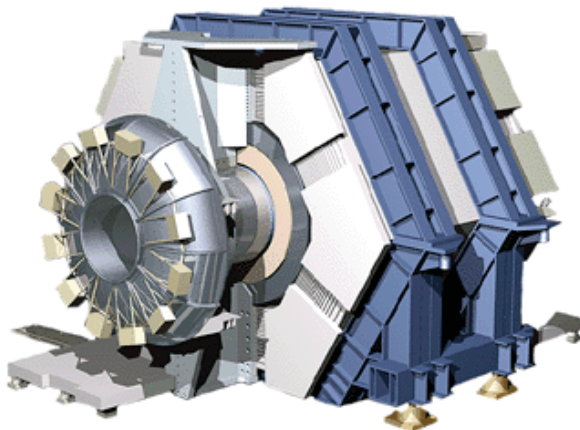


# SemiLeptonic B decays at the B factories

Roberto Sacco

on behalf of the BaBar and Belle Collaborations

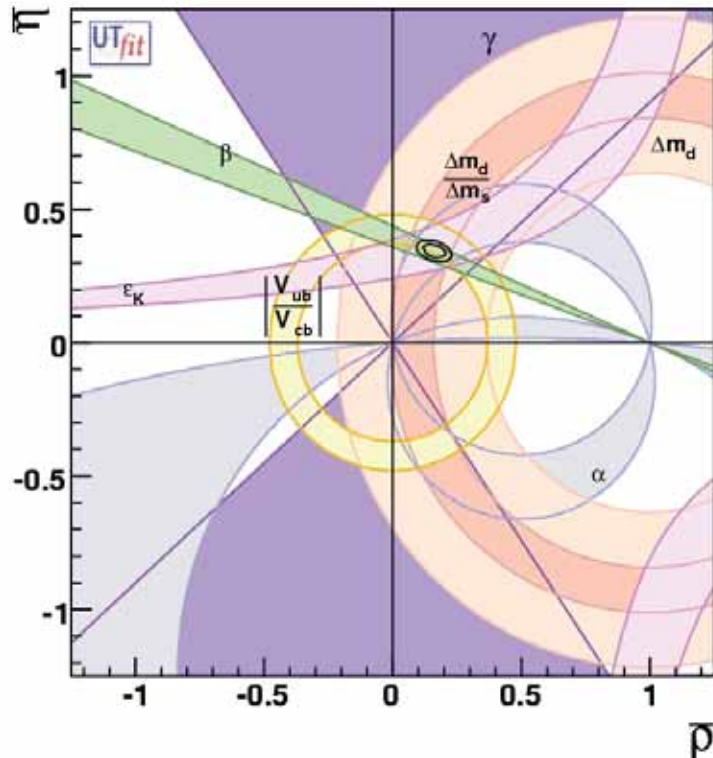
XLII Rencontres de Moriond, 10-17th March 2007, La Thuile, Italy



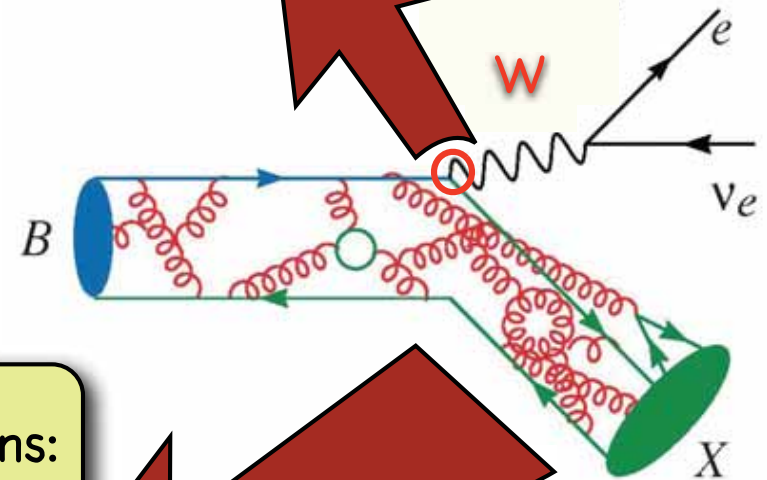
Queen Mary  
University of London

# Why SemiLeptonic decays?

Tree level decays where we can disentangle leptonic and hadronic currents - many theoretical developments in recent years



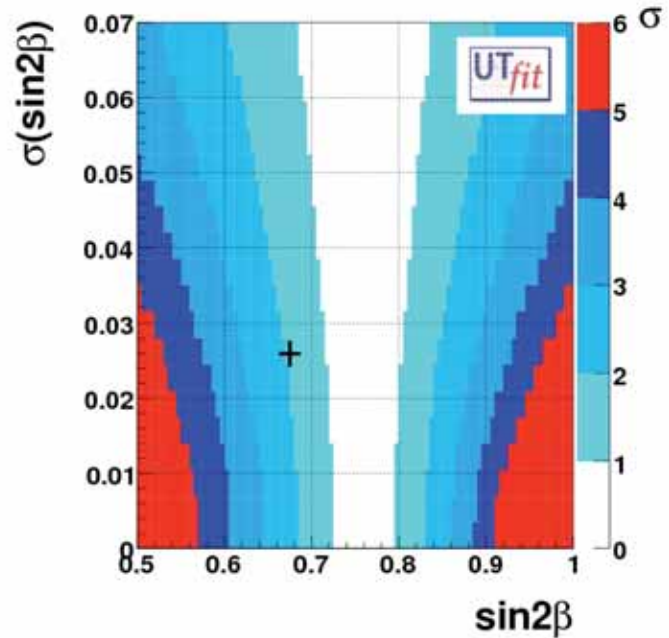
Sensitive to quark couplings to W  
 $\Rightarrow$  decay rate depends on  $|V_{ub}|$  and  $|V_{cb}|$   
 $\Rightarrow$  check SM predictions



Good tool to probe the structure of B mesons:

- $\Rightarrow$  inclusive decays: OPE, b & c quark mass
- $\Rightarrow$  exclusive decays: form factors

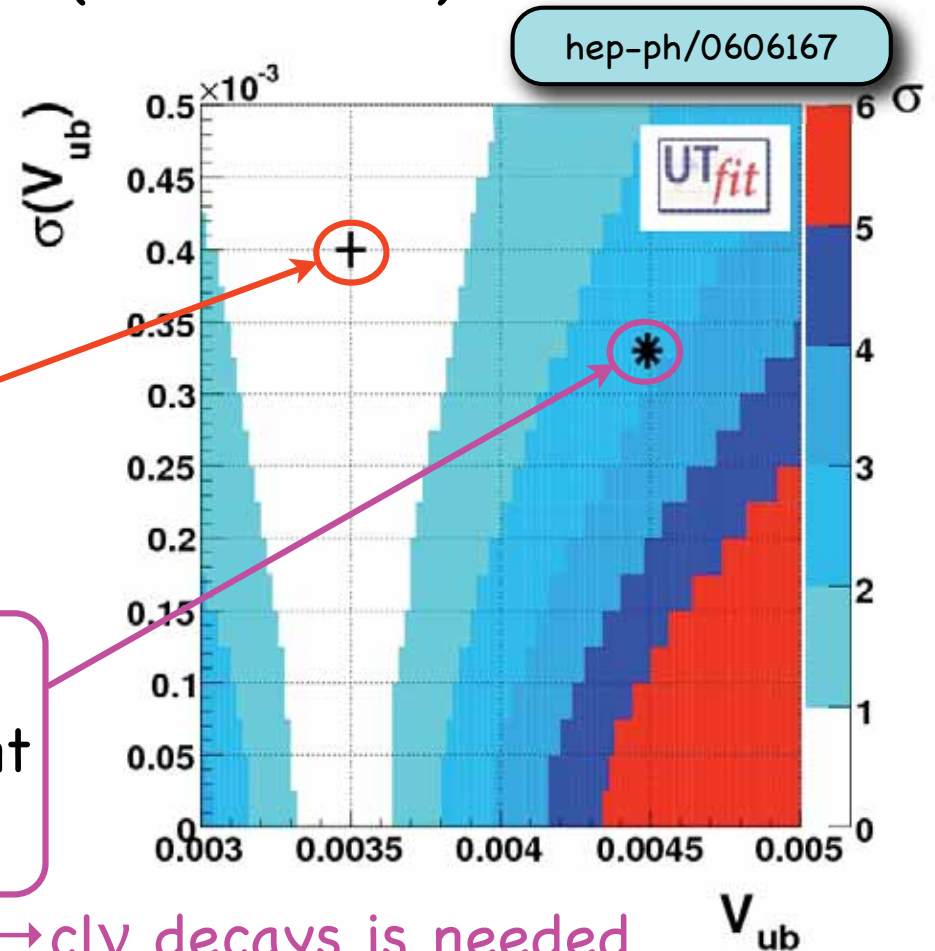
# The $|V_{ub}|$ puzzle



almost  $2\sigma$  difference between direct measurement of  $\sin 2\beta$  ( $0.674 \pm 0.026$ ) and the rest of the fit ( $0.755 \pm 0.040$ )

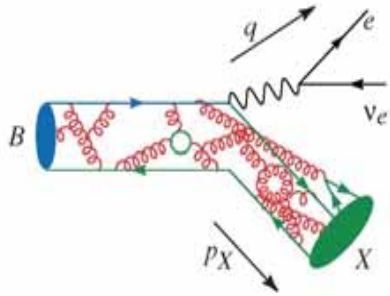
exclusive measurements  
(require knowledge of FFs from LQCD and QCDSR)

inclusive measurements  
(require knowledge of model-dependent non-perturbative parameters)



➡ better description of  $b \rightarrow clv$  decays is needed

# HQE parameters determination



fit to hadronic  
mass moments in  
 $B \rightarrow X_{cl\nu}$

fit to lepton  
energy moments in  
 $B \rightarrow X_{cl\nu}$

$$\Gamma_{cl\nu} = \frac{G_F m_b^5}{192\pi^3} |V_{cb}|^2 (1 + A_{ew}) A_{\text{pert}} A_{\text{nonpert}} \simeq |V_{cb}|^2 f_{\text{OPE}}(m_b, m_c, a_i)$$

fit to photon  
energy moments in  
 $B \rightarrow X_s \gamma$

## Kinetic Scheme

P. Gambino and N.Uraltsev, Eur.  
Phys. J. C34, 181 (2004)

## 1S Scheme

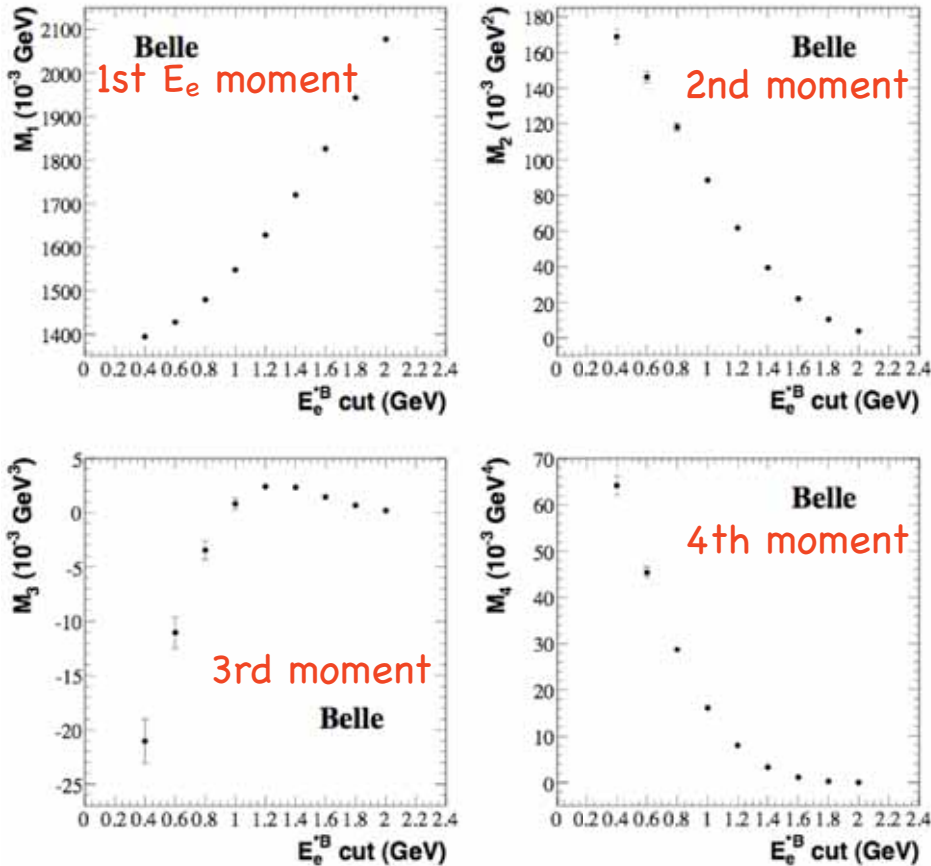
C.Bauer, Z.Ligeti, M.Luke, A.Manohar,  
M.Trott PRD 70 094017

# $E_e$ spectrum moments

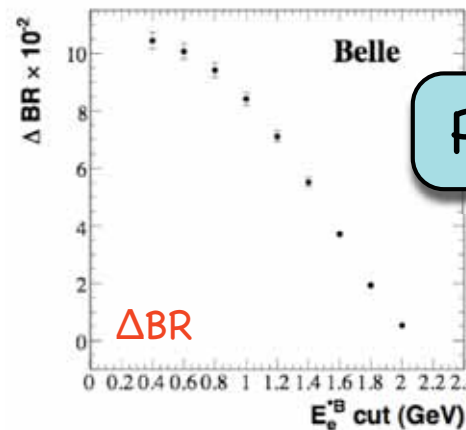
Experimental results:

BaBar: Phys. Rev. D69 111104 (2004), CLEO: Phys. Rev. D70 032003 (2004), DELPHI: Eur. Phys. J. C45, 35 (2006)

Most recent: from Belle collaboration on  $140 \text{ fb}^{-1}$



First four moments with threshold values for  $E_e$  from 0.4 to 2 GeV (correlations between measurements are included)



PRD75 032001 (2007)

$$BR(B^+)_{0.4\text{GeV}} = (10.79 \pm 0.25 \pm 0.27) 10^{-3}$$

$$BR(B^0)_{0.4\text{GeV}} = (10.08 \pm 0.30 \pm 0.22) 10^{-3}$$

# Hadronic mass spectrum moments

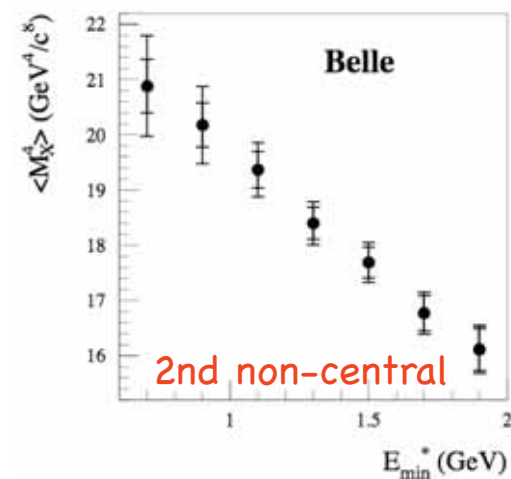
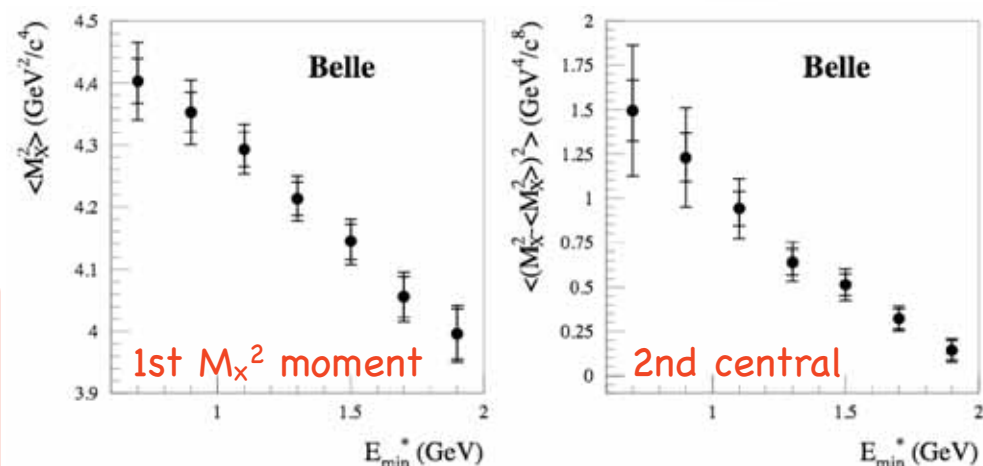
## Experimental results:

BaBar: Phys. Rev. D69 111103 (2004), CDF: Phys. Rev. D71 051103 (2005),  
CLEO: Phys. Rev. D70 032002 (2004), DELPHI: Eur. Phys. J. C45, 35 (2006)

Most recent: from Belle collaboration on  $140 \text{ fb}^{-1}$

PRD75 032005 (2007)

First, second central and second non-central moments with threshold values for  $E_e$  from 0.7 to 1.9 GeV  
(correlations between measurements are included)



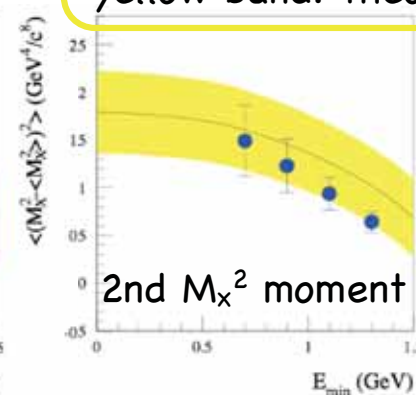
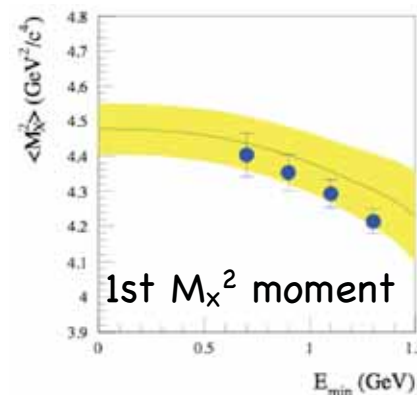
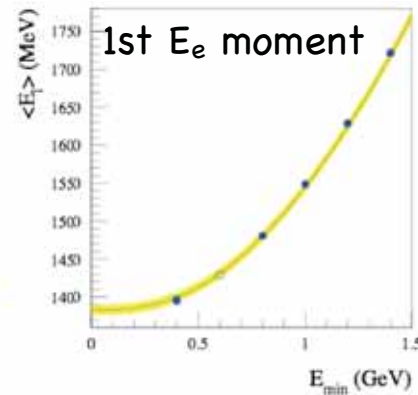
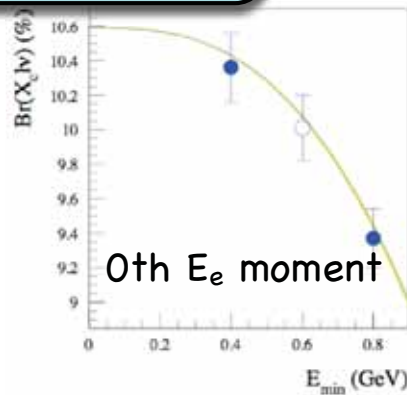
# HQE parameters and $|V_{cb}|$ : Kinetic Scheme

Spectral moments derived up to  $O(1/m_b^3)$ : determine 7 parameters

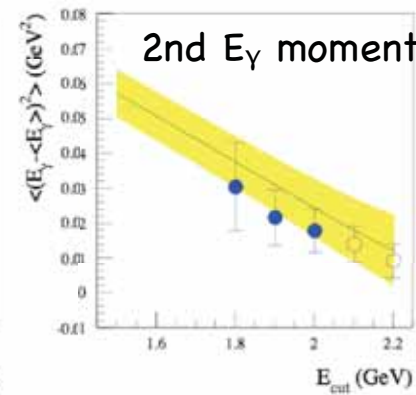
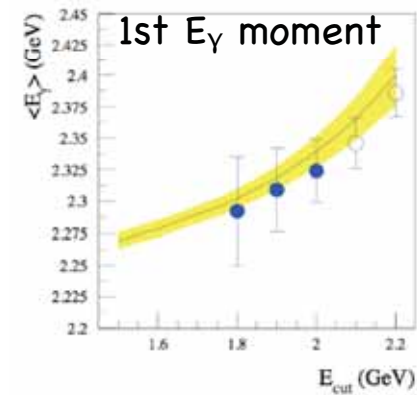
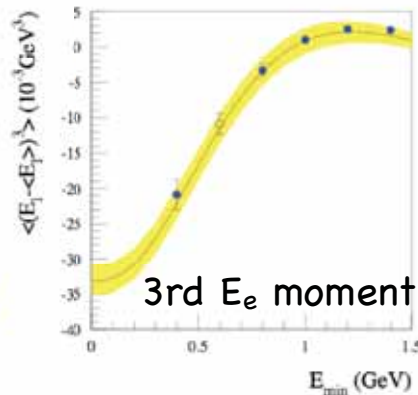
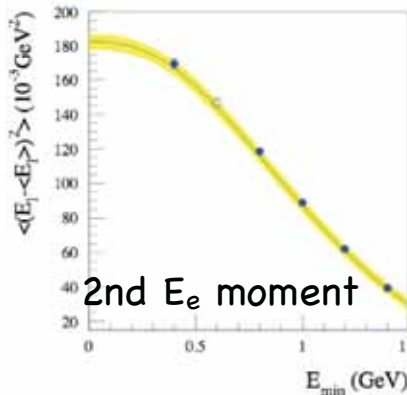
$$\text{BF}(B \rightarrow X_c l \nu), m_b, m_c, \mu_\pi^2, \rho_D^3, \mu_G^2, \rho_{LS}^3$$

$|V_{cb}|$  treated as 8th free parameter, related to SL width

hep-ex/0611047



yellow band: theory error



Belle fit 71 of their measured moments (including  $B \rightarrow X_s \gamma$ , hep-ex/0508005) taking into account experimental and theoretical uncertainties

# HQE parameters and $|V_{cb}|$ : Kinetic Scheme

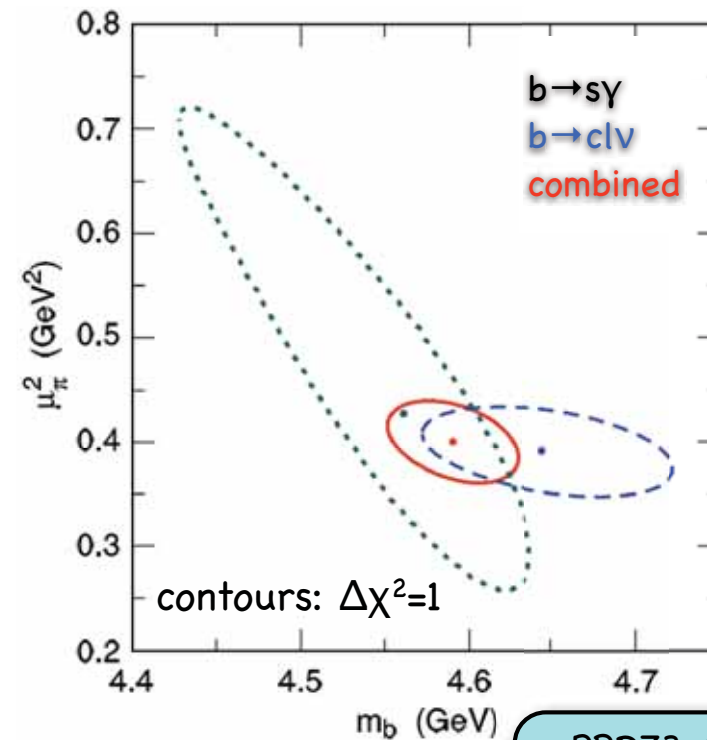
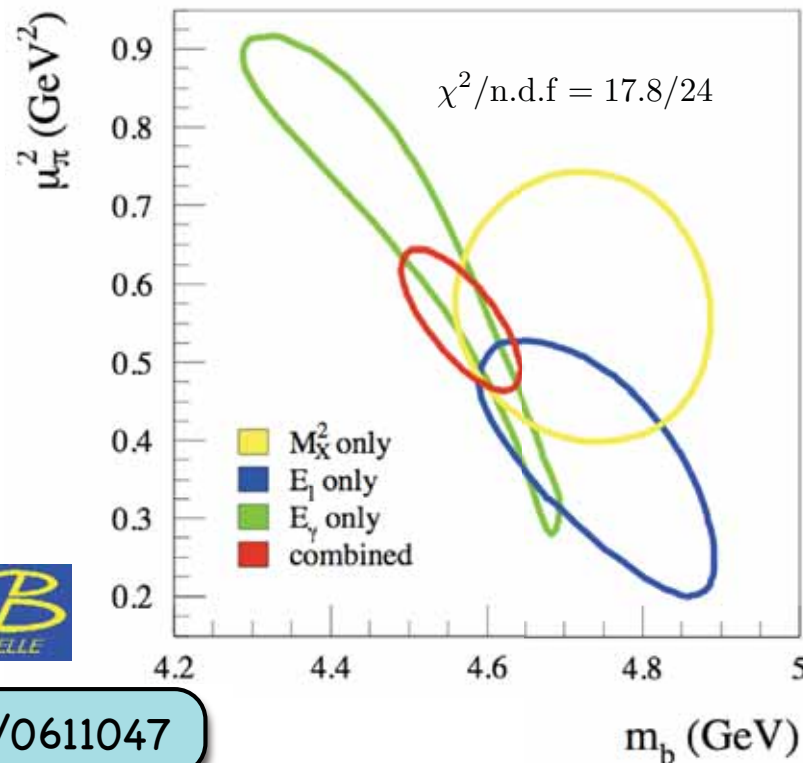
## Results

$$|V_{cb}| = (41.93 \pm 0.65_{\text{fit}} \pm 0.07_{\alpha_s} \pm 0.63_{\text{th}}) 10^{-3}$$

$$m_b = 4.564 \pm 0.076_{\text{fit}} \pm 0.003_{\alpha_s} \text{ GeV}$$

$$m_c = 1.105 \pm 0.116_{\text{fit}} \pm 0.005_{\alpha_s} \text{ GeV}$$

$$\text{BR}_{\text{clv}} = 10.590 \pm 0.164_{\text{fit}} \pm 0.006_{\alpha_s} \%$$



hep-ex/0611047

PRD73, 073008 (2006)

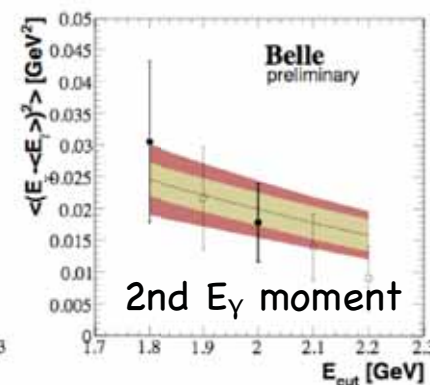
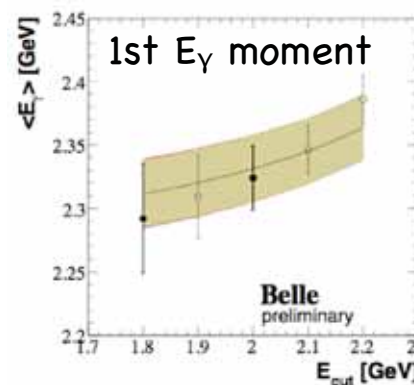
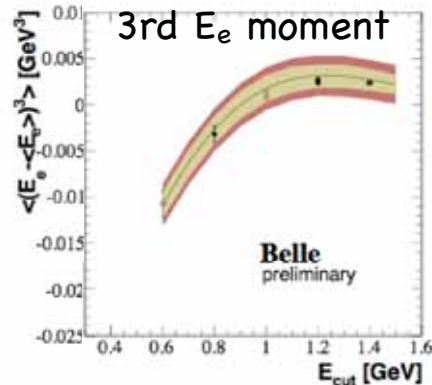
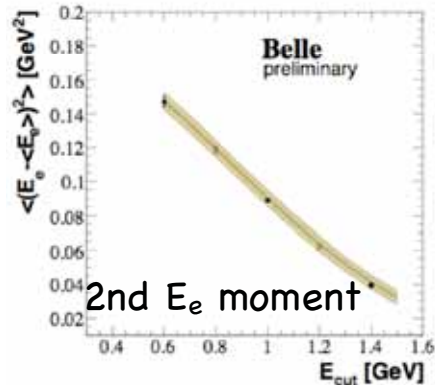
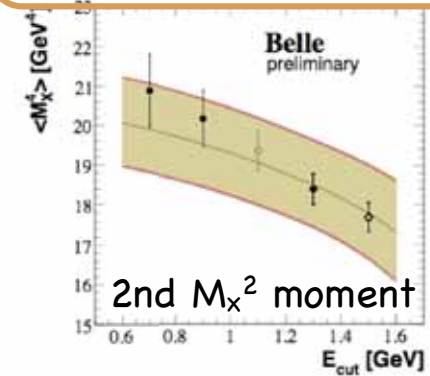
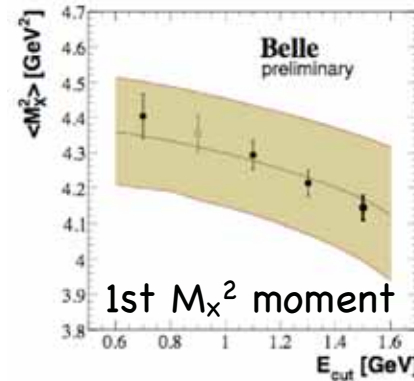
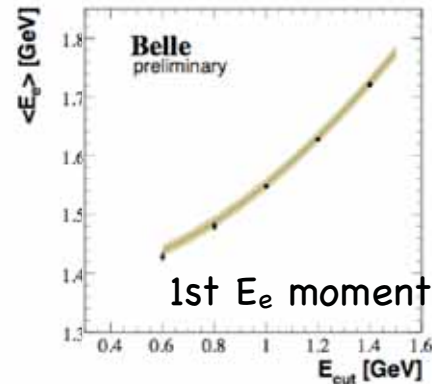
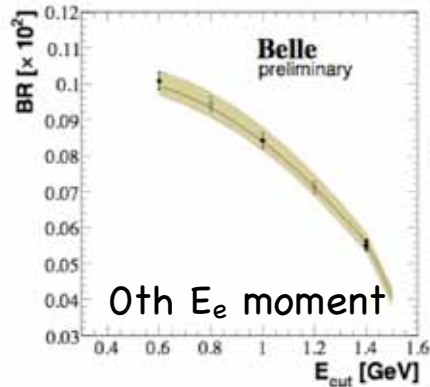


# HQE parameters and $|V_{cb}|$ : 1S Scheme

Truncated moments derived up to  $O(1/m_b^3)$

7 parameters can be determined with a  $\chi^2$  fit to moments:  $|V_{cb}|$ ,  $\Lambda$ ,  $\lambda_1$ ,  $\tau_1$ ,  $\tau_2$ ,  $\tau_3$ ,  $\rho_1$

brown band: theory error



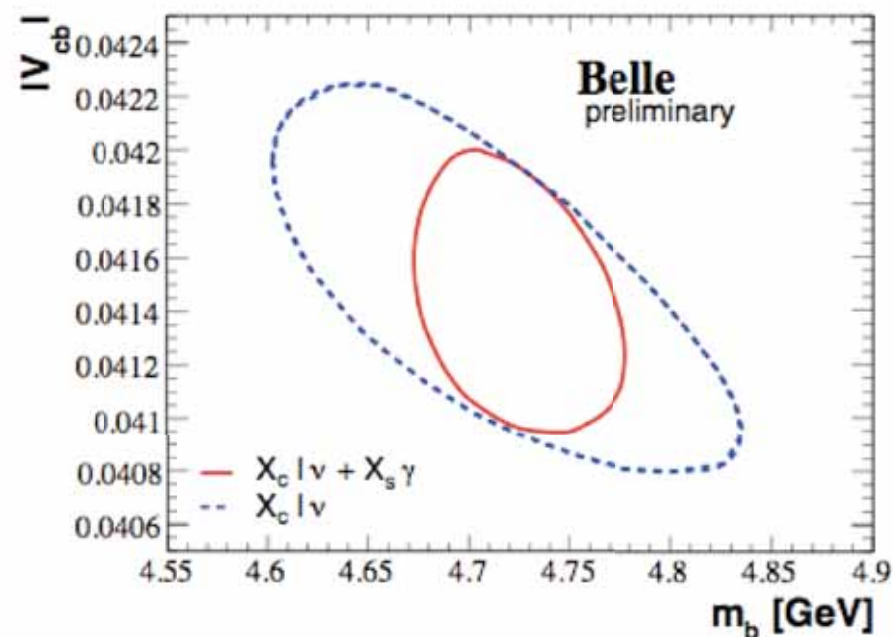
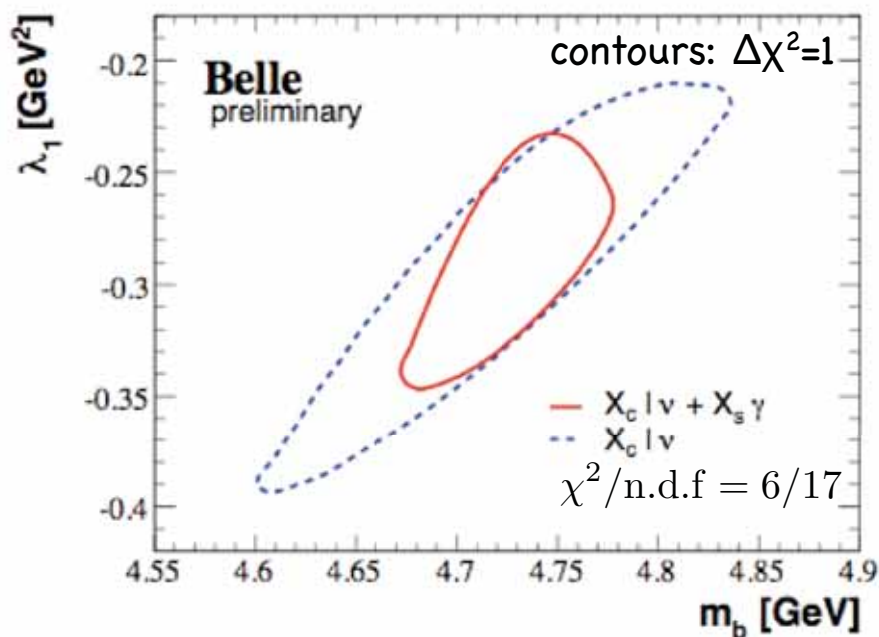
Belle fit 71 of their measured moments (including  $B \rightarrow X_s \gamma$ , hep-ex/0508005) taking into account experimental and theoretical uncertainties

# HQE parameters and $|V_{cb}|$ : 1S Scheme

$$\Lambda = m_{\Upsilon(1S)}/2 - m_b^{1S}$$

## Results

$$|V_{cb}| = (41.49 \pm 0.52_{\text{fit}} \pm 0.20_{\text{TB}}) 10^{-3}$$
$$m_b^{1S} = 4.729 \pm 0.048 \text{ GeV}$$
$$\lambda_1 = -0.30 \pm 0.04 \text{ GeV}^2$$



hep-ex/0611047

# HQE parameters from moments: conclusions

$$|V_{cb}| \text{ - Kinetic Scheme: } (41.93 \pm 0.65_{\text{fit}} \pm 0.07_{\alpha_s} \pm 0.63_{\text{th}}) 10^{-3}$$

$$|V_{cb}| \text{ - 1S Scheme: } (41.49 \pm 0.52_{\text{fit}} \pm 0.20_{\text{TB}}) 10^{-3}$$

Good agreement with measurements done using different data samples  
(BaBar, CLEO, CDF, DELPHI):

$$|V_{cb}| \text{ - Kinetic Scheme: } (41.96 \pm 0.23 \pm 0.35 \pm 0.59) 10^{-3}$$

Good agreement for other HQE parameters as well

O. Buchmüller and H. Flächer,  
PRD73, 073008 (2006)

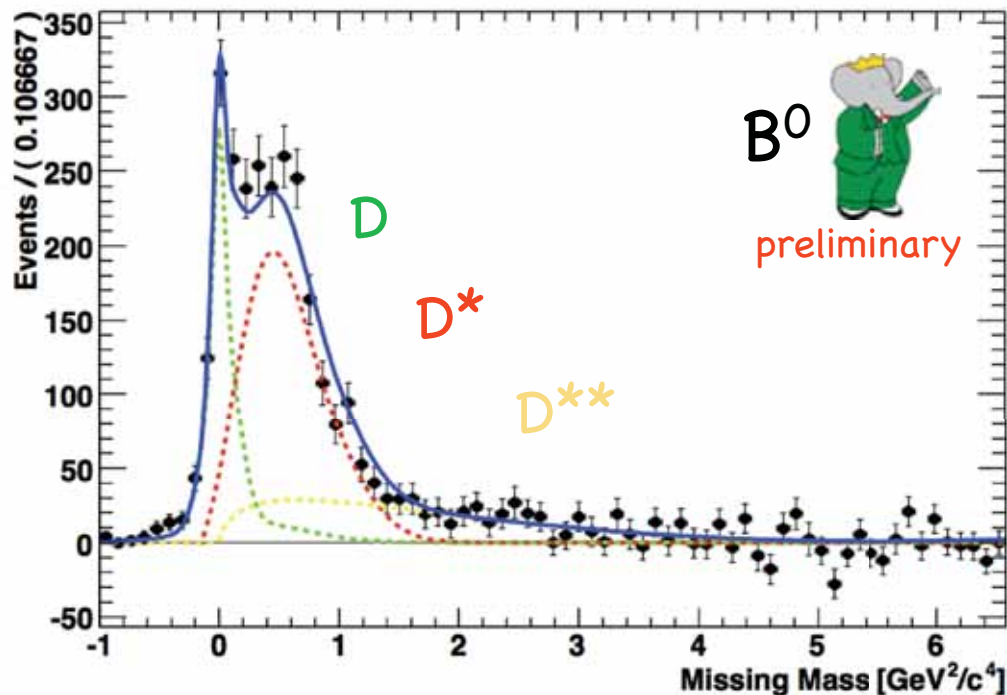
$|V_{cb}|$  measured at <2%

# Relative BFs for $B \rightarrow D/D^*/D^{**}l\nu$

Event selection: reconstruct  $D+l$  ( $p_{lep} > 0.6$  GeV/c) system, then  
fully reconstruct non-overlapping hadronic tag

Measure simultaneously  $D$ ,  $D^*$ ,  $D^{**}$  components using a global fit  
to lepton momentum, missing mass squared and additional  
charged particle multiplicity distributions

Missing Mass Fit



PDFs are built using  
exclusive  $D^{(*)}(\pi)l\nu$  data  
samples (minimize MC  
dependence and limited  
knowledge of  $D^{**}$  states)

# Relative BFs for $B \rightarrow D/D^*/D^{**}l\nu$

On  $340 \text{ fb}^{-1}$  BaBar measures:



**NEW!**

preliminary

| Ratio  | $B^-$ (%)              | $B^0$ (%)              |
|--|------------------------|------------------------|
| $\frac{\Gamma(B \rightarrow D l \bar{\nu}_\ell)}{\Gamma(B \rightarrow D X l \bar{\nu}_\ell)}$      | $22.7 \pm 1.4 \pm 1.6$ | $21.5 \pm 1.6 \pm 1.3$ |
| $\frac{\Gamma(B \rightarrow D^* l \bar{\nu}_\ell)}{\Gamma(B \rightarrow D X l \bar{\nu}_\ell)}$    | $58.2 \pm 1.8 \pm 3.0$ | $53.7 \pm 3.1 \pm 3.6$ |
| $\frac{\Gamma(B \rightarrow D^{**} l \bar{\nu}_\ell)}{\Gamma(B \rightarrow D X l \bar{\nu}_\ell)}$ | $19.1 \pm 1.3 \pm 1.9$ | $24.8 \pm 3.2 \pm 3.0$ |

|  |                             |
|--|-----------------------------|
| $\text{BF}(B \rightarrow D^0 l \nu)$     | $2.42 \pm 0.15 \pm 0.17 \%$ |
| $\text{BF}(B \rightarrow D^{*0} l \nu)$  | $6.20 \pm 0.19 \pm 0.32 \%$ |
| $\text{BF}(B \rightarrow D^{**0} l \nu)$ | $2.04 \pm 0.14 \pm 0.20 \%$ |
| $\text{BF}(B \rightarrow D^+ l \nu)$     | $2.19 \pm 0.16 \pm 0.13 \%$ |
| $\text{BF}(B \rightarrow D^{*+} l \nu)$  | $5.46 \pm 0.33 \pm 0.37 \%$ |
| $\text{BF}(B \rightarrow D^{**+} l \nu)$ | $2.52 \pm 0.32 \pm 0.31 \%$ |



Precision comparable  
to the current world  
knowledge of  
 $B \rightarrow D/D^*/D^{**}l\nu$  decays

Important input to all the analysis relying on accurate  
description of  $D/D^*/D^{**}$  hadronic mass region

BaBar has also a preliminary result on  $D^{**}$  narrow resonances

# $|V_{cb}|$ from $B^0 \rightarrow D^* \ell^+ \nu$

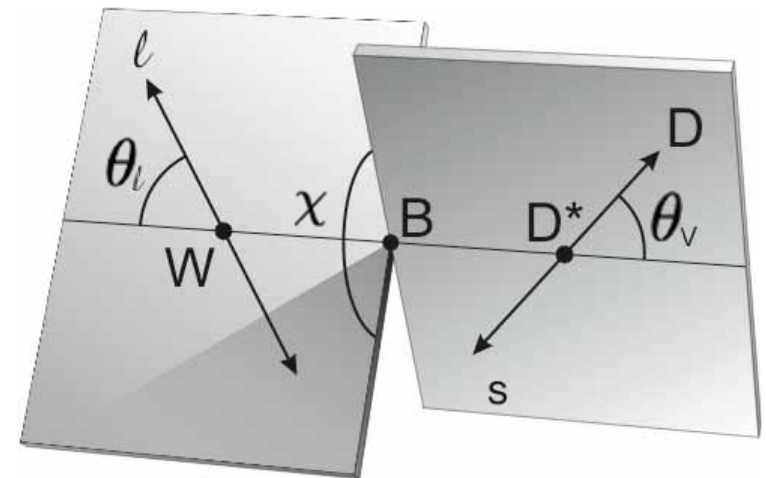
$$\frac{d\Gamma(B \rightarrow D^* \ell \nu)}{dq^2 d \cos \theta_\ell d \cos \theta_V d\chi} = \frac{G_F^2 |V_{cb}|^2}{48\pi^3} \mathcal{F}(w, \theta_\ell, \theta_V, \chi) \mathcal{G}(w)$$

w:  $D^*$  boost

expressed in terms of helicity amplitudes ( $D^*$  polarization)



expressed, in turn, by form factor ratios  $R_1, R_2$  and the slope  $h_{A_1}$  à la Caprini, Lellouch, Neubert



$$h_{A_1}(w) = h_{A_1}(1) [1 - \rho_{h_{A_1}}^2 z + (53\rho_{h_{A_1}}^2 - 15)z^2 - (231\rho_{h_{A_1}}^2 - 91)z^3]$$

$$z = \frac{\sqrt{w+1} - \sqrt{2}}{\sqrt{w+1} + \sqrt{2}}$$

# $|V_{cb}|$ from $B^0 \rightarrow D^{*-} l^+ \nu$

On  $79\text{fb}^{-1}$ , select  $D^{*-} l^+ \nu$  events, with  
 $p_{\text{lep}} > 1.2 \text{ GeV}/c$ ,  $D^{*-} \rightarrow D^0 \pi^-$   
 $D^0 \rightarrow K\pi, K\pi\pi^0, K\pi\pi\pi$

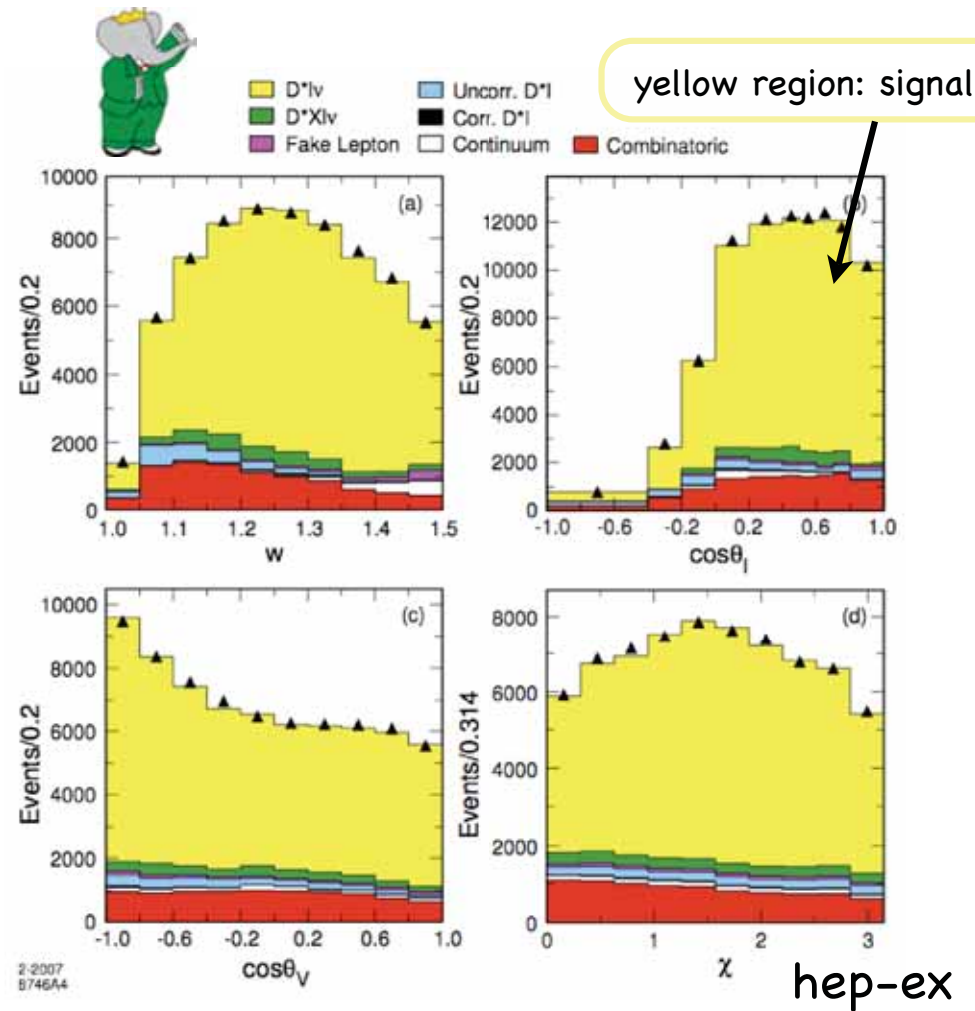
Data sample is divided in 10 bins of  
 $w$ ,  $\cos\theta_l$ ,  $\cos\theta_\nu$  and a combined  
 least  $\chi^2$  fit is performed

combine this result with Phys. Rev. D74  
 (2006) 092004 to obtain:

$$R_1 = 1.417 \pm 0.061 \pm 0.044$$

$$R_2 = 0.836 \pm 0.037 \pm 0.022$$

$$\rho^2 = 1.179 \pm 0.048 \pm 0.028$$

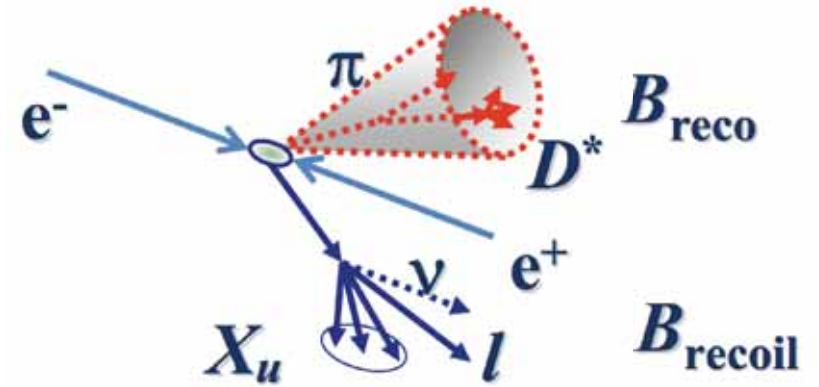


Using  $F(1) = 0.919^{+0.030}_{-0.035}$  estimate [Hashimoto et al, PRD 66 (2002) 014503]:

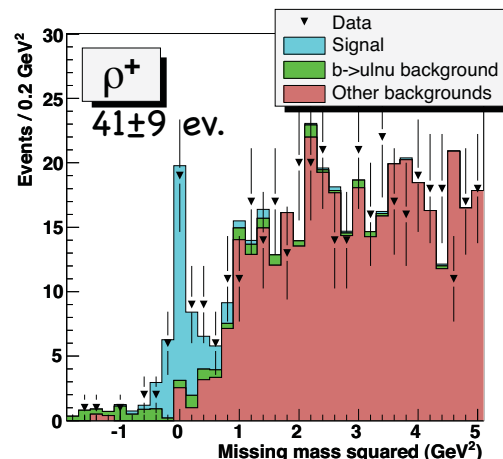
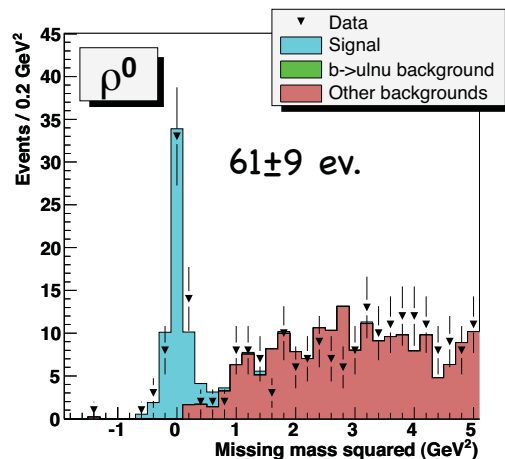
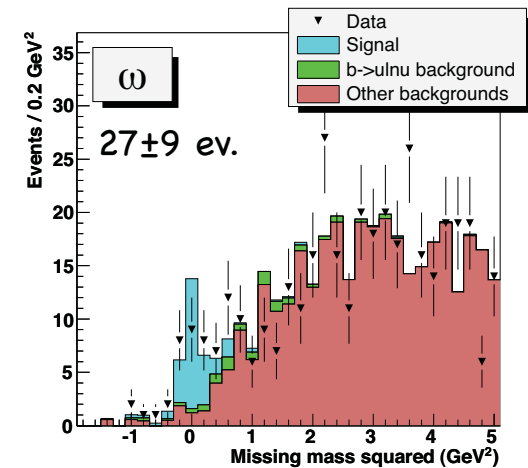
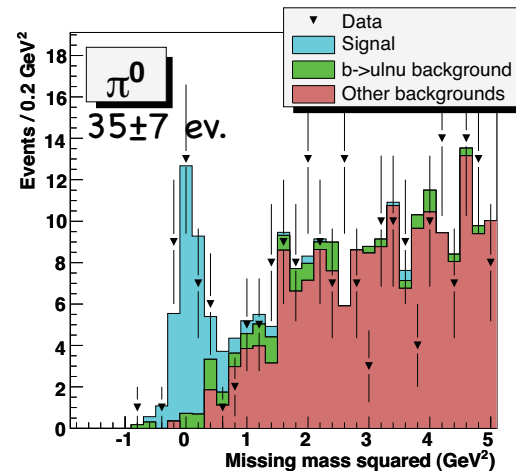
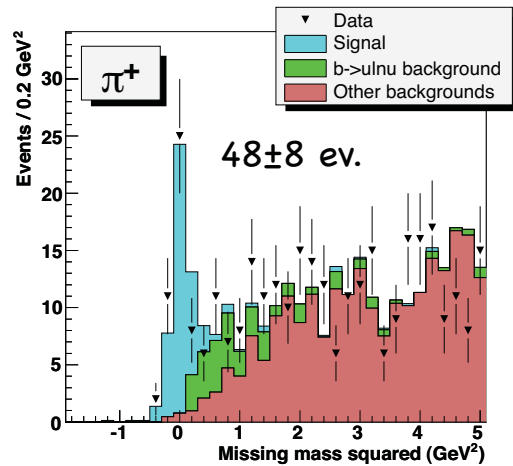
$$|V_{cb}| = (37.74 \pm 0.35_{\text{stat}} \pm 1.25_{\text{syst}} {}^{+1.23}_{-1.44}{}_{\text{th}}) 10^{-3}$$

# BRs for exclusive $B \rightarrow X_u l \nu$ decays

**Recoil technique**  
highest S/B ratio, low efficiencies



535M  $B\bar{B}$  pairs



hep-ex/0610054

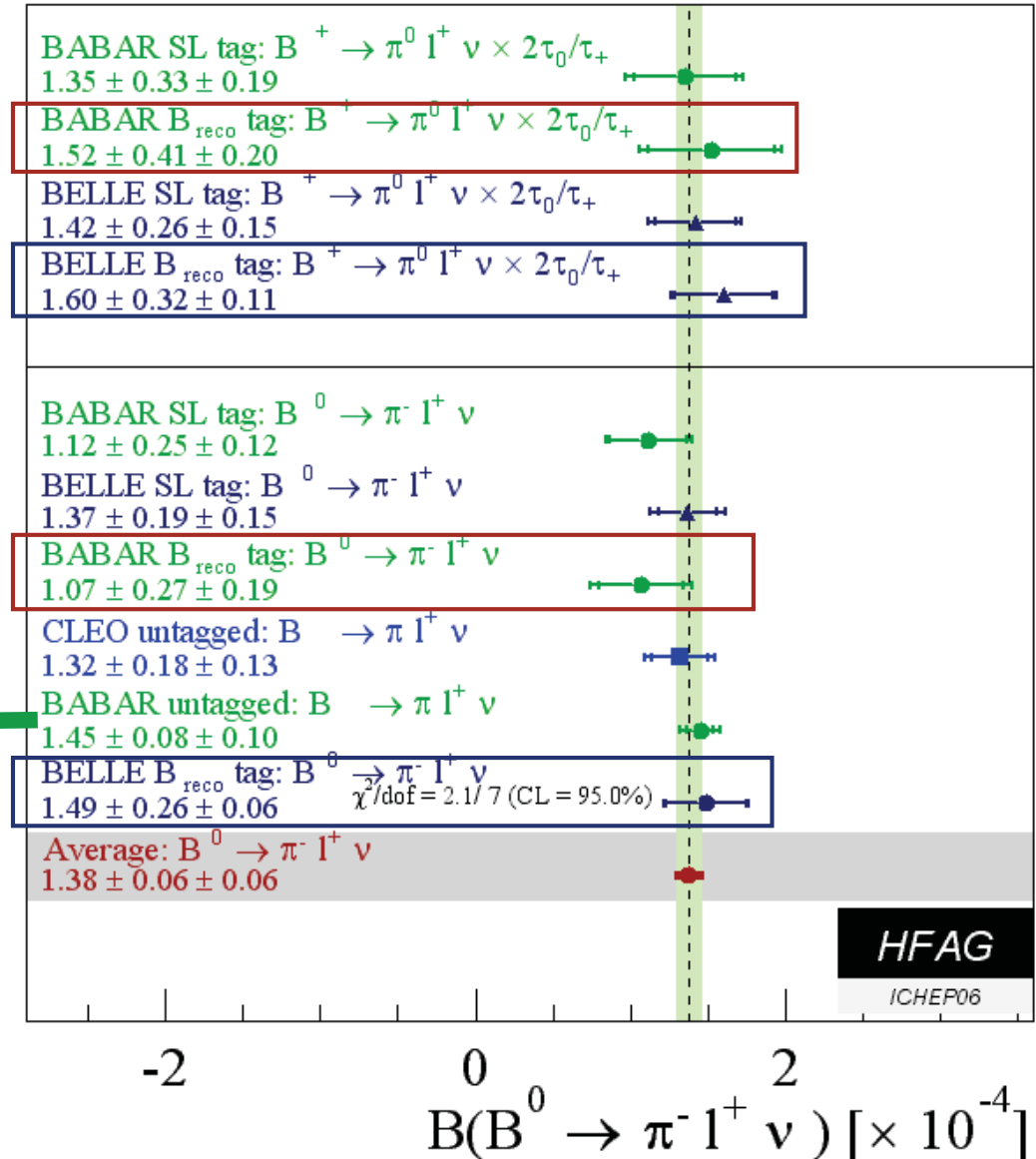
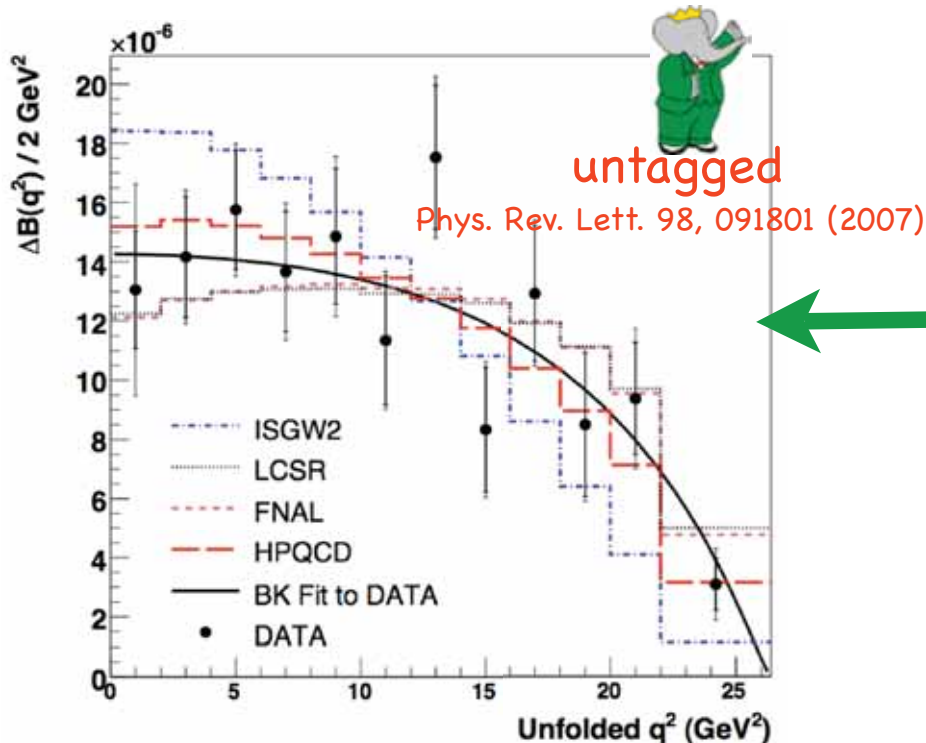


# BRs for exclusive $B \rightarrow X_u l \nu$ decays

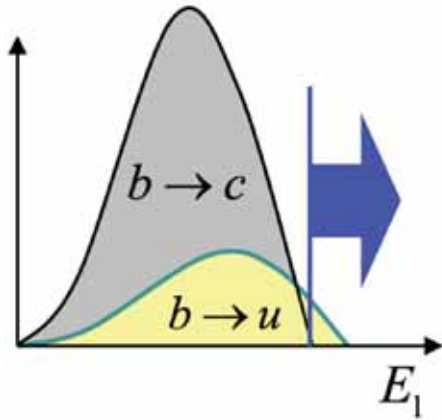
Belle measures  $\Delta$ BFs for  $\rho$  and  $\omega$ , in addition to  $\pi$ , extracting them in 3 bins of  $q^2$  to minimize errors from FF modelling

$B_{\text{reco}}$ -tag analyses have smaller syst. uncertainties, still statistically limited

improvements are expected with larger dataset



# $|V_{ub}|$ with reduced model dependence



$|V_{ub}|^2$  is proportional to  $B \rightarrow X_u l \nu$  branching fraction in limited region of phase space

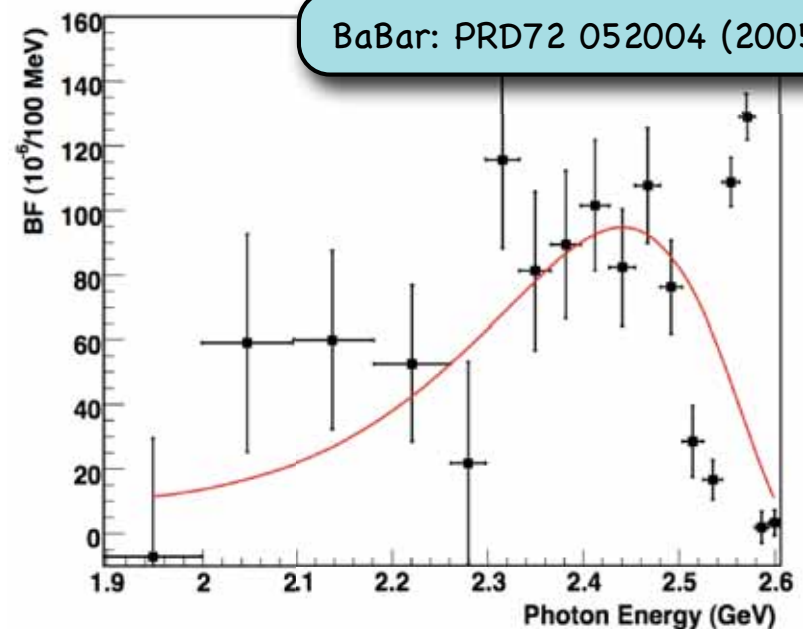
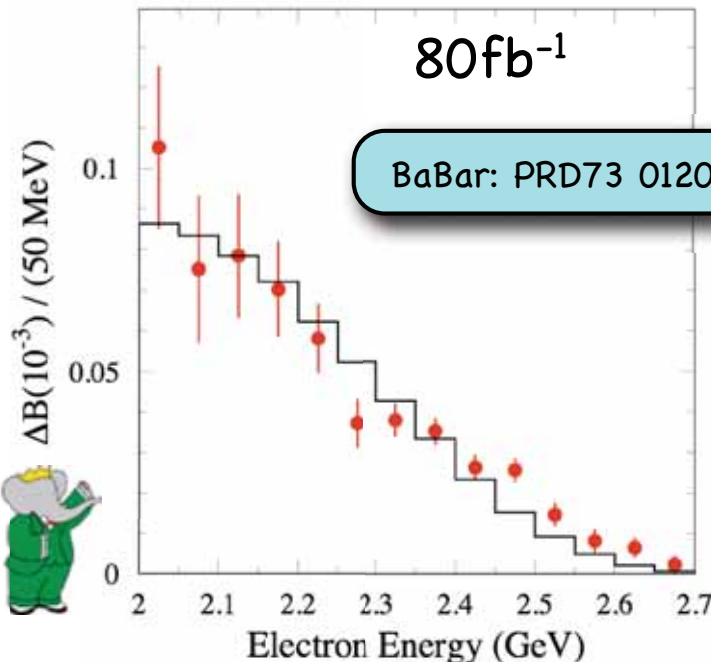
in inclusive SL decays

In this region the **theory (OPE) breaks down**, acceptance sensitive to **Fermi motion** of b quark inside B meson, parameterised by **Shape Functions**

SFs are assumed to be **universal**, at leading order, for  $b \rightarrow u$  and  $b \rightarrow s$  decays



Combine lepton-endpoint spectrum in  $B \rightarrow X_u e \nu$  decays with weighted photon-endpoint spectrum in  $B \rightarrow X_s \gamma$



# $|V_{ub}|$ with reduced model dependence

Different prescriptions to extract  $|V_{ub}|$ :

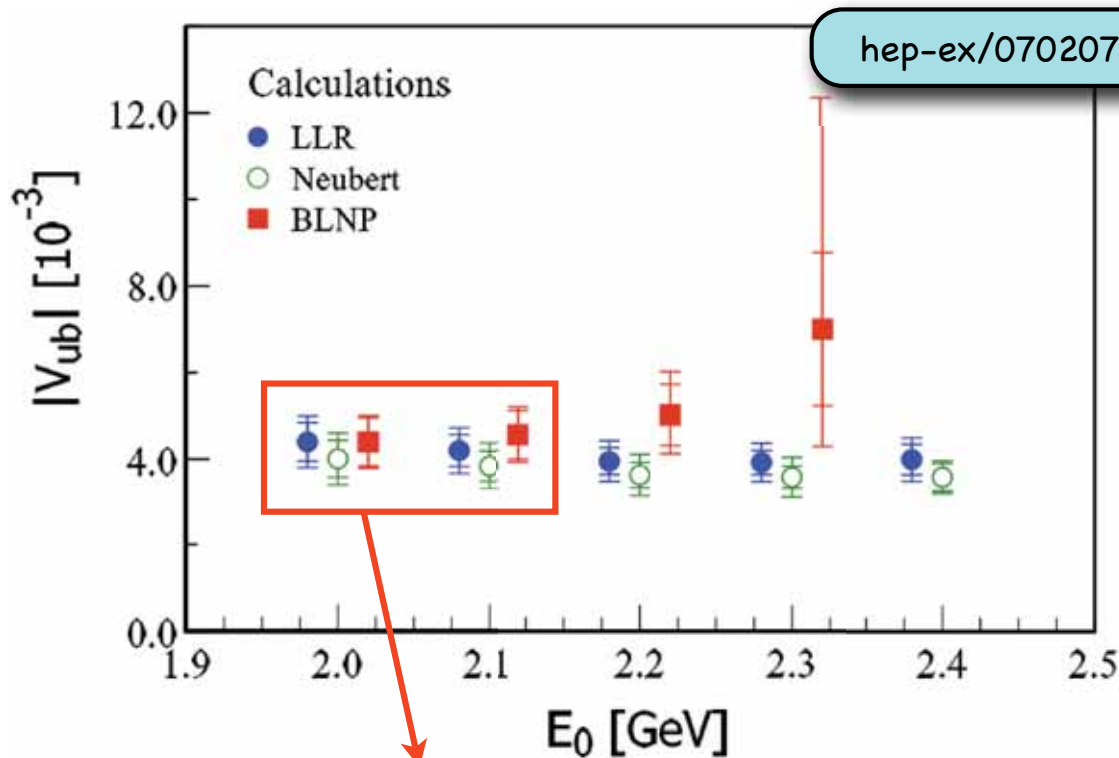
I - Leibovich, Low and Rothstein [Phys. Lett B513, 83 (2001)]

II - Neubert [Phys. Lett. B513, 88 (2001)]

III - Lange, Neubert and Paz [JHEP 0510, 084 (2005)]

Lange, JHEP 0601, 104 (2006)

two-loop calculation



measurement dominated by  
12% uncertainty on  $\Delta BF$   
( $B \rightarrow X_u e \nu$ ) and integral over  
 $B \rightarrow X_s \gamma$

improvements are  
expected with  
larger dataset

good agreement of 3 calculations  
lowest theory error ~5%

LNP:  $(4.40 \pm 0.30 \pm 0.41 \pm 0.23) 10^{-3}$   
SF-based:  $(4.44 \pm 0.25^{+0.42}_{-0.38} \pm 0.22) 10^{-3}$

# Conclusions

B factories are doing an excellent job of overconstraining the unitarity triangle:

$$|V_{cb}| = (41.49 \pm 0.52_{\text{fit}} \pm 0.20_{\text{TB}}) 10^{-3}$$

inclusive decays  
fits to moments

$$|V_{cb}| = (37.74 \pm 0.35_{\text{(stat)}} \pm 1.25_{\text{(syst)}} {}^{+1.23}_{-1.44(\text{th})}) 10^{-3}$$

exclusive decays

$$|V_{ub}| = (4.1 \pm 0.2_{\text{st}} \pm 0.20_{\text{sys}} {}^{+0.6}_{-0.4\text{FF}}) 10^{-3}$$

exclusive decays, untagged  
using HPQCD,  $q^2 > 16 \text{ GeV}^2$

$$|V_{ub}| = (4.40 \pm 0.30 \pm 0.41 \pm 0.23) 10^{-3}$$

inclusive decays, reduced  
model dependence

Extraction of  $|V_{ub}|$  with reduced model dependence is giving encouraging results

► improvements expected with larger dataset

Relative BFs for  $B \rightarrow D/D^*/D^{**} \ell \nu$  improve our understanding of such decays

Backup Slides

# HQE parameters and $|V_{cb}|$ : Kinetic Scheme



hep-ex/0611047

O. Buchmüller and H. Flächer,  
PRD73, 073008 (2006)

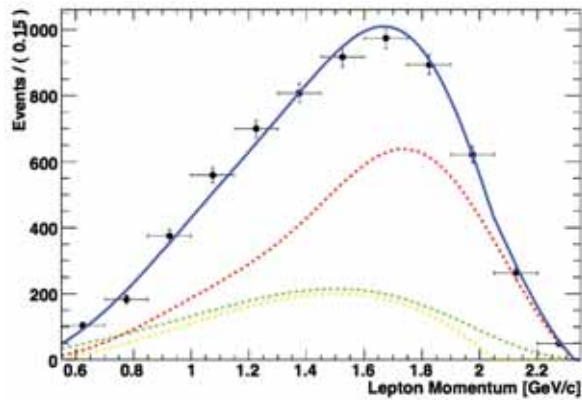
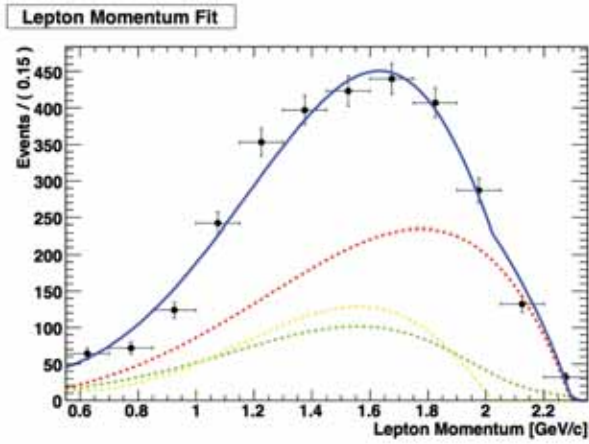
## Results

$$\begin{aligned} |V_{cb}| &= (41.93 \pm 0.65 \pm 0.07 \pm 0.63) 10^{-3} \\ m_b &= 4.564 \pm 0.076 \pm 0.003 \text{ GeV} \\ m_c &= 1.105 \pm 0.116 \pm 0.005 \text{ GeV} \\ \mu_\pi^2 &= 0.557 \pm 0.091 \pm 0.013 \text{ GeV}^2 \\ \mu_G^2 &= 0.358 \pm 0.060 \pm 0.003 \text{ GeV}^2 \\ \rho_D^3 &= 0.162 \pm 0.053 \pm 0.008 \text{ GeV}^3 \\ \rho_{LS}^3 &= -0.174 \pm 0.098 \pm 0.003 \text{ GeV}^3 \\ BR_{clv} &= 10.590 \pm 0.164 \pm 0.006 \% \end{aligned}$$

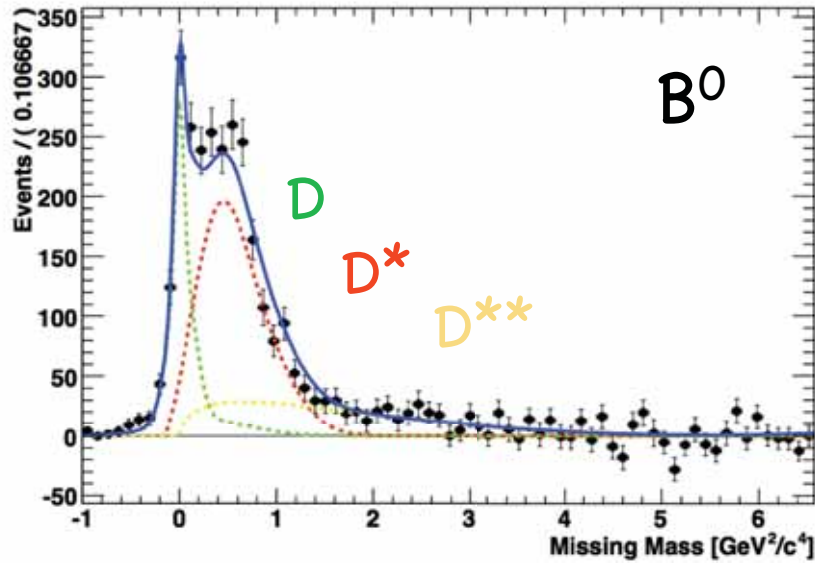
## Results

$$\begin{aligned} |V_{cb}| &= (41.96 \pm 0.23 \pm 0.35 \pm 0.59) 10^{-3} \\ m_b &= 4.590 \pm 0.025 \pm 0.030 \text{ GeV} \\ m_c &= 1.142 \pm 0.037 \pm 0.045 \text{ GeV} \\ \mu_\pi^2 &= 0.401 \pm 0.019 \pm 0.035 \text{ GeV}^2 \\ \mu_G^2 &= 0.297 \pm 0.024 \pm 0.046 \text{ GeV}^2 \\ \rho_D^3 &= 0.174 \pm 0.009 \pm 0.022 \text{ GeV}^3 \\ \rho_{LS}^3 &= -0.183 \pm 0.054 \pm 0.071 \text{ GeV}^3 \\ BR_{clv} &= 10.71 \pm 0.10 \pm 0.08 \% \end{aligned}$$

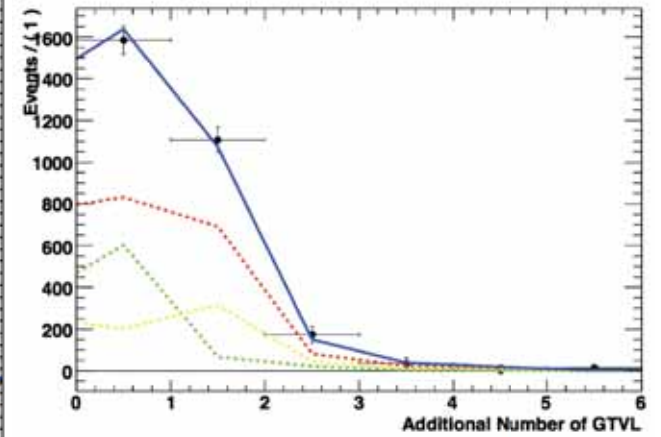
# Relative BFs for $B \rightarrow D/D^*/D^{**}l\nu$



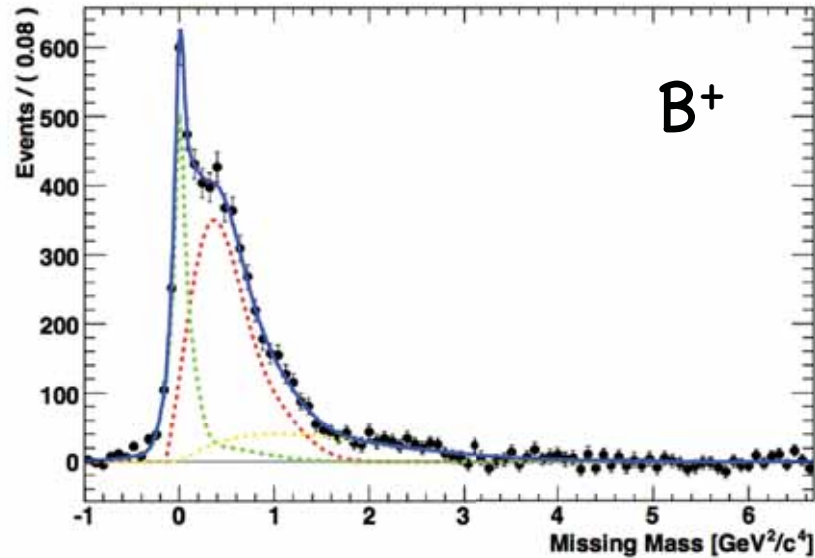
Missing Mass Fit



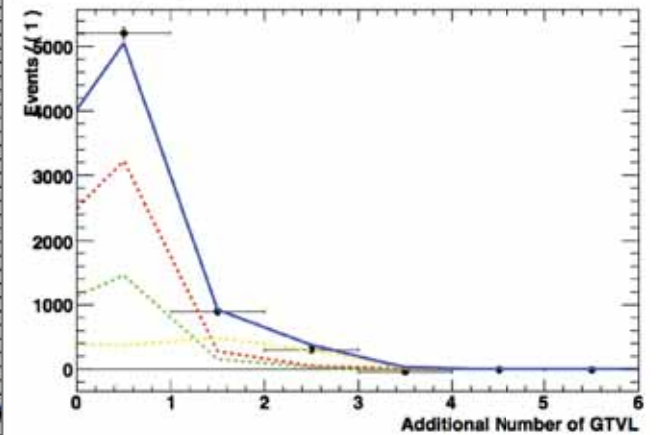
Track Multiplicity Fit



Missing Mass Fit



Track Multiplicity Fit

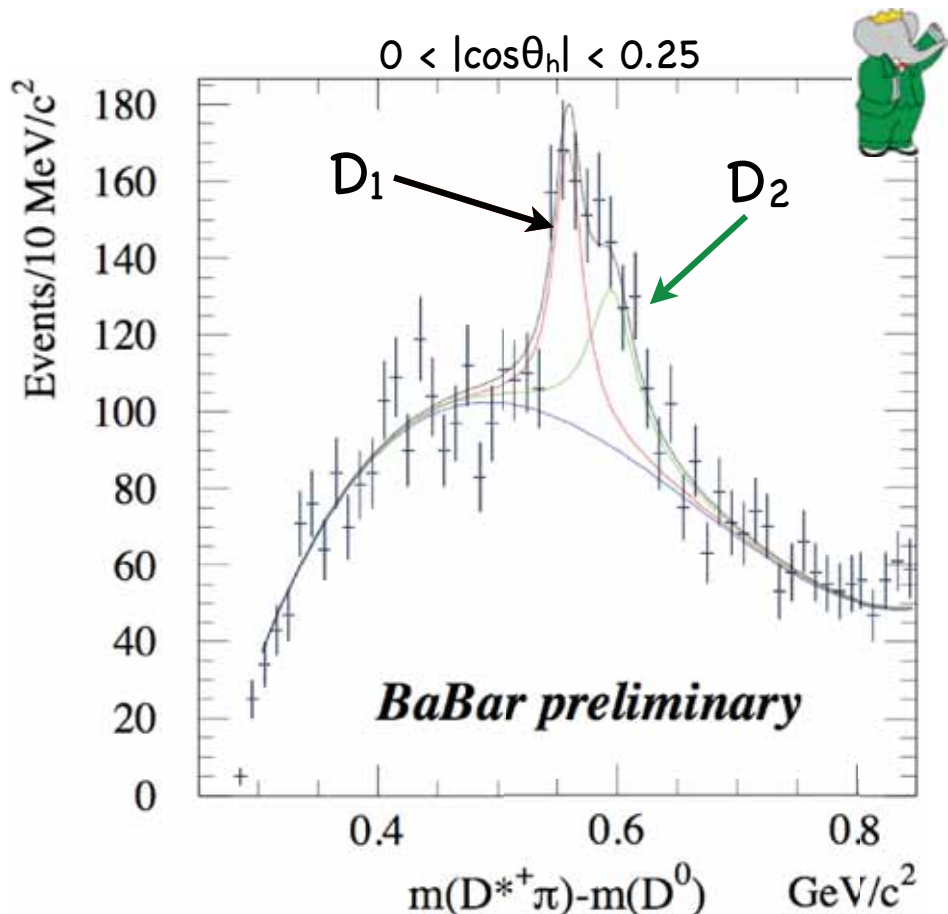


# $B \rightarrow D^{**} \ell \nu$ narrow resonances

$D^{**}$  is a nickname for states  $D^*(n\pi)$  with  $n > 0$ , including narrow resonances  $D_1, D_2^*$  + broad resonances  $D_0^*, D_1^*$  + non-resonant?

Uncertainty of  $D_1, D_2^*$  branching fractions still ~20-30%

BaBar does an inclusive selection of  $B \rightarrow D^{**} \ell \nu$  candidates, combining  $D^\pm$  or  $D^*$  with  $\pi^\pm$  to create  $D^{**}$  states



Simultaneous fit of  $D_1$  and  $D_2^*$   
in  $\Delta m = m(D^{**}) - m(D)$

$D_1$  vs.  $D_2^*$  components fit using 4 bins  
of  $D^* \rightarrow D\pi$  helicity angle  $|\cos\theta_h|$

$$\begin{aligned}
 \mathcal{B}(B^+ \rightarrow D_1^0 \ell^+ \nu_\ell) &= (4.48 \pm 0.26 \pm 0.35) \times 10^{-3} \\
 \mathcal{B}(B^+ \rightarrow D_2^{*0} \ell^+ \nu_\ell) &= (3.54 \pm 0.32 \pm 0.54) \times 10^{-3} \\
 \mathcal{B}(B^0 \rightarrow D_1^- \ell^+ \nu_\ell) &= (3.64 \pm 0.32 \pm 0.49) \times 10^{-3} \\
 \mathcal{B}(B^0 \rightarrow D_2^{*-} \ell^+ \nu_\ell) &= (2.70 \pm 0.35 \pm 0.43) \times 10^{-3}
 \end{aligned}$$