

Basic principles How to generate Inflation ? Predictions and observations

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1-Basic principles



What is Inflation ?

Period of accelerated expansion in the early Universe + it must have an end to allow gravity to form galaxies (reheating)

A.H. Guth, Phys. Rev. D23, 347, 1981

1-Basic principles

In equations (classical dynamics)...

NB: everywhere « comoving » is implicit and a is the scale factor





We want the Hubble radius today (0) to fit in the Hubble radius at the time of inflation (I):



 $(a_0H_0)^{-1} < (a_IH_I)^{-1}$.

at first order, with a simple back of the enveloppe calculation, it can be shown that this is equivalent to:

 $\frac{a_E}{a_I} > 10^{28} \quad \Rightarrow \quad \ln\left(\frac{a_E}{a_I}\right) > 64 \; .$

solved....given such constraint ! and this is where comes the « **about 60e-folds are required to solve the horizon problem** »

Why Inflation ?

Inflation was introduced to solve the problems of standard Big Bang cosmology: The horizon problem The flatness problem The monopole problem

Flatness problem

Total energy density and curvature:

$$1 - \Omega(a) = \frac{-k}{(aH)^2} \; ,$$

But we have seen that, during inflation: (aH)⁻¹ decreases !

The Monopole Problem:

Inflation allows for magnetic monopoles to exist as long as they were produced prior to the period of inflation. During inflation, their density drops exponentially,

1-Basic principles

Flatness and monopoles problems





2-Which mechanism for Inflation ?

1- The simplest way: homogeneous scalar field driven out of equilibrium

Consider a scalar field ϕ , the inflaton, minimally coupled to Einstein gravity:

$$S = \int \mathrm{d}^4 x \sqrt{-g} \left[\frac{M_{\rm pl}^2}{2} \mathcal{R} - \frac{1}{2} g^{\mu\nu} \partial_\mu \phi \partial_\nu \phi - V(\phi) \right]$$

The evolution equation of the scalar field is governed by the Klein Gordon equation:

 $\ddot{\phi} + 3H\dot{\phi} = -V'$ with $V' \equiv dV/d\phi$.

Here: the **potential acts like a force**, V', while the **expansion of the universe adds friction**: $H\dot{\phi}$.



NB: From Friedmann equations, we have:

$$\dot{H} = -\frac{1}{2} \frac{\dot{\phi}^2}{M_{\rm pl}^2} \qquad \qquad H^2 = \frac{1}{3M_{\rm pl}^2} \left[\frac{1}{2} \dot{\phi}^2 + V \right]$$

2-Which mechanism for Inflation ?

2- Even simpler: slow-roll

We can make ε explicit:

 $V(\phi)$

 $\varepsilon \equiv -\frac{\dot{H}}{H^2} = \frac{\frac{1}{2}\dot{\phi}^2}{M_{\rm pl}^2 H^2} < 1$

Inflation occurs if the kinetic term only makes a small contribution of the total energy

This is what is called the **slow-roll inflation** (no approximation so far!)

In order for this condition to persist the acceleration of the scalar field has to be small, we often define:

$$\eta = \frac{\dot{\varepsilon}}{H\varepsilon} = 2\frac{\ddot{\phi}}{H\dot{\phi}} - 2\frac{\dot{H}}{H^2}$$

which has to be small too !

To make sure that inflation occurs and persists (here is the approximation!):

Φ

$$\{\varepsilon, |\eta|\} \ll 1.$$

$$\epsilon_{v} \equiv \frac{M_{pl}^{2}}{2} \left(\frac{V'}{V}\right)^{2} , \quad |\eta_{v}| \equiv M_{pl}^{2} \frac{|V''|}{V}$$

$$V' = dV/d\phi$$

2-Which mechanism for Inflation ?

<u>3-But...there a lot of different inflation models !</u>

old, new, pre-owned, chaotic, quixotic, ergodic, ekpyrotic, autoerotic, faith-based, free-based, brane, braneless, brainless, supersymmetric, supercilious, natural, supernatural, *au natural,* hybrid, low-bred, white bread, one-field, two-field, left-field, eternal, internal, infernal, self-reproducing, self-promoting,

[adapted from R. Kolb]



3-Predictions of Inflation

Scalar and Tensor Perturbations

Inflation does predict the existence of two types of perturbations:

- fluctuations of the scalar inflaton field: **scalar perturbations**
- fluctuations of the gravitational field: tensor perturbations (or primordial gravitational waves, those are the B-modes!)



The tensor to scalar ratio, r, is given by:

$$r = \frac{T}{S} = 8M_{\rm Pl}^2 \left(\frac{V_\phi}{V}\right)^2 < 1$$

This is what we are trying to tackle in the **search for CMB B-modes**!

Tensor Perturbations Power Spectrum

slope: $n_{\rm T} = M_{\rm Pl}^2 \left(\frac{V_{\phi}}{V}\right)^2$

adapted from J. Martin]

3-Predictions of Inflation



Spatial flatness

Adiabatic initial Conditions

Nearly Gaussian initial fluctuations



Almost (but not exactly) scale-invariant scalar perturbations



Background of primordial gravitational waves



Tensor to scalar ratio



Table 5. Constraints on 1-parameter extensions to the base Λ CDM model for combinations of *Planck* power spectra, *Planck* lensing, and external data (BAO+JLA+H₀, denoted "ext"). All limits and confidence regions quoted here are 95 %.

Parameter	TT	TT+lensing	TT+lensing+ext	TT, TE, EE	TT, TE, EE+lensing	TT, TE, EE+lensing+ext
Ω _K	$-0.052\substack{+0.049\\-0.055}$	$-0.005^{+0.016}_{-0.017}$	$-0.0001^{+0.0054}_{-0.0052}$	$-0.040\substack{+0.038\\-0.041}$	$-0.004^{+0.015}_{-0.015}$	$0.0008^{+0.0040}_{-0.0039}$



Constraints on the correlated matter isocurvature mode amplitude parameter α , where $\alpha = 0$ corresponds to purely adiabatic perturbations.





4- Tests and Results

C. Caprini

primordial gravitational wave background

Observational bounds/sensitivities for SGWB



4- Tests and Results

[Planck 2015 results. XVII, arXiv :1502.01592] [Bicep2/KeckArray, arXiv:1510.09217]

tensor to scalar ratio



Still a long road to probe inflation



"No doubt about it, Ellington-we've mathematically expressed the purpose of the universe. God, how I love the thrill of scientific discovery!" ◇ Of course we are expecting a (short-term) measurement of primordial gravitational waves (through B-modes detection) !

Then still a long road to definitely state which mechanism led to Inflation and characterize its parameters (shape of the potential...)

 We will need all the cosmo data to get the overall picture (more accurate Ω_K,f_{NL},n_s...)
 S4/LiteBIRD/LSST/Euclid/LISA/SKA +cross-correlations (...)



More Inflation from galaxy clustering

 Primordial non-Gaussianity from the halo bispectrum Sefusatti et al 2

Sefusatti et al 2006, Baldauf et al 2011 Baldauf et al 2016, Doré et al 2015, ...

- Equilateral: $\sigma(f_{NL}) \sim 10$ Local: $\sigma(f_{NL}) < 1$
- Spectral index, n_s , and running α_s EUCLID: $\sigma(n_s) = 0.006 \rightarrow 0.002$ $\sigma(\alpha_s) = 0.009 \rightarrow 0.003$ Amendola et al 2016
- Features in the primordial power spectrum Chen et al 2016, Ballardini et al 2016,

Single field slow-roll inflation

0.005



SPHEREx galaxy clustering can reach $\sigma(f_{NL}) < 1$

[DePutter IPA 2016]