

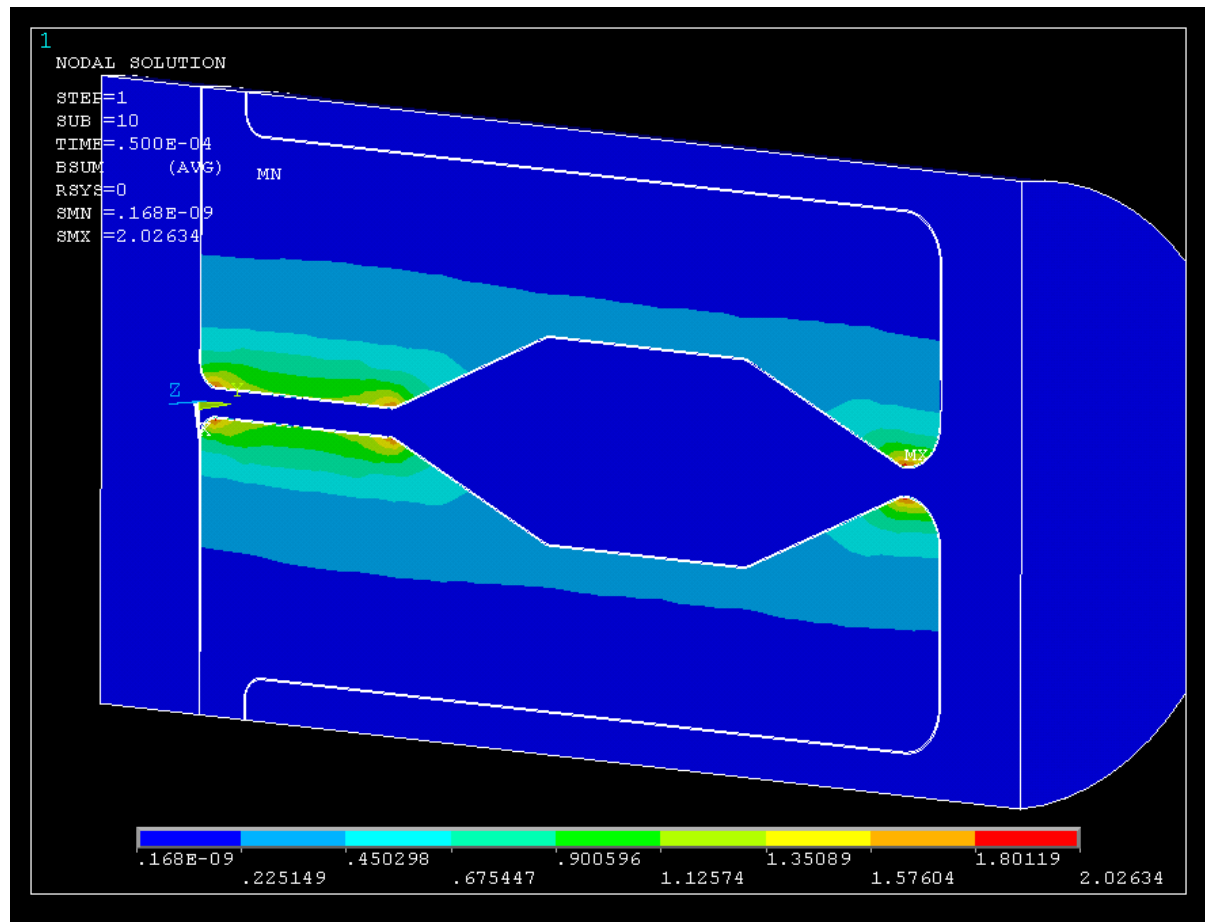
# Summary of WP4: simulation results for the horn and the target spheres

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AGH University of Science and Technology  
Krakow, Poland

Strasbourg, 08.11.2018

# Magnetic analysis

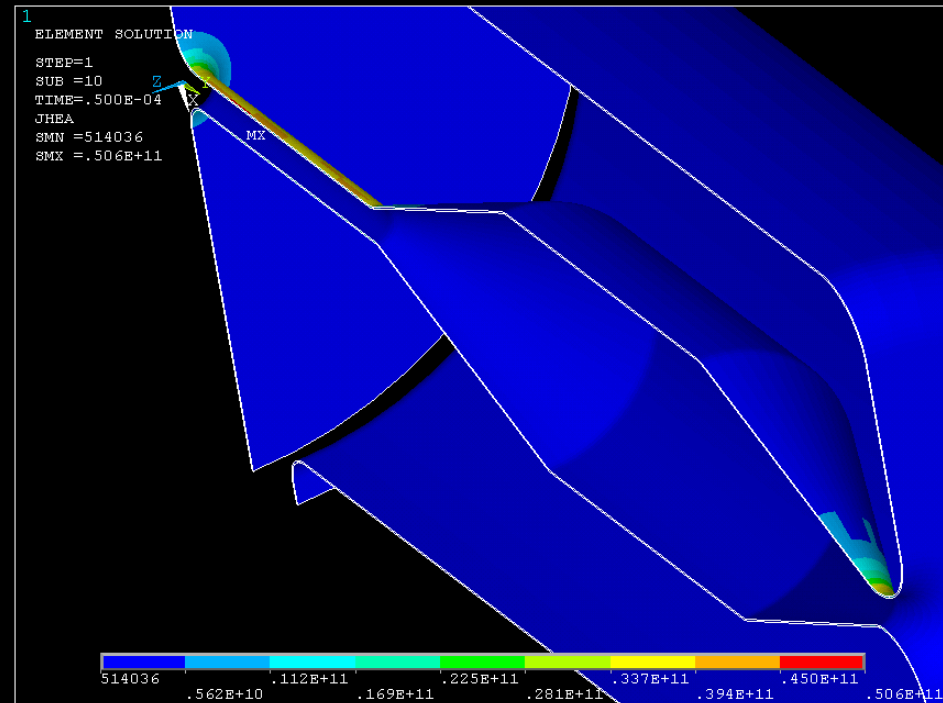
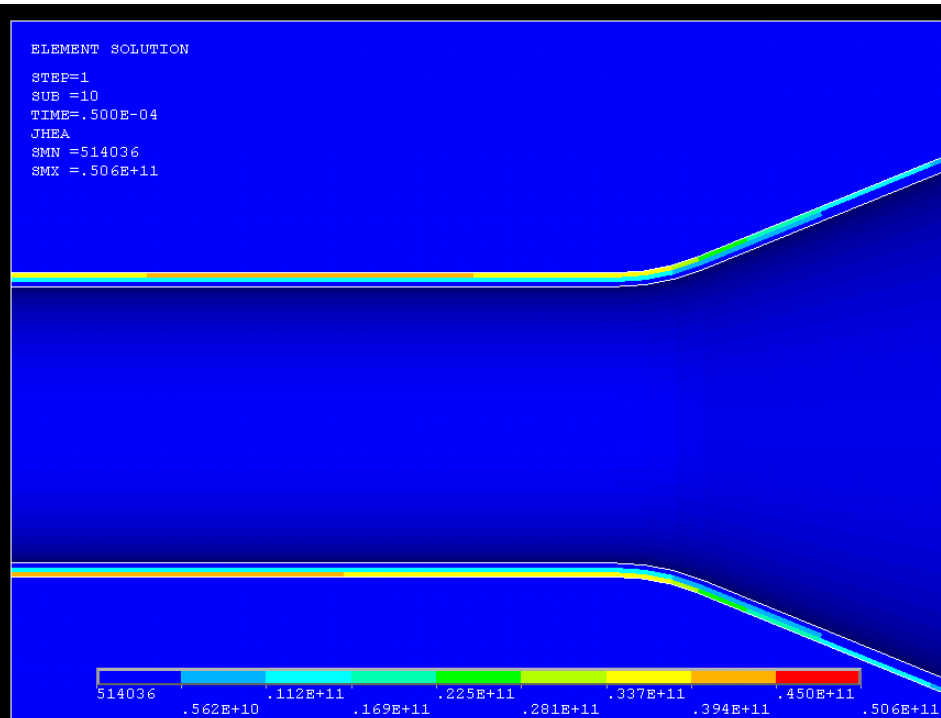
Magnetic flux  $B$  at  $t = 50\mu\text{s}$



# Magnetic analysis

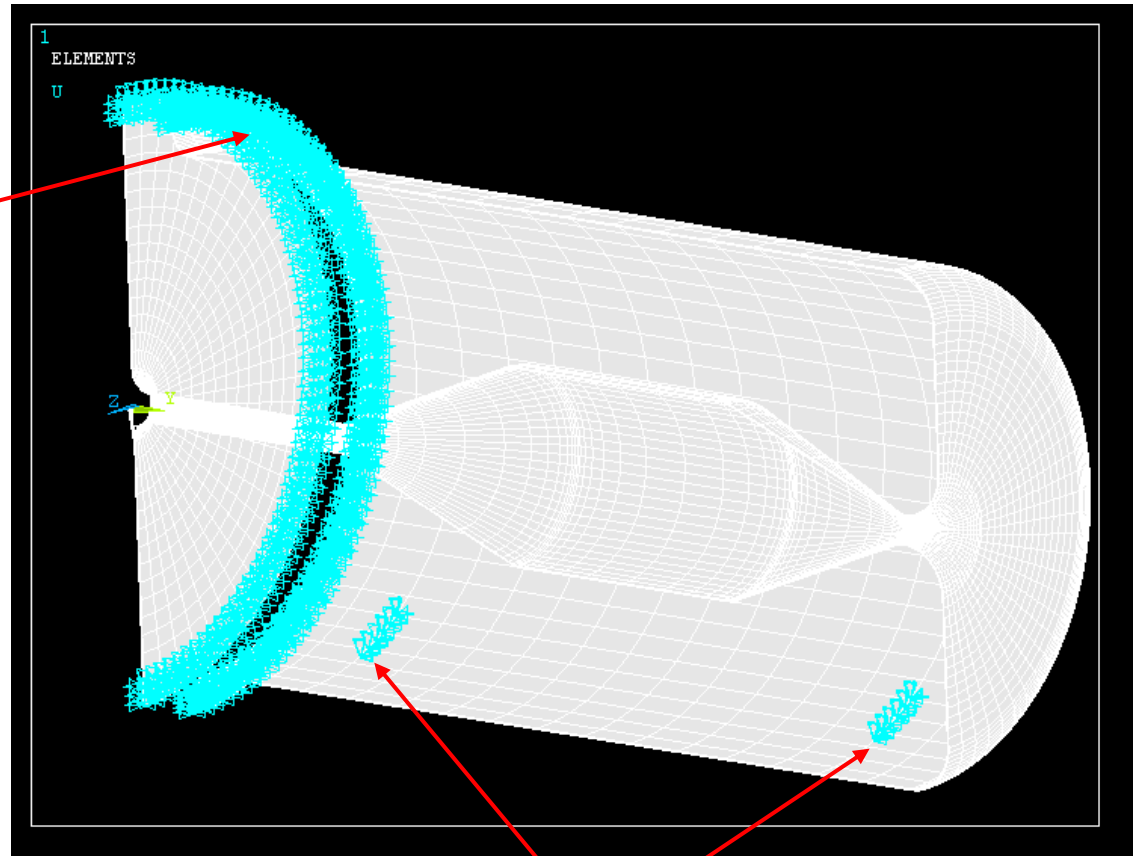
Joule heating at  $t = 50\mu\text{s}$

Skin effect



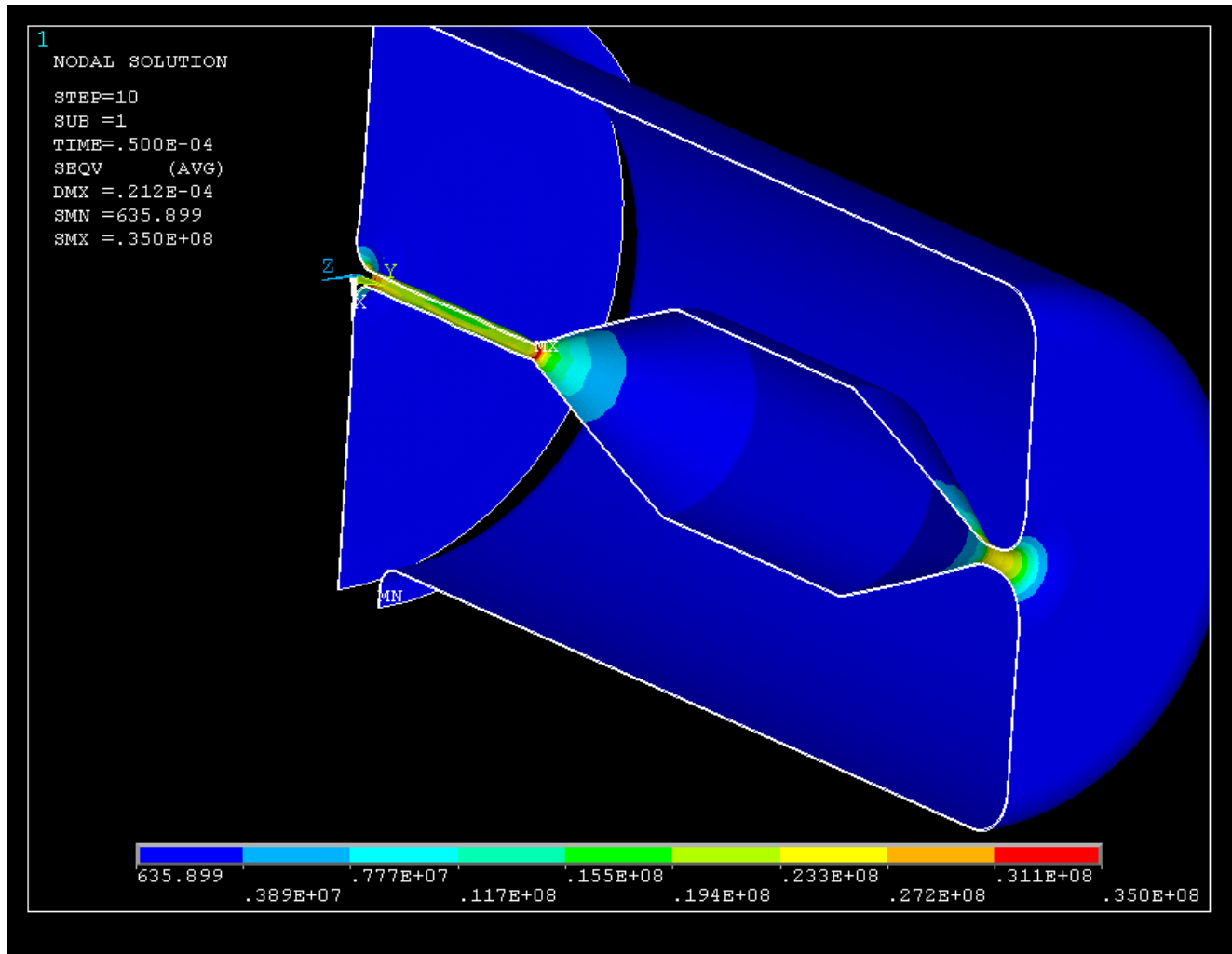
# Horn support in the structural analyses

fixed displacement in  
all directions



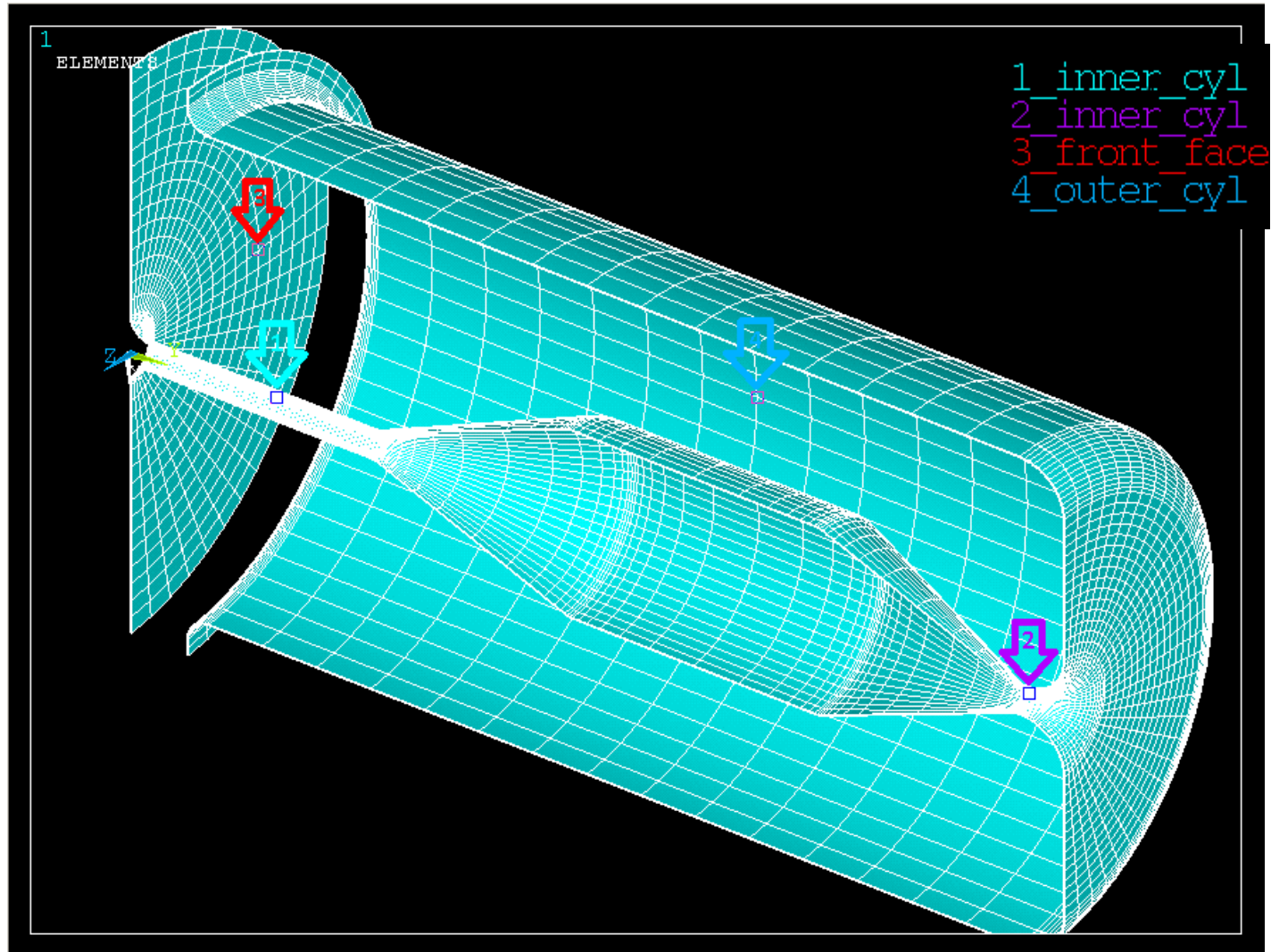
lateral displacements fixed

# von Mises stress



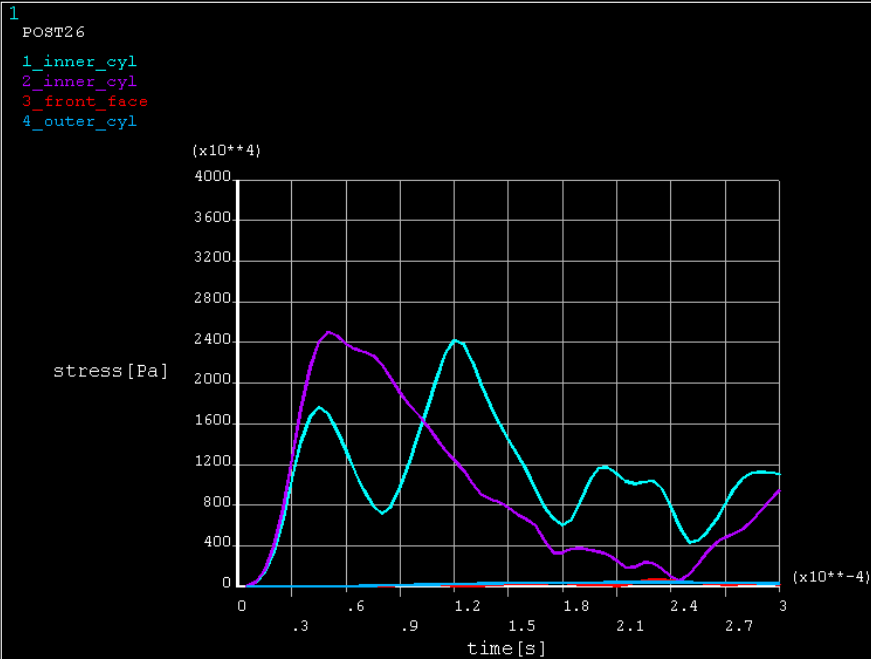
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# Results - location of the points

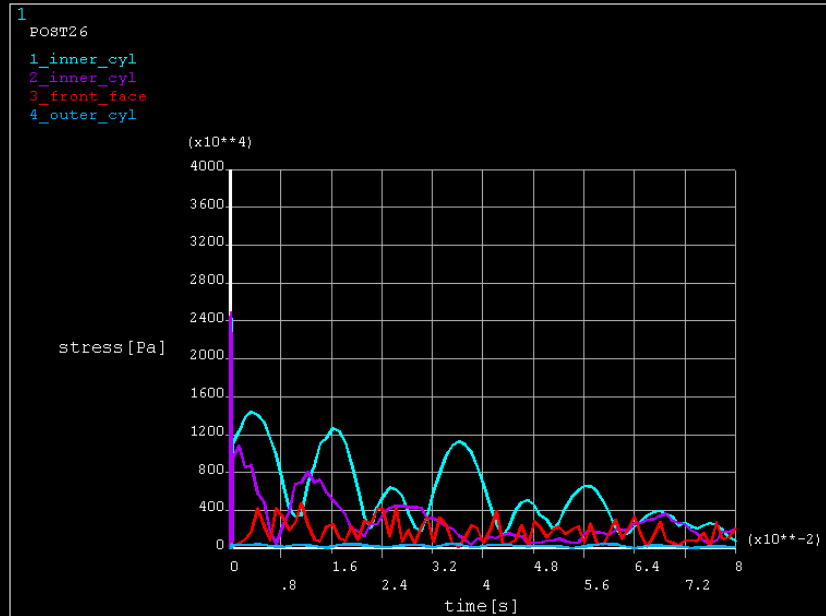


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# von Mises stress vs. time

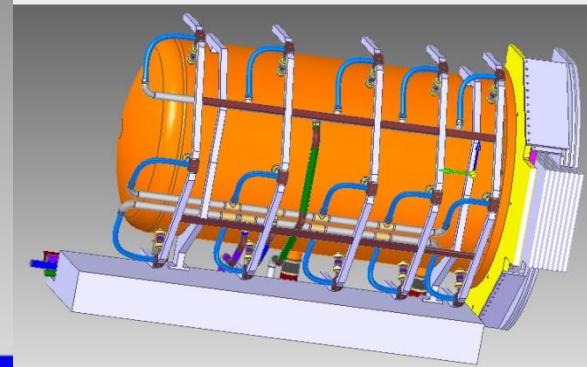
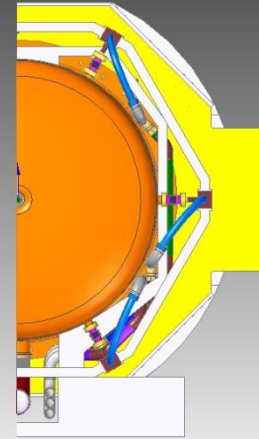
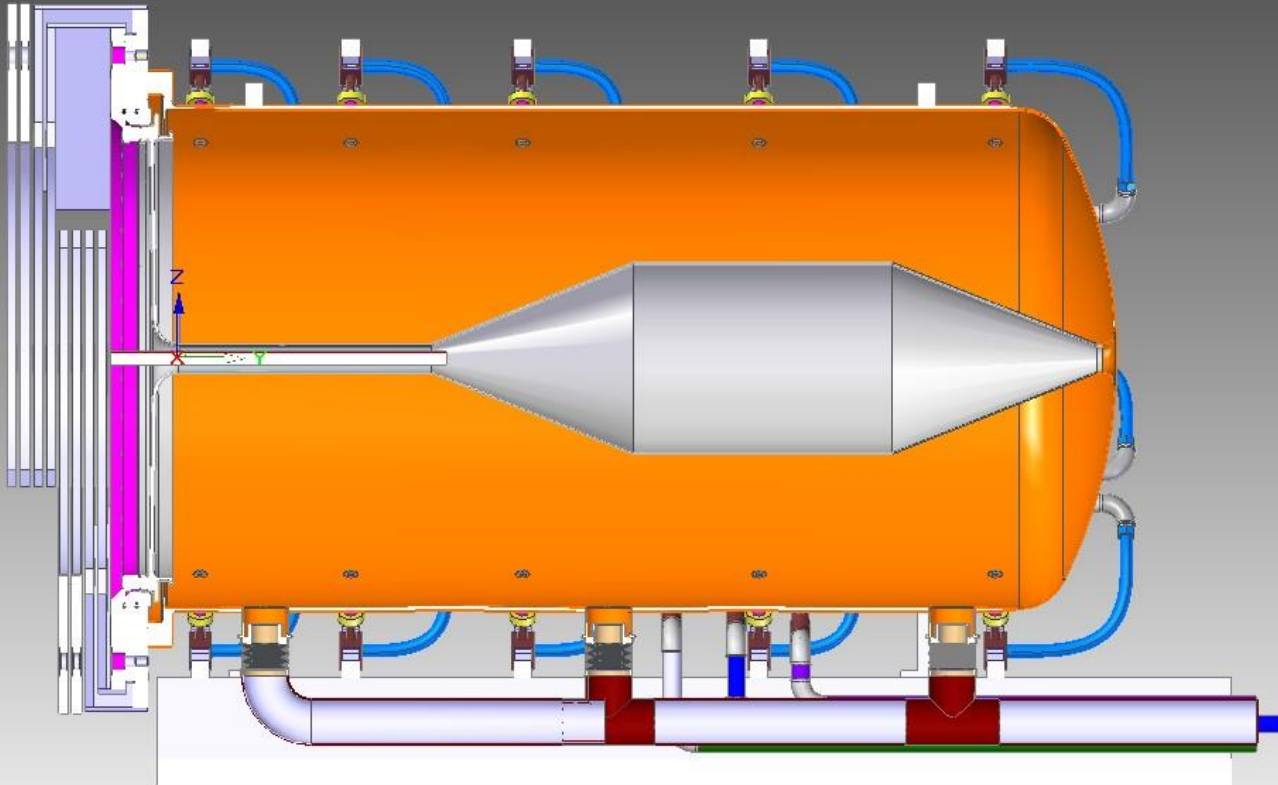


Nodal von Mises stresses 0 - 300us



Nodal von Mises stresses 0 - 0.08s

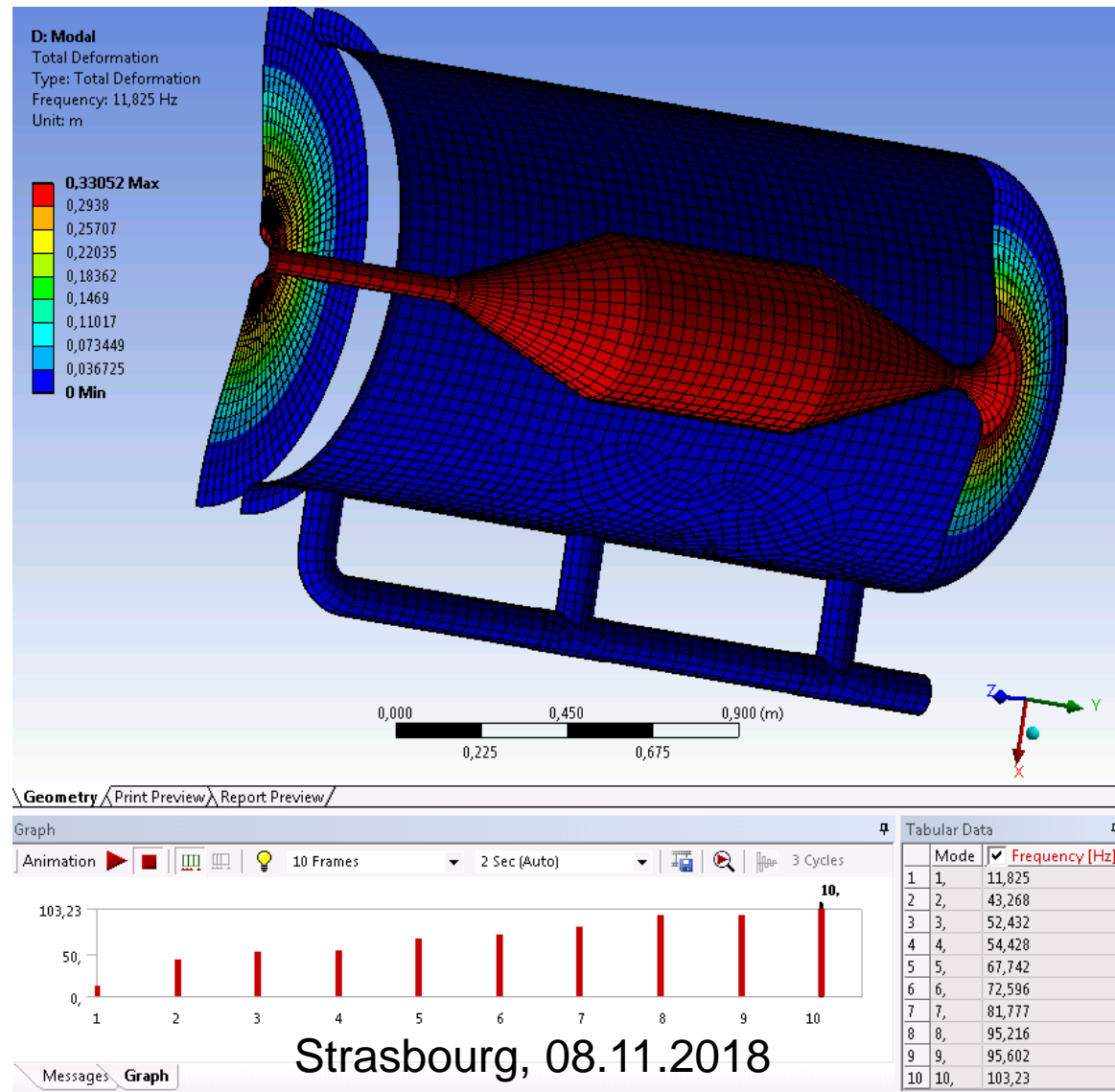
# Horn with auxiliary equipment – EUROnu geometry



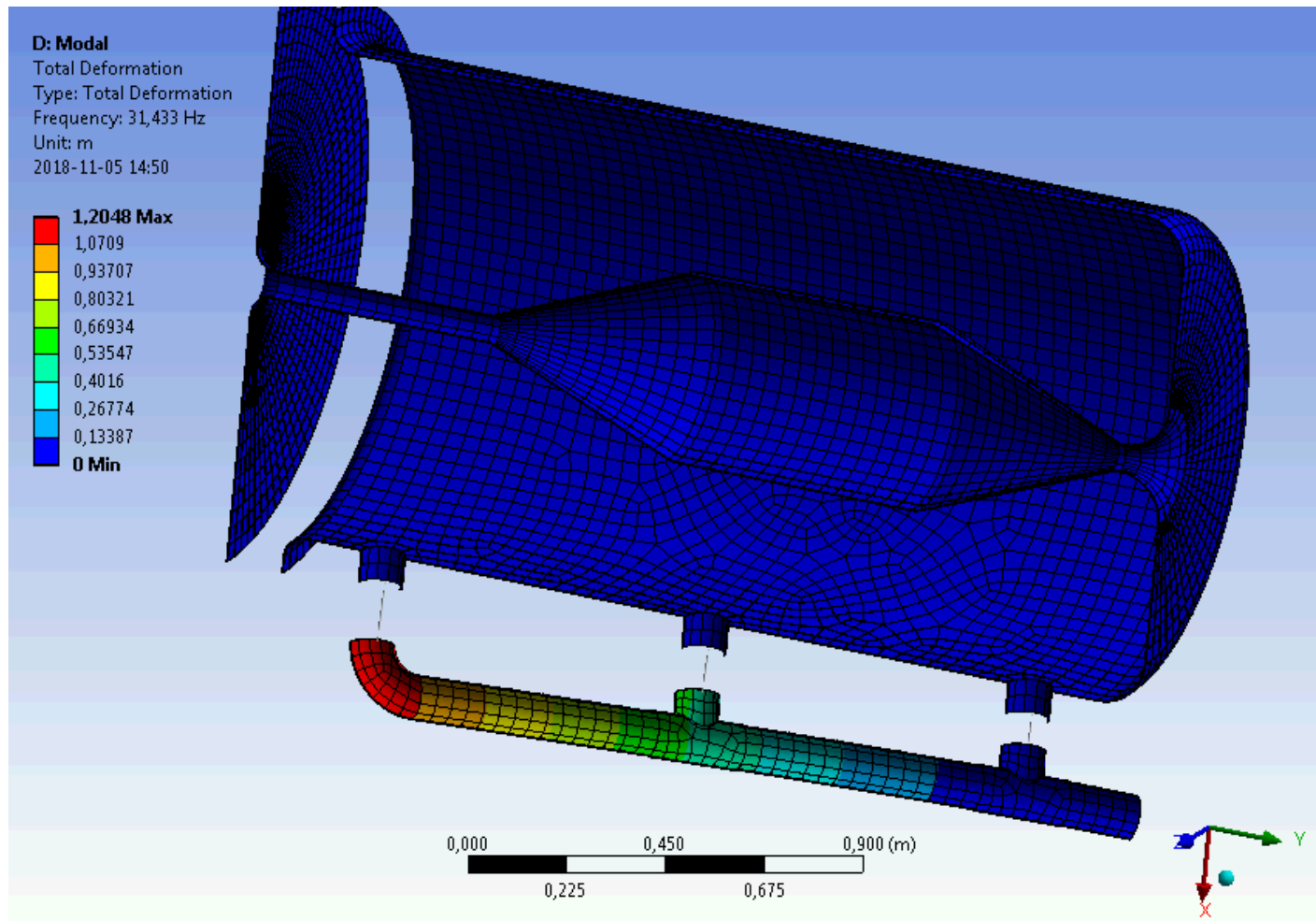
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# Horn with drainpipe

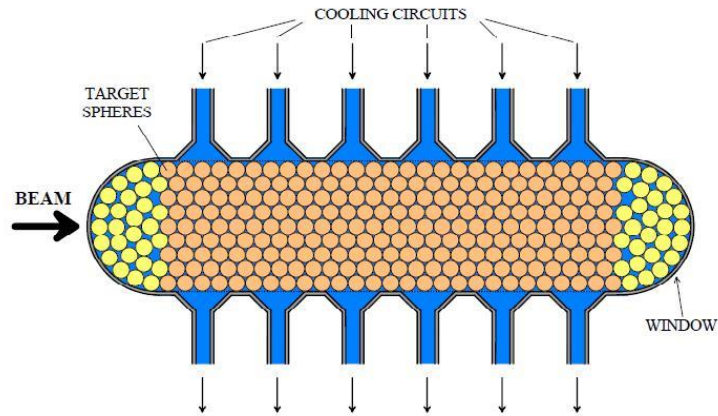


# Modal analysis

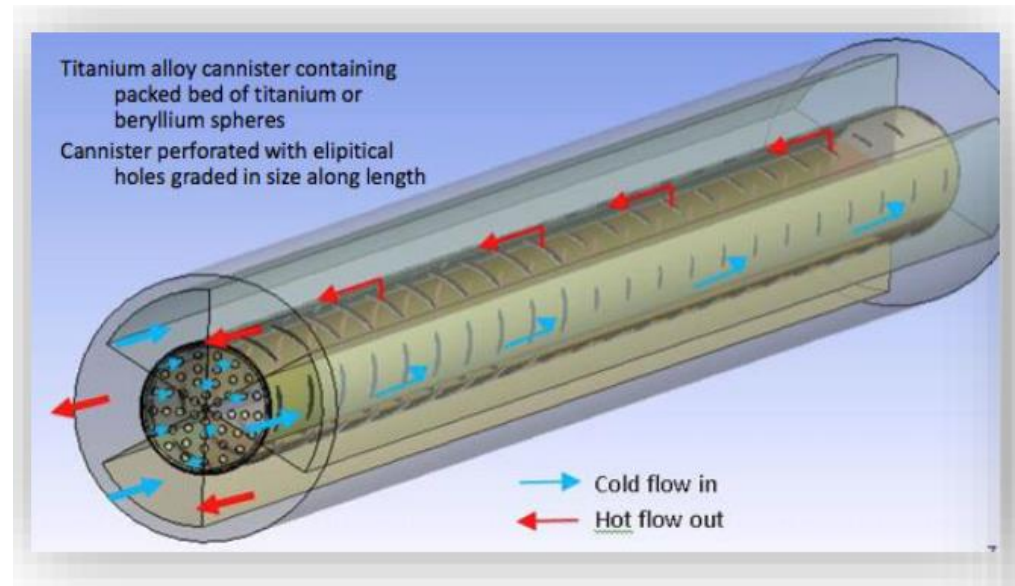


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# Motivation – granular (packed bed) target



Granular target proposed by P. Sievers at CERN (2001)



The pebble bed target studied at RAL (T.Davenne)

# Transient temperature in a solid sphere

A sphere with radius  $a=1$  mm is considered, with the following material properties (aluminium for test purposes, to be replaced by the constants of titanium):

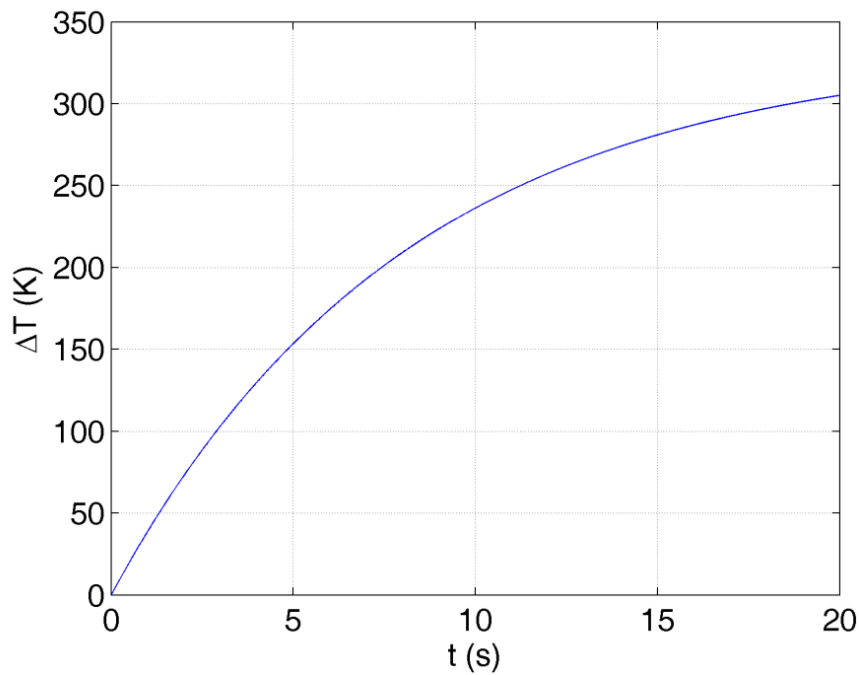
$K = 220$  W/mK      thermal conductivity

$c = 900$  J/kgK      specific heat

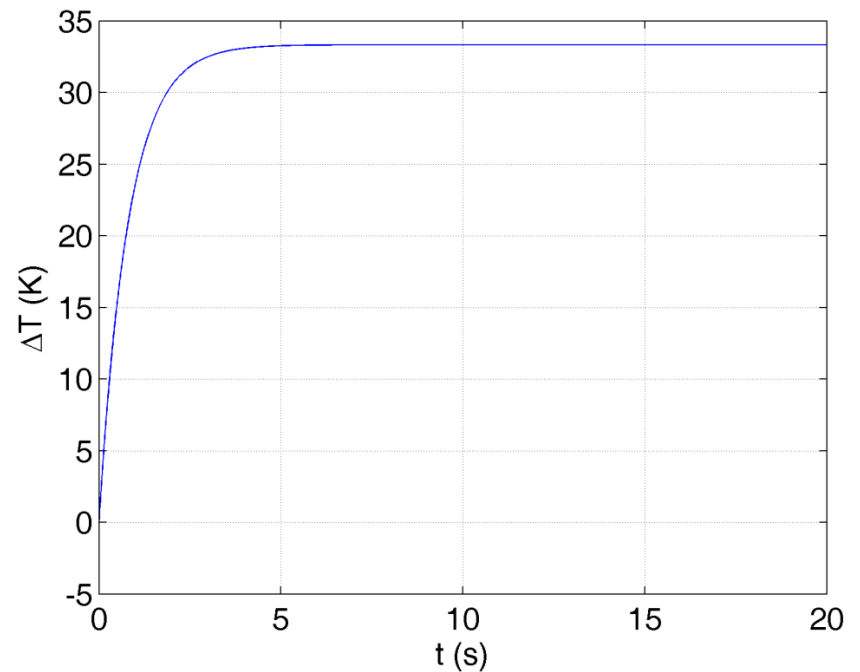
$\rho = 2.7 \cdot 10^3$  kg/m<sup>3</sup>      mass density

# Transient temperature in a solid sphere

Film coefficient  $H=100 \text{ W/m}^2\text{K}$

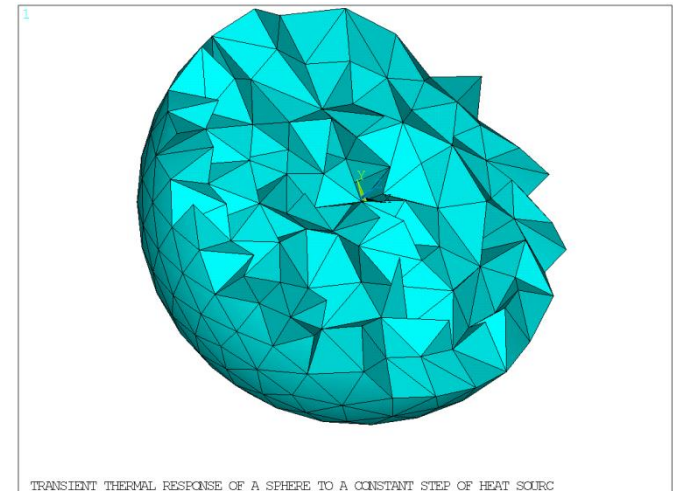
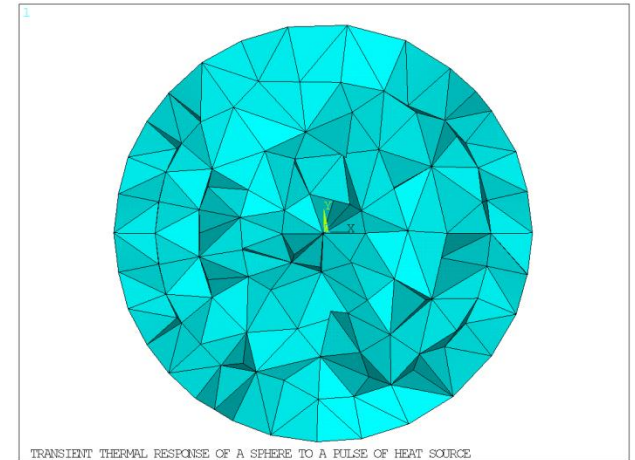
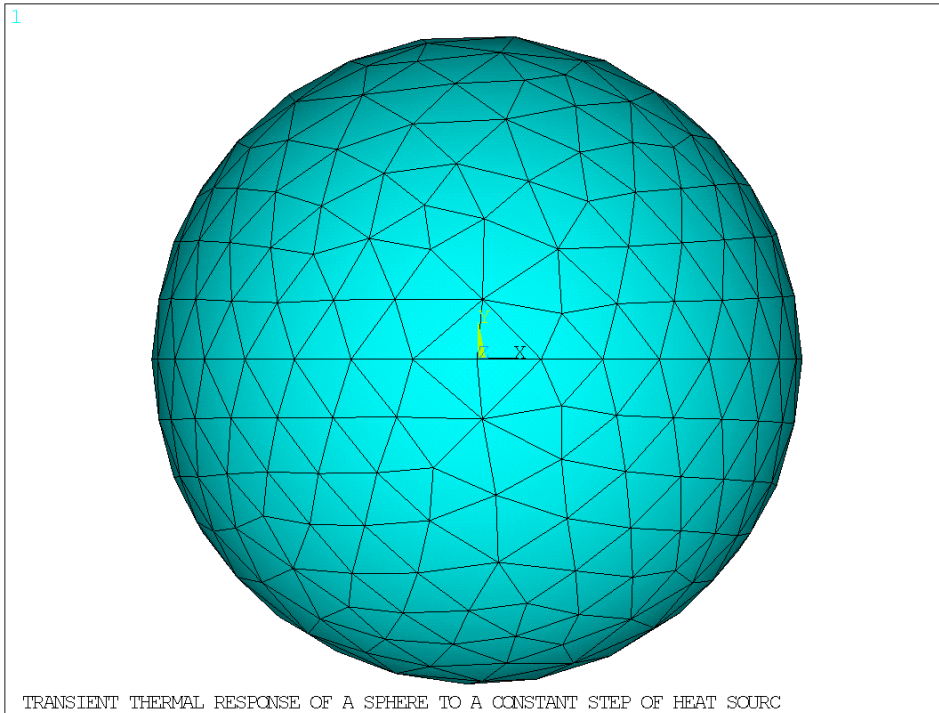


Film coefficient  $H=1000 \text{ W/m}^2\text{K}$



# Finite element model of a sphere

Free meshing with tetrahedral elements

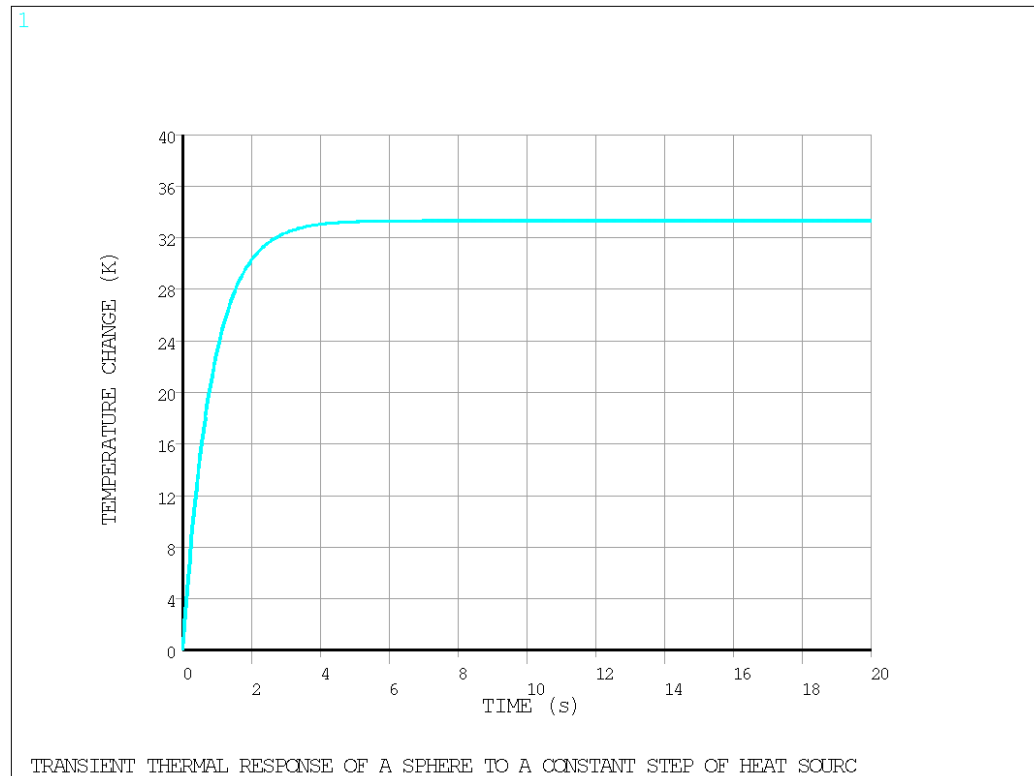
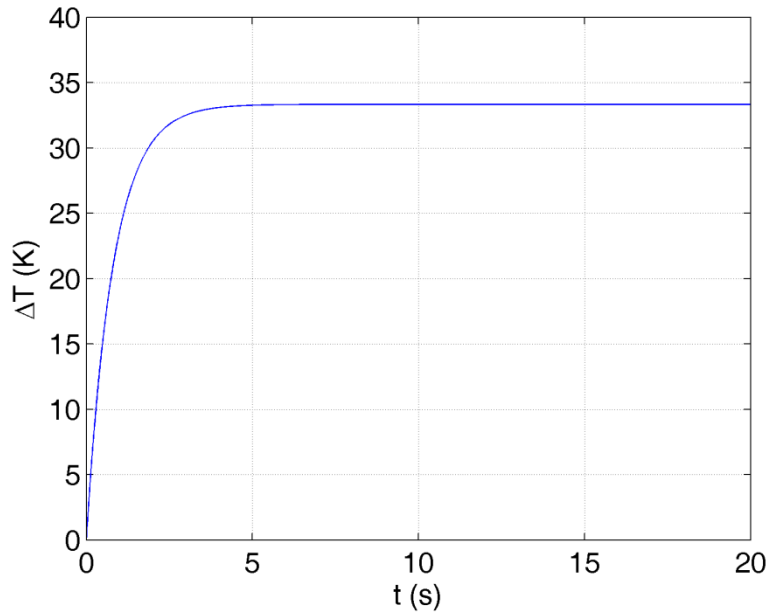


# Finite element vs. analytical solution

Film coefficient  $H=1000 \text{ W/m}^2\text{K}$

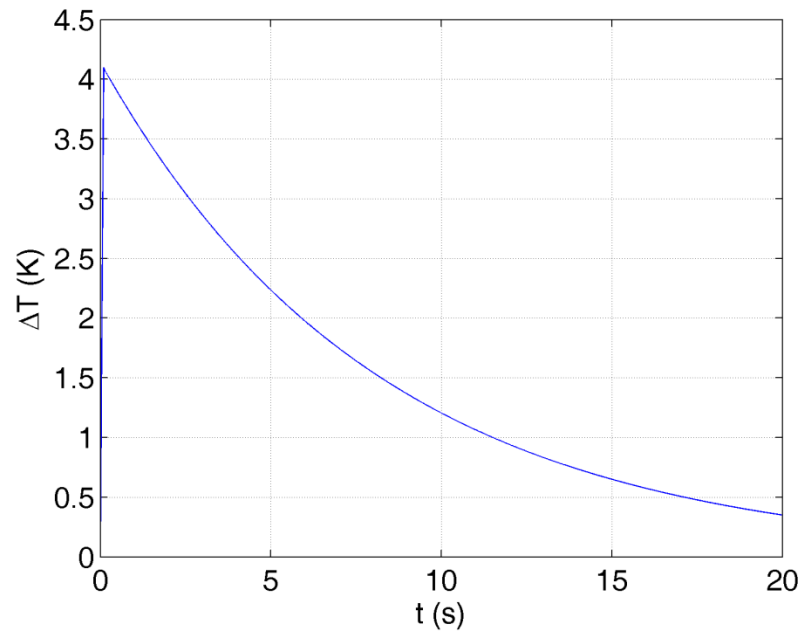
Ansys

Analytical

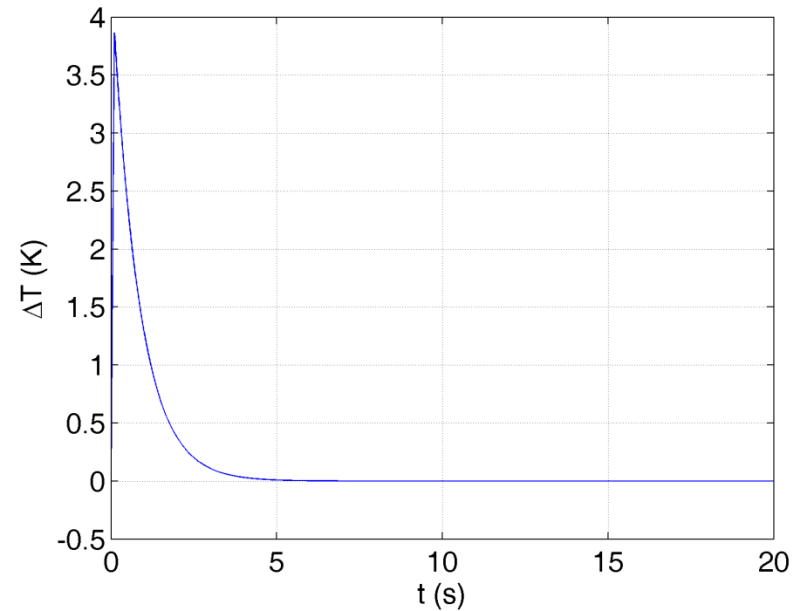


# Temperature in a sphere due to a heat pulse

Film coefficient  $H=100 \text{ W/m}^2\text{K}$

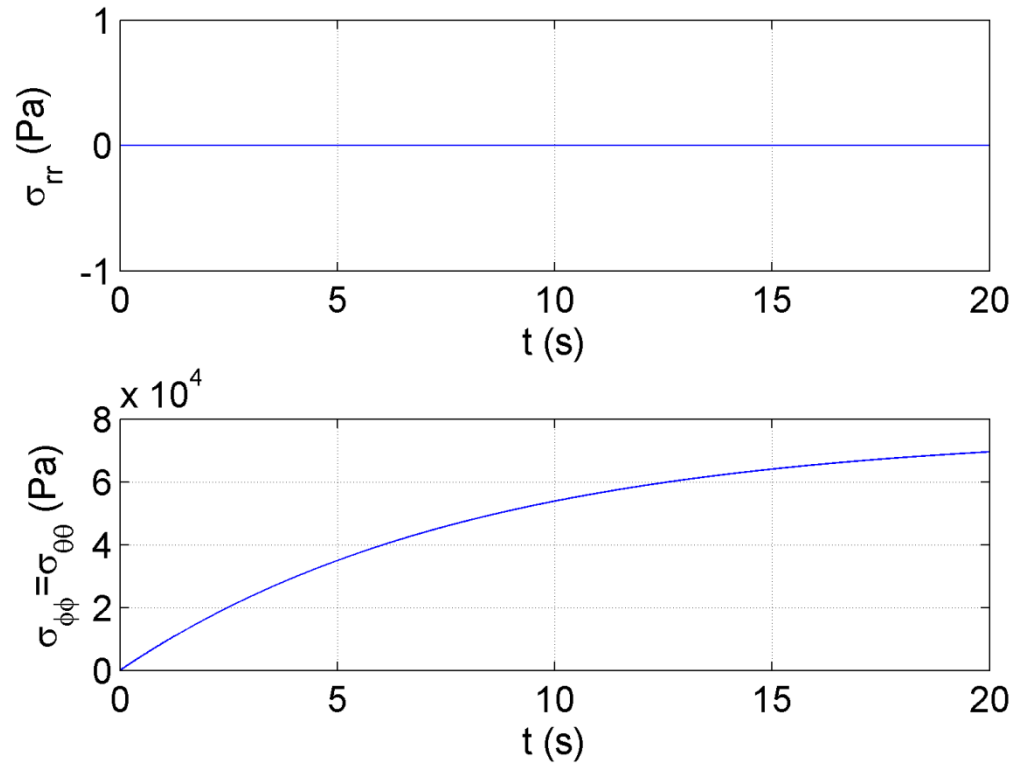


Film coefficient  $H=1000 \text{ W/m}^2\text{K}$





# Thermal stress in a sphere due to a heat source applied step-wise



# Thermal stress in a sphere – analytical vs. finite element solution

The values of thermal stress on the surface of a sphere with radius  $a=1$  mm, at time  $t=20$  s (the value of the film coefficient used was assumed to be  $H=100$  W/m<sup>2</sup>K)

Analytical	ANSYS	Relative error (ANSYS-analytical)/analytical
69549 (Pa)	69054 (Pa)	-0.7%

# Natural frequencies of axisymmetric vibration of an elastic sphere – analytical solution

The frequency equation of axisymmetric vibration modes:

$$(\lambda + 2\mu)[(2 - k^2 a^2) \sin(ka) - 2ka \cos(ka)] + 2\lambda[ka \cos(ka) - \sin(ka)] = 0$$

$$\lambda = \frac{\nu E}{(1 + \nu)(1 - 2\nu)}, \quad \mu = \frac{E}{2(1 + \nu)}$$

$$\omega = \sqrt{\frac{\lambda + 2\mu}{\rho}} k$$

# Natural frequencies of axisymmetric vibration of an elastic sphere – analytical solution

All natural vibration results are for a steel sphere with radius  $a=1$  mm, with the following material properties:  $E=2.1 \cdot 10^{11}$  N/m<sup>2</sup>,  $\nu=0.3$ ,  $\rho=7.8 \cdot 10^3$  kg/m<sup>3</sup>.

Roots of the frequency equation of the symmetric modes:

$ka : 2.6702, 6.0920, 9.3009, 12.4743$

The natural frequencies in Hz:

$f : 2.5584 \cdot 10^6$  Hz,  $5.8370 \cdot 10^6$  Hz,  $8.9116 \cdot 10^6$  Hz,  $11.952 \cdot 10^6$  Hz

# Natural frequencies – finite element vs. analytical solution

Lowest two natural frequencies of a steel sphere of radius  $a=1$  mm (the sphere is unrestrained on its surface)

Analytical	ANSYS	Relative error
$f_1 = 2.5584 \cdot 10^6$ Hz	$f_1 = 2.5559 \cdot 10^6$ Hz	-0.1%
$f_2 = 5.8370 \cdot 10^6$ Hz	$f_2 = 5.8424 \cdot 10^6$ Hz	0.1%

For the discussion of the non-radial vibration see the presentation during WP4

# Some future work

- Vibration transmission from the horn to the cooling piping
- The performance of the horn cooling system
- Fatigue life estimate of the horn and the spheres
- Thermal stress and wave propagation in a pebble bed target using composite material and numerical approach
- Target cooling issues
- Environmental effects (radiation damage, cavitation, etc.)