

# Flavour anomalies and (fundamental) partial compositeness

Presented by Peter Stangl

Laboratoire d'Annecy-le-Vieux  
de Physique Théorique



# Outline

- 1 Motivation: Flavour anomalies
- 2 Violation of lepton flavour universality in composite Higgs models
- 3 Flavour analysis of minimal fundamental partial compositeness
- 4 Summary

## Based on:

Wolfgang Altmannshofer, Christoph Niehoff, PS, David M. Straub [arXiv:1703.09189]

Wolfgang Altmannshofer, PS, David M. Straub [arXiv:1704.05435 ]

Christoph Niehoff, PS, David M. Straub [arXiv:1503.03865]

Francesco Sannino, PS, David M. Straub, Anders E. Thomsen [arXiv:1712.07646]

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## $b \rightarrow s \mu^+ \mu^-$ anomaly

Several LHCb measurements deviate from Standard model (SM) predictions by 2-3 $\sigma$ :

- ▶ Angular observable  $P'_5$  in  $B \rightarrow K^* \mu^+ \mu^-$ . LHCb, arXiv:1512.04442
- ▶ Branching ratios of  $B \rightarrow K \mu^+ \mu^-$ ,  $B \rightarrow K^* \mu^+ \mu^-$ , and  $B_s \rightarrow \phi \mu^+ \mu^-$ .

LHCb, arXiv:1403.8044, arXiv:1506.08777, arXiv:1606.04731

$$\mathcal{O}_9^\ell = (\bar{s} \gamma_\mu P_L b) (\bar{\ell} \gamma^\mu \ell)$$

$$\mathcal{O}_{10}^\ell = (\bar{s} \gamma_\mu P_L b) (\bar{\ell} \gamma^\mu \gamma_5 \ell)$$

see also fits by other groups:

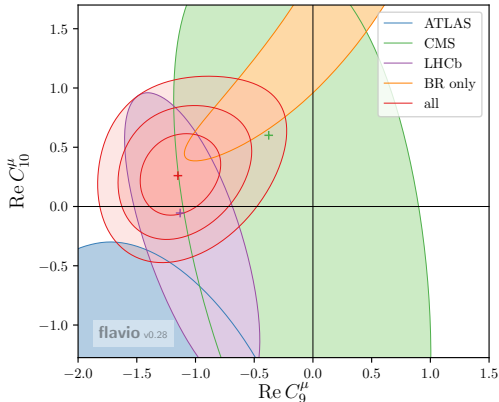
Capdevila et al., arXiv:1704.05340

D'Amico et al., arXiv:1704.05438

Geng et al., arXiv:1704.05446

Ciuchini et al., arXiv:1704.05447

Mahmoudi et al., arXiv:1611.05060



Altmannshofer, Niehoff, PS, Straub, arXiv:1703.09189

## Hints for LFU violation in neutral current decays

Measurements of lepton flavour universality (LFU) ratios  $R_K^{[1,6]}$ ,  $R_{K^*}^{[0.045,1.1]}$ ,  $R_{K^*}^{[1.1,6]}$  show deviations from SM by about  $2.5\sigma$  each.

LHCb, arXiv:1406.6482, arXiv:1705.05802

$$R_{K^{(*)}} = \frac{BR(B \rightarrow K^{(*)} \mu^+ \mu^-)}{BR(B \rightarrow K^{(*)} e^+ e^-)}$$

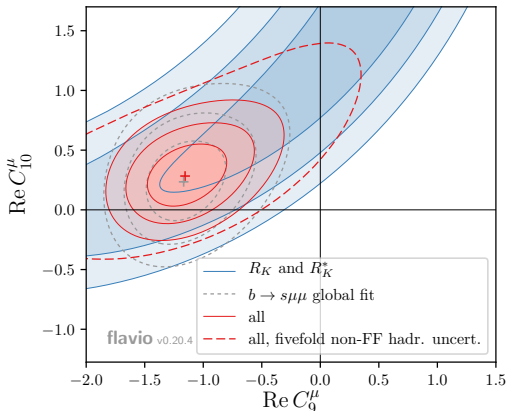
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Ciuchini et al., arXiv:1704.05447



Altmannshofer, PS, Straub, arXiv:1704.05435

# Hints for LFU violation in charged current decays

Measurements of LFU ratios  $R_D$  and  $R_{D^*}$  by BaBar, Belle, and LHCb show combined deviation from SM by 3.6-3.8 $\sigma$ .

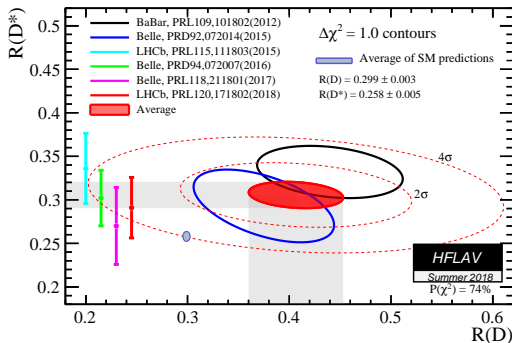
BaBar, arXiv:1205.5442, arXiv:1303.0571

LHCb, arXiv:1506.08614, arXiv:1708.08856

Belle, arXiv:1507.03233, arXiv:1607.07923, arXiv:1612.00529

$$R_{D^{(*)}} = \frac{BR(B \rightarrow D^{(*)} \tau \nu)}{BR(B \rightarrow D^{(*)} \ell \nu)}$$

$$\ell \in \{e, \mu\}$$



HFLAV, arXiv:1612.07233

# Explaining the anomalies

see also talk by M eril Reboud

## Construct model to address flavour anomalies

- ▶ Plethora of models constructed to specifically address flavour anomalies.

## This talk: analyze potential of existing models to explain anomalies

Consider models originally constructed to address **naturalness problem** of SM:

- ▶ **Composite Higgs model** (CHM) with **partial compositeness**.
- ▶ UV completion of CMH: **Minimal Fundamental Partial Compositeness**.

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# Composite Higgs models

## Solving the naturalness problem

- ▶ Higgs not elementary but bound state of new strong interaction.
- ▶ Lightness of Higgs compared to new physics scale:  
**Higgs as pseudo-Nambu-Goldstone boson (pNGB)**  
of spontaneously broken global symmetry.

Kaplan, Georgi,  
Phys.Lett. B136 (1984) 183  
Dugan, Georgi, Kaplan,  
Nucl.Phys. B254 (1985) 299

$$\mathcal{L} = \mathcal{L}_{\text{elementary}} + \mathcal{L}_{\text{composite}}$$

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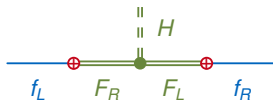
Kaplan, Georgi,  
 Phys.Lett. B136 (1984) 183  
 Dugan, Georgi, Kaplan,  
 Nucl.Phys. B254 (1985) 299

$$\mathcal{L} = \mathcal{L}_{\text{elementary}} + \mathcal{L}_{\text{composite}} + \mathcal{L}_{\text{mixing}}$$

## Avoiding flavour constraints

- ▶ **Elementary fermions** couple linearly to **composite fermions**.
- ▶ Mass eigenstates are mixture of both: **partial compositeness**.

Kaplan, Nucl. Phys. B365 (1991) 259–278



# Violation of LFU in composite Higgs models

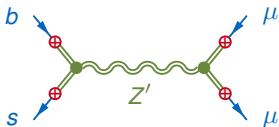
Niehoff, PS, Straub, arXiv:1503.03865

## Considering only anomalies in rare $B$ decays

$b \rightarrow s \mu \mu$  anomaly and hints for violation of LFU in  $R_K, R_{K^*}$  measurements.

## LFU violating $b \rightarrow s \mu \mu$ transition

Only one possibility to violate LFU in  $b \rightarrow s \mu \mu$  at tree-level:



## Experimental data suggests

- ▶  $C_9^\mu < 0$ : sizable left- and right-handed degrees of compositeness  $s_{\mu_L}$  and  $s_{\mu_R}$ .
- ▶  $C_9^\mu = -C_{10}^\mu < 0$ : only sizable  $s_{\mu_L}$ .

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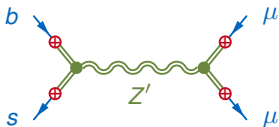
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 $s_{\mu_L} \cdot s_{\mu_R}$  enters  $\mu$  mass; has to be small!
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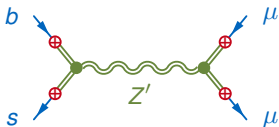
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- ▶  $C_9^\mu = -C_{10}^\mu < 0$ : only sizable  $s_{\mu_L}$ . Seems possible!

# Constraints

## Constraints from $B_s$ - $\bar{B}_s$ mixing

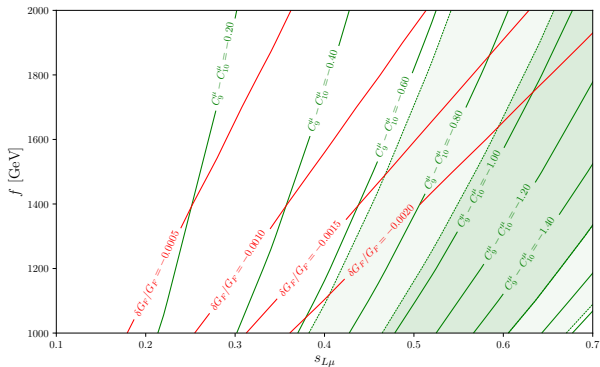
- ▶  $Z'bs$  coupling implies contribution to  $B_s$ - $\bar{B}_s$  mixing.
- ▶ Upper bound on  $Z'bs$  coupling leads to **lower bound on  $s_{\mu_L}$** .

## Constraints from electroweak precision tests

$Z'\mu_L\mu_L$  coupling generically implies corrections to  $Z\mu\mu$ ,  $W\mu\nu_\mu$ , and  $Z\nu_\mu\nu_\mu$  couplings.

- ▶  $Z\mu\mu$  coupling can be protected by discrete symmetry. Agashe et al., arXiv:hep-ph/0605341  
Agashe, arXiv:0902.2400
- ▶ Modification of  $W\mu\nu_\mu$  coupling leads to correction of Fermi constant.  
Yields **upper bound on  $s_{\mu_L}$** .
- ▶ Modified  $Z\nu_\mu\nu_\mu$  coupling can explain LEP  $2\sigma$  deficit in invisible  $Z$  width.  
*Improves agreement with data!*

# Results



$$C_9^\mu - C_{10}^\mu \approx \pm 0.92 \left[ \frac{1.7 \text{ TeV}}{f} \right] \left[ \frac{s_{\mu L}}{0.6} \right]^2 \left[ \frac{|\Delta M_s - \Delta M_s^{\text{SM}}|}{0.1 \Delta M_s^{\text{SM}}} \right]^{1/2}$$

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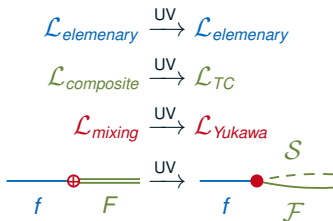


# Fundamental partial compositeness

Sannino, Strumia, Tesi, Vigiani, arXiv:1607.01659

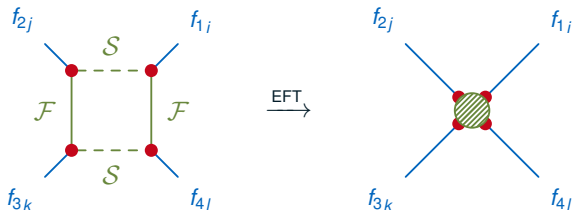
- ▶ New strong interaction: “Technicolor” (TC).
- ▶ SM fermions and vector bosons + “technifermions”  $\mathcal{F}$  + “techniscalars”  $\mathcal{S}$ .
- ▶ Higgs:  $(\mathcal{F}\mathcal{F})$  bound state.
- ▶ Composite fermions:  $(\mathcal{F}\mathcal{S})$  bound states.
- ▶ SM fermions  $f$  and TC fields  $\mathcal{F}$ ,  $\mathcal{S}$  coupled by fundamental Yukawa couplings  $y_f$ .

## Comparison with effective composite Higgs models



## Effective field theory at electroweak scale

- Consider effective field theory (EFT) of Minimal Fundamental Partial Compositeness (MFPC): **MFPC-EFT**. Cacciapaglia, Gertov, Sannino, Thomsen, arXiv:1704.07845



$$\propto (y_{f_1}^T y_{f_2})_{ij} (y_{f_3}^T y_{f_4})_{kl}$$

- Flavour structure** from **fundamental Yukawa couplings**.

# Flavour analysis of MFPC

Sannino, PS, Straub, Thomsen, arXiv:1712.07646

- ▶ Consider parameters of MFPC-EFT relevant for flavour observables.
- ▶ Constrain parameter space by
  - ▶ SM fermion masses and CKM elements,
  - ▶ Electroweak scale observables,
  - ▶ Low-energy flavour observables.
- ▶ Make predictions for LFU observables  $R_{K^{(*)}}$  and  $R_{D^{(*)}}$ .

## Electroweak scale observables

- ▶ Use MFPC-EFT at electroweak (EW) scale.
- ▶ Most important constraints: ratios of **Z partial widths** (measured at LEP),

$$R_e = \frac{\Gamma(Z \rightarrow q\bar{q})}{\Gamma(Z \rightarrow e\bar{e})}, \quad R_\mu = \frac{\Gamma(Z \rightarrow q\bar{q})}{\Gamma(Z \rightarrow \mu\bar{\mu})}, \quad R_\tau = \frac{\Gamma(Z \rightarrow q\bar{q})}{\Gamma(Z \rightarrow \tau\bar{\tau})},$$

$$R_b = \frac{\Gamma(Z \rightarrow b\bar{b})}{\Gamma(Z \rightarrow q\bar{q})}, \quad R_c = \frac{\Gamma(Z \rightarrow c\bar{c})}{\Gamma(Z \rightarrow q\bar{q})}.$$

# Low-energy flavour observables

- ▶ Match MFPC-EFT to weak effective Hamiltonian (WEH).
- ▶ **Meson-antimeson mixing**
  - ▶ Indirect  $CP$  violation in kaon mixing:  $\epsilon_K$ .
  - ▶ Mixing-induced  $CP$  asymmetries in  $B_d$  and  $B_s$  systems:  $S_{\psi K_S}$  and  $S_{\psi\phi}$ .
  - ▶ Mass differences in  $B_d$  and  $B_s$  systems:  $\Delta M_d$  and  $\Delta M_s$ .
- ▶ **Charged-current semi-leptonic decays** (CKM elements and  $e$ - $\mu$  universality)
  - ▶  $\text{BR}(\pi^+ \rightarrow e\nu)$ , based on  $d \rightarrow ue\nu$ .
  - ▶  $\text{BR}(K^+ \rightarrow \mu\nu)$ ,  $\text{BR}(K^+ \rightarrow e\nu) / \text{BR}(K^+ \rightarrow \mu\nu)$ , based on  $s \rightarrow ue\nu$ ,  $s \rightarrow u\mu\nu$ .
  - ▶  $\text{BR}(B \rightarrow De\nu)$ ,  $\text{BR}(B \rightarrow D\mu\nu)$ , based on  $b \rightarrow ce\nu$ ,  $b \rightarrow c\mu\nu$ .
  - ▶ **Predictions** for LFU observables  $R_D$  and  $R_{D^*}$ .
- ▶ **Neutral-current semi-leptonic decays**
  - ▶ **Predictions** for LFU observables  $R_K$  and  $R_{K^*}$ .

# Numerical method

## Parameter scan challenging

37 parameters (1 for strong coupling scale, 22 for fundamental Yukawa couplings, 14 for Wilson coefficients of MFPC-EFT)

## Strategy

To find **viable parameter points** satisfying all constraints:

### ► Step 1

- Construct  $\chi_{mass,CKM}^2$  function for quark masses and CKM elements depending only on 19 parameters.
- Numerically minimize  $\chi_{mass,CKM}^2$  for 100 k random starting points.
- Sample regions around local minima using Markov Chains from `pypmc` package to yield 1000 points for each minimum.

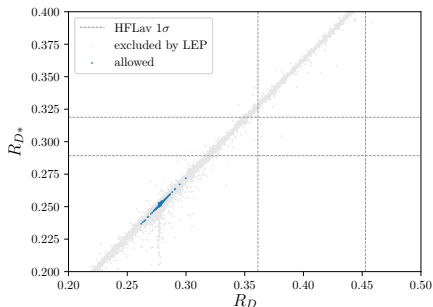
Yields 100 M points predicting correct quark masses and CKM elements.

### ► Step 2

- Randomly choose remaining 18 parameters for each point.
- Calculate EW scale and flavour observables using `flavio` code.

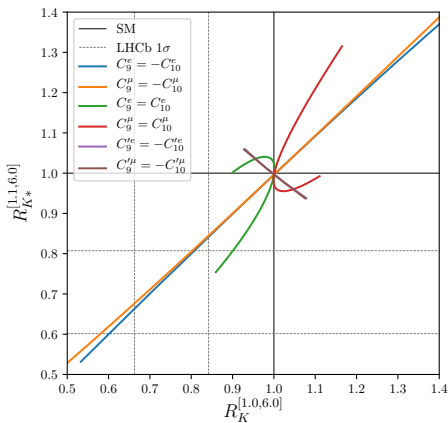
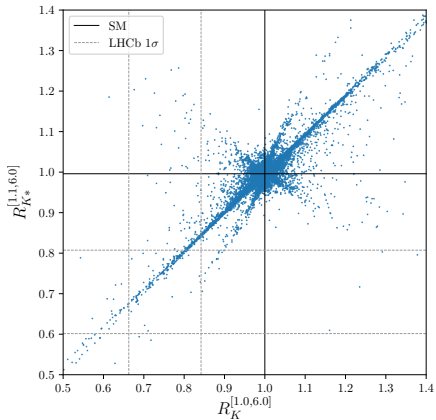
## Results

- ▶  $\epsilon_K$  provides very strong constraint, but can be satisfied by large number of parameter points.
- ▶ Tests of  $e$ - $\mu$  universality in charged-current decays are important constraints due to generic LFU violation from partial compositeness.
- ▶ Large deviation of  $R_{D^{(*)}}$  from SM value is in conflict with Z partial widths (modified  $Z_{\tau\tau}$  coupling).



# Results

- Anomalies in rare B decays can be explained!





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## Summary

CHM with sizable degree of compositeness of left-handed muons can explain anomalies in rare B decays.

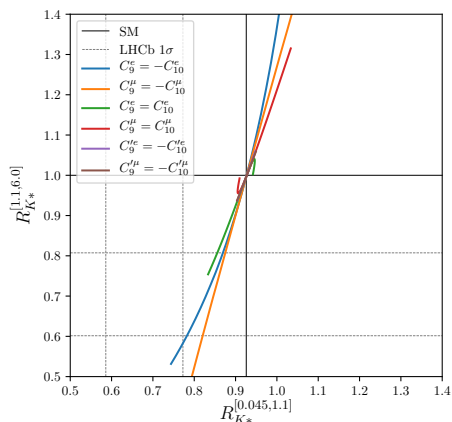
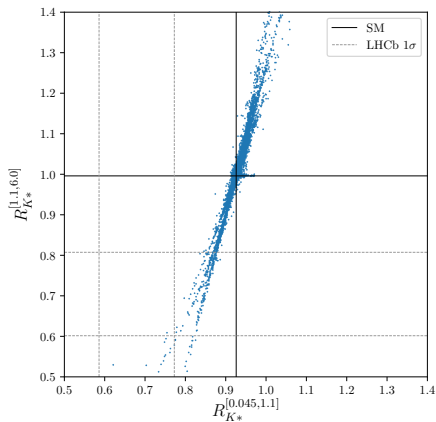
- ▶ Corresponds to new physics contribution to  $C_9^\mu = -C_{10}^\mu < 0$ .
- ▶ Predicts deviation in  $B_s$ - $\bar{B}_s$  mixing.
- ▶ Correction to Fermi constant yields strongest constraint from EWPT if tree level Z couplings are protected by discrete symmetry.

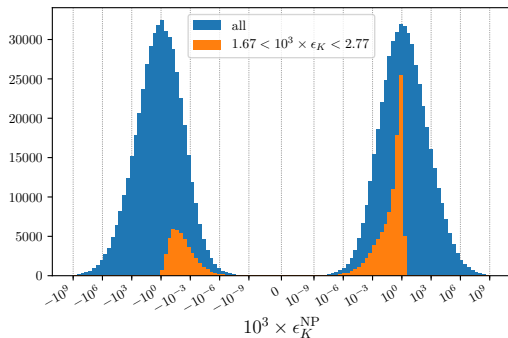
Performed comprehensive numerical analysis of flavour and EW scale effects of MFPC model.

- ▶ Numerical method allows for scan of high dimensional parameter space.
- ▶ Strongest constraints from  $\epsilon_K$ , but satisfied by large number of parameter points.
- ▶ Large deviation of  $R_{D^{(*)}}$  from SM value is in conflict with Z partial widths.
- ▶ Anomalies in rare B decays can be explained.

# Backup slides

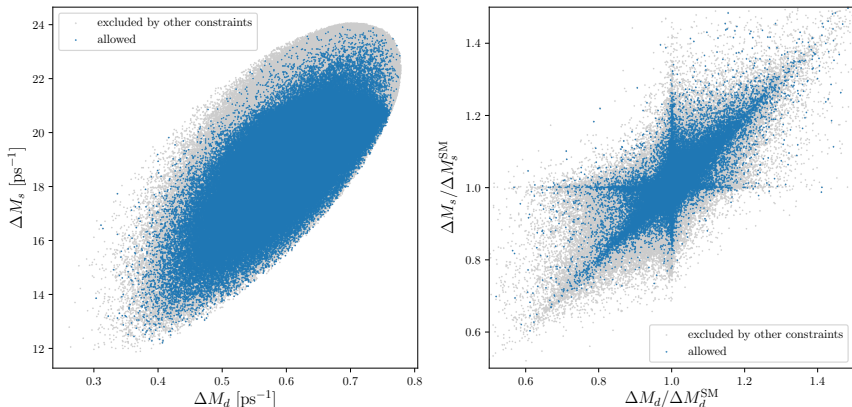
# $R_{K^*}$ predictions



$\epsilon_K$ 

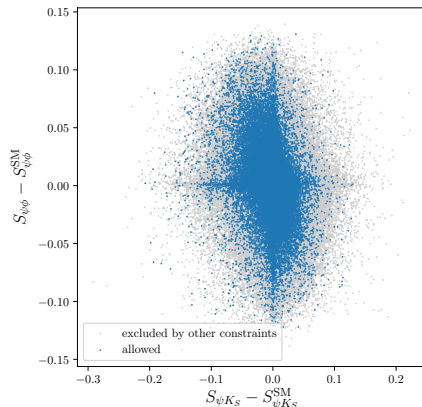
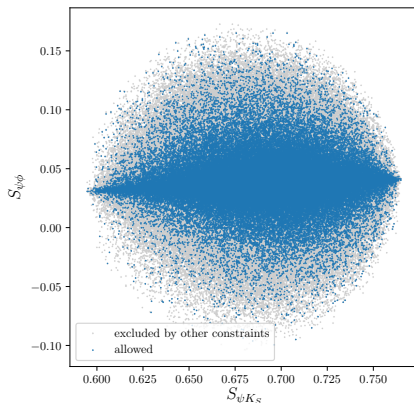
**Figure:** Histogram showing the NP contribution to  $\epsilon_K$  for a representative subset of all points that feature the right masses and CKM elements, compared to the points among those that pass the experimental constraint. A positive NP contribution corresponds to constructive interference with the SM.

## $\Delta M_d$ and $\Delta M_s$



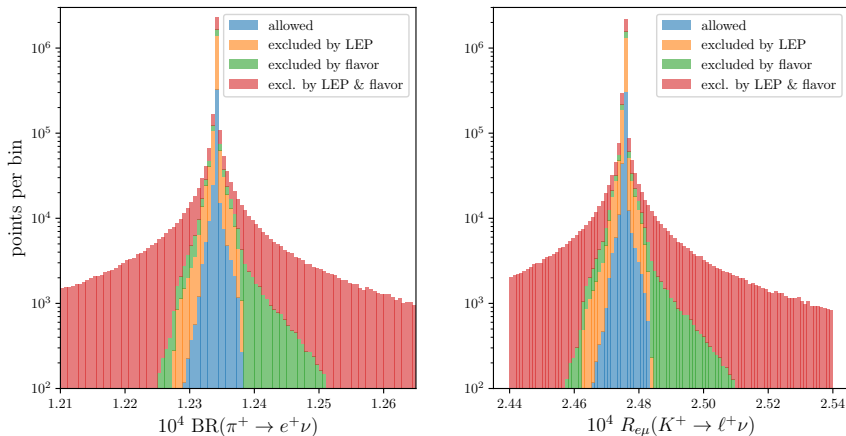
**Figure:** Predictions for  $\Delta M_d$  and  $\Delta M_s$ . Gray points are excluded by constraints other than  $\Delta F = 2$ . Blue points are allowed by all constraints.

# $S_{\psi K_S}$ and $S_{\psi\phi}$



**Figure:** Predictions for the mixing induced CP asymmetries in  $B^0 \rightarrow J/\psi K_S$  and  $B_s \rightarrow J/\psi\phi$ , sensitive to the  $B^0$  and  $B_s$  mixing phases. Gray points are excluded by constraints other than  $\Delta F = 2$ . Blue points are allowed by all constraints.

## $e$ - $\mu$ universality



**Figure:** Histogram showing distribution of predictions for two observables probing  $e$ - $\mu$  universality violation in  $Z$  couplings for all points passing  $\Delta F = 2$  constraints.

“excluded by flavour” is excluded by charged-current decays imposed as constraints.



# MFPC particle content

	$Q$	$\bar{u}$	$\bar{d}$	$L$	$\bar{\nu}$	$\bar{e}$	$\mathcal{F}_{\downarrow}$	$\bar{\mathcal{F}}_{\uparrow}$	$\bar{\mathcal{F}}_{\downarrow}$	$\mathcal{S}_q$	$\mathcal{S}_l$
$\text{Sp}(N)_{\text{TC}}$	<b>1</b>	<b>1</b>	<b>1</b>	<b>1</b>	<b>1</b>	<b>1</b>	<b>N</b>	<b>N</b>	<b>N</b>	<b>N</b>	<b>N</b>
$\text{SU}(3)_{\text{C}}$	<b>3</b>	$\bar{\mathbf{3}}$	$\bar{\mathbf{3}}$	<b>1</b>	<b>1</b>	<b>1</b>	<b>1</b>	<b>1</b>	<b>1</b>	$\bar{\mathbf{3}}$	<b>1</b>
$\text{SU}(2)_{\text{L}}$	<b>2</b>	<b>1</b>	<b>1</b>	<b>2</b>	<b>1</b>	<b>1</b>	<b>2</b>	<b>1</b>	<b>1</b>	<b>1</b>	<b>1</b>
$\text{U}(1)_{\text{Y}}$	$\frac{1}{6}$	$-\frac{2}{3}$	$\frac{1}{3}$	$-\frac{1}{2}$	0	1	0	$-\frac{1}{2}$	$\frac{1}{2}$	$-\frac{1}{6}$	$\frac{1}{2}$
$N_{\text{g}}$	3	3	3	3	3	3	1	1	1	3	3

**Table:** Quantum numbers of SM fields, TC fermions, and TC scalars in MFPC. The last line gives the number of generations  $N_{\text{g}}$ . All fermion fields are left-handed Weyl spinors.

## $b \rightarrow s \mu\mu$ analysis

Global fits to data using open source code `flavio`,  
including the following observables:

Straub et al. [[flav-io.github.io](https://github.com/flav-io/flavio)]

- ▶  $B^0 \rightarrow K^{*0} \mu^+ \mu^-$  angular observables

CDF [[public note 10894](#)], LHCb [[arXiv:1512.04442](#)],

ATLAS [[CONF-2017-023](#)], CMS [[arxiv:1507.08126](#)], PAS-BPH-15-008]

- ▶  $B_s \rightarrow \phi \mu^+ \mu^-$  angular observables

LHCb [[arXiv:1506.08777](#)]

- ▶  $\mathcal{B}(B^{0,\pm} \rightarrow K^{*0,\pm} \mu^+ \mu^-)$

LHCb [[arXiv:1403.8044](#), [arXiv:1606.04731](#)],

CMS [[arXiv:1507.08126](#)], CDF [[public note 10894](#)]

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LHCb [[arXiv:1506.08777](#)], CDF [[public note 10894](#)]

- ▶  $\mathcal{B}(B \rightarrow X_s \mu^+ \mu^-)$

BaBar [[arXiv:1312.5364](#)]

## $b \rightarrow s \mu\mu$ analysis

Not included:

- ▶ lepton-averaged observables:  
focus on new physics in  $b \rightarrow s \mu^+ \mu^-$
- ▶  $B \rightarrow K \mu^+ \mu^-$  angular observables:  
only relevant in presence of scalar or tensor operators  
Beaujean, Bobeth, Jahn, [arXiv:1508.01526]
- ▶  $B \rightarrow K^* \mu^+ \mu^-$  angular observables by Belle:  
unknown mixture of  $B^0$  and  $B^\pm$   
Belle [arXiv:1612.05014]
- ▶  $\Lambda_b \rightarrow \Lambda \mu^+ \mu^-$  by LHCb: large experimental uncertainties,  
central values not compatible with viable short-distance hypothesis  
LHCb [arXiv:1503.07138],  
Meinel, van Dyk [arXiv:1603.02974]

## $b \rightarrow s \mu\mu$ analysis

Coeff.	standard uncert.		$2 \times \text{FF}$ uncert.		$2 \times \text{non-FF}$ uncert.	
	best fit	pull	best fit	pull	best fit	pull
$C_9^{\text{NP}}$	-1.21	<b><math>5.2\sigma</math></b>	-1.13	<b><math>4.0\sigma</math></b>	-1.30	<b><math>4.4\sigma</math></b>
$C_{10}^{\text{NP}}$	+0.79	<b><math>3.4\sigma</math></b>	+0.57	$1.9\sigma$	+0.74	<b><math>2.9\sigma</math></b>
$C_9^{\text{NP}} = -C_{10}^{\text{NP}}$	-0.67	<b><math>4.8\sigma</math></b>	-0.64	<b><math>3.4\sigma</math></b>	-0.64	<b><math>4.0\sigma</math></b>
$C_9^{\text{NP}} = C_{10}^{\text{NP}}$	-0.30	$1.3\sigma$	-0.46	$1.8\sigma$	-0.14	$0.5\sigma$
$C'_9$	+0.19	$0.9\sigma$	+0.31	$1.0\sigma$	+0.36	$1.5\sigma$
$C'_{10}$	-0.10	$0.6\sigma$	-0.10	$0.4\sigma$	-0.23	$1.2\sigma$
$C'_9 = -C'_{10}$	+0.08	$0.8\sigma$	+0.11	$0.8\sigma$	+0.17	$1.4\sigma$
$C'_9 = C'_{10}$	+0.06	$0.3\sigma$	+0.11	$0.4\sigma$	-0.03	$0.1\sigma$