

# Dark Matter Bound States

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Talk at CoDyCE workshop, Lyon 30.08.2018

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M. Redi, A. Salvio, F. Sannino and A. Strumia

# The Effect of Unstable Bound States of Dark Matter

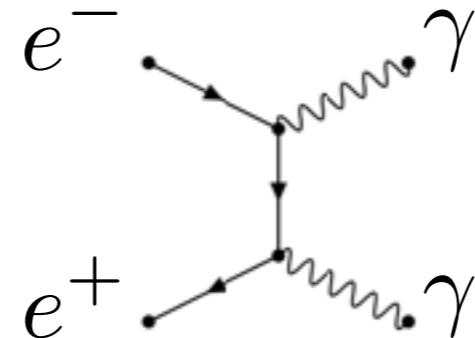
Process

Diagram

Cross-  
Section area

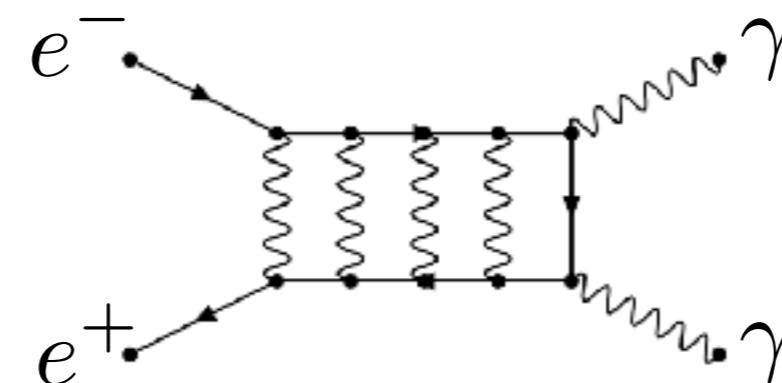
I)

$$e^+ e^- \rightarrow \gamma\gamma$$



II)

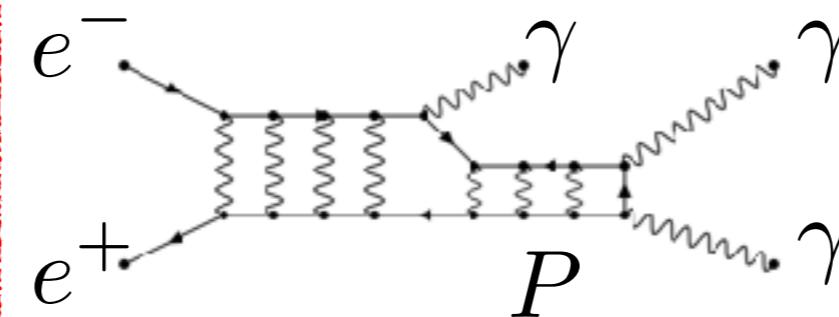
$$e^+ e^- \rightarrow P^* \rightarrow \gamma\gamma$$



III)

$$e^+ e^- \rightarrow P^* \rightarrow P\gamma$$

$$P \rightarrow \gamma\gamma$$



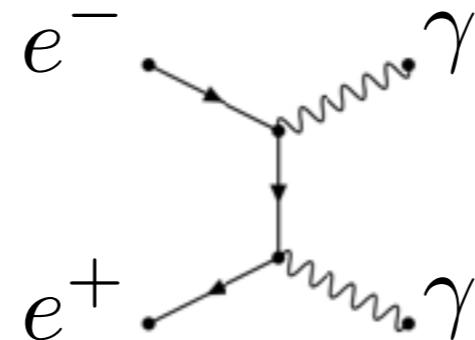
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## Diagram

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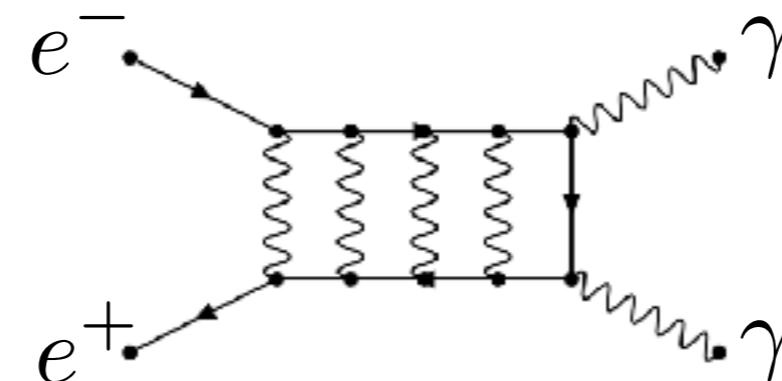


large  
velocity



II)

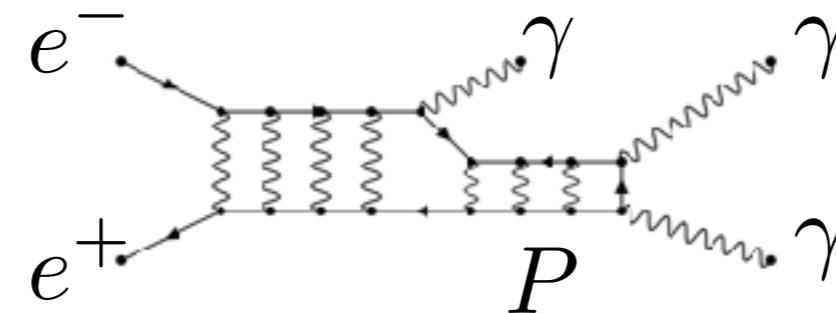
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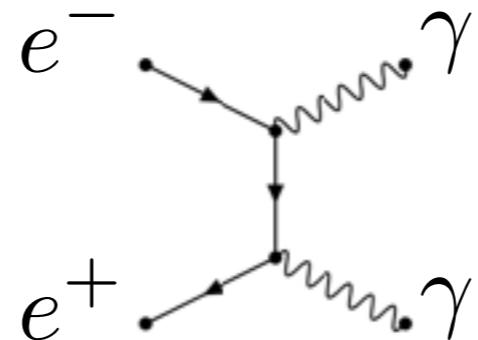
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# Cross- Section area

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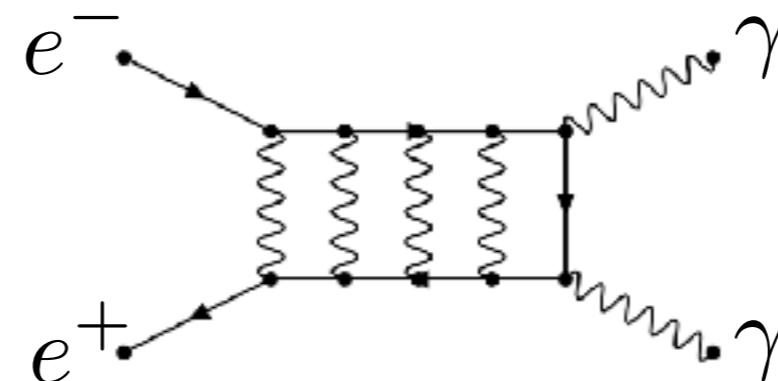
|                   |                   |
|-------------------|-------------------|
| large<br>velocity | small<br>velocity |
|-------------------|-------------------|



small  
velocity

II)

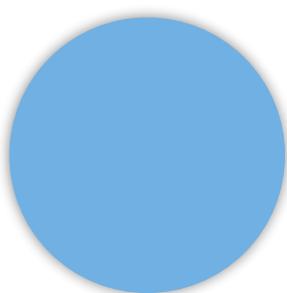
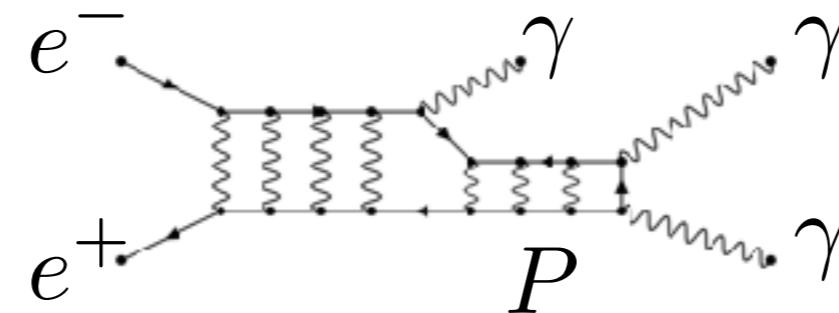
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# Non perturbative Effects

$$M_V < \alpha_{\text{eff}} M_\chi$$
$$R_{\text{Bohr}} < R_{\text{Yukawa}}$$

$$V(r) = -\alpha_{\text{eff}} \frac{e^{-M_V r}}{r} \approx -\alpha_{\text{eff}} \left( \frac{1}{r} - M_V \right)$$

$$E_{n\ell} \simeq \frac{\alpha_{\text{eff}}^2 M_\chi}{4n^2} - \alpha_{\text{eff}} M_V + \mathcal{O}(M_V^2).$$

# Non perturbative Effects

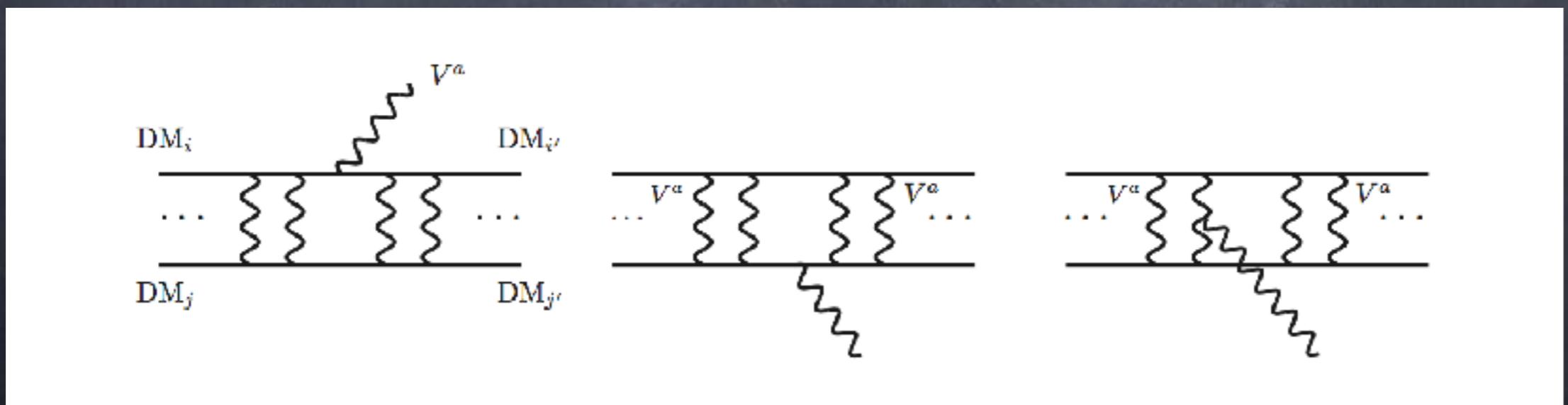
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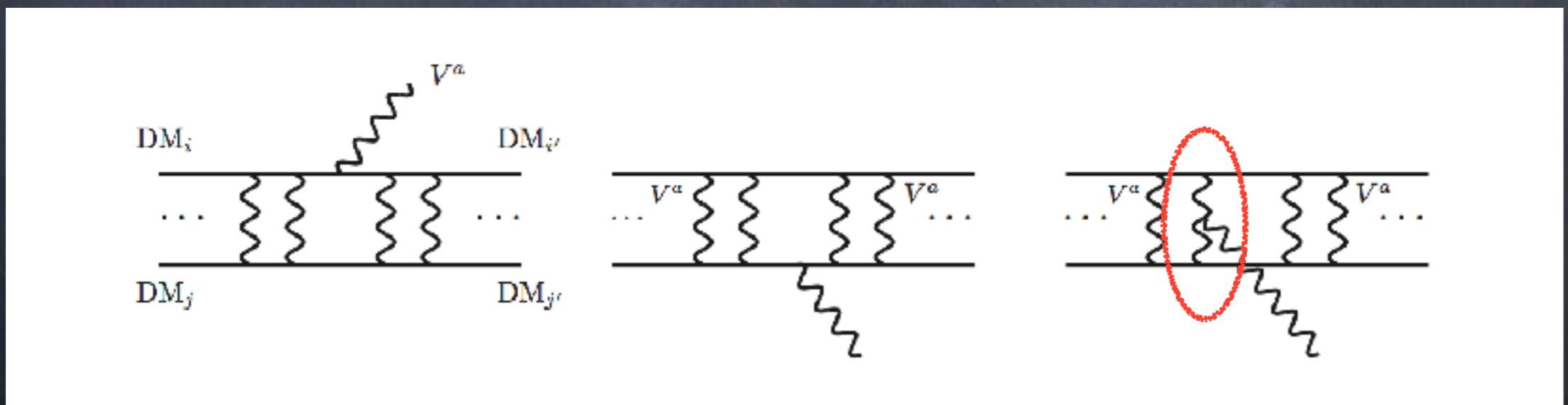
# Bound State Selection Rules

- The Group theory structure
- The wave function symmetry
- Angular momentum conservation  $\Delta L = 1$
- Energy conservation



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# Cosmological Impact

$$\frac{dY_{DM}}{dz} = -\frac{\langle \sigma v \rangle_{\text{ann}}}{z^2} (Y_{DM}^2 - Y_{eq.}^2) - \sum_i \frac{\langle \sigma v \rangle_{\text{bsf}}}{z^2} \left( Y_{DM}^2 - Y_{B_i} \frac{Y_{eq.}^2}{Y_{eq.}^{B_i}} \right)$$
$$\frac{dY_B}{dz} = \sum_i \frac{\langle \sigma v \rangle_{\text{bsf}}}{z^2} \left( Y_{DM}^2 - Y_{B_i} \frac{Y_{eq.}^2}{Y_{eq.}^{B_i}} \right) - \Gamma_B (Y_B - Y_{eq.}^B) + \text{decay of excited states.}$$

$$\frac{dY}{dz} = -\frac{\langle \sigma_{\text{eff}} v_{\text{rel}} \rangle s}{Hz} (Y_{\text{DM}}^2 - Y_{\text{DM}}^{\text{eq2}}) = -\frac{\lambda S(z)}{z^2} (Y_{\text{DM}}^2 - Y_{\text{DM}}^{\text{eq2}}),$$

$$S(z) = S_{\text{ann}}(z) + \left[ \frac{\sigma_0}{\langle \sigma_I v_{\text{rel}} \rangle} + \frac{g_\chi^2 \sigma_0 M_\chi^3}{2g_I \Gamma_{\text{ann}}} \left( \frac{z}{4\pi} \right)^{3/2} e^{-z E_{BI}/M_\chi} \right]^{-1}$$

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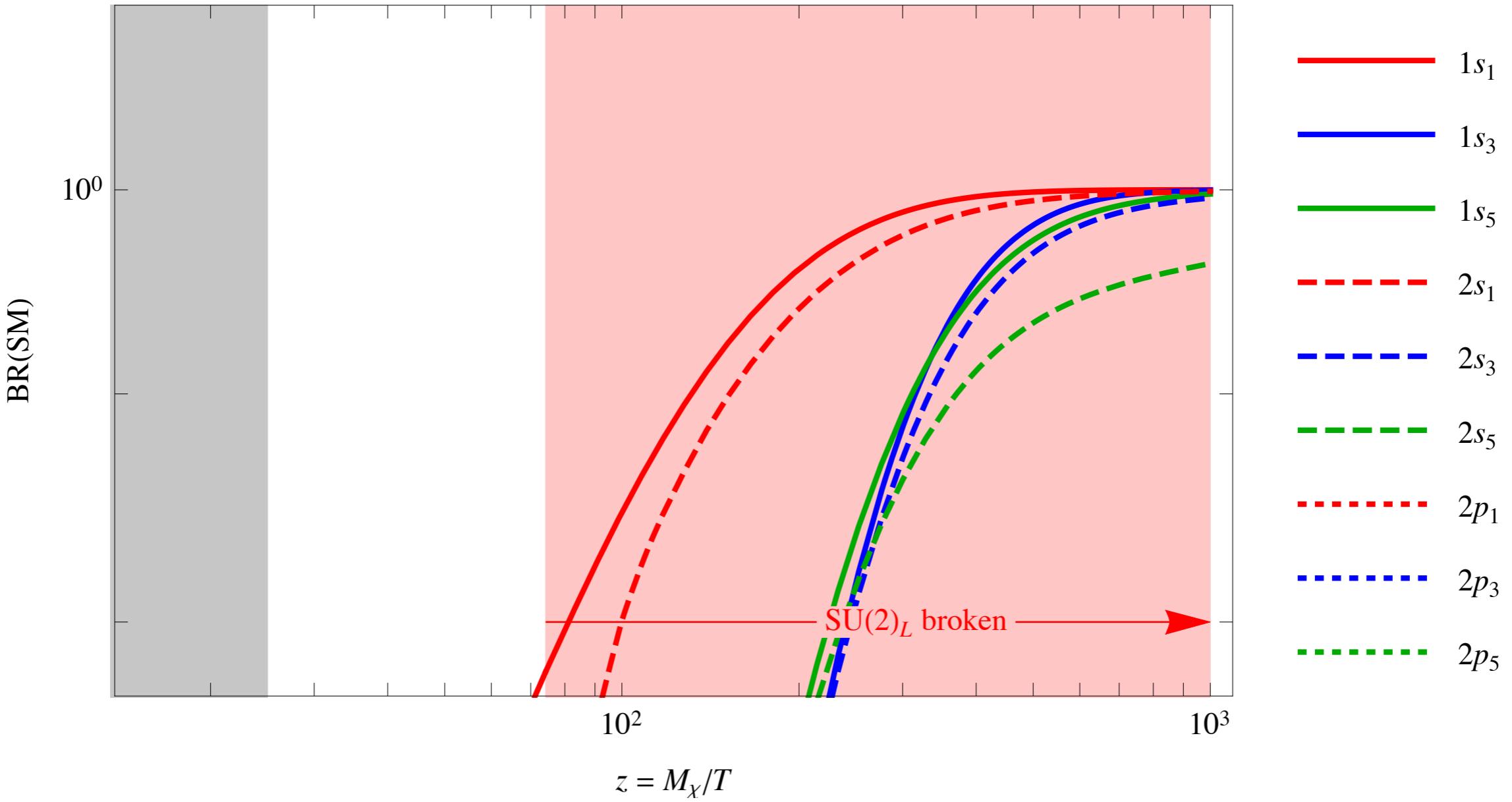
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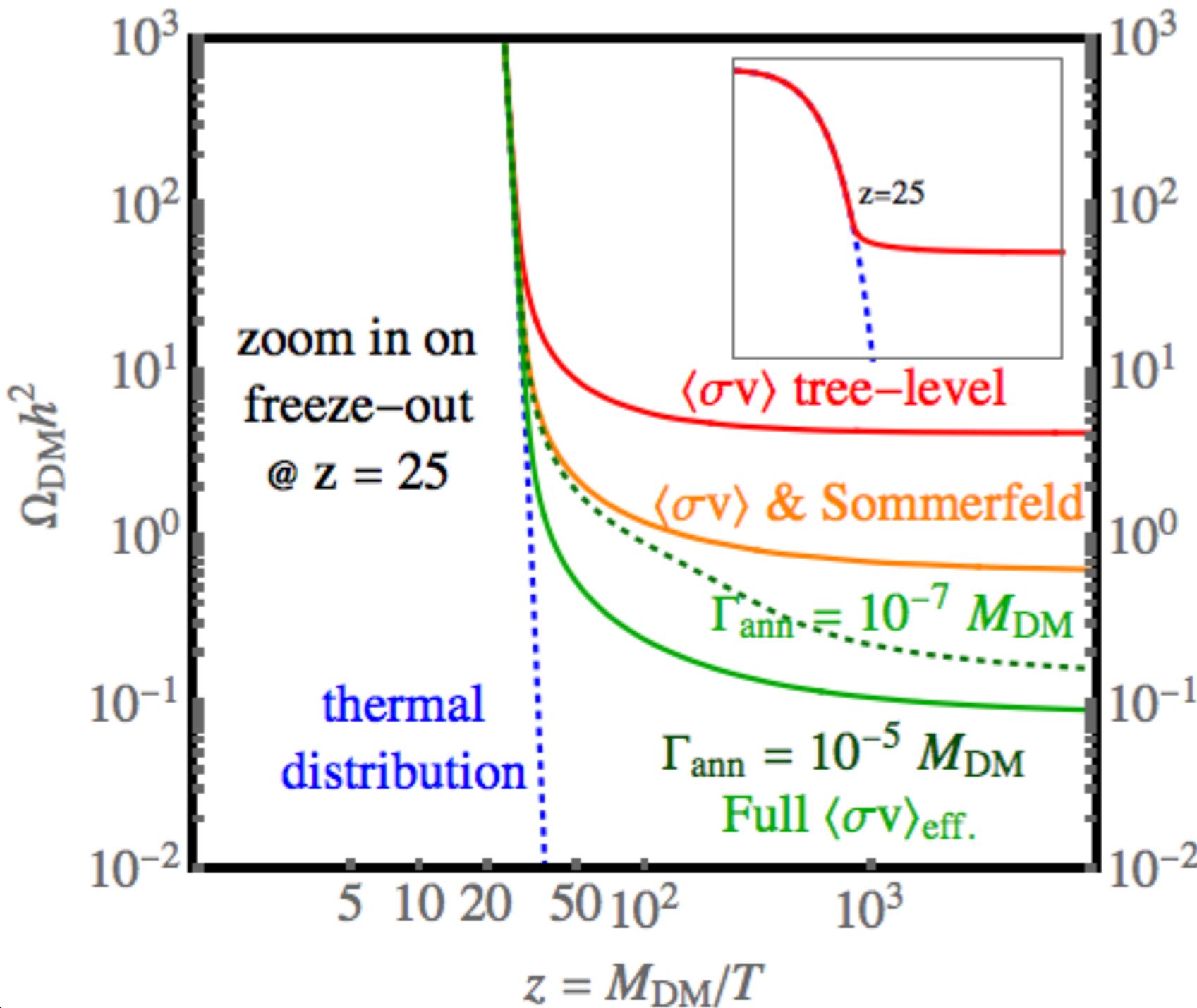
$\langle \sigma v \rangle_{\text{bsf}}$  BR(B → SM)

# Cosmological Impact

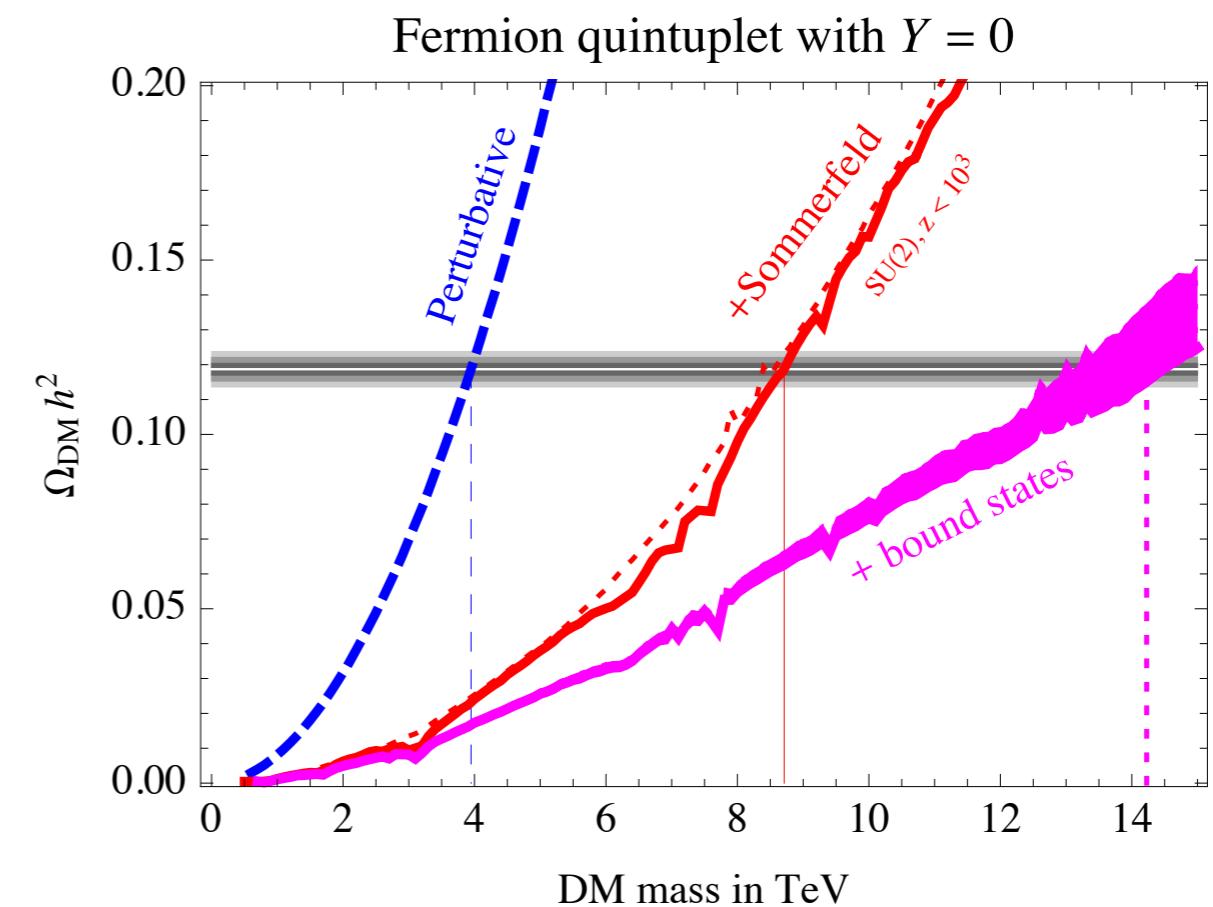
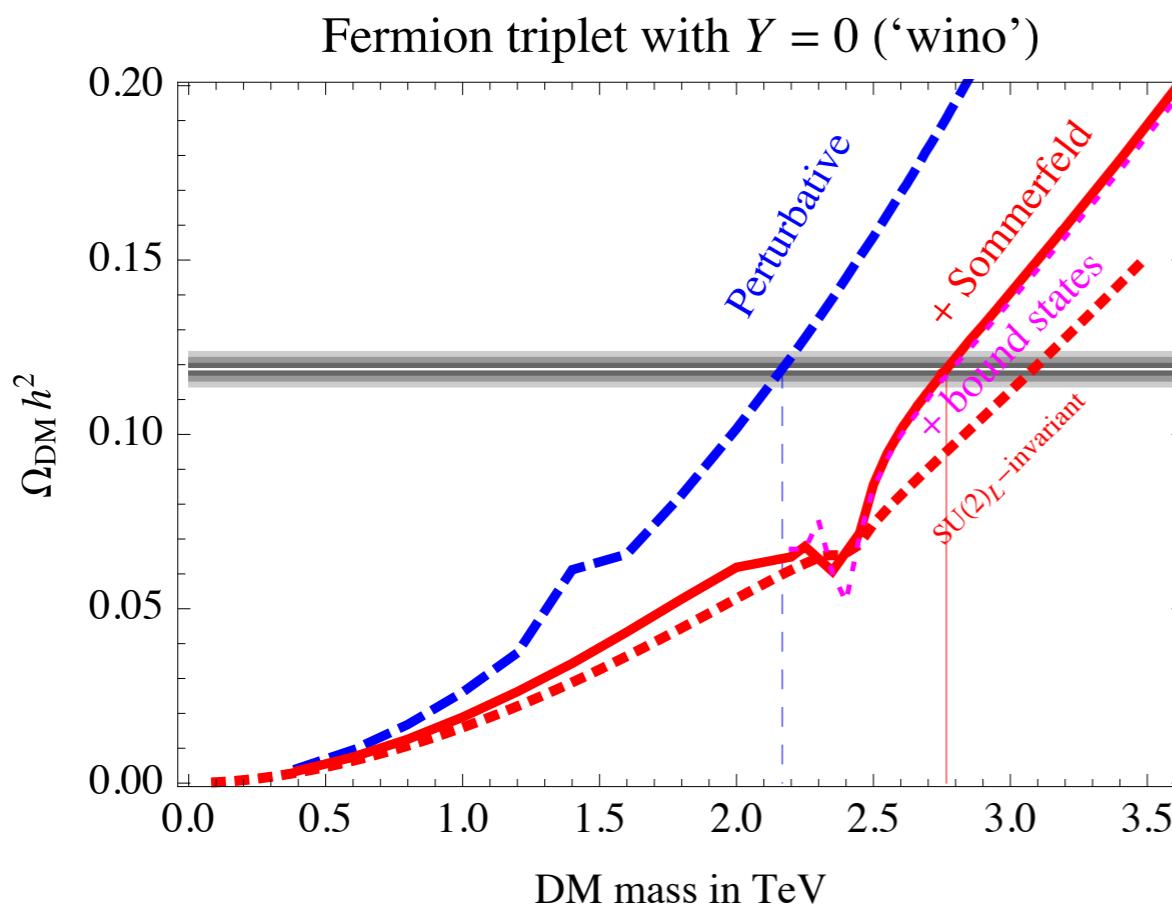
Fermion 5plet,  $M_\chi = 14$  TeV, Coulomb approximation



# Toy System



# Application I: The gauge portal



The Triplet  
(Wino)

The Quintuplet  
(Minimal Dark Matter)

# Summary I

- Bound State formation is an additional Non-perturbative effect which affects the DM annihilation cross section
- In models with sizeable gauge coupling and heavy dark matter candidates it can be the dominant effect setting the relic density
- Today bsf can lead to observable capture photon signals and give precision information about dark matter

Details in: JCAP 1705 (2017) no.05, 006  
arXiv:1702.01141

# Stable Bound States of Dark Matter

# Dark Matter stability

$$SU(N)_{\text{DC}} \times SU(3)_c \times SU(2)_L \times U(1)_{\text{em}}$$

$$SU(N)_{\text{DC}} \times SU(3)_c \times U(1)_{\text{em}}$$

| Standard Model of Elementary Particles |                |                |                |         |   |   |  |  |  |
|--|----------------|----------------|----------------|---------|---|---|--|--|--|
| three generations/vector-like fermions |                |                |                |         |   |   |  |  |  |
|  | I              | II             | III            |         |   |   |  |  |  |
| 4 gen. vector-like fermions            | N              | u              | c              | t       | g | H |  |  |  |
| QUARKS                                 | V              | d              | s              | b       | Y |   |  |  |  |
| LEPTONS                                | e              | μ              | τ              | Z boson |   |   |  |  |  |
|  | electron       | muon           | tau            |         |   |   |  |  |  |
|  | ν <sub>e</sub> | ν <sub>μ</sub> | ν <sub>τ</sub> | W boson |   |   |  |  |  |
| SCALAR BOSONS                          |                |                |                |         |   |   |  |  |  |

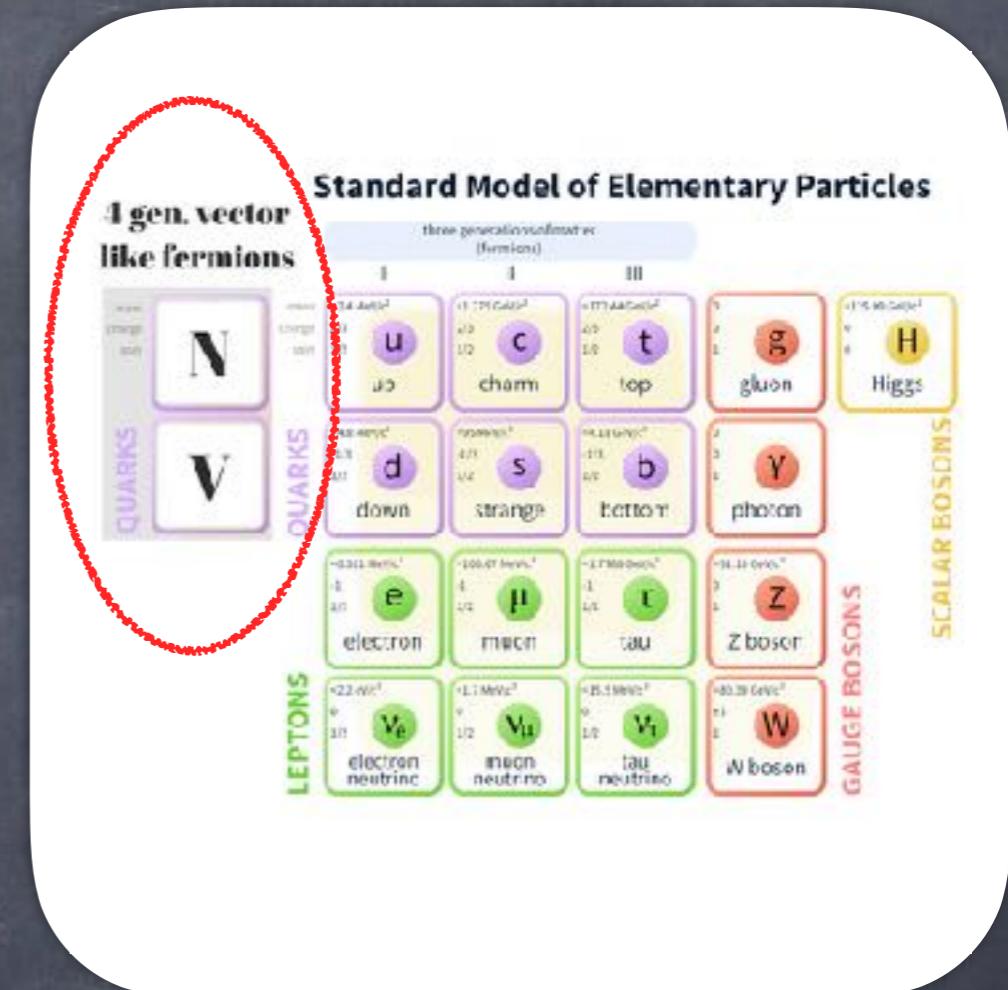
[1503.08749](#)

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New Baryon Number → DM candidate



[1503.08749](#)

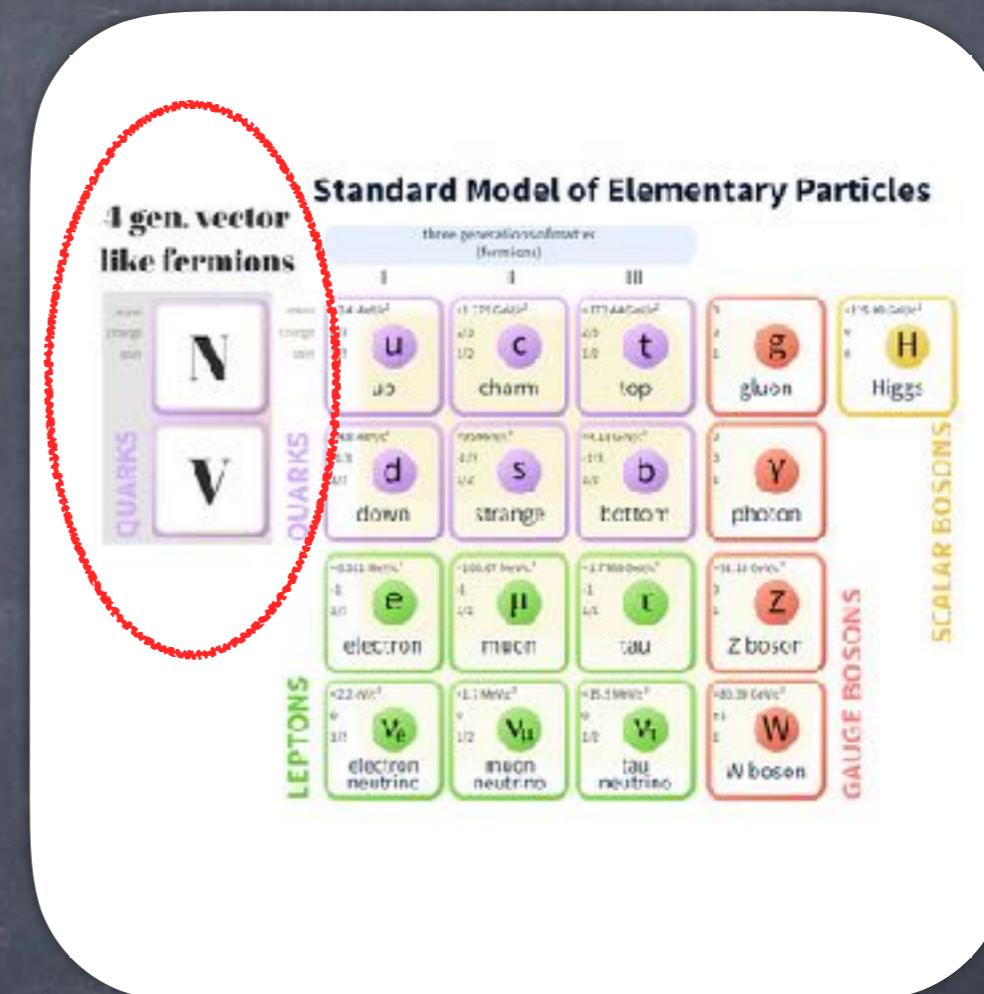
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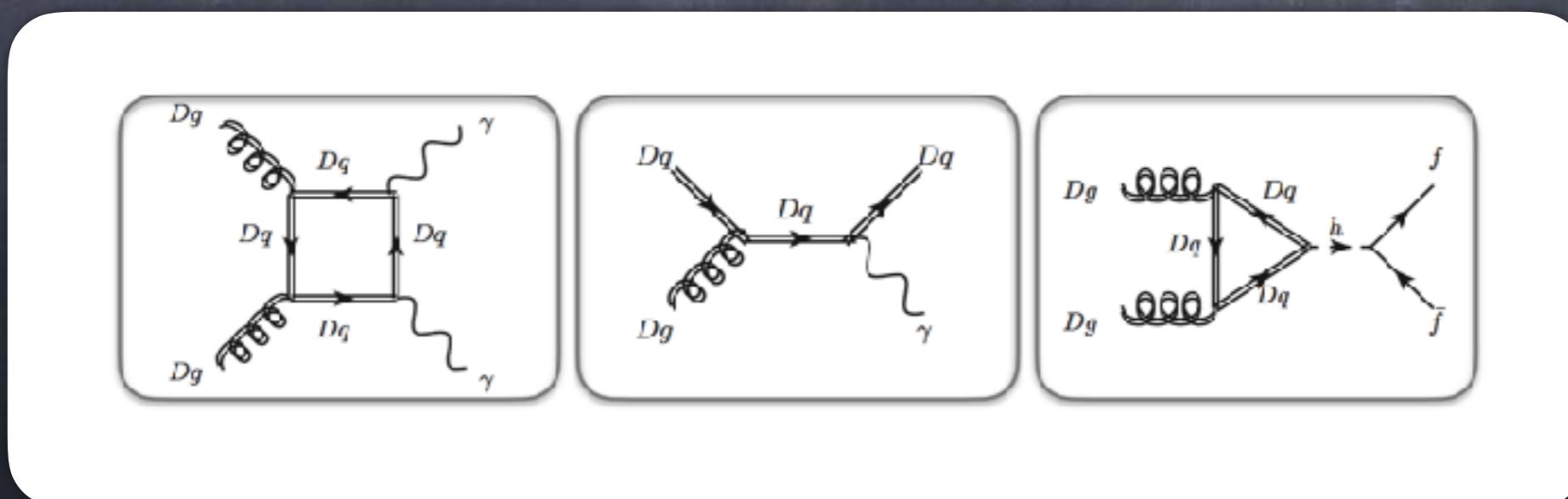
$$SU(N)_{\text{DC}} \times SU(3)_c \times U(1)_{\text{em}}$$

New Baryon Number → DM candidate

Thermal contact with the SM sector



[1503.08749](#)



# Dark Matter stability II

New Baryon Number → DM candidate

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Dim 5 Operators, lifetime too short

New Baryon Number → DM candidate

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Dim 5 Operators, lifetime too short

Dim 6 Operators, acceptable if...

New Baryon Number → DM candidate

# Dark Matter stability II

Dim 5 Operators, lifetime too short

Dim 6 Operators, acceptable if...

$$\mathcal{O}_6 \propto \frac{1}{\Lambda^2} QQQN_R$$

$$\Lambda > 10^{17} \text{ GeV}$$

$$\tau > 10^{18} \text{ sec}$$

New Baryon Number → DM candidate

The cut-off scale has to be close  
to the Plank scale

# Consequences of Dark Color

$$\begin{aligned}\mathcal{L} = \mathcal{L}_{SM} - \frac{\mathcal{G}_{\mu\nu}^{A2}}{4g_{DC}^2} + \frac{\theta_{DC}}{32\pi^2} \mathcal{G}_{\mu\nu}^A \tilde{\mathcal{G}}_{\mu\nu}^A \\ + \bar{Q}_i (iD - m_i) Q_i + y_{ij} H Q_i Q_j^c + h.c.\end{aligned}$$

# Consequences of Dark Color

- Structure formation implies no massless force mediator

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- Structure formation implies no massless force mediator
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# Consequences of Dark Color

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- If gauge group unbroken it has to confine
- Confinement before BBN required
- $Q$  in fund. rep. of  $SU(N)$ : stable particle is  $Q^N$

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# Composite WINO

Simple  
example  
Model-V:

$$SU(3)_{DC} \otimes SU(3)_c \otimes SU(2)_L \times U(1)_Y$$
$$V = (3, 1, 3, 0)$$
$$DC_b = (V, V, V) : (1, 1, 3, 0) \oplus (1, 1, 5, 0)$$

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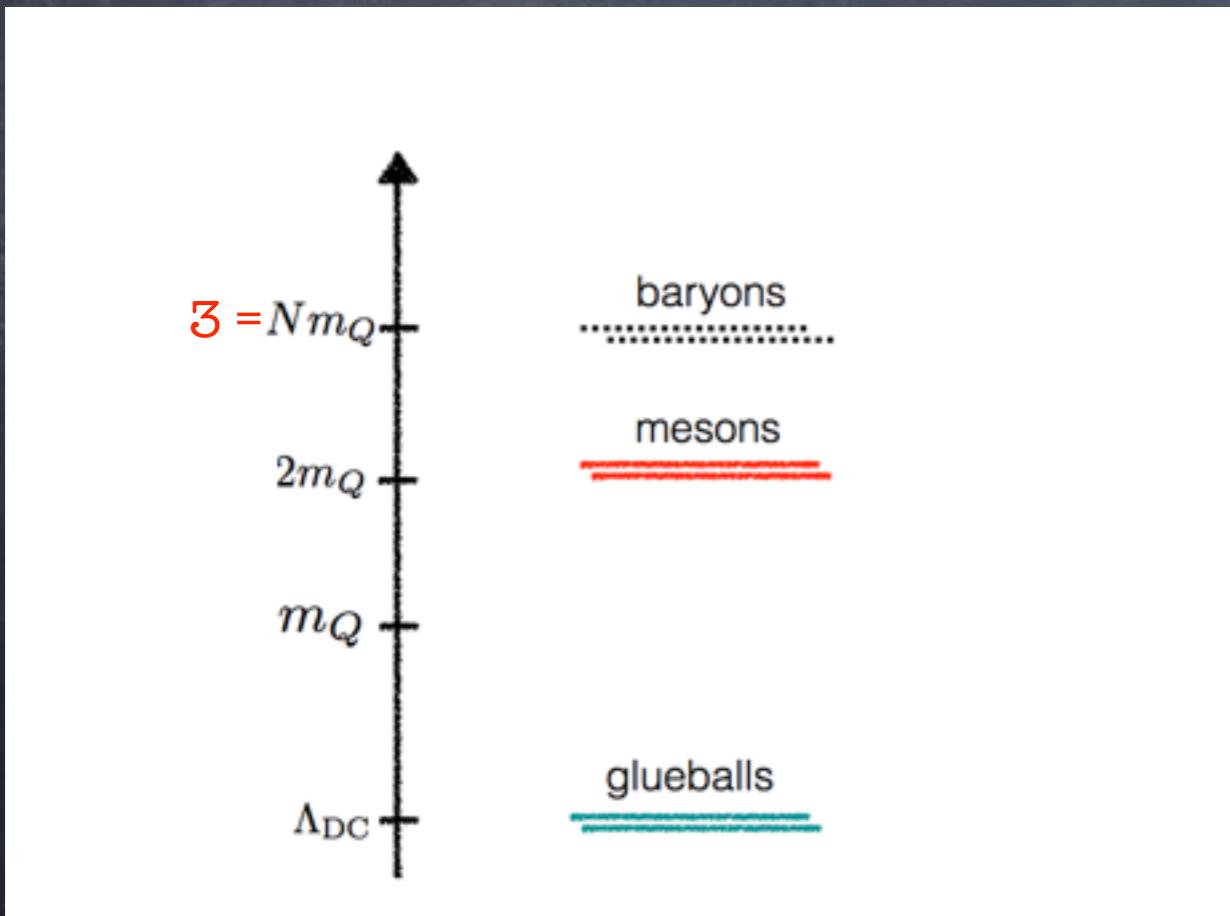
$$a_0 \ll \Lambda_{DC}^{-1}$$

$$\Lambda_{DC} \sim m_Q \exp \left[ -\frac{6\pi}{33 \alpha_{DC}(m_Q)} \right]$$

# Composite WINO

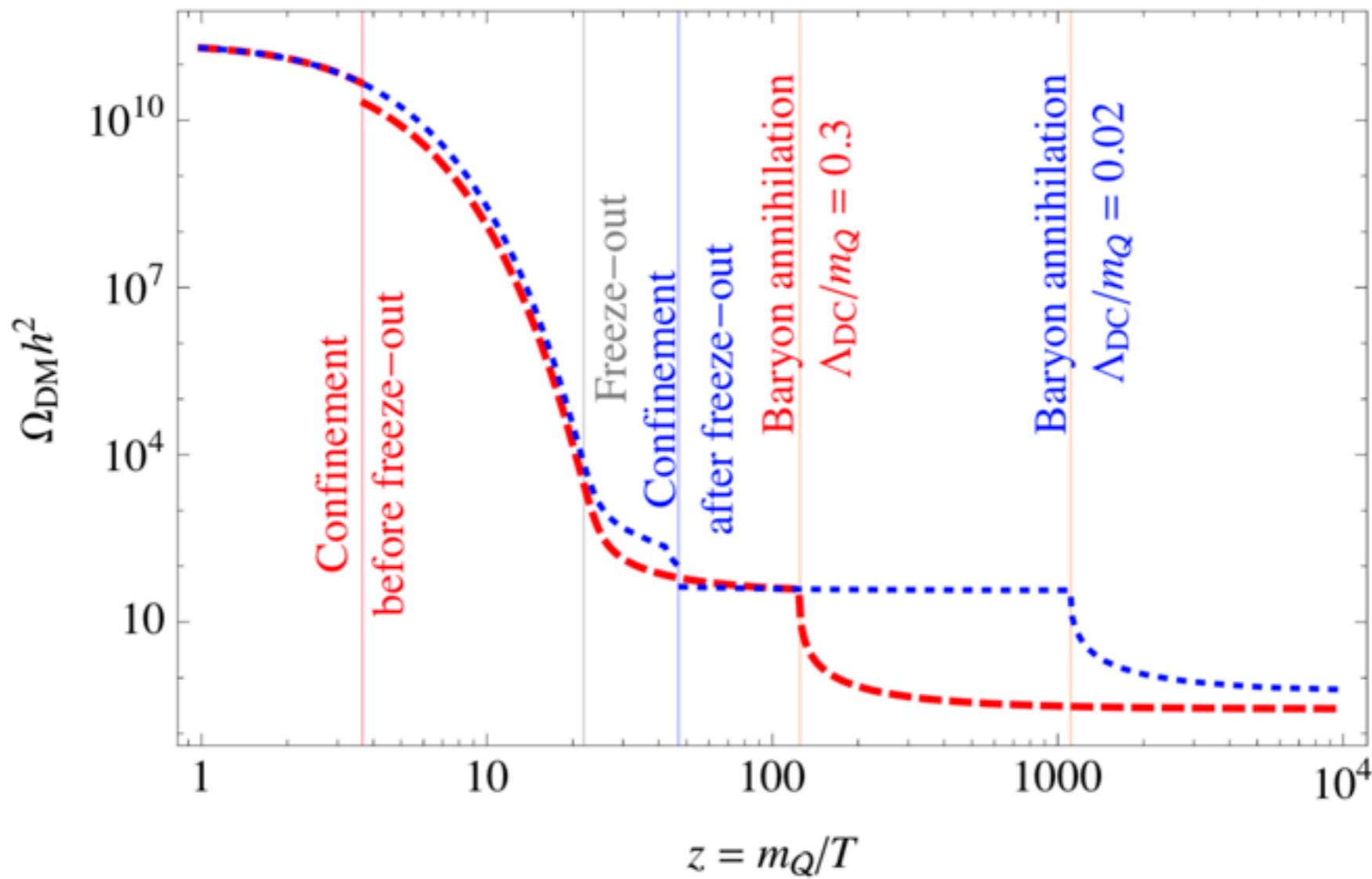
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# Freeze-out and Confinement



# Geometrical Confinement

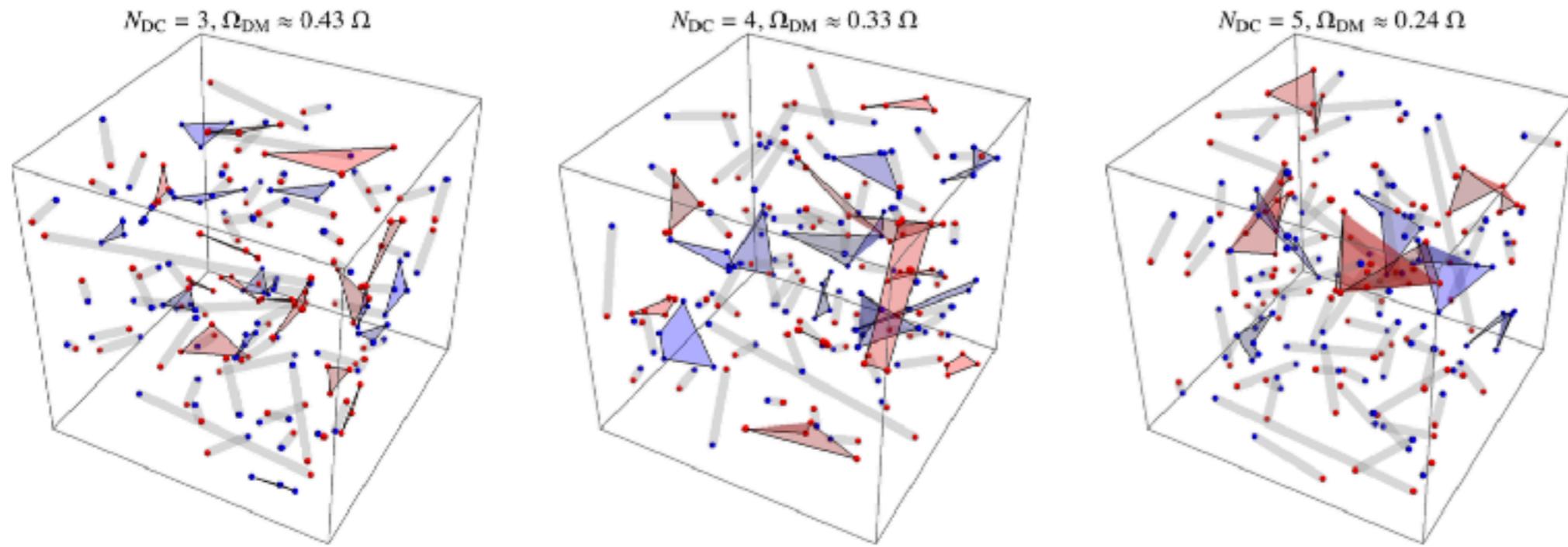
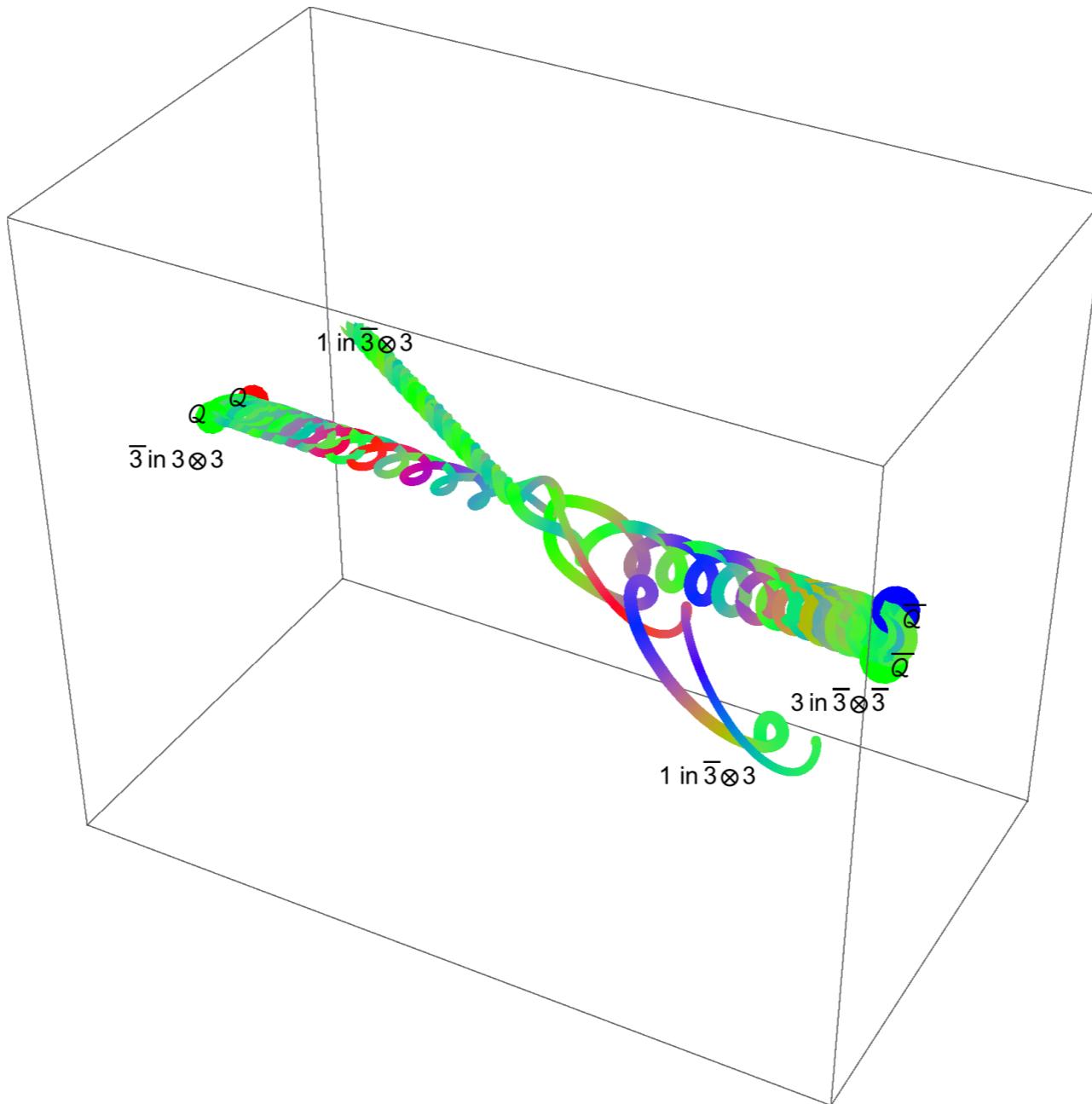


Figure 5: Examples of dark condensation for  $N_{DC} = 3$  (left), 4 (middle) and 5 (right). Dark quarks  $Q$  (anti-quarks  $\bar{Q}$ ) are denoted as red (blue) dots, placed at random positions. We assume that each DM particle combines with its dark nearest neighbour, forming either unstable  $Q\bar{Q}$  dark mesons (gray lines) or stable  $Q^{N_{DC}}$  dark baryons (red regions) and  $\bar{Q}^{N_{DC}}$  dark anti-baryons (blue regions).

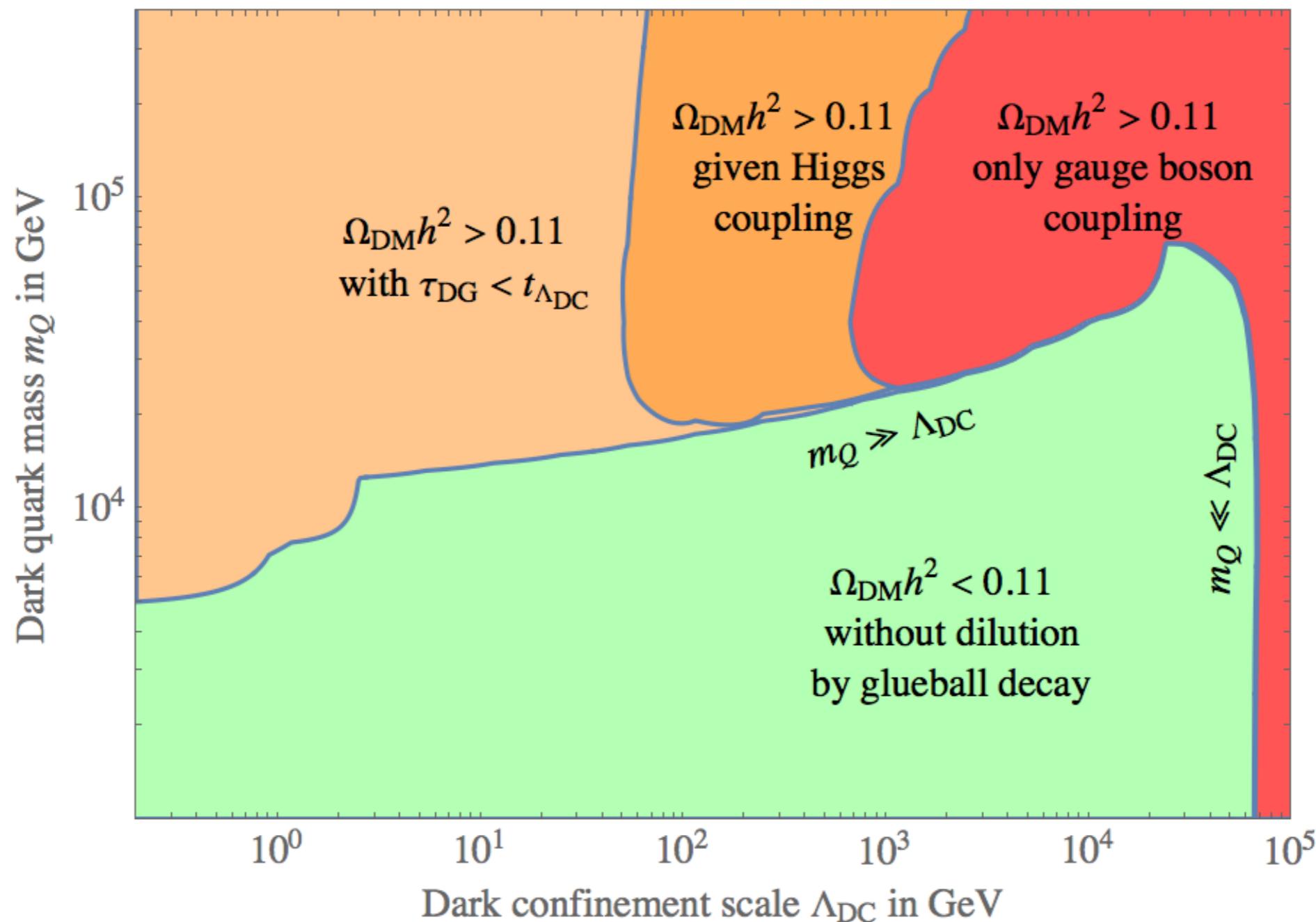
# Rearrangement annihilation

Meson  
toy  
model

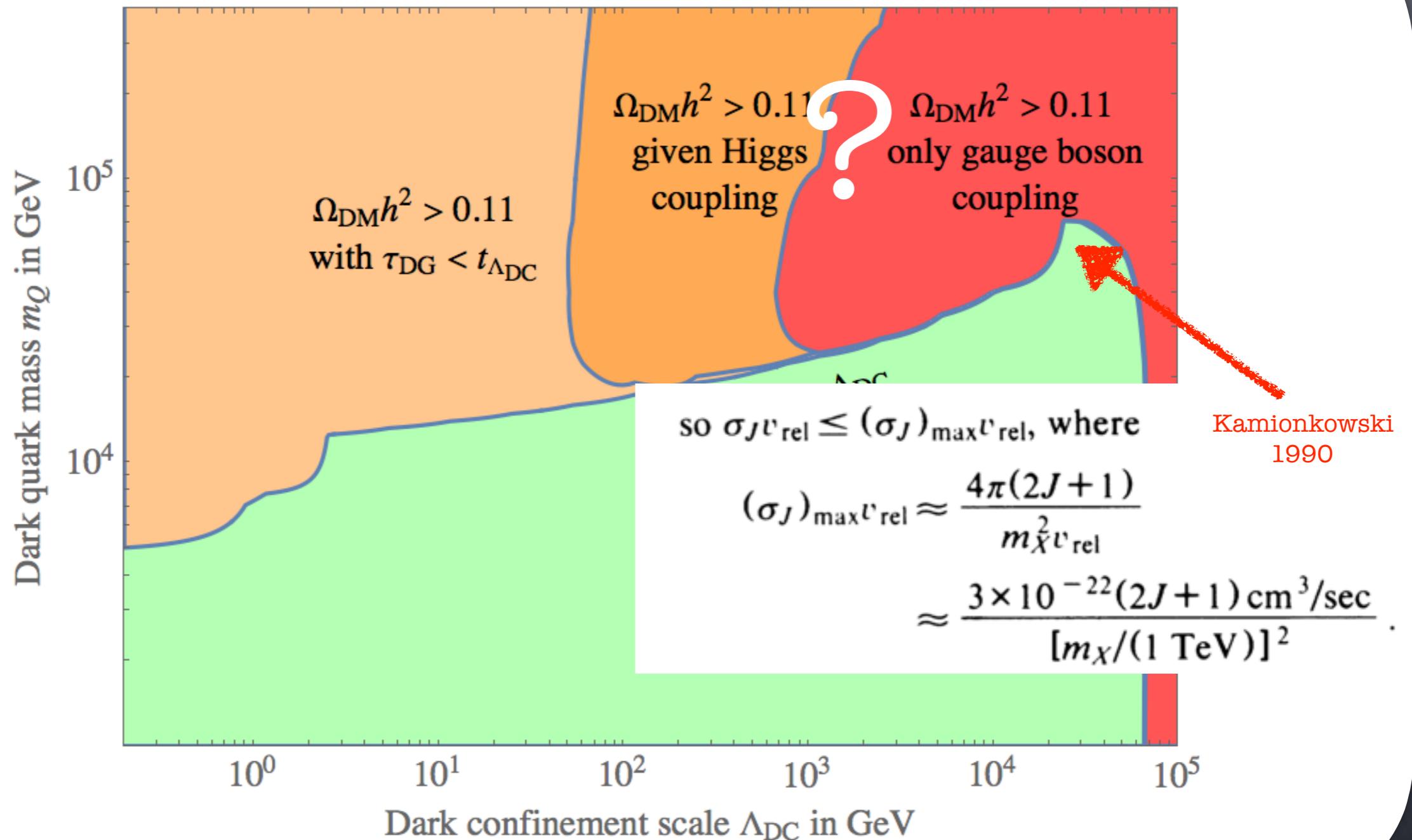


$$\sigma_{\text{ann}} v_{\text{rel}} \sim \frac{\pi a^2 v_{\text{rel}} / 2}{\sqrt{E_{\text{kin}} / E_B}} = \frac{\sqrt{2} \pi}{3 M_Q^2 \alpha_3} = 1.5 \cdot 10^{-24} \frac{\text{cm}^3}{\text{sec}} \times \left( \frac{20 \text{ TeV}}{M_{\text{DM}}} \right)^2 \left( \frac{0.1}{\alpha_3} \right).$$

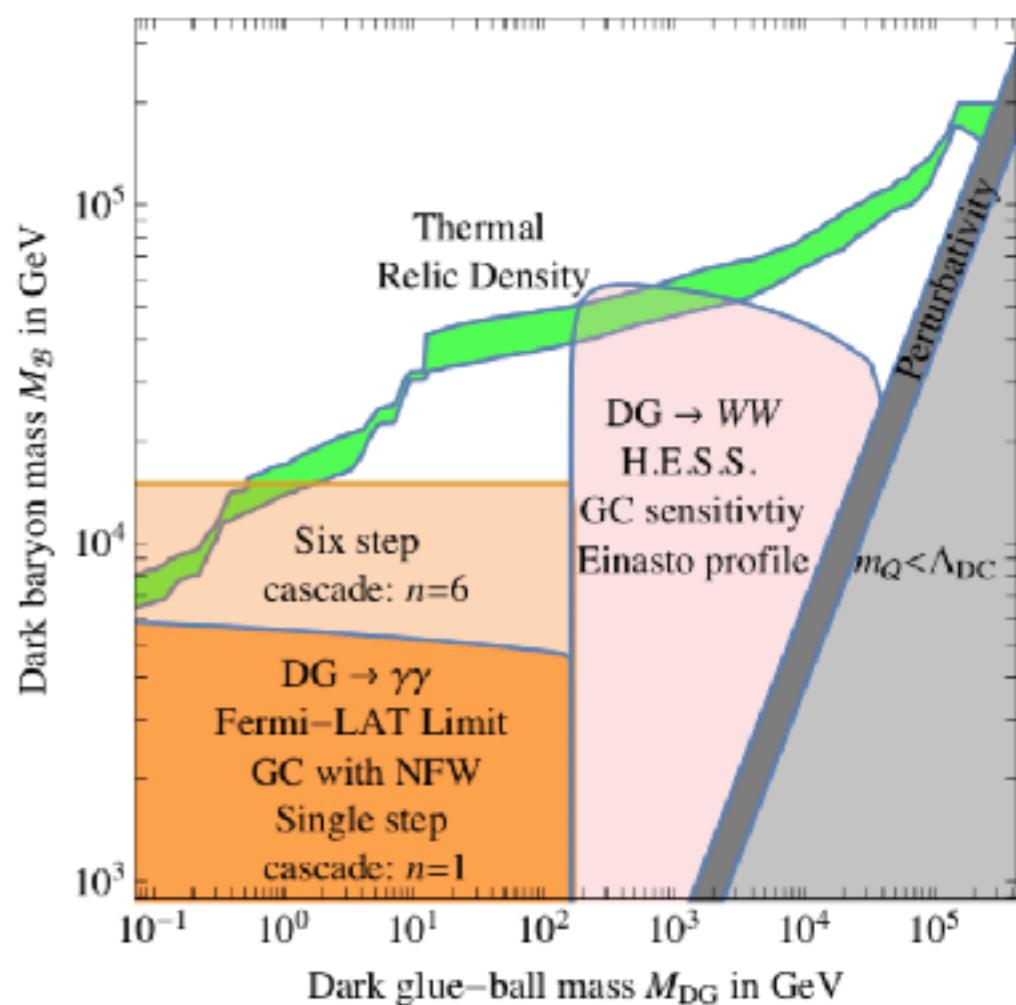
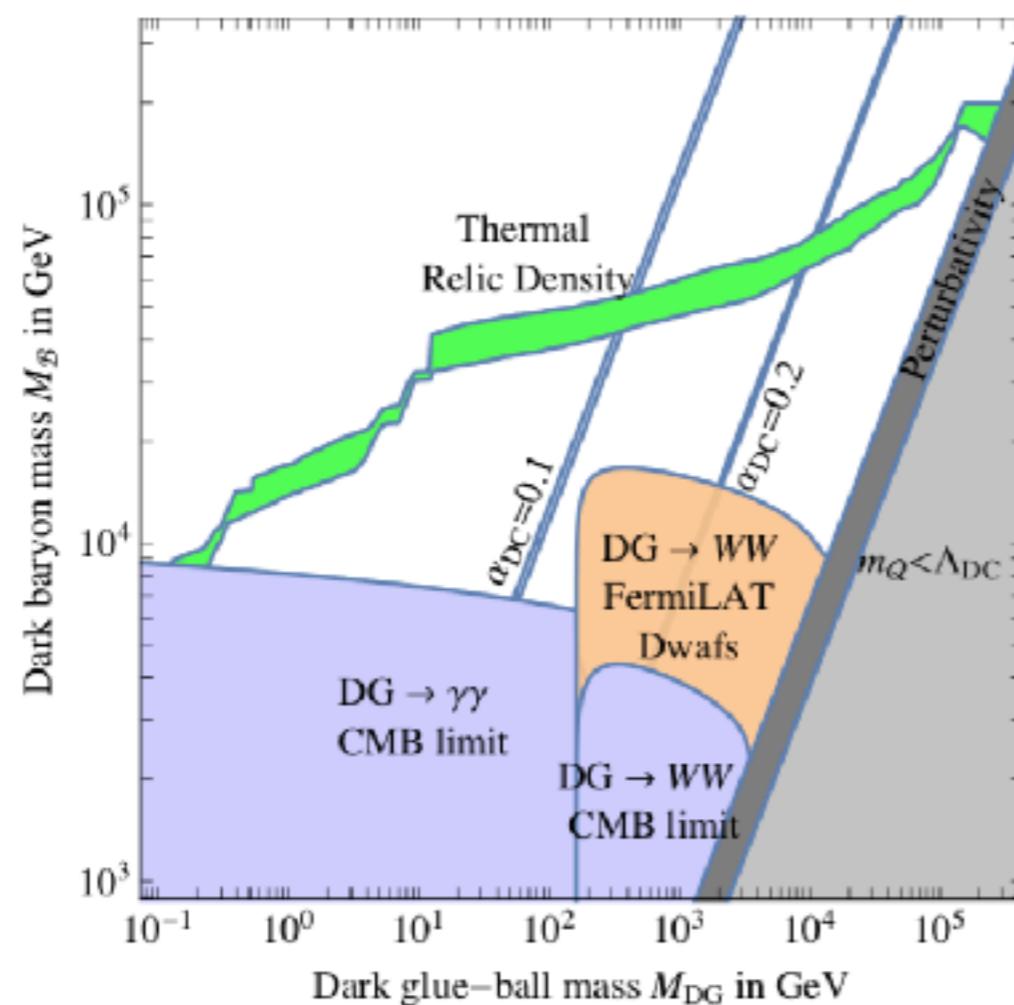
# The full thermal mass range



# The full thermal mass range



# Indirect Detection

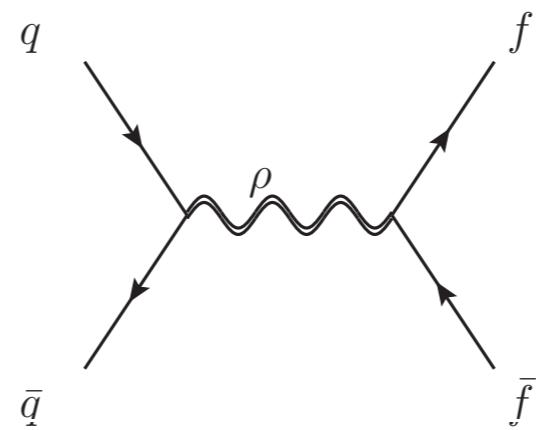


# LHC signals

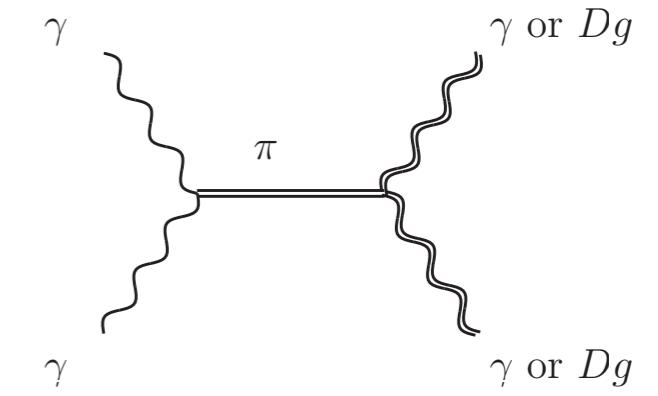
Direct production  
of a resonance

$$\Gamma(\rho \rightarrow f\bar{f}) = N_{DC} \frac{\alpha_{DC}^2}{12} \frac{|R_{n0}(0)|^2}{m_Q^2} T_2$$

$$\propto \alpha_{DC}^3$$



spin-1

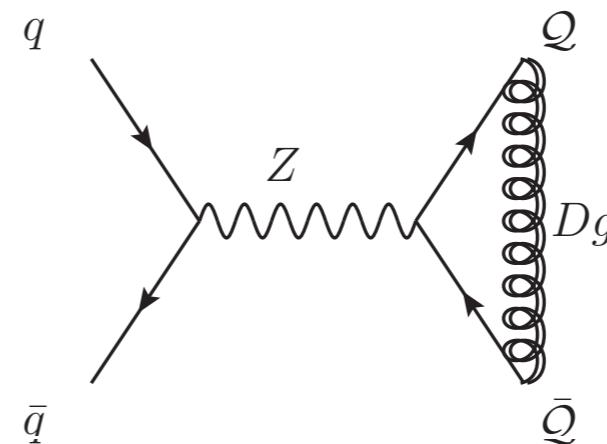


spin-0

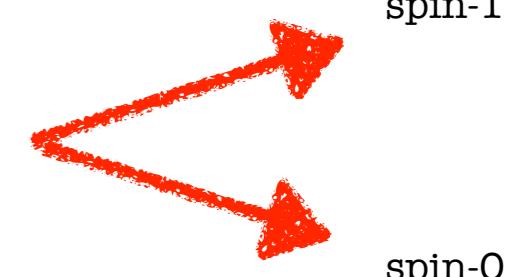
Drell-Yan production

$$\Gamma(\rho \rightarrow \text{Inv.}) \propto \alpha_{DC}^6$$

$$\Gamma(\pi \rightarrow \text{Inv.}) \propto \alpha_{DC}^5$$

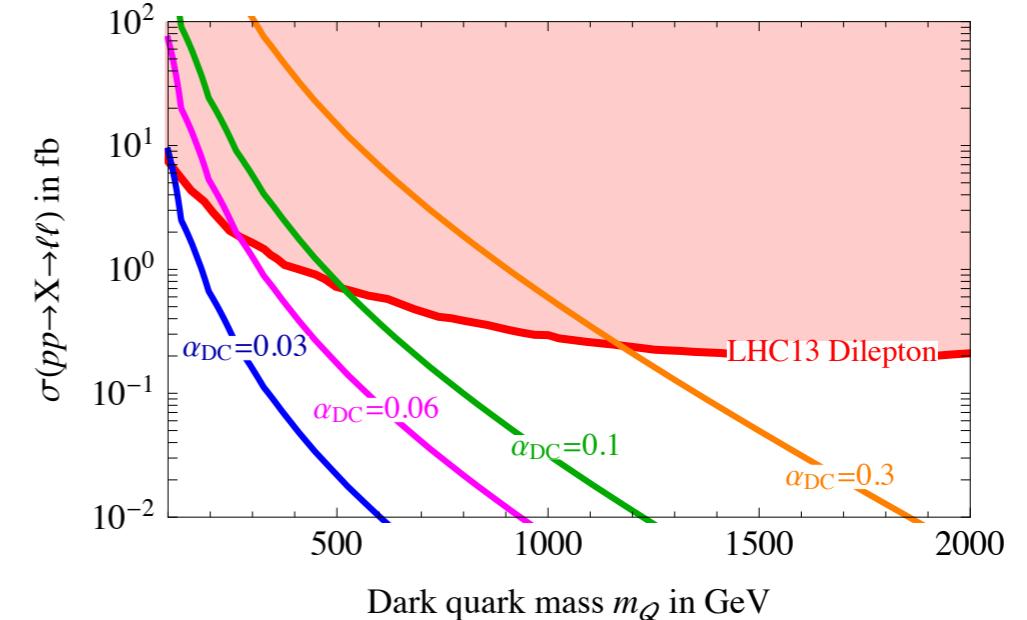
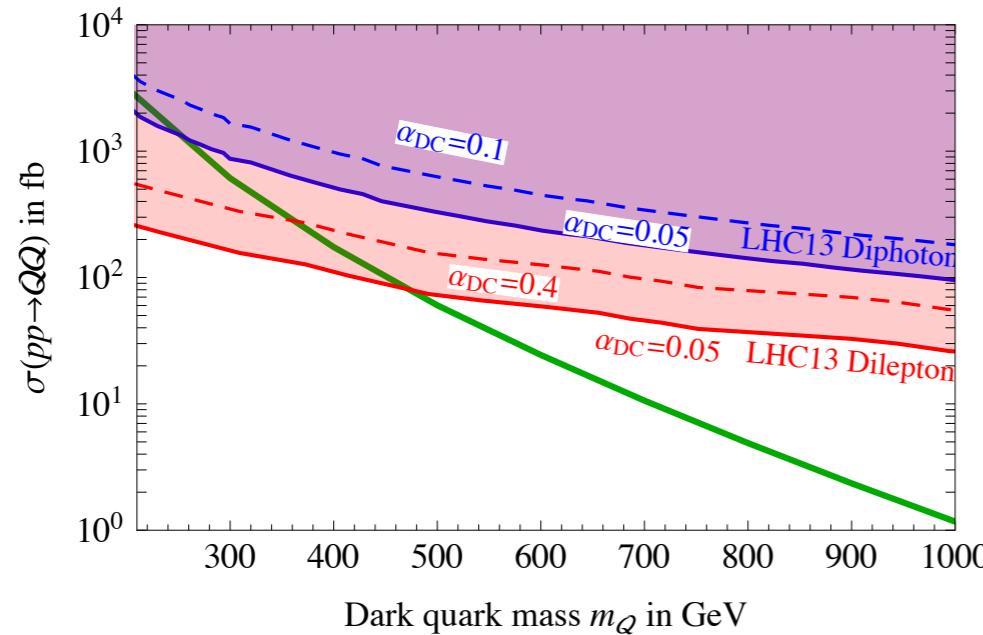


spin-1

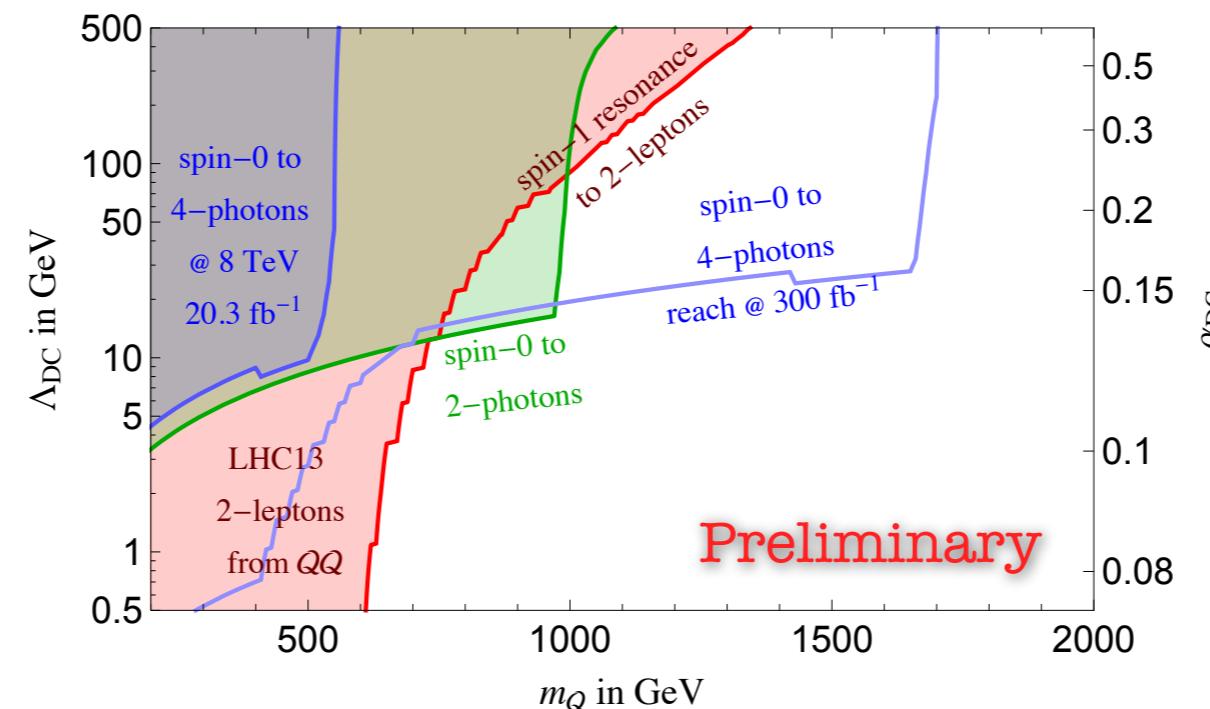


spin-0

# LHC limits

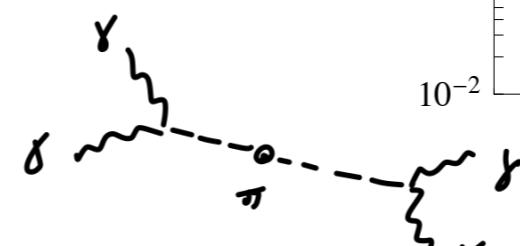
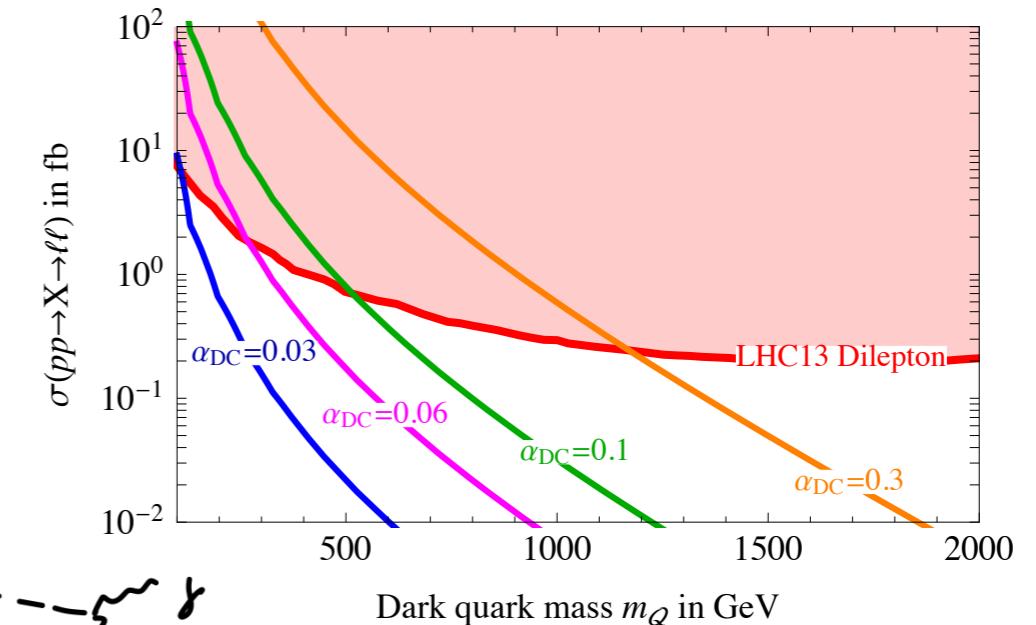
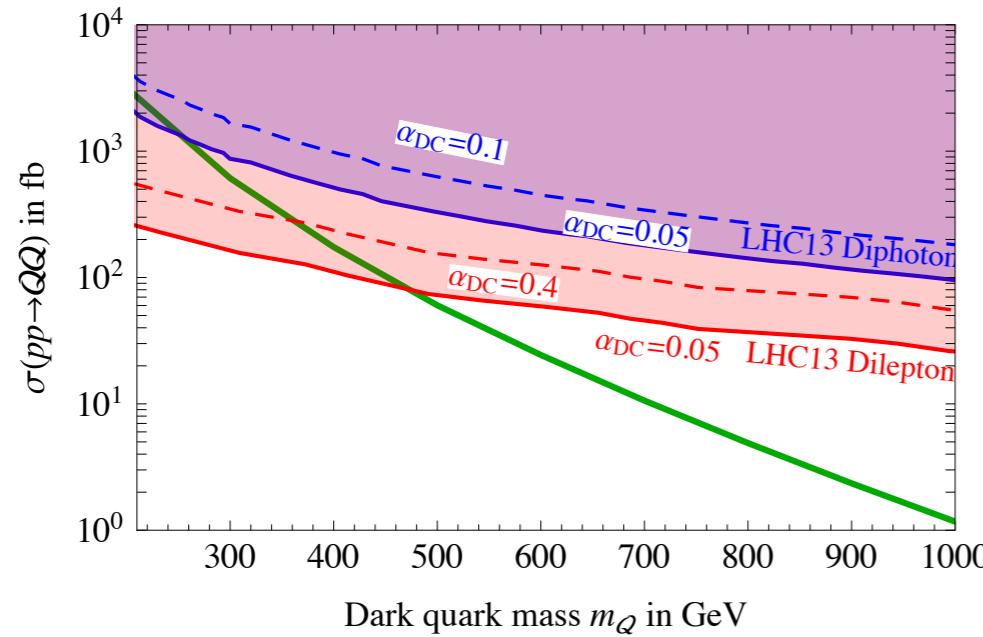


Compare to DD Limit  
on  $M_B = 3$   $m_Q = 780$  GeV  
thus:  $m_Q > 260$  GeV

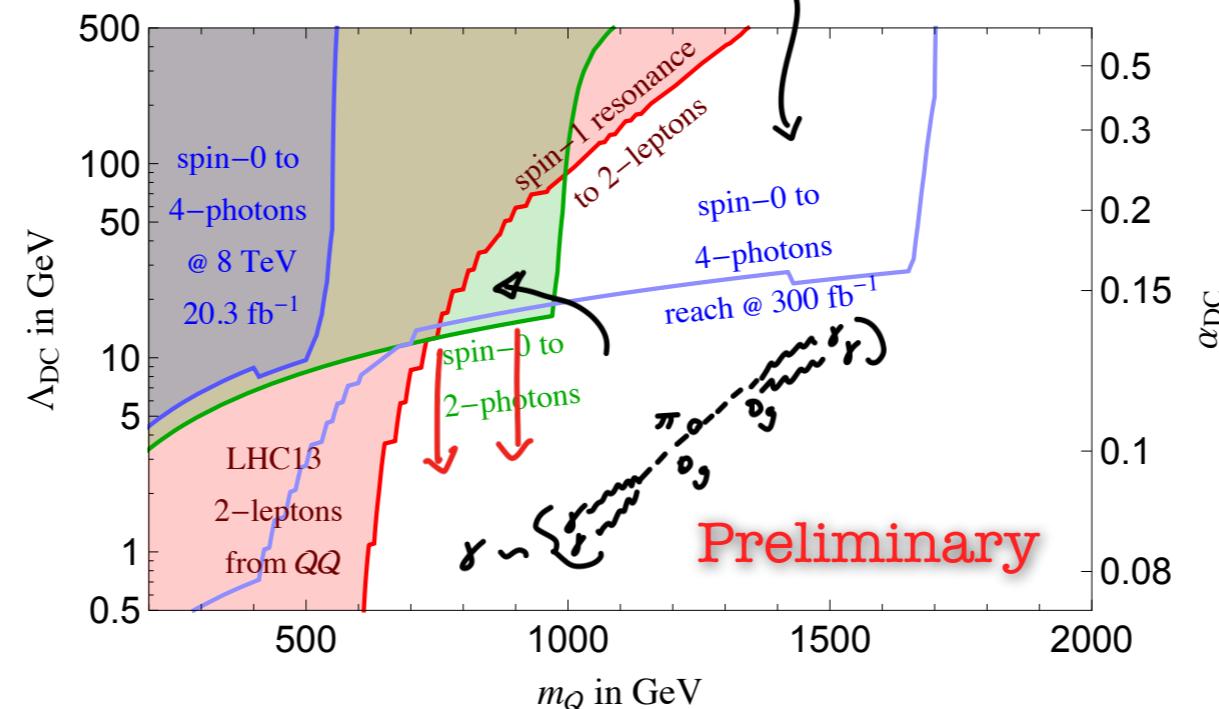


Thus  
 $M_B > 3$  TeV

# LHC limits

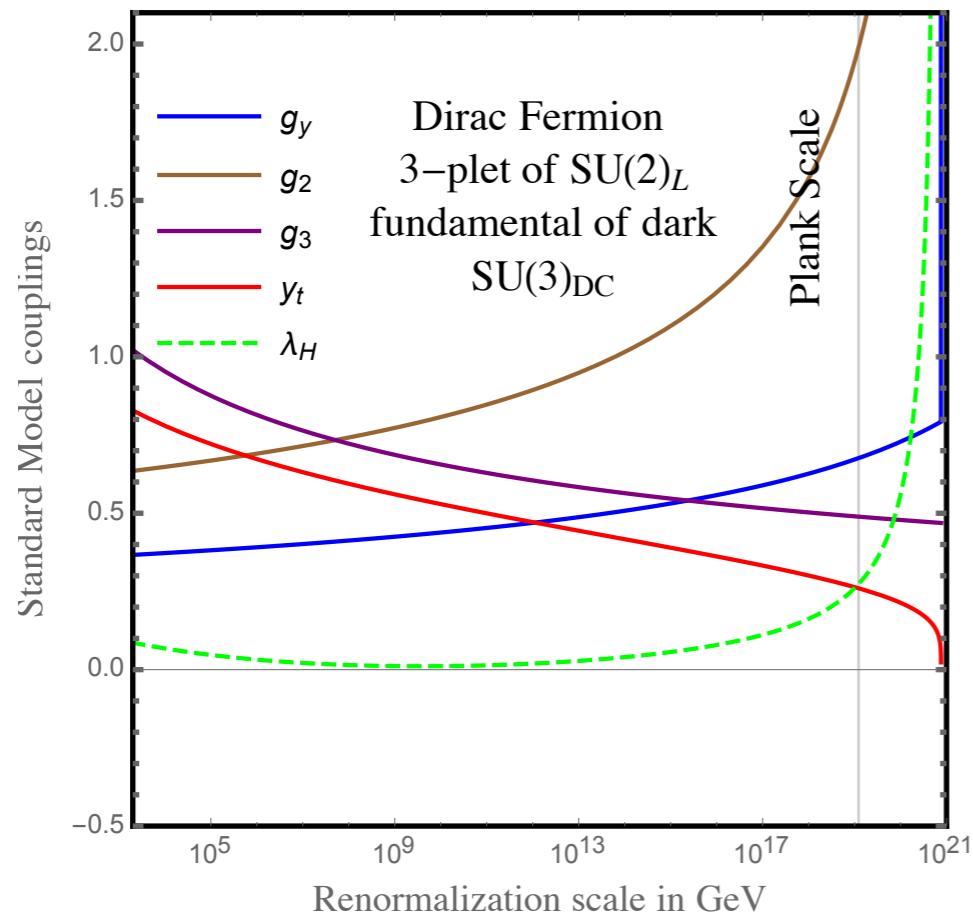


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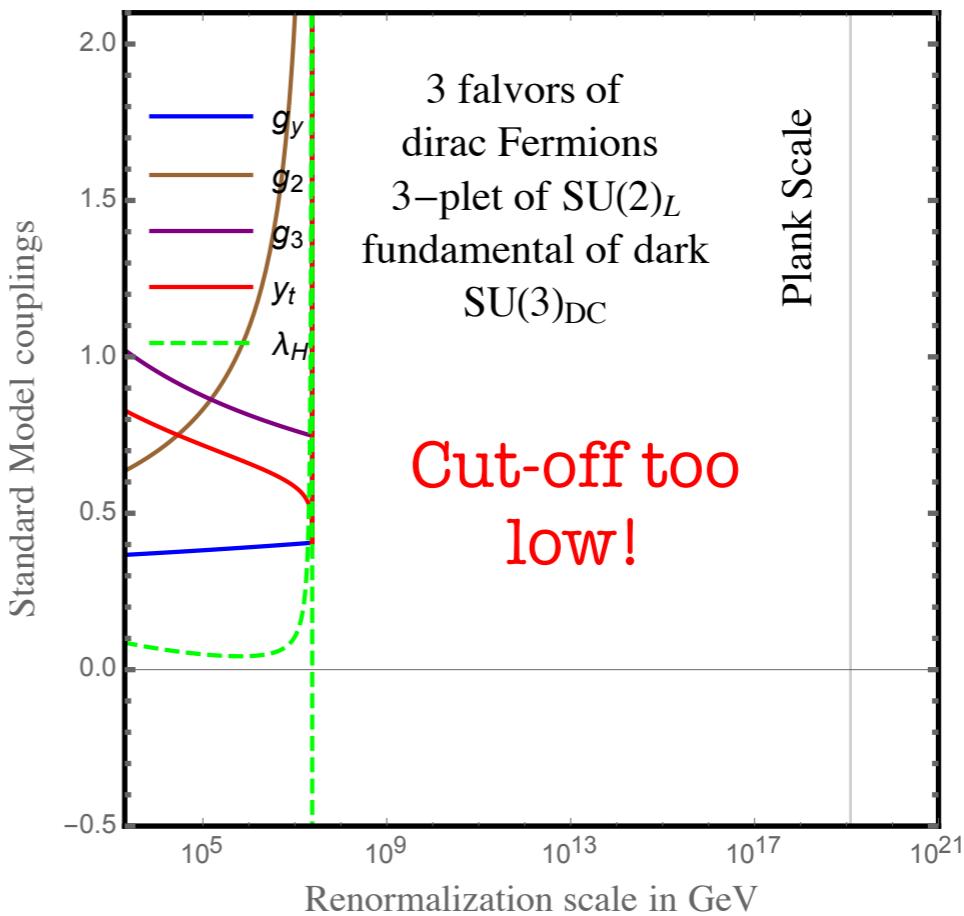
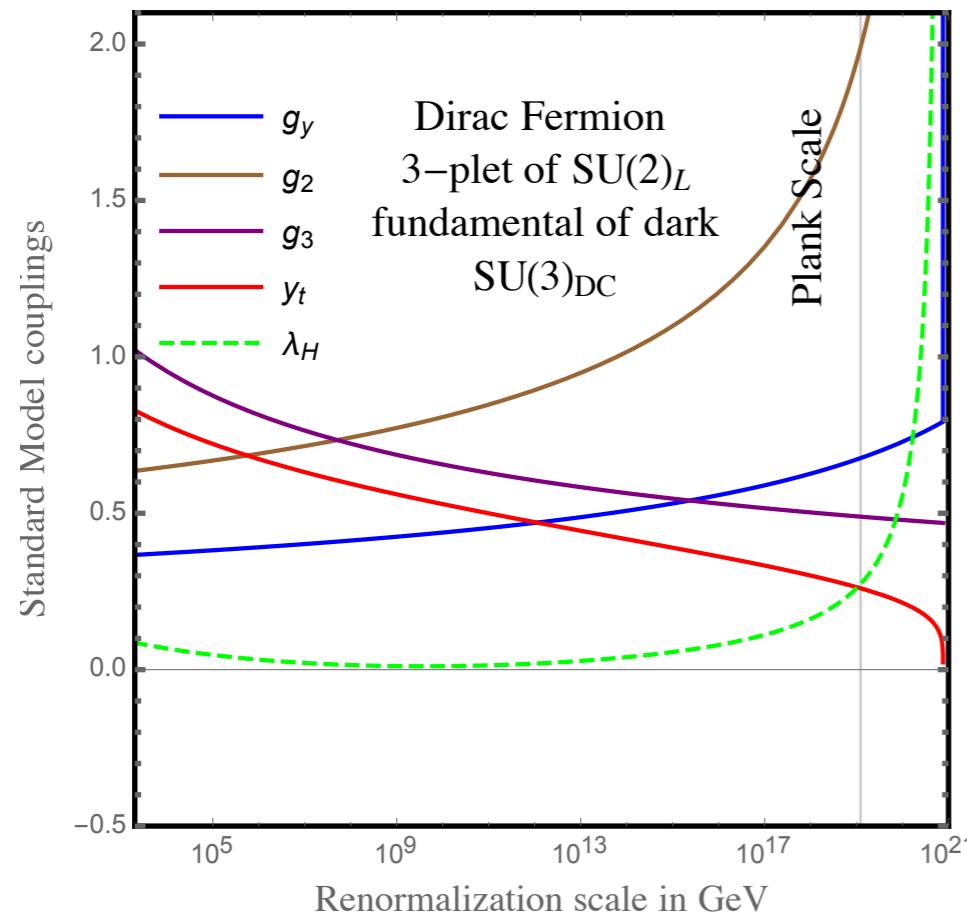


Thus  
 $M_B > 3$  TeV

# RG (in-)stability



# RG (in-)stability



# Better safe than sorry

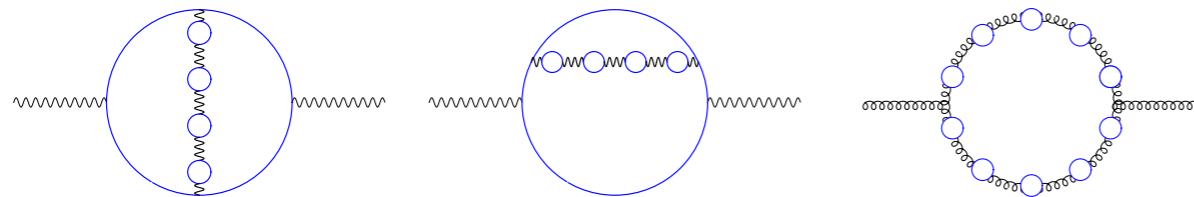
Leading diagrams in  $1/N_f$

1708.00437

G.M. Pelaggi, A.D. Plascencia, A. Salvio, F. Sannino, J.S., A. Struma

# Better safe than sorry

Leading diagrams in  $1/N_f$

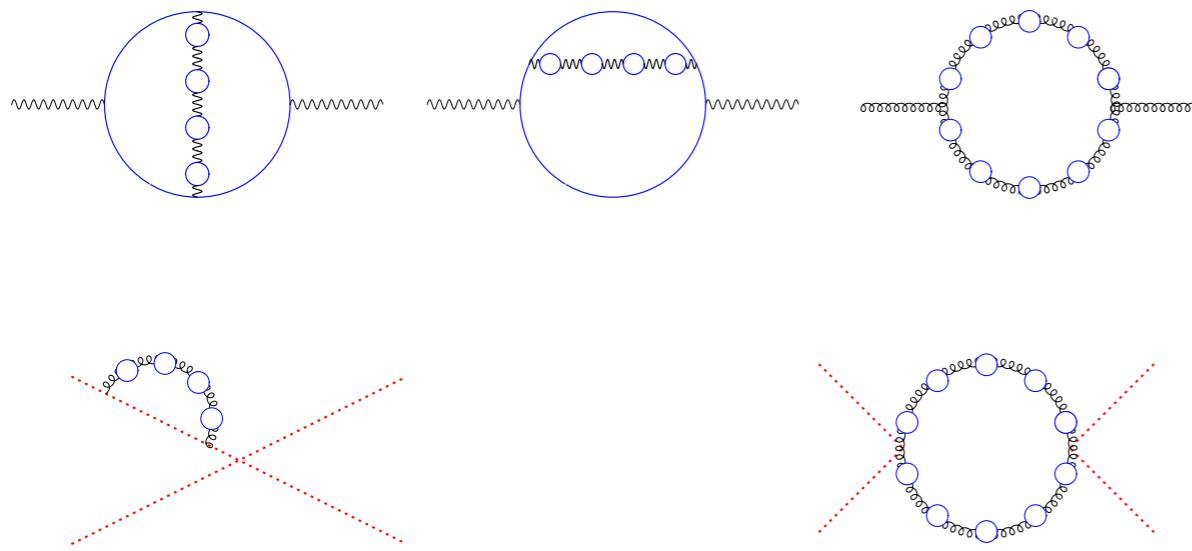


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Leading diagrams in  $1/N_f$

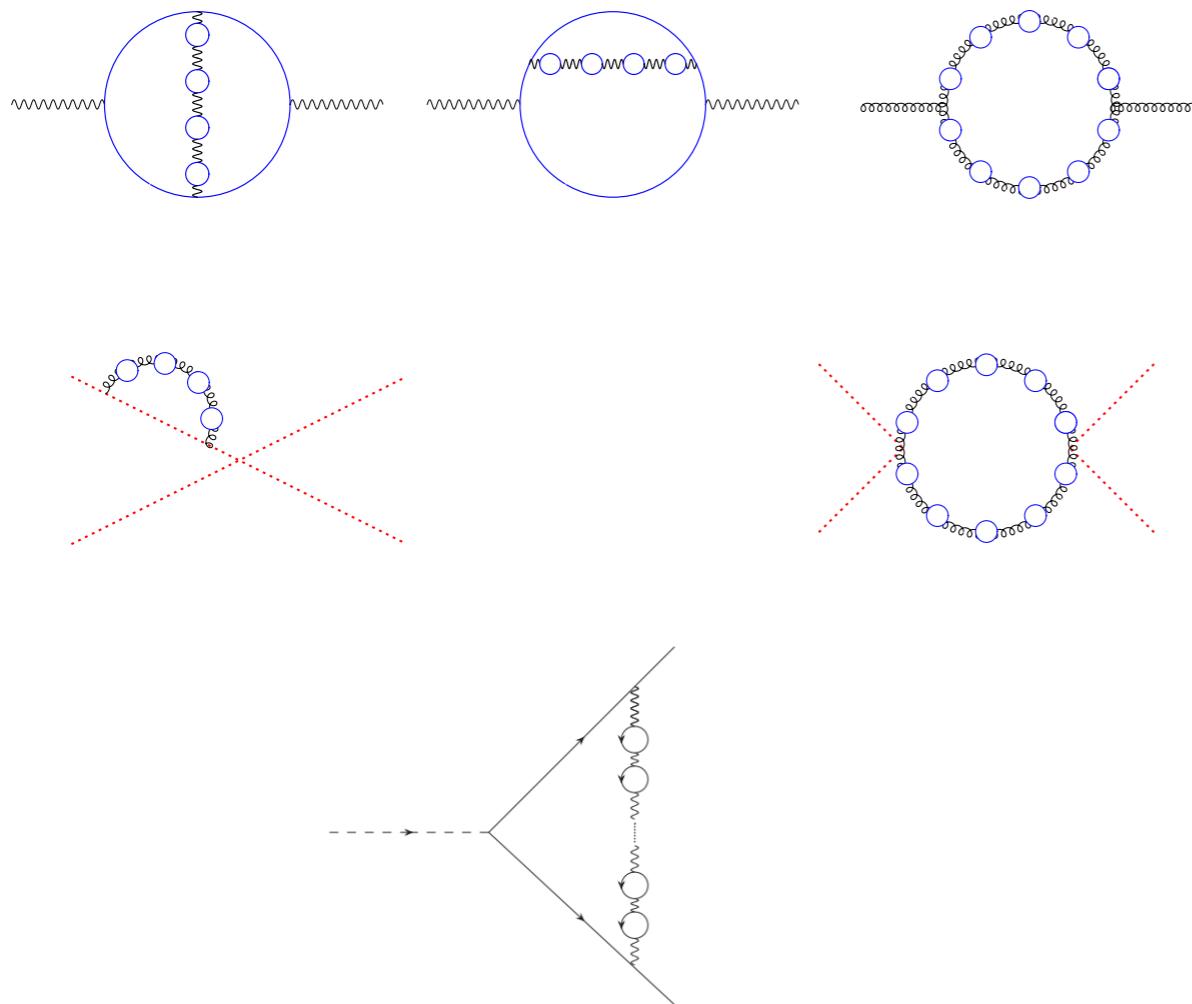


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# Better safe than sorry

Leading diagrams in  $1/N_f$

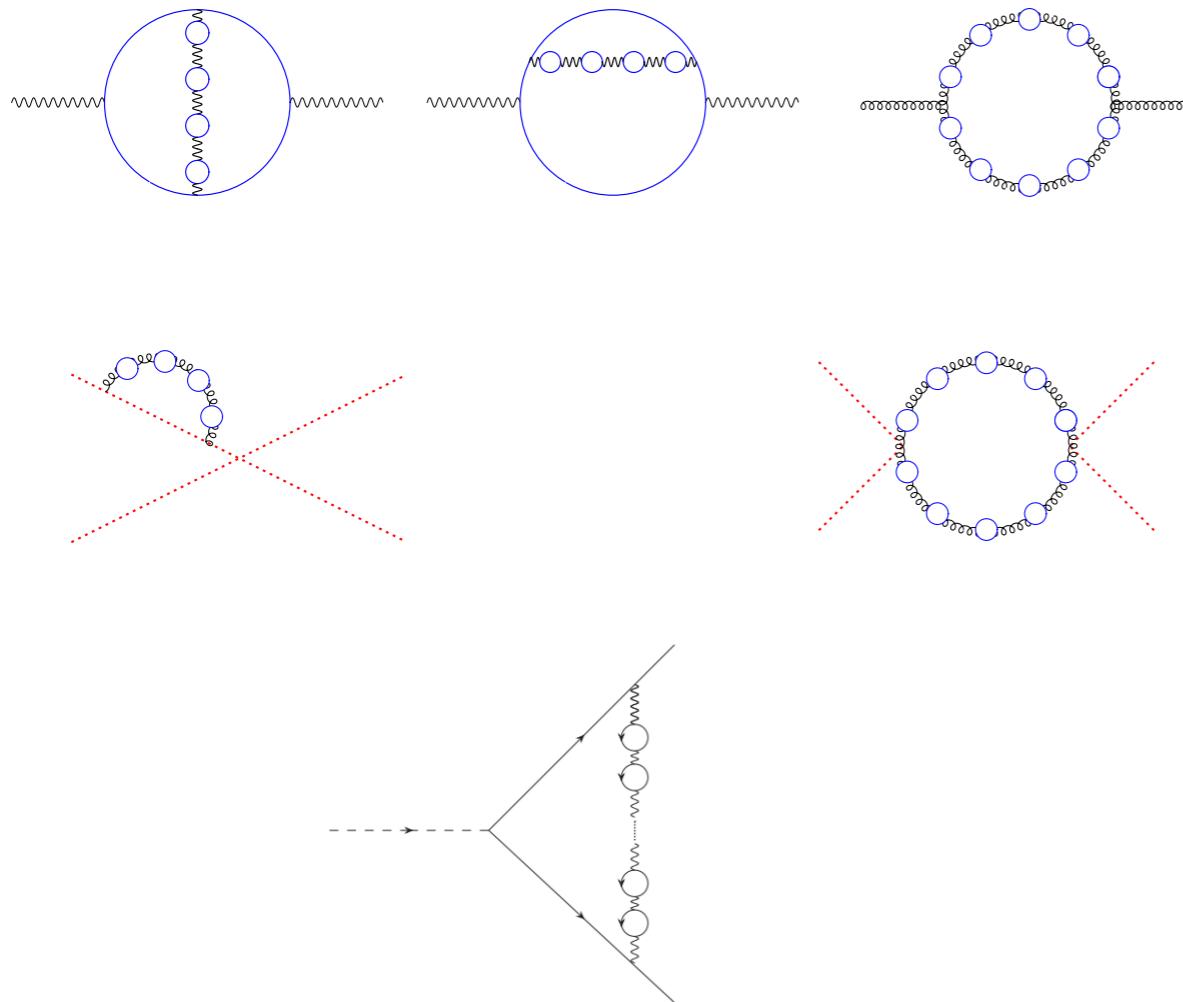


1708.00437

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# Better safe than sorry

Leading diagrams in  $1/N_f$



$$\begin{aligned} (4\pi)^2 \frac{dy_t}{d\ln \mu} &= \frac{9}{2} y_t^3 - y_t \left( 8g_3^2 + \frac{9}{4} g_2^2 R_y(A_2) + \frac{17}{12} g_Y^2 \right) \\ (4\pi)^2 \frac{d\lambda_H}{d\ln \mu} &= 24\lambda_H^2 + \lambda_H (12y_t^2 - 9g_2^2 R_\lambda(A_2) - 3g_Y^2) + \\ &\quad + \frac{9g_2^4}{8} R_g(A_2) + \frac{3g_Y^4}{8} + \frac{3g_2^2 g_Y^2}{4} R_g(A_2, 0) - 6y_t^4. \end{aligned}$$

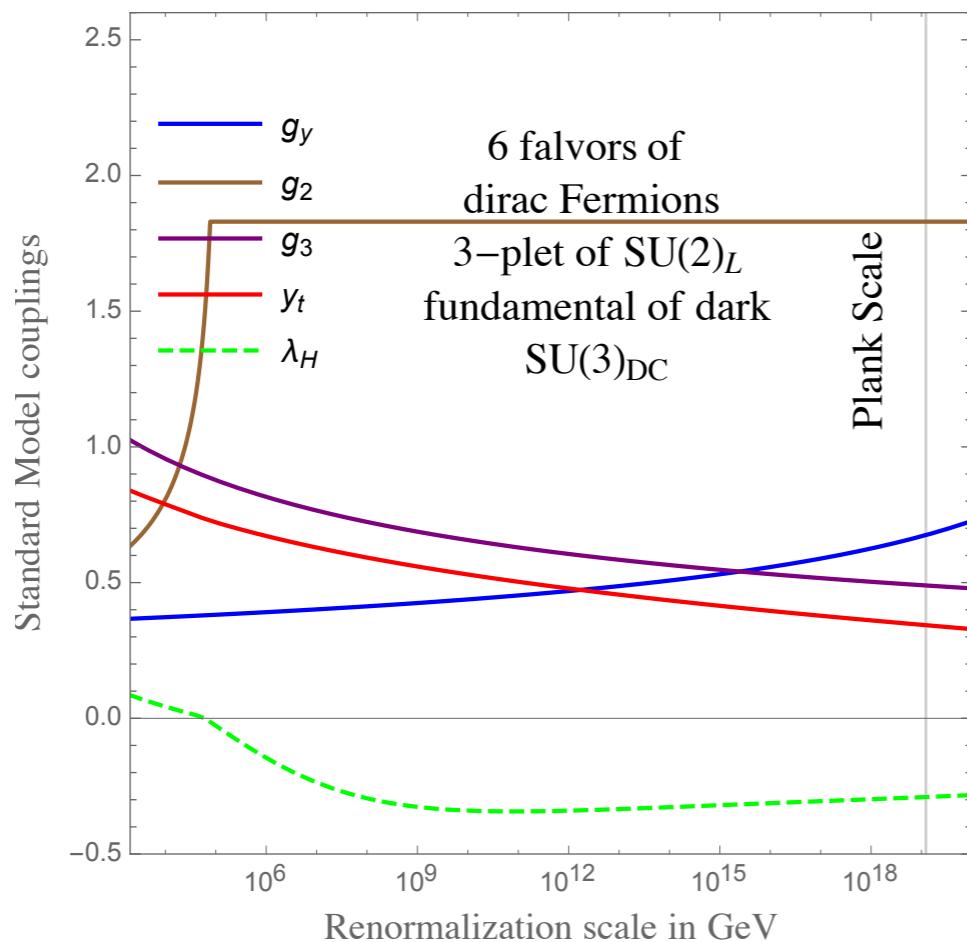
$$\begin{aligned} R_g(A, A) &= \frac{[(2A-3)A(H_A - 3H_{1-A} + 2H_{3-2A}) - 4A + 3]\Gamma(4-2A)}{18\Gamma(2-A)^3\Gamma(A+1)}, \\ R_g(A, 0) &= \frac{(3-2A)\Gamma(4-2A)}{18\Gamma(2-A)^3\Gamma(A+1)}, \\ R_\lambda(A) &= \frac{2(3-2A)\Gamma(4-2A)}{9A(4-2A)\Gamma(2-A)^3\Gamma(A)}. \end{aligned}$$

$$R_y(A) = \frac{(3-2A)^2(2-A)\sin(\pi A)\Gamma(2-2A)}{9\pi A\Gamma(3-A)^2} \left( 2 + A \frac{C_H}{C_{\psi_1} + C_{\psi_2}} \right)$$

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# Better safe than sorry



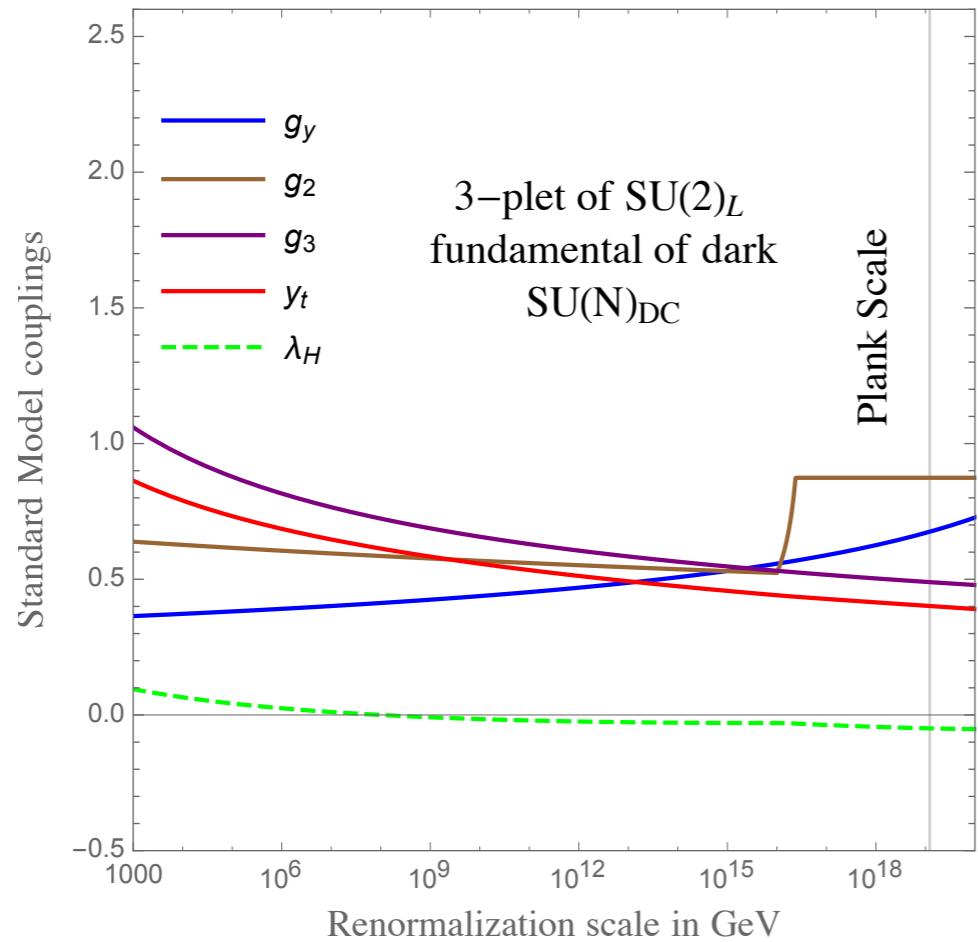
$$g_2^* \approx \frac{4\pi\sqrt{3}}{2\sqrt{I(R)N_f D_{R'}}$$

$$N_f \propto N_{DC}$$

for  $N_{DC} = 3$

$N_f < 60$

# Un-natural Dark Matter



for  $N_{DC} = 80$   
and  $M_{DM} = 10^{16}$  GeV

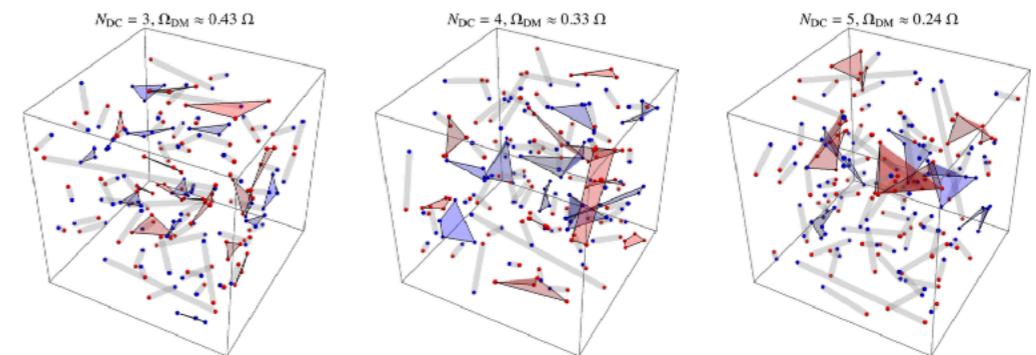


Figure 5: Examples of dark condensation for  $N_{DC} = 3$  (left), 4 (middle) and 5 (right). Dark quarks  $Q$  (anti-quarks  $\bar{Q}$ ) are denoted as red (blue) dots, placed at random positions. We assume that each DM particle combines with its dark nearest neighbour, forming either unstable  $Q\bar{Q}$  dark mesons (gray lines) or stable  $Q^{N_{DC}}$  dark baryons (red regions) and  $\bar{Q}^{N_{DC}}$  dark anti-baryons (blue regions).

$$\wp_B \approx \frac{1}{1 + 2^{N_{DC}-1}/N_{DC}}.$$

# Summary II

- Stable Dark Matter bound states may be related to new symmetries
- Opens up the parameter space for the WINO for example
- The full range possible, up to Unitarity bound
- Violation of unitarity bound?
- Beyond the minimal model, we need to be safe

Details in: JHEP 1710 (2017) 210  
[arXiv:1707.05380](#)

# Thank you!