

Primordial Black Holes

as

Dark Matter

Florian Kühnel

New from the Dark - Episode 3
Montpellier, 25th of May 2018



work in particular with
Bernard Carr
Katherine Freese
Jens Jasche
Pavel Naselsky
Tommy Ohlsson
Glenn Starkman

- ★ Formation of primordial black holes
- ★ Primordial black holes and particle dark matter
- ★ Aspects of primordial black holes and gravitational waves
- ★ Uncertainties of primordial black-hole constraints

PBH Generalities

- ★ Black-hole (BH) formation for $R < R_S$.
- ★ Astrophysical: From $10^9 M_\odot$ down to M_\odot but **not lower**.
- ★ Have a look at the density
 - To form smaller black holes we need higher density.
 - Compare to cosmological density
 - Formation at early times; **primordial black holes (PBHs)**.
- ★ Masses of primordial black holes:
 - $M(t = 10^{-23} \text{ s}) = 10^{15} \text{ g}$,
 - $M(t = 10^{-6} \text{ s}) = M_\odot$

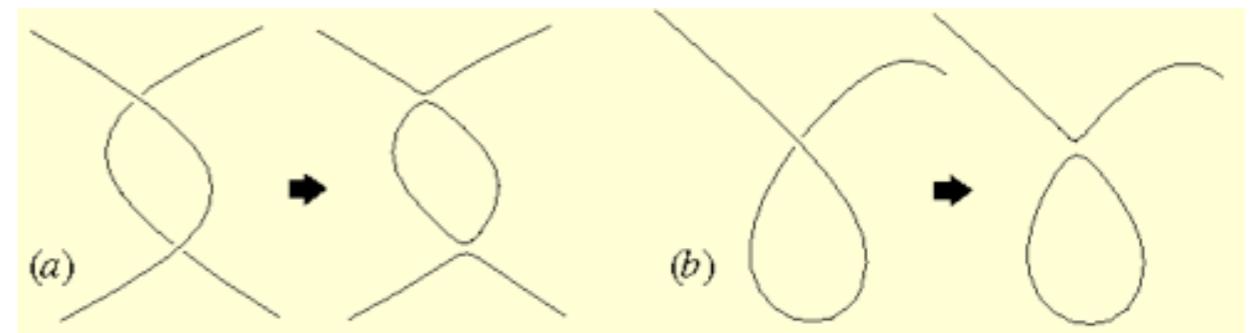
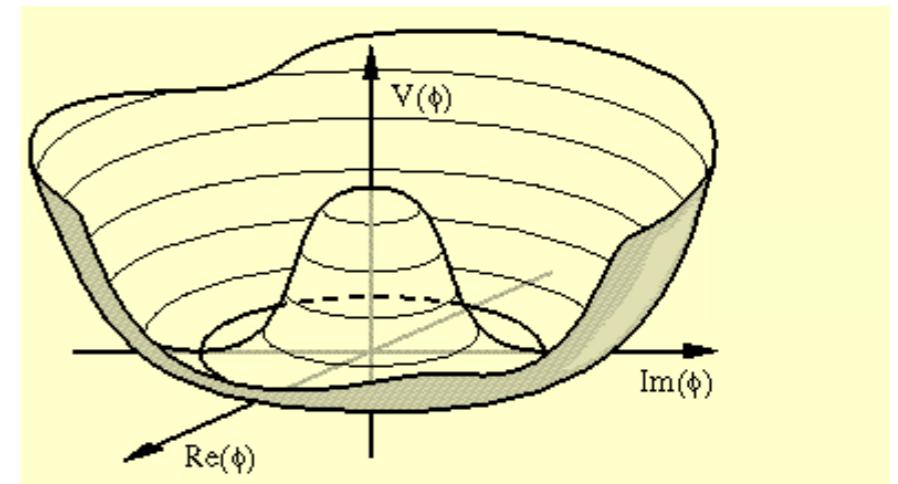
PBH Formation Mechanisms



★ Formation of primordial black holes

PBH Formation Mechanisms

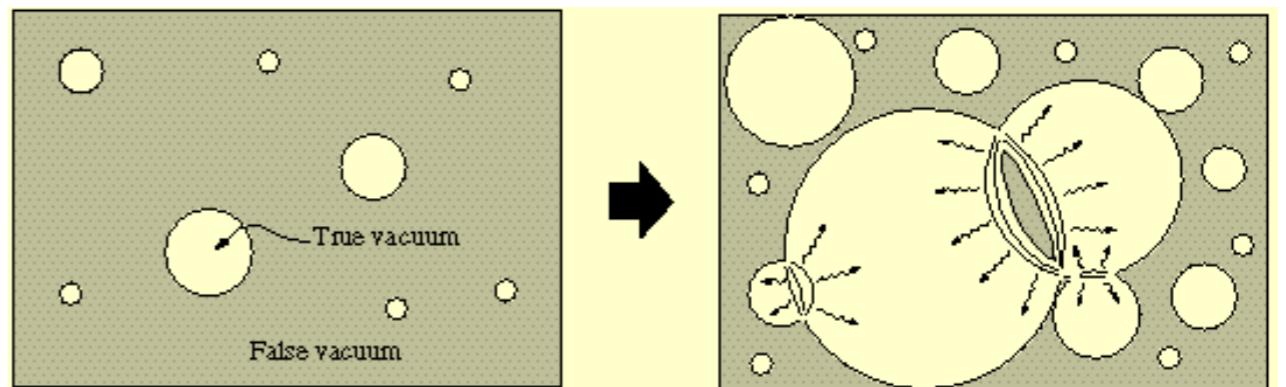
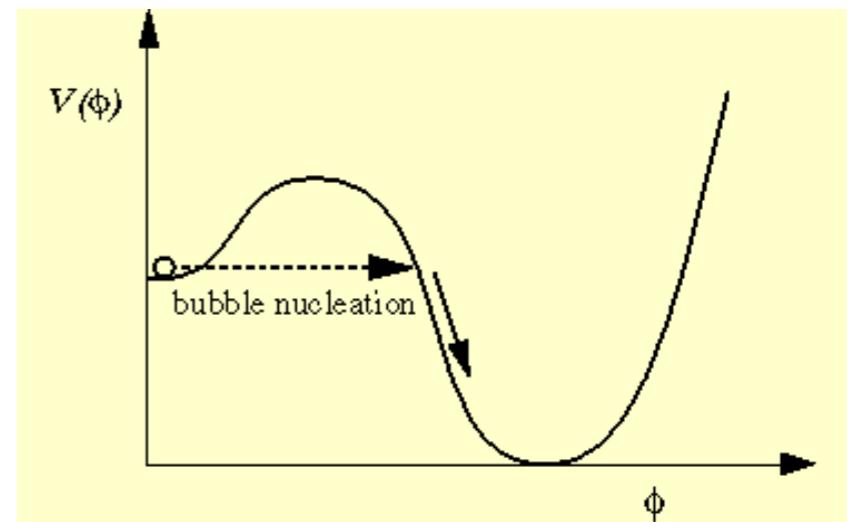
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- ★ Cosmic string loops



http://www.damtp.cam.ac.uk/research/gr/public/cs_top.html

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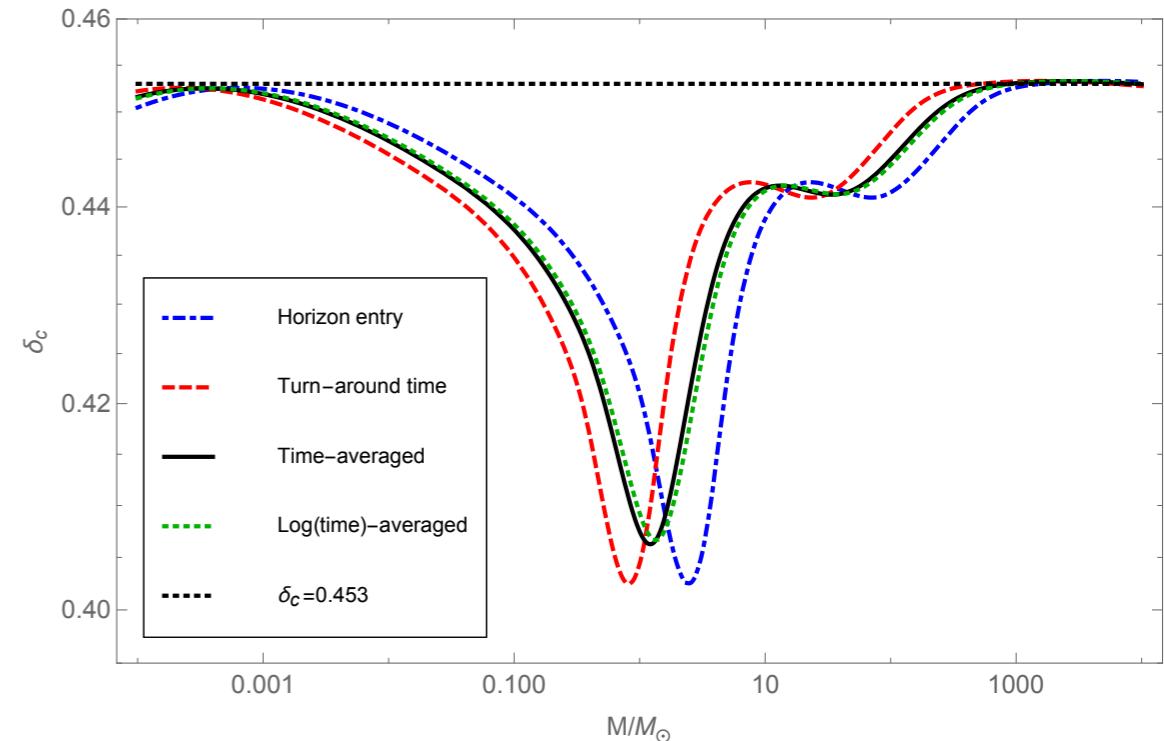
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 - ★ Bubble collisions
 - ★ Pressure reduction



[Byrnes *et al.* 2018]

PBH Formation Mechanisms

- ★ Formation of primordial black holes by
 - ★ Cosmic string loops
 - ★ Bubble collisions
 - ★ Pressure reduction
 - ★ Large density perturbations of inflationary origin

→ Simple estimate:

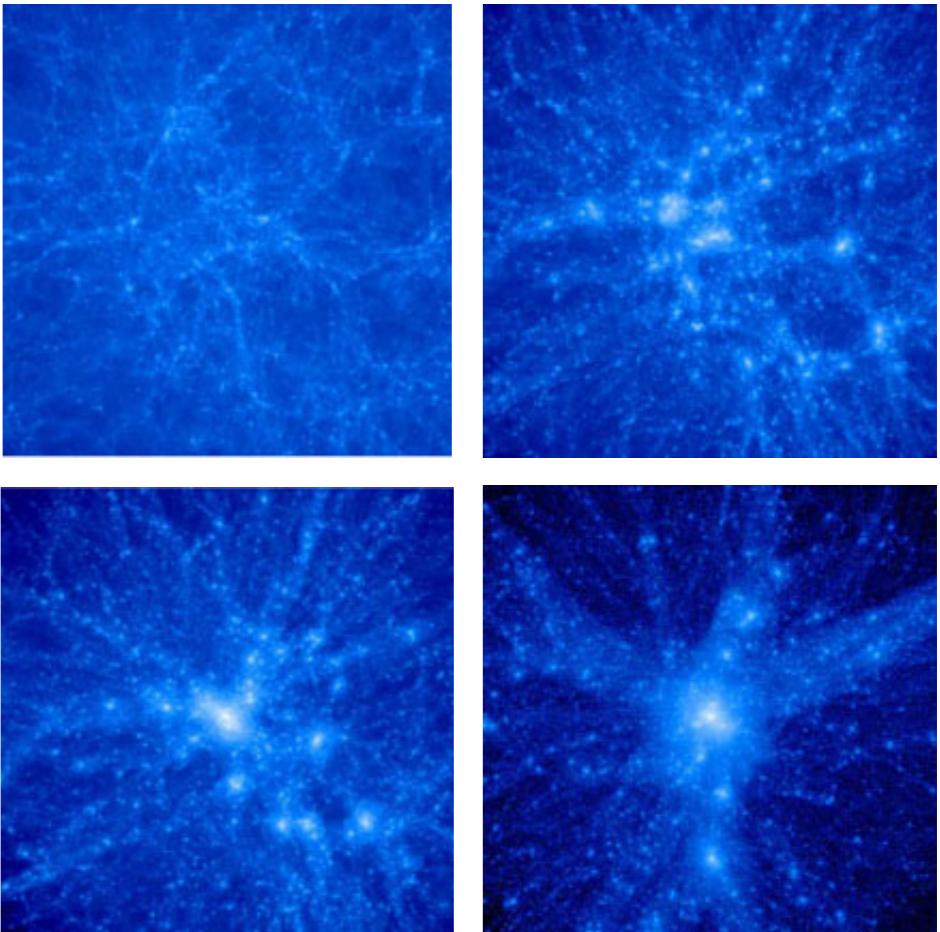
[Carr 1975]

$$R > R_J \Rightarrow \boxed{\delta_H > w}, \quad \text{for } p = w \rho$$

w > 0

scale of the over density

Jeans length



PBH — Probes of Scales



★ Probe a huge range of scales:

$M \sim 10^{-5}$ g **Quantum Gravity:**

Planck relics, Extra dimensions and higher-dimensional black holes, ...

$M \lesssim 10^{15}$ g **Early Universe:**

Baryogenesis, Nucleosynthesis, Reionisation, ...

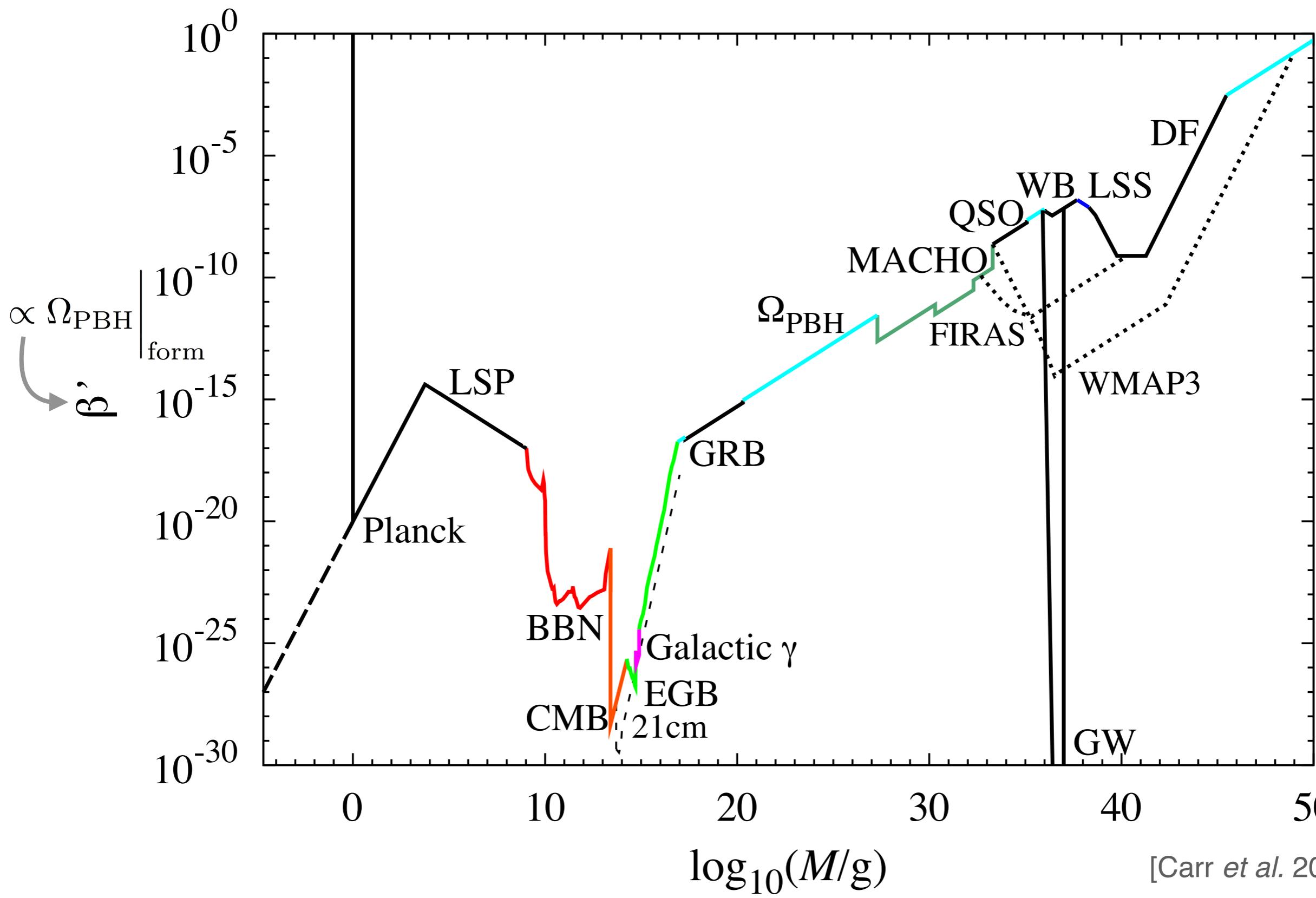
$M \sim 10^{15}$ g **High-Energy Physics:**

Cosmological and galactic gamma-rays, ...

$M \gtrsim 10^{15}$ g **Gravity:**

Critical phenomena,
Cold dark matter,
Dynamical effects, Lensing effects,
Gravitational waves,
Black holes in galactic nuclei, ...

PBH Constraints at Formation



Critical Collapse

- ★ Usually: Assume

$$M_{BH} \propto M_H$$

↑
horizon mass

- ★ Critical scaling:

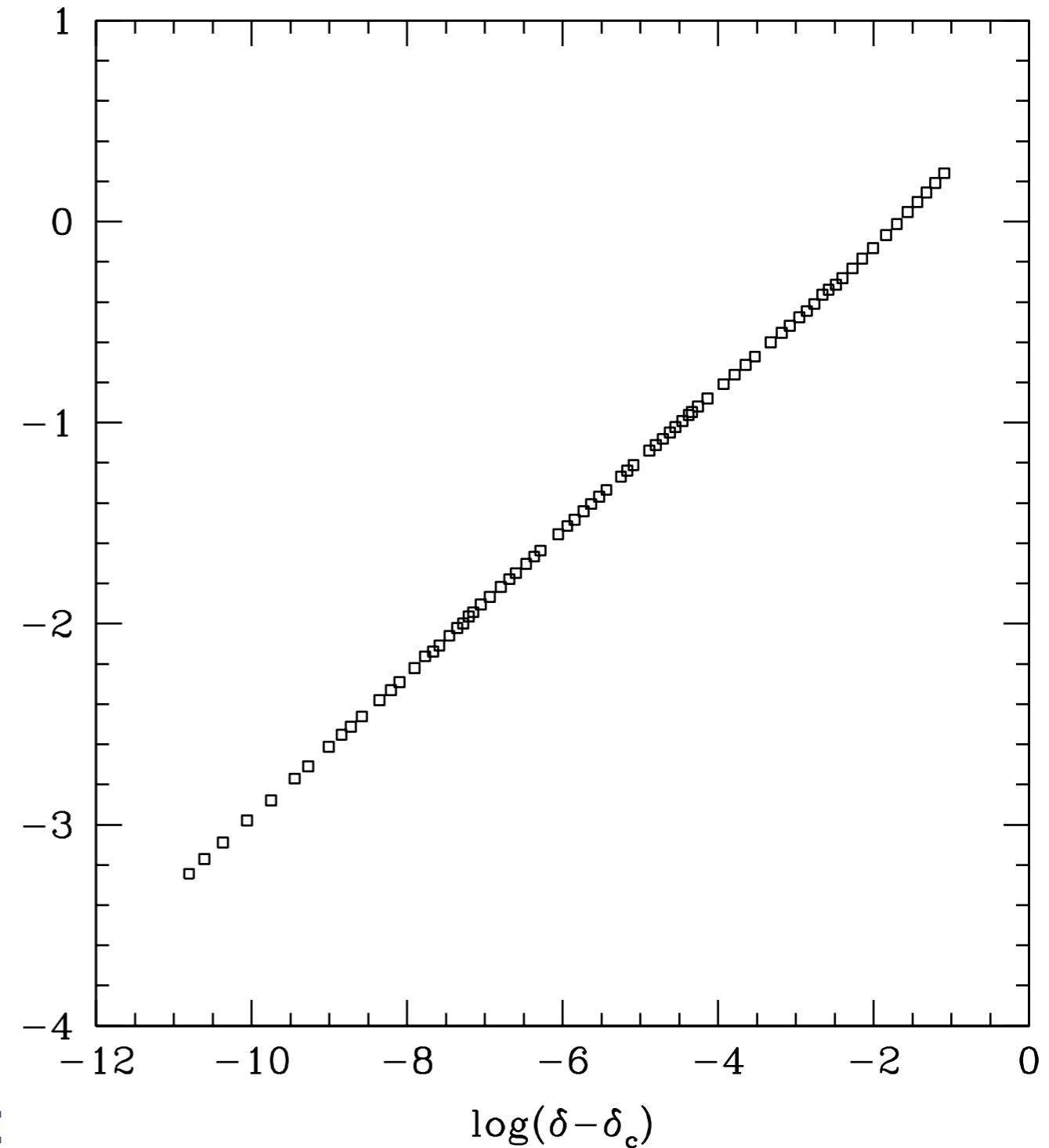
[Choptuik '93]

$$M_{BH} = k M_H (\delta - \delta_c)^\gamma$$

↓
density contrast

- ★ Radiation domination and for spherical Mexican-hat profile:

$$k \approx 3.3, \quad \delta_c \approx 0.45, \quad \gamma \approx 0.36$$



[Musco, Miller, Polnarev 2008]

Critical Collapse

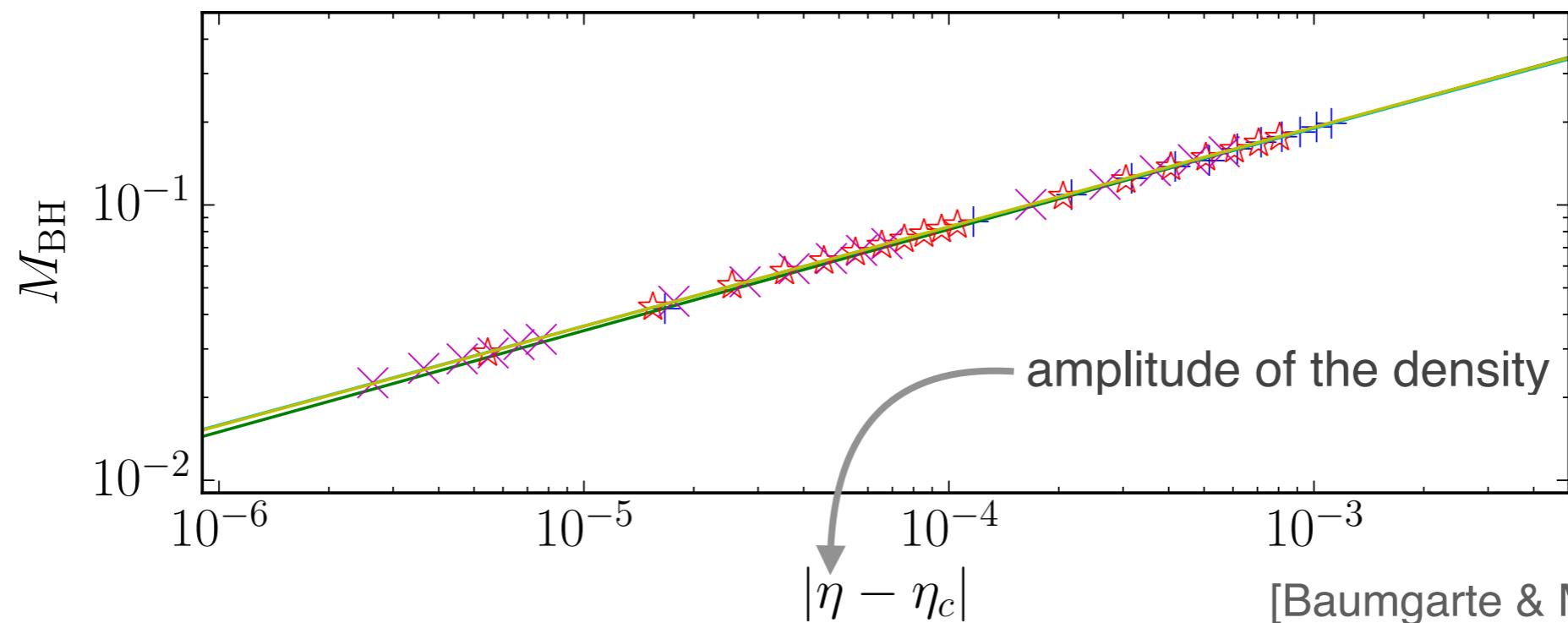
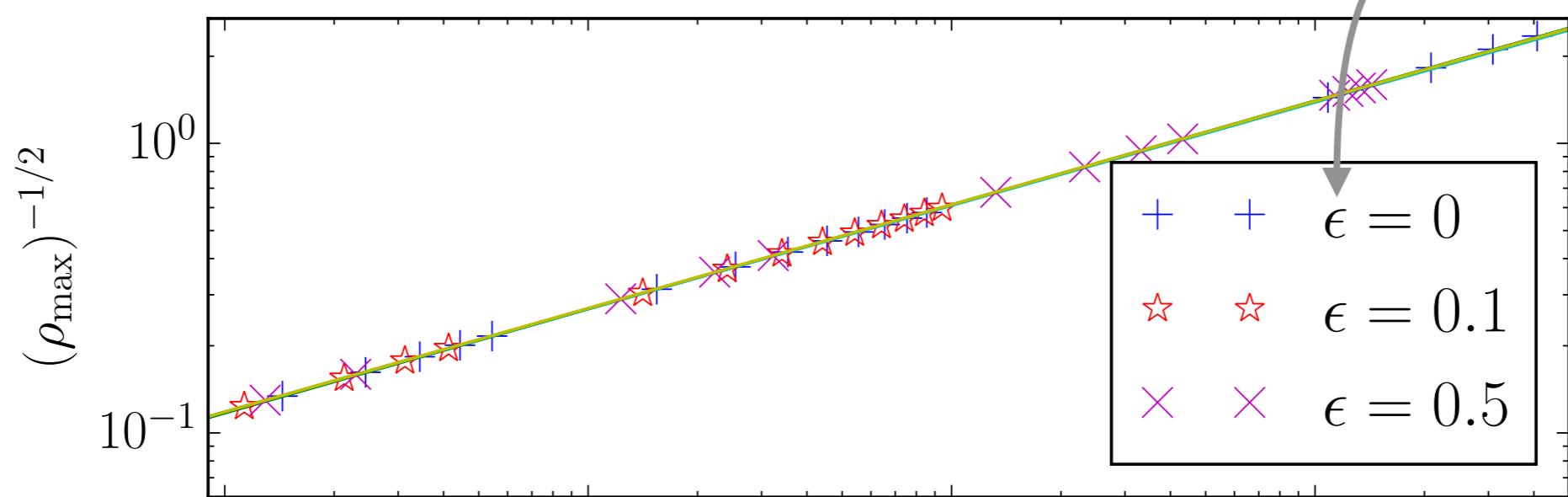


★ Critical collapse for **non-spherical** systems?

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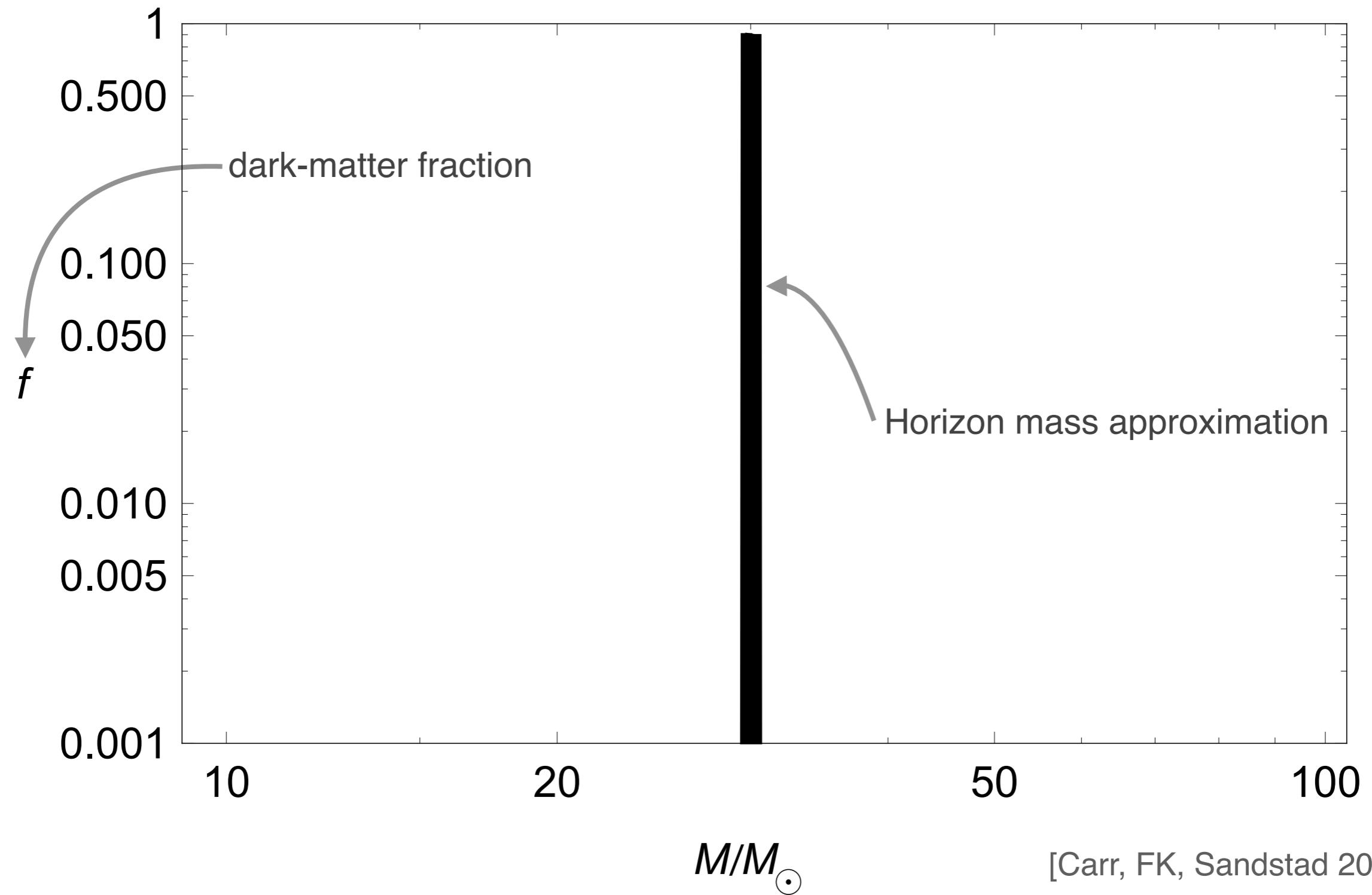
★ Axial symmetry $\rho(r, \theta) \sim \eta f_1(r)(1 + \epsilon f_2(r, \theta))$:



[Baumgarte & Montero 2015]

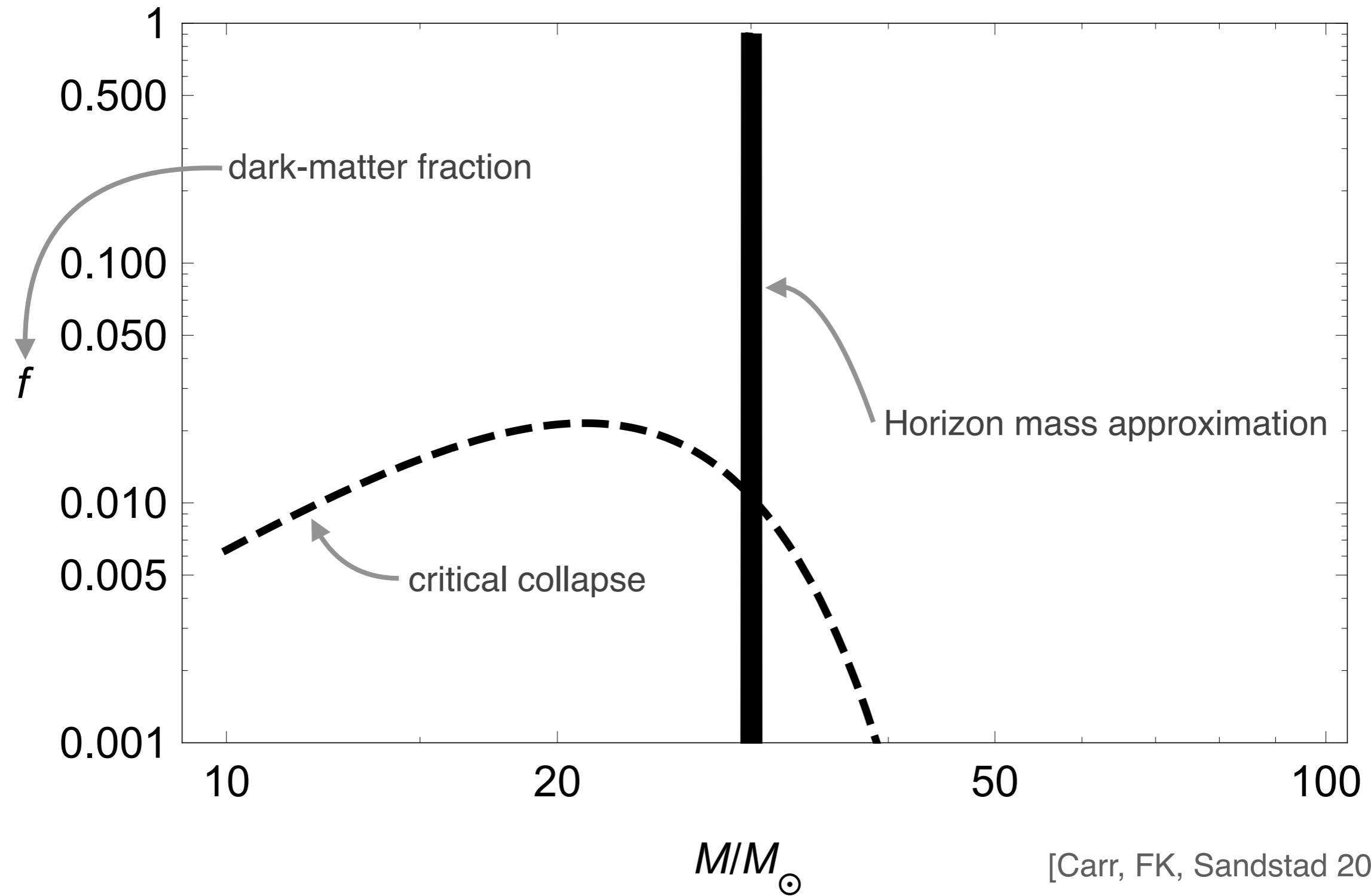
Critical Collapse

★ How would this look for **monochromatic** mass function?



Critical Collapse

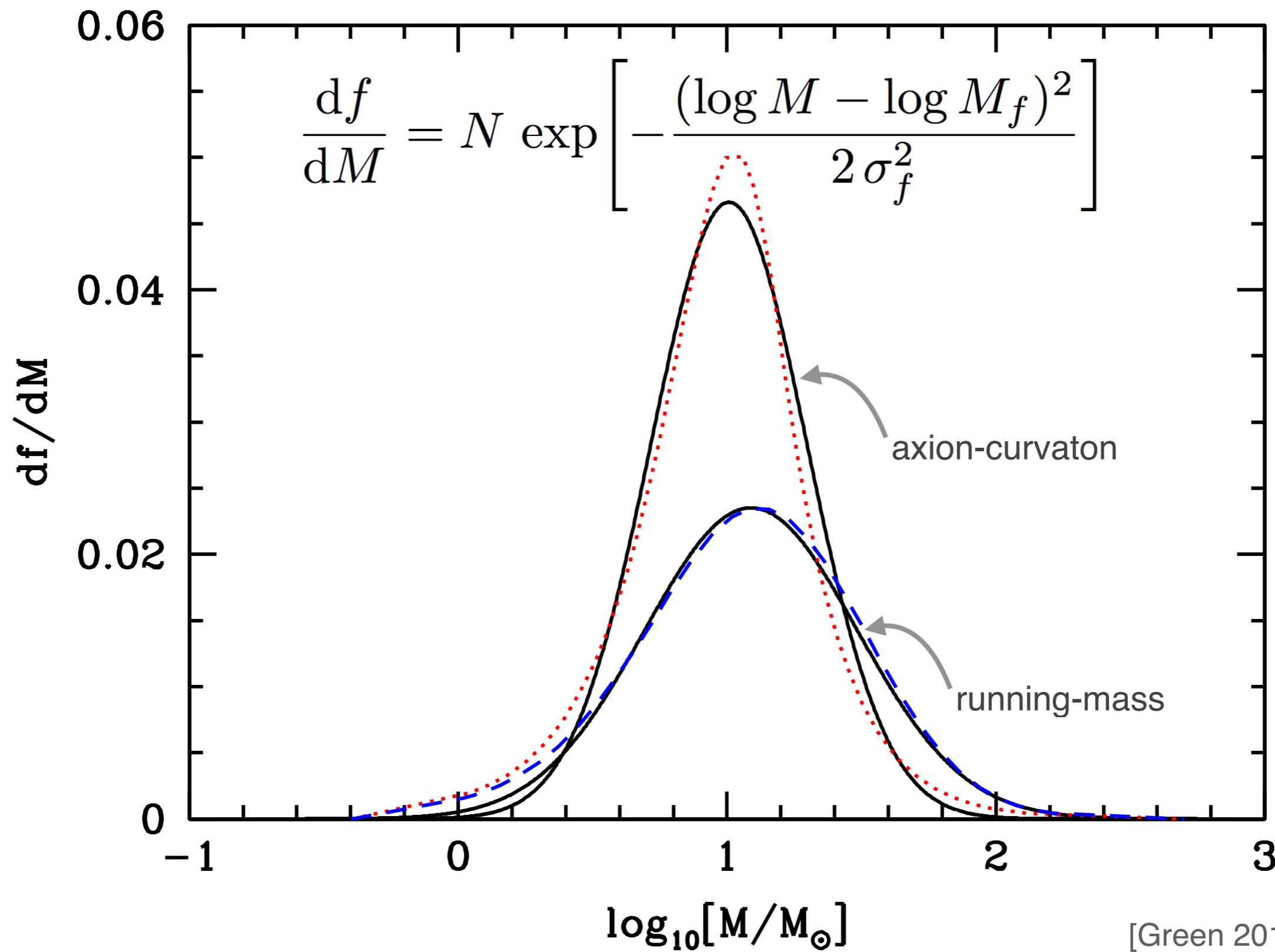
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More Systematic Study



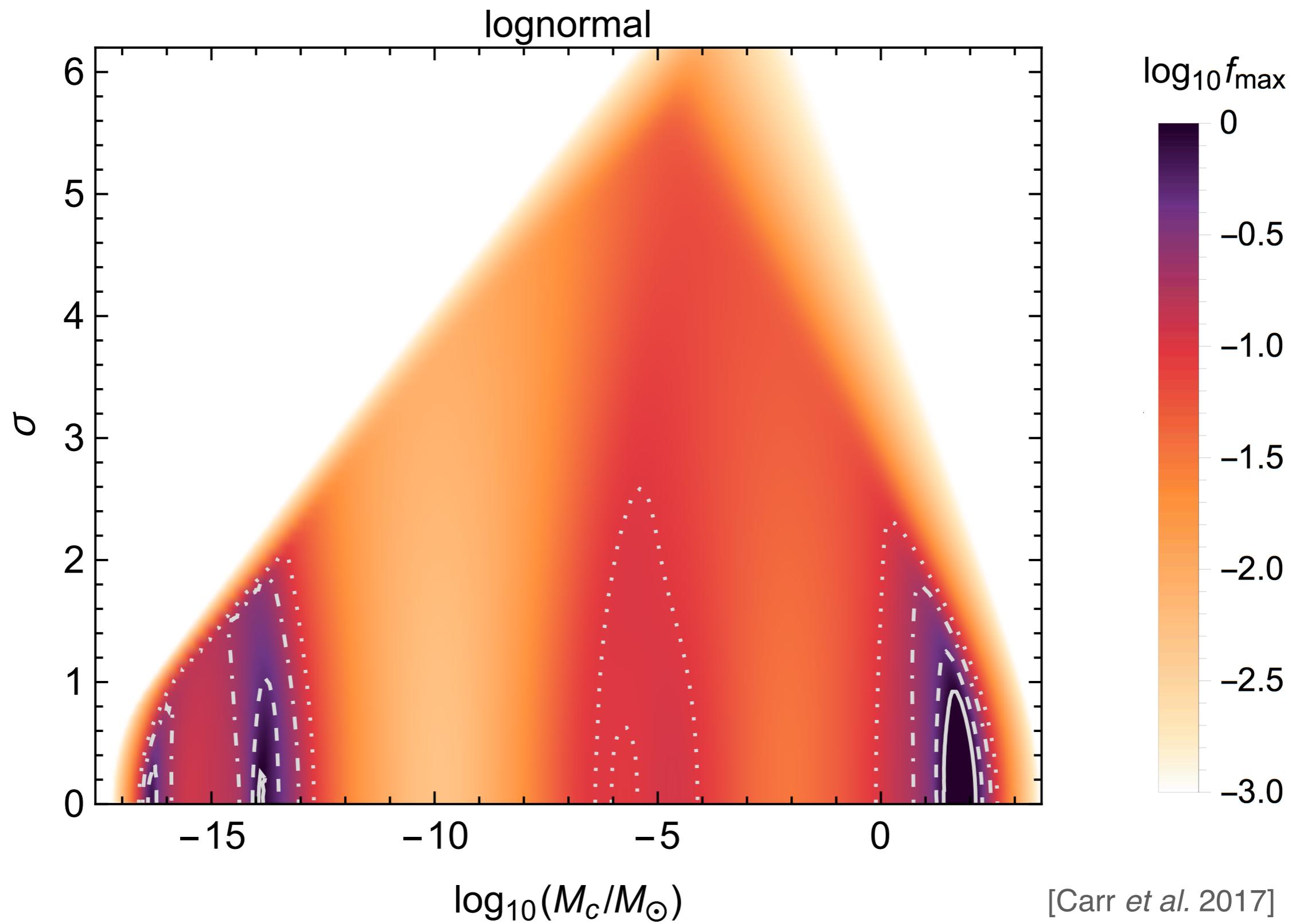
Oscar Klein
centre



More Systematic Study



Oskar Klein
centre



PBH & Particle Dark Matter



- ★ If PBHs do **not** constitute the entirety of the dark matter, the latter must necessarily contain **something else**.
- ★ One possibility: a **combined** scenario, e.g. **DM = PBHs + Particles**
- ★ Let us now study WIMP **annihilations** in PBH halos:
 - ★ The annihilation rate $\Gamma \propto n^2$.
 - Halo profile does matter; **enhancement** of Γ in density spikes.

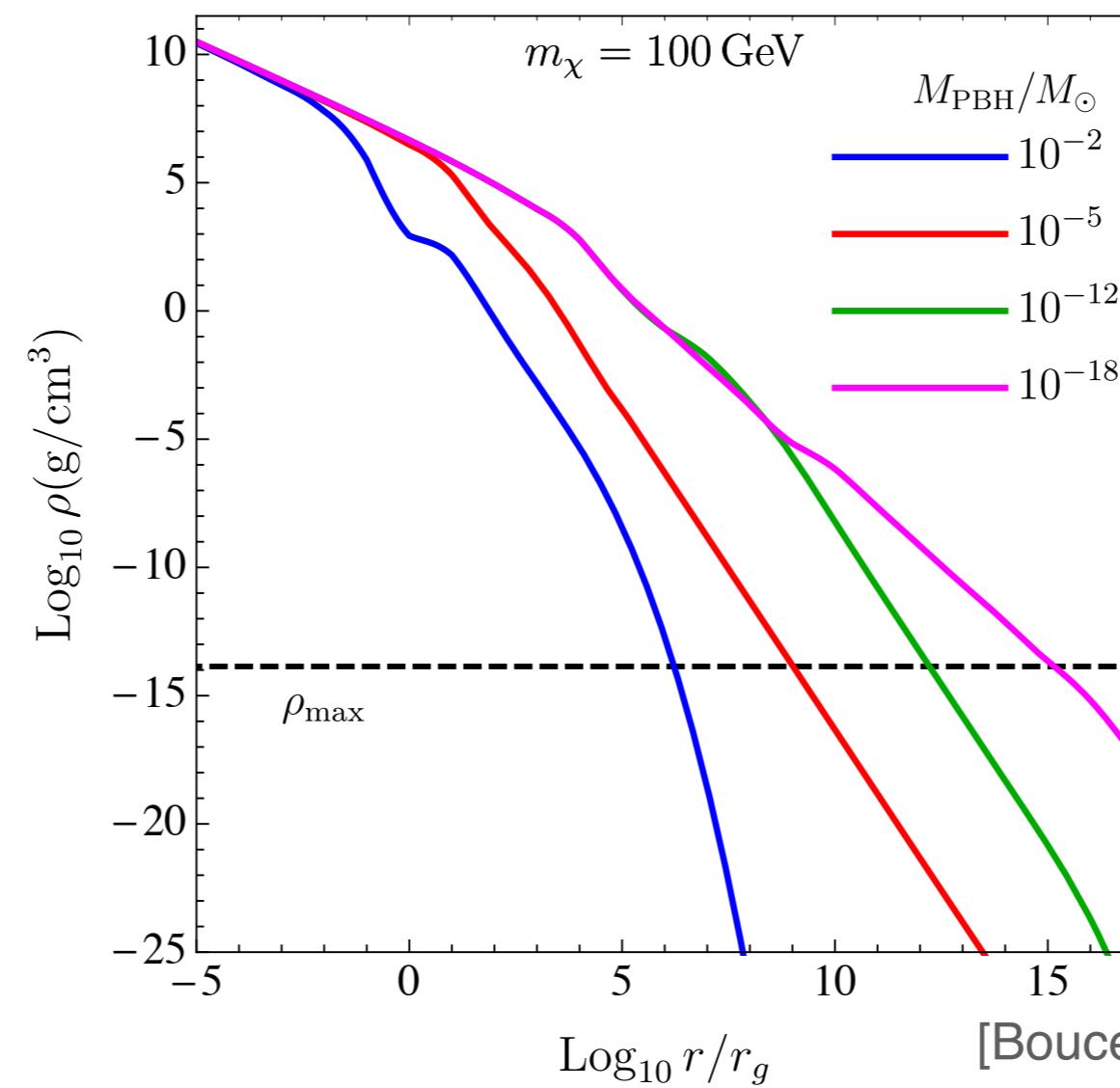
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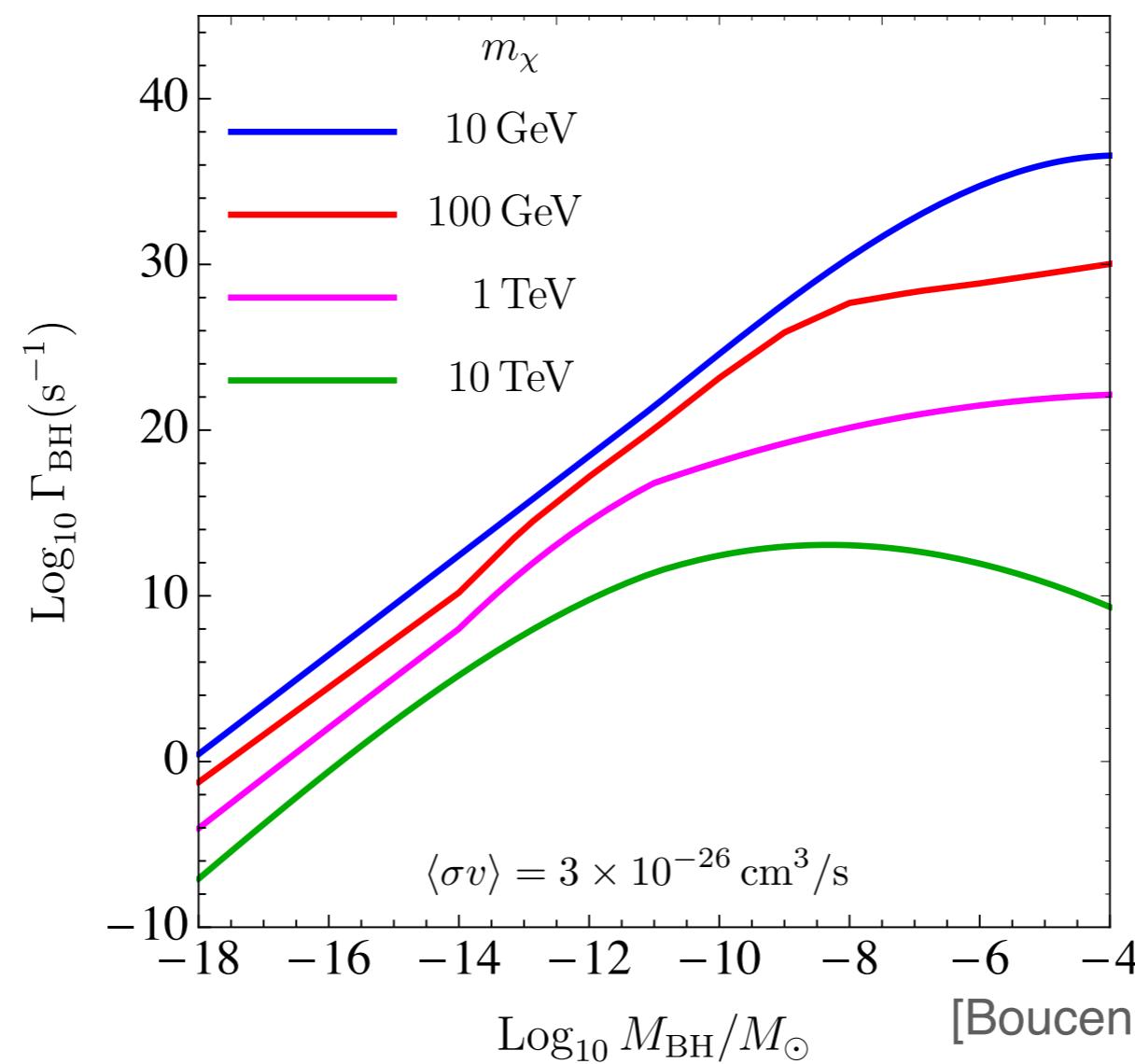
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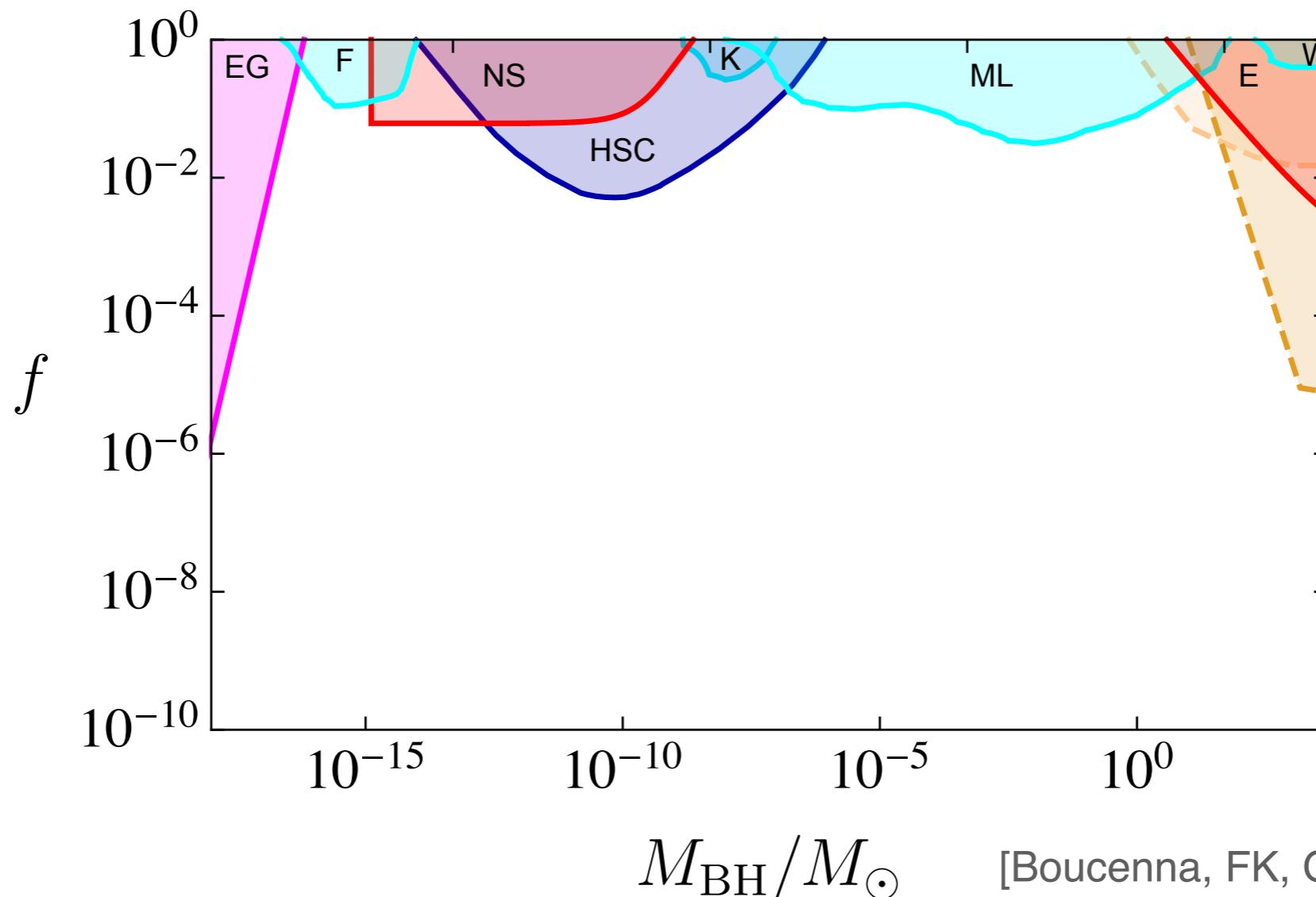
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 - 2) calculate the annihilation rate



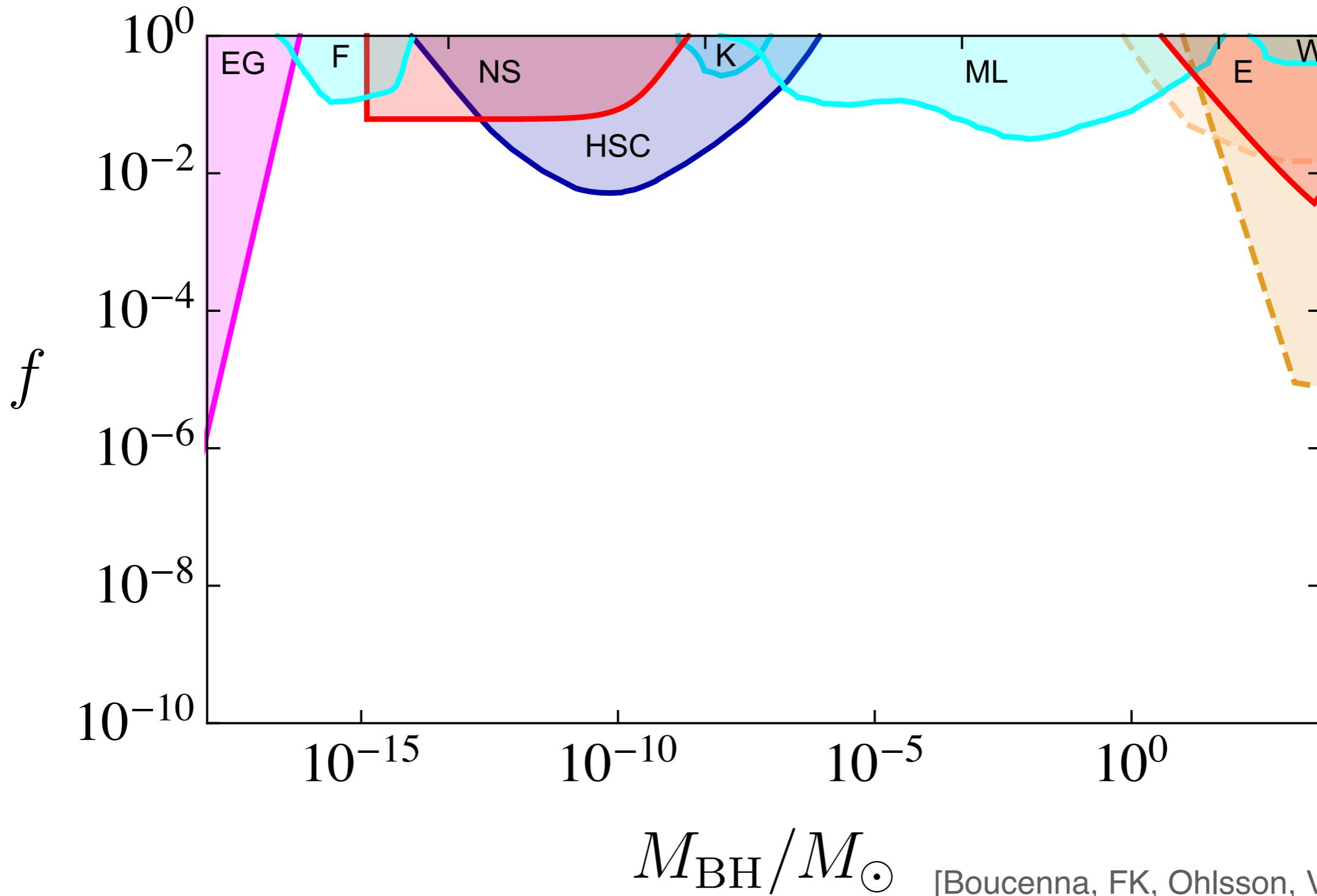
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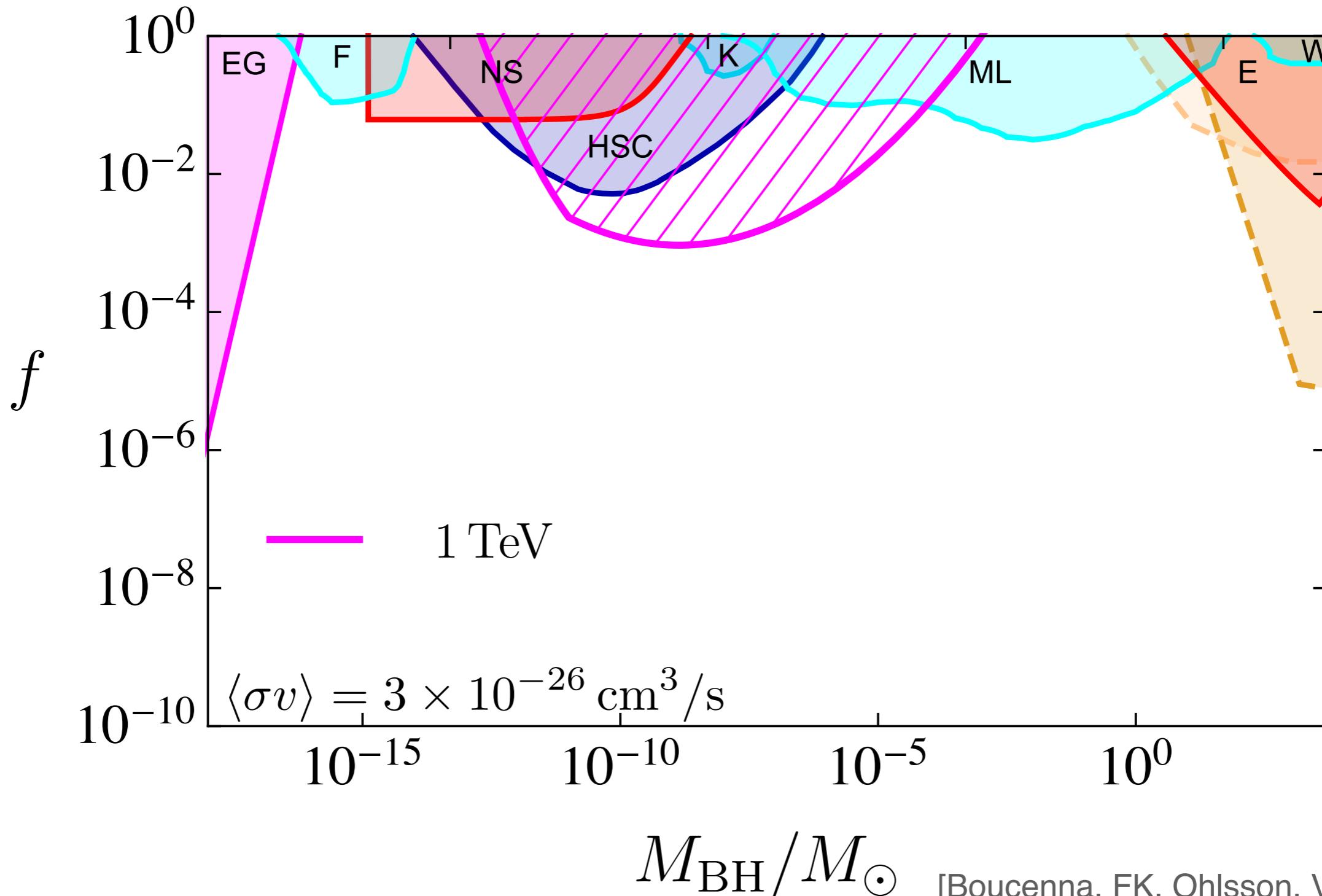
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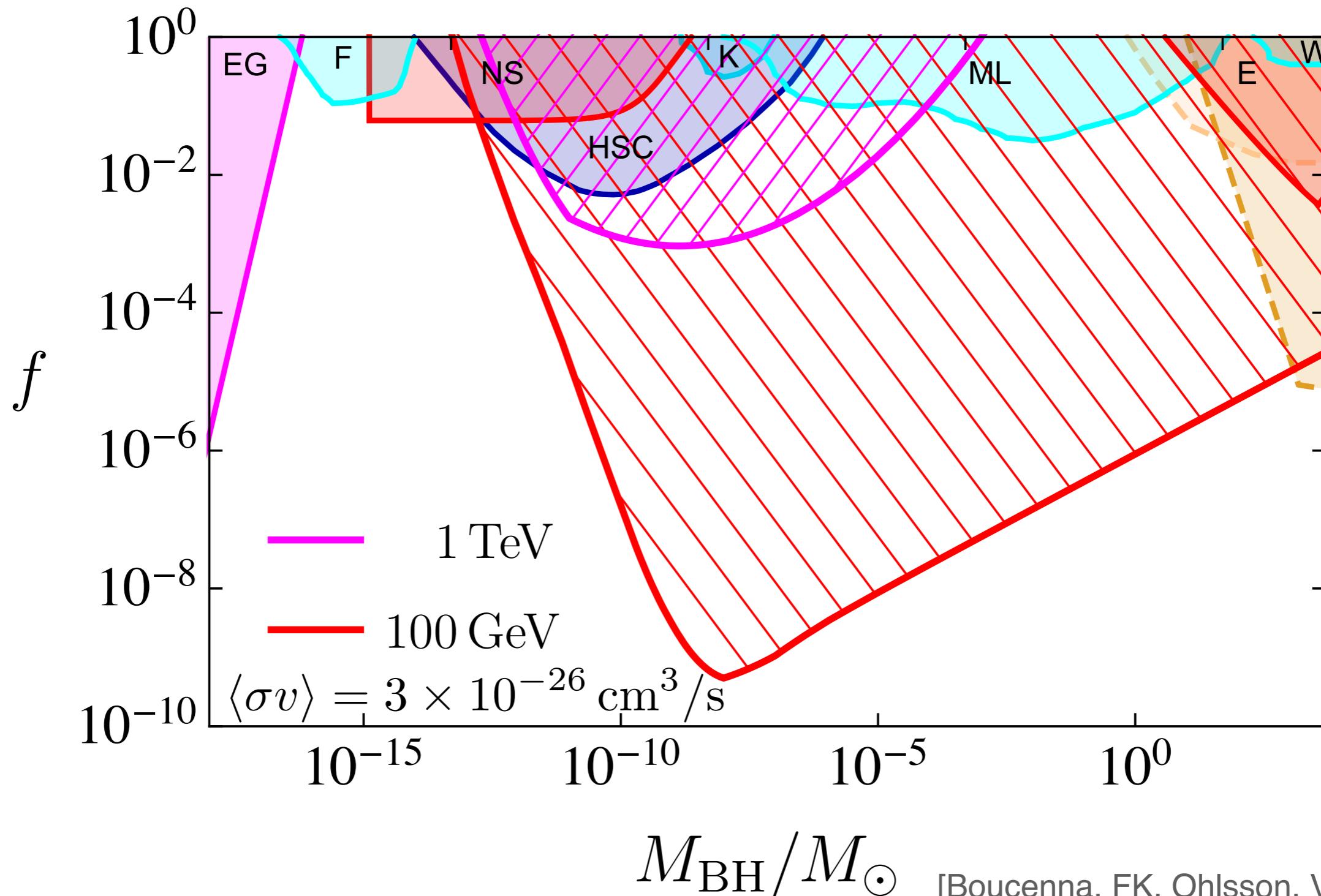
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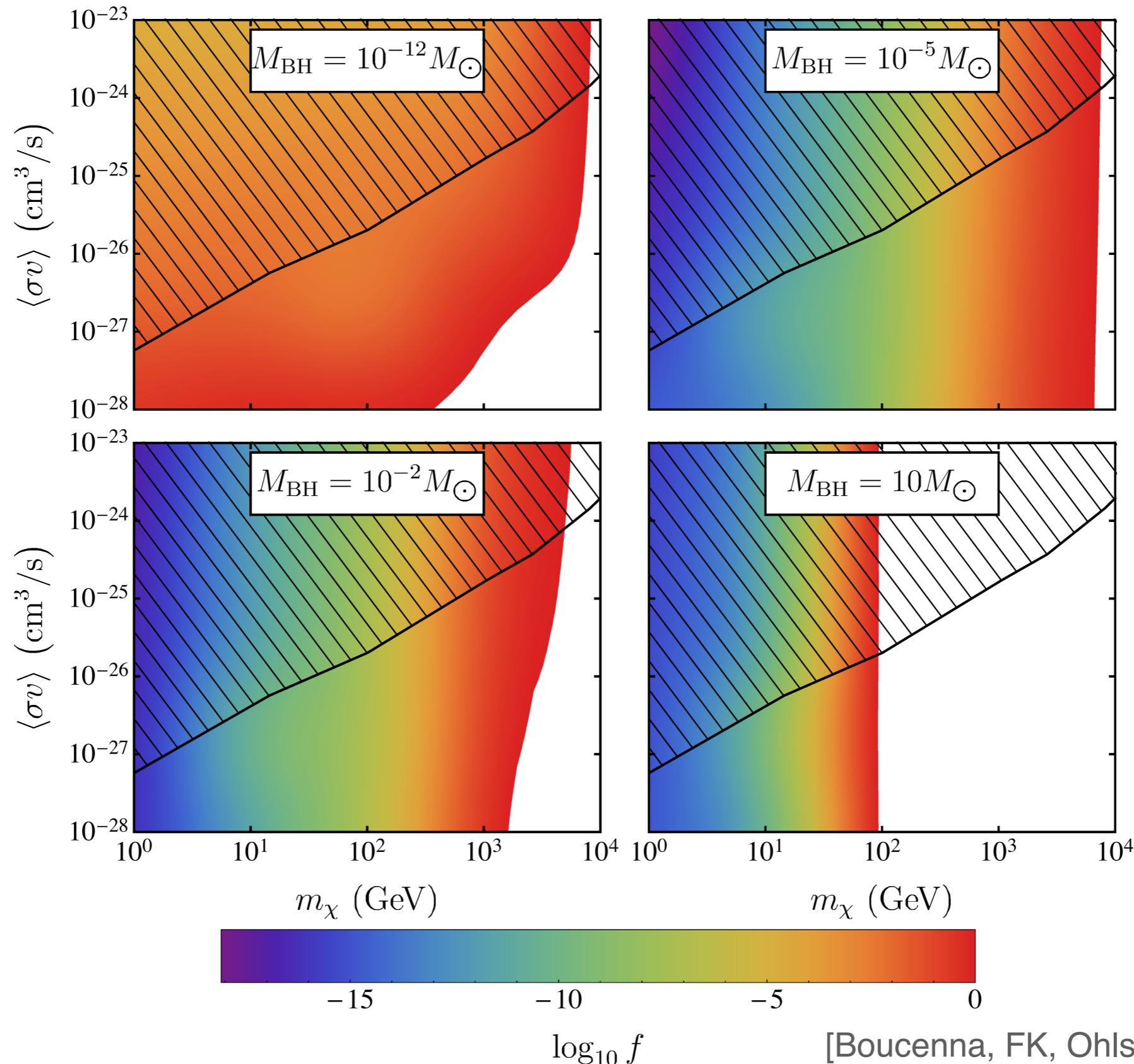


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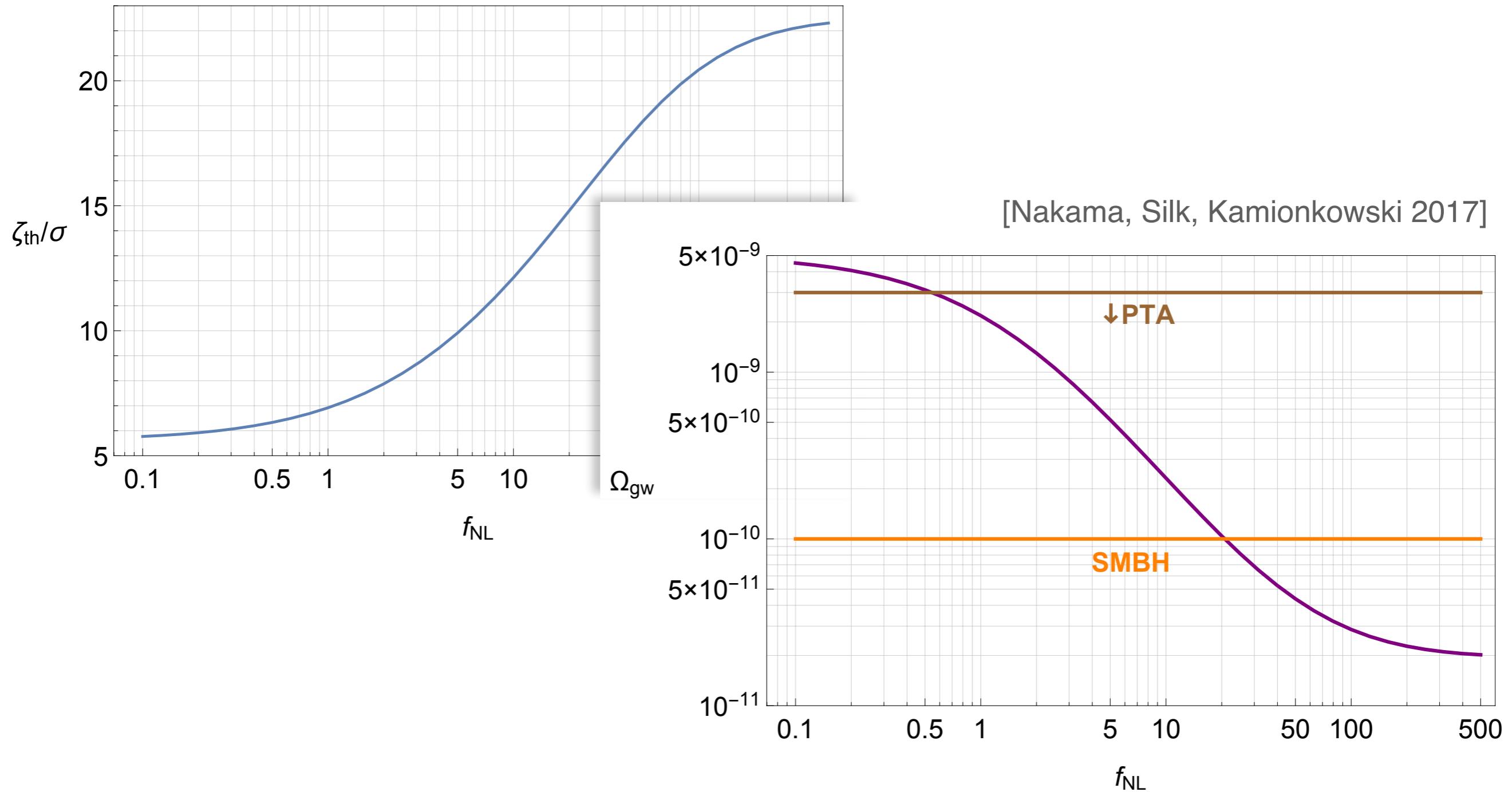
Gravitational Waves from PBHs



- ★ PBHs can emit **gravitational waves** in various instances and times.

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- ★ Gravitational waves from **PBH formation**.



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 - ★ Gravitational waves from **PBH formation**.
 - ★ Gravitational-wave emission from **PBH binaries**:
 - 1) Stochastic GW background

$$\Omega_{\text{gw}} \approx \frac{1}{\rho_c c^2} \int dz \frac{N(z)}{1+z} \left(\nu_r \frac{E_{\text{gw}}}{d\nu_r} \right) \Bigg|_{\nu_r = \nu(1+z)}$$

number of events

critical density

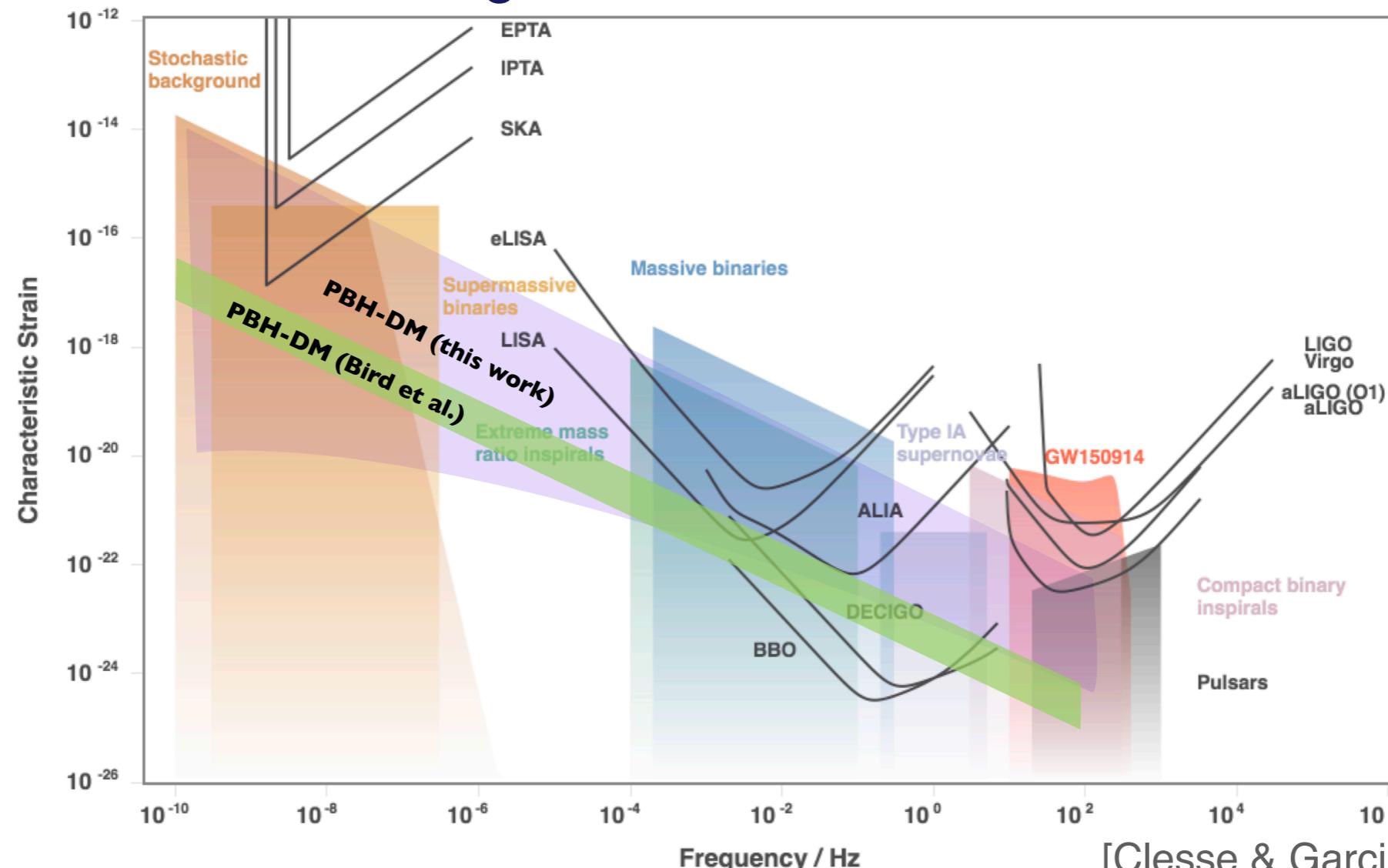
gravitational-wave energy per event

[Phinney 2001]

Annotations: A grey arrow points to the critical density term in the denominator of the integral. Another grey arrow points to the number of events term in the numerator. A third grey arrow points to the gravitational-wave energy per event term in the parentheses.

Gravitational Waves from PBHs

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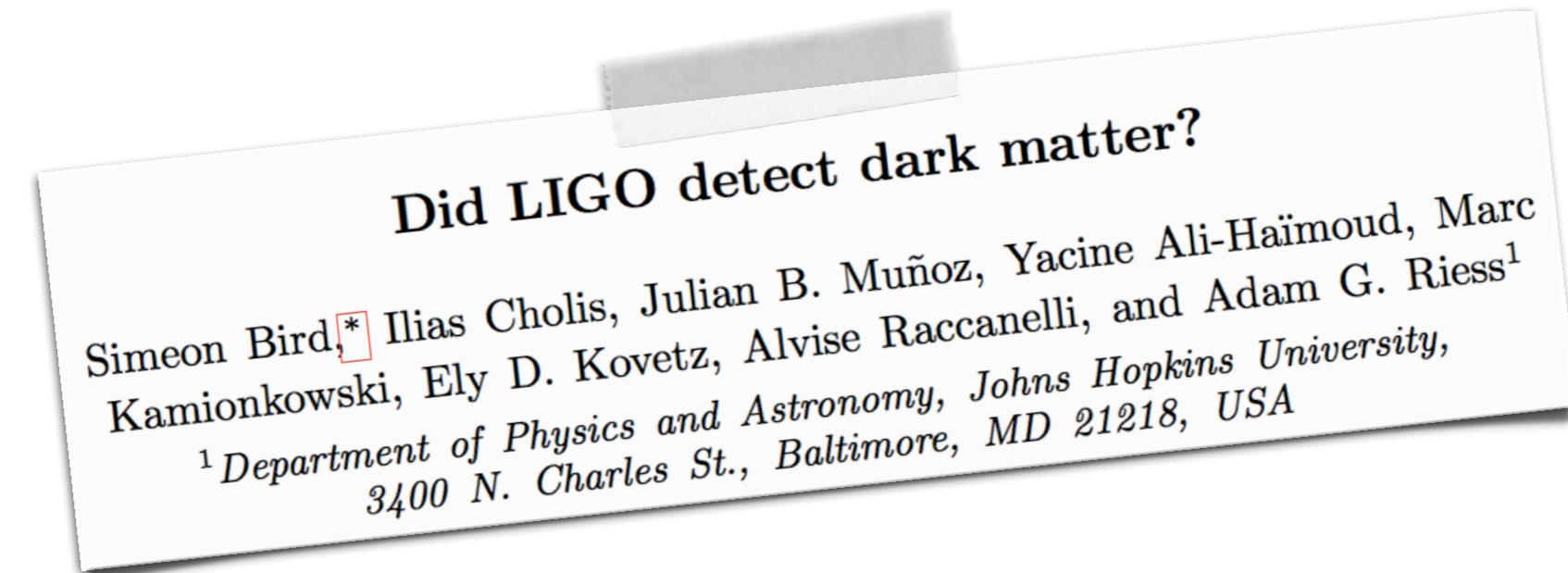


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Primordial black holes as dark matter

Bernard Carr,^{1,*} Florian Kühnel,^{2,†} and Marit Sandstad^{3,‡}

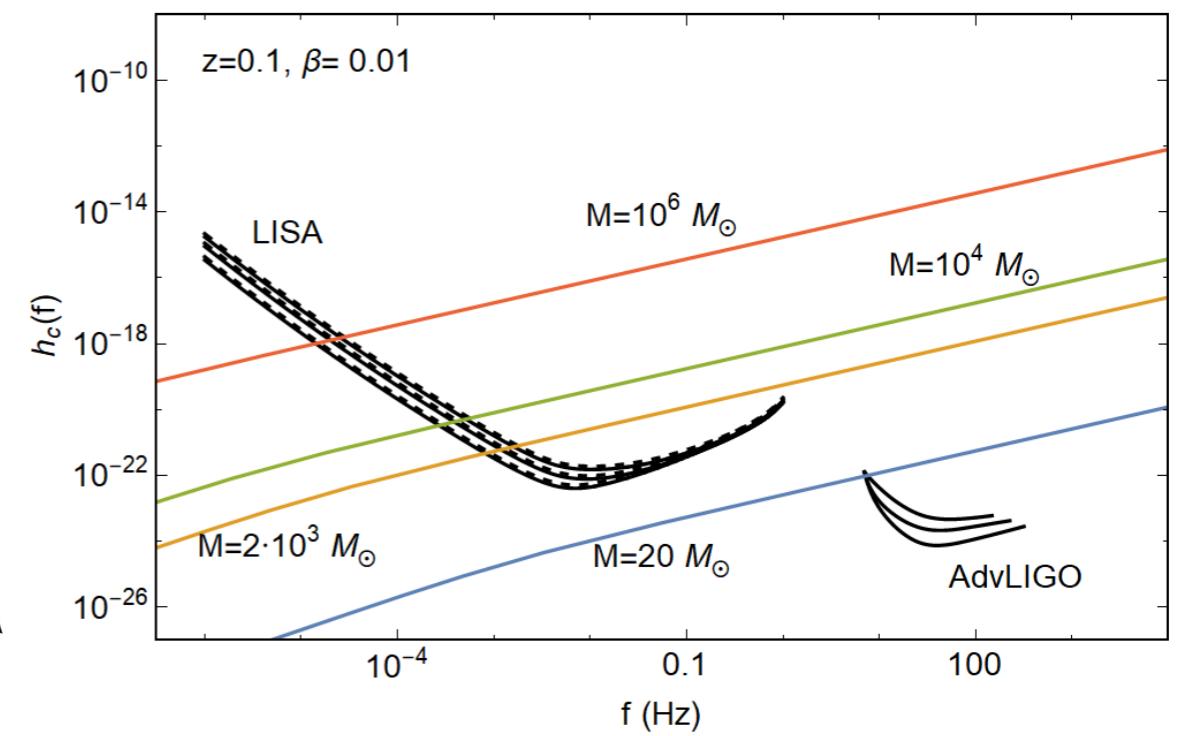
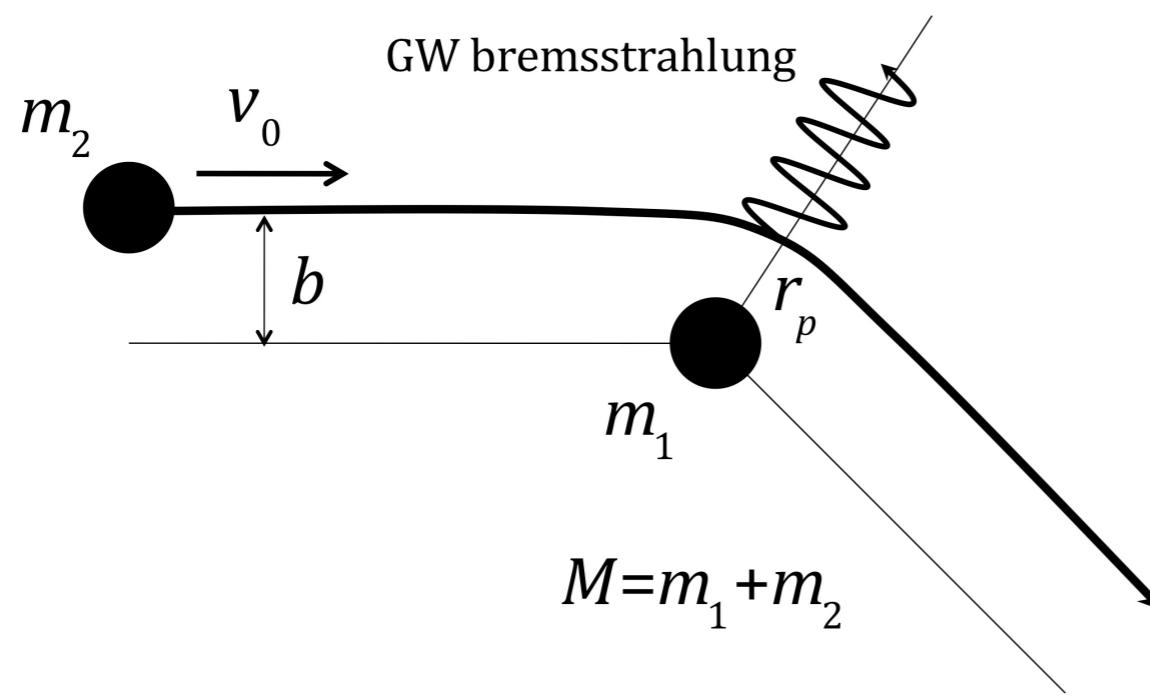
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(Received 8 August 2016; published 4 October 2016)*

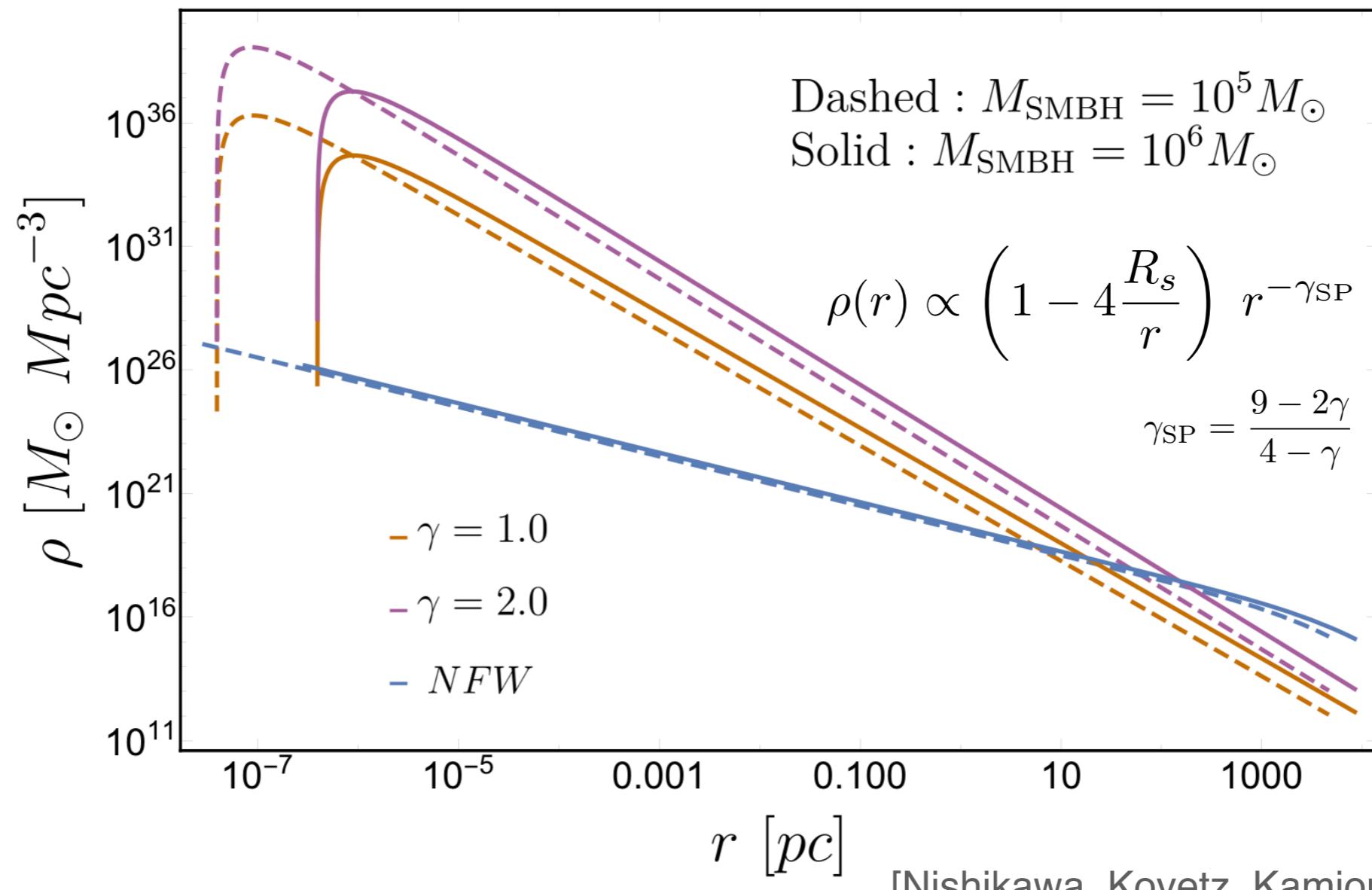
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 - ★ Gravitational-wave emission from **hyperbolic PBH encounters**.



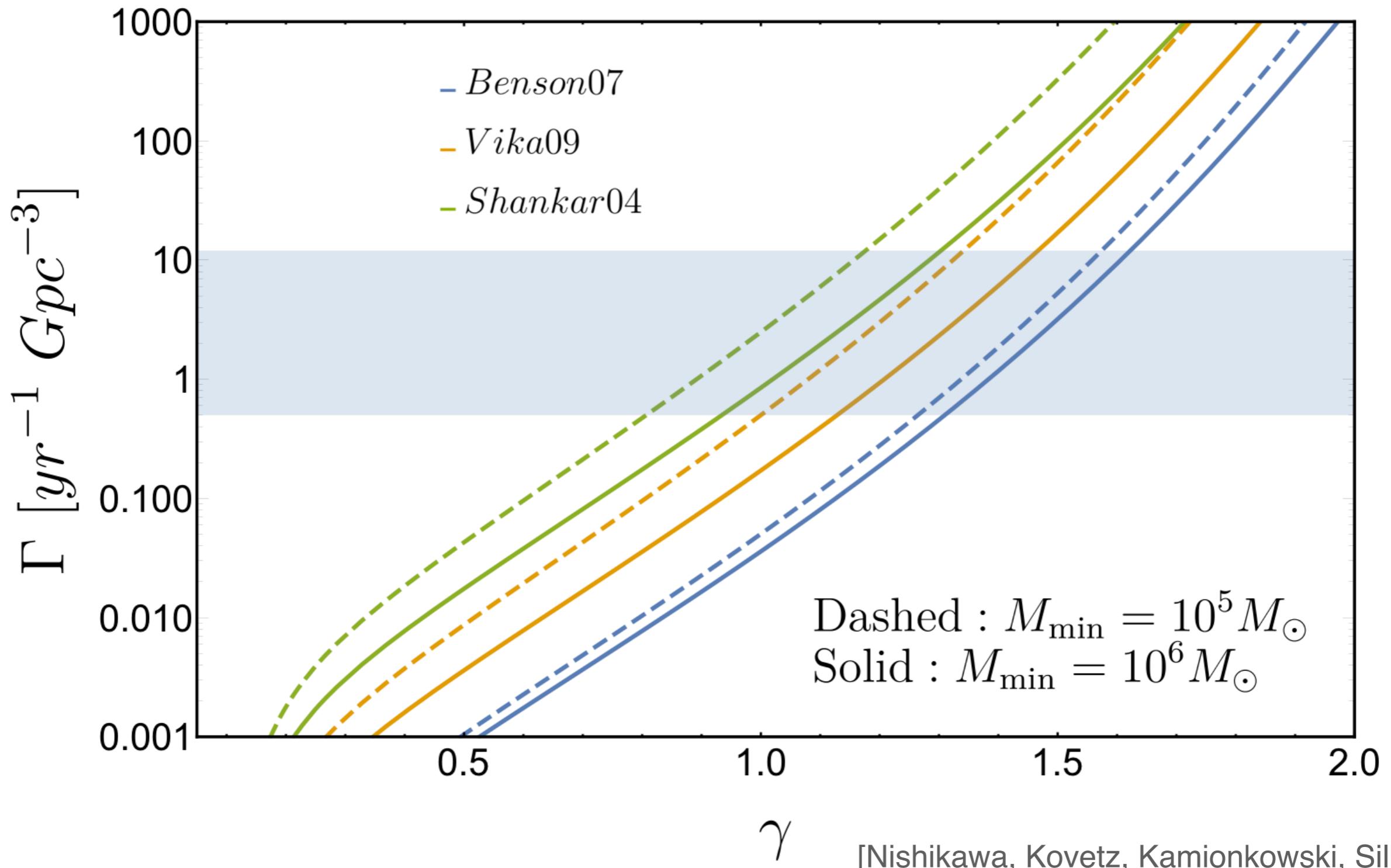
Gravitational Waves from PBHs

- ★ Look at regions of **high concentration** of dark matter.
 - Mergers of PBHs in **Galactic centres**.
 - ★ Adiabatic growth of SMBHs leads to formation of **DM spikes**.



Gravitational Waves from PBHs

★ Overall merger rate:



Gravitational Waves from PBHs



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$$M = 4 \times 10^6 M_\odot, f = 1 \text{mHz}$$

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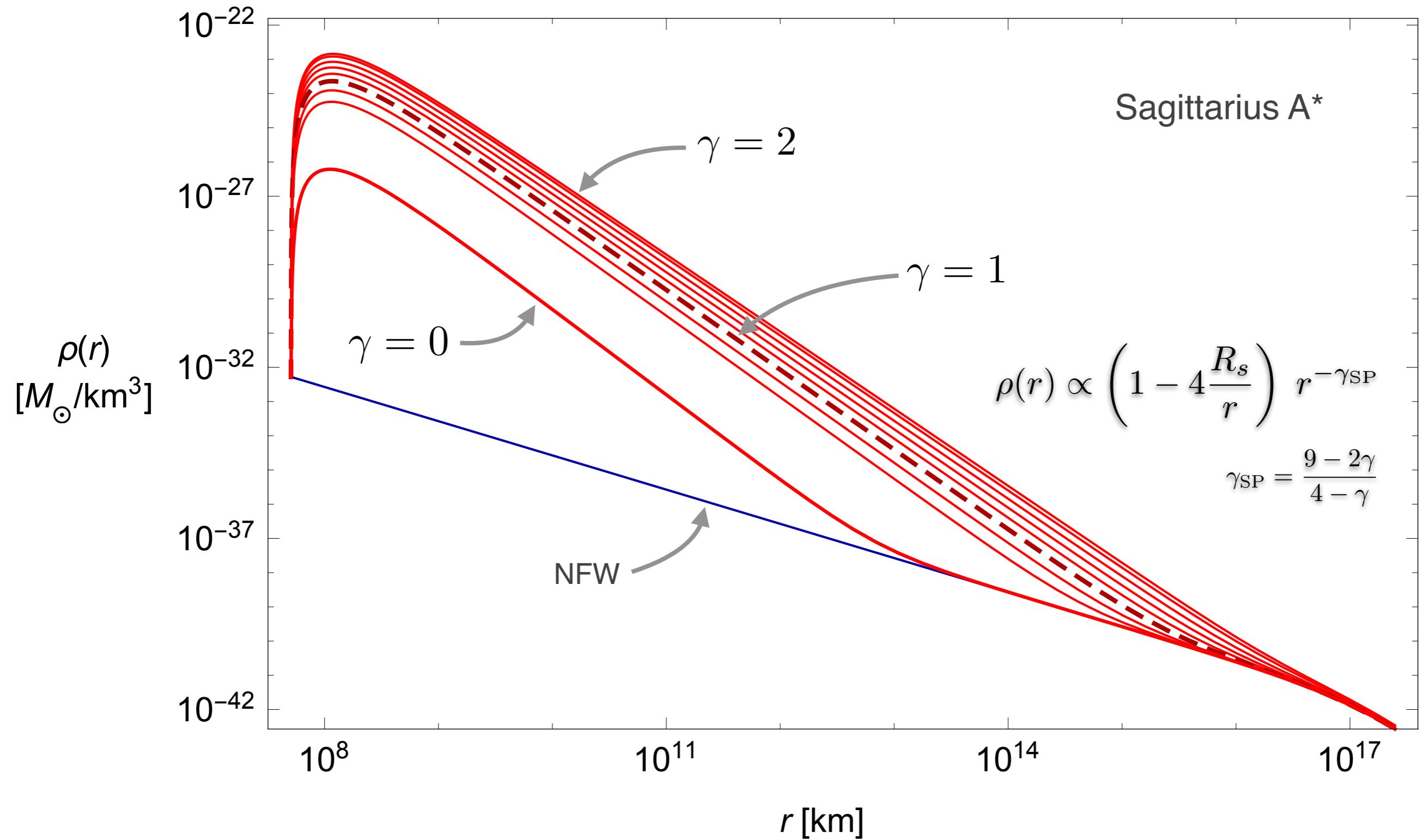
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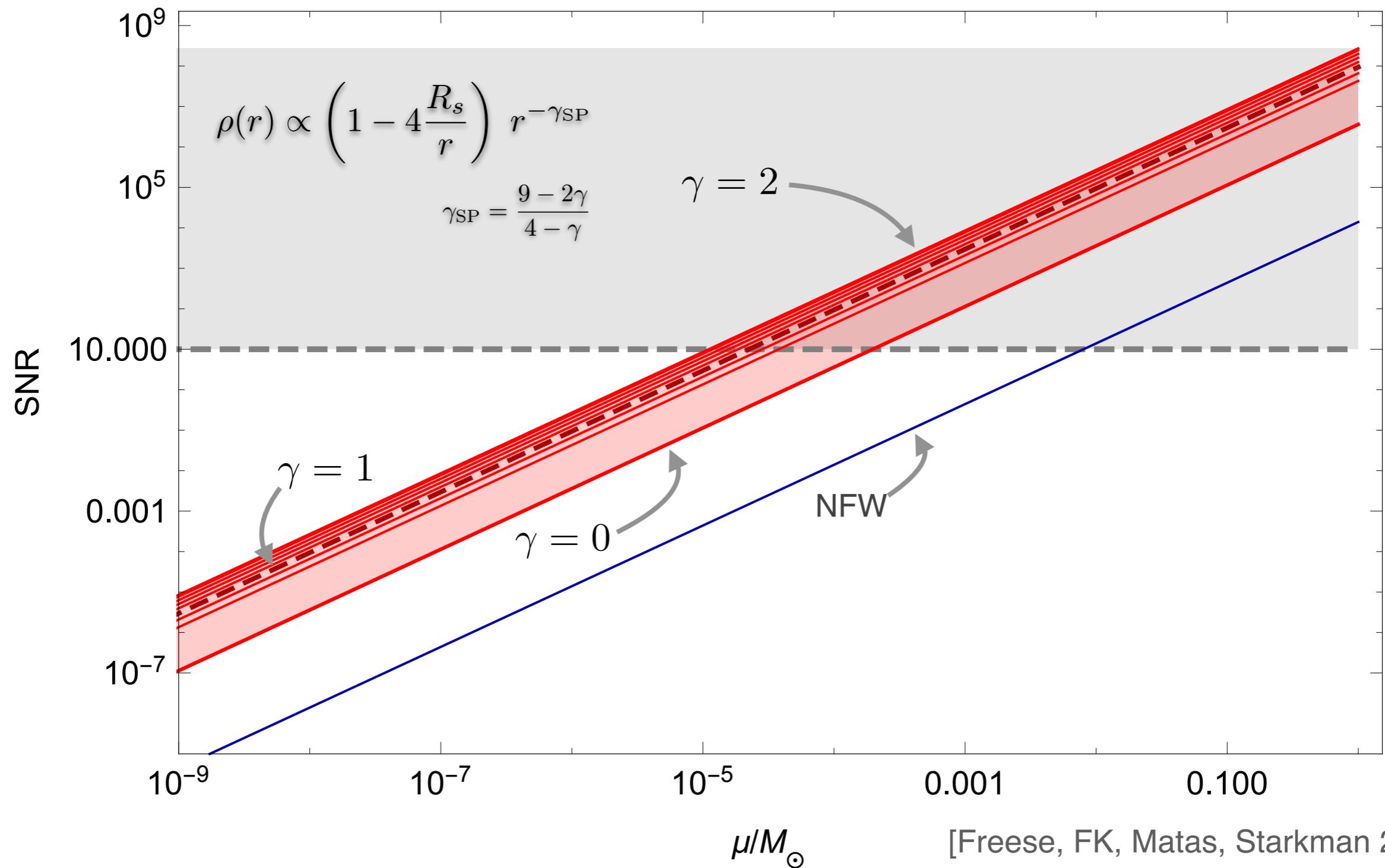
- ★ Continuous emission

Gravitational Waves from PBHs

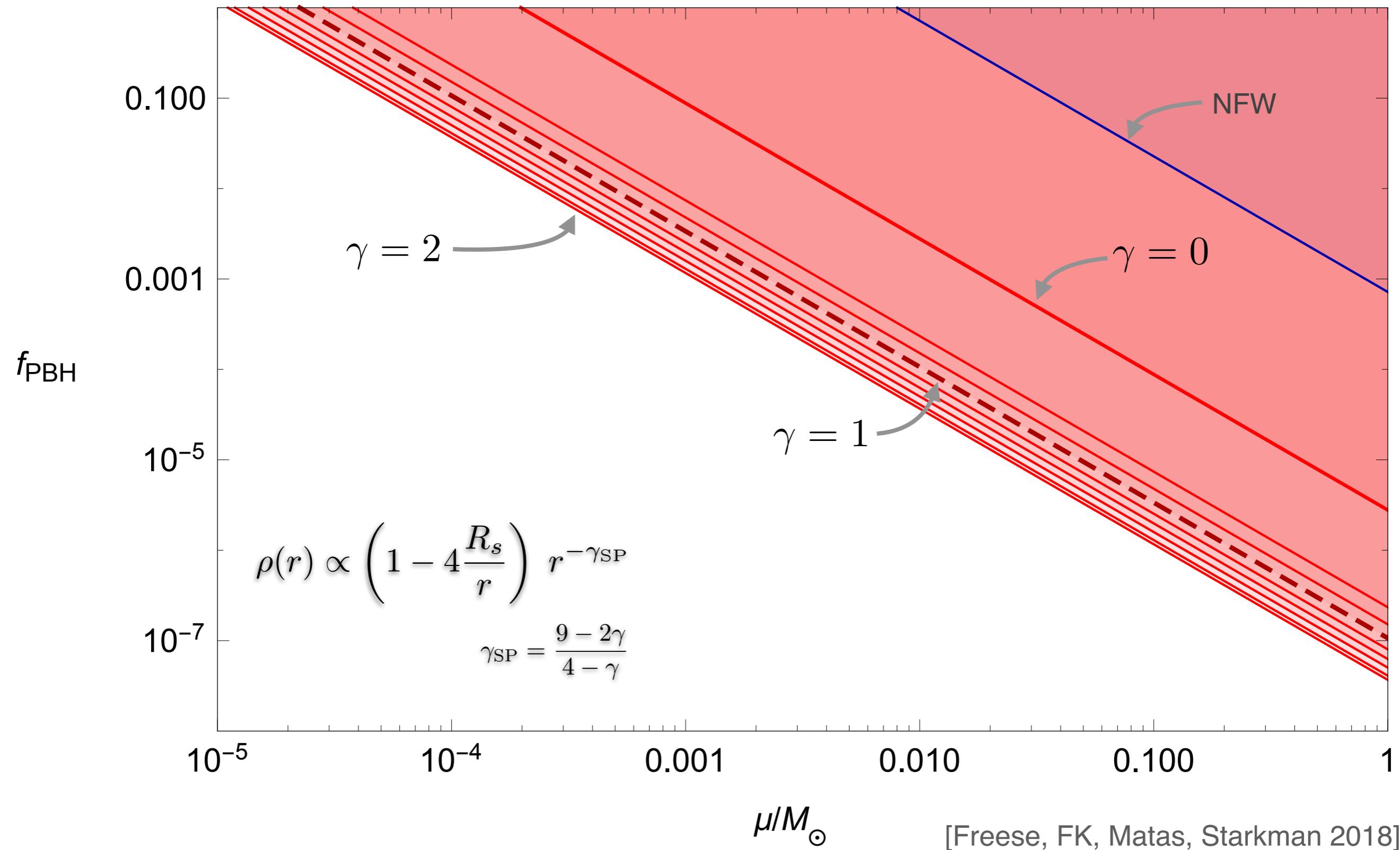


Gravitational Waves from PBHs

- ★ Make a conservative estimate for the detection prospects with **LISA**: Compute the **signal-to-noise ratio (SNR)**, assuming *circular orbits*.

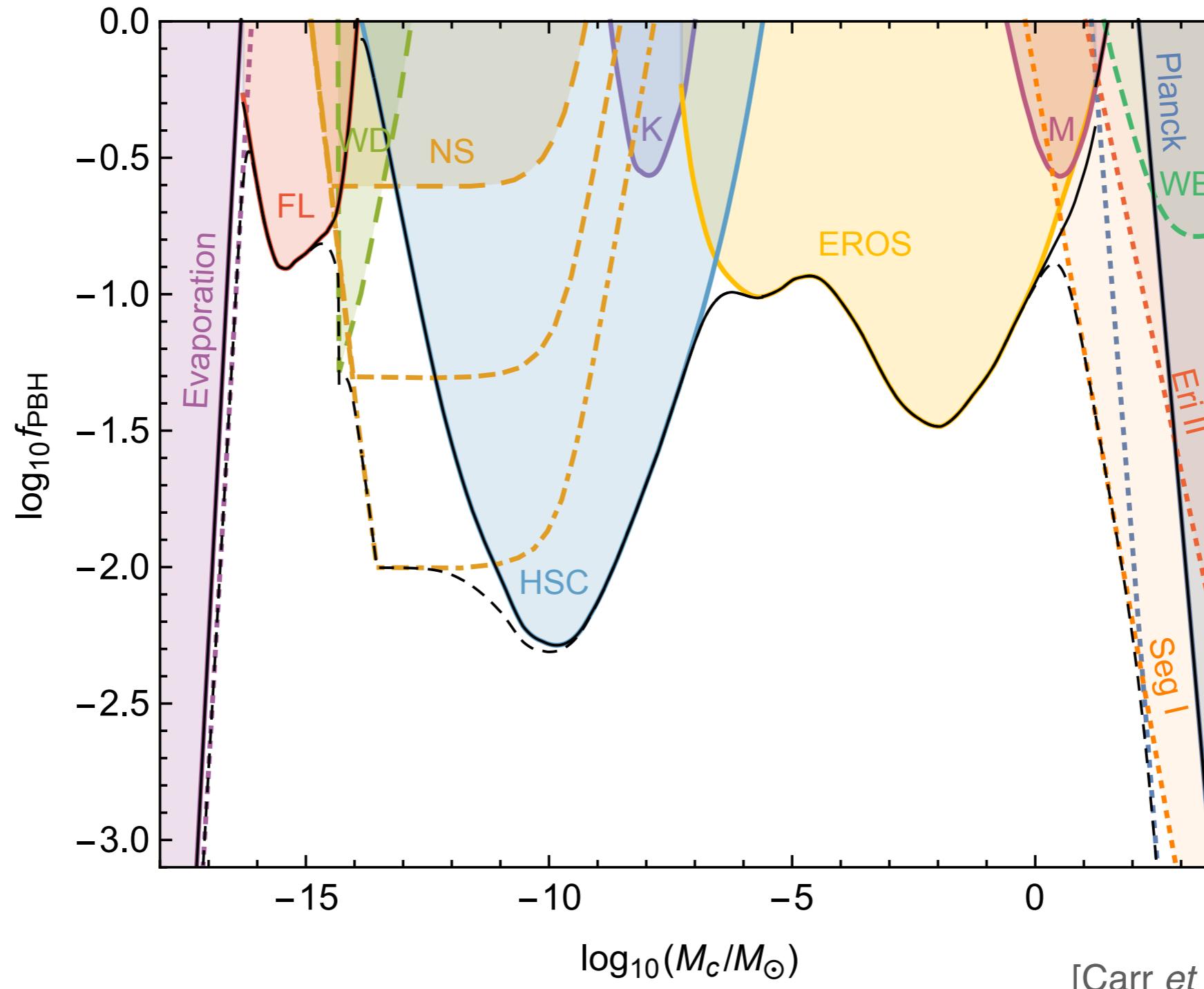


Gravitational Waves from PBHs



Constraints — Words of Caution

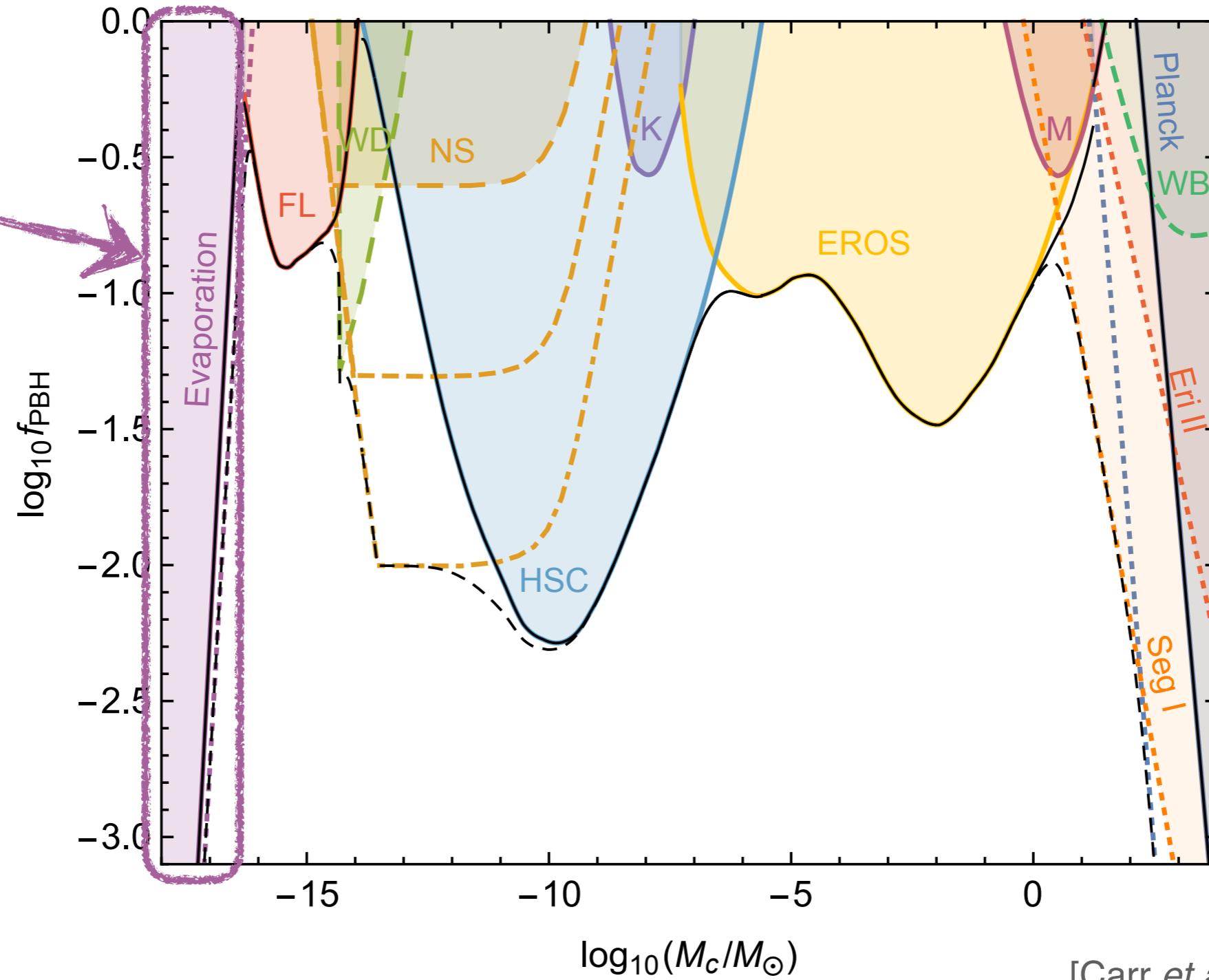
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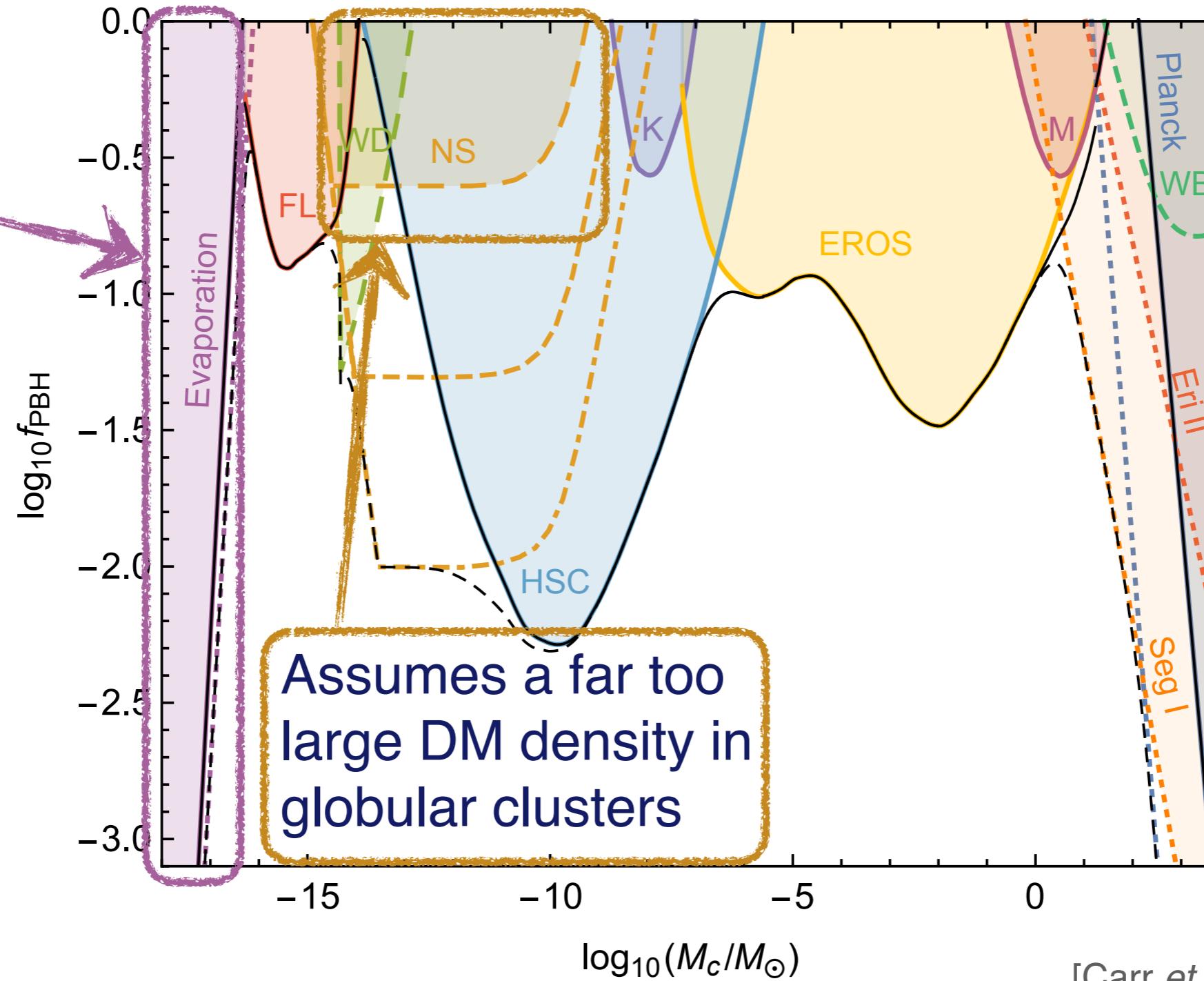
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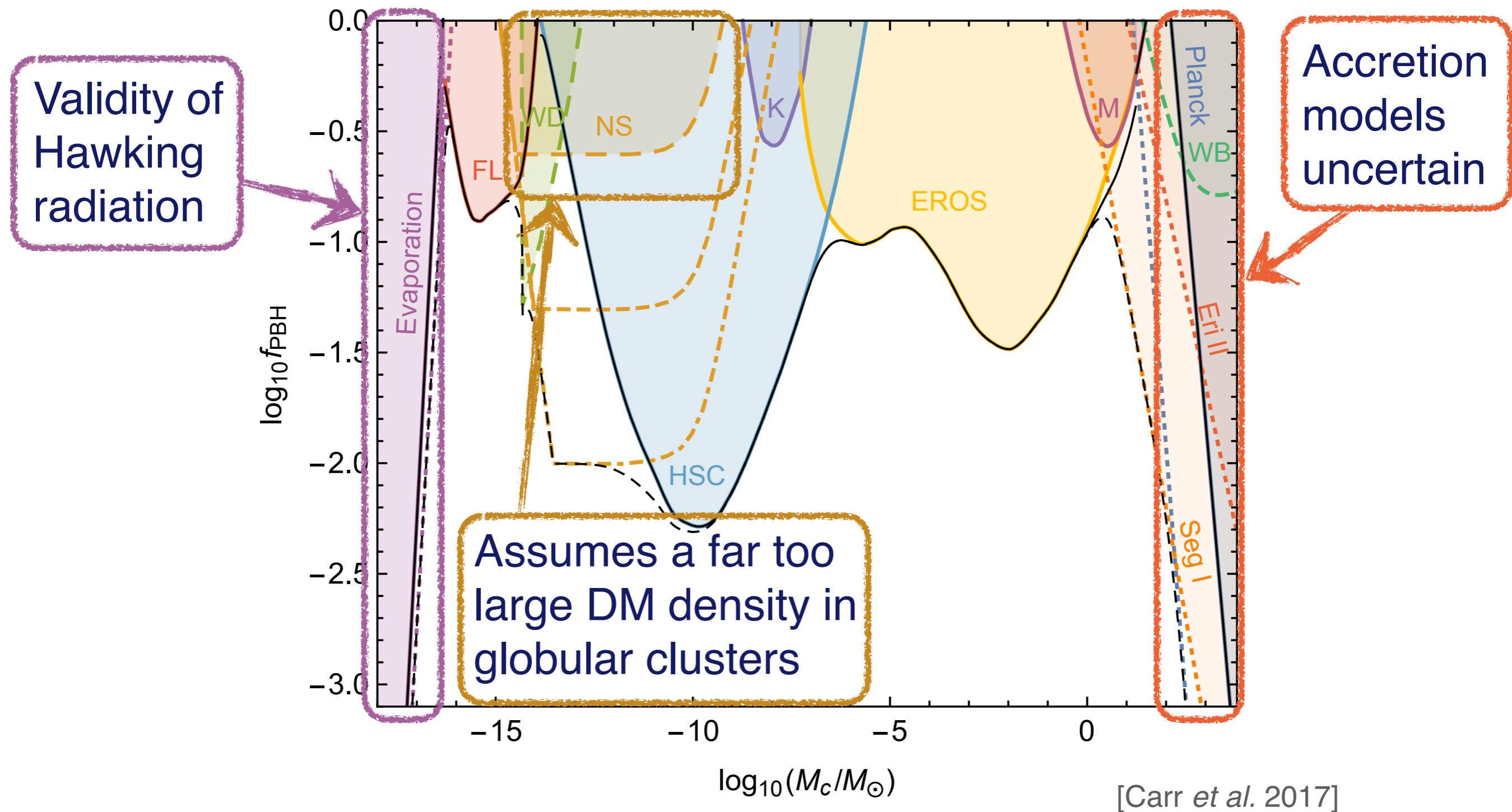
Validity of Hawking radiation



Assumes a far too large DM density in globular clusters

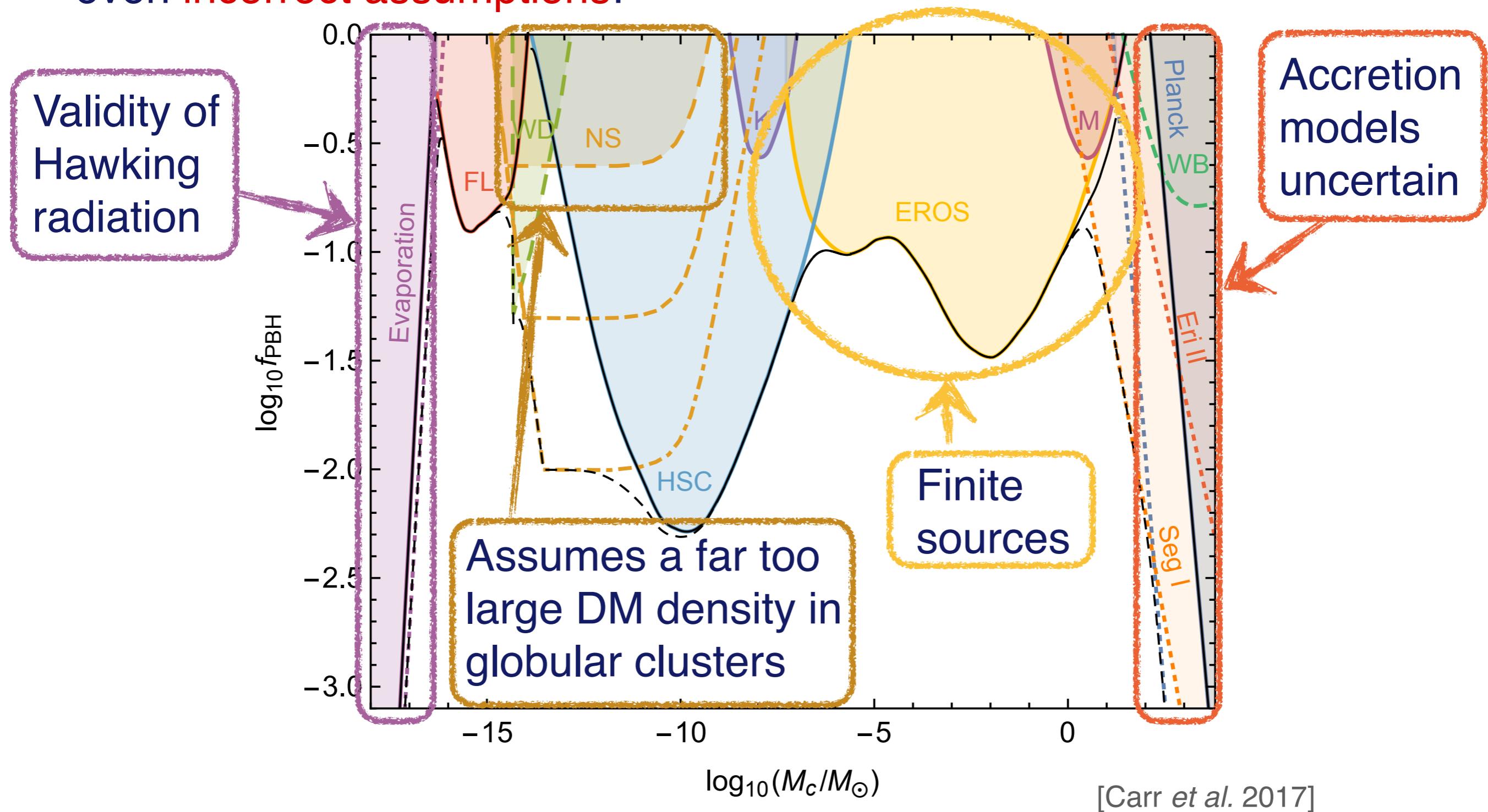
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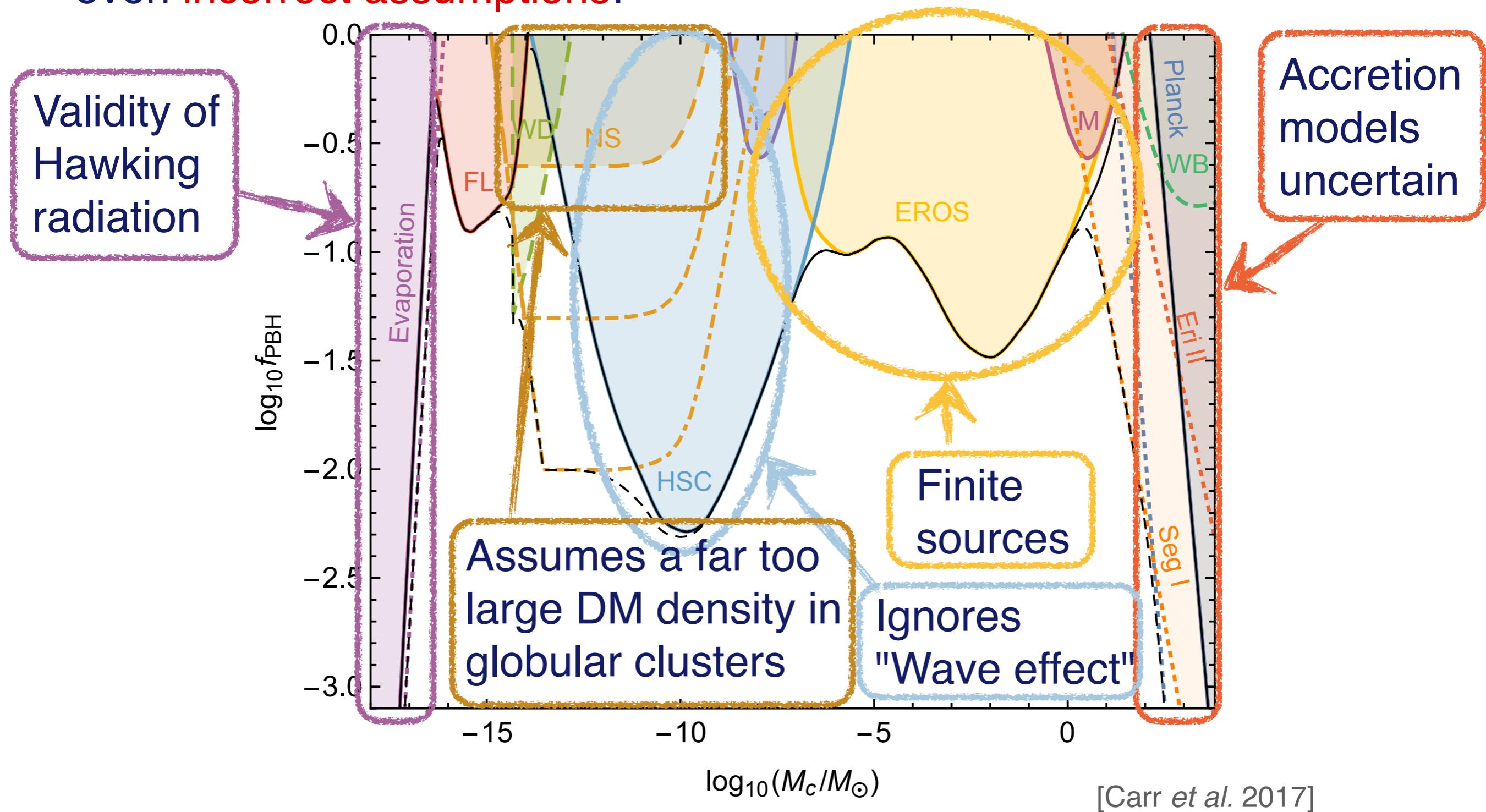
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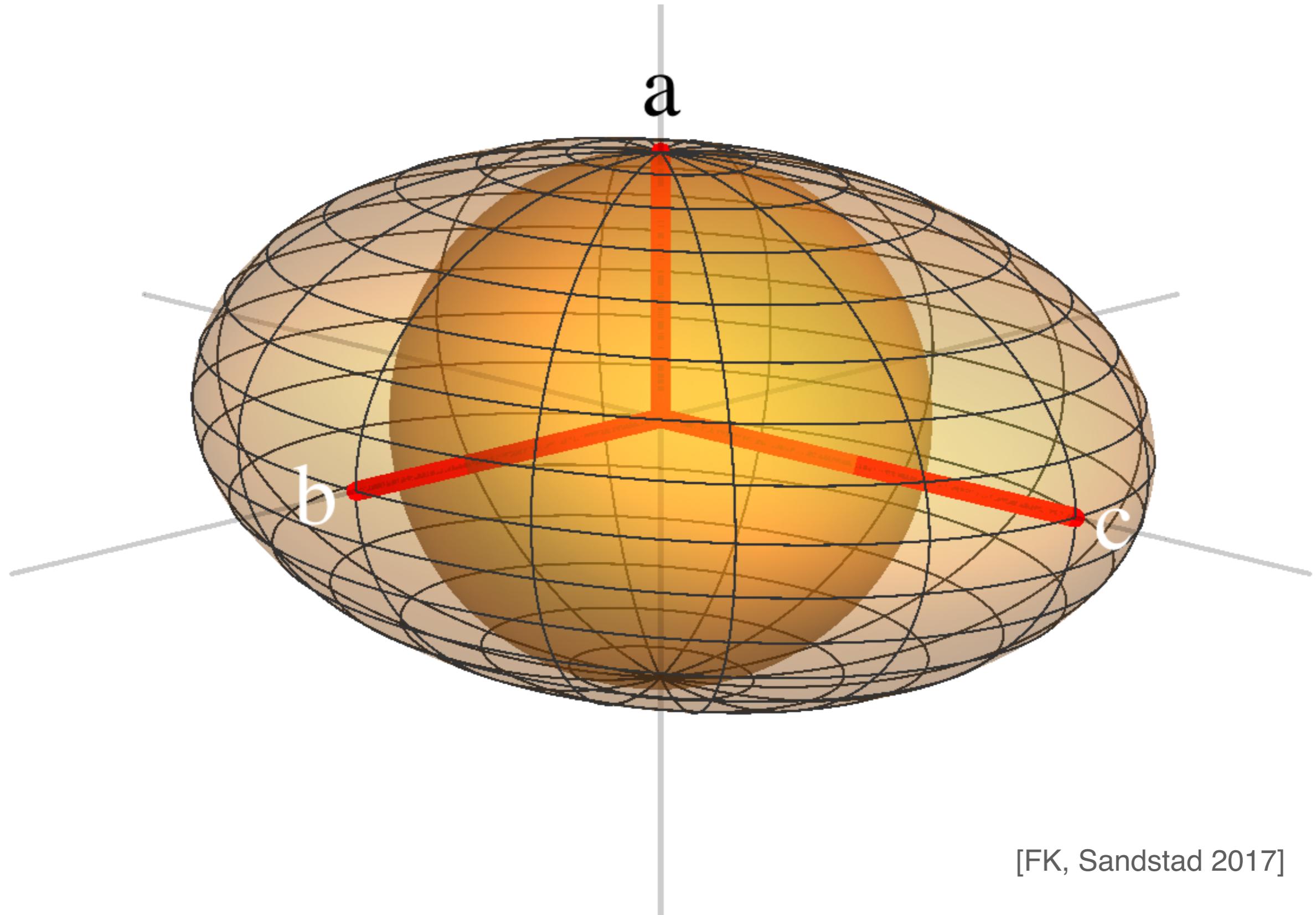


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→ We have to understand better:

- ★ Galactic dark-matter profile
- ★ Clustering
- ★ Accretion
- ★ Characteristics of the lensed sources (size, variability, ...)
- ★ Composition of "probes" in general
- ★ Velocity distribution
- ★ (Hawking radiation)
- ★ ...

Non-Spherical Effects



Non-Spherical Effects

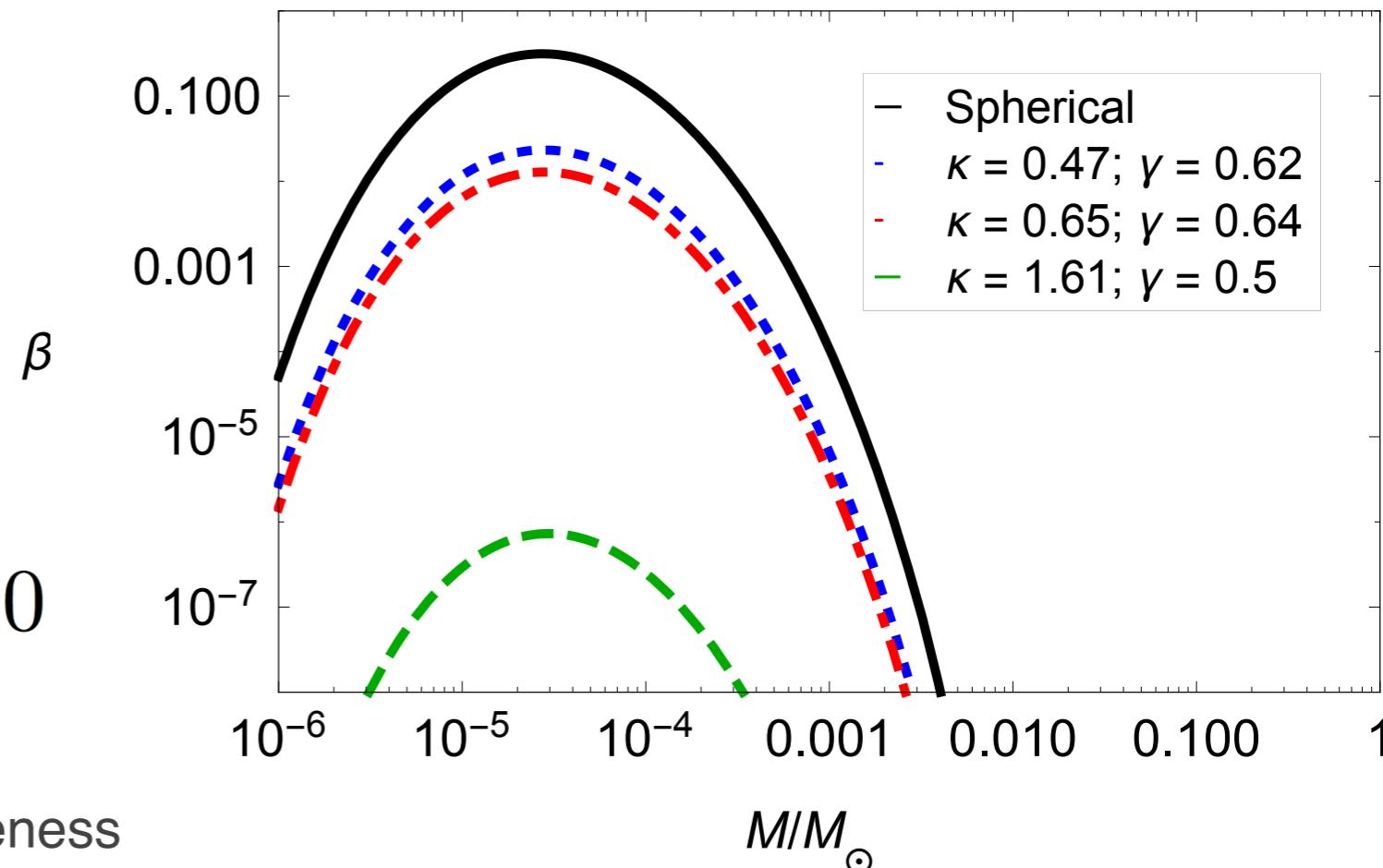
★ Non-Sphericity

[FK, Sandstad 2016]

$$\frac{\delta_{\text{ec}}}{\delta_c} \simeq 1 + \kappa \left(\frac{\sigma^2}{\delta_c^2} \right)^\gamma$$

ellipsoidal threshold
 spherical threshold
 ellipticity prolateness

$$\langle e \rangle = \frac{3\sigma}{\sqrt{10\pi}\delta}, \quad \langle p \rangle = 0$$

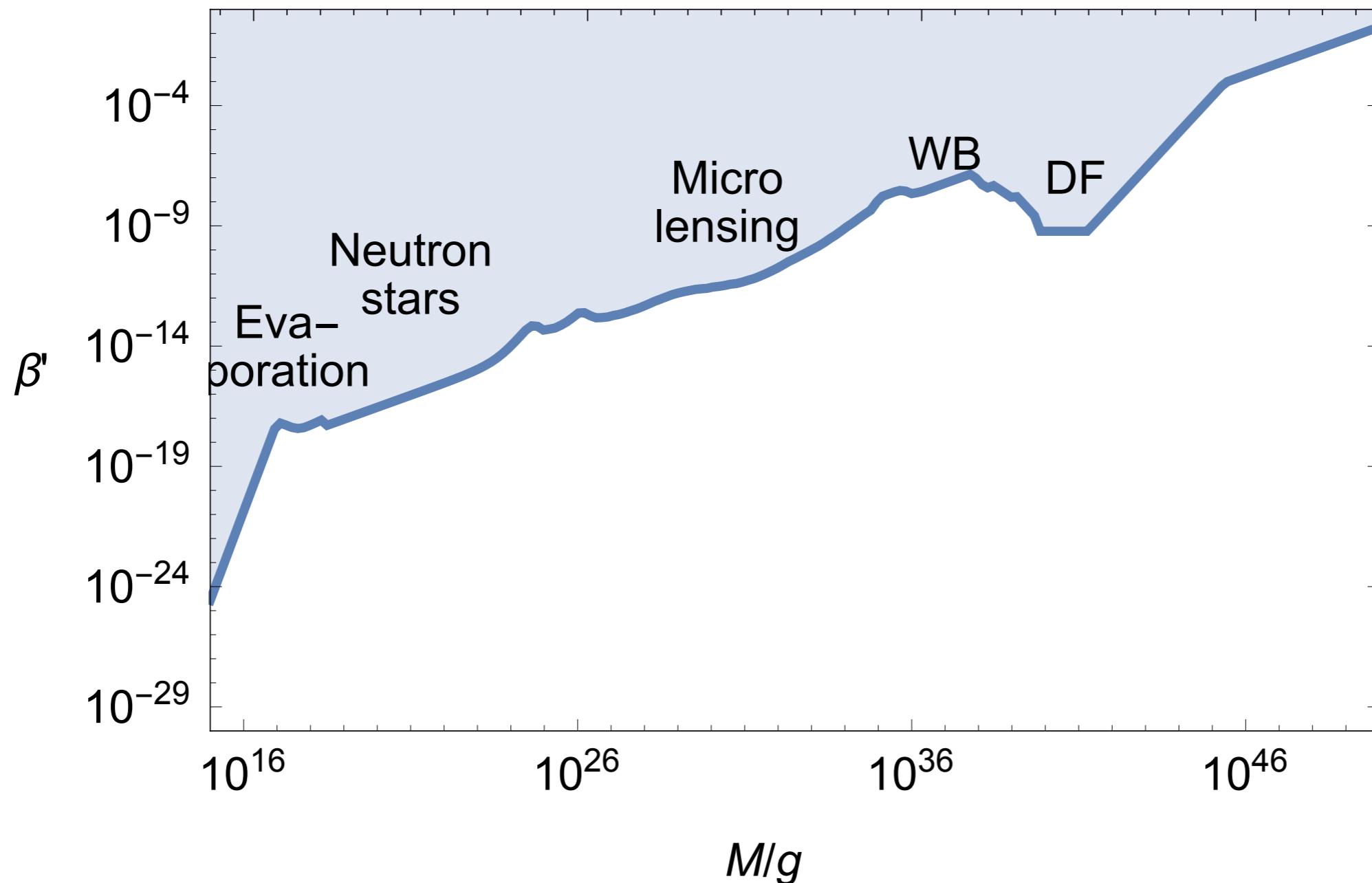


★ Simple estimate: As the collapse starts along shortest axis first,
 → consider collapse of largest enclosed sphere (green curve):

$$\frac{\delta_{\text{ec}}}{\delta_c} \simeq (1 + 3e) = 1 + \frac{9}{\sqrt{10\pi}} \left(\frac{\sigma^2}{\delta_c^2} \right)^{1/2}$$

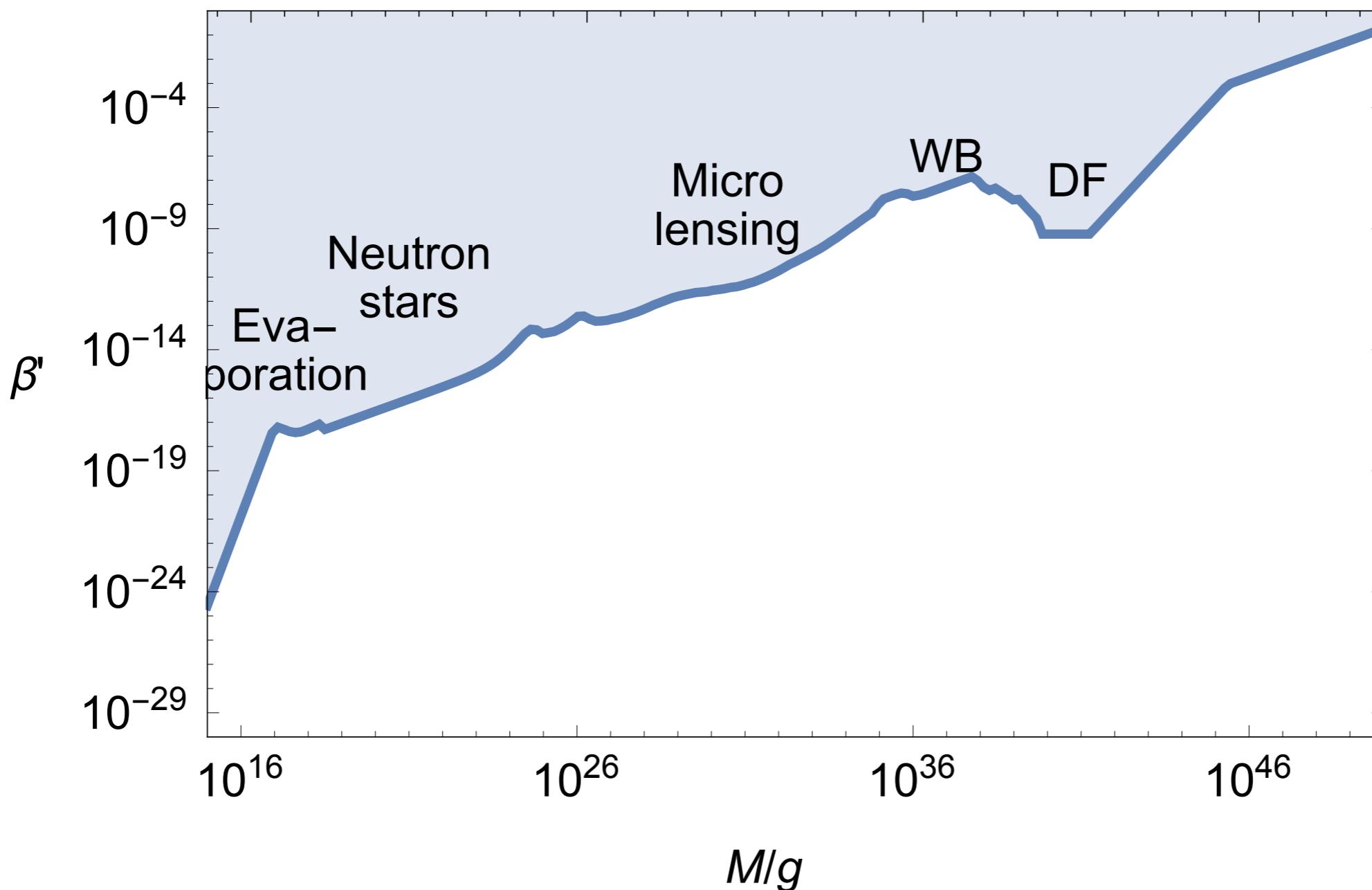
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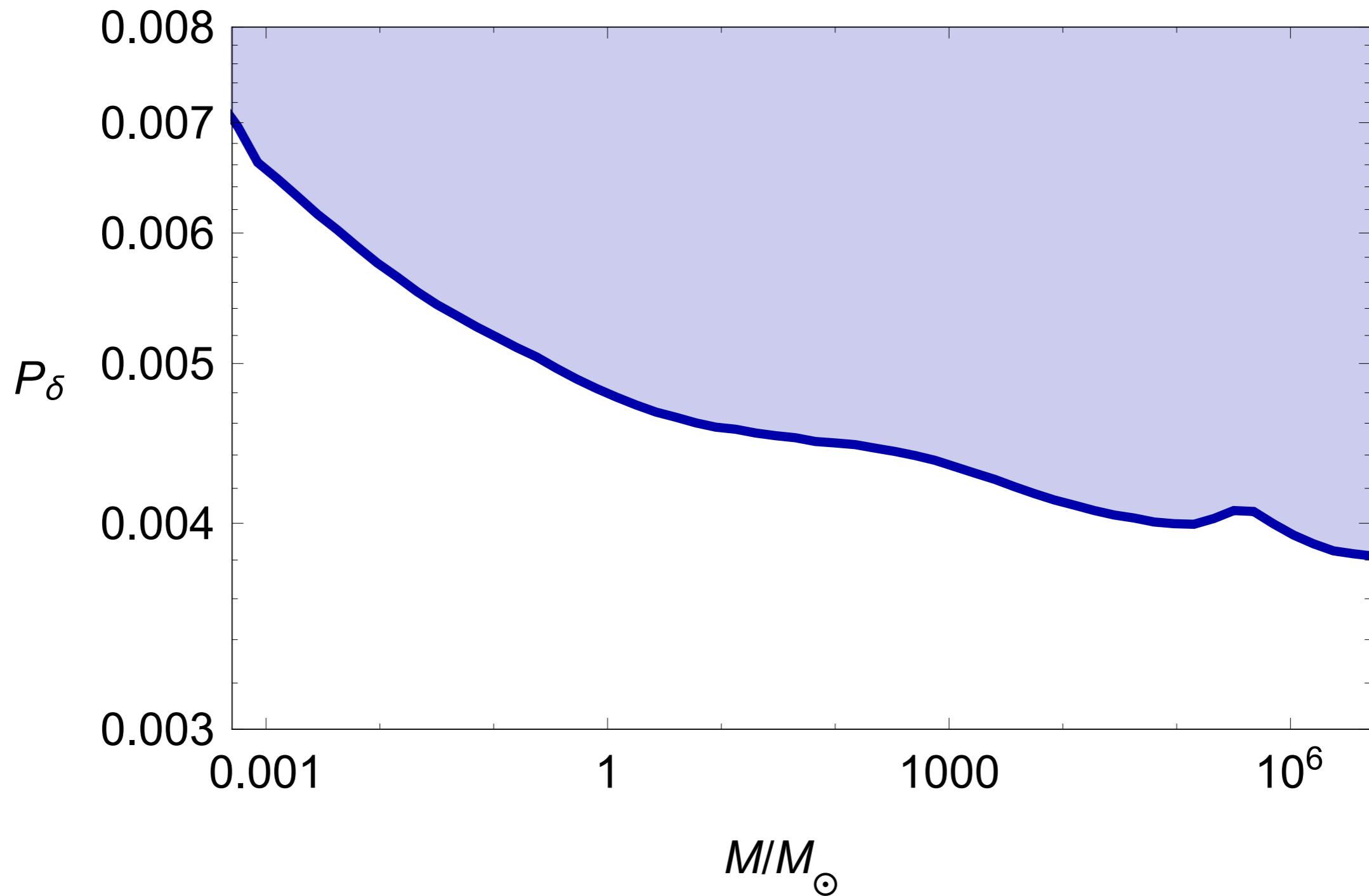
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- ★ Go back to the constraints at the time of formation:



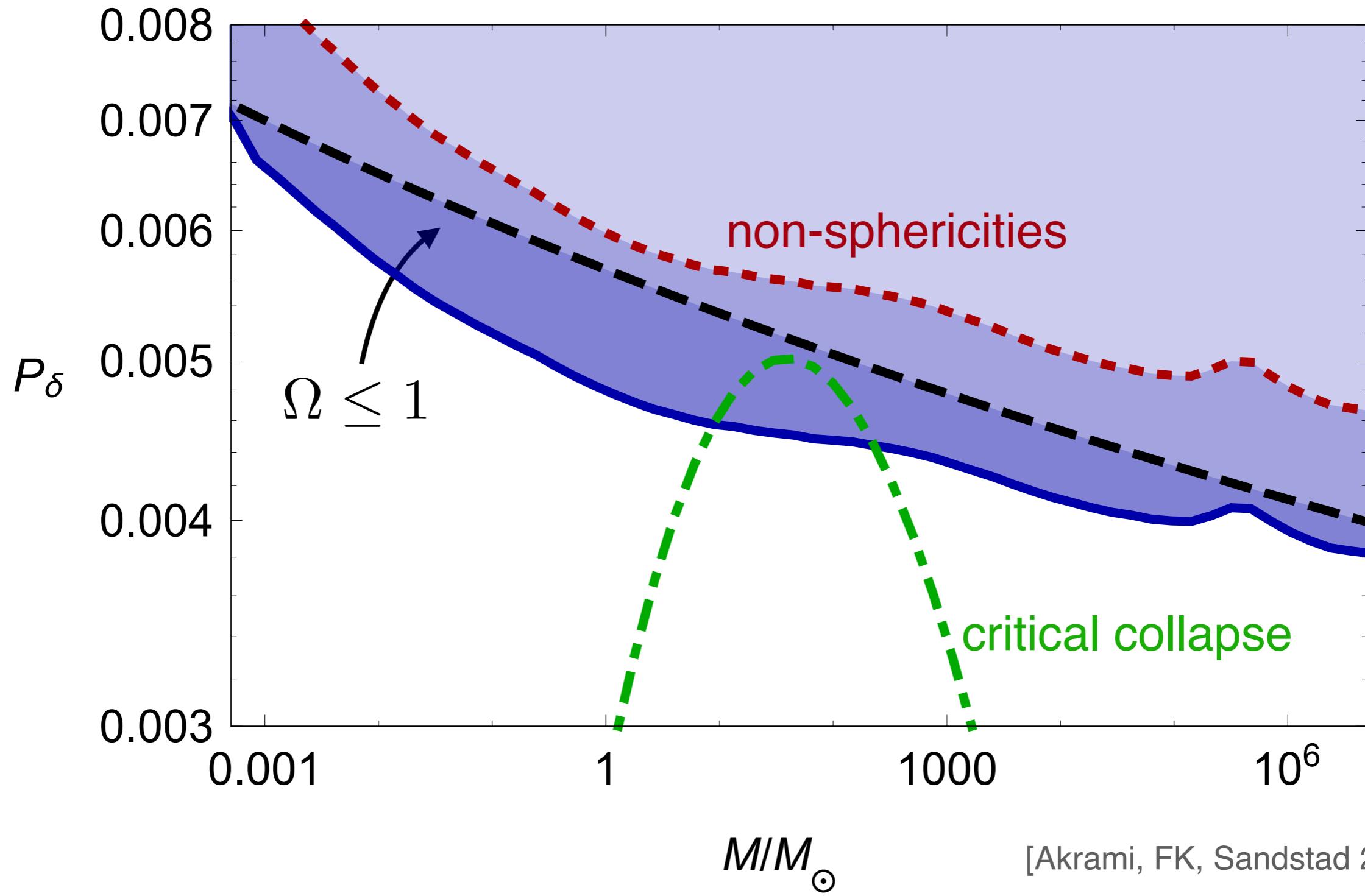
More Words of Caution

★ These constraints **naïvely** translate to:



Constraints on the Primordial Power Spectrum?

- ★ Take the uncertainty due to non-sphericities into account:



Conclusion

- ★ Primordial black holes are very **interesting!**
- ★ A detailed understanding of their **formation** is crucial.
- ★ **Gravitational-wave** signals from the **Galactic centre** may soon confirm the hypothesis that the Dark Matter is indeed comprised of primordial black holes.
- ★ Combined dark-matter scenarios (e.g. PBHs + WIMPs) can offer bright detection prospect.
- ★ Most of the primordial black holes constraints rely on **assumptions** whose **validity** is hard to quantify.