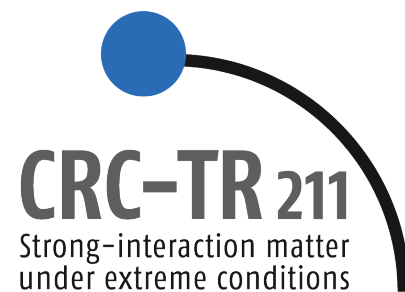


SMASH transport model for hadronic reactions

Jan Staudenmaier,

Stephan Endres, Vinzent Steinberg & Hannah Petersen

Workshop on two-pion and e+e- production in hadronic reactions
Orsay, 2018



Outline

- Introduction
- Model description: SMASH
- Results for
 - ... hadronic cross sections
 - ... e.m. form factors
 - ... dilepton production

Motivation

- elementary reactions offer one of the most important constraints for transport models
- probe for the resonance description (vacuum properties)
- measured cross sections for e.g. pion production valuable to constrain branching ratios, decay modes, cross section etc.

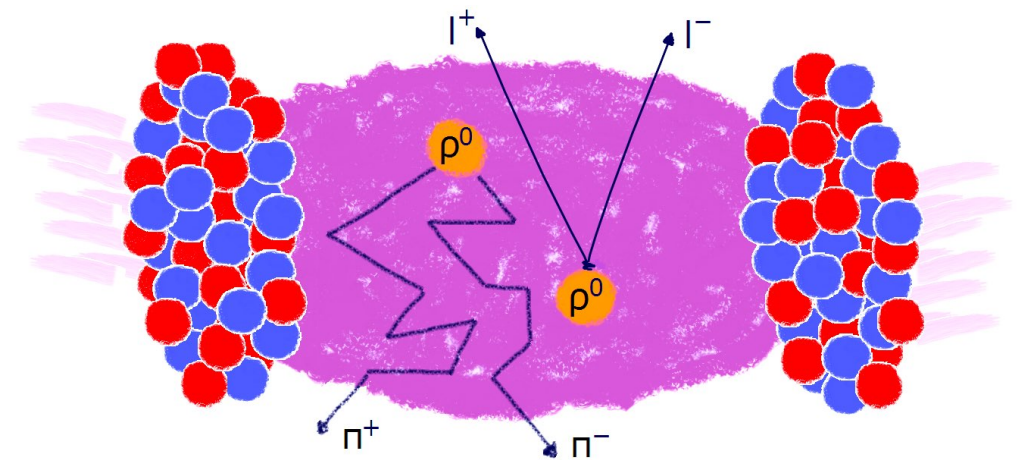
Dileptons

- only electromagnetic interaction: clean probe for hot and dense matter
- extract medium properties and medium modifications over whole lifetime of collision

Complementary constraint:

- on the dynamical evolution of the system
- on the resonance description (in vacuum and medium)

starting point = elementary reactions



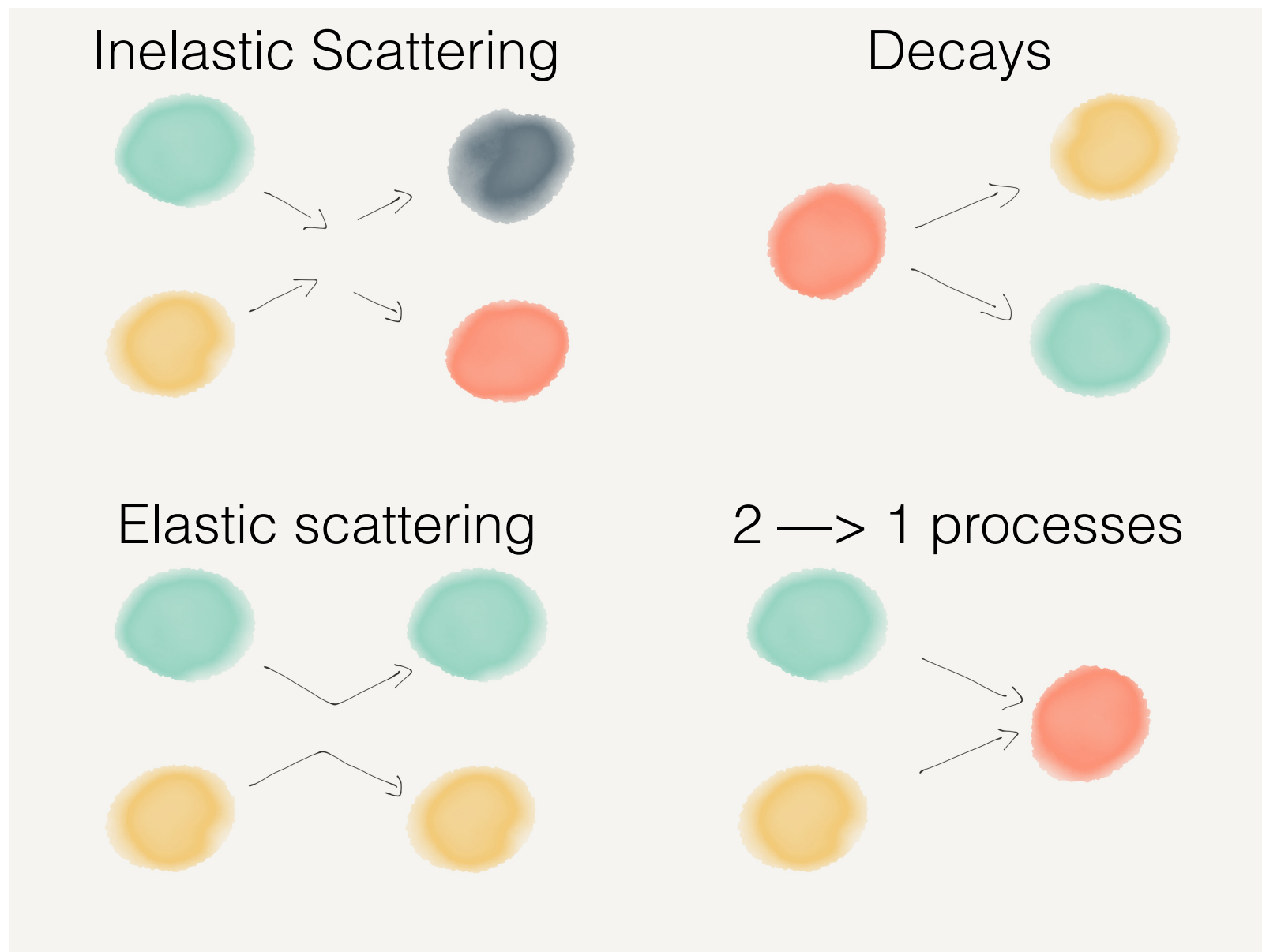
SMASH*

J. Weil et al, Phys. Rev. C 94, 054905 (2016)

- new modern transport approach for dilute non-equilibrium stages of HIC and low energy collisions
- goal: standard reference for hadronic system with vacuum properties
- scenarios: nuclear collisions, infinite matter, afterburner for hydrodynamic simulations
- features: geometric collision criterion, Test Particle Method, Mean-Field potentials, Fermi motion, Pauli blocking
- degrees of freedom: all well-known particles from PDG up to a mass of 2 GeV
 $\pi, \eta, \eta', \rho, \omega, \phi, K, \dots \quad N, N^*, \Delta, \Delta^*, \dots$
 - perturbative treatment of non-hadronic particles (photons, leptons)

* **S**imulating **M**any **A**ccelerated **S**trongly-interacting **H**adrons

Collision Term



- in few GeV energy regime decay and excitation of resonances dominate hadronic cross section
- work in progress: include string fragmentation

Dileptons in SMASH

- dileptons produced by resonance decays
- direct and Dalitz dilepton decay channels
- rare e.m. decays —> Time-Integration-Method / *Shining*
 - continuously perform dilepton decays and weight them by taking their decay probability into account (better statistics)
- for details and more results:

JS, J. Weil, V. Steinberg, S. Endres, H. Petersen
arXiv:1711.10297

Dilepton Decays

$$\rho \rightarrow e^+ e^-$$

$$\omega \rightarrow e^+ e^-$$

$$\phi \rightarrow e^+ e^-$$

$$\pi \rightarrow e^+ e^- \gamma$$

$$\eta \rightarrow e^+ e^- \gamma$$

$$\eta' \rightarrow e^+ e^- \gamma$$

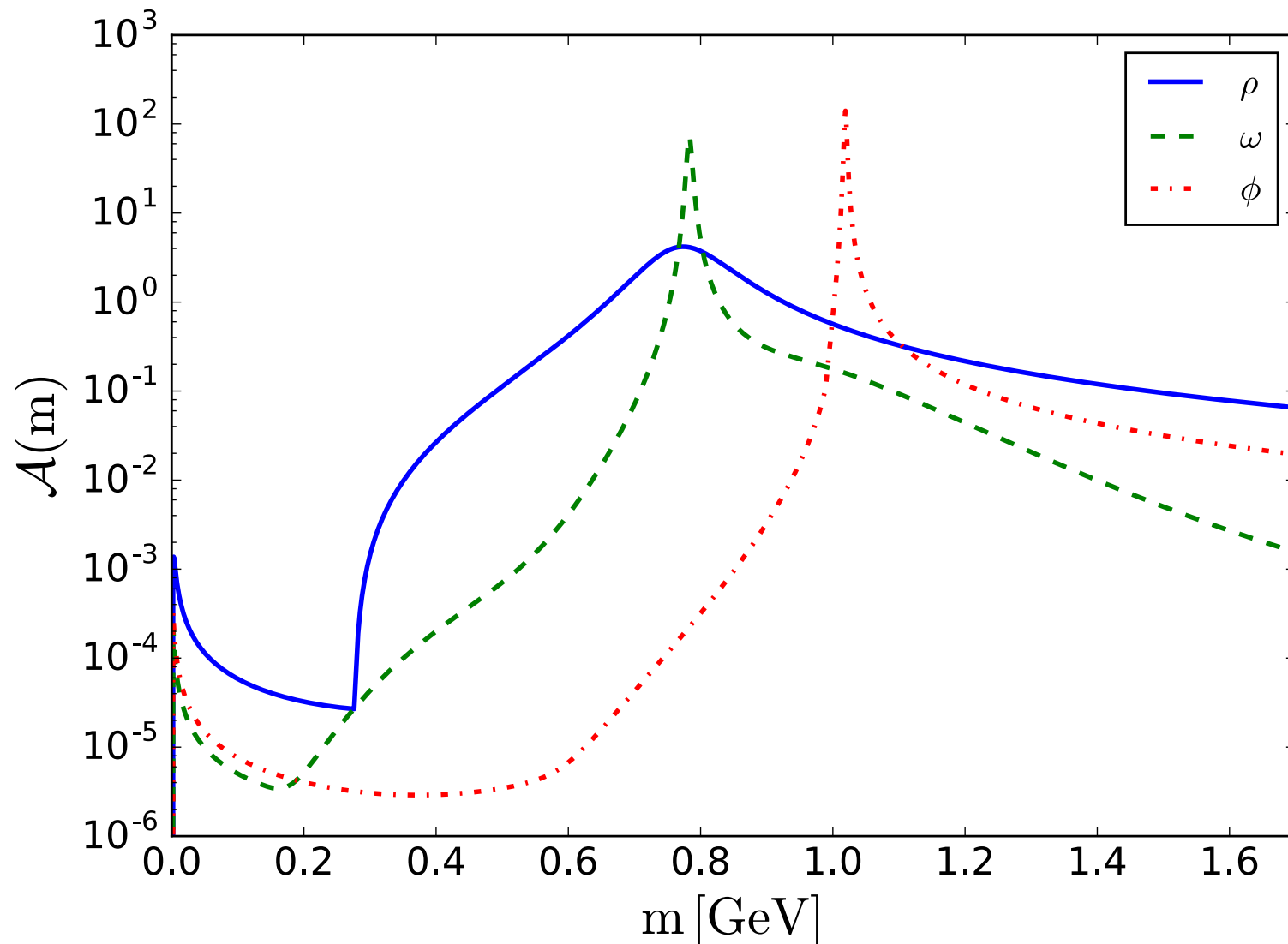
$$\omega \rightarrow e^+ e^- \pi^0$$

$$\phi \rightarrow e^+ e^- \pi^0$$

$$\Delta^+ \rightarrow e^+ e^- p$$

$$\Delta^0 \rightarrow e^+ e^- n^0$$

Spectral Functions

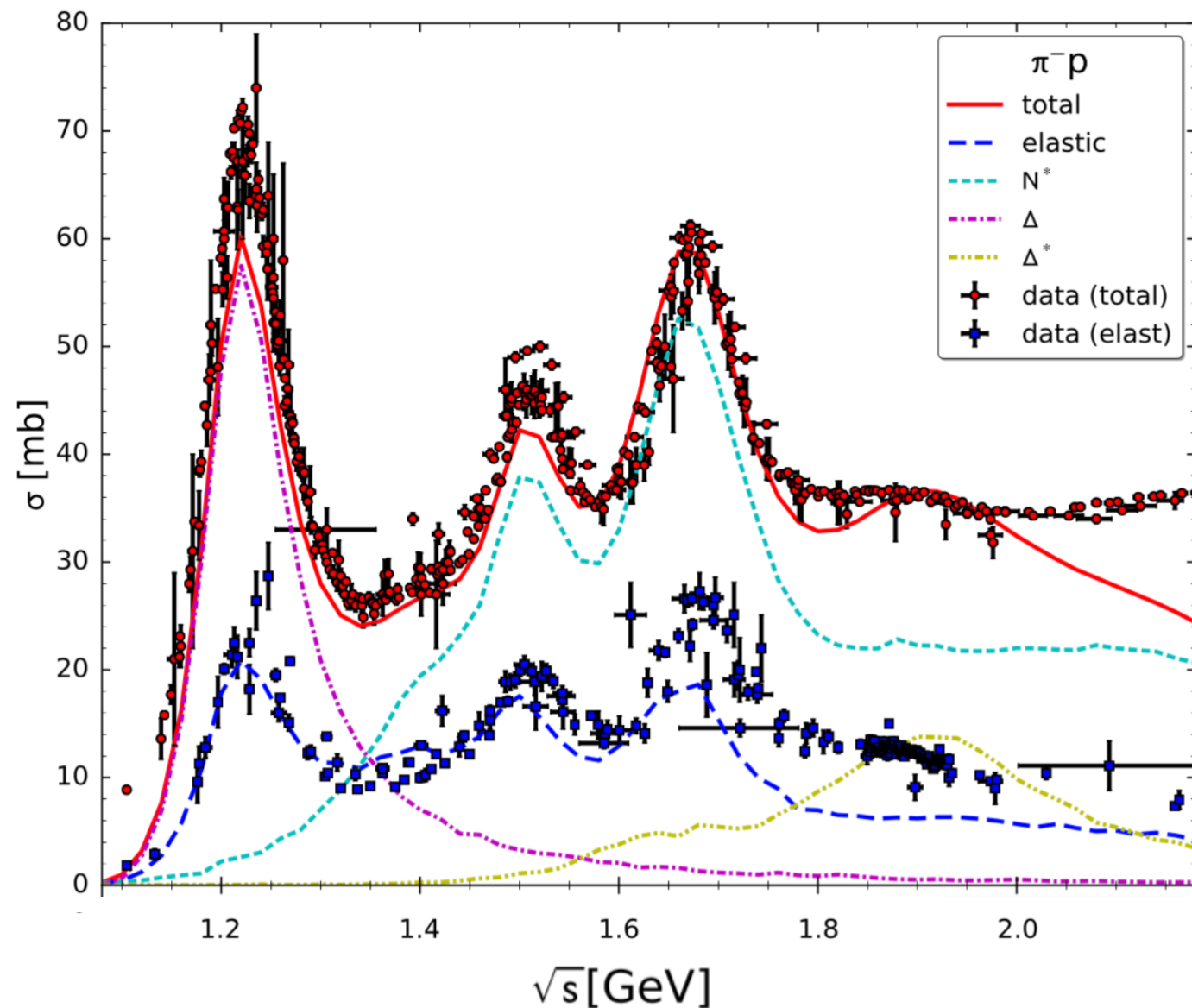


- relativistic Breit-Wigner (no density or temperature dependence $\rightarrow$ vacuum)
- spectral function for vector mesons take dilepton decay into account
- contributions below hadronic threshold from dilepton decay width

$$\mathcal{A}(m) = \frac{2\mathcal{N}}{\pi} \frac{m^2 \Gamma(m)}{(m^2 - M_0^2)^2 + m^2 \Gamma(m)^2}$$

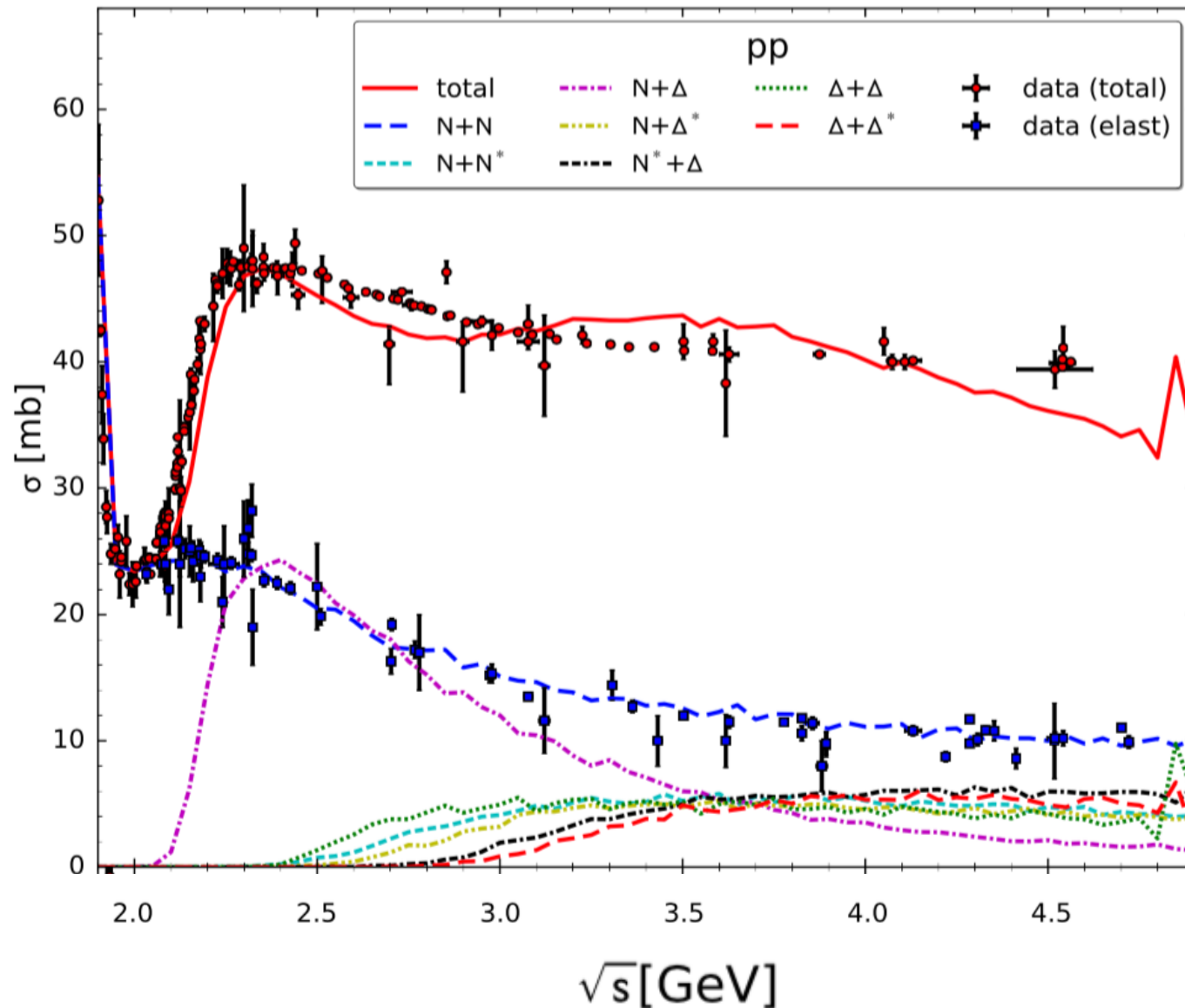
Results

Total Cross Section



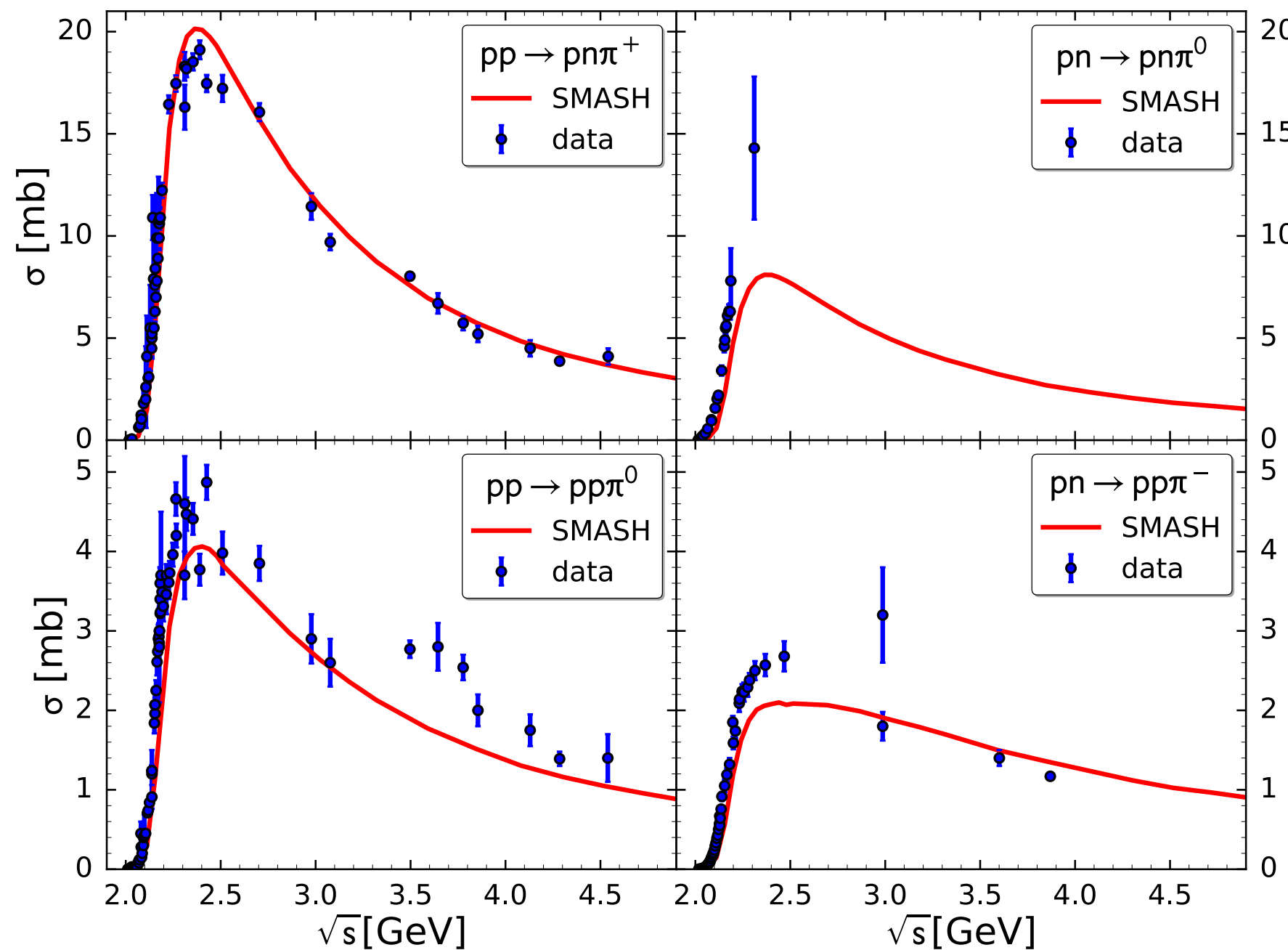
- total π -p cross section
- lowest excitation from Δ , additional contributions from N^* and Δ^*
- compatible with data up to 2 GeV

Total Cross Section



- total pp cross section
- parametrized elastic cross section
- many resonance contributions to inelastic cross section
- reasonable description of data up to 4 - 4.5 GeV

Single Pion Production

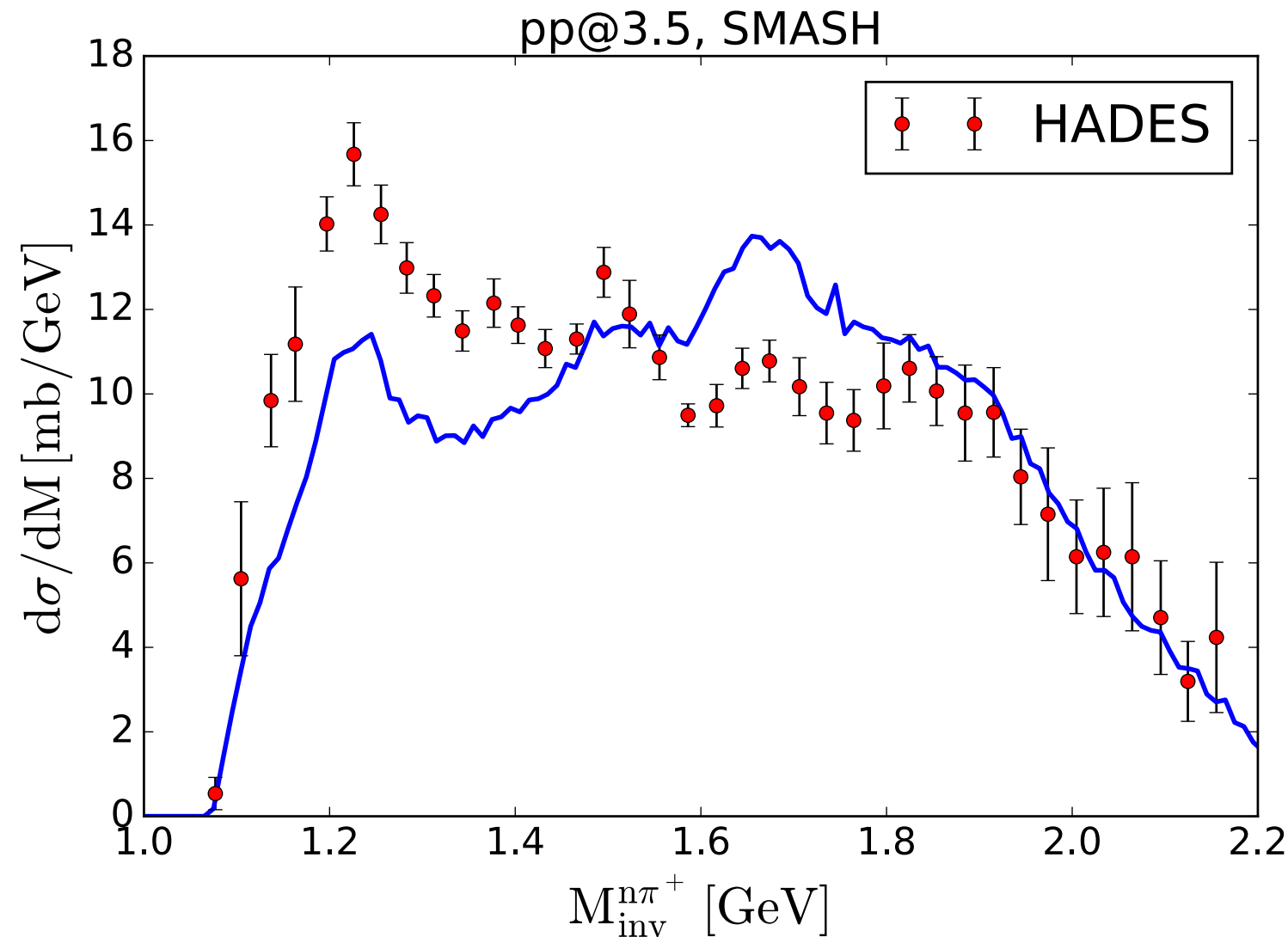


- exclusive cross section for single pion production in NN collisions
- dominant contribution from Δ resonance
- overall reasonable agreement with data

Exclusive Cross Section

$$pp \rightarrow pn\pi^+$$

HADES, *Eur. Phys. J., A50* (2014)



J. Weil et al, Phys. Rev. C 94 (2016)

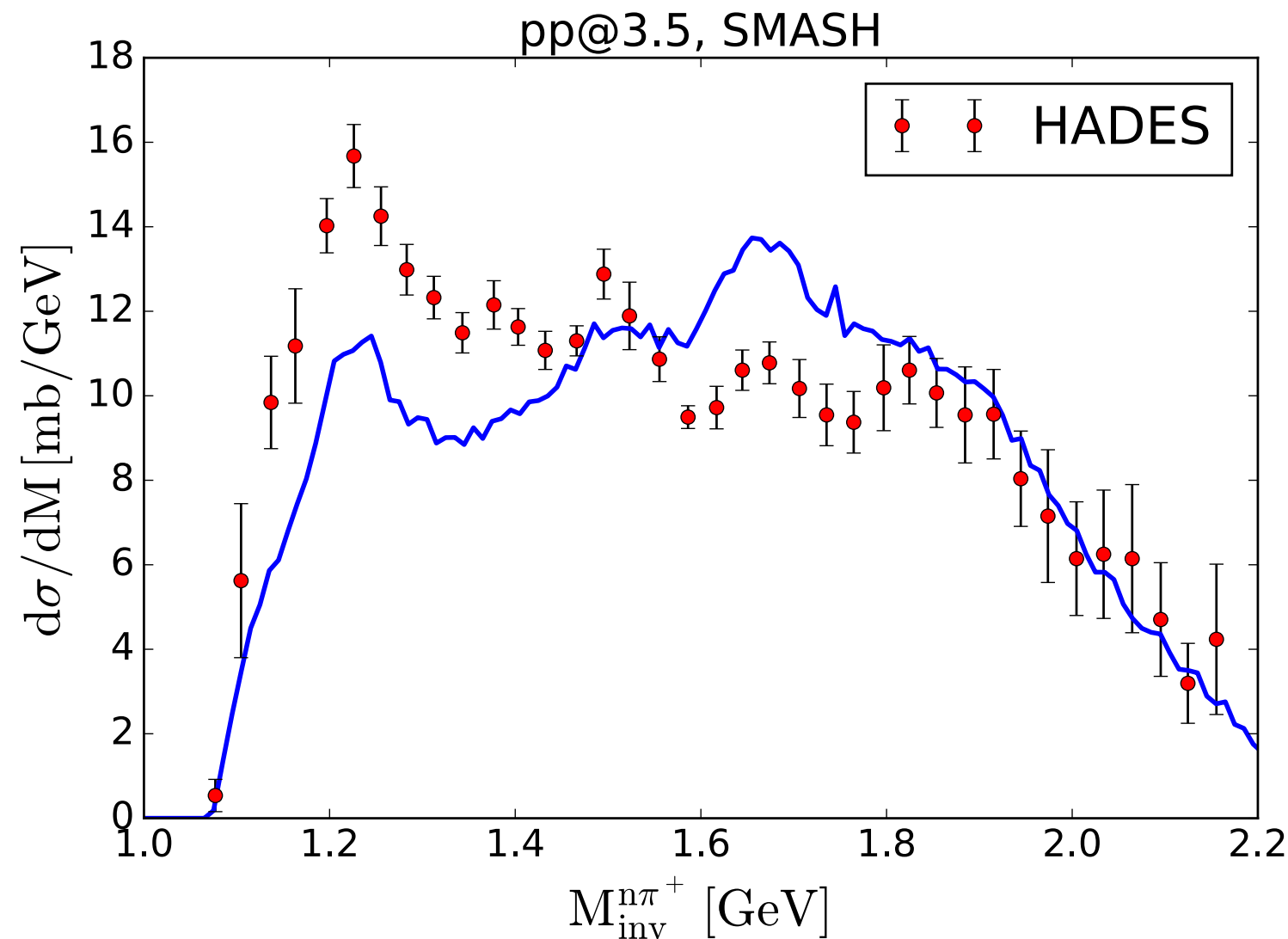
S.A. Bass et al, Prog. Part. Nucl. Phys. 41 (1998)

- invariant mass spectrum of $n\pi^+$
- probes baryonic resonance production cross section in primary NN reactions
- work in progress
- comparison to experimental data similar to UrQMD

Exclusive Cross Section

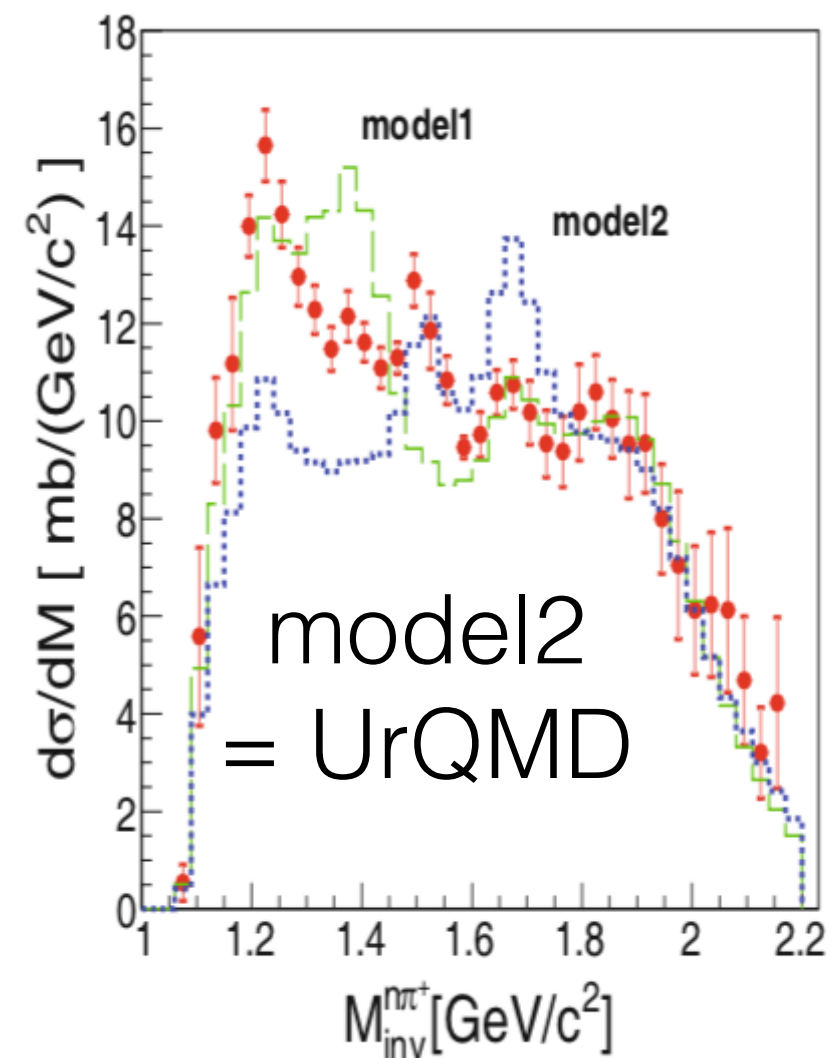
$$pp \rightarrow pn\pi^+$$

HADES, *Eur. Phys. J., A50* (2014)



J. Weil et al, Phys. Rev. C 94 (2016)

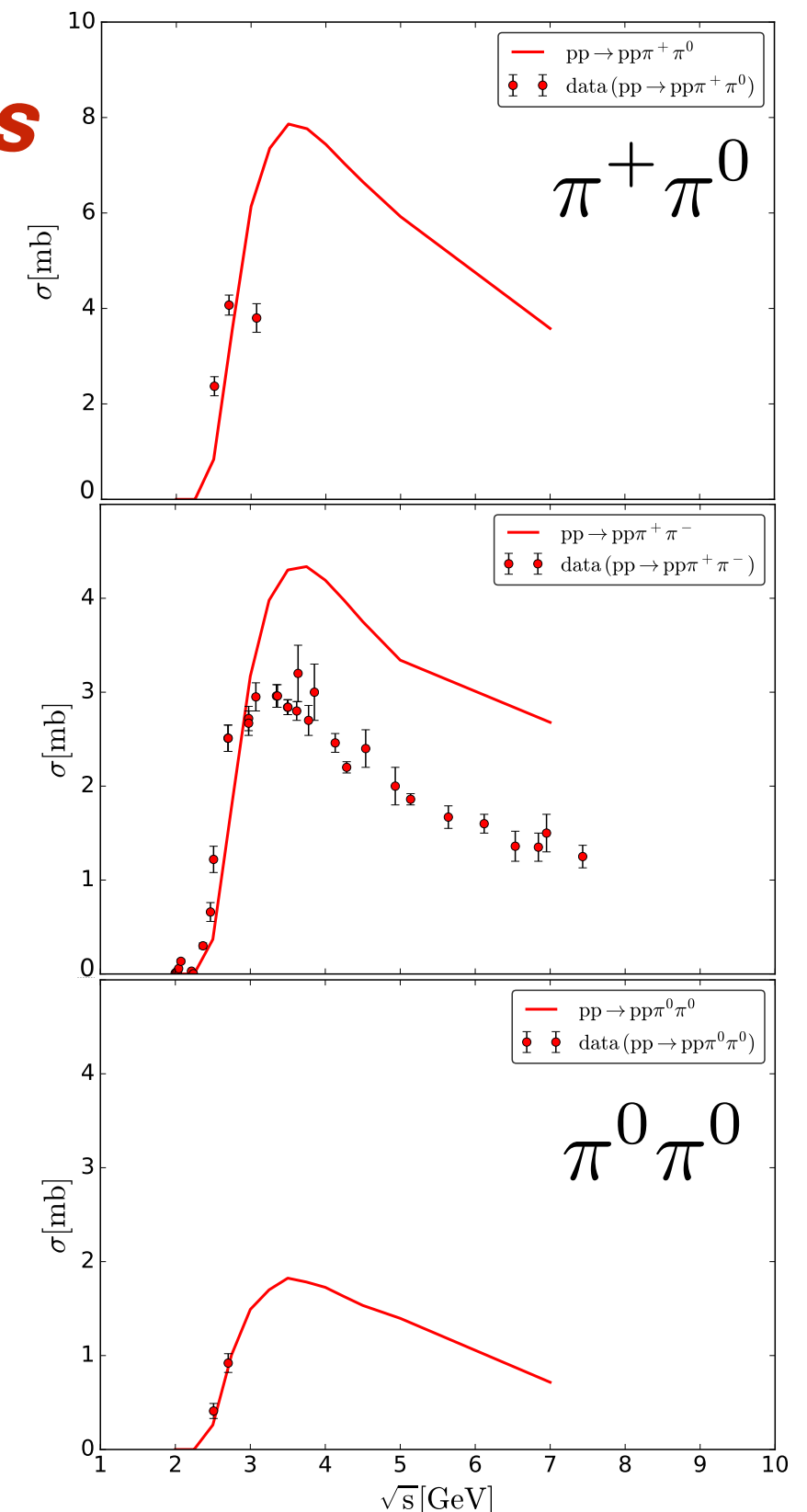
S.A. Bass et al, Prog. Part. Nucl. Phys. 41 (1998)



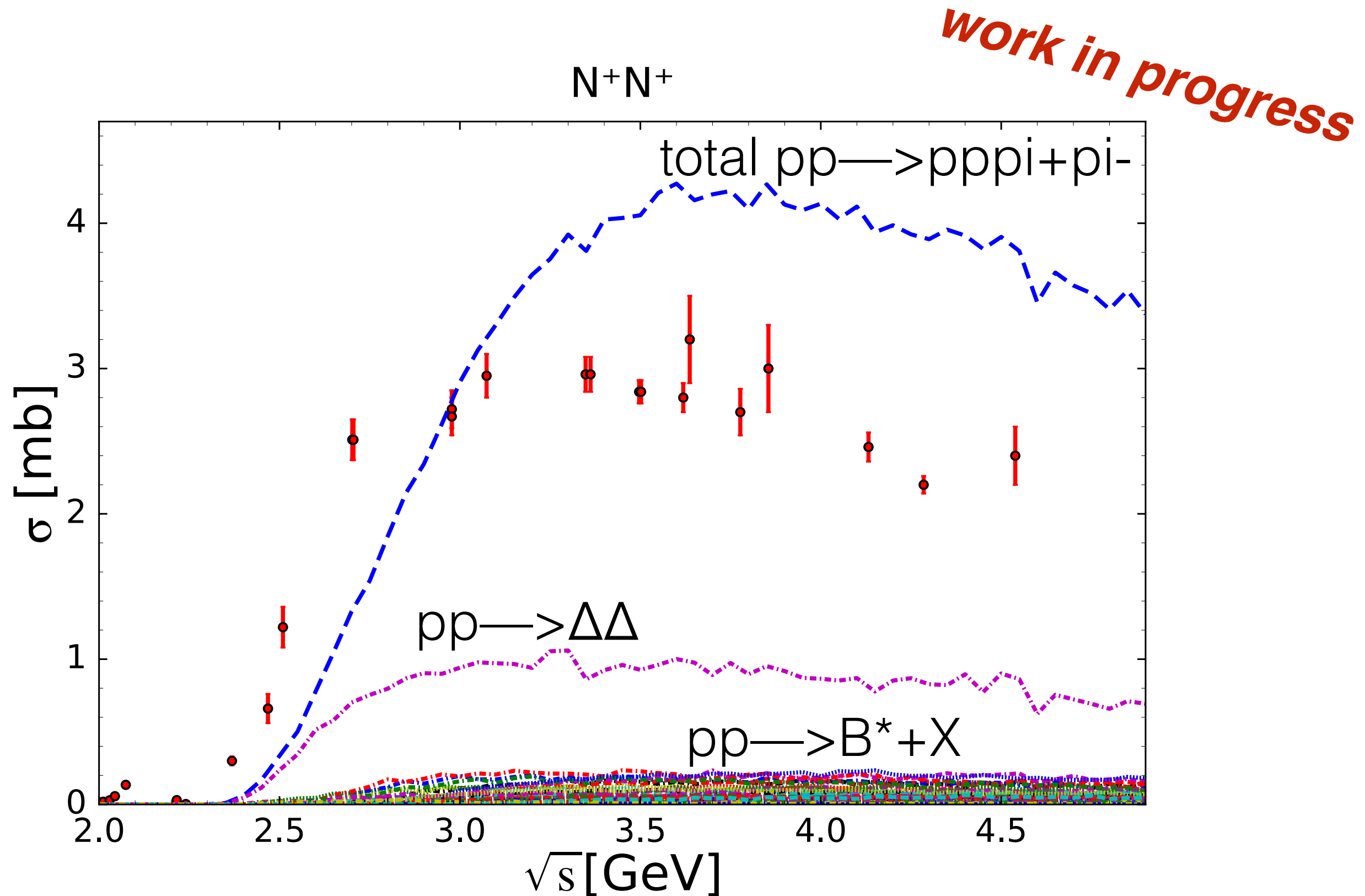
Two-Pion Production

work in progress

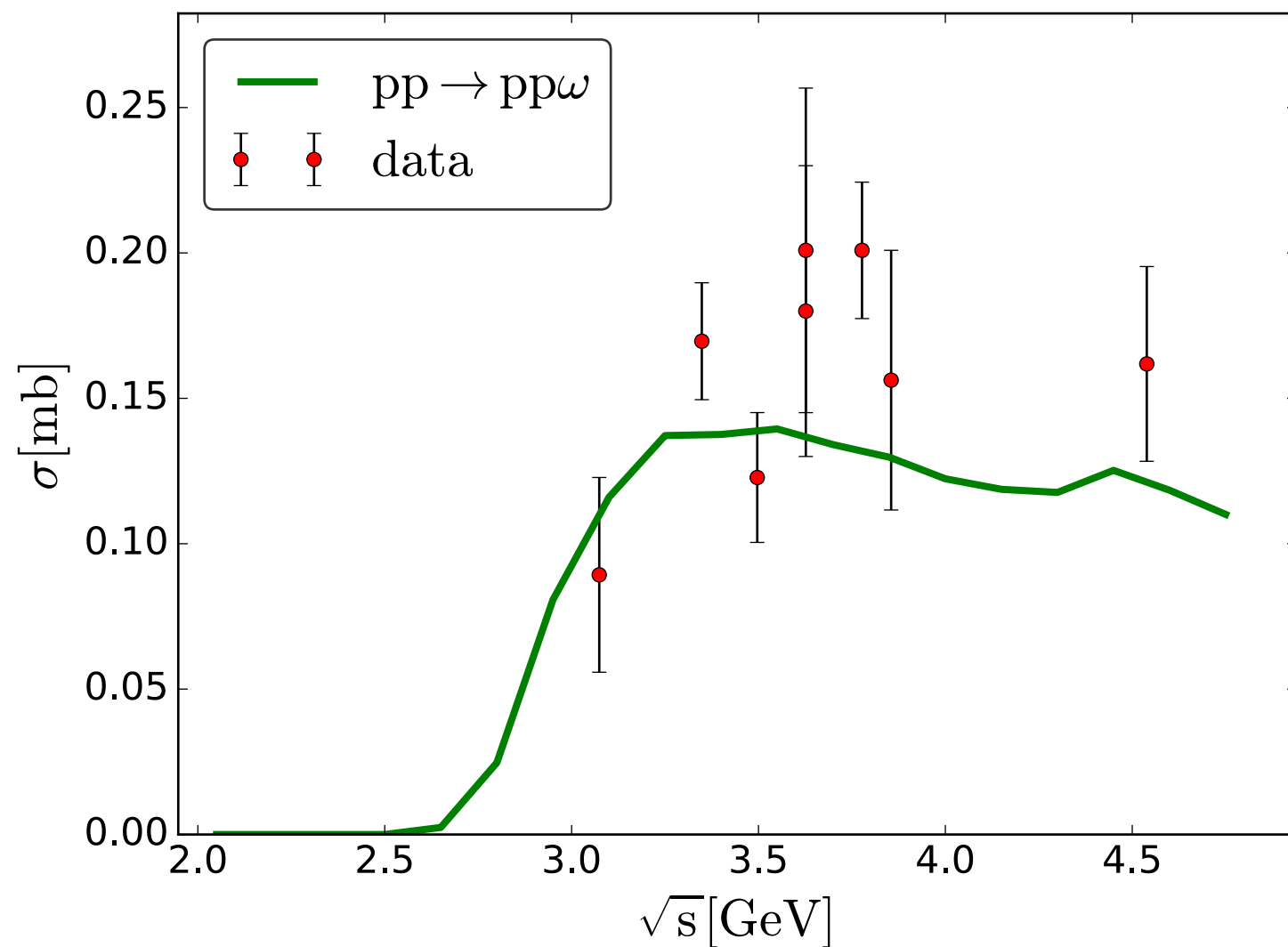
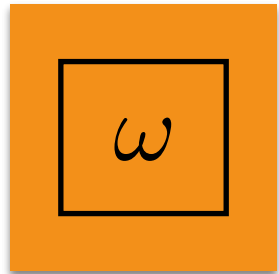
- current status for exclusive cross section for two-pion production in pp collisions
- experimental data not as well described (e.g. in $\pi^+\pi^-$)
- potential solutions:
 - improved matrix elements for $NN \rightarrow \Delta\Delta$ ($\Delta\Delta$ =dominant contribution)
 - constrain B.R. for heavy resonances
- feedback welcome



Two-Pion Contributions

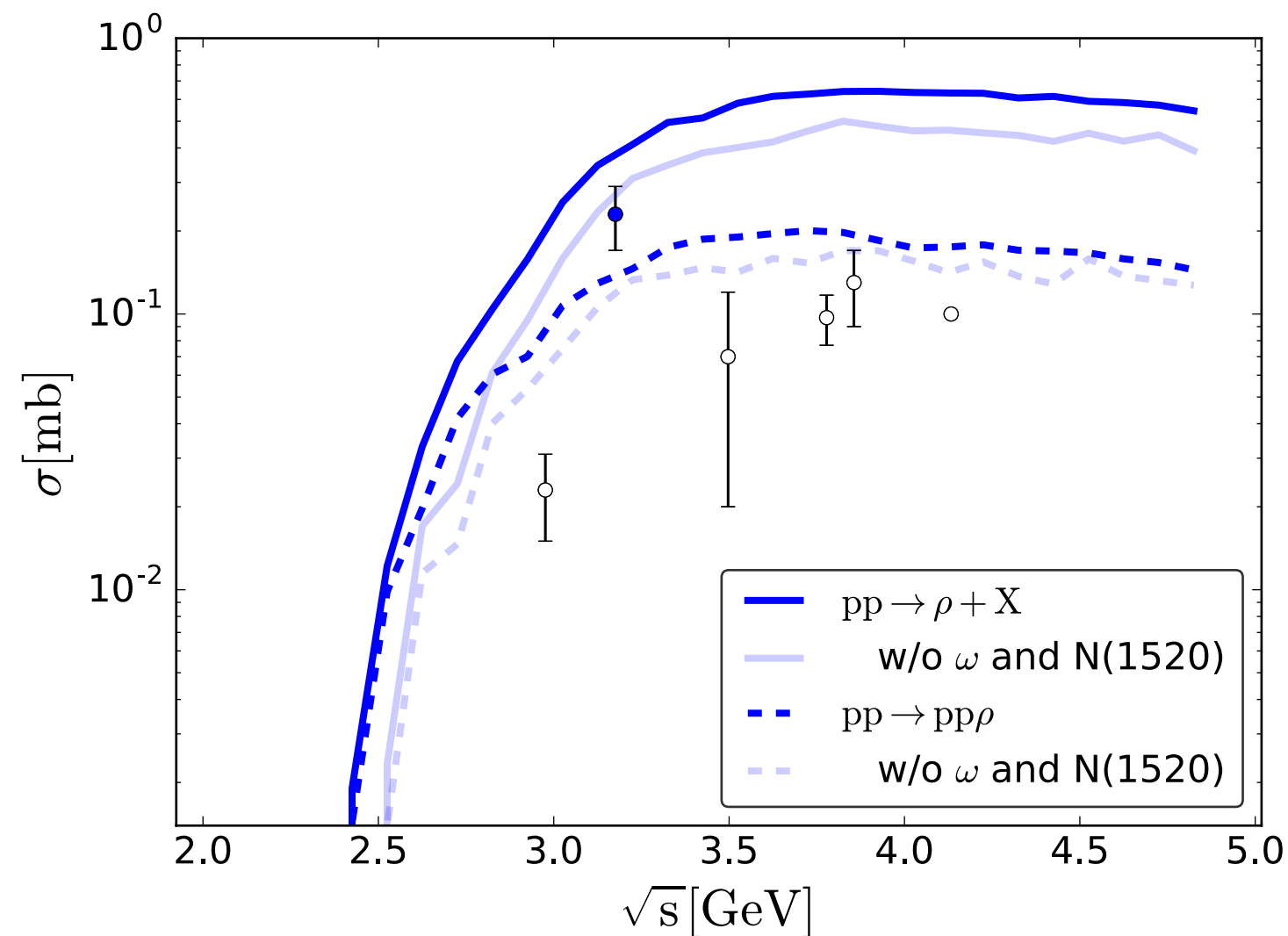
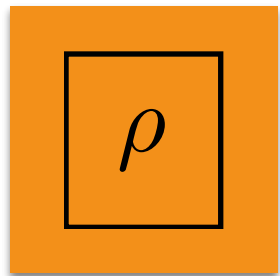


Exclusive Cross Section



- investigating the exclusive production cross section of resonances
- exclusive production of ω via $pp \rightarrow pp\omega$
- reasonable agreement with data for different energies

Exclusive Cross Section



- inclusive and exclusive production of ρ mesons in proton-proton
- overshooting for inclusive cross section may be caused by two step treatment of decays e.g.

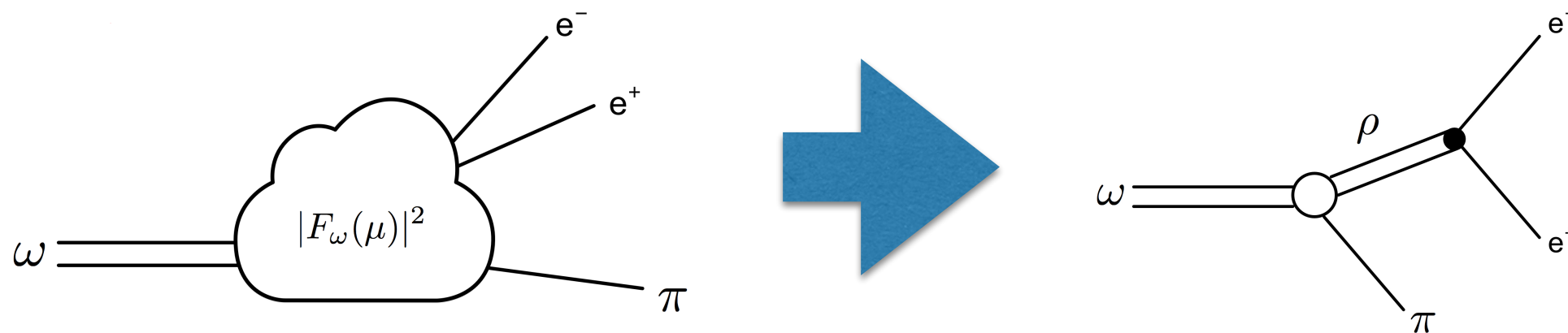
$$N^*(1520) \rightarrow N\rho \rightarrow Ne^+e^-$$

$$\omega \rightarrow \pi\rho \rightarrow 3\pi$$

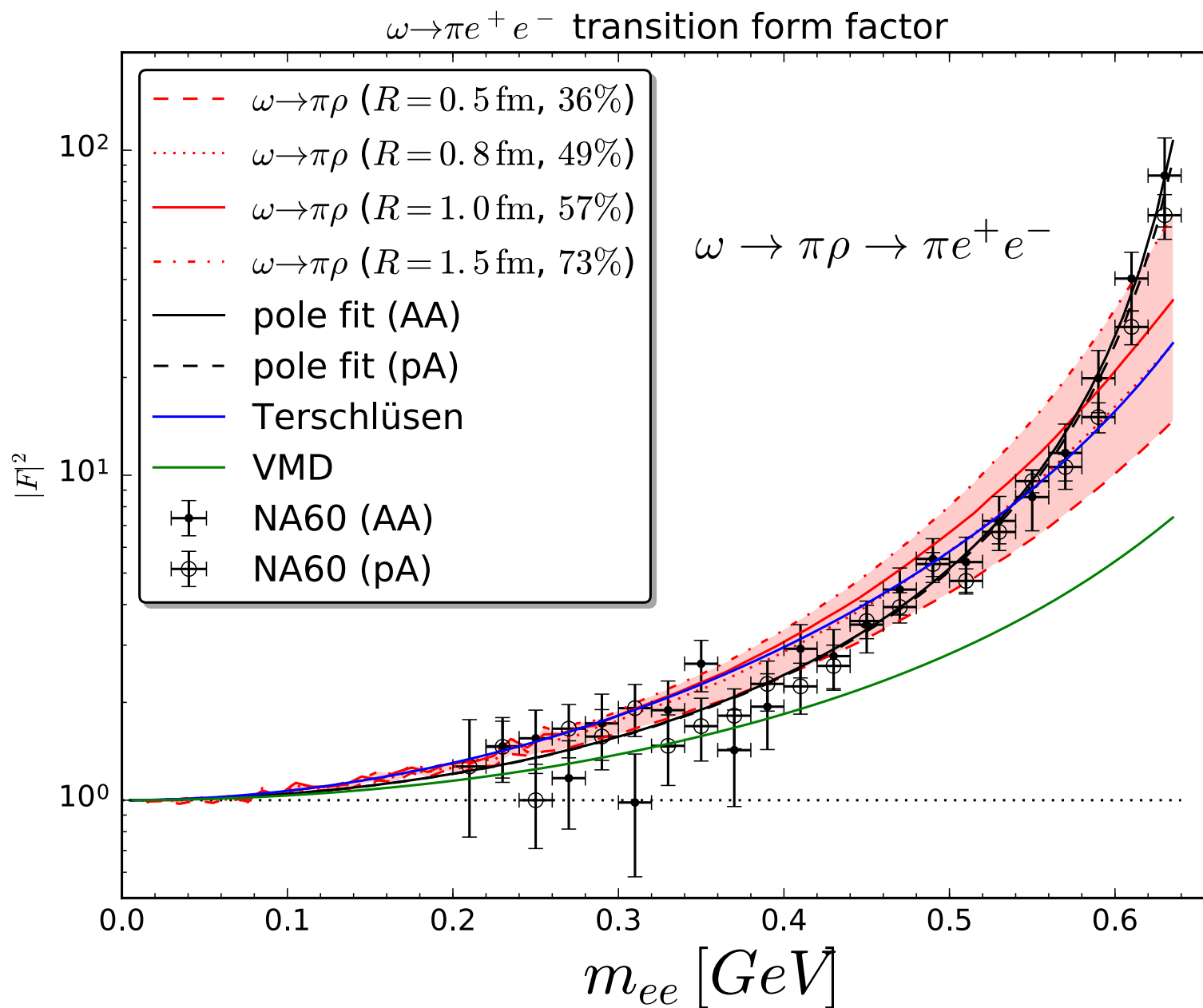
Form Factors

Form Factors

- dilepton routine was used to investigate the e.m. transition form factor of the omega dilepton Dalitz decay $\omega \rightarrow \pi^0 e^+ e^-$ *J. Weil, JS, Hannah Petersen, arXiv:1604.07028v1*
- decay described by two steps similar to hadronic ω decay into 3π : $\omega \rightarrow \rho\pi \rightarrow 3\pi$ (VMD-inspired)



Form Factors: ω



- comparison of our ansatz with NA60 data

Phys.Lett. B677 (2009) 260-266

- variation of B.R. and cutoff-parameter R

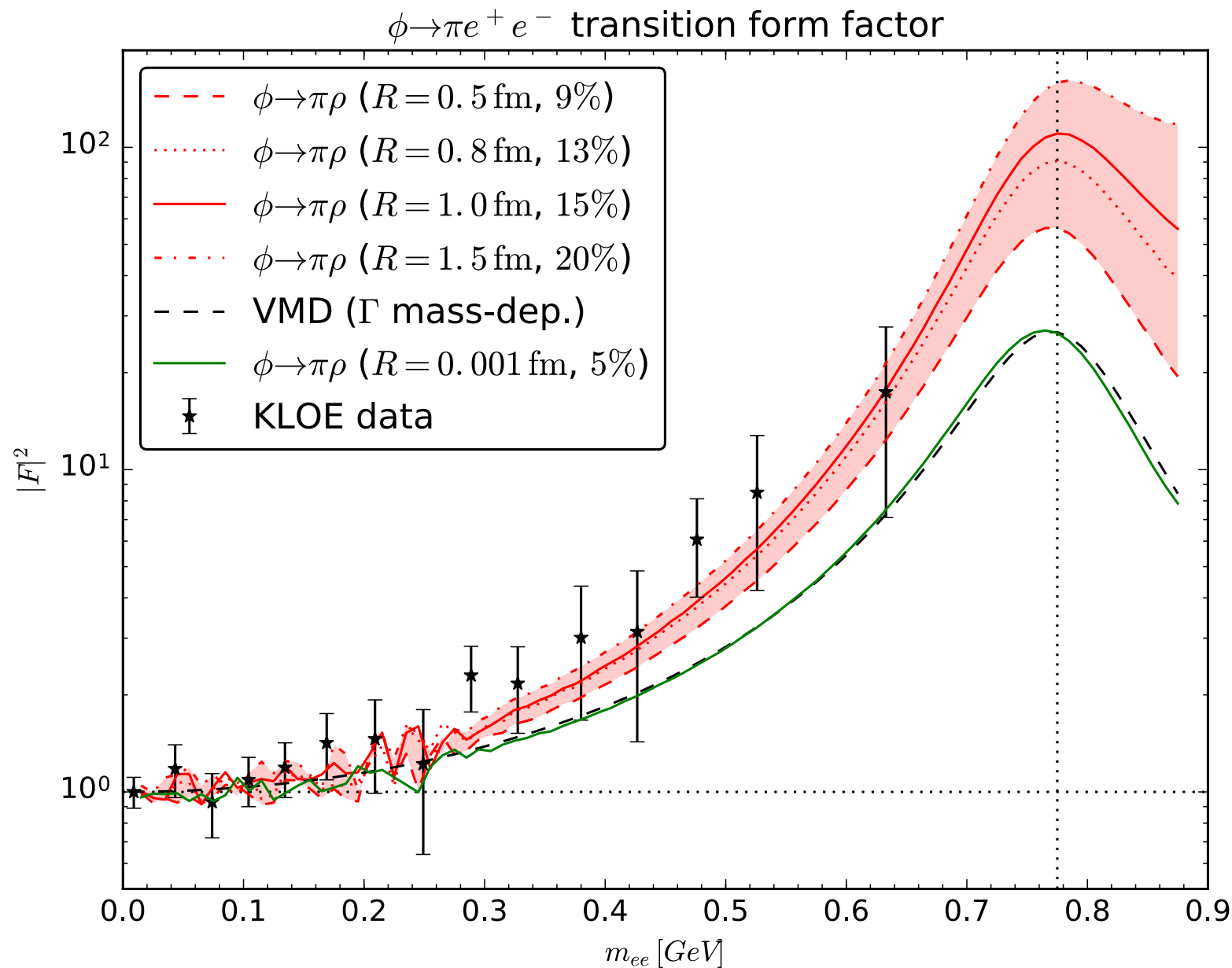
- description of data with B.R. of 57% possible

$$B.R.(\omega \rightarrow 3\pi) = 89\%$$

- also compatible with Terschlüsen approach

Terschlüsen, Strandberg, Leupold and Eichstädt, Eur. Phys. J. A 49 116

Form Factors: Φ

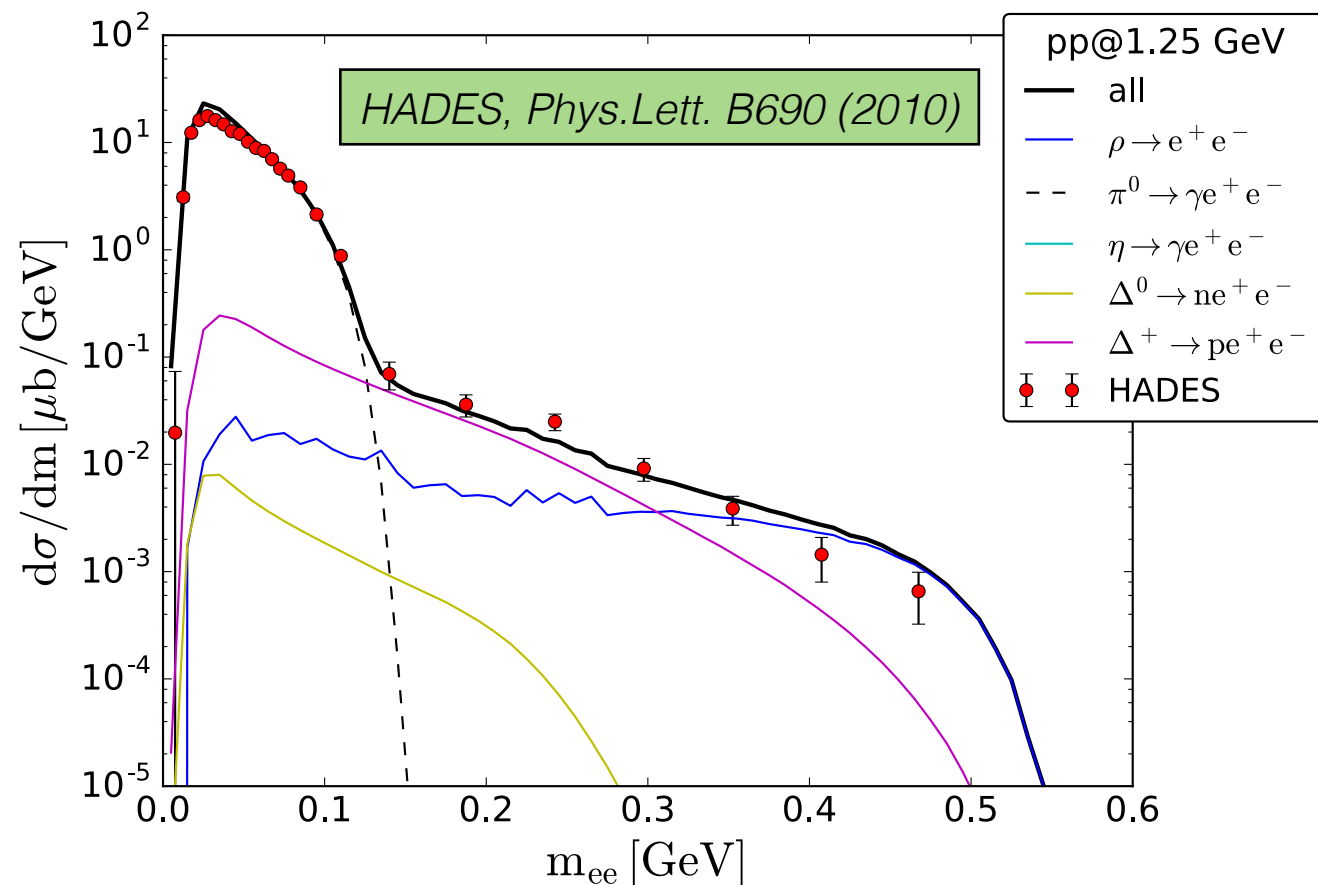


- same ansatz for the Φ meson
- comparison with data from KLOE
Phys. Lett. B 757 (2016) 362
- description of data suggests B.R. of 15% $B.R.(\phi \rightarrow 3\pi) = 15\%$
- again better description than „simple“ VMD

Dileptons

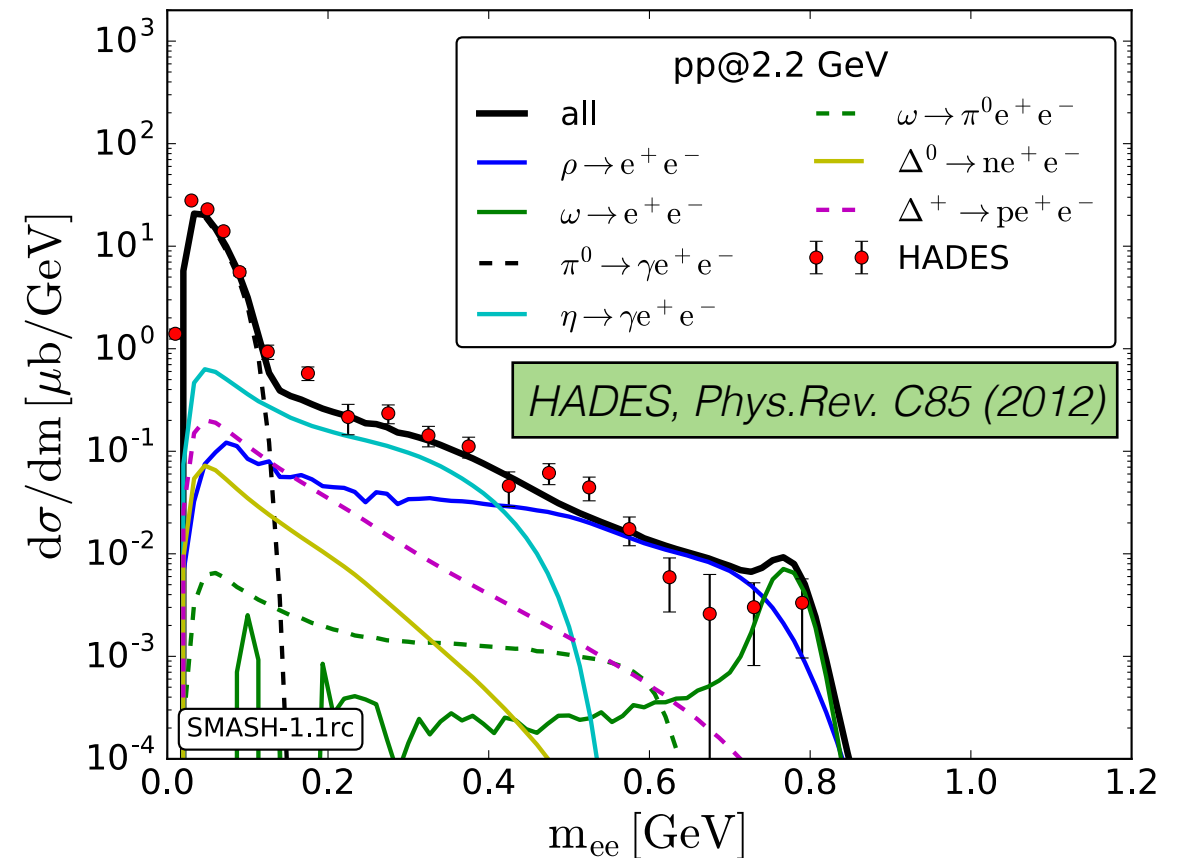
Low Energy pp Collisions

pp, 1.25 GeV



- dominant channels are π , ρ , Δ
- agreement with data

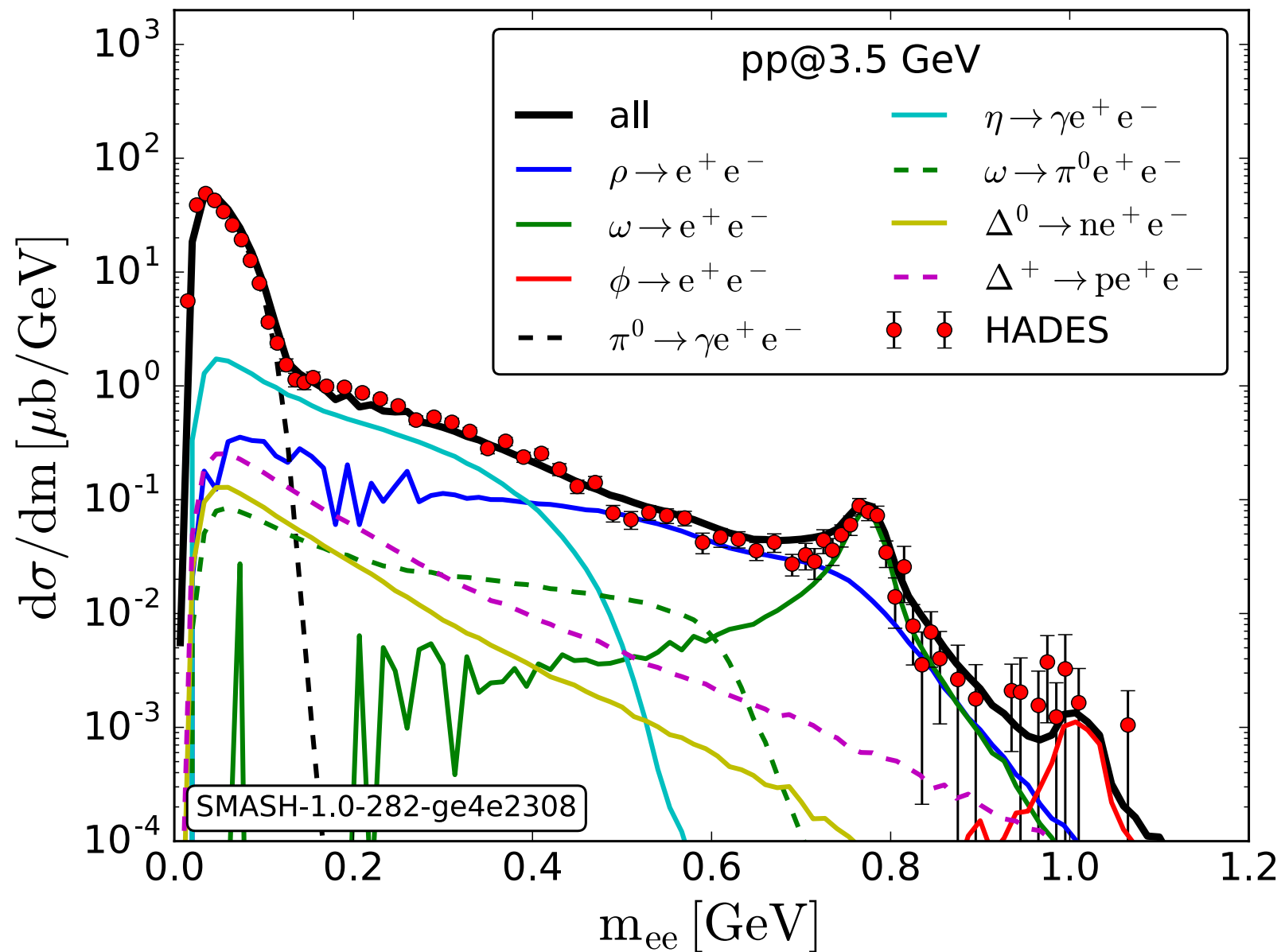
pp, 2.2 GeV



- above η threshold
- slight overproduction in high invariant mass region

Low Energy pp Collisions

pp, 3.5 GeV



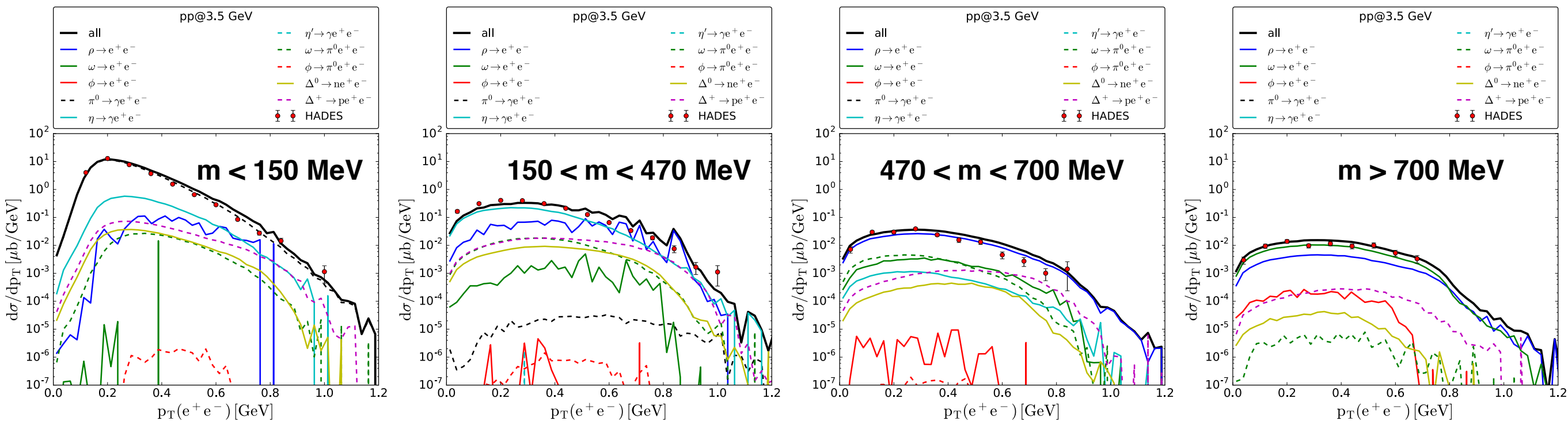
- invariant mass spectrum for pp collision with $E_{\text{kin}} = 3.5$ GeV
- constraining elementary reaction baseline
- sub-threshold contributions by direct vector mesons decays
- very good agreement with data

HADES, *Eur.Phys.J. A48* (2012)

p_T Spectra

HADES, *Eur.Phys.J. A48* (2012)

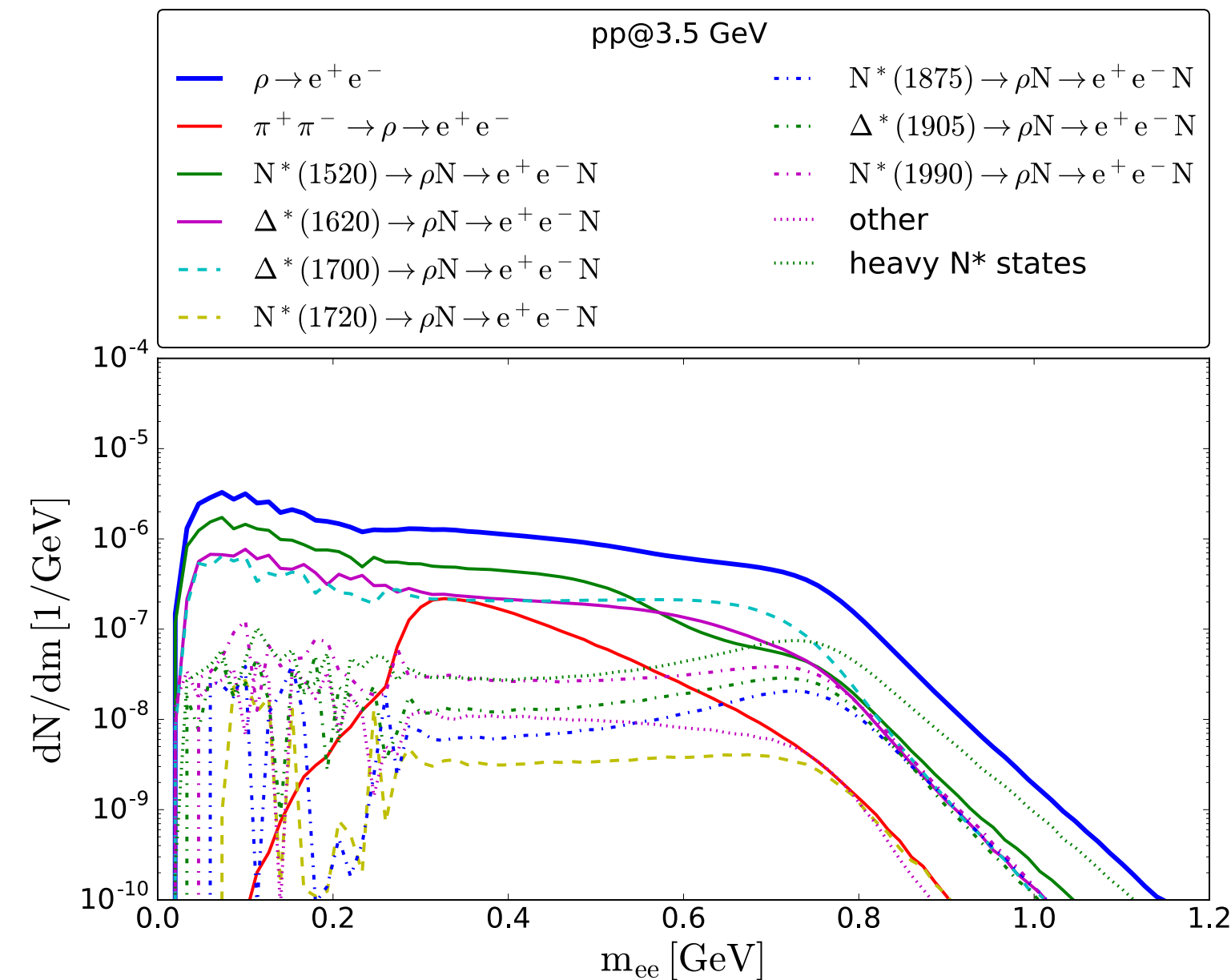
pp, 3.5 GeV



- comparison of p_T spectra for different invariant mass windows
- reasonable agreement for elementary reactions in all regions of phase space

ρ Origin in Dilepton Spectra

pp, 3.5 GeV



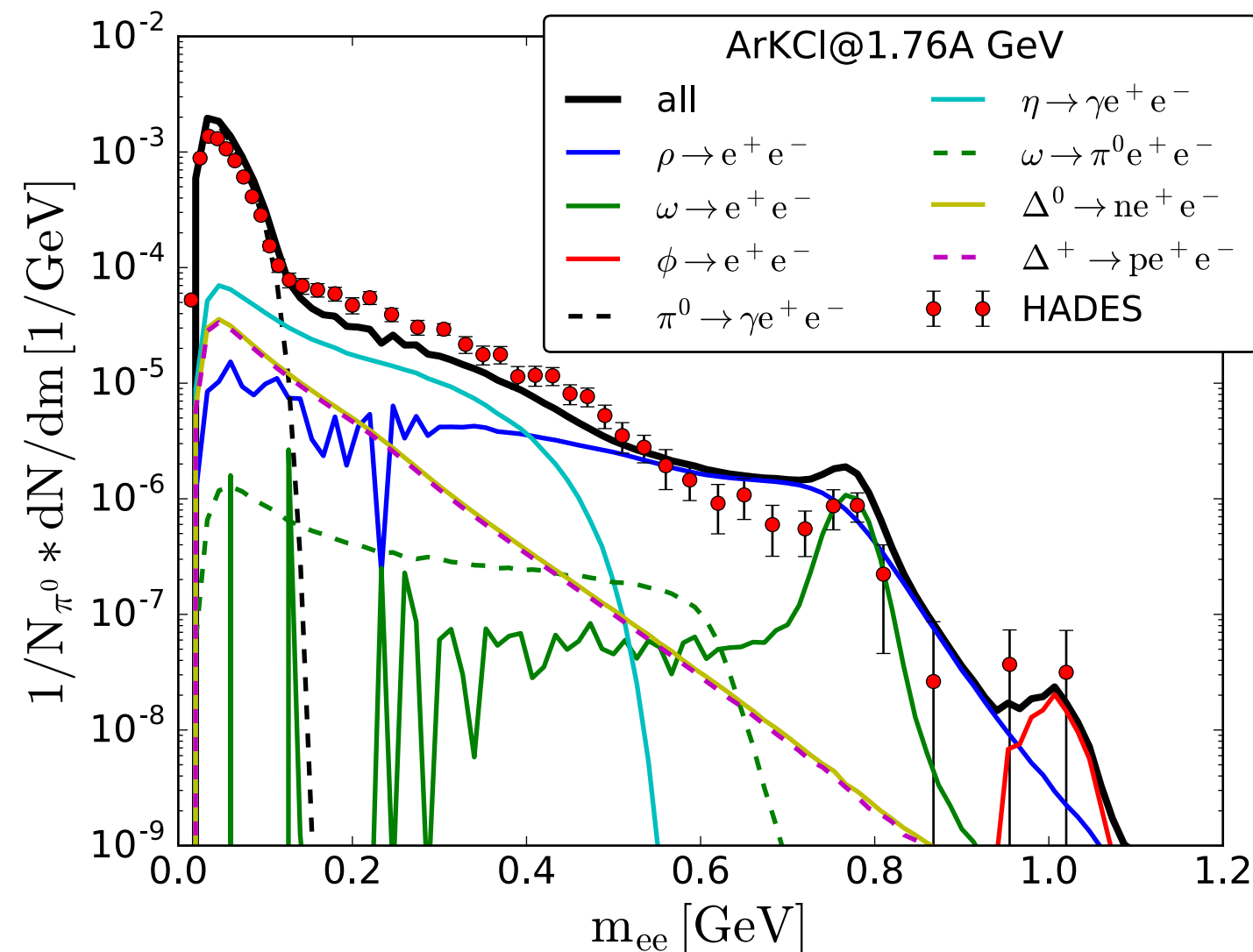
- different processes that produce ρ that decays into di-electrons
- valuable to understand the broad ρ contribution
- mostly baryonic resonance decays, plus small pion annihilation
- sub-threshold contribution by light baryonic resonance decays

Larger Systems: ArKCl

ArKCl, 1.76 AGeV

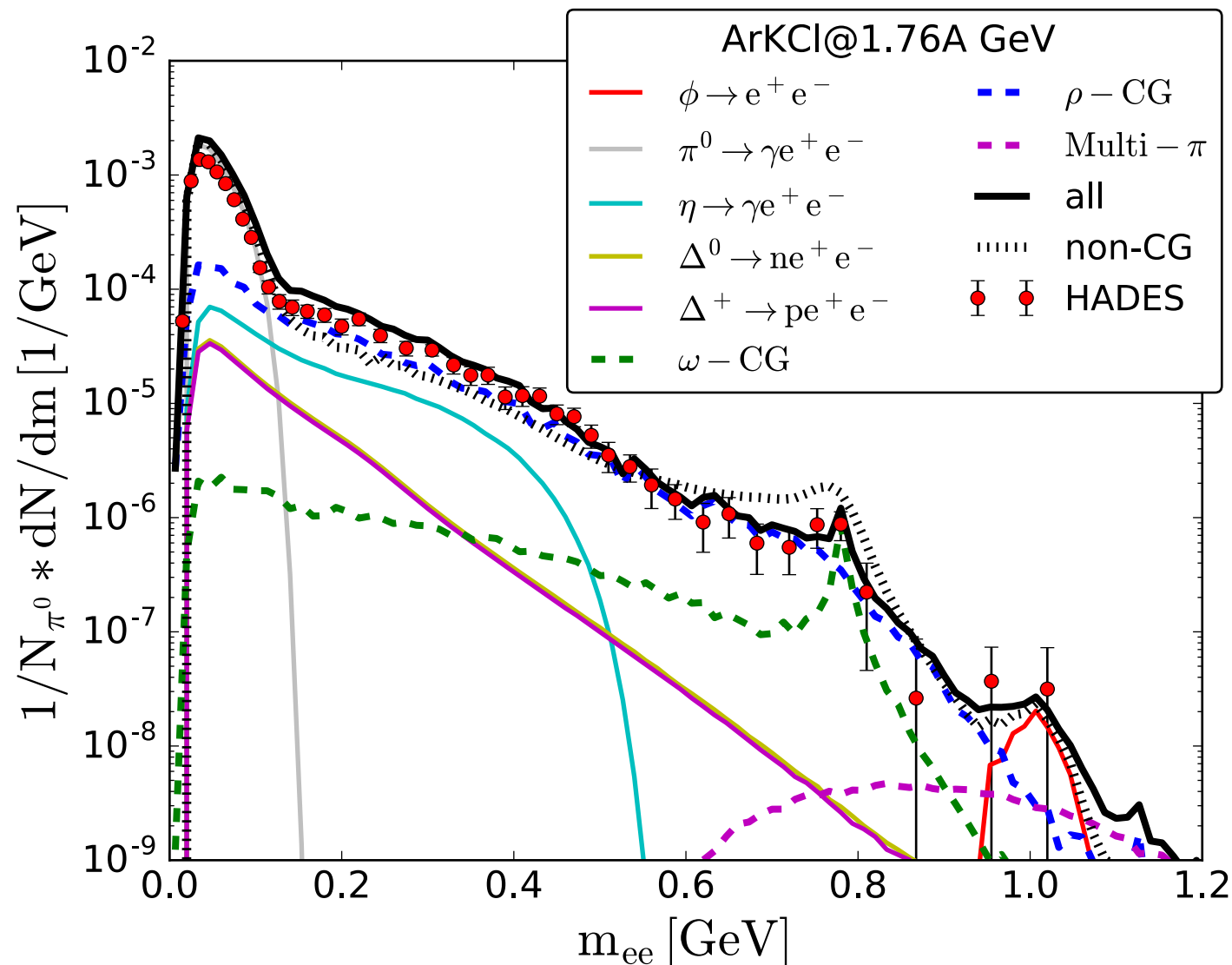
HADES, Phys.Rev. C84 (2011)

***based on elementary
baseline explore medium
effects in larger systems***



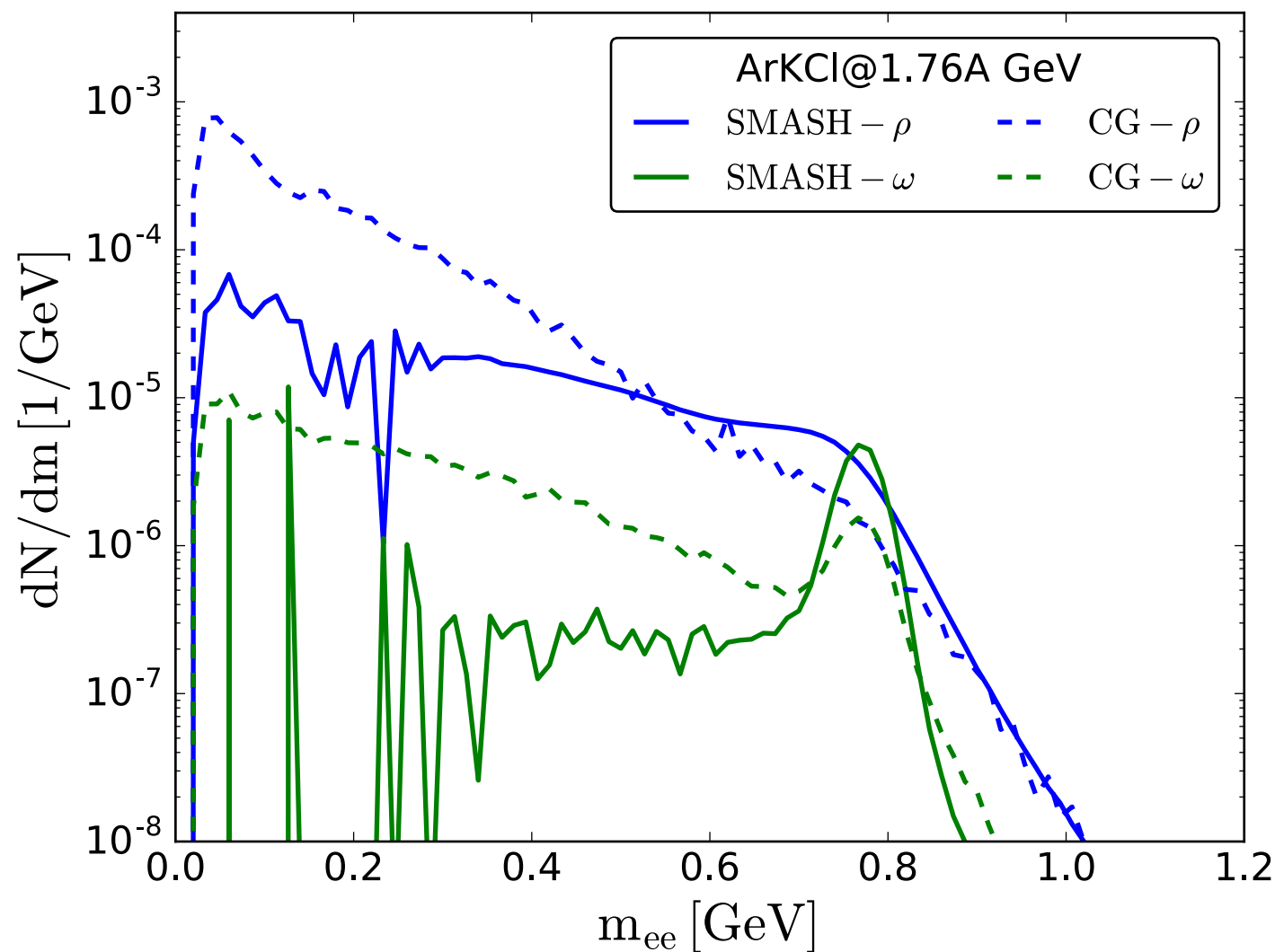
- ArKCl: example for larger system
- overestimation in rho pole mass region + underestimation in intermediate mass region
- vacuum resonances description insufficient?
explicit medium modification necessary?

Coarse-Graining Approach



- coarse-graining approach by Stephan Endres on SMASH evolution
Endres et al, Phys.Rev. C92 (2015)
- employs in-medium spectral function of vector mesons (ρ and ω)
Rapp, Wambach, Eur. Phys. J. A6 (1999)
- agreement with data suggest invariant mass spectrum of ArKCl sensitive to medium effects

Vector-meson Contributions

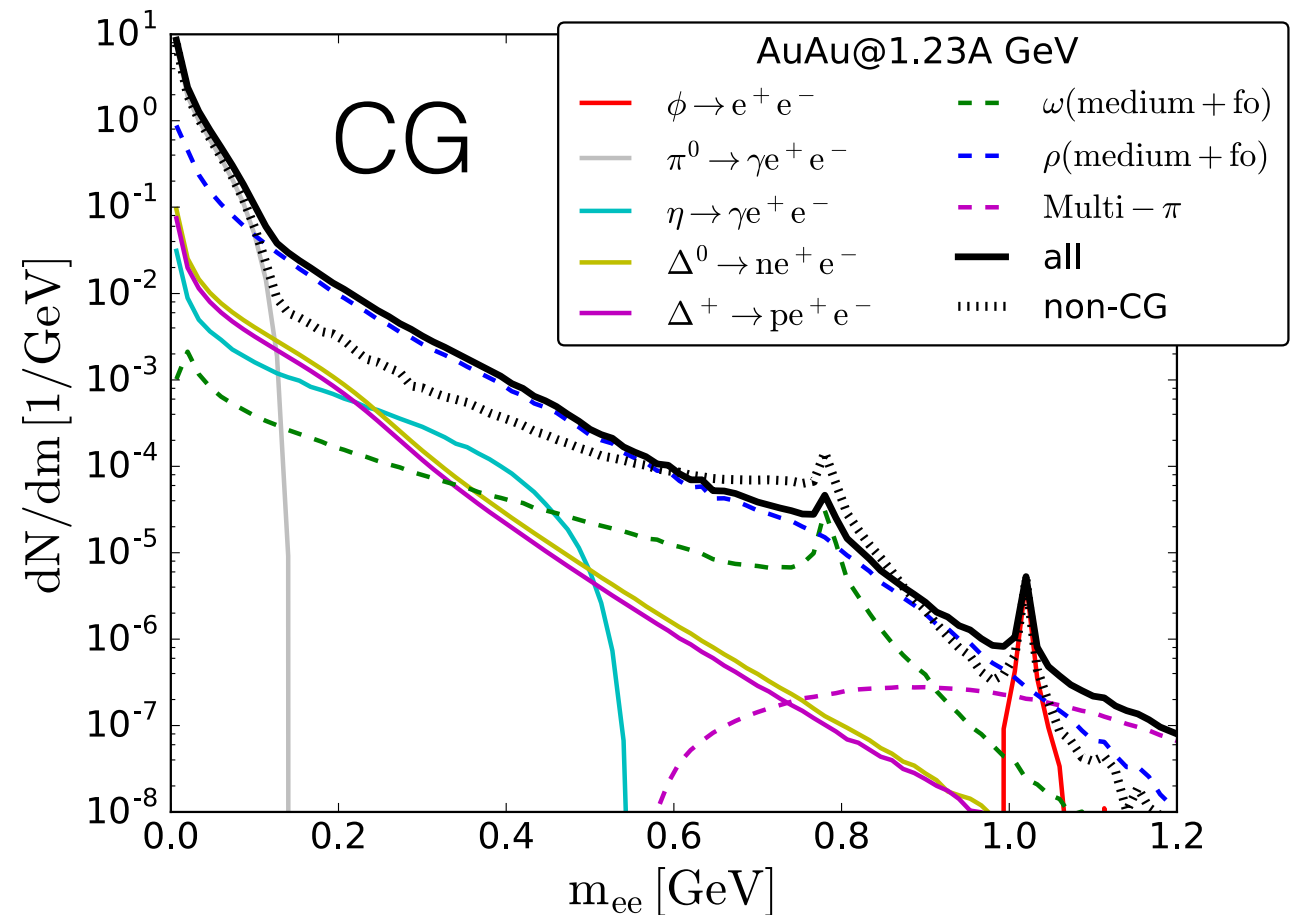
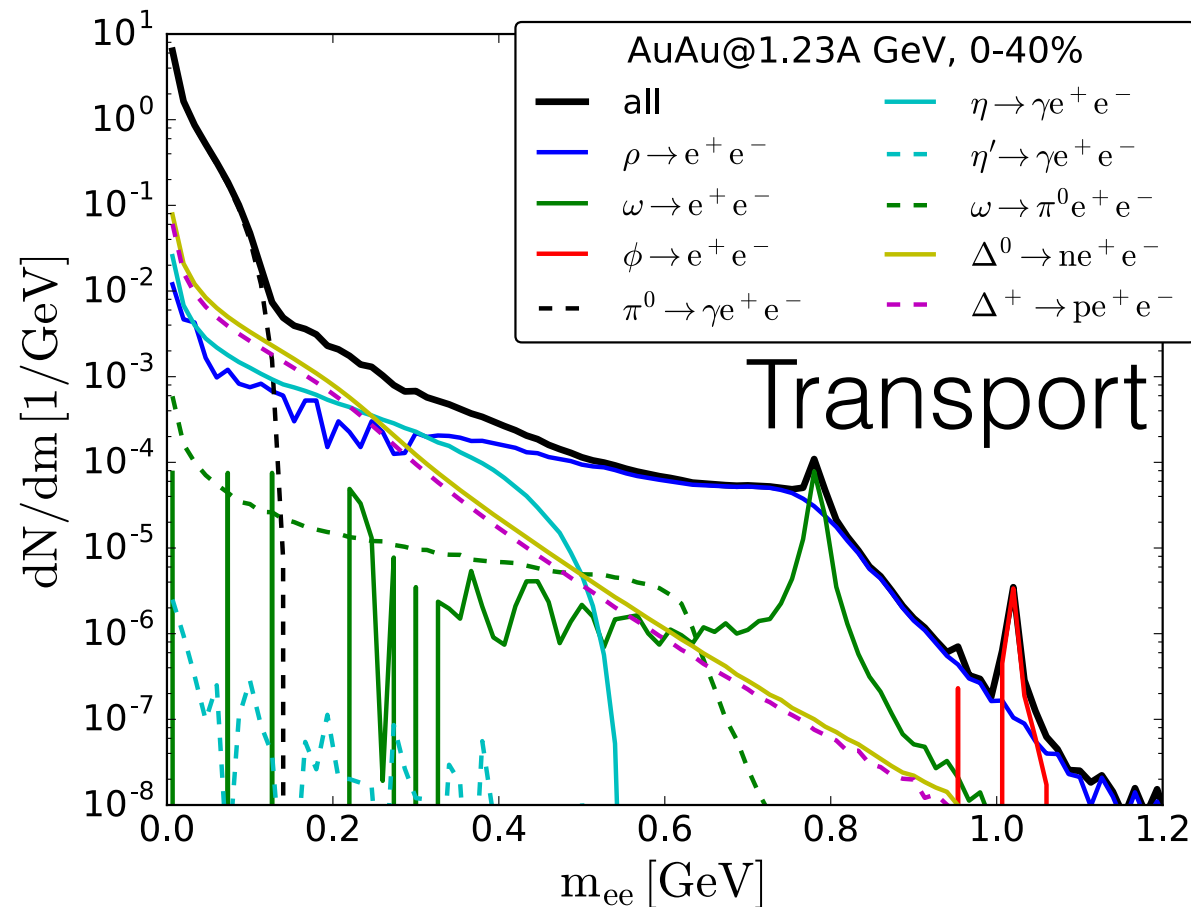


- comparison between vacuum and medium modified vector meson dilepton yields
- shift from pole mass region to low mass tail
- coupling between ρ and baryons in nuclear matter leads to low-mass tail for SMASH

$$B^* \rightarrow N\rho \rightarrow Ne^+e^-$$

Predictions for HADES

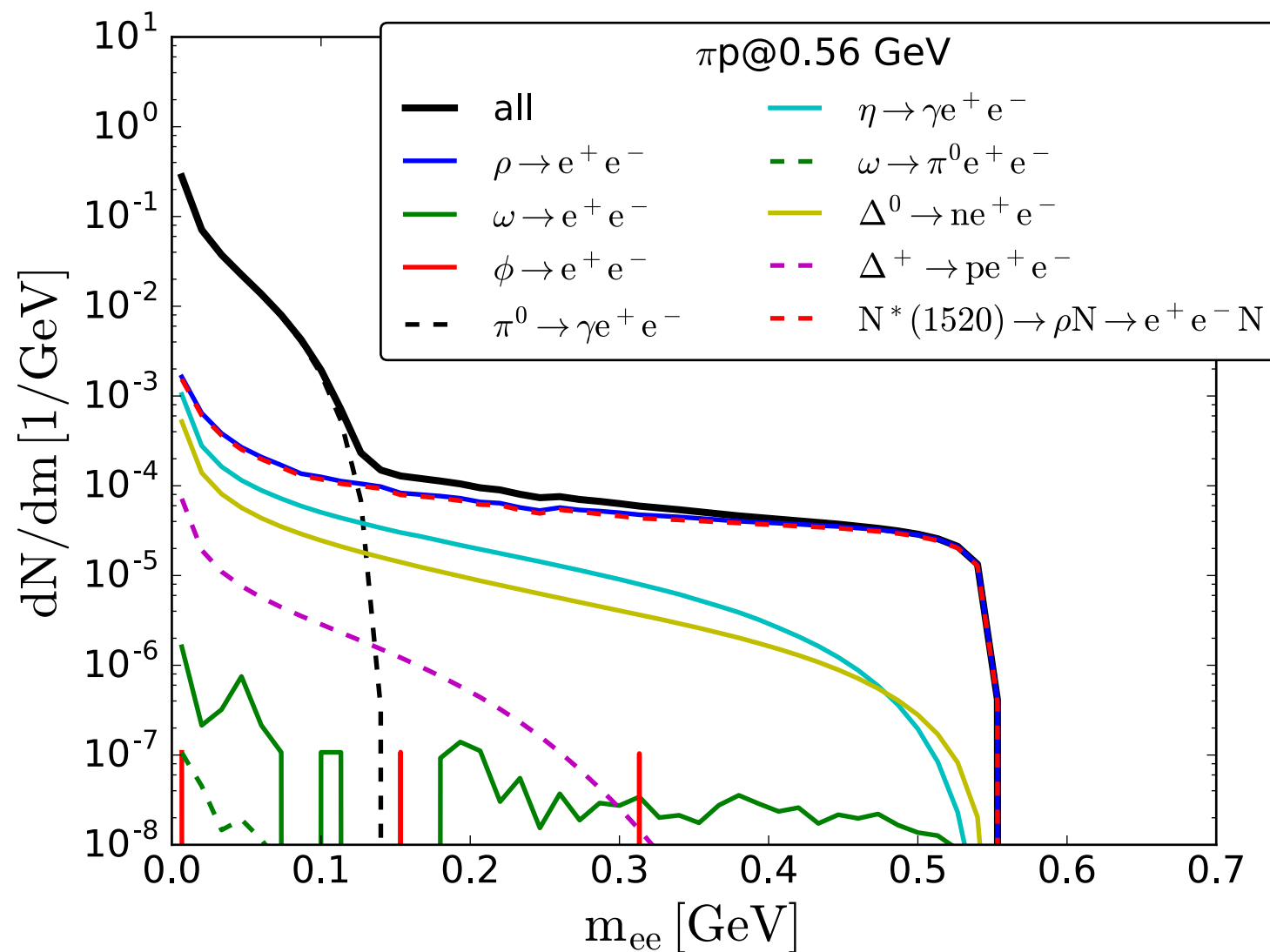
AuAu, 1.23 AGeV



- heavier system: sensitivity to medium effect increased

Predictions for HADES

$\pi p, 0.56 \text{ GeV}$



- $N^*(1520)$ dominant contribution to ρ yield
- probe $\rho - N^*(1520)$ coupling and treatment of $N^*(1520)$ dilepton Dalitz decays
- spectrum with VMD for $N^*(1520)$ Dalitz

$$N^*(1520) \rightarrow \rho N \rightarrow e^+ e^- N$$

Summary

Hadronic transport approaches offer excellent framework to study low-energy reactions.

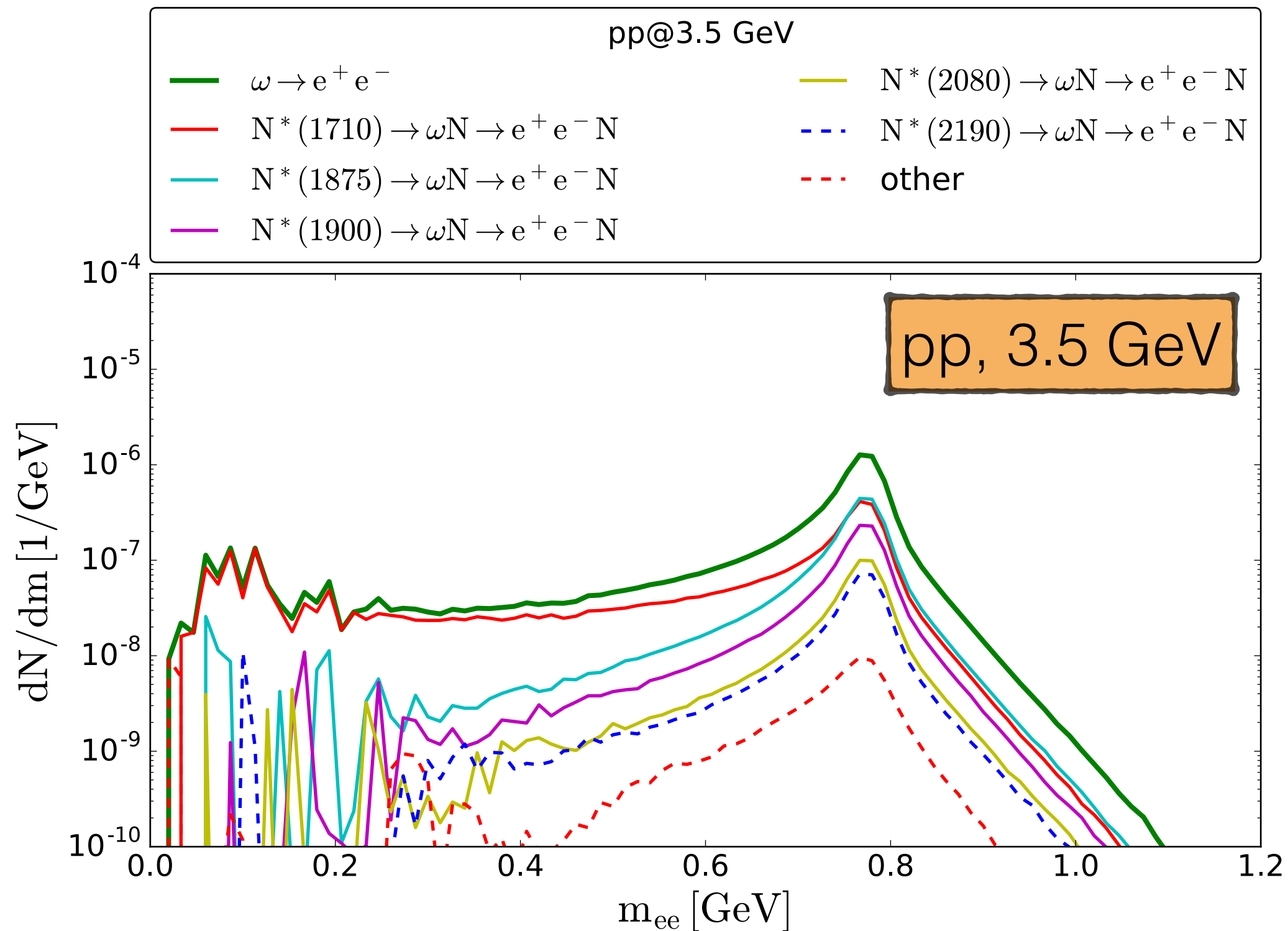
1. Total hadronic cross section agree with data for low energies
2. „Strict-VMD“ used to study the e.m. form factor of dilepton Dalitz decay of ω and Φ
3. Dilepton production for elementary reactions indispensable baseline to probe medium effects

—> SMASH will be open-sourced later this year

—> looking forward to new experimental results from HADES

Backup

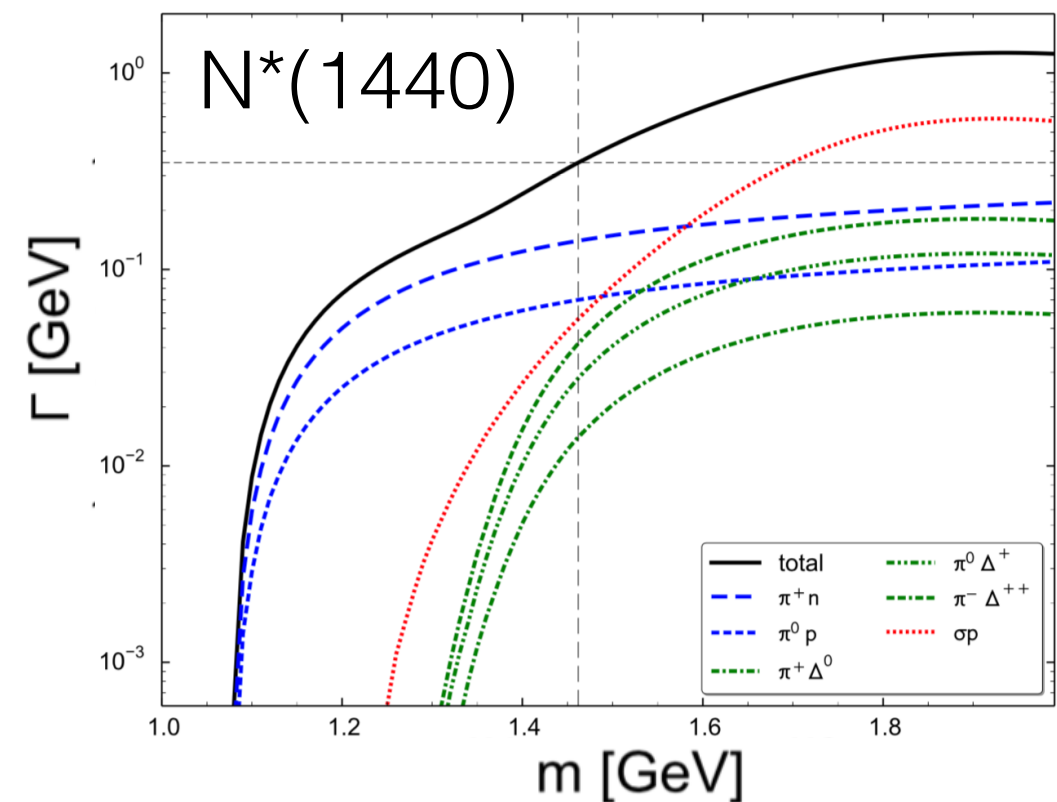
Omega Origin in Dilepton Spectra



Resonances

- Spectral Function
 - all unstable particles ("resonances") have relativistic Breit-Wigner spectral functions
- Decay Widths
 - particles stable, if width $< 10 \text{ keV}$ (π , η , K , ...)
 - treatment of Manley et al

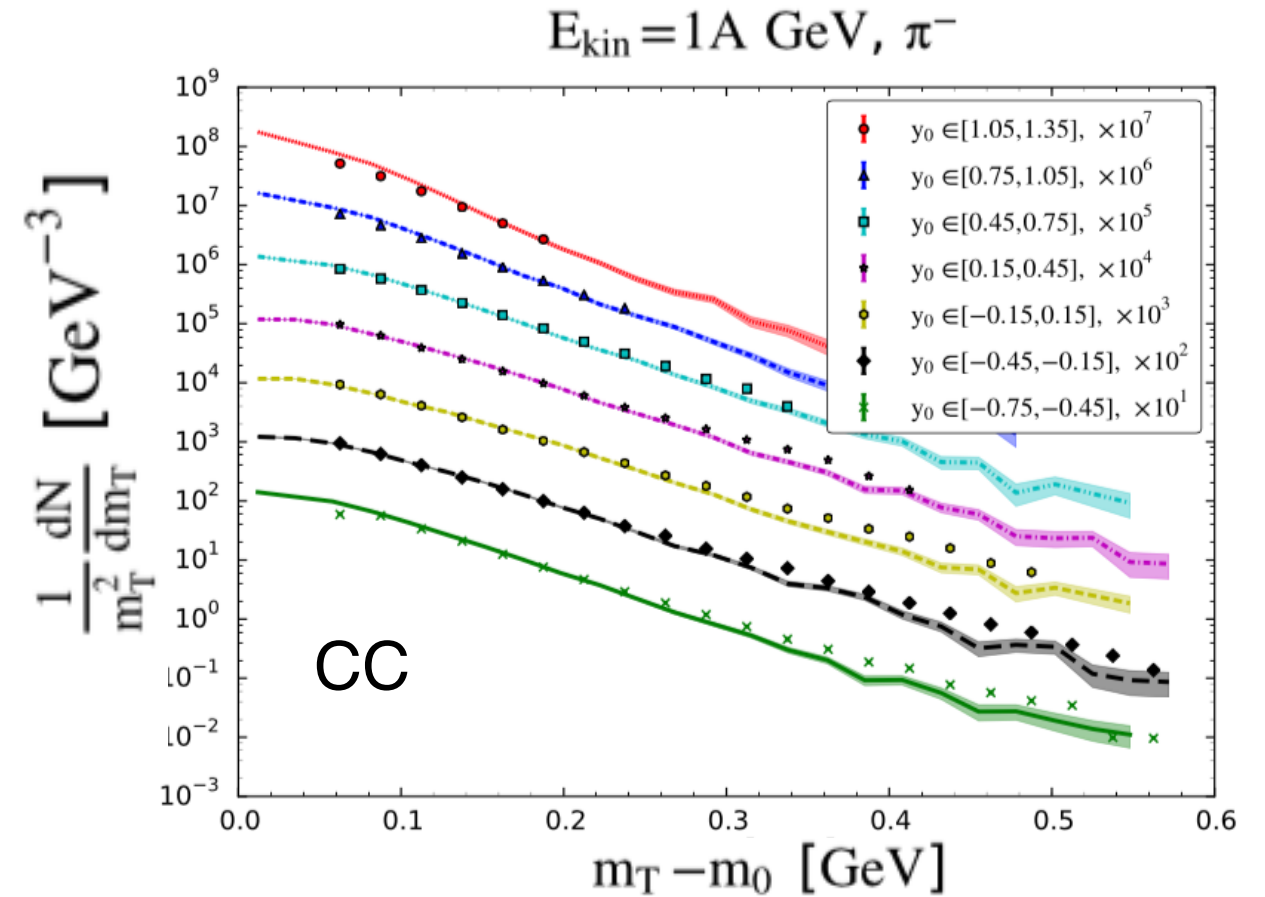
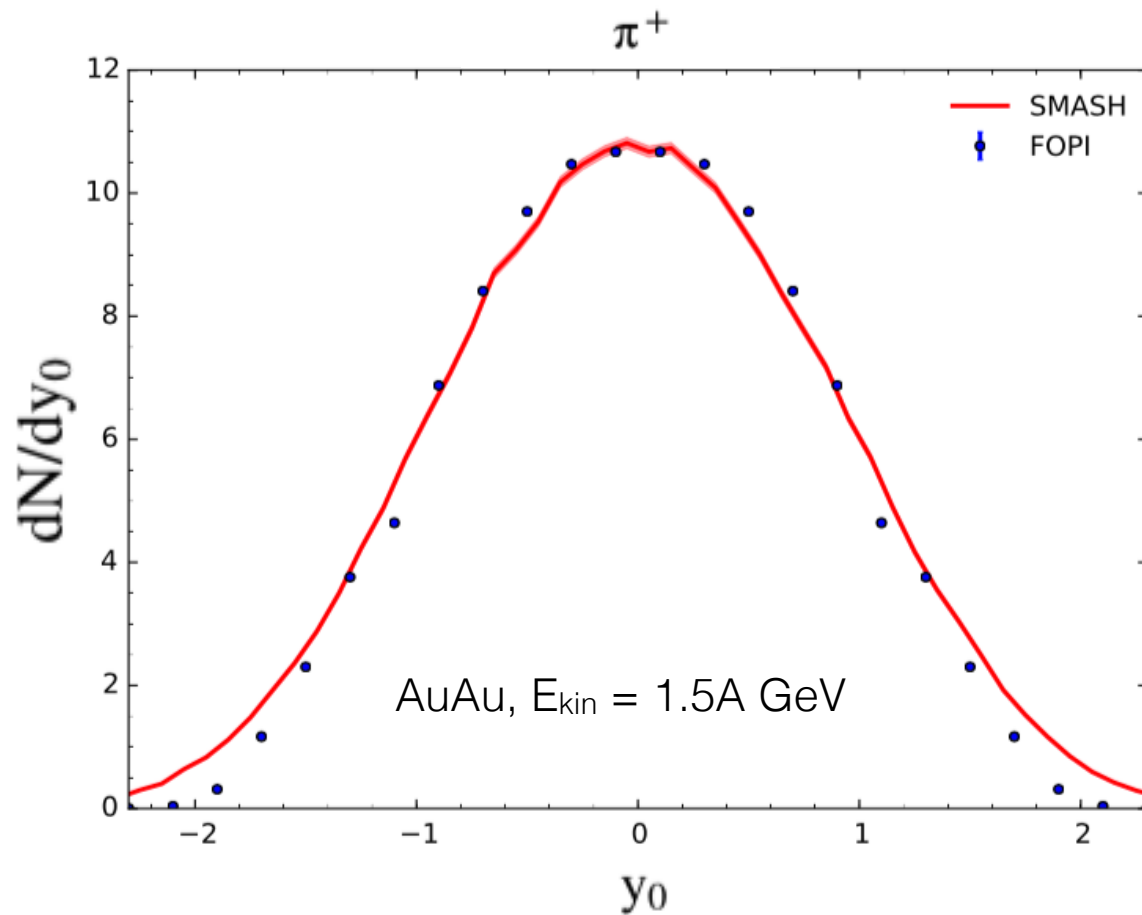
$$\mathcal{A}(m) = \frac{2\mathcal{N}}{\pi} \frac{m^2 \Gamma(m)}{(m^2 - M_0^2)^2 + m^2 \Gamma(m)^2}$$



$$\Gamma_{R \rightarrow ab} = \Gamma_{R \rightarrow ab}^0 \frac{\rho_{ab}(m)}{\rho_{ab}(M_0)}$$

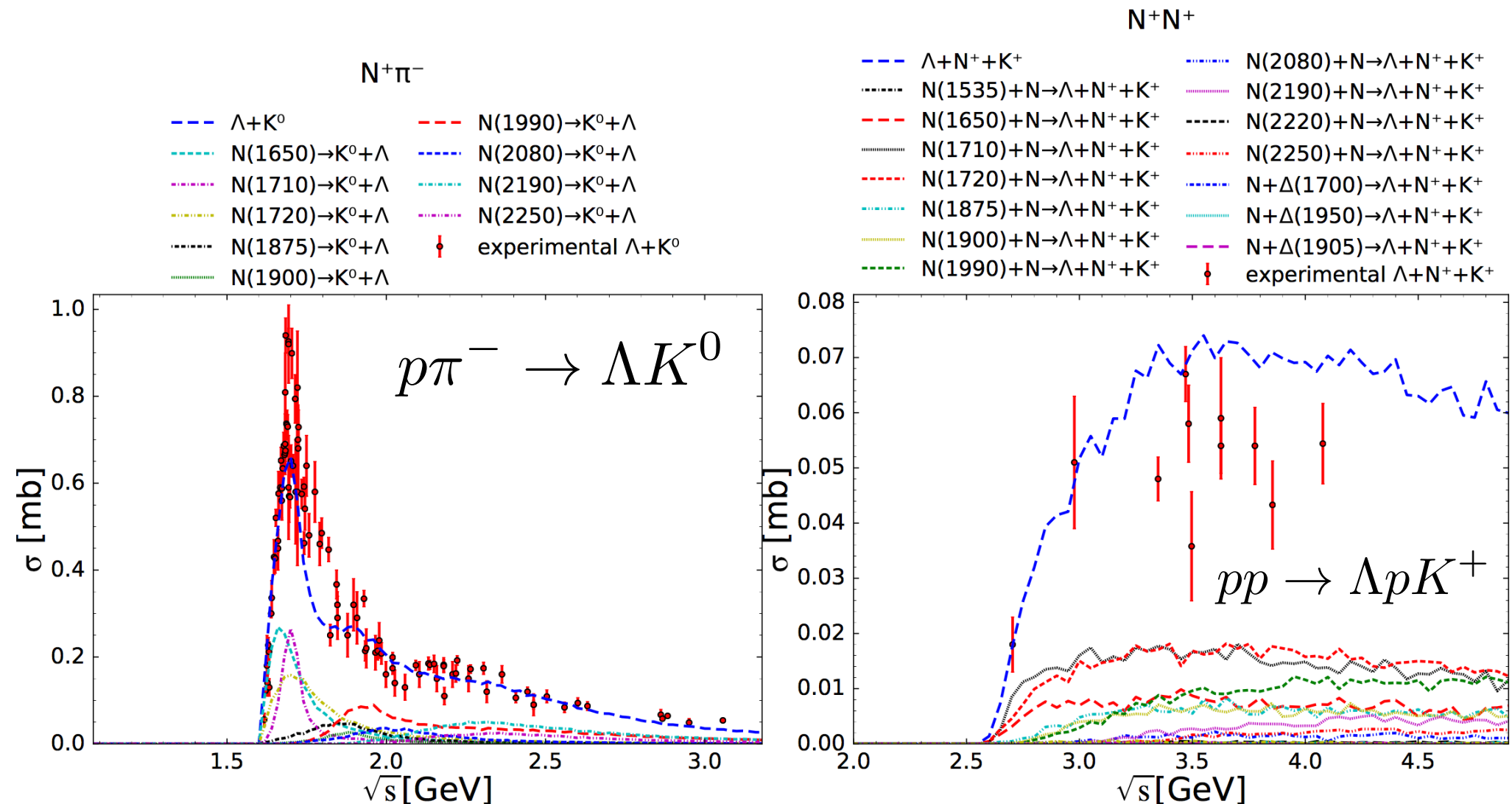
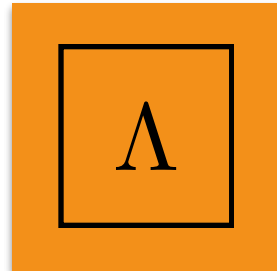
D. M. Manley and E. M. Saleski,
Phys. Rev. D 45, 4002 (1992)

Results for HIC



- shape of pion rapidity spectra reproduced
- transverse mass spectra compared with HADES data are in good agreement

Exclusive Cross Section



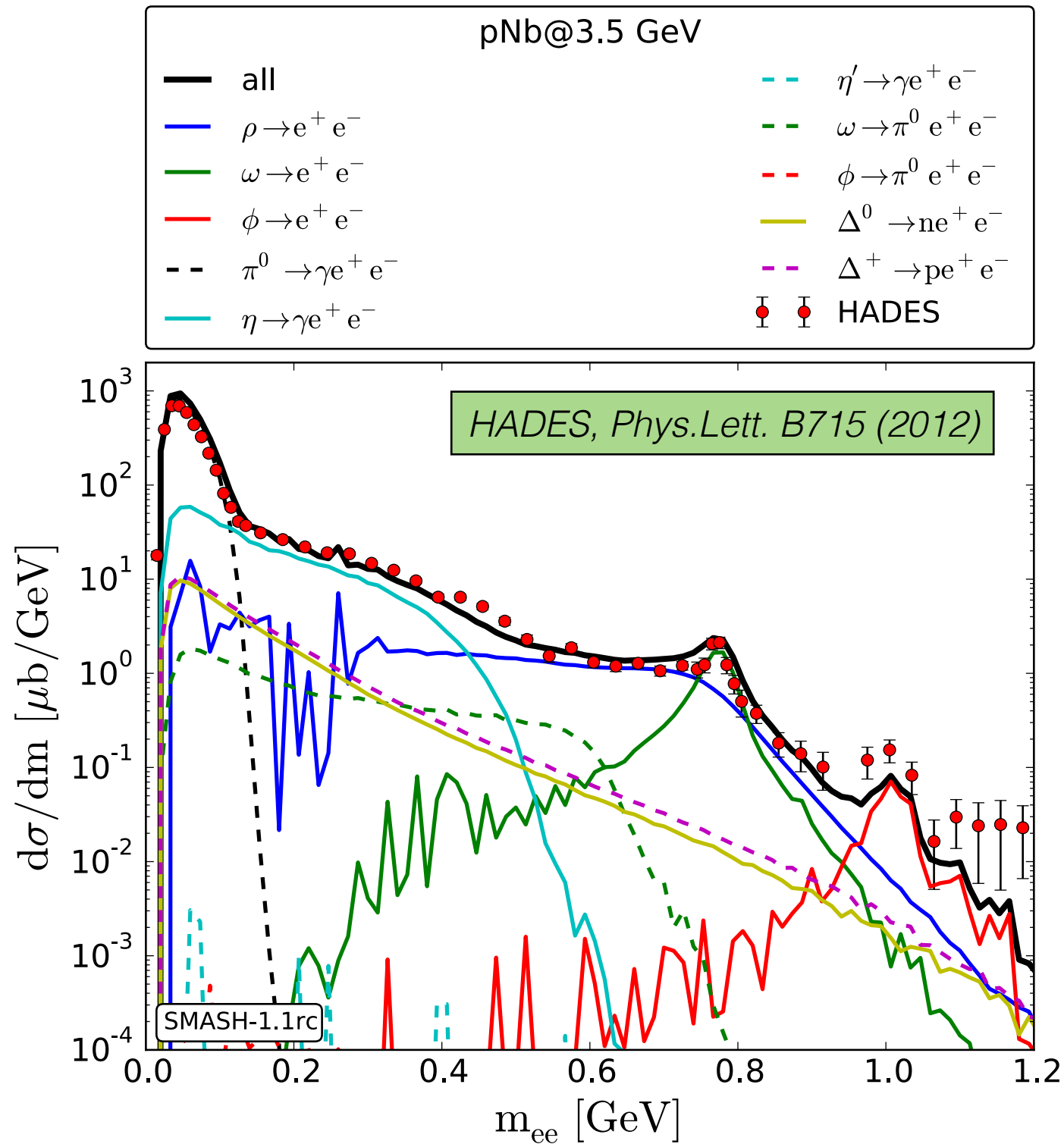
- B.R. constraint by exclusive production cross section of Λ hyperons

- building on data from PDG and PWA *Münzer, Fabbietti, arxiv:1703.01978 (2017)*

$$N^* \rightarrow \Lambda K$$

p+A

pNb, 3.5 GeV



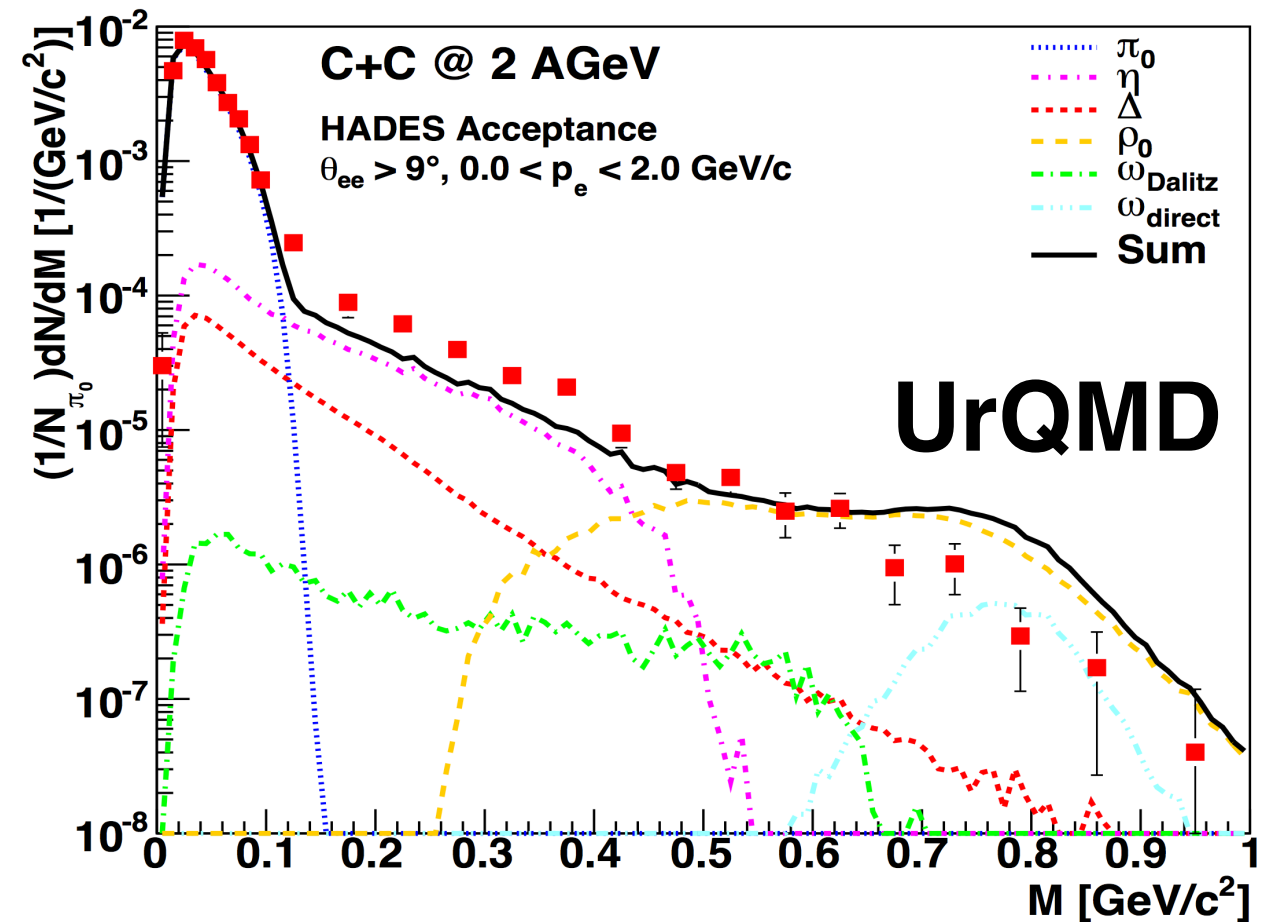
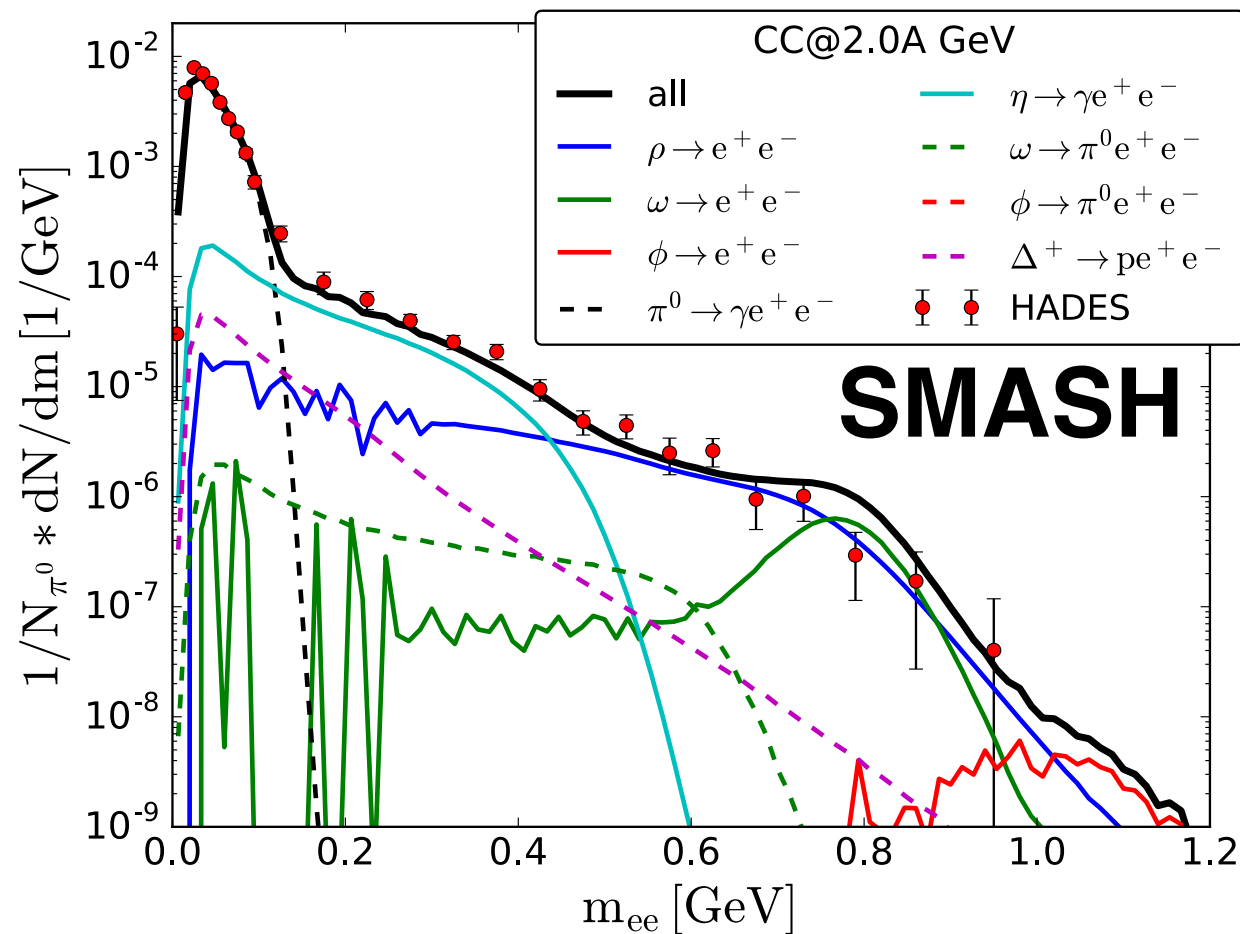
- pNb: cold nuclear matter scenario
- example for small system
- clear Φ peak, underestimated

A+A

HADES, Phys.Rev.Lett. 98 (2007)

CC, 2.0 AGeV

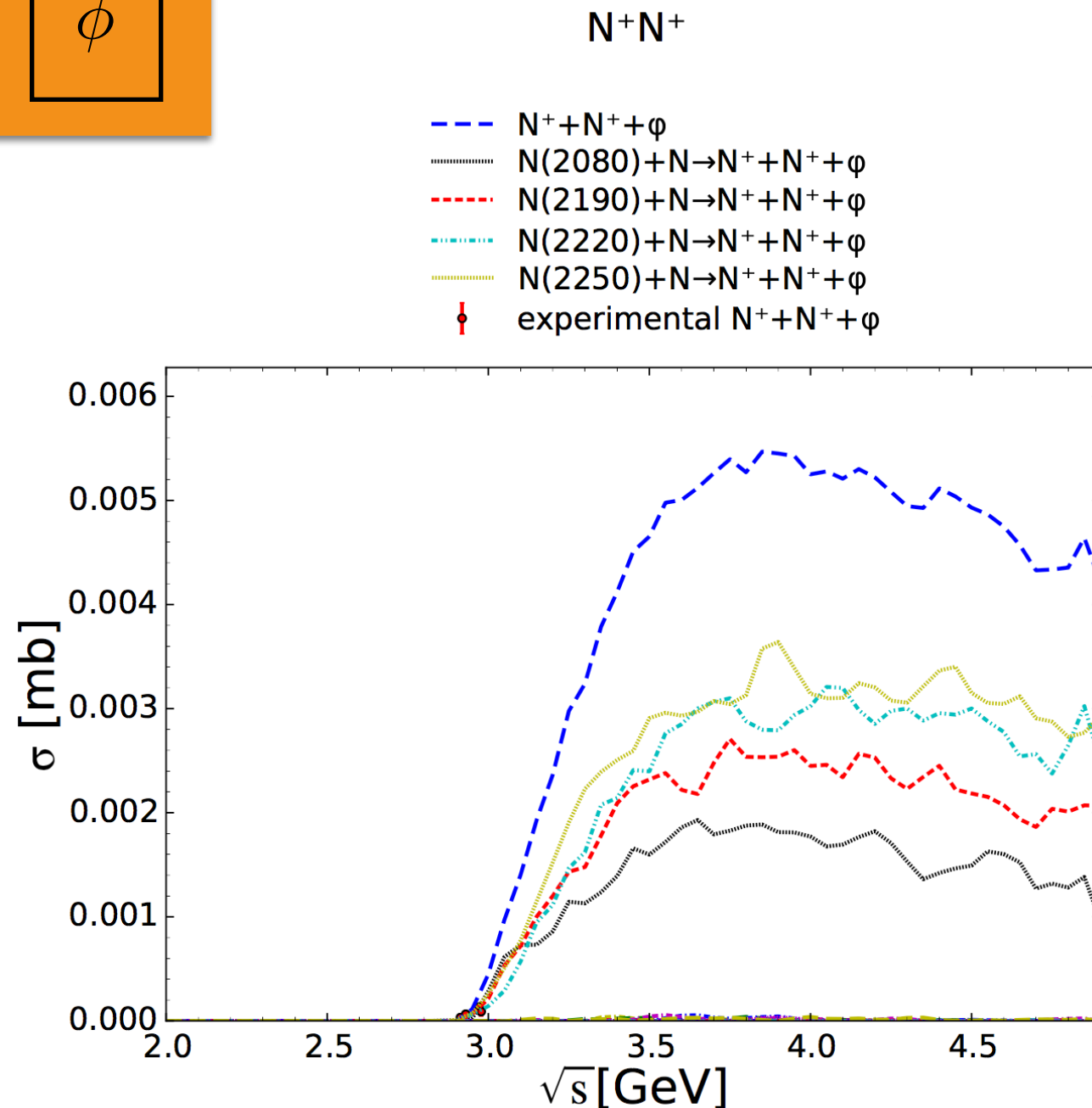
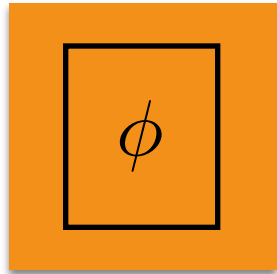
S. Endres et al., J.Phys.Conf.Ser. 426 (2013)



- SMASH and UrQMD compare similar to data
- different vector meson thresholds

—> good description for "small" pNb + CC system

Φ Production



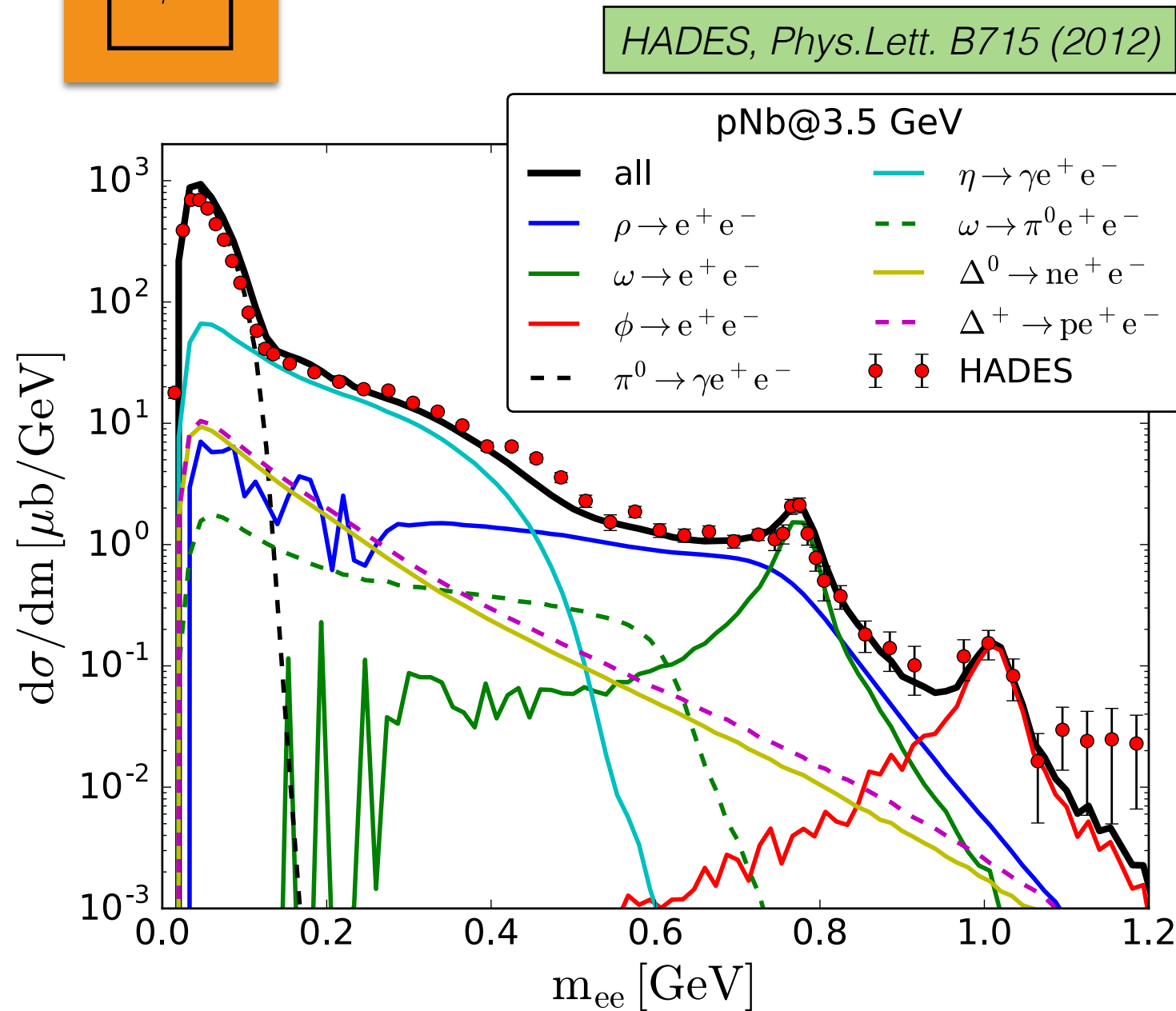
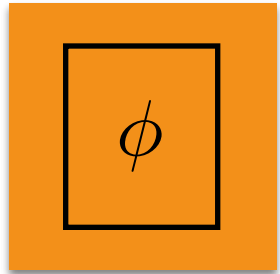
- simplified ansatz for Φ production: fixed B.R. for heavy $N^*(> 2000)$ resonances

J. Steinheimer et al., J. Phys. G43.1 (2016)

- experimentally not well known: not constrained by cross section
- constrain resonance properties with dileptons

$$N^* \rightarrow N\phi$$

Φ Production



- simplified ansatz for Φ production: fixed B.R. for heavy $N^*(> 2000)$ resonances

J. Steinheimer et al., J. Phys. G43.1 (2016)

- experimentally not well known: not constrained by cross section
- constrain resonance properties with dileptons

$$N^* \rightarrow N\phi$$

Rapidity spectra pp@3.5 GeV

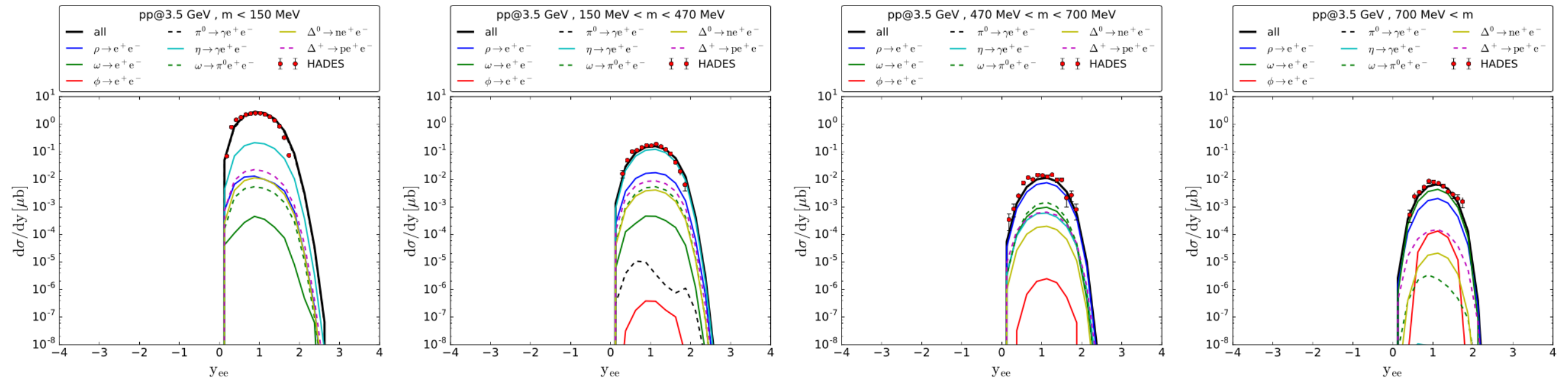
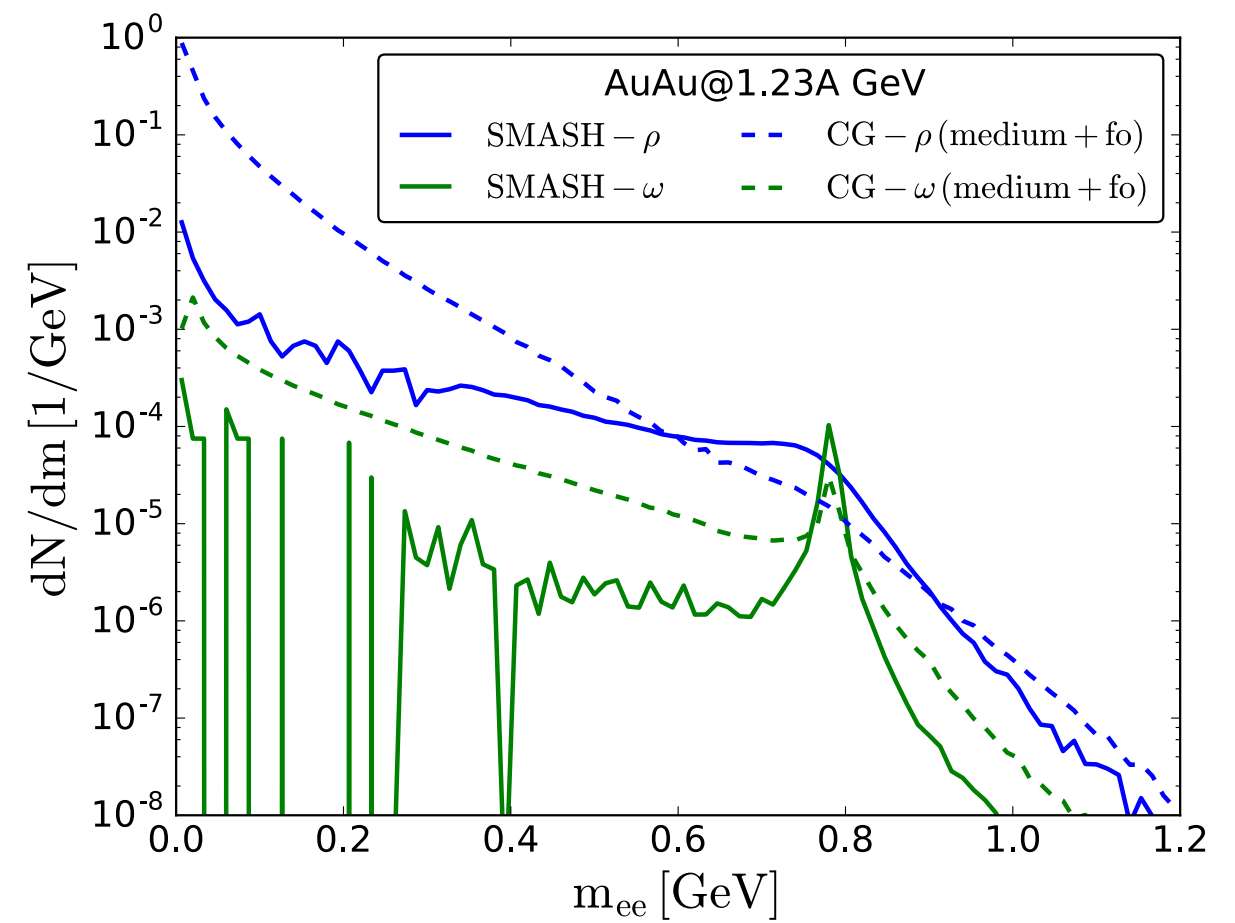
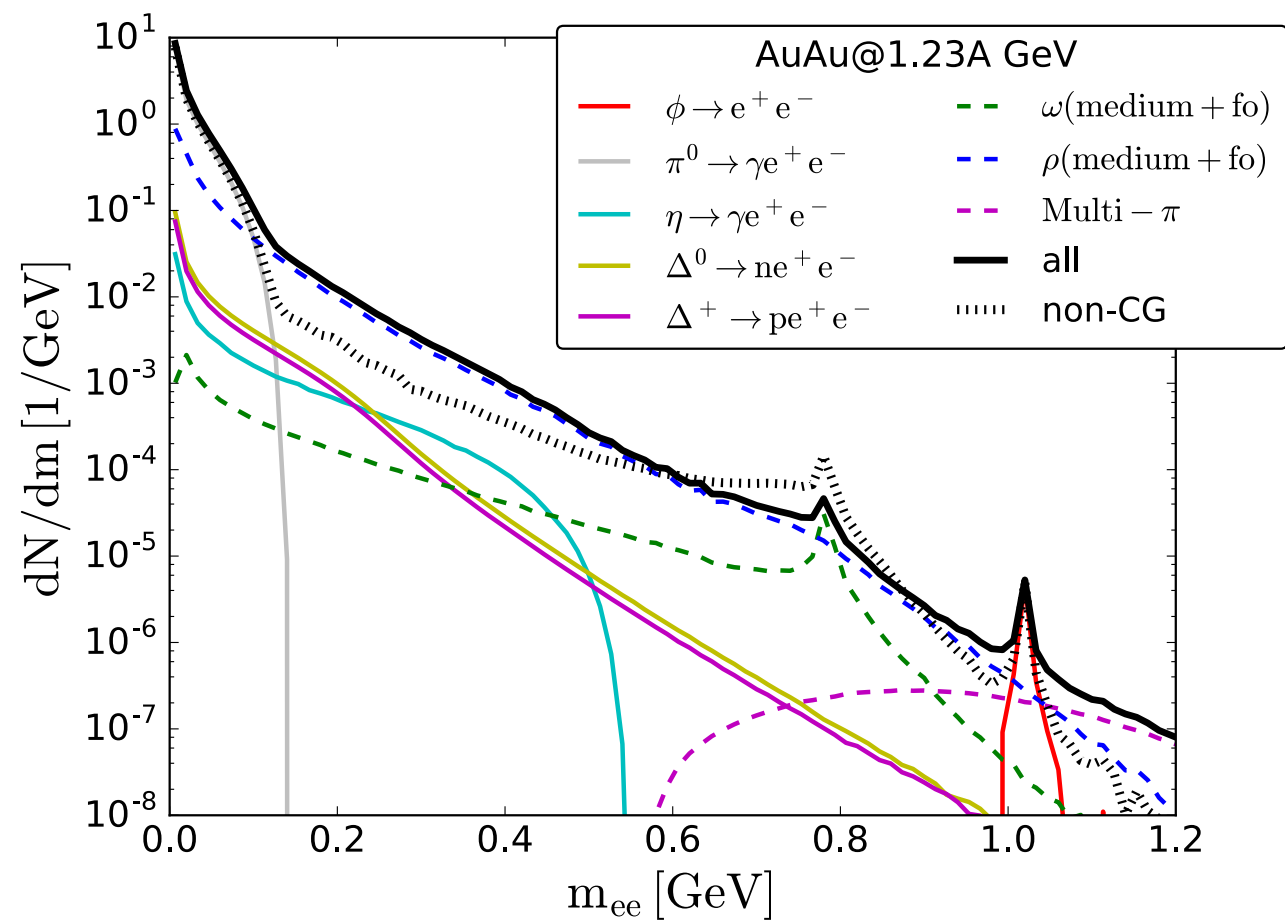
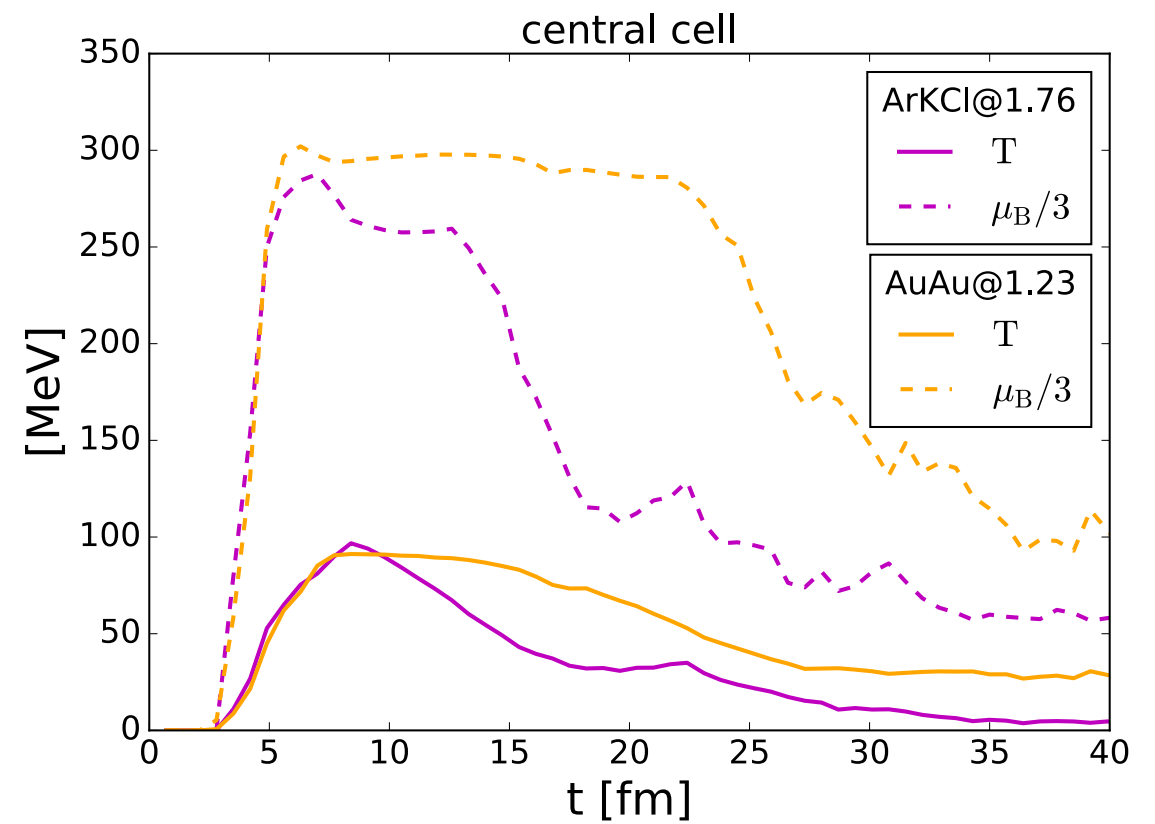
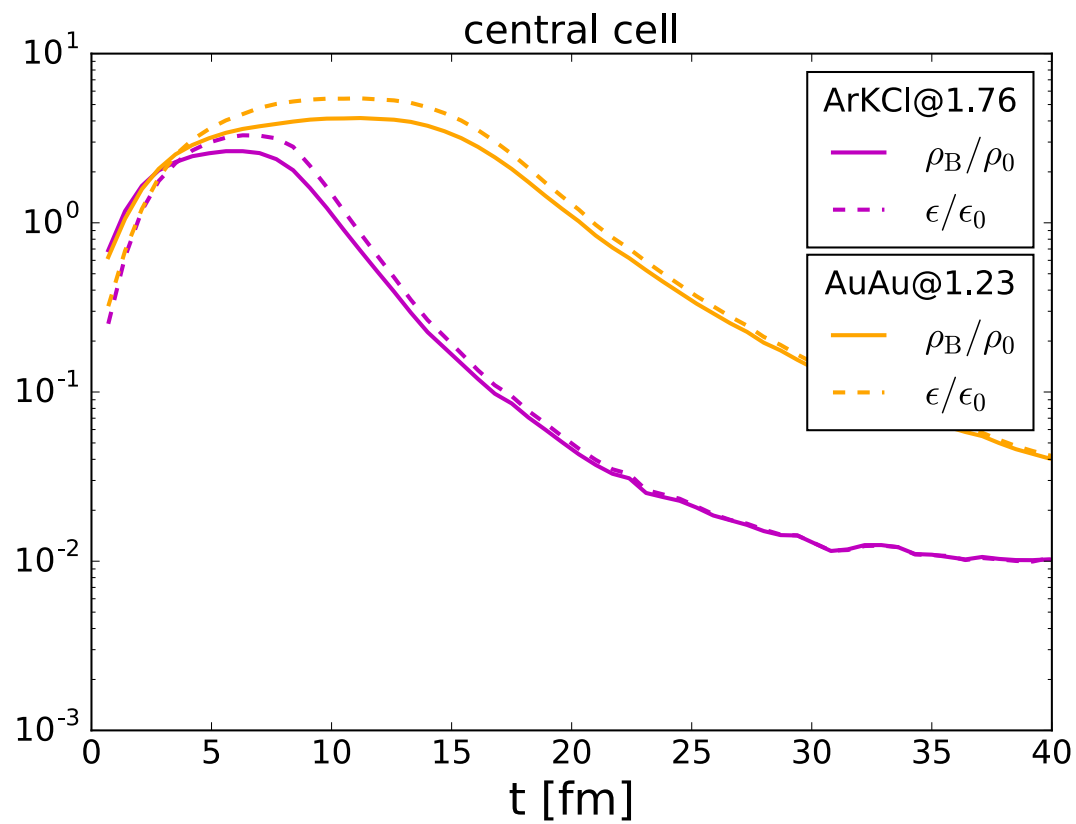


FIG. 24. Rapidity spectra of di-electrons produced by pp collisions at $E_{\text{kin}} = 3.5$ GeV in different invariant mass windows. Experimental data from [15].

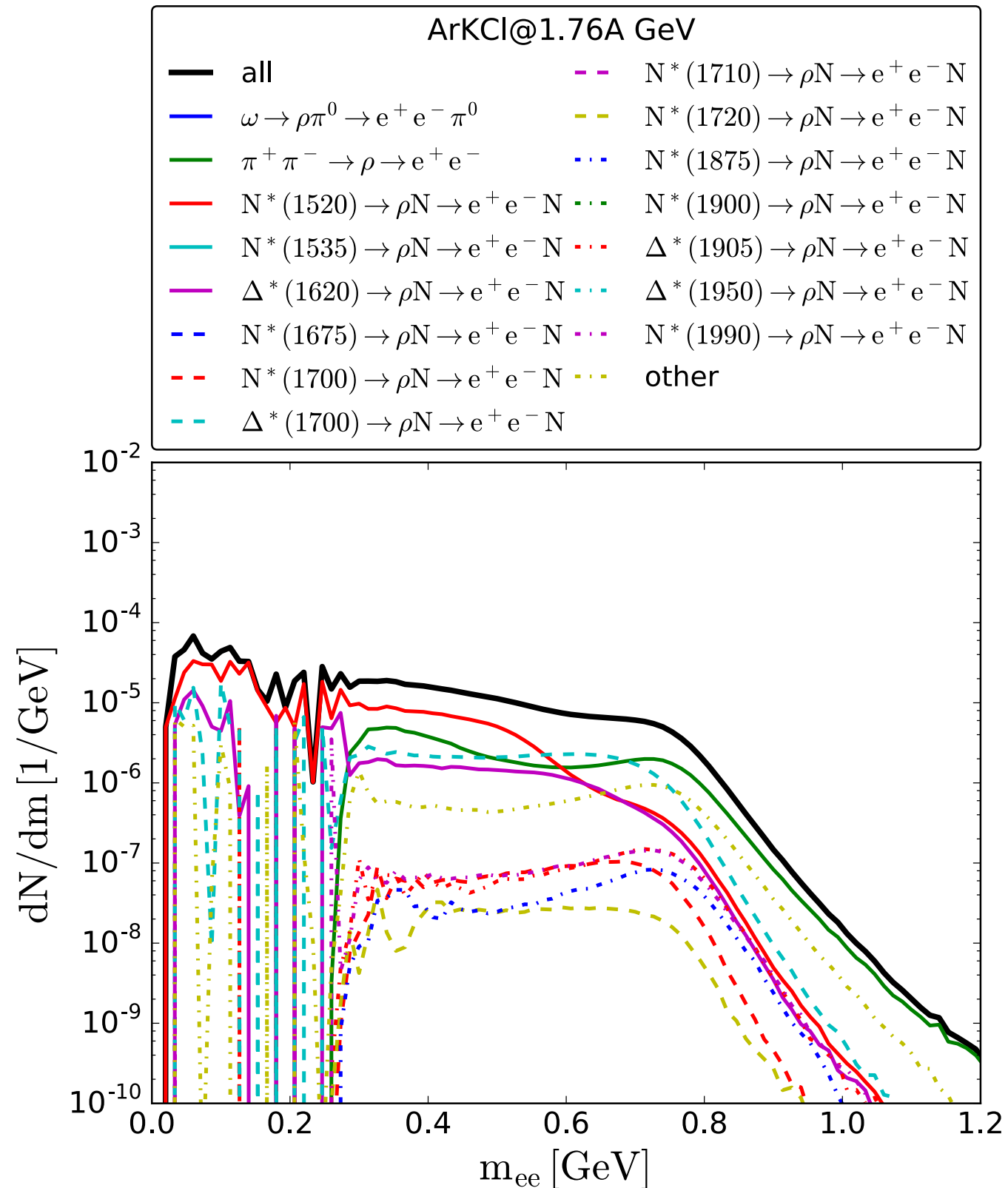
CG: AuAu



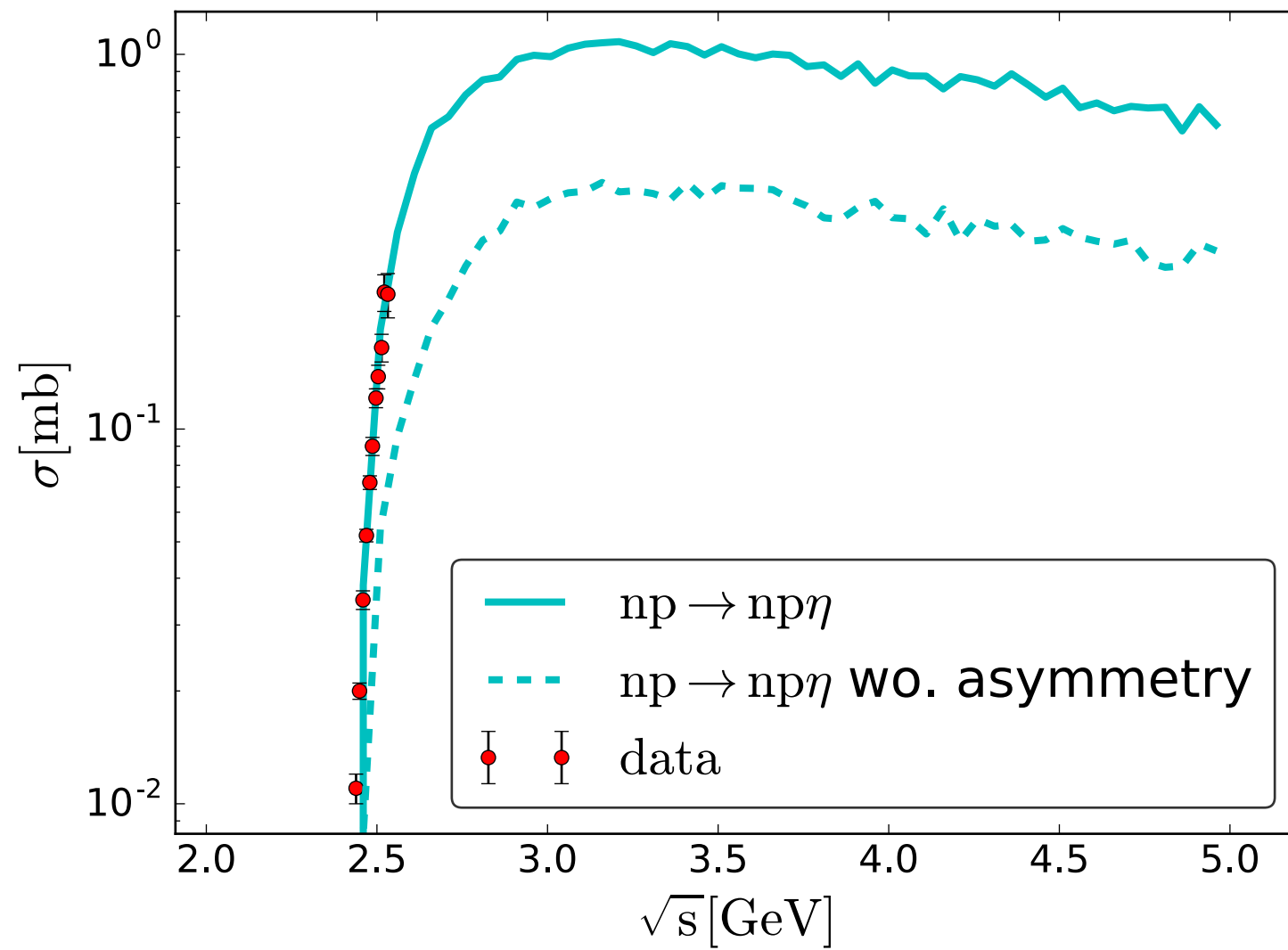
CG evolution



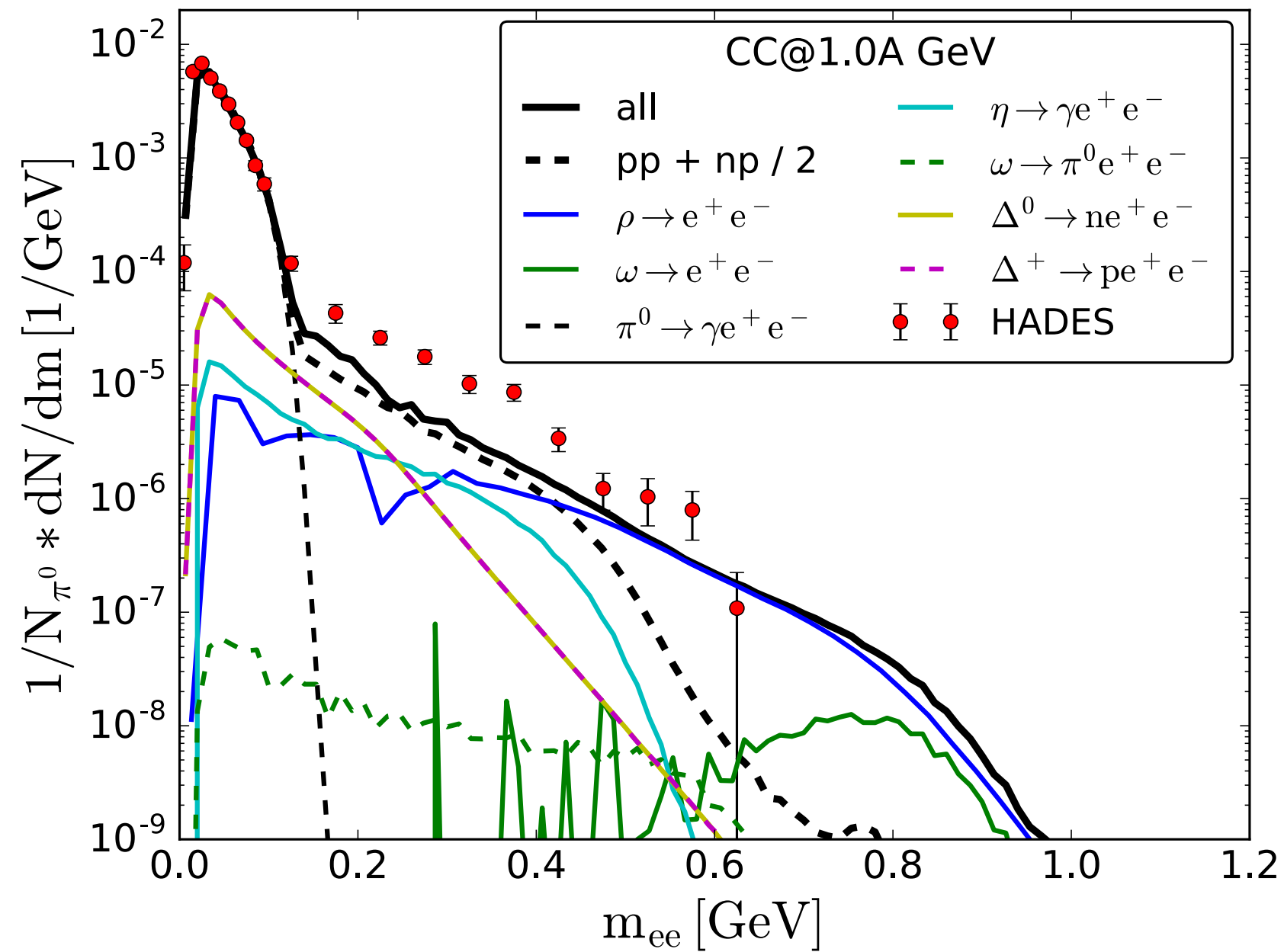
Rho origin in ArKCl



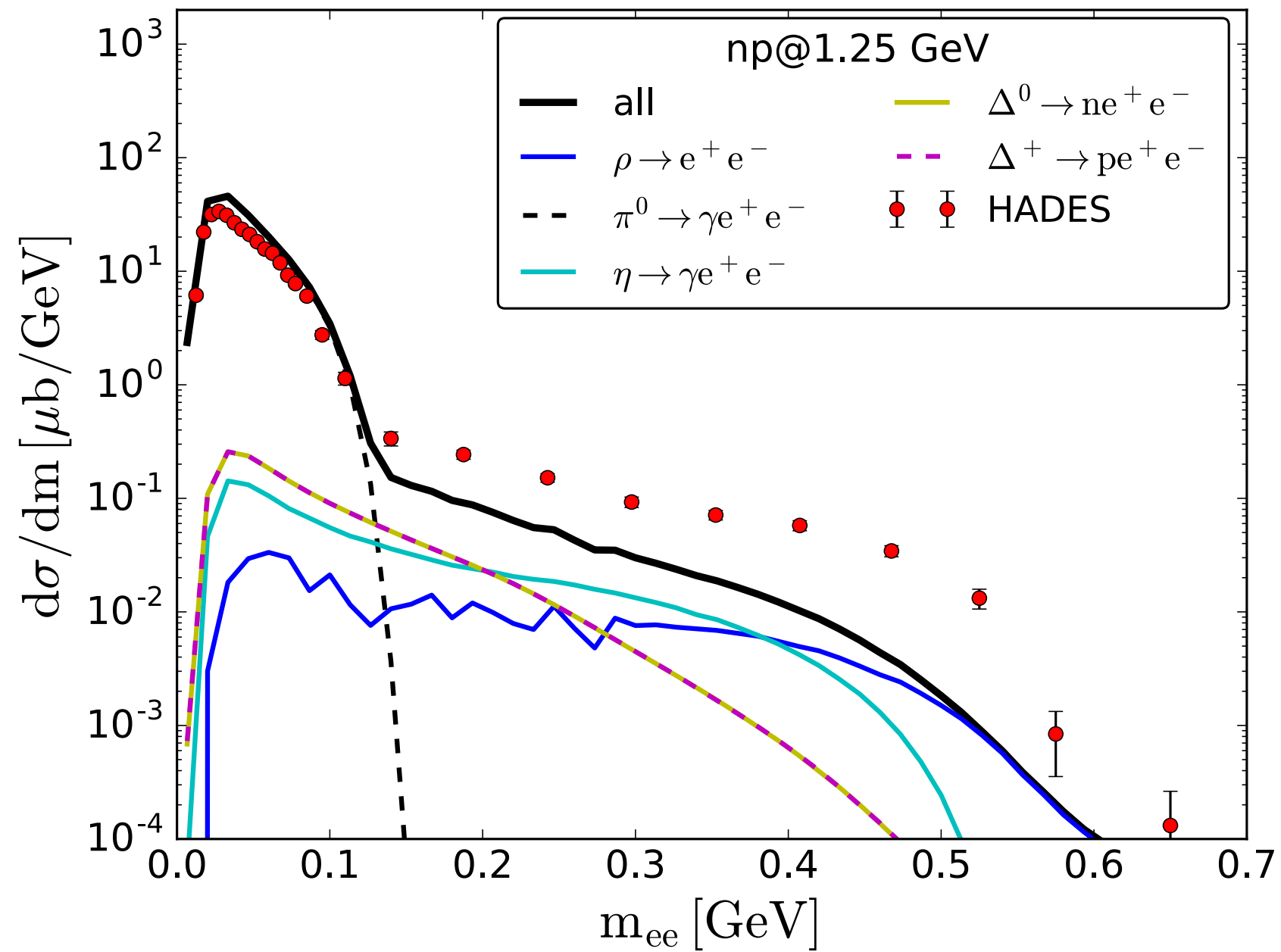
Eta Cross Section



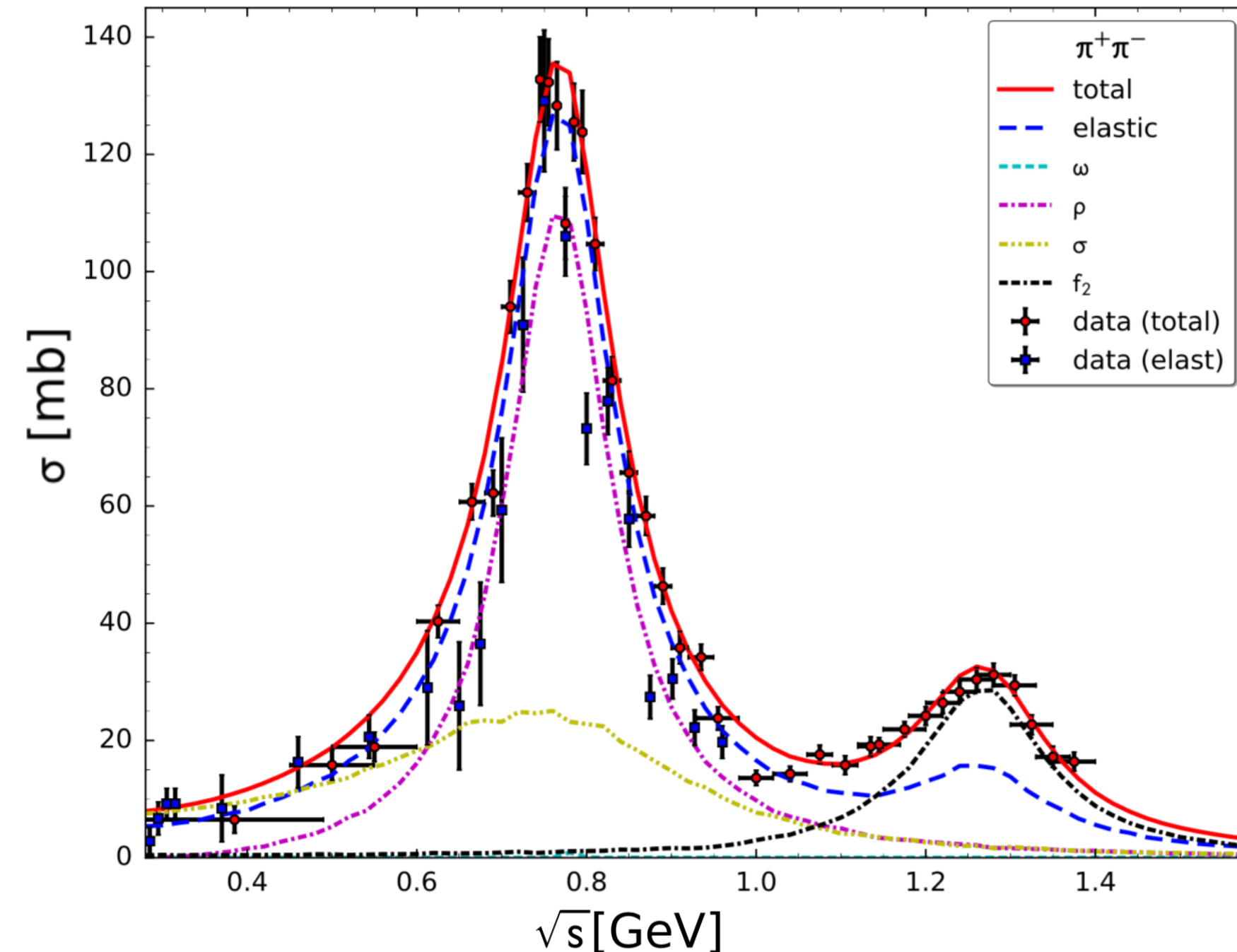
CC @ 1.0 A GeV



$d(n) + p$



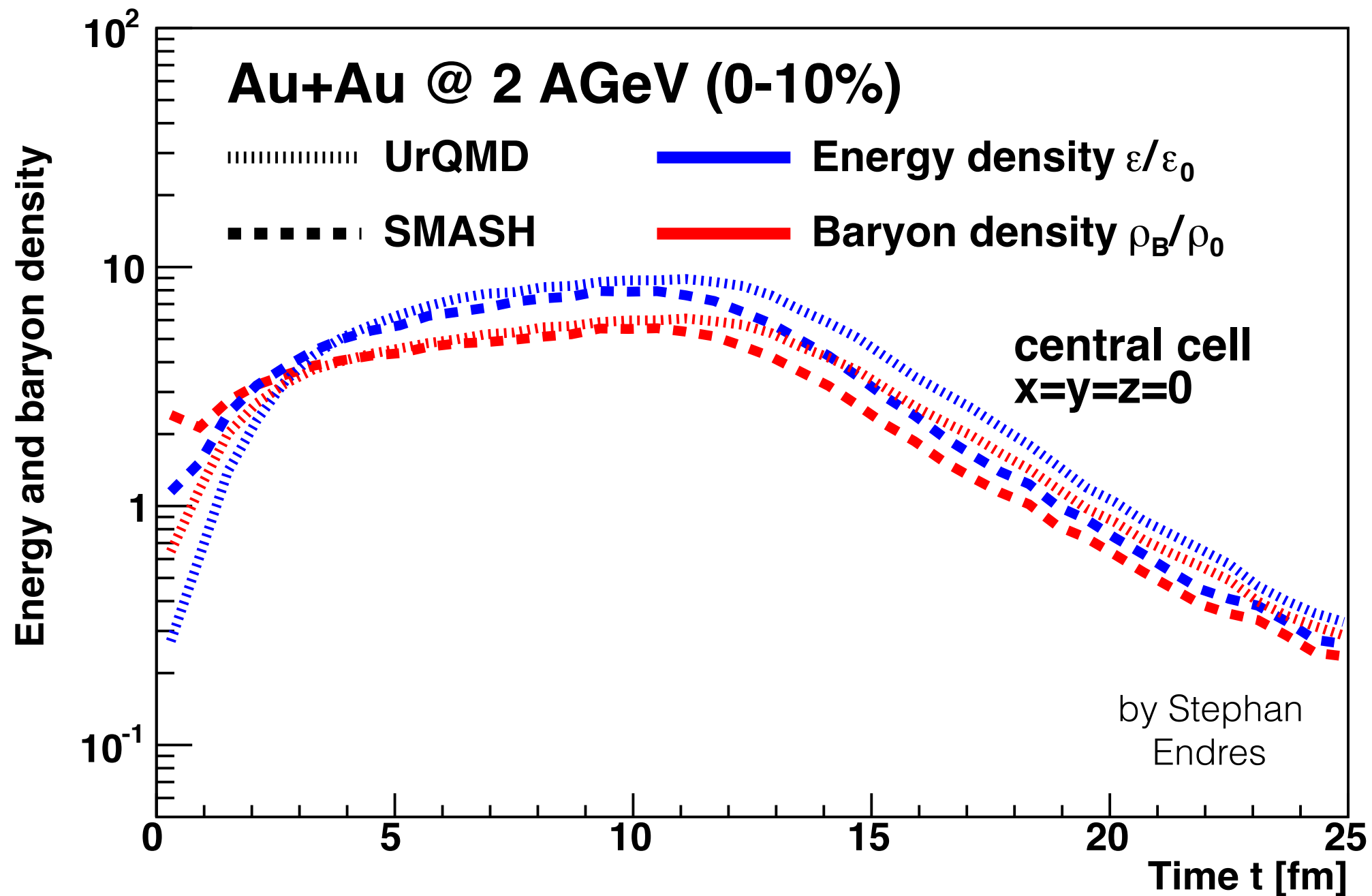
Elementary Cross Sections



- cross section for purely mesonic Pion scattering
- clear resonance pattern
- dominant contributions are the ρ and f_2 states

Comparison to UrQMD

time evolution of density at center of collision is very similar



SMASH status

- ✓ cross section described via resonances (few GeV)
- ✓ production of e.m. observables („integrated“)
- ✓ „exotic“ channels (*additive quark model*) $\Delta + \Lambda$
- ✓ baryon-antibaryon-annihilation + string fragmentation
 $p + \bar{p}$

new results:

- ✓ comparison with analytic solution of the Boltzmann equation
J. Tindall, J. Torres-Rincon, J.B. Rose, H. Petersen, arXiv:1612.06436
- ✓ „*hydro bubbles*“ - forced thermalisation of dense regions
D. Oliinychenko, Hannah Petersen, arXiv:1609.01087

Treatment of Manley

D. M. Manley and E. M. Saleski, Phys. Rev. D 45, 4002 (1992)

- scaling of on-shell decay width:

$$\Gamma_{R \rightarrow ab} = \Gamma_{R \rightarrow ab}^0 \frac{\rho_{ab}(m)}{\rho_{ab}(M_0)}$$

- definition of rho-function:

$$\rho_{ab}(m) = \int dm_a dm_b \mathcal{A}_a(m_a) \mathcal{A}_b(m_b) \times \frac{|\vec{p}_f|}{m} B_L^2(|\vec{p}_f|R) \mathcal{F}_{ab}^2(m)$$

Blatt Weisskopf functions

$$B_0^2 = 1$$

$$B_1^2(x) = x^2 / (1 + x^2)$$

...

- hadronic Form Factor:

$$\mathcal{F}_{ab}(m) = \frac{\lambda^4 + 1/4(s_0 - M_0^2)^2}{\lambda^4 + (m^2 - 1/2(s_0 + M_0^2))^2}$$

decay	λ [GeV]
$\pi\rho$	0.8
unstable mesons (e.g. $\rho N, \sigma N$)	1.6
unstable baryons (e.g. $\pi\Delta$)	2.0
two unstable daughters (e.g. $\rho\rho$)	0.6

M. Post, S. Leupold, U. Mosel, Nucl. Phys. A 741, 81 (2004)