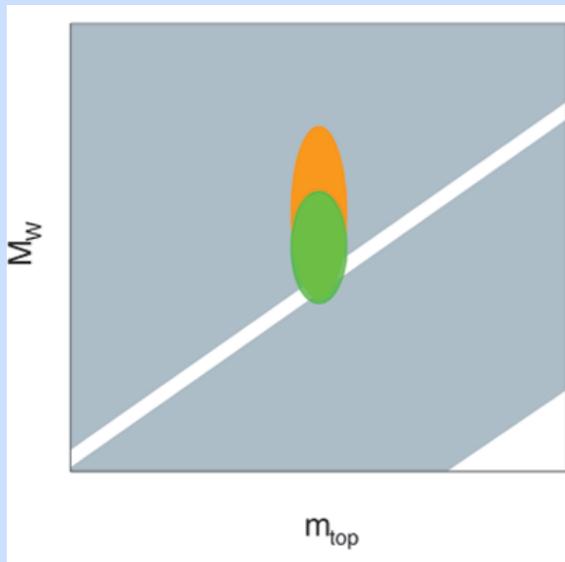
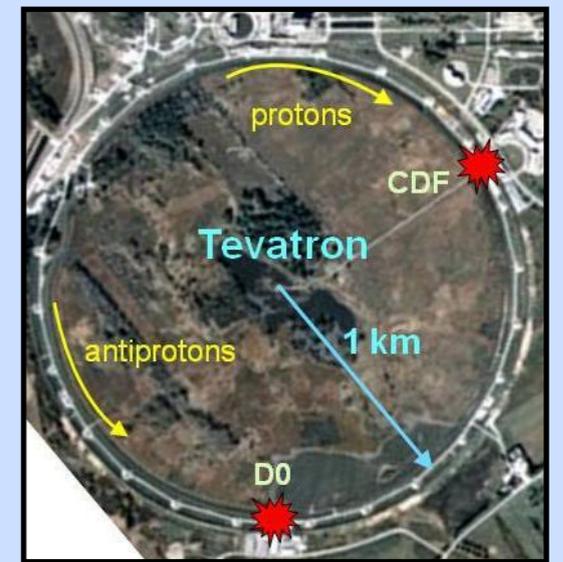


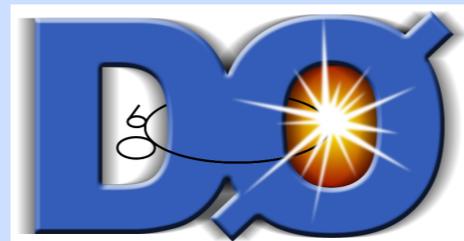
# Electroweak measurements at the Fermilab Tevatron



Chris Hays,  
Oxford University



*on behalf of the CDF and D0 Collaborations*



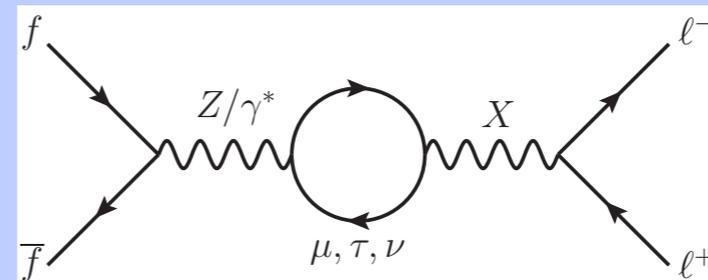
Rencontres de Moriond Electroweak  
12 March 2018

# Overview

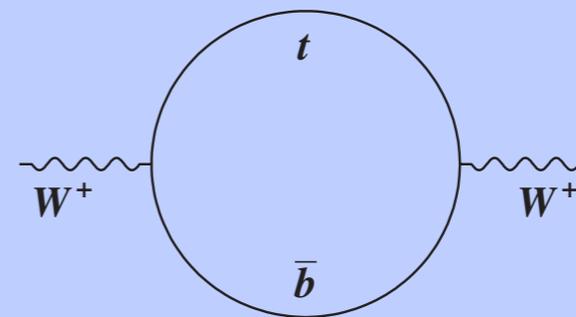
**Tevatron collider**



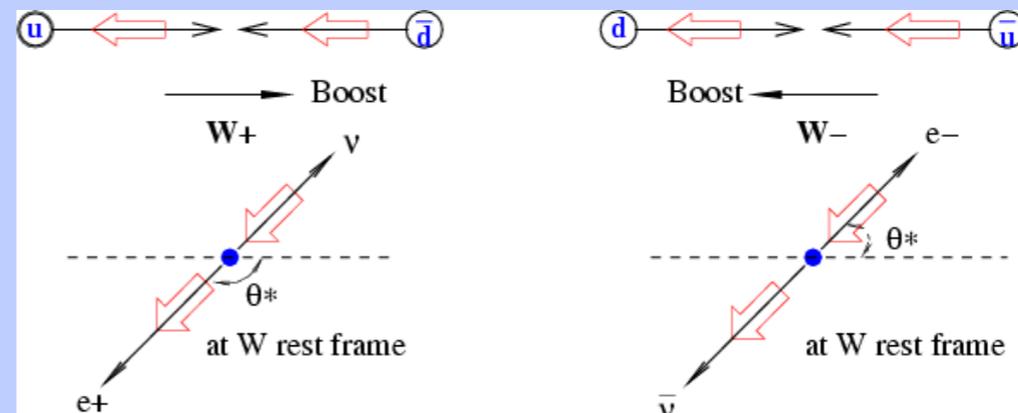
**Z boson couplings**



**W boson mass**



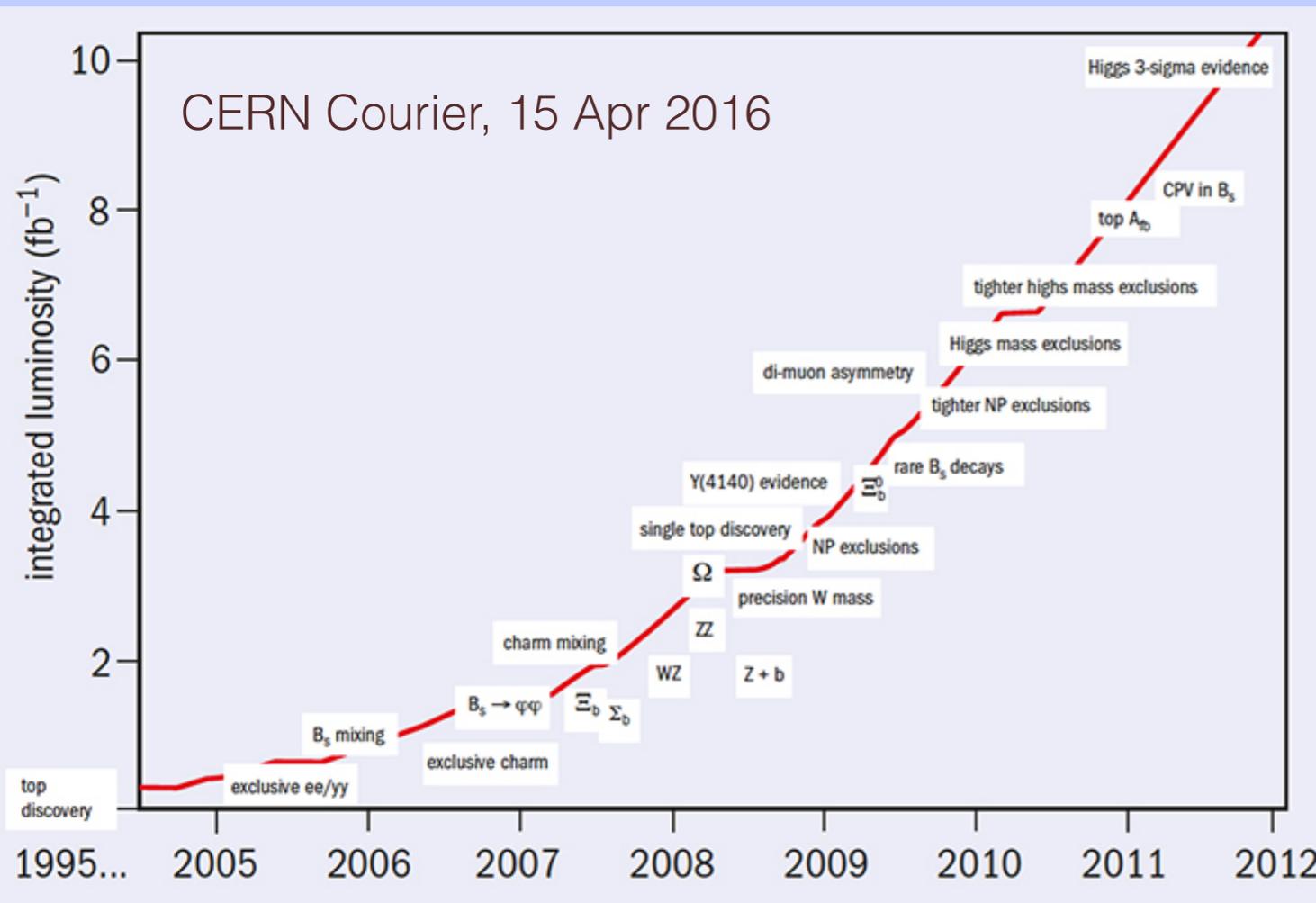
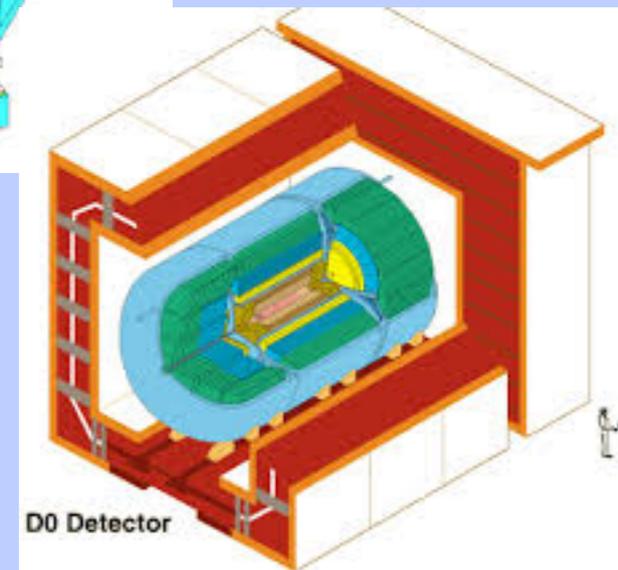
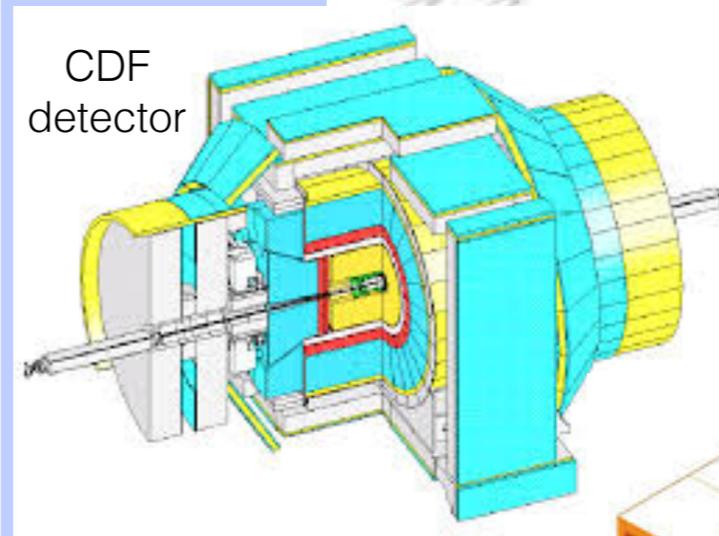
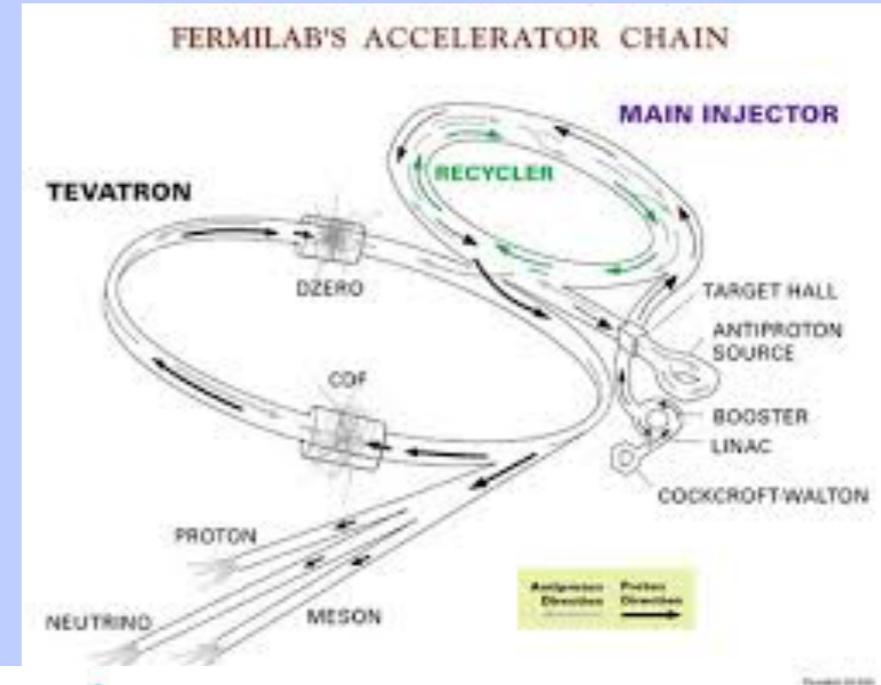
**W charge asymmetry**



# Fermilab Tevatron

The Fermilab Tevatron delivered  $>10 \text{ fb}^{-1}$  of proton-antiproton collisions at  $\sqrt{s}=1.96 \text{ TeV}$  from 2001-2011

Many discoveries and measurements made by the CDF and D0 experiments

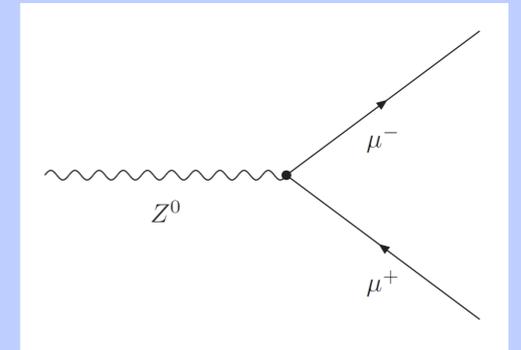


# Z boson couplings

Vector coupling of the Z boson to fermions has contributions from weak and hypercharge couplings (electroweak mixing)

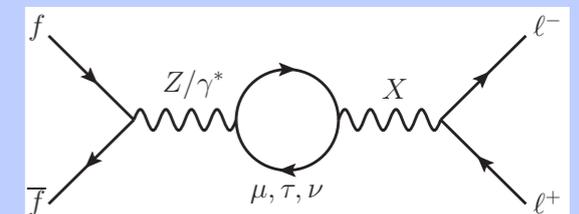
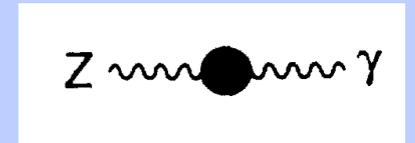
$$-i \frac{g}{2 \cos \theta_W} \bar{f} \gamma^\mu (g_V^f - g_A^f \gamma_5) f Z_\mu$$

$$g_V^f = T_3^f - 2Q_f \sin^2 \theta_W \quad \text{and} \quad g_A^f = T_3^f$$



Loop corrections modify the vector coupling relative to axial

Couplings can be affected by e.g. dark matter interacting with leptons



PLB 744, 330 (2015)

Forward-backward asymmetry of Z-pole leptons probes relative vector and axial couplings

$$\frac{\int_0^1 d \cos \theta \frac{d\sigma}{d \cos \theta} - \int_{-1}^0 d \cos \theta \frac{d\sigma}{d \cos \theta}}{\int_0^1 d \cos \theta \frac{d\sigma}{d \cos \theta} + \int_{-1}^0 d \cos \theta \frac{d\sigma}{d \cos \theta}} = \frac{3g_A^\ell g_V^\ell g_V^q g_A^q}{[(g_V^\ell)^2 + (g_A^\ell)^2][(g_V^q)^2 + (g_A^q)^2]}$$

Capture leading loop effects with the replacements  $g_V^f \rightarrow \sqrt{\rho_{eq}}(T_3^f - 2Q_f \kappa_f \sin^2 \theta_W)$  and  $g_A^f \rightarrow \sqrt{\rho_{eq}} T_3^f$

Define  $\sin^2 \theta_{\text{eff}}^f = \kappa_f \sin^2 \theta_W$

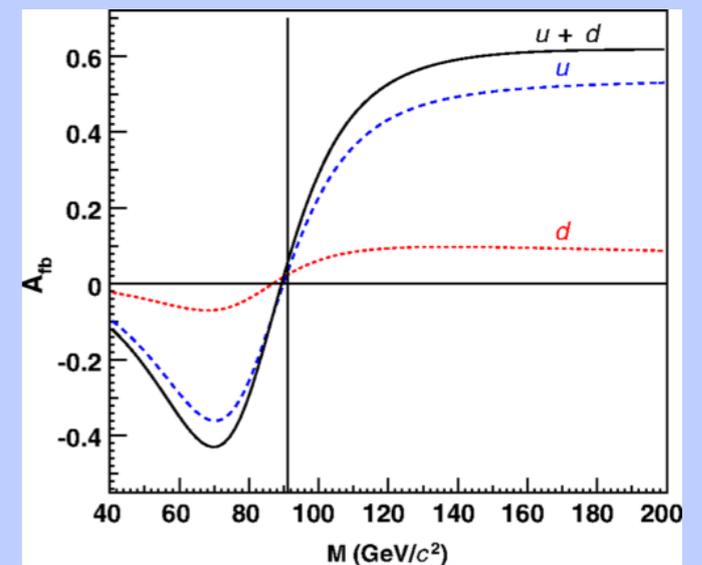
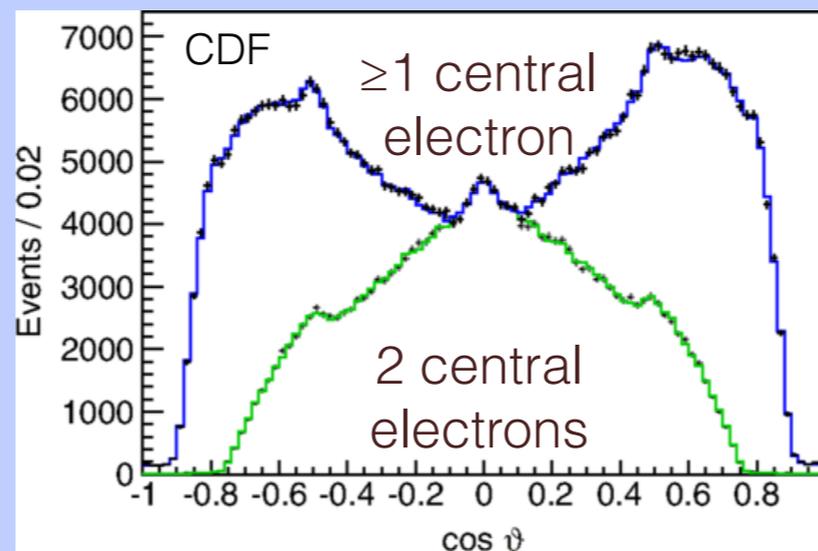
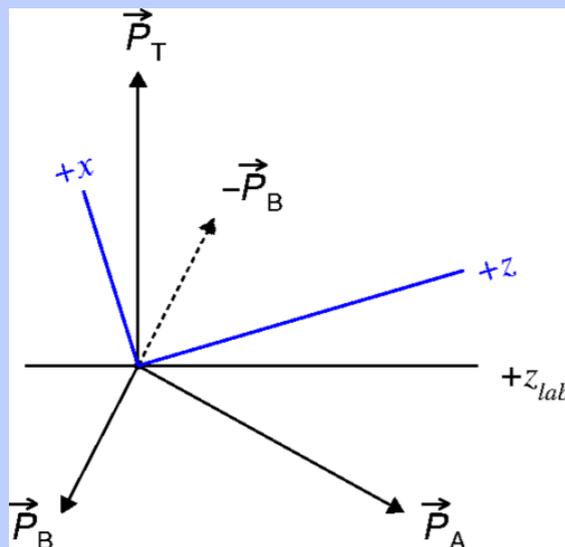
“Enhanced Born Approximation”

# Forward-backward asymmetry @ the Tevatron

Leptons have more sensitivity to  $\kappa$  variations: fix  $\kappa_q$  to the SM value and measure  $\sin^2\theta_{\text{eff}}^{\text{lept}}$

Measurement strategy:

*Measure number of selected negative leptons in the forward and backward regions as a function of mass*  
*Correct for detector acceptances and resolutions*



Experimental and theoretical requirements:

*Accurate simulation of detector response and acceptance*

*Accurate model of the parton distribution functions (affect detector acceptance & quark couplings)*

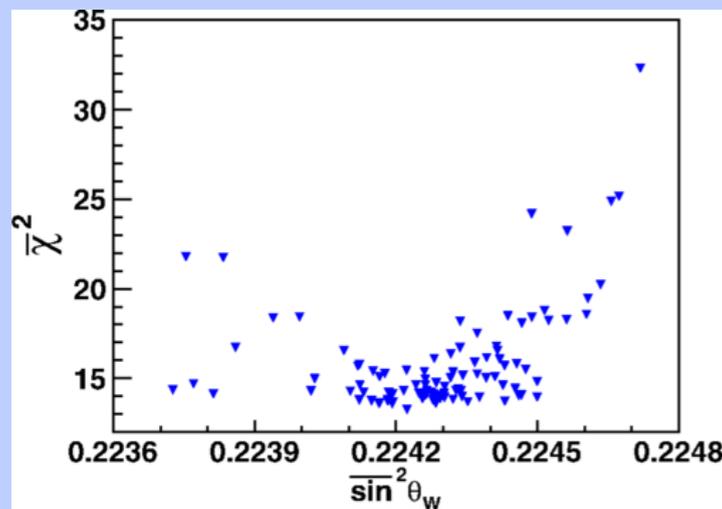
D0 & CDF have performed measurements in e and  $\mu$  channels with complete data sets

Final combination submitted for publication

# Forward-backward asymmetry @ the Tevatron

CDF use an event weighting to effectively measure asymmetry as a function of  $\cos\theta$   
 Reduces reliance on simulated acceptance

PRD 93, 112016 (2016)



Also constrain NNPDF sets in situ

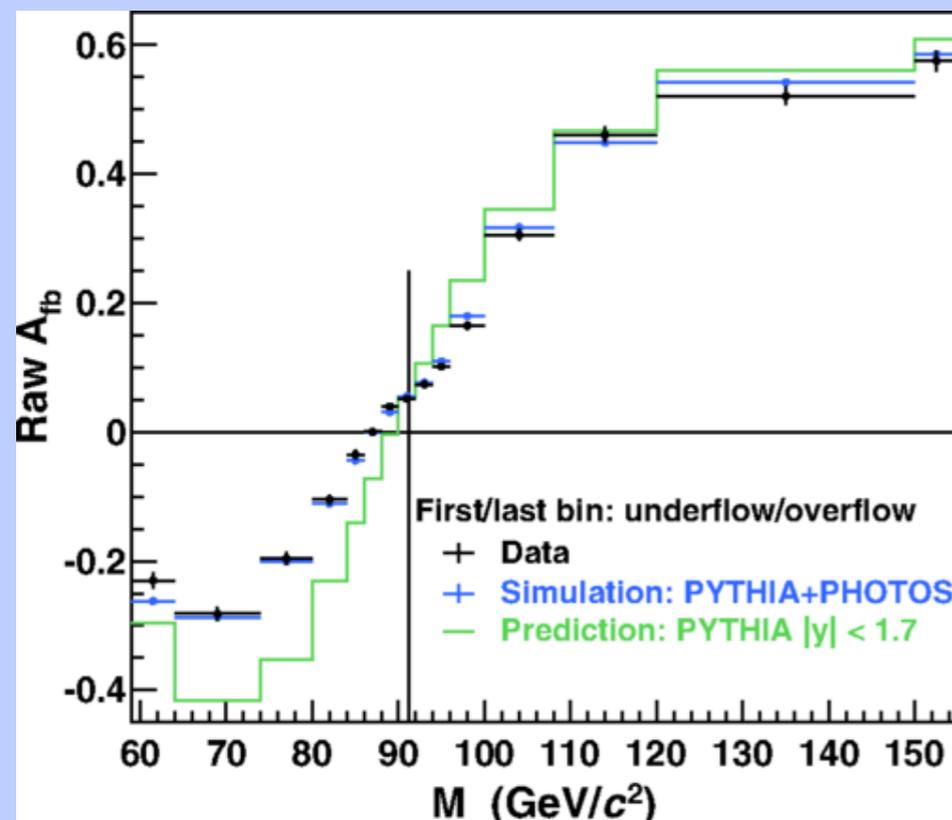
Source	$\sin^2 \theta_{\text{eff}}^{\text{lept}}$
Energy scale	$\pm 0.00003$
Backgrounds	$\pm 0.00002$
NNPDF-3.0 PDF	$\pm 0.00019$
QCD scale	$\pm 0.00002$
Form factor	–

$$A'_{\text{fb}} = \frac{N^+ - N^-}{N^+ + N^-} = \frac{8}{3} A_{\text{fb}} \left( \frac{|\cos \vartheta|}{1 + \cos^2 \vartheta + \dots} \right)$$

Weighting factor for  $A_{\text{fb}}(\cos\theta)$

e:  $\sin^2 \theta_{\text{eff}}^{\text{lept}} = 0.23248 \pm 0.00049 \pm 0.00019$

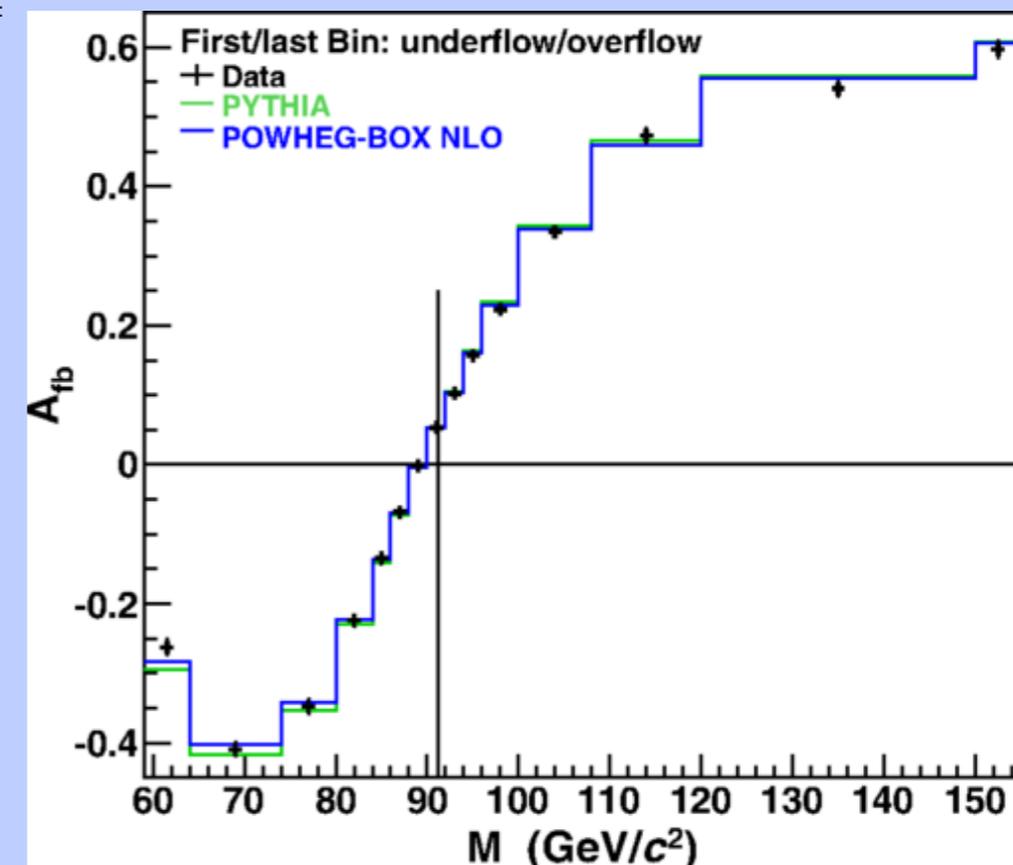
e +  $\mu$ :  $\sin^2 \theta_{\text{eff}}^{\text{lept}} = 0.23221 \pm 0.00043 \pm 0.00018$



Fully unfold asymmetry

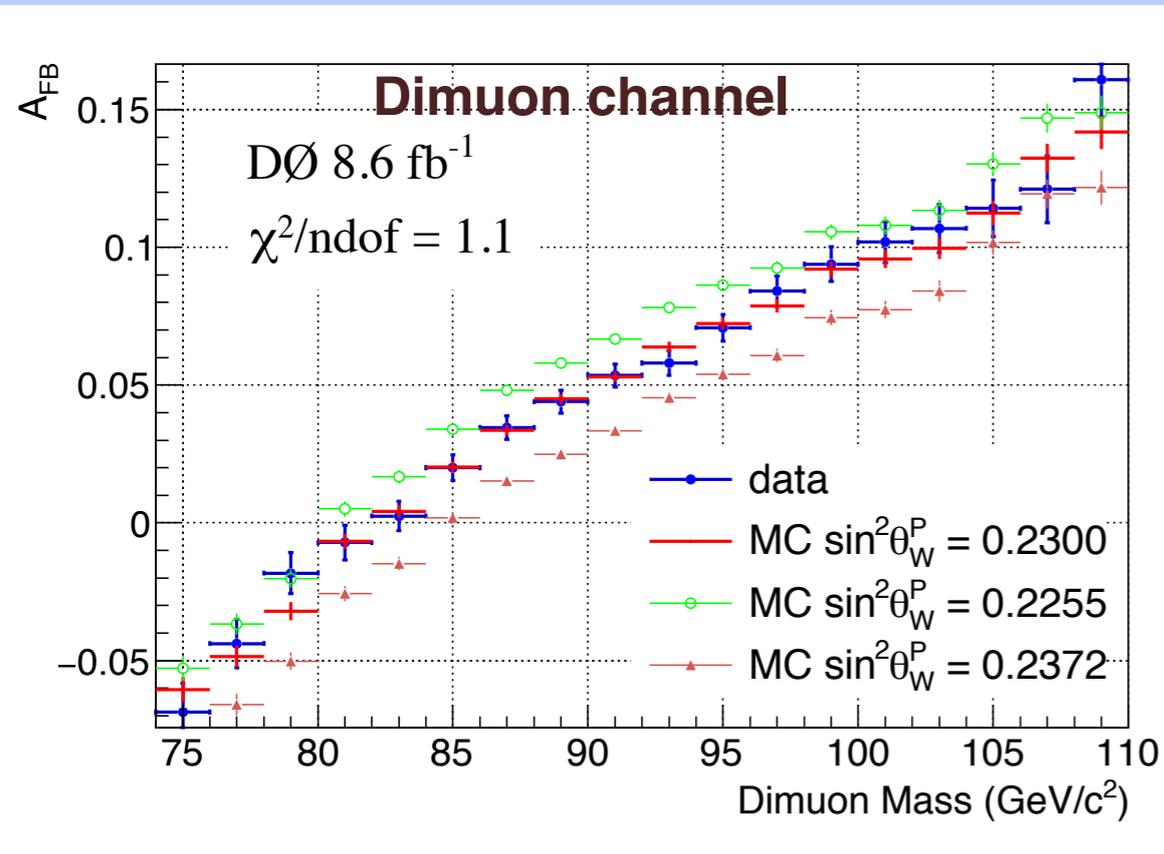


Allows for reinterpretation in any context



# Forward-backward asymmetry @ the Tevatron

D0 have recently completed a measurement in the muon channel using the full data set



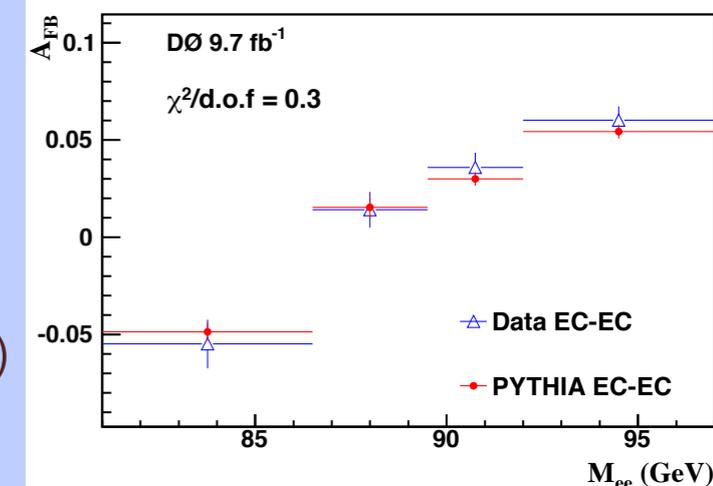
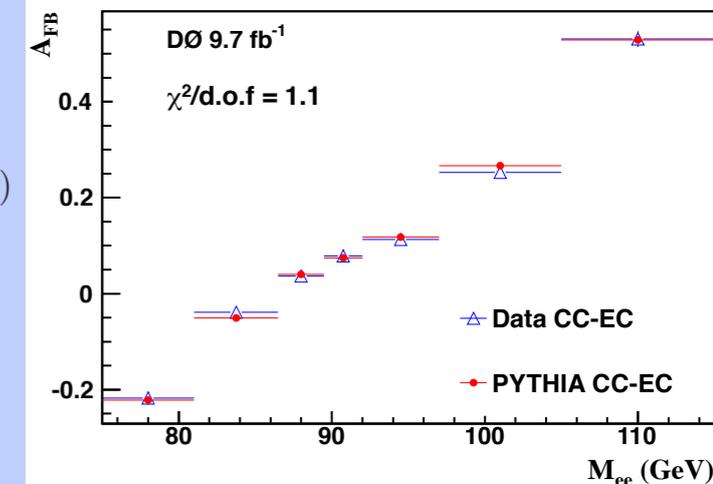
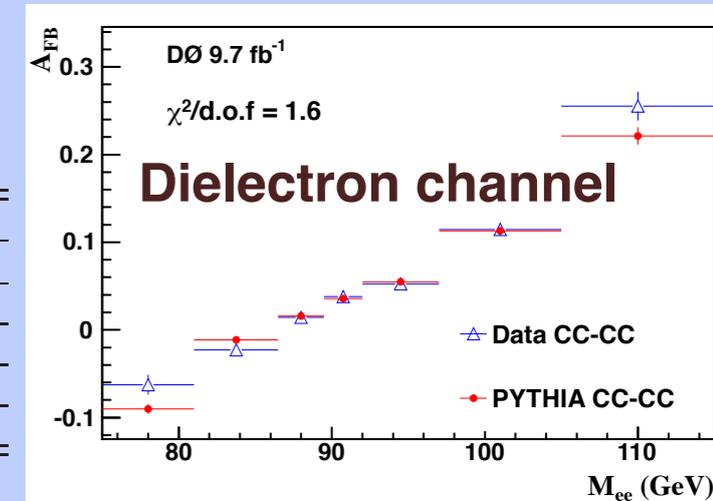
	$e^+e^-$ channel	$\mu^+\mu^-$ channel	Combined
$\sin^2\theta_{\text{eff}}^\ell$	0.23137	0.23016	0.23095
Statistical	0.00043	0.00059	0.00035
Systematic	0.00009	0.00006	0.00007
PDF	0.00017	0.00024	0.00019
Total	0.00047	0.00064	0.00040

$$\sin^2\theta_{\text{eff}}^\ell[\text{comb.}] = 0.23095 \pm 0.00035 \text{ (stat.)} \pm 0.00007 \text{ (syst.)} \pm 0.00019 \text{ (PDF)}$$

arXiv:1710.03951

Combine with previous measurement in electron channel to give a precision of two parts per thousand

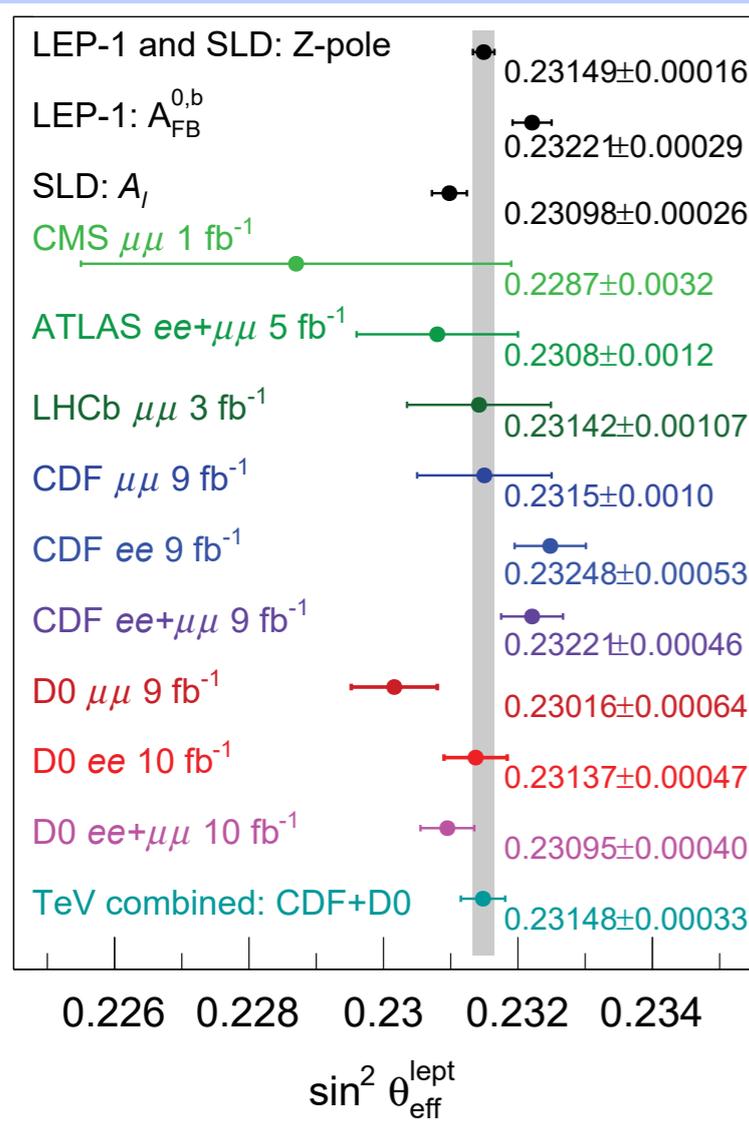
PRL 115, 041801 (2015)



# Forward-backward asymmetry @ the Tevatron

Combined results use common PDFs (NNPDF 3.0) and EW corrections (from ZFITTER)

Source	CDF inputs	Uncertainties on $\sin^2 \theta_{\text{eff}}^{\text{lept}}$	
		D0 inputs	Tevatron combination
Statistics	$\pm 0.00043$	$\pm 0.00035$	$\pm 0.00027$
Uncorrelated syst.	$\pm 0.00007$	$\pm 0.00007$	$\pm 0.00005$
PDF	$\pm 0.00016$	$\pm 0.00019$	$\pm 0.00018$

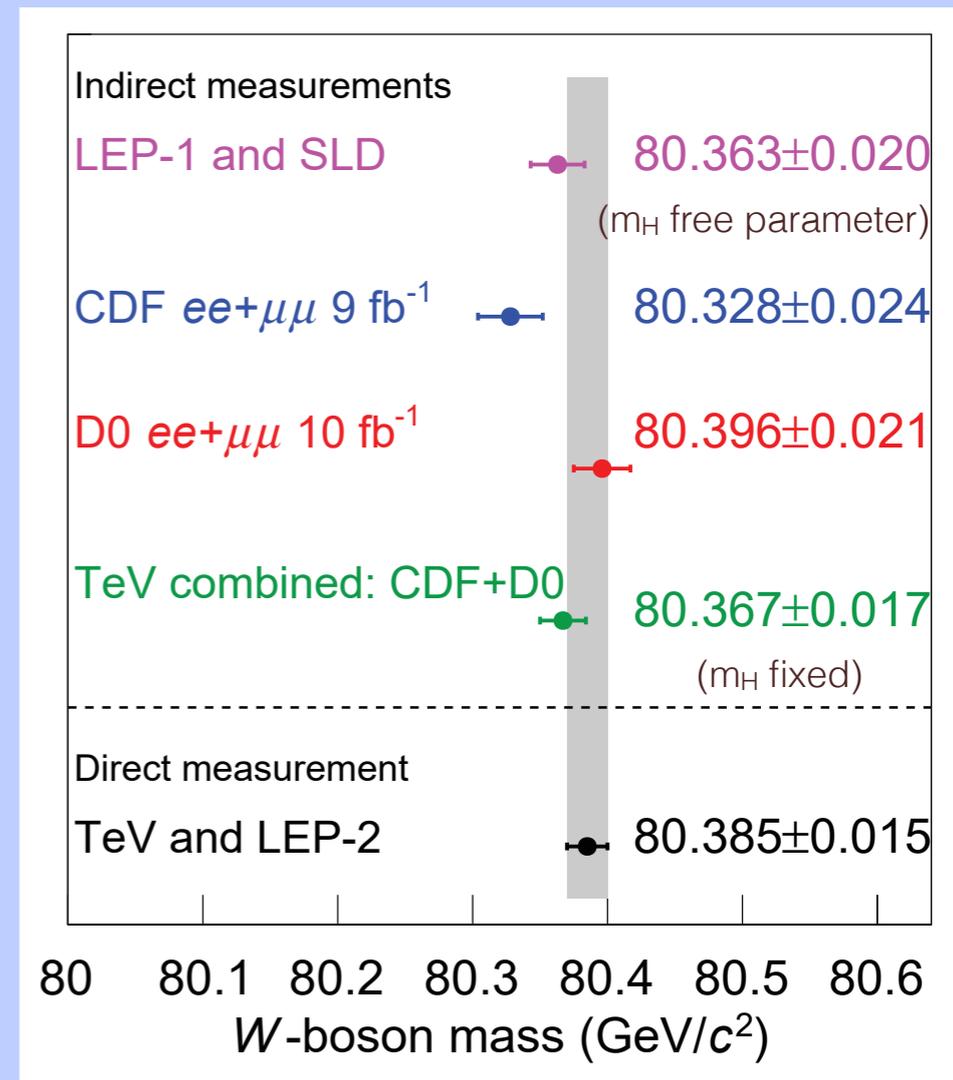


Tevatron uncertainty a factor of  $\sim 2$  higher than all  $e^+e^-$  measurements combined

Combined measurements consistent

Applying SM higher-order corrections indirectly determines  $W$  boson mass

Comparison with the direct measurement provides a test of the SM prediction



# W boson mass

W boson mass predicted at tree level using Fermi & EM couplings, and Z boson mass

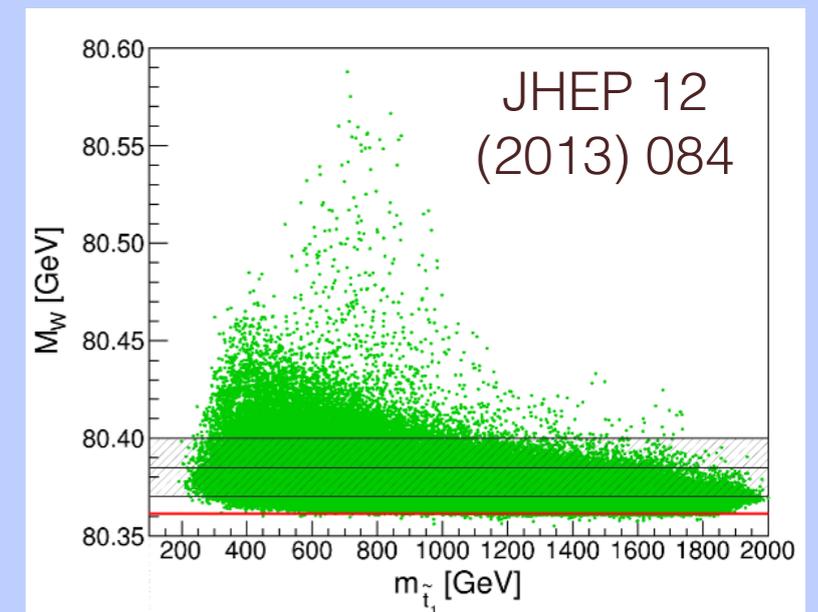
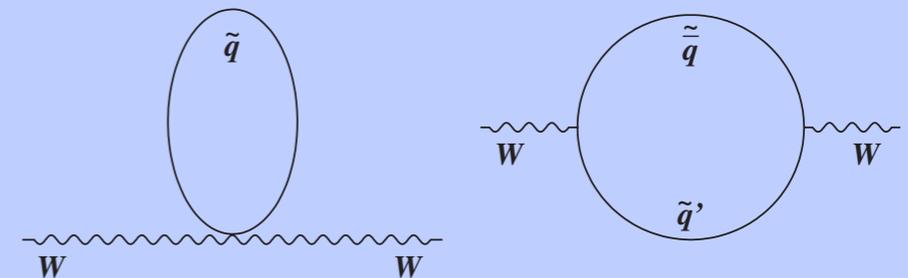
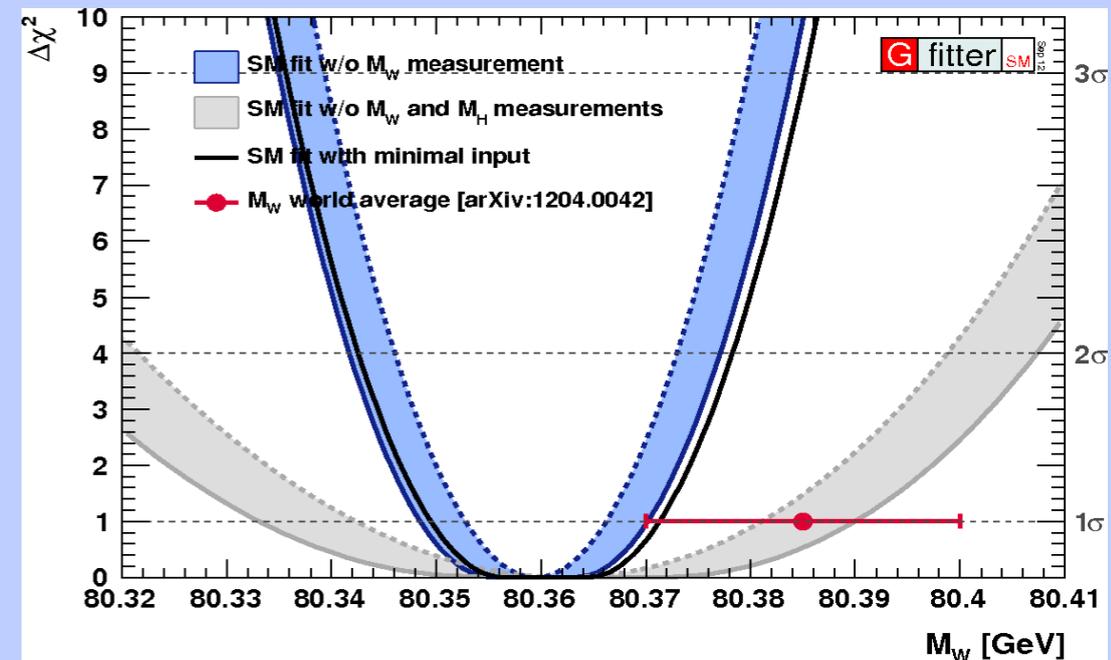
$$M_W^2 \left( 1 - \frac{M_W^2}{M_Z^2} \right) = \frac{\pi \alpha_{em}}{\sqrt{2} G_F} \frac{1}{1 - \Delta r}$$

Loop corrections constrained the Higgs boson mass prior to its discovery

Given the measured  $m_H$ , constrain loop corrections from Supersymmetry or other new physics

$$\Delta \rho_0^{\text{SUSY}} = \frac{3G_\mu}{8\sqrt{2}\pi^2} \left[ -\sin^2 \theta_{\tilde{t}} \cos^2 \theta_{\tilde{t}} F_0(m_{\tilde{t}_1}^2, m_{\tilde{t}_2}^2) - \sin^2 \theta_{\tilde{b}} \cos^2 \theta_{\tilde{b}} F_0(m_{\tilde{b}_1}^2, m_{\tilde{b}_2}^2) \right. \\ \left. + \cos^2 \theta_{\tilde{t}} \cos^2 \theta_{\tilde{b}} F_0(m_{\tilde{t}_1}^2, m_{\tilde{b}_1}^2) + \cos^2 \theta_{\tilde{t}} \sin^2 \theta_{\tilde{b}} F_0(m_{\tilde{t}_1}^2, m_{\tilde{b}_2}^2) \right. \\ \left. + \sin^2 \theta_{\tilde{t}} \cos^2 \theta_{\tilde{b}} F_0(m_{\tilde{t}_2}^2, m_{\tilde{b}_1}^2) + \sin^2 \theta_{\tilde{t}} \sin^2 \theta_{\tilde{b}} F_0(m_{\tilde{t}_2}^2, m_{\tilde{b}_2}^2) \right]$$

$$\rho = \frac{M_W^2}{M_Z^2 \cos^2 \theta_W} = \frac{1}{1 - \Delta \rho} \quad F_0(x, y) = x + y - \frac{2xy}{x - y} \ln \left( \frac{x}{y} \right).$$



# W boson mass @ the Tevatron

## Measurement strategy:

Measure momenta of charged lepton and neutrino in transverse plane

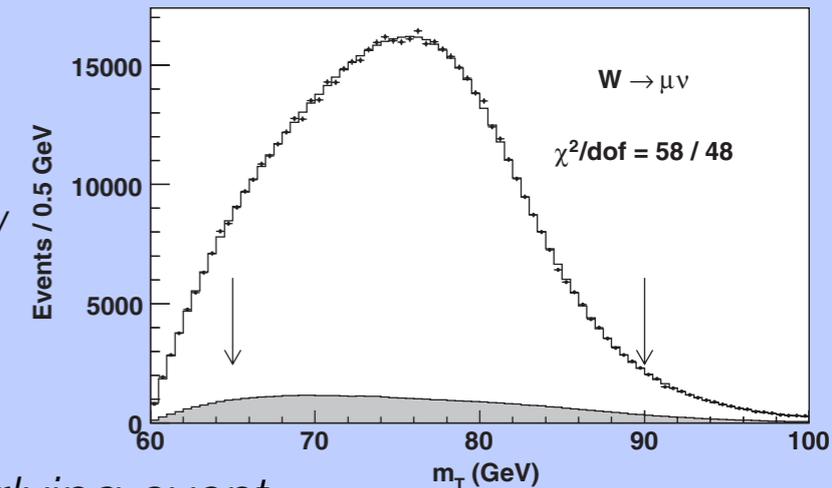
Construct the transverse mass in this plane and fit three distributions for  $m_W$

## Experimental and theoretical requirements:

Precise calibration of lepton momentum

Accurate calibration of detector response to initial-state radiation and underlying event

Accurate model of longitudinal and transverse momentum of the W boson



PRD 89,  
072003 (2014)

Tevatron instantaneous luminosities produce  $<10$  overlapping collisions on average

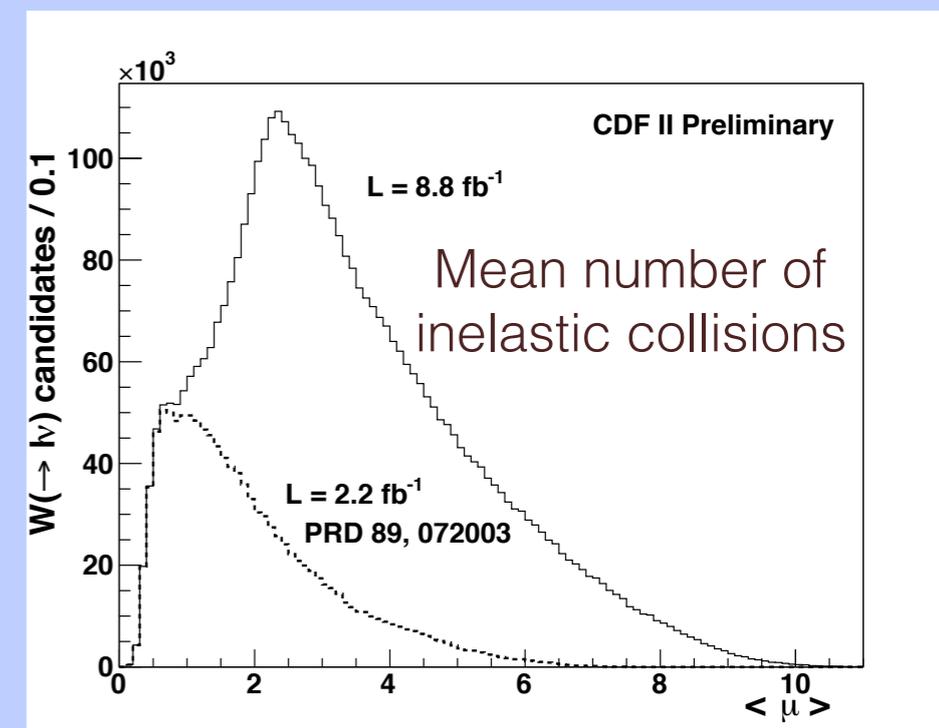
A large majority of W bosons are produced by valence quarks

CDF, 2.2 fb<sup>-1</sup>

D0, 4.3 fb<sup>-1</sup>

Source	Uncertainty (MeV)
Lepton energy scale and resolution	7
Recoil energy scale and resolution	6
Lepton removal from recoil	2
Backgrounds	3
<b>Experimental subtotal</b>	<b>10</b>
Parton distribution functions	10
QED radiation	4
$p_T(W)$ model	5
<b>Production subtotal</b>	<b>12</b>
<b>Total systematic uncertainty</b>	<b>15</b>
W-boson event yield	12
<b>Total uncertainty</b>	<b>19</b>

Source	Uncertainty (MeV)
Electron energy calibration	16
Electron resolution model	2
Electron shower modeling	4
Electron energy loss model	4
Recoil energy scale and resolution	5
Electron efficiencies	2
Backgrounds	2
<b>Experimental subtotal</b>	<b>18</b>
Parton distribution functions	11
QED radiation	7
$p_T(W)$ model	2
<b>Production subtotal</b>	<b>13</b>
<b>Total systematic uncertainty</b>	<b>22</b>
W-boson event yield	13
<b>Total uncertainty</b>	<b>26</b>



# W boson mass @ the Tevatron

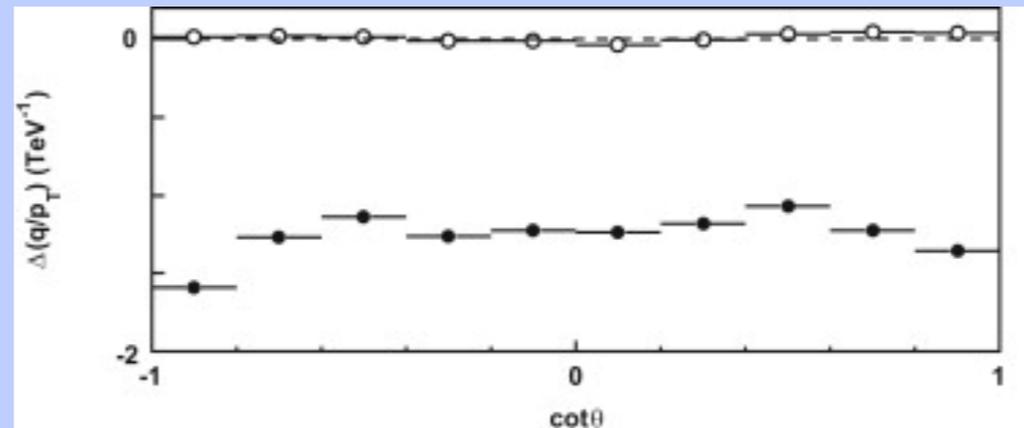
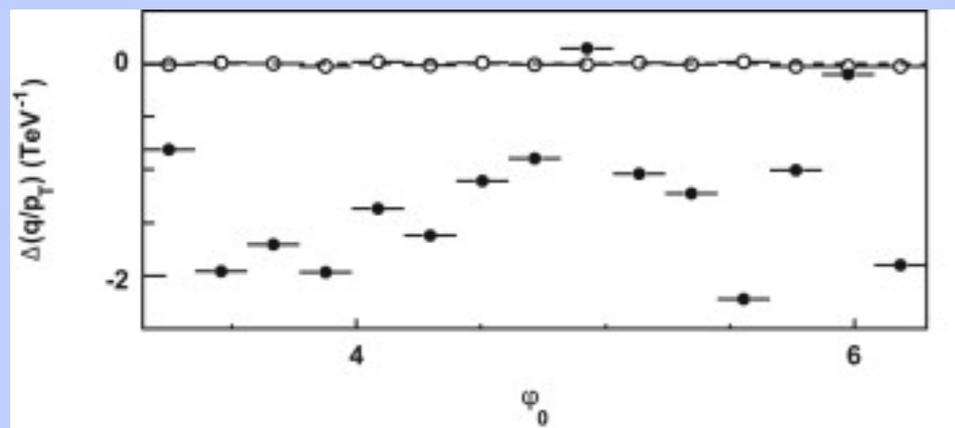
CDF & D0 analysing complete data sets

CDF tracker alignment for  $m_W$  updated

NIM A 762, 85 (2014)

*Azimuthal dependencies removed*

*Polar dependencies removed*



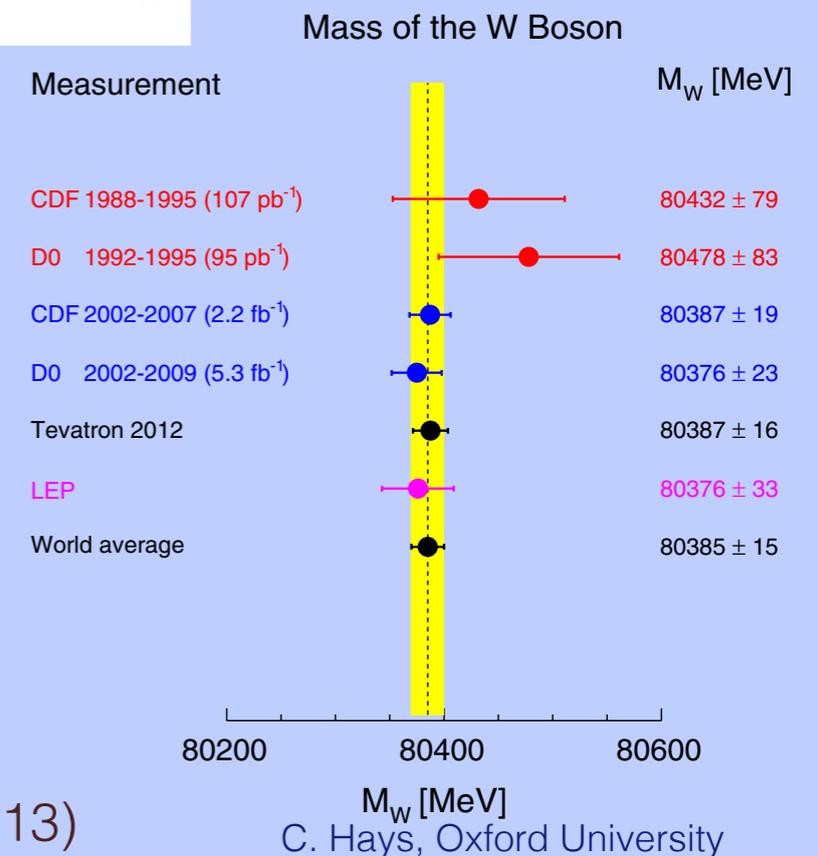
*Locations of wires at ends of drift chamber relatively aligned with cosmic tracks to a statistical precision of ~1 micron*

4.2 million  $W \rightarrow l\nu$  candidates in complete CDF data set

Potential to reduce Tevatron uncertainty to ~10 MeV (~0.01%)

*Will require reduction of PDF uncertainty to ~5 MeV*

Important to include Tevatron charge asymmetry measurements in PDFs



PRD 88,  
052018 (2013)

# W boson charge asymmetry @ the Tevatron

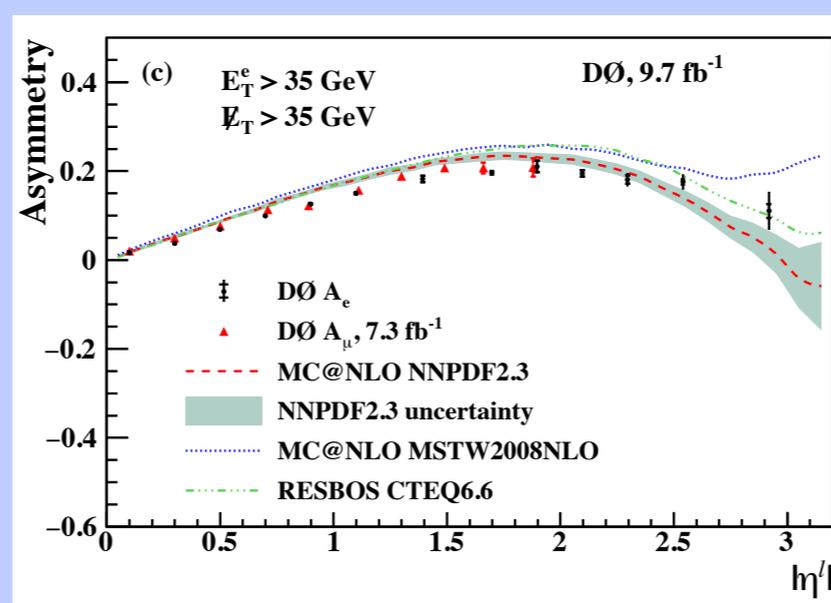
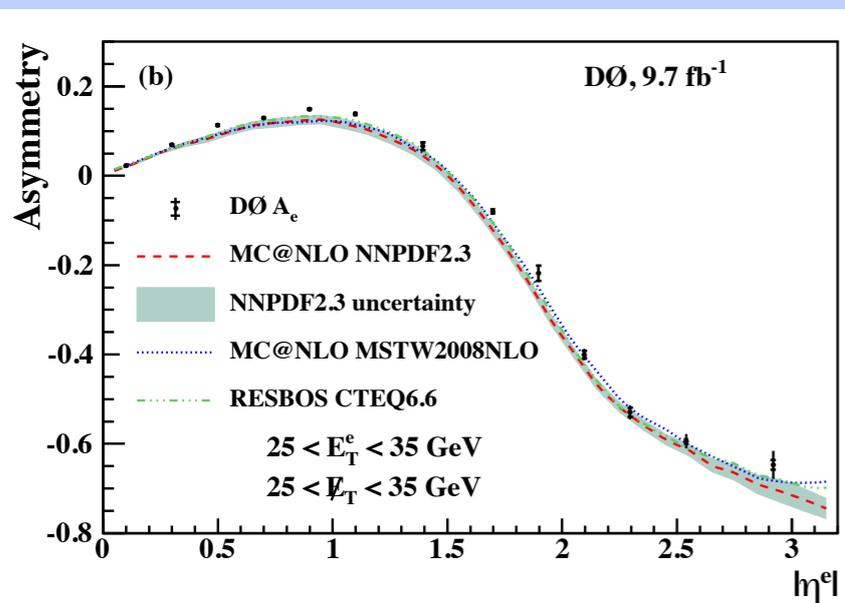
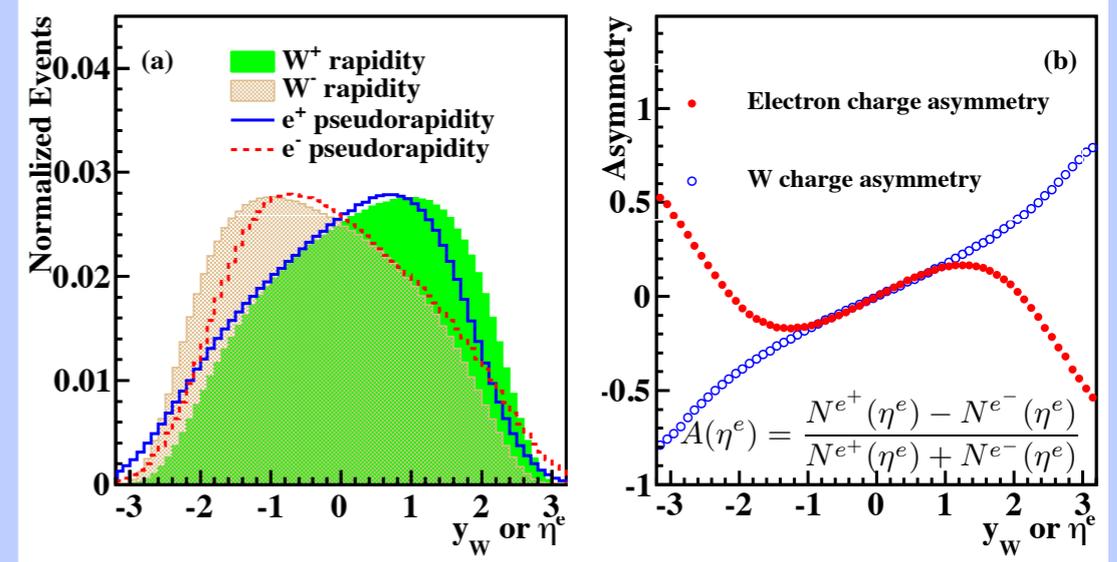
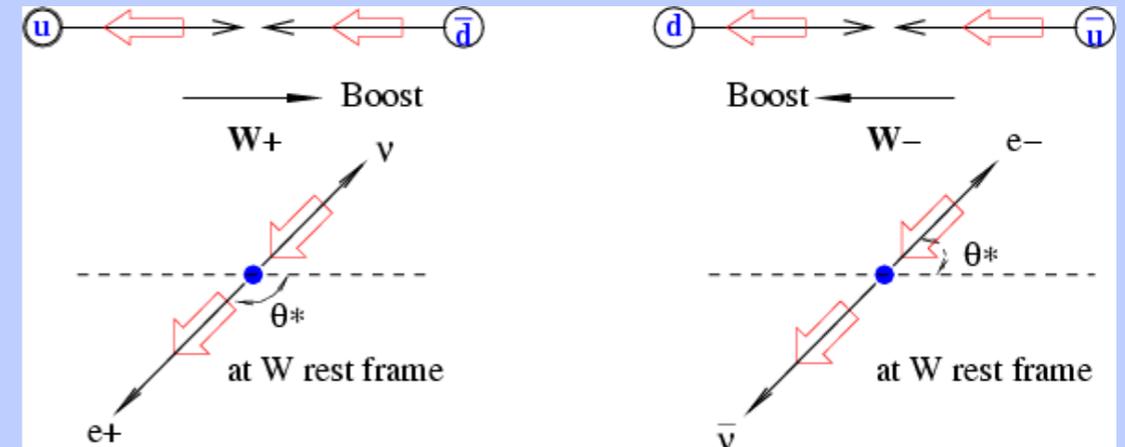
PRL 102, 181801 (2009)

Asymmetry in valence u and d quark momentum distributions leads to  $W^+/W^-$  asymmetry as a function of boson rapidity

Left-handed decay counteracts asymmetry for charged leptons

Comparisons of measurements in ranges of lepton  $p_T$  to predictions constrains PDFs

D0 asymmetries with complete data set included in NNPDF 3.1



PRD 91, 032007 (2015)

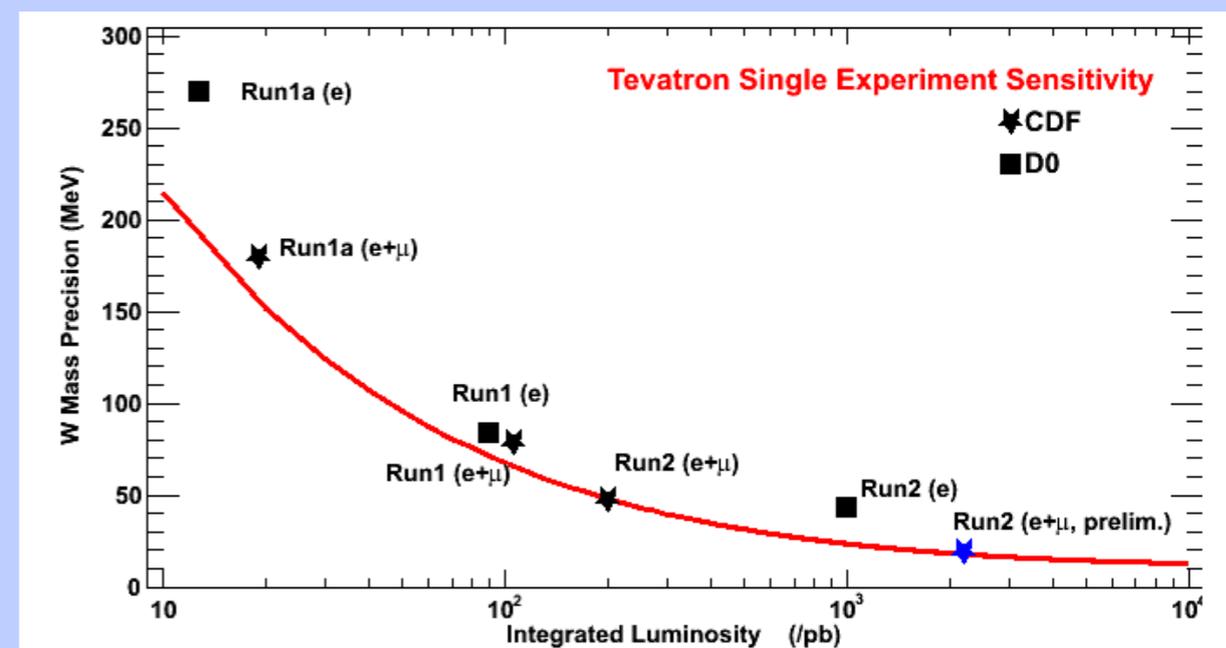
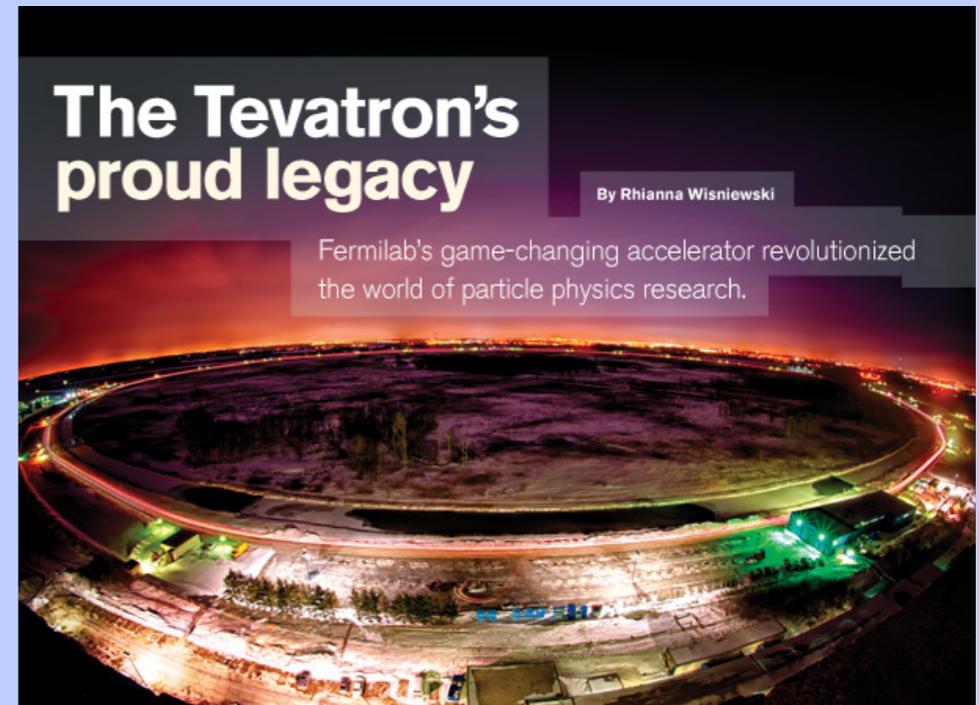
CDF electron asymmetry with complete data set ongoing

# Summary

Tevatron completing legacy electroweak measurements

**Z boson coupling** final measurements combined

**W boson mass** final measurements ongoing



# Summary

Tevatron completing legacy electroweak measurements

**Z boson coupling** final measurements combined

**W boson mass** final measurements ongoing

