

# Precision Measurements in Neutron Decay

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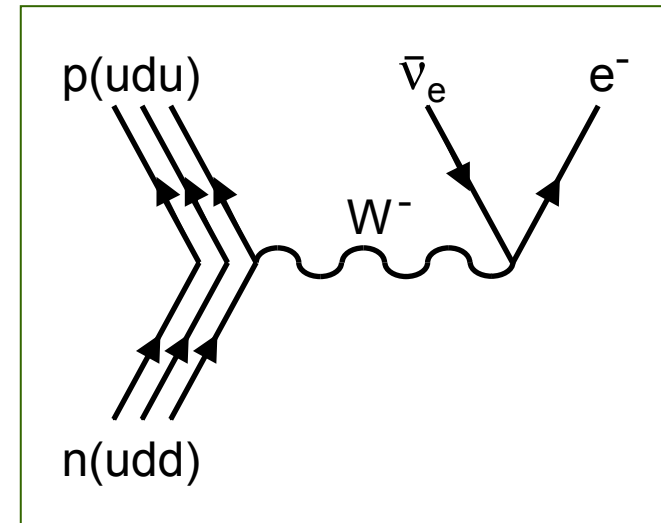
PERKEO II Collaboration



# Neutron Decay

- Lifetime  $\tau \approx 15$  min
- electron  $E_{\max} = 782$  keV
- only first particle generation
- Standard Model, V–A Theory:

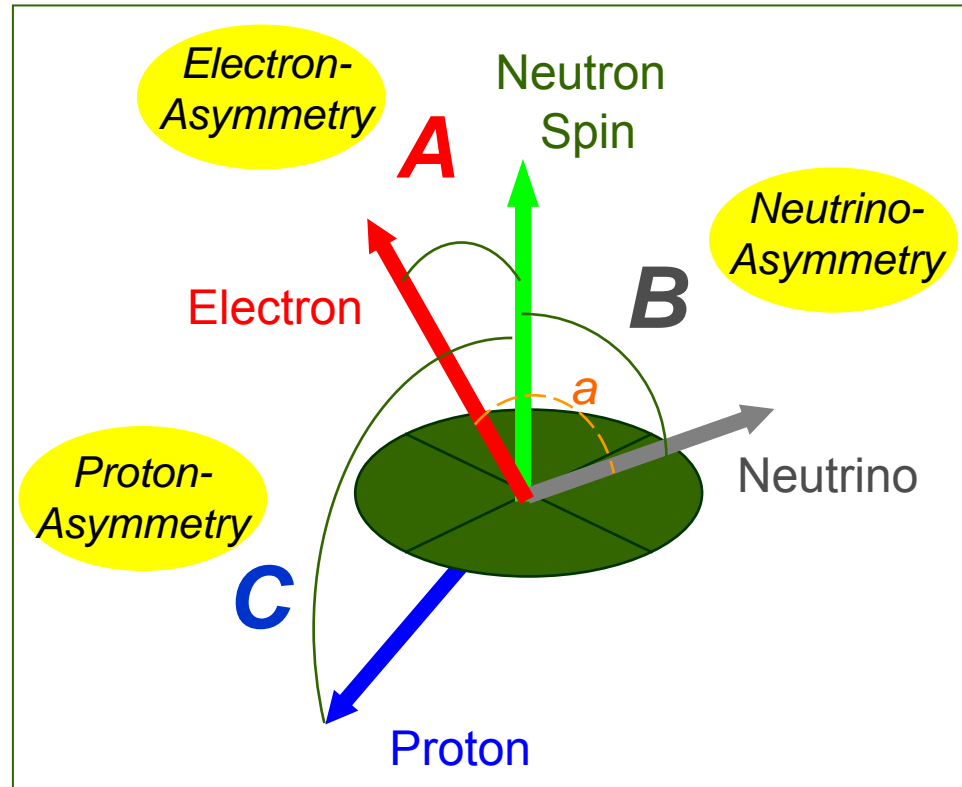
$$\tau \propto \frac{1}{|V_{ud}|^2 (g_V^2 + 3g_A^2)} \quad \lambda = \frac{g_A}{g_V}$$



Neutron Physics  
= Particle Physics at low Energy



# (Our) Observables in Neutron Decay



Transition  
Probability:

$$d\omega \propto G_F^2 |V_{ud}|^2 F(E) \left( 1 + a \frac{\mathbf{p}_e \mathbf{p}_\nu}{EE_\nu} + b \frac{m_e}{E} + \langle \mathbf{s}_n \rangle \left[ A \frac{\mathbf{p}_e}{E} + B \frac{\mathbf{p}_\nu}{E_\nu} + D \frac{\mathbf{p}_e \times \mathbf{p}_\nu}{EE_\nu} \right] \right)$$



# 1. Determination of $\lambda = g_A/g_V$

- Electron Asymmetry: 
$$A = -2 \frac{\lambda^2 + \lambda}{1 + 3\lambda^2}$$

- All semileptonic processes are governed by this number:

Cosmology	Primordial element formation ( $^2\text{H}$ , $^3\text{He}$ , $^4\text{He}$ , $^7\text{Li}$ , ... )	$n + e^+ \rightarrow p + \nu'_e$ $p + e^- \rightarrow n + \nu_e$ $n \rightarrow p + e^- + \nu'_e$	$\sigma_\nu \sim 1/\tau$ $\sigma_\nu \sim 1/\tau$ $\tau$	
Astronomy	Solar cycle Neutron star formation	$p + p \rightarrow ^2\text{H} + e^+ + \nu_e$ $p + p + e^- \rightarrow ^2\text{H} + \nu_e$ etc. $\sim (g_A/g_V)^5$ $p + e^- \rightarrow n + \nu_e$		
Particle Physics	Pion decay Neutrino detectors Neutrino forward scattering W and Z production	$\pi^- \rightarrow \pi^0 + e^- + \nu'_e$ $\nu'_e + p \rightarrow e^+ + n$ $\nu_e + n \rightarrow e^- + p$ etc. $u' + d \rightarrow W^- \rightarrow e^- + \nu'_e$ etc.		

courtesy of D. Dubbers



## 2. Right-handed Currents in weak i.a.

- Weak interaction is **maximally parity violating** in the SM
- SM describes parity violation; no motivation given  $SU(3)_c \otimes SU(2)_L \otimes U(1)$
- Cosmology: early universe should be LR-symmetric

### Left-Right-Symmetric Models *eg: PRL 38, 22 (1977)*

- $SU(4)_{EC} \otimes SU(2)_L \otimes SU(2)_R \longrightarrow SU(3)_c \otimes SU(2)_L \otimes U(1)$
- 2 bosons ( $W_1, W_2$ ) in the „symmetric base“;  $W_2$  very heavy

$$\begin{pmatrix} W_L \\ W_R \end{pmatrix} = \begin{pmatrix} \cos \zeta & -\sin \zeta \\ e^{i\phi} \sin \zeta & e^{i\phi} \cos \zeta \end{pmatrix} \begin{pmatrix} W_1 \\ W_2 \end{pmatrix} \quad \lambda' = \frac{g'_A}{g'_V} \quad \delta = \frac{m_1^2}{m_2^2}$$

**v-asymmetry  $B$  is sensitive right-handed currents**



# Right-handed Currents?

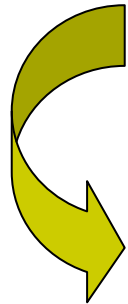
## Standard Model

$$A = -2 \frac{\lambda^2 + \lambda}{1 + 3\lambda^2}$$

$$B = 2 \frac{\lambda^2 - \lambda}{1 + 3\lambda^2}$$

$$a = \frac{1 - \lambda^2}{1 + 3\lambda^2}$$

$$R_{ft} = \frac{2}{1 + 3\lambda^2} \quad R_{ft} = \frac{f^R \tau_n \ln(2)}{ft_{0+ \rightarrow 0+}}$$



## Manifest LR-Symmetric Model

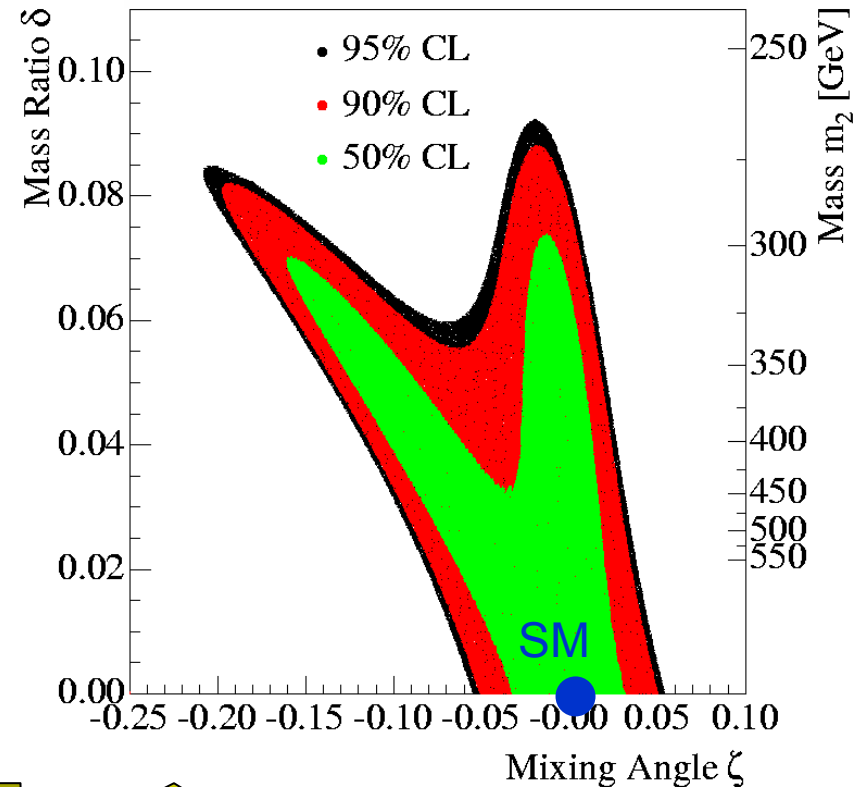
$$A = 2 \frac{\lambda'(r_V r_A - 1) + \lambda'^2(r_A^2 - 1)}{(1 + r_V^2) + 3\lambda'^2(1 + r_A^2)}$$

$$B = 2 \frac{\lambda'^2(1 - r_A^2) + \lambda'(r_V r_A - 1)}{(1 + r_V^2) + 3\lambda'^2(1 + r_A^2)}$$

$$a = \frac{(1 + r_V^2) - \lambda'^2(1 + r_A^2)}{(1 + r_V^2) + 3\lambda'^2(1 + r_A^2)}$$

$$R_{ft} = \frac{2(1 + r_V^2)}{(1 + r_V^2) + 3\lambda'^2(1 + r_A^2)}$$

$$(A, B, \tau_n) \rightarrow (\lambda', \zeta, \delta = \frac{m_1^2}{m_2^2})$$





# 3. Scalar and Tensor Couplings

Most general Lagrangian:

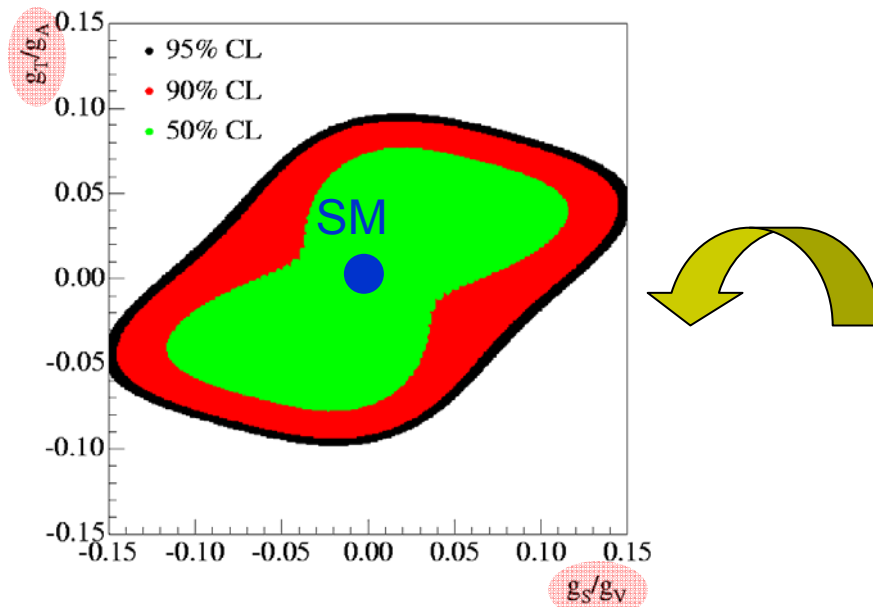
$$\mathcal{L} = \sum_k (\bar{p}\Omega_k n) (\bar{e}\Omega_k (g_k + g'_k \gamma^5) \nu_e) + \text{h.c.}$$

$$\begin{aligned} \Omega_S &= 1 && \text{Scalar} \\ \Omega_V &= \gamma^\mu && \text{Vector} \\ \Omega_T &= \frac{1}{\sqrt{2}} \sigma^{\mu\nu} && \text{Tensor} \\ \Omega_A &= \gamma^\mu \gamma^5 && \text{Axial-vector} \\ \Omega_P &= \gamma^5 && \text{Pseudo-scalar} \end{aligned}$$

Right-handed Scalar and Tensor Model:

e.g.: *Sov.J.Nucl. Phys.* **53**, 260 (1991); *Rev.Mod.Phys.* **78**, 991 (2006)

$$\frac{g'_V}{g_V} = 1 \quad \frac{g'_A}{g_A} = 1 \quad \frac{g'_S}{g_V} = -\frac{g_S}{g_V} \quad \frac{g'_T}{g_A} = -\frac{g_T}{g_A}$$



$$\begin{aligned} A &= -2 \frac{g_A^2 + g_A g_V + g_S g_T + g_T^2}{g_V + 2g_A^2 + g_S + 3g_T^2} \\ B &= 2 \frac{g_A^2 - g_A g_V + g_S g_T - g_T^2}{g_V + 2g_A^2 + g_S + 3g_T^2} \\ a &= \frac{g_V^2 - g_A^2 - g_S^2 + g_T^2}{g_V + 2g_A^2 + g_S + 3g_T^2} \\ C &= 4x_C \frac{g_A g_V + g_T^2}{g_V + 2g_A^2 + g_S + 3g_T^2} \\ R_{ft} &= 2 \frac{g_V^2 + g_S^2}{g_V + 2g_A^2 + g_S + 3g_T^2} \end{aligned}$$

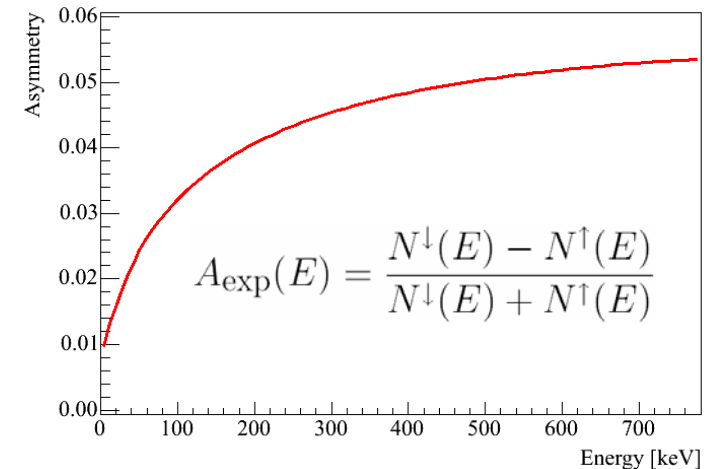
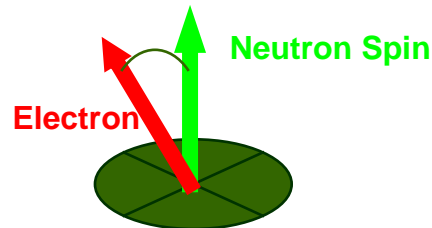
$$x_C = 0.27484$$

# The experimental Signature

Systematically clean method: Integration over two hemispheres

- Electron Asymmetry  $A$

→ measure only electrons

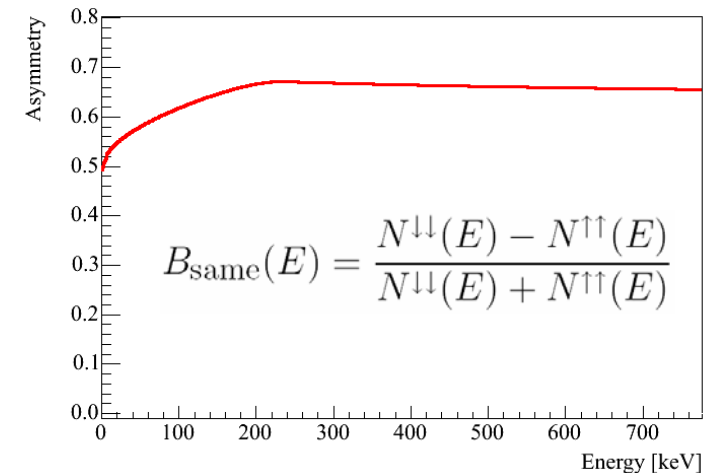
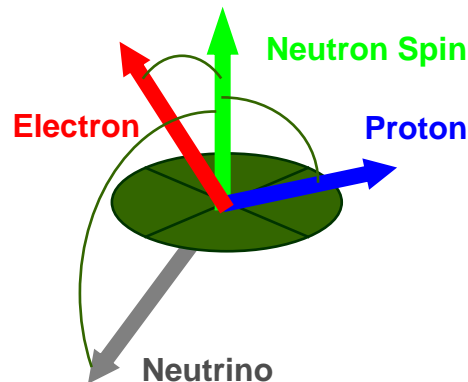


- Neutrino Asymmetry  $B$  – same hemisphere

→ coincidence measurement

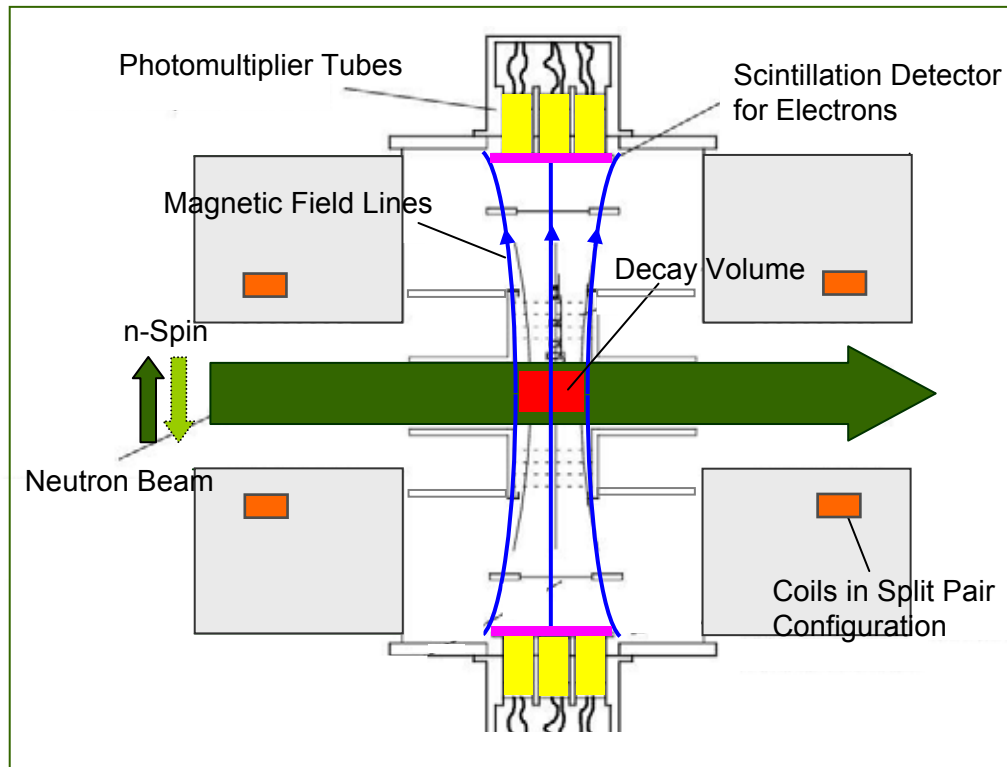
→ low dependence on energy calibration and energy resolution

→ obtain proton asymmetry  $C$  from  $B$ -measurement





# The Spectrometer: PERKEO II



## Magnetic field (1 T):

- perpendicular to neutron beam
- parallel alignment of neutron spin
- separation into hemispheres  
 ⇒ integration over hemispheres  
 ⇒  $2 \times 2 \pi$  detector
- guide  $e^-$ ,  $p$  onto detectors  
 ⇒ detect all particles
- low background

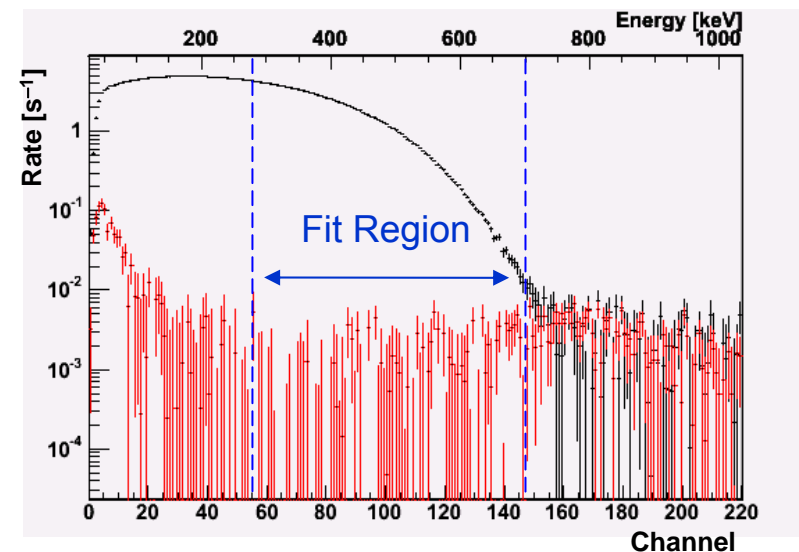
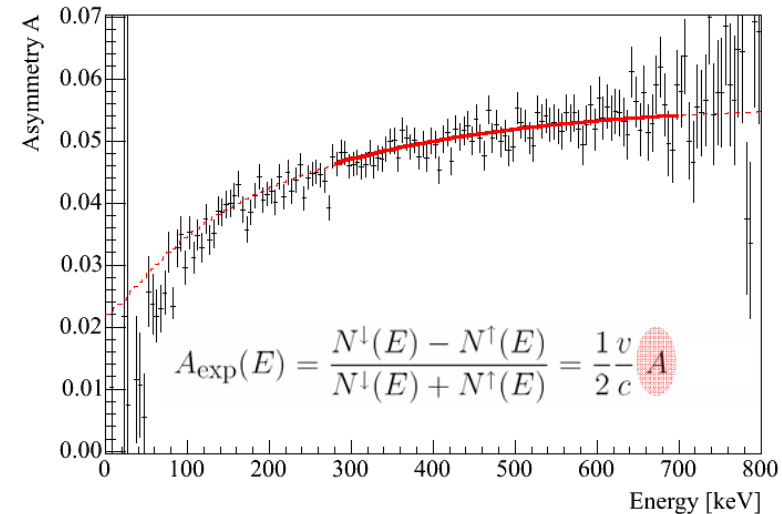
# Electron Asymmetry A

Results of PhD thesis D. Mund

- Polarization heavily improved (Supermirror Polarizers and  $^3\text{He}$  cells)
- 160 Million Events
- Still limited by Statistics
- Small Background effects (0.1%).  
Background cannot be further reduced with this setup
- almost no (0.4%) corrections to asymmetry A are left

Our Result (*preliminary*):

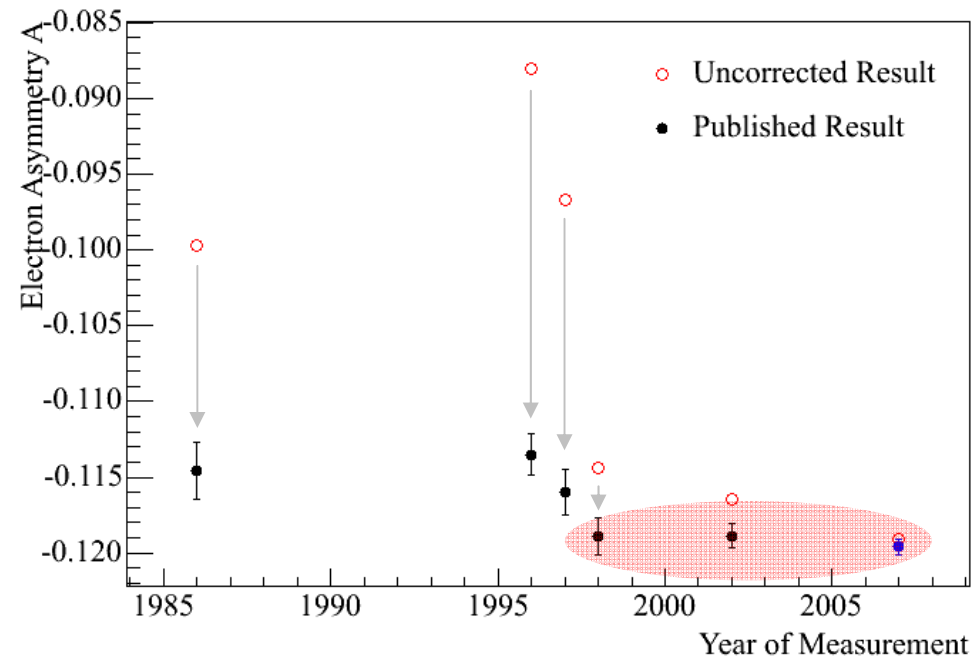
$$A = -0.1196(5)$$





# Electron Asymmetry Results

- Result confirms former PERKEO II measurements
- Only PERKEO values have **small corrections**
- averaging all results is not reasonable



- (our) new mean value:

$$A_{\text{PII}} = 0.1193(4)$$

$$\lambda_{\text{PII}} = -1.2749(11)$$

error: 0.09%

*preliminary*





# Result: Asymmetry $B$

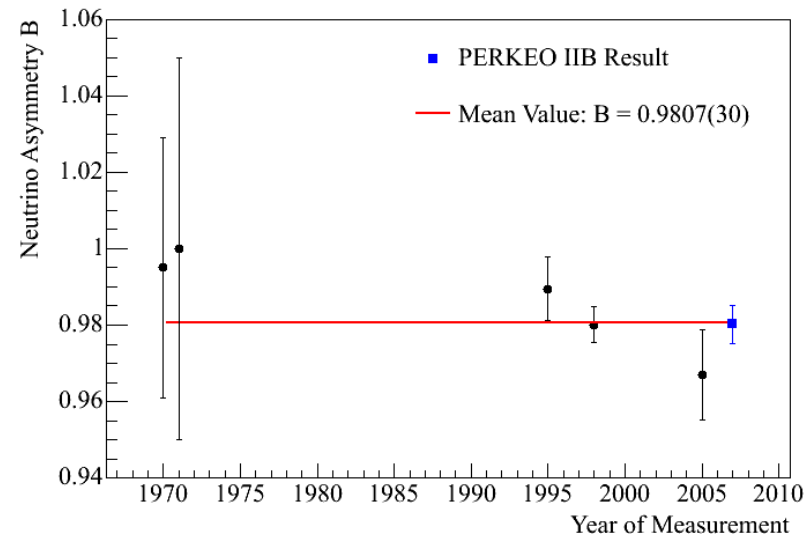
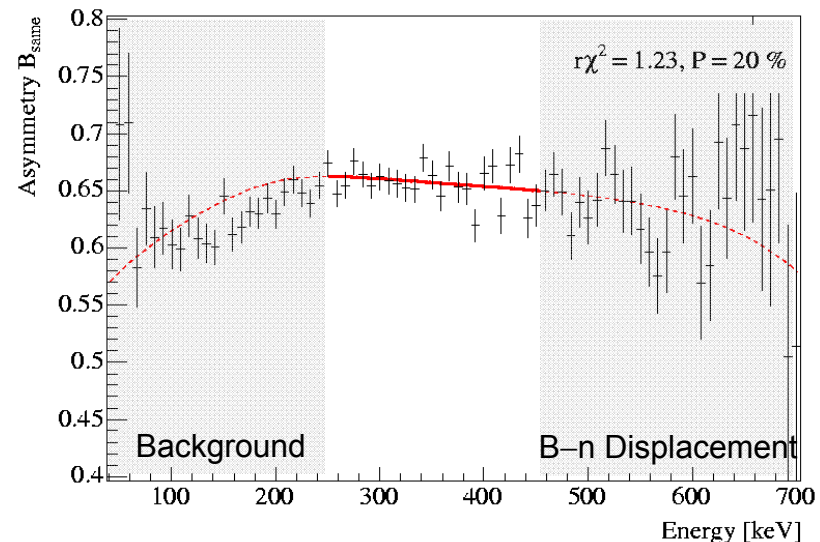
- only experiment that measures  $B$  in the same hemisphere
- ⇒ result is almost independent from detector calibration
- result limited by statistics and error in beam position relative to magn. field (→ magnetic mirror effect)

Our Result:

$$B = 0.9802(50)$$

New mean Value:

$$B_{\text{mean}} = 0.9807(30)$$





# Proton–Asymmetry C

- measure proton emission w.r.t. neutron spin:  $N^\uparrow$ ,  $N^\downarrow$   
(coincidence measurement with electrons)
- use electron spectra and **integrate** over electron energy  $E$

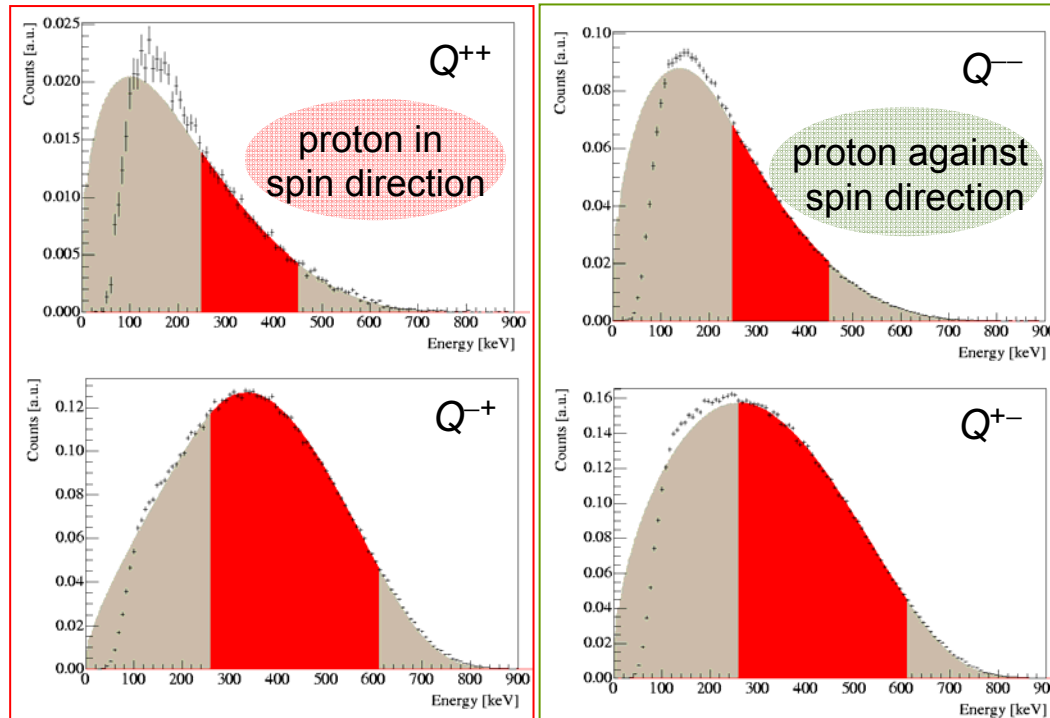
$$N^\uparrow = Q^{++}(E) + Q^{-+}(E) \quad N^\downarrow = Q^{--}(E) + Q^{+-}(E)$$

- define **Proton–Asymmetry**

$$C = \frac{\int(Q^{++}(E) + Q^{-+}(E))dE}{\int(Q^{++}(E) + Q^{-+}(E))dE + \int(Q^{--}(E) + Q^{+-}(E))dE} - \frac{\int(Q^{--}(E) + Q^{+-}(E))dE}{\int(Q^{++}(E) + Q^{-+}(E))dE + \int(Q^{--}(E) + Q^{+-}(E))dE}$$

- Problem: Energy threshold for electron detection
- PERKEO II (2001):  $C = -0.238(11)$  *PhD M. Kreuz, J. Res. NIST. 110 (2005)*

# Proton–Asymmetry C: Results



- 1) One-parameter fit
- 2) Extrapolation
- 3) Integration

Our Result:

$$C = -0.2377(36)$$

- first precision measurement of  $C$
- error dominated by extrapolation and detector calibration
- $C$  is better known than  $e$ – $\nu$  correlation  $a$
- new SM Tests possible:

$$C = x_C(A + B)$$



# Input Parameters for $\chi^2$ -Scans

- Electron Asymmetry

$$A_{\text{PDG}} = -0.1173(13)$$

$$A_{\text{PII}} = -0.1193(4)$$

PDG 2006, error scaled with 2.3  
only PERKEO II, including new result  
only small corrections

- Neutrino Asymmetry

$$B = 0.9807(30)$$

new mean value

- Proton Asymmetry

$$C = -0.2377(36)$$

first precise value

- e– $\nu$  correlation

$$a = -0.103(4)$$

PDG 2006

- Neutron Lifetime

$$\tau_{\text{PDG}} = 885.7(8) \text{ s}$$

$$\tau_{\text{Ser}} = 878.5(8) \text{ s}$$

$$\tau_{\text{mean}} = 882.0(14) \text{ s}$$

PDG 2006

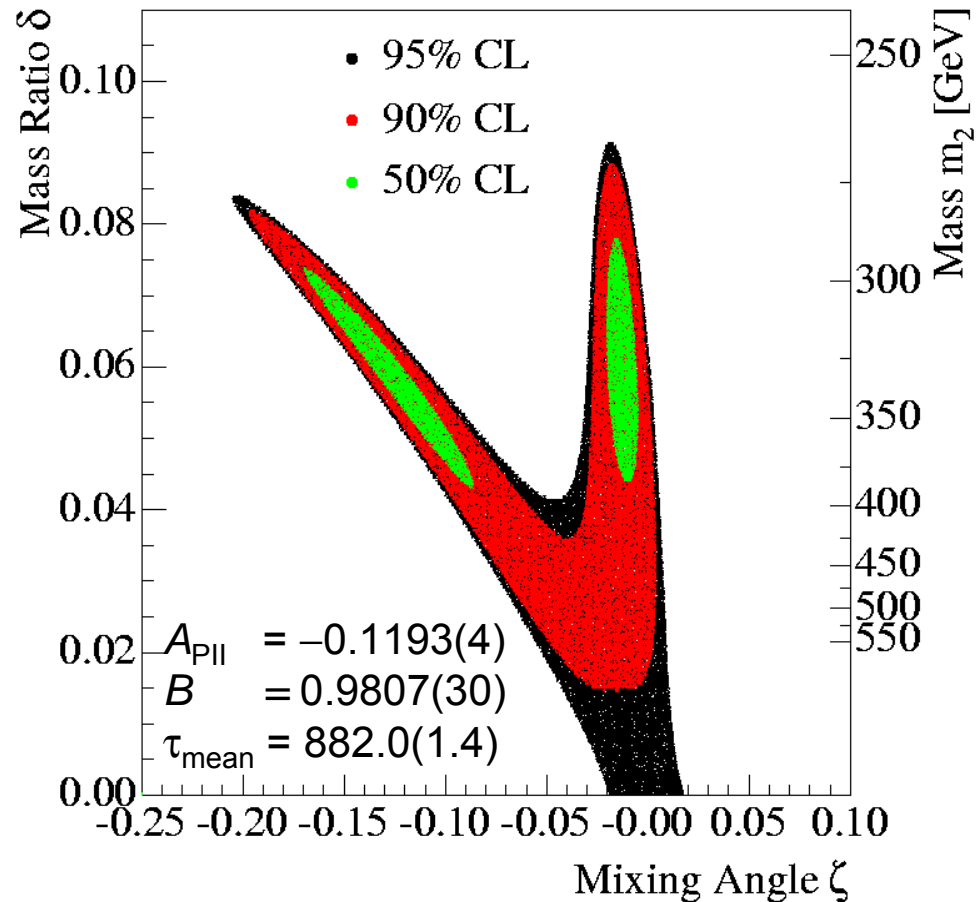
Serebrov 2005

*PLB 605, 72 (2005)*

scaling factor 2.47



# Right-handed Currents



Neutron Decay Limits (90 % CL):

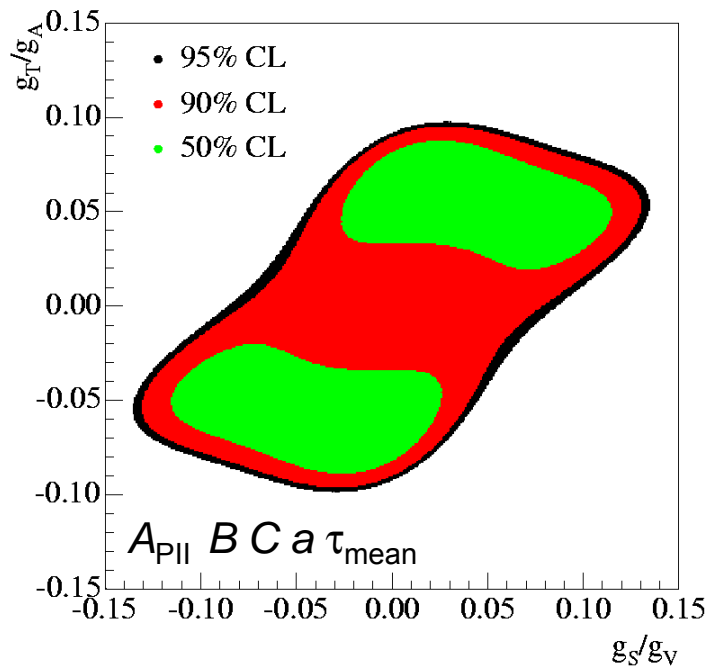
$$-0.1968 \leq \zeta \leq 0.0040$$

$$\delta \leq 0.0885$$

$$\Rightarrow m_2 \geq 270 \text{ GeV}$$

Standard Model included  
in 95 % CL contour.

# Scalar and Tensor Couplings



Neutron decay limits (90% CL):

$$|g_S/g_V| \leq 0.130$$

$$|g_T/g_A| \leq 0.0948$$

Standard Model agrees with data.

$g_S \rightarrow$  superallowed  $\beta$ -decays:  $|g_S/g_V| \leq 0.0013$  [PRL 94, 092502 \(2005\)](#)

$g_T \rightarrow$  very good limits from n-decay



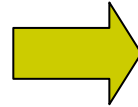
# Summary

PERKEO II allows to measure angular correlations in neutron decay very precisely with low corrections

$$A = -0.1195(5) \text{ *prelim.*}$$

$$B = 0.9802(50)$$

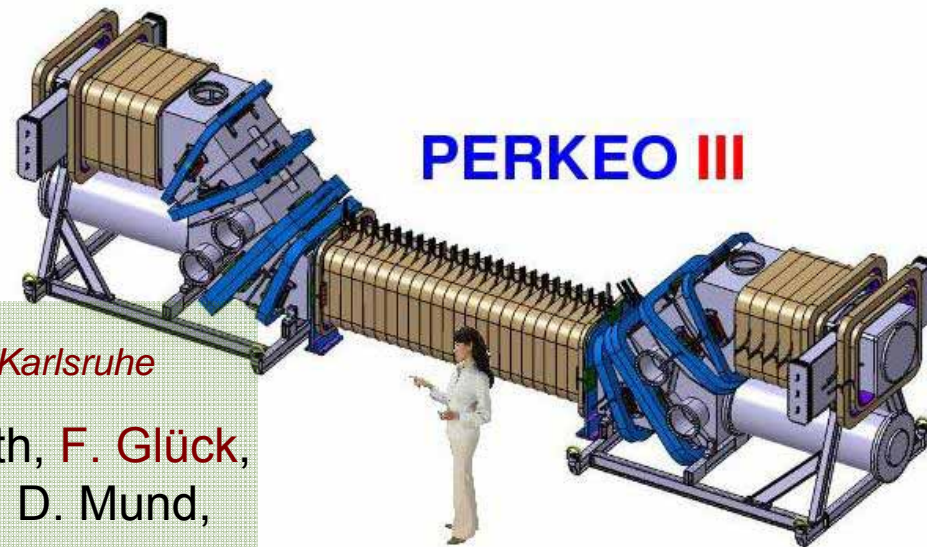
$$C = -0.2377(36)$$



$$\lambda = -1.2749(11) \text{ *prelim.*}$$

Standard Model tests

The Future: PERKEO III  
currently takes data @ ILL



**The Team** *Uni Heidelberg, ILL, FZ Karlsruhe*

H. Abele, M. Brehm, M. Deissenroth, **F. Glück**,  
J. Krempel, **M. Kreuz**, B. Märkisch, D. Mund,  
**A. Petoukhov**, M. S., **T. Soldner**



# Backup

# Transition probability

Transition probability for polarized neutrons:

$$d\omega \propto G_F^2 |V_{ud}|^2 F(E) \left( 1 + a \frac{\mathbf{p}_e \mathbf{p}_\nu}{EE_\nu} + b \frac{m_e}{E} + \langle \mathbf{s}_n \rangle \left[ A \frac{\mathbf{p}_e}{E} + B \frac{\mathbf{p}_\nu}{E_\nu} + D \frac{\mathbf{p}_e \times \mathbf{p}_\nu}{EE_\nu} \right] \right)$$

e-v-correlation

$$a = -0.103(4)$$

$\beta$ -asymmetry

$$A = -0.1173(13)$$

$\nu$ -asymmetry

$$B = 0.901(4)$$

triple correlation

$$D = -4(6) \cdot 10^{-4}$$

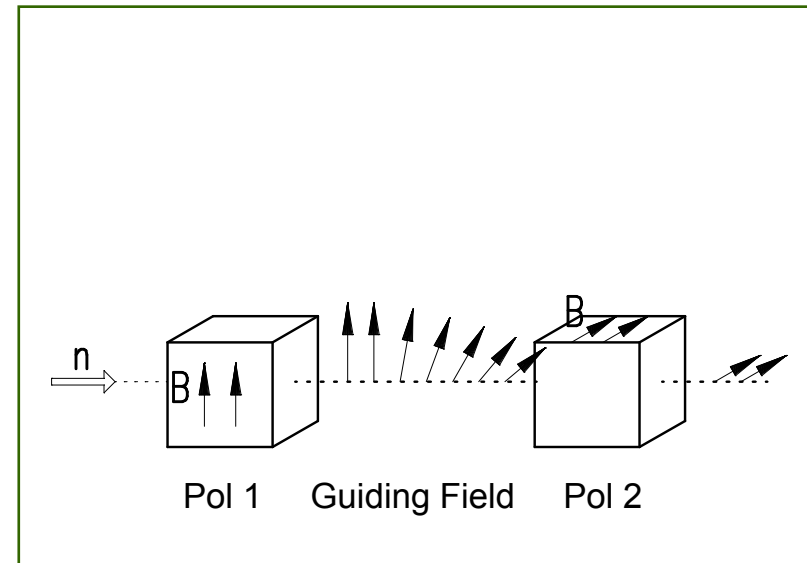
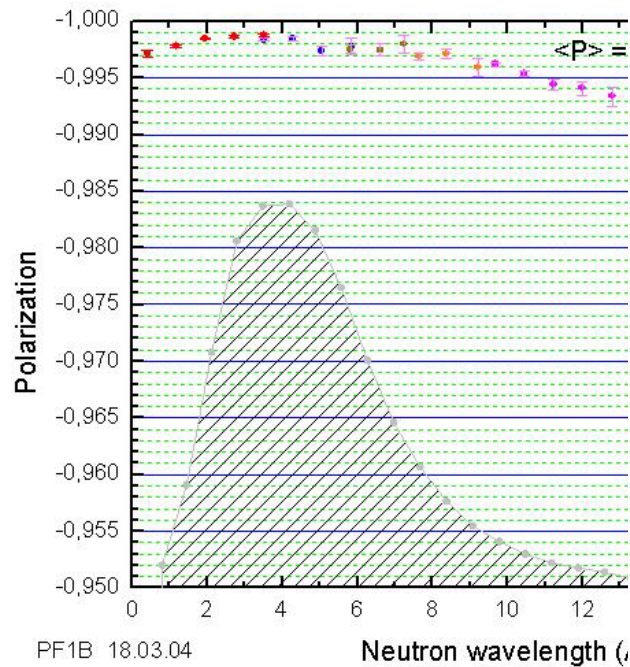
All values from PDG 2006

# Polarization

- **Polarization:** 2 supermirror-polarizers in „crossed-geometry“
- **Analysis:** 2 supermirror-analyzers and  $^3\text{He}$ -cells

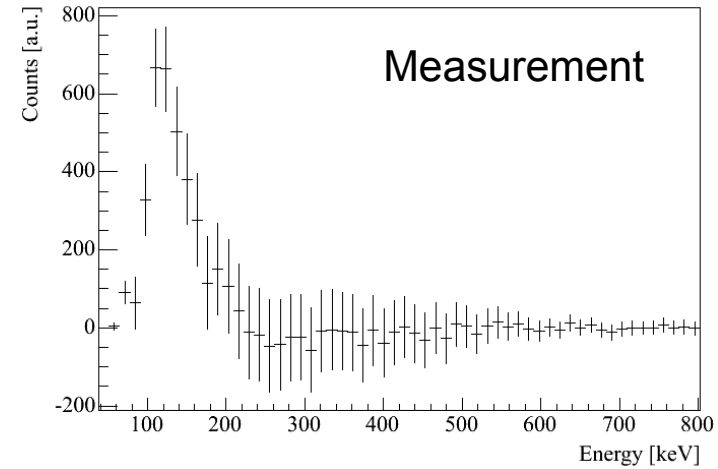
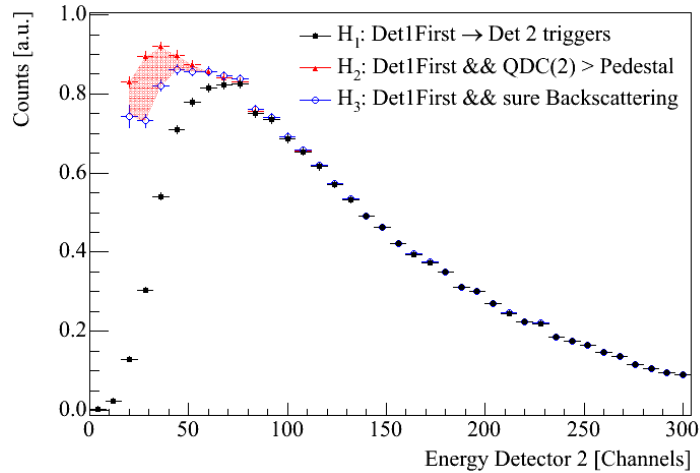
$P = (99.72 \pm 0.10) \% \quad F = (100.0 \pm 0.1) \%$

⇒ systematic error is considerably reduced



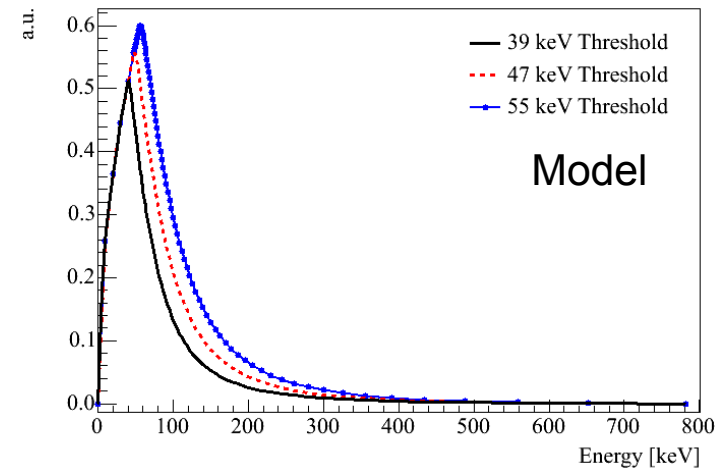


# Electron Backscattering



	total BS	wrong assignment
Det 1 First	4.9(2) %	0.15(4) %
Det 2 First	4.5(3) %	0.19(5) %

Backscattering effects are negligible above a threshold of 220 keV.

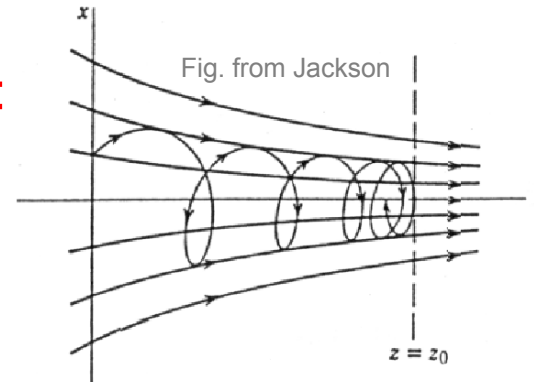




# B-n-Displacement

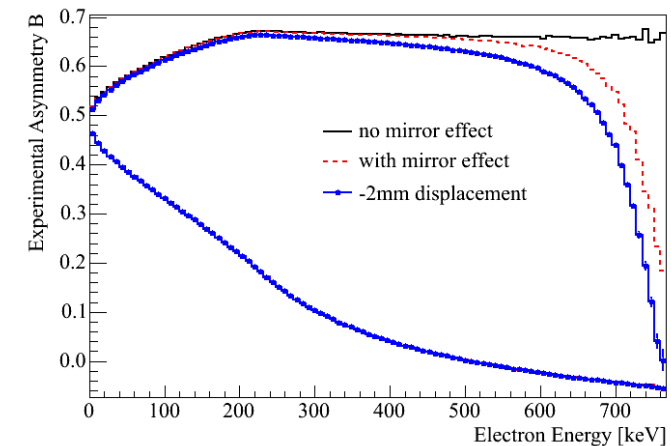
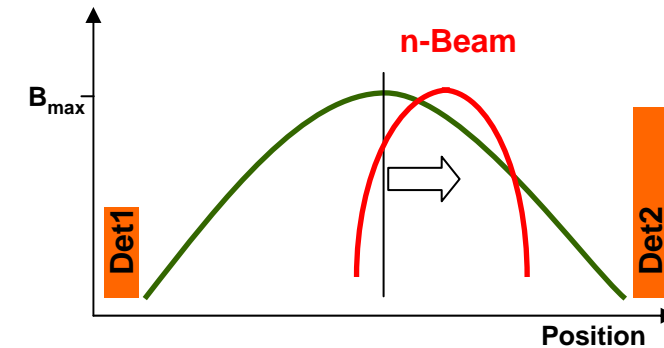
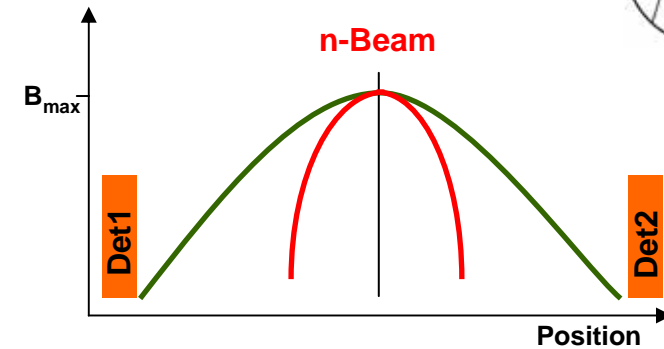
⇒ Changes count rates in detectors

**Magnetic  
Mirror Effect:**



⇒ Changes asymmetries

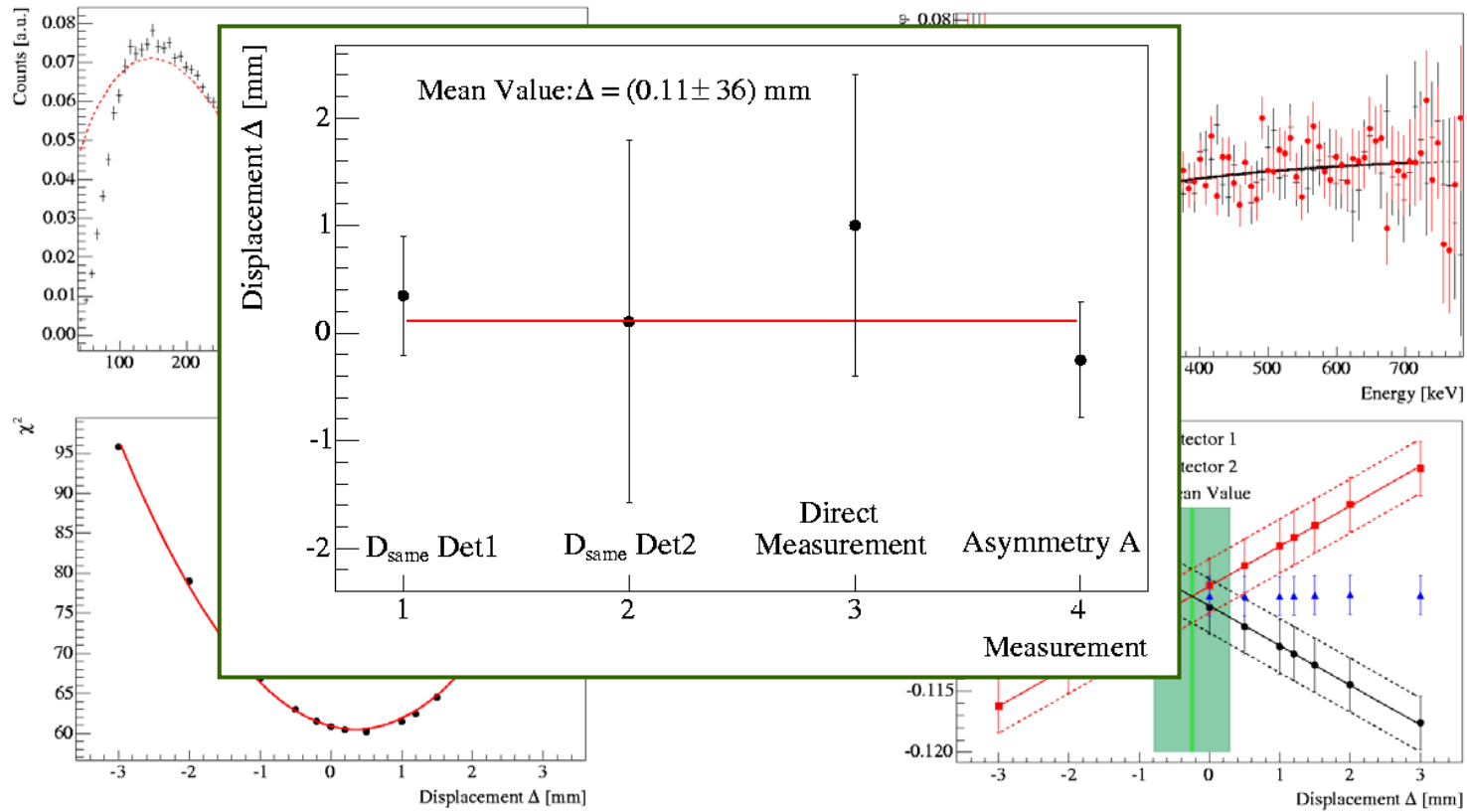
- Large effect on  $B$  (same hemisphere)
- Displacement cancels when asymmetry is averaged over two detectors
- we have only one good Detector!
- BUT: Determine  $\Delta$  from data!
- Corrections from MC-simulations





# Determination of Displacement

- 1) Direct Measurement
- 2)  $\chi^2$ -Minimization of Sum-Spectrum
- 3) Analysis of  $\beta$ -Asymmetry A

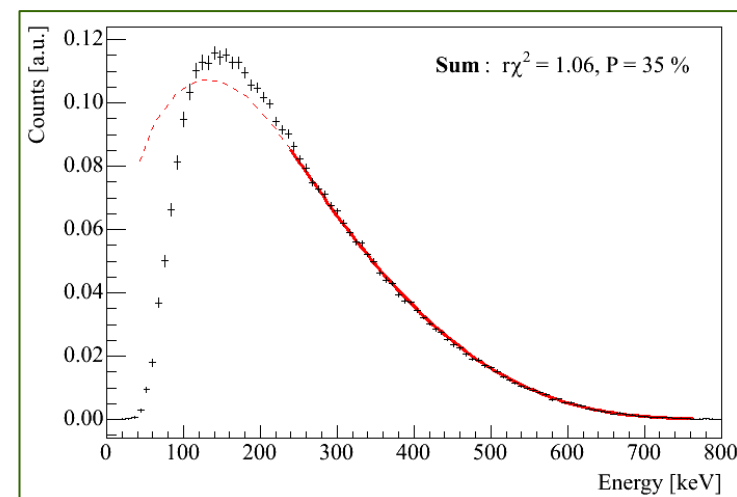
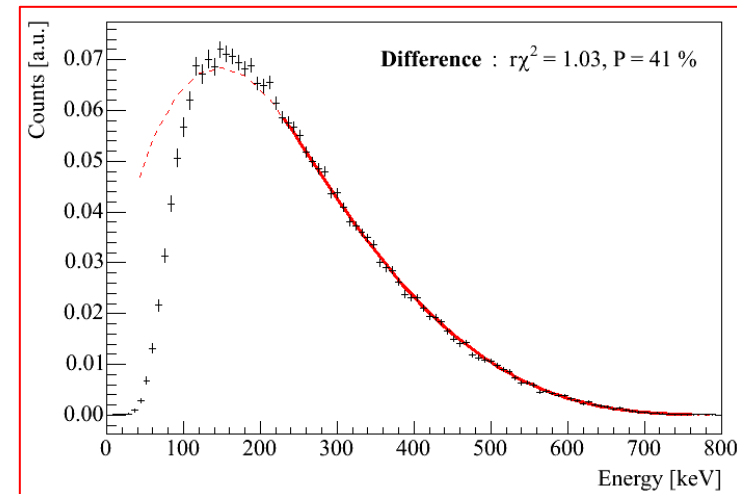


# Data Analysis

- Information available for analysis:
  - Electron Energy Spectra
  - Proton TOF
  - different detector combinations
  - Background measured and suppressed by coincidence
  - accidental coincidences measured
  - full  $e^-$  backscattering information

- $$B_{\text{same}}(E) = \frac{N^{\downarrow\downarrow}(E) - N^{\uparrow\uparrow}(E)}{N^{\downarrow\downarrow}(E) + N^{\uparrow\uparrow}(E)}$$

- 1 Parameter Fits!
- all spectra are well described above 240 keV





# Corrections and Errors: Asymmetry $B$

	Detector 1		Detector 2	
	Corr. [%]	Error [%]	Corr. [%]	Error [%]
Polarization	+0.3	0.1	+0.3	0.1
Flipper-Efficiency		0.1		0.1
<b>Statistics</b>		<b>1.22</b>		<b>0.36</b>
Coincidence Measurement	-0.29	0.07	-0.18	0.04
Detector		0.02		0.02
Systematics				
Mirror Effect	+0.44	0.05	+0.44	0.05
Displacement	-0.10	<b>0.32</b>	+0.10	<b>0.32</b>
Other	-0.13	0.07	-0.13	0.07
Other Coefficients		0.07		0.07
<b>Sum</b>	<b>+0.22</b>	<b>1.28</b>	<b>+0.53</b>	<b>0.52</b>

# Current Limits on right-handed Currents

PDG 2006

PDG gives no limit for  $\zeta$ !

## Limit on $W_L$ - $W_R$ Mixing Angle $\zeta$

Lighter mass eigenstate  $W_1 = W_L \cos \zeta - W_R \sin \zeta$ . Light  $\nu_R$  assumed unless noted. Values in brackets are from cosmological and astrophysical considerations.

VALUE	CL%	DOCUMENT ID	TECN	COMMENT
••• We do not use the following data for averages, fits, limits, etc. •••				
< 0.12	95	38 ACKERSTAFF 99D	OPAL	$\tau$ decay
< 0.013	90	39 CZAKON 99	RVUE	Electroweak
< 0.0333		40 BARENBOIM 97	RVUE	$\mu$ decay
< 0.04	90	41 MISHRA 92	CCFR	$\nu N$ scattering
-0.0006 to 0.0028	90	42 AQUINO 91	RVUE	
[none 0.00001-0.02]		43 BARBIERI 89B	ASTR	SN 1987A
< 0.040	90	44 JODIDIO 86	ELEC	$\mu$ decay
-0.056 to 0.040	90	44 JODIDIO 86	ELEC	$\mu$ decay

All limits depend heavily on assumptions!  
 $\Rightarrow$  Every new input is useful.

## $W_R$ (Right-Handed $W$ Boson) MASS LIMITS

Assuming a light right-handed neutrino, except for BEALL 82, LANGACKER 89B, and COLANGELO 91.  $g_R = g_L$  assumed. [Limits in the section MASS LIMITS for  $W'$  below are also valid for  $W_R$  if  $m_{\nu_R} \ll m_{W_R}$ .] Some limits assume manifest left-right symmetry, i.e., the equality of left- and right Cabibbo-Kobayashi-Maskawa matrices. For a comprehensive review, see LANGACKER 89B. Limits on the  $W_L$ - $W_R$  mixing angle  $\zeta$  are found in the next section. Values in brackets are from cosmological and astrophysical considerations and assume a light right-handed neutrino.

VALUE (GeV)	CL%	DOCUMENT ID	TECN	COMMENT
> 715	90	13 CZAKON 99	RVUE	Electroweak
••• We do not use the following data for averages, fits, limits, etc. •••				
[> 3300]	95	14 CYBURT 05	COSM	Nucleosynthesis; light $\nu_R$
> 310	90	15 THOMAS 01	CNTR	$\beta^+$ decay
> 137	95	16 ACKERSTAFF 99D	OPAL	$\tau$ decay
>1400	68	17 BARENBOIM 98	RVUE	Electroweak, Z-Z' mixing
> 549	68	18 BARENBOIM 97	RVUE	$\mu$ decay
> 220	95	19 STAHL 97	RVUE	$\tau$ decay
> 220	90	20 ALLET 96	CNTR	$\beta^+$ decay
> 281	90	21 KUZNETSOV 95	CNTR	Polarized neutron decay
> 282	90	22 KUZNETSOV 94B	CNTR	Polarized neutron decay
> 439	90	23 BHATTACH... 93	RVUE	Z-Z' mixing
> 250	90	24 SEVERIJNS 93	CNTR	$\beta^+$ decay

## MASS LIMITS for $W'$ (Heavy Charged Vector Boson Other Than $W$ ) in Hadron Collider Experiments

Couplings of  $W'$  to quarks and leptons are taken to be identical with those of  $W$ . The following limits are obtained from  $p\bar{p} \rightarrow W'X$  with  $W'$  decaying to the mode indicated in the comments. New decay channels (e.g.,  $W' \rightarrow WZ$ ) are assumed to be suppressed. UA1 and UA2 experiments assume that the  $t\bar{b}$  channel is not open.

VALUE (GeV)	CL%	DOCUMENT ID	TECN	COMMENT
>800	95	ABAZOV 04C	D0	$W' \rightarrow q\bar{q}$
••• We do not use the following data for averages, fits, limits, etc. •••				
225-536	95	1 ACOSTA 03B	CDF	$W' \rightarrow t\bar{b}$
none 200-480	95	2 AFFOLDER 02C	CDF	$W' \rightarrow WZ$
>786	95	3 AFFOLDER 01I	CDF	$W' \rightarrow e\nu, \mu\nu$
>660	95	4 ABE 00	CDF	$W' \rightarrow \mu\nu$
none 300-420	95	5 ABE 97G	CDF	$W' \rightarrow q\bar{q}$
>720	95	6 ABACHI 96C	D0	$W' \rightarrow e\nu$
>610	95	7 ABACHI 95E	D0	$W' \rightarrow e\nu, \tau\nu$
>652	95	8 ABE 95M	CDF	$W' \rightarrow e\nu$
>251	90	9 ALITTI 93	UA2	$W' \rightarrow q\bar{q}$
none 260-600	95	10 RIZZO 93	RVUE	$W' \rightarrow q\bar{q}$
>220	90	11 ALBAJAR 89	UA1	$W' \rightarrow e\nu$
>209	90	12 ANSARI 87D	UA2	$W' \rightarrow e\nu$

<sup>1</sup> The ACOSTA 03B quoted limit is for  $M_{W'} \gg M_{\nu_R}$ . For  $M_{W'} < M_{\nu_R}$ ,  $M_{W'}$  between 225 and 566 GeV is excluded.

<sup>2</sup> The quoted limit is obtained assuming  $W'WZ$  coupling strength is the same as the ordinary  $WWZ$  coupling strength in the Standard Model. See their Fig. 2 for the limits on the production cross sections as a function of the  $W'$  width.