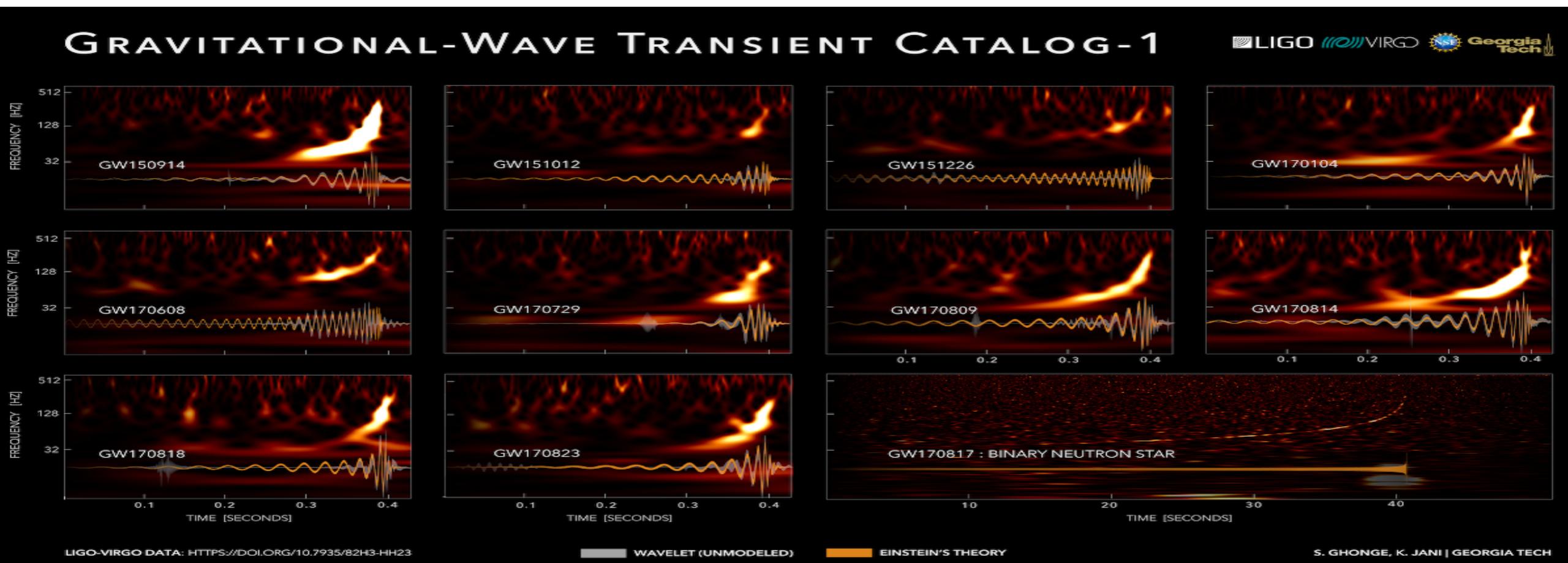


Gravitational waves from compact binary coalescences



*Ed Porter
APC/CNRS*

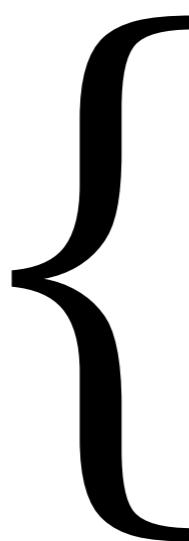


Cosmic Explosions 19, Cargese, Corsica, 27/05-05/06



Topics Covered

- Part 1



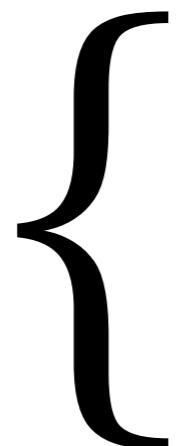
Matched Filtering

CBC waveform modelling

Data treatment

CBC searches and parameter estimation

- Part 2



01/02 detections

Fundamental physics and extreme matter

Astrophysics and Cosmology

PART 1



What is matched filtering?

- GWs are analogous to 1D sound waves
- Optimal linear filter for weak signals buried in random Gaussian noise
- Also known as optimal or Wiener filtering
- Works by correlating a known signal model (template) with the data



Constructing the optimal linear filter

- Starting with data : $s(t) = h(t) + n(t)$, $n(t) \gg h(t)$
- Define the correlation between the data and a real filter as

$$C(\tau) = \int_{-\infty}^{\infty} dt s(t)F(t + \tau) = \int_{-\infty}^{\infty} df \tilde{s}(f)\tilde{F}^*(f)e^{2\pi if\tau}$$

- To evaluate the signal-to-noise ratio [SNR], $\rho = \frac{S}{N}$
- we define the filtered signal

$$S = \langle C(\tau) \rangle = \int_{-\infty}^{\infty} df \langle \tilde{s}(f) \rangle \tilde{F}^*(f)e^{2\pi if\tau} = \int_{-\infty}^{\infty} df \tilde{h}(f)\tilde{F}^*(f)e^{2\pi if\tau}$$

- using $\langle n(t) \rangle = 0$



Constructing the optimal linear filter

- For stationary, Gaussian noise, the variance is

$$\langle N^2 \rangle = \left[\langle C^2(\tau) \rangle - \langle C(\tau) \rangle^2 \right]_{h(t)=0} = \int_{-\infty}^{\infty} df df' \langle \tilde{n}(f) \tilde{n}^*(f') \rangle \tilde{F}(f) \tilde{F}^*(f') e^{2\pi i \tau(f-f')}$$

- Defining a two-sided power spectral density $\langle \tilde{n}(f) \tilde{n}^*(f') \rangle = \delta(f-f') S_h(f)$

- we can now write $\langle N^2 \rangle = \int_{-\infty}^{\infty} df |\tilde{F}(f)|^2 S_h(f)$

- defining the SNR as $\rho = \frac{S}{N} = \frac{\int_{-\infty}^{\infty} df \tilde{h}(f) \tilde{F}^*(f) e^{2\pi i f \tau}}{\left[\int_{-\infty}^{\infty} df |\tilde{F}(f)|^2 S_h(f) \right]^{1/2}}$



Constructing the optimal linear filter

- Defining a noise-weighted inner product

$$\langle a | b \rangle = 2 \int_0^\infty \frac{df}{S_n(f)} \tilde{a}(f) \tilde{b}^*(f) + c.c.$$

- the SNR now becomes

$$\frac{S}{N} = \frac{\left\langle \tilde{h}(f) | S_n(f) \tilde{F}(f) e^{2\pi if\tau} \right\rangle}{\left\langle S_n(f) \tilde{F}(f) | S_n(f) \tilde{F}(f) \right\rangle^{1/2}}$$

- To optimise the SNR, we require $\tilde{F}(f) || \tilde{h}(f)$
- allowing us to define the optimal linear filter as $\tilde{F}(f) = \frac{\tilde{h}(f)}{S_n(f)} e^{-2\pi if\tau}$
- and the optimal SNR as $\rho_{opt} = \langle h | h \rangle^{1/2}$



Response to a GW

- The response at each detector is

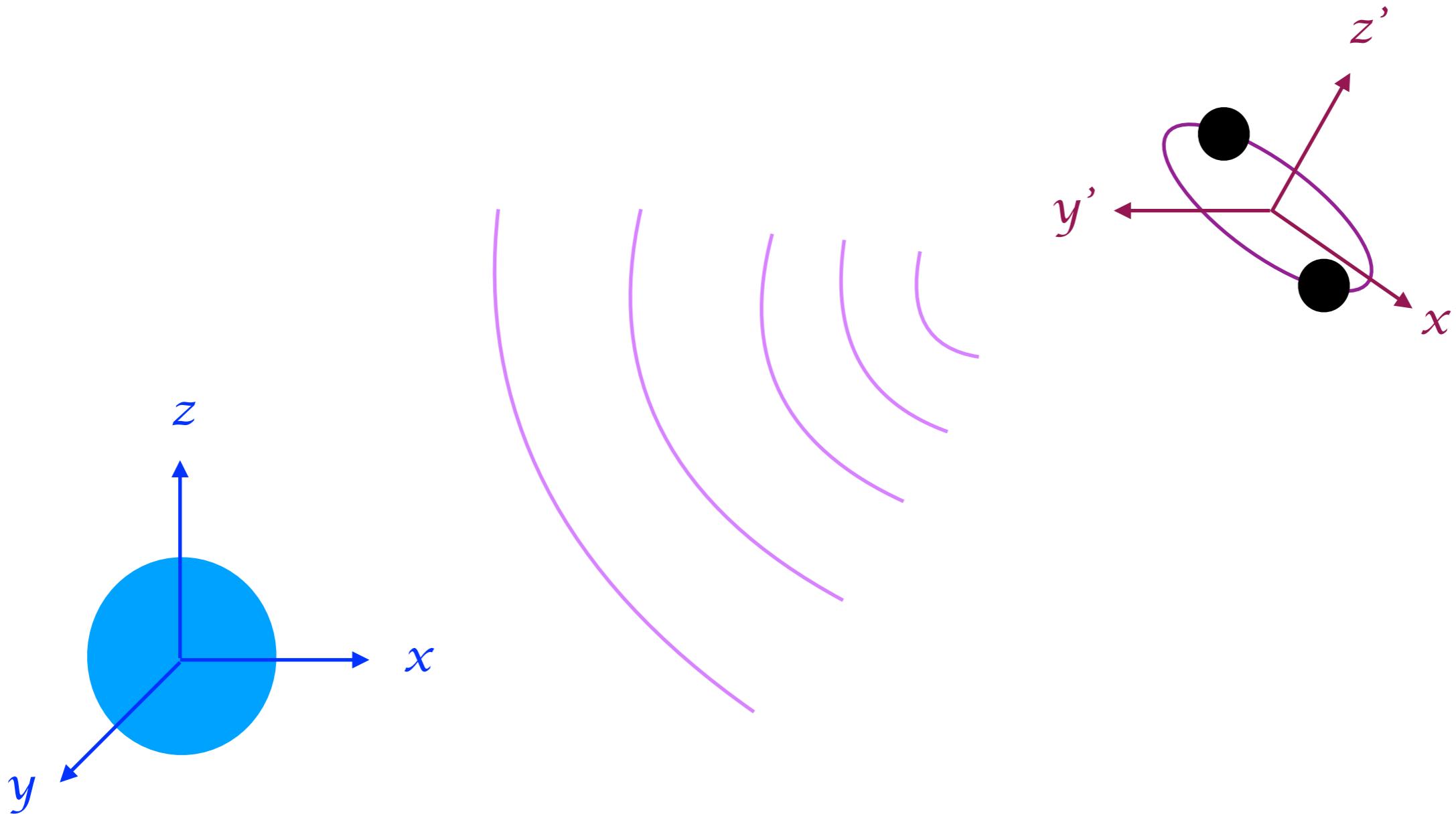
$$h_i(t) = h_+(t + \tau_i)F_i^+ + h_\times(t + \tau_i)F_i^\times$$

- where (h_+, h_\times) are the GW polarisations
- and (F^+, F^\times) are the detector pattern response
- In general, the GWs are defined by 15-17 parameters that we can define as extrinsic and intrinsic



Extrinsic Parameters (Positional)

$$h_i(t) = h_+(t + \tau_i) F_i^+ + h_\times(t + \tau_i) F_i^\times$$

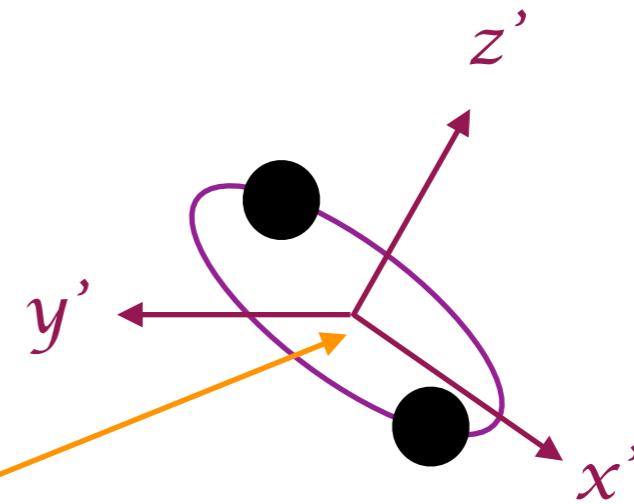
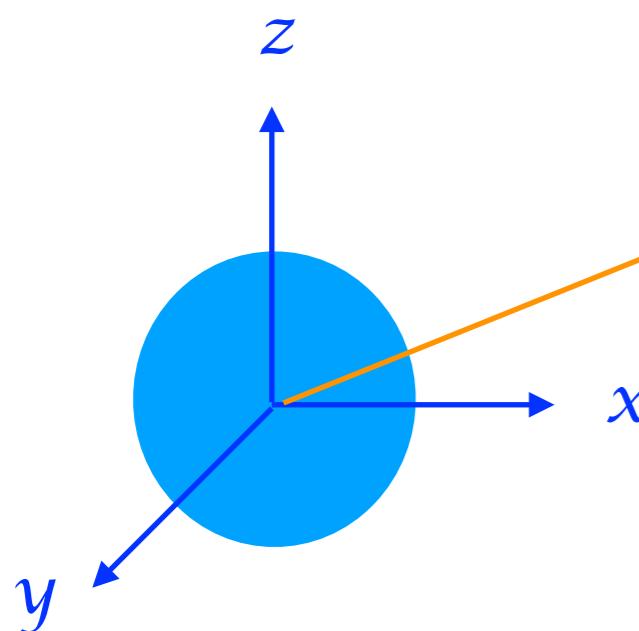


Luminosity Distance

$$h_i(t) = h_+(t + \tau_i) F_i^+ + h_\times(t + \tau_i) F_i^\times$$

Parameters

1

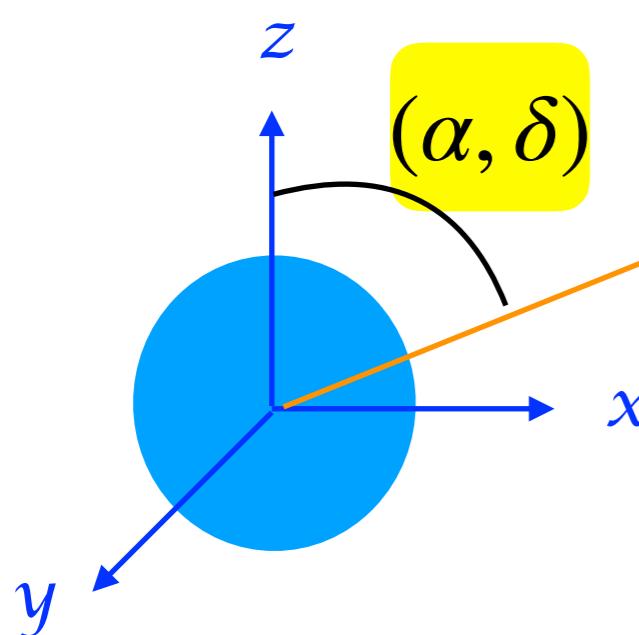


Sky Position

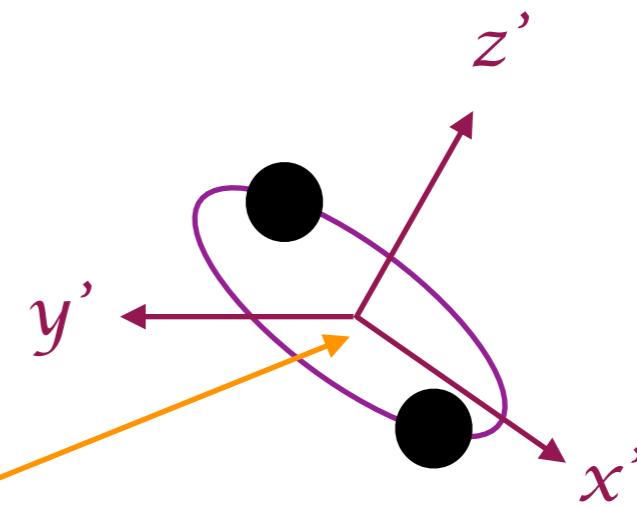
$$h_i(t) = h_+(t + \tau_i) F_i^+ + h_\times(t + \tau_i) F_i^\times$$

Parameters

3



D_L

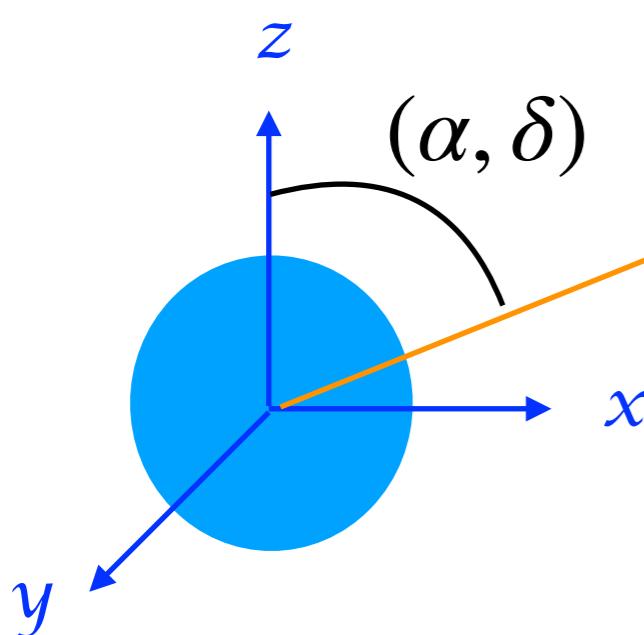


Inclination Angle

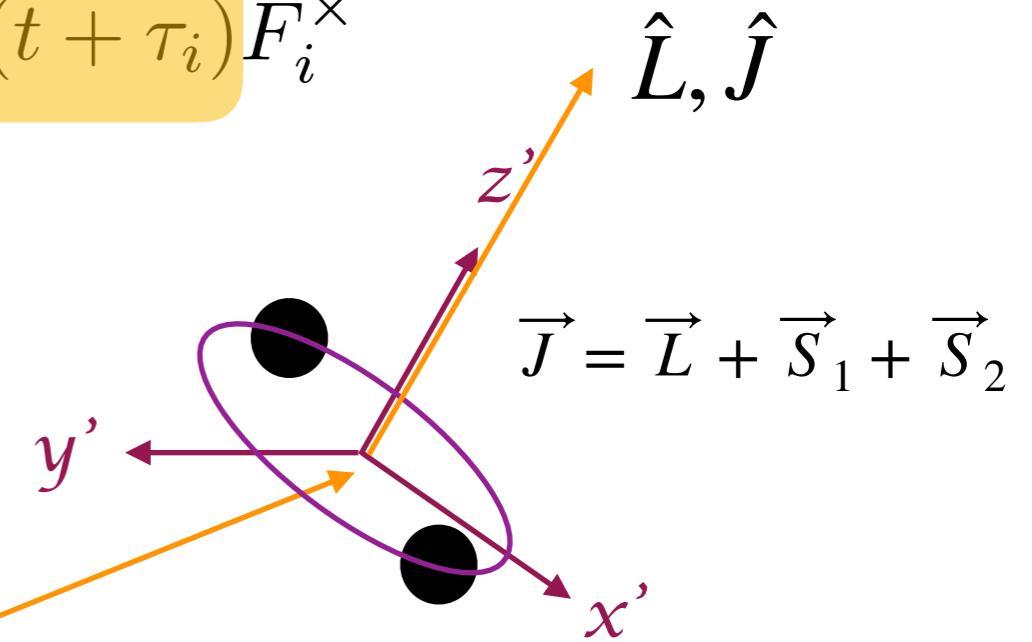
$$h_i(t) = h_+(t + \tau_i) F_i^+ + h_\times(t + \tau_i) F_i^\times$$

Parameters

4



$$D_L \hat{n}$$



$$\cos i = \hat{n} \cdot \hat{L} \quad (\text{non-spinning})$$

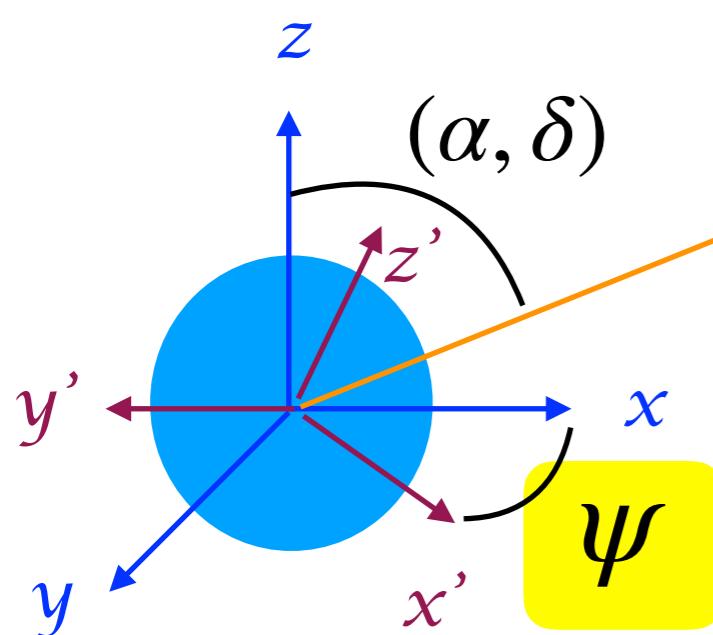
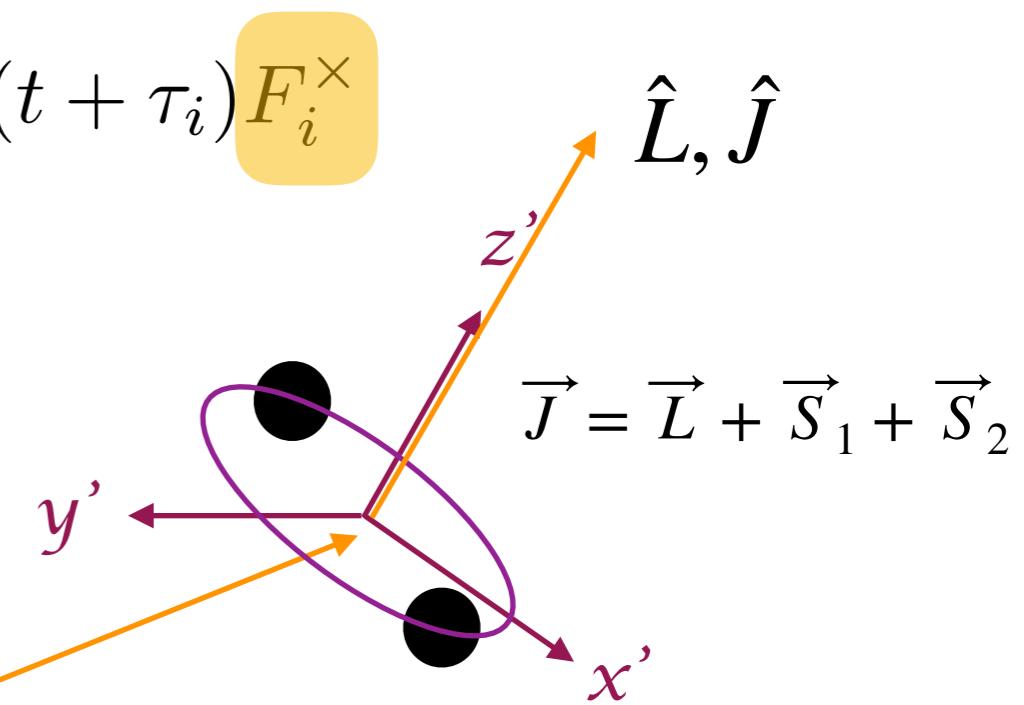
$$\cos \theta_{Jn} = \hat{n} \cdot \hat{J} \quad (\text{spinning})$$

Polarisation Angle

Parameters

5

$$h_i(t) = h_+(t + \tau_i) F_i^+ + h_\times(t + \tau_i) F_i^\times$$



$$D_L \hat{n}$$

$$\cos i = \hat{n} \cdot \hat{L} \quad (\text{non-spinning})$$

$$\cos \theta_{Jn} = \hat{n} \cdot \hat{J} \quad (\text{spinning})$$

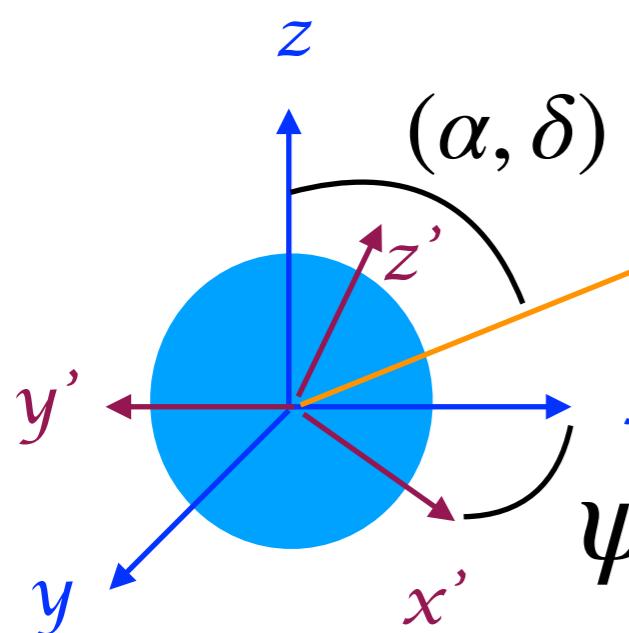
Reference Time and Phase

$$h_i(t) = h_+(t + \tau_i) F_i^+ + h_\times(t + \tau_i) F_i^\times$$

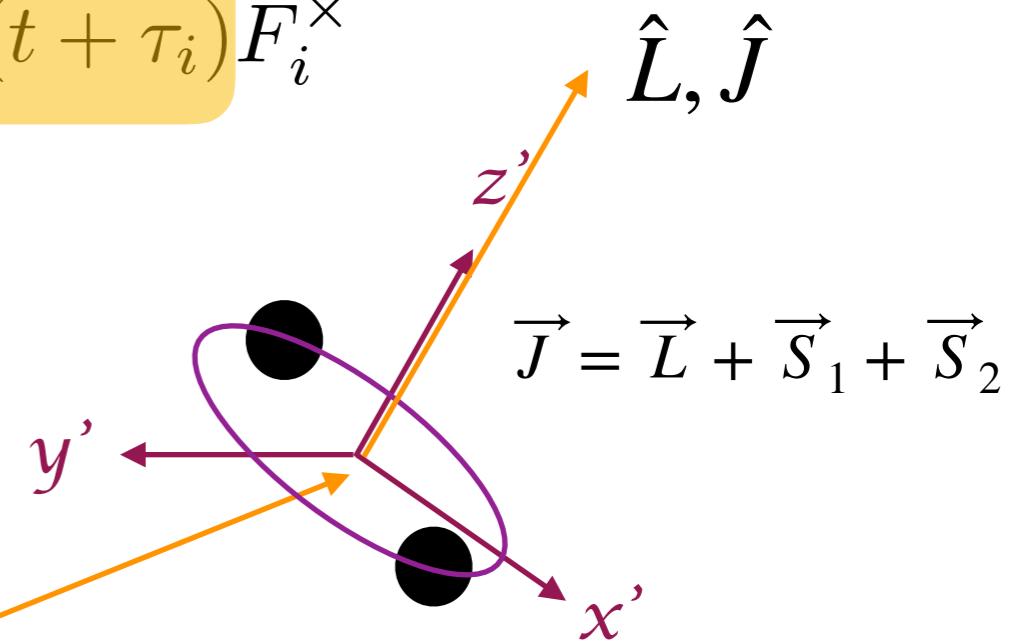
Parameters

7

(t_{ref}, ϕ_{ref})



$$D_L \hat{n}$$

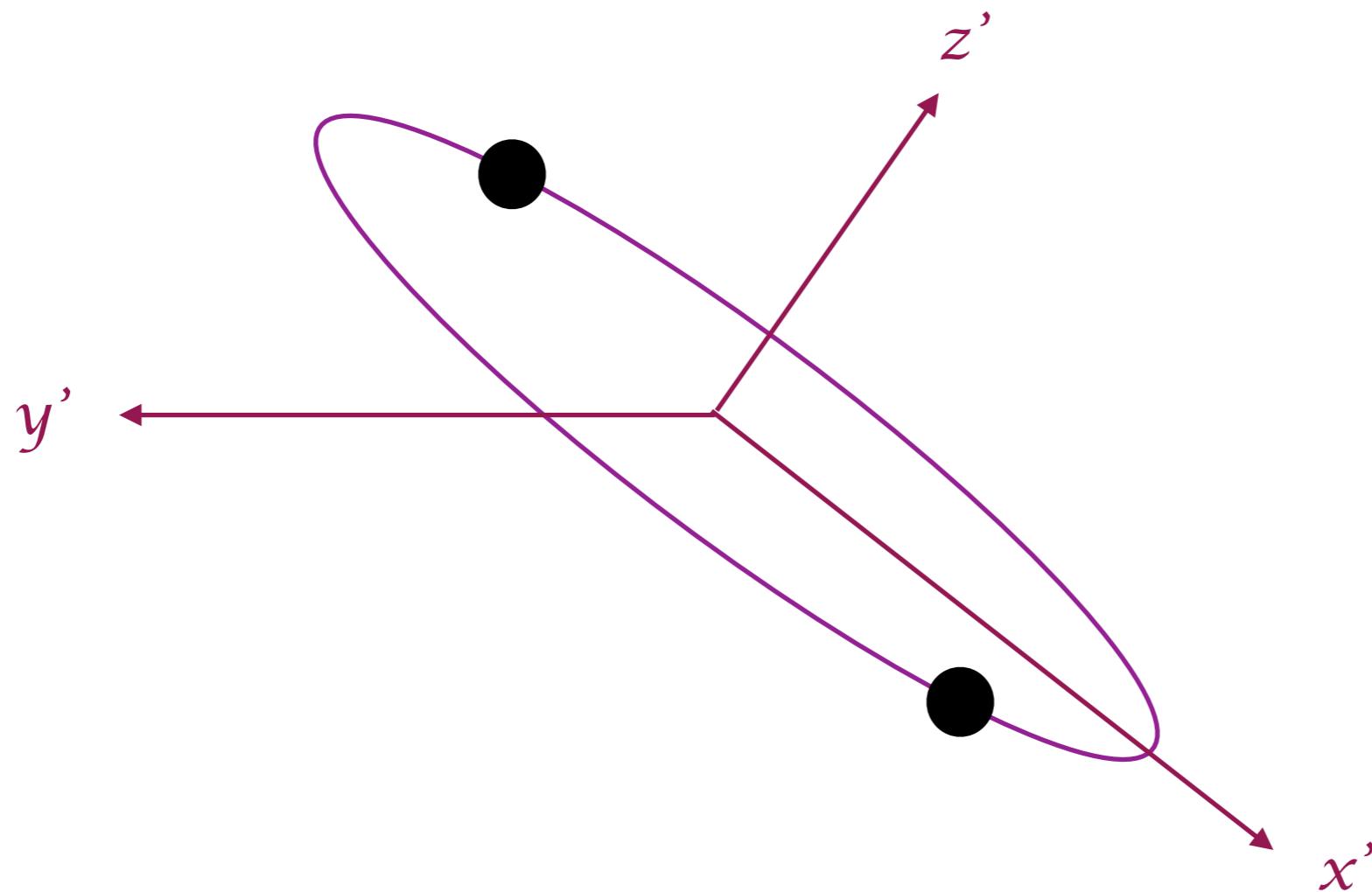


$$\cos i = \hat{n} \cdot \hat{L} \quad (\text{non-spinning})$$

$$\cos \theta_{Jn} = \hat{n} \cdot \hat{J} \quad (\text{spinning})$$

Intrinsic Parameters (Dynamical)

$$h_i(t) = h_+(t + \tau_i) F_i^+ + h_\times(t + \tau_i) F_i^\times$$

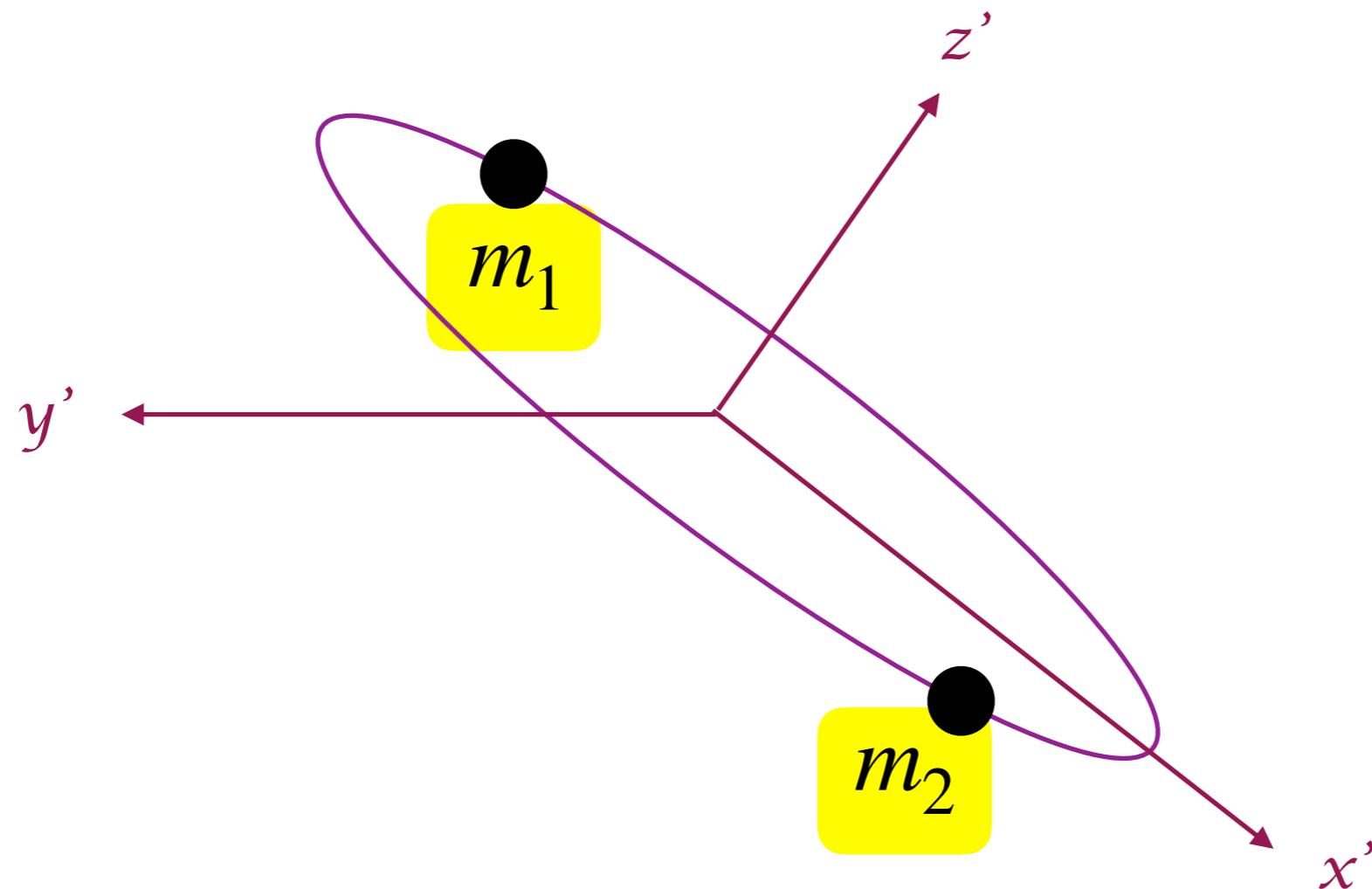


Intrinsic Parameters (Dynamical)

$$h_i(t) = h_+(t + \tau_i) F_i^+ + h_\times(t + \tau_i) F_i^\times$$

Parameters

9

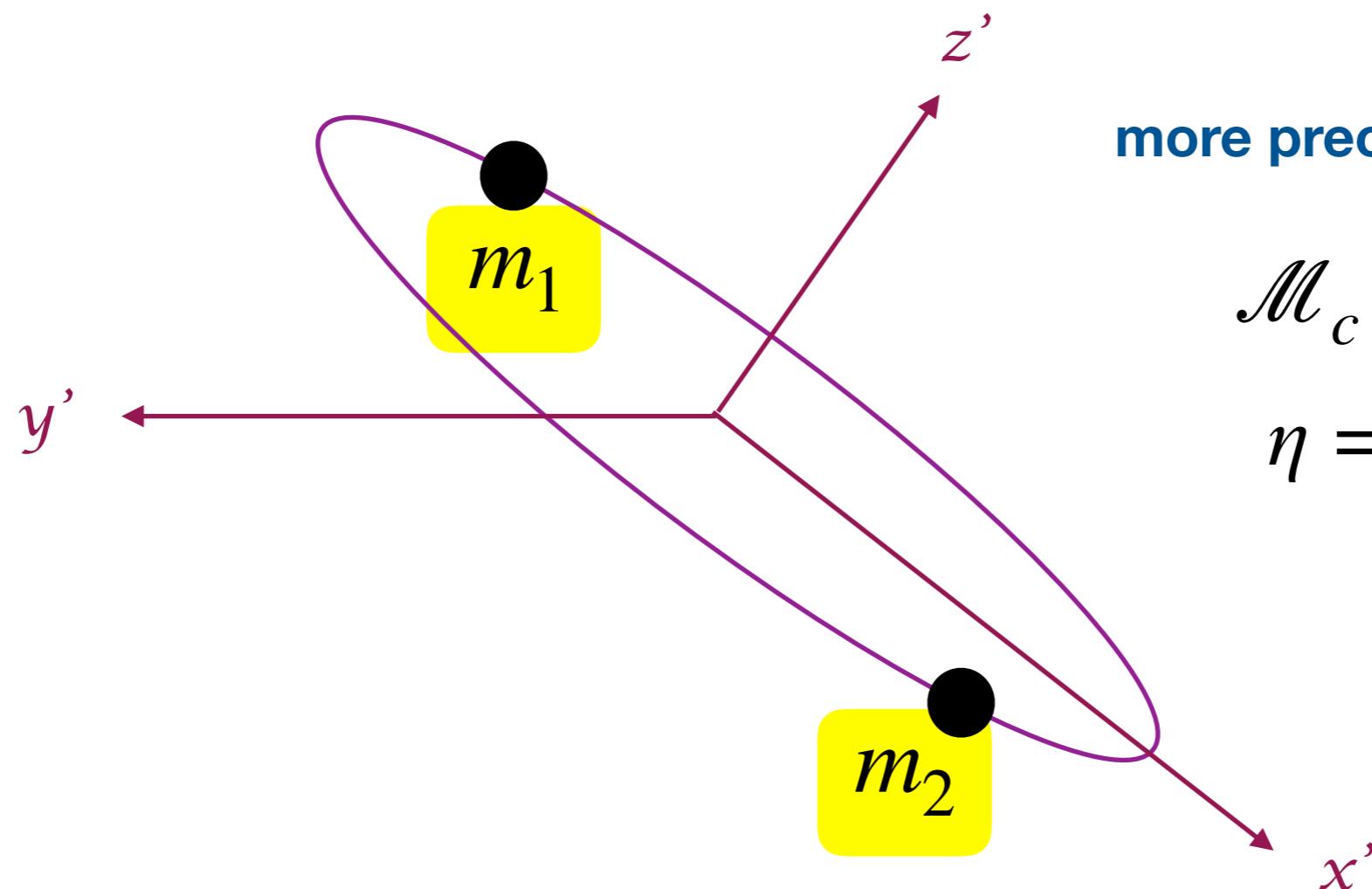


Intrinsic Parameters (Dynamical)

$$h_i(t) = h_+(t + \tau_i) F_i^+ + h_\times(t + \tau_i) F_i^\times$$

Parameters

9



more precisely, we use

$$\mathcal{M}_c = mn^{3/5}$$

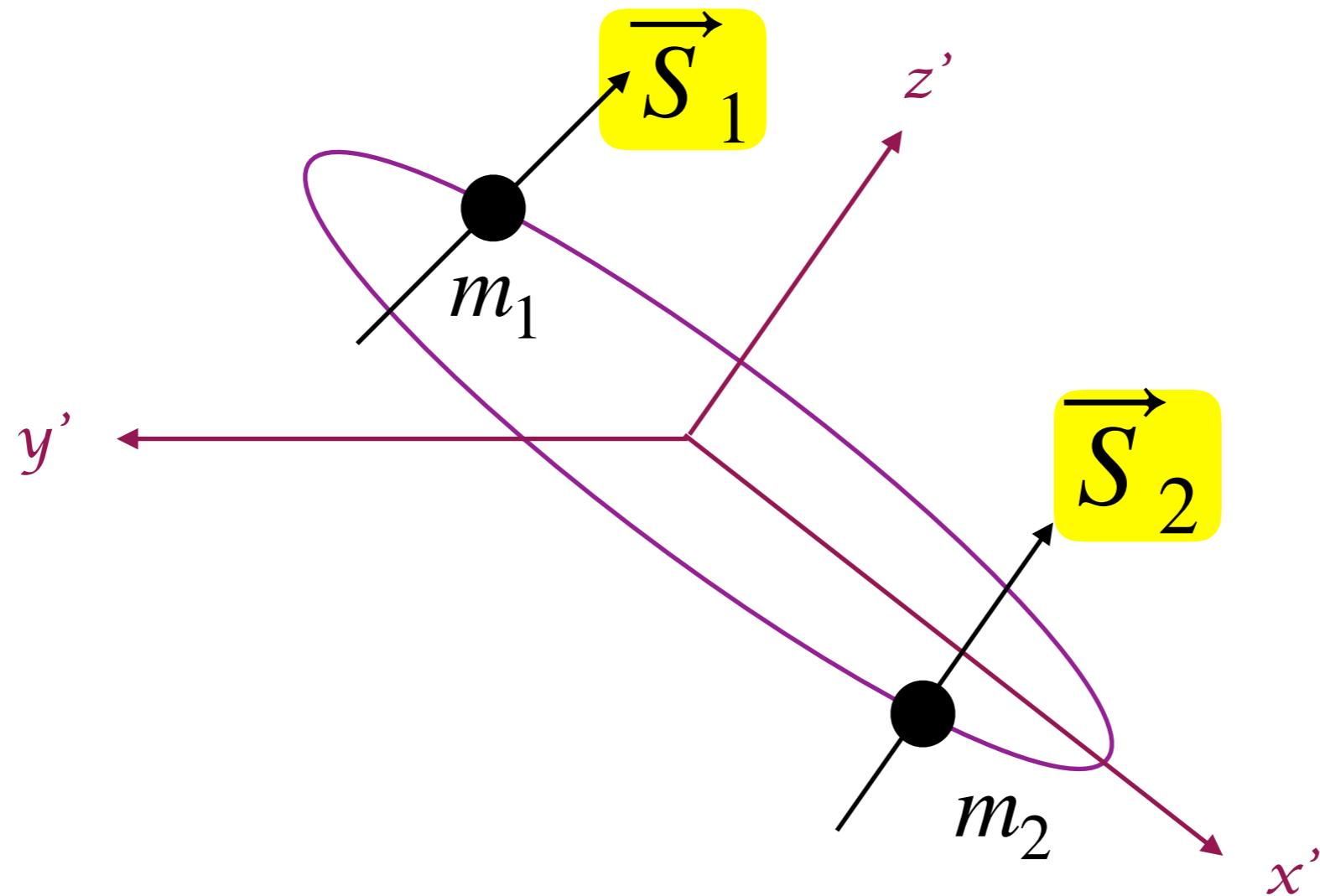
$$\eta = m_1 m_2 / m^2$$

Intrinsic Parameters (Dynamical)

$$h_i(t) = h_+(t + \tau_i) F_i^+ + h_\times(t + \tau_i) F_i^\times$$

Parameters

15



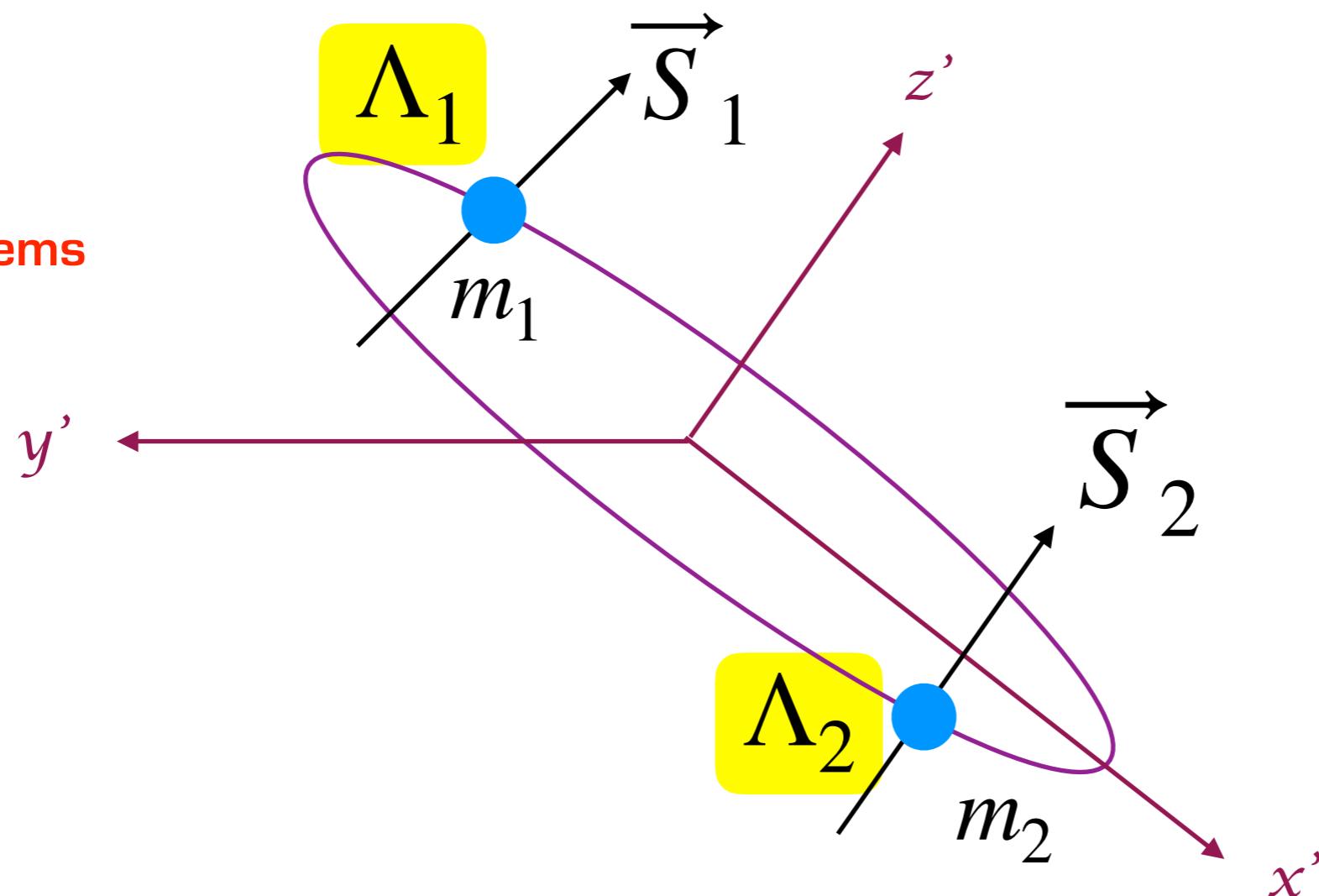
Intrinsic Parameters (Dynamical)

$$h_i(t) = h_+(t + \tau_i) F_i^+ + h_\times(t + \tau_i) F_i^\times$$

Parameters

17

For BNS systems

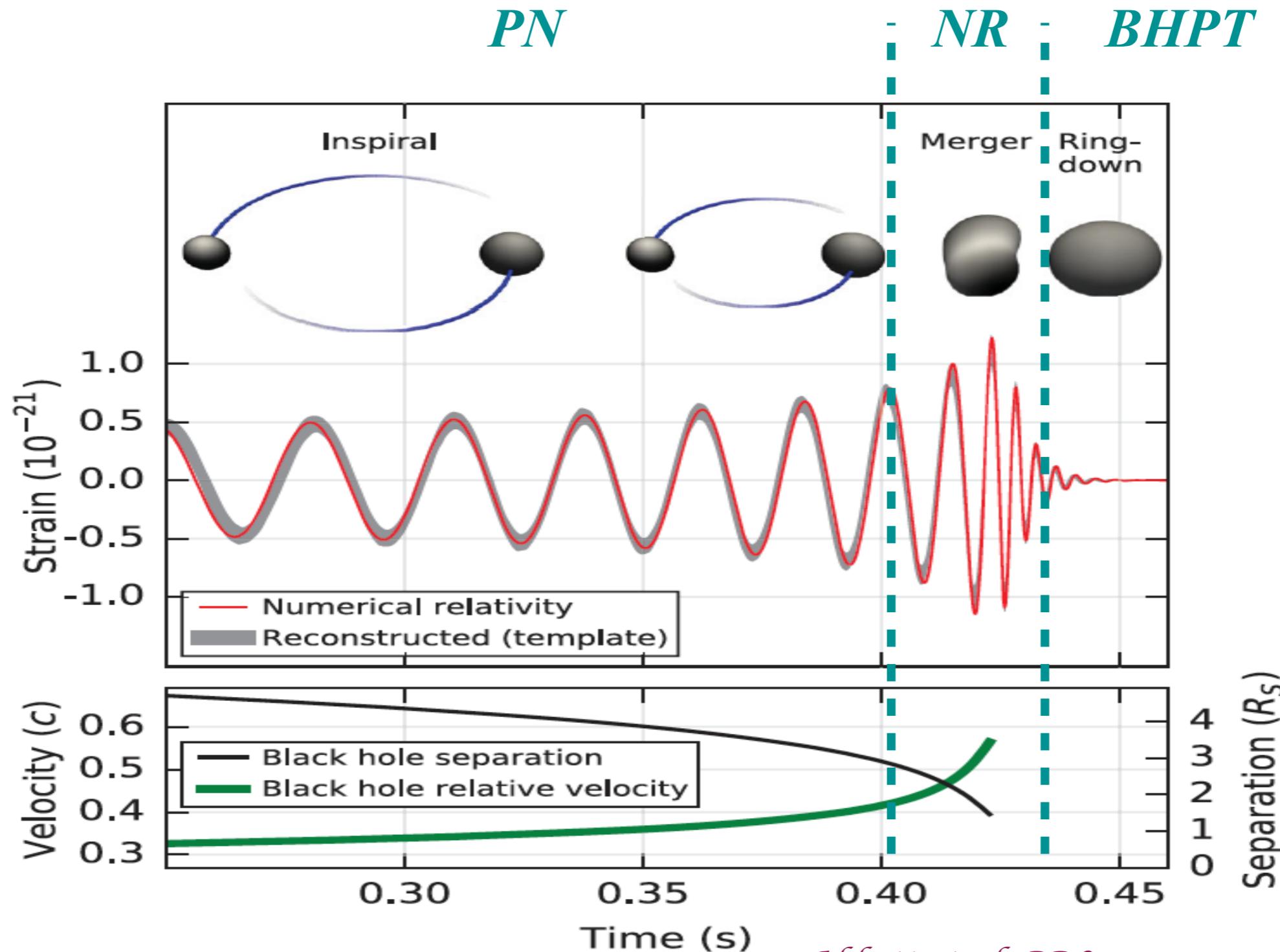


Modelling the Phase

- Remember, matched filtering needs phase coherence
- Newtonian mechanics : analytic solution to 2-body problem, no solution to the generic 3-body problem
- GR : no solution to the 2-body problem
- Modelling requires a combination of analytic and numerical relativity



Time-Domain Morphology of a CBC Signal



Inspiral

- Wide separation, i.e. $v_{orb} \ll c$
- To start we can write the TD polarisations as

$$h_+(t) = \frac{2(1 + \cos^2(\iota))m\eta}{D_L} \cos \Phi(t) , \quad h_\times(t) = -\frac{4 \cos(\iota)m\eta}{D_L} \sin \Phi(t)$$

- where $\eta = m_1 m_2 / m^2$, and $\Phi(t) \equiv \Phi_{GW}(t) = 2\Phi_{orb}(t)$
- We can then write the GW phase as a PN expansion

$$\Phi(t) = \phi_N(t) + \phi_2(t) + \phi_3(t) + \dots$$

- in terms of a small parameter $\nu = (\pi m f)^{1/3}$, where f is the GW frequency, and the sub-script corresponds to the power of (v/c) correction



Inspiral

- In the early inspiral, we can assume $\dot{f}_{orb}/f_{orb}^2 \ll 1$
- This allows us to use the energy balance equation $F(t) = -m \frac{dE(t)}{dt}$
- and calculate the phase evolution

$$\frac{d\phi}{dt} - \frac{v^3}{m} = 0$$

$$\frac{dv}{dt} + \frac{F(v)}{mE'(v)} = 0$$



$$t(v) = t_{ref} + m \int_v^{v_{ref}} dv \frac{E'(v)}{F(v)}$$

$$\phi(v) = \phi_{ref} + \int_v^{v_{ref}} dv v^3 \frac{E'(v)}{F(v)}$$



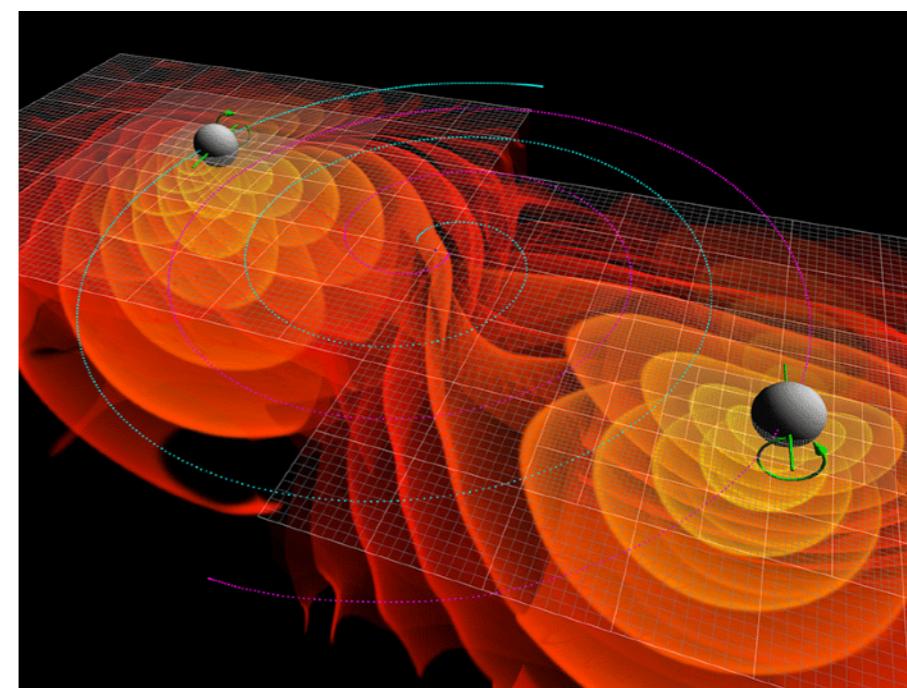
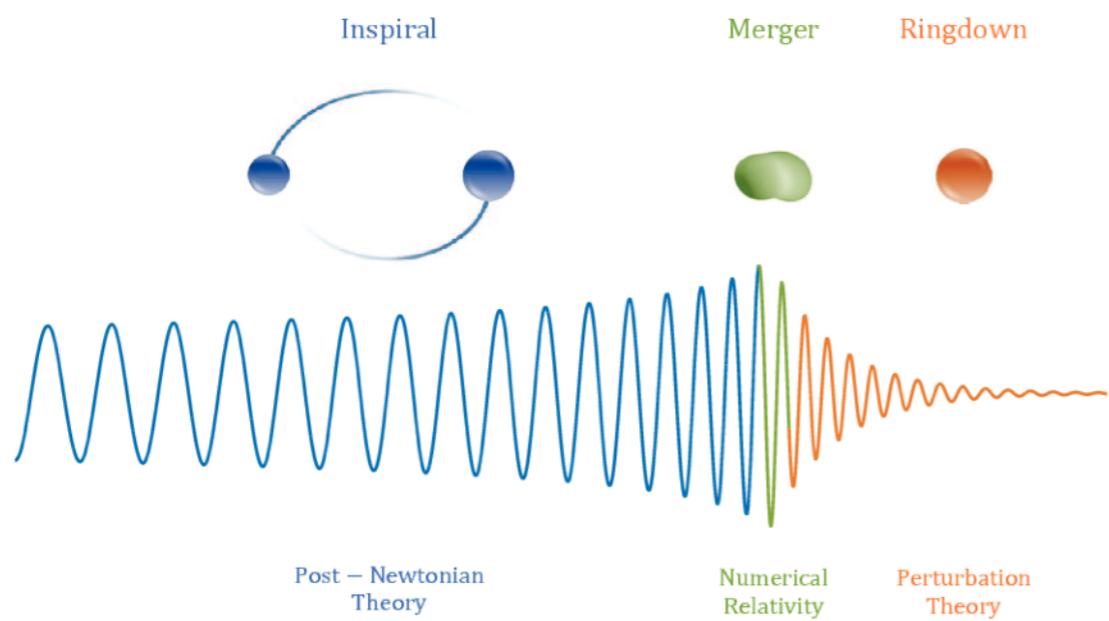
Limits of the PN expansion

- Both $E'(v)$ and $F(v)$ have a PN (power) series solution
- How we treat the ratio $E'(v)/F(v)$ leads to different PN families
- Each PN series is asymptotically divergent, meaning...
 - ...different families have differing levels of accuracy,
 - ...a higher approximation does not guarantee higher accuracy,
 - ...the PN approximation should break down at the LSO ($\sim R=6M$)
 - ...but in fact, breaks down much sooner ($R\sim 12M$)



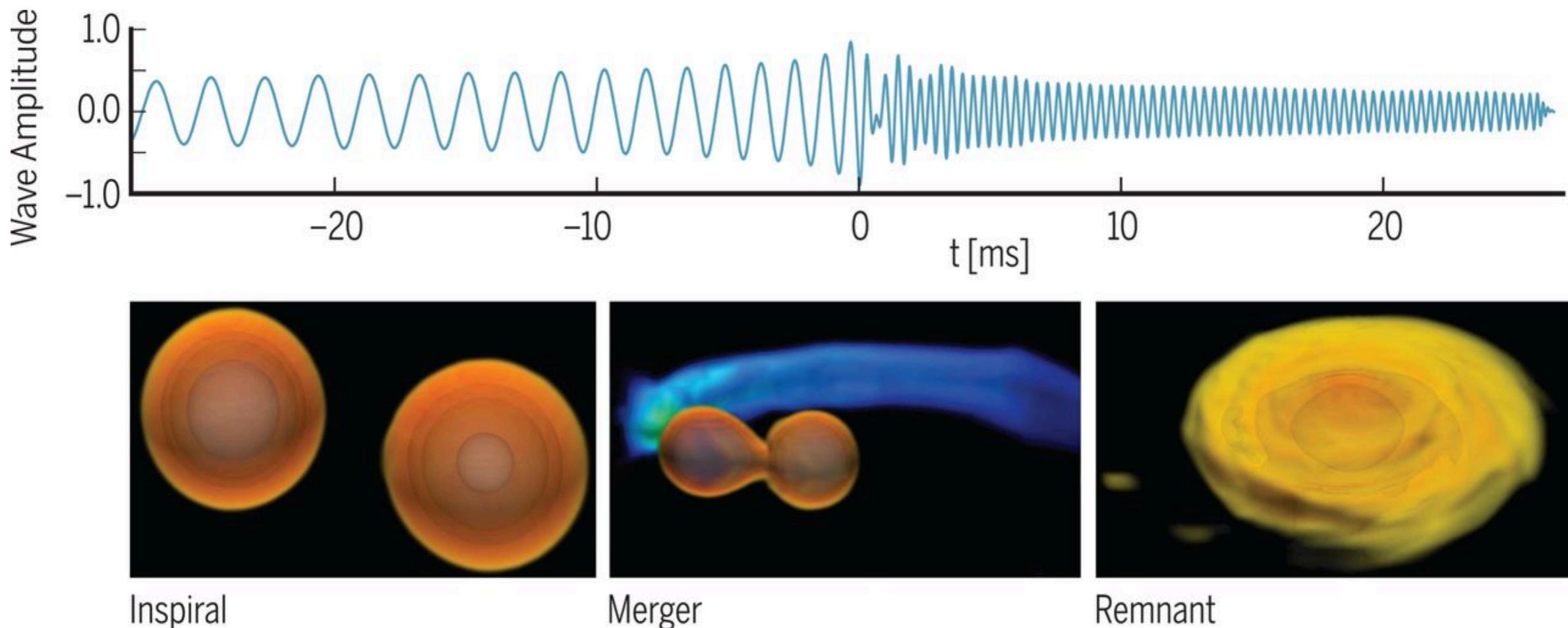
Late Inspiral / Merger

- Both the late inspiral and merger need to be solved numerically
- A relatively small number of cycles can take months to generate on a supercomputer



Late Inspiral / Merger

- NR becomes even more important as we try and simulate BNS and NSBH systems



B. Brugmann, Science 361, 336 (2018)



Ringdown

- The final black hole rings like a bell that's been struck
- An analytic solution exists using black hole perturbation theory
- The energy is radiated in a series of quasi-normal modes
- These modes can be used to test the no-hair theorem
- No evidence of the QNMs as of yet



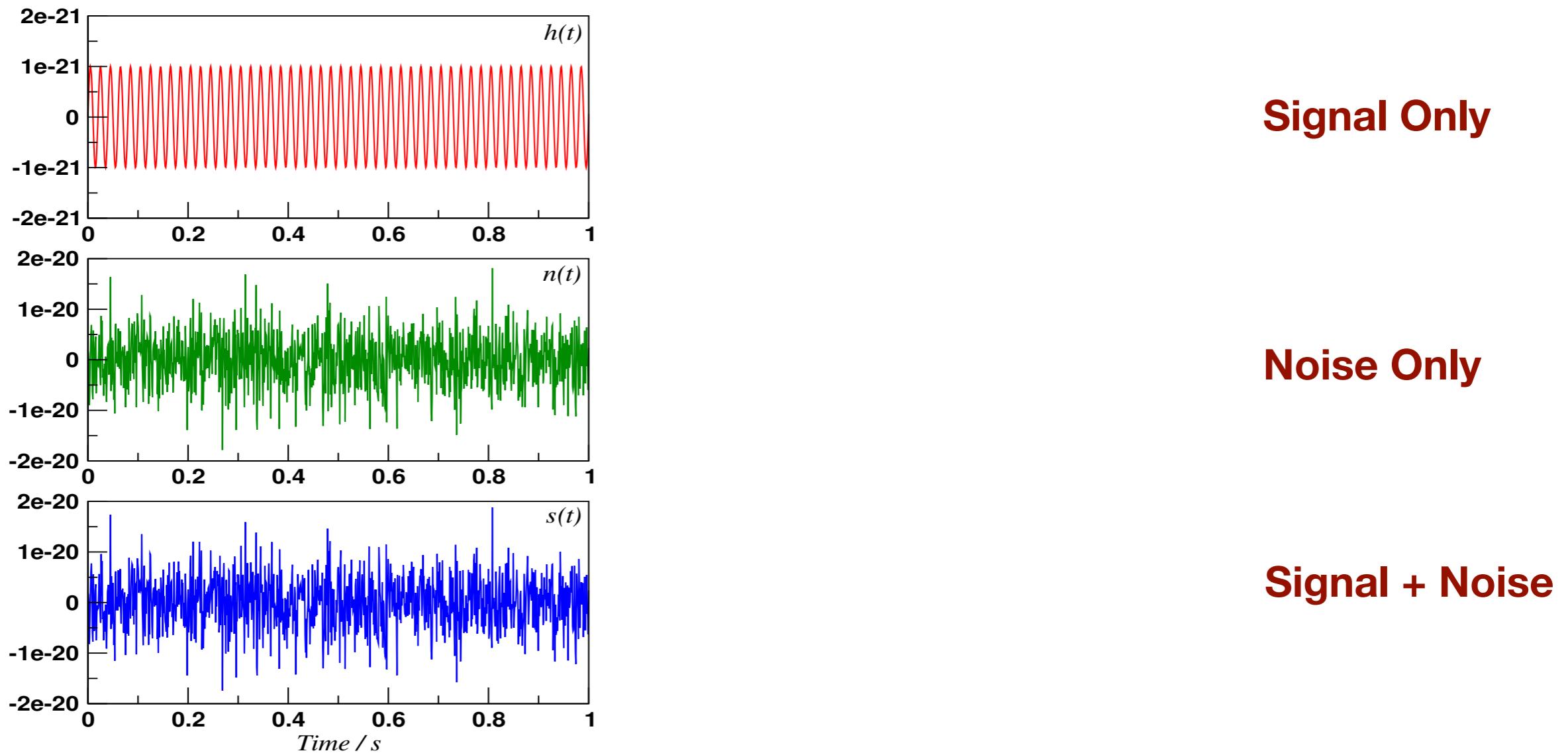
Hybrid Waveforms

- NR waveforms are expensive to generate and use
- For efficient data analysis, we use approximate analytical solutions
 - PN - Inspiral only
 - EOB - solves Hamilton's equations along the trajectory. Calibrated using NR waveforms
 - IMRPhenom - frequency domain analytic waveform, also calibrated using NR waveforms
- As we don't know if our waveforms are perfectly accurate, different families allow us to keep systematics under control
- New waveform families include eccentricity, tidal forces, precession etc.



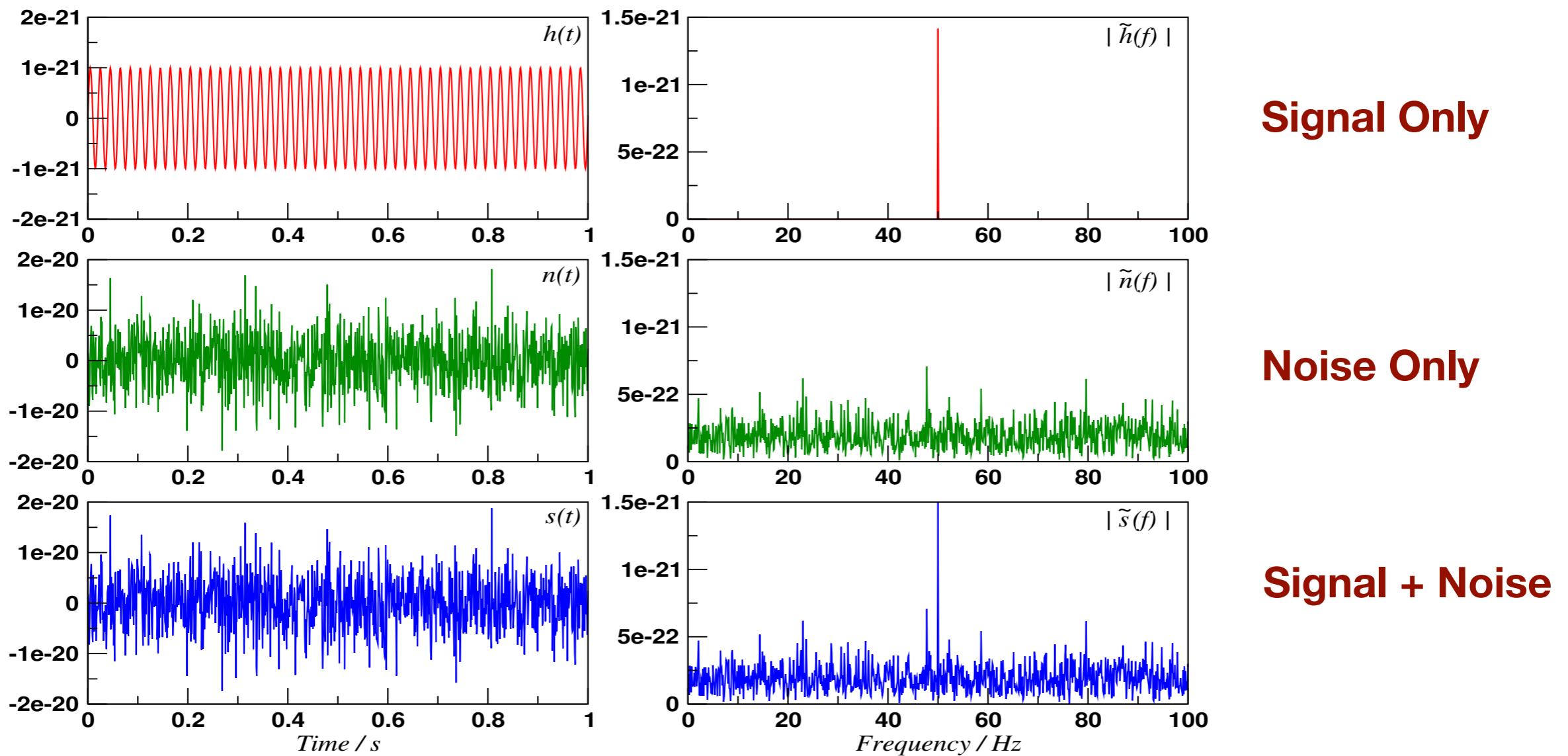
Treating the Data

- Easiest to work in Fourier domain
- e.g. Sine-wave with $f=50$ Hz buried in random Gaussian noise



Treating the Data

- Easiest to work in Fourier domain
- e.g. Sine-wave with $f=50$ Hz buried in random Gaussian noise



Fourier Domain Waveforms

- Stationary phase approximation
- Start with a generalised Fourier integral $I = \int F(\omega) e^{i\varphi(\omega)} d\omega$
- Assume $F(\omega)$ varies slowly compared to $\varphi(\omega)$. As the phase rapidly varies, the integral averages to zero except where $\varphi(\omega)$ has an extremum
- So find points where $d\varphi/d\omega = 0$ and Taylor expand the phase

$$\varphi(\omega) = \varphi(\omega_{sp}) + \frac{1}{2}\varphi''(\omega - \omega_{sp})^2 + \dots$$

- Evaluate the integral in the vicinity of extrema, and sum if more than one saddle point

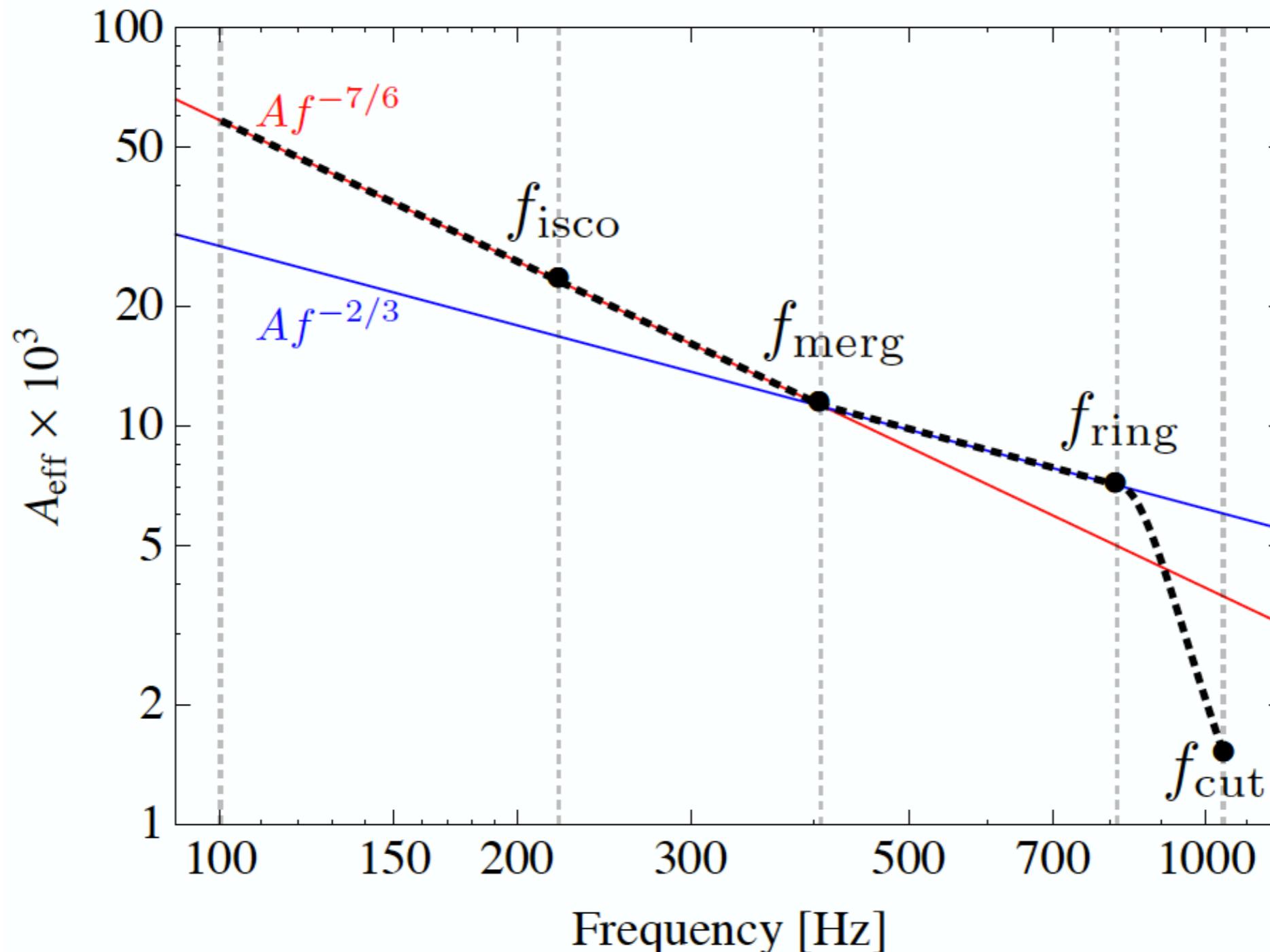
$$I = F(\omega_{sp}) e^{i\varphi(\omega_{sp})} \int e^{\frac{i}{2}\varphi(\omega-\omega_{sp})^2} d\omega$$

- Fresnel type integral with standard solution, leading to

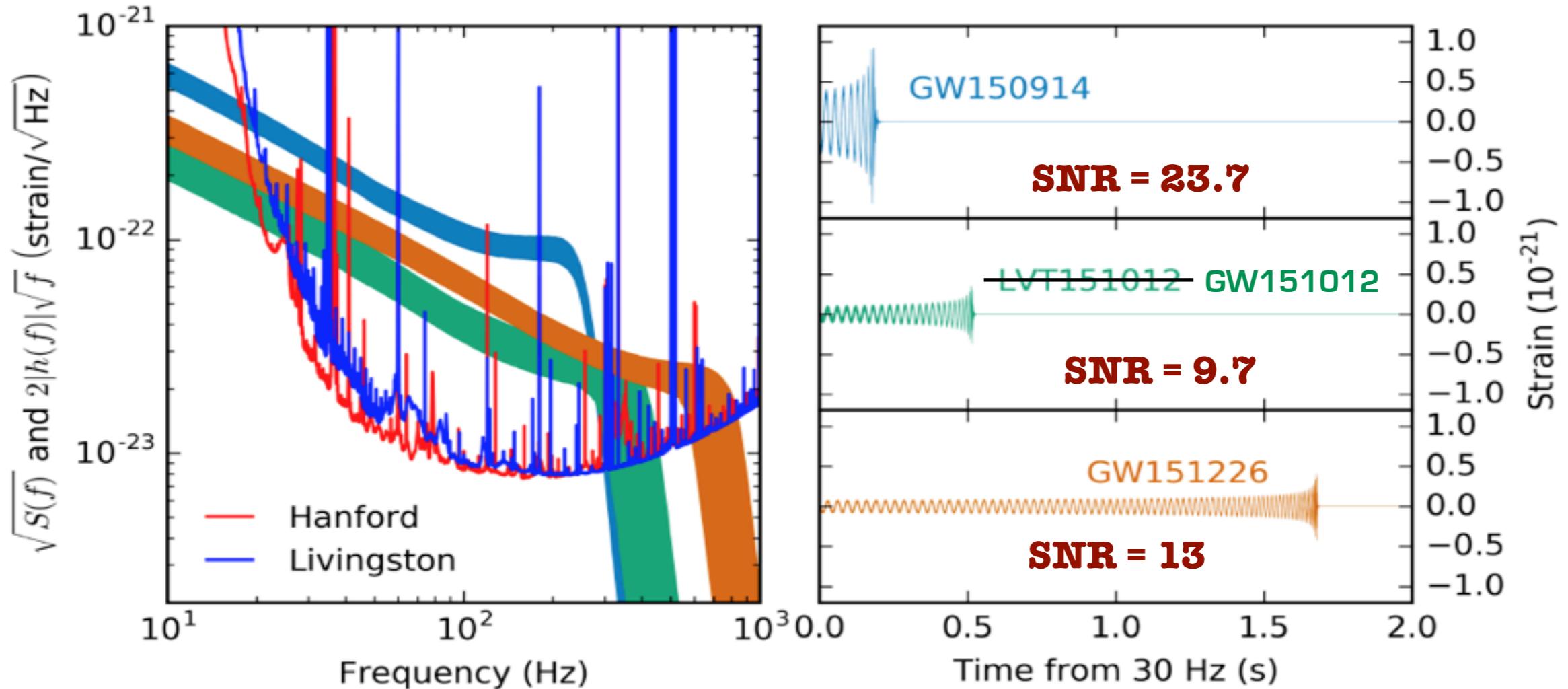
$$\tilde{h}(f) = A f^{-7/6} e^{i\varphi(f)}$$



Frequency Domain CBC Waveform Morphology



WAVEFORM COMPARISONS



- Maximum frequency inversely proportional to total mass
- Most of the SNR comes from the merger - ringdown

Abbott et al, PRX 6, 041015 (2016)



Sampling the data

- Our analysis is best represented in the Fourier domain
- So given a continuous signal $h(t)$, the FT is $\tilde{h}(f) = \int_{-\infty}^{\infty} dt h(t)e^{-2\pi i f t}$
- However, we need a digital representation, i.e. $h(t) \Rightarrow h_j = h(t_j)$
- Given a sampling frequency f_s , we define $\Delta t = 1/f_s$
- With time domain data of N samples, total observation time $T_{obs} = N \Delta t$, the discrete FT is given by
- $\tilde{h}_k = \sum_{j=0}^{N-1} h_j e^{-2\pi i j k / N}$ where each sample has a frequency $f_k = k / T_{obs}$
- But how do we choose f_s ?



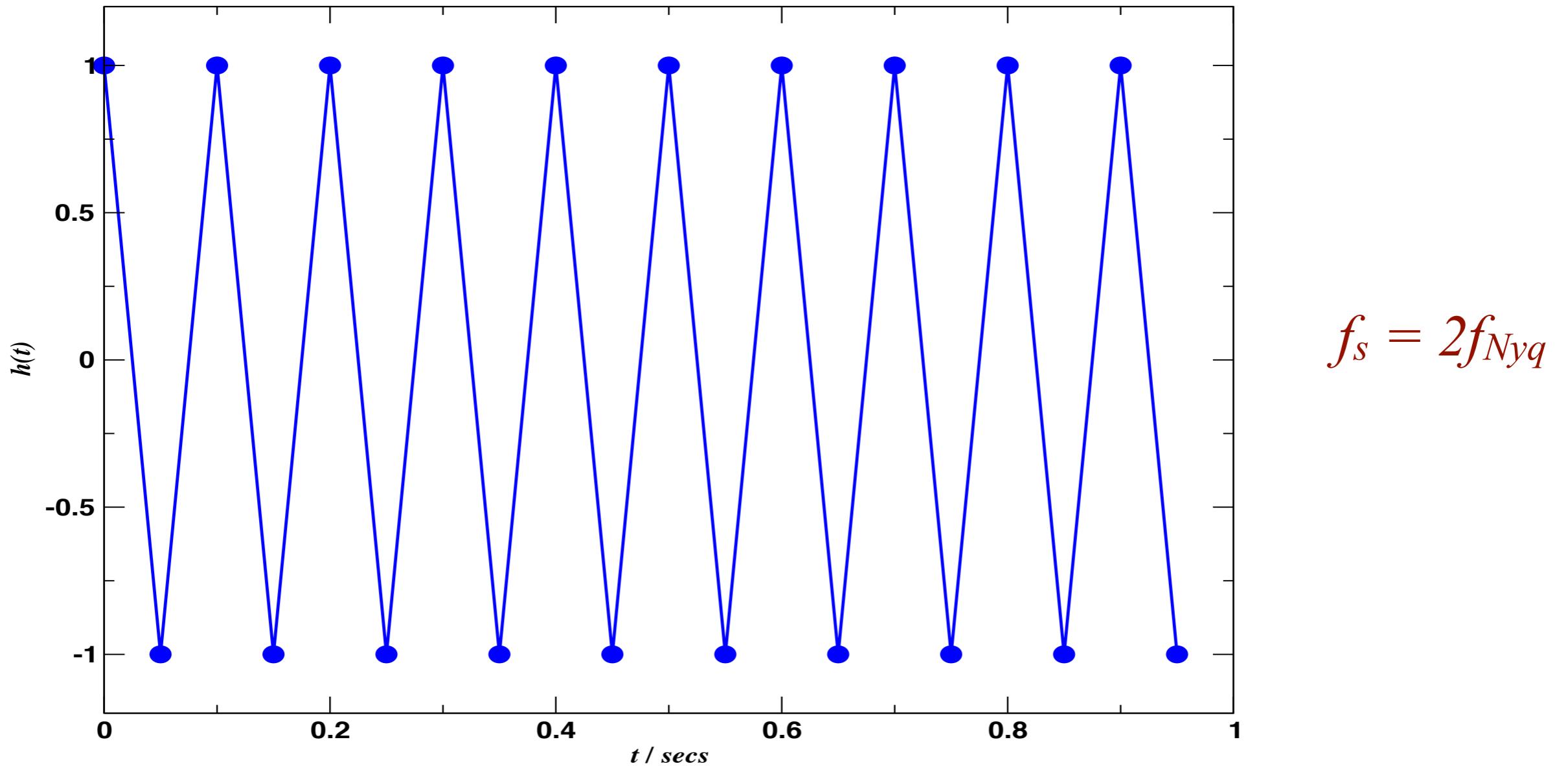
Sampling the data

- Nyquist theorem prescribes how to digitally represent a continuous signal
 - It defines a critical or Nyquist frequency taken to be the highest frequency content of the signal
 - Define:
 - Nyquist frequency - $f_{Nyq} \equiv f_{max}$
 - Sampling frequency - $f_s \geq 2f_{Nyq}$
 - Sampling period - $\Delta t = 1/f_s$
 - Sampling at less than twice the Nyquist frequency leads to “aliasing”
 - For GWs, if the sampling frequency is $f_s = 4096 \text{ Hz}$, the highest frequency signal we can model is $f_{max} = 2048 \text{ Hz}$
-



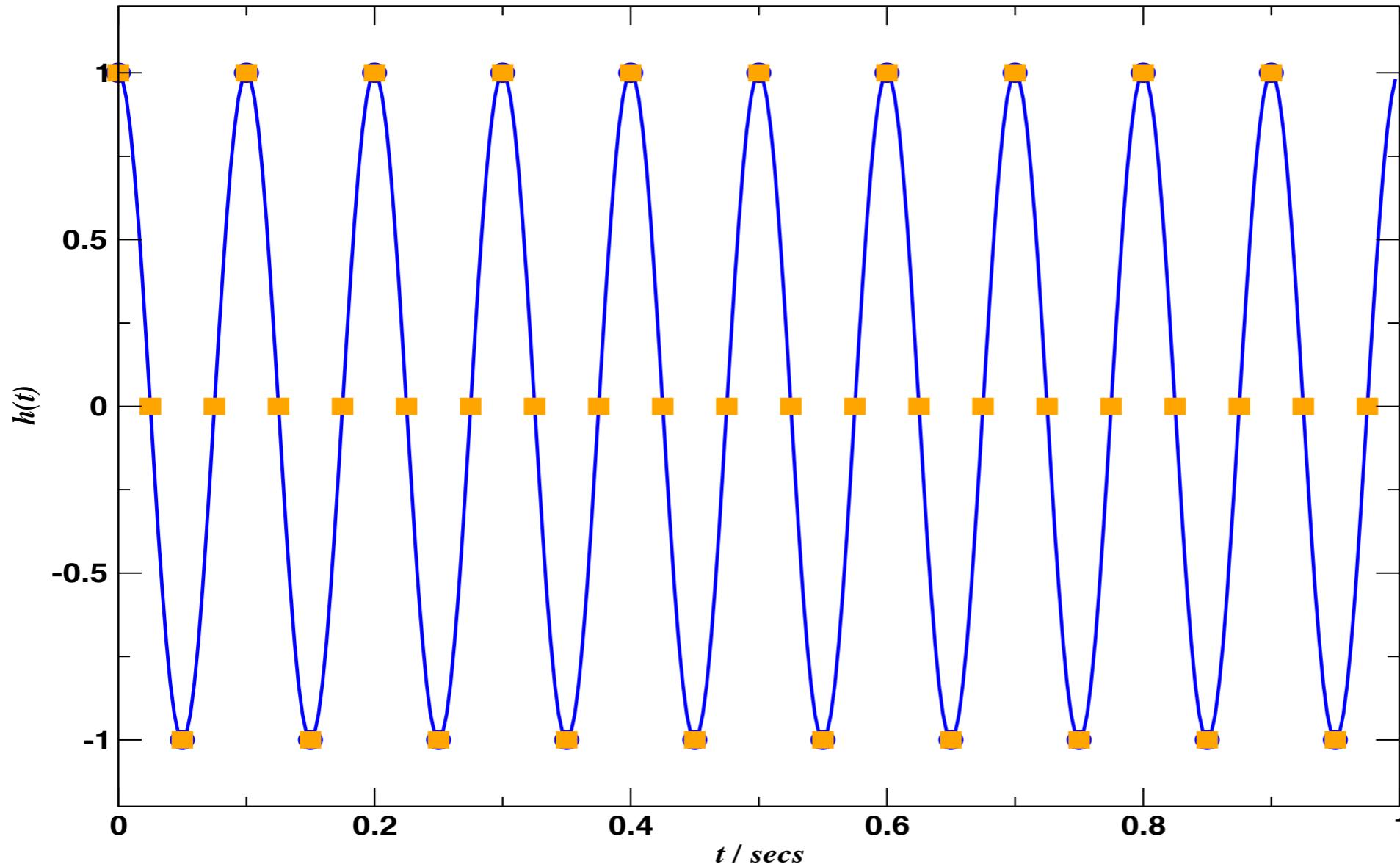
Sampling the data

- Example : sine-wave with $f = 10 \text{ Hz}$, $T_{obs} = 1 \text{ sec}$, $dt = 1/f_s$



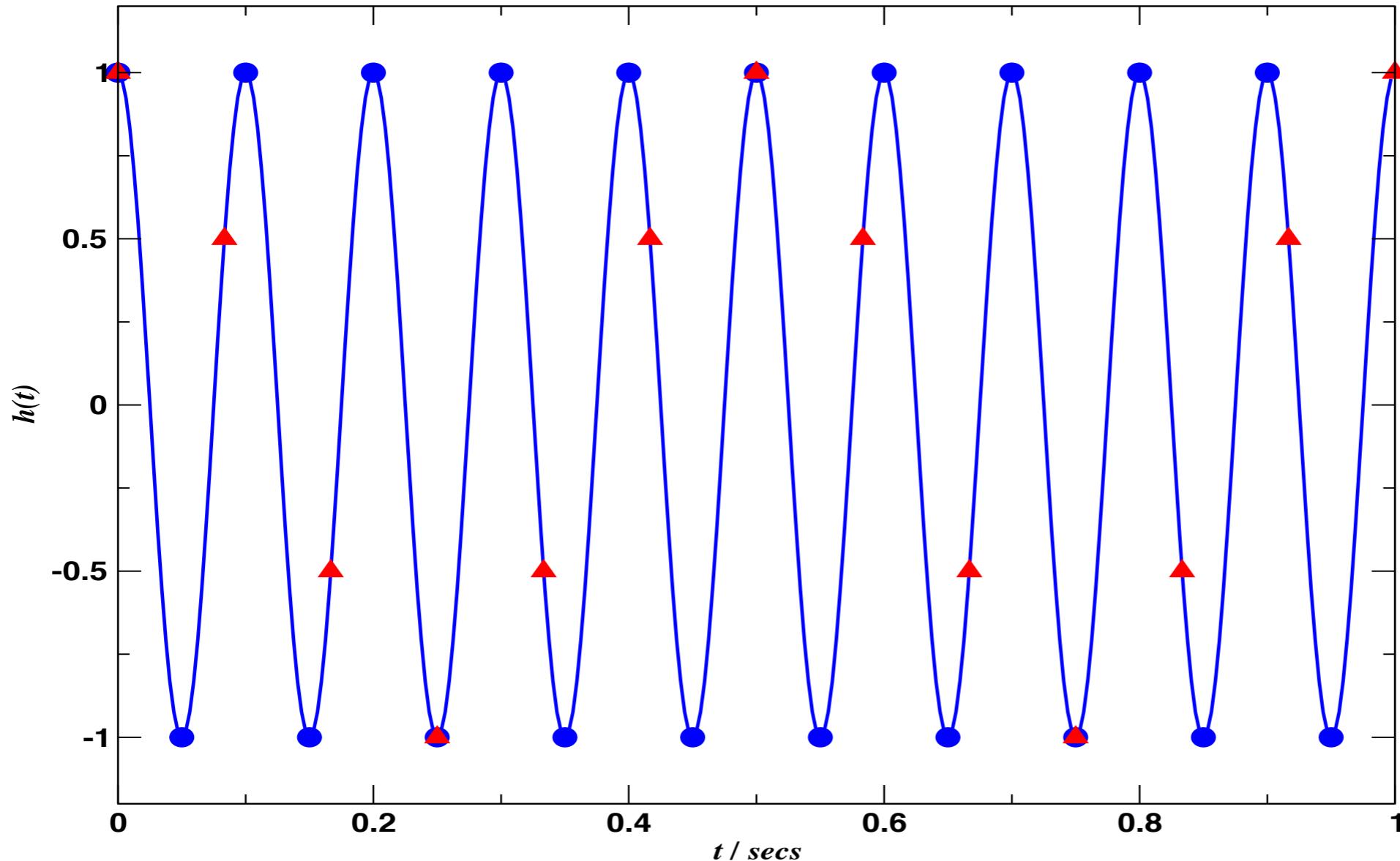
Sampling the data

- If I oversample...?



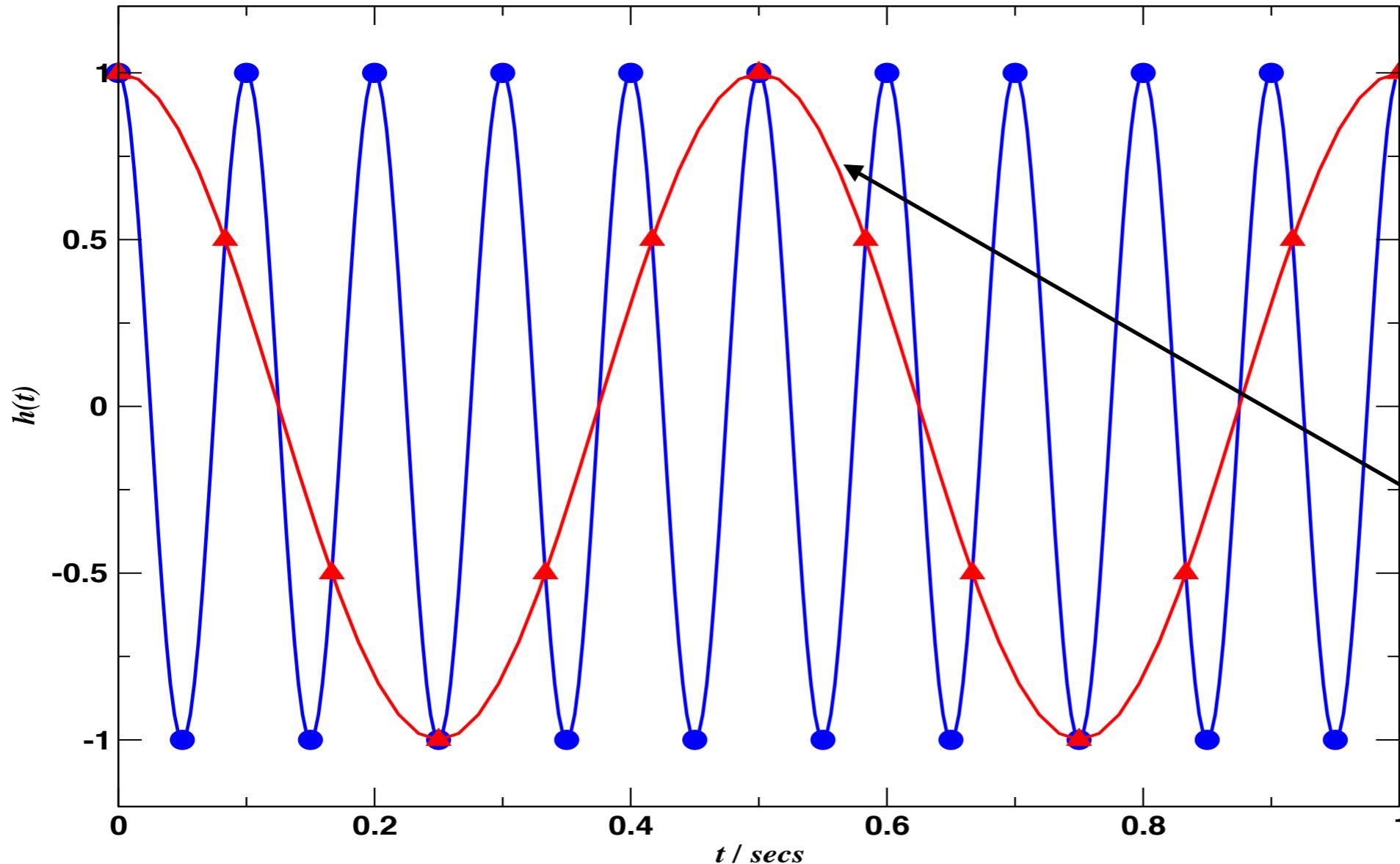
Sampling the data

- and if I undersample...?



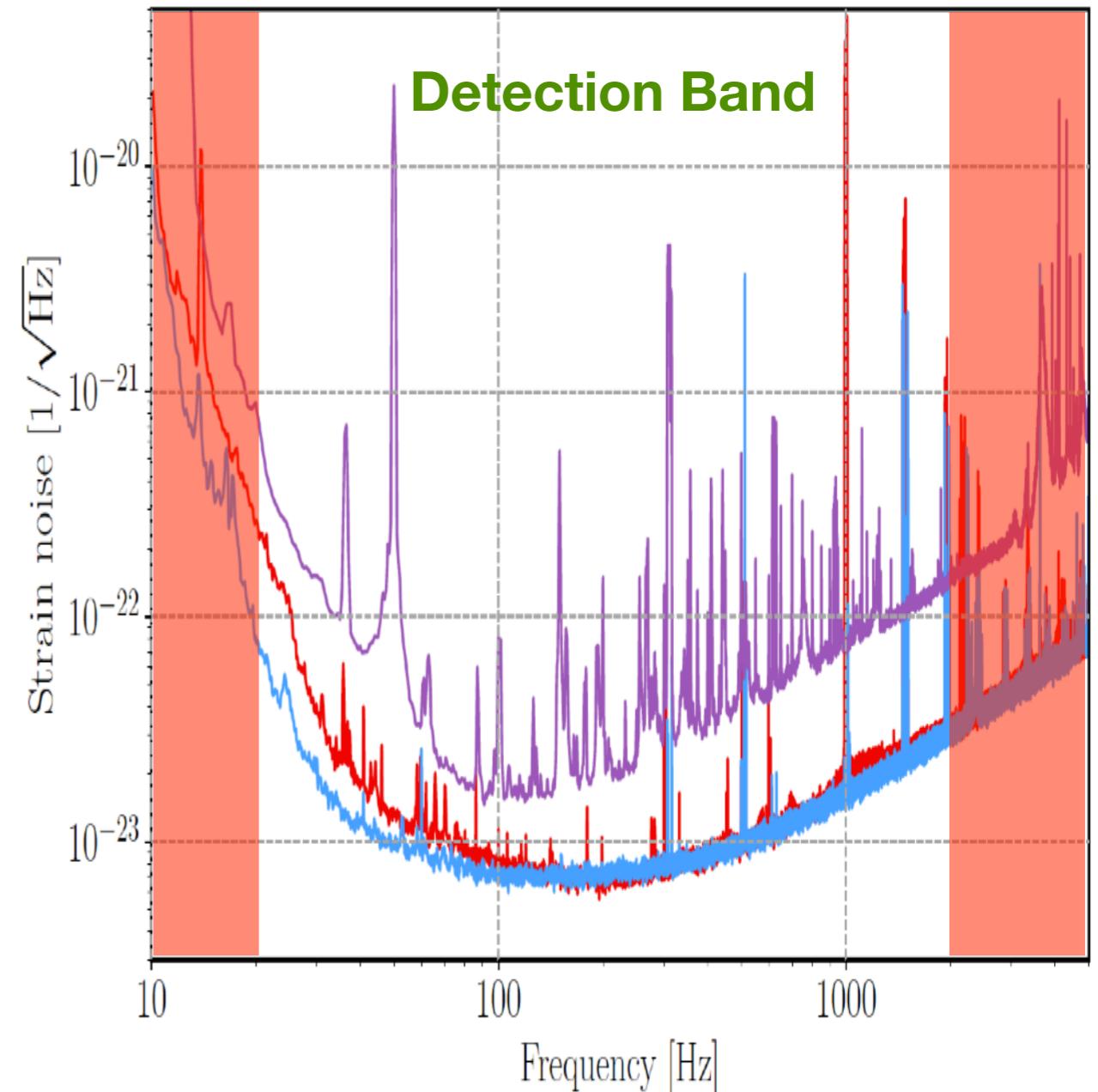
Sampling the data

- I get aliasing!!



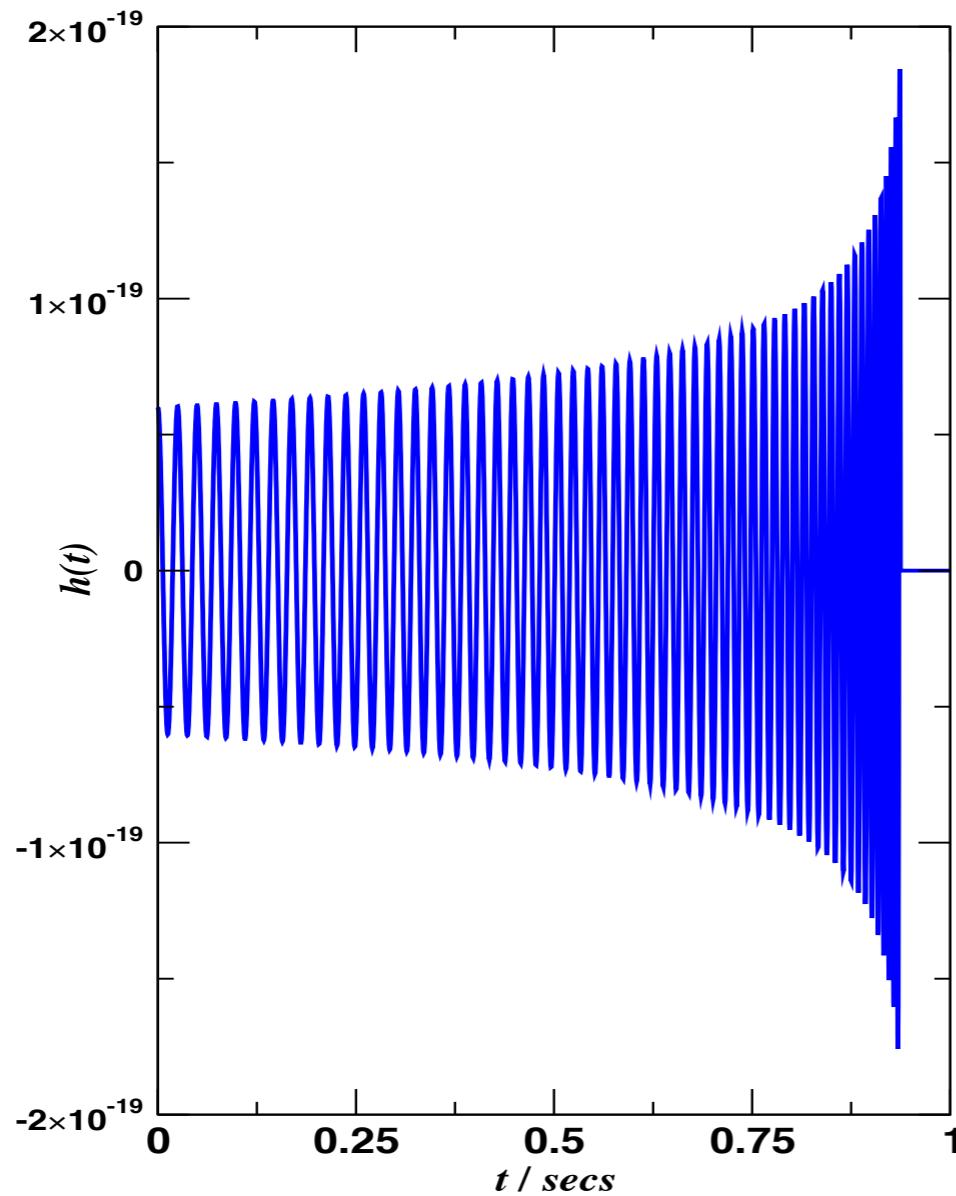
Low and High-band pass filtering

- Detectors very noisy below 20Hz and above 2kHz
- High pass filter > 20Hz
- Low pass filter < 2kHz



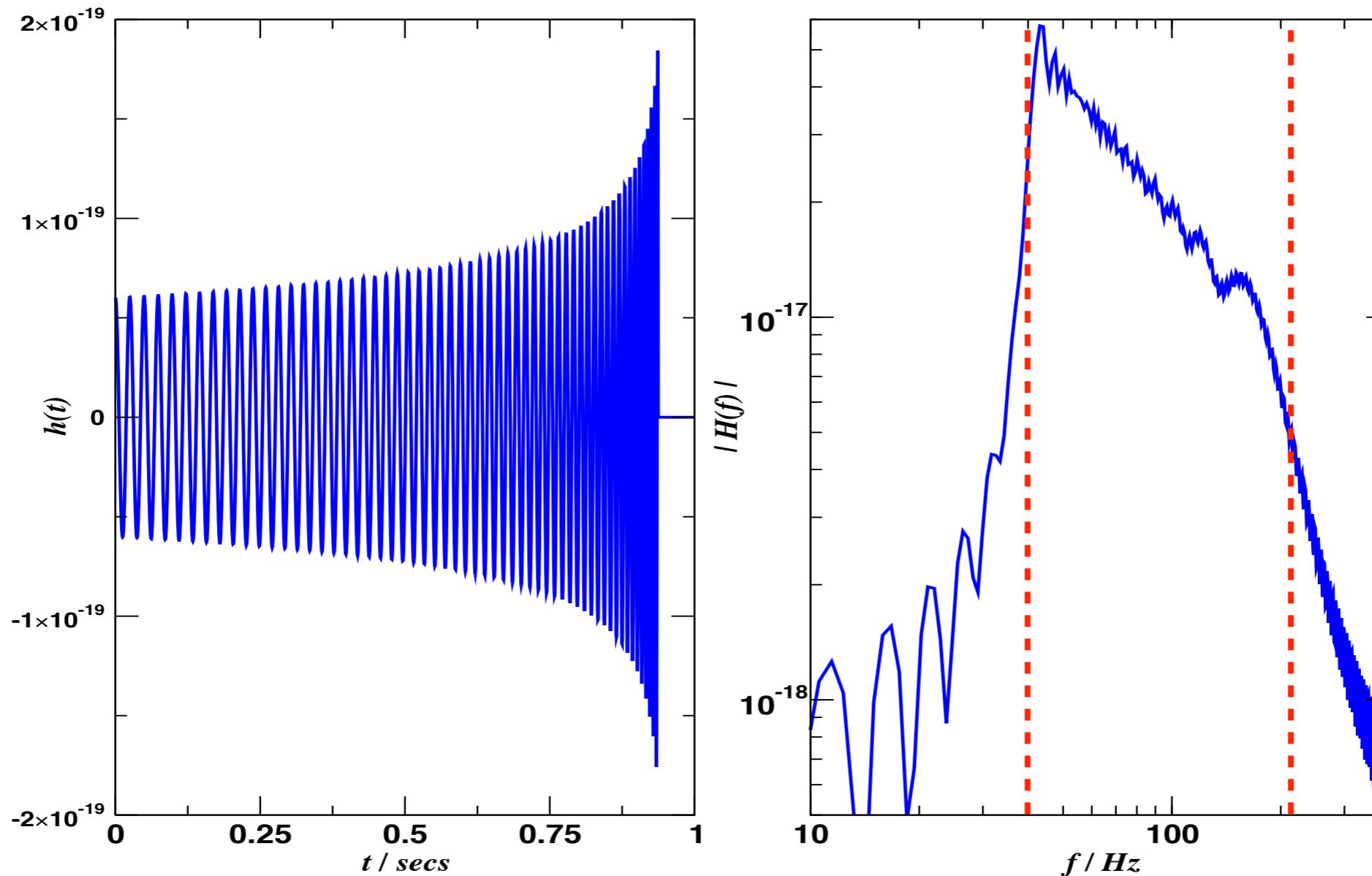
Windowing the data

“Newtonian” inspiral chirp for a (10,10) solar mass system



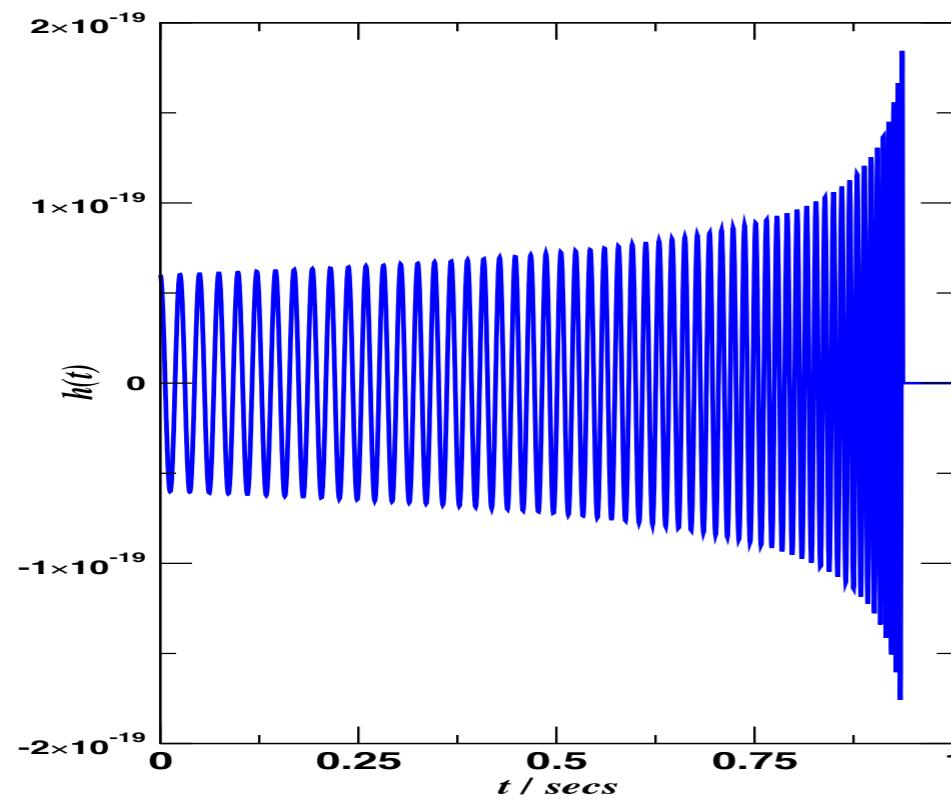
Windowing the data

large oscillations, spectral leakage...what's going on?

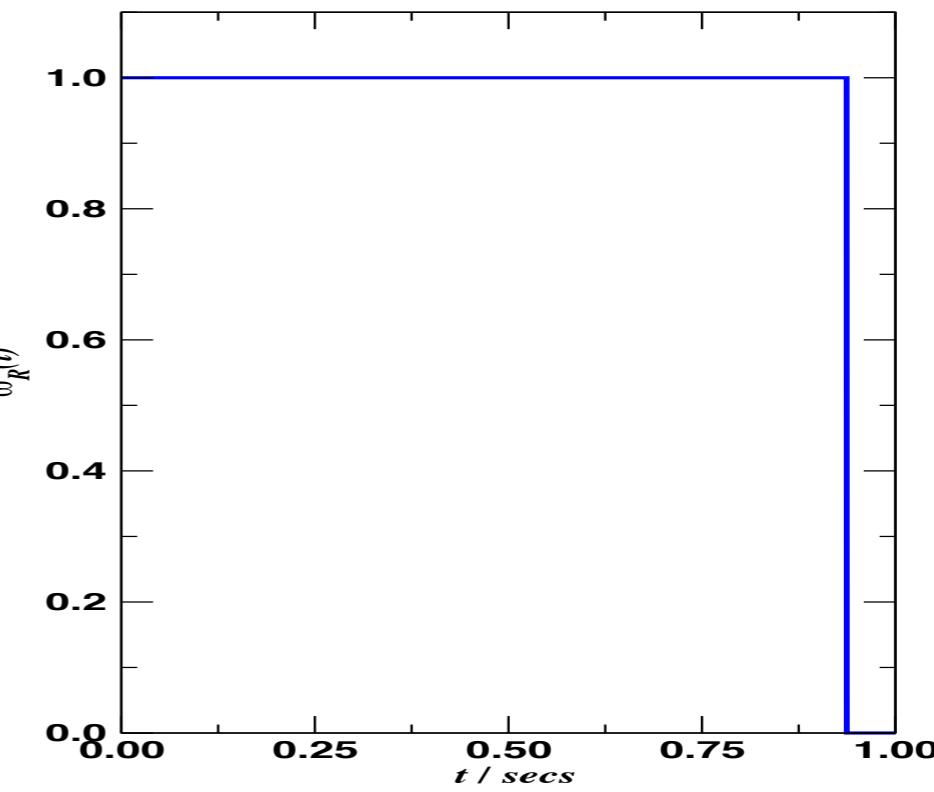


Windowing the data

- Our signal starts abruptly at $t = 0$, and finishes abruptly at $t = 0.973$ secs
- Equivalent to multiplying the signal with a rectangular window function
- and....?

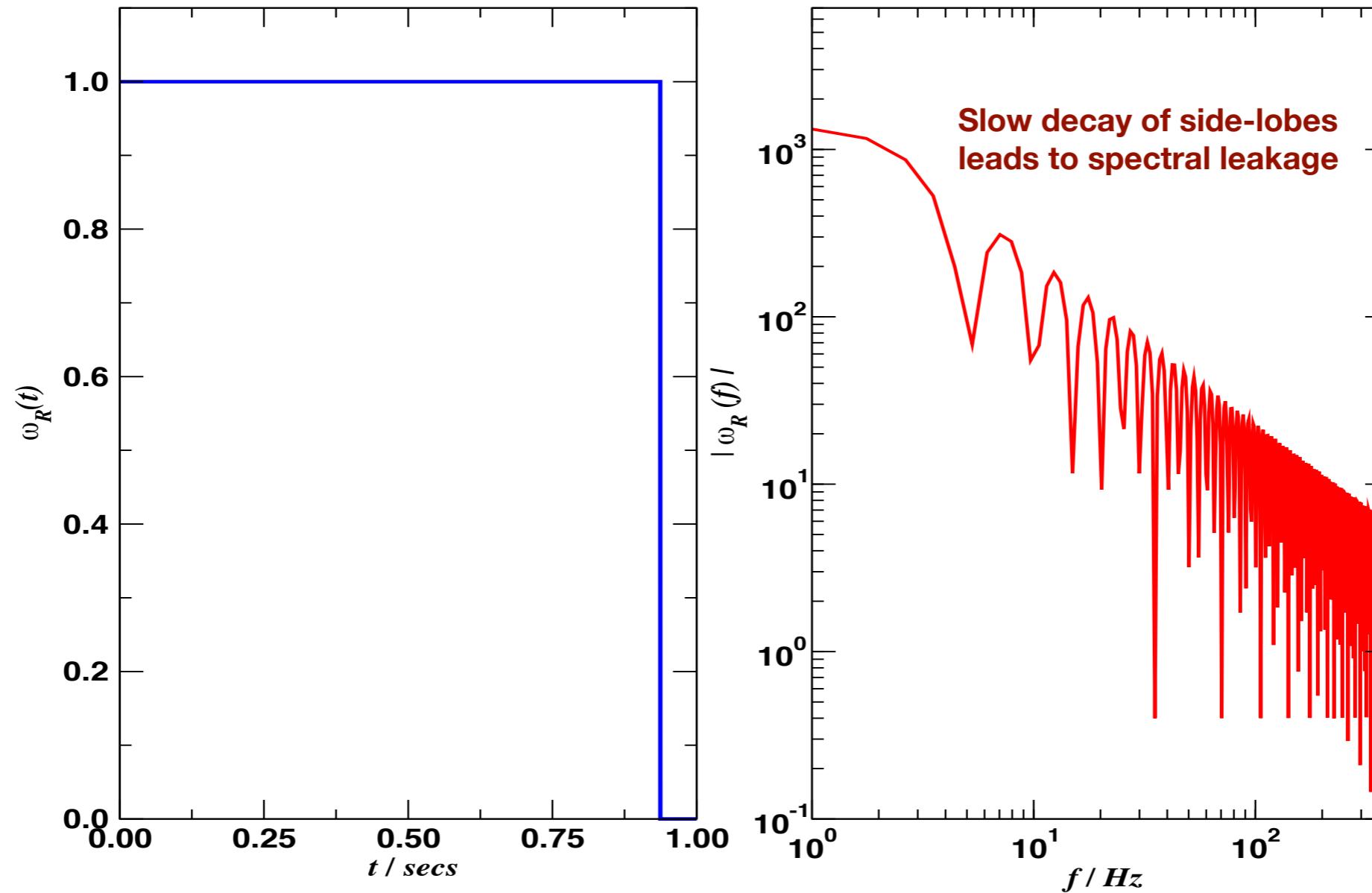


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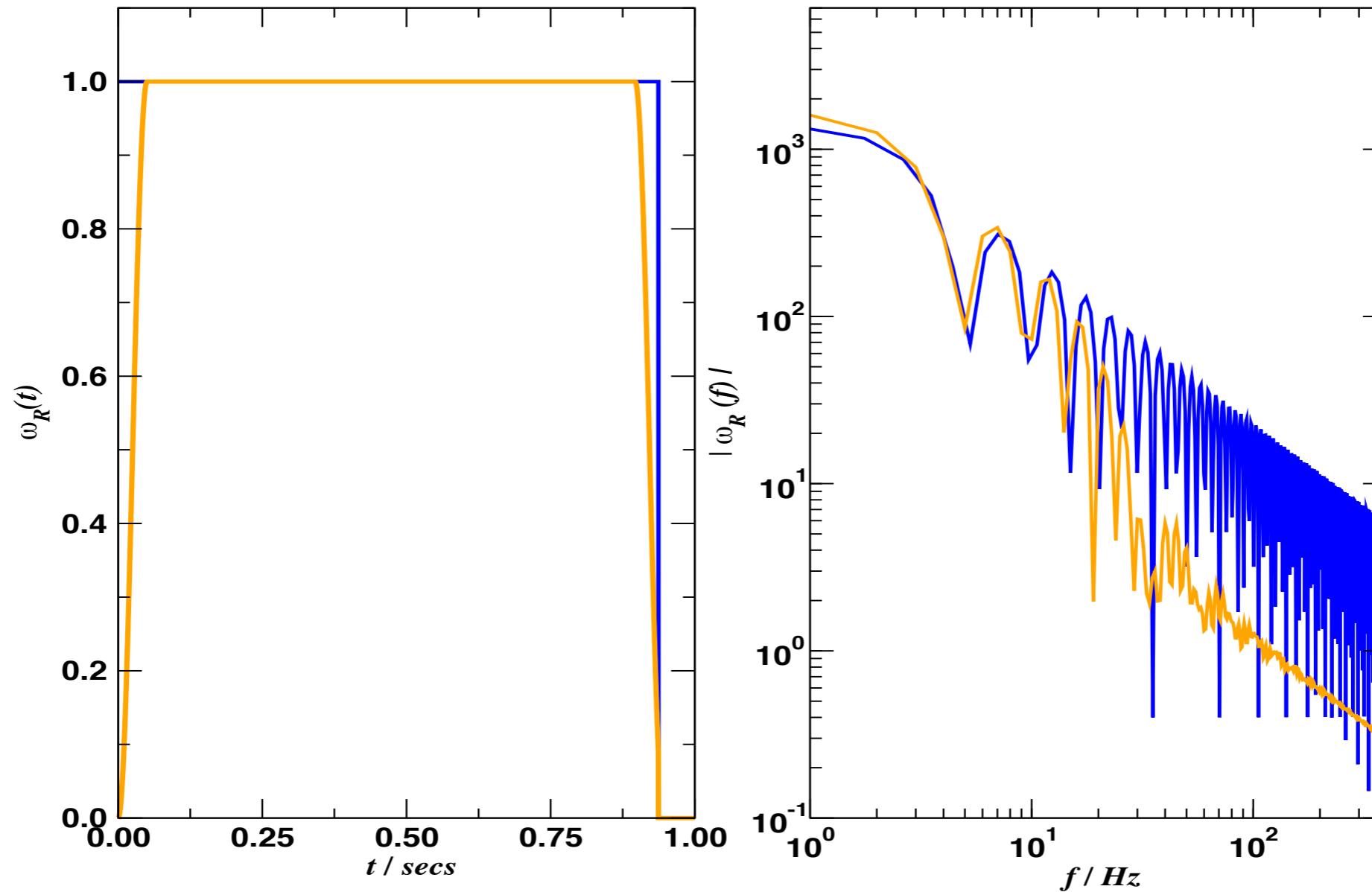
Windowing the data

FT of a rectangular window function



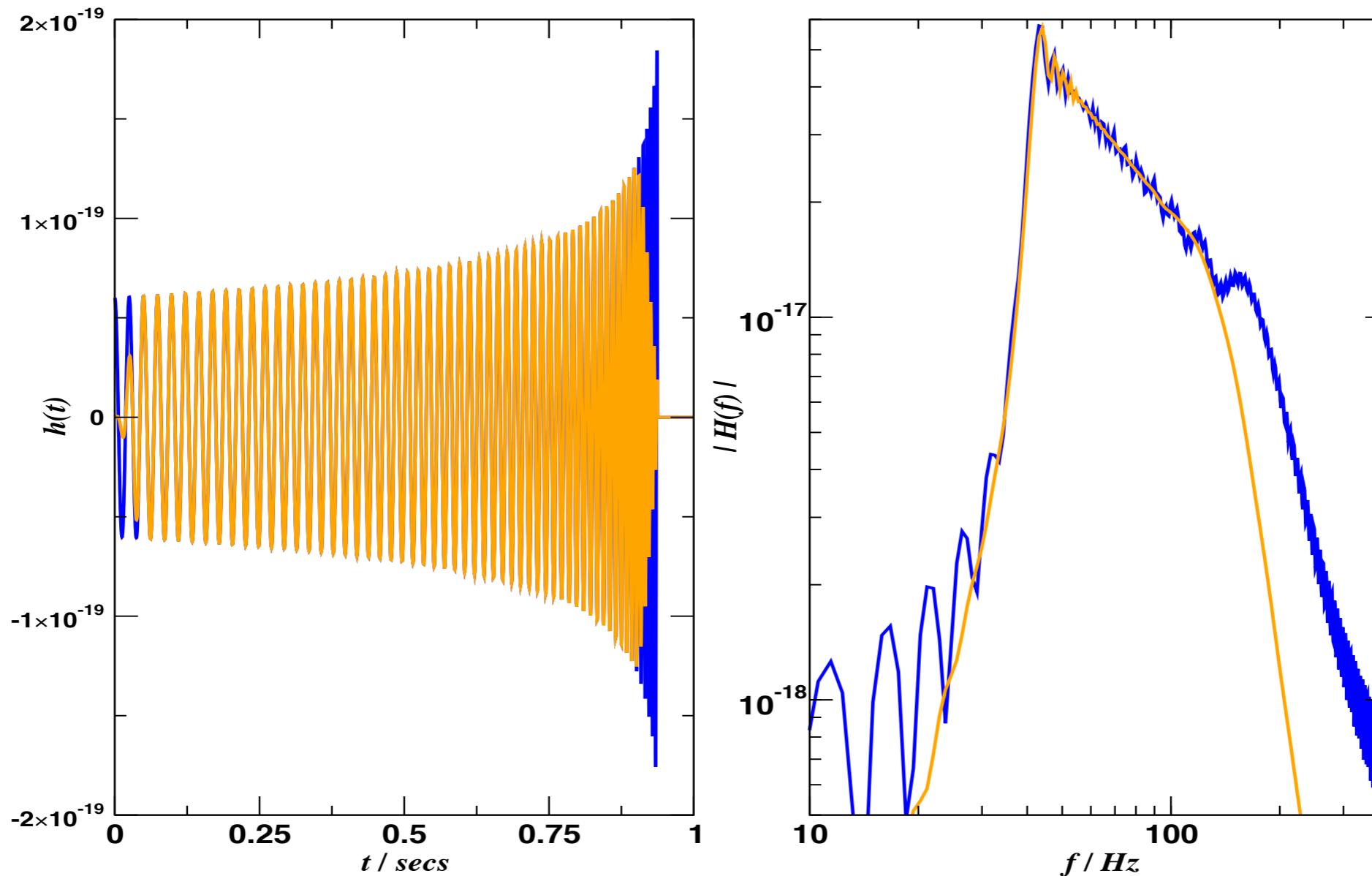
Windowing the data

FT of a 1/2-Hann window function

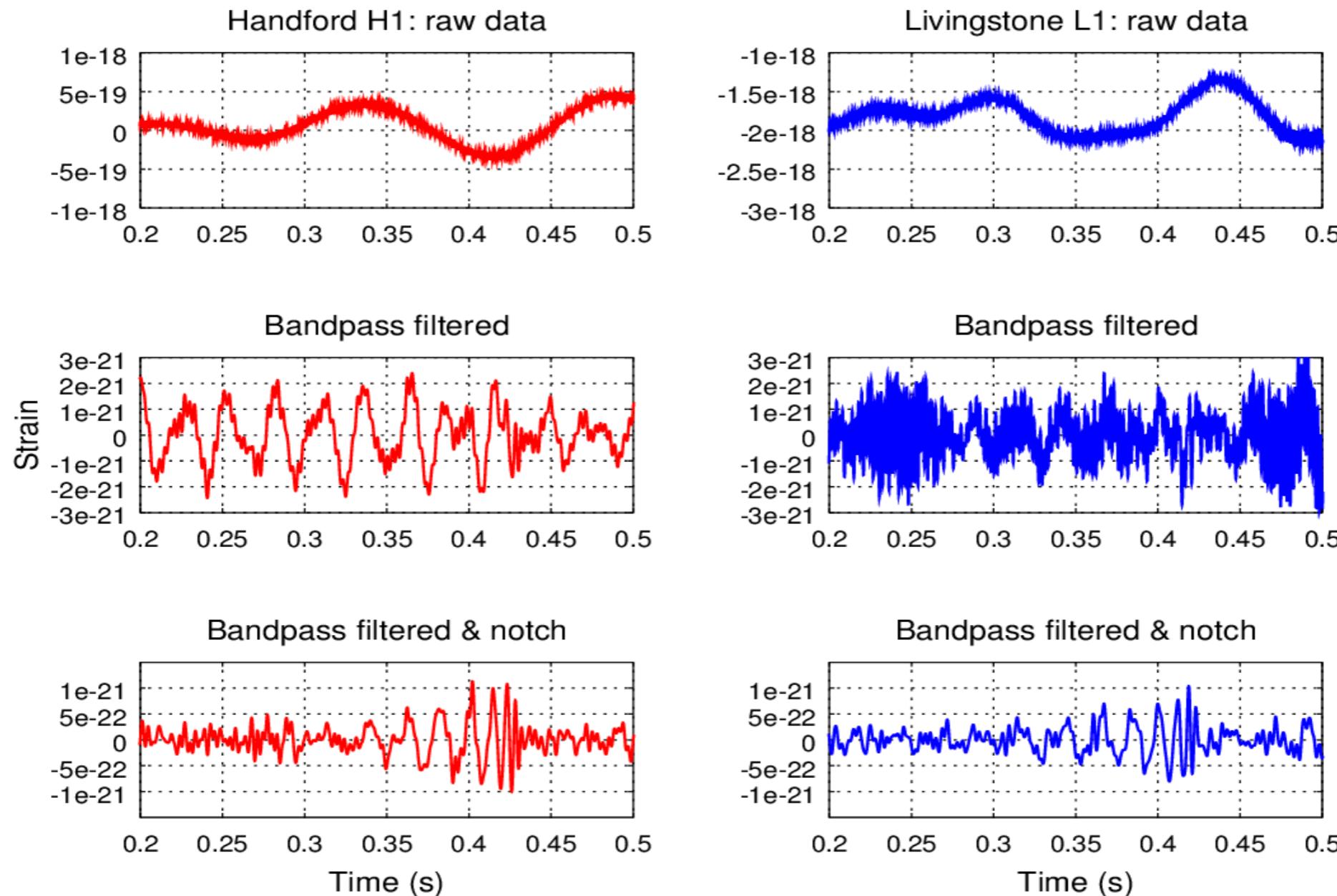


Windowing the data

FT of a chirp waveform using a 1/2-Hann window function



Application to real data



Primer on GW data analysis

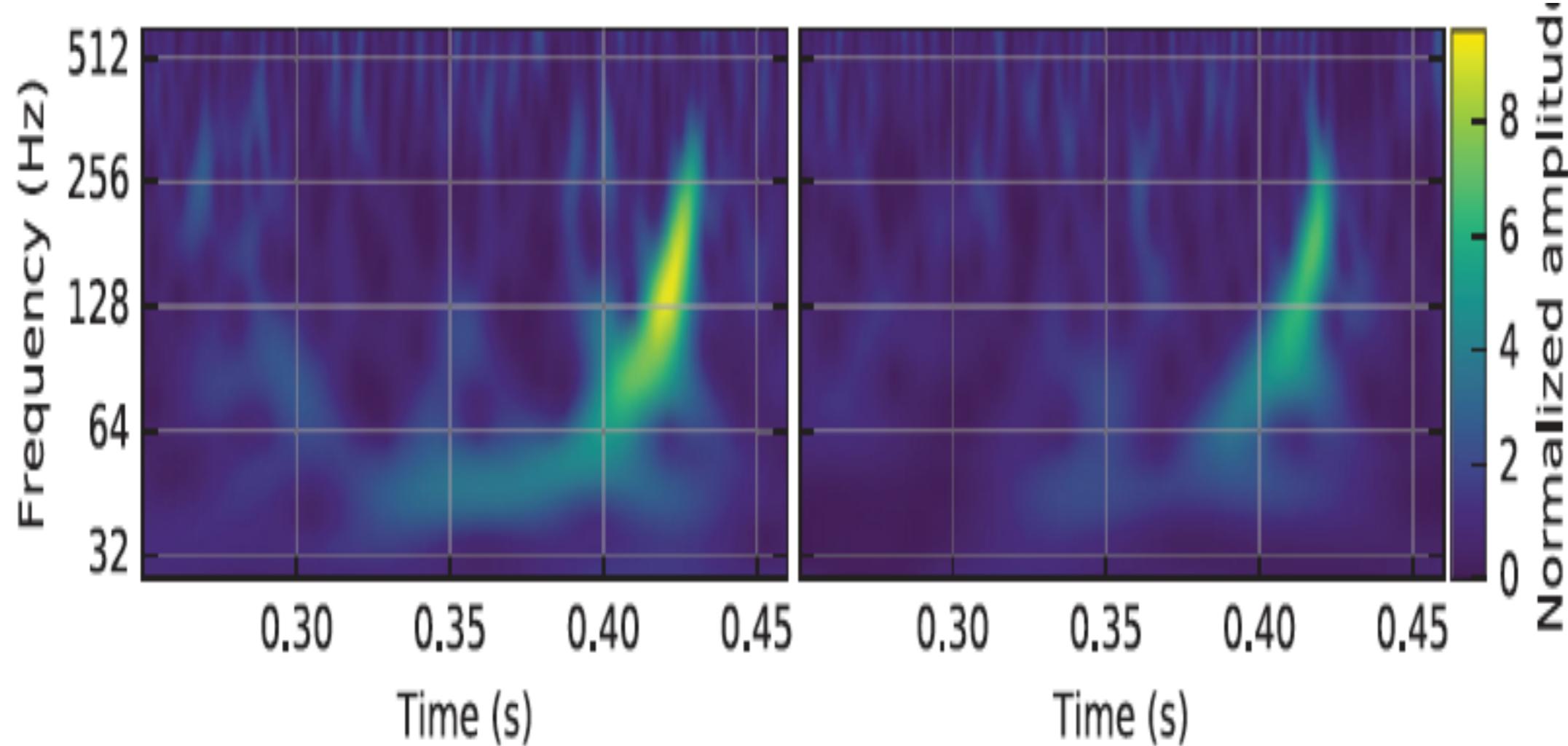
- Two parts:
 - Detection
 - Parameter estimation (Bayesian inference)



Time-Frequency Analysis

GW150914

Abbott et al, PRL 116, 061102 (2016)

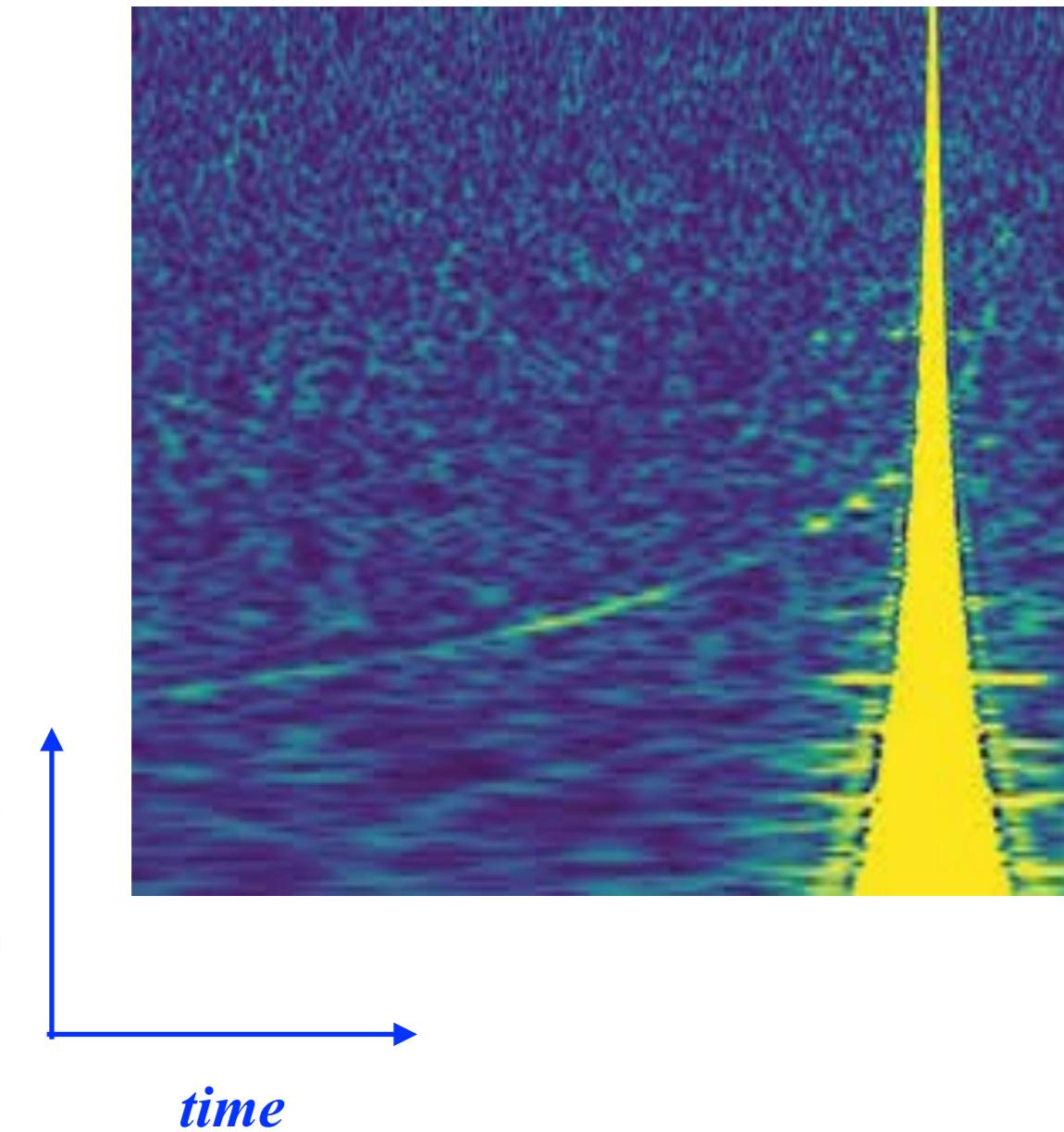


First GW detection was made by the cWB pipeline

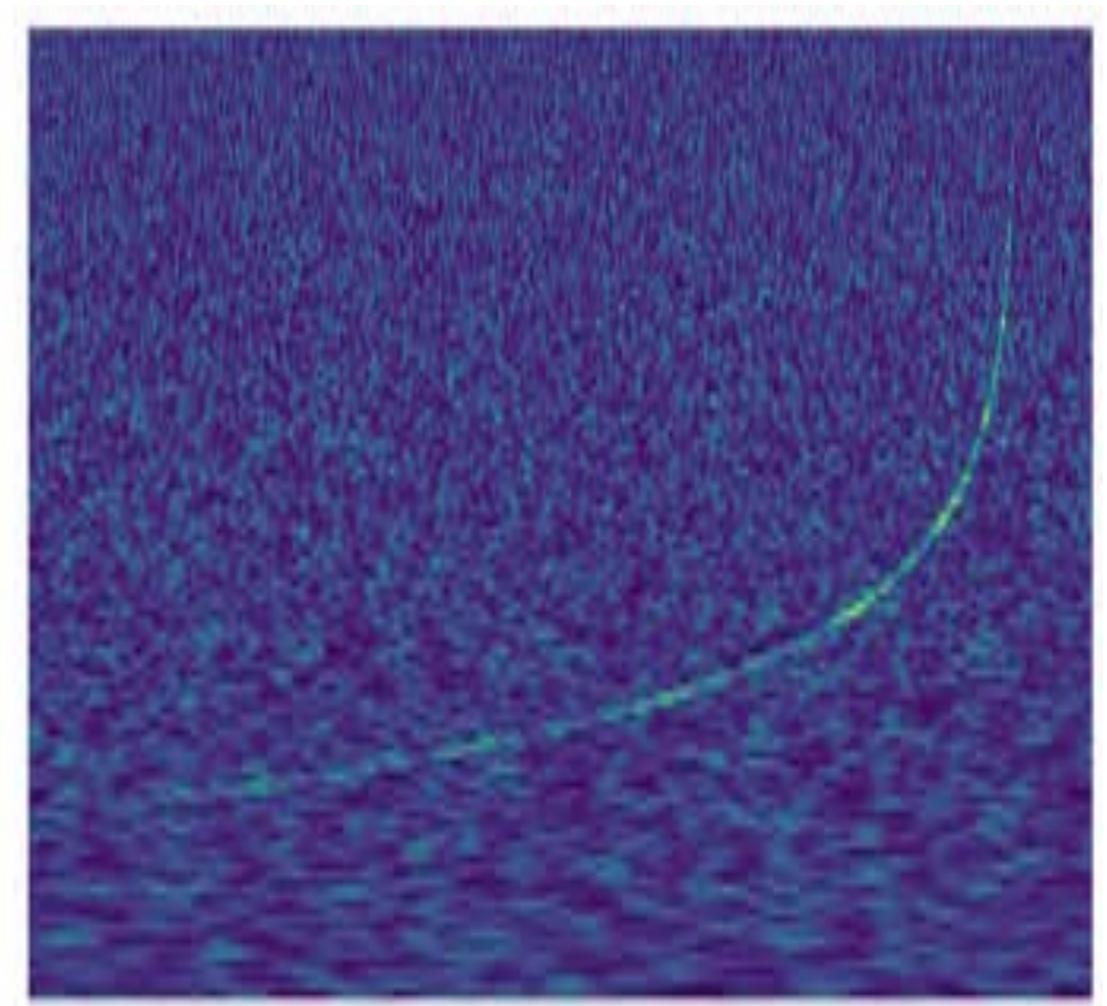


Time-Frequency Analysis

GW170817+glitch



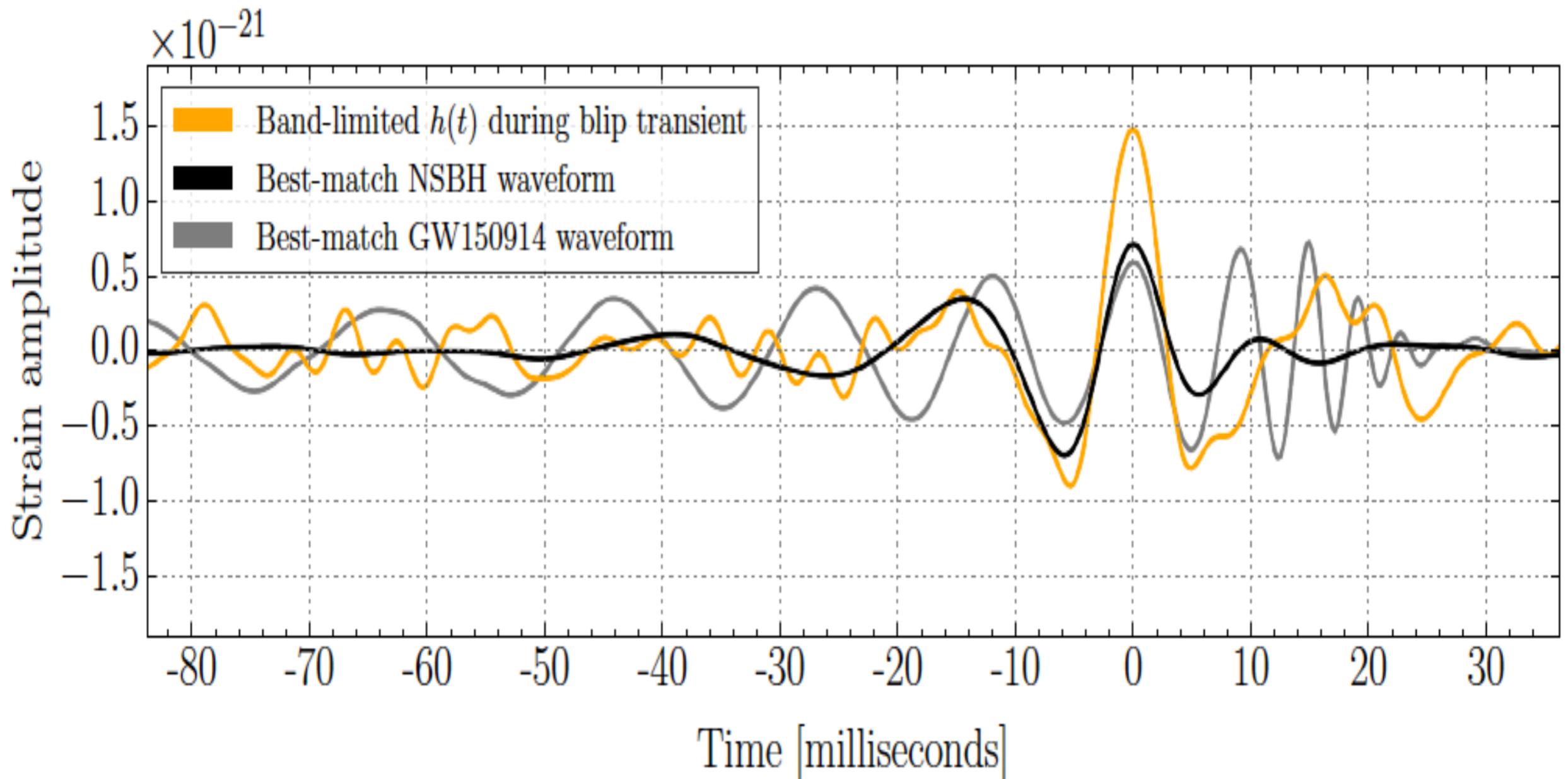
GW170817+glitch removed



Abbott et al, PRL 116, 061102 (2016)

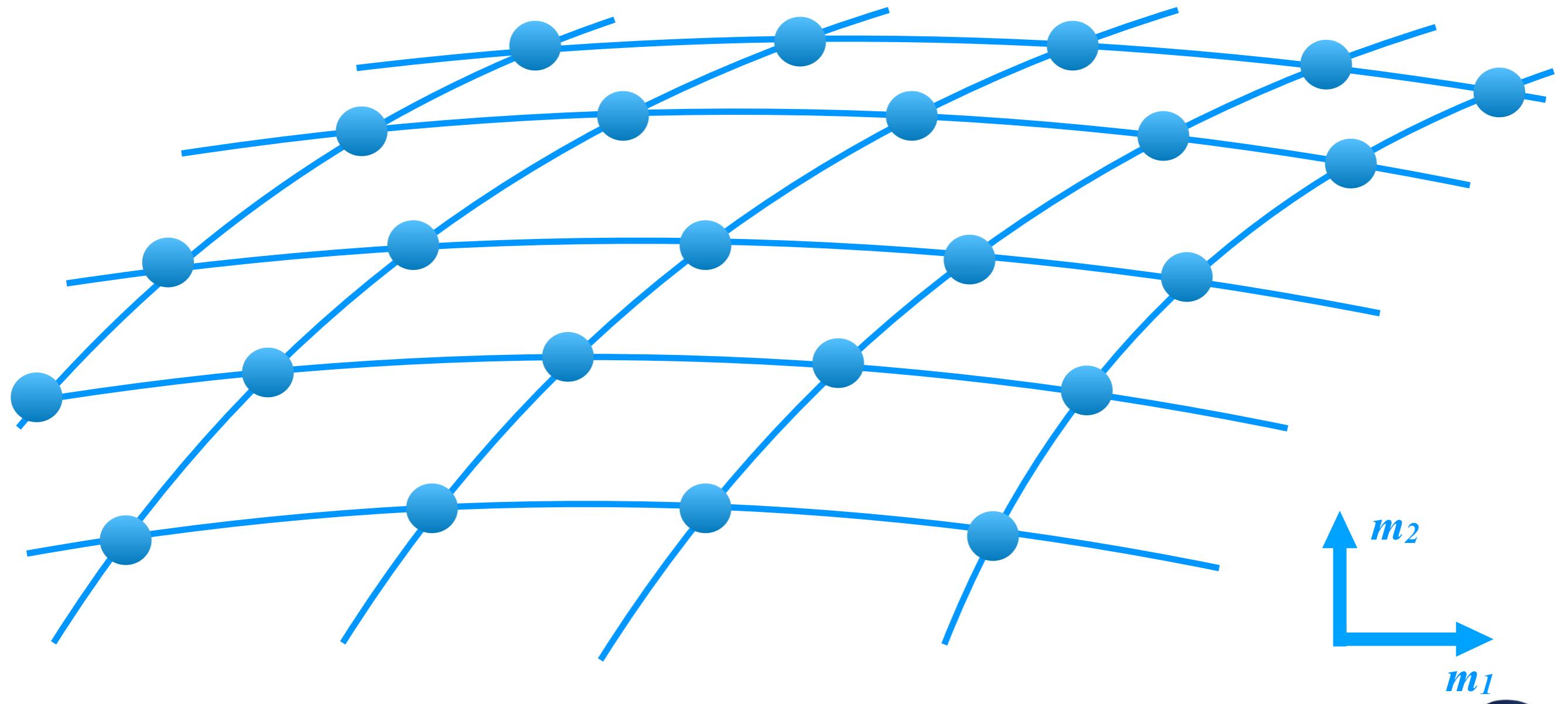


Glitches



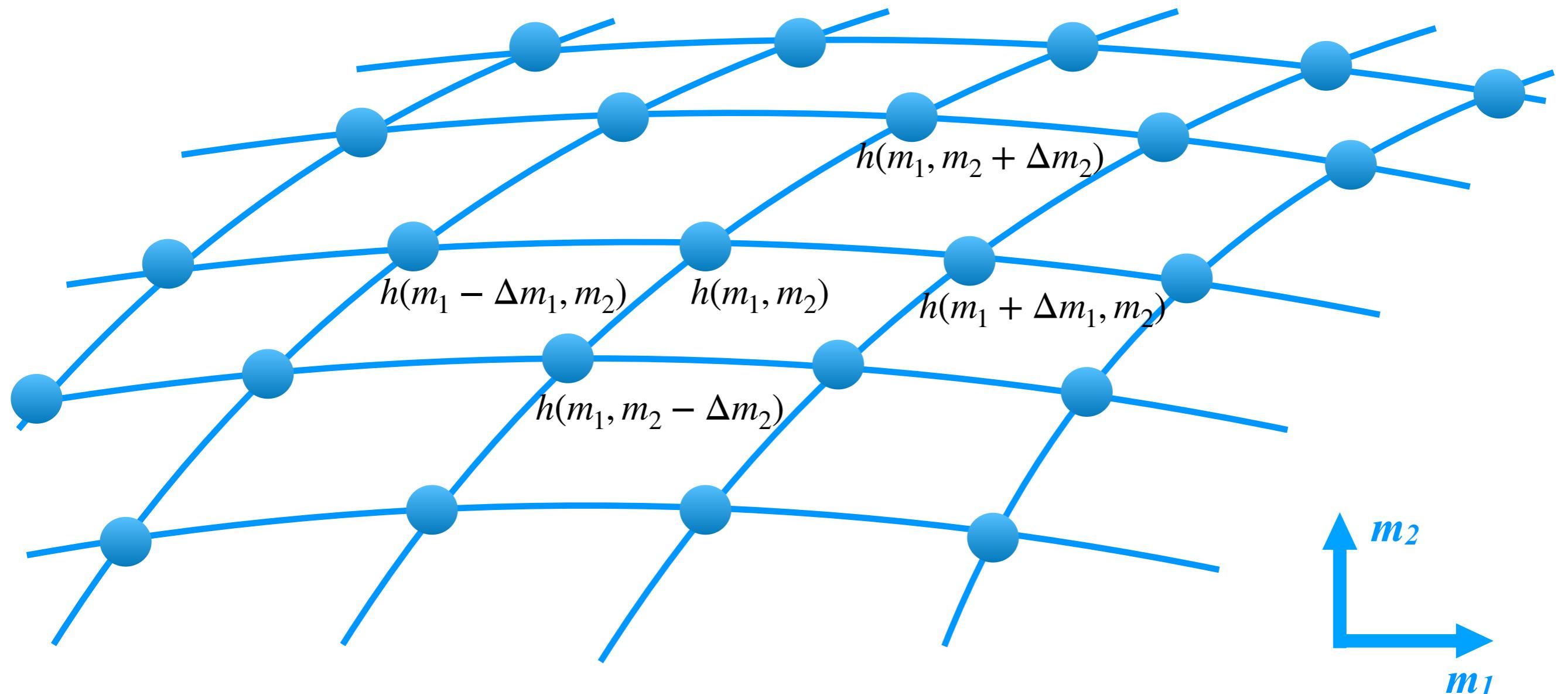
Detection

- Template Grid : assume 2D



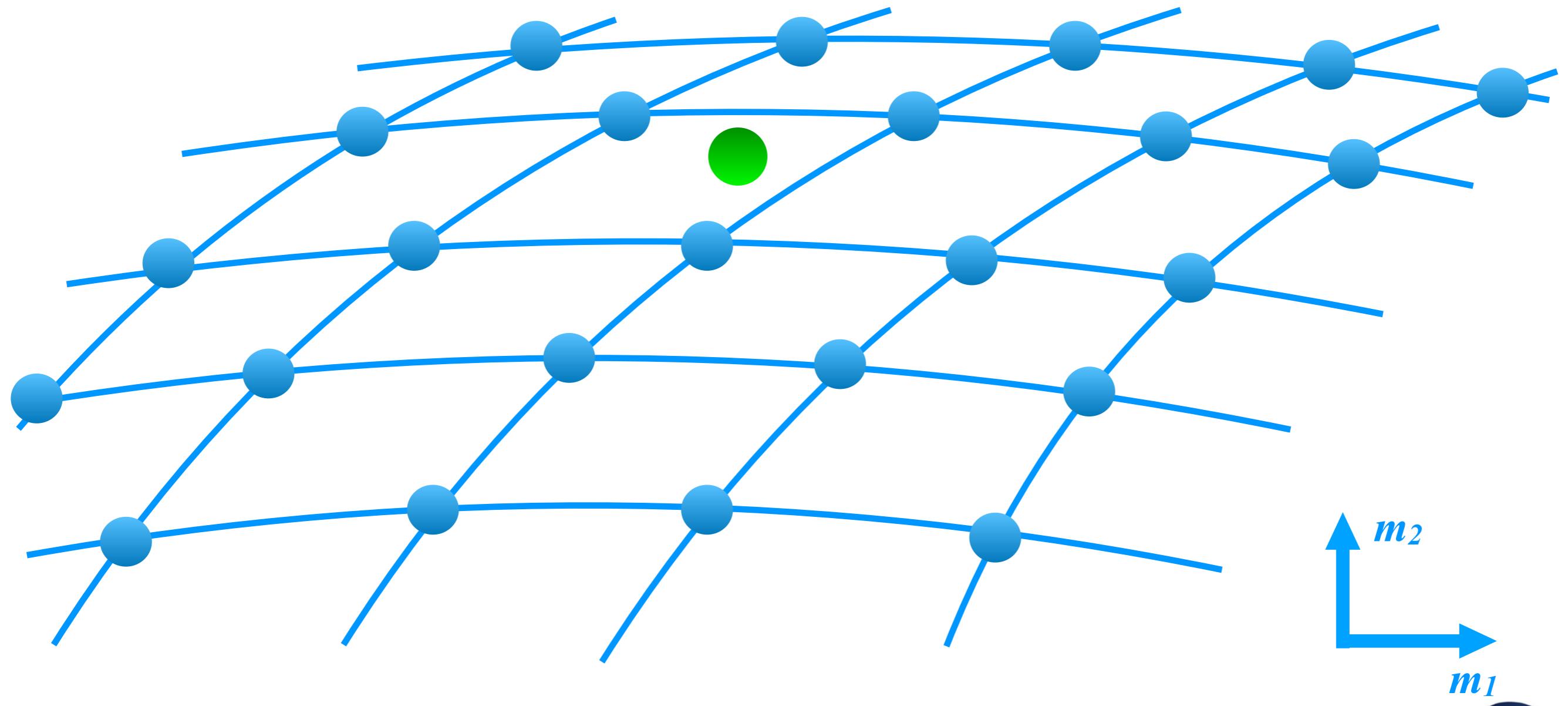
Detection

- Template Grid



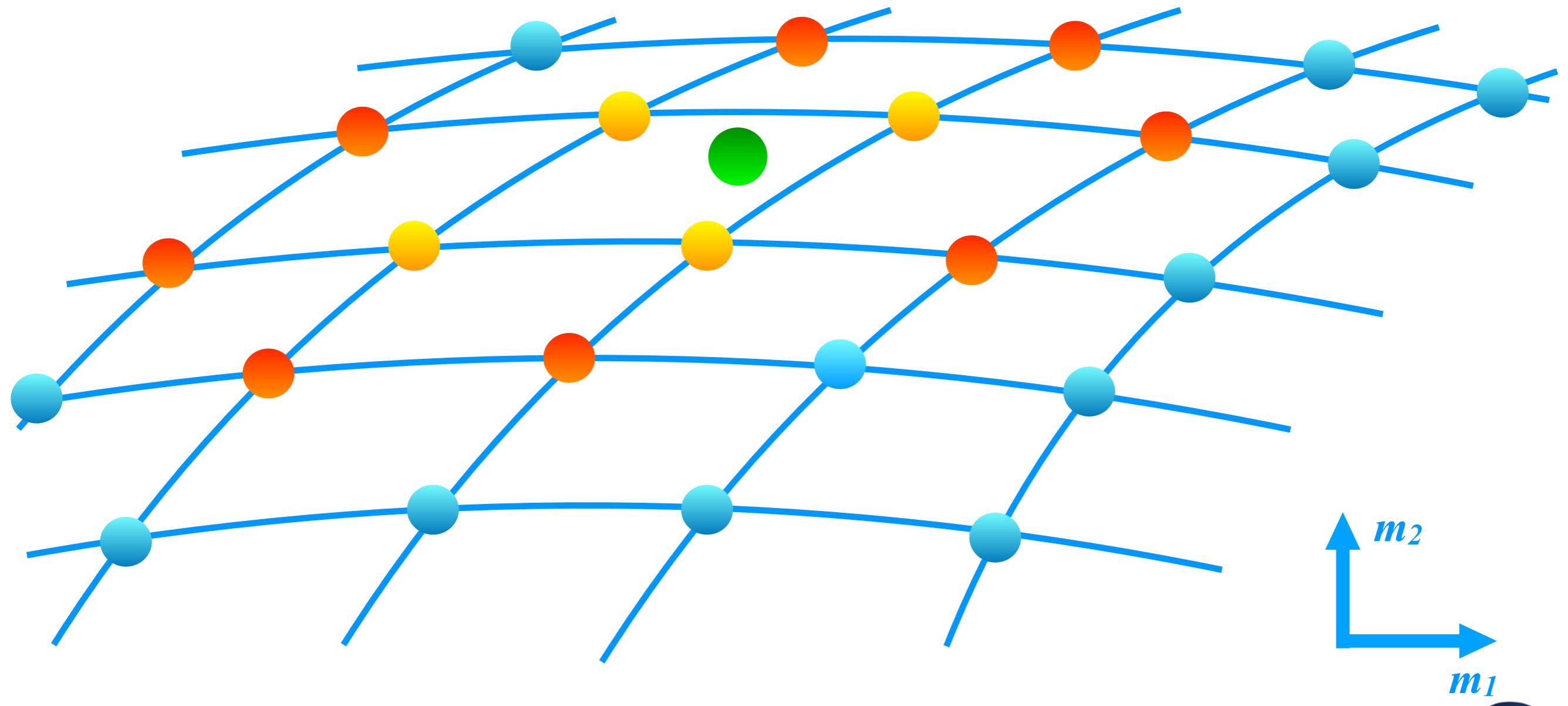
Detection

- Template Grid

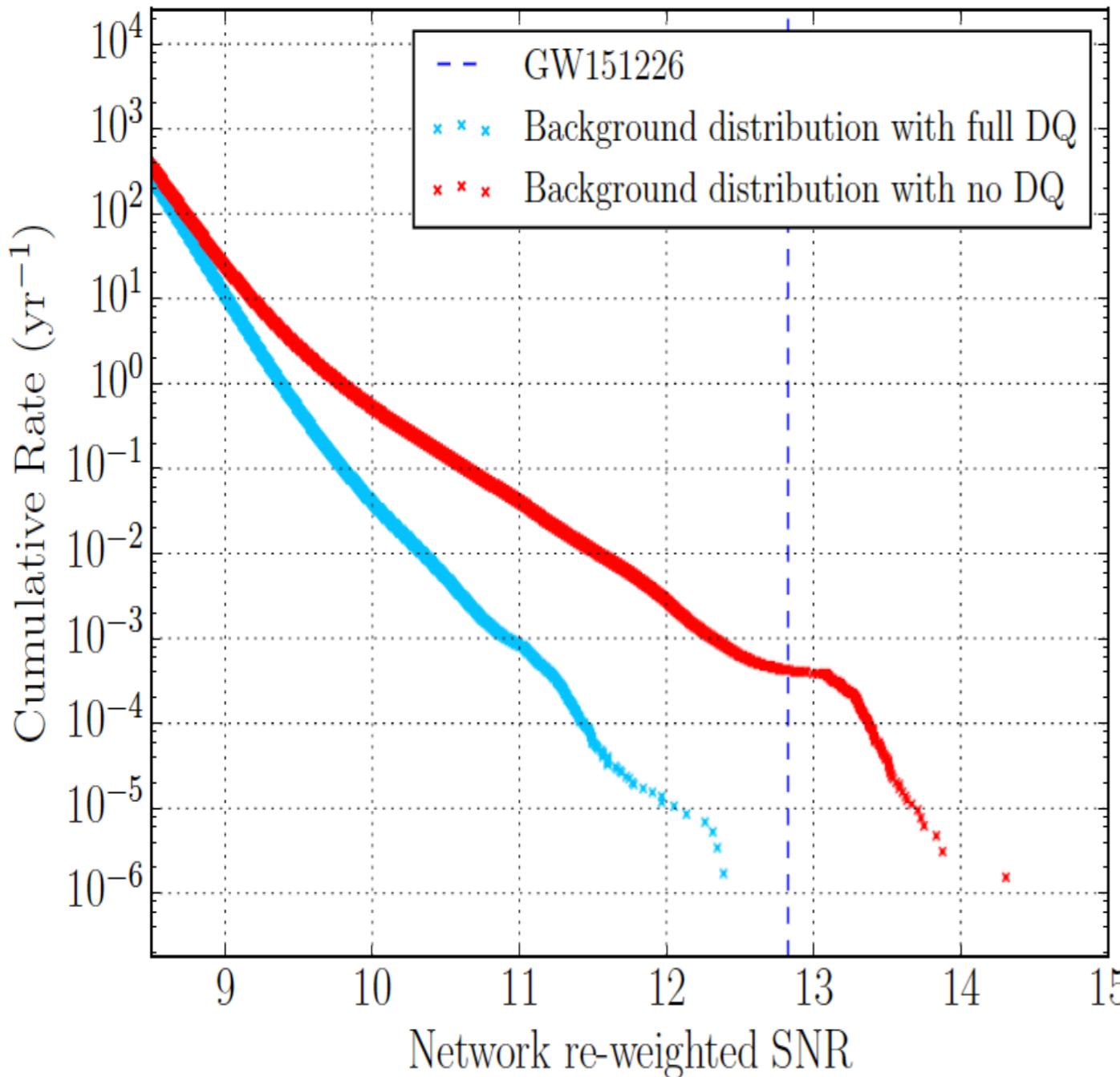


Detection

- Template Grid



Data Quality & Detector Characterisation



Detector Characterisation improved the FAR of GW151226 by a factor of 500: from 1/320 years to 1/183000 years

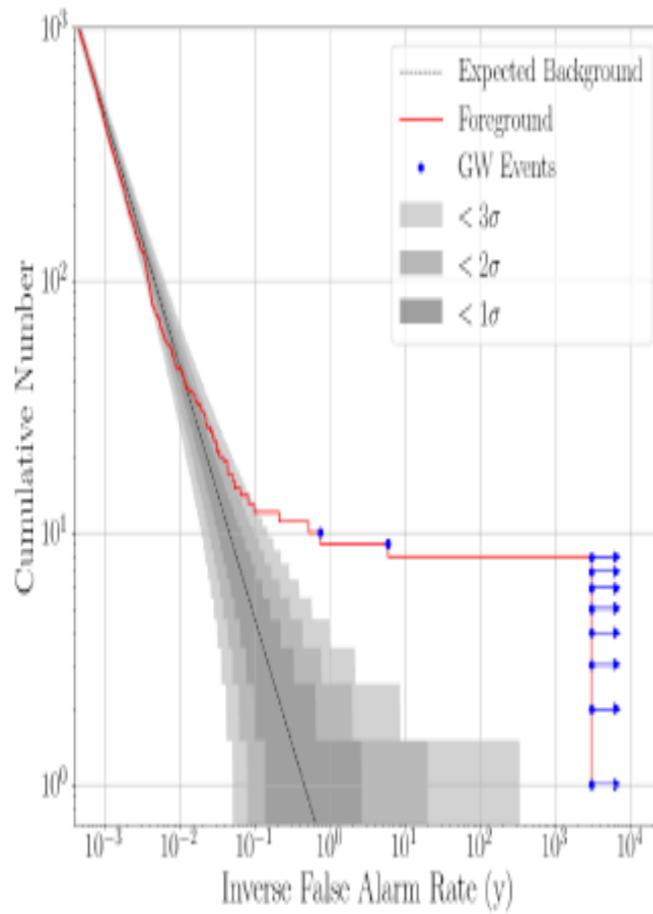
Also need to calibrate the time series: reduce the error in amplitude and phase measurement

B. Abbott, CQG 2018

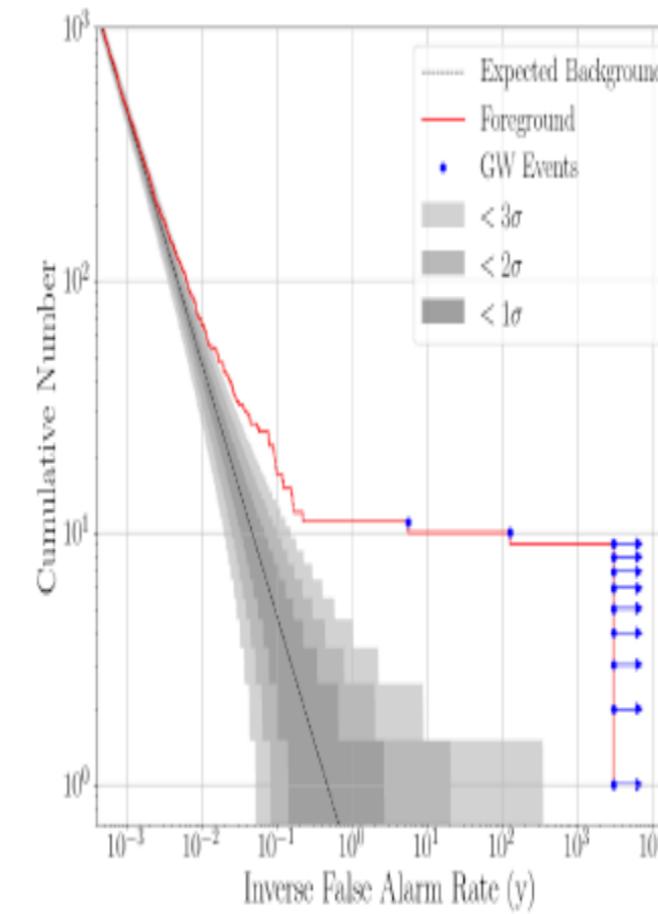


False Alarm Rates

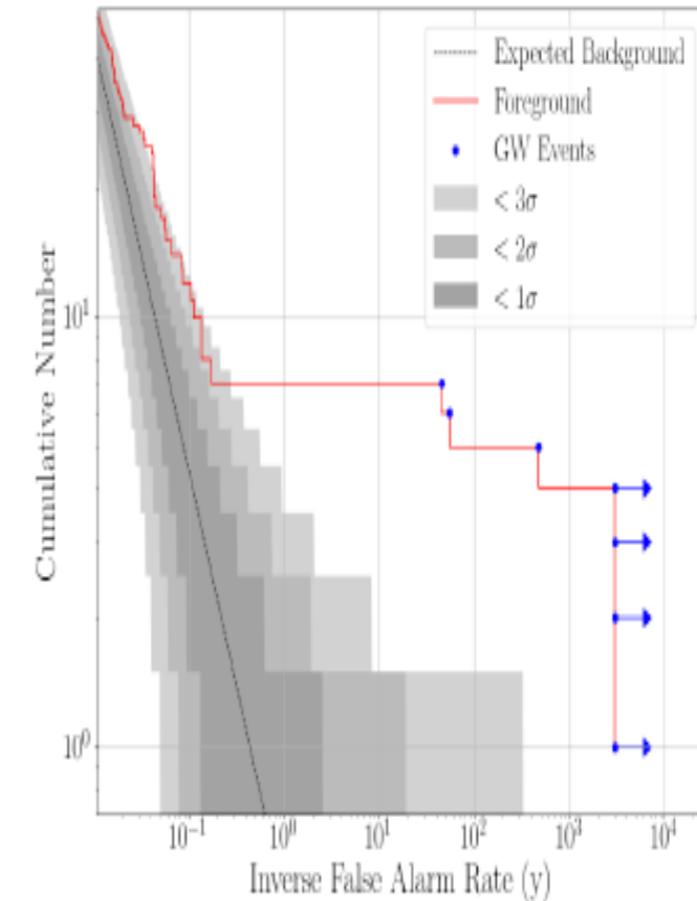
PyCBC



GstLAL



cWB



Abbott et al, arXiv:1811.12907 (2018)

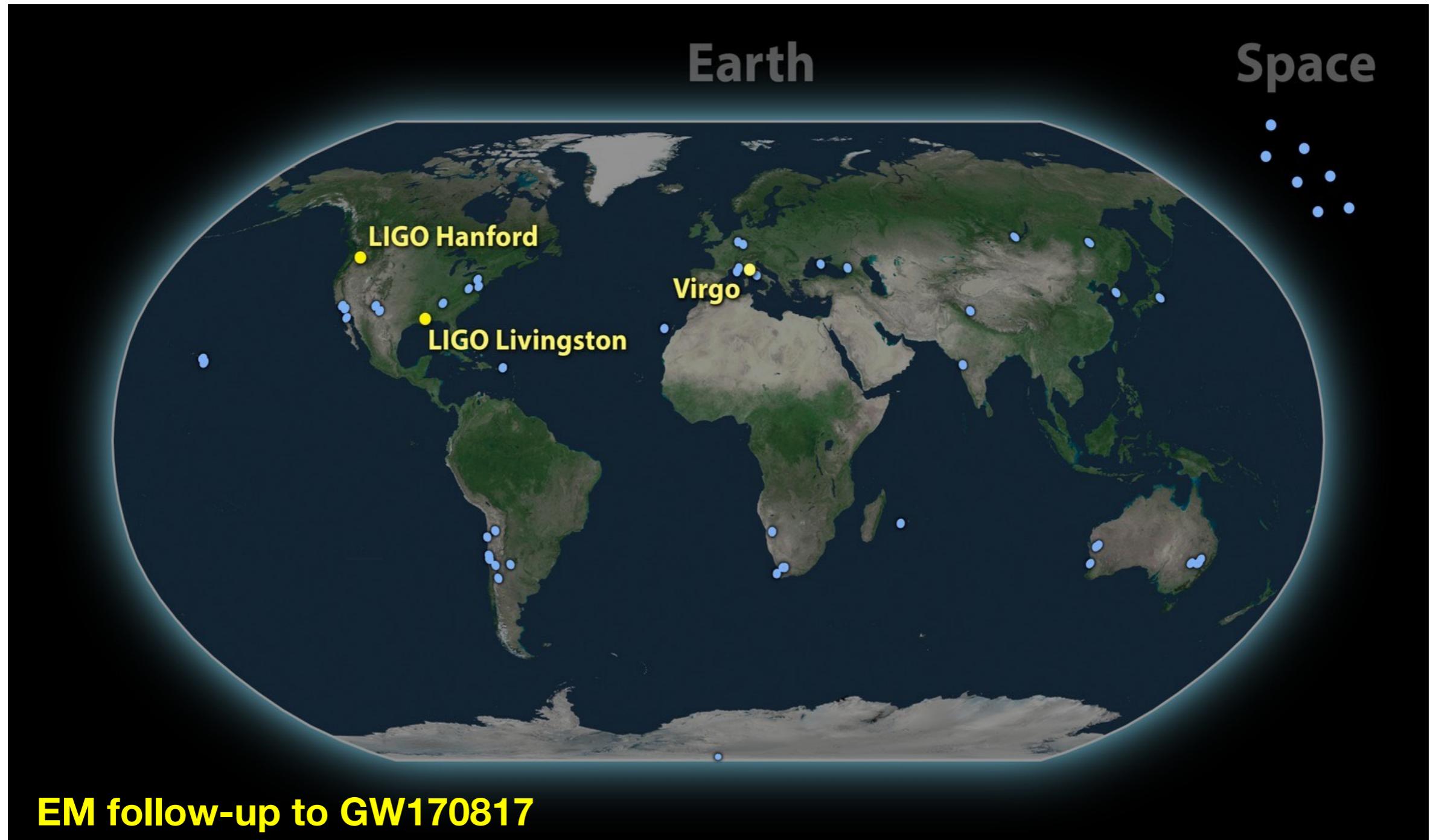


Low-latency Analysis

- First alert goes out to the astronomical community within minutes
- Alert contains a 3D sky-map, an “EM-bright” flag, and for O3 a data quality statement
- Further circulars are sent as data comes in
- Updated sky-maps sent to external community until an EM counterpart has been found, or there is no improvement in the map.



EM FOLLOW-UP



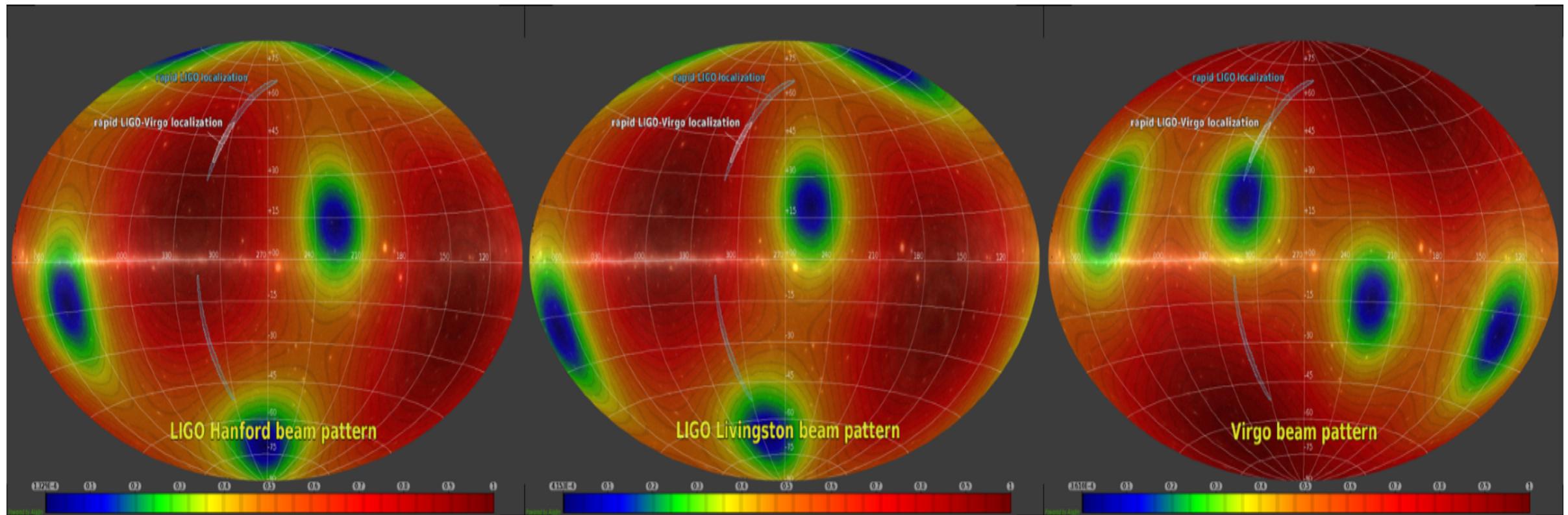
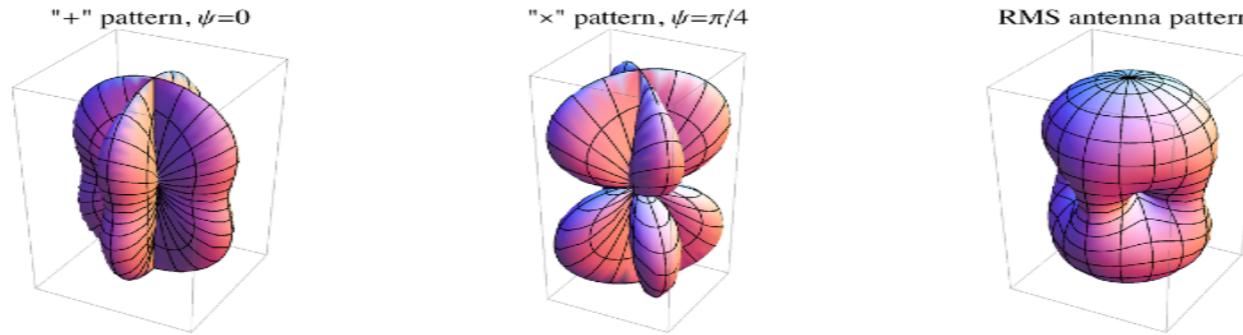
www.ligo.caltech.edu/images

Cosmic Explosions 19, Cargese, Corsica, 27/05-05/06



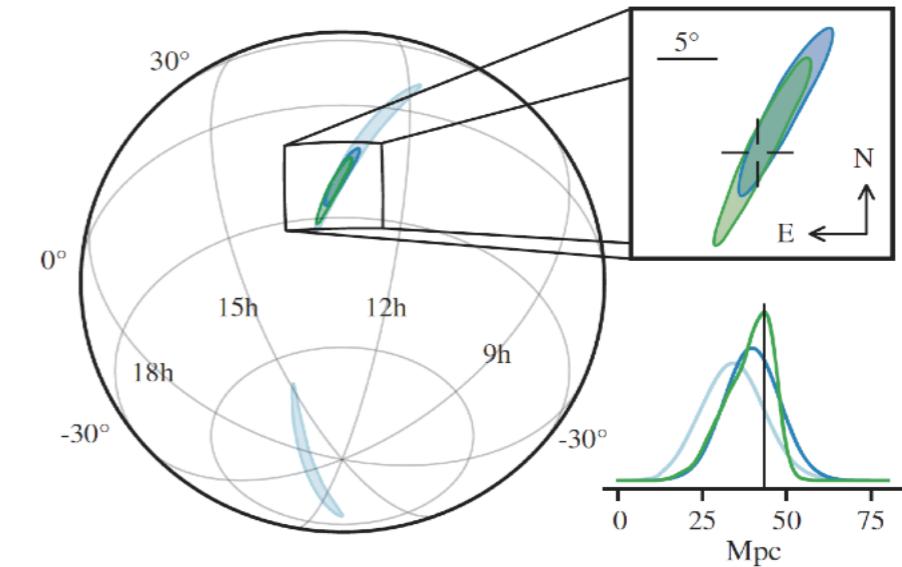
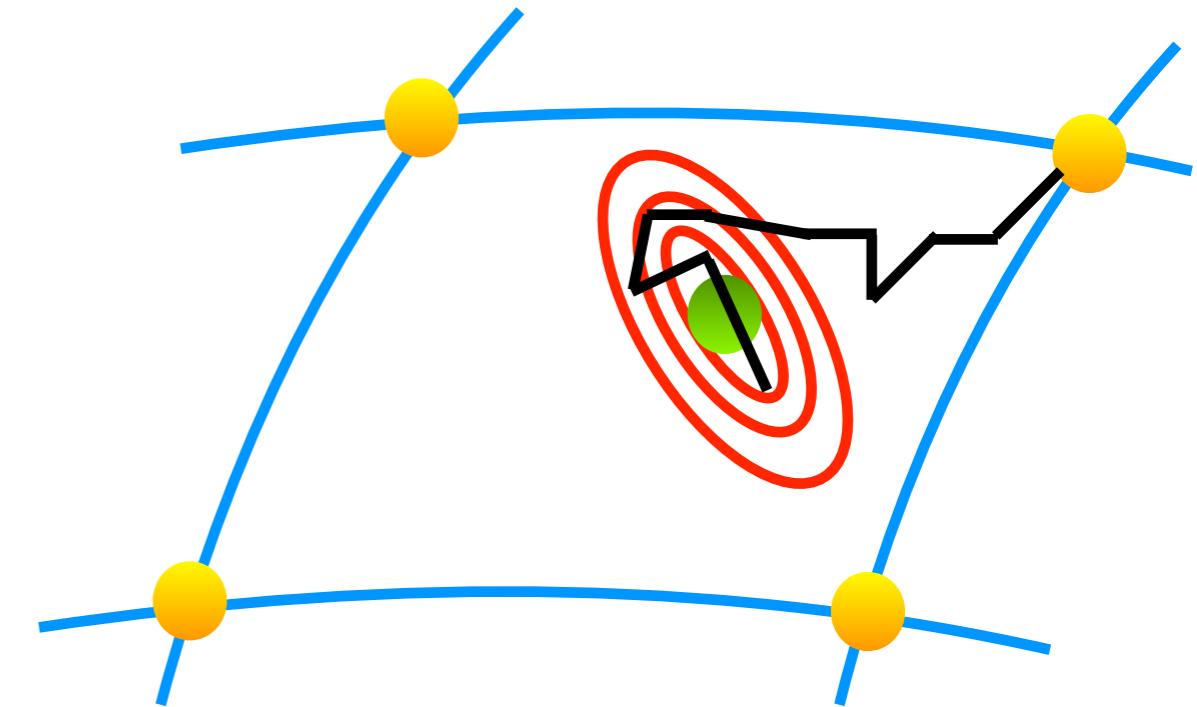
Sky Localisation

$$h_i(t) = h_+(t + \tau_i)F_i^+ + h_\times(t + \tau_i)F_i^\times$$



Bayesian Inference

- Use stochastic samplers
- Extract astrophysical parameters
- Provide posterior distributions...
- ...and confidence intervals

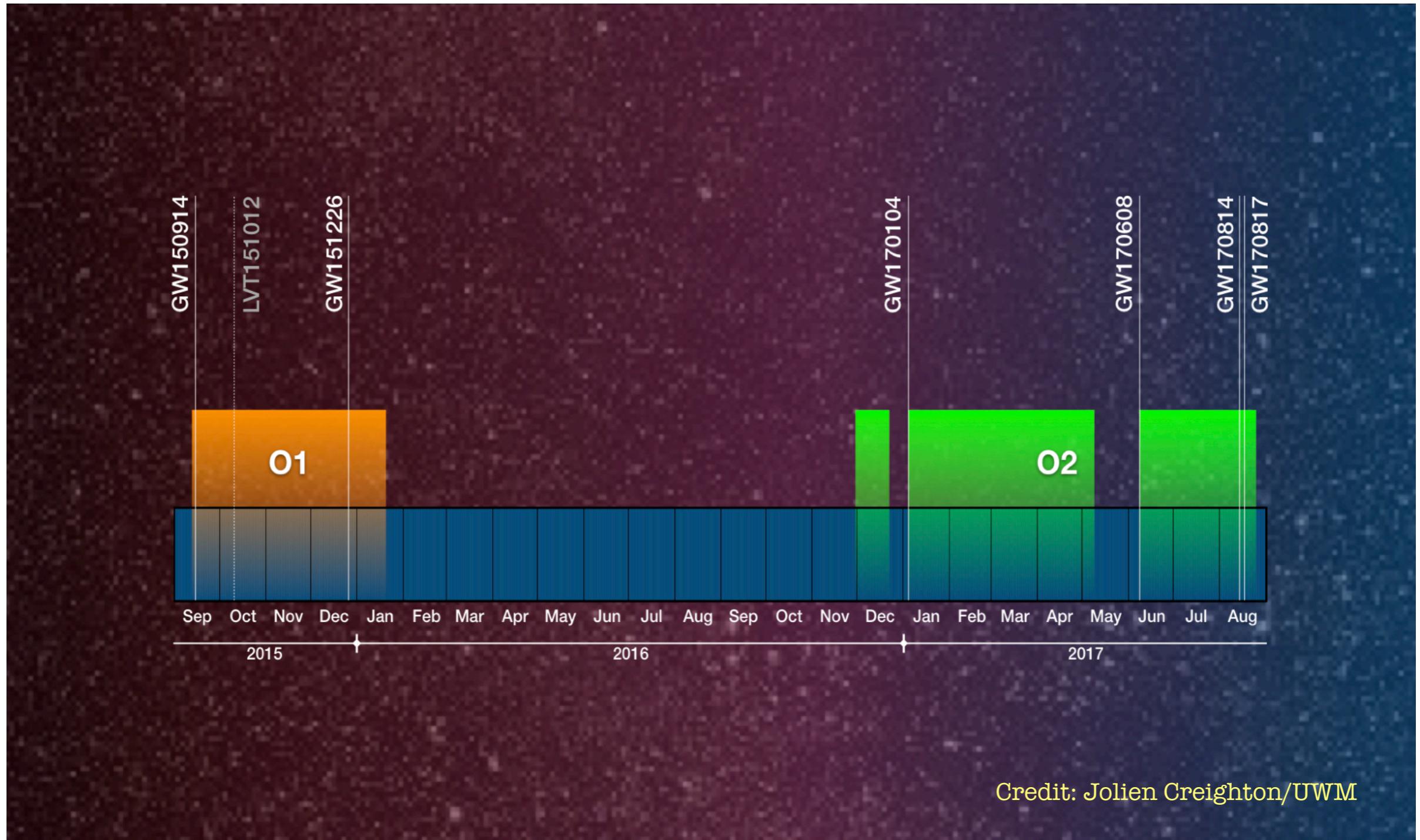


GW170817, B. Abbott et al, PRL 119, 161101 (2017)

PART 2

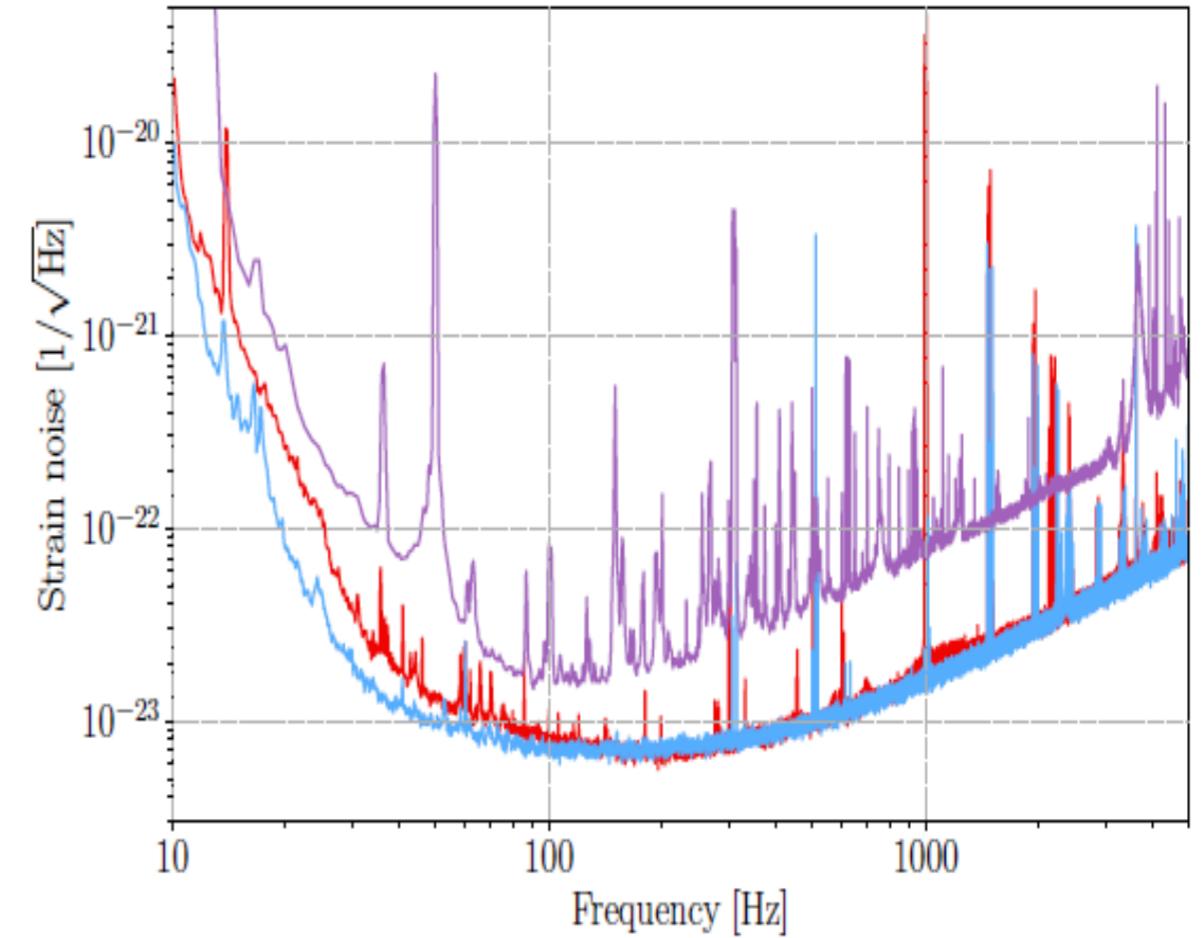
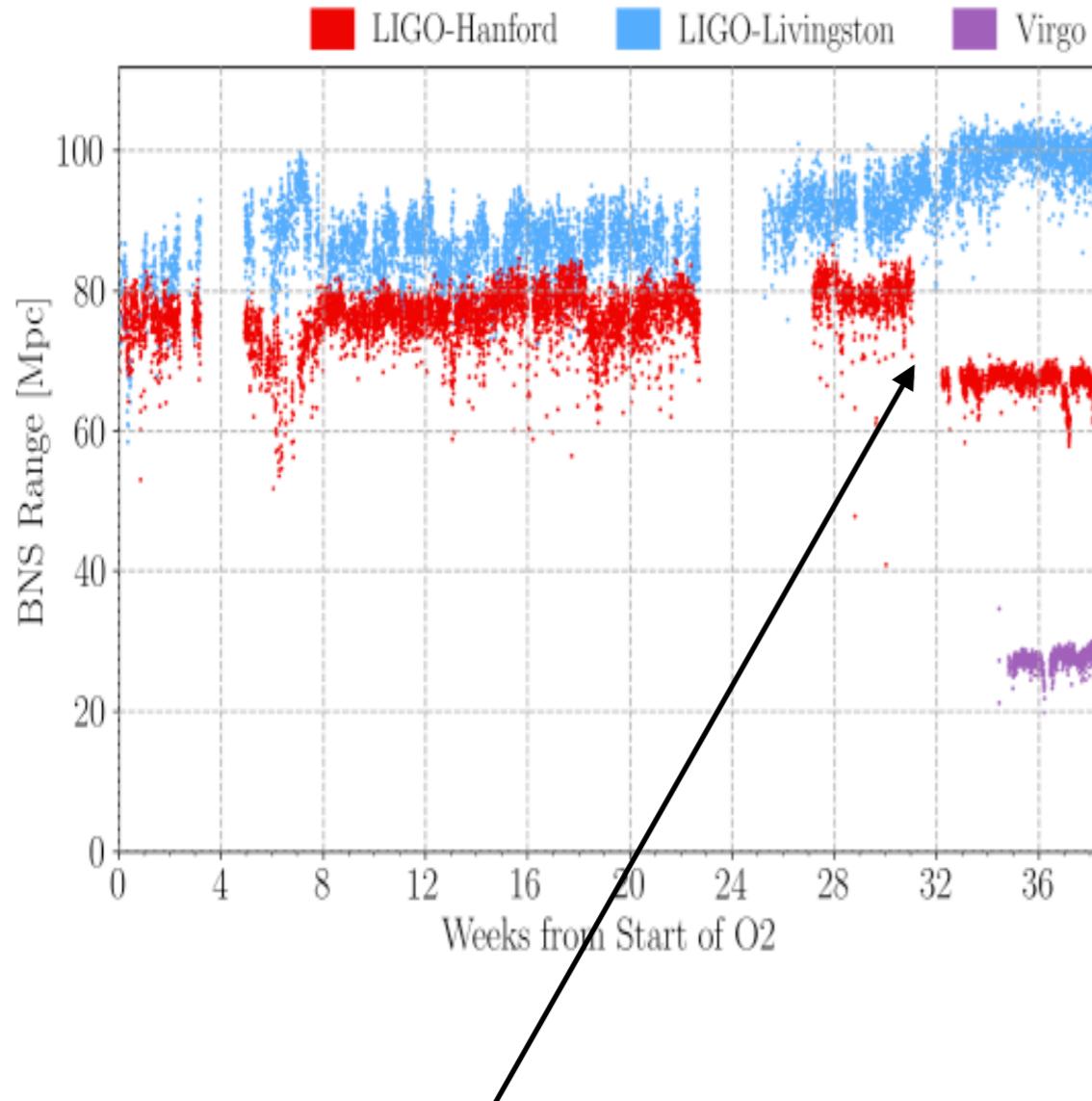
[LIGO'S GRAVITATIONAL-WAVE DETECTIONS]





Credit: Jolien Creighton/UWM





Earthquake in Montana (~700kms)



What do we measure with GWs?

- Redshift masses - need an EM counterpart or assume a cosmology to get detector frame masses, i.e. $m_i^{\text{det}} = (1+z)m_i$
- Direct measure of luminosity distance, D_L
- Spins
- All sky detector - sky position and orientation via triangulation / time delays
- inclination - highly correlated with luminosity distance
- tidal deformation (NSs)



GWTC-1 results

Event	m_1/M_\odot	m_2/M_\odot	\mathcal{M}/M_\odot	χ_{eff}	M_f/M_\odot	a_f	$E_{\text{rad}}/(M_\odot c^2)$	$\ell_{\text{peak}}/(\text{erg s}^{-1})$	d_L/Mpc	z	$\Delta\Omega/\text{deg}^2$
GW150914	$35.6^{+4.8}_{-3.0}$	$30.6^{+3.0}_{-4.4}$	$28.6^{+1.6}_{-1.5}$	$-0.01^{+0.12}_{-0.13}$	$63.1^{+3.3}_{-3.0}$	$0.69^{+0.05}_{-0.04}$	$3.1^{+0.4}_{-0.4}$	$3.6^{+0.4}_{-0.4} \times 10^{56}$	430^{+150}_{-170}	$0.09^{+0.03}_{-0.03}$	180
GW151012	$23.3^{+14.0}_{-5.5}$	$13.6^{+4.1}_{-4.8}$	$15.2^{+2.0}_{-1.1}$	$0.04^{+0.28}_{-0.19}$	$35.7^{+9.9}_{-3.8}$	$0.67^{+0.13}_{-0.11}$	$1.5^{+0.5}_{-0.5}$	$3.2^{+0.8}_{-1.7} \times 10^{56}$	1060^{+540}_{-480}	$0.21^{+0.09}_{-0.09}$	1555
GW151226	$13.7^{+8.8}_{-3.2}$	$7.7^{+2.2}_{-2.6}$	$8.9^{+0.3}_{-0.3}$	$0.18^{+0.20}_{-0.12}$	$20.5^{+6.4}_{-1.5}$	$0.74^{+0.07}_{-0.05}$	$1.0^{+0.1}_{-0.2}$	$3.4^{+0.7}_{-1.7} \times 10^{56}$	440^{+180}_{-190}	$0.09^{+0.04}_{-0.04}$	1033
GW170104	$31.0^{+7.2}_{-5.6}$	$20.1^{+4.9}_{-4.5}$	$21.5^{+2.1}_{-1.7}$	$-0.04^{+0.17}_{-0.20}$	$49.1^{+5.2}_{-3.9}$	$0.66^{+0.08}_{-0.10}$	$2.2^{+0.5}_{-0.5}$	$3.3^{+0.6}_{-0.9} \times 10^{56}$	960^{+430}_{-410}	$0.19^{+0.07}_{-0.08}$	924
GW170608	$10.9^{+5.3}_{-1.7}$	$7.6^{+1.3}_{-2.1}$	$7.9^{+0.2}_{-0.2}$	$0.03^{+0.19}_{-0.07}$	$17.8^{+3.2}_{-0.7}$	$0.69^{+0.04}_{-0.04}$	$0.9^{+0.05}_{-0.1}$	$3.5^{+0.4}_{-1.3} \times 10^{56}$	320^{+120}_{-110}	$0.07^{+0.02}_{-0.02}$	396
GW170729	$50.6^{+16.6}_{-10.2}$	$34.3^{+9.1}_{-10.1}$	$35.7^{+6.5}_{-4.7}$	$0.36^{+0.21}_{-0.25}$	$80.3^{+14.6}_{-10.2}$	$0.81^{+0.07}_{-0.13}$	$4.8^{+1.7}_{-1.7}$	$4.2^{+0.9}_{-1.5} \times 10^{56}$	2750^{+1350}_{-1320}	$0.48^{+0.19}_{-0.20}$	1033
GW170809	$35.2^{+8.3}_{-6.0}$	$23.8^{+5.2}_{-5.1}$	$25.0^{+2.1}_{-1.6}$	$0.07^{+0.16}_{-0.16}$	$56.4^{+5.2}_{-3.7}$	$0.70^{+0.08}_{-0.09}$	$2.7^{+0.6}_{-0.6}$	$3.5^{+0.6}_{-0.9} \times 10^{56}$	990^{+320}_{-380}	$0.20^{+0.05}_{-0.07}$	340
GW170814	$30.7^{+5.7}_{-3.0}$	$25.3^{+2.9}_{-4.1}$	$24.2^{+1.4}_{-1.1}$	$0.07^{+0.12}_{-0.11}$	$53.4^{+3.2}_{-2.4}$	$0.72^{+0.07}_{-0.05}$	$2.7^{+0.4}_{-0.3}$	$3.7^{+0.4}_{-0.5} \times 10^{56}$	580^{+160}_{-210}	$0.12^{+0.03}_{-0.04}$	87
GW170817	$1.46^{+0.12}_{-0.10}$	$1.27^{+0.09}_{-0.09}$	$1.186^{+0.001}_{-0.001}$	$0.00^{+0.02}_{-0.01}$	≤ 2.8	≤ 0.89	≥ 0.04	$\geq 0.1 \times 10^{56}$	40^{+10}_{-10}	$0.01^{+0.00}_{-0.00}$	16
GW170818	$35.5^{+7.5}_{-4.7}$	$26.8^{+4.3}_{-5.2}$	$26.7^{+2.1}_{-1.7}$	$-0.09^{+0.18}_{-0.21}$	$59.8^{+4.8}_{-3.8}$	$0.67^{+0.07}_{-0.08}$	$2.7^{+0.5}_{-0.5}$	$3.4^{+0.5}_{-0.7} \times 10^{56}$	1020^{+430}_{-360}	$0.20^{+0.07}_{-0.07}$	39
GW170823	$39.6^{+10.0}_{-6.6}$	$29.4^{+6.3}_{-7.1}$	$29.3^{+4.2}_{-3.2}$	$0.08^{+0.20}_{-0.22}$	$65.6^{+9.4}_{-6.6}$	$0.71^{+0.08}_{-0.10}$	$3.3^{+0.9}_{-0.8}$	$3.6^{+0.6}_{-0.9} \times 10^{56}$	1850^{+840}_{-840}	$0.34^{+0.13}_{-0.14}$	1651

• 10 BBHs

Abbott et al, arXiv:1811.12907 (2018)

GWTC-1 results

Event	m_1/M_\odot	m_2/M_\odot	\mathcal{M}/M_\odot	χ_{eff}	M_f/M_\odot	a_f	$E_{\text{rad}}/(M_\odot c^2)$	$\ell_{\text{peak}}/(\text{erg s}^{-1})$	d_L/Mpc	z	$\Delta\Omega/\text{deg}^2$
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GW151226	$13.7^{+8.8}_{-3.2}$	$7.7^{+2.2}_{-2.6}$	$8.9^{+0.3}_{-0.3}$	$0.18^{+0.20}_{-0.12}$	$20.5^{+6.4}_{-1.5}$	$0.74^{+0.07}_{-0.05}$	$1.0^{+0.1}_{-0.2}$	$3.4^{+0.7}_{-1.7} \times 10^{56}$	440^{+180}_{-190}	$0.09^{+0.04}_{-0.04}$	1033
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● Massive energy output

Abbott et al, arXiv:1811.12907 (2018)

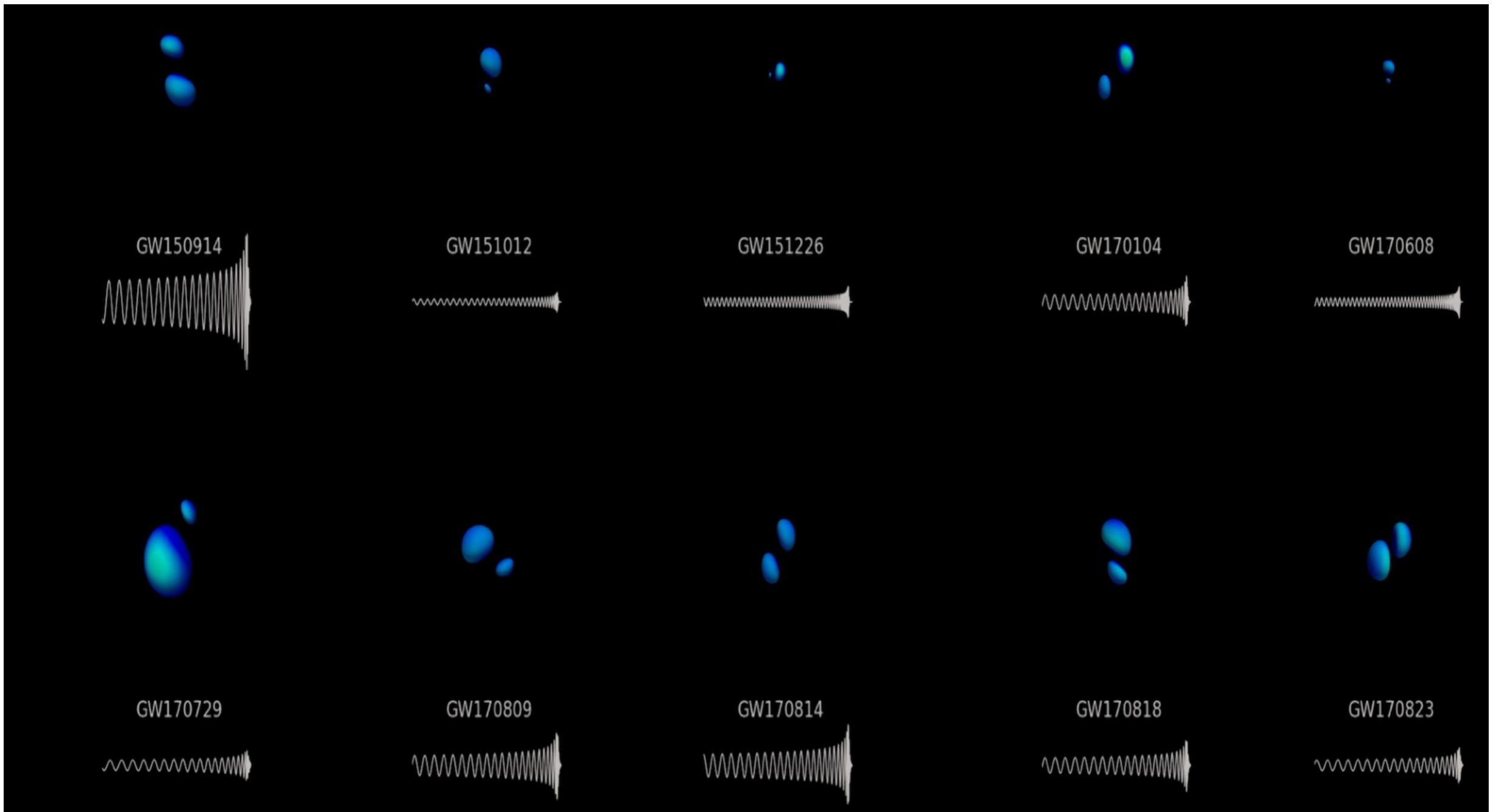
GWTC-1 results

Event	m_1/M_\odot	m_2/M_\odot	\mathcal{M}/M_\odot	χ_{eff}	M_f/M_\odot	a_f	$E_{\text{rad}}/(M_\odot c^2)$	$\ell_{\text{peak}}/(\text{erg s}^{-1})$	d_L/Mpc	z	$\Delta\Omega/\text{deg}^2$
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GW151226	$13.7^{+8.8}_{-3.2}$	$7.7^{+2.2}_{-2.6}$	$8.9^{+0.3}_{-0.3}$	$0.18^{+0.20}_{-0.12}$	$20.5^{+6.4}_{-1.5}$	$0.74^{+0.07}_{-0.05}$	$1.0^{+0.1}_{-0.2}$	$3.4^{+0.7}_{-1.7} \times 10^{56}$	440^{+180}_{-190}	$0.09^{+0.04}_{-0.04}$	1033
GW170104	$31.0^{+7.2}_{-5.6}$	$20.1^{+4.9}_{-4.5}$	$21.5^{+2.1}_{-1.7}$	$-0.04^{+0.17}_{-0.20}$	$49.1^{+5.2}_{-3.9}$	$0.66^{+0.08}_{-0.10}$	$2.2^{+0.5}_{-0.5}$	$3.3^{+0.6}_{-0.9} \times 10^{56}$	960^{+430}_{-410}	$0.19^{+0.07}_{-0.08}$	924
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GW170818	$35.5^{+7.5}_{-4.7}$	$26.8^{+4.3}_{-5.2}$	$26.7^{+2.1}_{-1.7}$	$-0.09^{+0.18}_{-0.21}$	$59.8^{+4.8}_{-3.8}$	$0.67^{+0.07}_{-0.08}$	$2.7^{+0.5}_{-0.5}$	$3.4^{+0.5}_{-0.7} \times 10^{56}$	1020^{+430}_{-360}	$0.20^{+0.07}_{-0.07}$	39
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• Most massive and distant source

Abbott et al, arXiv:1811.12907 (2018)

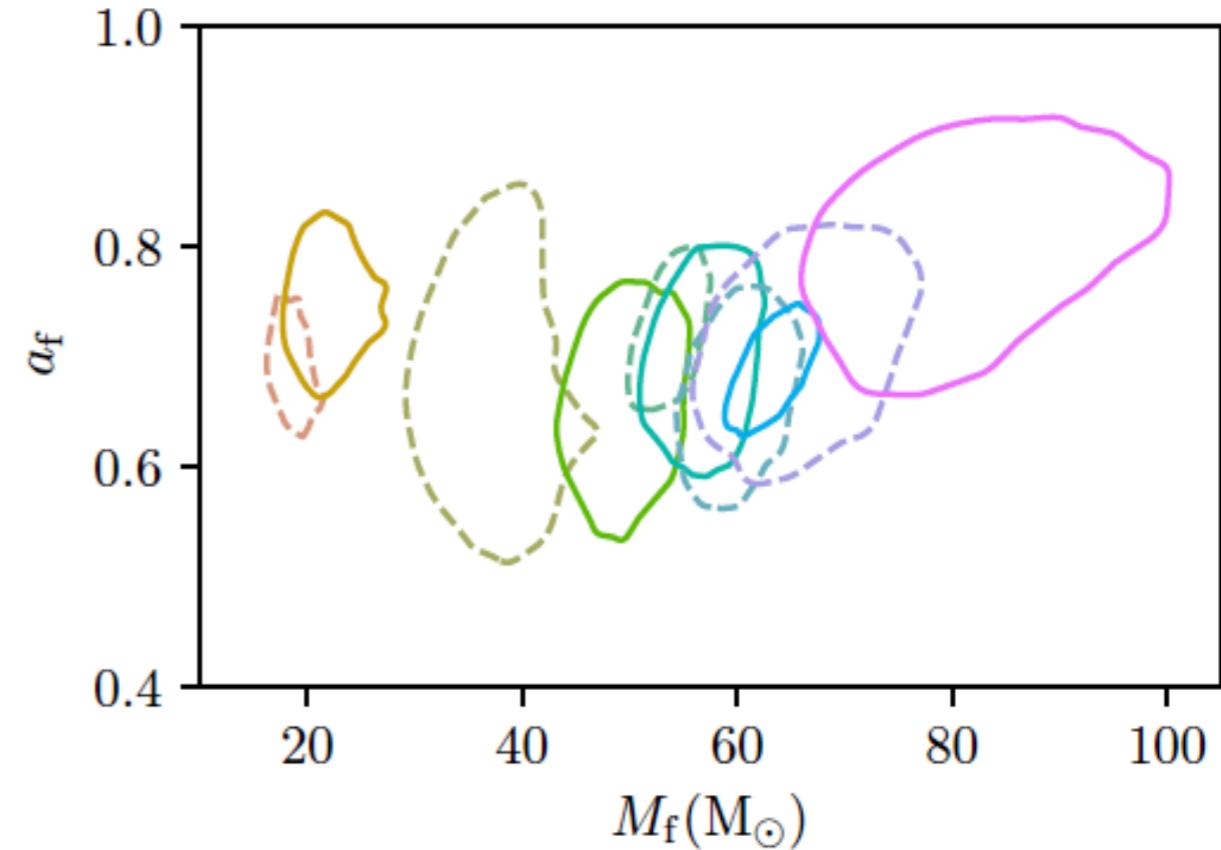
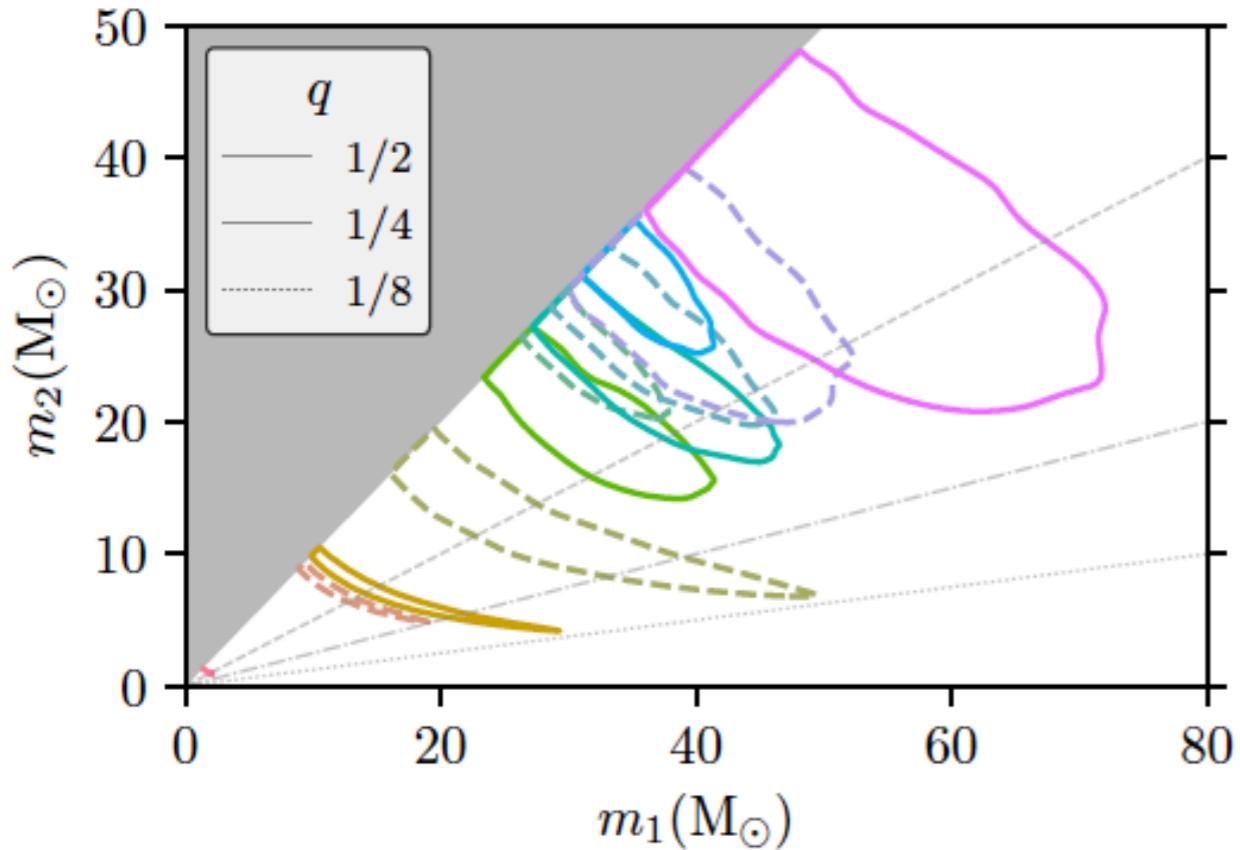
GWTC-1 results



ligo.caltech.edu



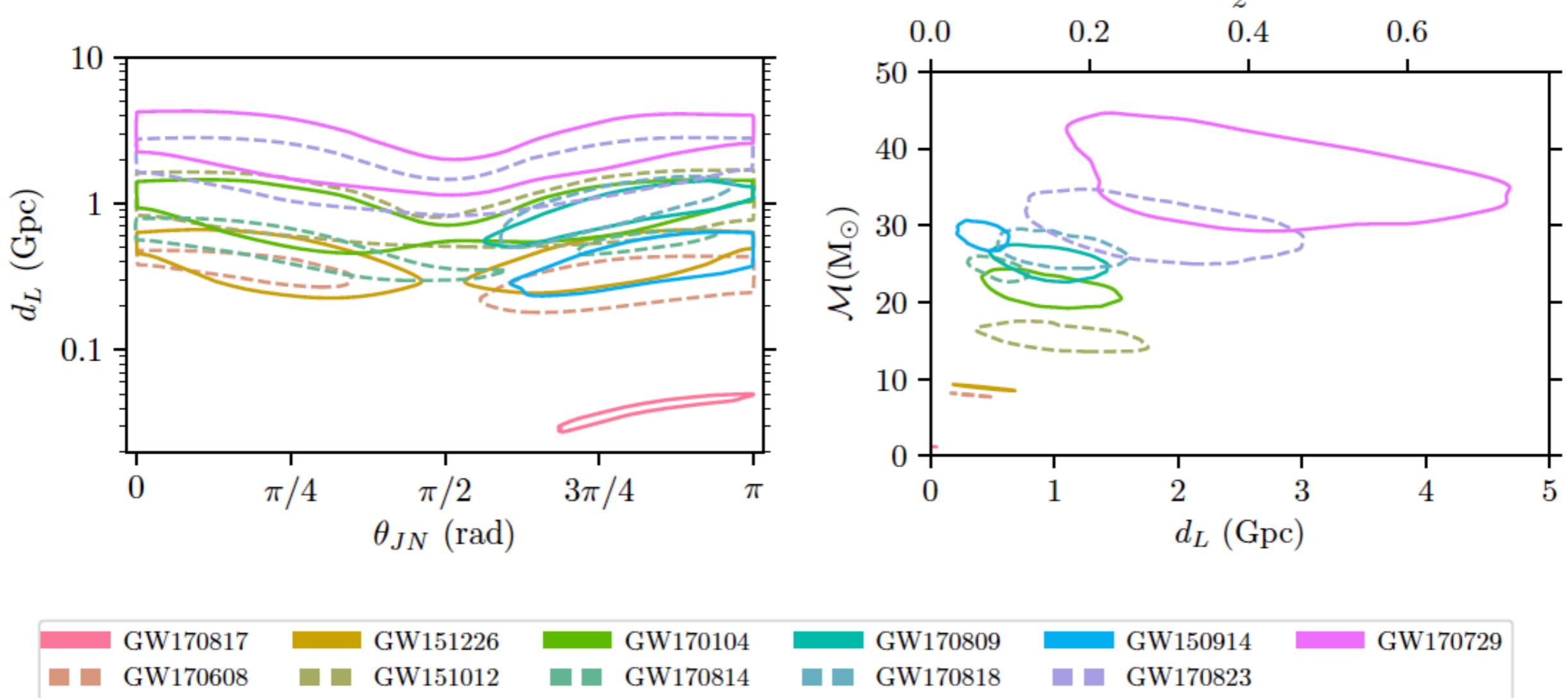
BBH Masses



GW170817	GW151226	GW170104	GW170809	GW150914	GW170729
GW170608	GW151012	GW170814	GW170818	GW170823	

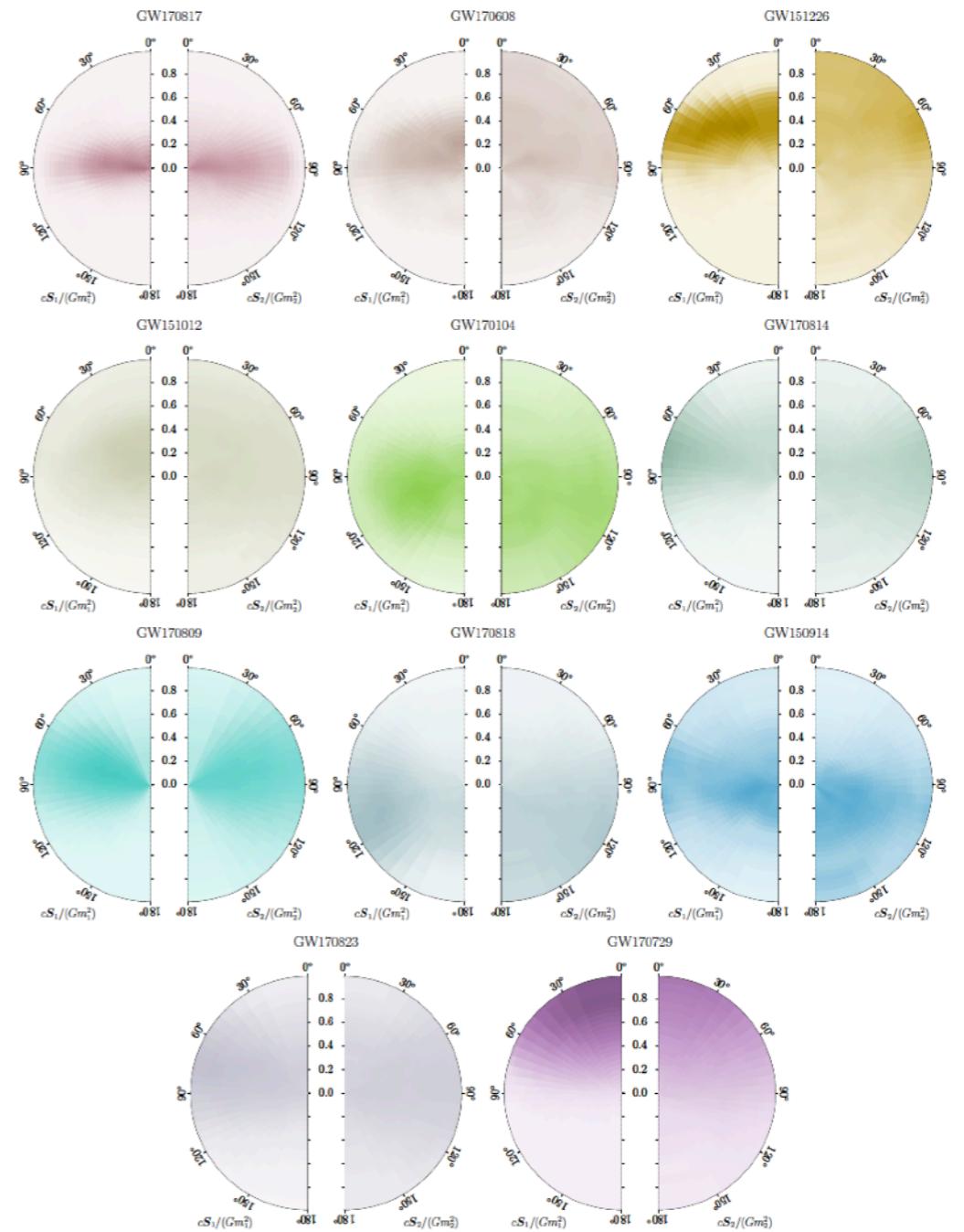
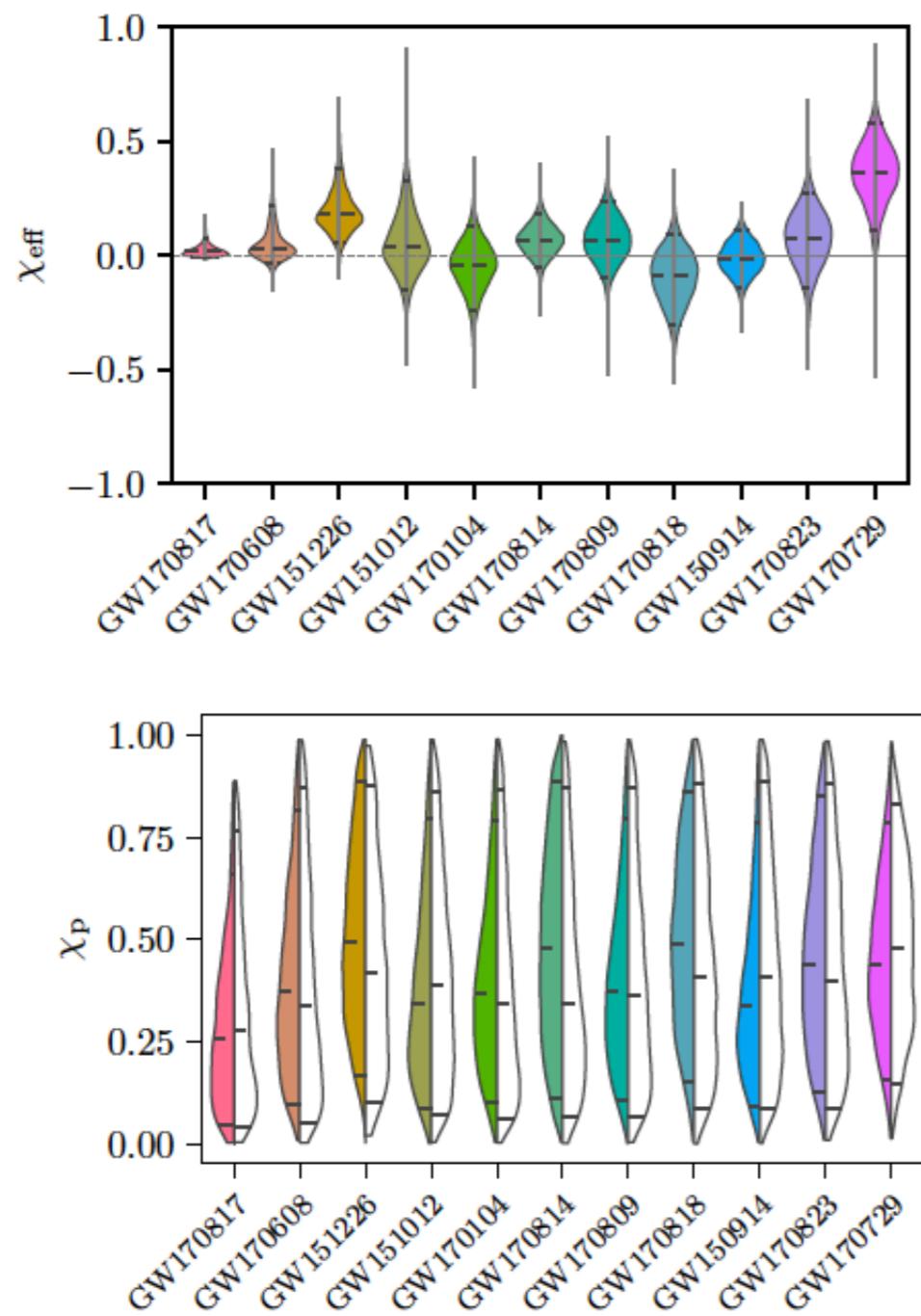
Abbott et al, arXiv:1811.12907 (2018)

BBH Distance



Abbott *et al*, arXiv:1811.12907 (2018)

BBH Spins



Abbott et al, arXiv:1811.12907 (2018)



Cosmic Explosions 19, Cargese, Corsica, 27/05-05/06



GWTC-1 results

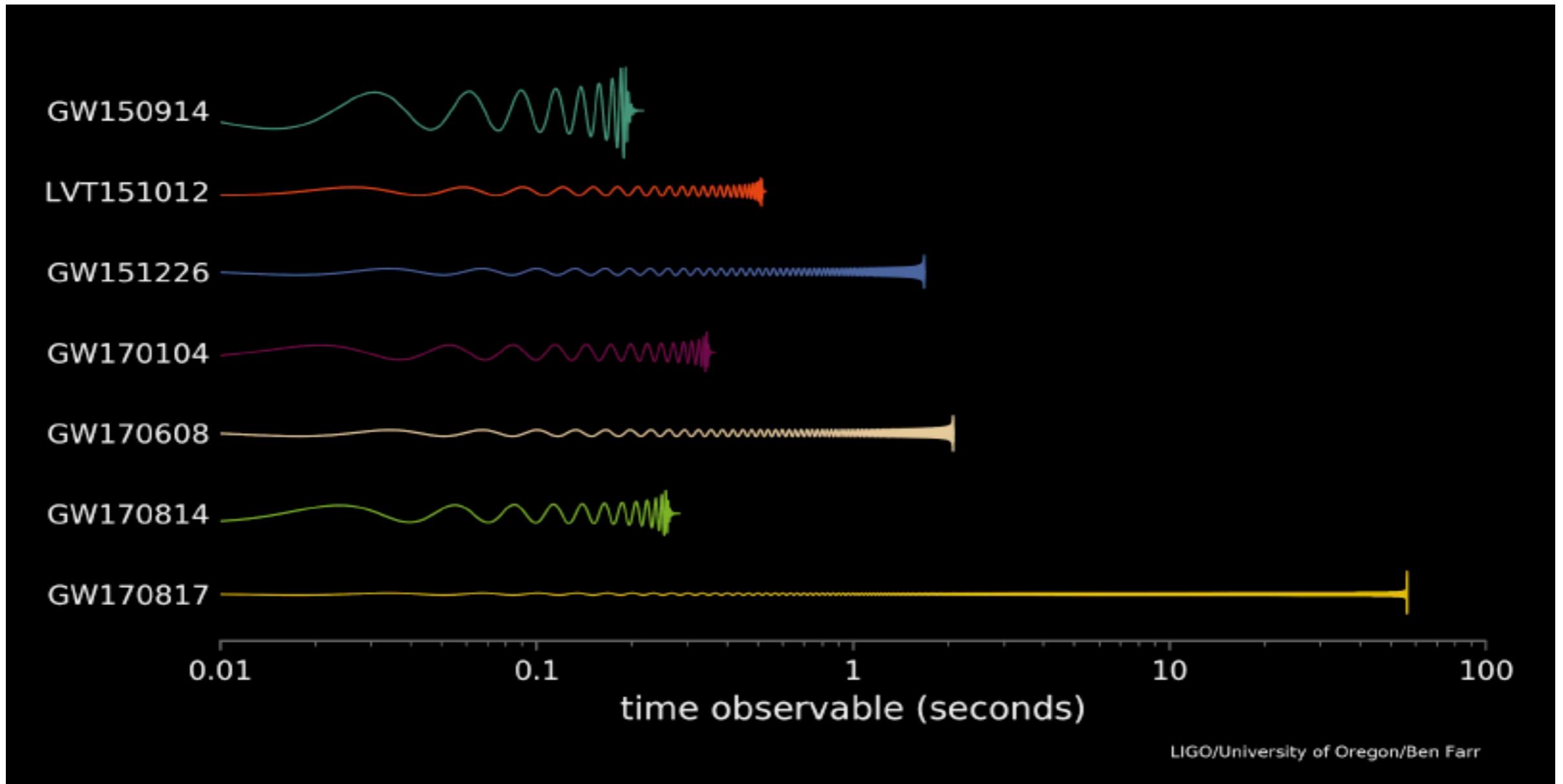
Event	m_1/M_\odot	m_2/M_\odot	\mathcal{M}/M_\odot	χ_{eff}	M_f/M_\odot	a_f	$E_{\text{rad}}/(M_\odot c^2)$	$\ell_{\text{peak}}/(\text{erg s}^{-1})$	d_L/Mpc	z	$\Delta\Omega/\text{deg}^2$
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GW151012	$23.3^{+14.0}_{-5.5}$	$13.6^{+4.1}_{-4.8}$	$15.2^{+2.0}_{-1.1}$	$0.04^{+0.28}_{-0.19}$	$35.7^{+9.9}_{-3.8}$	$0.67^{+0.13}_{-0.11}$	$1.5^{+0.5}_{-0.5}$	$3.2^{+0.8}_{-1.7} \times 10^{56}$	1060^{+540}_{-480}	$0.21^{+0.09}_{-0.09}$	1555
GW151226	$13.7^{+8.8}_{-3.2}$	$7.7^{+2.2}_{-2.6}$	$8.9^{+0.3}_{-0.3}$	$0.18^{+0.20}_{-0.12}$	$20.5^{+6.4}_{-1.5}$	$0.74^{+0.07}_{-0.05}$	$1.0^{+0.1}_{-0.2}$	$3.4^{+0.7}_{-1.7} \times 10^{56}$	440^{+180}_{-190}	$0.09^{+0.04}_{-0.04}$	1033
GW170104	$31.0^{+7.2}_{-5.6}$	$20.1^{+4.9}_{-4.5}$	$21.5^{+2.1}_{-1.7}$	$-0.04^{+0.17}_{-0.20}$	$49.1^{+5.2}_{-3.9}$	$0.66^{+0.08}_{-0.10}$	$2.2^{+0.5}_{-0.5}$	$3.3^{+0.6}_{-0.9} \times 10^{56}$	960^{+430}_{-410}	$0.19^{+0.07}_{-0.08}$	924
GW170608	$10.9^{+5.3}_{-1.7}$	$7.6^{+1.3}_{-2.1}$	$7.9^{+0.2}_{-0.2}$	$0.03^{+0.19}_{-0.07}$	$17.8^{+3.2}_{-0.7}$	$0.69^{+0.04}_{-0.04}$	$0.9^{+0.05}_{-0.1}$	$3.5^{+0.4}_{-1.3} \times 10^{56}$	320^{+120}_{-110}	$0.07^{+0.02}_{-0.02}$	396
GW170729	$50.6^{+16.6}_{-10.2}$	$34.3^{+9.1}_{-10.1}$	$35.7^{+6.5}_{-4.7}$	$0.36^{+0.21}_{-0.25}$	$80.3^{+14.6}_{-10.2}$	$0.81^{+0.07}_{-0.13}$	$4.8^{+1.7}_{-1.7}$	$4.2^{+0.9}_{-1.5} \times 10^{56}$	2750^{+1350}_{-1320}	$0.48^{+0.19}_{-0.20}$	1033
GW170809	$35.2^{+8.3}_{-6.0}$	$23.8^{+5.2}_{-5.1}$	$25.0^{+2.1}_{-1.6}$	$0.07^{+0.16}_{-0.16}$	$56.4^{+5.2}_{-3.7}$	$0.70^{+0.08}_{-0.09}$	$2.7^{+0.6}_{-0.6}$	$3.5^{+0.6}_{-0.9} \times 10^{56}$	990^{+320}_{-380}	$0.20^{+0.05}_{-0.07}$	340
GW170814	$30.7^{+5.7}_{-3.0}$	$25.3^{+2.9}_{-4.1}$	$24.2^{+1.4}_{-1.1}$	$0.07^{+0.12}_{-0.11}$	$53.4^{+3.2}_{-2.4}$	$0.72^{+0.07}_{-0.05}$	$2.7^{+0.4}_{-0.3}$	$3.7^{+0.4}_{-0.5} \times 10^{56}$	580^{+160}_{-210}	$0.12^{+0.03}_{-0.04}$	87
GW170817	$1.46^{+0.12}_{-0.10}$	$1.27^{+0.09}_{-0.09}$	$1.186^{+0.001}_{-0.001}$	$0.00^{+0.02}_{-0.01}$	≤ 2.8	≤ 0.89	≥ 0.04	$\geq 0.1 \times 10^{56}$	40^{+10}_{-10}	$0.01^{+0.00}_{-0.00}$	16
GW170818	$35.5^{+7.5}_{-4.7}$	$26.8^{+4.3}_{-5.2}$	$26.7^{+2.1}_{-1.7}$	$-0.09^{+0.18}_{-0.21}$	$59.8^{+4.8}_{-3.8}$	$0.67^{+0.07}_{-0.08}$	$2.7^{+0.5}_{-0.5}$	$3.4^{+0.5}_{-0.7} \times 10^{56}$	1020^{+430}_{-360}	$0.20^{+0.07}_{-0.07}$	39
GW170823	$39.6^{+10.0}_{-6.6}$	$29.4^{+6.3}_{-7.1}$	$29.3^{+4.2}_{-3.2}$	$0.08^{+0.20}_{-0.22}$	$65.6^{+9.4}_{-6.6}$	$0.71^{+0.08}_{-0.10}$	$3.3^{+0.9}_{-0.8}$	$3.6^{+0.6}_{-0.9} \times 10^{56}$	1850^{+840}_{-840}	$0.34^{+0.13}_{-0.14}$	1651

• 1st ever BNS and best resolved event

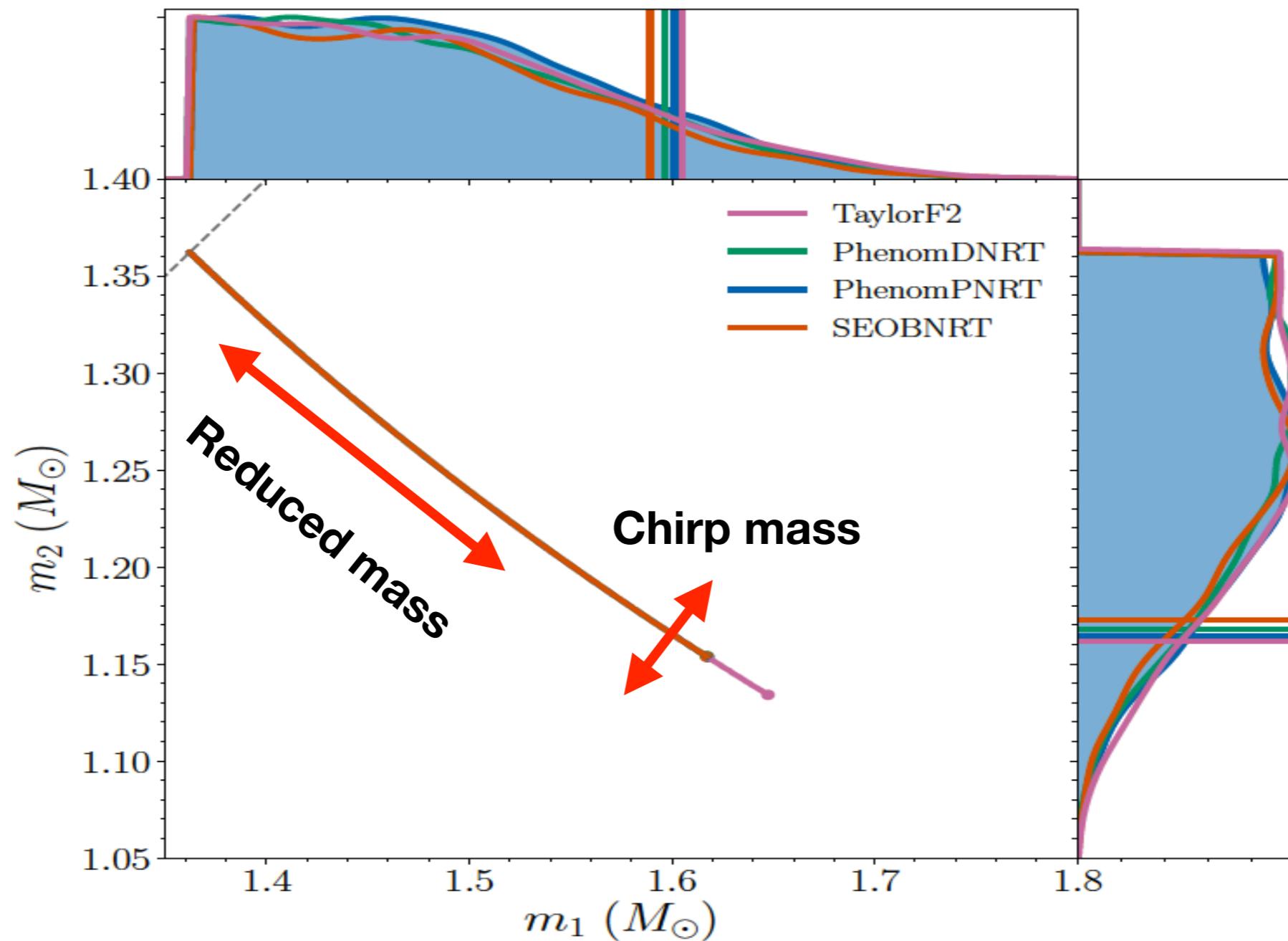
Abbott et al, arXiv:1811.12907 (2018)

Common question....

- ⌚ ...how do we know GW170817 was a BNS?



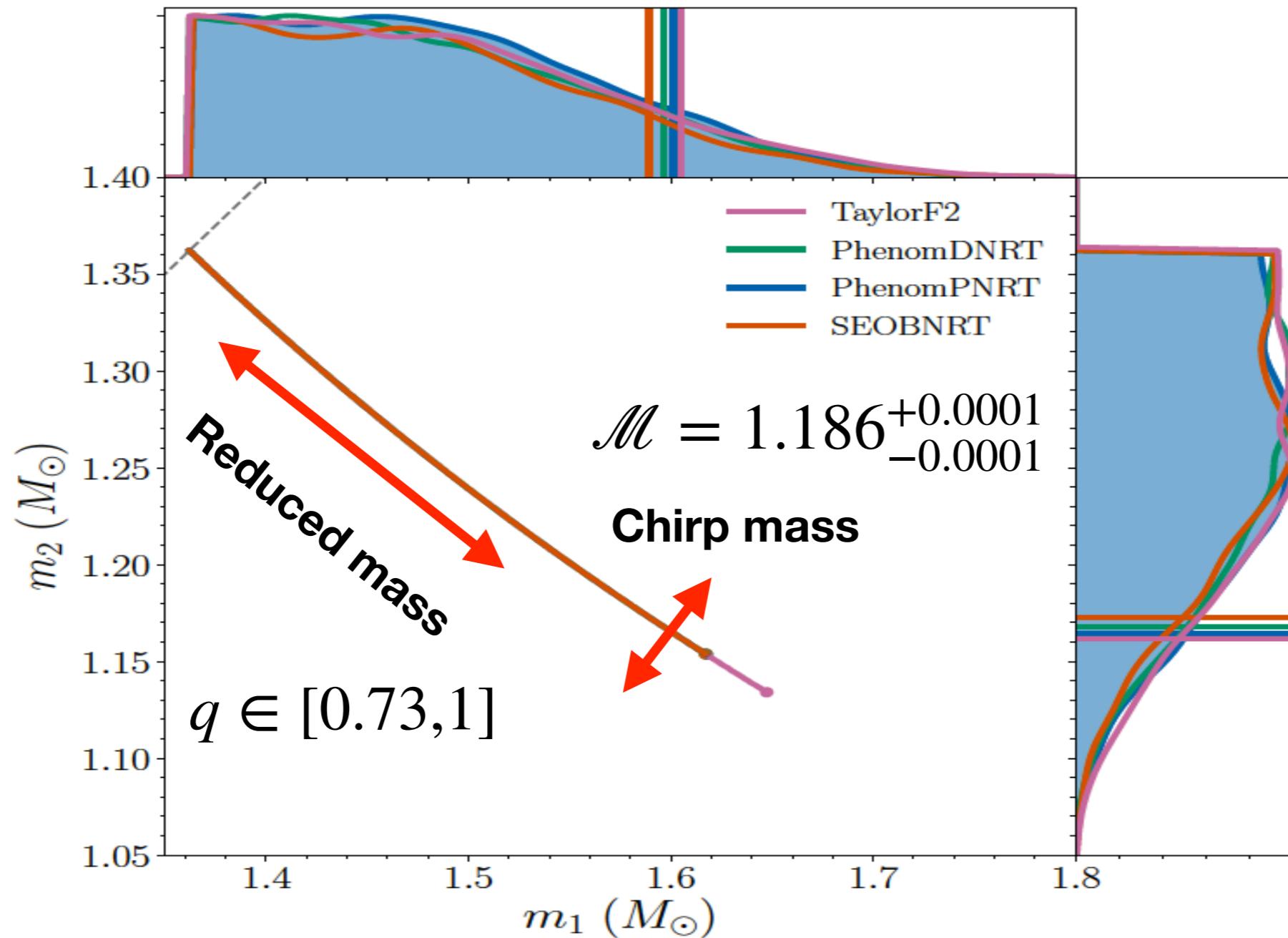
How well do we measure NS mass?



Abbott et al, arXiv:1805.11579 (2018)



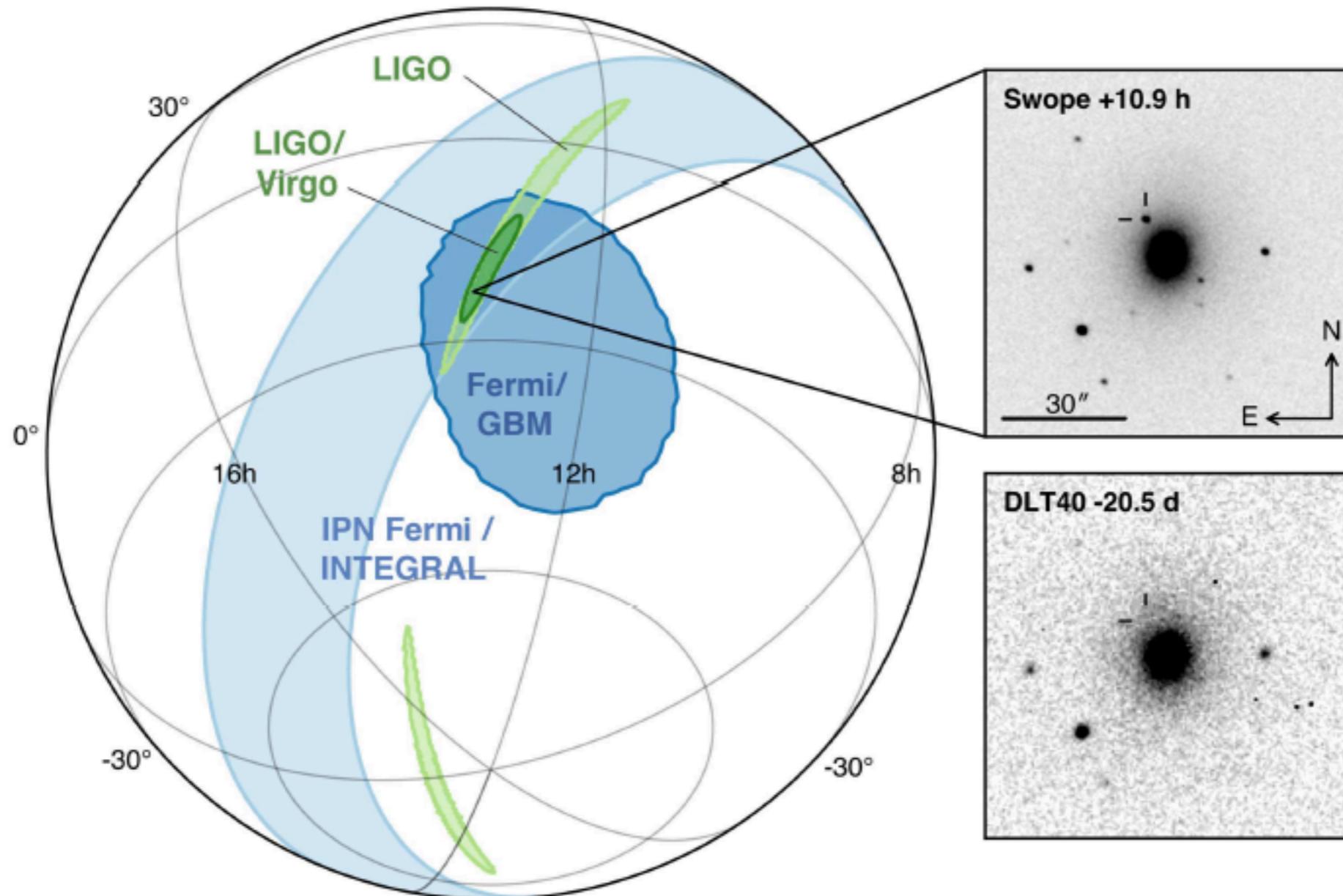
How well do we measure NS mass?



Abbott et al, arXiv:1805.11579 (2018)



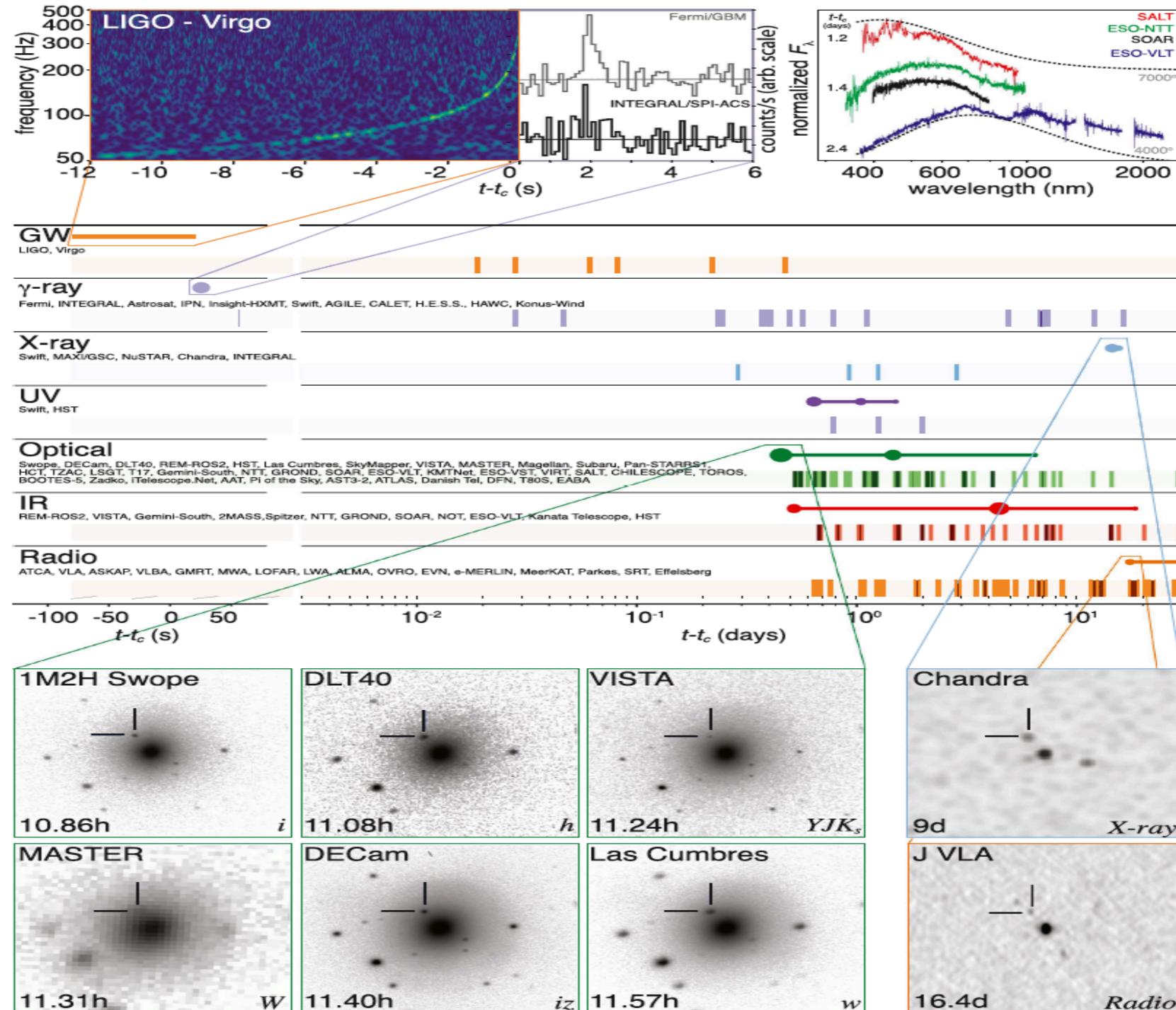
GRB Association



www.ligo.caltech.edu/images



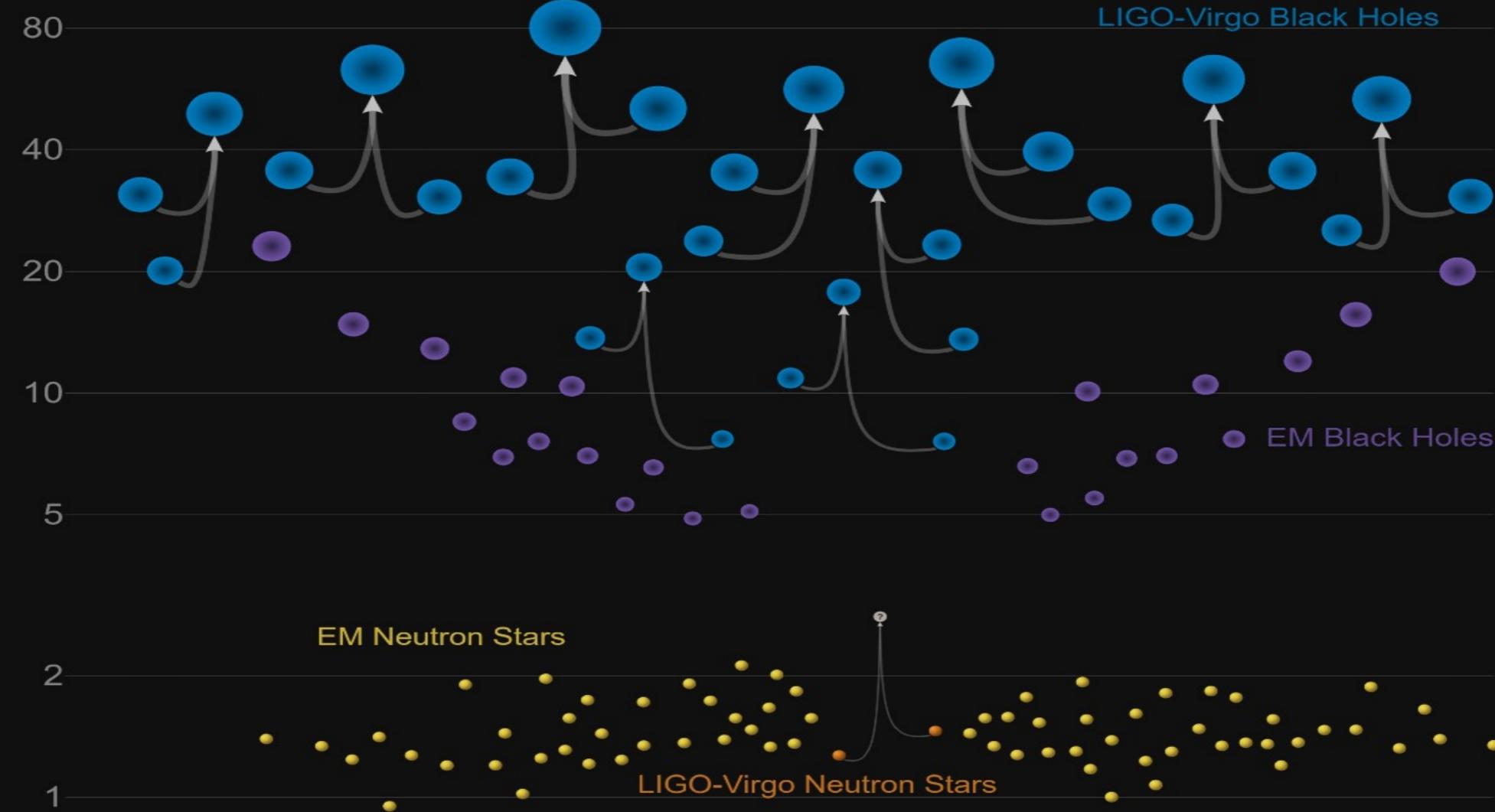
EM Follow-up Timeline



Abbott et al, ApJ Letters 848, L13 (2017)

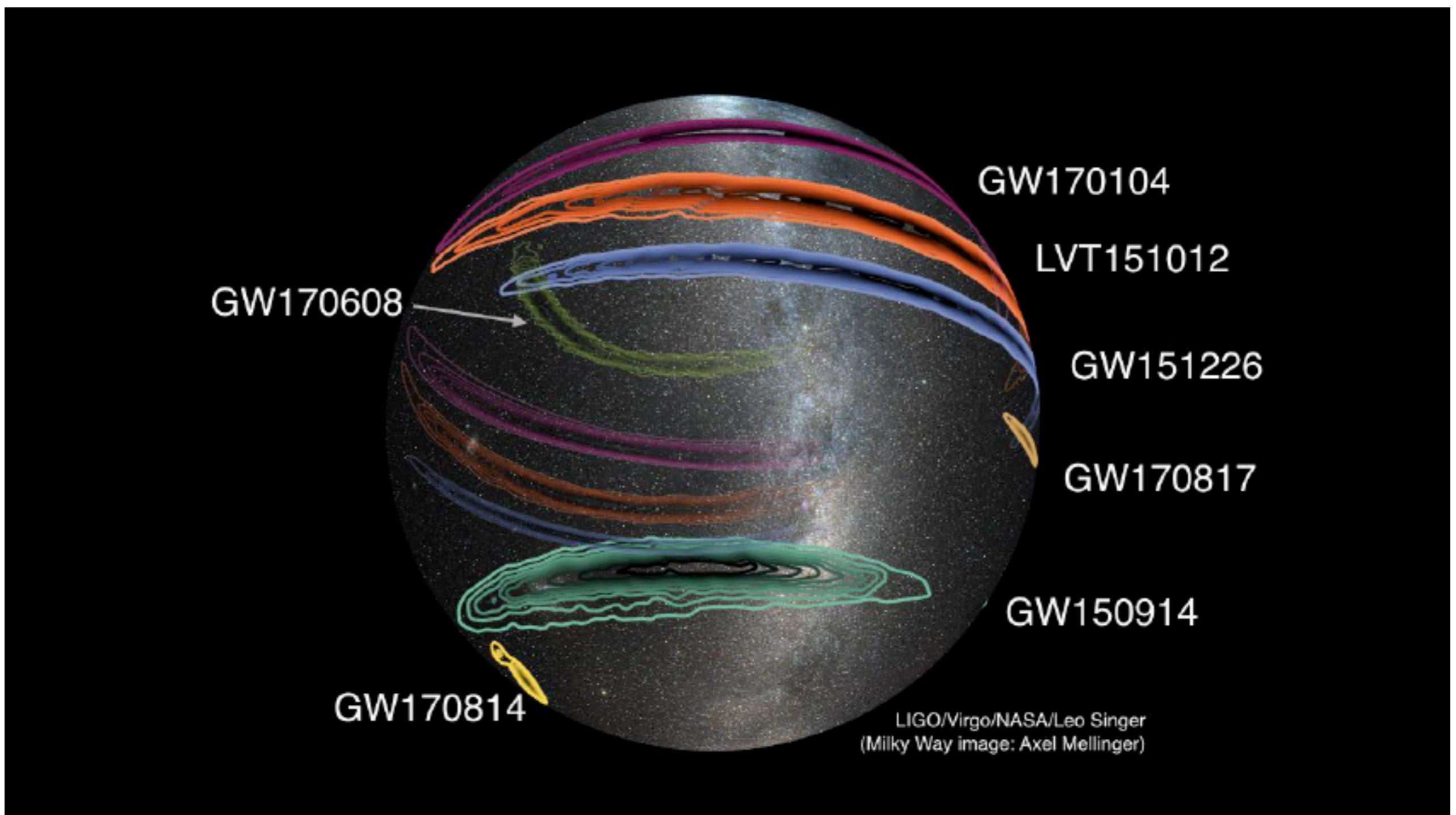


Masses in the Stellar Graveyard *in Solar Masses*



LIGO-Virgo | Frank Elavsky | Northwestern

www.ligo.caltech.edu/images

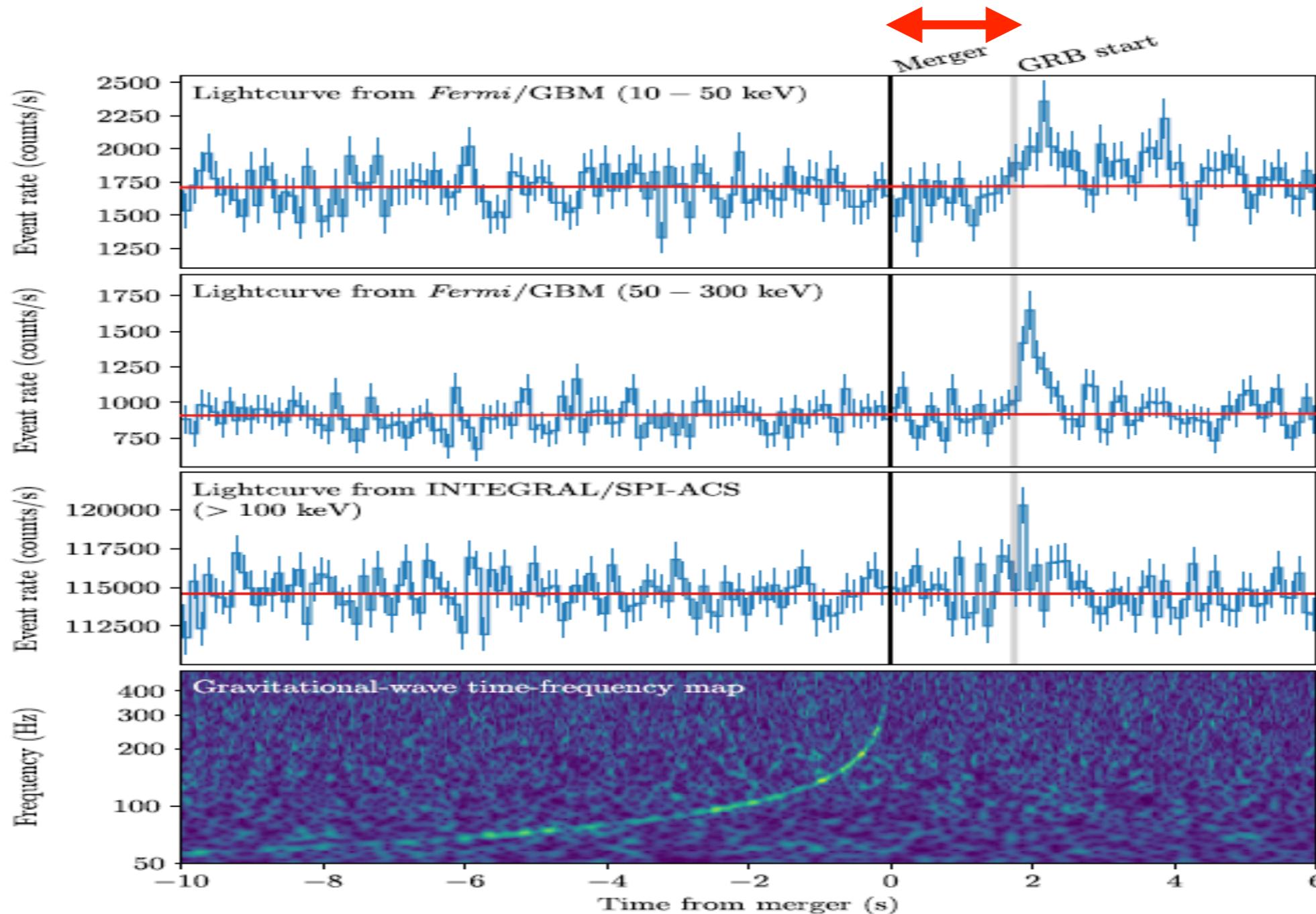


So, what can we do?

- Fundamental physics
- Astrophysics
- Extreme MatterCosmology
- Cosmology



Fundamental Physics



Abbott et al, *ApJ Letters* 848, L13 (2017)



Fundamental Physics

- ⌚ The time delay between the GW and GRB detections over 1.3×10^8 Lyrs was
(N.B. analysis allows for +/- 10 secs)

$$\Delta t = (1.74 \pm 0.05) \text{ s}$$

- ⌚ Defining the fractional difference between the speed of light and GWs as

$$\frac{c_g - c}{c} \approx c \frac{\Delta t}{D_L}$$

- ⌚ We find the following constraint

$$-3 \times 10^{-15} \leq \frac{\Delta c}{c} \leq 7 \times 10^{-16}$$

- ⌚ Large consequences for cosmological theories

Abbott et al, ApJ Letters 848, L13 (2017)

Fundamental Physics

	$c_g = c$	$c_g \neq c$
Horndeski	General Relativity quintessence/k-essence [42] Brans-Dicke/ $f(R)$ [43, 44] Kinetic Gravity Braiding [46]	quartic/quintic Galileons [13, 14] Fab Four [15, 16] de Sitter Horndeski [45] $G_{\mu\nu}\phi^\mu\phi^\nu$ [47], Gauss-Bonnet
beyond H.	Derivative Conformal (20) [18] Disformal Tuning (22) DHOST with $A_1 = 0$	quartic/quintic GLPV [19] DHOST [20, 48] with $A_1 \neq 0$

Viable after GW170817 Non-viable after GW170817



with extension to: Einstein-Aether, Horava gravity, Generalised Proca, TeVeS, massive gravity, bigravity, multi-gravity, MOND-like theories

arXiv:1710.05901, 1710.06394, 1710.05893, 1710.05877...

Fundamental Physics

- Shapiro delay is defined as $\Delta t_s = -\frac{1+\gamma}{c} \int_{r_e}^{r_o} U(r(l))dl$
- γ is the PPN parameter parameterising a deviation from Einstein-Maxwell theory
- Conservative bound on $\Delta\gamma = |\gamma_{GW} - \gamma_{EM}| \leq 2 \frac{\Delta t}{\Delta t_s}$
- is $-2.6 \times 10^{-7} \leq \Delta\gamma \leq 1.2 \times 10^{-6}$
- Newer result (S. Boran et al, 1710.06168) using more sophisticated dark matter halo model gives $\Delta\gamma \leq 3.9 \times 10^{-8}$
- implying that MOND-like dark matter emulator theories are ruled out, as the GWs would have arrived 1000 days before the EM emission



Fundamental Physics

● Fourier domain waveform

$$\tilde{h}(f) = A(f) e^{i\Psi_{GR}(f)}$$

● GW inspiral phase to 3.5 PN order, i.e. $(v/c)^7$

$$\begin{aligned}\Psi_{GR}(f) = & 2\pi f t_c + \phi_c - \frac{\pi}{4} + \frac{3}{128} \left[\psi_0(\pi M f)^{-5/3} + \psi_1(\pi M f)^{-4/3} + \psi_2(\pi M f)^{-1} \right. \\ & \left. \psi_3(\pi M f)^{-2/3} + \psi_4(\pi M f)^{-1/3} + \psi_5 + \psi_6(\pi M f)^{1/3} + \psi_7(\pi M f)^{2/3} + \right]\end{aligned}$$



Fundamental Physics

- ➊ Fourier domain waveform

$$\tilde{h}(f) = A(f)e^{i\Psi_{GR}(f)}$$

- ➋ GW inspiral phase to 3.5 PN order, i.e. $(v/c)^7$

$$\begin{aligned} \Psi_{GR}(f) = & 2\pi f t_c + \phi_c - \frac{\pi}{4} + \frac{3}{128} \left[\psi_0(\pi M f)^{-5/3} + \psi_1(\pi M f)^{-4/3} + \psi_2(\pi M f)^{-1} \right. \\ & \left. \psi_3(\pi M f)^{-2/3} + \psi_4(\pi M f)^{-1/3} + \psi_5 + \psi_6(\pi M f)^{1/3} + \psi_7(\pi M f)^{2/3} + \right] \\ & + \text{scalar-tensor theory at the -1PN order, i.e. } f^{7/3} \end{aligned}$$

*Einstein-Aether
Khronometric* *Massive Graviton*
Dynamical Chern-Simons

+ scalar-tensor theory at the -1PN order, i.e. $f^{7/3}$



Fundamental Physics

Set $\psi_k \rightarrow \psi_k (1 + \delta\psi_k)$

Phenomenological phase

$$\Psi(f) = \Psi_{GR}(f) + \Psi_{NGR}(f)$$

Phenomenological waveform

$$\tilde{h}(f) = A(f) e^{i\Psi_{GR}(f)} e^{i\Psi_{NGR}(f)}$$

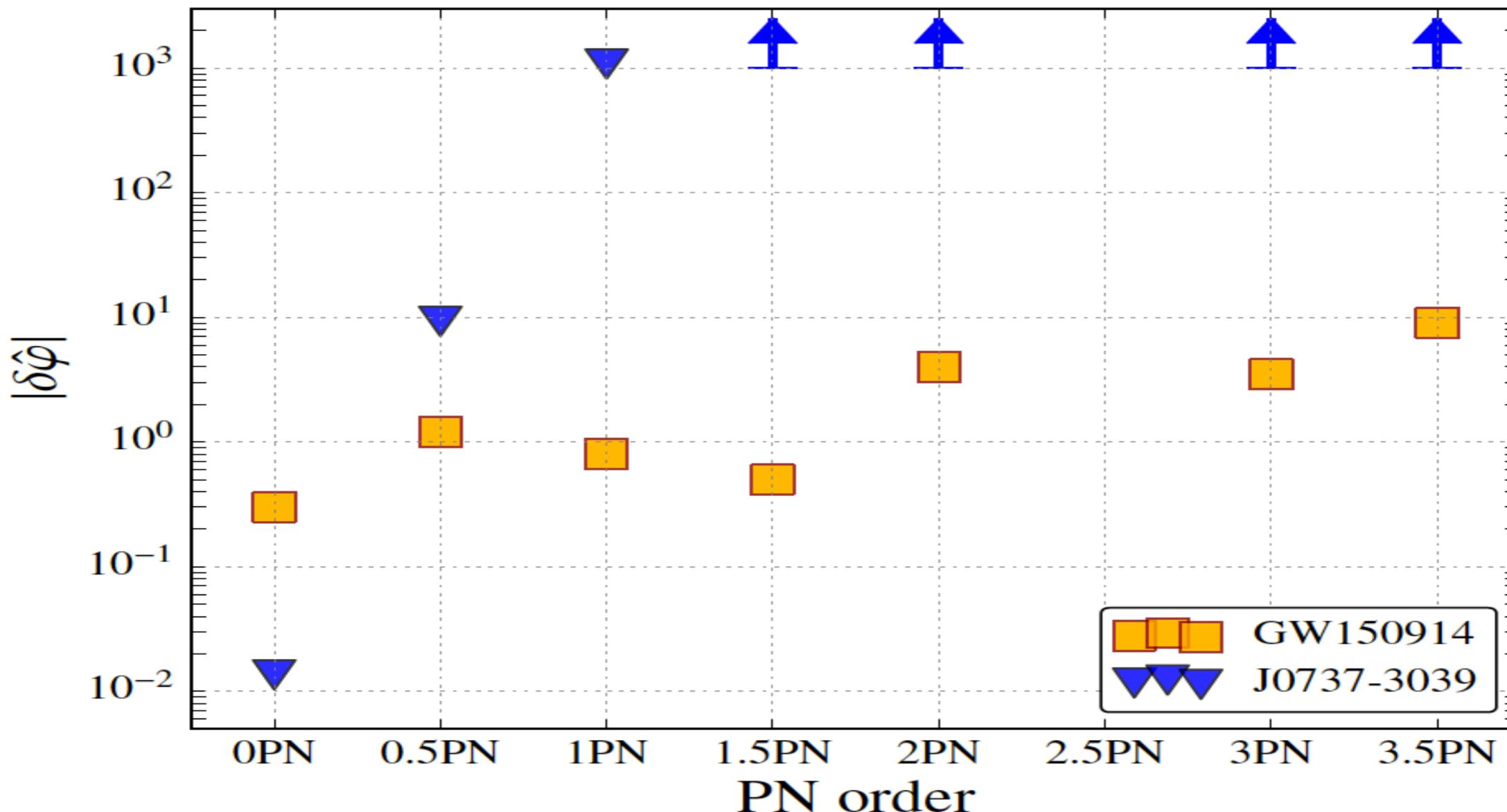
Has been demonstrated that it is enough to search for the dominant effect



Fundamental Physics



Test of the PN approximation during inspiral



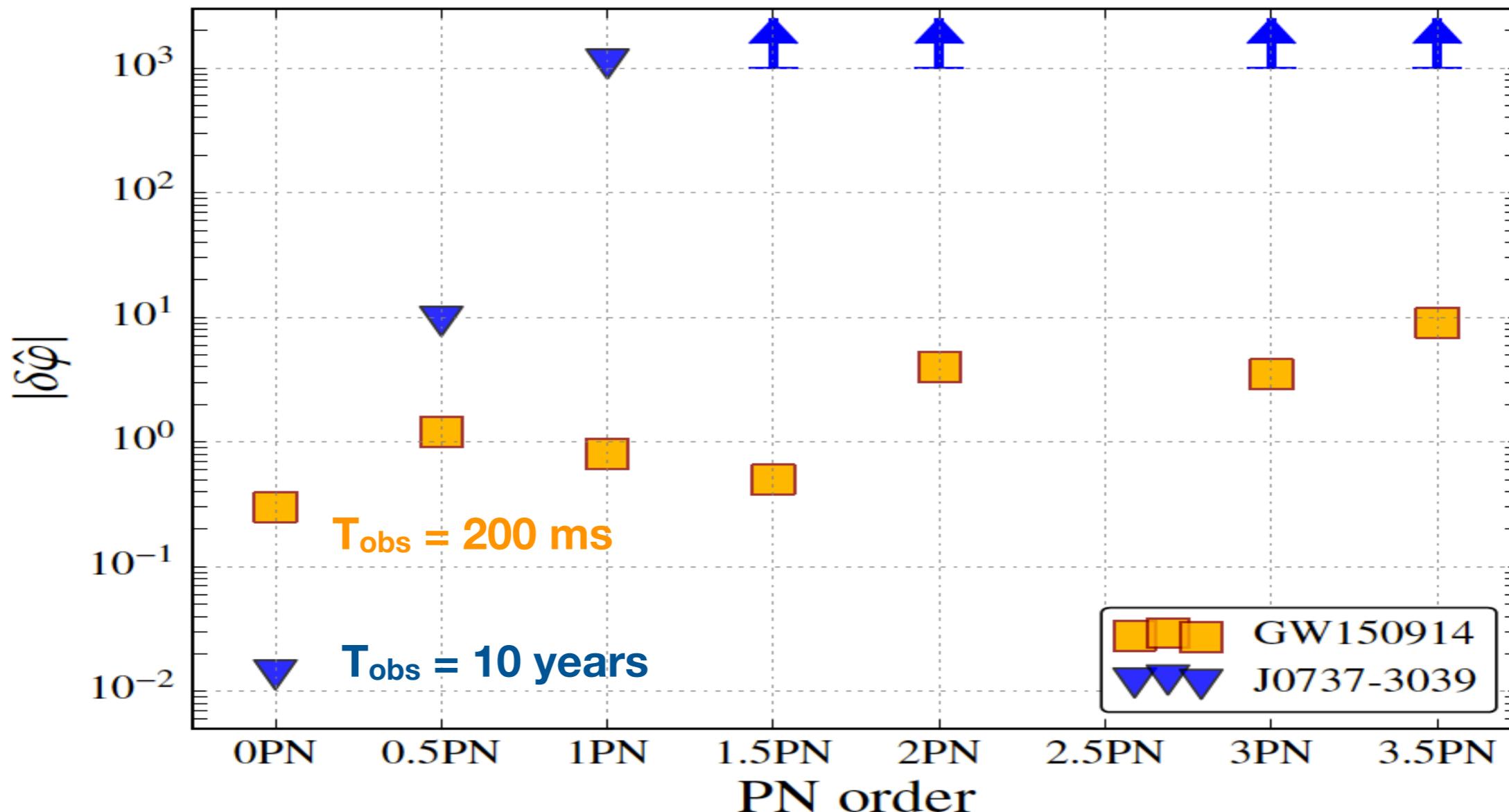
Abbott et al, arXiv:1903.04467



Fundamental Physics



Test of the PN approximation during inspiral



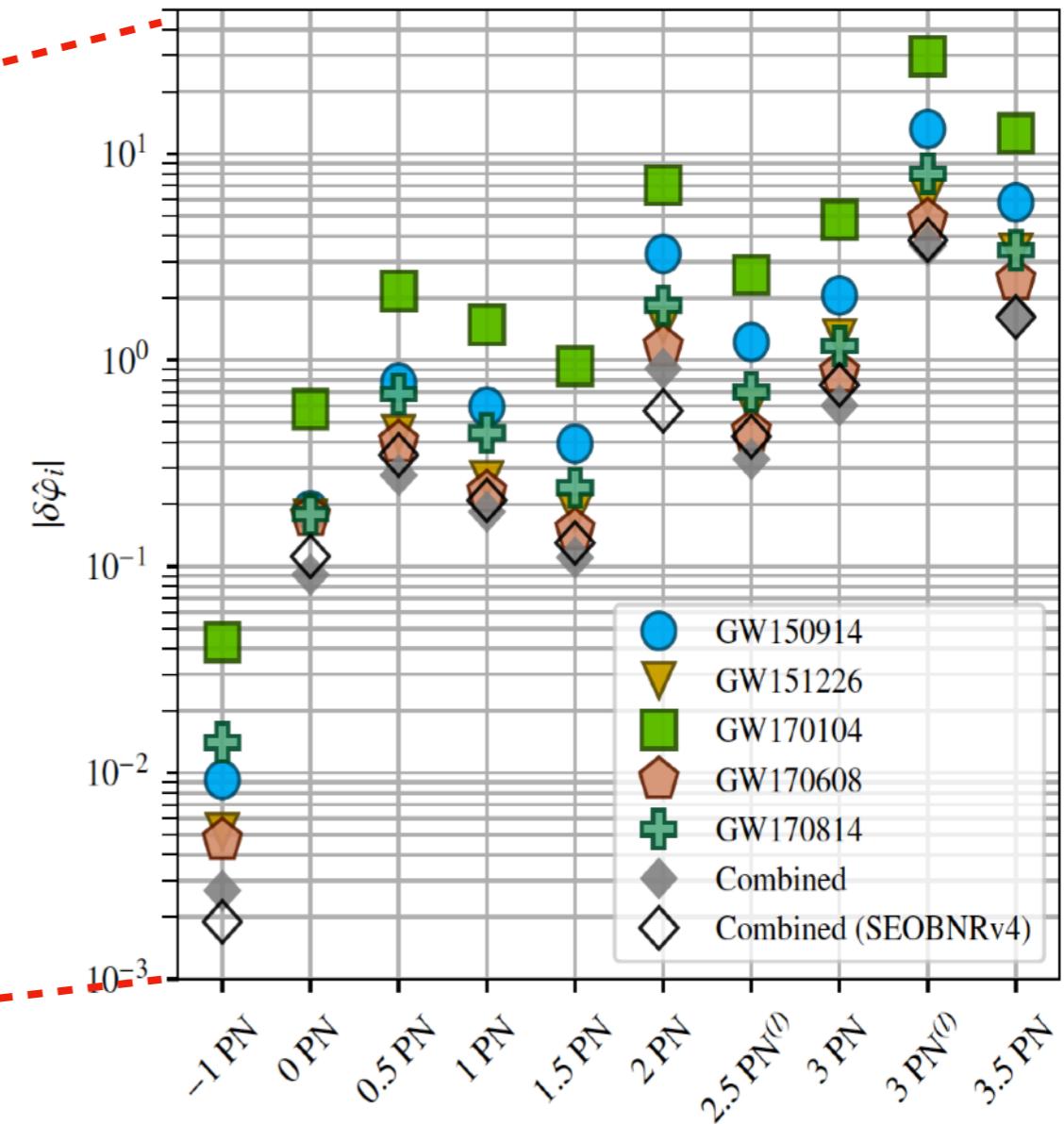
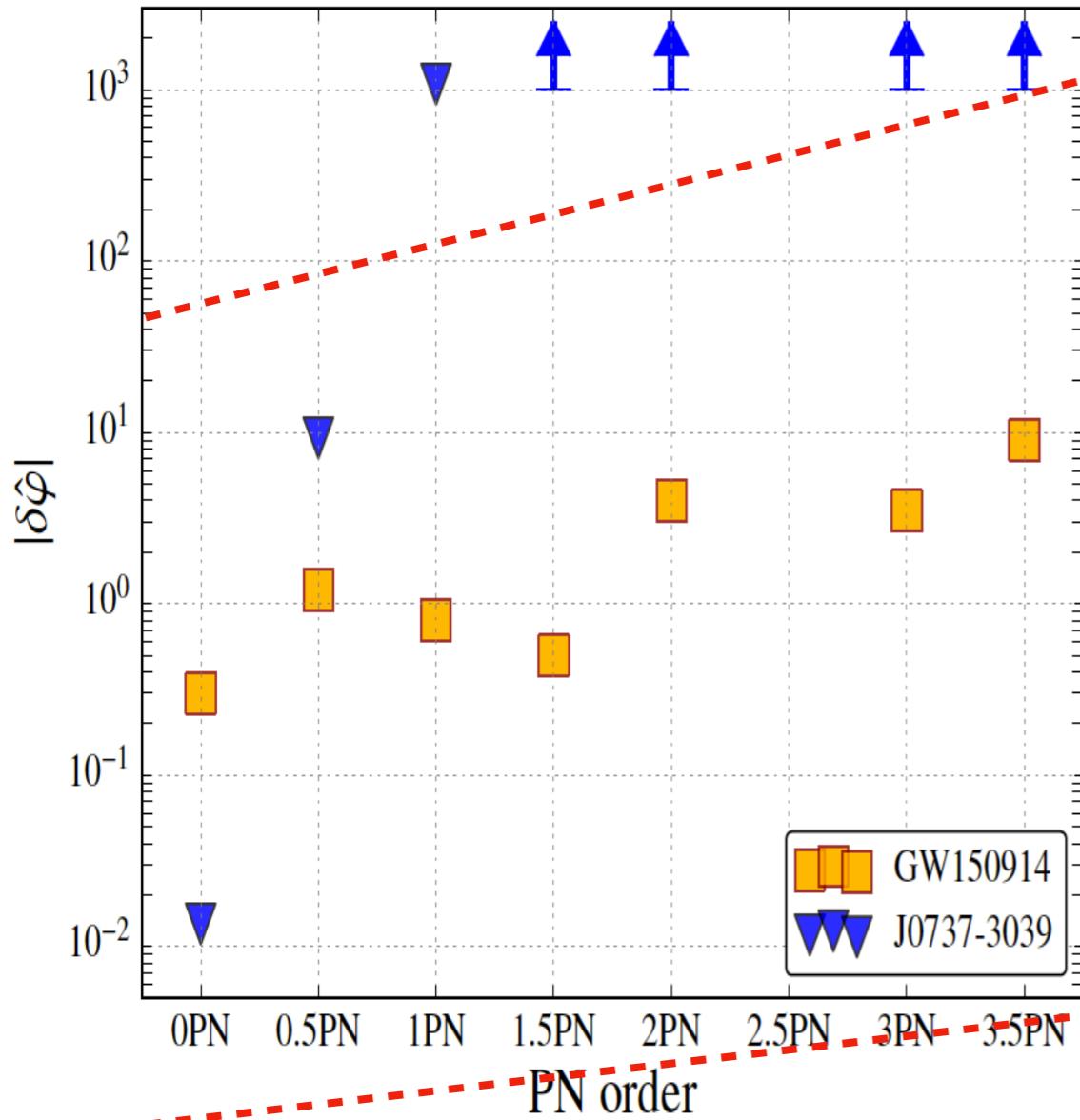
Abbott et al, arXiv:1903.04467



Fundamental Physics



Test of the PN approximation during inspiral

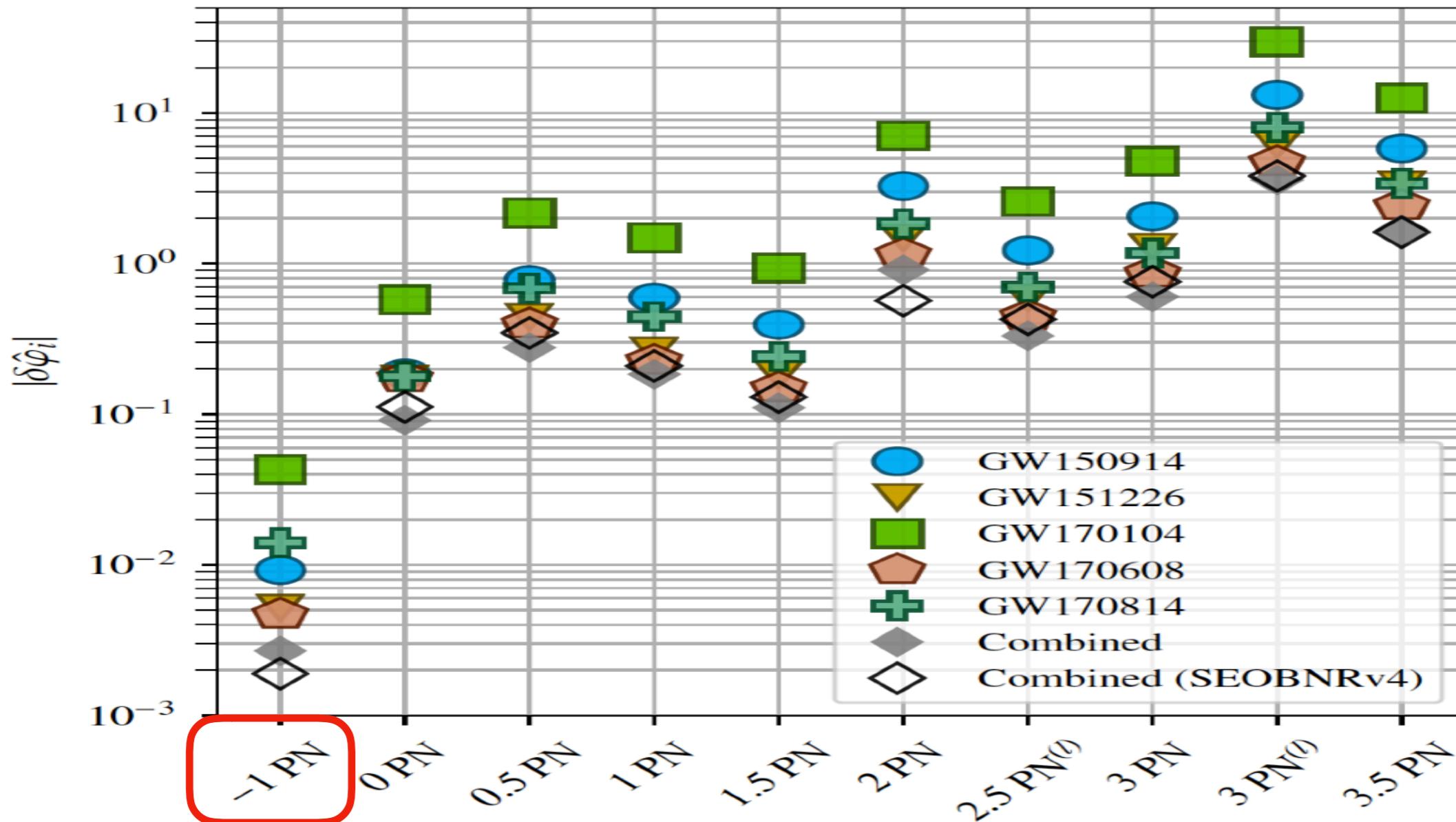


Abbott et al, arXiv:1903.04467

Fundamental Physics



Test for dipole radiation



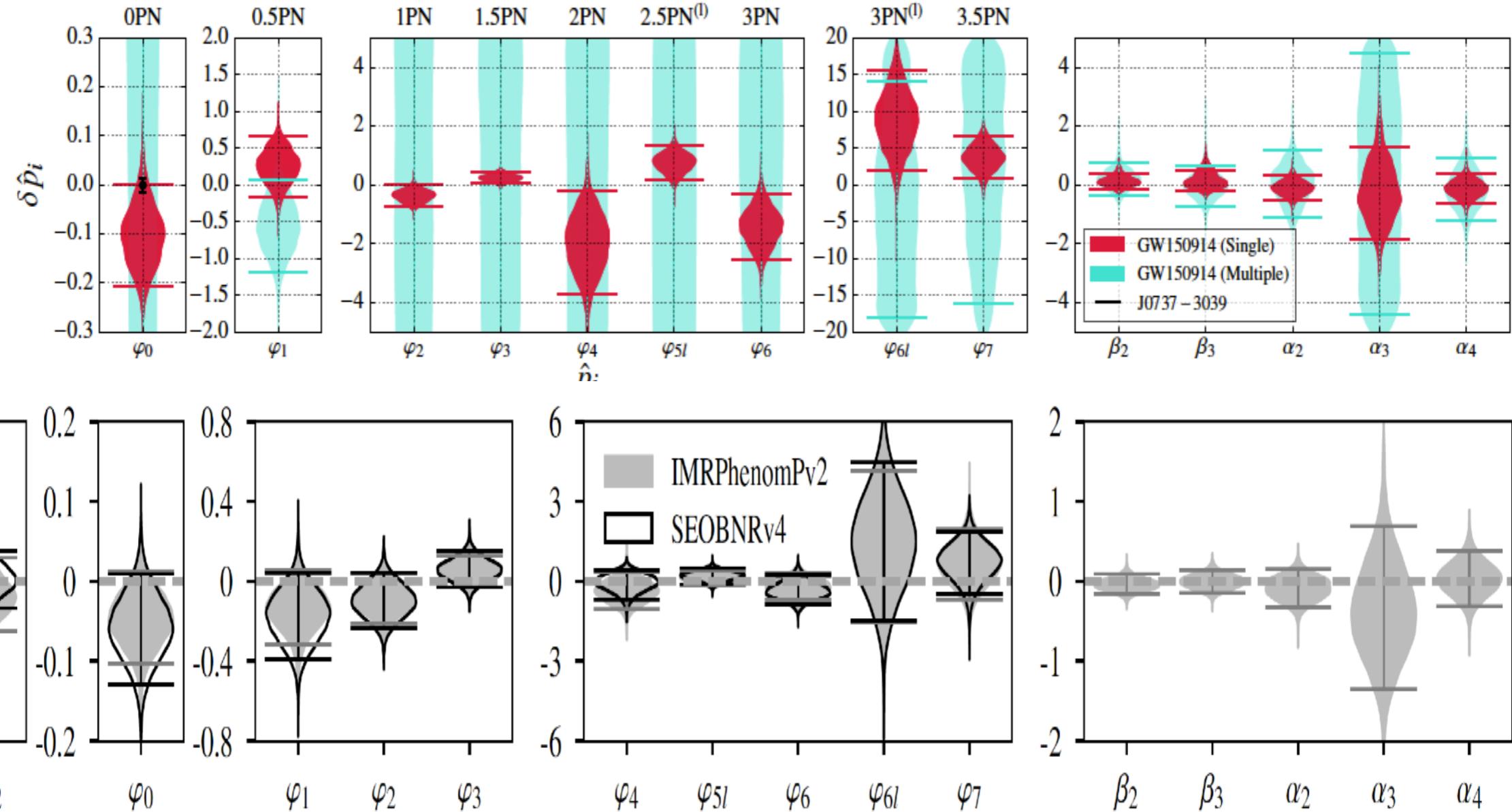
Abbott et al, arXiv:1903.04467



Fundamental Physics

If GR is correct, the deviation $\delta\hat{p}_i$ should be 0

GW150914



Abbott et al, arXiv:1903.04467



Fundamental Physics

- Assume a dispersion relationship of the form

$$E^2 = p^2 c^2 + A p^\alpha c^\alpha, \alpha \geq 0$$

- modifying the GW group velocity as

$$v_g/c = 1 + (\alpha - 1)AE^{\alpha-2}/2$$

- which changes the phase of the GW

$$\delta\Psi = \begin{cases} \frac{\pi}{\alpha-1} \frac{AD_\alpha}{(hc)^{2-\alpha}} \left[\frac{(1+z)f}{c} \right]^{\alpha-1} & \alpha \neq 1 \\ \frac{\pi AD_\alpha}{hc} \ln \left(\frac{\pi GM^{\det} f}{c^3} \right) & \alpha = 1 \end{cases}$$

Abbott et al, PRL 118, 221101 (2017)



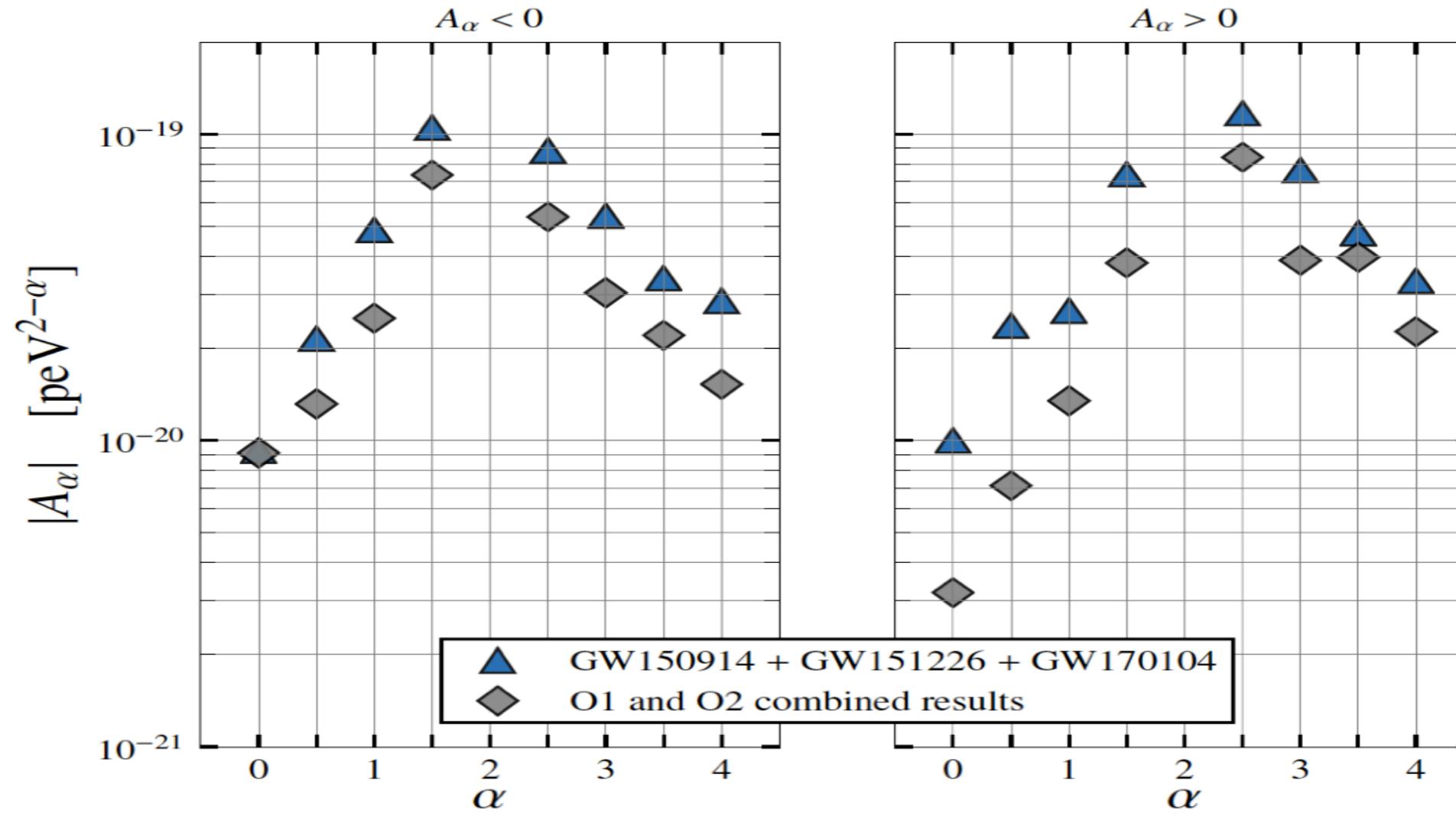
Fundamental Physics

Can probe the following theories:

- * Double special relativity $A = \eta_{dsrt}$, $\alpha = 3$
- * Extra-dimensional gravity $A = -\alpha_{edt}$, $\alpha = 4$
- * Horava-Lifshitz gravity $A = \kappa_{hl}^4 \mu_{hl}^2 / 16$, $\alpha = 4$
- * Massive gravity $A = (m_g c^2)^2$, $\alpha = 0$
- * Multifractional spacetime $A = (-3^{1-\alpha/2}) 2 E_*^{2-\alpha} / (3 - \alpha)$, $\alpha = 2 - 3$



Fundamental Physics

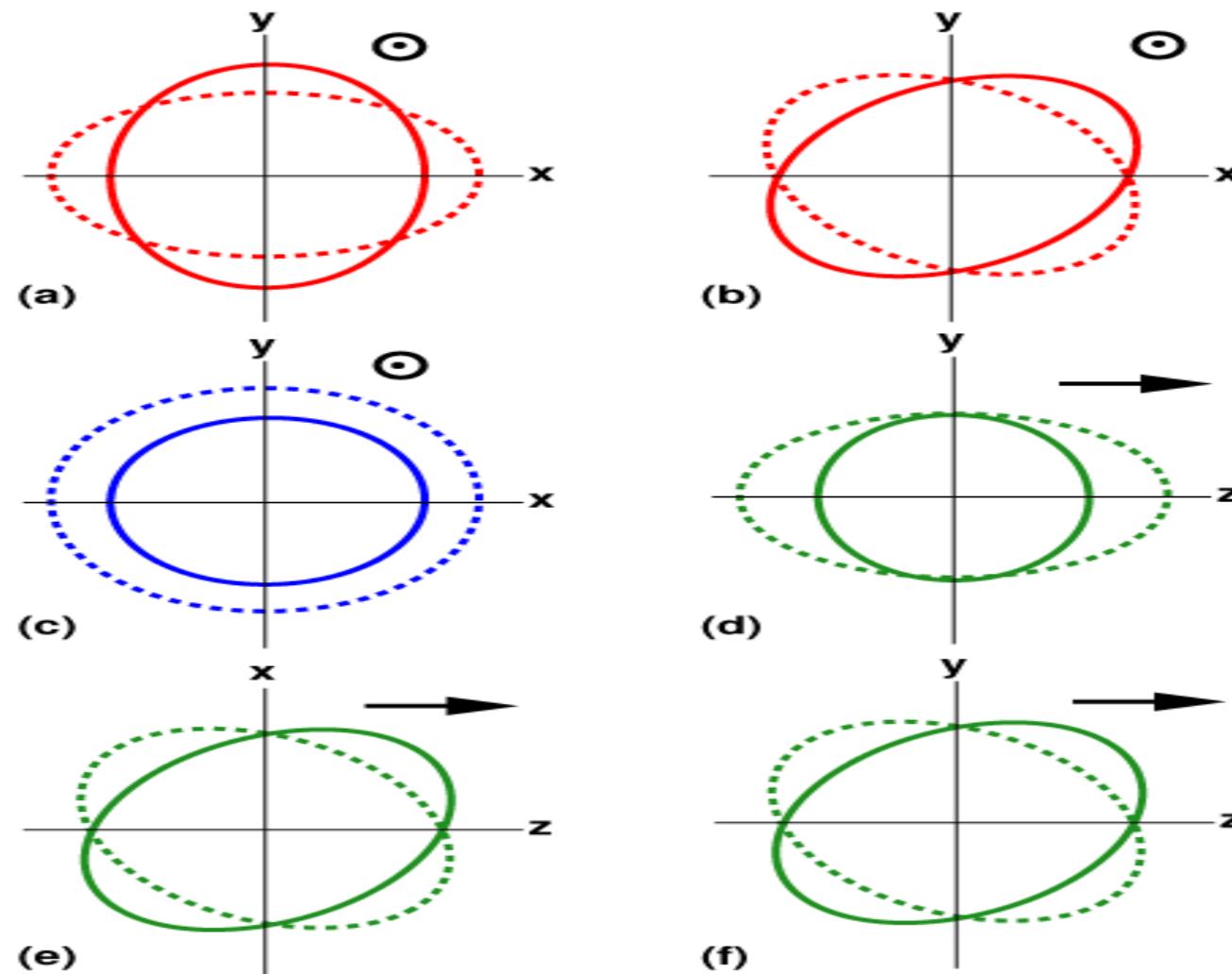


- ⌚ A_0 corresponds to a massive graviton
- ⌚ O1/O2 results give $m_g \leq 5 \times 10^{-23} \text{ eV}/c^2$ or $\lambda_g > 2.4 \times 10^{13} \text{ km}$

Abbott et al, arXiv:1903.04467

Fundamental Physics

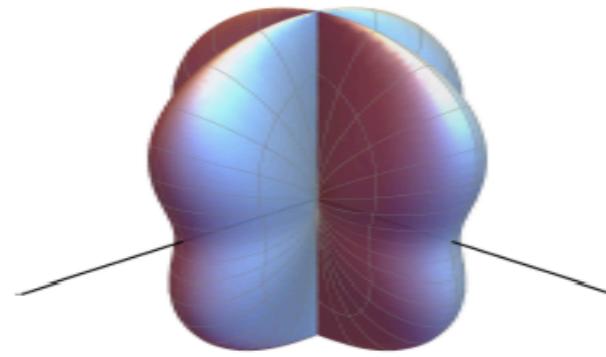
- In generic metric theories, GWs can have up to 6 polarisations coming from the 6 independent components of the Riemann tensor.
- Test possible due to inclusion of Advanced Virgo



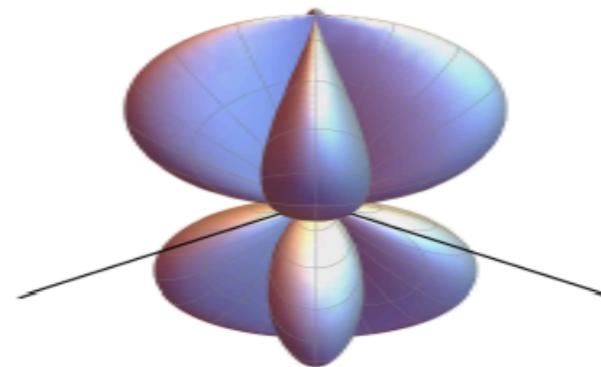
Fundamental Physics

Different polarisations produce a different response at the detector

Tensor

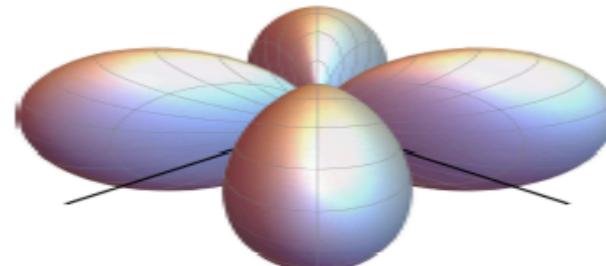


(a) Plus (+)

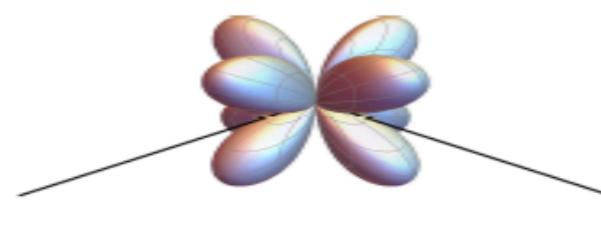


(b) Cross (x)

Vector

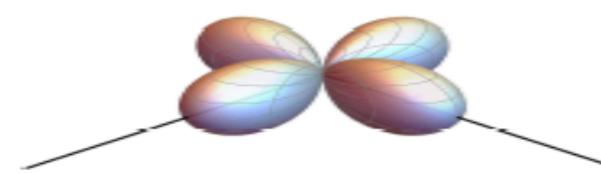


(c) Vector-x (x)



(d) Vector-y (y)

Scalar



(e) Scalar (s)

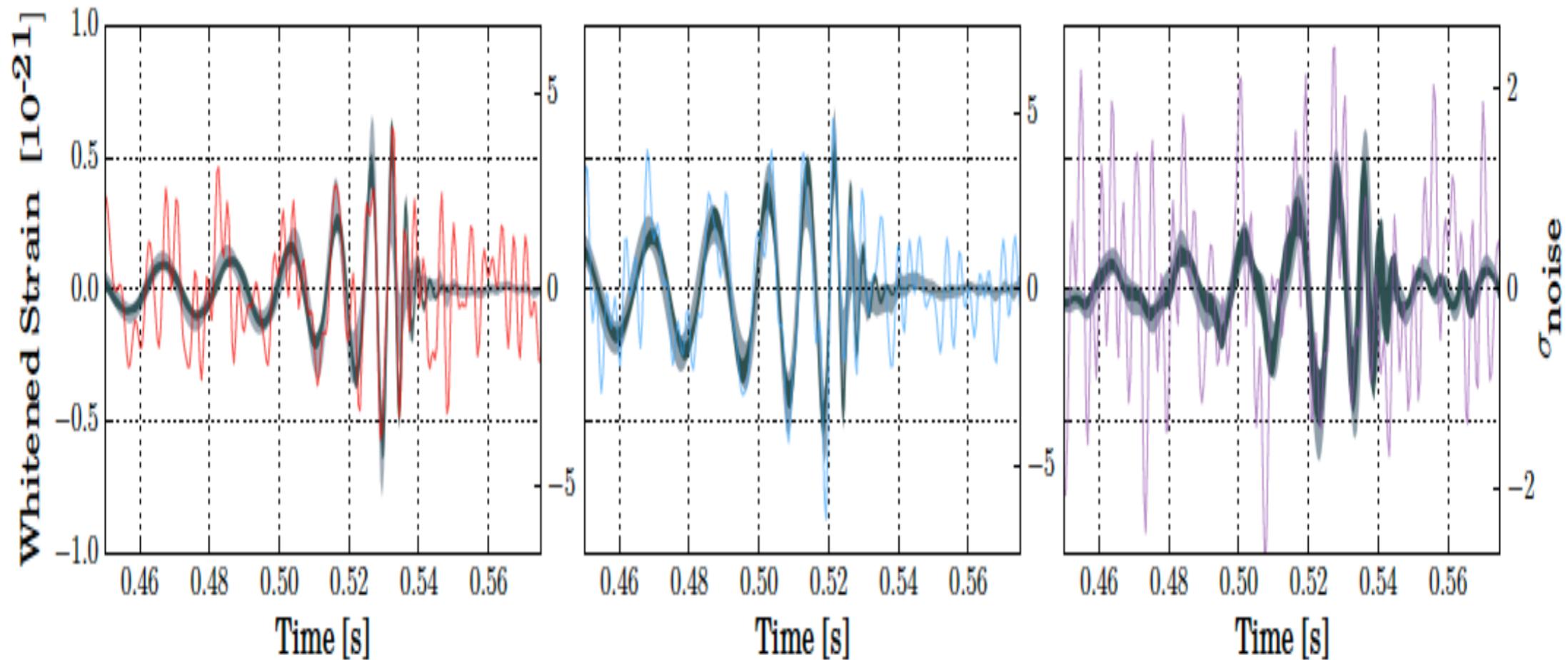
$$\begin{aligned} T:V &= 200:1 \\ T:S &= 1000:1 \end{aligned}$$

Credit: Max Isi



Fundamental Physics

Is this really surprising...?



Abbott et al, PRL 119, 141101 (2017)

GR templates match the phase of the data extremely well!!

**Already heavily constrains how much non-tensorial polarisation there can be,
as well as the level of potential dipole radiation!**



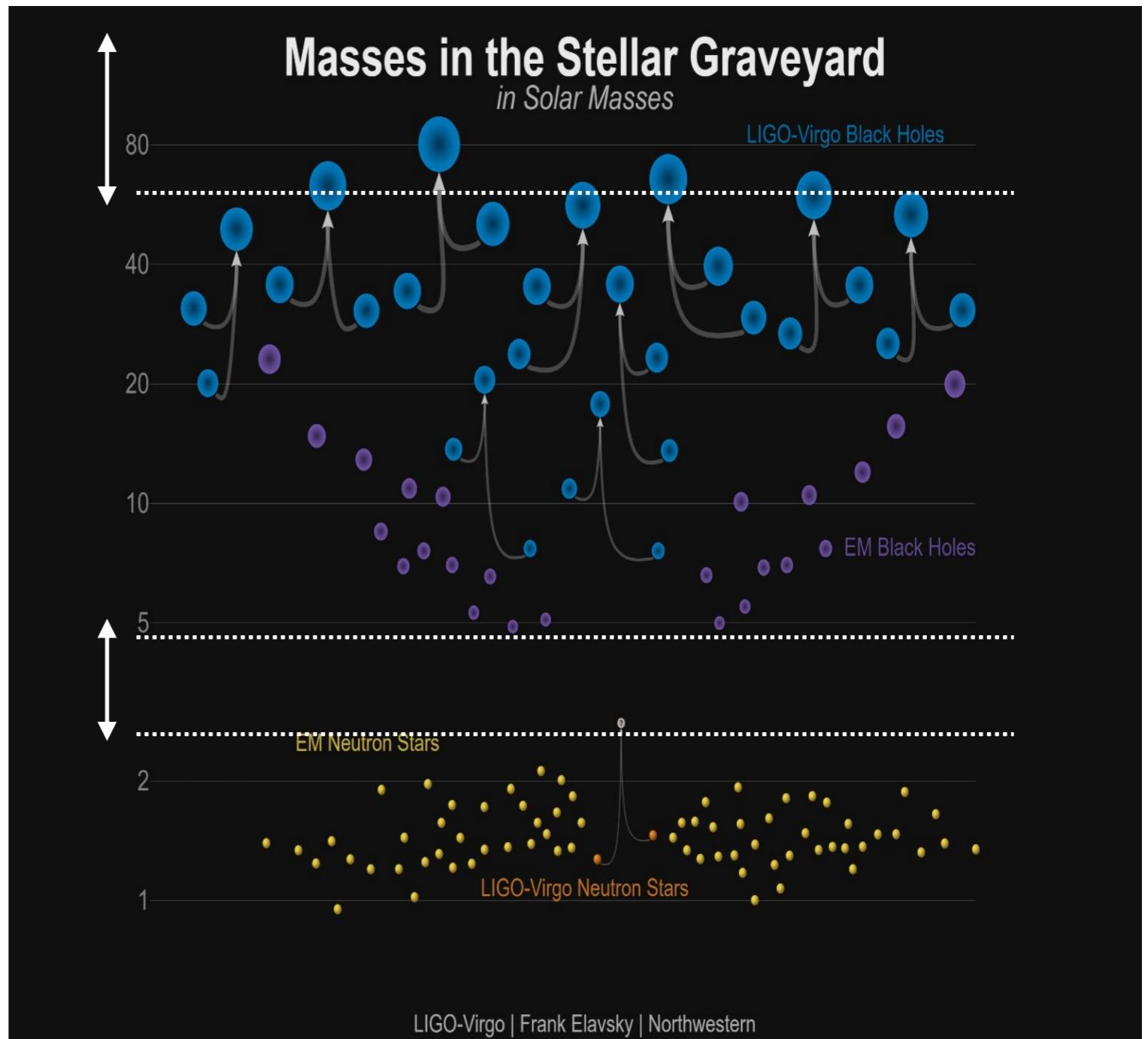
Astrophysics

- Uncertainty in formation channels
 - galactic field evolution
 - dynamical capture in globular clusters
- How does the common envelope phase actually work?
- Role of metallicity?
- Do natal kicks in SN play a role?
- How does mass transfer efficiency affect binary evolution?
- What is the merger rate for binary systems?



ASTROPHYSICS

- Two possible mass gaps
- $>3 M_{\odot}$: nuclear EOS
- $<5 M_{\odot}$: binary evolution
- $> 50 M_{\odot}$: PISN

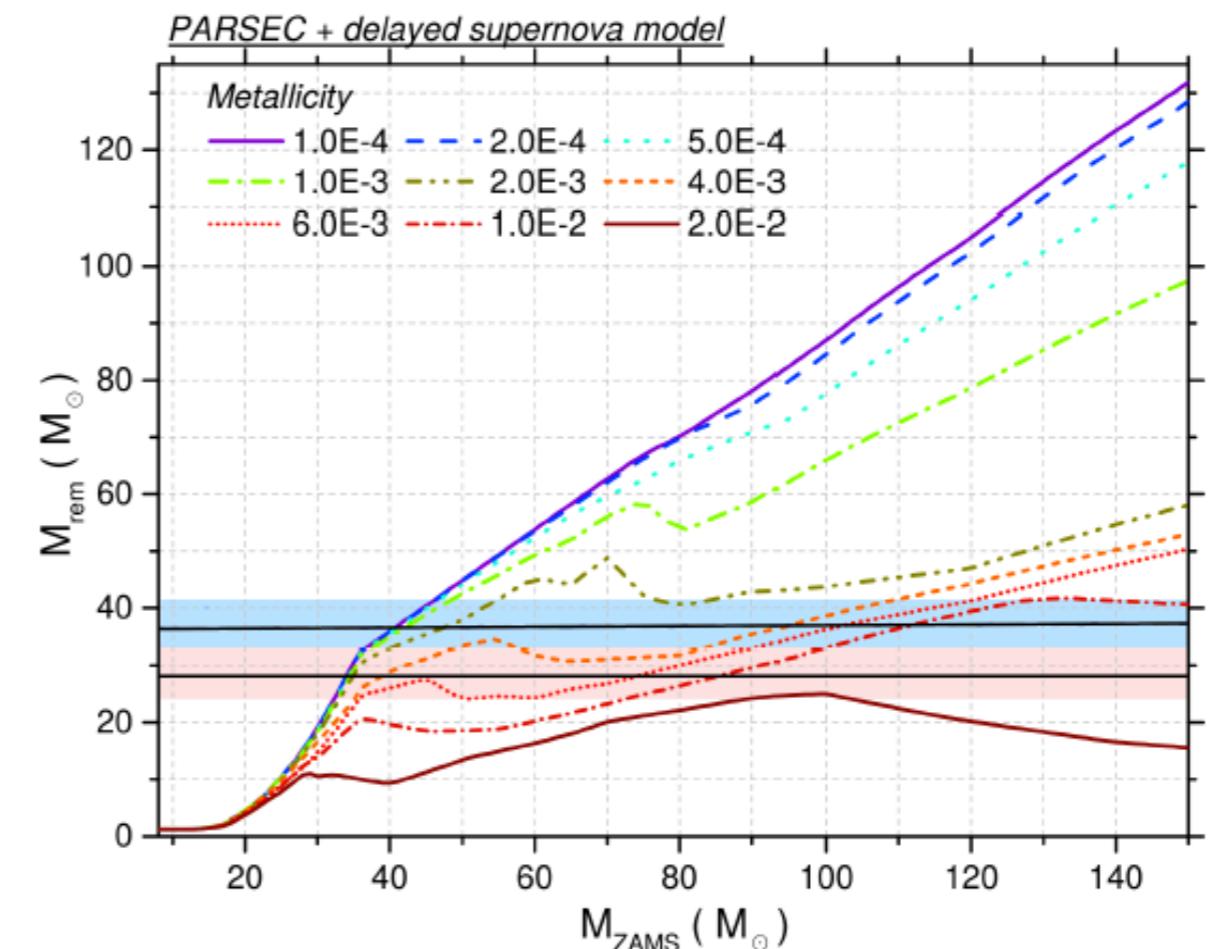
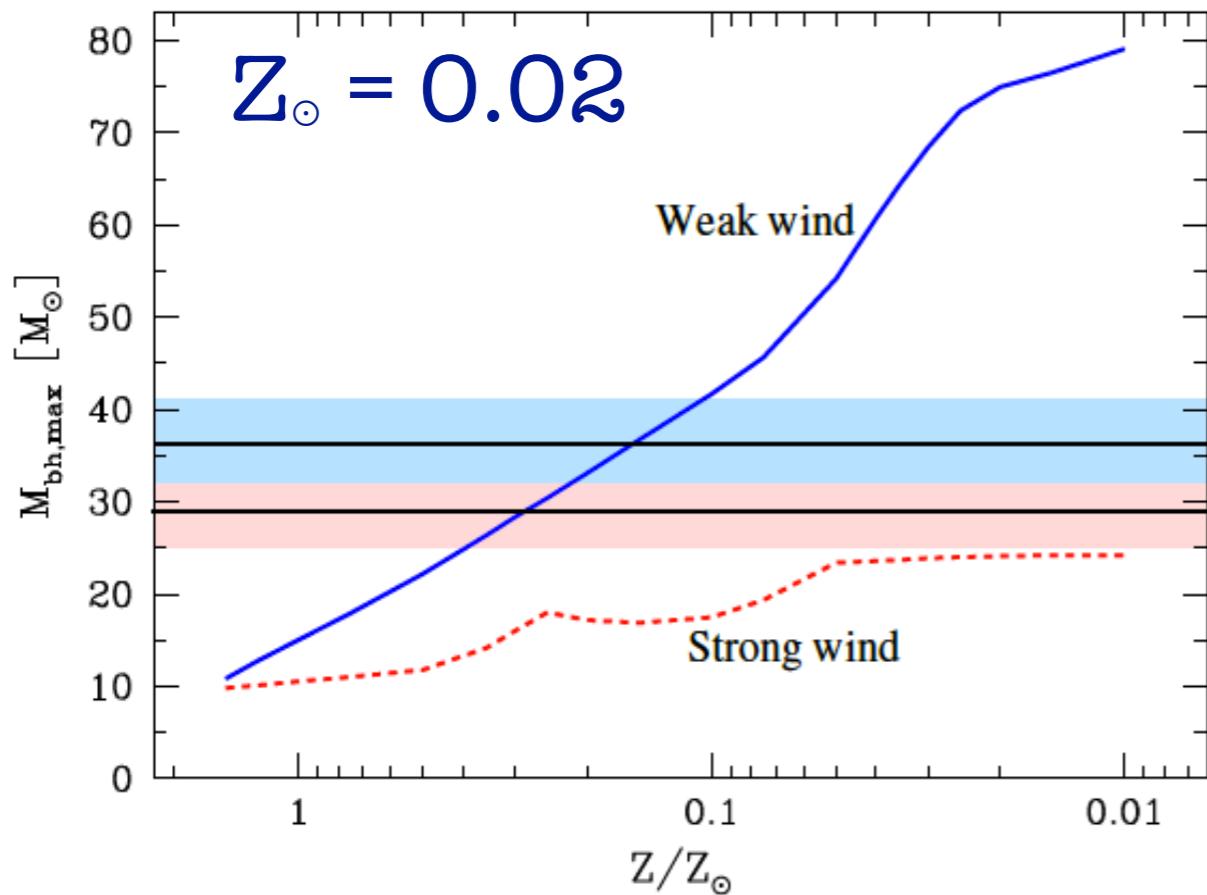


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BH FORMATION

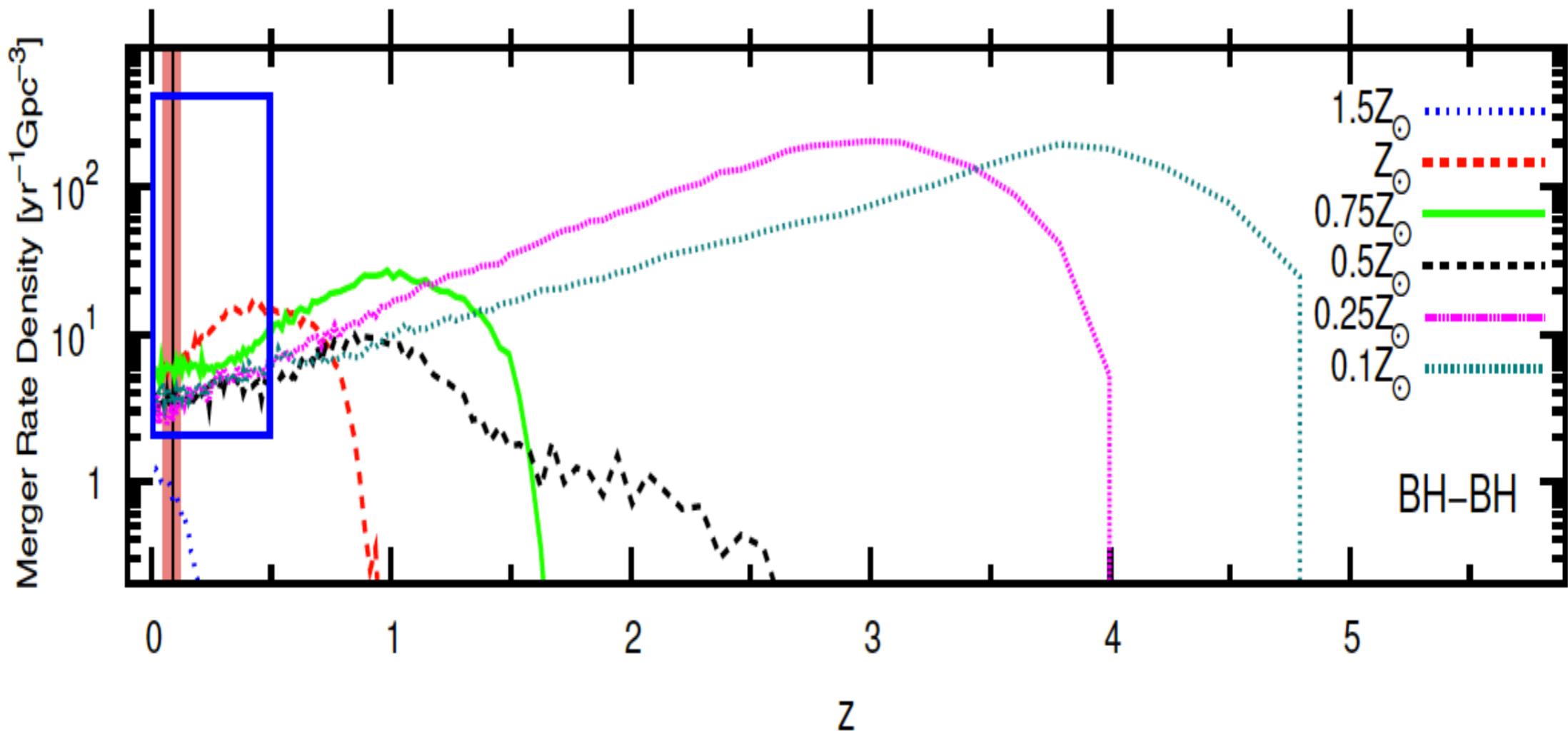
e.g. GW150914



- Weak winds and low metallicity produce large BHs
- The lower the metallicity, the smaller the progenitor needed

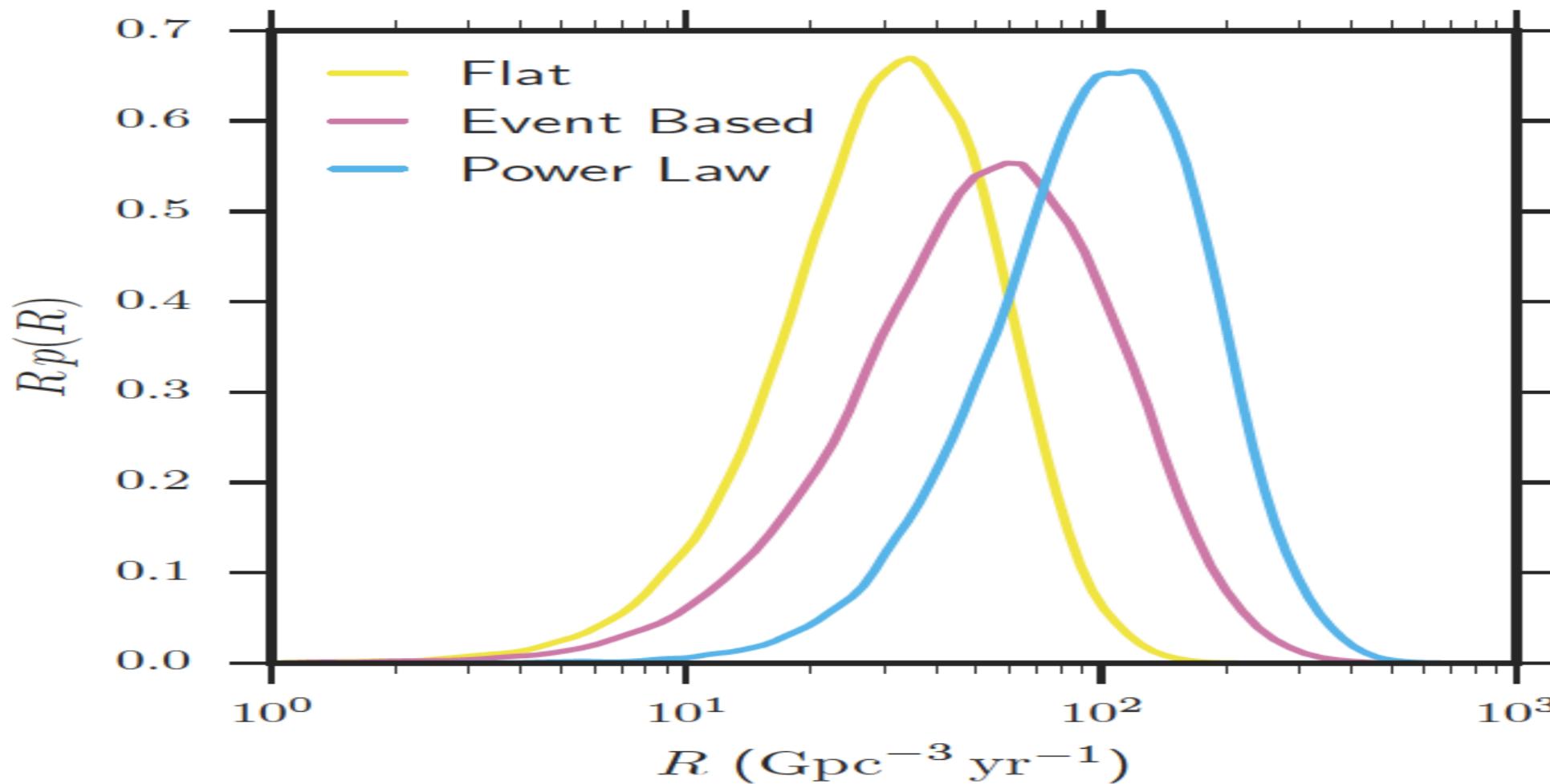
Abbott et al, *Astrophys.J.* 818 (2016) L22

BBH mergers in the local Universe



- ⌚ Not yet possible to measure the BH mass function
- ⌚ Our detections are consistent with
 - ⌚ dynamical formation in GCs
 - ⌚ isolated field binaries

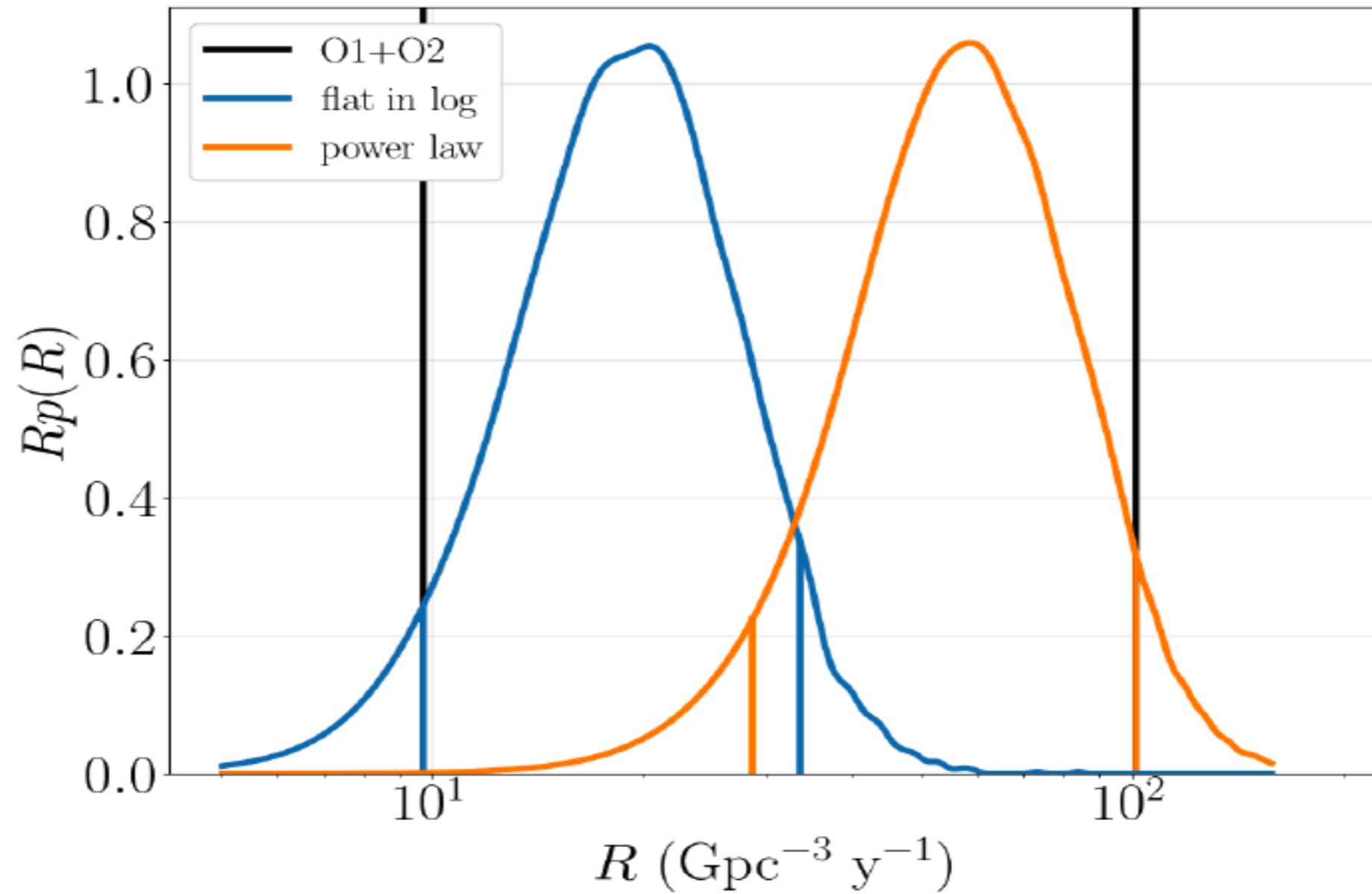
01 BBH Rates



- Flat distribution in the log of the individual masses
- Power law distribution in the primary mass, uniform in the secondary
- Event based
- Combined O1 rate estimate : $9-240 \text{ Gpc}^{-3} \text{yr}^{-1}$ (90% CI)

Abbott et al, Phys.Rev. X6 (2016) no.4, 041015

O1 + O2 BBH RATES



$9.7 - 101 \text{ Gpc}^{-3} \text{yr}^{-1}$

B. Abbott et al, arXiv:1811.12907



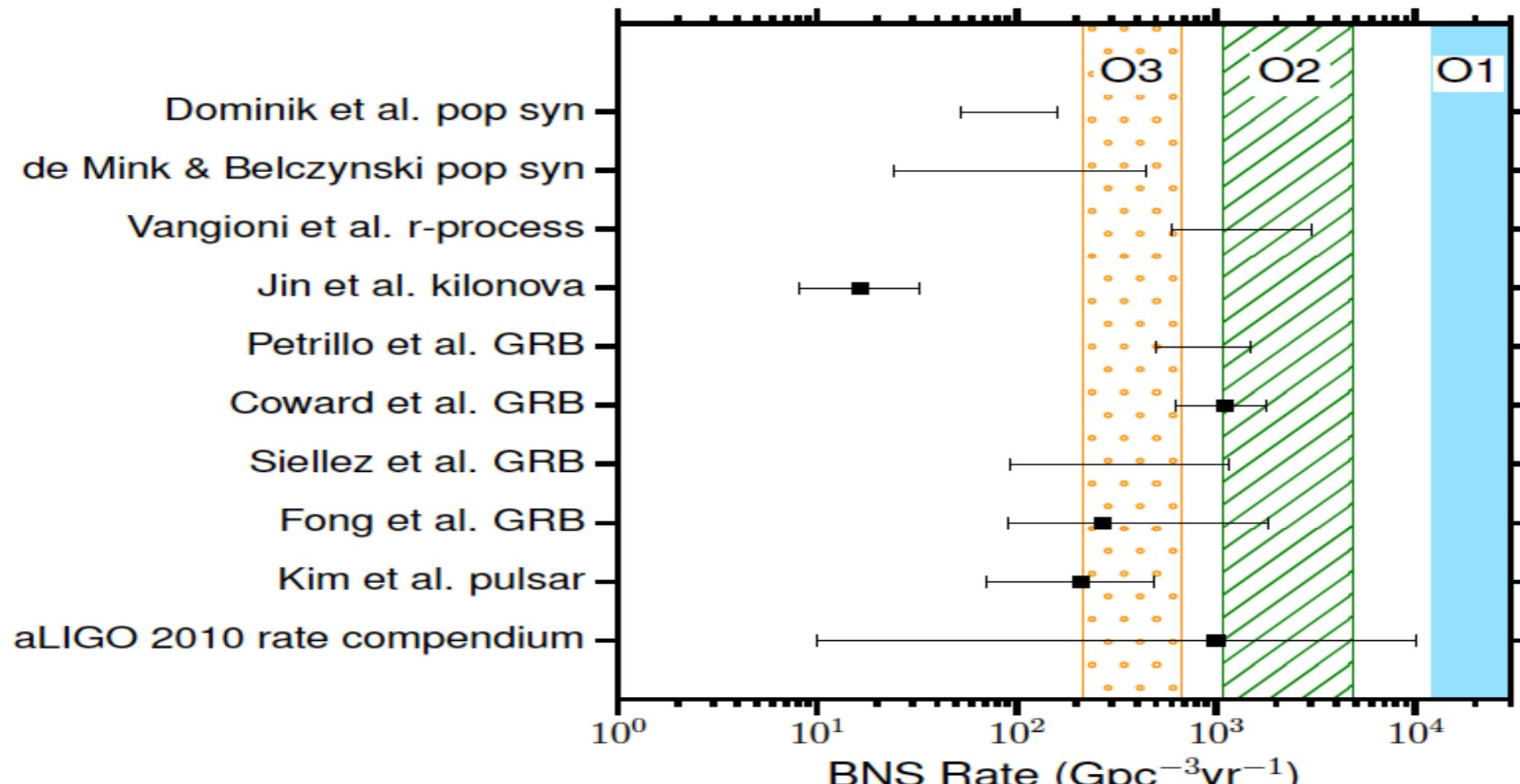
BBH Formation Channels

- ➊ If we assume a single formation channel, lower limit disfavours
 - ➊ dynamical formation in low-mass GCs
 - ➋ very high natal kicks in isolated binaries ($> 100s$ km/s)
 - ➌ combination of very low CE binding energy with high efficiency ejection

- ➋ If we assume multiple simultaneous formation channels
 - ➊ nothing can be ruled out



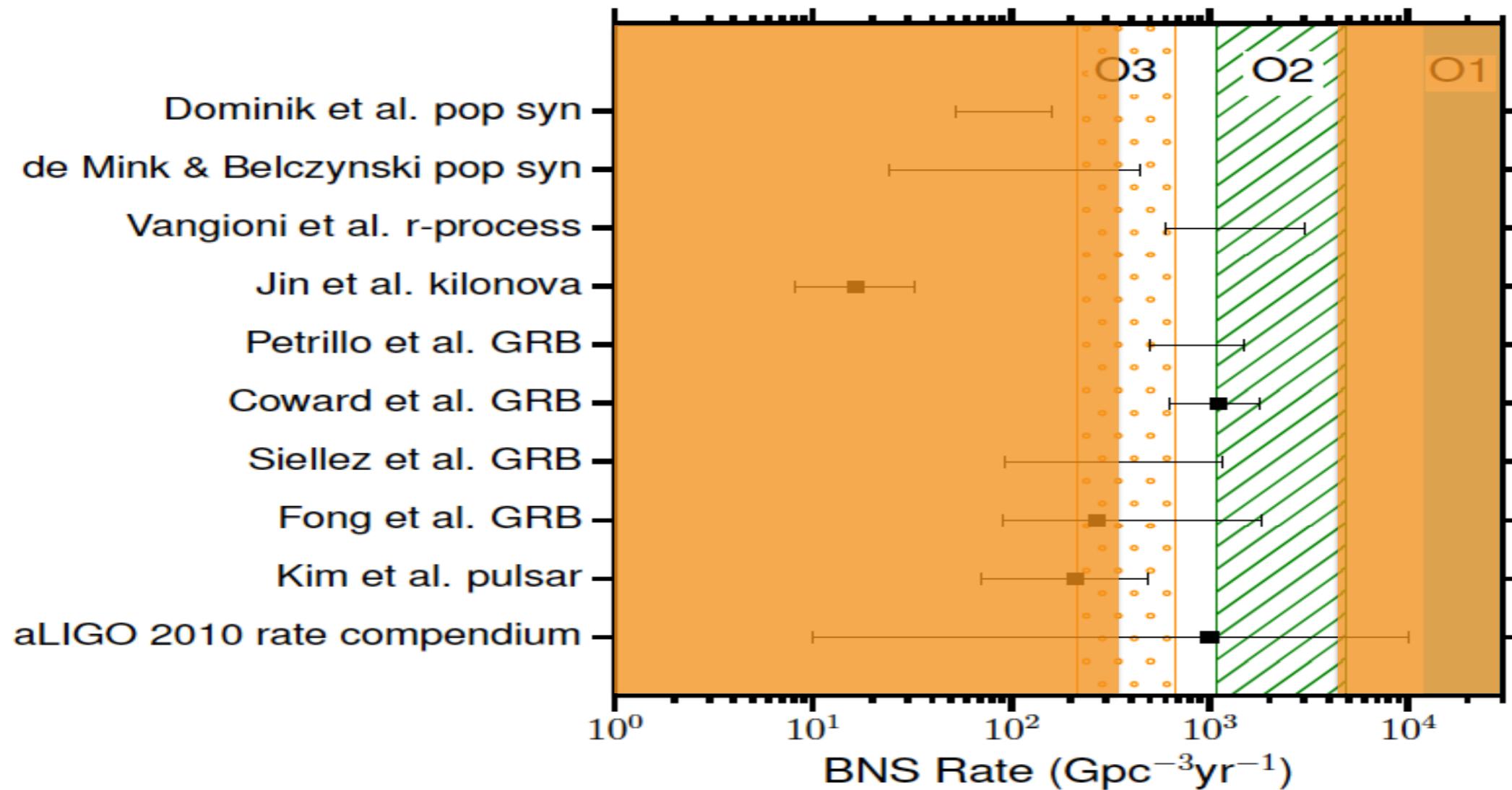
BNS Event Rates



O1 : $\mathcal{R} < 12,600 \text{ Gpc}^{-3} \text{yr}^{-1}$

Abbott et al, *ApJ 832, L21 (2016)*

BNS Event Rates

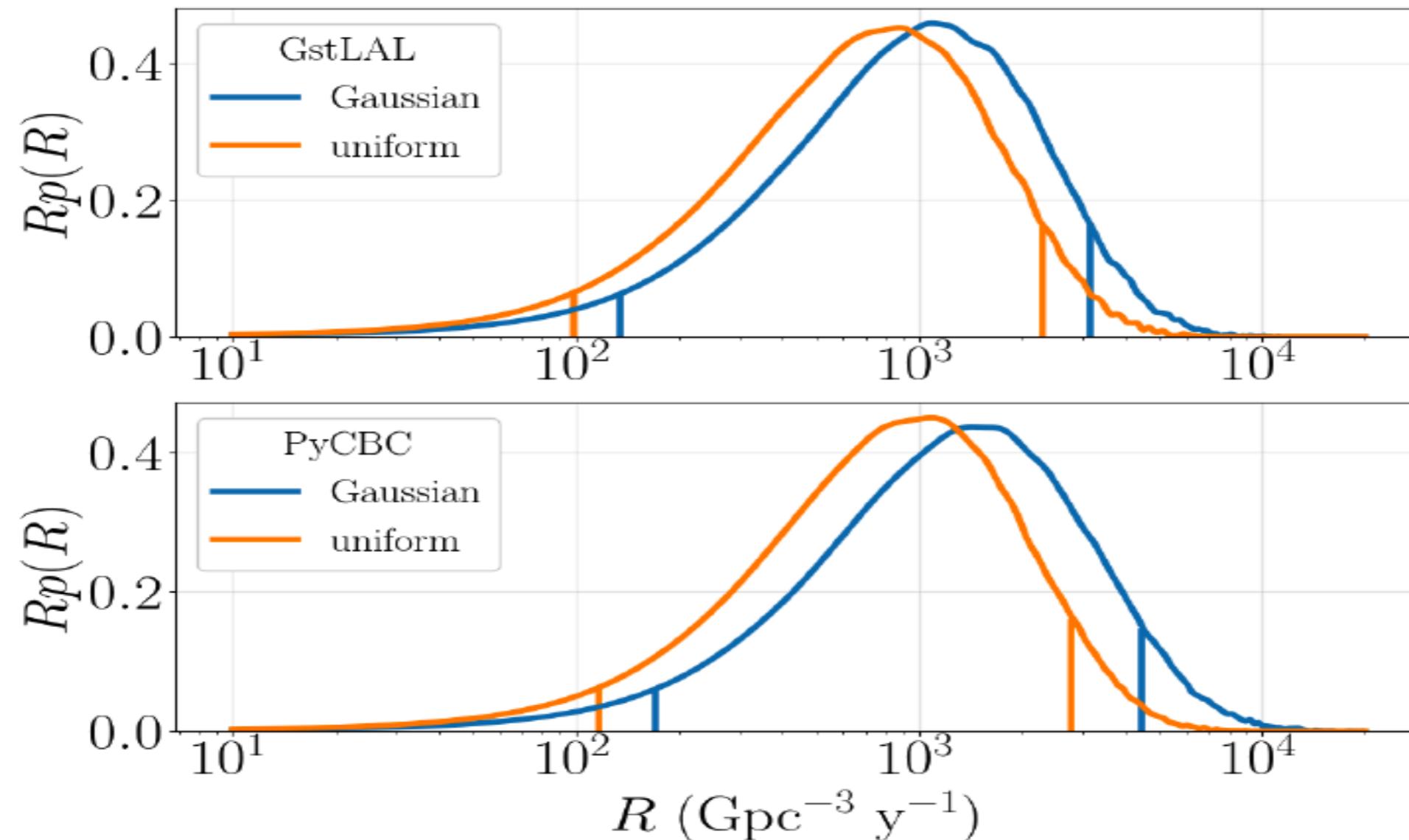


after GW170817, assuming a population uniform in with uniform component mass in the range $[1,2] M_\odot$: $\mathcal{R} = 320 - 4740 \text{ Gpc}^{-3} \text{ yr}^{-1}$

Abbott et al, *PRL* 119, 161101 (2017)



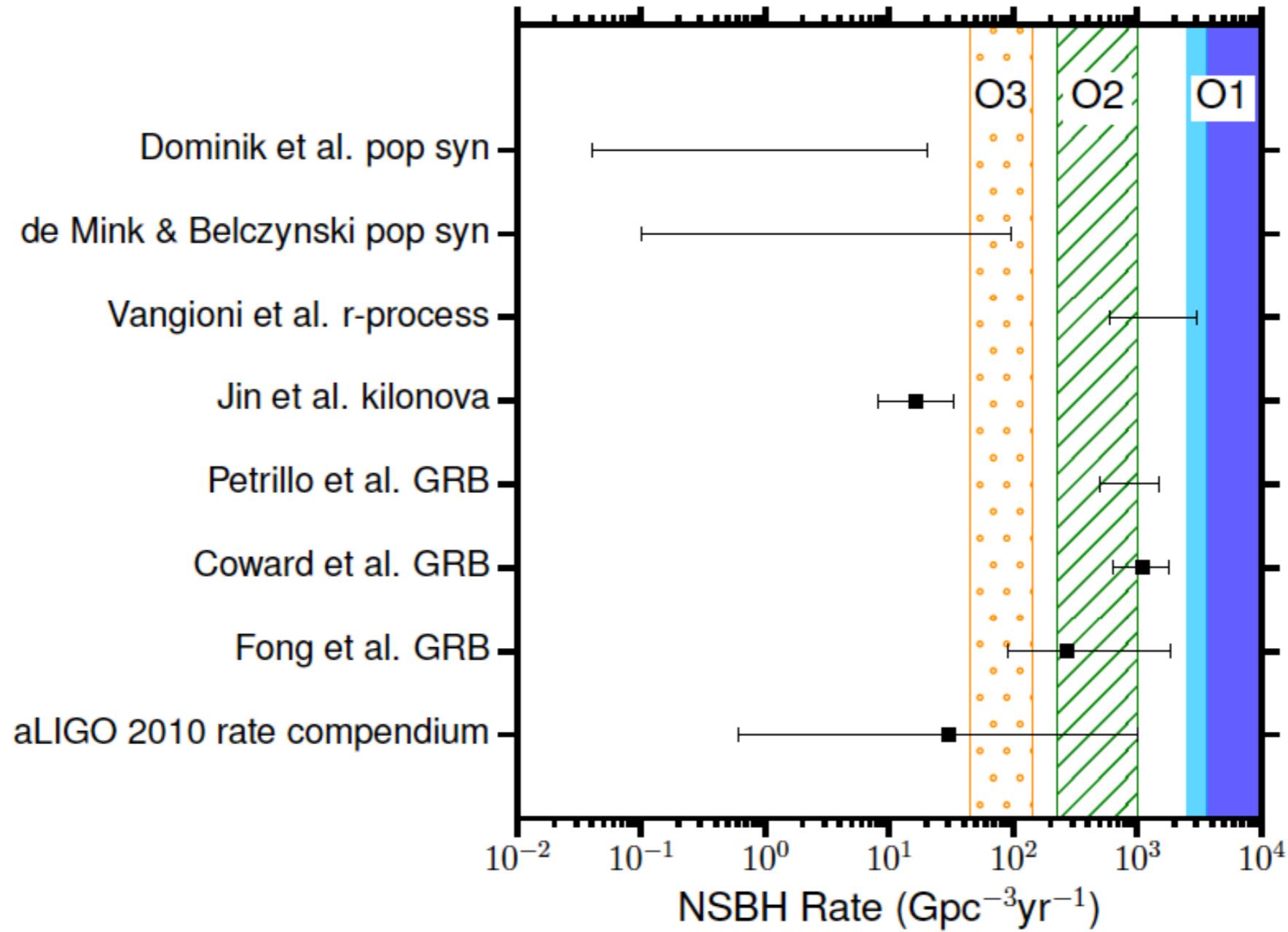
BNS Event Rates



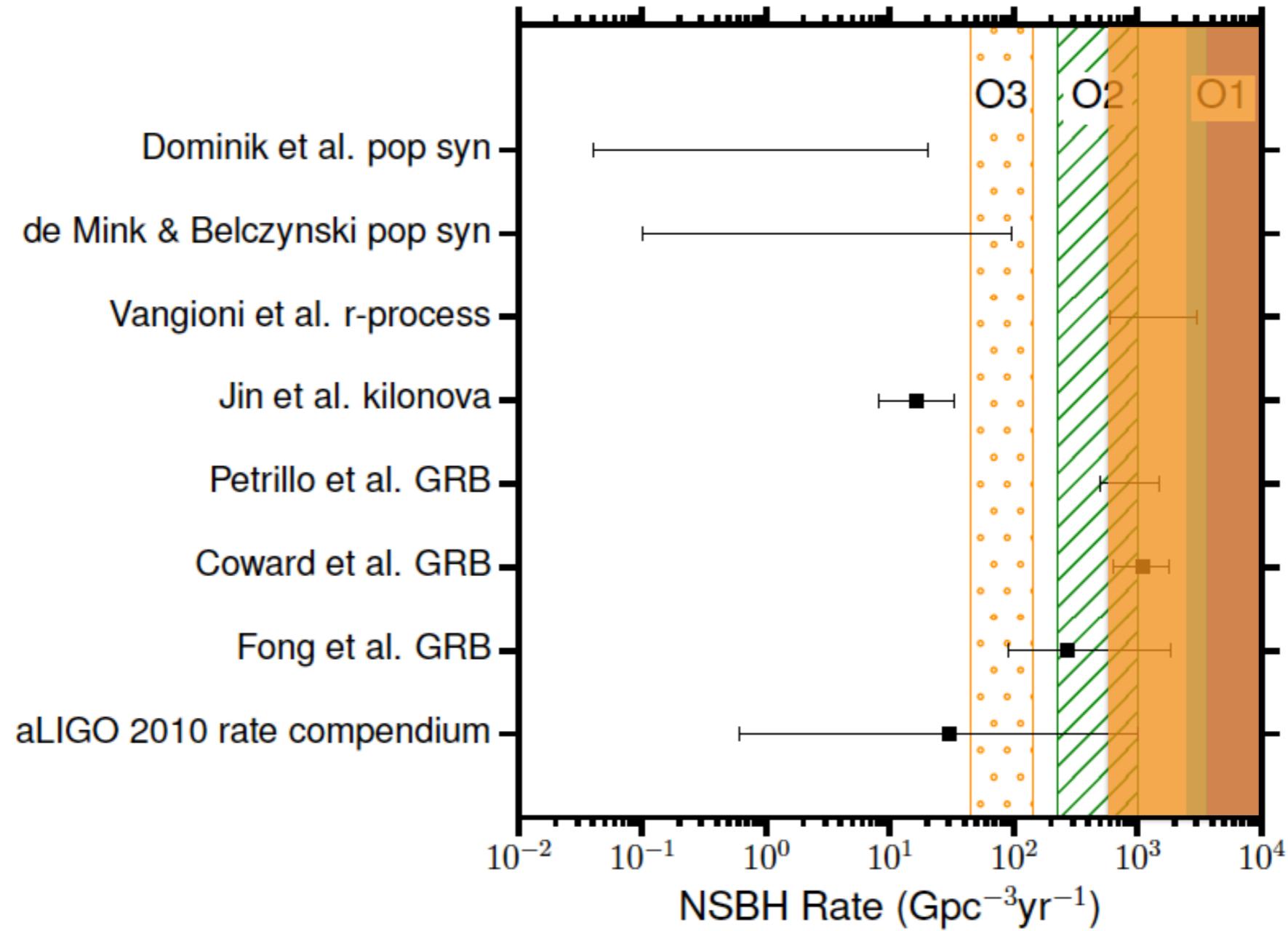
Combined 01+02 result using new population models: $\mathcal{R} = 110 - 3840 \text{ Gpc}^{-3} \text{ yr}^{-1}$



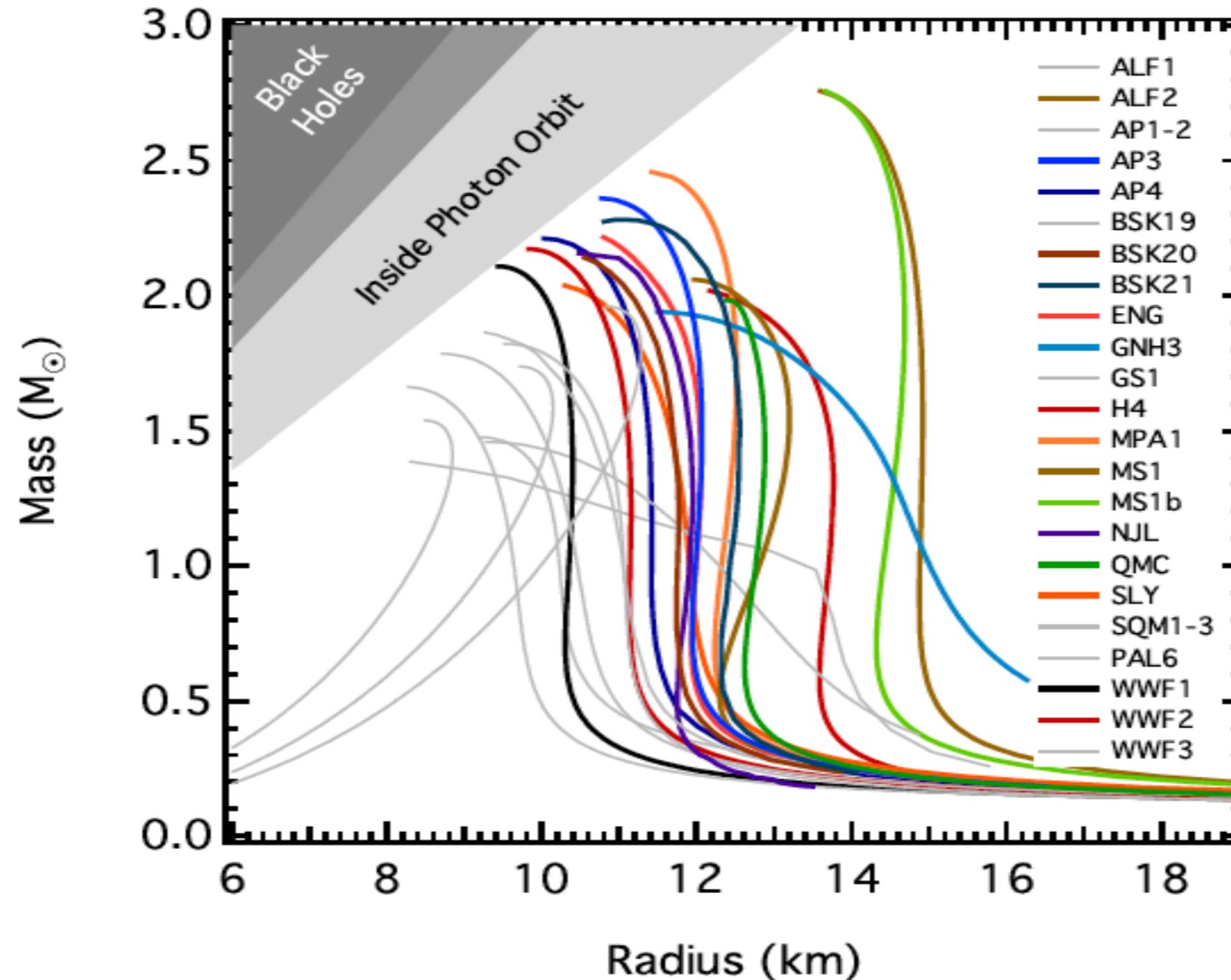
BHNS Rates



BHNS Rates

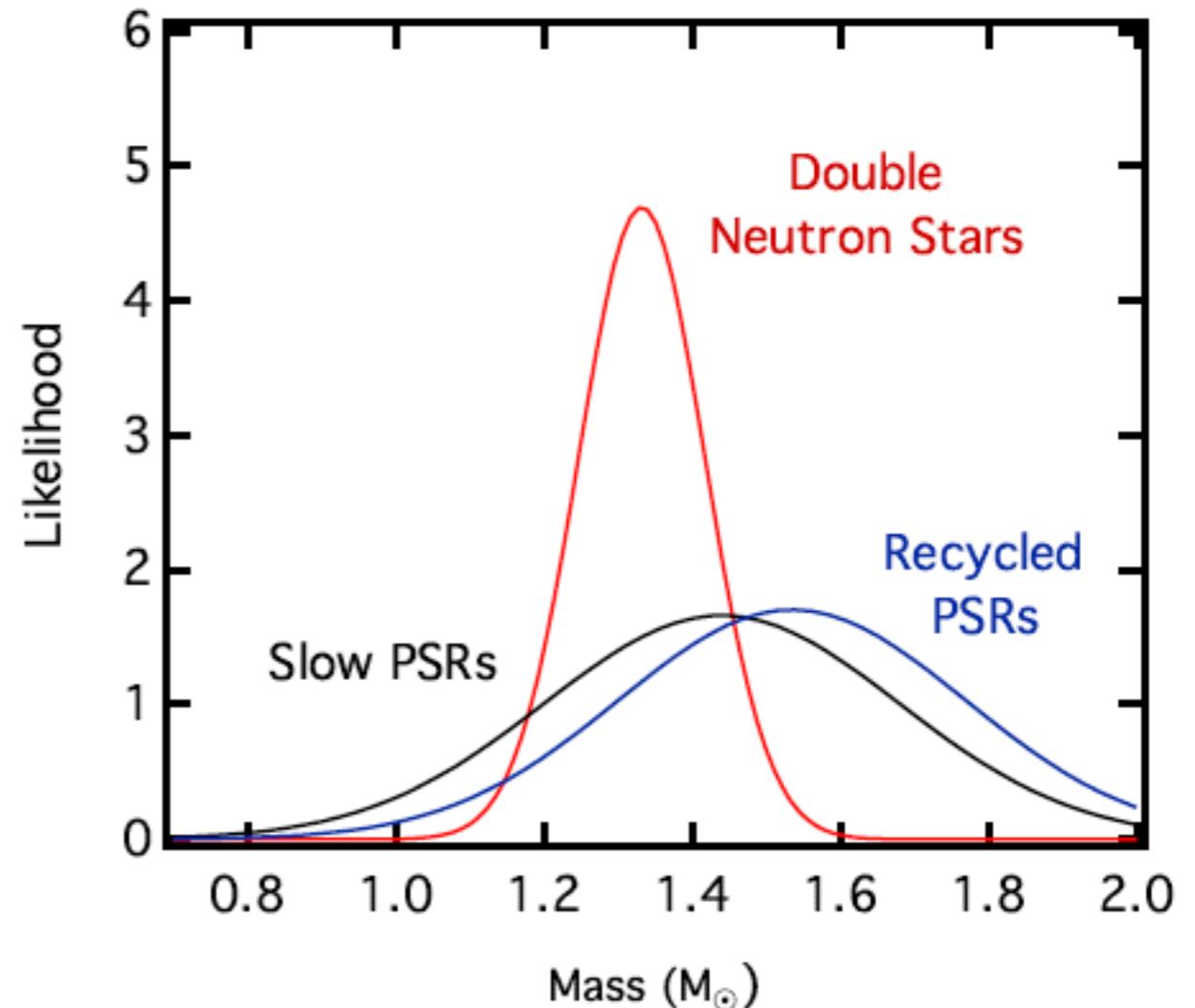
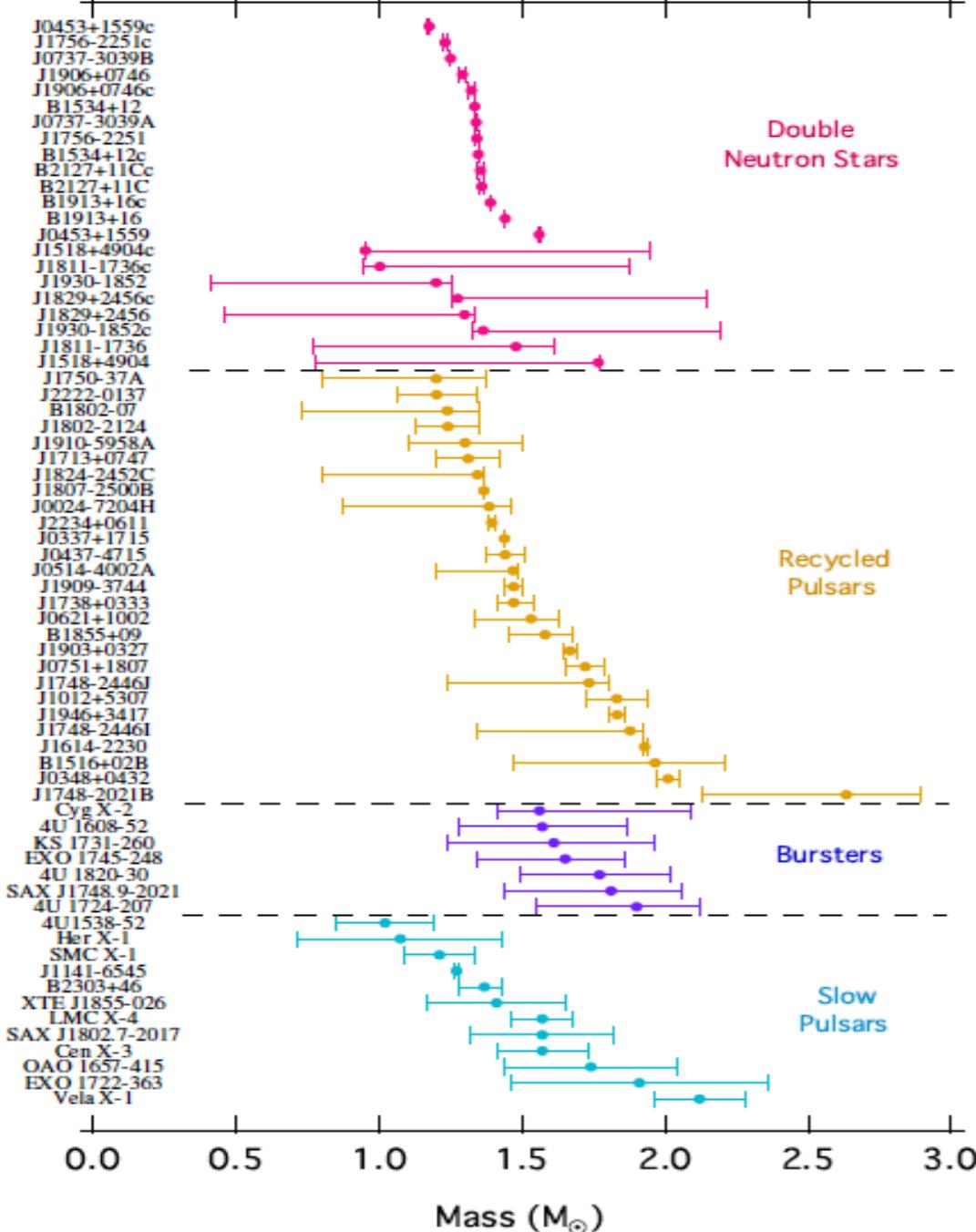


NS Equation of State



Özel & Freire, Ann. Rev. Astron. Astrophys 54, 401 (2017)

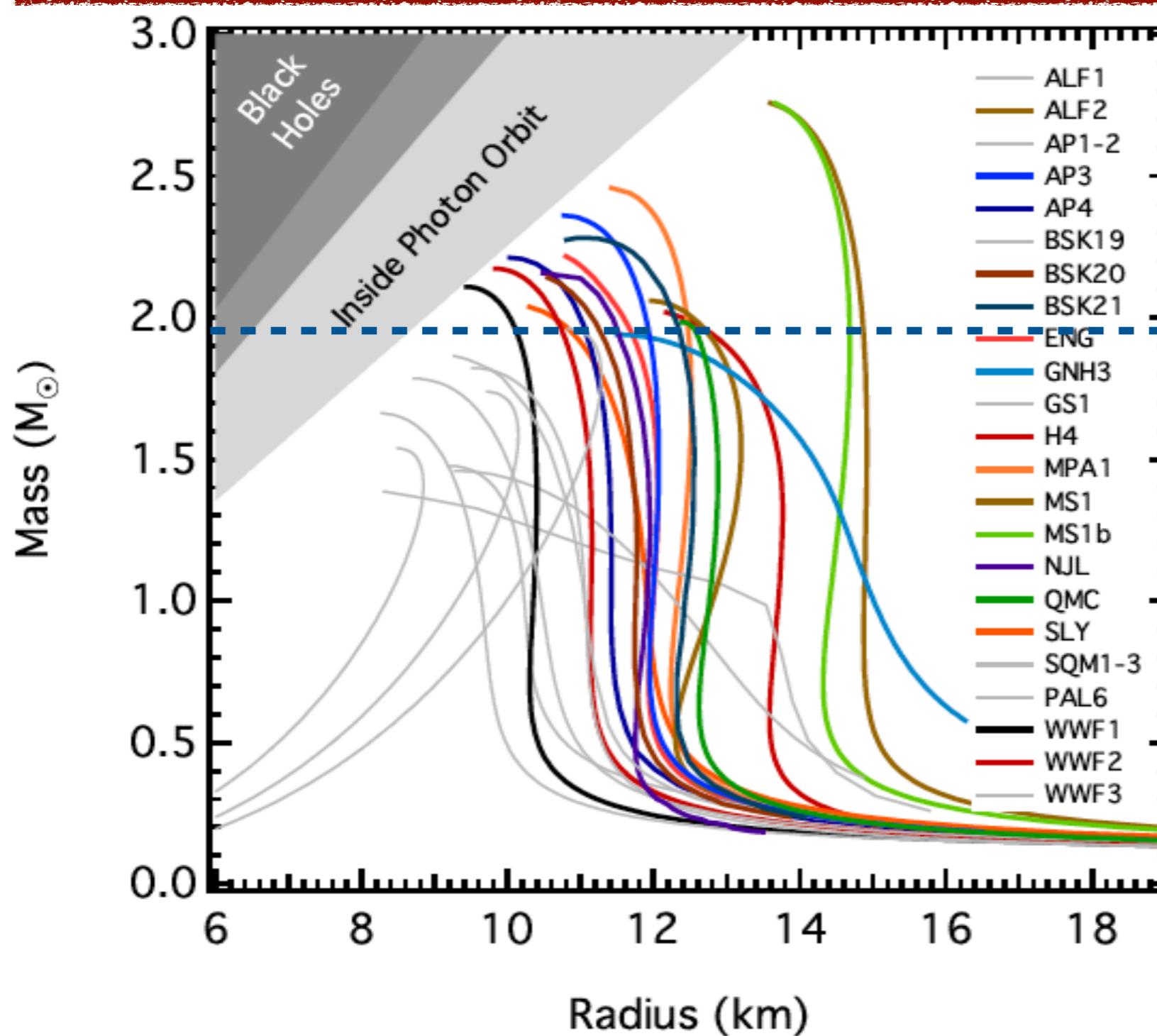
NS Equation of State



J0348+0432 : $2.01 \pm 0.04 M_{\odot}$

Özel & Freire, Ann.Rev.Astron.Astrophys 54, 401 (2017)

NS Equation of State



J0348+0432 (MSP-WD)



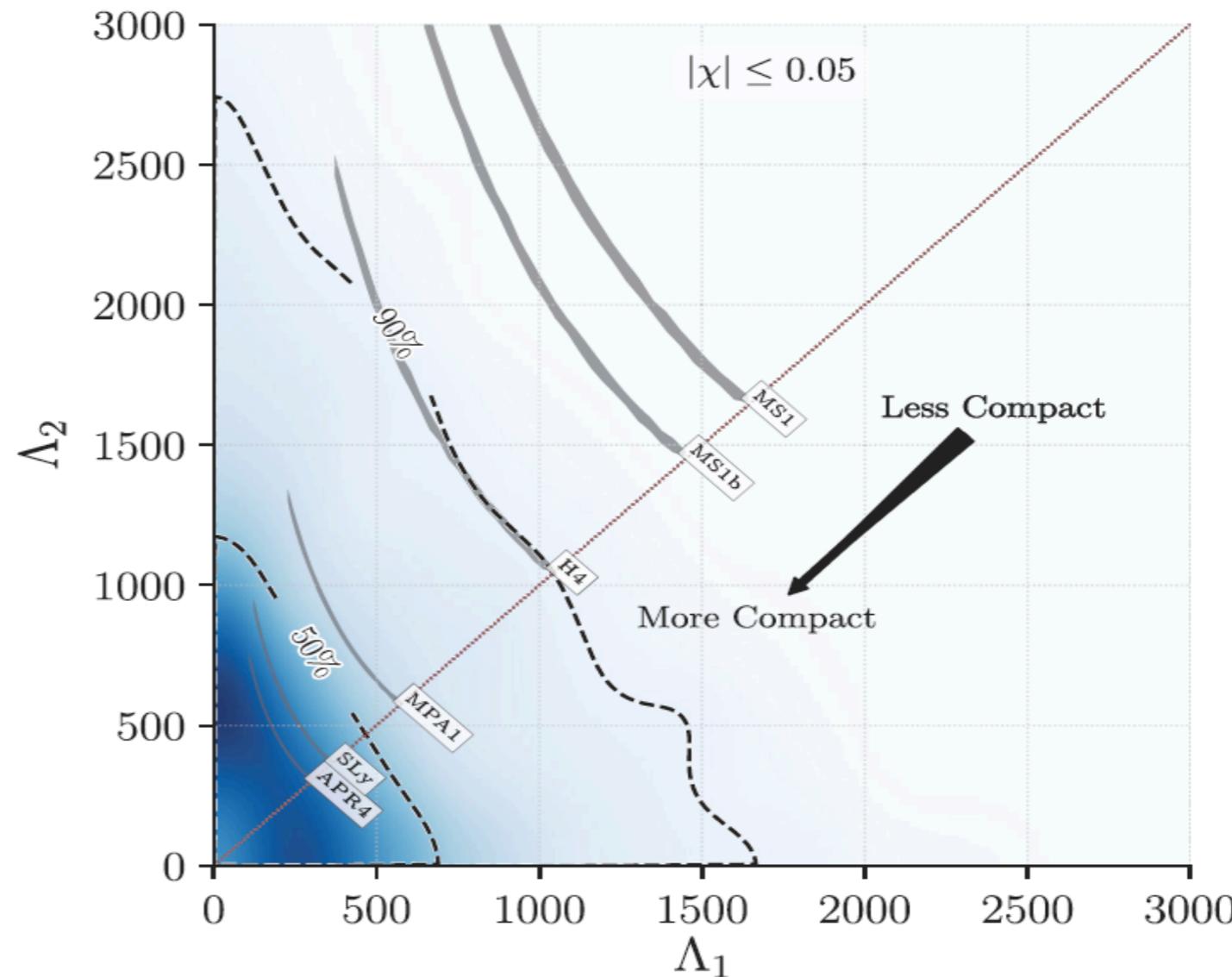
NS Equation of State

$30 \leq f/\text{Hz} \leq 2048$

$m_1 \in (1.36, 1.6) M_\odot$

$m_2 \in (1.17, 1.36) M_\odot$

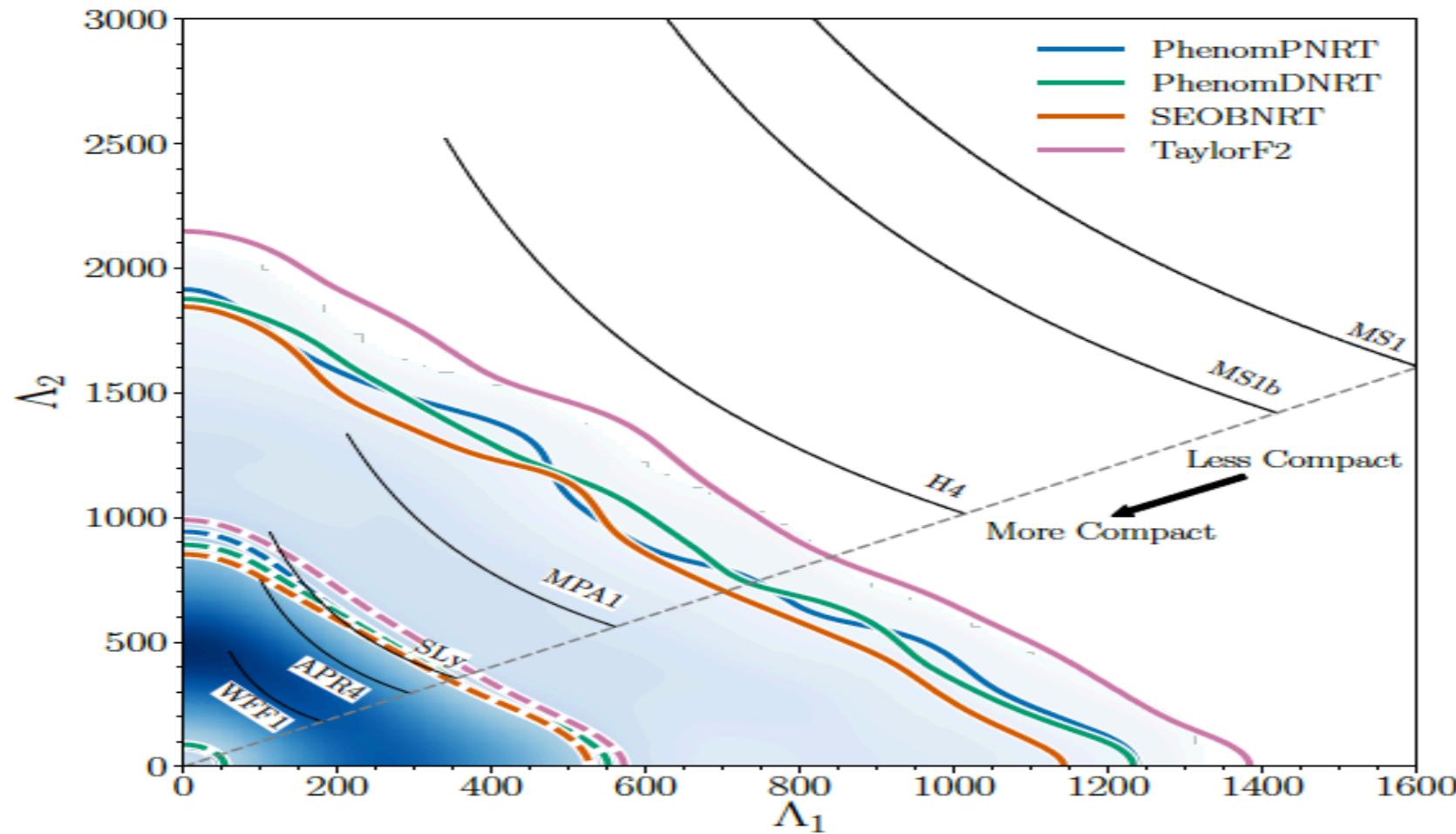
$\tilde{\Lambda}_{1.4} \leq 900$



Assume low spins - consistent with NS observations

Abbott et al, PRL 119, 161101 (2017)

NS Equation of State



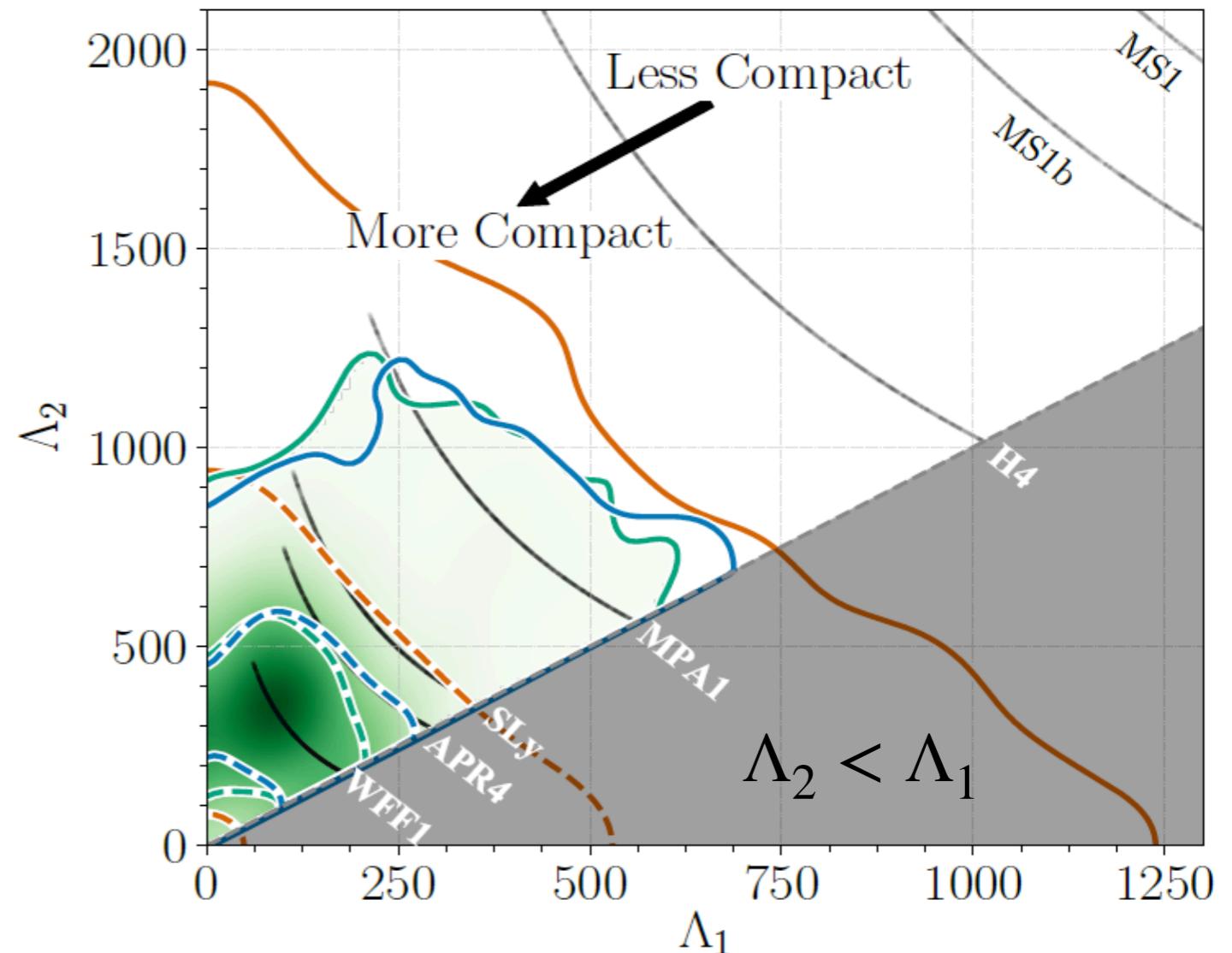
- New analysis beginning at 23 Hz (~ 1500 extra cycles) with better modelling
- No assumption on binary components
- No assumptions on EOS - independent variation
- sky error reduced to 16 deg² (using sky position given by SSS17A/AT 2017 gfo)
- Bound on $\Lambda_1 - \Lambda_2$ is 20% smaller

Abbott et al, arXiv:1805.11579 (2018)



NS Equation of State

- Assume 2 NSs with identical EOS
- 2 EOS methodologies
 - EOS-insensitive :
 - $\Lambda_a(\Lambda_s, q)$
 - $\Lambda - C$
 - Parameterised EOS (no max mass)
 - Spectral parameterisation*
 - Original detection results
- 90% CI for $\Lambda_1 - \Lambda_2$ shrinks by ~ 3

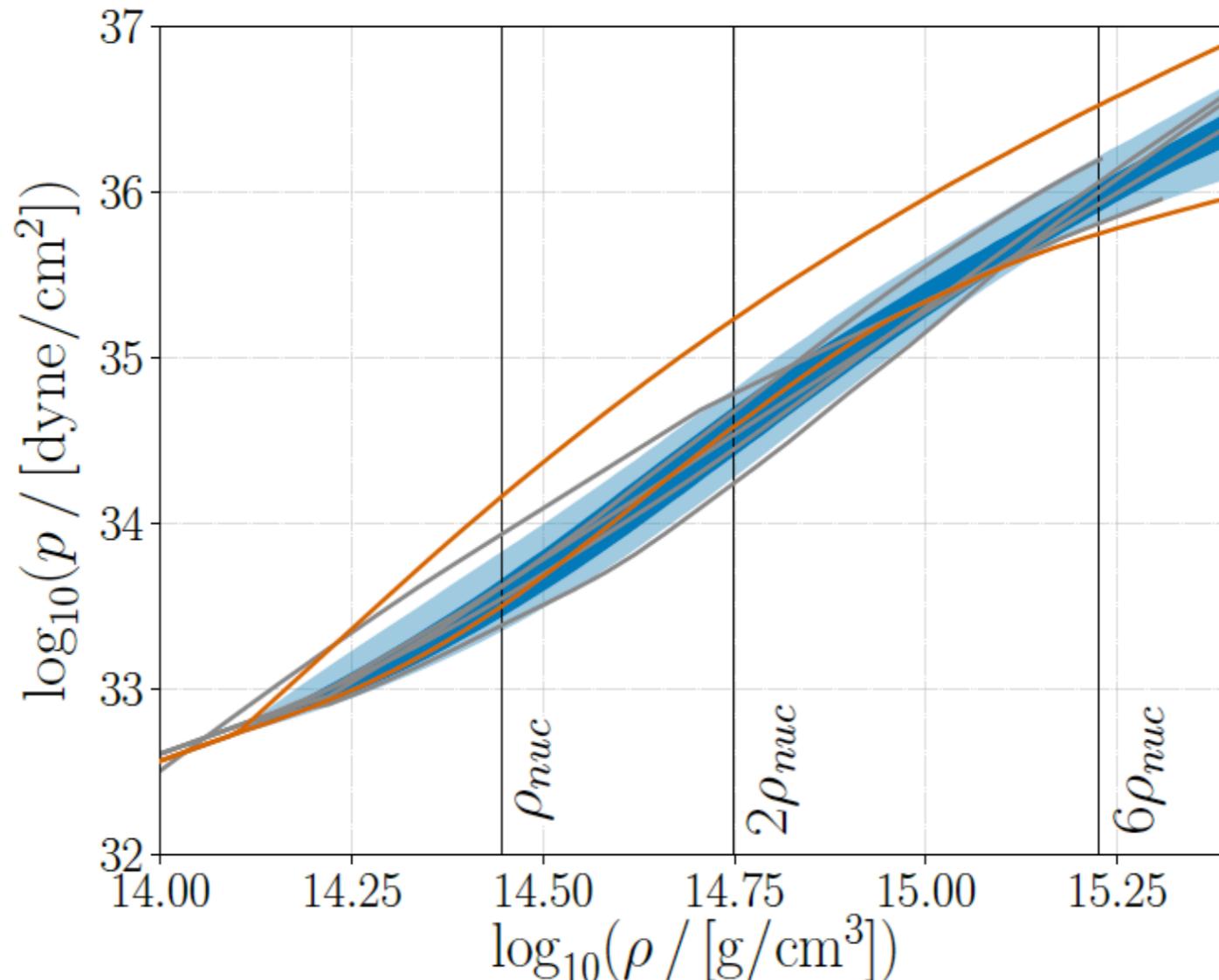


$$\Lambda_{1.4} = 190^{+390}_{-120}$$

Abbott et al, arXiv:1805.11581 (2018)

NS Equation of State

Now assume spectral parameterisation + maximum NS mass = $1.97 M_{\odot}$



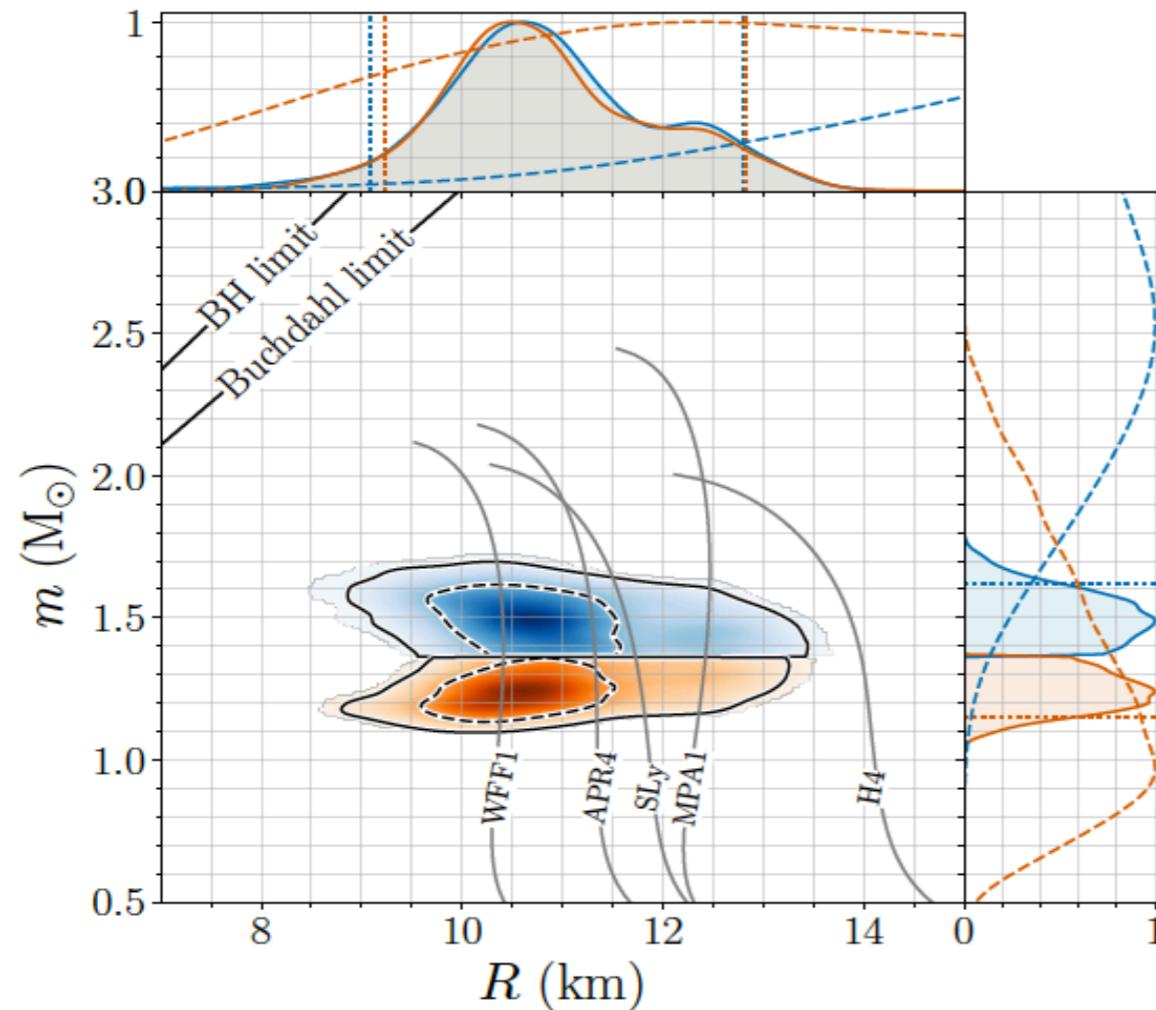
$$p(2\rho_{nuc}) = 3.5^{+2.5}_{-1.7} \times 10^{34} \text{ dyne cm}^{-2}$$

Abbott et al, arXiv:1805.11581 (2018)



NS Equation of State

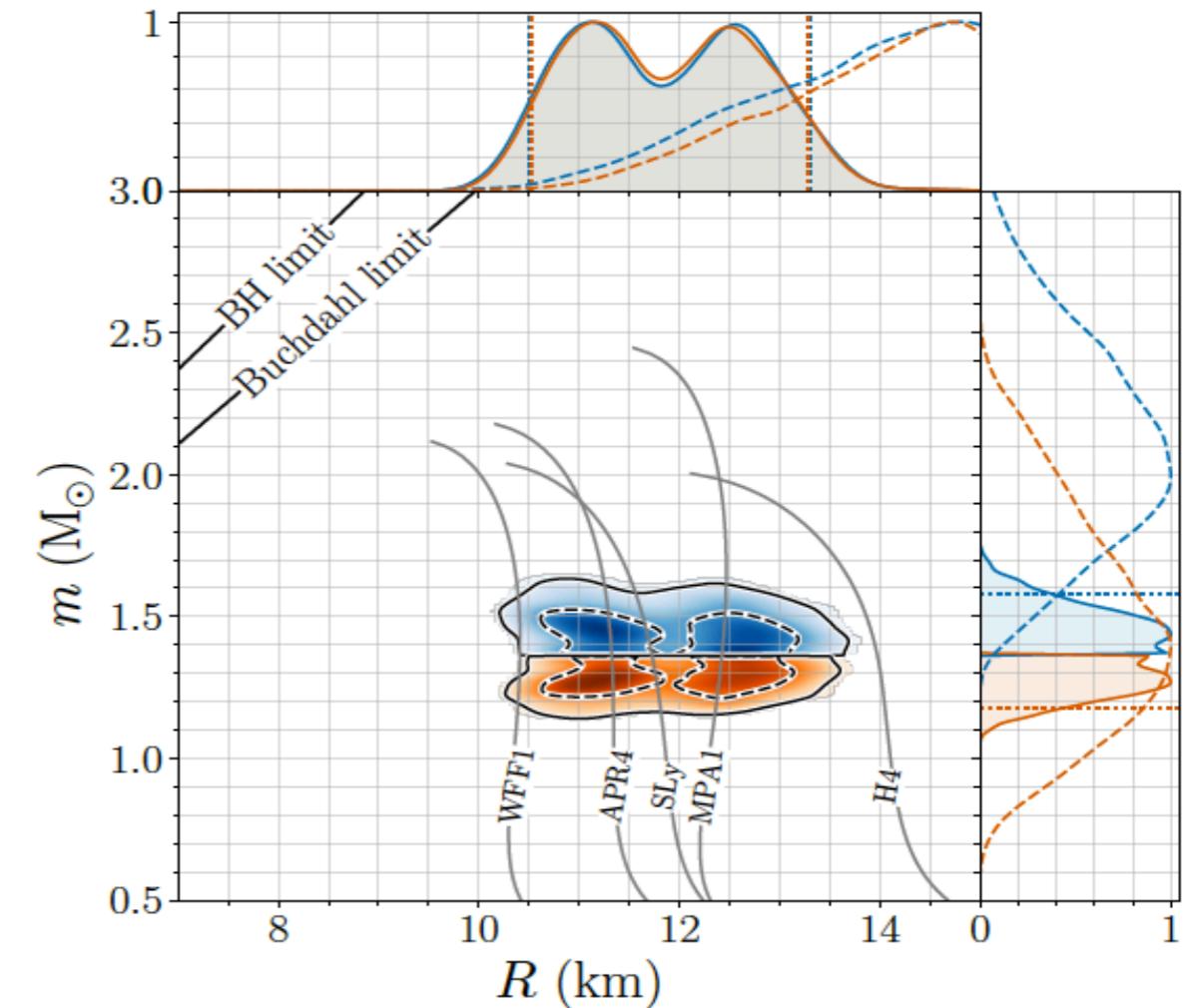
**EOS-ins
(GW only)**



$$R_1 = 10.8^{+2.0}_{-1.7} \text{ km}$$

$$R_2 = 10.7^{+2.1}_{-1.5} \text{ km}$$

**Spec.Param + max. NS mass
(GW + EM)**



$$R_1 = 11.9^{+1.4}_{-1.4} \text{ km}$$

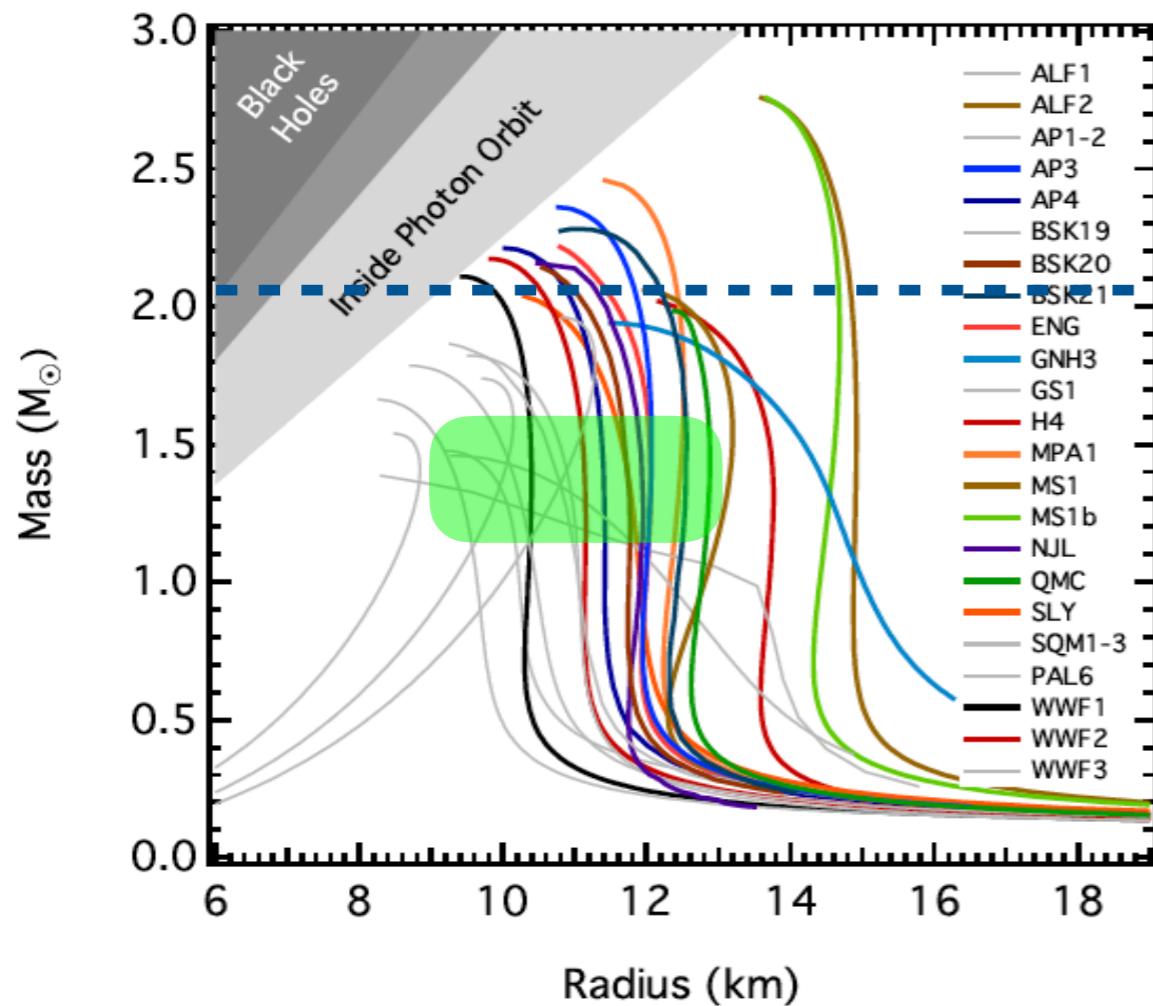
$$R_2 = 11.9^{+1.4}_{-1.4} \text{ km}$$

Abbott et al, arXiv:1805.11581 (2018)

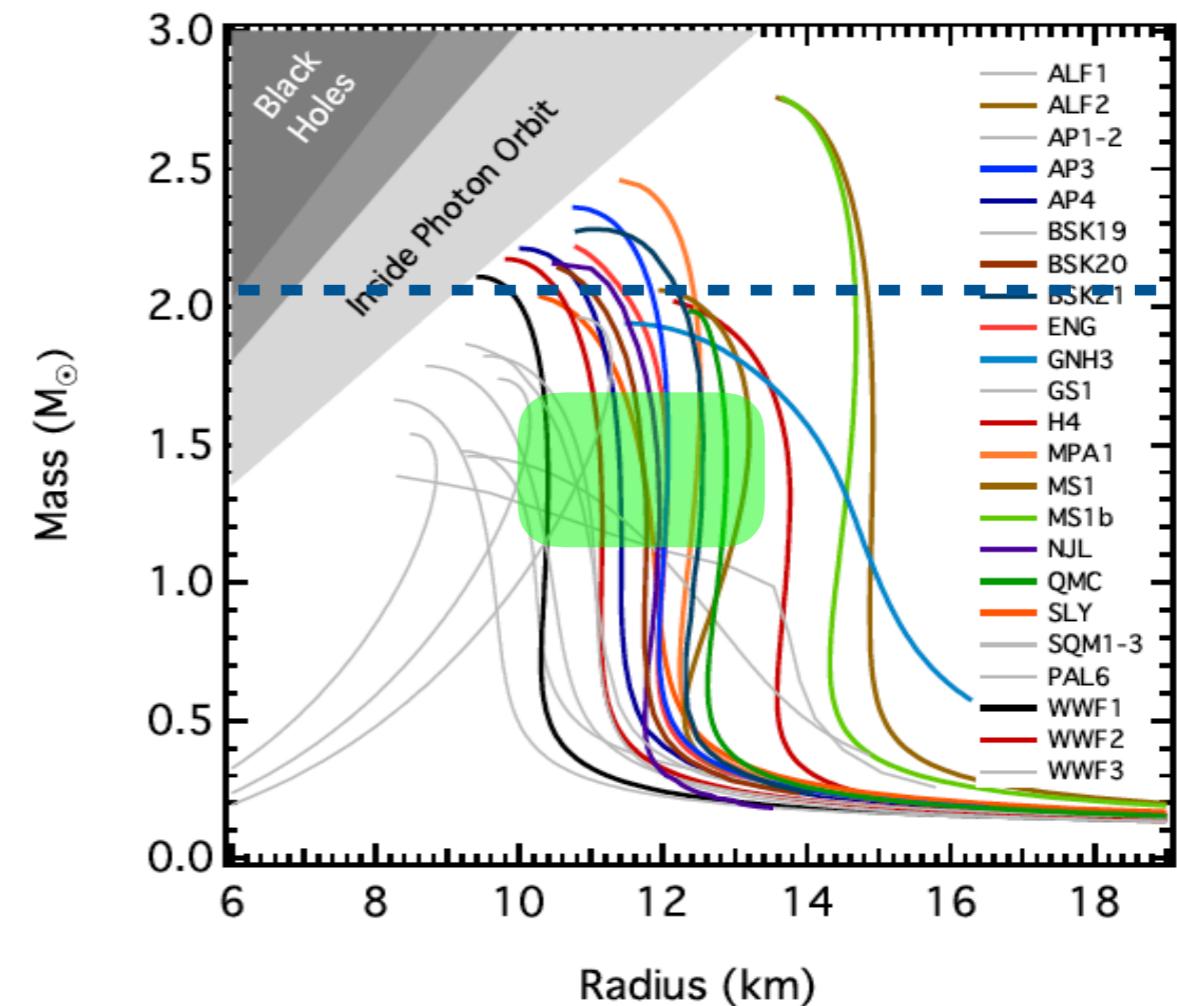


NS Equation of State

EOS-ins



Spec.Param + min. NS mass



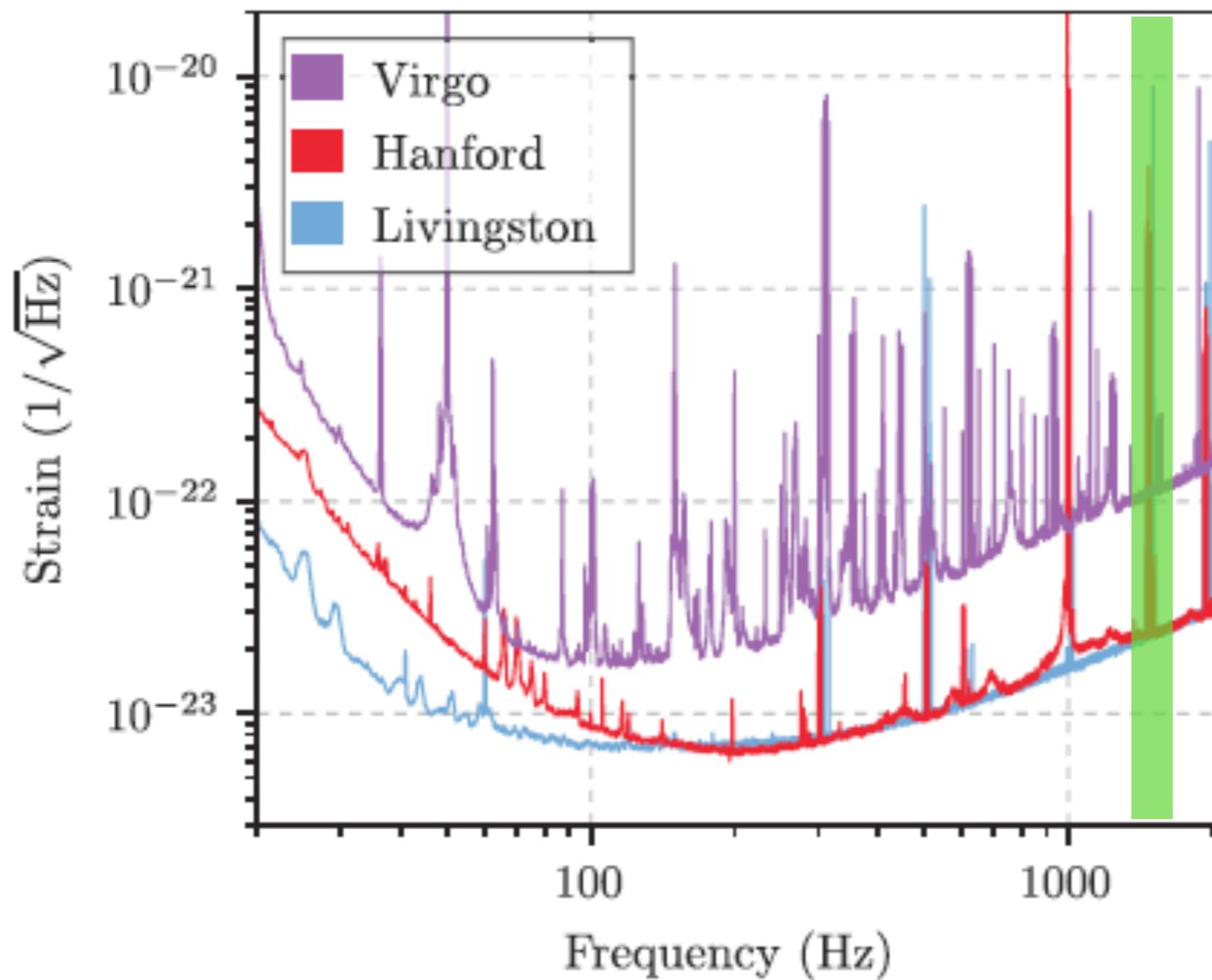
GW + EM gives much tighter constraint



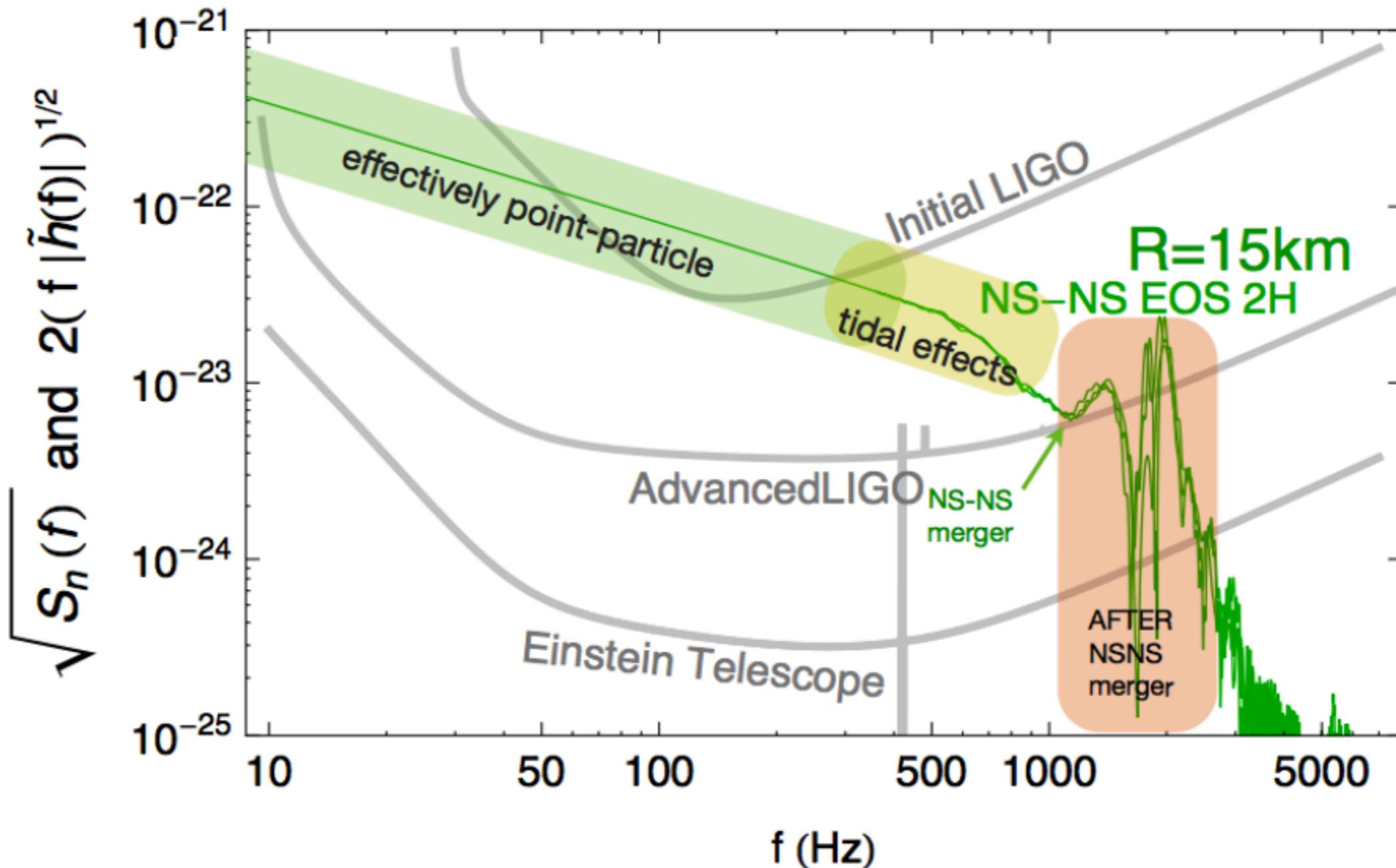
Post-merger remnant

Q: So what is the remnant of the merger?

A: From GWs - we don't know. High frequency signal dominated by photon shot noise



Post-merger remnant



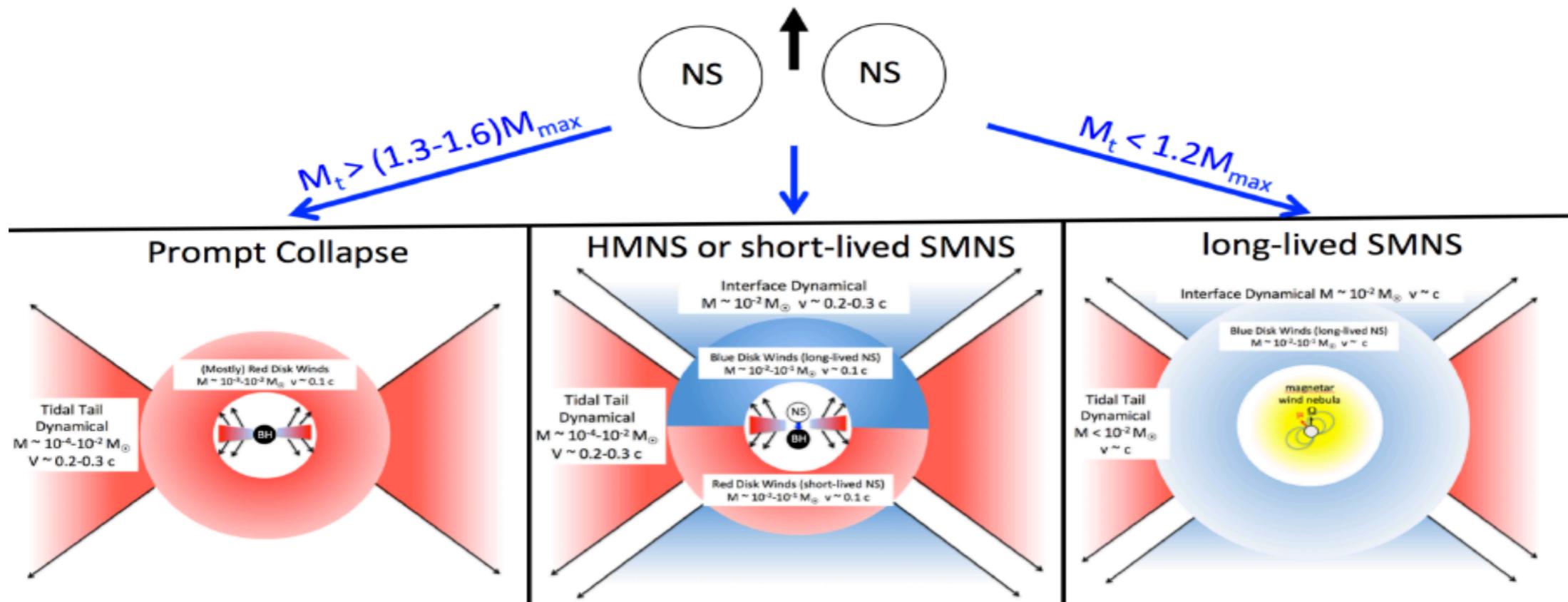
S. Usman et al (2018)



NS Equation of State

Q: So what is the remnant of the merger?

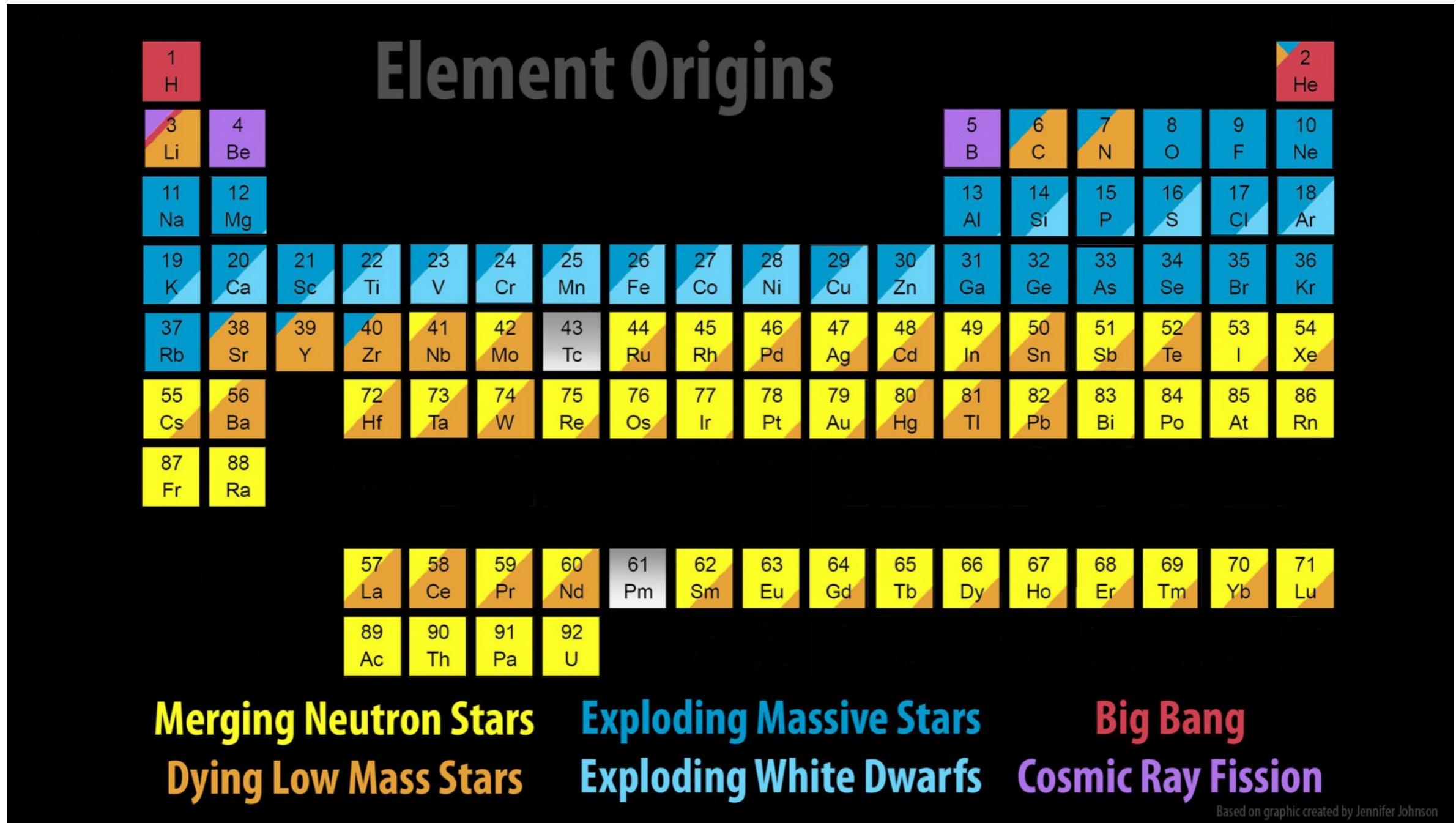
A: From EM - unclear! Some people believe prompt collapse to BH, others believe in the formation of a transient hypermassive NS



Margalit et al (2017)



Extreme Matter

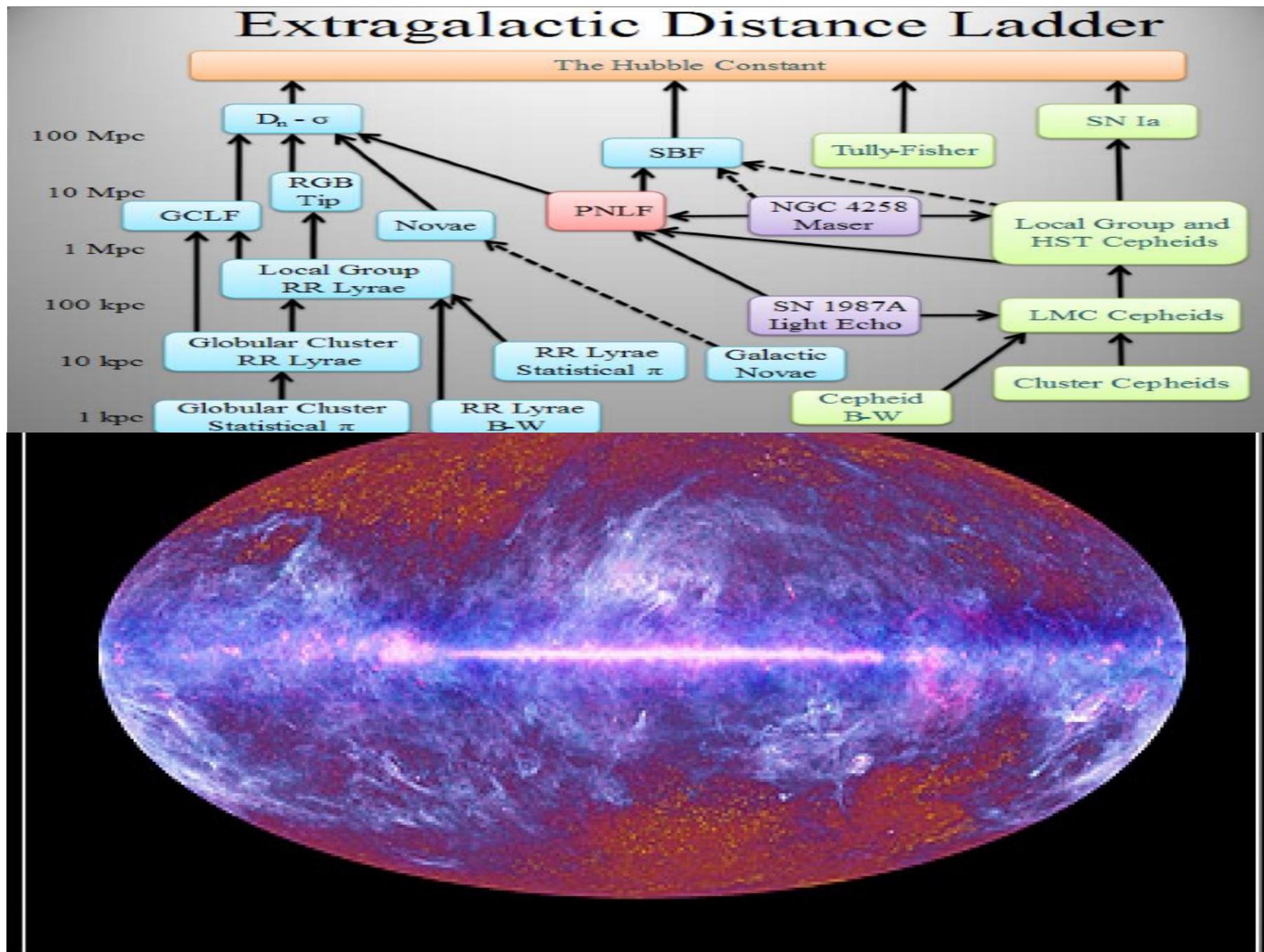


Credit: Jennifer Johnson/SDSS

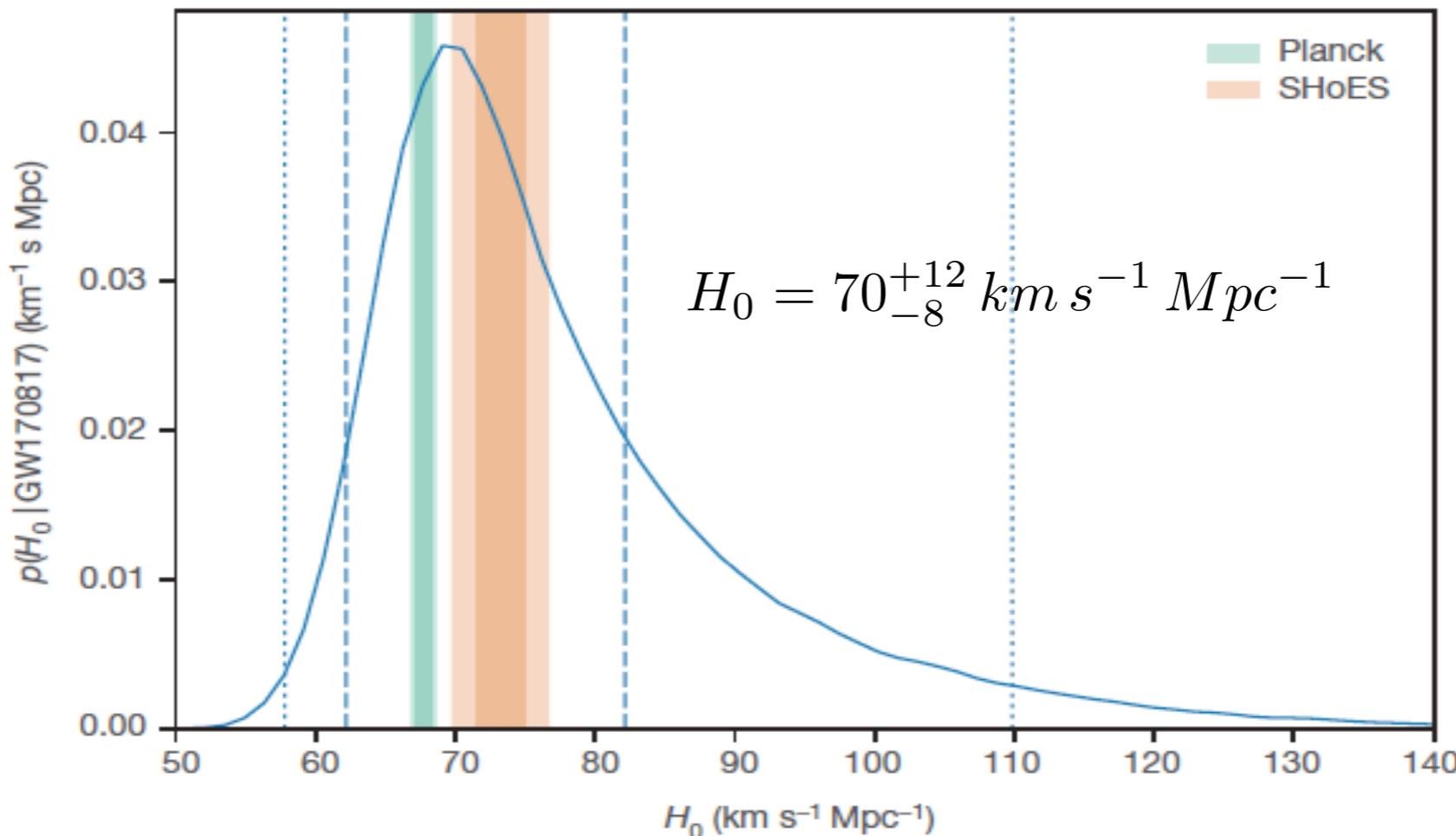


Cosmology

Astrophysics
Cosmology



Cosmology



- ➊ N.B. No cosmic distance ladder needed!!
- ➋ GW astronomy measures luminosity distance directly over cosmic scales

Abbott et al, Nature (2017)

Conclusion

- Thank you for your attention

