

Gravitational Waves: where do they come from and what do they tell us


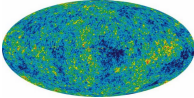
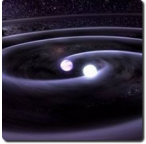
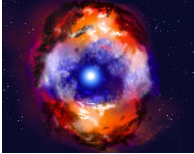
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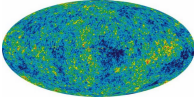
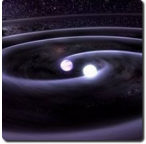
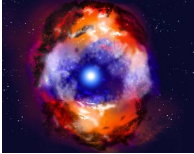
- Gravitational wave sources
- Gravitational wave data analysis
- Observed gravitational waves signals

Part 1: gravitational wave sources

4 families of potential GW signal morphologies

	precisely modeled	uncertain form
permanent	<p>Deformed rotating neutron stars</p> 	<p>Incoherent sum of unresolved sources Primordial GW background</p> 
transient	<p>Cosmic strings cusps, kinks Coalescence of neutron stars or black holes</p> 	<p>Star quakes, Non spherically symmetric stellar collapse, ...</p> 

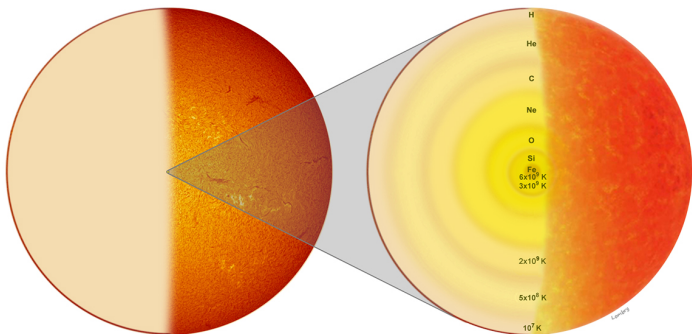
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Compact binary coalescence

- Only source detected so far
- Black hole - black hole (BH-BH) binary
- BH - Neutron star (NS)
- NS - NS
- duration \sim min, frequency \sim 10 Hz - 1 kHz, amplitude $h \sim 10^{-23}$ at 10 Mpc

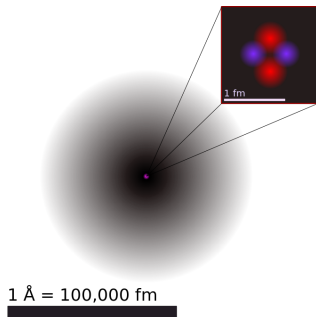
Compact stars



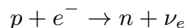
● Origin of compacts:

- ▶ Pressure from nuclear reaction preventing gravitational collapse
- ▶ For stellar masses greater than $10M_{\odot}$ no reaction in iron core
- ⇒ core supported by electron degeneracy
- ▶ ~ 1000 km iron core collapses ⇒ supernova
- ▶ Depending on amount of matter falling back on collapsed core
 - Neutron star, $1-3 M_{\odot}$
 - Black hole, $5-50 M_{\odot}$
- ▶ Neutron star, black hole size ~ 10 km in radius ⇒ compact
- ▶ Stellar graveyard

Neutron star

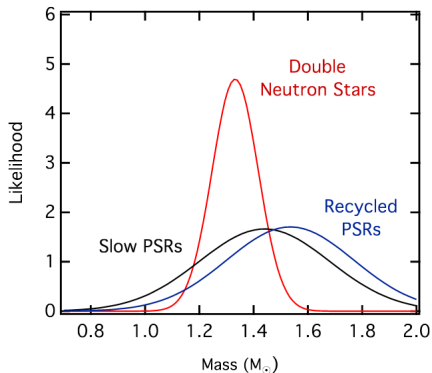
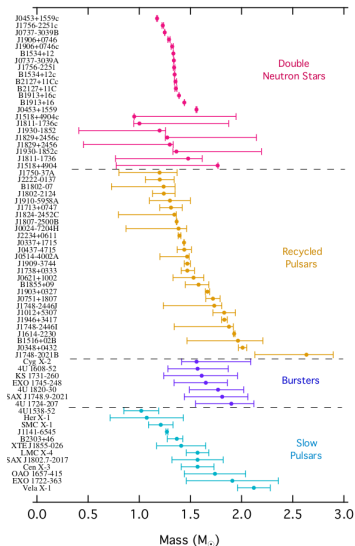


- Atoms composed of three ingredients
 - ▶ neutron
 - ▶ proton
 - ▶ electrons
- Electron capture during core collapse



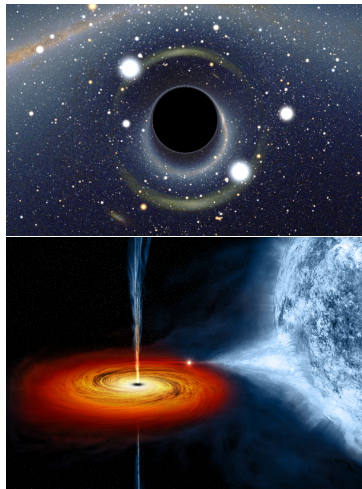
- neutron star \sim 10 km ball with nuclear density
- pulsar: special case of neutron stars with large magnetic fields and radio emission pulsing with rotation

Neutron star



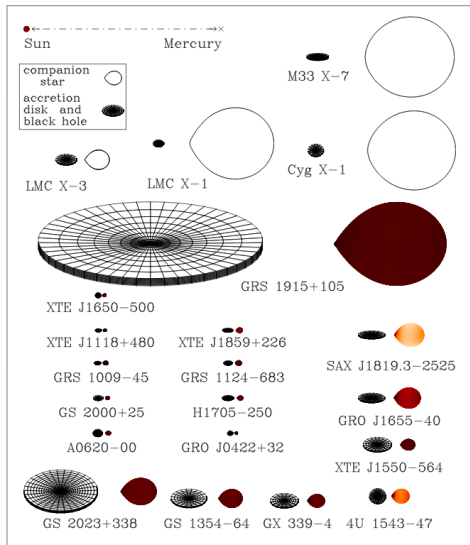
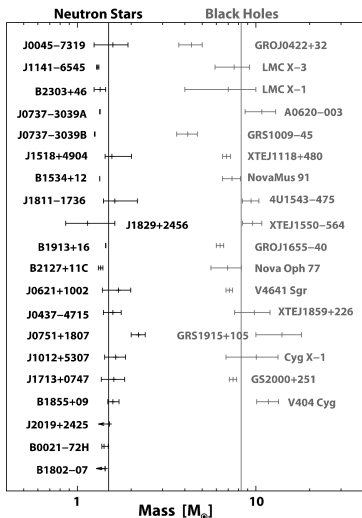
- Neutron stars (pulsars) in binary system
- Masses measured from orbital parameters
- For double neutron stars mass distribution much more narrow
 ⇒ Particular evolution conditions needed to form double neutron stars?

Black holes



- Gravitation strong enough that photons can't escape
 - ⇒ Black hole horizon
- What happens inside the black hole horizon is not known but no influence on outside universe
- Geometrical objects defined by two quantities
 - ▶ Mass (scalar)
 - ▶ Spin (vector)
- Black holes were observed from X-ray emission of gas falling into the black hole

Black holes



• mass gap?

• BH mass measured from orbital parameters

Binary system: GW generation

- Binary system of two compact objects

- ▶ Masses m_1 and m_2
- ▶ Distance between objects a
- ▶ Total mass $M = m_1 + m_2$
- ▶ Reduced mass $\mu = \frac{m_1 m_2}{M}$

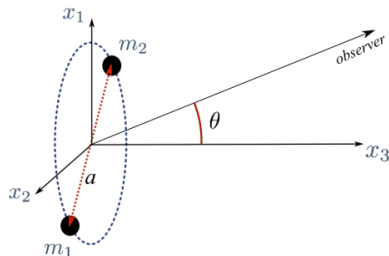
- Newtonian approximation

- ▶ 3rd Kepler's law $\omega = \sqrt{\frac{GM}{a^3}}$

- Assume circular orbit and observer at large distance $R \gg a$

- Point object coordinates

$$x_1(t) = \frac{a}{2} \cos \omega t, \quad x_2(t) = \frac{a}{2} \sin \omega t, \quad x_3(t) = 0$$



Gravitational source quadrupolar approximation

Approximation: far field + slow moving source

- Mass distribution quadrupolar moment

$$\begin{aligned} I_{ij} &= \int (x_i x_j - \frac{1}{3} \delta_{ij} \delta_{km} x^k x^m) \rho(x) d^3x \\ &= \frac{\mu a^2}{2} \begin{pmatrix} (\frac{1}{3} + \cos(2\omega t)) & \sin(2\omega t) & 0 \\ \sin(2\omega t) & (\frac{1}{3} - \cos(2\omega t)) & 0 \\ 0 & 0 & 0 \end{pmatrix}. \end{aligned}$$

- Source of gravitational waves

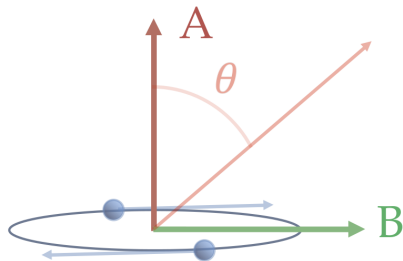
$$G_{\mu\nu} = \frac{8\pi G}{c^4} T_{\mu\nu} \quad \longrightarrow \quad h_{jk}^{TT} = \frac{2G}{Rc^4} \underbrace{P_{jkmn}}_{\text{projection}} \ddot{I}^{mn}(t - \frac{R}{c}),$$

- Resulting waveform

$$\begin{aligned} h_+ &= -\frac{4G}{Rc^4} \mu a^2 \omega^2 \frac{1 + \cos^2 \theta}{2} \cos 2\omega t \\ h_\times &= -\frac{4G}{Rc^4} \mu a^2 \omega^2 \cos \theta \sin 2\omega t, \end{aligned}$$

Binary coalescence: GW generation geometry

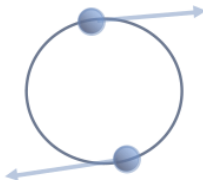
$$h_{jk}^{TT} = \frac{2G}{Rc^4} \underbrace{P_{jkmn}}_{\text{projection}} \ddot{I}^{mn} \left(t - \frac{R}{c} \right),$$



$$h_{+} = -\frac{4G}{Rc^4} \mu a^2 \omega^2 \frac{1 + \cos^2 \theta}{2} \cos 2\omega t$$

$$h_{\times} = -\frac{4G}{Rc^4} \mu a^2 \omega^2 \cos \theta \sin 2\omega t,$$

- Observer A sees two polarizations, $\cos \theta = 1$



- Observer B sees one polarizations, $\cos \theta = 0$



Binary coalescence: GW power

$$h_+ = -\frac{4G}{Rc^4} \mu a^2 \omega^2 \frac{1 + \cos^2 \theta}{2} \cos 2\omega t$$

$$h_\times = -\frac{4G}{Rc^4} \mu a^2 \omega^2 \cos \theta \sin 2\omega t,$$

- Radiated power per unit solid angle

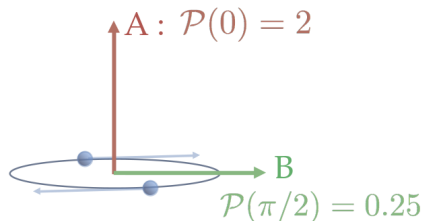
$$\frac{dP}{d\Omega} = \frac{c^3}{16\pi G} \left\langle \left(\dot{h}_+ \right)^2 + \left(\dot{h}_\times \right)^2 \right\rangle = \frac{2G\mu^2 a^4 \omega^6}{\pi c^5} \mathcal{P}(\Omega)$$

$$\mathcal{P}(\Omega) = \frac{1}{4} (1 + 6 \cos^2 \theta + \cos^4 \theta)$$

- Radiated power non-zero in all directions

- Total radiated power

$$P_{\text{GW}} = \frac{32G\mu^2 a^4 \omega^6}{5c^5}$$



GW power: some examples

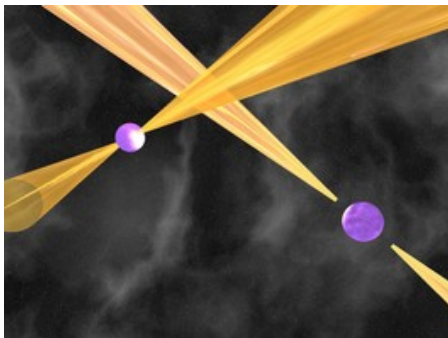
- Sun-Jupiter system

$$m_J = 1.9 \times 10^{27}, \quad a = 7.8 \times 10^{11} \quad \omega = 1.68 \times 10^{-7} s^{-1}$$

$$\Rightarrow P_{\text{GW}} = 5 \times 10^3 J/s$$

- ▶ Negligible compared to the sun $L_{\odot} \simeq 3.8 \times 10^{26} J/s$
- Binary pulsar PSR 1913+16 (Hulse and Taylor)

$$P_{\text{GW}} = 7.35 \times 10^{24} J/s$$



Radiated power: orbit shrinks, emission frequency increases

- Potential energy and Kepler's law

$$E = -G \frac{m_1 m_2}{2a}, \quad \omega^2 = \frac{GM}{a^3}$$

$$\Rightarrow \dot{E} = -G^{2/3} \frac{m_1 m_2}{2M^{1/3}} \frac{2}{3} \dot{\omega} \omega^{-1/3}$$

- Match orbital energy loss to radiated GW energy

$$\dot{E} = -P_{\text{GW}} \Rightarrow G^{2/3} \frac{m_1 m_2}{2M^{1/3}} \frac{2}{3} \dot{\omega} \omega^{-1/3} = \frac{32G\mu^2 a^4 \omega^6}{5c^5}$$

- Use Kepler's law to substitute a by ω

$$\frac{\dot{\omega}}{\omega^2} = \frac{96}{5} \frac{G^{5/3}}{c^5} \frac{\mu}{M} (M\omega)^{5/3}$$

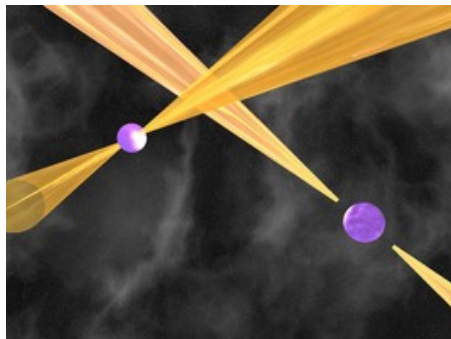
- GW frequency is $2\pi f_{\text{GW}} = 2\omega$

$$\dot{f}_{\text{GW}} = \frac{96}{5} \frac{G^{5/3}}{c^5} \pi^{8/3} \mathcal{M}^{5/3} f_{\text{GW}}^{11/3}$$

- Where we define the chirp mass that drives the frequency evolution

$$\mathcal{M} = \mu^{3/5} M^{2/5}$$

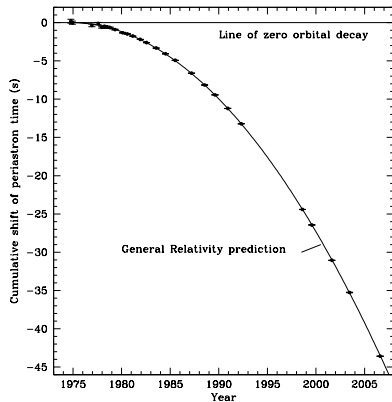
Indirect observation of GWs



Indirect observation of gravitational radiation

- $\phi(t) = \int^t \omega(t) dt$
- Orbital period measured through Doppler effects on radio pulses
- Follows GR with $\sim 10^{-3}$ precision

“double” pulsar PSR1913+16



Hulse-Taylor Nobel Prize 1993

Post-newtonian (PN) corrections needed

- Development of GR around the newtonian limit $\epsilon = \left(\frac{v}{c}\right)^2$
 - v – speed of the two stars, $v = (GM\omega)^{1/3}$
- For example orbital phase development

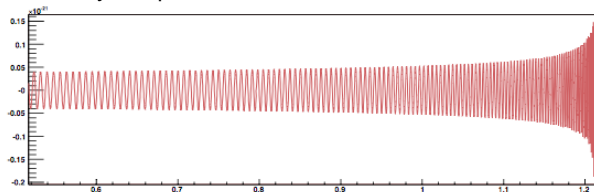
$$\phi(t) = \phi_N \times \sum_k \phi_{\frac{k}{2}PN} v^k$$

- High order correction become rapidly complex

k	N	2	3	4	5
\mathcal{F}_k	$\frac{32\eta^2 v^{10}}{5}$	$-\frac{1247}{336} - \frac{35\eta}{12}$	4π	$-\frac{44711}{9072} + \frac{9271\eta}{504} + \frac{65\eta^2}{18}$	$-\left(\frac{8191}{672} + \frac{535\eta}{24}\right)\pi$
t_k^v	$-\frac{5m}{256\eta v^8}$	$\frac{743}{252} + \frac{11\eta}{3}$	$-\frac{32\pi}{5}$	$\frac{3058673}{508032} + \frac{5429\eta}{504} + \frac{617\eta^2}{72}$	$-\left(\frac{7729}{252} + \eta\right)\pi$
ϕ_k^v	$-\frac{1}{16\eta v^5}$	$\frac{3715}{1008} + \frac{55\eta}{12}$	-10π	$\frac{15293365}{1016064} + \frac{27145\eta}{1008} + \frac{3085\eta^2}{144}$	$\left(\frac{38645}{672} + \frac{15\eta}{8}\right)\pi \ln\left(\frac{v}{v_{\text{iso}}}\right)$
ϕ_k^t	$-\frac{2}{\eta\theta^5}$	$\frac{3715}{8064} + \frac{55\eta}{96}$	$-\frac{3\pi}{4}$	$\frac{9275495}{14450688} + \frac{284875\eta}{258048} + \frac{1855\eta^2}{2048}$	$\left(\frac{38645}{21504} + \frac{15\eta}{256}\right)\pi \ln\left(\frac{\theta}{\theta_{\text{iso}}}\right)$
F_k^t	$\frac{\theta^3}{8\pi m}$	$\frac{743}{2688} + \frac{11\eta}{32}$	$-\frac{3\pi}{10}$	$\frac{1855099}{14450688} + \frac{56975\eta}{258048} + \frac{371\eta^2}{2048}$	$-\left(\frac{7729}{21504} + \frac{3}{256}\eta\right)\pi$
τ_k	$\frac{3}{128\eta}$	$\frac{5}{9}\left(\frac{743}{84} + 11\eta\right)$	-16π	$2\phi_4^v$	$\frac{1}{3}(8\phi_5^v - 5t_5^v)$

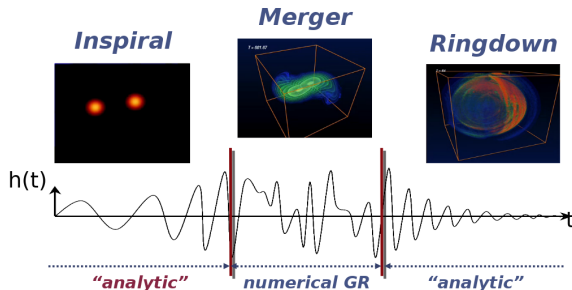
Example waveform

- Analytical part we looked at



$$P_{\text{GW}} = \frac{32G\mu^2 a^4 \omega^6}{5c^5}$$

- Full picture



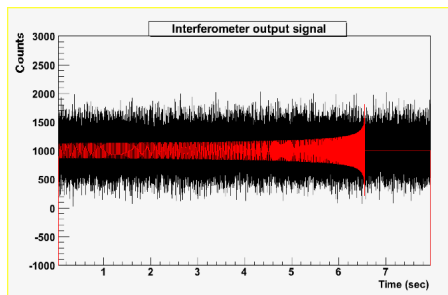
Part 2: gravitational wave data analysis

The problem

- Signal buried in noise

$$d(t) = n(t) + s(t)$$

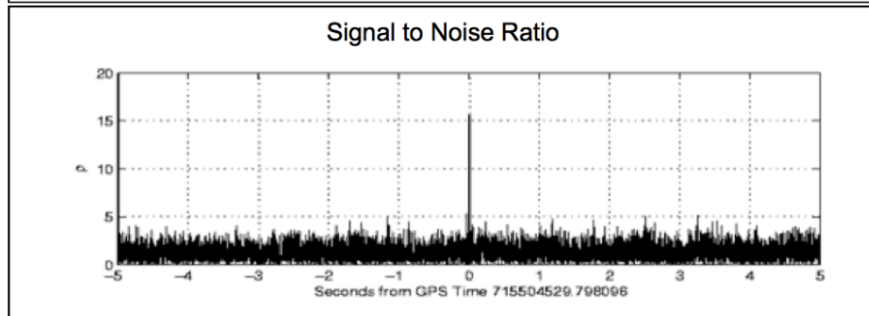
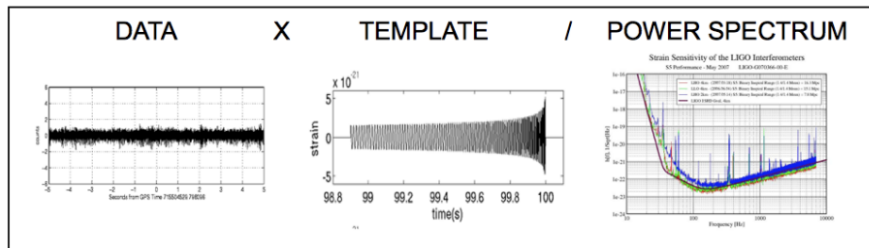
Data = Noise + Signal



- Noise is stochastic (random variable)
- Signal time evolution is known (post-newtonian expansion)

⇒ Use signal shape knowledge (templates)

Solution: matched filtering



Known signal in independent Gaussian noise

$$d(t) = n(t) + s(t)$$

- Independent Gaussian noise

$$P(n(t_0)) = \frac{1}{\sqrt{2\pi\sigma^2}} e^{-\frac{n(t_0)^2}{2\sigma^2}}$$

- H_0 hypothesis – there is only noise

$$P(d(t)|H_0) \propto e^{-\frac{d_1^2}{2\sigma^2}} \times e^{-\frac{d_2^2}{2\sigma^2}} \times \dots = \exp\left(-\sum_{i=1}^N \frac{d_i^2}{2\sigma^2}\right)$$

- H_1 hypothesis – there is a signal s in the noise

$$P(d(t)|H_1) \propto e^{-\frac{(d_1-s_1)^2}{2\sigma^2}} \times e^{-\frac{(d_2-s_2)^2}{2\sigma^2}} \times \dots = \exp\left(-\sum_{i=1}^N \frac{(d_i - s_i)^2}{2\sigma^2}\right)$$

- Likelihood ratio of each hypothesis

$$\frac{P(d(t)|H_1)}{P(d(t)|H_0)} = \exp\left(-\sum_{i=1}^N \frac{(d_i - s_i)^2 - d_i^2}{2\sigma^2}\right) = \exp\left(\sum_{i=1}^N \frac{2d_i s_i - s_i^2}{2\sigma^2}\right)$$

Known signal in independent Gaussian noise

- Likelihood ratio of each hypothesis

$$L = \log \frac{P(d(t)|H_1)}{P(d(t)|H_0)} = 2 \sum_{i=1}^N \frac{d_i s_i}{2\sigma^2} - \sum_{i=1}^N \frac{s_i^2}{2\sigma^2}$$

⇒ Correlation between data and expected signal tells which hypothesis is more likely

- Unknown parameters – signal amplitude (source distance)

$$s_i \rightarrow A s_i$$

$$L(A) = 2A \sum_{i=1}^N \frac{d_i s_i}{2\sigma^2} - A^2 \sum_{i=1}^N \frac{s_i^2}{2\sigma^2}$$

- Find analytically the maximum of L , most likely signal amplitude A

$$\frac{\partial L}{\partial A} = 2 \sum_{i=1}^N \frac{d_i s_i}{2\sigma^2} - 2A \sum_{i=1}^N \frac{s_i^2}{2\sigma^2} = 0 \quad \Rightarrow \quad A = \frac{\sum_{i=1}^N \frac{d_i s_i}{2\sigma^2}}{\sum_{i=1}^N \frac{s_i^2}{2\sigma^2}}$$

$$\max_A L(A) = 2 \frac{\left(\sum_{i=1}^N \frac{d_i s_i}{2\sigma^2}\right)^2}{\sum_{i=1}^N \frac{s_i^2}{2\sigma^2}} - \frac{\left(\sum_{i=1}^N \frac{d_i s_i}{2\sigma^2}\right)^2}{\sum_{i=1}^N \frac{s_i^2}{2\sigma^2}} = \frac{\left(\sum_{i=1}^N \frac{d_i s_i}{2\sigma^2}\right)^2}{\sum_{i=1}^N \frac{s_i^2}{2\sigma^2}}$$

Signal templates

$$\max_A L(A) = \frac{\left(\sum_{i=1}^N \frac{d_i s_i}{2\sigma^2}\right)^2}{\sum_{i=1}^N \frac{s_i^2}{2\sigma^2}}$$

- Normalized signal template

$$u_i = \frac{s_i}{\sqrt{\sum_{i=1}^N \frac{s_i^2}{2\sigma^2}}}$$

- Standard form of detection statistic

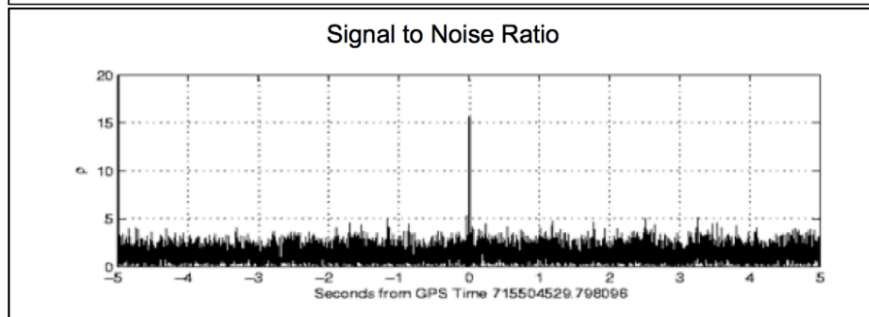
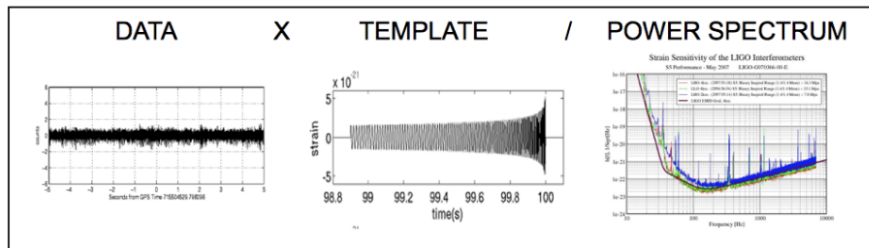
$$\max_A L(A) = \left(\sum_{i=1}^N \frac{d_i u_i}{2\sigma^2}\right)^2 = \text{SNR}^2$$

- In practice noise is correlated in time but independent in frequency domain

$$\max_A L(A) = \left(\sum_{i=1}^N \frac{\tilde{d}_k \tilde{u}_k}{2\sigma_k^2}\right)^2$$

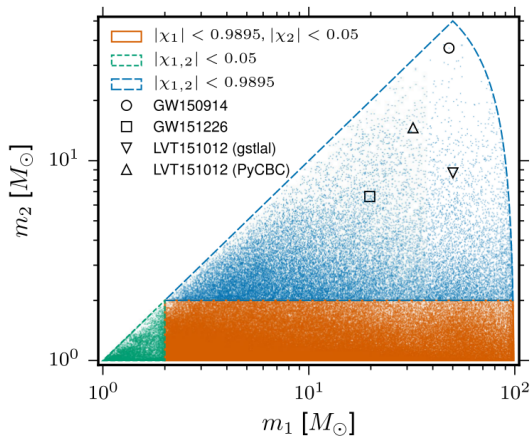
- Maximization (masses of objects, ...) on other parameters is done numerically

Solution: matched filtering



$$\max_A L(A) = \left(\sum_{k=1}^N \frac{\tilde{d}_k \tilde{u}_k}{2\sigma_k^2} \right)^2$$

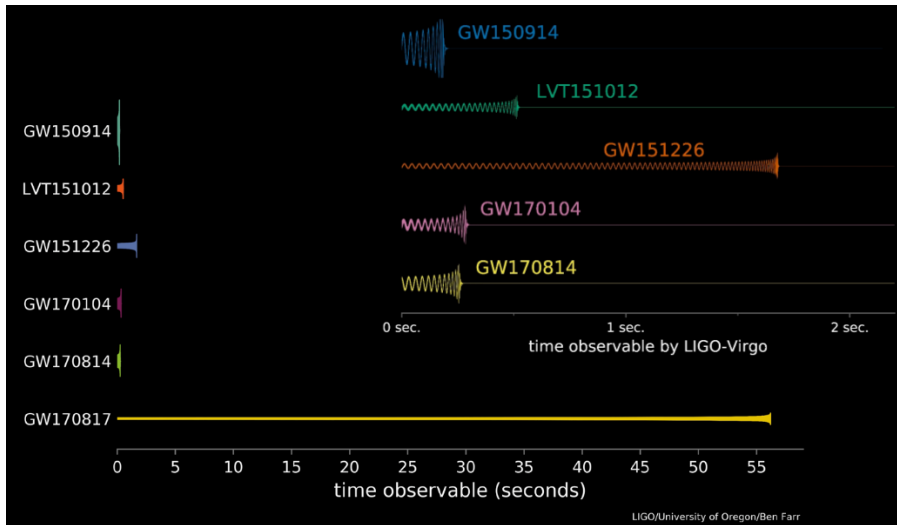
Search over large parameter space



$$\max_{m_1, m_2} L(m_1, m_2) = \left(\sum_{i=1}^N \frac{\tilde{d}_k \tilde{u}_k(m_1, m_2)}{2\sigma_k^2} \right)^2$$


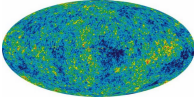
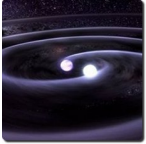
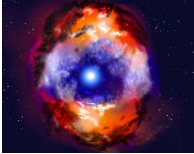
- $\sim 250 \times 10^3$ templates
- Include NS-NS, NS-BH, BH-BH

Signal diversity



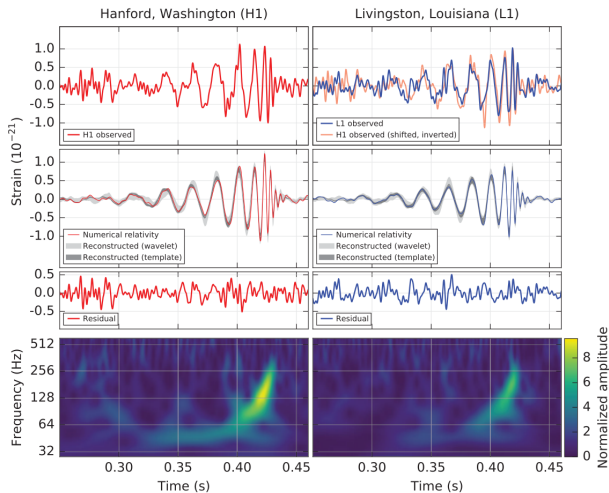
- Waveforms of signals detected so far

4 families of potential GW signal morphologies

	precisely modeled	uncertain form
permanent	<p>Deformed rotating neutron stars</p> 	<p>Incoherent sum of unresolved sources Primordial GW background</p> 
transient	<p>Cosmic strings cusps, kinks Coalescence of neutron stars or black holes</p> 	<p>Star quakes, Non spherically symmetric stellar collapse, ...</p> 

Part 3: gravitational wave results

GW150914: First direct detection of GWs

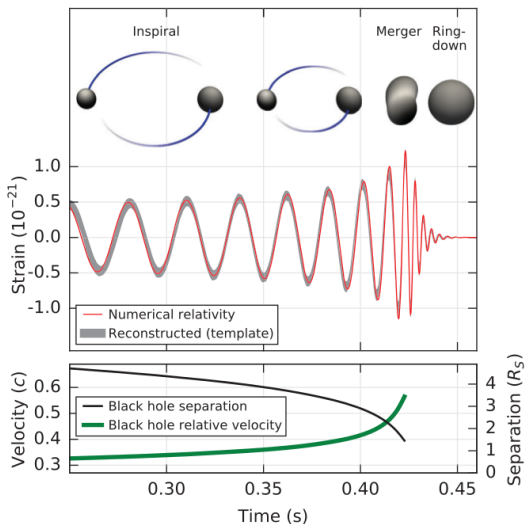


- GW150914 – 2015 September 14
- short signal: 0.1 second
- highest frequency is ~ 250 Hz

GW150914: First direct detection of GWs

Waveforms without noise

Waveform shape matches general relativity prediction



- GW frequency \Rightarrow twice the orbital frequency $\Rightarrow \sim$ orbit from Kepler's law
- Relativistic collision $v \sim 0.5c$, fastest double neutron star known $v/c \simeq 2 \times 10^{-3}$

Gravitational wave carry away energy

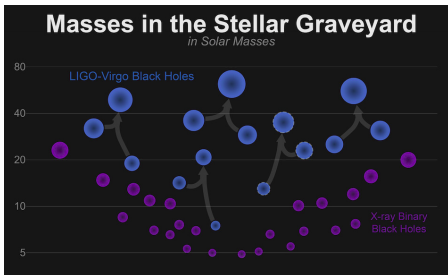
Primary black hole mass	$36_{-4}^{+5} M_{\odot}$
Secondary black hole mass	$29_{-4}^{+4} M_{\odot}$
Final black hole mass	$62_{-4}^{+4} M_{\odot}$
Final black hole spin	$0.67_{-0.07}^{+0.05}$
Luminosity distance	410_{-180}^{+160} Mpc
Source redshift z	$0.09_{-0.04}^{+0.03}$

- GW amplitude correspond to 3 solar masses emitted

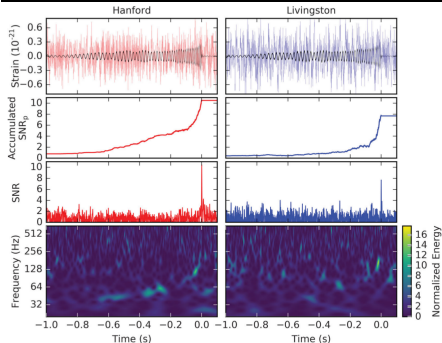
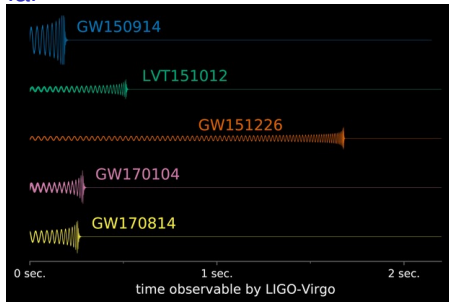
$$\frac{dP}{d\Omega} = \frac{c^3}{16\pi G} \left\langle \left(\dot{h}_+ \right)^2 + \left(\dot{h}_\times \right)^2 \right\rangle$$

- Nuclear reaction 0.1-0.3% mass conversion, here it is $\sim 4\%$
- Not a surprise, known for 40 years

Several other binary BH detected so far



- Heavier than most black hole observed through X-rays
- Templates necessary to detect weaker signals



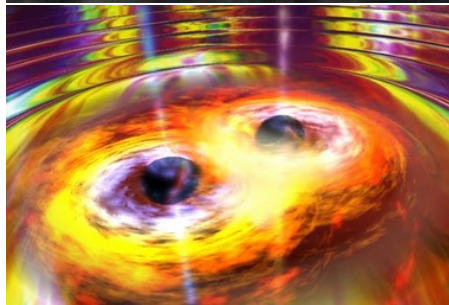
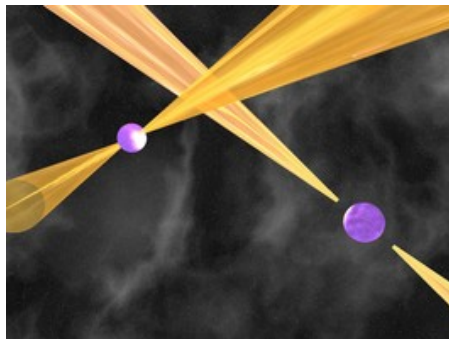
Testing general relativity (GR)

PSR J0737-3039

- Most relativistic binary pulsar known
- orbital velocity $\frac{v}{c} \sim 2 \times 10^{-3}$

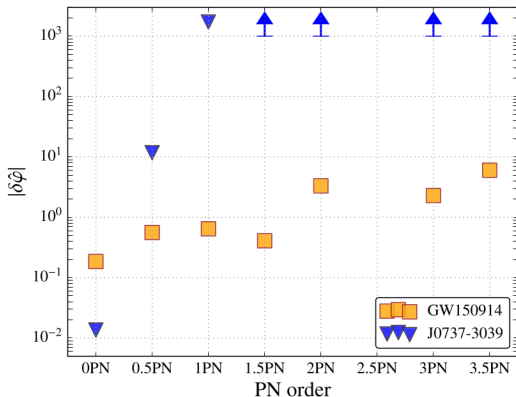
Binary black hole GW

- large velocity, strong gravitational field
- orbital velocity $\frac{v}{c} \sim 0.5$



Deviation from general relativity

k	N	2	3	4	5
\mathcal{F}_k	$\frac{32\eta^2 v^{10}}{5}$	$-\frac{1247}{336} - \frac{35\eta}{12}$	4π	$-\frac{44711}{9072} + \frac{9271\eta}{504} + \frac{65\eta^2}{18}$	$-\left(\frac{8191}{672} + \frac{535\eta}{24}\right)\pi$
t_k^v	$-\frac{5m}{256\eta^8}$	$\frac{743}{252} + \frac{11\eta}{3}$	$-\frac{32\pi}{5}$	$\frac{3058673}{508032} + \frac{5422\eta}{504} + \frac{617\eta^2}{72}$	$-\left(\frac{7729}{252} + \eta\right)\pi$
ϕ_k^v	$-\frac{1}{16\eta v^5}$	$\frac{3715}{1008} + \frac{55\eta}{12}$	-10π	$\frac{15293365}{1016064} + \frac{27145\eta}{1008} + \frac{3085\eta^2}{144}$	$\left(\frac{38645}{672} + \frac{15\eta}{8}\right)\pi \ln\left(\frac{v}{v_{\text{iso}}}\right)$
ϕ_k^t	$-\frac{2}{\eta\theta^5}$	$\frac{3715}{8064} + \frac{55\eta}{96}$	$-\frac{3\pi}{4}$	$\frac{9275495}{14450688} + \frac{284875\eta}{258048} + \frac{1855\eta^2}{2048}$	$\left(\frac{38645}{21504} + \frac{15\eta}{256}\right)\pi \ln\left(\frac{\theta}{\theta_{\text{iso}}}\right)$
F_k^t	$\frac{\theta^3}{8\pi m}$	$\frac{743}{2688} + \frac{11\eta}{32}$	$-\frac{3\pi}{10}$	$\frac{1855099}{14450688} + \frac{56975\eta}{258048} + \frac{371\eta^2}{2048}$	$-\left(\frac{7729}{21504} + \frac{3\eta}{256}\right)\pi$
τ_k	$\frac{3}{128\eta}$	$\frac{5}{9}\left(\frac{743}{84} + 11\eta\right)$	-16π	$2\phi_4^v$	$\frac{1}{3}(8\phi_5^v - 5t_5^v)$



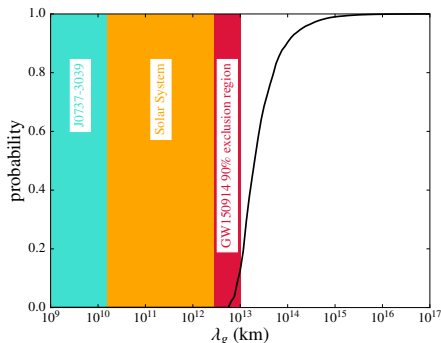
- Double neutron star has small $(v/c) \simeq 2 \times 10^{-3}$
- $\delta\phi$ in units of GR prediction

Dispersion relation and graviton mass

$$E^2 = p^2 c^2 + m_g^2 c^4$$

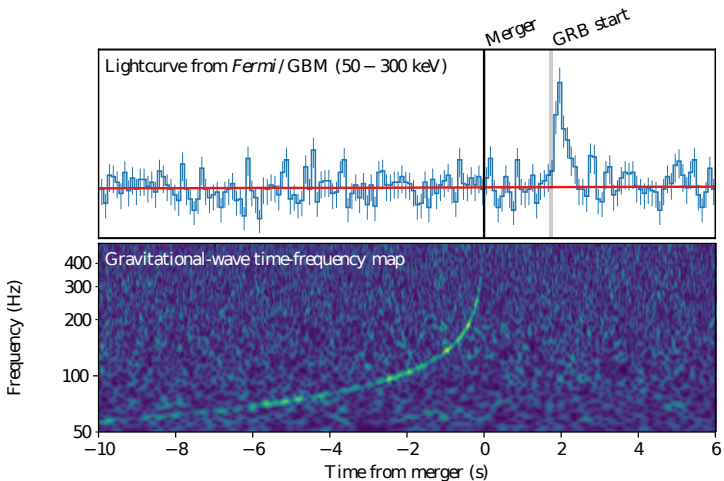
scale at which G/r^2 fails: $\lambda_g = \frac{h}{m_g c}$

$$\frac{v_g^2}{c^2} \equiv \frac{c^2 p^2}{E^2} \simeq 1 - \frac{h^2 c^2}{\lambda_g^2 E^2}$$



- ⇒ Low energy (frequency) GW propagate slower (slowed down by mass)
- ⇒ Low frequency GW would arrive after instead of before high frequency GWs!
- ⇒ $\lambda_g > 1 \times 10^{13} \text{ km} \sim 0.5 \text{ parsec} \Leftrightarrow m_g < 1.2 \times 10^{-22} \text{ eV}/c^2$

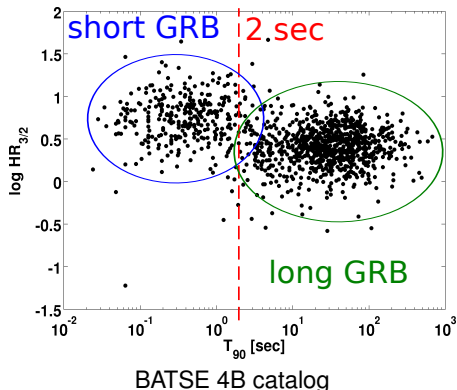
GW170817 and GRB 170817A



- Gamma-ray bursts starts 1.74 s after the merger

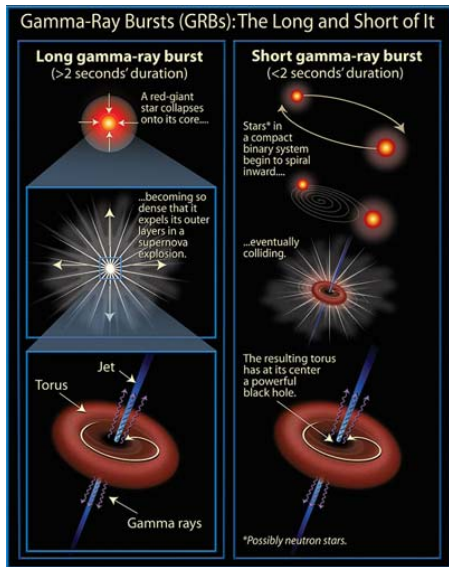
Gamma-ray bursts

- Observational definition → a burst of γ -rays (10 keV – 1 MeV)
- Discovered in the 70's by nuclear bomb test surveillance satellites



- T_{90} - duration of 90% of photon counts ($\sim 15 - 300$ keV)
- Two observational populations:
 - ▶ short-hard GRBs $T_{90} \lesssim 2$ s
spectrum peaks at higher energy
 - ▶ long-soft GRBs $T_{90} \gtrsim 2$ s
spectrum peaks at lower energy

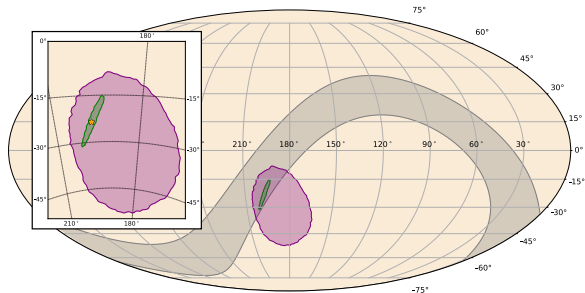
Gamma-ray burst models



credit: Ute Kraus

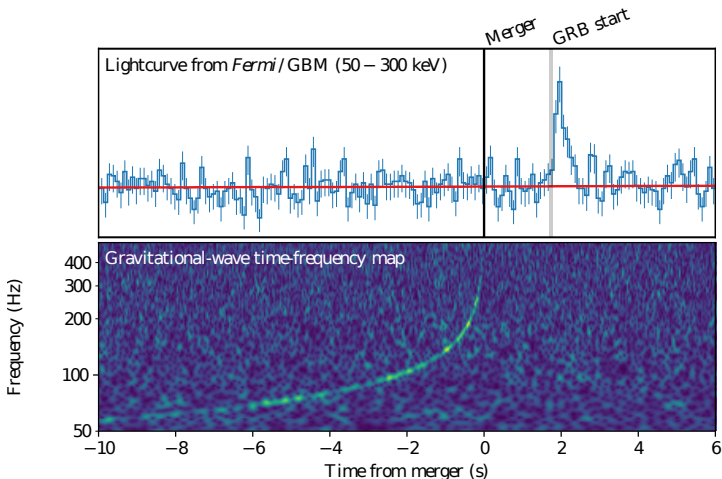
- Long GRBs
 - ⇒ Massive rapidly spinning star collapse and explosion
 - ⇒ Confirmed by several association to Supernovae
- Short GRBs
 - ⇒ Coalescence of a neutron star and a compact object
 - ⇒ Common in the outskirts of old galaxies

GW170817 / GRB 170817A have a common origin



- 1.74 s time delay vs 0.12 short GRB per day \Rightarrow p-value 5×10^{-6}
 - sky location overlap \Rightarrow p-value 0.01
 - p-value 5×10^{-8} or 5.3σ
- \Rightarrow (Some) short gamma-ray bursts are indeed due to binary neutron star mergers

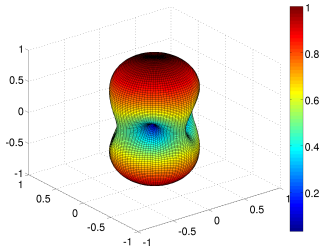
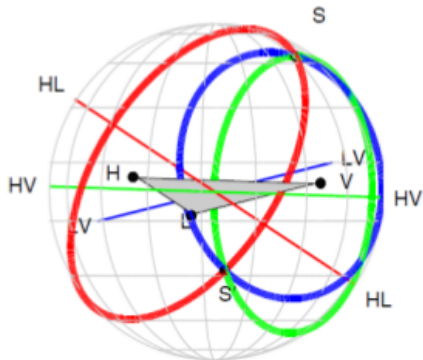
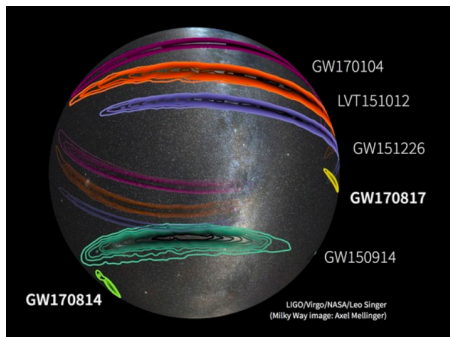
GW170817 and GRB 170817A



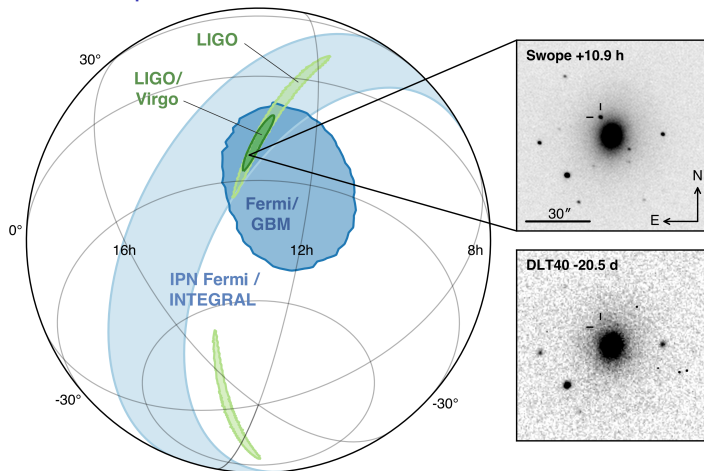
- Gamma-ray bursts starts 1.74 s after the merger
- ⇒ (Some) short gamma-ray bursts are indeed due to binary neutron star mergers

Gravitational wave sky localization

- Primarily time delay
 - ▶ 2 detectors: ring on the sky
 - ▶ 3 detectors: intersection of 2 rings
- Amplitude information helps



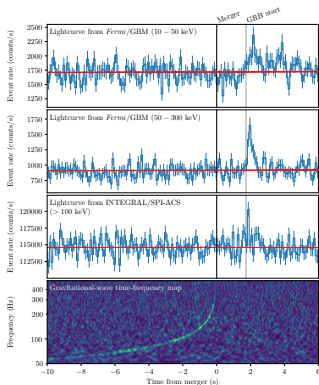
An optical counterpart



- Localized in the sky by 3 GW detectors
- Observed near a galaxy (NGC 4993) 130 million light years away (40 Mpc)

⇒ A kilonova

GW170817 / GRB 170817A - fundamental physics test



- 1.74 s delay over 130 million years of propagation
- Assuming gamma emission delayed by [0,10] s

$$-3 \times 10^{-15} \leq \frac{v_{\text{GW}} - v_{\text{EM}}}{v_{\text{EM}}} \leq 7 \times 10^{-16}$$

- Shapiro effect: gravitational potential slows clocks down
- ⇒ Equivalence principle test, GW and EM clocks are affected the same, $\gamma_{\text{GW}} = \gamma_{\text{EM}} = 1$
- Only using Milky Way potential at large distances (100 kpc)

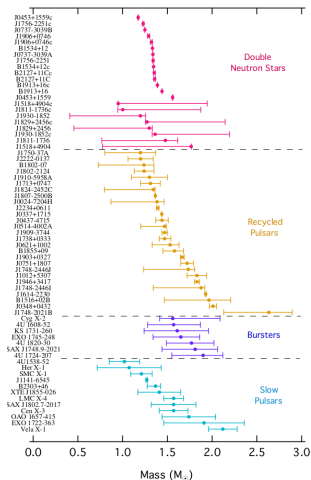
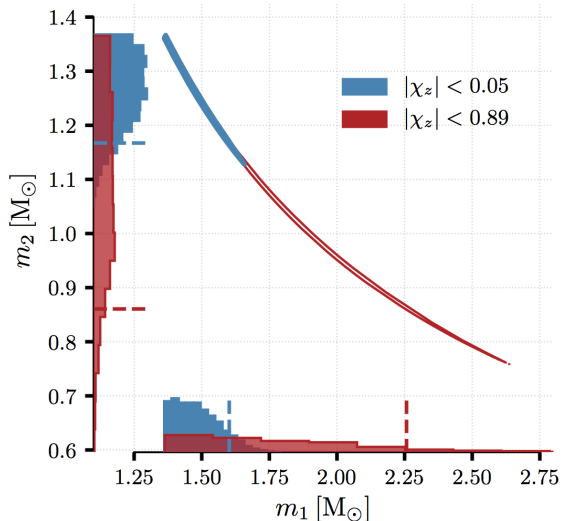
$$-2.6 \times 10^{-7} \leq \gamma_{\text{GW}} - \gamma_{\text{EM}} \leq 1.2 \times 10^{-6}$$

GW170817 / GRB 170817A - fundamental physics test

	$c_g = c$	$c_g \neq c$
Horndeski	General Relativity quintessence/k-essence [46] Brans-Dicke/ $f(R)$ [47] [48] Kinetic Gravity Braiding [50]	quartic/quintic Galileons [13] [14] Fab Four [15] de Sitter Horndeski [49] $G_{\mu\nu}\phi^\mu\phi^\nu$ [51], $f(\phi)$ -Gauss-Bonnet [52]
beyond H.	Derivative Conformal (19) [17] Disformal Tuning (21) quadratic DHOST with $A_1 = 0$	quartic/quintic GLPV [18] quadratic DHOST [20] with $A_1 \neq 0$ cubic DHOST [23]
	Viable after GW170817	Non-viable after GW170817

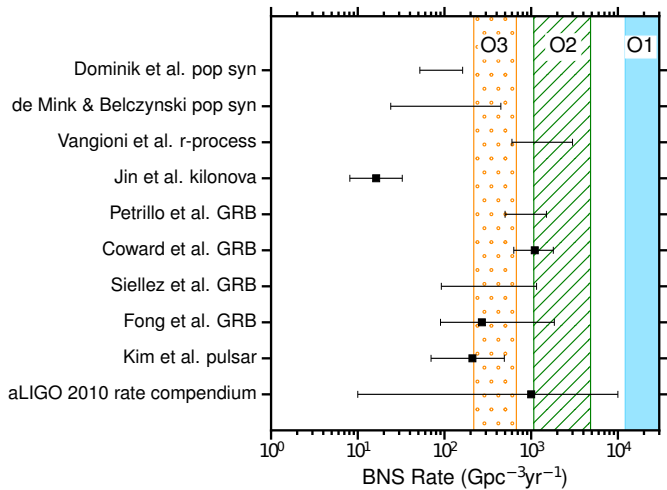
- Prediction of $\frac{v_{\text{GW}} - v_{\text{EM}}}{v_{\text{EM}}} \simeq 10^{-4}$ ruled out by 10 orders of magnitude
- Many GR modification to explain dark matter or dark energy are excluded

A collision of two neutron stars

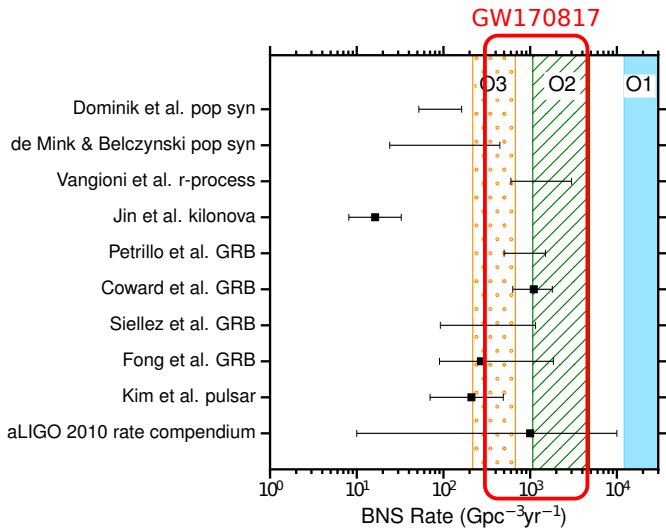


- Very small possibility that heavier object is a rapidly spinning light black hole

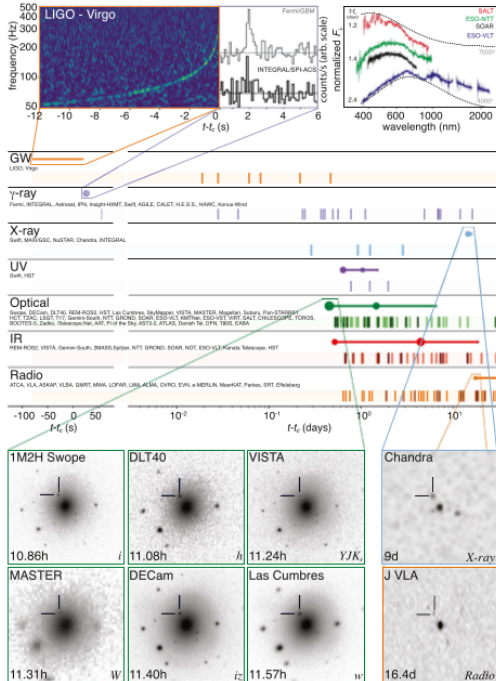
Single event \Rightarrow a measure of the BNS merger rate



Single event \Rightarrow a measure of the BNS merger rate

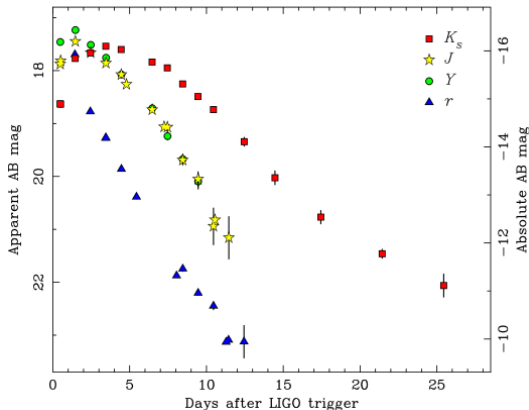
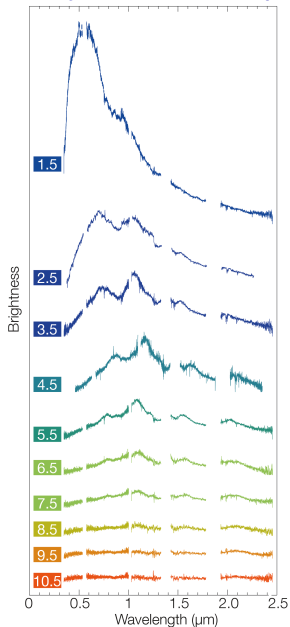


- Measured merger rate: $300 - 5000 \text{ Gpc}^{-3}\text{yr}^{-1}$
- compatible with O1 upper limit, r-process nucleosynthesis and GRB rate



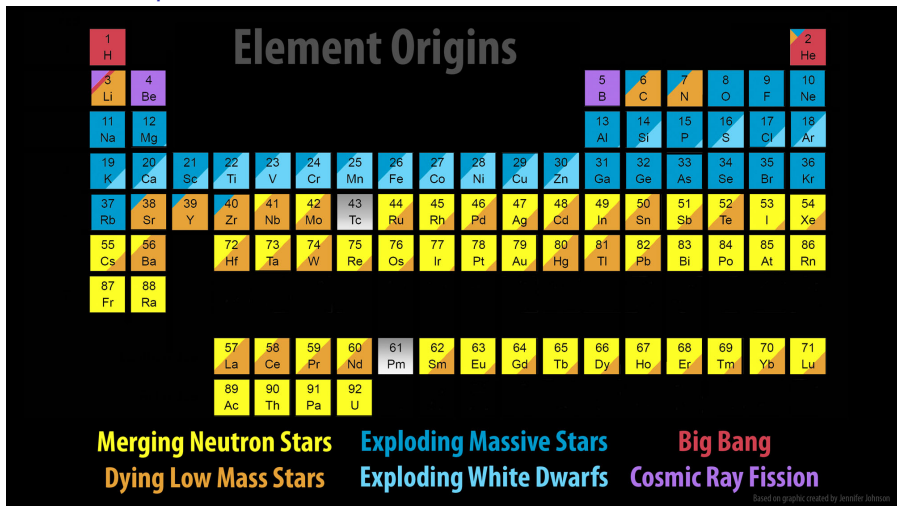
A complicated astrophysical event

A very well studied optical transient



- “kilonova” – 1% of supernova
- much faster evolution, days instead of weeks
- spectral lines broadening measures eject speed $\sim 0.1c$
- previously 2 tentative observations in 15 years

Where do expensive metals come from



- r-process (rapid neutron capture) power the optical transient
- Good explanation of origin of heavy elements in the universe

- Gravitational wave sources
- Gravitational wave data analysis
- Observed gravitational waves signals

r-Process simulation

EM measurement of NS mass-radius

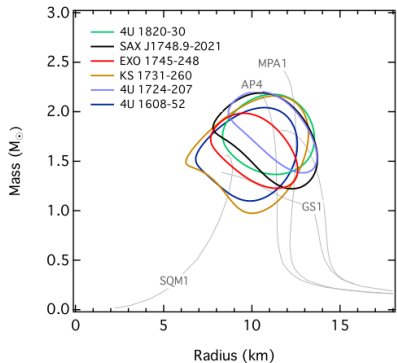
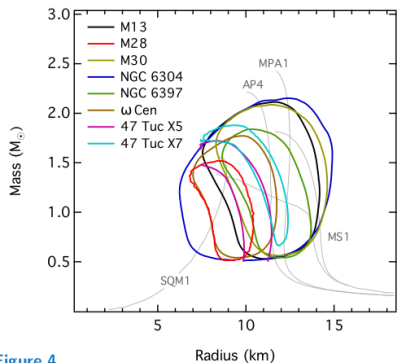
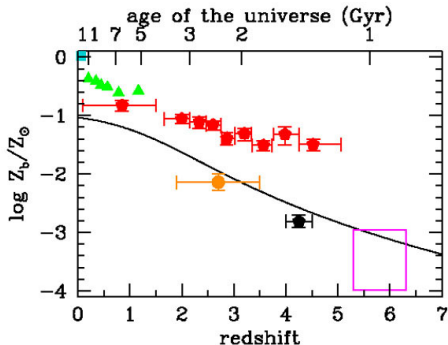
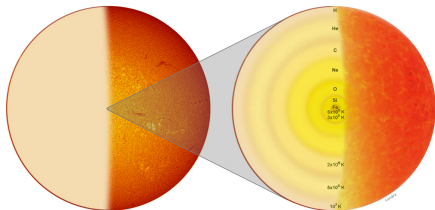


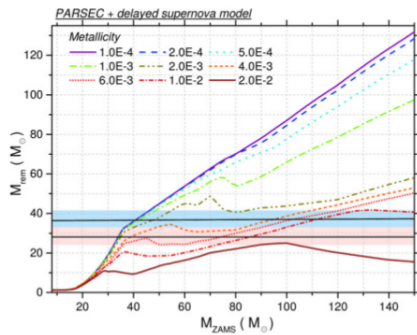
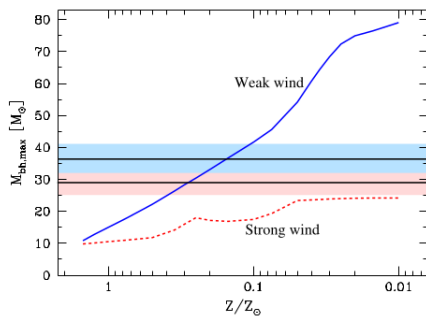
Figure 4

Black hole merger masses are large



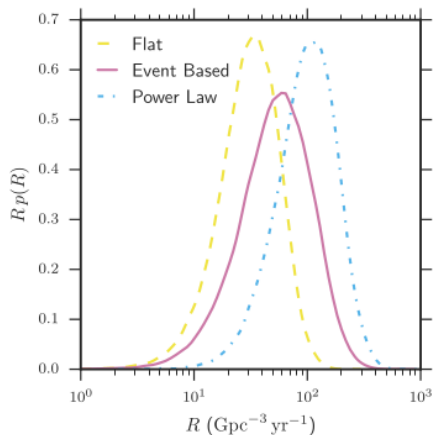
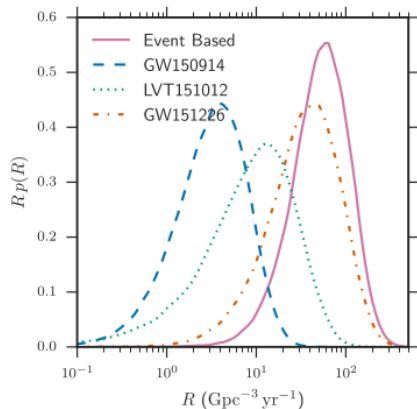
- Photons from nuclear reaction push stellar envelope outwards
- Cross section is higher if envelope contains “metals” (not hydrogen or helium)
- Supernova produce and disseminate metals
→ metallicity of stars increases with universe age

Black hole merger masses are large



- Models of stellar winds did not allow BH masses larger than $25M_{\odot}$
- Confirms recent models of stellar wind
- The binary BH system formed in an environment with $Z < Z_{\odot}/2$

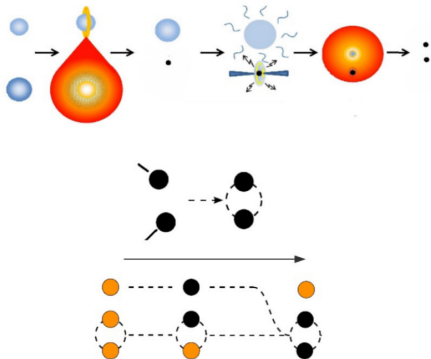
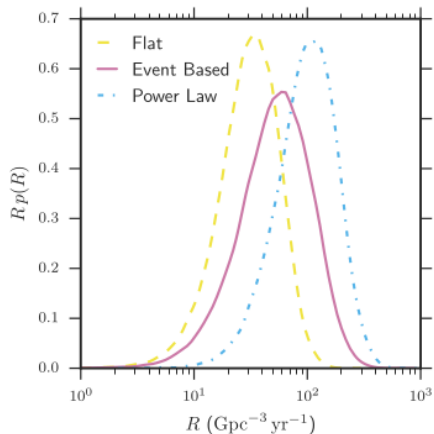
Black hole merger rate



$$R_{\text{eventbased}} \simeq \frac{1}{T_{\text{obs}} V_{\text{obs, GW150914}}} + \frac{1}{T_{\text{obs}} V_{\text{obs, LVT151012}}} + \frac{1}{T_{\text{obs}} V_{\text{obs, GW151226}}}$$

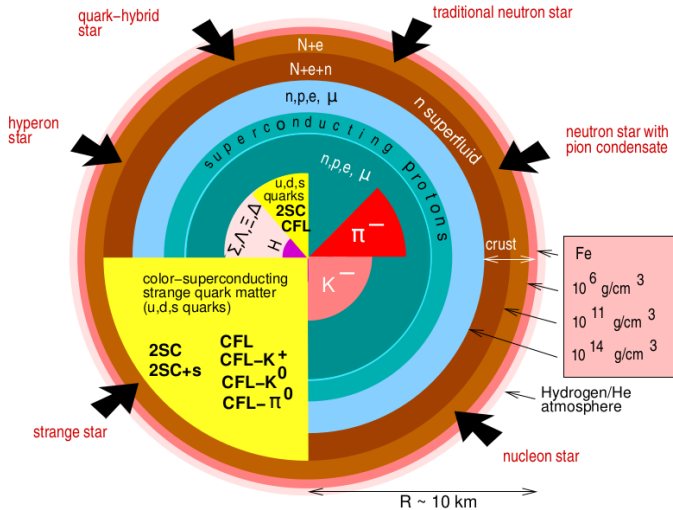
- Detectors horizon is smaller for lighter BH binaries \Rightarrow smaller volume
- flat in logarithm $p(m_1, m_2) \propto m_1^{-1} m_2^{-2}$
- powerlaw $p(m_1) \propto m_1^{-2.35}$, $p(m_2) \propto \theta(m_1 - m_2)$

Black hole merger rate



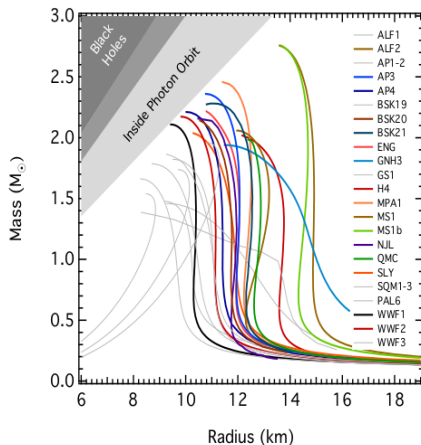
- Measured rate $R = 9 - 240 \text{ Gpc}^{-3}\text{yr}^{-1}$
- Models were predicting $R = 0.1 - 300 \text{ Gpc}^{-3}\text{yr}^{-1}$
- Exclude a few models and parameter space that were predicting $R \lesssim 1 \text{ Gpc}^{-3}\text{yr}^{-1}$

Neutron star structure and equation of state



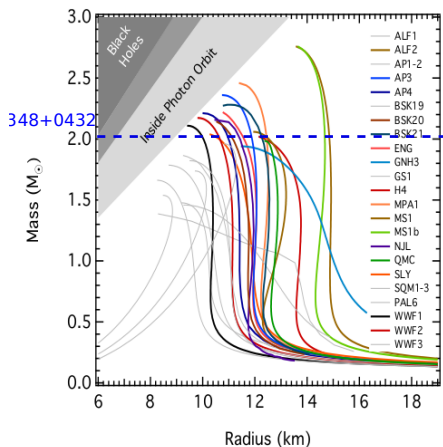
- Strange state of matter may exist in neutron star cores

Neutron star equation of state



- EOS: Pressure = $f(\text{density})$
- Governs relation between neutron star mass and radius
- Heavier neutron stars are smaller!
- Stiff equation of state (rapid pressure increase) \rightarrow large neutron star
- Soft equation of state (slow pressure increase) \rightarrow small neutron star

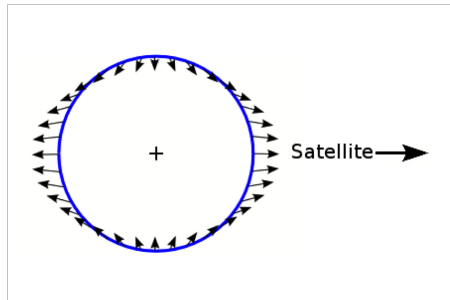
Neutron star equation of state



- J0348+0432 (MSP-WD) mass $2.01 \pm 0.04 M_{\odot}$
- Soft equation of state has small maximum NS mass

Tidal deformability

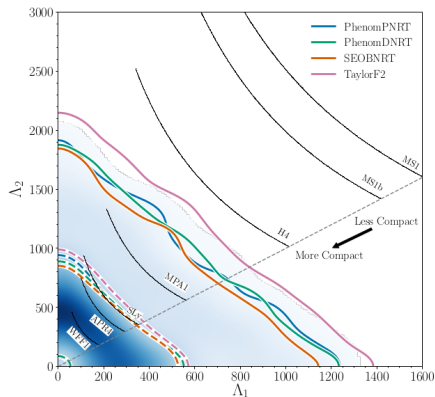
$$\Lambda = \frac{2}{3} k_2 \left(\frac{c^2 R}{Gm} \right)^5$$



- Λ parameter changing gravitational wave phase
- k_2 dimensionless quantity (Love number) characterizing tidal deformability
- R neutron star radius
- m neutron star mass
- Large neutron star (stiff EOS) have higher tidal effect
- Tidal deformation causes neutron stars to merger faster (additional energy loss)
- GW encodes a combination of both stars deformabilities

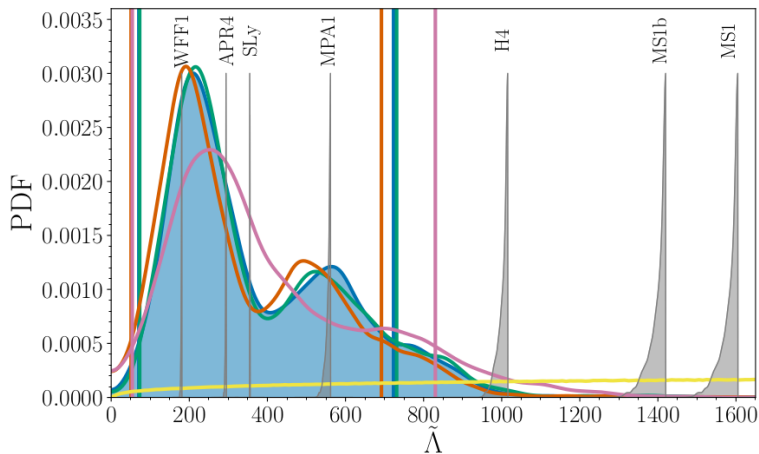
$$\tilde{\Lambda} = \frac{16}{13} \frac{(m_1 + 12m_2)m_1^4\Lambda_1 + (m_2 + 12m_1)m_2^4\Lambda_2}{(m_1 + m_2)^5}$$

Tidal deformability



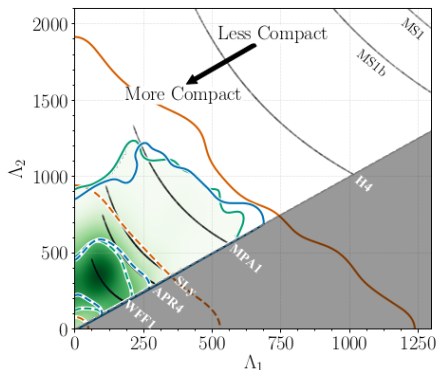
- NS tidal deformation speeds up binary coalescence
- Disfavors stiff equations of states that result in large neutron stars

Tidal deformability



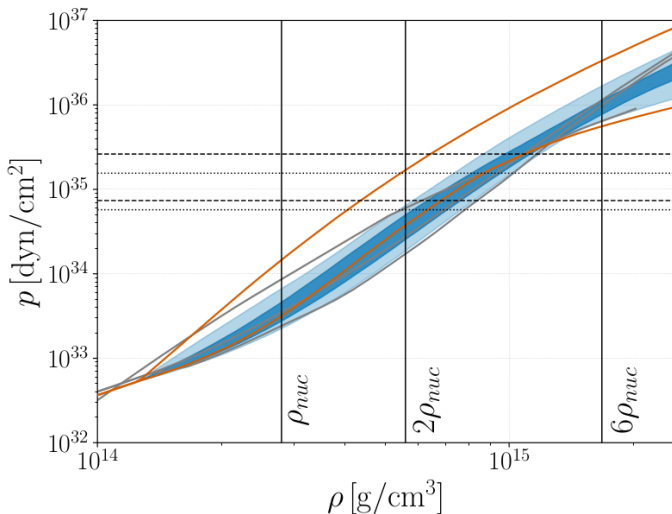
- $50 < \tilde{\Lambda} < 830$

Assuming equal EOS for both neutron stars



- Λ_1, Λ_2 can still be different because of unequal mass
 - $70 < \tilde{\Lambda} < 580$
 - Green: same EOS, max mass $> 1.97 M_{\odot}$
 - Blue: same EOS
 - Red: independent EOS
- ⇒ Not a proof that objects are not BHs, boson stars, ...

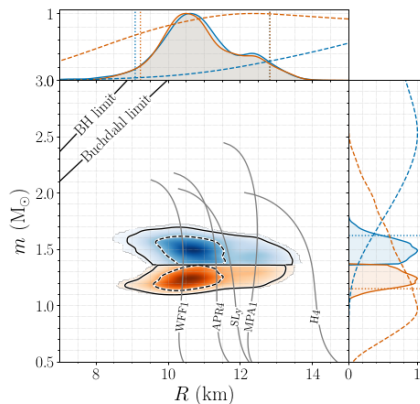
A measurement of the equation of state



- Soft equation of state are favored

A measurement of the equation of state

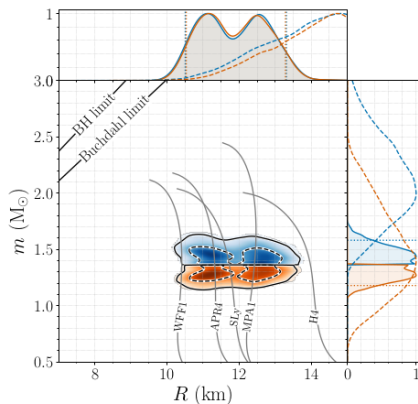
- Tidal deformability only



$$9.1 \text{ km} < R_1 < 12.8 \text{ km}$$

$$9.2 \text{ km} < R_2 < 12.8 \text{ km}$$

- Parametrized EOS
& EOS allow $M_{\text{NS}} > 1.97M_{\odot}$

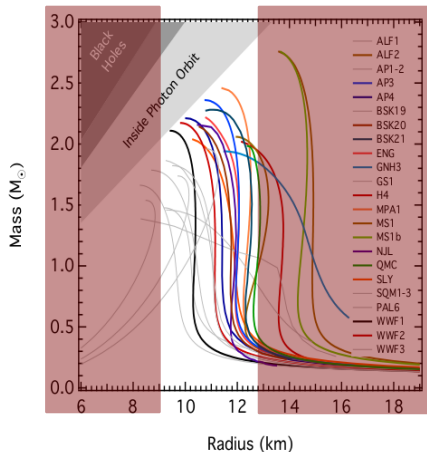


$$10.5 \text{ km} < R_1 < 13.3 \text{ km}$$

$$10.5 \text{ km} < R_2 < 13.3 \text{ km}$$

A measurement of the equation of state

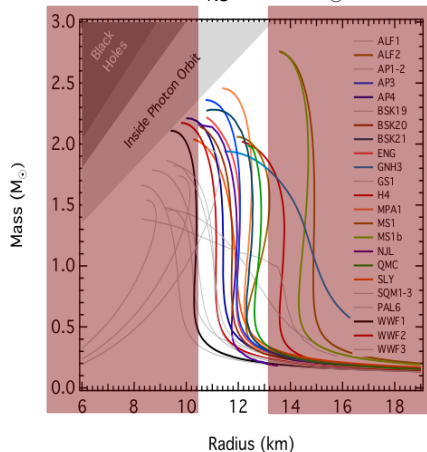
- Tidal deformability only



$$9.1 \text{ km} < R_1 < 12.8 \text{ km}$$

$$9.2 \text{ km} < R_2 < 12.8 \text{ km}$$

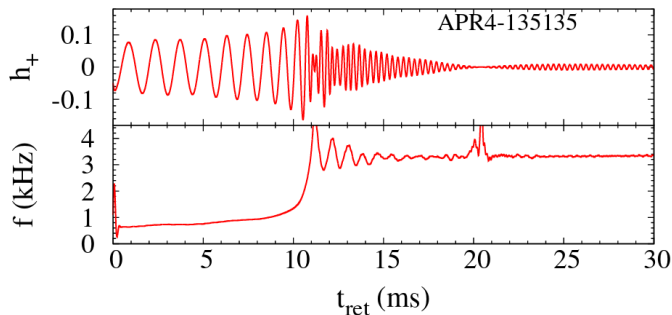
- Parametrized EOS & EOS allow $M_{\text{NS}} > 1.97M_{\odot}$



$$10.5 \text{ km} < R_1 < 13.3 \text{ km}$$

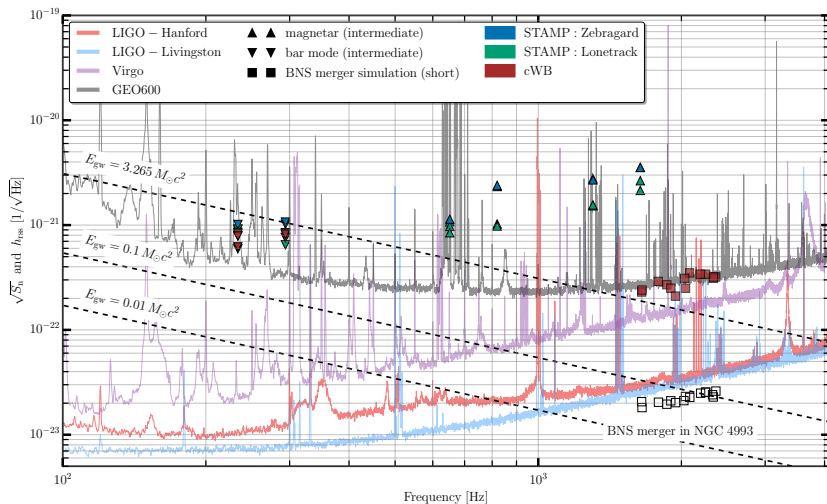
$$10.5 \text{ km} < R_2 < 13.3 \text{ km}$$

Post-merger scenarios



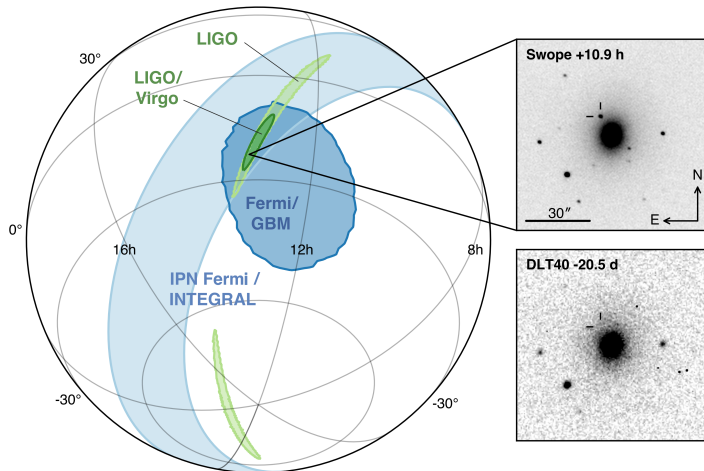
- prompt collapse to a BH
 - ▶ Small amplitude and high frequency signal \rightarrow not detectable
- hypermassive NS collapsing to a BH $\lesssim 1$ s
 - ▶ Numerical relativity simulations, short signal
- supramassive or stable NS with $\gtrsim 10$ s lifetime
 - ▶ Semi-analytical computation of unstable modes

No direct information on post-merger signal



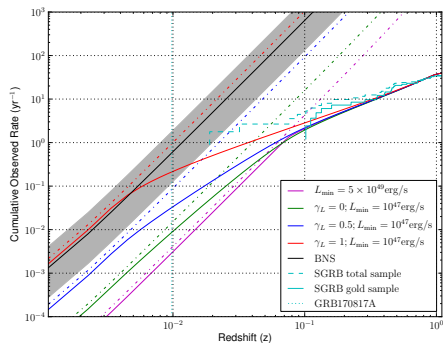
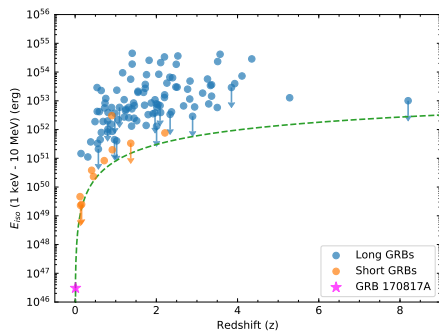
- A detectable signal \sim most of remnant evaporating in gravitational waves

An optical counterpart



- Localized in the sky by 3 GW detectors
- Observed near a galaxy (NGC 4993) \Rightarrow known redshift

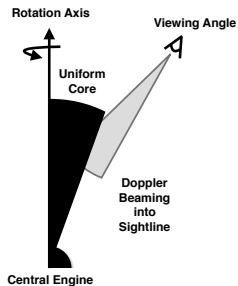
A very faint gamma-ray burst



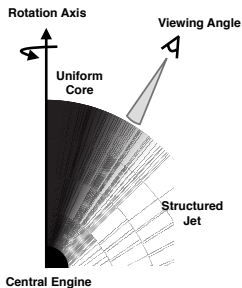
- More nearby faint GRBs than previously thought
- Gamma-ray detectors (satellites) miss most of them

A very faint gamma-ray burst – seen off axis?

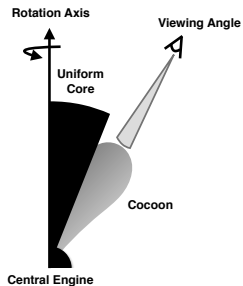
Scenario i: Uniform Top-hat Jet



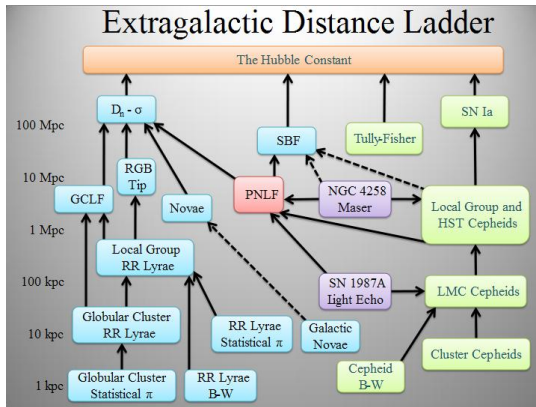
Scenario ii: Structured Jet



Scenario iii: Uniform Jet + Cocoon



Hubble constant rely on a long chain of measurements



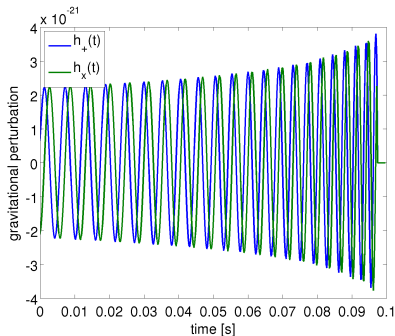
- Potential for systematic error at each step
- Gravitational wave measure distance directly

Measuring Hubble's constant with GWs

All potential GWs sources $z \lesssim 0.1$: $H_0 = c \frac{z}{D_L}$

$$\begin{bmatrix} h_+(t) \\ h_\times(t) \end{bmatrix} = \underbrace{\frac{A(t; (1+z)\mathcal{M})}{D_L}}_{\text{enveloppe}} \underbrace{\begin{bmatrix} (1 + \cos^2 \iota) \cos(\Psi(t)) \\ 2 \cos \iota \sin(\Psi(t)) \end{bmatrix}}_{\text{polarized oscillations}}$$

- $A(t; (1+z)\mathcal{M})$ - GW shape sets absolute amplitude of the waveform
- D_L - luminosity distance
- ι - binary inclination angle - degenerate with luminosity distance (polarization is hard to measure)
- z - redshift - degenerate with the mass of the binary



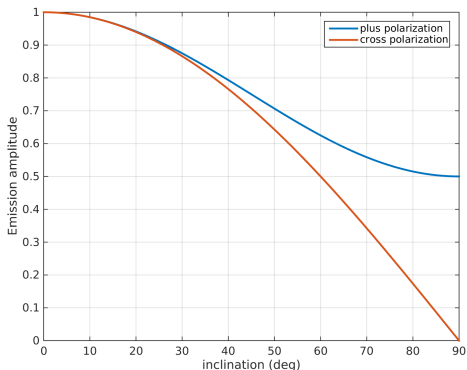
Measuring Hubble's constant with GWs

$$\begin{bmatrix} h_+(t) \\ h_\times(t) \end{bmatrix} = \frac{A(t; (1+z)\mathcal{M})}{D_L} \begin{bmatrix} (1 + \cos^2 \iota) \cos(\Psi(t)) \\ 2 \cos \iota \sin(\Psi(t)) \end{bmatrix}$$

Several approaches

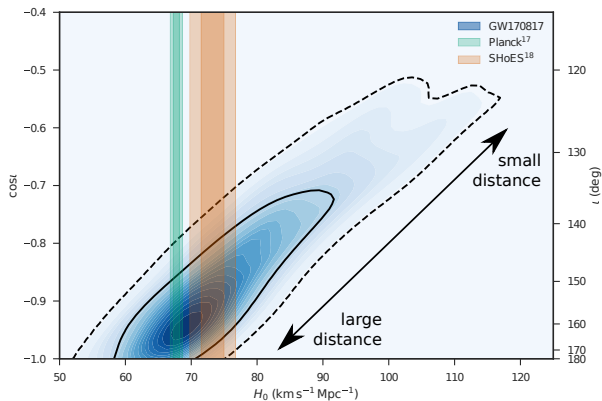
- Combine GW and GRB observation
 - ▶ **redshift** given by EM observations
 - ▶ GW shape yields absolute amplitude
 - Measure D_L from GW amplitude
 - ▶ D_L vs inclination degeneracy
- Use GW information alone
 - ▶ Assume \mathcal{M} known - binary neutron star system
 - Measure **redshift** from GW shape
 - ▶ GW shape yields absolute amplitude
 - Measure D_L from GW amplitude
 - ▶ Dozens of events per year
 - helps breaking the D_L vs inclination degeneracy

Distance vs inclination degeneracy – direct measurement



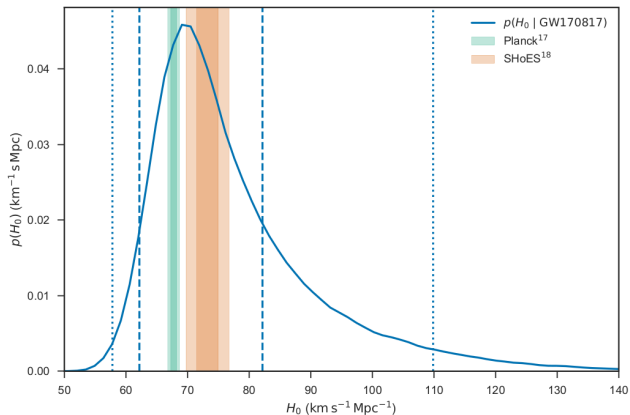
- LIGO Hanford and Livingston aligned
 - ⇒ sensitive to only one polarization
- A strong signal in 3 detectors
 - ⇒ measure polarization: circular vs linear
 - ⇒ direct measurement of system inclination only for inclination > 50 deg

Distance vs inclination degeneracy



- Clear degeneracy $\Rightarrow \cos i \propto 1/D$

Hubble constant measurement



- Inclination degeneracy is limiting but more events will statistically reduce it