

Lepton distribution from top-quark

A probe of new physics and top-polarization

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by

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top-quark : A looking glass

The mass of the top-quark is very large ($m_t \sim 175 \text{ GeV}$)

- top-mass being close to electro-weak scale, its couplings are sensitive to EWSB. Any new physics of EWSB (or mass generation) affects top-couplings with other particles.

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We have a clean looking glass for new physics.

Anomalous t -decay

Anomalous tbW vertex :

$$\Gamma^\mu = \frac{g}{\sqrt{2}} \left[\gamma^\mu (f_{1L} P_L + f_{1R} P_R) - \frac{i\sigma^{\mu\nu}}{m_W} (p_t - p_b)_\nu (f_{2L} P_L + f_{2R} P_R) \right]$$

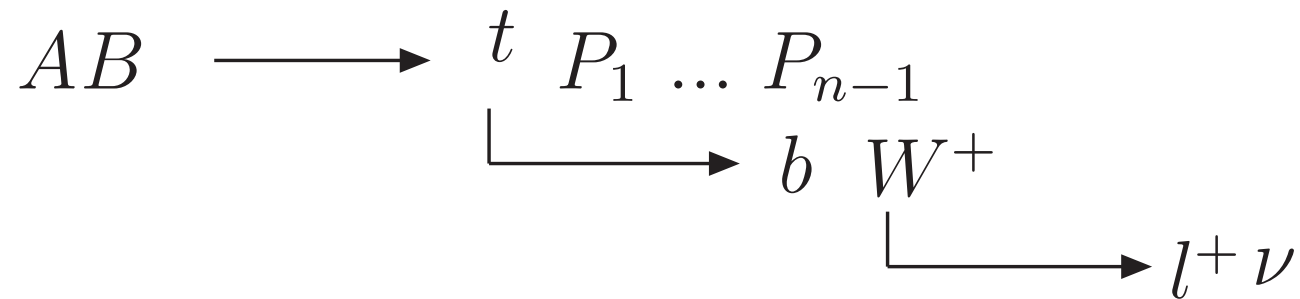
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- In the SM, $f_{1L} = 1$, $f_{1R} = 0$, $f_{2L} = 0$, $f_{2R} = 0$.
- Contribution from f_{1R} , f_{2L} are proportional to m_b .

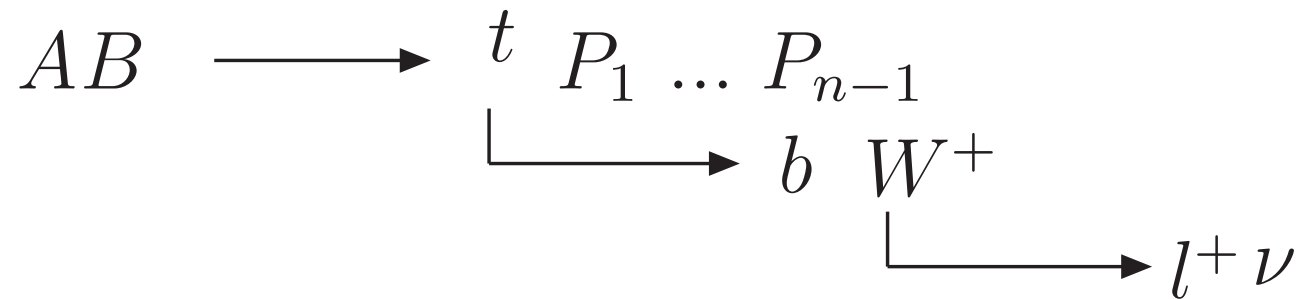
Lepton distribution



Lepton distribution is independent of anomalous tbW coupling if

- t -quark is on-shell; narrow-width approximation for t -quark,
- anomalous couplings f_{1R} , f_{2R} and f_{2L} are small,
- narrow-width approximation for W -boson,
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- narrow-width approximation for W -boson,
- b -quark is mass-less,
- $t \rightarrow bW(l\nu_\ell)$ is the only decay channel for t -quark.

Decay distribution

Narrow-width approximation for t -quark \Rightarrow

$$\overline{|\mathcal{M}|^2} = \frac{\pi \delta(p_t^2 - m_t^2)}{\Gamma_t m_t} \sum_{\lambda, \lambda'} \rho(\lambda, \lambda') \Gamma(\lambda, \lambda')$$

where,

$$\rho(\lambda, \lambda') = M_\rho(\lambda) M_\rho^*(\lambda') \quad \text{and} \quad \Gamma(\lambda, \lambda') = M_\Gamma(\lambda) M_\Gamma^*(\lambda').$$

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$$\rho(\lambda, \lambda') = M_\rho(\lambda) M_\rho^*(\lambda') \quad \text{and} \quad \Gamma(\lambda, \lambda') = M_\Gamma(\lambda) M_\Gamma^*(\lambda').$$

$$d\sigma = \sum_{\lambda, \lambda'} \left[\frac{(2\pi)^4}{2I} \rho(\lambda, \lambda') \delta^4(k_A + k_B - p_t - \sum_i^{n-1} p_i) \frac{d^3 p_t}{2E_t (2\pi)^3} \prod_i^{n-1} \frac{d^3 p_i}{2E_i (2\pi)^3} \right] \\ \times \left[\frac{1}{\Gamma_t} \left(\frac{(2\pi)^4}{2m_t} \Gamma(\lambda, \lambda') \delta^4(p_t - p_b - p_\nu - p_\ell) \frac{d^3 p_b}{2E_b (2\pi)^3} \frac{d^3 p_\nu}{2E_\nu (2\pi)^3} \right) \frac{d^3 p_\ell}{2E_\ell (2\pi)^3} \right].$$

Decay distribution

Production part ($\phi_t = 0$) :

$$\int \frac{d^3 p_t}{2E_t(2\pi)^3} \prod_i^{n-1} \frac{d^3 p_i}{2E_i(2\pi)^3} \frac{(2\pi)^4}{2I} \rho(\lambda, \lambda') \delta^4 \left(k_A + k_B - p_t - \left(\sum_i^{n-1} p_i \right) \right)$$
$$= d\sigma_{2 \rightarrow n}(\lambda, \lambda') dE_t d\cos\theta_t.$$

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Decay part (in rest rest frame of t -quark) :

$$\frac{1}{\Gamma_t} \frac{(2\pi)^4}{2m_t} \int \frac{d^3 p_\ell}{2E_\ell (2\pi)^3} \frac{d^3 p_b}{2E_b (2\pi)^3} \frac{d^3 p_\nu}{2E_\nu (2\pi)^3} \Gamma(\lambda, \lambda') \delta^4(p_t - p_b - p_\nu - p_\ell)$$

$$= \frac{1}{32\Gamma_t m_t} \frac{E_\ell}{(2\pi)^4} \frac{\langle \Gamma(\lambda, \lambda') \rangle}{m_t E_\ell} dE_\ell d\Omega_\ell dp_W^2.$$

Angular brackets stands for averaging over $\phi = (\phi_b - \phi_\ell)$.

Decay density matrix

In the rest frame of t -quark, we have

$$\begin{aligned}\langle \Gamma(\pm, \pm) \rangle &= g^4 m_t E_\ell^0 |\Delta_W(p_W^2)|^2 (1 \pm \cos \theta_l) \times F(E_\ell^0), \\ \langle \Gamma(\pm, \mp) \rangle &= g^4 m_t E_\ell^0 |\Delta_W(p_W^2)|^2 (\sin \theta_l e^{\pm i \phi_l}) \times F(E_\ell^0).\end{aligned}$$

where $\Delta_W(p_W^2) = \frac{1}{p_W^2 - m_W^2 + i \Gamma_W m_W}$

$$\begin{aligned}F(E_\ell^0) &= \left[(m_t^2 - m_b^2 - 2p_t \cdot p_l) \left(|f_{1L}|^2 + \Re(f_{1L} f_{2R}^*) \frac{m_t}{m_W} \frac{p_W^2}{p_t \cdot p_l} \right) \right. \\ &\quad \left. - 2\Re(f_{1L} f_{2L}^*) \frac{m_b}{m_W} p_W^2 - \Re(f_{1L} f_{1R}^*) \frac{m_b m_t}{p_t \cdot p_l} p_W^2 \right]\end{aligned}$$

In general,

$$\langle \Gamma(\lambda, \lambda') \rangle = (m_t E_\ell^0) |\Delta(p_W^2)|^2 g^4 A(\lambda, \lambda') F(E_\ell^0)$$

Angular distribution of lepton

Combining production and decay part, we have

$$\begin{aligned} d\sigma &= \frac{1}{32 \Gamma_t m_t (2\pi)^4} \left[\sum_{\lambda, \lambda'} d\sigma_{2 \rightarrow n}(\lambda, \lambda') \times g^4 A^{c.m.}(\lambda, \lambda') \right] \\ &\times dE_t d\cos\theta_t d\cos\theta_\ell d\phi_\ell \\ &\times E_\ell F(E_\ell) |\Delta(p_W^2)|^2 dE_\ell dp_W^2 \end{aligned}$$

and

$$\Gamma_t \propto \int E_\ell F(E_\ell) |\Delta(p_W^2)|^2 dE_\ell dp_W^2$$

Contribution from anomalous tbW couplings cancels between numerator and denominator, if $t \rightarrow bW$ is the only decay channel.

\Rightarrow Lepton angular distribution is independent of anomalous tbW interactions.

Energy distribution of lepton

The E_ℓ distribution (in the lab frame) depends both on

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The E_ℓ^0 distribution (in the top-rest-frame) depends only on the possible **new physics in t -decay**.

$$\frac{d\sigma}{dE_\ell^0} \propto \int E_t^0 F(E_t^0) |\Delta(p_W^2)|^2 dp_W^2$$

Independent of production mechanism of t -quark !!

Polarization of t -quark

Polarized cross-sections :

$$\int \frac{d^3 p_t}{2E_t (2\pi)^3} \left(\prod_{i=1}^{n-1} \frac{d^3 p_i}{2E_i (2\pi)^3} \right) \frac{(2\pi)^4}{2I} \rho(\lambda, \lambda') \delta^4 \left(k_A + k_B - p_t - \left(\sum_{i=1}^{n-1} p_i \right) \right) = \sigma(\lambda, \lambda').$$

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Polarization density matrix :

$$P_t = \frac{1}{2} \begin{pmatrix} 1 + \eta_3 & \eta_1 - i\eta_2 \\ \eta_1 + i\eta_2 & 1 - \eta_3 \end{pmatrix},$$

$$\eta_3 = (\sigma(+, +) - \sigma(-, -)) / \sigma_{tot}$$

$$\eta_1 = (\sigma(+, -) + \sigma(-, +)) / \sigma_{tot}$$

$$i \eta_2 = (\sigma(+, -) - \sigma(-, +)) / \sigma_{tot}$$

Polarization of t -quark

Polarization through leptonic decay of t -quark :

$$\begin{aligned}\frac{\eta_3}{2} &= \frac{\sigma(p_\ell \cdot s_3 < 0) - \sigma(p_\ell \cdot s_3 > 0)}{\sigma(p_\ell \cdot s_3 < 0) + \sigma(p_\ell \cdot s_3 > 0)} \\ \frac{\eta_2}{2} &= \frac{\sigma(p_\ell \cdot s_2 < 0) - \sigma(p_\ell \cdot s_2 > 0)}{\sigma(p_\ell \cdot s_2 < 0) + \sigma(p_\ell \cdot s_2 > 0)} \\ \frac{\eta_1}{2} &= \frac{\sigma(p_\ell \cdot s_1 < 0) - \sigma(p_\ell \cdot s_1 > 0)}{\sigma(p_\ell \cdot s_1 < 0) + \sigma(p_\ell \cdot s_1 > 0)}\end{aligned}$$

$$s_i \cdot s_j = -\delta_{ij} \quad p_t \cdot s_i = 0$$

For $p_t^\mu = E_t(1, \beta_t \sin \theta_t, 0, \beta_t \cos \theta_t)$, we have

$$s_1^\mu = (0, -\cos \theta_t, 0, \sin \theta_t), \quad s_2^\mu = (0, 0, 1, 0), \quad s_3^\mu = E_t(\beta_t, \sin \theta_t, 0, \cos \theta_t)/m_t.$$

Polarization of t -quark

η_2 : transverse polarization normal to the production plane.

Simplest quantity to measure;

requires reconstruction of t -production plane;

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Angular distribution in lab frame can be used as a qualitative measure of the t -polarization.

Polarization through angular distribution

For demonstration, we chose $\gamma\gamma \rightarrow t\bar{t}$ process with/without Higgs exchange contribution.

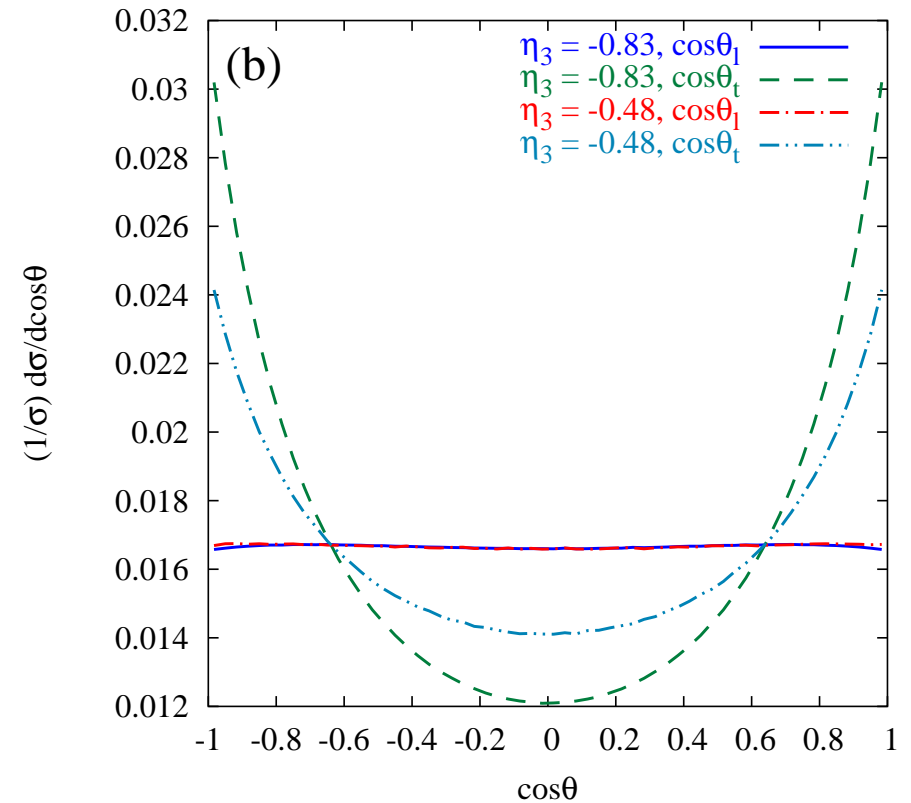
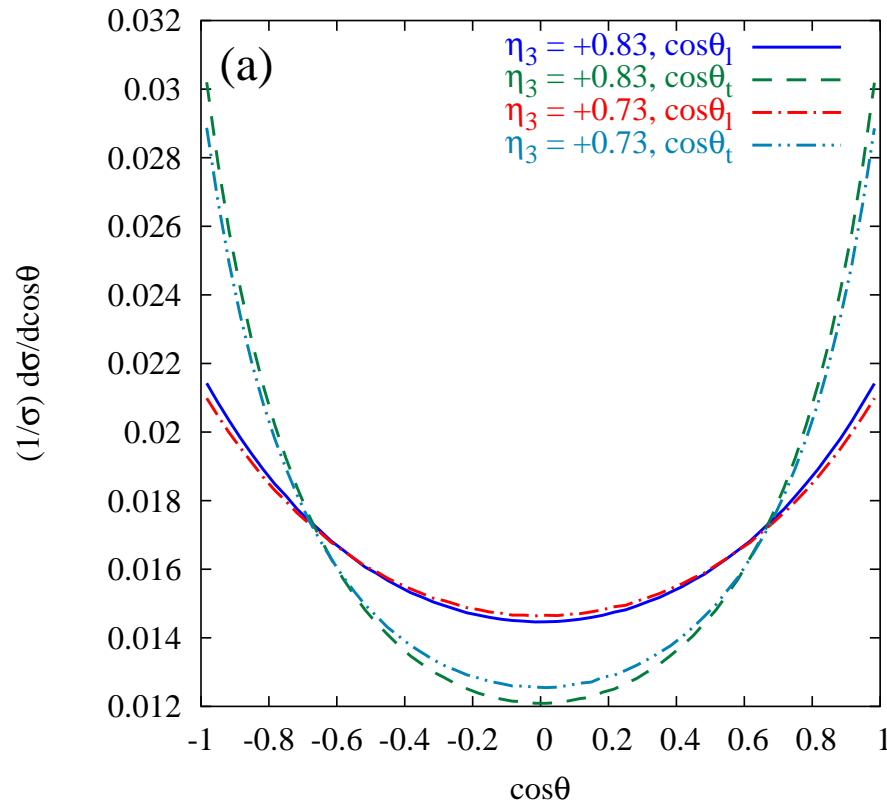
$$m_\phi = 500 \text{ GeV}; \Gamma_\phi = 2.5 \text{ GeV},$$
$$S_t = 0.2, P_t = 0.4, S_\gamma = 4.0 + i 0.5 \text{ and } P_\gamma = 1.25 + i 2.0.$$

Polarized ideal photon spectrum is used.

Assumptions :

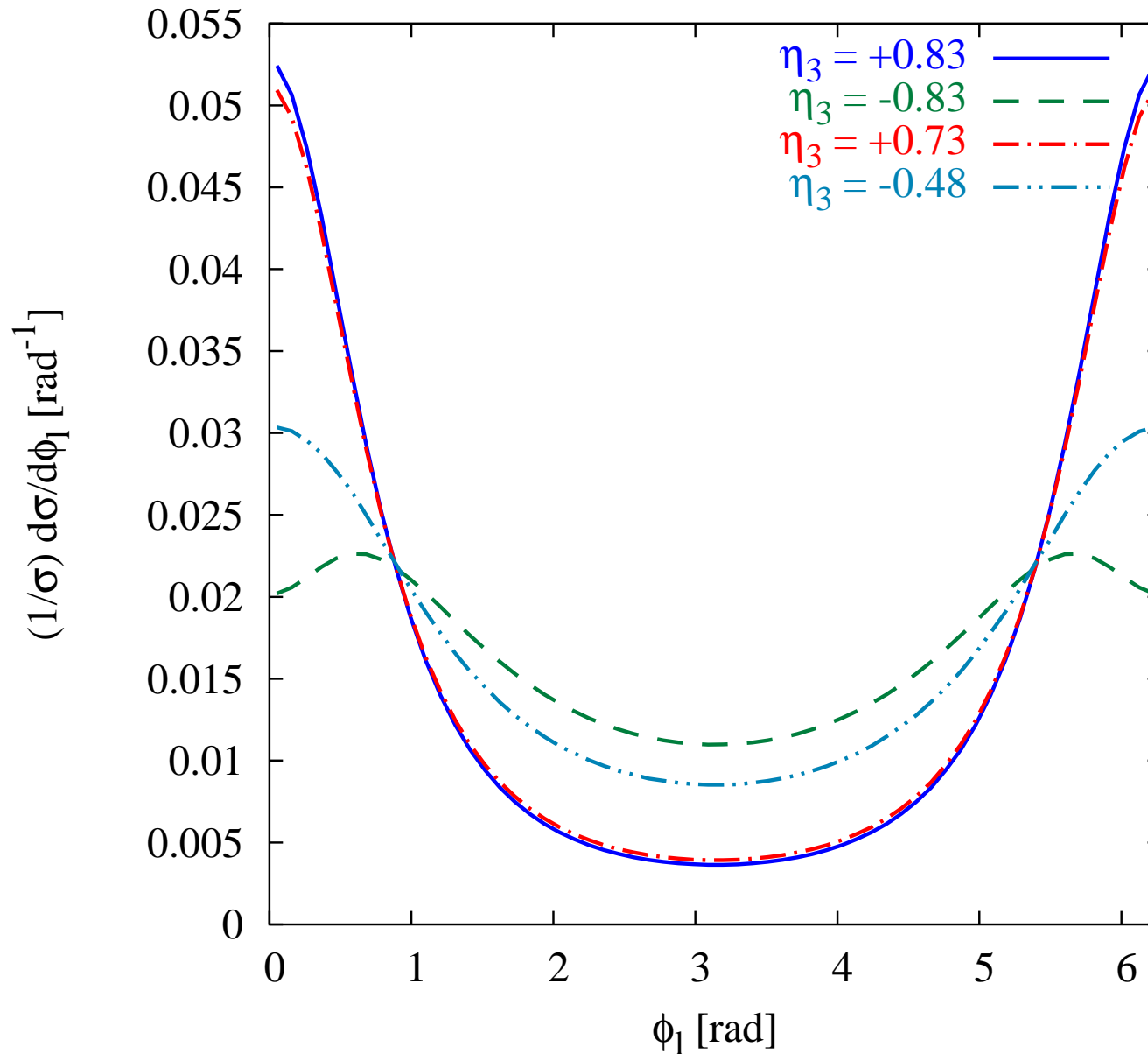
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- anomalous tbW couplings are small
- W -boson is on-shell
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Polarization through angular distribution



$$\eta_1 = 0 \text{ and } \eta_2 = 0$$

Polarization through angular distribution



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- Polarization of t -quark can be measured (quantitatively) through angular asymmetries of decay leptons.
- Angular distribution of decay lepton in the lab-frame is a good qualitative probe of t -polarization; quantitatively better for negative polarizations.