

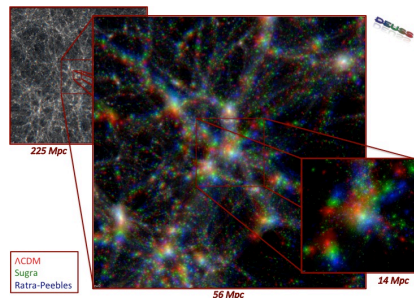
Numerical simulations for cosmology

(with a special focus on dark energy)

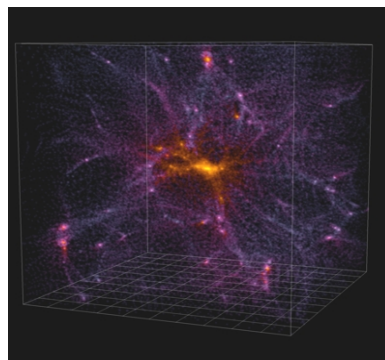
Yann RASERA

Colloque National Dark Energy 2018

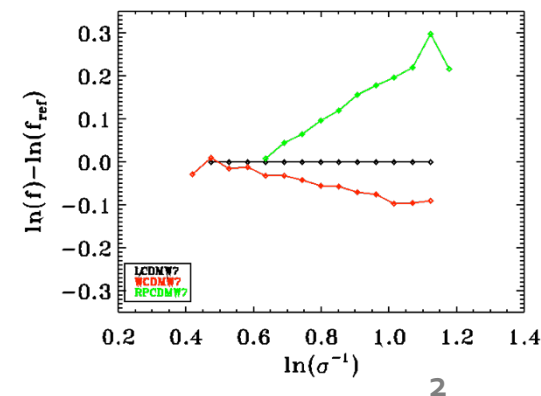
- I. Why do we need simulations for the dark energy problem ?
- II. Simulations: how to proceed ?
- III. What kind of results? Illustrative example about the imprints of minimally coupled dark energy on *cosmic structure formation*
- IV. Conclusion and perspective



October 24th, 2018



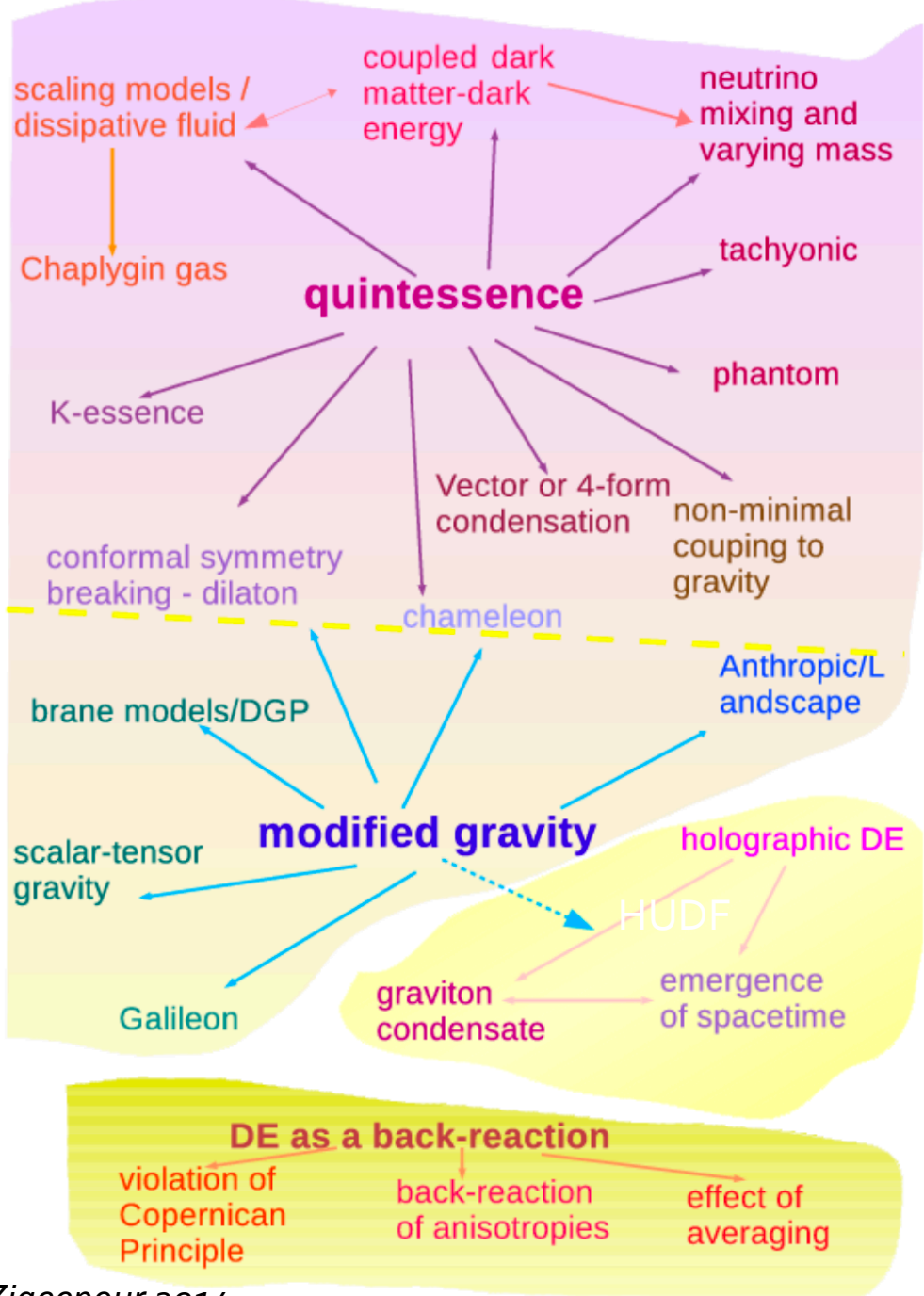
Colloque Dark Energy 2018



I. Why do we need simulations for the dark energy problem ?

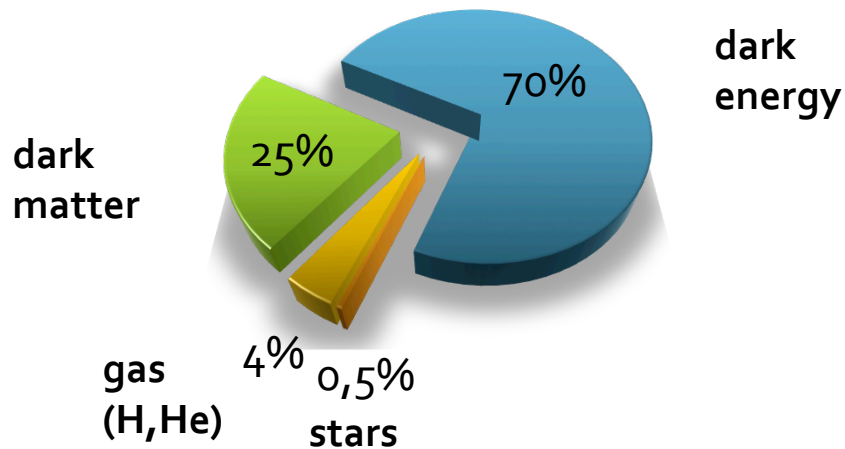
WHAT IS THE NATURE OF DARK ENERGY ?

VARIOUS POSSIBILITIES

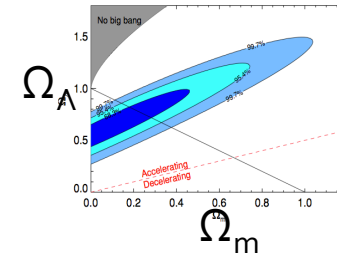


• MAIN OBSERVATIONAL CONSTRAINTS FOR DE

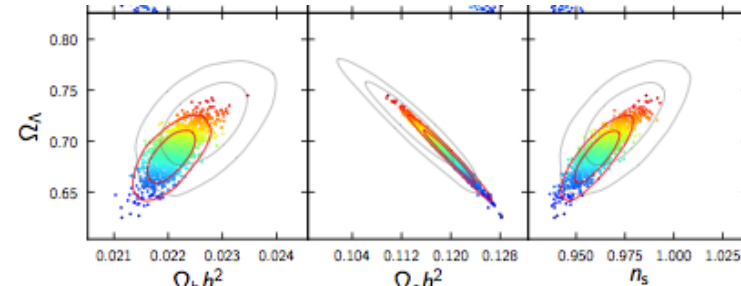
- **Homogenous:** SNIa (UNION, SNLS) \rightarrow luminosity distances
- **Early linear:** CMB (WMAP, Planck) \rightarrow angular distances



- **Non linear:**
 - Baryon Acoustic Oscillations (SDSS, 2dF, BOSS, wiggleZ) \rightarrow angular & radial distance + **linear** assumptions for peak position + assumptions shape
 - Weak lensing (CFHTLS, Planck) \rightarrow matter power spectrum **prescription** + projection
 - Cluster Counts (Chandra, XMM, Planck) \rightarrow linear growth rate + **universal mass function assumption** + geometry

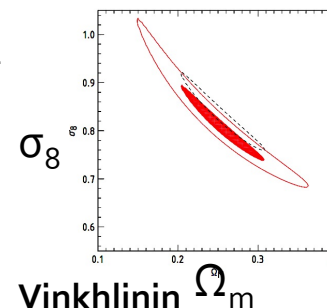
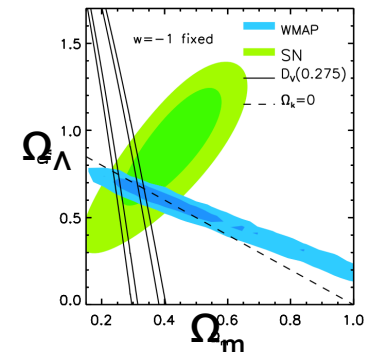


Conley
et al. 2011

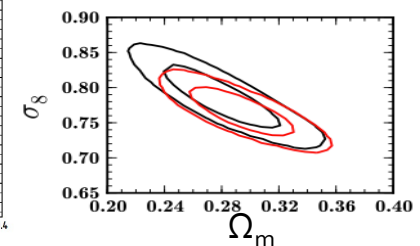


Planck
et al. 2013

Percival
et al. 2010



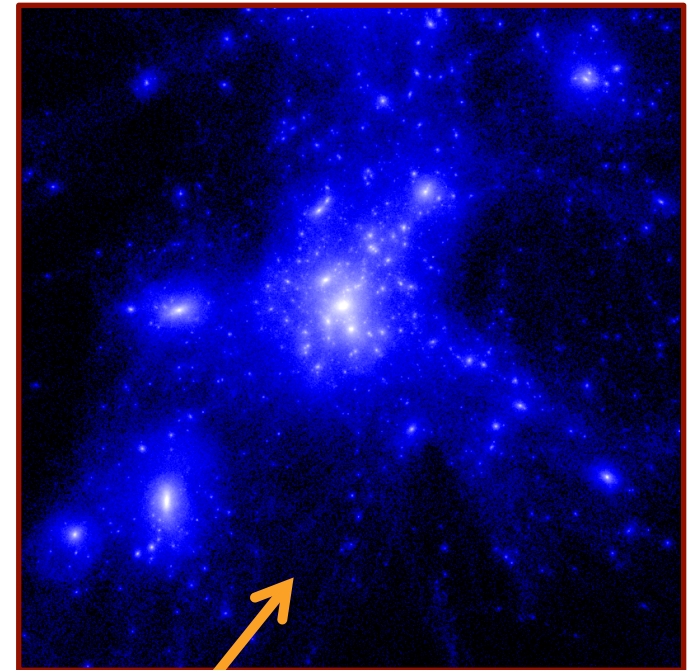
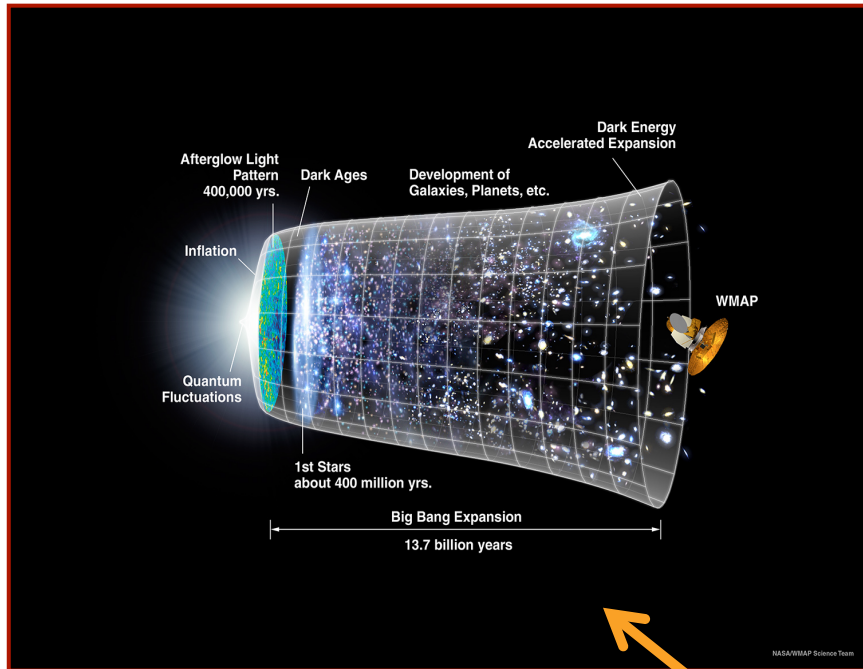
Vinkhlinin
et al. 2009



Planck
et al. 2013b 5

WHAT IS THE NATURE OF DARK ENERGY ?

•NEW OR REFINED PROBES: NON-LINEAR REGIME OF STRUCTURE FORMATION



**Non linear imprints of DARK ENERGY on COSMIC STRUCTURES ?
How to probe DARK ENERGY with COSMIC STRUCTURES?**

NON-LINEARITIES => NUMERICAL SIMULATIONS

II. Simulations: how to proceed ?

STRUCTURATION: INHOMOGENEOUS UNIVERSE

- Scalar perturbation of FRW metric in newtonian gauge

$$ds^2 = -c^2 dt^2 \left(1 + 2\frac{\psi}{c^2}\right) + a^2 \left(1 - 2\frac{\phi}{c^2}\right) \left(\frac{dr^2}{1 - kr^2} + r^2 d\theta^2 + r^2 \sin(\theta)^2 d\phi^2\right)$$

- Geodesics equations+ Poisson equation

Chisari&Zaldarriaga, 2011
Adamek et al, 2016

$$\frac{d^2 \mathbf{x}}{d\eta^2} + \frac{a'}{a} \frac{d\mathbf{x}}{d\eta} = -\nabla\phi + \cancel{3\phi' \frac{d\mathbf{x}}{d\eta}}, \quad d\eta = \frac{dt}{a}$$

$$\Delta\phi = 4\pi G a^2 \bar{\rho} \delta + 3 \frac{a'}{a} \left(\cancel{\phi'} + \cancel{\frac{a'}{a} \phi} \right)$$

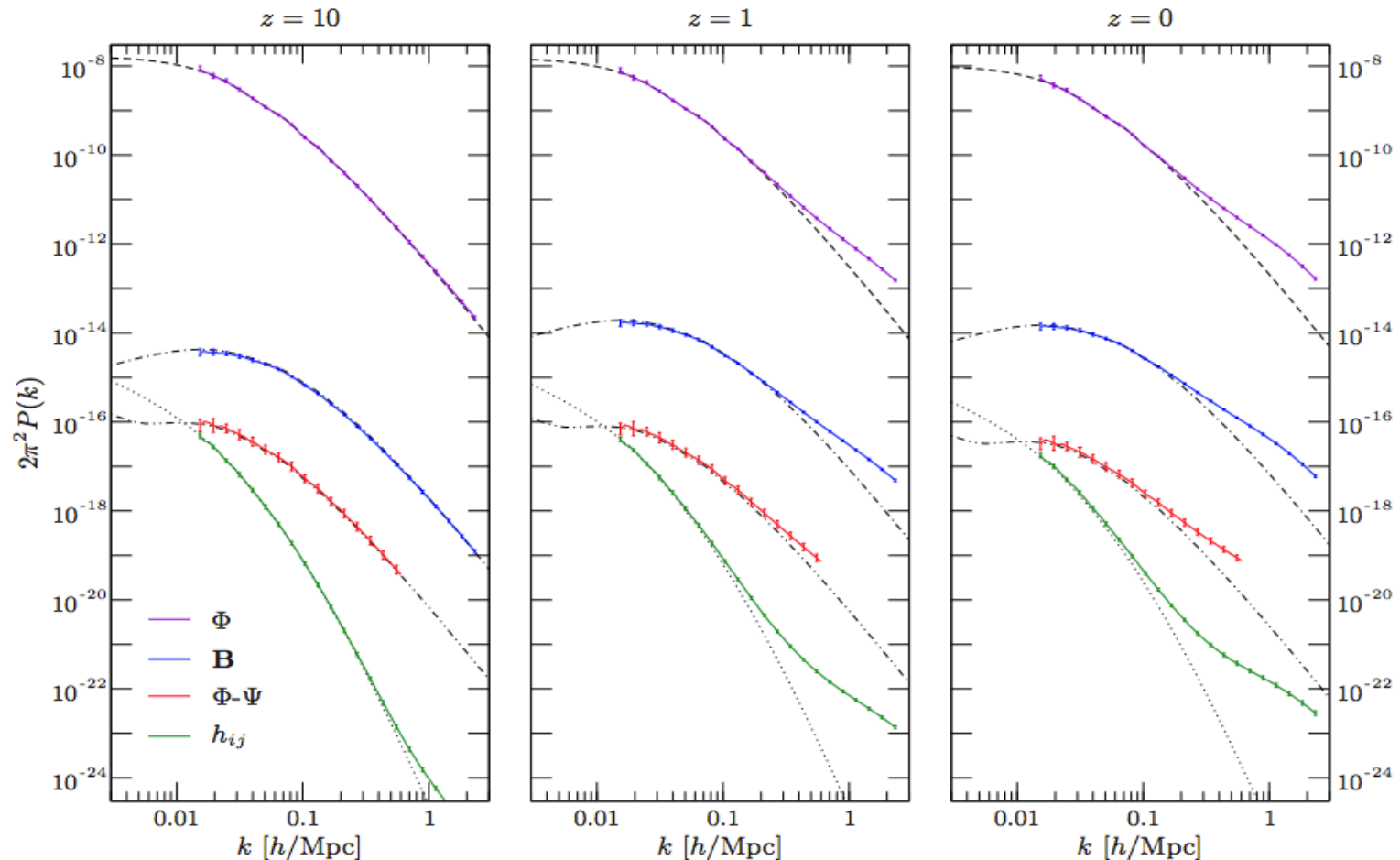
- Evolution equation: Boltzmann equation in an expanding universe

$$\frac{\partial f}{\partial t} + \frac{\mathbf{p}}{ma^2} \cdot \nabla f - m \nabla \Phi \cdot \nabla_{\mathbf{p}} f = \left(\cancel{\frac{\partial f}{\partial t}} \right)_{\text{coll}} \quad \mathbf{p} = ma^2 \dot{\mathbf{x}}$$

Collisionless
Dark Matter

SHOULD WE CARE ABOUT RELATIVISTIC EFFECTS FOR THE DYNAMICS ?

Adamek,
Daverio,
Durrer &
Kunz, 2016



- ⇒ Relativistic effects seem (a priori) weak for the dynamics.
- ⇒ See the talk of N.Kaiser for the question of backreaction which is related
- ⇒ Special care: all of this was done in the weak field approximation + in Poisson Gauge + at finite resolution + in LCDM + with no neutrino + torus topology

- **Main approaches**

- Solving the N-body pb for all single particles of DM => not tractable because $N_{\text{DM}} > 10^{30}$
- Solving the equation in 6D with a grid method (Yoshikawa et al, 2013) => very intense
- Solving in 6D but taking advantage that the phase space is mostly empty (Hahn et al, 2013; Sousbie&Colombi 2016) => very accurate but still intense
- Fluid approach => the hierarchy of moments never stops
- Sampling the phase space with particles (i.e. this is a Monte Carlo method) => N-Body approach, widely used because good compromise between accuracy/simplicity/speed. Be careful each particle represents a “cloud” of DM particles not a single DM particle!

- **N-body approach**

- PP approach => too slow $O(N^2)$ operations
 - PM approach => use a fixed grid to compute Poisson : $O(N \ln N)$ but fixed resolution
 - Tree code => use group of particles to compute the force from far away particles (example PKDGRAV, HOT)
 - PM-AMR => PM but with adaptive grid (example RAMSES, ART, ENZO)
 - Various hybrid methods such as TreePM (example GADGET, TPM)
- => in any case $O(N)$ or $O(N \ln N)$ + adaptive resolution

The example of RAMSES (Teyssier, 2002)

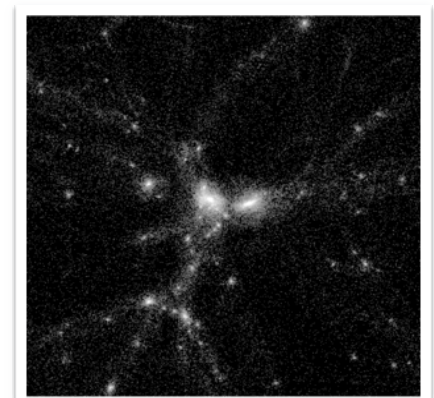
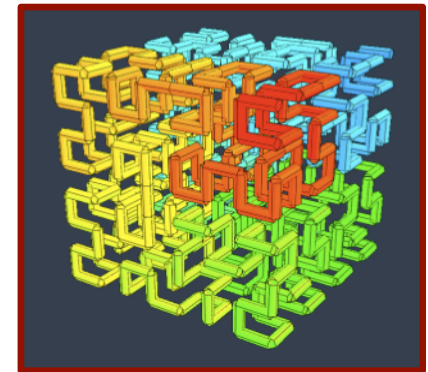
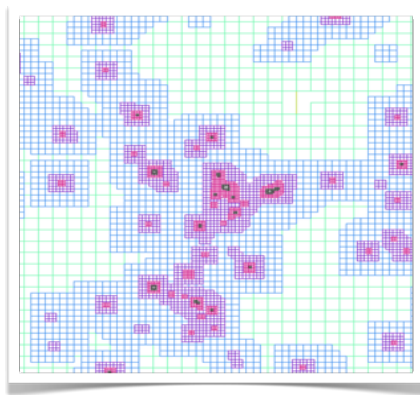
=> PM – AMR method

• Purpose

- Compute the formation of large scale structures in an expanding universe
- Ingredient : dark matter
- Good force resolution thanks to a hierarchy of AMR grids
- Overdensity based refinement criterion: pseudo-lagrangian approach
- Parallelized with MPI using a Peano-Hilbert domain decomposition

• Physics/Methods

- Expansion rate: use of supercomoving coordinates
- Periodic boundary conditions
- N-Body solver: Particle-Mesh
- Density: Cloud in Cell
- Poisson equation: solved by multigrid method (Guillet&Teyssier)
- Time-step: adaptive

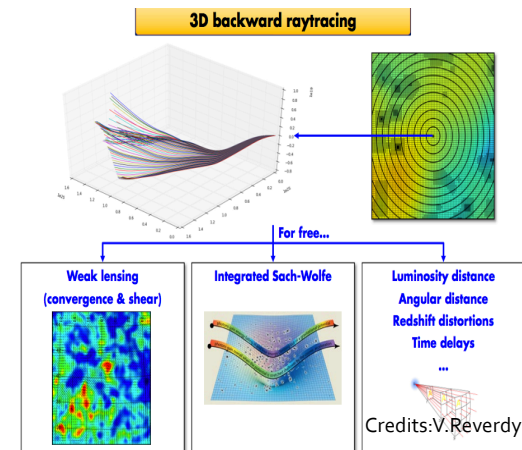
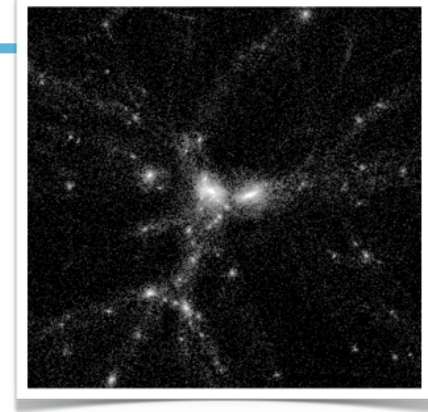


Taking into account dark energy dynamics (non exhaustive)

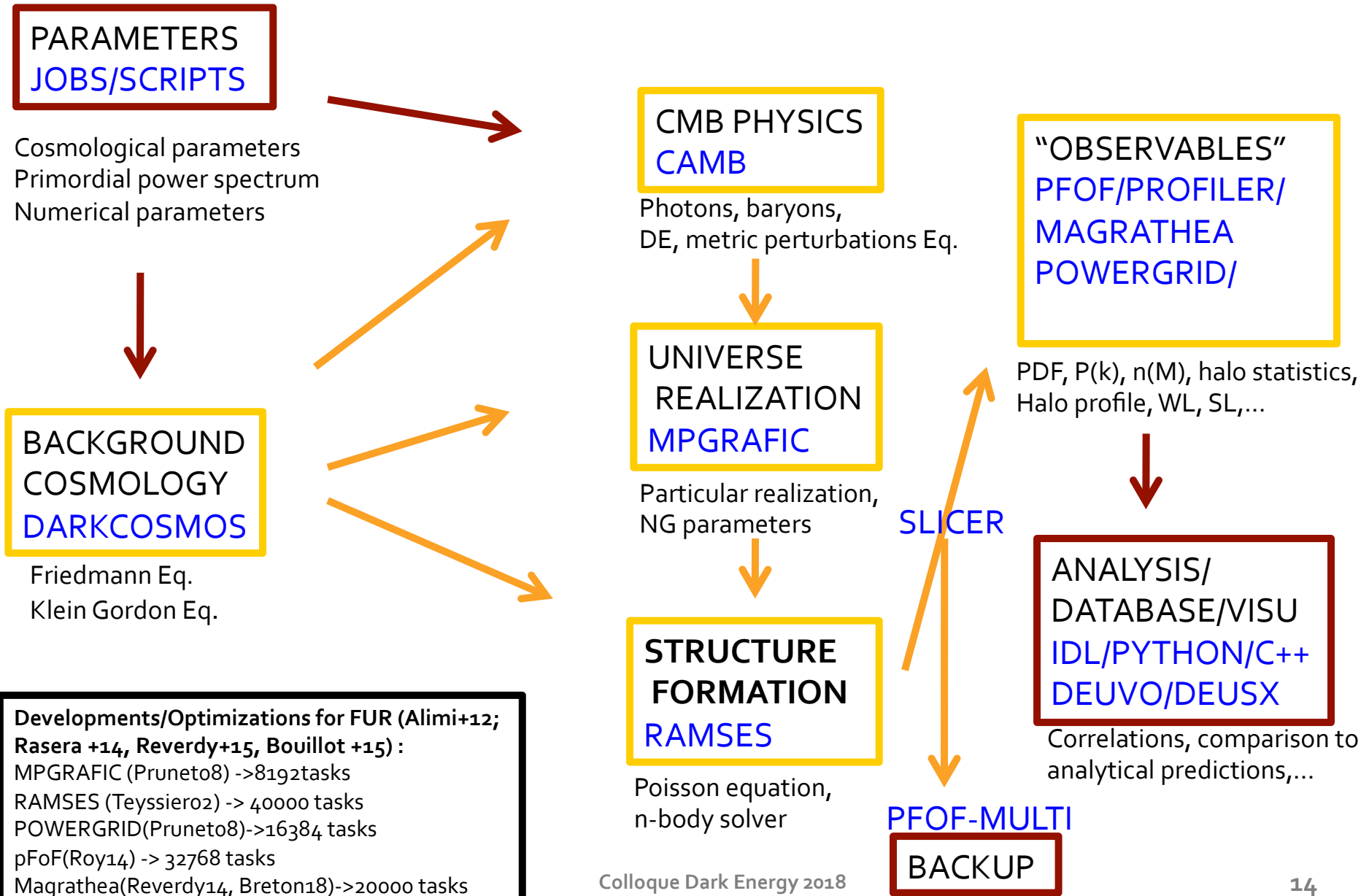
- **Lambda**
 - Dark energy density is a constant in space and time
 - Sim examples: many, not the goal of this talk
- **W and (Wo-Wa) parameterization**
 - Minor-modification of FLRW equations
 - Sim examples: Coyote Universe, Abacus cosmos, Full Universe Run,...
- **Minimally coupled dark energy (quintessence or similar)**
 - Solve Klein Gordon equation for scalar fields => change background expansion and linear calculation (CAMB, CLASS) because quintessence doesn't collapse.
 - Sim example: Dark Energy Universe Simulation Series, Full Universe Run, Codecs,...
- **Coupled dark energy**
 - G is changed as well as the effective mass of DM particles
 - Sim Examples: Codecs, sim by Maccio et al, 2004,...
- **Modified gravity (scalar tensor or similar)**
 - Need to solve a non-linear Poisson equation (cannot use FFT for example) for the scalar field
 - Sim examples (using parallel code with adaptive resolution): f(R) (Li et al, 2012; Puchwein et al, 2013; Llinares et al, 2014), DGP (Li et al, 2013), Galileon (Li et al, 2013), Symmetron (Llinares & Mota 2013; Llinares 2014),....

Don't forget initial conditions generation and post-processing: these are critical and heavy steps

- **Initial condition generators**
 - Assume gaussian random field
 - Use of Lagrangian Perturbation theory
- **Structure finder (halo, voids)**
 - Use local or enclosed overdensity to define group of particles
- **Dark matter to light connection (depend on the source):**
 - Dark matter: DM emission
 - Galaxies: Abundance matching, Halo occupation distribution, SAM, hydro simulations
 - Lyman-alpha: probabilistic approach, ...
- **Ray-tracer**
 - Launch light-rays to replace structures in redshift space
 - Weak-lensing, Redshift Space Distortions
- **Estimator of the 2/3/4 points correlation function (power spectrum/bispectrum/trispectrum)**
 - Pair counts
 - Grid method
 - Fourier method



Our cosmological pipeline as an example

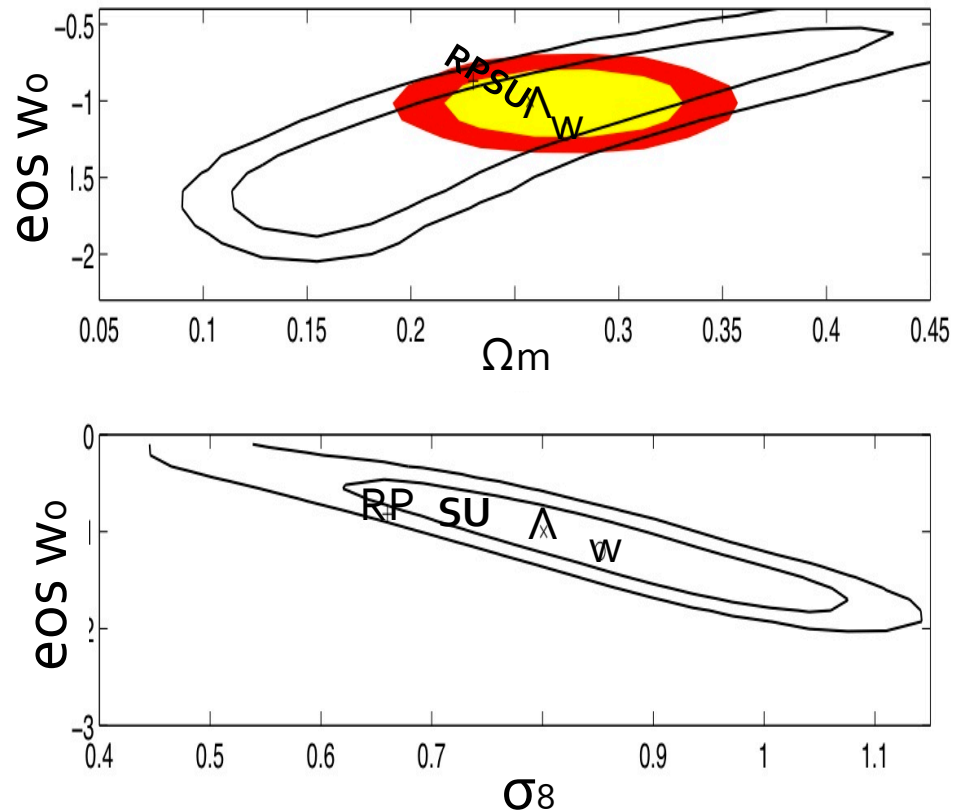


III What kind of results? Illustrative example about the imprints of minimally coupled dark energy on *cosmic structure formation*

COSMOLOGICAL MODELS

REALISTIC DARK ENERGY MODELS

- **4 DE models**
 - Λ -CDM ($w=-1$)
 - Quintessence model with Ratra-Peebles potential RP-CDM ($w(z)>-1$)
 - Quintessence model with SUGRA potential SU-CDM ($w(z)>-1$)
 - Ghost model w -CDM ($w=-1.2$)
- **Pre-selection of viable dark energy models:**
 - Likelihood analysis of the combined SNIa UNION dataset and WMAP7-years data
 - CAMB modified to take into account quintessence clustering
- **Varying the equation of states implies:**
 - lower matter density for larger w
 - lower amplitude of power spectrum for larger w



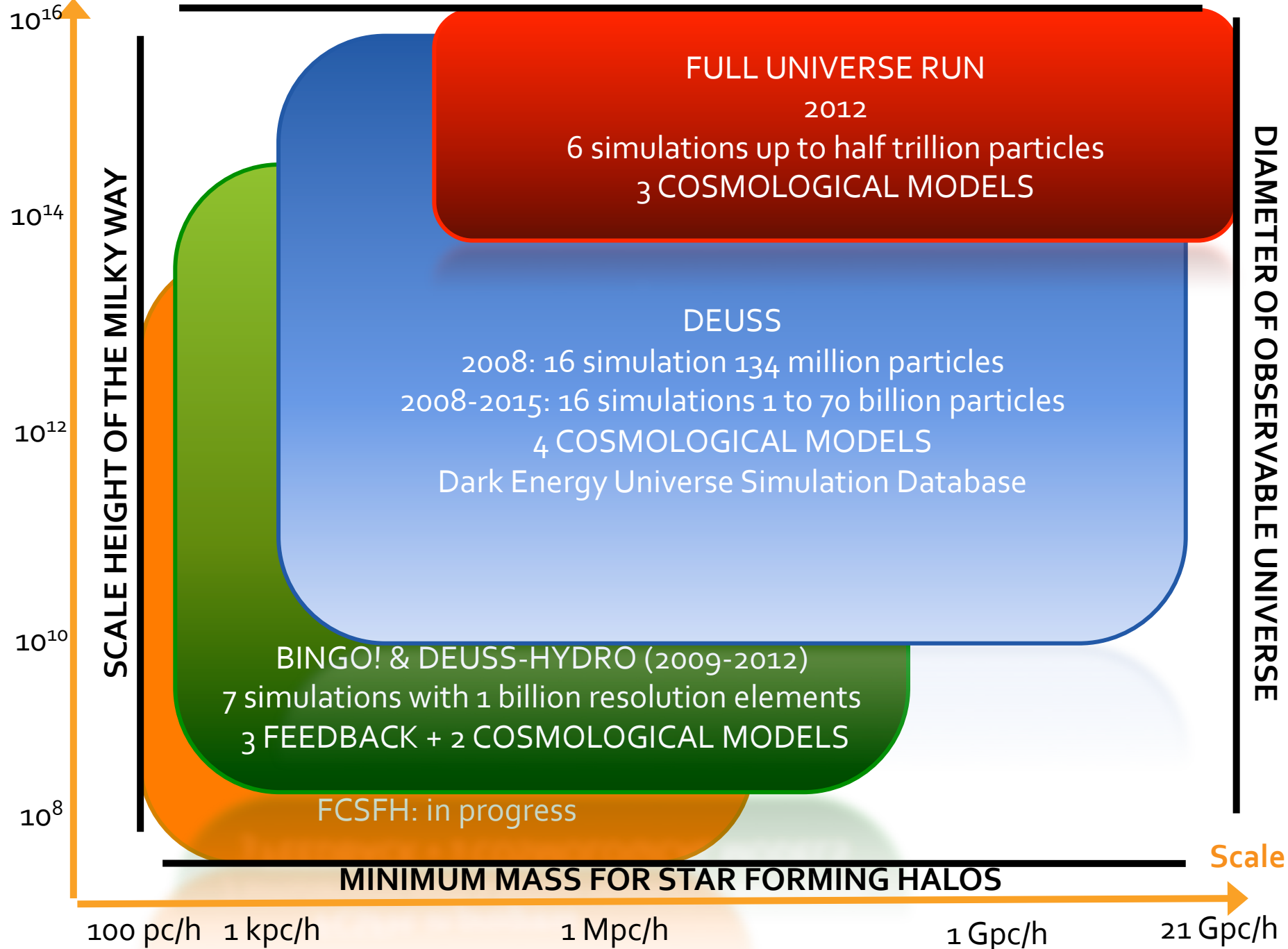
Halo mass (M_{sun}/h)

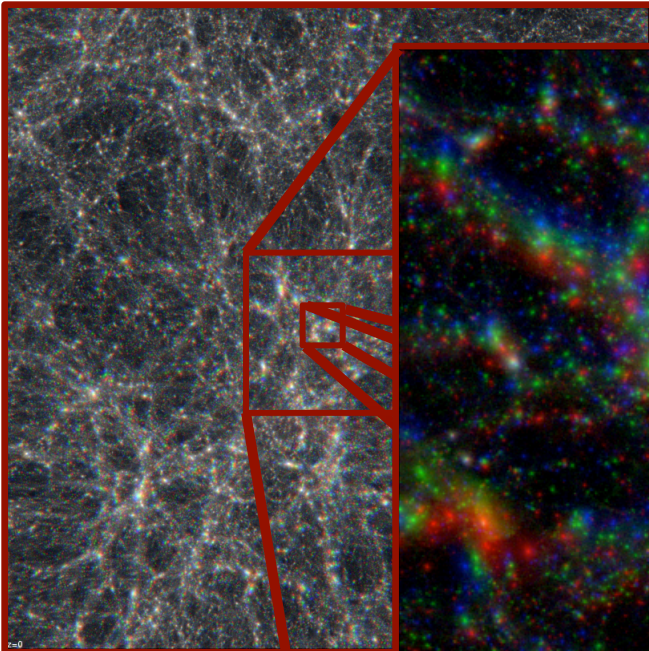
MOST MASSIVE HALO OF THE UNIVERSE



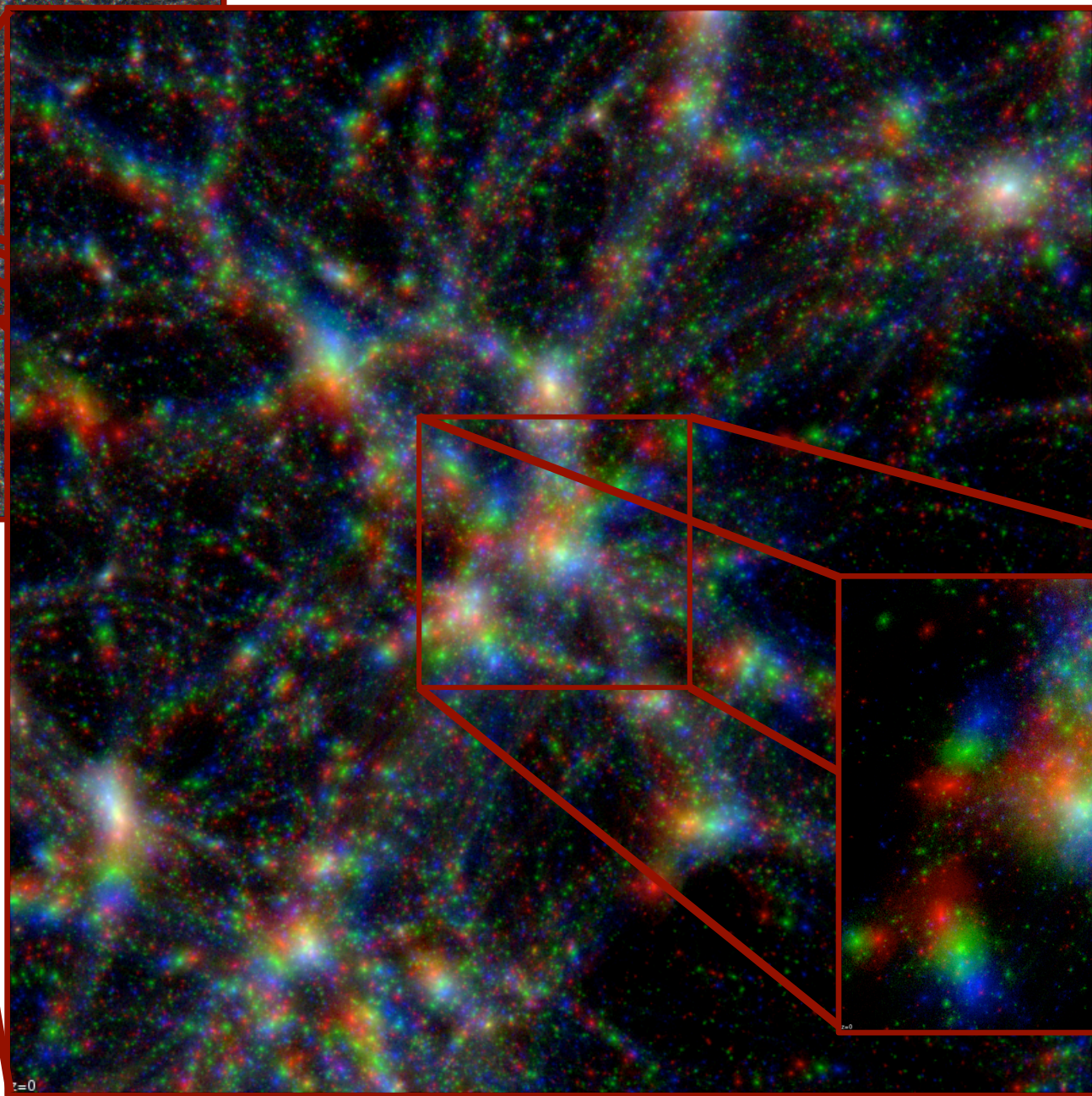
Halo mass (M_{sun}/h)

MOST MASSIVE HALO OF THE UNIVERSE

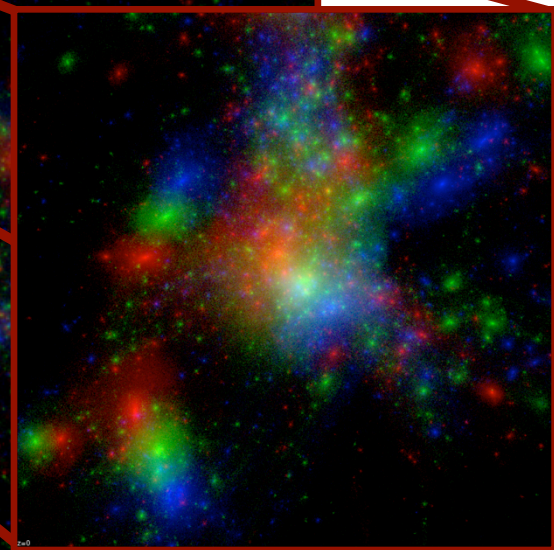




225 Mpc



56 Mpc



14 Mpc

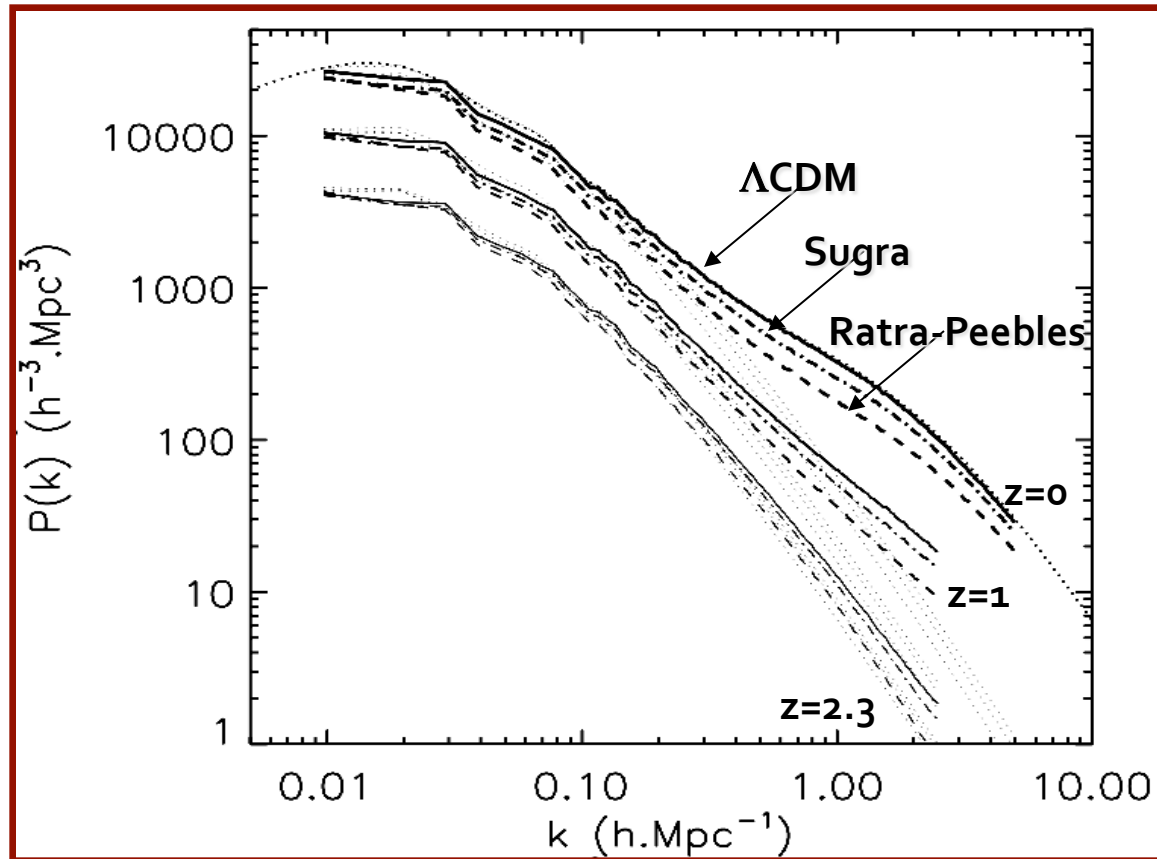
Λ CDM
Sugra
Ratra-Peebles

DEUSS

IMPRINTS OF DE ON THE MATTER POWER SPECTRUM

Power spectrum
estimator: POWMES
(Colombi et al, 2009)

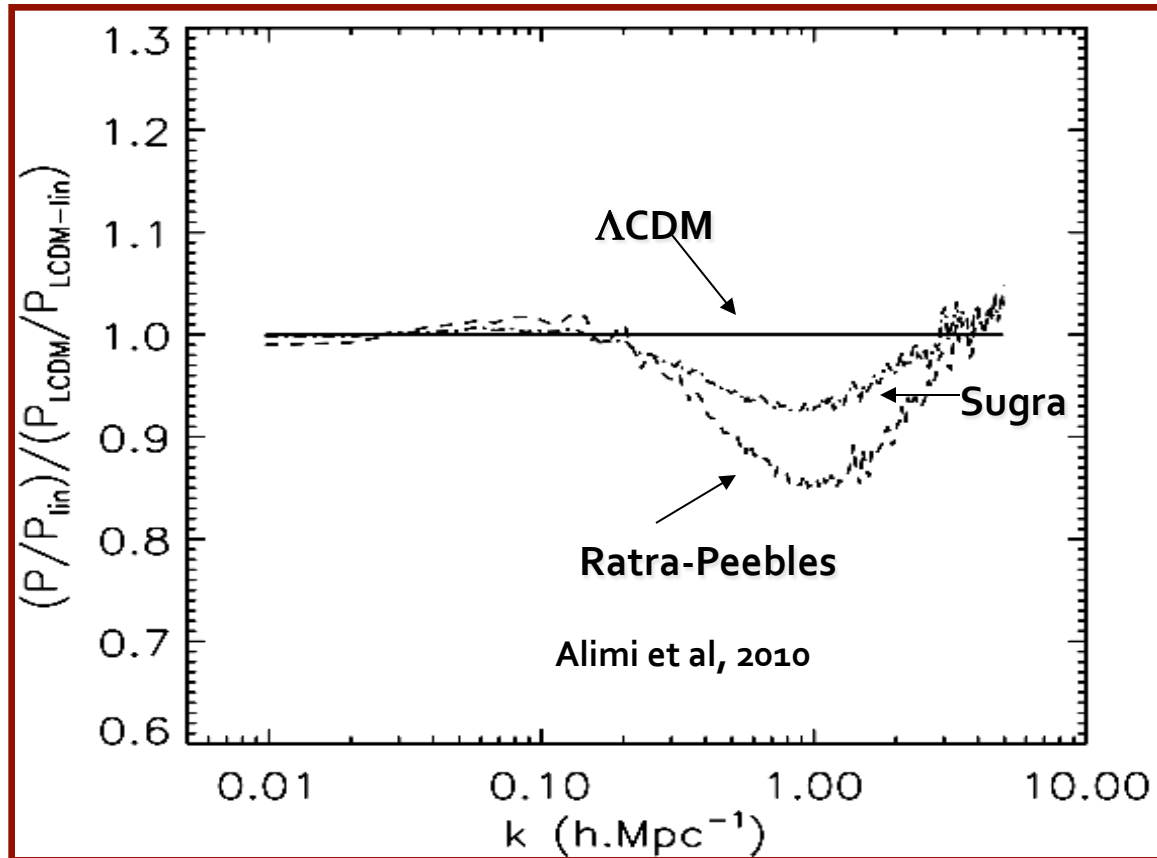
3 cosmologies are in
good agreement
with SDSS



- **GOAL:** isolate contributions to the non-linear matter power spectrum
- **First (linear regime):** linear power spectrum normalization and shape

IMPRINTS OF DE ON THE MATTER POWER SPECTRUM

Let's remove the
linear contribution
and take Λ CDM as a
reference



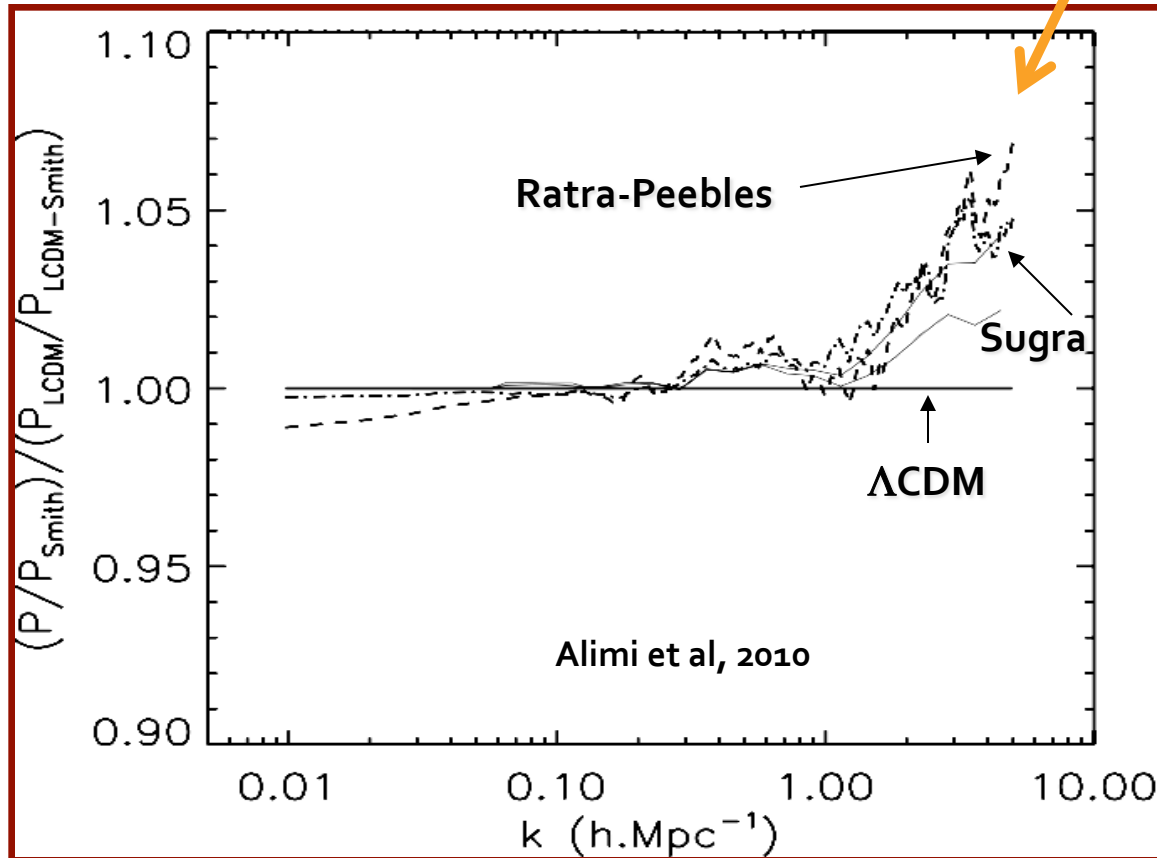
- **Second contribution (quasi-linear regime):** non-linear amplification of linear growth rate
- **Third contribution (sable-clustering regime):** saturation-virialization

IMPRINTS OF DE ON THE MATTER

POWER SPECTRUM

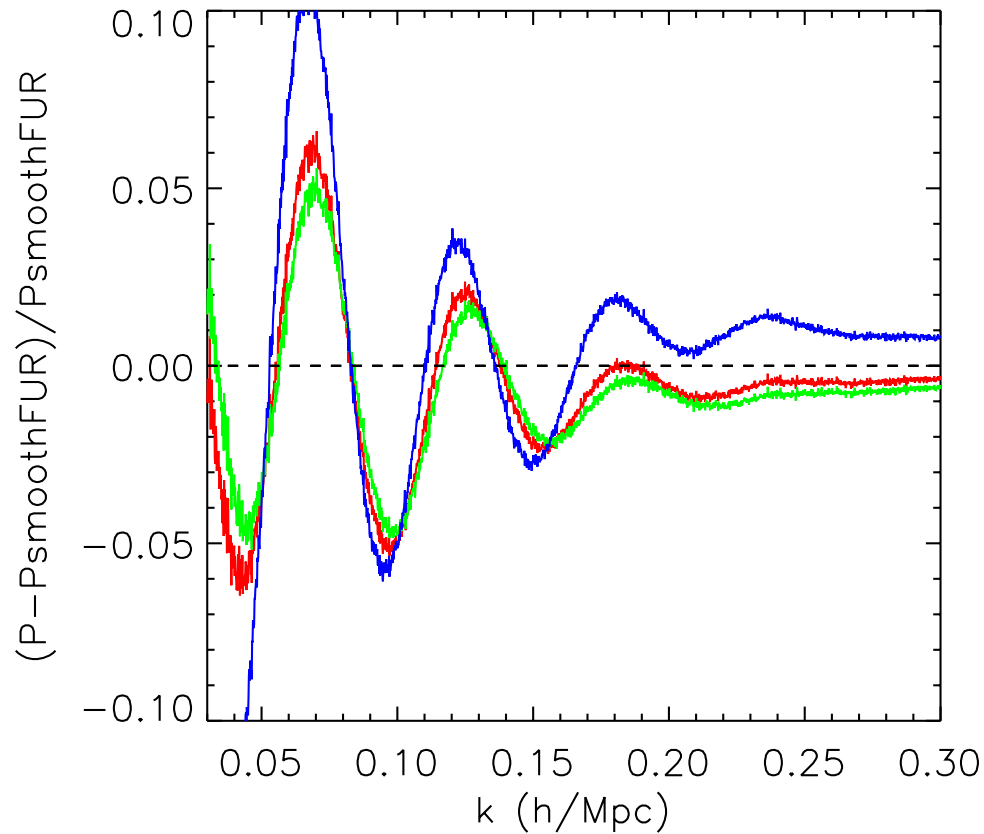
HALO SCALE

Let's remove
previous
contributions:
normalization by
Smith et al, 2003



- Deviations from self-similar predictions
- Flaw: Most of the current predictions are instantaneous
- **Fourth contribution** : history of structure formation

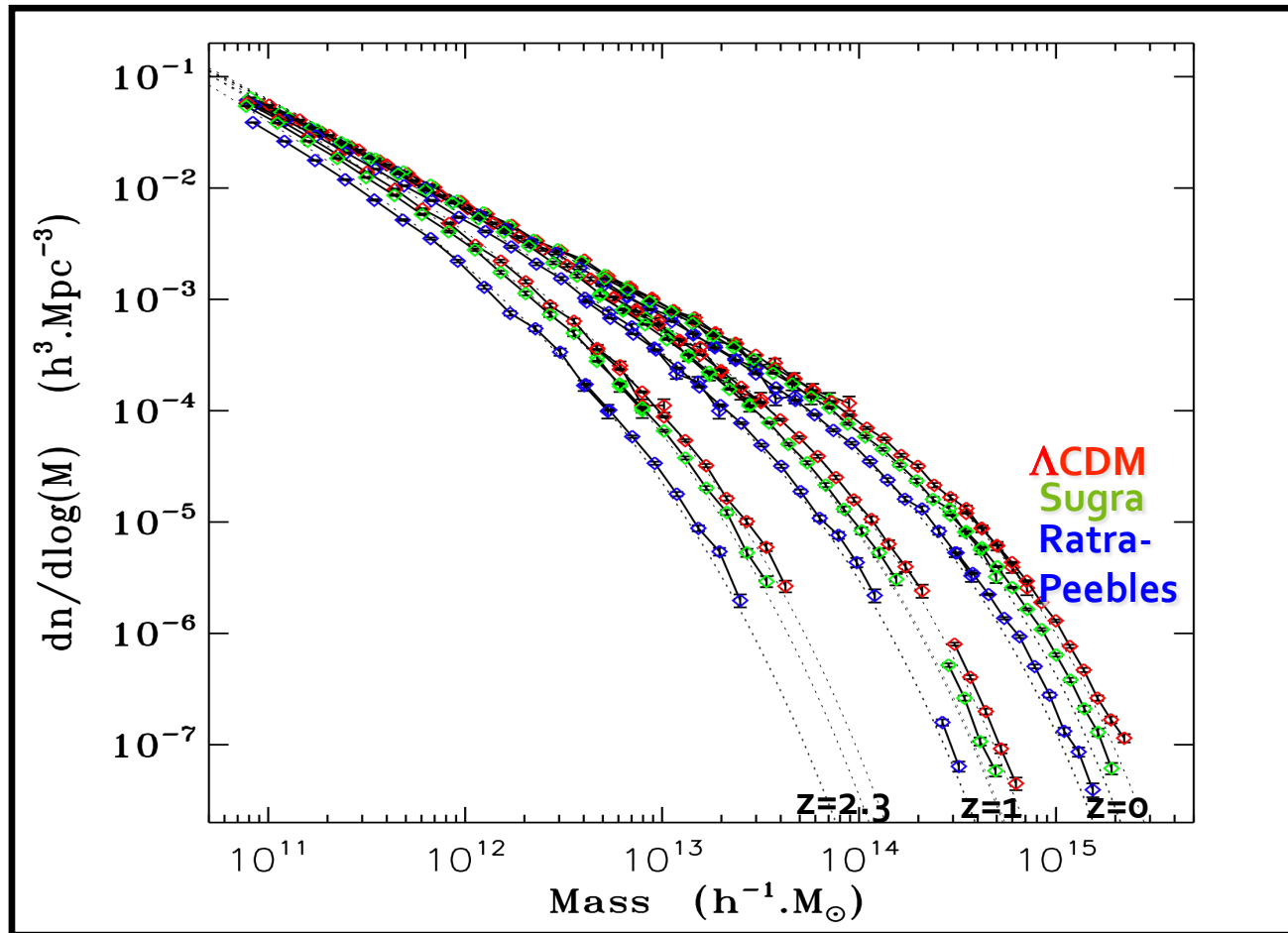
IMPRINTS OF DE ON BAO



From Full
Universe
Run

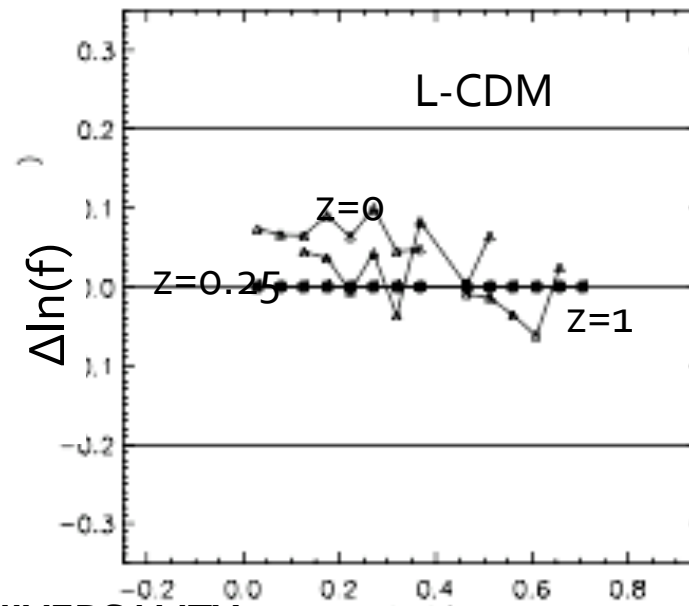
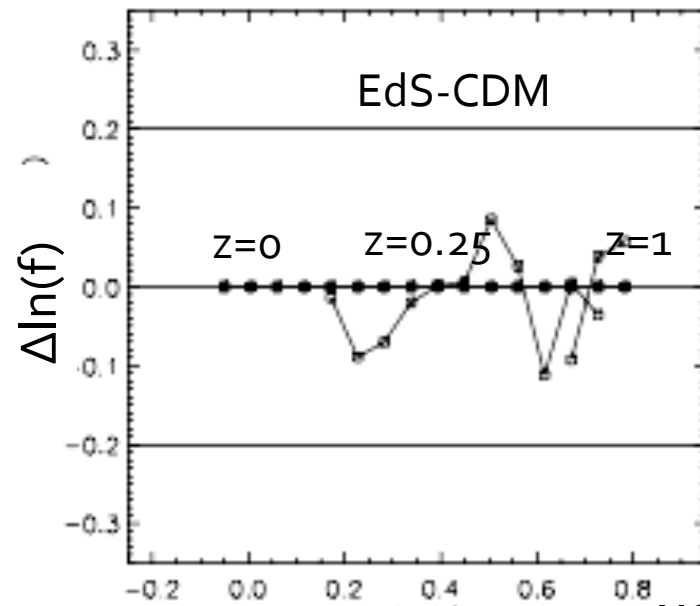
- Non trivial shift, damping, tilt...

IMPRINTS OF DE ON THE HALO MASS FUNCTION



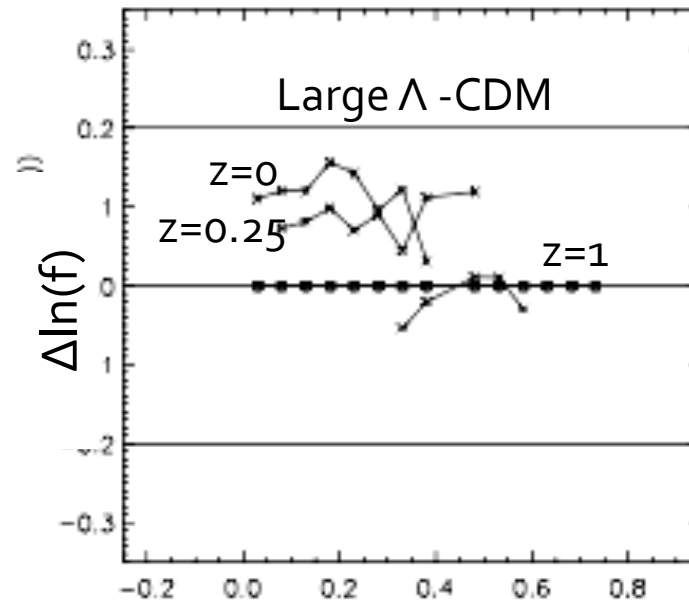
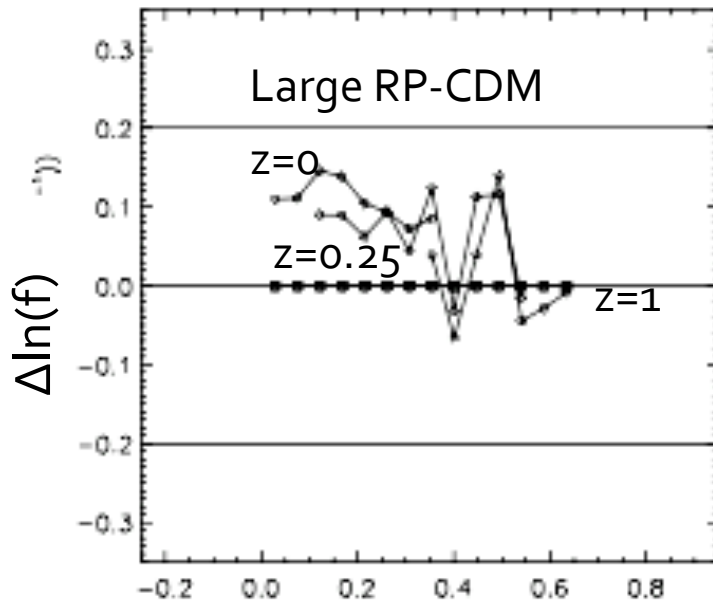
- DE changes the amplitude and shape of the mass function dn/dM

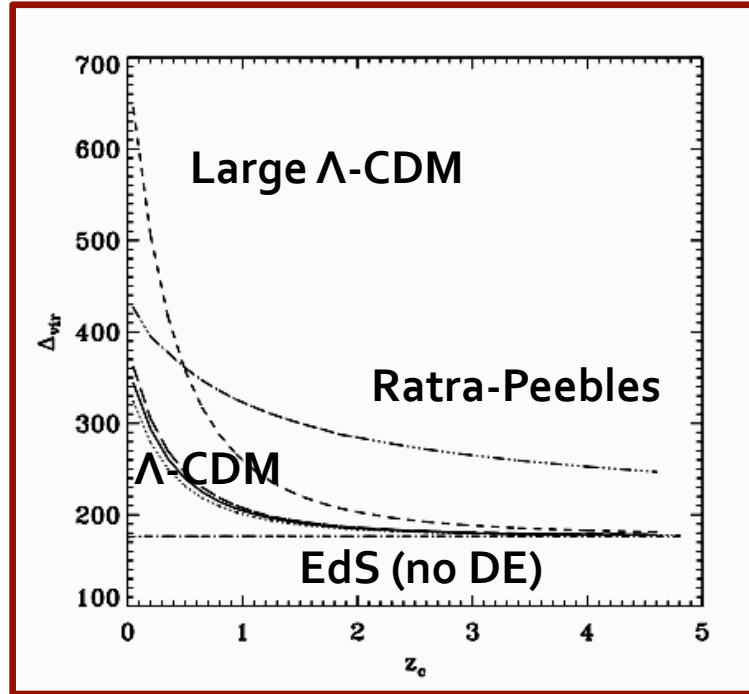
- DE changes the multiplicity function $f(\sigma, z; X) \equiv \frac{M}{\rho_0} \frac{dn_X(M, z)}{d \ln \sigma^{-1}}$



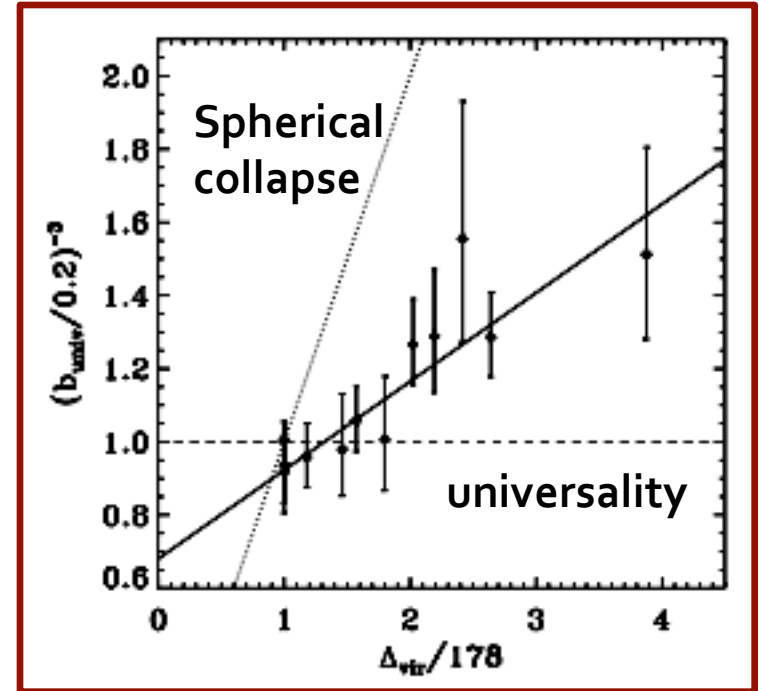
**NON UNIVERSALITY
RELATED TO DARK ENERGY**

**Courtin
et al 2011**





redshift



Virial overdensity from spherical collapse

NON-UNIVERSALITY

The halo mass function at $z=0$ does depend of the underlying dark energy model.

Deviations below 20% are **NEW PROBES FOR DARK ENERGY!!!**

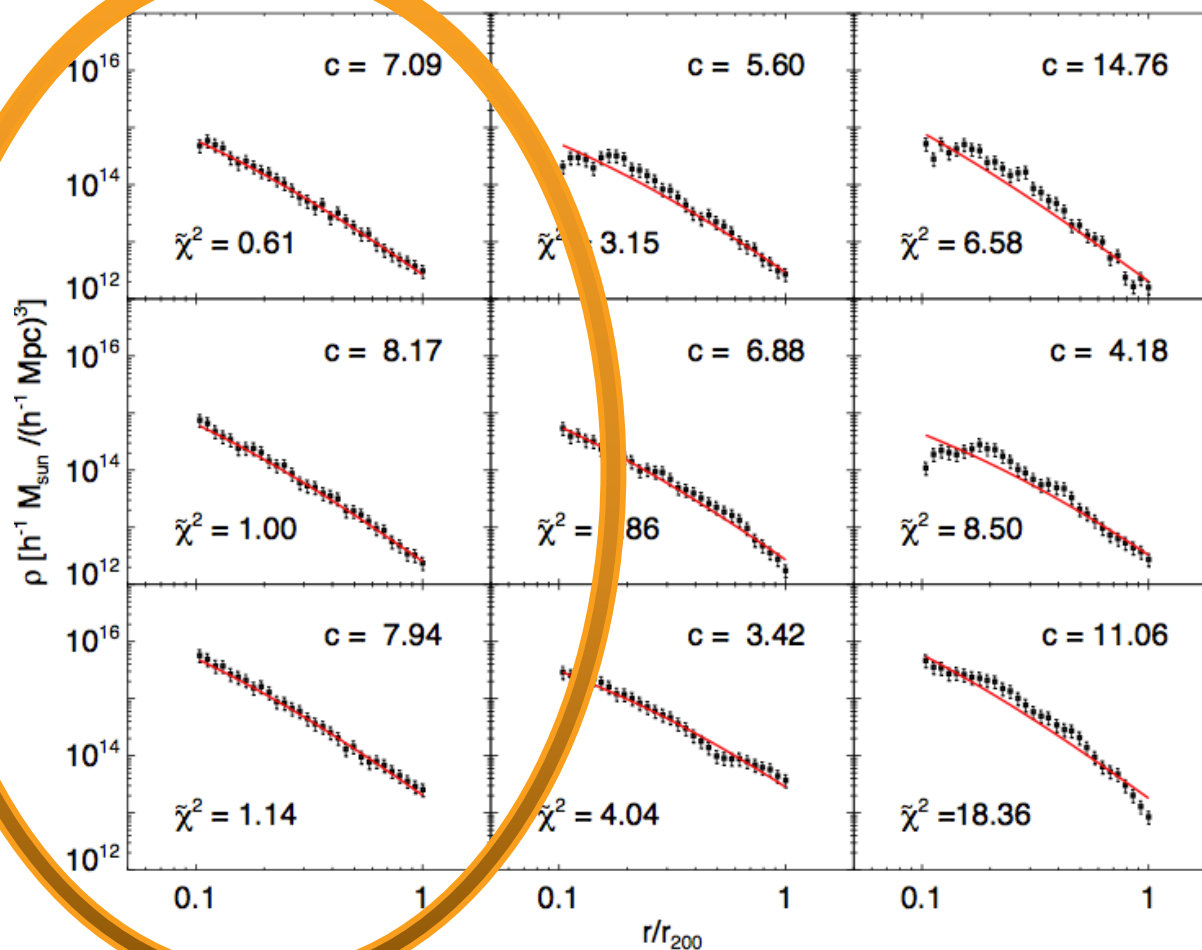
They depend on the amount and equation of state of dark energy.

The mass function can be predicted at the 5% level.

Rem: different from "non-universality" in Tinker et al, 2008 which is related to SO halo finder

3D DENSITY PROFILE

$$\text{NFW fit } \rho_{\text{NFW}}(r) = \frac{M_{200}}{4\pi[\ln(1+c) - c/(1+c)]} \times \frac{1}{r \left(\frac{r_{200}}{c} + r \right)^2}$$



IMPRINTS OF DE ON DM HALO PROFILE

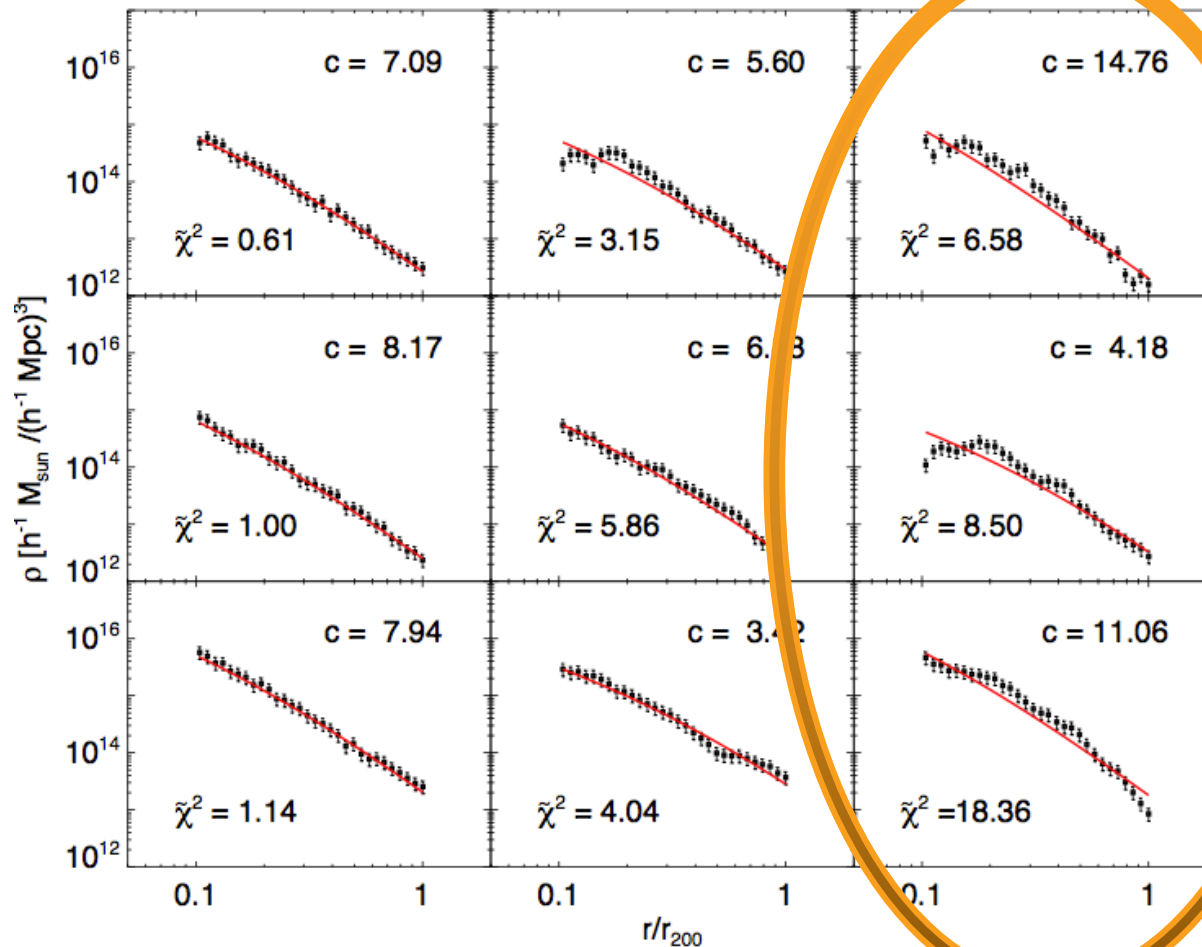
cosmology	$\frac{c_0}{c_0^{\Lambda\text{CDM}}}$	$\frac{D_+(\infty)}{D_+^{\Lambda\text{CDM}}(\infty)}$	$\frac{D_+(z_{\text{coll}})}{D_+^{\Lambda\text{CDM}}(z_{\text{coll}})}$
ΛCDM	1	1	1
RP	1.06 ± 0.011	1.07	1.07 ± 0.0003
SUGRA	1.16 ± 0.013	1.22	1.19 ± 0.004
DECDM	1.18 ± 0.013	1.19	1.18 ± 0.001
OCDM	1.49 ± 0.018	1.64	1.61 ± 0.01

Dolag et al, 2004

- PRO: interesting correlation between concentration and linear growth rate history (Dolag et al, 2004) or mass accretion history (Zhao et al, 2009 and references therein)
- CON: use a small sub-sample of all halos OR select relaxed halos OR use median
- CON: sensitive to the details of fitting procedure

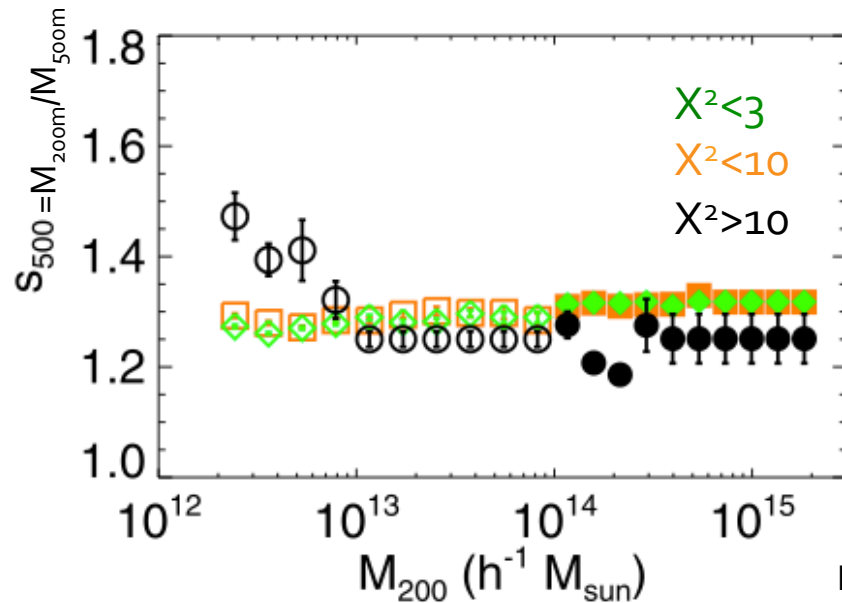
3D DENSITY PROFILE

$$\text{NFW fit } \rho_{\text{NFW}}(r) = \frac{M_{200}}{4\pi[\ln(1+c) - c/(1+c)]} \times \frac{1}{r \left(\frac{r_{200}}{r} + 1 \right)^2}$$

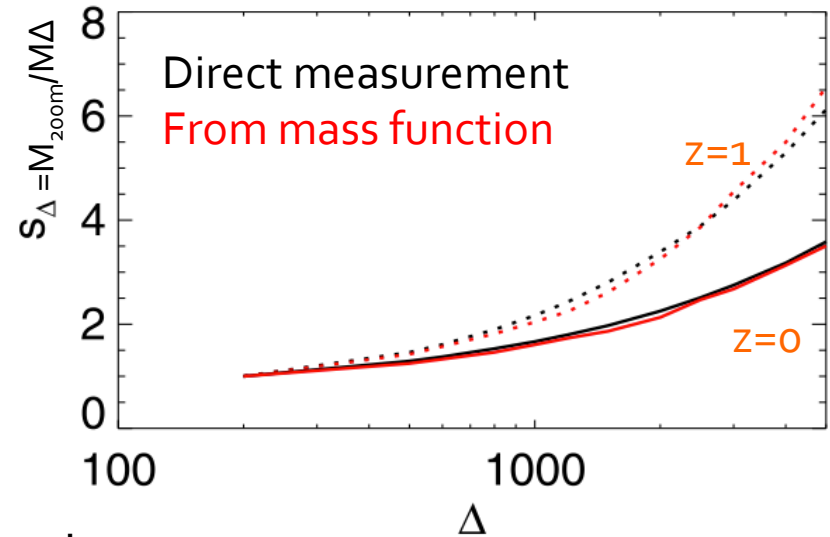


- A fraction of halos density profile are not well fitted by simple function form (such as Navarro-Frenk-White (NFW) formula)
- This fraction depends on cosmology => informations are lost

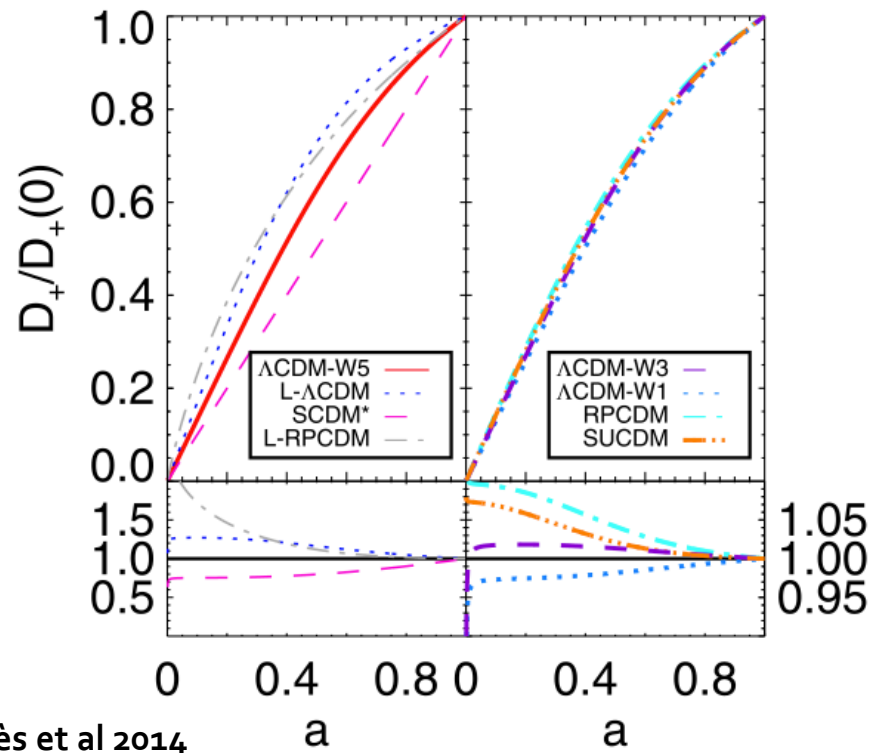
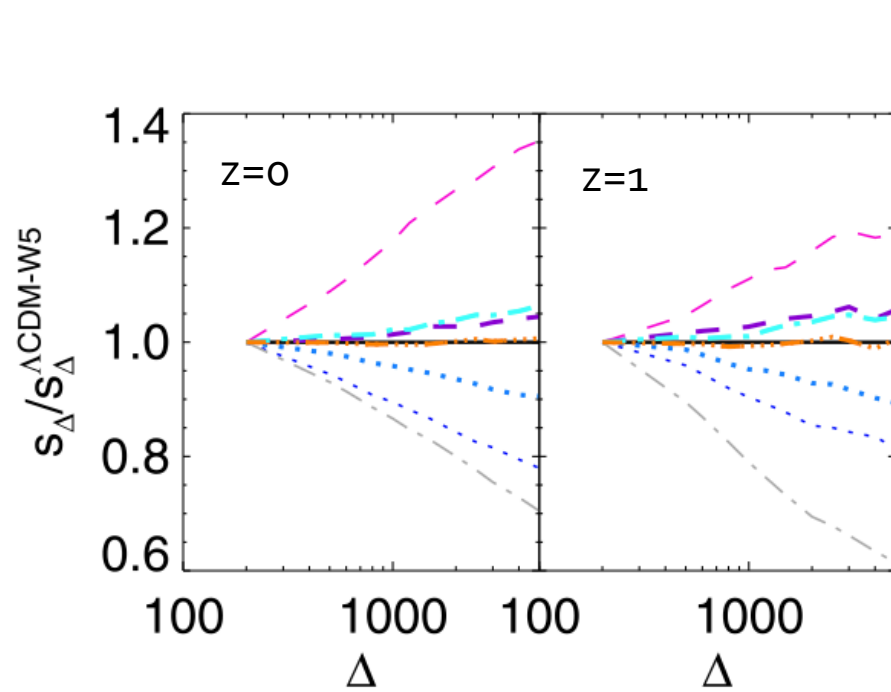
NICE PROPERTIES OF "SPARSITY"



Balmès et al 2014

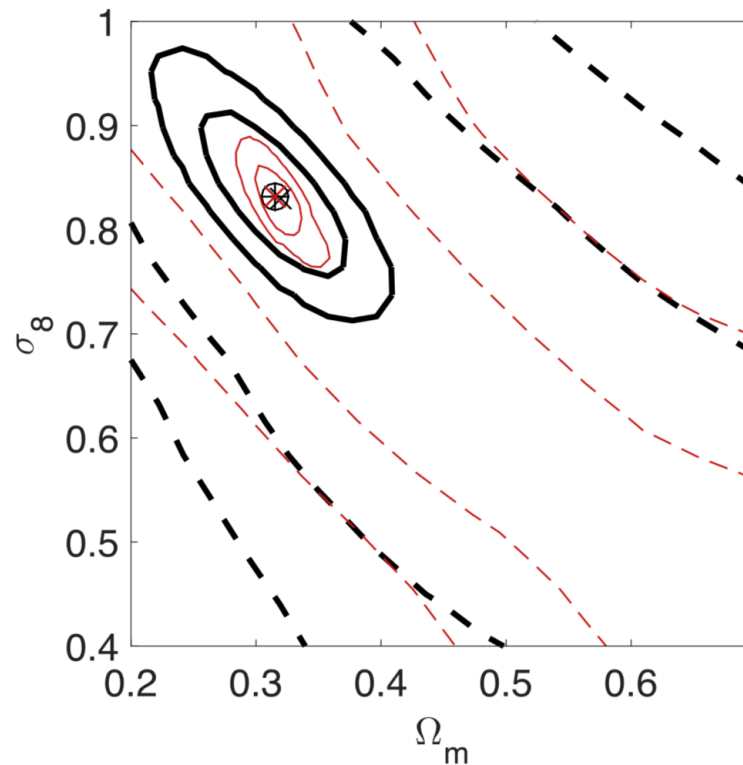


- Non-parametric measure of the profile -> SPARSITY: $s_{\Delta_1 \Delta_2} \equiv \frac{M_{\Delta_1}}{M_{\Delta_2}}$
- Nice properties: very weak dependance on mass
- Direct link with the mass function: $\int_{M_2}^{M_1} \frac{dn}{d \ln M_{\Delta}} \frac{d \ln M_{\Delta}}{M_{\Delta}} = \langle s_{\Delta} \rangle \int_{\langle s_{\Delta} \rangle M_2}^{\langle s_{\Delta} \rangle M_1} \frac{dn}{d \ln M_{200}} \frac{d \ln M_{200}}{M_{200}},$
- No fitting procedure : only 2 points needed!



Balmès et al 2014

- Generalization of the result to the average « sparsity » (ie average profile) of all halos
- More robust: non parametric



Corasaniti et al, 2017

- Black lines: 1 and 2-sigma contours assuming 1% (continuous) and 20% (dashed) average error on sparsity
 => profile of dark matter halos can be a probe of the dark energy

V/ Conclusion and perspective

•Main questions

- What is the nature of dark energy? => Many possibilities.
- New or refined probe in non-linear regime? => simulations
- Sims: Bridge between theory/analytical models/observations

•Simulations

- Weak-field + collisionless Boltzmann => Vlasov Poisson
- N-body approach
- Importance of initial conditions generation, halo detection, ray-tracer, etc.

• Simulated models

- Λ CDM, w CDM, quintessence, coupled dark energy models
- $f(R)$, scalar tensor
- Still very limited compared to the gigantic space of possibilities

• Imprints of minimally coupled dark energy on cosmic structures

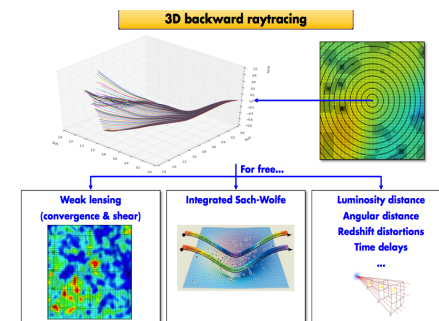
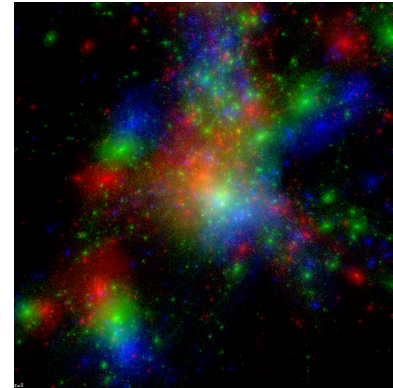
- Choice of “realistic” models (Viable/Solar system/GW/CMB/SNIA)
- Power spectrum+Mass function+Halo profile
- Weak Lensing, Redshift Space Distortion (on going Breton+18)

• Imprints of other dark energy models on cosmic structure

- Similar philosophy but specific signatures=> vast literature

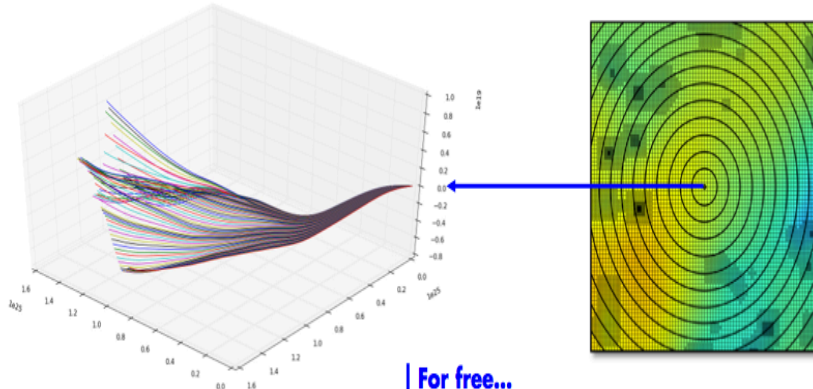
•Future:

- Larger and/or more resolved sims
- Wider class of DE models
- Baryon effects
- New observables and observational constraints



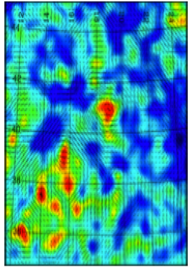
TOWARDS NEW PROBES OF THE DARK SECTOR

3D backward raytracing

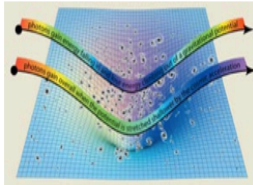


For free...

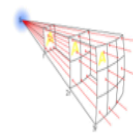
Weak lensing
(convergence & shear)



Integrated Sachs-Wolfe



Luminosity distance
Angular distance
Redshift distortions
Time delays
...



RAYGALGROUPSIMS
LIGHTCONES

ZMAX=10
400 deg²

ZMAX=2
2500 deg²

ZMAX=0.5
Full sky

ONION SHELLS
+
AMR
+
GRAVITY
+
TIME DERIVATIVE

- Various applications of our relativistic ray-tracer Magrathea (Reverdy 2014; Breton et al, 2018)
 - **Relativistic halo catalogs (RSD, WL, etc) from RayGalGroupSims simulation now available**
 - WCDM sim is on going
- => FEEL FREE TO ASK QUESTION TO MICHEL-ANDRES BRETON WHO IS HERE