

# Sterile neutrino dark matter

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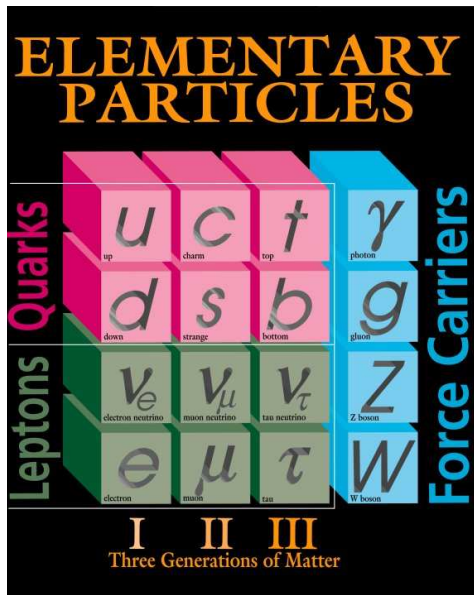
together with M. Shaposhnikov, A. Boyarsky *and many others*

**IDM 2010**

**Montpellier. July 29, 2010**

# Dark matter - a fundamental physics problem

- Is evidence for missing mass convincing? — **yes**
- If dark matter is made of particles – **what are they?**



**Dark matter particles are not part of the Standard Model of particle physics**

# Why (and where) we expect new physics?

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- **Dark matter** (not a SM particle!)
  - particles with weak cross-section will have correct abundance  $\Omega_{\text{DM}}$  (“WIMP miracle”). **New scale**  $\sim 1$  TeV
  - Axions. **New scale**  $10^{10} - 10^{12}$  GeV.
- **Baryon asymmetry of the Universe:** what ensured that for each  $10^{10}$  anti-protons there was  $10^{10} + 1$  proton in the early Universe?
  - **Sakharov conditions:** CP-violation; B-number violation; out-of-equilibrium particles.
  - **Example:** Out-of-equilibrium decay of heavy lepton  $\chi$  at temperatures  $M_{\text{EW}} < T_{\text{decay}} < M_{\chi}$  produces correct baryon-to-entropy ratio for  $M_{\chi} > 10^{11}$  GeV – **new energy scale**
- **Fine-tuning problems:** CP-problem, hierarchy problem, grand unification, cosmological constant problem

## Example : WIMPs

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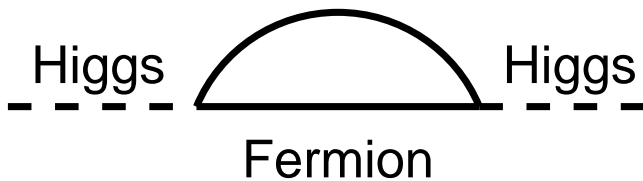
<sup>40</sup>WIMP<sup>©</sup> is a copyrighted trademark of the Chicago group, standing for **Weakly Interacting Massive Particle**.

- Many particle physicists would like a new physics to appear around 100 GeV–10 TeV scale.
- Most popular candidates: **WIMPs** – stable particles produced in *thermal freeze-out*:  $\dot{n} + 3Hn = -\langle\sigma|v|\rangle(n^2 - n_{\text{eq}}^2)$
- Main properties of WIMPs:
  - Stable particles
  - Annihilate into ordinary matter (unitarity bound: annihilation cross-section is bounded  $\sigma \lesssim \frac{1}{m_\chi^2}$ )
  - mass :  $\sim$  GeV – TeV range
  - Decouple from plasma non-relativistic (“cold”)
- WIMPs can be searched in direct detection experiments (interaction of galactic WIMPs with laboratory nucleons).

# Hierarchy problem

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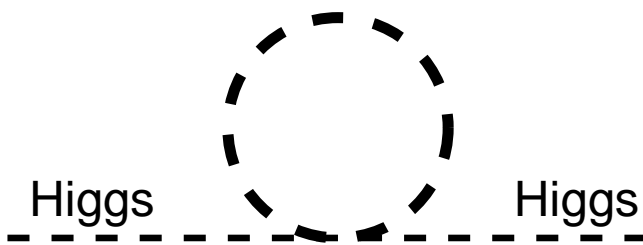
Quantum corrections to the Higgs mass:



? ↓

$$100 \text{ GeV} < M_H < 300 \text{ GeV}$$

↑



- Masses of fermions are provided by the Higgs field
- Fermion corrections to the Higgs mass are proportional to their mass  $M_f^2$ .
- Contributions from heavy fermions ( $M_f \gg 100 \text{ GeV}$ ) would make Higgs mass heavy  $M_H \sim M_f$
- To keep Higgs boson light, one should “unnaturally” **fine-tune** the parameters of the model to cancel fermions’ contribution by that of Higgs

## Alternatives?

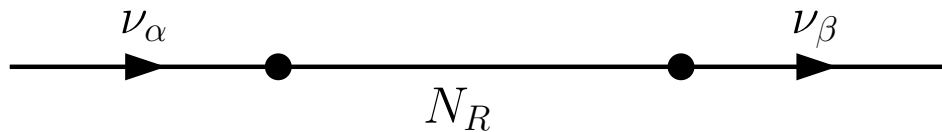
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Build a model that resolves several  
BSM phenomena within its framework.  
Worry about fine-tunings later

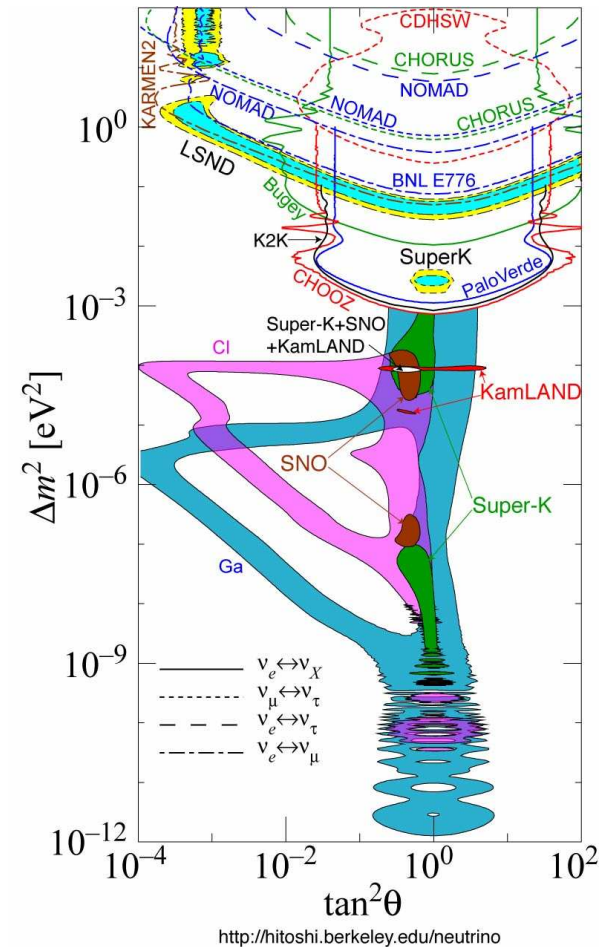
# Neutrino oscillations

- Experiments on neutrino oscillations determined **two** mass differences between neutrino mass states

- Sterile (right-handed) neutrinos** provide the simplest and natural extension of the Minimal SM that describe oscillations.



- Make leptonic sector of the SM symmetric.



## See-saw Lagrangian

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Add right-handed neutrinos  $N_I$  to the Standard Model

$$\mathcal{L}_{\text{right}} = i\bar{N}_I \not{\partial} N_I + \underbrace{\begin{pmatrix} \bar{\nu}_e \\ \bar{\nu}_\mu \\ \bar{\nu}_\tau \end{pmatrix} \begin{pmatrix} F \langle H \rangle \end{pmatrix}}_{\text{Dirac mass } M_D} \begin{pmatrix} N_1 \\ N_2 \\ \dots \end{pmatrix} + \underbrace{\begin{pmatrix} N_1^c \\ N_2^c \\ \dots \end{pmatrix} \begin{pmatrix} M \end{pmatrix}}_{\text{Majorana mass}} \begin{pmatrix} N_1 \\ N_2 \\ \dots \end{pmatrix}$$

$\nu_\alpha = \tilde{H} L_\alpha$ , where  $L_\alpha$  are left-handed lepton doublets

- Active masses are given via usual **see-saw formula**:

$$(m_\nu) = -M_D \frac{1}{M_I} M_D^T \quad ; \quad M_D \ll M_I$$

- Neutrino mass matrix – **7 parameters**. Dirac+Majorana mass matrix – **11 (18) parameters** for 2 (3) sterile neutrinos. **Two** sterile neutrinos are enough to fit the neutrino oscillations data.

**Scale of Dirac and Majorana masses is not fixed!**



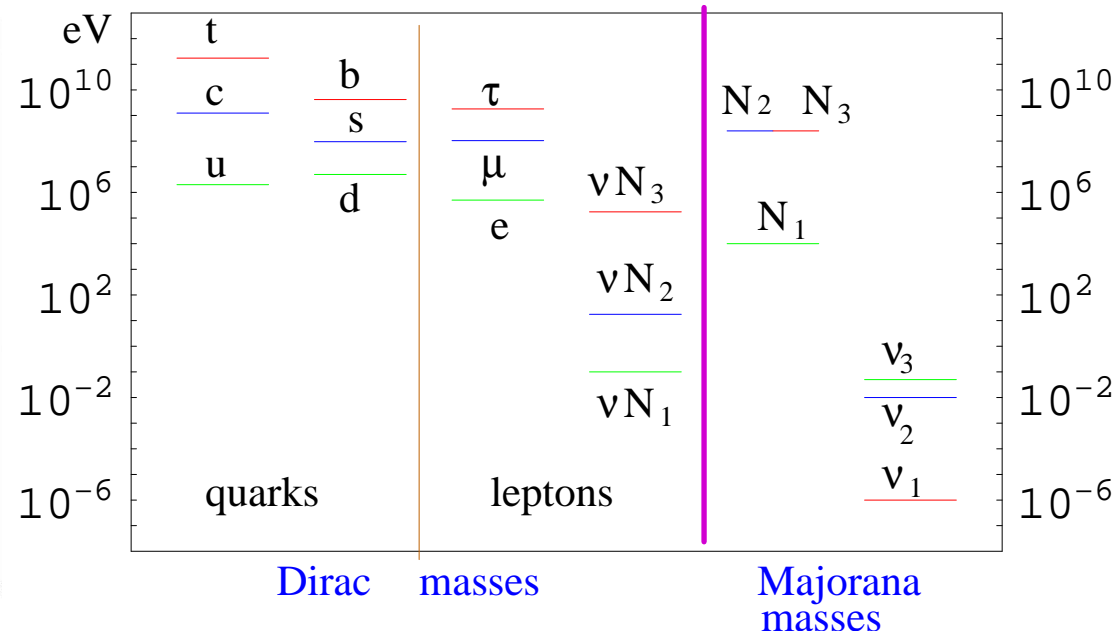
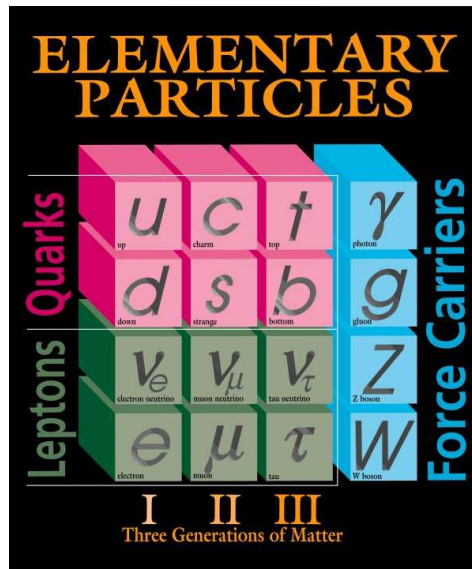
## The scale of right-handed masses?

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### “Popular” choices of see-saw parameters

- Yukawa couplings  $F_{\alpha I} \sim 1$ , i.e. Dirac masses  $M_D \sim M_t$ . Majorana masses  $M_I \sim 10^{15}$  GeV.
- Attractive features:
  - Provides a mechanism of baryon asymmetry of the Universe
  - Scale of Majorana masses is possibly related to GUT scale
- This model **does not provide the dark matter particle**
- Alternative? Choose Majorana masses  $M_I$  of the order of masses of other SM fermions and make Yukawa couplings small

# Neutrino minimal Standard Model ( $\nu$ MSM)



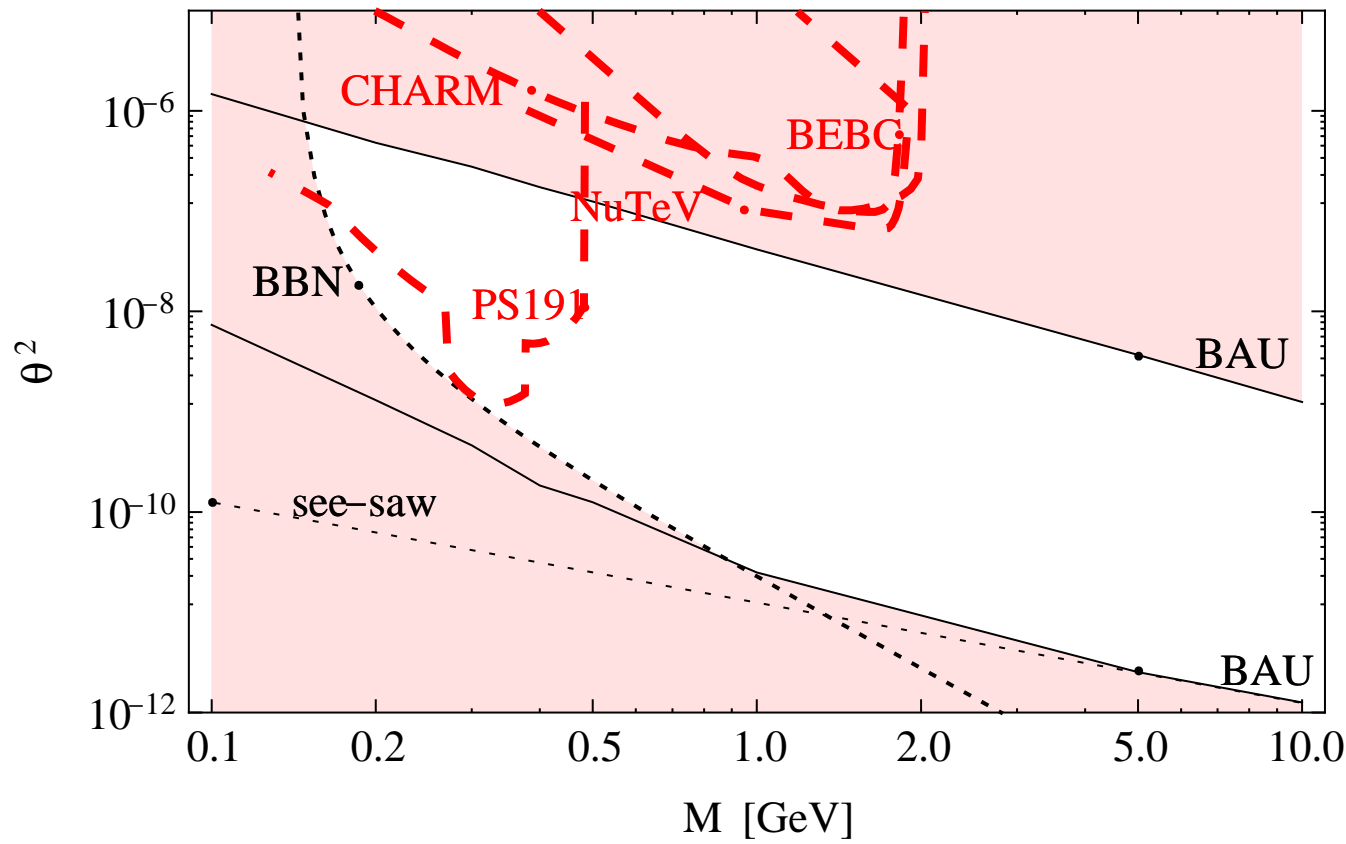
The model solves several *beyond the Standard Model problems*

- ✓ ... explains neutrino oscillations
- ✓ ... matter-antimatter asymmetry of the Universe
- ✓ ... provides a viable dark matter candidate that can be cold, **warm** or **mixed** (cold+warm)

## Choosing parameters of the $\nu$ MSM

- If  $M_{2,3} \sim 10 \text{ MeV} - 20 \text{ GeV}$  and  $\Delta M_{2,3} \ll M_{2,3}$   $\nu$ MSM explains **baryon asymmetry** of the Universe.
- Neutrino experiments can be explained within the same choice of parameters.

Asaka,  
Shaposhnikov  
'05;  
Canetti,  
Shaposhnikov  
'10



## Parameters of the third sterile neutrino?

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- The third sterile neutrino can couple to the SM arbitrarily weakly.  
**Dark matter candidate?**
- Any DM candidate must be
  - Produced in the early Universe and have correct relic abundance
  - Be stable or cosmologically long-lived
  - Very weakly interacting with electromagnetic radiation (“dark”)
  - Allow to explain the observed large scale structure

## Mass of sterile neutrino DM?

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- The model-independent lower limit on the mass of **fermionic** DM
- The smaller is the DM particle mass – the bigger is the number of particles within some region of phase-space density (defined by velocity dispersion  $\sigma$  and size  $R$ )
- For fermions Pauli principle restricts number of fermions
- Bound on any fermionic DM improved to become

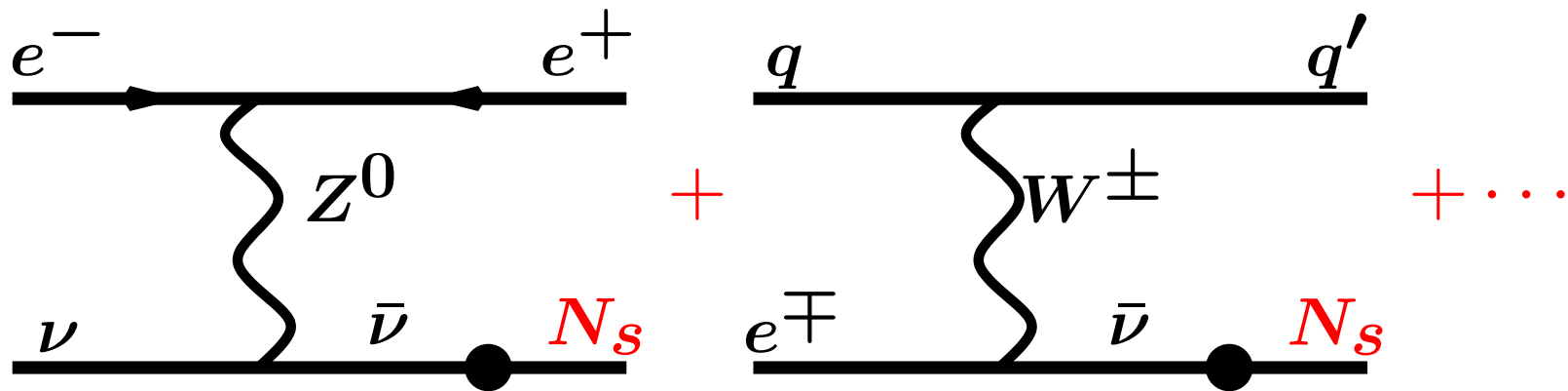
$$M_s > 0.41 \text{ keV}$$

Tremaine,  
Gunn (1979)

Boyarsky,  
O.R.,  
Iakubovskyi'08

## How sterile neutrino DM is produced?

- Phenomenologically acceptable values of  $\theta_1$  are so small, that the rate of this interaction  $\Gamma$  of sterile neutrino with the primeval plasma is much slower than the expansion rate ( $\Gamma \ll H$ )  
 $\Rightarrow$  Sterile neutrino are never in **thermal equilibrium**
- **Simplest scenario:** sterile neutrino in the early Universe interact with the rest of the SM matter via **neutrino oscillations:**



- Production is sharply peaked at

$$T_{\max} \simeq 130 \left( \frac{M_s}{\text{keV}} \right)^{1/3} \text{ MeV}$$

## Production through oscillations

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- Sterile neutrinos have non-equilibrium spectrum of primordial velocities, roughly proportional to the spectrum of active neutrinos

$$f_s(p) \propto \frac{\theta^2}{\exp(\frac{p}{T_\nu}) + 1}$$

- Their amount less than that of active neutrinos

$$\Omega_s h^2 \propto \theta^2 \frac{M_s}{94 \text{ eV}} \quad \text{recall: SM neutrinos } \Omega_\nu h^2 = \frac{\sum m_\nu}{94 \text{ eV}}$$

- Average momentum  $\langle p_s \rangle \sim \langle p_\nu \rangle \gg M_s$  – **sterile neutrinos are produced relativistic**

# Resonant production

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- The presence of lepton asymmetry in primordial plasma makes **active-sterile mixing** much more effective – **resonant production**
- Typically, one expect the lepton asymmetry to be  $\sim \eta_B$  (sphalerons equilibrate the two)
- In the  $\nu$ MSM CP-violating scatterings/decays of sterile neutrinos continue to generate lepton asymmetry **below** the sphaleron scale thus making it significantly large than  $\eta_B$
- The value of lepton asymmetry can be as large as

$$L_6 \equiv 10^6 \frac{n_{\nu_e} - n_{\bar{\nu}_e}}{s} \lesssim 700$$

(present BBN bound  $L_6^{\text{BBN}} \lesssim 2500$ )

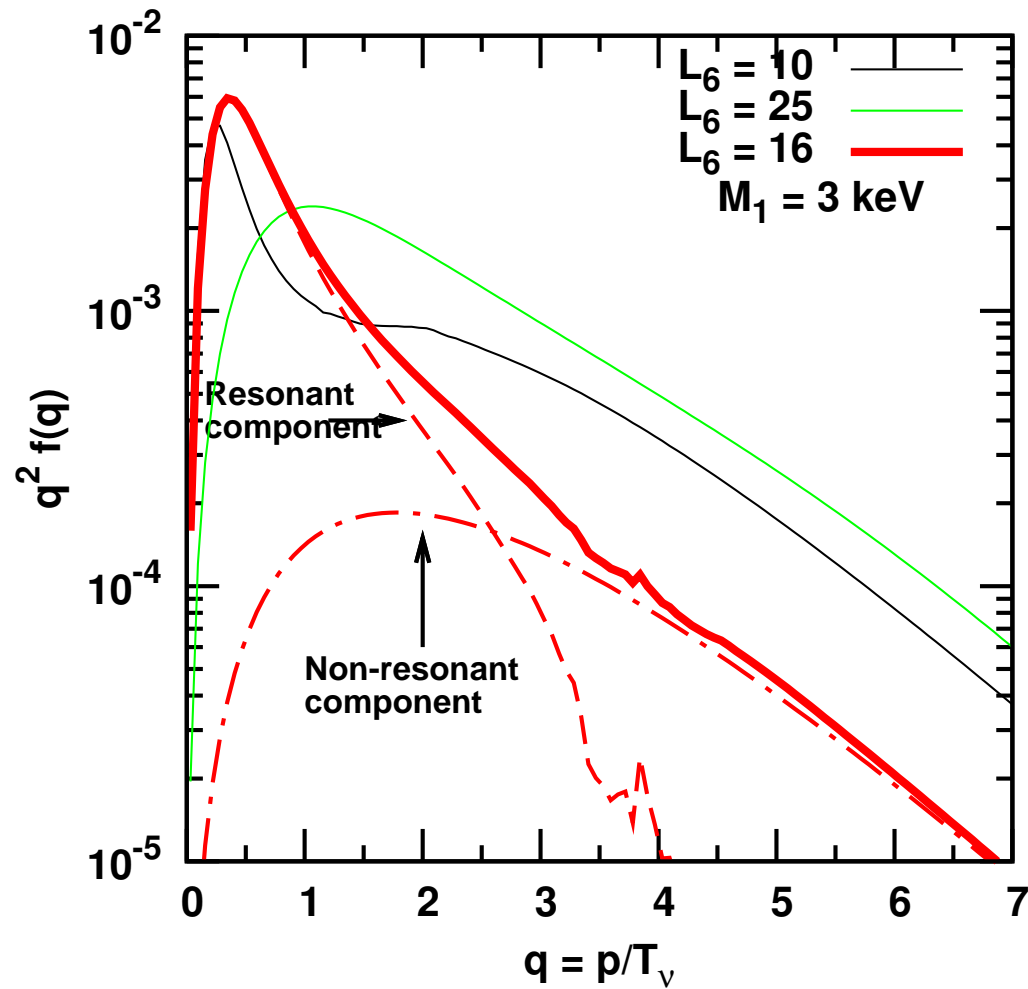
Shi Fuller'98  
Laine,  
Shaposhnikov

Shaposhnikov

Serpico,  
Raffelt'05



# RP sterile neutrino spectra



Laine, Shaposhnikov'08; Boyarsky, O.R., Shaposhnikov'09

# Sterile neutrinos and structure formation

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- Sterile neutrinos are ultra-relativistic at production

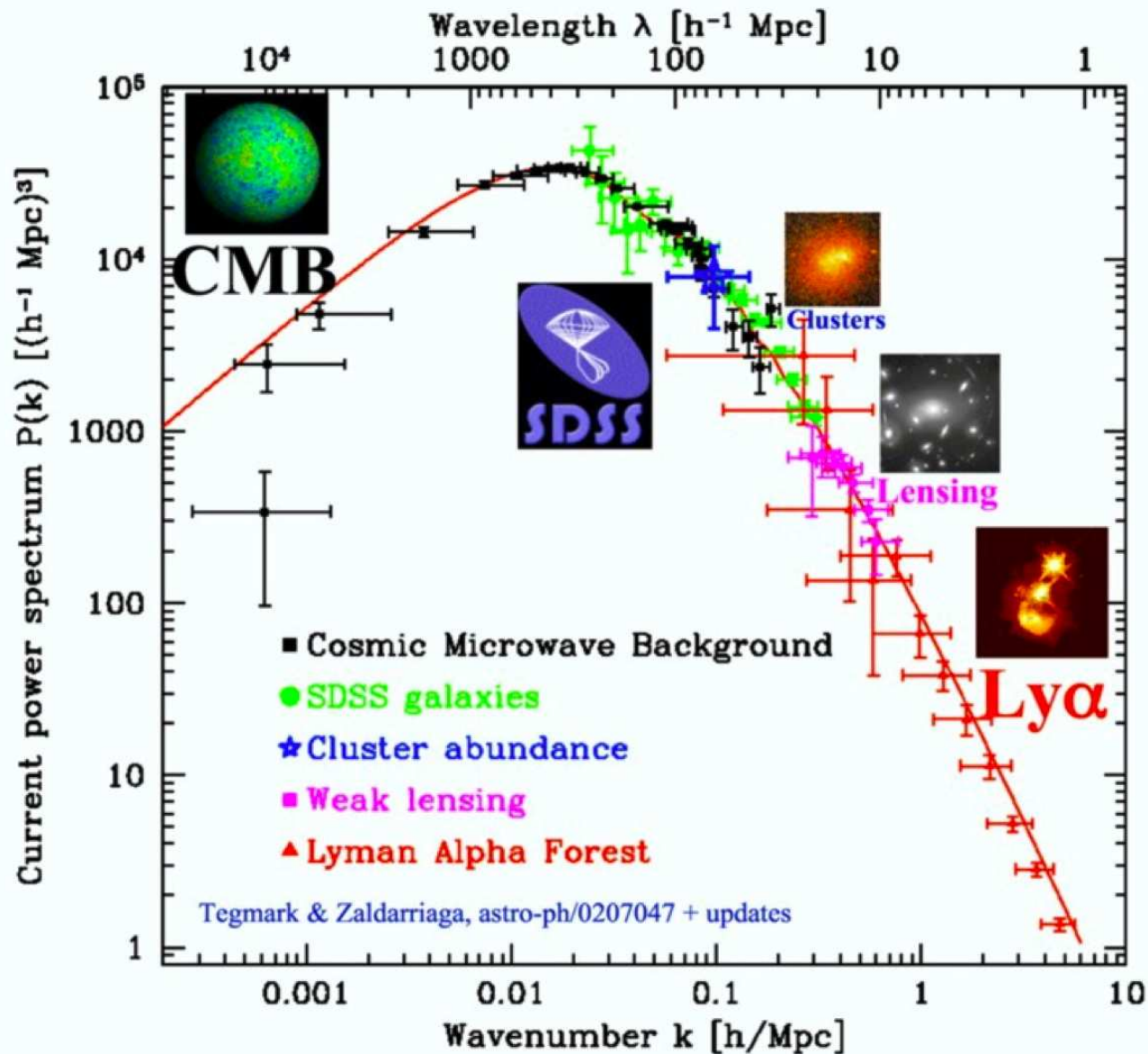
- DM particles erase primordial spectrum of density perturbations on scales up to the DM particle horizon – **free-streaming length**

$$\lambda_{FS}^{co} = \int_0^t \frac{v(t') dt'}{a(t')}$$

- Comoving free-streaming lengths peaks around  $t_{nr}$  when  $\langle p \rangle \sim m$
- Free-streaming horizon determines suppression scale of power spectrum of density perturbations.
- An order of magnitude estimate for the free-streaming scale?

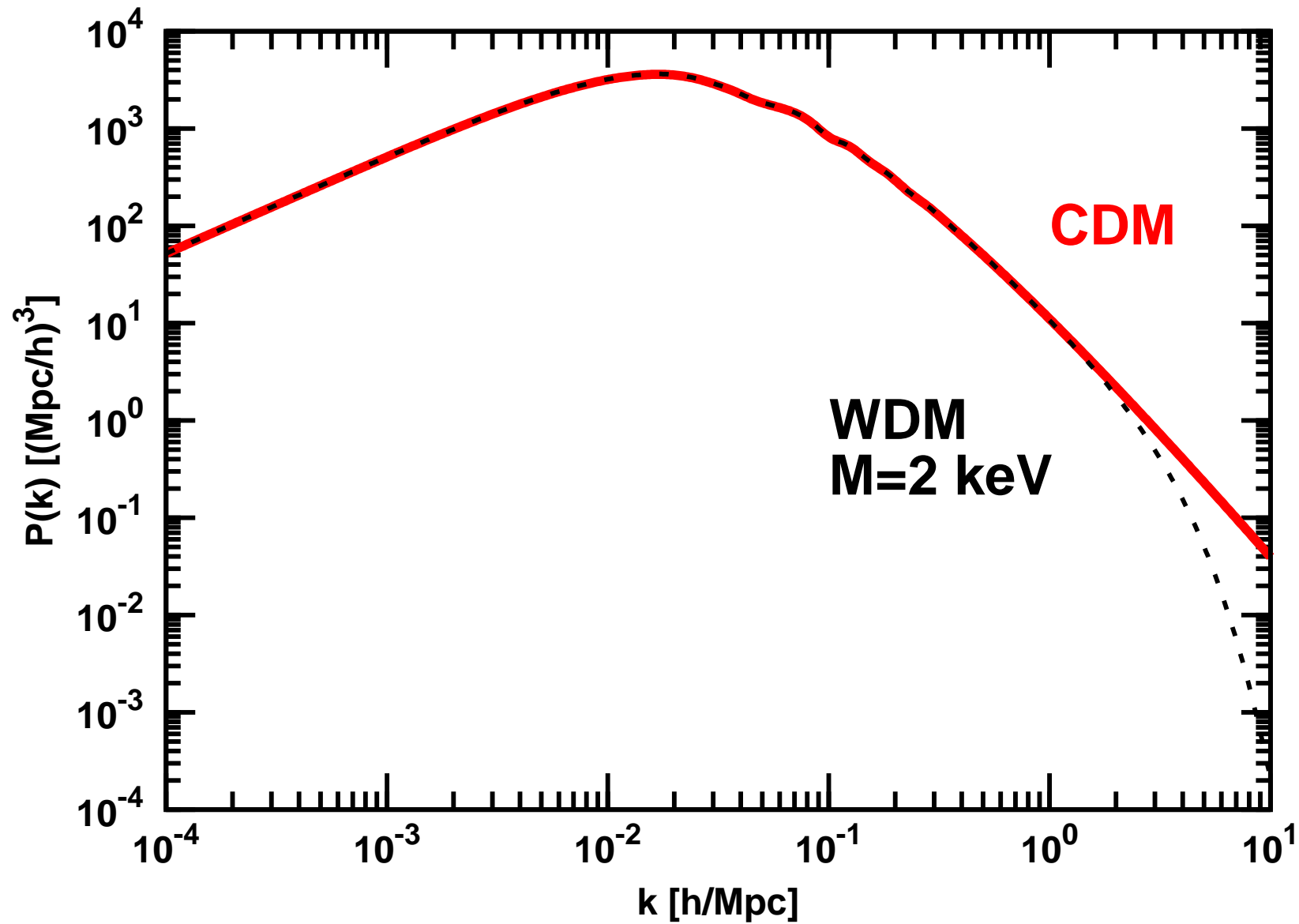
$$\lambda_{FS}^{co} \sim 1 \text{ Mpc} \left( \frac{\text{keV}}{M_s} \right) \frac{\langle p_s \rangle}{\langle p_\nu \rangle}$$

# Power spectrum of density fluctuations

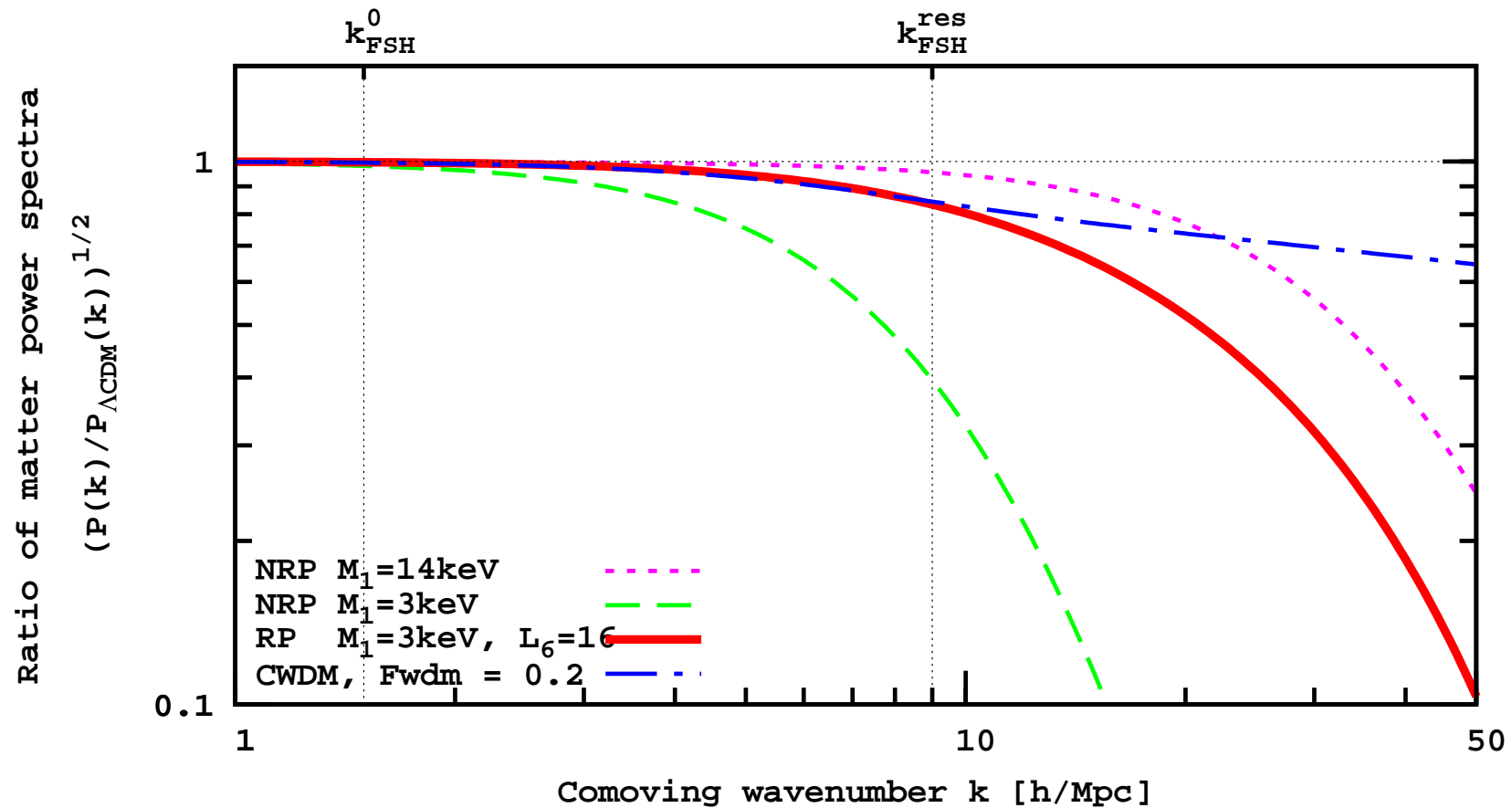


Max Tegmark  
Univ. of Pennsylvania  
max@physics.upenn.edu  
TAUP 2003  
September 5, 2003

# Influence of primordial velocities



# Power spectrum for sterile neutrinos



Boyarsky, Lesgourgues, **O.R.**, Viel JCAP, PRL 2009;

Boyarsky, **O.R.**, Shaposhnikov Ann. Rev. Nucl. Part. Sci. 2009

# Lyman- $\alpha$ forest and cosmic web

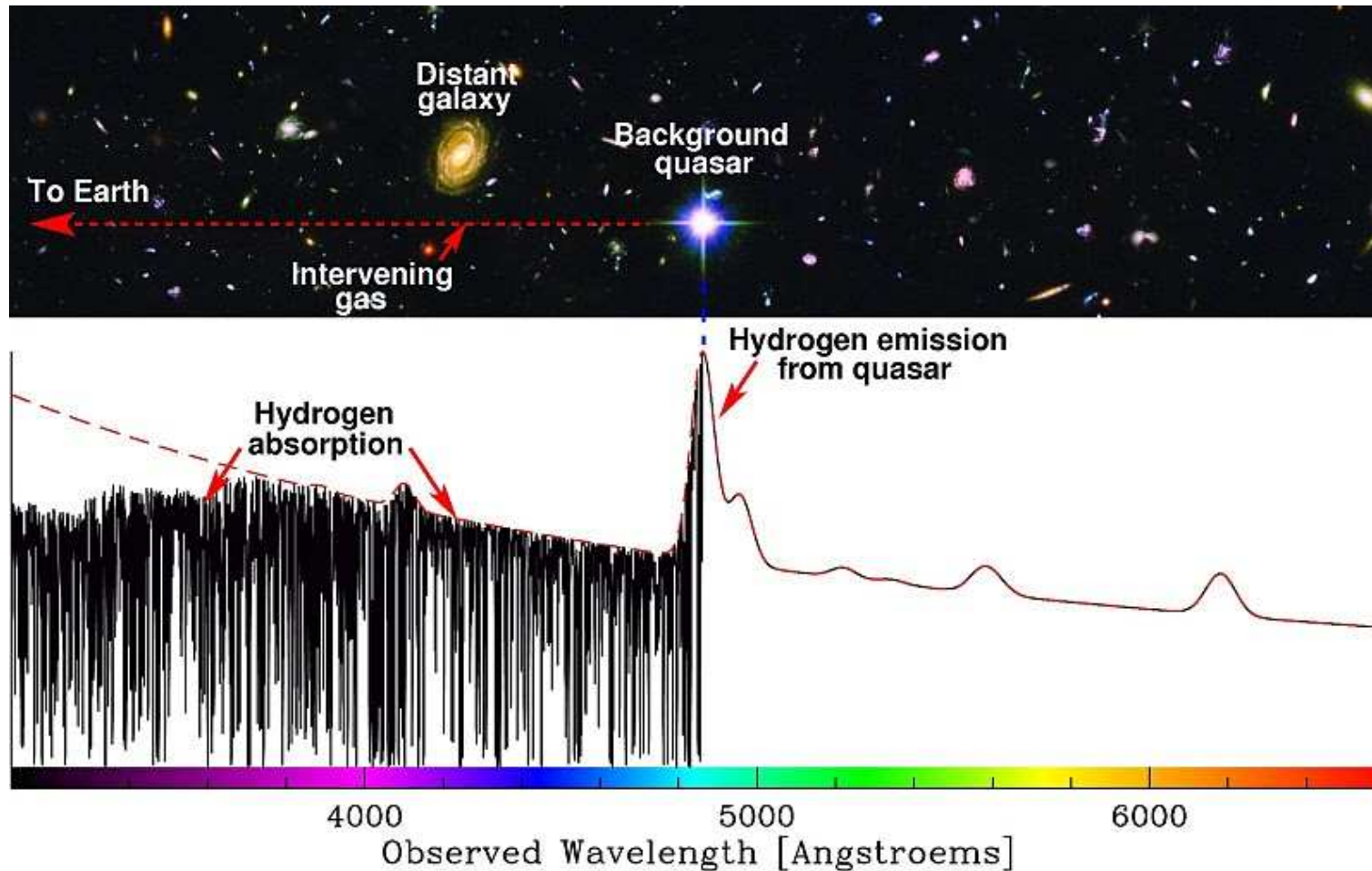
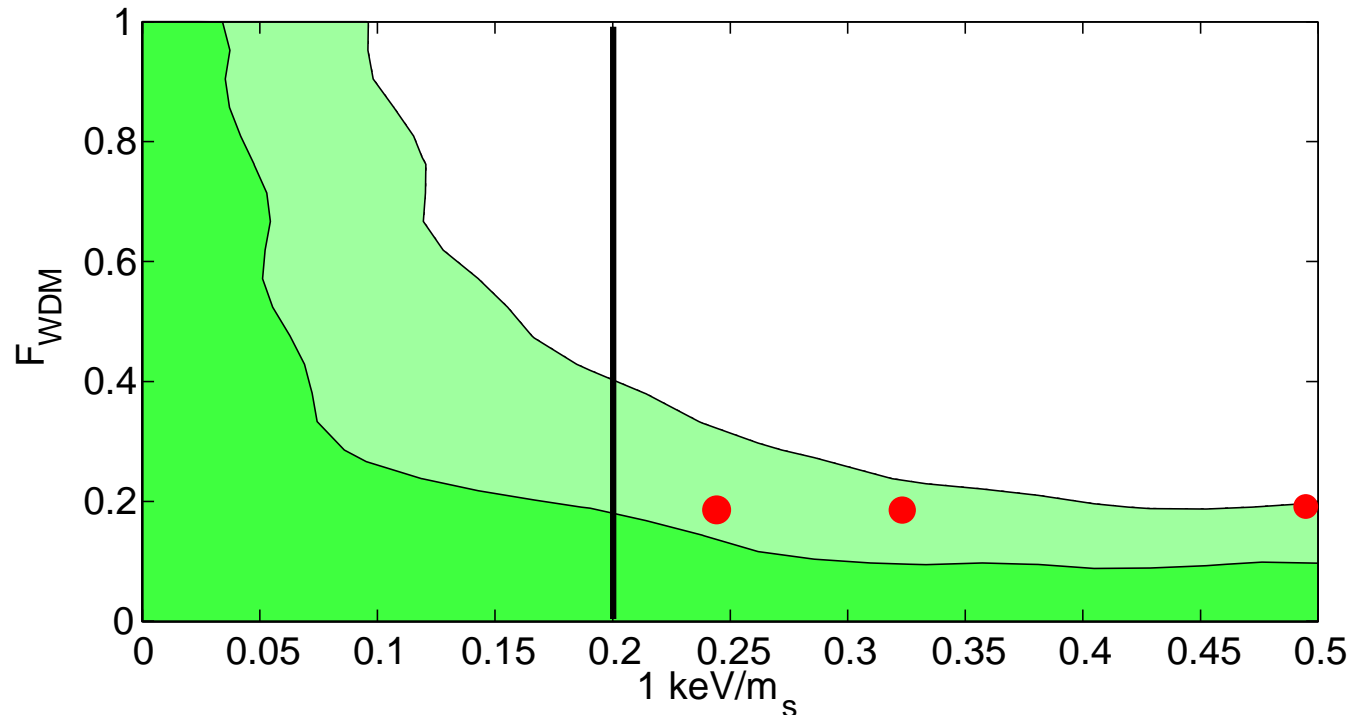


Image: Michael Murphy, Swinburne University of Technology, Melbourne, Australia

Neutral hydrogen in intergalactic medium is a tracer of overall matter density. Scales  $0.3h/\text{Mpc} \lesssim k \lesssim 3h/\text{Mpc}$

# Lyman- $\alpha$ bounds on CDM+WDM mixture

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JCAP'09;  
PRL'09

$$F_{\text{WDM}} = \frac{\Omega_{\text{WDM}}}{\Omega_{\text{WDM}} + \Omega_{\text{CDM}}}$$

Lyman- $\alpha$  allows to restrict the shape of primordial velocity spectrum, rather than free-streaming (for example, a fraction of warm DM ( $F_{\text{WDM}}$ ) for given mass)

# Lifetime of sterile neutrino DM candidate

- Dominant decay channel for sterile neutrino (for  $M_s < 1$  MeV) is  $N \rightarrow 3\nu$ .

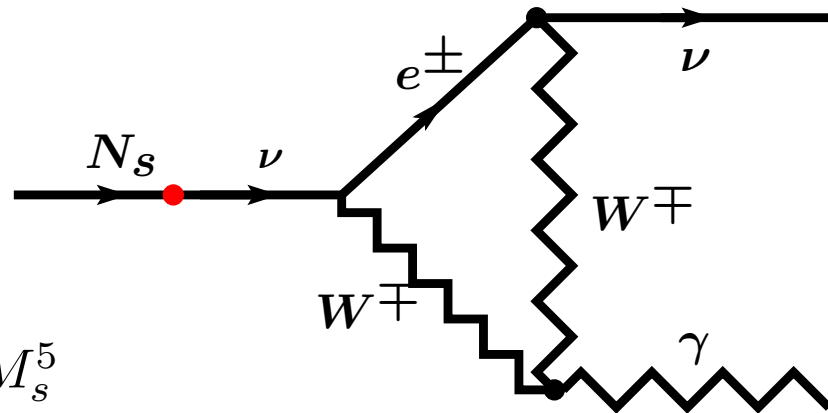
Wolfenstein  
Pal (1982)

- Life-time  $\tau = 5 \times 10^{26} \text{sec} \times \left(\frac{\text{keV}}{M_s}\right)^5 \left(\frac{10^{-8}}{\theta^2}\right)^2$

Barger Phillips  
Sarkar (1995)

- Subdominant **radiative decay channel**

– Photon energy:  $E_\gamma = \frac{M_s}{2}$



Dolgov  
Hansen (2000)

– Radiative decay width:

$$\Gamma_{\text{rad}} = \frac{9 \alpha_{\text{EM}} G_F^2}{256 \cdot 4\pi^4} \sin^2(2\theta) M_s^5$$

Abazajian  
Fuller Tucker  
(2001)

- Sterile neutrino DM **is not completely dark**. Its decay signal can be searched for in the spectra of astrophysical objects.

Boyarsky, O.R.  
et al.  
(2006-2009)

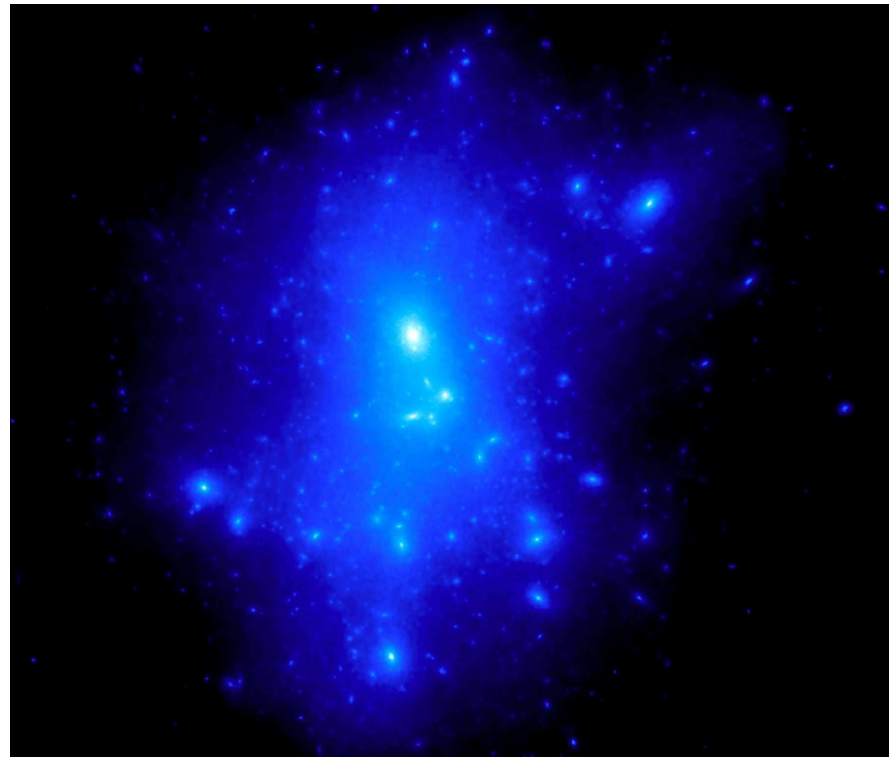


# Search for dark matter particles

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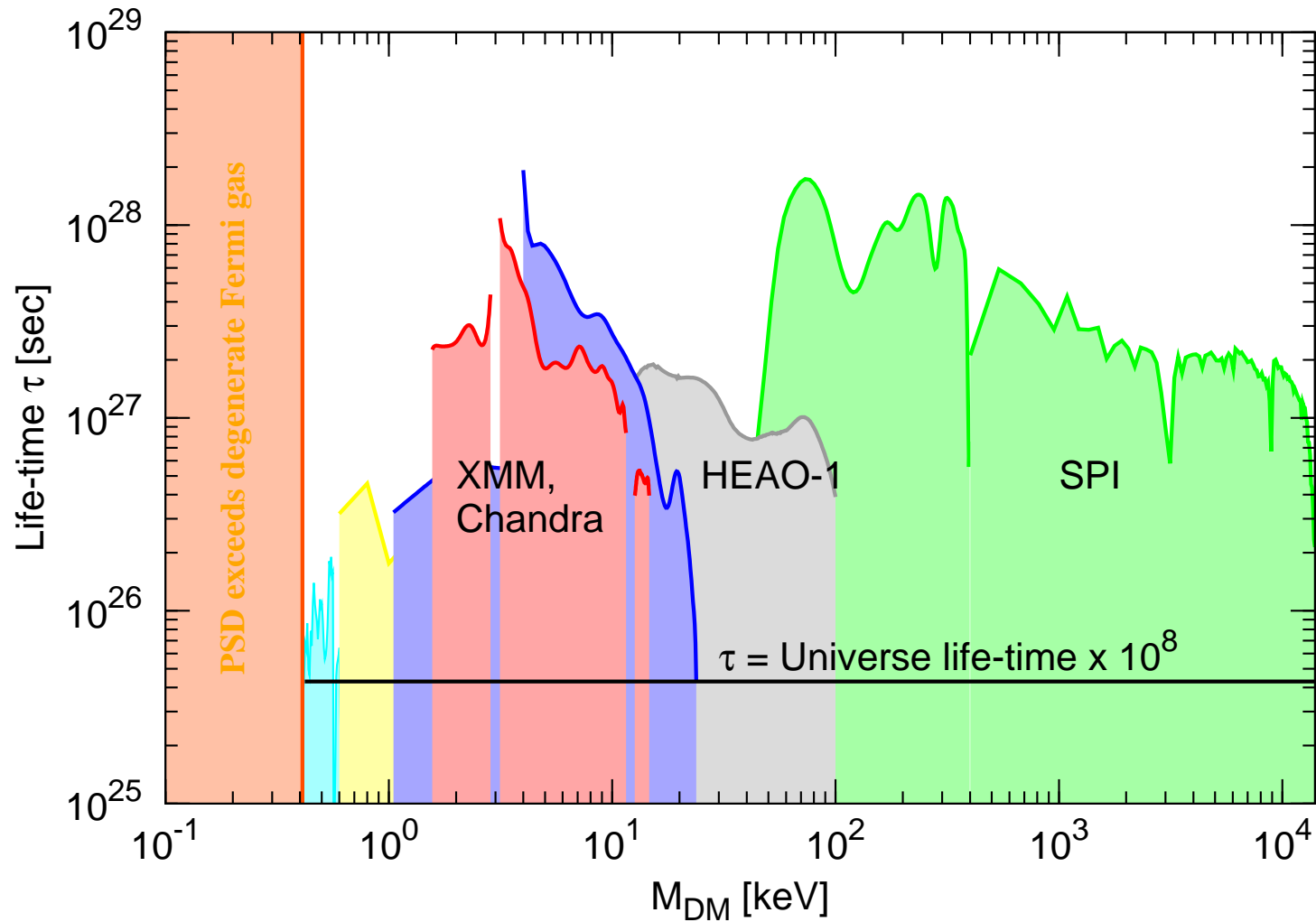
- DM may be decaying with a cosmologically long life-time (age of the Universe or even longer). Can we detect such decay?
- **Yes!** if you multiply a small number (probability of decay) with a large number (typical amount of DM particles in a galaxy  $\sim 10^{70}-10^{100}$ )

$$\text{Signal} \propto \int_{\text{line of sight}} \rho_{\text{DM}}(r) dl$$



Expected signal from a galaxy at a particular energy

# Restrictions on life-time of decaying DM



Results of almost **20** published works.

**MW (HEAO-1)**  
 Boyarsky, O.R.  
 et al. 2005

**Coma and Virgo clusters**  
 Boyarsky, O.R.  
 et al.

**Bullet cluster**  
 Boyarsky, O.R.  
 et al. 2006

**LMC+MW(XMM)**  
 Boyarsky, O.R.  
 et al. 2006

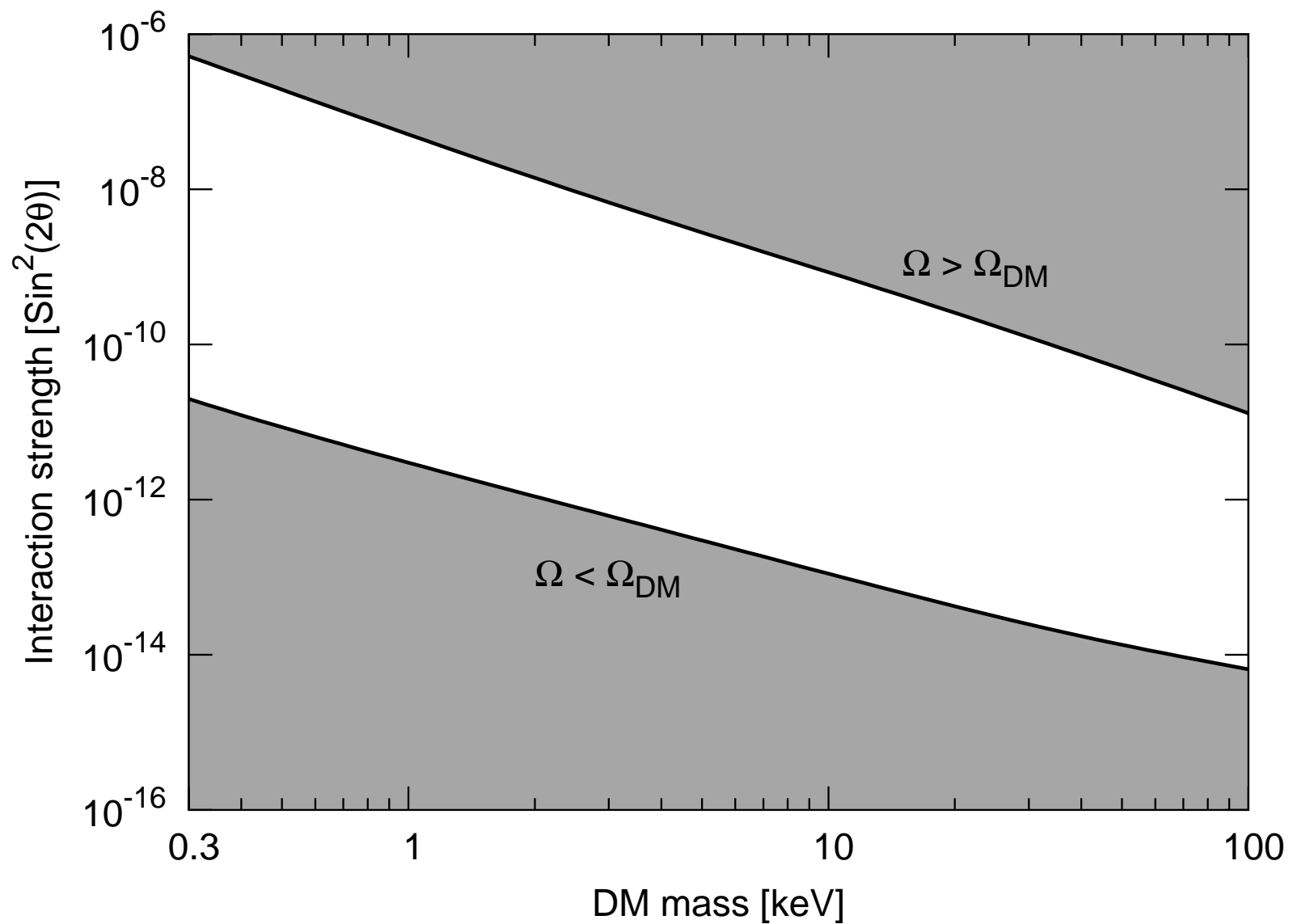
**MW** Riemer-Sørensen et al.; Abazajian et al.

**MW (XMM)**  
 Boyarsky, O.R.  
 et al. 2007

**M31** Watson et al. 2006; Boyarsky et al. 2007

# Window of parameters of sterile neutrino DM

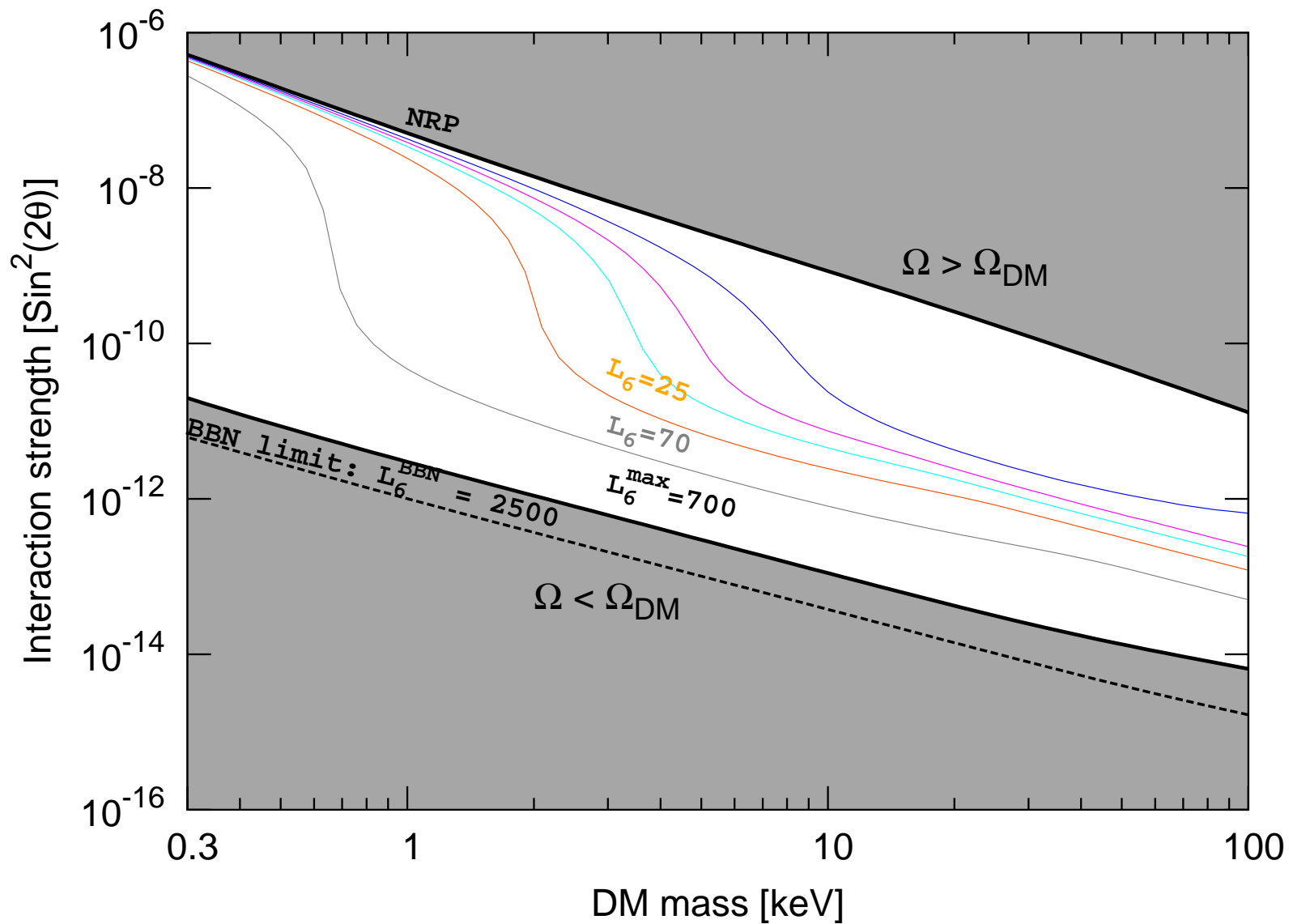
Laine,  
Shaposhnikov



# Window of parameters of sterile neutrino DM

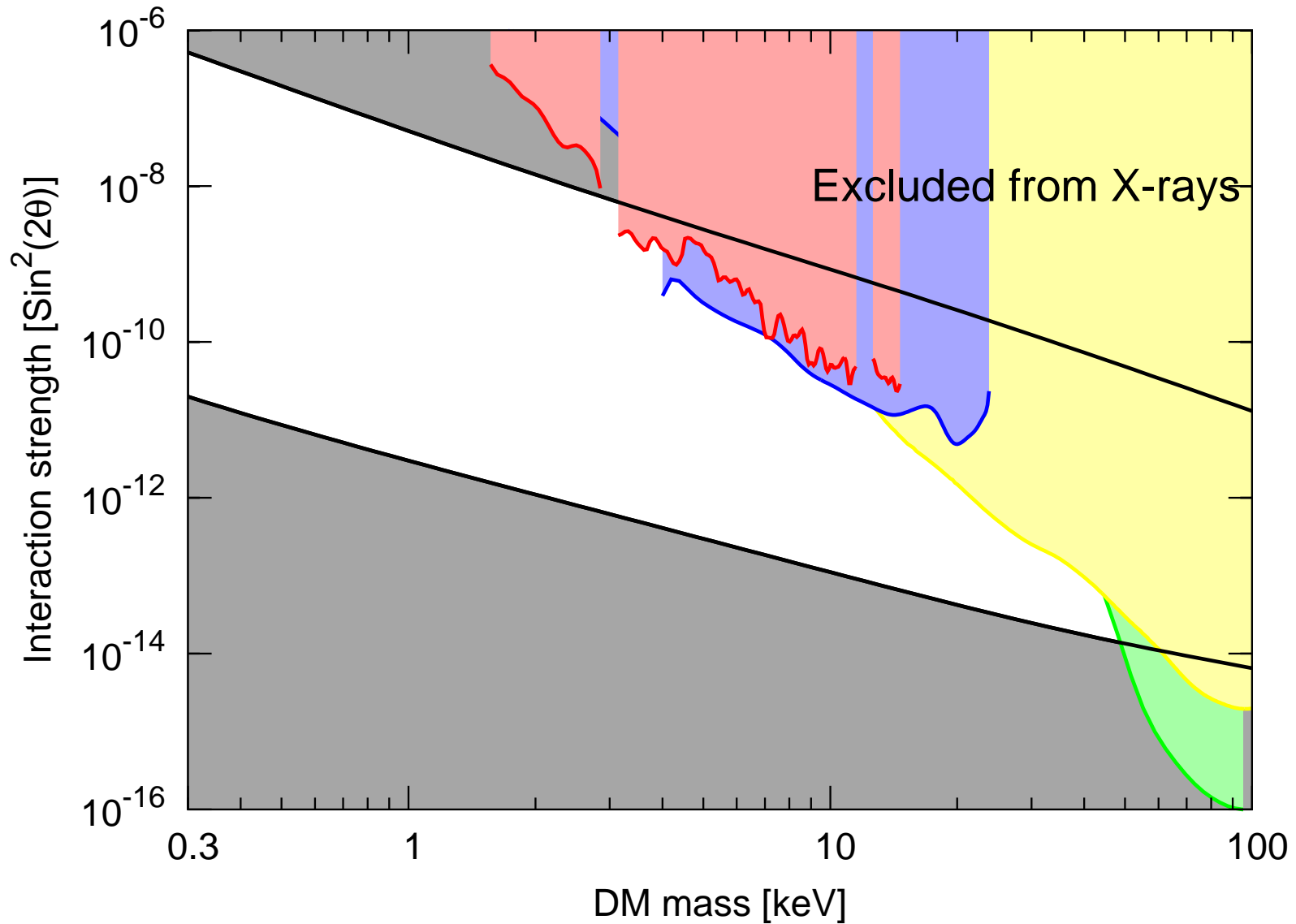
Asaka, Laine,  
Shaposhnikov

Laine,  
Shaposhnikov



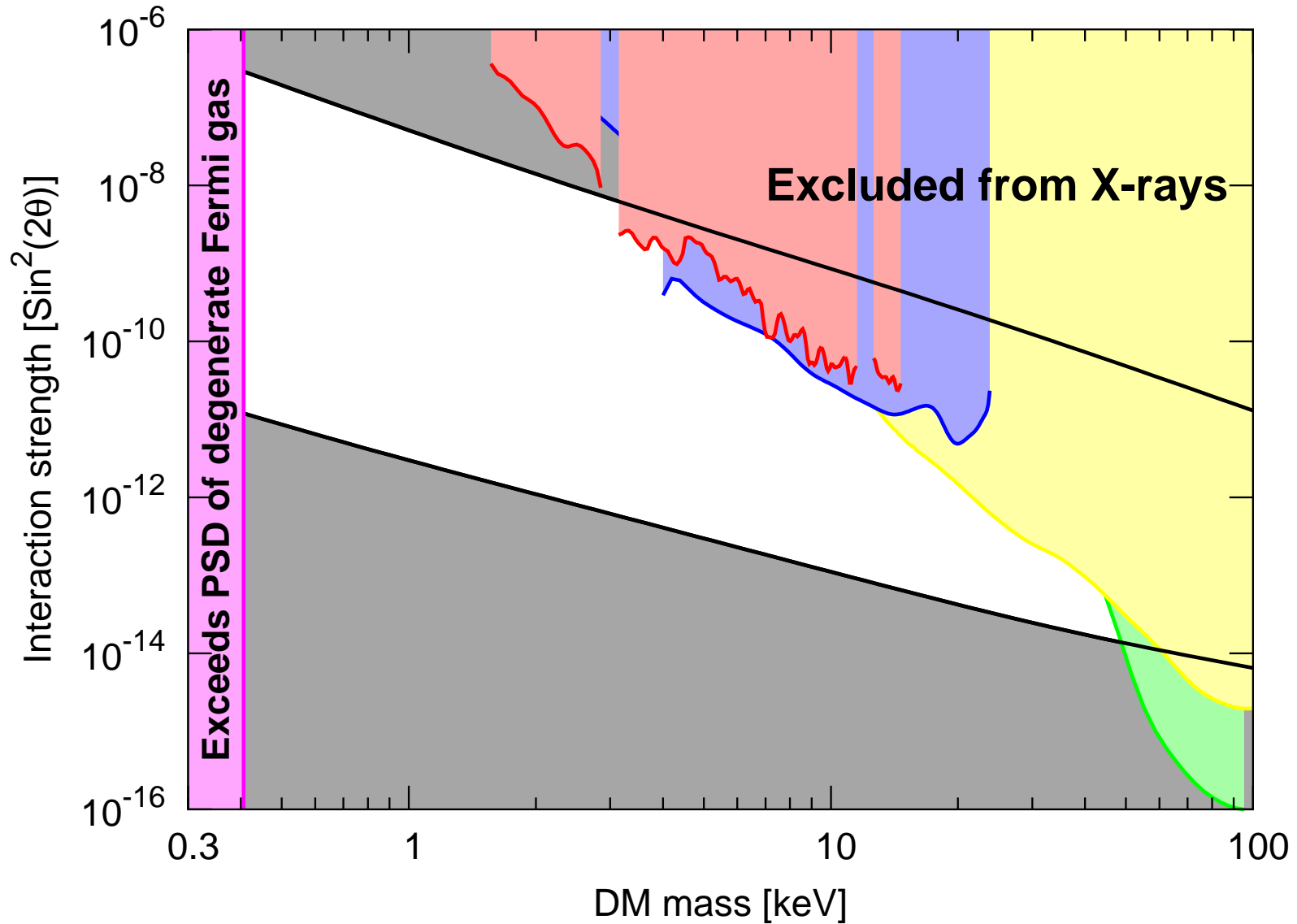
# Window of parameters of sterile neutrino DM

Boyarsky, O.R.  
et al.  
2005-2008



# Window of parameters of sterile neutrino DM

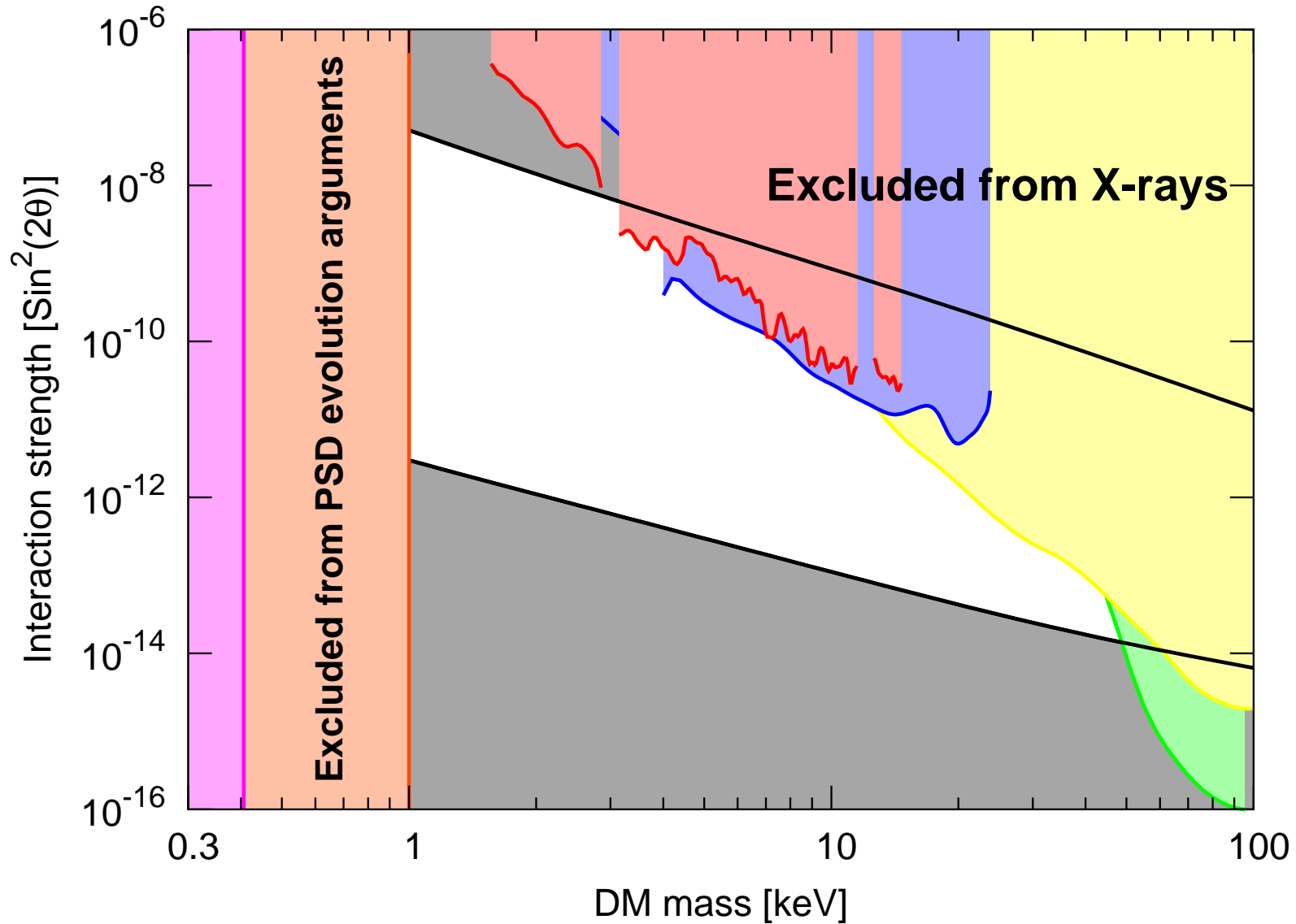
Boyarsky,  
Ruchayskiy et  
al. 2005-2008



# Window of parameters of sterile neutrino DM

Boyarsky,  
Ruchayskiy et  
al. 2005-2008

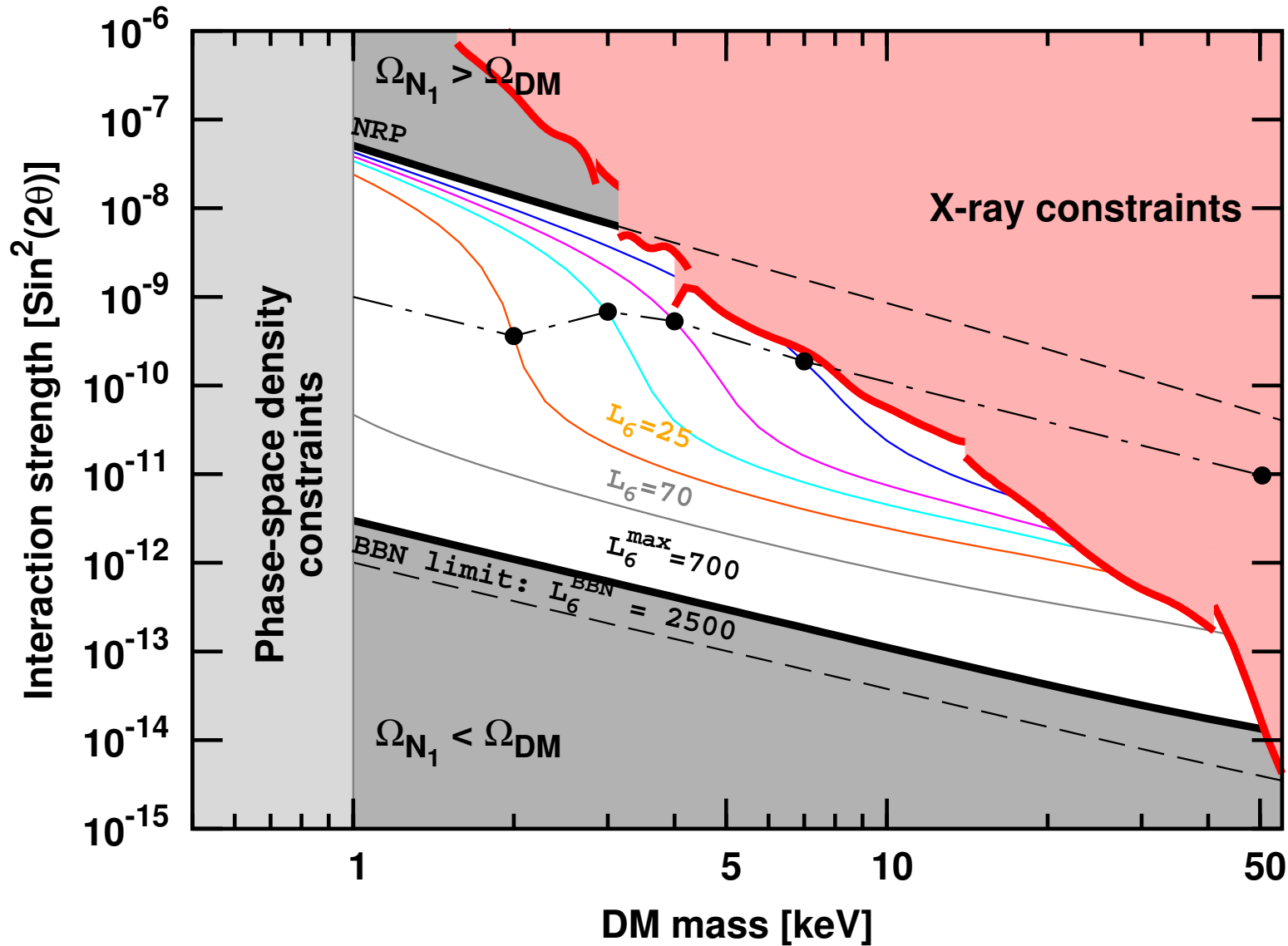
Boyarsky,  
O.R.,  
Iakubovskyi,  
2008



# Sterile neutrino DM in the $\nu$ MSM

Boyarsky,  
O.R.,  
Lesgourgues,  
Viel  
[0812.3256]

Boyarsky,  
O.R.,  
Shaposhnikov  
[0901.0011]

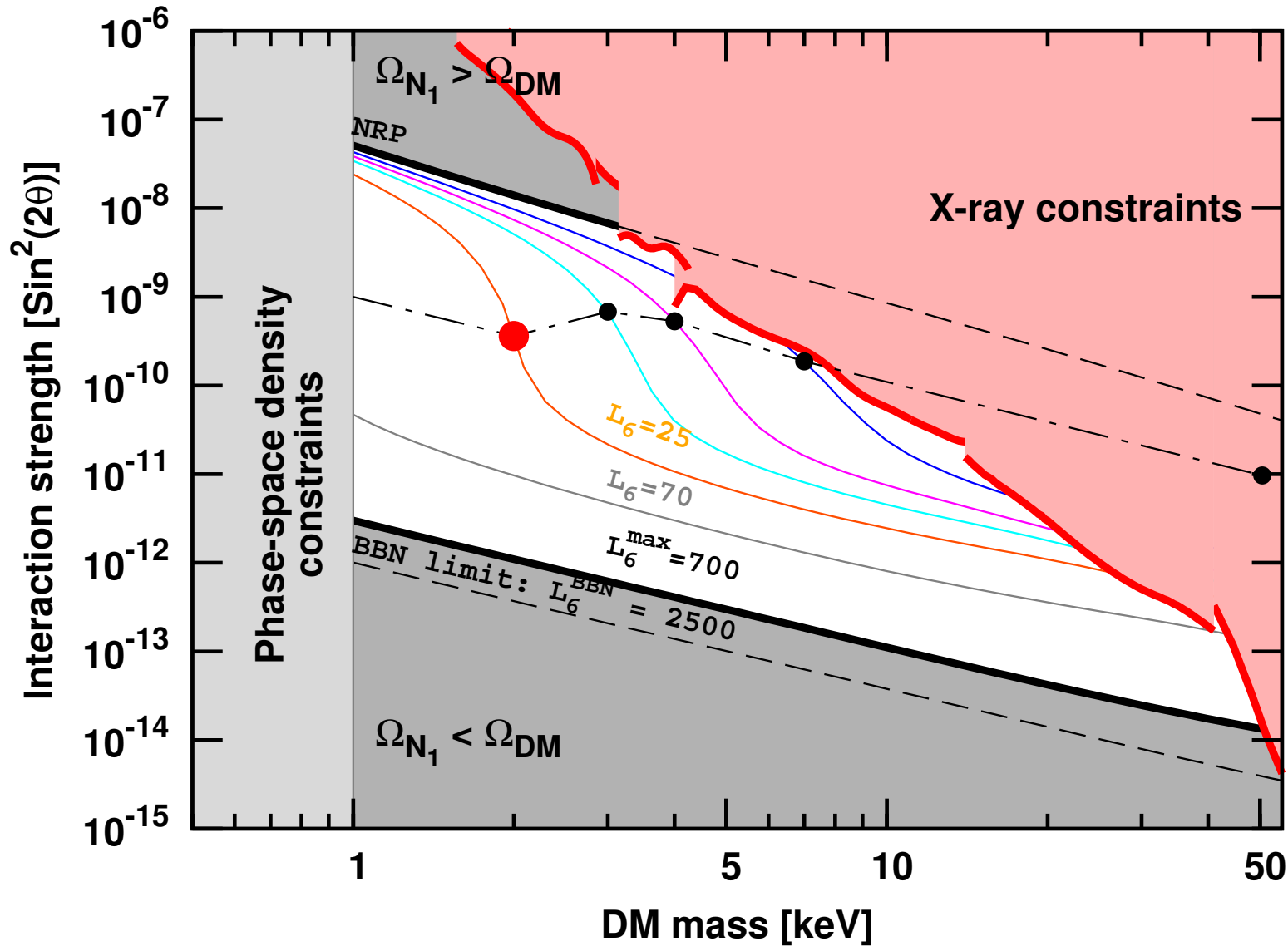




# Sterile neutrino DM in the $\nu$ MSM

Boyarsky,  
O.R.,  
Lesgourgues,  
Viel  
[0812.3256]

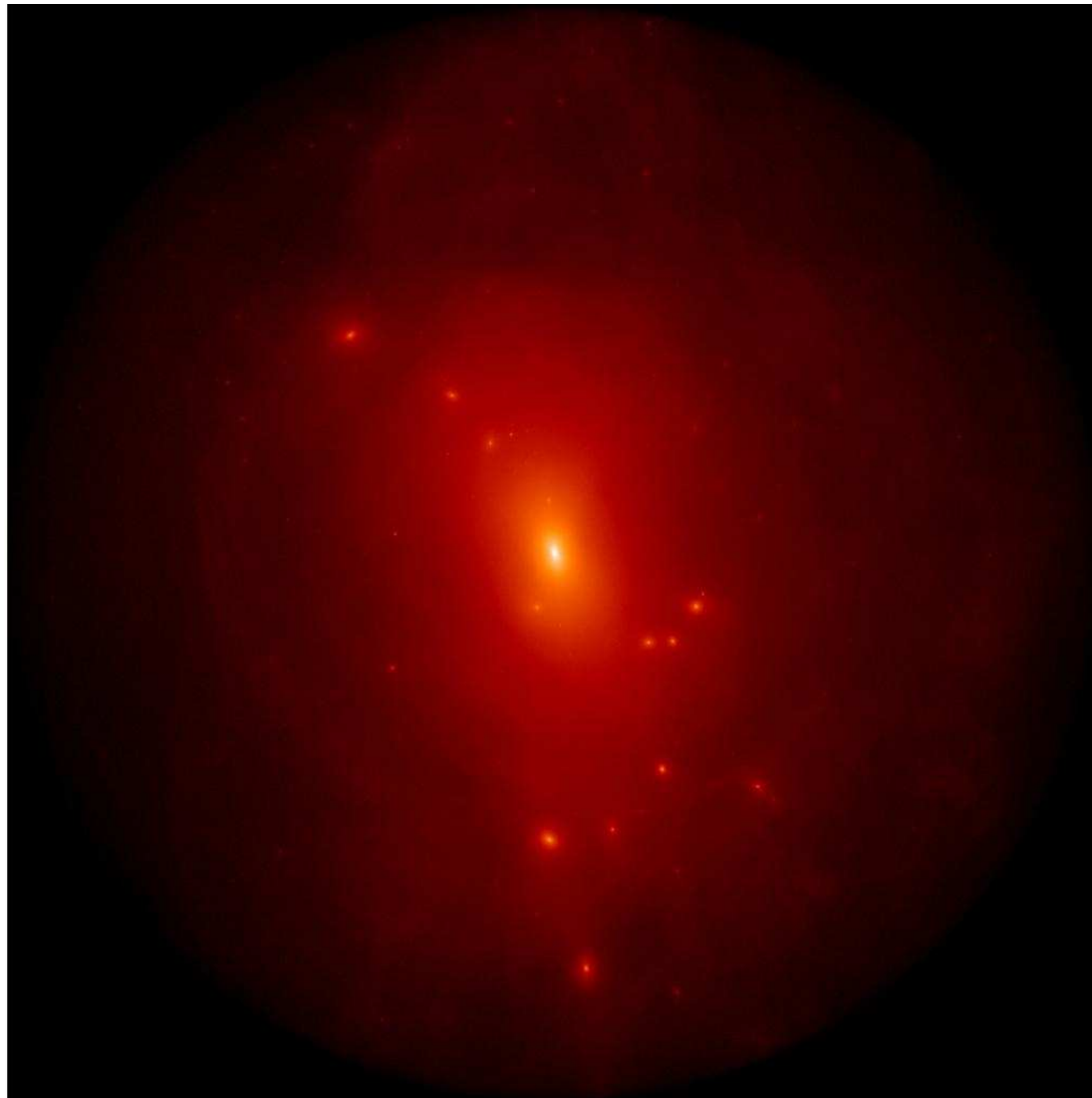
Boyarsky,  
O.R.,  
Shaposhnikov  
[0901.0011]



# Halo substructure with sterile neutrino DM

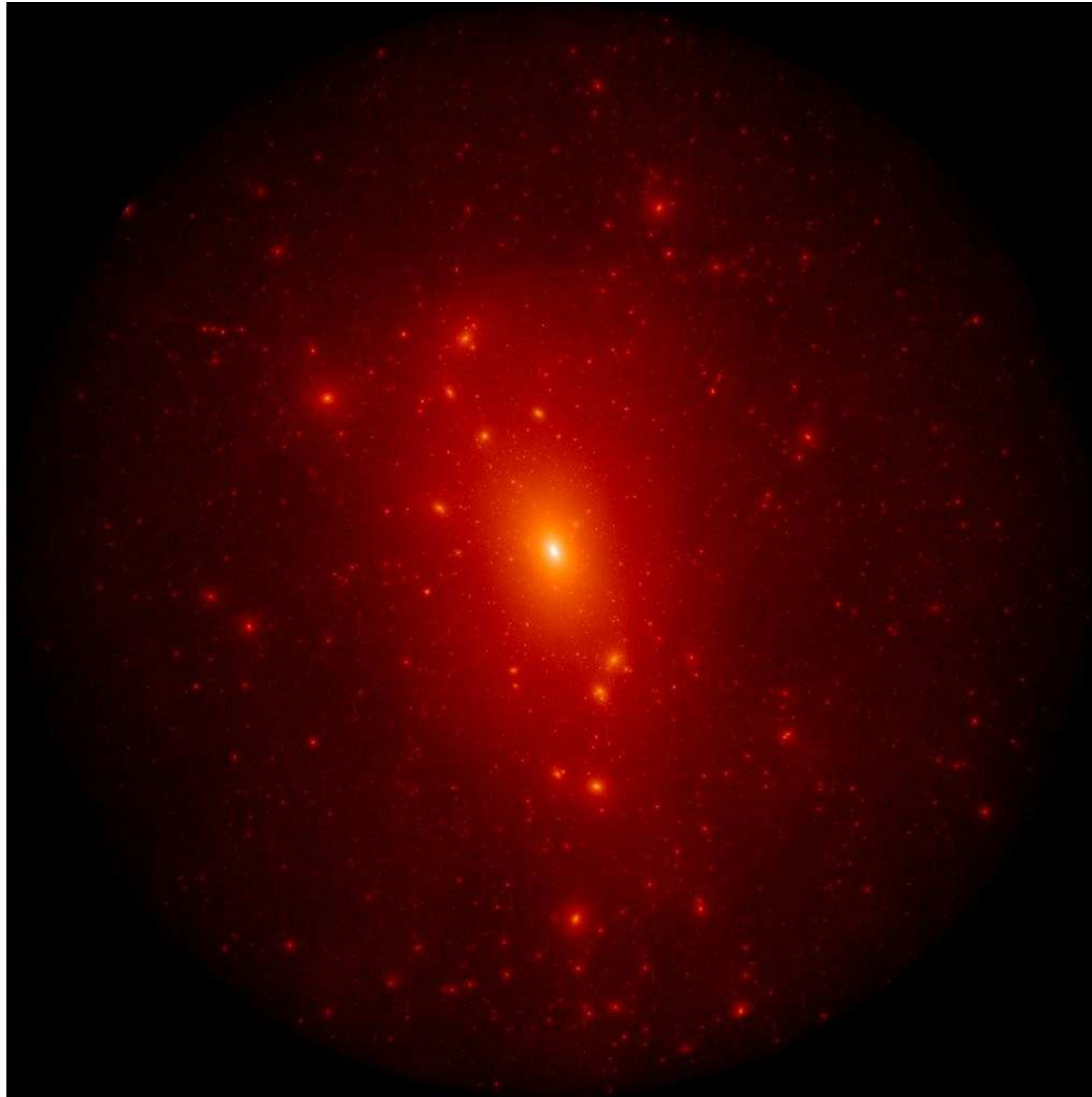
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work in  
progress



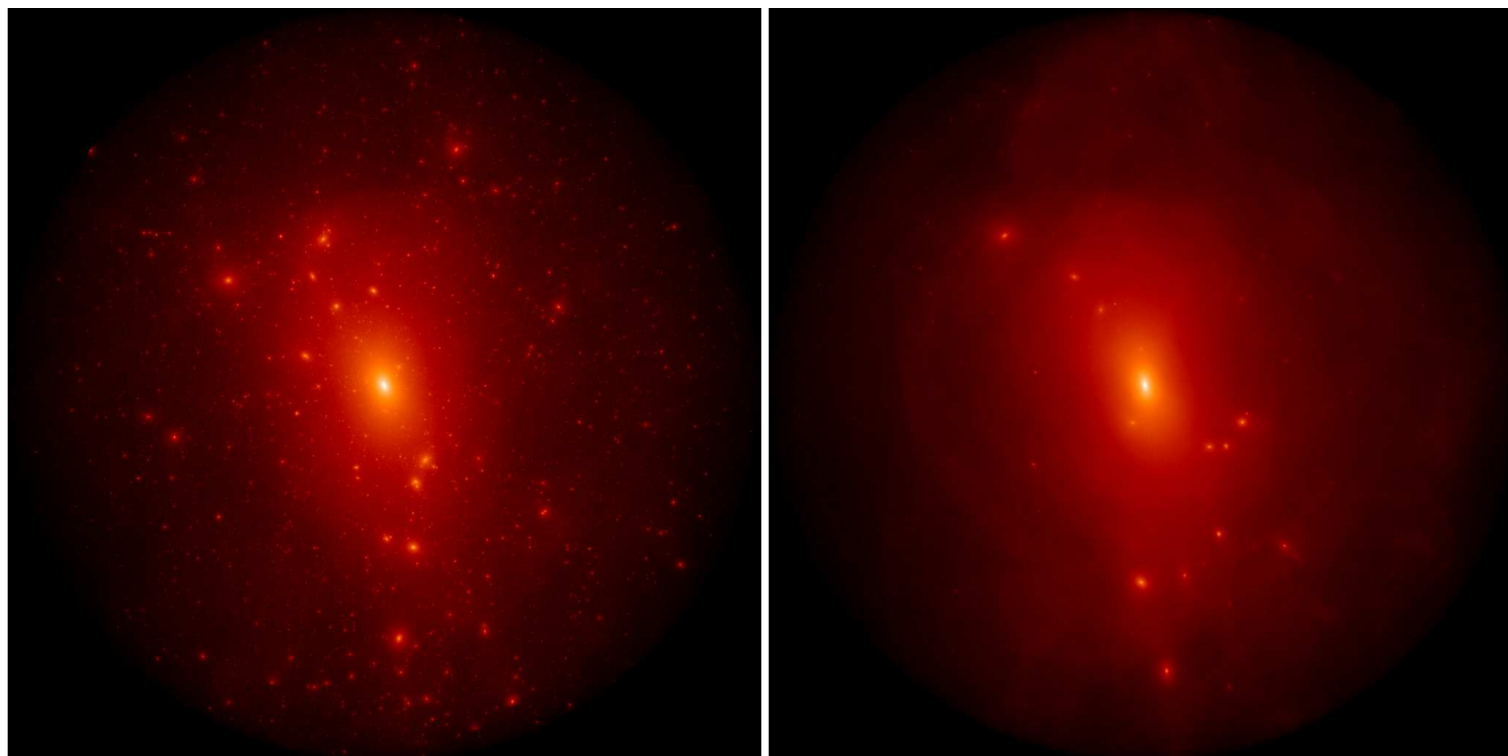
## Halo substructure with CDM

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# Halo substructure with sterile neutrino DM

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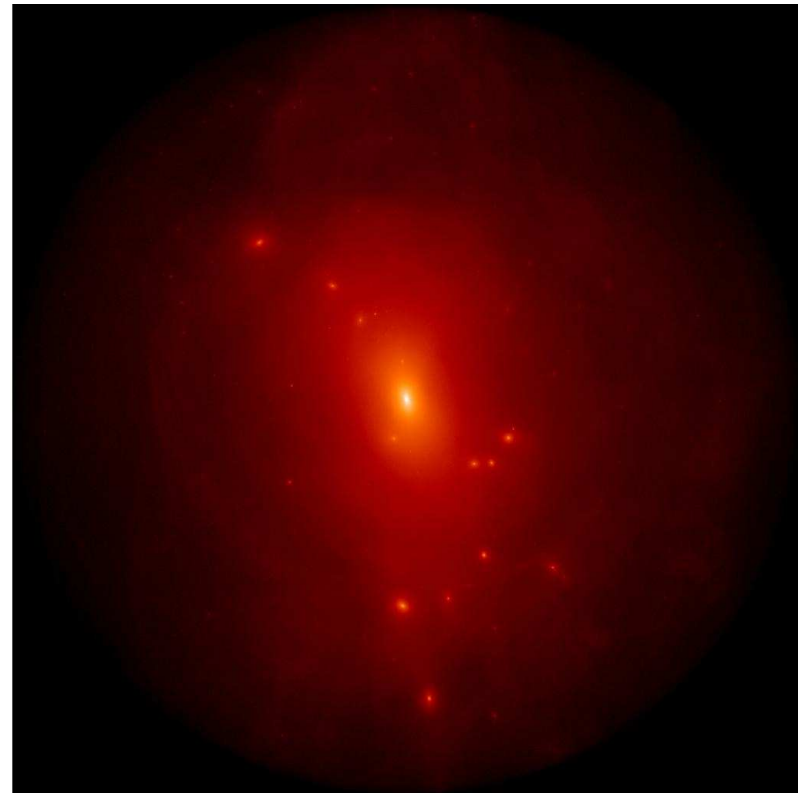
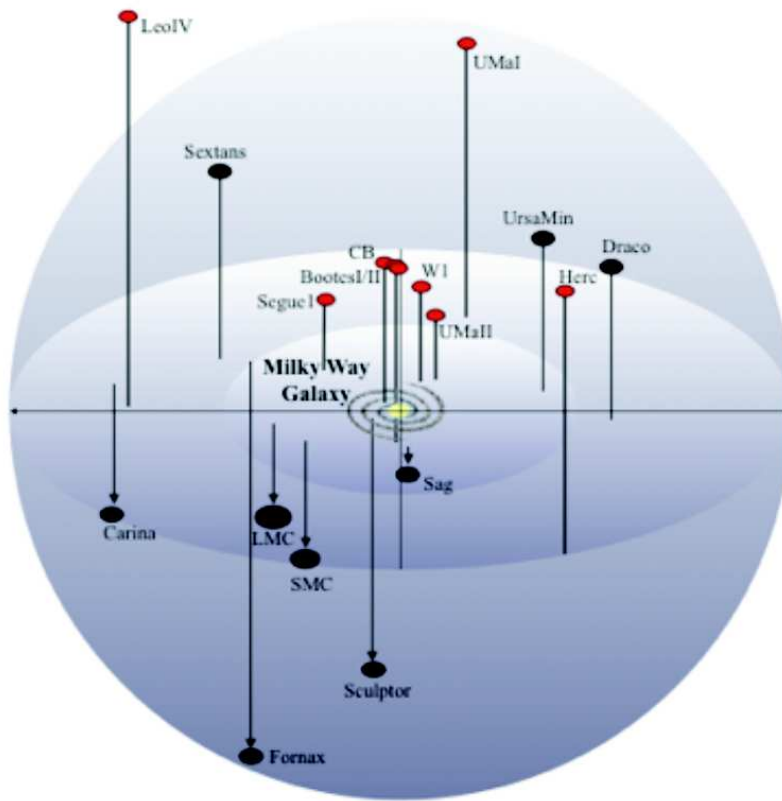


*Aq-A-2 CDM halo*

**PRELIMINARY:** *Aq-A-2 halo* made of sterile neutrino DM (Gao, Theuns, Frenk, O.R., ...)

- Simulated sterile neutrino DM halo (right) is fully compatible with the Lyman- $\alpha$  forest data but provides a structure of Milky way-size halo different from CDM

# Halo substructure with sterile neutrino DM



Observed substructures within our Galaxy. M. Geha  
2010

**PRELIMINARY:** *Aq-A-2 halo* made of sterile  
neutrino DM (Gao, Theuns, Frenk, O.R., ...)

- Simulated sterile neutrino DM halo (right) is fully compatible with the Lyman- $\alpha$  forest data but provides a structure of Milky way-size halo different from CDM

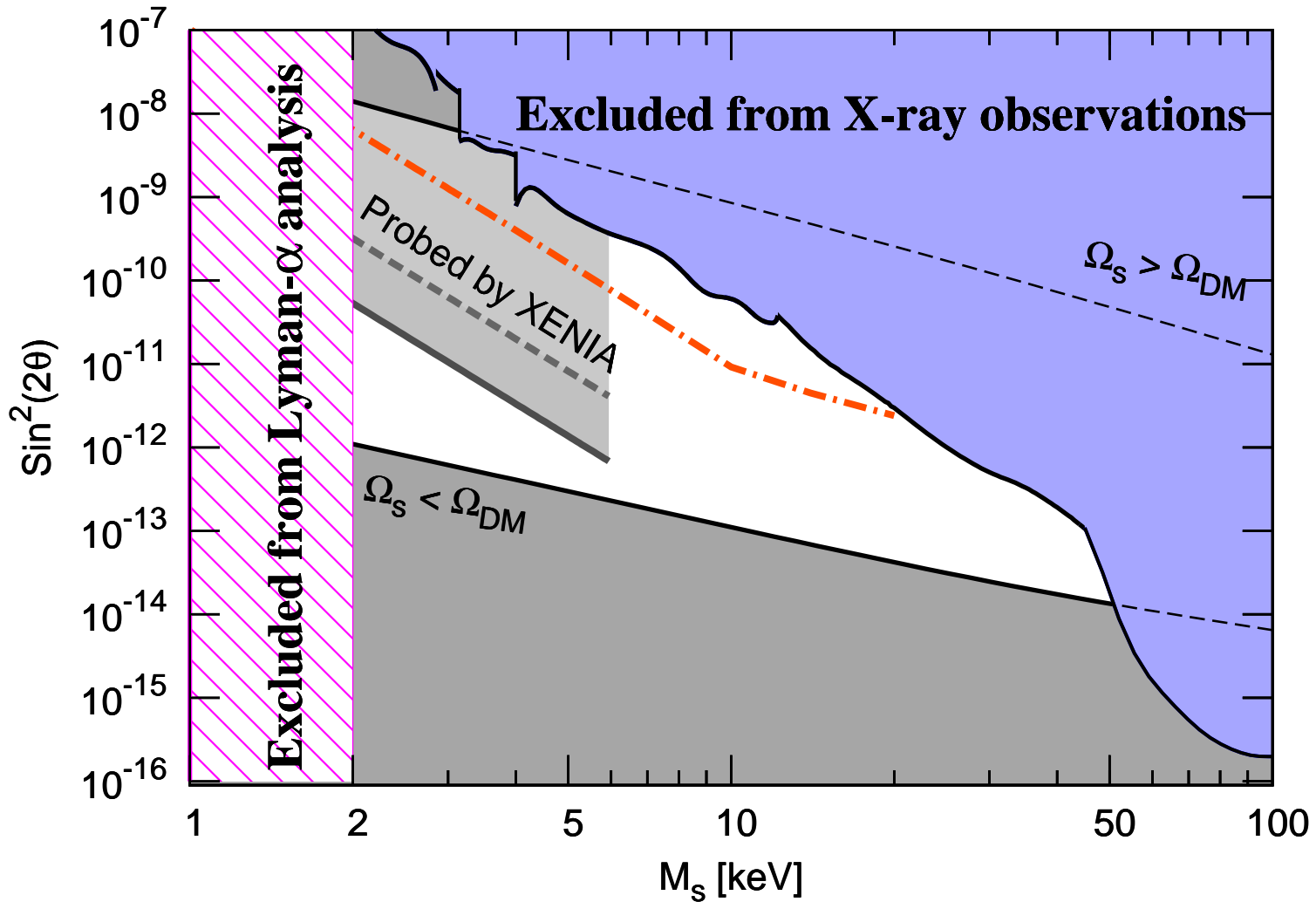
# Astrophysical searches for decaying DM

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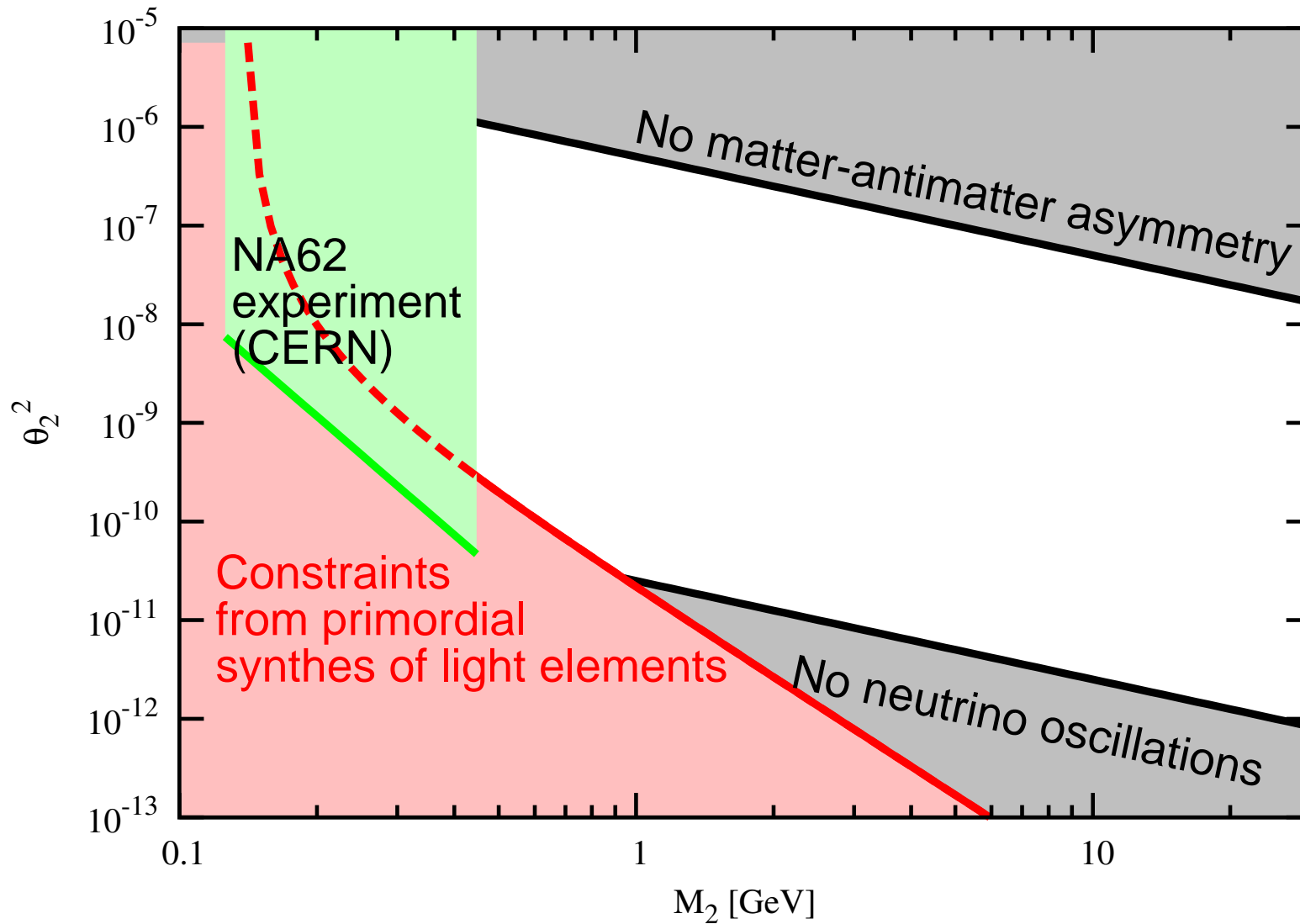
- Sterile neutrino DM candidates are hard to search in labs
- The decaying dark matter is a unique all-sky signal, with variations, correlated with the distribution of galaxies/galaxy clusters
- If any candidate decay line is found, the distribution of its intensity over the sky can be predicted and checked against observations.
- This makes the search for decaying dark matter a **direct detection experiment**
- New instruments (EDGE/XENIA) – White paper for ESA's call for Fundamental physics roadmap

Bezrukov,  
Shaposhnikov

# Improved bounds on DM decay



# Probing other sterile neutrinos





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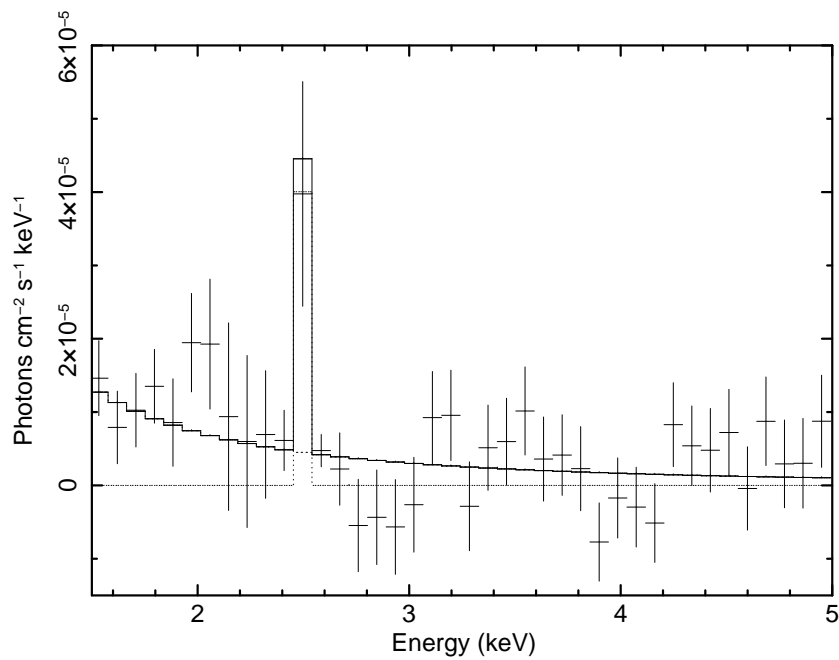
**Main conclusion:** sterile neutrino is a viable dark matter candidate.

Astrophysics and cosmology are the main tools to find/rule out sterile neutrino DM.

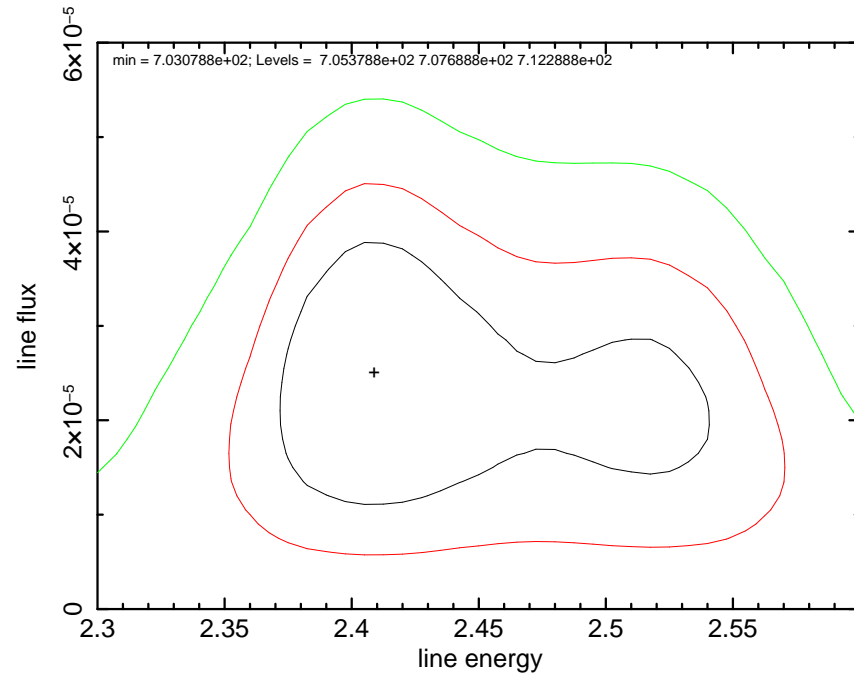
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**THANK YOU FOR YOUR  
ATTENTION**

# Example: Spectral feature in Willman 1



[Loewenstein & Kusenko [0912.0552]]



68%, 90% and 99% confidence intervals

## Checking for DM line in dSphs

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- $E_{\text{line}} = (2.51 \pm 0.07) \text{ keV}$   
2.44 keV – 2.58 keV ( $1\sigma$ )  
2.30 keV – 2.72 keV ( $3\sigma$ )
- **Line flux**  $F_{\text{Wil1}} = (3.53 \pm 1.95) \times 10^{-7} \text{ photons/cm}^2/\text{sec}$  (68% CL)
- No significant lines were found in spectra of dSphs
- We obtain the following exclusions

	2.44 – 2.58 keV	2.30 – 2.72 keV
<b>Fornax dSph:</b>	$5.1\sigma$	$3.3\sigma$
<b>Sculptor dSph:</b>	$3.0\sigma$	$2.5\sigma$
<b>Fornax + Sculptor</b>	$5.9\sigma$	$4.1\sigma$

- In case of the DM decay origin of the line we were expecting about  $4\sigma$  detection from Fornax. However adding the line makes fit worse.

## Checking for DM line in M31

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Exclusion from	2.44 – 2.58 keV	2.30 – 2.72 keV
Fornax + Sculptor dSph:	5.9 $\sigma$	4.1 $\sigma$

### Andromeda galaxy

- Diffuse spectrum above 2 keV is a featureless power law

MNRAS'08  
[0709.2301]

	2.44 – 2.58 keV	2.30 – 2.72 keV
M31, 1kpc < $R$ < 3kpc:	22.7 $\sigma$	20.1 $\sigma$
M31, 5 kpc off-center: circle radius 3 kpc	10.4 $\sigma$	10.4 $\sigma$
M31, both regions	24.9 $\sigma$	23.3 $\sigma$

1001.0644

- Extremely significant exclusion from central 8 kpc of Andromeda!
- All bounds are based on the conservative DM estimate from [Widrow & Dubinski'05]!

# Checking for DM line in M31

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- Exclusion from Fornax and Sculptor dSphs:

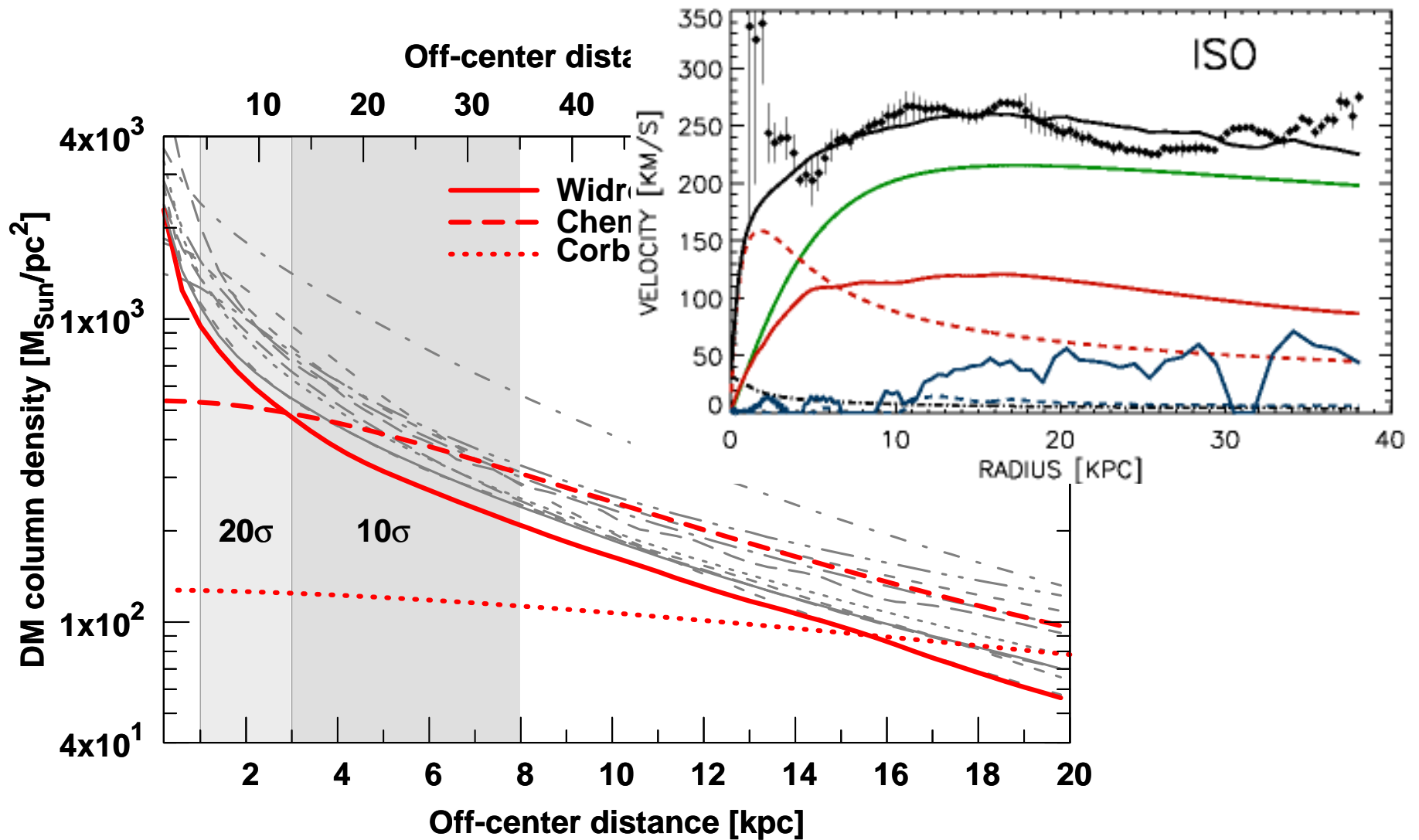
2.44 – 2.58 keV	2.30 – 2.72 keV
$5.9\sigma$	$4.1\sigma$

- Exclusion from **central 8 kpc of Andromeda**:

2.44 – 2.58 keV	2.30 – 2.72 keV	DM model
$24.9\sigma$	$23.3\sigma$	[Widrow & Dubinski'05]
$7.9\sigma$	$6.9\sigma$	[Corbelli et al.'09]

1001.0644

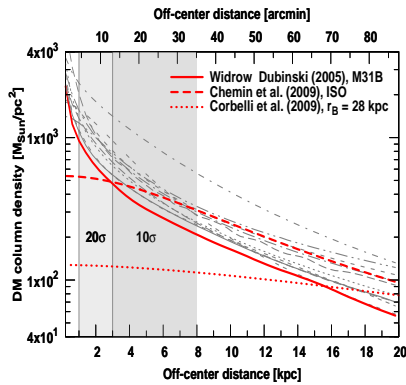
# Checking for DM line in M31



In the final version of the paper we processed observations in the region 10 – 20 kpc

1001.0644v2

# Summary of exclusions



“Consensus model”  
(Widrow & Dubinski, M31B)

Minimal DM amount  
(Corbelli et al., Burkert  
profile,  $r_B = 28$  kpc,  
 $M/L = 8$ )

68% CL:  
2.44 keV –  
2.58 keV

99%CL:  
2.30 keV –  
2.72 keV

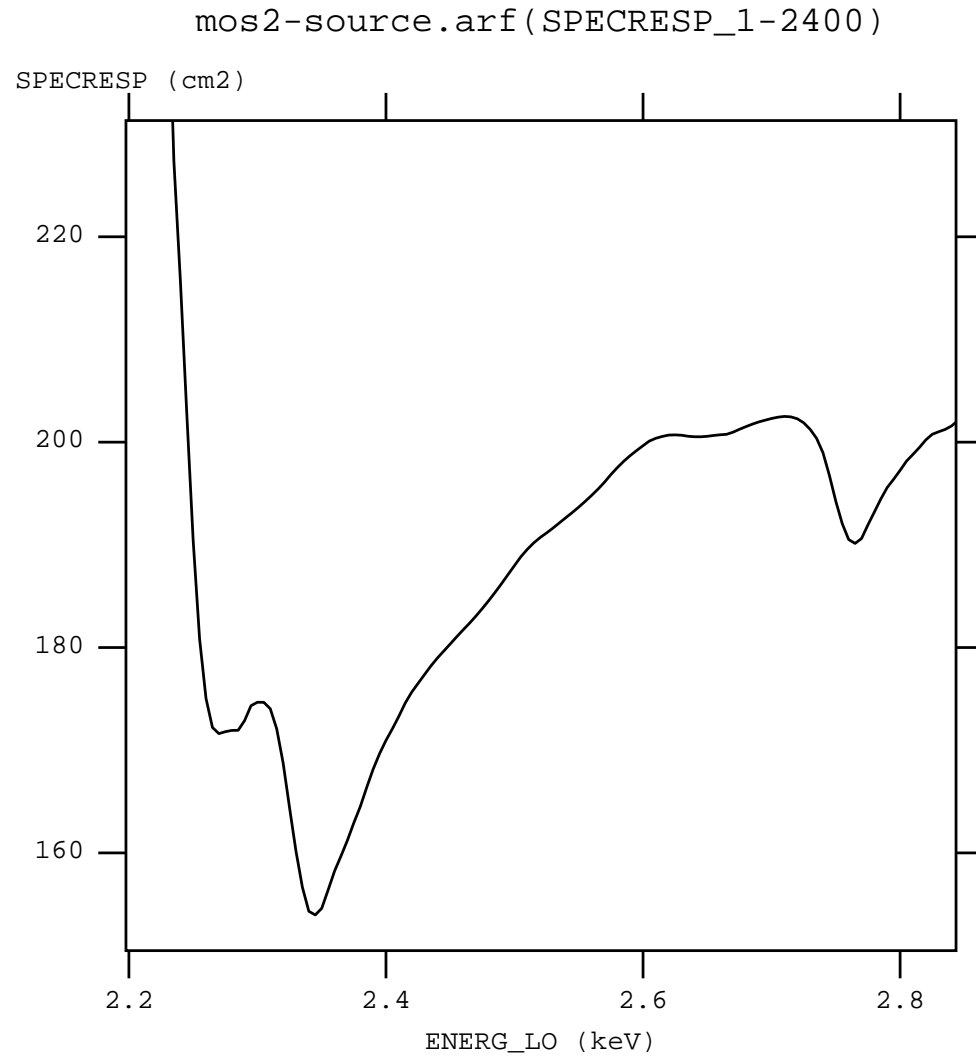
	68%CL	99%CL	68%CL	99%CL
M31 within 8 central kpc	$24.9\sigma$	$23.3\sigma$	$7.9\sigma$	$6.9\sigma$
M31 10–20 kpc off-center	$12.0\sigma$	$10.7\sigma$	$11.7\sigma$	$10.6\sigma$
All M31 obs.	$28.2\sigma$	$26.2\sigma$	$13.6\sigma$	$13.2\sigma$
All M31 + Fornax	$29.0\sigma$	$26.7\sigma$	$15.2\sigma$	$14.0\sigma$

- The DM origin of the spectral feature in Willman 1 at  $\sim 2.5$  keV is **excluded with  $14\sigma$  significance!**



# Effective area around absorption edge

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## Parameters of Aquarius simulation

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Name	$m_p$ [ $M_\odot$ ]	$\epsilon$ [pc]	$N_{\text{hr}}$	$N_{\text{lr}}$	$N_{50}$
Aq-A-1	$1.712 \times 10^3$	20.5	4,252,607,000	144,979,154	1,473,568,512
Aq-A-2	$1.370 \times 10^4$	65.8	531,570,000	75,296,170	184,243,536
Aq-A-3	$4.911 \times 10^4$	120.5	148,285,000	20,035,279	51,391,468

---

Basic parameters of the Aquarius simulations.  $m_p$  is the particle mass,  $\epsilon$  is the gravitational softening length,  $N_{\text{hr}}$  is the number of high resolution particles, and  $N_{\text{lr}}$  the number of low resolution particles filling the rest of the volume.  $M_{200} = 1.839 \times 10^{12} M_\odot$  is the virial mass of the halo, defined as the mass enclosed in a sphere with mean density 200 times the critical value.  $r_{200} = 245$  kpc gives the corresponding virial radius.  $M_{50} = 2.524 \times 10^{12} M_\odot$ . Finally,  $N_{50}$  gives the number of simulation particles within  $r_{50} = 433$  kpc.

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[Back to CDM+WDM halo simulation](#)

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