

# Constraints on the size of the extra dimension from KK gravitino decay

hep-ph/0702183

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# About Gravitino

- Local Susy : Supergravity.
- Gravitino (spin  $3/2$ ) susy partner of graviton.
- Gravitino can be a problem for cosmology:
  - Can disturb BBN because of its decay during or after.  
BBN starts nearly at  $t = 0.76$  sec (so for  $T = 1$  MeV). Gravitino lifetime runs from one second to  $10^8$  secondes for masses between 20 TeV to 200 GeV. This implies a bound on gravitino abundance: so on reheating temperature because gravitino abundance nearly proportionnal to reheating temperature. Between  $10^5$  GeV and  $10^8$  GeV : See Kohri and al. (2006).
  - Baryogenesis through leptogenesis because this theory needs large reheating temperature  $> 10^9$  GeV.

# Framework

- 5D supergravity compactified on  $S^1/Z_2$  orbifold.
- Only gravitational fields can propagate in the bulk. Graviton and Gravitino have Kaluza-Klein excitations.
- Two branes (orbifold fixed points): hidden sector on one brane, MSSM on the other.
- Radion stabilized : Standard Friedman equation.
- R-parity is conserved. The LSP is stable. LSP chosen: the lightest Neutralino : candidate for Dark Matter.
- In the present work : gravitinos are produced during the reheating period after inflation by scattering processes.

- First KK mode (the 0 mode) of gravitino: heavy enough to decay before BBN starts. Its mass calculated to 26.4 TeV. Possible in Anomaly mediation or in a mix between Anomaly mediation and Scherk-Scharwz mechanism.
- KK gravitinos decay into SM particles and Susy partners (see the interaction Lagrangian). Consequence: Non thermal production of LSPs.
- Dark matter density constrained to be (see Seljak and al. (2006))

$$0.106 < \Omega h^2 < 0.123, \text{ with a central value around } 0.114 \quad (1)$$

- Dark matter density made of thermal production and non thermal production from KK gravitino decay :

$$0.106 \leq \Omega_{th} h^2 + \Delta\Omega h^2 \leq 0.123 \quad (2)$$

- Only the gravitino modes decaying after thermal freeze-out of neutralino contribute to the non-thermal production of neutralinos.

## Interaction KK gravitino-MSSM

We find the interactions of each KK mode with matter and gauge fields after integrating on the fifth dimension the interaction part of the 5D action.  
(for details: see hep-ph/0702183)

$$\mathcal{L}_{interKK}^{4d} = \sum_{n=0}^{\infty} \left( -\frac{1}{\sqrt{2M}} e g_{ij^*} \tilde{D}_\nu \phi^{*j} \chi^i \sigma^\mu \bar{\sigma}^\nu \psi_{n,\mu} - \frac{1}{\sqrt{2M}} e g_{ij^*} \tilde{D}_\nu \phi^i \bar{\chi}^j \bar{\sigma}^\mu \sigma^\nu \bar{\psi}_{n,\mu} \right. \\ \left. - \frac{i}{2M} e \left( \psi_{n,\mu} \sigma^{\nu\lambda} \sigma^\mu \bar{\lambda}_{(a)} + \bar{\psi}_{n,\mu} \bar{\sigma}^{\nu\lambda} \bar{\sigma}^\mu \lambda_{(a)} \right) F_{\nu\lambda}^{(a)} \right) \quad (3)$$

Each KK mode has the same interaction with matter and gauge fields.

## Masses and lifetime

Lifetime :

$$\tau_k = 1.4 \cdot 10^7 \times \left( \frac{M_k}{100 \text{ GeV}} \right)^{-3} \text{ Sec} \quad (4)$$

Masses : see Bagger and al. (2002) and Curtis and al. (2004)

$$M_k = M_0 + \frac{k}{R} \quad (5)$$

# Production processes

$$A : g^a + g^b \longrightarrow \tilde{g}^c + G$$

$$B : g^a + \tilde{g}^b \longrightarrow g^c + G$$

$$C : g^a + \tilde{q}_i \longrightarrow q_j + G$$

$$D : g^a + q_i \longrightarrow \tilde{q}_j + G$$

$$E : q_i + \tilde{q}_j \longrightarrow g^a + G$$

$$F : \tilde{g}^a + \tilde{g}^b \longrightarrow \tilde{g}^c + G$$

$$G : \tilde{g}^a + q_i \longrightarrow q_j + G$$

$$H : \tilde{g}^a + \tilde{q}_i \longrightarrow \tilde{g}^c + G$$

$$I : q_i + q_j \longrightarrow \tilde{g}^a + G$$

$$J : \tilde{q}_i + \tilde{q}_j \longrightarrow \tilde{g}^a + G$$

## Abundance for the 0 mode

$$Y_{3/2} \simeq 1.9 \times 10^{-12} \times \left( \frac{T_R}{10^{10} \text{ GeV}} \right) \left[ 1 + 0.045 \ln \left( \frac{T_R}{10^{10} \text{ GeV}} \right) \right] \left[ 1 - 0.028 \ln \left( \frac{T_R}{10^{10} \text{ GeV}} \right) \right], \quad (6)$$

see Kohri and al.(2006)

Where  $Y_{3/2} = \frac{n_{3/2}}{s}$  and  $n_{3/2}$  is the number density,  $s$  is the entropy density.

$Y = \frac{n}{s}$  is the density per comoving volume.

$Y_{3/2}$  is found by solving the Boltzmann equation:  $\frac{dn_{3/2}}{dt} + 3Hn_{3/2} = C_{3/2}$



## Abundance for modes $k > 0$

We have to take into account in our calculation the different masses of gravitino modes. We find as a good approximation this rule for the abundance of the different modes:

$$\begin{aligned} Y_{3/2}^k &= Y_{3/2}^0, & \text{for } M^k \leq T_{\text{R}} & \text{ and} \\ Y_{3/2}^k &= 0, & \text{for } M^k > T_{\text{R}} & \end{aligned} \quad (7)$$

## Numerical cases

$$\Omega_{th} h^2 = 3.614222 \cdot 10^6 \frac{m_{lsp}}{1 \text{ GeV}} x_f^2 e^{-x_f} \quad (8)$$

We choose :

| Cases  | $x_f$   | $T_f(\text{GeV})$ | $\Omega_{th} h^2$ | $(\Delta\Omega_{th} h^2)_{min}$ | $(\Delta\Omega_{th} h^2)_{max}$ | $M_n(\text{GeV})$   |
|--------|---------|-------------------|-------------------|---------------------------------|---------------------------------|---------------------|
| Case 1 | 28.7787 | 4.1697            | 0.114             | -                               | 0.009                           | $9.844 \times 10^6$ |
| Case 2 | 29.6006 | 4.0540            | 0.053             | 0.053                           | 0.070                           | $9.661 \times 10^6$ |
| Case 3 | 30.4224 | 3.9445            | 0.025             | 0.081                           | 0.098                           | $9.486 \times 10^6$ |

Table 1: *The three numerical cases for  $m_{lsp} = 120 \text{ GeV}$*

## Equations of constraints

Abundance of gravitinos is related to  $T_R$  and number of KK modes is related to the size of the extra dimension. To respect the requirement on the dark matter density we find:

For  $M^n \leq T_R$ :

$$R^{-1} = \frac{M^n - M^0}{E \left[ \Delta\Omega h^2 \frac{\rho_c}{m_{lsp} s_0 h^2} \frac{1}{1.9 \times 10^{-12} \times \frac{T_R}{10^{10}} \left[ 1 + 0.045 \ln \left( \frac{T_R}{10^{10}} \right) \right] \left[ 1 - 0.028 \ln \left( \frac{T_R}{10^{10}} \right) \right]} \right]} - 1 \quad (9)$$

For  $M^n > T_R$ ,  $M^n$  is replaced by  $T_R$  in the above equation.

## Maximum reheating temperature

If there is only one gravitino mode, there is a maximum reheating temperature:

| case 1                         | case 2                            | case 3                            |
|--------------------------------|-----------------------------------|-----------------------------------|
| $1.455 \cdot 10^9 \text{ GeV}$ | $1.088 \cdot 10^{10} \text{ GeV}$ | $1.521 \cdot 10^{10} \text{ GeV}$ |

Table 2: *Maximum reheating temperature*

# KK gravitons

Masses:

$$m_k = \frac{k}{R} \quad (10)$$

Abundance:

$$Y_m = \frac{1485}{256\pi^5 M g^{*1/2} g_S^*} m \int_{m/T_R}^{\infty} x^3 K_1(x) dx \quad (11)$$

Where  $g^*$  and  $g_S^*$  are taken constant equal to 10 since most of the lifetime of the gravitons that we consider is after  $T = 1$  MeV.

Lifetime:

$$\tau = 3.310 \times \frac{\pi M^2}{m^3} \text{ GeV}^{-1} \quad (12)$$

For details see hep-ph/0702183.

We checked that for  $R^{-1} \geq 1$  TeV, BBN was not disturbed by decay of KK gravitons using the curves given by Jedamzik (2006).

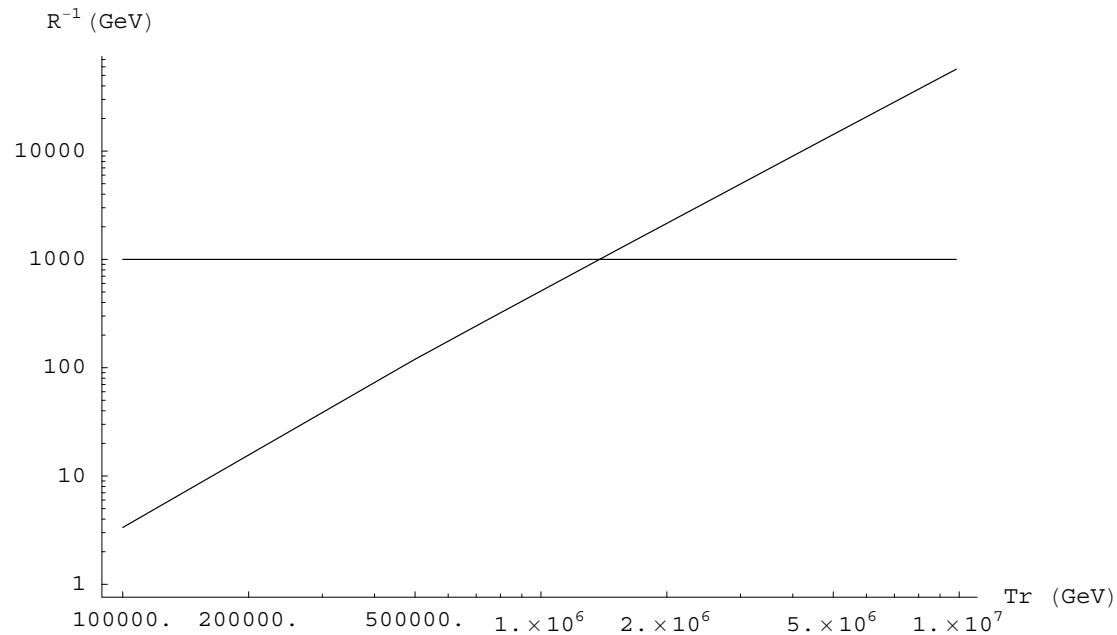


Figure 1: Case 1.  $T_R$  less than  $9.84 \cdot 10^6$  GeV. The excluded zone is below the diagonal curve and below the straight line  $R^{-1} = 1$  TeV if the KK gravitons constraint is taken into account.

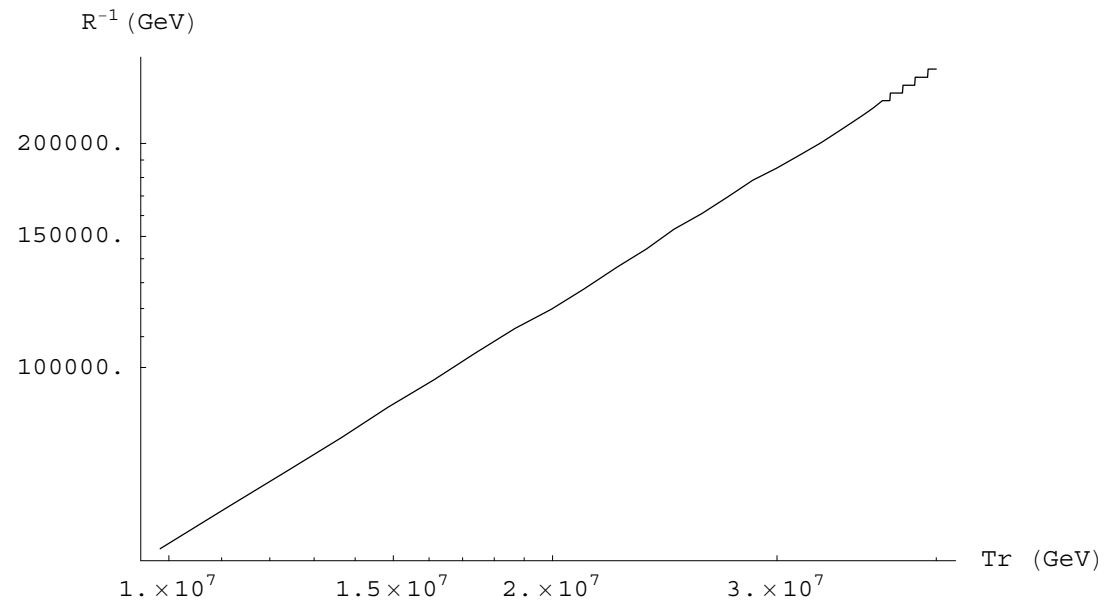


Figure 2: Case 1.  $9.84 \cdot 10^6 \text{ GeV} \leq T_R \leq 4 \cdot 10^7 \text{ GeV}$ . The excluded zone is below the curve.

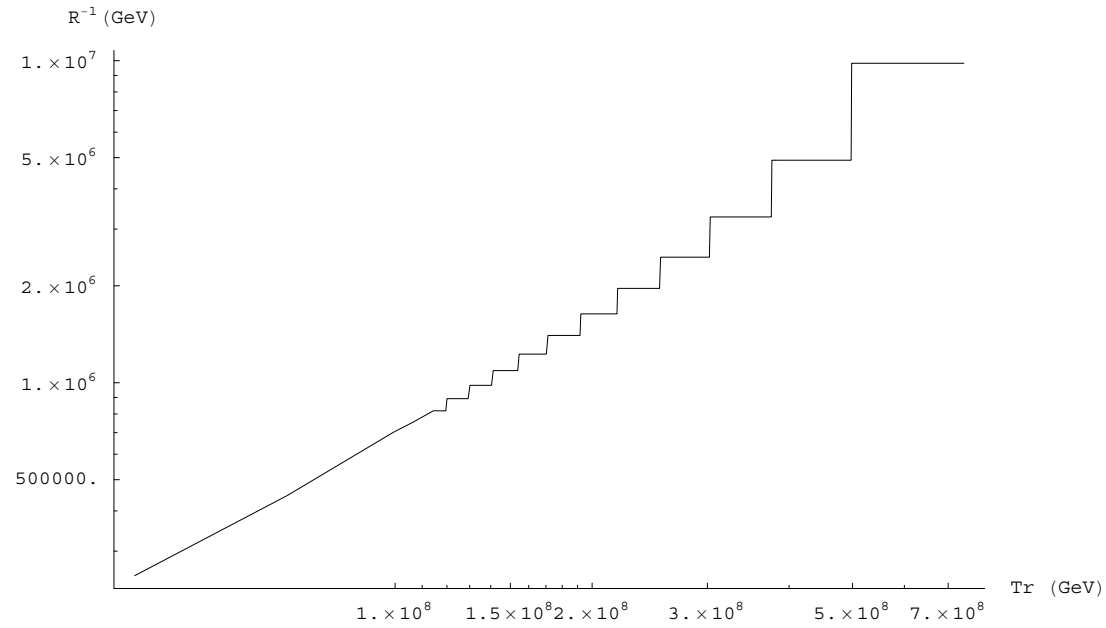


Figure 3: Case 1.  $4 \cdot 10^7 \text{ GeV} \leq T_R \leq 7.396 \cdot 10^8 \text{ GeV}$ . The excluded zone is below the curve.



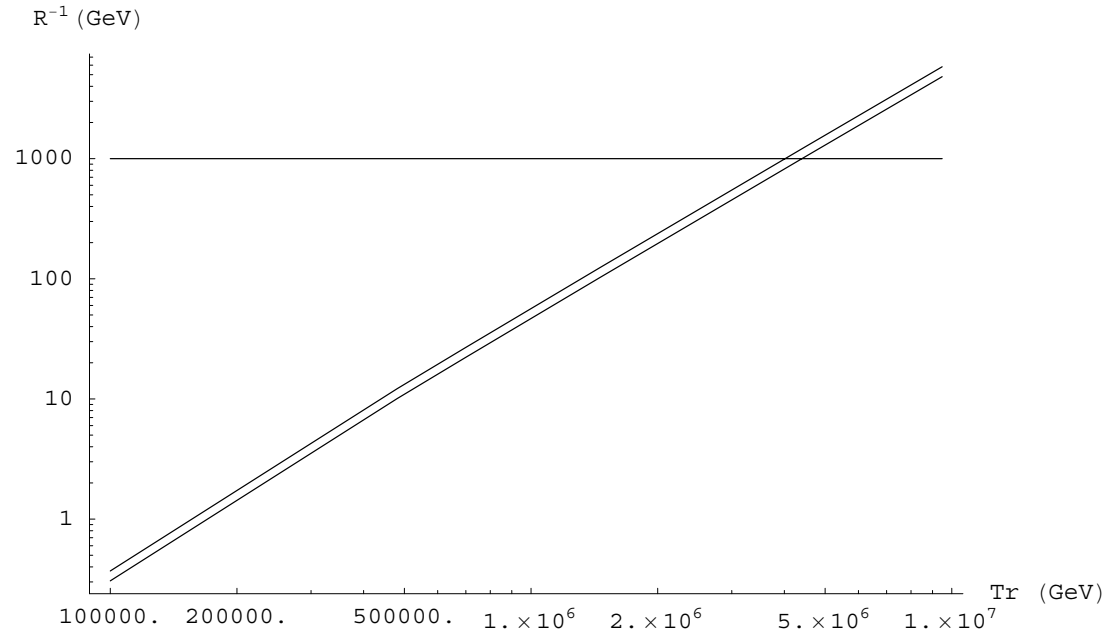


Figure 4:  $T_R$  less than  $9.48 \cdot 10^6$  GeV. Only the band between the two diagonal curves is allowed. The zone below the straight line  $R^{-1} = 1$  TeV is excluded if KK gravitons constraint is taken into account. In that case a minimum value for  $T_R$  appears equal to  $4.02 \cdot 10^6$  GeV.

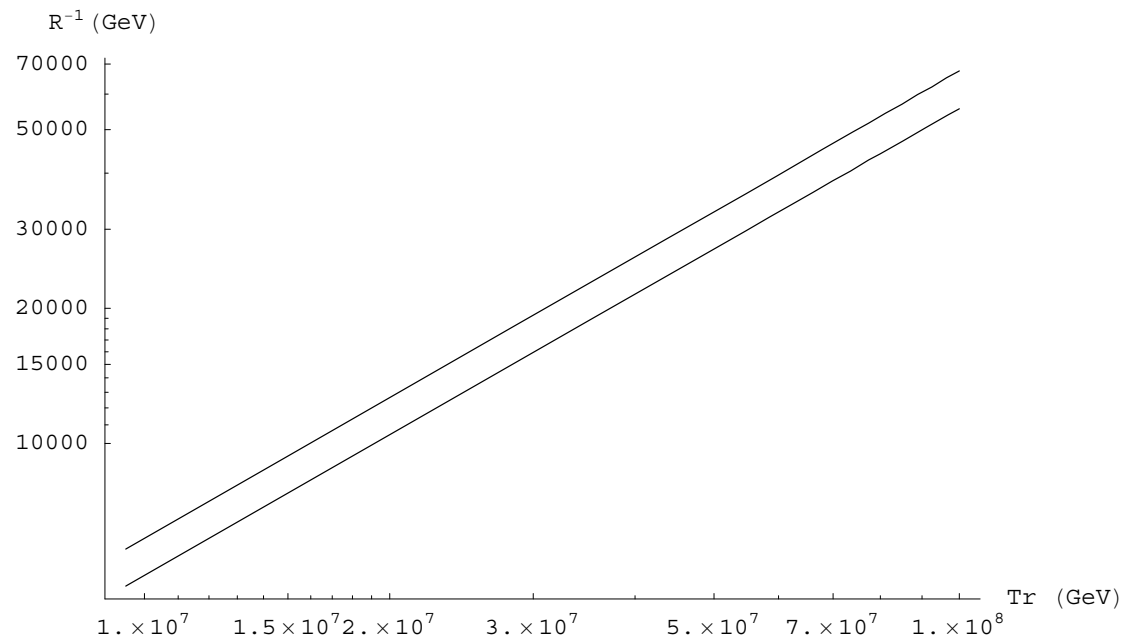


Figure 5: Case 3.  $9.48 \cdot 10^6 \text{ GeV} \leq T_R \leq 10^8 \text{ GeV}$ . Only the band between the two curves is allowed.

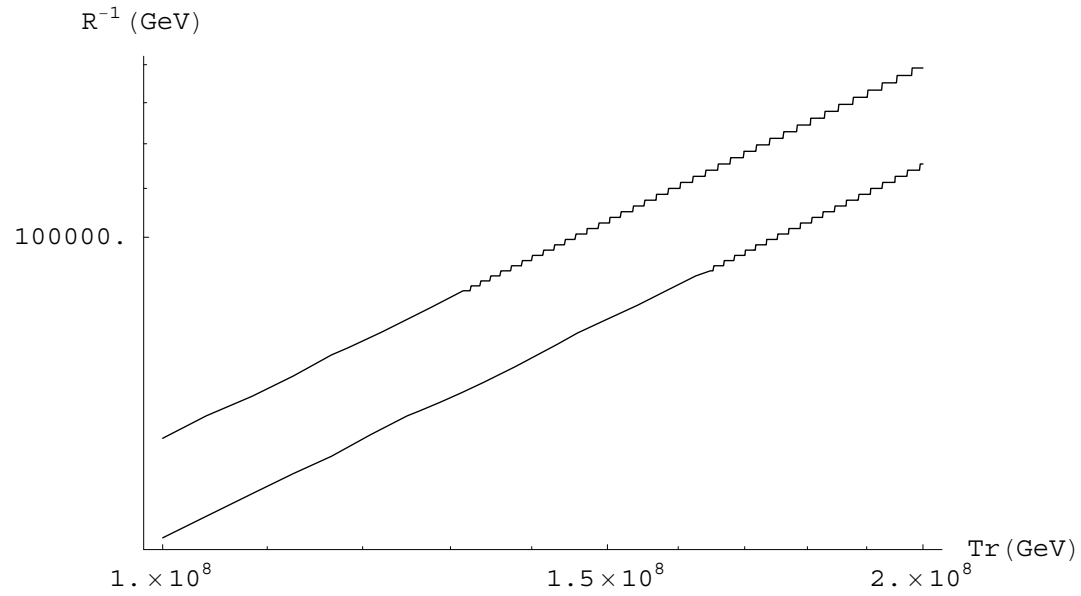


Figure 6:  $10^8 \text{ GeV} \leq T_R \leq 2 \cdot 10^8 \text{ GeV}$ . Only the band between the two curves is allowed.

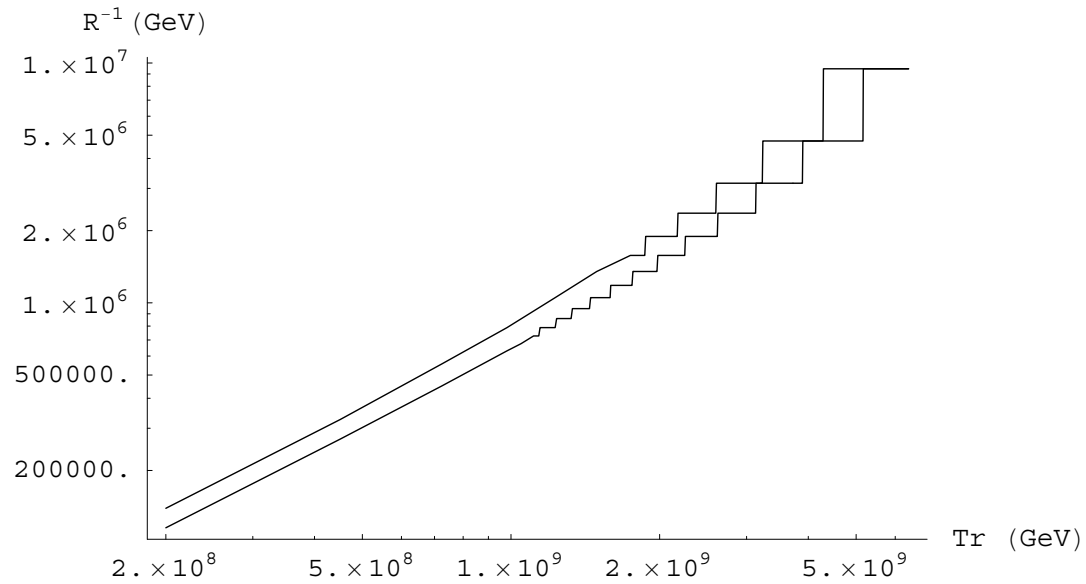


Figure 7: Case 3.  $2 \cdot 10^8 \text{ GeV} \leq T_R \leq 6.385 \cdot 10^9 \text{ GeV}$ . Only the band between the two curves is allowed.

# Conclusion

- Cosmological models with high reheating temperature i.e.  $10^5$  GeV to  $10^{10}$  GeV in the framework of a 5D supergravity compactified on  $S^1/Z_2$  where matter and gauge fields live on tensionless branes at the orbifold fixed points.
- Framework can be linked to Horava-Witten M-theory where a 5 dimensional stage of the universe appears in which bulk fields are gravitational and where supersymmetry is natural but also to theories of baryogenesis through leptogenesis which imply large reheating temperature.
- Assumption that dark matter is made by the lightest supersymmetric particle which is supposed to be the lightest neutralino.
- Neutralinos density is a sum of a thermal production and a non thermal production from gravitino decay.
- Gravitinos in the model do not disturb BBN because they are heavy enough to decay before BBN starts. Heavy gravitinos are natural in a certain class of Susy breaking models (anomaly mediation and mix between anomaly and Scherk Schwarz mechanism).

We find:

- Curves of constraints between the size  $R$  of the extra-dimension and the reheating temperature of the Universe after inflation.
- Results independent from the susy mass spectrum since the gravitino is heavy enough to make negligible the influence of other susy particles.
- Size of the radius  $R$  is not only bounded by a maximum value but also by a minimum value in a range of possible values for the thermal production of neutralinos and in a range of values for the reheating temperature.
- KK gravitons may disturb BBN. For  $R^{-1}$  above 1 TeV it is not the case. It implies a bound on the reheating temperature which can not be lower than a minimum value in the cases where the radius  $R$  is bounded by a minimum value.

A few perspectives:

- To look at RS model : so to include a cosmological constant. Problem (?): Non standard cosmology at high energy.
- To include new elements in the calculation of the thermal production of gravitinos (see Rychkov and Strumia (2007))
- To treat more accurately the problem of KK gravitons with BBN. (Work with Jedamzik)
- Cold + Warm dark matter ? (with Jedamzik and al.)