

LFNU in $b \rightarrow s$ transitions in next-to-minimal 331 models

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Based on work in collab. with S. Descotes-Genon
and M. Moscati arXiv:1711.03101

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"From Flavour to New Physics"

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Motivations

- Anomalies in B decays

Already discussed yesterday, thank you

LHCb has been able to probe very rare $b \rightarrow s \ell \ell$ and challenging $b \rightarrow c \ell \nu$ transitions.

Vinícius Franco Lima

- For the first time, we observe in particle physics a large set of **coherent deviations** in observables:

1 in $b \rightarrow s \mu^+ \mu^-$: P'_5 , $\mathcal{B}_{B^+ \rightarrow K^{*+} \mu^+ \mu^-}$, $\mathcal{B}_{B_s \rightarrow \phi \mu^+ \mu^-}$ (low and large-recoil).

2 in LFUV observables: $R_K, R_{K^*}, Q_{4,5}$

Joaquim Matias

Siavash Neshatpour

- $B \rightarrow K^* \mu^+ \mu^-$ angular observable P'_5 (or S_5): **2.8** and **3.0 σ** in [4.0-6.0] and [6.0-8.0] GeV^2 bins with 3 fb^{-1} at LHCb
- $\text{BR}(B_s \rightarrow \phi \mu^+ \mu^-)$: **3.2 σ** tension in the [1-6] GeV^2 bin with 3 fb^{-1} at LHCb (2015)

Anomalies in the decay of the B meson were reported through the measurements of the $b \rightarrow s \ell \ell$ transitions in the form of foll. ratio:

$$R_K = \frac{\mathcal{B}(B^+ \rightarrow K^+ \mu^+ \mu^-)}{\mathcal{B}(B^+ \rightarrow K^+ e^+ e^-)} \bigg|_{q^2=1-6 \text{ GeV}^2} = 0.745^{+0.090}_{-0.074} (\text{stat}) \pm 0.036 (\text{syst})$$

$R_K^{\text{SM}} = 1.003$

Abhishek Iyer

etc, etc....

Flavor anomalies

$b \rightarrow s \mu^+ \mu^-$ anomaly

Several LHCb measurements deviate from Standard model (SM) predictions by 2-3 σ :

- Angular observable P'_5 in $B \rightarrow K^* \mu^+ \mu^-$. LHCb, arXiv:1512.04442
- Branching ratios of $B \rightarrow K \mu^+ \mu^-$, $B \rightarrow K^* \mu^+ \mu^-$, and $B_s \rightarrow \phi \mu^+ \mu^-$. LHCb, arXiv:1403.8044, arXiv:1506.08777, arXiv:1606.04731

Hints for LFU violation in neutral current decays

Measurements of lepton flavor universality (LFU) ratios $R_K^{[1,6]}$, $R_{K^*}^{[0.045,1.1]}$, $R_{K^*}^{[1.1,6]}$ show deviations from SM by about 2.5 σ each. LHCb, arXiv:1406.6482, arXiv:1705.05802

Hints for LFU violation in charged current decays

Measurements of LFU ratios R_D and R_{D^*} by BaBar, Belle, and LHCb show combined deviation from SM by 4 σ .

BaBar, arXiv:1205.5442, arXiv:1303.0571
LHCb, arXiv:1506.08614, arXiv:1708.08856
Belle, arXiv:1507.03233, arXiv:1607.07923, arXiv:1612.00529
HFLAV, arXiv:1612.07233

Peter Stangl

BSM experimental status (also extensively discussed)

Categories of anomalous observables

- Angular observables and branching ratios → “hadronically challenged”
- Ratios: theoretically «clean»

OUTLINE

- ❖ Focus on $b \rightarrow s l l$ decays
- ❖ Choose a viable 331 model allowing LFNU
- ❖ Express Wilson coefficients in that frame
- ❖ Compare with global fits & additional constraints

331 models main features: 1)

P. Frampton '92,
F. Pisano and V. Pleitez, '92...

gauge group

$$SU(3)_c \times SU(3)_L \times U(1)_X$$

spontaneously broken to

$$\rightarrow SU(3)_c \times SU(2)_L \times U(1)_Y$$

spontaneously broken to

$$\rightarrow SU(3)_c \times U(1)_Q$$

$$\hat{Q} = a\hat{T}^3 + \frac{\hat{Y}}{2} = a\hat{T}^3 + \beta\hat{T}^8 + X\mathbb{1}$$

arbitrary a and β

$$a = 1$$

embed isospin doublets $SU(2)_L \times U(1)_Y$ into $SU(3)_L \times U(1)_X$

$$\beta = \pm 1/\sqrt{3}$$

no new particle with exotic charges

$$\beta = -1/\sqrt{3}$$

331 models main features: 2)

Anomaly free

Equal number of 3 and $\bar{3}$ fermionic representations

Minimal 331 model example:

e.g. Buras et al. 1211.1237, 1311.6729,
1405.3850, Diaz et al. 0411263, 309280....

quarks in $SU(3)_L$

2 families x3(color) 3

1 family x3(color) $\bar{3}$

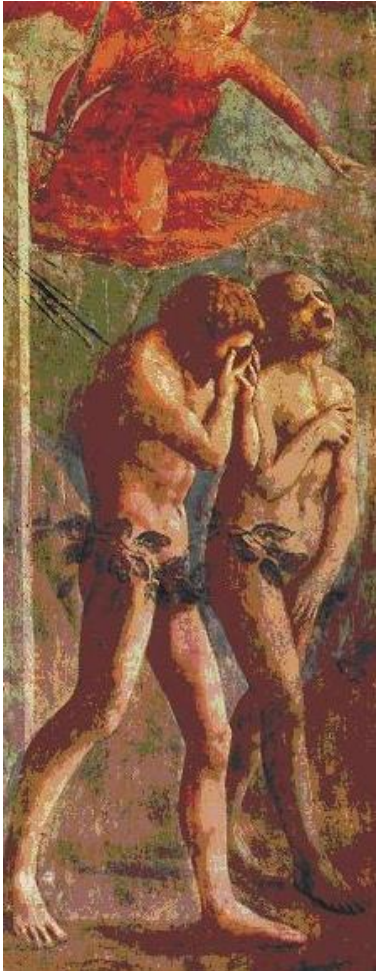
Lepton

All three families fixed to $\bar{3}$

Same representation:
LFNU not allowed

Is that conclusive?

Is there a next-to-minimal 331 model which is compatible with current LFNU hints?



First step towards:

Can 331 models be excluded on the basis of actual anomalies?

Masaccio, 1424

Anomaly cancellation in next-to-minimal 331 models

For the left-handed components

J. M. Cabarcas, et al. 1212.3586, 1310.1407...

- three generations of quarks

$$Q_m^L = \begin{pmatrix} d_m^L \\ -u_m^L \\ \bar{B}_m^L \end{pmatrix} \sim (3, \bar{3}, 0), \quad m = 1, 2$$

$$Q_3^L = \begin{pmatrix} u_3^L \\ d_3^L \\ T_3^L \end{pmatrix} \sim (3, 3, \frac{1}{3})$$

- five generations of leptons

$$\ell_1^L = \begin{pmatrix} e_1^{-L} \\ -\nu_1^L \\ E_1^{-L} \end{pmatrix} \sim (1, \bar{3}, -\frac{2}{3}),$$

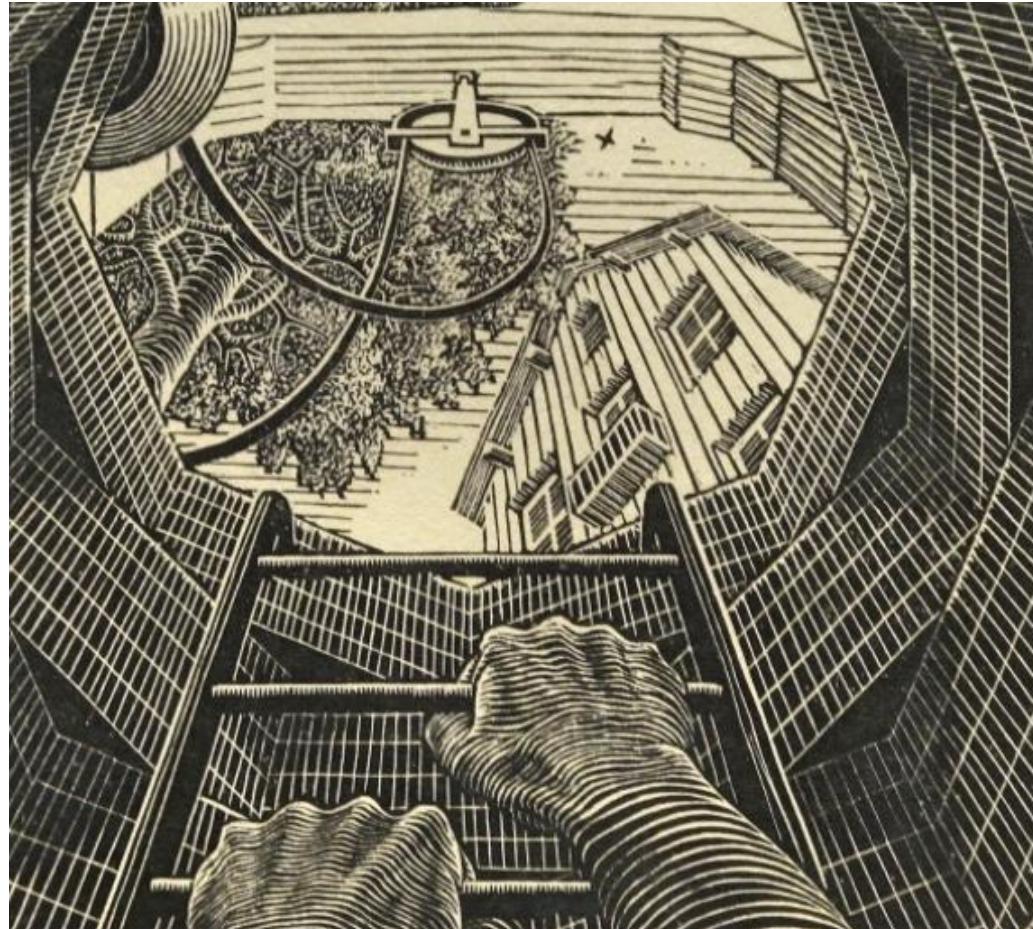
$$\ell_n^L = \begin{pmatrix} \nu_n^L \\ e_n^{-L} \\ N_n^{0L} \end{pmatrix} \sim (1, 3, -\frac{1}{3}), \quad n = 2, 3$$

$$\ell_4^L = \begin{pmatrix} N_4^{0L} \\ E_4^{-L} \\ P_4^{0L} \end{pmatrix} \sim (1, 3, -\frac{1}{3}),$$

$$\ell_5^L = \begin{pmatrix} (E_4^{-R})^c \\ N_5^{0L} \\ (e_3^{-R})^c \end{pmatrix} \sim (1, 3, \frac{2}{3}).$$

SM particles

Analyzing a next-to-minimal 331 model with 5 lepton generations



Escher, 1946

$SU(3)_L \times U(1)_X$ Gauge Bosons

$$W_\mu = W_\mu^a T^a = \frac{1}{2} \begin{pmatrix} W_\mu^3 + \frac{1}{\sqrt{3}} W_\mu^8 & \sqrt{2} W_\mu^+ & W_\mu^4 - i W_\mu^5 \\ \sqrt{2} W_\mu^- & -W_\mu^3 + \frac{1}{\sqrt{3}} W_\mu^8 & W_\mu^6 - i W_\mu^7 \\ W_\mu^4 + i W_\mu^5 & W_\mu^6 + i W_\mu^7 & -\frac{2}{\sqrt{3}} W_\mu^8 \end{pmatrix} \quad W_\mu^a \quad a = 1 \dots 8$$

Charged

$$W_\mu^\pm = \frac{1}{\sqrt{2}} (W_\mu^1 \mp i W_\mu^2)$$

$$V_\mu^\pm = \frac{1}{\sqrt{2}} (W_\mu^6 \mp i W_\mu^7)$$

Neutral

$$W^3, W^{4,5}, W^8, X$$

Mixing patterns among neutral particles

$$W^3, W^{4,5}, W^8, X \xrightarrow[\Lambda_{NP}]{\theta_{331}} W^3, W^{4,5}, B, Z' \xrightarrow[\Lambda_{EW}]{\theta_W} W^{4,5}, Z', A, Z$$

$$\sin \theta_{331} = \frac{g}{\sqrt{g^2 + \frac{g_X^2}{18}}}$$

$$\tan \theta_W = -\sqrt{3} \cos \theta_{331}$$

θ_W Weinberg angle

g $SU(3)_L$ gauge coupling constant

g_X $U(1)_X$ gauge coupling constant

$$\frac{g_X^2}{g^2} = \frac{6 \sin^2 \theta_W}{1 - (1 + \beta^2) \sin^2 \theta_W}$$

$$\epsilon = \Lambda_{EW} / \Lambda_{NP}$$

V^\pm

W^\pm

Massive 1SSB

Massive 2SSB

New particle content

heavy quarks

$$B_{1,2}, T_3$$

heavy leptons

$$E_1^-, E_4^-, N_{2,3,4,5}^0, P_4^0$$

gauge bosons

$$V^\pm, W^{4,5}, Z'$$

extended Higgs sector

$$SU(3)_L \text{ triplets } \chi, \eta, \rho \quad \text{sextets } S_1, S_b, S_c$$

Yukawa coupling

$$D = \begin{pmatrix} d_1 \\ d_2 \\ d_3 \\ B_1 \\ B_2 \end{pmatrix}, \quad U = \begin{pmatrix} u_1 \\ u_2 \\ u_3 \\ T_3 \end{pmatrix} \quad \begin{aligned} D^L &= V^{(d)} D'^L & D^R &= W^{(d)} D'^R \\ U^L &= V^{(u)} U'^L & U^R &= W^{(u)} U'^R \end{aligned}$$

Quark masses defined upon rotation of 5×5 (4x4) unitary matrices

$$\frac{g}{\sqrt{2}} W_\mu^+ \bar{U}^L \gamma^\mu \mathcal{V} D^L = \frac{g}{\sqrt{2}} W_\mu^+ \bar{U}^L \gamma^\mu \begin{pmatrix} 1 & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 \end{pmatrix} D^L = V_{mn}^{CKM} \frac{g}{\sqrt{2}} W_\mu^+ \bar{U}_m'^L \gamma^\mu D_n'^L$$

$$V^{CKM} = V^{(u)\dagger} \mathcal{V} V^{(d)}$$

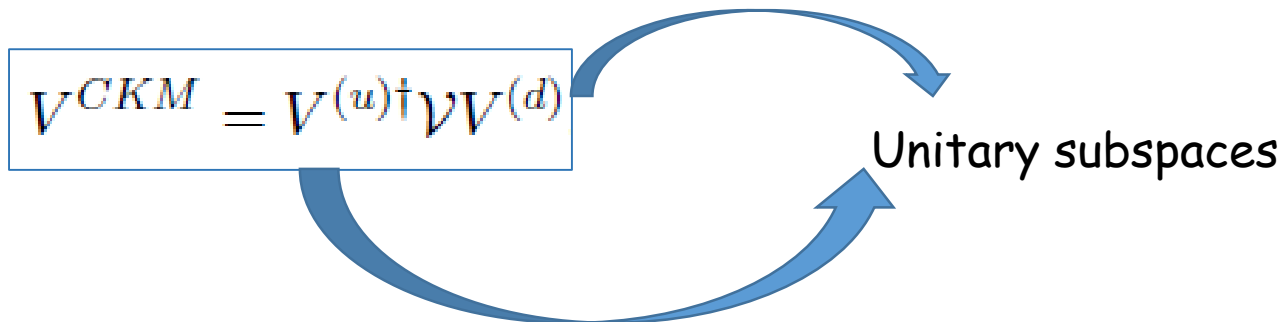
In general not unitary

Mixing patterns

Order by order diagonalization

$$\epsilon = \Lambda_{\text{EW}} / \Lambda_{\text{NP}}$$

- at order ϵ^0 , the SM fields are massless and they only mix among themselves; massive exotic particles mix also only among themselves;
- at order ϵ^1 , there is only mixing between SM and exotic particles;
- the ϵ^2 correction yields a mixing among all the particles of the same flavour vector.



3x 3 SM Unitary at LO

Facing anomalies



Hieronymus Bosch 1482

Effective Analysis $b \rightarrow s l l$ transitions

$$\mathcal{H}_{\text{eff}} = -\frac{4G_F}{\sqrt{2}} V_{tb} V_{ts}^* \sum_i C_i O_i$$

$$\begin{aligned} O_9^\ell &= \frac{e^2}{16\pi^2} (\bar{s} \gamma_\mu P_L b) (\bar{\ell} \gamma^\mu \ell) & O_{9'}^\ell &= \frac{e^2}{16\pi^2} (\bar{s} \gamma_\mu P_R b) (\bar{\ell} \gamma^\mu \ell) \\ O_{10}^\ell &= \frac{e^2}{16\pi^2} (\bar{s} \gamma_\mu P_L b) (\bar{\ell} \gamma^\mu \gamma^5 \ell) & O_{10'}^\ell &= \frac{e^2}{16\pi^2} (\bar{s} \gamma_\mu P_R b) (\bar{\ell} \gamma^\mu \gamma^5 \ell) \end{aligned}$$

- SM $C_9^\ell \simeq 4.1$ $C_{10}^\ell \simeq -4.3$

- BSM contributions in C_9^μ or $(C_9^\mu, C_{9'}^\mu)$ or (C_9^μ, C_{10}^μ) from both LFUV observables and angular observables: additional operators fitted values constrained to remain small

Descotes-Genon et al., 15,
Capdevila et al. 17,
Altmannshofer et al.,
Genget al. 17, Ciuchini et
al. 17, Hurth et al. 17....

BSM contributions

neutral gauge bosons $W^{4,5}, Z', Z, A$

Lowest level in ε

Interactions Z and Z' with RH quarks

$$\mathcal{L}_{Z'} = \frac{\cos \theta_{331}}{g_X} Z'_\mu \left\{ \frac{\sqrt{2} g_X^2}{3\sqrt{3}} \bar{U}^R \gamma^\mu U^R - \frac{g_X^2}{3\sqrt{6}} \bar{D}^R \gamma^\mu D^R \right\}$$

$$\mathcal{L}_Z = \cos \theta_W g Z_\mu \left\{ -2 \cos^2 \theta_{331} \bar{U}^R \gamma^\mu U^R + \cos^2 \theta_{331} \bar{D}^R \gamma^\mu D^R \right\}$$

identity in flavour space: no contribution to $C'_{9,10}$

Z' $(\bar{q}_k q_l)(\bar{\ell}_i \ell_j)$ flavour structure

$$\mathcal{H}_{\text{eff}} \supset \frac{g_X^2}{54 \cos^2 \theta_{331}} \frac{1}{M_{Z'}^2} V_{3k}^{(d)*} V_{3l}^{(d)} \frac{4\pi}{\alpha} \left\{ \left[-\frac{1}{2} V_{1i}^{(e)*} V_{1j}^{(e)} + \frac{1 - 6 \cos^2 \theta_{331}}{2} W_{3i}^{(e)*} W_{3j}^{(e)} + \frac{1 + 3 \cos^2 \theta_{331}}{4} \delta_{ij} \right] O_9^{klij} + \right. \\ \left. + \left[\frac{1}{2} V_{1i}^{(e)*} V_{1j}^{(e)} + \frac{1 - 6 \cos^2 \theta_{331}}{2} W_{3i}^{(e)*} W_{3j}^{(e)} + \frac{-1 + 9 \cos^2 \theta_{331}}{4} \delta_{ij} \right] O_{10}^{klij} \right\}$$

Z

$$\mathcal{H}_{\text{eff}} \supset \frac{\cos^2 \theta_W (1 + \cos^2 \theta_{331})}{8} \frac{g^2}{M_Z^2} \frac{4\pi}{\alpha} \sum_{\lambda} \hat{V}_{\lambda k}^{(d)*} \hat{V}_{\lambda l}^{(d)} \delta_{ij} \left\{ (-1 + 9 \cos^2 \theta_{331}) O_9^{klij} + (1 + 3 \cos^2 \theta_{331}) O_{10}^{klij} \right\}$$

no other contributions: A diagonal, $W^{4,5}$ higher order in ε

Wilson coefficients and LFV

$$\mathcal{H}_{\text{eff}} \supset C_9^{ij} O_9^{ij} + C_{10}^{ij} O_{10}^{ij}$$

k, l quark index fixed at b, s
i, j lepton flavours

$$C_9^{ij} = f^{Z'} \left[-\frac{1}{2} \lambda_{ij}^{(L)} + \frac{1 - 2 \tan^2 \theta_W}{2} \lambda_{ij}^{(R)} + \frac{1 + \tan^2 \theta_W}{4} \delta_{ij} \right] + f^Z (-1 + 3 \tan^2 \theta_W) \delta_{ij}$$

$$C_{10}^{ij} = f^{Z'} \left[\frac{1}{2} \lambda_{ij}^{(L)} + \frac{1 - 2 \tan^2 \theta_W}{2} \lambda_{ij}^{(R)} + \frac{-1 + 3 \tan^2 \theta_W}{4} \delta_{ij} \right] + f^Z (1 + \tan^2 \theta_W) \delta_{ij}$$

$$f^{Z'} = -\frac{1}{2\sqrt{2}G_F V_{tb} V_{ts}^*} \frac{4\pi}{\alpha} \frac{1}{3 - \tan^2 \theta_W} \frac{g^2}{M_{Z'}^2} V_{3k}^{(d)*} V_{3l}^{(d)}$$

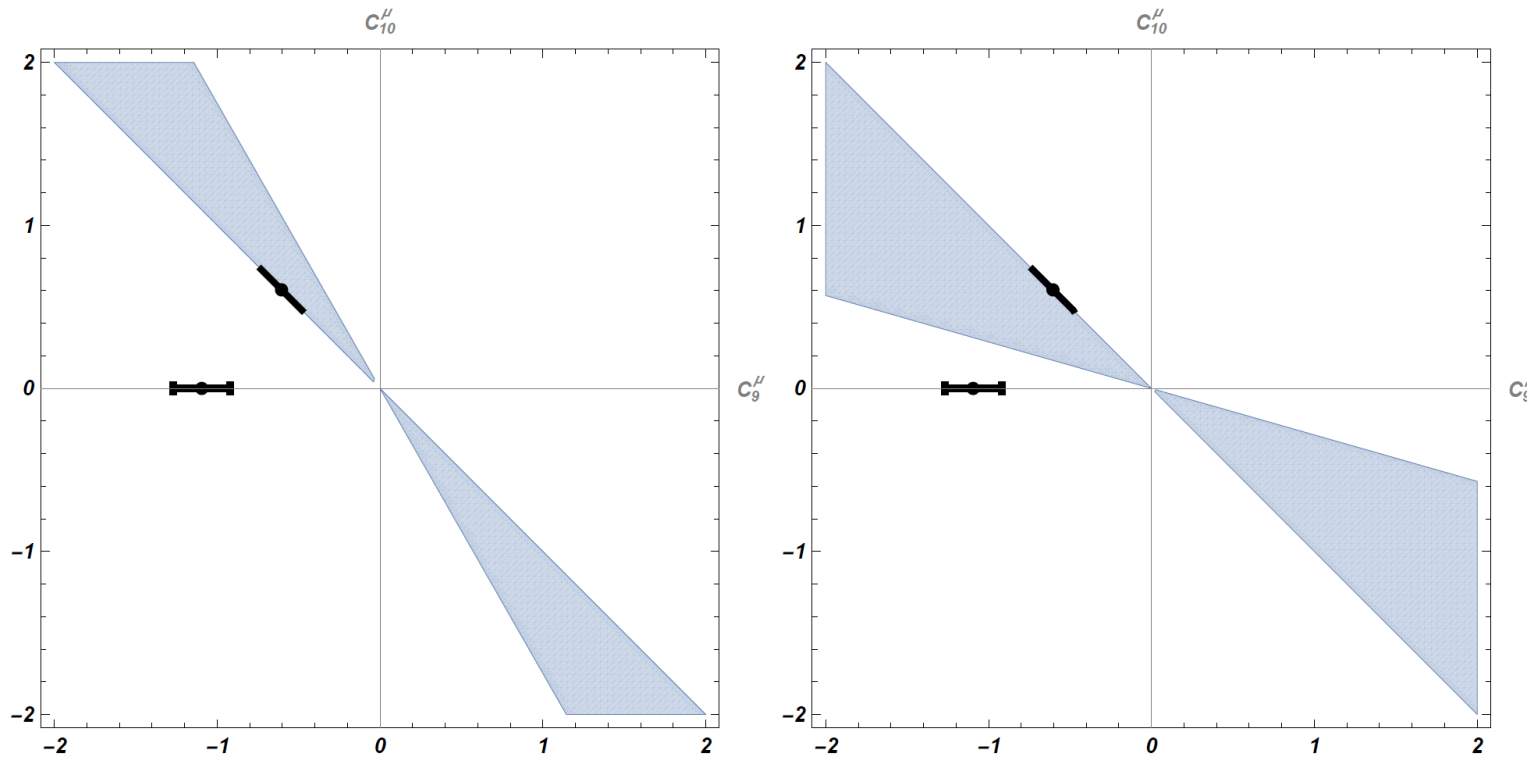
$$f^Z = -\frac{1}{2\sqrt{2}G_F V_{tb} V_{ts}^*} \frac{4\pi}{\alpha} \frac{\cos^2 \theta_W (3 + \tan^2 \theta_W)}{24} \frac{g^2}{M_Z^2} \sum_{\lambda} \hat{V}_{\lambda k}^{(d)*} \hat{V}_{\lambda l}^{(d)}$$

$$\lambda_{ij}^{(L)} = V_{1i}^{(e)*} V_{1j}^{(e)} \quad \lambda_{ij}^{(R)} = W_{3i}^{(e)*} W_{3j}^{(e)}$$

Both LFNU and LFV could
be induced by Z' (only)

- LFV excluded
- No BSM $C_{9,10}^e$

Data and global fits driven constraints (See yesterday talks)



- NP in $C_9^{\mu} = -C_{10}^{\mu}$ with the 1σ interval $[-1.18, -0.84]$
- NP in $C_9^{\mu} = -C_{10}^{\mu}$ with the 1σ interval $[-1.27, -0.92]$
- NP in $C_9^{\mu} = -C_{10}^{\mu}$, within the 1σ interval $[-0.73, -0.48]$.

Global fits

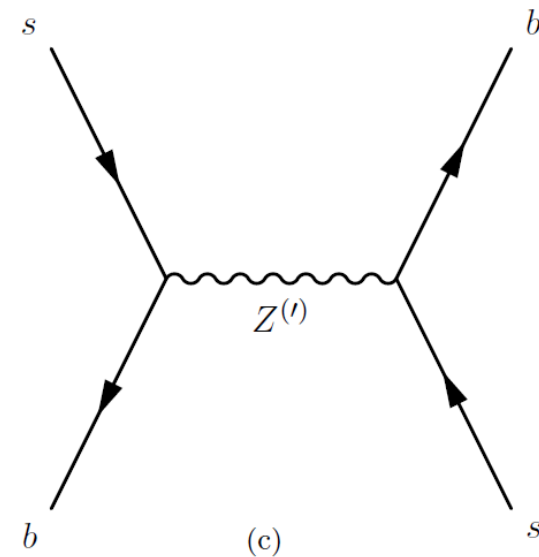
Descotes-Genon et al., 15,
 Capdevila et al. 17,
 Altmannshofer et al., Genget al.
 17, Ciuchini et al. 17, Hurth et
 al. 17....

Constraints from $B_s - \overline{B}_s$ mixing

BSM Z contribution: ε suppressed

BSM Z' contribution

$$\begin{aligned}\mathcal{H}_{\text{eff}} &\supset \frac{g_X^2}{54M_{Z'}^2 \cos^2 \theta_{331}} (V_{3k}^{*(d)} V_{3l}^{(d)})^2 (\overline{D}_k \gamma^\mu D_l) (\overline{D}_k \gamma^\mu D_l) = \\ &= \frac{8G_F}{\sqrt{2}(3 - \tan^2 \theta_W)} \frac{M_W^2}{M_{Z'}^2} (V_{3k}^{*(d)} V_{3l}^{(d)})^2 (\overline{D}_k \gamma^\mu D_l) (\overline{D}_k \gamma^\mu D_l)\end{aligned}$$



SM Z contribution

$$\mathcal{H}_{\text{eff}}^{\text{SM}} = (V_{ts}^* V_{tb})^2 \frac{G_F^2}{4\pi^2} M_W^2 \hat{\eta}_B S\left(\frac{\overline{m}_t^2}{M_W^2}\right) (\overline{s}_L \gamma^\mu b_L) (\overline{s}_L \gamma^\mu b_L)$$

$S\left(\frac{\overline{m}_t^2}{M_W^2}\right) \simeq 2.35$, for a top mass of about 165 GeV, and
 $\hat{\eta}_B = 0.8393 \pm 0.0034$, which comprises "QCD corrections.

$$r_{B_s} = \left| \frac{C_{\text{NP}}}{C_{\text{SM}}} \right| = \frac{32\pi^2 |V_{32}^{*(d)} V_{33}^{(d)}|^2}{\sqrt{2}(3 - \tan^2 \theta_W) |V_{ts}^* V_{tb}|^2 G_F M_W^2 \hat{\eta}_B S} \frac{M_W^2}{M_{Z'}^2}$$

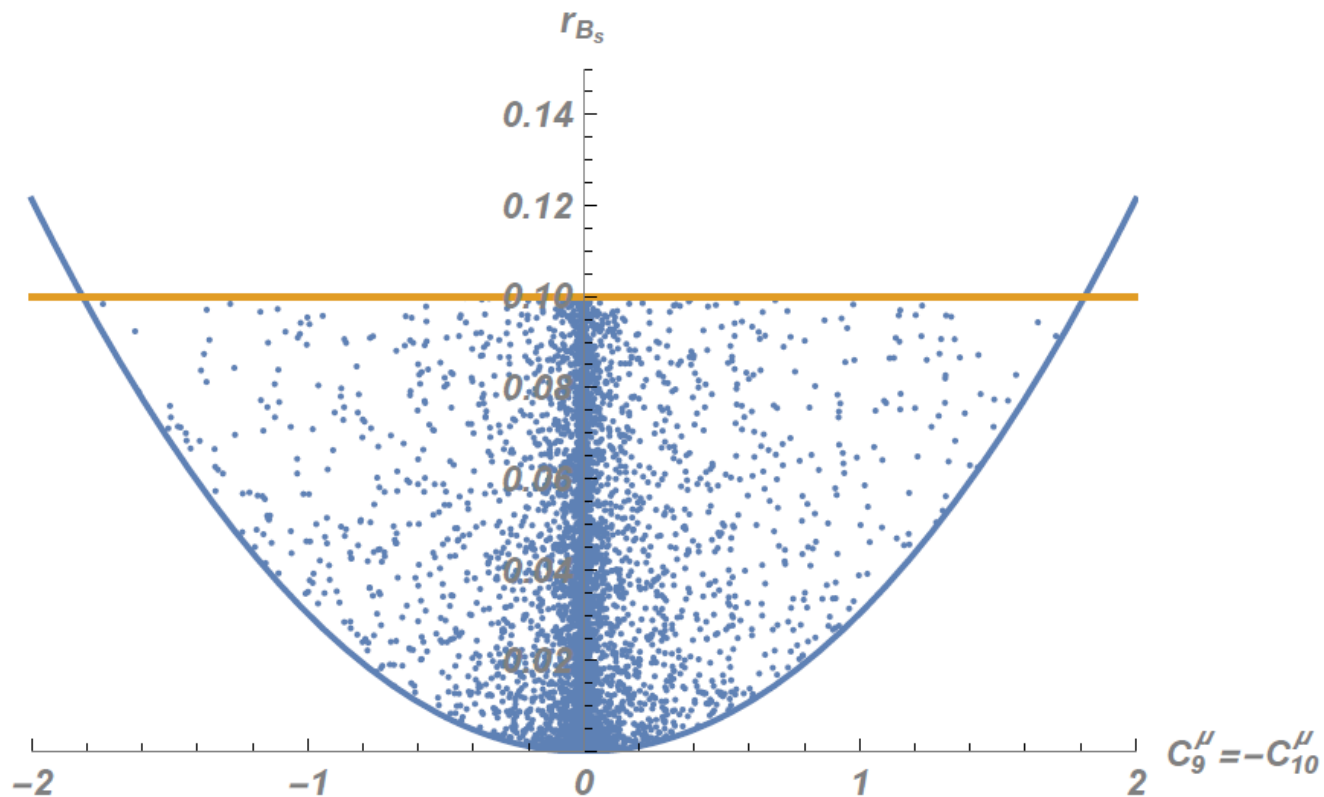


Figure 3: Allowed points in the (C_9^μ, r_{B_s}) plane.

$$d = V_{32}^{*(d)} V_{33}^{(d)}$$

$$d \in [-1,1]$$

$$\frac{M_W}{M_{Z'}} \in [0,0.3]$$

$$r_{B_s} \leq 0.1$$

Agreement global fits
 Lenz et al 1203.0238,
 J. Charles et al. 1309.2293.

Conclusions

- Preliminary analysis of LFNU of a Z' model embedded in a more global extension, the 331 model
- next-to-minimal assumptions: 5 lepton families + no LFV + no BSM in C^e
- NP scenarios in agreement with global fits are allowed