

Recent progress of nuclear dynamics studies with TDDFT

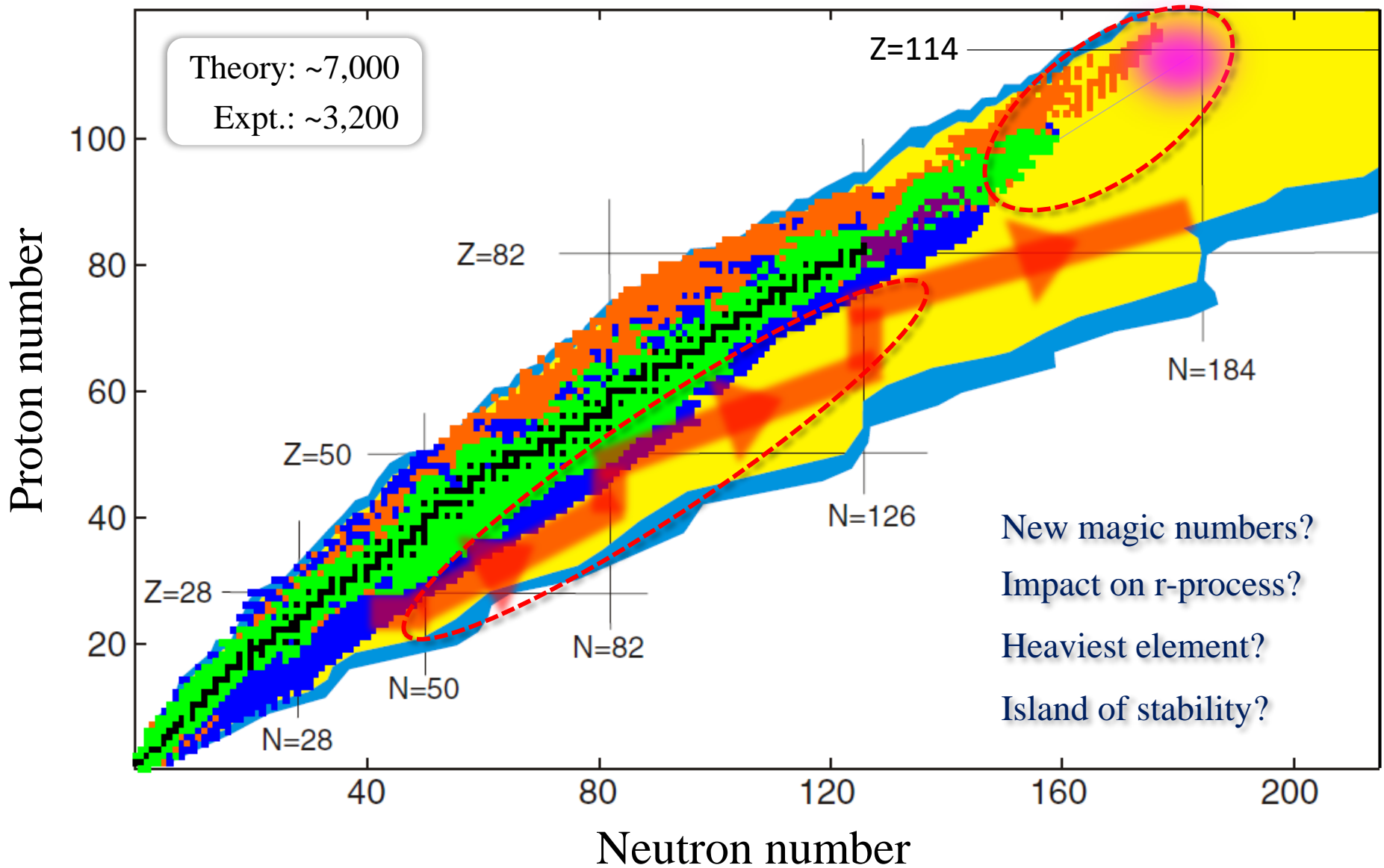
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Center for Interdisciplinary Research
Institute for Research Promotion, Niigata University, Japan

Progress #1

Development of “TDHF+GEMINI”
for unstable nucleus production

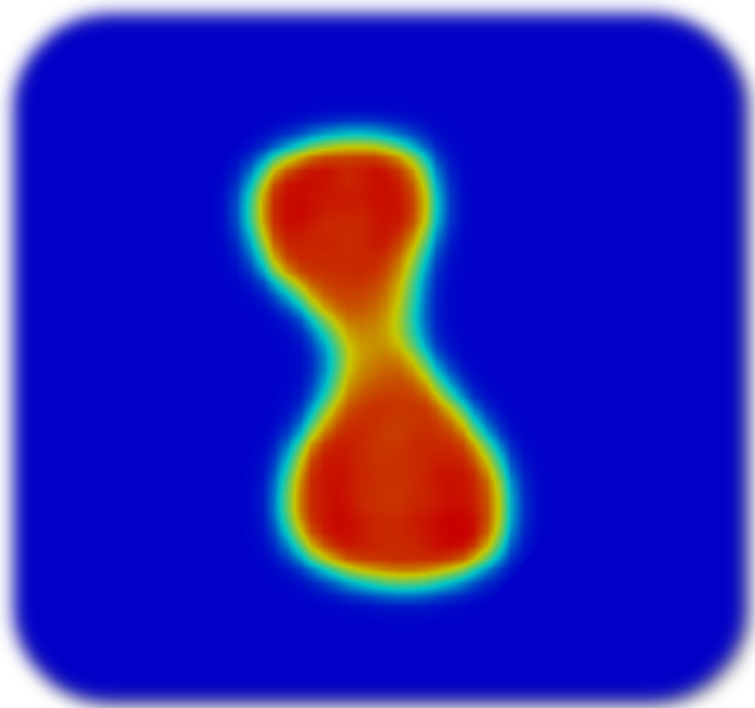
How can we create yet-unknown neutron-rich nuclei?



How to compute production cross sections?

We have developed: **TDDFT + PNP + GEMINI**

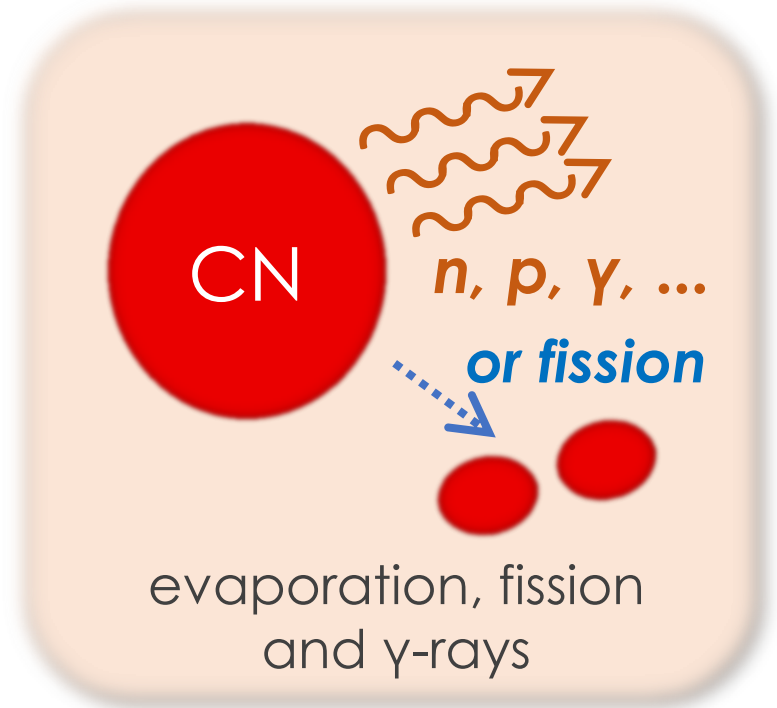
TDDFT



Reaction dynamics
(10^{-21} - 10^{-20} sec)

+

GEMINI++



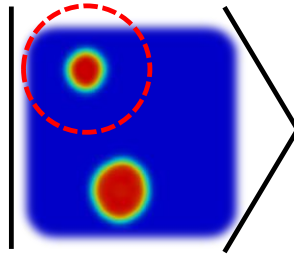
De-excitation
(10^{-18} - 10^{-16} sec)

How to compute production cross sections?

We have developed: **TDDFT + PNP + GEMINI**

✓ Particle number projection (PNP)

$$|\Phi_{N,Z}(b)\rangle = \hat{P}_N \hat{P}_Z |\Phi(b)\rangle = \hat{P}_N \hat{P}_Z$$



C. Simenel, PRL105(2010)192701

PNP operator:

$$\hat{P}_n = \frac{1}{2\pi} \int_0^{2\pi} e^{i(n - \hat{N}_V)\theta} d\theta$$

➤ Transfer probabilities and cross sections

KS and K. Yabana, PRC88(2013)014614

$$P_{N,Z}(b) = \langle \Phi_{N,Z}(b) | \Phi_{N,Z}(b) \rangle = P_N(b) P_Z(b)$$



$$\sigma_{N,Z} = 2\pi \int b P_{N,Z}(b) db$$

➤ Expectation values

KS and K. Yabana, PRC90(2014)064614

$$\mathcal{O}_{N,Z}(b) = \frac{\langle \Phi_{N,Z}(b) | \hat{O}_V | \Phi_{N,Z}(b) \rangle}{\langle \Phi_{N,Z}(b) | \Phi_{N,Z}(b) \rangle}$$



$$J_{N,Z}(b), E_{N,Z}^*(b)$$

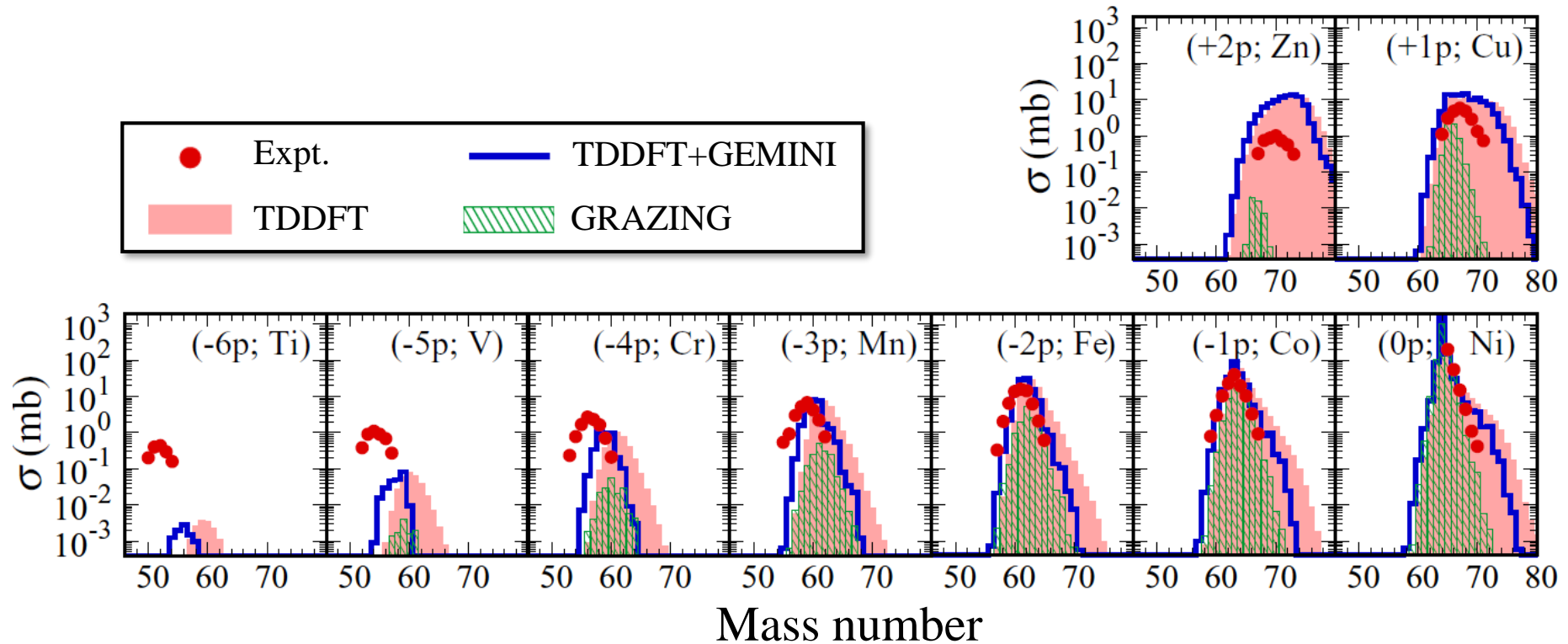
Inputs for a statistical model

➤ Secondary deexcitation processes

KS, PRC96(2017)014615

Evaporation/Fission/Gamma by GEMINI++ [R.J. Charity, PRC82(2010)014610]

Production cross section for projectile-like fragments



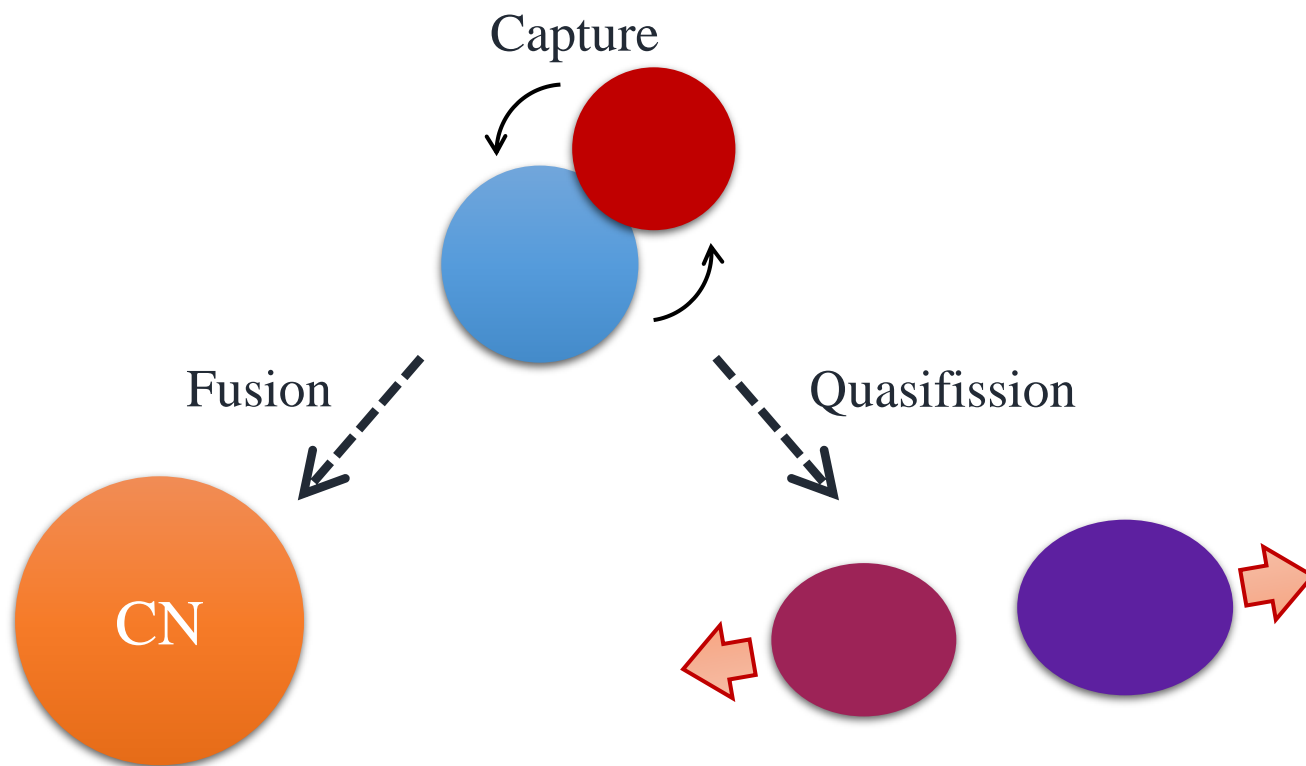
Expt.: L. Corradi et al., PRC59(1999)261

Progress #2

Study of Quasifission dynamics

Quasifission process

A fast ($\sim 10^{-21}$ - 10^{-20} sec) fission process before compound nucleus formation (fusion)

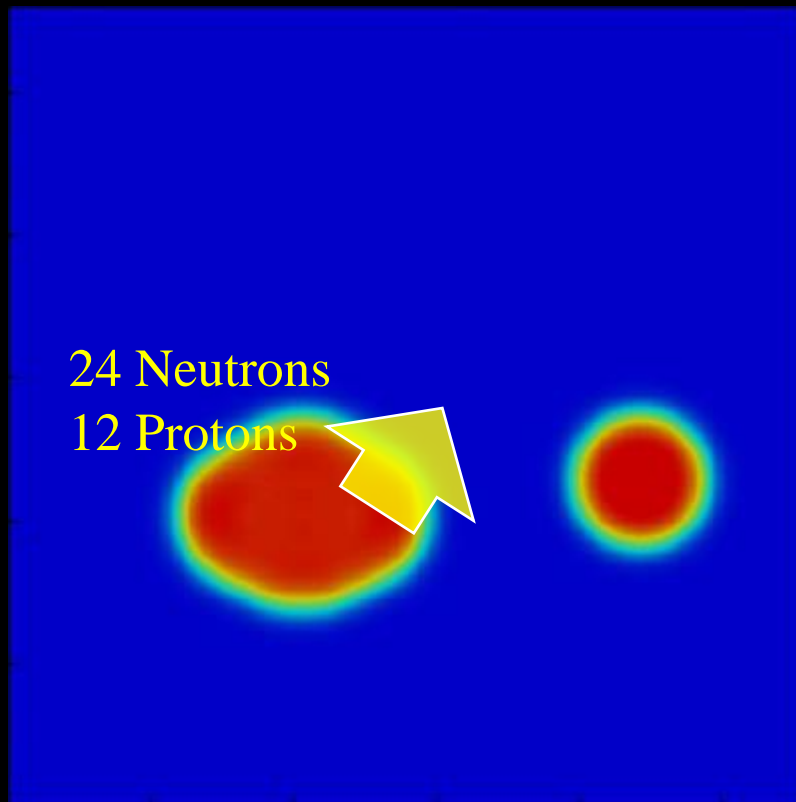


$$\sigma_{ER} \sim W_{\text{surv}} * \sigma_{\text{cap}} * P_{\text{CN}}$$

Quasifission dynamics in TDHF

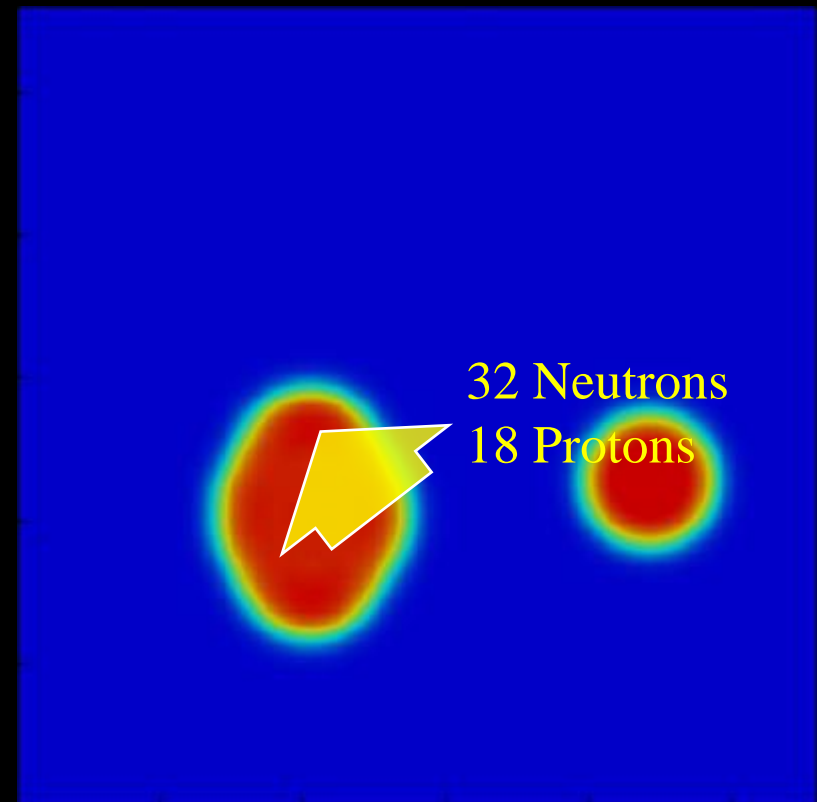
Tip collision

Shell effects of ^{208}Pb



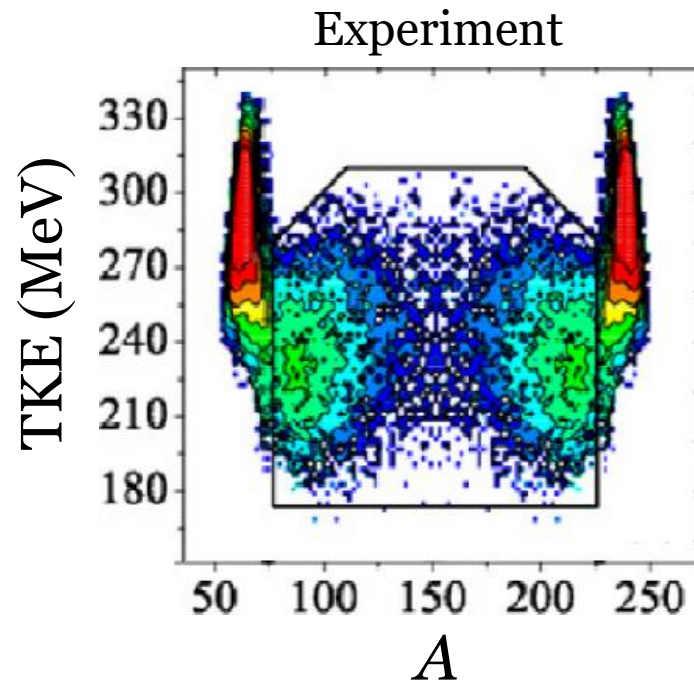
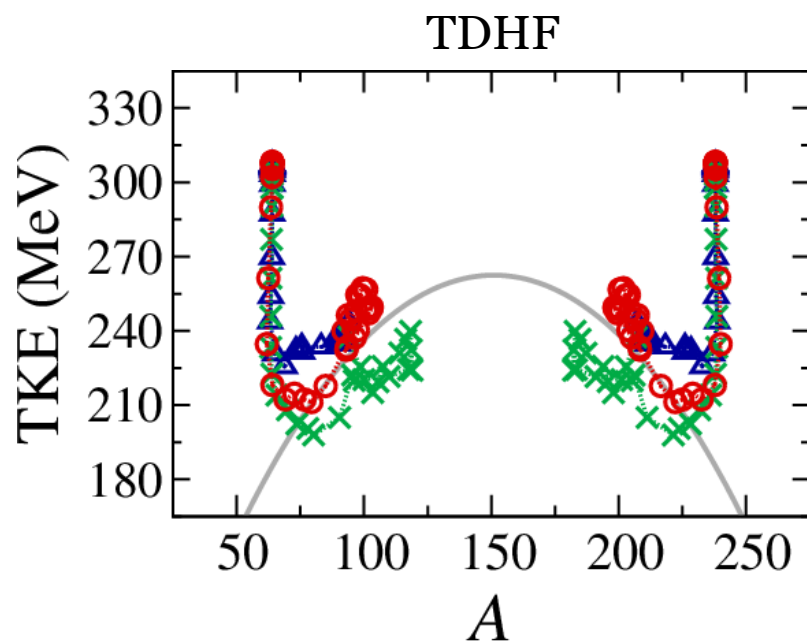
Side collision

More mass-symmetric



TDHF provides quantitative description of quasifission dynamics

TKE-A distribution: Comparison with experimental data

Expt.: E.M. Kozulin *et al.*, PLB686(2010)227

Progress #3

Quantitative description of the mass width in DIC

This work is based on our recent PRL paper:


PHYSICAL REVIEW LETTERS **120**, 022501 (2018)

**Exploring Zeptosecond Quantum Equilibration Dynamics:
From Deep-Inelastic to Fusion-Fission Outcomes in $^{58}\text{Ni} + ^{60}\text{Ni}$ Reactions**

E. Williams,^{1,*} K. Sekizawa,² D. J. Hinde,¹ C. Simenel,¹ M. Dasgupta,¹ I. P. Carter,¹ K. J. Cook,¹ D. Y. Jeung,¹
S. D. McNeil,¹ C. S. Palshetkar,^{1,†} D. C. Rafferty,¹ K. Ramachandran,^{1,‡} and A. Wakhle¹

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 (Received 16 August 2017; revised manuscript received 27 October 2017; published 10 January 2018)

performed in collaboration with *Australian National University (ANU)*



E. Williams



D.J. Hinde



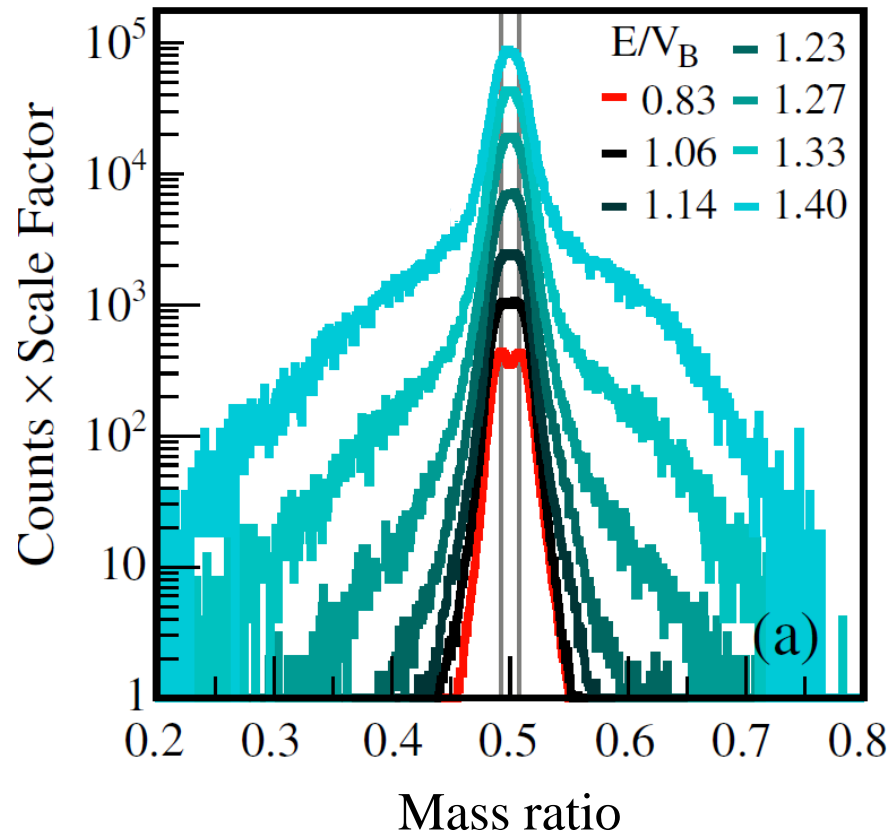
M. Dasgupta



C. Simenel



Mass distributions of $^{58}\text{Ni}+^{60}\text{Ni}$ at various energies



Mass ratio:

$$M_R = \frac{M_i}{M_1 + M_2}$$

Variational space can be controlled by “state” and “observable”

- The action-like quantity defined by Balian and Vénéroni

$$J = \text{Tr} [\hat{A}(t_1) \hat{D}(t_1)] - \int_{t_0}^{t_1} \text{Tr} \left[\hat{A}(t) \left(\frac{d\hat{D}(t)}{dt} + i[\hat{H}(t), \hat{D}(t)] \right) \right] dt$$

$\hat{D}(t)$: describes the state of the system

$\hat{A}(t)$: describes the evolution of the observable in the Heisenberg picture

R. Balian and M. Vénéroni, Phys. Rev. Lett. **47**, 1353 (1981); Ann. Phys. **216**, 351 (1992).
C. Simenel, Phys. Rev. Lett. **106**, 112501 (2011); Eur. Phys. J. A **48**, 152 (2012).

- **Unrestricted variation** (w.r.t. either A or D)



TDSE

- **Slater determinant** & one-body observable



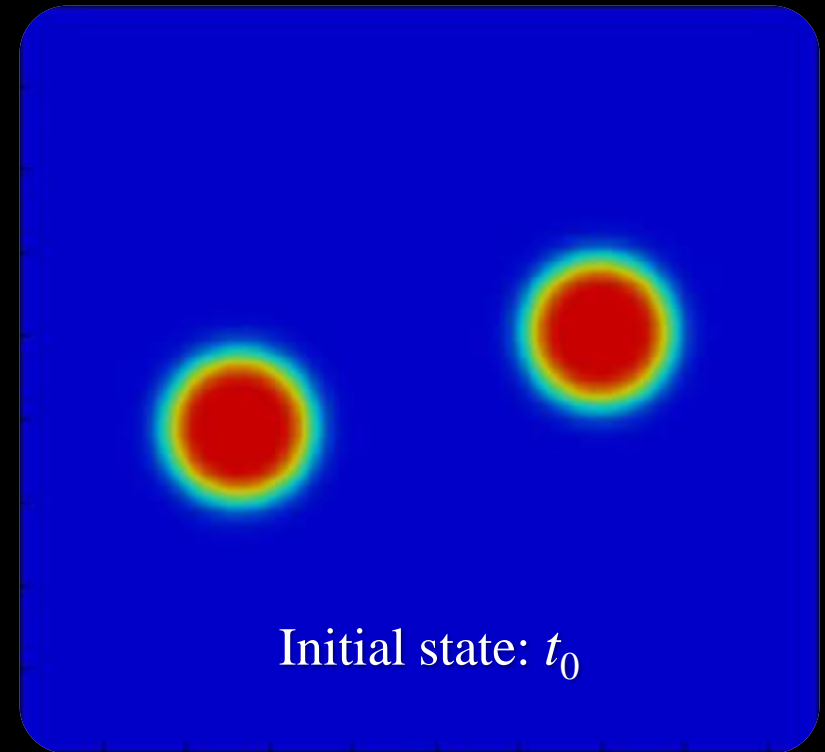
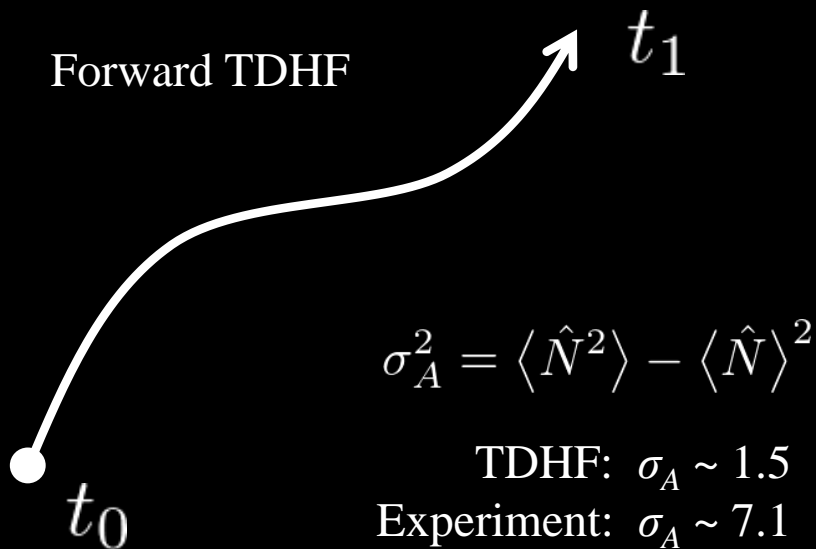
TDHF

- **Slater determinant** & fluctuations of one-body observable



TDRPA

Numerical implementation of BV prescription for the mass width

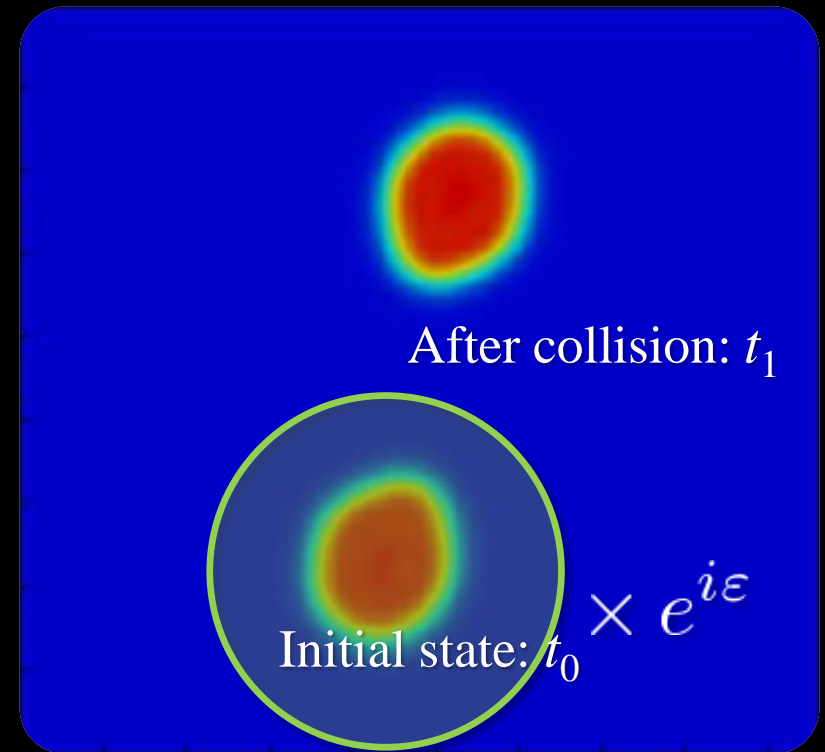
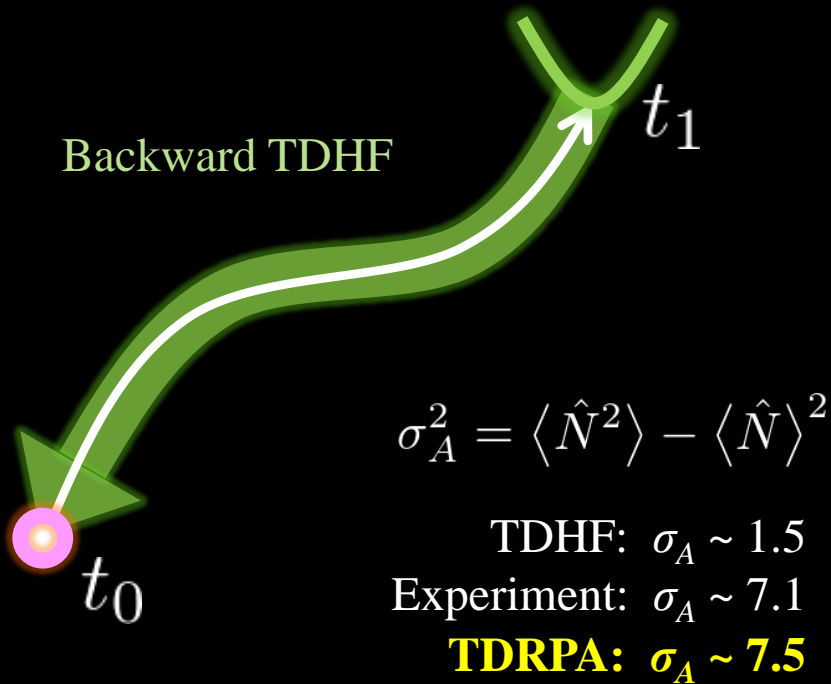


Numerical implementation of BV prescription for the mass width

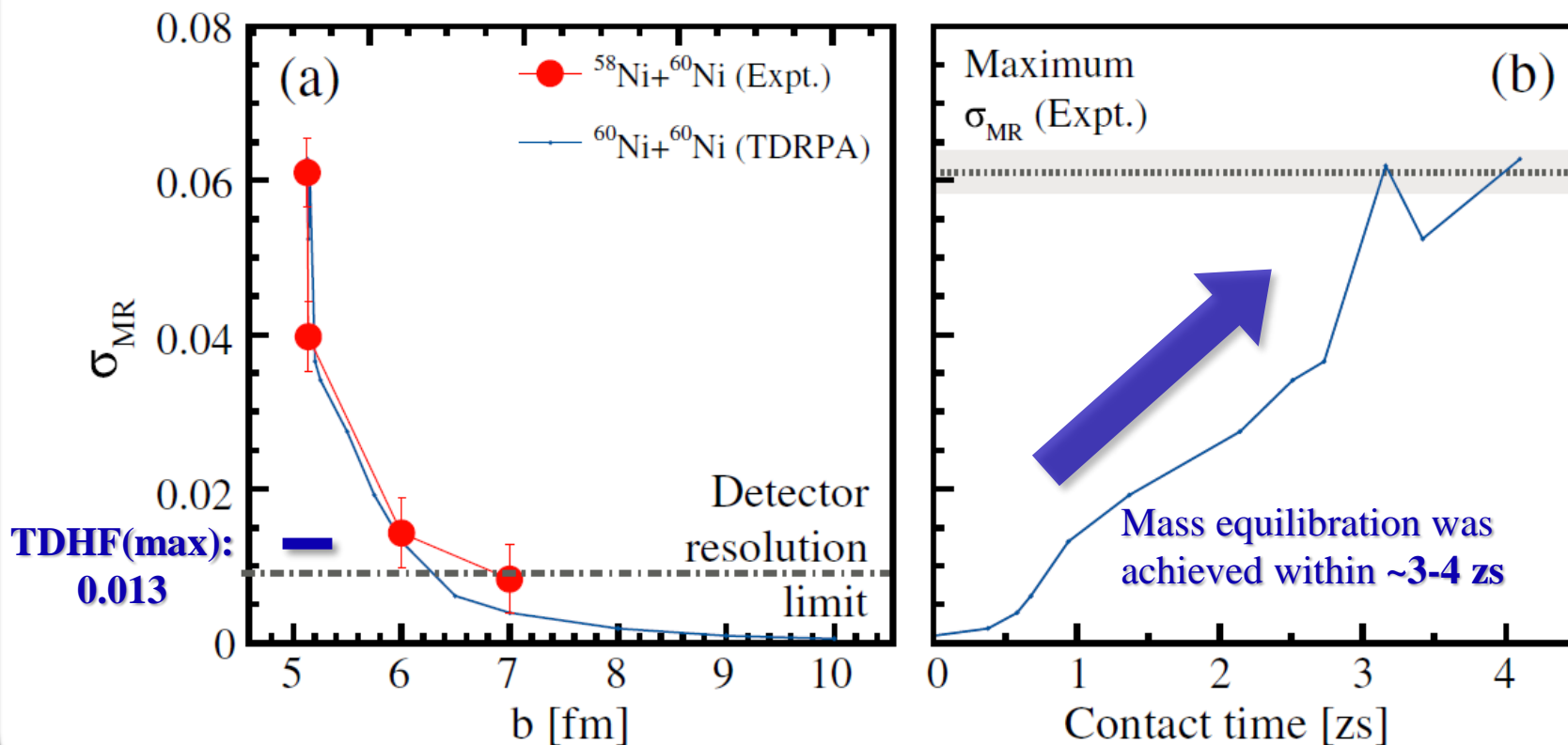
The Balian-Vénéroni prescription:

$$\sigma_X^2(t_1) = \lim_{\varepsilon \rightarrow 0} \frac{\text{Tr}\{[\rho(t_0) - \rho_X(t_0, \varepsilon)]^2\}}{2\varepsilon^2}$$

$$\rho_X(t_1, \varepsilon) = e^{i\varepsilon\hat{X}} \rho(t_1) e^{-i\varepsilon\hat{X}}$$

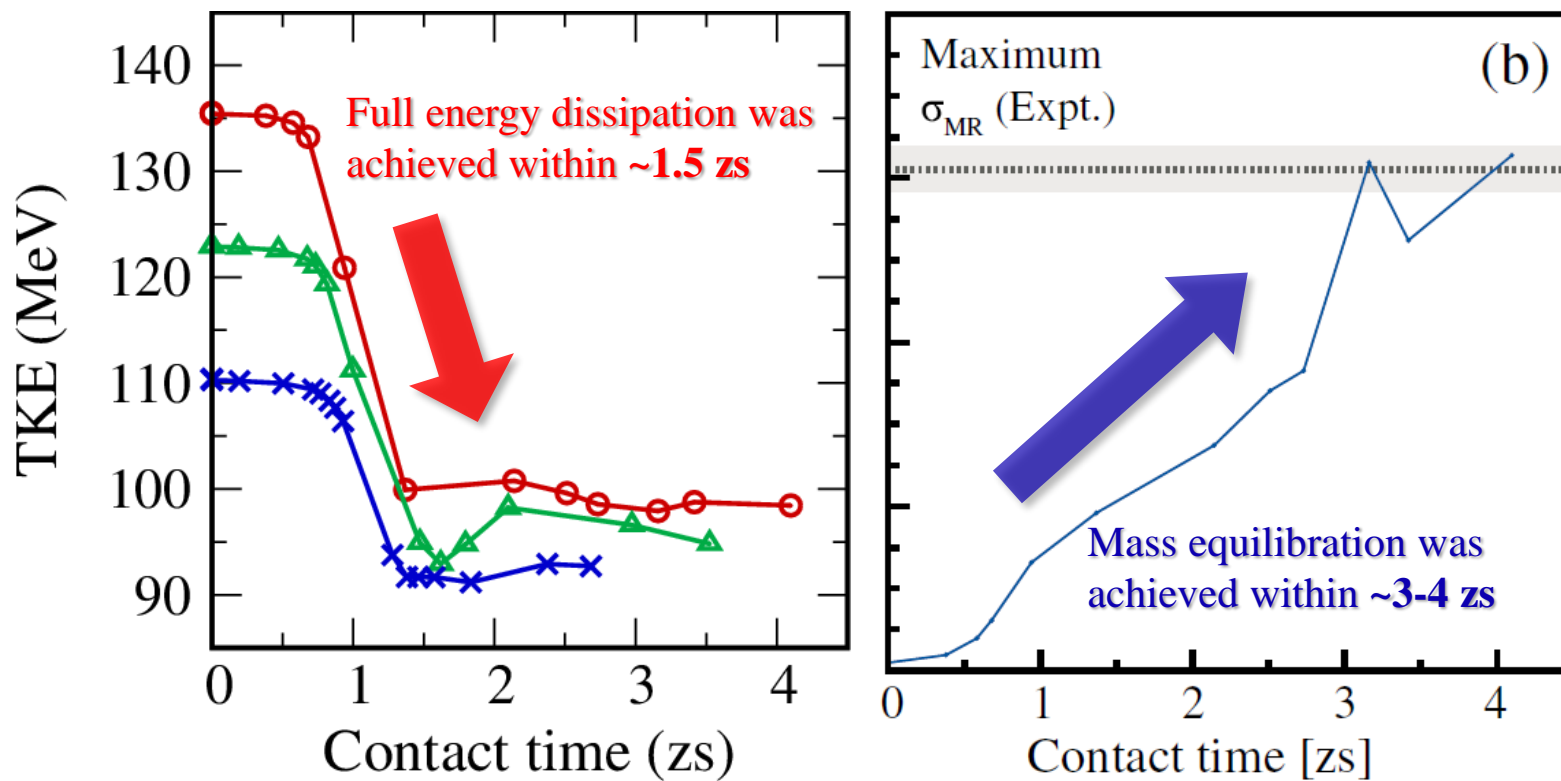


TDRPA quantitatively reproduced the experimental data

Width of the mass ratio distribution, σ_{MR} : Expt. vs Theory

TDRPA quantitatively reproduced the experimental data

Width of the mass ratio distribution, σ_{MR} : Expt. vs Theory



What's more?

Inclusion of pairing - TDSLDA

TDSLDA: TDDFT with local treatment of pairing

Kohn-Sham scheme is extended for non-interacting quasiparticles

➤ TDSLDA equations (formally equivalent to TDHFB or TD-BdG equations)

$$i\hbar \frac{\partial}{\partial t} \begin{pmatrix} u_{k,\uparrow}(\mathbf{r}, t) \\ u_{k,\downarrow}(\mathbf{r}, t) \\ v_{k,\uparrow}(\mathbf{r}, t) \\ v_{k,\downarrow}(\mathbf{r}, t) \end{pmatrix} = \begin{pmatrix} h_{\uparrow\uparrow}(\mathbf{r}, t) & h_{\uparrow\downarrow}(\mathbf{r}, t) & 0 & \Delta(\mathbf{r}, t) \\ h_{\downarrow\uparrow}(\mathbf{r}, t) & h_{\downarrow\downarrow}(\mathbf{r}, t) & -\Delta(\mathbf{r}, t) & 0 \\ 0 & -\Delta^*(\mathbf{r}, t) & -h_{\uparrow\uparrow}^*(\mathbf{r}, t) & -h_{\uparrow\downarrow}^*(\mathbf{r}, t) \\ \Delta^*(\mathbf{r}, t) & 0 & -h_{\downarrow\uparrow}^*(\mathbf{r}, t) & -h_{\downarrow\downarrow}^*(\mathbf{r}, t) \end{pmatrix} \begin{pmatrix} u_{k,\uparrow}(\mathbf{r}, t) \\ u_{k,\downarrow}(\mathbf{r}, t) \\ v_{k,\uparrow}(\mathbf{r}, t) \\ v_{k,\downarrow}(\mathbf{r}, t) \end{pmatrix}$$

$$h_{\sigma} = \frac{\delta E}{\delta n_{\sigma}} \quad : \text{ s.p. Hamiltonian}$$

$$\Delta = -\frac{\delta E}{\delta \nu^*} \quad : \text{ pairing field}$$

$$n_{\sigma}(\mathbf{r}, t) = \sum_{E_k < E_c} |v_{k,\sigma}(\mathbf{r}, t)|^2 \quad : \text{ number density}$$

$$\nu(\mathbf{r}, t) = \sum_{E_k < E_c} u_{k,\uparrow}(\mathbf{r}, t) v_{k,\downarrow}^*(\mathbf{r}, t) \quad : \text{ anomalous density}$$

$$\mathbf{j}_{\sigma}(\mathbf{r}, t) = \hbar \sum_{E_k < E_c} \text{Im}[v_{k,\sigma}^*(\mathbf{r}, t) \nabla v_{k,\sigma}(\mathbf{r}, t)] \quad : \text{ current}$$

A large number (10^4 - 10^6) of 3D coupled non-linear PDEs have to be solved!!

of qp orbitals ~ # of grid points

TDSLDA: TDDFT with local treatment of pairing

Kohn-Sham scheme is extended for non-interacting quasiparticles

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Supercomputing!!

$$h_{\sigma} = \frac{\delta E}{\delta n_{\sigma}} : \text{s.p. Hamiltonian}$$

$$n_{\sigma}(\mathbf{r}, t) = \sum_{E_k < E_c} |v_{k,\sigma}(\mathbf{r}, t)|^2 : \text{number density}$$

$$\nu(\mathbf{r}, t) = \sum_{E_k < E_c} u_{k,\uparrow}(\mathbf{r}, t) v_{k,\downarrow}^*(\mathbf{r}, t) : \text{anomalous density}$$

$$\Delta = -\frac{\delta E}{\delta \nu^*} : \text{pairing field}$$

$$\mathbf{j}_{\sigma}(\mathbf{r}, t) = \hbar \sum_{E_k < E_c} \text{Im}[v_{k,\sigma}^*(\mathbf{r}, t) \nabla v_{k,\sigma}(\mathbf{r}, t)] : \text{current}$$

A large number (10⁴-10⁶) of 3D coupled non-linear PDEs have to be solved!!

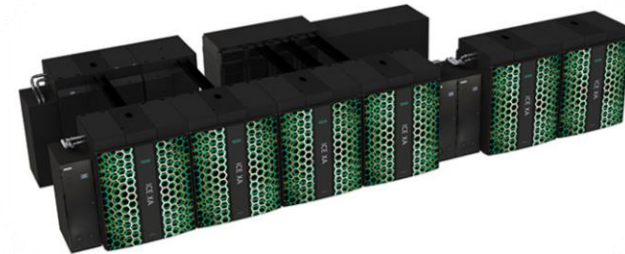
of qp orbitals ~ # of grid points

*The number indicates the rank according to the TOP500 list (June 2018)

Piz Daint, CSCS, Switzerland (No. 6)

TITAN, ORNL, USA (No. 7)

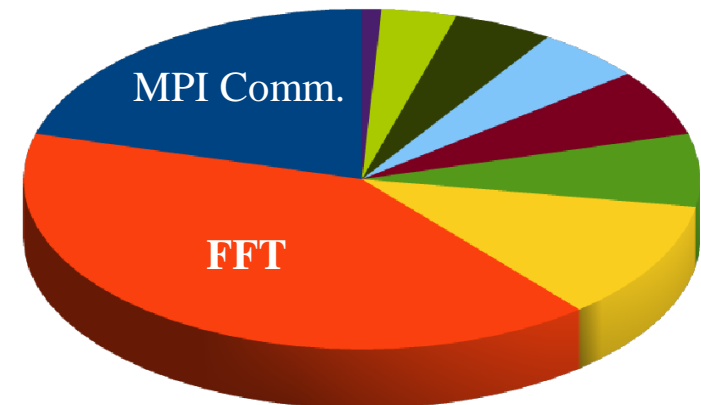
TSUBAME3.0, Japan (No. 19)



**The fastest machine:
Summit, ORNL, USA
GPU, 188 PFlops/s**

Present computing capabilities:

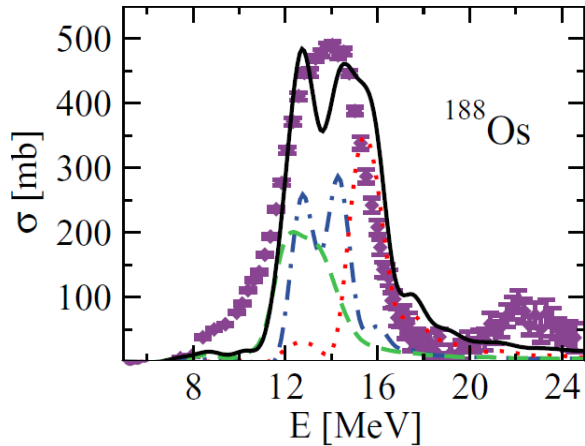
- ✓ Full 3D (w/o symmetry restrictions)
- ✓ Volume as large as 100^3 lattice points
- ✓ Evolution up to 10^6 time steps (as long as 10^{-19} sec)



■ MPI communication ■ FFT
■ Multiply vectors by momentum (kx,ky,kz) ■ Compute and subtract qpe
■ Other ■ Normalize wave-functions
■ ABM formulas (predictor, corrector) ■ Construct densities
■ Compute potentials

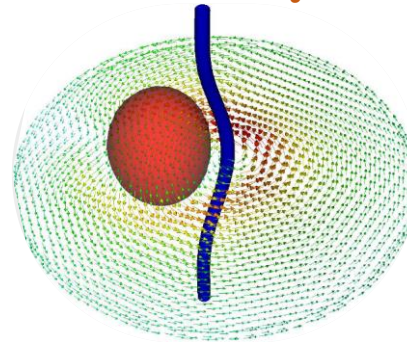
TDSLDA is a versatile tool!!

IVGDR



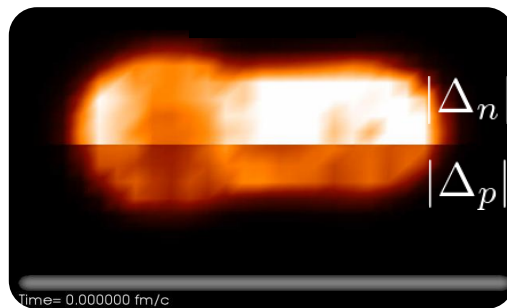
Phys. Rev. C **84**, 051309(R) (2011)
I. Stetcu, A. Bulgac, P. Magierski, and K.J. Roche

Vortex-nucleus dynamics



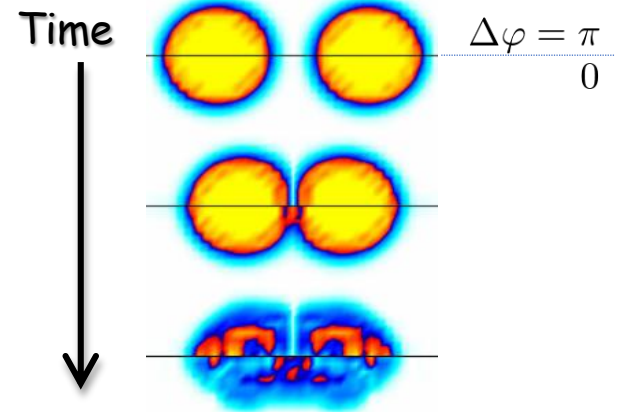
Phys. Rev. Lett. **117**, 232701 (2016)
G. Wlazłowski, K.S., P. Magierski, A. Bulgac, and M.M. Forbes

Induced fission of ²⁴⁰Pu



Phys. Rev. Lett. **116**, 122504 (2016)
A. Bulgac, P. Magierski, K.J. Roche, and I. Stetcu

Low-energy heavy ion reactions



Phys. Rev. Lett. **119**, 042501 (2017)
P. Magierski, K.S., and G. Wlazłowski

Takeaway message

- ✓ One-body dissipation and fluctuation, together with the pairing, may be sufficient to describe various nuclear dynamics

Dynamic effects of pairing

TDHFB

Solitonic excitations, quantum vortices,
inner crust of neutron stars,

Main reaction outcomes

...

Fluctuations/correlations

TDHF

Average number of nucleons,
TKE, scattering angles,
contact times, ...

TDRPA

Width of mass, charge distributions,
correlation between n/p transfers,
...

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