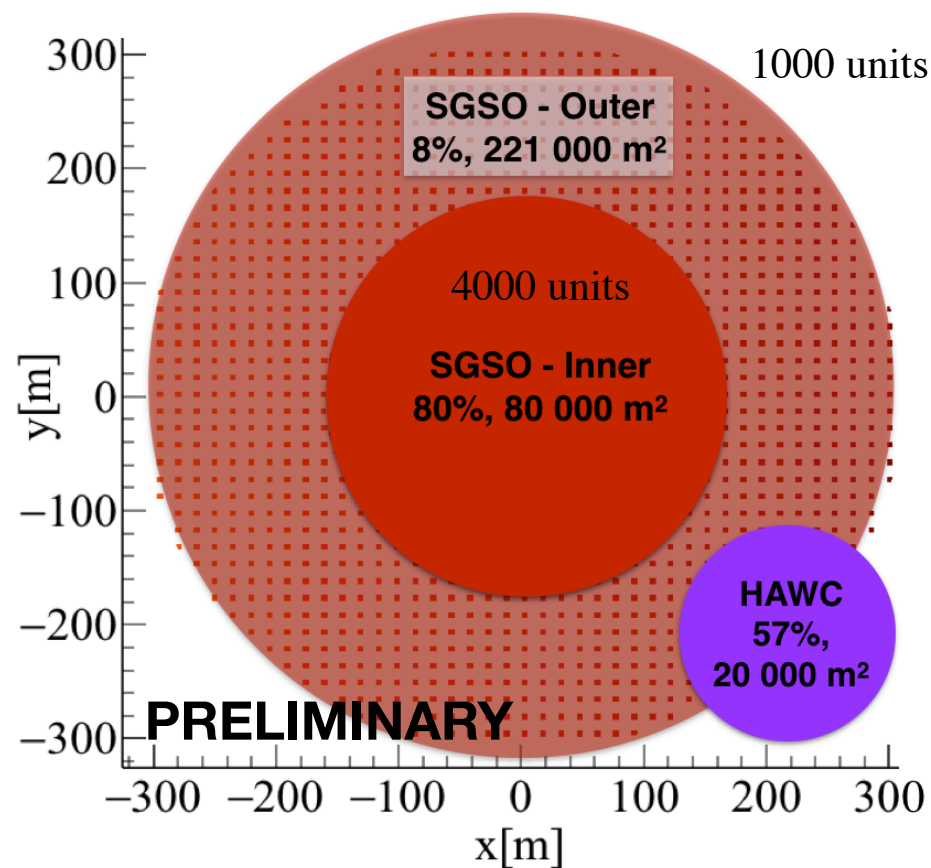
ELIV potential limits from HAWC

n=2 and energy unc. of 25%.

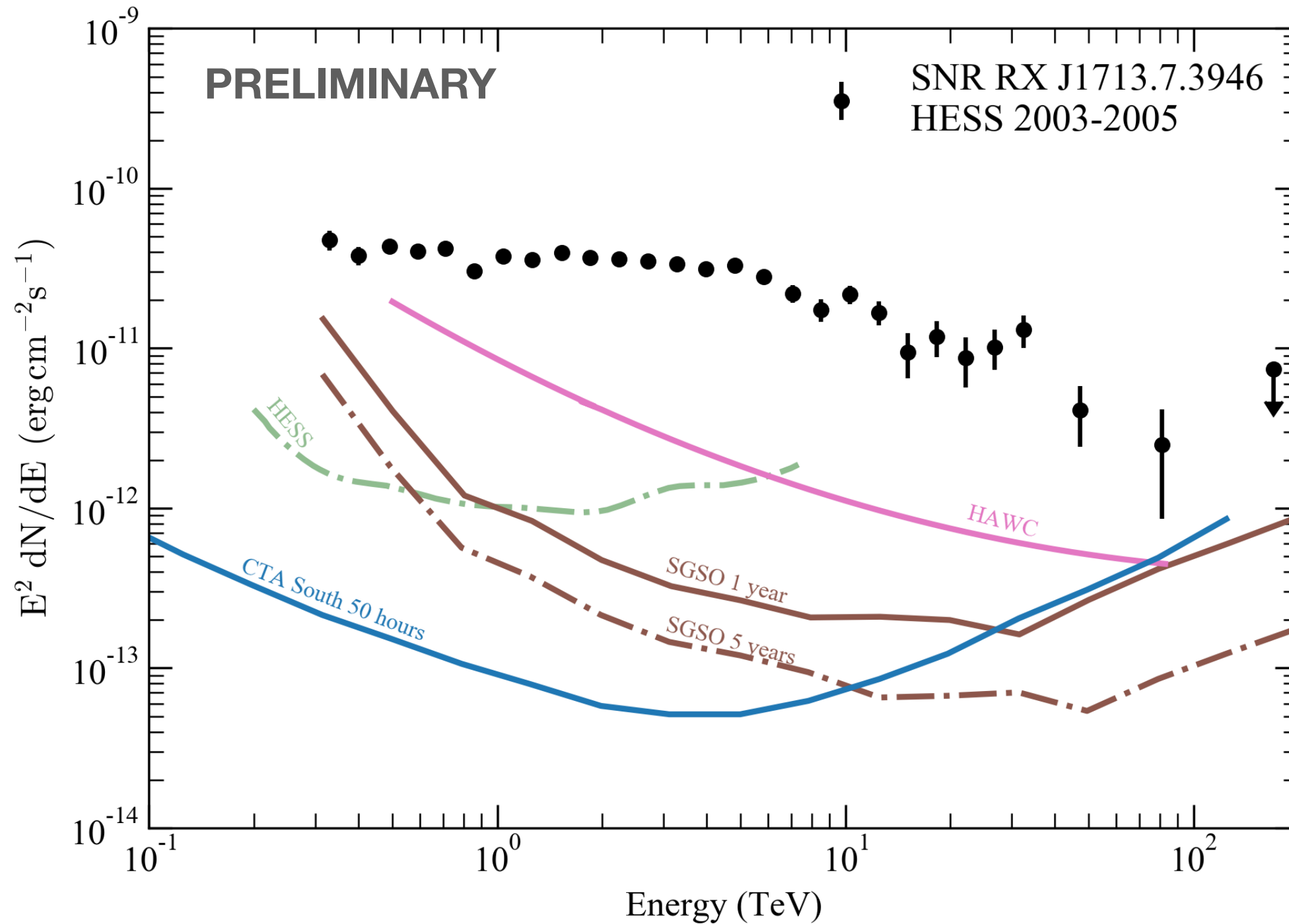
Searching LIV signatures with SGSO



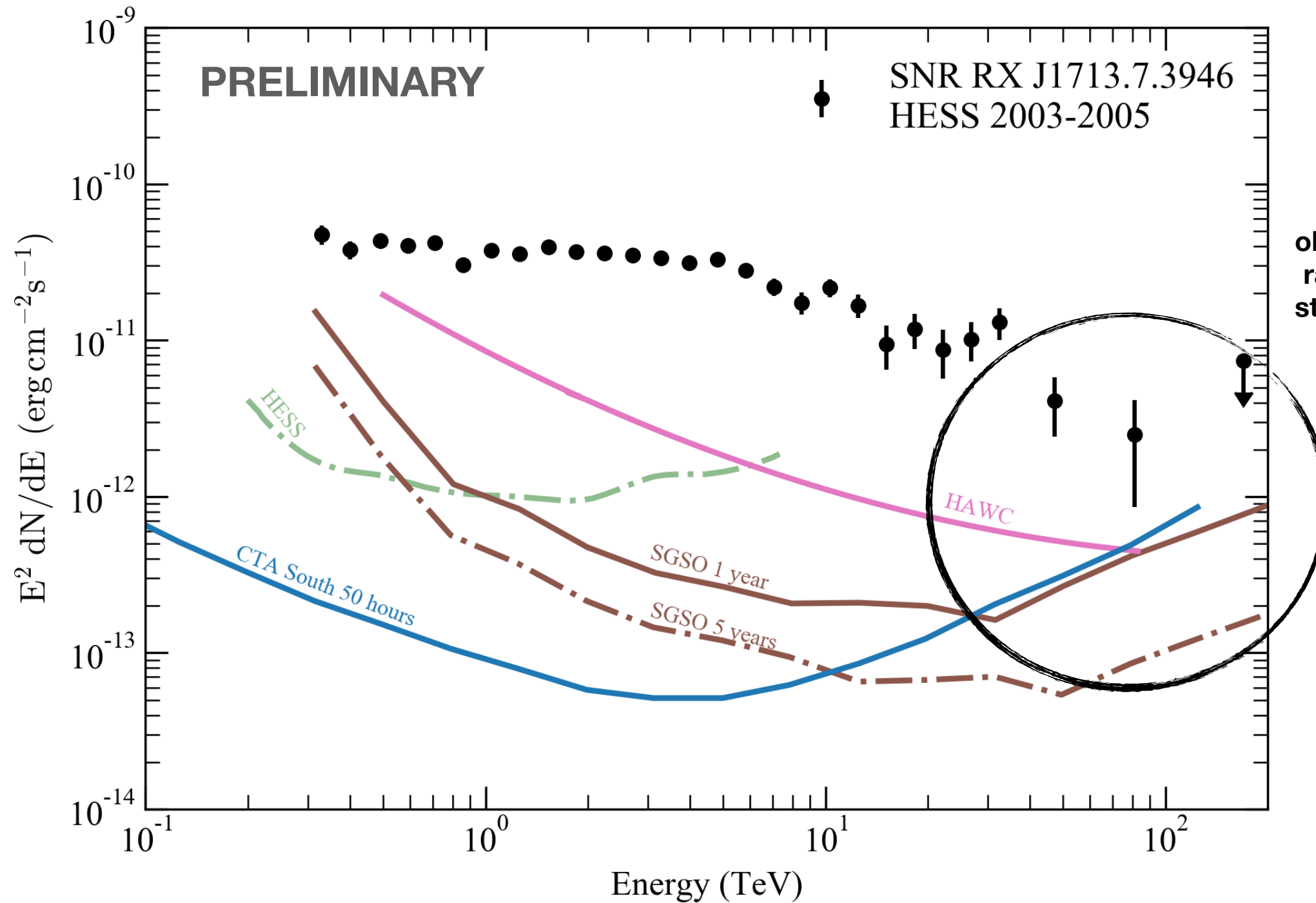
Cerro Vecar, province of Salta, Argentina.



Searching LIV signatures with SGSO



Searching LIV signatures with SGSO



The higher the
observed gamma-
ray energy is, the
stringent the limit!

Searching LIV signatures with SGSO

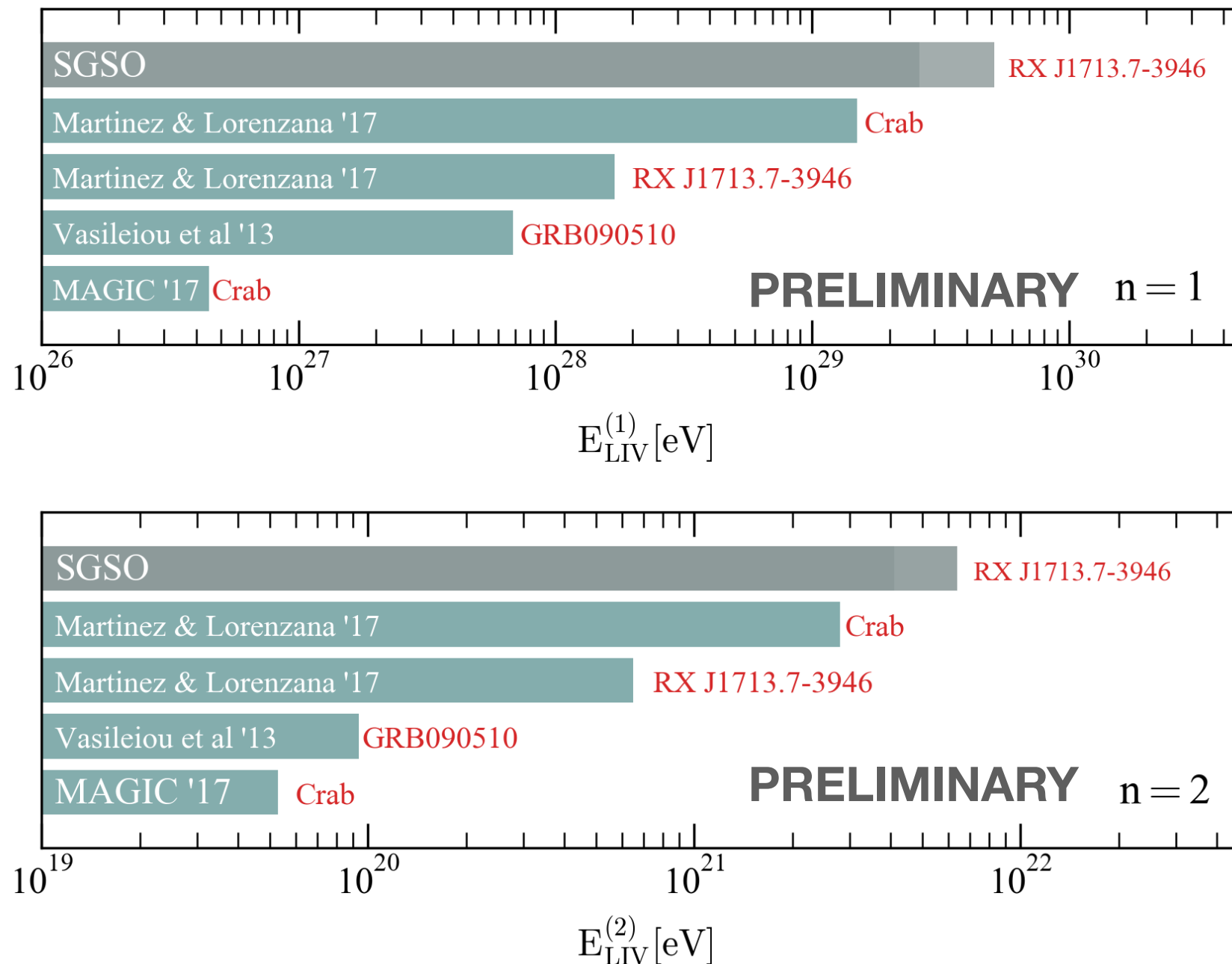


Fig. 1

LIV energy scale limits from superluminal searches including a potential reference of SGSO by measuring RXJ1713.7-3946 photons at **80 TeV** and **100 TeV** and the absence of photon decay into electron-positron pairs.

White paper in
preparation

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 - ii. Limits

Pair Production

$$\gamma_{VHE} \gamma_{BKG} \rightarrow e^+ e^-$$

$$\Lambda_{\gamma,n} x_{\gamma}^{n+2} + x_{\gamma} - 1 = 0$$

$$x_{\gamma} = \frac{E_{\gamma}}{E_{\gamma}^{LI}}, \quad \Lambda_{\gamma,n} = \frac{E_{\gamma}^{LI(n+1)}}{4\epsilon} \delta_{\gamma,n}$$

$$\Lambda_n < 0$$

Threshold-shifts

$$\Lambda_n = 0$$

LI scenario

$$\Lambda_n > 0$$

+2nd Threshold

The threshold equation

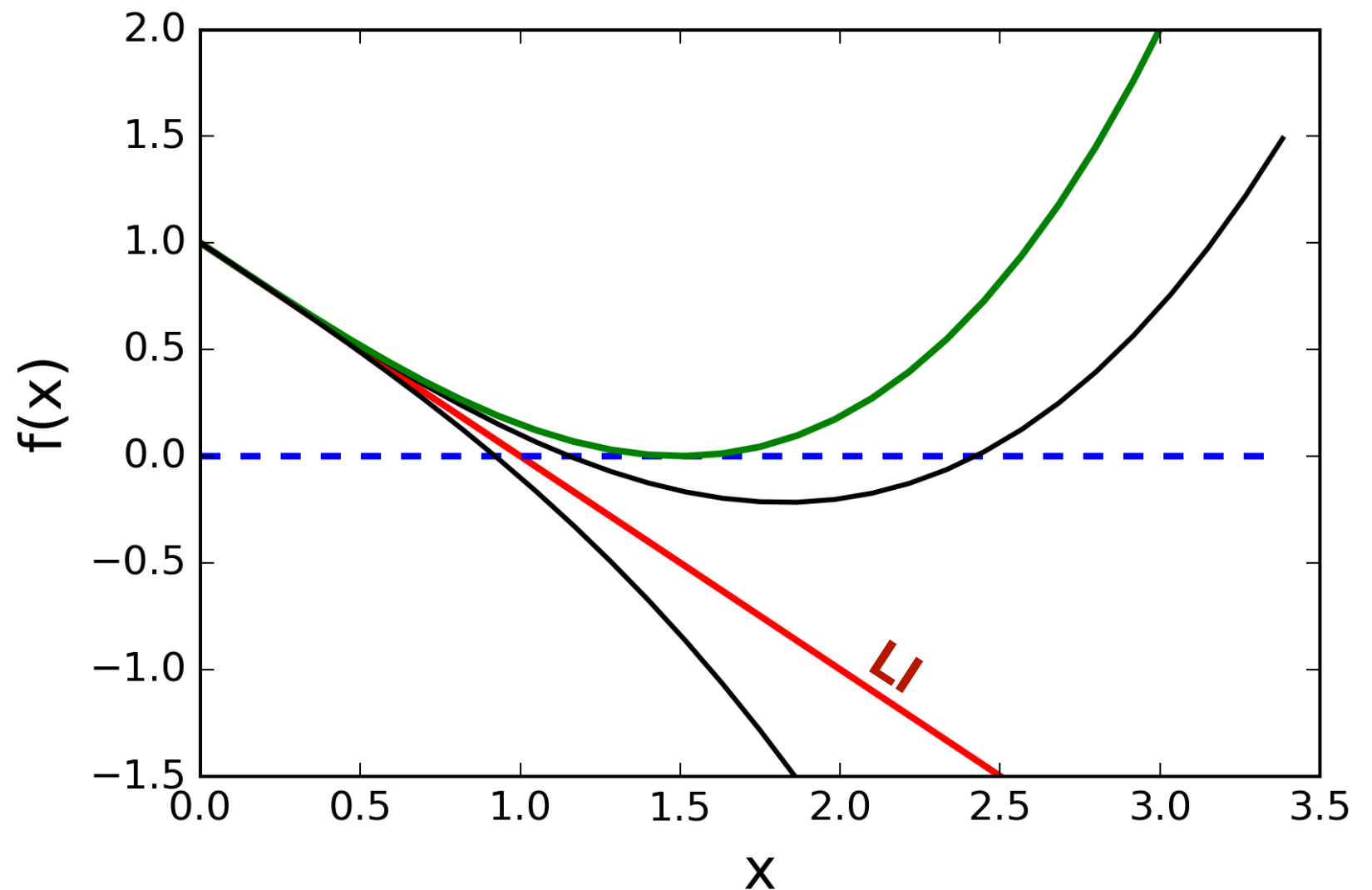
$$\delta_{\gamma,n} E_{\gamma}^{n+2} + 4E_{\gamma}\epsilon - m_e^2 \frac{1}{K(1-K)} = 0$$

Critical point

$$\delta_{\gamma,n}^{lim} = -4 \frac{\epsilon}{E_{\gamma}^{LI(n+1)}} \frac{(n+1)^{n+1}}{(n+2)^{n+2}}$$

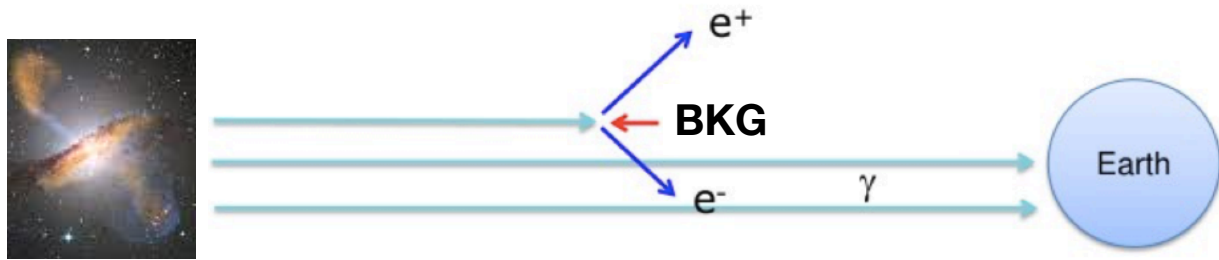
Background:

$$\epsilon_{th}^{LIV} = \frac{m_e^2}{4E_{\gamma}K(1-K)} - \frac{\delta_{\gamma,n}E_{\gamma}^{n+1}}{4}$$

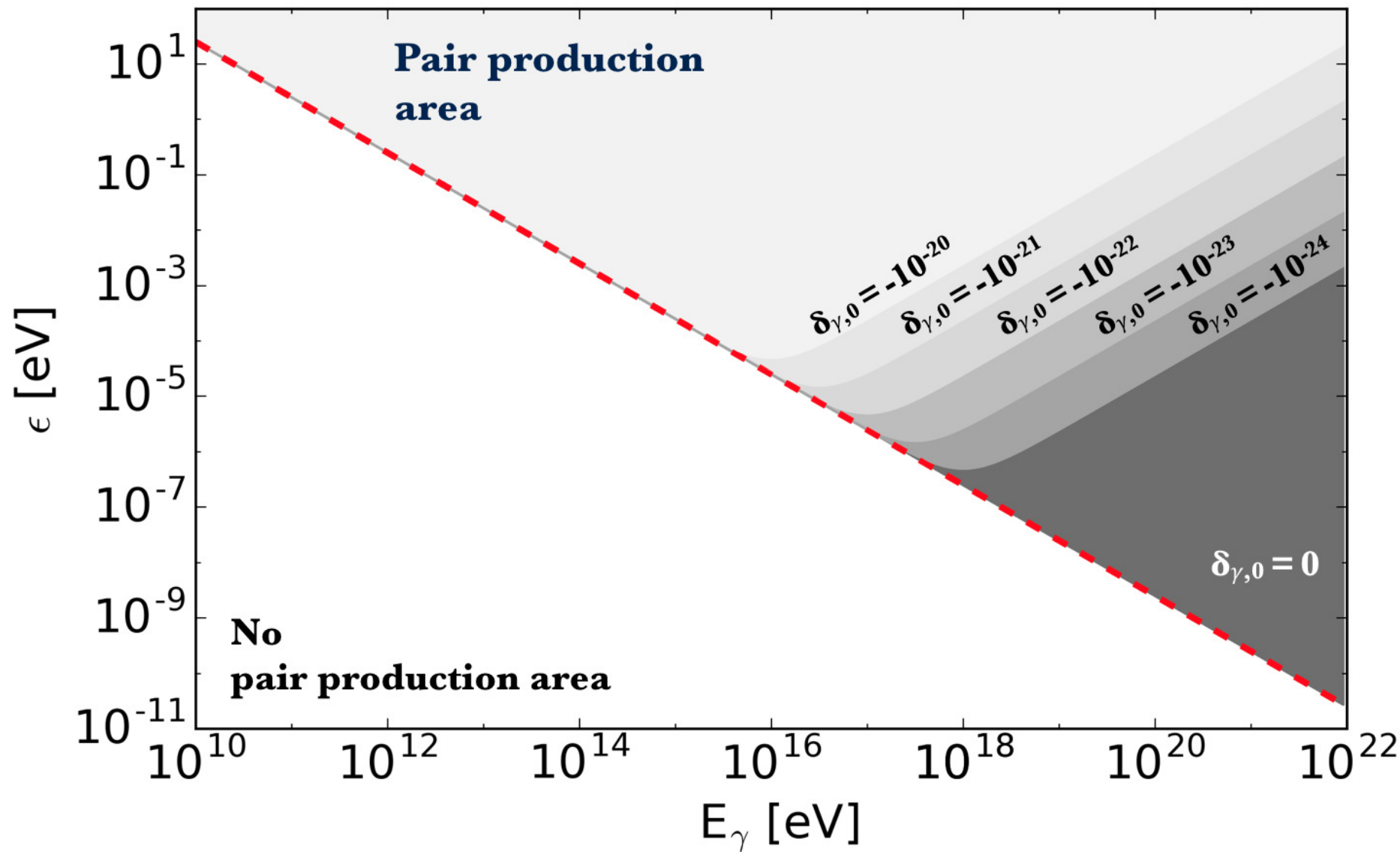


Pair Production

$$\gamma_{VHE} \gamma_{BKG} \rightarrow e^+ e^-$$



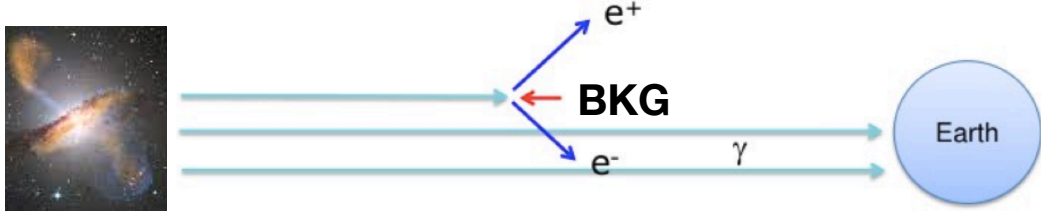
$$\epsilon_{th}^{LIV} = \frac{m_e^2}{4E_\gamma K(1-K)} - \frac{\delta_{\gamma,n} E_\gamma^{n+1}}{4}$$



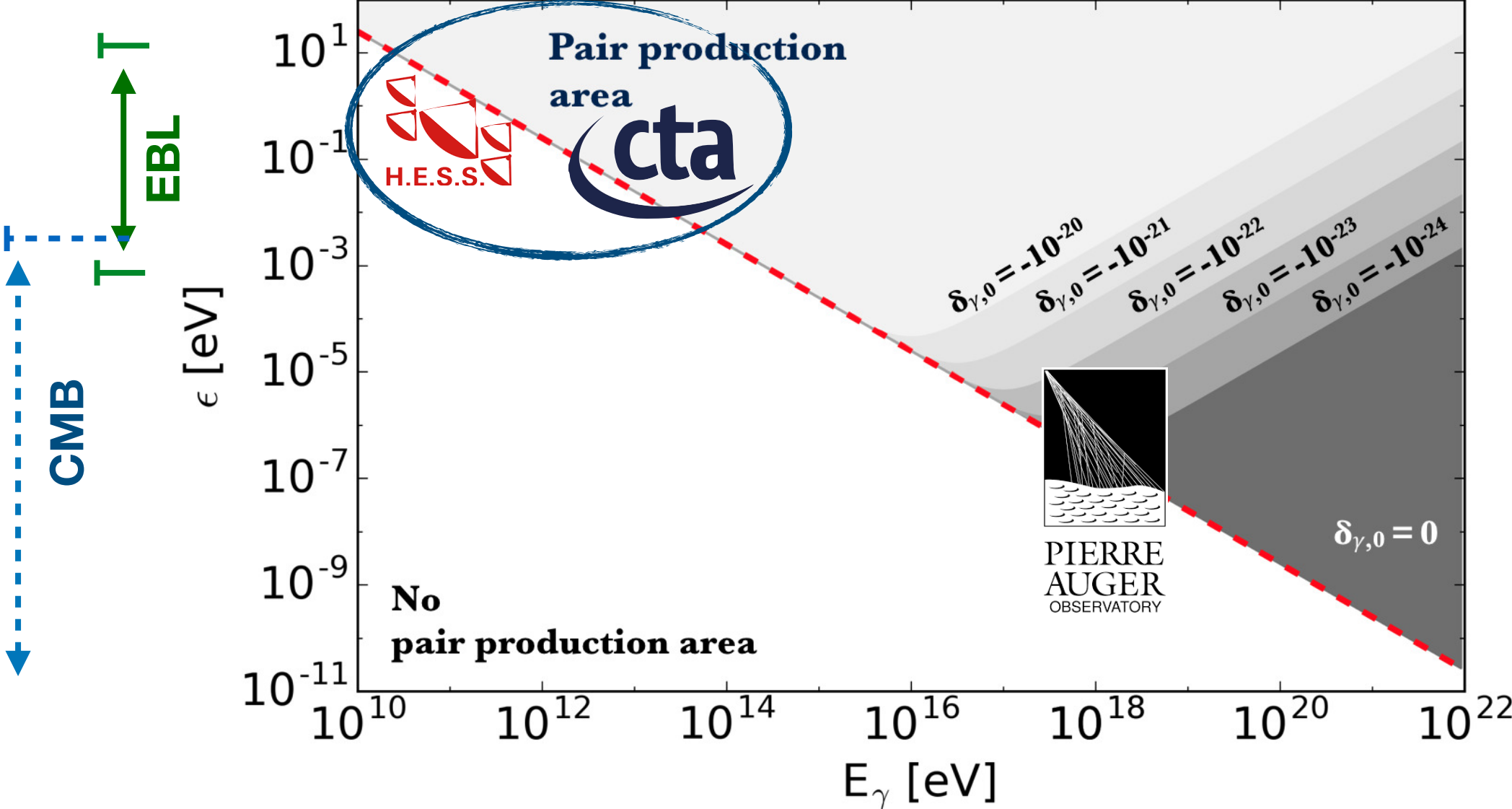
Allowed region change with the LIV parameter and the Energy

Pair Production

$$\gamma_{VHE} \gamma_{BKG} \rightarrow e^+ e^-$$

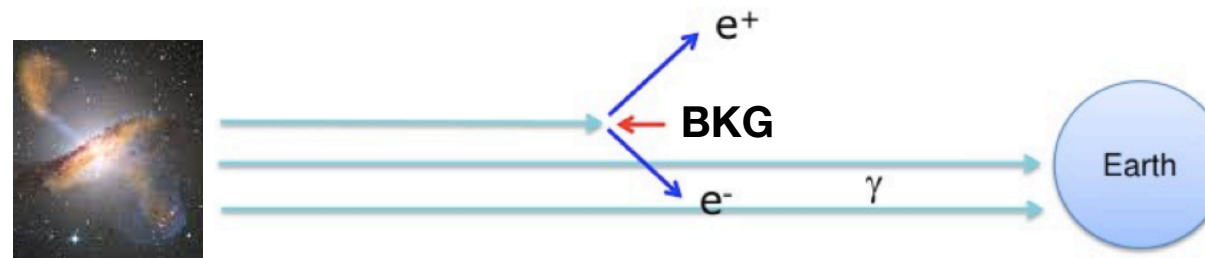


$$\epsilon_{th}^{LIV} = \frac{m_e^2}{4E_\gamma K(1-K)} - \frac{\delta_{\gamma,n} E_\gamma^{n+1}}{4}$$



... deeper LIV effects

Optical depth



$$\tau_{\gamma}(E_{\gamma}, z, n) = \int_0^z dz \frac{c}{H_0(1+z) \sqrt{\Omega_{\Lambda} + \Omega_M(1+z)^3}}$$

The distance element

$$\times \int_{\epsilon_{th}}^{\infty} d\epsilon n_{\gamma}(\epsilon, z)$$

Density of BKG photons

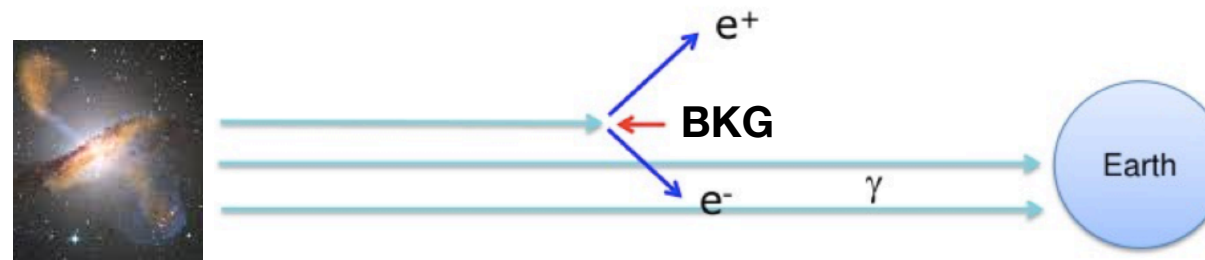
$$\times \int_{-1}^1 d(\cos \theta) \frac{1 - \cos \theta}{2} \sigma(E_{\gamma}, \epsilon, z, \cos \theta)$$

Pair Production cross section

Breit & Wheeler 1934; Heitler 1960

De Angelis, Alessandro et al.
Mon.Not.Roy.Astron.Soc.
432 (2013) 3245-3249

Optical depth + LIV



$$\tau_\gamma(E_\gamma, z, \eta, n, E_{LIV}^{(n)}) = \int_0^z dz \frac{c}{H_0(1+z) \sqrt{\Omega_\Lambda + \Omega_M(1+z)^3}}$$

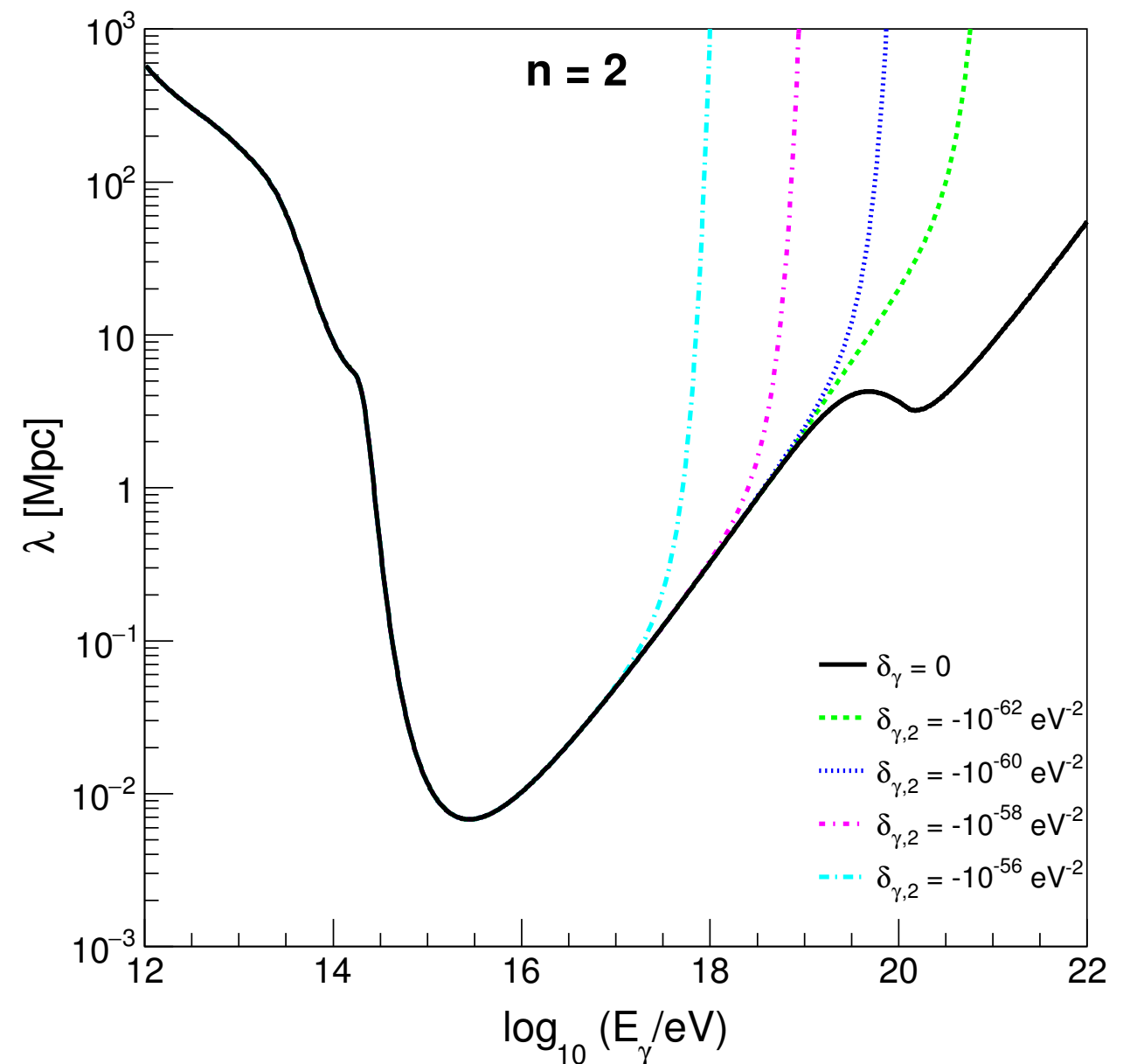
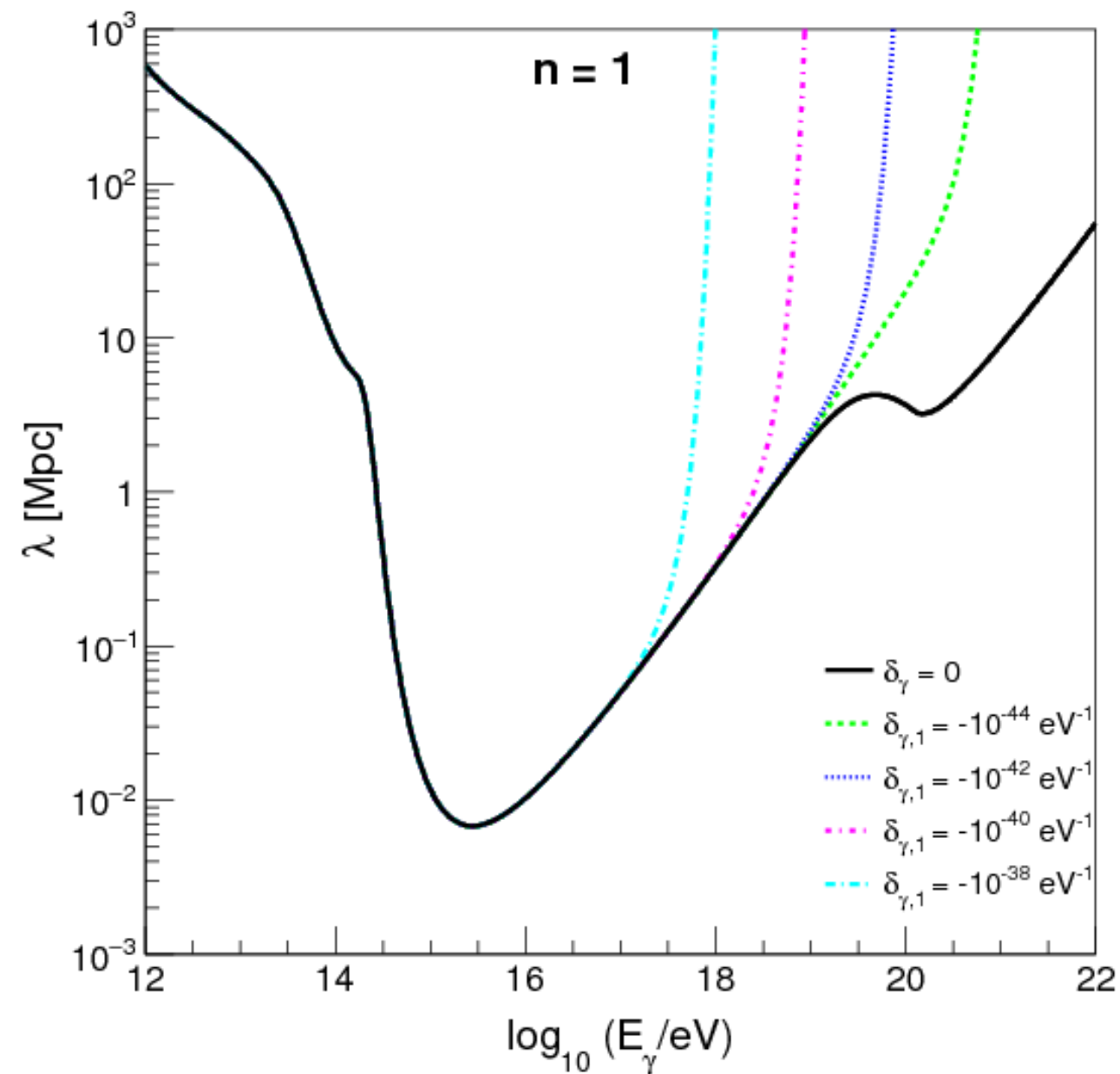
$$\times \int_{\epsilon_{th}^{LIV}}^{\infty} d\epsilon n_\gamma(\epsilon, z) \times \int_{-1}^1 d(\cos \theta) \frac{1 - \cos \theta}{2} \sigma(E_\gamma, \epsilon, z, \cos \theta)$$

↑
LIV

$$\epsilon_{th}^{LIV} = \frac{m_e^2}{4E_\gamma K(1-K)} - \frac{\delta_{\gamma,n} E_\gamma^{n+1}}{4}$$

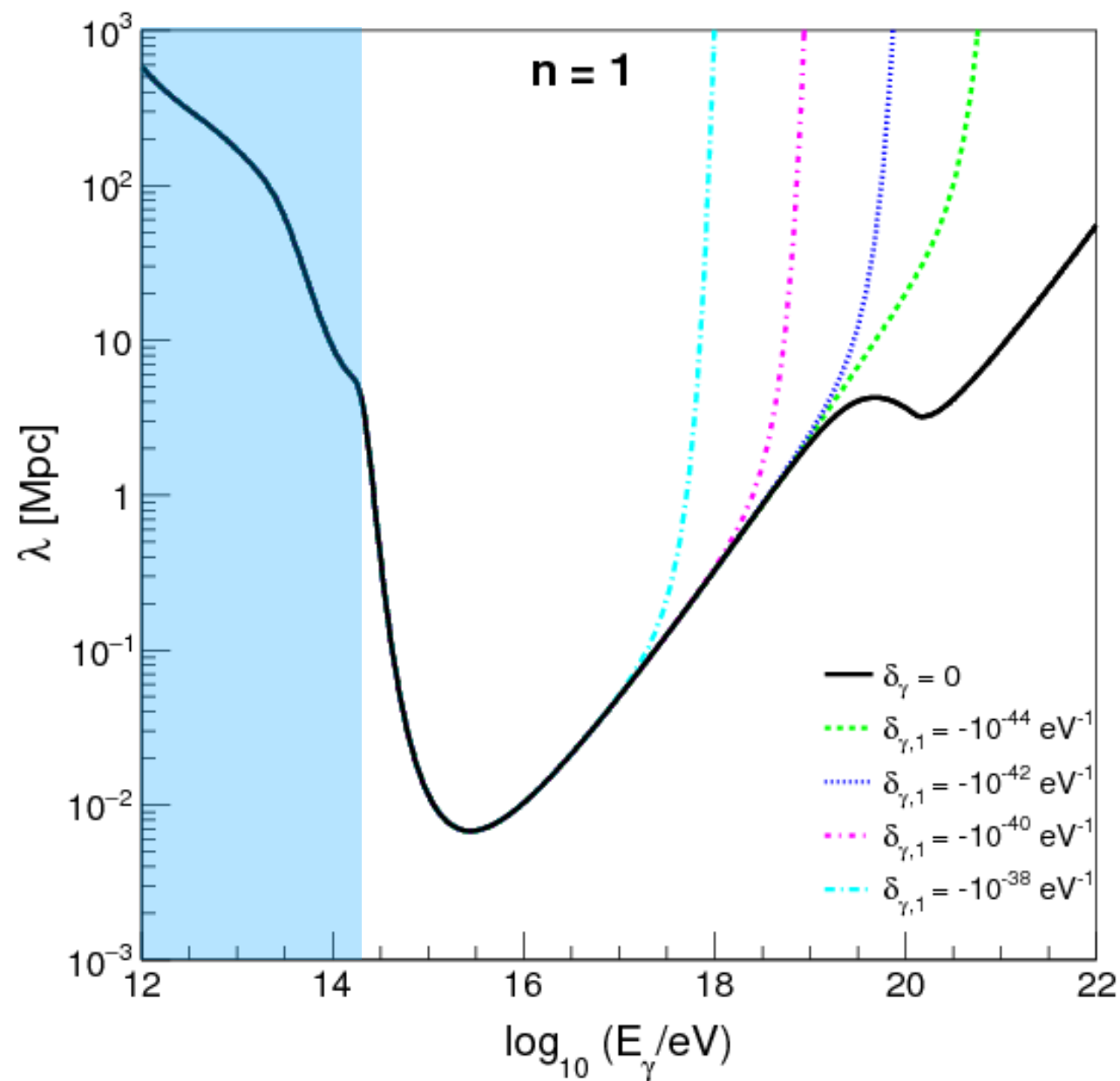
Optical depth + LIV

$$\tau_\gamma(E_\gamma, z, n, E_{LIV}^{(n)}) = \int_0^z dz \frac{c}{H_0(1+z)\sqrt{\Omega_\Lambda + \Omega_M(1+z)^3}} \int_{\epsilon_{th}^{LIV}}^\infty d\epsilon n_\gamma(\epsilon, z) \int_{-1}^1 d(\cos\theta) \frac{1 - \cos\theta}{2} \sigma(E_\gamma, \epsilon, z, \cos\theta)$$

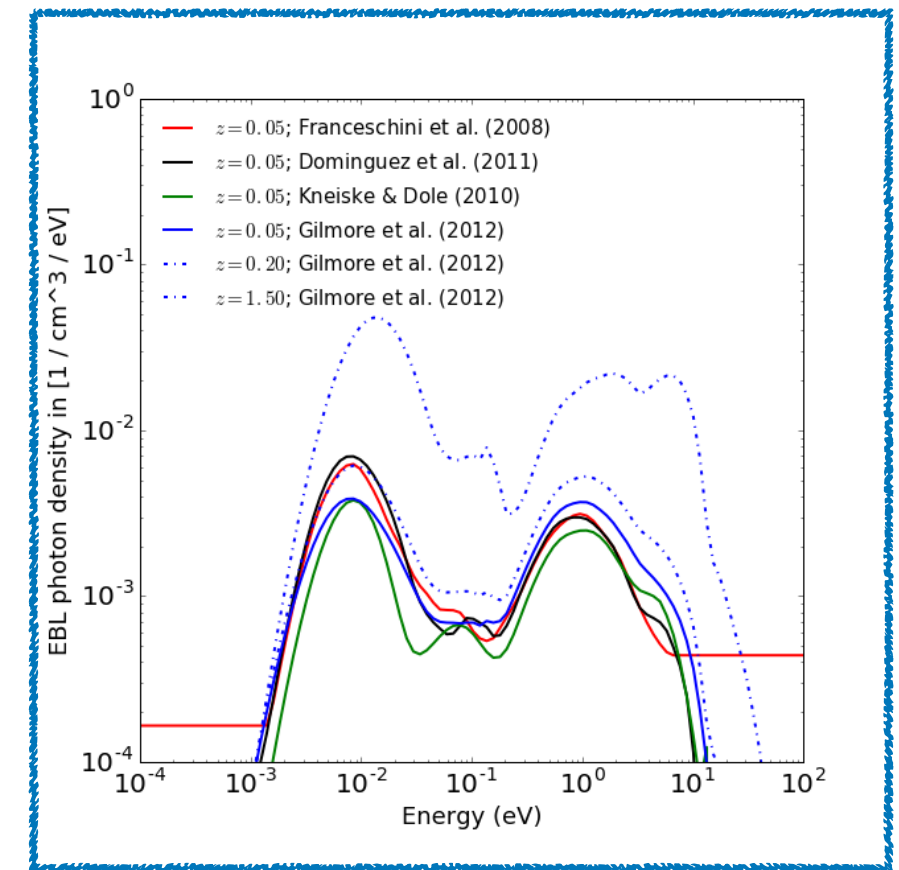


Optical depth + LIV

$$\tau_\gamma(E_\gamma, z, n, E_{LIV}^{(n)}) = \int_0^z dz \frac{c}{H_0(1+z)\sqrt{\Omega_\Lambda + \Omega_M(1+z)^3}} \int_{\epsilon_{th}^{LIV}}^\infty d\epsilon n_\gamma(\epsilon, z) \int_{-1}^1 d(\cos\theta) \frac{1 - \cos\theta}{2} \sigma(E_\gamma, \epsilon, z, \cos\theta)$$



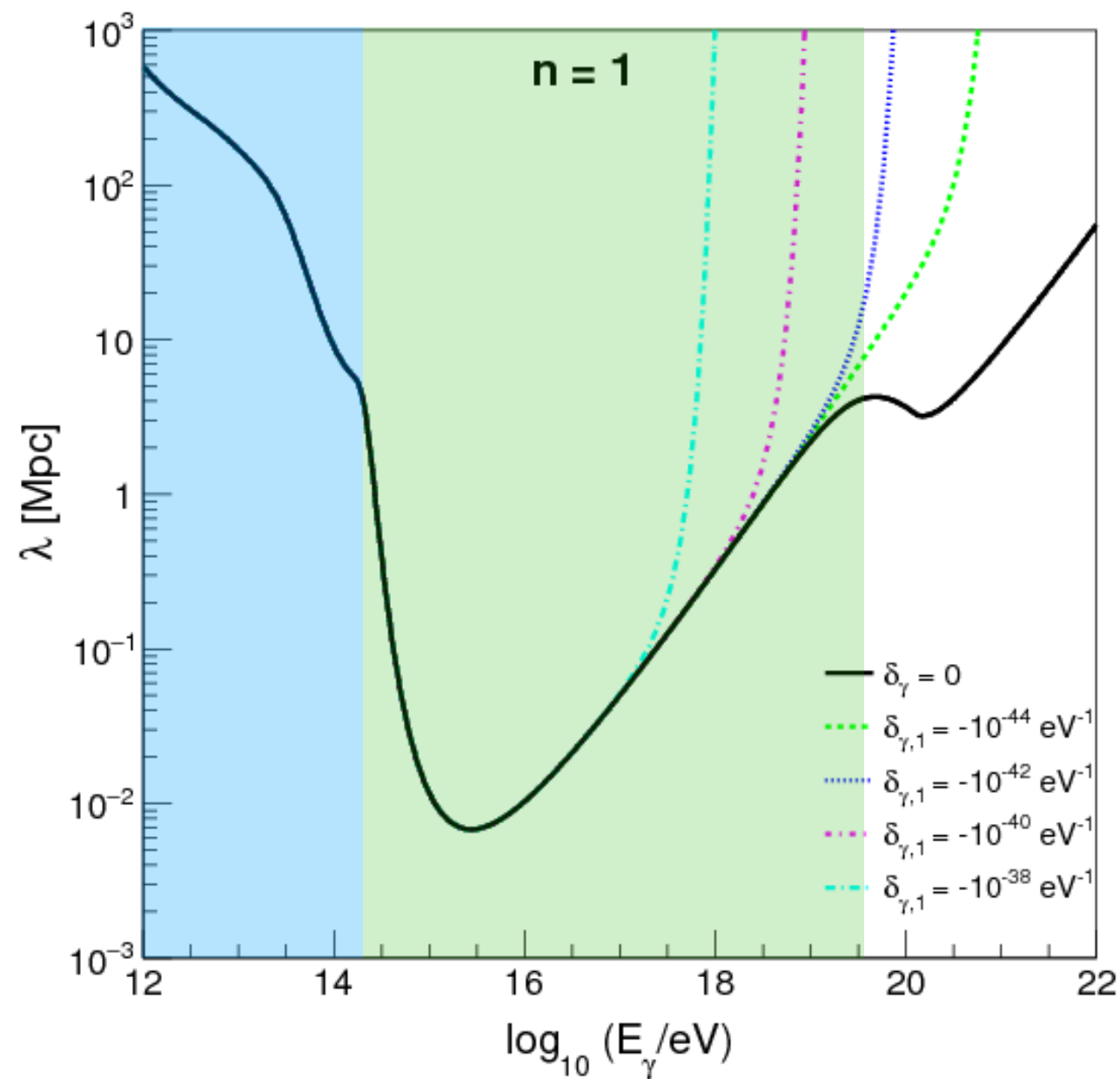
BKG density
EBL-photons



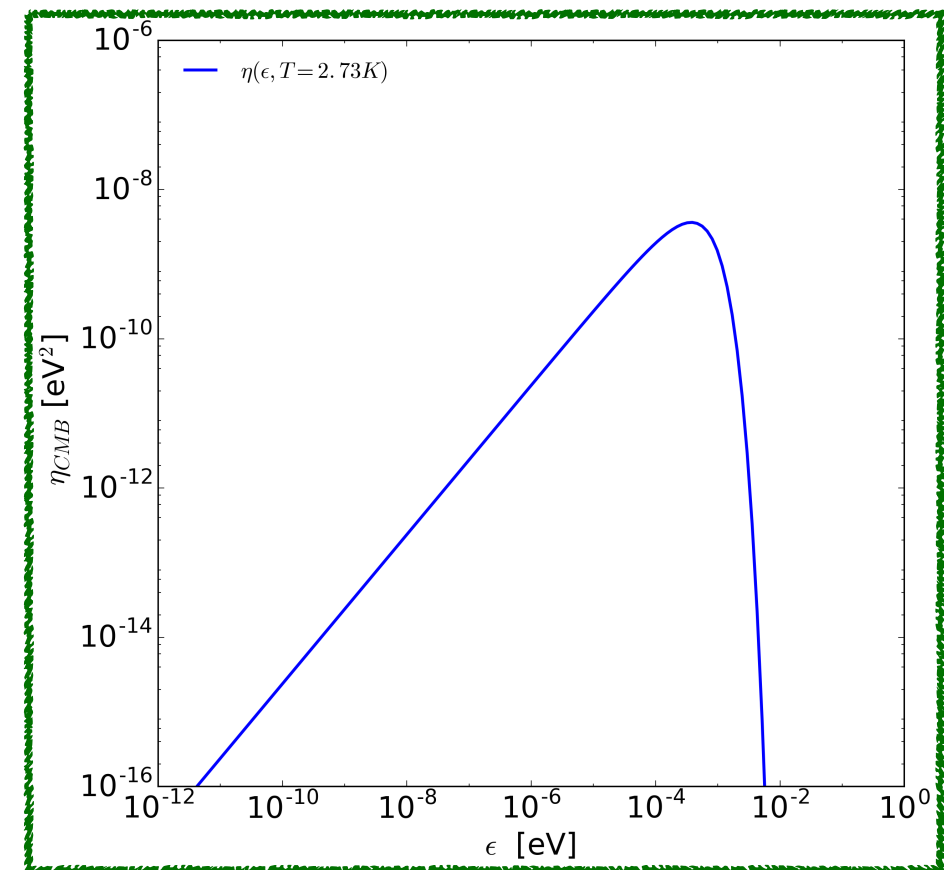
EBL: Gilmore & Ramirez-Ruiz (2010)

Optical depth + LIV

$$\tau_\gamma(E_\gamma, z, n, E_{LIV}^{(n)}) = \int_0^z dz \frac{c}{H_0(1+z)\sqrt{\Omega_\Lambda + \Omega_M(1+z)^3}} \int_{\epsilon_{th}^{LIV}}^\infty d\epsilon n_\gamma(\epsilon, z) \int_{-1}^1 d(\cos\theta) \frac{1 - \cos\theta}{2} \sigma(E_\gamma, \epsilon, z, \cos\theta)$$

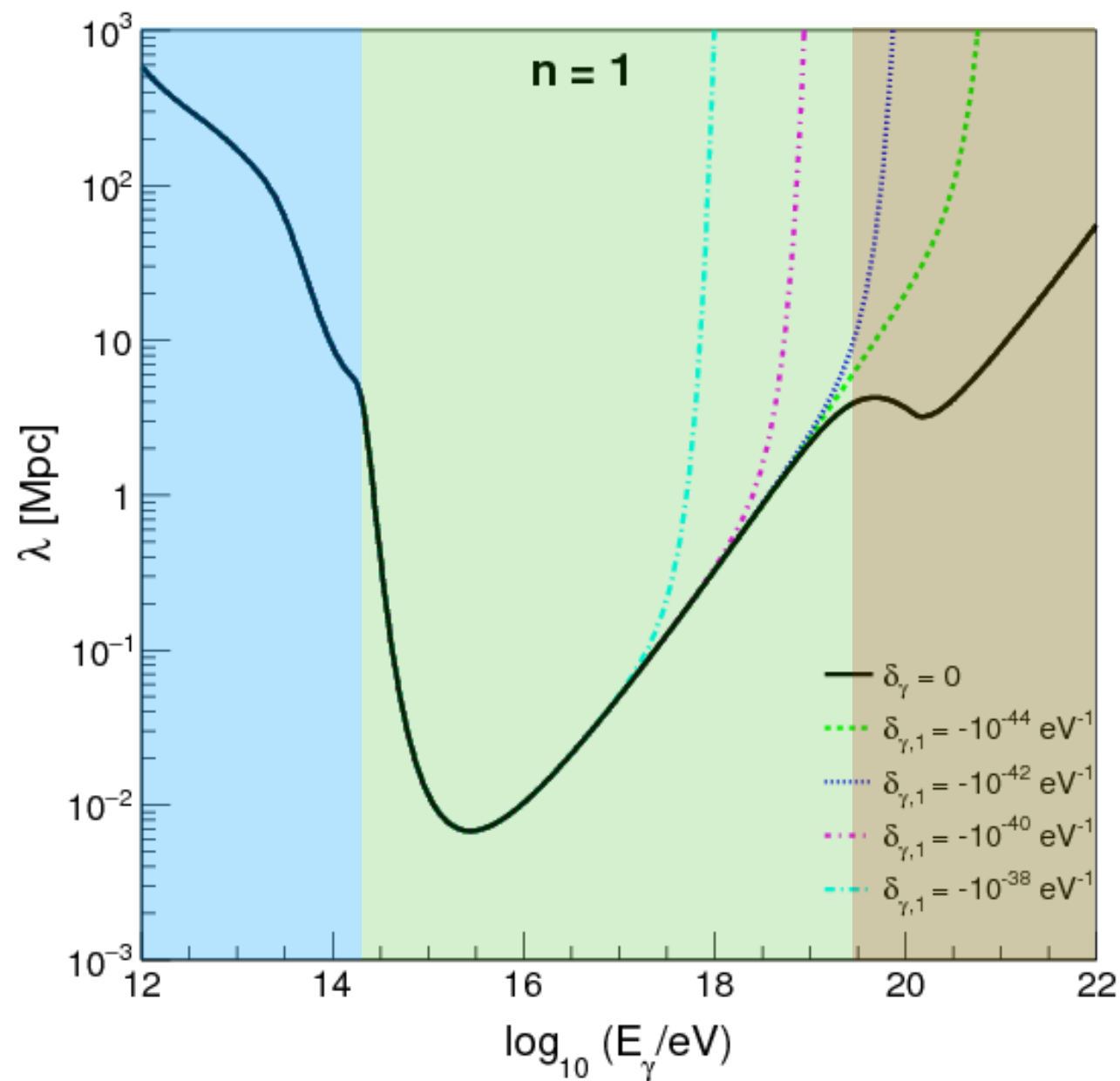


BKG density
CMB-photons



Optical depth + LIV

$$\tau_\gamma(E_\gamma, z, n, E_{LIV}^{(n)}) = \int_0^z dz \frac{c}{H_0(1+z)\sqrt{\Omega_\Lambda + \Omega_M(1+z)^3}} \int_{\epsilon_{th}^{LIV}}^\infty d\epsilon n_\gamma(\epsilon, z) \int_{-1}^1 d(\cos\theta) \frac{1 - \cos\theta}{2} \sigma(E_\gamma, \epsilon, z, \cos\theta)$$



BKG density
Radio-photons

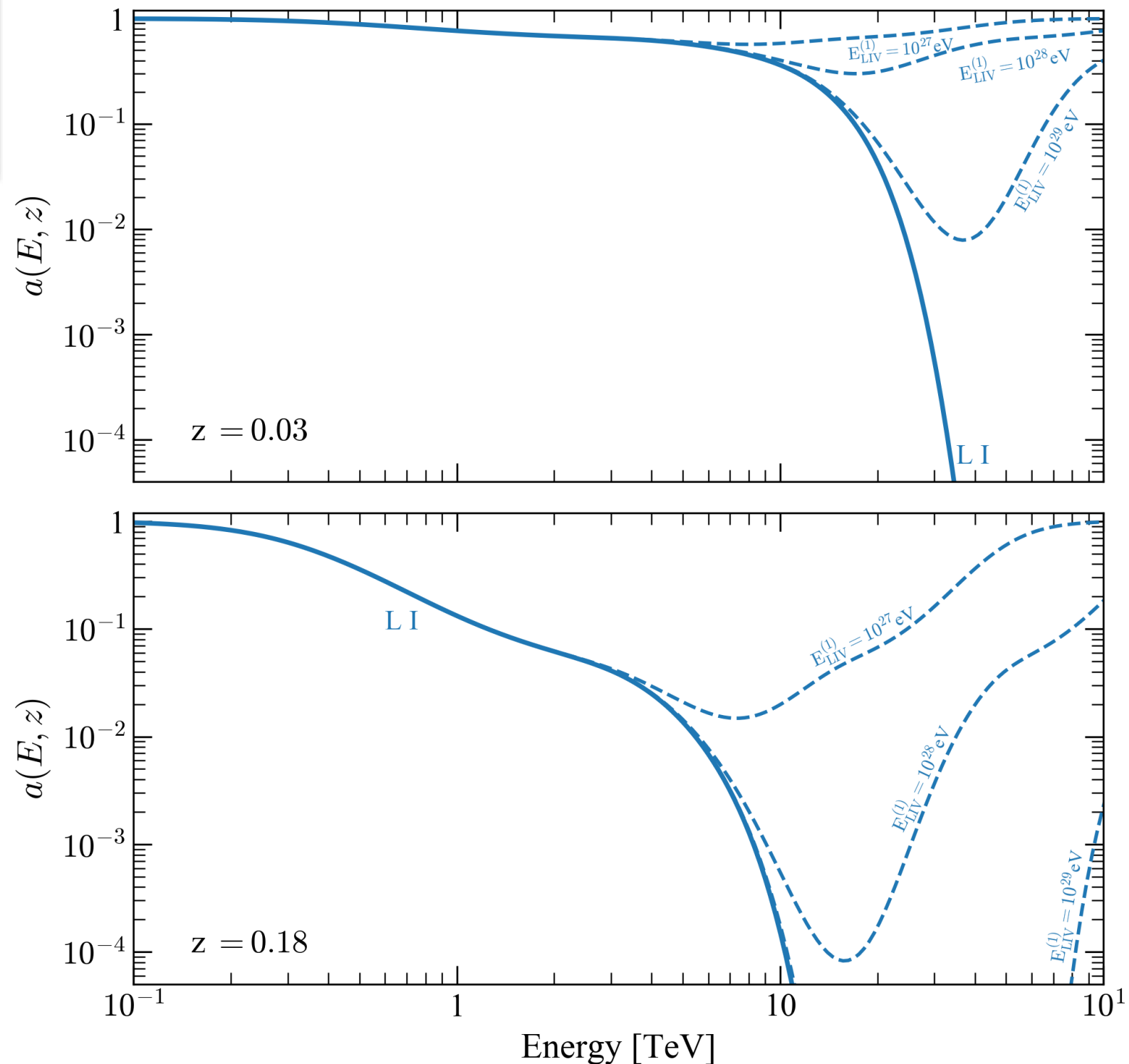
Data from Gervasi et al.
(2008)

EBL-Attenuation + LIV

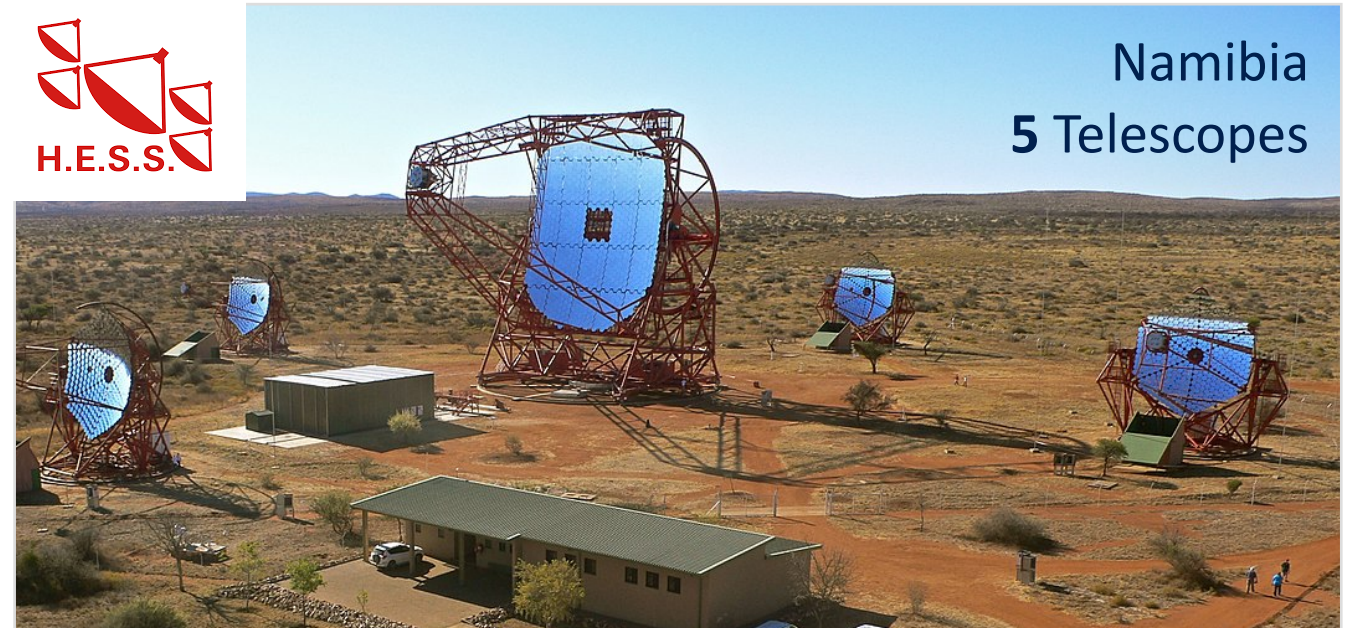
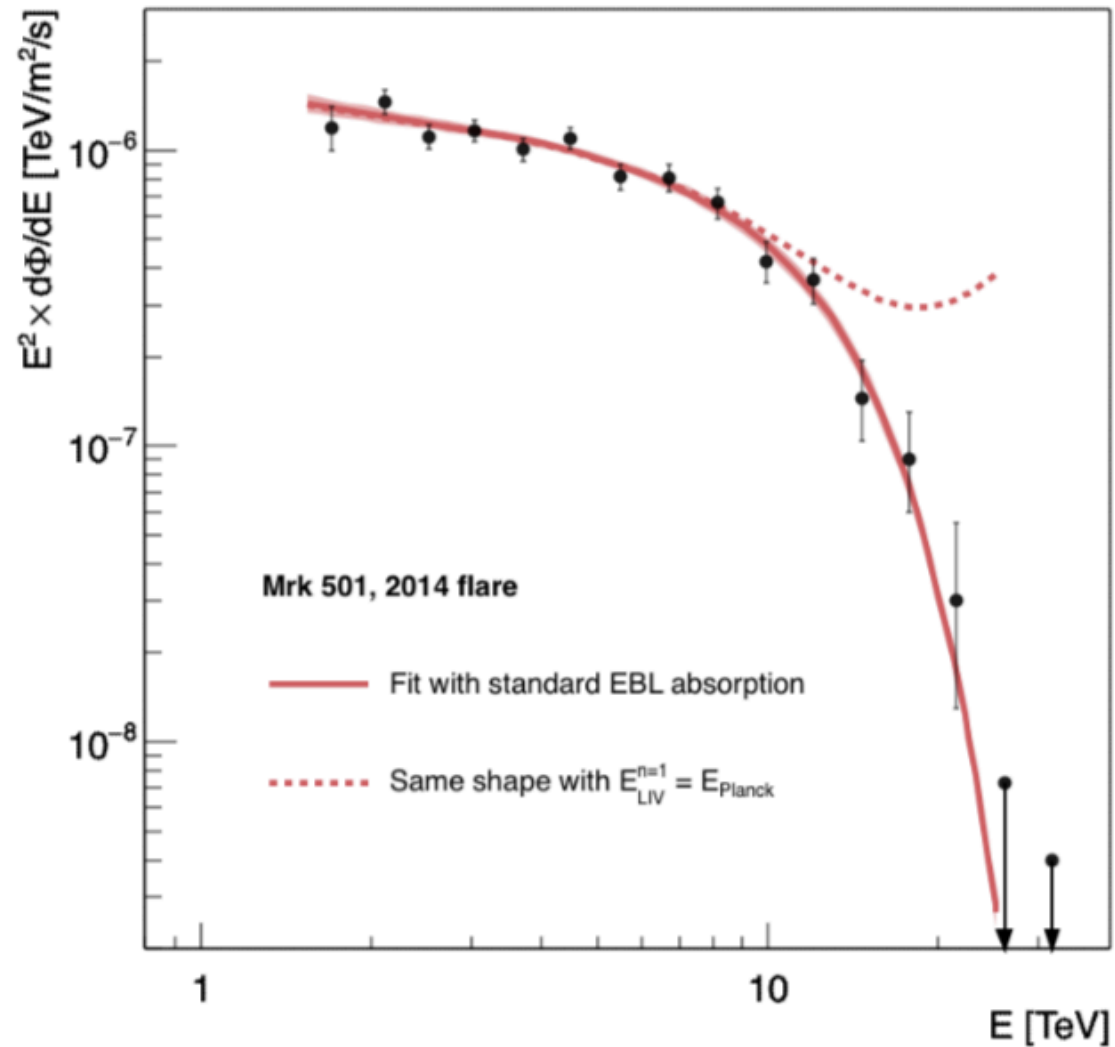
$$a(E, z) = e^{-\tau(E, z)}$$

The intensity of the LIV effect depends on

- ▶ E_γ :
The energy of the γ -ray
- ▶ E_{LIV} :
The LIV energy scale
- ▶ z :
The distance of the source.



EBL-Attenuation + LIV



	2σ	3σ	5σ
n=1	2.8×10^{28} eV ($2.29 \times E_{Planck}$)	1.9×10^{28} eV ($1.6 \times E_{Planck}$)	1.04×10^{28} eV ($0.86 \times E_{Planck}$)
n=2	7.5×10^{20} eV	6.4×10^{20} eV	4.7×10^{20} eV

Lorentz and Brun for the HESS collaboration, RICAP16, 2016.

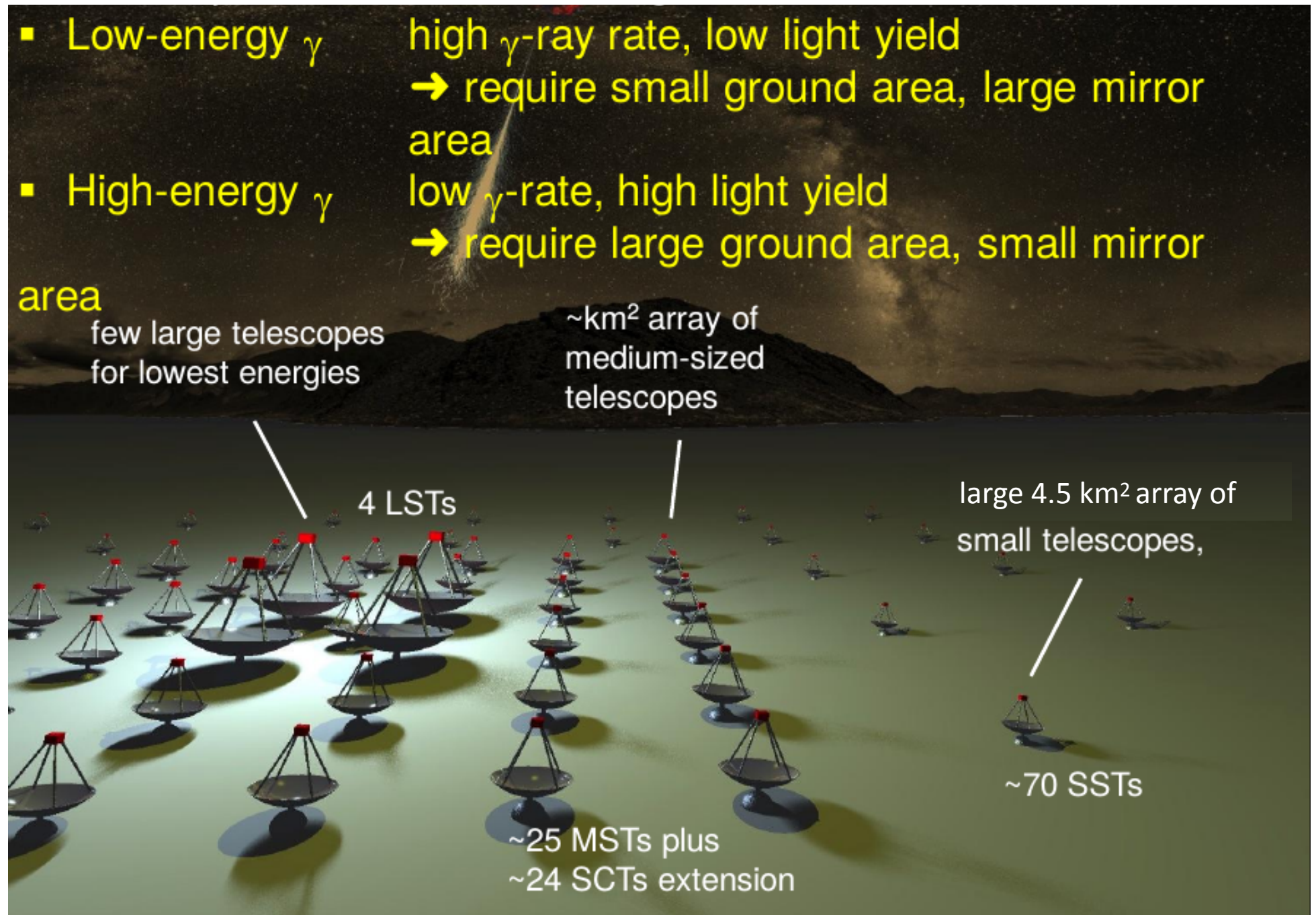
Cherenkov Telescope Array

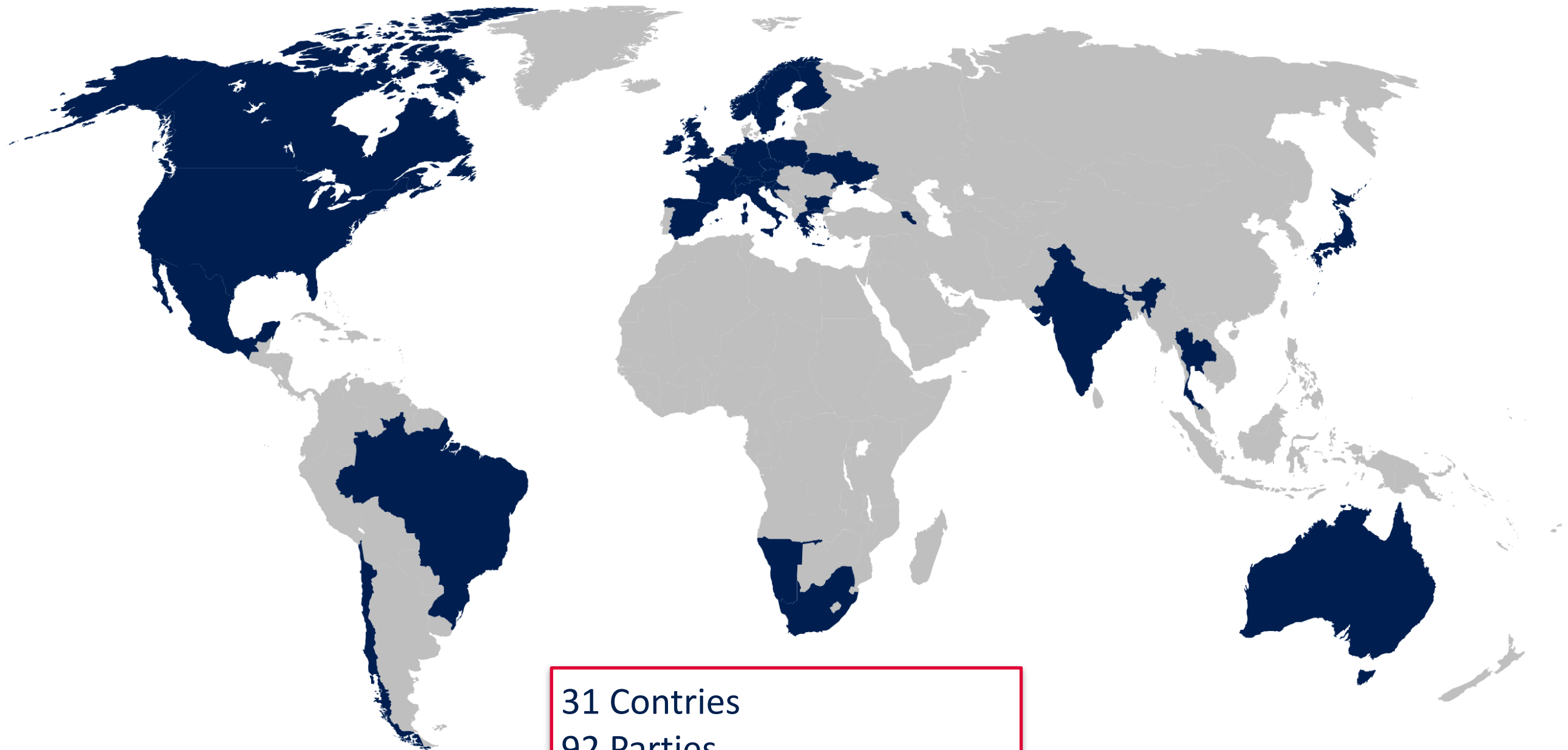


99 Telescopes

- 4 LST
- 25 MST
- 70 SSTs

Energy range
20 GeV - 300 TeV





31 Countries
92 Parties
202 Institutes
1466 members (513 FTE)

UNAM



- 7 Scientist
 - Ruben Alfaro
 - Alejandro Lara
 - William Lee
 - Maria Magdalena
 - Lukas Nellen
 - Andrés Sandoval
 - Gagik Tovmassian
- 2 Engineers
 - Fernando Garfias
 - Arturo Iriarte



CTA Brazil

12 Institutions

25 Scientists

16 Students

5 Technicians

CTA - SP - MST

- **IFSC- USP**
 - Prof. Vitor de Souza
 - Profa. Manuela Vecchi
 - Profa. Cibelle Celestino
 - Dr. Humberto Huerta
 - Dr. Aion Viana
 - Edyvania Martins
 - Rodrigo Lang
 - Luan Arbeletche
 - Andres Delgado
 - Rodrigo Guedes Lang
 - Danielle Kaori
- **IF-USP**
 - Prof. Edivaldo Moura
 - Douglas Pimentel
- **UFABC**
 - Prof. Marcelo Leigui
 - Raquel de Almeida
- **UFSCar**
 - Dr. Gustavo Rojas
- **UFPR**
 - Prof. Rita de Cássia
- **EEL / USP**
 - Prof. Fernando Catalani
 - Prof. Carlos Todero
- **SAIFR / IFT - UNESP**
 - Dr. Fabio Iocco
 - Dr Ekaterina Karukes
 - Maria Benito

CTA - SP - SST

- **IAG – USP**
 - Profa. Elisabete dal Pino
 - Prof. Rodrigo Nemmen
 - Dr. Rafael Batistai
 - Dr. Chandra Singh
 - Dr. Grzegorz Kowal
 - Dr. Reinaldo Lima
 - Dr. Paramita Barai
 - Dr. Luis Kadowki
 - Dr. Claudio Melioli
 - Dr. Juan Ramirez
 - Tania Torrejon
 - Renato Gimenes
 - Pankaj Kushwaha
 - Saib Hussain
 - Carlos Fermino
 - Raniere Menezes
 - William Bohórquez
 - Lucas Santos
- **UNICSul**
 - Prof. Anderson Caproni
- **EACH / USP**
 - Prof. Diego Falceta-Gonçalves
 - Mohammad Ali

CTA - Rio

- **CBPF**
 - Prof. Ulisses de Almeida
 - Prof. Ronald Shellard
 - Bruno Arsioli
 - Bernardo Fraga
 - Rodrigo Cardoso
 - Amanda Carvalho



The Array Locations



Array Coordinates

Latitude: 24° 41' 0.34" South
Longitude: 70° 18' 58.84" West



CTA South
Chile, Paranal

~5 km²

area covered by the array of telescopes



CTA North
Spain, La Palma

~0.5 km²

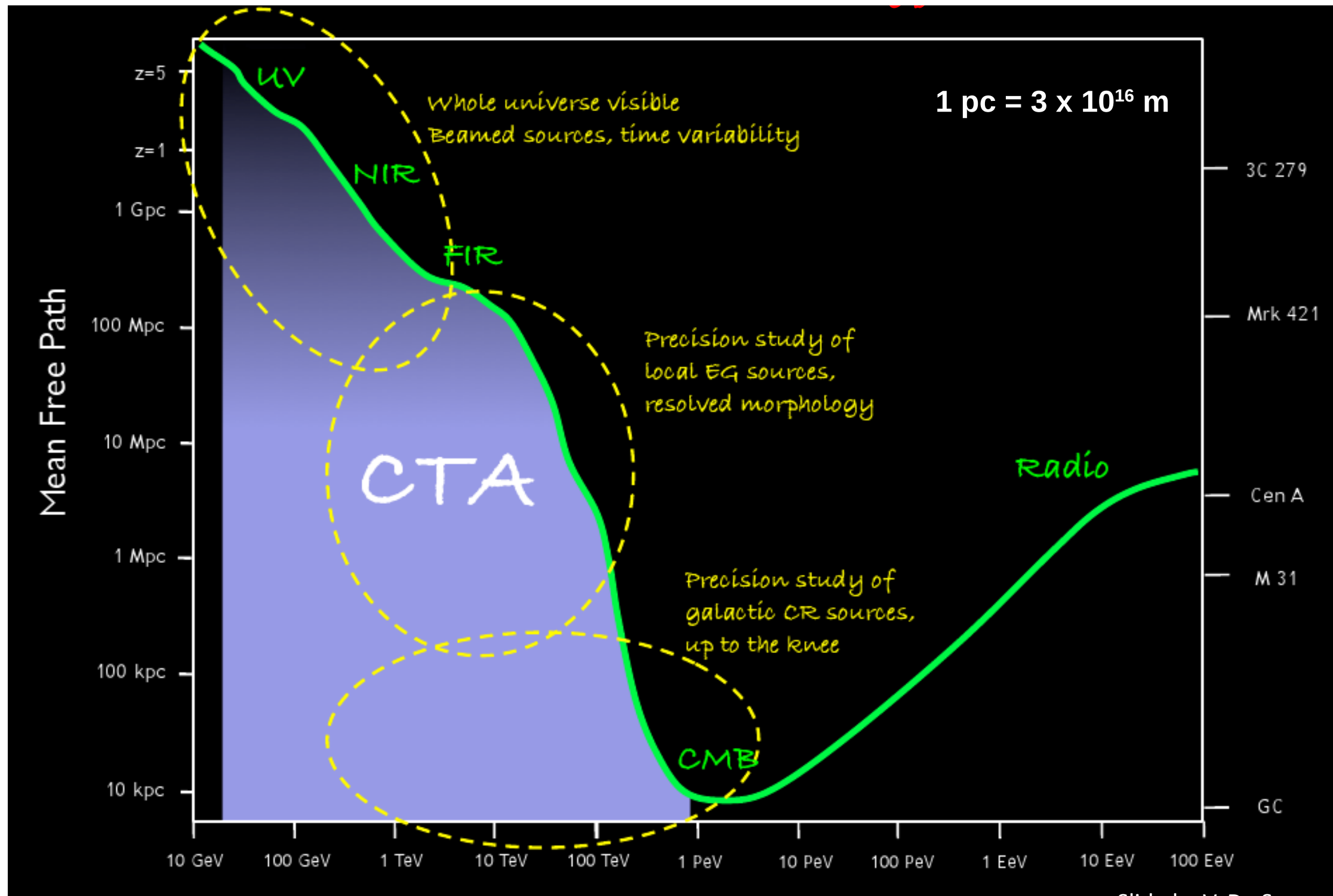
area covered by the array of telescopes



Array Coordinates

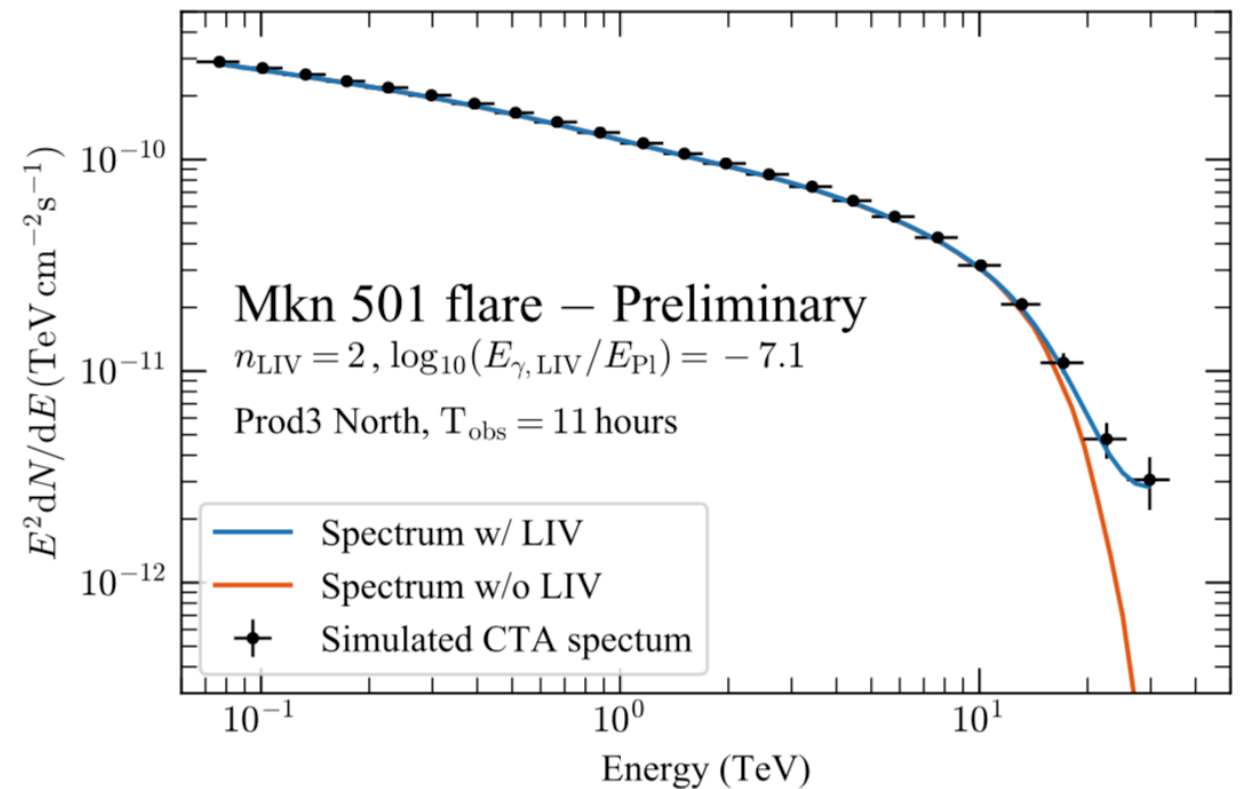
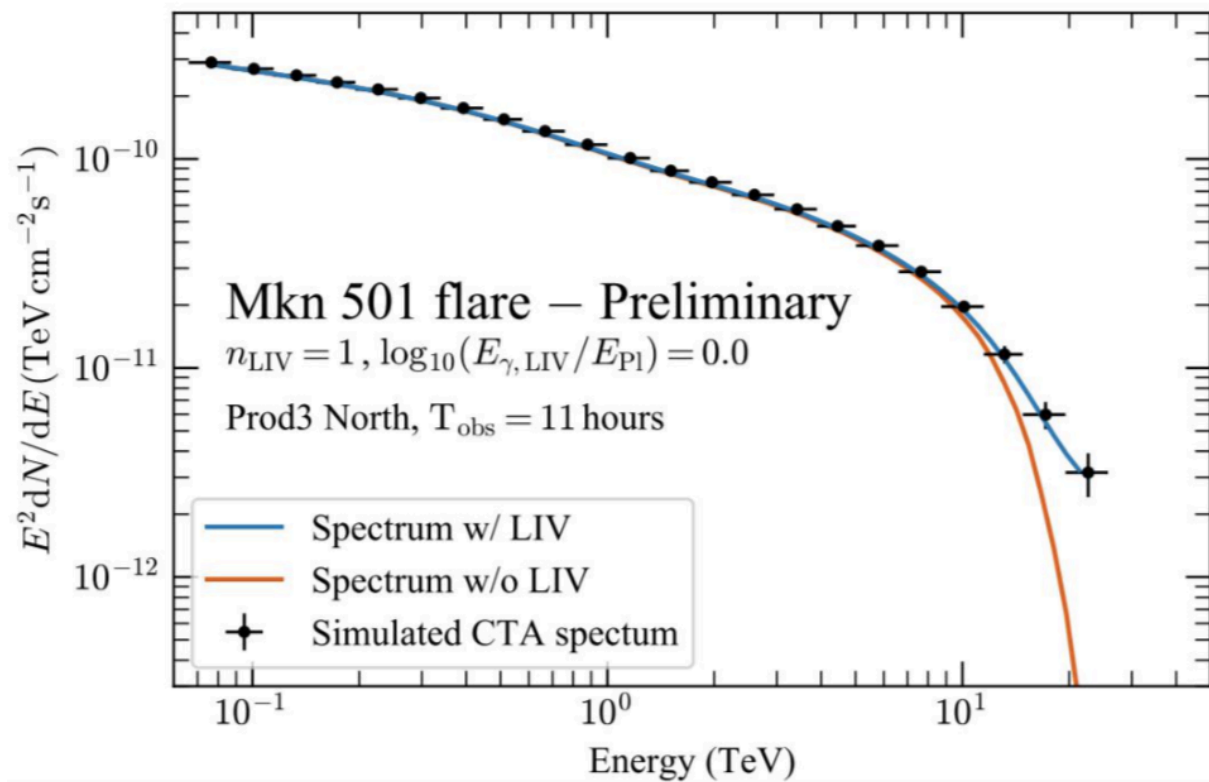
Longitude: 17° 53' 31.218" West
Latitude: 28° 45' 43.7904" North

The γ -ray horizon



Slide by V. De Souza

EBL-Attenuation + LIV



LIV TeV Horizon

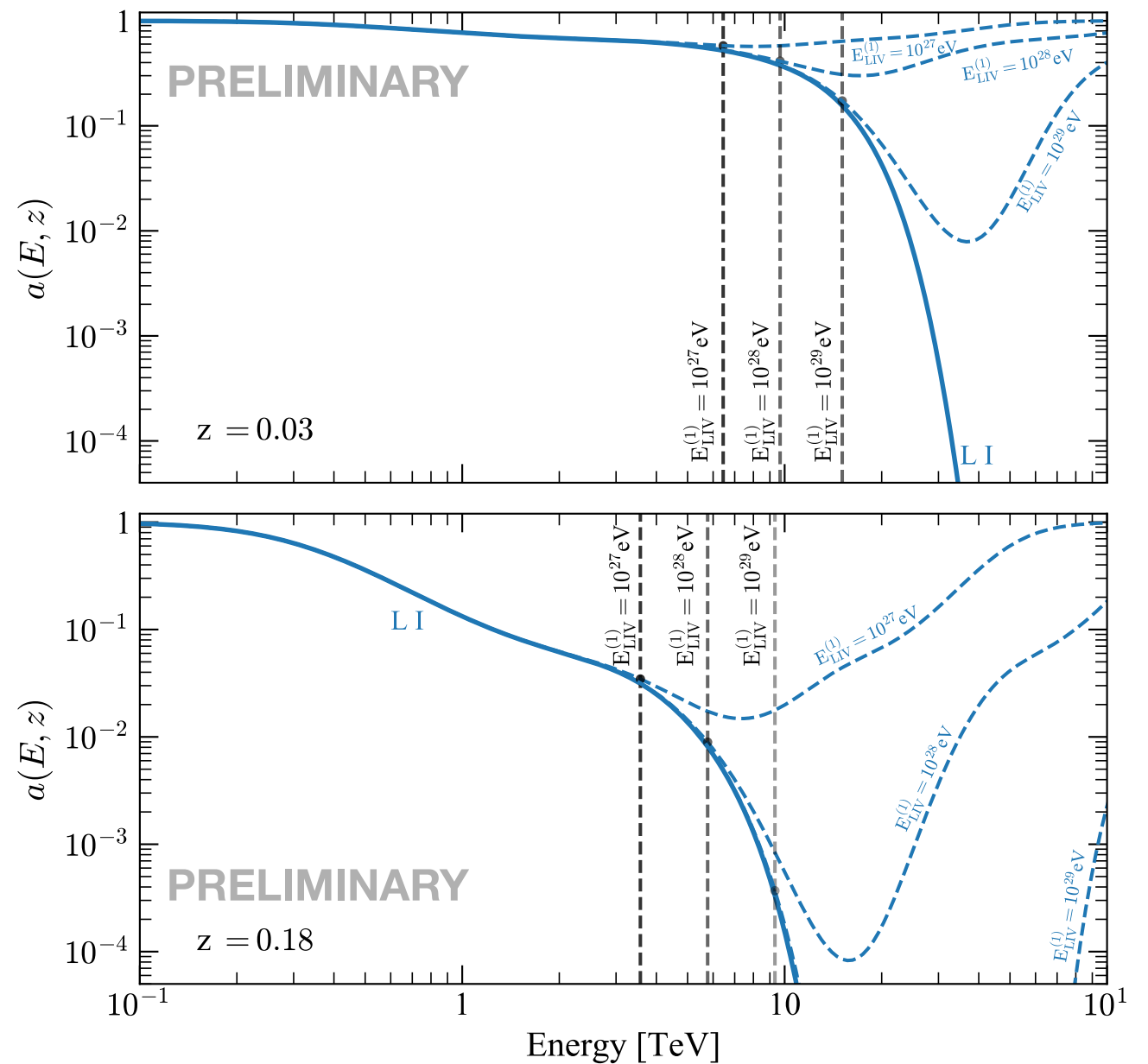
...Why use only one source?

**There are ~111
measured energy
spectra in the
TeVCat !**

LIV TeV Horizon

...Why use only one source?

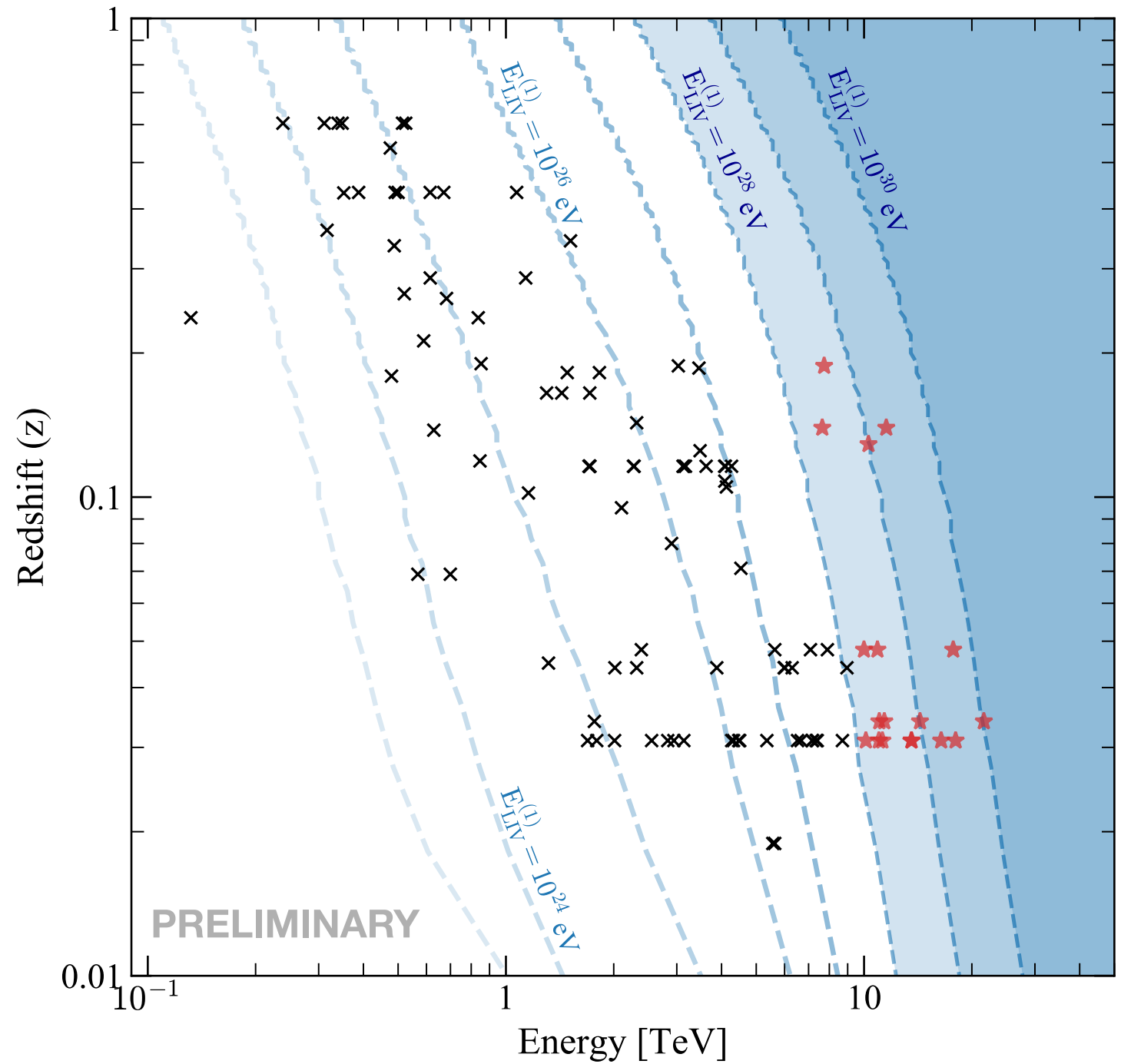
There are ~111
measured energy
spectra in the
TeVCat !



LIV TeV Horizon

...Why use only one source?

There are ~111
measured energy
spectra in the
TeVCat !



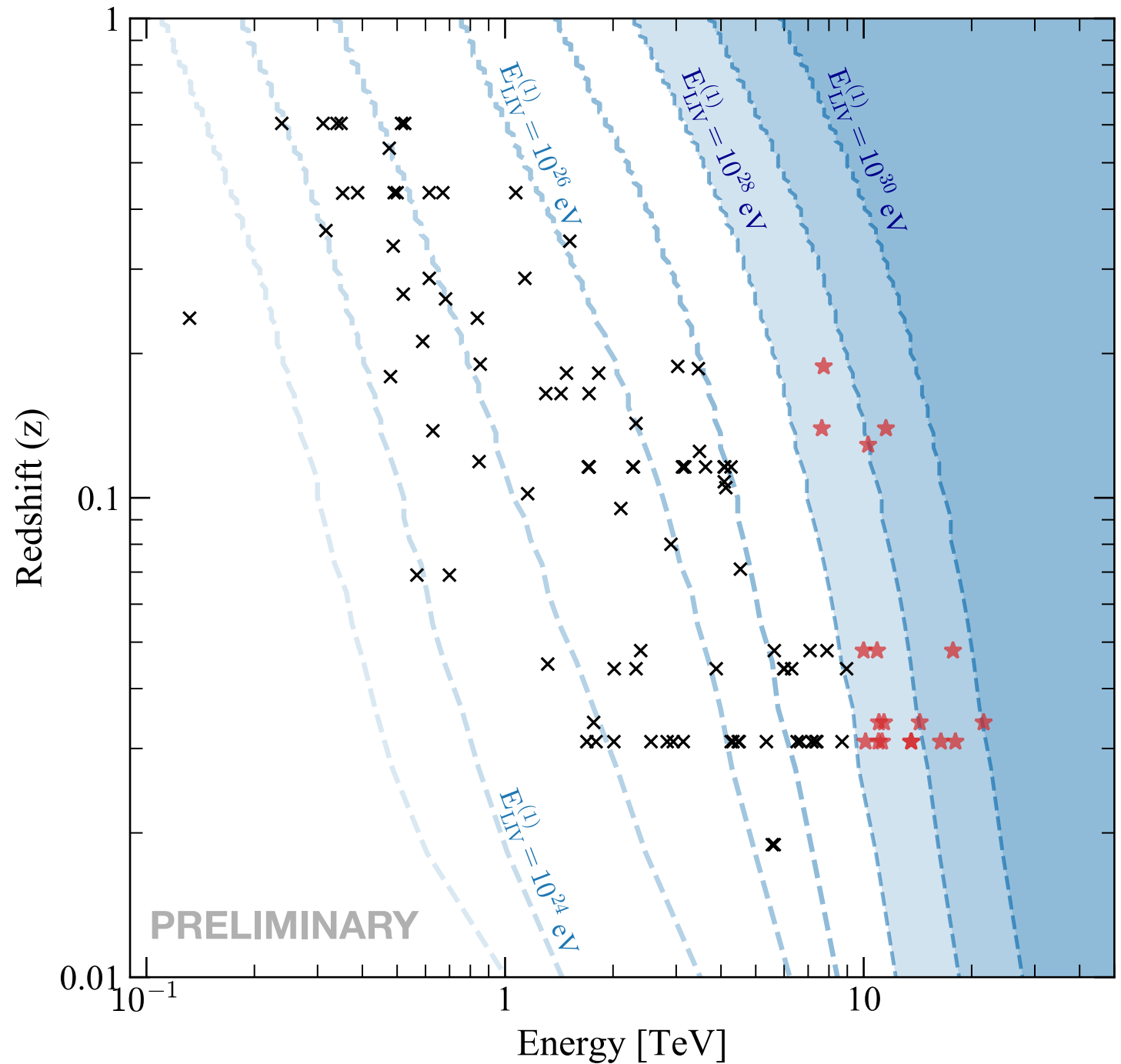
LIV TeV Horizon

...Why use only one source?

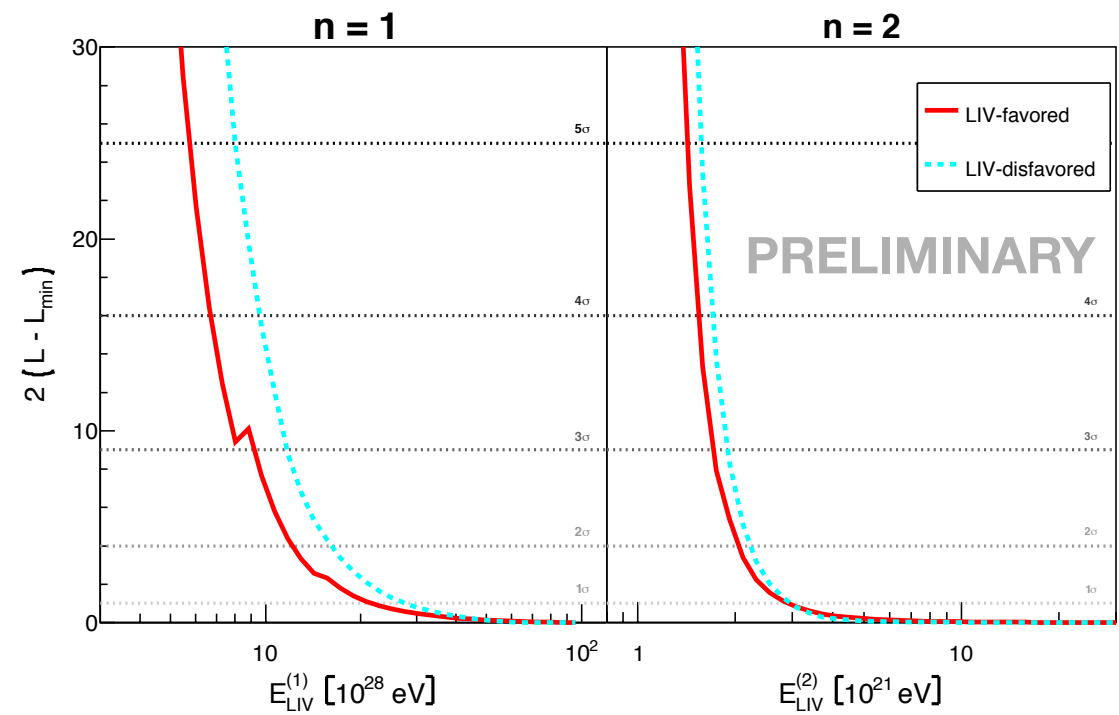
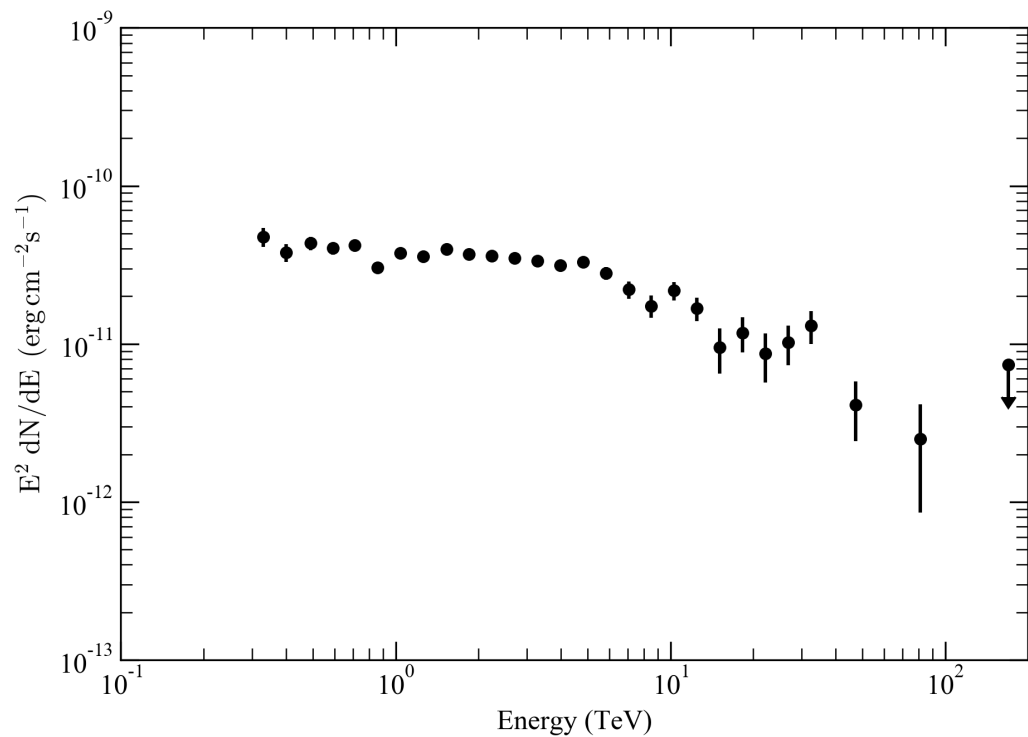
There are ~111
measured energy
spectra in the
TeVCat !



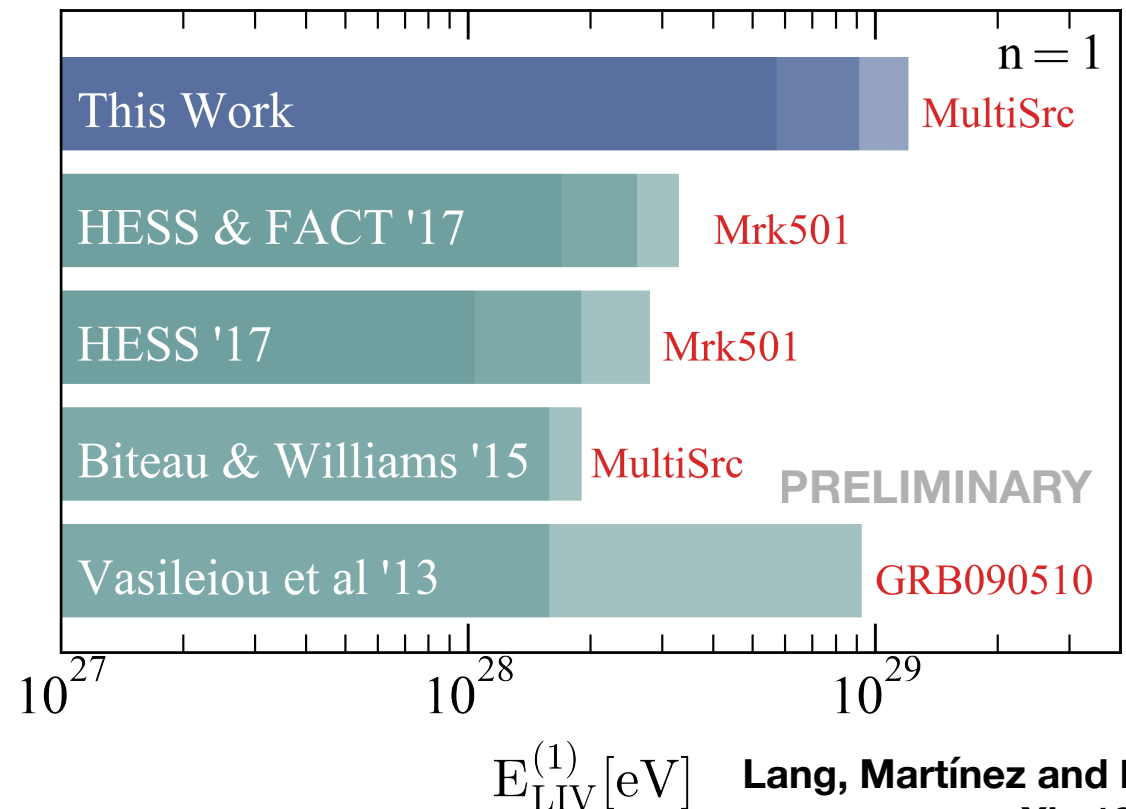
only 18 spectra from 6
sources
have the potential to
show LIV effects
(constrain LIV)



New best LIV limits!

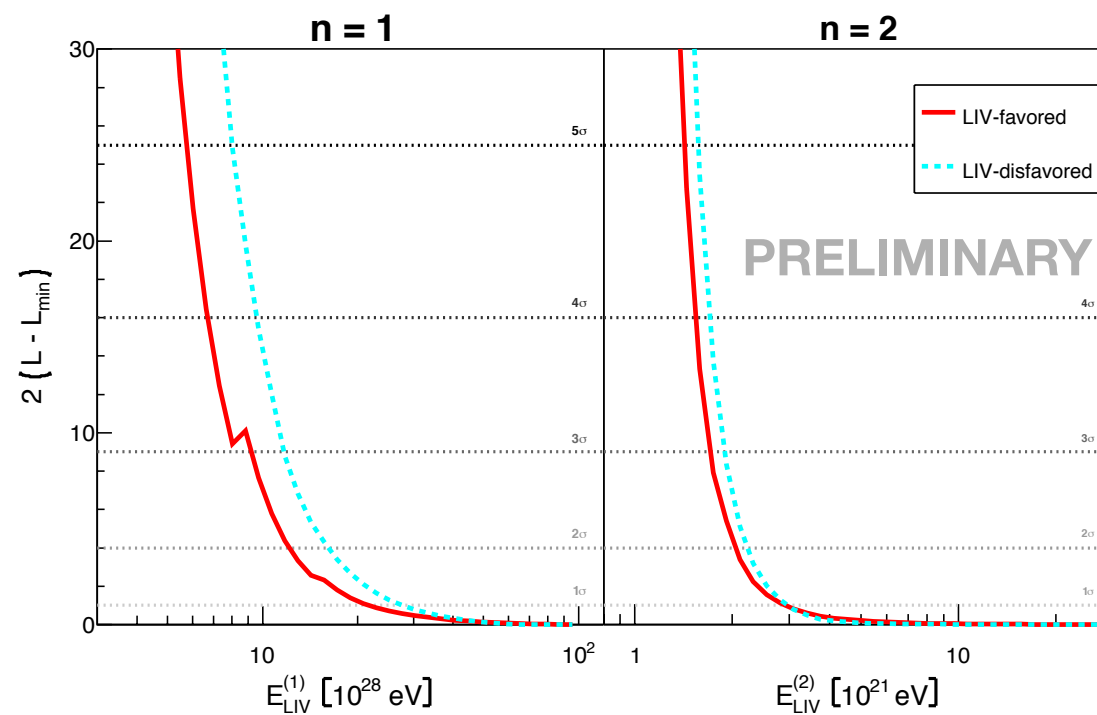
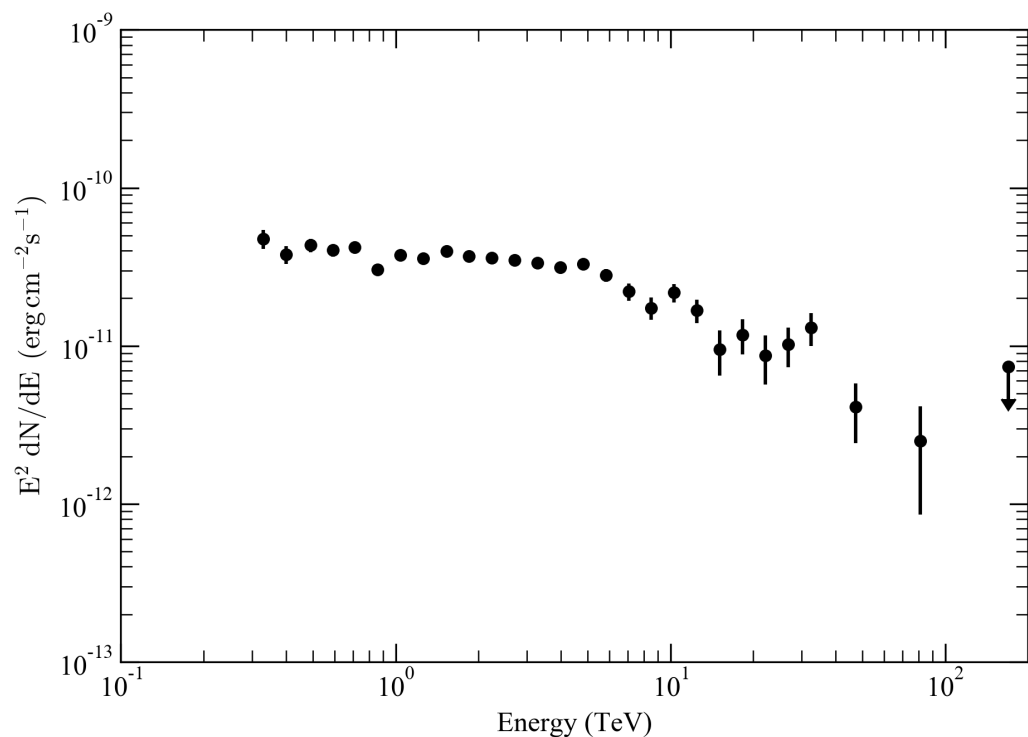


- ▶ Choices of the EBL models
- ▶ Model of the intrinsic spectrum
- ▶ Energy resolution
- ▶ Selection of spectra Selection of energy bins to be used in the calculation of the intrinsic energy spectra

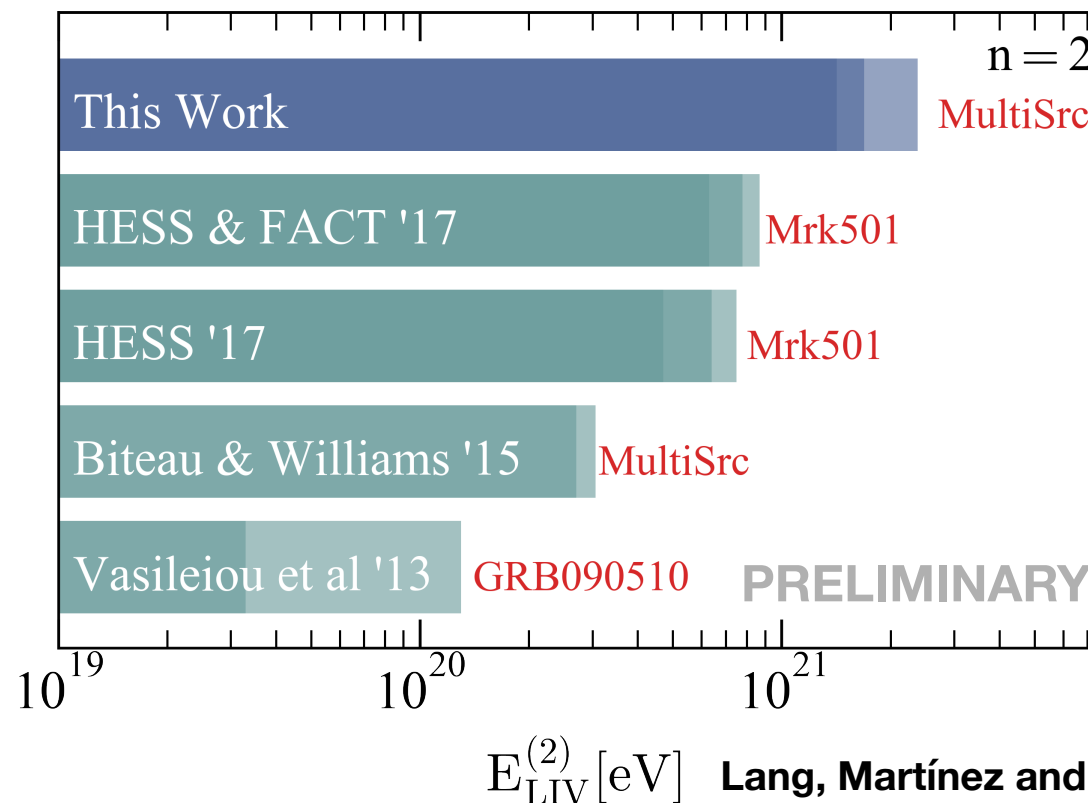


Lang, Martínez and De Souza
arXiv:1810.13215
Submitted

New best LIV limits!

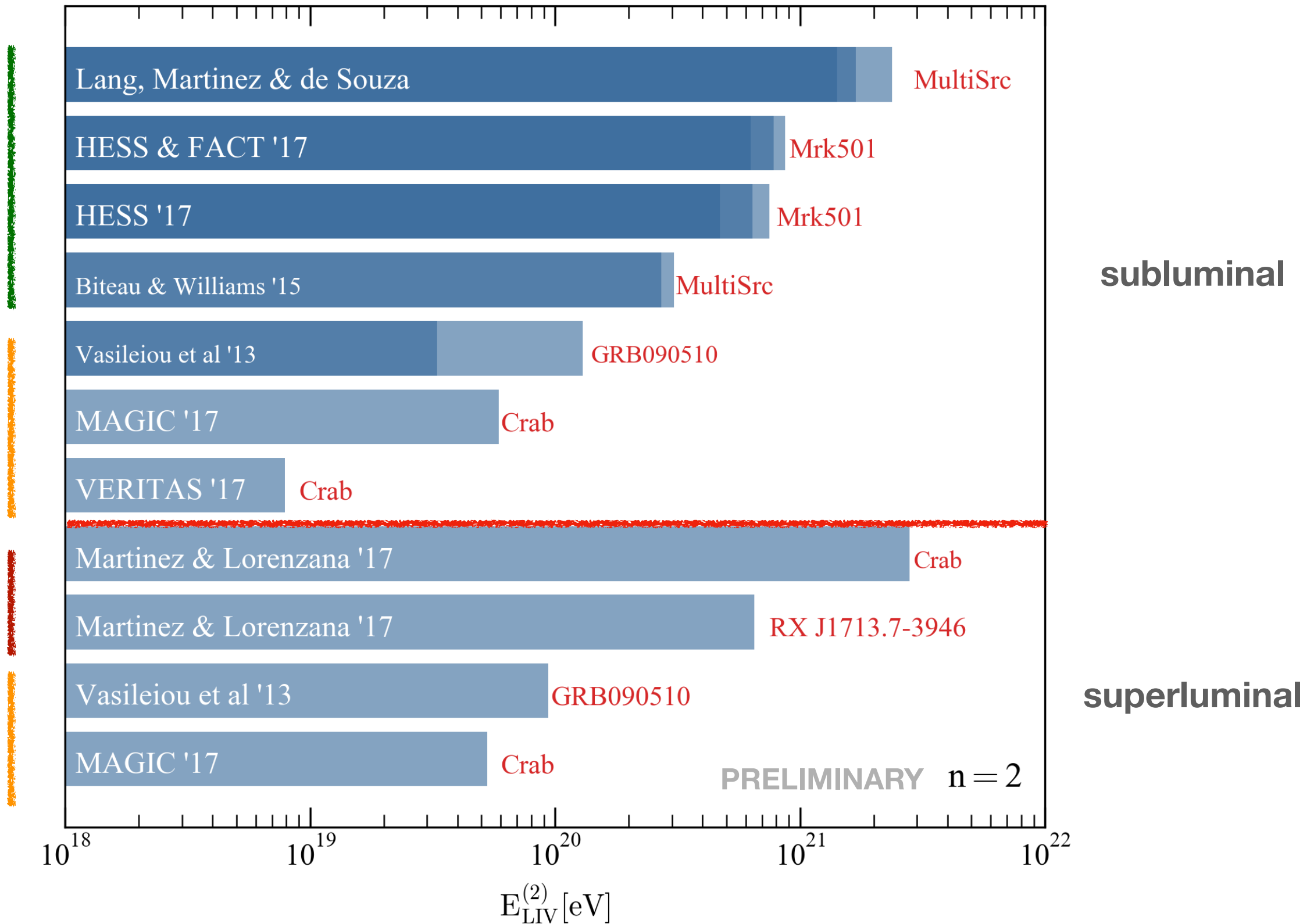


- ▶ Choices of the EBL models
- ▶ Model of the intrinsic spectrum
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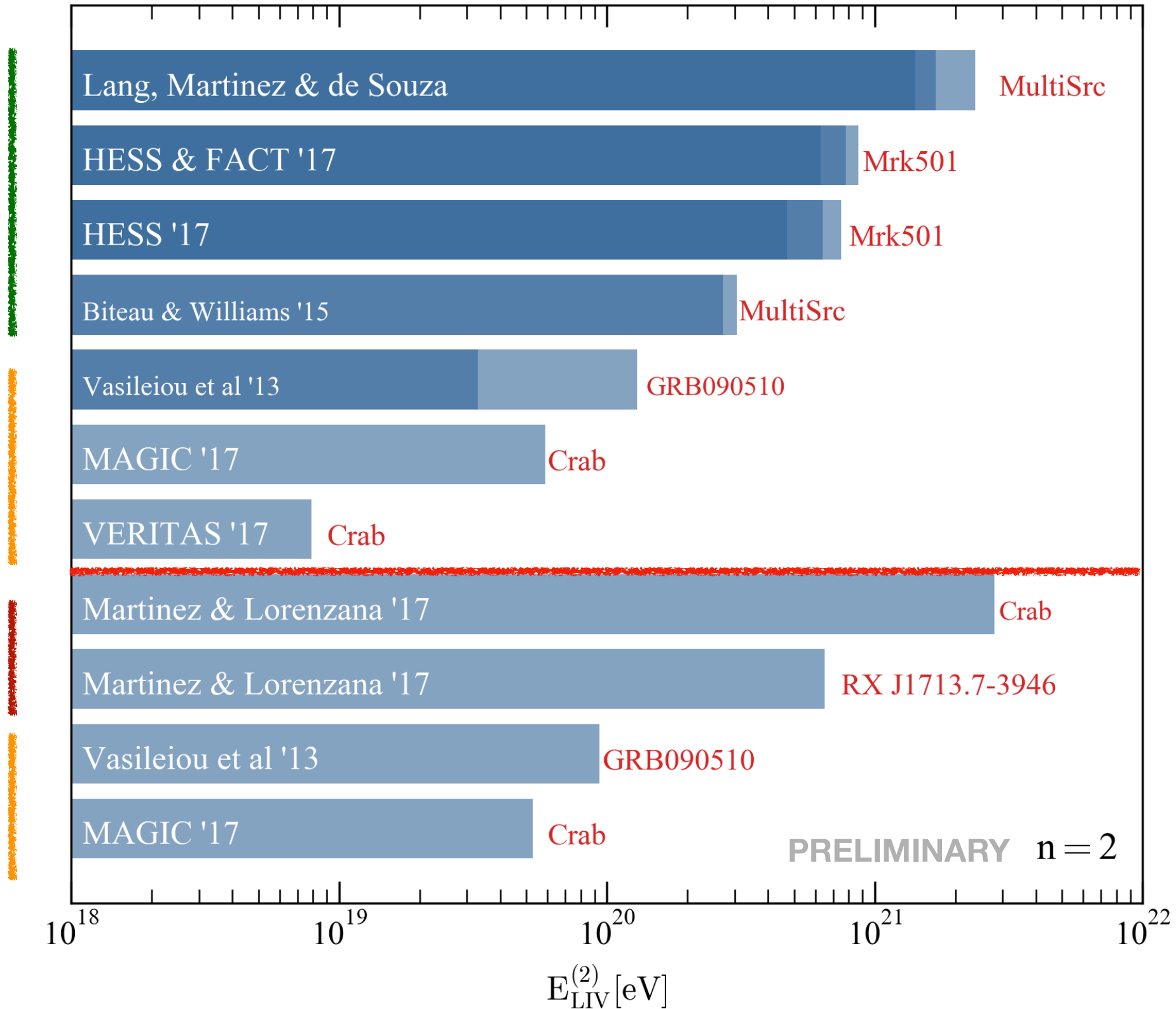


$E_{LIV}^{(2)}$ [eV] Lang, Martínez and De Souza
arXiv:1810.13215
Submitted

LIV limits : γ -rays



LIV limits : γ -rays



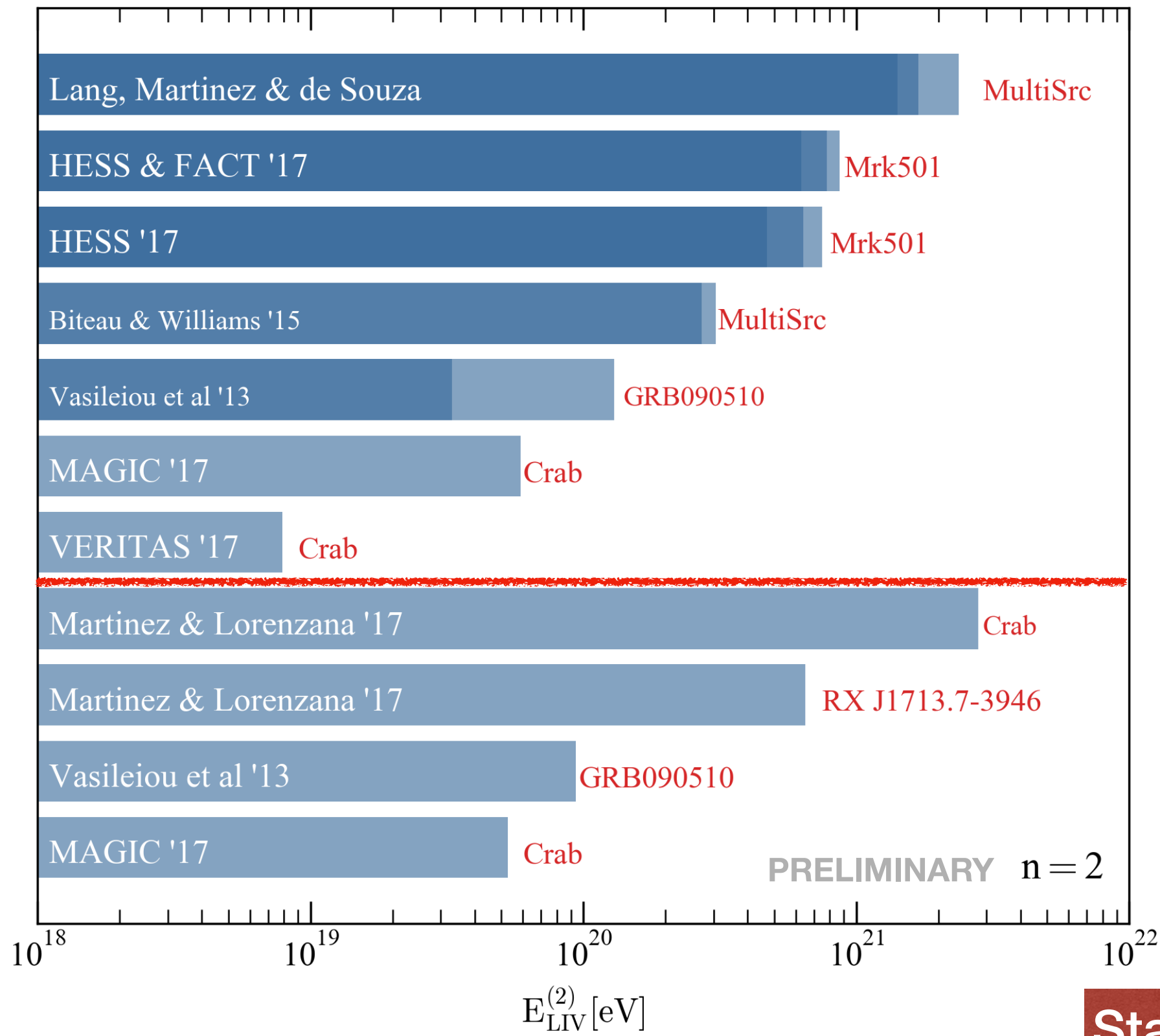
LIV limits : γ -rays

Pair production shift threshold

Time energy dependent delay

Photon decay

Time energy Dependent delay



Stay tuned...

Conclusions and remarks I

- ❖ **Astroparticle physics has recently reached the status of precision science** due to the construction of new observatories, operating innovative technologies and the detection of large numbers of events and sources.
 - ➔ The precise measurements of cosmic and gamma rays can be used as test for fundamental physics, such as the Lorentz invariance violation.
- ❖ We have established **the best limits** to the LIV energy scale to the superluminal and subluminal regime.
- ❖ We developed **a new analysis procedures for searching LIV signatures** using multiple TeV measured energy spectra.
- ❖ We are studying the potential to test / constrain LIV signatures with **HAWC, SGSO and CTA**

- I. Lorentz invariance violation (LIV)

- II. Limits: TeV γ -rays
 - i. Time Energy Dependent delay

 - ii. Photon Decay

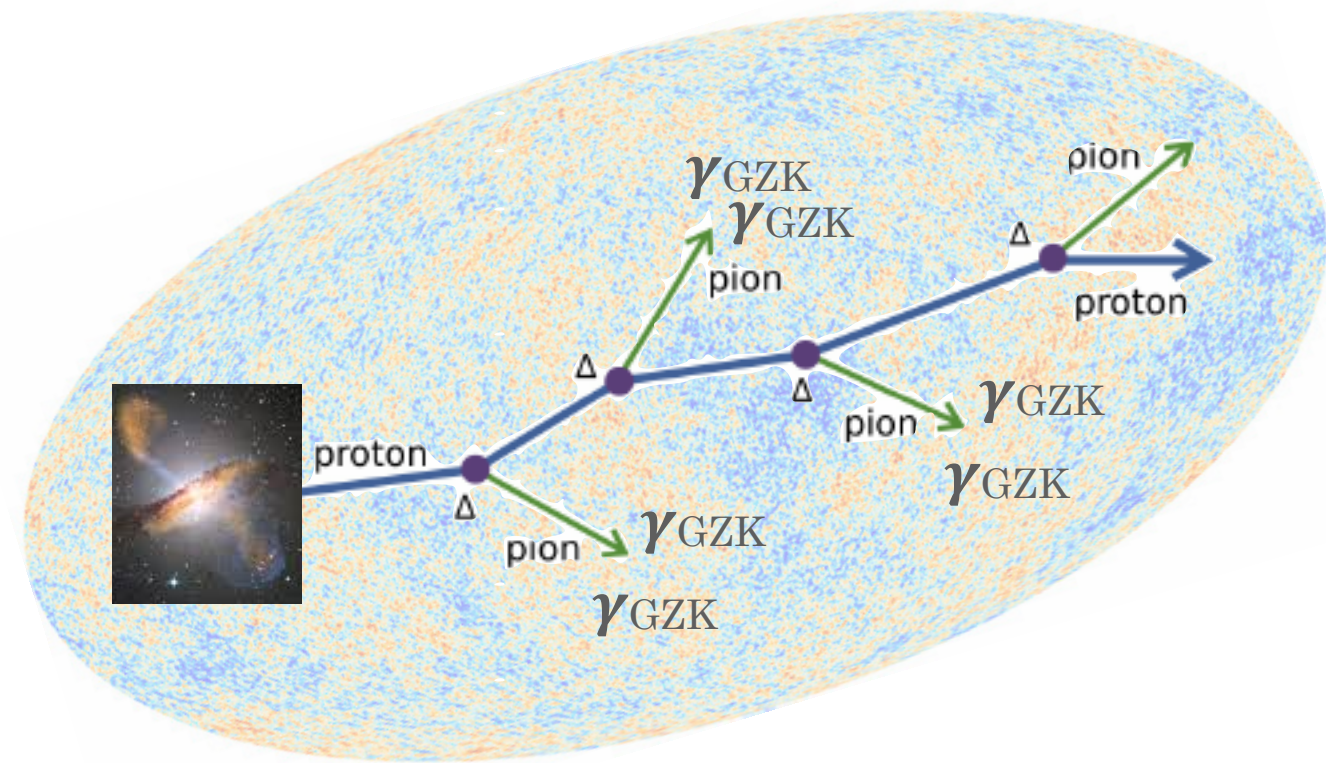
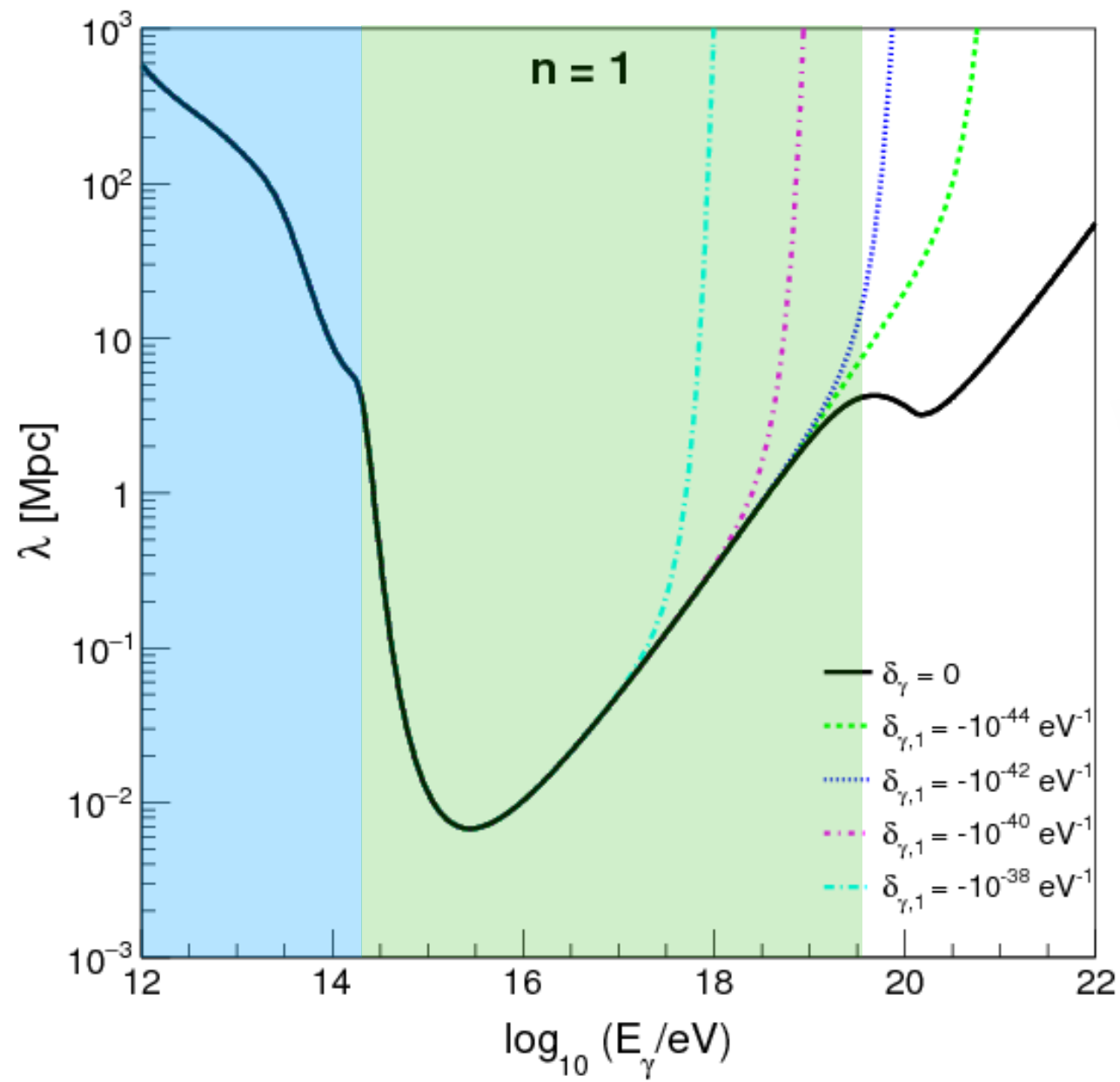
 - iii. Pair production threshold shifts

III. UHECR

- i. GZK-photons + LIV**

- ii. Limits

GZK photons + LIV



Model of UHECR Sources

$$\frac{dN}{dE_s} = \begin{cases} E_s^{-\Gamma}, & \text{for } R_s < R_{\text{cut}} \\ E_s^{-\Gamma} e^{1-R_s/R_{\text{cut}}}, & \text{for } R_s \geq R_{\text{cut}} \end{cases},$$

1. C_1 : Aloisio et al. (2014);
2. C_2 : Unger, Farrar, & Anchordoqui (2015)—Fiducial model (Unger et al. 2015);
3. C_3 : Unger et al. (2015) with the abundance of galactic nuclei from (Olive & Group 2014);
4. C_4 : Berezhinsky, Gazizov, & Grigorieva (2007)—Dip model (Berezhinsky et al. 2006).

Parameters of the Four Source Models Used in This Paper

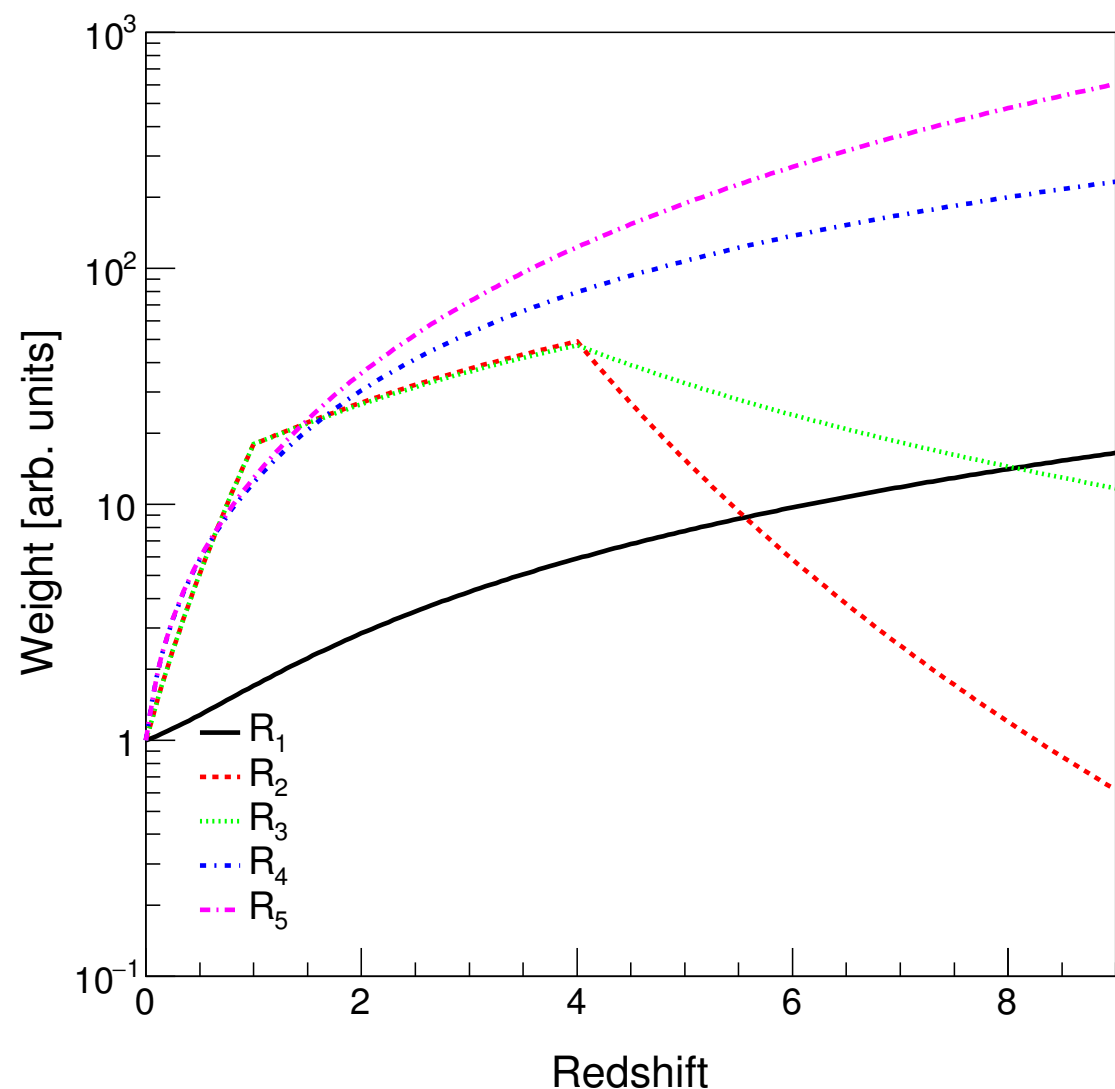
Model	Γ	$\log_{10}(R_{\text{cut}}/V)$	fH	fHe	fN	fSi	fFe
C_1	1	18.699	0.7692	0.1538	0.0461	0.0231	0.00759
C_2	1	18.5	0	0	0	1	0
C_3	1.25	18.5	0.365	0.309	0.121	0.1066	0.098
C_4	2.7	∞	1	0	0	0	0

Note. Γ is the spectral index, R_{cut} is the rigidity cutoff and fH , fHe , fN , fSi , and fFe are the fractions of each nuclei.

Model of UHECR Sources

Models of Source Distribution

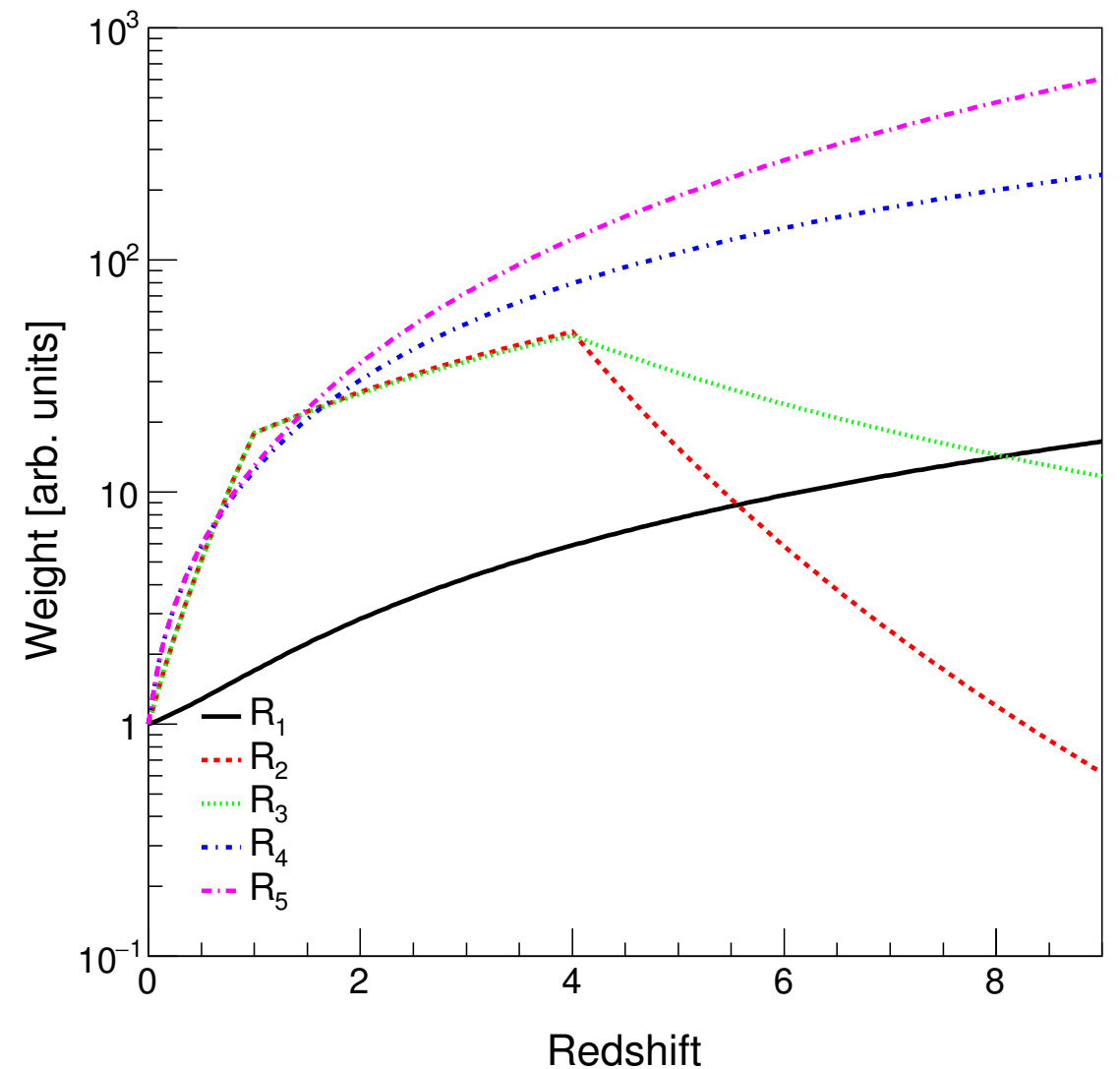
1. R_1 : sources are uniformly distributed in a comoving volume;
2. R_2 : sources follow the star formation distribution given in Hopkins & Beacom (2006). The evolution is proportional to $(1+z)^{3.4}$ for $z < 1$, to $(1+z)^{-0.26}$ for $1 \leq z < 4$ and to $(1+z)^{-7.8}$ for $z \geq 4$;
3. R_3 : sources follow the star formation distribution given in Yüksel et al. (2008). The evolution is proportional to $(1+z)^{3.4}$ for $z < 1$, to $(1+z)^{-0.3}$ for $1 \leq z < 4$ and to $(1+z)^{-3.5}$ for $z \geq 4$;
4. R_4 : sources follow the GRB rate evolution from Le & Dermer (2007). The evolution is proportional to $(1+8z)/[1+(z/3)^{1.3}]$;
5. R_5 : sources follow the GRB rate evolution from Le & Dermer (2007). The evolution is proportional to $(1+11z)/[1+(z/3)^{0.5}]$.



Model of UHECR Sources

Models of Source Distribution

1. R_1 : sources are uniformly distributed in a comoving volume;
2. R_2 : sources follow the star formation distribution given in Hopkins & Beacom (2006). The evolution is proportional to $(1+z)^{3.4}$ for $z < 1$, to $(1+z)^{-0.26}$ for $1 \leq z < 4$ and to $(1+z)^{-7.8}$ for $z \geq 4$;
3. R_3 : sources follow the star formation distribution given in Yüksel et al. (2008). The evolution is proportional to $(1+z)^{3.4}$ for $z < 1$, to $(1+z)^{-0.3}$ for $1 \leq z < 4$ and to $(1+z)^{-3.5}$ for $z \geq 4$;
4. R_4 : sources follow the GRB rate evolution from Le & Dermer (2007). The evolution is proportional to $(1+8z)/[1+(z/3)^{1.3}]$;
5. R_5 : sources follow the GRB rate evolution from Le & Dermer (2007). The evolution is proportional to $(1+11z)/[1+(z/3)^{0.5}]$.



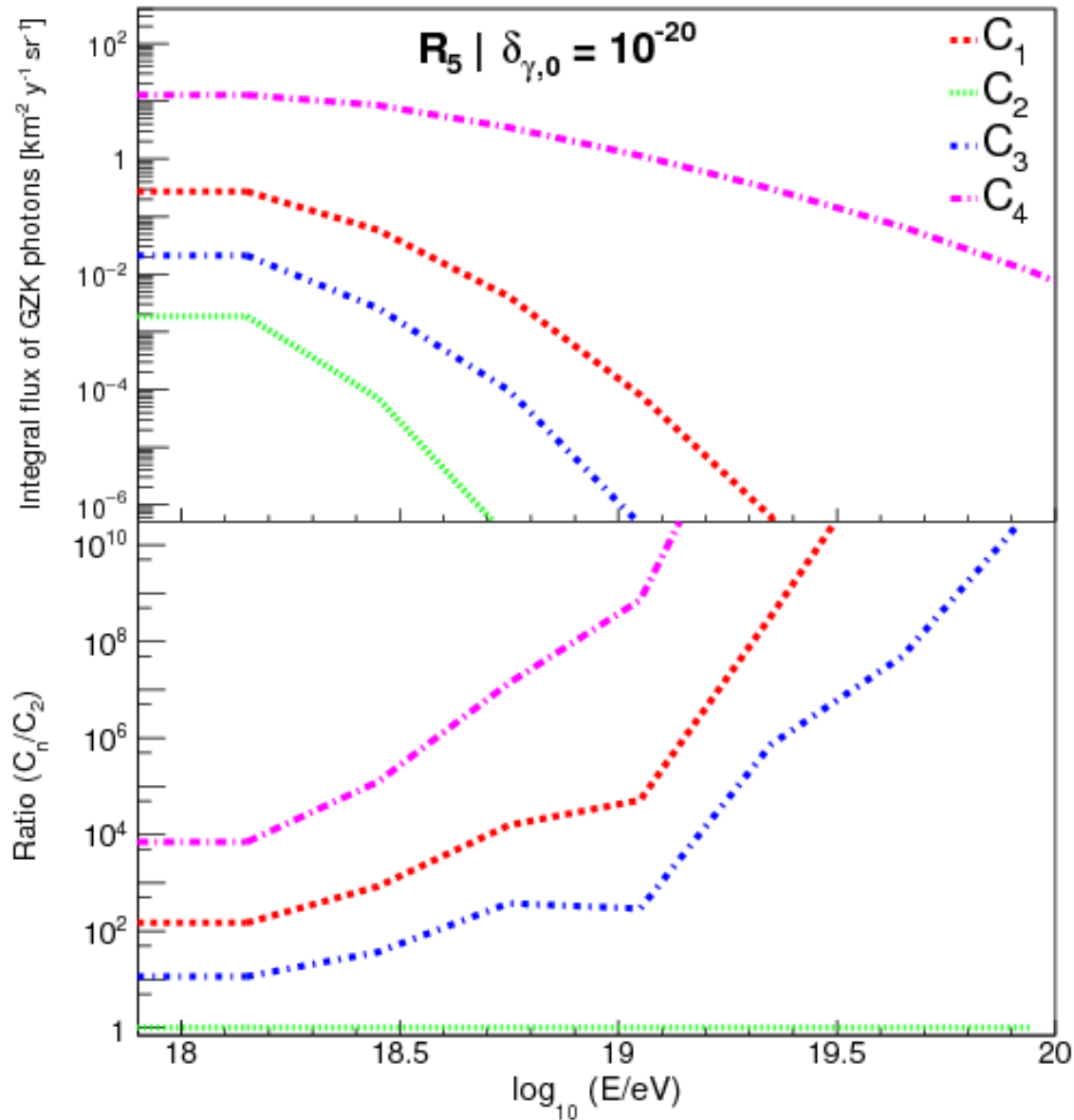
CRPropa3/EleCA

(Settimo & Domenico 2015; Batista et al. 2016)

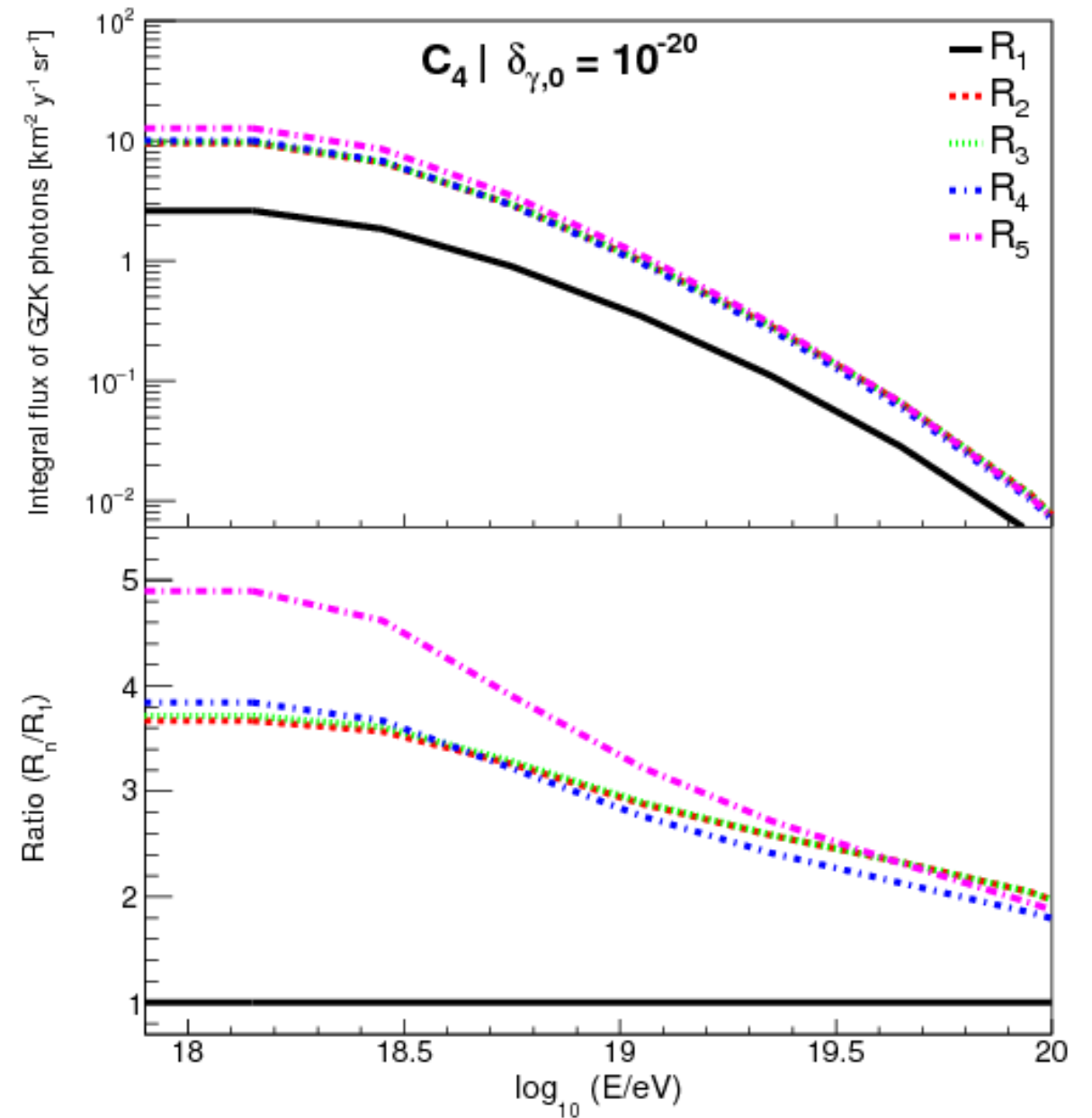
Lang, Martinez & De Souza
ApJ 853, no.1, 23 (2018)

Integral flux of GZK photons + LIV

... for each source model



... for each source evolution model

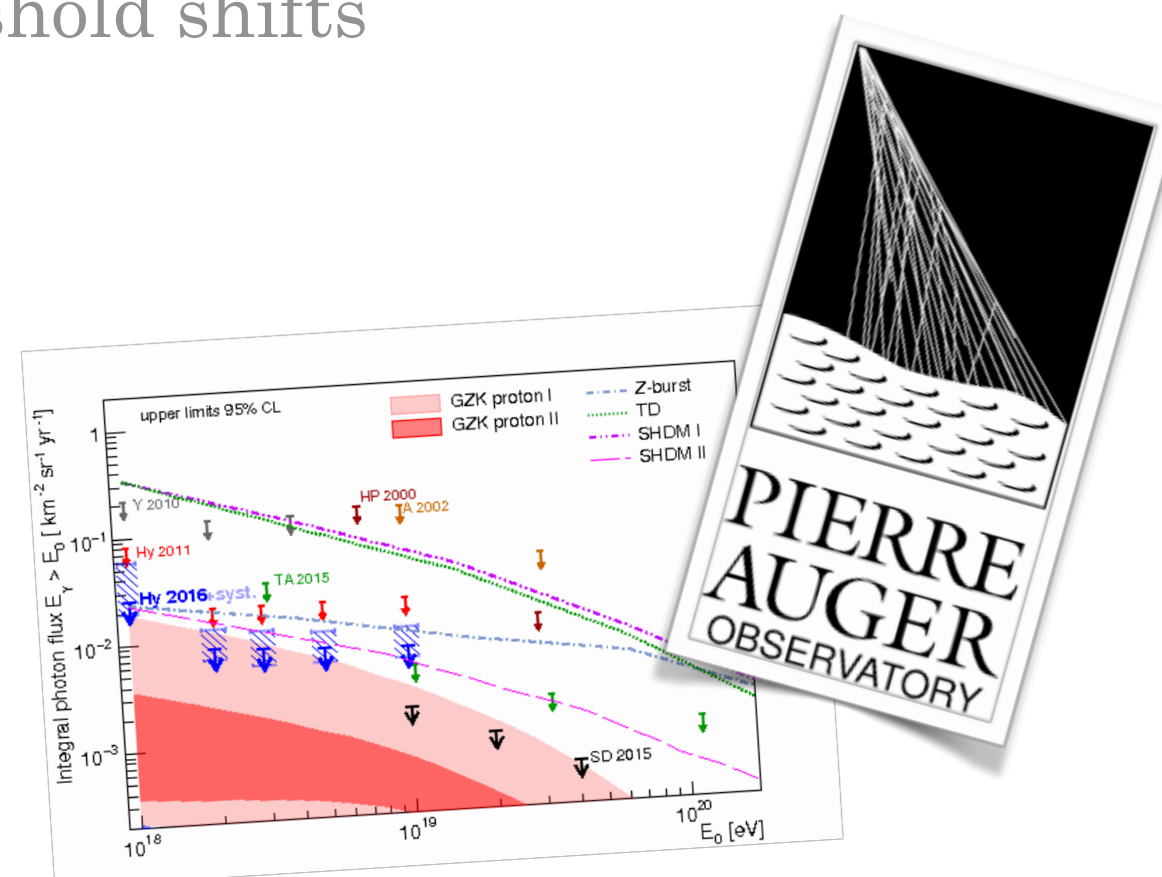


Different LIV coefficients result in a shift up an down

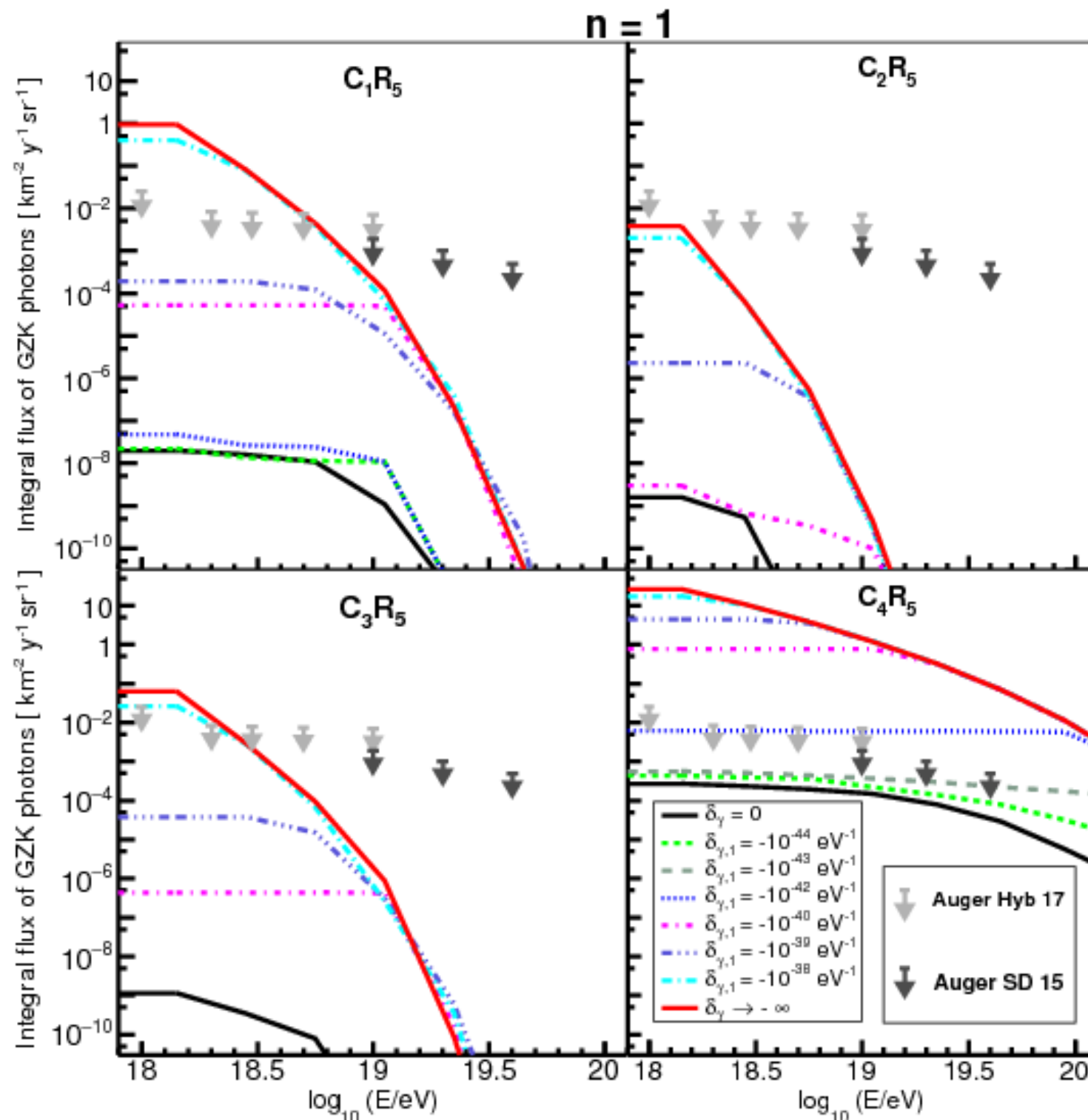
Index

- I. Lorentz invariance violation (LIV)
- II. Limits: TeV γ -rays
 - i. Time Energy Dependent delay
 - ii. Photon Decay
 - iii. Pair production threshold shifts
- III. UHECR

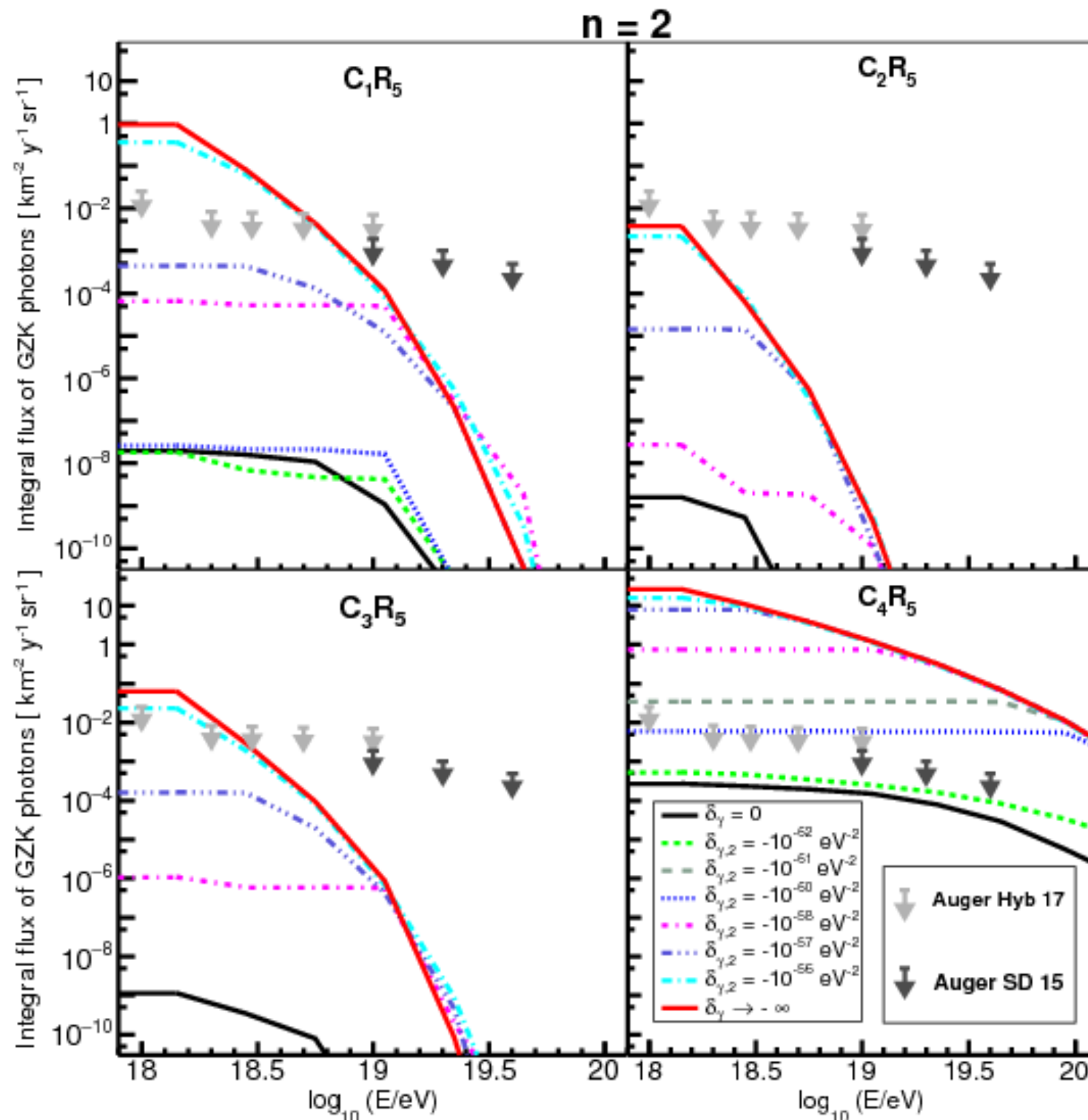
- i. GZK-photons + LIV
- ii. **Limits**



GZK photon flux + LIV



GZK photon flux + LIV



Model C₃R₅ was shown to (best) describe the energy spectrum, composition, and arrival direction of UHECR*

Limits on the LIV Coefficients Imposed by This Work for Each Source Model and LIV Order (n)

Model	$\delta_{\gamma,0}^{\text{limit}}$	$\delta_{\gamma,1}^{\text{limit}} (\text{eV}^{-1})$	$\delta_{\gamma,2}^{\text{limit}} (\text{eV}^{-2})$
C_1R_5	$\sim -10^{-20}$	$\sim -10^{-38}$	$\sim -10^{-56}$
C_2R_5
C_3R_5	$\sim -10^{-20}$	$\sim -10^{-38}$	$\sim -10^{-56}$
C_4R_5	$\sim -10^{-22}$	$\sim -10^{-42}$	$\sim -10^{-60}$

Limits on the LIV Coefficients Imposed by Other Works Based on Gamma-Ray Propagation

Model	$\delta_{\gamma,0}^{\text{limit}}$	$\delta_{\gamma,1}^{\text{limit}} (\text{eV}^{-1})$	$\delta_{\gamma,2}^{\text{limit}} (\text{eV}^{-2})$
Galaverni & Sigl (2008a)	...	-1.97×10^{-43}	-1.61×10^{-63}
H.E.S.S.—PKS 2155–304 (2011)	...	-4.76×10^{-28}	-2.44×10^{-40}
Fermi—GRB 090510 (2013)	...	-1.08×10^{-29}	-5.92×10^{-41}
H.E.S.S.—Mrk 501 (2017)	...	-9.62×10^{-29}	-4.53×10^{-42}

Limits on the LIV Coefficients Imposed by This Work for Each Source Model and LIV Order (n)

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Model	$\delta_{\gamma,0}^{\text{limit}}$	$\delta_{\gamma,1}^{\text{limit}} (\text{eV}^{-1})$	$\delta_{\gamma,2}^{\text{limit}} (\text{eV}^{-2})$
Galaverni & Sigl (2008a)	...	-1.97×10^{-43}	-1.61×10^{-63}
H.E.S.S.—PKS 2155–304 (2011)	...	-4.76×10^{-28}	-2.44×10^{-40}
Fermi—GRB 090510 (2013)	...	-1.08×10^{-29}	-5.92×10^{-41}
H.E.S.S.—Mrk 501 (2017)	...	-9.62×10^{-29}	-4.53×10^{-42}

Conclusions and remarks II

- ❖ We studied the effect of possible LIV in the propagation of photons in the universe.
- ❖ The **mean-free path of the pair production** interaction was calculated **considering LIV effects**.
- ❖ We found that even moderate LIV coefficients introduce a significant change in the mean-free path of the interaction.
- ❖ **The GZK photon flux including LIV was obtained** for different source models and source distribution models.
- ❖ **Limits to the LIV** coefficient were established based on source models **compatible with the most updated data of UHECR**.
- ▶ The limits presented here are several orders of magnitude more restrictive than previous calculations based on the arrival time of TeV photons; however, the comparison is not straightforward due to different systematics of the measurements and energy of the photons.

Thanks!