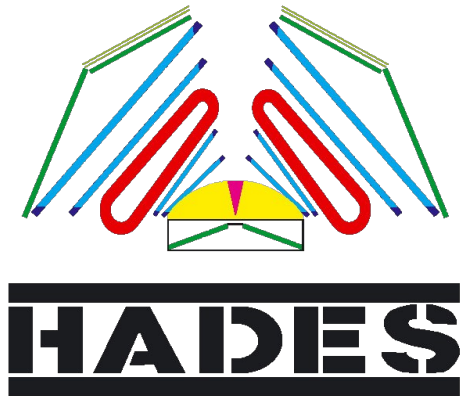


Workshop on Two-Pion and e^+e^- Production in Hadronic Reactions



**Event Generator
for e^+e^- Production
in $\pi^- p$ Reactions**

Outline:

1. Motivations.
2. Cocktail simulations.
3. New event generator:
assumptions and results.
4. SDME formalism and
new microscopic model
by E. Speranza and Collaborators.
5. Comparison to the data.

I. Denisenko, A. Sarantsev (Bonn-Gatchina)

Izabela Ciepał (IFJ PAS)

Piotr Salabura (JU)

Motivations

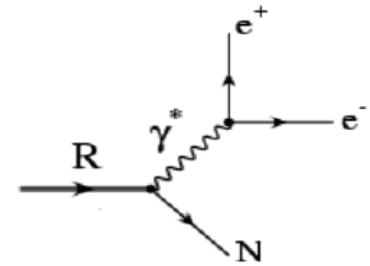
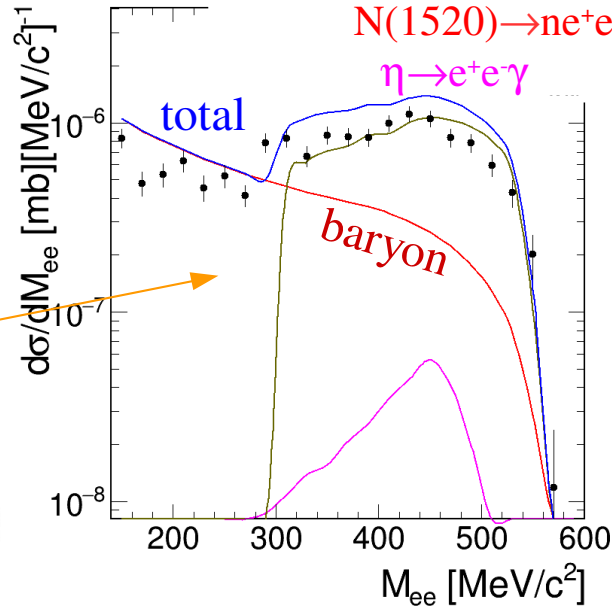
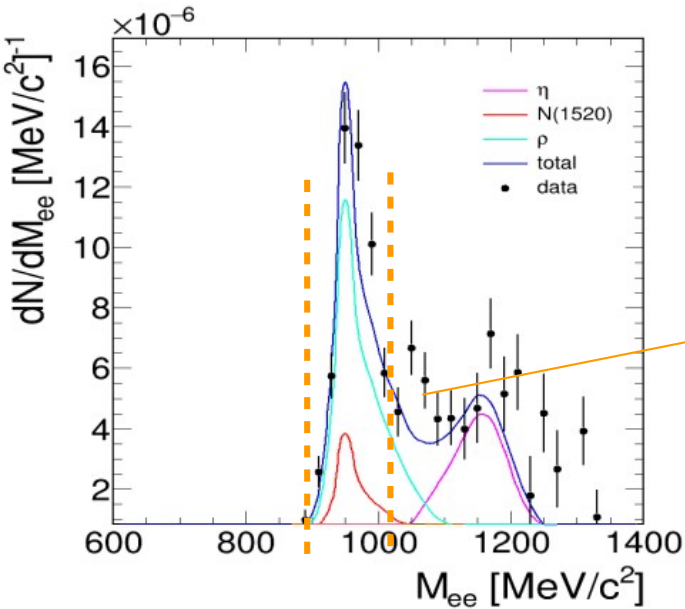
exclusive $\pi^- p \rightarrow e^+ e^- n$ @ $\sqrt{s} \sim 1.5$ GeV

$$0.9 < M_{ee}^{\text{miss}} < 1.03 \text{ GeV}/c^2$$

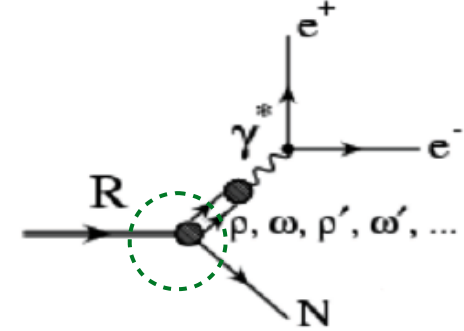
$$\pi^0 \rightarrow e^+ e^- \gamma$$

$$N(1520) \rightarrow n e^+ e^-$$

$$\eta \rightarrow e^+ e^- \gamma$$



QED:
point-like $R\text{-}\gamma^*$ vertex
M. Zetenyi/M. I. Krivoruchenko



VMD:
em. transition FF (M_{ee})

B. Ramstein contribution from Hades CM GSI
F. Scozzi Orsay

Models - “simple” cocktail simulations:

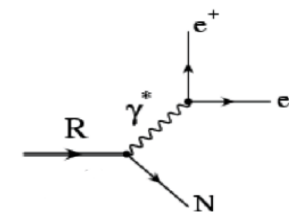
baryon (?) – “QED” calculated as only D13(1520) Dalitz (with σ of $\pi^- p \rightarrow n \gamma$),

Motivations

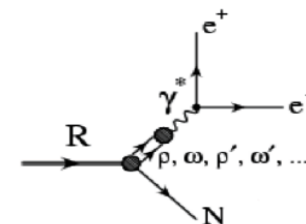
exclusive $\pi^- p \rightarrow e^+ e^- n$ @ $\sqrt{s} \sim 1.5$ GeV

Models - “simple” cocktail simulations:

- very strong contribution from ρ (using strict VDM), ρ -meson contribution derived from PWA of 2 pion channels ($n\pi^+\pi^-$, $p\pi^-\pi^0$)
(W. Przygoda contribution from CM Frankfurt)



QED:
point-like R- γ^* vertex
M. Zetenyi/M. I. Krivoruchenko



VMD:
em. transition FF (M_{ee})

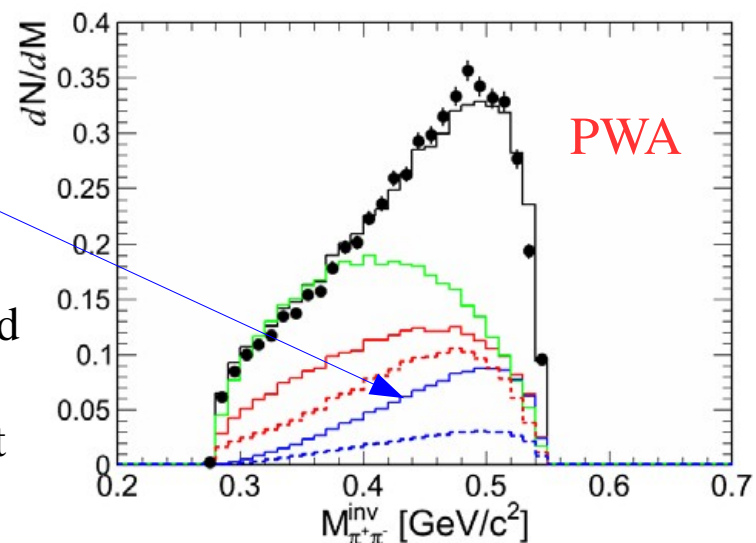
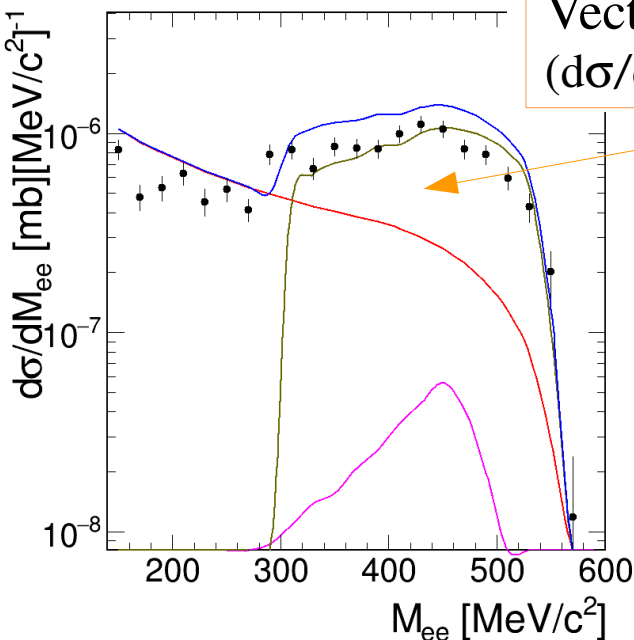
Vector Dominance Model

$$(d\sigma/dM_{ee}) = (d\sigma/dM_{\pi\pi}) * BR(M_{ee}=M_\rho) * (M_\rho/M_{ee})^3$$

off-shell
 $\rho \rightarrow e^+ e^-$

off-shell
 $\rho \rightarrow \pi^+ \pi^-$

ρ cross section obtained from $\pi p \rightarrow \pi^+ \pi^- n$ in the same experiment



Coctail @ $p=0.69$ GeV/c, $\sqrt{s}\sim 1.5$ GeV

Landolt-Börnstein, Crystal Ball

$N(1520) \rightarrow n e^+e^-$	20.5 mb
$\Delta(1232) \rightarrow n e^+e^-$	8.4 mb
$\eta \rightarrow \gamma e^+e^-$	1 mb
$\rho \rightarrow e^+e^-$	2.3 mb

$\pi^+ p \rightarrow n \pi^0$	9.2 mb
(π^0 Dalitz)	
$\pi^+ p \rightarrow n \pi^0 \pi^0$	$2*1.88 = 3.8$ mb
(single π^0 Dalitz)	
$\pi^- p \rightarrow n \pi^- \pi^0$	3.72 mb

Branching Ratios:

π^0 : 0.012

$\Delta(1232)$: $4*10^{-5}$

$N(1232)$: $4*10^{-5}$

η : 0.006

N^* contribution **does not** include coherent contributions from various resonances



alternative way is to use PWA decomposition of πp and event generator from Bonn-Gatchina

New Event Generator

→ based on Partial Wave Solutions of the Bonn-Gatchina group

Code in two parts, to generate:

1. **signal:**

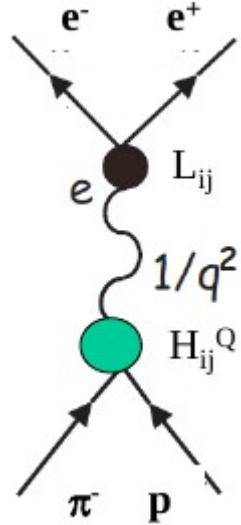
assumptions:

- $\pi^- p \rightarrow N^* \rightarrow \gamma^* N \rightarrow e^+ e^- n$ and $\pi^- p \rightarrow N^* \rightarrow \gamma N$ (VMD), real and virtual photon are produced by the same “hadronic” part of the amplitude (no FF),
- use known γn cross section and description of γn final state (PWA),
- only transvers virtual photon polarization (as for real photon),

2. **background:** $n \pi^0$, $n \pi^0 \pi^0$, $p \pi^0 \pi^-$

- use angular distributions provided by PWA from fits to world data

$\pi^- p \rightarrow e^+ e^- n$ – Formula for Lepton Production



$$d\sigma = \frac{(2\pi)^4}{4|k|\sqrt{s}} \left(H_{\mu\nu} \frac{e^2}{Q^4} L^{\mu\nu} \right) d\Phi_{ne+e-}^3,$$

$H_{\mu\nu}$ (**hadronic tensor**) - hadron production and decay to γ^*

(dependence on spin and parity of the transition FF):

input either from theory or from data (PWA), ..

$L_{\mu\nu}$ (**lepton tensor**) - transition $\gamma^* \rightarrow e+e-$ (**known from QED**)

$d\Phi$ - phase space factor

E. Speranza et al., Phys.Lett.B764 (2017) 282-288

$$d\sigma \sim \sum_{pol} |A|^2 = \sum_{\lambda, \lambda'} \rho_{\lambda, \lambda'}^{had} \rho_{\lambda, \lambda'}^{lep}$$

Spin Density Matrix Elements (SDME):

$$\rho_{\lambda, \lambda'}^{had} = \epsilon^\mu(k, \lambda) H_{\mu\nu} \epsilon^\nu(k, \lambda')^* \quad \text{hadron decay to } \gamma^*$$

$$\rho_{\lambda, \lambda'}^{lep} = \epsilon^\mu(k, \lambda) L^{\mu\nu} \epsilon^\nu(k, \lambda')^* \quad \gamma^* \text{ decay to } e+e- \text{ (QED)}$$

**virtual photon polarization
(in the helicity basis):**

transverse $\epsilon^\mu(k, -1) = \frac{1}{\sqrt{2}}(0, 1, -i, 0)$

longitudinal $\epsilon^\mu(k, 0) = (0, 0, 0, 1)$

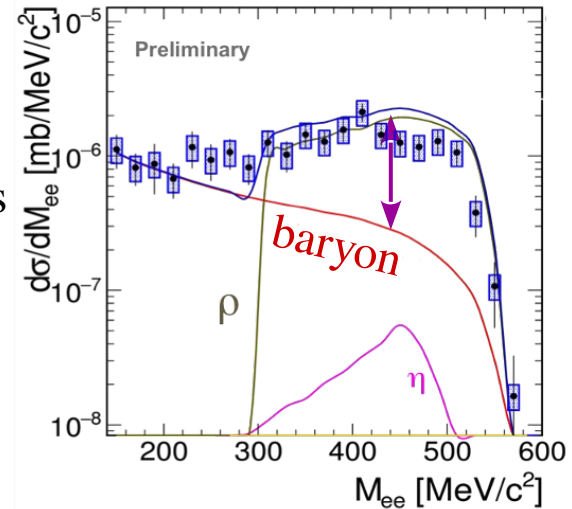
transverse $\epsilon^\mu(k, +1) = \frac{1}{\sqrt{2}}(0, 1, i, 0)$

$\pi^- p \rightarrow e^+ e^- n$ – Angular Distributions

known from QED

$$\frac{d\sigma}{dM d\cos\theta_{y^*} d\cos\theta_e} \sim \sum_{\lambda, \lambda'} \rho_{\lambda, \lambda'}^{had} \rho_{\lambda, \lambda'}^{lep}$$

additional information
on the electromagnetic
structure of the transition



- invariant mass shows deviation from point-like baryon transitions
- additional information on the electromagnetic transitions can be provided by the angular distribution
- SDME depend on m_{y^*} , $z = \cos\theta_{CM}^{y^*}$

the amplitude for the decay of a vector particle in two fermions:

$$\frac{|A|^2}{\sigma} = \frac{1}{N} \left(8m_e^2 + 8|\mathbf{k}|^2 \left[1 - \tilde{\rho}_{11}^{(H)} + \cos^2\theta \left(3\tilde{\rho}_{11}^{(H)} - 1 \right) + \sqrt{2} \sin(2\theta) \cos\phi \operatorname{Re}\tilde{\rho}_{10}^{(H)} + \sin^2\theta \cos(2\phi) \operatorname{Re}\tilde{\rho}_{1-1}^{(H)} \right] \right)$$

4 parameters: θ_{e^+, e^-} , φ_{e^+, e^-} , m_{y^*} , $z = \cos\theta_{CM}^{y^*}$

→ SDME can be extracted from fit to the angular distributions

F. Scozzi contribution from CM Frankfurt, Trento

B. Ramstein contribution from Hades CM GSI

Separation of Resonance Contributions

→ microscopic model including N(1440) and N(1520) excitations in s and u-channels and VDM electromagnetic form factors

E. Speranza et al., Phys.Lett.B764 (2017) 282-288

$$\lambda_\theta = \frac{3\rho_{11} - 1}{1 - \rho_{11}}$$

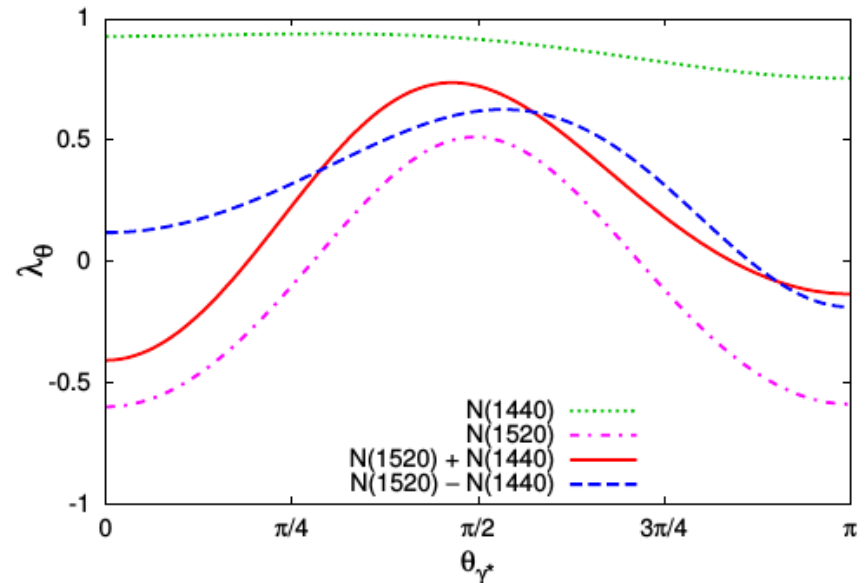
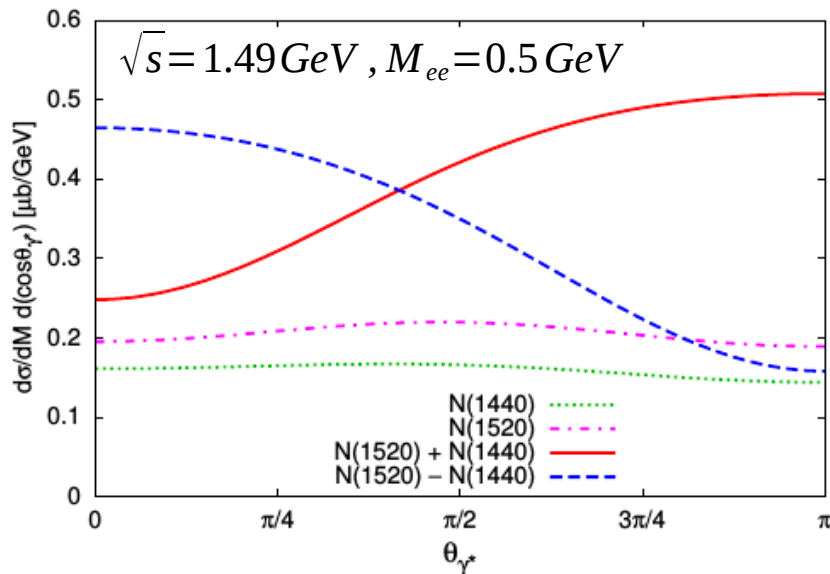
anisotropy coefficient

→ info on the virtual photon polarization

$$\frac{d\sigma}{dM d\cos\theta_{\gamma^*} d\cos\theta_e} \propto \Sigma_\perp (1 + \cos^2\theta_e) + \Sigma_\parallel (1 - \cos^2\theta_e)$$

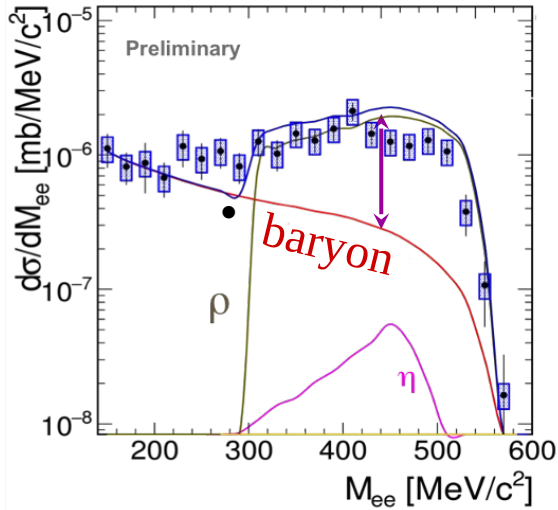
$$\propto A(1 + \lambda_\theta(\theta_{\gamma^*}, M) \cos^2\theta_e)$$

angular distributions depends on spin and parity of resonance state (λ_θ from the model):



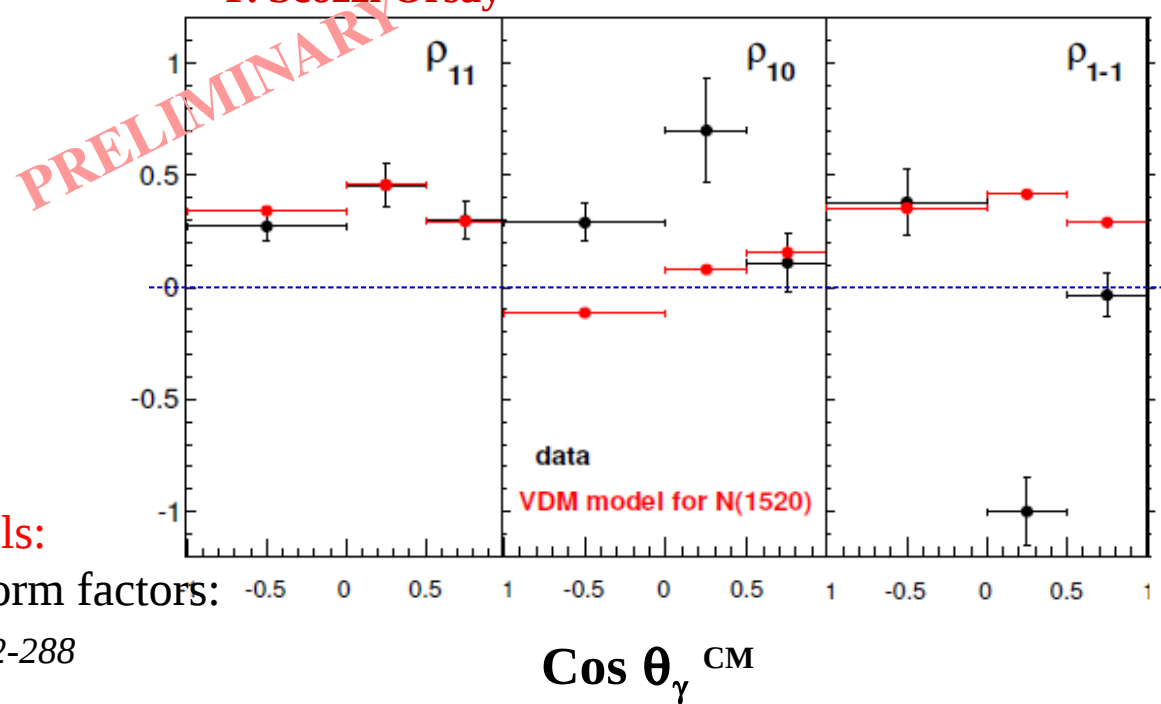
$\pi^- p \rightarrow e^+ e^- n$ – Angular Distributions

additional information
on the electromagnetic
structure of the transition



$M_{ee} > 400 \text{ MeV}/c^2$

B. Ramstein contribution from Hades CM GSI
F. Scozzi Orsay



For real γ , $\rho_{11}=1/2$, $\rho_{10}=0$

Microscopic model s and u channels:

N(1440) and N(1520) with VDM form factors:

E. Speranza et al, Phys.Lett. B764 (2017) 282-288

➔ low statistics but still valid information on the electromagnetic structure of the transition can be drawn:

- presence of **longitudinal** contribution
- data are consistent with pure N(1520) in VDM model

New Event Generator

- virtual photon

→ real photon estimation (no longitudinal polarization, no FF),
total cross section from experimental data:

$$\sigma_{\pi p \rightarrow \gamma n} \approx 2 \sigma_{\gamma n \rightarrow \pi p} \quad (\text{related via detailed balance})$$

+ Partial Wave Analysis

separation into resonances: @ $\sqrt{s} \sim 1.5$ GeV:
dominance of **D₁₃** and **S₁₁**

coherent sum of s, t, u channels is taken

→ the production cross section for **S11** and **D13**
in π -p is **7.6** and **18.7 mb**, respectively (PWA)

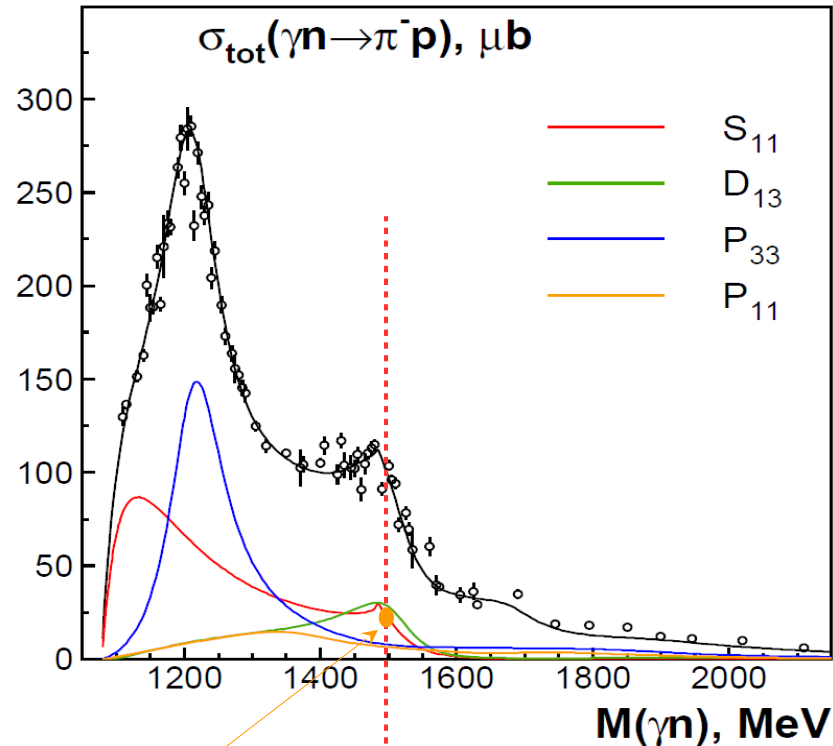
→ $\sigma(\pi\text{-}p \rightarrow n\gamma)$ can be calculated as:

S11: $7.6 * 0.0034$ (BR) = **26 μb**

D13: $18.7 * 0.022$ (BR) = **43 μb**

Remaining part of 60 μb comes from
non-resonant background contribution
(~ 17 and 34 mb, respectively)

→ $\sigma(e^+e^-)$: factor **1/137**



60 μb

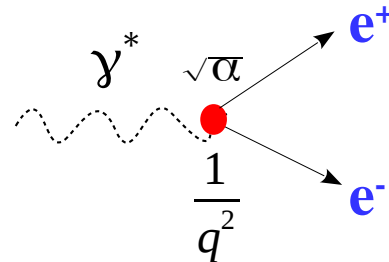
New Event Generator

- virtual photon

→ real photon estimation :

α/q^4 - photon propagator

$z = \cos \theta_{\gamma^*}$



= 1

$$\frac{d\sigma_{\pi p \rightarrow n e^+ e^-}^\perp}{dz} = \frac{d\sigma_{\pi p \rightarrow \gamma n}}{dz} \frac{\alpha}{3\pi q^4} \left[\frac{h_{xx}(q^2, z) + h_{yy}(q^2, z)}{h_{xx}(0, z) + h_{yy}(0, z)} \right] \left(1 - \frac{2m_n^2}{s} + \frac{m_n^4}{s^2} \right)^{-\frac{1}{2}} \times$$

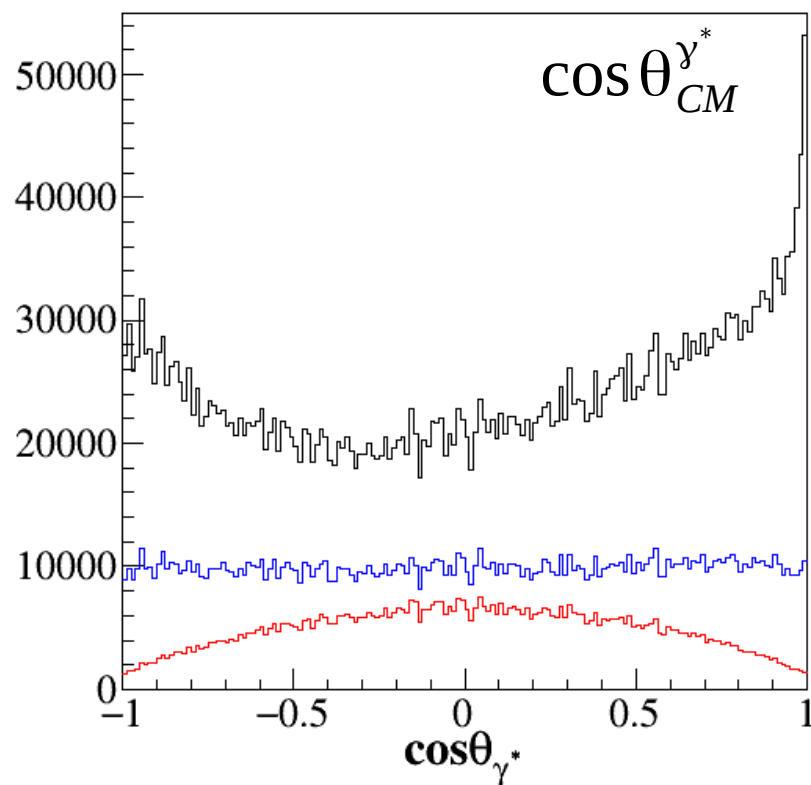
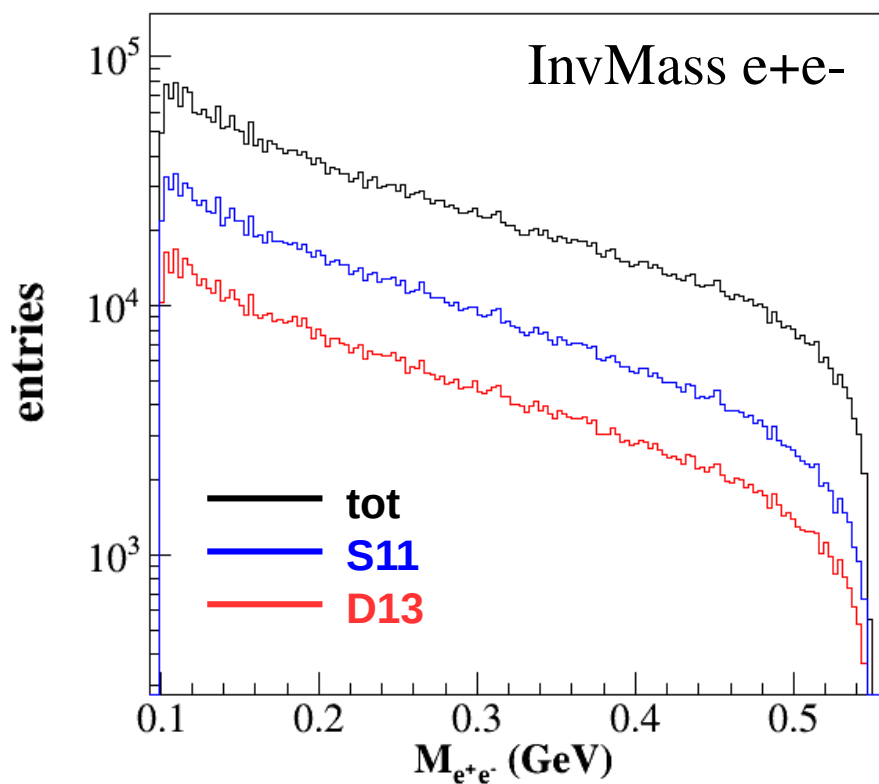
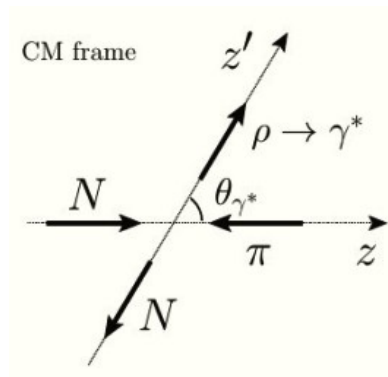
$$(2m_e^2 + q^2) \sqrt{1 - \frac{2(m_n^2 + q^2)}{s} + \frac{(m_n^2 - q^2)^2}{s^2}} \sqrt{1 - \frac{4m_e^2}{q^2}} dq^2 dz.$$

integration of the lepton tensor over the lepton angles

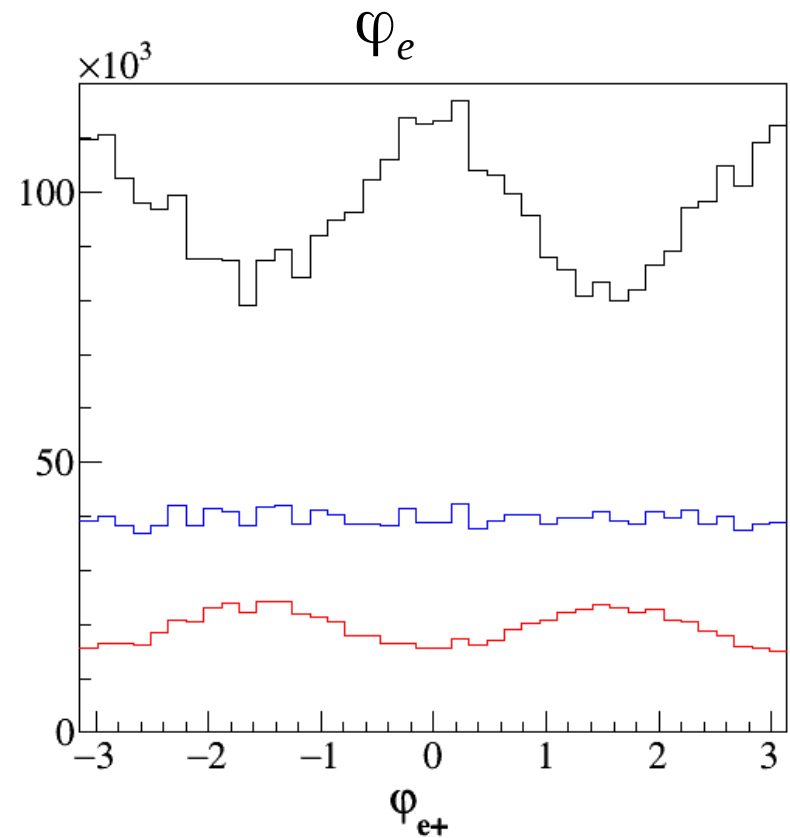
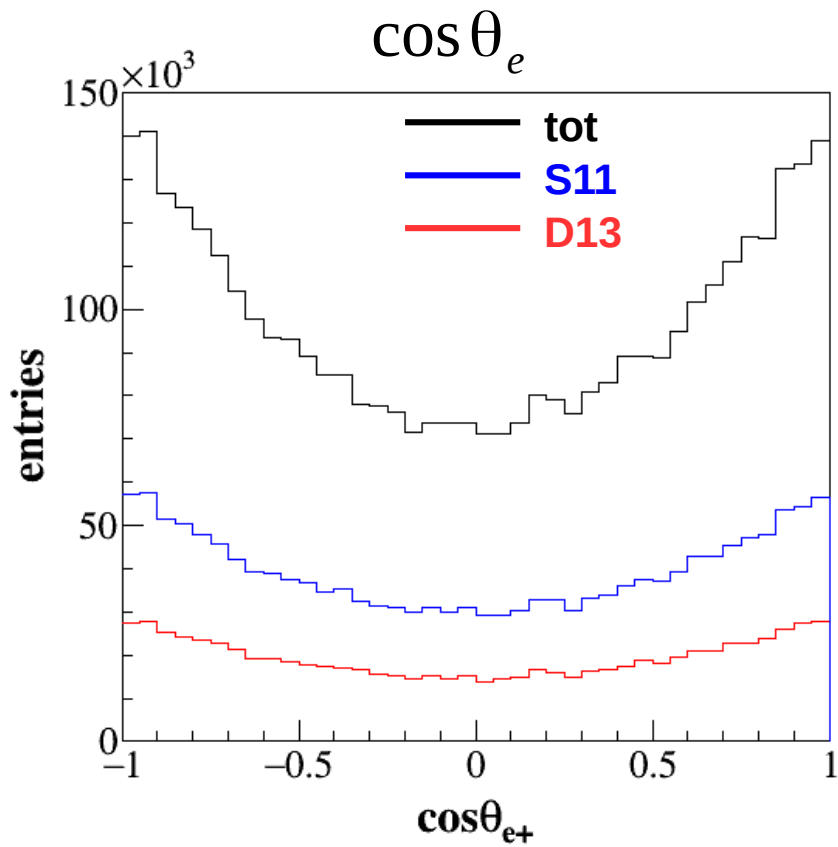
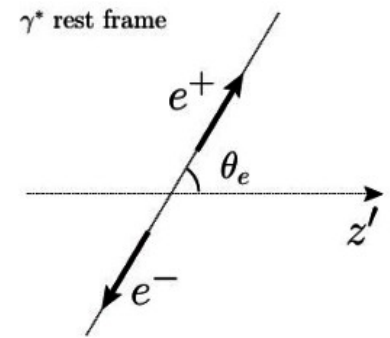
$$\frac{\phi_{ne+e}^{(3)}}{\phi_{n\gamma}^{(2)}}$$

3- and 2-body phase space difference

Signal Simulations



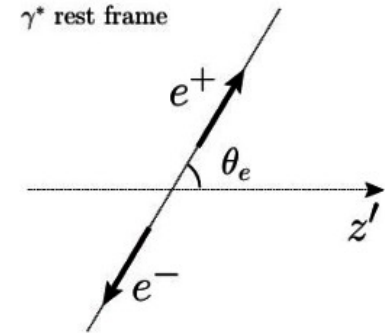
Signal Simulations



$$\pi^0 \rightarrow \gamma\gamma^* \rightarrow \gamma e^+e^-$$

1. photon virtuality q^2 is randomized (according to VDM):

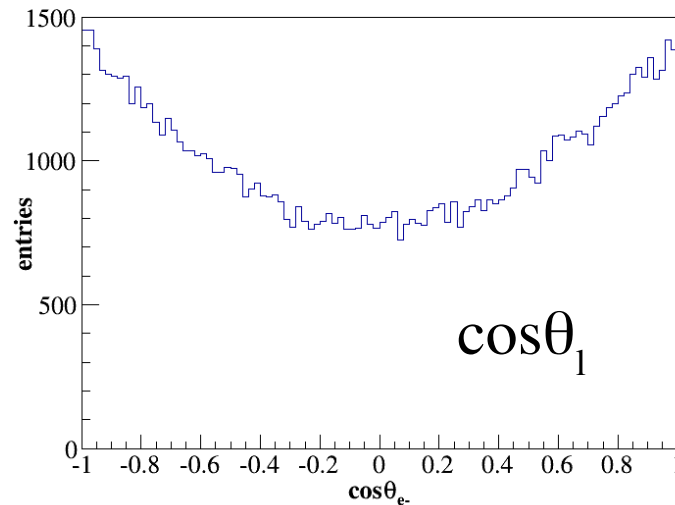
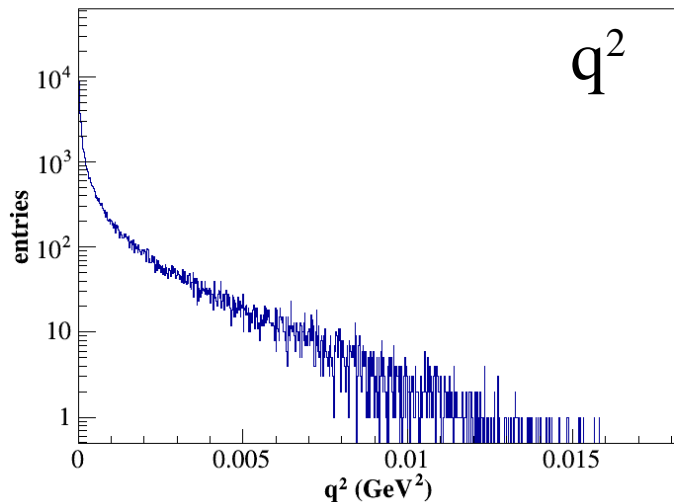
$$\frac{d\Gamma(\pi^0 \rightarrow \gamma e^+ e^-)}{dq^2 \Gamma(\pi^0 \rightarrow \gamma\gamma)} = \frac{2\alpha}{3\pi} \left[1 - \frac{4m_e^2}{q^2}\right]^{1/2} [q^2 + 2m_e^2] \frac{1}{q^4} \left[1 - \frac{q^2}{m_{\pi^0}^2}\right]^3 |F(q^2)|^2$$



2. angular distributions are generated

$$(q^2 + 2m_e^2) \rightarrow \frac{3}{2} (|k|^2(1 + \cos^2 \theta_l) + 2m_e^2)$$

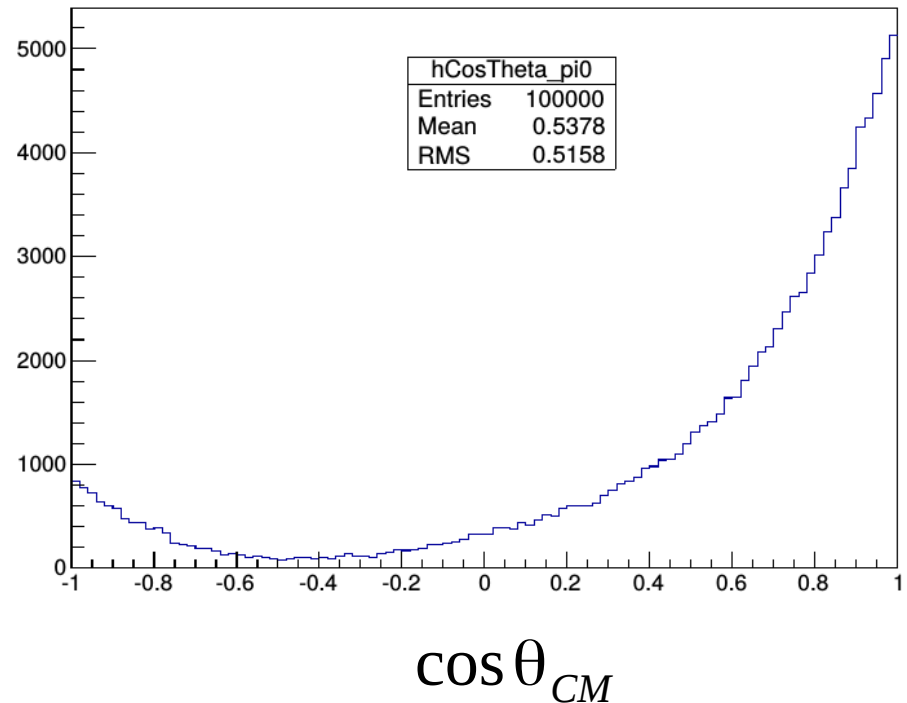
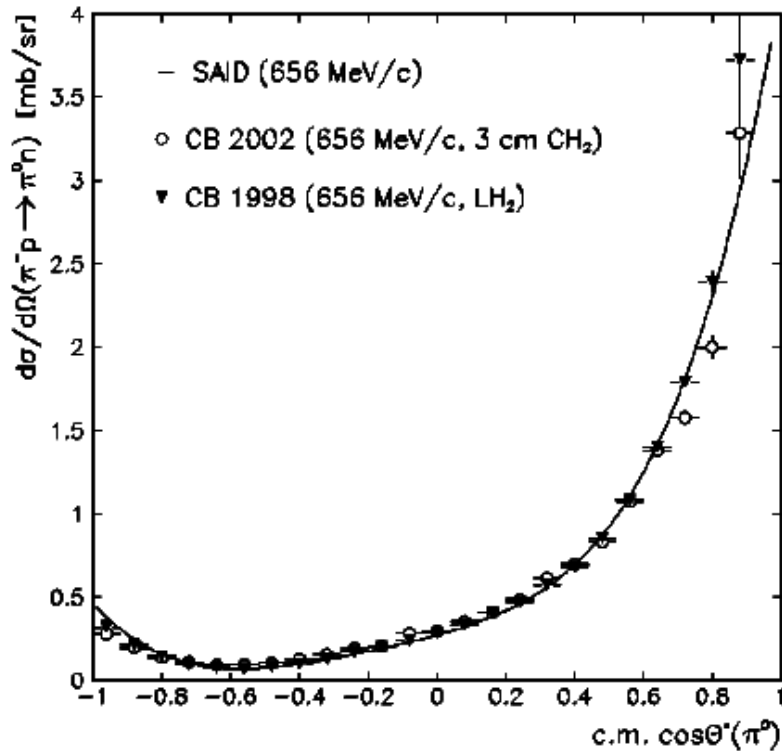
$k=k(q^2)$ – momentum of a lepton in a γ^* reference frame



1. $\pi^- p \rightarrow \pi^0 n$ @ 690 MeV/c

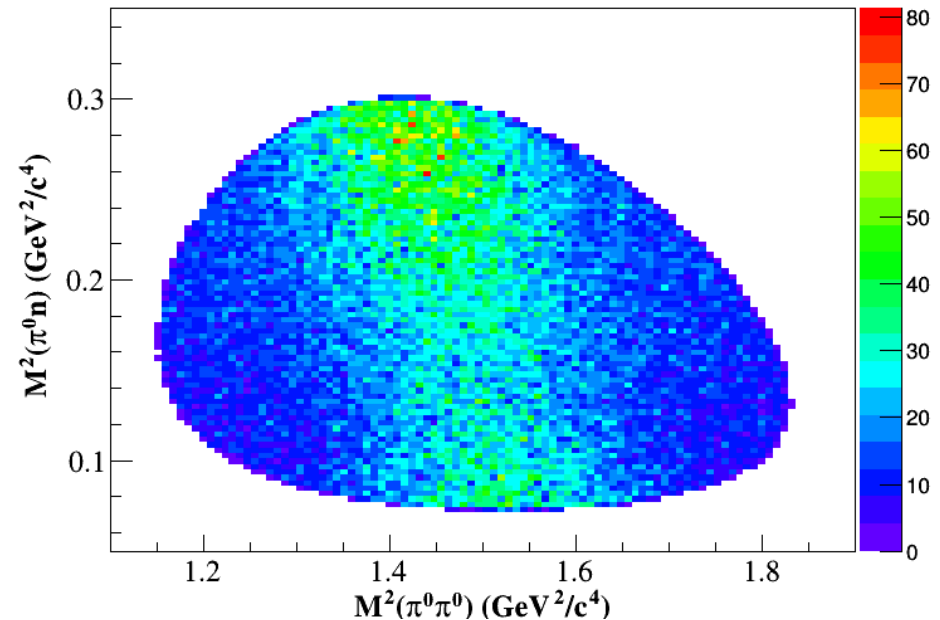
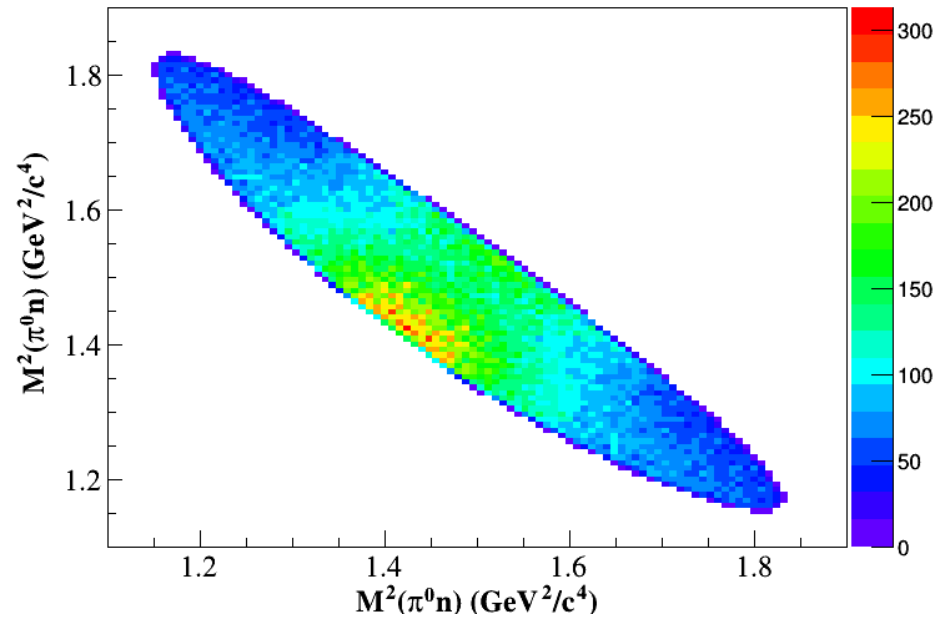
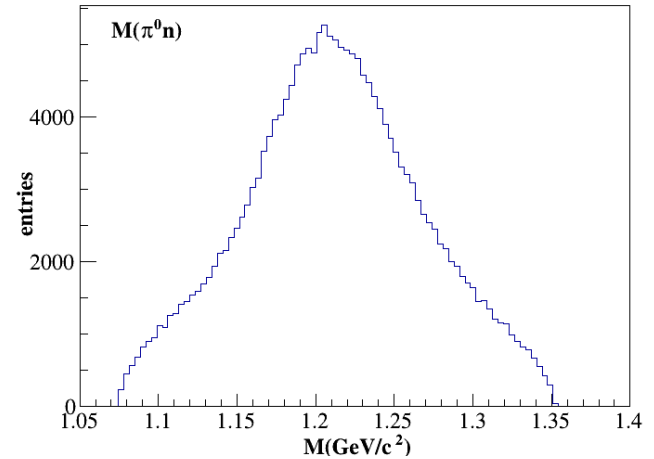
Generated events vs SAID PWA

Total cross section: $\sigma_{\pi n} = 8.33 \pm 0.41$ mb, $p=690$ MeV/c

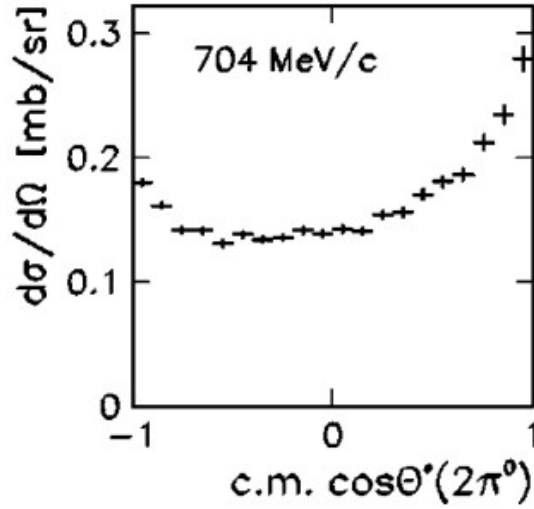
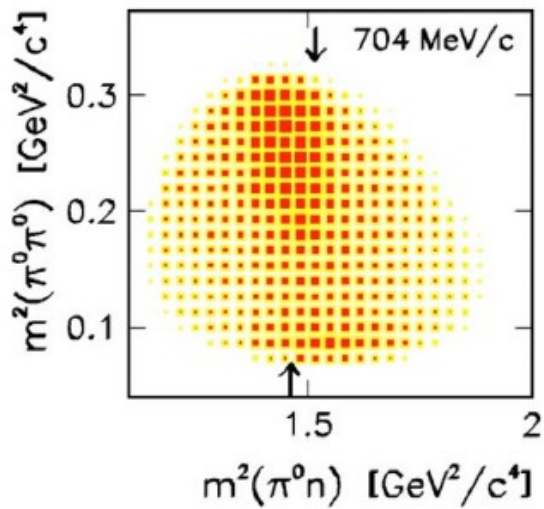


$\pi^- p \rightarrow \pi^0 \pi^0 n$

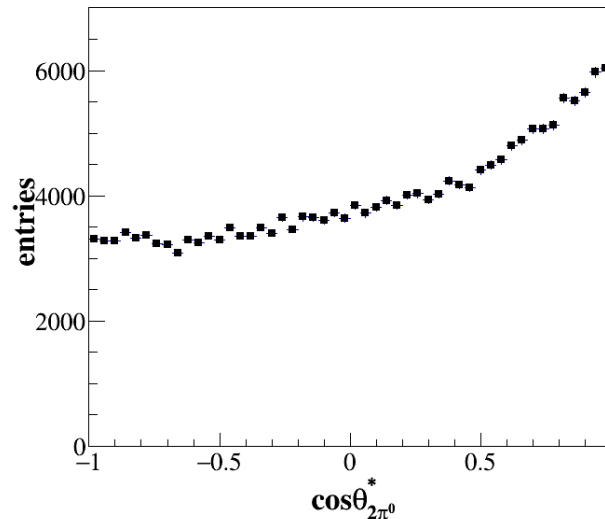
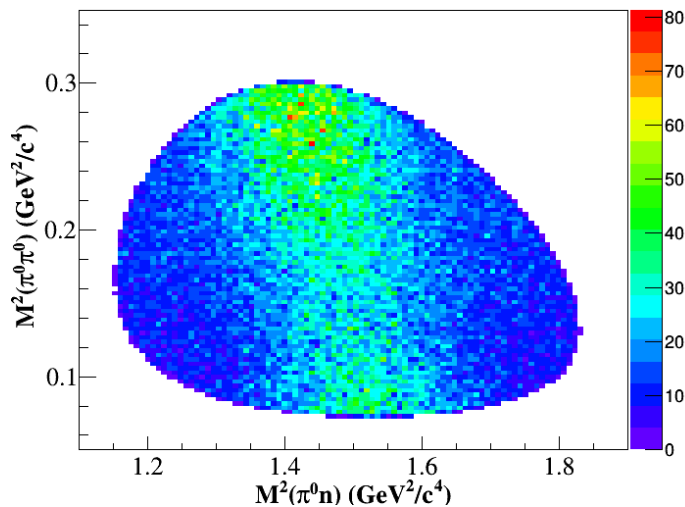
1. the phase space is weighted according to Bonn-Gatchina PWA solution,
2. random π^0 is chosen,
3. its decay to γe^+e^- is simulated



$\pi^-p \rightarrow \pi^0\pi^0n$ in comparison to data



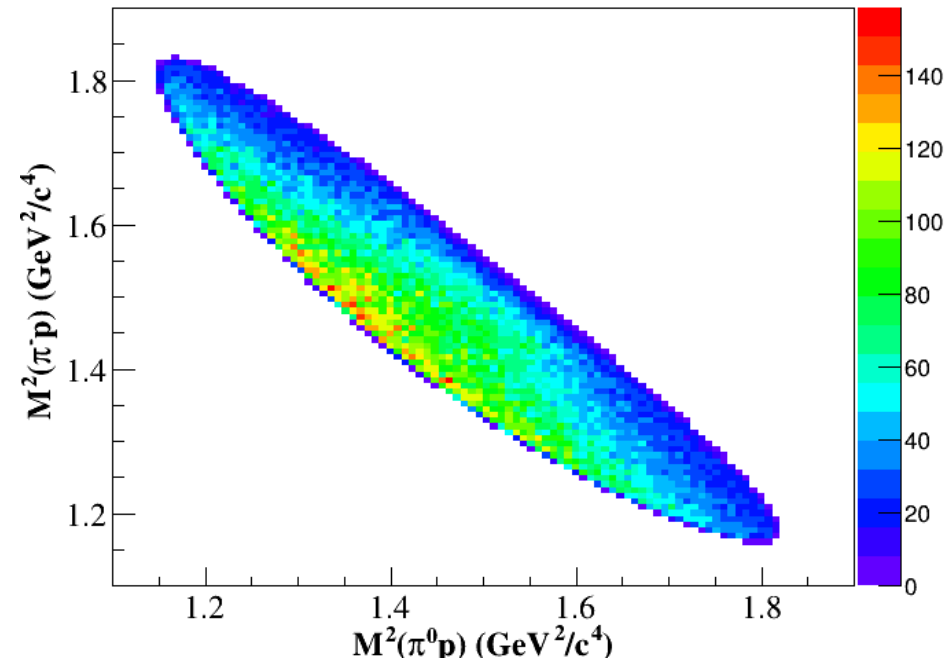
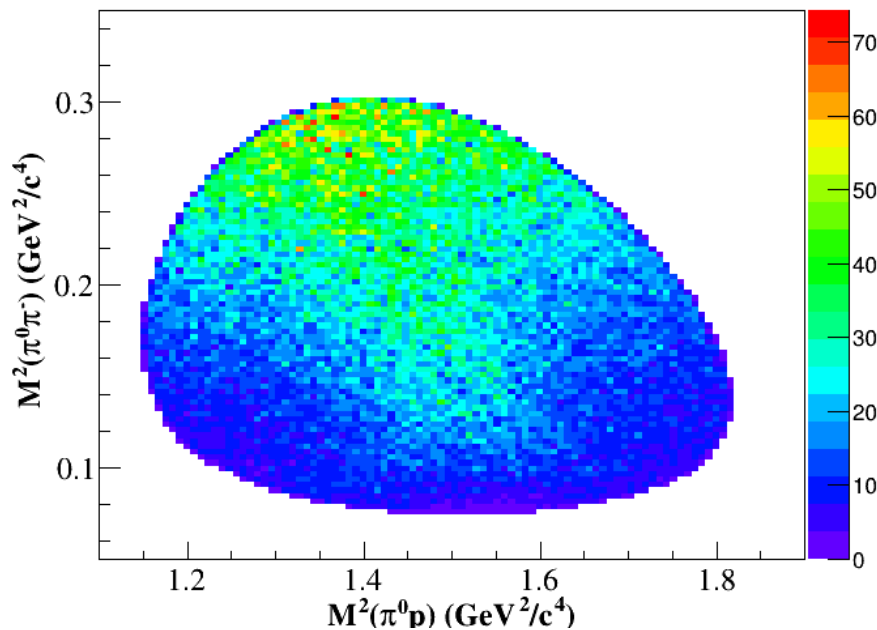
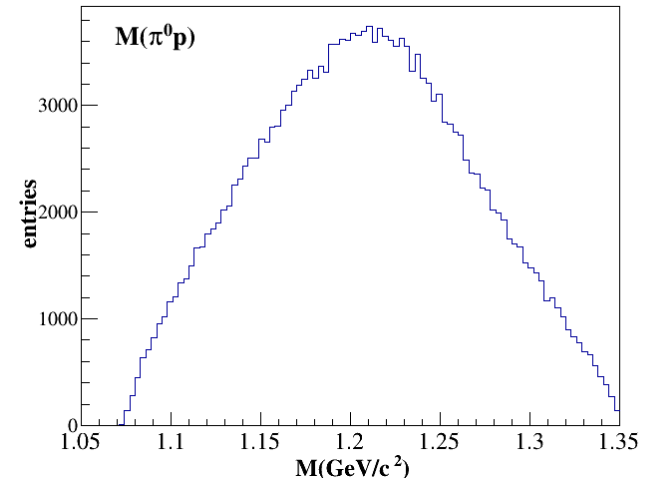
Crystal Ball data
 @ $p = 704$ MeV/c
Phys. Rev. C 69, 045202(2004)



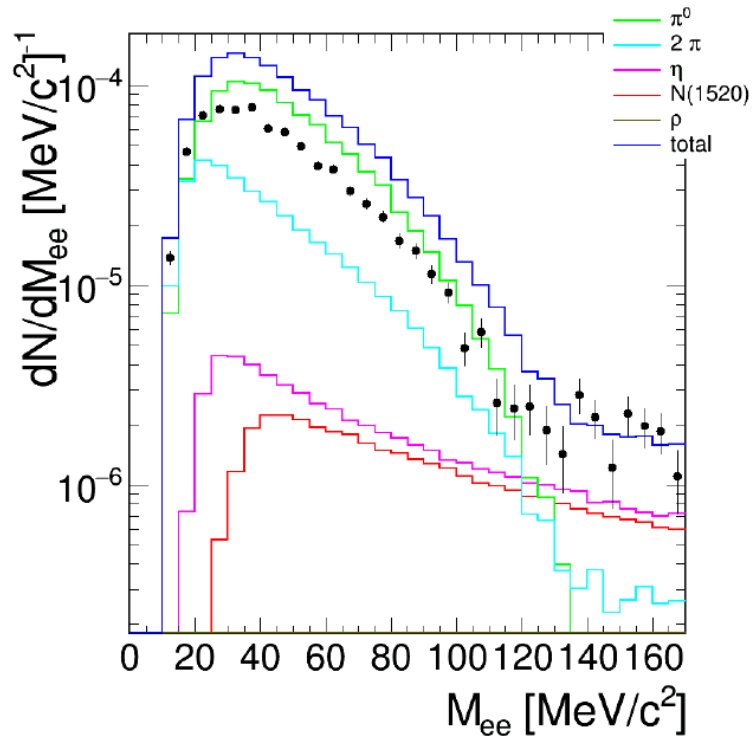
Generator
 @ $p = 690$ MeV/c

$\pi^- p \rightarrow \pi^0 \pi^- p$

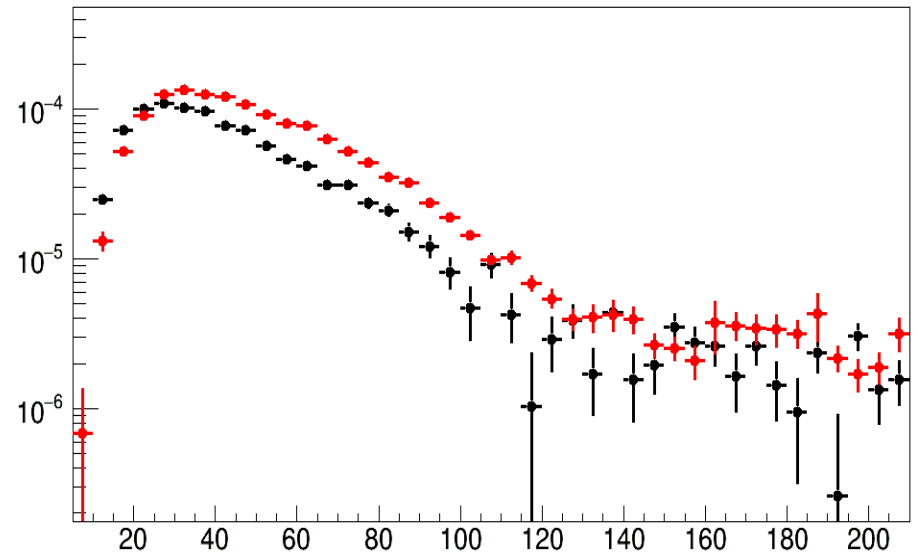
1. the phase space is weighted according to Bonn-Gatchina PWA solution,
2. random π^0 is chosen,
3. its decay to γe^+e^- is simulated



PLUTO cocktail (16.6 mb)

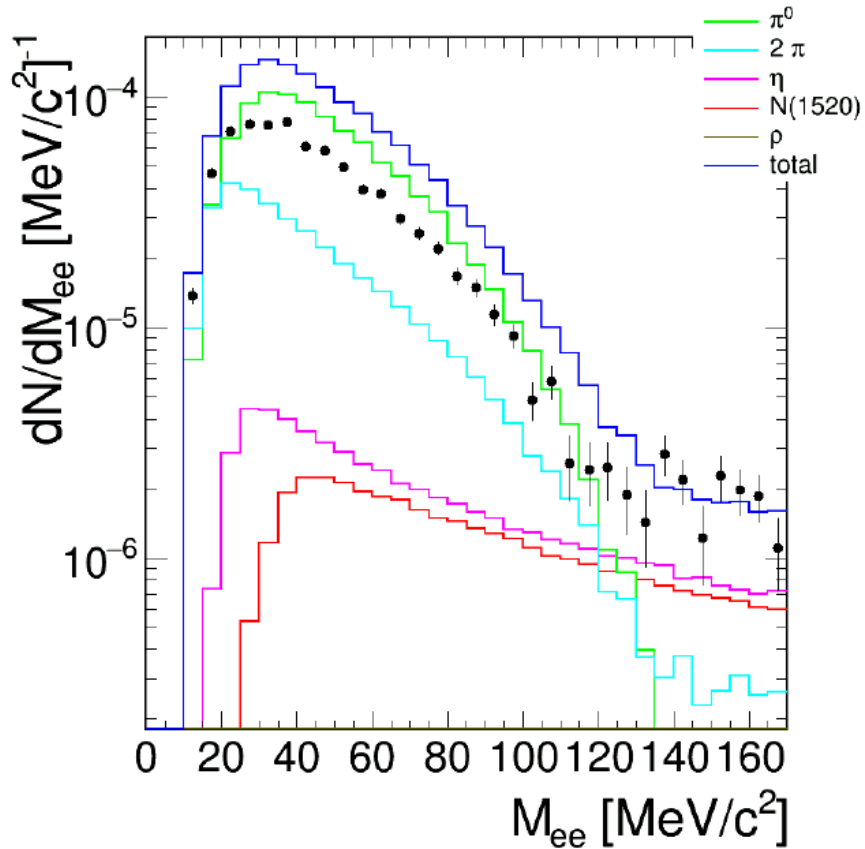


GiBUU (19 mb)

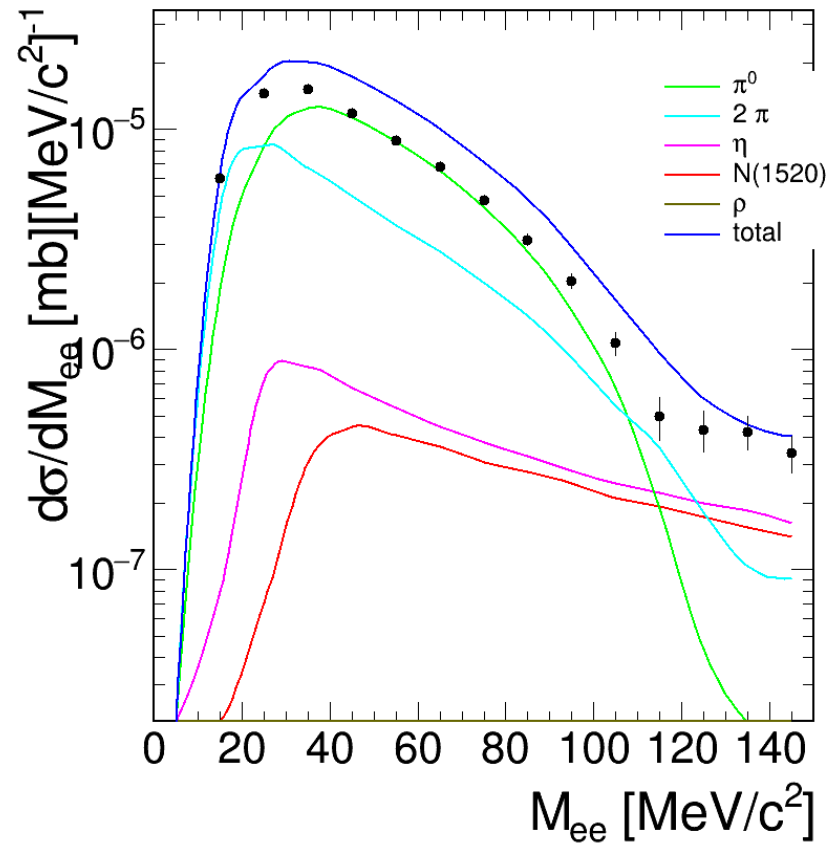


→ model dependence of the π^0 peak in acceptance

PLUTO cocktail (16.6 mb)



New event generator with proper angular distribution



Summary & Outlook

The code will be used to:

- fit Spin Density Matrix Elements (**SDME**) from data inside the HADES acceptance (based on method used by Bonn-Gatchina) evaluate the systematics of SDME extraction.

Plans:

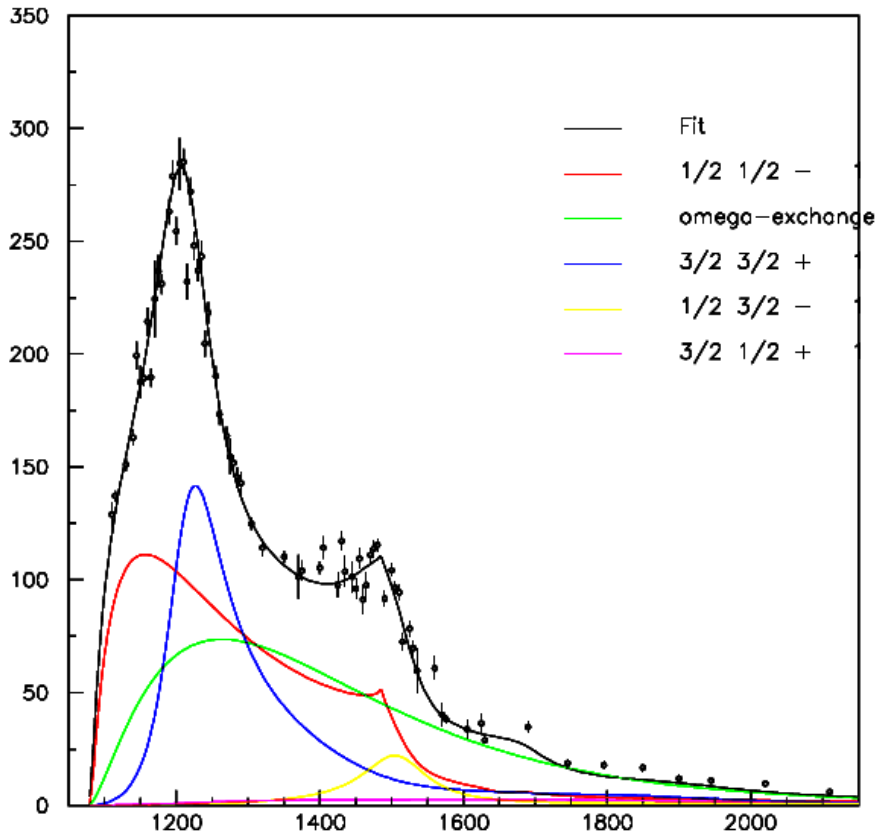
- extract SDME from the data
- further consistency checks of the generator
- comparison with the coefficients calculated with the GSI model (Speranza et al.)
- compare with the Hades distributions in the acceptance



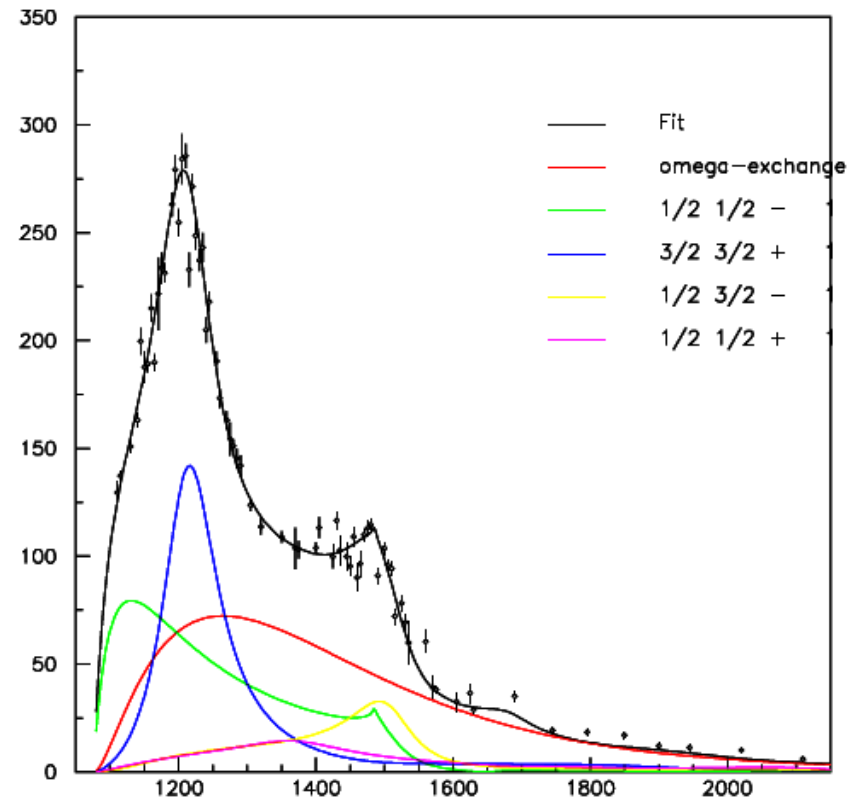
**Thank You
for
Your Attention**

Backup

S11/D13 ~ 2:1
projection on s channel



S11/D13 ~ 1:1
s, t, u channels summed coherently



	D13	S11
Andrey PWA	0.23% ($BR_{n\gamma}$)	0.35% ($BR_{n\gamma}$)
Res. prop. (Andrey's PWA)-BW widths	$\Gamma_{\text{tot}} = 114 \text{ MeV}$ $\Gamma_{n\gamma} = 260 \text{ keV (BR=0.23\%)}$	$\Gamma_{\text{tot}} = 116 \text{ MeV}$ $\Gamma_{n\gamma} = 400 \text{ keV (BR=0.35\%)}$
PDG (2017)	$BR_{n\gamma} = 0.3\text{-}0.53\%$	$BR_{n\gamma} = 0.01\text{-}0.25\% (!)$
Zetenyi/Wolf	$BR_{n\gamma} = 0.42\%$	$BR_{n\gamma} = 0.15\%$