

Flaxion

a minimal extension to solve puzzles in the standard model

Koichi Hamaguchi (University of Tokyo)

@Moriond EW 2018, Mar. 13, 2018

Based on

Y. Ema, KH, T. Moroi, K. Nakayama, arXiv:1612.05492 [JHEP 1701 (2017) 096],

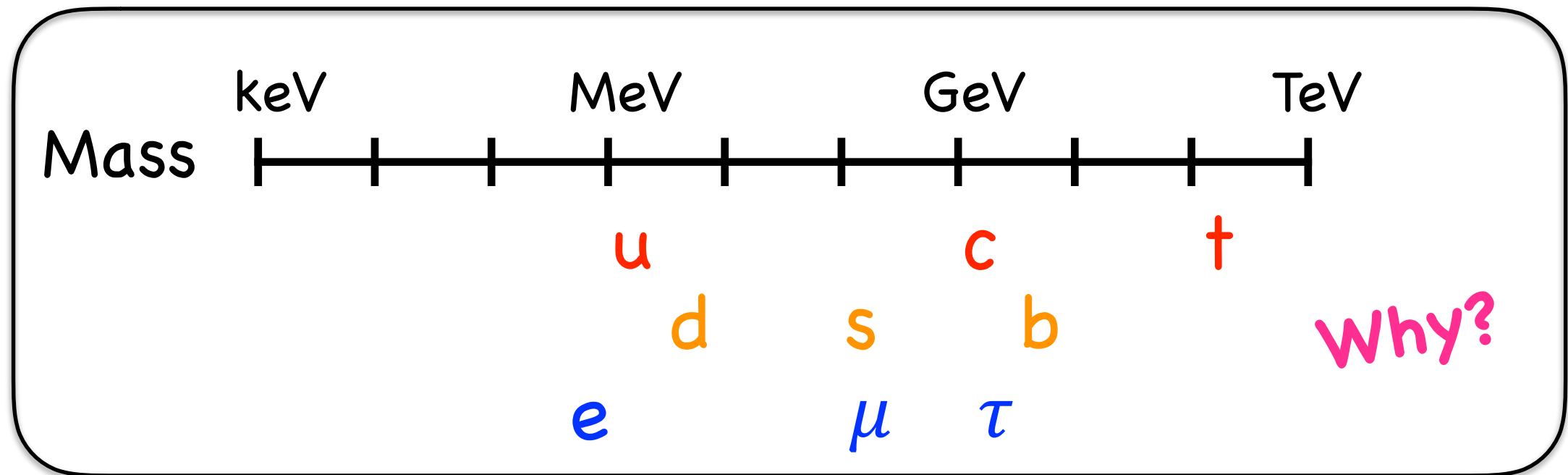
Y. Ema, D. Hagiwara, KH, T. Moroi, K. Nakayama, arXiv:1802.07739.

Summary:

$$U(1)_{FN} = U(1)_{PQ}$$

Summary:

We proposed a new model (scenario) that explains the hierarchical flavor structure of quarks/leptons,



and solves the strong CP problem,

$$\mathcal{L}_\theta = \frac{\alpha_s}{8\pi} \theta F_a^{\mu\nu} \tilde{F}_{a\mu\nu}, \quad \bar{\theta} = \theta + \arg \det m_q$$

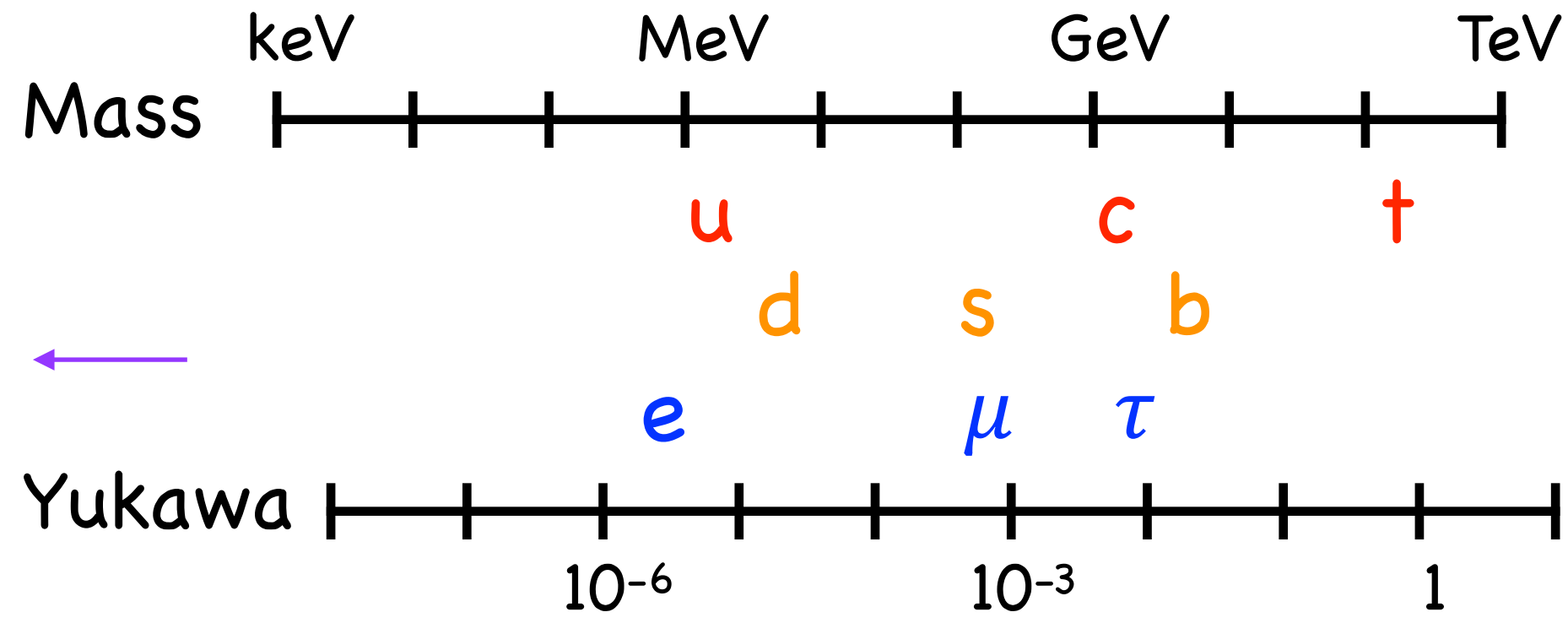
$$|\bar{\theta}| \lesssim 10^{-10} \text{ from neutron EDM}$$

Why?

and includes DM, Leptogenesis, and Inflation.

Q: What's the origin of the quark and lepton mass hierarchy and mixings ??

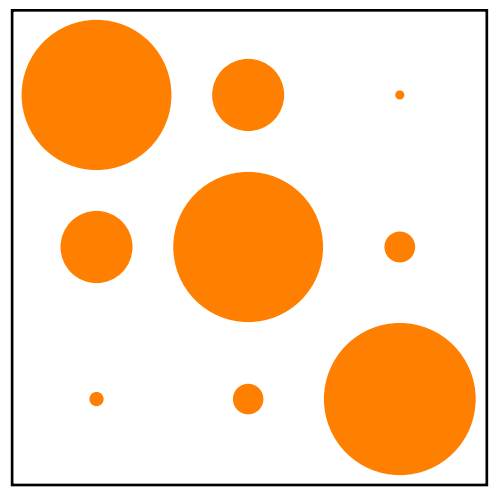
cf. Talks by
R. Alonso
J. Fuentes-Martín
 on Sunday.



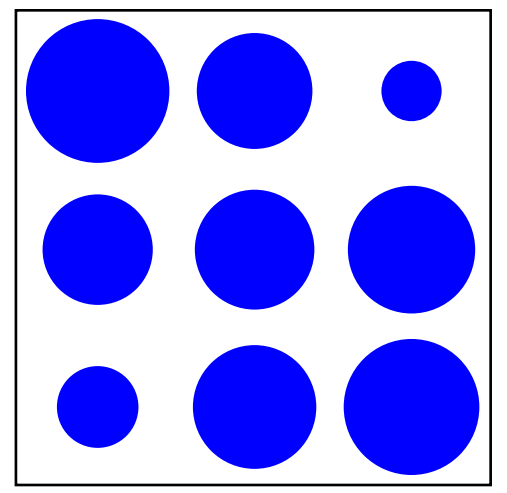
$$\hat{y}_{ij}^u \overline{Q}_i H u_{Rj}$$

large hierarchy

quark mixing



neutrino mixing



A simple possibility:

a spontaneously broken global U(1) symmetry. [Froggatt-Nielsen,'79]

$$\hat{y}_{ij}^u \overline{Q}_i H u_{Rj}$$



up-type quark
Yukawa couplings
in the Standard Model

A simple possibility:

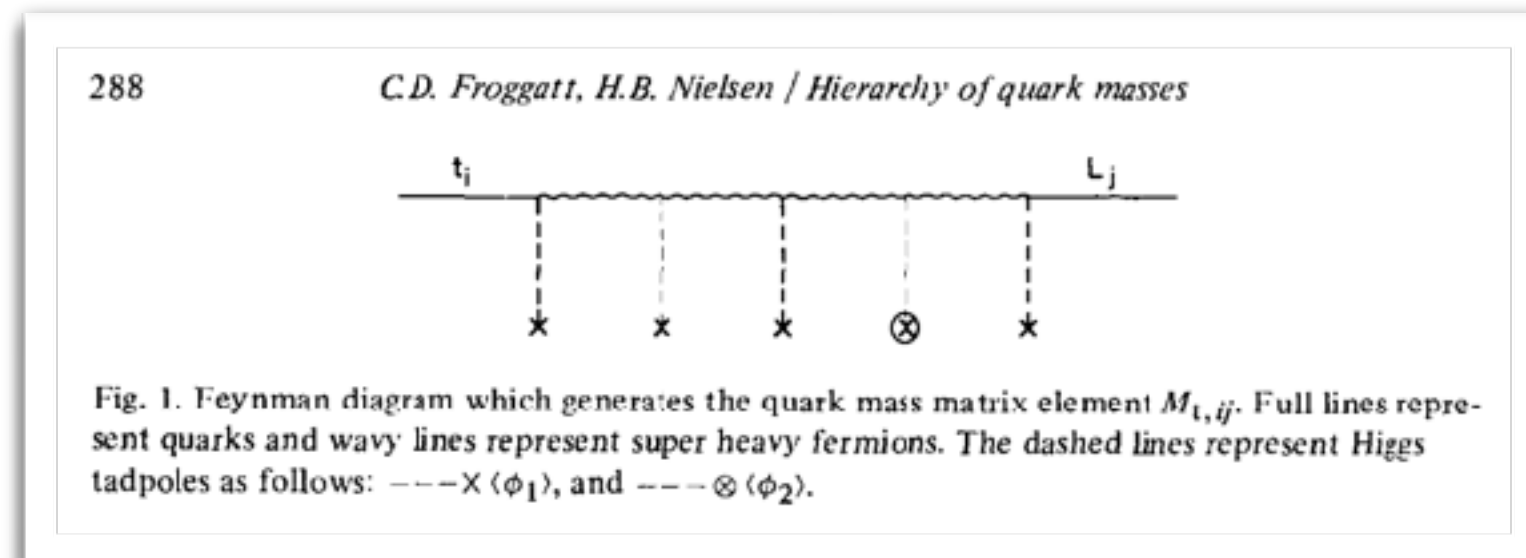
a spontaneously broken global U(1) symmetry. [Froggatt-Nielsen,'79]

	Q_i	u_{Rj}	H	ϕ ← New complex scalar:
U(1) charge	q_{Q_i}	q_{u_j}	0	+1 Flavon

$$\cancel{\hat{y}_{ij}^u \overline{Q}_i H u_{Rj}} \quad \longrightarrow \quad y_{ij}^u \left(\frac{\phi}{M} \right)^{q_{Q_i} - q_{u_j}} \overline{Q}_i H u_{Rj}$$

cutoff scale

up-type quark
Yukawa couplings
in the Standard Model



A simple possibility:

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	Q_i	u_{Rj}	H	ϕ ← New complex scalar:
U(1) charge	q_{Q_i}	q_{u_j}	0	+1

Flavon

$$\cancel{\hat{y}_{ij}^u \overline{Q}_i H u_{Rj}} \longrightarrow y_{ij}^u \left(\frac{\langle \phi \rangle}{M} \right)^{q_{Q_i} - q_{u_j}} \overline{Q}_i H u_{Rj}$$

→ After U(1) breaking by $\langle \phi \rangle \neq 0$,

$$m_{ij}^u = y_{ij}^u \underbrace{\epsilon^{q_{Q_i} - q_{u_j}} \langle H \rangle}_{\text{Mass hierarchy and mixings}}$$

↑
O(1)

where $\frac{\langle \phi \rangle}{M} \equiv \epsilon < 1$

Example:

$$q_Q = \{3, 2, 0\}, q_u = \{-5, -1, 0\}$$

$$\rightarrow m^u \sim \begin{pmatrix} \epsilon^8 & \epsilon^4 & \epsilon^3 \\ \epsilon^7 & \epsilon^3 & \epsilon^2 \\ \epsilon^5 & \epsilon & 1 \end{pmatrix}$$

↑ ↑ ↑
up charm top

A simple possibility:

a spontaneously broken global U(1) symmetry. [Froggatt-Nielsen,'79]

Our setup:

$$\begin{aligned}\mathcal{L} = & y_{ij}^d \left(\frac{\phi}{M}\right)^{n_{ij}^d} \bar{Q}_i H d_{Rj} + y_{ij}^u \left(\frac{\phi}{M}\right)^{n_{ij}^u} \bar{Q}_i \tilde{H} u_{Rj} \\ & + y_{ij}^l \left(\frac{\phi}{M}\right)^{n_{ij}^l} \bar{L}_i H l_{Rj} + y_{i\alpha}^\nu \left(\frac{\phi}{M}\right)^{n_{i\alpha}^\nu} \bar{L}_i \tilde{H} N_{R\alpha} \\ & + \frac{1}{2} y_{\alpha\beta}^N \left(\frac{\phi}{M}\right)^{n_{\alpha\beta}^N} M \overline{N_{R\alpha}^c} N_{R\beta} + \text{h.c.}\end{aligned}$$

We also introduce
2 or 3 right-handed neutrinos.

where $\frac{\langle\phi\rangle}{M} \equiv \epsilon \simeq 0.2$

$$\begin{cases} n_{ij}^u = q_{Q_i} - q_{u_j}, \\ n_{ij}^d = q_{Q_i} - q_{d_j}, \\ n_{ij}^l = q_{L_i} - q_{l_j}, \\ n_{i\alpha}^\nu = q_{L_i} - q_{N_\alpha} \\ n_{\alpha\beta}^N = -q_{N_\alpha} - q_{N_\beta}. \end{cases}$$

A simple possibility:

a spontaneously broken global U(1) symmetry. [Froggatt-Nielsen,'79]

Then, **Quark** mass hierarchy as well as **CKM** angles are naturally explained as e.g.,

$$\begin{cases} q_Q = \{3, 2, 0\}, \\ q_u = \{-5, -1, 0\}, \\ q_d = \{-4, -3, -3\} \end{cases} \rightarrow \begin{cases} m_{ij}^u \sim \begin{pmatrix} \epsilon^8 & \epsilon^4 & \epsilon^3 \\ \epsilon^7 & \epsilon^3 & \epsilon^2 \\ \epsilon^5 & \epsilon & 1 \end{pmatrix} \langle H \rangle, \\ m_{ij}^d \sim \begin{pmatrix} \epsilon^7 & \epsilon^6 & \epsilon^6 \\ \epsilon^6 & \epsilon^5 & \epsilon^5 \\ \epsilon^4 & \epsilon^3 & \epsilon^3 \end{pmatrix} \langle H \rangle, \end{cases} \rightarrow \begin{cases} \text{diag}(m_u) \sim (\epsilon^8, \epsilon^3, 1) \langle H \rangle, & \mathbf{u, c, t} \\ \text{diag}(m_d) \sim (\epsilon^7, \epsilon^5, \epsilon^3) \langle H \rangle, & \mathbf{d, s, b} \\ V_{\text{CKM}} \sim \begin{pmatrix} 1 & \epsilon & \epsilon^3 \\ \epsilon & 1 & \epsilon^2 \\ \epsilon^3 & \epsilon^2 & 1 \end{pmatrix} \end{cases}$$

A simple possibility:

a spontaneously broken global U(1) symmetry. [Froggatt-Nielsen,'79]

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Lepton masses and **MNS** angles are also explained as

$$\begin{cases} q_L = \{1, 0, 0\}, \\ q_e = \{-8, -5, -3\}, \\ q_N = \{q_{N_1}, q_{N_2}, (q_{N_3})\} \end{cases} \rightarrow \begin{cases} m_{ij}^\ell \sim \begin{pmatrix} \epsilon^9 & \epsilon^6 & \epsilon^4 \\ \epsilon^8 & \epsilon^5 & \epsilon^3 \\ \epsilon^8 & \epsilon^5 & \epsilon^3 \end{pmatrix} \langle H \rangle, \\ m_{ij}^\nu \sim \begin{pmatrix} \epsilon^2 & \epsilon & \epsilon \\ \epsilon & 1 & 1 \\ \epsilon & 1 & 1 \end{pmatrix} \frac{\langle H \rangle^2}{M}, \end{cases} \rightarrow \begin{cases} \text{diag}(m_e) \sim (\epsilon^9, \epsilon^5, \epsilon^3) \langle H \rangle, & \mathbf{e, \mu, \tau} \\ \text{diag}(m_\nu) \sim (\epsilon^2, 1, 1) \frac{\langle H \rangle^2}{M}, \\ V_{\text{MNS}} \sim \begin{pmatrix} 1 & \epsilon & \epsilon \\ \epsilon & 1 & 1 \\ \epsilon & 1 & 1 \end{pmatrix} \end{cases}$$

q_N -dependence cancels

because of the **seesaw** formula.

large 2-3 mixing

[cf. Sato-Yanagida,'98, Ramond,'98]

Standard Model

Quark and lepton
mass hierarchy
and mixings.

Neutrino
masses
and mixings.

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Standard Model

+ **one complex scalar
with $U(1)_F$**

ϕ : flavon

+ 2 (or 3)
right-handed
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seesaw

Our setup:

$$\mathcal{L} = y_{ij}^d \left(\frac{\phi}{M}\right)^{n_{ij}^d} \bar{Q}_i H d_{Rj} + y_{ij}^u \left(\frac{\phi}{M}\right)^{n_{ij}^u} \bar{Q}_i \tilde{H} u_{Rj}$$

$$+ y_{ij}^l \left(\frac{\phi}{M}\right)^{n_{ij}^l} \bar{L}_i H l_{Rj} + y_{i\alpha}^\nu \left(\frac{\phi}{M}\right)^{n_{i\alpha}^\nu} \bar{L}_i \tilde{H} N_{R\alpha}$$

$$+ \frac{1}{2} y_{\alpha\beta}^N \left(\frac{\phi}{M}\right)^{n_{\alpha\beta}^N} M \overline{N_{R\alpha}^c} N_{R\beta} + \text{h.c.}$$

can explain the quark and lepton mass hierarchy and mixings.

OK, but..... **What's new?**

Froggatt-Nielsen paper was in 1979.....

Our setup:

$$\mathcal{L} = y_{ij}^d \left(\frac{\phi}{M} \right)^{n_{ij}^d} \bar{Q}_i H d_{Rj} + y_{ij}^u \left(\frac{\phi}{M} \right)^{n_{ij}^u} \bar{Q}_i \tilde{H} u_{Rj}$$

$$+ y_{ij}^l \left(\frac{\phi}{M} \right)^{n_{ij}^l} \bar{L}_i H l_{Rj} + y_{i\alpha}^\nu \left(\frac{\phi}{M} \right)^{n_{i\alpha}^\nu} \bar{L}_i \tilde{H} N_{R\alpha}$$

$$+ \frac{1}{2} y_{\alpha\beta}^N \left(\frac{\phi}{M} \right)^{n_{\alpha\beta}^N} M \overline{N_{R\alpha}^c} N_{R\beta} + \text{h.c.}$$

POINT: The global, spontaneously broken U(1) flavor symmetry is **anomalous** under SU(3)_c, which means... the Peccei-Quinn mechanism (to solve the strong CP problem) is automatically included:

$$U(1)_F = U(1)_{PQ} !! \text{ "Flaxion"}$$

* As far as we know, this simple realization has not been studied explicitly before.

cf. related earlier works, **Wilczek,'82**, Geng-Ng,'89, Berezhiani-Khlopov,'91, Babu-Barr,'92, Albrecht et.al.,'10, Fong-Nardi,'13, Ahn,'14,'16, Celis et.al.,'14,.....

[arXiv:1612.05492](#) [[pdf](#), [ps](#), [other](#)]

Flaxion: a minimal extension to solve puzzles in the standard model

[Yohei Ema](#), [Koichi Hamaguchi](#), [Takeo Moroi](#), [Kazunori Nakayama](#)

Comments: 23 pages, 1 figure; v2: version published in JHEP

Subjects: **High Energy Physics – Phenomenology (hep-ph)**

[arXiv:1612.08040](#) [[pdf](#), [other](#)]

The Axiflavoron

[Lorenzo Calibbi](#), [Florian Goertz](#), [Diego Redigolo](#), [Robert Ziegler](#), [Jure Zupan](#)

Comments: 6 pages, typos corrected, references added

Subjects: **High Energy Physics – Phenomenology (hep-ph)**

Flaxion

$$\begin{array}{c} \phi \\ \text{flavon} \end{array} = \frac{1}{\sqrt{2}} (\varphi + i \text{axion} a)$$

Flaxion

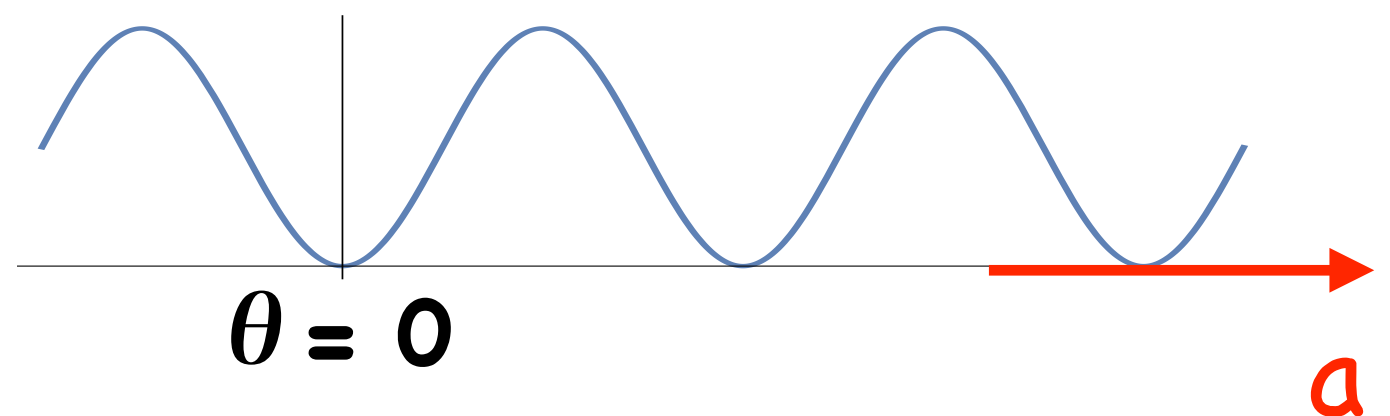
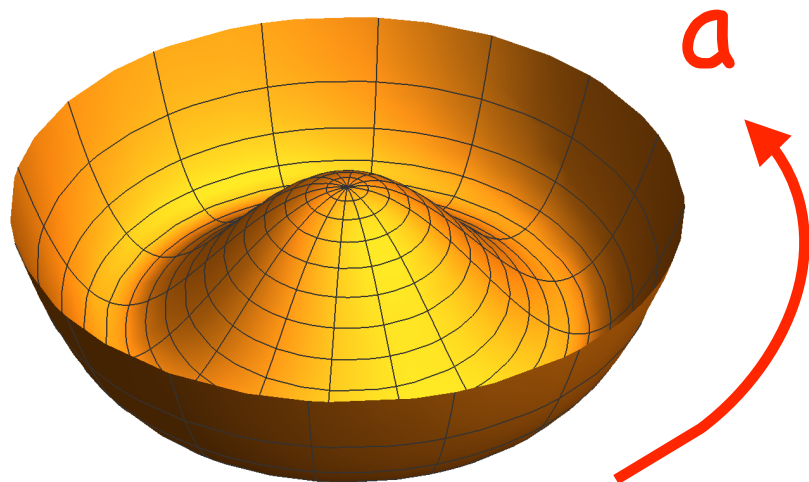
$$\underset{\text{flavon}}{\phi} = \frac{1}{\sqrt{2}} (\underset{\text{axion}}{\varphi} + ia)$$

(1) Strong CP problem is solved by the PQ mechanism.

[Peccei-Quinn,'77]

$$\mathcal{L} = \frac{g_s^2}{32\pi^2} \frac{a}{f_a} G_{\mu\nu}^a \tilde{G}^{a\mu\nu} \quad \text{where} \quad f_a = \frac{\sqrt{2}\langle\phi\rangle}{N_{\text{DW}}}, \quad N_{\text{DW}} = \sum_i (2q_{Q_i} - q_{u_i} - q_{d_i})$$

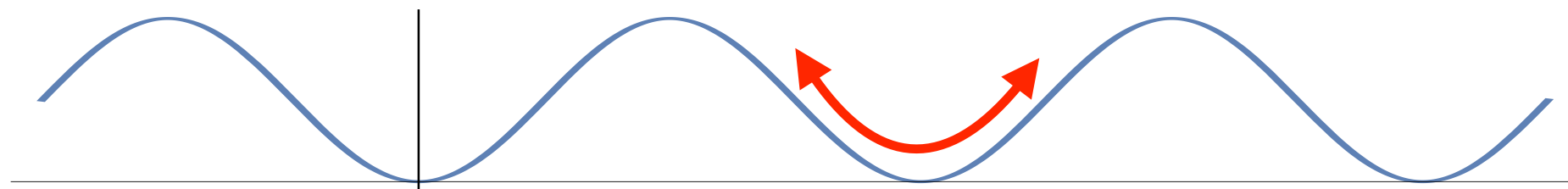
(In the example before, $N_{\text{DW}} = 26$.)



Flaxion

$$\underset{\text{flavon}}{\phi} = \frac{1}{\sqrt{2}} (\underset{\text{axion}}{\varphi} + ia)$$

- (1) **Strong CP problem is solved** by the PQ mechanism.
- (2) The axion can be **the dark matter**.



$$\Omega_a h^2 = 0.18 \theta_i^2 \left(\frac{f_a}{10^{12} \text{ GeV}} \right)^{1.19} \cdot \quad [\text{Turner,'86}]$$

Flaxion

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- (1) **Strong CP problem is solved** by the PQ mechanism.
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Any new prediction?

Flaxion

$$\underset{\text{flavon}}{\phi} = \frac{1}{\sqrt{2}} (\underset{\text{axion}}{\varphi} + ia)$$

- (1) **Strong CP problem is solved** by the PQ mechanism.
- (2) The axion can be **the dark matter**.

Any new prediction?

.....Yes!

- (3) Characteristic flavor-changing signals
are predicted.

(3) Characteristic flavor-changing signals.

$$\begin{aligned} \mathcal{L} = & y_{ij}^d \left(\frac{\phi}{M} \right)^{n_{ij}^d} \bar{Q}_i H d_{Rj} + y_{ij}^u \left(\frac{\phi}{M} \right)^{n_{ij}^u} \bar{Q}_i \tilde{H} u_{Rj} \\ & + y_{ij}^l \left(\frac{\phi}{M} \right)^{n_{ij}^l} \bar{L}_i H l_{Rj} + y_{i\alpha}^\nu \left(\frac{\phi}{M} \right)^{n_{i\alpha}^\nu} \bar{L}_i \tilde{H} N_{R\alpha} \\ & + \frac{1}{2} y_{\alpha\beta}^N \left(\frac{\phi}{M} \right)^{n_{\alpha\beta}^N} M \bar{N}_{R\alpha}^c N_{R\beta} + \text{h.c.} \end{aligned}$$

$$\longrightarrow -\mathcal{L} = \sum_{f=u,d,l} \left[m_{ij}^f \left(1 + \frac{h}{\sqrt{2}\langle H \rangle} \right) + \frac{m_{ij}^f n_{ij}^f (s + ia)}{\sqrt{2}\langle \phi \rangle} \right] \bar{f}_{Li} f_{Rj} + \text{h.c.}$$

They are not simultaneously diagonalized.
 → flavor changing processes.

The most stringent bound comes from $K^+ \rightarrow \pi^+ a$.

$$\text{Br}(K^+ \rightarrow \pi^+ a) \simeq 3 \times 10^{-10} \left(\frac{10^{10} \text{ GeV}}{f_a} \right)^2 \underbrace{\left(\frac{26}{N_{\text{DW}}} \right)^2 \left| \frac{(\kappa_{\text{AH}}^d)_{12}}{m_s - m_d} \right|^2}_{O(1)} < 7.3 \times 10^{-11}$$

[BNL-E787, E949]

$$\rightarrow f_a \gtrsim 2 \times 10^{10} \text{ GeV}$$

CERN NA62 experiment can improve the sensitivity !!

Flaxion Scenario

Quark and lepton
mass hierarchy
and mixings.

Neutrino
masses
and mixings.

seesaw

Standard Model

+ **one complex scalar**
with $U(1)_F = U(1)_{PQ}$

$$\phi = \frac{1}{\sqrt{2}} (\varphi + ia)$$

flavon

+ 2 (or 3)
right-handed
neutrinos.

Strong CP
problem.

Dark
Matter.

Flaxion Scenario

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flavon axion

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Quark and lepton
mass hierarchy
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Neutrino
masses

and mixings. *seesaw*

characteristic
signal:

$$K \rightarrow \pi a$$

Strong CP
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Dark
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What about
the real part?

Flaxion Scenario

Quark and lepton mass hierarchy and mixings.

Neutrino masses and mixings.

seesaw

Standard Model
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flavon **inflaton** **axion**

+ 2 (or 3) right-handed neutrinos.

characteristic signal:
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Strong CP problem.

Dark Matter.

Inflation !

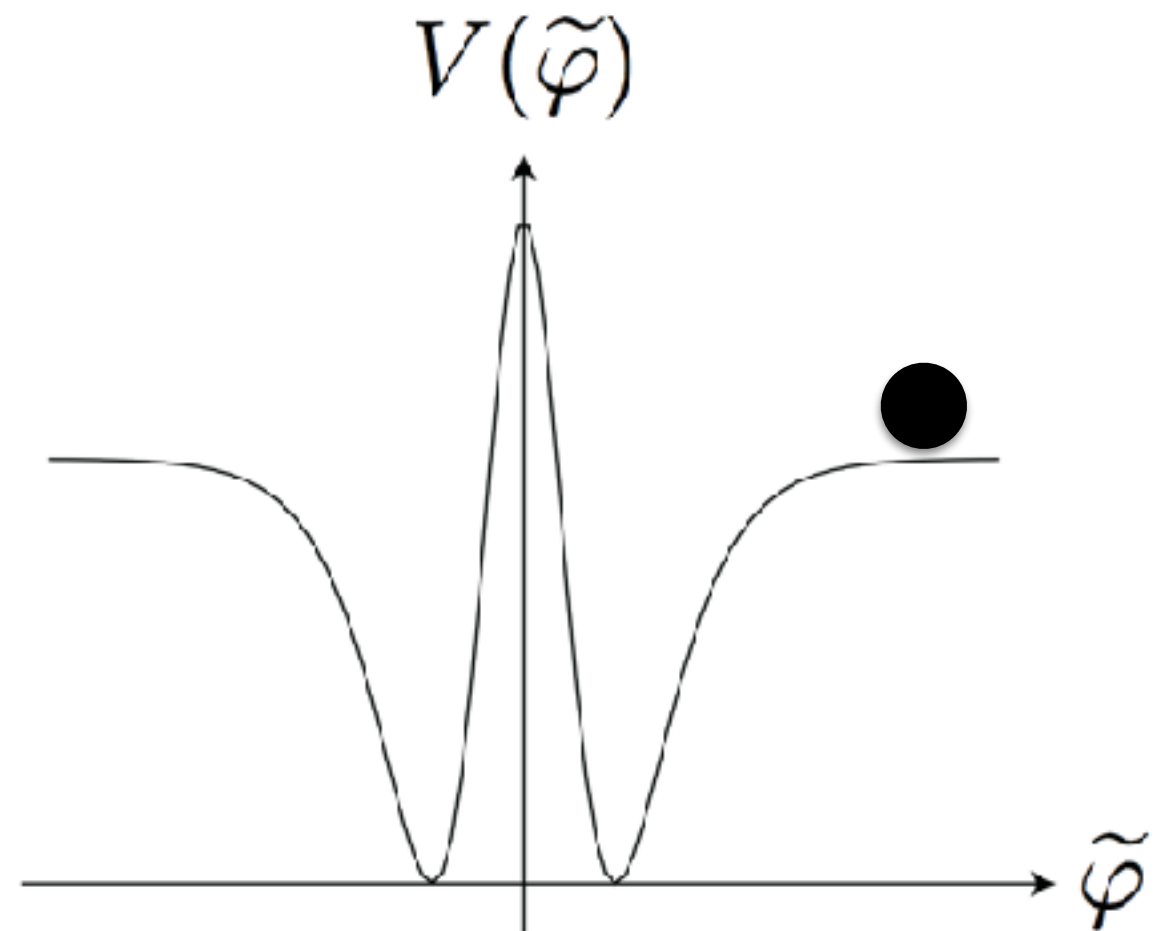
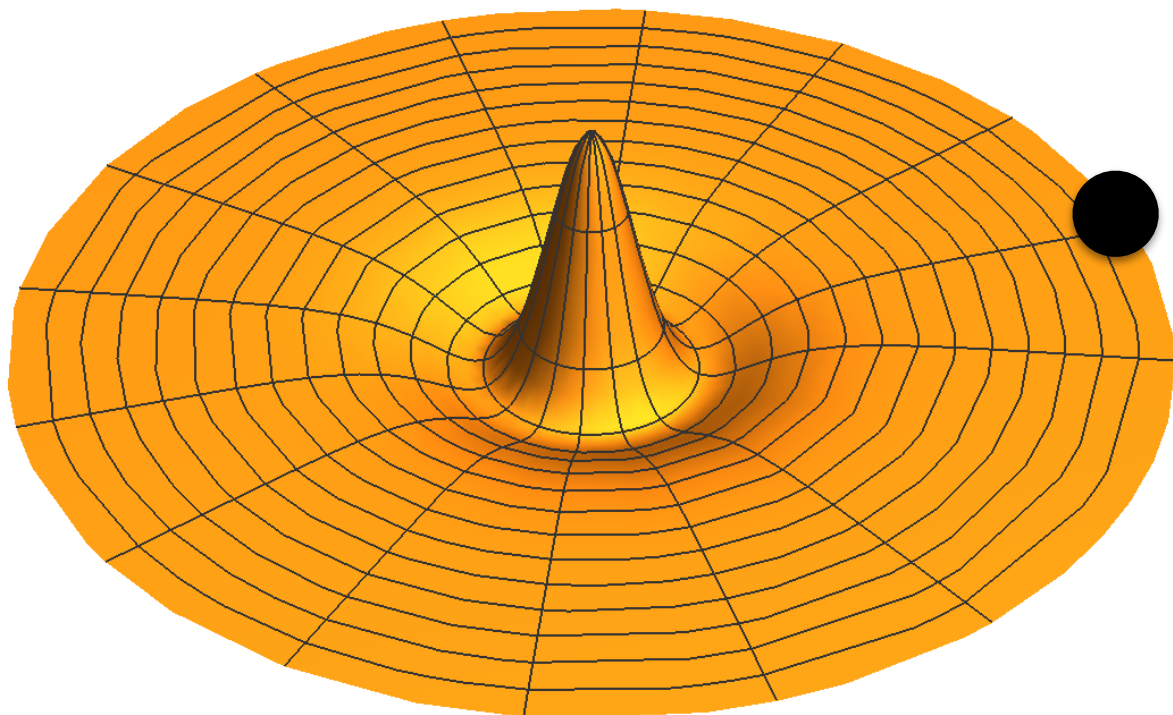
Flaxion Inflation:

$$\mathcal{L} = -\frac{|\partial\phi|^2}{(1 - |\phi|^2/\Lambda^2)^2} - \lambda_\phi (|\phi|^2 - v_\phi^2)^2$$

$$v_\phi < \Lambda < \sqrt{2}v_\phi$$

canonical field $\tilde{\varphi}$:

$$\frac{\varphi}{\sqrt{2}\Lambda} \equiv \tanh\left(\frac{\tilde{\varphi}}{\sqrt{2}\Lambda}\right)$$



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Curvature fluctuation:

$P_{\zeta} = 2.2 \times 10^{-9}$ [Planck,'15] is reproduced

for $\lambda_\phi \lesssim 1$ and $\Lambda \gtrsim 10^{13}$ GeV, which is consistent with the scale for flaxion DM.

(n_s, r) is in the Planck best-fit region.

The U(1) symmetry is never restored \rightarrow No Domain wall.

Isocurvature fluctuation is suppressed.

Reheating temperature is high enough for Leptogenesis.

$(T_R \approx 10^{12} - 10^{14} \text{ GeV})$

("strong washout")

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See Backup slides for details.

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Flaxion Scenario

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+ **one complex scalar**
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$$\phi = \frac{1}{\sqrt{2}} (\varphi + ia)$$

flavon inflaton axion

+ 2 (or 3)
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characteristic
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Strong CP
problem.

Dark
Matter.

Quark and lepton
mass hierarchy
and mixings.

Neutrino
masses
and mixings. *seesaw*

Inflation.

Flaxion Scenario

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seesaw

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solves DW and isocurvature problems

P_{ζ} & (n_s, r) in the Planck best-fit region

Inflation.

Flaxion Scenario

Quark and lepton mass hierarchy and mixings.

Neutrino masses and mixings.

Baryon asymmetry of the Universe.

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seesaw

Leptogenesis

solves DW and isocurvature problems

High enough reheating

P_{ξ} & (n_s, r) in the Planck best-fit region

Inflation.

Summary

Flaxion Scenario

Quark and lepton mass hierarchy and mixings.

Neutrino masses and mixings.

Baryon asymmetry of the Universe.

Standard Model
 + **one complex scalar**
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seesaw
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P_{ξ} & (n_s, r)
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Inflation.

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Backup

Summary

Flaxion Scenario

Lagrangian

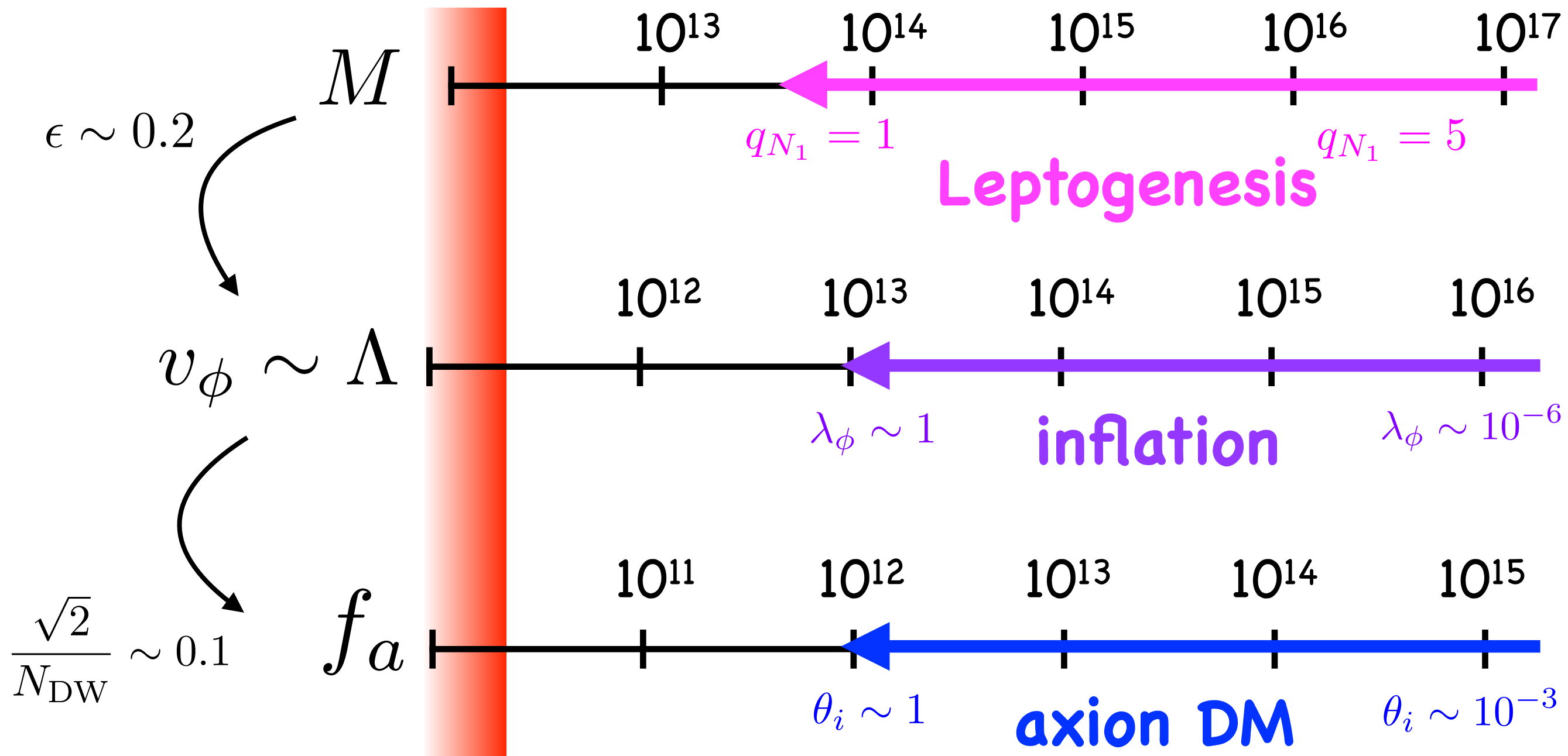
$$\begin{aligned} \mathcal{L} = & -\frac{|\partial\phi|^2}{(1 - |\phi|^2/\Lambda^2)^2} - \lambda_\phi (|\phi|^2 - v_\phi^2)^2 \\ & + y_{ij}^d \left(\frac{\phi}{M}\right)^{n_{ij}^d} \bar{Q}_i H d_{Rj} + y_{ij}^u \left(\frac{\phi}{M}\right)^{n_{ij}^u} \bar{Q}_i \tilde{H} u_{Rj} \\ & + y_{ij}^l \left(\frac{\phi}{M}\right)^{n_{ij}^l} \bar{L}_i H l_{Rj} + y_{i\alpha}^\nu \left(\frac{\phi}{M}\right)^{n_{i\alpha}^\nu} \bar{L}_i \tilde{H} N_{R\alpha} \\ & + \frac{1}{2} y_{\alpha\beta}^N \left(\frac{\phi}{M}\right)^{n_{\alpha\beta}^N} M \overline{N_{R\alpha}^c} N_{R\beta} + \text{h.c.} \end{aligned}$$

Summary

Flaxion Scenario

scale

GeV



$K \rightarrow \pi a$
 [BNL-E787, 949]

CERN-NA62

Supersymmetric flaxion ?

$$W = \lambda X (\phi \bar{\phi} - v_\phi^2)$$

- Cosmology becomes nontrivial; **gravitino, sflaxion,...**
- SUSY flavor/CP,
- R-parity violation,
- Inflation model,...

Other constraints?

$$\begin{aligned} (\kappa_{\text{H}}^f)_{ij} &= \frac{1}{2} (V^{f\dagger} \hat{q}_Q V^f - U^{f\dagger} \hat{q}_f U^f)_{ij} (m_j^f + m_i^f), \\ (\kappa_{\text{AH}}^f)_{ij} &= \frac{1}{2} (V^{f\dagger} \hat{q}_Q V^f + U^{f\dagger} \hat{q}_f U^f)_{ij} (m_j^f - m_i^f). \end{aligned}$$

- $K^+ \rightarrow \pi^+ a$

$$f_a \gtrsim 2 \times 10^{10} \text{ GeV} \left(\frac{26}{N_{\text{DW}}} \right) \left| \frac{(\kappa_{\text{AH}}^d)_{12}}{m_s} \right|$$

$$\text{Br}(K^+ \rightarrow \pi^+ a) \lesssim 7.3 \times 10^{-11}$$

$$\Gamma(K^+ \rightarrow \pi^+ a) = \frac{m_K^3}{32\pi v_\phi^2} \left(1 - \frac{m_\pi^2}{m_K^2} \right)^3 \left| \frac{(\kappa_{\text{AH}}^d)_{12}}{m_s - m_d} \right|^2$$

- $\mu \rightarrow e a \gamma$

$$f_a \gtrsim 1 \times 10^8 \text{ GeV} \left(\frac{26}{N_{\text{DW}}} \right) \left| \frac{(\kappa_{\text{AH}}^l)_{12}}{m_\mu} \right|$$

$$\text{Br}(\mu \rightarrow e a \gamma) \lesssim 1.1 \times 10^{-9},$$

- SN1987A

$$\frac{f_a}{|C_N|} \gtrsim 1 \times 10^9 \text{ GeV}.$$

$$\mathcal{L} = \sum_{N=p,n} \frac{C_N m_N}{f_a} i a \bar{N} \gamma_5 N.$$

$$C_p \simeq -0.4 \text{ and } |C_n| \ll |C_p| \text{ for } N_{\text{DW}} \gg 1.$$

- cooling of the white dwarf stars. (g_{aee})

$$f_a \gtrsim 7 \times 10^7 \text{ GeV} \left(\frac{26}{N_{\text{DW}}} \right) \left| \frac{(\kappa_{\text{H}}^l)_{11}}{m_e} \right|$$

Decay	Physics	Present limit	NA62
$\pi^+\mu^+e^-$	LFV	$1.3 \cdot 10^{-11}$	$0.7 \cdot 10^{-12}$
$\pi^+\mu^-e^+$	LFV	$5.2 \cdot 10^{-10}$	$0.7 \cdot 10^{-12}$
$\pi^-\mu^+e^+$	LNV	$5.0 \cdot 10^{-10}$	$0.7 \cdot 10^{-12}$
$\pi^-e^+e^+$	LNV	$6.4 \cdot 10^{-10}$	$2.0 \cdot 10^{-12}$
$\pi^-\mu^+e^+$	LNV	$1.1 \cdot 10^{-9}$	$0.4 \cdot 10^{-12}$
$\mu^-\nu e^+e^+$	LFV/LNV	$2 \cdot 10^{-8}$	$4.0 \cdot 10^{-12}$
$e^-\nu\mu^+\mu^+$	LNV	No data	$1.0 \cdot 10^{-12}$
$\pi^+\chi^0$	New particle	$5.9 \cdot 10^{-11}, M_\chi = 0$	$1.0 \cdot 10^{-12}$
$\pi^+\chi\chi$	New particle	No data	$1.0 \cdot 10^{-12}$
$\pi^+\pi^+e^-\nu$	$\Delta S \neq \Delta Q$	$1.2 \cdot 10^{-8}$	$1.0 \cdot 10^{-11}$
$\pi^+\pi^+\mu^-\nu$	$\Delta S \neq \Delta Q$	$3.0 \cdot 10^{-6}$	$1.0 \cdot 10^{-11}$
$\pi^+\gamma$	Angular momentum	$2.3 \cdot 10^{-9}$	$1.0 \cdot 10^{-11}$
$\mu^+\nu_h, \nu_h \rightarrow \nu\gamma$	Heavy neutrino	Limits up to $M\nu_h = 350 MeV/c^2$	$1.0 \cdot 10^{-12}$
R_K	LU	$(2.488 \pm 0.010) \cdot 10^{-5}$	2x better
$\pi^+\gamma\gamma$	ChPT	< 500 events	10^5 events
$\pi^0\pi^0e^+\nu$	ChPT	66000 events	$O(10^6)$ events
$\pi^0\pi^0\mu^+\nu$	ChPT		$O(10^5)$ events

Table 2: NA62 sensitivities for other rare decay channels

[arXiv:1407.8213]

The NA62 experiment at CERN: status and perspectives

[NA62 Collaboration](#)

$B^+ \rightarrow K^+ a$??

[arXiv:1612.08040] Phys.Rev. **D95** (2017) 095009

The Axiflavor

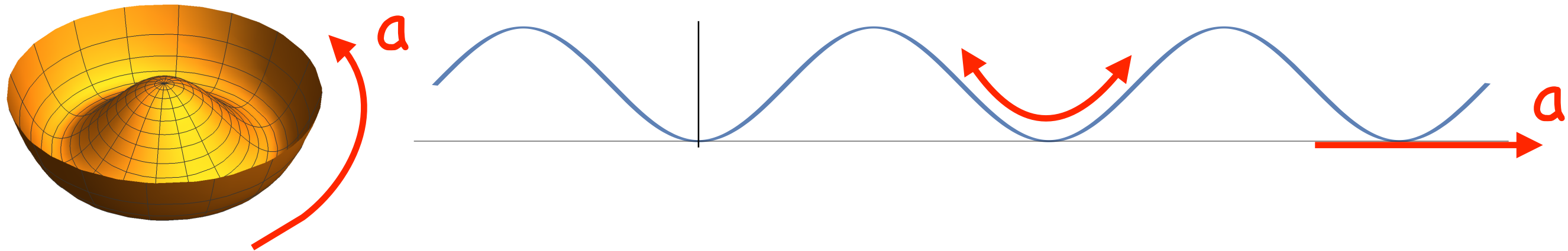
[L. Calibbi](#), [F. Goertz](#), [D. Redigolo](#), [R. Ziegler](#), [J. Zupan](#)

$$\text{BR}(B^+ \rightarrow K^+ a) \simeq 1.4 \cdot 10^{-12} \left(\underbrace{\frac{m_a}{0.1 \text{ meV}}}_{\kappa_{bs}/N} \times \frac{\kappa_{bs}}{N} \right)^2$$

$\kappa_{bs}/N \sim \mathcal{O}(1)$.

$$\simeq \left(\frac{6 \times 10^9 \text{ GeV}}{f_a} \right)^2$$

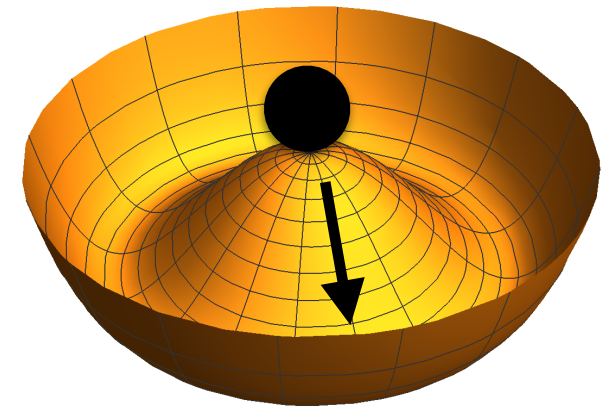
Flaxion Dark Matter:



Case 1: U(1) is broken after inflation.

-> **Domain Wall !**

In the flaxion scenario, typically $N_{\text{DW}} \neq 1$, and this possibility is **excluded**.

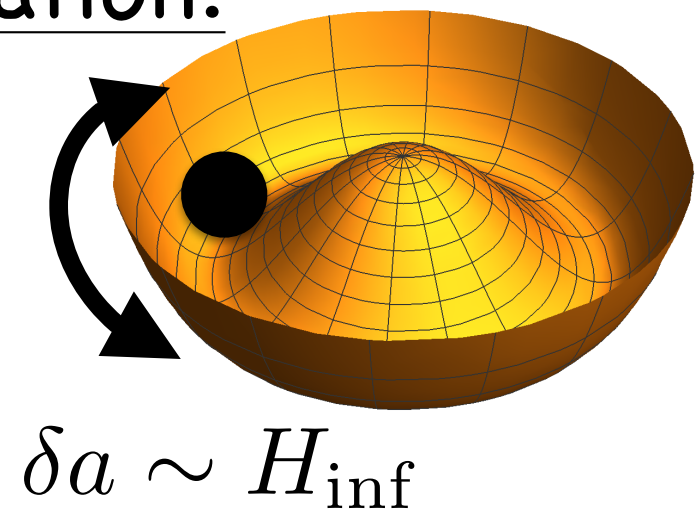


Case 2: U(1) was already broken during inflation.

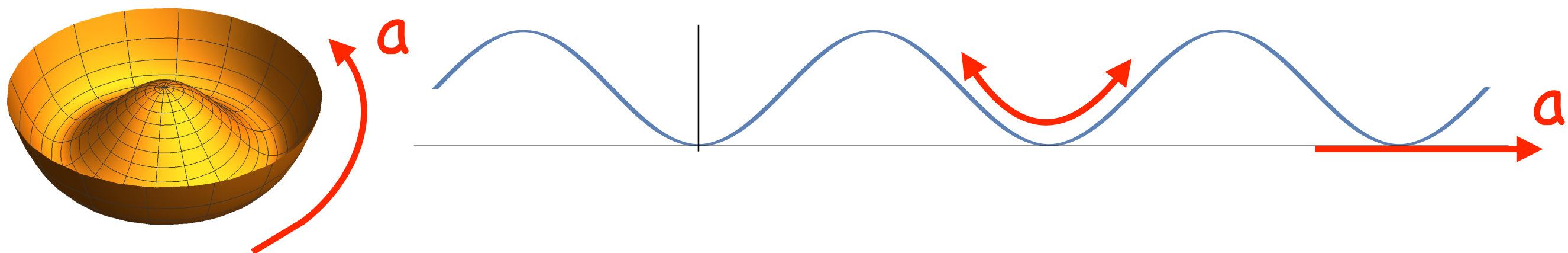
Quantum fluctuation during inflation leads to **DM isocurvature** perturbation, which is severely constrained [Planck,'15].

-> **Strong bound on inflation scale.**

$$H_{\text{inf}} \lesssim 3 \times 10^7 \text{ GeV } \theta_i^{-1} \left(\frac{10^{12} \text{ GeV}}{f_a} \right)^{0.19} .$$



Flaxion Dark Matter:



Case 1: U(1) is broken after inflation.

-> **Domain Wall !**

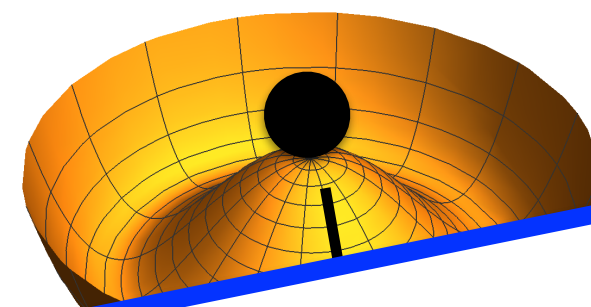
In the flaxion scenario, typically $N_{\text{DW}} \neq 1$, and this possibility is **excluded**.

Case 2: U(1) is broken during inflation.

Quantum fluctuations
leads to **DM**
which is severe

-> **Strong bounds on inflation scale.**

$$H_{\text{inf}} \lesssim 3 \times 10^7 \text{ GeV } \theta_i^{-1} \left(\frac{10^{12} \text{ GeV}}{f_a} \right)^{0.19} .$$



No problem in "flaxion-inflation" scenario !

$$\delta a \sim H_{\text{inf}}$$

Flaxion Inflation:

$$\mathcal{L} = -\frac{|\partial\phi|^2}{(1 - |\phi|^2/\Lambda^2)^2} - \lambda_\phi (|\phi|^2 - v_\phi^2)^2$$

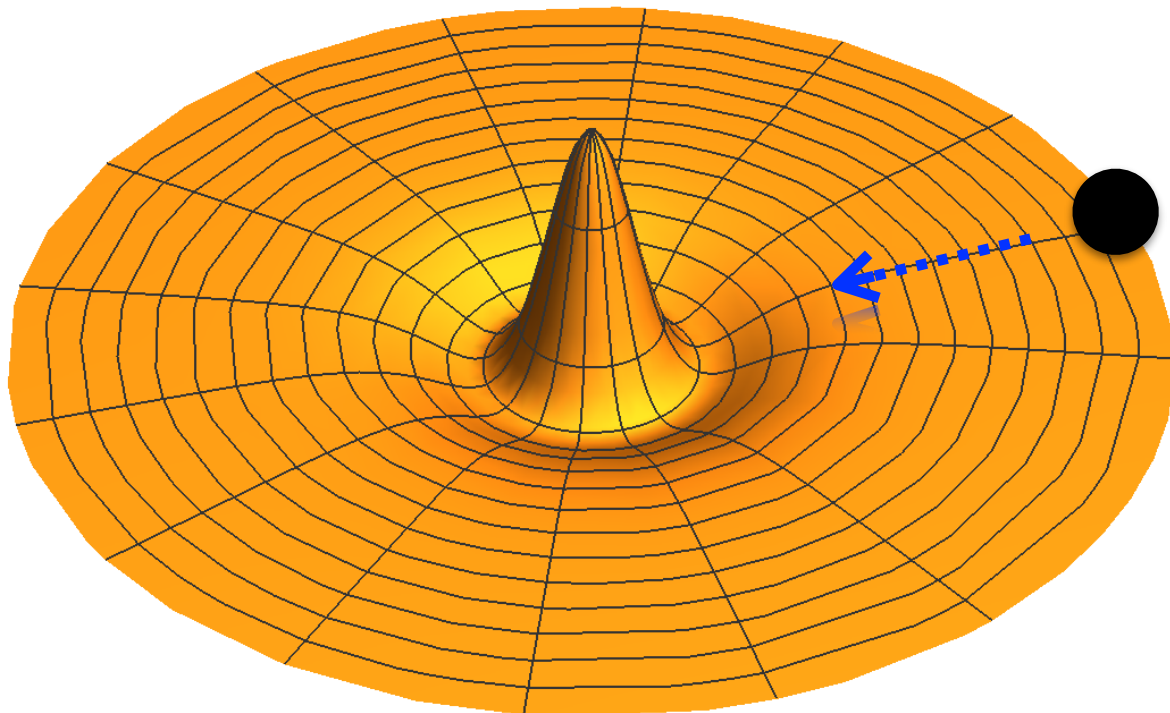
- The U(1) symmetry is never restored

-> No Domain wall.

$$v_\phi < \Lambda < \sqrt{2}v_\phi$$

canonical field $\tilde{\varphi}$:

$$\frac{\varphi}{\sqrt{2}\Lambda} \equiv \tanh\left(\frac{\tilde{\varphi}}{\sqrt{2}\Lambda}\right)$$



Flaxion Inflation:

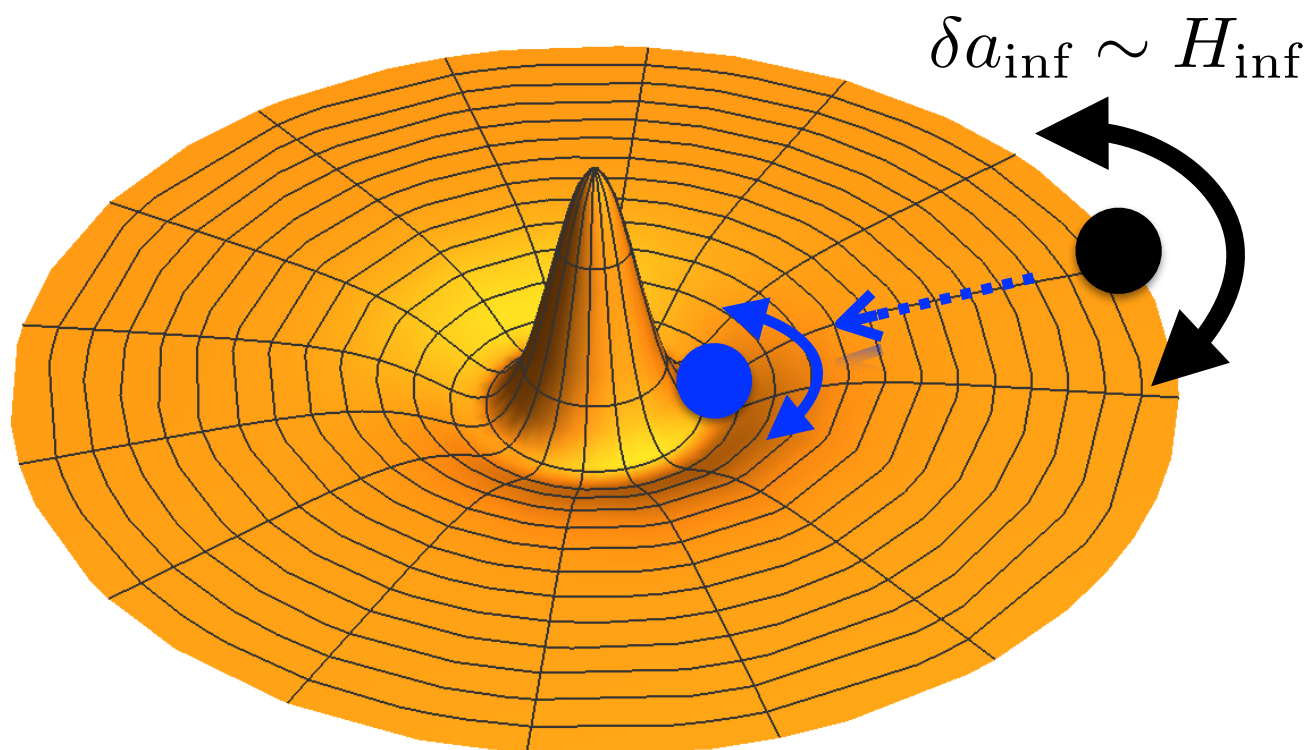
$$\mathcal{L} = -\frac{|\partial\phi|^2}{(1 - |\phi|^2/\Lambda^2)^2} - \lambda_\phi (|\phi|^2 - v_\phi^2)^2$$

- The U(1) symmetry is never restored
→ No Domain wall.
- Isocurvature fluctuation is suppressed.

$$v_\phi < \Lambda < \sqrt{2}v_\phi$$

canonical field $\tilde{\varphi}$:

$$\frac{\varphi}{\sqrt{2}\Lambda} \equiv \tanh\left(\frac{\tilde{\varphi}}{\sqrt{2}\Lambda}\right)$$



Flaxion Inflation: Reheating and Leptogenesis

Inflaton partial decay rate into RHNs,

$$\Gamma(\tilde{\varphi} \rightarrow N_R N_R) \simeq \sum_{\alpha\beta} \frac{|y_{\alpha\beta}^N n_{\alpha\beta}^N \epsilon^{n_{\alpha\beta}^N - 1}|^2}{32\pi} \Delta^2 m_\varphi$$

$$\Delta \equiv 1 - v_\phi^2/\Lambda^2$$

$$m_\varphi \sim 3 \times 10^{13} \text{ GeV} (v_\phi/\Lambda)$$



$$H_{\text{inf}} \simeq 5 \times 10^8 \text{ GeV} \left(\frac{\Lambda}{10^{14} \text{ GeV}} \right)$$

Reheating is completed almost instantaneously.

Reheating temperature

$$T_R \sim 10^{12} - 10^{14} \text{ GeV}.$$

Flaxion Inflation: Reheating and Leptogenesis

... and **thermal leptogenesis** [Fukugita-Yanagida,'86]
can work successfully for **$m_{N_1} \simeq O(10^{12})$ GeV** !

.....
In more details,...

Final baryon asymmetry: $\frac{n_B}{s} \simeq \epsilon_1 \kappa_f \frac{28}{79} \left(\frac{n_{N_1}}{s} \right)_{\text{th}} \simeq 1.3 \times 10^{-3} \epsilon_1 \kappa_f$

Asymmetry parameter: $\epsilon_1 = \frac{3}{16\pi} \frac{m_{N_1} m_{\nu 3}}{v_{\text{EW}}^2} \delta_{\text{eff}} \simeq 1 \times 10^{-4} \left(\frac{m_{N_1}}{10^{12} \text{ GeV}} \right) \left(\frac{m_{\nu 3}}{0.05 \text{ eV}} \right) \delta_{\text{eff}}$

Effective neutrino mass: $\tilde{m}_{\nu 1} \equiv \sum_k |\epsilon^{n_{k1}^\nu} y_{k1}^\nu|^2 v_{\text{EW}}^2 / m_{N_1} \sim m_{\nu 3}$

-> Efficiency factor $\kappa_f \sim 3 \times 10^{-3}$ (strong washout region)

Altogether, **observed asymmetry $n_B/s \simeq 0.9 \times 10^{-10}$ can be obtained for $m_{N_1} \simeq O(10^{12})$ GeV**, corresponding to

$q_{N_1} = 1 - 5$ for $M \sim O(10^{14} - 10^{17})$ GeV

Proton decay ?

$$\mathcal{L} \sim \frac{QQQL}{M^2}, \quad \frac{uude}{M^2}, \quad \frac{QQue}{M^2}, \quad \frac{QLud}{M^2}$$

→ In the case of example charge assignments, the most dangerous one is the last one.

With $O(1)$ coefficients,

$$M > 5 \times 10^{14} \text{ GeV}$$

is sufficient to suppress it.