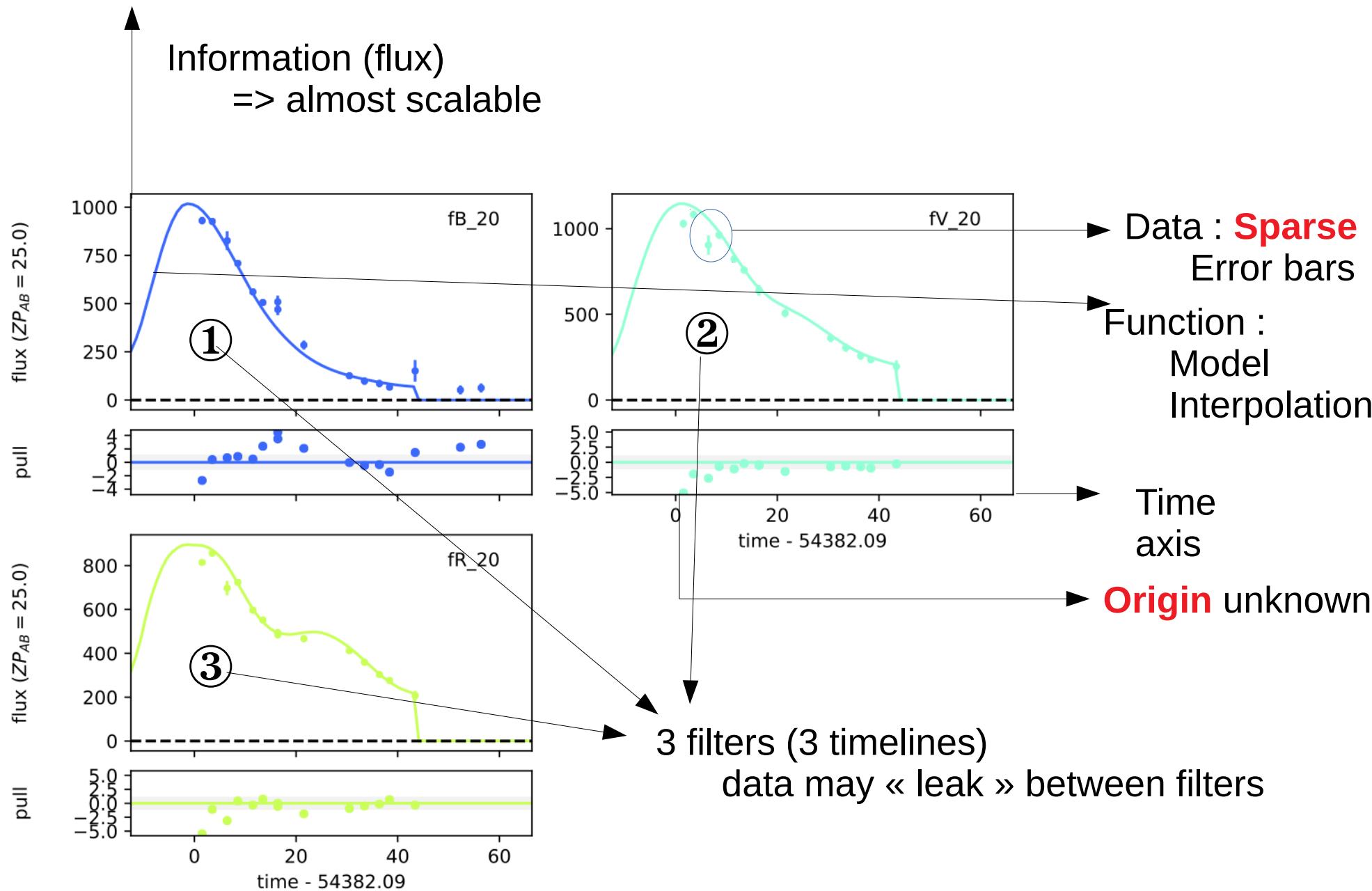


Time Series

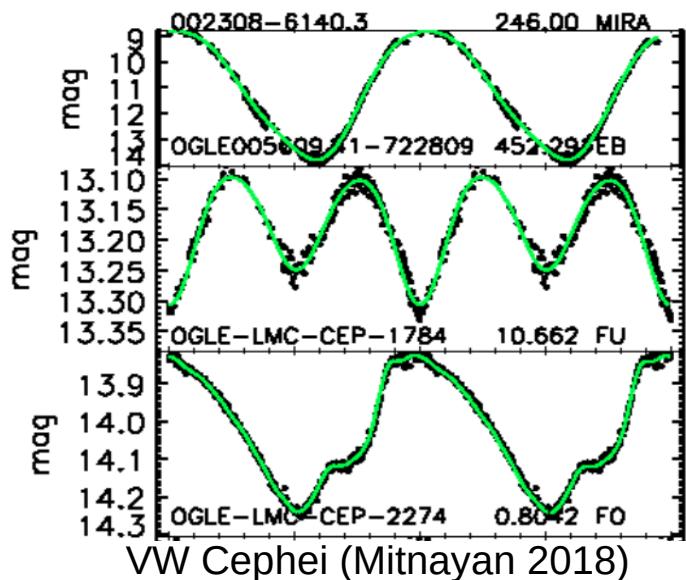
An ~~astronomer~~ personal view ...

« time » series



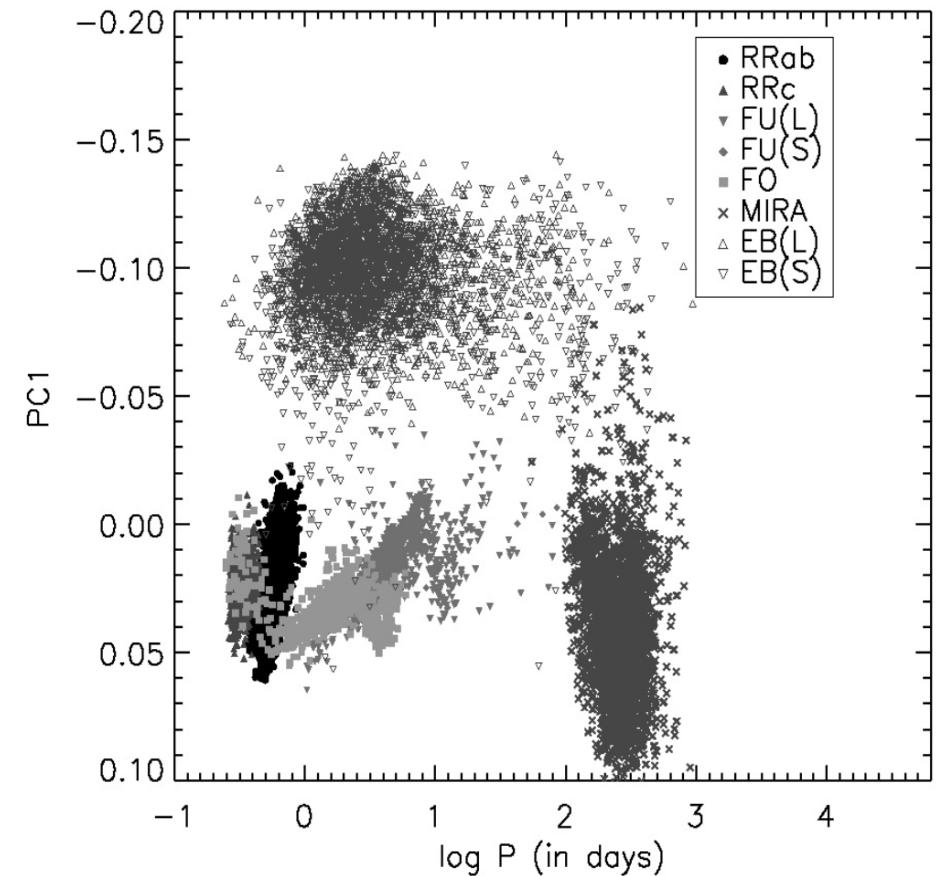
Different time series

Periodic



Fourier Transform

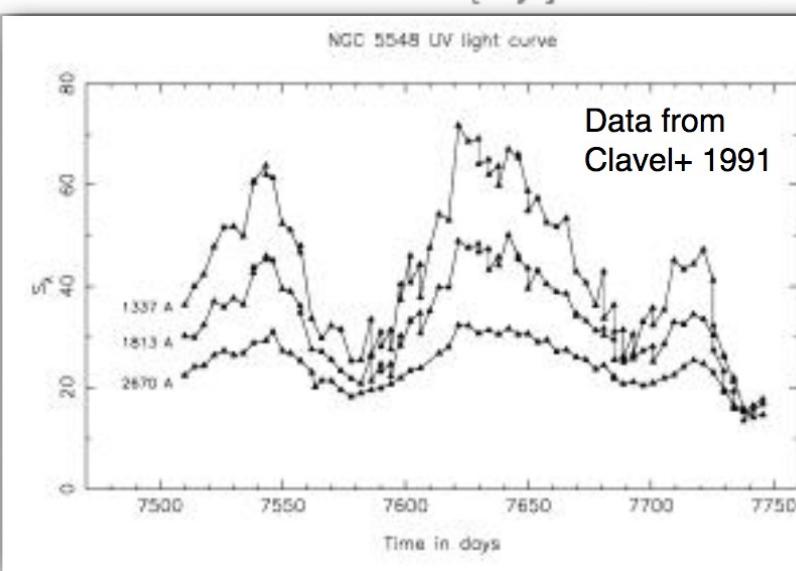
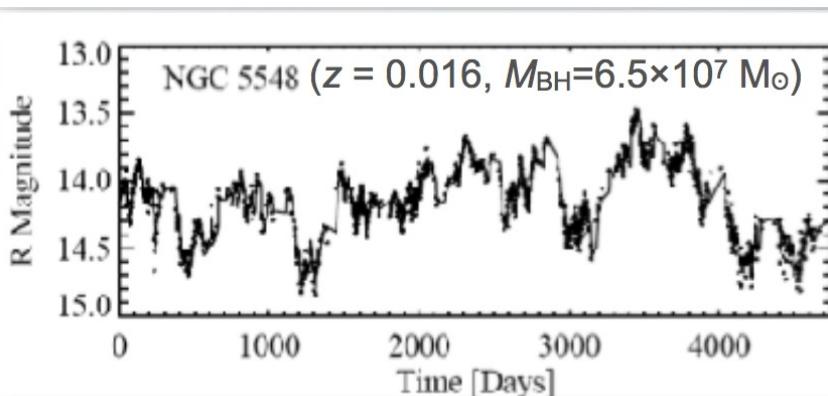
Then :
PCA+Clustering



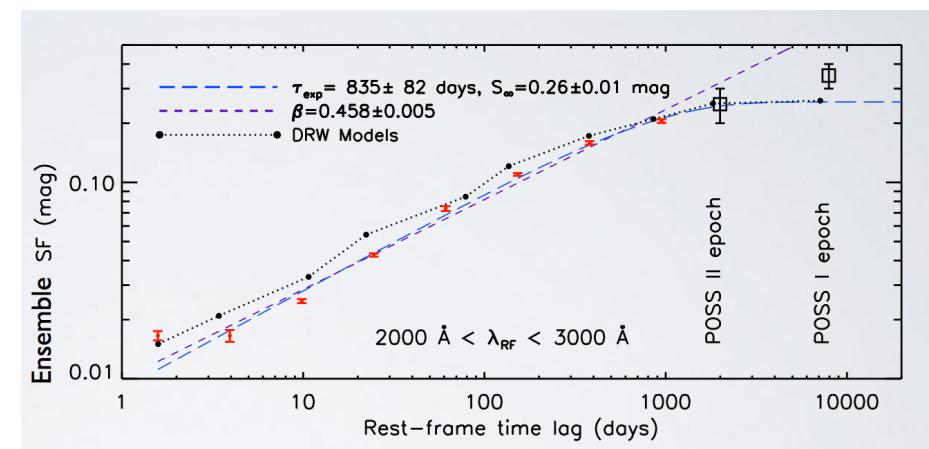
Deb & Singh 2009

Different time series

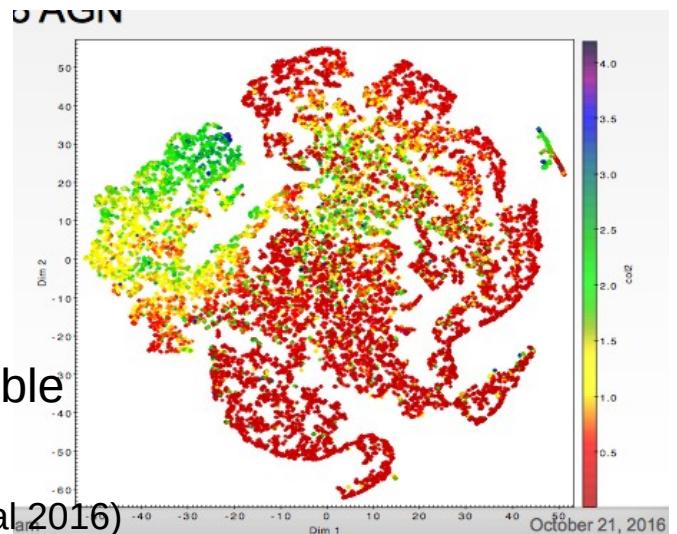
Aperiodic (dense)



Structure Function Analysis
RMS(Δm) at Δt



Classification possible
(Continuous
Autoregressive
Moving Average; Kasliwal 2016)
t-SNE



Transients :

Heterogeneous sparse time sampling

- Intermediate representation (features)
 - Template fitting
 - Non-parametric interpolation / Discretization
 - Basis of functions
 - Dealing with « holes »
 - Then : usual classifier
- Direct approach
 - e.g. Recurrent Neural Networks

Application to SN data

Lochner 2016

ArXiv 1603:00882

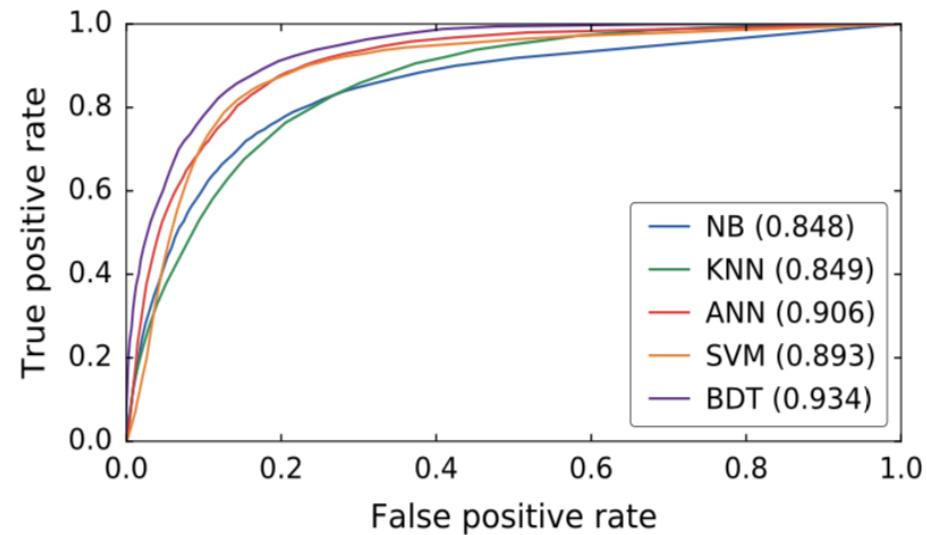
3 approaches :

- Template fitting (1 Class has a reliable template)
- Parametric approach (Light-curve as a parametrised function)
- Wavelet decomposition
 - Gaussian process interpolation
 - Wavelet decomposition (à trous/symlet)
 - Dimensionality reduction (PCA)

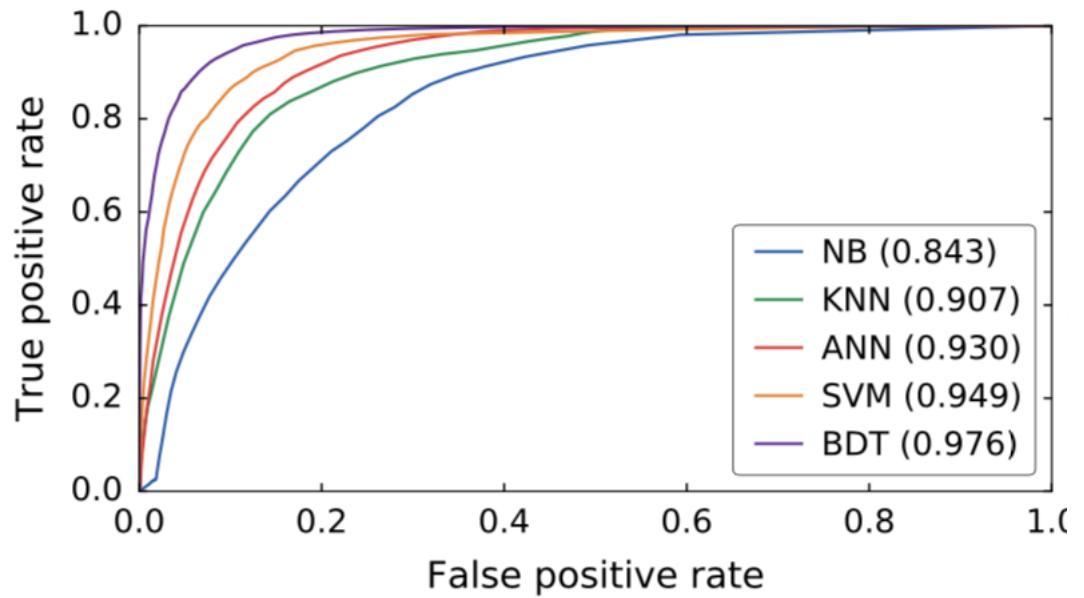
Then : Machine learning (Naive Bayes, KNN, ANN, BDT, SVM)

(Deep learning : not competitive for this case)

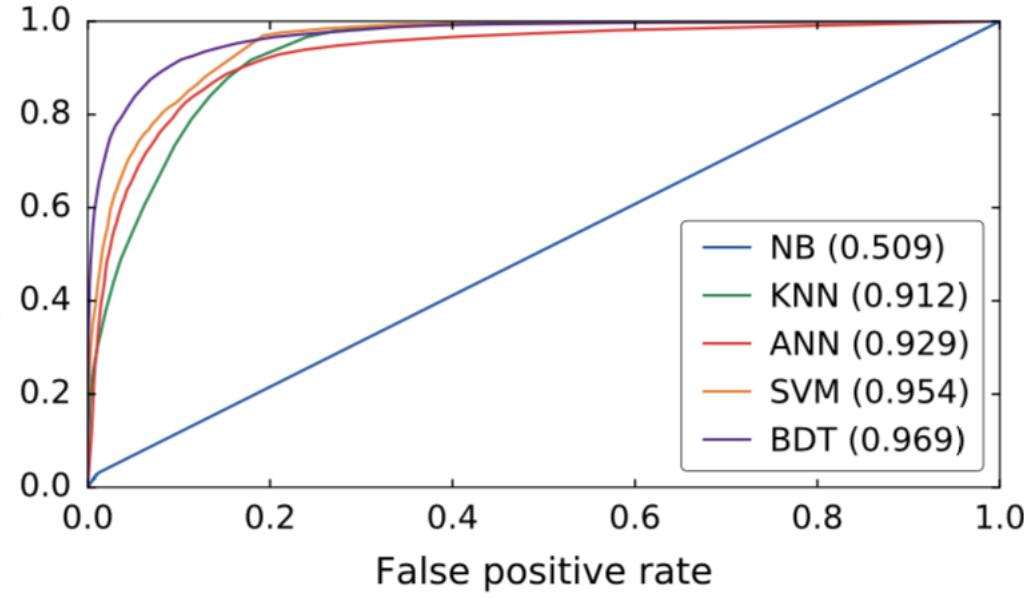
Results



(c) Parametric model 1, no redshift



(a) SALT2 model, no redshift

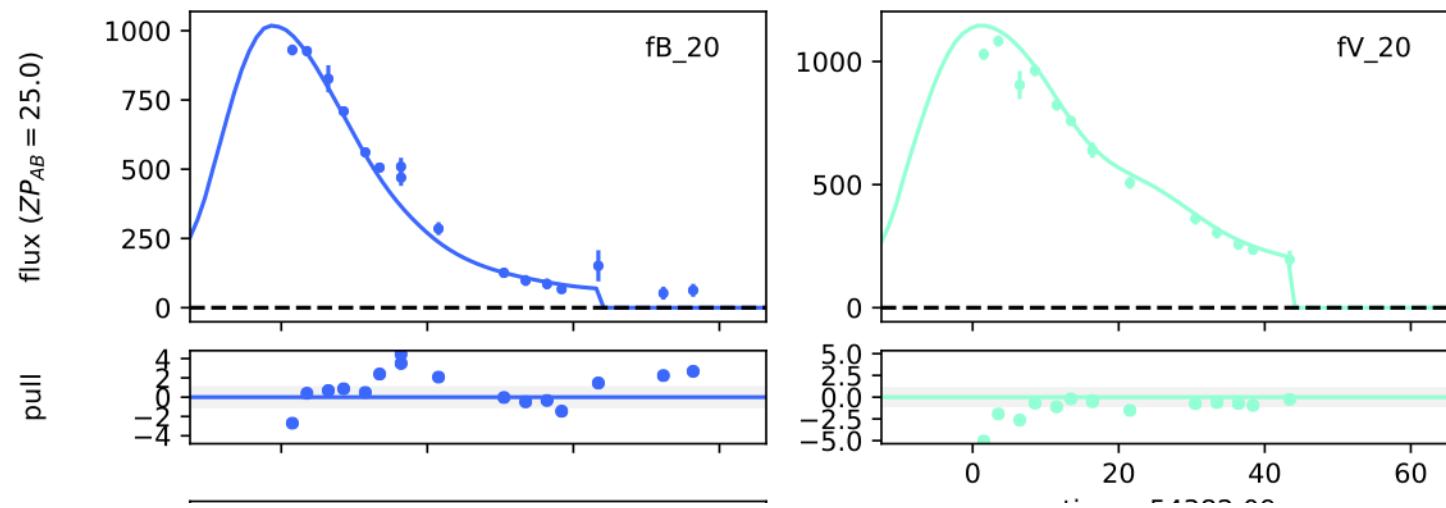


(g) Wavelets, no redshift

Template fitting

$z = 0.041174000$
 $t_0 = 54382.089$
 $q_1 = -0.25084467$
 $q_2 = 3.0024568$
 $q_3 = 1.3046436$

$A = -0.31078499$
 $M_g = 36.331659$
mw $ebv = 0.22910000$
mw $r_v = 3.1000000$



Pro : parametrization well known for 1 class
low dimensionality output
statistical goodness of fit
ingredient of likelihood ratio

To be improved
template for the other class(es)
automatic template generation ?

Parametric approach

$$F(t) = A \left(\frac{t - \phi}{\sigma} \right)^k \exp \left(-\frac{t - \phi}{\sigma} \right) k^{-k} e^k + \Psi(t),$$

where

$$\Psi(t) = \begin{cases} 0 & -\infty < t < \infty \\ \text{cubic spline} & \phi < t < \tau \\ \psi & \tau < t < \infty \end{cases},$$

To be improved :

result depends on function description (can be poor)

is it possible to automate the search for a few families of functions ?

Is it worth investigating more ?

Wavelet decomposition

Pro :

Basis of function provides natural feature extraction scheme
(remark : templates are based on basis of functions - splines)

Some questions :

Is there a need for interpolating the data before projecting on the basis ?

- null values when no data available
- null values already present in original data...

Errors may be poorly handled

Some care required for time translation invariance

Is this the best way to go ?

Last remarks

- Feature extraction may depend on classes to be found
 - Physical classes (Transient/Variable, Supernova types, ...)
 - Empirical classes (clustering of metadata...)
 - For instance, GP use an « average » function
- Can we skip the time interpolation ?
 - Lot of missing values...
 - Other formulations (RNN)
- The ideal solution should be robust / reprensentativeness issue
 - Templates are ; more difficult for NN