

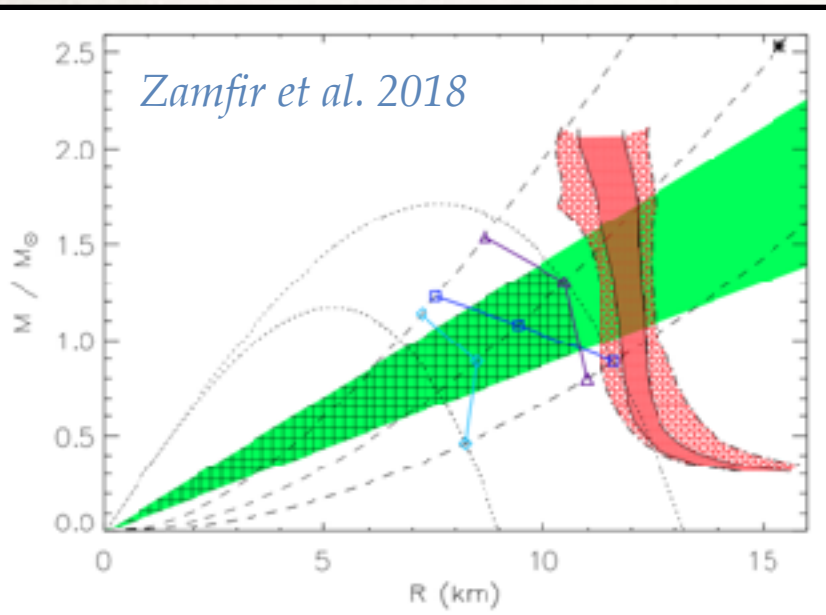
Dense Matter Equation of State constraints with Observations of Neutron Stars

Sebastien Guillot

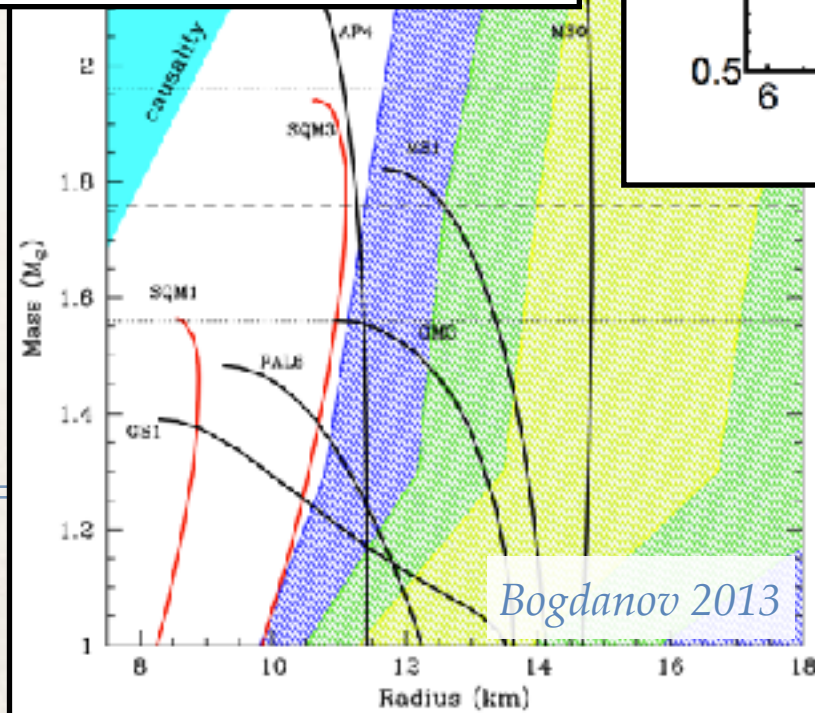
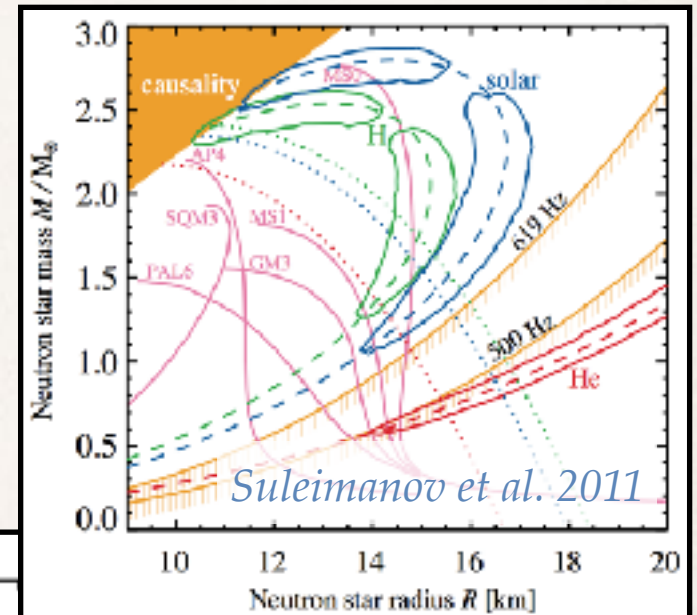
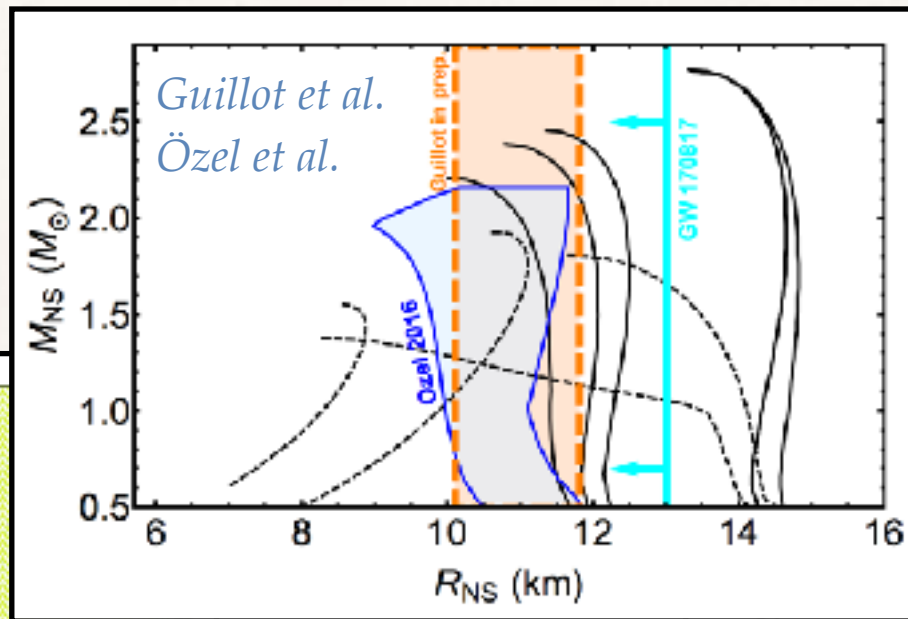


Post-doc CNES

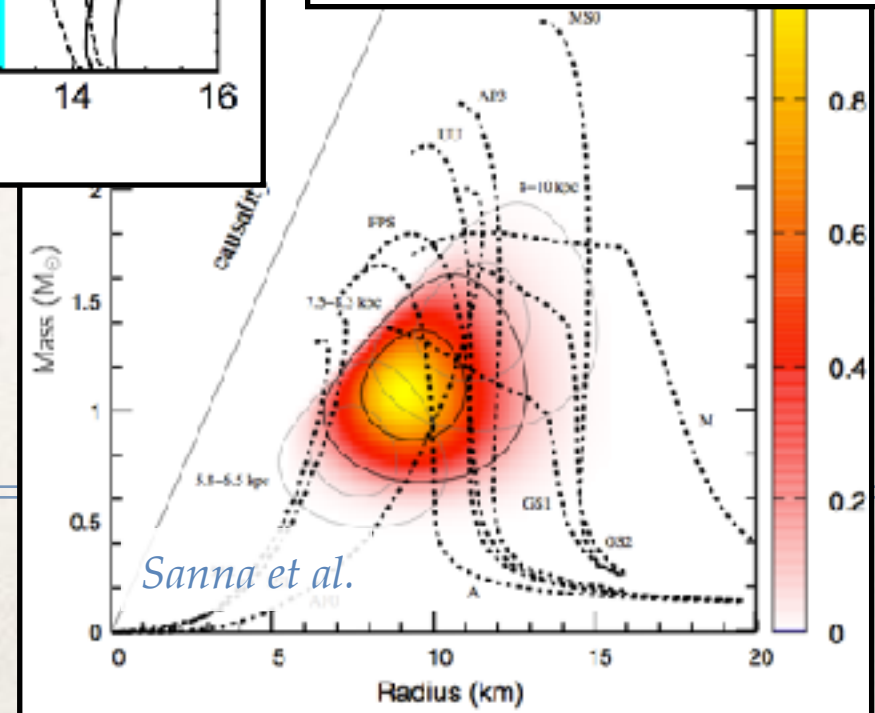
Zamfir et al. 2018



*Guillot et al.
Özel et al.*

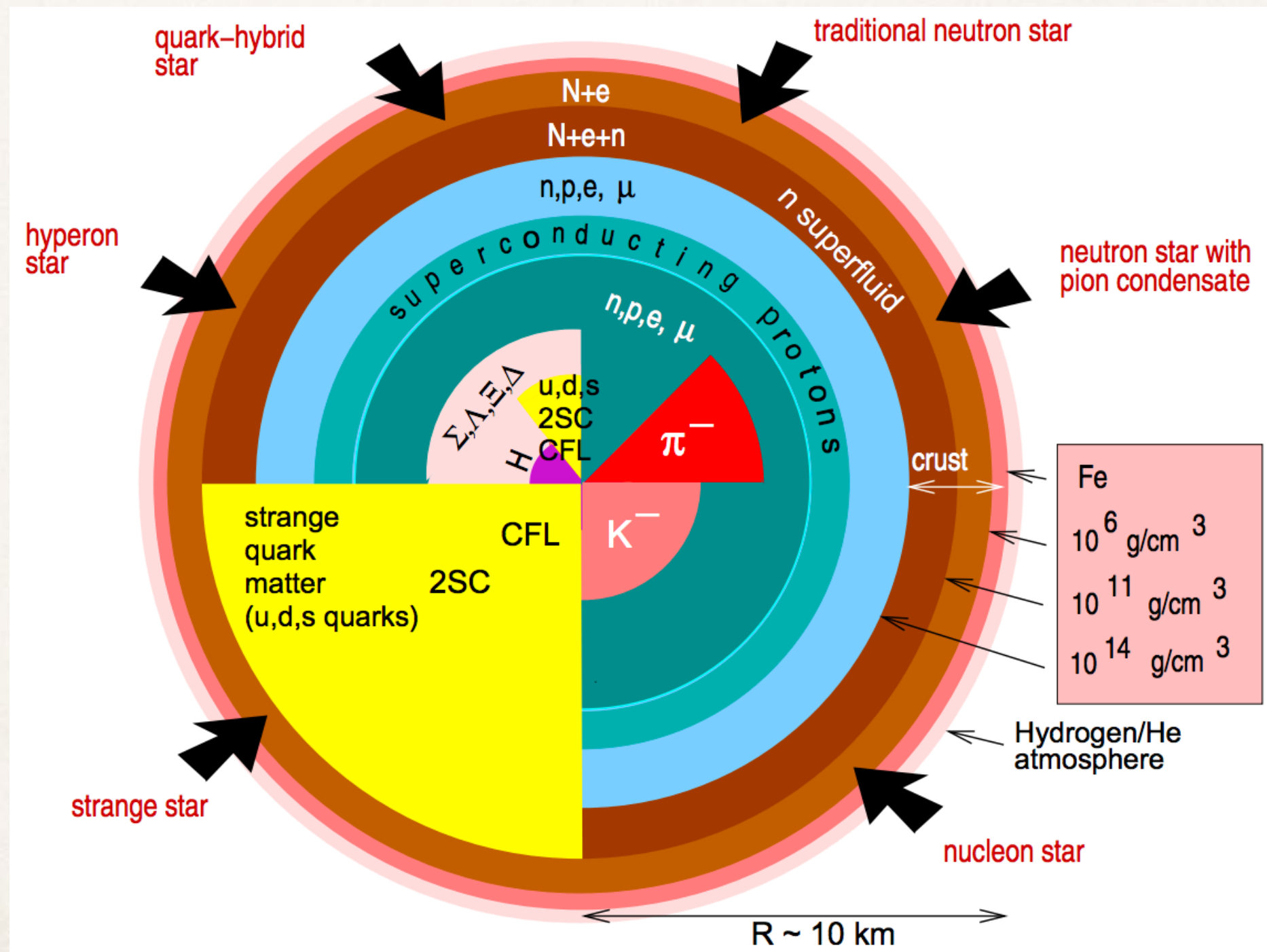


Bogdanov 2013

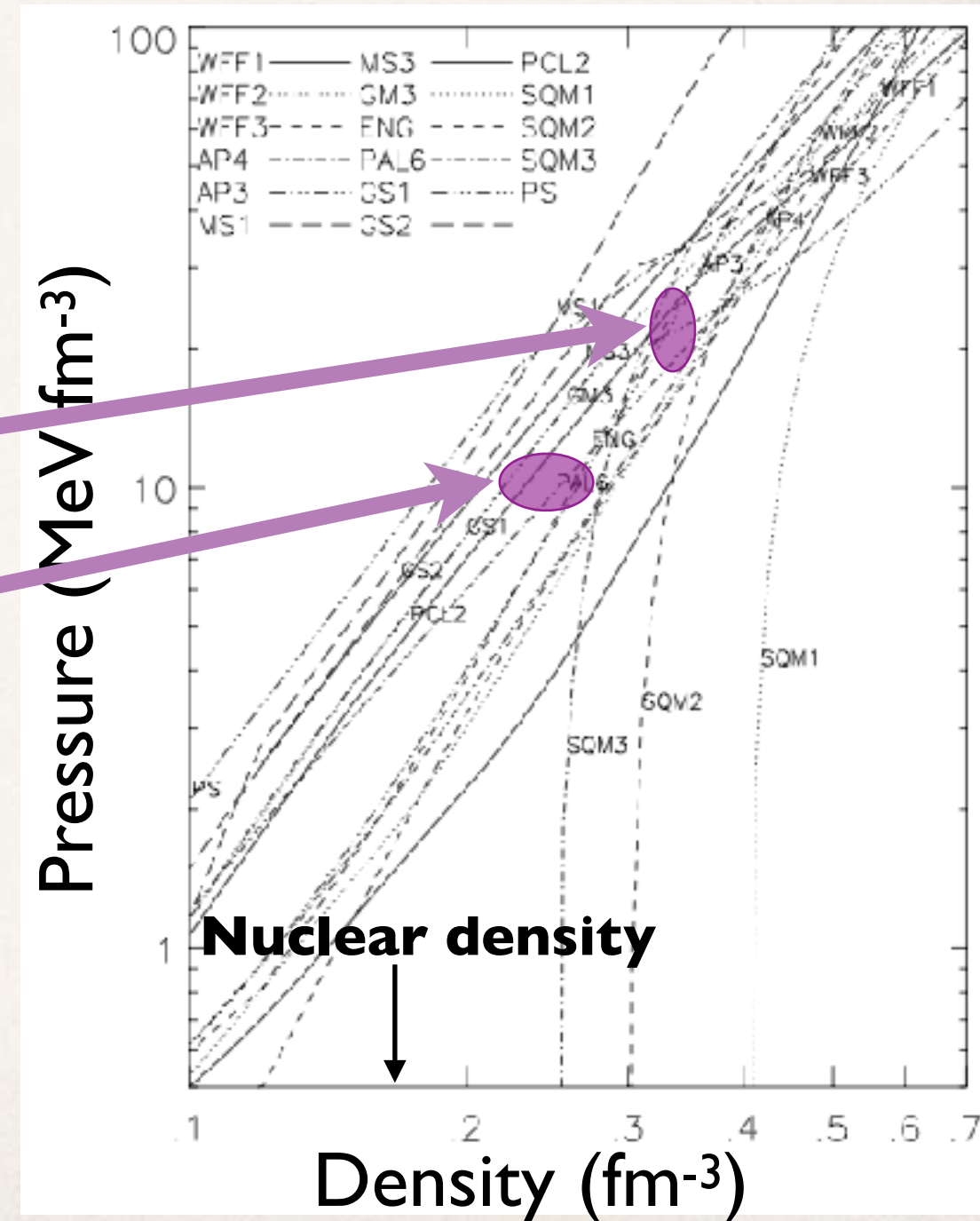
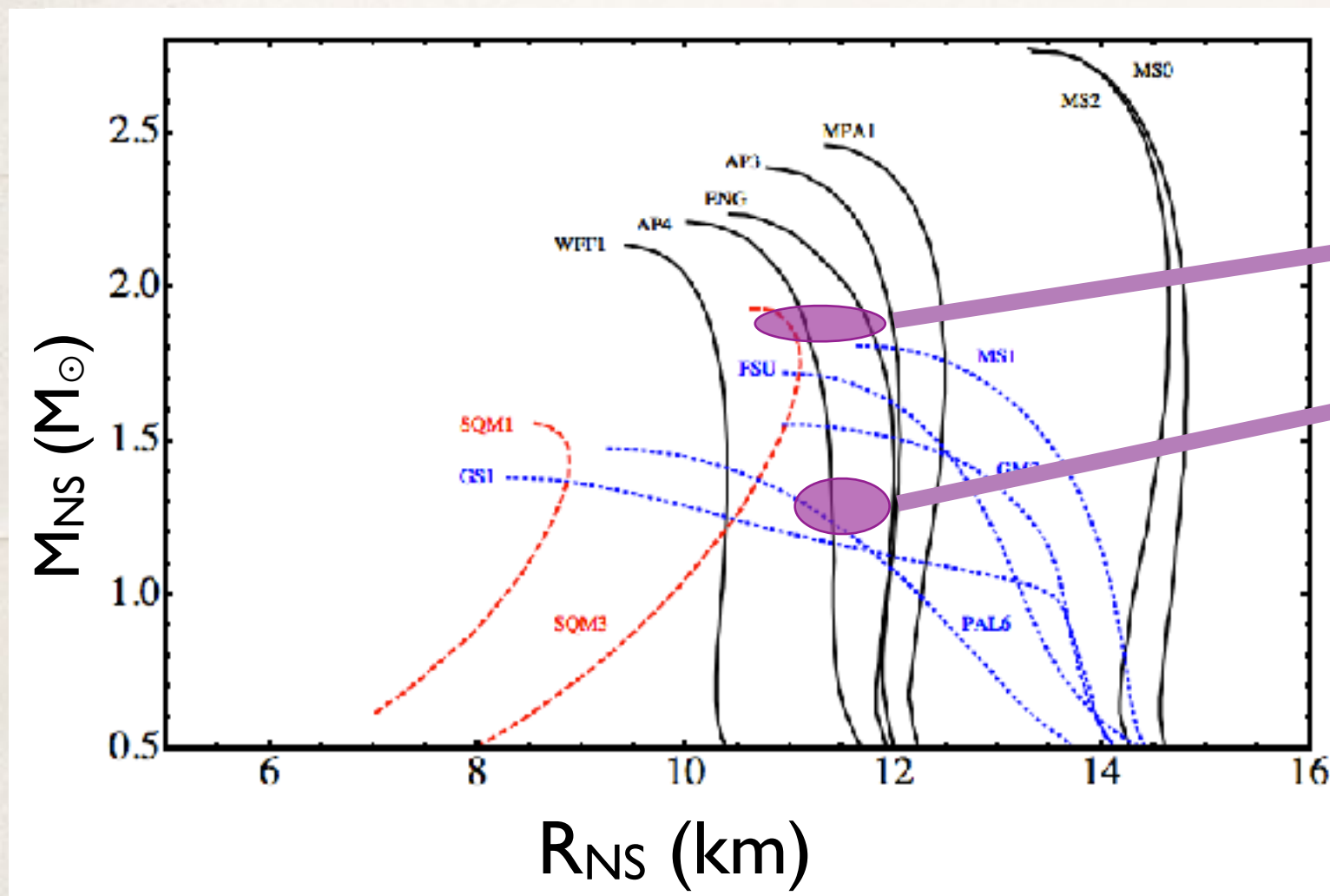


Sanna et al.

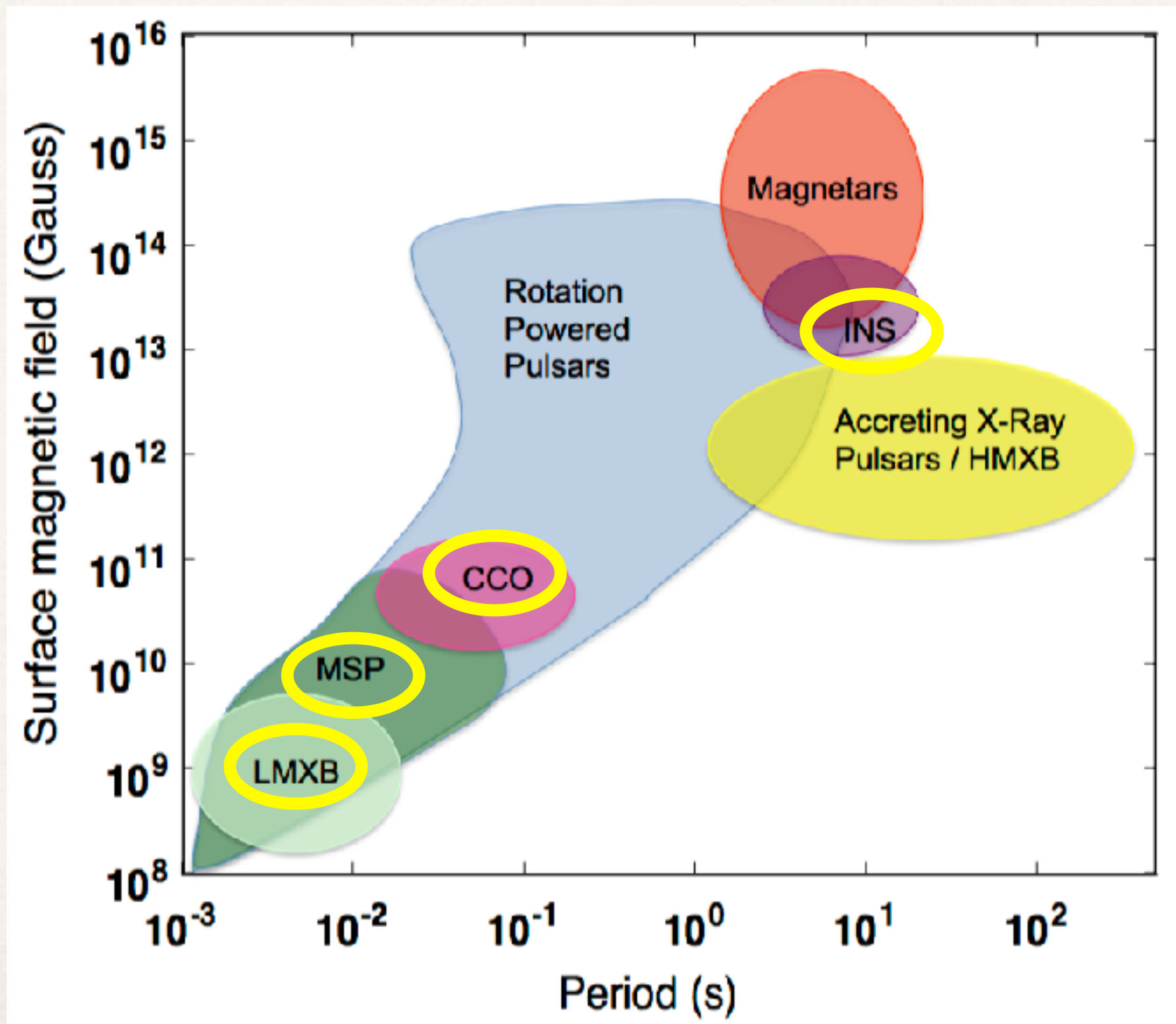
The internal structure of neutron stars is still unknown and many theories are proposed.



Dense nuclear matter is described by an equation of state $P(\rho)$. But what is it?

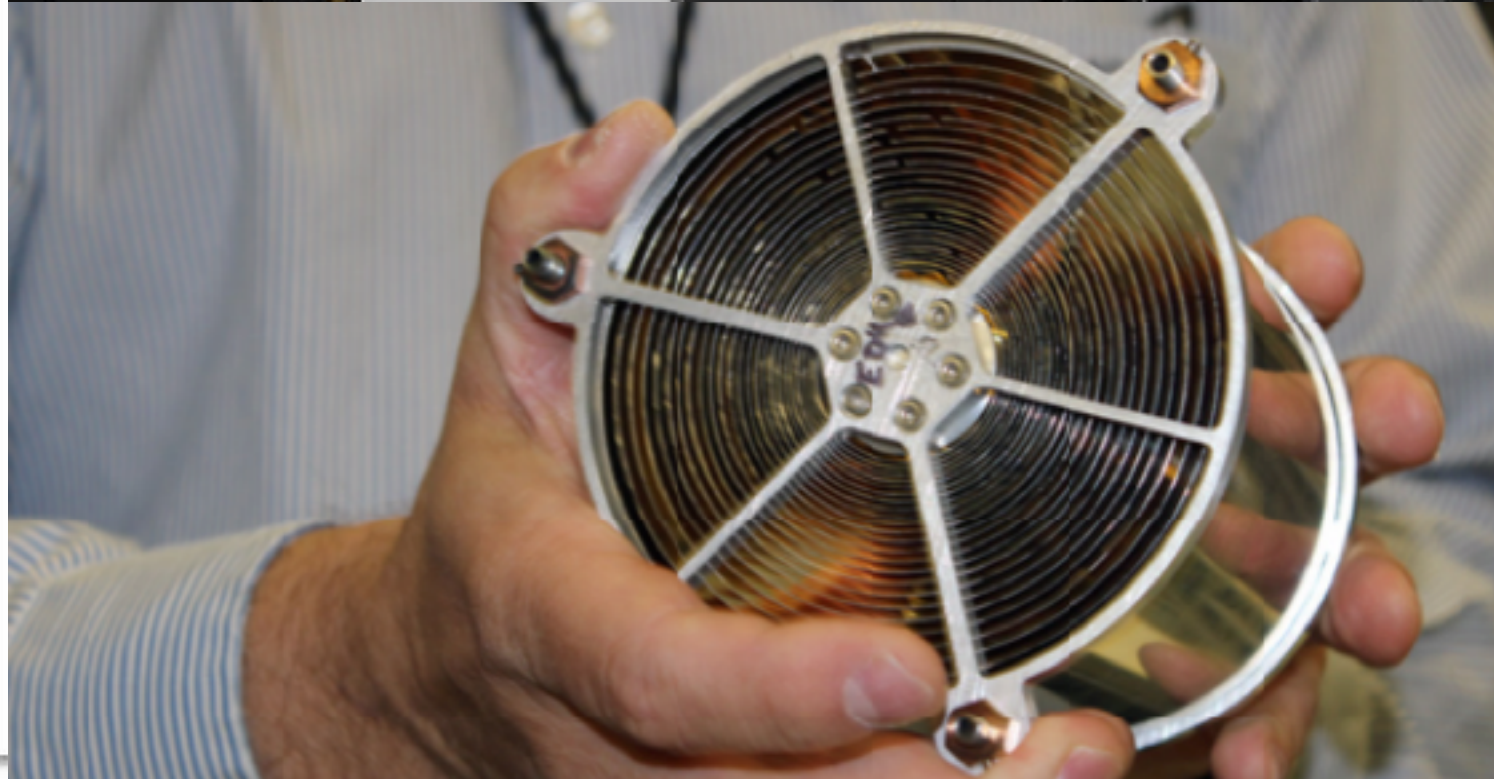
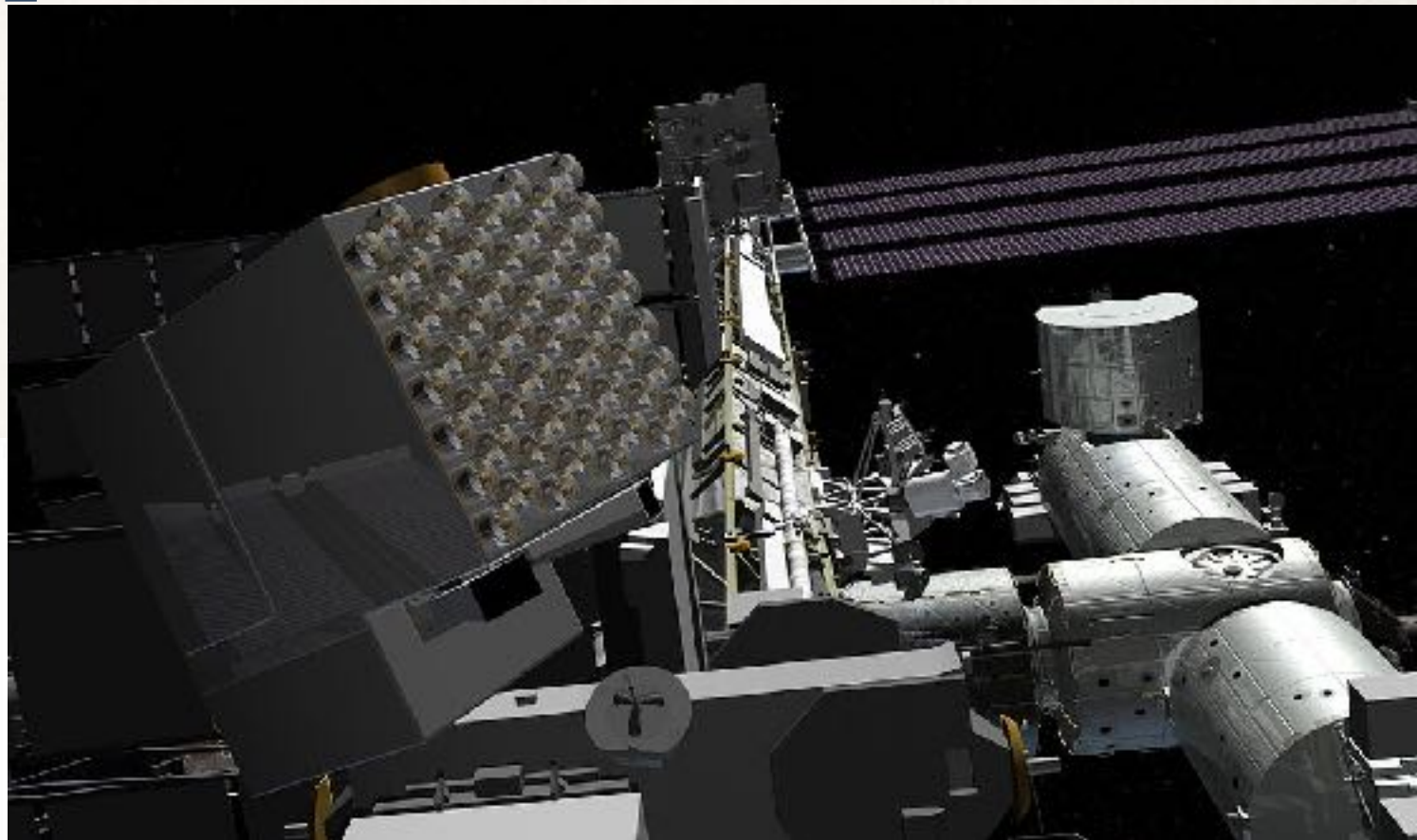
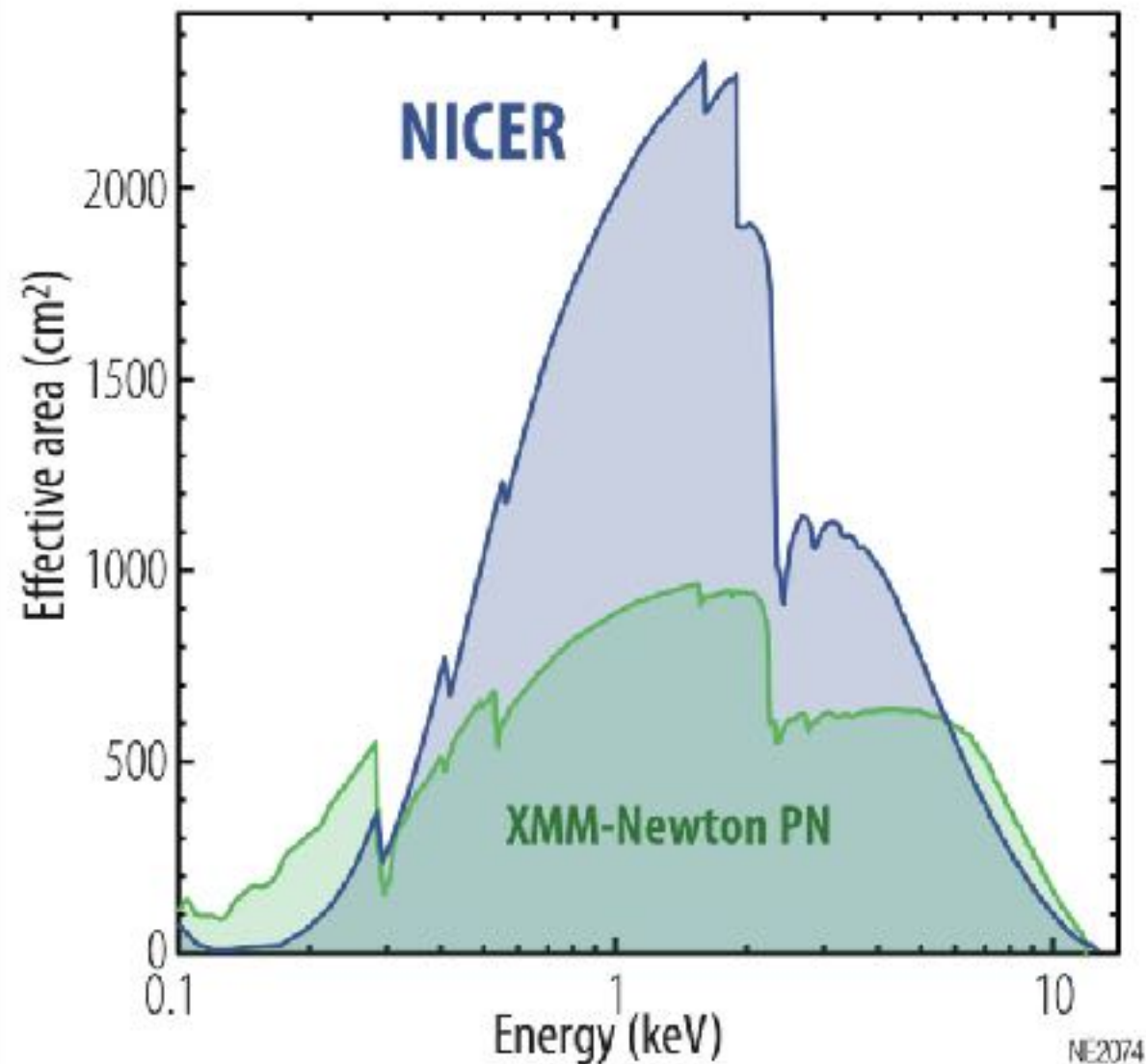


Neutron stars with different properties and observational signatures can be useful for R_{NS} measurements.

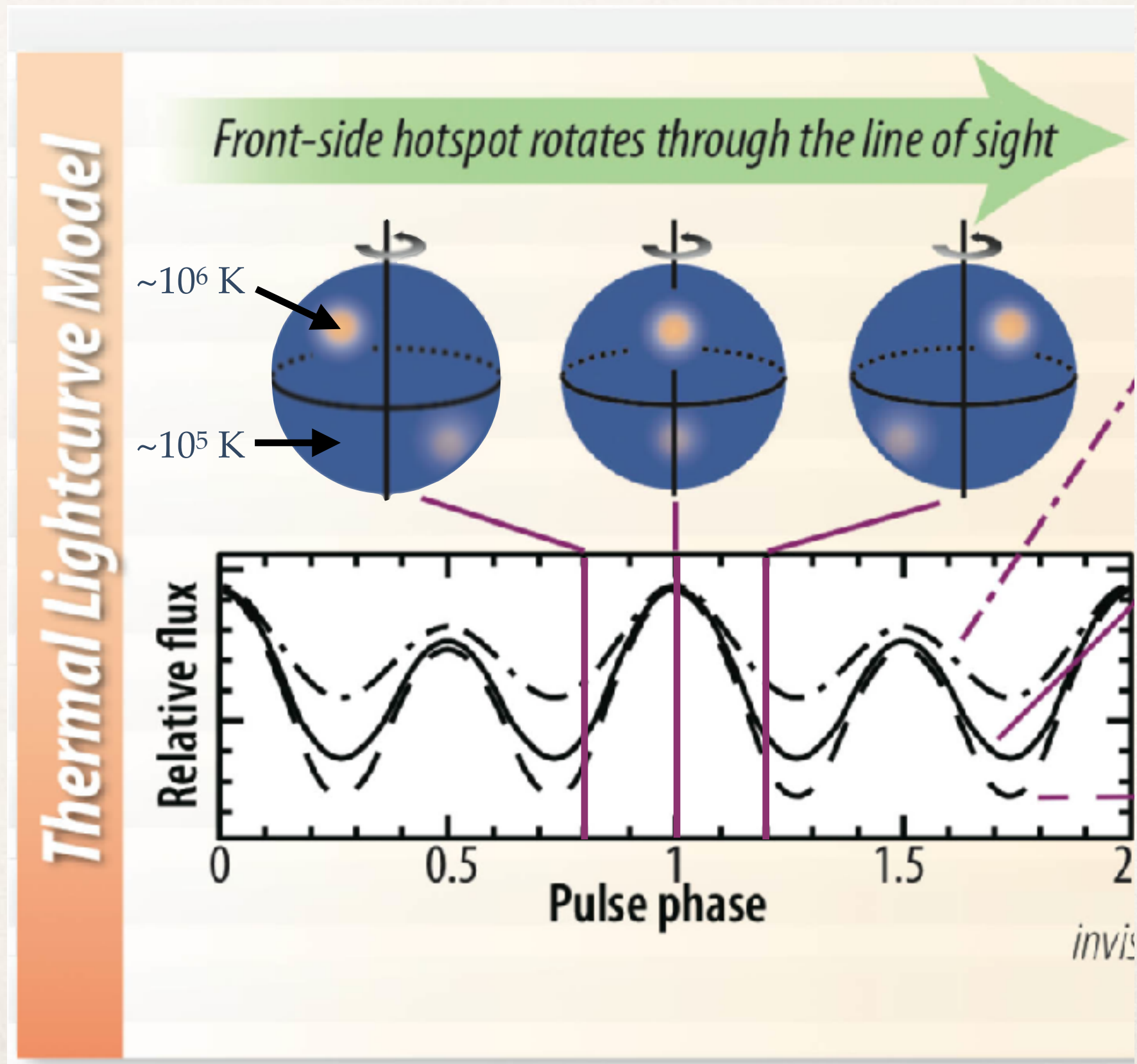


NICER's main science goal is to measure R_{NS} for four millisecond pulsars.

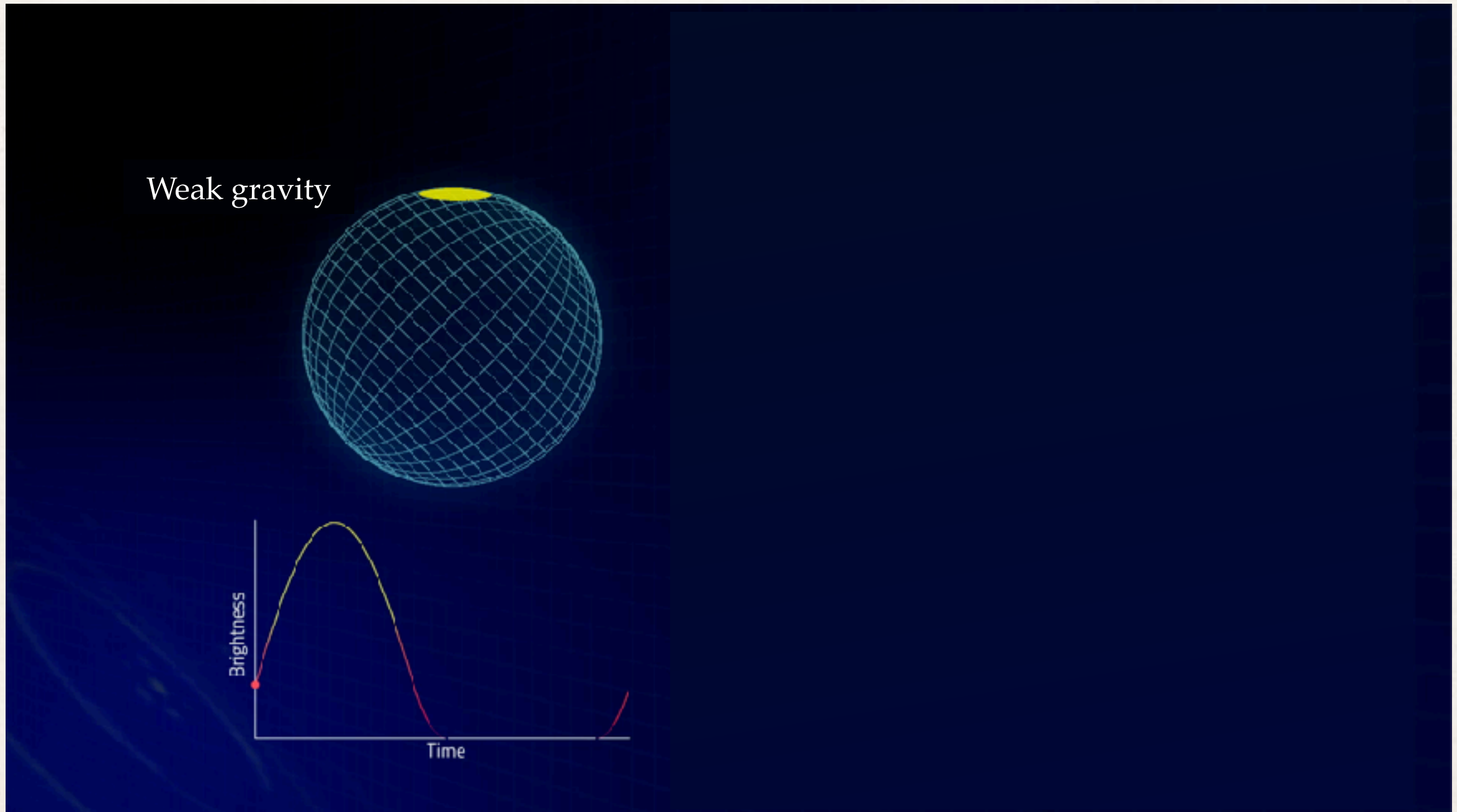
Launched in June 2017



The pulsed emission caused by hot spots on a rotating neutron star can help measure the compactness.

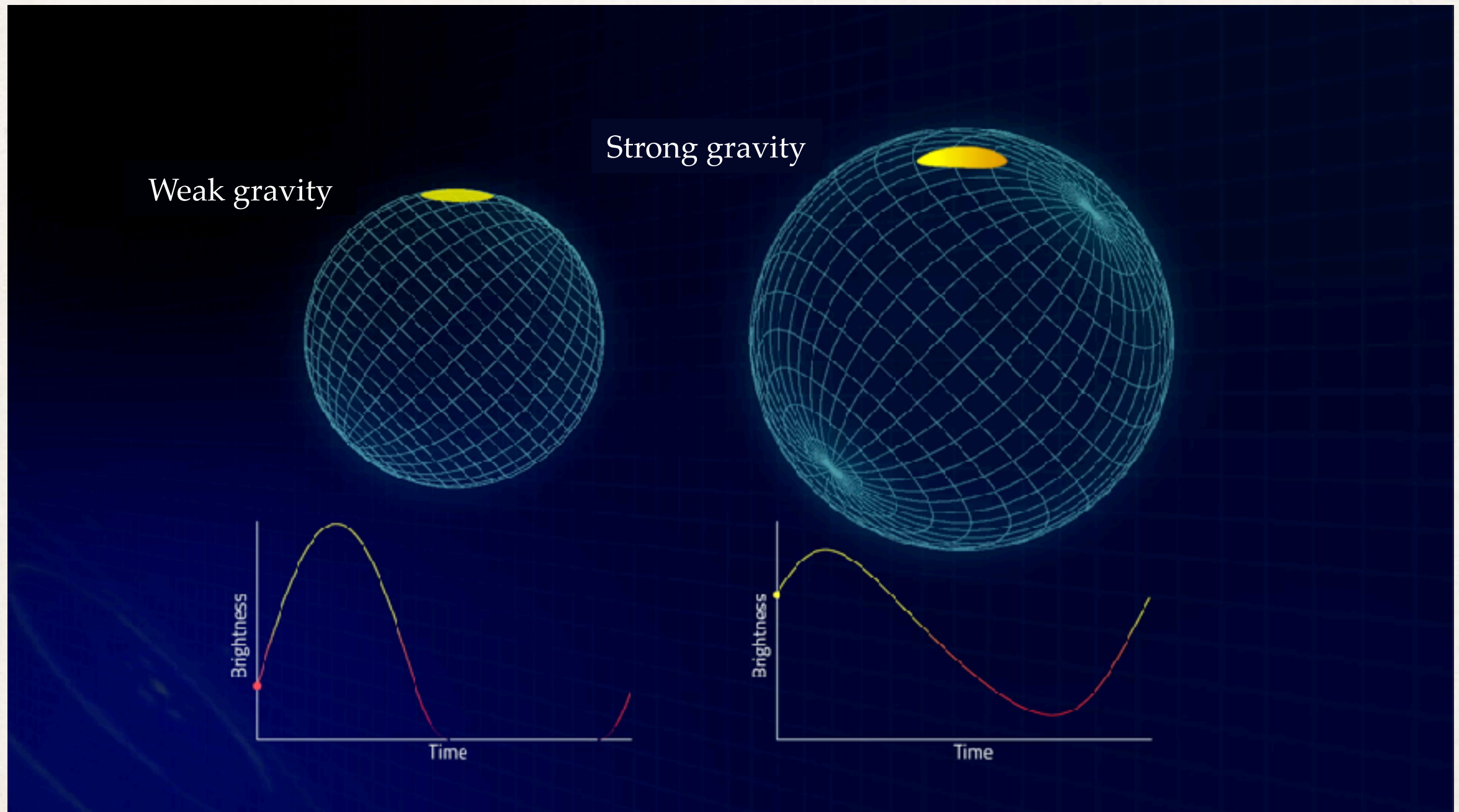


Strong gravity permits seeing beyond the hemisphere of the neutron star.



Credits: S. Morsink

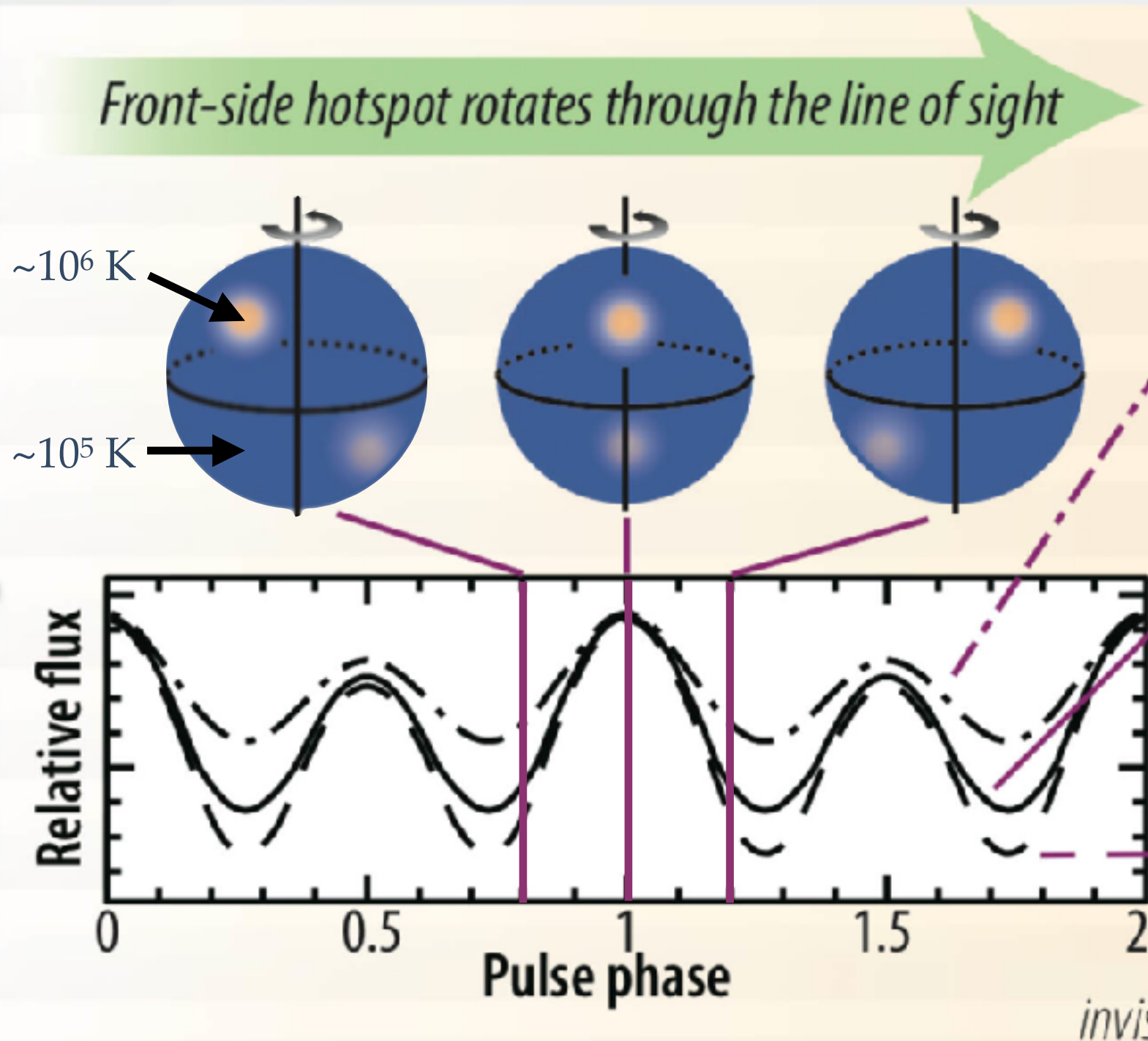
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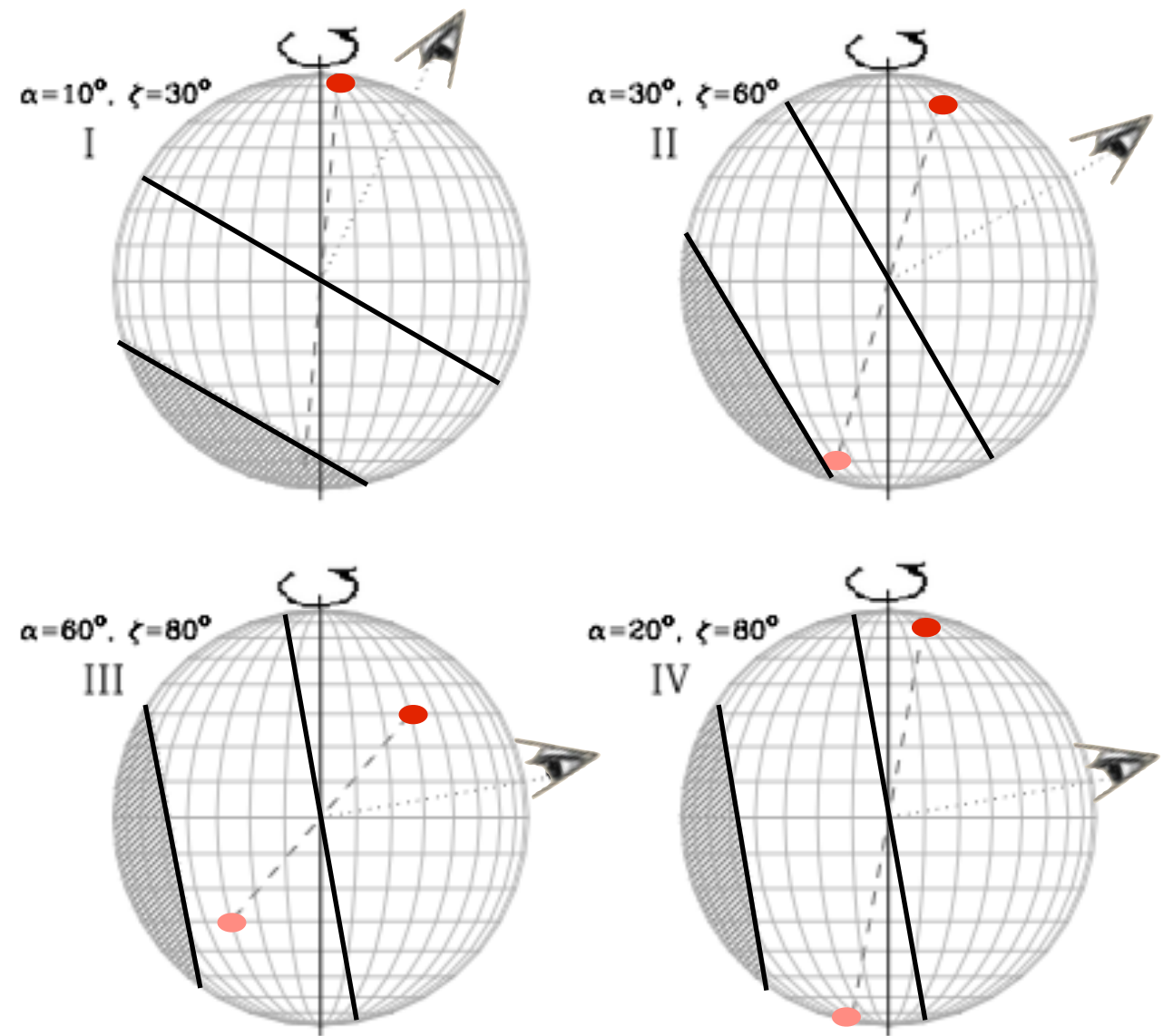
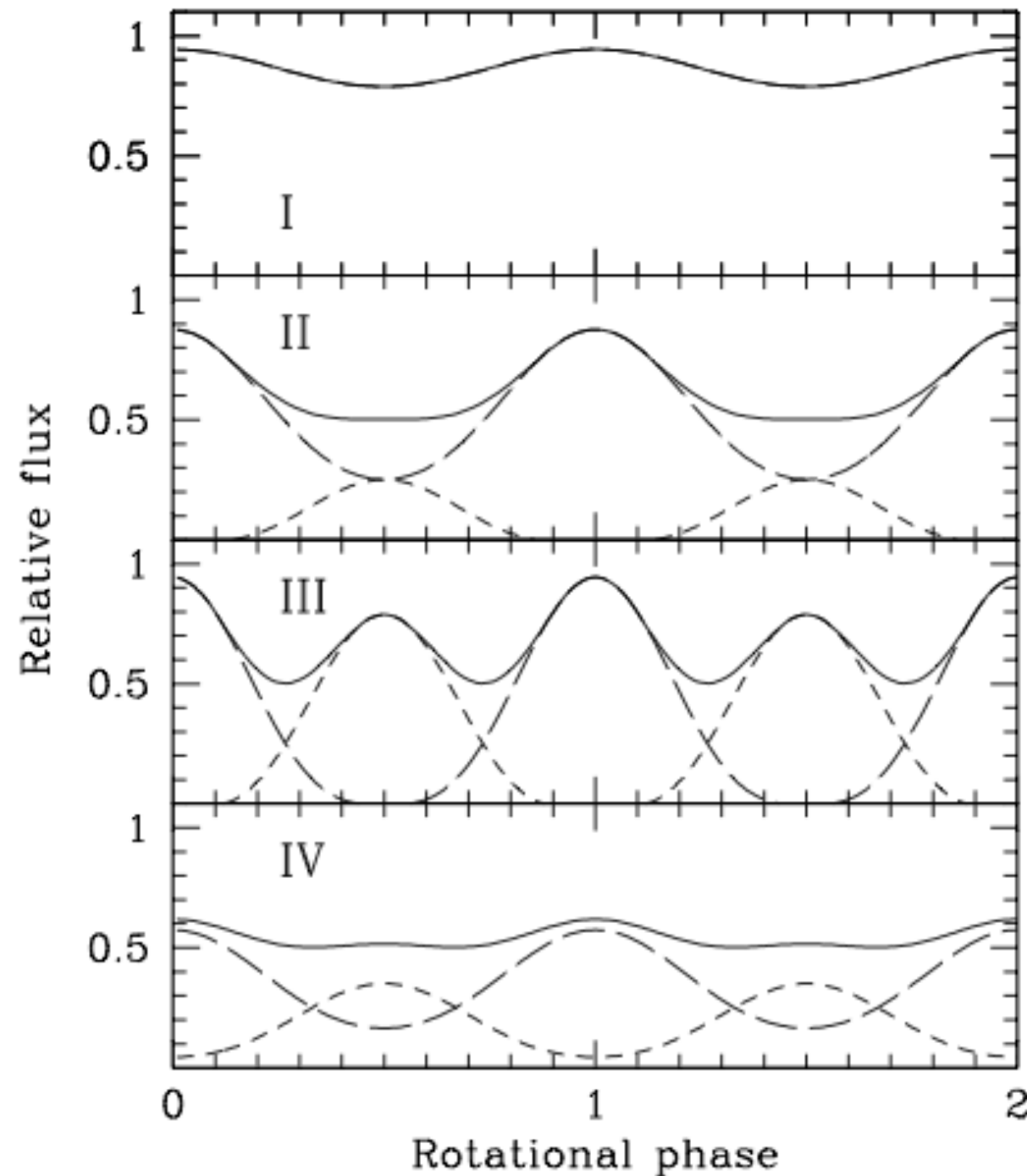
Credits: S. Morsink

The pulsed emission caused by hot spots on a rotating neutron star can help measure the compactness.

Thermal Lightcurve Model



The pulsed emission caused by hot spots on a rotating neutron star can help measure the compactness, but this depends on the system geometry.

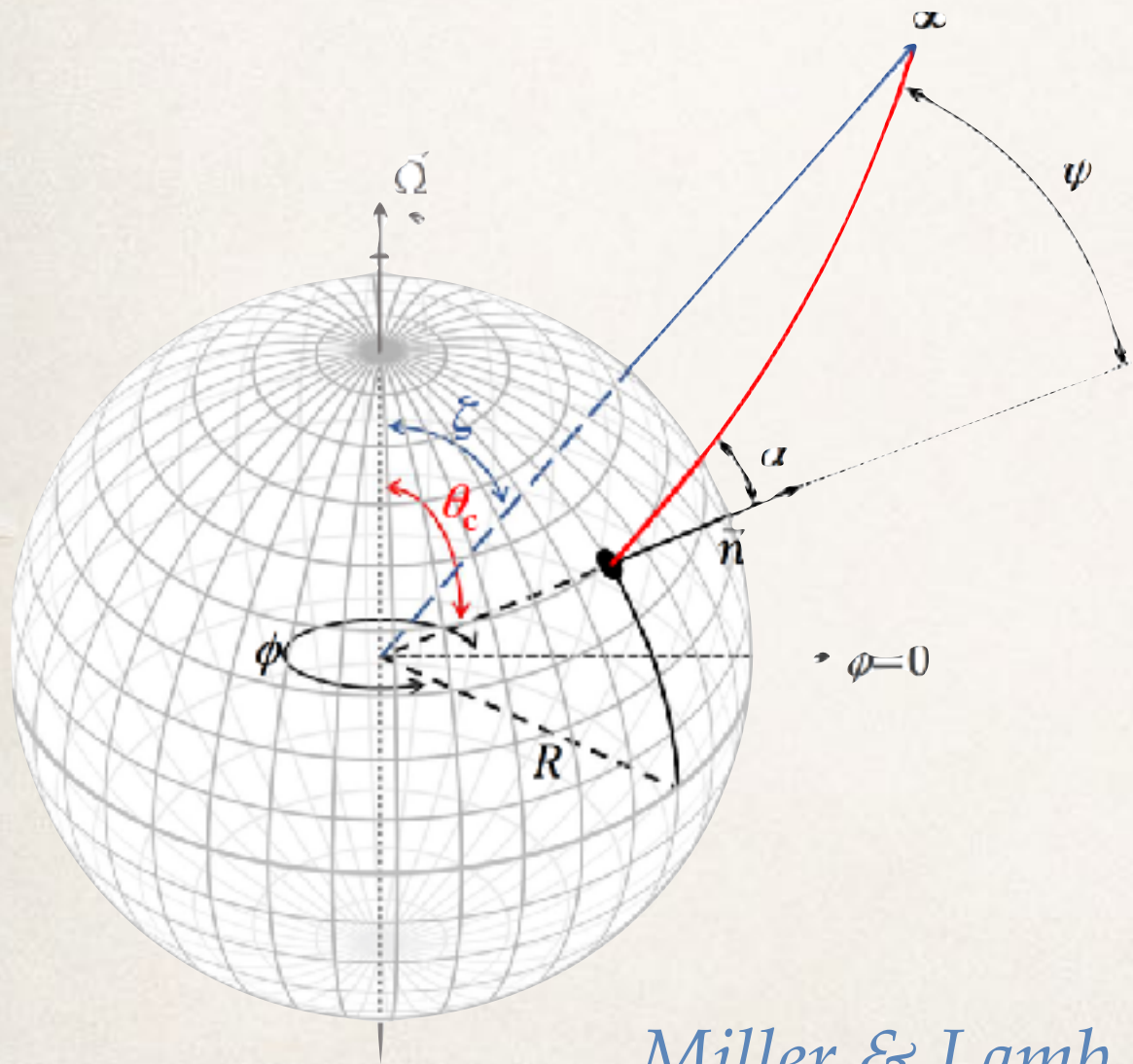


$M_{\text{NS}} = 1.4 M_{\odot}$, $R_{\text{NS}} = 10 \text{ km}$
(Bodganov et al. 2008)

Two main ingredients are necessary to model the lightcurve of millisecond pulsars.

General relativity

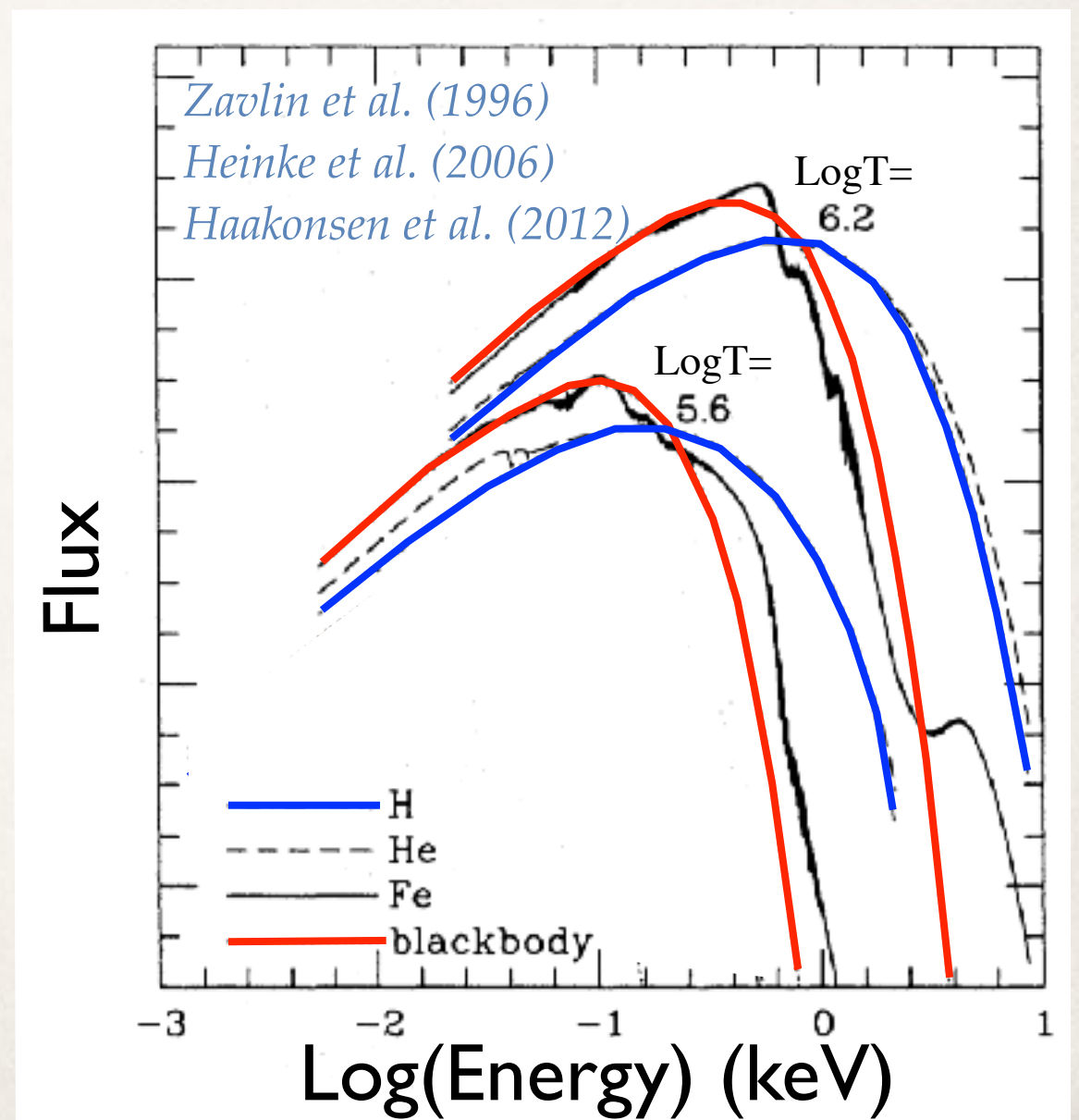
Schwarzschild metric + time delays,
doppler boosts / aberration + oblate star



Miller & Lamb 1998
Morsink et al. 2007

Surface emission model

Low-magnetic field,
fully-ionized H or He atmosphere



**NICER now routinely observes four key
target millisecond pulsars.**

Analysis is in progress...

There are some difficulties involved with the lightcurve modelling technique used by NICER.

- ♦ Atmospheric composition?
- ♦ Hot spots properties (these are fitted, but there are some degeneracies)
- ♦ Difficult to precisely determine the NICER background (non X-ray and X-ray backgrounds)

What's new?

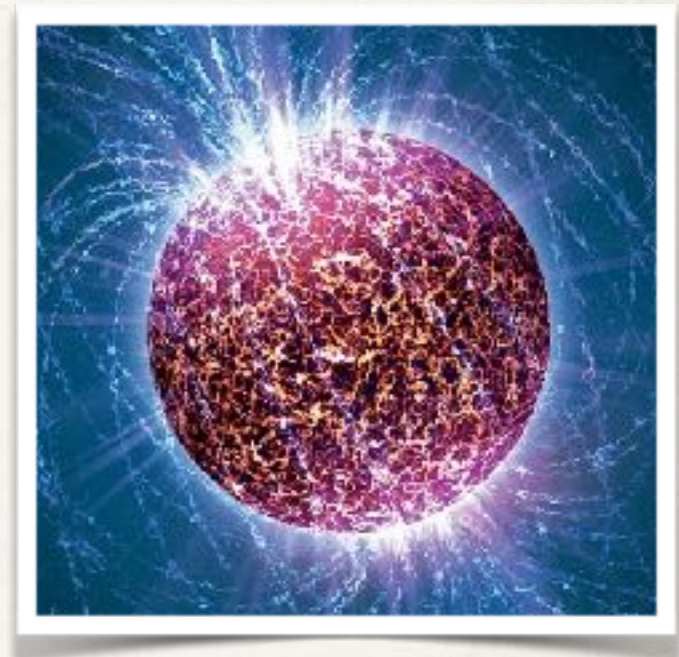


Stay tuned...

X-ray observations of thermally-cooling neutron stars permit obtaining the radius.

To measure the radius, we need to:

- ♦ observe / model the surface emission,
- ♦ know the distance independently.



$$F_X \propto \left(\frac{R_\infty}{D} \right)^2 \sigma T^4$$

Neutron stars in
quiescent low-mass X-ray
binaries

Neutron stars in
supernova remnants

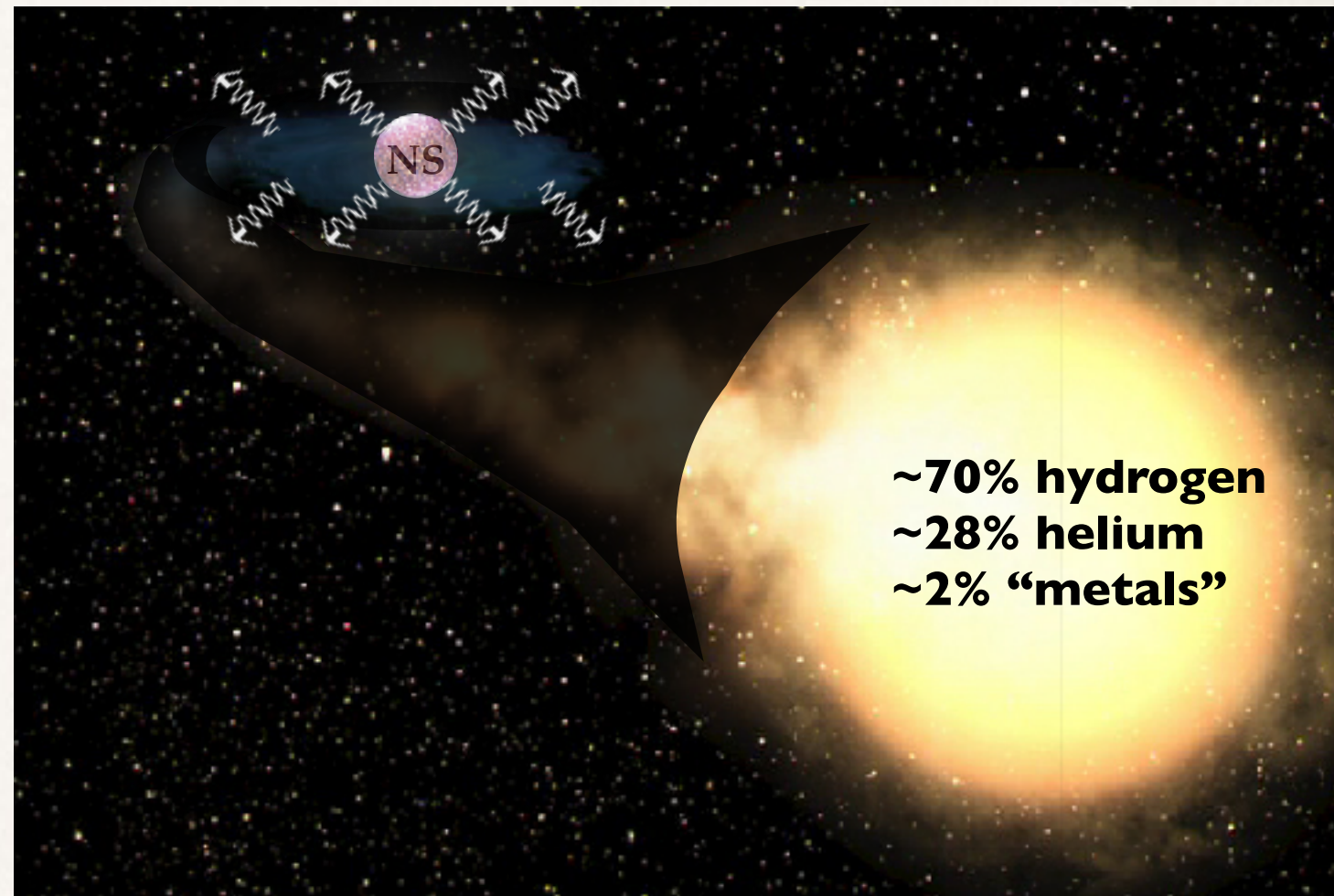
Thermally-cooling
isolated neutron stars

Neutron stars with
thermonuclear bursts

Quiescent low-mass X-ray binaries are ideal systems for radius measurements.

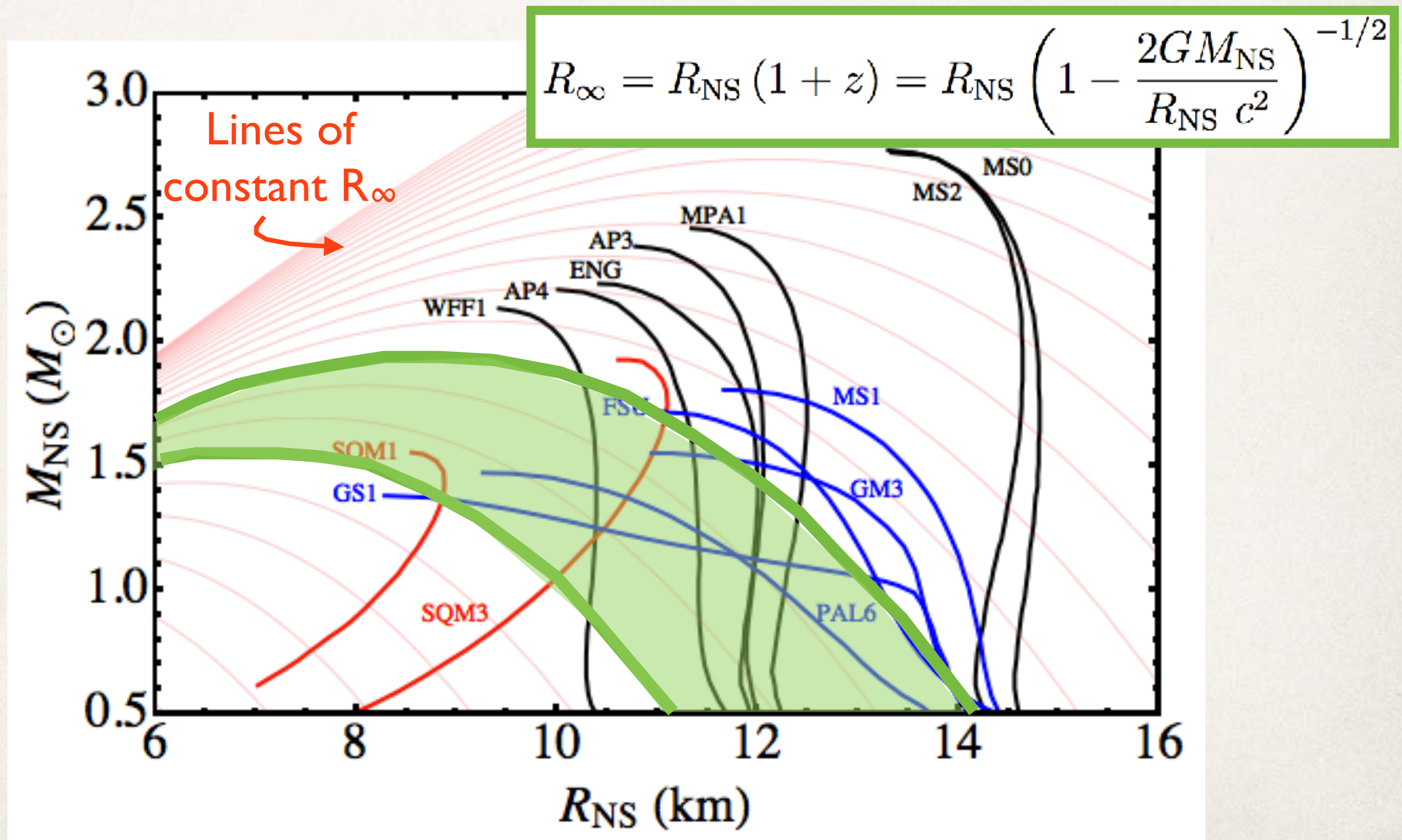
Surface thermal emission at $T_{\text{eff}} \sim 10^6$ K, powered by residual heat from the deep crust radiating outwards through the atmosphere with $L_X = 10^{32-33}$ erg/sec

$$F_X \propto \left(\frac{R_\infty}{D} \right)^2 \sigma T^4$$

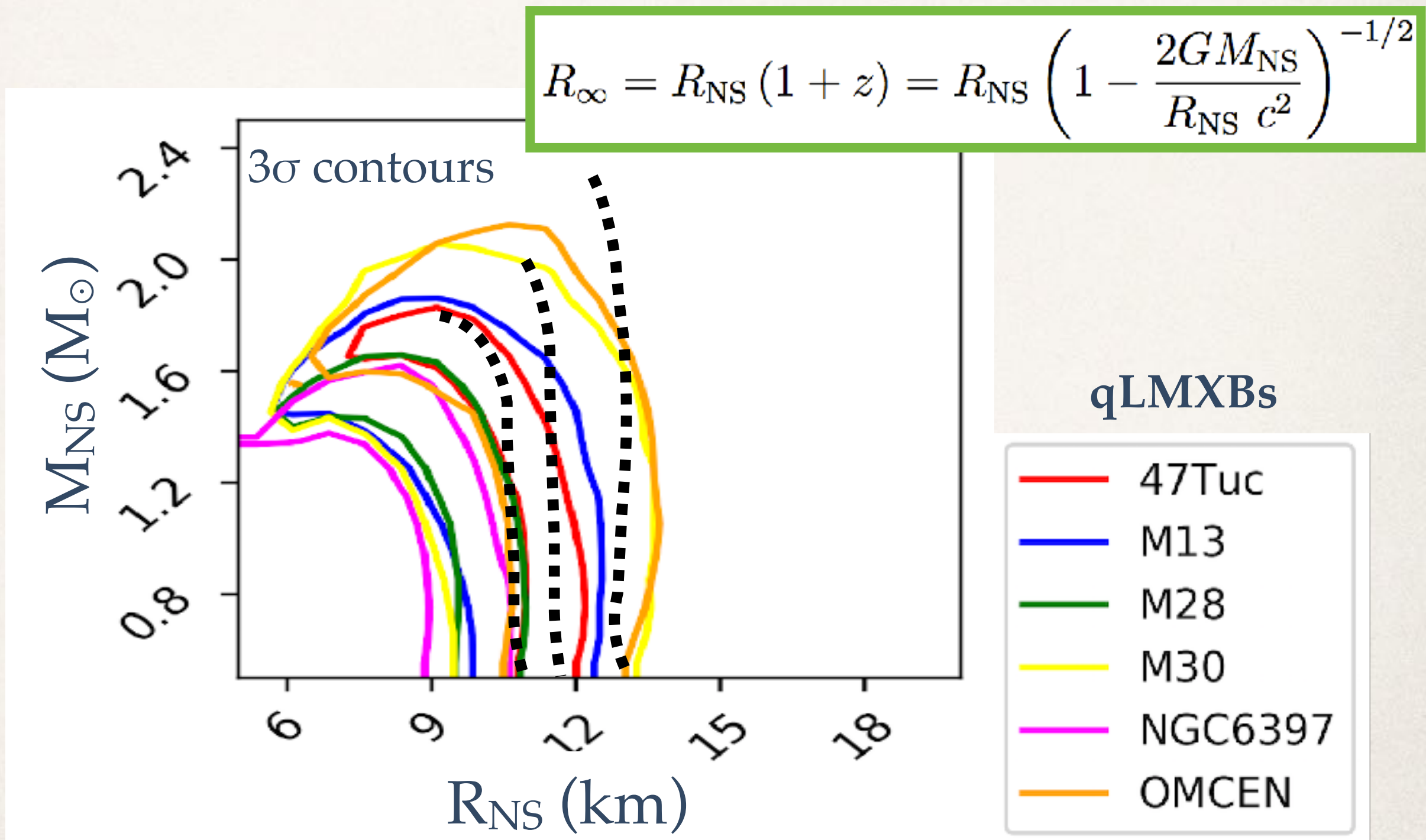


$$R_\infty = R_{\text{NS}} (1 + z) = R_{\text{NS}} \left(1 - \frac{2GM_{\text{NS}}}{R_{\text{NS}} c^2} \right)^{-1/2}$$

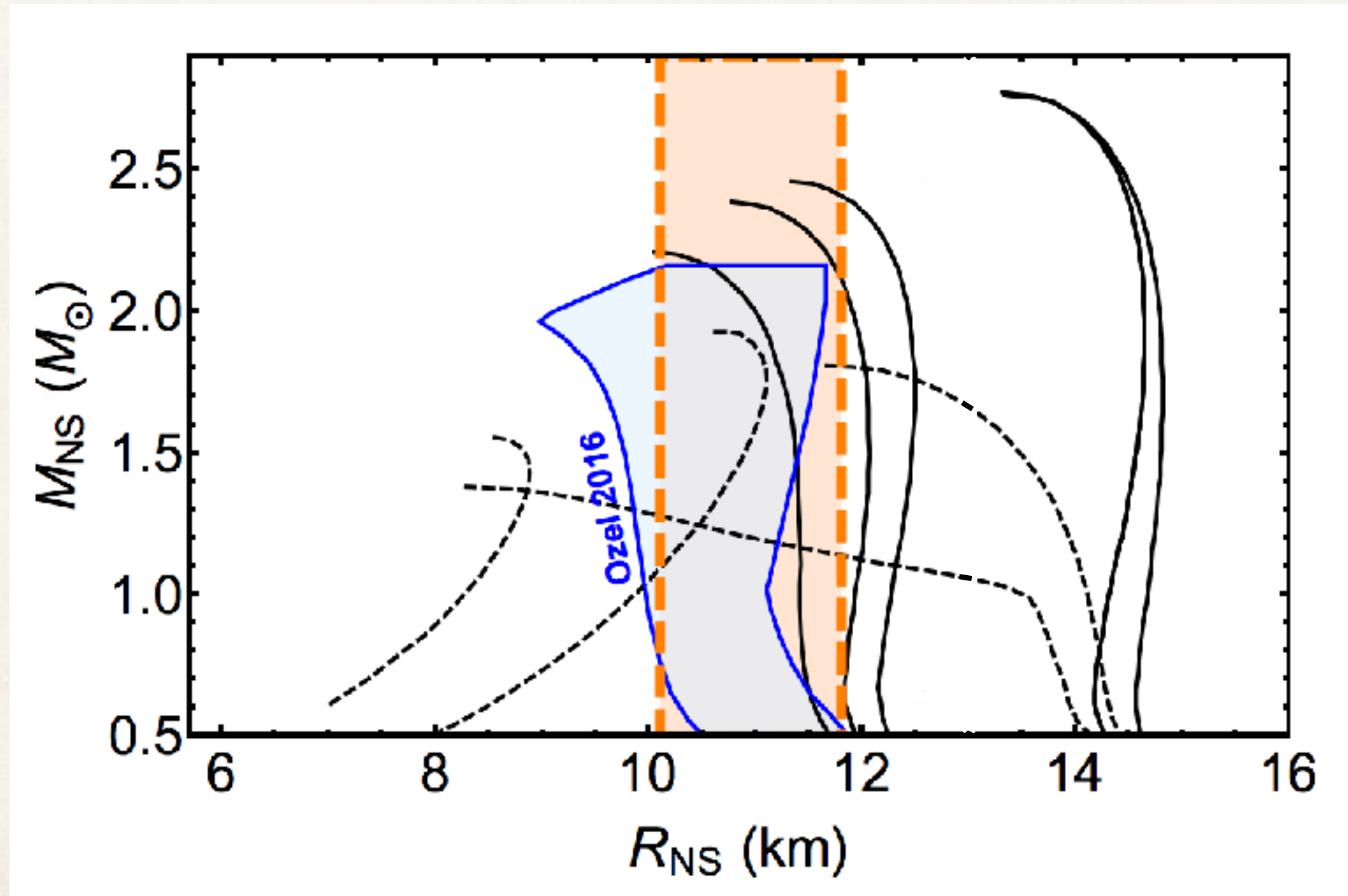
Because of gravitational redshift, the radius is degenerate with the unknown mass.



We want to find which equation of state is common to all these M-R measurements.



Some constraints have been obtained using these analytical parameterisations of the EoS.



Özel et al. (2016)

Updated results (2017)

There are some difficulties involved with the surface thermal emission technique.

- ♦ **NS atmospheric composition**
- ♦ **NS surface temperature distribution**
- ♦ **NS magnetic field and rotation**
- ♦ **Need to parameterise the EoS**

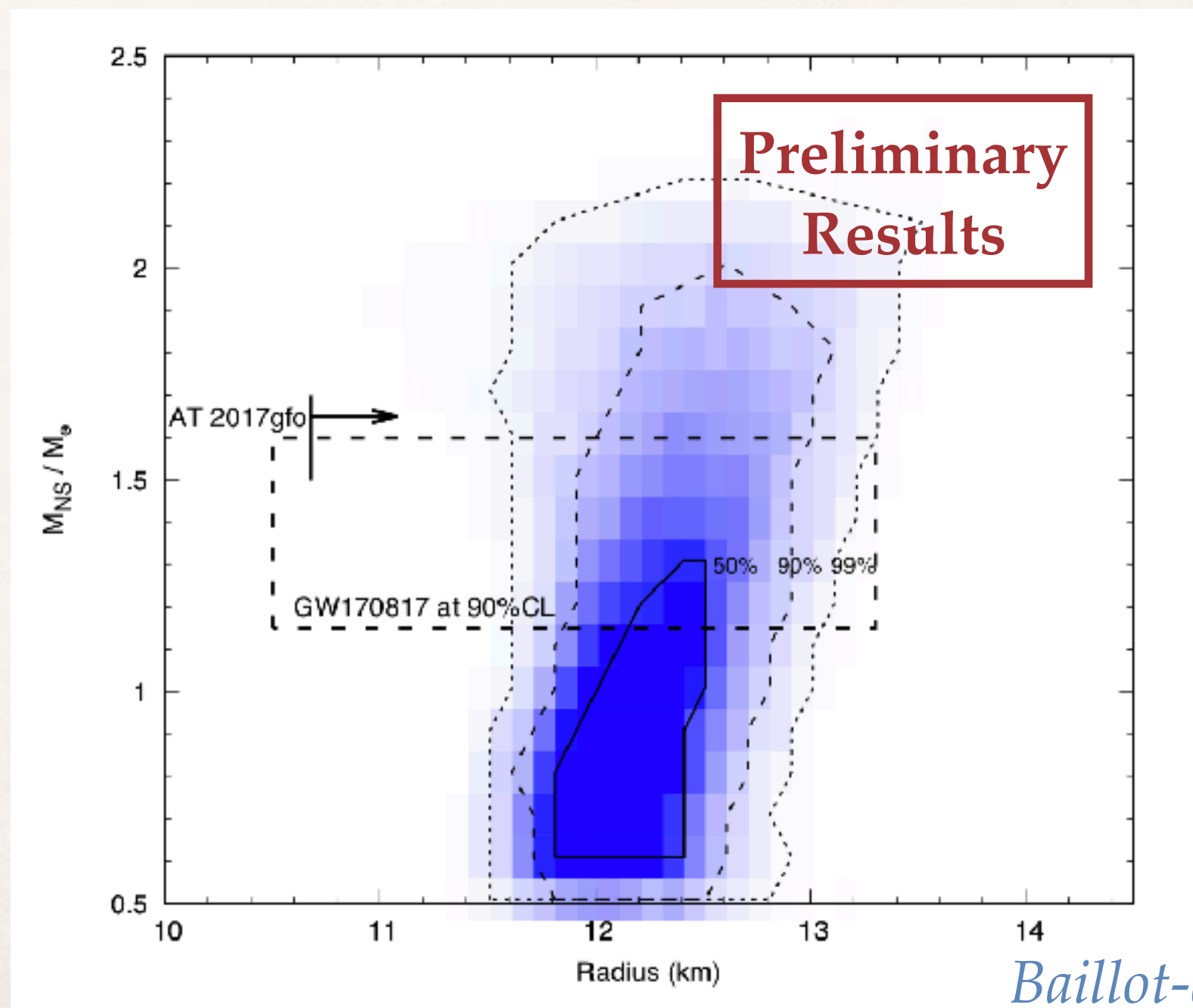
) Multi-wavelength
observations can
help!

What's new?

- ♦ **New X-ray data (from Chandra X-ray Observatory)**
- ♦ **New distances (expected from Gaia DR3)**
- ♦ **New method (realistic parameterisation of the EoS)**

Using a realistic parameterisation of the equation of state, we improve on previous estimates.

$$P = f(\rho, E_{\text{sat}}, E_{\text{sym}}, L_{\text{sym}}, K_{\text{sym}}, K_{\text{sat}}, Q_{\text{sat}}, \dots)$$

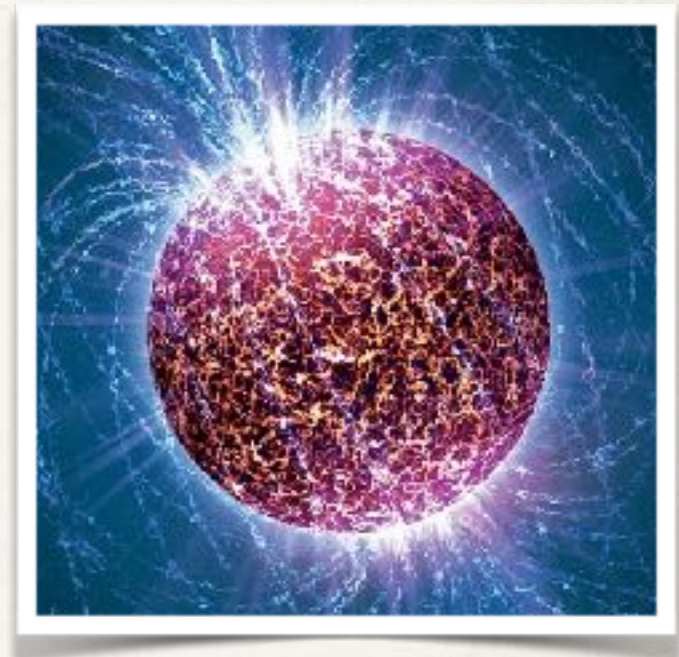


Baillot-d'Etivaux, et al.

X-ray observations of thermally-cooling neutron stars permit obtaining the radius.

To measure the radius, we need to:

- ♦ observe / model the surface emission,
- ♦ know the distance independently.



$$F_X \propto \left(\frac{R_\infty}{D} \right)^2 \sigma T^4$$

Neutron stars in
quiescent low-mass X-ray
binaries

Neutron stars in
supernova remnants

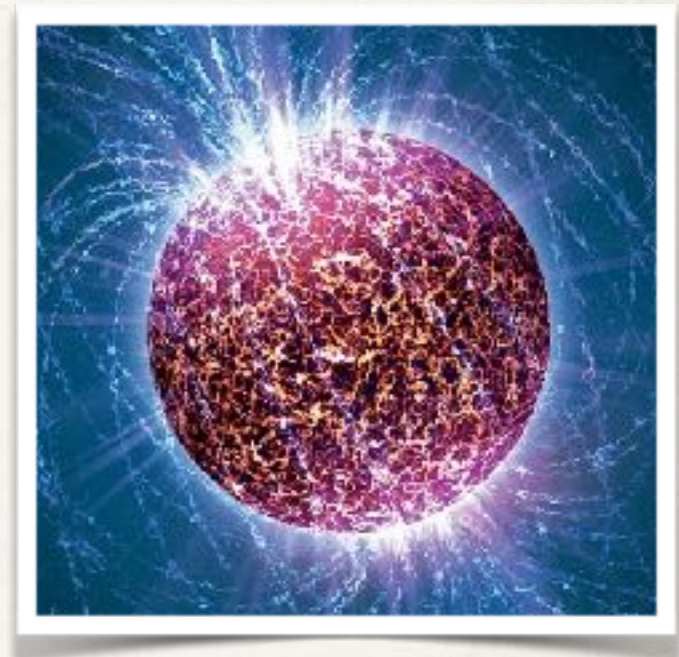
Neutron stars with
thermonuclear bursts

Thermally-cooling
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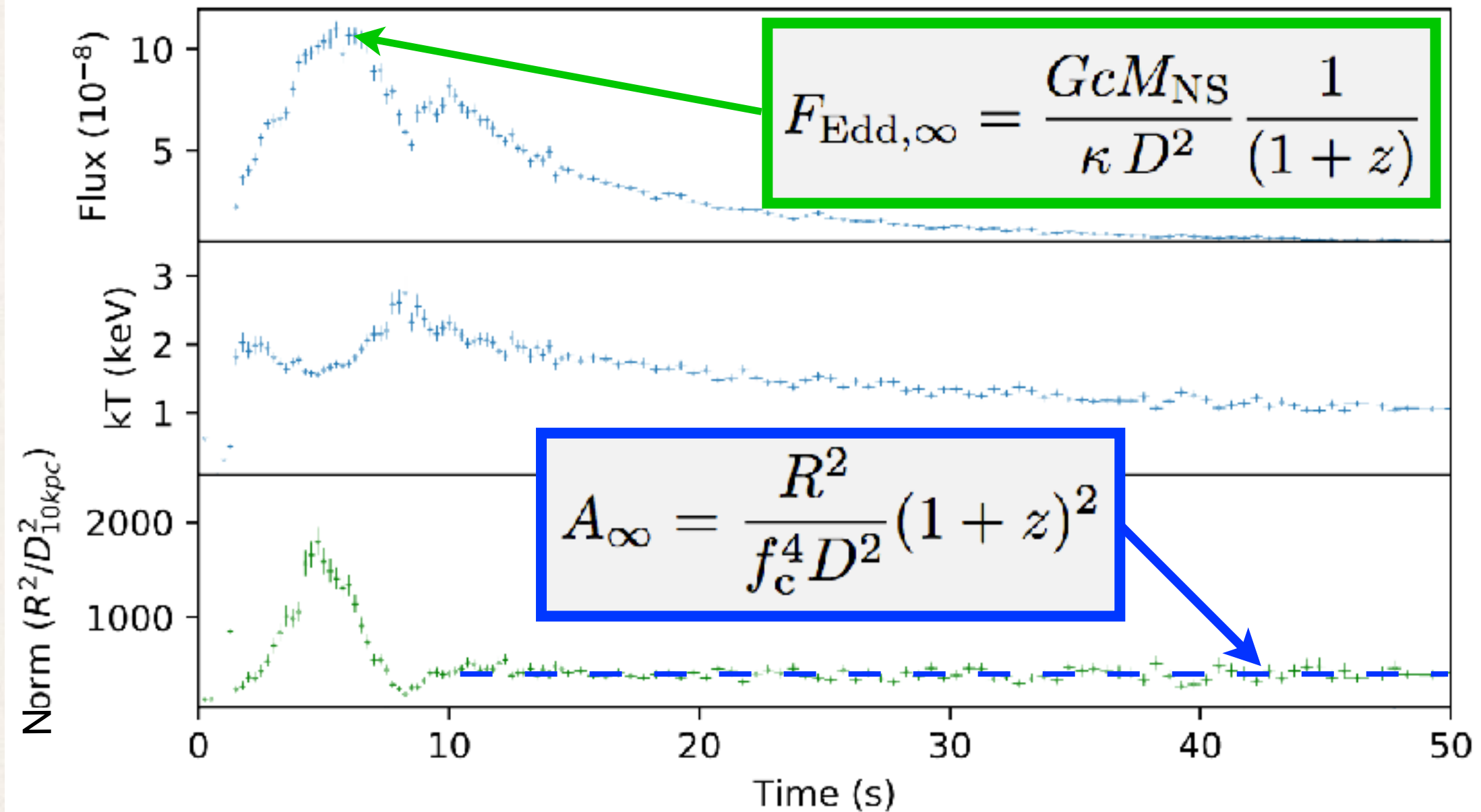
Thermally-cooling
isolated neutron stars

Some LMXBs exhibiting thermonuclear bursts with Photospheric Radius Expansion.



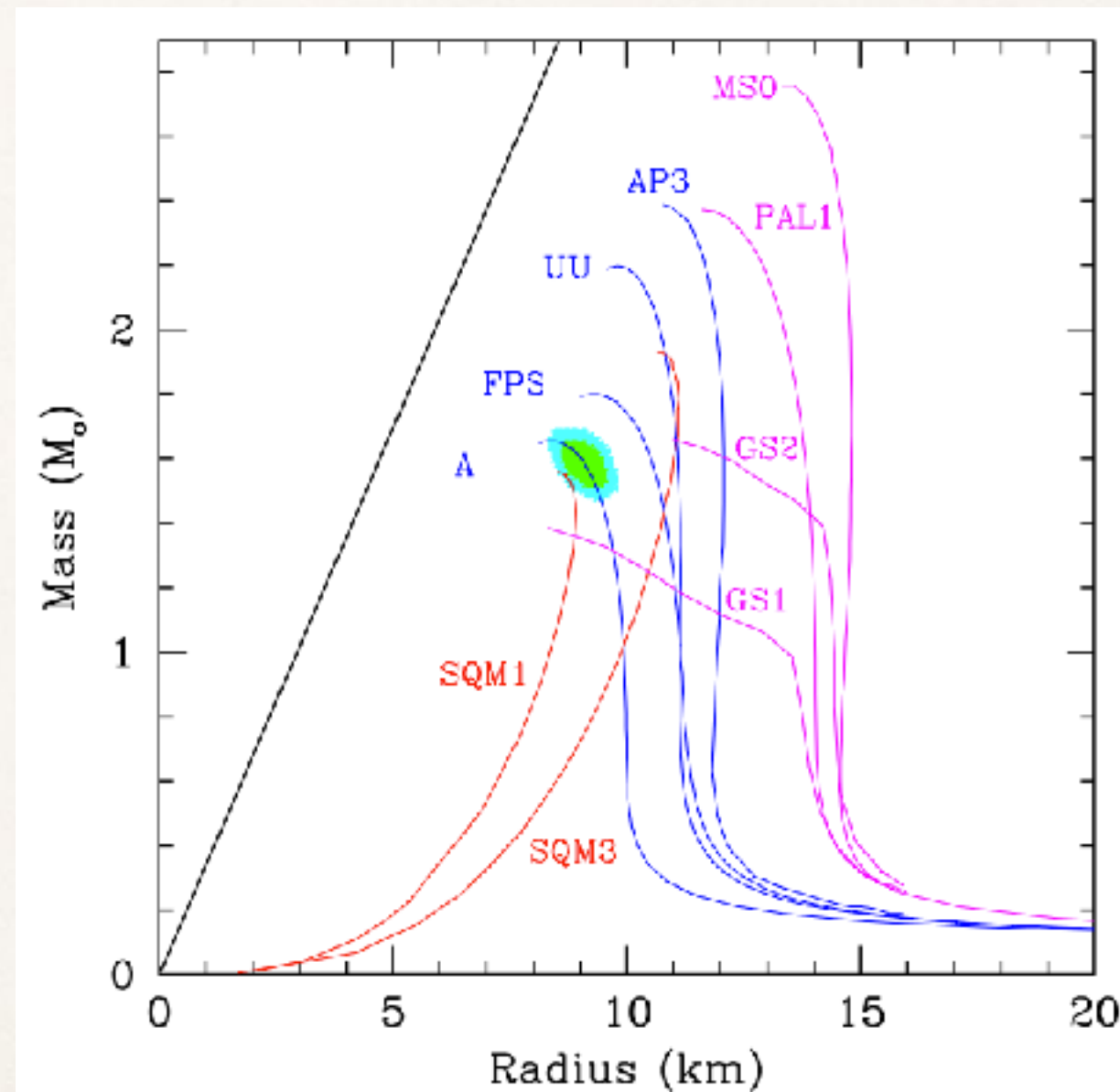
$$L_{\text{Edd}} = \frac{4\pi G c M_{\text{NS}}}{\kappa}$$

The peak flux correspond to the Eddington flux, and the cooling tail gives the size of the emitting area.



with $(1+z) = \left(1 + \frac{2GM_{\text{NS}}}{c^2 R_{\text{NS}}}\right)^{-1/2}$

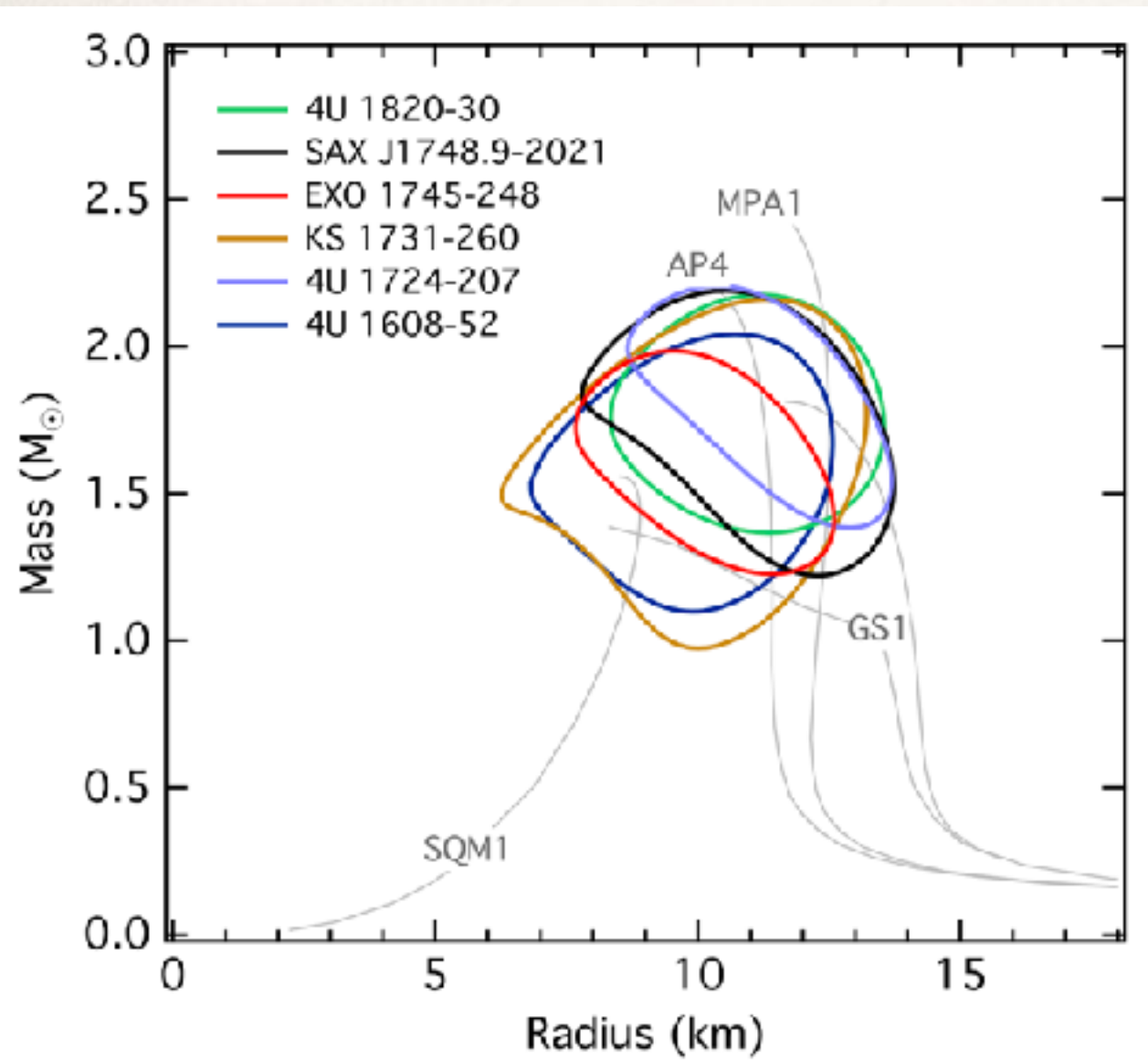
Different analyses and types of sources result in different constraints...



4U 1820-30

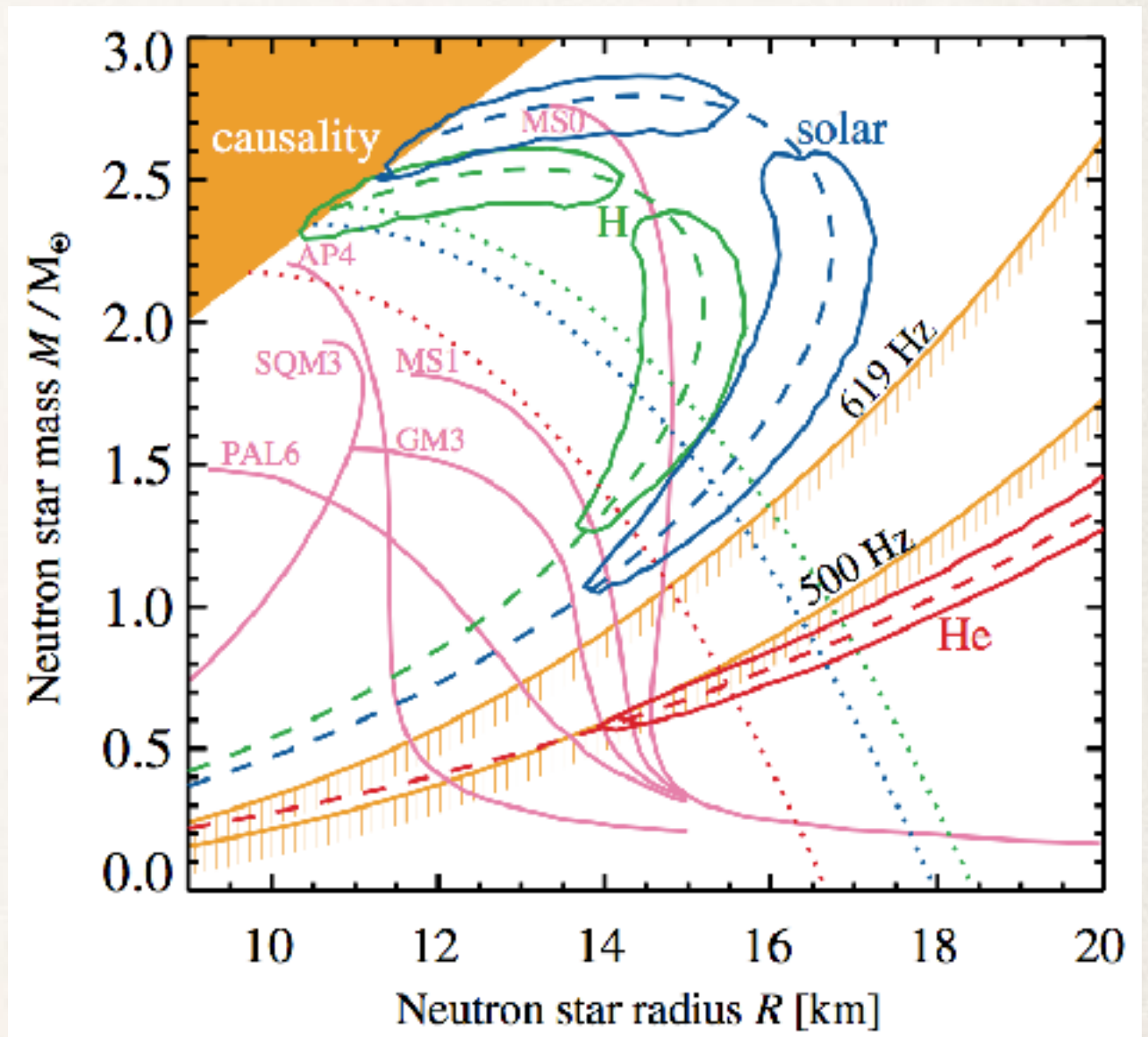
Güver et al. 2010

Different analyses and types of sources result in different constraints...It's a heated debate!



Data-driven selection of
(high-soft state) bursts

Özel et al. 2016



Theory-driven selection of
low-hard state bursts

Suleimanov et al. 2011

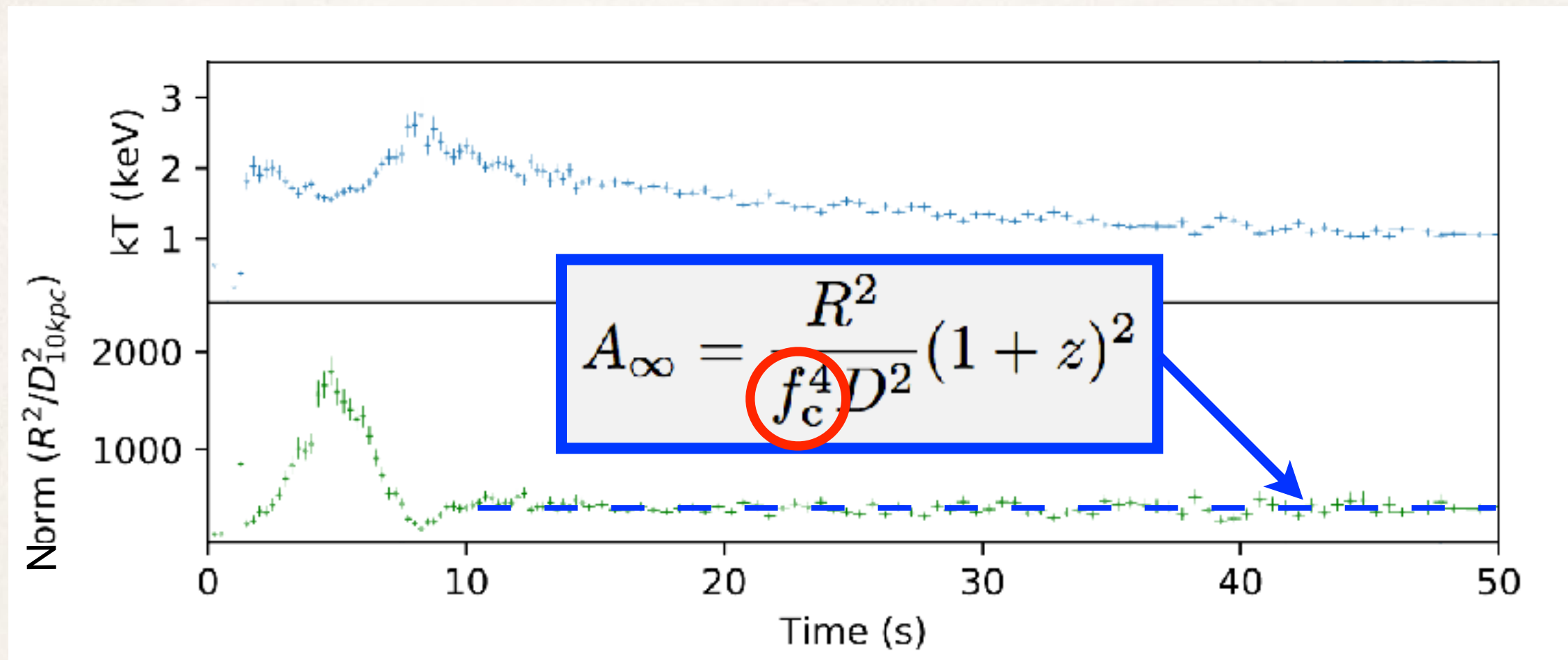
There are some difficulties involved with the Type I X-ray burst technique.

- ♦ Atmosphere modelling (i.e., the conversion to/from a blackbody with a colour correction factor f_c)
- ♦ Neutron star atmospheric composition
- ♦ Distance sometimes unknown

What's new?

- ♦ **New method!**
- ♦ **New instrument (NICER)**
- ♦ **New “problem”**

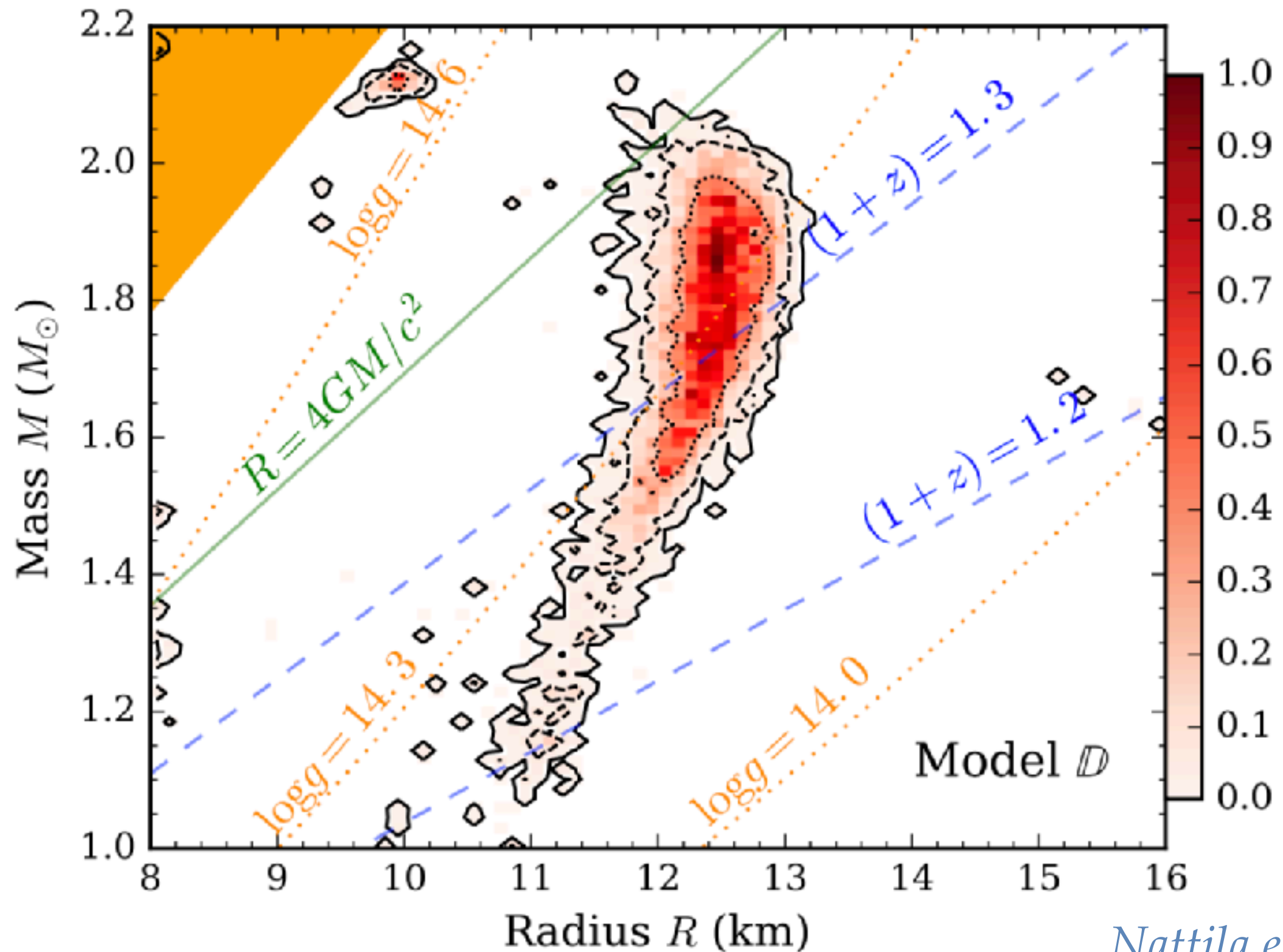
Until recently, the thermal emission was fit with a Planck function, and a colour-correction was used.



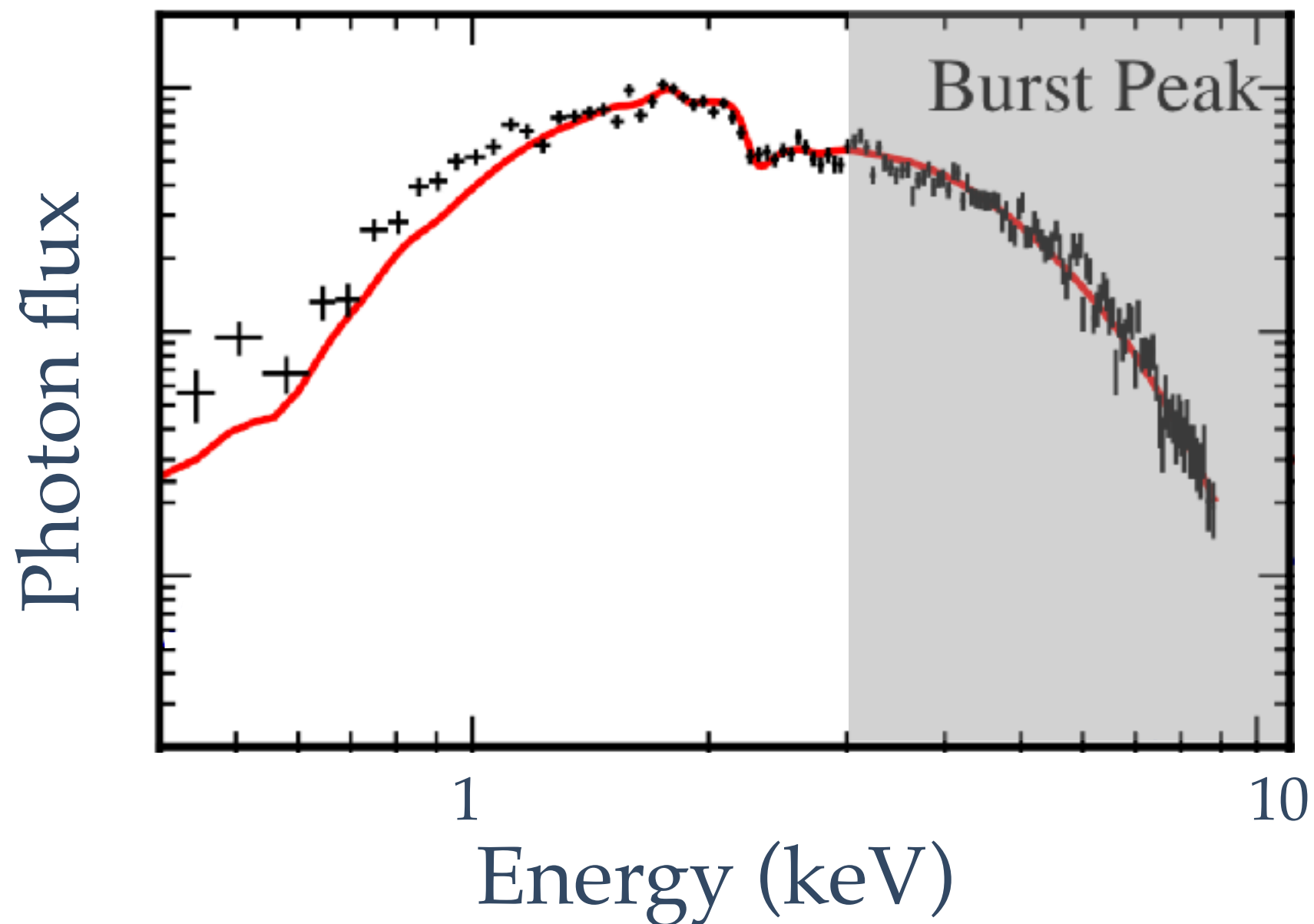
f_c is model dependent!

Solution: fit every single spectrum with realistic model

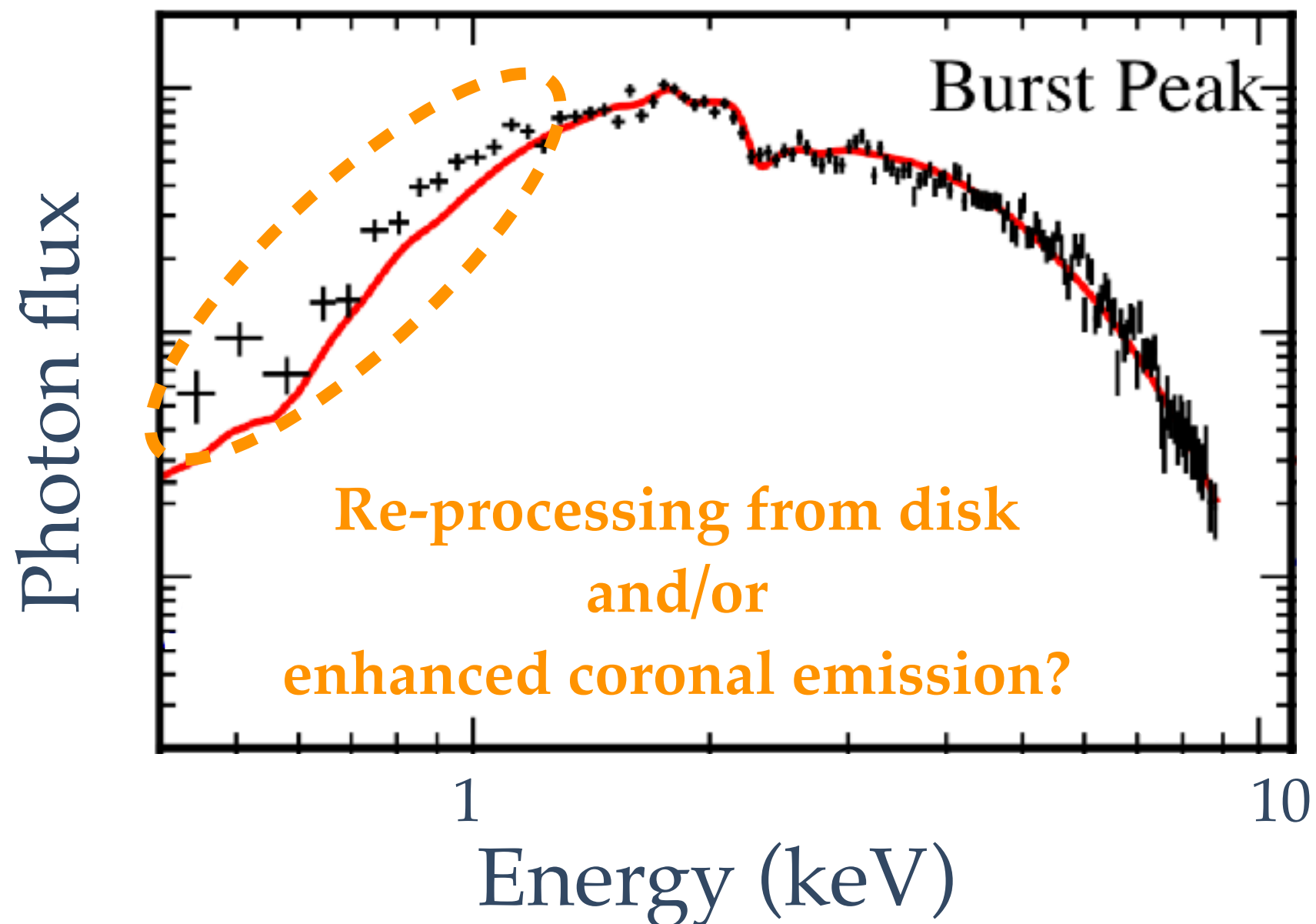
Recent work




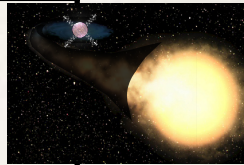
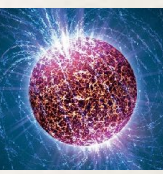
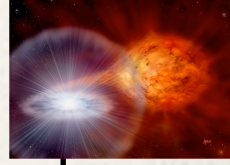


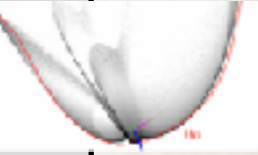
The observation of type I X-ray burst with NICER showed the presence of a un-modelled soft-E excess.




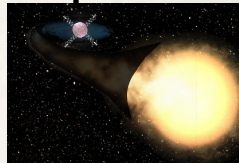
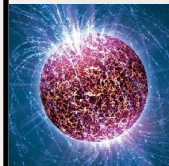
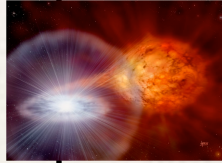



The observation of type I X-ray burst with NICER showed the presence of a un-modelled soft-E excess.



Summary – Current status

Pulse-profile of MSP	NICER will produce 4 precise R_{NS} measurements	
Quiescent low-mass X-ray binaries	Some uncertainties related to assumptions. Need parameterisation of EOS (or masses).	
Isolated neutron stars (and CCOs)	Atmosphere modelling difficult (e.g. magnetic field and composition)	
Type-I X-ray bursts	Some modelling uncertainties. Understand the effects of accretion?	
GW from NS-NS merger	Promising technique! But only 1 event so far	
Moment of inertia (radio timing)	Spin-orbit coupling needs decades of data	
Moment of inertia (bow-shock PWN)	Two attempts: See Bejger et al. (2002); Romani et al. (2017)	
Max. rotation of NSs	Look for more pulsars and hope for a faster one	

Summary – Current results

Pulse-profile of MSP	CAN'T TELL YOU!!!	
Quiescent low-mass X-ray binaries	$R_{\text{NS}} \sim 10 - 13 \text{ km}$	
Isolated neutron stars (and CCOs)	$R_{\text{NS}} \sim 10 - 14 \text{ km}$	
Type-I X-ray bursts	$R_{\text{NS}} \sim 11 - 13 \text{ km}$	
GW from NS-NS merger	$R_{\text{NS}} \sim 10.5 - 13.5 \text{ km}$	
Moment of inertia (radio timing)	No results yet	
Moment of inertia (bow-shock PWN)	$I = 2.4 \times 10^{45} \text{ g cm}^2$ – Romani et al. (2017)	
Max. rotation of NSs	Limits from fastest pulsar: $R_{\text{NS}} < 17 \text{ km}$	