

The role of lepton flavours in leptogenesis

François-Xavier Josse-Michaux

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Baryon asymmetry of the Universe

- From cosmological observations the matter-antimatter density is deduced :

$$\eta_B \equiv \frac{n_b - n_{\bar{b}}}{n_\gamma} \approx 6 \times 10^{-10}$$

- Sakharov's conditions must be fulfilled :
 - B violation
 - C and CP violation
 - Departure from thermal equilibrium
- } hard to satisfy within the SM

Massive neutrinos through the See-Saw mechanism

- We add right-handed neutrinos (N) of Majorana type with mass scale $M \gg M_{\text{ew}}$

$$\mathcal{L} \propto \frac{1}{2} M N^2 + Y_\nu L H N$$

- Light ν masses are generated through the see-saw mechanism

$$m_\nu \approx \frac{(\langle H^0 \rangle Y_\nu)^2}{M}$$

$$1 \text{ eV} = \frac{(1 \text{ GeV})^2}{10^9 \text{ GeV}}$$


Sakharov's conditions : fulfilled

- L is violated

Equilibrium sphaleron interactions convert L into B

- CP violation in N decays

$$\epsilon_{\text{CP}} \equiv \frac{\Gamma_{(\text{N} \rightarrow \text{LH})} - \Gamma_{(\text{N} \rightarrow \bar{\text{L}}\text{H})}}{\Gamma_{(\text{N} \rightarrow \text{LH})} + \Gamma_{(\text{N} \rightarrow \bar{\text{L}}\text{H})}} \neq 0$$

- Out-of-equilibrium if $\dot{\phi} < H(M)$. Requires small couplings $Y \ll 1$ 

Leptogenesis in the standard picture : the « one-flavour approximation »

- The evolution of the lepton asymmetry is governed by the Boltzmann equations for the abundancies :

$$Y_{N_1}'(z) = - \frac{\Gamma_{(N \rightarrow \ell H)}}{H(M_1)} \cdot \gamma_D(z) \cdot (Y_{N_1}(z) - Y_{N_1}^{eq}(z))$$

$$Y_\ell'(z) = \epsilon_{CP} \cdot \frac{\Gamma_{(N \rightarrow \ell H)}}{H(M_1)} \cdot \gamma_D(z) (Y_{N_1}(z) - Y_{N_1}^{eq}(z)) - \frac{\Gamma_{(N \rightarrow \ell H)}}{H(M_1)} \cdot \gamma_{ID}(z) \cdot Y_\ell(z)$$

- The lepton asymmetry is partially converted into a baryon asymmetry through sphaleron interactions :

$$Y_B \approx \frac{1}{3} Y_\ell$$

- If $\Gamma_{(N \rightarrow \ell H)} \gg H(M_1)$, the lepton asymmetry is strongly washed-out, we cannot generate enough baryon asymmetry.

Thermal rate

- Interaction term involving charged lepton Yukawas:

$$\mathcal{L} \propto h_\alpha \bar{L}^\alpha H e_{R\alpha}$$

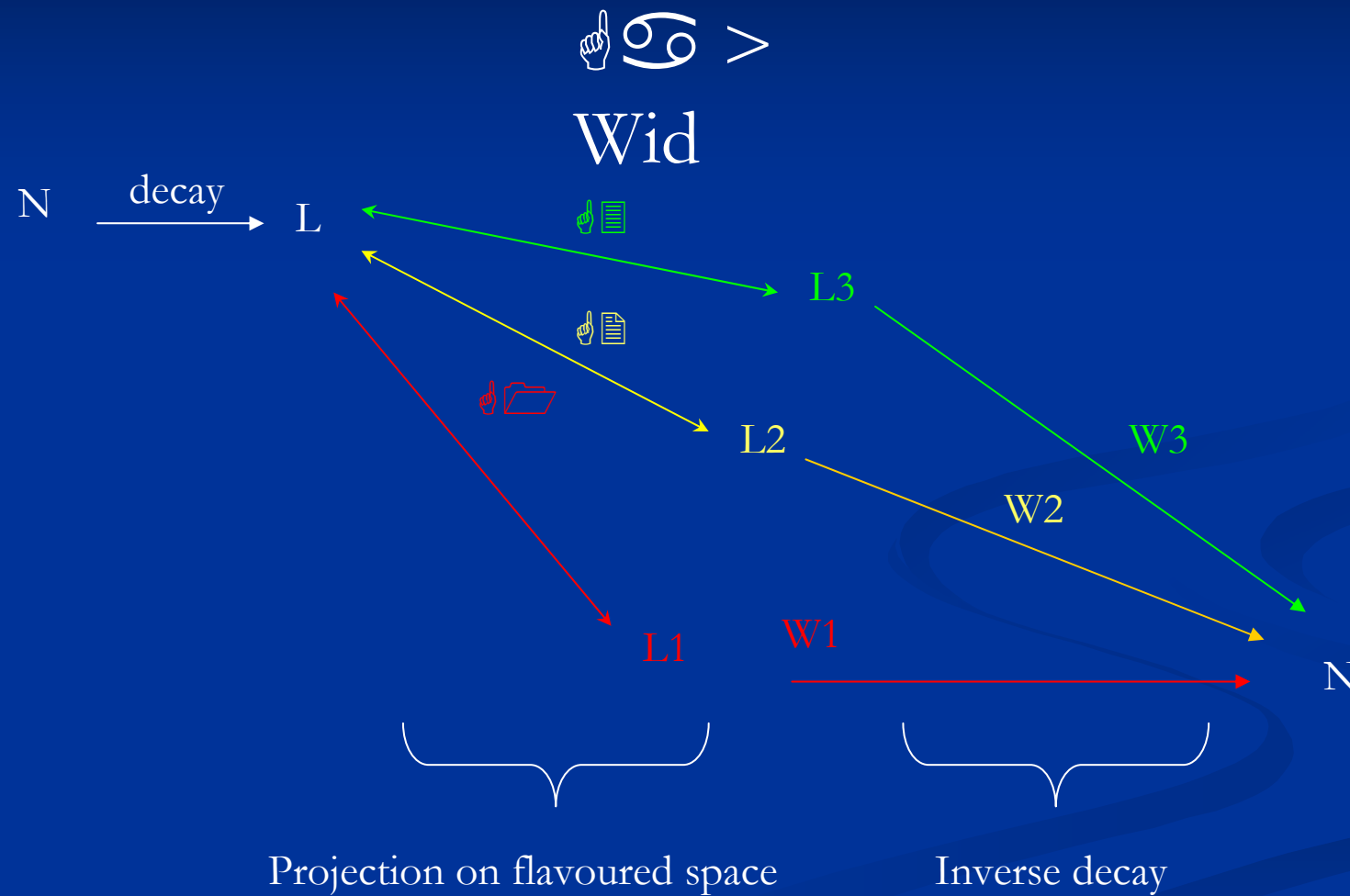
- Thermal rate :

$$\Gamma_\alpha(T) \approx 5 \times 10^{-3} h_\alpha^2 T$$

- If this rate is in-equilibrium, it can project the lepton asymmetry onto flavour-space.

For this we need to compare Γ_α with typical interactions of leptogenesis.

Flavour projection



Flavour projection

$\epsilon <$

Wid

$N \xrightarrow{\text{decay}} L$

Inverse decay

N

Lepton flavours

- The flavours are relevant if the interaction rates involving the charged lepton Yukawa are in equilibrium, and if :

$$\Gamma_{\alpha}(T \approx M_1) \gtrsim \frac{\Gamma_{(N \rightarrow \ell_{\alpha} H)}}{H(M_1)} \cdot \gamma_{ID}(T \approx M_1) \equiv W_{\alpha}(M_1)$$

- Depending on M_1 , different flavour structures are possible :

$M_1 \gtrsim 10^{12} \text{ GeV}$: flavours are indistinguishable.

$10^9 \text{ GeV} \lesssim M_1 \lesssim 10^{12} \text{ GeV}$: \blacklozenge Yukawa interactions are in equilibrium. The \blacklozenge flavour can be distinguished, but neither the \bigcirc nor the e flavours can.

$M_1 \lesssim 10^9 \text{ GeV}$: \bigcirc Yukawas are in equilibrium. All flavours are indistinguishable.

Flavoured quantities

We must study flavoured asymmetries and therefore consider :

- flavoured CP asymmetries : $\epsilon_{\alpha} = \frac{\Gamma(N \rightarrow \ell_{\alpha} H) - \Gamma(N \rightarrow \bar{\ell}_{\alpha} H)}{\Gamma(N \rightarrow \ell H) + \Gamma(N \rightarrow \bar{\ell} H)}$

- Flavoured wash-out strenghts : $\frac{\Gamma(N \rightarrow \ell_{\alpha} H)}{H(M1)} \equiv \kappa_{\alpha}$

- BE for flavoured asymmetries :

$$Y'_{\alpha}(z) = \epsilon_{\alpha} \cdot \kappa \cdot \gamma_D(z) \cdot (Y_{N_1}(z) - Y_{N_1}^{eq}(z)) - \kappa_{\alpha} \cdot \gamma_{ID}(z) \cdot Y_{\alpha}(z)$$

The baryon asymmetry : $Y_B \approx \frac{1}{3} \sum Y_{\alpha}$

Notice that : $\sum_{\alpha} \kappa_{\alpha} Y_{\alpha} \neq \sum_{\alpha} \kappa_{\alpha} \sum_{\alpha} Y_{\alpha}$

Influence on the baryon asymmetry

- The baryon asymmetry depends on how each individual asymmetry is washed-out : if for example

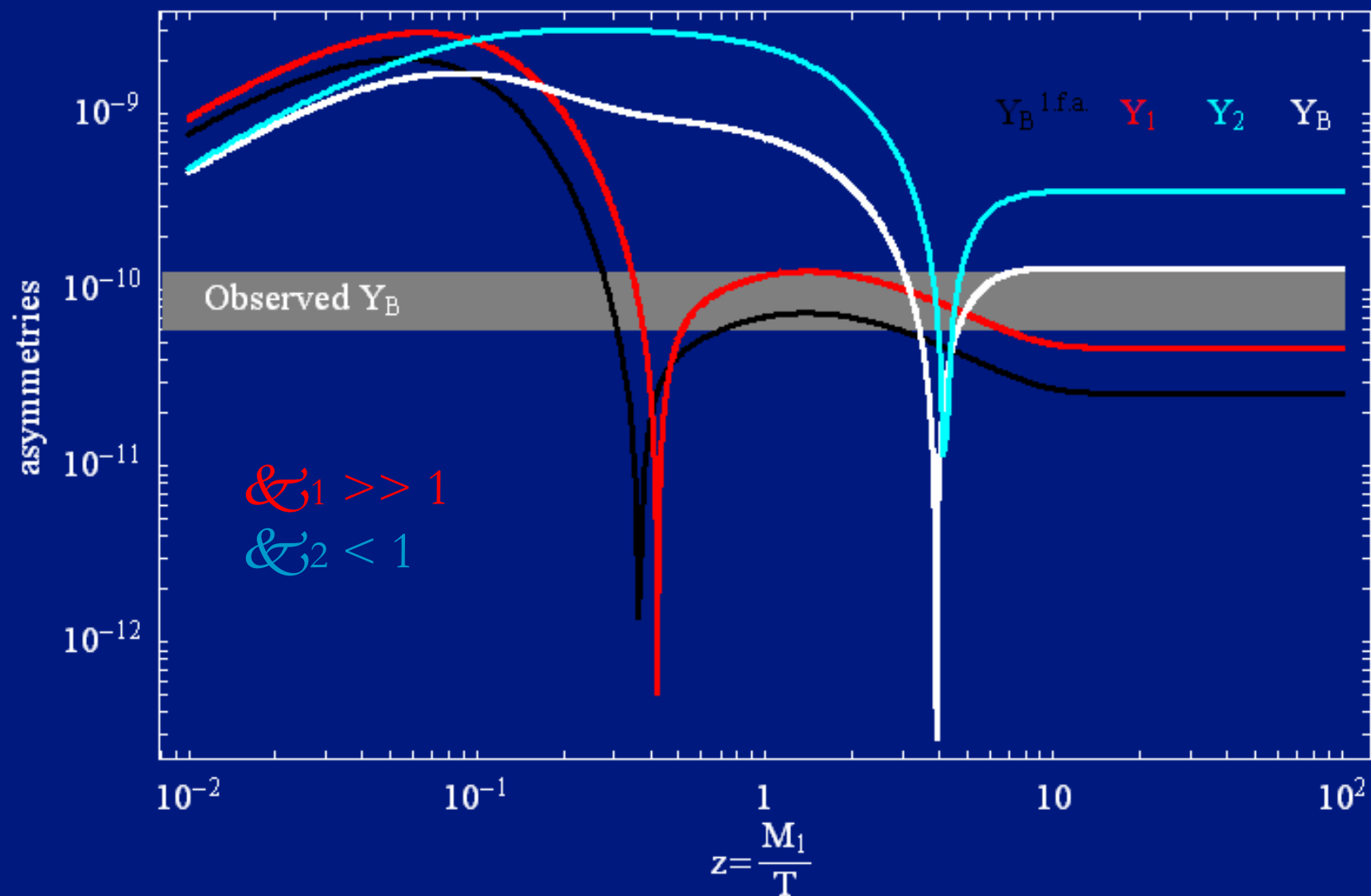
$$Y_B \approx Y_1 + Y_2$$

$\kappa_1 \gg 1$ Y_1 is strongly washed-out and too small

$\kappa_2 < 1$ Y_2 is weakly washed-out and may be sufficient

- Y_B will be mainly composed of Y_2 , and therefore weakly washed-out.

Influence on the baryon asymmetry



Bound on light neutrino mass

- In the standard picture, a bound on m_ν had been derived from the necessity that the wash-out \mathcal{E} should not be too strong. This scenario of Leptogenesis could have been ruled-out for higher measured m_ν .
- When we include lepton flavours, we do not have such constraints on \mathcal{E} , so m_ν is only upper-constrained by cosmological observations.

Conclusion :

- For $M_1 \lesssim 10^{12} \text{ GeV}$, lepton flavours are relevant.
- The baryon asymmetry can be enhanced compared to the standard picture
- No upper-bound on m_{ν}