

SVD : Single Value Decomposition

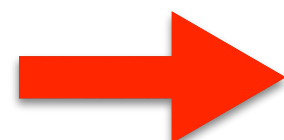
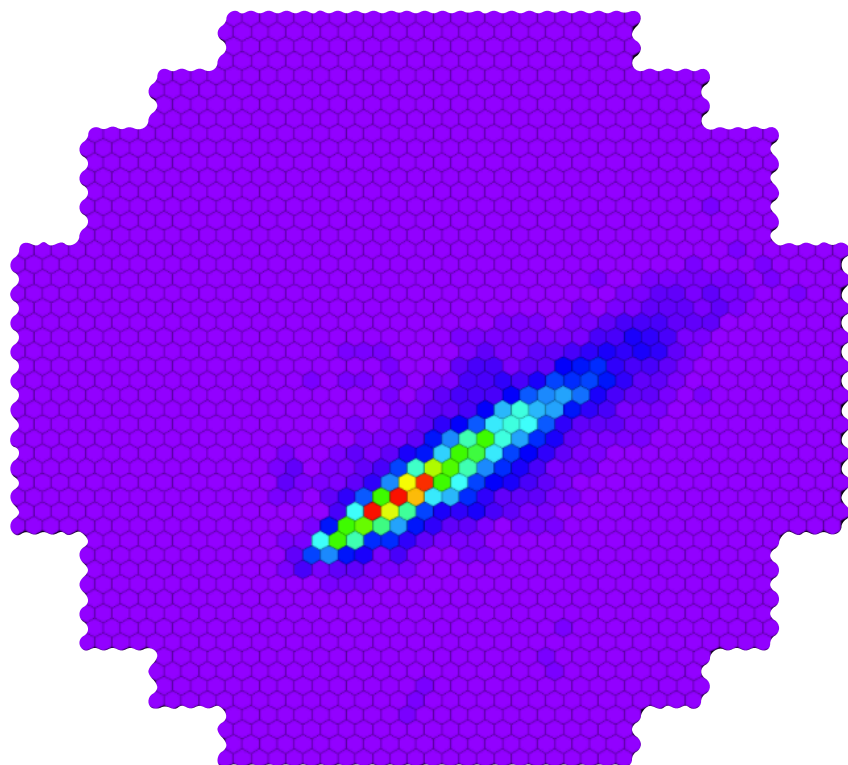
a new HPC template method

CEA-LAPP meeting - 15 January 2018

Florian Gaté for the LAPP

Motivations

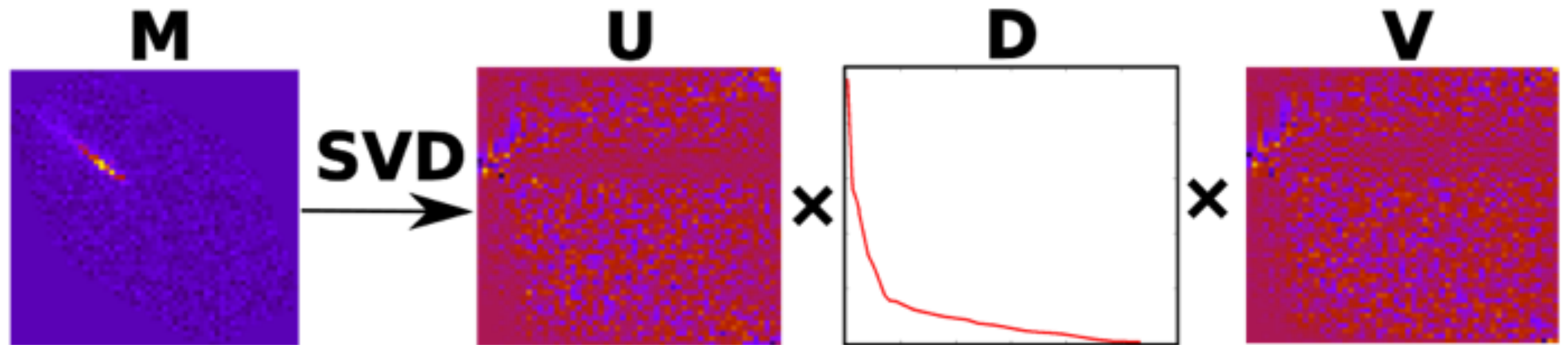
- Apply template method for reconstruction of shower parameters to CTA
- Current methods: comparison of full images
 - huge amount of data makes the process slow
 - can we reduce the images and keep same amount of information?



Single value decomposition

Single value decomposition method

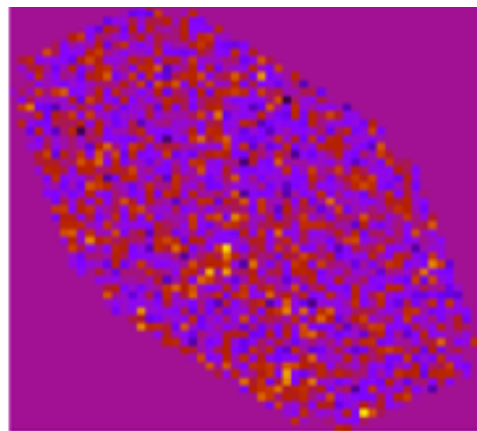
- the image is decomposed into 2 unitary matrices (U,V) and 1 diagonal matrix (D)



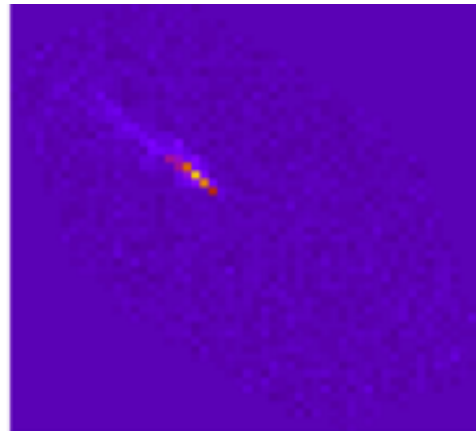
- the single values (SV) of the diagonal matrix (D) are highly correlated to the image morphology
- similar images give similar SV

➡ Compare SV instead of full images

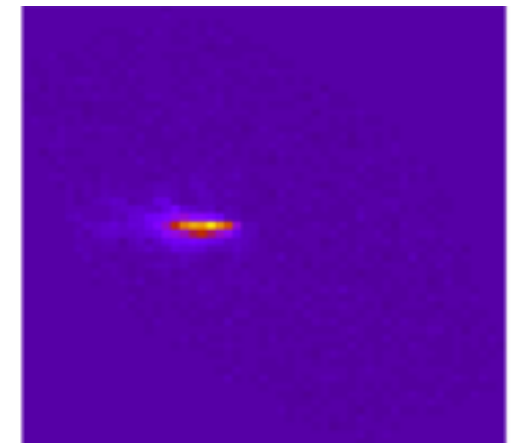
Single value decomposition method: example



Noise

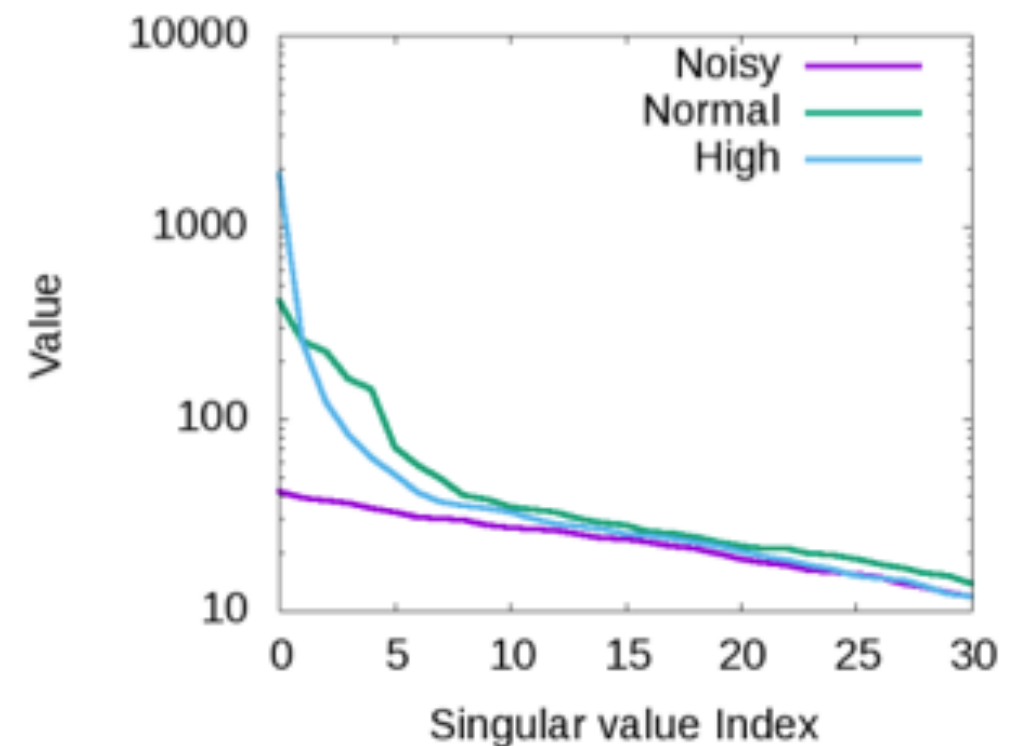


normal S/N



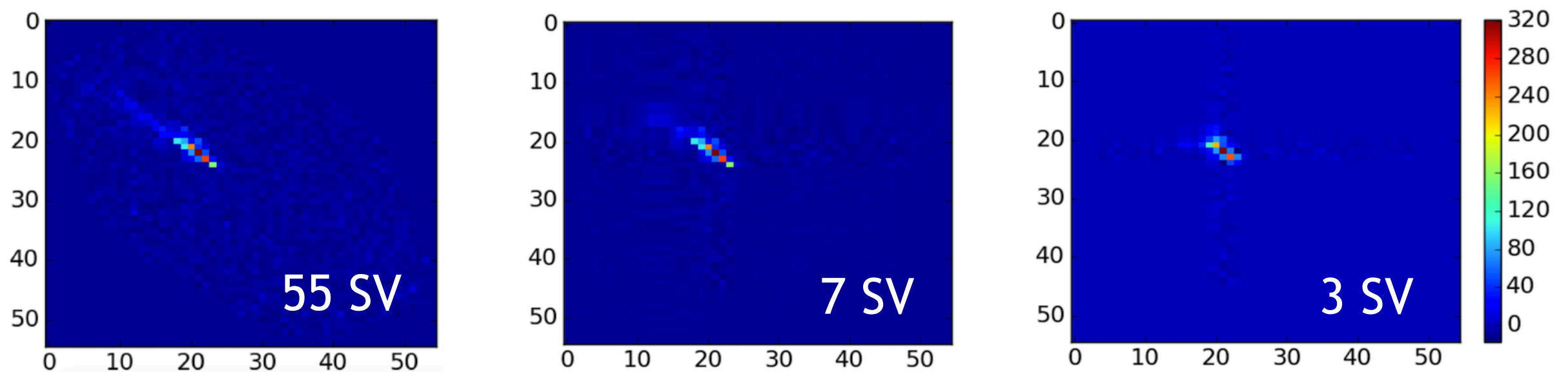
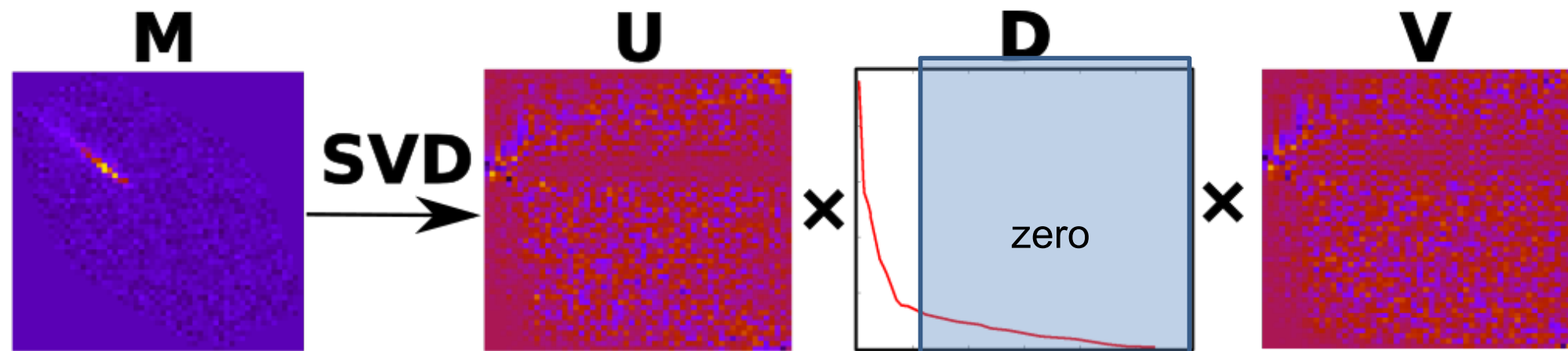
high S/N

- SV spectrum depends on image morphology
- noisy behavior is eventually reached
- keep only the first single values?



Single value decomposition method: example

- Influence of number SV: reconstruction of the image



- last SV account for the noisy part
- keep a sufficient number of SV to not loose information (tests ongoing)

SVD template model

- model parameters:

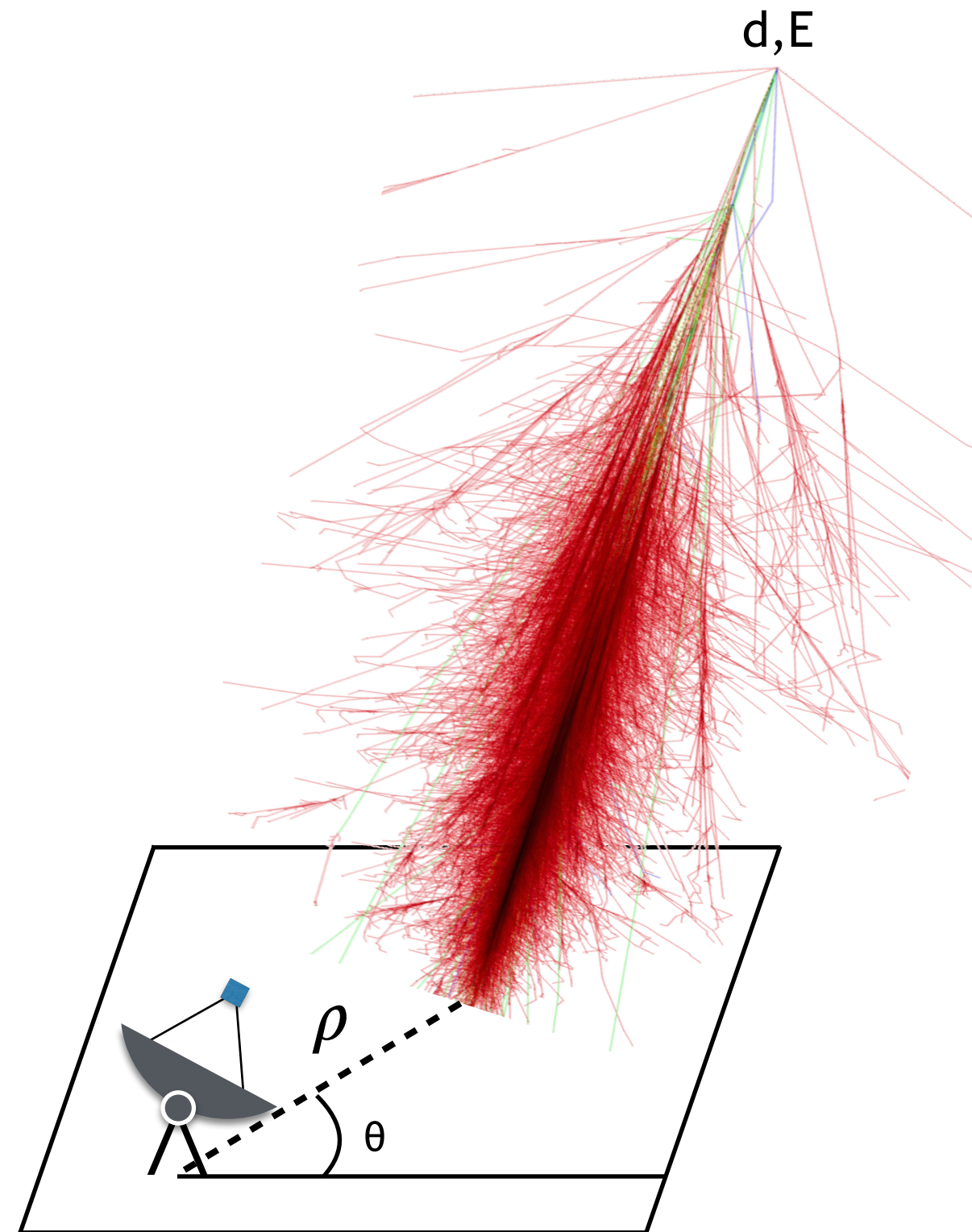
E : energy

d : first interaction depth

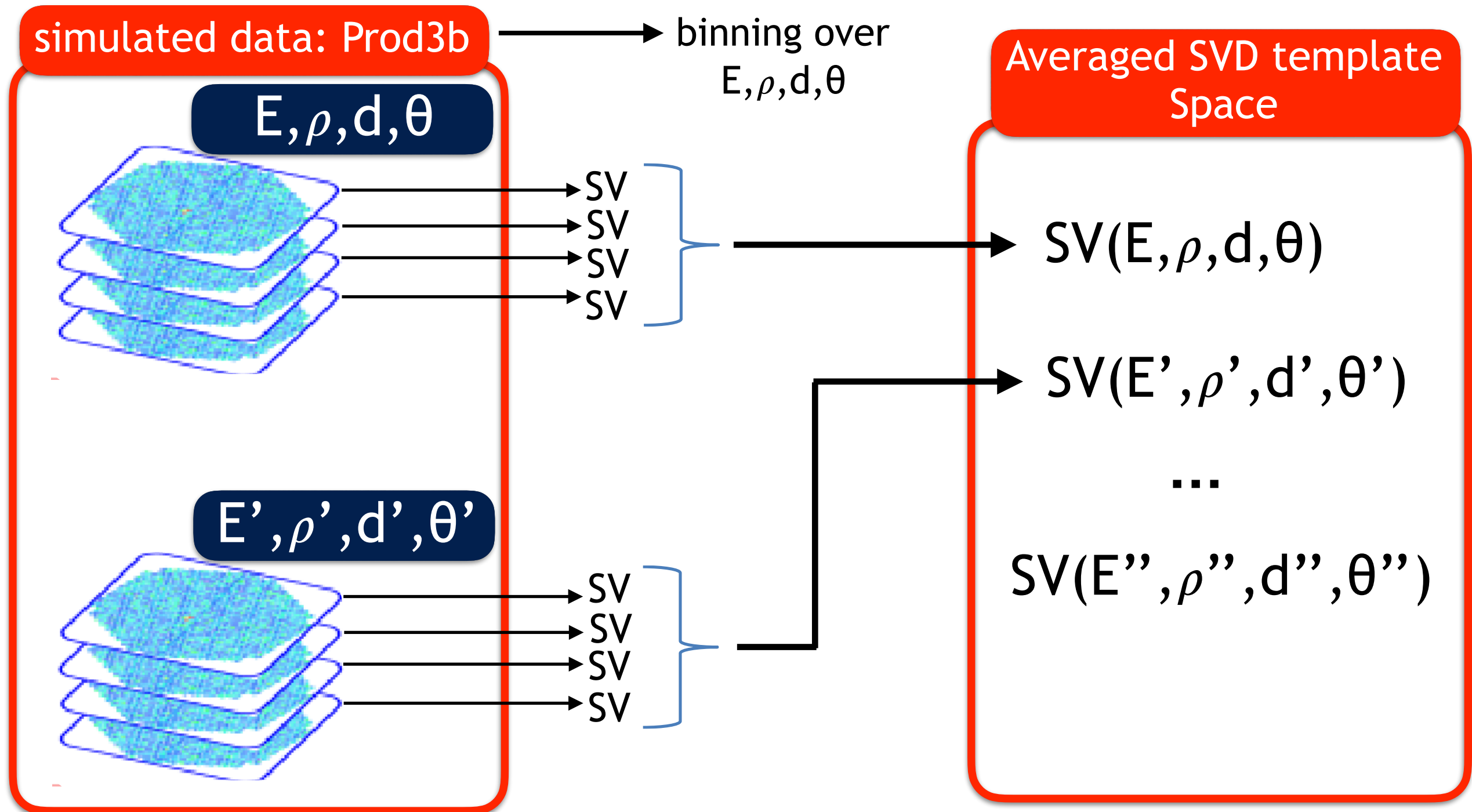
ρ : impact parameter

θ : angular distance

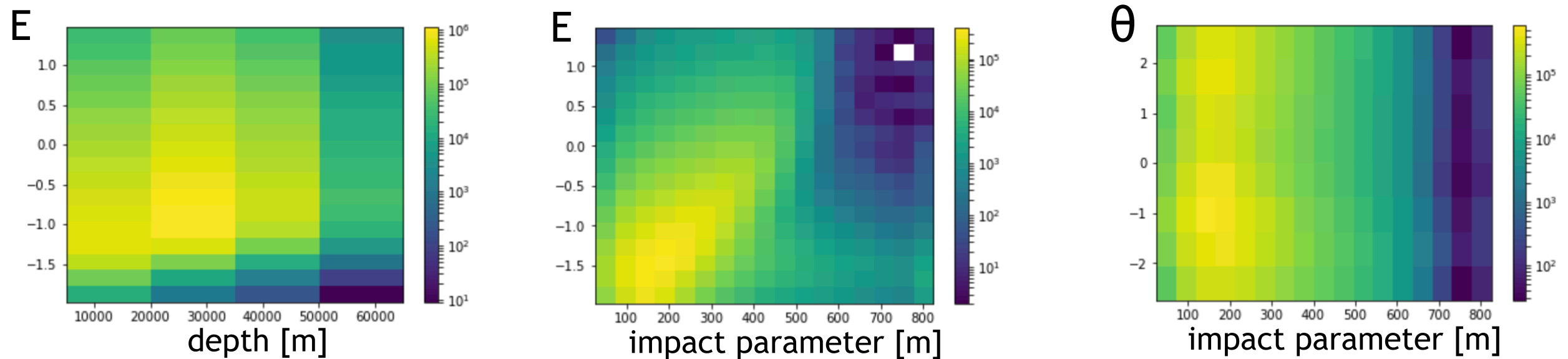
α : distance from camera center



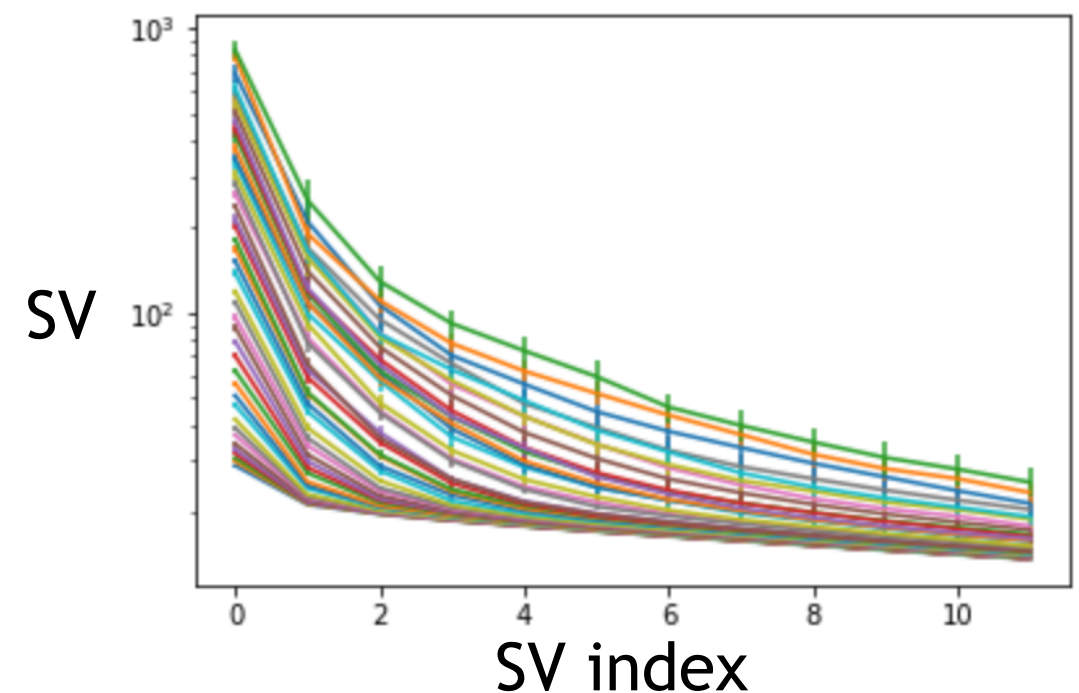
SVD template model creation



SVD template model: binned parameters space

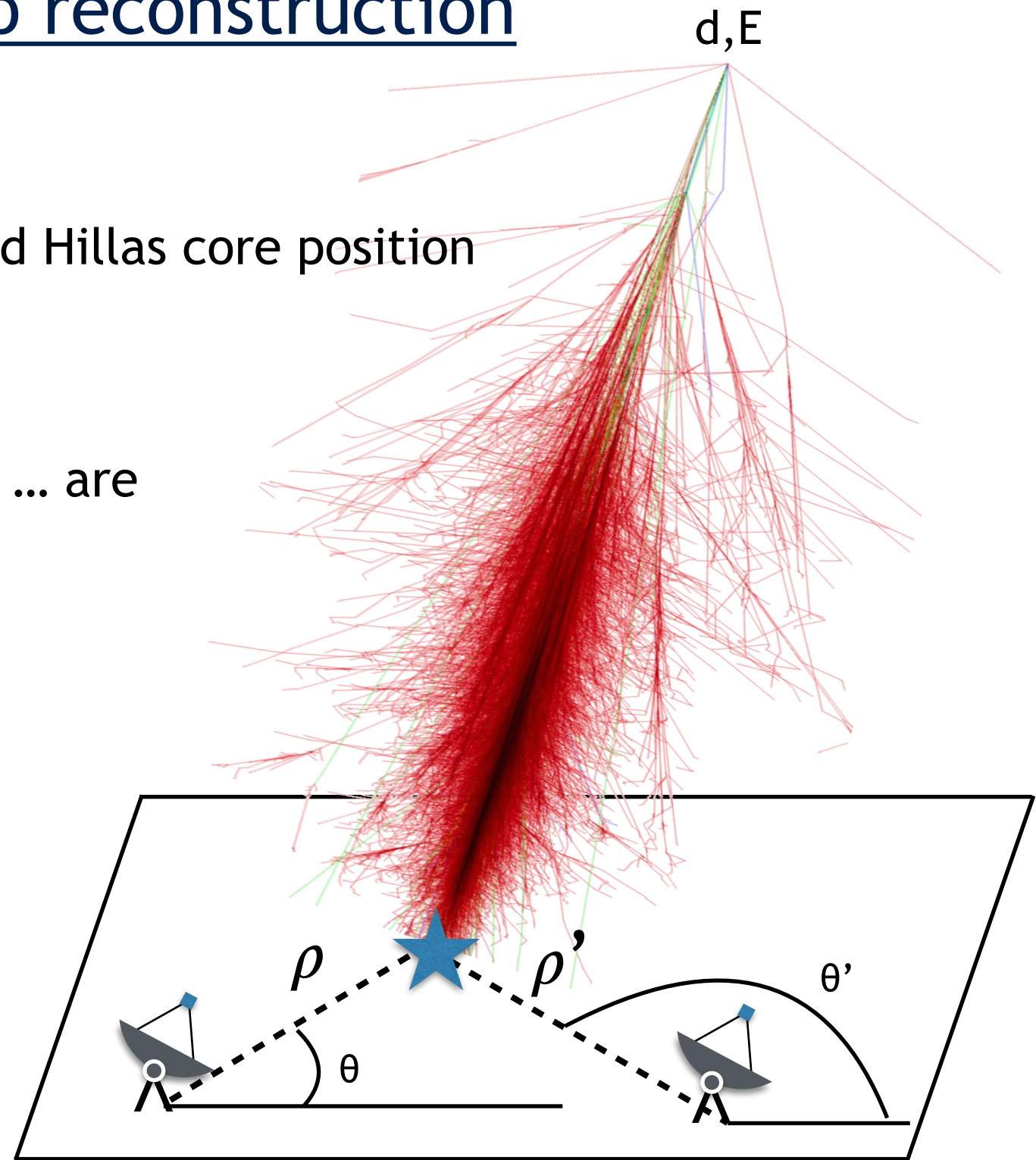


- SV spectra for fixed ρ, d, θ and different E
- higher SV = higher energy
- less fluctuations on lower SV index

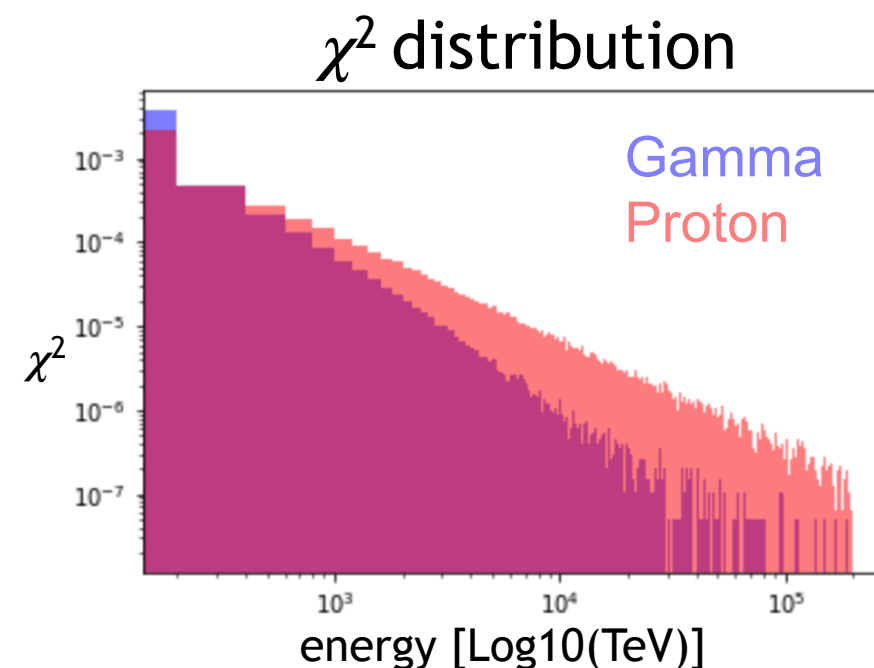
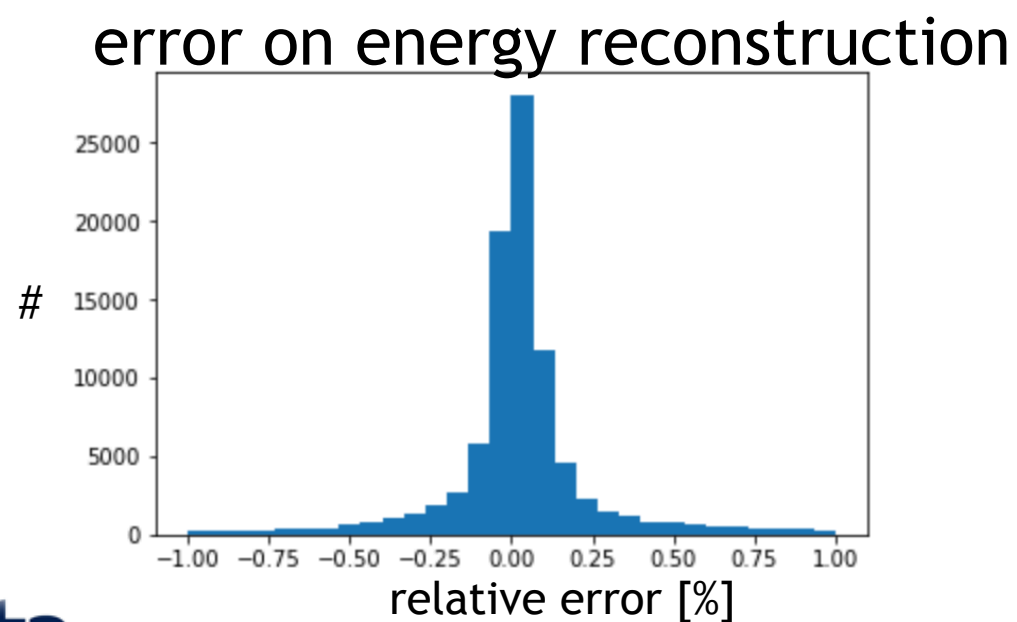
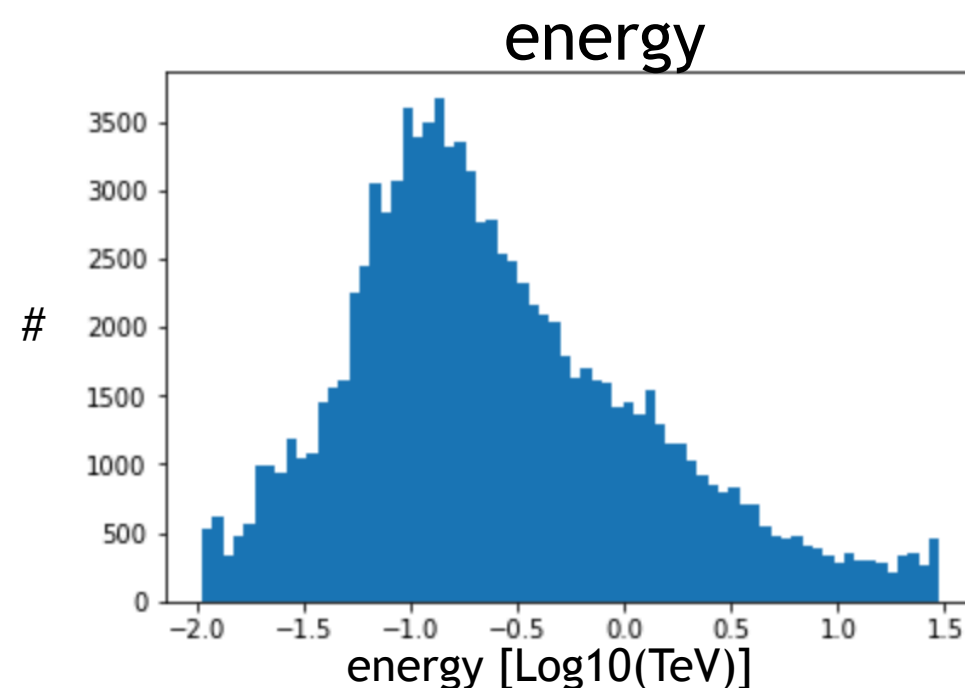
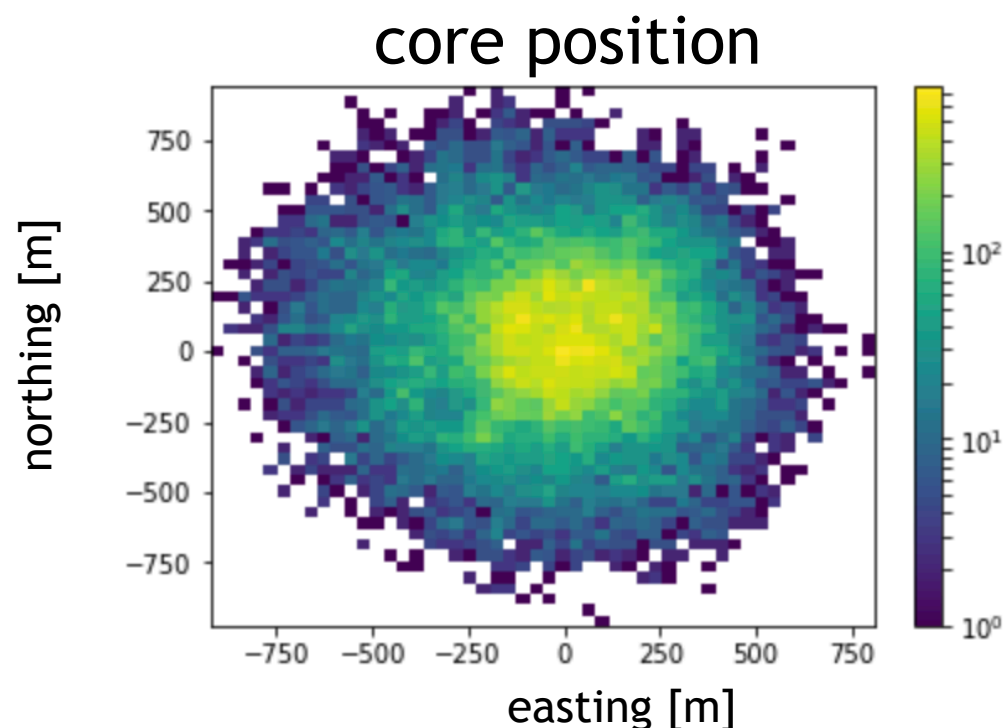


SVD template model: stereo reconstruction

- scan the core position over a grid
- if Hillas successful, scan only around Hillas core position
- for each position:
 - the SV spectra for (ρ, θ) , (ρ', θ') , ... are retrieved
 - all (d, E) combination are tested
- compute χ^2 test to converge to most likely model
- reconstruction of (E, ρ, d)



SVD template model: parameters reconstruction



Conclusion:

- a promising fast template method
- best χ^2 cut removes 70% of protons and 30% of gammas
- error on reconstructed energy: ~15% (30% few months ago)

Ongoing work:

- Number of considered single values (12 in this case)
- Study of the model parameters