

.

Closing talk: Flavor anomalies, model independent and new physics considerations

From flavor to new physics.

Lyon, France

Amarjit Soni, BNL-HET

04/20/2018



Clarification

- **Closing talkNOT A SUMMARY**
- **CLOSING TALK ~ LAST TALK of this very nice meeting in a really nice flavory town on flavor physics**
- **Of course, in the past several years, I have been giving considerable attention to these anomalies.....So will make some observations based on presentations here and elsewhere and come up with important take home messages from my perspective**
- **Bound to be subjective.....Sorry**

Outline

- several looming deviations from SM ...i.e. “anomalies”
- For each case:
- briefly mention reservations for expt & for theory/comments
- Model independent collider implications *→ In ATLAS, CMS; also in IF*
- Assuming NP is a source: array of BSMs
- An illustration, of one minimal, well motivated setup for a BSM origin
- Summary, Outlook & emphasize 4 taking home

SET OF KEY ANOMALIES

Anomalies galore!

- $RD(*) \sim 46(?)$
- $RK(*) : 2.66(R_K) ;$

- $g-2 \dots BNL'06 \Rightarrow FNAL \text{ expt. } \sim 3.66$ *main lattice progress by RBC-UKQCD & others*

- ϵ' : a personal obsession....for a long^{^3} time \Rightarrow 'cause of the strong conviction that it is super-sensitive to NP

EVER LOOMING

216[PRL 2015] $\Rightarrow \sim 1200$ ~~now~~ $\Rightarrow \sim 1400$

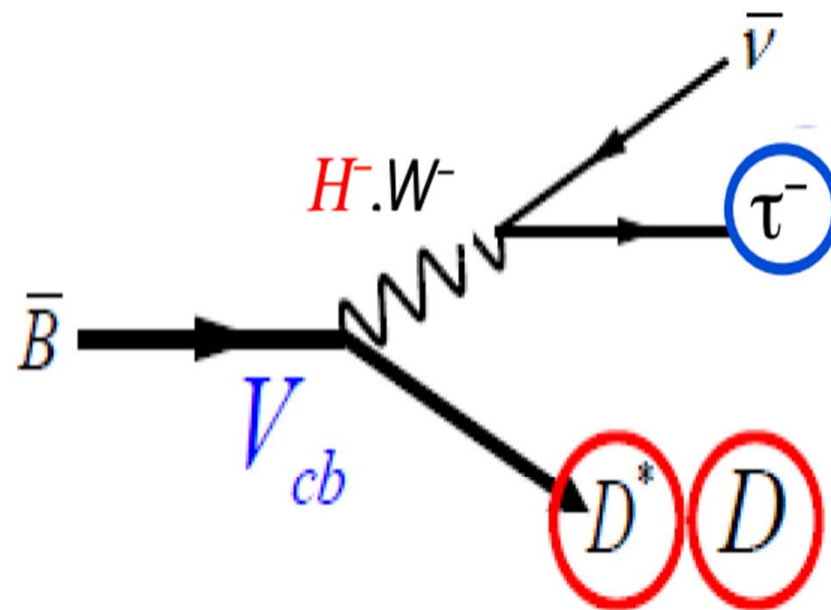
[2.1σ (2.9σ Buras; Nierste) $\Rightarrow ??$]few more months to new

In seeking BSM scenarios it is important to keep all these [INCLUDING ϵ'] + Higgs radiative stability in mind

RD(*)



Exclusive $B \rightarrow D^{(*)}\tau\nu$



RA LUTH (BABAR)

'CP May 2012
(HEFEL, China)

MANUEL FRANCO
SEVILLA
PhD Thesis

Independent of
 V_{cb} !

- To test the SM Prediction, we measure

$$R(D) = \frac{\Gamma(\bar{B} \rightarrow D\tau\nu)}{\Gamma(\bar{B} \rightarrow D\ell\nu)} \quad R(D^*) = \frac{\Gamma(\bar{B} \rightarrow D^*\tau\nu)}{\Gamma(\bar{B} \rightarrow D^*\ell\nu)}$$

Leptonic τ
decays only

Several experimental and theoretical uncertainties cancel in the ratio!

- DD^* events are fully reconstructed.

$l = \mu \text{ or } e$

Improving constraints on $\tan\beta/m_H$ using $B \rightarrow D \tau \bar{\nu}$

Ken Kiers* and Amarjit Soni†

Department of Physics, Brookhaven National Laboratory, Upton, New York 11973-5000

(Received 12 June 1997)

We study the q^2 dependence of the exclusive decay mode $B \rightarrow D \tau \bar{\nu}$ in type-II two Higgs doublet models (2HDM's) and show that this mode may be used to put stringent bounds on $\tan\beta/m_H$. There are currently rather large theoretical uncertainties in the q^2 distribution, but these may be significantly reduced by future measurements of the analogous distribution for $B \rightarrow D(e, \mu) \bar{\nu}$. We estimate that this reduction in the theoretical uncertainties would eventually (i.e., with sufficient data) allow one to push the upper bound on $\tan\beta/m_H$ down to about 0.06 GeV^{-1} . This would represent an improvement on the current bound by about a factor of 7. We

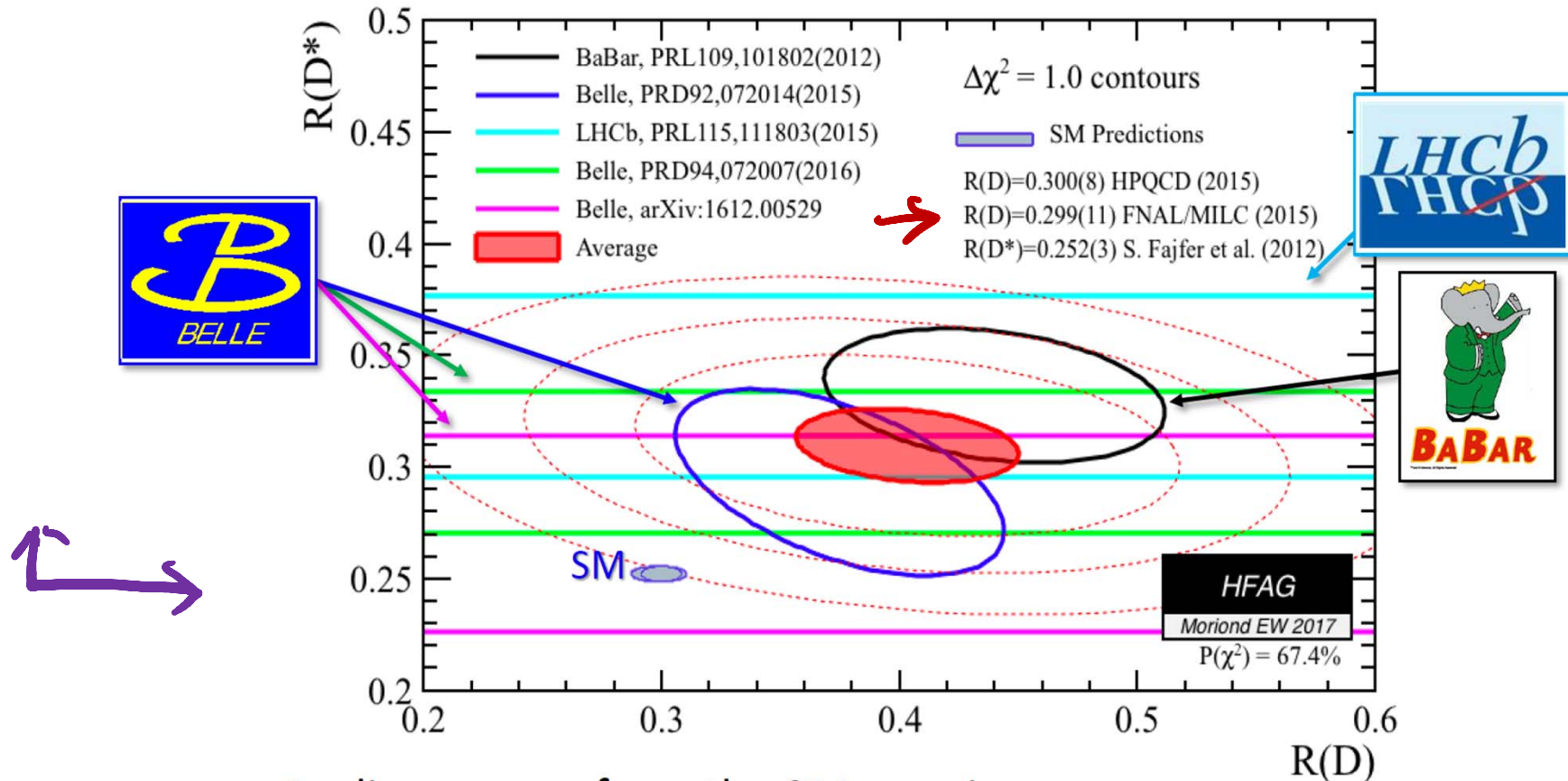
FF
F₁, F₀
↓
P
↓
used HQS

⇒ followed up by Nierste et al; Fajfer et al '12
/08

■ $R(D^{(*)})$ by HFAG

Hirose [BELLE]@EW
MORIOND Mar. 2017

11/15



- $\sim 4\sigma$ discrepancy from the SM remains
 - All the experiments show the larger $R(D^{(*)})$ than the SM
- More precise measurements at Belle II and LHCb are essential

Belle deviations quite mild

Lepton universality tests

- In the SM, ratios

Handwritten green notes:
 $\bar{b} \rightarrow \bar{u} \mu^+ \mu^-$
 $\bar{b} \rightarrow \bar{u} e^+ e^-$

$$R_K = \frac{\int d\Gamma[B^+ \rightarrow K^+ \mu^+ \mu^-]/dq^2 \cdot dq^2}{\int d\Gamma[B^+ \rightarrow K^+ e^+ e^-]/dq^2 \cdot dq^2}$$

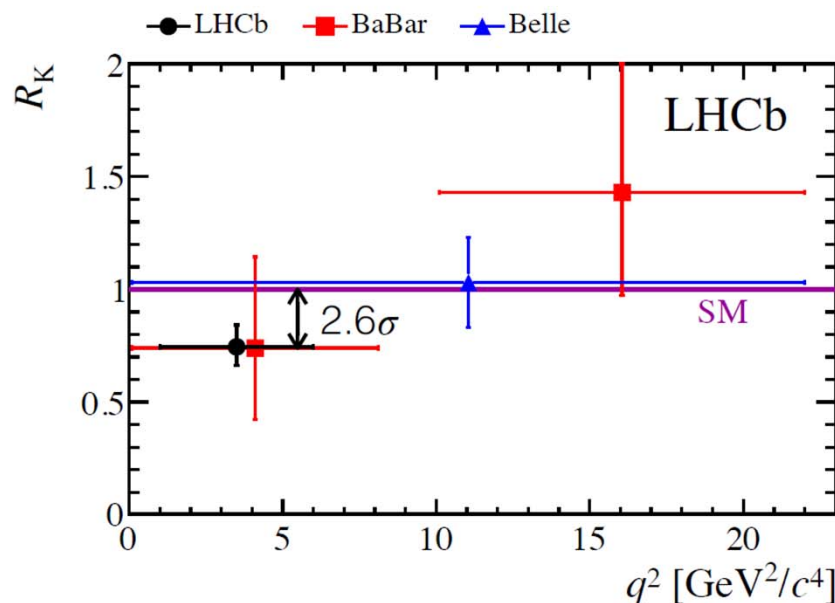
Handwritten red notes:
 LHCb introduced such & well defined ratios

only differ from unity by phase space — the dominant SM processes couple equally to the different lepton flavours.

- Theoretically clean since hadronic uncertainties cancel in the ratio.
- Experimentally challenging due to differences in muon/electron reconstruction (in particular Bremsstrahlung from the electrons).
 - ➔ Take double ratios with $B \rightarrow J/\psi X$ decays to cancel possible sources of systematic uncertainty.
 - ➔ Correct for migration of events in q^2 due to FSR/Bremsstrahlung using MC (with PHOTOS).

Lepton universality tests

- We have interesting hints of non-universal lepton couplings in LHCb run 1 dataset:



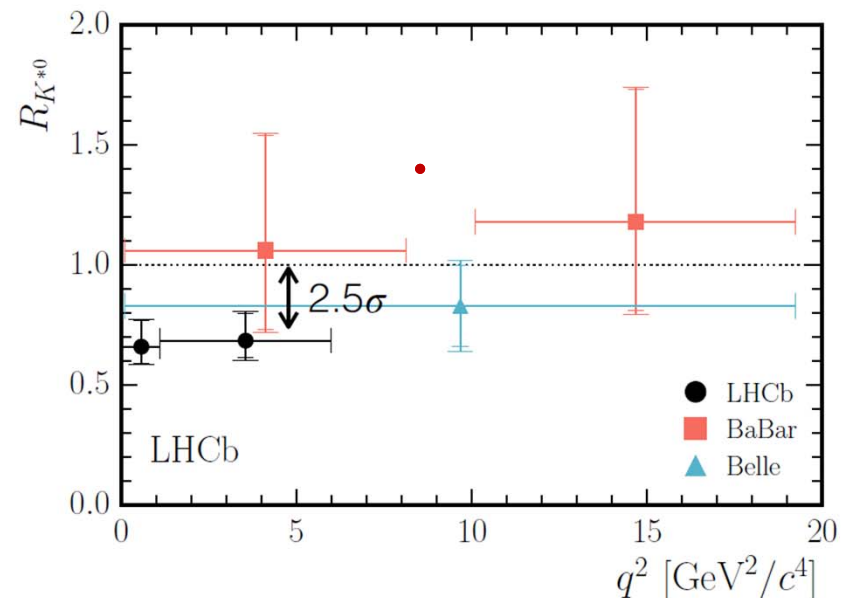
[LHCb, PRL113 (2014) 151601]

[LHCb, LHCb-PAPER-2017-013]

[BaBar, PRD 86 (2012) 032012]

[Belle, PRL 103 (2009) 171801]

Radiative Correction See Tsion et al



NB $R_K \approx 0.8$ is a prediction of one class of model explaining the $B^0 \rightarrow K^{*0} \mu^+ \mu^-$ angular observables, see $L_\mu - L_\tau$ models
W. Altmannshofer et al. [PRD 89 (2014) 095033]

RECENT UPDATES FROM EXPERIMENT AND FROM THEORY

R(D*) Status

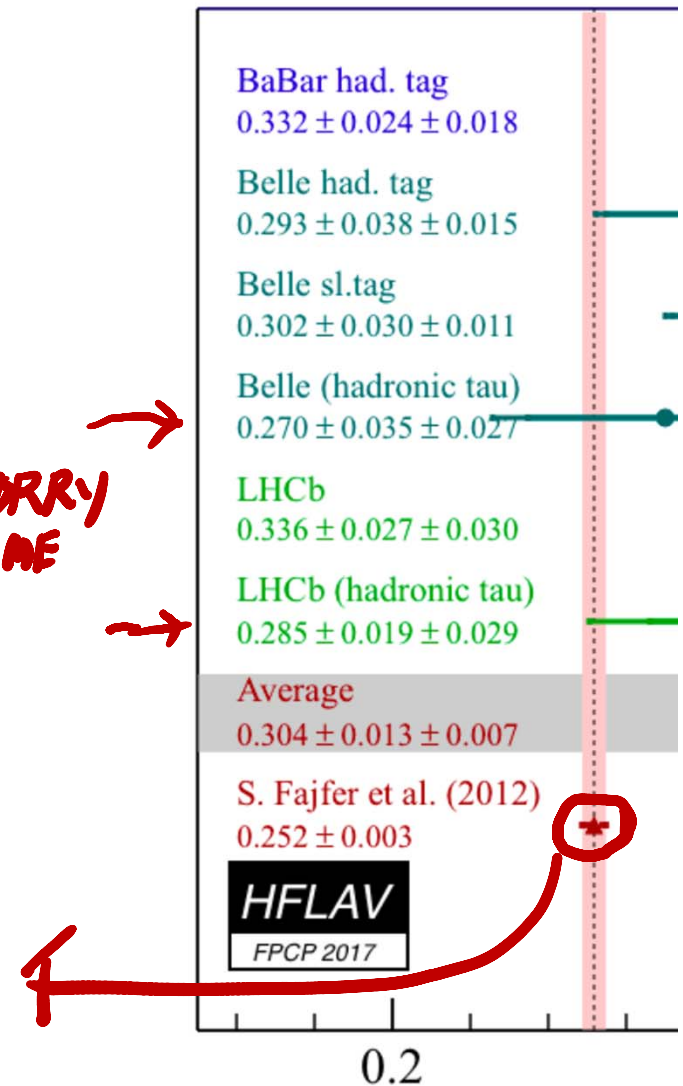
LHCb results have been incorporated on world average compilation.

Currently R(D*) shows a tension of 3.4σ with respect to SM prediction.

BR_{D}: 4 with 225; 2 with 12*

MISLEADING

**WORRY
SOME**

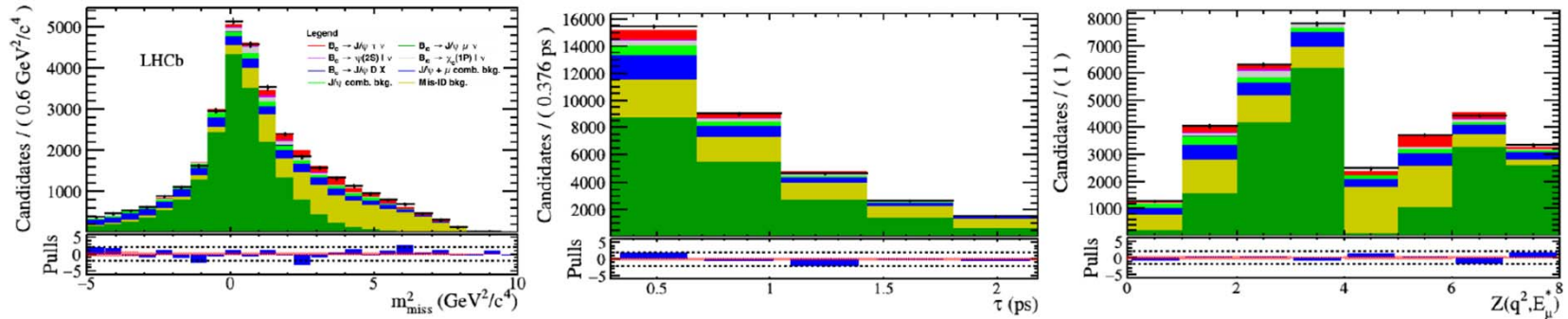


$$B_c \rightarrow J/\psi \tau \nu$$

2 PM Jan 2018

Greg Ciezarek,
on behalf of the LHCb collaboration

$$B_c \rightarrow \frac{b \rightarrow W \tau \nu}{\tau} J/\psi$$

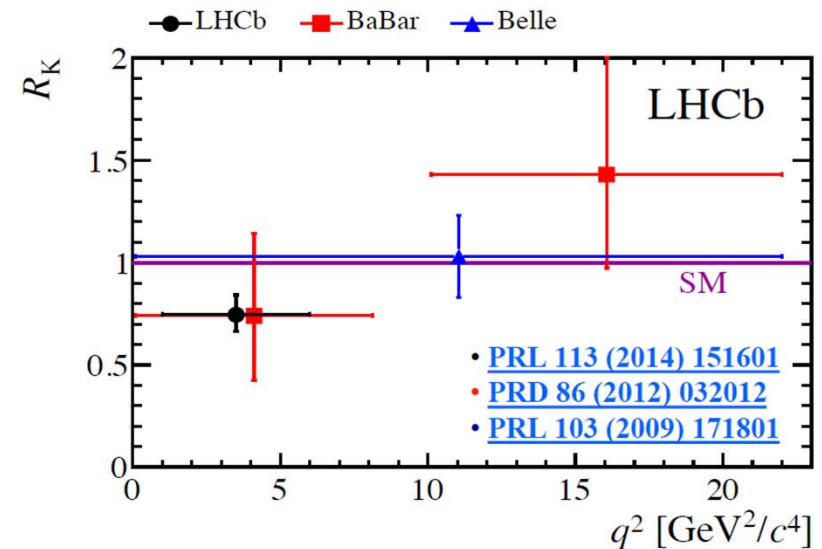
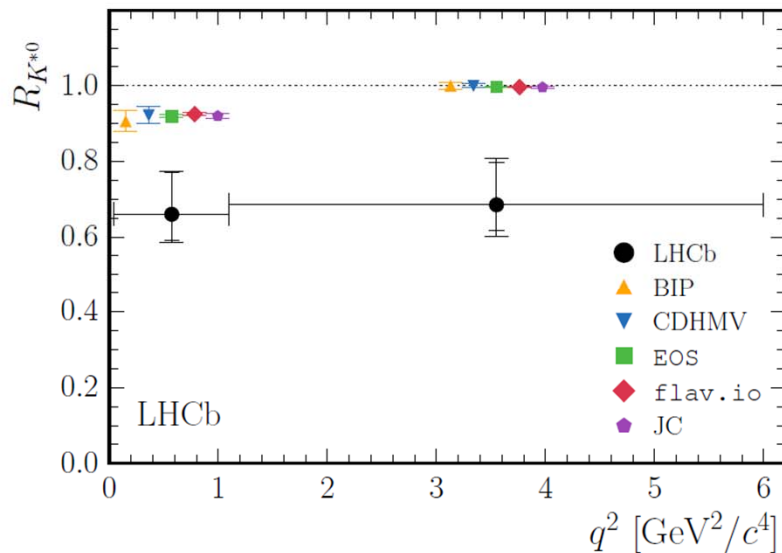
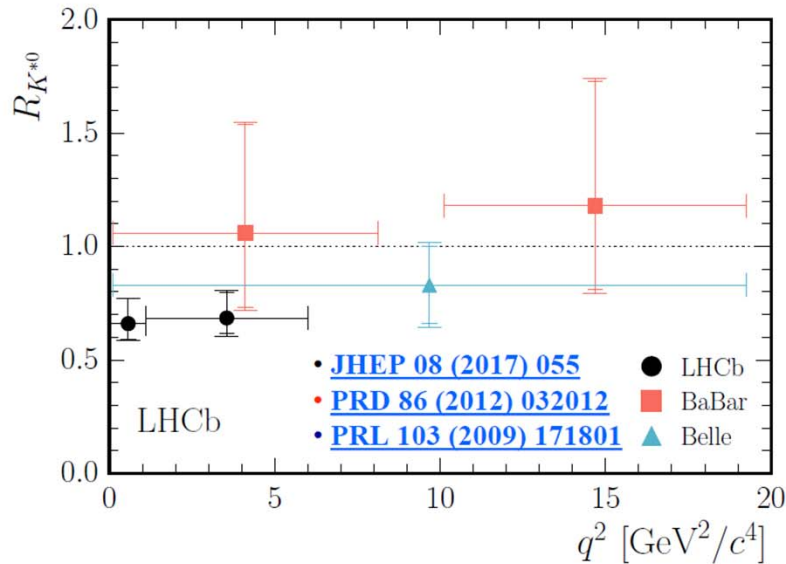


- $R_{J/\psi} \equiv B_c \rightarrow J/\psi \tau \nu / B_c \rightarrow J/\psi \mu \nu$
- Measured using very similar techniques to $\mathcal{R}(D^*)$, on run 1 data
- $R_{J/\psi} = 0.71 \pm 0.17 \pm 0.18$
 - $\sim 2\sigma$ from SM
 - But nearly as far from consistency with $\mathcal{R}(D^*)$
- LHCb-PAPER-2017-035 (Run 1 data)

Theory here
is trivial
 $\sim NR$ Bound State

Lepton Universality results

R_{K^} shows similar results as R_K !*



R_K : Central- q^2 : 2.6σ from SM

R_{K^*} : Low- q^2 : 2.1 - 2.3σ from SM

R_{K^*} : Central- q^2 : 2.4 - 2.5σ from SM

Rusa Mandul, PhD Thesis [IMSc Chennai]

- Another hint of deviation (at a level of more than 3σ), for a particular neutral-current decay mode is evinced by $B_s \rightarrow \phi\mu\mu$ [8, 62, 63].

LHCb

$$\Phi \equiv \frac{d}{dq^2} \text{BR}(B_s \rightarrow \phi\mu\mu) \Big|_{q^2 \in [1:6] \text{ GeV}^2} = \begin{cases} (2.58_{-0.31}^{+0.33} \pm 0.08 \pm 0.19) \times 10^{-8} \text{ GeV}^{-2} & (\text{exp.}) \\ (4.81 \pm 0.56) \times 10^{-8} \text{ GeV}^{-2} & (\text{SM}). \end{cases} \quad (6.2.3)$$

where $q^2 = m_{\mu\mu}^2$. Intriguingly, the q^2 region where this measurement has relatively low error (and data is quoted) is virtually the same as that for R_K and $R_{K^*}^{\text{central}}$. This

M. Patel et al: LHCb may be able to give R_ϕ .
That would be great

Concerns on SM-theory

- Good news is that lattice[FERMIL-MILC] study largely confirms pheno calculations for R_D [our RBC-UKQCD, Witzel et al needs bit more time]
- For $B \Rightarrow D^*$ **no complete lattice study so far**; 4 rather than 2 FF, so , from the lattice perspective, anticipate appreciably larger errors than for $B \Rightarrow D$
- Therefore, $O(1\%)$ errors in RD^* (and in fact smaller than in RD) are difficult to understand; lattice results should come in some months
- HFLAG should update the SM-theory with more realistic errors otherwise their fig is bit misleading
- Meantime recent phenomenological study of Bernlochner, Ligeti, Papucci and Robinson, 1703.05330 [and even more recently...is/are very timely and greatly appreciated.]
- For now, for RD^* , keeping these recent calculations and other reservations in mind best (conservative) guess is $RD^* \sim 0.258 \pm 0.020$ [based on FERMIL-MILC error for RD]

$\sim 4\%$

guess 8%.

2016, Casalino, Schacht ^{3%} & EPS

REMARKABLY: FOR R_D^* CENTRAL VALUE OF
BEST THEORY ESTIMATE APPEARS BIT
HIGHER THAN ALL ~ 6 MEASUREMENTS!

+2 $f_{\pi} R_D$

Flavor anomalies; Lyon; A Soni(BNL-HET)

Comments on Theory

- For RD and RD^* , non-lattice pheno efforts are on good, theo. grounds based on HQS....unlikely to be off by much
- Need however precise lattice results esp for $B \Rightarrow D^*$...see next p.
- For FCNC $B \Rightarrow K(^*)$ II, LUV tests **theory is essentially irrelevant**
- FCNC, $B \Rightarrow K(^*)$ II, **absolute measured rates vs SM, theory is not reliable** because of serious LD, non-perturbative contaminations

RBC-UKQCD [WITZEL, JUTTNER, TSANG, FLYNN, LEHNER, IZUBUCHI + AS] work in progress

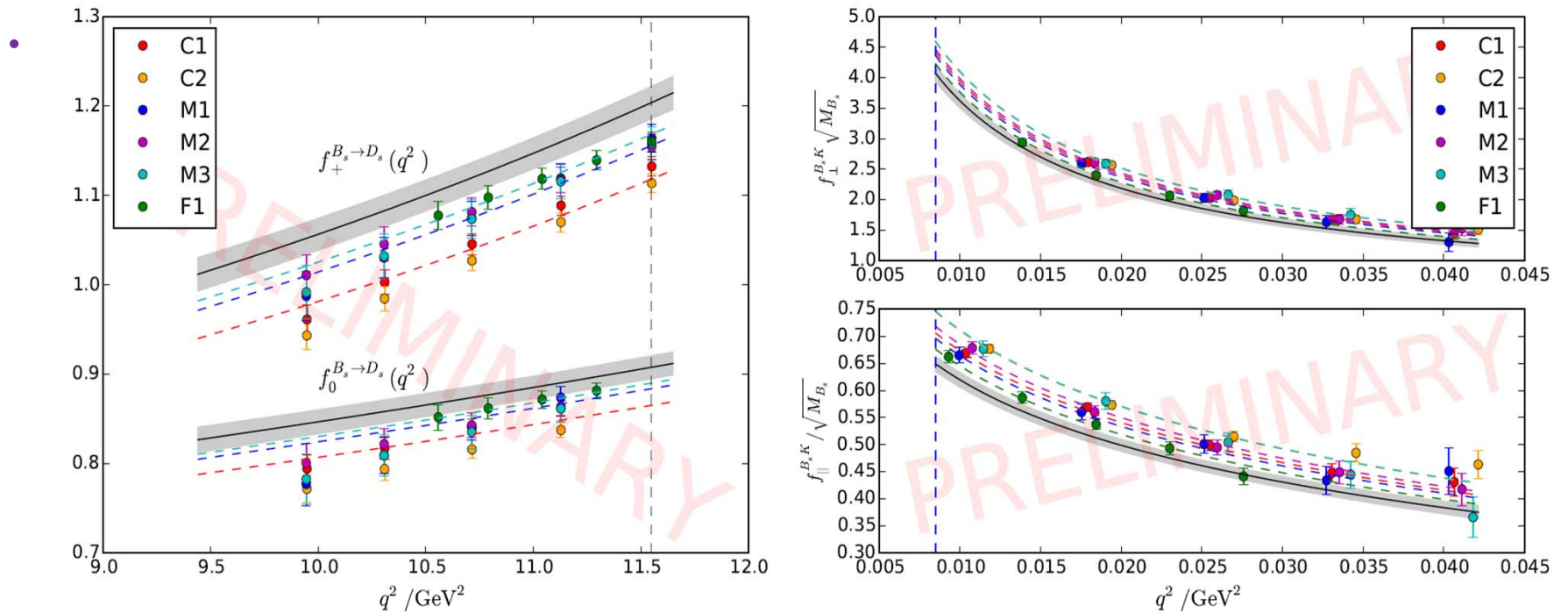


Figure 4. Chiral-continuum extrapolation for semi-leptonic form factors for $B_s \rightarrow D_s \ell \nu$ (left) and $B_s \rightarrow K \ell \nu$ (right). Performing a simple pole-ansatz for $B_s \rightarrow D_s$ we directly fit the phenomenological form factors f_+ and f_0 . For $B_s \rightarrow K$ we use heavy meson chiral perturbation theory and show the fit to the “lattice” form factors $f_{||}$ and f_{\perp} . The colored data points show results for our lattice calculations obtained at three values of the lattice spacing, whereas the black lines with the gray error band shows the chiral-continuum extrapolation. Only the statistical uncertainties are shown and no kinematical constraints are imposed.

~ 6 months

Comments/Reservations pros & cons on Expts p1 of 2

- For $RD(^*)$, $B \Rightarrow D(^*) \tau \nu$; most experimental results are with $\tau \Rightarrow \mu \nu \nu$ i.e 2 ν 'sso D^{**} potential contamination is a serious problem, in my view, as I have been stressing for past few years
- With that perspective in mind, **it is worrystome that 2 new results, one from Belle and the other from LHCb with $\tau \Rightarrow \text{hadrons} + \nu$ [i.e. 1 ν] is basically in agreement with SM though central value is mildly higher [i.e. roughly within $\sim 1-\sigma$]**

Comments/Reservations pros & cons on Expts p2 of 2

- **HFLAV**: Its high time they update their SM theory blob. It is true that combining theoretical predictions is bit difficult but **it is not good that they continue showing only predictions based on 2012 when recent ones with larger errors exist**. This can be esp. **misleading** since using these recent calculations [not my work] will for sure **reduce the tension with the SM**.

See, as an illustration how ADS' handles this a bit later.

Reg. $RK(^*)$ μ/e UV

- Needless to say its of profound importance, if true
- If true not just $B \Rightarrow K$, $B \Rightarrow K^*$ but also $B_s \Rightarrow \phi$, B-baryon decays should show it
- **Current statistics is marginal; more final states are needed and even more important other experiments esp. BELLE (II) confirmation is essential**
- This can take years as Br are $O(10^{-6})$ so not easy even for Belle-II;
- **however, Belle-II will be able to do RXs...inclusive and that will likely have more sensitivity for them; See P Urquijo @ LIO**
- **OTOH, LHCb will have B_s and B-baryons; See M. Patel @ LIO**

SURVEY OF BSMS

Array of BSM approaches to address flavor anomalies

- **Model ind eff L:** Greljo; Camalich; Mandal;
LQ: Fajfer; Luzio; Neubert; Silva; Becirevic;
- **[Partial]Composite/warped:** Stangl; Ahmady; Barbieri;
Panico; Blanke ...**Natural set up for flavor Non-Universality**
- **SUSY-like:** Hiller; ADS'=> RPV3 **Natural flavor Non-Universality**
- **More BSMs:** Guadagnoli; Grinstein; Jung; Ricciardi; Fuentes-Martin; Neshatpour; Crivelin
- **New approaches:** Valli; Camalich;
- **Status + Outlook:** Matias....**Nice update ...some diff of opinion**

EXPT: Status + (near) future outlook

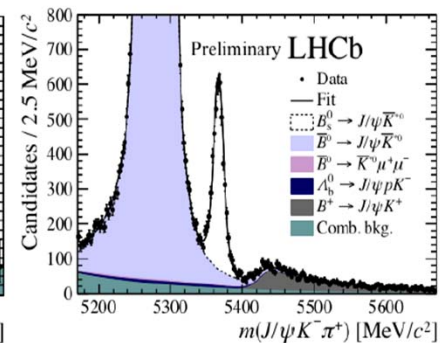
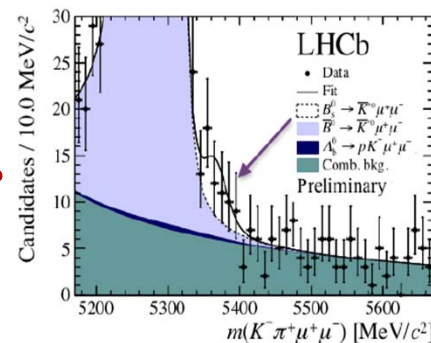
- Martinez; Lima; Bertolini @LHCb
- Urquijo; Goi; @ Belle-II
- Patel @ LHCb-UG

$$B_s^0 \rightarrow \bar{K}^{*0} \mu^+ \mu^- \text{ [LHCb-PAPER-2018-004]}$$

Run1 + part Run2 (2015 and 2016) data (4.6 fb^{-1})

$N(B_s^0 \rightarrow \bar{K}^{*0} \mu^+ \mu^-) = 38 \pm 12$, 3.4σ above bkg-only hypothesis
(first evidence)

$\mathcal{B}(B_s^0 \rightarrow \bar{K}^{*0} \mu^+ \mu^-) = [2.9 \pm 1.0(\text{stat}) \pm 0.2(\text{syst}) \pm 0.3(\text{norm})] \times 10^{-8}$
(first measurement) !!

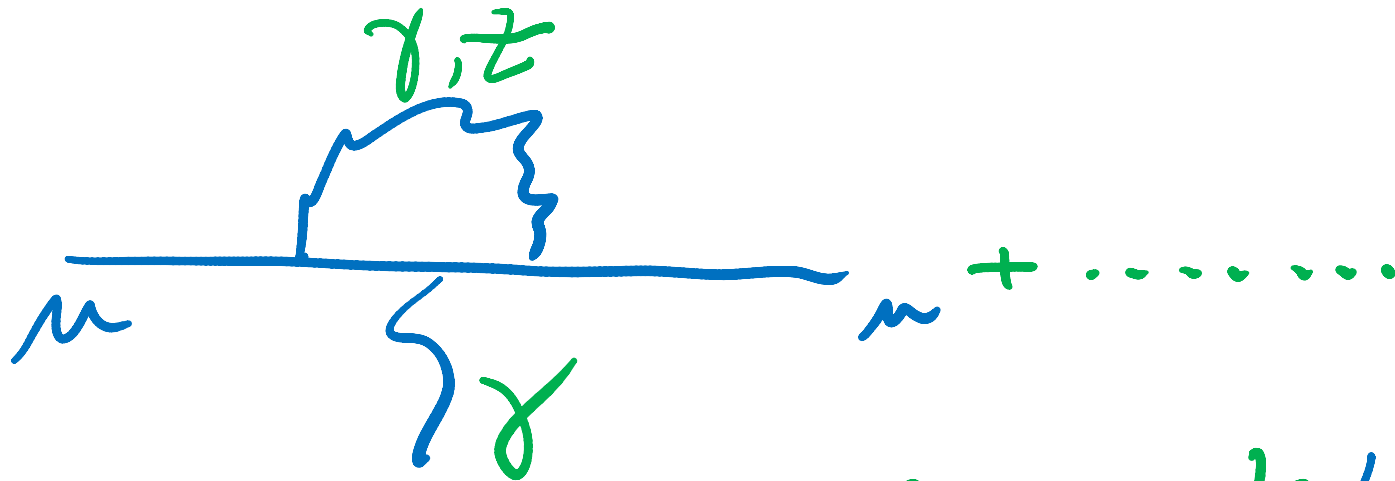


CONGRATS
LHCb
FANTASTIC!!
XTREMELY IMPT TO
Go for LHCb upgrades...

Menu...more

- **SM/CKM....Hurth; Rusov**
- **Model independent tests@collider: Isidori; Kamenik; Hou; Nardecchia; ADS';**
- **Model Independent @ IF: Mandal; Fajfer; Neubert;**
- **Kaons [SM/NP]: Buras; D'Ambrosio; Pich**

NOW FEW WORDS ON MUON G-2



BNL expt b_6
 ~ 3.56 deviation

POSSIBLE CONNECTION OF G-2 TO OTHER FLAVOR ANOMALIES

**MUON MAY NOT BE JUST A HEAVY
ELECTRON: KILE, KOBACH AND AS**

PRD 2015

Table 1

Constraints on lepton-flavor violating and conserving processes. For the last four observables, the experimental null results are given in terms of a dimension-6 operator, suppressed by two orders of Λ , which can be interpreted as the nominal scale of new physics.

Observable	Limit
$\text{Br}(\mu \rightarrow 3e)$	$< 1.0 \times 10^{-12}$ [1]
$\text{Br}(\mu \rightarrow e\gamma)$	$< 5.7 \times 10^{-13}$ [1]
$\text{Br}(\tau \rightarrow 3e)$	$< 2.7 \times 10^{-8}$ [1]
$\text{Br}(\tau \rightarrow e^- \mu^+ \mu^-)$	$< 2.7 \times 10^{-8}$ [1]
$\text{Br}(\tau \rightarrow e^+ \mu^- \mu^-)$	$< 1.7 \times 10^{-8}$ [1]
$\text{Br}(\tau \rightarrow \mu^- e^+ e^-)$	$< 1.8 \times 10^{-8}$ [1]
$\text{Br}(\tau \rightarrow \mu^+ e^- e^-)$	$< 1.5 \times 10^{-8}$ [1]
$\text{Br}(\tau \rightarrow 3\mu)$	$< 2.1 \times 10^{-8}$ [1]
$\text{Br}(\tau \rightarrow \mu\gamma)$	$< 4.4 \times 10^{-8}$ [1]
$\text{Br}(\tau \rightarrow e\gamma)$	$< 3.3 \times 10^{-8}$ [1]
μ - e conversion	$\Lambda \gtrsim 10^3 \text{ TeV}$ [5]
$e^+e^- \rightarrow e^+e^-$	$\Lambda \gtrsim 5 \text{ TeV}$ [3]
$e^+e^- \rightarrow \mu^+\mu^-$	$\Lambda \gtrsim 5 \text{ TeV}$ [3]
$e^+e^- \rightarrow \tau^+\tau^-$	$\Lambda \gtrsim 4 \text{ TeV}$ [3]

Ist gen not
sensitive to
NP
+
(g-2)_e

UV



C ALSO A. IYER & LYON

KILIC, KOBACH
+ AS

PRD 2015

SPONTANEOUS

Maybe 1st

gen. is

fundamental
& its protection
from NP

QUICK UPDATE ON G-2

$(g-2)_\mu$ on + off the Lattice

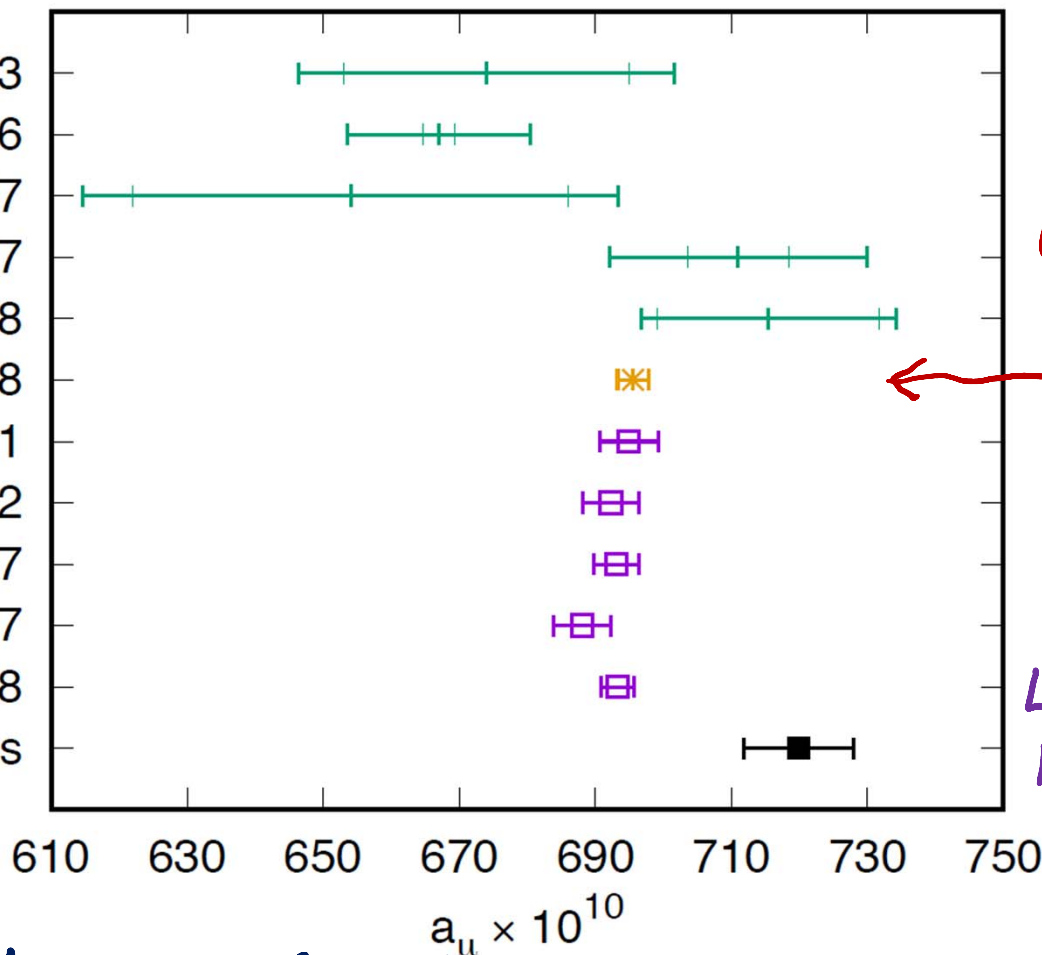
PURE
Lattice

ETMC 2013
HPQCD 2016
Mainz 2017
BMW 2017
RBC/UKQCD 2018
RBC/UKQCD 2018

Pheno

HLMNT 2011
DHMZ 2012
DHMZ 2017
Jegerlehner 2017
KNT 2018

No new physics



C Lehner
et al
RBC-
UKQCD
HYBRID

Lattice we
INITIATED
BY T. BLUM
~2004
while at BNL

SUMMARY: C. LEHNER (BNL)

We need to improve the precision of our pure lattice result so that it can distinguish the "no new physics" results from the cluster of precise R-ratio results.

Lunch Seminar 03/09/18

Personal take on g-2

- If you take pheno estimate of hadronic VP contributions via use of R-ratio method deviation for BNL-expt $\sim 3.6 \sigma$ so likely culprit is under-estimate error on theory of around $\frac{1}{2}\%$; though recently RBC-UKQCD lattice hybrid method finds support for this pheno estimate
- Need to wait on pure lattice result after another factor of 4-5 reduction in error, may take another 2-3 years
- By that time improved experimental results should also become available
- Final verdict may need another 2-3 years

Bottom line

- NP or not depends critically not just on precise experiment but also reliable SM prediction from the lattice become mandatory
- Experiment + Lattice M.E. has the last word....[of course should be stressed that the lattice calculations often require sophisticated and demanding and essential input from perturbation theory]
- Experimental results often attained at huge cost can be used effectively, iff commensurate theory predictions are available.....mantra for past several decades

A.S. in Proceedings of Lattice '85 (FSU)..1st Lattice meeting ever attended

The matrix elements of some penguin operators control in the standard model another CP violation parameter, namely ϵ'/ϵ .^{6,8)} Indeed efforts are now underway for an improved measurement of this important parameter.¹⁰⁾ In the absence of a reliable calculation for these parameters, the experimental measurements, often achieved at tremendous effort, cannot be used effectively for constraining the theory. It is therefore clearly important to see how far one can go with MC techniques in alleviating this old but very difficult

**With C. Bernard
[UCLA]**

Flavor anomalies; Lyon; A Soni(BNL-HET)

- **Already heard pheno perspective on $K \Rightarrow \pi\pi$ and ε' in nice talks from Buras and also from Pich**
- **So I skip exptal route for ε' and such**

LATTICE QUEST FOR EPSILON'

FROM THEORY

$K \rightarrow 2\pi$

$$\text{Re}\left(\frac{\epsilon'}{\epsilon}\right) = \frac{\omega}{\sqrt{2}|\epsilon|} \left[\frac{\text{Im}(A_2)}{\text{Re}(A_2)} - \frac{\text{Im}(A_0)}{\text{Re}(A_0)} \right];$$

$I = 2 \text{ amp}$

$I = 0 \text{ amp}$

$$\omega \approx \frac{\text{Re} A_2}{\text{Re} A_0}$$

$\frac{\text{Re} A_0}{\text{Re} A_2} \sim 25 \quad \Delta I = 1/2 \text{ Puzzle}$

INDIRECT CP
BNL '64
Cronin + Fitch
NP

$$|\epsilon| = 2.228(11) \times 10^{-3},$$

$\bar{s} \xrightarrow{k^+} u$ $\bar{s} \xrightarrow{k_s} d$

DIRECT CP

$$\text{Re}(\epsilon'/\epsilon) = 1.65(26) \times 10^{-3}.$$

$\epsilon' \sim \mathcal{O}(10^{-6})!$

CERN + FNAL ~ 2004

For simplicity: 1st strategy via ChPT

PHYSICAL REVIEW D

VOLUME 32, NUMBER 9

1 NOVEMBER 1985

Application of chiral perturbation theory to $K \rightarrow 2\pi$ decays

BDSPW '84

Claude Bernard, Terrence Draper,* and A. Soni

Department of Physics, University of California, Los Angeles, California 90024

H. David Politzer and Mark B. Wise

Department of Physics, California Institute of Technology, Pasadena, California 91125

(Received 3 December 1984)

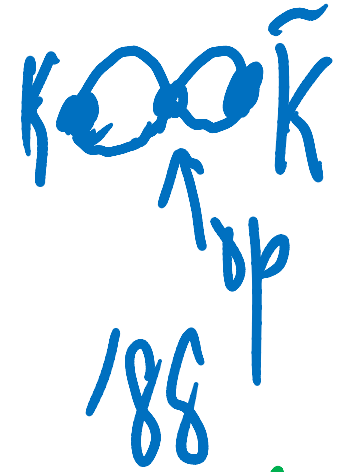
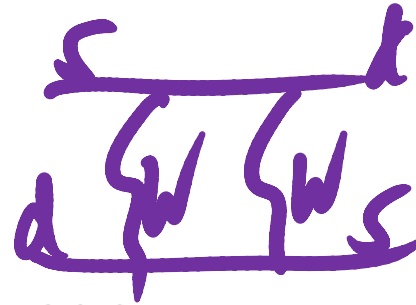
Chiral perturbation theory is applied to the decay $K \rightarrow 2\pi$. It is shown that, to quadratic order in meson masses, the amplitude for $K \rightarrow 2\pi$ can be written in terms of the unphysical amplitudes $K \rightarrow \pi$ and $K \rightarrow 0$, where 0 is the vacuum. One may then hope to calculate these two simpler amplitudes with lattice Monte Carlo techniques, and thereby gain understanding of the $\Delta I = \frac{1}{2}$ rule in K decay. The reason for the presence of the $K \rightarrow 0$ amplitude is explained: it serves to cancel off unwanted renormalization contributions to $K \rightarrow \pi$. We make a rough test of the practicability of these ideas in Monte Carlo studies. We also describe a method for evaluating meson decay constants which does not require a determination of the quark masses.

used extensively on lattice for 20 years \Rightarrow NLD

J. LAIHO PD
THICK $\sim 1/3$

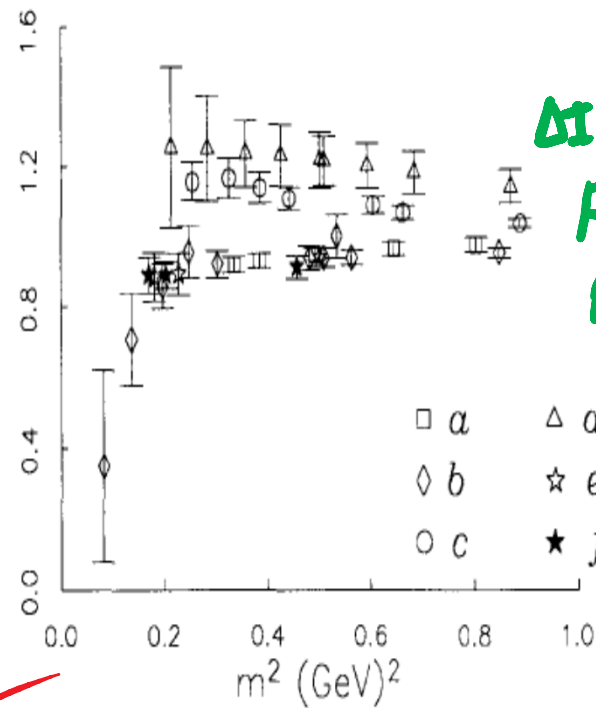
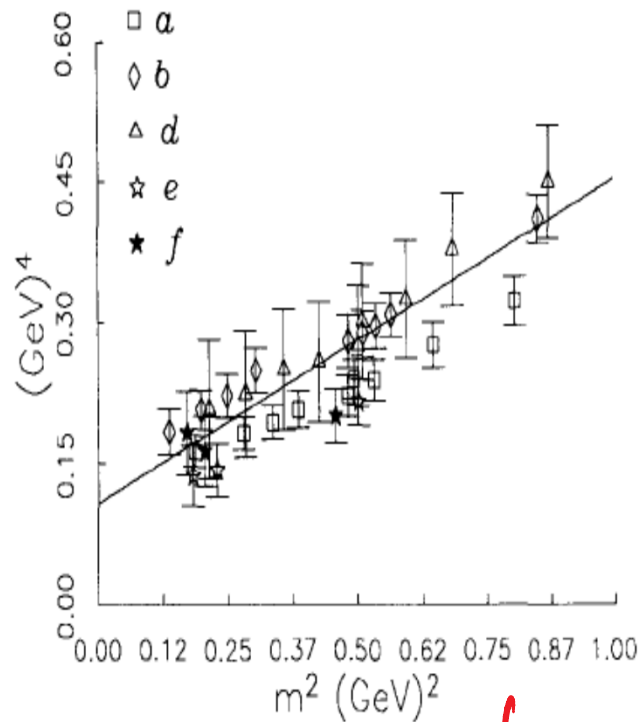
Flavor anomalies: Bernard, A. Soni (BNL-HET)

$$\langle K | (\bar{s} \gamma_\mu d)^2 | \bar{K} \rangle$$



162

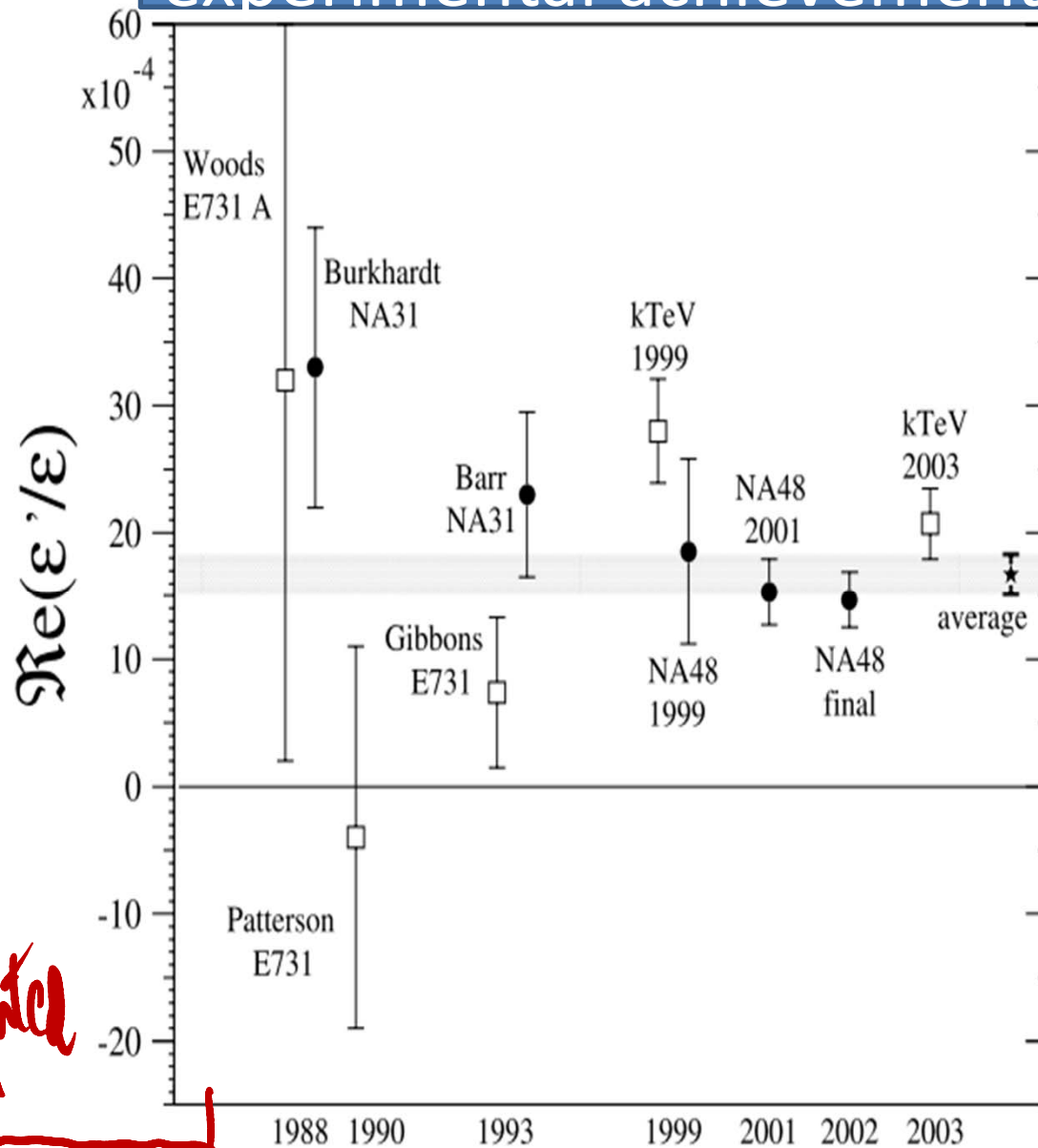
C. Bernard, A. Soni / Weak matrix elements on the lattice



$\Delta I = 0$ channel
 For more
 PATHOLOGICAL
 with Wilson
 Fermion
 'cause of
 power div

XS violation by $K - \bar{K} \Rightarrow$ FINE TUNING $\left[\frac{1}{a^n}\right]$
 PROBLEM

A monumental experimental achievement!



Komrad
kleinknecht
"Uncleing CPV"

$16.6(2.3) \times 10^{-4}$
PDG

CB+AS
LATTICE
WORK STARTED

Flavor anomalies; Lyon; A Soni(BNL-HET)

Inspired I.P. by papers of
Shamir [+Furman] +
discussions with Creutz

QCD with domain wall quarks

T. Blum* and A. Soni†

Department of Physics, Brookhaven National Laboratory, Upton, New York 11973

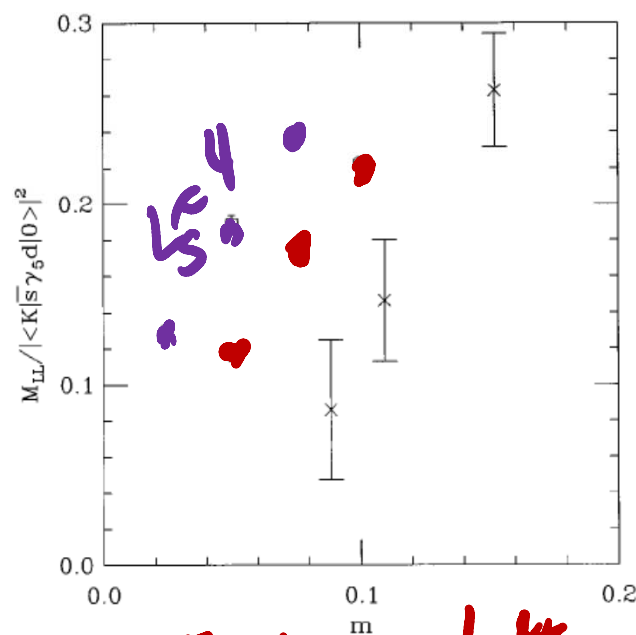
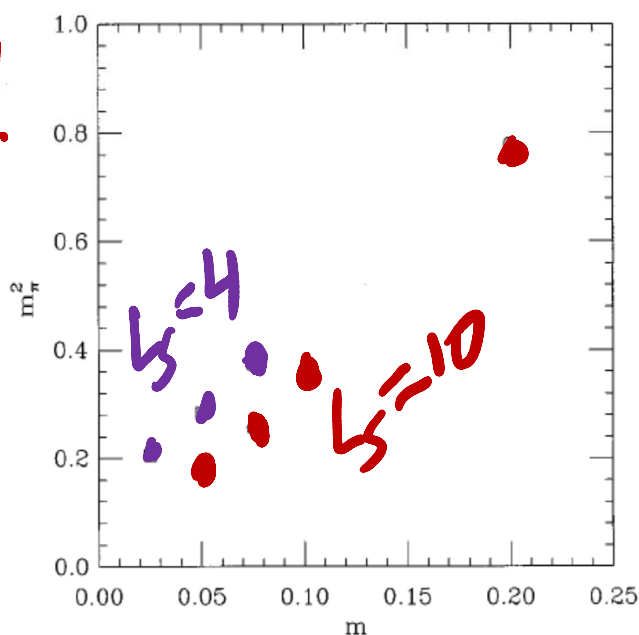
(Received 27 November 1996)

1st Simulation
with DWQ

→ '96-97

DWQ
preserve
CHIRAL SYM
even
at $a \neq 0$!!!
==

We present lattice calculations in QCD using Shamir's variant of Kaplan fermions which retain the continuum $SU(N)_L \times SU(N)_R$ chiral symmetry on the lattice in the limit of an infinite extra dimension. In particular, we show that the pion mass and the four quark matrix element related to $K_0-\bar{K}_0$ mixing have the expected behavior in the chiral limit, even on lattices with modest extent in the extra dimension, e.g., $N_5=10$. [S0556-2821(97)00113-6]



Excellent
Chiral
Symmetry
with $N_5=10$
Sites in
5th dim.

MAJOR BREAK THROUGH For $K \rightarrow \pi\pi$ Lattice Calculations

$K \rightarrow 2\pi$ ChPT

with DWQ in Quenched Approx

1st application
of BDSPW's 84

with DWQ

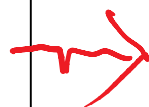
RBC:

Founding members

Christ, Mawhinney

Blum, AS

~ '98



RBC Collaboration

Kaon matrix elements and CP violation from quenched lattice QCD: The 3-flavor case

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We report the results of a calculation of the $K \rightarrow \pi\pi$ matrix elements relevant for the $\Delta I = 1/2$ rule and ϵ'/ϵ in quenched lattice QCD using domain wall fermions at a fixed lattice spacing $a^{-1} \sim 2$ GeV. Working in the three-quark effective theory, where only the u , d , and s quarks enter and which is known perturbatively to next-to-leading order, we calculate the lattice $K \rightarrow \pi$ and $K \rightarrow |0\rangle$ matrix elements of dimension six, four-fermion operators. Through lowest order chiral perturbation theory these yield $K \rightarrow \pi\pi$ matrix elements, which we then normalize to continuum values through a nonperturbative renormalization technique. For the ratio of isospin amplitudes $|A_0|/|A_2|$ we find a value of 25.3 ± 1.8 (statistical error only) compared to the experimental value of 22.2, with individual isospin amplitudes 10%–20% below the experimental values. For ϵ'/ϵ , using known central values for standard model parameters, we calculate $(-4.0 \pm 2.3) \times 10^{-4}$ (statistical error only) compared to the current experimental average of $(17.2 \pm 1.8) \times 10^{-4}$. Because we find a large cancellation between the $I=0$ and $I=2$ contributions to ϵ'/ϵ , the result may be very sensitive to the approximations employed. Among these are the use of quenched QCD, lowest order chiral perturbation theory, and continuum perturbation theory below 1.3 GeV. We also calculate the kaon B parameter B_K and find $B_{K,MS}(2 \text{ GeV}) = 0.532(11)$. Although currently unable to give a reliable systematic error, we have control over statistical errors and more simulations will yield information about the effects of the approximations on this first-principles determination of these important quantities.

$K \rightarrow 2\pi$ & ϵ'/ϵ

"Flagship Project"

Now ~ 20 yrs!

1st Large Scale Simulation

with DWQ

also CP-PACS PRO'03

QCDSP

~ '98 → ~ '05 1 TF

→ CMP / OI. ←
 a powerful new method
 ↑

Direct $K \rightarrow \pi\pi$ (a la Lellouch-Lüscher), using finite volume correlation* functions, [i.e. w/o ChPT] RBC initiates around 2005.

~ 2007

RBC-UKQCD (mostly)

Boyle, Sachrajda, Jexal
 I
 Edinburgh
 II
 Southampton

* Allows to bypass Maini-Testa theorem

COMMON Interest: use of DWA for simulations

$$\Delta S=1 \text{ } H_W$$

W L & NLO

Buchalla, Buras, Lautenbacher
RMP 196; Cinquini et al 95

$$H_W = \frac{G_F}{\sqrt{2}} V_{us}^* V_{ud} \sum_{i=1}^{10} [z_i(\mu) + \tau y_i(\mu)] Q_i(\mu).$$

Re A_0

For Im A_0

CORE of the calculation:

$$m_i = \langle k | Q_i | \pi \pi \rangle$$

from the Lattice
Needed

$$\tau = -V_{ts}^* V_{td} / V_{us}^* V_{ud}.$$

Tree

$$Q_1 = (\bar{s}_\alpha d_\alpha)_L (\bar{u}_\beta u_\beta)_L,$$

$$Q_2 = (\bar{s}_\alpha d_\beta)_L (\bar{u}_\beta u_\alpha)_L,$$

$$Q_3 = (\bar{s}_\alpha d_\alpha)_L \sum_{q=u,d,s} (\bar{q}_\beta q_\beta)_L,$$

$$Q_4 = (\bar{s}_\alpha d_\beta)_L \sum_{q=u,d,s} (\bar{q}_\beta q_\alpha)_L,$$

$$Q_5 = (\bar{s}_\alpha d_\alpha)_L \sum_{q=u,d,s} (\bar{q}_\beta q_\beta)_R,$$

$$Q_6 = (\bar{s}_\alpha d_\beta)_L \sum_{q=u,d,s} (\bar{q}_\beta q_\alpha)_R,$$

$$Q_7 = \frac{3}{2} (\bar{s}_\alpha d_\alpha)_L \sum_{q=u,d,s} e_q (\bar{q}_\beta q_\beta)_R,$$

$$Q_8 = \frac{3}{2} (\bar{s}_\alpha d_\beta)_L \sum_{q=u,d,s} e_q (\bar{q}_\beta q_\alpha)_R,$$

$$Q_9 = \frac{3}{2} (\bar{s}_\alpha d_\alpha)_L \sum_{q=u,d,s} e_q (\bar{q}_\beta q_\beta)_L,$$

$$Q_{10} = \frac{3}{2} (\bar{s}_\alpha d_\beta)_L \sum_{q=u,d,s} e_q (\bar{q}_\beta q_\alpha)_L,$$

EWP

~~I=2~~

QCD

$I=0$

$m_q \rightarrow 0$

$\rightarrow \text{const}$

$m \rightarrow 0$

$\frac{S \mu_d}{e_9}$
QCD

$\frac{S \mu_d}{e_9}$
 $\frac{S \mu_d}{e_9}$

EWP

Acknowledge many significant contributions off & on the lattice

- While focus is on lattice calculations of $K \Rightarrow \pi\pi$ primarily by our RBC-UKQCD Collab
- Over the years many important contributors, in particular:
- (Mary K)Gaillard, (Ben) Lee; Altarelli, Maiani; Shifman, Vainshtein, Zhakrov; Gilman + Wise; Buras & Co; Martinelli & Co; (Claude) Bernard; de Rafael; Pich, Bijnsens.....

DIRECT $K \rightarrow \pi\pi$
[No ChPT]

Results for ε'

Using $\text{Re}(A_0)$ and $\text{Re}(A_2)$ from experiment and our lattice values for $\text{Im}(A_0)$ and $\text{Im}(A_2)$ and the phase shifts,

and our lattice values for

EW P

QCDP

USING 216 independent measurements

RBC-UKQCD PRL'15
EDITOR'S CHOICE

$$\text{Re} \left(\frac{\varepsilon'}{\varepsilon} \right) = \text{Re} \left\{ \frac{i\omega e^{i(\delta_2 - \delta_0)}}{\sqrt{2}\varepsilon} \left[\frac{\text{Im}A_2}{\text{Re}A_2} - \frac{\text{Im}A_0}{\text{Re}A_0} \right] \right\}$$

LARGE CANCELLATION!!
(80-85%)

$$= \frac{1.38(5.15)(4.43) \times 10^{-4}}{16.6(2.3) \times 10^{-4}}, \quad \begin{array}{l} \text{(this work)} \\ \text{(experiment)} \end{array}$$

Full accounting
of all errors

Bearing in mind the largish errors in this first calculation, we interpret that our result are consistent with experiment at $\sim 2\sigma$ level

$$\omega = \frac{\text{Re}A_2}{\text{Re}A_0} \sim 0.045$$

Computed $\text{Re}A_2$ excellent agreement with expt
Computed $\text{Re}A_0$ good agreement with expt
Offered an "explanation" of the Delta $I=1/2$ Enhancement [c later]

12/03/2017

Scalars 2017; HET-BNL; soni

42

BuA AS et al use own LME \Rightarrow effect is ~ 2.95
Nienste. ~ 11

Flavor anomalies; Lyon; A Soni(BNL-HET)

50

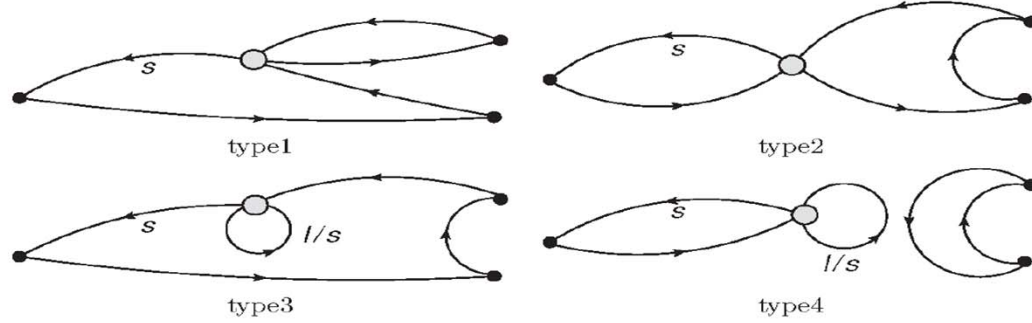


FIG. 1. Examples of the four types of diagram contributing to the $\Delta I = 1/2$, $K \rightarrow \pi\pi$ decay. Lines labeled ℓ or s represent light or strange quarks. Unlabeled lines are light quarks.

i	Re(A_0)(GeV)	Im(A_0)(GeV)
1	$1.02(0.20)(0.07) \times 10^{-7}$	0
2	$3.63(0.91)(0.28) \times 10^{-7}$	0
3	$-1.19(1.58)(1.12) \times 10^{-10}$	$1.54(2.04)(1.45) \times 10^{-12}$
4	$-1.86(0.63)(0.33) \times 10^{-9}$	$1.82(0.62)(0.32) \times 10^{-11}$
5	$-8.72(2.17)(1.80) \times 10^{-10}$	$1.57(0.39)(0.32) \times 10^{-12}$
6	$3.33(0.85)(0.22) \times 10^{-9}$	$-3.57(0.91)(0.24) \times 10^{-11}$
7	$2.40(0.41)(0.00) \times 10^{-11}$	$8.55(1.45)(0.00) \times 10^{-14}$
8	$-1.33(0.04)(0.00) \times 10^{-10}$	$-1.71(0.05)(0.00) \times 10^{-12}$
9	$-7.12(1.90)(0.46) \times 10^{-12}$	$-2.43(0.65)(0.16) \times 10^{-12}$
10	$7.57(2.72)(0.71) \times 10^{-12}$	$-4.74(1.70)(0.44) \times 10^{-13}$
Tot	$4.66(0.96)(0.27) \times 10^{-7}$	$-1.90(1.19)(0.32) \times 10^{-11}$

TABLE I. Contributions to A_0 from the ten continuum, $\overline{\text{MS}}$ operators $Q_i(\mu)$, for $\mu = 1.53$ GeV. Two statistical errors are shown: one from the lattice matrix element (left) and one from the lattice to $\overline{\text{MS}}$ conversion (right). See the Supplemental Material at [URL to be inserted] for tables of the separate matrix elements in the lattice, RI/SMOM and $\overline{\text{MS}}$ schemes as well as the renormalization matrices which relate them.

While ReA0 and ReA2 and δ_2 agree well with expt a possible difficulty: δ_0

- The continuum and our lattice determinations of strong phase difference differs at the $\sim 2\sigma$ level:

$$\phi_{\epsilon'} = \delta_2 - \delta_0 + \frac{\pi}{2} = \begin{cases} (42.3 \pm 1.5)^\circ & \text{PDG [2]} \\ (54.6 \pm 5.8)^\circ & \text{RBC [47, 48]} \end{cases}$$

$$\phi_{\epsilon} \sim 43.5 \pm 0.5^\circ$$

mit direkter accessibler expt
Colangelo et al
RBC-UKQCD

Fortunately, due to the central value of the combination $\delta_2 - \delta_0 + \pi/2 - \phi_{\epsilon}$ and to the large uncertainties in the determination of the various matrix elements, these two choices yield almost identical results; ~~for definiteness, we~~

9/18/2017

hehner, lunghi + AS, 1508.01801

51

Sensitivity of ϵ' to strong phase(s)

$$\text{Re}\left(\frac{\epsilon'}{\epsilon}\right) = \text{Re}\left(\frac{\omega e^{i(\delta_2 - \delta_0 + \pi/2)}}{\sqrt{2}\epsilon} \left[\frac{\text{Im}(A_2)}{\text{Re}(A_2)} - \frac{\text{Im}(A_0)}{\text{Re}(A_0)} \right]\right)$$

See also
Lehner, Lunghi + AS P18'16

$$\cos(\delta_2 - \delta_0 + \pi/2 - \phi_\epsilon)$$

$$\xrightarrow{\quad} 43.5 \pm 0.5^\circ \text{ "PDG"}$$

$$\phi_{\epsilon'} \sim 42.3 \pm 1.5^\circ \text{ [Colangelo, Gasser, Leutwyler]}$$

$$\Rightarrow \cos(\) \Rightarrow 0.99978; \quad \phi_{\epsilon'} = 54.6 \pm 5.8^\circ \text{ RGE-UKQD PRL'15}$$

$$\Rightarrow 0.981 \quad \text{phase diff} \sim 26^\circ \text{ BUT } \epsilon' \text{ totally insensitive!!}$$

Diff $\sim 2\%$ on ϵ'

LmC2017; SIEGEN; HET-BNL;soni

52

Significant effort is being put now to calculate and understand
pi pi rescattering phases from diff pts of view

Generation of New gauge configs
For past 7~3 years

SUPERCOMPUTERS OVER 3 CONTINENTS!

Progress in the calculation of ϵ' on the lattice

C. Kelly

Resource	Million BG/Q equiv core-hours	Independent cfigs.
USQCD (BNL 512 BG/Q nodes)	50	220
RBRC/BNL (BNL 512 BG/Q nodes)	17	50
UKQCD (DiRAC 512 BG/Q nodes)	17	50
NCSA (Blue Waters)	108	380
KEK (KEKSC 512 BG/Q nodes)	74	296
Total	266	996

Table 1: A breakdown of the various resources we intend to utilize. Note that we require 4 molecular dynamics time units per independent configuration

4 diff. states

Total of ~1400 independent
By now ~1300 configs
measurements
done

Guess estimate of reduction of errors

- $\delta(\text{Im } A_0)$ from 65% \Rightarrow 20-25%
- $\delta(\text{Re } A_0)$ from 35% \Rightarrow 15-20% [don't use for ϵ' for now]
- Uncorrelated fits (due to lack of stat) \Rightarrow

Very good chance we'll be able to correlated fits *now*
with > 1200 *Possible bonus: reduction in errors (2014)*

- Systematic error from $\sim 27\% \Rightarrow \sim 20\%$
- Effect on ϵ' unclear : 'cause of hefty cancellations

$$\text{Re} \left[\frac{\epsilon'}{\epsilon} \right] \propto$$

$$\left[\frac{\text{Im } A_2}{\text{Re } A_2} - \frac{\text{Im } A_0}{\text{Re } A_0} \right] \rightarrow \delta \sim 60\%$$

Additional Improvements/checks in lattice ε' determination underway for past ~ 2 years

- EM+ isospin

Under extensive study

*Pheno estimate $\sim 15 \pm 8\%$.
Cirigliano, Neufeld, Ecker + Pich '03*

- Completely diff method(s)

UConn PhD Student Dan Hoying

- I) excited $\pi\pi$ state

CU PhD '16 Dan Murphy ChPT works!!

- II) Revisit ChPT

well for physical π, K masses & NLO!

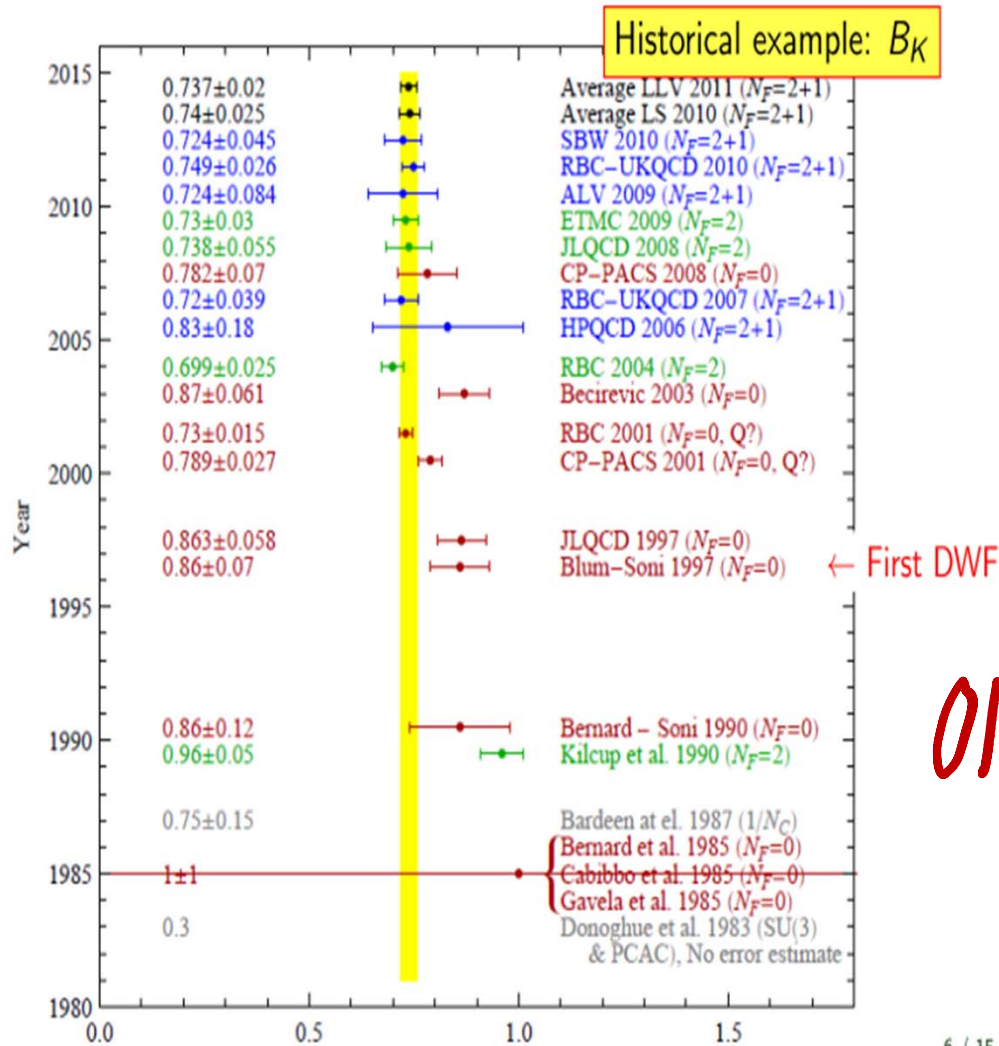
→ Reexamine BDSPW'84, Laiho + AS'04 for ε'

***underlying method is systematically improvable
=>multitude of successful demonstrations by now***

- BK in full QCD with DWF '07 RBC-UKQCD error O(7%)
- Since ~2012 many discretizations , WA error O(1-2%)
- Re A2 from ~25% around 2012 to now ~10% (now no longer due to lattice but only only due to perturbation theory error upto NLO!)
- Kl3, A2, fB's , BB's.....
- Quark masses; in particular ms no longer anywhere around ~150 MeV [used to be PDG value] but now ~100 MeV.
- ***No doubt that A0 and ϵ' will also go that way for quite sometime to come.....to ~10% total in another ~ 3-5years!.***

After that EM& isospin effects need to be ascertained quantitatively;
WIP

Power of the lattice: Only method to systematically reduce the NP error!



AB-initio Calculations

$$B_K = \frac{\langle K | (\bar{s} \gamma_\mu s) | K \rangle^2}{8/3 g^2 m_K^2}$$

ONE ILLUSTRATION

6 / 15

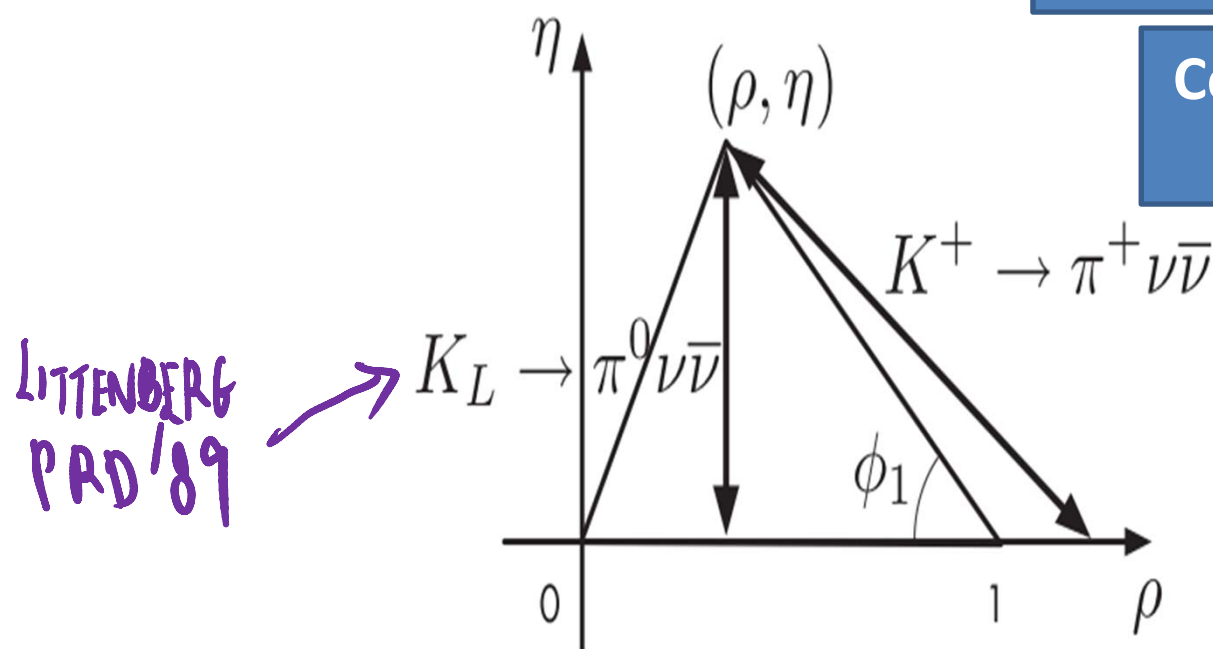
***MANY IMPLICATIONS, AS ONE
EXAMPLE:K-UT***

See Lehman, Longhi + AS PUB'16

K-UT: A dream for some

Blucher, Winstein and
Yamanaka '09; see
also Buras

Construction of a
Kaon UT



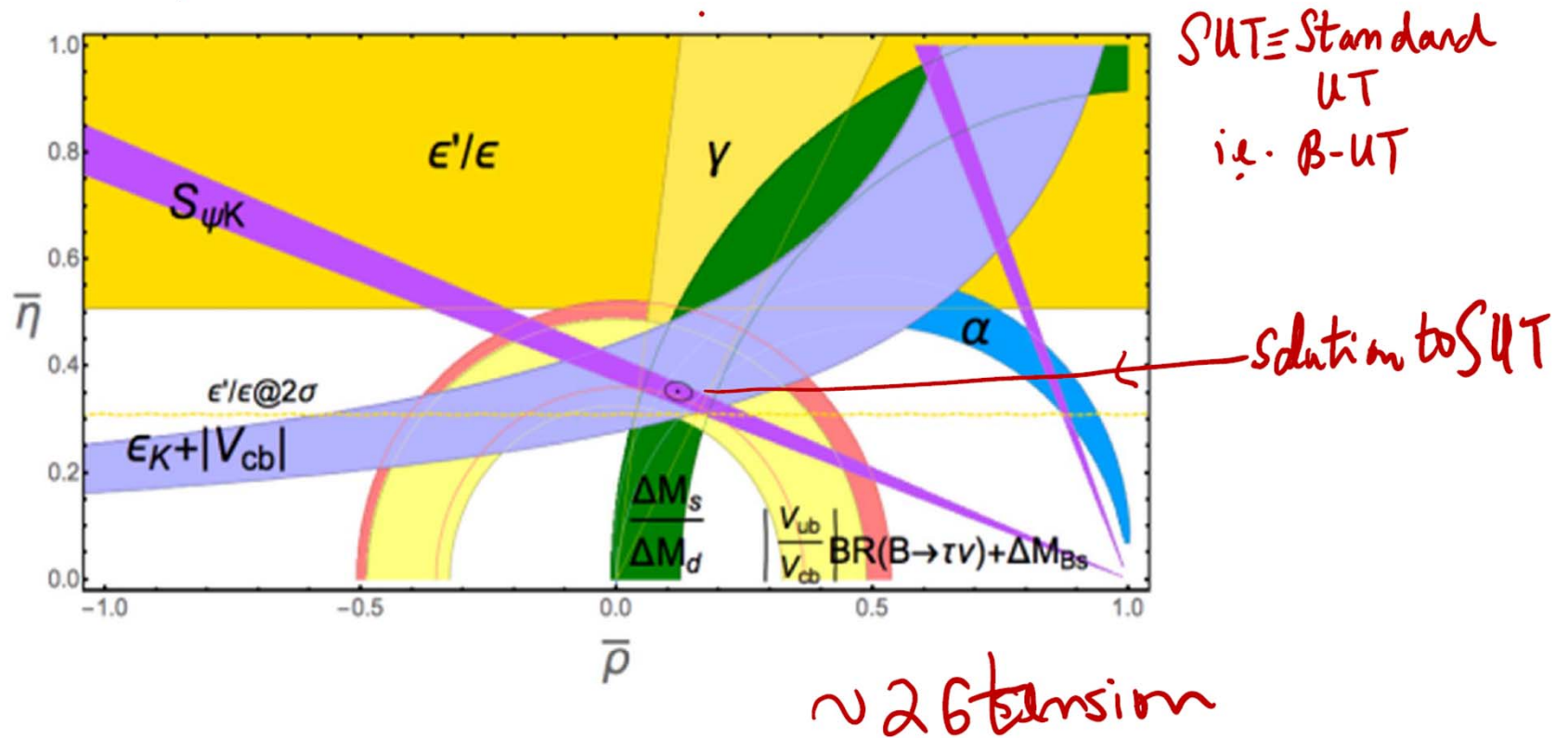
LITTENBERG
PAD '89

Lehner + Longhi + AS
PLB '2016

Fig. 14. Unitarity triangle.

Instead of (or in addition to) $K_L \rightarrow \pi^0 \nu \bar{\nu}$ can now plan on using ϵ'/ϵ

Lattice ϵ'/ϵ & SUT: CIRCA ~ 2015



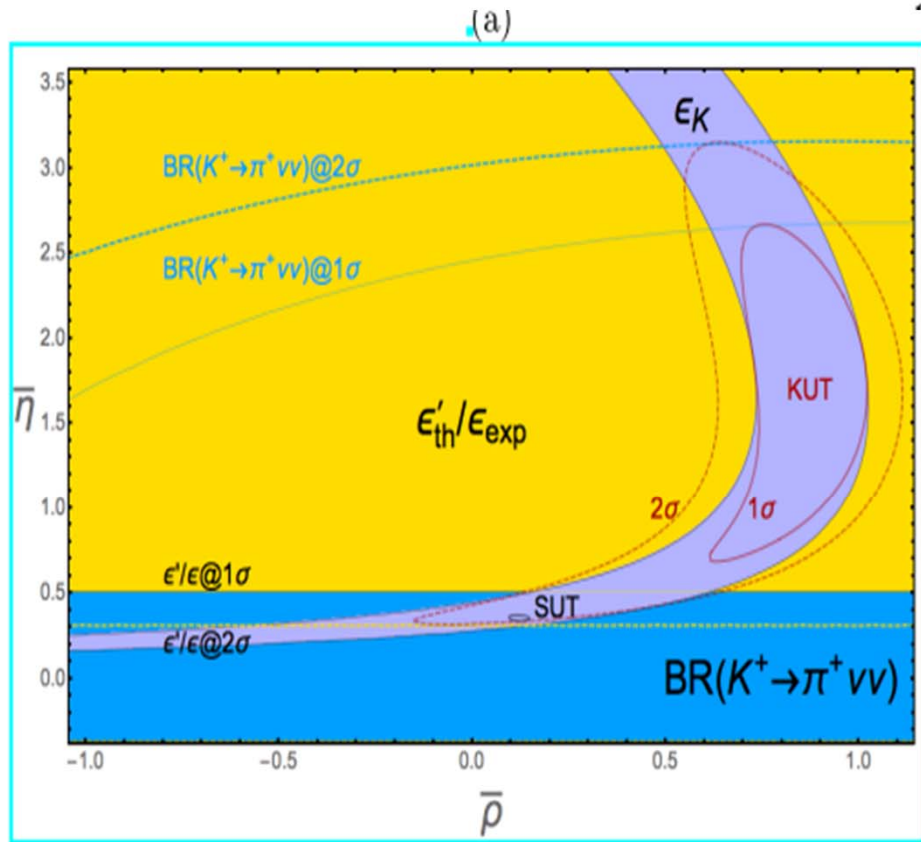
Sketch of an emerging K-UT: 3 key Kaonic inputs.

I ϵ_K induced CP

II

$$\text{BR}(K^+ \rightarrow \pi^+ \nu \bar{\nu}) = \begin{cases} (8.64 \pm 0.60) \times 10^{-11} & \text{SM} \\ (17.3^{+11.5}_{-10.5}) \times 10^{-11} & \text{E949} \end{cases}$$

BNL



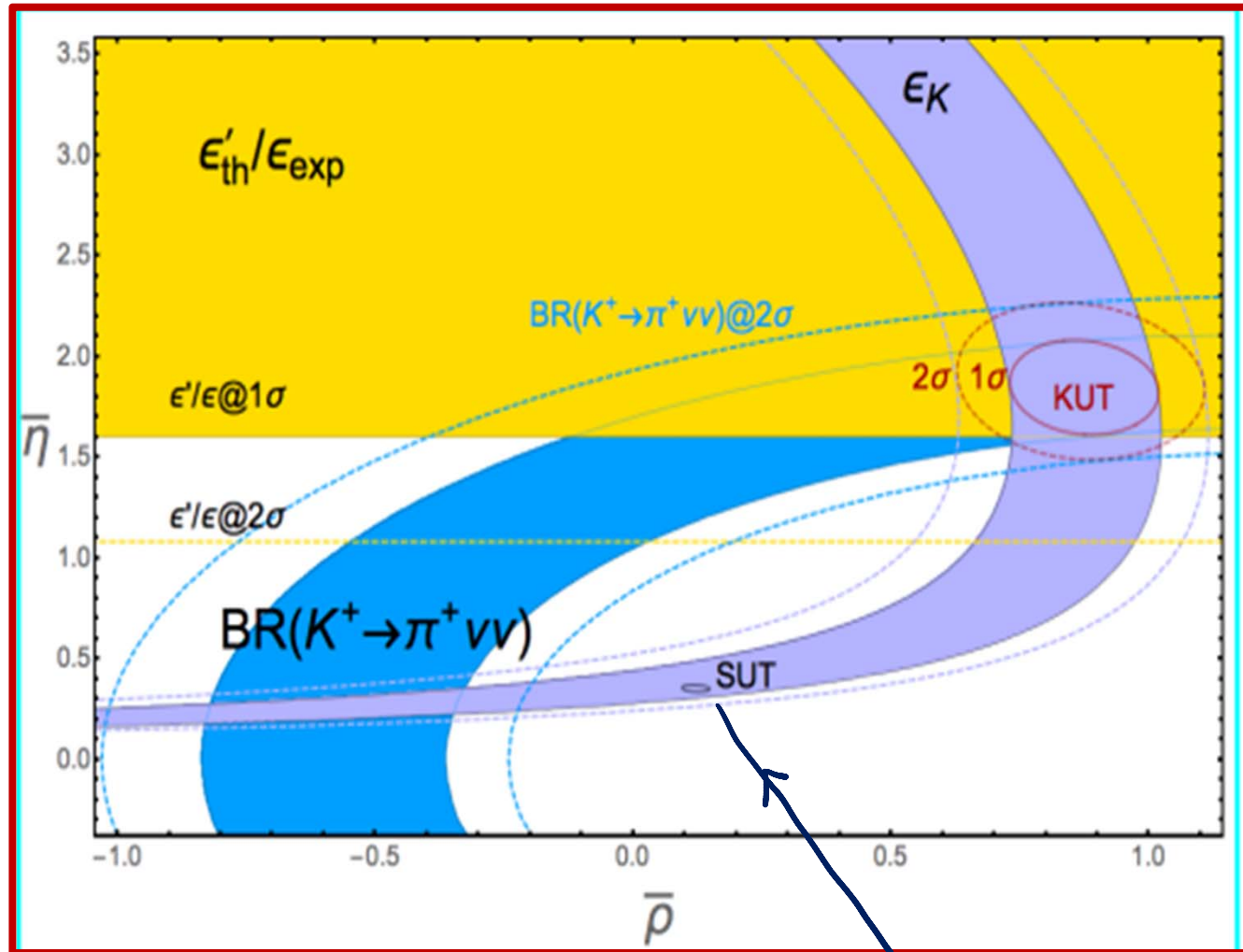
III

$$\text{Re}\left(\frac{\epsilon'}{\epsilon}\right)_K = \begin{cases} (16.7 \pm 1.6) \times 10^{-4} \\ (1.36 \pm 5.21_{\text{stat}} \pm 4.49_{\text{syst}}) \times 10^{-4} \end{cases}$$

PDG 2015

ABCT + UKACD '15

POSSIBLE KUT CIRCA 2020: DUE NA62 + RBC-UKQCD



NO unique
\$\beta, \eta\$

Assumed:
NA62, 100
events with
~7% error
RBC-UKQCD,
 $\delta(\text{Im}A_0) \sim 18\%$
[current ~60%]

Lehner, Lunghi + AS PLB'16

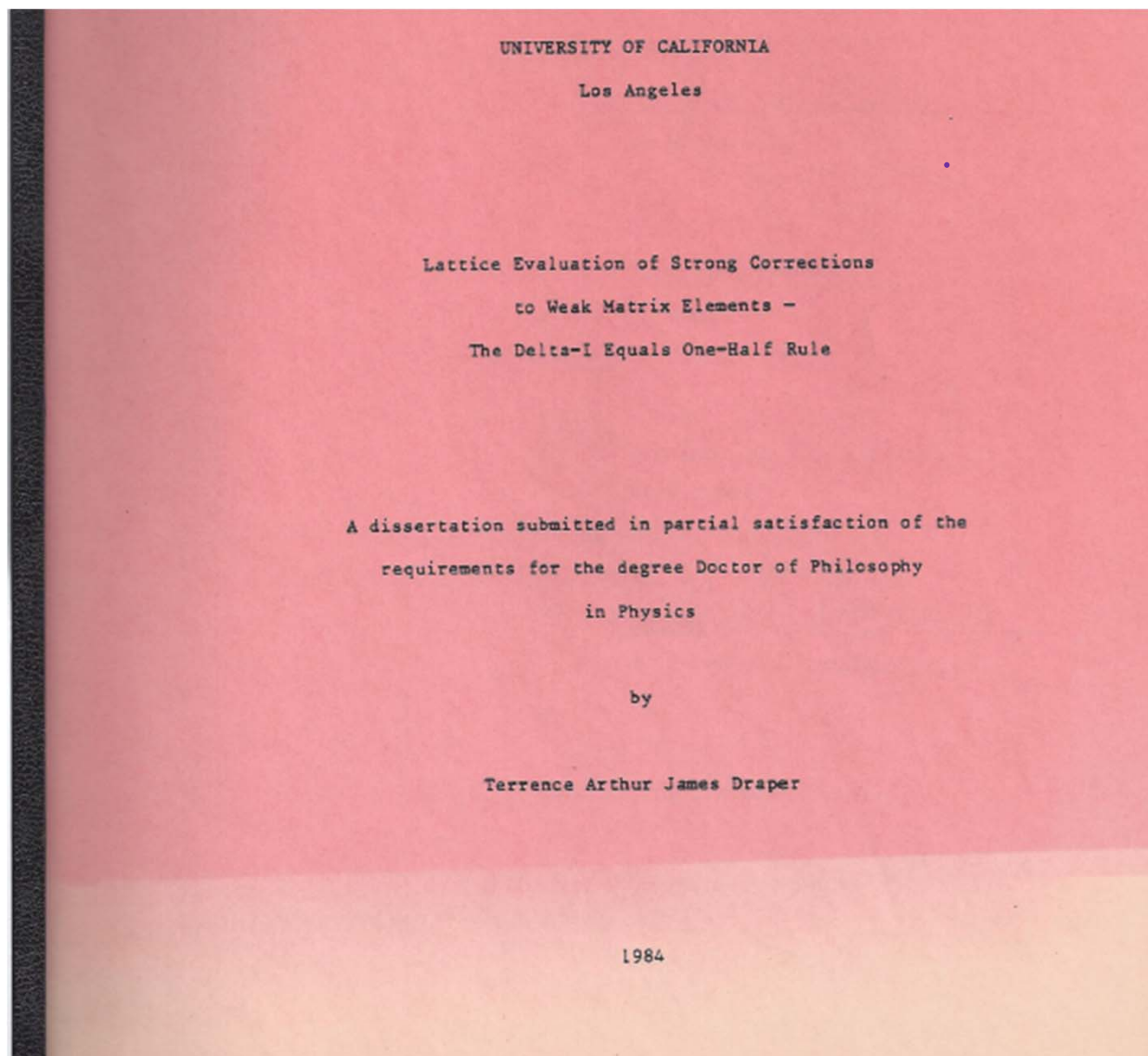
Flavor anomalies; Lyon; A Soni(BNL-HET)

"Standard" (B) UT

**ITS MY $\sim 36^{\text{TH}}$ YEAR ON $K \Rightarrow \pi\pi$ &
 ϵ'WHY?**



The 1st
Ph D
Thesis



Grew from
End of year
Beer Party
~ June 20, 1982!
[UCLA]

MOTHER of all (lattice) calculations to date: A Personal Perspective

- Calculation $K \Rightarrow \pi\pi$ & ϵ' were the reasons I went into lattice over 1/3 of a century ago!
- *9 + (3 new) PhD thesis*: Terry Draper (UCLA'84), George Hockney(UCLA'86), Cristian Calin (Columbia=CU'01), Jack Laiho(Princeton'04), Sam Li(CU'06), Matthew Lightman(CU'09), Elaine Goode(Southampton'10), Qi Liu(CU'12), Daiqian Zhang(CU'15)+ [new ones starting from CU, U Conn and Southampton] + many PD's & junior facs.. obstacles & challenges (**and of course “mistakes”!**) ad infinitum.....

***WHY FOCUS with SUCH intense
DETERMINATION
All these many many years?***

UNDERLYING REALIZATION

***ϵ' : MOST LIKELY A GEM IN
SEARCH OF NEW PHENOMENA***

Contrarian/Complementary view

- **flavor physics is actually hanging by perhaps the weakest link i.e. a single CP-phase endowed by the 3g –SM.**
- **In many ways this is a contrarian (or complementary) point of view, in sharp contrast to the overwhelming majority following the naturalness lamp post via Higgs radiative stability.**
- **ϵ' due to its miniscule value, esp because it results from unnatural large cancellations seemed clearly highly vulnerable...The mantra being followed for a very very long time**

Its presumed importance:

- lies in its very small size => Perhaps new phenomena has a better chance of showing up
- Smallness also renders it exceedingly sensitive monitor of flavor –alignment
- **Simple naturalness arguments strongly suggest ϵ' very sensitive to BSM – CP odd phases**
- In many ways, (superficially) ϵ' is rather analogous to nedmboth being very sensitive to BSM-CP phases; however, key diff for (now) nedm expt is the key, theory has marginal role, in sharp contrast to ϵ'
- **Understanding ϵ' , nedm are extremely important for uncovering new physics and/or learning how naturalness really works in nature**



IF YOU BUILD IT THEY WILL COME

Flavor anomalies; Lyon; A Soni(BNL-HET)

*If there is new physics around
below ~ 5 TeV, there is an excellent
chance that ε' will find it!*

[of course requires accurate theory calculation...
RBC-UKQCD plans for X5 in stat and appreciable
improvements in systematic in ~ 2 years]

Soni's ϵ' Rule

- If ϵ' ends up being due SM then:
 - 1. Other anomalies, $RD(*)$, $RK(*)$, $g-2$ will ALL go away
 - 2. ~~It~~ *If so, that* will give us a vitally important new info on naturalness

MODEL INDEPENDENT IMPLICATIONS OF $R_D^{(*)}$ ANOMALIES FOR [LHC] COLLIDER EXPERIMENTS: SAMPLE ILLUSTRATIONS

Implications of Anomalies

- **For Collider: From Isidori ; Kamenik; ADS';
Luzio; Hou;**
- **FOR IF: Guadagnoli; Fajfer; Neubert; Mandal;
Fuentes-Martin**

Conclusions

FUENTES-MARTIN

It is possible to find **well-motivated** combined explanations of the B anomalies, compatible with current data in both low- and high-energies

C ALSO Mandal

The model I presented, a **Pati-Salam flavor deconstruction**, predicts several characteristic smoking-gun signatures that differentiate it from other solutions

- $\Delta R_{D^*}/\Delta R_D \simeq 0.45$
- NP in $b \rightarrow s\tau\tau \sim b \rightarrow s\mu\mu$ and $b \rightarrow s\tau\mu \sim \mathcal{O}(5) \times b \rightarrow s\mu\mu$
- Possibility of a deficit in $\Delta B = 2$ & CP violation involving the 3rd quark family
- Possible large enhancements in $B \rightarrow \tau\nu$

← !!

← C ALSO NPS '16

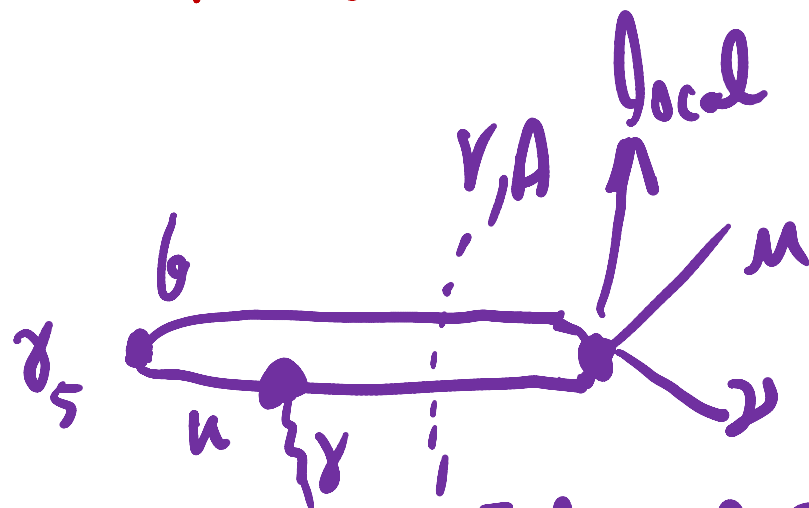
If the anomalies are really pointing to NP, **new experimental indications** (both in high- p_T and at low energies) will show up soon in several observables

Exciting times ahead of us. Let's have fun

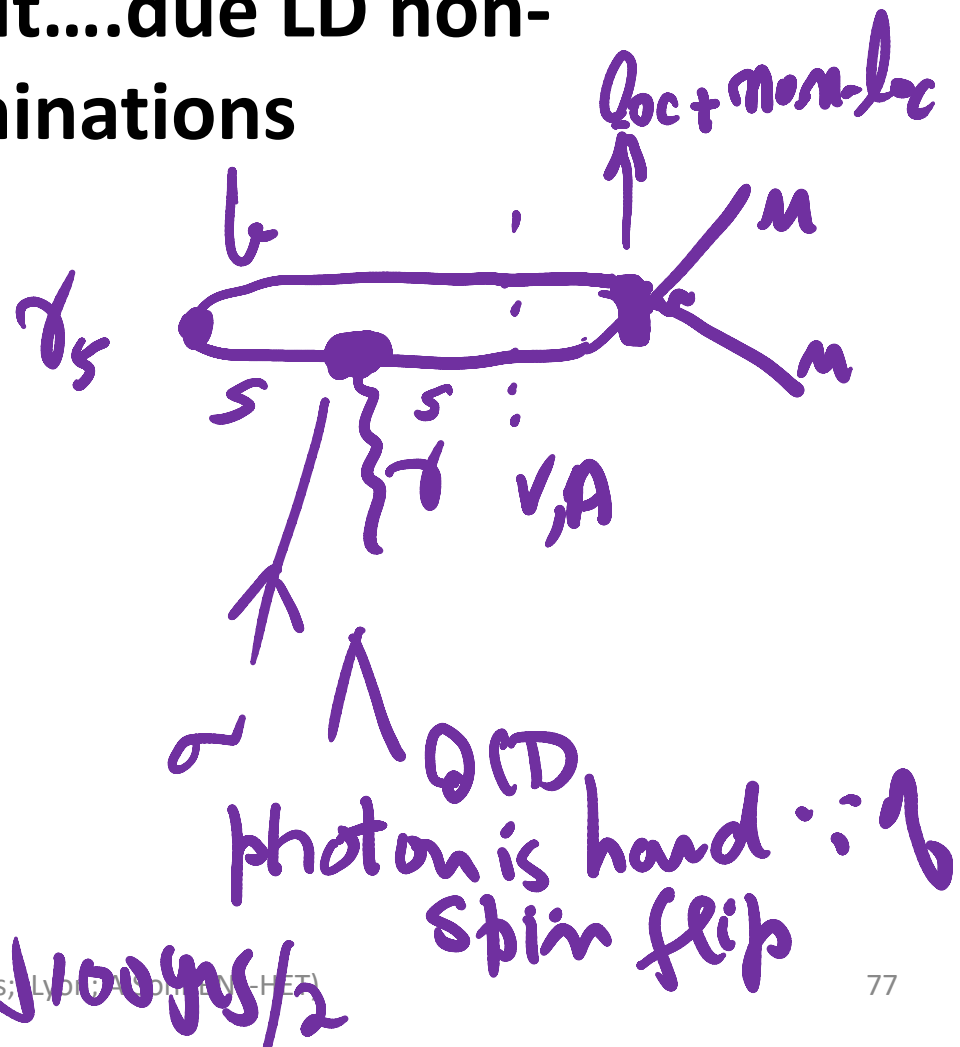
Guadagnoli $B(s) \Rightarrow \mu \mu \gamma$

- Nice idea but difficult...due LD non-perturbative contaminations

LATTICE INPUT Seems Essential



See Atwood, Eilam, AS

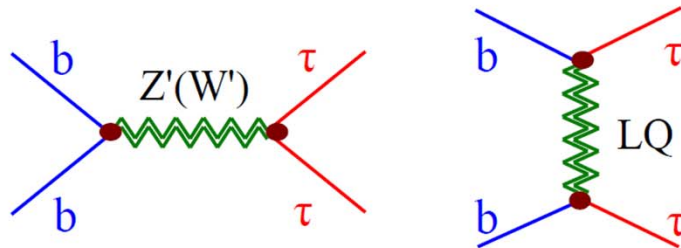


Flavor anomalies; Lybri, Aspin, HET

► EFT-type considerations [The main problems]

Three main problems identified in the recent literature (*driven mainly by R_D*):

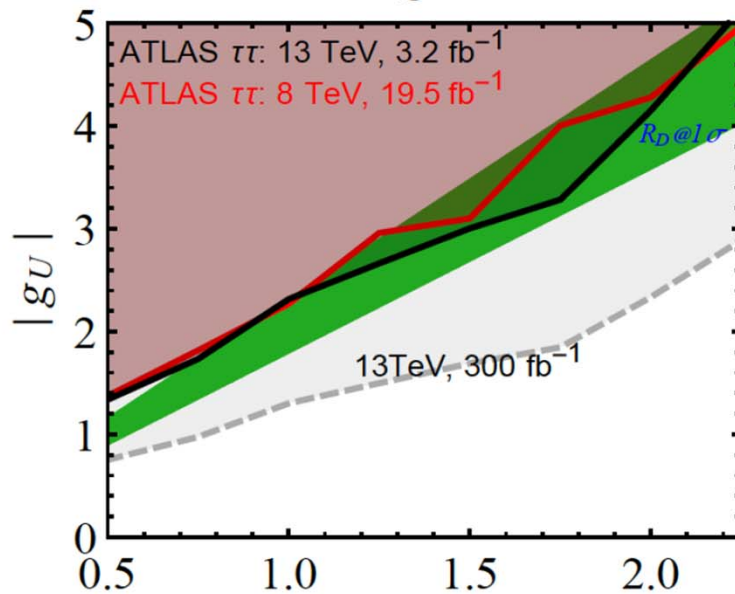
I. high- p_T constraints



Naïve EFT scale

[from R_D - setting $g, \lambda \rightarrow 1$]: $\Lambda \sim 700$ GeV

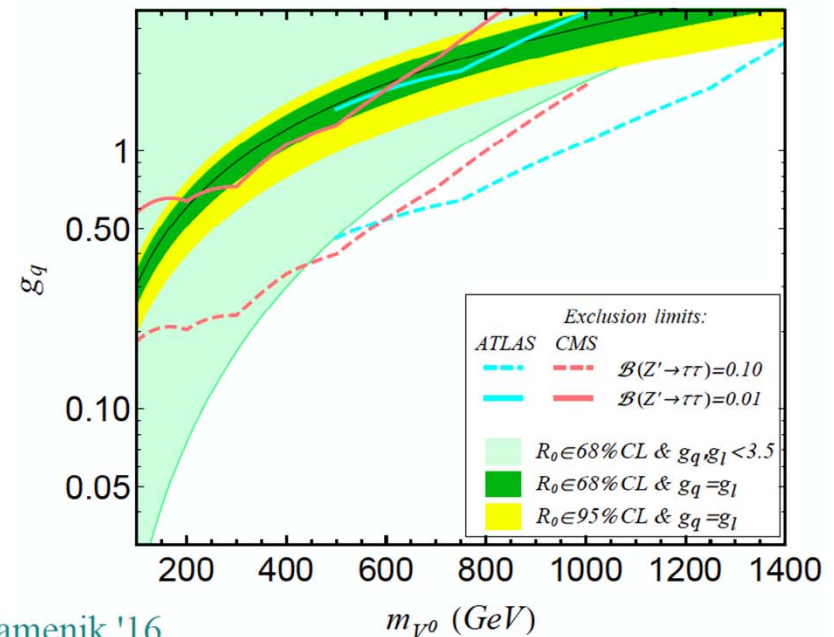
Vector LQ exclusion



M_U (TeV)

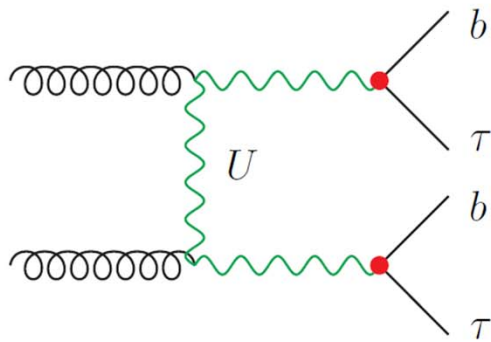
Faroughy, Greljo, Kamenik '16

Z' exclusion

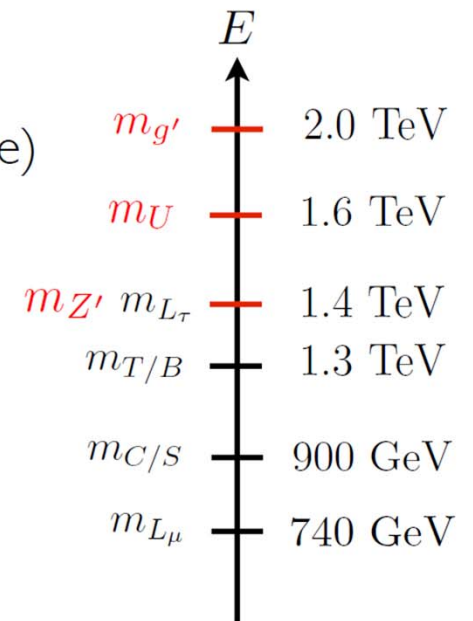


High- p_T searches


- LQ pair production via QCD
 - 3rd generation final states (fixed by anomaly and $SU(2)_L$ invariance)



$$\begin{cases} U \rightarrow b\tau^+, & \text{BR.} = 50 \% \\ U \rightarrow t\bar{\nu}, & \text{BR.} = 50 \% \end{cases}$$



[CMS search for spin-0, 1703.03995
recast for spin-1 1706.01868 (see also 1706.05033) + Moriond EW update]

$m_U \gtrsim 1.5 \text{ TeV}$  LQ mass sets the overall scale: $M_{g'} \simeq \sqrt{2} M_U$ $M_{Z'} \simeq \frac{1}{\sqrt{2}} M_U$

ALTMANNSHOFFER, Dev + AS
1704.06659 + Seq, WIP

MODEL INDEPENDENT IMPLICATIONS OF RD(*) ANOMALIES FOR [LHC] COLLIDER EXPERIMENTS

- In a nut-shell B-experiments seem to find anomalous behavior in the underlying $b \Rightarrow c \text{ tau } \nu$
- This necessarily [by XSym] implies there should be analogous anomaly in $g + c \Rightarrow b \text{ tau } \nu \dots \Rightarrow \text{pp} \Rightarrow b \text{ tau } \nu$
- *Thus it immediately leads to inescapable search channels for possible NP at the high energy frontier for ATLAS & CMS and these are urgently urged*

Xsymm implications of anomalies for colliders

ADD!

$R_{D^{(*)}}$ ANOMALY: A POSSIBLE HINT FOR ...

PHYSICAL REVIEW D **96**, 095010 (2017)

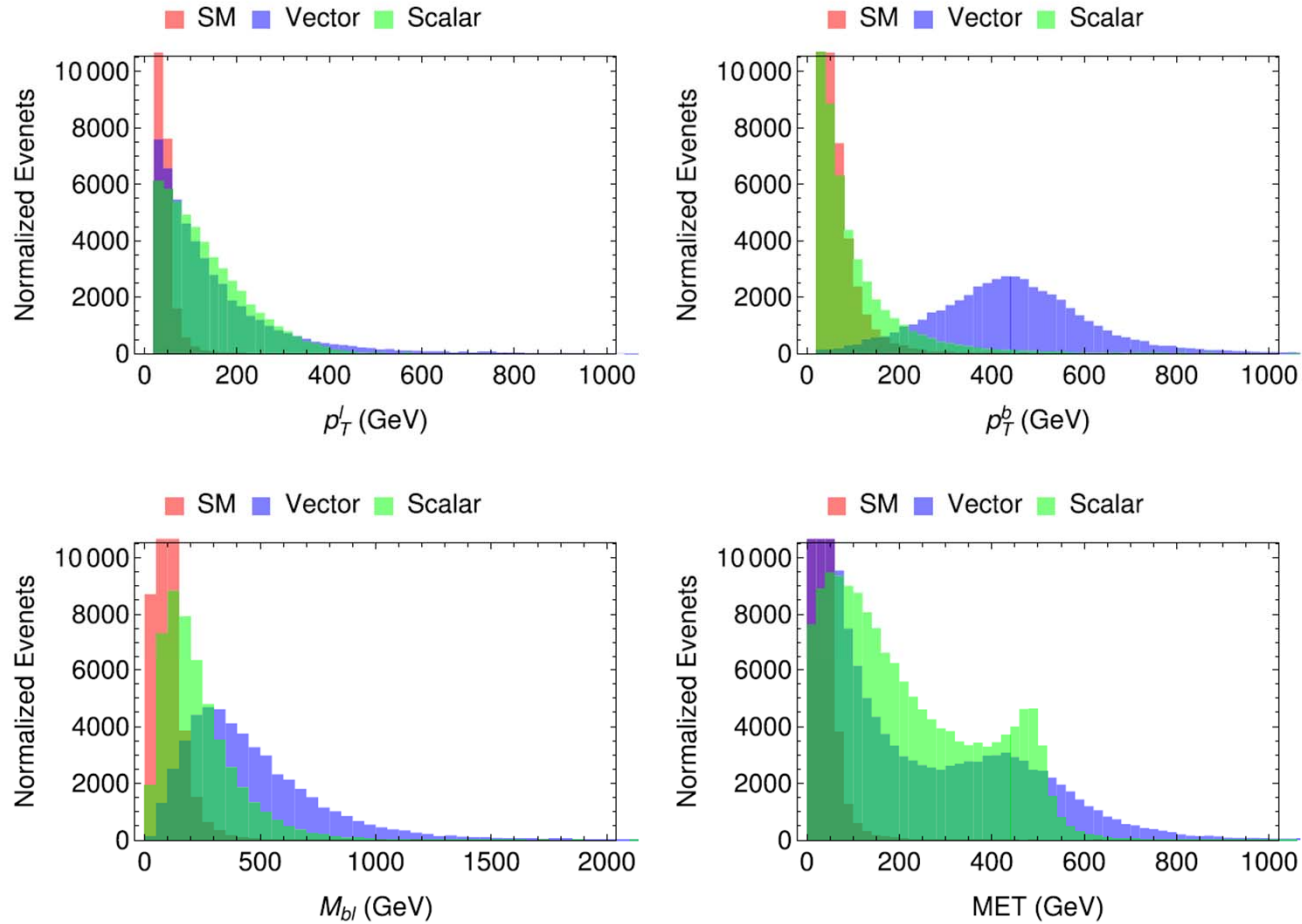


FIG. 1. Normalized kinematic distributions for the $pp \rightarrow b\tau\nu \rightarrow b\ell + \cancel{E}_T$ signal and background.

EXPECT DISTINCTIVE NP CONTRIBUTIONS IN COLLIDERS

ANOMALY: POSSIBLY A HINT FOR (NATURAL) SUSY-WITH RPV

- **ASSUMING the anomaly is REAL & HERE TO STAY [BIG ASSUMPTION due to caveats mentioned]**
- **Anomaly involves simple tree-level semi-leptonic decays**
- **Also $b \Rightarrow \tau$ (3rd family)**
- **Speculate: May be related to Higgs naturalness**
- **Seek minimal solution: perhaps 3rd family super-partners(a lot) lighter than other 2 gens > proton decay concerns may not be relevant=> RPV [“natural” SUSY]**
- **RPV natural setting for LUV ...can accommodate $g-2$ and ϵ s’ if needs be**
- **Collider signals tend to get a lot harder than (usual-RPC) SUSY**

RPV_3 preserves gauge coupling unification irrespective of # of effective gens. 1, 2 or 3.

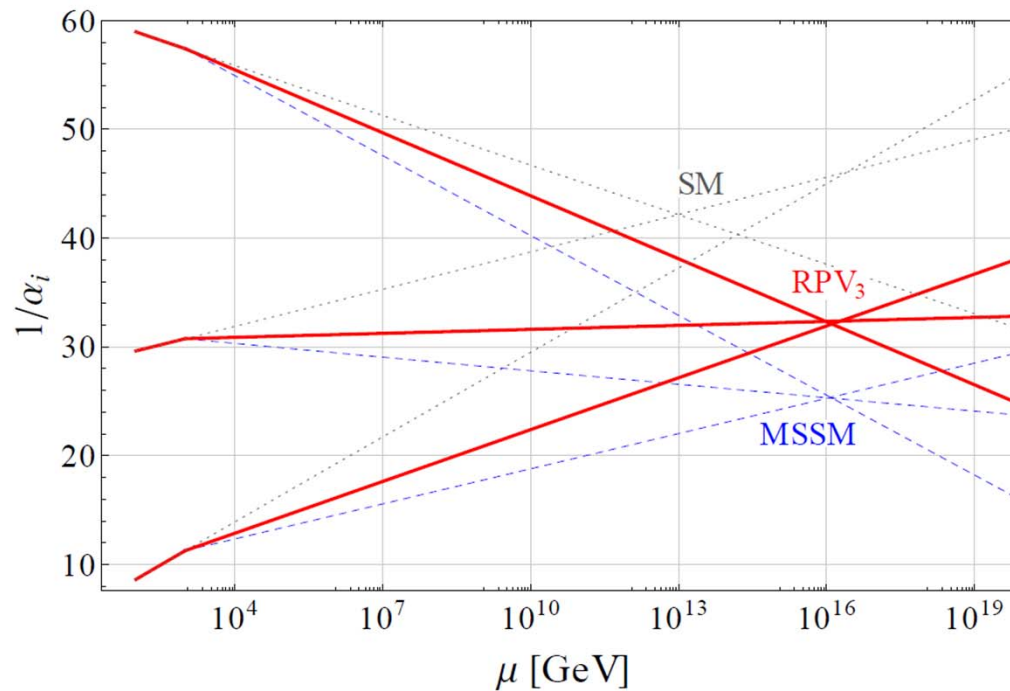


FIG. 2. RG evolution of the gauge couplings in the SM, MSSM and with partial supersymmetrization.

Unification scale stays same, only value of couplings shifts

For pheno relevant terms:

ADS' PRD 2017

$$\mathcal{L} = \lambda'_{ijk} [\tilde{\nu}_{iL} \bar{d}_{kR} d_{jL} + \tilde{d}_{jL} \bar{d}_{kR} \nu_{iL} + \tilde{d}_{kR}^* \bar{\nu}_{iL}^c d_{jL} \\ - \tilde{e}_{iL} \bar{d}_{kR} u_{jL} - \tilde{u}_{jL} \bar{d}_{kR} e_{iL} - \tilde{d}_{kR}^* \bar{e}_{iL}^c u_{jL}] + \text{H.c.}$$

) RPV₃ interaction

← D/m-6

→ FNRP(*)

$$\mathcal{L}_{\text{eff}} \supset \frac{\lambda'_{ijk} \lambda'^*_{mnk}}{2m_{\tilde{d}_{kR}}^2} \left[\bar{\nu}_{mL} \gamma^\mu \nu_{iL} \bar{d}_{nL} \gamma_\mu d_{jL} \right. \\ \left. - \underline{\nu_{mL} \gamma^\mu e_{iL} \bar{d}_{nL} \gamma_\mu \left(V_{\text{CKM}}^\dagger u_L \right)_j} + \text{h.c.} \right] \\ - \frac{\lambda'_{ijk} \lambda'^*_{mjn}}{2m_{\tilde{u}_{jL}}^2} \bar{e}_{mL} \gamma^\mu e_{iL} \bar{d}_{kR} \gamma_\mu d_{nR} ,$$

NOTE:

ITS
SM-like!

For addressing RK(*) in RPV, see e.g. Das et al , 1705.09188

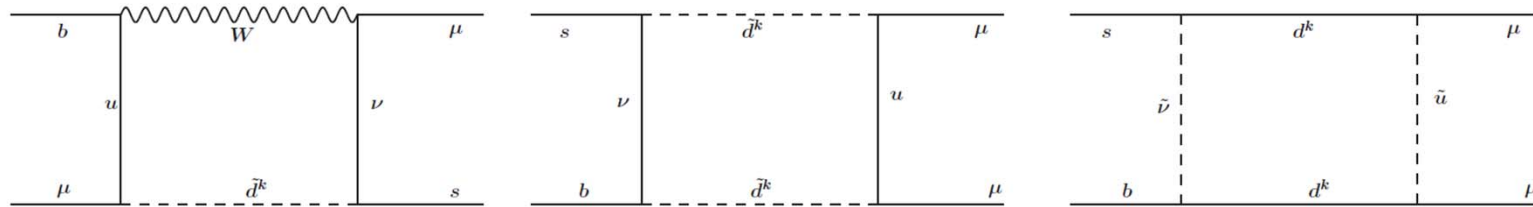


FIG. 1: Representative diagrams for $b \rightarrow s \mu^+ \mu^-$ transition in R -parity violating interactions.

g-2 with RPV has a long history, see, e.g. Kim, Kyae and Lee, PLB 2001

We (ALTMANNSHÖFER+DEV+AS) are examining + update in light of current flavor anomalies **WORK IN PROGRESS**

CONSTRAINTS: TIGHTENING EXPT'S NOOSE AGAINST SPECIFIC MODELS

Table 13-6. Model-dependent effects of new physics in various processes.

Model	CP Violation		Rare Decays	$D^0-\bar{D}^0$ Mixing
	$B_d^0-\bar{B}_d^0$ Mixing	Decay Ampl.		
MSSM	$\mathcal{O}(20\%)$ SM Same Phase	No Effect	$B \rightarrow X_s \gamma$ – yes $B \rightarrow X_s l^+ l^-$ – no	No Effect
SUSY – Alignment	$\mathcal{O}(20\%)$ SM New Phases	$\mathcal{O}(1)$	Small Effect	Big Effect
SUSY – Approx. Universality	$\mathcal{O}(20\%)$ SM New Phases	$\mathcal{O}(1)$	No Effect	No Effect
R -Parity Violation	Can Do	Everything	Except Make	Coffee
MHDM	\sim SM/New Phases	Suppressed	$B \rightarrow X_s \gamma, B \rightarrow X_s \tau \tau$	Big Effect
2HDM	\sim SM/Same Phase	Suppressed	$B \rightarrow X_s \gamma$	No Effect
Quark Singlets	Yes/New Phases	Yes	Saturates Limits	$Q = 2/3$
Fourth Generation	\sim SM/New Phases	Yes	Saturates Limits	Big Effect
LRM – $V_L = V_R$	No Effect	No Effect	$B \rightarrow X_s \gamma, B \rightarrow X_s l^+ l^-$	No Effect
– $V_L \neq V_R$	Big/New Phases	Yes	$B \rightarrow X_s \gamma, B \rightarrow X_s l^+ l^-$	No Effect
DEWSB	Big/Same Phase	No Effect	$B \rightarrow X_s \ell \ell, B \rightarrow X - s \nu \bar{\nu}$	Big Effect

though in many cases further data may limit the available parameter space. In the more exciting eventuality that the results are not consistent with Standard Model predictions, the full pattern of the discrepancies both in rare decays and in CP -violating effects will help point to the preferred extension, and possibly rule out others. In either case there is much to be learned.

constraints

- Direct searches via $pp \rightarrow \tilde{b}\tilde{b} \rightarrow \tau^+ \tau^- t\bar{t}$

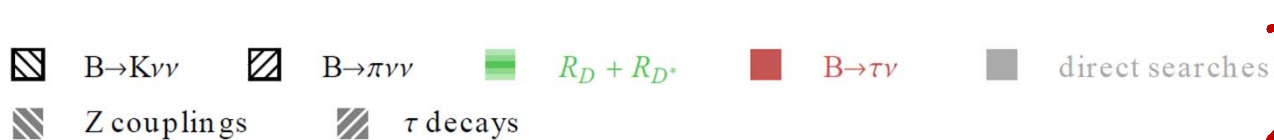
Indirect constraints considered due $B \Rightarrow \tau \nu$; $\pi \tau \nu$;
 $\pi(K) \nu \nu \dots$
 Also $B_c \Rightarrow \tau \nu \dots$

To a/c (within 1σ) of expt for $RD(^*)$ needs largish $\lambda'_{333} \sim 1 - 2$ range with quite heavy sbottoms but such large couplings develop landau pole below GUT scale. We require couplings stay perturbative below GUT so with $\lambda'_{333} < \sim 1$,

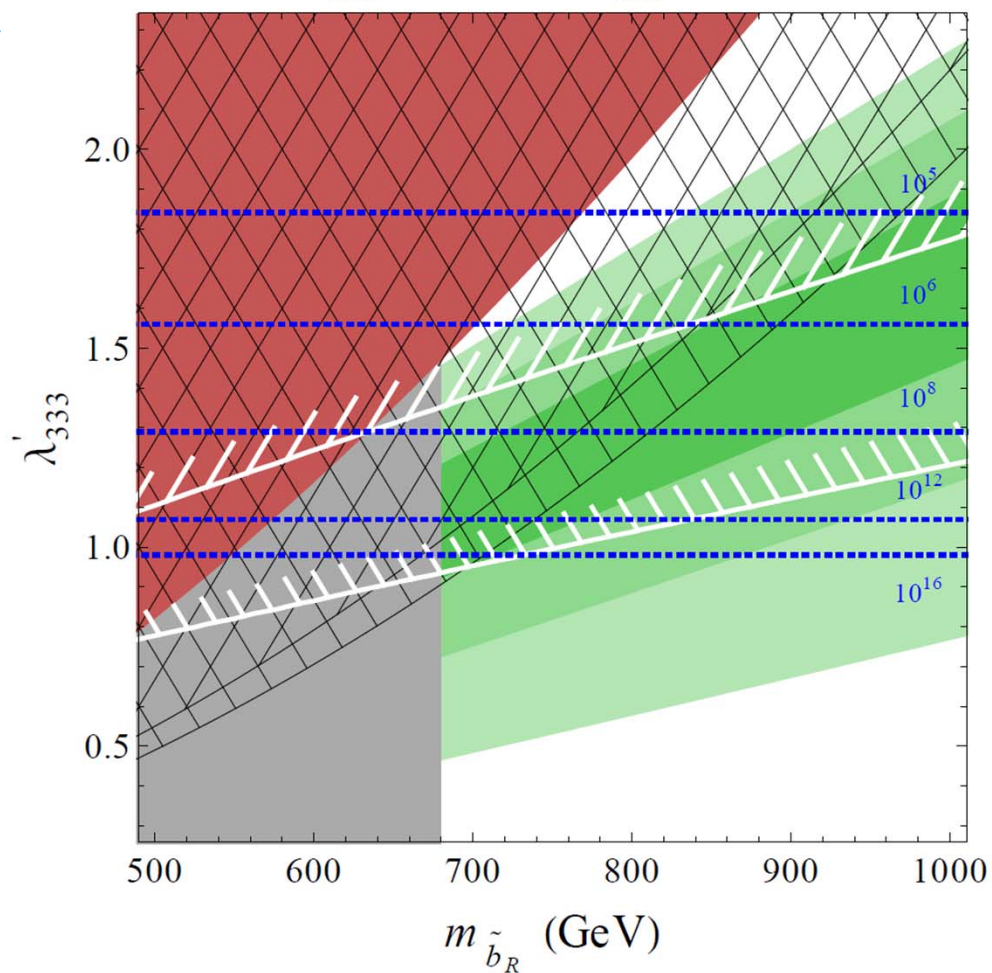
\Rightarrow TAKE HOME: This version of RPV is actually (surprisingly) well constrained

\Rightarrow With improved measurements $RD(^*)$ in RPV3 may be difficult

As a specific illustration



$$\lambda'_{313} = -0.05, \lambda'_{323} = 0.01$$

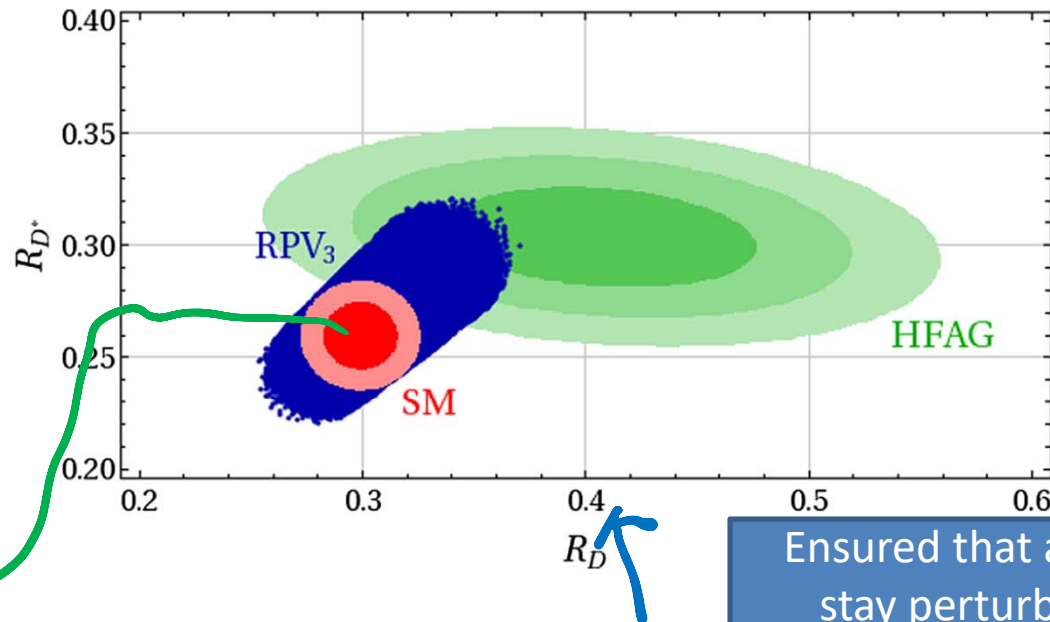


Constraints imposed

FIG. 3. RPV parameter space satisfying the $R_{D^{(*)}}$ anomaly and other relevant constraints.

RPV3 allows
 $R_D = (.254-.371)$
 $R_D^* = (.220-.320)$
 Contrast Fuentes-
 Martin:
 $\frac{\Delta R_D^*}{\Delta R_D} \approx 0.45$

*More
 Realistic
 SM Blob*



HFAG dec2016
 $R_D = .403 \pm .040 \pm .024$
 $R_D^* = .310 \pm .015 \pm .008$
 LHCb 06/06/17
 $R_D^* = 0.305$

Ensured that all RPV3 couplings
 stay perturbative up to GUT

FIG. 4. The SM predictions (red), experimental world average (green), and accessible values in our RPV-SUSY scenario (blue) in the R_D vs. R_D^* plane. For the SM, bearing in mind recent works [17,20,22] we are taking $(R_D^{\text{SM}}, R_{D^*}^{\text{SM}}) = (0.299 \pm 0.011, 0.260 \pm 0.010)$.

all constraints.....RPV(blue) region obtained by scanning with
 sbottom mass 680-1000Gev, $0 < \lambda_{333} < 2; |\lambda_{323}| < 0.1; |\lambda_{313}| < 0.3$

IN CLOSING

Contrarian/Complementary view

- **flavor physics is actually hanging by perhaps the weakest link i.e. a single CP-phase endowed by the 3g –SM.**
- **In many ways this is a contrarian (or complementary) point of view, in sharp contrast to the overwhelming majority following the naturalness lamp post via Higgs radiative stability.**
- **In this context it is useful to stress**

Importance of the “IF”: score card

- Beta decay $\Rightarrow G_f \Rightarrow W....$
- Huge suppression of $KL \Rightarrow \mu\mu$; miniscule $\Delta m_K \Rightarrow$ charm
- $KL \Rightarrow 2\pi$ but very rarely; mostly to $3\pi \Rightarrow$ CP violation \Rightarrow 3 families
- Largish B_d –mixing \Rightarrow large top mass
- etc.....
- \Rightarrow **extremely unwise to put all eggs in HEF**
- Complementary info from IF can be a crucial guide for pointing to new thresholds as well as provide important clues to the nature of the signals there from

Summary and Outlook..[p1 of 2]

- Hints of LUV [from 3 B experiments] in sl B decays are interesting though not yet compelling despite the claimed 4.1 sigma; FCNC mu/e LUV indications in B=K (and K*) || are also extremely interesting and may well be related to LUV in sl B....If so similar mu/e LUV should be seen in FCNC channels [e.g] in baryonic B decays as well as a multitude of other channels.
- Though not yet compelling; OTOH no good reason that experimental hints are wrong. While we are accustomed to respecting LU the sensitivities of the current experiments are better than the past.
- This is not a violation of SR or GR, but only of accepted dogma; experimental results on LUV therefore deserve serious attention.
- That is my interest, try get to the bottom of it all AFAP using on & off the lattice tools
- Accurate SM predictions are usually very challenging and demanding but are extremely important; BSM scenarios are easy to cook up but $1/N^{N'}$ of being correct with $N, N' > 1000$
- However, in the context of BSM note also the truly impressive constraints on models that past decade or so studies have resulted [as illustrated by RPV3].
- More data from LHCb from Run 2 < 1 year should help and further ~2 years down Belle II should start to help more....On the theory side, of critical importance is FF for $B \Rightarrow D^*$...should start to get results in ~ 6 months to 1 year RBC/UKQCD as well as others
- FCNC mu/e LUV so far only LHCb data shows the effect...confirmation from other experiments would be extremely helpful.

Summary and Outlook ...p.2

- It may well be that BNL's observed $g-2$ signals of possible NP were just a precursor to these observations in B decays.
- Lattice progress in $g-2$ by RBC-UKQCD as well as global efforts are impressive ...But needs to reduce errors further by $\sim X4$...Expect next reduction $X2$ in a year or so
- ϵ' : RBC-UKQCD should be able to appreciably improve their 2015 result of ~ 2.1 sigma tension, in <6 months
- Personally, this is the ~ 36 th year of trying to tame this really wild beast; so it'd be welcome indeed.
- **There is now an exciting and may be even a revolutionary possibility that one or more of these avenues will show significant departure from SM in $\sim 1-2$ years**

XTRAS

Lattice computation of the decay constants of B and D mesons

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(Received 1 July 1993)

Semileptonic decays on the lattice: The exclusive 0^- to 0^- case

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Lattice study of semileptonic decays of charm mesons into vector mesons

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(Received 30 September 1991)

We present our lattice calculation of the semileptonic form factors for the decays $D \rightarrow K^*$, $D_s \rightarrow \phi$, and $D \rightarrow \rho$ using Wilson fermions on a $24^3 \times 39$ lattice at $\beta=6.0$ with 8 quenched configurations. For $D \rightarrow K^*$, we find for the ratio of axial form factors $A_2(0)/A_1(0) = 0.70 \pm 0.16^{+0.19}_{-0.13}$. Results for other form factors and ratios are also given.

PIONEERING WORKS leading to
modern Day UT

SU(3) flavor breaking in hadronic matrix elements for $B-\bar{B}$ oscillations

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Later DMs
CDF, DCP

⇒

Flavor anomalies; Lyon, 8 September

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- Christoph Lehner
- Meifeng Lin

- RBRC

- Amarjit Soni
- **Chris Kelly**
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- Shigemi Ohta (KEK)
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- Luchang Jin
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- Greg McGlynn
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- Connecticut

- Tim Blum

FOUNDING members of RBC Collab: Blum, Christ, Mawhinney + A S