

Effects of Residue Background Events in Direct Detection Experiments on Determining Properties of Halo Dark Matter

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based on [arXiv:1003.5277](https://arxiv.org/abs/1003.5277) [hep-ph], JCAP 1006, 029



Model-independent data analyses

- Motivation

- Reconstruction of the WIMP velocity distribution

- Determination of the WIMP mass

Effects of residue background events

- Measured recoil spectrum

- On the determination of the WIMP mass

- On the reconstruction of the WIMP velocity distribution

Summary



Model-independent data analyses



Motivation

- Differential event rate for elastic WIMP-nucleus scattering

$$\frac{dR}{dQ} = \mathcal{A} F^2(Q) \int_{v_{\min}}^{v_{\max}} \left[\frac{f_1(v)}{v} \right] dv$$

Here

$$v_{\min} = \alpha \sqrt{Q}$$

is the minimal incoming velocity of incident WIMPs that can deposit the recoil energy Q in the detector.

$$\mathcal{A} \equiv \frac{\rho_0 \sigma_0}{2m_\chi m_{r,N}^2} \quad \alpha \equiv \sqrt{\frac{m_N}{2m_{r,N}^2}} \quad m_{r,N} = \frac{m_\chi m_N}{m_\chi + m_N}$$

ρ_0 : WIMP density near the Earth

σ_0 : total cross section ignoring the form factor suppression

$F(Q)$: elastic nuclear form factor

$f_1(v)$: one-dimensional velocity distribution of halo WIMPs



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Reconstruction of the WIMP velocity distribution

- **Ansatz:** reconstructing the **measured** recoil spectrum in the n th Q -bin

$$\left(\frac{dR}{dQ} \right)_{\text{expt, } Q \simeq Q_n} \equiv r_n e^{k_n(Q - Q_{s,n})} \quad r_n \equiv \frac{N_n}{b_n}$$

- Logarithmic slope and shifted point in the n th Q -bin

$$\overline{Q - Q_n}|_n \equiv \frac{1}{N_n} \sum_{i=1}^{N_n} (Q_{n,i} - Q_n) = \left(\frac{b_n}{2} \right) \coth \left(\frac{k_n b_n}{2} \right) - \frac{1}{k_n}$$

$$Q_{s,n} = Q_n + \frac{1}{k_n} \ln \left[\frac{\sinh(k_n b_n / 2)}{k_n b_n / 2} \right]$$

- Reconstructing the **one-dimensional WIMP velocity distribution**

$$f_1(v_{s,n}) = \mathcal{N} \left[\frac{2Q_{s,n} r_n}{F^2(Q_{s,n})} \right] \left[\frac{d}{dQ} \ln F^2(Q) \Big|_{Q=Q_{s,n}} - k_n \right]$$

$$\mathcal{N} = \frac{2}{\alpha} \left[\sum_a \frac{1}{\sqrt{Q_a} F^2(Q_a)} \right]^{-1} \quad v_{s,n} = \alpha \sqrt{Q_{s,n}}$$



Determination of the WIMP mass

- Estimating the moments of the WIMP velocity distribution

$$\langle v^n \rangle = \alpha^n \left[\frac{2Q_{\min}^{1/2} r_{\min}}{F^2(Q_{\min})} + I_0 \right]^{-1} \left[\frac{2Q_{\min}^{(n+1)/2} r_{\min}}{F^2(Q_{\min})} + (n+1)I_n \right]$$

$$I_n = \sum_a \frac{Q_a^{(n-1)/2}}{F^2(Q_a)}$$

$$r_{\min} = \left(\frac{dR}{dQ} \right)_{\text{expt}, Q=Q_{\min}} = r_1 e^{k_1(Q_{\min} - Q_{s,1})}$$

[M. Drees and CLS, JCAP 0706, 011]



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[M. Drees and CLS, JCAP 0706, 011]

- Determining the WIMP mass

$$m_X |_{\langle v^n \rangle} = \frac{\sqrt{m_X m_Y} - m_X \mathcal{R}_n}{\mathcal{R}_n - \sqrt{m_X / m_Y}}$$

$$\mathcal{R}_n = \left[\frac{2Q_{\min,X}^{(n+1)/2} r_{\min,X} / F_X^2(Q_{\min,X}) + (n+1)I_{n,X}}{2Q_{\min,X}^{1/2} r_{\min,X} / F_X^2(Q_{\min,X}) + I_{0,X}} \right]^{1/n} \left(X \longrightarrow Y \right)^{-1} \quad (n \neq 0)$$

[CLS and M. Drees, arXiv:0710.4296]

- With the assumption of a dominant SI WIMP-nucleus interaction

$$m_X |_{\sigma} = \frac{(m_X / m_Y)^{5/2} m_Y - m_X \mathcal{R}_{\sigma}}{\mathcal{R}_{\sigma} - (m_X / m_Y)^{5/2}}$$

$$\mathcal{R}_{\sigma} = \frac{\mathcal{E}_Y}{\mathcal{E}_X} \left[\frac{2Q_{\min,X}^{1/2} r_{\min,X} / F_X^2(Q_{\min,X}) + I_{0,X}}{2Q_{\min,Y}^{1/2} r_{\min,X} / F_Y^2(Q_{\min,Y}) + I_{0,Y}} \right]$$

[M. Drees and CLS, JCAP 0806, 012]



Effects of residue background events



Measured recoil spectrum

- Background spectrum

- ▶ Target-dependent exponential background spectrum

$$\left(\frac{dR}{dQ}\right)_{\text{bg,ex}} = \exp\left(-\frac{Q/\text{keV}}{A^{0.6}}\right)$$

- ▶ Constant background spectrum



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- Background window

- ▶ Entire experimental possible energy range (0 – 100 keV)
- ▶ Low energy range (0 – 50 keV)
- ▶ High energy range (50 – 100 keV)



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- ▶ Entire experimental possible energy range (0 – 100 keV)
- ▶ Low energy range (0 – 50 keV)
- ▶ High energy range (50 – 100 keV)

- (Naively) simulate

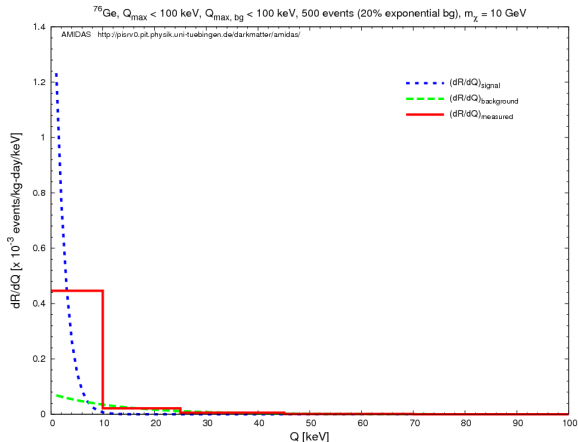
- ▶ only a few residue background events
- ▶ induced by two or more different sources



Measured recoil spectrum

- Measured recoil spectrum

(^{76}Ge , 0 – 100 keV, exponential bg 0 – 100 keV, 500 events, 20% bg, $m_\chi = 10$ GeV)



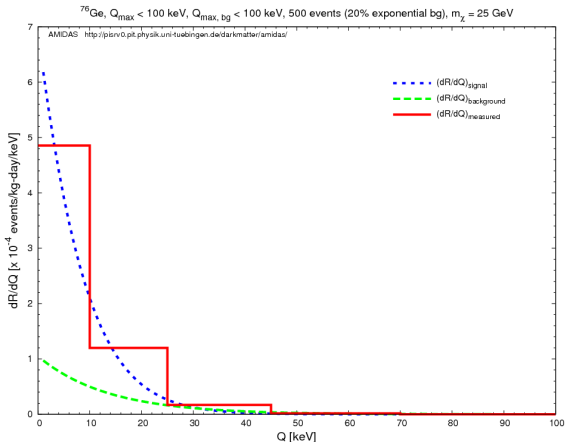
[Y. T. Chou and CLS, arXiv:1003.5277, accepted by JCAP]



Measured recoil spectrum

- Measured recoil spectrum

(^{76}Ge , 0 – 100 keV, exponential bg 0 – 100 keV, 500 events, 20% bg, $m_\chi = 25$ GeV)

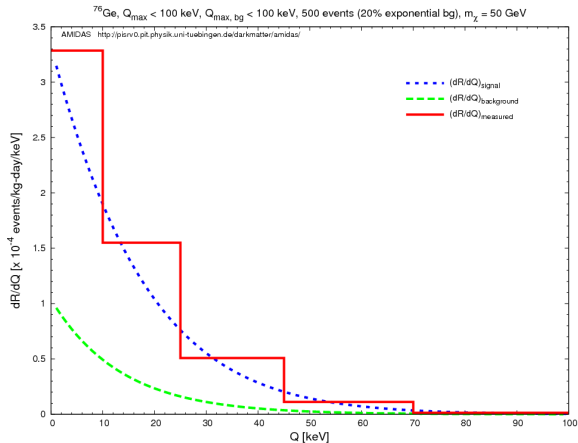


[Y. T. Chou and CLS, arXiv:1003.5277, accepted by JCAP]

Measured recoil spectrum

- Measured recoil spectrum

(^{76}Ge , 0 – 100 keV, exponential bg 0 – 100 keV, 500 events, 20% bg, $m_\chi = 50$ GeV)

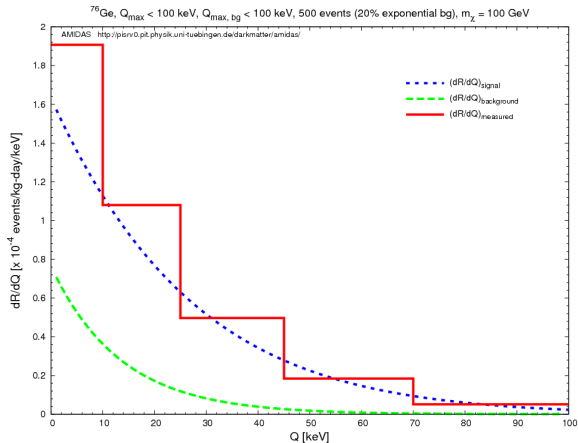


[Y. T. Chou and CLS, arXiv:1003.5277, accepted by JCAP]

Measured recoil spectrum

- Measured recoil spectrum

(^{76}Ge , 0 – 100 keV, exponential bg 0 – 100 keV, 500 events, 20% bg, $m_\chi = 100$ GeV)

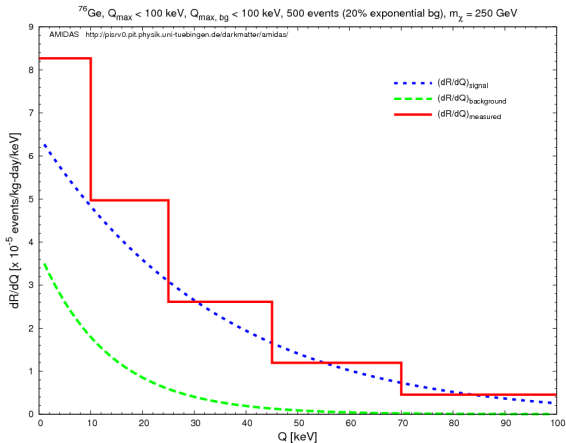


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Measured recoil spectrum

- Measured recoil spectrum

(^{76}Ge , 0 – 100 keV, exponential bg 0 – 100 keV, 500 events, 20% bg, $m_\chi = 250$ GeV)



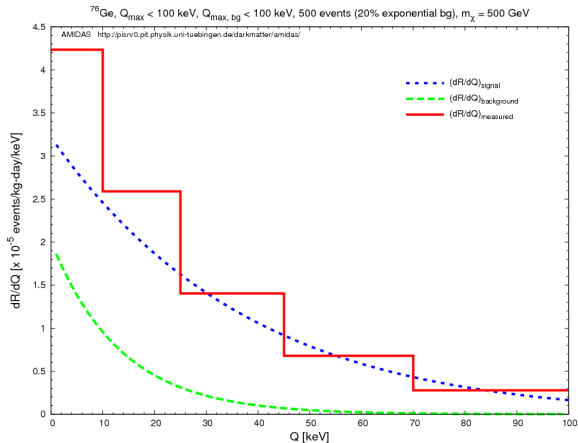
[Y. T. Chou and CLS, arXiv:1003.5277, accepted by JCAP]



Measured recoil spectrum

- Measured recoil spectrum

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[Y. T. Chou and CLS, arXiv:1003.5277, accepted by JCAP]

- └ Effects of residue background events
 - └ On the determination of the WIMP mass



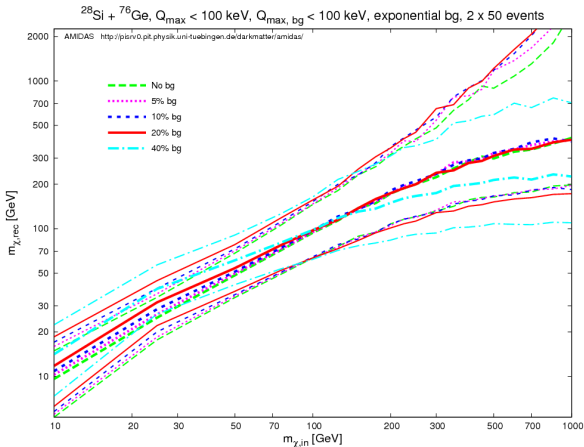
On the determination of the WIMP mass



On the determination of the WIMP mass

- Reconstructed $m_{\chi, \text{rec}}$

($^{28}\text{Si} + ^{76}\text{Ge}$, 0 – 100 keV, exponential bg 0 – 100 keV, 2×50 events)



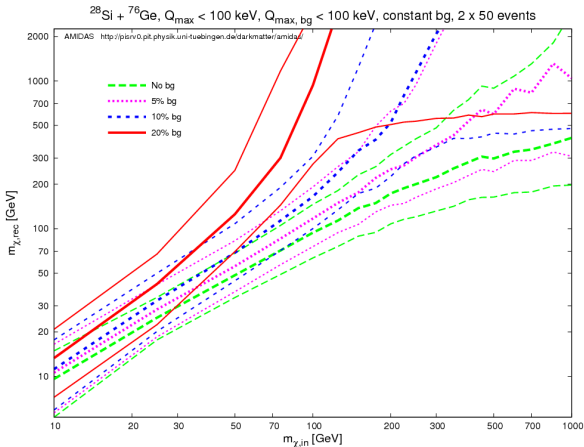
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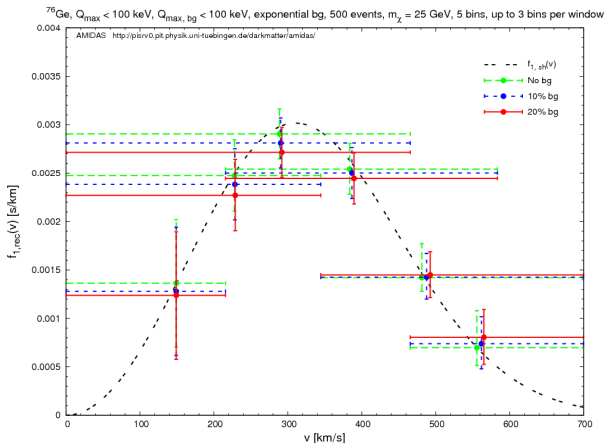


On the reconstruction of the WIMP velocity distribution

On the reconstruction of the WIMP velocity distribution

- Reconstructed $f_{1,\text{rec}}(v_s, n)$

(^{76}Ge , 0 – 100 keV, exponential bg 0 – 100 keV, 500 events, $m_\chi = 25 \text{ GeV}$)



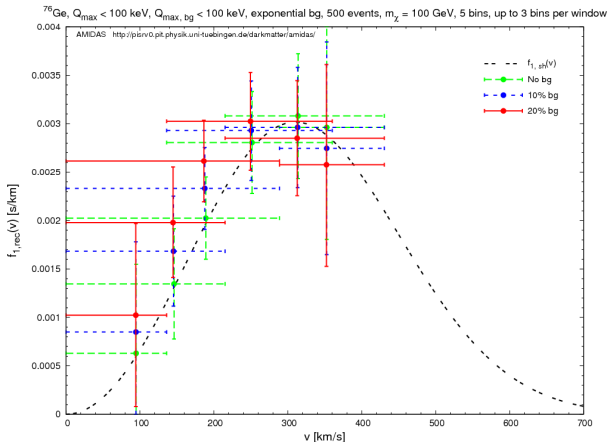
[CLS, JCAP 1006, 029]



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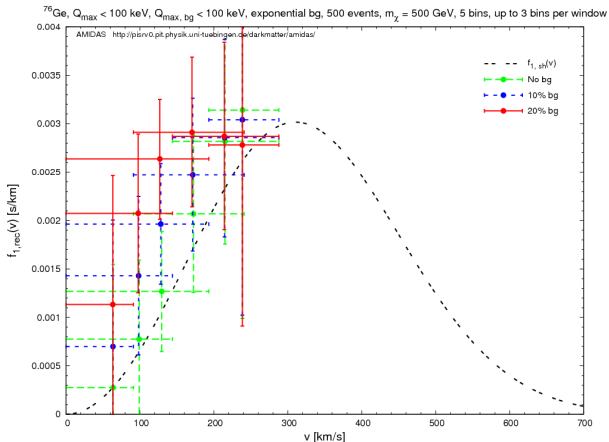
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On the reconstruction of the WIMP velocity distribution

- Reconstructed $f_{1,\text{rec}}(v_s, n)$

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[CLS, JCAP 1006, 029]



On the reconstruction of the WIMP velocity distribution

- Kinematic maximal cut-off of the recoil energy

$$Q_{\max, \text{kin}} = \frac{v_{\text{esc}}^2}{\alpha^2}$$

- Reconstruction of the one-dimensional WIMP velocity distribution

$$f_1(v_{s,n}) = \mathcal{N} \left[\frac{2Q_{s,n}r_n}{F^2(Q_{s,n})} \right] \left[\frac{d}{dQ} \ln F^2(Q) \Big|_{Q=Q_{s,n}} - k_n \right]$$

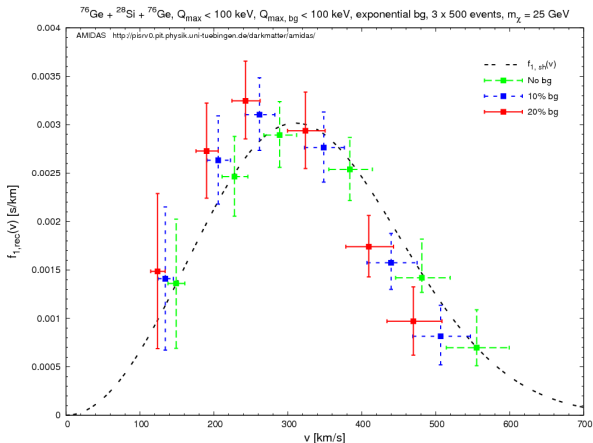
$$\mathcal{N} = \frac{2}{\alpha} \left[\sum_a \frac{1}{\sqrt{Q_a} F^2(Q_a)} \right]^{-1}$$

$$v_{s,n} = \alpha \sqrt{Q_{s,n}}$$

$$\alpha \equiv \sqrt{\frac{m_N}{2m_{r,N}^2}} = \frac{1}{\sqrt{2m_N}} \left(1 + \frac{m_N}{m_\chi} \right)$$

On the reconstruction of the WIMP velocity distribution

- Reconstructed $f_{1,rec}(v_{s,n})$ with reconstructed $m_{\chi,rec}$
 $(^{76}\text{Ge} + ^{28}\text{Si} + ^{76}\text{Ge}, 0 - 100 \text{ keV}, \text{exponential bg}, 3 \times 500 \text{ events}, m_{\chi} = 25 \text{ GeV})$

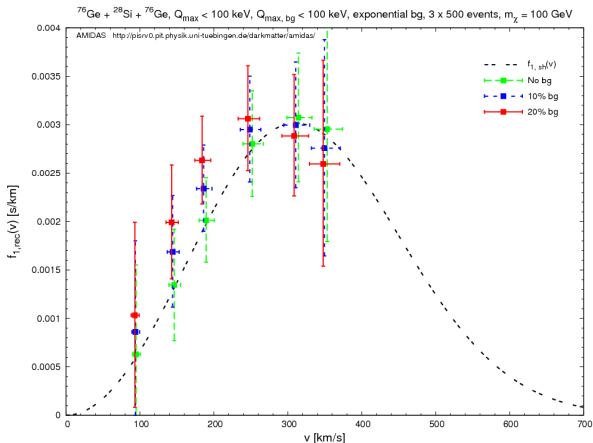


[CLS, JCAP 1006, 029]



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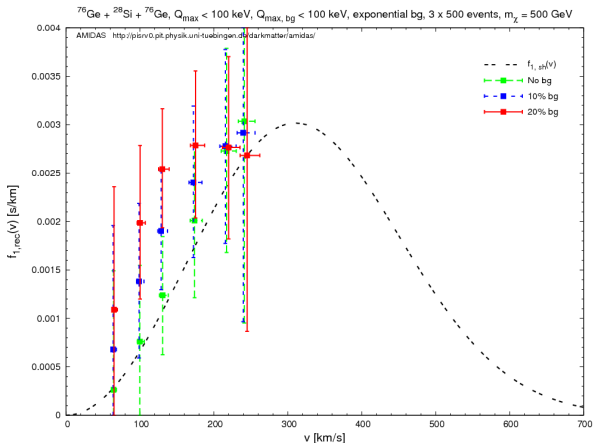


[CLS, JCAP 1006, 029]



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[CLS, JCAP 1006, 029]



Summary



Summary

- For determining m_χ
 - Background contribution in high/low energy ranges would over-/underestimate the reconstructed WIMP mass, especially if WIMPs are lighter/heavier than $\sim 50/200$ GeV.
 - Maximal acceptable background ratio is $\sim 10\% - 20\%$.



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- For estimating $|f_p|^2$

Preliminary results will be given at SUSY10!



Summary

Thank you very much for your attention

[<http://myweb.ncku.edu.tw/~clshan/Publications/Talks/>]