



# Nuclear observables

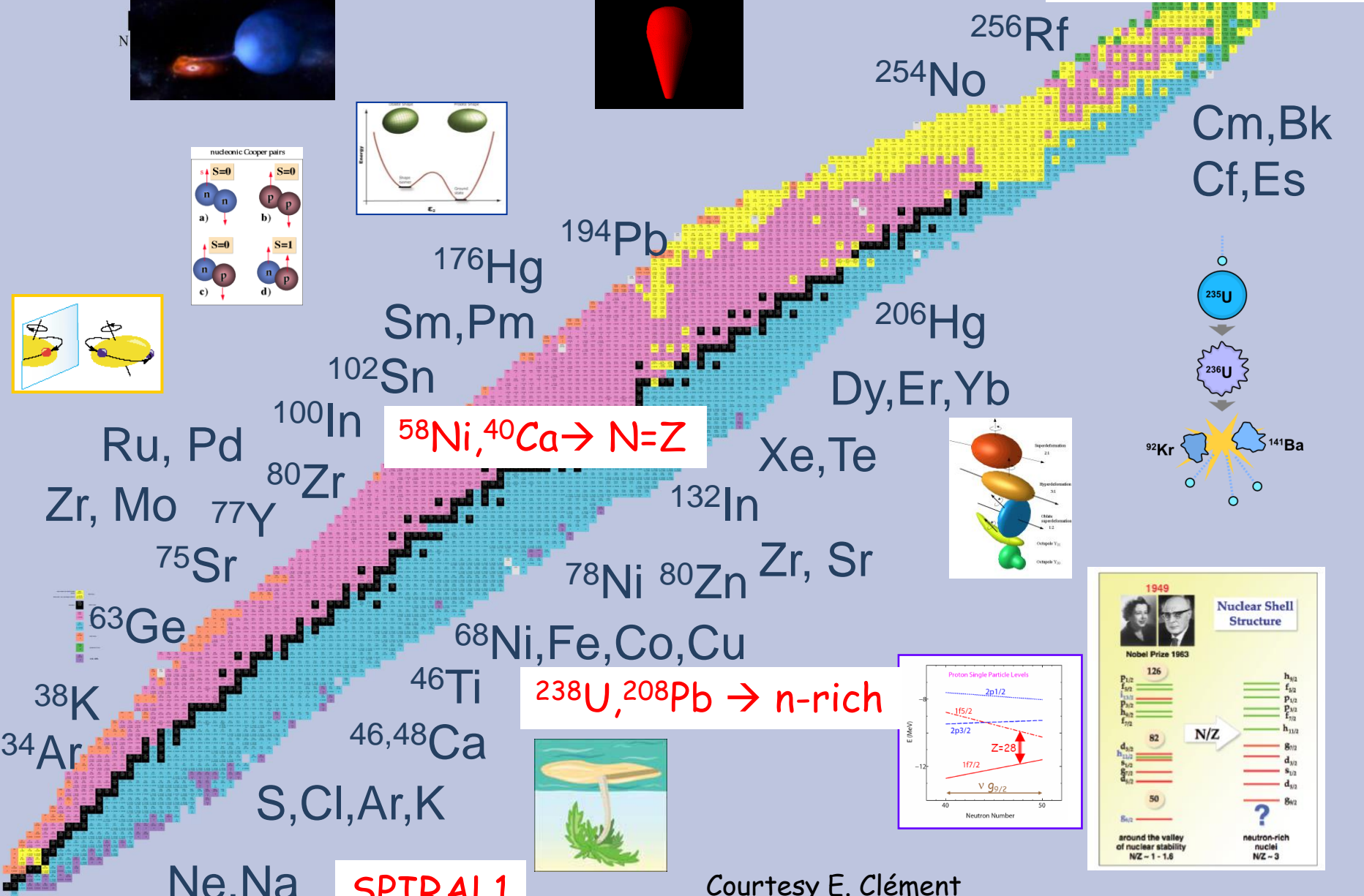
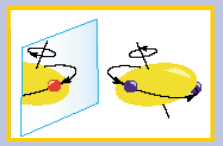
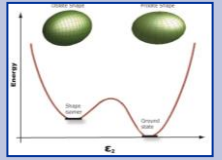
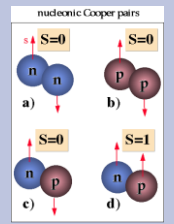
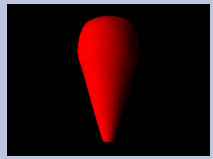
G. Duchêne

Du noyau aux étoiles (From nuclei to stars)  
e-mail : [gilbert.duchene@iphc.cnrs.fr](mailto:gilbert.duchene@iphc.cnrs.fr)

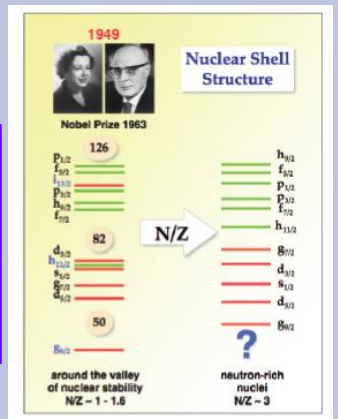
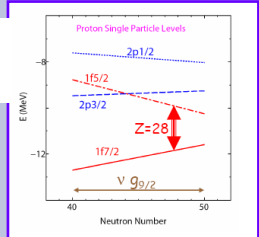
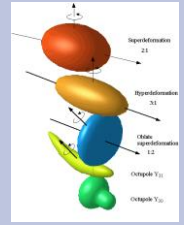
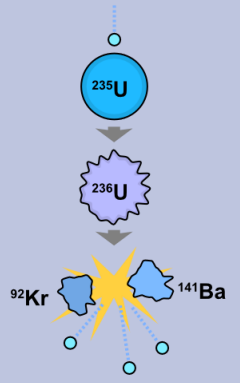
1. Introduction
2. Radiation-matter interactions and detectors for charged particle and  $\gamma$  rays
3. Nuclear reactions
4. Nuclear structure and observables
5. Perspectives

# The physics case of AGATA@GANIL is the in-beam $\gamma$ -ray spectroscopy of exotic nuclei populated by heavy-ions collisions at the Coulomb Barrier

$^{48}\text{Ca}, ^{50}\text{Ti} \rightarrow \text{SHE}$



Cm, Bk  
Cf, Es



Courtesy E. Clément

**SPIRAL1**

# Lecture plan

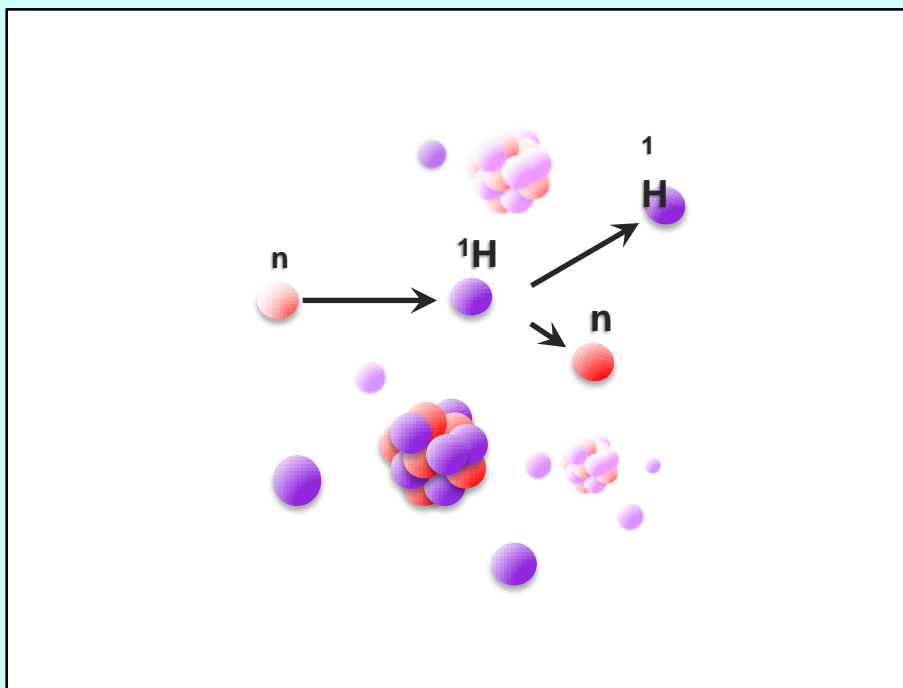
1. Introduction
2. Radiation-matter interactions and detectors for charged particle and  $\gamma$  rays
3. Nuclear reactions
4. Nuclear structure and observables
5. Perspectives

## Emitted particles in nuclear reactions

- Neutrons
- Charged particles (protons, alphas, electrons)
- Fragments ( $Z, A$ )
- $\gamma$  rays

## Neutrons

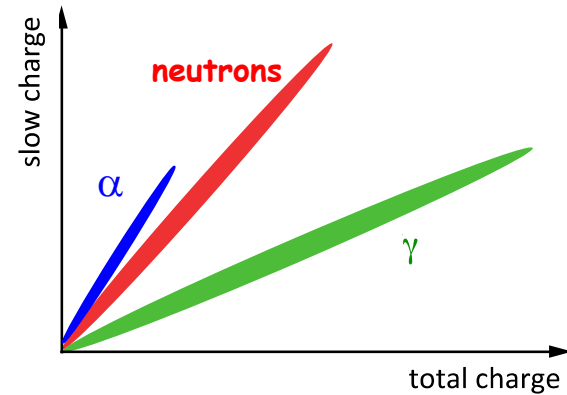
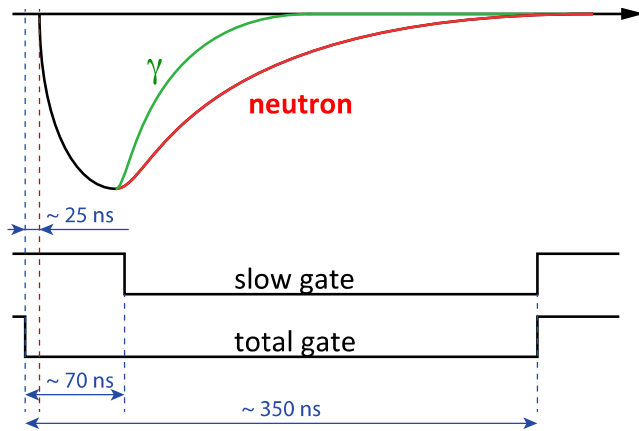
- For  $E_n > 500$  keV mainly elastic scattering  $n + H \rightarrow n + H$
- Recoil induces atomic excitations
- Prompt and delayed fluorescence



# Radiation-matter interactions and detectors

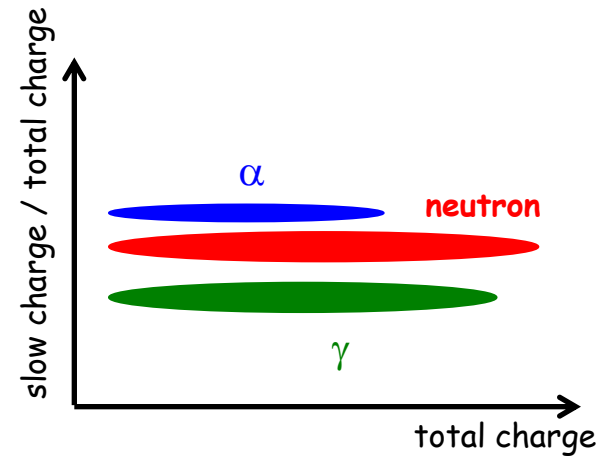
## Neutrons

### ➤ Neutron - $\gamma$ discrimination



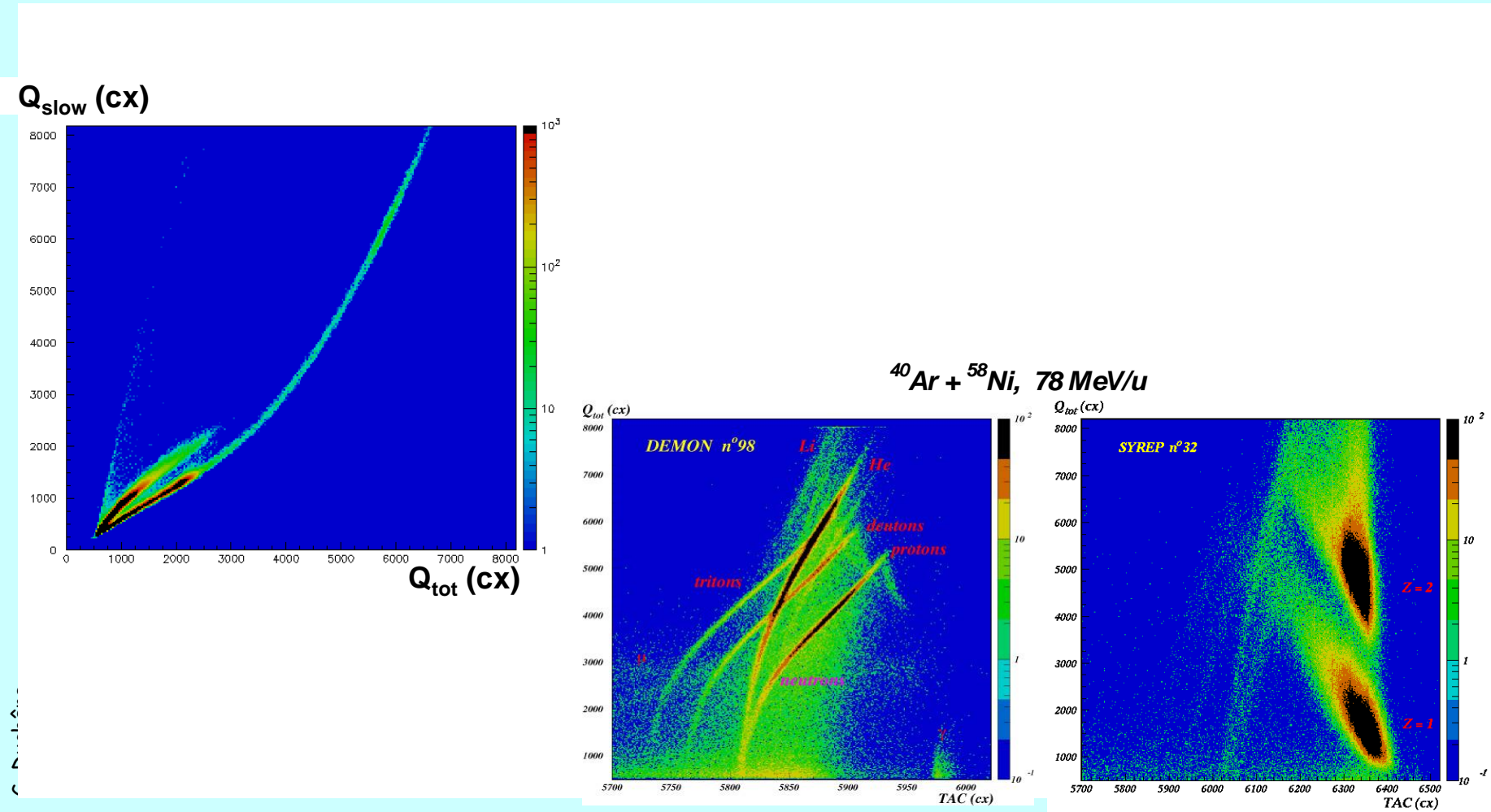
- organic liquids : NE213, BC501A, ...
- crystals: anthracen, stilben (organics)  
clyc ( $\text{Cs}_2\text{LiYCl}_6$ )  
(also for slow neutrons)
- plastics: (no n- $\gamma$  discrimination)  
except EJ299 ... (new)

mainly...



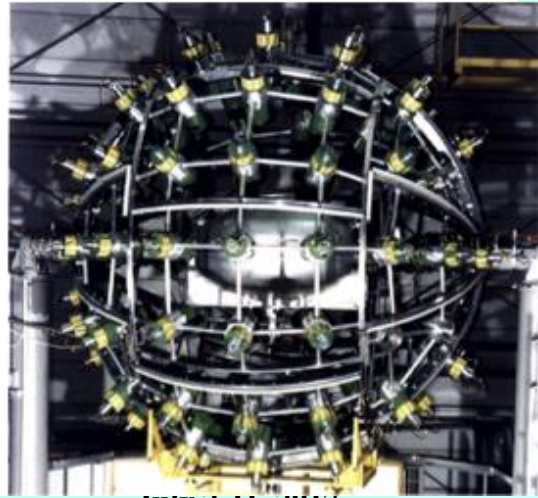
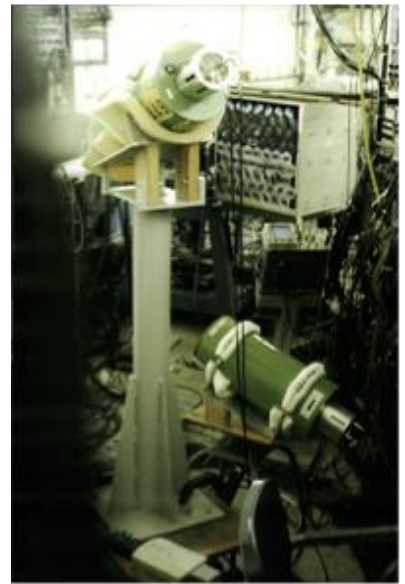
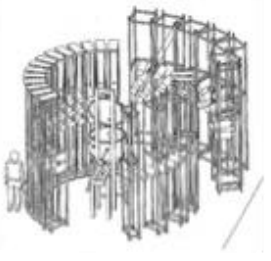
## Neutrons

- Neutron -  $\gamma$  discrimination



# DEMON:

modular neutron detector





## Charged particles

### ➤ Bethe formula

$$-\frac{dE}{dx} = \frac{4\pi z^2 e^4}{m_e c^2 \beta^2} N Z \left[ \ln \frac{2m_e c^2}{I} \beta^2 \gamma^2 - \beta^2 \right]$$

Linear stopping power

### ➤ incident particle

- z charge state of the particle
- $\beta = v/c$
- $\gamma = 1/(1 - \beta^2)$

### ➤ penetrated material

- Z atomic number of the material
- N number of atoms per volume unit
- I ionisation potential (~10 eV to few 10 keV)

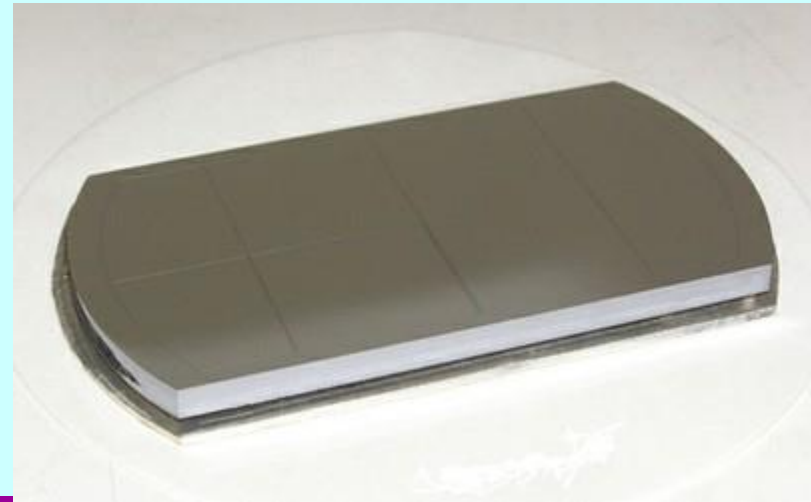
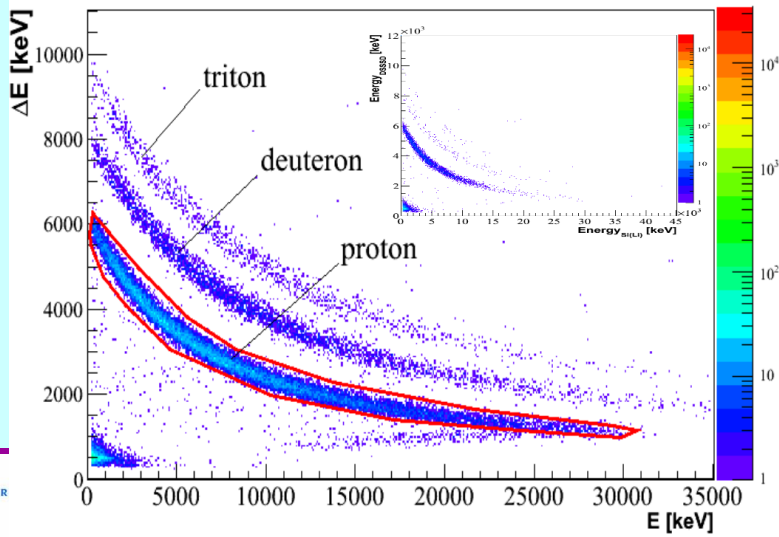
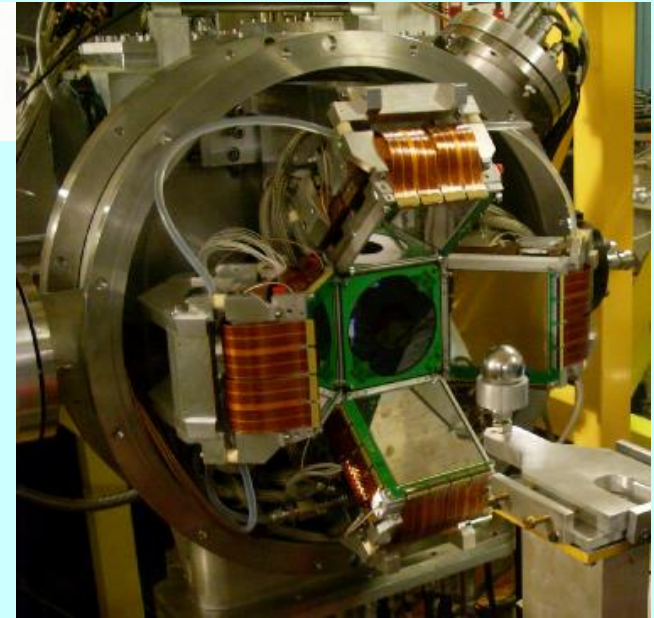
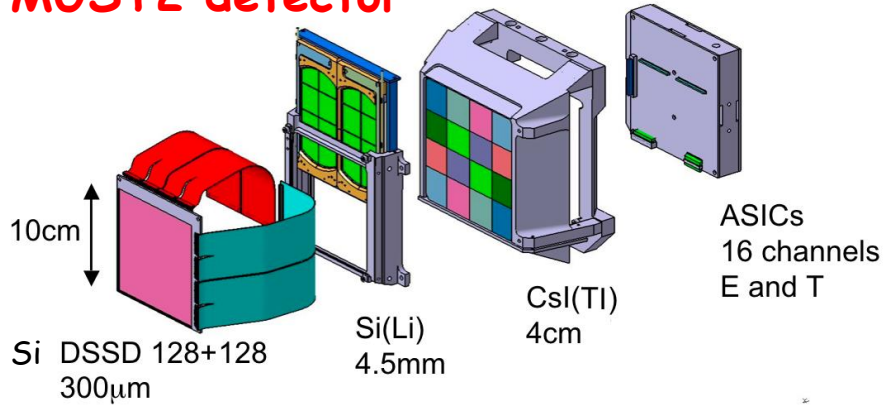
# Radiation-matter interactions and detectors

## Charged particles

- Particle identification

$$E \times \Delta E \propto Az^2$$

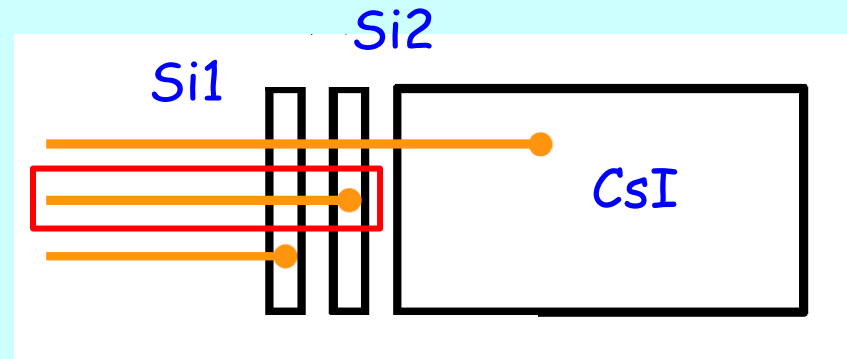
## MUST2 detector



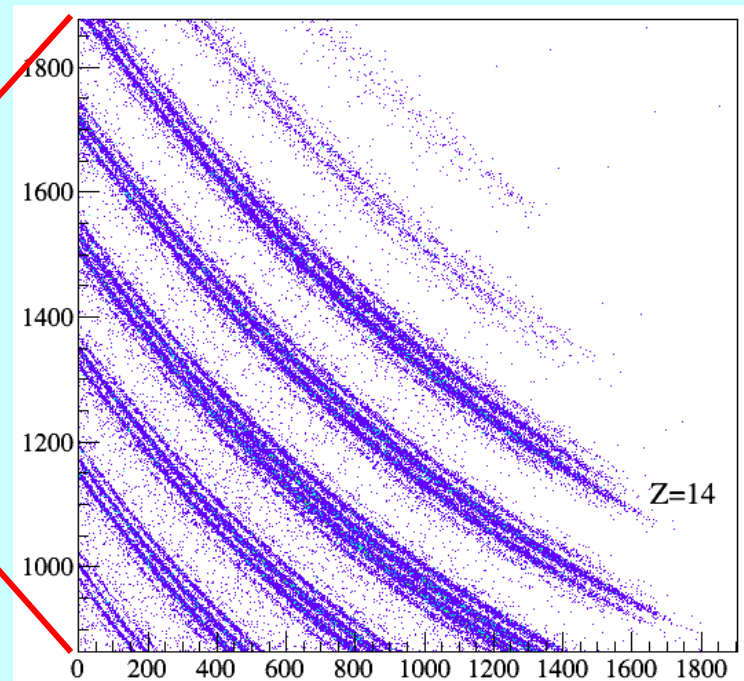
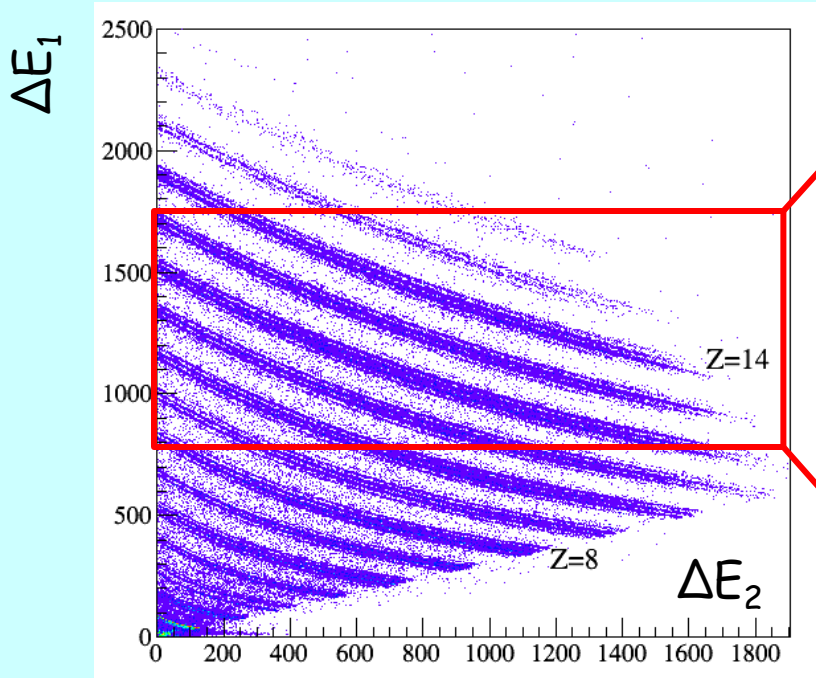
# Radiation-matter interactions and detectors

## Fragments

- Particle identification
  - ❑ Si detectors (FAZIA)
  - ❑ Telescope of 2  $\Delta E$  Si det. and 1 CsI det.
  - ❑ Pulse-shape analysis



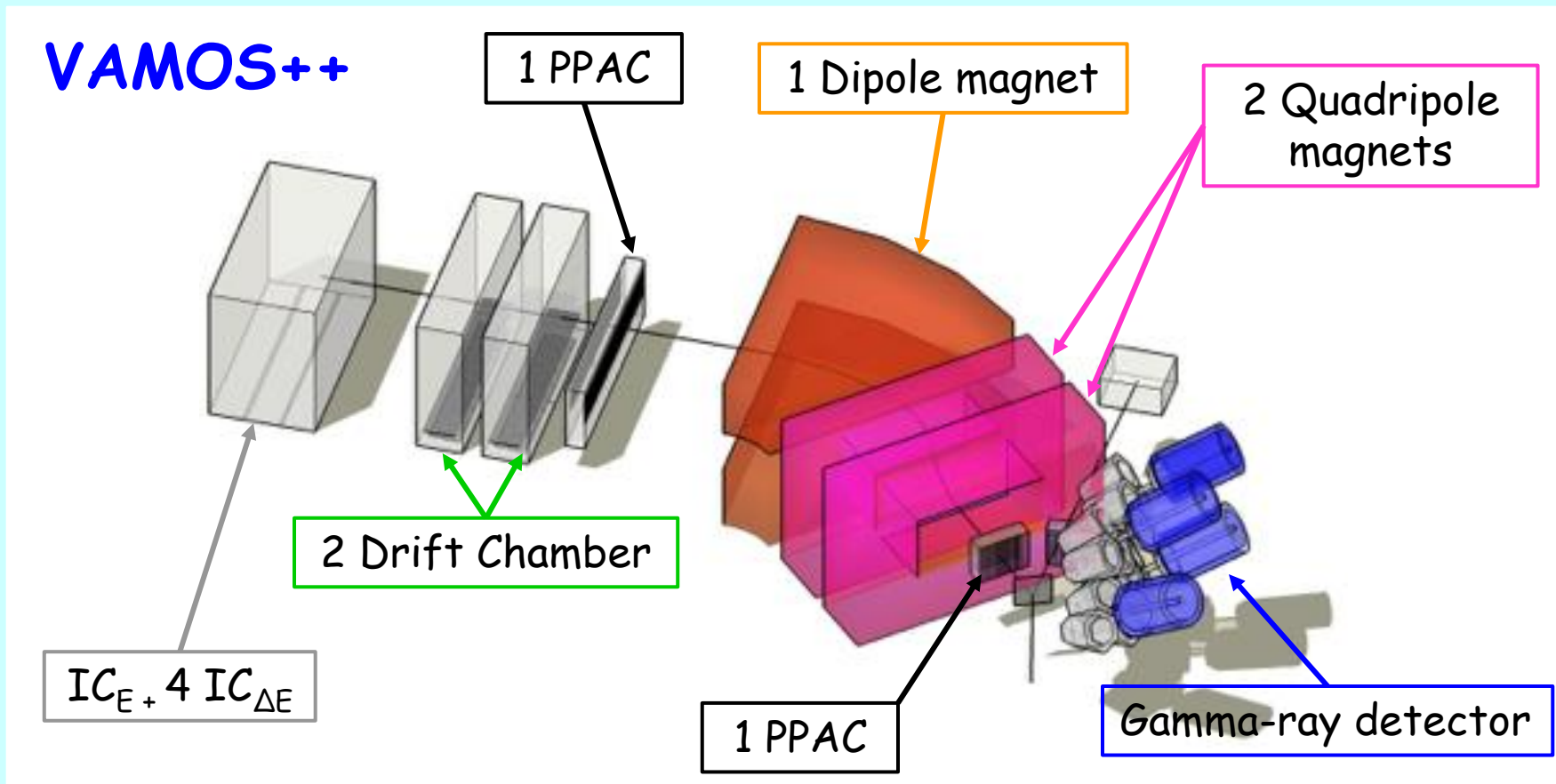
## Case of fragments stopped in the Si2



Courtesy G. Verde and D. Gruyer

## Fragments

- Particle identification
- Spectrometer

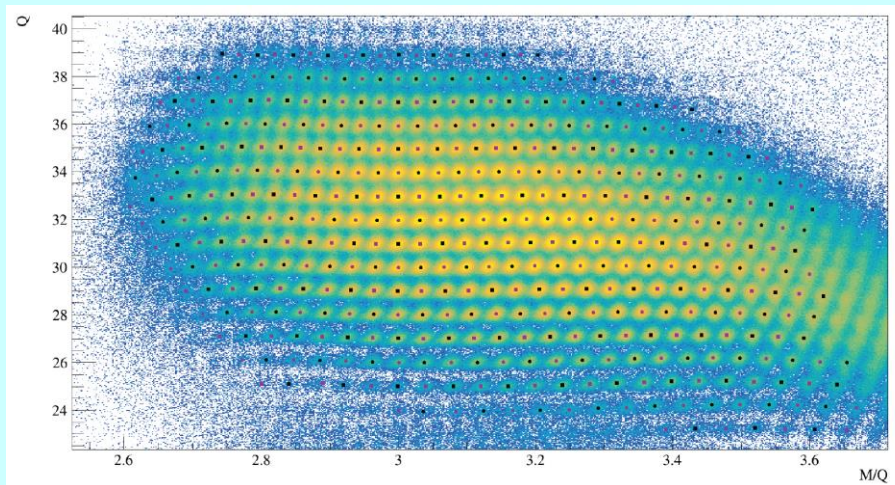
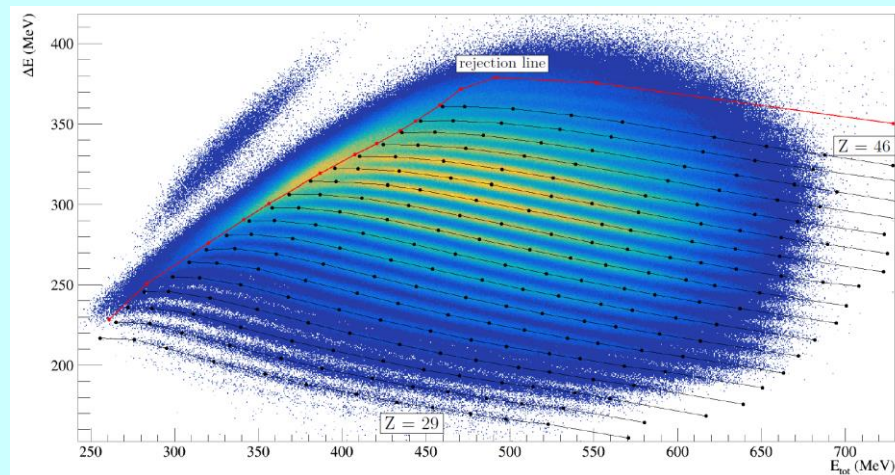


VAMOS drawing courtesy A. Lemasson

## Fragments

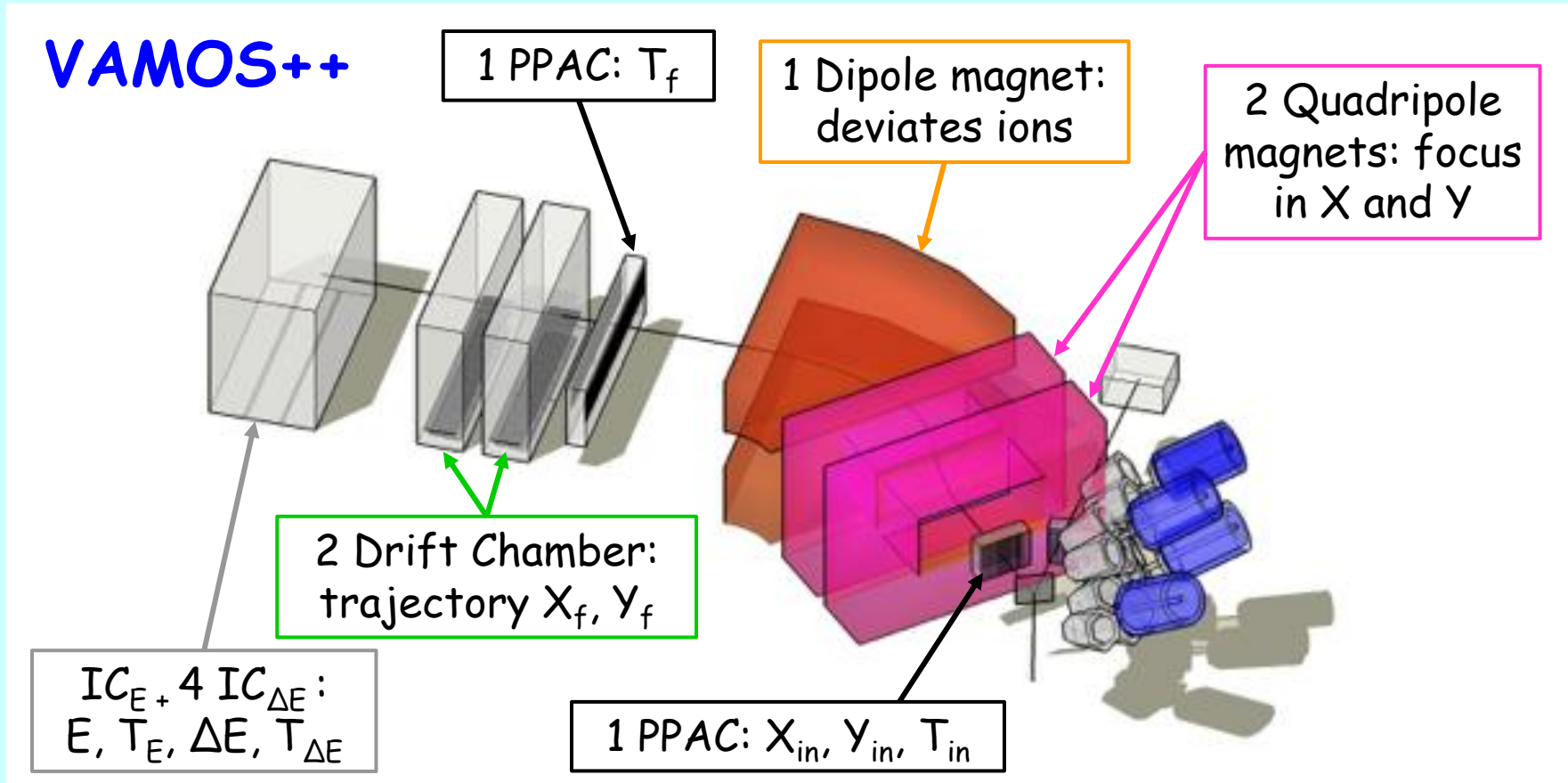
### ➤ Spectrometer

- ❑ Magnets: focus in X and Y (quadrupoles) and deviate the ions for mass selection (dipole)
- ❑ PPAC: (Parallel Plate Avalanche Counter)
  - ❖ Gaseous detector
  - ❖ Ion trajectory ( $X_{in}, Y_{in}$ )
  - ❖ Time of flight ( $ToF = T_f - T_{in}$ )
  - ❖ Velocity ( $v = L/ToF$ )
- ❑ Drift chamber:
  - ❖ Gaseous detector
  - ❖ Ion trajectory ( $X_f, Y_f$ )
- ❑ IC: (Ionisation chamber)
  - ❖ Gaseous detector
  - ❖ Z identification ( $\Delta E, E$ )
  - ❖ Mass/Charge state ( $M/Q$ ) determination
  - ❖ Mass determination



## Fragments

- Particle identification
- ❑ Spectrometer

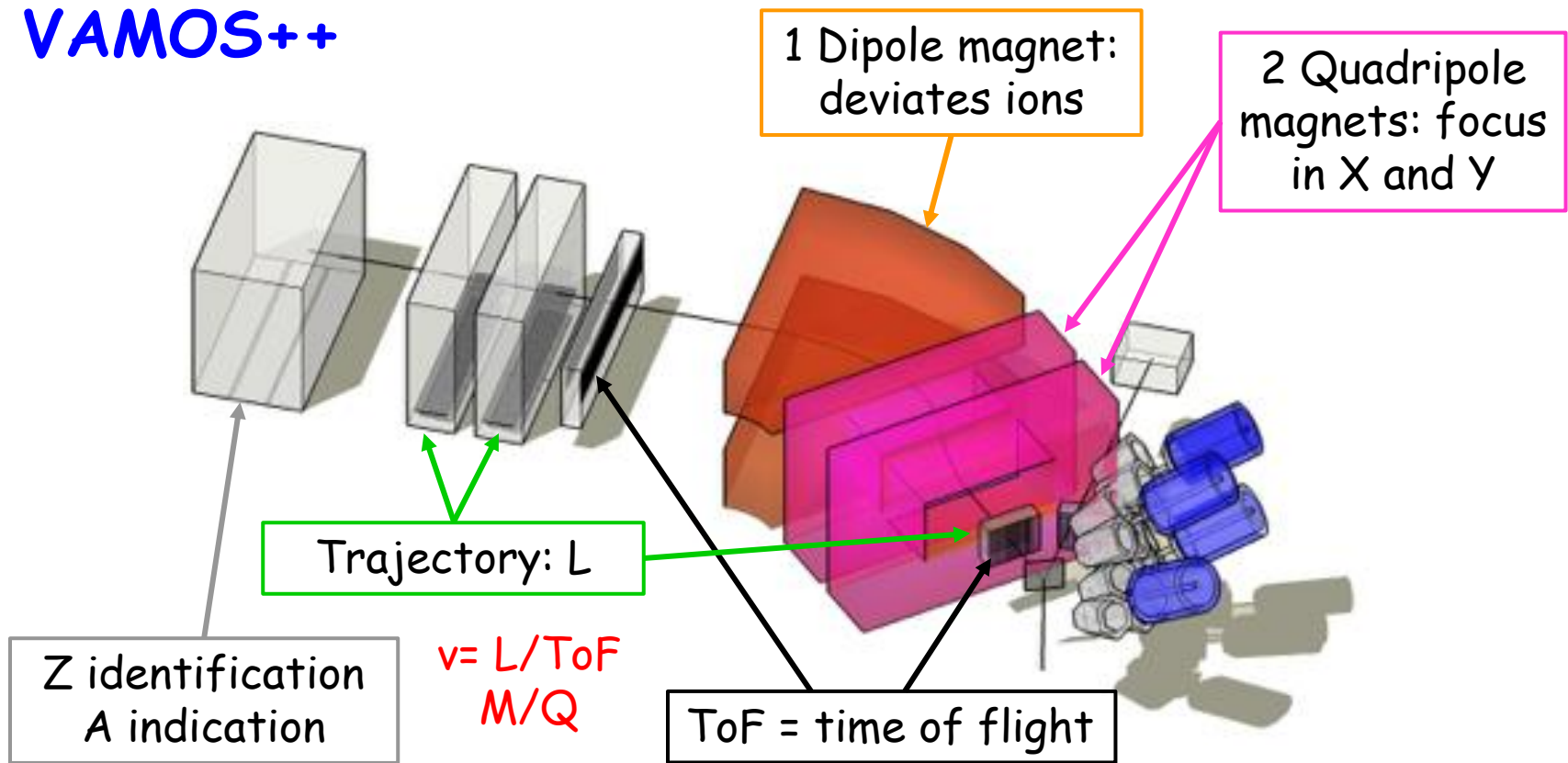


G. Duchêne

## Fragments

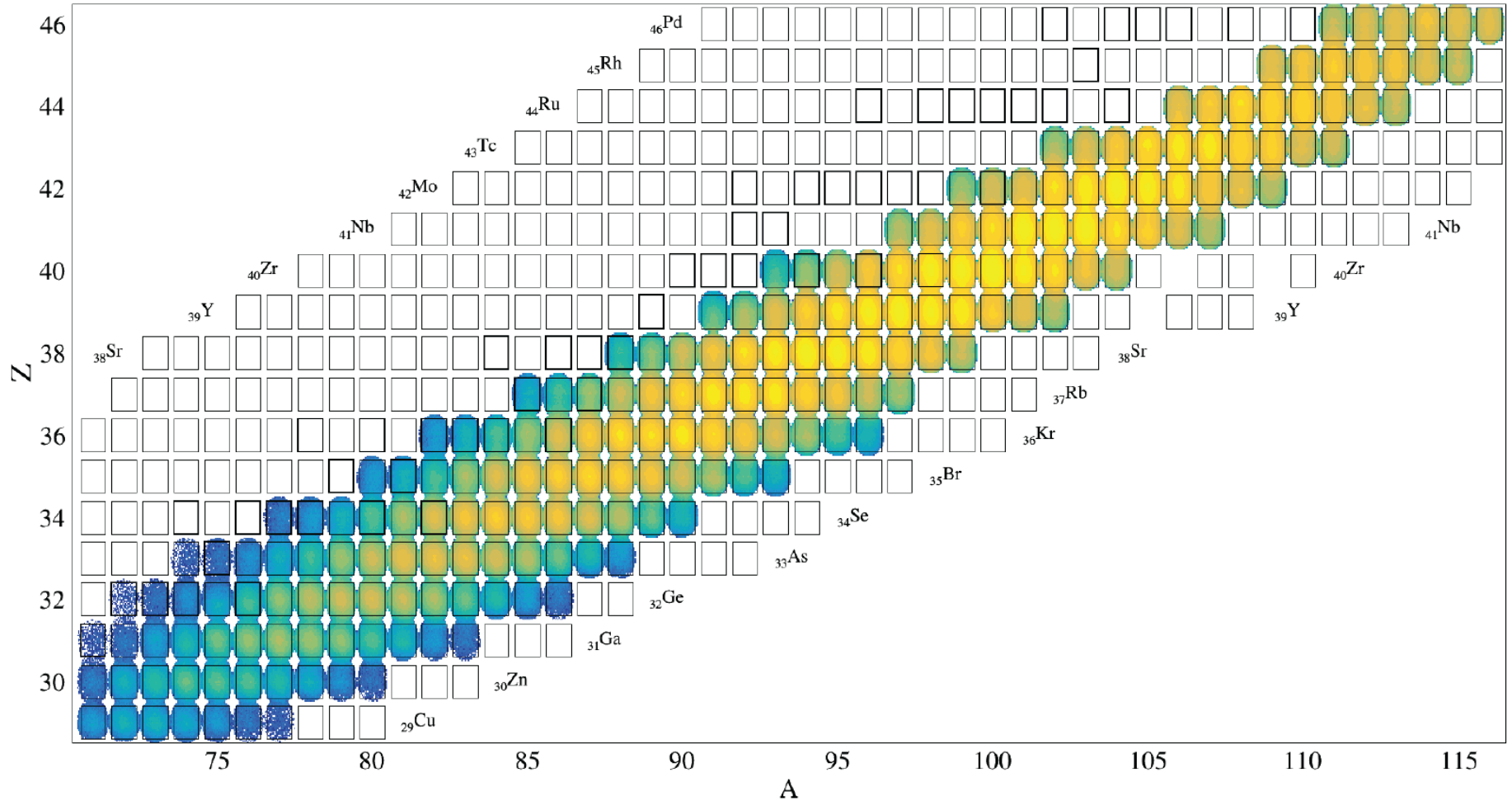
- Particle identification
- Spectrometer

## VAMOS++



## Fragments

➤ Spectrometer



C. Duchêne



## $\gamma$ rays

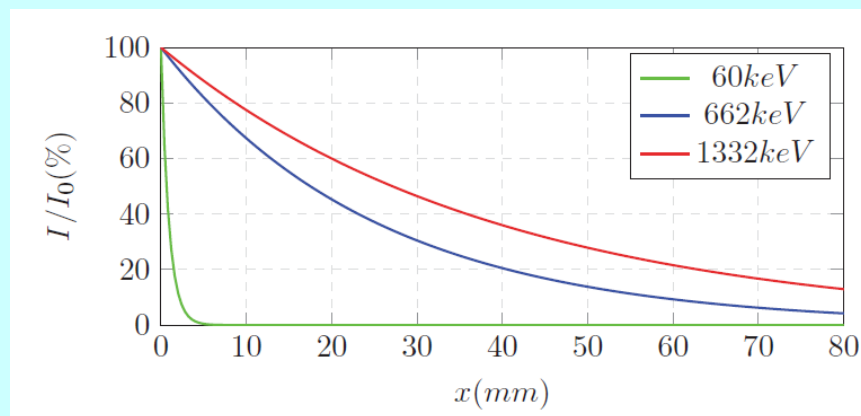
### ➤ Transmission

$$I(x) = I_0 e^{-\mu x}$$

- ❑  $\mu$  is the total absorption coefficient
- ❑  $x$  thickness of material
- ❑  $\mu$  depends on the material and on the  $\gamma$ -ray energy

### ➤ $\gamma$ -ray detection

- ❑ Energy transfer to primary charged particle and secondary ones
- ❑ Detection of the charges



## $\gamma$ rays

### ➤ Photoelectric effect

- Full photon energy transfer to one electron

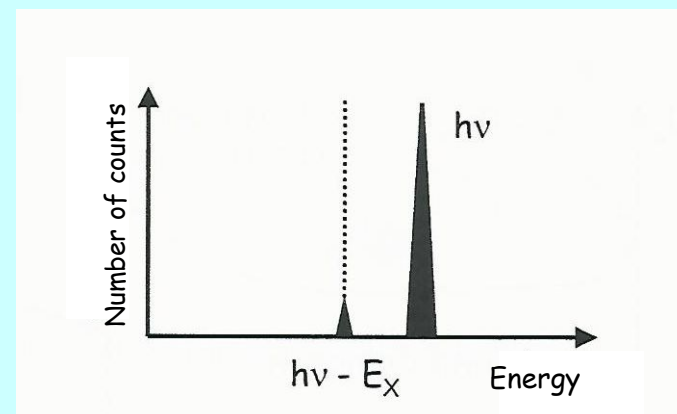
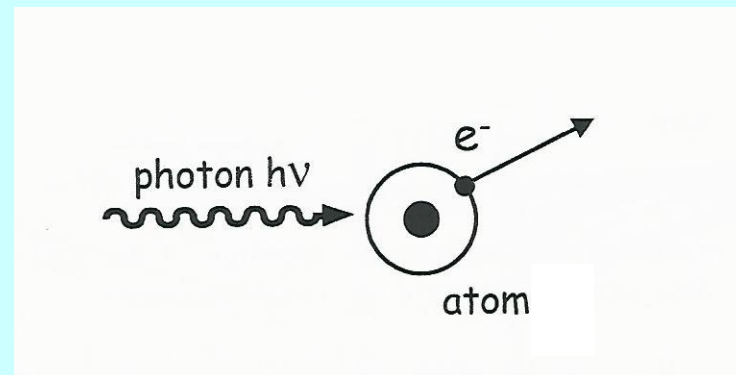
$$E_\gamma = h\nu$$

$$E_{e^-} = h\nu - B_{e^-}$$

$$\sigma_{\text{photo}} \sim (h\nu)^{-3,5} \cdot Z^5$$

Fast cross section reduction with energy

Strongly depend of Z of material/detector



# Radiation-matter interactions and detectors

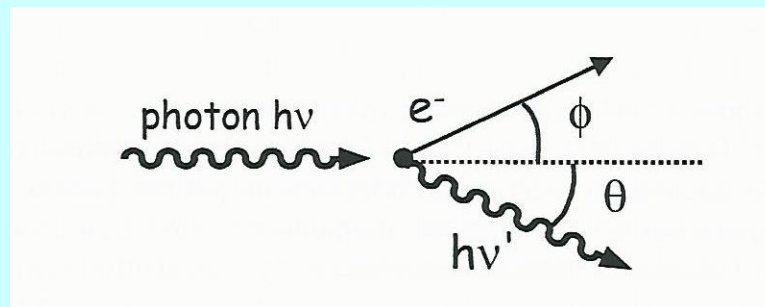
## γ rays

### ➤ Compton effect

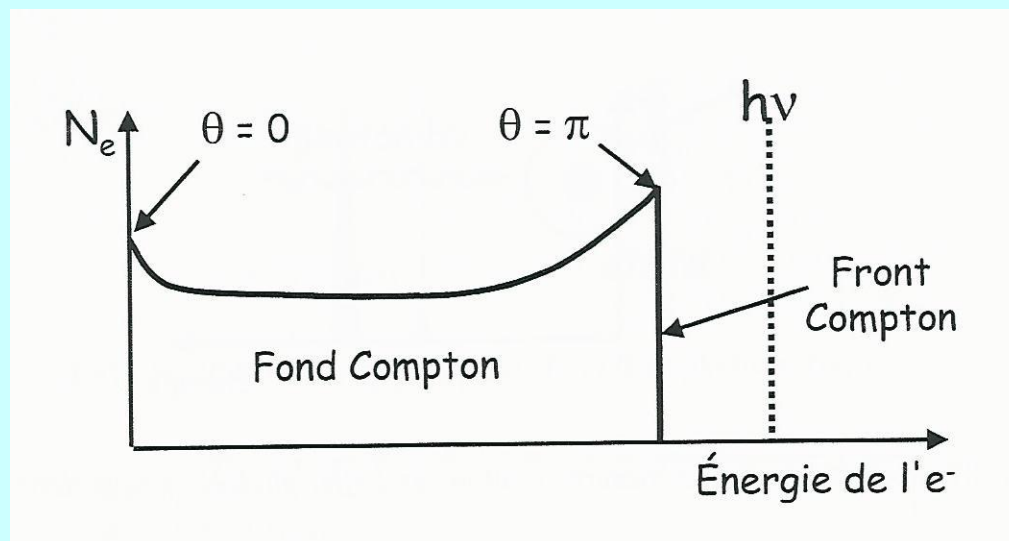
- Elastic scattering of a photon on a quasi-free electron

$$h\nu' = \frac{h\nu}{1 + \frac{h\nu}{m_e c^2} (1 - \cos \theta)}$$

$$E_{e^-} = h\nu - h\nu'$$



The electron energy varies continuously with  $\theta$



# Radiation-matter interactions and detectors

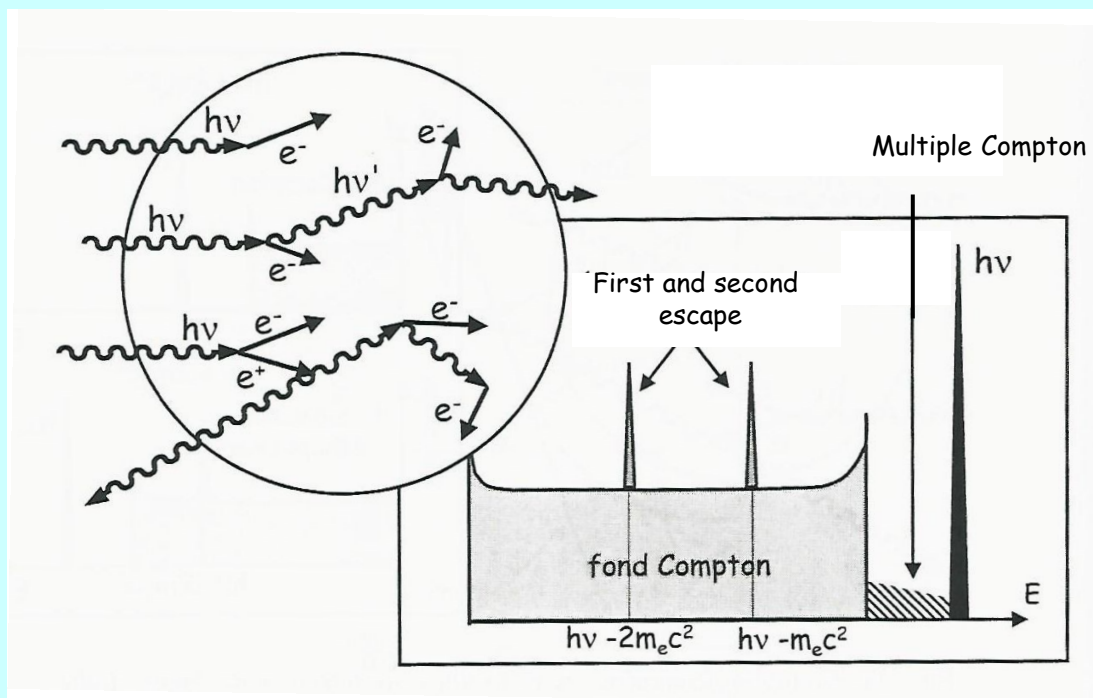
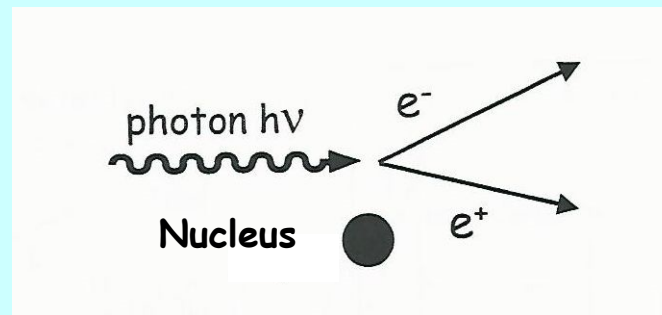
## $\gamma$ rays

### ➤ Pair creation

- A photon is materialised in one electron and one positron

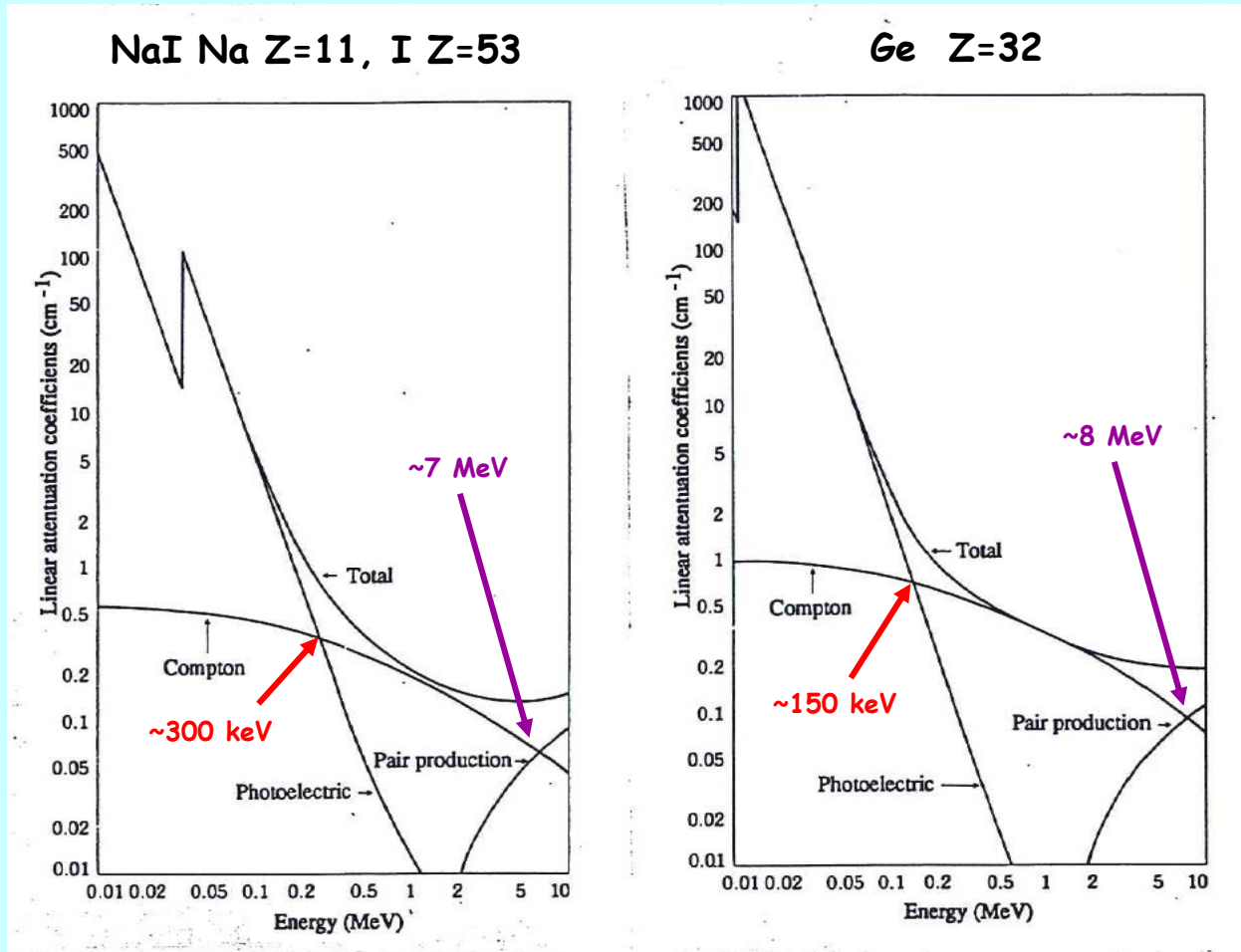
$$h\nu > 2 m_e c^2 (1,022 \text{ MeV})$$

$$E_{e^-} = E_{e^+} = \frac{1}{2}(h\nu - 2 m_e c^2)$$



## $\gamma$ rays

- Total absorption coefficient  $\mu = \mu_{\text{Photoelectric}} + \mu_{\text{Compton}} + \mu_{\text{Pair creation}}$

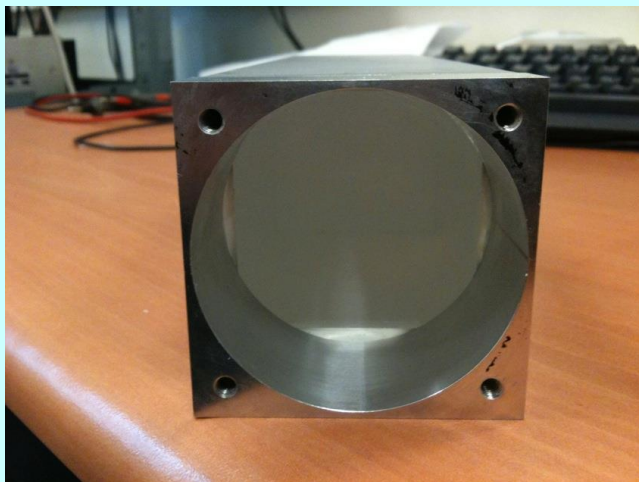
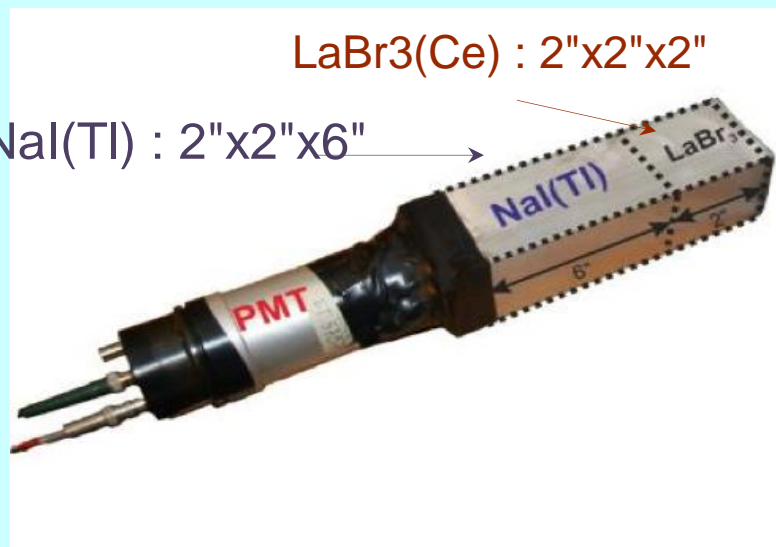


# Radiation-matter interactions and detectors

## $\gamma$ rays

### ➤ Gamma-ray detectors

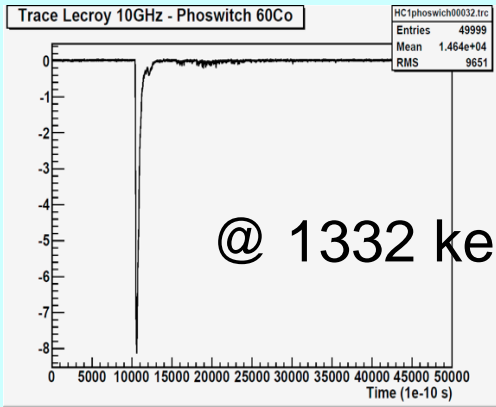
- ❑ Scintillators -> PARIS detector
- ❑ Phoswitch: front  $\text{LaBr}_3$  crystal  
back NaI crystal  
One photomultiplier (PMT)
- ❑ Large detection efficiency
- ❑ Fast timing response and good energy resolution ( $\text{LaBr}_3$ )



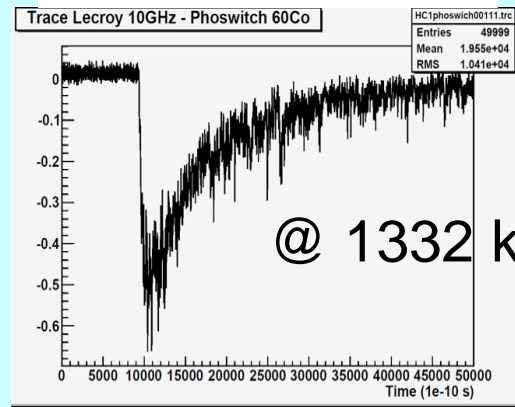
## $\gamma$ rays

- Gamma-ray detectors
  - ❑ PARIS detector performance

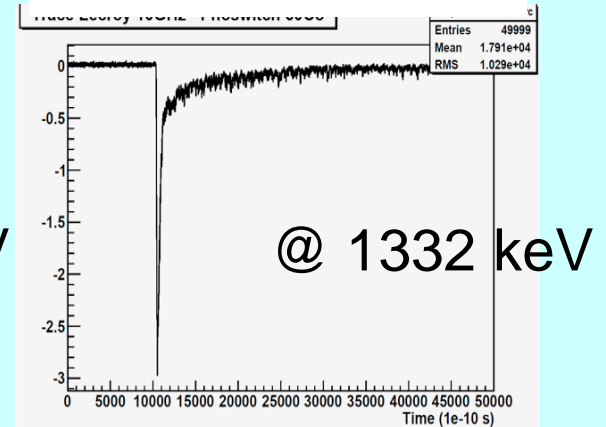
$\gamma$  interaction in LaBr<sub>3</sub>  
only



$\gamma$  interaction in NaI  
only

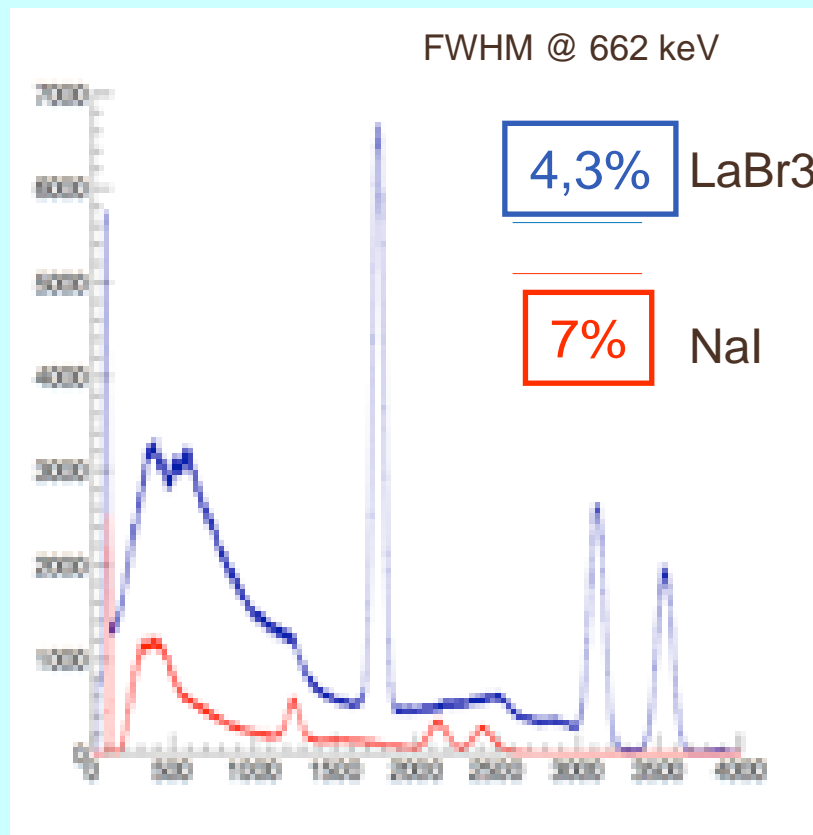
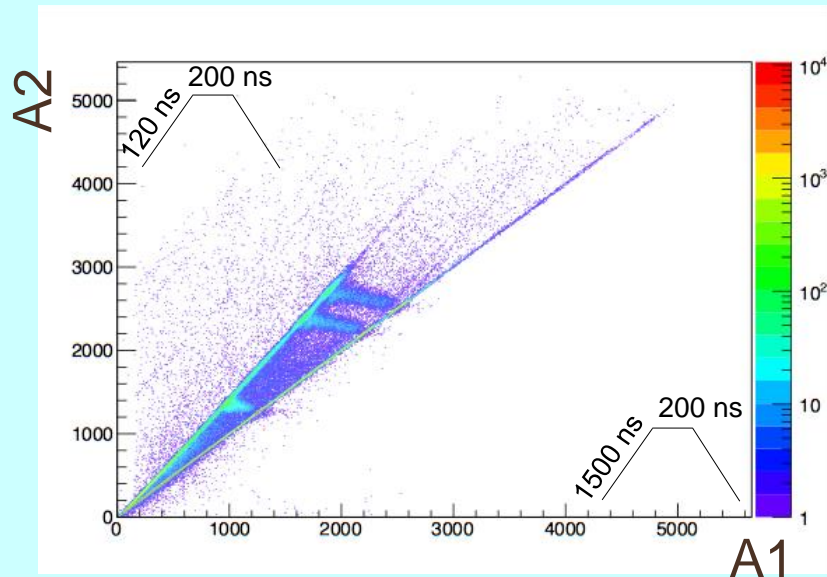


$\gamma$  interaction in both  
shells



## $\gamma$ rays

- Gamma-ray detectors
  - ❑ PARIS detector performance using digital electronics

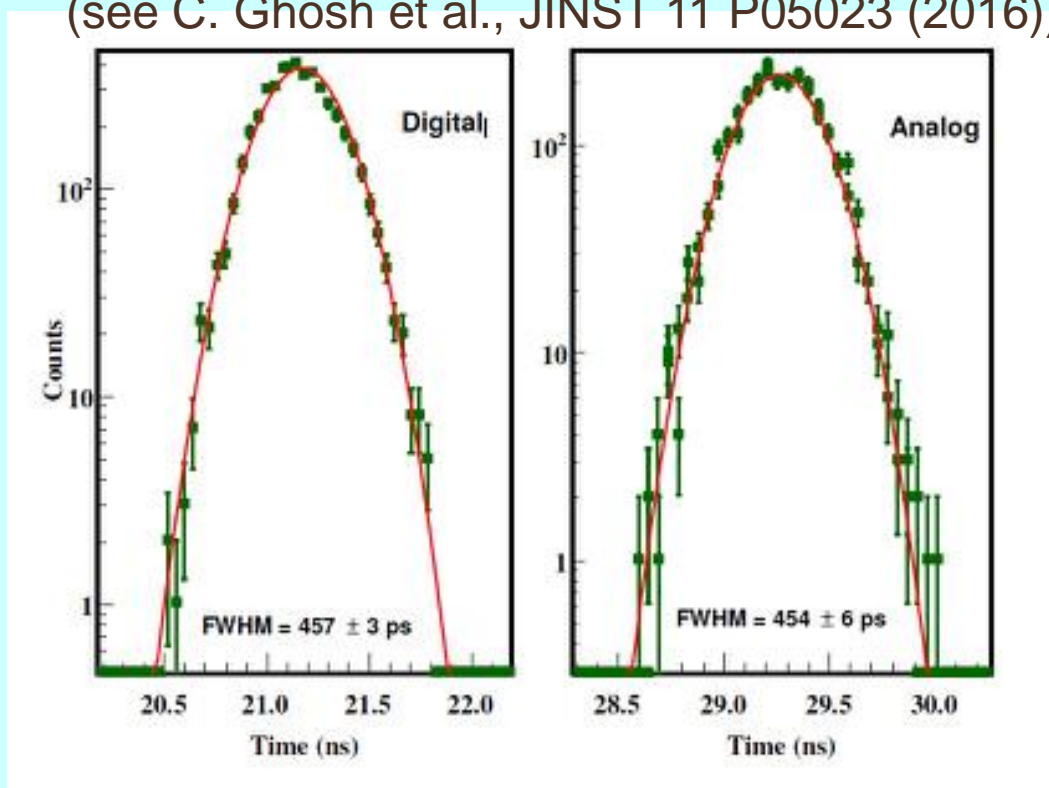




## $\gamma$ rays

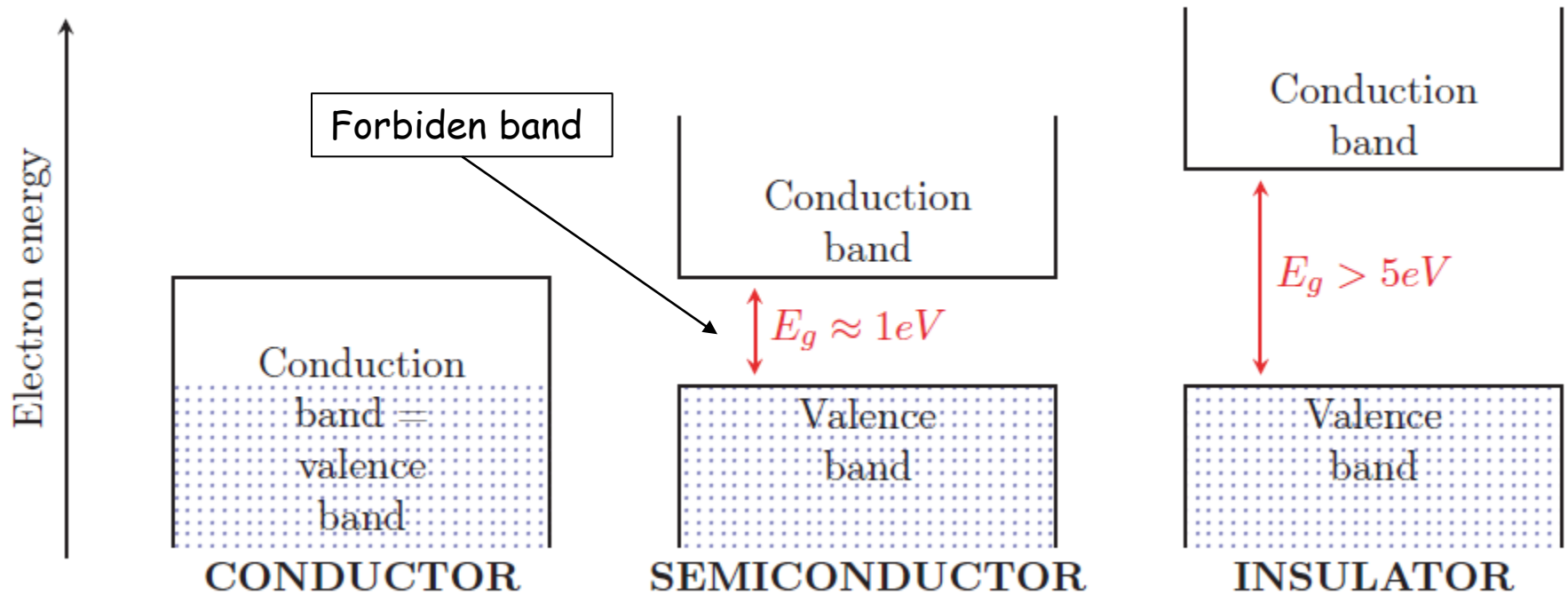
- Gamma-ray detectors
  - ❑ PARIS detector timing performance

(see C. Ghosh et al., JINST 11 P05023 (2016))



## $\gamma$ rays

- Gamma-ray detectors
  - ❑ Semiconductors (Si, Ge)



## γ rays

- Gamma-ray detectors
  - ❑ Semiconductors characteristics

Semiconductors	Forbidden band at 300 K	Electron-hole pair creation energy W
Si	1.12 eV	3.61 eV (300 K)
Ge	0.67 eV	2.96 eV (90 K)
Diamant C	5.47 eV	13.2 eV (300K)
GaAs	1.43 eV	4.27 eV
CdTe	1.5 eV	4.43 eV (300 K)
HgI <sub>2</sub>	2.1 eV	4.15 eV

$$N = E_{\gamma} / W$$

for Ge and a 1 MeV γ ray

$N > 300\,000$  pairs e-h

**Good energy resolution**

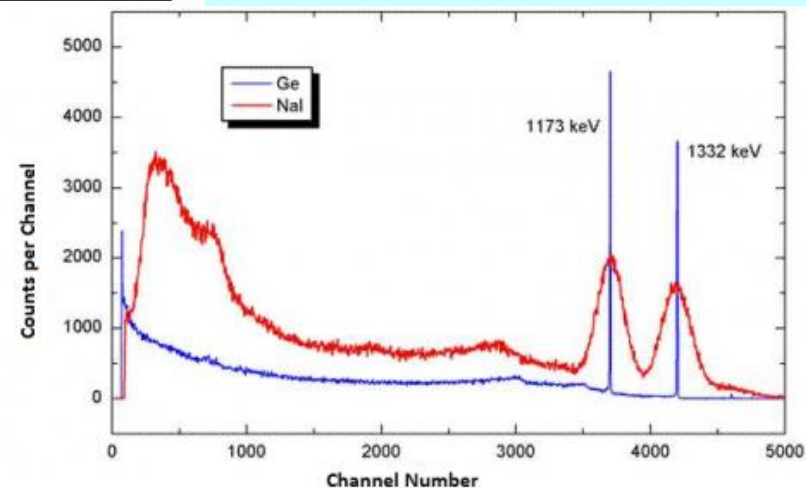
FWHM = Full Width Half Maximum

FWHM (NaI) / E ~ 8%

FWHM (LaBr<sub>3</sub>) / E ~ 3-4%

FWHM (<sup>14</sup>Si) / E ~ 1.5% → X rays

FWHM (<sup>32</sup>Ge) / E ~ 0.2% → γ rays

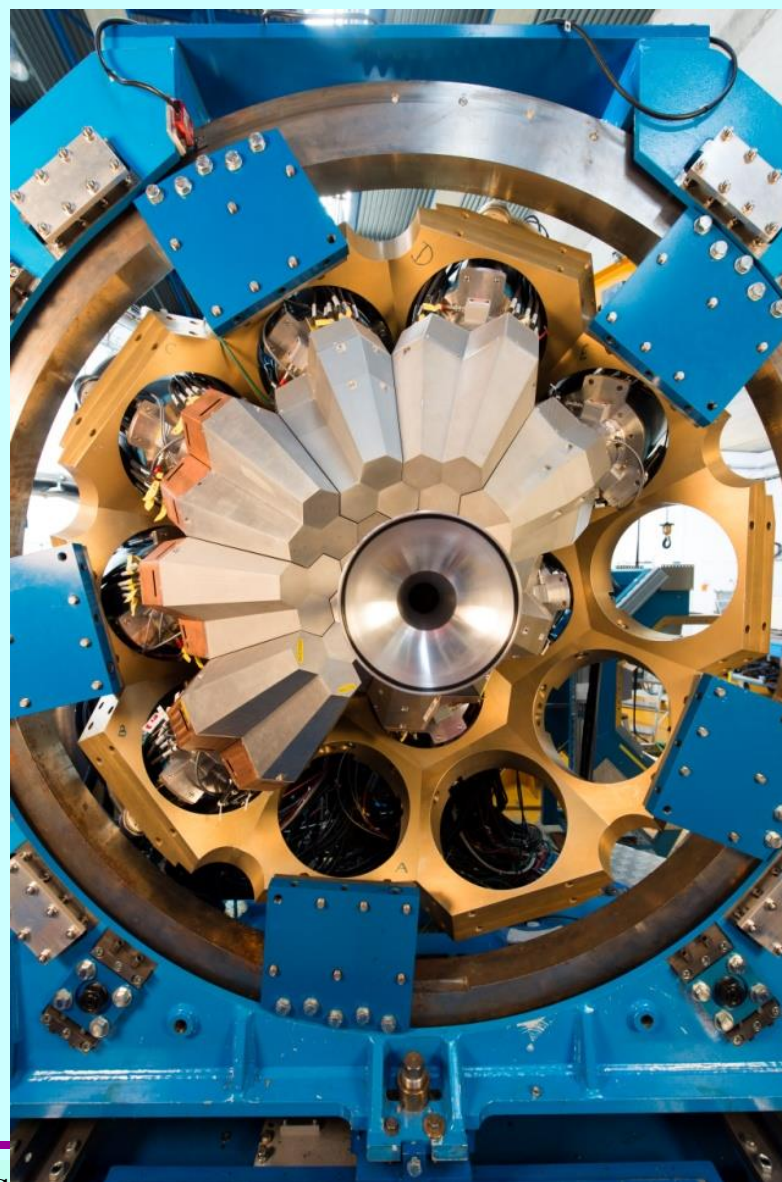
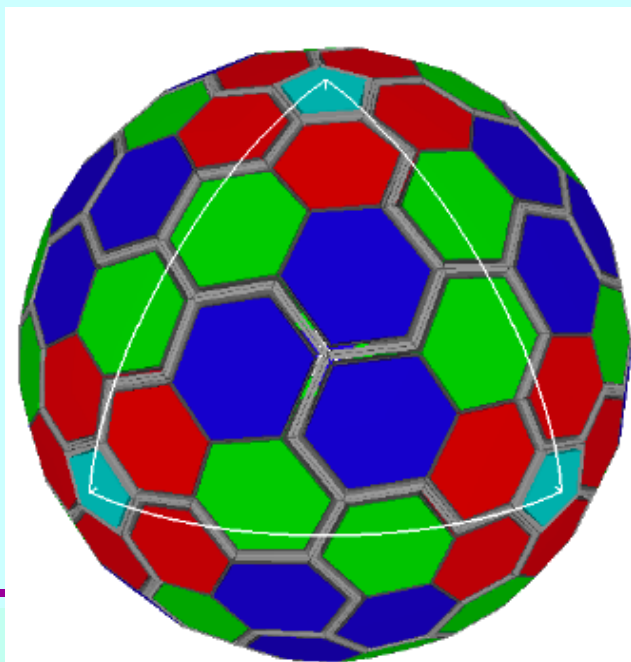


# Multi-detector AGATA for $\gamma$ -ray detection

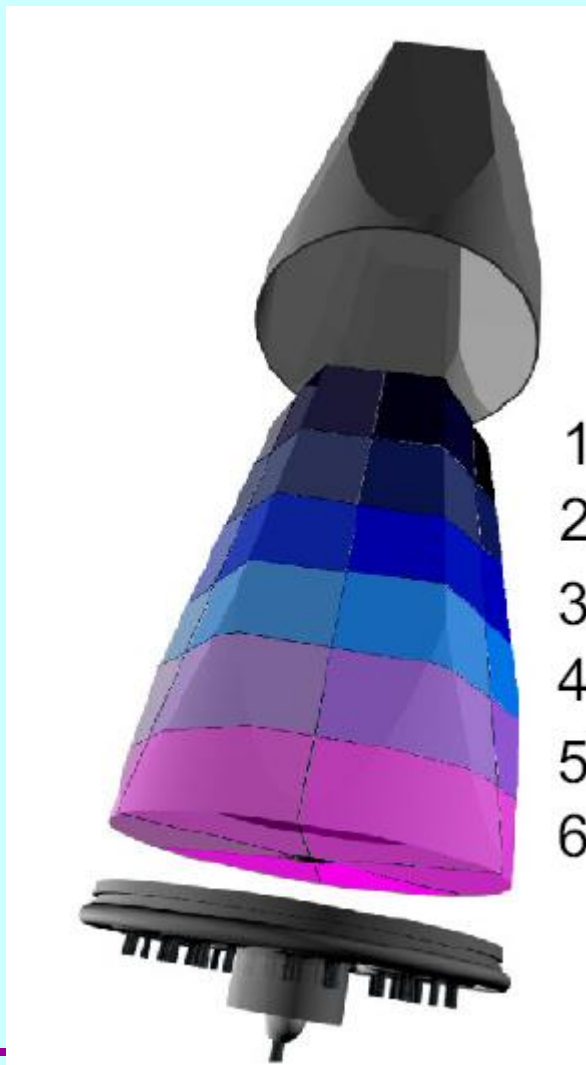
Solely composed of Ge crystals

Pulse-shape analysis +  $\gamma$ -ray tracking

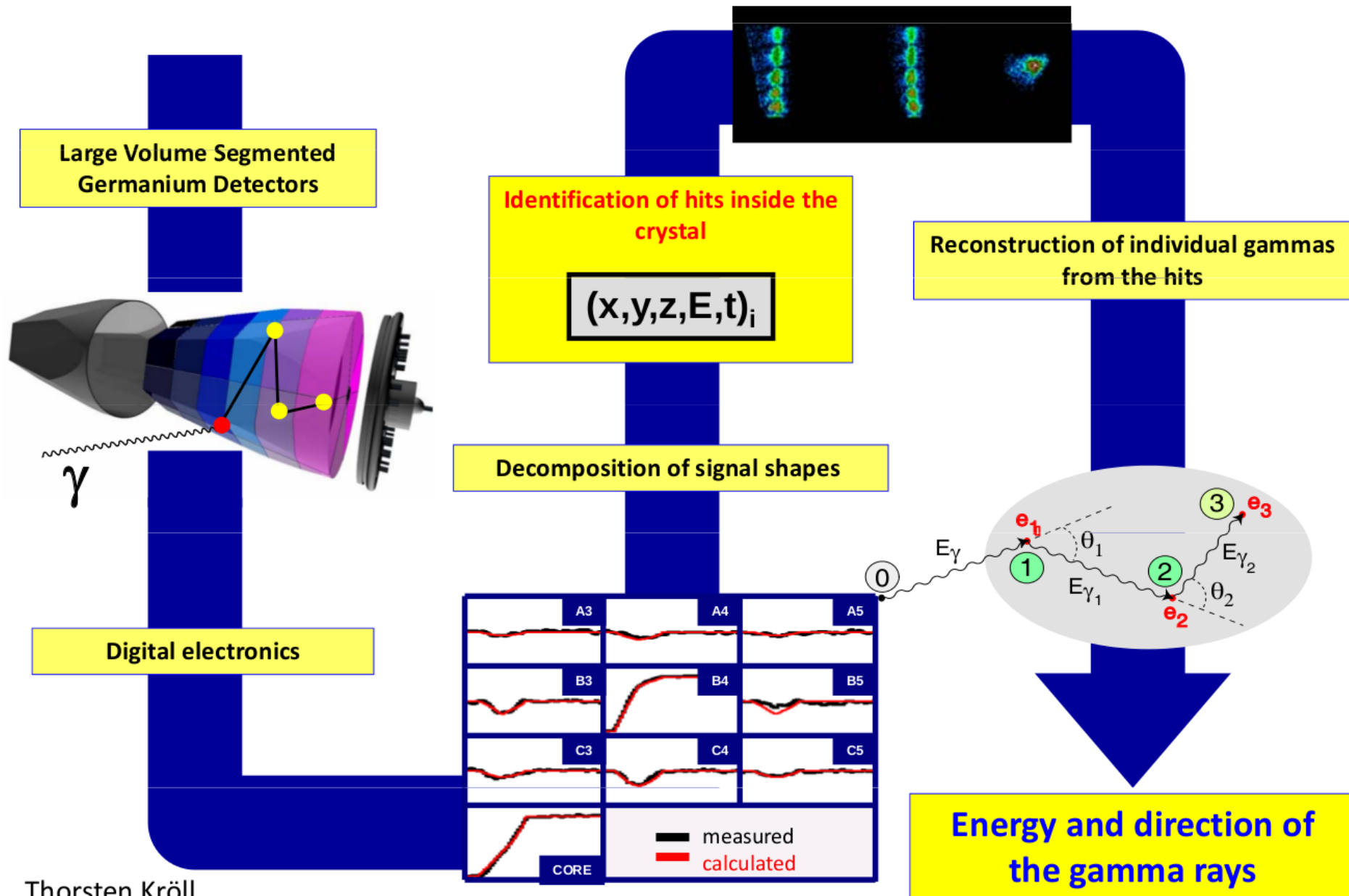
- Today: 35 Ge crystals each segmented in 36+1 (1295 channels)
- In 2030: 180 crystals (6660 channels)



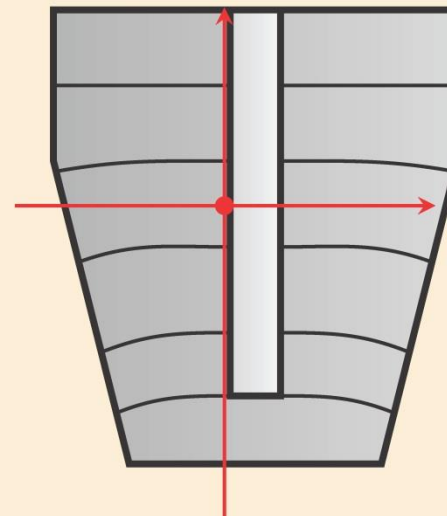
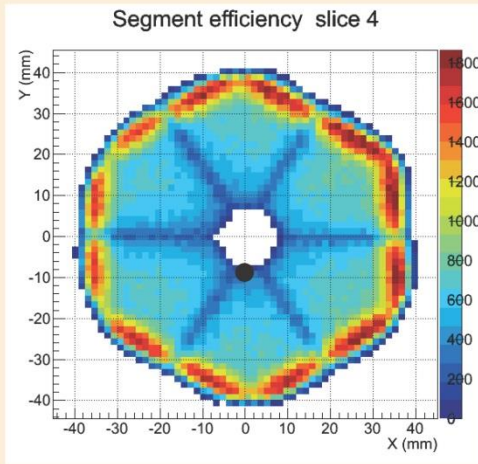
# Multi-detector AGATA for $\gamma$ -ray detection



# Gamma-Ray Tracking Paradigm

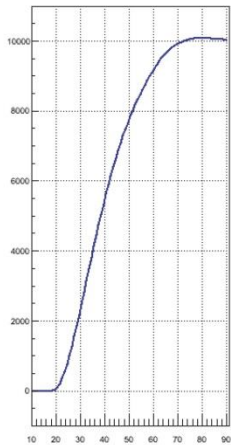


3D partial PSCS

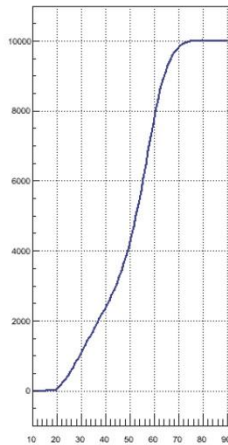


( 0 ; -6.5 ; 50 )

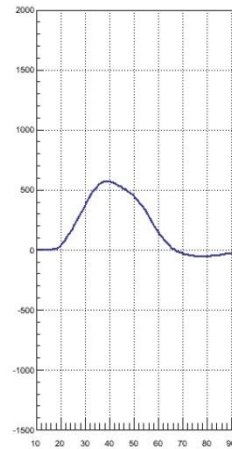
Core



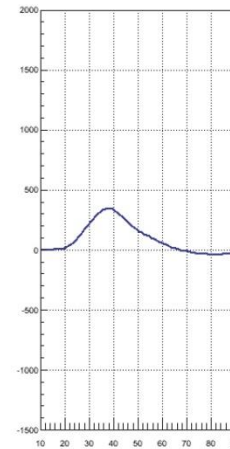
Segment hit



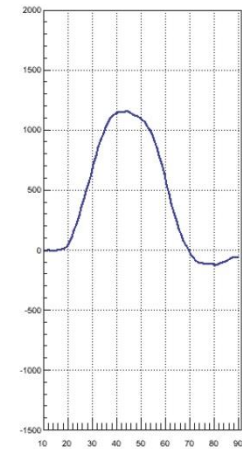
Left seg.



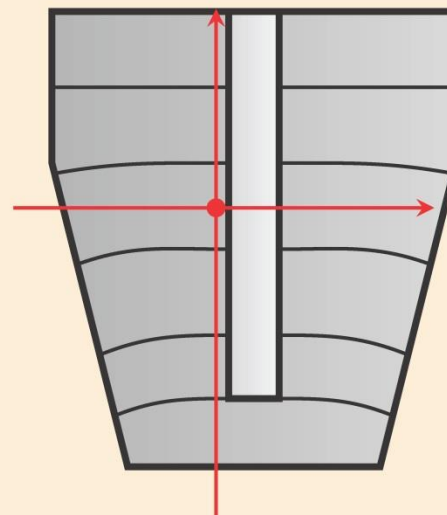
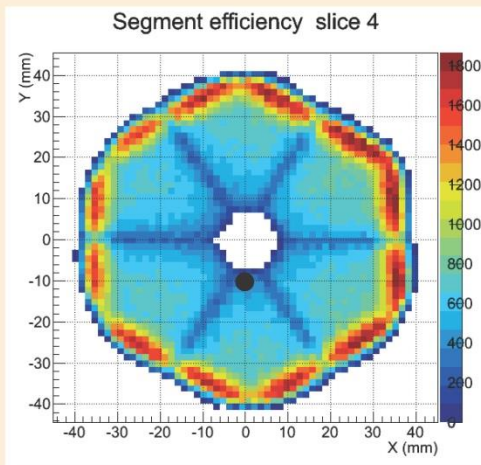
Right seg.



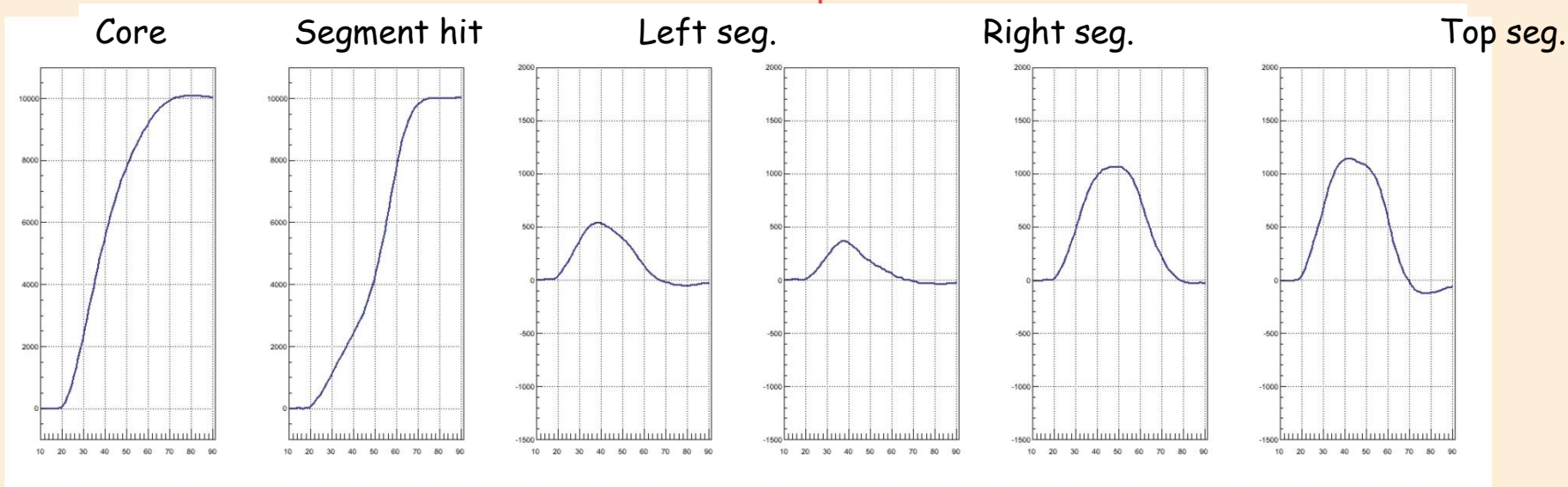
Top seg.



# 3D partial PSCS

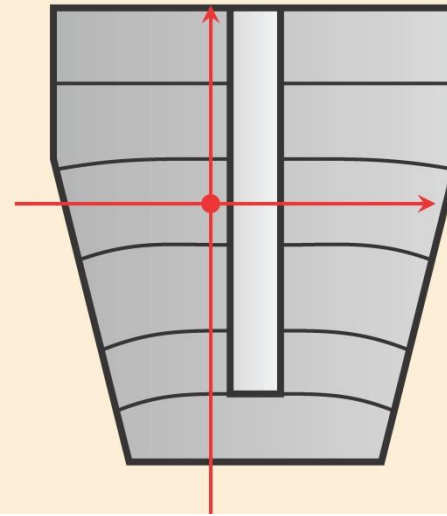
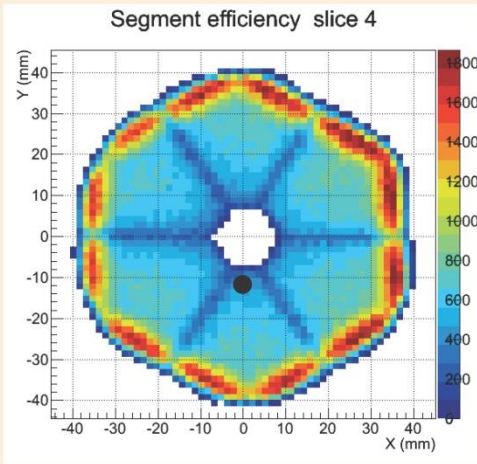


( 0 ; -8.0 ; 50)



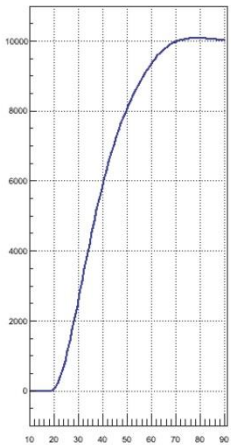


3D partial PSCS

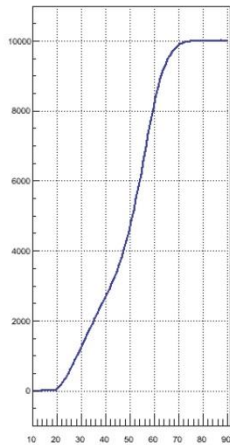


( 0 ; -9.5 ; 50 )

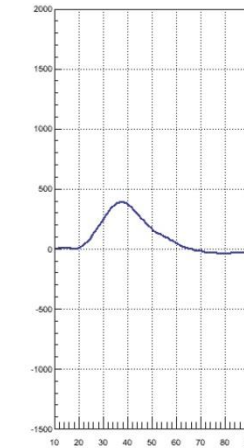
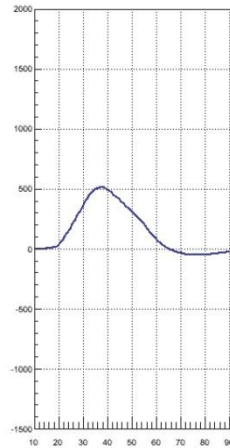
Core



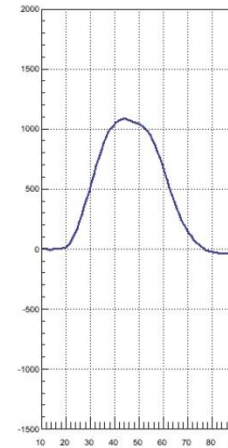
Segment hit



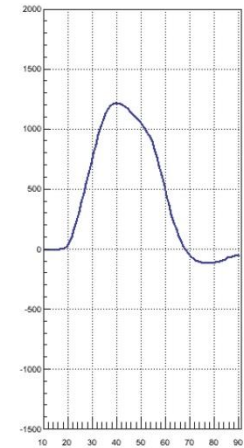
Left seg.



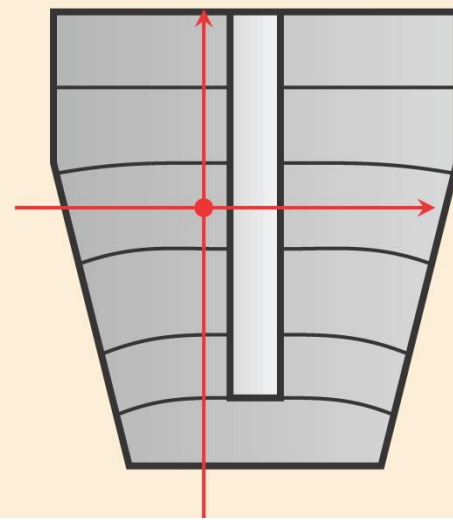
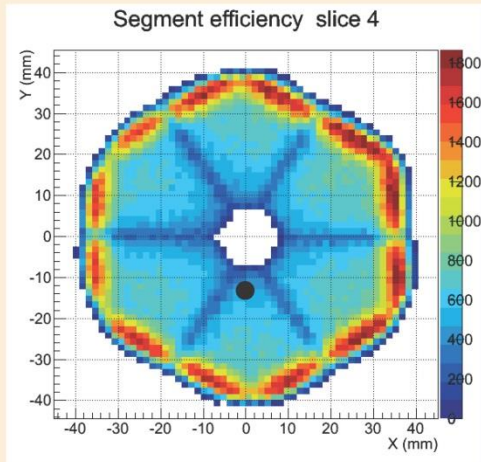
Right seg.



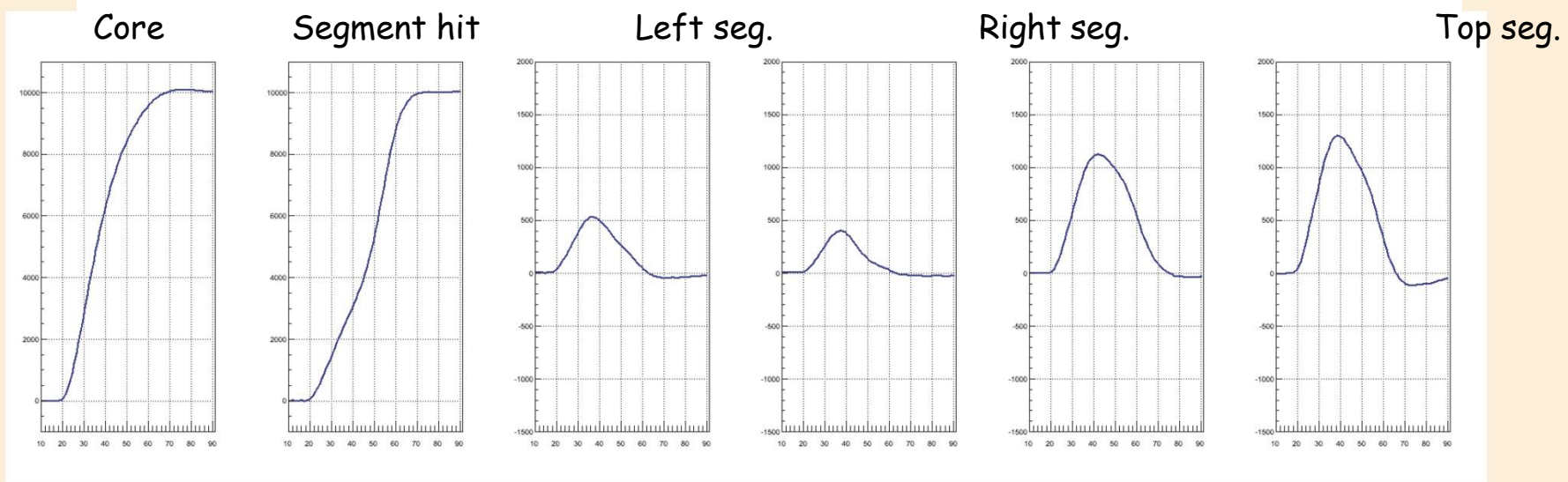
Top seg.



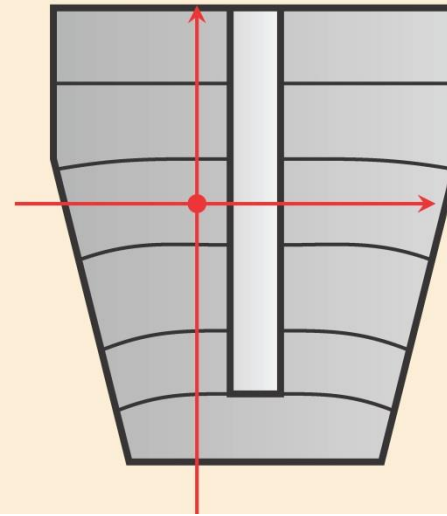
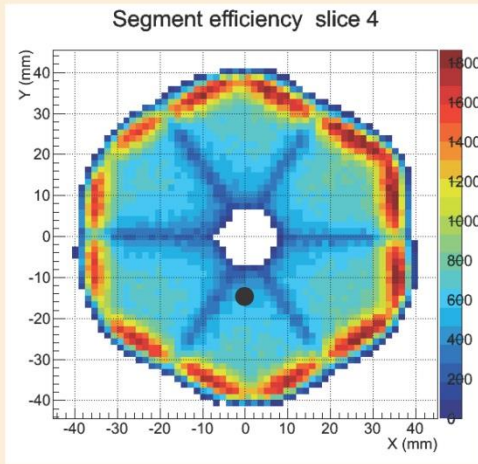
3D partial PSCS



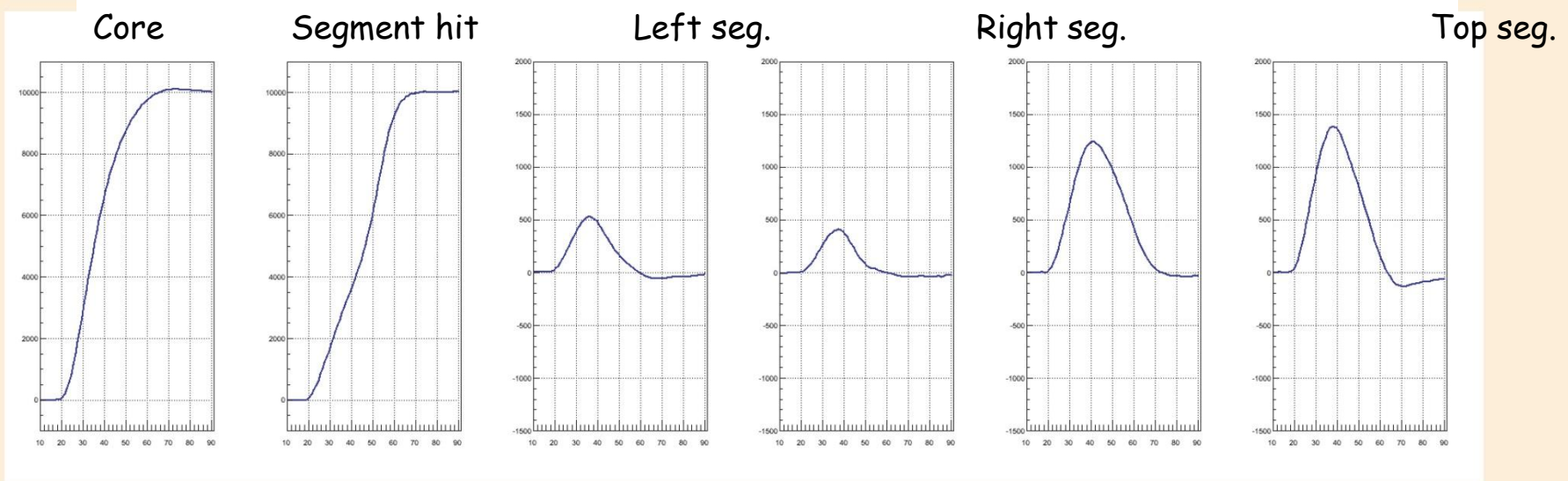
( 0 ; -11.0 ; 50 )



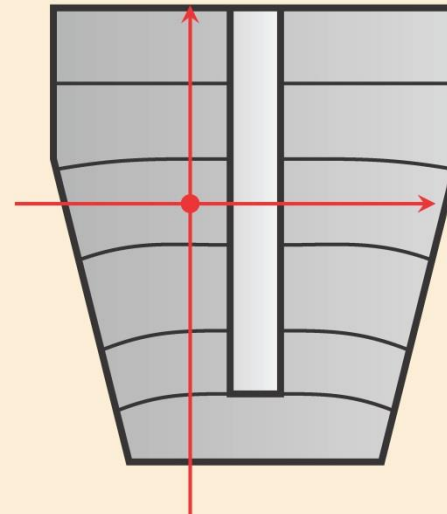
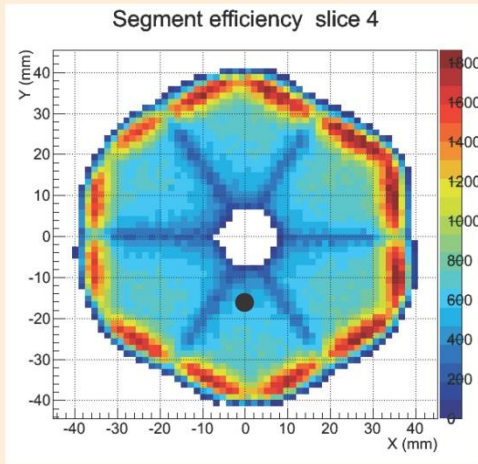
3D partial PSCS



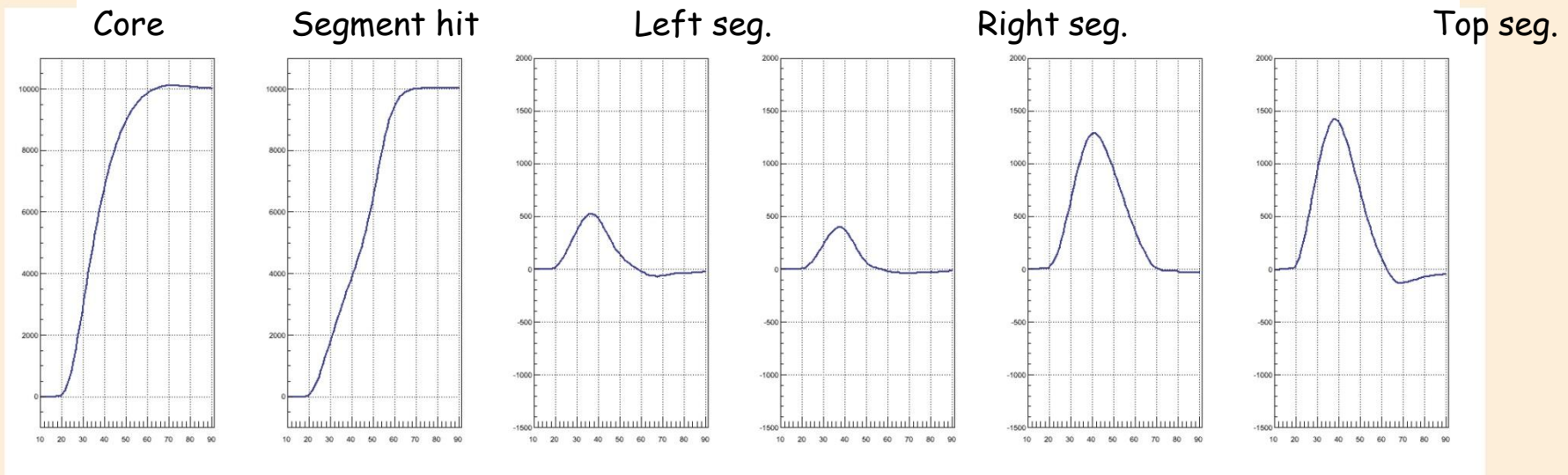
( 0 ; -12.5 ; 50)



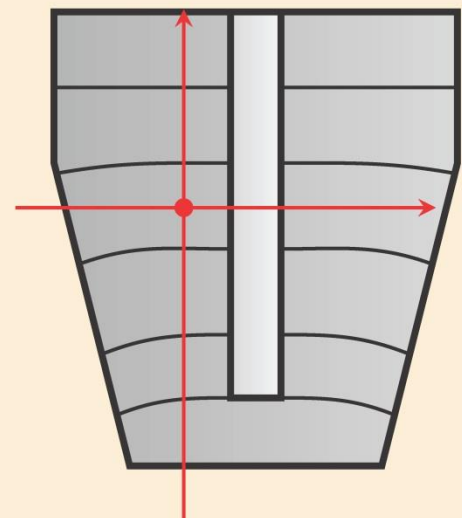
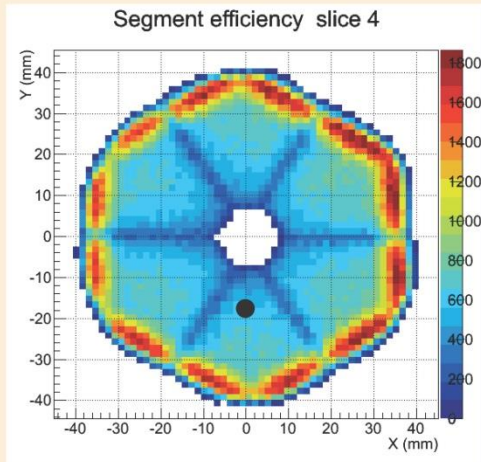
3D partial PSCS



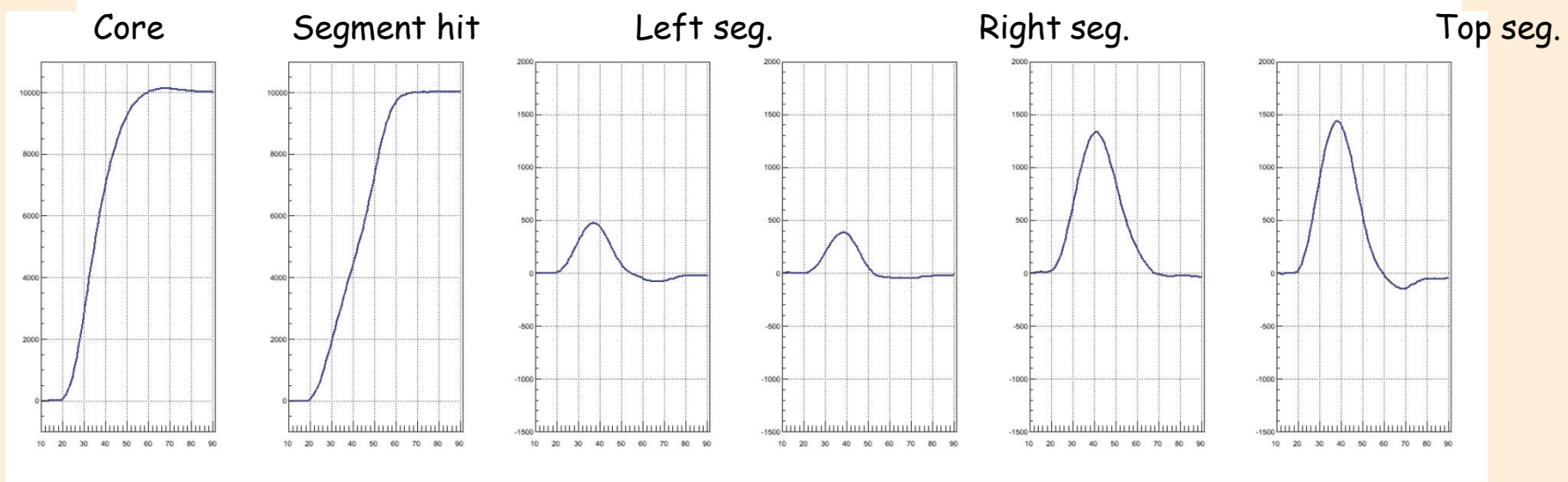
( 0 ; -14.0 ; 50)



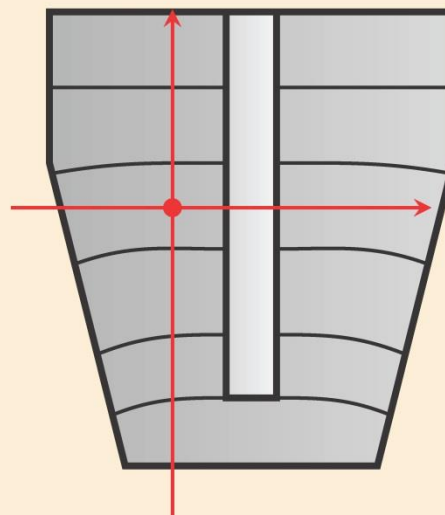
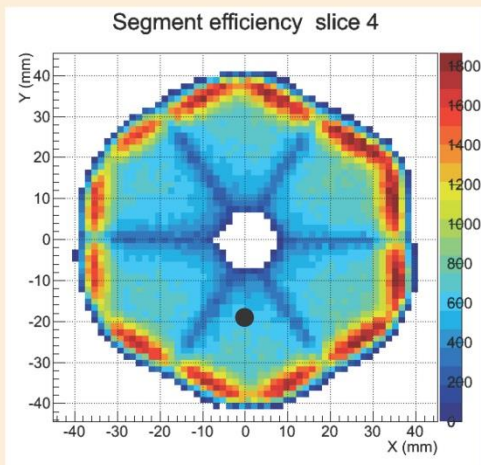
3D partial PSCS



( 0 ; -15.5 ; 50)

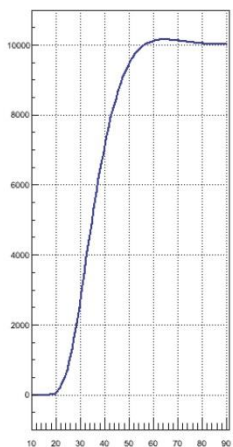


3D partial PSCS

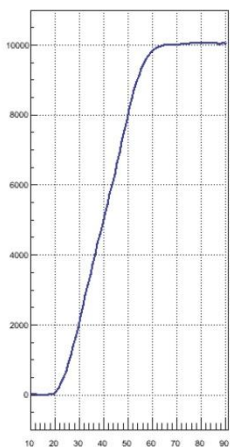


( 0 ; -17.0 ; 50)

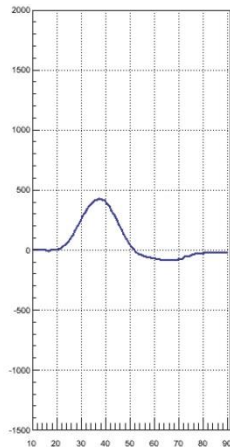
Core



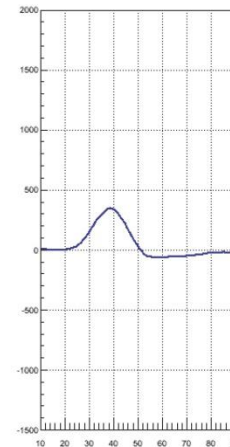
Segment hit



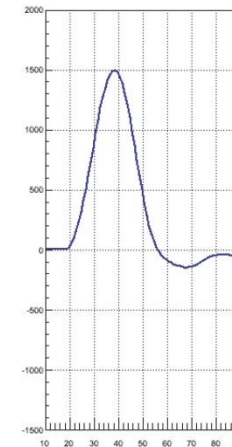
Left seg.



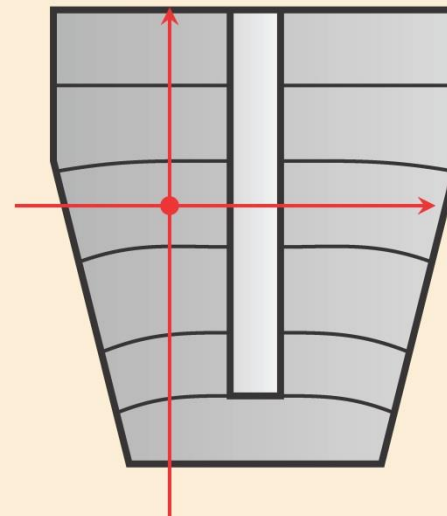
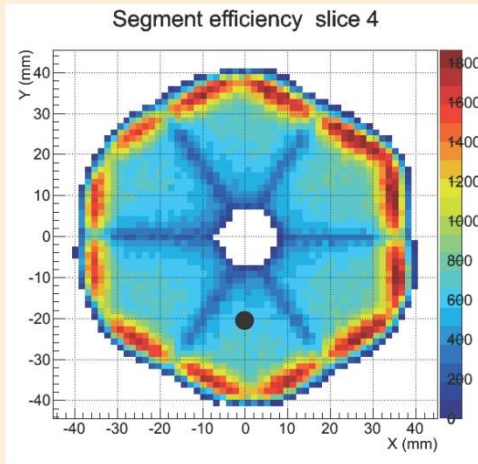
Right seg.



Top seg.

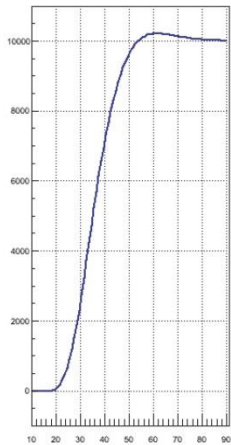


3D partial PSCS

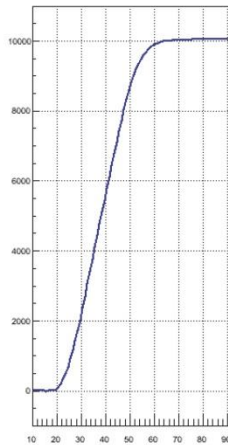


( 0 ; -18.5 ; 50)

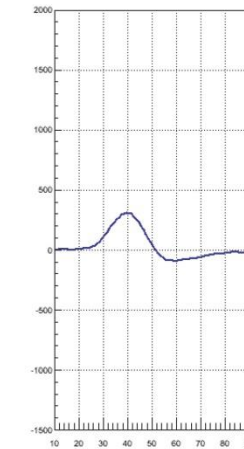
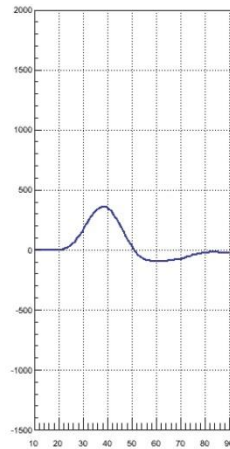
Core



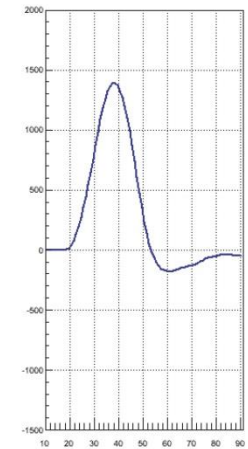
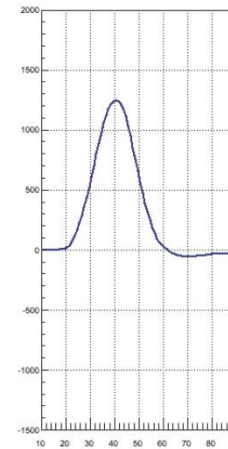
Segment hit



Left seg.

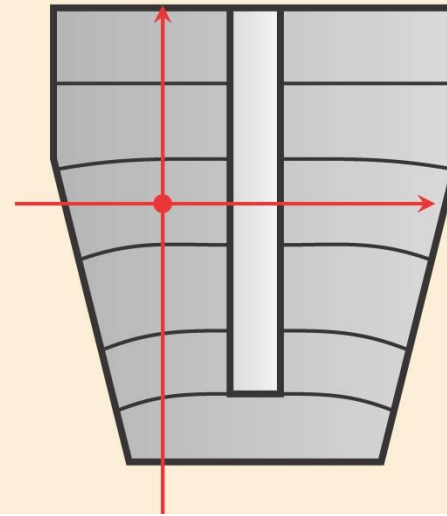
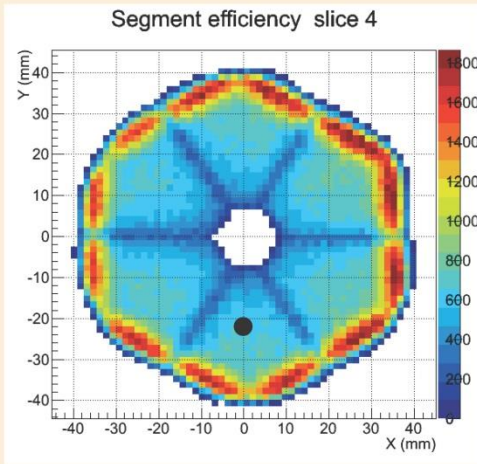


Right seg.

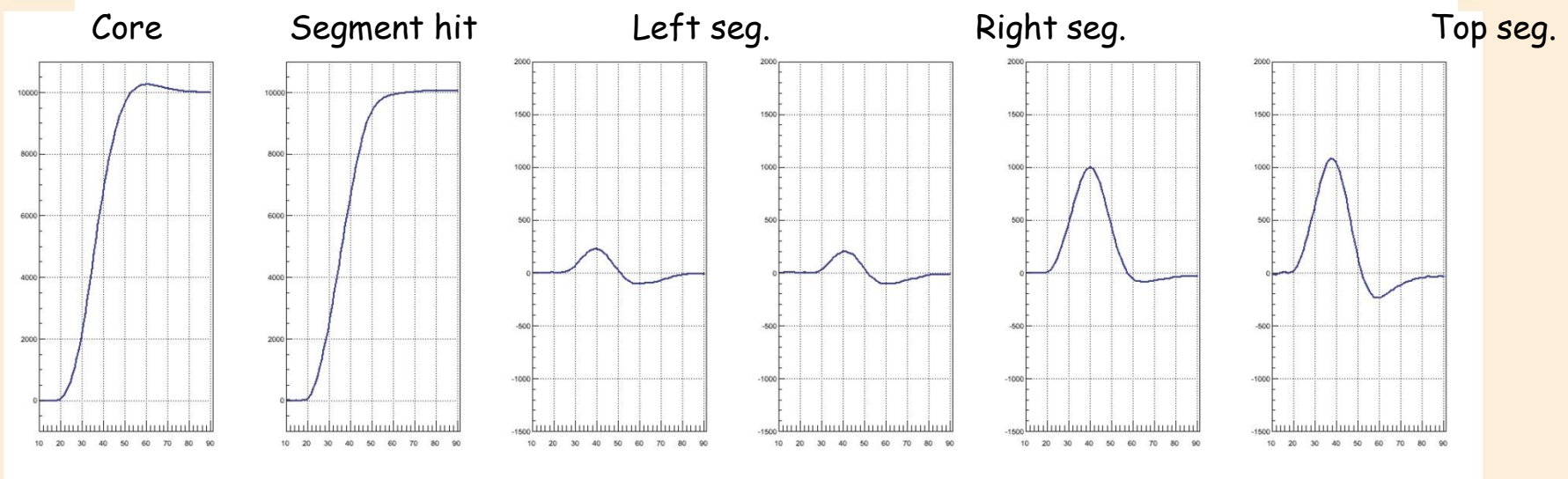


Top seg.

3D partial PSCS

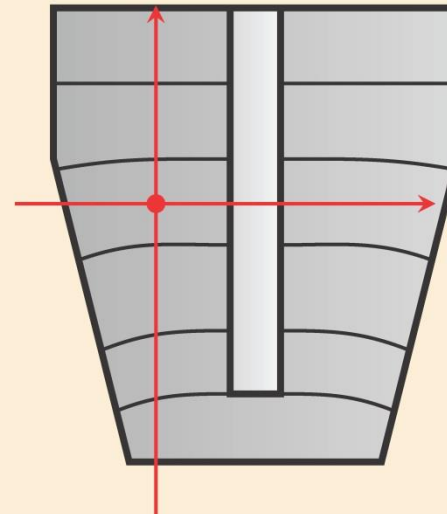
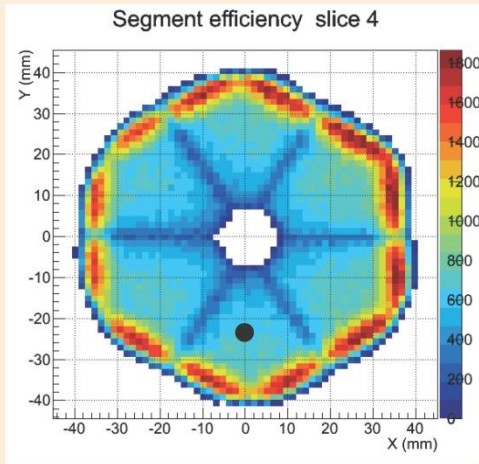


( 0 ; -20.0 ; 50)

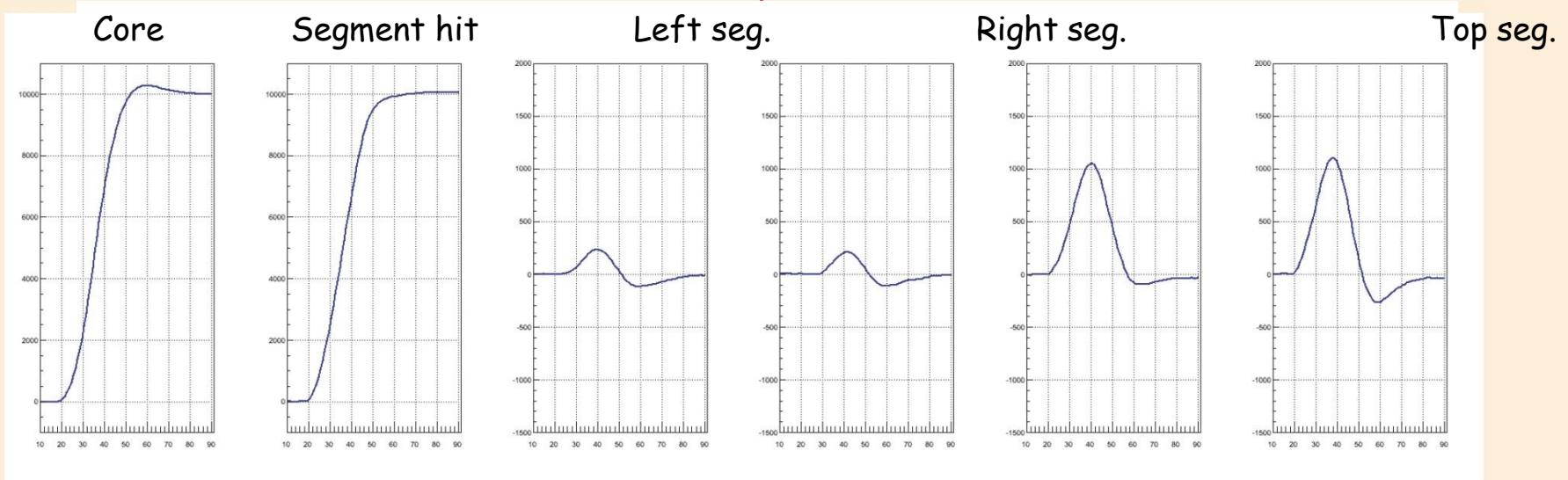




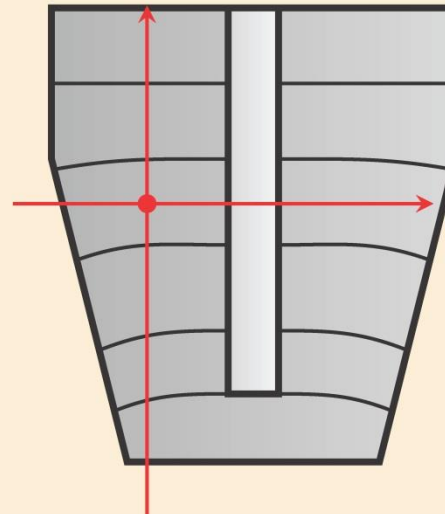
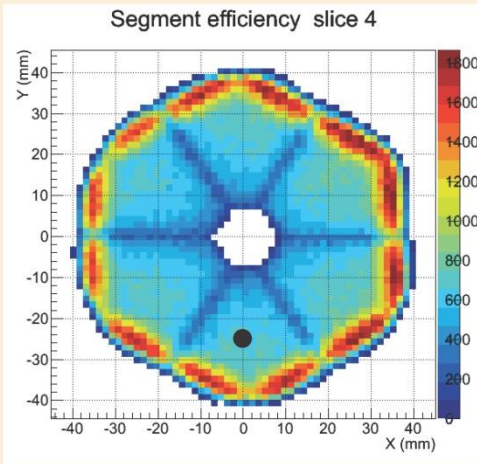
3D partial PSCS



( 0 ; -21.5 ; 50)

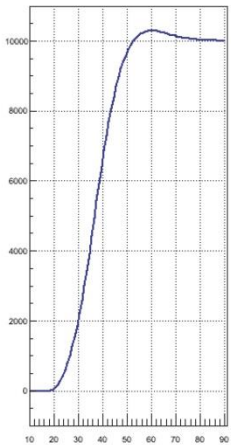


3D partial PSCS

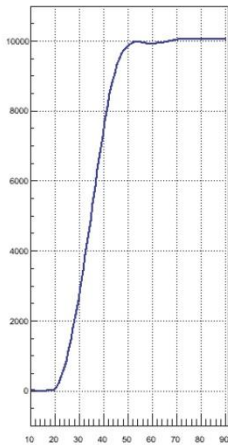


( 0 ; -23.0 ; 50)

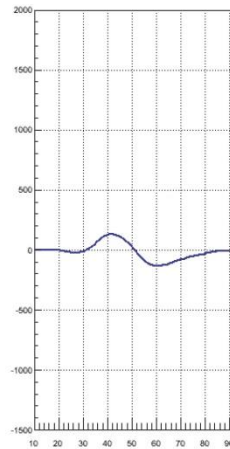
Core



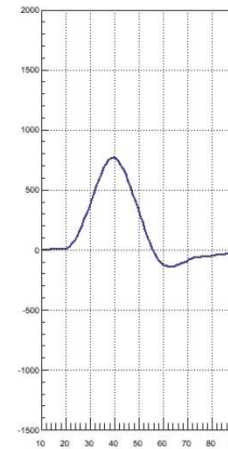
Segment hit



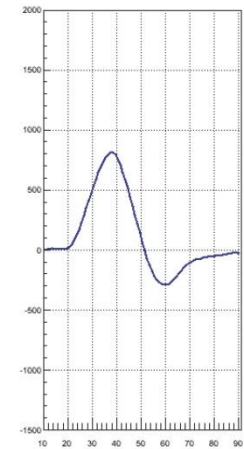
Left seg.



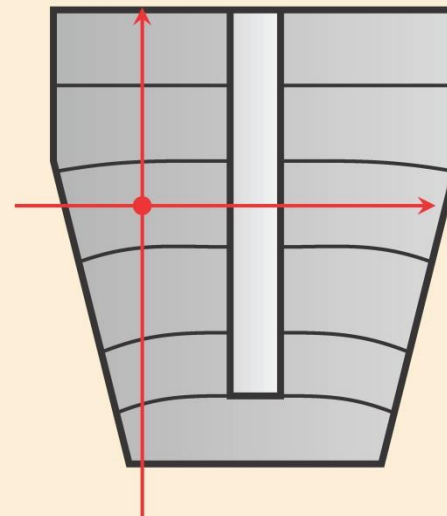
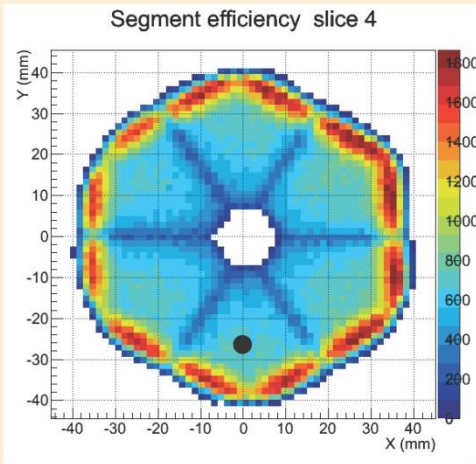
Right seg.



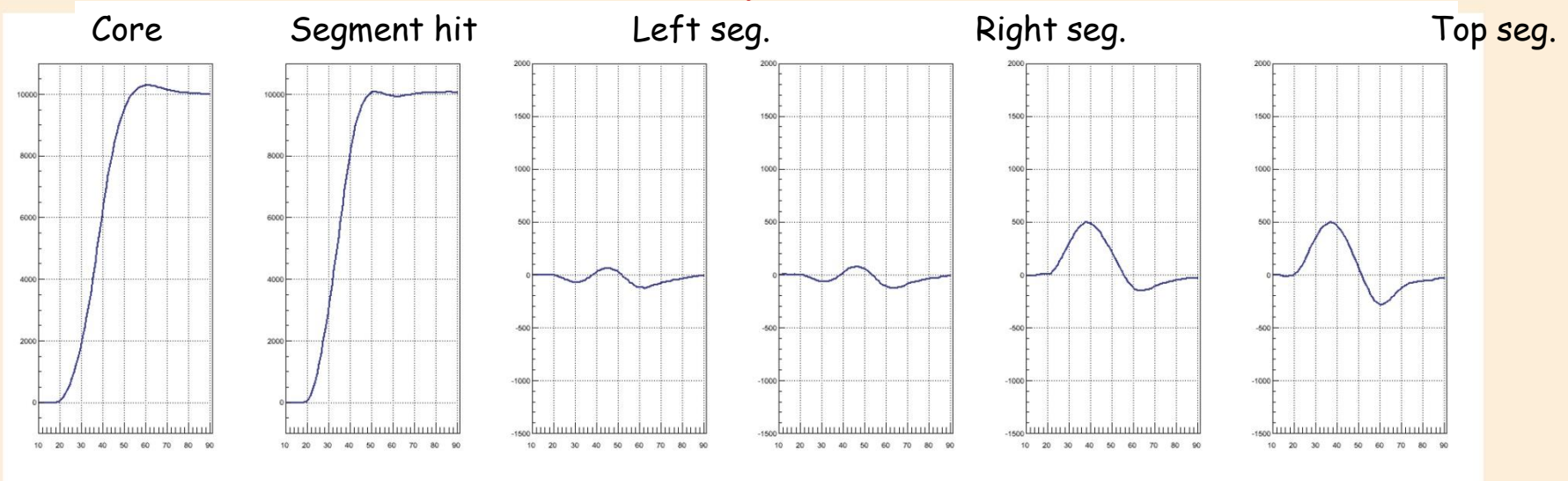
Top seg.



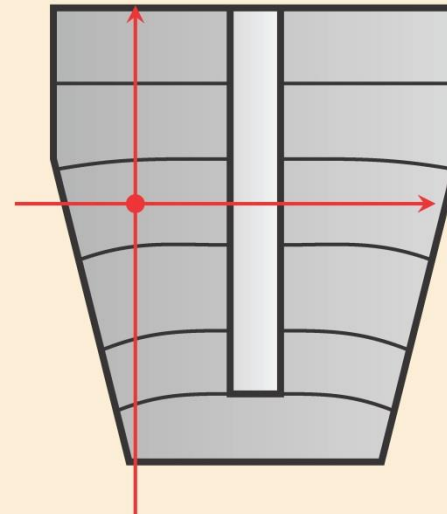
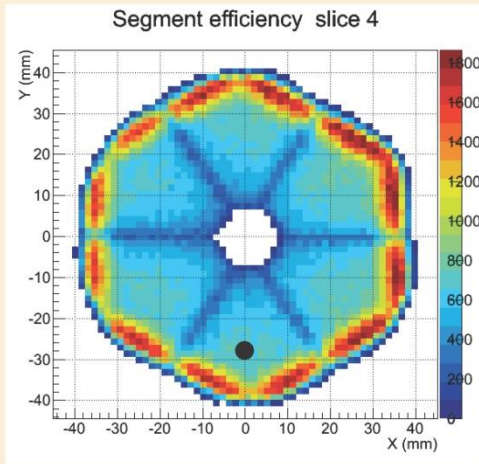
3D partial PSCS



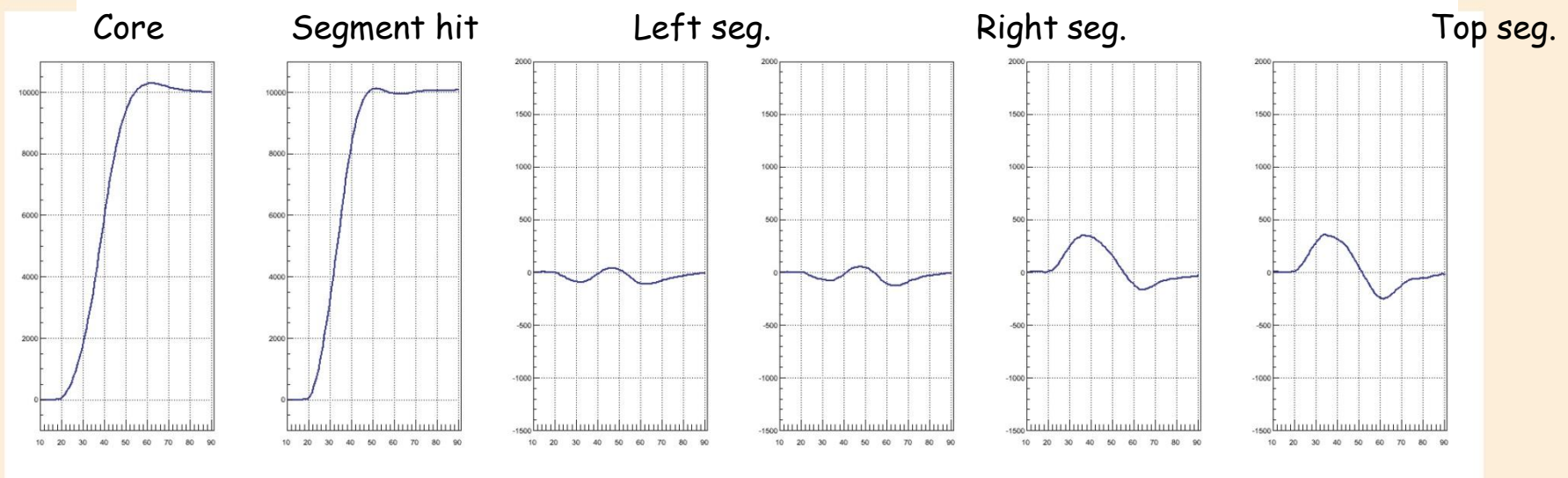
( 0 ; -24.5 ; 50)



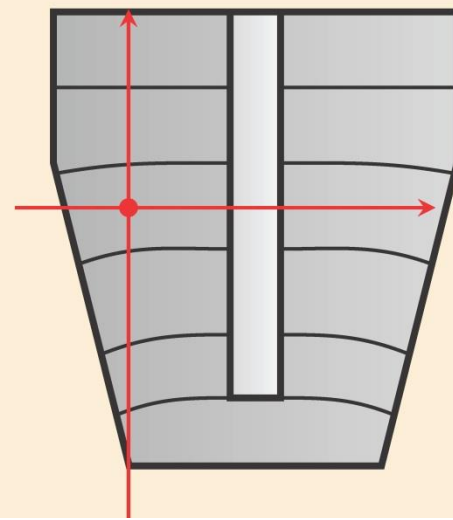
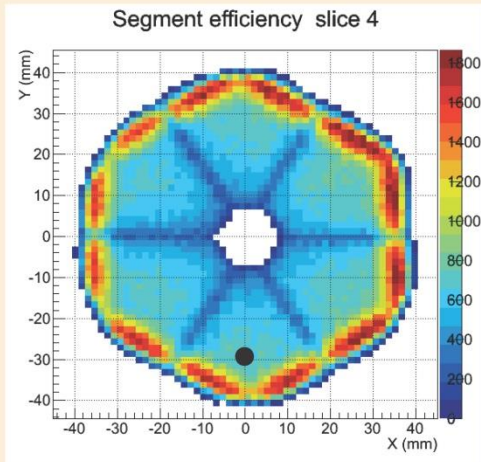
3D partial PSCS



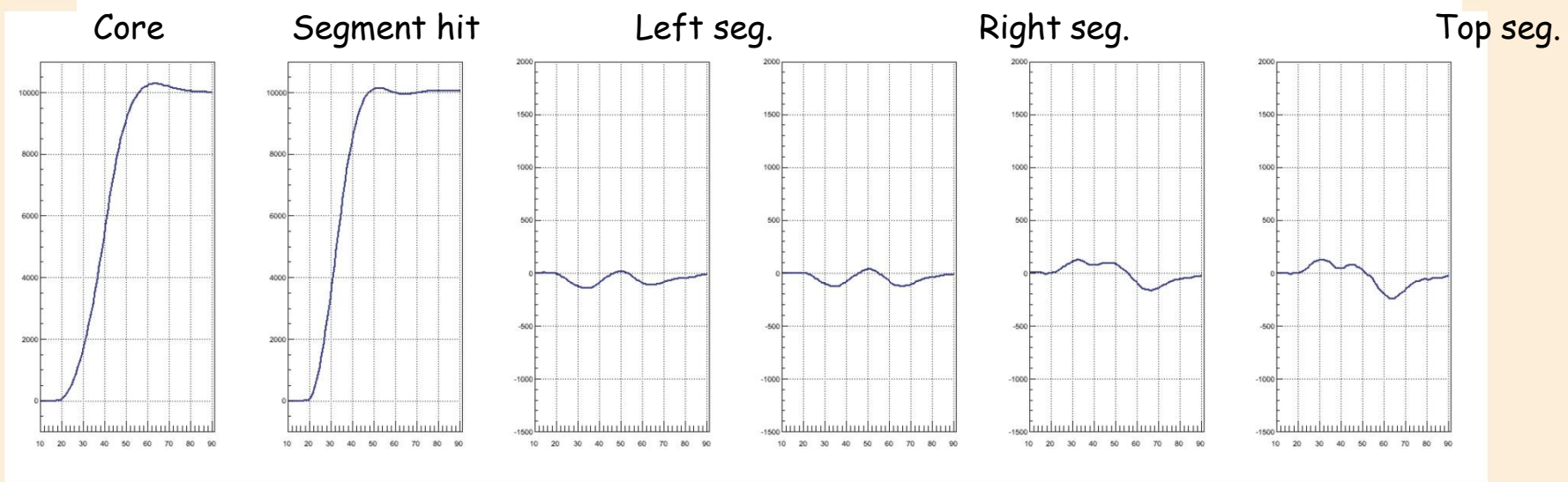
( 0 ; -26.0 ; 50)



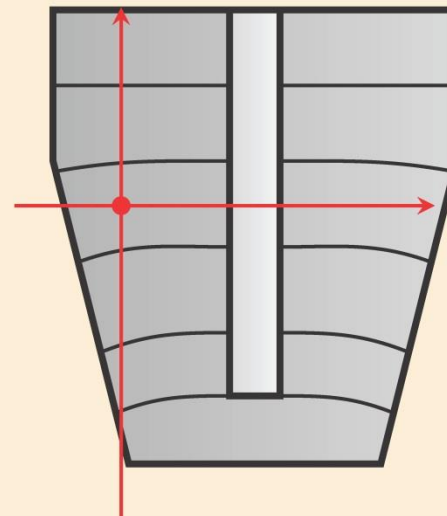
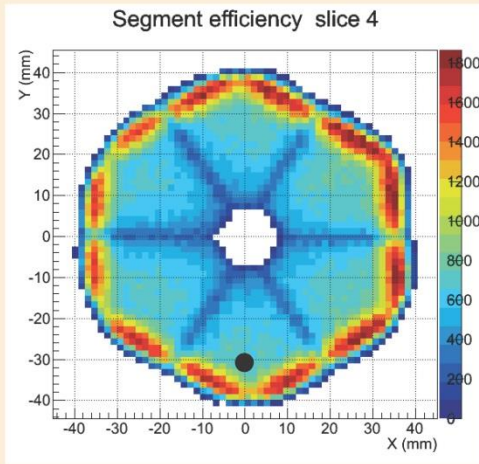
# 3D partial PSCS



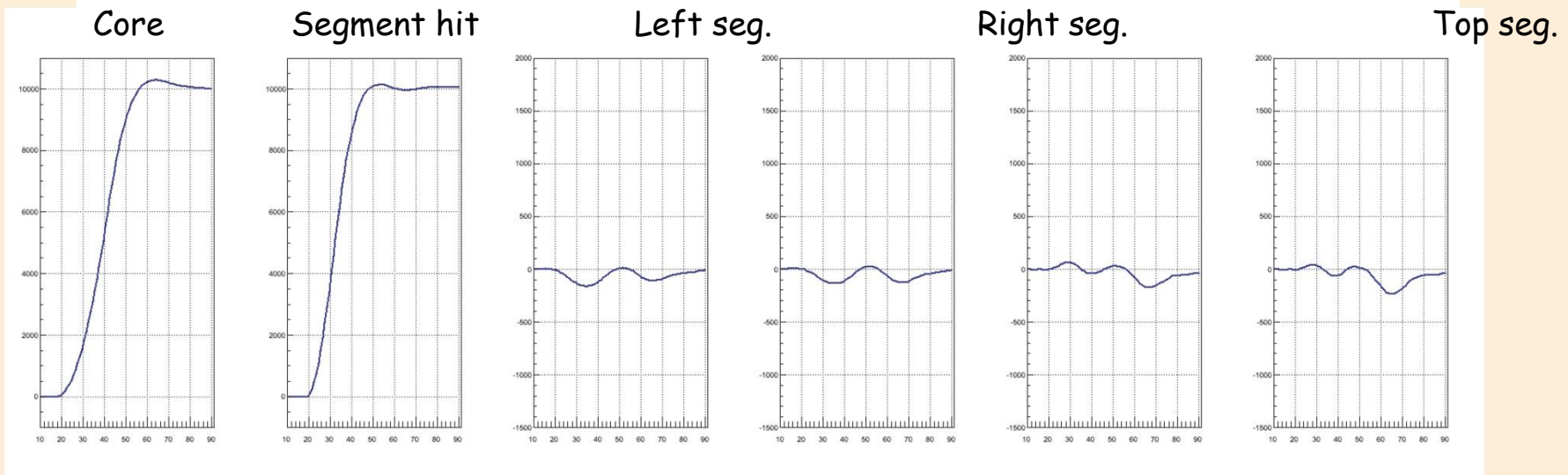
( 0 ; -27.5 ; 50)



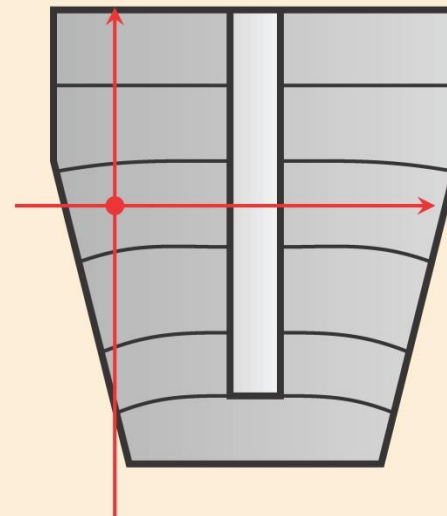
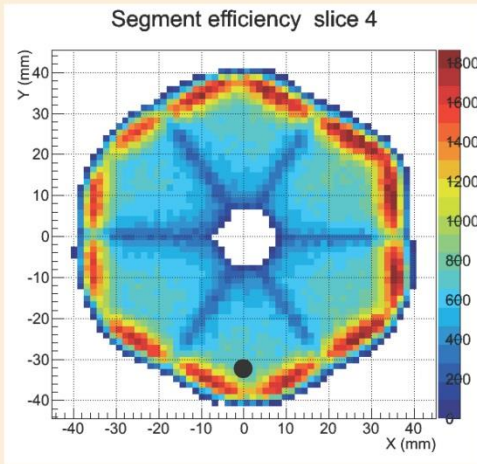
3D partial PSCS



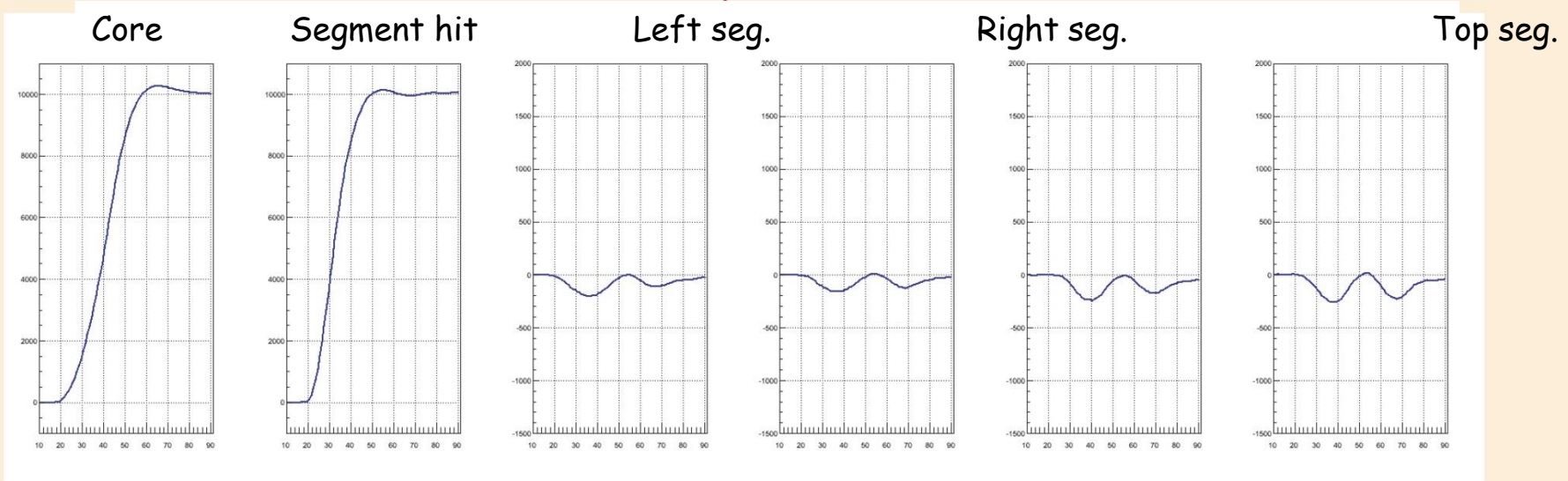
( 0 ; -29.0 ; 50)



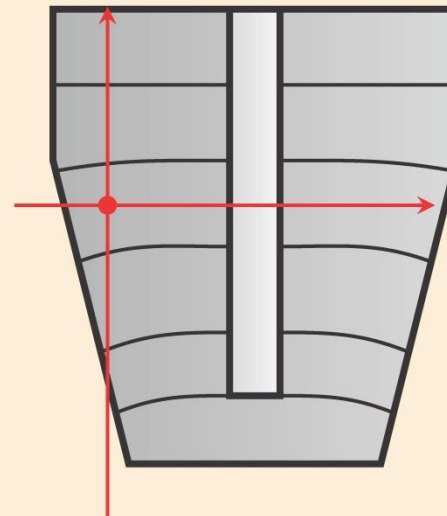
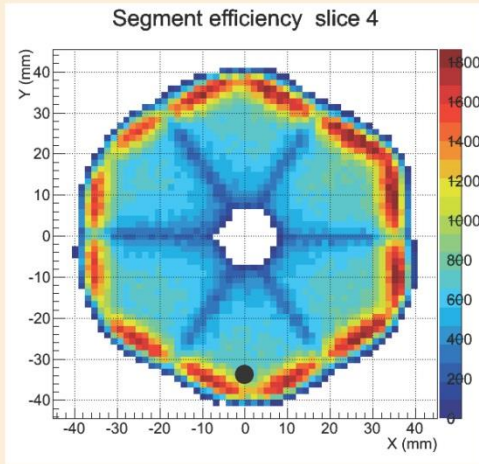
3D partial PSCS



( 0 ; -30.5 ; 50)

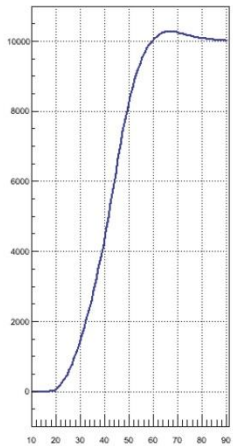


3D partial PSCS

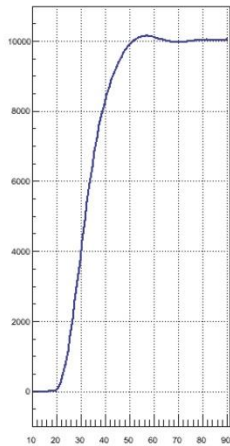


( 0 ; -32.0 ; 50)

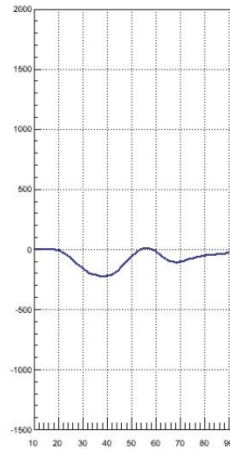
Core



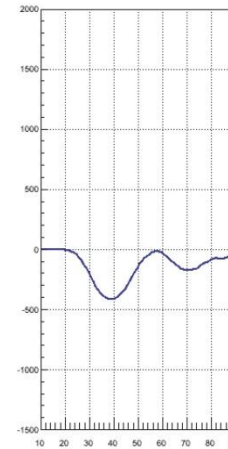
Segment hit



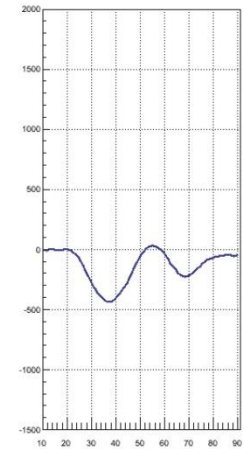
Left seg.



Right seg.

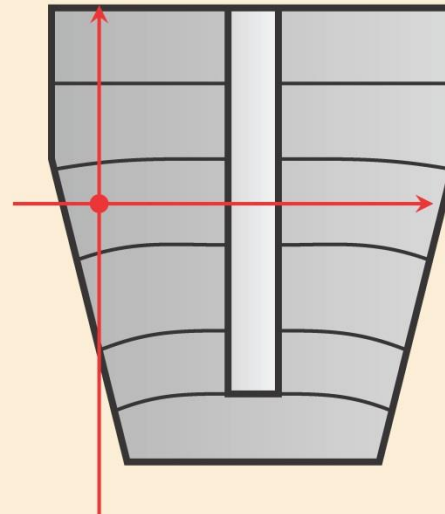
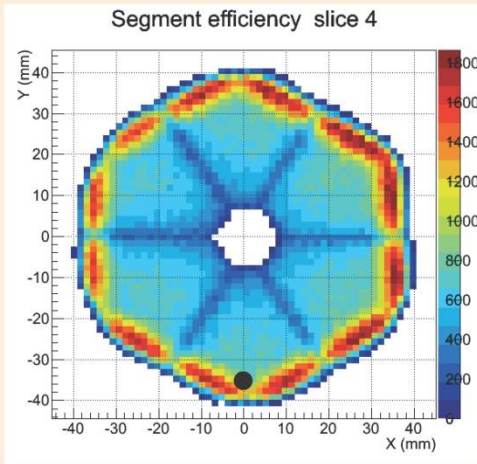


Top seg.

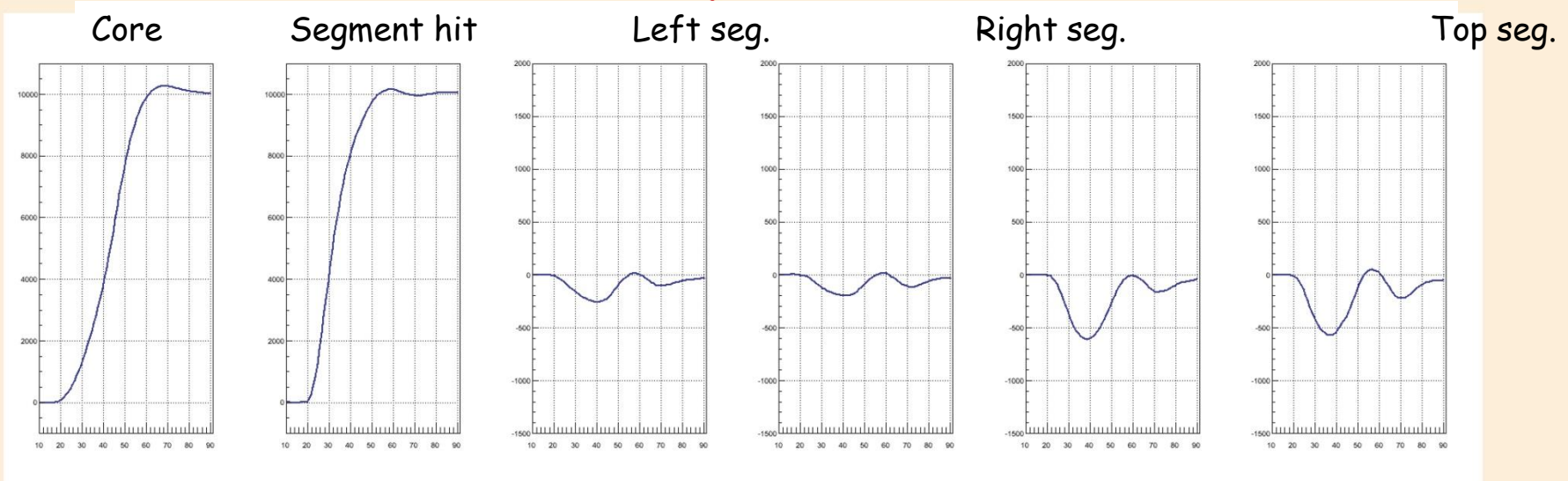




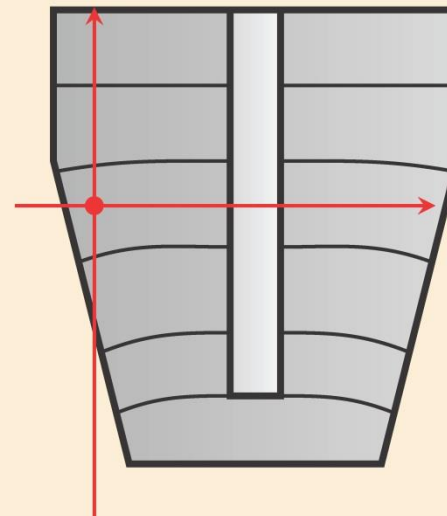
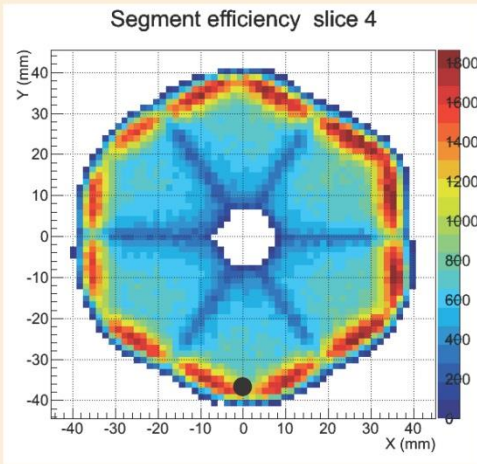
### 3D partial PSCS



( 0 ; -33.5 ; 50 )

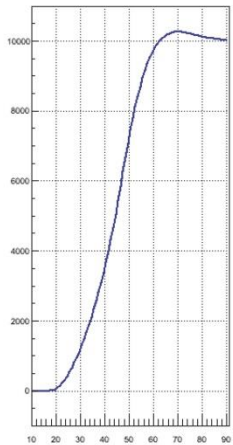


3D partial PSCS

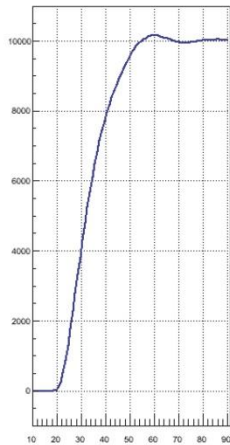


( 0 ; -35.0 ; 50)

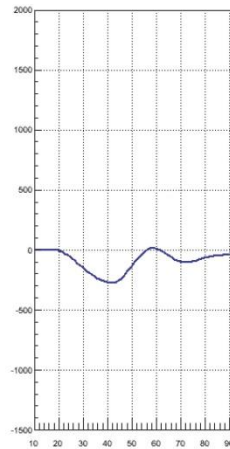
Core



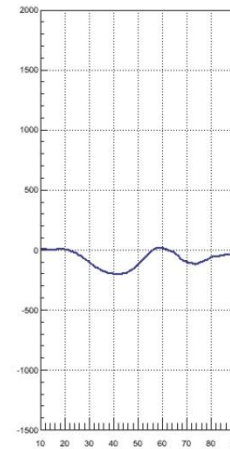
Segment hit



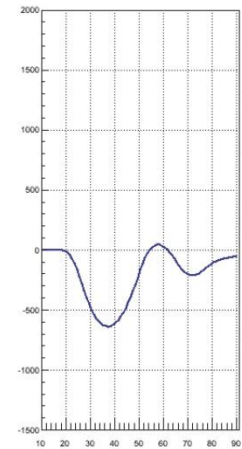
Left seg.



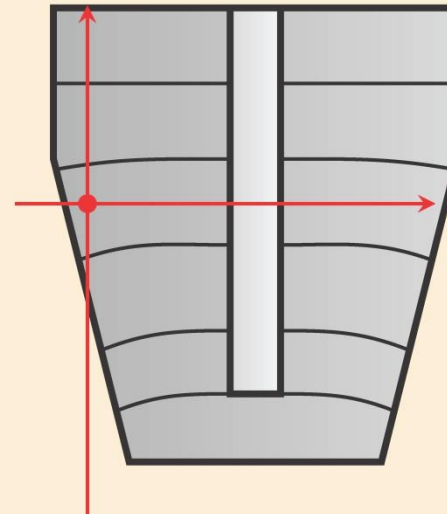
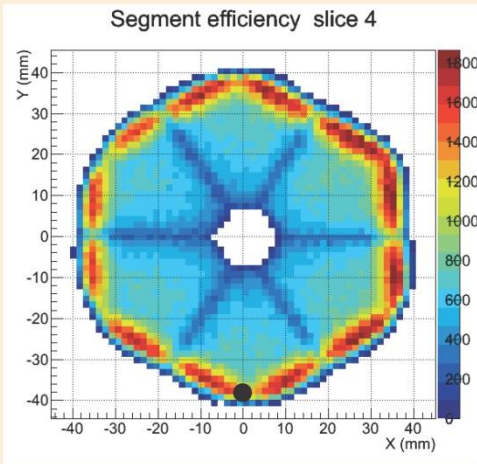
Right seg.



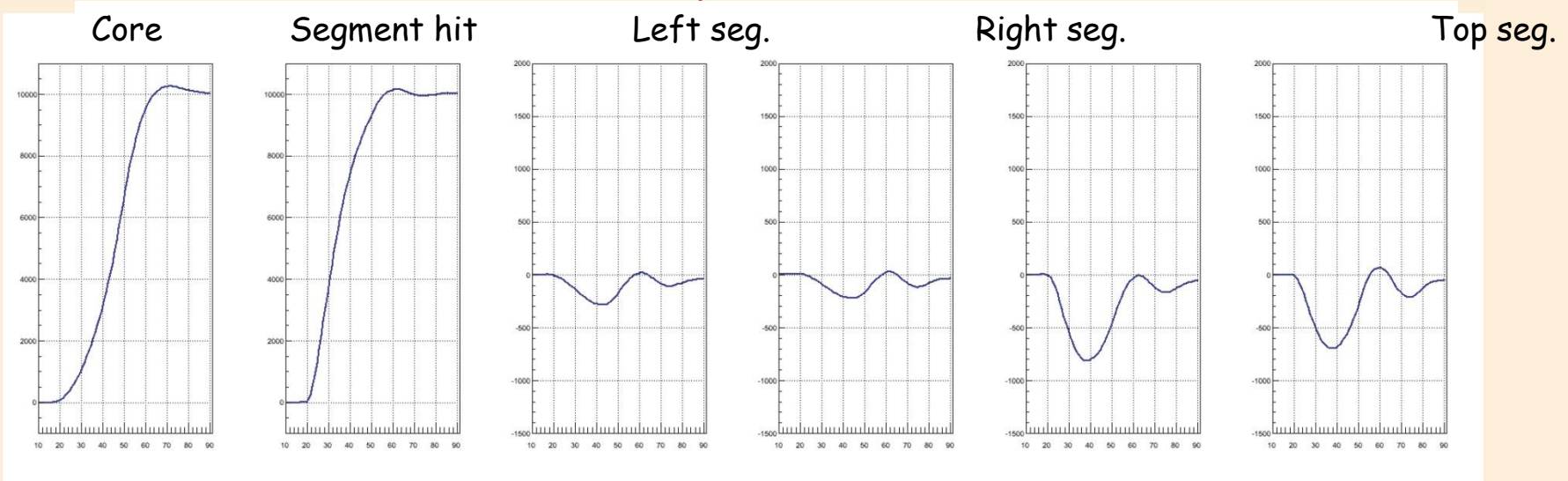
Top seg.



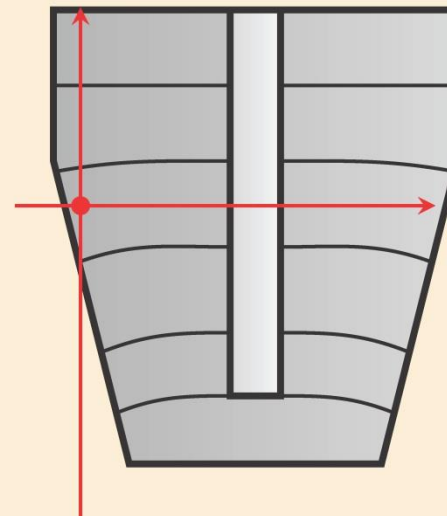
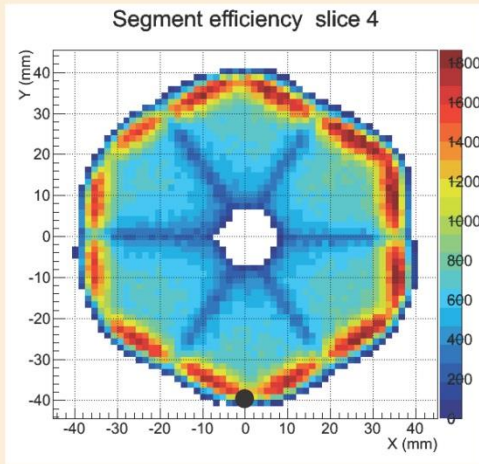
3D partial PSCS



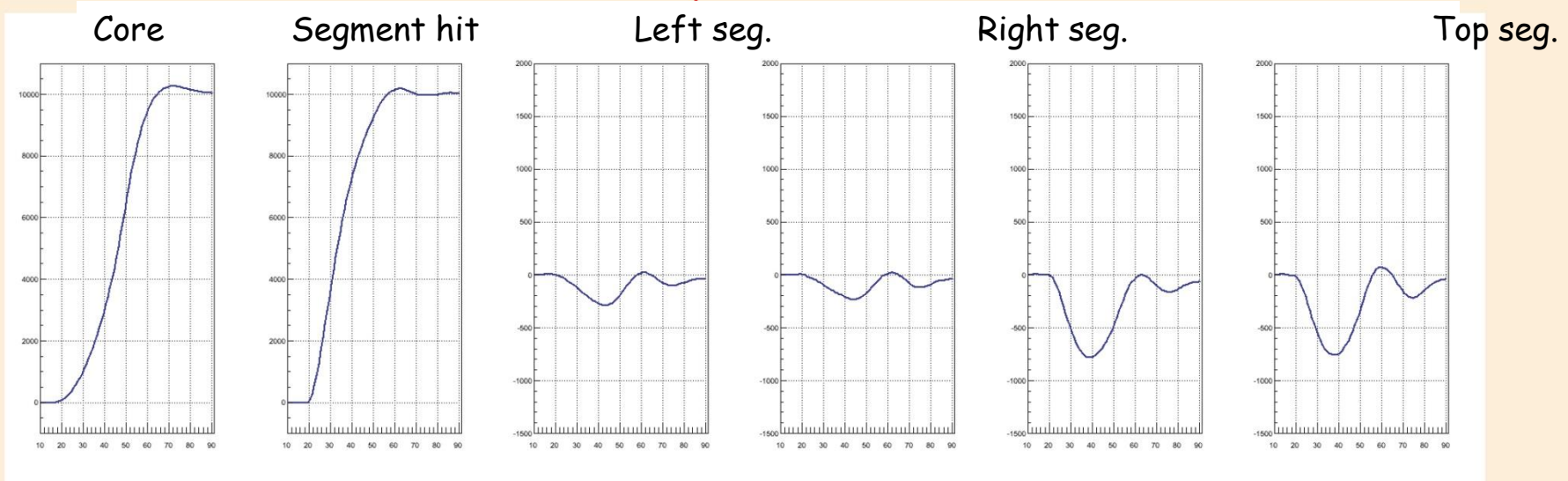
( 0 ; -36.5 ; 50)



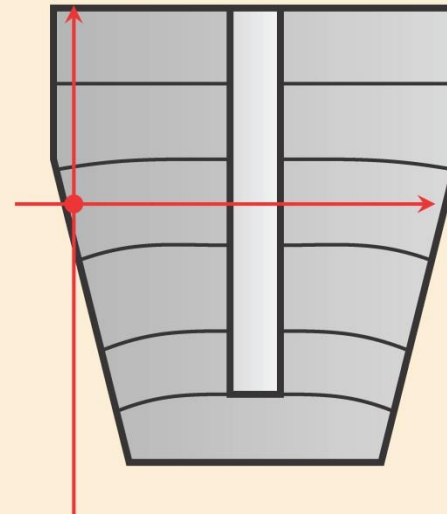
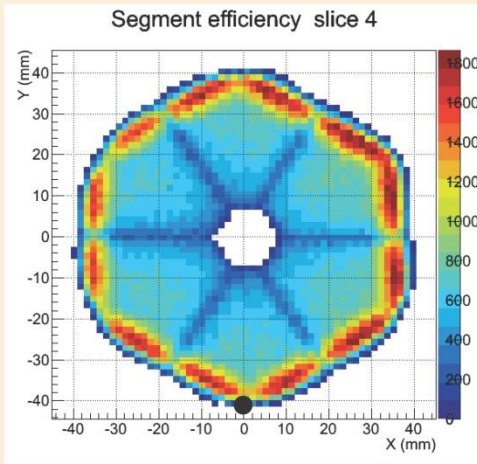
### 3D partial PSCS



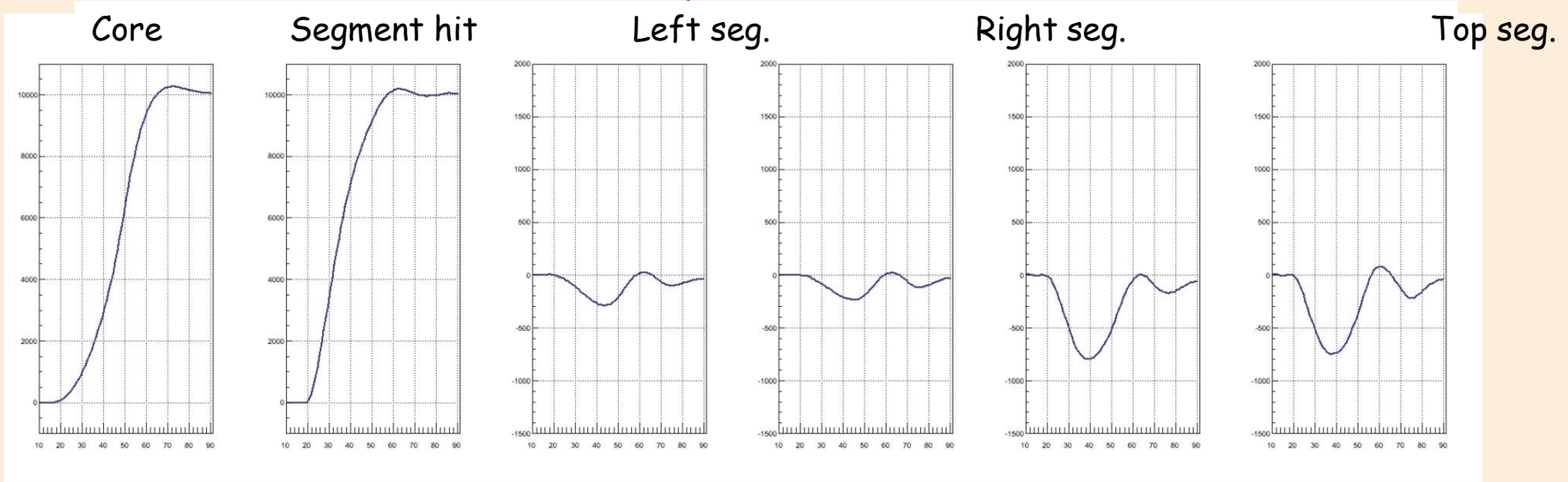
( 0 ; -38.0 ; 50)



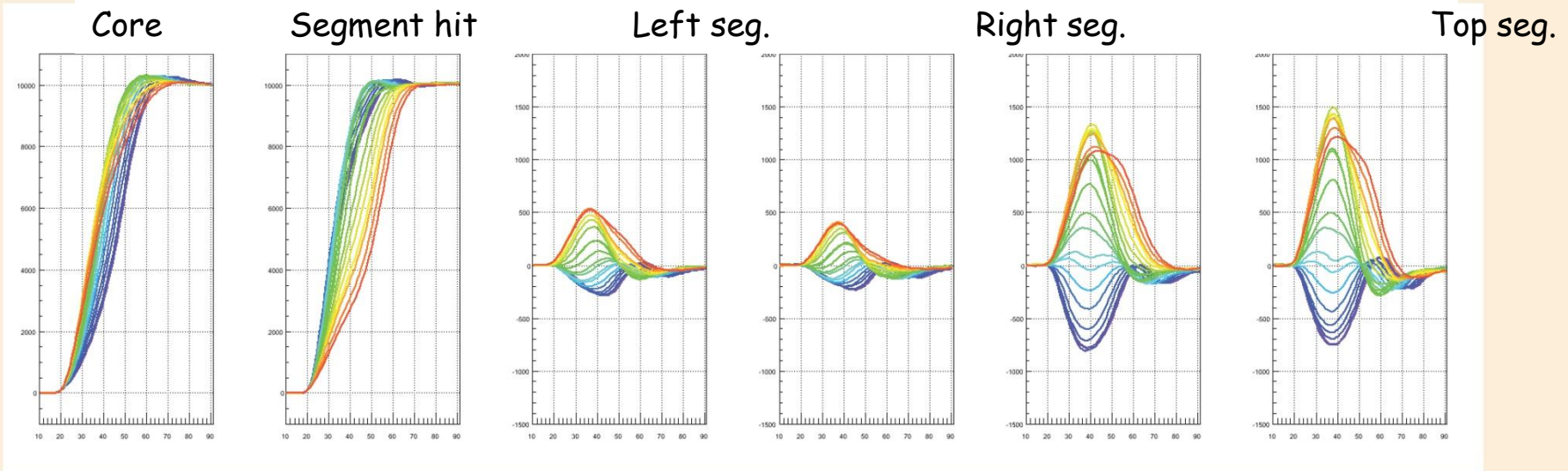
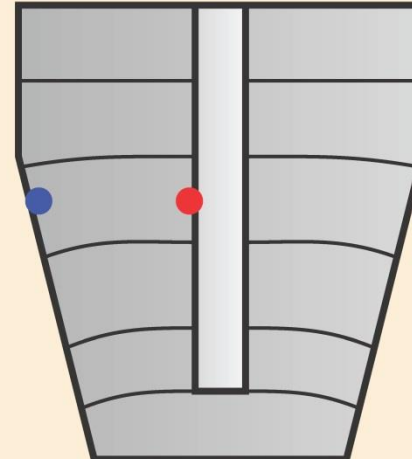
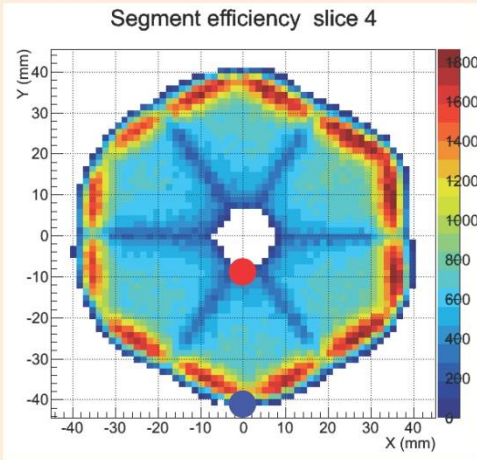
3D partial PSCS



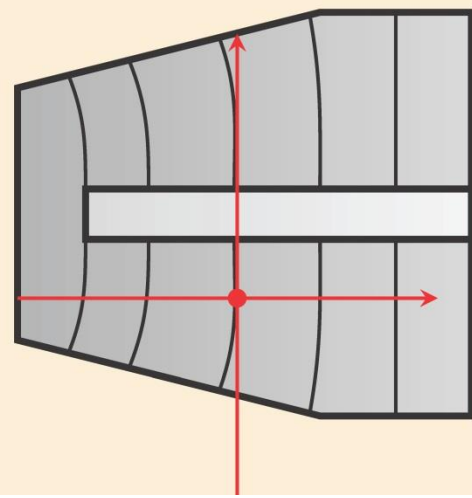
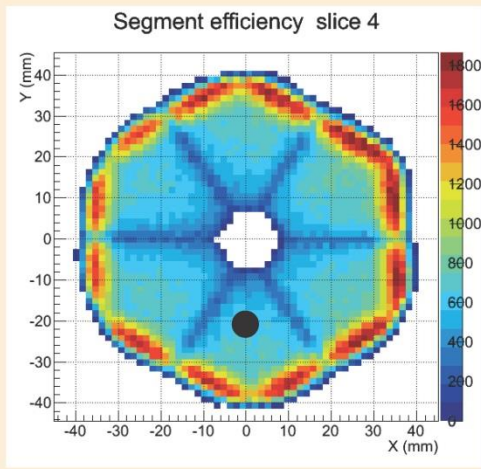
( 0 ; -39.5 ; 50)



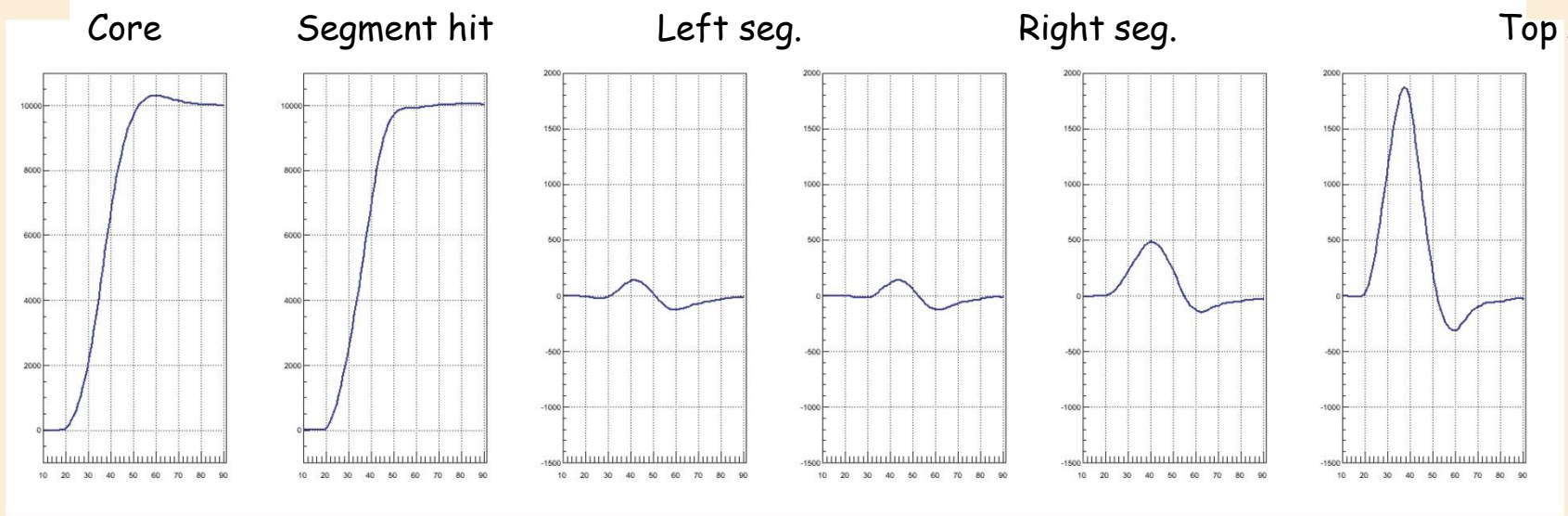
# 3D partial PSCS



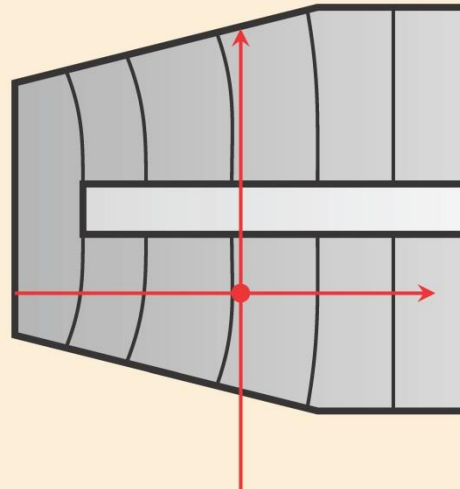
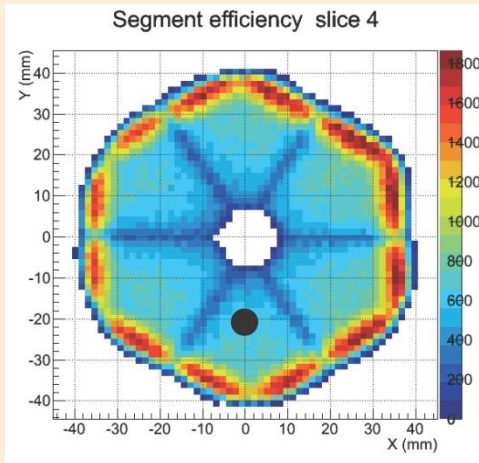
3D partial PSCS



( 0 ; -23 ; 43 )



3D partial PSCS



( 0 ; -23 ; 44 )

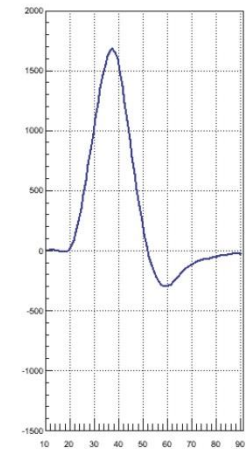
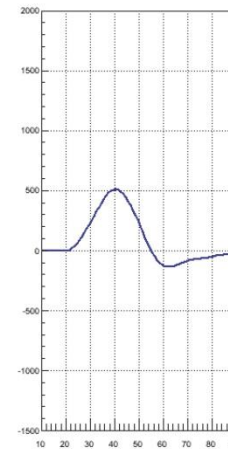
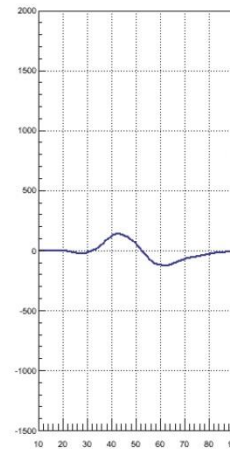
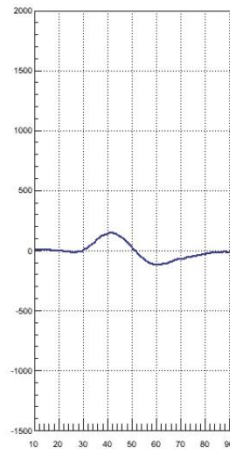
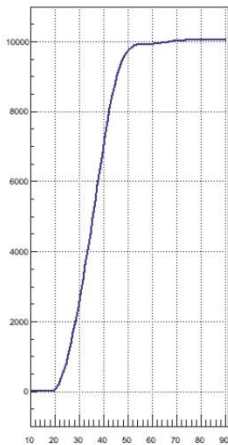
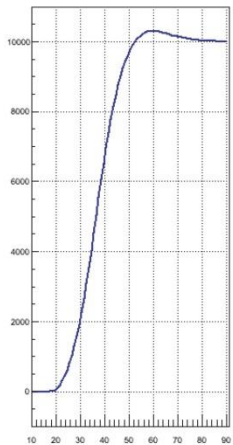
Core

Segment hit

Left seg.

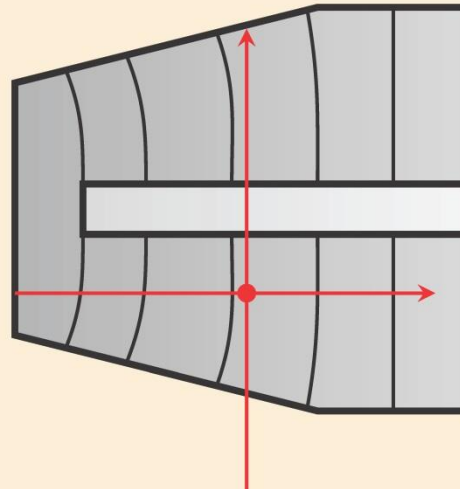
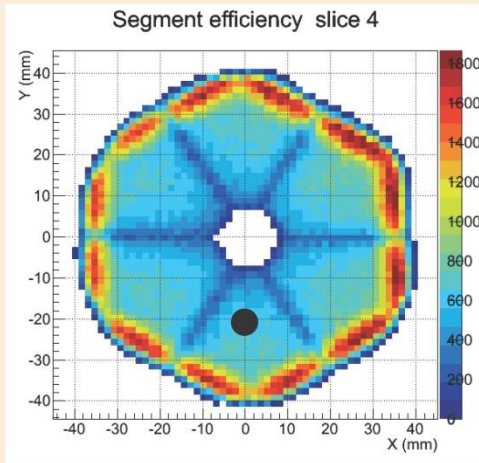
Right seg.

Top seg.



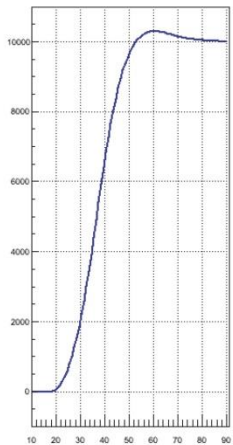


# 3D partial PSCS

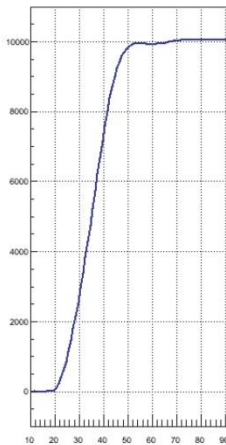


( 0 ; -23 ; 45 )

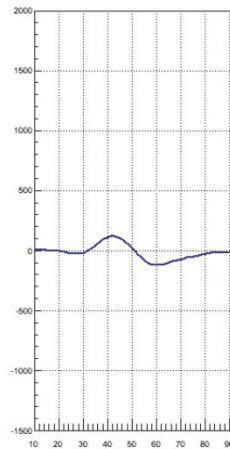
Core



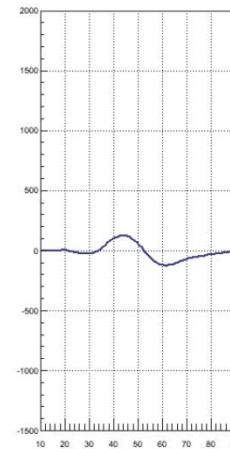
Segment hit



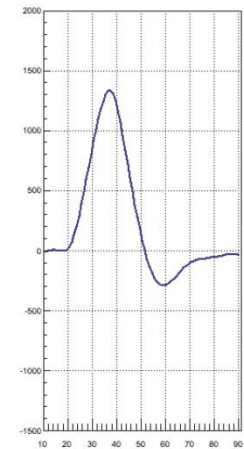
Left seg.



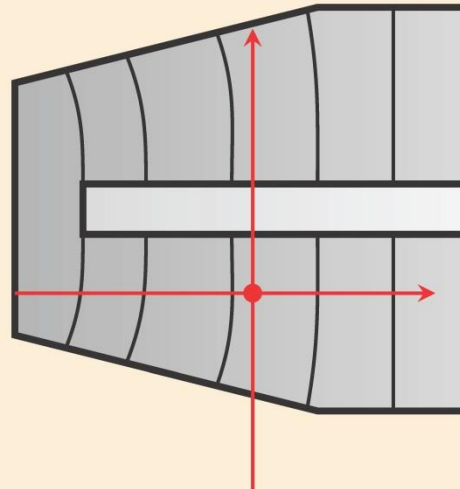
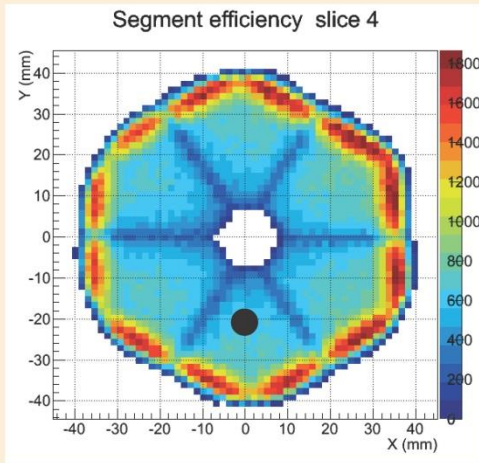
Right seg.



Top seg.



3D partial PSCS



( 0 ; -23 ; 46 )

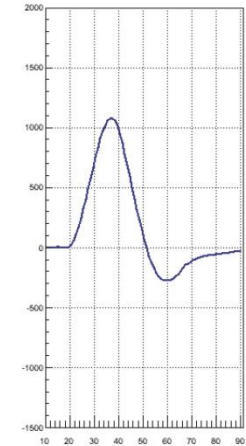
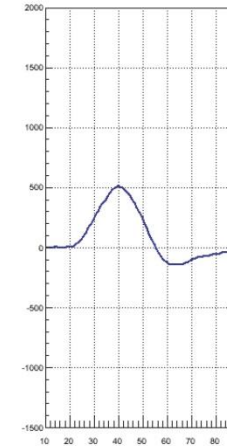
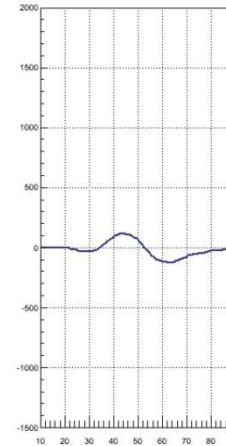
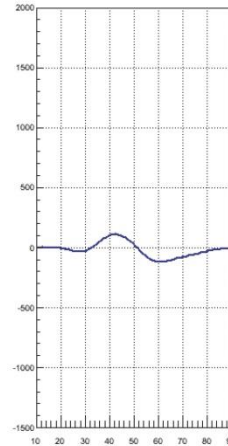
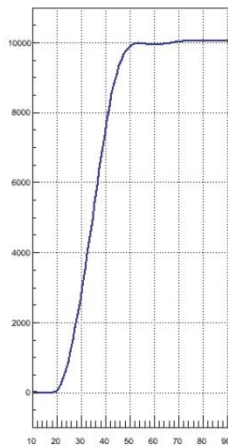
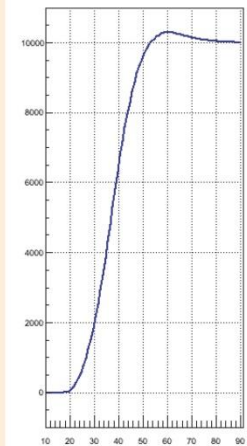
Core

Segment hit

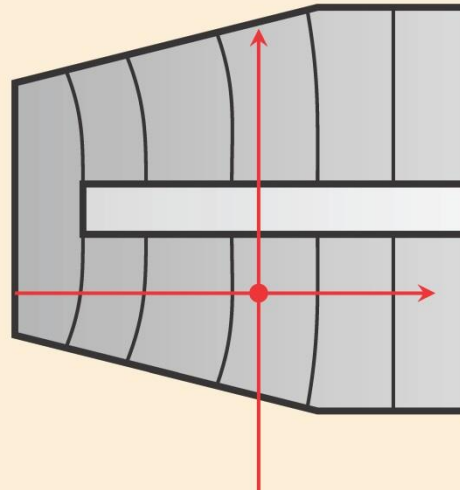
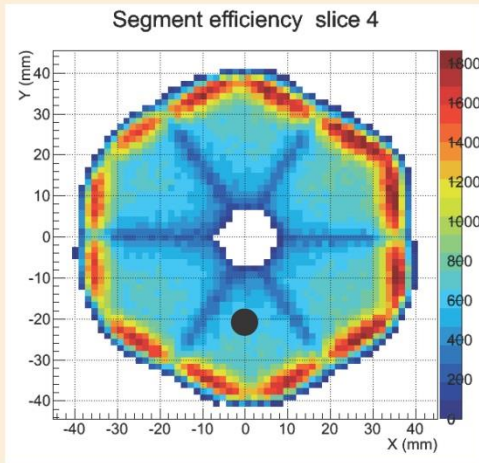
Left seg.

Right seg.

Top seg.



3D partial PSCS



( 0 ; -23 ; 47 )

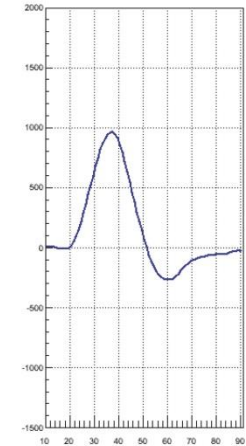
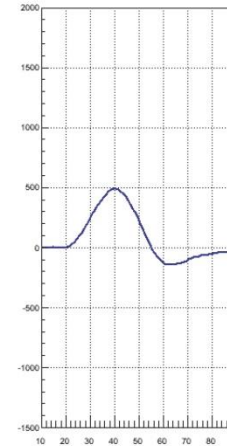
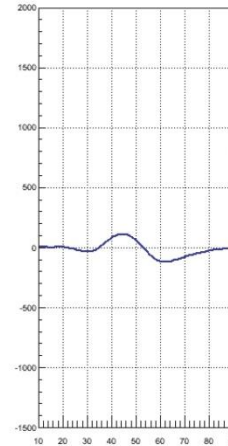
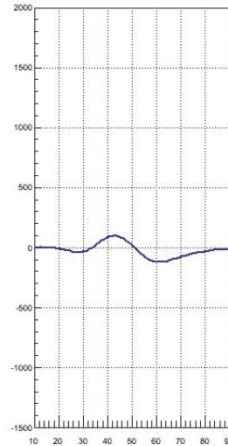
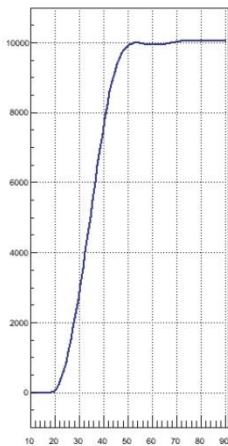
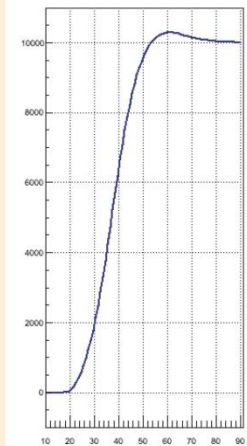
Core

Segment hit

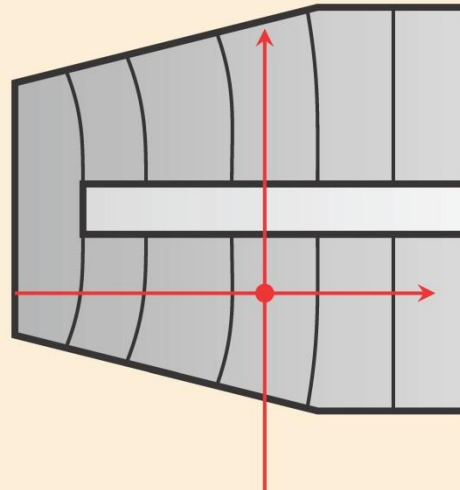
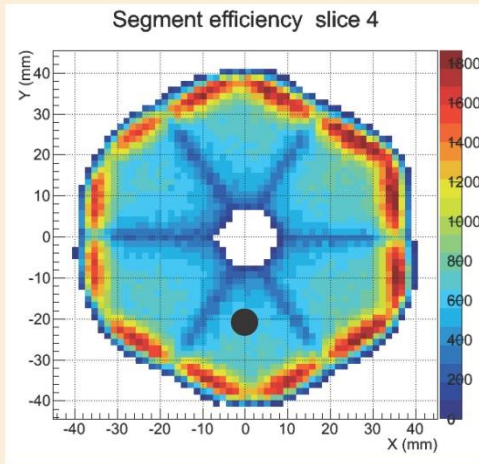
Left seg.

Right seg.

Top seg.

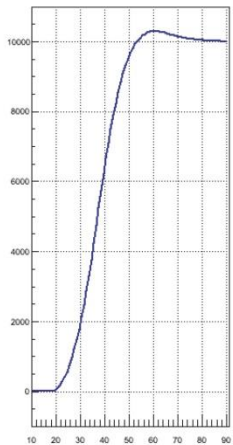


### 3D partial PSCS

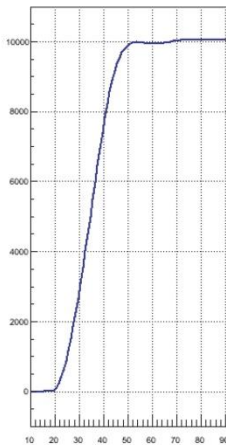


( 0 ; -23 ; 48 )

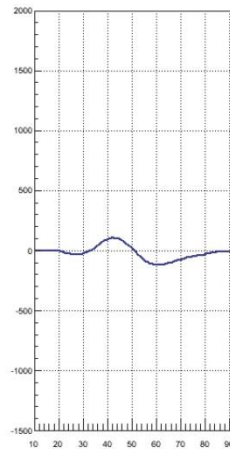
Core



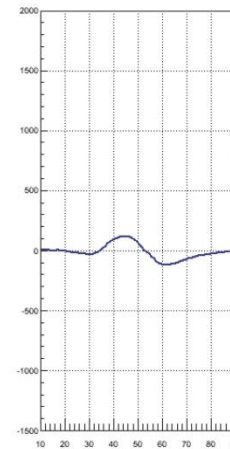
Segment hit



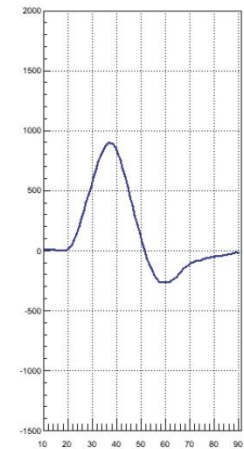
Left seg.



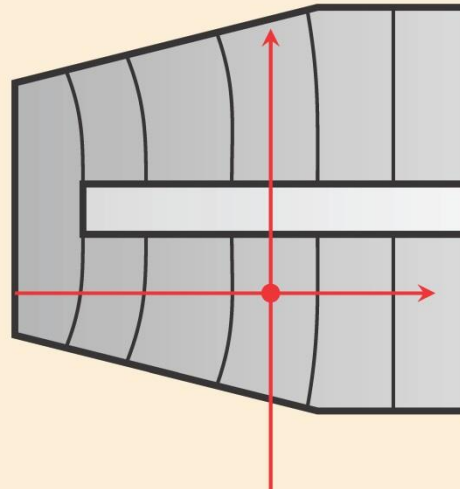
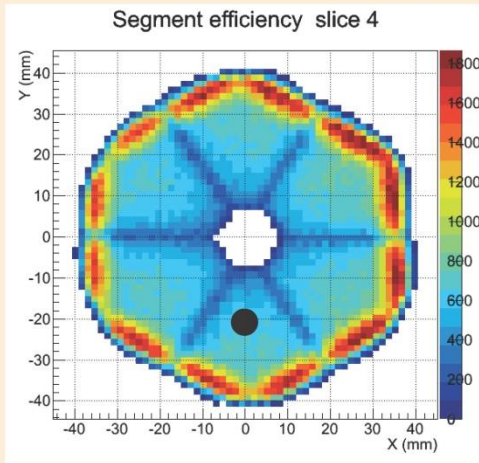
Right seg.



Top seg.



3D partial PSCS



( 0 ; -23 ; 49 )

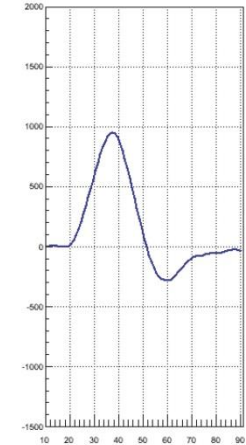
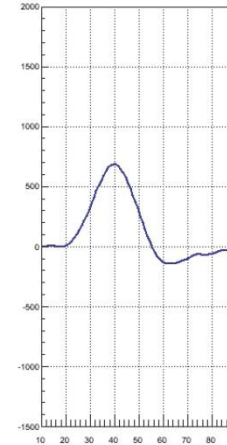
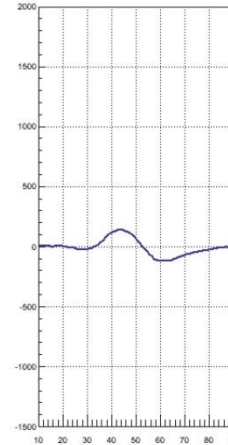
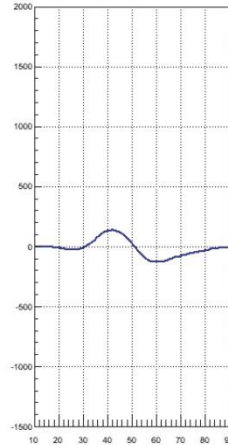
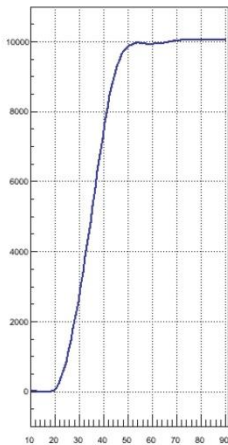
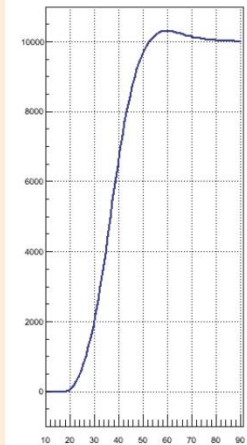
Core

Segment hit

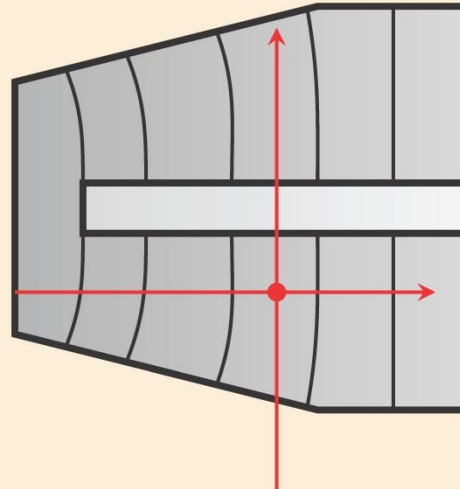
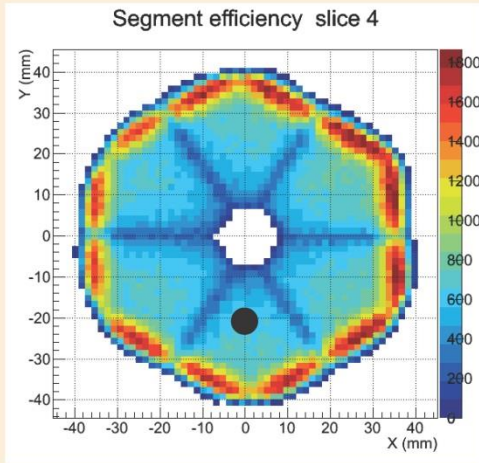
Left seg.

Right seg.

Top seg.



3D partial PSCS



( 0 ; -23 ; 50 )

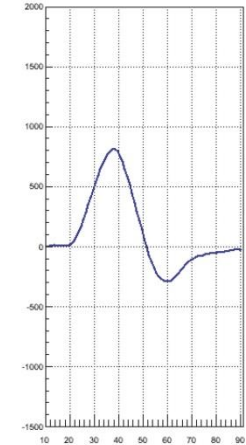
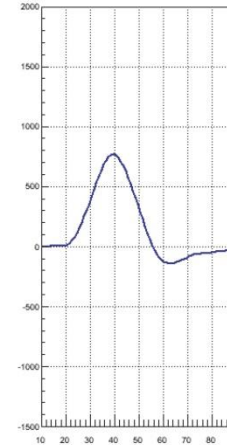
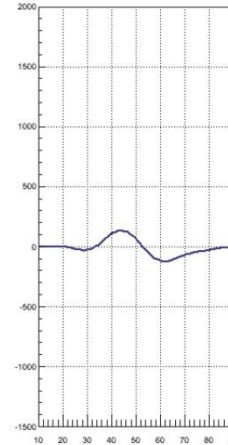
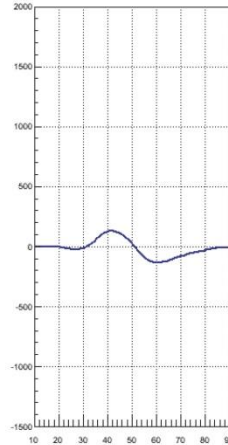
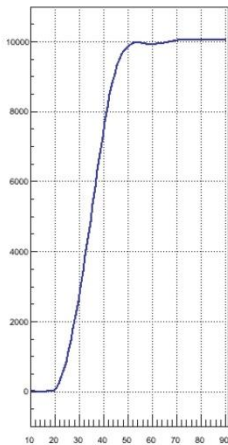
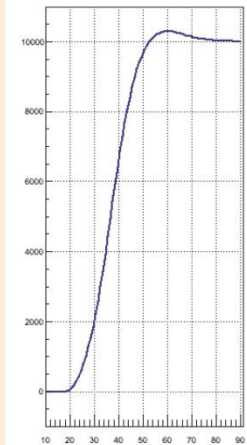
Core

Segment hit

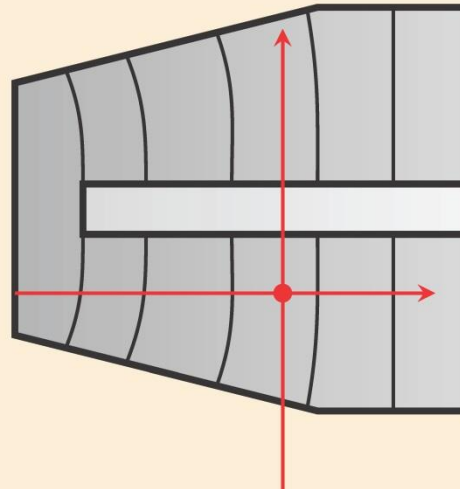
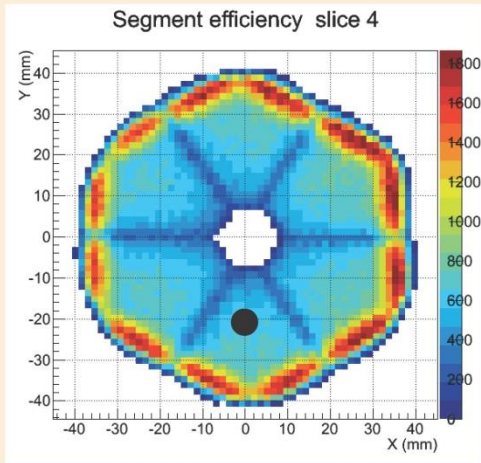
Left seg.

Right seg.

Top seg.



3D partial PSCS



( 0 ; -23 ; 51 )

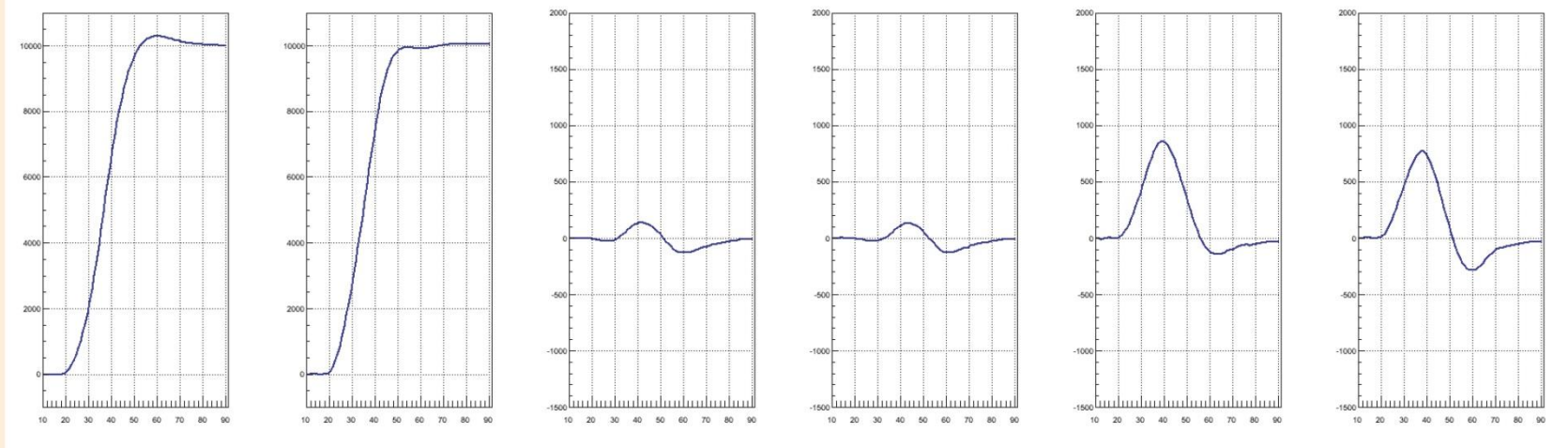
Core

Segment hit

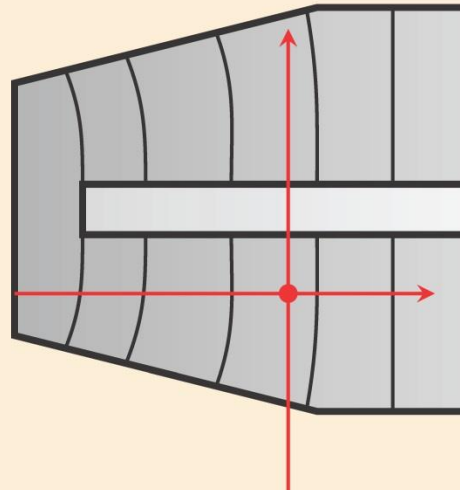
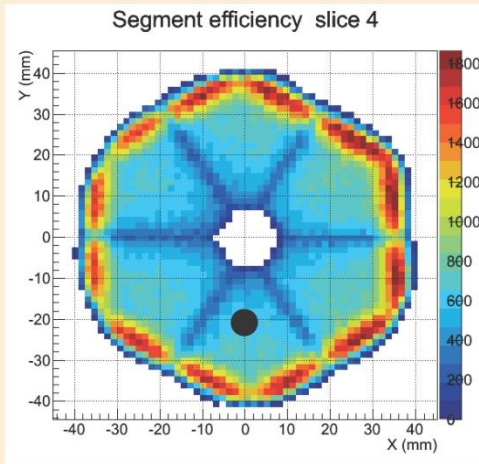
Left seg.

Right seg.

Top seg.



3D partial PSCS



( 0 ; -23 ; 52 )

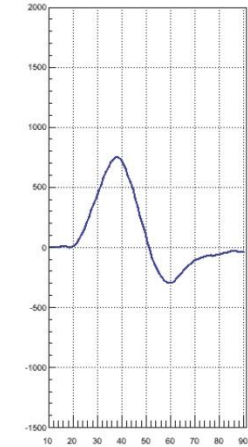
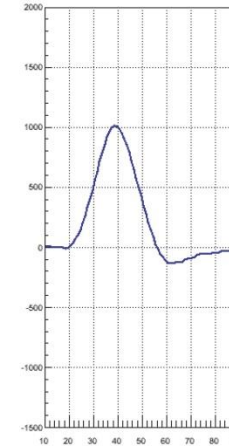
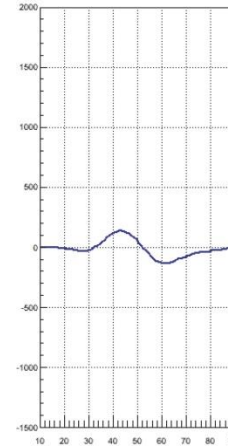
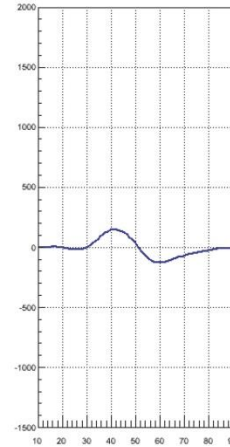
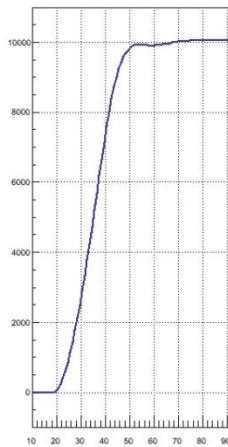
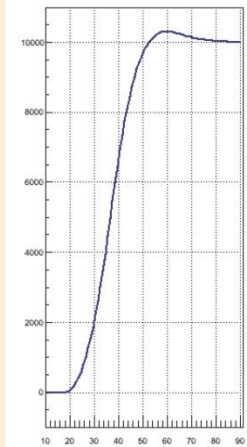
Core

Segment hit

Left seg.

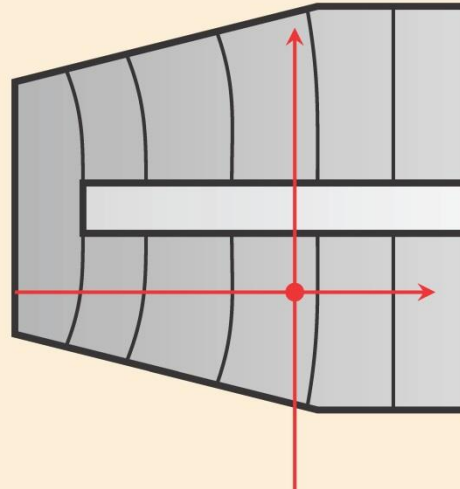
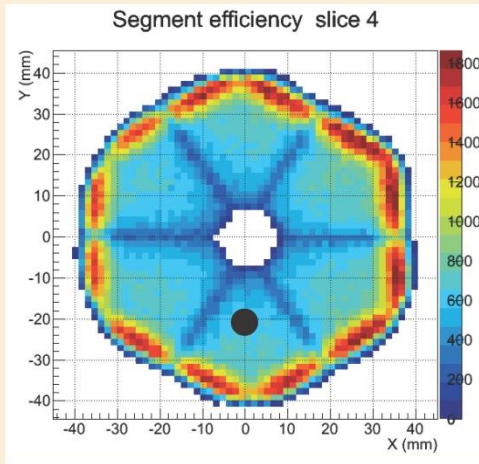
Right seg.

Top seg.



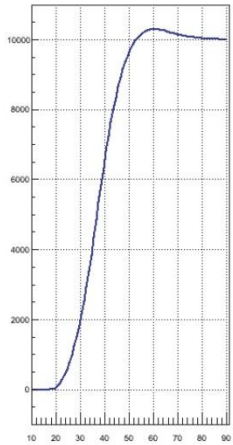


# 3D partial PSCS

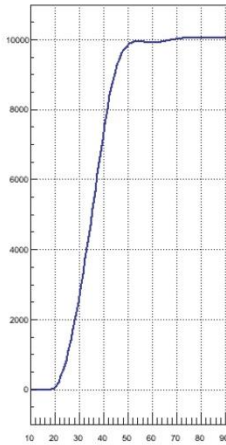


( 0 ; -23 ; 53 )

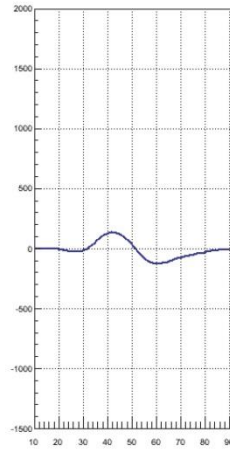
Core



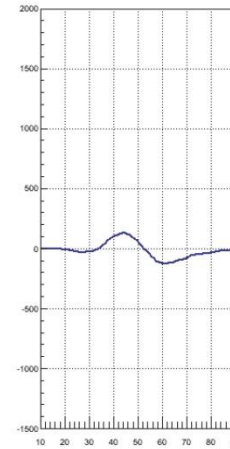
Segment hit



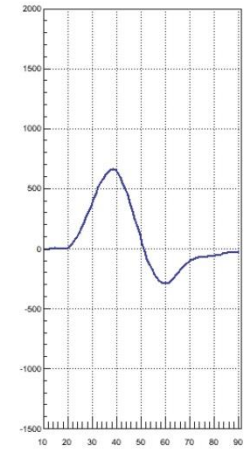
Left seg.



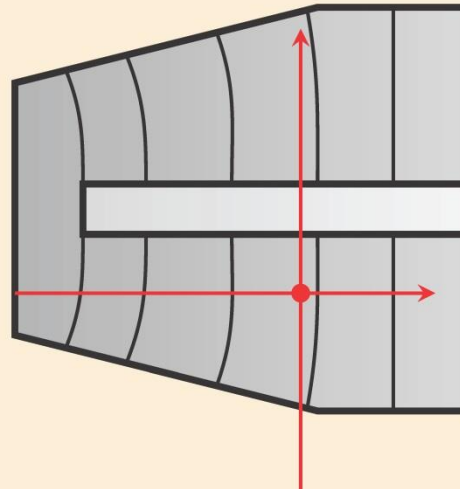
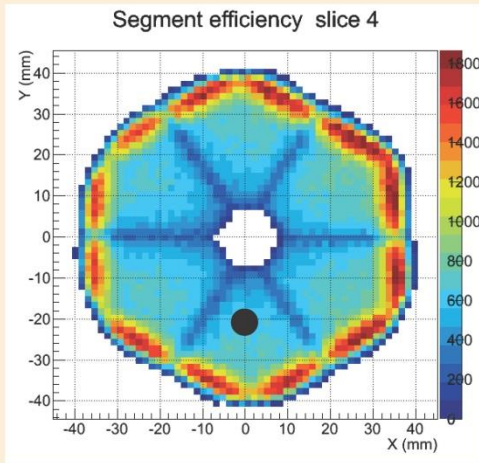
Right seg.



Top seg.



### 3D partial PSCS



( 0 ; -23 ; 54 )

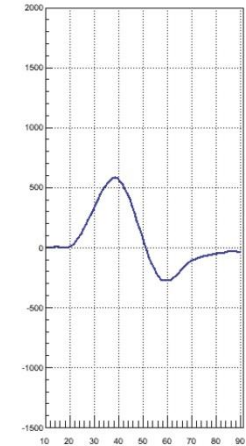
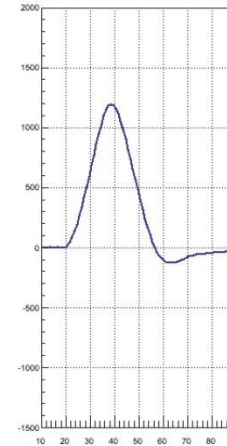
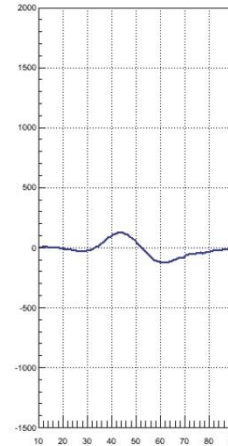
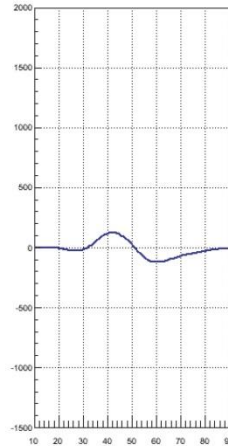
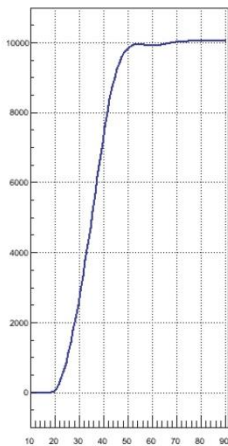
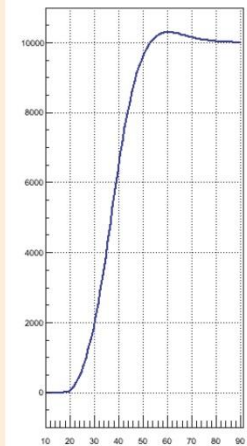
Core

Segment hit

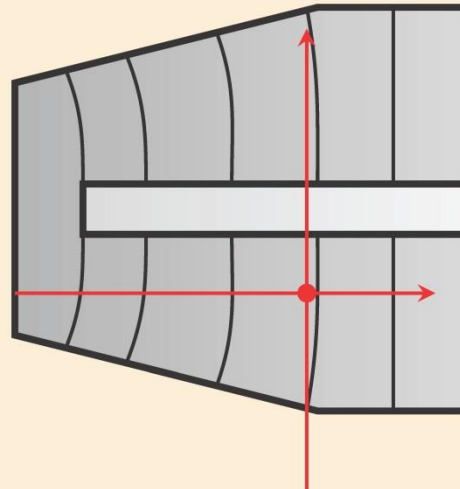
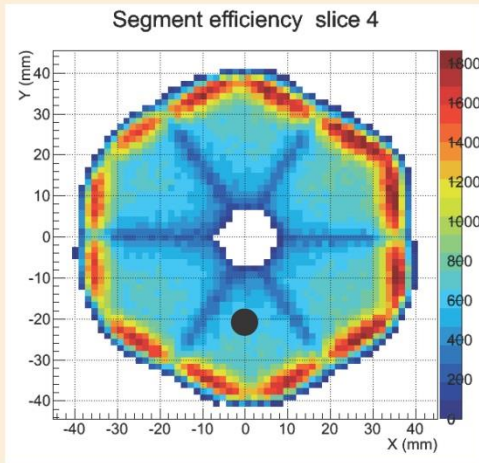
Left seg.

Right seg.

Top seg.

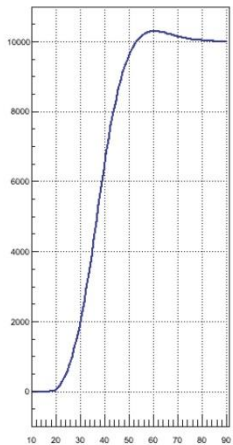


### 3D partial PSCS

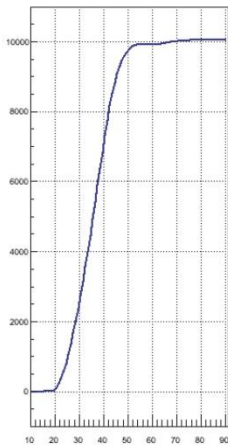


( 0 ; -23 ; 55 )

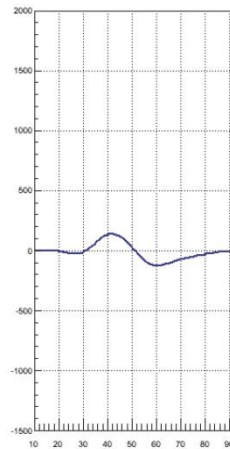
Core



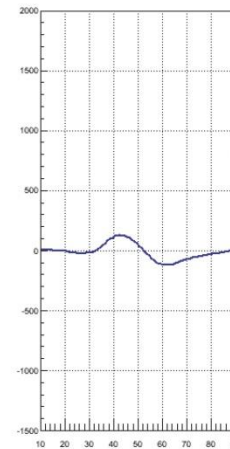
Segment hit



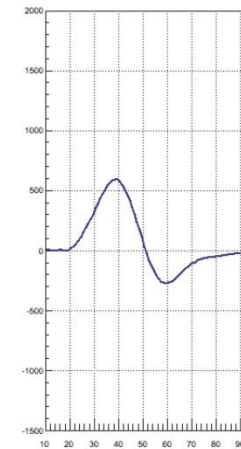
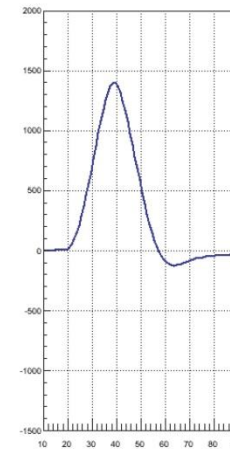
Left seg.



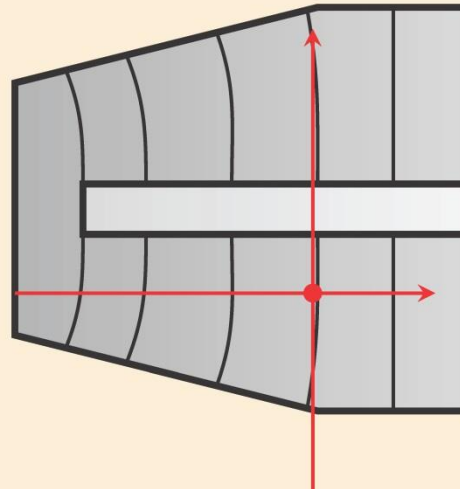
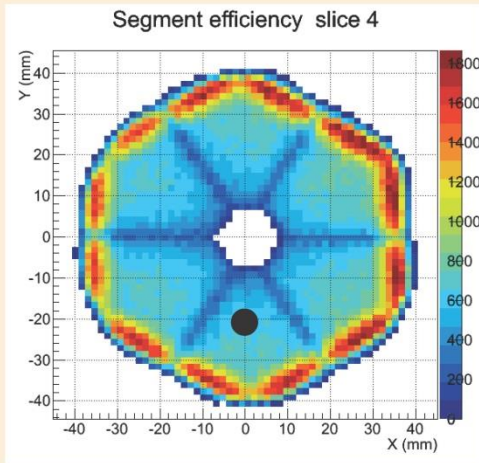
Right seg.



Top seg.

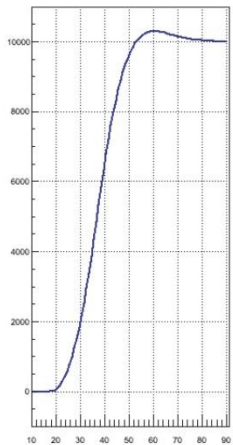


3D partial PSCS

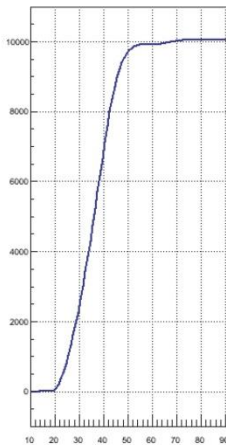


( 0 ; -23 ; 56 )

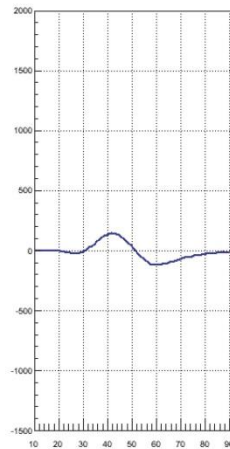
Core



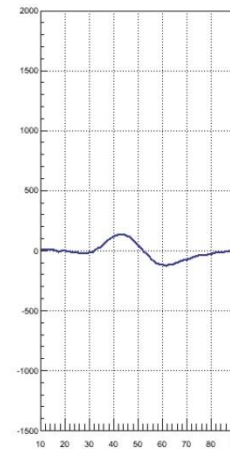
Segment hit



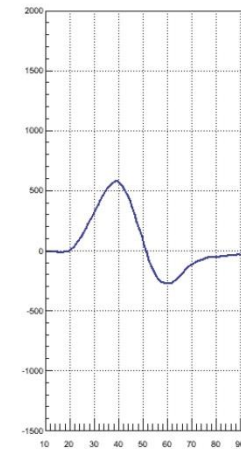
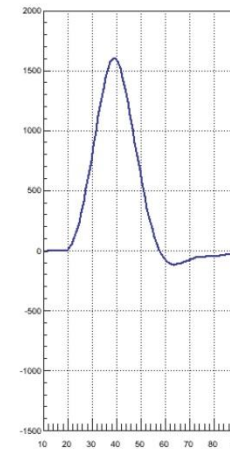
Left seg.



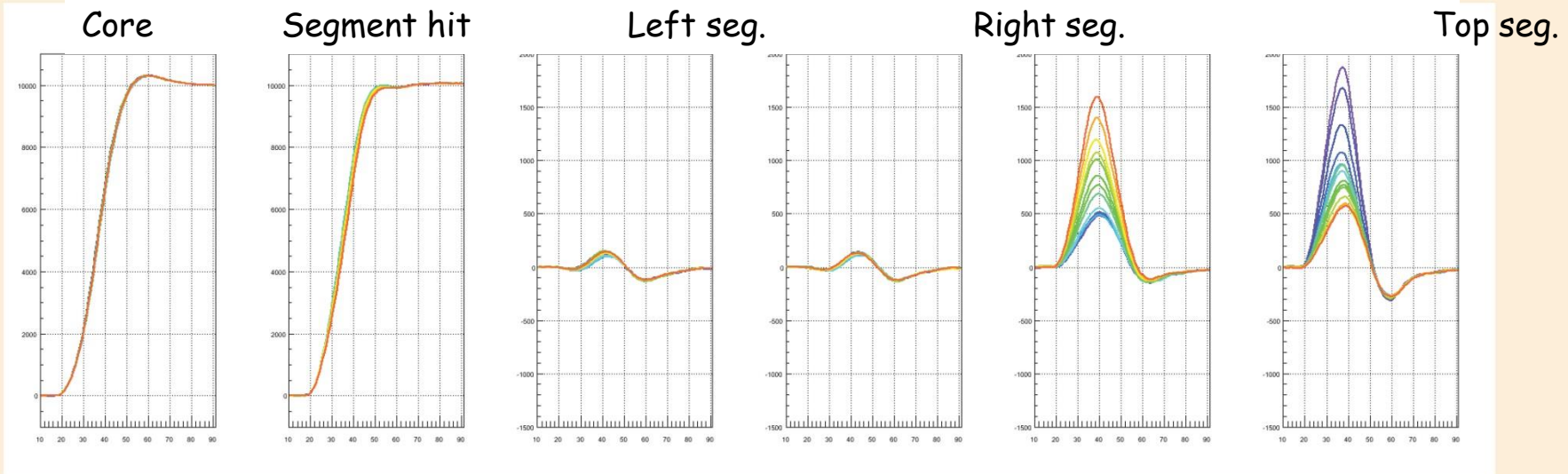
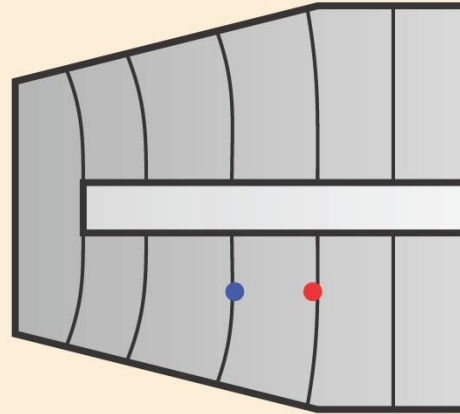
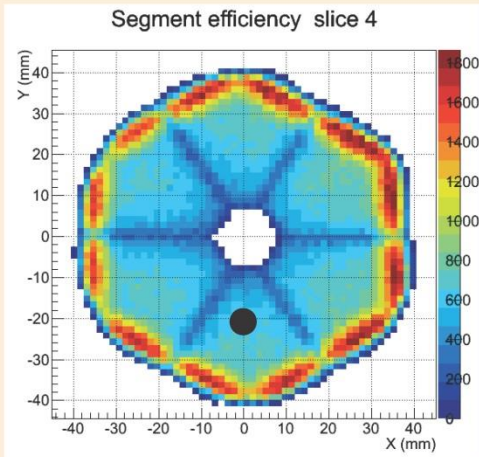
Right seg.



Top seg.

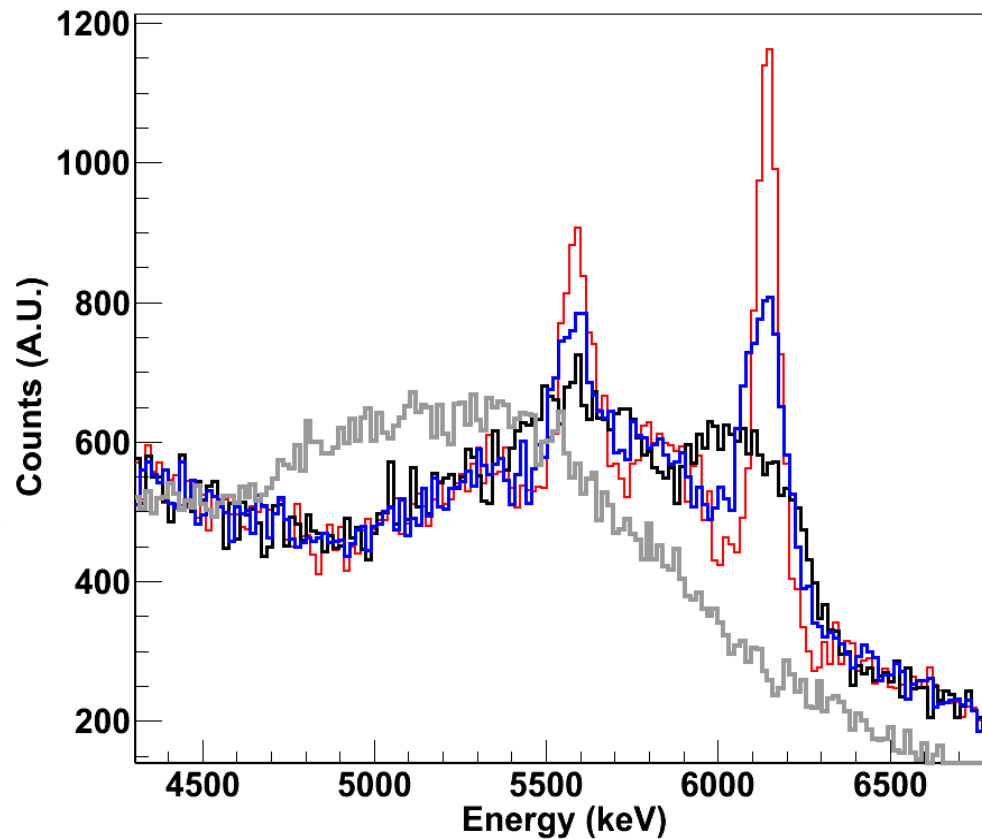
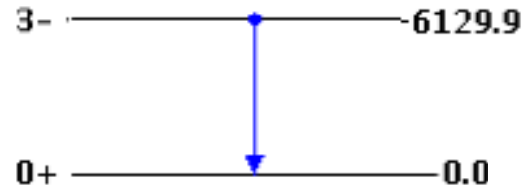


3D partial PSCS



**16O**

No Dopp Corr  
Crystal Centers  
Segment Centers  
PSA+Tracking



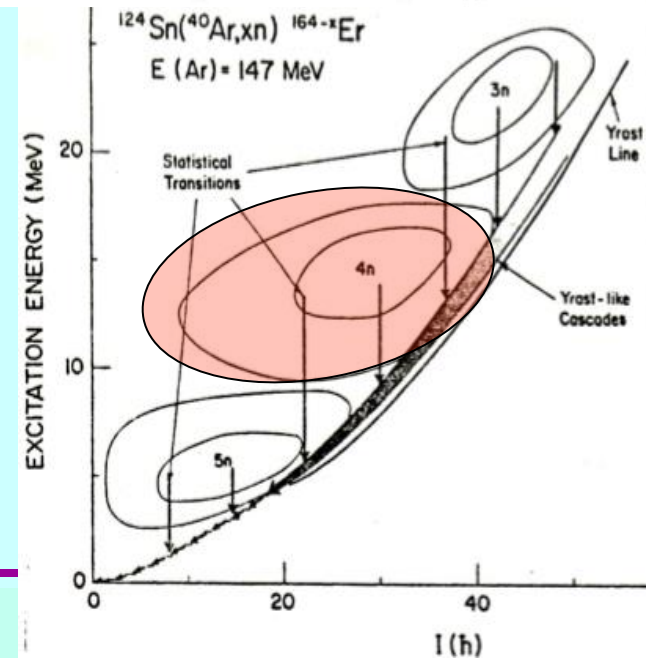
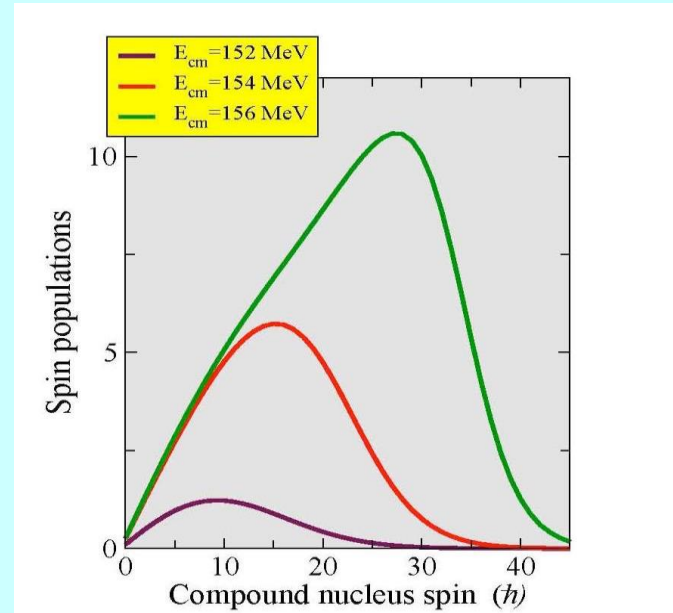
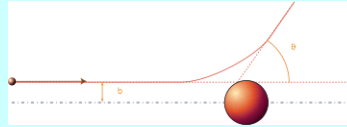
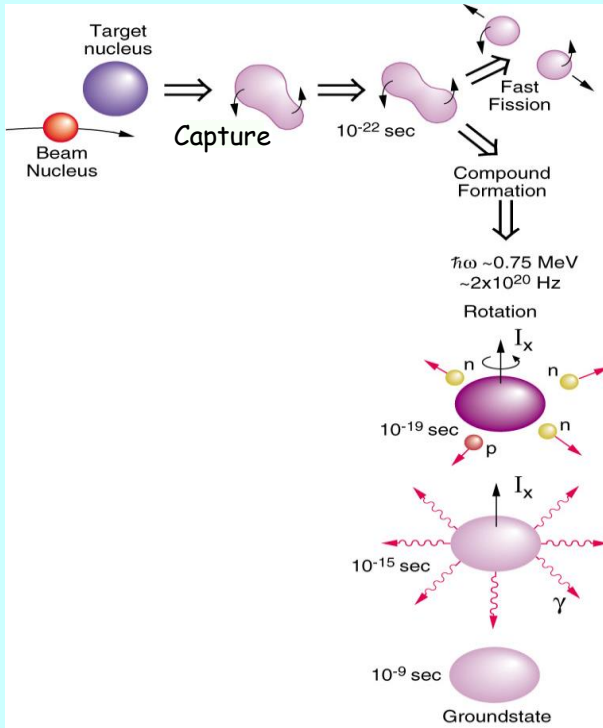
# Lecture plan

1. Introduction
2. Radiation-matter interactions and detectors for charged particle and  $\gamma$  rays
3. Nuclear reactions
4. Nuclear structure and observables
5. Perspectives

## Fusion -evaporation

- Central collisions ( $E_{\text{beam}} \sim 6 \text{ MeV/u}$ )

$$\vec{l} = \vec{r} \wedge \vec{p}$$

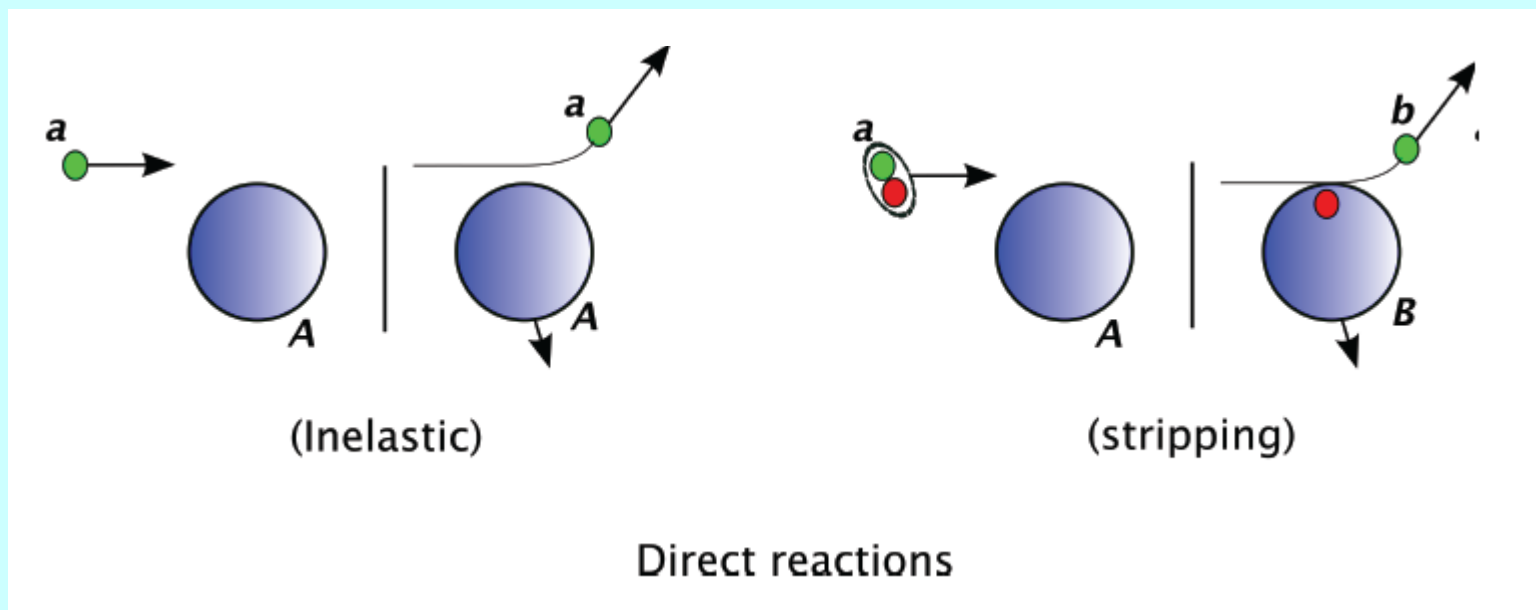




# Nuclear reactions

## Transfert of nucleon

- Peripheral collisions (direct reactions) with 10 - 25 MeV/u beam energy
- Energy exchange, internal excitation → inelastic channel
- Energy exchange, internal excitation and transfer of few nucleons → transfer
  - ❑ Stripping channel: one nucleon of the projectile is transferred to the target
  - ❑ Pick up channel: one nucleon of the target is transferred to the projectile



- ❑ Get information on the orbital on which the nucleon has been transferred

# Nuclear reactions

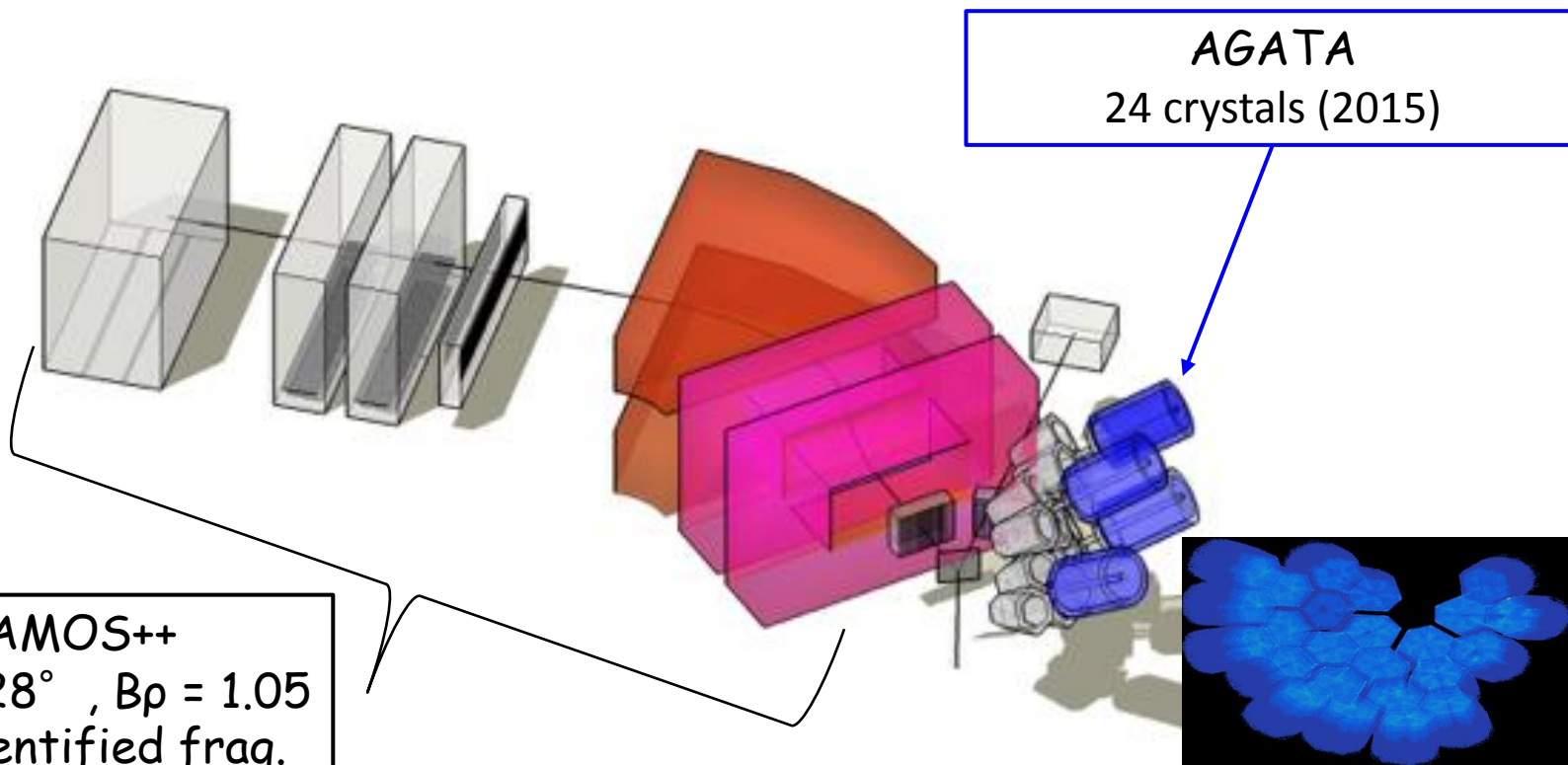
## Fusion-fission

- Fusion → compound nucleus → fission
  - ❑ Production of hundreds fragments can be identified
  - ❑ Neutron-rich isotopes populated
  - ❑ Large total cross-section (~250 mb)
  - ❑ Angular momentum transfer (~20-30  $\hbar$ )
  
- Inverse kinematics
  - ❑ Fast recoiling fission fragments
  - ❑ Forward focused fragments better entering in the magnet
  
- Systematic study of exotic-nuclei structure

## AGATA-VAMOS++ (exp at GANIL)

- Ge detector coupled to a spectrometer

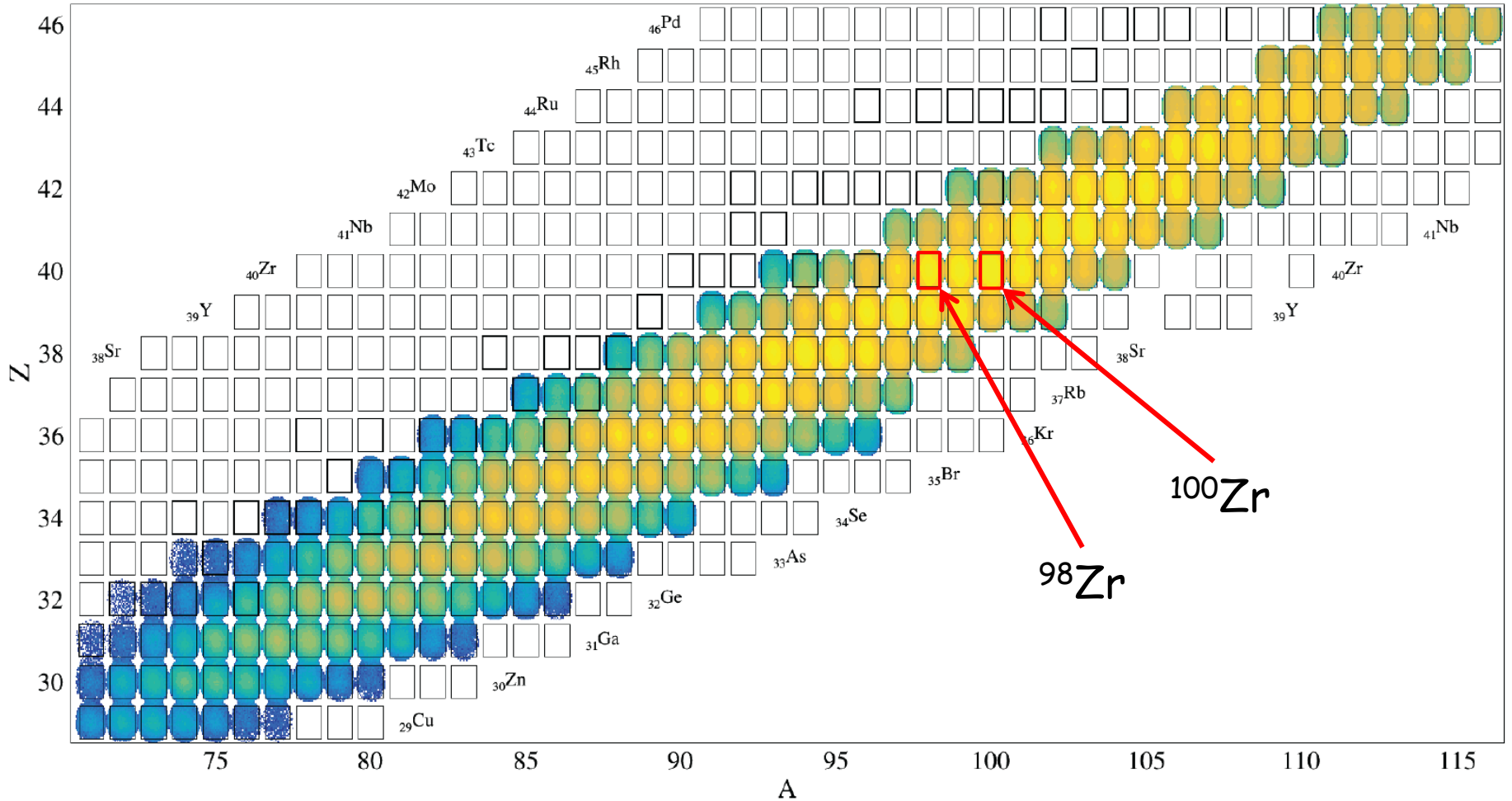
$^{238}\text{U}$  @ 6.2 MeV/u +  $^9\text{Be}$



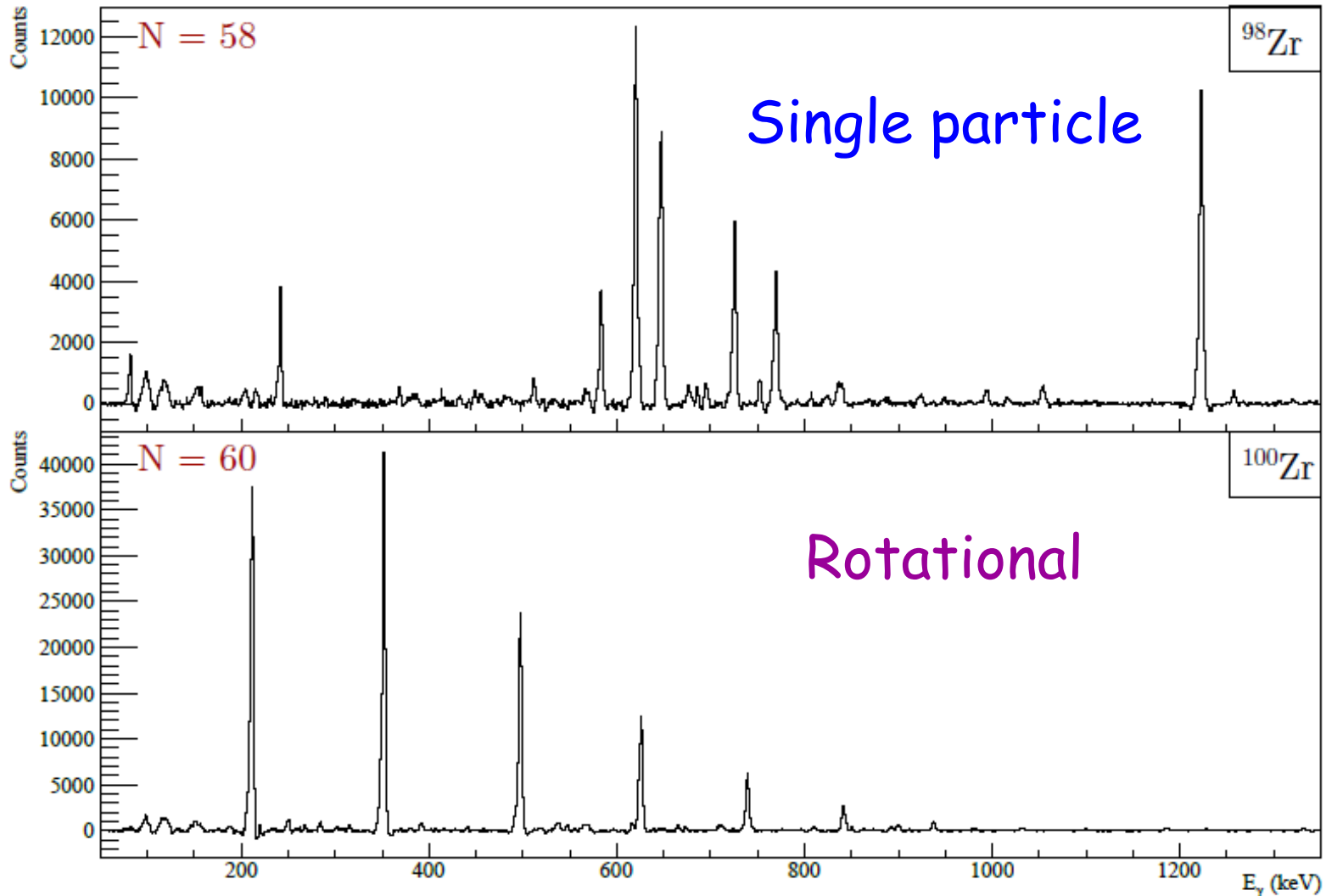
AGATA  
24 crystals (2015)

VAMOS++  
 $\theta_{\text{Vamos}} = 28^\circ$ ,  $B\rho = 1.05$   
205 identified frag.

# Case of an experiment @ GANIL



# Selected nucleus in VAMOS - Prompt gamma-rays in AGATA



Courtesy J. Dudouet

# Lecture plan

1. Introduction
2. Radiation-matter interactions and detectors for charged particle and  $\gamma$  rays
3. Nuclear reactions
4. Nuclear structure and observables
5. Perspectives

## Spin coupling

➤  $\vec{J} = \vec{I}_1 + \vec{I}_2 \quad |I_1 - I_2| \leq J \leq I_1 + I_2$

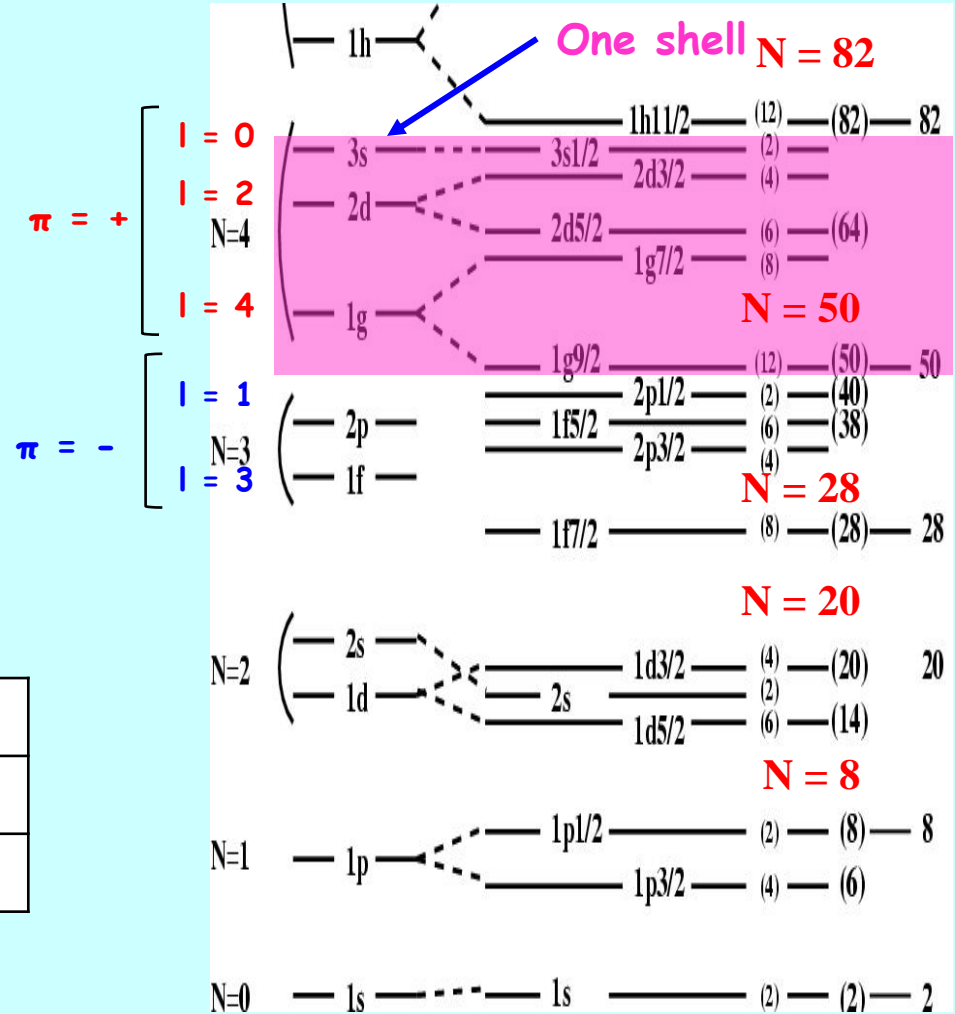
➤ Nucleons are fermion:  $s=1/2$

➤ On orbitals with momentum  $l$

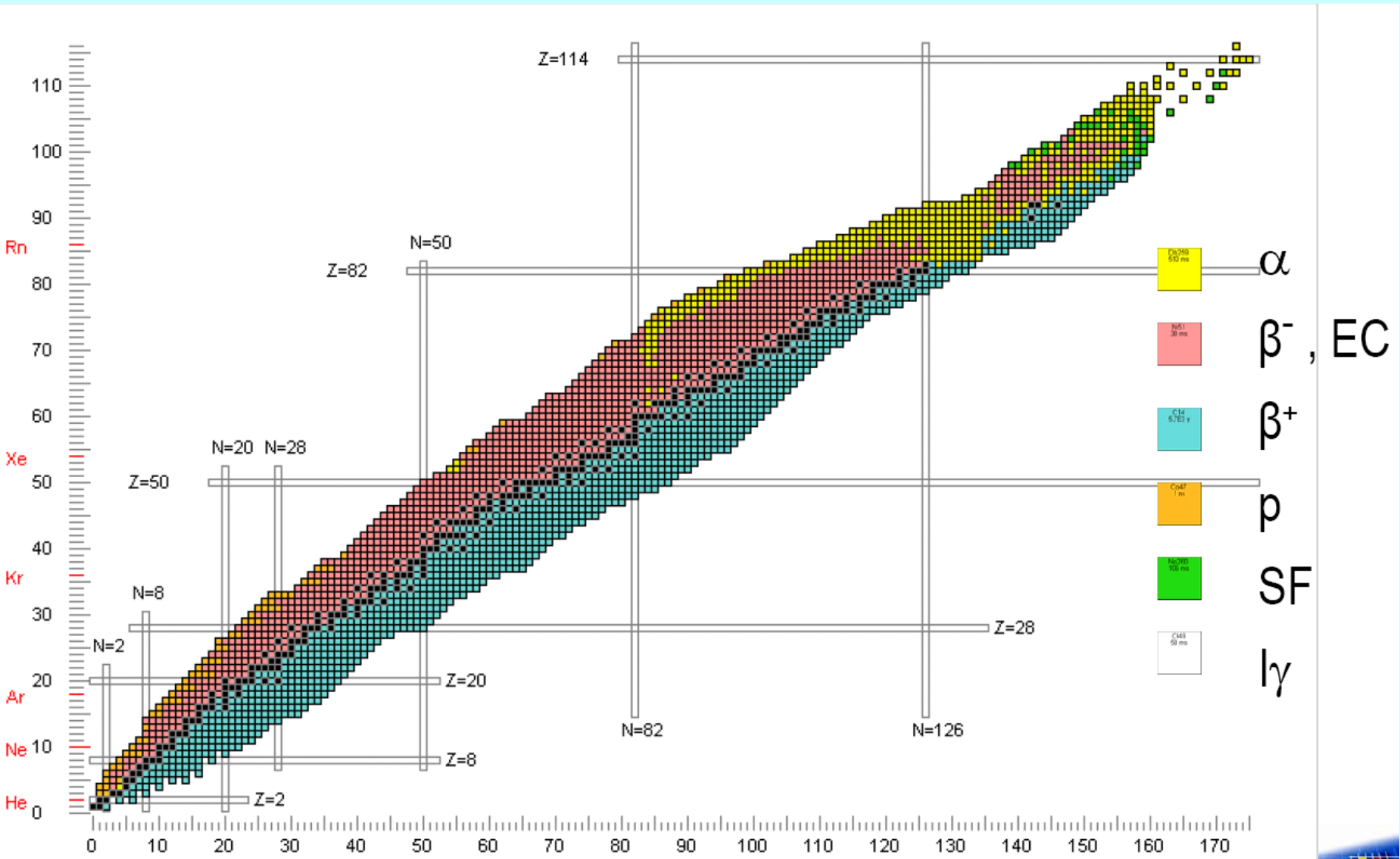
➤ Nucleon spin  $\vec{j} = \vec{l} + \vec{s} \quad j = l + \frac{1}{2}$  or  $l - \frac{1}{2}$

## Orbital parity: $\pi = (-1)^l$

$l$	0	1	2	3	4	5
	s	p	d	f	g	h
$\pi$	+	-	+	-	+	-



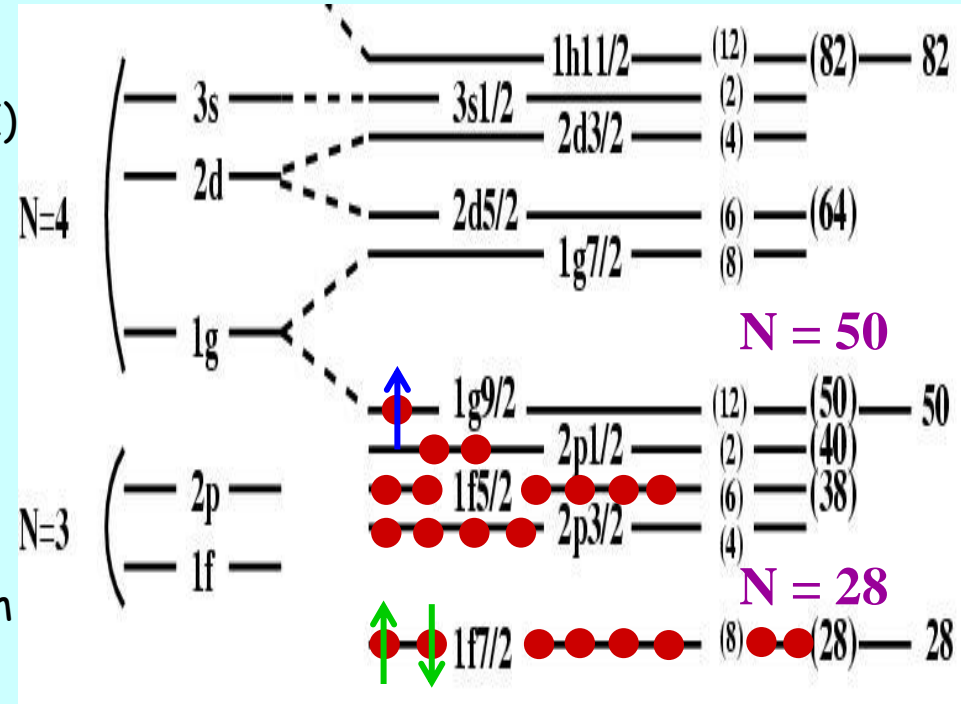
# Magic numbers





## Nucleus

- Composed of two liquids, protons (Z) and neutrons (N)
- Protons and neutrons are placed on orbitals independently
- Number of nucleon per orbital  
 $n = 2j + 1$
- Spin J of the nucleus; projections m  
 $J = \sum_i j_i$  with  $-J \leq m \leq j$



Protons (π) or neutrons (ν)

- Parity of the nucleus

$$\pi_{\text{nucleus}} = \prod_i \pi_i$$

- Pairing: 2 nucleons on same orbital couple their spin to zero

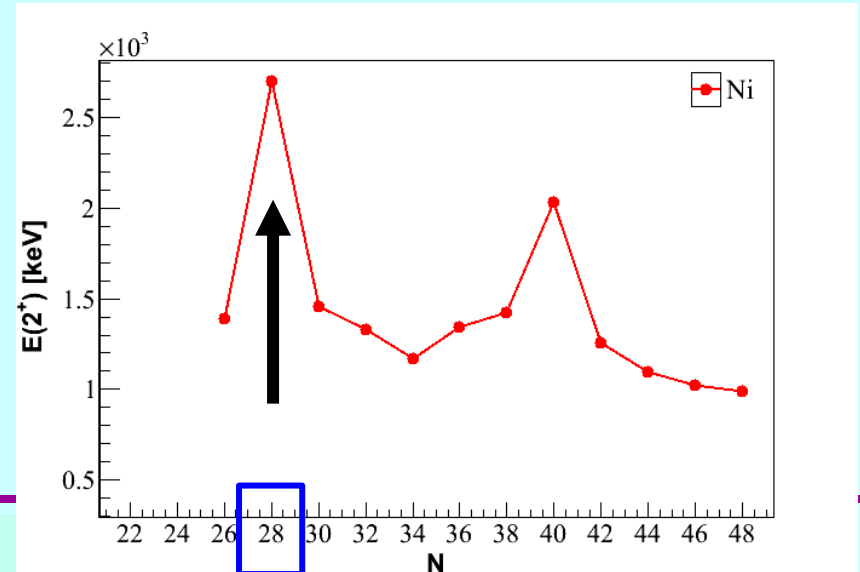
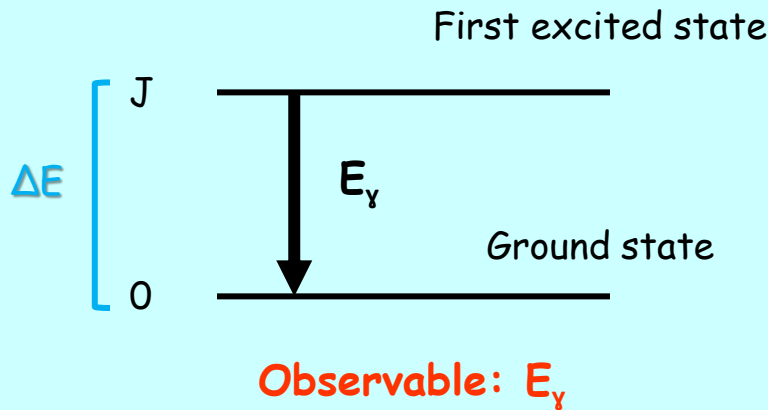
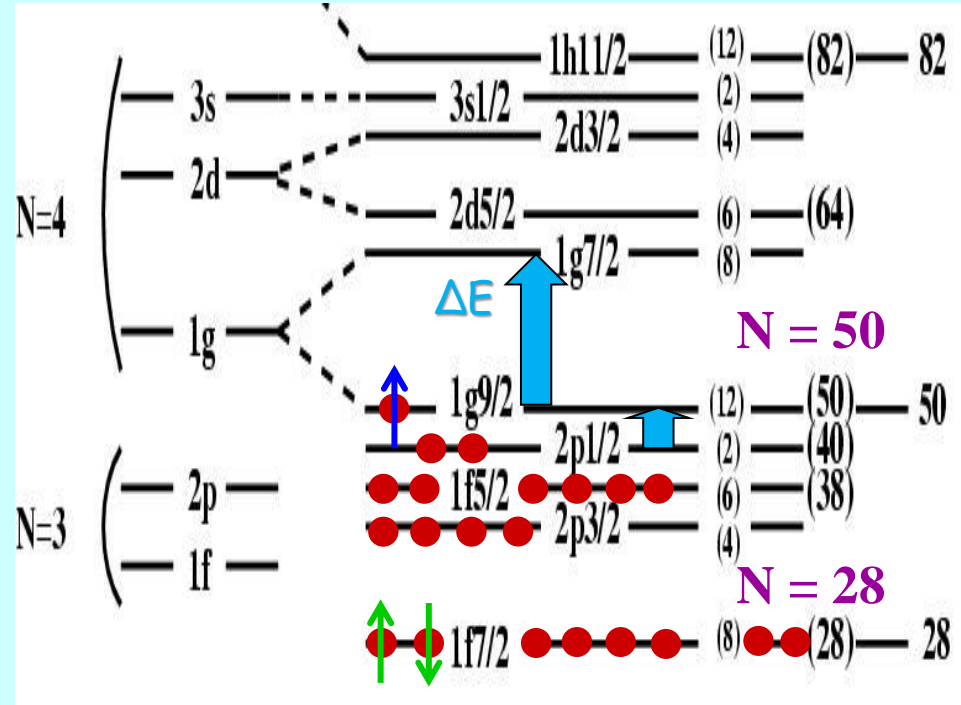
- ❑ Ground state spin of even-even nuclei:  $J = 0$
- ❑ Ground state spin of odd-even nuclei:  $J = j_{\text{single nucleon}}$

# Basic rules

## Nucleus

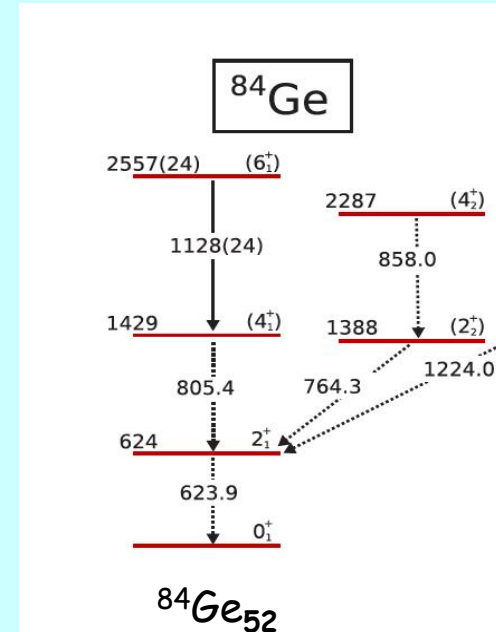
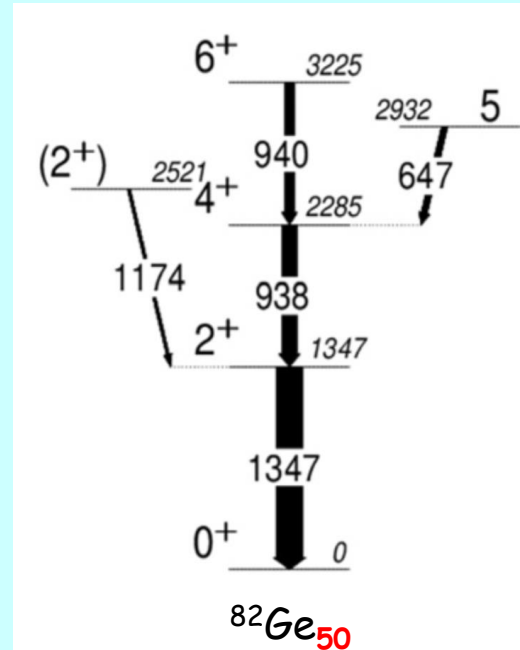
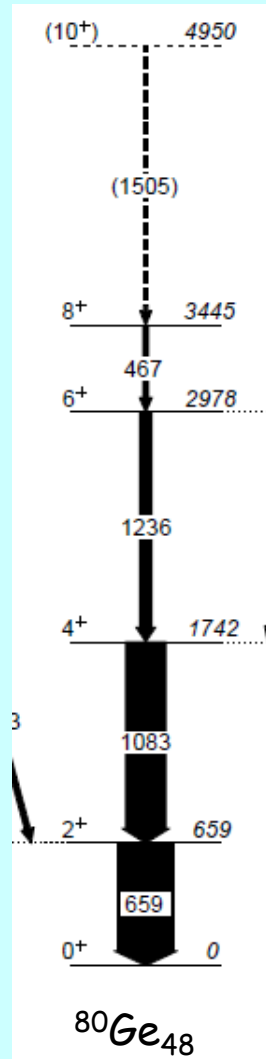
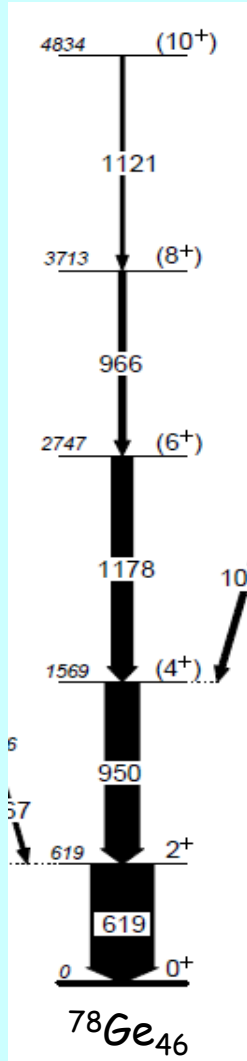
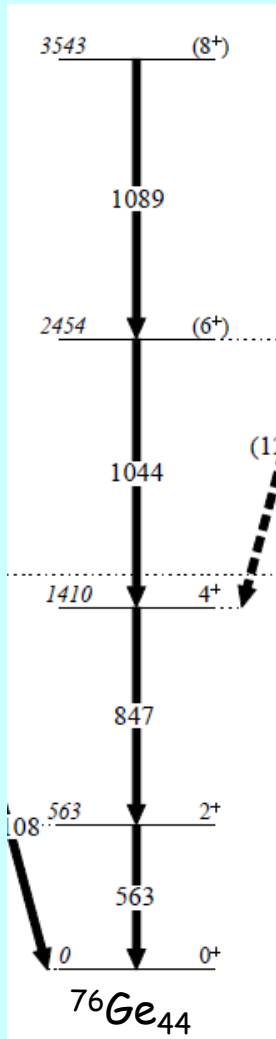
- Nucleon excitations within a shell need moderate energy
- Nucleon excitations across a shell gap need large energy
- Nucleus level scheme  

$$\Delta E = E_{\text{gap}} + E_{\text{pairing}} + E_{\text{correlations}}$$



# First 2<sup>+</sup> excitation energy E\*(2<sup>+</sup>)

Even Ge isotopes: Z=32

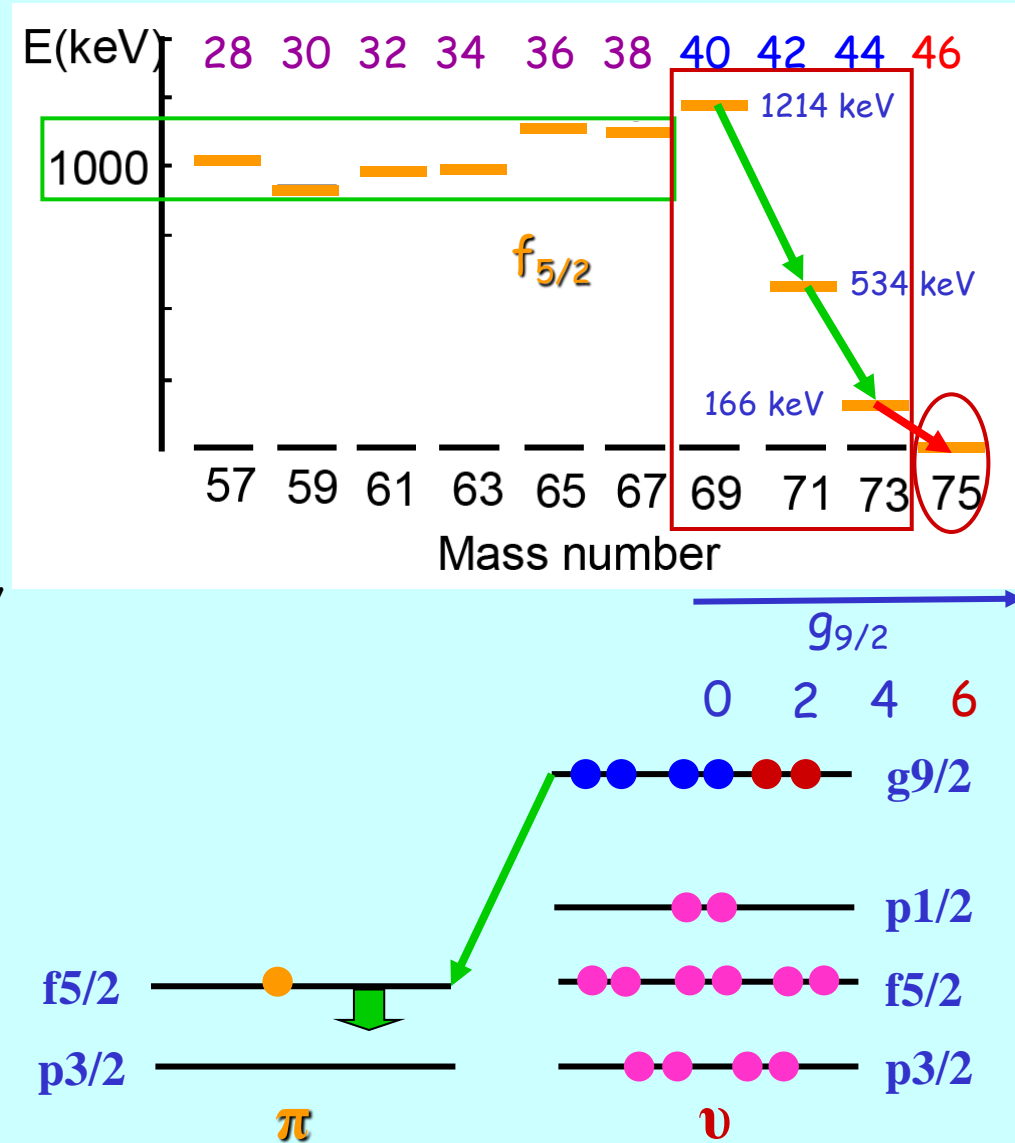


G. Duchêne

## Systematics

- Evolution of level energy (Indicator)
- Odd Cu:  $Z=29$ , even  $N$
- Ground state  $3/2^-$  (orbital  $p_{3/2}$ )
- Excited state  $5/2^-$  (orbital  $f_{5/2}$ )
- One proton promoted from  $p_{3/2}$  to  $f_{5/2}$
- Almost constant excitation energy  $E^* \sim 1$  MeV of the  $5/2^-$  state up to  $N=40$
- For  $N > 40$  ( $A > 69$ )  $g_{9/2}$  neutron orbital start to fill
- $E^* (5/2^-)$  strongly reduces

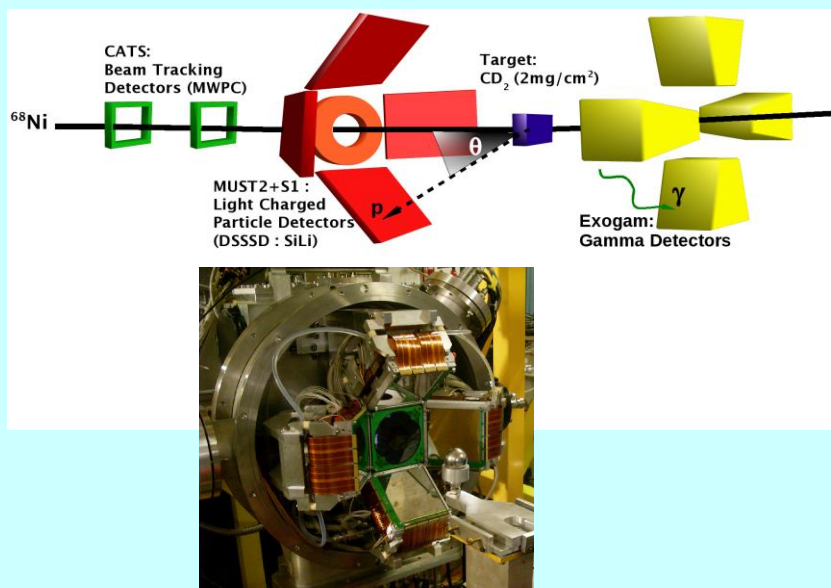
**Proton  $f_{5/2}$  - neutron  $g_{9/2}$  interaction**



# Orbital momentum assignment

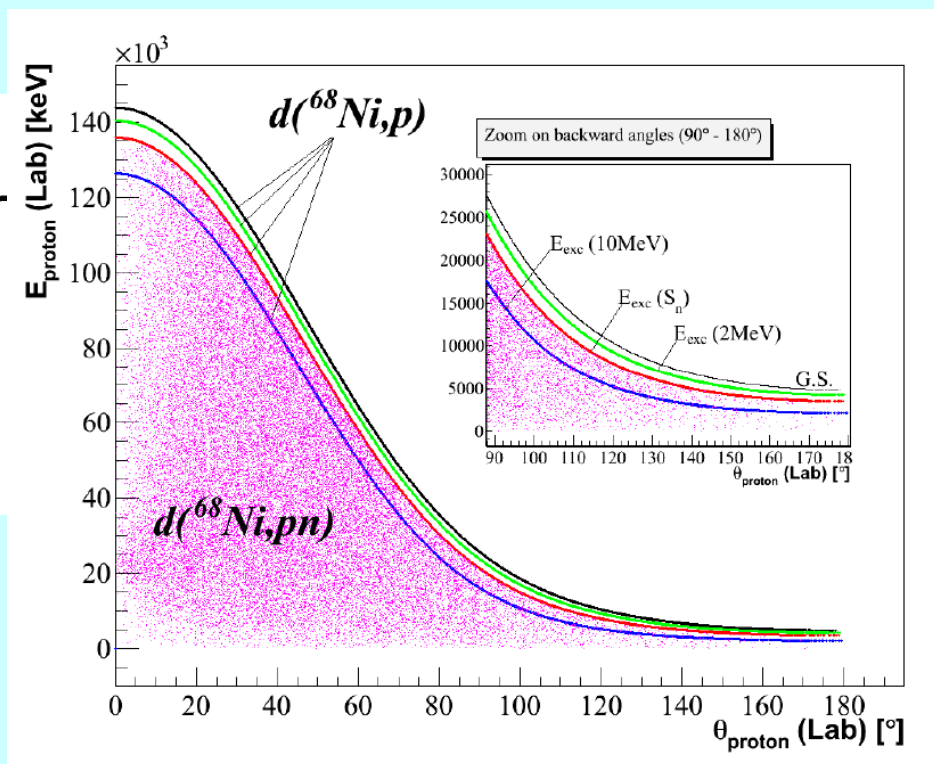
## Direct reaction

- $^{68}\text{Ni} + d \rightarrow ^{69}\text{Ni} + p$
- Orbital populated by the neutron with momentum  $l$
- Proton energy and angular distribution is affected by the neutron destination

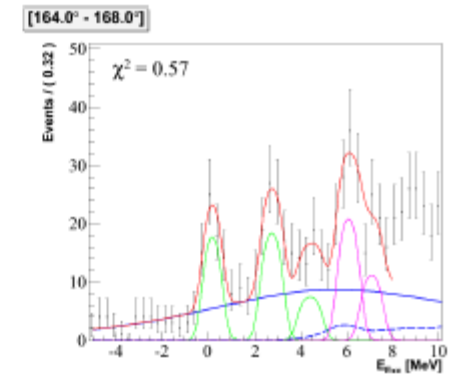
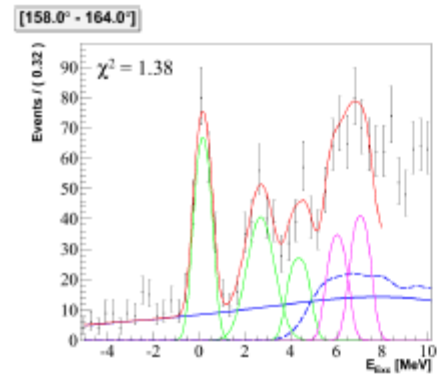
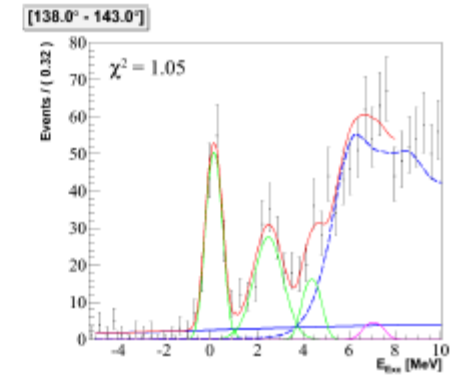
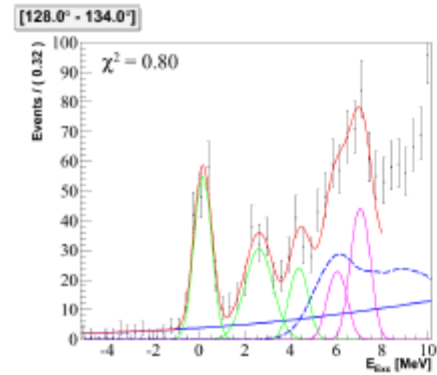
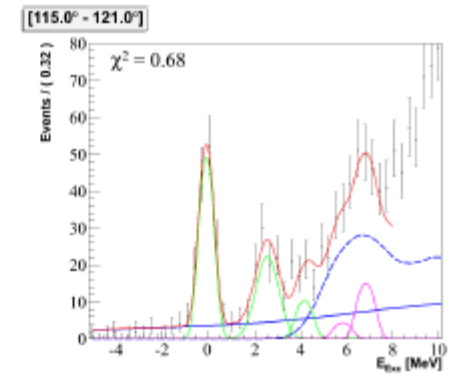
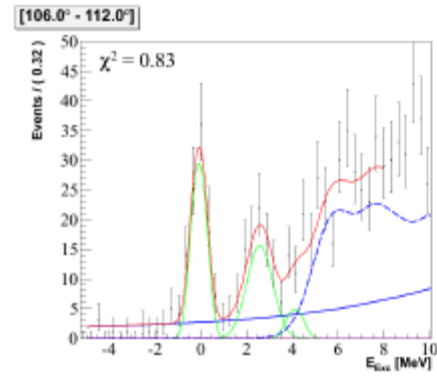
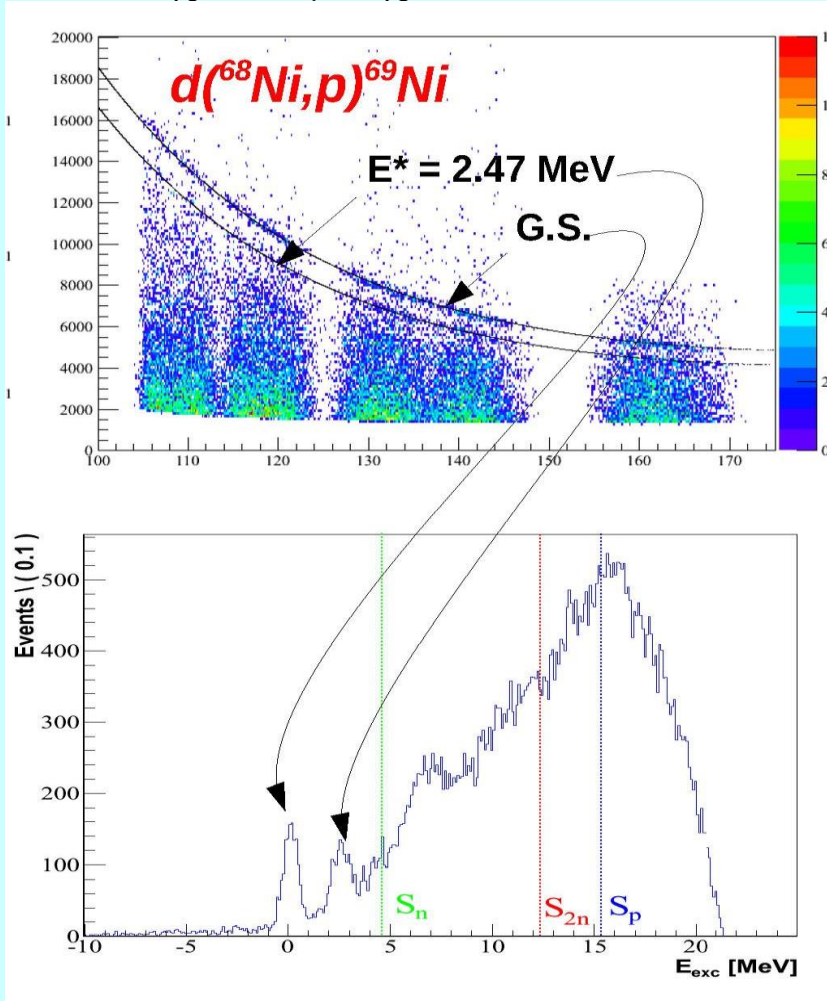


## Observables

- p energy  $\rightarrow$  excitation energy of the level populated
- p angular distribution  $\rightarrow l$

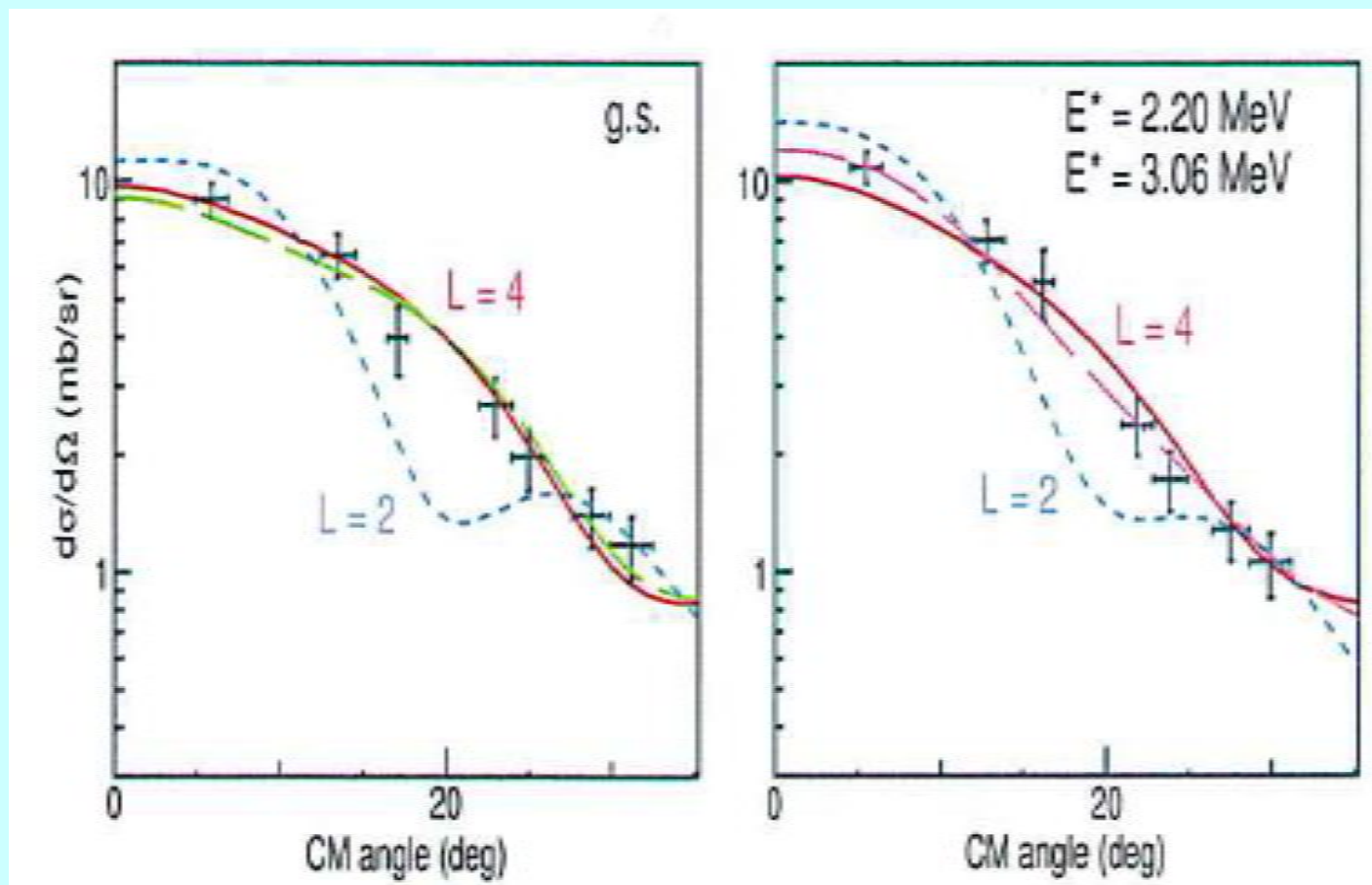


## Direct reaction



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# Orbital momentum assignment

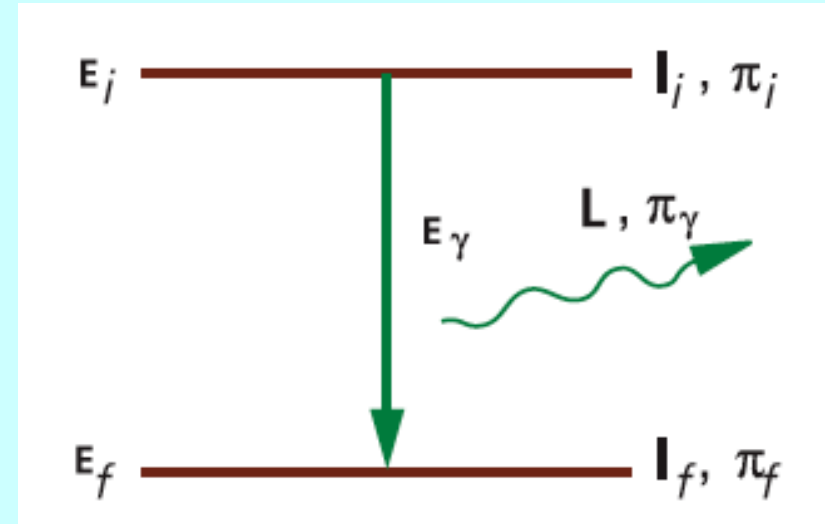


## Direct reaction

- With polarised d  $\rightarrow j = l \pm \frac{1}{2}$

## γ-ray transition

- Energy conservation:  $E_f = E_i - E_\gamma$   
i = initial; f = final
- Parity conservation:  $\pi_\gamma = \pi_i \cdot \pi_f$ 
  - ❑  $\pi_\gamma = (-1)^l$  for an electric transition E
  - ❑  $\pi_\gamma = (-1)^{l+1}$  for a magnetic transition M
- Spin:  $|I_i - I_f| \leq l \leq I_i + I_f$



Transition	Désignation	$L_\gamma$	$\pi_\gamma$
Dipolaire électrique	E1	1	-1
Dipolaire magnétique	M1	1	+1
Quadripolaire électrique	E2	2	+1
Quadripolaire magnétique	M2	2	-1
Octupolaire électrique	E3	3	-1



## $\gamma$ -ray transition

Examples:

->  $2^+ \rightarrow 0^+$  transition:

$$2-0 \leq l \leq 2+0; l=2; \pi_\gamma = +1$$

**electric transition E2**

->  $4^+ \rightarrow 2^+$  transition:

$$4-2 \leq l \leq 4+2; l=2, 3, 4, 5, 6$$

E2, M3, E4, M5, E6

$$\pi_\gamma = (+1).(+1) = +1$$

E2 favored vs M3

**electric transition E2**

->  $4^+ \rightarrow 2^-$  transition:

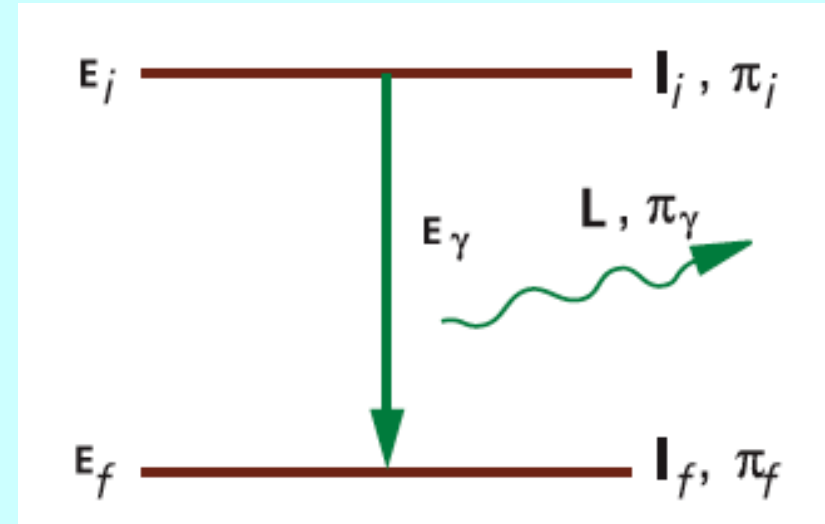
$$2 \leq l \leq 6; l=2, 3, 4, 5, 6$$

M2, E3, M4, E5, M6

$$\pi_\gamma = (+1).(-1) = -1$$

M2 unfavored vs E3

**E3 or mixed M2+E3 transition**



->  $3^+ \rightarrow 2^+$  transition:

$$1 \leq l \leq 5; l=1, 2, 3, 4, 5$$

M1, E2, M3, E4, M5

$$\pi_\gamma = (+1).(+1) = +1$$

M1 unfavored vs E2

**2mixed M1+E2 transition**

# Transition probabilities

## Charge distribution of the nucleus

- Electric or magnetic dipole described in  $l$  order  $r^\lambda \cdot Y_{\lambda\mu}(\theta, \varphi)$
- Lowest orders are most likely
- Reduced matrix element for a transition from  $J_i$  to  $J_f$  with projections  $m_i$  and  $m_f$

$$B(\sigma, \lambda; J_i \rightarrow J_f) = \sum_{m_f \mu} \left| \langle \alpha_f; J_f m_f | M(\sigma, \lambda \mu) | \alpha_i; J_i m_i \rangle \right|^2 \quad \text{with } m_f = m_i + \lambda$$

Following Wigner-Eckart

$$B(\sigma, \lambda; J_i \rightarrow J_f) = \frac{1}{2J_i + 1} \left| \langle \alpha_f \| M(\sigma, \lambda) \| \alpha_i \rangle \right|^2$$

where the multipolar electric moment writes

$$M(E\lambda\mu) = \int_{\text{noyau}} \rho(r) \cdot r^\lambda Y_{\lambda\mu}(\hat{r}) \cdot dv$$

and the multipolar magnetic moment writes

$$M(M\lambda\mu) = \frac{-1}{c(\lambda + 1)} \int_{\text{noyau}} j(r) \cdot (r \times \nabla) r^\lambda Y_{\lambda\mu}(\hat{r}) \cdot dv$$

## Amplitude of transition probability

$$\Gamma_{if}(\{EL \text{ ou } ML\}; J_i \rightarrow J_f) = \frac{2(L+1)}{L[(2L+1)!!]^2} \frac{1}{\hbar} \left( \frac{\hbar\omega}{\hbar c} \right)^{2L+1} B(\{EL \text{ ou } ML\}; J_i \rightarrow J_f)$$

where  $\hbar = 6.58211899(16) \cdot 10^{-19} \text{ keV} \cdot \text{s}$

$B(EL)$  en unité de  $e^2 \text{ fm}^{2L}$

$\hbar c = 197,3269631(49) \cdot 10^3 \text{ keV} \cdot \text{fm}$

$B(ML)$  en unité de  $(e\hbar / 2Mc)^2 \text{ fm}^{2L-2}$

$$\Gamma_w(E1) = 1.59 \times 10^{15} \cdot E^3 \cdot B(E1) \quad \Gamma_w(M1) = 1.76 \times 10^{13} \cdot E^3 \cdot B(M1)$$

$$\Gamma_w(E2) = 1.22 \times 10^9 \cdot E^5 \cdot B(E2) \quad \Gamma_w(M2) = 1.35 \times 10^7 \cdot E^5 \cdot B(M2)$$

$$\Gamma_w(E3) = 5.67 \times 10^2 \cdot E^7 \cdot B(E3) \quad \Gamma_w(M3) = 6.28 \times 10^0 \cdot E^7 \cdot B(M3)$$

$$\Gamma_w(E4) = 1.69 \times 10^{-4} \cdot E^9 \cdot B(E4) \quad \Gamma_w(M4) = 1.87 \times 10^{-6} \cdot E^9 \cdot B(M4)$$

in Weisskopf unit

Transitions of smallest  $L$  predominate

Electric transitions predominate on magnetic transitions

# Transition probability and half life

## Half life of a state

$$\Gamma_{if}(\{EL \text{ ou } ML\}; J_i \rightarrow J_f) = \frac{2(L+1)}{L[(2L+1)!!]^2} \frac{1}{\hbar} \left( \frac{\hbar\omega}{\hbar c} \right)^{2L+1} B(\{EL \text{ ou } ML\}; J_i \rightarrow J_f)$$

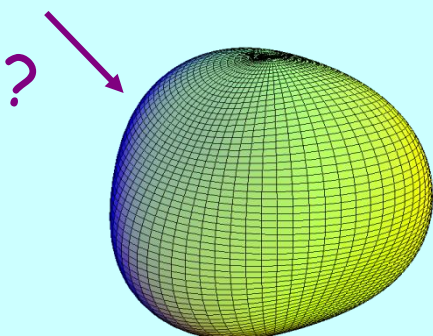
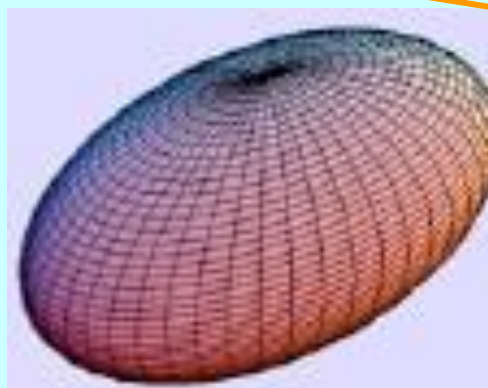
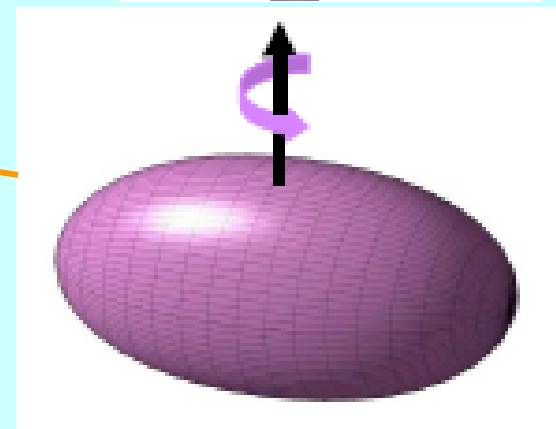
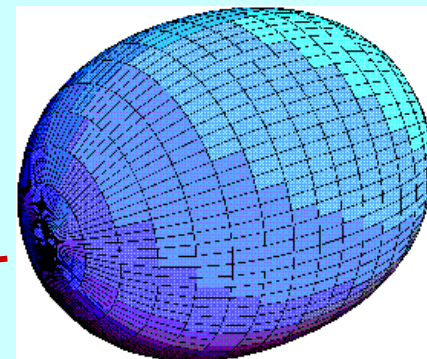
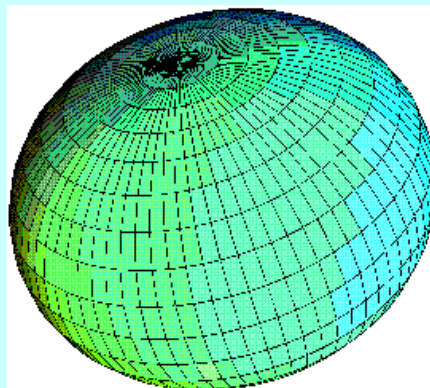
- The transition-probability amplitude  $\Gamma_{if}$  is related to the half life of state "i"
- Heisenberg:  $\hbar = \tau_i \cdot \Gamma_i$  with  $\Gamma_i = \sum_f \Gamma_{if}(\sigma\lambda)$  including all decay paths
- Half life is deduced  $T_{1/2} = \tau \cdot \ln(2) = \frac{\hbar \cdot \ln(2)}{\Gamma}$

State half life depend on

- initial and final spins
- single-particle configuration of the initial and final states

# Nuclear shapes

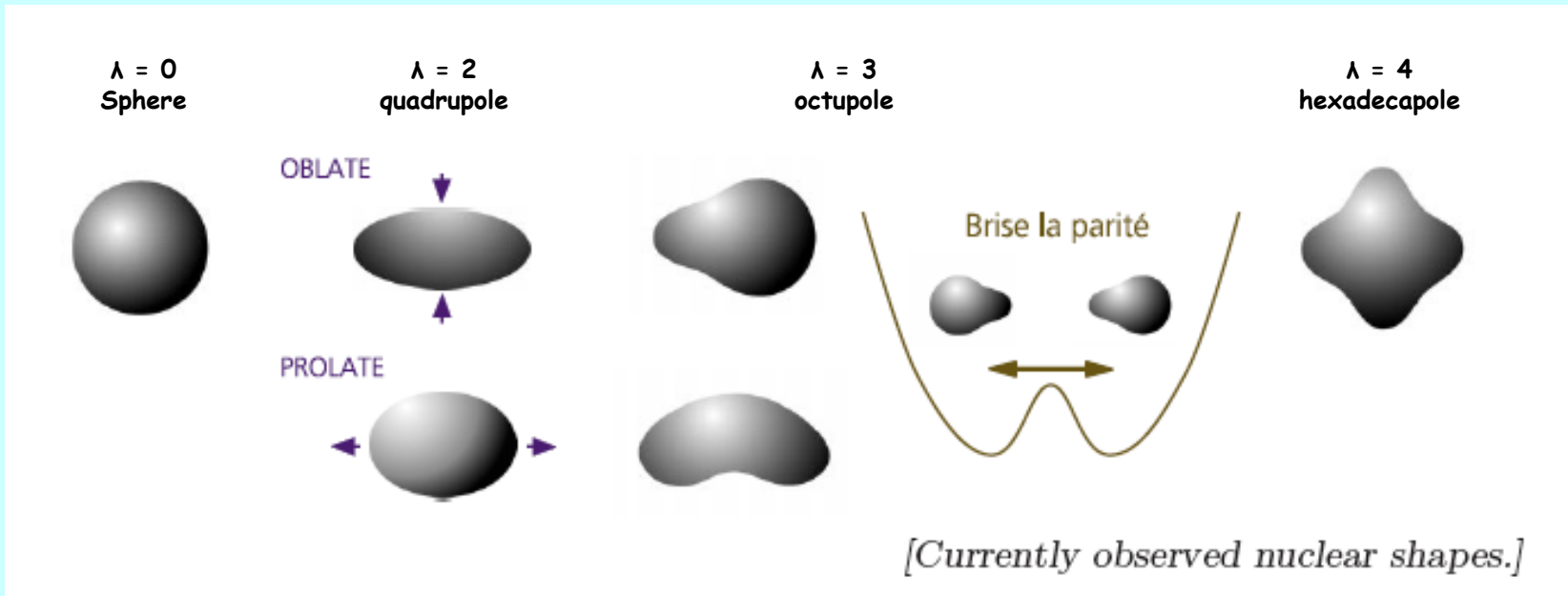
- Spherical
- Oblate
- Prolate
- Super deformed
- Triaxial
- Pyramidal ?

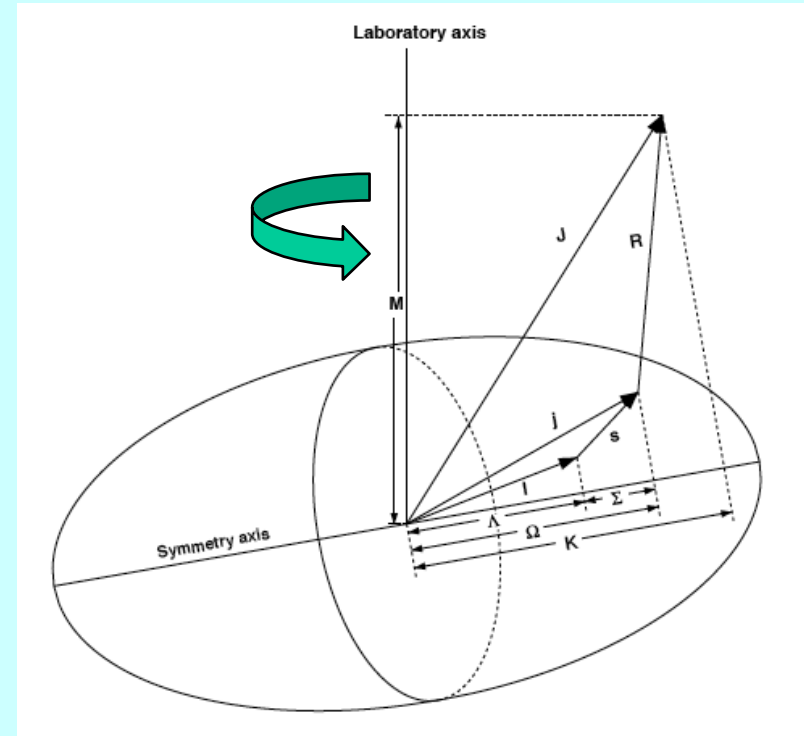
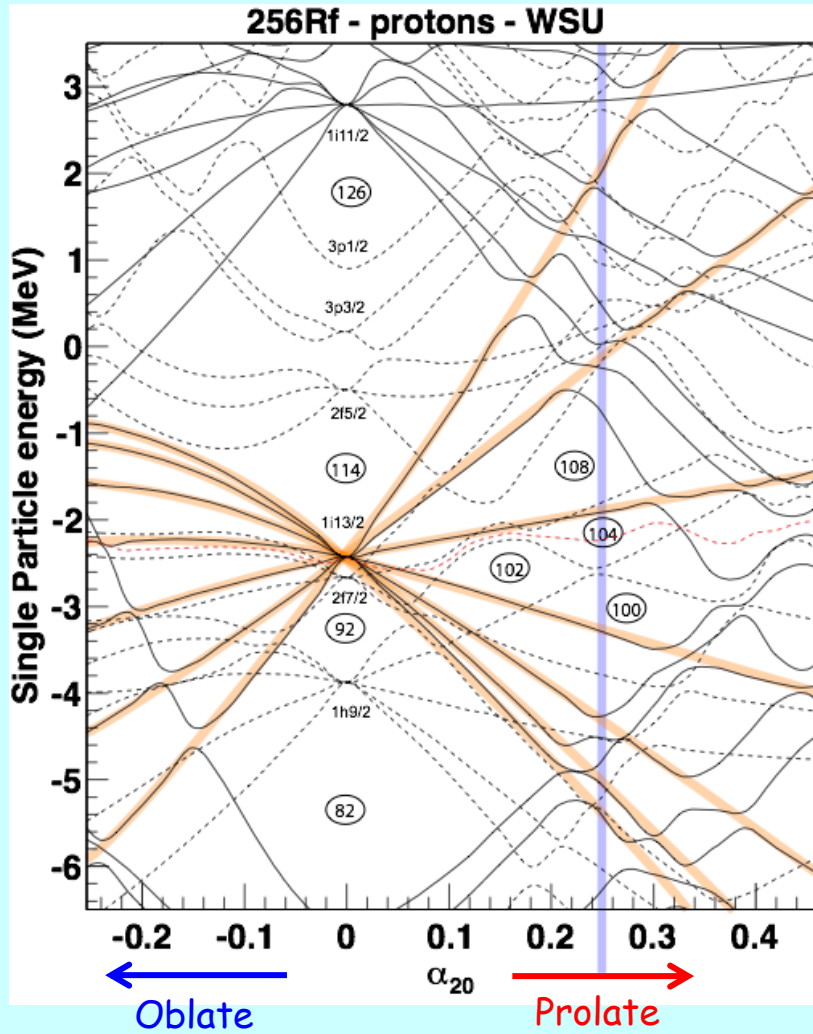


# Nuclear shapes

## Nuclear shape parametrisation

$$R(\theta, \phi) = R_0 \left[ 1 + \sum_{\lambda=2}^{\infty} \sum_{\mu=-\lambda}^{\lambda} \alpha_{\lambda\mu}^* Y_{\lambda\mu}(\theta, \phi) \right].$$





# Rotational bands

Excitation energy

$$E_{rot} = \frac{\hbar^2 [I(I+1) - K^2]}{2\mathfrak{I}}$$

$\gamma$ -ray transition energy

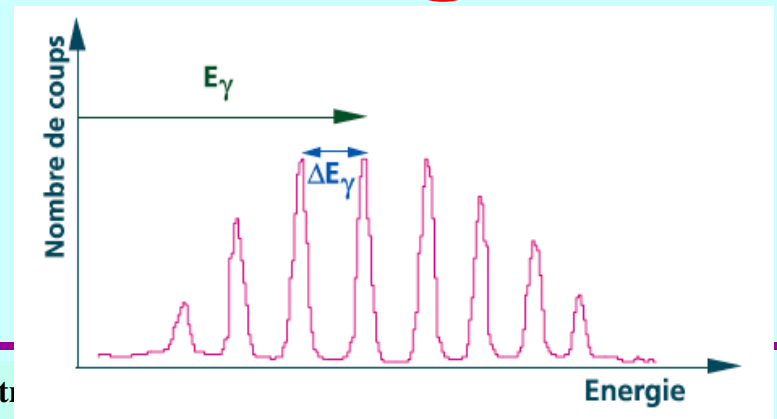
$$E_\gamma = \Delta E_{rot}$$

$$E_\gamma(I \rightarrow I-2) = \frac{\hbar^2 [I(I+1) - (I-2)(I-1)]}{2\mathfrak{I}} = \frac{\hbar^2 [4I-2]}{2\mathfrak{I}}$$

Difference between two consecutive transitions

$$\Delta E_\gamma(I, I-2) = \frac{\hbar^2 [4I-2]}{2\mathfrak{I}} - \frac{\hbar^2 [4(I-2)-2]}{2\mathfrak{I}} = \frac{4\hbar^2 [I - (I-2)]}{2\mathfrak{I}} = \frac{4\hbar^2}{\mathfrak{I}} \text{ Constant !!}$$

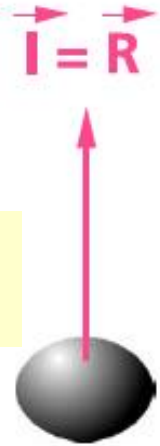
Regular spacing of  $\gamma$  rays





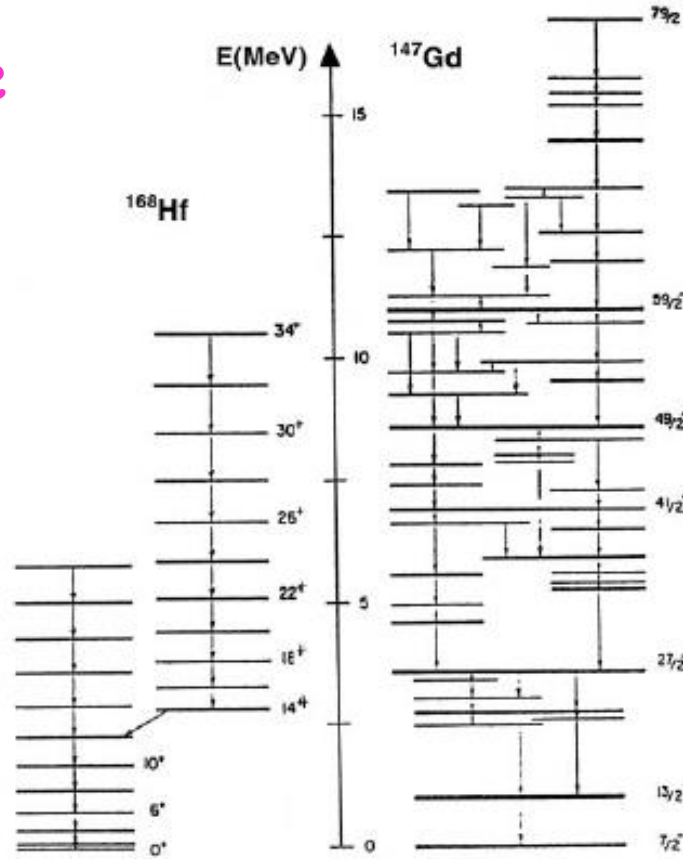
# Nuclear shapes

Collective



$\Gamma \sim 100 Wu$   
 $\tau \sim 100 fs$

Regular  
level scheme

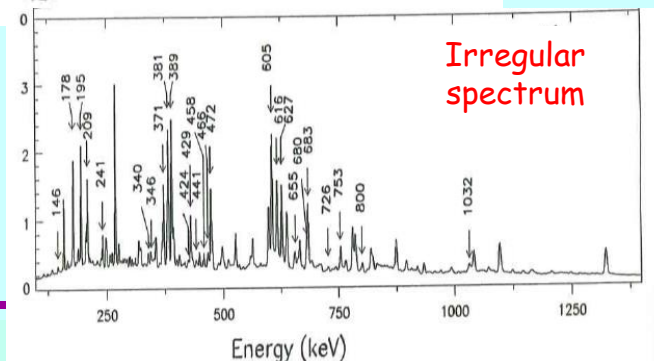
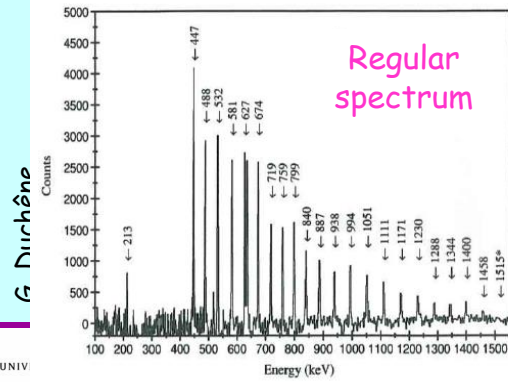


Individual



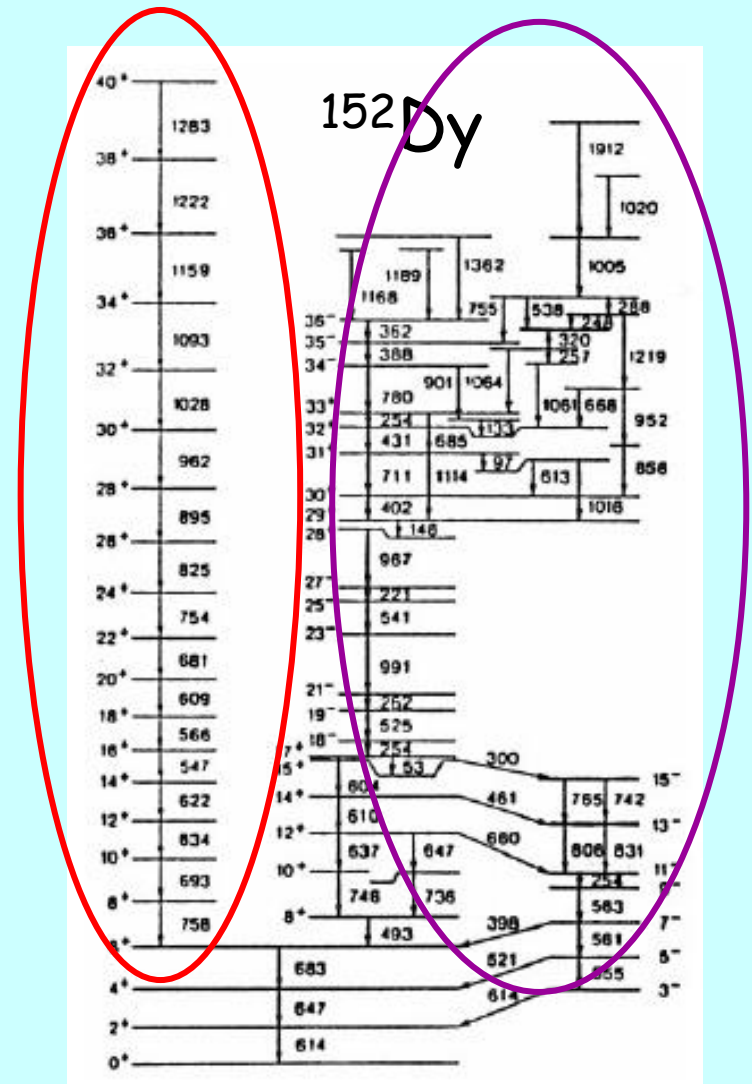
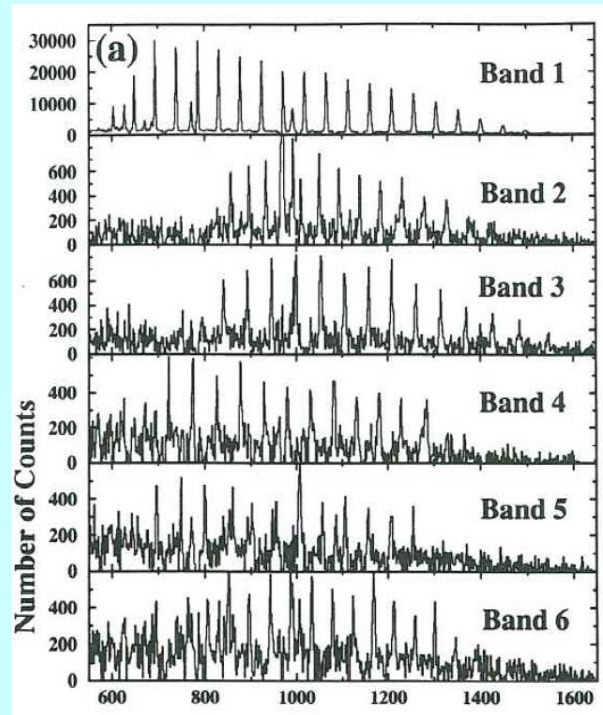
$\Gamma \sim \text{few } Wu$   
 $\tau > 10 ps$

Irregular  
level scheme



## Super deformed prolate shape

- $\Gamma \sim 2000 W_u$
- $\tau \sim 10$  fs



- Shape coexistence with **normal deformed**, single particle states

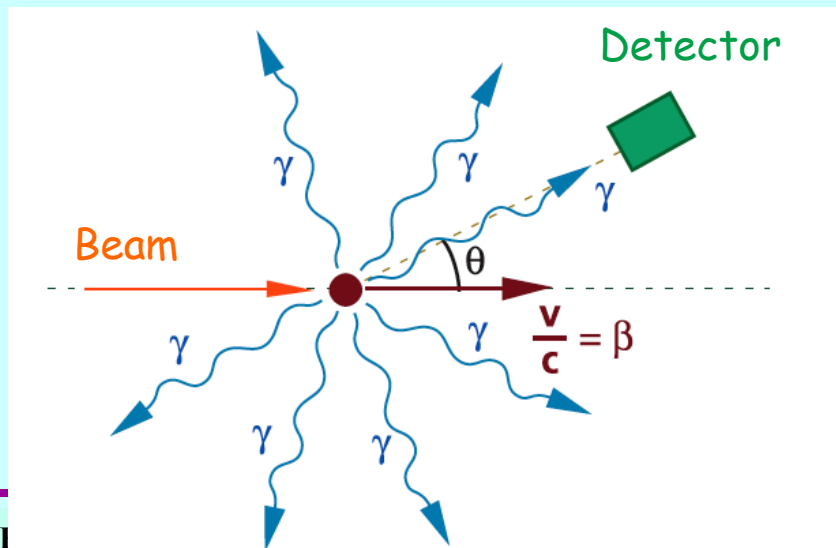
## Many techniques

- DSAM (Doppler Shift Attenuation Method) -> below ps
- Plunger -> ps to ns
- Fast scintillators (LaBr<sub>3</sub>) -> ps to ns
- ToF -> > μs

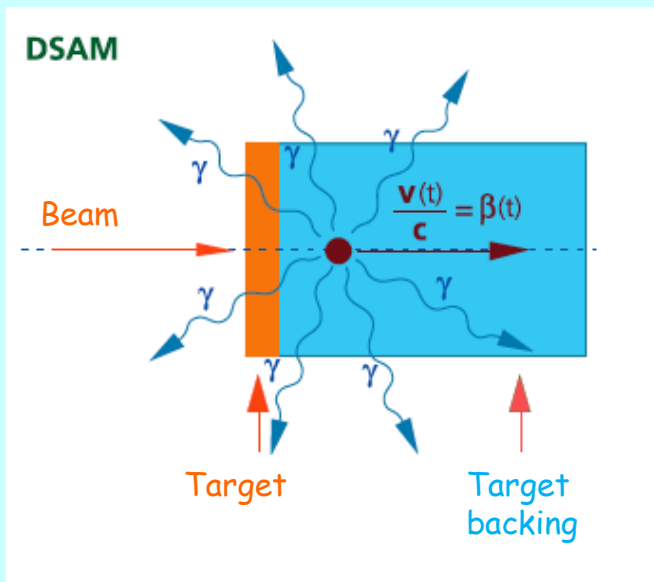
## Doppler effect

- $v$  = recoil velocity of the nucleus
- Detected energy depend on the angle of the detector relative to the beam axis

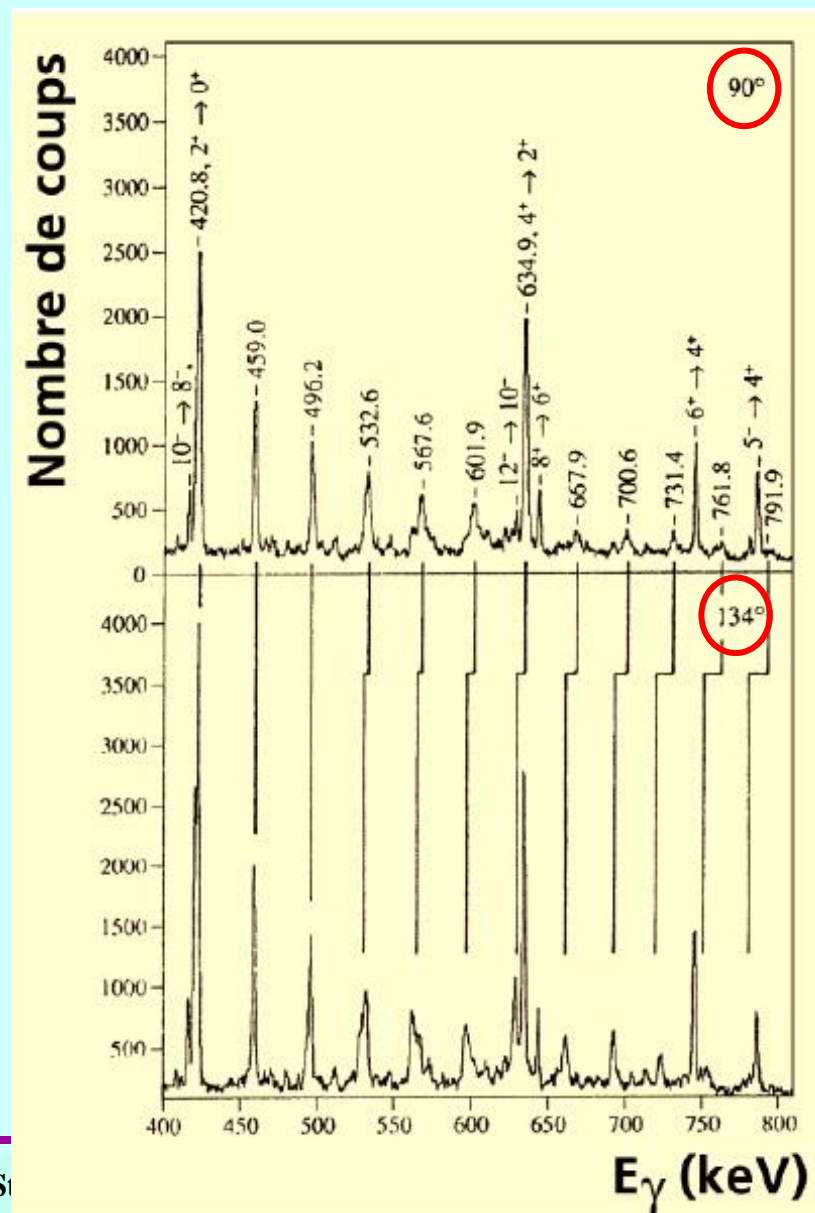
$$\Delta E_{\gamma}(\theta, E_{\gamma}) = E_{\gamma} \frac{v}{c} \cos(\theta).$$



## DSAM



- Nucleus de-excitation during the slowing down in the backing of the target
- Varying velocity  $\rightarrow$  different Doppler shift
- Depend on the stopping power of the target and backing
- Lifetimes from 10 fs to few 100 fs

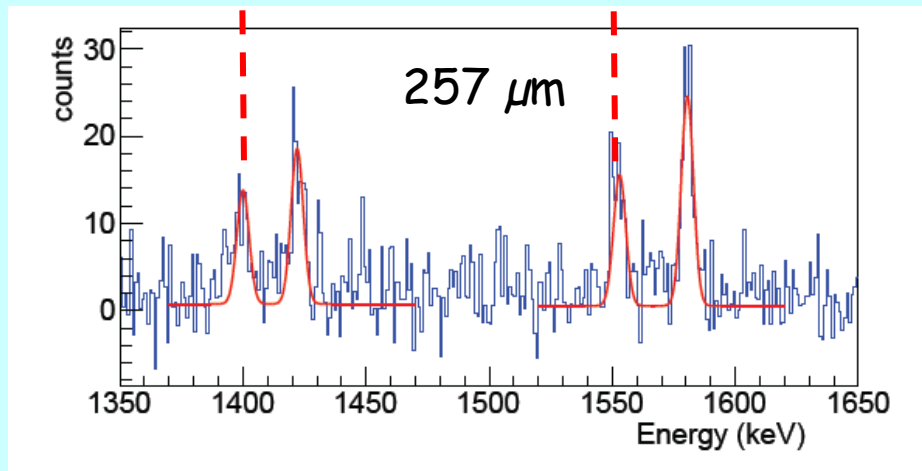
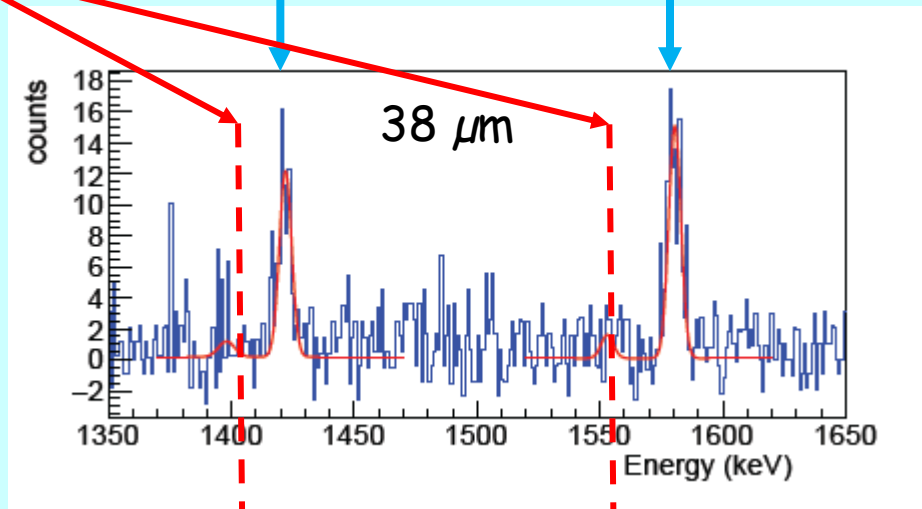
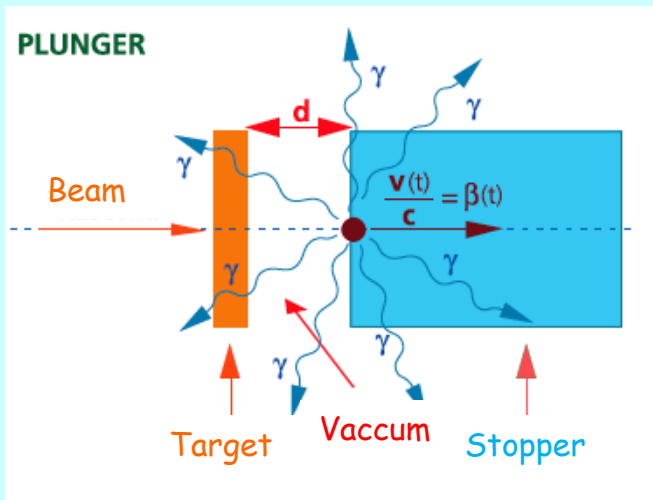


# Nuclear lifetime measurements

## Plunger

N flight component

Stopped components



- Nucleus de-excitation
  - ❑ during the flight in vacuum (Doppler shifted)
  - ❑ At rest in the stopper
- Two velocities → two peaks
- Varies with distance  $d$  and lifetime  $\tau$
- Lifetimes from ps to ns

# Angular distributions

## Spin alignment

- In the plan perpendicular to the beam
- Aligned nuclear states ( $m \sim 0$ )
- Anisotropic  $\gamma$ -ray emission (not uniform emission in  $4\pi$ )

$$\vec{l} = \vec{r} \wedge \vec{p}$$

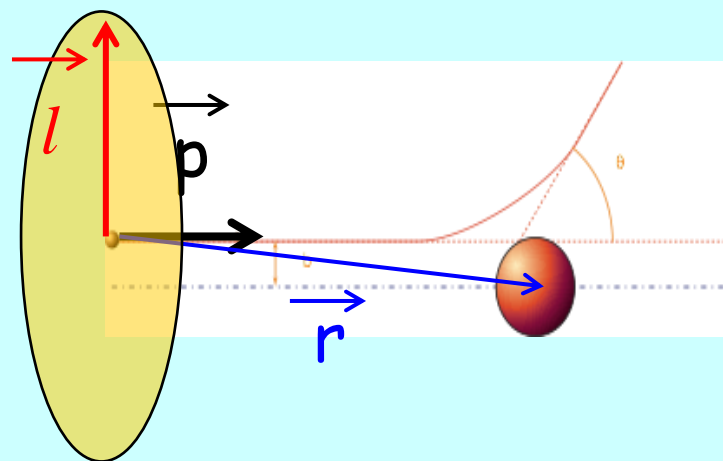
## Angular distribution

- Distribution of normalised intensity

$$w(\theta) = \frac{I_\gamma(\theta)}{I_\gamma} = 1 + a_2 P_2(\cos \theta) + a_4 P_4(\cos \theta) + \dots$$

where

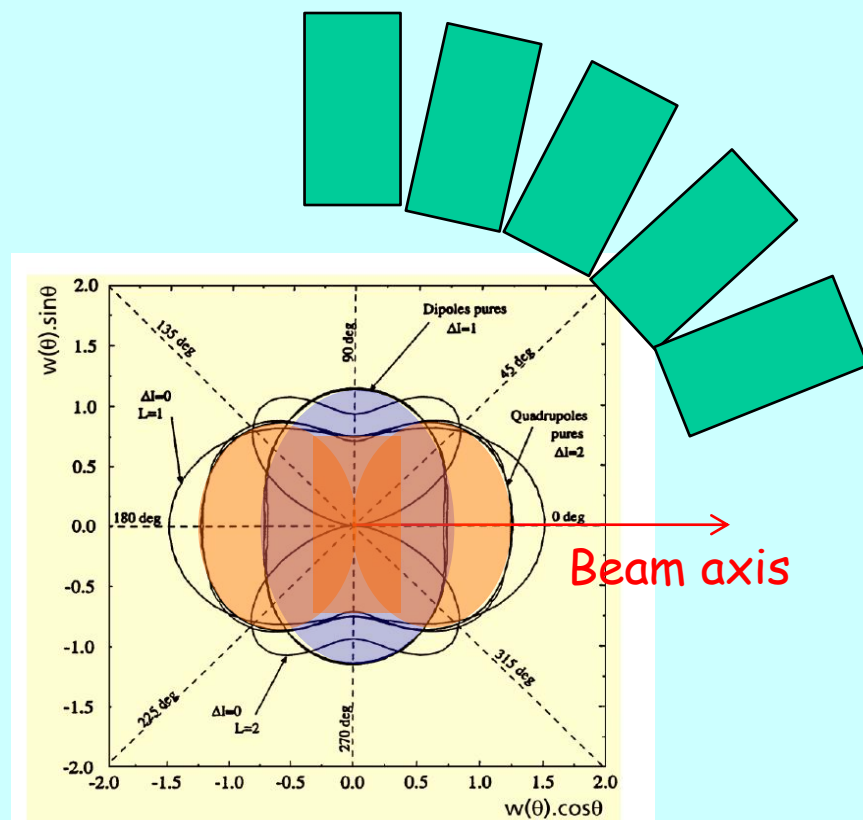
- ❑  $\theta$  = angle between  $\gamma$  ray (detector) and beam axis
- ❑  $P_i(\cos \theta)$  = Legendre polynomials
- ❑ Pure dipole ( $l=1$ ):  $a_2$  negative and  $a_4=0$
- ❑ Stretched quadrupole ( $l=2$ ):  $a_2$  positive and  $a_4 < 0$  and small



# Angular distributions

## Angular distribution

- $\gamma$ -ray intensity varies with angle  $\theta$  versus beam axis
- For pure stretched ( $\Delta I=1$ ) dipole transitions
  - ❑ max at  $90^\circ$
  - ❑ Smallest at  $0^\circ$
- For pure stretched ( $\Delta I=2$ ) quadrupole transitions
  - ❑ max at  $\sim 45^\circ$
  - ❑ Important at  $0^\circ$
  - ❑ Smallest at  $90^\circ$

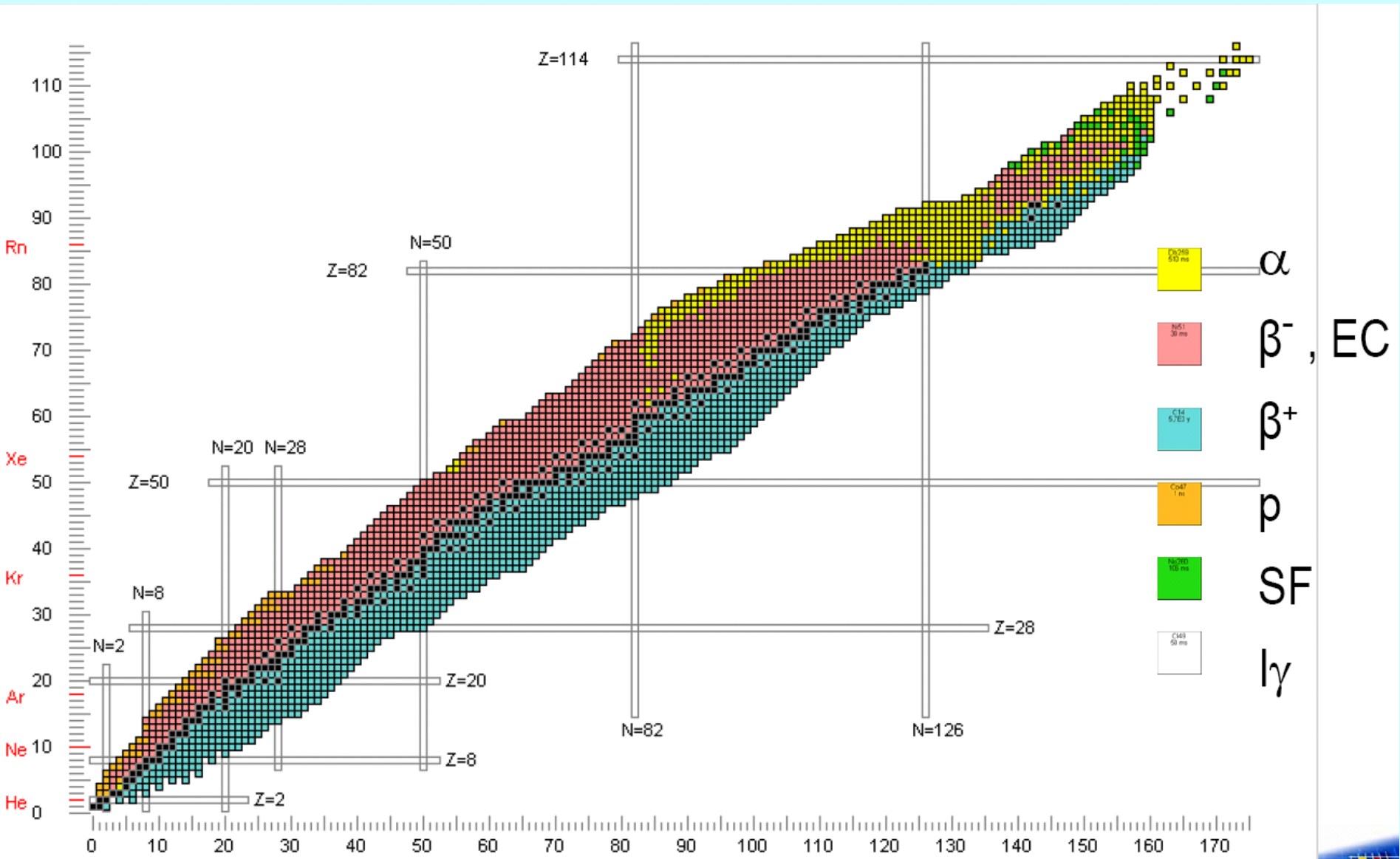


# Lecture plan

1. Introduction
2. Radiation-matter interactions and detectors for charged particle and  $\gamma$  rays
3. Nuclear reactions
4. Nuclear structure and observables
5. Perspectives



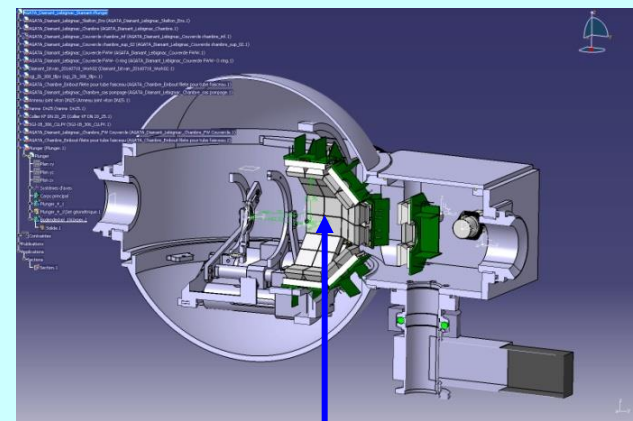
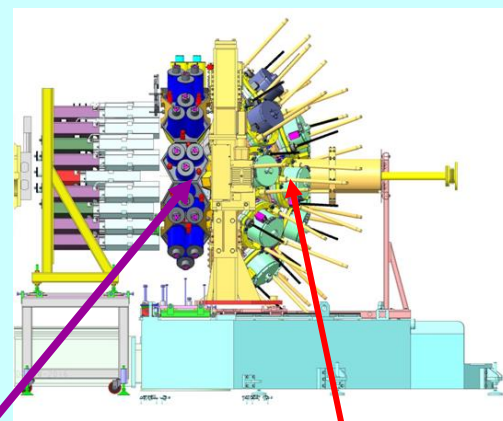
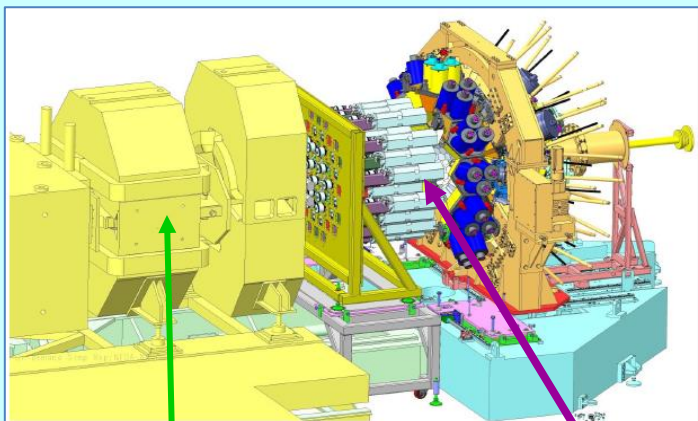
# Magic numbers



## Coupling of different detectors to AGATA

- GANIL physics campaigns  
2018

8 experiments using AGATA+NEDA (+DIAMANT) (+LaBr3) (+plunger)



VAMOS++  
spectrometer

NEDA + neutron-wall  
Neutron detector

AGATA  
for  $\gamma$  detection

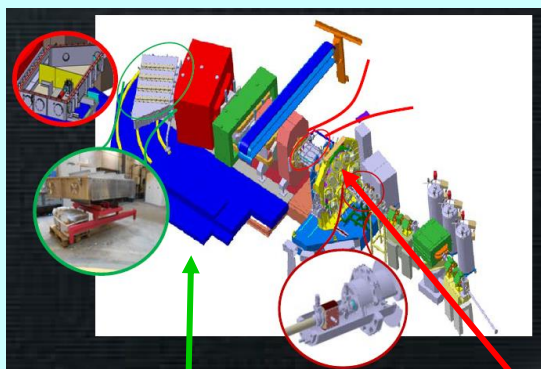
DIAMANT  
for p,  $\alpha$  detection

Structure study of  $N \sim Z$  nuclei and around  $^{100}\text{Sn}$

G. Duchêne

## Coupling of different detectors to AGATA

- GANIL physics campaigns  
2019 - (2020)

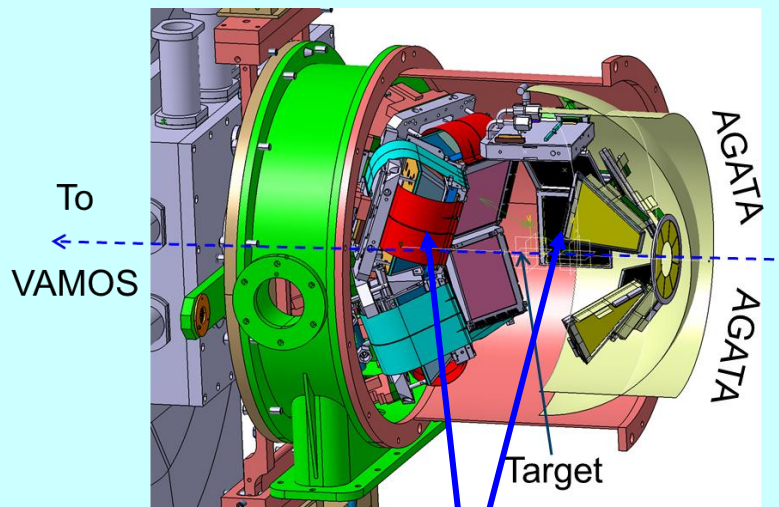


VAMOS  
spectrometer  
in Gas Filled Mode  
(GFM)

AGATA  
for  $\gamma$  detection

Structure study of  
superheavy elements

Nucleon transfer spectroscopy  
using **SPIRAL1 ISOL** beams



MUGAST  
for  $p, \alpha$  detection

## New accelerators for exotic beam

- SPES in 2022 (Legnaro, Italy) -> radioactive beams up to  $10^8$  particule per sec
- HIE-ISOLDE in 2020 (CERN, Switzerland) -> radioactive beams up to  $10^8$  part. per sec
  - ❑ ISOL technique (fission products reaccelerated)

### Structure study of neutron-rich nuclei around $^{78}\text{Ni}$ and above

- FAIR in 2025 (Darmstadt, Germany) -> intense radioactive beams at high energy
  - ❑ Fragmentation technique

### Structure study of exotic nuclei

- GANIL SPIRAL2 (Caen, France) -> very intense stable beam (2018)  
-> very intense exotic beams (ISOL technique) ??

### Structure study of exotic nuclei