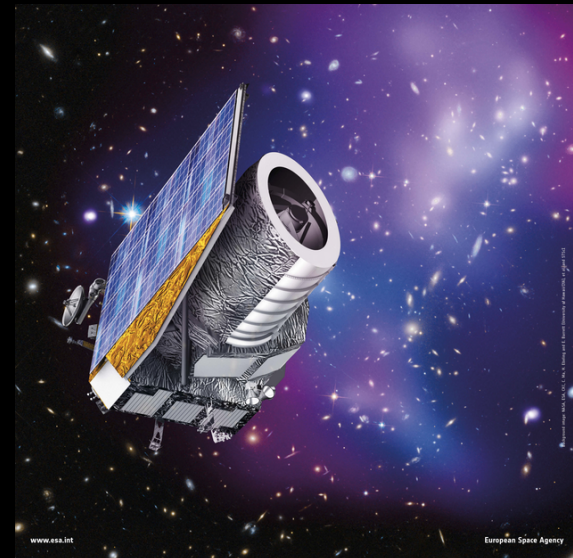


LSST-DESC Calibration Workshop '18

Slitless spectro-photometry

Disclaimer

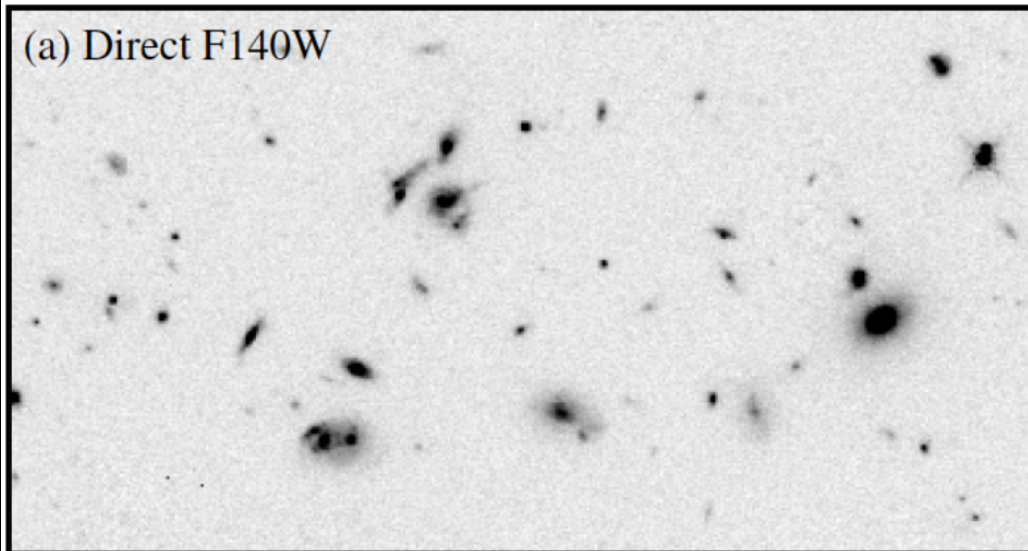
- 1st time around, hi!
- No specific info. on AuxTel spectrograph properties nor observing modes
- Experience in ground-based *integral field* spectro-photometry (SNfactory/SNIFS) and space-born slitless spectrography (Euclid/NISP-S)



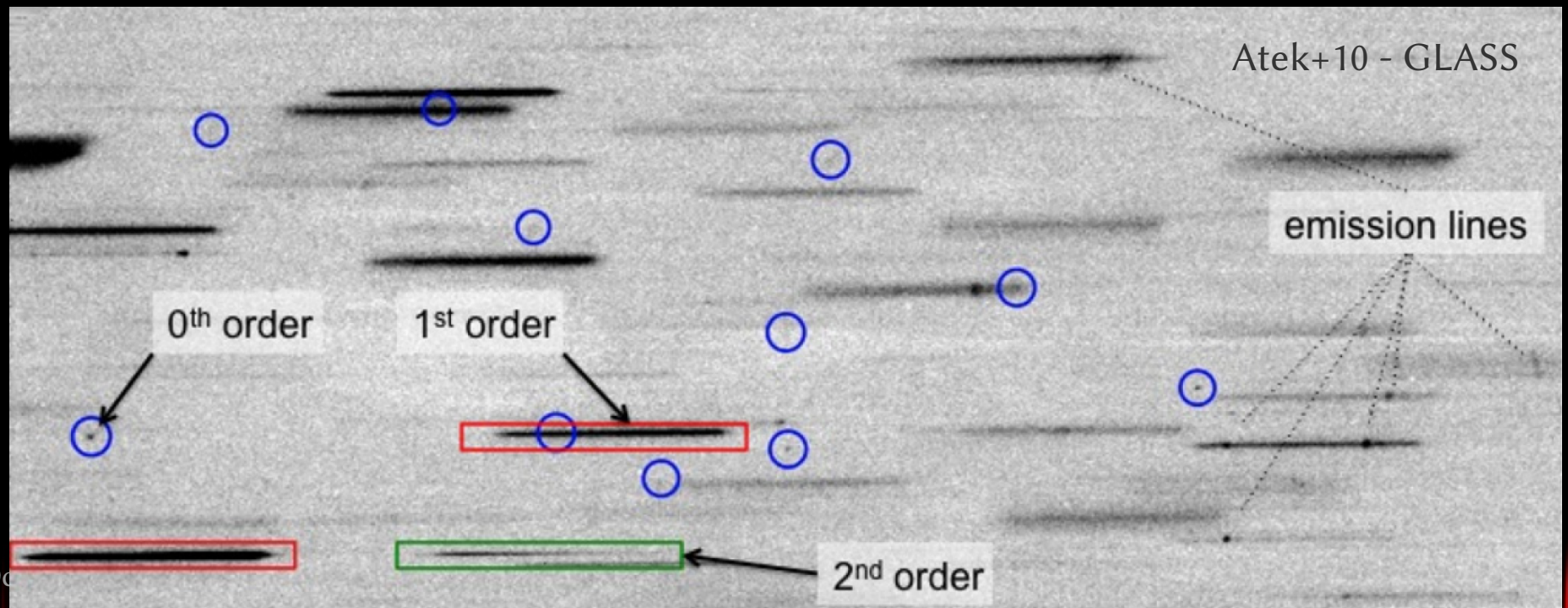
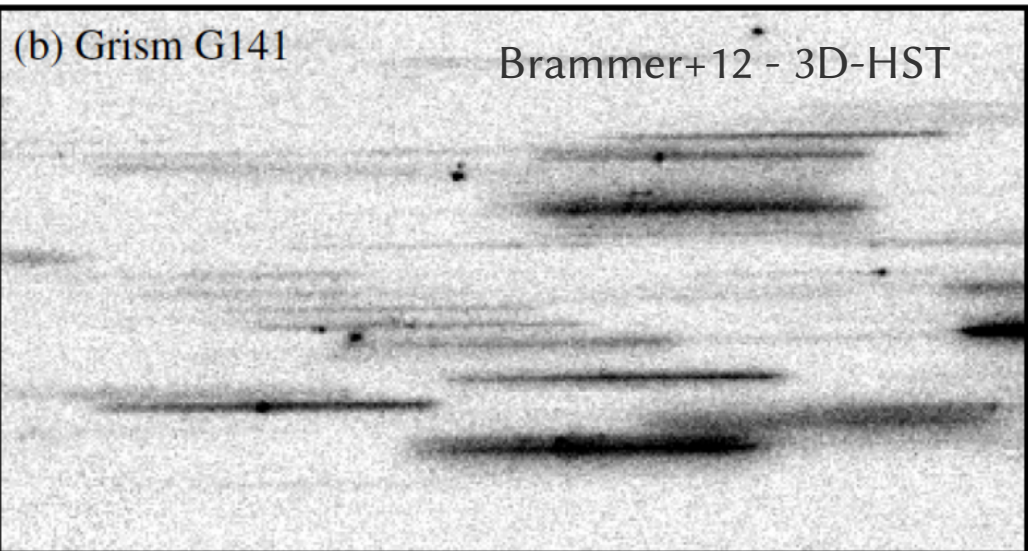
Modeling slitless spectroscopy

Slitless spectroscopy

(a) Direct F140W



(b) Grism G141



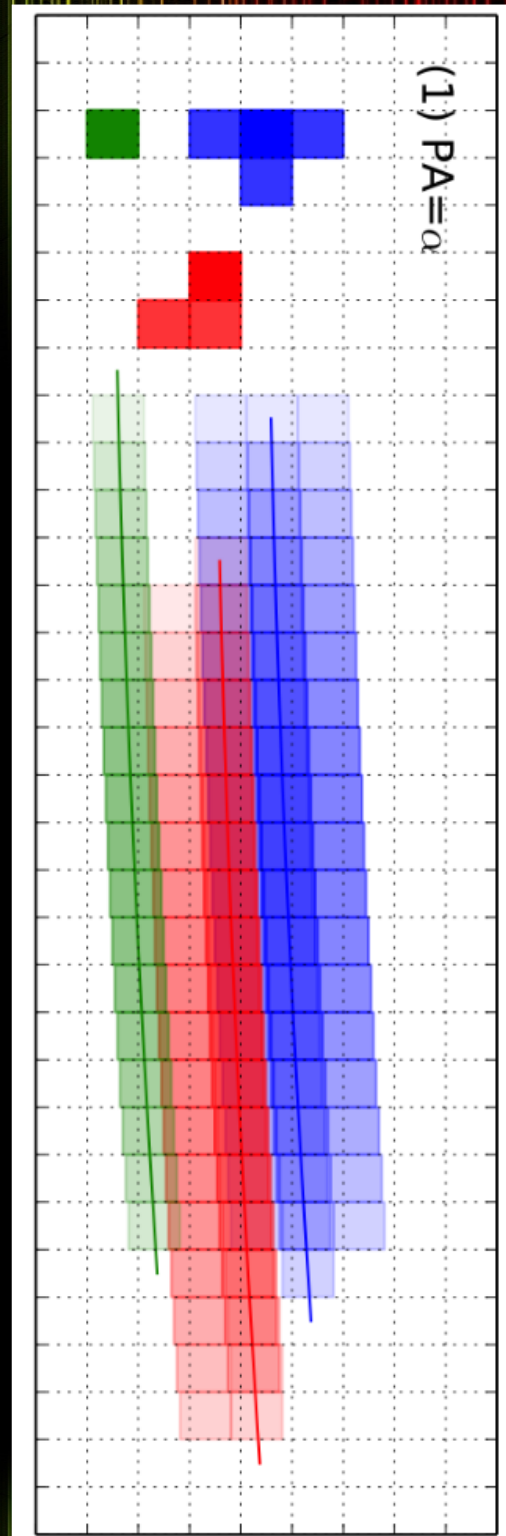
Slitless spectroscopy

- Advantages

- ◆ Large FoV and high multiplexing
- ◆ Simple to build and to use

- Drawbacks

- ◆ Cross-contamination: overlap of different objects (potentially at different orders)
 - ▶ Mitigation: multi-PA observations & decont. model
- ◆ Self-contamination: mixing of spatial and spectral information
 - ▶ Spectral resolution is dependent of source size/seeing conditions
- ◆ High background level



Traditional approach

- Standard “aXe-like” (Kümmel+09)
 - ◆ Empirical modeling of the spectral trace
 - ▶ Cross-dispersion: geometric distortions
 - ▶ Along dispersion: wavelength solution
 - ◆ Decontamination from neighbor sources
 - ◆ Cross-dispersion integration → 1D spectrum
 - ▶ Potentially x-disp. profile weighted (“optimal extraction”)
 - ◆ Multi-PA spectra are averaged *a posteriori*
 - ▶ But see LINEAR (Ryan+18) for 1st steps toward a forward model
- No handling of self-confusion
 - ◆ Spectral resolution is degenerate with source size (extent/PSF/seeing)
 - ◆ Correct for point sources observed in space, suboptimal otherwise

Intrinsic & observable flux

- Source is characterized by intrinsic flux distribution $C(\mathbf{r}, \lambda)$
 - ◆ E.g. a star: $C(\mathbf{r}, \lambda) = S(\lambda) \times \delta(\mathbf{r} - \mathbf{r}_0)$
 - ◆ Separable source: $C(\mathbf{r}, \lambda) = S(\lambda) \times F(\mathbf{r})$
- Atmosphere + Instrument is characterized by *Impulse Response Function* (supposed stationary)
 - ◆ mapping from intrinsic coords to obs. coords (astrometry, λ -calib)
 - ◆ spread around mean position
 - ◆ may include transmission
- *Observable flux* $O(\mathbf{r}, \lambda) \equiv (C \otimes P)(\mathbf{r}, \lambda)$
 - ◆ Only if you have an Integral Field Spectrograph!

Direct imaging

- IRF can be decomposed in two components
 - ◆ a centered shape component P_0 (aka PSF/LSF)
 - ◆ an offset component P_Δ
 - ▶ usually ignored by *ad hoc* registration of the PSF
- Direct imaging (photometry)
 - ◆ $P_0 = \text{PSF}$, $P_\Delta \approx \delta(\mathbf{r})$
 - ▶ but chromatic aberrations & ADR correspond to a non-trivial P_Δ
 - ◆ Broadband image: $I(\mathbf{r}) = \int d\lambda O(\mathbf{r}, \lambda)$
 - ▶ $\approx (\bar{C} \otimes \bar{P}_0)(\mathbf{r})$ for a weakly chromatic separable source

Dispersed imaging

- Slitless spectroscopy

- ◆ P_0 = Point/Line Spread Function

- ◆ $P_{\Delta}(\mathbf{r}, \lambda) = \delta(\mathbf{r} - \Delta(\lambda))$ where $\Delta(\lambda)$ is the dispersion law

- ◆ Dispersed image: $I(\mathbf{r}) = \int d\lambda (C \otimes P_0)(\mathbf{r} - \Delta(\lambda), \lambda)$

- ◆ In spatial Fourier domain:

$$\hat{I}(\mathbf{k}) = \int d\lambda \hat{C}(\mathbf{k}, \lambda) \hat{P}_0(\mathbf{k}, \lambda) e^{-i2\pi \mathbf{k} \cdot \Delta(\lambda)}$$

- ◆ Under the separability assumption and a weakly chromatic PSF

$$\hat{I}(\mathbf{k}) \approx \hat{F}(\mathbf{k}) \hat{\bar{P}}_0(\mathbf{k}) \int d\lambda S(\lambda) e^{-i2\pi \mathbf{k} \cdot \Delta(\lambda)}$$

- ▶ Almost the Fourier Transform of $S(\lambda)$!

Dispersed image modeling

- $\hat{I}(\mathbf{k}) = \int d\lambda \hat{C}(\mathbf{k}, \lambda) \hat{P}_0(\mathbf{k}, \lambda) e^{-i2\pi \mathbf{k} \cdot \Delta(\lambda)} \approx \hat{F}(\mathbf{k}) \hat{\bar{P}}_0(\mathbf{k}) \int d\lambda S(\lambda) e^{-i2\pi \mathbf{k} \cdot \Delta(\lambda)}$

I = dispersed image, $F \otimes \bar{P}_0 \approx$ broadband image

S = spectrum, Δ = dispersion law

- Different approaches

- ◆ Efficient simulation (for all dispersion orders)

- ◆ Backward extraction of $S(\lambda)$

- ▶ Assume dispersion law $\Delta(\lambda)$ and broadband image $F \otimes \bar{P}_0$

- ▶ Estimate $S(\lambda)$ from Wiener-Hunt deconvolution

- ◆ Forward model of dispersed image $I(\mathbf{r})$, e.g.

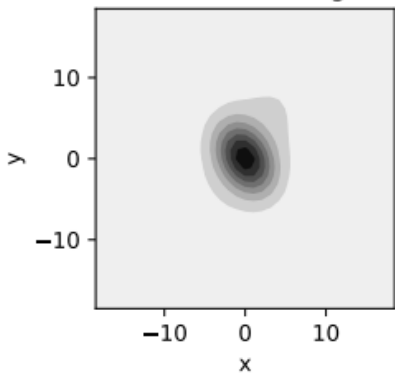
- ▶ Calibration of dispersion law $\Delta(\lambda)$, of transmission $T(\lambda)$

- ▶ Simple galaxy model: $S(\lambda) =$ template + redshift

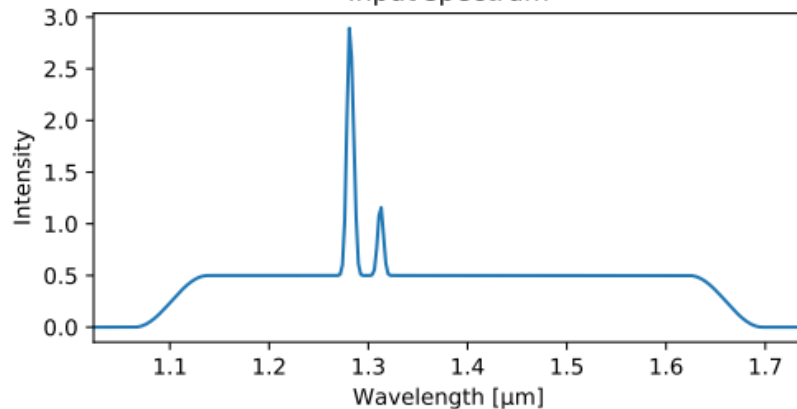
- ▶ More complex model, e.g. galaxy kinematics (Outini+18, in prep.)

WFC3/G141 (3D-HST) simulation

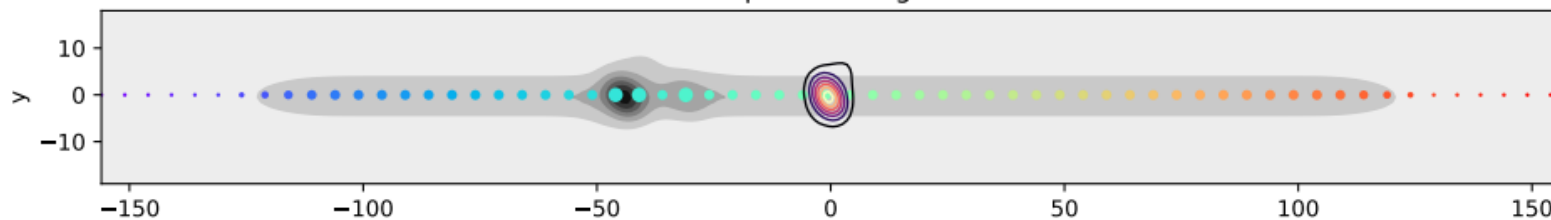
Broadband image



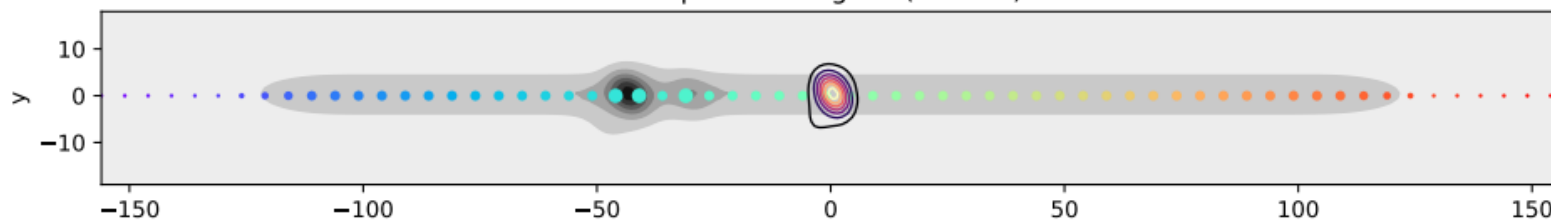
Input spectrum



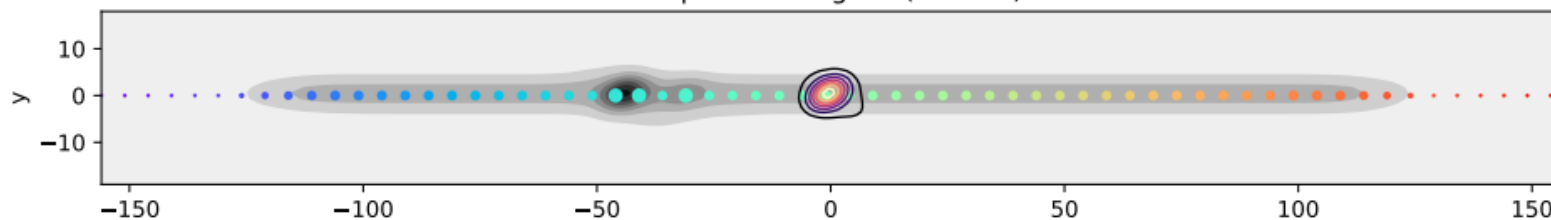
Dispersed image \rightarrow



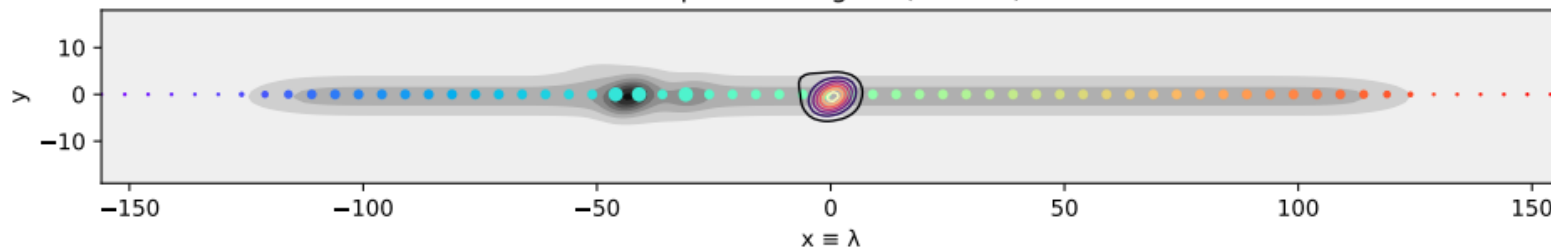
Dispersed image \leftarrow (rotated)



Dispersed image \uparrow (rotated)

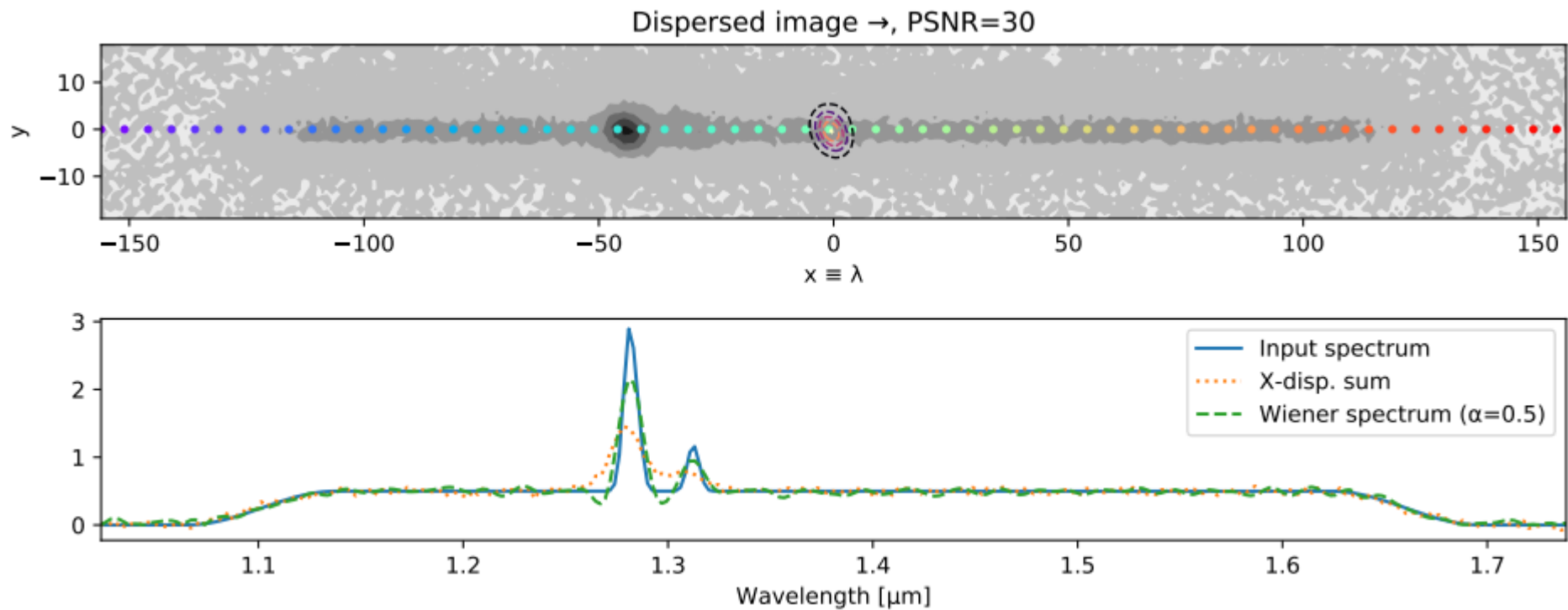


Dispersed image \downarrow (rotated)

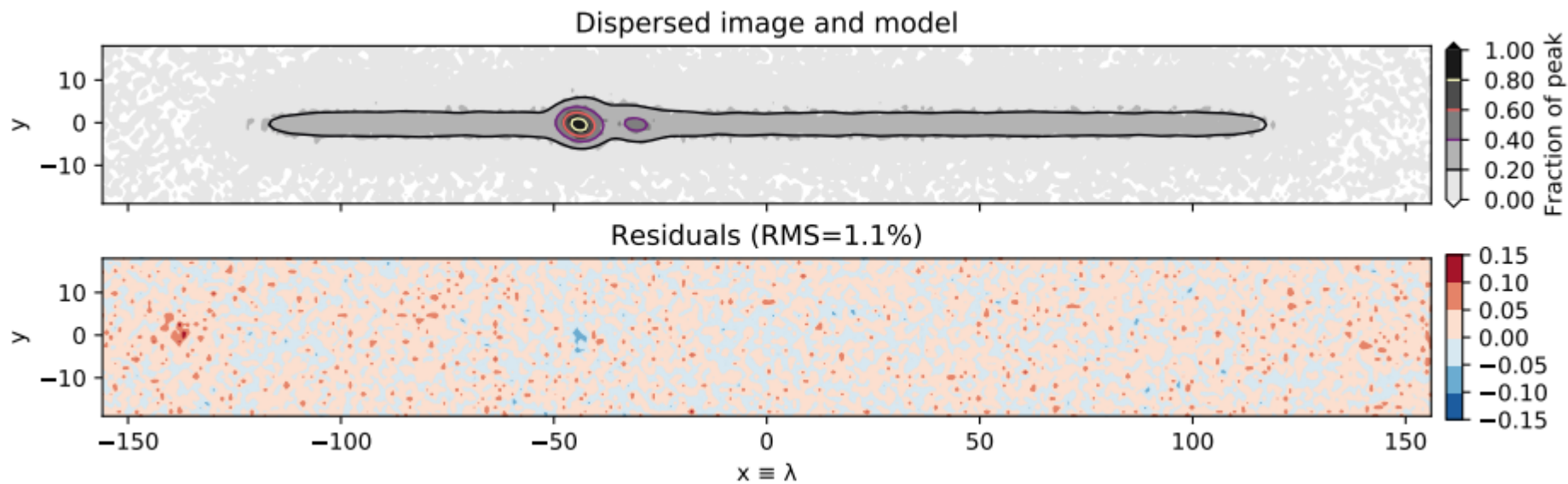


Copin 2018, in prep.

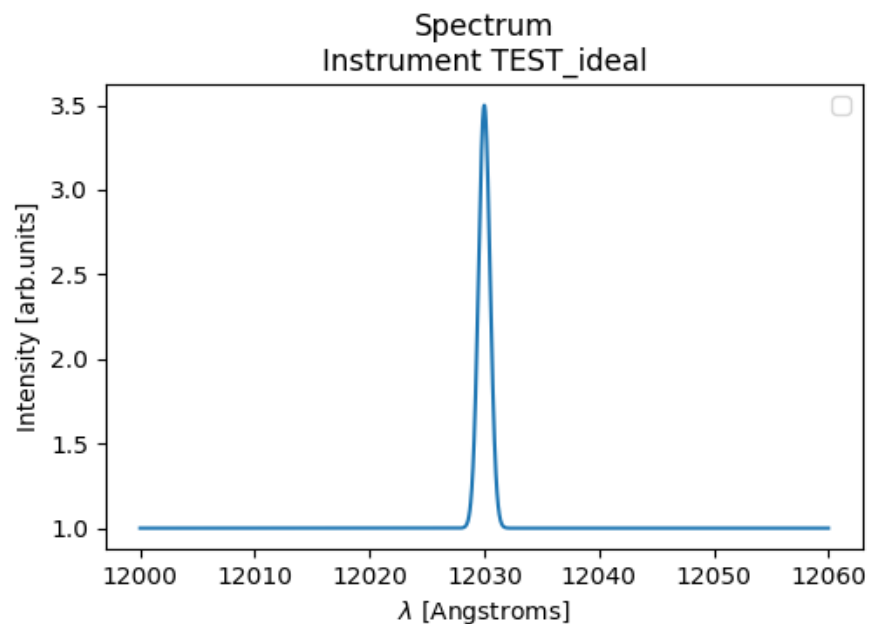
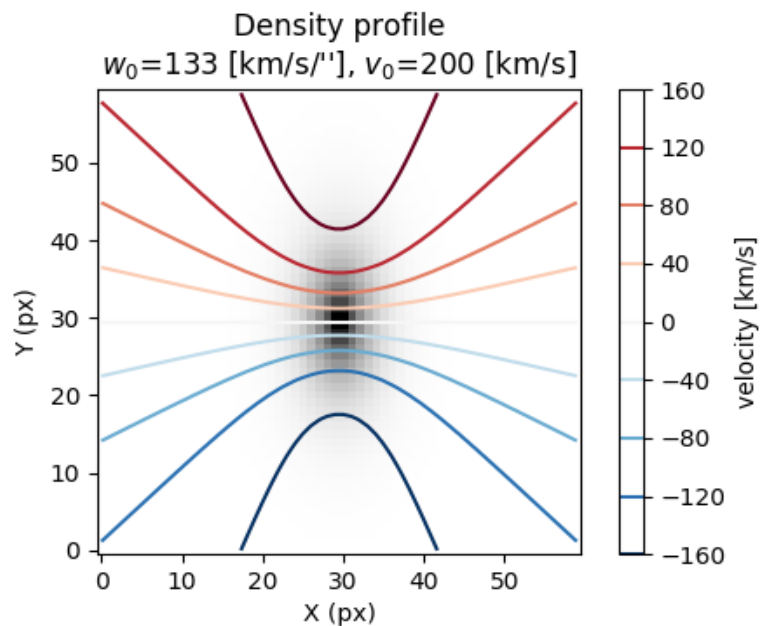
Oct. 2018



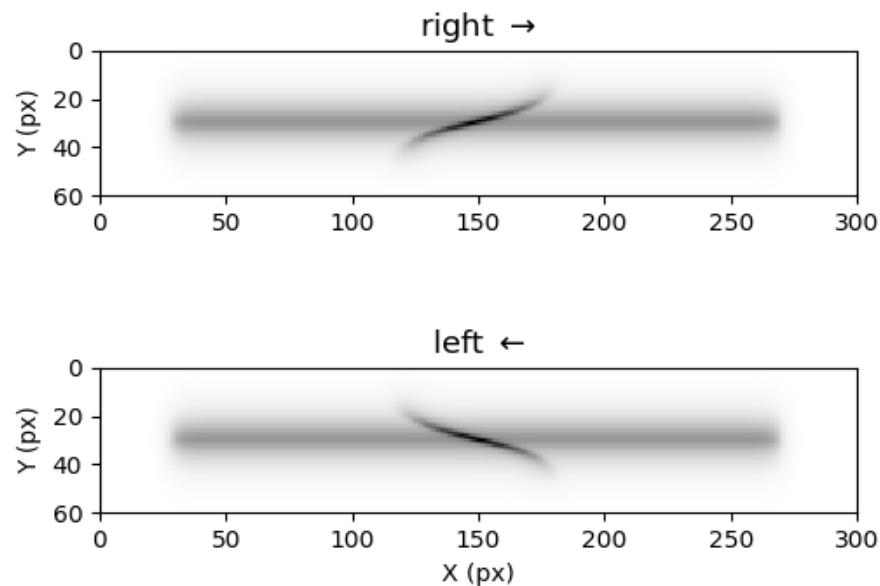
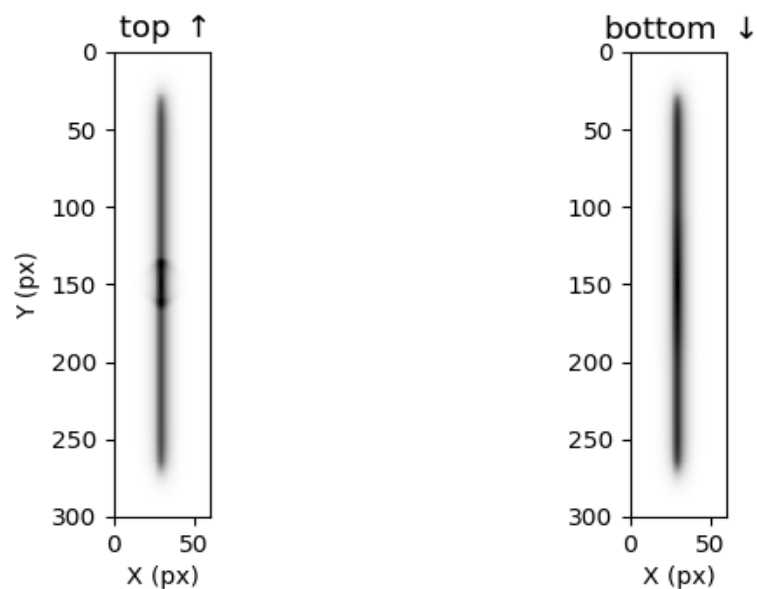
Copin 2018, in prep.



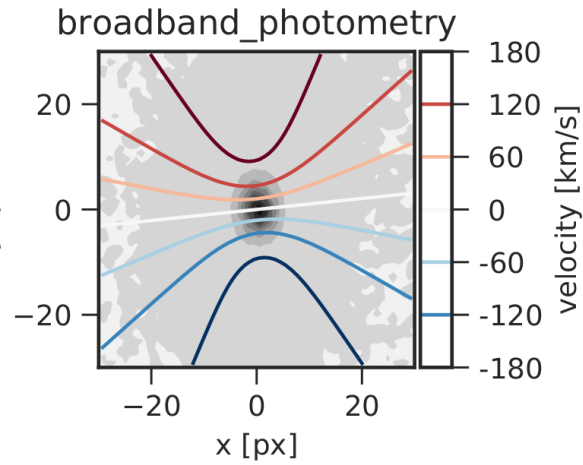
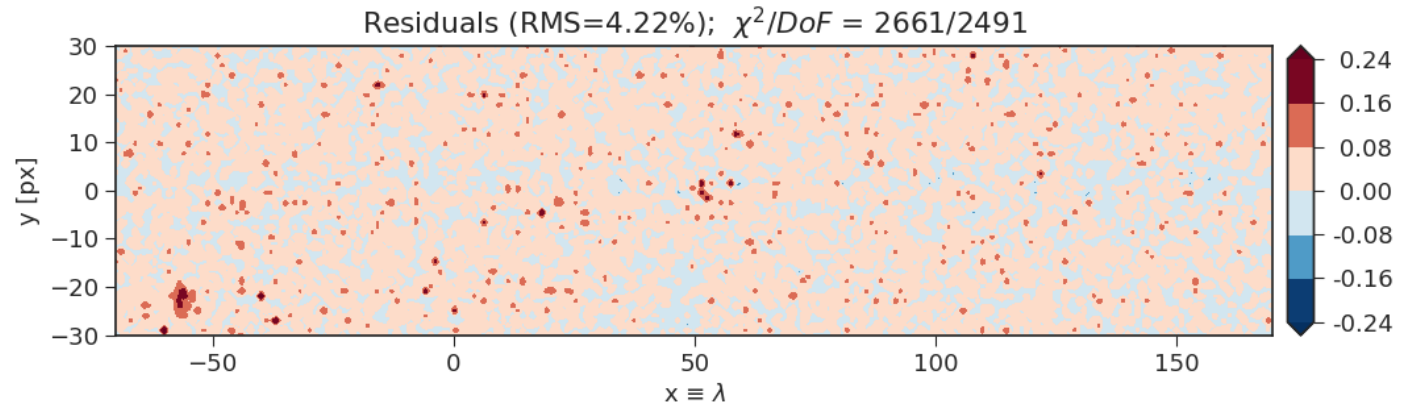
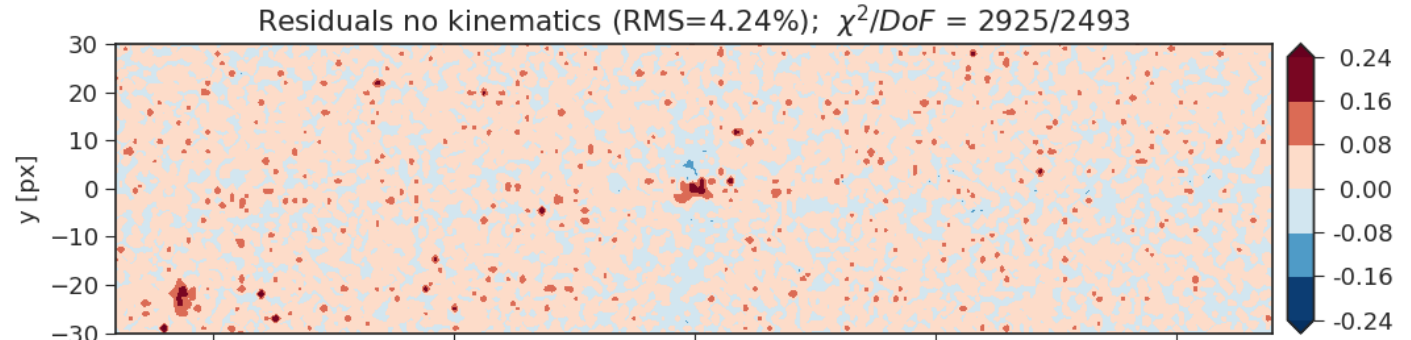
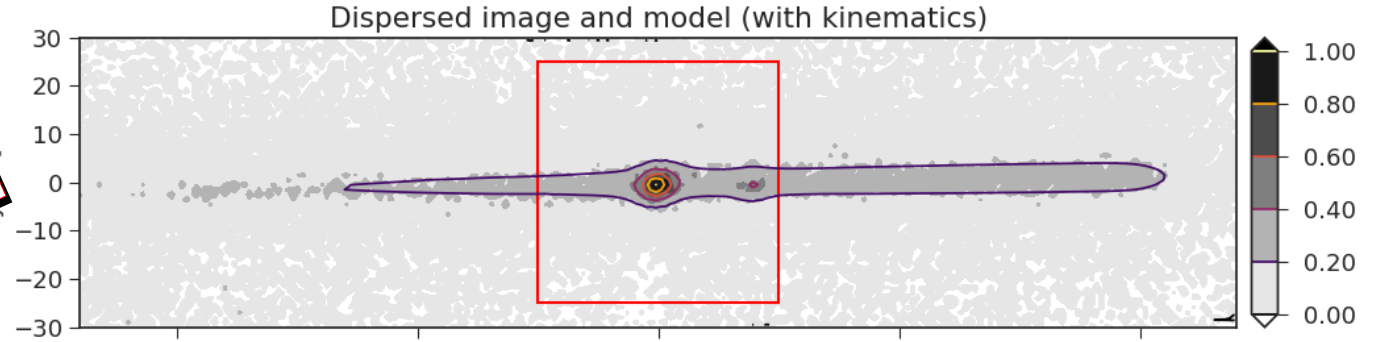
Galaxy $r=1.0''$, $i=60.0$ [deg], $PA=0.0$ [deg]
Instrument TEST_ideal [D=0.2 A/px]



emission line $H\alpha$: $\lambda_0=12030.0$ [Angstroms] $\rightarrow z=0.83$



PRELIMINARY



Cold disk, velocity curve: $v(r) = v_0 \tanh(w_0 r / v_0)$

$$v_0 \sin i = 205 \pm 24 \text{ km.s}^{-1}$$

$$w_0 \sin i = 232 \pm 25 \text{ km.s}^{-1}.\text{arcsec}^{-1}$$

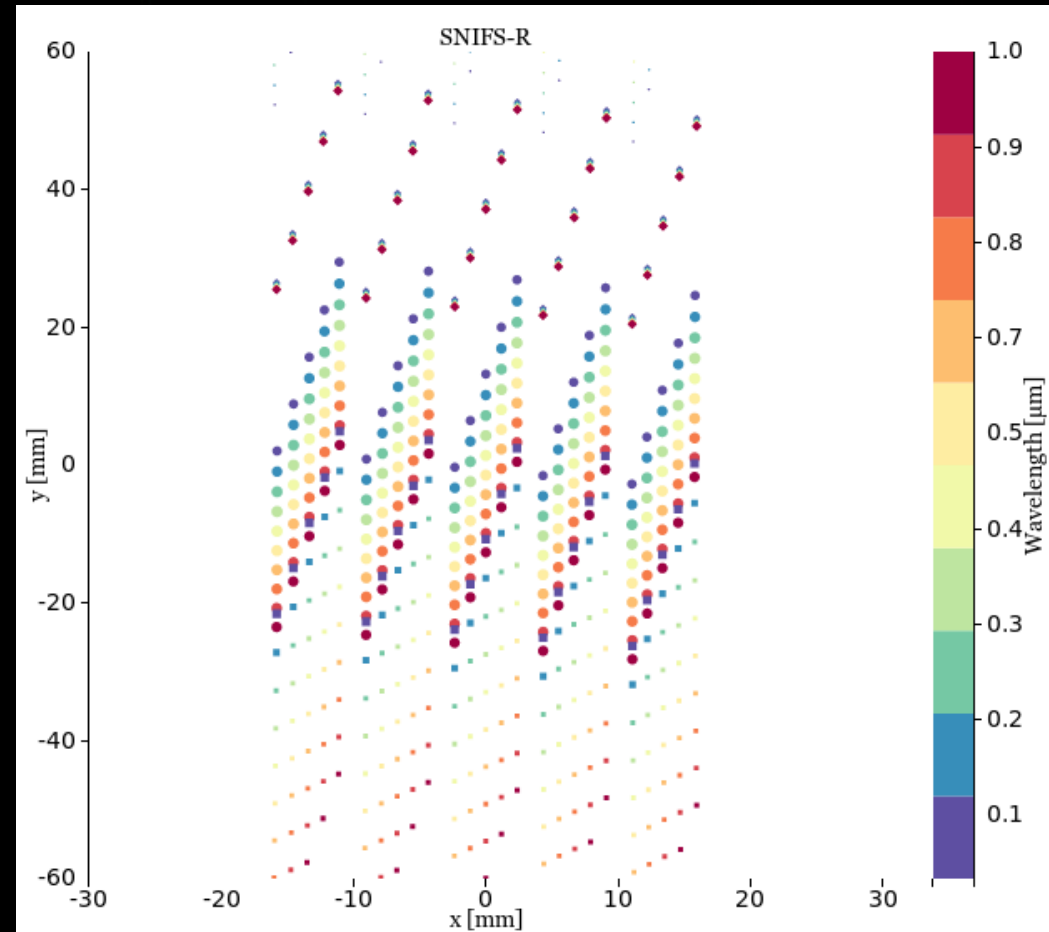
Dispersed imaging of stars

- Point sources are easier: $C(\mathbf{r}, \lambda) = \delta(\mathbf{r}) \times S(\lambda)$
 - ◆ $I(\mathbf{r}) = \text{TF}^{-1}(\int d\lambda \hat{P}_0(\mathbf{k}, \lambda) S(\lambda) e^{-i2\pi \mathbf{k} \cdot \Delta(\lambda)})$
 - ◆ Simultaneous fit of dispersed image $I(\mathbf{r})$
 - ▶ spectral trace: dispersion law $\Delta(\lambda)$
 - ▶ spectral shape: instrumental PSF and seeing P_0
 - ▶ flux: $S = T \times S^*$ where T = transmission, S^* = ref. flux
 - ◆ Spectro-photometry will derive from proper modeling of these different components
 - ▶ Dispersed imaging is *closer* to “imaging” than “spectroscopy”
 - ▶ Most tools are readily available from photometry

The (not so difficult?) path to slitless spectro-photometry

Instrumental model

- Dispersion law $\Delta(\lambda)$ as a function of position in FP
 - ◆ Effective geometrical model
- Instrumental PSF as a function of position in FP
 - ◆ Can be derived from 1st principles (WF propagation)
 - ◆ or adjusted empirically
 - ◆ More naturally expressed in Fourier domain



<http://spectrogrism.readthedocs.org>

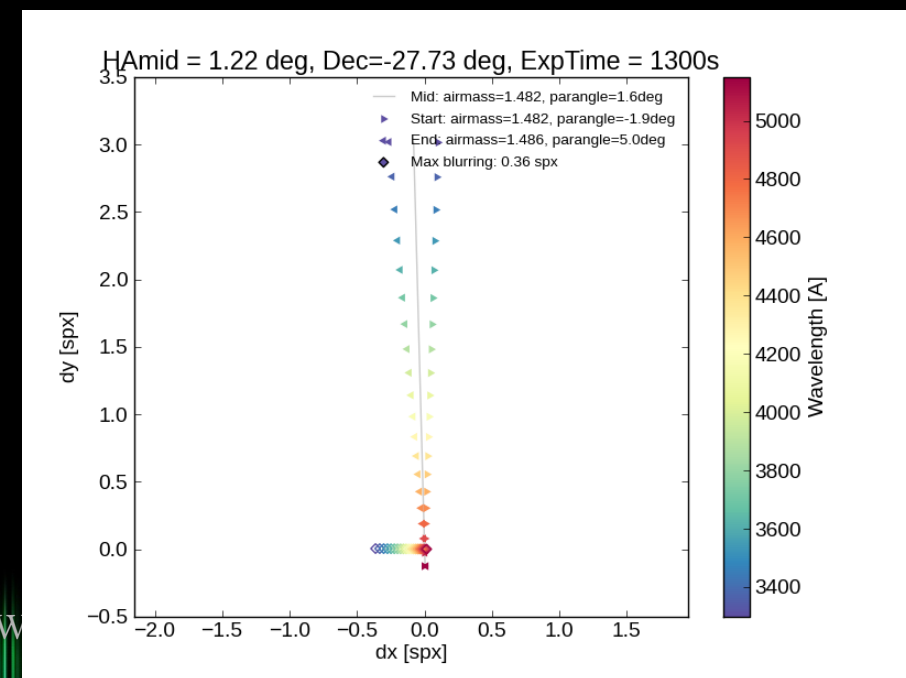
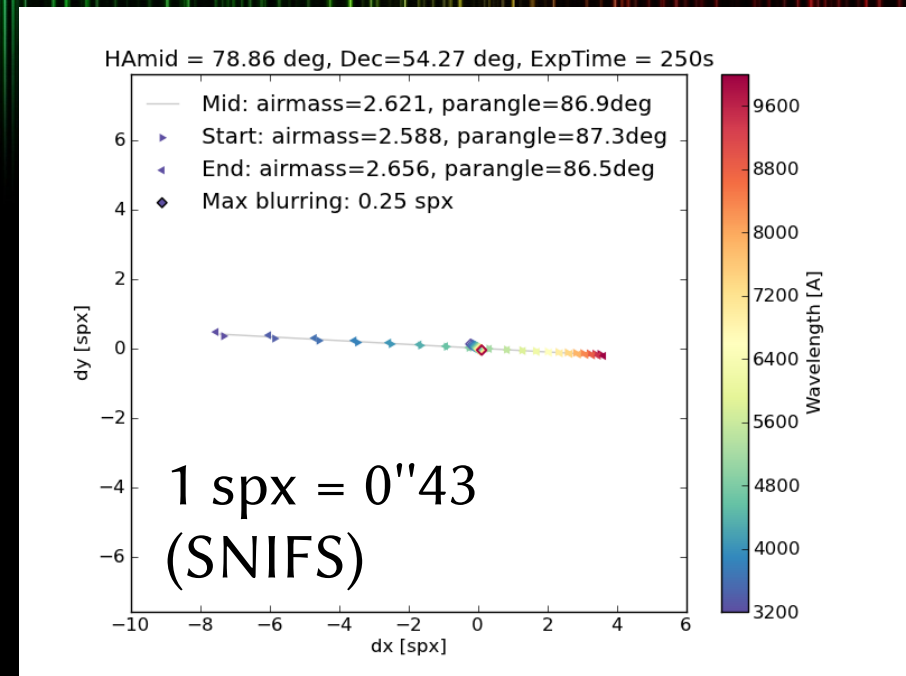
Atmospheric Differential Refraction

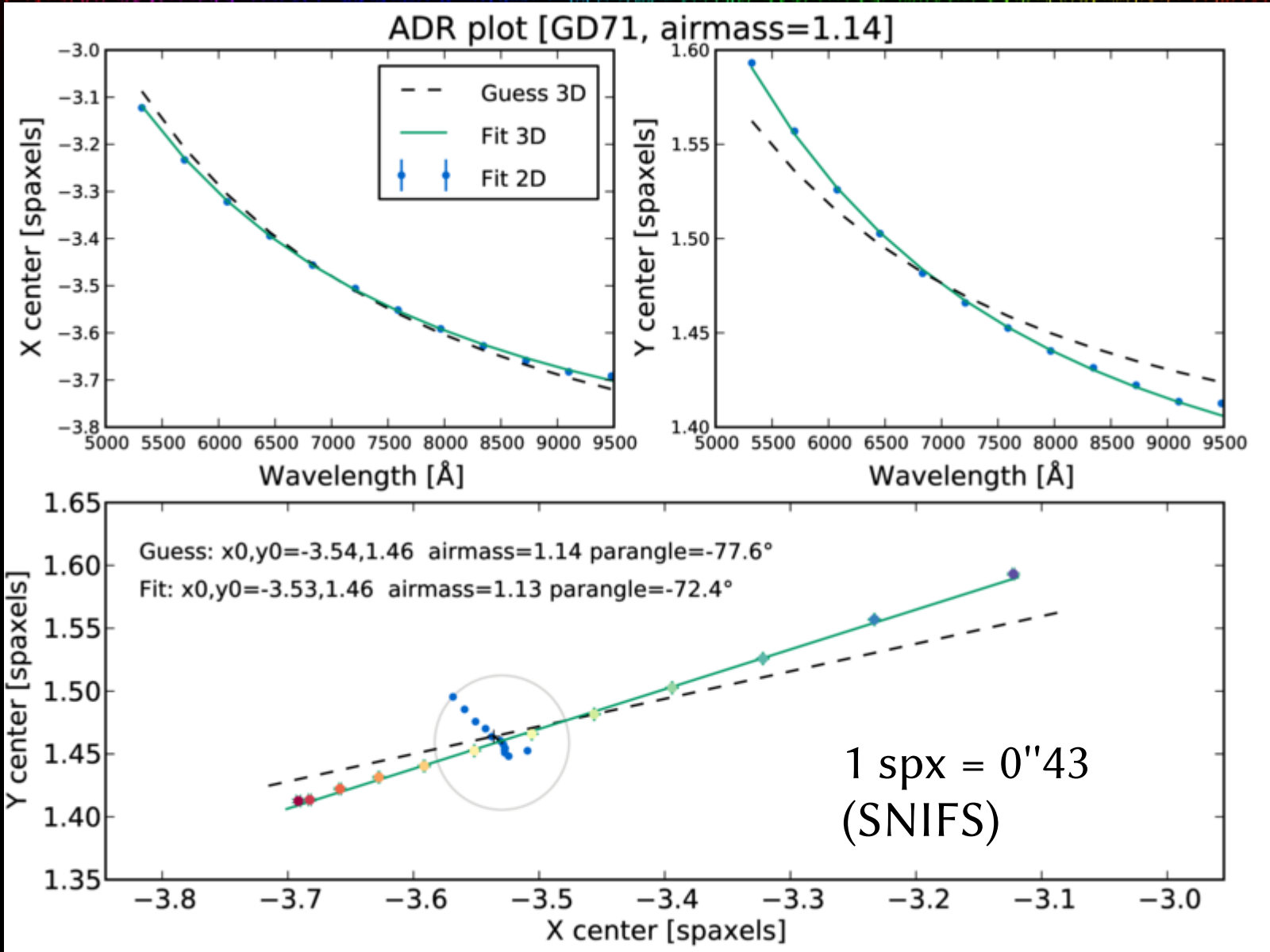
- Instantaneous ADR:

- ◆ distortion of spectral trace
- ◆ distortion of wave. solution
- ◆ $\Delta(\lambda) = \Delta_{\text{Disp}}(\lambda) + \Delta_{\text{ADR}}(\lambda)$

- Integrated ADR ($t_{\text{exp}} > 0$)

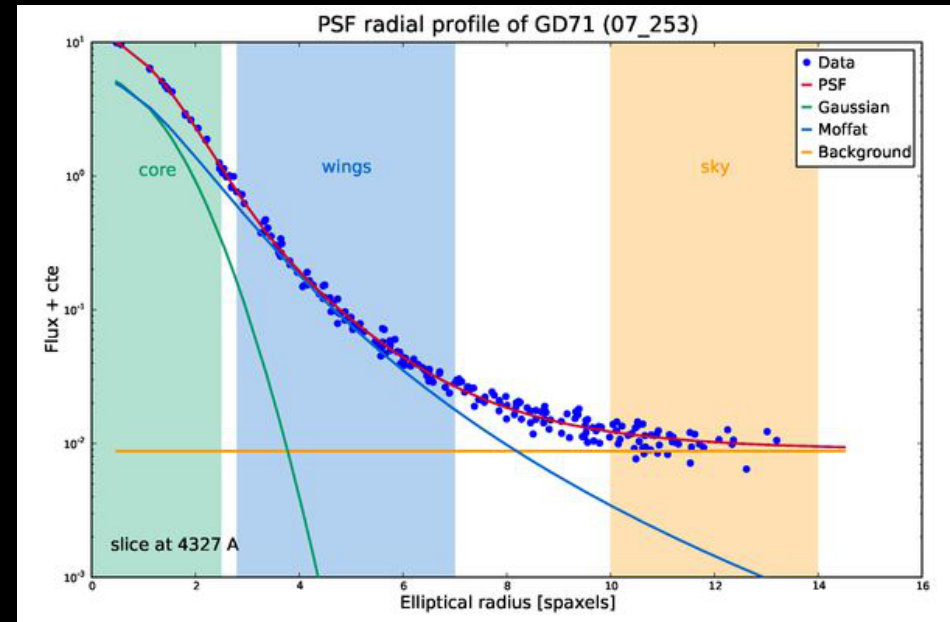
- ◆ widening of spectral trace
- ◆ spectral res. degradation
- ◆ flux-weighted time-average
- ◆ same formalism w/ $\Delta_{\text{ADR}}(\lambda, t)$





Seeing (atmospheric PSF)

- Historical SNIFS PSF (Buton09)
 - ◆ Gaussian for the core
 - ◆ Moffat for the wings
 - ◆ Correlated parameters
- Observed PSF has more wings than plain Kolmogorov profile
 - ◆ $n_{\text{eff}} \sim 4.5/3$ rather than $5/3$
 - ◆ Chrom. dependency is OK
- Current development (see also Xin+18):
 - ◆ Seeing: Kolmogorov/von Kármán profile
 - ◆ Instrument: eff. profile ($K \otimes G$)
 - ◆ Guiding: Gaussian



Atmospheric transmission

- You know better than me
 - ◆ Multi-component expansion
 - ◆ Constraints from external probes
- What is a photometric night? At which level? Over which time-scale?

Reference spectra

- Recalibration of the spectro-photometric standard stars (S^*)
 - ◆ Intrinsic consistency wrt/within Calspec: “standard star network”
 - ◆ Absolute flux/color calibration (e.g. StarDice, SCALA: Lombardo+17)
- Work in Progress in SNfactory
 - ◆ 14 years of repeated observations of 70 stars
 - ◆ spectro-photometry at mmag-scale

Conclusions

- Slitless spectro-photometry is within reach
- Good understanding of dispersed image
 - ◆ Self-confusion is properly handled for punctual sources
 - ◆ **Assuming proper cross-contamination**
 - ▶ flexibility in dispersion orientation and/or multi-PA observations
 - ▶ multi-order decontamination
- Appropriate models of the different components
 - ◆ spectral trace: dispersion law $\Delta(\lambda)$
 - ◆ spectral shape: instrumental PSF and seeing P_0
 - ◆ flux: $S = T \times S^*$ where T = transmission, S^* = ref. flux