



# Amplitude analysis of $B^0_s \rightarrow K^0_S K^\pm \pi^\mp$ decays

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Workshop on multi-body charmless  $b$ -hadron decays

Funded by



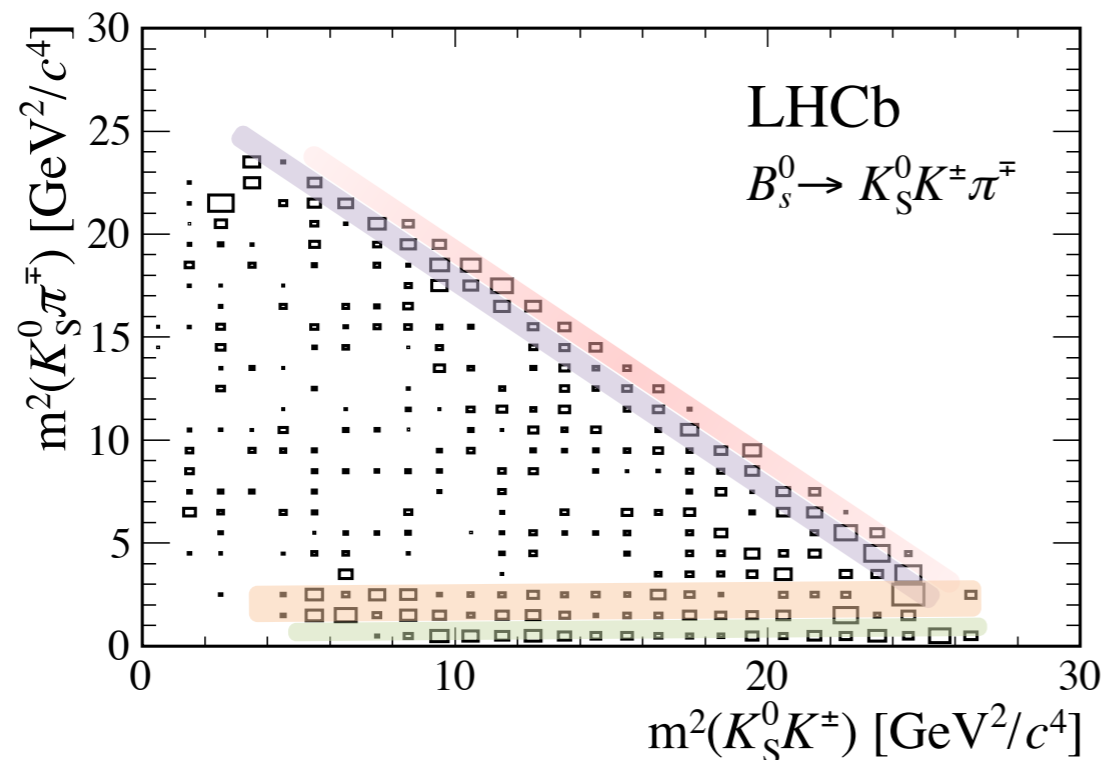
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# Amplitude analysis of $B_s^0 \rightarrow K^0 K^\pm \pi^\mp$

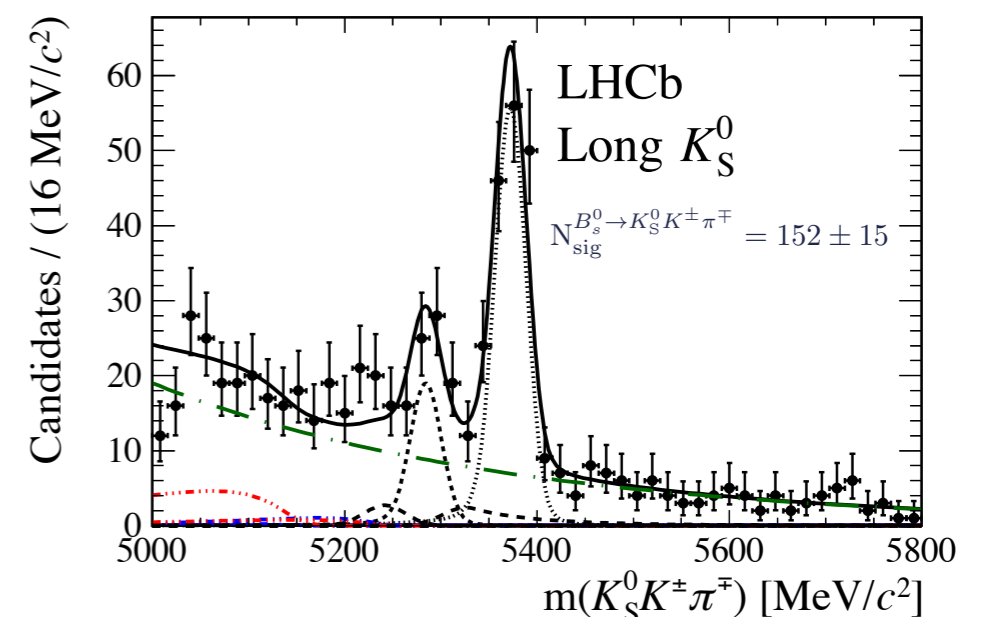
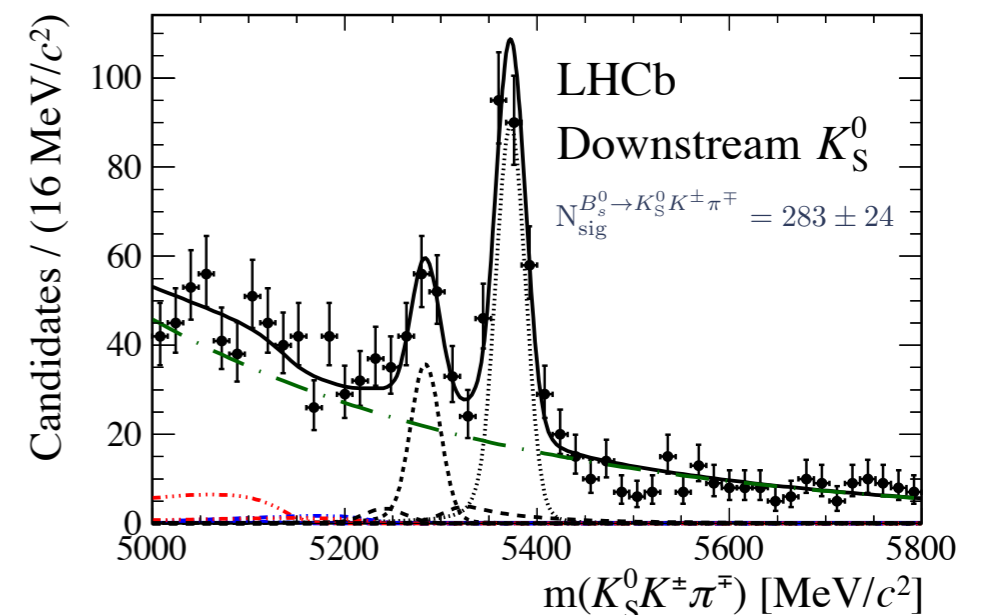
Search for  $\cancel{CP}$  in charmless 3-body decays of neutral  $B$  mesons to final states containing a  $K^0$  meson

- CKM angle  $\gamma$  using  $B_s^0 \rightarrow K^* K$  in an isospin analysis
- Non-zero  $\Delta\Gamma_s$  allows effective lifetime measurement
- U-spin multiplet  $B_s^0 \rightarrow K^{*0} K^0 (K^{*0} K^0)$  to  $B^0 \rightarrow K^* K$



Study of  $B_{(s)}^0 \rightarrow K_S^0 h^+ h'^-$  decays with first observation of  $B_s^0 \rightarrow K_S^0 K^\pm \pi^\mp$  and  $B_s^0 \rightarrow K_S^0 \pi^+ \pi^-$

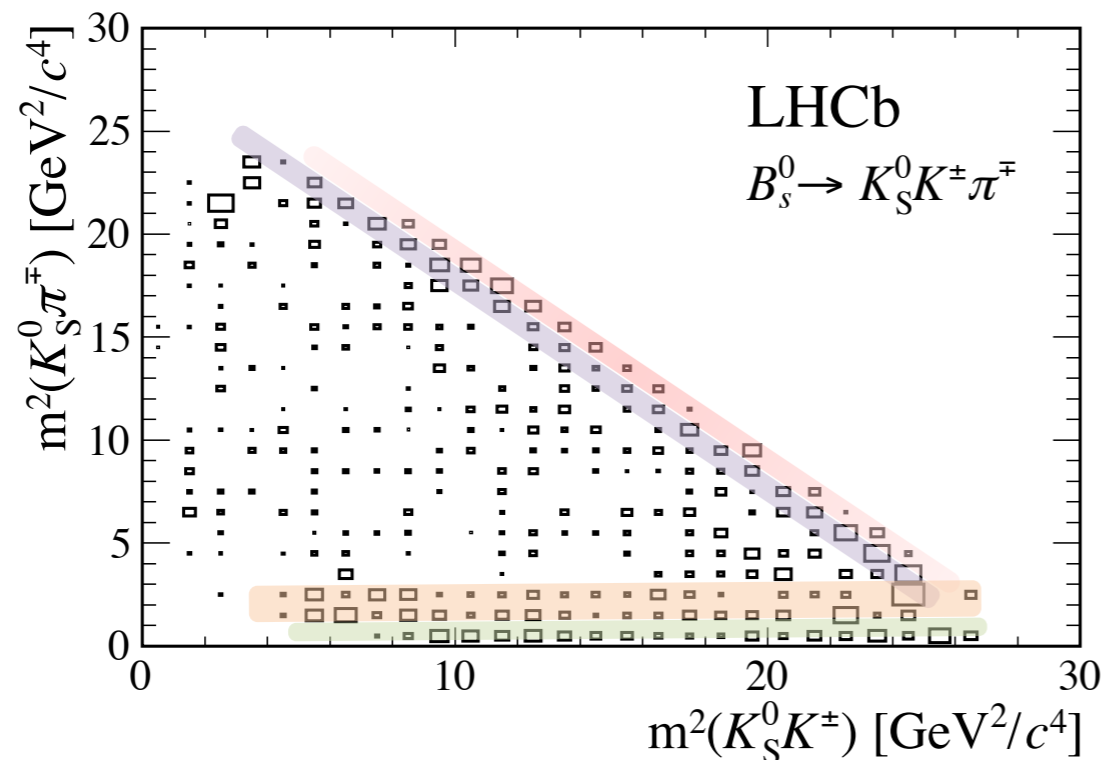
JHEP 10 (2013) 143



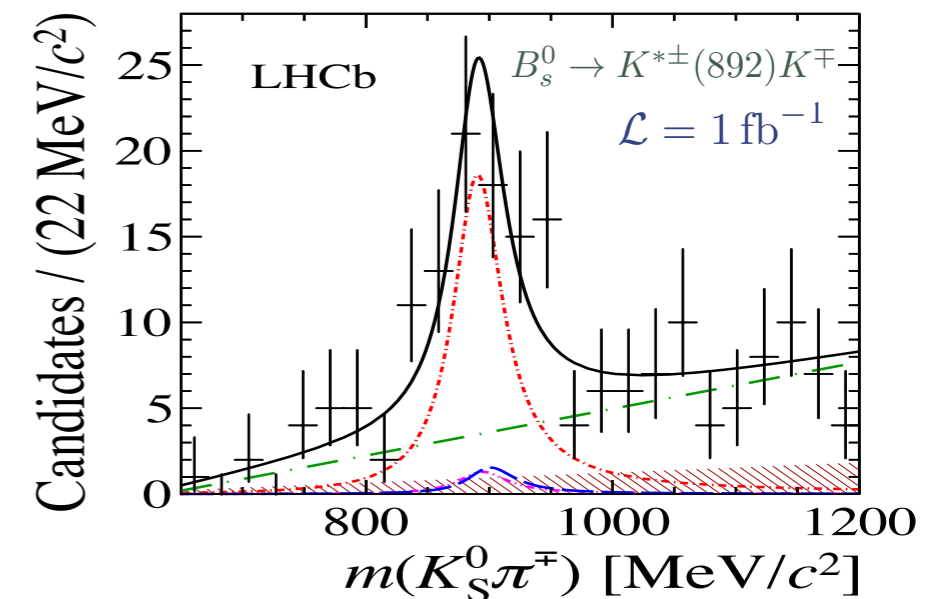
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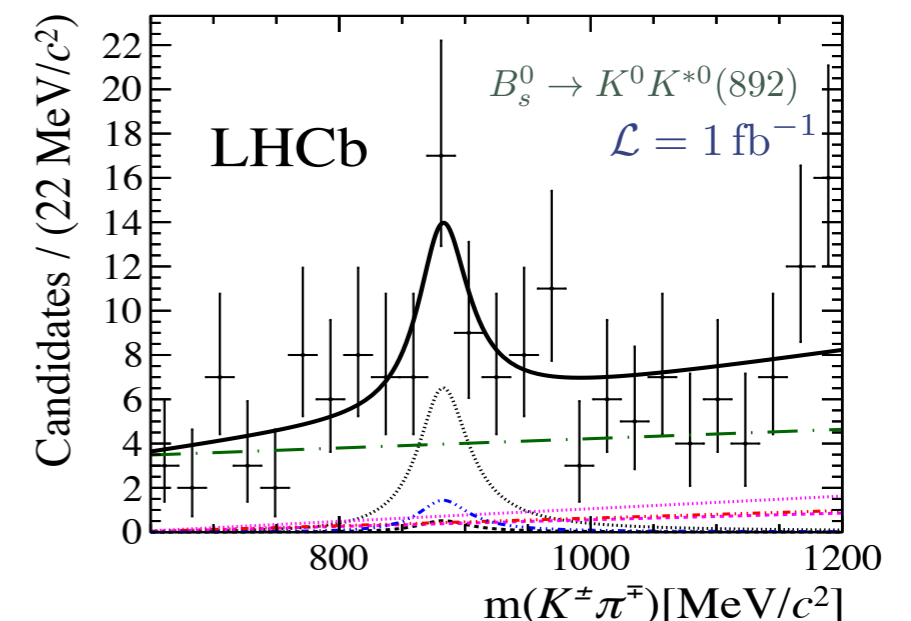
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New J.Phys. 16 (2014) 12, 123001



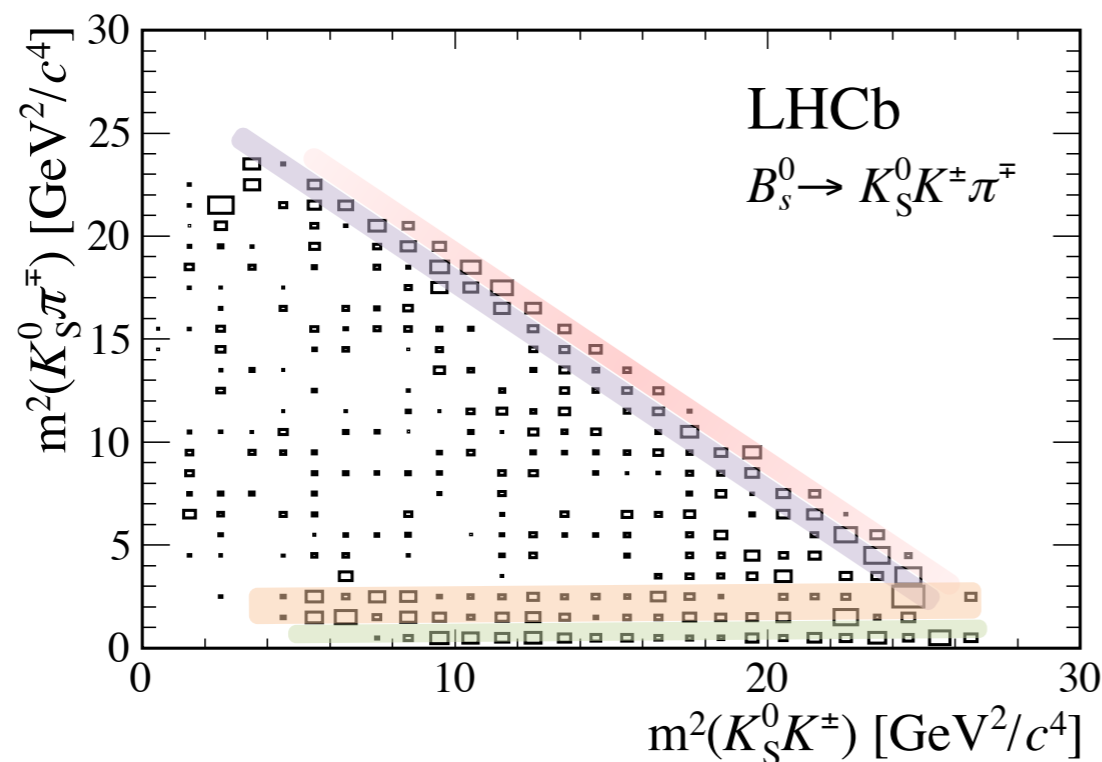
JHEP 1601 (2016) 012



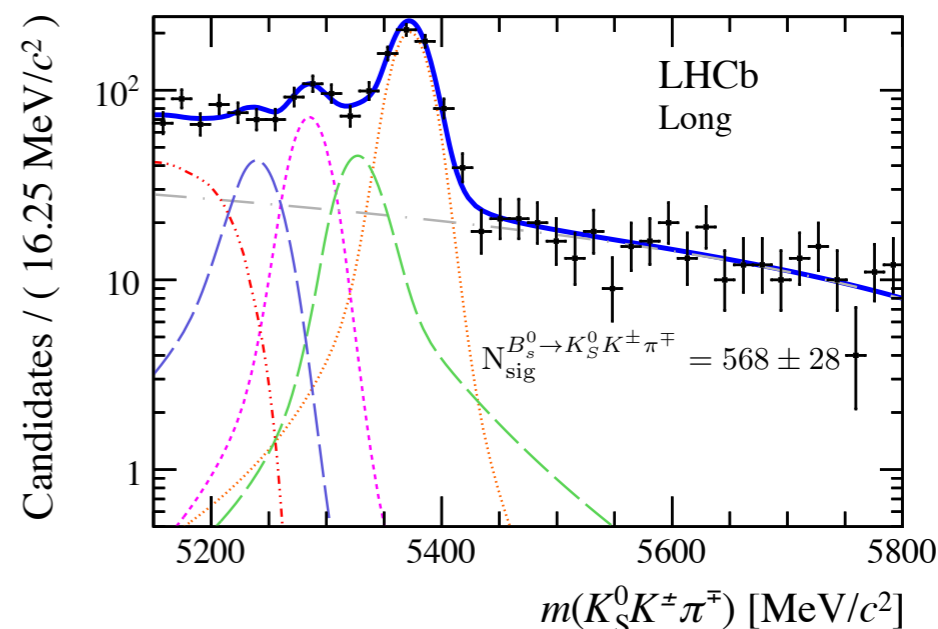
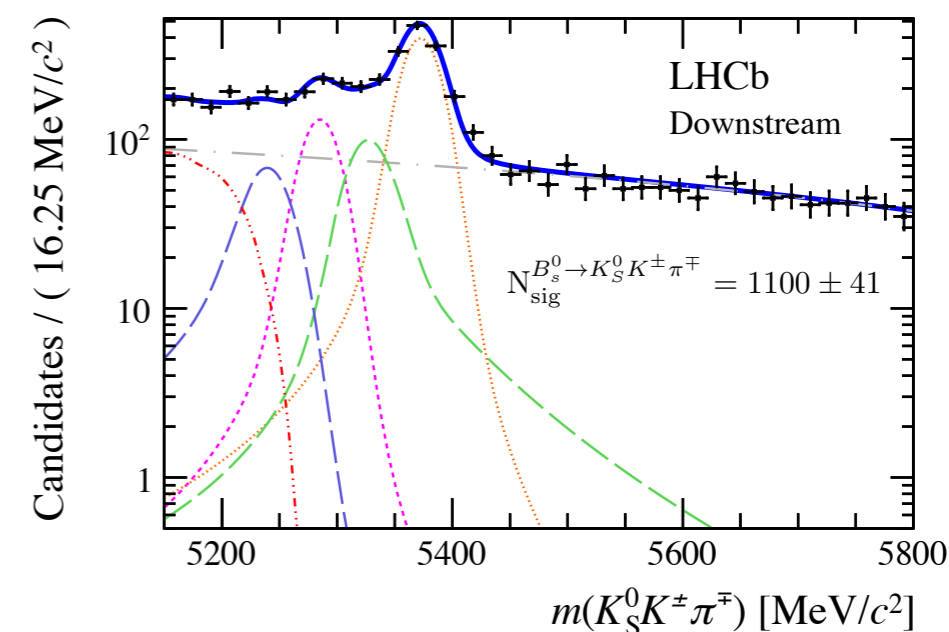
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Updated branching fraction measurements  
of  $B_{(s)}^0 \rightarrow K_S^0 h^+ h'^-$  decays  
JHEP 11 (2017) 027



# Overview of the analysis status



This talk covers some aspects of the first Dalitz analysis of  $B^0_s \rightarrow K^0_S K^\pm \pi^\mp$  decays

[ $3 \text{ fb}^{-1}$  Run-I (2011/12) at 7/8 TeV]

- “Effective” untagged time-integrated Dalitz-Plot analysis strategy has been used  
[limited statistics for flavour tagging]
- Dataset selection, efficiency and background modelling common to all  $K^0_S h^+ h^-$  modes  
[optimised FoM for DP analysis]
- Dalitz-plot fitting results and systematics  
[BR measurements and first observations of the  $K\pi$  S-wave contribution]





# Amplitude fit model features for $B^0_s \rightarrow K^0_S K^\pm \pi^\mp$ decays

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[Non-public results]:  $\mathcal{L} = 3\text{fb}^{-1} - 2011 + 2012$  dataset

**Method: effective untagged time-integrated analysis**

[LHCb-ANA-2014-045]

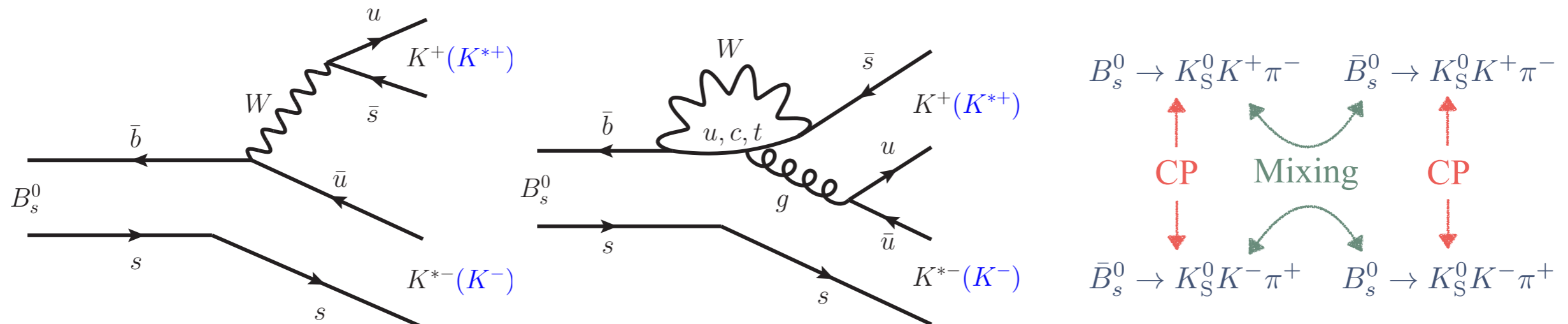


# $B_s^0 \rightarrow K^0 K^\pm \pi^\mp$ decay features

Decay channel  $B_s^0 \rightarrow K_S^0 K^\pm \pi^\mp$  corresponds in fact to four different DP's:

$B_s^0(\bar{B}_s^0) \rightarrow K_S^0 K^+ \pi^-$  and  $B_s^0(\bar{B}_s^0) \rightarrow K_S^0 K^- \pi^+$  final states.

Leading diagrams are dominated by either  $K^*(892)$  or  $K^*(1430)$  contributions:



| $\bar{B}_s^0 \rightarrow \bar{K}^0 K^+ \pi^-$ | Reference             |                        | $\bar{B}_s^0 \rightarrow \bar{K}^0 K^- \pi^+$ | Reference             |                        |
|---|-----------------------|------------------------|---|-----------------------|------------------------|
|   | PRD 89 (074025)       | arXiv:1401.5948        |   | PRD 89 (074025)       | arXiv:1401.5948        |
| $K^{*0} \bar{K}^0$                            | $1.5^{+2.4}_{-0.9}$   | $0.7^{+1.7}_{-0.5}$    | $\bar{K}^{*0} K^0$                            | $3.8^{+0.8}_{-0.7}$   | $2.3^{+0.6}_{-0.5}$    |
| $K^{*-} K^+$                                  | $3.5^{+0.7}_{-0.7}$   | $2.3^{+0.6}_{-0.5}$    | $K^{*+} K^-$                                  | $2.6^{+2.7}_{-1.1}$   | $1.3^{+2.0}_{-0.9}$    |
| $K_0^{*0}(1430) \bar{K}^0$                    | $0.6^{+0.9}_{-0.4}$   | $0.5^{+1.2}_{-0.4}$    | $\bar{K}_0^{*0}(1430) K^0$                    | $14.5^{+3.3}_{-2.9}$  | $16.6^{+5.1}_{-4.3}$   |
| $K_0^{*-}(1430) K^+$                          | $14.5^{+3.2}_{-2.9}$  | $15.5^{+4.5}_{-3.9}$   | $K_0^{*+}(1430) K^-$                          | $1.0^{+1.0}_{-0.4}$   | $0.9^{+1.4}_{-0.5}$    |
| Non resonant                                  | $23.8^{+9.9}_{-6.7}$  | $12.3^{+12.6}_{-6.3}$  | Non Resonant                                  | $24.2^{+0.9}_{-5.1}$  | $12.9^{+13.2}_{-6.6}$  |
| Total   | $35.3^{+15.7}_{-9.8}$ | $33.7^{+20.9}_{-12.0}$ | Total   | $36.7^{+14.9}_{-9.0}$ | $34.2^{+21.1}_{-12.0}$ |

Theory predictions

# $B^0_s \rightarrow K^0 K^\pm \pi^\mp$ decay-time formalism

The decay-time distribution for  $B^0_s$  and  $\bar{B}^0_s$  meson decays to a final state  $f$  (e.g.  $B^0_s \rightarrow K^0_s K^+ \pi^-$ ) can be written as:

$$\frac{d}{dt} \Gamma_{\bar{B}^0_s \rightarrow f}(t) = \frac{\mathcal{N}_f e^{-t/\tau(B^0_s)}}{2\tau(B^0_s)} \left[ \cosh\left(\frac{\Delta\Gamma_s t}{2}\right) + S_f \sin(\Delta m_s t) - C_f \cos(\Delta m_s t) + A_f^{\Delta\Gamma_s} \sinh\left(\frac{\Delta\Gamma_s t}{2}\right) \right]$$

$$\frac{d}{dt} \Gamma_{B^0_s \rightarrow f}(t) = \frac{\mathcal{N}_f e^{-t/\tau(B^0_s)}}{2\tau(B^0_s)} \left[ \cosh\left(\frac{\Delta\Gamma_s t}{2}\right) - S_f \sin(\Delta m_s t) + C_f \cos(\Delta m_s t) + A_f^{\Delta\Gamma_s} \sinh\left(\frac{\Delta\Gamma_s t}{2}\right) \right]$$

$$S_f \equiv \frac{2\Im(\lambda_f)}{1 + |\lambda_f|^2}$$

$$C_f \equiv \frac{1 - |\lambda_f|^2}{1 + |\lambda_f|^2}$$

$$A_f^{\Delta\Gamma_s} \equiv -\frac{2\Re(\lambda_f)}{1 + |\lambda_f|^2}$$

$$\lambda_f = \left| \frac{\bar{A}_f}{A_f} \right| e^{i(\phi_s^f + \delta_f)}$$

In the case of  $B^0_s$  decays, the integration between zero and infinity leads to :

$$\mathcal{N}_f = \left( |A_f|^2 + |\bar{A}_f|^2 \right) \times \frac{1 - y^2}{1 + y A_f^{\Delta\Gamma_s}}$$

**Premise:** additional information on the phases between amplitudes from the  $A^{\Delta\Gamma}$  term.

$$*y = \tau(B^0_s) \Delta\Gamma_s / 2$$



# $B^0_s \rightarrow K^0 K^\pm \pi^\mp$ decay-time formalism

The additional final state has a similar decay time equation. Hence, one can access:

$$\begin{aligned} \frac{\mathcal{N}_{\bar{f}}}{\mathcal{N}_f} &= \frac{(|A_{\bar{f}}|^2 + |\bar{A}_{\bar{f}}|^2)(1 - y^2)/(1 + yA_{\bar{f}}^{\Delta\Gamma_s})}{(|A_f|^2 + |\bar{A}_f|^2)(1 - y^2)/(1 + yA_f^{\Delta\Gamma_s})} \\ &= \frac{1 + yA_f^{\Delta\Gamma_s}}{1 + yA_{\bar{f}}^{\Delta\Gamma_s}} = \frac{1 + R_f^2 - 2yR_f \cos(\phi_s^f + \delta_f)}{1 + R_f^2 - 2yR_f \cos(\phi_s^f - \delta_f)} \end{aligned}$$

- Even in absence of ~~CP~~ in decay, in general  $N_f \neq N_{\bar{f}}$
- With no CP in decay, the asymmetry between  $N_f$  and  $N_{\bar{f}}$  is limited to  $2yR_f/(1+R_f^2)$
- If  $\cos(\phi_s + \delta) = \cos(\phi_s - \delta) \rightarrow$  no ~~CP~~ in the interference between mixing and decay.

In this framework different Dalitz plot analyses can be performed:

Method I: Untagged and time integrated  
Method II: Untagged and time-dependent  
Method III: Tagged time-dependent

Sensitivity studies in a non-LHCb paper is being performed. Results for  $B^0_s \rightarrow K^0_S \pi \pi$

C14-07-02 arXiv:1411.2018

# $B^0_s \rightarrow K^0 K^\pm \pi^\mp$ Dalitz-plot analysis

Note that for  $B^0_s \rightarrow K^0_s K^\pm \pi^\mp$  decays there are four amplitudes, which even in the absence of  $\mathcal{CP}$ , two independent amplitudes remain,  $A_f$  and  $\bar{A}_f$ .

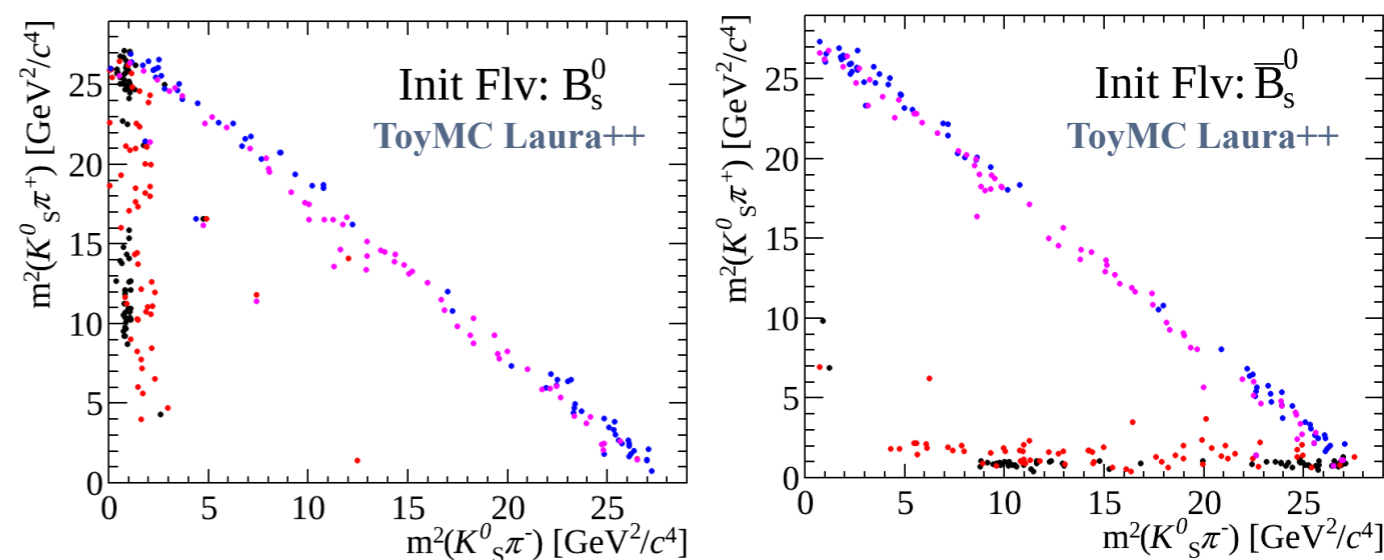
In an untagged analysis it is in general impossible to disentangle the two components, except:

- $[B^0 \rightarrow K^+ \pi^- \pi^0]$  - Final state assumed to be flavour-specific, so that one of the two possible contributions vanishes.

Phys.Rev. D83 (2011) 112010

- $[B^0_{(s)} \rightarrow K^0_s \pi^+ \pi^-]$  - In time-integrated DP analyses, resonances are either flavour specific (e.g.  $K^{*+} \pi^-$ ) or self-conjugate (e.g.  $K^0_s \rho^0$ ).

LHCb-PAPER-2017-033, arXiv:1712.09320



- **Remark:** cannot perform a untagged Dalitz-plot analysis of a non-self-conjugate, non-flavour-specific final state without some assumption on  $A_f$  and  $\bar{A}_f$ .

# $B^0_s \rightarrow K^0 K^\pm \pi^\mp$ Dalitz-plot analysis

Consider an untagged decay-time-integrated Dalitz-plot analysis for  $B^0_s \rightarrow K^0_s K^\pm \pi^\mp$ , the simplified combined decay time for a final state is given as

$$\Gamma_{\bar{B}^0_s \rightarrow f}(t) + \Gamma_{B^0_s \rightarrow f}(t) = \frac{\mathcal{N}_f e^{-t/\tau(B^0_s)}}{\tau(B^0_s)} \left[ \cosh \frac{\Delta\Gamma_s t}{2} - A_f^{\Delta\Gamma_s} \sinh \frac{\Delta\Gamma_s t}{2} \right]$$

Integrating over time and inserting the definitions, the signal probability density function that can be used in a fit is determined to be

$$\mathcal{P}_f^{\text{sig}}(s, t) = \frac{|\mathcal{A}_f|^2 + |\bar{\mathcal{A}}_f|^2 - 2\mathcal{D}\text{Re}(\mathcal{A}_f^* \bar{\mathcal{A}}_f)}{\int \int_{DP} |\mathcal{A}_f|^2 + |\bar{\mathcal{A}}_f|^2 - 2\mathcal{D}\text{Re}(\mathcal{A}_f^* \bar{\mathcal{A}}_f) ds dt} \quad \mathcal{D} = \frac{\int_0^\infty \epsilon(t) e^{-\Gamma_s t} \sinh \frac{\Delta\Gamma_s t}{2} dt}{\int_0^\infty \epsilon(t) e^{-\Gamma_s t} \cosh \frac{\Delta\Gamma_s t}{2} dt}$$

$$\begin{aligned} \mathcal{A}_f &\leftrightarrow \bar{\mathcal{A}}_f \\ \mathcal{A}_f &\rightarrow e^{i\phi} \mathcal{A}_f \\ \bar{\mathcal{A}}_f &\rightarrow e^{-i\phi} \bar{\mathcal{A}}_f \end{aligned}$$

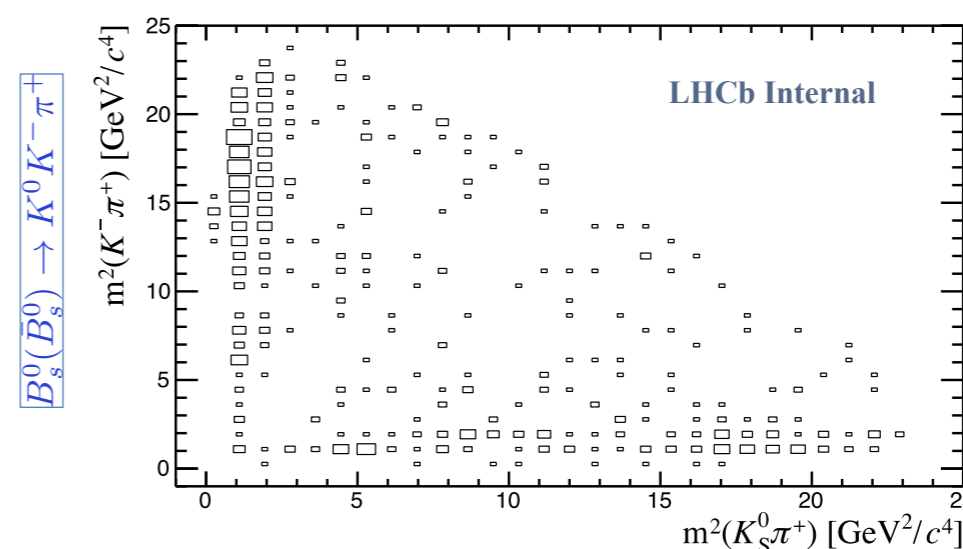
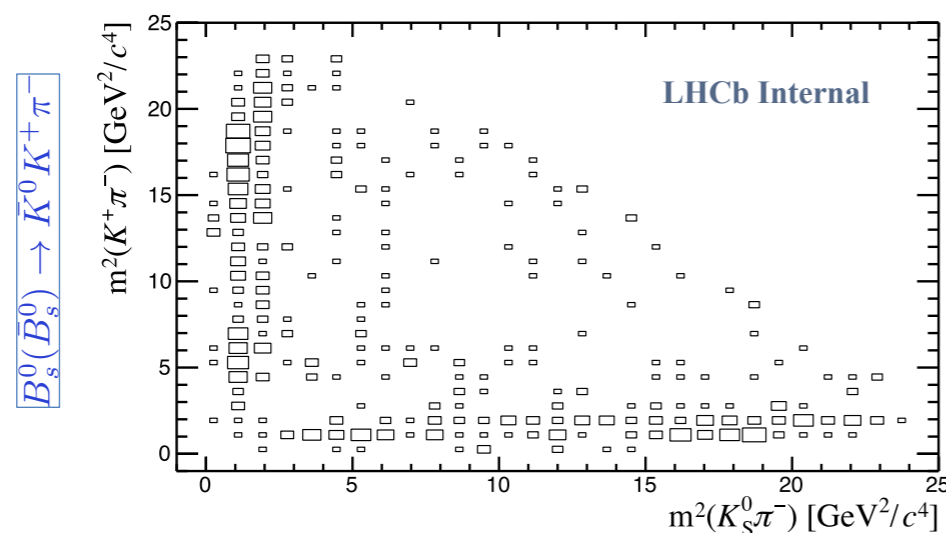
**Conclusion:** either time-dependent or independent analyses cannot be performed without the need of *flavour tagging* for  $B^0_s \rightarrow K^0_s K^\pm \pi^\mp$  decays.

# $B_s^0 \rightarrow K^0 K^\pm \pi^\mp$ Dalitz-plot strategy

Flavour-tagging is unattractive with the current statistics, so an effective DP model is used:

$$\mathcal{P}_f^{\text{sig}}(s, t) = \frac{|\mathcal{A}_f(s, t)|^2}{\int \int_{DP} |\mathcal{A}_f(s, t)|^2 ds dt}$$

$$\widehat{FF}_j = \frac{\int \int_{DP} |c_j F_j(s, t)|^2 ds dt + \int \int_{DP'} |\bar{c}_j \bar{F}_j(s', t')|^2 ds' dt'}{\int \int_{DP} |\sum_k c_k F_k(s, t)|^2 ds dt + \int \int_{DP'} |\sum_k \bar{c}_k \bar{F}_k(s', t')|^2 ds' dt'}$$



Although the presence of CP violation can be investigated, due to the approximations in the model, the complex coefficients obtained are not of trivial interpretation.



## Analysis selection in a nutshell

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Remark: common strategy developed for all  $K^0 h^+ h^-$  channels

**Dataset, mass fit, efficiency and background maps**



# Dalitz-plot selection strategy

Series of studies to enhance the DP signal yield and/or the amplitude fit sensitivity

- Alternative MVA approaches investigated, (e.g. uBDT and Neurobayes using *sWeights*)
- PID criteria: DLL to ProbNN variables

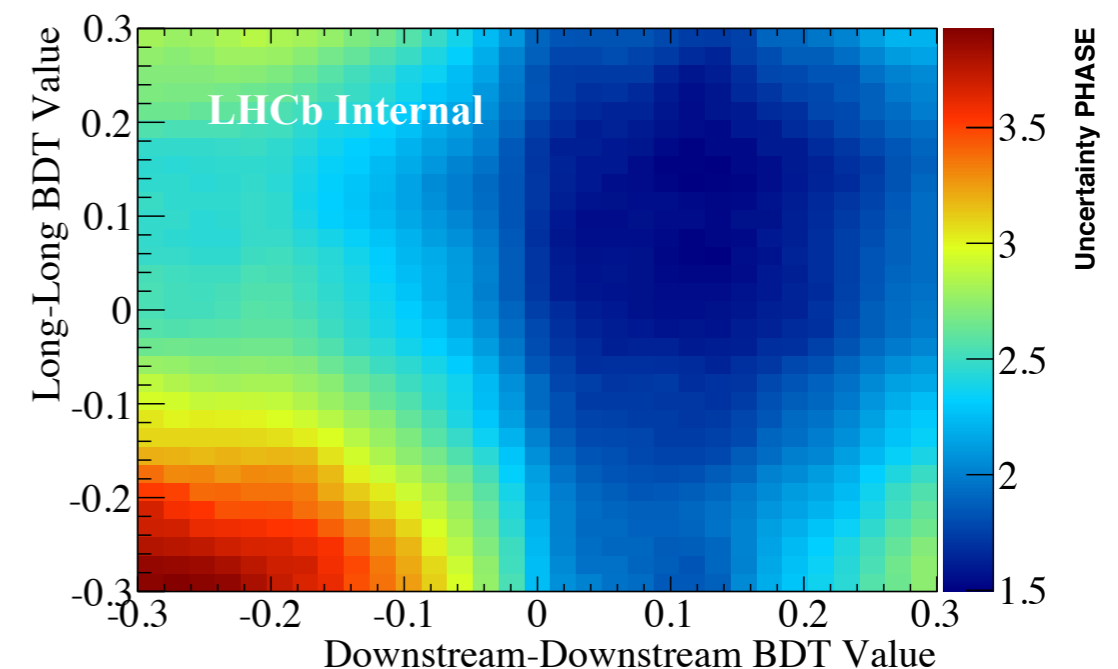
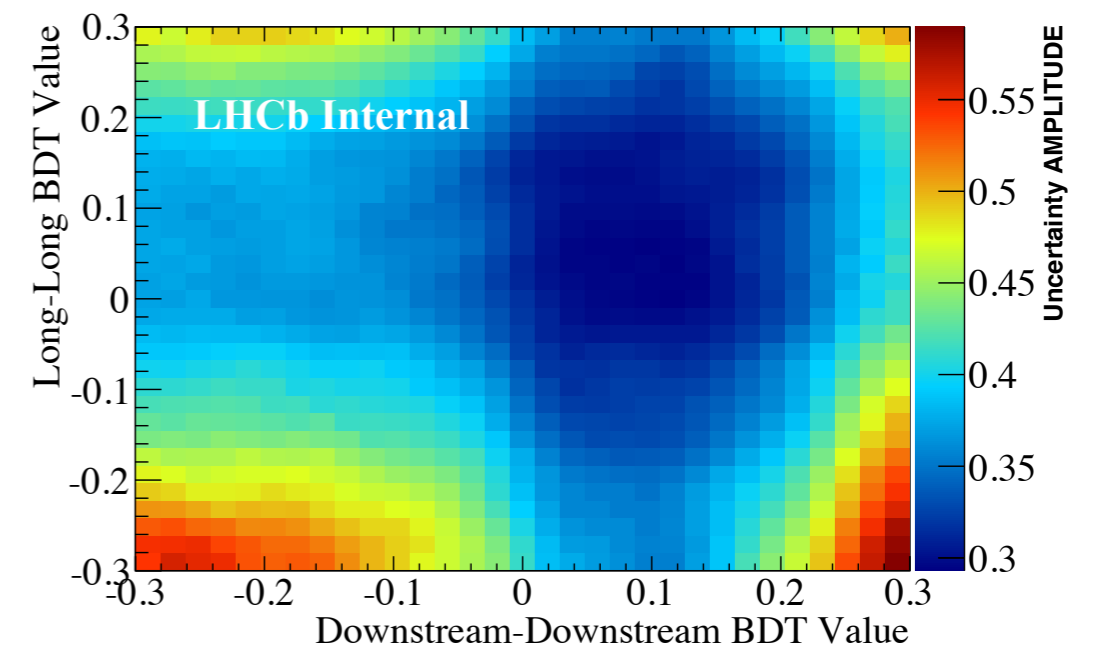
DP FoM optimisation for the optimal isobar parameter sensitivity (Stat+Syst effects)

$$\text{FoM}_1 = \frac{S}{\sqrt{S+B}} \quad \text{FoM}_2 = \frac{S^2}{(S+B)^{3/2}} \quad \text{FoM}_3 = \frac{\epsilon_{\text{sig}}}{a/2 + \sqrt{B}}$$

**Method:** : series of ToyMC studies have been done to verify the uncertainties on the DP observables.

**Results:** FoM<sub>2</sub> seems to provide the best response

Selection technique for  
 $B_s^0 \rightarrow K_S^0 K^\pm \pi^\mp$  Dalitz plot  
optimisation  
LHCb-INT-2015-003

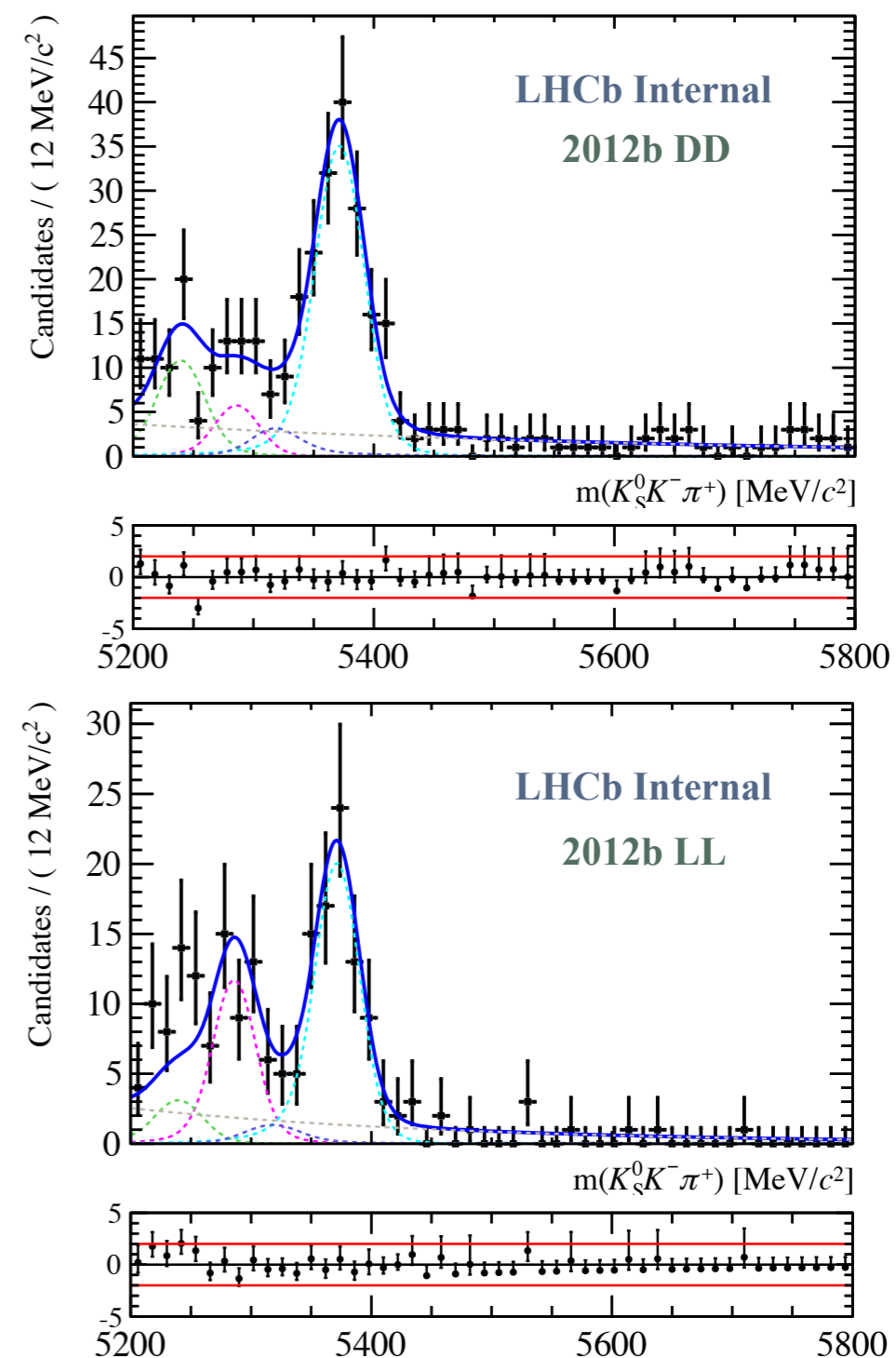


# Mass fit model and results

Strategy similar to the BR paper, where a simultaneous fit of all \*four\* hypotheses combinations is performed splitting between DD/LL and 2011/2012a/2012b

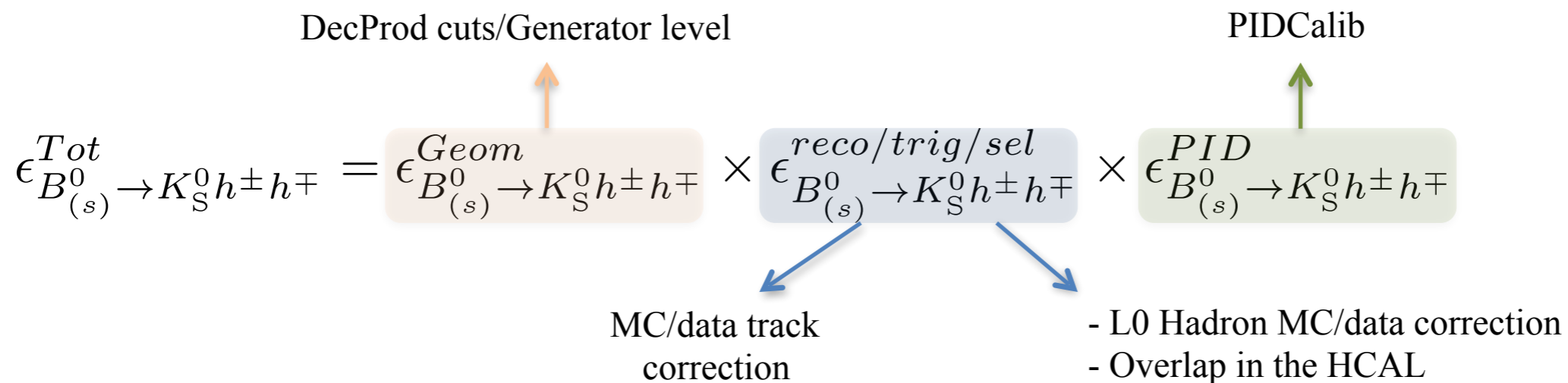
- Split between the two final state charge types
- Total yields correspond to  $\sim 430 K_S^0 K^+ \pi^-$  and  $\sim 490 K_S^0 K^- \pi^+$  events

| Final state       | $K_S^0$ | Year  | $B_s^0$ -signal |                  | Combinatorial |                  | Cross-feed  |
|-------------------|---------|-------|-----------------|------------------|---------------|------------------|-------------|
|                   |         |       | $2.5\sigma$     | Full fit         | $2.5\sigma$   | Full fit         | $2.5\sigma$ |
| $K_S^0 K^+ \pi^-$ | DD      | 2011  | 72.1            | $73.6 \pm 10.6$  | 22.1          | $108.3 \pm 15.1$ | 1.7         |
|                   |         | 2012a | 45.7            | $48.2 \pm 8.6$   | 14.3          | $70.1 \pm 12.1$  | 1.1         |
|                   |         | 2012b | 130.0           | $135.3 \pm 13.6$ | 17.9          | $87.4 \pm 13.8$  | 3.1         |
|                   | LL      | 2011  | 74.6            | $76.2 \pm 9.8$   | 8.4           | $44.1 \pm 9.8$   | 1.8         |
|                   |         | 2012a | 36.8            | $38.5 \pm 7.7$   | 11.2          | $58.8 \pm 11.2$  | 0.9         |
|                   |         | 2012b | 71.9            | $73.5 \pm 10.6$  | 13.6          | $71.7 \pm 13.1$  | 1.7         |
| $K_S^0 K^- \pi^+$ | DD      | 2011  | 71.4            | $72.8 \pm 10.3$  | 16.1          | $78.9 \pm 12.7$  | 1.3         |
|                   |         | 2012a | 65.2            | $68.8 \pm 9.6$   | 9.5           | $46.2 \pm 9.9$   | 1.2         |
|                   |         | 2012b | 158.6           | $165.1 \pm 15.2$ | 21.3          | $104.1 \pm 15.0$ | 2.9         |
|                   | LL      | 2011  | 75.7            | $77.3 \pm 9.8$   | 7.4           | $39.0 \pm 10.2$  | 1.4         |
|                   |         | 2012a | 38.5            | $40.3 \pm 8.1$   | 11.2          | $58.9 \pm 11.9$  | 0.7         |
|                   |         | 2012b | 80.0            | $81.7 \pm 10.4$  | 9.5           | $50.1 \pm 12.3$  | 1.4         |



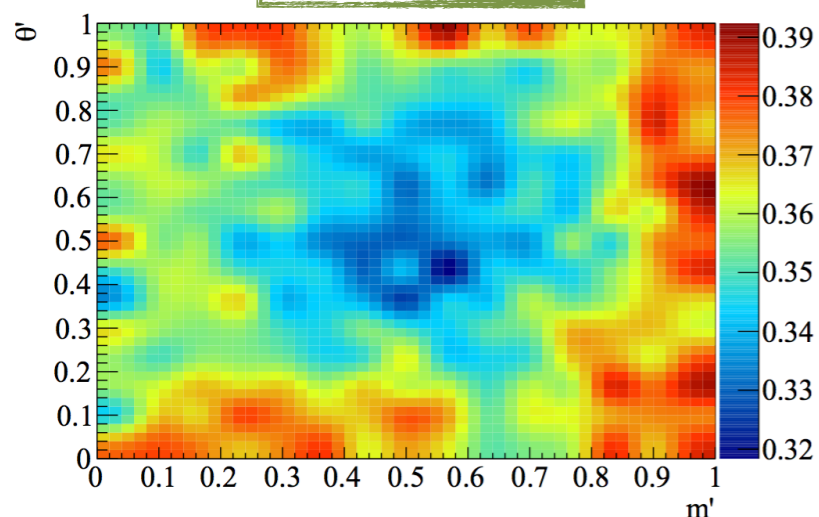
# Efficiency map strategy and corrections

Similar approach used in similar Dalitz plot analyses (e.g. PRL 113 (2014) 162001):

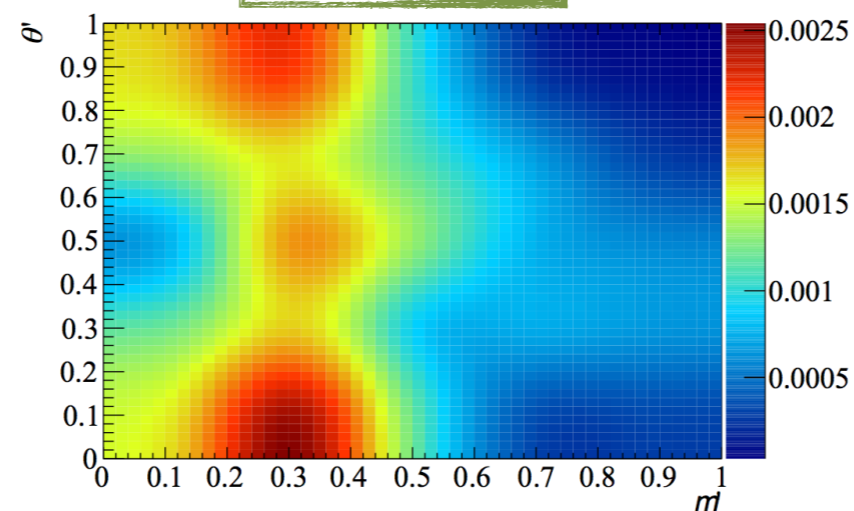


In summary, e.g.  $B_s^0 \rightarrow K_S^0 K^+ \pi^-$  DD 2011:

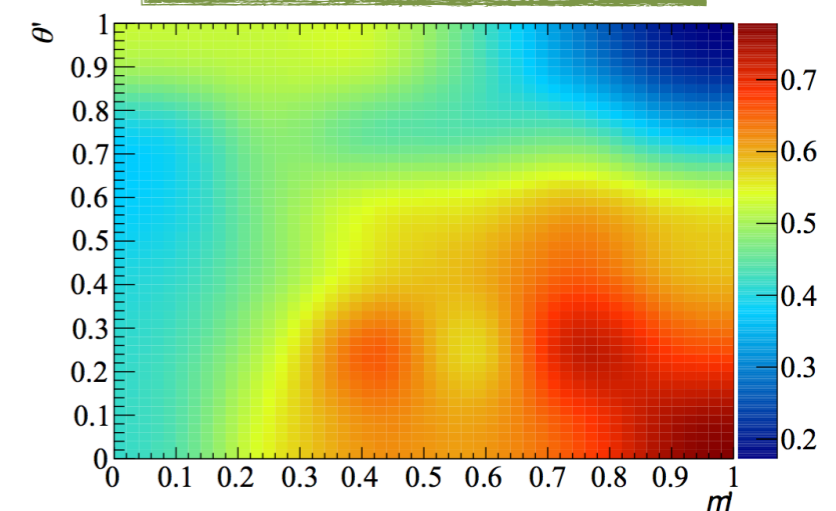
Geometry



Selection



Particle identification



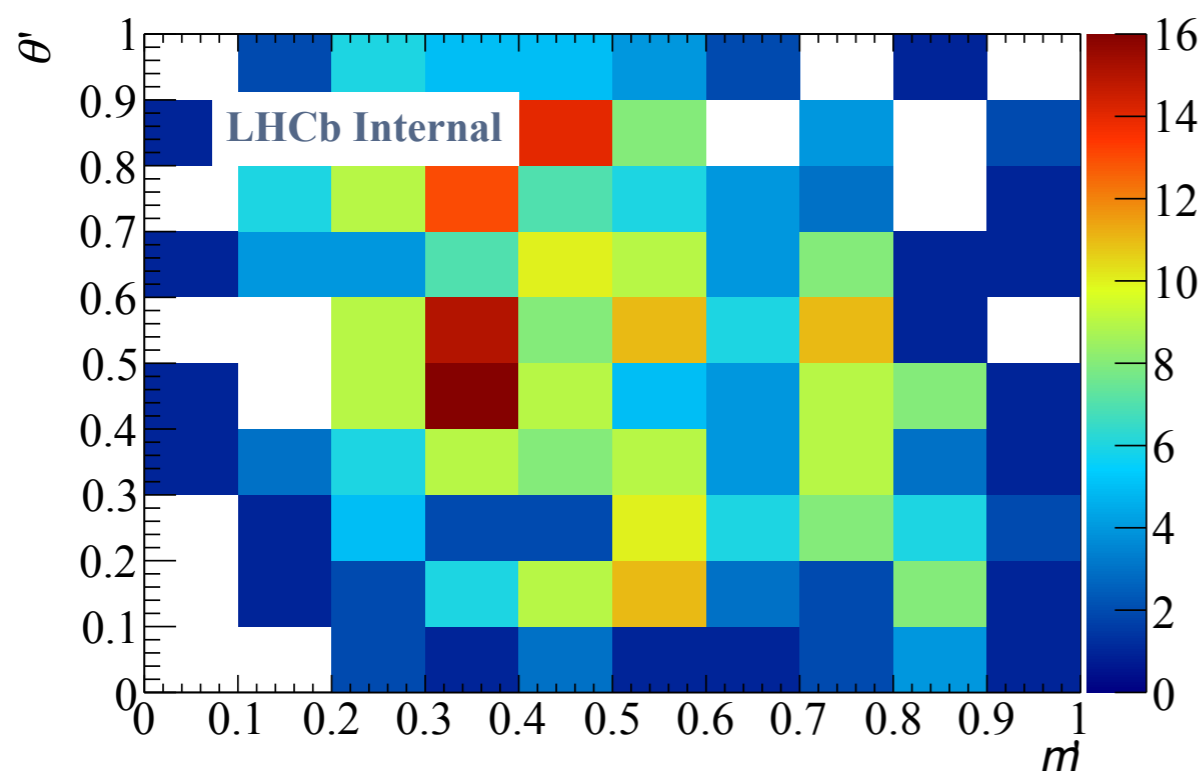


# Background distributions

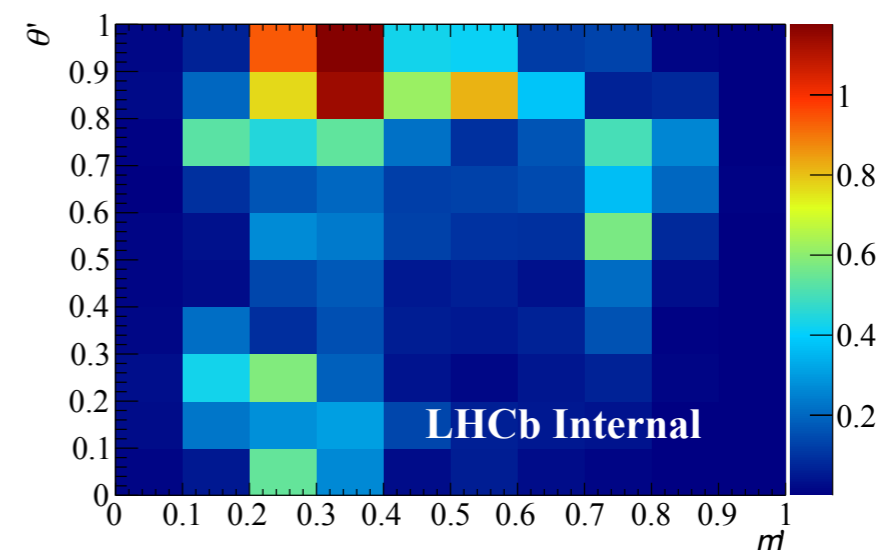
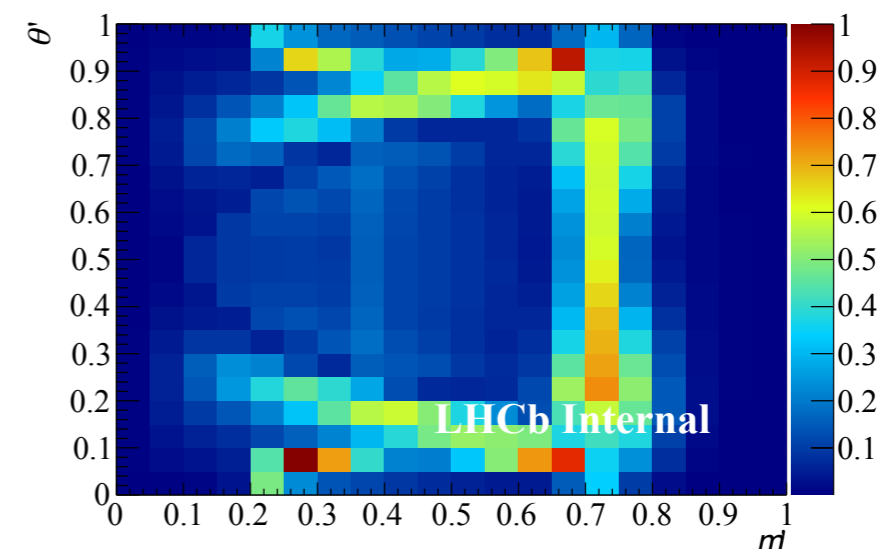


Two main contributions are considered in the model: combinatorial ( $\sim 10\%$ ) and cross-feed from  $B^0 \rightarrow K^0_S \pi^+ \pi^-$  decays ( $3\%$ ).

**Combinatorial bkg:** right side-band is statistically limited after the full selection (loose selection)



**Crossfeed:** re-weight MC samples using ToyMC inspired by BaBar model





## Dalitz-Plot fit machinery and results

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[Non-public results]:  $\mathcal{L} = 3\text{fb}^{-1} - 2011 + 2012$  dataset

**First amplitude analysis of  $B^0_s \rightarrow K^0 K^\pm \pi^\mp$  decays using an Isobar approach**



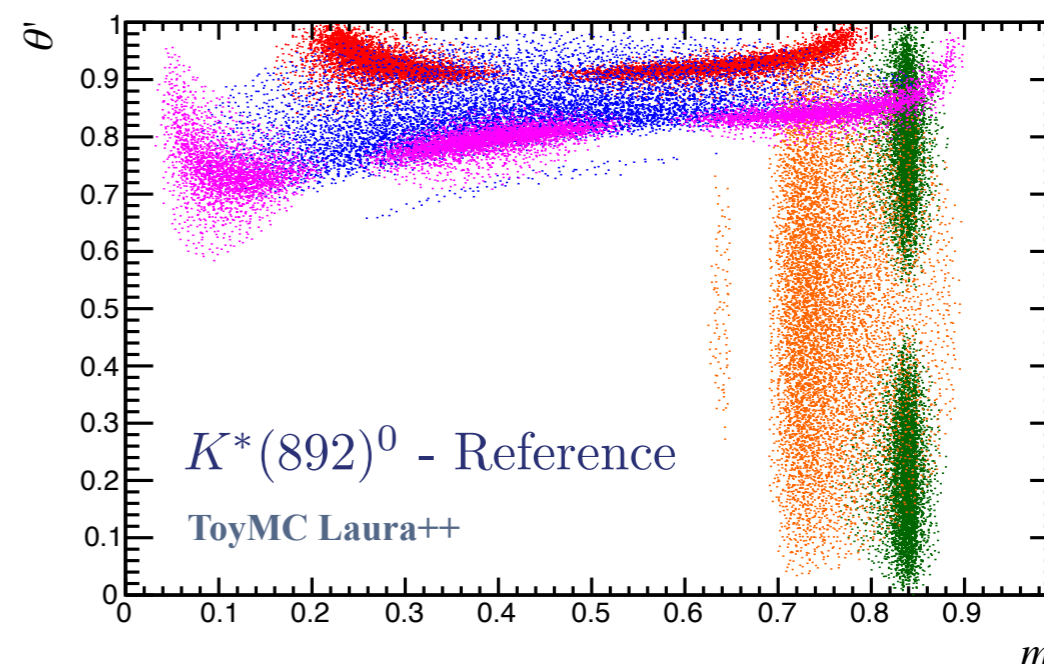
# Dalitz-plot fitting

Simultaneous unbinned DP fit based on the  $\mathcal{J}$ Fit [arXiv:1409.5080] framework is performed for each event  $i$  and signal/background  $k$  component as

$$\mathcal{L} = \prod_i^{N_c} \left[ \sum_k N_k \mathcal{P}_k (m_i^2(K^\pm \pi^\mp), m_i^2(K_S^0 \pi^\mp)) \right]$$

$$m' \equiv \frac{1}{\pi} \arccos \left( 2 \frac{m_{K^\pm \pi^\mp} - m_{K^\pm \pi^\mp}^{\min}}{m_{K^\pm \pi^\mp}^{\max} - m_{K^\pm \pi^\mp}^{\min}} - 1 \right)$$

$$\theta' \equiv \frac{1}{\pi} \theta_{K^\pm \pi^\mp}$$

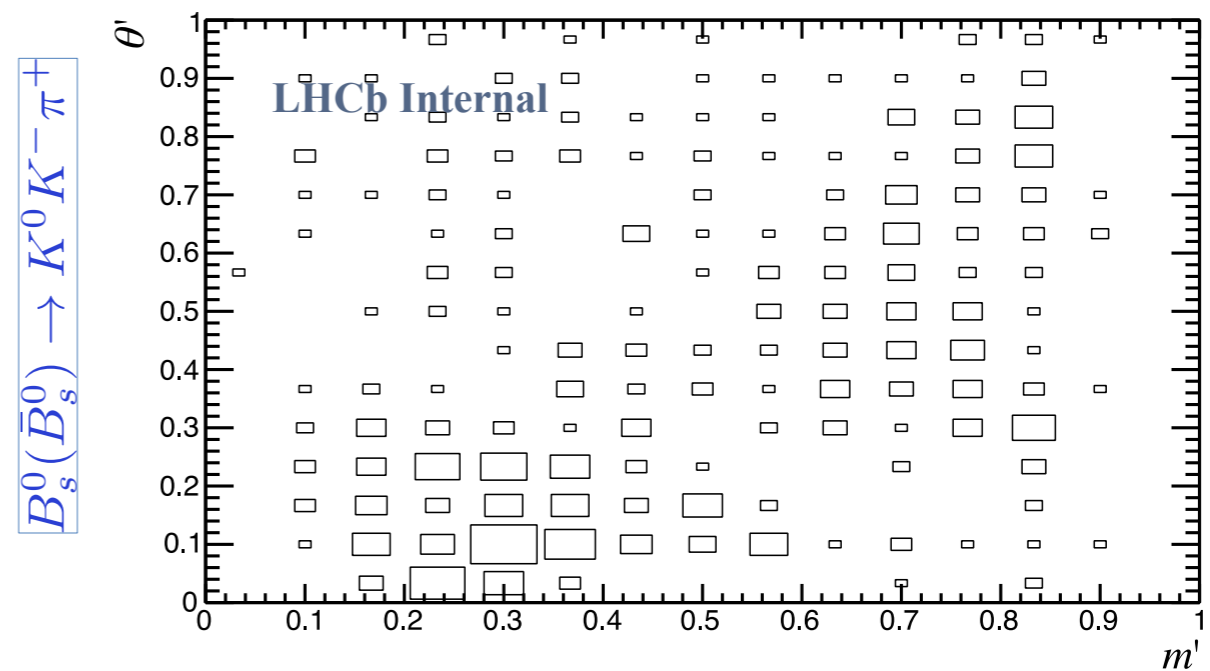
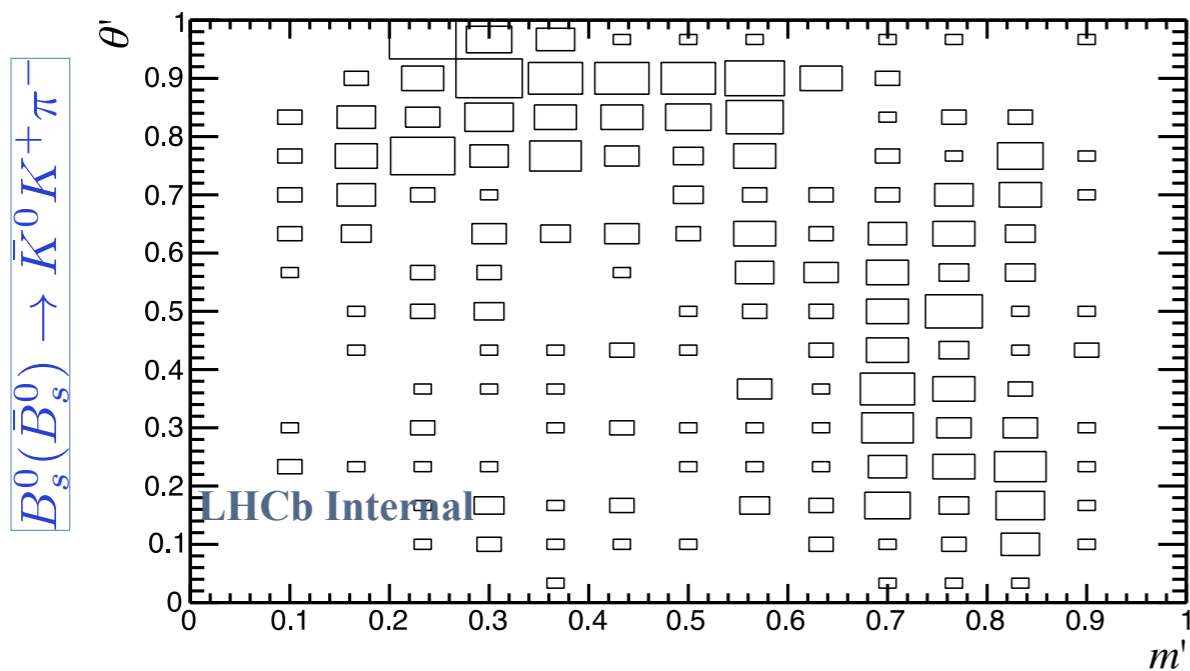
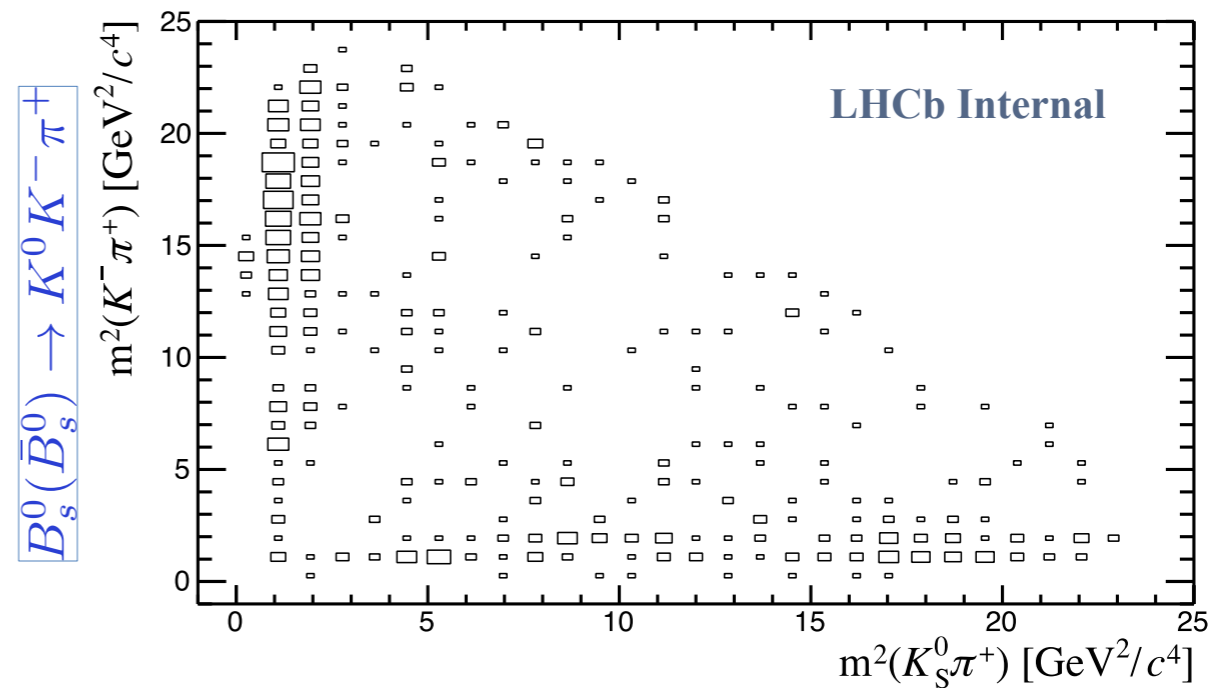
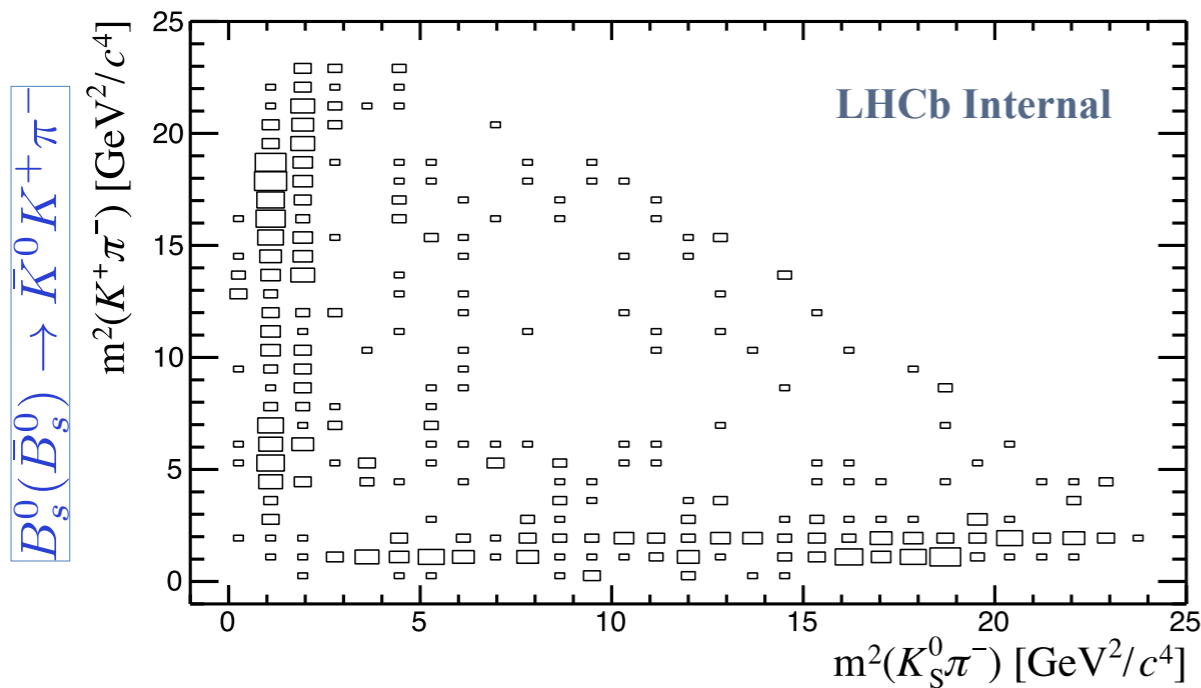


| Resonance         | Spin | Model  | Mass (MeV/ $c^2$ ) | Width (MeV)    |
|-------------------|------|--------|--------------------|----------------|
| $K^*(892)^0$      | 1    | Rel BW | $895.81 \pm 0.19$  | $47.4 \pm 0.6$ |
| $K^*(892)^\pm$    | 1    | Rel BW | $891.66 \pm 0.26$  | $50.8 \pm 0.9$ |
| $K_0^*(1430)^0$   | 0    | LASS   | $1425 \pm 50$      | $270 \pm 80$   |
| $K_0^*(1430)^\pm$ | 0    | LASS   | $1425 \pm 50$      | $270 \pm 80$   |
| $K_2^*(1430)^0$   | 2    | Rel BW | $1432.4 \pm 1.3$   | $109 \pm 5$    |
| $K_2^*(1430)^\pm$ | 2    | Rel BW | $1425.6 \pm 1.5$   | $98.5 \pm 2.7$ |

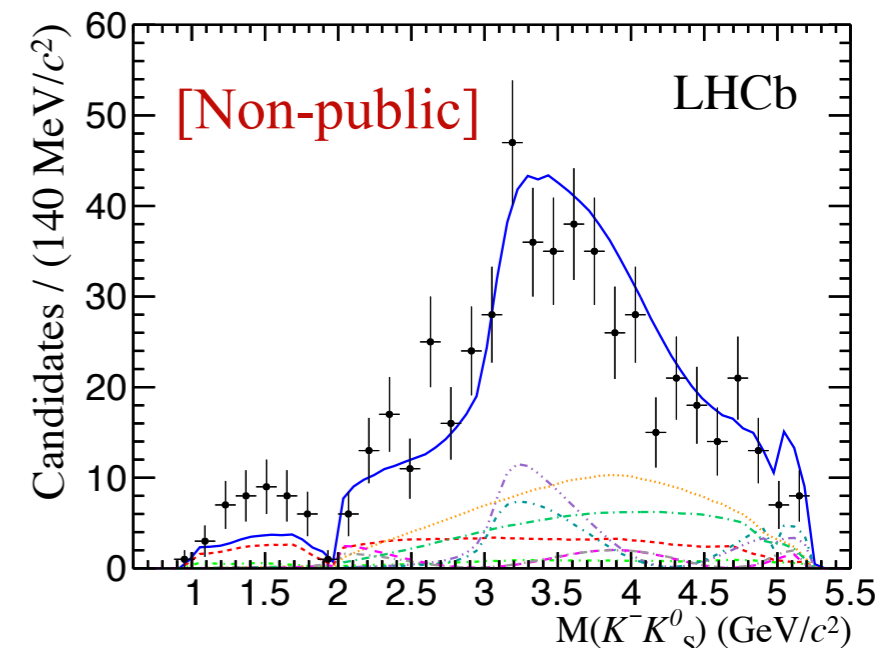
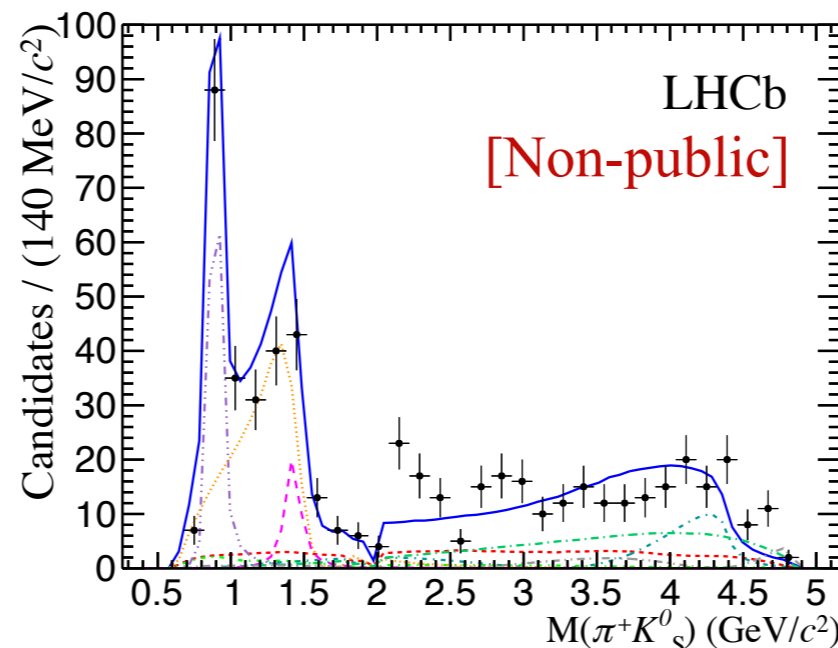
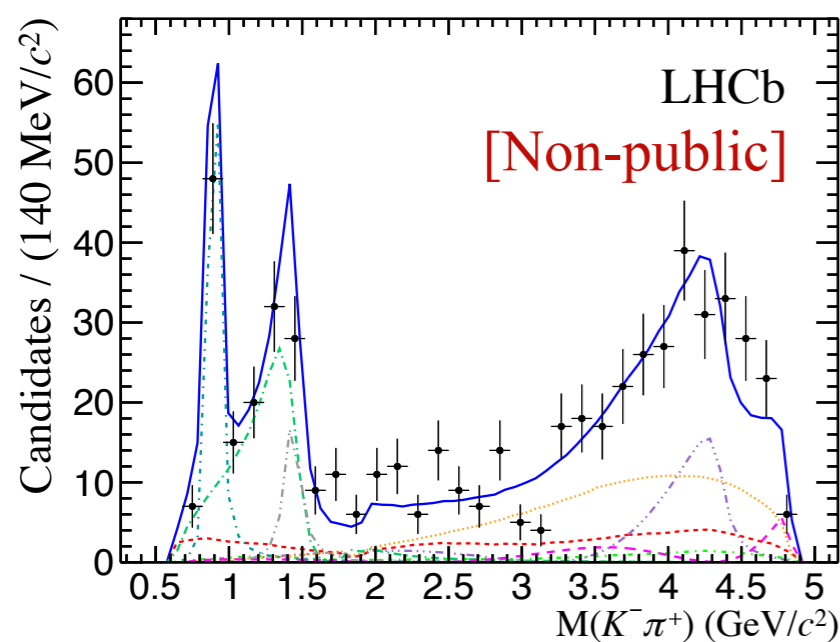
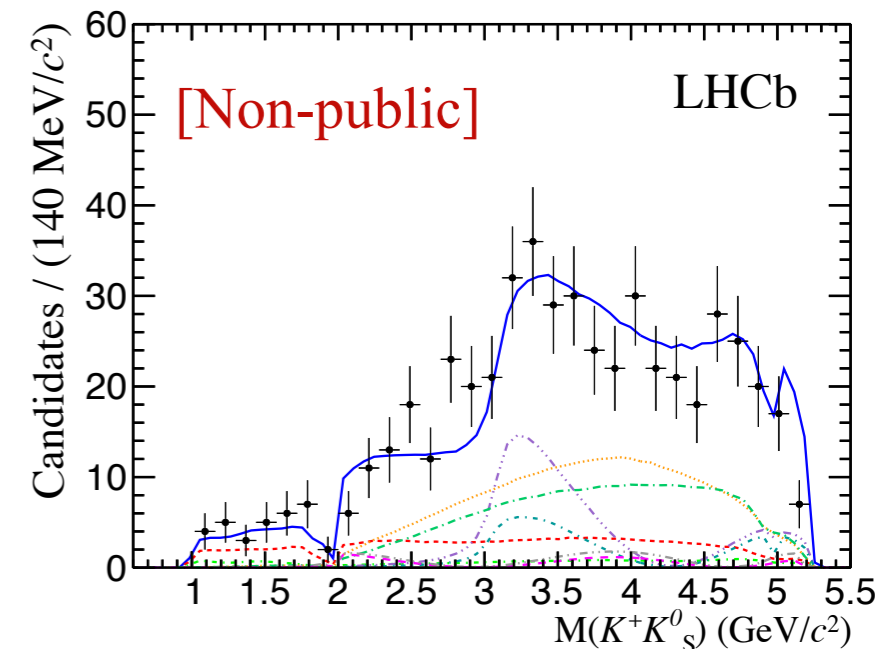
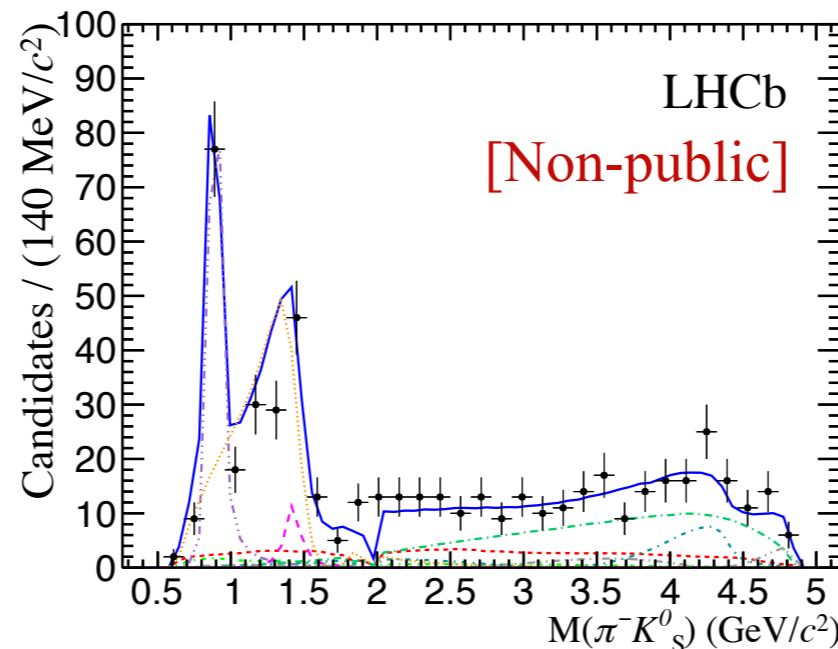
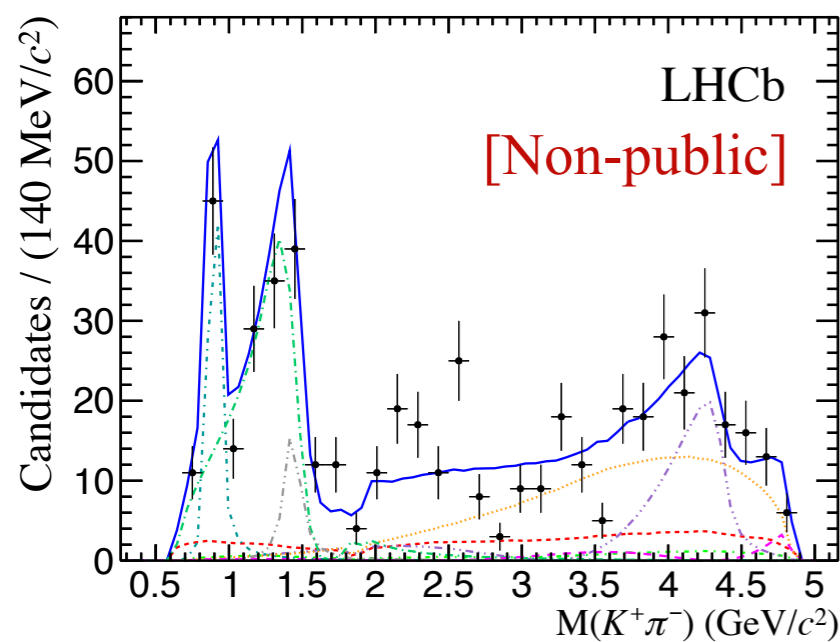
## Multiple solutions :

- It is possible the during the process of minimisation the fit finds multiple solutions.
- To ensure a global minimum, each fit is repeated **100** times with randomised values
- The solution with the smallest negative log-likelihood is taken as the default result.

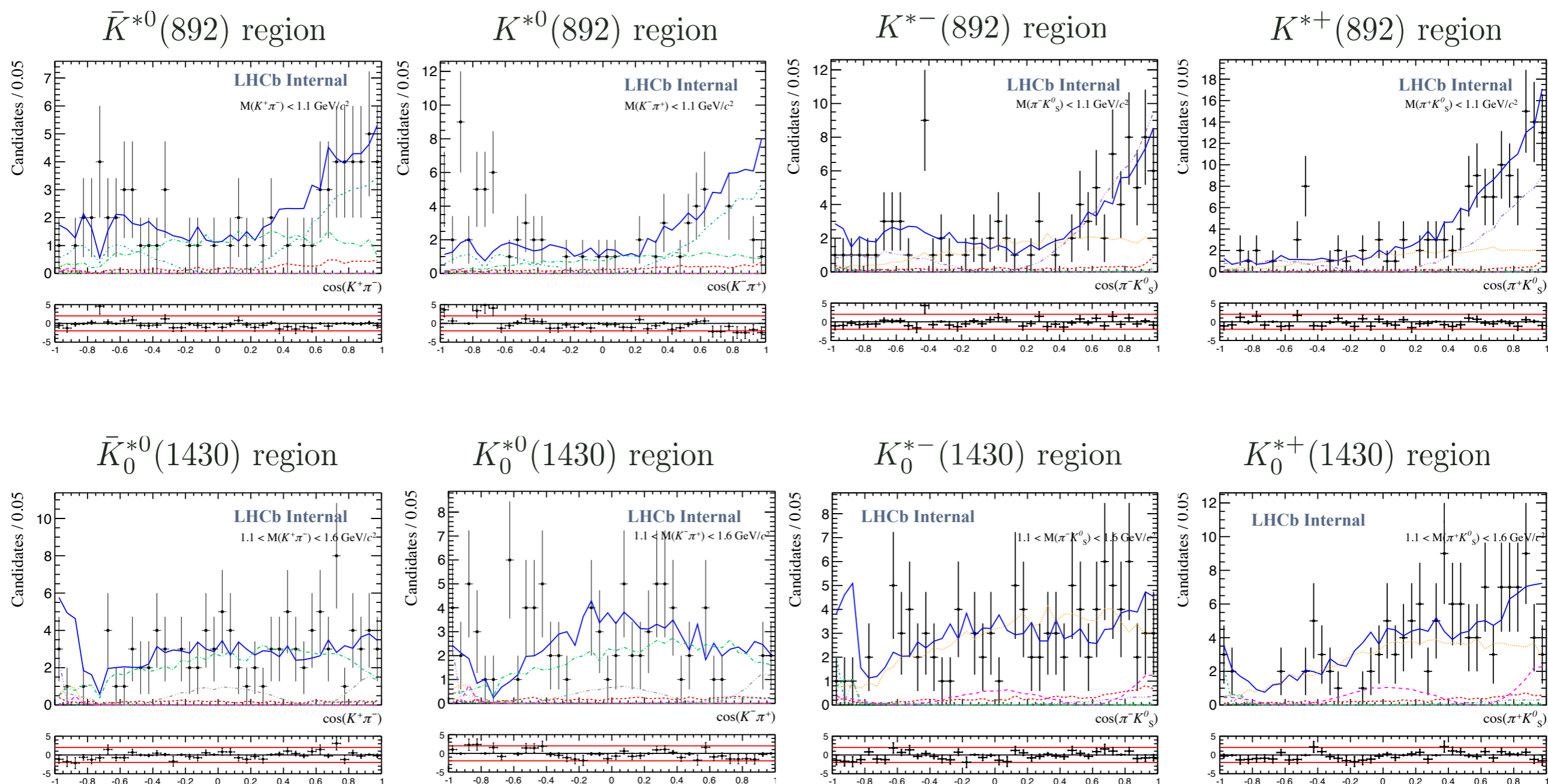
# Phase-space distributions



# Fit results - Invariant mass projections



# Fit results - helicity angle projections



# Fit results - isobar parameters

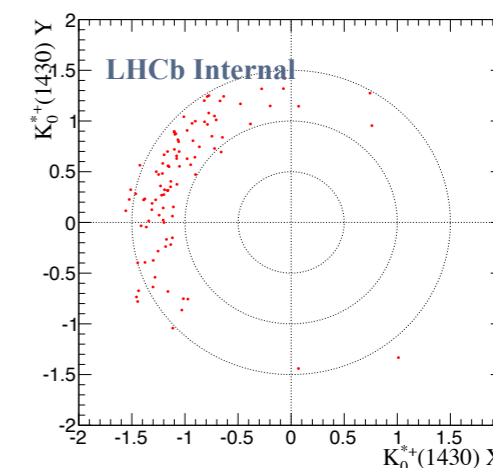
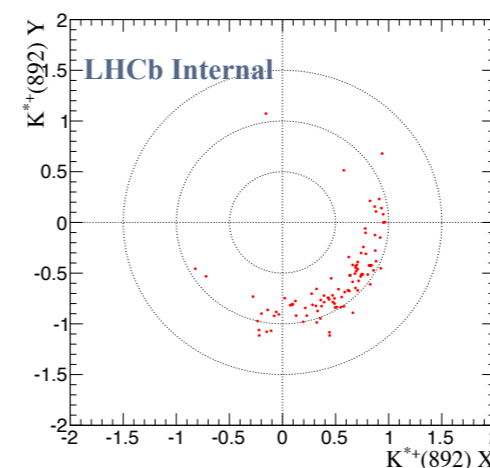
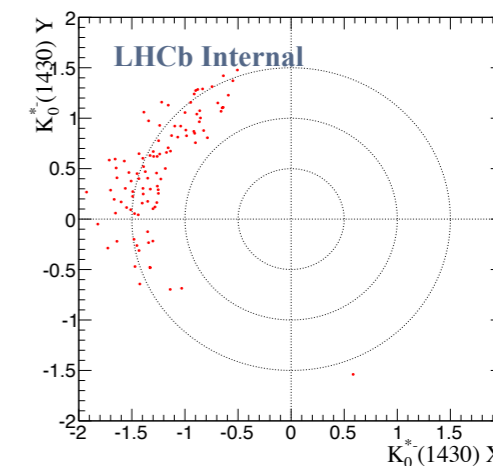
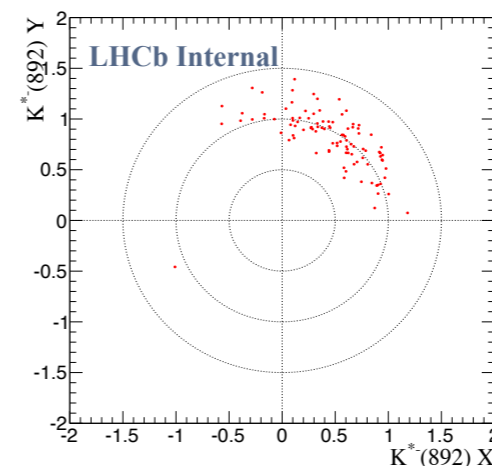
$$B_s^0(\bar{B}_s^0) \rightarrow K_S^0 K^+ \pi^-$$

| Resonance             | Fit fraction (%) | Isobar model coefficients |                  |
|-----------------------|------------------|---------------------------|------------------|
|                       |                  | Real part                 | Imaginary part   |
| $\bar{K}^*(892)^0$    | $13.2 \pm 2.4$   | 1.00                      | 0.00             |
| $\bar{K}_0^*(1430)^0$ | $33.9 \pm 2.9$   | $-1.33 \pm 0.24$          | $0.90 \pm 0.31$  |
| $\bar{K}_2^*(1430)^0$ | $5.9 \pm 4.0$    | $0.01 \pm 0.20$           | $-0.67 \pm 0.15$ |
| $K^*(892)^-$          | $15.6 \pm 1.5$   | $0.28 \pm 0.48$           | $1.05 \pm 0.19$  |
| $K_0^*(1430)^-$       | $30.2 \pm 2.6$   | $-1.45 \pm 0.24$          | $0.42 \pm 0.58$  |
| $K_2^*(1430)^-$       | $2.9 \pm 1.3$    | $0.05 \pm 0.19$           | $-0.47 \pm 0.14$ |
| Total fit fraction    | 102              |                           |                  |

$$B_s^0(\bar{B}_s^0) \rightarrow K_S^0 K^- \pi^+$$

| Resonance          | Fit fraction (%) | Isobar model coefficients |                  |
|--------------------|------------------|---------------------------|------------------|
|                    |                  | Real part                 | Imaginary part   |
| $K^*(892)^0$       | $19.2 \pm 2.3$   | 1.00                      | 0.00             |
| $K_0^*(1430)^0$    | $27.0 \pm 4.1$   | $1.13 \pm 0.17$           | $-0.38 \pm 0.34$ |
| $K_2^*(1430)^0$    | $7.7 \pm 2.8$    | $-0.48 \pm 0.18$          | $0.41 \pm 0.21$  |
| $K^*(892)^+$       | $13.4 \pm 2.0$   | $-0.59 \pm 0.32$          | $0.59 \pm 0.32$  |
| $K_0^*(1430)^+$    | $28.5 \pm 3.6$   | $1.17 \pm 0.23$           | $-0.32 \pm 0.57$ |
| $K_2^*(1430)^+$    | $5.8 \pm 1.9$    | $-0.16 \pm 0.25$          | $0.52 \pm 0.14$  |
| Total fit fraction | 102              |                           |                  |

Stability checks for observed differences in the isobar parameters indicated good determination of fit fractions



## Signal/background yields from mass fit

- Statistical: propagate using covariance matrix RMS from ensemble of 100 fits
- Fixed Parameters: similar to stat errors
- Alternative model: 1-CB and constraints on the background shape (nominal diff)

## Background modelling

- Histograms are varied 100x and the data is refitted RMS from ensemble

## Efficiency mapping

- Maps: similar to background model
- PIDCalib: different binning scheme

## Fit intrinsic bias

- Pseudo-experiments

## Fixed parameters in the DP fit

- Mass and widths of all resonances
- Blatt-Weisskopf radius parameters
- LASS parameters  $r$  and  $a$
- Fit is repeated varying each of these and RMS of distribution is examined

## $K\pi$ S-wave model

- EFKLLM model is examined

## Addition/removal marginal components

- Examples: insertion of insertion of the  $a_2(1320)^\pm$  resonance

## “Effective” flavour average approach

- Time-dependent toys to assign mis-modelling of the model approximation





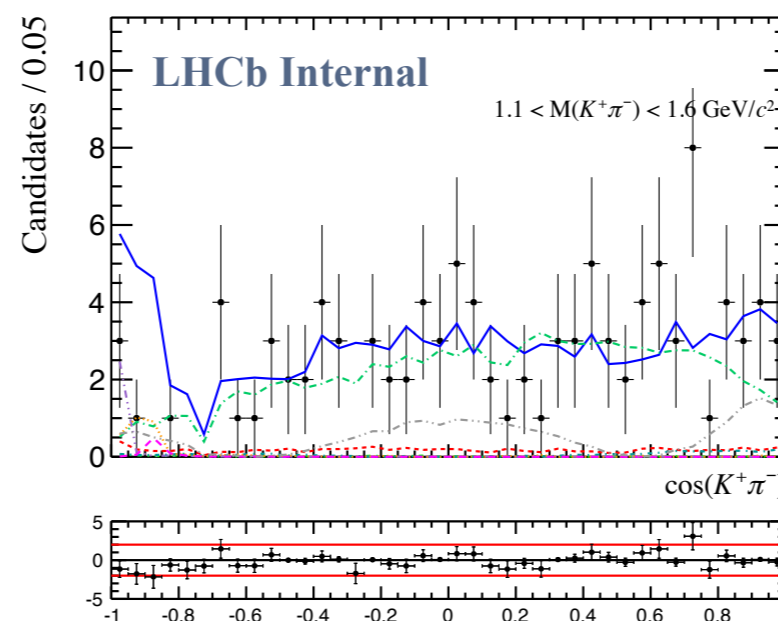
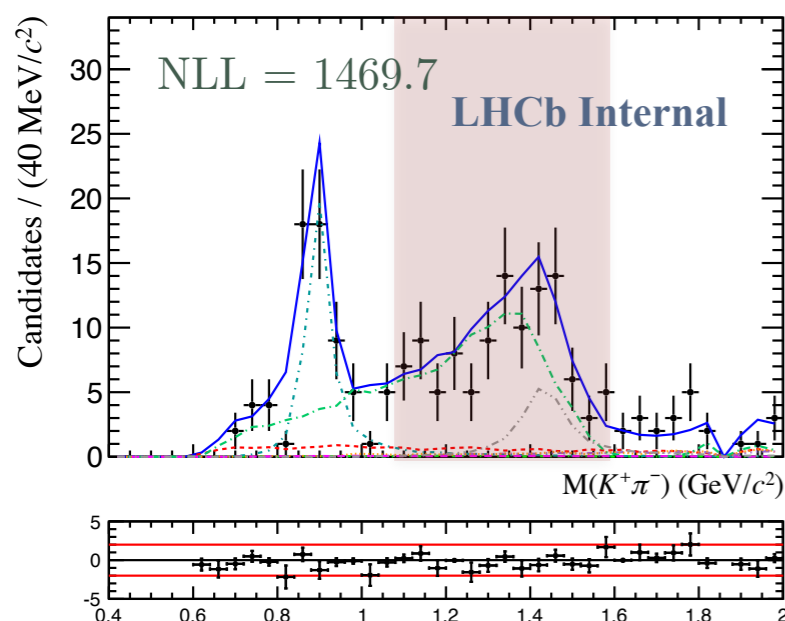
# Systematic uncertainties summary

The results for the various sources of systematic uncertainties are given below:

| Resonance             | Yields | Eff. | Bkg. SDP | Fit fraction (%) uncertainties |           |            |            | Total |
|-----------------------|--------|------|----------|--------------------------------|-----------|------------|------------|-------|
|                       |        |      |          | Fit Bias                       | Add. Res. | Fixed Par. | Model Alt. |       |
| $K^*(892)^-$          | 0.19   | 0.52 | 0.18     | 0.19                           | 0.03      | 0.71       | 5.40       | 5.48  |
| $K_0^*(1430)^-$       | 0.12   | 0.63 | 0.23     | 0.34                           | 0.06      | 2.12       | 22.00      | 22.1  |
| $K_2^*(1430)^-$       | 0.14   | 0.29 | 0.12     | 0.58                           | 0.10      | 1.82       | 2.20       | 2.94  |
| $\bar{K}^*(892)^0$    | 0.22   | 0.40 | 0.18     | 0.92                           | 0.02      | 0.35       | 7.00       | 7.09  |
| $\bar{K}_0^*(1430)^0$ | 0.16   | 0.89 | 0.34     | 0.36                           | 0.06      | 4.38       | 3.30       | 5.58  |
| $\bar{K}_2^*(1430)^0$ | 0.13   | 0.69 | 0.31     | 1.30                           | 0.20      | 4.42       | 3.60       | 5.90  |
| $K^*(892)^+$          | 0.39   | 0.62 | 0.12     | 0.46                           | 0.12      | 0.75       | 1.10       | 1.60  |
| $K_0^*(1430)^+$       | 0.47   | 0.69 | 0.38     | 0.76                           | 0.16      | 6.44       | 13.00      | 14.6  |
| $K_2^*(1430)^+$       | 0.07   | 0.41 | 0.20     | 0.24                           | 0.15      | 4.13       | 4.50       | 6.14  |
| $K^*(892)^0$          | 0.37   | 0.39 | 0.34     | 0.25                           | 0.25      | 0.51       | 3.00       | 3.13  |
| $K_0^*(1430)^0$       | 0.36   | 0.62 | 0.43     | 0.79                           | 0.67      | 0.90       | 3.90       | 4.22  |
| $K_2^*(1430)^0$       | 0.14   | 0.37 | 0.23     | 0.80                           | 0.06      | 1.04       | 5.50       | 5.67  |

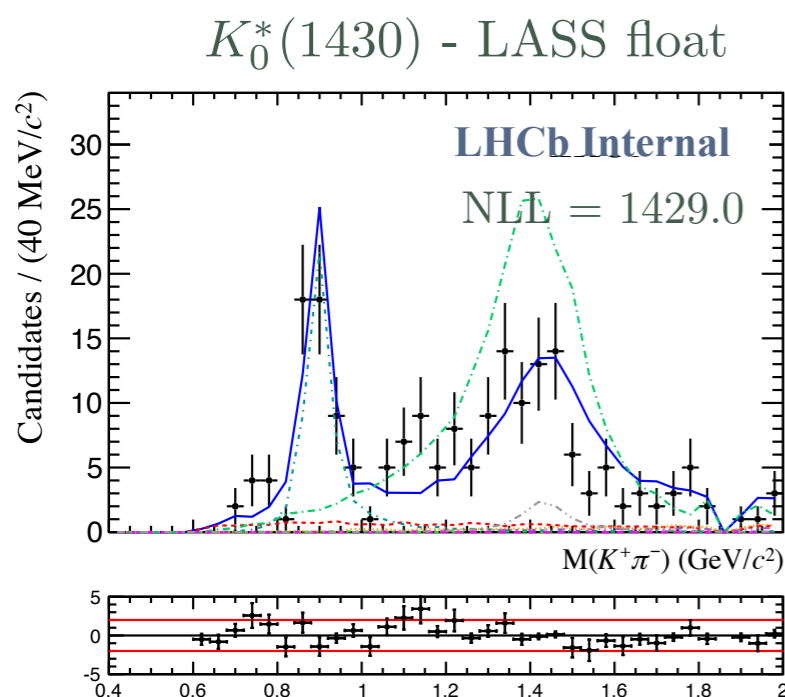
Dominant uncertainties come from the  $K\pi$  S-wave model, e.g. the choice of the alternative line shapes to the LASS model for the  $K^{*\pm,0}(1430)$  states

# Slice in $m(K^\pm\pi^\mp)$ region: 1.1 - 1.6 GeV

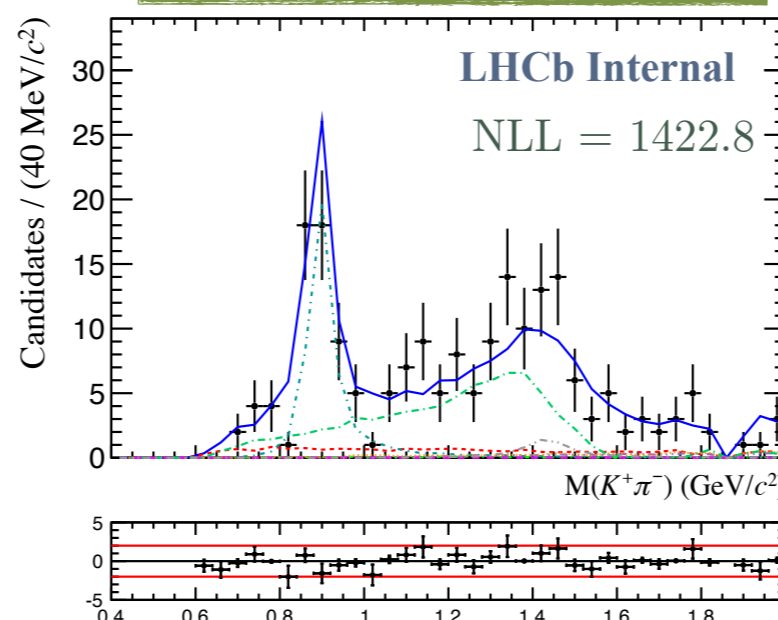


The  $K\pi$  spectrum is modelled:

- $K^*(892)$  [Rel BW]
- $K^*_0(1430)$  [LASS fixed]
- $K^*_2(1430)$  [Rel BW]



Phys. Rev. D 83, 039903 (2011)  
 $K^*_0(1430)$  - EFKLLM

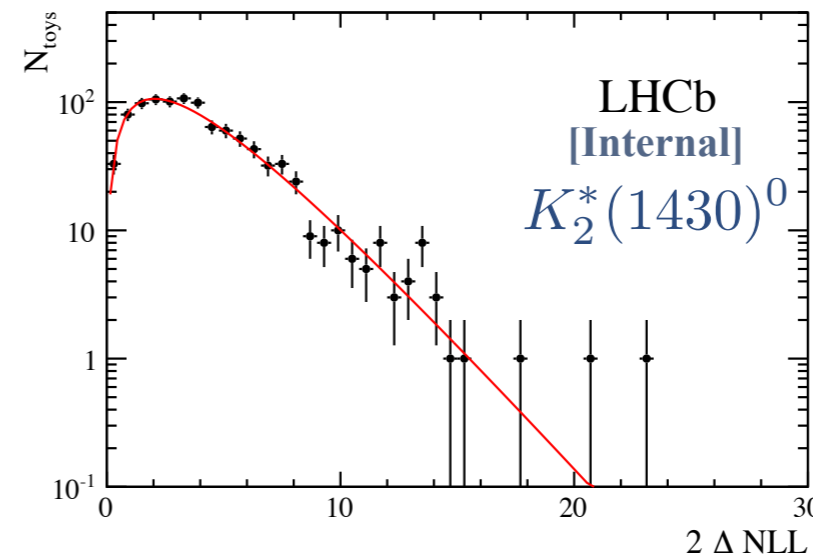
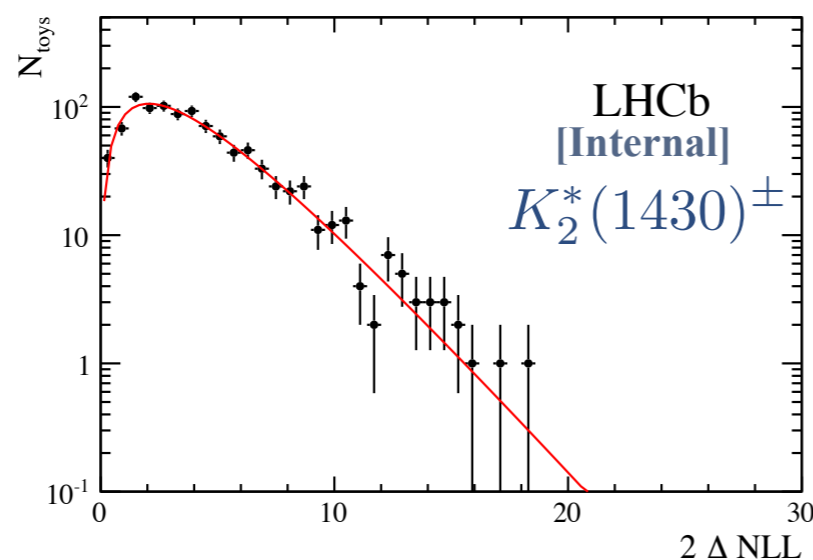
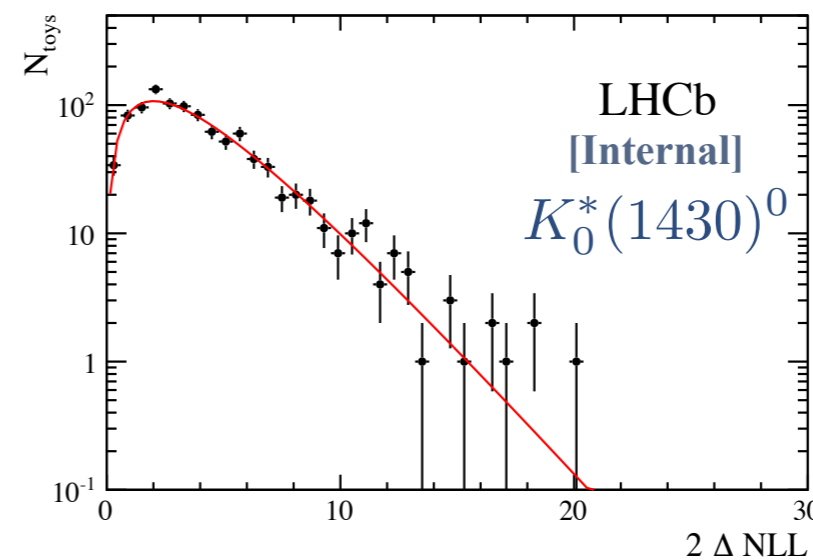
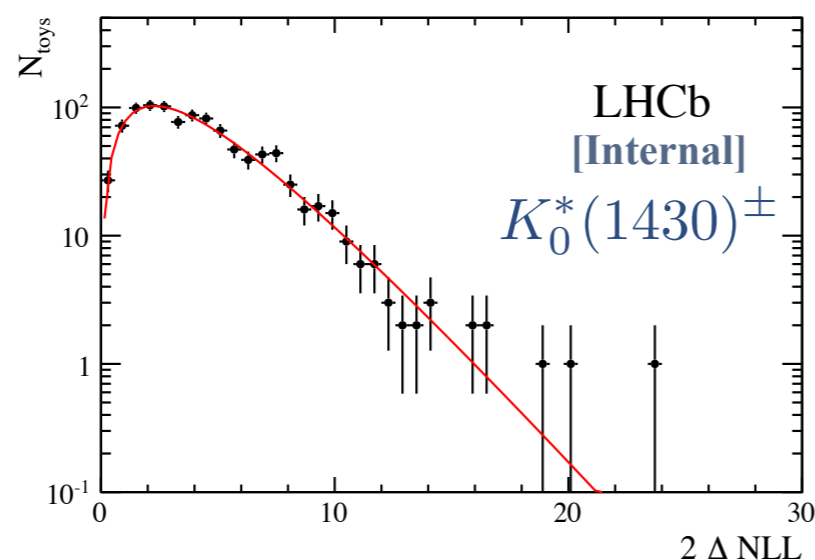


Many alternative scenarios have been investigated:

EFKLLM is used as alternative lineshape model (large systematics)

# Significance of the $K^{*(\pm,0)}(1430)$ states

Series of ensembles were generated and fitted with and without the resonance included



$K_0^*(1430)$  resonances are seen with more than 15 standard deviations

# Branching ratio results

The fit fractions of the resonant components can be converted into quasi-two-body BF:

$$\mathcal{B}(B_s^0 \rightarrow K^* K) = \widehat{FF}_j \times \mathcal{B}(B_s^0 \rightarrow \bar{K}^0 K^\pm \pi^\mp)$$

$$\mathcal{B}(B_s^0 \rightarrow \bar{K}^0 K^\pm \pi^\mp) = (73.6 \pm 5.7 \pm 6.9 \pm 3.0) \times 10^{-6}$$

$$\begin{aligned} \mathcal{B}(B_s^0 \rightarrow K^*(892)^\pm K^\mp) &= (18.6 \pm 1.2 \pm 0.8 \pm 2.8 \pm 2.0) \times 10^{-6} \\ \mathcal{B}(B_s^0 \rightarrow K_0^*(1430)^\pm K^\mp) &= (31.3 \pm 2.3 \pm 0.7 \pm 17.8 \pm 3.3) \times 10^{-6} \\ \mathcal{B}(B_s^0 \rightarrow K_2^*(1430)^\pm K^\mp) &= (10.3 \pm 2.5 \pm 1.1 \pm 11.5 \pm 1.1) \times 10^{-6} \\ \mathcal{B}(B_s^0 \rightarrow \bar{K}^*(892)^0 \bar{K}^0) &= (19.8 \pm 2.8 \pm 1.2 \pm 3.0 \pm 2.1) \times 10^{-6} \\ \mathcal{B}(B_s^0 \rightarrow \bar{K}_0^*(1430)^0 \bar{K}^0) &= (33.0 \pm 2.5 \pm 0.9 \pm 6.1 \pm 3.5) \times 10^{-6} \\ \mathcal{B}(B_s^0 \rightarrow \bar{K}_2^*(1430)^0 \bar{K}^0) &= (16.8 \pm 4.5 \pm 1.7 \pm 14.8 \pm 1.8) \times 10^{-6} \end{aligned}$$

- Results are in good agreement with, and more precise than, the previous measurements
- Measurements for  $K^{*\pm 0}(1430)$  are largely dominated by S-wave modelling

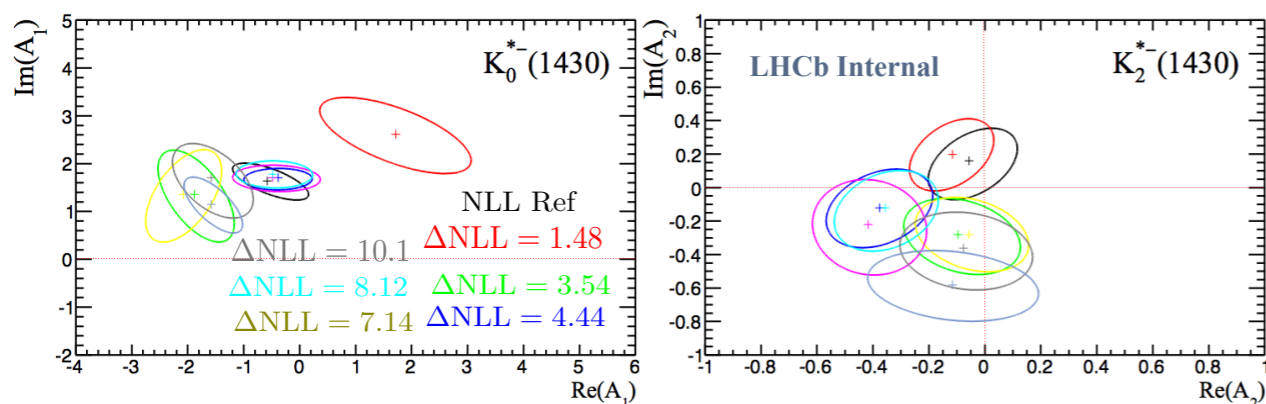


## Summary

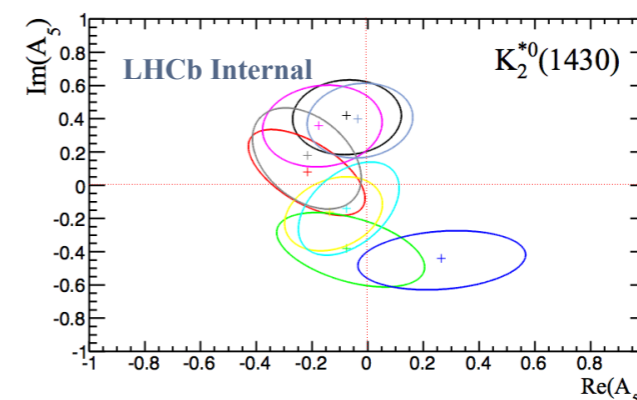
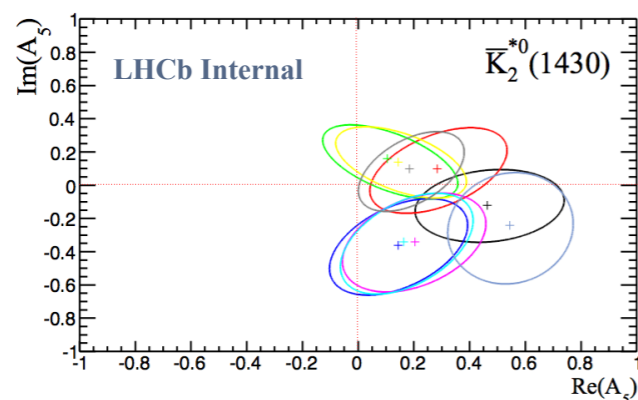
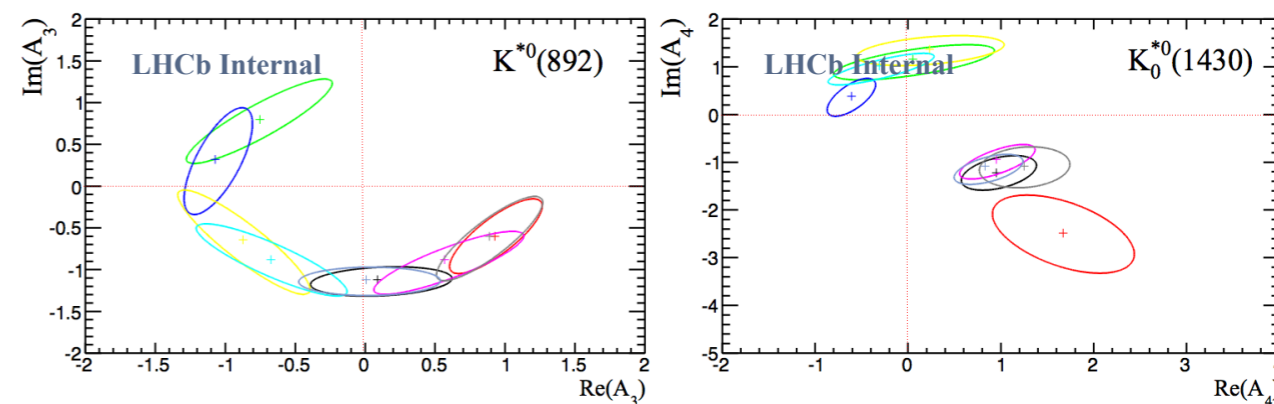
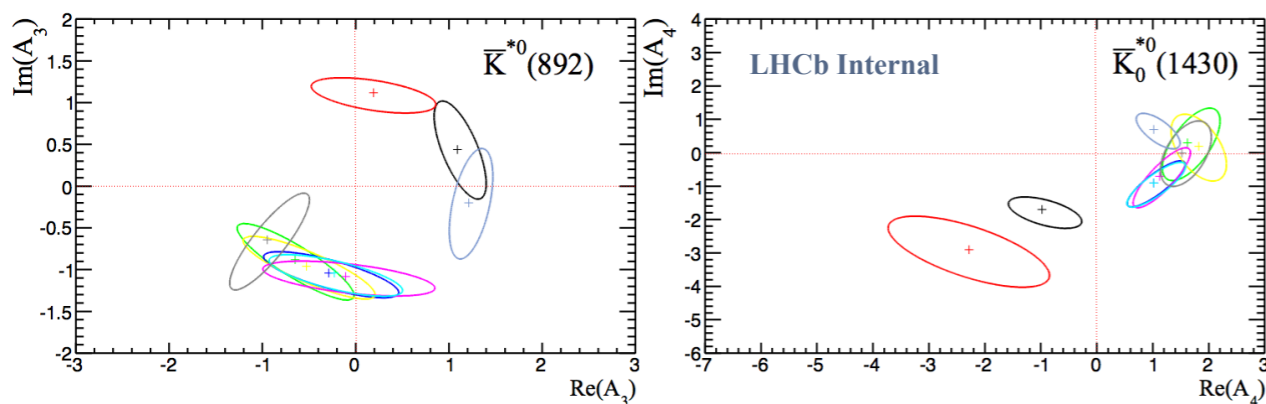
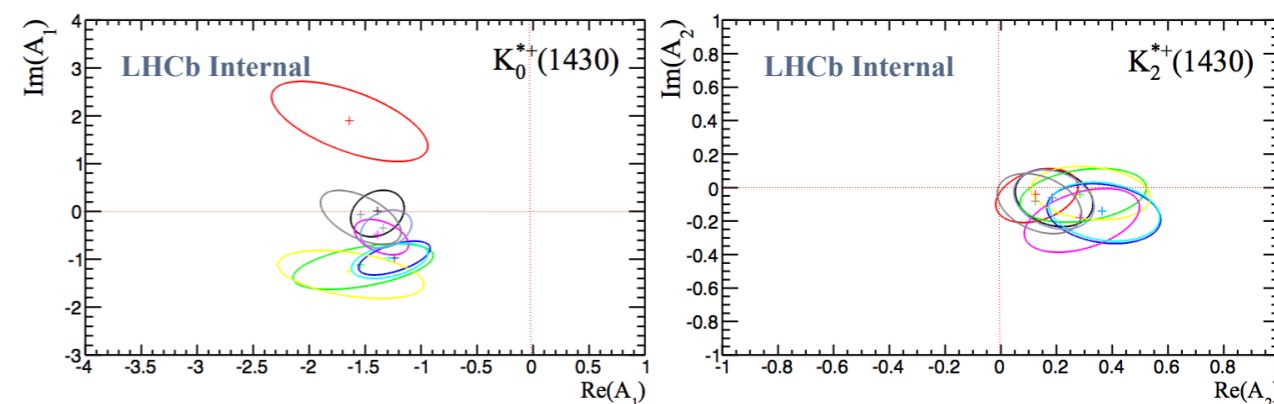
- Due to the approximations in the amplitude model, an untagged time independent approach can only provide information about the fit fractions
- All the steps of the analysis are finalised and paper draft is close to completion
  - ◆ Results for  $K^{*0,\pm}(892)$  resonances indicate a good agreement with previous measurements
  - ◆ Systematics related to the  $K^{*}(1430)$  resonances are currently the limiting factor in the measurement
  - ◆ Nevertheless, first observation of the  $K^{*}(1430)$  states is obtained
- Full potential (e.g.  $CP$ ) of this channel will be only possible in LHCb Run 3-4

# Secondary minima

Isobar parameters for  $K^0_S K^+ \pi^-$



Isobar parameters for  $K^0_S K^- \pi^+$



# FoM selection optimisation framework

**Framework** : machinery developed to extract inputs from data and MC and provide to Laura++ to produce Toy MC's.

