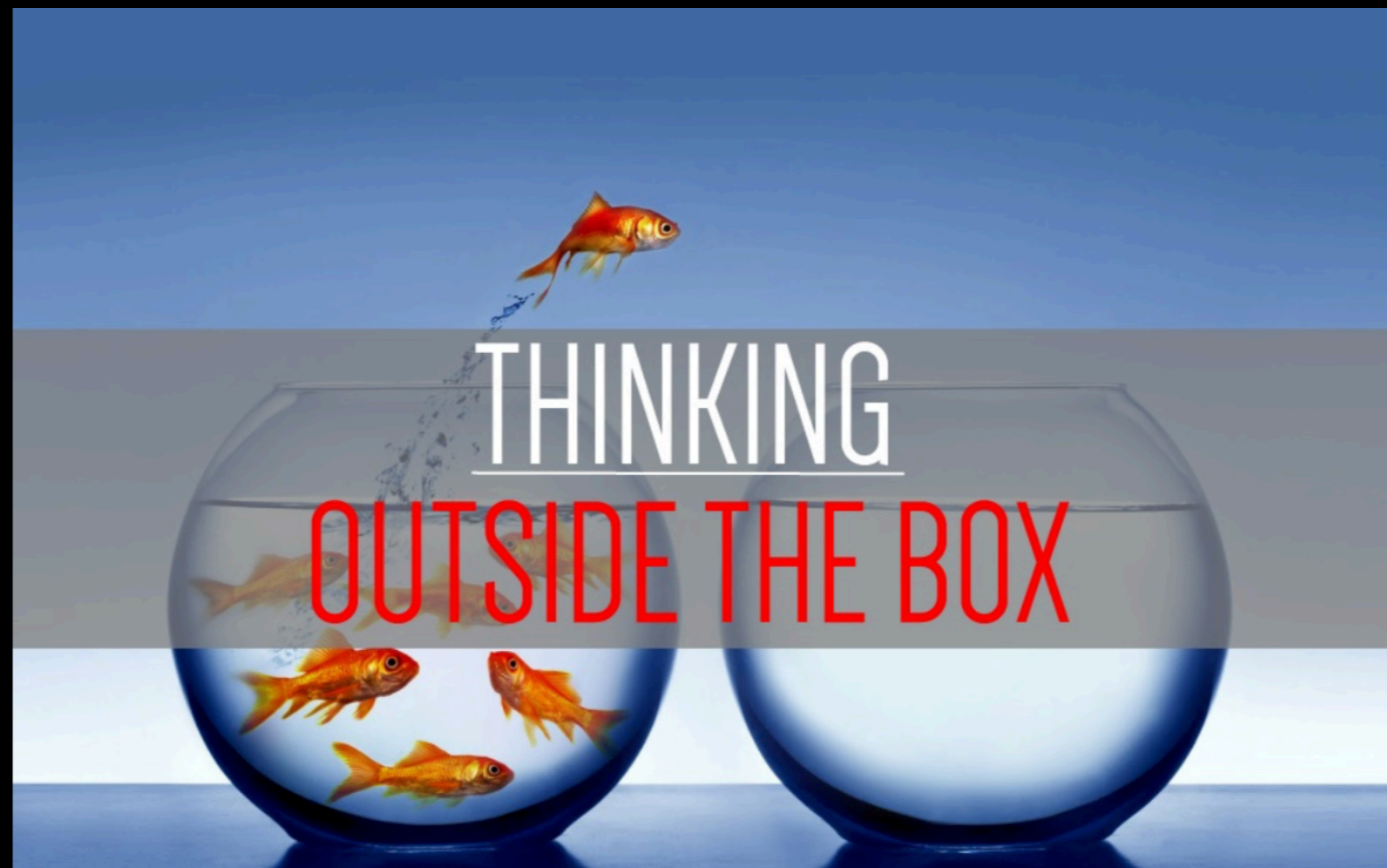


# On B anomalies: *fitting outside the box*

Based on **JHEP** 1606 (2016) 116, **EPJ C**77 (2017) 688 + work in progress



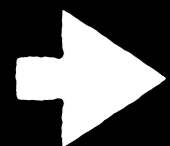
**Mauro Valli** — INFN Rome —

04/18/2018

LIO International Conference on Flavour Physics  
— FROM FLAVOUR TO NEW PHYSICS —



No tree-level flavor changing neutral currents  
in the Standard Model (SM).



SENSITIVITY TO NEW PHYSICS (NP)

E.g.: in  $b$  to  $s$   $\ell\ell$  transitions!

THESE DAYS MAY BE PARTICULARLY EXCITING:

$\sim 3.5 \sigma$

Angular analysis of  $B \rightarrow K^* \mu\mu$

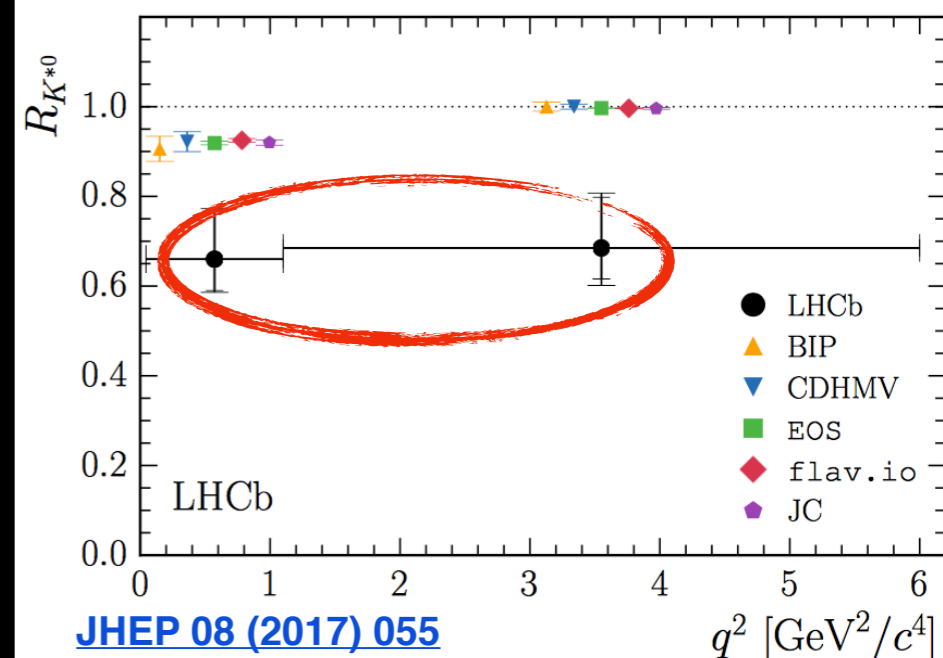
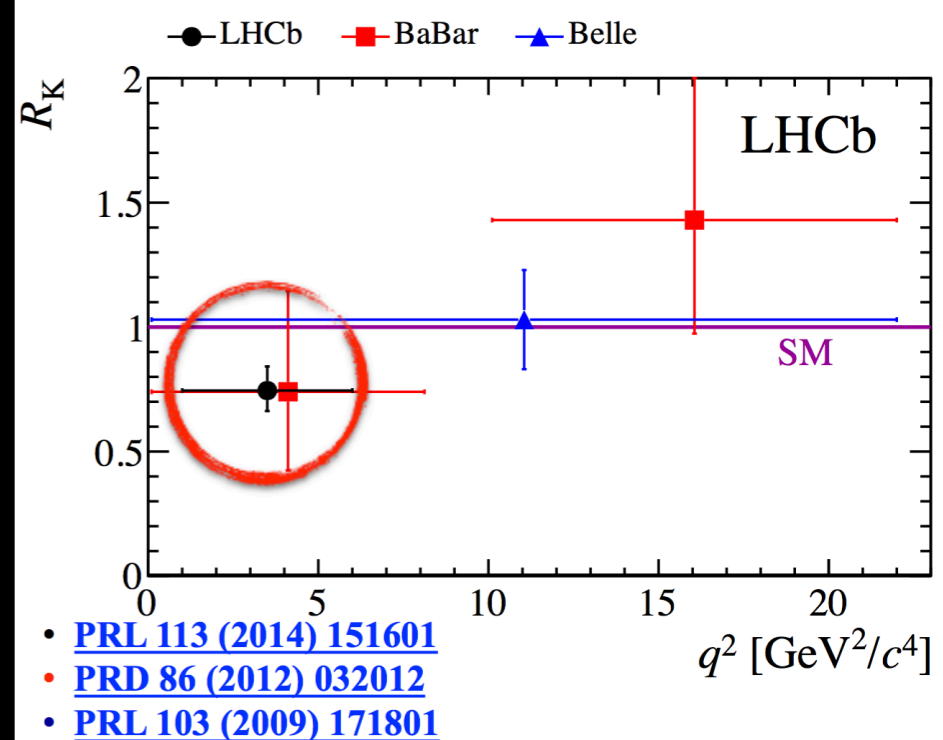
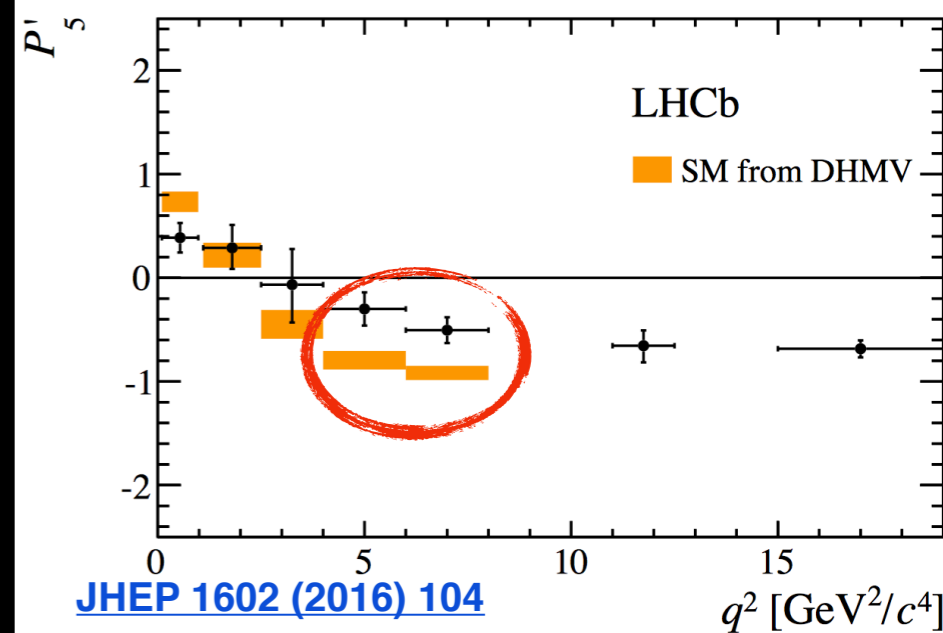
$\sim 2.5 \sigma$

$R_{K,K^*}$  measurements!

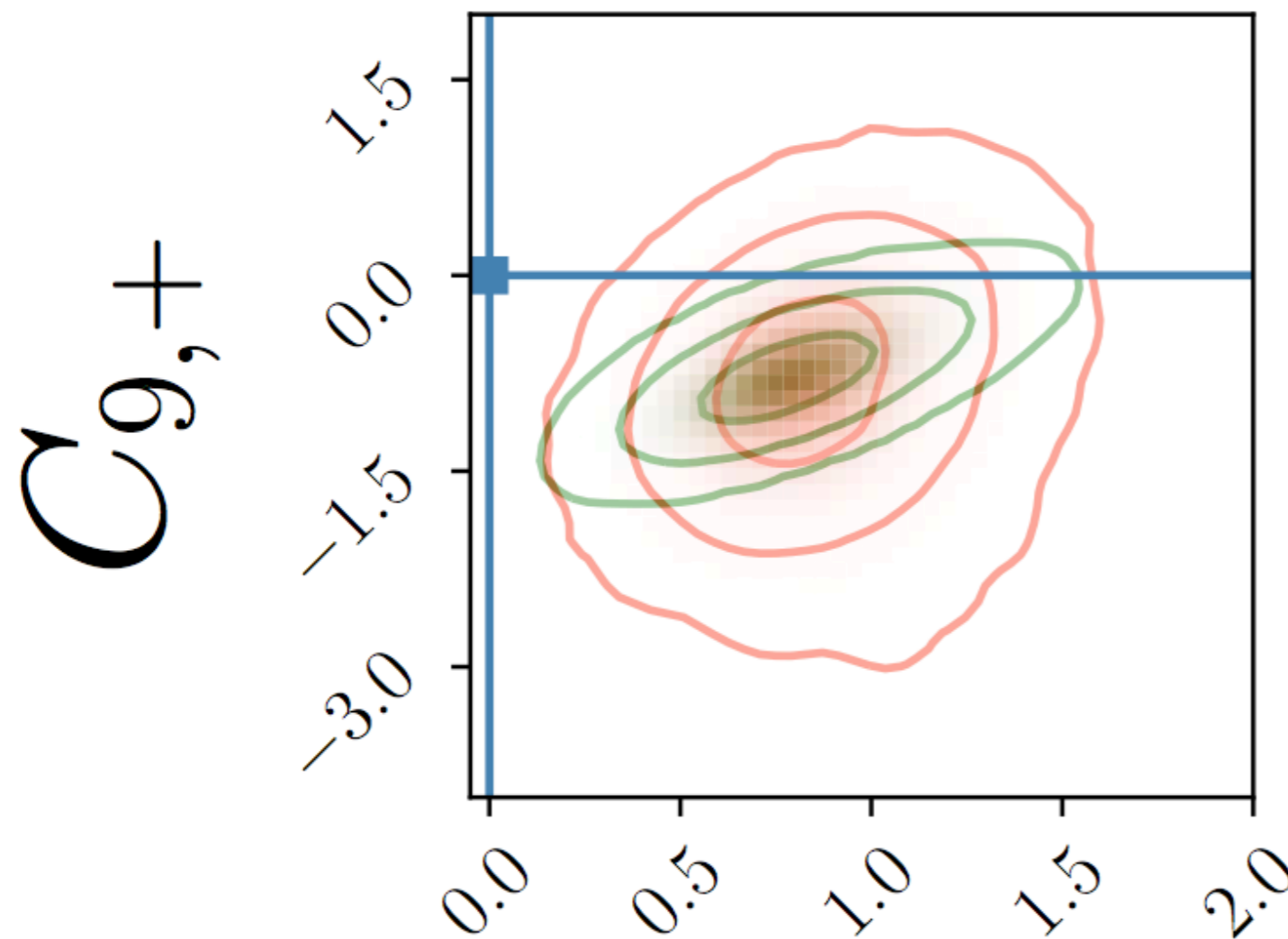
+ deviations in BR of other modes

ALSO: POSSIBLE CORRELATION WITH  $b \rightarrow c$   
IN LIGHT OF HFLAV AVERAGE ON  $R_D, R_{D^*} \dots$   
INTRIGUING (BUT FAR FROM GRANTED)!

MY FOCUS HERE FALLS ON  $b \rightarrow s \ell\ell$  ANOMALIES.



# A GLIMPSE ON WHAT WE WILL TALK ABOUT.



$$C_{9,\ell} \leftrightarrow \frac{\bar{s}_L \gamma_\mu b_L \bar{\ell} \gamma^\mu \ell}{Q_{9,\ell}}$$

■ “optimistic”  
approach to  
QCD effects

■ conservative  
approach to  
QCD effects

$$\pm \equiv \frac{1}{2} (\mu \pm e)$$

$$C_{9,-}$$

# ANATOMY OF $B \rightarrow K^{(*)} \ell \ell$ IN THE SM

$$H_{\lambda}^{(V)}(q^2) \propto 2 \frac{m_b m_B}{q^2} \left( C_7^{\text{eff}} + \Delta C_{7,\lambda}^{\text{QCDf}}(q^2) \right) \tilde{T}_{\lambda}(q^2) + C_9^{\text{eff}}(q^2) \tilde{V}_{\lambda}(q^2)$$

HELICITY AMPLITUDES :  $\lambda = \pm, 0$ .

$$+ \Delta C_{9,\lambda}^{\text{QCDf}}(q^2) + 16\pi^2 \frac{m_B^2}{q^2} \tilde{h}_{\lambda}(q^2),$$

$$H^{(P)}(q^2) \propto 2 \frac{m_{\ell} m_B}{q^2} C_{10} \left( 1 + \frac{m_s}{m_b} \right) \tilde{S}(q^2), \quad H_{\lambda}^{(A)}(q^2) \propto C_{10} \tilde{V}_{\lambda}(q^2).$$

- SHORT DISTANCE @ DIM 6

*SM Wilson coeffs @  $\sim m_b$ :  $C_7 \sim -1/3$ ,  $C_9 \sim 4$ ,  $C_{10} \sim -4$*

- FORM FACTORS FOR  $B \rightarrow K^{(*)}$

*state-of-the-art from LQCD & LCSR computations*

- QCD CONTRIBUTIONS FROM C x C & PENGUINS

*QCD factorization for leading effects of  $O(\Lambda_{\text{QCD}}/m_b)$ ,*

*but non-factorizable power corrections also present.*

# BAYESIAN FIT OF $B \rightarrow K^{(*)} \ell \ell$

## - HELICITY AMPLITUDES FROM STATE-OF-THE-ART OF THE THEORY:

Z-EXPANSION FROM LCSR / LQCD

(Bayley et al.'15, Bharucha et al.'15)

QCD FACTORIZATION COMPUTATIONS

(Beneke et al.'01, Beneke et al.'09)

PHENOMENOLOGICAL APPROACH FOR  
NON-FACTORIZABLE POWER CORRECTIONS

NEW PHYSICS WILSON COEFFICIENTS



57 TO 77 PARAMETERS  
VARIED IN  $b \rightarrow s \ell \ell$  FITS  
(PRIORS: GAUSSIAN/FLAT)

## - FIT AVAILABLE EXP INFO. IN THIS TALK THE FOCUS WILL BE ON:

LHCb CP-CONSERVING ANGULAR OBS + BRs FOR  $K^{(*)}$  MODES AT  
LARGE RECOIL, BELLE DATA ON  $P'_4$  &  $P'_5$ ,  $B_s \rightarrow \ell \ell$  FROM HFLAV.

## - BAYESIAN MODEL COMPARISON WITH INFORMATION CRITERION:

$$IC \equiv -2\overline{\ln \mathcal{L}} + 4\sigma_{\ln \mathcal{L}}^2$$

# DICHOTOMY OF $B \rightarrow K^* \ell \ell$ IN THE SM

Phenomenological  
Data Driven (PDD)

$$\tilde{h}_\lambda(q^2) = \sum_k \tilde{h}_\lambda^{(k)} \left( \frac{q^2}{\text{GeV}^2} \right)^k \quad \text{up to } k=2, \text{ 16 real coeffs are involved}$$

$\Delta C_9$

$\Delta C_7$

$$\left\{ (C_9^{\text{eff}} + h_-^1) V_{L-} + \frac{m_B^2}{q^2} \left[ \frac{2m_b}{m_B} (C_7^{\text{eff}} + h_-^0) T_{L-} - 16\pi^2 h_-^2 q^4 \right] \right\}$$

$$\left\{ (C_9^{\text{eff}} + h_-^1) \tilde{V}_{L0} + \frac{m_B^2}{q^2} \left[ \frac{2m_b}{m_B} (C_7^{\text{eff}} + h_-^0) \tilde{T}_{L0} - 16\pi^2 (\tilde{h}_0^0 + \tilde{h}_0^1 q^2) \right] \right\}$$

$$\left\{ (C_9^{\text{eff}} + h_-^1) V_{L+} + \frac{m_B^2}{q^2} \left[ \frac{2m_b}{m_B} (C_7^{\text{eff}} + h_-^0) T_{L+} - 16\pi^2 (h_+^0 + h_+^1 q^2 + h_+^2 q^4) \right] \right\}$$

DO NOT HAVE  $C_{7,9}$  SHORT-DISTANCE COUNTERPART!

WE CONSTRAIN THIS SET REQUIRING TO MATCH AS ABSOLUTE VALUE  
LCSR RESULTS **ONLY** FOR  $q^2 \leq \text{GeV}^2$  (Khodjamirian et al. '10).

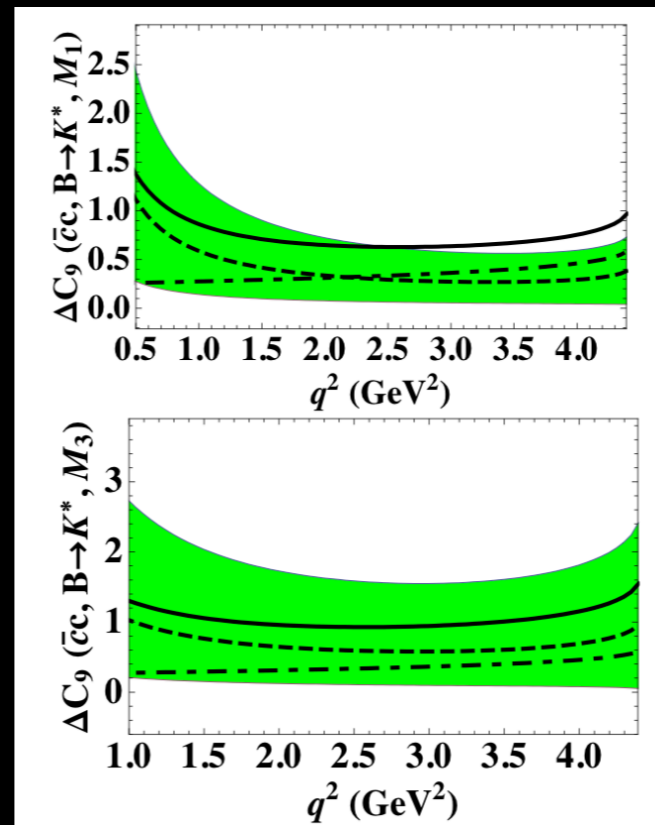
WE ALSO REQUIRE  $|h_+/h_-| \ll 1$  AT LARGE RECOIL (Jager & Camalich '14).

# DICHOTOMY OF $B \rightarrow K^* \ell \ell$ IN THE SM

Phenomenological  
Model Driven (PMD)

NEW HERE

WE DO NOT LONGER  
TRANSLATE THIS INTO  
“THEORY DATA POINTS”.  
(as in Ciuchini`17 et al.)



LCSR COMPUTATION  
+ DISPERSION REL.  
Khodjamirian et al. `10

Results recently  
corroborated by:  
Bobeth et al. `17  
Blake et al. `17

WE NOW ADOPT THE PARAMETRIZATION FOR THE DISPERSION RELATION:

$$\Delta C_{9,i}^{(c\bar{c})}(q^2) = \frac{r_{1,i} \left(1 - \frac{\bar{q}^2}{q^2}\right) + \Delta C_{9,i}^{(c\bar{c})}(\bar{q}^2) \frac{\bar{q}^2}{q^2}}{1 + r_{2,i} \frac{\bar{q}^2 - q^2}{m_{J/\psi}^2}}$$

$i = 1, 2, 3$

AS ABSOLUTE VALUE (TIMES PHASE FACTOR), ASSIGNING FLAT PRIORS.

# DICHOTOMY OF $B \rightarrow K^* \ell \ell$ IN THE SM

update of Ciuchini '16

**Phenomenological  
Model Driven (PMD)**

$$\overline{\ln \mathcal{L}} = -48.7$$

$$\sigma_{\ln \mathcal{L}}^2 = 6.9$$

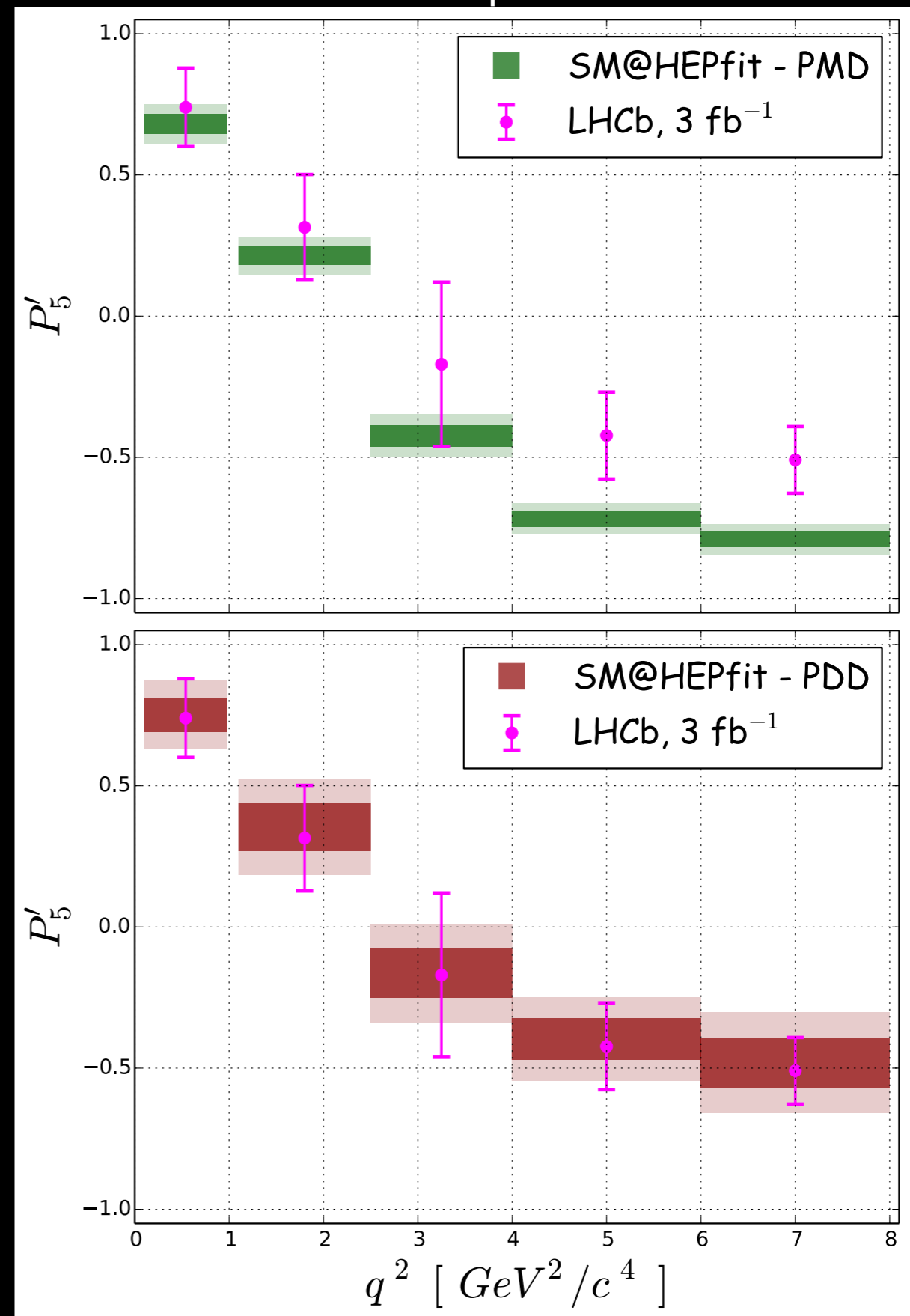
$$P'_5 = \frac{S_5}{\sqrt{F_L(1 - F_L)}}$$

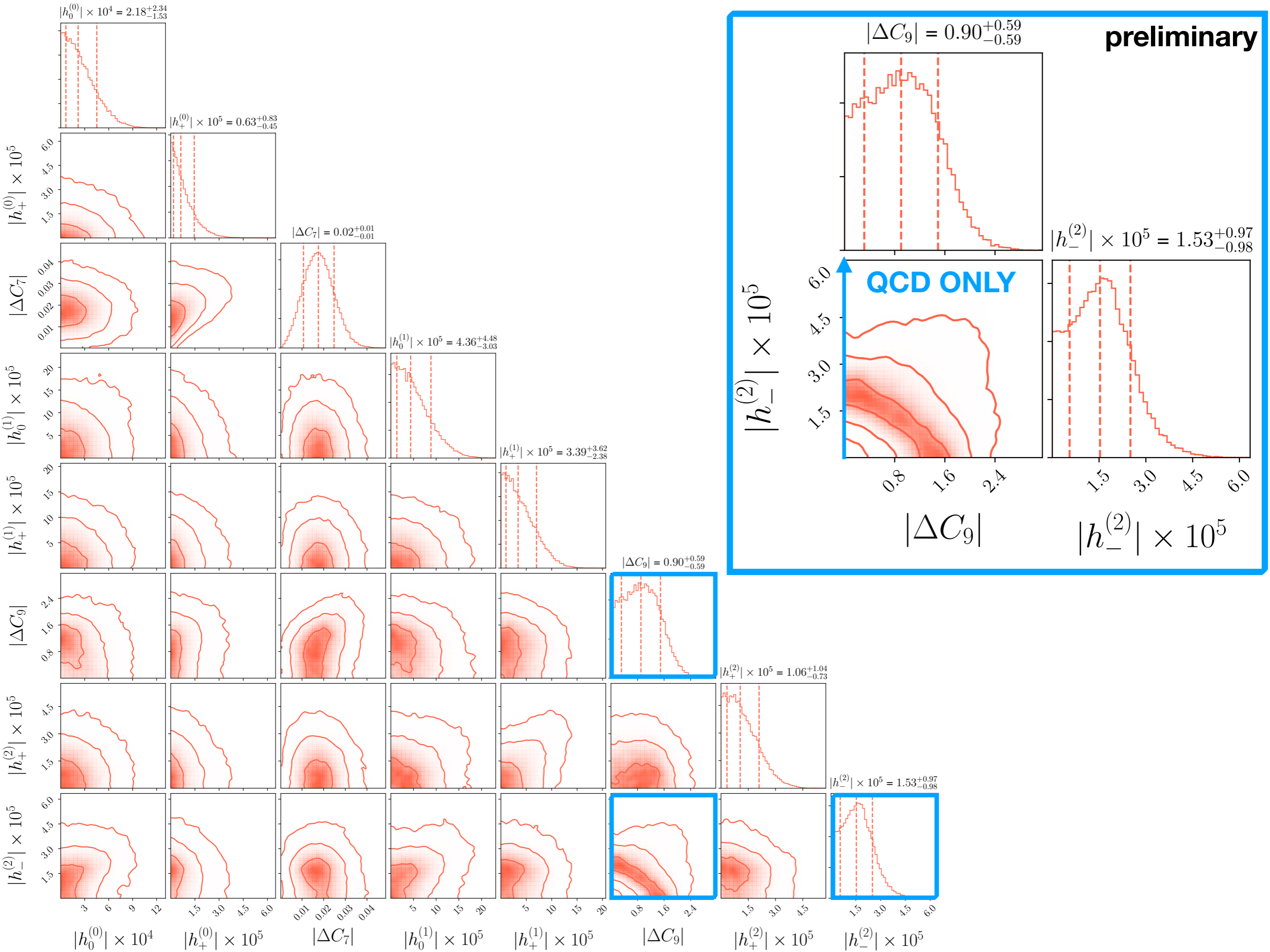
Matias et al. '12

**Phenomenological  
Data Driven (PDD)**

$$\overline{\ln \mathcal{L}} = -38.5$$

$$\sigma_{\ln \mathcal{L}}^2 = 6.1$$



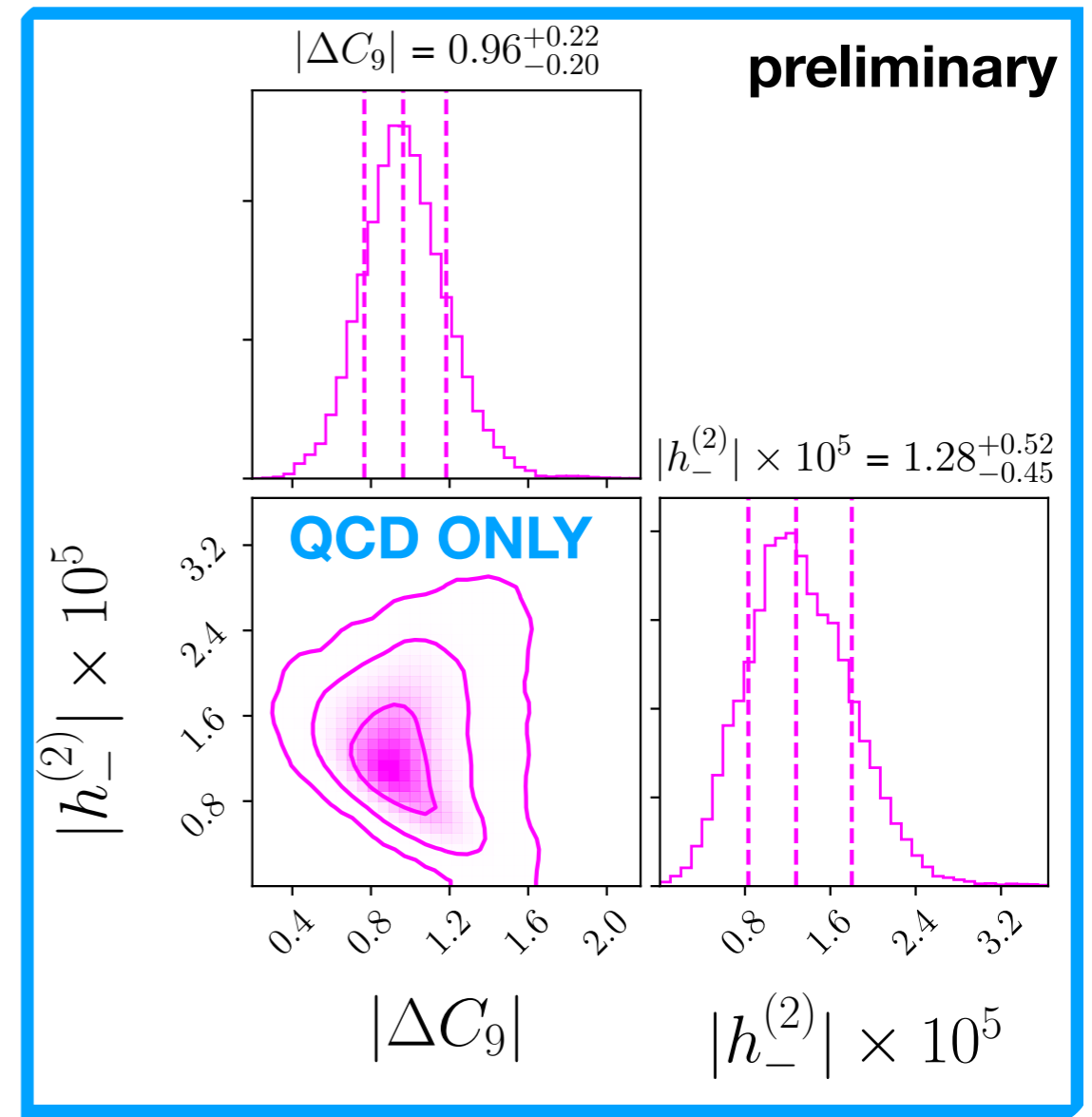
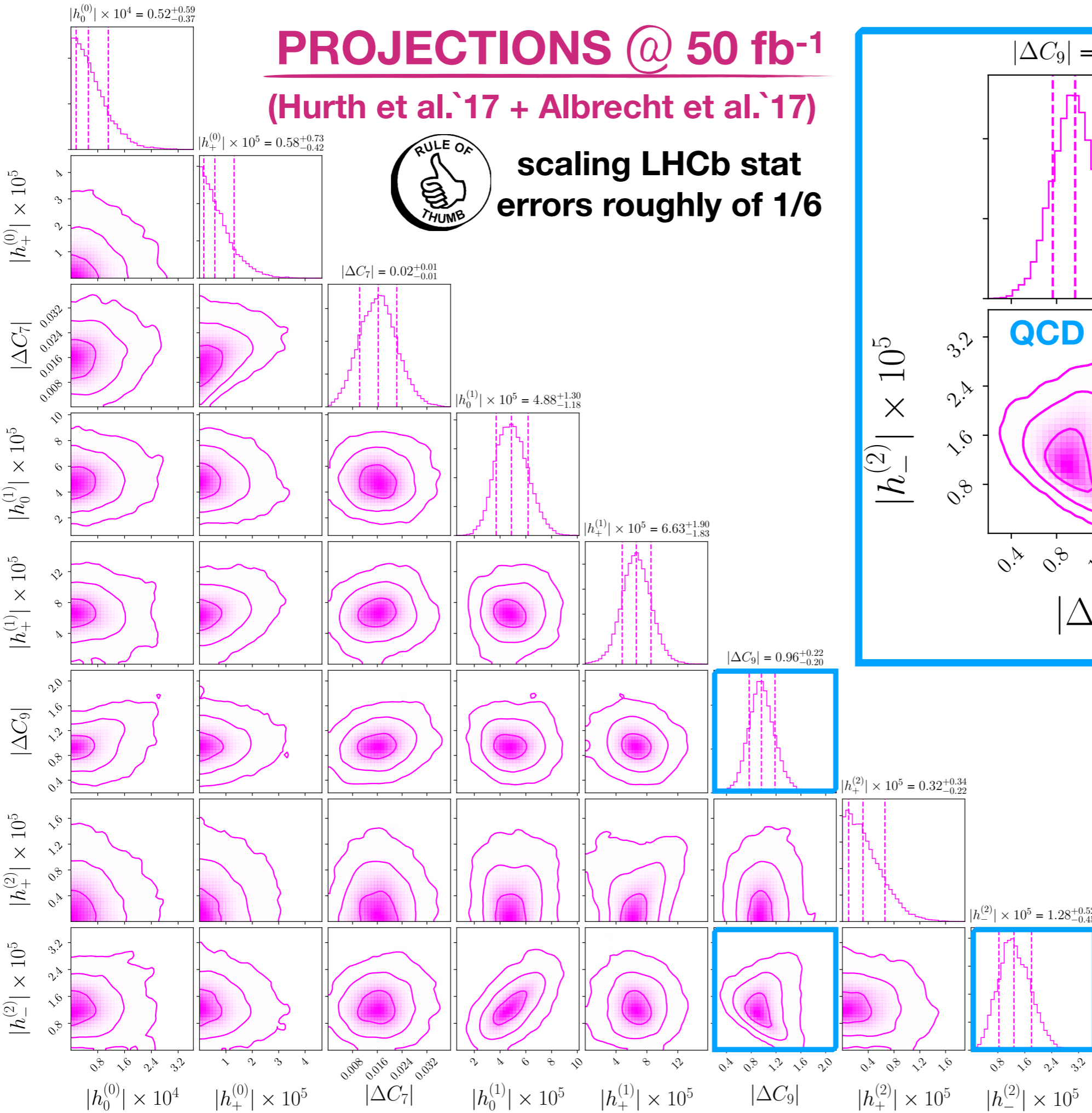


# PROJECTIONS @ 50 fb<sup>-1</sup>

(Hurth et al.`17 + Albrecht et al.`17)



scaling LHCb stat  
errors roughly of 1/6



preliminary

**NOW ...**

State-of-the-art global analyses of  $b \rightarrow s \ell \ell$  measurements show evidence for NP at the  $5\sigma$  -  $6\sigma$  level, commonly associated to  $Q_{9,\mu}$ .

*Altmannshofer et al. '17*

*Capdevila et al. '17*

*Ciuchini et al. '17*

*D'Amico et al. '17*

*Geng et al. '17*

*Hiller & Nisandzic '17*

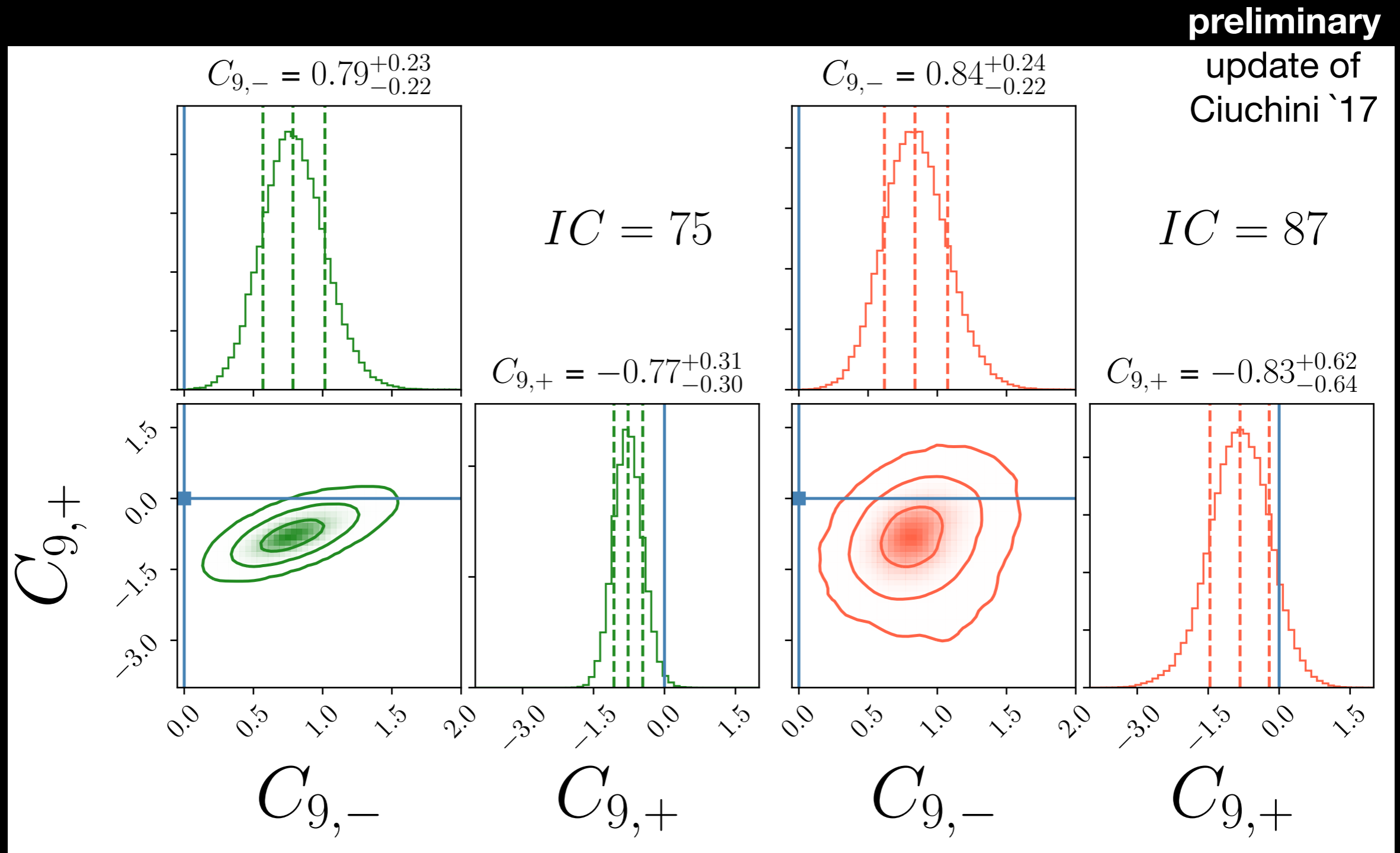
*... + many others!*

**BUT ...**

*I) Are data unambiguously pointing to NP in muonic vectorial current?*

*II) What is the role of unknown QCD power corrections in this business?*

# NP IN $B \rightarrow K^{(*)} \ell \ell$ FROM VECTORIAL COUPLINGS

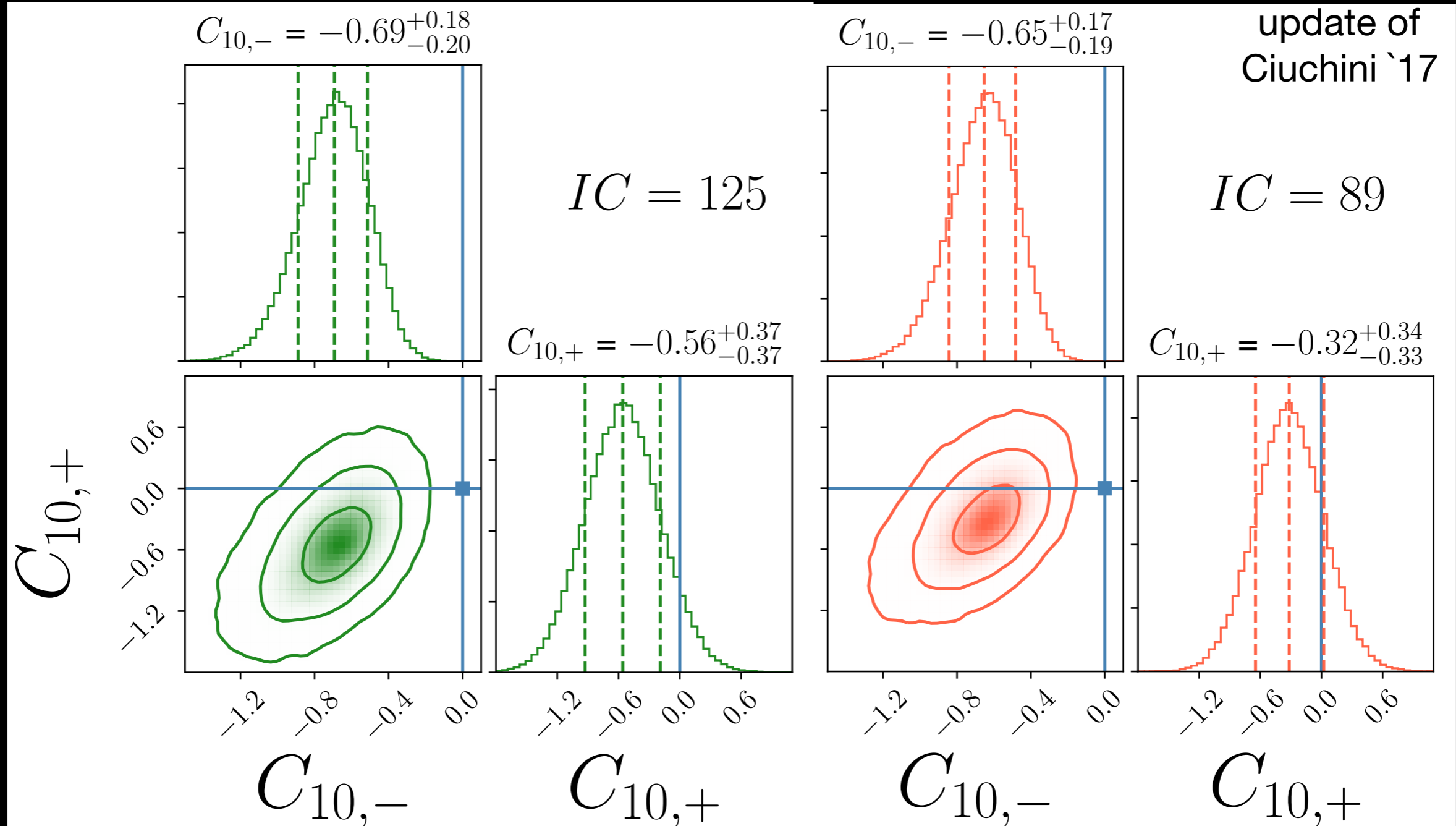


MINUS COEFFICIENT IS PROBED BY LUV OBS.  
MINIMALITY CURRENTLY REWARDS **PMD**.

# NP IN $B \rightarrow K^{(*)} \ell \ell$ FROM AXIAL COUPLINGS

preliminary

update of  
Ciuchini '17

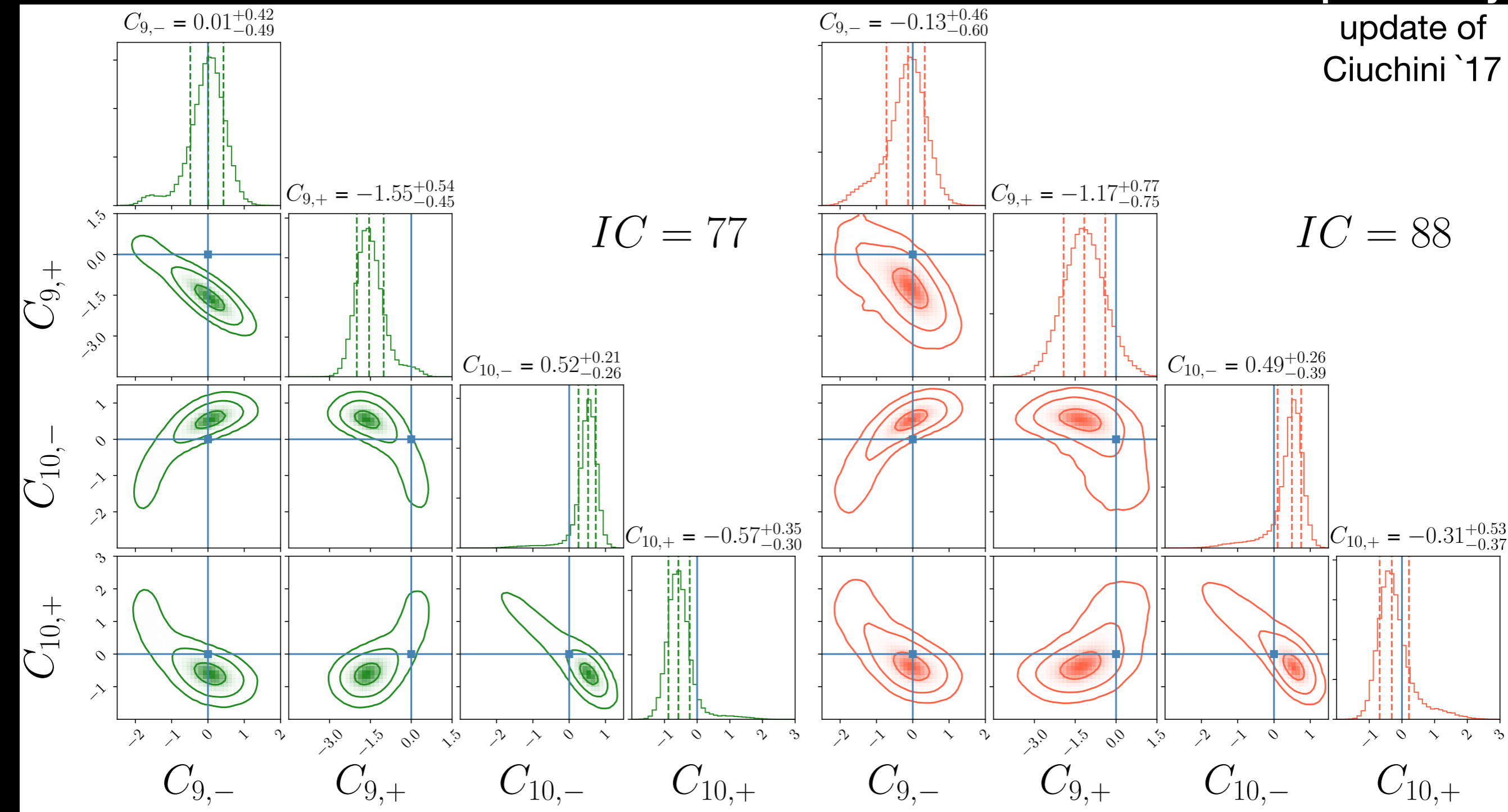


MINUS COMBINATION DETERMINED AGAIN BY LUV.  
IN **PDD** AXIAL SOLUTION AS VIABLE AS VECTOR ONE.

# AXIAL & VECTOR NP IN $B \rightarrow K^{(*)} \ell \ell$

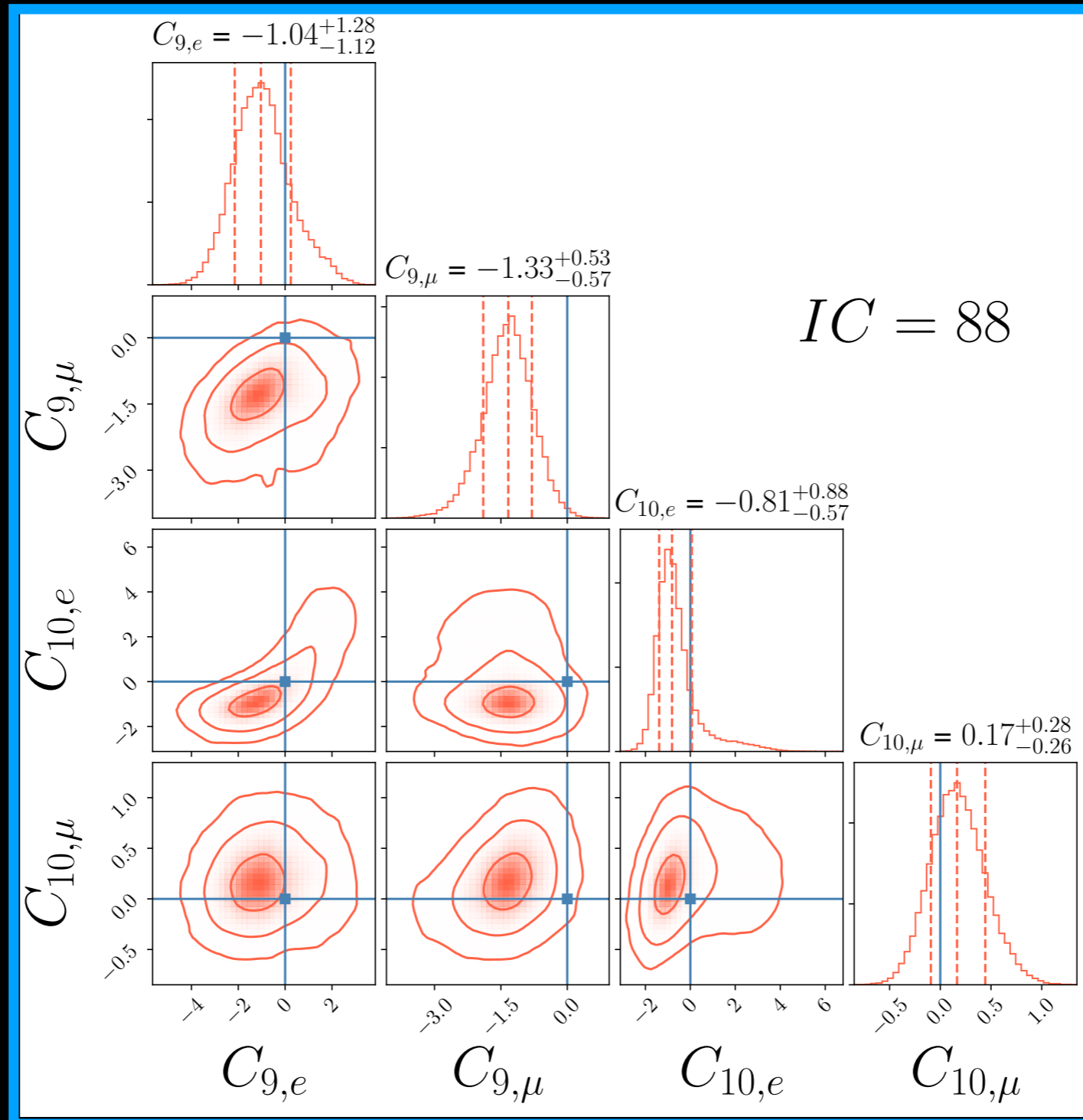
preliminary

update of  
Ciuchini '17



**“POLLUTED” PLUS-DIRECTION IN  $C_9$  IS SELECTED BY DATA  
IN STRONG CORRELATION WITH AXIAL COEFFICIENTS.**

# AXIAL & VECTORIAL NP IN $B \rightarrow K^{(*)} \ell \ell$

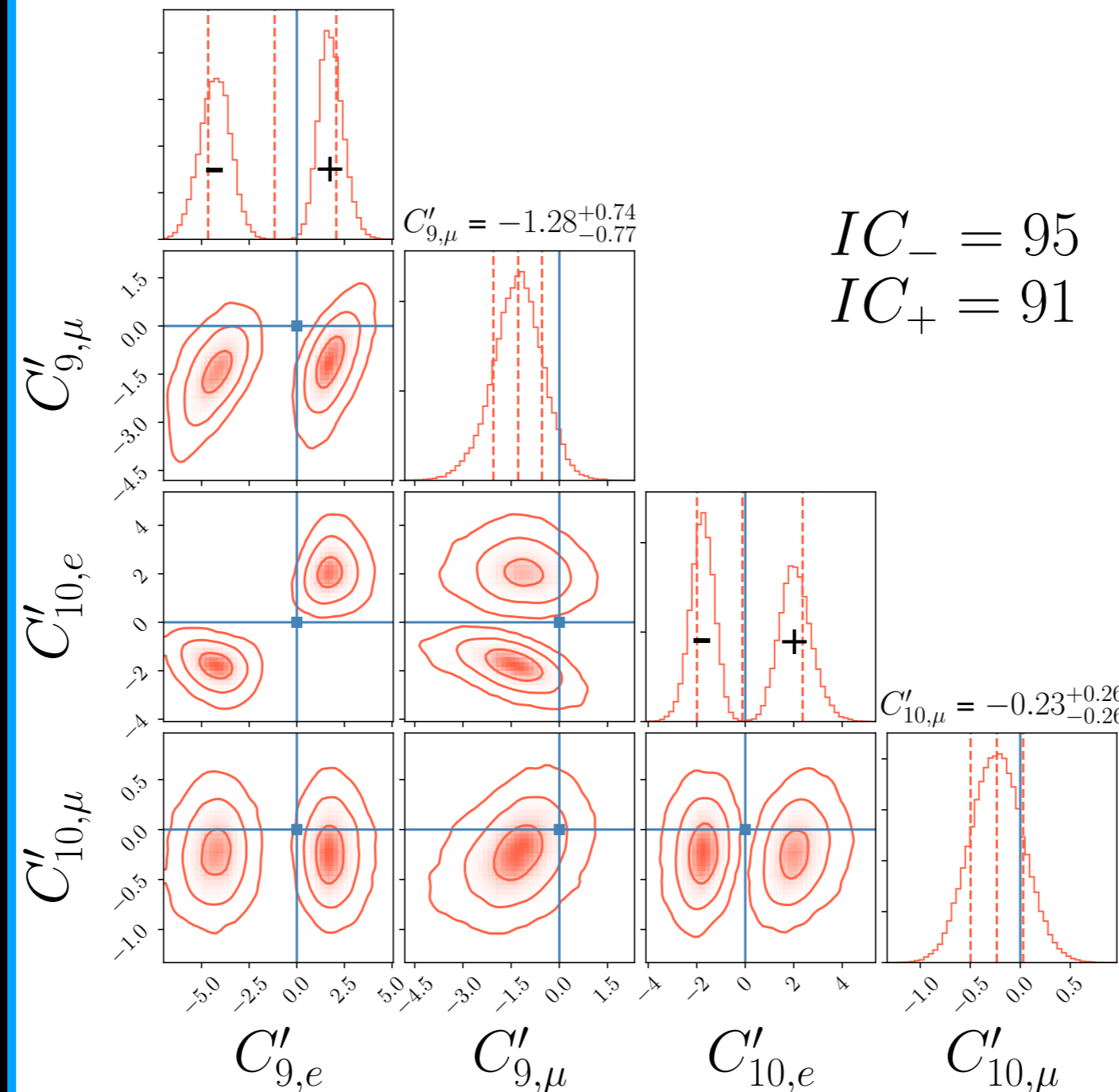


preliminary  
update of  
Ciuchini '17

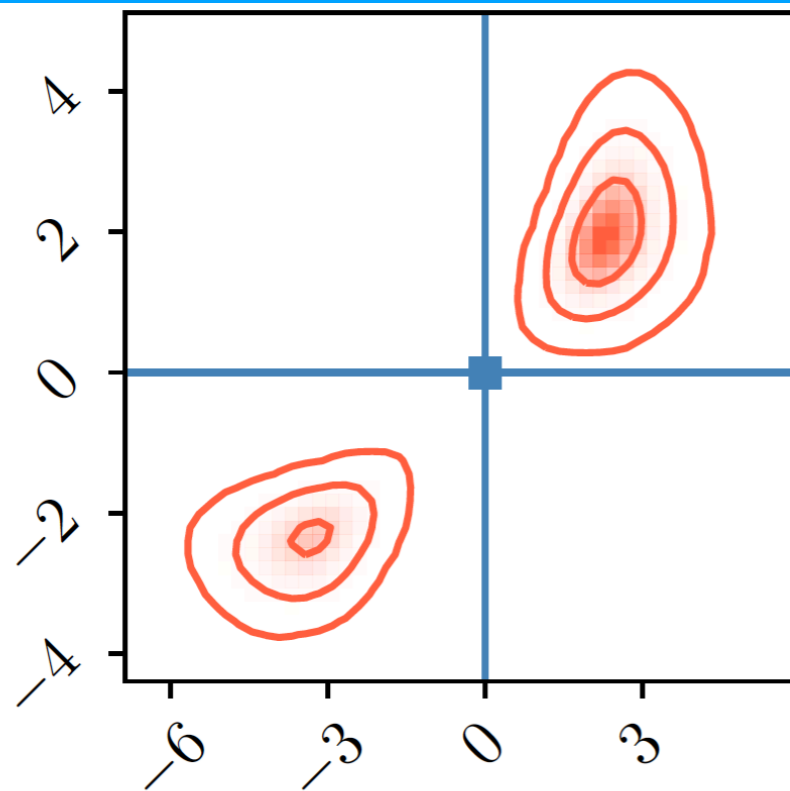
**BACK TO LEPTON-FLAVORED BASIS, SUCH CORRELATIONS  
HIGHLIGHT PREFERENCE FOR MUONIC VECTORIAL NP.**

# (AXIAL & VECTORIAL)' NP IN $B \rightarrow K^{(*)} \ell \ell$

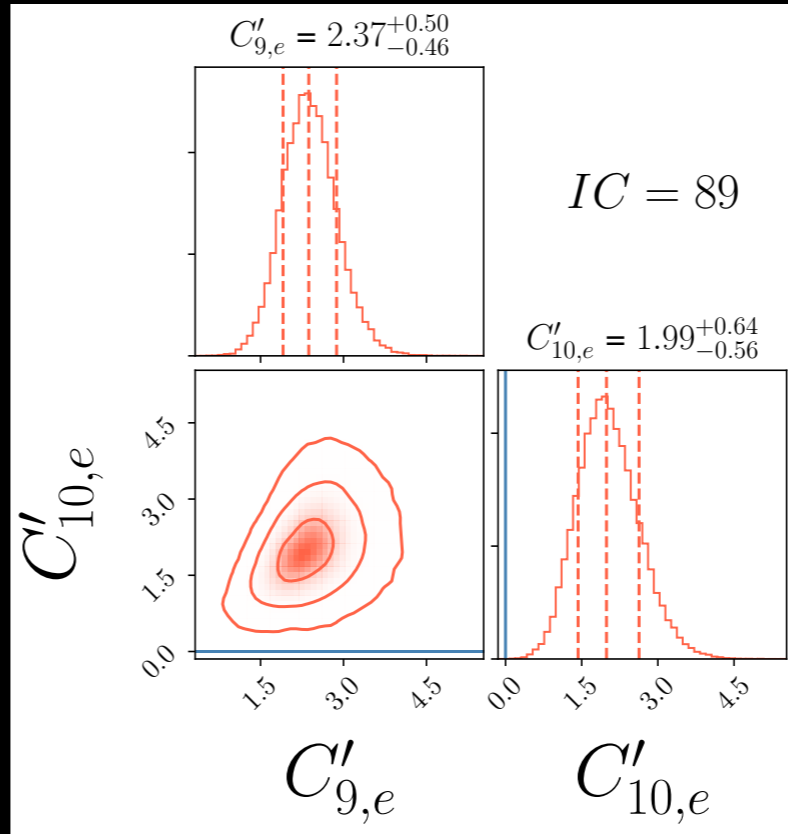
preliminary



DETERMINATION OF ELECTRON COEFFS STANDS OUT.  
 BUT EVEN IN **PDD** V+A b TO s CURRENT (A BIT) DISFAVORED.

$C'_{10,e}$ 

preliminary

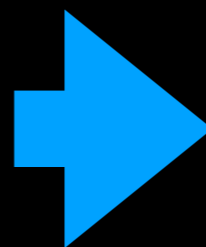
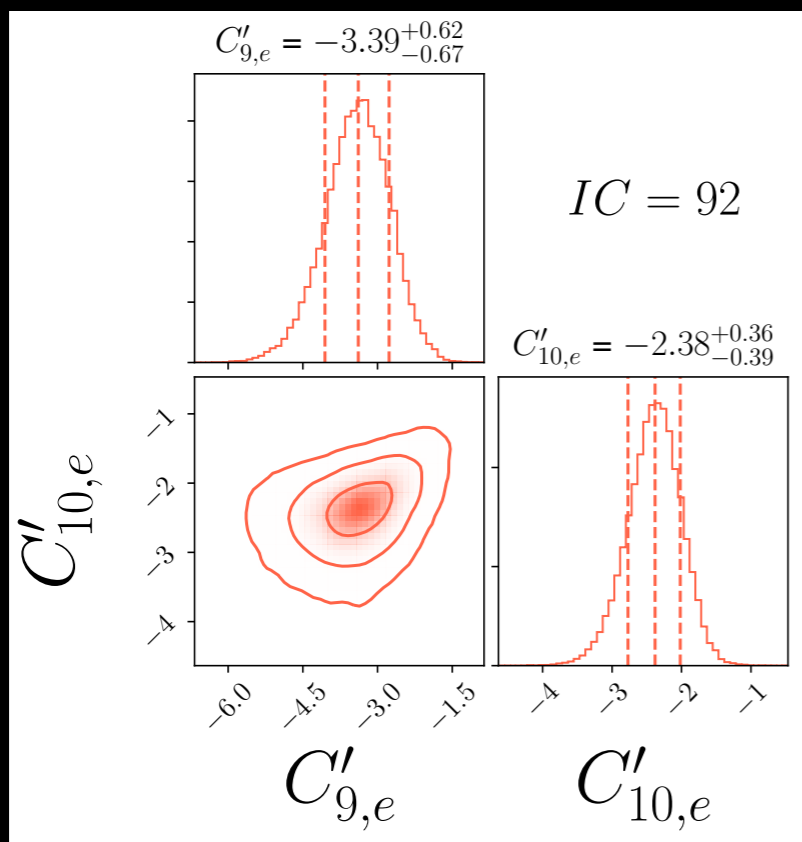
 $C'_{9,e}$ 

BIMODALITY  
DRIVEN BY  $P'^{BELLE}_{4,5}$ .

MODES CAN  
BE SEPARATELY  
INVESTIGATED.

## V+A with NP in ELECTRONS

- IN **PMD** BOTH SOLUTIONS ARE STRONGLY DISFAVORED.
- IN **PDD** BOTH SOLUTIONS ARE ACTUALLY AVAILABLE.



BELLE & LHCb DATA ON  
ELECTRONS MILDLY POINT  
TO SCENARIO  $C'_{9,10e} > 0$ .

# CONCLUSIONS

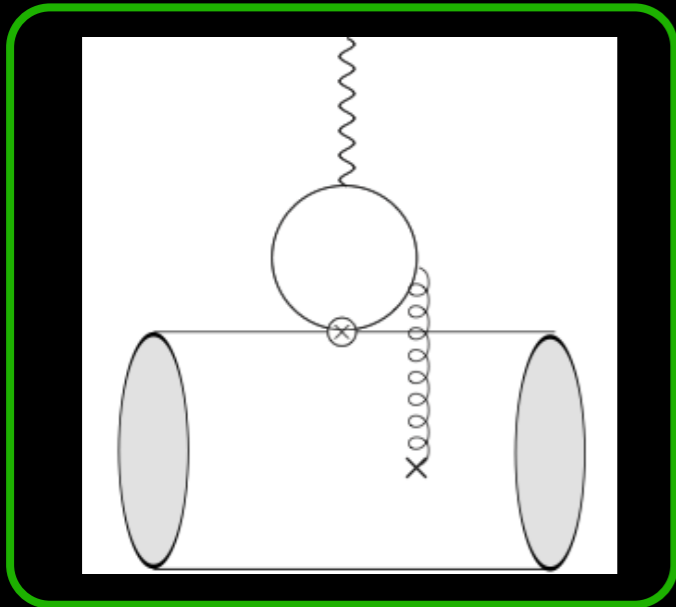
- I) A CONSERVATIVE APPROACH TO HADRONIC UNCERTAINTIES HIGHLIGHTS THE CRUCIAL ROLE OF LUV MEASUREMENTS IN THE ANALYSIS OF NP EFFECTS IN  $b \rightarrow s \ell \ell$  TRANSITIONS
- II) AS THE MOST ECONOMIC SOLUTION, NP IN  $Q_{9,\mu}$  IS PREFERRED BY DATA.
- III) OTHER NP SCENARIOS MAY BE OF INTEREST IF WE HAVE GOOD REASONS TO DISCARD “OCCAM’S RAZOR” ARGUMENT  
( NOTE THAT NONE OF THEM PROVIDES AN EXPLANATION FOR THE FIRST BIN OF  $R_{K^*}$ ! )
- IV) LHCb UPGRADE (+ BELLE II) WILL HAVE THE SENSITIVITY TO PIN DOWN QCD POWER CORRECTIONS + IMPROVE LUV DATASET.  
**EXCITING TIMES AHEAD!**



*THANK YOU !*

**BACK-UP**

## The “charm-loop” effect



Khodjamirian et al. `10

$$h_{\lambda}(q^2) = \frac{\epsilon_{\mu}^*(\lambda)}{m_B^2} \int d^4x e^{iqx} \langle \bar{K}^* | T \{ j_{\text{em}}^{\mu}(x) \mathcal{H}_{\text{eff}}^{\text{had}}(0) \} | \bar{B} \rangle$$

Correlator expanded on the light-cone:  
LCSR estimate based on small  $q^2$ .

Single soft gluon approximation, i.e. first term of expansion in  $\Lambda_{\text{QCD}}^2 / (4 m_c^2 - q^2)$

Dispersion relation in order to extrapolate to physical charm resonances

## THE OUTCOME MORE RECENTLY RE-INVESTIGATED BY:

1) pheno model using resonance data over the full di-muon spectrum

Blake et al. `17

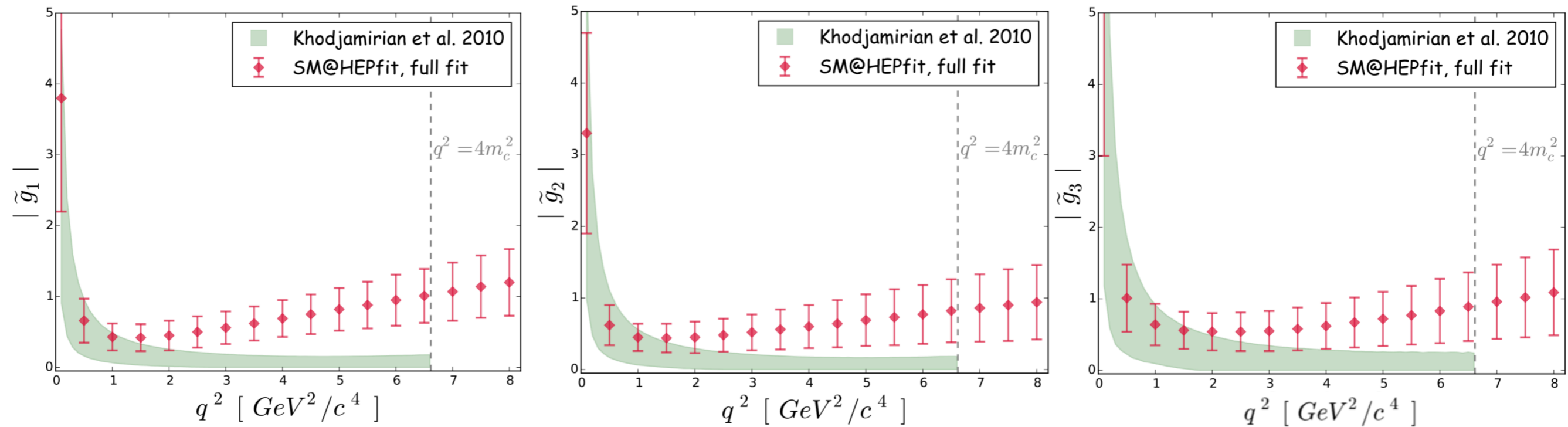
2) replacing dispersion relation with z-expansion, constraining coefficients via analyticity +  $B \rightarrow \Psi(n) K^*$  data + QCDF & LCSR at small  $q^2$ .

Bobeth et al. `17

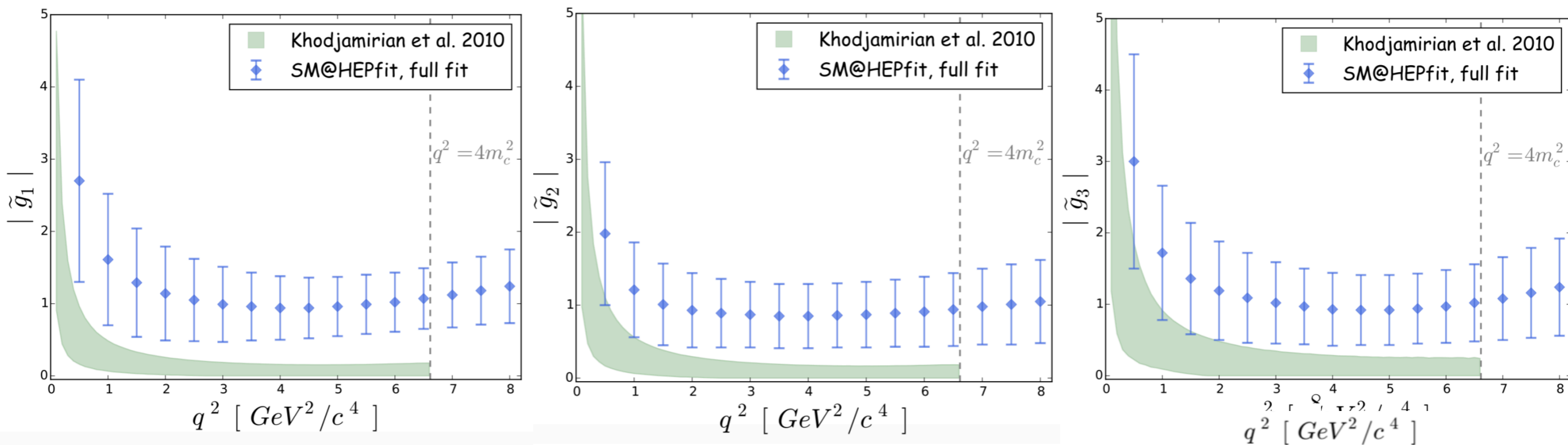
**1) AND 2) ARE NOT FREE FROM ASSUMPTIONS / APPROXIMATIONS.**

As an overall shift on  $C_9$ , our result comes with some  $q^2$  dependence:

update of Ciuchini et al.'16



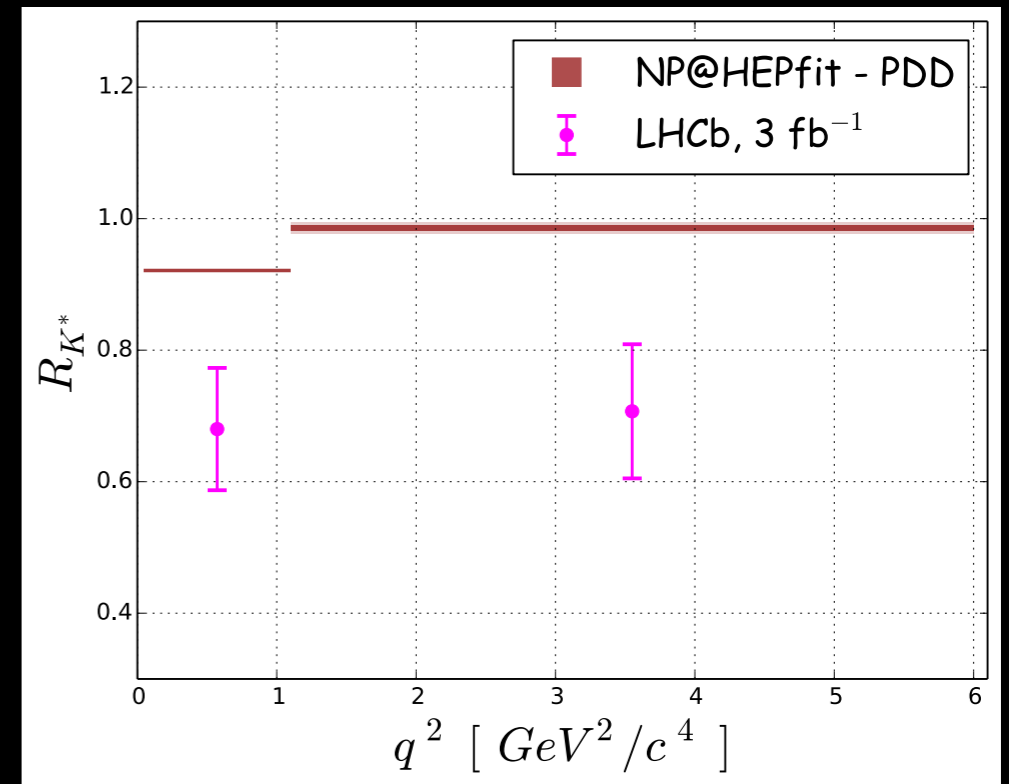
HOWEVER, THIS DEPENDS ON OUR THEORY INPUT FROM LCSR AT  $q^2 < \text{GeV}^2$ :



# OTHER POSSIBILITIES?

## (PSEUDO)-SCALAR OPERATORS

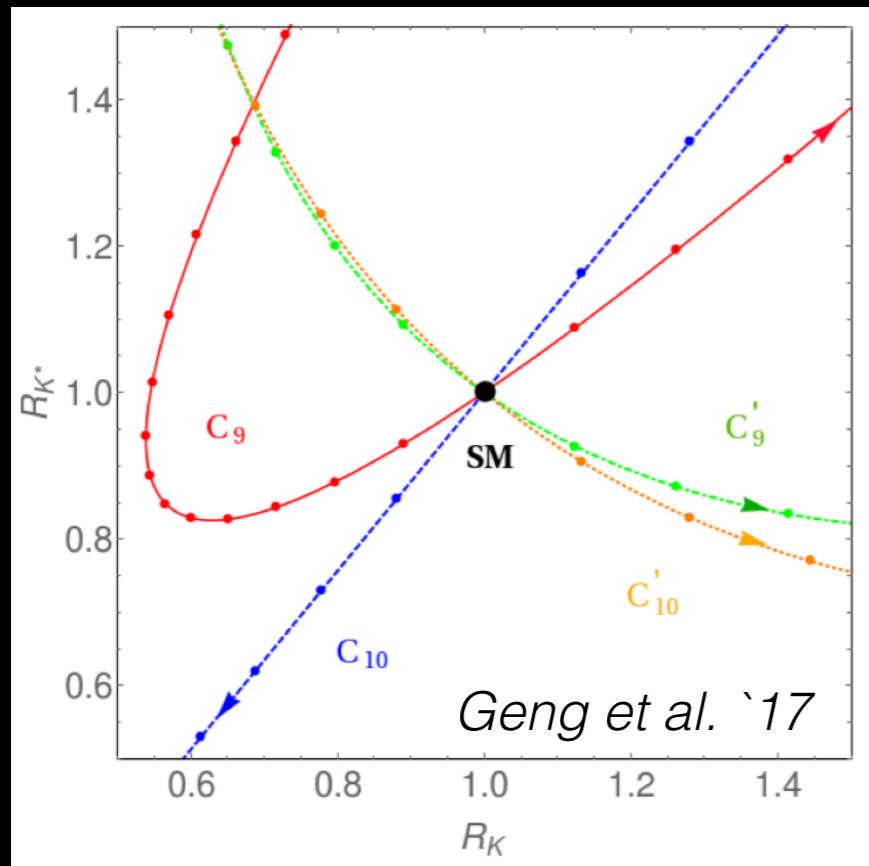
- 4 OPERATORS FOR LEPTON FLAVOR
- CONSTRAINTS FROM  $B_s \rightarrow \Pi$
- ANGULAR OBSERVABLES INFORMATIVE AS WELL



preliminary

THEY MAY ADDRESS  $R_K$  (see, e.g., *Bobeth et al.* '07).

IN PDD, THIS SCENARIO IS ACTUALLY IN TENSION “ONLY” WITH  $R_{K^*}$ .



AXIAL / VECTOR-LIKE OPERATORS  
INVOLVING RH  $b \rightarrow s$  CURRENTS:

OUTCOME FROM SINGLE-OPERATOR  
STUDY NOT VERY ENCOURAGING ...

... BUT MULTIPLE COMBINATIONS  
WOULD ALSO BE POSSIBLE!