# Scalar Leptoquarks and B anomalies

Svjetlana Fajfer



Physics Department, University of Ljubljana and Institute J. Stefan, Ljubljana, Slovenia





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Experimental status: of - B anomalies  $R_{D(*)}$  and  $R_{K(*)}$ 

Effective Lagrangian approach:  $R_{D(*)}$  and  $R_{K(*)}$ 

Scalar Leptoquarks solution of  $R_{D(*)}$  and  $R_{K(*)}$ 

Flavour constraints on LQs

Interpretation: sign of LFU violation?



Signature at LHC

B physics anomalies: experimental results ≠ SM predictions!

charged current (SM tree level)

$$R_{D^{(*)}} = \frac{BR(B \to D^{(*)} \tau \nu_{\tau})}{BR(B \to D^{(*)} \mu \nu_{\mu})}$$
 3.9σ



$$\frac{BR(B_c \to J/\Psi \mu \nu_{\tau})}{BR(B_c \to J/\Psi \mu \nu_{\mu})} = 0.71 \pm 0.17 \pm 0.18$$

2017 ~2 σ LHCb result





Effective Lagrangian approach for  $b \to c \tau \nu_{\tau} decay$ 



If NP scale is above electroweak scale, NP effective operators have to respect  $SU(3) \times SU(2)_{L} \times U(1)_{Y}$ 

$$\mathcal{H}_{eff} = \frac{4G_F}{\sqrt{2}} V_{cb} \bar{c} \gamma_{\mu} P_L b , \bar{\nu} \gamma^{\mu} P_L \tau + \frac{1}{\Lambda} \Sigma_i c_i O_i$$

$$(\bar{c} \gamma_{\mu} P_L b) (\bar{\tau} \gamma^{\mu} P_L \nu)$$

$$(\bar{c} \gamma_{\mu} P_R b) (\bar{\tau} \gamma^{\mu} P_L \nu)$$

$$(\bar{c} P_R b) (\bar{\tau} P_L \nu)$$

$$(\bar{c} P_L b) (\bar{\tau} P_L \nu)$$

$$(\bar{c} \sigma^{\mu\nu} P_L b) (\bar{\tau} \sigma_{\mu\nu} P_L \nu)$$

$$\text{ no } \nu_R$$

P<sub>5</sub>' in  $B \to K^* \mu^+ \mu^-$  (angular distribution functions) 3 $\sigma$ 

$$R_{K} = \frac{\mathcal{B}(B \to K\mu\mu)_{q^{2} \in [1,6] \text{GeV}^{2}}}{\mathcal{B}(B \to Kee)_{q^{2} \in [1,6] \text{GeV}^{2}}} = 0.745 \pm_{0.074}^{0.090} \pm 0.036$$

$$R_{K^{*}}^{\text{low}} = \frac{\mathcal{B}(B \to K\mu\mu)_{q^{2} \in [0.045, 1.1] \text{GeV}^{2}}}{\mathcal{B}(B \to Kee)_{q^{2} \in [0.045, 1.1] \text{GeV}^{2}}} = 0.660 \pm_{0.070}^{0.110} \pm 0.024$$

$$R_{K^{*}}^{\text{central}} = \frac{\mathcal{B}(B \to K\mu\mu)_{q^{2} \in [1.1,6] \text{GeV}^{2}}}{\mathcal{B}(B \to Kee)_{q^{2} \in [1.1,6] \text{GeV}^{2}}} = 0.685 \pm_{0.069}^{0.113} \pm 0.047,$$

$$2.2 \,\sigma - 2.4 \sigma$$

 $R_{\kappa}$  and  $R_{\kappa^*}$  and New Physics

$$\begin{aligned} \mathcal{H}_{\text{eff}} &= -\frac{4G_F}{\sqrt{2}} V_{tb} V_{ts}^* \left[ \sum_{i=1}^6 C_i(\mu) \mathcal{O}_i(\mu) + \sum_{i=7,\dots,10} \left( C_i(\mu) \mathcal{O}_i(\mu) + C_i'(\mu) \mathcal{O}_i'(\mu) \right) \right] \\ \mathcal{O}_9 &= \frac{e^2}{g^2} (\bar{s} \gamma_\mu P_L b) (\bar{\ell} \gamma^\mu \ell) \,, \qquad \mathcal{O}_{10} = \frac{e^2}{g^2} (\bar{s} \gamma_\mu P_L b) (\bar{\ell} \gamma^\mu \gamma_5 \ell) \end{aligned}$$

Global analysis suggests no NP in

$$C_9^{\mu} = -C_{10}^{\mu} = -0.64$$
  
 $C_9^{\mu} = -C_{10}^{\mu} \in (-0.85, -0.50)$ 

Capdevila et al., 1704.05340 Similar result obtained by Altmannshofer et al, 1704.05435



How to approach to anomalies?

• Is the anomaly SM or NP?

• First step at low energies: to construct effective Lagrangian which might explain experimental data;

• Find new particle which can mimic effective Lagrangian; Check all other low energy flavour constraints, check electroweak observables, include LHC direct searches for NP;

• Make consistent model of NP!

## Effective Lagrangian approach: NP in third generation

Feruglio, Paradisi, Pattori, 1606.00524; Battacharaya et al., 1412.7164; Glashow, Guadagnoli and Lane, 1411.0565 NP couples preferentially to third generation.

$$\mathcal{L}_{\rm NP} = \frac{C_1}{\Lambda^2} \left( \bar{q}_{3L} \gamma^{\mu} q_{3L} \right) \left( \bar{\ell}_{3L} \gamma_{\mu} \ell_{3L} \right) + \frac{C_3}{\Lambda^2} \left( \bar{q}_{3L} \gamma^{\mu} \tau^a q_{3L} \right) \left( \bar{\ell}_{3L} \gamma_{\mu} \tau^a \ell_{3L} \right)$$

Paradigm: only one new mediator leading to such effective Lagrangian!

Spin	Color singlet	Color tripet
0	2HDM	Scalar LQ P parity - sbottom
1	W' ,Z'	Vector LQ





1) 1974 Salam & Pati: partial unification of quark and leptons –four color charges, left-right symmetry;

2) GUT models contain them as gauge bosons (e.g. Georgi-Glashow 1974);

3) Within GUT they can be scalars too;

4) 1997 false signal et DESY (~200 GeV);

5) In recent years LQ might offer explanations of B physics anomalies;

6) LHC has bounds on the masses of  $LQ_1, LQ_2, LQ_3$  of the order ~ 1 TeV.

Leptoquarks in  $R_{K}$  and  $R_{D(*)}$ 

# Suggested by many authors: naturally accomodate LUV and LFV

color SU(3), weak isospin SU(2) , weak hypercharge U(1)

 $Q=I_3 + Y$ 

S	$U(3) \times SU(2) \times U(1)$	Spin	Symbol	Type	3B + L
	$(\overline{3},3,1/3)$	0	$S_3$	$LL\left(S_{1}^{L} ight)$	-2
	$({f 3},{f 2},7/6)$	0	$R_2$	$RL(S_{1/2}^{L}), LR(S_{1/2}^{\bar{R}})$	0
L	$({f 3},{f 2},1/6)$	0	$\tilde{R}_2$	$RL(\tilde{S}_{1/2}^L), \ \overline{LR}$	0
	$(\overline{3},1,4/3)$	0	$ ilde{S}_1$	$RR( ilde{S}_0^R)$	-2
	$(\overline{f 3}, {f 1}, 1/3)$	0	$S_1$	$LL\left(S_{0}^{L} ight),RR\left(S_{0}^{R} ight),\overline{RR}$	-2
	$(\overline{3},1,-2/3)$	0	$ar{S}_1$	$\overline{RR}$	-2
	$({f 3},{f 3},2/3)$	1	$U_3$	$LL\left(V_{1}^{L} ight)$	0
	$({f \overline{3}},{f 2},5/6)$	1	$V_2$	$RL(V_{1/2}^{L}), LR(V_{1/2}^{R})$	-2
	$(\overline{3}, 2, -1/6)$	1	$ ilde{V}_2$	$RL(\tilde{V}_{1/2}^L), \ \overline{LR}$	-2
Γ	$({f 3},{f 1},5/3)$	1	$U_1$	$RR(V_0^R)$	0
	$({f 3},{f 1},2/3)$	1	$U_1$	$LL(V_0^L), RR(V_0^R), \overline{RR}$	0
	$({\bf 3},{\bf 1},-1/3)$	1	$ar{U}_1$	$\overline{RR}$	0

F=3B +L fermion number; F=0 no proton decay at tree level (see Assad et al, 1708.06350)

Doršner, SF, Greljo, Kamenik Košnik, (1603.04993)



Helps to know: according to Asad, Fornal Grinstein 1708.06350; proton decay at tree cannot be mediated by U(3,1,2/3).

If vector LQ is not a gauge boson – difficult to handle!

Possible to make Pati-Salam-like unified model vector LQ- gauge boson!: Di Luzio, Greljo, Nardecchia, 1708.08450; Bordone et al, 1712.01368; Callibi, Crivellin, Li, 1709.00692, Marzocca, 1803.10972. Admir's talk!

One scalar Leptoqaurk resolving both B anomalies:

(3,2,1/6)Tree level solutions for  $R_{D(*)}$  and  $R_{K(*)}$ 

Right-handed neutrino introduced LQ (3,2,1/6)

 $|M_{SM}|^2 + |M_{LQ}|^2$  Becirevic et al, 1608.08501 passes all flavor constraints, but leads to R\_{\rm K\*}>1!



# Two LQs solution of $R_{D(*)}$ and $R_{K(*)}$

(3,3,1/3) + (3,1,-1/3) Crivellin et al, 1703.09226, Marzocca, 1803.10972.

$$\nu$$

$$b$$

$$\overline{\Phi_1 + \Phi_3}$$

$$c$$

$$b$$

$$\overline{\Phi_1 - \Phi_3}$$

$$s$$

$$b$$

$$\overline{\Phi_1 - \Phi_3}$$

$$s$$

$$b$$

$$\overline{\Phi_3}$$

$$s$$

- (3,3,1/3) alone has a proper structure according to effective Lagrangian it couples to only left-handed quarks and leptons.
- it leads to to large contribution in  $B o K^{(*)} 
  u ar{
  u}$

Buttazzo, Greljo, Isidori, Marzocca 1706.07808 :

$$C_S = -C_1 - 3C_3$$
,  $C_T = C_1 - C_3$ 

radiative corrections to Z → ττ,νν
 observables are enhanced by the factor of 3, implying a ~ 1.5σ tension in R<sub>D(\*)</sub>;

Potentially large sµ coupling disfavored by Ds/K  $\longrightarrow$ µv





Leptoquarks are natural within GUT theories!



 $\tilde{R}_2$ 

d

- GUT possible with light scalar LQs within SU(5) if there are 2 LQs (Doršner, SF, Greljo, Kamenik, Košnik 1603.04993) ;
- LQ S<sub>3</sub>, if accommodated within SU(5) does not cause proton decay, Doršner, SF, Faroughy, Košnik 1706.07779;
- Neutrino masses might be explained with 2 light LQs within a foop (Doršner, SF, Košnik, 1701.08322);

## New Proposal: Two Leptoquarks

D. Becirevic, I. Dorsner, , S. F, D. Faroughy, N. Kosnik and O. Sumensari 1804.xxxxx

Not complete V-A picture of NP!

Scalar LQ better than Vector LQ – simpler UV completion;

 $R_2 = (3,2,7/6)$  contains two states with electric charges 5/3 and 2/3.

$$\begin{aligned} \mathcal{L}_{R_2} &= (Vy_R)^{ij} \, \bar{u}_{Li} \ell_{Rj} R_2^{(5/3)} + y_R^{ij} \, \bar{d}_{Ri} \ell_{Rj} R_2^{(2/3)} & \text{Flavour basis!} \\ &+ (y_L U)^{ij} \, \bar{u}_{Ri} \nu_{Lj} R_2^{(2/3)} - y_L^{ij} \, \bar{u}_{Ri} \ell_{Lj} R_2^{(5/3)} + \text{h.c.} \\ \mathbf{S}_3 &= (\mathbf{\bar{3}}, \mathbf{3}, \mathbf{1}/\mathbf{3}) \text{ contains three states with electric charges } S_3^{2/3}, S_3^{-1/3}, S_3^{-4/3} \end{aligned}$$

$$\mathcal{L}_{S_3} = y^{ij} \, \bar{Q}_i^C i \tau_2 (\vec{\tau} \cdot \vec{S}_3) L_j + \text{h.c.}$$

#### Mass eigenstate basis:

$$\mathcal{L}_{R_{2}\&S_{3}} = + (V_{\text{CKM}} y_{R} E_{R}^{\dagger})^{ij} \bar{u}_{Li}' \ell_{Rj}' R_{2}^{(5/3)} + (y_{R} E_{R}^{\dagger})^{ij} \bar{d}_{Li}' \ell_{Rj}' R_{2}^{(2/3)} + (U_{R} y_{L} U_{\text{PMNS}})^{ij} \bar{u}_{Ri}' \nu_{Lj}' R_{2}^{(2/3)} - (U_{R} y_{L})^{ij} \bar{u}_{Ri}' \ell_{Lj}' R_{2}^{(5/3)} - (y U_{\text{PMNS}})^{ij} \bar{d}_{Li}' \nu_{Lj}' S_{3}^{(1/3)} - \sqrt{2} y^{ij} \bar{d}_{Li}' \ell_{Lj}' S_{3}^{(4/3)} + \sqrt{2} (V_{\text{CKM}}^{*} y U_{\text{PMNS}})_{ij} \bar{u}_{Li}' \nu_{Lj}' S_{3}^{(-2/3)} - (V_{\text{CKM}}^{*} y)_{ij} \bar{u}_{Li}' \ell_{Lj}' S_{3}^{(1/3)} + \text{h.c.} u_{L,R}' = U_{L,R} u_{L,R}, \ d_{L,R}' = D_{L,R} d_{L,R}, \ \ell_{L,R}' = E_{L,R} \ell_{L,R}, \ \nu_{L}' = N_{L} \nu_{L} V_{\text{CKM}} = U_{L} D_{L}^{\dagger} \qquad U_{\text{PMNS}} \equiv E_{L} N_{L}^{\dagger}$$

We assume following:  $y_R = y_R^T$   $y = -y_L$  from SU(5) GUT

Appealing feature: the same coupling for S<sub>3</sub> and R<sub>2</sub>

$$y_R E_R^{\dagger} = \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & y_R^{b\tau} \end{pmatrix}, \ U_R y_L = \begin{pmatrix} 0 & 0 & 0 \\ 0 & y_L^{c\mu} & y_L^{c\tau} \\ 0 & 0 & 0 \end{pmatrix}, \ U_R = \begin{pmatrix} 1 & 0 & 0 \\ 0 & \cos\theta & -\sin\theta \\ 0 & \sin\theta & \cos\theta \end{pmatrix}$$

Parameters:  $m_{R_2}$ ,  $m_{S_3}$ ,  $y_R^{b au}$ ,  $y_L^{c\mu}$ ,  $y_L^{c au}$  and heta

Phenomenology suggest  $\theta \approx \pi/2$  and  $y_R$  complex!

# Explaining $R_{K(*)}$

$$R_{K(*)}(exp) < R_{K(*)}(SM)$$

# Explaining $R_{D(*)}$

Not V-A explanation: T and S from R<sub>2</sub> very small contribution from S<sub>3</sub>

$$\mathcal{L}_{\text{eff}} = -\frac{4 G_F}{\sqrt{2}} V_{cb} \left[ (1 + g_V) (\bar{u}_L \gamma_\mu d_L) (\bar{\ell}_L \gamma^\mu \nu_L) + g_S(\mu) (\bar{u}_R d_L) (\bar{\ell}_R \nu_L) \right. \\ \left. + g_T(\mu) (\bar{u}_R \sigma_{\mu\nu} d_L) (\bar{\ell}_R \sigma^{\mu\nu} \nu_L) \right] + \text{h.c.}$$

$$g_{S} = 4 g_{T} = \frac{y_{L}^{u\ell'} (y_{R}^{d\ell})^{*}}{4\sqrt{2} m_{R_{2}}^{2} G_{F} V_{ud}} \bigg|_{\mu = m_{R_{2}}} \qquad g_{V} = -\frac{y_{d\ell'} (Vy^{*})_{u\ell}}{4\sqrt{2} m_{S_{3}}^{2} G_{F} V_{ud}}$$

$${
m S_3creates}\,{
m g_v}\,\,S_3^{-2/3}$$

# Important constraints

Tree level constraints

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$$R_{e/\mu}^{K \text{ exp}} = 2.488(10) \times 10^{-5}$$

$$R_{e/\mu}^{K} = \frac{\Gamma(K^{-} \to e^{-}\bar{\nu})}{\Gamma(K^{-} \to \mu^{-}\bar{\nu})} \qquad R_{e/\mu}^{K \text{ SM}} = 2.477(1) \times 10^{-5}$$

$$R_{\mu/e}^{D^{(*)}} = \frac{\Gamma(B \to D^{(*)}\mu\bar{\nu})}{\Gamma(B \to D^{(*)}e\bar{\nu})} \qquad \text{PDG} \qquad R_{\mu/e}^{D \text{ exp}} = 0.995(45)$$

$$\mathcal{B}(\tau \to \mu\phi) < 8.4 \times 10^{-8} \qquad R_{\mu/e}^{D^{*} \text{ exp}} = 1.04(5)$$

$$\text{Loop constraints} \qquad \qquad \Delta m_{B_{s}}^{\text{exp}} = 17.7(2) \text{ ps}^{-1} \qquad (19.0 \pm 2.4) \text{ ps}^{-1}$$

$$Z \to \mu\mu, Z \to \tau\tau, Z \to \nu\nu$$

$$R_{\mu/e}^{\mu} = 0.995(45)$$

$$R_{\mu/e}^{D^{*} \text{ exp}} = 1.04(5)$$

$$\frac{g_V^{\tau}}{g_V^e} = 0.959(29), \frac{g_A^{\tau}}{g_A^e} = 1.0019(15) \qquad \frac{g_V^{\mu}}{g_V^e} = 0.961(61), \frac{g_A^{\mu}}{g_A^e} = 1.0001(13)$$
$$N_{\nu}^{\exp} = 2.9840(82)$$

#### **Results and Predictions**



$$+ g_T(\mu) \left( \bar{u}_R \sigma_{\mu\nu} d_L \right) \left( \bar{\ell}_R \sigma^{\mu\nu} \nu_L \right) \Big]$$

$$(\mu = m_{\Delta}) = 4 g_T(\mu = m_{\Delta}) = \frac{y_L^{u\ell'} (y_R^{d\ell})^*}{4\sqrt{2} m_{R_2}^2 G_F V_{ud}},$$
$$g_V = -\frac{y_{d\ell'} (Vy^*)_{u\ell}}{4\sqrt{2} m_{S_3}^2 G_F V_{ud}},$$

For  $\operatorname{Re}[g_S^{\tau}] = 0$  we get  $\operatorname{Im}[g_S^{\tau}]| = 0.59^{+0.13(+0.20)}_{-0.14(-0.29)}$ 

#### Constraints



 $R_{\nu\nu} = B(B \rightarrow K \nu \nu)/B(B \rightarrow K \nu \nu)^{SM}$ 

## Predictions



Increase of  $\mathcal{B}(B\to K\nu\bar{\nu})$  by  $\gtrsim 50\%$  in comparison with SM value

Upper and lower bounds on the LFV rates:  $B(B \rightarrow K\mu\tau) \ge 2 \times 10^{-7}$ Becirevic et al, 1608.07583





$$\mathcal{B}(B_c \to \tau \nu) < 30\%$$

Alonso, Grinstein, Camalich, 1611.06676

new FF estimate QCDSR + latt (Becirevic et al., 2018)

 $R_{J/\psi} > R_{J/\psi}^{SM}$ 

LHC constraints on LQ couplings

Processes in t-channel  $~pp 
ightarrow au^+ au^-$ 



Flavour anomalies generate s  $\tau$ , b $\tau$  and c $\tau$  relatively large couplings. s quark pdf function for protons are ~ 3 times lagrer contribution then for b quark.

Light LQ  $\rightarrow$  impact on the shape of pp  $\rightarrow$  II distributions (Faroughy, Greljo and Kamenik, 1609.07138, Greljo and Marzocca, 1704.09015)

- Recast Atlas searches for  $pp \rightarrow (Z' \rightarrow)\tau\tau$  leads to bounds on  $R_2$  and (weak) ones on  $S_3$  for our  $\theta \approx \pi/2$
- $pp \rightarrow \mu\mu$  not very useful to us, but LQ pair-production data are
- Experimental bounds with 3.2 fb<sup>-1</sup> result in constraints not competitive with those obtained from flavor data. Projecting to 100 fb<sup>-1</sup>:



## Direct searches (projections to 100 fb<sup>-1</sup>)



# Light Leptoquarks in SU(5) GUT

- Scalars:  $R_2 \in 45$ , 50,  $S_3 \in 45$ . SM matter fields in  $5_i$  and  $10_i$ ;
- $R_2$  does not have diquark couplings no proton decay. Operators  $10_i 10_j 45$ Might lead to proton decay (Dorsner, SF, Kosnik, 1701.08322).

Available operators

$$\begin{aligned} \mathbf{10}_{i}\mathbf{5}_{j}\underline{45} &: \quad y_{2\ ij}^{RL}\overline{u}_{R}^{i}R_{2}^{a}\varepsilon^{ab}L_{L}^{j,b}, \quad y_{3ij}^{LL}\overline{Q^{c}}_{L}^{i,a}\varepsilon^{ab}(\tau^{k}S_{3}^{k})^{bc}L_{L}^{j,c} \\ \mathbf{10}_{i}\mathbf{10}_{j}\underline{50} &: \quad y_{2\ ij}^{LR}\overline{e}_{R}^{i}R_{2}^{a}*Q_{L}^{j,a} \end{aligned}$$

- by breaking SU(5) to SM the two  $R_2$ 's mix one can be light and the other (very) heavy.
- the Yukawa couplings determined from flavor physics remain perturbative (<  $\sqrt{4\pi}$  ) up to the GUT scale;



Summary



- Building a viable model which accommodates B-physics anomalies and remains consistent with all other measured flavor observables is difficult;
- We propose a minimalistic model with two light (O(1 TeV)) scalar leptoquarks. Model passes all constraints and satisfactorily accommodates B-physics anomalies. ( $g_s$  complex, i.e. one Yukawa must be complex - e.g.  $y^{b\tau}_R$ );
- Model is of "V A" structure in describing b  $\rightarrow$  sll, but it is NOT for b  $\rightarrow$  clv. At  $\mu = m_{R2}$ , effective b  $\rightarrow$  c couplings satisfy  $g_S = -g_P = 4g_T$ ;
- Our model is GUT inspired and allows for unification with only two LQ's. Yukawa couplings remain perturbative after 1-loop running to  $\Lambda_{GUT}$ ;
- Results of the direct LHC searches might soon become relevant constraints too. Opportunities for direct searches at LHC!

# Thanks!



"It doesn't matter how beautiful your theory is, it doesn't matter how smart you are. If it doesn't agree with experiment, it's wrong. "

Richard P. Feynman

# SU(5) GUT with (3,3,1/3) + (3,2,1/6) Doršner, SF, Faroughy, Košnik

- GUT possible with light scalar LQs within SU(5) if there are 2 LQs (Doršner, SF, Greljo, Kamenik, Košnik 1603.04993) ;
- LQ S<sub>3</sub>, if accommodated within SU(5) does not cause proton decay;
- Neutrino masses might be explained with 2 light LQs within a loop (Doršner, SF, Košnik, 1701.08322);



Constraints from flavor observables

 $(g-2)_{\mu}$  $B_c \rightarrow \tau \nu$  $B \to K^{(*)} \nu \bar{\nu}$  $B_{s}^{0} - \bar{B}_{s}^{0}$  $B \to D \mu \nu_{\mu}$  $K \to \mu \nu_{\mu}$  $D_{d,s} \rightarrow \tau, \mu \nu$  $K \to \pi \mu \nu_{\mu}$  $W \to \tau \bar{\nu}, \ \tau \to \ell \bar{\nu} \nu$  $Z \to b\bar{b} \qquad Z \to l^+ l^-$ 

Becirevic et al, 1608.07583, 1608.08501 Alonso et al, 1611.06676,...





 $R_{D(*)}$  is resolved in hatched (2  $\sigma$ ) and doubly hatched (1  $\sigma$ ) regions, the b  $\rightarrow$  sµµ puzzle is resolved in dashed-hatched region at 1  $\sigma$ . Region below the black line with a hatching is in 1  $\sigma$  agreement with Rµ/e. Recent update on SM value of R<sub>D(\*)</sub>

Bigi, Gambino, Schacht 1707.09509

"Luke's theorem does not protect the form factors from  $1/m^2$  corrections, it is therefore natural to expect  $1/m^2$  corrections of order 10-20%, and one cannot exclude that occasionally they can be even larger".

 $A_1(1) = 0.857(41)$  $A_1(1) = 0.906(13)$ 

approach now includes HQET constraints with realistic uncertainties and improves on the CLN parametrization in several ways. Belle: 1608.06931



-0.17(35337)

	Operator		Fierz identity	Allowed Current	$\delta \mathcal{L}_{ ext{int}}$
$\mathcal{O}_{V_L}$	$(\bar{c}\gamma_{\mu}P_{L}b)(\bar{\tau}\gamma^{\mu}P_{L} u)$			$({f 1},{f 3})_0$	$(g_q ar q_L oldsymbol{ au} \gamma^\mu q_L + g_\ell ar \ell_L oldsymbol{ au} \gamma^\mu \ell_L) W_\mu'$
$\mathcal{O}_{V_R}$	$(\bar{c}\gamma_{\mu}P_{R}b)(\bar{\tau}\gamma^{\mu}P_{L} u)$				
$\mathcal{O}_{S_R}$	$\left(ar{c}P_Rb ight)\left(ar{ au}P_L u ight)$				$(\lambda - 1) + \lambda - (1 + \lambda) \overline{a} $
$\mathcal{O}_{S_L}$	$(\bar{c}P_Lb)(\bar{ au}P_L u)$			$(1, 2)_{1/2}$	$(\lambda_d q_L a_R \phi + \lambda_u q_L u_R i \tau_2 \phi' + \lambda_\ell \ell_L e_R \phi)$
$\mathcal{O}_T$	$(\bar{c}\sigma^{\mu\nu}P_Lb)(\bar{\tau}\sigma_{\mu\nu}P_L\nu)$				
$\mathcal{O}'_{\mathcal{V}}$	$(\bar{\tau}\gamma_{\mu}P_{I}b)(\bar{c}\gamma^{\mu}P_{I}\nu)$	$\longleftrightarrow$	Oul	$({f 3},{f 3})_{2/3}$	$\lambda ar q_L oldsymbol{ au} \gamma_\mu \ell_L oldsymbol{U}^\mu$
$\mathbf{v}_{V_L}$	$(\prime \prime \mu \Gamma L \sigma) (\circ \prime \Gamma L \nu)$	· · /	$\mathcal{O}_{V_L}$	(9.1)	$() \overline{z} \rightarrow (l + \tilde{)} \overline{d} \rightarrow (c + ) U^{\mu}$
$\mathcal{O}_{V_R}'$	$(\bar{ au}\gamma_{\mu}P_{R}b)(\bar{c}\gamma^{\mu}P_{L} u)$	$\longleftrightarrow$	$-2\mathcal{O}_{S_R}$	$\langle 0, 1 \rangle_{2/3}$	$(\lambda q_L \gamma_\mu \ell_L + \lambda a_R \gamma_\mu e_R) U'$
$\mathcal{O}_{S_R}'$	$\left(ar{ au}P_Rb ight)\left(ar{c}P_L u ight)$	$\longleftrightarrow$	$-rac{1}{2}\mathcal{O}_{V_R}$		
$\mathcal{O}_{S_L}'$	$\left(ar{ au}P_Lb ight)\left(ar{c}P_L u ight)$	$\longleftrightarrow$	$-\frac{1}{2}\mathcal{O}_{S_L} - \frac{1}{8}\mathcal{O}_T$	$({f 3},{f 2})_{7/6}$	$(\lambda  ar{u}_R \ell_L +  ilde{\lambda}  ar{q}_L i  au_2 e_R) R$
$\mathcal{O}_T'$	$(\bar{\tau}\sigma^{\mu\nu}P_Lb)(\bar{c}\sigma_{\mu\nu}P_L\nu)$	$\longleftrightarrow$	$-6\mathcal{O}_{S_L} + \frac{1}{2}\mathcal{O}_T$		
$\mathcal{O}_{V_L}''$	$(ar{ au}\gamma_{\mu}P_{L}c^{c})(ar{b}^{c}\gamma^{\mu}P_{L} u)$	$\longleftrightarrow$	$-\mathcal{O}_{V_R}$		
$\mathcal{O}_{V_R}''$	$\left( ar{ au} \gamma_{\mu} P_R c^c  ight) \left( ar{b}^c \gamma^{\mu} P_L  u  ight)$	$\longleftrightarrow$	$-2\mathcal{O}_{S_R}$	$(ar{3}, 2)_{5/3}$	$(\lambda  \bar{d}_R^c \gamma_\mu \ell_L + \tilde{\lambda}  \bar{q}_L^c \gamma_\mu e_R) V^\mu$
$\mathcal{O}_{S_R}^{\prime\prime}$	$\left(ar{ au}P_Rc^c ight)\left(ar{b}^cP_L u ight)$	$\longleftrightarrow$	$\frac{1}{2}\mathcal{O}_{V_L}\Big\langle$	$(ar{3},3)_{1/3}$	$\lambdaar{q}_L^c i  au_2 oldsymbol{ au} \ell_L oldsymbol{S}$
$\mathcal{O}_{S_L}^{\prime\prime}$	$\left(ar{ au}P_Lc^c ight)\left(ar{b}^cP_L u ight)$	$\longleftrightarrow$	$-\frac{1}{2}\mathcal{O}_{S_L} + \frac{1}{8}\mathcal{O}_T$	$\Big angle \left. ig angle (ar{f 3}, f 1)_{1/3}  ight.$	$(\lambda  \bar{q}_L^c i \tau_2 \ell_L + \tilde{\lambda}  \bar{u}_R^c e_R) S$
${\cal O}_T''$	$\left  \left( \bar{\tau} \sigma^{\mu\nu} P_L c^c \right) \left( \bar{b}^c \sigma_{\mu\nu} P_L \nu \right) \right.$	$\longleftrightarrow$	$-6\mathcal{O}_{S_L} - \frac{1}{2}\mathcal{O}_T$		

From Freytsis, Ligeti, and Ruderman, arXiv:1506.08896 Comment: neutrino SM-like!