



Exploring the partonic phase at finite chemical potential within heavy-ion collisions

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arXiv:1903.10257





- Explore the QCD phase diagram at finite temperature and chemical potential through heavy-ion collisions
- Available information:
 - Experimental data at SPS, BES at RHIC
 - Lattice QCD calculation

Probes of the QGP at finite (T, μ_B)





- Goal: Study the properties of strongly interacting matter under extreme conditions from a microscopic point of view
- Realization: dynamical many-body transport approach

Parton-Hadron-String-Dynamics (PHSD)

- Explicit parton-parton interactions, explicit transiton from hadronic to partonic degrees of freedom
- Transport theory: off-shell transport equations in phase-space representation based on Kadanoff-Baym equations for the partonic and hadronic phase



W.Cassing, E.Bratkovskaya, PRC 78 (2008) 034919; NPA831 (2009) 215; W.Cassing, EPJ ST 168 (2009) 3









Introduction

DQPM

Implementation in PHSD Results

Summarv

QCD EoS, partonic interactions

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Lattice data at finite (T, μ_B)

Taylor series of thermodynamic quantities in terms of (μ_B/T)

Implementation in PHSD Results

For the pressure, we get:

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Introduction

 $\frac{P}{T^4} = c_0(T) + c_2(T) \left(\frac{\mu_B}{T}\right)^2 + c_4(T) \left(\frac{\mu_B}{T}\right)^4 + c_6(T) \left(\frac{\mu_B}{T}\right)^6 + \mathcal{O}\left(\mu_B^8\right) = c_0(T) + c_2(T) \left(\frac{\mu_B}{T}\right)^2 + c_4(T) \left(\frac{\mu_B}{T}\right)^4 + c_6(T) \left(\frac{\mu_B}{T}\right)^6 + \mathcal{O}\left(\mu_B^8\right) = c_0(T) + c_2(T) \left(\frac{\mu_B}{T}\right)^2 + c_4(T) \left(\frac{\mu_B}{T}\right)^4 + c_6(T) \left(\frac{\mu_B}{T}\right)^6 + \mathcal{O}\left(\mu_B^8\right) = c_0(T) + c_2(T) \left(\frac{\mu_B}{T}\right)^2 + c_4(T) \left(\frac{\mu_B}{T}\right)^4 + c_6(T) \left(\frac{\mu_B}{T}\right)^6 + \mathcal{O}\left(\mu_B^8\right) = c_0(T) + c_2(T) \left(\frac{\mu_B}{T}\right)^2 + c_4(T) \left(\frac{\mu_B}{T}\right)^4 + c_6(T) \left(\frac{\mu_B}{T}\right)^6 + \mathcal{O}\left(\mu_B^8\right) = c_0(T) + c_2(T) \left(\frac{\mu_B}{T}\right)^2 + c_4(T) \left(\frac{\mu_B}{T}\right)^4 + c_6(T) \left(\frac{\mu_B}{T}\right)^6 + \mathcal{O}\left(\mu_B^8\right) = c_0(T) + c_2(T) \left(\frac{\mu_B}{T}\right)^4 + c_6(T) \left(\frac{\mu_B}{T}\right)^6 + \mathcal{O}\left(\mu_B^8\right) = c_0(T) + c_0(T) \left(\frac{\mu_B}{T}\right)^6 + c_0(T) \left(\frac{\mu_B}{T}\right)^6$

Conditions of heavy-ion collisions

$$\langle n_{\rm S} \rangle = 0$$
 and $\langle n_{\rm O} \rangle = 0.4 \langle n_{\rm B} \rangle$

EPJ Web Conf. 137 (2017) 07008

Ŏ.10

0.15

0.20

0.25

0.30

Isentropic trajectories for (T, μ_R)

Implementation in PHSD Results

Correspondance $s/n_B \leftrightarrow$ collisional energy

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 $s/n_B = 420 \leftrightarrow 200 \text{ GeV}$

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 $s/n_B = 420 \leftrightarrow 200 \text{ GeV}$

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= 144 ↔ 62.4 GeV

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□ Correspondance $s/n_B \leftrightarrow$ collisional energy

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 $s/n_B = 420 \leftrightarrow 200 \text{ GeV}$

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- = 144 ↔ 62.4 GeV
- = 94 \leftrightarrow 39 GeV

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 $s/n_B = 420 \leftrightarrow 200 \text{ GeV}$

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- = 144 ↔ 62.4 GeV
- = 94 ↔ 39 GeV
- = 70 ↔ 27 GeV

Summary

Isentropic trajectories for (T, μ_B)

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Isentropic trajectories - IQCD EoS 0.6 Correspondance $s/n_B \leftrightarrow$ $\mu_{\rm B}^{\prime}/T = 1$ 420 collisional energy $S/n_B = 14_4$ 11 1.94 0.5 s/n_B $\mu_B/T \neq 2$ $s/n_B = 420 \leftrightarrow 200 \text{ GeV}$ Sus and \$ 0.4 = 144 ↔ 62.4 GeV [GeV] $\mu_{\rm B}/T = 3$ 0.3 = 94 ↔ 39 GeV $\mu_{B}/T = 4$ = 70 ↔ 27 GeV 0.2 $\mu_{B}/T = 5$ = 51 ↔ 19.6 GeV 0.1 0.0 0.2 0.4 0.6 0.8 1.0 0.0 μ_B [GeV] EPJ Web Conf. 137 (2017) 07008

Implementation in PHSD Results

Isentropic trajectories for (T, μ_B)

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Isentropic trajectories - IQCD EoS 0.6 Correspondance $s/n_B \leftrightarrow$ $\mathbf{u}_{\mathbf{B}}^{\prime}/\mathbf{T} = \mathbf{u}_{\mathbf{B}}^{\prime}$ 420 s/n_B = 144 collisional energy II 1 94 0.5 s/n_B $\mu_B/T \neq 2$ $s/n_B = 420 \leftrightarrow 200 \text{ GeV}$ 500 5 0.4 = 144 ↔ 62.4 GeV [GeV] $\mu_{\rm B}/T = 3$ 0.3 = 94 ↔ 39 GeV $\mu_{B}/T = 4$ = 70 ↔ 27 GeV 0.2 $\mu_B/T = 5$ = 51 ↔ 19.6 GeV 0.1 = 30 ↔ 14.5 GeV 0.0 0.2 1.0 0.4 0.6 0.8 0.0 μ_B [GeV] EPJ Web Conf. 137 (2017) 07008

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Isentropic trajectories for (T, μ_B)

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Summary

 Resummed properties of the quasiparticles are specified by scalar complex self-energies:

gluon propagator: $\Delta^{-1} = P^2 - \Pi$ & quark propagator $S_q^{-1} = P^2 - \Sigma_q$ gluon self-energy: $\Pi = M_g^2 - i2g_g\omega$ & quark self-energy: $\Sigma_q = M_q^2 - i2g_q\omega$

- **Real part of the self-energy: thermal mass (M_g, M_q)**
- Imaginary part of the self-energy: interaction width of partons (γ_g , γ_q)

Peshier, Cassing, PRL 94 (2005) 172301; Cassing, NPA 791 (2007) 365: NPA 793 (2007)

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Introduction

Modeling of the quark/gluon masses and widths (inspired by HTL calculations)

$$M_g^2(T,\mu_B) = \frac{g^2(T,\mu_B)}{6} \left(\left(N_c + \frac{1}{2} N_f \right) T^2 + \frac{N_c}{2} \sum_q \frac{\mu_q^2}{\pi^2} \right)$$
$$M_{q(\bar{q})}^2(T,\mu_B) = \frac{N_c^2 - 1}{8N_c} g^2(T,\mu_B) \left(T^2 + \frac{\mu_q^2}{\pi^2} \right)$$
$$\gamma_{q(\bar{q})}(T,\mu_B) = \frac{1}{3} \frac{N_c^2 - 1}{2N_c} \frac{g^2(T,\mu_B)T}{8\pi} \ln \left(\frac{2c}{g^2(T,\mu_B)} + 1 \right)$$
$$\gamma_g(T,\mu_B) = \frac{1}{3} N_c \frac{g^2(T,\mu_B)T}{8\pi} \ln \left(\frac{2c}{g^2(T,\mu_B)} + 1 \right)$$

• Only one parameter (c = 14.4) + (
$$T$$
, μ_B)- dependent coupling constant to determine from lattice results

Introduction

T [GeV]

Scaling hypothesis at finite $\mu_B \approx 3\mu_a$

$$g^{2}(T/T_{c},\mu_{B}) = g^{2}\left(\frac{T^{*}}{T_{c}(\mu_{B})},\mu_{B}=0\right)$$

with the effective temperature

$$T^* = \sqrt{T^2 + \mu_q^2/\pi^2}$$

and the critical temperature at finite μ_B

$$T_c(\mu_B) = T_c \sqrt{1 - \alpha \mu_B^2}$$

0.15

0.20

0.25

0.30

T [GeV]

0.35

0.40

0.45

0.50

$$T_c(\mu_B) = T_c \sqrt{1 - \alpha \mu_B^2}$$

0.0

2

3

T/Tc(μ_B)

12

7

6

8 9 1 0

Blaizot, Iancu, Rebhan, Phys. Rev. D 63 (2001) 065003

Note: The contribution of longitudinal gluons is neglected in the calculation of thermodynamic quantities

Implementation in PHSD Results Summary

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QGP:

in equilibrium off equilibrium

Landau-matching condition:

Xu et al., Phys.Rev. C96 (2017), 024902

$$T^{\mu\nu}u_{\nu} = \epsilon u^{\mu} = (\epsilon g^{\mu\nu})u_{\nu}$$

Introduction

Calculation of the baryon current in each cells of the PHSD

$$J_B^{\mu} = \sum_{i} \frac{p_i^{\mu}}{E_i} \frac{(q_i - \bar{q}_i)}{3}$$

Lorentz transformation to obtain the local baryon density:

$$n_B = \gamma_E \left(J_B^0 - \vec{\beta_E} \cdot \vec{J_B} \right) = \frac{J_B^0}{\gamma_E}$$

with $\vec{\beta_E} = \vec{J_B} / J_B^0$ being the Eckart velocity.

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Illustration for HIC ($\sqrt{s_{NN}} = 17$ GeV)

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under extreme conditions

Introduction

R 21

under extreme conditions

Illustration for HIC ($\sqrt{s_{NN}} = 200 \text{ GeV}$) Strong-interaction matter under extreme conditions Au+Au 200GeV - 5% central $N_{cells}(T,\mu_B)/N_{cells}^{tot}$ [%] Au+Au 200GeV 0-5% central: x = y = 0 0.40 0.8 0.35 0.7 0.42 Temperature T [GeV] 0.30 t = 0.15 fm/c 0.6 0.25 t = 0.25 fm/c [GeV] 0.5 0.29 0.20 0.4 ⊢ 0.15 0.3 0.15 0.10 0.2 PHSD5.0 - |y_{cell}| < 1 0.05 0.1 t < 0.5 fm/c 0.015 -3 -2 2 -1 0 1 3 0.00 -0.025 0.000 0.025 0.050 0.075 **y**_{cell} μ_B [GeV]

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- μ_B obtained from a statistical analysis of exp. data
- $\square \mu_B \text{ probed in PHSD} \\ \text{simulations around} \\ \text{the chemical freeze} \\ \text{out temperature } T_{ch}$
- Two completely different quantities!!!

Summary

CRC-TR 211 Strong-interaction matter under extreme conditions

Implementation in PHSD Results

Summary

Traces of the QGP at finite μ_B in observables of heavy-ion collsions

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Comparison between three different results:

- **1)** PHSD 4.0 : only $\sigma(T)$ and M(T)
- **2)** PHSD 5.0 : with $\sigma(\sqrt{s}, T, \mu_B = 0)$ and $M(T, \mu_B = 0)$
- **3)** PHSD 5.0 : with $\sigma(\sqrt{s}, T, \mu_B)$ and $M(T, \mu_B)$

Results for HIC ($\sqrt{s_{NN}} = 200 \text{ GeV}$)

Introduction

2.5

3.0

Results for HIC ($\sqrt{s_{NN}} = 17$ GeV)

Implementation in PHSD Results

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Results for HIC ($\sqrt{s_{NN}} = 7.6$ GeV)

Implementation in PHSD

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Results

Summary

- $\Box \quad (T, \mu_B)$ -dependent cross sections and masses have been implemented in PHSD
- **u** High- μ_B regions are probed at low $\sqrt{s_{NN}}$ or high rapidity regions
- But, QGP fraction is small at low $\sqrt{s_{NN}}$: no effects seen in bulk observables
- Outlook:
 - > Study more sensitive probes to finite- μ_B dynamics
 - Use of a more sophisticated QuasiParticle Model with momentum dependent masses and widths
 - > Possible 1st order phase transition at larger μ_B ?

Thank you for your attention!

Energy density and baryon density

Illustration of the energy density and baryon density

