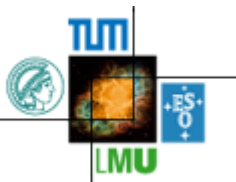


Kaon Flavour News

Andrzej J. Buras
(Technical University Munich, TUM-IAS)



Lyon
April 2018



Overture

Stars of KAON Flavour Physics

$$\varepsilon_K, \Delta M_K$$

$$\varepsilon'/\varepsilon$$

$$K^+ \rightarrow \pi^+ \nu \bar{\nu}$$

$$K_L \rightarrow \pi^0 \nu \bar{\nu}$$

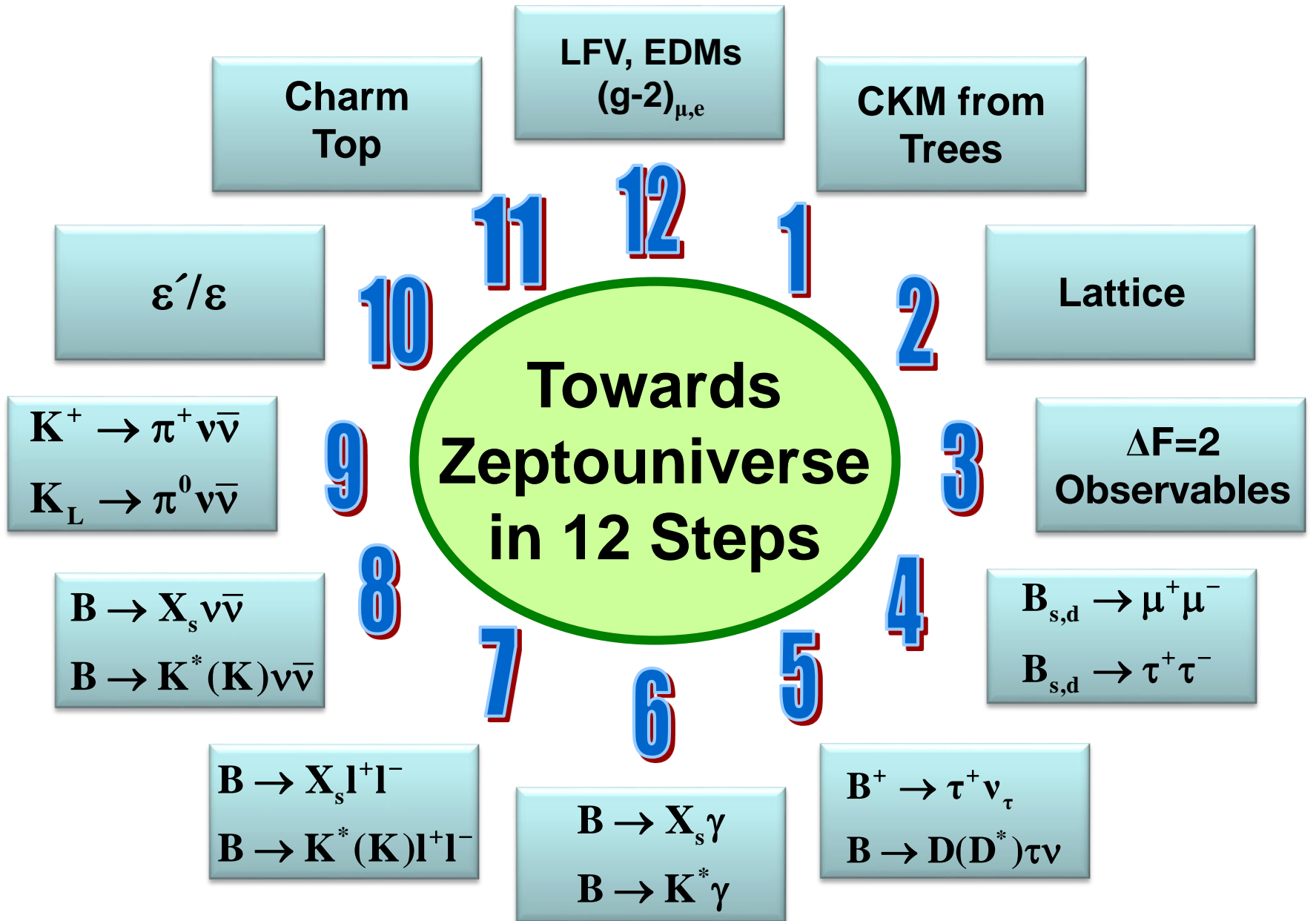
$$K_{L,S} \rightarrow \mu^+ \mu^-$$

$$K_L \rightarrow \pi^0 l^+ l^-$$

$\Delta I = 1/2$ Rule

They all can give some information about very short distance scales but to identify new physics, correlations with $B_{s,d}$ and D observables, EDMs, Lepton physics crucial

In particular if we want to reach Zeptouniverse without any direct hints from the LHC



Impact of QCD at SD and LD Scales

(K-physics)

SD

Fully under control: NLO + NNLO

AJB: „Climbing NLO and NNLO Summits of Weak Decays“

(1102.5650; last update 2014)

(Munich, Rome + Gorbahn, Brod,
(early 1990s) Haisch, Jäger,
Nierste, Cerda-Sevilla)

LD

Lattice QCD

(ETM, SWME, RBC-UKQCD, ...)

(Numerical sophisticated tedious calculations lasting
many years)

Analytic

Dual QCD

(Bardeen, AJB, Gérard, 1985 →)

(Much faster than LQCD, very suitable for
non-leptonic transitions)
($K^0 - \bar{K}^0$ mixing, $K \rightarrow \pi\pi$)

Chiral Perturbation
Theory

(Gasser, Leutwyler, 1980 →)

(Much faster than LQCD, very suitable for
leptonic, semi-leptonic decays)
($K_L \rightarrow \pi\ell$, $K \rightarrow \ell\ell$, $K \rightarrow \pi\nu\bar{\nu}$)

Plan for next 38 min

1.

Dual QCD News

2.

ε'/ε strikes back

3.

$K \rightarrow \pi\nu\bar{\nu}$
in the Standard Model



4.

Implications for ε'/ε , ε_K , $K \rightarrow \pi\nu\bar{\nu}$
(Z' - FCNCs) ΔM_K

5.

BSM for ε'/ε

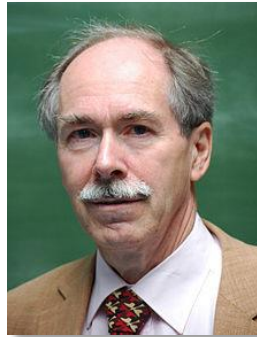
6.

Summary

1.

Dual QCD

Large N
QCD



Gerard 't Hooft
(1974)



Edward Witten
(1979, 1980)

At Large N QCD becomes a theory of weakly interacting mesons

with coupling $\frac{1}{f_\pi^2} \sim \frac{1}{N}$



In the strict Large N limit QCD becomes a free theory of mesons.

Dual QCD Approach for Weak Decays

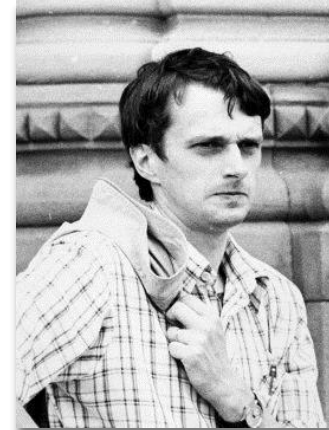
1985



W. Bardeen

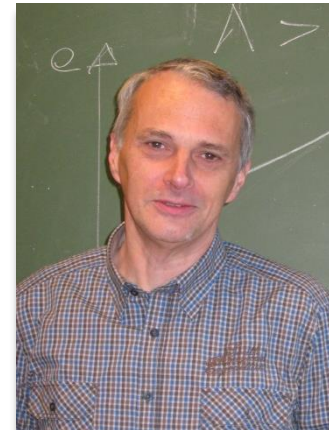
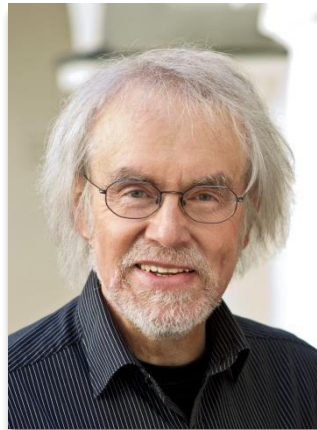


AJB



J.-M. Gérard

2014

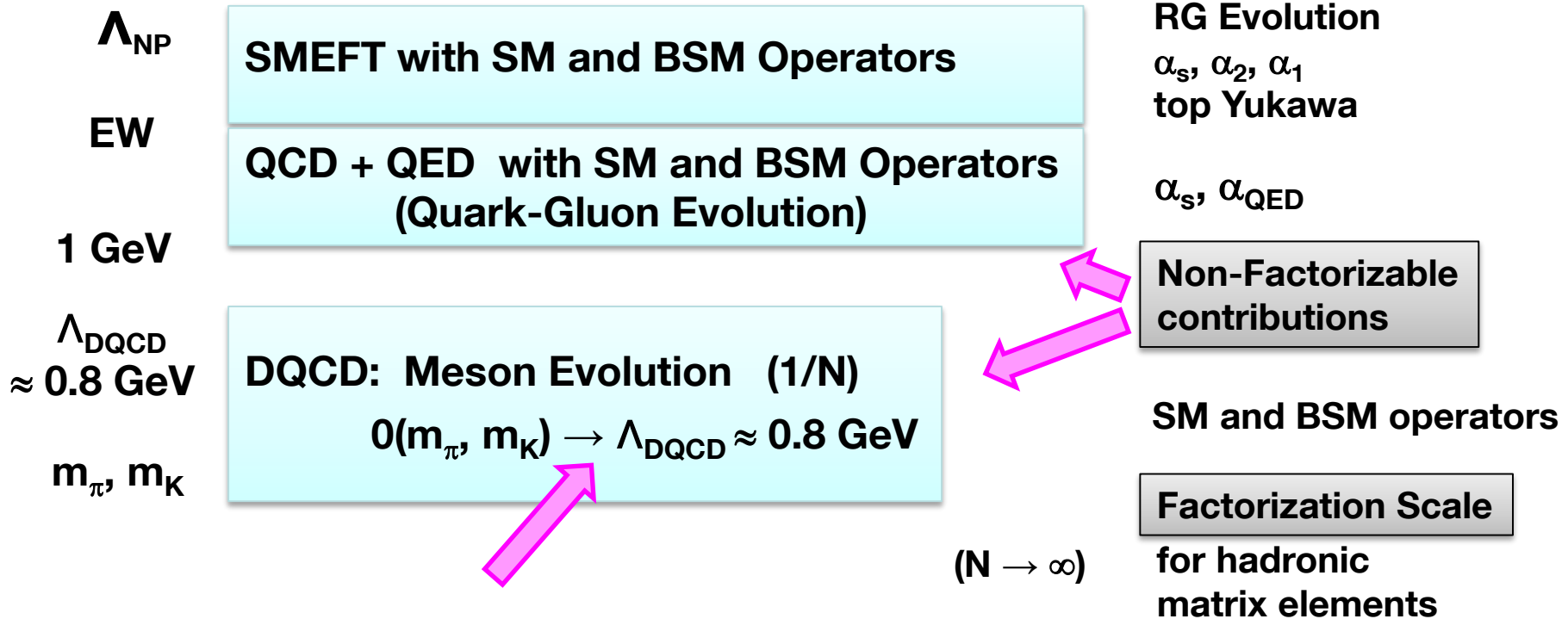


Basic Structure of DQCD for $K \rightarrow \pi\pi$, $K^0 - \bar{K}^0$ mixing

$(\varepsilon'/\varepsilon, \varepsilon, \Delta I = 1/2 \text{ Rule}, \Delta M_K)$

SM and BSM Operators

Reviews: 1401.1385, 1408.4820



Crucial strong dynamics
 Responsible for $\Delta I = 1/2$ Rule, $\varepsilon'/\varepsilon, \varepsilon, \Delta M_K, K \rightarrow \pi\pi$ in general.

The Main Role of DQCD

1. Efficient approximate method for obtaining results for non-leptonic decays: years, even decades before Lattice QCD.

(1985-2012)

2. Giving insight in numerical results obtained by Lattice QCD at 2-3 GeV.

Progress in
LQCD
↓
(2012 →)

3. The only existing QCD method allowing to study analytically the dominant dynamics between m_K and 1 GeV.

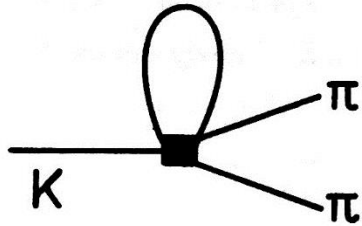
MESON EVOLUTION

:

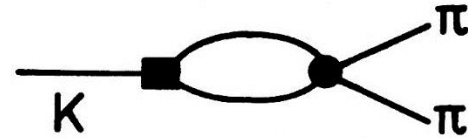
The pattern of operator mixing found to agree with SD mixing. both for SM and BSM operators.

Meson Evolution

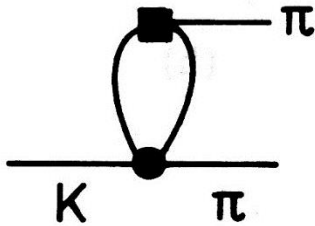
Loops with a physical cutt-off Λ



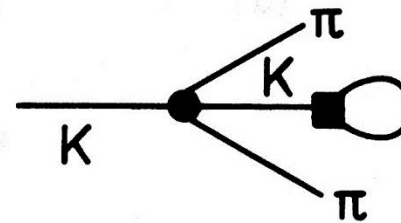
(a)



(b)



(c)



(d)

Very different philosophy from Chiral PTh

No dimensional regularisation !!!

$\Delta I = 1/2$ Rule

$$R = \frac{\text{Re } A_0}{\text{Re } A_2} \approx 22.4$$

Since 1955

Gell-Mann Pais
 $R = \sqrt{2}$ in Fermi-Theory
 (No QCD)

1974

Octet Enhancement
 (Current-Current Operators) } (Altarelli + Maiani
 Gaillard + Lee)

$R \approx 3$

(Asymptotic Freedom)
 SD evolution

1976

QCD Penguins (Shifman et al)
 (Fit hadronic matrix elements
 at $\mu = 0.3 \text{ GeV} \rightarrow \varepsilon'/\varepsilon \sim 0(10^{-2})$)
 (Gilman + Wise)

1986

Dual QCD (BBG)

(Main
 Dynamics
 Behind
 $\Delta I = 1/2$ Rule)

Octet Enhancement including LD part (Meson Evolution)
 QCD Penguins at 10%

2014:

$R = 16.0 \pm 1.5$

FSI ? (Pich)
 New Physics ?
 (1404.3824, G')
 AJB, De Fazio, Girschbach

2015

RBC-UKQCD

$R = 31 \pm 11$

(2012)

Confirmation of Octet Enhancement

\hat{B}_K Parameter for $K^0 - \bar{K}^0$ Mixing, ε_K

1986

Donoghe et al
Pich + Rafael

$$\hat{B}_K \approx 0.33$$

$$\hat{B}_K \approx 0.4$$

Lattice QCD

$$\hat{B}_K \approx 1$$

1987

BBG

$$\hat{B}_K = 0.67 \pm 0.07$$

$$\hat{B}_K = 0.75 \quad (\text{Large N limit})$$

2018

BBG

$$\hat{B}_K = 0.73 \pm 0.02$$

Lattice QCD:

$$\hat{B}_K = 0.766 \pm 0.010$$

$$\text{Gérard: } \hat{B}_K < 0.75$$

QCD and Electroweak Penguin Matrix Elements

1986

BBG strict Large N limit

$$B_6^{1/2} = B_8^{3/2} = 1$$

$$(\mu \approx 0(m_\pi))$$

2015

AJB + Gérard
1507.06326

Including 1/N
(meson evolution
for B_6, B_8)

$$B_6^{1/2} < B_8^{3/2} < 1$$

$$\text{at } \mu \geq 1\text{GeV}$$

More about it later.

2018 Results in DQCD

: BSM hadronic
Matrix elements

★ 1.

Matrix elements of chromomagnetic penguins
AJB + Gérard 1803.08052 (First on-shell $K \rightarrow \pi\pi$
calculation to date)

Confirmation of $K \rightarrow \pi$ matrix element
by ETM collaboration 1712.09824

$$B_{\text{CMO}} \approx 1/3$$

Much smaller
than early
estimates in
chiral quark
model

★ 2.

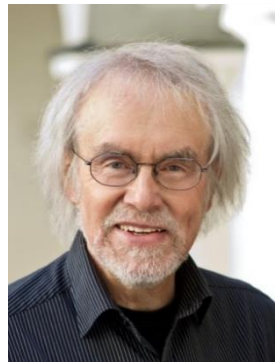
Explanation of BSM B_i parameters ($K^0 - \bar{K}^0$ Mixing)
obtained by Lattice QCD 1804.02401 (AJB + Gérard)

★ 3.

More Results this Summer



Jason Aebischer



AJB



J.-M. Gérard

Section 2

ε'/ε strikes back

2015 Anatomy of ε'/ε : 1507.06345



AJB



Martin Gorbahn



Sebastian Jäger



Matthias
Jamin



AJB



Jean-Marc Gérard

Large N news
1507.06326

FSI
1603.05686

ε'/ε strikes back (CP-Violation in $K_L \rightarrow \pi\pi$)

New results on hadronic matrix elements of QCD penguin (B_6) and electroweak penguin (B_8) operators

Large N approach to QCD

$$: B_6 < B_8 < 1$$



Upper Bound on ε'/ε in the Standard Model

AJB + Gérard (1507.06326)

Supported by Lattice QCD

$$: B_6 = 0.57 \pm 0.19 \quad B_8 = 0.76 \pm 0.05$$

RBC-UKQCD

Anatomy of ε'/ε in the Standard Model

: NLO

$$(\varepsilon'/\varepsilon)_{SM} = (1.9 \pm 4.5) \cdot 10^{-4}$$

AJB, Gorbahn, Jäger, Jamin (1507.06345)

$$(\varepsilon'/\varepsilon)_{SM} = (6.0 \pm 2.4) \cdot 10^{-4} \text{ for } B_6 = B_8 = 0.76$$

$$(8.6 \pm 3.2) \cdot 10^{-4} \text{ for } B_6 = B_8 = 1.0$$

$$(\varepsilon'/\varepsilon)_{exp} = (16.6 \pm 2.3) \cdot 10^{-4}$$

Possible New Physics

Implications for $K \rightarrow \pi\nu\bar{\nu}$

Z' general (AJB, Buttazzo, Knecht, 1507.08672)

Littlest Higgs Model (Blanke, AJB, Recksiegel, 1507.06316)

331 Models (AJB, De Fazio, 1512.02869, 1604.02344)

New Strategy (AJB, 1601.00005)

Vector-like Quarks (Bobeth, AJB, Celis, Jung, 1609.04783)

Leptoquarks (Bobeth, AJB, 1712.01295)

More papers later

(1703.04753)

2016 Standard Model Results

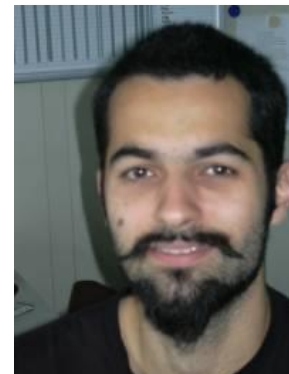
Teppei Kitahara



Ulrich Nierste



Paul Tremper



NLO

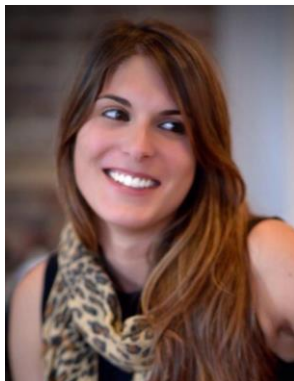
$$\left(\varepsilon'/\varepsilon\right)_{\text{SM}} = (1 \pm 5) \cdot 10^{-4}$$

1607.06727

2018

First NNLO Result for $(\varepsilon'/\varepsilon)_{\text{SM}}$

Maria Cerda-Sevilla



Martin Gorbahn



Sebastian Jäger



Ahmet Kokulu



New
IAS
Postdoc

New
TUM
Postdoc

Four dominant contributions to ε'/ε in the SM

AJB, Jamin, Lautenbacher (1993); AJB, Gorbahn, Jäger, Jamin (2015)

$$\text{Re}(\varepsilon'/\varepsilon) = \left[\frac{\text{Im}(V_{td} V_{ts}^*)}{1.4 \cdot 10^{-4}} \right] 10^{-4} \left[-3.6 + 21.4 \cdot B_6^{(1/2)} + 1.2 - 10.4 \cdot B_8^{(3/2)} \right]$$

(NLO) (Q₄)

(V-A) ⊗ (V-A) QCD Penguins	(V-A) ⊗ (V+A) QCD Penguins	(V-A) ⊗ (V-A) EW Penguins	(V-A) ⊗ (V+A) EW Penguins
-------------------------------	-------------------------------	------------------------------	------------------------------

From ReA₀ From ReA₂

Assumes that ReA₀ and ReA₂ ($\Delta I=1/2$ Rule) fully described by SM (includes isospin breaking corrections)

Extracted from



RBC-UKQCD

$B_6^{(1/2)} = B_8^{(3/2)} = 1$ in the large N limit

: $B_6^{(1/2)} = 0.57 \pm 0.19$ $B_8^{(3/2)} = 0.76 \pm 0.05$

Why $B_6^{(1/2)} < B_8^{(3/2)} < 1$?

and not $B_6^{(1/2)} > 1$, $B_8^{(3/2)} < 1$ (Pallante, Pich... FSI
2000)

Answer in Large N (Dual QCD) Approach

AJB + Gérard (1507.06326)

Before 2015 it was wrongly assumed that

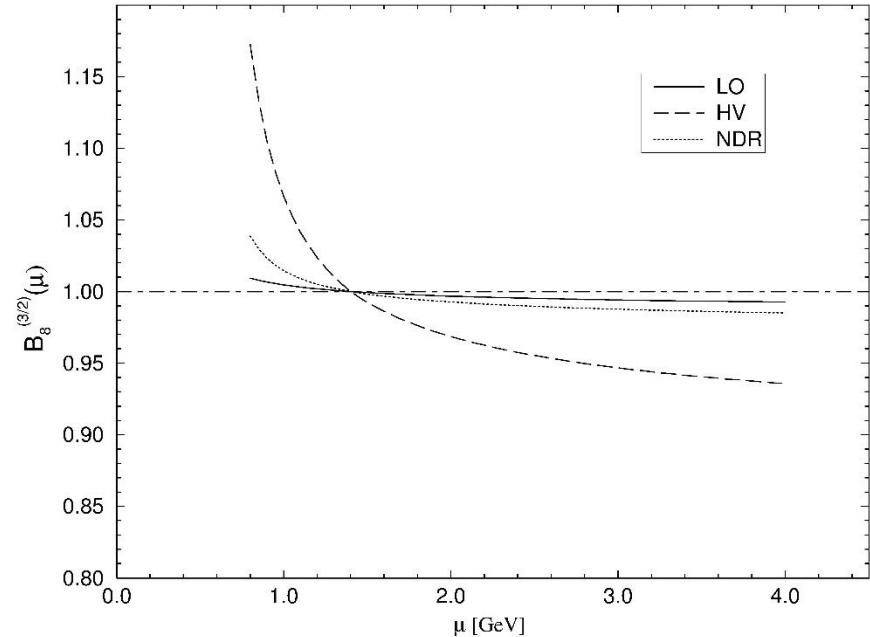
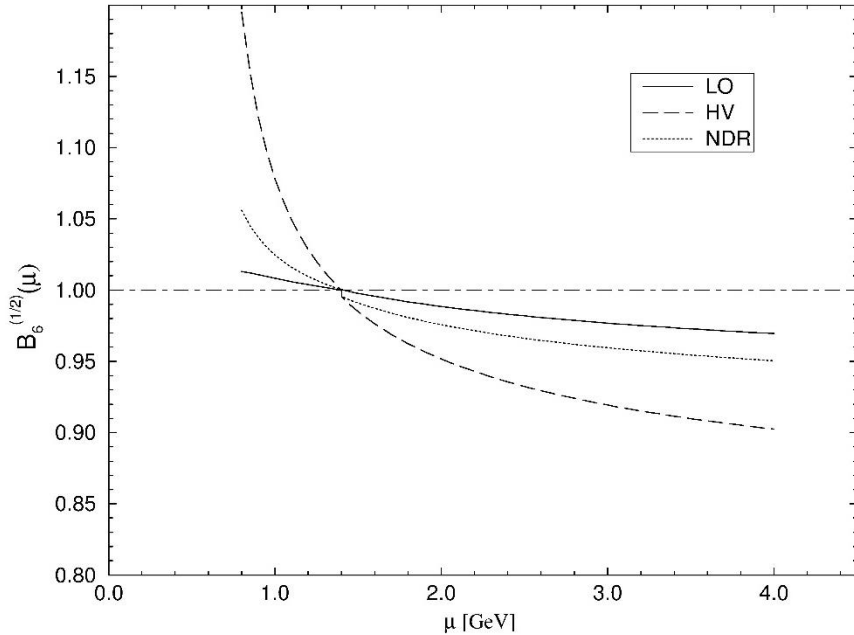
$$B_6^{(1/2)} = B_8^{(3/2)} = 1 \quad \text{at } \mu \approx 0(1 \text{ GeV})$$

But $B_6^{(1/2)} = B_8^{(3/2)} = 1$ is large N prediction
for $\mu = m_\pi$ not $\mu = 0(1 \text{ GeV})$

Meson evolution $m_\pi \rightarrow \mu = 0(1 \text{ GeV})$ suppresses
 $B_6^{(1/2)}$ and $B_8^{(3/2)}$ below 1 and $B_6^{(1/2)}$ stronger than $B_8^{(3/2)}$
in accordance with quark evolution for $\mu > 1 \text{ GeV}$

B_6 and B_8 in the Perturbative Regime (1993!)

AJB, Jamin, Lautenbacher, (9303284)

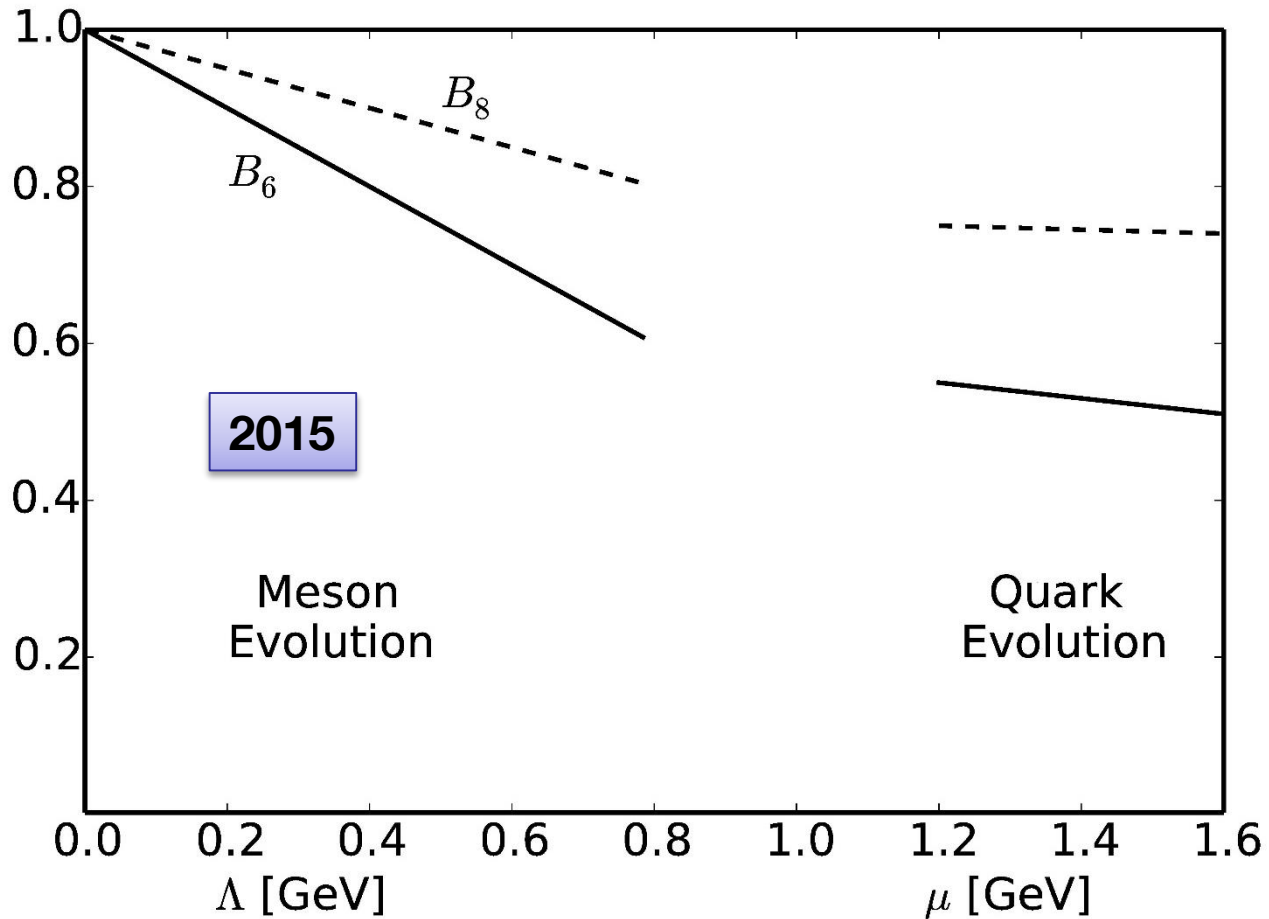


B_6 and B_8 decrease with increasing μ !

Note $B_6 = B_8 = 1$ at $\mu = m_c$ wrong!!

Scale Dependence of B_6 and B_8

AjB+ Gerard (1507.06326)



FSI in $K \rightarrow \pi\pi$

AJB, Gérard 1603.05686

**Relevant for $\Delta I=1/2$ Rule
(in agreement with Pallante, Pich,...)**

**Less important for ε'/ε
(in variance with Pallante, Pich,...)**

**New application of dual QCD to $K \rightarrow \pi l^+ l^-$
(Caluccio-Leskow, D'Ambrosio, Greynat, Nath, 1604.09721)**

(see next talk)

As the existence of Meson Evolution has been questioned over last 30 years by some Chiral Experts by some Lattice Experts

Let me demonstrate its existence
by considering BSM operators in $(K^0 - \bar{K}^0 \text{ Mixing})$

Very
good
test !

Important

: The controversial issue of
Final State interactions is
absent here !!!

and four parameters to our disposal B_2, B_3, B_4, B_5

ΔS = 2 Operators in SUSY Basis

SM

$$O_1 = \left(\bar{s}^\alpha \gamma_\mu P_L d^\alpha \right) \left(\bar{s}^\beta \gamma_\mu P_L d^\beta \right) \rightarrow B_1$$

BSM

$$\left\{ \begin{array}{l} O_2 = \left(\bar{s}^\alpha P_L d^\alpha \right) \left(\bar{s}^\beta P_L d^\beta \right) \rightarrow B_2 \\ O_3 = \left(\bar{s}^\alpha P_L d^\beta \right) \left(\bar{s}^\beta P_L d^\alpha \right) \rightarrow B_3 \\ O_4 = \left(\bar{s}^\alpha P_L d^\alpha \right) \left(\bar{s}^\beta P_R d^\beta \right) \rightarrow B_4 \\ O_5 = \left(\bar{s}^\alpha P_L d^\beta \right) \left(\bar{s}^\beta P_R d^\alpha \right) \rightarrow B_5 \end{array} \right.$$

$$\langle O_i(\mu) \rangle \approx \frac{B_i(\mu)}{m_s^2(\mu)}$$

$$B_1(0) = 0.75 \Rightarrow B_1(0.7 \text{ GeV}) = 0.62 \quad || \quad 0.61 = B_1(1 \text{ GeV}) \Leftarrow 0.53 = B_1(3 \text{ GeV})$$

$N \rightarrow \infty$

Meson Evolution

Gap filled
vector mesons
(2014)

Quark-Gluon
Evolution

LQCD

DQCD

Explaining Values for B_2, B_3, B_4, B_5 from Lattice QCD

(AJB + Gérard, 1804.02401)

(ETM15, SWME, RBC-QCD)

μ	B_2	B_3	B_4	B_5	$K^0 - \bar{K}^0$ mixing
3 GeV	0.49	0.77	0.90	0.65	AJB Lattice Average ($\pm 5\%$)
Quark Gluon Evolution ↓ 1 GeV					<div style="border: 1px solid black; padding: 2px; display: inline-block;"> $B_2=B_3=B_4=B_5=1$ </div> <div style="border: 1px solid black; padding: 2px; display: inline-block;"> Vacuum insertion </div>
} gap : Vector mesons					
(0.70) GeV	0.79	0.96	0.83	0.30	Meson Evolution in the chiral limit
Meson Evolution ↑ Factorization Scale ≈ 0	1.2	3.0	1.0	0.23	← $N \rightarrow \infty$

Important !

$$\langle \mathbf{0}_i(\mu) \rangle \approx \frac{B_i(\mu)}{m_s^2(\mu)}$$

Similar to B_6 and B_8

No FSI
Meson evolution
Exhibited much
clearer than in
 $K \rightarrow \pi\pi$

This insight in B_i values from Lattice has been
obtained from DQCD without ANY input beyond $\Lambda \approx m_\rho$
(Only pseudoscalar masses, F_K and α_{QCD} involved)

No low-energy constants L_i etc. familiar from Chiral Pert. Th.

Question : Can this insight be obtained from Chiral Pert. Th. ?

ε'/ε anomaly is the largest anomaly in flavour physics !

Based on DQCD,
not Lattice yet !

(A.J. Buras)

$$(\varepsilon'/\varepsilon) = (\varepsilon'/\varepsilon)_{\text{SM}} + (\varepsilon'/\varepsilon)_{\text{NP}}$$

$$(\varepsilon'/\varepsilon)_{\text{NP}} = \kappa_{\varepsilon'} \cdot 10^{-3}$$

$$0.5 < \kappa_{\varepsilon'} < 1.5$$

$$(\varepsilon'/\varepsilon)_{\text{SM}} < (6.0 \pm 2.4) \cdot 10^{-4}$$

$$(\varepsilon'/\varepsilon)_{\text{exp}} = (16.6 \pm 2.3) \cdot 10^{-4}$$

Dual
QCD

Section 3

$$\mathbf{K}^+ \rightarrow \pi^+ \nu \bar{\nu} \text{ and } \mathbf{K}_L \rightarrow \pi^0 \nu \bar{\nu}$$

in the Standard Model

1503.02693



AJB



D. Buttazzo

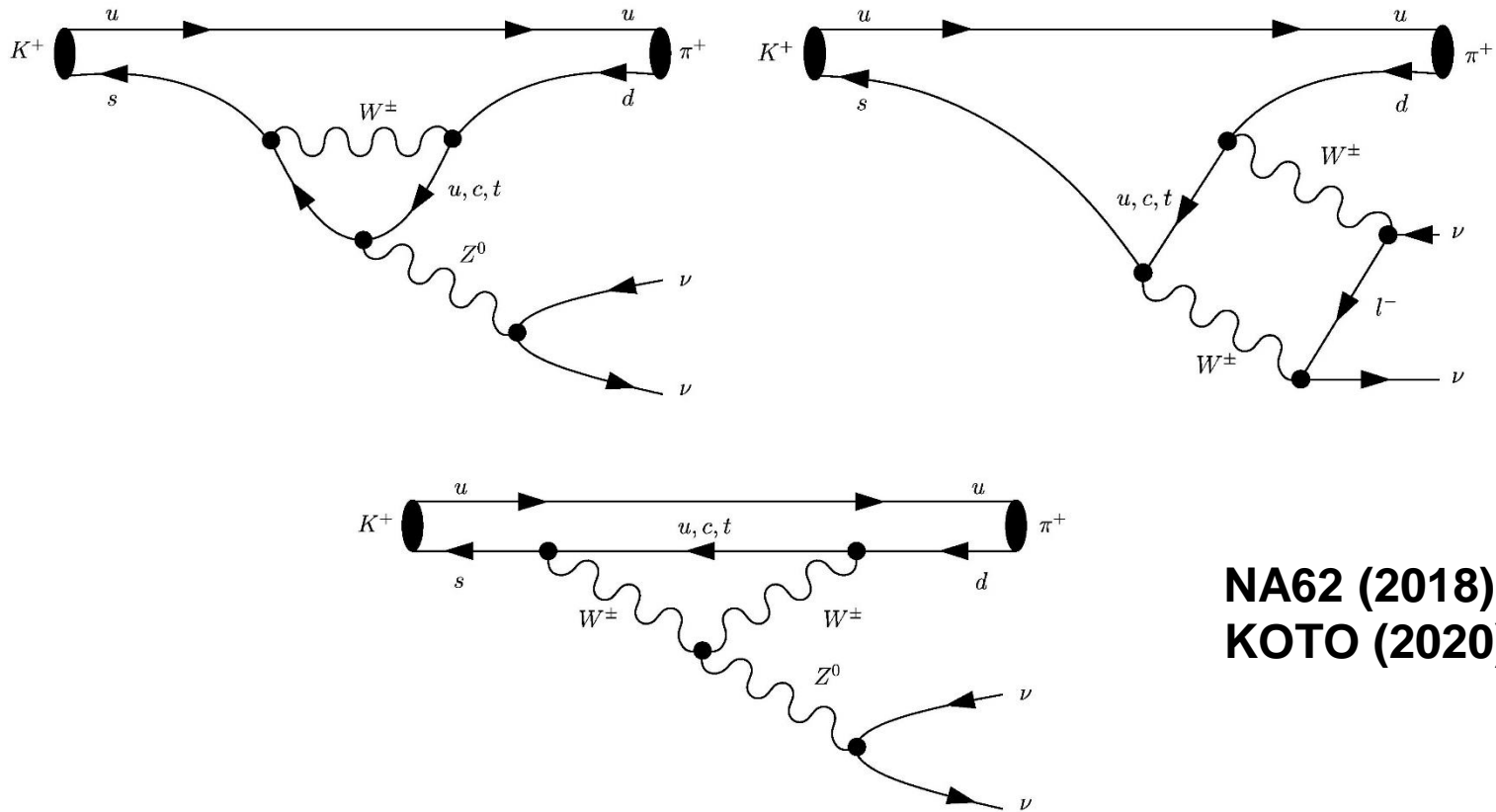


J. Girrbach-Noe



R. Kneijens

Waiting for $K^+ \rightarrow \pi^+ \nu \bar{\nu}$ and $K_L \rightarrow \pi \nu \bar{\nu}$



NA62 (2018)
KOTO (2020)

AJB, M. Lautenbacher, G. Ostermaier (9303284)

AJB, F. Schwab, S. Uhlig (0405132)

$K^+ \rightarrow \pi^+ \nu \bar{\nu}$ and $K_L \rightarrow \pi^0 \nu \bar{\nu}$ in the SM

QCD Corrections:

NLO Buchalla, AJB; Misiak, Urban (93, 98)
 NNLO AJB, Gorbahn, Haisch, Nierste (2005)

NLO EW Corrections:

Large m_t : Buchalla, AJB (1997)
 Exact NLO (m_t): Brod, Gorbahn, Stamou (2010)
 " " (m_c): Brod, Gorbahn (2008)

LD Effects:

Isidori, Mescia, Smith (2005)
 Mescia, Smith (2007)

+ Isospin breaking corrections



TH uncertainties at the level of 2% in BR

Unique in Flavour Physics !!

But significant parametric uncertainties

Data

due to $|V_{ub}|, |V_{cb}|, \gamma$



NA62 : 1 Event !

$$\text{Br}(K^+ \rightarrow \pi^+ \nu \bar{\nu}) = (17.3 \pm 11) \cdot 10^{-11}$$

$$\text{Br}(K_L \rightarrow \pi^0 \nu \bar{\nu}) \leq 2.6 \cdot 10^{-8}$$

CKM Uncertainties

AJB, Buttazzo,
Girrbach-Noe,
Knegjens
1503.02693

$$\text{Br}(\text{K}^+ \rightarrow \pi^+ \nu \bar{\nu}) = (8.39 \pm 0.30) \cdot 10^{-11} \left[\frac{|V_{cb}|}{0.0407} \right]^{2.8} \left[\frac{\gamma}{73.2^\circ} \right]^{0.74}$$
$$\text{Br}(\text{K}_L \rightarrow \pi^0 \nu \bar{\nu}) = (3.36 \pm 0.05) \cdot 10^{-11} \left[\frac{|V_{ub}|}{3.88 \cdot 10^{-3}} \right]^2 \left[\frac{|V_{cb}|}{0.0407} \right]^2 \left[\frac{\sin \gamma}{\sin(73.2)} \right]^2$$

$$\text{Br}(\text{K}^+ \rightarrow \pi^+ \nu \bar{\nu}) = (8.39 \pm 0.58) \cdot 10^{-11} \left[\frac{\gamma}{73.2^\circ} \right]^{0.81} \left[\frac{\bar{\text{Br}}(\text{B}_s \rightarrow \mu^+ \mu^-)}{3.4 \cdot 10^{-9}} \right]^{1.42} \left[\frac{227.7}{F_{B_s}} \right]^{2.84}$$
$$\text{Br}(\text{K}^+ \rightarrow \pi^+ \nu \bar{\nu}) = (8.39 \pm 1.11) \cdot 10^{-11} \left[\frac{|\varepsilon_K|}{2.23 \cdot 10^{-3}} \right]^{1.07} \left[\frac{\gamma}{73.2^\circ} \right]^{-0.11} \left[\frac{V_{ub}}{3.88 \cdot 10^{-3}} \right]^{-0.95}$$

$$\text{Br}(\text{K}^+ \rightarrow \pi^+ \nu \bar{\nu}) = (8.4 \pm 1.0) \cdot 10^{-11}$$
$$\text{Br}(\text{K}_L \rightarrow \pi^0 \nu \bar{\nu}) = (3.4 \pm 0.6) \cdot 10^{-11}$$

Section 3

$\varepsilon'/\varepsilon, \varepsilon_K, \mathbf{K} \rightarrow \pi\nu\bar{\nu}, \Delta\mathbf{M}_K$

beyond SM

AJB (1601.00005)

**What are the implications
of NP in ε'/ε and ε_K on
 $\mathbf{K} \rightarrow \pi\nu\bar{\nu}$ and $\Delta\mathbf{M}_K$?**

ε'/ε within SM

$$\varepsilon'/\varepsilon \sim \left[\frac{\text{Re } A_2}{\text{Re } A_0} \text{Im } C_6 \langle Q_6 \rangle_0 - \text{Im } C_8 \langle Q_8 \rangle_2 + \text{smaller contributions} \right]$$
$$\left\{ \frac{\text{Re } A_2}{\text{Re } A_0} \approx \frac{1}{22} \quad \frac{\text{Im } C_6}{\text{Im } C_8} \approx 90 \quad \frac{\langle Q_8 \rangle_2}{\langle Q_6 \rangle_0} \approx 2 \right\} \Rightarrow \text{strong cancellations}$$

ε'/ε beyond SM (Q_6, Q_8, Q'_6, Q'_8)

- 1.** Generally Q_8 wins over Q_6 because $\left(\frac{\text{Im } C_6}{\text{Im } C_8} \right)^{\text{NP}} \approx 0(1)$ but can provide $\Delta(\varepsilon'/\varepsilon) > 0$
- 2.** Q_6 wins over Q_8 in the presence of a flavour symmetry forbidding Q_8
- 3.** Chromomagnetic operators (not in this talk)

General Z' at Work

Can solve anomalies in R_K, R_{K^*}, P_5'
(many papers)

Here : $\varepsilon'/\varepsilon, K^+ \rightarrow \pi^+ \nu \bar{\nu}, K_L \rightarrow \pi^0 \nu \bar{\nu}, \Delta M_K$

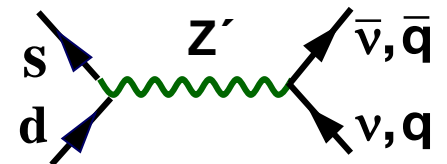


Q_6, Q_6' – QCD Penguin operators

Q_8, Q_8' – Electroweak Penguin operators

$$Q_6 = (\bar{s}_\alpha d_\beta)_{V-A} \sum_q (\bar{q}_\beta q_\alpha)_{V+A}$$

$$Q_8 = (\bar{s}_\alpha d_\beta)_{V-A} \sum_q e_q (\bar{q}_\beta q_\alpha)_{V+A}$$



Strategy (Z')

AJB (1601.00005)

$$\left(\varepsilon'/\varepsilon\right)^{NP} = \kappa_{\varepsilon'} \cdot 10^{-3}$$

$$0.5 \leq \kappa_{\varepsilon'} \leq 1.5$$

(Im)

$$\varepsilon_{\kappa}^{NP} = \kappa_{\varepsilon} \cdot 10^{-3}$$

$$0.1 \leq \kappa_{\varepsilon} \leq 0.4$$

(Im, Re)

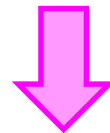
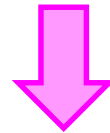
ε_{κ} more important than $K_L \rightarrow \mu^+\mu^-$ in Z' models

Re and Im Parts: Z' Couplings

$\Delta_L^{sd}(Z')$, $\Delta_R^{sd}(Z')$

$$K^+ \rightarrow \pi^+ \nu \bar{\nu}, \quad K_L \rightarrow \pi^0 \nu \bar{\nu}, \quad K_L \rightarrow \mu^+ \mu^-, \quad \Delta M_K$$

(Re, Im) (Im) (Re) (Im, Re)



Basic Structure of NP Contributions

AJB (1601.00005)

$$\begin{array}{ll} (\varepsilon'/\varepsilon)^{\text{NP}} \rightarrow \text{Im} & \varepsilon_{\text{K}}^{\text{NP}} \rightarrow \text{Im} \cdot \text{Re} \\ (\kappa_{\varepsilon'} \geq 0.5) & (\kappa_{\varepsilon} \geq 0.1) \\ \Delta M_{\text{K}}^{\text{NP}} \sim \left[(\text{Re})^2 - (\text{Im})^2 \right] \end{array}$$

Dominance of $Q_6 (Q_6')$ \Rightarrow $\text{Im} \gg \text{Re} \Rightarrow \left\{ \Delta M_{\text{K}}^{\text{NP}} < 0 \right\}$
(large)

Dominance of $Q_8 (Q_8')$ \Rightarrow $\text{Re} \gg \text{Im} \Rightarrow \left\{ \Delta M_{\text{K}}^{\text{NP}} > 0 \right\}$
(small)



**Distinction between
these scenarios**

Main Message

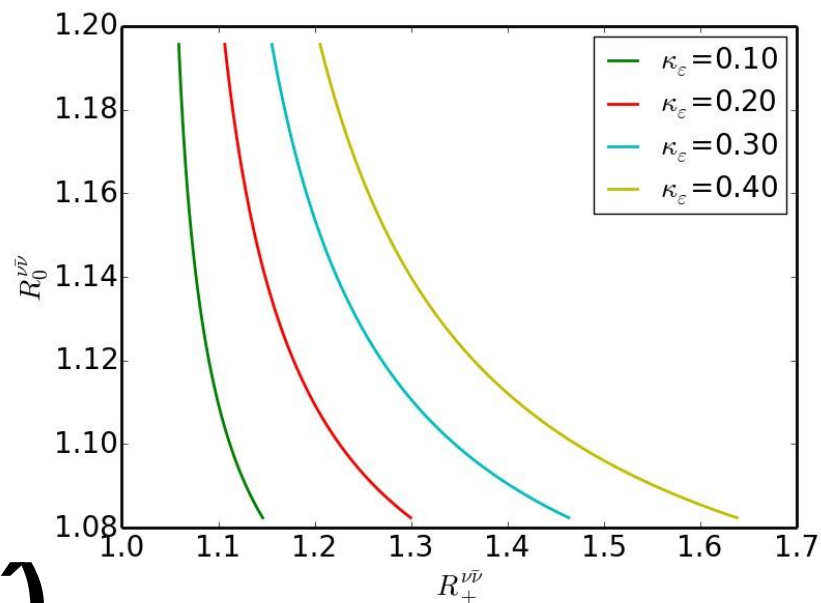
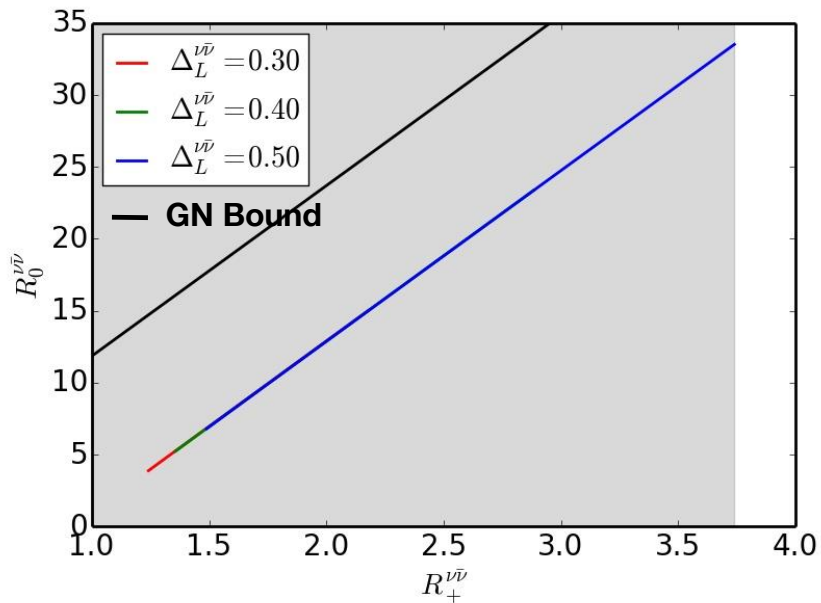


Correlation between ε'/ε and $K \rightarrow \pi\nu\bar{\nu}$ in Z' scenarios depends on whether QCP Penguin (Q_6) or EWP (Q_8) dominates NP in ε'/ε

QCDP (Q₆)

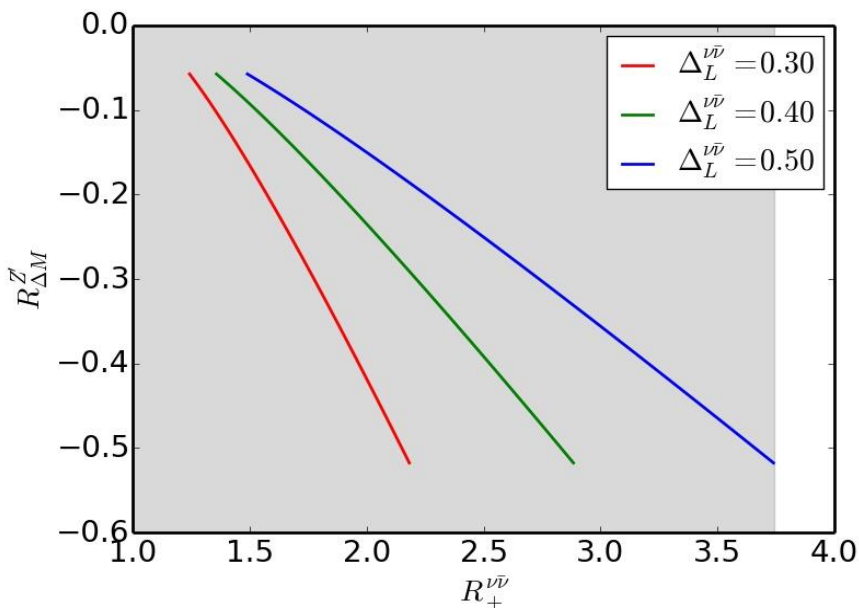
(0.5 < κ_ε' < 1.5)

EWP (Q₈)



(Z)

(R_{ΔM}^{Z'} > 0 but small)

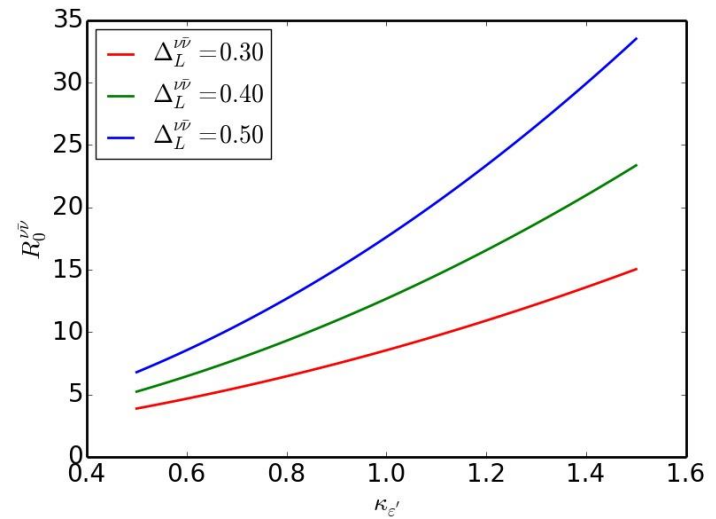
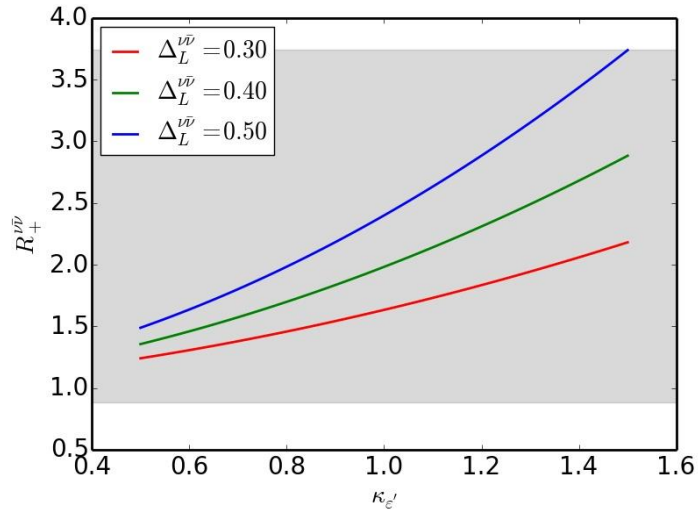


$$R_+^{v\bar{v}} = \frac{\text{Br}(K^+ \rightarrow \pi^+ v\bar{v})}{\text{Br}(K^+ \rightarrow \pi^+ v\bar{v})_{\text{SM}}}$$

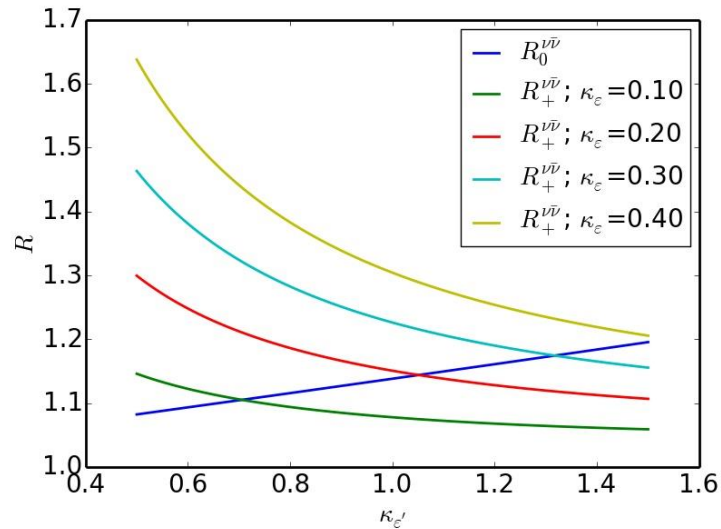
$$R_0^{v\bar{v}} = \frac{\text{Br}(K_L \rightarrow \pi^0 v\bar{v})}{\text{Br}(K_L \rightarrow \pi^0 v\bar{v})_{\text{SM}}}$$

$$R_{\Delta M}^{Z'} = \frac{(\Delta M_K)^{\text{NP}}}{(\Delta M_K)^{\text{exp}}}$$

QCD Penguin (Q_6)



Electroweak Penguin (Q_8)



(Z)

Section 5

BSM Models and ϵ'/ϵ

NP Models and ε'/ε Anomaly

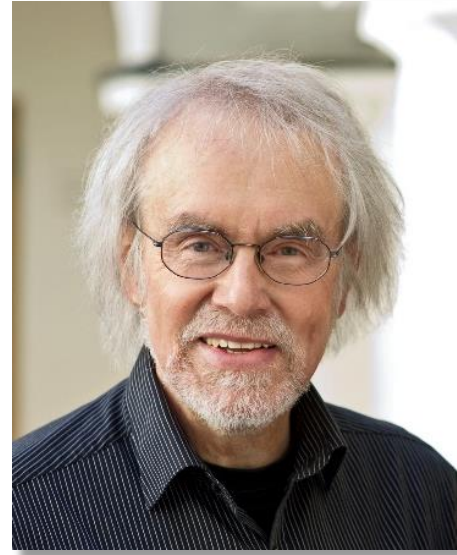
Littlest Higgs (T parity)	Blanke, AJB, Recksiegel (1507.06316)
Z-FCNC	AJB (1601.00005), Bobeth, AJB, Celis, Jung (1703.04753) Endo, Kitahara, Mishima, Yamamoto (1612.08839)
Z'-Models	AJB (1601.00005), AJB, Buttazzo, Knegjens (1507.08672)
331- Models	AJB, De Fazio (1512.02869, 1604.02344)
Vector-Like Quarks	Bobeth, AJB, Celis, Jung (1609.04783)
SUSY	Tanimoto, Yamamoto (1603.07960) Kitahara, Nierste, Tremper (1604.07400) Endo, Mishima, Ueda, Yamamoto (1608.01444) Crivellin, D'Ambrosio, Kitahara, Nierste (1703.05786) Endo, Goto, Kitahara, Mishima, Ueda, Yamamoto (1712.04959)
Right-handed Currents	Cirigliano, Dekens, De Vries, Meraghetti (1703.04751)
$SU(2)_L \otimes SU(2)_R \otimes U(1)_{B-L}$	Haba, Umeeda, Yamada (1802.09903)
Leptoquark Models	Bobeth, AJB (1712.01295)

Leptoquarks meet ε'/ε and rare K Processes

1712.01295



Christoph Bobeth



AJB

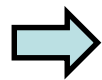
ε'/ε and rare K Processes

1.

Assuming that the upper bound on $(\varepsilon'/\varepsilon)_{\text{SM}}$ from Dual QCD is correct: Largest anomaly!

2.

But in contrast to R_D, R_{D^*} (LQs contribute there at tree level) in ε'/ε leptoquarks contribute at one-loop (RG running and box contributions)



Large $\text{Im}(Y)$ couplings required

3.

Problems with rare decays

$K \rightarrow \pi \nu \bar{\nu}$, $K_L \rightarrow \pi^0 l^+ l^-$, $K_S \rightarrow \mu^+ \mu^-$ (tree – level)

but also ΔM_K , ε_K

Leptoquark Models

Scalar Leptoquark

S_1

\tilde{S}_1

R_2

\tilde{R}_2

S_3

$SU(2)_L$

singlet

singlet

doublet

doublet

triplet

Vector Leptoquarks

U_1

\tilde{U}_1

V_2

\tilde{V}_2

U_3

Favoured
by B-physics
anomalies

U_1

Barbieri et al
Isidori et al
Crivellin et al

S_1, S_3

Crivellin et al
(1703.09226)
Buttazzo et al
(1706.07808)

S_3, \tilde{R}_2

Fajfer et al
(1706.0779)

Eliminating Leptoquarks as origin of ε'/ε anomaly

Bobeth + AJB 1712.01295

Step 1

\tilde{U}_1, \tilde{V}_2

do not contribute to ε'/ε

Step 2

$\tilde{S}_1, \tilde{R}_2, S_3, U_3$

do not generate Q_8 operator through RG

Im (Yukawa) very large
to get ε'/ε



Bounds on $K \rightarrow \pi\nu\bar{\nu}$
 $K_L \rightarrow \pi^0 l^+ l^-$, ΔM_K
strongly violated

Step 3

S_1, R_2, V_2, U_1

almost ruled out

Disfavoured

$$C_9^{NP} = C_{10}^{NP}$$

Favoured
by B-physics

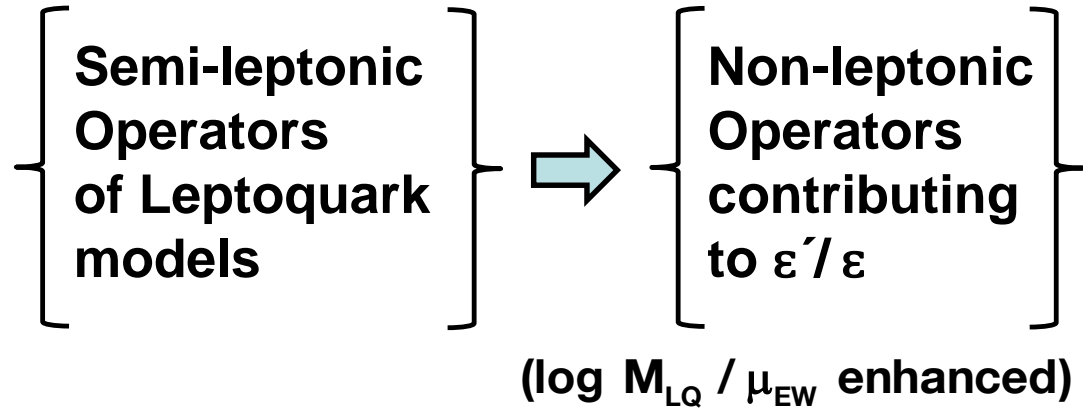
$$(C_9^{NP} = -C_{10}^{NP})$$

Basic Dynamics for ε'/ε in Leptoquark Models

Renormalization
Electroweak Evolution
from M_{LQ} to low-energy
+ QCD evolution
enhancing Q_8

(SMEFT)

Box-Diagrams in
models with left-handed
and right-handed
couplings contributing
directly to ε'/ε (Q_8)



: selects

S_1, R_2, U_1, V_2

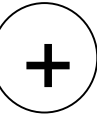


Favoured by
B-physics anomalies

U_1 Model meets ε'/ε and rare K Decays

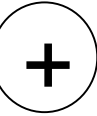
1.

Generation of Q_8 through RG group!



2.

No tree-level contributions to $K \rightarrow \pi \nu \bar{\nu}$, generated through RG but still consistent with bounds even for $\kappa_{\varepsilon'} \approx 1.0$

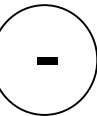


3.

If only left-handed or right-handed couplings present ruled out through

$$\left(\begin{array}{l} K_L \rightarrow \pi^0 e^+ e^-, K_L \rightarrow \pi \mu^+ \mu^+, \\ K_S \rightarrow \mu^+ \mu^- \end{array} \right)$$

(the only hope: couplings between τ and d, s)

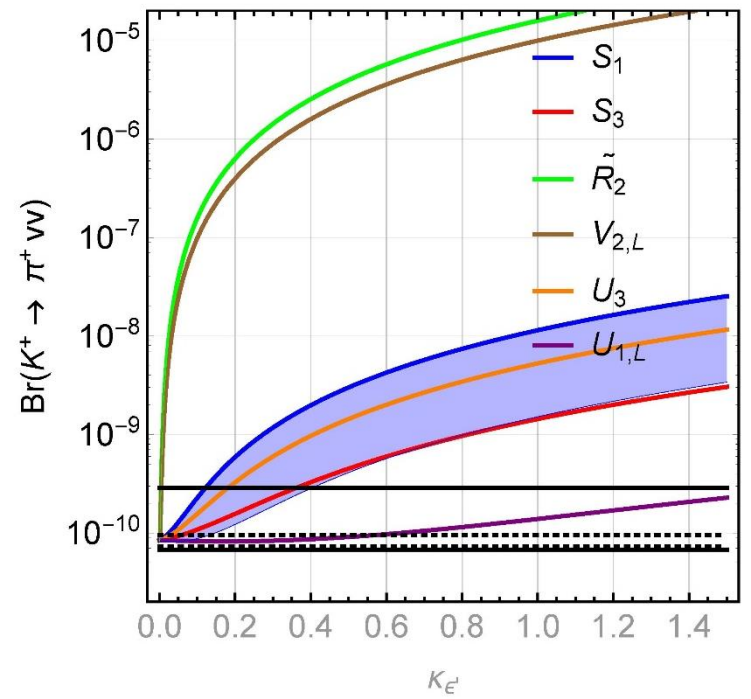
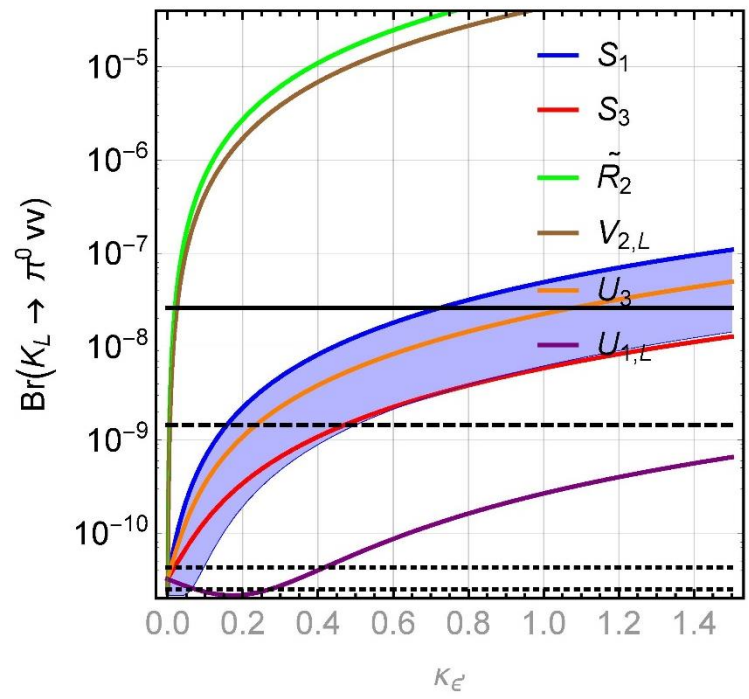


4.

Box contributions with left- and right-handed couplings could help but UV completion needed to do the calculation. Would also generate LR contributions to $\Delta M_K, \varepsilon_K$: very dangerous!

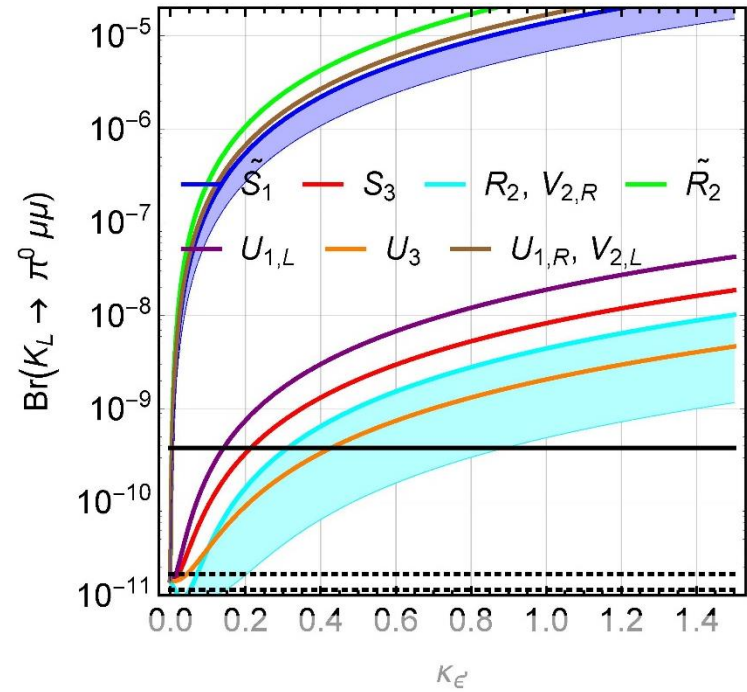
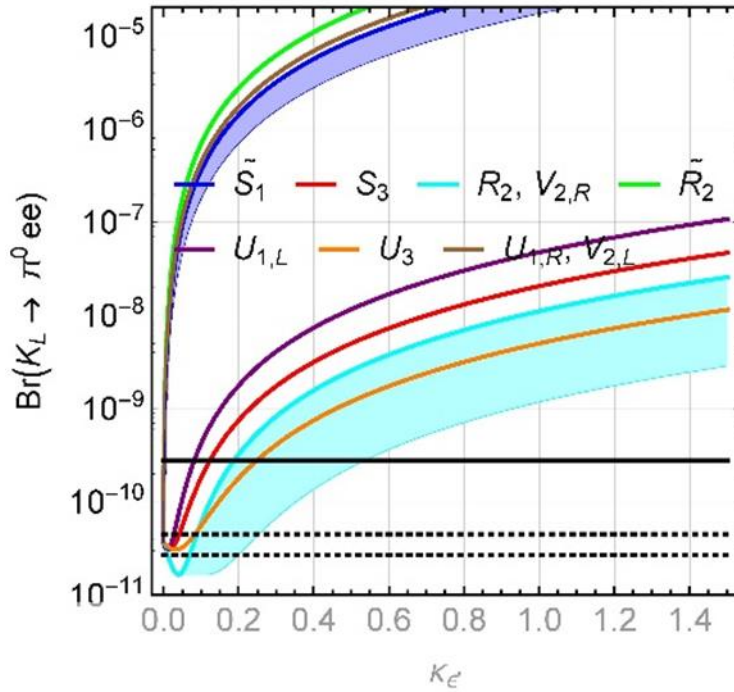


Leptoquarks facing ε'/ε and $K \rightarrow \pi\nu\bar{\nu}$



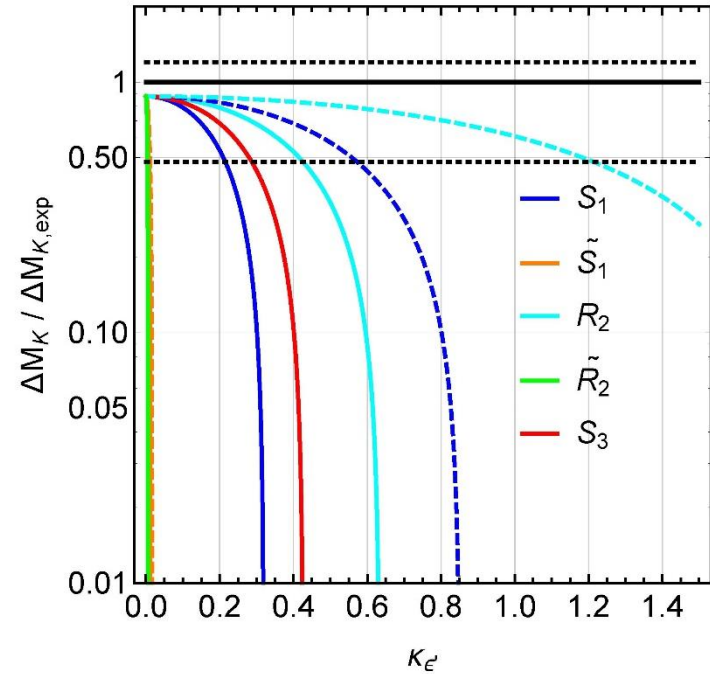
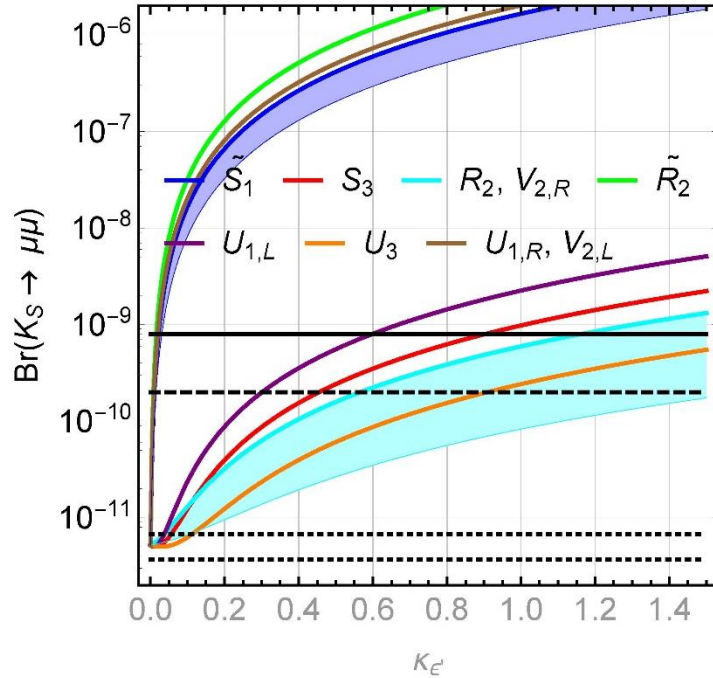
Exp. Bound
 Grossman-Nir Bound

Leptoquarks facing ε'/ε and $K_L \rightarrow \pi^0 l^+ l^-$



— Exp. Bound

Leptoquarks facing ε'/ε and $K_S \rightarrow \mu\mu$



Exp. Bound (LHCb 2017)
 Future LHCb Bound

Main Messages on LQs in ε'/ε and rare K Decays

If improved lattice calculations will confirm the ε'/ε anomaly at the level $(\varepsilon'/\varepsilon)_{\text{NP}} \geq 5 \cdot 10^{-4}$ LQs are likely not responsible for it.

But if ε'/ε anomaly disappears large NP effects from LQs in rare K decays still possible.

(Need non-zero couplings to first generation!!)

(Need imaginary couplings!)

(Need both left-handed and right-handed couplings!)

In contrast to most explanations of B-anomalies

Main Messages from this Talk



The inclusion of meson evolution in the phenomenology of any non-leptonic transition like $K^0 - \bar{K}^0$ mixing, $K \rightarrow \pi\pi$ decays ($\Delta I = 1/2$ Rule, ε'/ε) is mandatory !

Meson Evolution is hidden in LQCD results but among analytic approaches only DQCD takes this important QCD dynamics into account.

**DQCD
Prediction**

· ε'/ε anomaly will be confirmed by RBC-UKQCD this summer !

Open Questions for Coming Years

$$\text{Br}(K^+ \rightarrow \pi^+ \nu \bar{\nu})?$$

NA62

$$\text{Br}(K_L \rightarrow \pi^0 \nu \bar{\nu})?$$

KOTO

$$B \rightarrow K(K^*) \nu \bar{\nu}?$$

Belle

$$(\varepsilon'/\varepsilon)_{SM}, \kappa_{\varepsilon'} ?$$

$$(\varepsilon_K)_{SM}, \kappa_{\varepsilon} ?$$

$$(\Delta M_K)_{SM} ?$$

New Anomalies in Flavour Physics (B, D, LFV)?

New Particles discovered at the LHC?

What about $\Delta I=1/2$ Rule?

(New Physics at 10-20% ?)

Lattice QCD

Can hopefully answer this question.

Coming Years

Flavour Precision Era

LHC Upgrade
E = 14 TeV
(CERN)

Precision
 $B_{d,s}$ – Meson
Decays
LHCb, CMS
KEK (Japan)

★
 $K^+ \rightarrow \pi^+ \nu \bar{\nu}$ ($\sim 10^{-10}$) (CERN)
 $K_L \rightarrow \pi^0 \nu \tilde{\nu}$ ($\sim 3 \cdot 10^{-11}$) J-PARC
(Japan)

Lepton Flavour
Violation

$$\mu \rightarrow e \gamma$$

$$\mu \rightarrow e e e$$

$$\tau \rightarrow \mu \gamma, \tau \rightarrow 3 \mu$$

Electric
Dipole
Moments

★
 $(g-2)_\mu$

Improved
Lattice
Gauge Theory
Calculations

★
 ε'/ε

$$\Delta I = \frac{1}{2} \text{ Rule,}$$
$$\Delta M_K$$

Neutrinos

**Exciting Times are just
ahead of us !!!**

**Exciting Times are just
ahead of us !!!**

Thank You !

Finding Anomaly in ϵ'/ϵ Norway: 2015

