

Galaxy cluster mass estimate from weak lensing signal

Mariana Penna-Lima

in collaboration with: Dominique Boutigny, Nicolas Chotard and
Céline Combet

Laboratoire d'Annecy de Physique des Particules - LAPP

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Galaxy Cluster Cosmology



Abell 1689

Largest gravitationally bound
structures in the universe:
86% DM, 12% ICM (hot gas),
2% galaxies

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$$\frac{d^2 N}{dz d \ln M} = A_{\text{survey}} \frac{c}{H(z)} D_c^2(z) \frac{dn(M, z)}{d \ln M}$$

$$\text{MF: } \frac{dn(M, z)}{d \ln M} = -\frac{\rho_m(z)}{M} f(\sigma_M, z) \frac{1}{\sigma_M} \frac{d\sigma_M}{d \ln M}$$

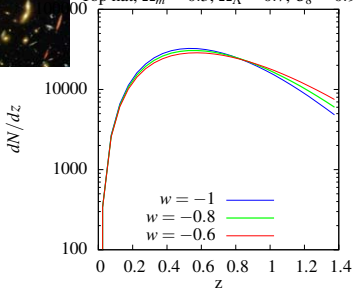
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Top hat, $\Omega_m = 0.3$, $\Omega_\Lambda = 0.7$, $\sigma_8 = 0.9$



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Uncertainty Sources

- Multiplicity function $f(\sigma_M, z)$: nonlinear regime of halo/cluster formation.

N-body simulations: results depend on the halo mass definition.

- Tinker et al. (2008): 5% precision at $z = 0$.
- McClintock et al. (2018): 1% precision at $z = 0$.

The latter is required such that this uncertainty is negligible in the LSST era.

- Biased cosmological parameter estimators: cluster counts
 - Bias on Ω_c , σ_8 and w : $\sim 25\%$ of the respective error bar.

[M. Penna-Lima et al. JCAP 05 \(2014\) 039](#)

- Photometric redshift

- $z^{\text{phot}} = z^{\text{true}} + z^{\text{bias}} \pm \sigma_z^0(1+z)$

- Large surveys:

Dark Energy Survey (DES) – 5 filters, 5,000 deg², $\sigma_z^0 = 0.03$, $z \lesssim 1.4$;

Javalambre Physics of the Accelerating Universe Astrophysical Survey (J-PAS) – 56 filters, 8,500 deg², $\sigma_z^0 = 0.003$, $z \lesssim 1.5$;

Euclid Satellite – 7 filters, $\sigma_z^0 = 0.025 - 0.053$, $z \lesssim 2.0$;

Large Synoptic Survey Telescope (LSST) – 6 filters (ugrizy), 18,000 deg²,
 $\sigma_z^0 \leq 0.02$, $z^{\text{bias}} < 0.003$, $z \lesssim 1.0$

Uncertainty Sources - cluster mass

- Main source of uncertainties.
- Mass is not directly observed.

Determining the relationships between survey observables and halo mass represents the most difficult and complex challenge for cluster cosmology. LSST DESC Science Roadmap

- Mass proxies:
 - X-ray: total luminosity L_x , temperature T_x , thermal energy $Y_x = M_{gas} T_x$
 - mm (Sunyaev-Zeldovich effect): Compton-y parameter Y_{SZ}
 - Optical/IR: richness λ , weak lensing (WL) shear

Unbinned cluster count:

$$\frac{d^2 N(\lambda_i, z_i^{\text{phot}}, \vec{\theta})}{dz^{\text{phot}} d\lambda} = \int d \ln M \int d\lambda^{\text{true}} \int dz^{\text{true}} \Phi(M, z)$$
$$\times \frac{d^2 N(M, z^{\text{true}}, \vec{\theta})}{dz^{\text{true}} d \ln M} P(\lambda_i | \lambda^{\text{true}}) P(\lambda^{\text{true}} | \ln M) P(z_i^{\text{phot}} | z^{\text{true}})$$

- The mass proxy relations must be calibrated to within 5% level over the mass and redshift ranges in order to access the full constraining power of galaxy clusters. Hao, Rozo and Wechsler (2010), von der Linden et al. (2014)
- WL most promising - absolute mass (not sensitive to gas astrophysics).
- WL individual mass estimates incur smaller bias than X-ray, but they are noisy.
- Use multi-wavelength data to measure low-scatter mass proxies relations (e.g., X-ray) and their covariances identifying the optimal combination of follow-up observables to enhance LSST cluster science.

Mass scale calibration *Planck* and CLASH

- $\ln(M_{\odot}/M_0) = \ln(1 - b_{\odot}) + A_{\odot} \ln(M_{true}/M_0)$
- The SZ relation is usually calibrated with WL measurements assuming $A_{SZ} = A_{WL} = 1.0$ e $b_{WL} = 0.0$

$$\frac{M_{SZ}}{M_{WL}} = 1 - b_{SZ}.$$

- Previous analyses provided underestimated error bars of b_{SZ} .
- Mainly due to strong assumptions on the other parameters.
- Introduced a new method to calibrate the mass-observable relations: pseudo cluster counts.

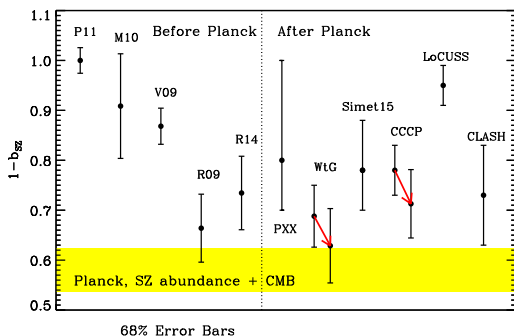
$$\mathcal{L} = \prod_i \frac{1}{N} \int_{-\infty}^{\infty} d \ln M_{True} n(M_{True}, z^i) P(M_{PL}^{(i)}, M_{CL}^{(i)} | M_{True}, \vec{\theta}),$$

$$P(M_{PL}, M_{CL} | M_{True}, \vec{\theta}) = \int d \ln M_{SZ} d \ln M_L P(M_{PL} | M_{SZ}) \\ \times P(M_{CL} | M_L) P(\ln M_{SZ}, \ln M_L | M_{True}, \vec{\theta})$$

e

$$n(M_{True}, z) = f(M_{True}) \frac{dn(M_{True}, z)}{d \ln M_{True}} \frac{d^2 V}{dz d\Omega}.$$

Calibrating the *Planck* cluster mass scale with CLASH



- *Planck* and *Cluster Lensing And Supernova survey with Hubble* (CLASH): 21 clusters in common.
- We fit 11 parameters: A_{SZ} , b_{SZ} , σ_{SZ} , A_L , b_L , σ_L , ρ , selection function
- Reduced tension between CMB and clusters, 1.34σ .

M. Penna-Lima, J. Bartlett, E. Rozo, J-B Melin, et al., *A&A* 604, A89 (2017),
[arXiv:1608.05356](https://arxiv.org/abs/1608.05356)

- **CLMassMod**: Cluster masses from weak-lensing shear maps
- Quantify mass-modeling systematics
- DESC - Galaxy Clusters Key Projects
 - Absolute Mass Calibration I (DC1): Analyze shear maps from DM only simulations.
 - Absolute Mass Calibration II (DC2): Extend to DM + baryons simulations.
 - Analysis of DC3 Mock Lightcone and pre-cursor data. CC/SV observing plan: Apply to DC3 and cluster precursor dataset.

Lensing masses with photo-z distributions

- Background galaxies are magnified and distorted by the gravitational potential of the cluster (lens).
- Measured quantity - reduced shear: the ellipticities of galaxies (e_1, e_2) (bulge and disk) corrected for point spread function (PSF) effects. Tonegawa et al. (2018)
- Reduced shear (theory):

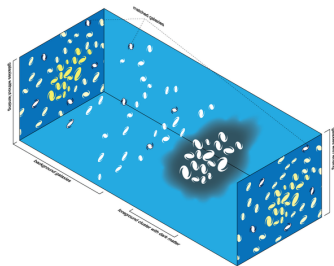
$$g = \frac{\beta_s(z_b)\gamma_\infty(R)}{1 - \beta_s(z_b)\kappa_\infty(R)}, \text{ where } \beta_s = \frac{D_{LS}}{D_S} \frac{D_\infty}{D_{L,\infty}}$$

- Convergence $\kappa(R)$ and tangential shear $\gamma(R)$ are functions of the surface mass density $\Sigma(R)$:

$$\kappa(R) = \frac{\Sigma(R)}{\Sigma_c},$$

$$\gamma(R) = \frac{\Delta\Sigma}{\Sigma_c} = \frac{\bar{\Sigma}(<R) - \Sigma(R)}{\Sigma_c},$$

$$\text{where } \Sigma_c = \frac{c^2}{4\pi G} \frac{D_S}{D_L D_{LS}}.$$



By Michael Sachs

Lensing masses with photo-z distributions

- Mass estimates using the full photometric redshift posterior distributions of individual galaxies.
- Method used in the Weighing the Giants analyses. von der Linden et al. (2014), Applegate et al. (2014)
- They showed systematic biases in the mean mass of the sample can be controlled.
- In their analyses $\Sigma(R) = \Sigma_{\rho}(R) = \int d\chi \rho \left(\sqrt{R^2 + \chi^2} \right)$
- ρ is the matter density profile.
- Navarro-Frenk-White (1996) (NFW):
$$\rho(r) = \frac{\delta_c \rho_{crit}}{(r/r_s)(1+r/r_s)^2}, \quad \delta_c = \frac{\Delta}{3} \frac{c^3}{\ln(1+c) - \frac{c}{1+c}},$$
 c is the concentration parameter and r_s is the scale radius.

Posterior

$$\mathcal{P}(M|\hat{g}) = P(M) \int_{\forall \alpha} P(\vec{\alpha}) \prod_i \int_z P(\hat{g}_i|g(z, M), \vec{\alpha}) P_i(z) dz d\vec{\alpha},$$

- $P(M)$: prior on the cluster mass
- $P(\hat{g}_i|g(z, M), \vec{\alpha})$: Voigt distribution (convolution of Gaussian and Lorentz distributions)
- $P_i(z)$: redshift probability distribution of the i -th galaxy
- $\vec{\alpha}$: Voigt profile and shear calibration parameters
- $g(z, M)$ (\hat{g}): reduced shear (measured)

Effects to take into account to compute the surface mass density $\Delta\Sigma$ (in addition to the cluster/halo profile term $\Delta\Sigma_\rho(R)$):

- Miscentering: the observed systems may be incorrectly centered affecting the shear profile. Johnston et al. 2007
This term introduces two new parameters: the fraction of miscentered clusters p_{CC} , and the offset between the true and the estimated center R_{off} .
- 2-halo term $\Delta\Sigma_{2h}$: correction to the halo profile for larger scales than \approx the Virial radius (or R_Δ) due to the surrounding matter. Depends on the halo bias and the linear matter power spectrum.

- No-weak shear $\Delta\Sigma_{nw}$: massive clusters may not satisfy the weak lensing regime, i.e., $g_t \approx \gamma_t$, if $\gamma_t \ll 1$ and $\kappa \ll 1$.
- Central point mass associated to the BCG. $\Delta\Sigma_{BCG}$

$$\Delta\Sigma = \frac{M_{BCG}}{\pi R^2} + p_{cc} [\Delta\Sigma_{\rho}(R) + \Delta\Sigma_{nw}(R)] \\ + (1 - p_{cc})\Delta\Sigma_{misc}(R) + \Delta\Sigma_{2h}(R)$$

See, e.g., Parroni et al. (2017), Vitorelli et al. (2018), Pereira et al. (2018), Cibirka et al. (2017) and references therein.

Implement other matter density profiles:

- Diemer & Kravtsov, Einasto, ...

Independent implementation: Numerical Cosmology library (NumCosmo) Vitenti and Penna-Lima ascl:1408.013, github

Conclusions and next steps

- Absolute cluster mass calibration - WL most promising
- Relative cluster mass calibration (LSST follow-up with X-ray data)
- Requirements to better constrain cosmological models
- Individual cluster mass estimates via WL: simulations
- Implemented in NumCosmo
- Include corrections to compute the surface mass density and, consequently, the reduced shear: miscentering, 2-halo term, ...
- Implement other matter density profiles: Diemer & Kravtsov, Einasto, ...
- Obtain cluster mass estimates: DC2 and real data