

# EXOTIC SPECTROSCOPY



AD POLOSA  
SAPIENZA UNIV. OF ROME.

# X & Z RESONANCES

AMONG THE BEST ESTABLISHED STATES

	$X(3872)$	$Z_c^{\pm,0}(3900)$	$Z_c^{\pm,0}(4020)$	$Z_b^{\pm,0}(10610)$	$Z_b^{\pm,0}(10650)$
	$D^0 \bar{D}^{*+}$	$\bar{D}^0 D^{*+}$	$\bar{D}^{*0} D^{*+}$	$\bar{B}^0 B^{*+}$	$\bar{B}^{*0} B^{*+}$
$\delta$	$\approx 0$	+7.8	+6.7	+2.7	+1.8

(VALUES IN MeV.)

~ EVERYONE AGREES THAT THEY ARE  
 $Q\bar{Q}q'\bar{q}$  HELD TOGETHER  
OR JUST CUSPS (??)

# BINDING 4-QUARKS

SUPPOSE 4 QUARKS ARE PRODUCED (PROMPT OR IN SOME HEAVY MESON DECAY):  $Q \bar{Q} q' \bar{q}'$ .

1) THEY FORM  $Q \bar{q}' + \bar{Q} q'$

2) THEY FORM  $Q \bar{Q} + q' \bar{q}'$

THE TWO MESONS FLY AWAY FROM EACH OTHER

3) THEY FORM  $[Q q'] + [\bar{Q} \bar{q}']$

WHAT HAPPENS MAY DEPEND ON INITIAL CONDITIONS.

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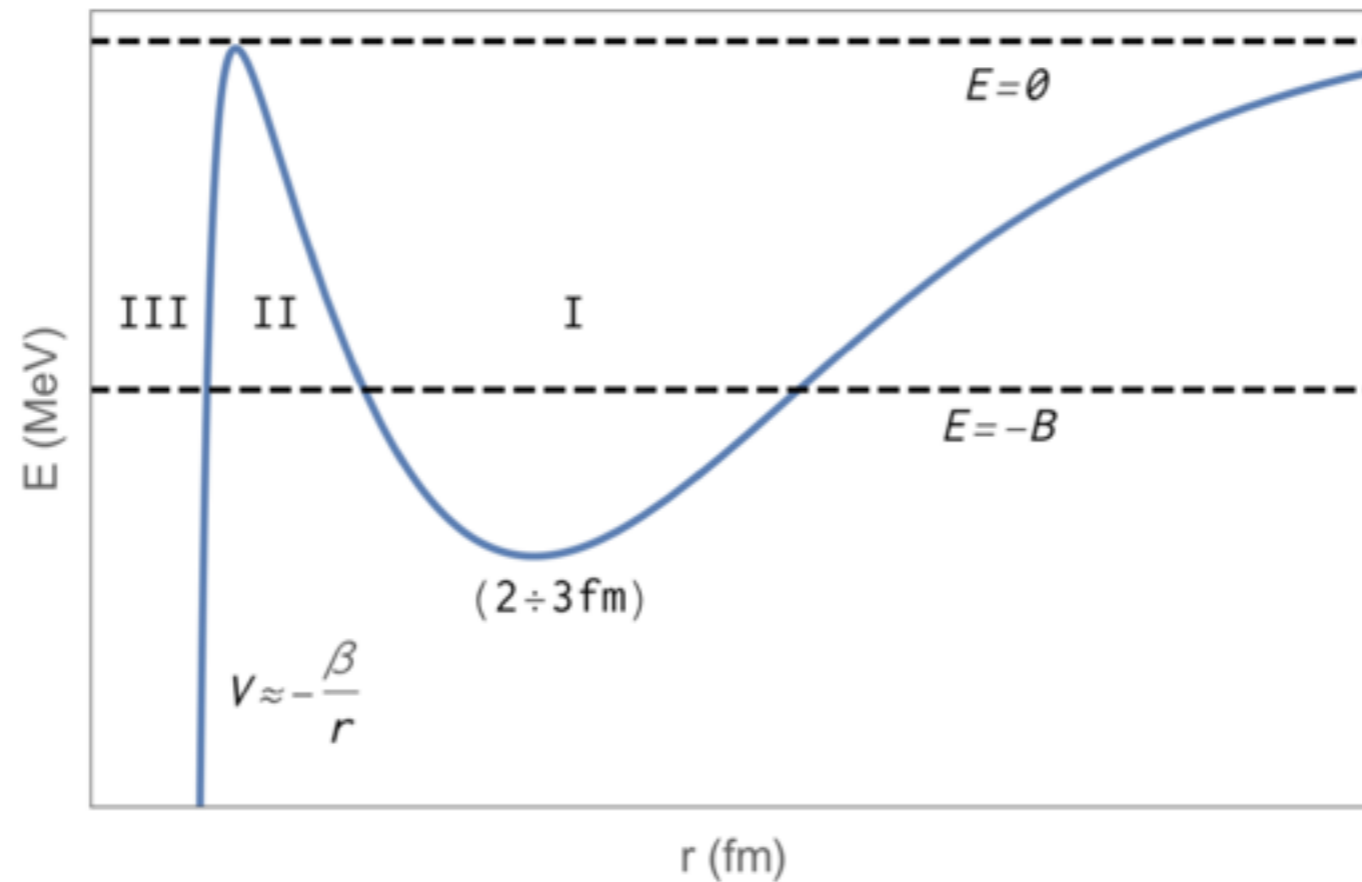
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3.1) THE TWO DIQUARKS ARE SQUEEZED IN A VOLUME  $\lesssim 1 \text{ fm}^3$ . THE SYSTEM MAY BE INDISTINGUISHABLE FROM 1) OR 2)

3.2) THE TWO DIQUARKS ARE SEPARATED IN SPACE...

# HYPOTHETIC DIQUARK POTENTIAL



DISTANCE BETWEEN  
TWO DIQUARKS



THE BARRIER IN II CAN MAKE THE TETRAQUARK  
METASTABLE.

# A BARRIER?

THERE IS NO BARRIER AT  $L=0$ !  
HOWEVER

1) THE HAMILTONIAN

$$H = 2K \left( \mathbf{S}_q \cdot \mathbf{S}_{\bar{q}} + \mathbf{S}_{\bar{q}} \cdot \mathbf{S}_{\bar{q}} \right)$$

DESCRIBES VERY WELL THE PATTERN OF MASS

	<u>Z(4020)</u>	1+-
1++	<u>X(3872)</u>	<u>Z(3900)</u> 1+-

2)  $\mathcal{B}(X \rightarrow J/\psi) \ll \mathcal{B}(X \rightarrow D^0 \bar{D}^{*0})$

[ ALSO NATURAL FOR A HADRON MOLECULE,  
BUT REMEMBER  $\delta > 0$  ]

# A BARRIER?

SUPPOSE THE ENERGY STORED IN THE 4 QUARKS IS DISTRIBUTED TO FORM A DIQUARK-ANTIDIQUARK SYSTEM

$$E = \tilde{m}_1 + \tilde{m}_2 - B$$

FALL APART

$$E = m_1 + m_2 + \delta$$

$m_1$  &  $m_2$  meson masses

$\tilde{m}_1$  &  $\tilde{m}_2$  diquark masses.

**VERY BROAD STATES**

BARRIER

LIGHT QUARKS SWAP THROUGH THE BARRIER

$$T \propto e^{-2\sqrt{2m_q |B|} l}$$

**NARROW STATES**



## FINAL STATES

$$\Gamma \approx \frac{\pi^5}{2a^3} \frac{(\tilde{m}|B|)^{3/2}}{m_q m^{3/2}} \mathcal{T} \sqrt{\delta}$$

$$= A(a, m, \tilde{m}, B) \sqrt{\delta}$$

Rewrite  $A$  in terms of  $F$  (leaving aside numerical constants which appear both in  $Z_c/Z_b$  decays)

$$F_Q = \frac{(\tilde{m}|B|)^{3/2}}{l_Q^3 m^{3/2}} R_Q^{-1} \exp(-2\sqrt{2m_Q|B_Q|}l_Q)$$

↑ taken from data

ARE THERE ANY SOLUTIONS TO THE EQUATION?

$$F_Q = F_c$$

## FINAL STATES: DATA

$$\frac{\Gamma(X \rightarrow \psi \rho)}{\Gamma(X \rightarrow DD^*)} = \frac{\tau_{\psi \rho}}{\tau_{DD^*}} R_c$$

$$\frac{\Gamma(Z'_6 \rightarrow \gamma(1S)\pi)}{\Gamma(Z'_6 \rightarrow B^* B^*)} = \frac{\tau_{\gamma \pi}}{\tau_{B^* B^*}} R_b$$

$$R_c^{\text{exp}} \sim 10^{-3}; \quad R_b^{\text{exp}} \sim 10^{-4}$$

FOR US

$$R_Q \equiv \left[ \frac{\exp(-\sqrt{2m_Q |B|} l)}{\exp(-\sqrt{2m_q |B|} l)} \right]^2$$

## FINAL STATES

$$\Gamma \approx \frac{\pi^5}{2a^3} \frac{(\tilde{m}|B|)^{3/2}}{m^{5/2}} T \sqrt{\delta}$$
$$= A(a, m, \tilde{m}, B) \sqrt{\delta}$$

Rewrite  $A$  in terms of  $F$  (leaving aside inessential numerical constants)

$$F_Q = \frac{(\tilde{m}|B|)^{3/2}}{l_Q^3 m^{5/2}} R_Q^{-1} \exp(-2\sqrt{2m_Q|B_Q|}l_Q)$$

↑ taken from data

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## CONSTANT A?

WE USE THE CONSTITUENT QUARK MASS VALUES (MeV)

$$m_c = 1710 \quad m_b = 5043$$

$$\tilde{m}_c = 1976 \quad \tilde{m}_b = 5815$$

$$-B_c = M_X - 2\tilde{m}_c \approx -100$$

$$l_c = 2fm \text{ (see the barrier)}$$

$$\text{Require } B_b \approx 2.5 B_c$$

We find then

$$A_b = A_c$$

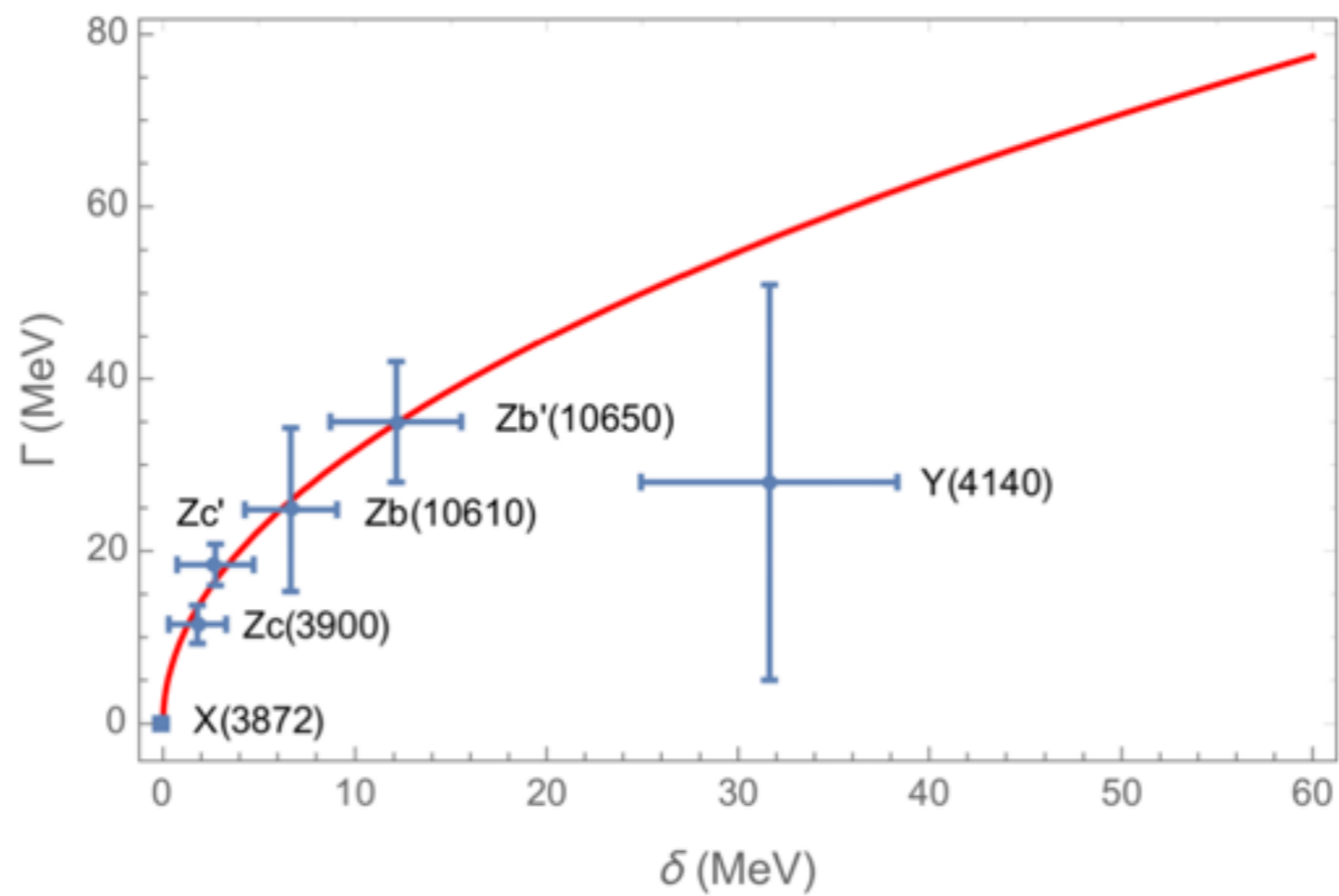
provided that

$$l_b \approx 0.8 l_c$$

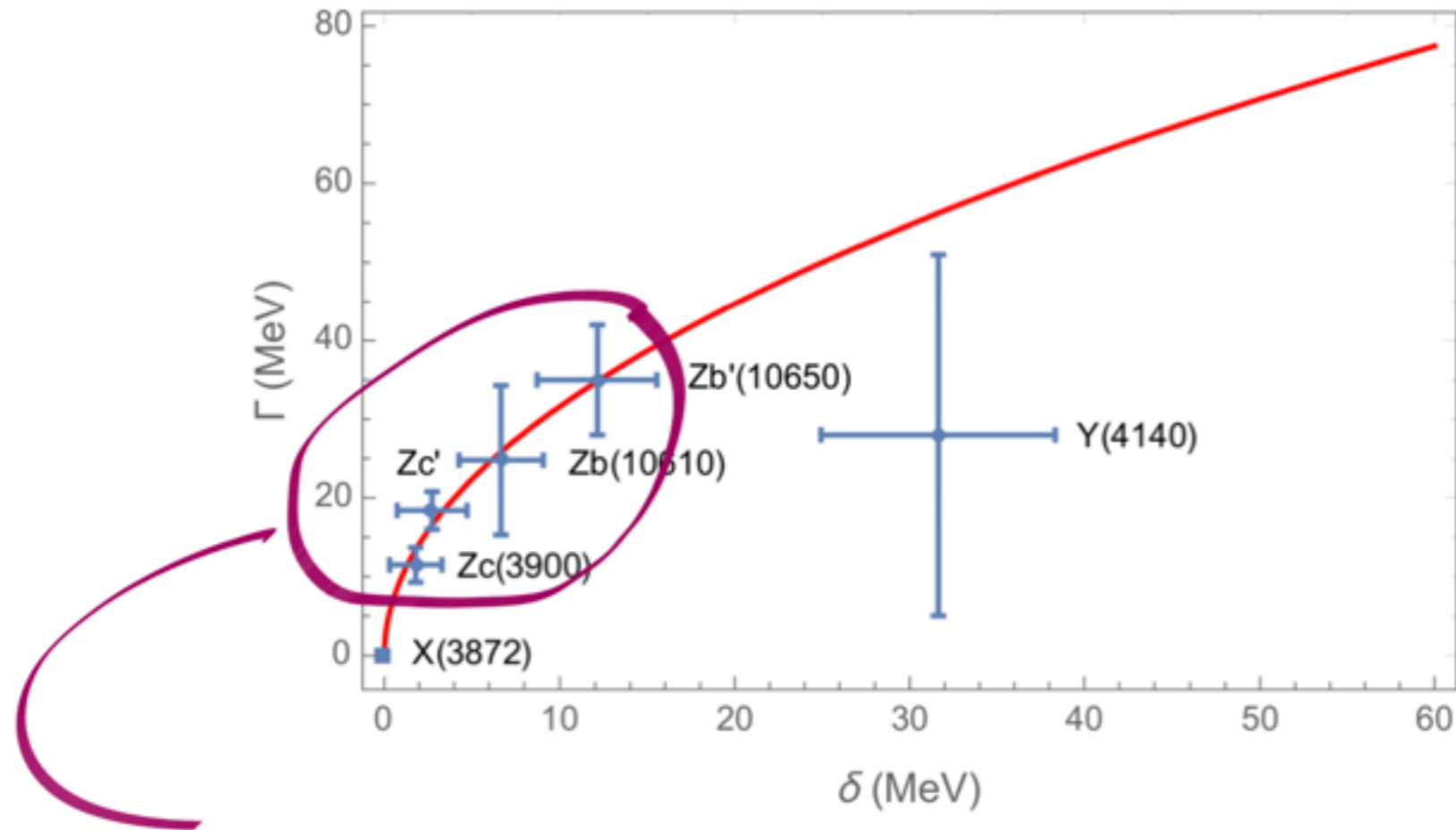
$$\text{THUS } \Gamma = A\sqrt{\delta}$$

WITH CONSTANT A'''

$$\underline{\Gamma = A\sqrt{\delta} ?}$$



$$\underline{\Gamma = A\sqrt{\delta} ?}$$



*Zc & Zb with same A,*

[ OBSERVED ORIGINALLY BY  
ESPOSITO, PILLONI, ADP  
PLB 758 (2016) 292 ]

## OTHER CONSEQUENCES

THE TETRAQUARK IS A TWO-SCALES SYSTEM

- 1) THE SIZE OF A DIQUARK  $\tilde{r}$
- 2) THE SIZE OF THE DIQUARK-ANTI-DIQUARK BOUND STATE  $r$

$$\lambda = r/\tilde{r} > 1$$

AN APPROPRIATE CHOICE OF  $\lambda$  GIVES

$$M(X_u) - M(X_d) \cong 0$$

[Maiani - ADP - Riquer  
PLB778 (2018) 247  
1803.06883]

# $X_u - X_d$ DEGENERACY

BECAUSE OF THIS DEGENERACY

1)  $X_d$  &  $X^\pm$  HAVE ONLY CHARMONIUM DECAY MODES ( $D^+ \bar{D}^{*-}$ ,  $D^+ \bar{D}^{*0}$  TOO HEAVY)

2)  $X_u$  &  $X_d$  GET MIXED

$$X_1 = C\phi \frac{X_u + X_d}{\sqrt{2}} + S\phi \frac{X_u - X_d}{\sqrt{2}}$$

$$X_2 = -S\phi \frac{X_u + X_d}{\sqrt{2}} + C\phi \frac{X_u - X_d}{\sqrt{2}}$$

Mass eigenstates in the isospin basis.

$X^\pm$  should be found only in  $\psi/\omega$  modes.

The prejudice is that  $\Gamma(X^0 \rightarrow \psi \rho^0) \simeq \Gamma(X^\pm \rightarrow \psi \rho^\pm)$



## COMPARISON TO DATA

$$R^0(B^0) = \frac{B^0 \rightarrow k^0 \chi^0 \rightarrow k^0 \psi 3\pi}{B^0 \rightarrow k^0 \chi^0 \rightarrow k^0 \psi 2\pi} = 1.4 \pm 0.6$$

$$R^0(B^+) = \frac{B^+ \rightarrow k^+ \chi^0 \rightarrow k^+ \psi 3\pi}{B^+ \rightarrow k^+ \chi^0 \rightarrow k^+ \psi 2\pi} = 0.7 \pm 0.4$$

ISOSPIN  
VIOLATING  
MODES

$$R^-(B^0) = \frac{B^0 \rightarrow k^+ \chi^- \rightarrow k^+ \psi \rho^-}{B^0 \rightarrow k^0 \chi^0 \rightarrow k^0 \psi \rho^0}$$

$$R^+(B^+) = \frac{B^+ \rightarrow k^0 \chi^+ \rightarrow k^0 \psi \rho^+}{B^+ \rightarrow k^+ \chi^0 \rightarrow k^+ \psi \rho^0}$$

MODES WITH  $\chi^\pm$

$$\left. \begin{array}{l} R^-(B^0) \stackrel{!}{\leq} 1 \\ R^+(B^+) \stackrel{!}{\leq} 0.5 \end{array} \right\} \text{exclusions.}$$

# TWO AMPLITUDES

$$\underbrace{\bar{b}d}_{B^0} \rightarrow \bar{c}c\bar{s} + (d\bar{d} \vee u\bar{u}) + d$$

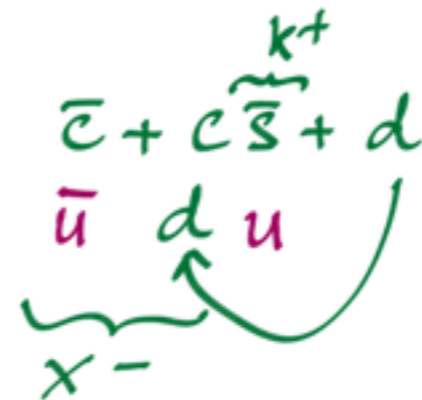
if  $k$  is formed from  $\bar{s}$  + spectator  $d$  :  $A_1$   
 " " " " " " + "sea"  $d$  :  $A_2$

$$\text{Amp}(B^0 \rightarrow X_d K^0) \sim A_1 + A_2$$

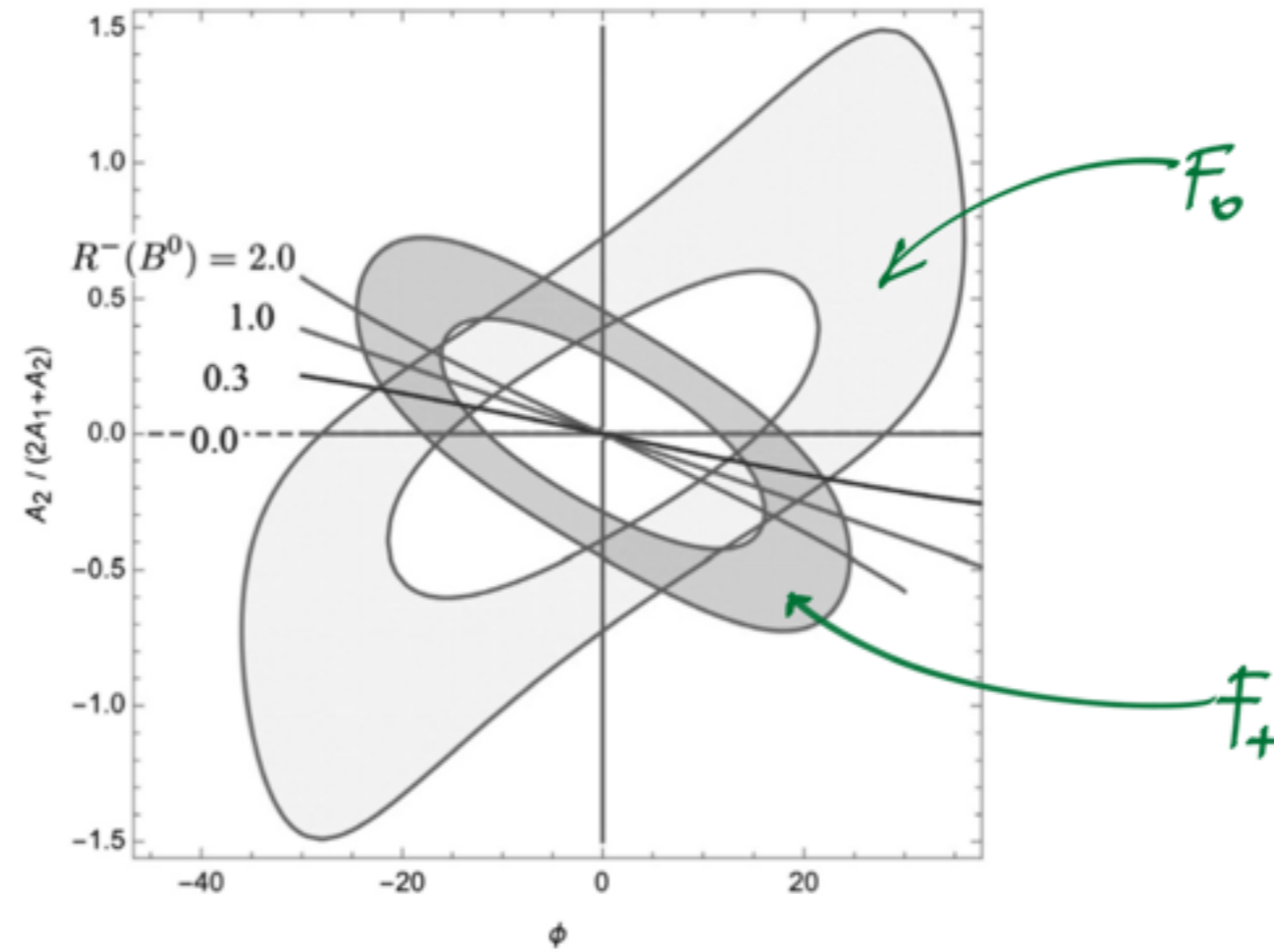
$$\text{Amp}(B^0 \rightarrow X_u K^0) \sim A_1$$

$$\text{Amp}(B^0 \rightarrow X^- K^+) \sim A_2$$

Similarly for  $B^+$



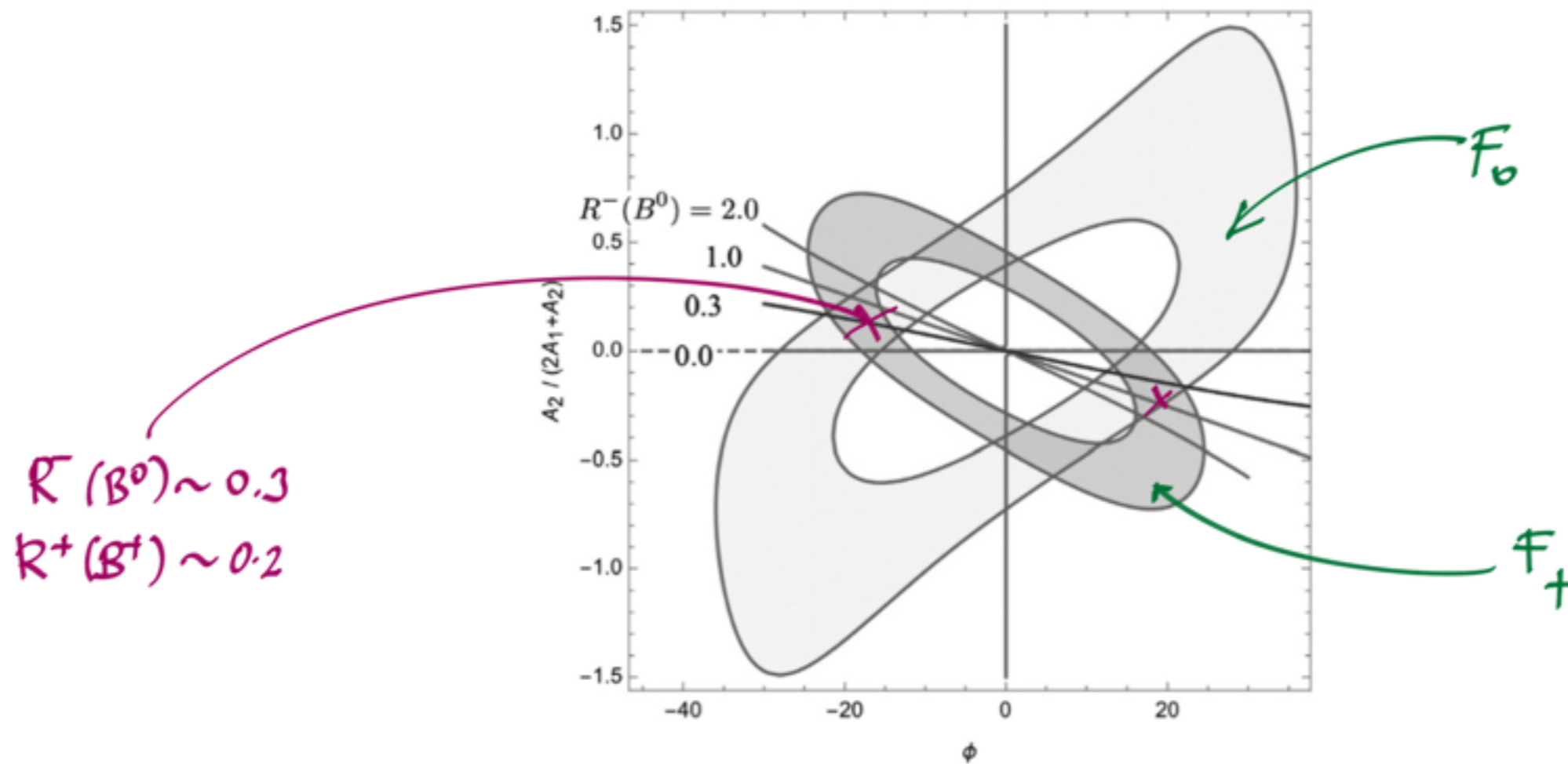
# OTHER CONSEQUENCES



$$R^0(B^0) = \frac{I=1}{I=0} \propto F_0\left(\phi, \frac{A_2}{2A_1 + A_2}\right) \frac{p_e}{p_w}$$

$$R^0(B^+) \propto F_+\left(\phi, \frac{A_2}{2A_1 + A_2}\right) \frac{p_e}{p_w}$$

# OTHER CONSEQUENCES



$R^-(B^0) \sim 0.3$   
 $R^+(B^+) \sim 0.2$

OVERLAP REGIONS CORRESPOND TO PARAMETERS  $(\phi, A_1, A_2)$  REPRODUCING EXPERIMENTAL VALUES FOR BOTH  $F_+$  &  $F_0$ .

HOWEVER SOLUTIONS WITH  $\phi \approx 0$  HAVE  $R^-(B^0) \approx 2$  — excluded.

SOLUTIONS WITH  $\phi \approx \pm 20$  HAVE  $R^-(B^0) \lesssim 2$ .

PRESENT LIMIT IS  $R^-(B^0) \lesssim 1$  &  $R^+(B^+) \lesssim 0.5$

## REMARKS

21/03/2018

1. Why  $X^\pm(3872)$  seem to be absent?

Because the  $A_2$  amplitude can be very small, for certain values of  $\phi$

2. Where does the  $\phi$  mixing comes from?

Even a very small  $q\bar{q}$  annihilation amplitude in the tetraquark could produce sizeable mixing if  $M(X_u) \simeq M(X_d)$

3. Where does the  $X_u - X_d$  degeneracy comes from?

If the tetraquark is a system with two length scales,  $l$  and  $\bar{l}$ , their ratio can be chosen so as  $M(X_u) \simeq M(X_d)$

21 / 29

Annex18

## REMARKS

4. Why two length scales?

Because it seems that there is an effective repulsion at very short distances of the diquark - anti-diquark pair.

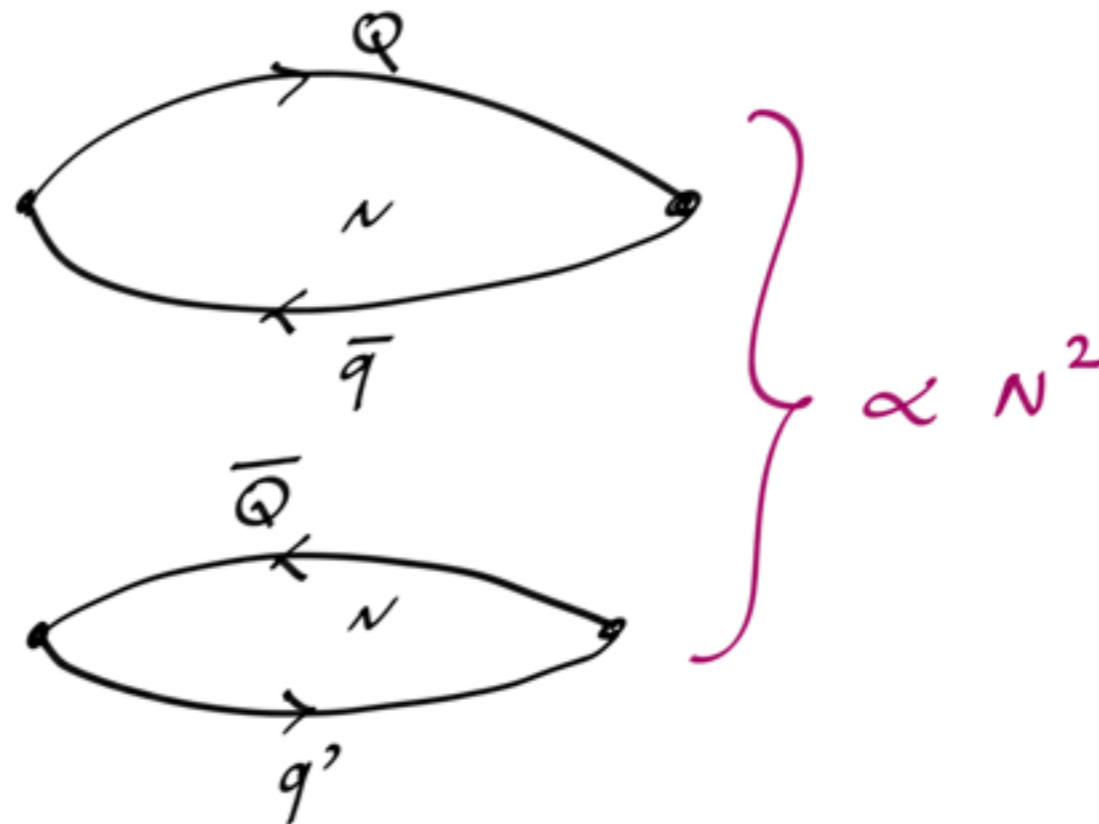
5. Other clues on this repulsion?

- Spin - Spin interactions work as if tetraquarks were segregated at some distance apart.
- Tunneling disfavors  $\psi/\omega$  decays
- A fit  $\Gamma = A\sqrt{s}$  works for both  $Z_c$  and  $Z_x$  resonances.

# THE LARGE- $N$ EXPANSION & TETRAQUARKS

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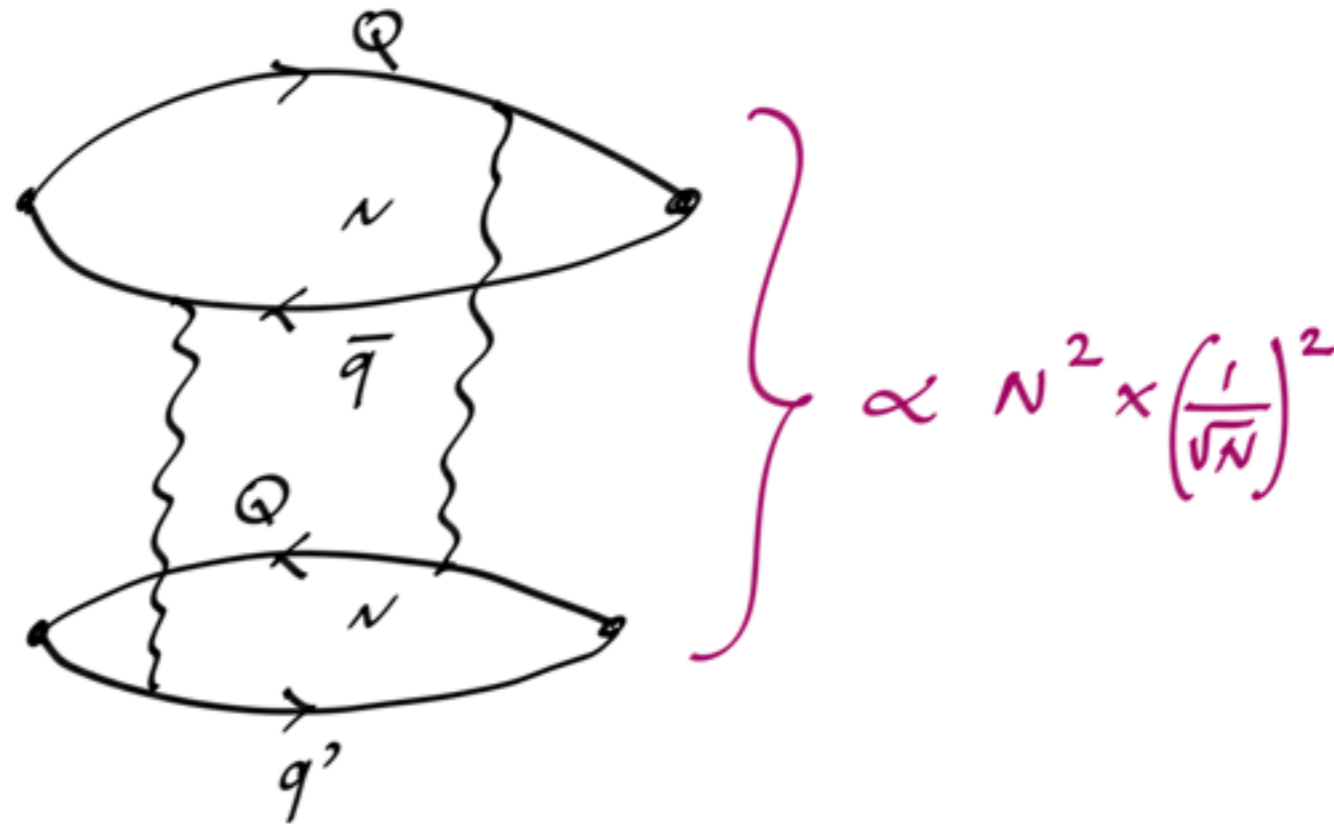
S. WEINBERG, PRL 110 (2013) 261601



# THE LARGE-N EXPANSION & TETRAQUARKS

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S. WEINBERG PRL 110 (2013) 261601



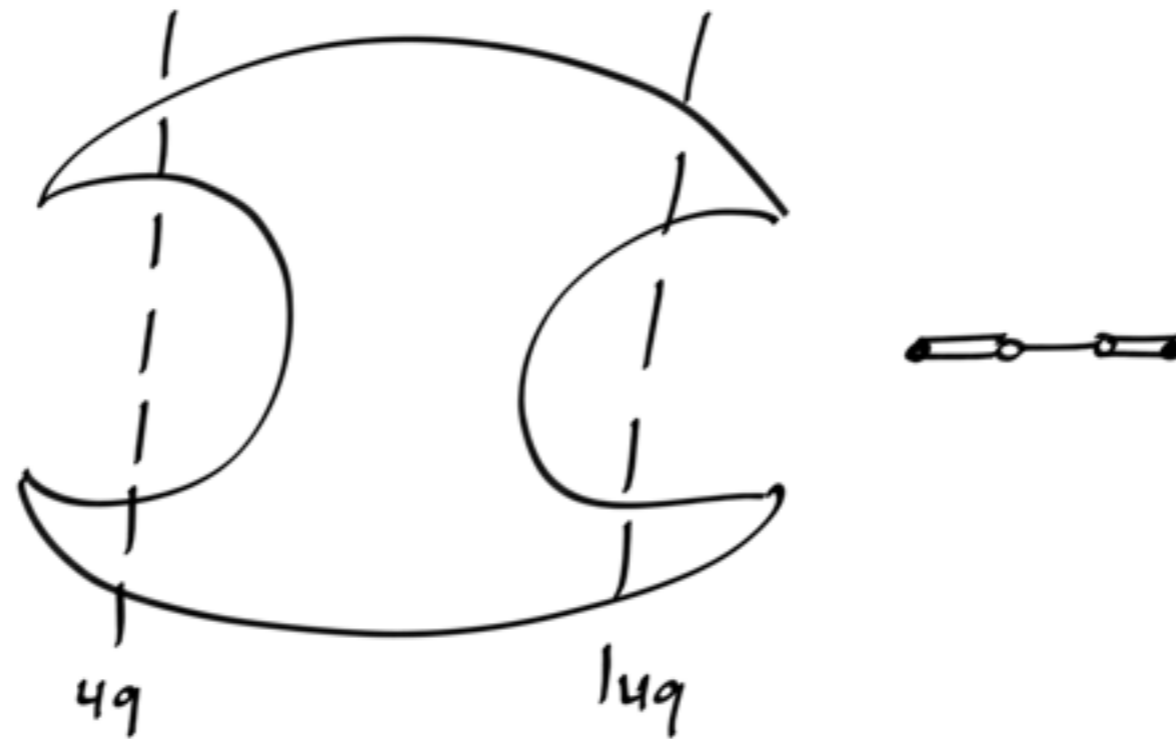
FOR LARGE  $N$  ( $N \rightarrow \infty$ ) THE DIAGRAM W/ NO  
GLUONS WINS — FALL APART DECAY OF THE  
TETRAQUARK. (COLEMAN, WITEN)



# THE LARGE- $N$ EXPANSION & TETRAQUARKS

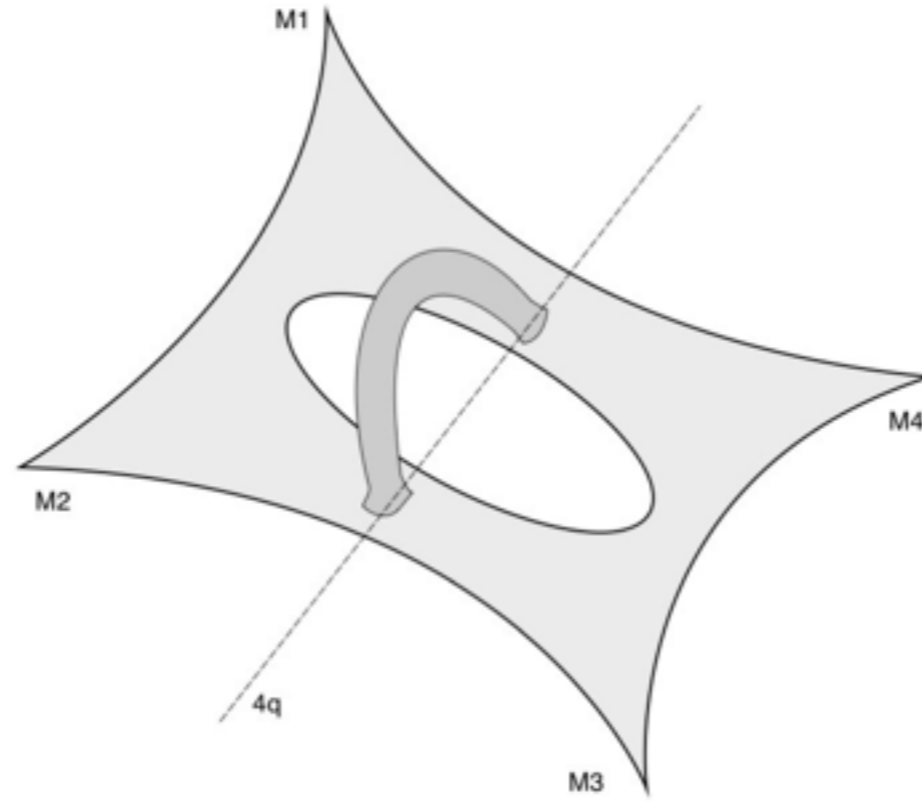
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S. WEINBERG PRL 110 (2013) 261601

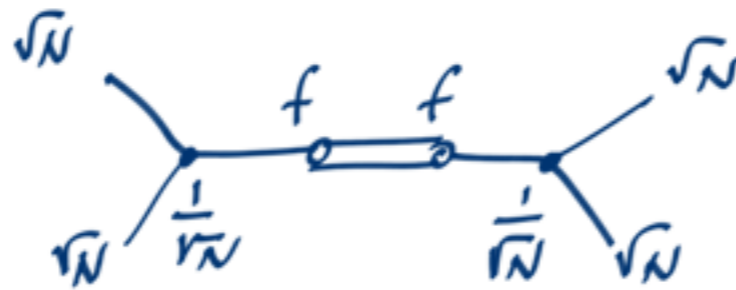


" IF THERE IS A TETRAQUARK MESON POLE  
IN THE CONNECTED PART OF THE PROPAGATOR  
WHAT DIFFERENCE DOES IT MAKE IF ITS  
RESIDUE IS SMALLER WRT THE DISCONNECTED  
PART? "

# NON PLANAR DIAGRAMS



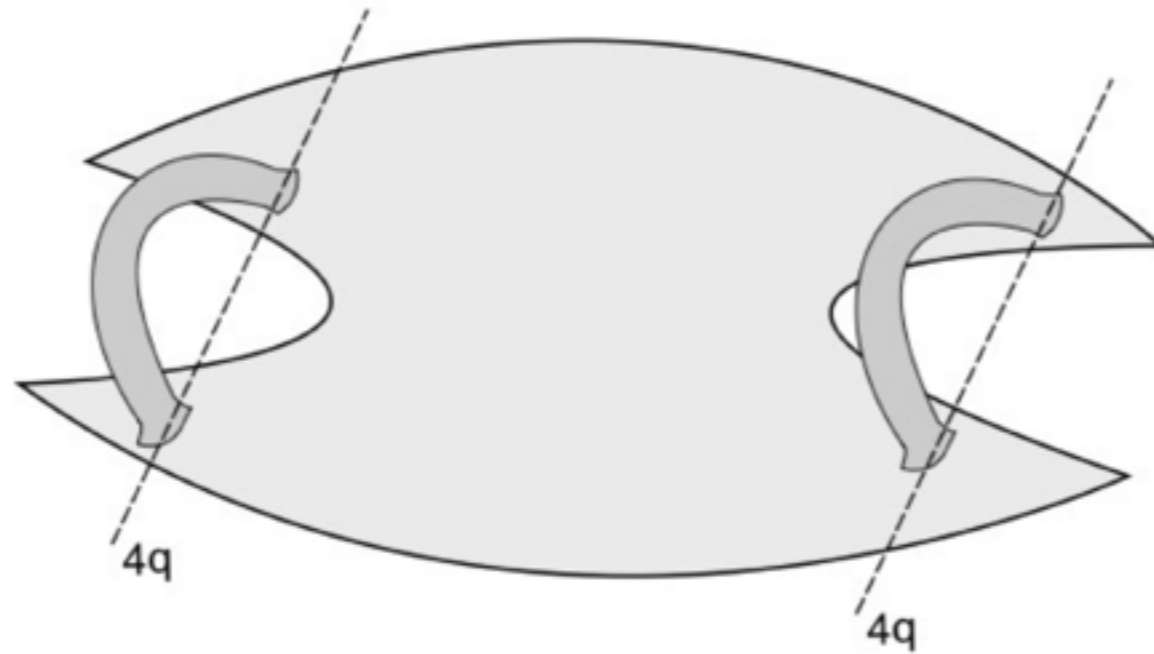
$$N^\alpha = N^{2-L-2H} = N^{2-2-2} = \frac{1}{N^2}$$



$$N f^2 \sim \frac{1}{N^2}$$

$$f \sim \frac{1}{N\sqrt{N}}$$

# NON PLANAR DIAGRAMS



$$N^{2-2-2H} = N^{2-1-4} = N^{-3}$$

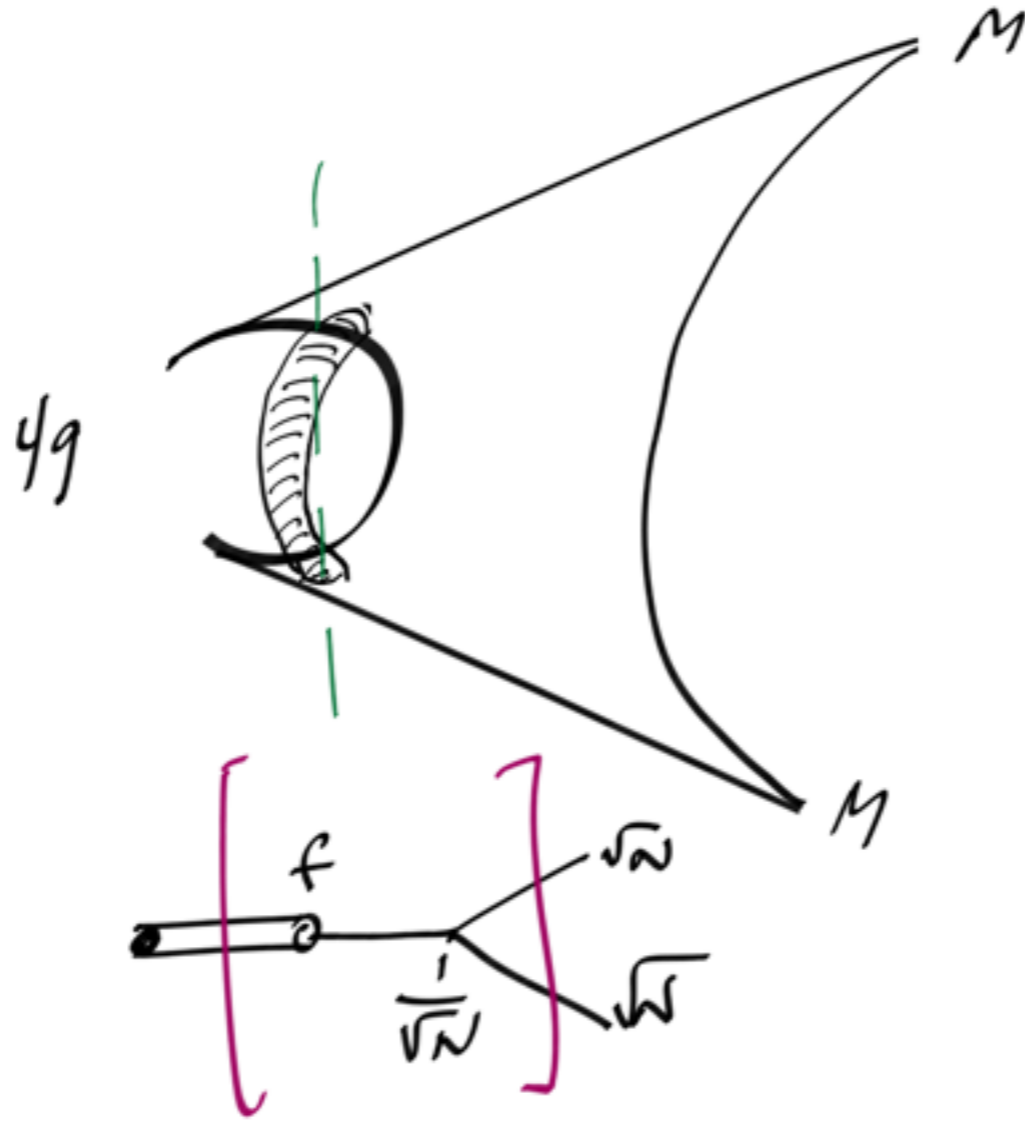
$$f_{4q} \text{ --- } f \text{ --- } f \text{ --- } f_{4q}$$

$$f_{4q}^2 \frac{1}{N^3} \sim \frac{1}{N^3}$$

$$f_{4q} \sim N^0$$

[ OBSERVED IN MAIANI, ADP, RIGUER JHEP 1606(2016)160  
4 1803.06883 ]

# DECAY



$$g \sim f \frac{1}{\sqrt{N}} = \frac{1}{N^2}$$

TETRAQUARKS CAN BE VERY NARROW

# *AUXILIARY SLIDES*



# X(3872)

A  $D^0(0^-) \bar{D}^{*0}(1^-)$  MOLECULE?

Suppose there is some  $V(r)$  between  $D^0$  &  $D^{*0}$

$$V(r) = -g \frac{e^{-r/r_0}}{r} \quad \text{with } r_0 \sim \frac{1}{m_\pi}$$

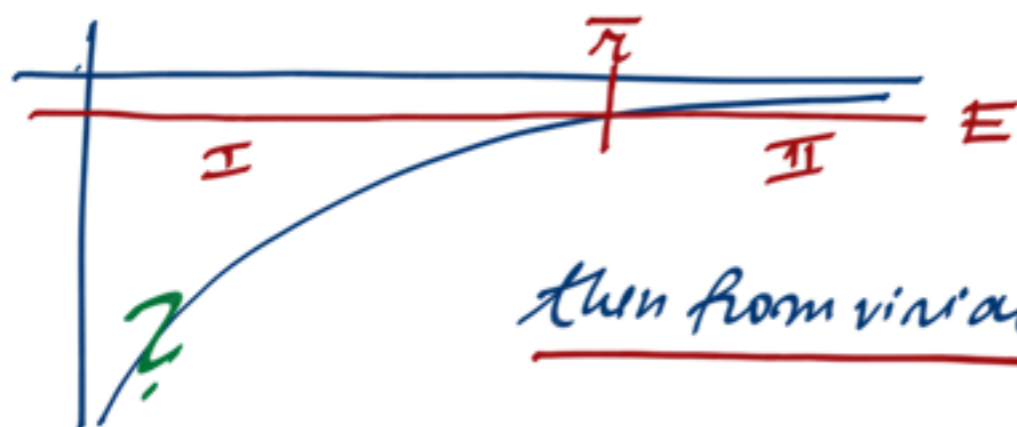
The VIRIAL THEOREM gives

$$2 \langle T \rangle = \left\langle \sum_{i=1}^3 r_i \partial_i V \right\rangle = \left\langle r \frac{\partial}{\partial r} V(r) \right\rangle$$

i.e.

$$\langle H \rangle = -\langle T \rangle + \frac{g}{r_0} \langle e^{-r/r_0} \rangle$$

$$= -\frac{\langle p^2 \rangle}{2m} + \frac{g}{r_0} \exp\left(-\frac{\langle r \rangle}{r_0}\right)$$

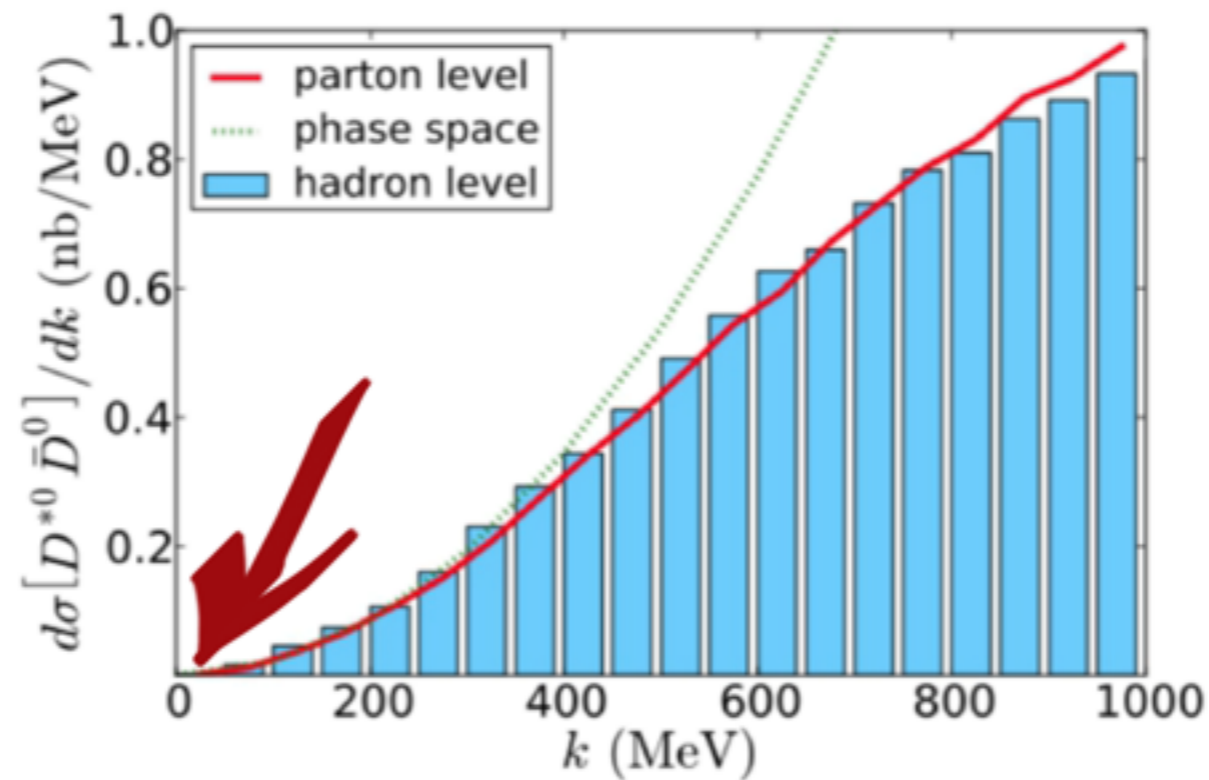


FOR SHALLOW BOUND STATES

$$\langle r \rangle \approx \frac{1}{\sqrt{2m|E|}} \approx 10 \text{ fm} \gg r_0$$

then from virial:  $\sqrt{\langle p^2 \rangle} \approx 2m |E| \approx 20 \text{ MeV}$

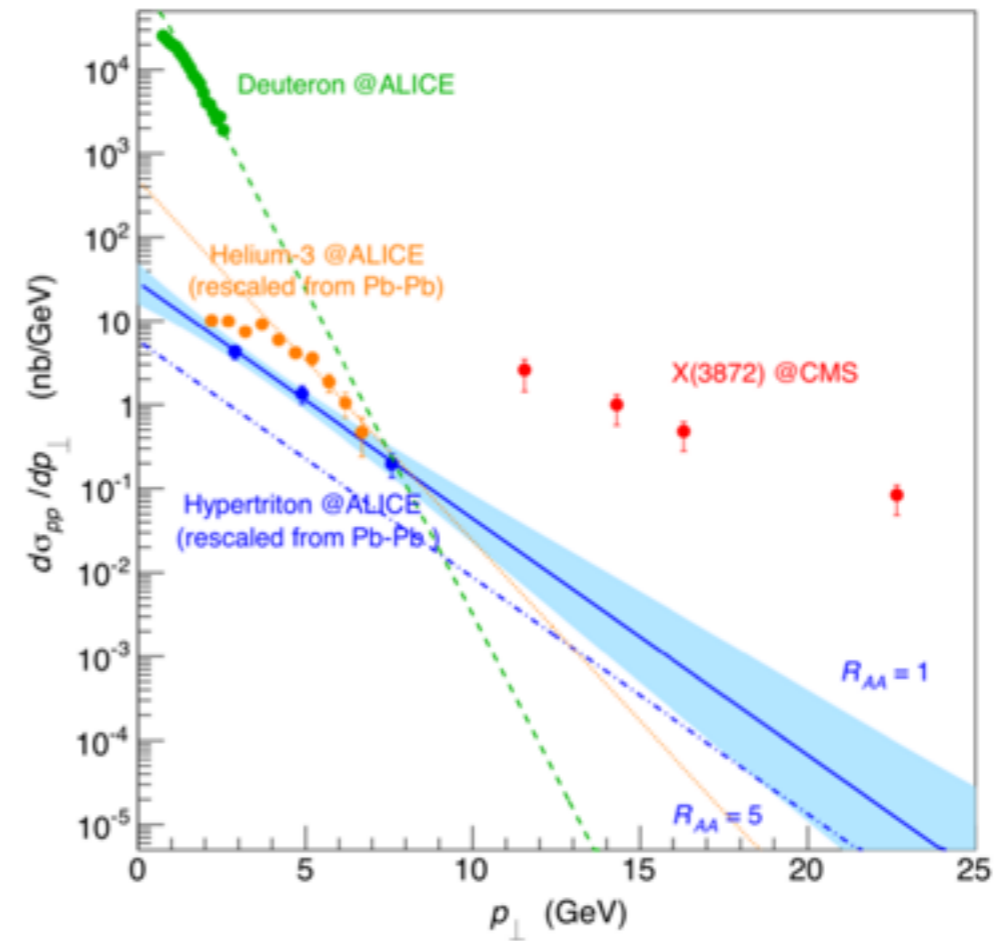
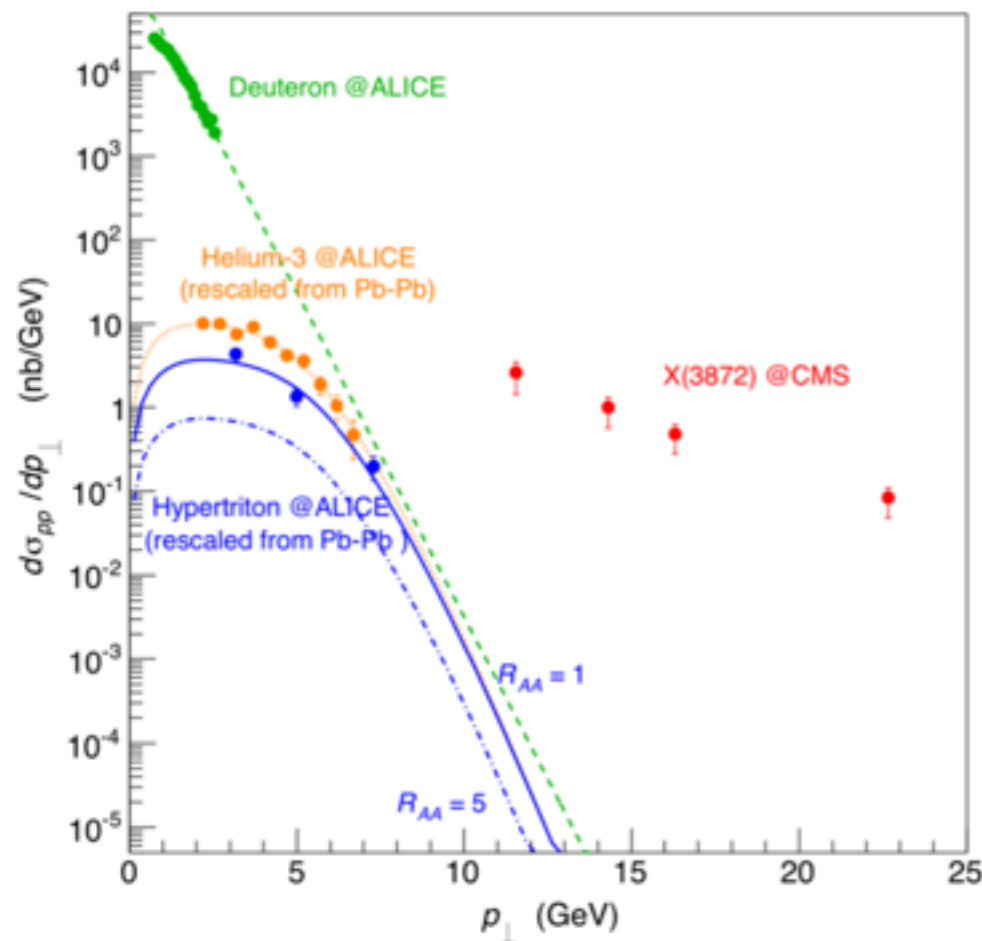
# X PRODUCTION AT HADRON COLLIDERS



$p_T(D^{*0} \bar{D}^0) > 5 \text{ GeV}$  and  $|\eta(D^{*0} \bar{D}^0)| < 0.6$   
in  $p\bar{p}$  @ 1.96 TeV

FROM ARTOISENET & BRAATEN PRD 81 (2010) 014013  
SAME RESULTS FOUND BY  
BIGNAMINI & AL. PRL 103 (2009) 162001

# X PRODUCTION AT HADRON COLLIDERS



THE X PRODUCTION DOES NOT SEEM COMPARABLE  
TO THAT OF 'REAL' HADRON MOLECULES.  
(What about other states in pp?)

[FROM ESPOSITO ET AL. PRD 92 (2015)]  
1508.00295



## THE $Z_c$ 's & $Z_b$ 's

RECALL

$$\chi_u \sim \frac{A}{\sqrt{2}} (D^0 \bar{D}^{*0} - D^{*0} \bar{D}^0)$$

$$\chi_d \sim \frac{A}{\sqrt{2}} (D^+ \bar{D}^{*-} - D^{*-} \bar{D}^+)$$

SIMILARLY

$$Z_c \sim \frac{\beta}{\sqrt{2}} (D^0 \bar{D}^{*0} - D^{*0} \bar{D}^0) + c \underbrace{D^{*0} \times \bar{D}^{*0}}_{\text{phase space forbidden}}$$

The nontrivial dependence  
of BARRIER PENETRATION  
FACTORS FROM LIGHT QUARK SPINS  
ALLOWS  $Z_c \rightarrow DD^*$ .

$Z_c$  HAS NOT (YET?) BEEN OBSERVED IN B DECAYS.  
WE COULD HAVE  $\varphi \approx 0$  ( $\theta \approx 45^\circ$ ) SO THAT  $Z_c$  &  $Z_b$   
CORRESPOND TO  $I=0$  &  $I=1$ , AND SIZEABLE  $R^{0\pm}$   
(as well as  $R^{\pm\mp}$ ).

## OPEN QUESTIONS

—  $Z_c^{\pm,0}, Z_c'^{\pm,0}$  IN B DECAYS?

—  $Z_c^{\pm,0}, Z_c'^{\pm,0}$  IN PROMPT pp COLLISIONS?

[Same question for  $Z_c$ 's]

FINAL STATES LIKE  $J/4 \pi^+$  SHOULD BE FEASIBLE.

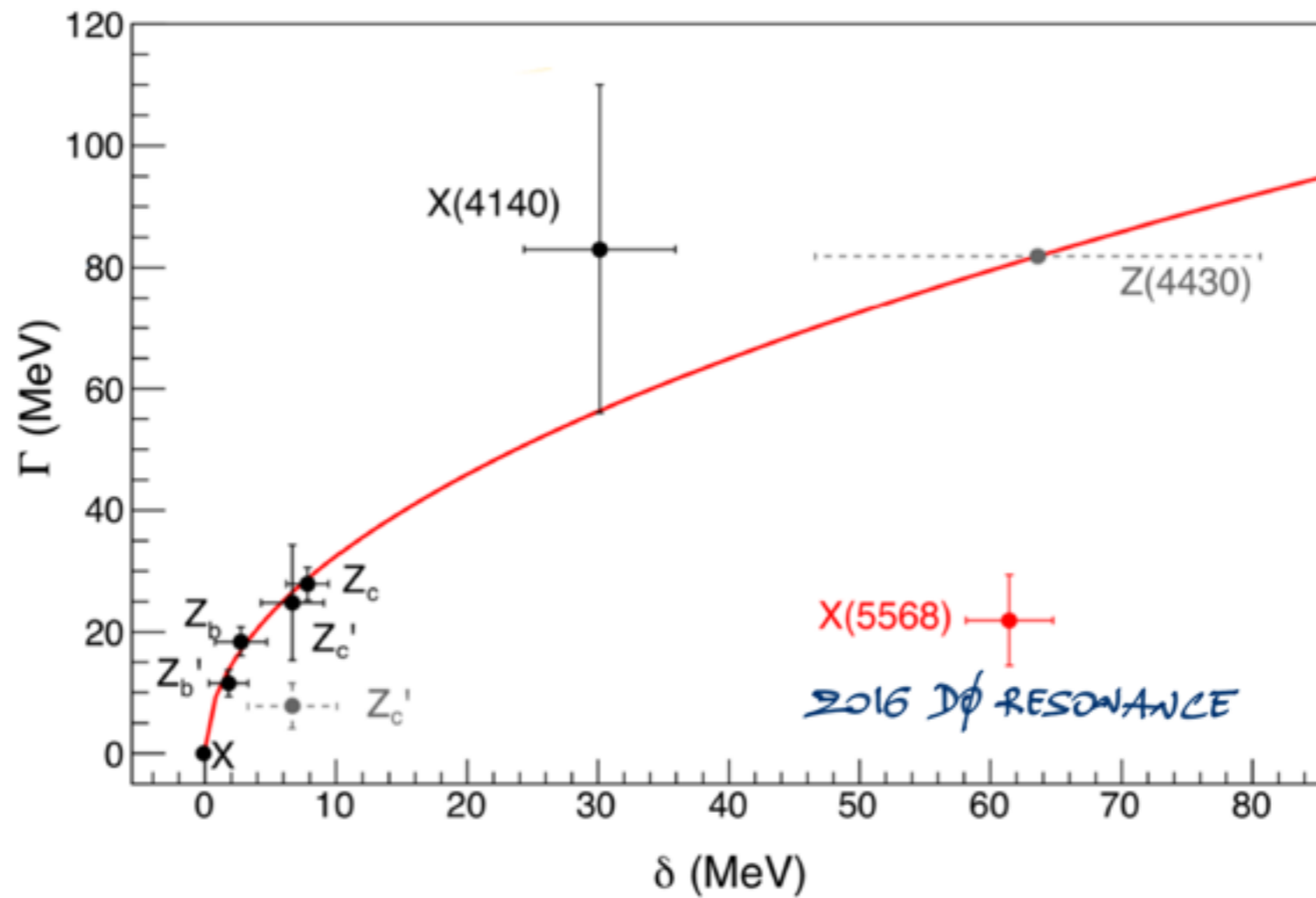
— Which resolution can be needed to measure the mass of the  $X^0$  in  $D\bar{D}^{*0}$  and in  $J/4 p$ ?

$M(X_{\ell}) - M(X_{\ell'})$  could be  $\approx 0$ , but this is worth being investigated.

— What about the  $X_{\ell}^0$  ( $\rightarrow B^0 \bar{B}^{*0}$ )?

# LIFETIME

INDEED THE TOTAL WIDTH OF  $X, Z_c, Z_c'$  STATES APPEARS TO BE DOMINATED BY THEIR DECAYS INTO CLOSE MESON-MESON THRESHOLDS



$$\Gamma = A \sqrt{\delta}$$

[ESPOSITO ET AL.  
PLB 758 (2016) 292]



$$A = (10.3 \pm 1.3) \text{ MeV}^{1/2} \quad \chi^2/\text{DOF} = 1.2/5$$