

# Footprints of LQs: from $B$ to $K$ rare decays

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# Outline

- 1 Introduction
- 2  $s \rightarrow d\nu\bar{\nu}$  transitions
- 3 Pheno of two LQ models
- 4 Results for  $K \rightarrow \pi\nu\bar{\nu}$

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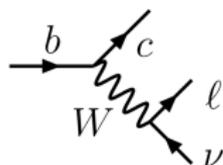
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# B-physics anomalies

SM  $\sim$  respects LFU (Lepton Flavor Universality)  $\Rightarrow R_X^{q_{\ell\ell}^2 \gg m_\ell^2} \simeq 1$

[talks by (exp) Lucio Martinez, Franco Lima, Urquijo, Patel; (theo) Matias, Neshatpour, Valli, Hurth]

## Charged Currents



$$R_{D^{(*)}} = \frac{\mathcal{B}(B^0 \rightarrow D^{(*)-} \tau^+ \nu)}{\mathcal{B}(B^0 \rightarrow D^{(*)-} (e^+, \mu^+) \nu)}$$

[BaBar, Belle; BaBar, Belle, LHCb]

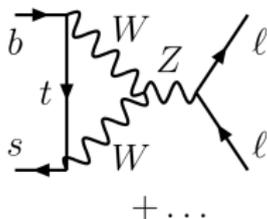
$\sim 2 - 3.4\sigma$  (w/ SM)

$$R_{J/\psi} = \frac{\mathcal{B}(B_c^+ \rightarrow (J/\psi) \tau^+ \nu)}{\mathcal{B}(B_c^+ \rightarrow (J/\psi) \mu^+ \nu)}$$

[LHCb'17]

$\sim 2\sigma$  (w/ SM)

## Neutral Currents



$$R_{K^{(*)}} = \frac{\mathcal{B}(B \rightarrow K^{(*)} \mu^+ \mu^-)}{\mathcal{B}(B \rightarrow K^{(*)} e^+ e^-)}$$

[BaBar, Belle, LHCb; LHCb'17]

$\sim 2.1 - 2.6\sigma$  (w/ SM)

BRs and angular obs.  
in  $b \rightarrow s \mu^+ \mu^-$

[LHCb, Belle, ATLAS, CMS]

$\sim 2.2 - 2.9\sigma$  (w/ SM)

Pattern of deviations w.r.t. the SM  $\rightarrow$  NP LFUV

# Correlation with different flavor sectors

$\Lambda_{NP}^{b \rightarrow c, s} \sim \mathcal{O}(1, 100) \text{ TeV} \Rightarrow$  direct searches,  
low-energy precision observables

GIM suppression and CKM suppression:

$$\mathcal{L}_{\text{eff}} \supset -\frac{1 - 0.3i}{(180 \text{ TeV})^2} (\bar{s}_L \gamma_\mu d_L) (\bar{\nu}_L \gamma^\mu \nu_L) + \text{h.c.}$$

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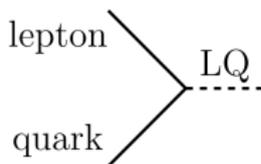
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**HERE:** discuss what can be learned from rare kaon decays  
in some specific NP contexts

LQs: couplings to quarks and leptons  
 $\Rightarrow$  effects in (semi-)leptonic decays,  
suppressed effects in  $B_s^0 - \bar{B}_s^0$

[Bauer+'15, Medeiros V.+'15, Barbieri+'15, Fajfer+'15]



[talks by Stangl, Iyer, T. You, Greljo, Di Luzio, Nardecchia, Fuentes-Martin, Fajfer, Guadagnoli, Jung, Rodriguez Sanchez, Kirk]

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# Experimental overview

## Present experimental bounds

$$\mathcal{B}_{\text{exp}}(K^+ \rightarrow \pi^+ \nu \bar{\nu}) < 3.35 \times 10^{-10} \quad @ \quad 90 \% \text{ CL}$$

[BNL-E787, E949]

$$\mathcal{B}_{\text{exp}}(K_L \rightarrow \pi^0 \nu \bar{\nu}) < 2.6 \times 10^{-8} \quad @ \quad 90 \% \text{ CL}$$

[KEK-E391a]

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[KEK-E391a]

## Near/coming future

NA62/CERN:  $K^\pm \rightarrow \pi^\pm \nu \bar{\nu}$ ; KOTO/J-PARC:  $K_L \rightarrow \pi^0 \nu \bar{\nu}$  (CPV)



$$\mathcal{B}_{\text{exp}}(K^+ \rightarrow \pi^+ \nu \bar{\nu}) < 11 \times 10^{-10} \quad @ \quad 90 \% \text{ CL}$$

[NA62, preliminary]

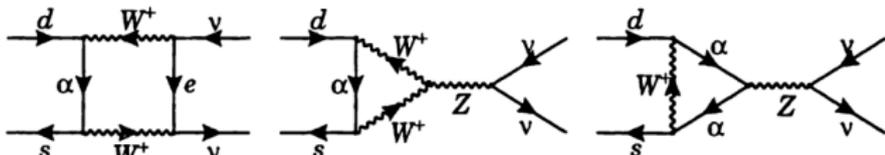
$$\mathcal{B}_{\text{exp}}(K_L \rightarrow \pi^0 \nu \bar{\nu}) < 5.1 \times 10^{-8} \quad @ \quad 90 \% \text{ CL}$$

[KOTO]

NA62 and KOTO: anticipated accuracies of  $\sim 10\%$

# Theoretical overview

[talks by Buras, D'Ambrosio]



$$\mathcal{B}_{SM}(K^+ \rightarrow \pi^+ \nu\bar{\nu}) =$$

$$\kappa_+(1 + \Delta_{QED}) \left[ \left( \frac{\text{Im}[\lambda_t]}{\lambda_{CKM}^5} X_t \right)^2 + \left( \frac{\text{Re}[\lambda_c]}{\lambda_{CKM}} (P_c^{\text{pert}} + \delta P_{c,u}^{\text{non-pert.}}) + \frac{\text{Re}[\lambda_t]}{\lambda_{CKM}^5} X_t \right)^2 \right]$$

$$\mathcal{B}_{SM}(K_L \rightarrow \pi^0 \nu\bar{\nu}) = \kappa_L \left( \frac{\text{Im}[\lambda_t]}{\lambda_{CKM}^5} X_t \right)^2,$$

$$\lambda_q = V_{qs}^* V_{qd}$$

[Buras'98, Buras+'15]

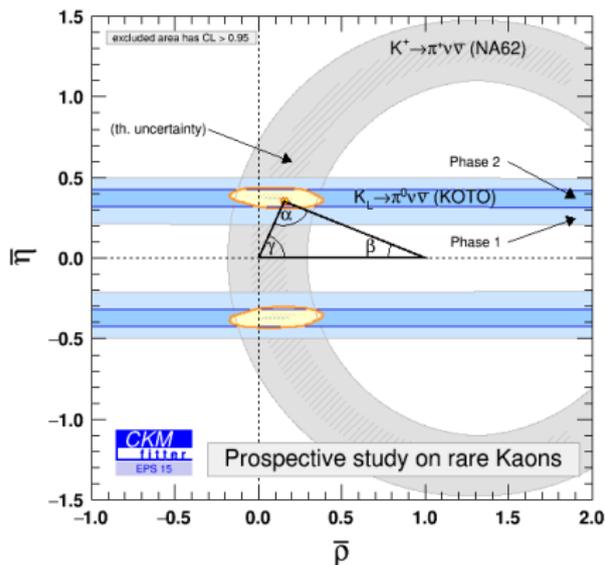
- $\kappa_+, \kappa_L$ , non-pert. inputs: semileptonic kaon decays [Mescia+'07]
- $X_t$ : NLO QCD corrections [Buchalla+'93,'99, Misiak+'99]  
NLO electroweak corrections [Brod+'10]
- $P_c^{\text{pert}}$ : NNLO QCD corrections [Gorbahn+'04, Buras+'05,'06]  
NLO electroweak corrections [Brod+'08]
- $\delta P_{c,u}^{\text{non-pert.}}$  [Isidori+'05]

# Impact on the SM

Main uncertainties:

$\mathcal{B}_{SM}(K^\pm)$	$\mathcal{B}_{SM}(K_L)$
$P_c^{\text{pert.}}$ : 5%	$ V_{ub} $ : 3%
$\delta P_{c,u}^{\text{non. pert.}}$ : 3%	$\gamma$ : 2%
$ V_{cb} $ : 3%	

[CKMfitter, preliminary]



## Theoretical predictions in the SM framework

Global fit extraction of  $|V_{ub}|$ ,  $|V_{cb}|$ ,  $\lambda$ ,  $\gamma$ : [Ocariz, Camacho, Descotes-Genon]

$$\mathcal{B}_{SM}(K^+ \rightarrow \pi^+ \nu \bar{\nu}) = 0.882_{-0.098}^{+0.092} \times 10^{-10} \quad (\sim 10\%) \quad \text{[CKMfitter, preliminary]}$$

$$\mathcal{B}_{SM}(K_L \rightarrow \pi^0 \nu \bar{\nu}) = 0.314_{-0.018}^{+0.017} \times 10^{-10} \quad (\sim 5\%) \quad \text{[CKMfitter, preliminary]}$$

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# Structure of LQ contributions to neutral currents

Measurements:  $R_K/R_K^{SM}$  and  $R_{K^*}/R_{K^*}^{SM} < 1$

Couplings of **scalar** LQs to SM fermions

$SU(3)_C \times SU(2)_L \times U(1)_Y$	down-type quarks	chiral structure	@ tree-level $R_K/R_K^{SM}, R_{K^*}/R_{K^*}^{SM}$
$S_3 = (\bar{\mathbf{3}}, \mathbf{3}, 1/3)$	$\bar{d}_L^c \nu_L, \bar{d}_L^c \ell_L$	$\bar{s} \gamma_\rho P_L b \cdot \bar{\ell} \gamma^\rho P_L \ell$	$< 1, < 1$
$R_2 = (\mathbf{3}, \mathbf{2}, 7/6)$	$\bar{d}_L \ell_R$	$\bar{s} \gamma_\rho P_L b \cdot \bar{\ell} \gamma^\rho P_R \ell$	$\approx 1, \approx 1$
$\tilde{R}_2 = (\mathbf{3}, \mathbf{2}, 1/6)$	$\bar{d}_R \ell_L, \bar{d}_R \nu_L$	$\bar{s} \gamma_\rho P_R b \cdot \bar{\ell} \gamma^\rho P_L \ell$	$< 1, > 1$
$\tilde{S}_1 = (\bar{\mathbf{3}}, \mathbf{1}, 4/3)$	$\bar{d}_R^c \ell_R$	$\bar{s} \gamma_\rho P_R b \cdot \bar{\ell} \gamma^\rho P_R \ell$	$\approx 1, \approx 1$
$S_1 = (\bar{\mathbf{3}}, \mathbf{1}, 1/3)$	$\bar{d}_L^c \nu_L$		$= 1, = 1$

(w/  $\nu_R$ , also  $\bar{S}_1 = (\bar{\mathbf{3}}, \mathbf{1}, -2/3)$ , and new couplings of  $\tilde{R}_2, S_1$ )

→ **Tree-level:**  $S_3$

→ Transition  $s \rightarrow d \nu \bar{\nu}$  @ tree-level:  $S_3, \tilde{R}_2, S_1$

# LQ contributions to neutral currents

- Loop-level: other LQs can also imply  $R_K/R_K^{SM}, R_{K^*}/R_{K^*}^{SM} < 1$   
 $S_3, R_2, S_1$  [Bauer+'15, Bečirević+'16]
- Sacrifices “elegance” of semi-leptonic effects w/ LQs,  
 but follows structure of the SM
- Conversely, it may require large couplings

# Specific LQ models

→ In the following, we consider and compare:

- a  $S_3$  model (“Triplet model”) [Doršner+’17]

- a  $R_2$  model (“Doublet model”) [Bečirević+’16]

→ **Substantial differences:**  $b \rightarrow s\ell\ell$  at different orders

→ Vector LQs: **renormalizability** requires larger spectrum

[cf. talk by Di Luzio]

[Barbieri+’15’16, Buttazzo+’17, Greljo+’17, Fajfer+’16, Bordone+’17]

→ In the following, focus on correlations w/  $b \rightarrow s\ell\bar{\ell}$ , and  $b \rightarrow s\nu\bar{\nu}$

## $R_2$ model: features

Interactions with SM fermions:

$$\mathcal{L}_{R_2}^Y = (V_{CKM} \times g_R)_{ij} \bar{u}^i P_R e^j R_2^{5/3} + (g_R)_{ij} \bar{d}^i P_R e^j R_2^{2/3} \\ + (g_L)_{ij} \bar{u}^i P_L \nu^j R_2^{2/3} - (g_L)_{ij} \bar{u}^i P_L e^j R_2^{5/3} + \text{h.c.}$$

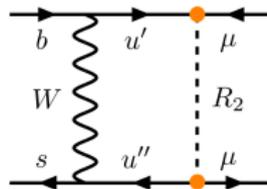
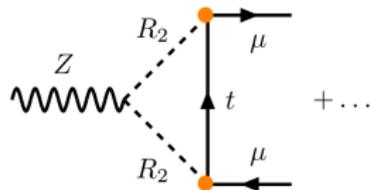
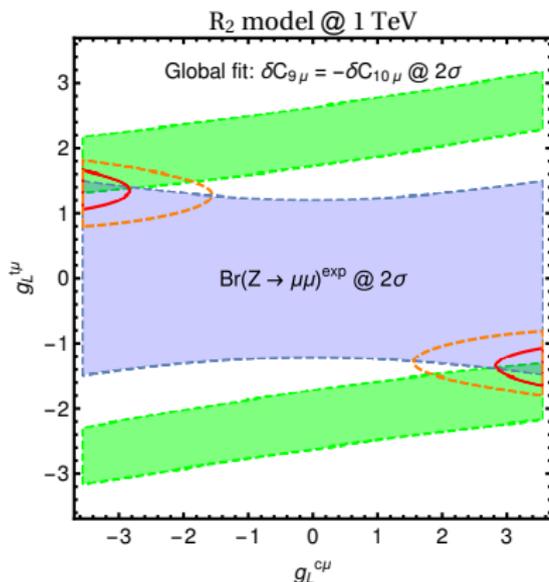
$$g_R = 0_{3 \times 3}, \quad g_L = \begin{pmatrix} 0 & 0 & 0 \\ 0 & g_L^{c\mu} & g_L^{c\tau} \\ 0 & g_L^{t\mu} & g_L^{t\tau} \end{pmatrix}, \quad m_{R_2}$$

[Bečirević+'17]

- Avoid **tree-level contributions** to  $B$ -decays w/ the *wrong* chirality
- $R_{D^{(*)}}$  not addressed ( $g_R^{b\tau} \neq 0$  strongly constrained)
- Consistently avoid first generation couplings
- **No tree-level** contribution to  $s \rightarrow d\nu\bar{\nu}$

# $R_2$ model: phenomenology

- $g_L^{c\tau} \approx 0$ ,  $g_L^{t\tau} \approx 0$  for large  $g_L^{c\mu}$ ,  $g_L^{t\mu}$  due to  $\tau \rightarrow \mu\gamma$



[Bečirević+'17]

- $(g - 2)_\mu$  worsen by  $\gtrsim 1\sigma$  (for  $g_L^{c\mu}$ ,  $g_L^{t\mu} < \sqrt{4\pi}$ )
- Collider bounds:  $m_{R_2} \gtrsim 650$  GeV (assuming  $t\nu$ ,  $t\tau$  dominate)

# $S_3$ model: features

Interactions with SM fermions:

$$\mathcal{L}_{S_3}^Y \equiv -y_{ij} \bar{d}_L^{Ci} \nu_L^j S_3^{1/3} - (V_{CKM}^* \times y)_{ij} \bar{u}_L^{Ci} e_L^j S_3^{1/3} \\ - \sqrt{2} y_{ij} \bar{d}_L^{Ci} e_L^j S_3^{4/3} + \sqrt{2} (V_{CKM}^* \times y)_{ij} \bar{u}_L^{Ci} \nu_L^j S_3^{-2/3} + \text{h.c.}$$

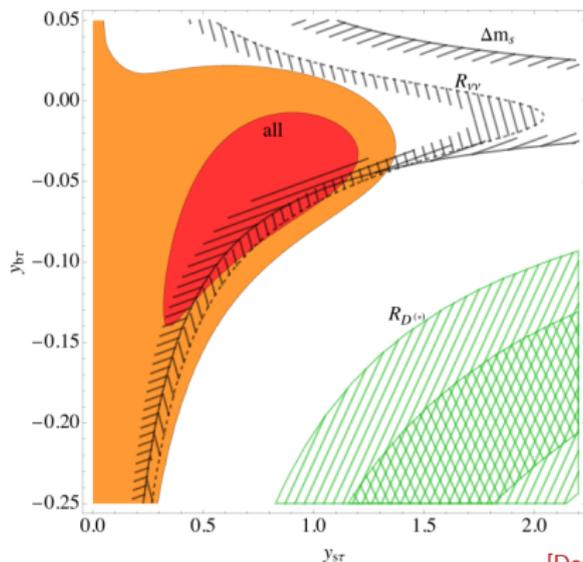
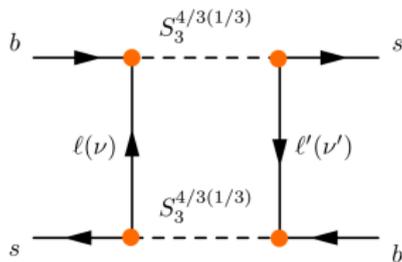
$$y = \begin{pmatrix} 0 & 0 & 0 \\ 0 & y_{s\mu} & y_{s\tau} \\ 0 & y_{b\mu} & y_{b\tau} \end{pmatrix}, \quad V_{CKM}^* \times y \approx \begin{pmatrix} 0 & \lambda y_{s\mu} & \lambda y_{s\tau} \\ 0 & y_{s\mu} & y_{s\tau} \\ 0 & y_{b\mu} & y_{b\tau} \end{pmatrix}, \quad m_{S_3}$$

[Doršner+'17]

- Chiral LQ, one single coupling matrix
- With the **choice**  $y_{d\mu} = \mathbf{0} \Rightarrow$  **no**  $s \rightarrow d\nu\bar{\nu}$  @ tree-level

# $S_3$ model: phenomenology

$b \rightarrow s\mu^+\mu^-$ ,  $b \rightarrow s\nu_{\mu,\tau}\bar{\nu}_{\mu,\tau}$   
at the tree-level



[Doršner+'17]

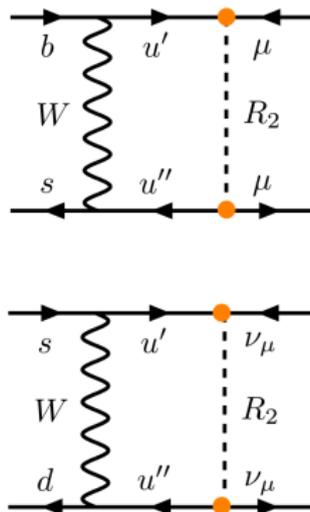
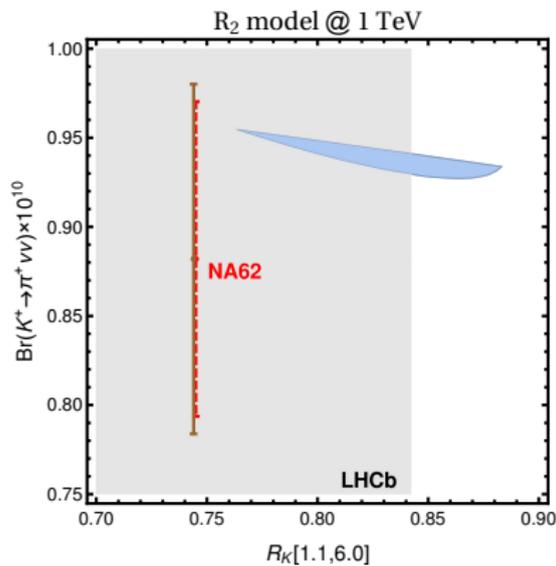
- $R_{\nu\nu}^{(*)} = \frac{\mathcal{B}(B \rightarrow K^{(*)}\nu\bar{\nu})}{\mathcal{B}(B \rightarrow K^{(*)}\nu\bar{\nu})_{SM}}$ ,  $\Delta m_s(B_s^0\bar{B}_s^0)$
- $R_{D^{(*)}}$  not accommodated
- Collider bounds on LQ pair and  $\tau\tau$  production satisfied

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# Results for the $R_2$ model

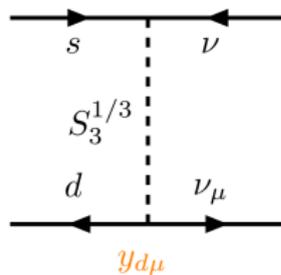
Effects induced by muon couplings:  $\{g_L^{c\mu}, g_L^{t\mu}\}_{1\sigma}$



Max. enhancement of **9%** for  $K^\pm \rightarrow \pi^\pm \nu \bar{\nu}$  and **5%** for  $K_L \rightarrow \pi^0 \nu \bar{\nu}$

Results for the  $S_3$  model +  $y_{d\mu}$ 

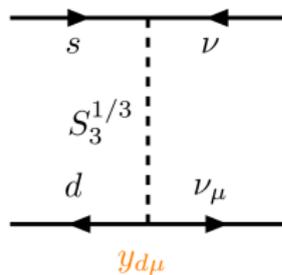
$$y = \begin{pmatrix} 0 & y_{d\mu} & 0 \\ 0 & y_{s\mu} & y_{s\tau} \\ 0 & y_{b\mu} & y_{b\tau} \end{pmatrix}$$



- Relax the initial requirement of  $y_{d\mu} = 0$  (here, real)

Results for the  $S_3$  model +  $y_{d\mu}$ 

$$y = \begin{pmatrix} 0 & y_{d\mu} & 0 \\ 0 & y_{s\mu} & y_{s\tau} \\ 0 & y_{b\mu} & y_{b\tau} \end{pmatrix}$$

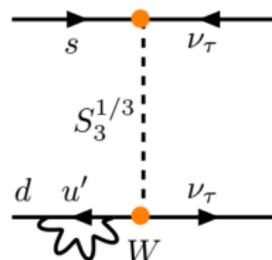
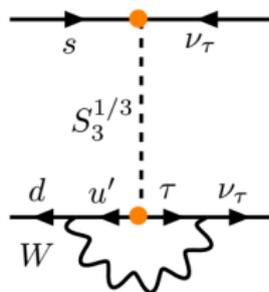
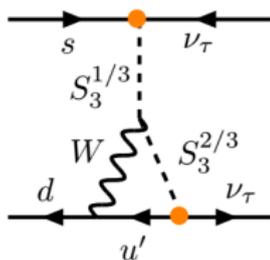


- Relax the initial requirement of  $y_{d\mu} = 0$  (here, real)
- The experimental bound of  $K^\pm \rightarrow \pi^\pm \nu \bar{\nu}$  sets  $|y_{d\mu}| \lesssim 3 \times 10^{-4}$
- Much stronger than the **LNV**  $\tau \rightarrow \mu + K_S^0$  [Davidson+'10]

Results for the  $S_3$  model

- SM:  $|V_{td} V_{ts}| \sim \lambda^5$
- $1/\lambda^2$  enhancement

(NP: vertex)  
gauge-inv.  
combination

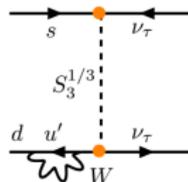
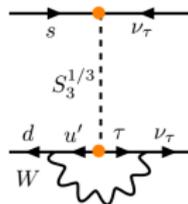
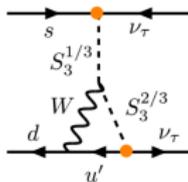
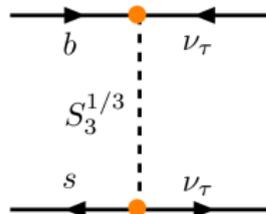
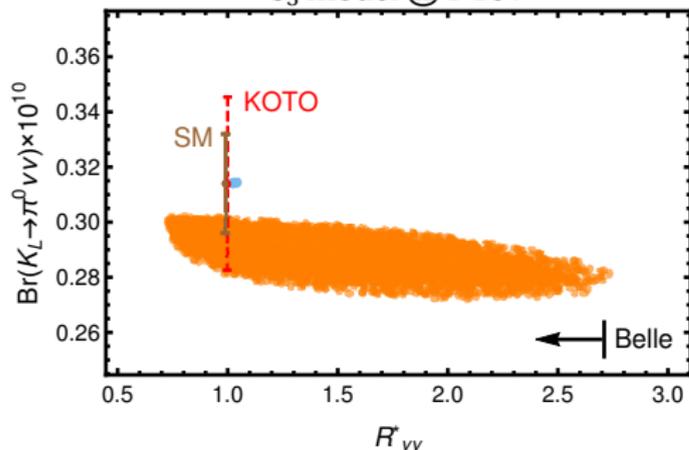


	$c$	$t$	$cc$	$ct, tc$	$tt$
(SM)	$g^4 \lambda$	$g^4 \lambda^5$			
(NP: vertex)	$g^2 \lambda y_{sT}^2$	$g^2 \lambda^3 y_{sT} y_{bT}$			
(NP: Box)			$g^2 \lambda y_{sT}^2$	$g^2 \lambda^3 y_{sT} y_{bT}$	$g^2 \lambda^5 y_{bT}^2$

Results for the  $S_3$  model,  $y_{d\mu}^{\text{tree}} = 0$ 

tau couplings:

$$y_{d\tau} \stackrel{1 \text{ TeV}}{=} [(3.8 + 1.5i)y_{b\tau} \rightarrow - (0.16 + 0.06i)y_{s\tau}] \times 10^{-4}$$

 $S_3$  model @ 1 TeV

Max. suppression of **10%** for  $K^\pm \rightarrow \pi^\pm \nu \bar{\nu}$  and **14%** for  $K_L \rightarrow \pi^0 \nu \bar{\nu}$

# Comparison

**Important modulations** ( $\gtrsim$  theo. unc.) also for  $S_1 + S_3$ :  
 suppression of  $\sim 24\%$  for  $K^\pm \rightarrow \pi^\pm \nu \bar{\nu}$ ,  $\sim 34\%$  for  $K_L \rightarrow \pi^0 \nu \bar{\nu}$

[Crivellin+'17]

# Comparison

**Important modulations** ( $\gtrsim$  theo. unc.) also for  $S_1 + S_3$ :  
 suppression of  $\sim 24\%$  for  $K^\pm \rightarrow \pi^\pm \nu \bar{\nu}$ ,  $\sim 34\%$  for  $K_L \rightarrow \pi^0 \nu \bar{\nu}$

[Crivellin+'17]

$(sd)(\ell\ell)$  transitions in the SM: large  $\mathcal{B}(K^\pm \rightarrow \pi^\pm \ell^+ \ell^-)$  points to  
 large long-distance effects from  $K \rightarrow \pi \gamma^*$

→ The SD from NP do not produce large effects to  $(sd)(\ell\ell)$

# Conclusion

- $B$ -physics anomalies: perhaps a true guide for extending the SM
- Need other flavor sectors to shape the SM extension
- **Important exp. progress in the coming years in  $K$ -physics** & theoretically clean observables
- Correlation among different sectors strongly depends on specific NP model: considered scalar LQs here
- Same couplings in  $b \rightarrow s\mu^+\mu^-$  and/or  $b \rightarrow s\nu\bar{\nu}$  also in  $s \rightarrow d\nu\bar{\nu}$  for the models studied beyond the tree level
- Found modulations of  $\sim 10\%$  even for loop contributions

Merci!

# Structure of LQ contributions to neutral currents

## Couplings of **vector** LQs to SM fermions

$SU(3)_C \times SU(2)_L \times U(1)_Y$	down-type quarks	chiral structure	@ tree-level $R_K/R_K^{SM}, R_{K^*}/R_{K^*}^{SM}$
$U_3 = (\mathbf{3}, \mathbf{3}, 2/3)$	$\bar{d}_L \nu_L, \bar{d}_L l_L$	$\bar{s} \gamma_\rho P_L b \cdot \bar{\ell} \gamma^\rho P_L l$	$< 1, < 1$
$V_2 = (\bar{\mathbf{3}}, \mathbf{2}, 5/6)$	$\bar{d}_R^c \nu_L, \bar{d}_R^c l_L,$ $\bar{d}_L^c l_R$	$\bar{s} \gamma_\rho P_R b \cdot \bar{\ell} \gamma^\rho P_L l$ $\bar{s} \gamma_\rho P_L b \cdot \bar{\ell} \gamma^\rho P_R l$	$< 1, > 1$ $\approx 1, \approx 1$
$\tilde{V}_2 = (\bar{\mathbf{3}}, \mathbf{2}, -1/6)$			$= 1, = 1$
$\tilde{U}_1 = (\mathbf{3}, \mathbf{1}, 5/3)$			$= 1, = 1$
$U_1 = (\mathbf{3}, \mathbf{1}, 2/3)$	$\bar{d}_L l_L,$ $\bar{d}_R l_R$	$\bar{s} \gamma_\rho P_L b \cdot \bar{\ell} \gamma^\rho P_L l$ $\bar{s} \gamma_\rho P_R b \cdot \bar{\ell} \gamma^\rho P_R l$	$< 1, < 1$ $\approx 1, \approx 1$

(w/  $\nu_R$ , also  $\bar{U}_1, = (\mathbf{3}, \mathbf{1}, -1/3)$ , and new couplings of  $\tilde{V}_2$ )

## Couplings of scalar LQs to SM fermions

LQs	Structures of the couplings	
	down-type	up-type
$S_3 = (\bar{\mathbf{3}}, \mathbf{3}, 1/3)$	$\bar{d}_L^c \nu_L, \bar{d}_L^c l_L,$	$\bar{u}_L^c \nu_L, \bar{u}_L^c l_L$
$R_2 = (\mathbf{3}, \mathbf{2}, 7/6)$	$\bar{d}_L l_R,$	$\bar{u}_L l_R, \bar{u}_R l_L, \bar{u}_R \nu_L$
$\tilde{R}_2 = (\mathbf{3}, \mathbf{2}, 1/6)$	$\bar{d}_R l_L, \bar{d}_R \nu_L$	
$\tilde{S}_1 = (\bar{\mathbf{3}}, \mathbf{1}, 4/3)$	$\bar{d}_R^c l_R$	
$S_1 = (\bar{\mathbf{3}}, \mathbf{1}, 1/3)$	$\bar{d}_L^c \nu_L,$	$\bar{u}_L^c l_L, \bar{u}_R^c l_R$

## Couplings of vector LQs to SM fermions

LQs	Structures of the couplings	
	down-type	up-type
$U_3 = (\mathbf{3}, \mathbf{3}, 2/3)$	$\bar{d}_L \nu_L, \bar{d}_L \ell_L,$	$\bar{u}_L \nu_L, \bar{u}_L \ell_L$
$V_2 = (\bar{\mathbf{3}}, \mathbf{2}, 5/6)$	$\bar{d}_R^c \nu_L, \bar{d}_R^c \ell_L, \bar{d}_L^c \ell_R,$	$\bar{u}_L^c \ell_R$
$\tilde{V}_2 = (\bar{\mathbf{3}}, \mathbf{2}, -1/6)$		$\bar{u}_R^c \ell_L, \bar{u}_R^c \nu_L$
$\tilde{U}_1 = (\mathbf{3}, \mathbf{1}, 5/3)$		$\bar{u}_R \ell_R$
$U_1 = (\mathbf{3}, \mathbf{1}, 2/3)$	$\bar{d}_L \ell_L, \bar{d}_R \ell_R,$	$\bar{u}_L \nu_L$