

# The Dark side of Flavor

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Martti Raidal, Elena Venturini

**based on:**

PRL 119 (2017) 031801 M. Fabbriches, EG, B.Mele

PRD 95 (2017) 035005 EG, M.Raidal, L.Marzola

PRD 94 (2016) 115013 EG, B.Mele, M.Raidal, E.Venturini

PRD 89 (2014) 015008 EG, M.Raidal



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# Outline

- Flavor model: theoretical framework
  - Yukawa couplings as effective couplings
  - generated by a Dark Sector
  - solution to the flavor hierarchy problem
- Phenomenological implications
- New FCNC signatures
- Conclusions

# Flavor Hierarchy Problem

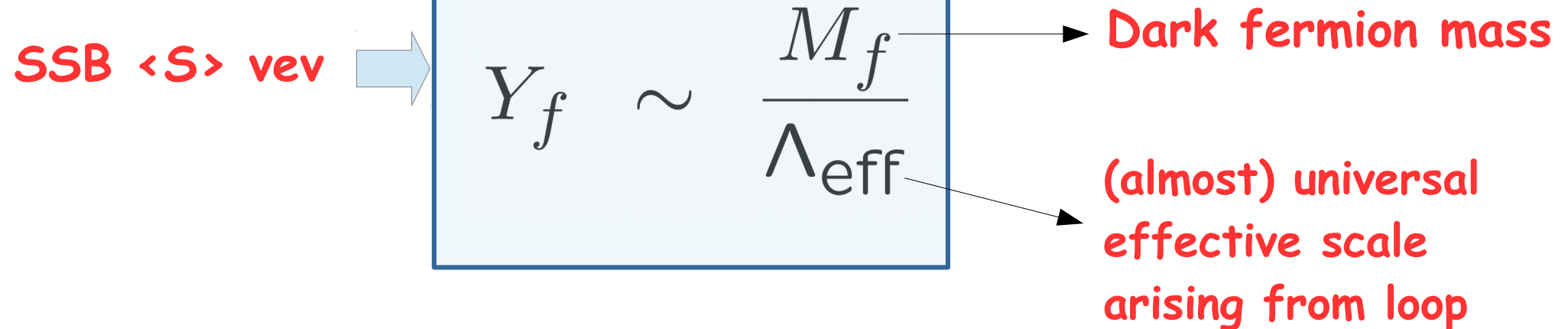
- Large hierarchy in SM fermion masses suggest
- Yukawa's arise as low energy effective couplings
- easier to justify the large hierarchy
- First attempt → Froggatt-Nielsen mechanism
- require ad-hoc high dim operators → origin unknown
- A new proposal: effective Yukawa couplings generated by a renormalizable theory → require a Dark Sector

# Effective Yukawa: Theoretical framework

EG, Raidal, PRD 89 (2014)  
E. Ma, PRL 112 (2014)

- **Main paradigm:** 4-dim Yukawa operators ( $Y_s$ )  
forbidden by some symmetry  $\Sigma$   
but can arise from operators of dim-5
- Assume existence of a Dark sector, with Dark-Fermions
- generate dark-chiral symmetry breaking **non-perturbatively**  
so that **DF** mass hierarchies exist
- Transfer **DF** mass hierarchy to **SM** using appropriate  
messenger sector (**via renormalizable interact.**)
- Effective  **$Y_s$**  arise at 1-loop after **SSB** of  $\Sigma$

From operators of dim-5  $(\bar{\psi}_L^f H_L \psi_R^f) S + h.c.$



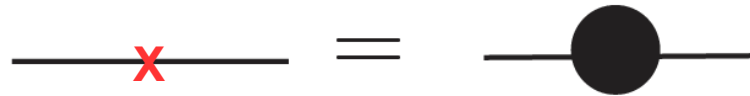
- for each SM fermion there exists a massive Dark-fermion in the Dark sector ( $\sim$  rescaled SM fermion spectrum)
- Non-perturbative dynamics in Dark sector responsible of generating  $M_f$  hierarchy (see next slides)

# Dark-Fermions mass hierarchy

- Large hierarchy of Yukawa's suggests some non-perturbative, exponential mechanism for dark-fermion masses  $M_f$
- Possible realization: via Nambu & Jona-Lasinio (NJL) mechanism
- dynamical mass "m" arises as a non-trivial solution of the self-consistent mass gap equation

$$m = \Sigma(\hat{p}, m)|_{\hat{p}=m}$$

self-energy



perturbative solution  $m=0$  always there

true ground state corresponds to non-trivial solution  $m \neq 0$  .

# Lee-Wick mechanism for ChSB

**Toy model:** massless fermions charged under U(1) gauge + the Lee-Wick term in the gauge sector

Lee-Wick, PRD 2 (1970) 1033;  
NPB 9 (1969) 209.

$$\mathcal{L} = -\frac{1}{4} F_{\mu\nu} F^{\mu\nu} + \frac{1}{\Lambda^2} (\partial^\alpha F_{\alpha\mu}) (\partial^\beta F_\beta^\mu) + i\bar{\psi}\gamma_\mu D^\mu\psi$$

$$D_\mu = \partial_\mu + igA_\mu$$

$$F_{\mu\nu} = \partial_\mu A_\nu - \partial_\nu A_\mu$$

spin-1 ghost in the spectrum with mass  $\sim \Lambda$

**ChSB induced by U(1) Lee-Wick term**

**fermion mass generated non-perturbatively**

EG, PRD 77 (2008) 055020

**Non-trivial solution obtained using the NJL approach**

# Dynamical fermion mass hierarchy

- **N fermions** coupled to **U(1) + Lee-Wick term**

Lee-Wick, PRD 2 (1970) 1033;  
NPB 9 (1969) 209.

## Mass-gap solution

EG, PRD 77 (2008)

EG, Raidal, PRD 89 (2014)

$$M_f = \Lambda \exp \left\{ -\frac{2\pi^2}{3\alpha(\Lambda)q_f^2} + \frac{1}{4} \right\}$$

valid for weak coupling regime  $\alpha \ll 1$

$\Lambda \rightarrow$  Lee-Wick ghost mass

- non-universal U(1) charges  $\rightarrow$  exponential mass spread



- other mechanism based on **Miransky scaling**:

U(1) @ strong coupling  $\rightarrow$  requires **criticality** (  $\alpha > \alpha_c = \pi/3$  )

$\Lambda_c$  energy scale where

U(1) becomes strong

$$m_\psi \approx 4\Lambda_c e^{-\frac{\pi\alpha_c}{\sqrt{\alpha - \alpha_c}}}$$



**embed this idea into effective Yukawa →**

# Yukawa hierarchy

EG, Raidal, PRD 89 (2014)

- requires exact U(1) gauge symmetry in Dark sector
- Dark fermions charged under U(1) in dark sector

$$Y_f \sim M_f \sim \exp \left\{ -\frac{\gamma}{\alpha q_f^2} \right\}$$

$\alpha$  U(1) fine-structure c.  
 $q_f$  U(1) quantum charges  
 $\gamma \sim$  anomalous dimension

- Yukawa's hierarchy related to U(1) charges

- A good matching of observed spectrum for charges O(1)

$$\bar{\alpha}(\Lambda) = 0.14, \quad q_{U_3} = 1 \text{ and } q_{D_3} = 0.9. \quad q_{E_3} = 1$$

$\psi:$	$U_2$	$D_2$	$U_1$	$D_1$
$q_\psi$	0.88	0.82	0.77	0.76

$\psi:$	$E_2$	$E_1$	$N_3$	$N_2$	$N_1$
$q_\psi$	0.92	0.81	0.65	0.59	0.55

$$m_{N_1} = 1 \text{ eV}, \quad m_{N_2} = 10^{-3} \text{ eV}, \quad \text{and } m_{N_3} = 10^{-6} \text{ eV}$$

# Enforced by LR gauge symmetry

EG, Marzola, Raidal,  
PRD 95 (2015)

■  $g_L = g_R = g$

$$SU(2)_L \times SU(2)_R \times U(1)_Y$$



$$H_L$$



$$H_R$$

only  $SU(2)$  Higgs doublets

■ dim-4 Yukawa operator forbidden

■ NO Higgs bi-doublets (to avoid dim-4 Yukawa operators)

■ lowest dim (gauge-invariant) operator (dim-5)

$$\frac{1}{\Lambda_{\text{eff}}} \left( \bar{\psi}_L^f H_L \right) \left( H_R^\dagger \psi_R^f \right) + h.c.$$

■ Yukawa's generated after **SSB of  $SU(2)_R$**

■ **Strong CP problem automatically solved !**

# Interactions Lagrangian in LR models required to generate Yukawa couplings

Dark fermions

$SU(2)_L$ -doublet messenger fields

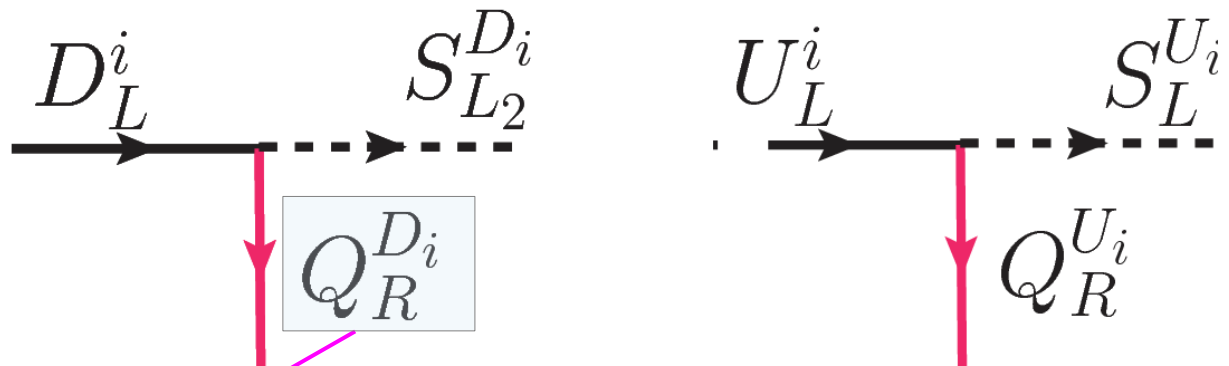
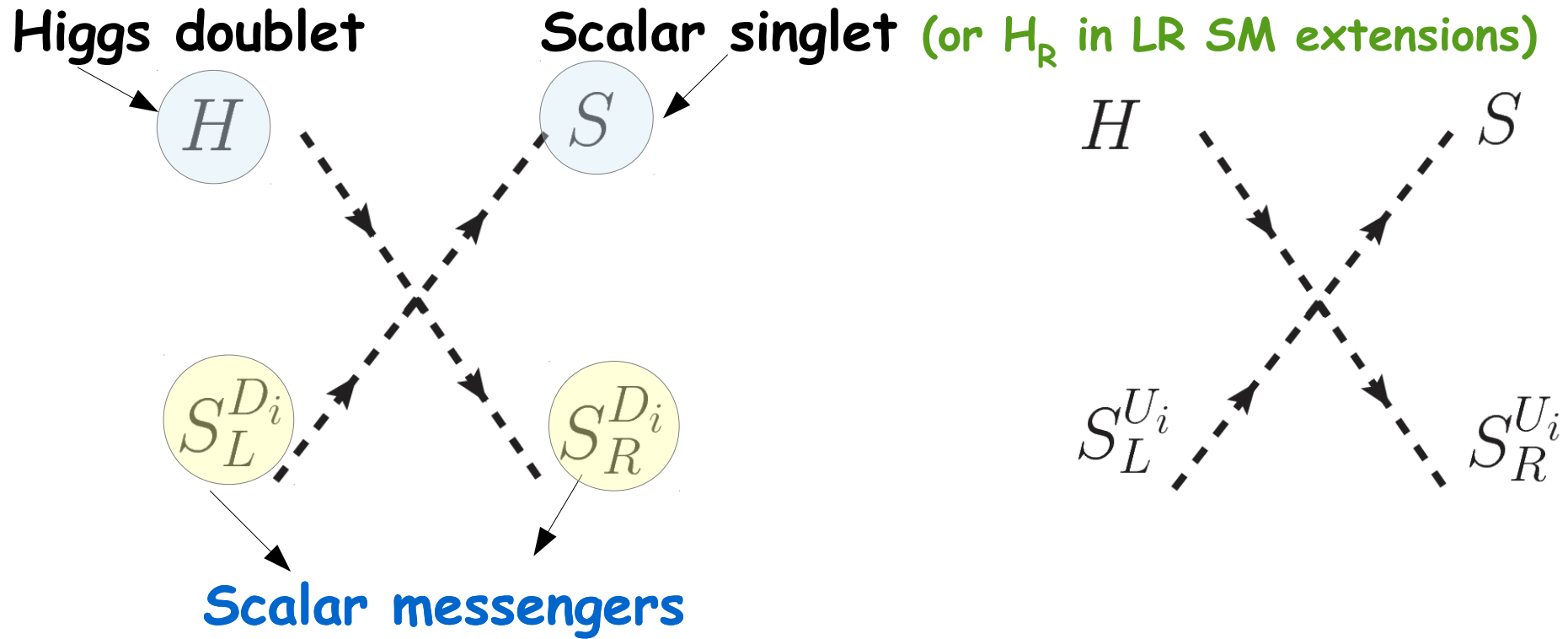
$$\begin{aligned}
 \mathcal{L}_{MS}^I = & g_L \left( \sum_{i=1}^N [\bar{q}_L^i Q_R^{U_i}] \hat{S}_L^{U_i} + \sum_{i=1}^N [\bar{q}_L^i Q_R^{D_i}] \hat{S}_L^{D_i} \right) \\
 & + g_R \left( \sum_{i=1}^N [\bar{q}_R^i Q_L^{U_i}] \hat{S}_R^{U_i} + \sum_{i=1}^N [\bar{q}_R^i Q_L^{D_i}] \hat{S}_R^{D_i} \right) \\
 & + \lambda \sum_{i=1}^N \left( \tilde{H}_L^\dagger \hat{S}_L^{U_i} \hat{S}_R^{U_i \dagger} \tilde{H}_R + H_L^\dagger \hat{S}_L^{D_i} \hat{S}_R^{D_i \dagger} H_R \right) + h.c.,
 \end{aligned}$$

$\downarrow$   
 4-scalar coupling of Higgses to fermions

(LR symmetry  $\rightarrow g_L = g_R$ )

$SU(N) \rightarrow U(1)^N \times Z_N$  symmetry

# Minimal set of new interactions



+  $L \leftrightarrow R$

Dark fermions

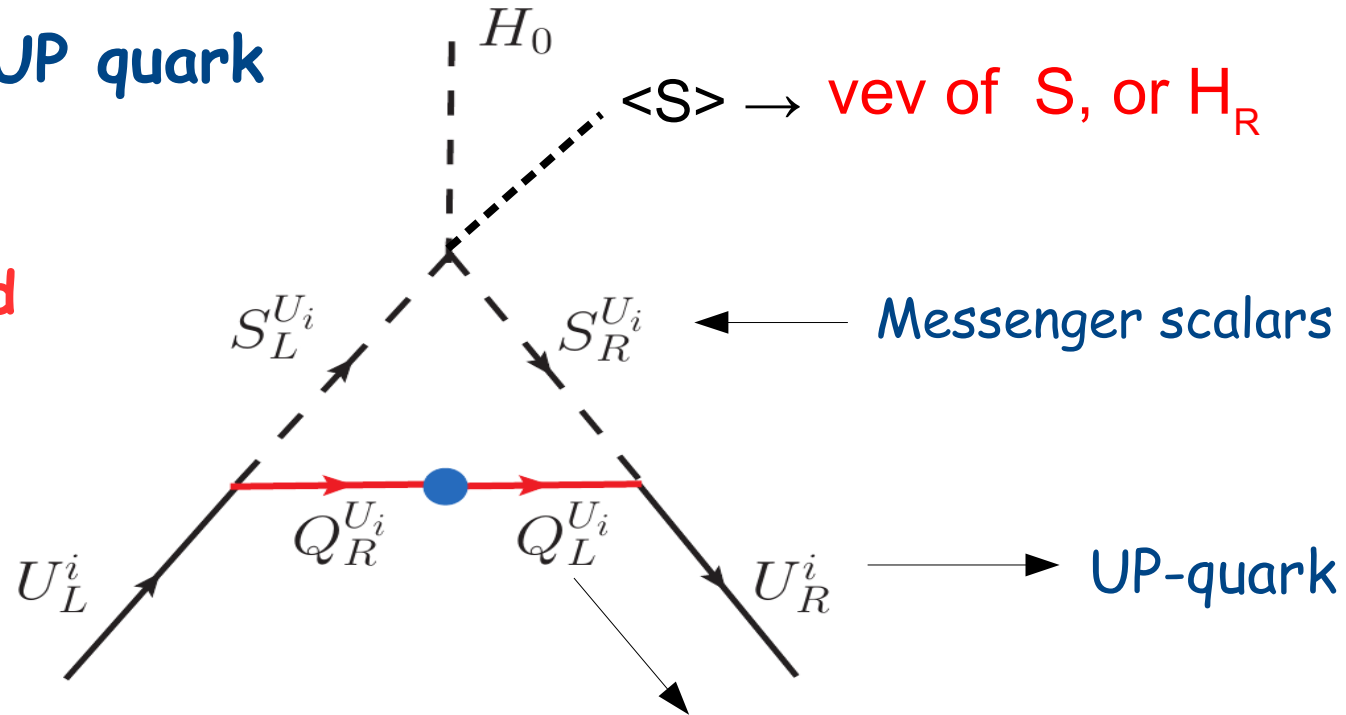
universal couplings  $\rightarrow U(1)^N \times Z_N$

# Higgs Yukawa's radiatively generated at 1-loop

Via higher order dim. operators  $\rightarrow \bar{U}_L U_R H S$  finite at any order

Yukawa coupling UP quark

$H_0$  = Higgs field



$Q$  = Dark-Fermions  
(SM gauge singlets)

●  $\rightarrow M_f$  = mass of Dark-fermion  $f$

$$Y_f \sim \frac{M_f}{\Lambda_{\text{eff}}}$$

Yukawas follow  $M_f$  hierarchy !

# Messenger mass matrix

$$M_S^2 = \begin{pmatrix} m_L^2 & \Delta \\ \Delta & m_R^2 \end{pmatrix}$$

$$\Delta = \frac{1}{2} \lambda v_R v_L$$

Assume flavor universal structure

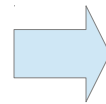
Eigenvalues  $\rightarrow m_{\pm}^2 = \frac{1}{2} \left( m_L^2 + m_R^2 \pm [(m_L^2 + m_R^2)^2 + 4\Delta]^2 \right)^{1/2}$

LR symmetry requires  $\rightarrow m_L^2 = m_R^2 \equiv \bar{m}^2$

$$m_{\pm}^2 = \bar{m}^2 (1 \pm \xi)$$

mixing parameter  $\xi = \frac{\Delta}{\bar{m}^2}$

to avoid tachions  
and color-charge breaking minima



$$0 < \xi < 1$$

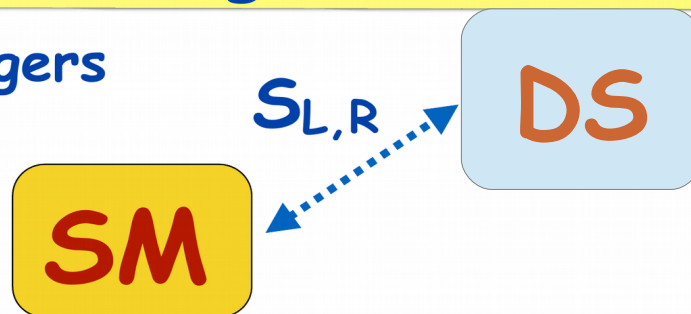
# Summary of model's features

■ **Dark fermions stable** [due to exact  $U(1)$ -dark gauge symmetry]

- ▶ having long-range interactions mediated by a massless dark photon
- ▶ Rescaled spectrum of SM fermions

■ **heavy scalar messengers  $S_{L,R}$**

▶ heavy scalar messengers (squark/slepton-like)



■ avoiding stability requires colored messengers to be heavy  $\gg$  TeV scale

■ EW messengers could be lighter, below TeV scale

Messengers (Scalars)

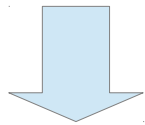
Fields	Spin	$SU(2)_L$	$U(1)_Y$	$SU(3)_c$	$U(1)_F$
$\hat{S}_L^{D_i}$	0	1/2	1/3	3	$-q_{D_i}$
$\hat{S}_L^{U_i}$	0	1/2	1/3	3	$-q_{U_i}$
$S_R^{D_i}$	0	0	-2/3	3	$-q_{D_i}$
$S_R^{U_i}$	0	0	4/3	3	$-q_{U_i}$
$Q^{D_i}$	1/2	0	0	0	$q_{D_i}$
$Q^{U_i}$	1/2	0	0	0	$q_{U_i}$
$S_0$	0	0	0	0	0

Dark Sector (Fermions+Scalar)



- Dynamics responsible of dark-fermion masses predicts an unbroken  $U(1)$

A main phenomenological implication



a massless dark-photon in the spectrum

# Massless Dark photons

- Different from massive Dark photons scenarios

- On-shell massless DP can be fully decoupled from SM sector at tree-level B. Holdom, *Phys Lett.* 166 B (1986) 196

- Interact with SM fields only via high-dimensional operators suppressed by  $1/M^{D-4}$

- Present bounds on massive DP do not apply (tree-level couplings with SM fields assumed)

- Large couplings in Dark sector allowed

# Massless Dark Photon signatures

- DP discovery channel in Higgs boson physics:

EG, Heikinheimo, Mele, Raidal, PRD 90 (2014)  
Biswas, EG, Heikinheimo, Mele PRD 93 (2016)

$$H \rightarrow \gamma \bar{\gamma}$$

→ non-decoupling

- no results by CMS and ATLAS yet

Decoupling (suppressed by UV scale)

- 9 new FCNC processes

$$f \rightarrow f' \bar{\gamma}$$

$f = t, b, c, s, \tau, \mu$

EG, Mele, Raidal, Venturini, PRD 94 (2016)

- DP discovery channel in Kaon physics

$$K^+ \rightarrow \pi^+ \pi^0 \bar{\gamma}$$

EG, Mele, Fabbrichesi, PRL 119 (2017)

- New Z boson decay

$$Z \rightarrow \gamma \bar{\gamma}$$

(evading Landau-Yang Th.)

EG, Mele, Fabbrichesi, arXiv:1712.05412  
To appear on PRL

# FCNC fermion decays into dark photon

$$f \rightarrow f' \bar{\gamma}$$

# CKM matrix origin

in the basis of weak-gauge eigenstates (no CKM mixing  $X_{ij} \rightarrow \delta_{ij}$ )

$$\begin{aligned} \tilde{\mathcal{L}}_{MS}^I &= \left\{ g_L \left( \sum_{i,j=1}^N \left[ \bar{q}_L^i (X_L^U)_{ij} Q_R^{U_j} \right] \hat{S}_L^{U_j} + \sum_{i,j=1}^N \left[ \bar{q}_L^i (X_L^D)_{ij} Q_R^{D_j} \right] \hat{S}_L^{D_j} \right) \right. \\ &+ \left. g_R \left( \sum_{i,j=1}^N \left[ \bar{u}_R^i (X_R^U)_{ij} Q_L^{U_j} \right] S_R^{U_j} + \sum_{i,j=1}^N \left[ \bar{d}_R^i (X_R^D)_{ij} Q_L^{D_j} \right] S_R^{D_j} \right) \right\} \end{aligned}$$

radiative generation of Yukawa implies

$$Y_{ij}^{U,D} \sim \left( X_L^{U,D} \dagger \cdot \hat{Y}^{U,D} \cdot X_R^{U,D} \right)_{ij}$$

$$\hat{Y}^{U,D} = \text{diag}[Y_1^{U,D}, Y_2^{U,D}, Y_3^{U,D}]$$

**Yukawas** can be diagonalized as usual by a bi-unitary transformation

$$\text{diag}[Y^{U,D}] = V_{L,R}^{U,D \dagger} \cdot Y^{U,D} \cdot V_{L,R}^{U,D} \implies \text{CKM matrix } K = V_L^U \dagger \cdot V_L^D.$$

minimal flavor violation requires  $\rightarrow X_{L,R}^{U,D} \sim \mathbf{1} + \Delta_{L,R}^{U,D}$   $|\Delta_{L,R}^{U,D}| \ll 1$

no reason why  $X_L^{U,D}$  should be unitary

**After rotation to quark-mass eigenstates**

$$X_{L,R}^U \implies \rho_{L,R}, \quad X_{L,R}^D \implies \eta_{L,R}$$

$$\rho_{L,R} \equiv V_{L,R}^{U \dagger} \cdot X_{L,R}^U$$

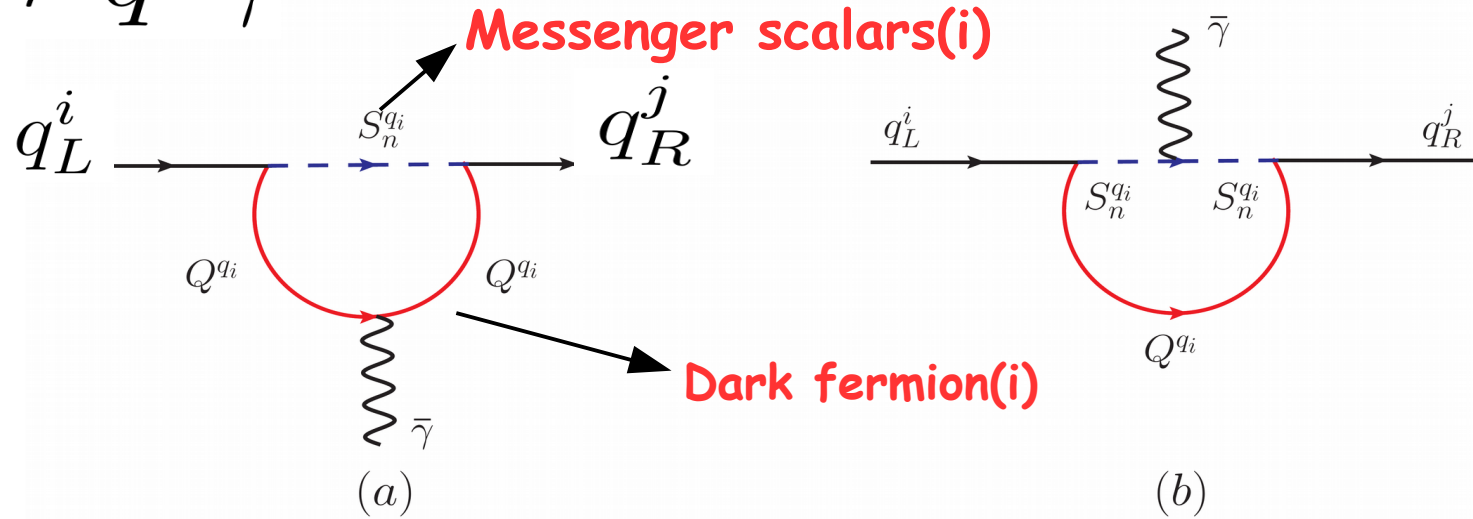
$$\eta_{L,R} \equiv V_{L,R}^{D \dagger} \cdot X_{L,R}^D$$

$\rho_{L,R}, \eta_{L,R} \implies$  **general matrices**

# FCNC decays of SM fermions into a Dark Photon

EG, Mele, Raidal, Venturini, PRD 94 (2016)

$$q^i \rightarrow q^j \bar{\gamma}$$



- DP coupled to SM fermions by FC magnetic-dipole operators

$$\mathcal{L}_{\text{eff}} = \sum_{q=U,D} \sum_{i,j=1}^3 \left( \frac{1}{2(\Lambda_L^q)_{ij}} \left[ \bar{q}_R^j(x) \sigma_{\mu\nu} \bar{F}^{\mu\nu}(x) q_L^i(x) \right] + \frac{1}{2(\Lambda_R^q)_{ij}} \left[ \bar{q}_L^j(x) \sigma_{\mu\nu} \bar{F}^{\mu\nu}(x) q_R^i(x) \right] \right)$$

$\bar{F}_{\mu\nu}$  = dark photon field strength

- suppressed by scales  $\Lambda_{L,R}$  proportional to typical messenger mass scale

- Decay width

$$\Gamma(q^i \rightarrow q^j \bar{\gamma}) = \frac{m_{q_i}^3}{16\pi^3} \left( \frac{1}{(\Lambda_L^q)_{ij}^2} + \frac{1}{(\Lambda_R^q)_{ij}^2} \right)$$

## Effective scales for UP-quark transitions (exact in $\xi, x$ )

neglecting mass of final fermion

$$\frac{1}{(\Lambda_L^U)_{ij}} = \frac{\bar{e} m_{U_i}}{\bar{m}_U^2} \left[ \bar{e}_i^U \frac{\rho_R^{ji}}{\rho_R^{ii}} F_{LR}(x_i^U, \xi_U) - \frac{g_R^2}{16\pi^2} \sum_{k=1}^3 \bar{e}_k^U \rho_R^{jk} \rho_R^{ki} F_{RR}(x_k^U, \xi_U) \right]$$

$$\frac{1}{(\Lambda_R^U)_{ij}} = \frac{\bar{e} m_{U_i}}{\bar{m}_U^2} \left[ \bar{e}_i^U \frac{\rho_L^{ji}}{\rho_L^{ii}} F_{RL}(x_i^U, \xi_U) - \frac{g_L^2}{16\pi^2} \sum_{k=1}^3 \left( \bar{e}_k^U \rho_L^{jk} \rho_L^{ki} F_{LL}(x_k^U, \xi_U) \right. \right.$$

$$\left. \left. + \left( \frac{\bar{m}_U^2}{\bar{m}_D^2} \right) \bar{e}_k^D \eta_L^{jk} \eta_L^{ki} F_{LL}(x_k^D, \xi_D) \right) \right],$$

$$F_{RR}(x, \xi) = F_{LL}(x, \xi) \quad F_{RL}(x, \xi) = F_{LR}(x, \xi) \rightarrow \text{Loop functions}$$

leading term  $\rightarrow$  dark-fermion mass term absorbed into quark mass

Effective scale proportional to the decaying fermion mass

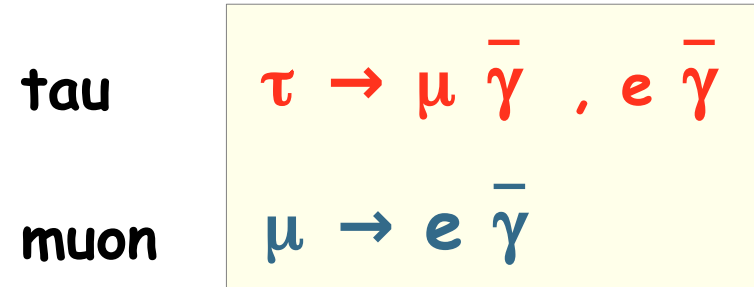
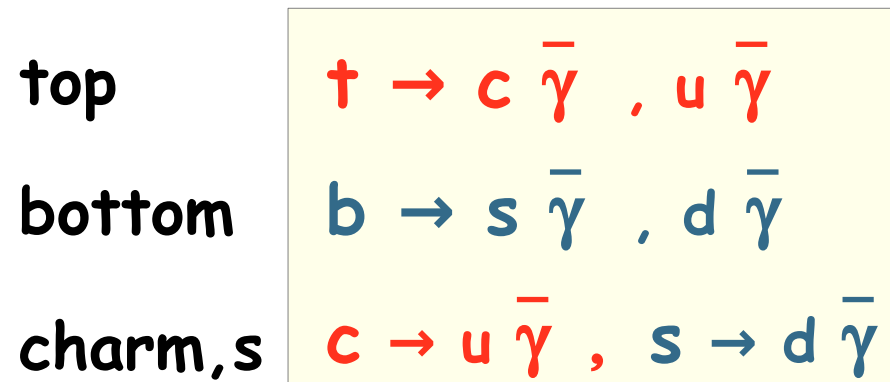
$$\Gamma(q^i \rightarrow q^j \bar{\gamma}) \sim \frac{m_{q_i}^5 \bar{\alpha}}{16\pi^3 \bar{m}_q^4} \times |\text{loop functions}|^2$$



# FCNC decays of SM fermions into a Dark Photon

EG, Mele, Raidal, Venturini, PRD 94 (2016)

- 9 new kind of FCNC signatures predicted !



final fermion balanced by a massless invisible ( $\nu$ -like) system

- Large and possibly measurable BRs are allowed, up to

- $BR(b \rightarrow q \bar{\gamma}) \sim 10^{-4} - 10^{-3}$

- $BR(c \rightarrow u \bar{\gamma}) \sim 10^{-8} - 10^{-4}$

- $BR(t \rightarrow q \bar{\gamma}) \sim 10^{-10} - 10^{-7}$

- $BR(\mu \rightarrow e \bar{\gamma}) \sim 10^{-10} - 10^{-9}$

- $BR(\tau \rightarrow l \bar{\gamma}) \sim 10^{-10} - 10^{-6}$

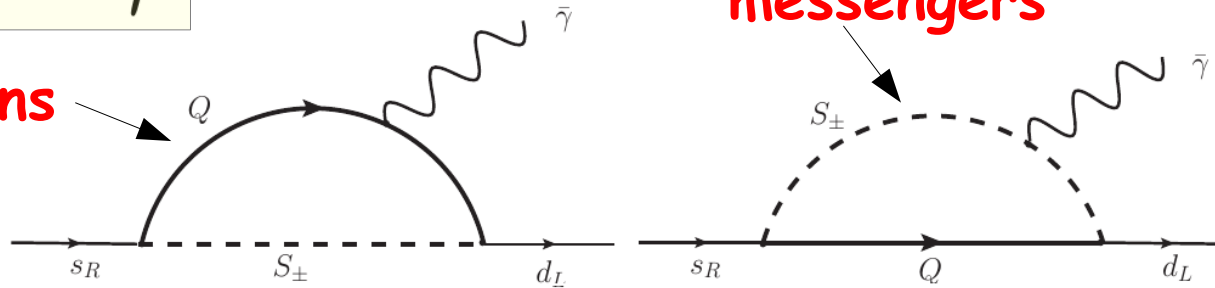
depending on various parameters and on flavor universality structure of messenger sector

# FCNC Kaon decay into a massless Dark photon

Fabbrichesi, EG, Mele, PRL 119 (2017)

$$s \rightarrow d \bar{\gamma}$$

Dark-fermions



Effective Hamiltonian

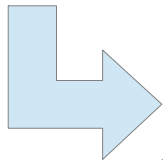
$$\mathcal{H}_{eff}^{\Delta S=1} = \frac{e_D}{64 \pi^2} \frac{\xi}{\Lambda} \hat{Q}$$

$\xi \rightarrow$  FC couplings  $\xi = g_L g_R / 2$   
 $\Lambda \rightarrow$  DF ~ messenger mass

FCNC magnetic-dipole operator

$$\hat{Q} = (\bar{s} \sigma^{\mu\nu} d) \bar{F}_{\mu\nu}$$

Dark-photon



$$K^+ \rightarrow \pi^+ \pi^0 \bar{\gamma}$$

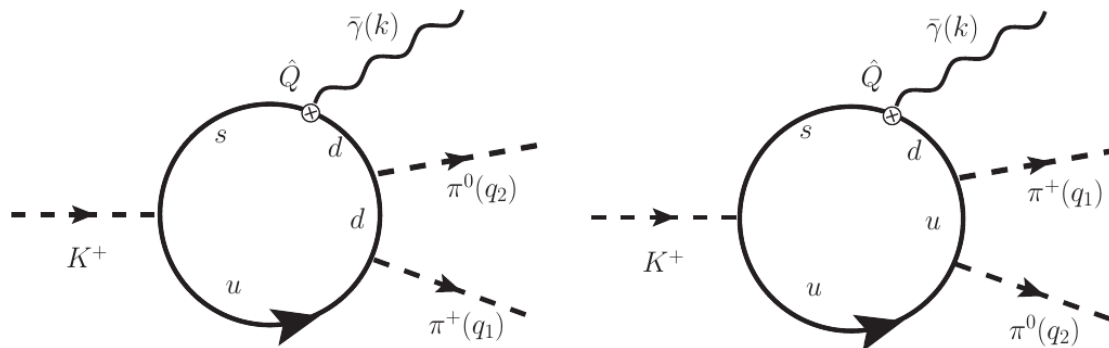
$K^+ \rightarrow \pi^+ \bar{\gamma} \Rightarrow$  for massless dark photon identically vanishes

$$K^+(p) \rightarrow \pi^+(q_1) \pi^0(q_2) \bar{\gamma}(k)$$

$$\langle \bar{\gamma} \pi^+ \pi^0 | \mathcal{H}_{eff}^{\Delta S=1} | K^+ \rangle = \frac{M(z_1, z_2)}{m_K^3} \varepsilon_{\mu\nu\rho\sigma} q_1^\nu q_2^\rho k^\sigma \varepsilon^\mu(k)$$

$$\frac{d^2\Gamma}{dz_1 dz_2} = \frac{m_K}{(4\pi)^3} |M(z_1, z_2)|^2 \{ z_1 z_2 [1 - 2(z_1 + z_2) - r_1^2 - r_2^2] - r_1^2 z_2^2 - r_2^2 z_1^2 \}, \quad \text{where } z_i = k \cdot q_i / m_K^2 \text{ and } r_i = M_{\pi_i} / m_K$$

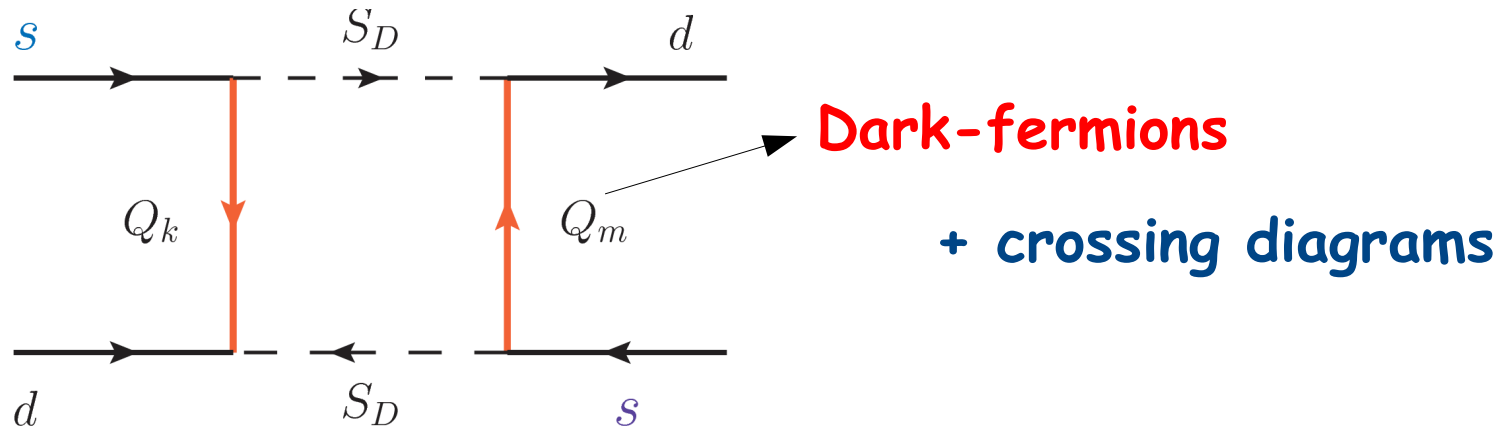
## Matrix element estimated using the Chiral-Quark model



$D_0, D_{00}$  usual PV functions

$$\frac{M(z_1, z_2)}{m_K^3} = \frac{e_D}{32\pi^2} \frac{\xi}{\Lambda} \frac{M^3}{\pi^2 f^3} \left[ M^2 D_0(0, m_\pi^2, m_\pi^2, m_K^2; 2m_K^2 z_1 + m_\pi^2, m_K^2(1 - 2z_1 - 2z_2); M, M, M, M) \right. \\ \left. - D_{00}(0, m_\pi^2, m_\pi^2, m_K^2; 2m_K^2 z_1 + m_\pi^2, m_K^2(1 - 2z_1 - 2z_2); M, M, M, M) + (z_1 \leftrightarrow z_2) \right].$$

# NLO contributions to $\Delta S=2$ effective Hamiltonian



$$\mathcal{H}_{eff}^{\Delta S=2} = \sum_i^5 C_i Q_i + \sum_{i=1}^3 \tilde{C}_i \tilde{Q}_i$$

$$\mu = 2 \text{ GeV}$$

$$\langle Q_i \rangle = \langle K^0 | Q_i | \bar{K}^0 \rangle$$

	$Q_1, \tilde{Q}_1$	$Q_2, \tilde{Q}_2$	$Q_3, \tilde{Q}_3$	$Q_4$	$Q_5$
$\langle Q_i \rangle$	$\bar{d}_L^\alpha \gamma_\mu s_L^\alpha \bar{d}_L^\beta \gamma_\mu s_L^\beta, (L \leftrightarrow R)$	$\bar{d}_R^\alpha s_L^\alpha \bar{d}_R^\beta s_L^\beta, (L \leftrightarrow R)$	$\bar{d}_R^\alpha s_L^\beta \bar{d}_R^\beta s_L^\alpha, (L \leftrightarrow R)$	$\bar{d}_R^\alpha s_L^\alpha \bar{d}_L^\beta s_R^\beta$	$\bar{d}_R^\alpha s_L^\beta \bar{d}_L^\beta s_R^\alpha$
$C_i(\Lambda)$	$1/3 m_K f_K^2 B_1(\mu)$	$-5/2 X_K m_K f_K^2 B_3(\mu)$	$1/24 X_K m_K f_K^2 B_3(\mu)$	$1/4 X_K m_K f_K^2 B_4(\mu)$	$1/12 X_K m_K f_K^2 B_5(\mu)$
	$-1/24 C^2$	0	$1/12 C^2$	$1/6 C^2$	$1/6 C^2$

$$C^2 = \xi^2 / (16\pi^2 \Lambda^2) \quad \xi = g_L g_R / 2$$

$$X_K(\mu) = (m_K / (m_d(\mu) + m_s(\mu)))^2$$

# A simplified model (1 dark-fermion + messenger fields)

$$\text{BR}(K^+ \rightarrow \pi^+ \pi^0 \bar{\gamma}) \simeq 1.31 \alpha_D \eta^2 \frac{\xi^2}{\Lambda^2}$$

■  $\Lambda \rightarrow$  Dark sector mass scale

## NLO $K$ - $\bar{K}$ mixing constraints



[TeV]

$$\Delta M_K = 8.47 \times 10^{-13} \frac{\xi^2}{\Lambda^2}$$

[TeV]

$$\text{BR}(K^+ \rightarrow \pi^+ \pi^0 \bar{\gamma}) \lesssim 1.6 \times 10^{-7}$$

Large BR of order  $10^{-8}$ - $10^{-7}$  possible

Fabbrichesi, EG, Mele, PRL 119 (2017)  
 $\text{BR}(K^+ \rightarrow \pi^+ \pi^0 \bar{\gamma})$

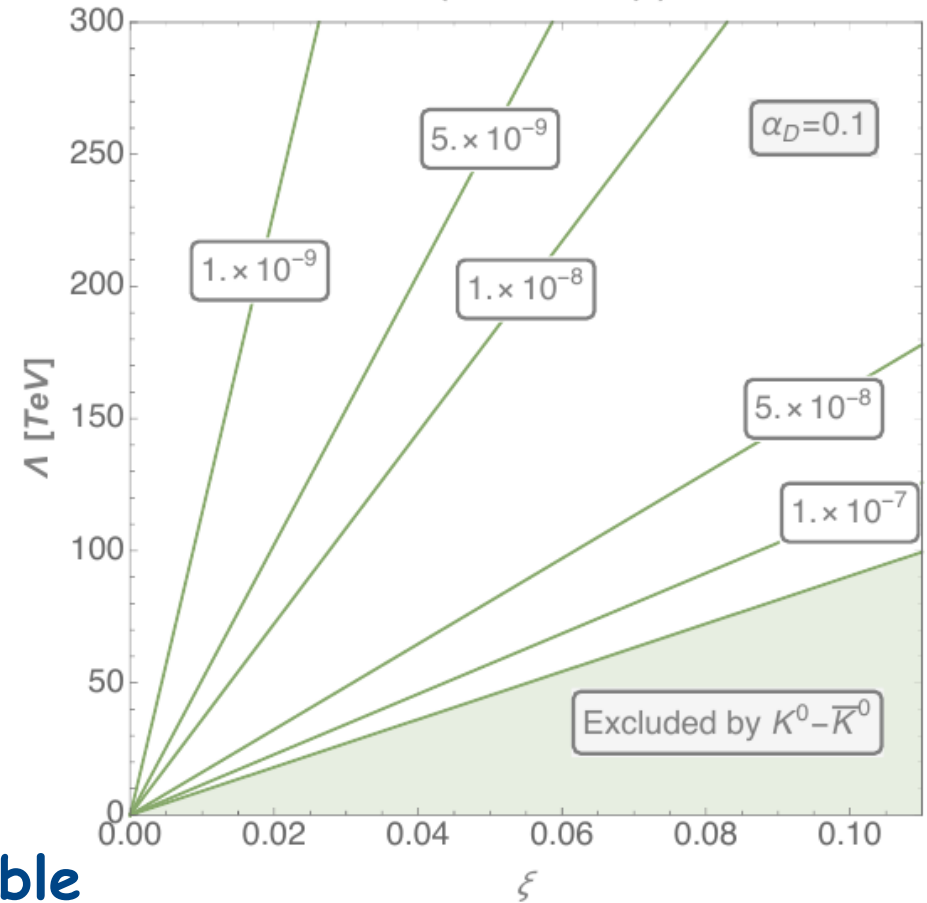


FIG. 3:  $\text{BR}(K^+ \rightarrow \pi^+ \pi^0 \bar{\gamma})$  as a function of the effective scale  $\Lambda$  and coupling  $\xi = g_L g_R / 2$ , for a representative choice of the coupling strength  $\alpha_D = 0.1$ .

# Conclusions

Origin of Yukawa might require existence of a Dark Sector as predicted by a recent proposal to naturally explain Yukawa hierarchy

Dark sector might have long distance interactions mediated by an unbroken  $U(1)_F$  that forecasts a massless Dark Photon

Higgs boson can be the SM portal to Dark Photons

rich phenomenological implications @ LHC and linear colliders

search for dark photons in  $H \rightarrow \gamma \bar{\gamma}$ , and  $H \rightarrow Z \bar{\gamma}$

In FCNC sector: new 9 processes predicted

$t \rightarrow (c,u) \bar{\gamma}$ ,  $b \rightarrow (s,d) \bar{\gamma}$ ,  $c \rightarrow u \bar{\gamma}$ ,  $s \rightarrow d \bar{\gamma}$ ,  $\tau \rightarrow l \bar{\gamma}$ ,  $\mu \rightarrow e \bar{\gamma}$

not yet experimentally investigated

FCNC  $s \rightarrow d \bar{\gamma}$  transition: golden channel

$K^+ \rightarrow \pi^+ \pi^0 + \bar{\gamma}$

large available rates BR  $\sim 10^{-8} - 10^{-7}$

currently under consideration by NA62 @ CERN

# Backup slides

# Yukawa coupling

- prediction at 1-loop (in LR symmetric scheme, exact in  $\xi$ )

$$Y_f = \left( \frac{\lambda g_L g_R}{16\pi^2} \right) \left( \frac{\xi M_{Q_f} \sqrt{2}}{v_L} \right) f_1(x_f, \xi)$$

vev  $\langle H_R \rangle$  reabsorbed in mixing  $\xi$

$$x_f = M_{Q_f}^2 / \bar{m}^2$$

- After EWSB

$$M_{Q_f} = m_f \left( \frac{16\pi^2}{g_L g_R} \right) \frac{1}{\xi f_1(x_f, \xi)}$$

Dark-fermion mass  $\gg$  SM fermion mass

$f_1(x, \xi)$  loop function of order  $O(1)$

Dark fermion spectrum  $\sim$  rescaled spectrum of SM one



# Phenomenological constraints

- avoid existence of charged stable particle (DM constraints)
- due to the Flavor universality of messenger mass sector
  - ▶ lightest messenger state required to be heavier than the heaviest DF (associated to the top-quark)

$$m_- \geq M_{Q_t}$$


$$\bar{m} \geq m_t \left( \frac{16\pi^2}{g_L g_R} \right) F(\xi)$$

implying lower bounds on  $v_R$

$$v_R \geq \frac{2m_t^2}{\lambda v_L} \left( \frac{16\pi^2}{g_L g_R} \right)^2 \xi F(\xi)^2$$

# Lower bounds on messenger masses

## ■ at large $\xi$ mixing

$$\bar{m}_U \geq \frac{(110 \text{ TeV}) K_t(\bar{m})}{g_L g_R} \sqrt{1 - \xi_U}$$

$$\bar{m}_D \geq \frac{(3 \text{ TeV}) K_b(\bar{m})}{g_L g_R} \sqrt{1 - \xi_D}$$

## ■ at small $\xi$ mixing

$$\bar{m}_U \geq \frac{(55 \text{ TeV}) K_t(\bar{m})}{\xi_U g_L g_R}$$

$$\bar{m}_D \geq \frac{(1.5 \text{ TeV}) K_b(\bar{m})}{\xi_D g_L g_R}$$

$K_{t,b}$  renormalization factors  $K_{t,b}(\bar{m}) < 1$

■ Colored-messenger masses naturally above TeV scale

■ EW messengers potentially lighter  $\rightarrow$  relaxed lower bound

■ hierarchy among  $SU(2)_L$  and  $SU(2)_R$  naturally explained !

# Top quark case $\text{BR}(t \rightarrow q \bar{\gamma})$ ( $q=c,u$ )

## from exp. upper bounds on $\text{BR}(t \rightarrow q \gamma)$

- for  $\xi_U = 0.1$ , and  $x_3^U = 0.8$  (small-mixing regime)

$$\text{BR}^{(t \rightarrow u \gamma)}(t \rightarrow u \bar{\gamma}) < 1.8 \times 10^{-2} \left( \frac{\bar{\alpha}}{0.1} \right)$$

$$\text{BR}^{(t \rightarrow c \gamma)}(t \rightarrow c \bar{\gamma}) < 2.3 \times 10^{-1} \left( \frac{\bar{\alpha}}{0.1} \right)$$

- for  $\xi_U = 0.8$ , and  $x_3^U = 0.1$  (large-mixing regime)

$$\text{BR}^{(t \rightarrow u \gamma)}(t \rightarrow u \bar{\gamma}) < 3.4 \times 10^{-2} \left( \frac{\bar{\alpha}}{0.1} \right)$$

$$\text{BR}^{(t \rightarrow c \gamma)}(t \rightarrow c \bar{\gamma}) < 4.4 \times 10^{-1} \left( \frac{\bar{\alpha}}{0.1} \right)$$

large BR are allowed from  $\text{BR}(t \rightarrow q \gamma)$

# DM and Vacuum stability bounds on $BR(t \rightarrow q \bar{\gamma})$

Excluded by  
lightest messenger  
mass  $< 1$  TeV

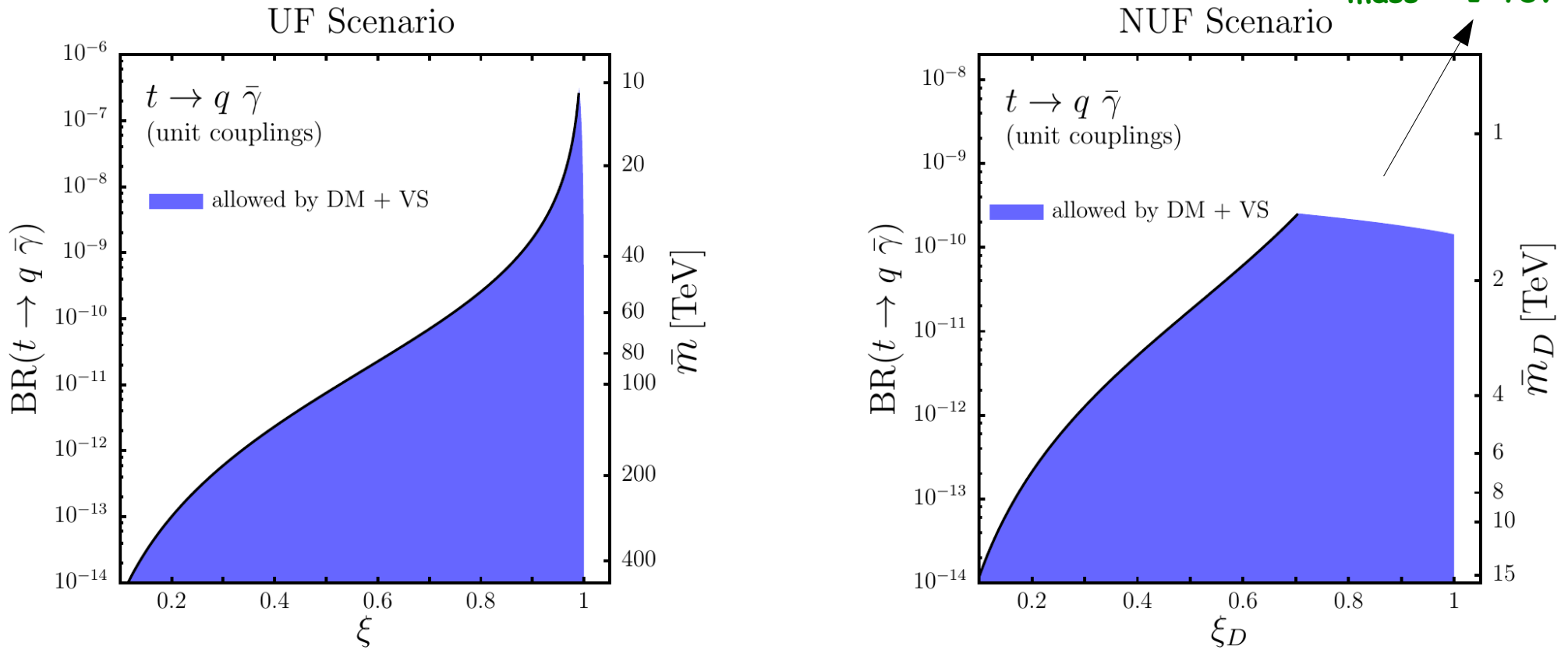
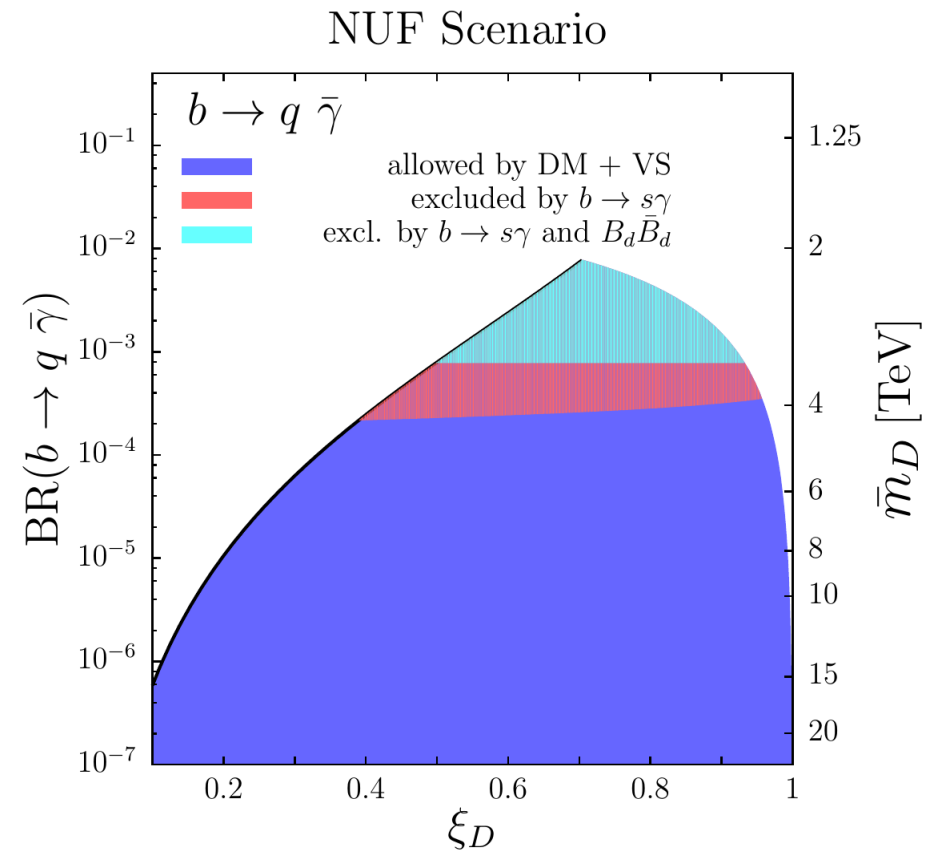
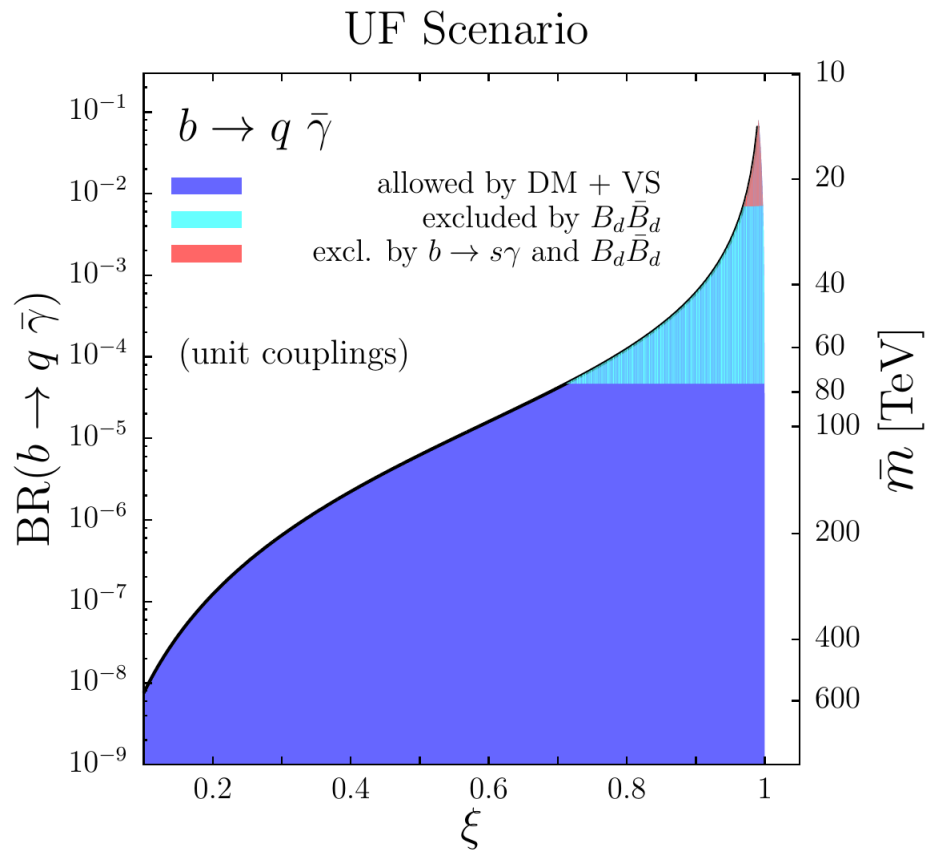


Figure 3: Allowed regions (colored areas) by DM and vacuum stability (VS) constraints for  $BR(t \rightarrow q \bar{\gamma})$  and for the average messenger mass scales  $\bar{m}$  and  $\bar{m}_D$ , versus the corresponding mixing  $\xi$  and  $\xi_D$ , in the UF (left) and NUF (right) scenarios, respectively.

**DM and Vacuum stability can set very strong upper bounds on BR**  
**(due to large width of top and lower bounds on  $\bar{m}$  above TeV scale)**

# Bottom quark case $BR(b \rightarrow q \bar{\gamma})$ ( $q=d,s$ )



Large values of BR possible in both universal and non-universal flavor Scenario (enhancement due to the tiny width of b)

# Charm quark case $BR(c \rightarrow u \bar{\gamma})$

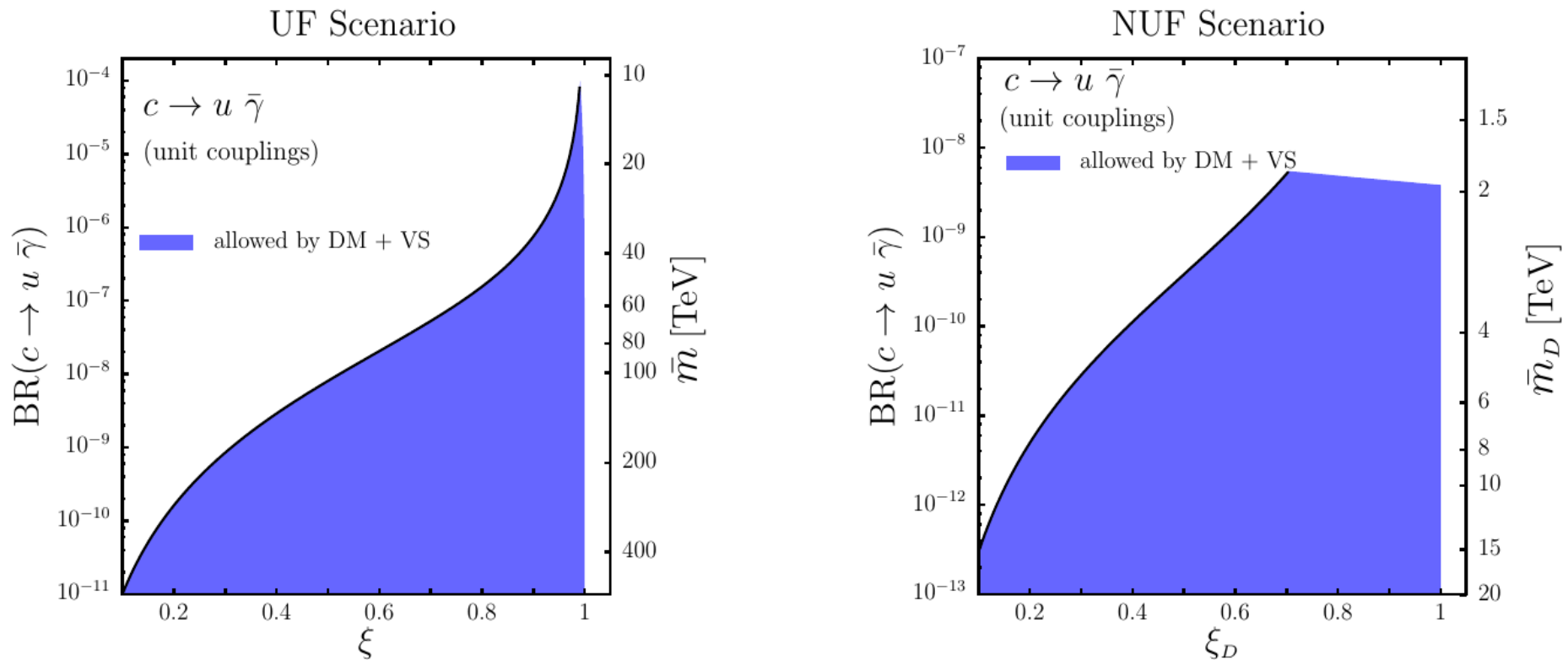


Figure 6: Allowed regions (colored areas) by DM and vacuum-stability (VS) constraints for  $BR(c \rightarrow u \bar{\gamma})$  and for the average messenger mass scales  $\bar{m}$  and  $\bar{m}_D$ , versus the corresponding mixing  $\xi$  and  $\xi_D$ , in the UF (left) and NUF (right) scenarios, respectively. In the left (right) plots we assume  $\bar{e} \bar{e}_2^U \rho_L^{12} / \rho_L^{22} \simeq 1$  ( $\bar{e} \bar{e}_2^D \eta_L^{12} / \eta_L^{22} \simeq 1$ ) with all other matrix elements of flavor matrices set to zero.

**Large values of BR possible !**

# FV Leptonic decays $\text{BR}(l \rightarrow l' \bar{\gamma})$

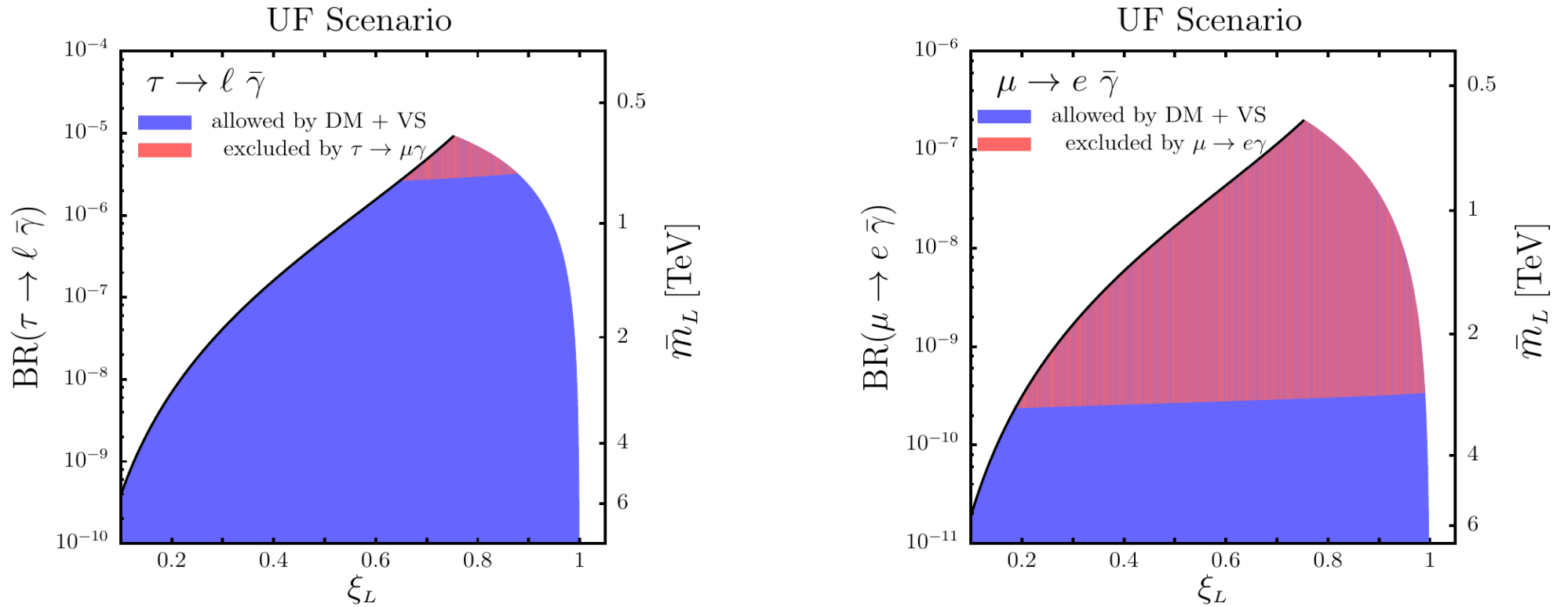


Figure 8: Regions allowed by DM and vacuum stability (VS) constraints for  $\text{BR}(\tau \rightarrow \ell \bar{\gamma})$  (left) and  $\text{BR}(\mu \rightarrow e \bar{\gamma})$  (right), and for the average messenger mass scale  $\bar{m}_L$ , versus the mixing  $\xi_L$ , in the UF scenario (blue areas). Superimposed red areas are the subregions excluded by direct constraints on  $\text{BR}(\ell \rightarrow \ell' \gamma)$ . In the left (right) plot, we assume  $\bar{e} \bar{e}_3^L \tilde{\eta}_L^{j3} / \tilde{\eta}_L^{33} = 10^{-2}$  ( $\bar{e} \bar{e}_3^L \tilde{\eta}_L^{12} / \tilde{\eta}_L^{22} = 10^{-4}$ ), with  $j = 1, 2$ .