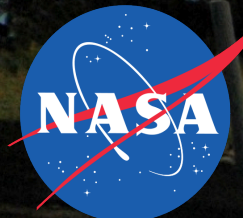


# The APOLLO Lunar Ranging Program

James Battat  
Wellesley College



DSU 2018, Annecy le Vieux  
June 28, 2018



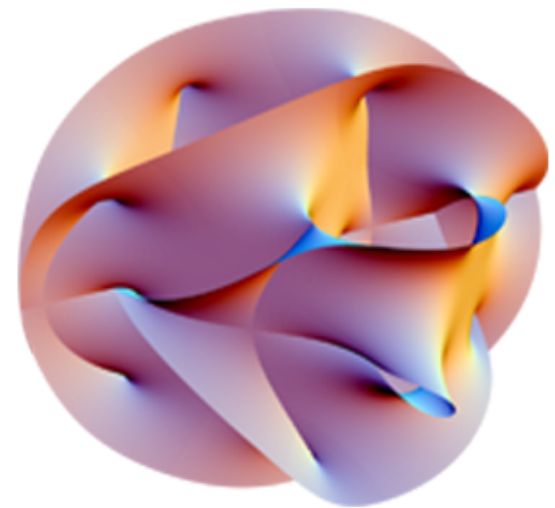


# Outline

- Motivation & science capability of LLR
- Historical LLR performance
- APOLLO system and status  
< 1-2 mm range ~~precision~~ accuracy
- Computational model improvements underway  
to extract gravitational physics constraints

# The motivation to search

- All fundamental forces deserve experimental scrutiny
- General Relativity and Quantum Mechanics are fundamentally incompatible. Gravity is relatively *poorly tested*
- Scalar fields from string-inspired models can produce measurable effects:
  - Violation of equivalence principle
  - Time variation of fundamental constants
- Precision tests of gravity provide incisive tests of post-Einstein theories



# LLR: a precision probe of gravity

these are **existing** constraints – expect 10x improvement with APOLLO

- Weak EP  $\Delta a/a \ 10^{-13}$
- Strong EP  $\eta \ 10^{-4}$
- $1/r^2$  deviations  $10^{-10} F_G$
- $(dG/dt)/G \ 10^{-12} \text{ yr}^{-1}$  (1% over the age of the Universe)
  
- Gravitomagnetism  $0.1\%$
- Geodetic precession  $0.5\%$

Earth-Moon has  $v^2/c^2 \sim 10^{-8}$  in the Solar System frame  
Expect relativistic phenomena of order  $(10^{-8})(4e8) \text{ m} \sim 4 \text{ m}$

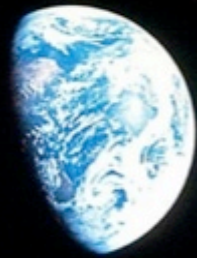


# LLR: a precision probe of gravity

these are **existing** constraints – expect 10x improvement with APOLLO

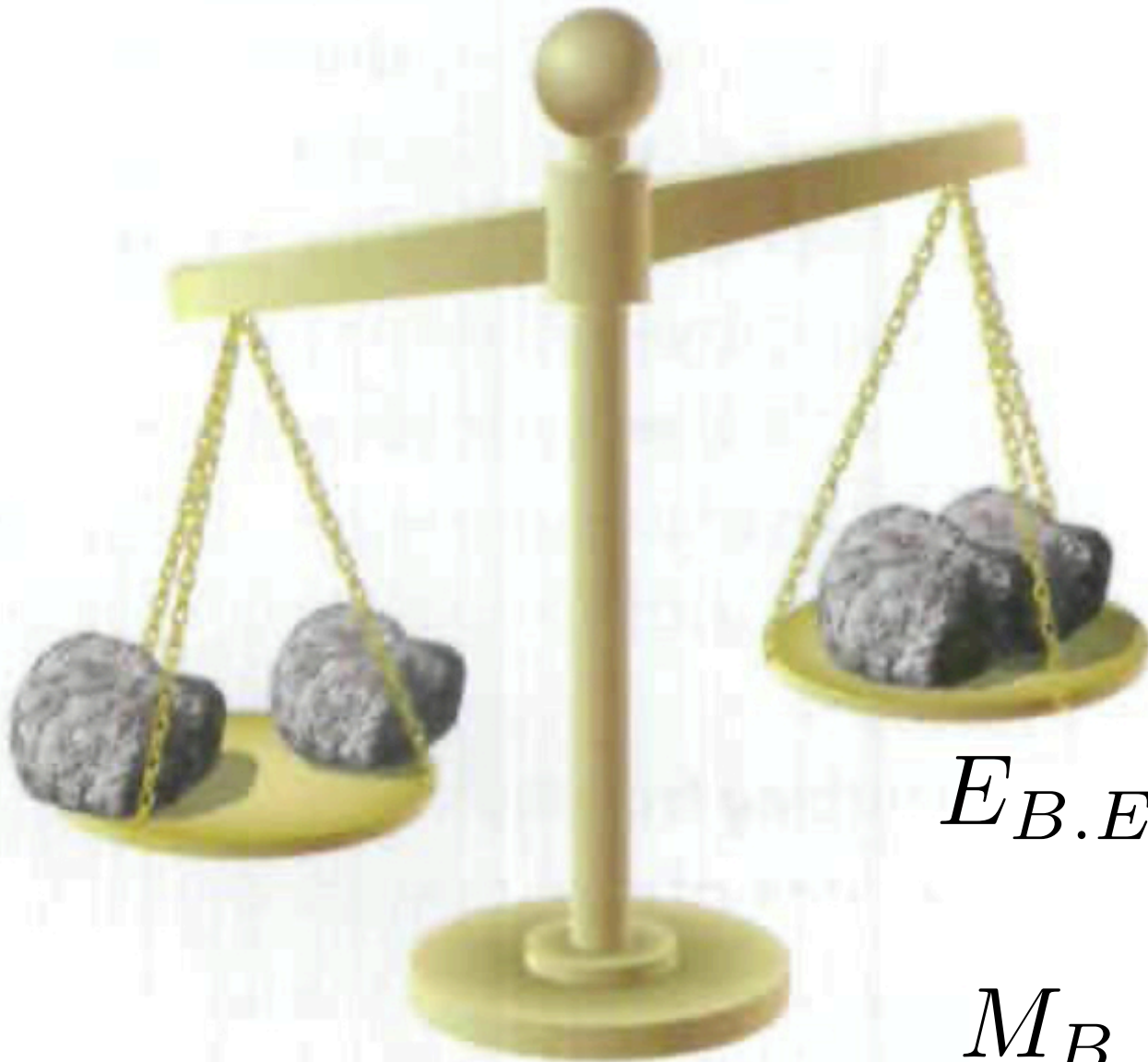
- Weak EP  $\Delta a/a$   $10^{-13}$  ← MICROSCOPE  $10^{-14}$   
Touboul et al., PRL 2017 (arXiv:1712.01176)
- Strong EP  $\eta$   $10^{-4}$  ← Pulsar triple system  
J0337+1715
- $1/r^2$  deviations  $10^{-10} F_G$   
Gusinskaia et al., J. Phys. Conf. (2017)  
but no limits published yet...
- $(dG/dt)/G$   $10^{-12} \text{ yr}^{-1}$
- Gravitomagnetism 0.1%
- Geodetic precession 0.5%

# The Equivalence Principles



Weak: Mass, composition  
Strong: Binding energy

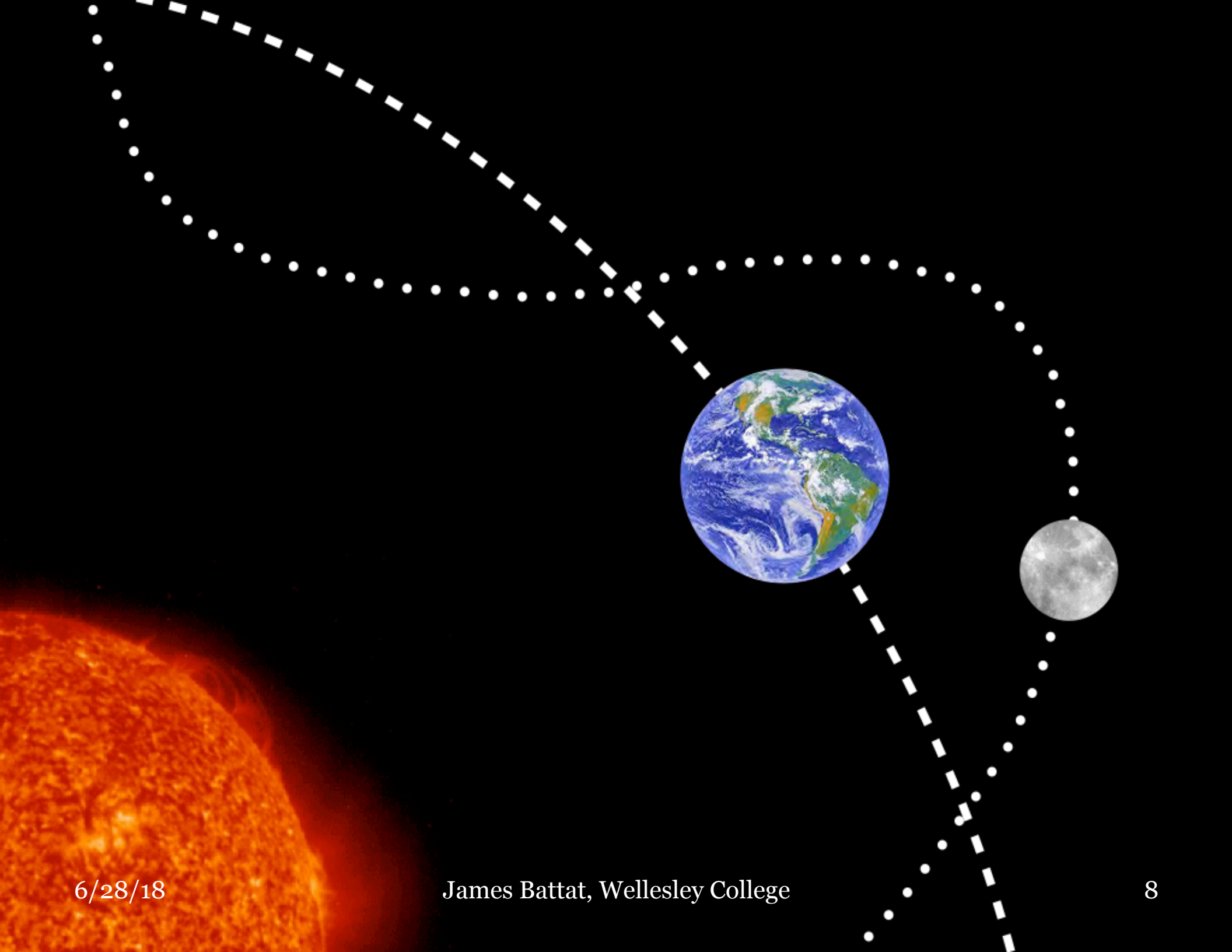
# Strong Equivalence Principle



$$E_{B.E.} = -\frac{GM_1M_2}{R}$$

$$M_{B.E.} = \frac{E_{B.E.}}{c^2}$$



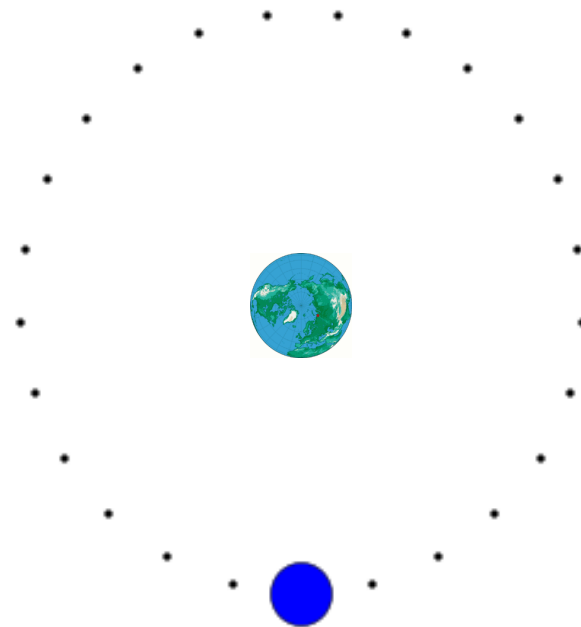


6/28/18

James Battat, Wellesley College

# EP Violation in the Lunar Orbit

“Nominal” Lunar orbit

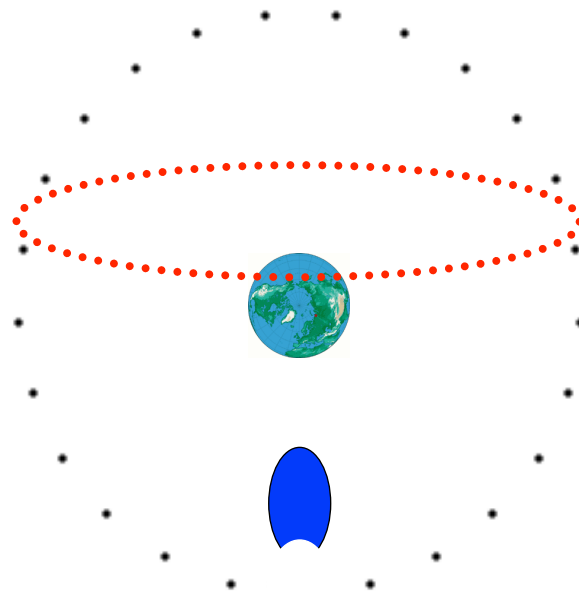


to the Sun

# EP Violation in the Lunar Orbit

“Nominal” Lunar orbit

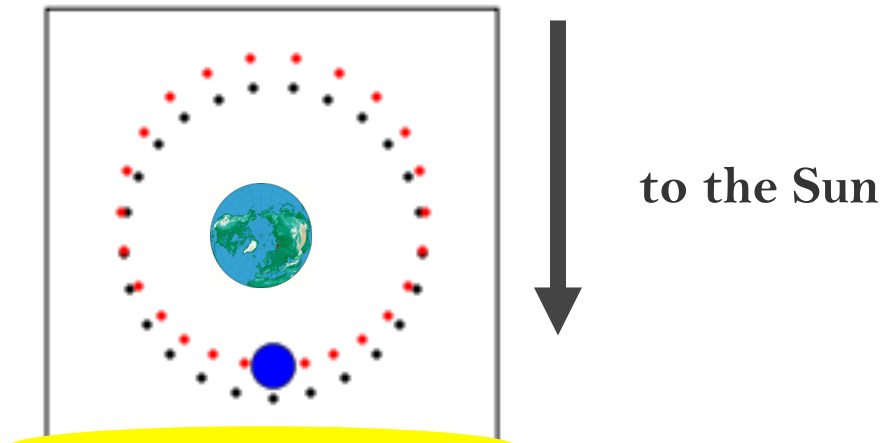
Orbit under EP violation  
(polarized)



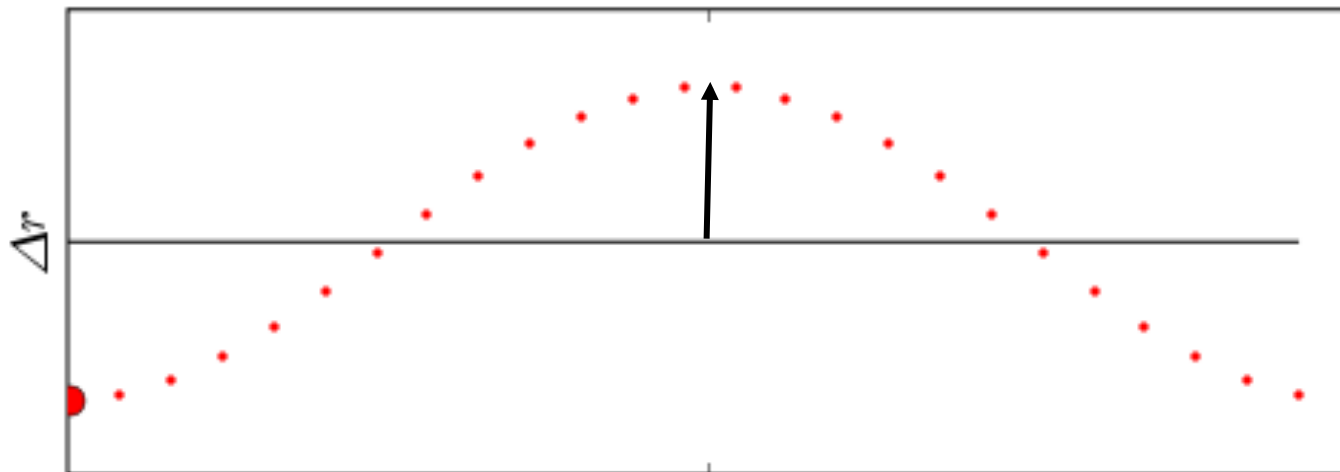
to the Sun



# SEP Violation in the Lunar Orbit



$$\Delta r = 13.1\eta \cos D \text{ meters}$$



$$\eta \leq 5 \times 10^{-4}$$

by LLR

New Moon

Full Moon

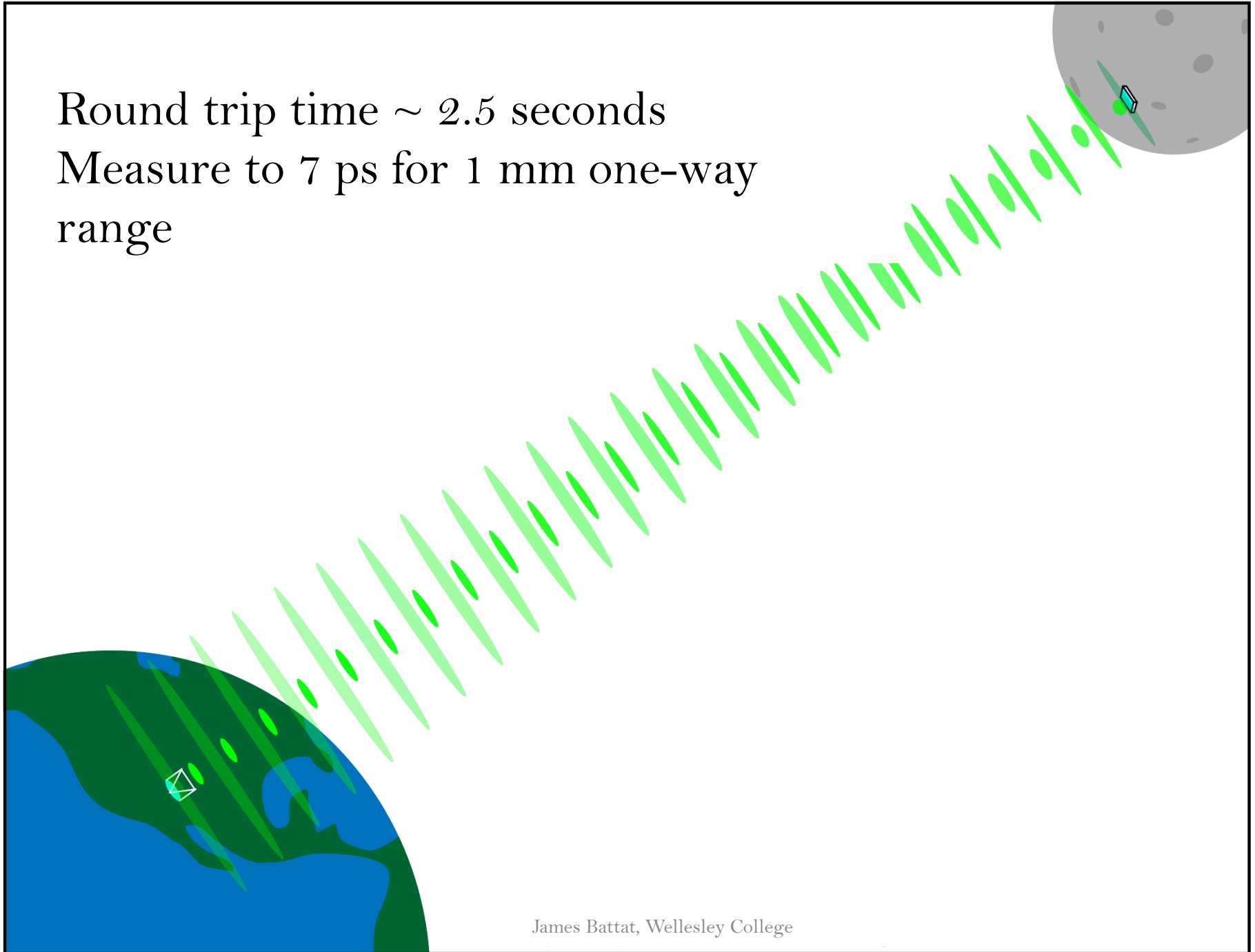
New Moon

← 29.53 days →

# Lunar Laser Ranging 101

Round trip time  $\sim 2.5$  seconds

Measure to 7 ps for 1 mm one-way  
range



Big Bang Theory: making it look easy!





# Lunar Laser Ranging 102

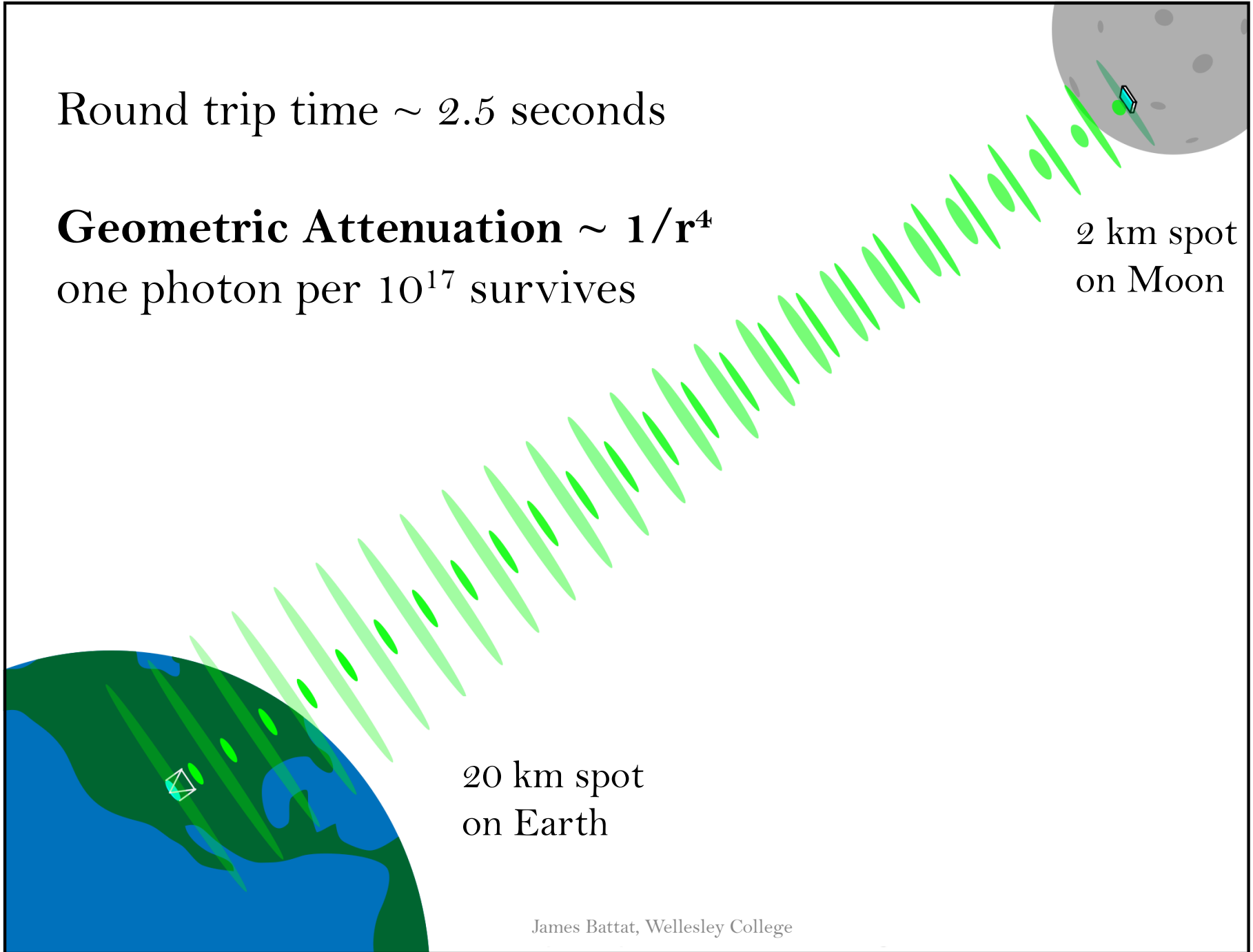
Round trip time  $\sim 2.5$  seconds

**Geometric Attenuation**  $\sim 1/r^4$

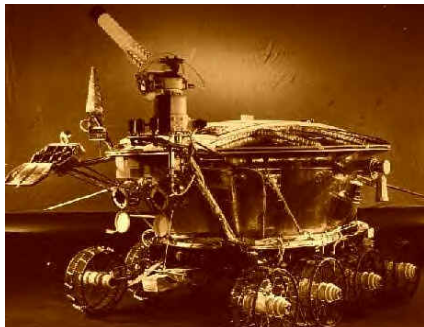
one photon per  $10^{17}$  survives

2 km spot  
on Moon

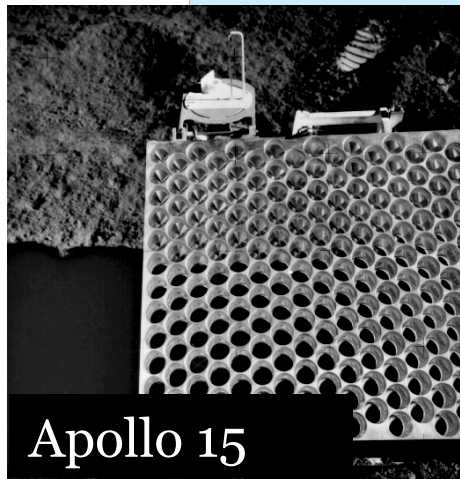
20 km spot  
on Earth



# LLR Targets

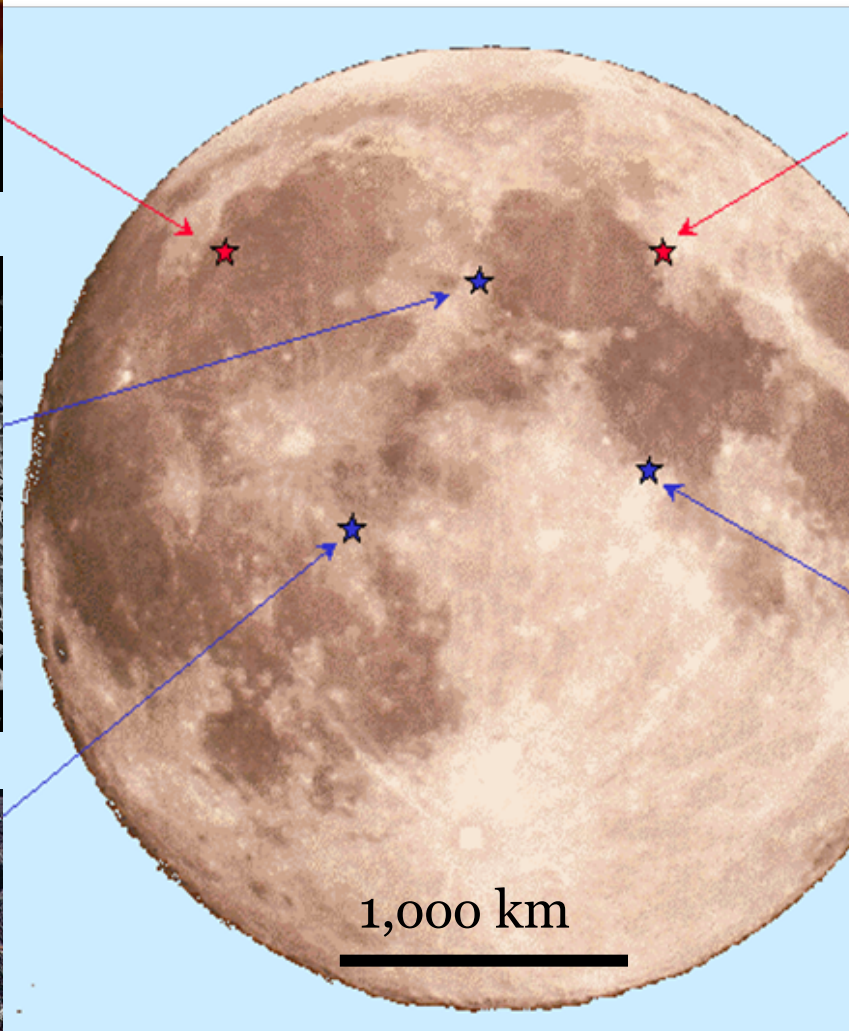
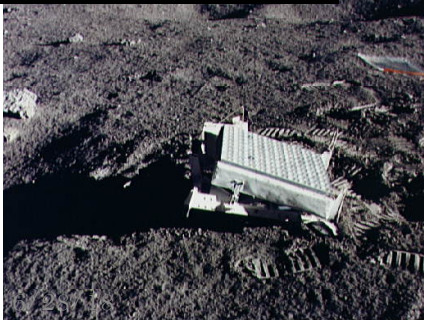


Lunokhod 1



Apollo 15

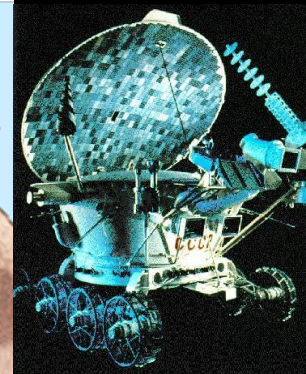
Apollo 14



1,000 km

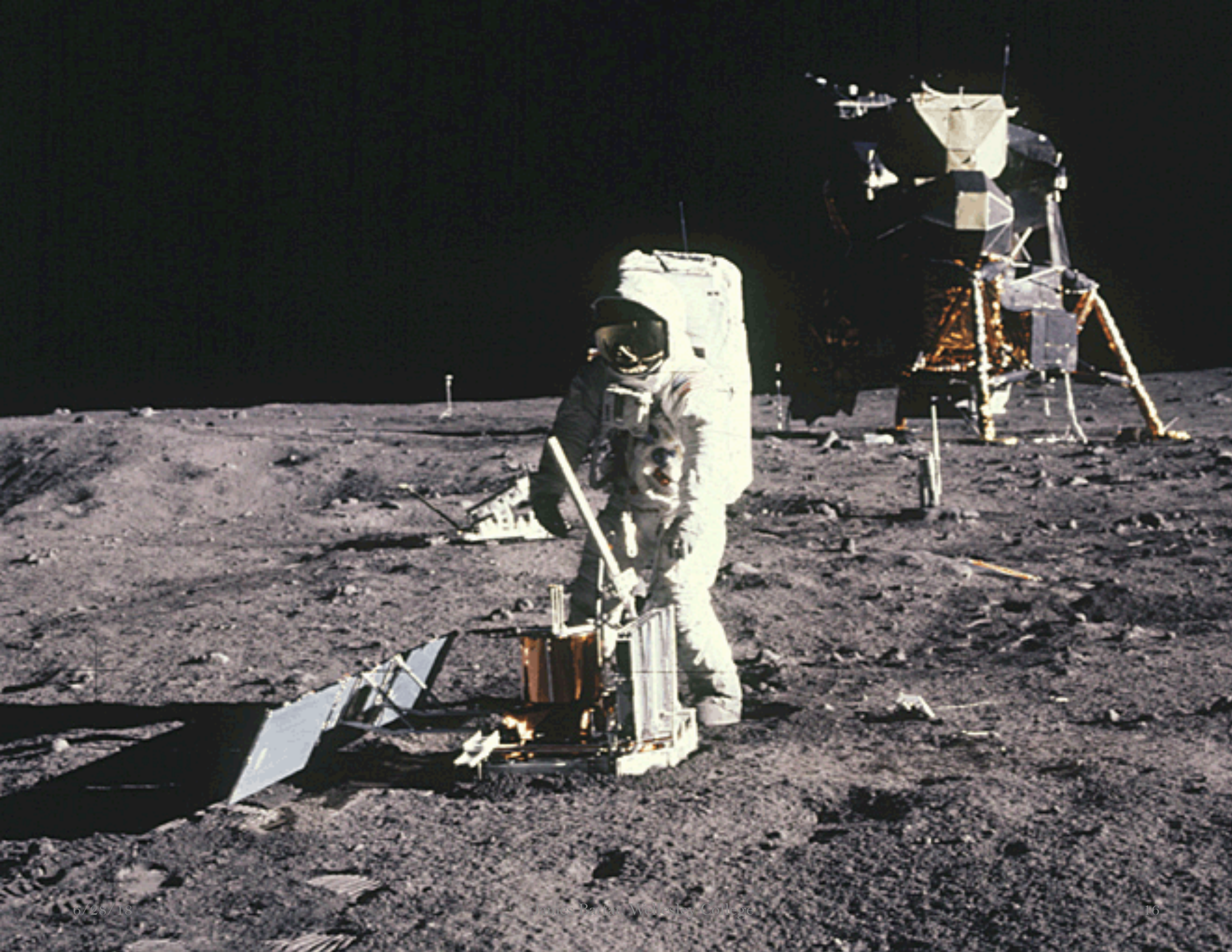


Lunokhod 2



Apollo 11

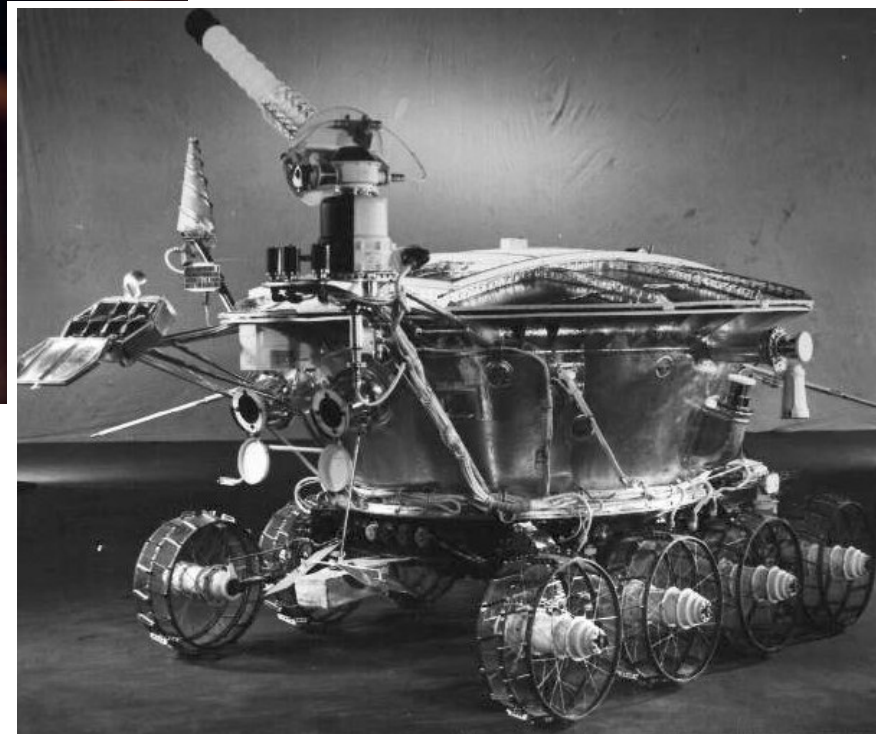
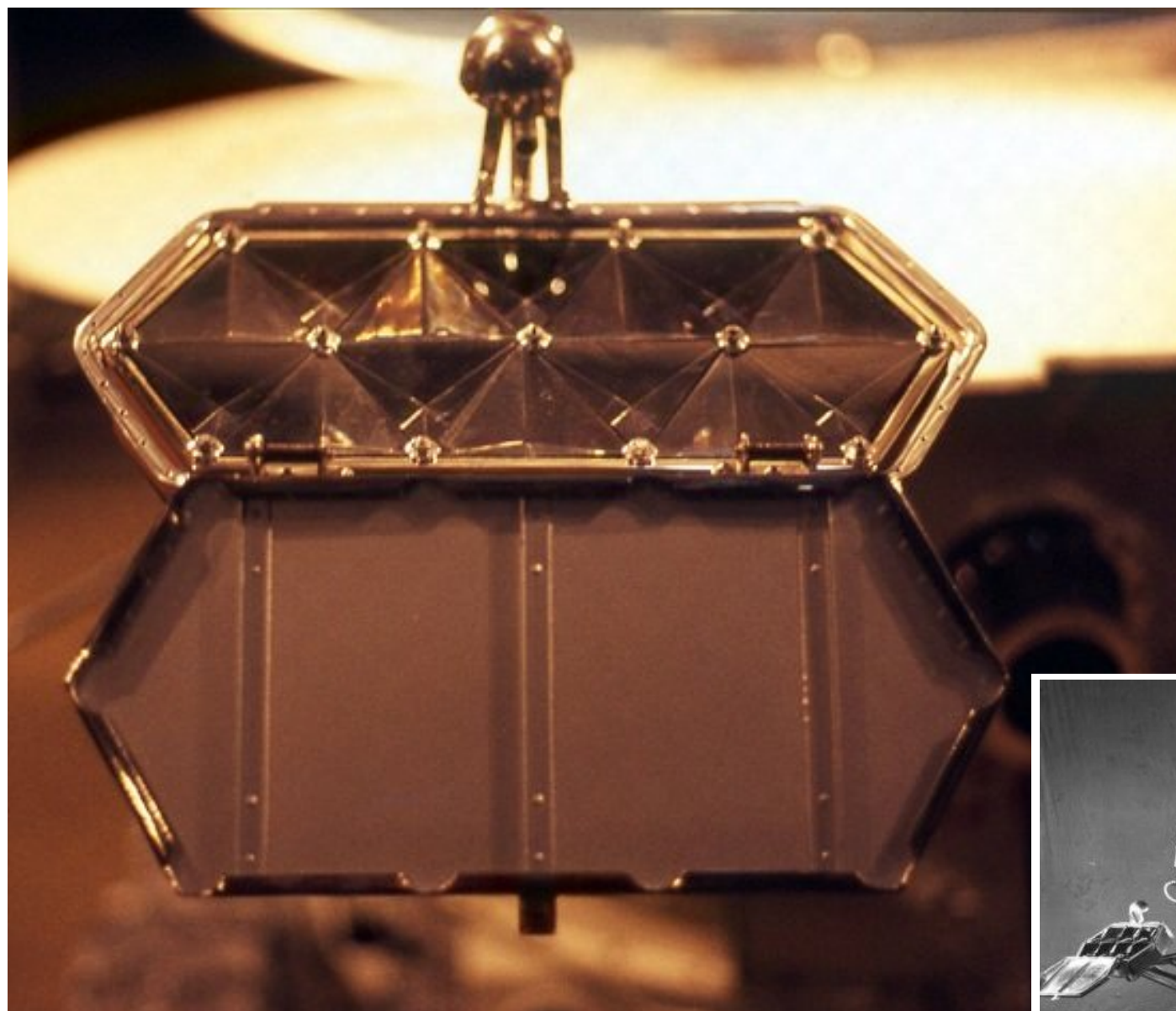


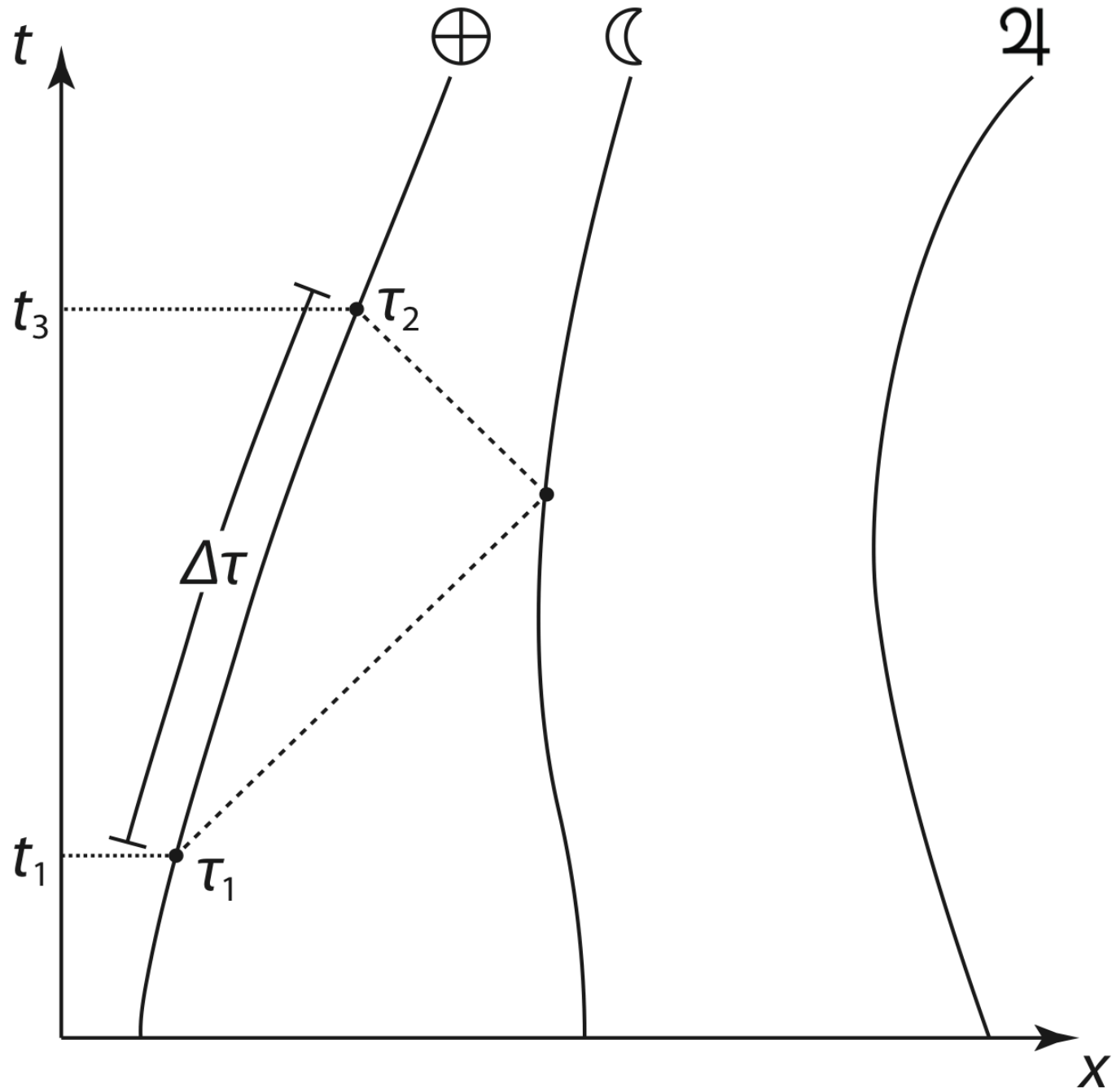








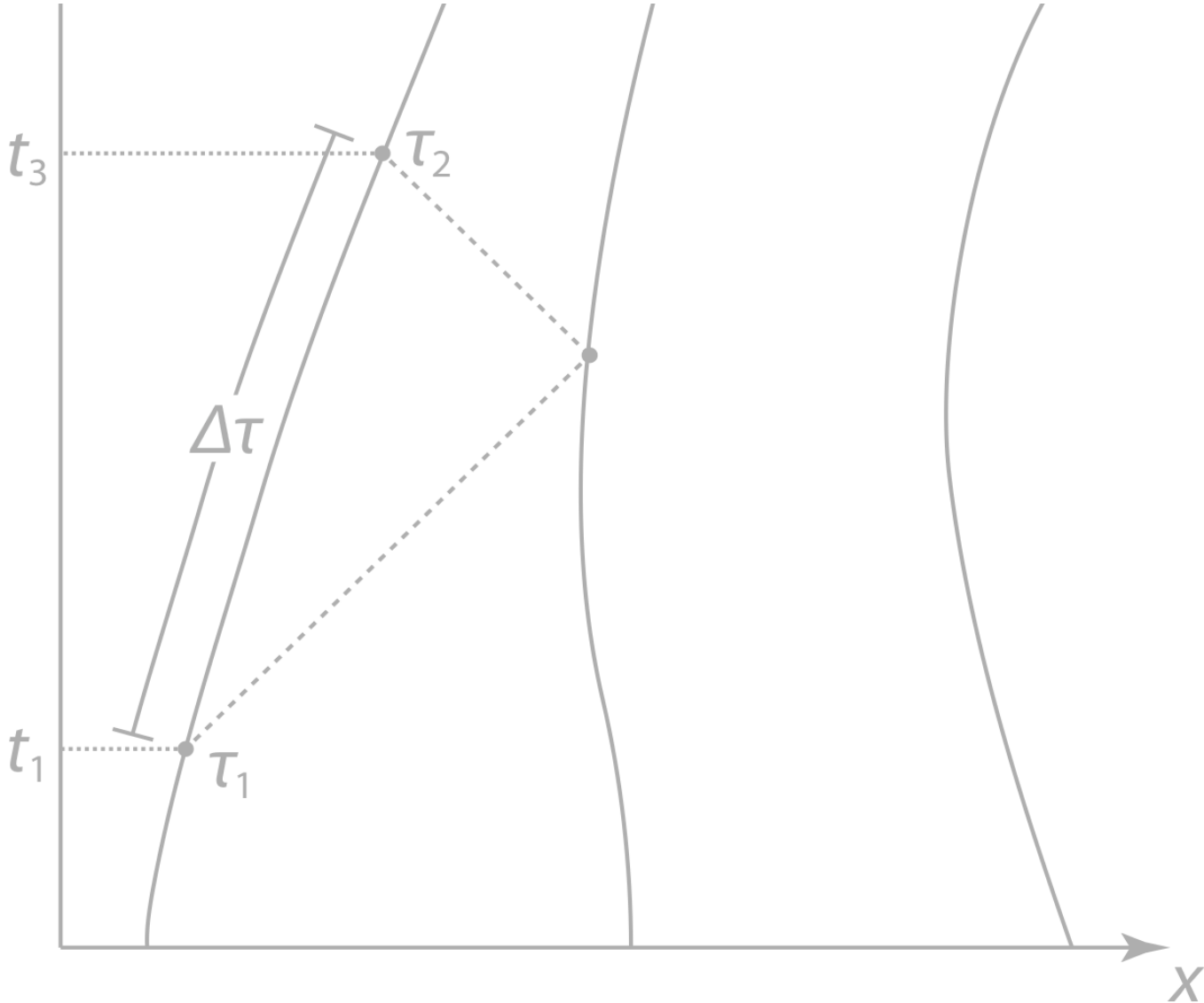




$t$  ↑



5120150116134120000000025037908297936370610118 384552B 72948 2713 5320A 477A

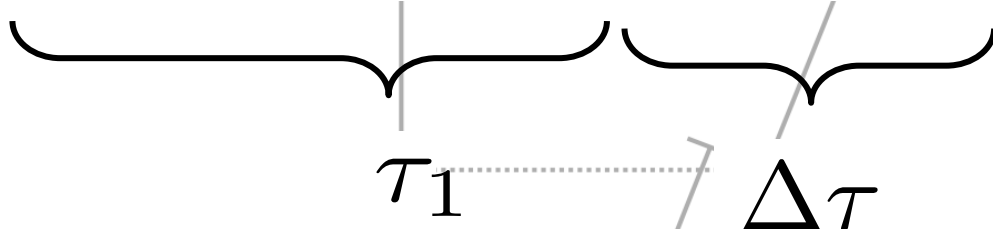


$t$  ↑



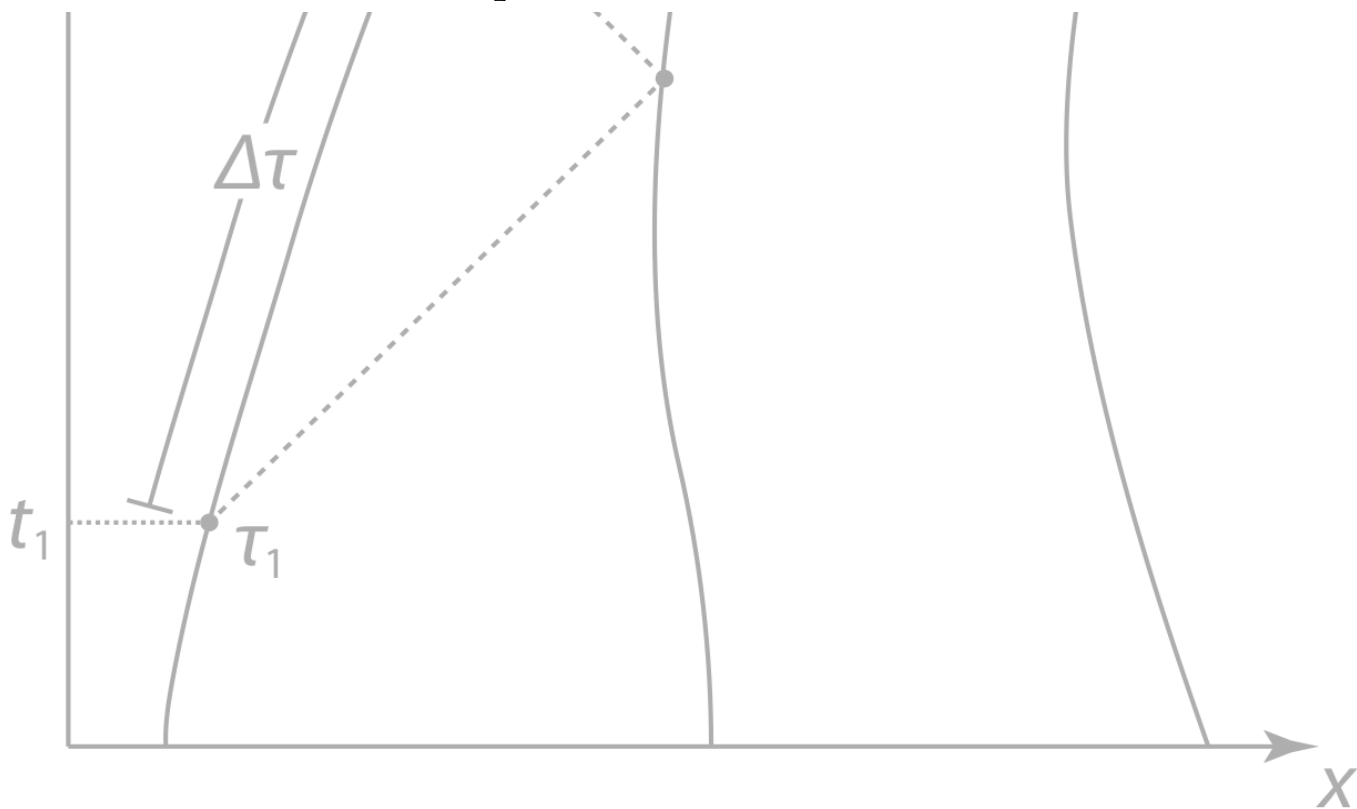
21

5120150116134120000000025037908297936370610118 384552B 72948 2713 5320A 477A



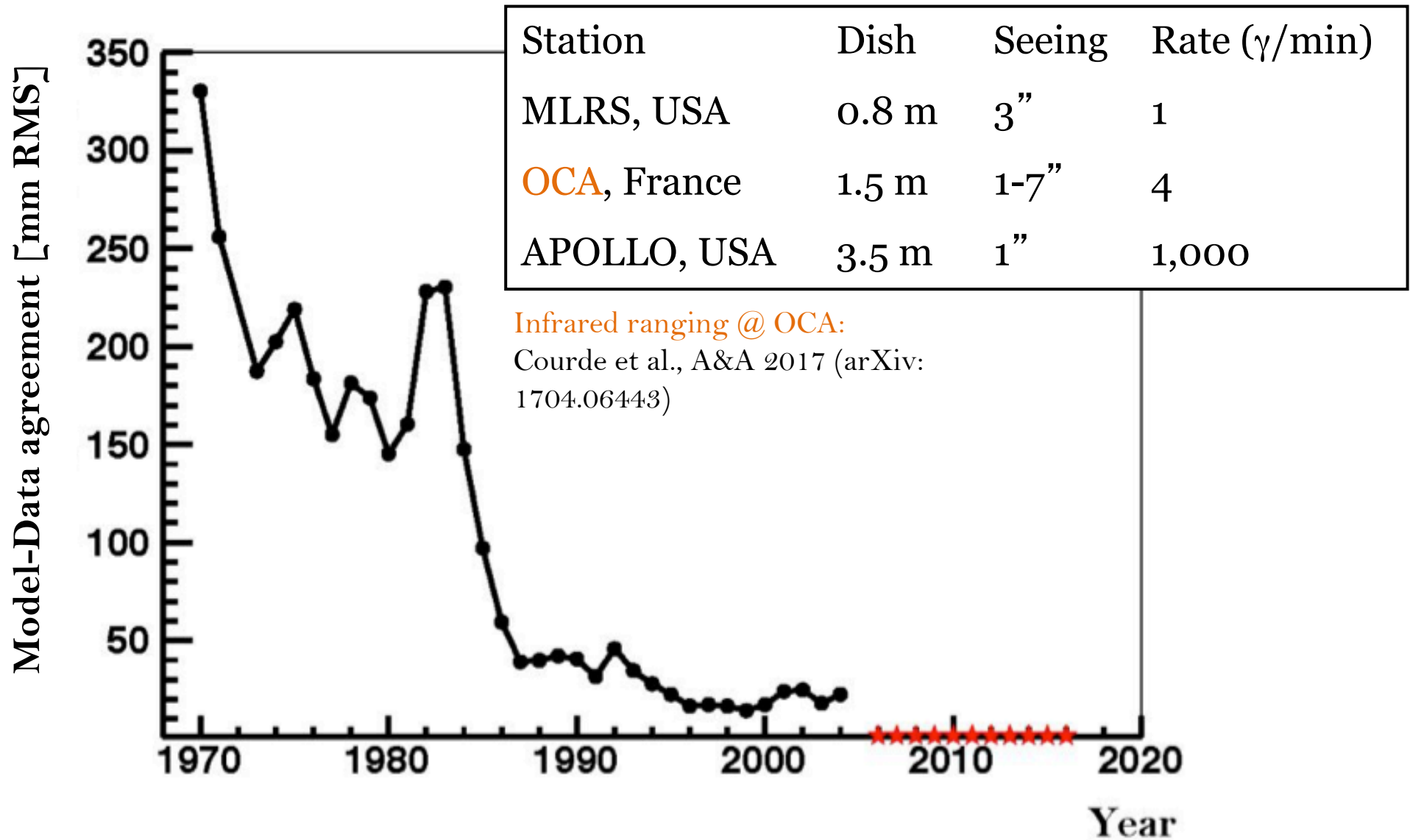
2015 Jan 16 13:41:20

Round trip time = 2.5037908297936 seconds

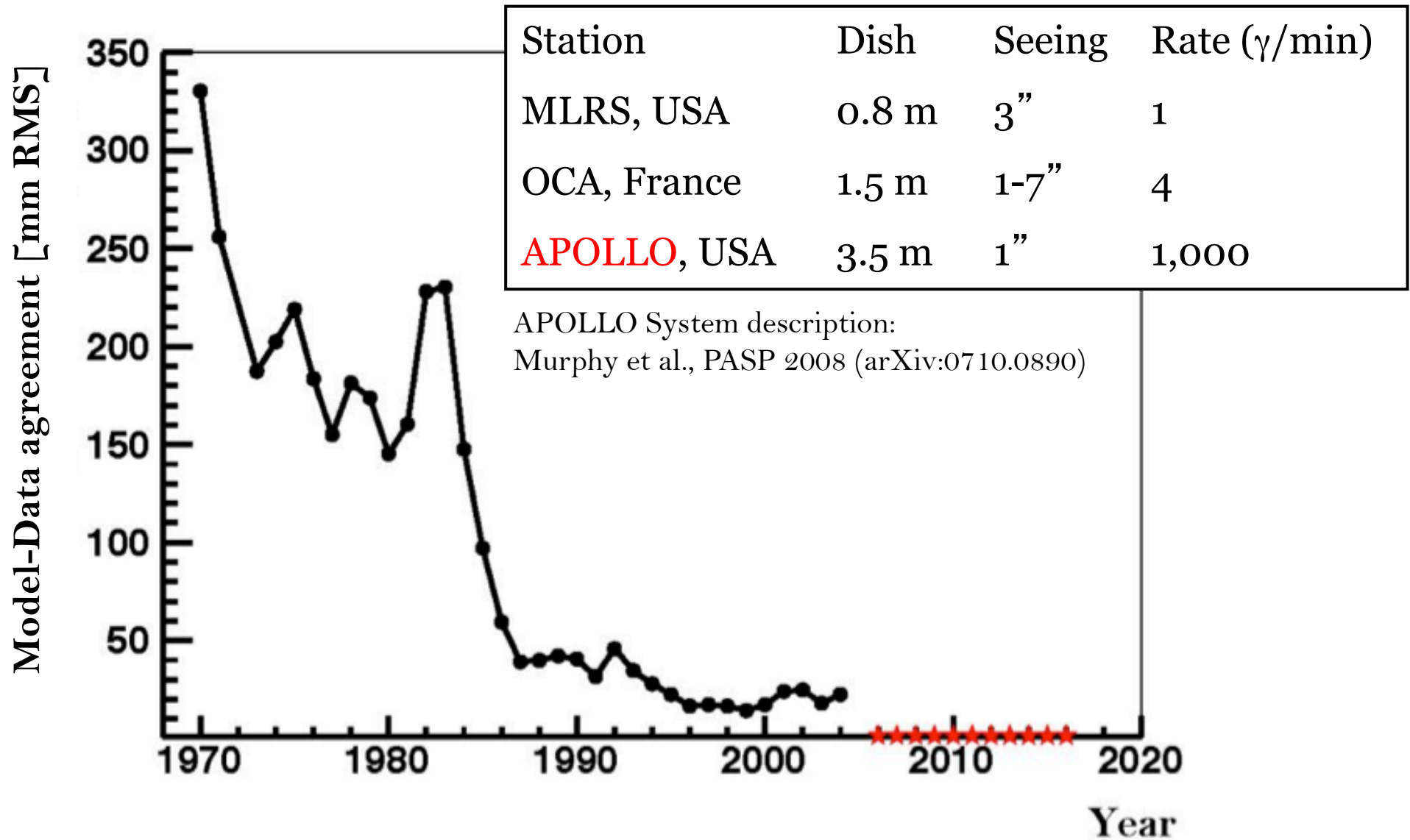




# Historical Laser Ranging Performance

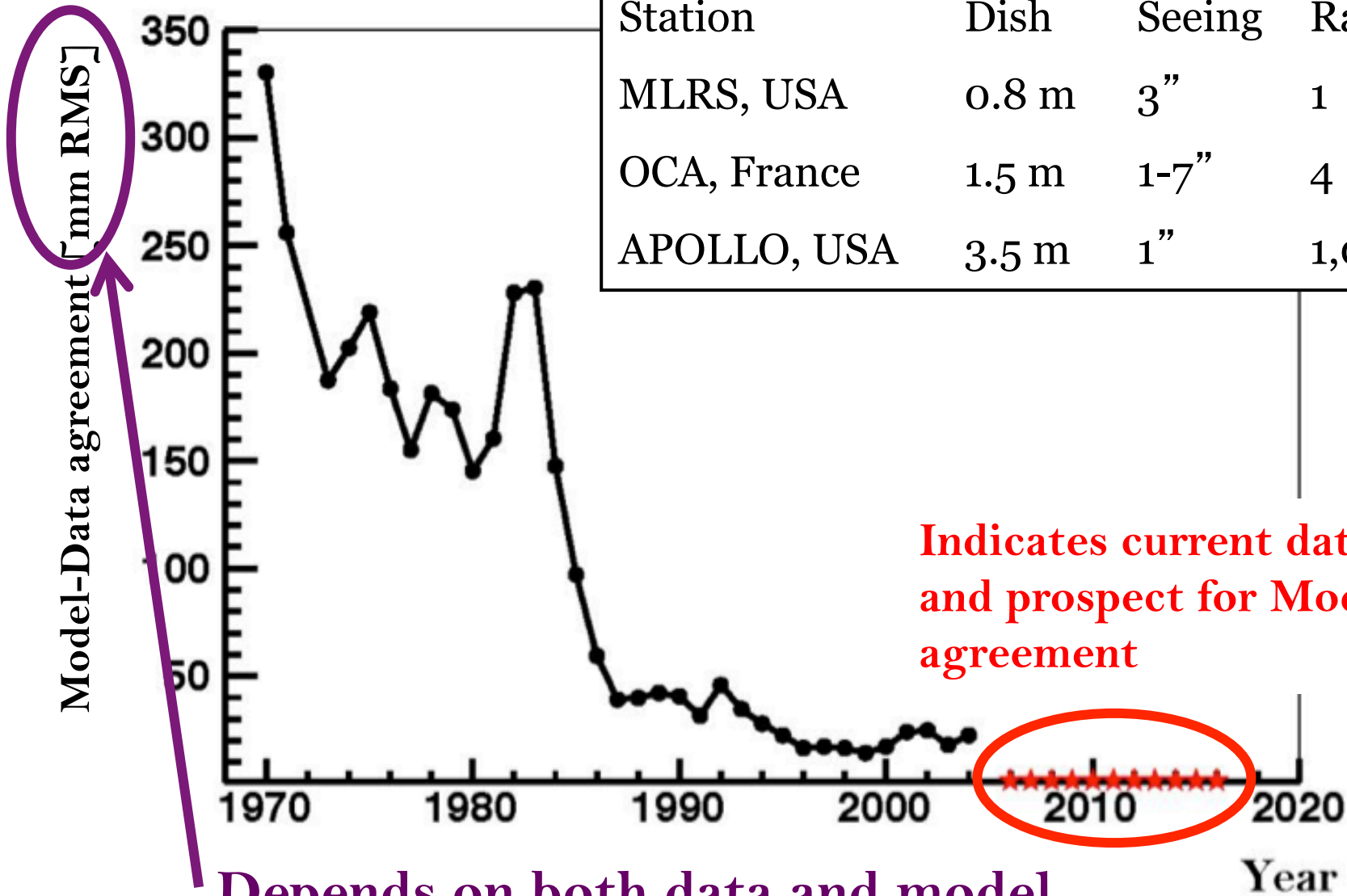


# Historical Laser Ranging Performance

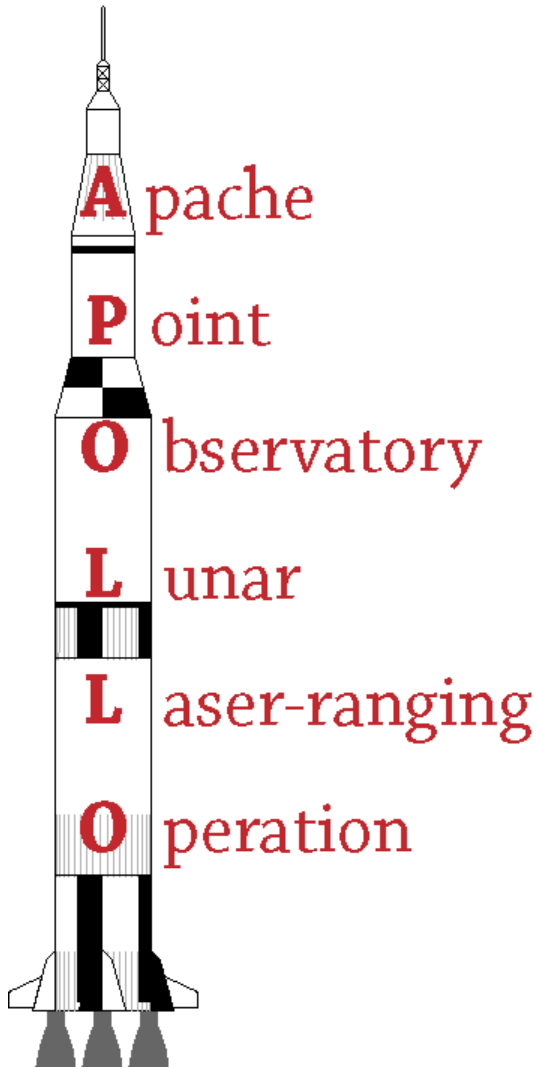


# Historical Laser Ranging Performance

Station	Dish	Seeing	Rate ( $\gamma$ /min)
MLRS, USA	0.8 m	3"	1
OCA, France	1.5 m	1-7"	4
APOLLO, USA	3.5 m	1"	1,000



# APOLLO Collaboration



## **U.C. San Diego**

Tom Murphy (PI)

Bob Reasenberg

Nick Colmenares

Sanchit Sabhlok

## **Wellesley College**

James Battat

## **U. Washington**

Eric Adelberger

Erik Swanson

## **Harvard University**

Christopher Stubbs

John Chandler

Irwin Shapiro

## **Humboldt State U.**

C. D. Hoyle

## **Northwest Analysis**

Ken Nordtvedt

## **Apache Point Observatory**

Russet McMillan



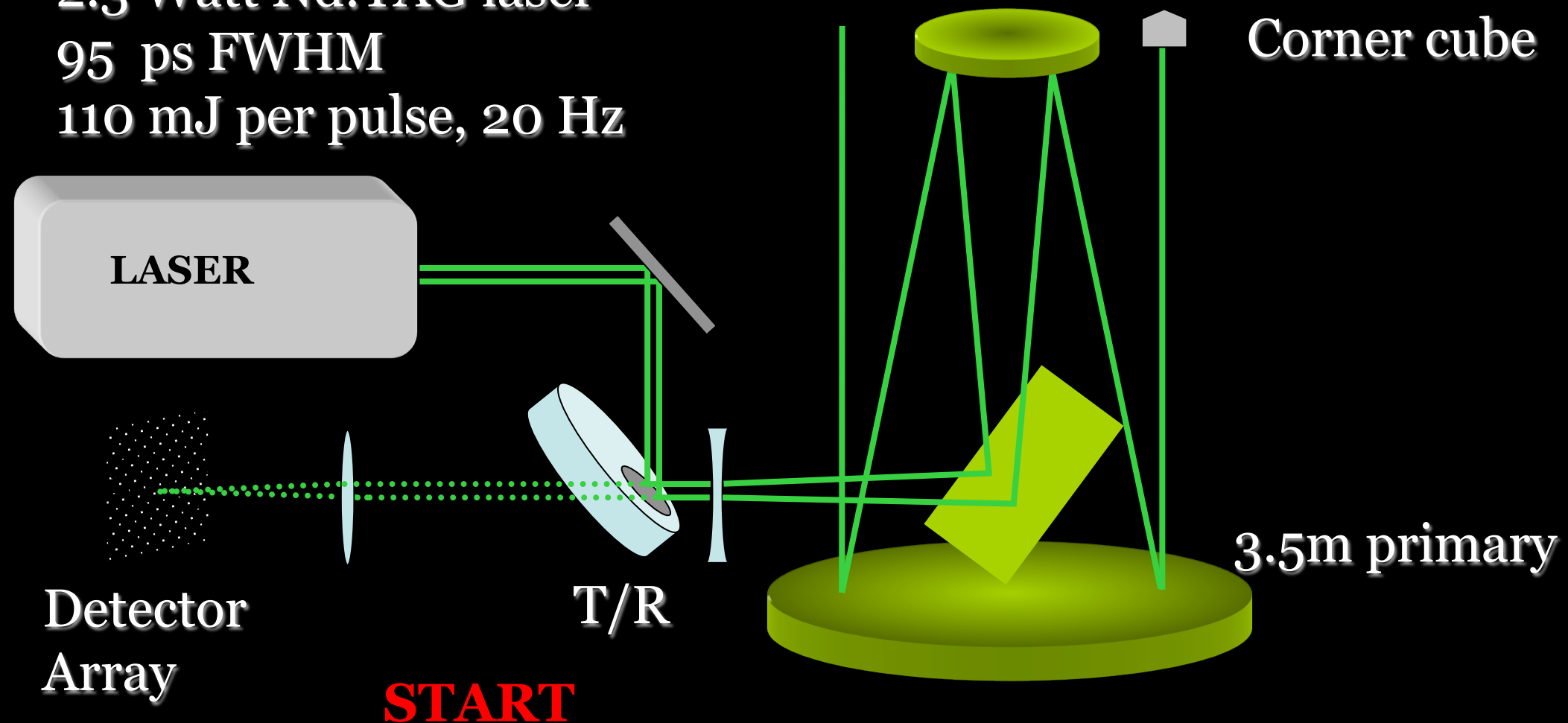
# APOLLO: The Earth-End



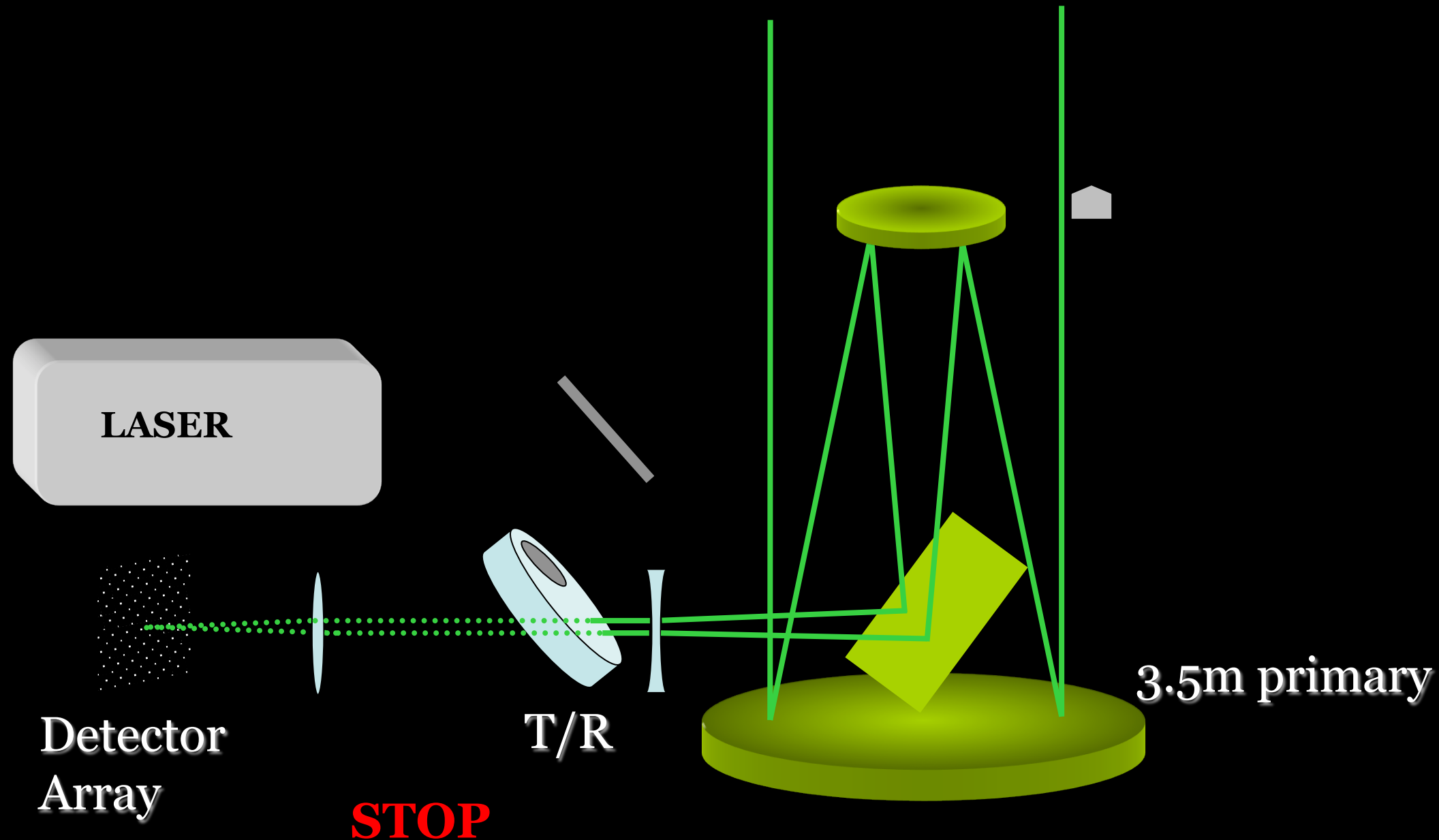


# Laser Ranging Apparatus: Transmit

2.3 Watt Nd:YAG laser  
95 ps FWHM  
110 mJ per pulse, 20 Hz

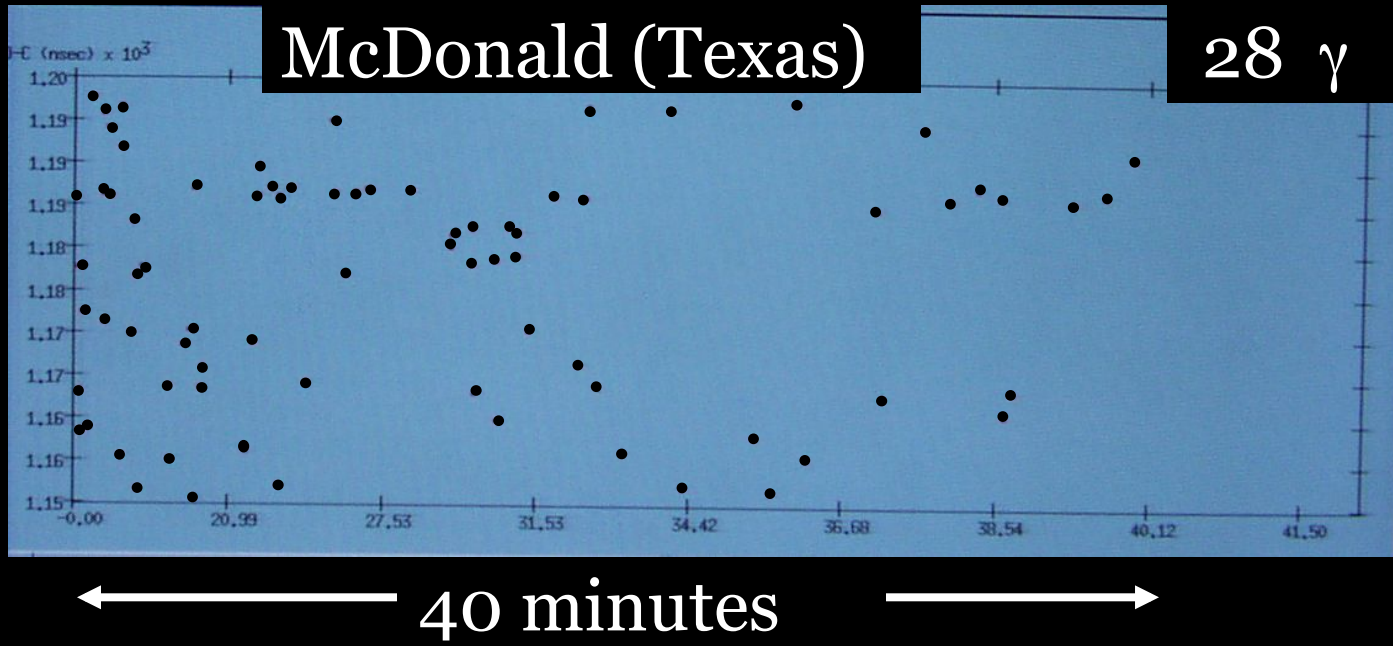


# Laser Ranging Apparatus: Receive



# Then

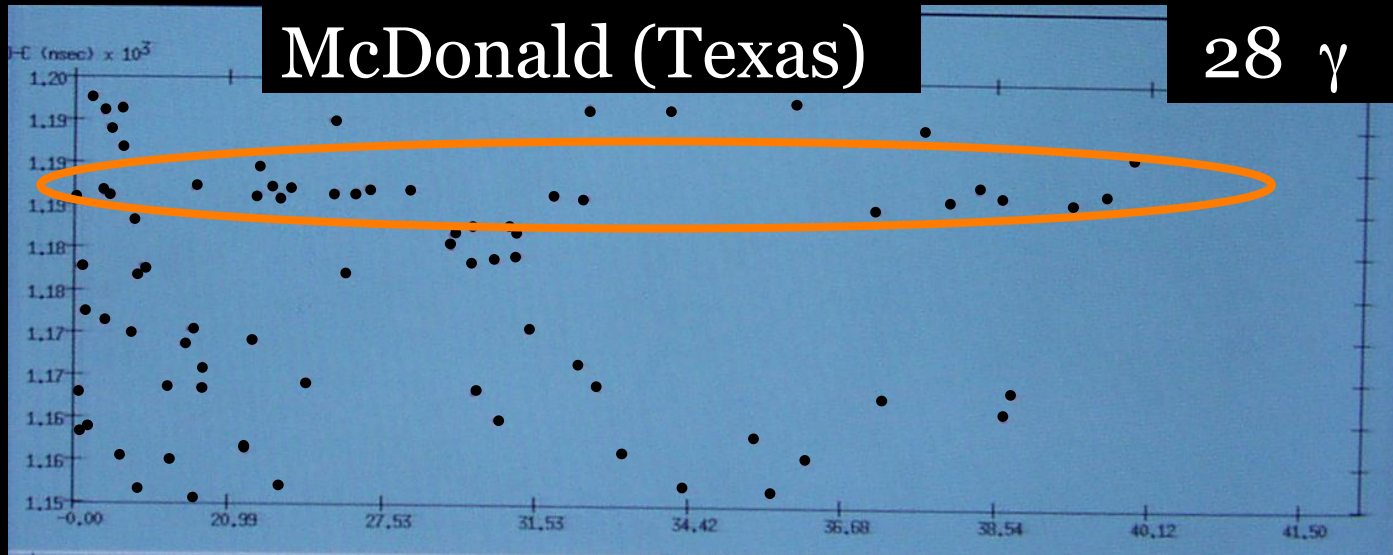
Observed Minus Theory





# Then

Observed Minus Theory

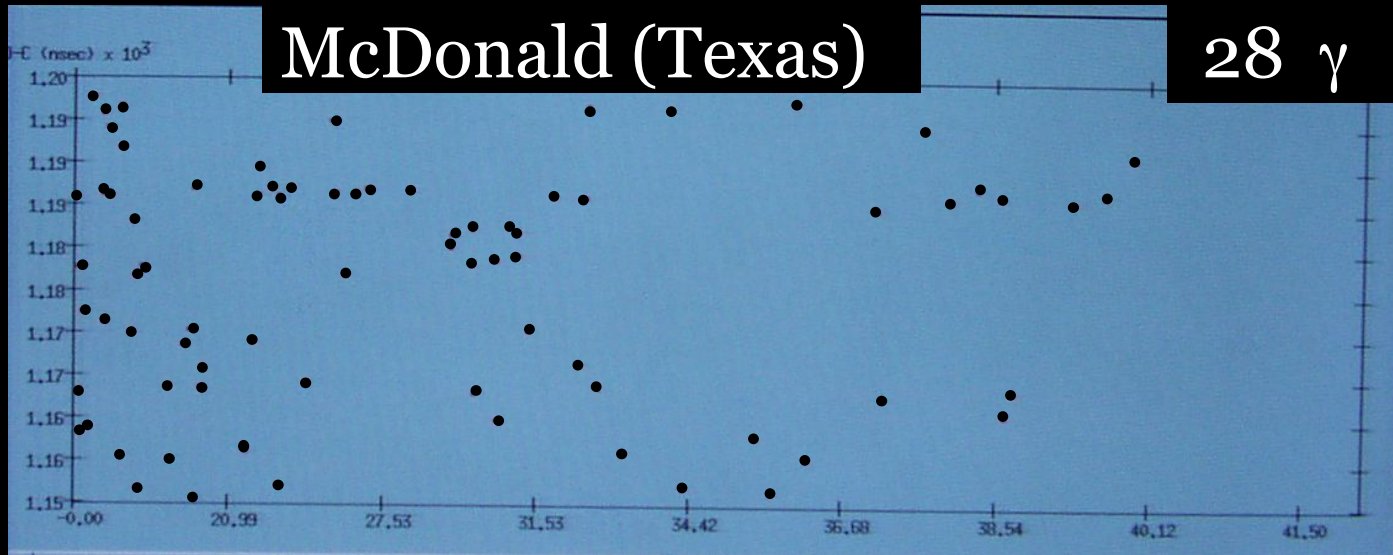


peut-être?

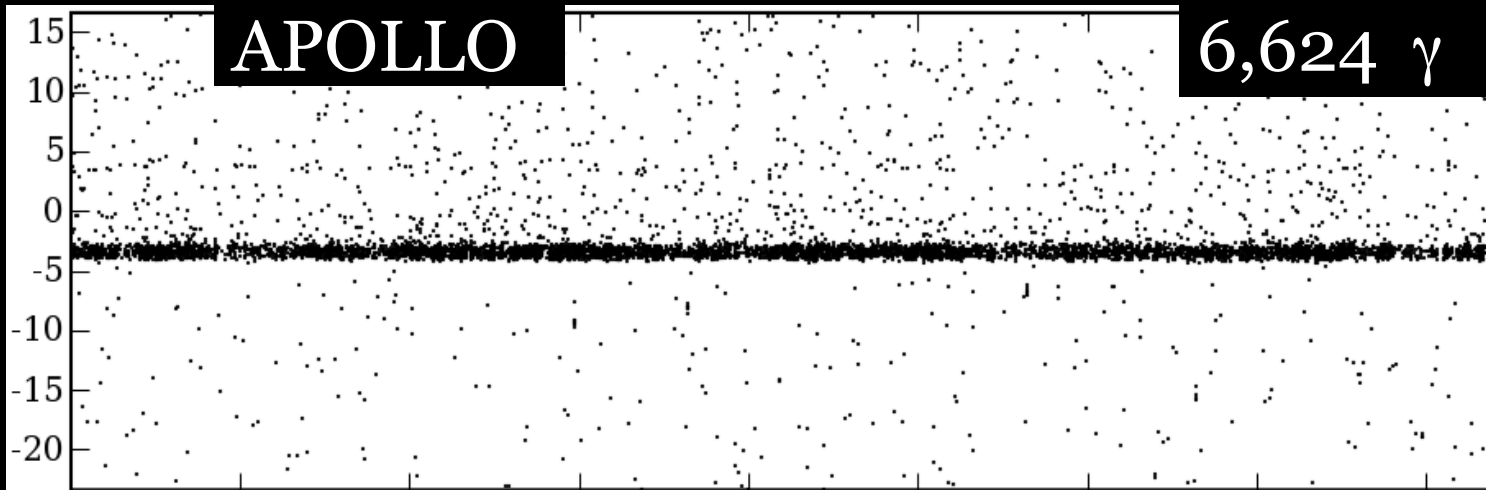
← 40 minutes →

# Now

Observed Minus Theory



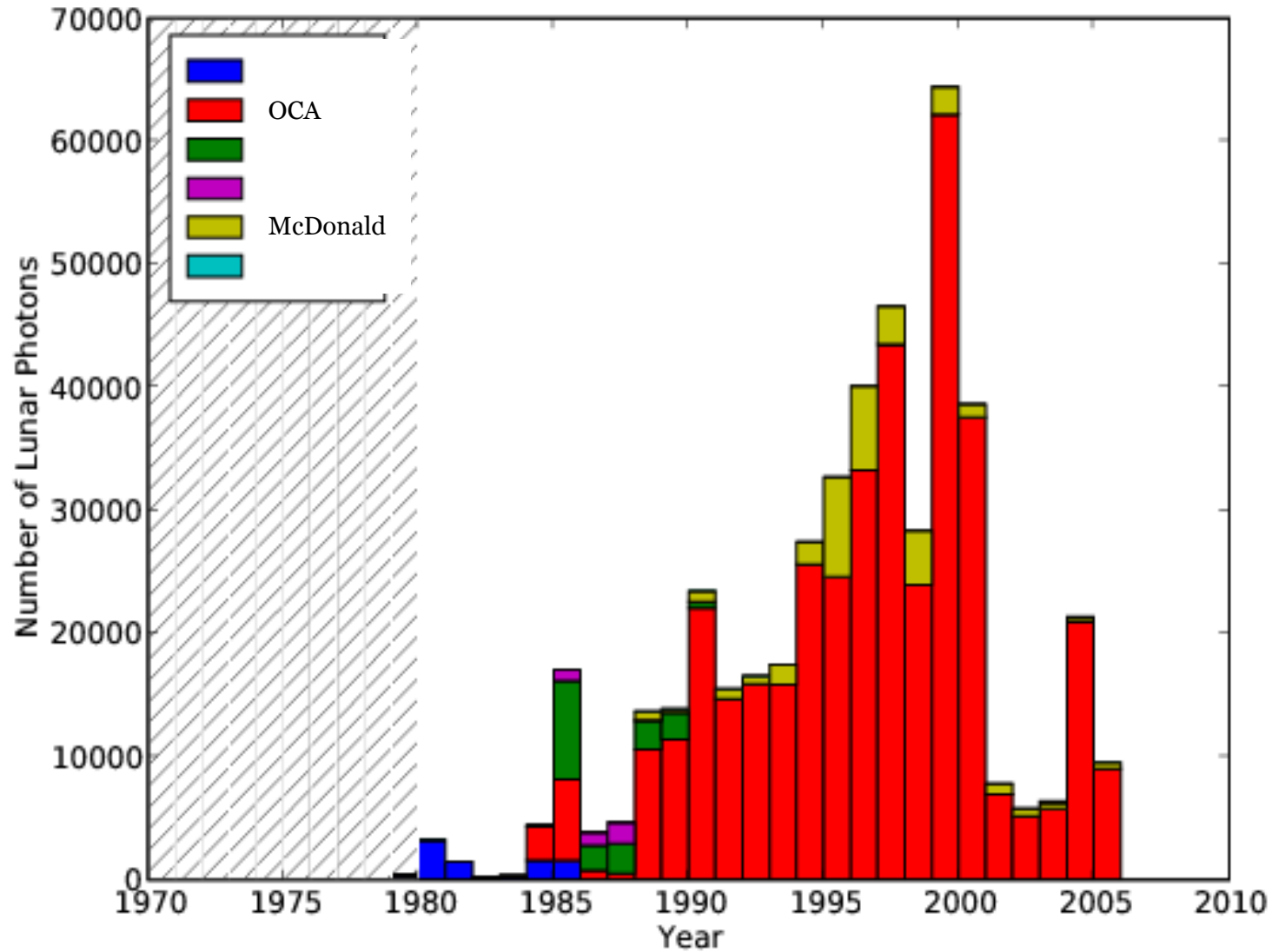
40 minutes



40 ns

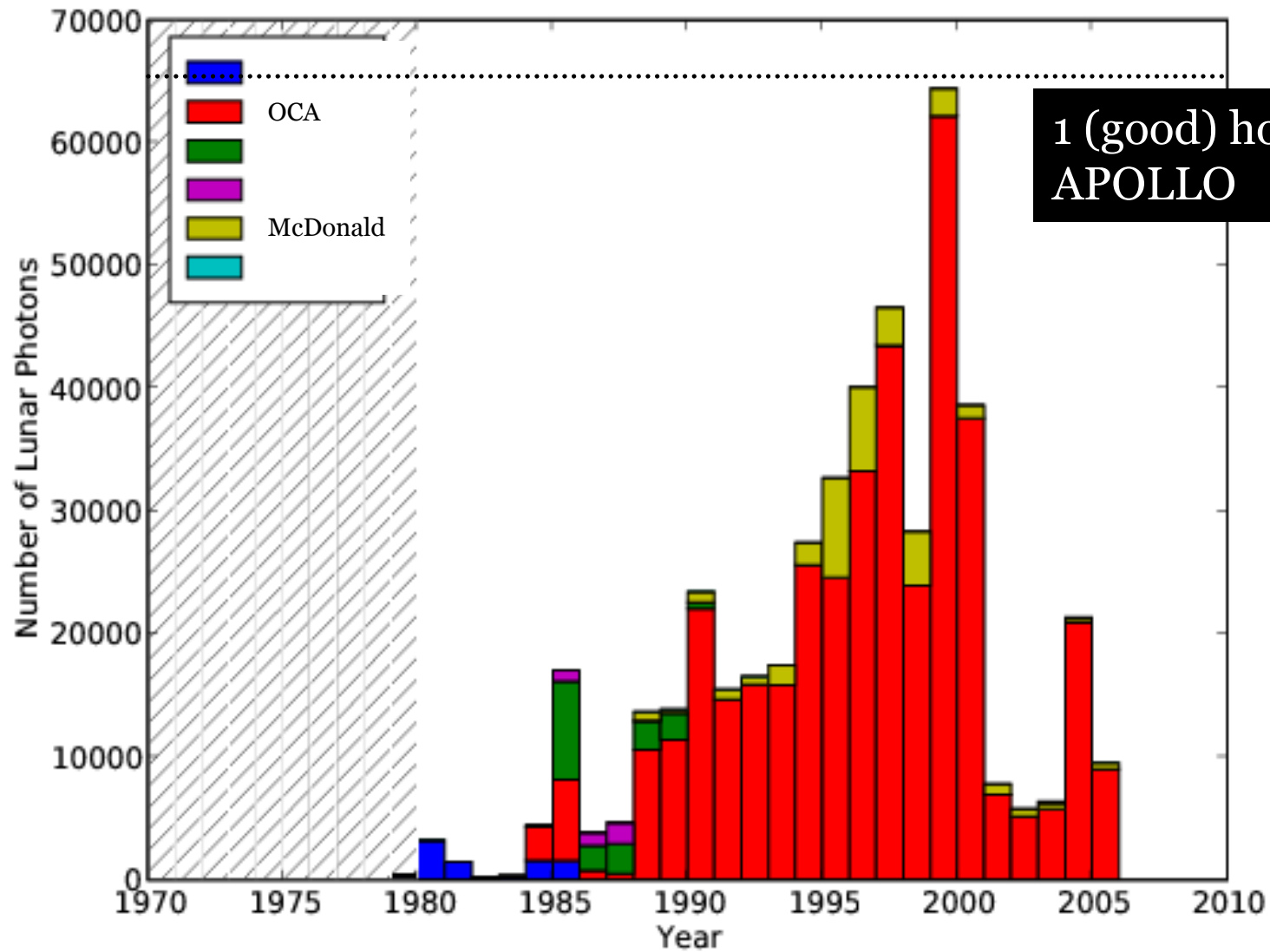
4 minutes

# Yearly Photon Yield





# Yearly Photon Yield

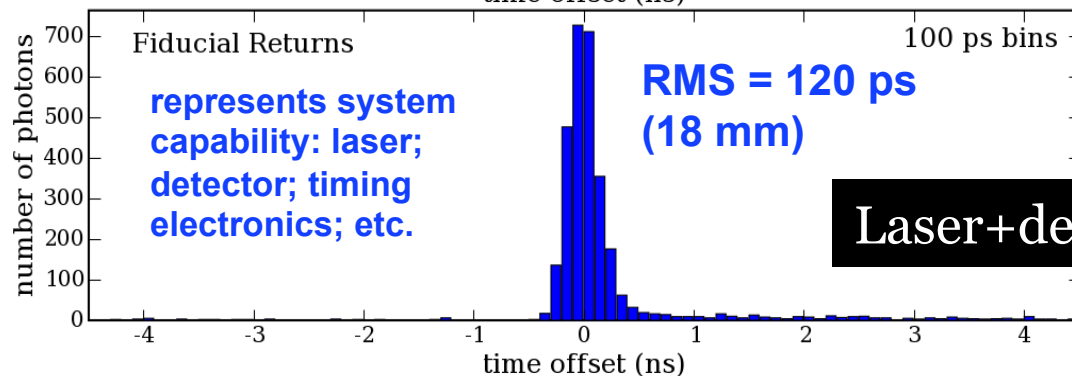
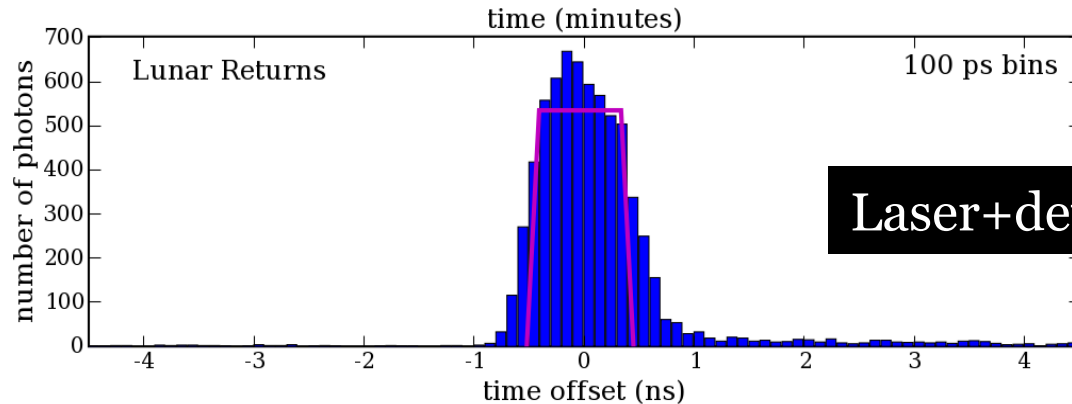
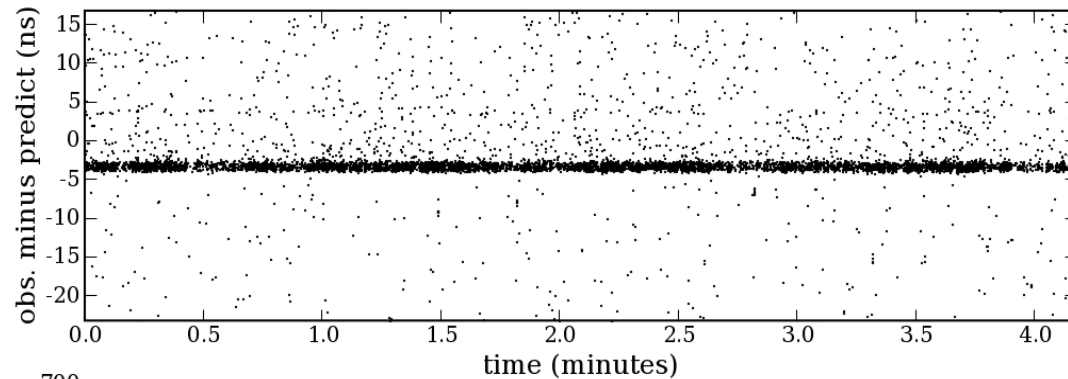


# Sub-mm precision ranging demonstrated

Apollo 15

2007.11.19

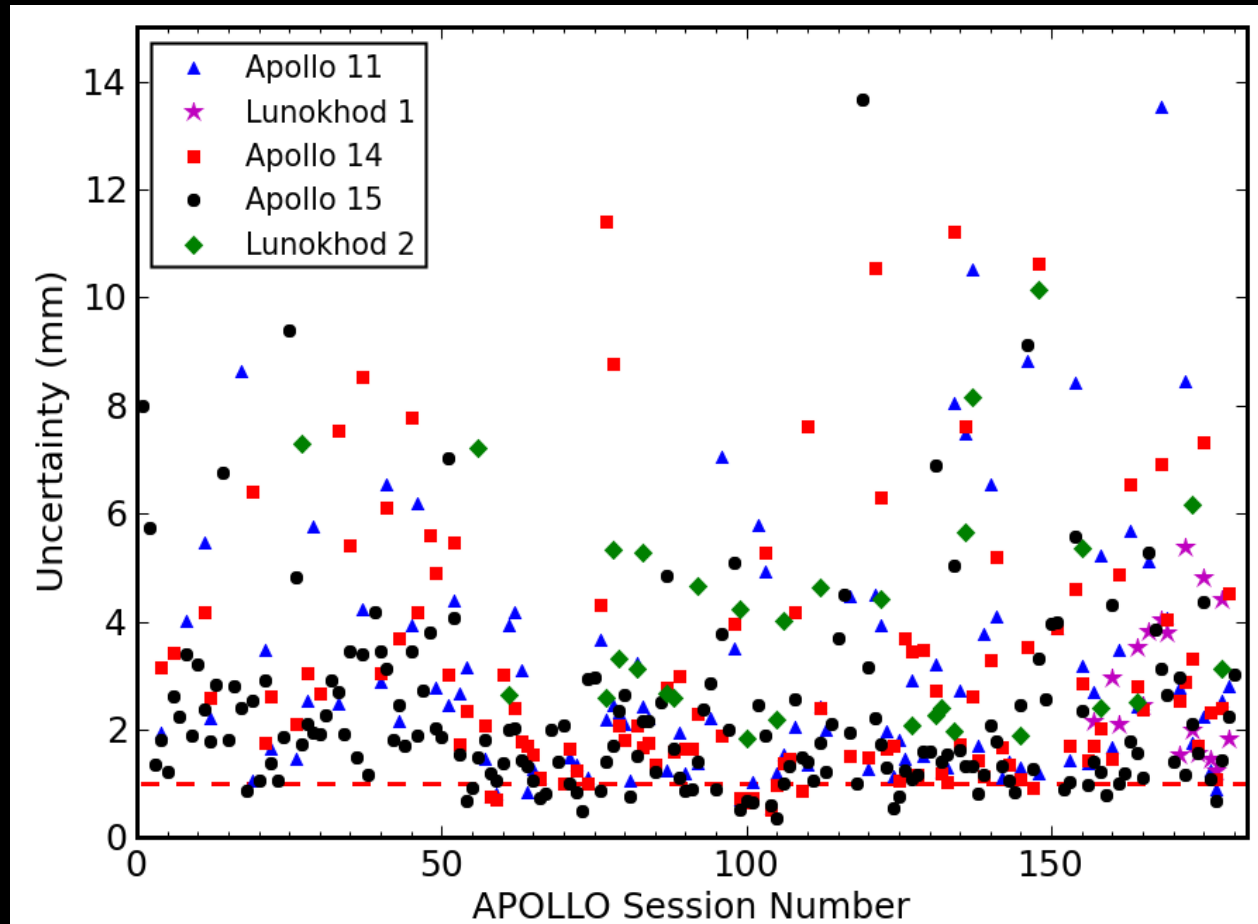
- 6624 photons in 5000 shots
- 369,840,578,287.4 ± 0.8 mm
- 4 detections with 10 photons



Limitation: lunar libration & size of reflector array

We cannot resolve individual corner cubes within an array

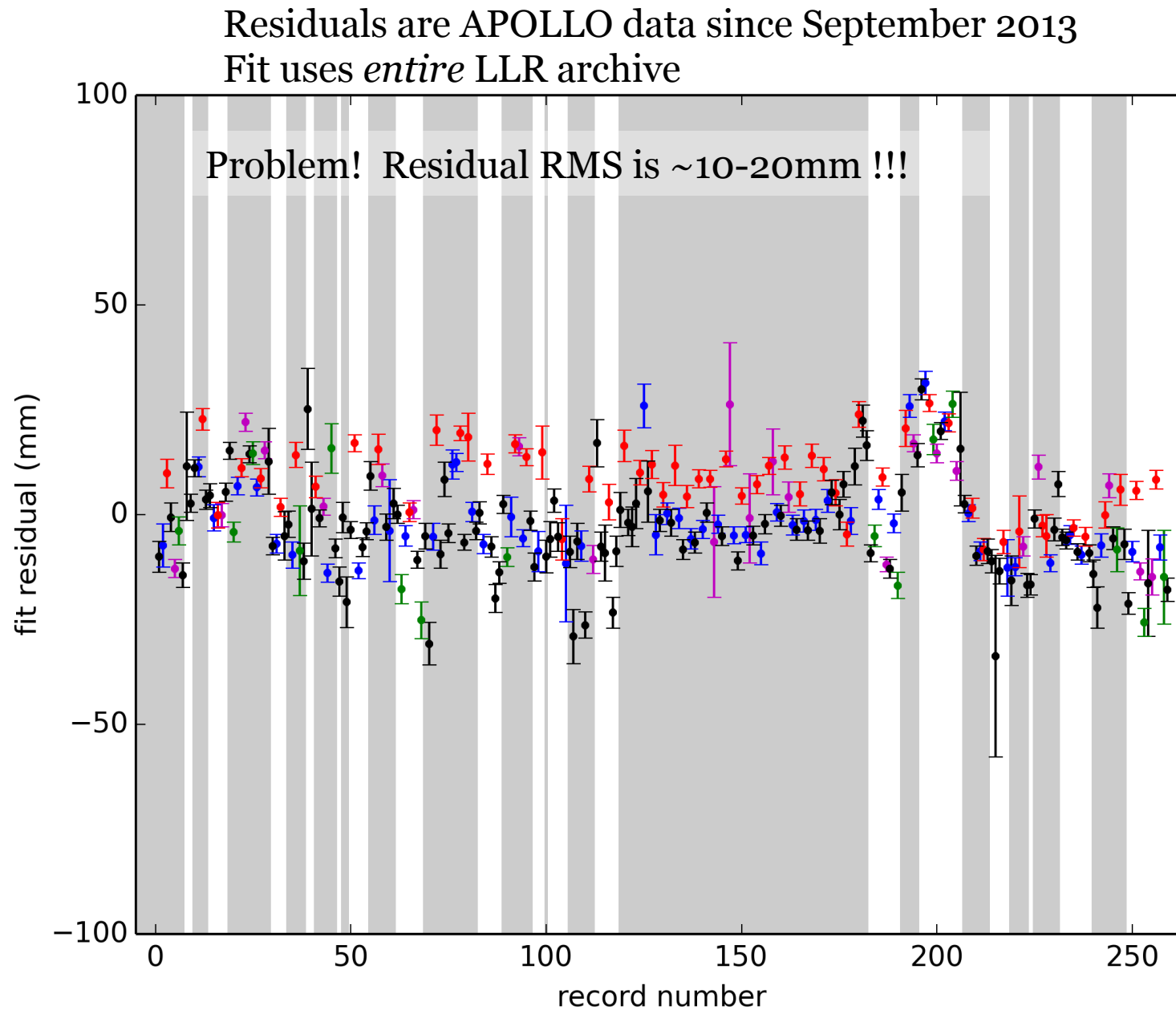
# APOLLO Data Precision



- Uncertainties are **per night, per reflector**; pre-APOLLO sub-centimeter rare
- Medians are **2.4**, **2.7**, **2.4**, 1.8, **3.3** mm for **A11**, **L1**, **A14**, A15, **L2**, respectively
- Combined nightly median range error is 1.4 mm

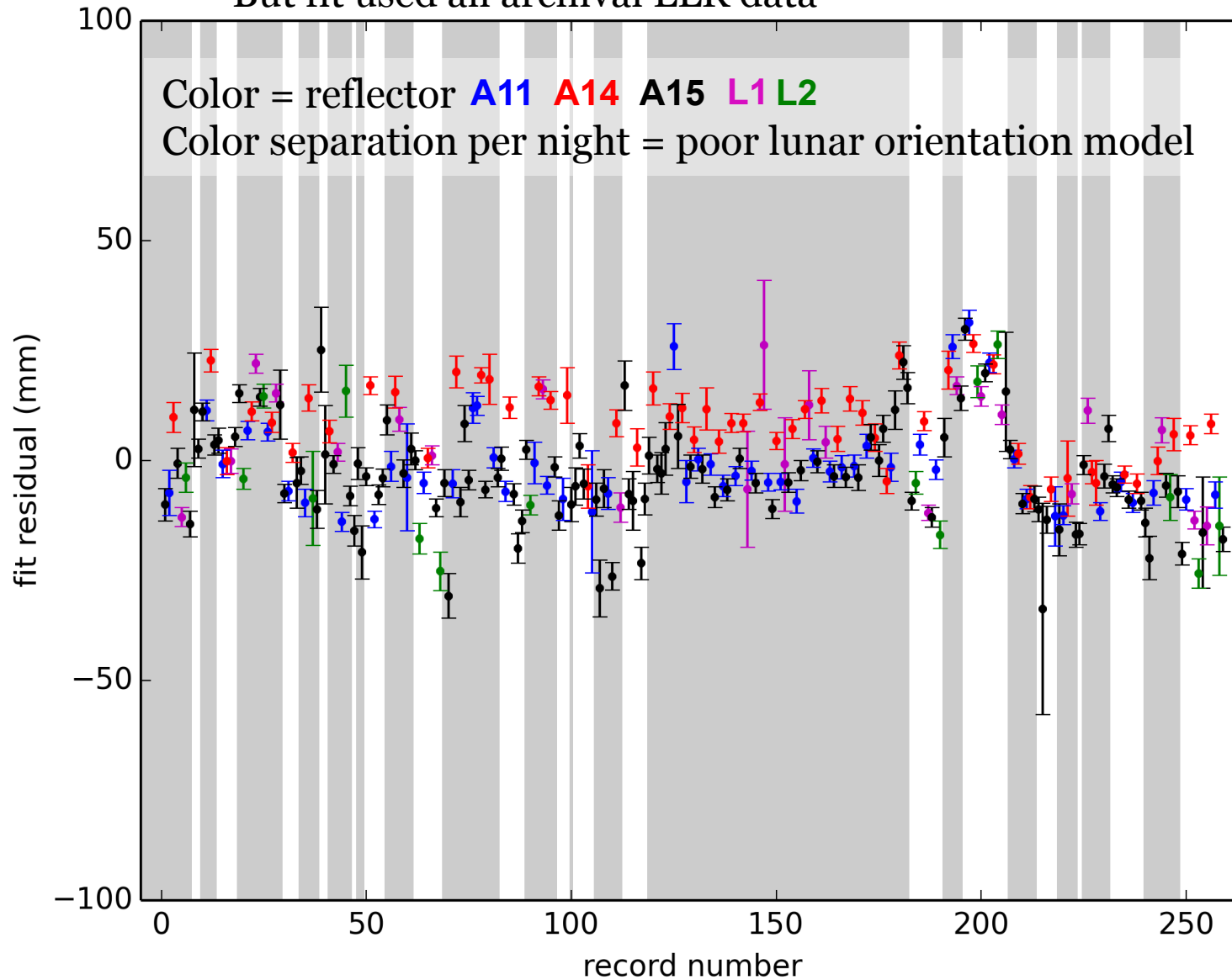


# Model vs. Data comparison



# Model vs. Data comparison

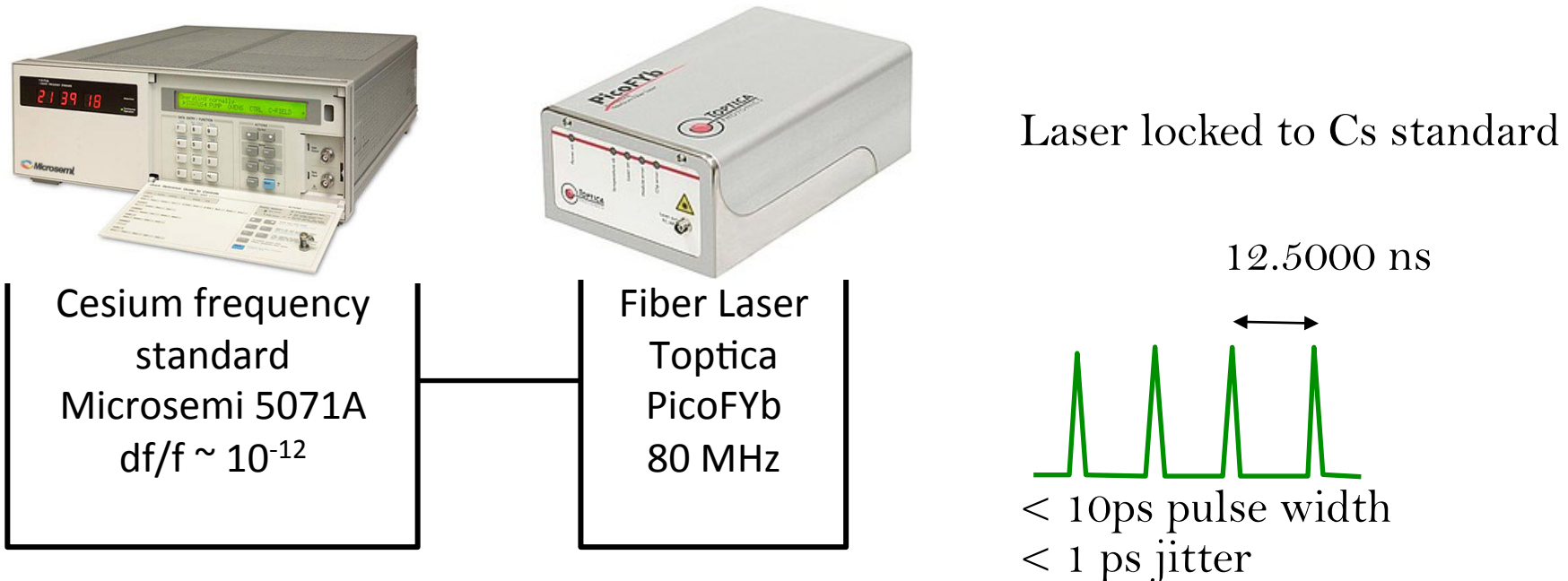
Residuals are APOLLO data since September 2013  
But fit used all archival LLR data



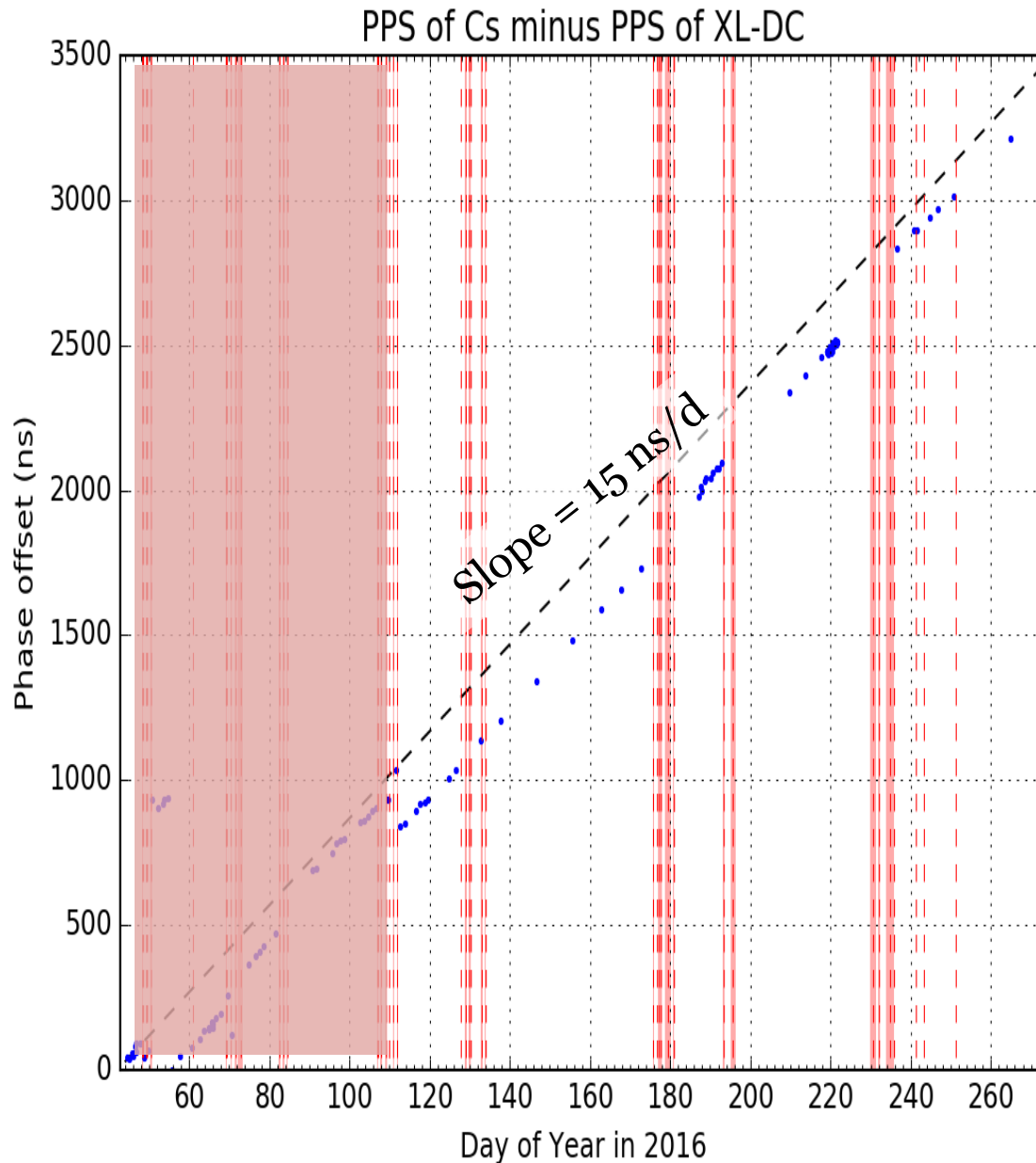
# Absolute Calibration System

Adelberger et al. CQG, 2017 arXiv:1706.09550

- Calibration laser pulses inserted at a known rate
  - Simultaneous with lunar ranging
- An “optical ruler” overlaid on data.



# Aside: Gravitational Redshift



Atomic clock at 2.8 km  
vs.  
GPS clock “at” sea level

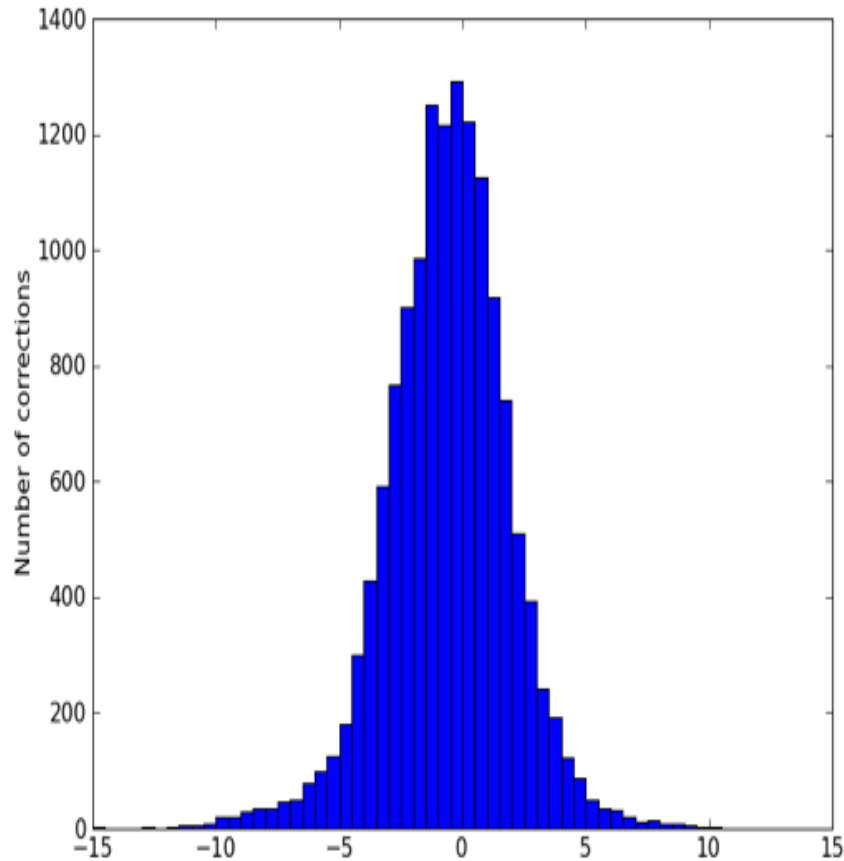
$$\Delta f / f$$

Gravitational Redshift:  $3.0 \times 10^{-13}$   
Cs clock intrinsic:  $-1.3 \times 10^{-13}$   
Net:  $1.7 \times 10^{-13}$

Predict: 15 ns/day phase accumulation



# Measure GPS-Cs clock offset



GPS has excellent long-term stability, but worse short-term stability than Cs.

GPS clock offsets equivalent to  $\sim 2.5$  mm added in quadrature to the raw range precision.

Now use the Cs clock (sub-mm)

Have back-corrected our 10-year data archive as well!

GPS clock offset [mm one-way lunar range]



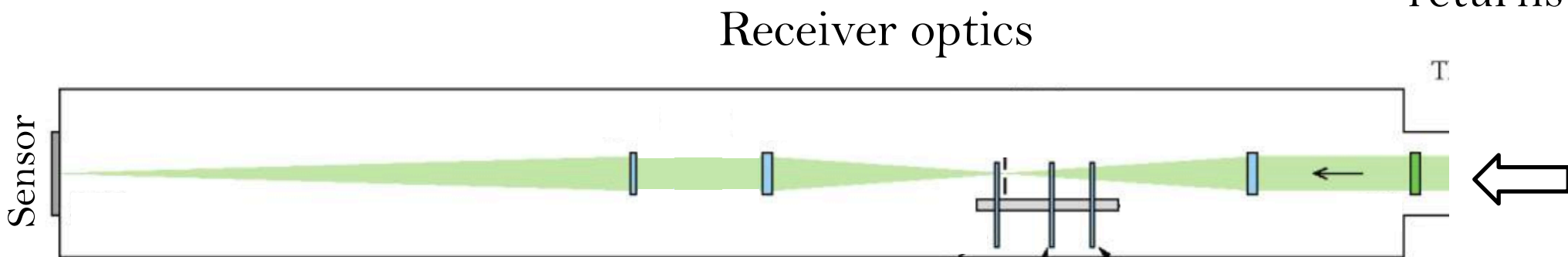
vs.



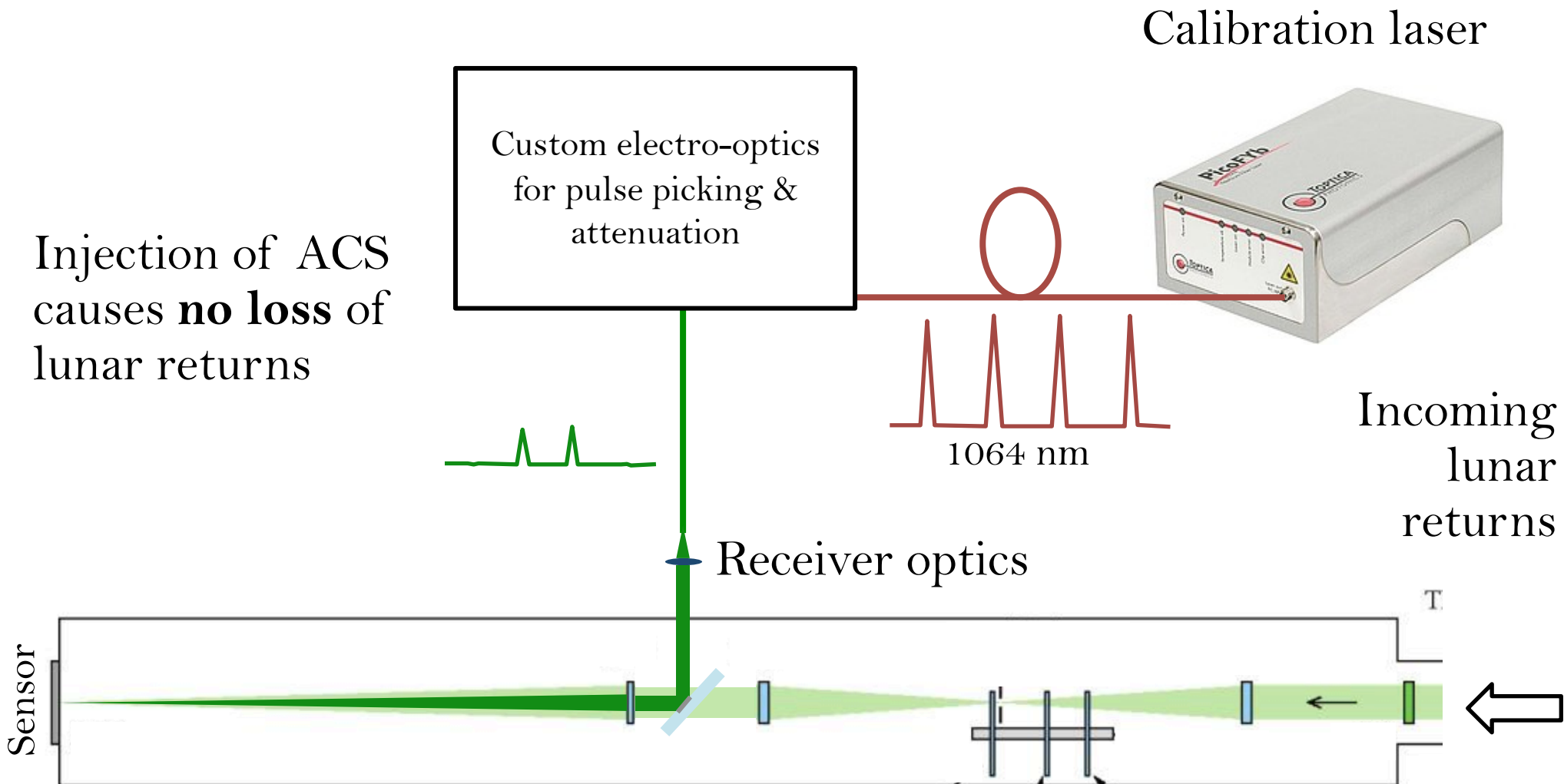
# Laser ranging with ACS overlay

No lunar photons in center of collimated beam  
because of shadow of telescope secondary mirror.

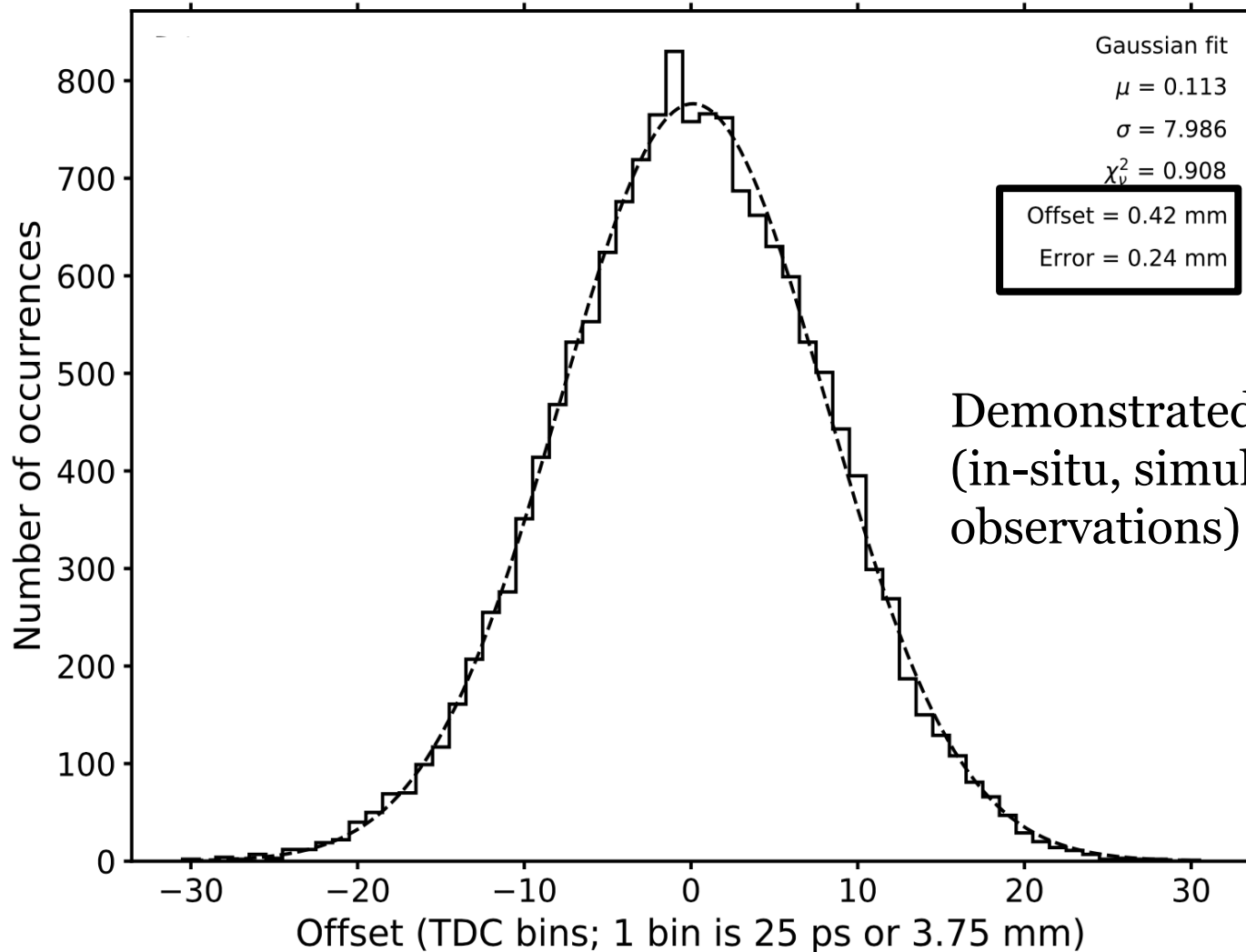
Incoming  
lunar  
returns



# Laser ranging with ACS overlay



# Compare APOLLO measurements of $\Delta t$ of ACS pulse pairs with $N \approx 12.500000$ ns

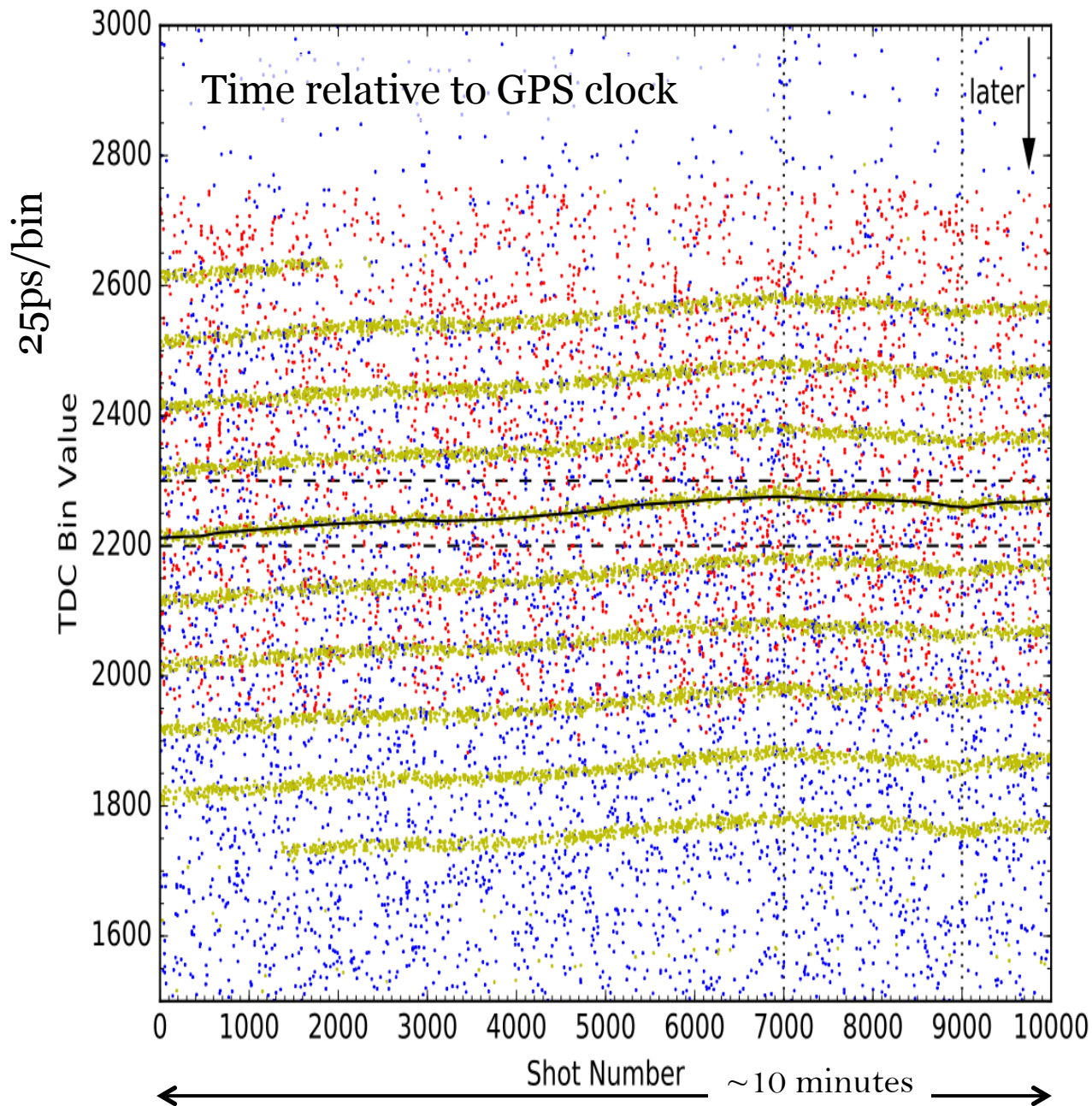


Demonstrated sub-mm timing accuracy  
(in-situ, simultaneous with LLR  
observations)

Adelberger et al. CQG, 2017 arXiv:1706.09550



# ACS calibration atop Lunar Returns 2016.09.12



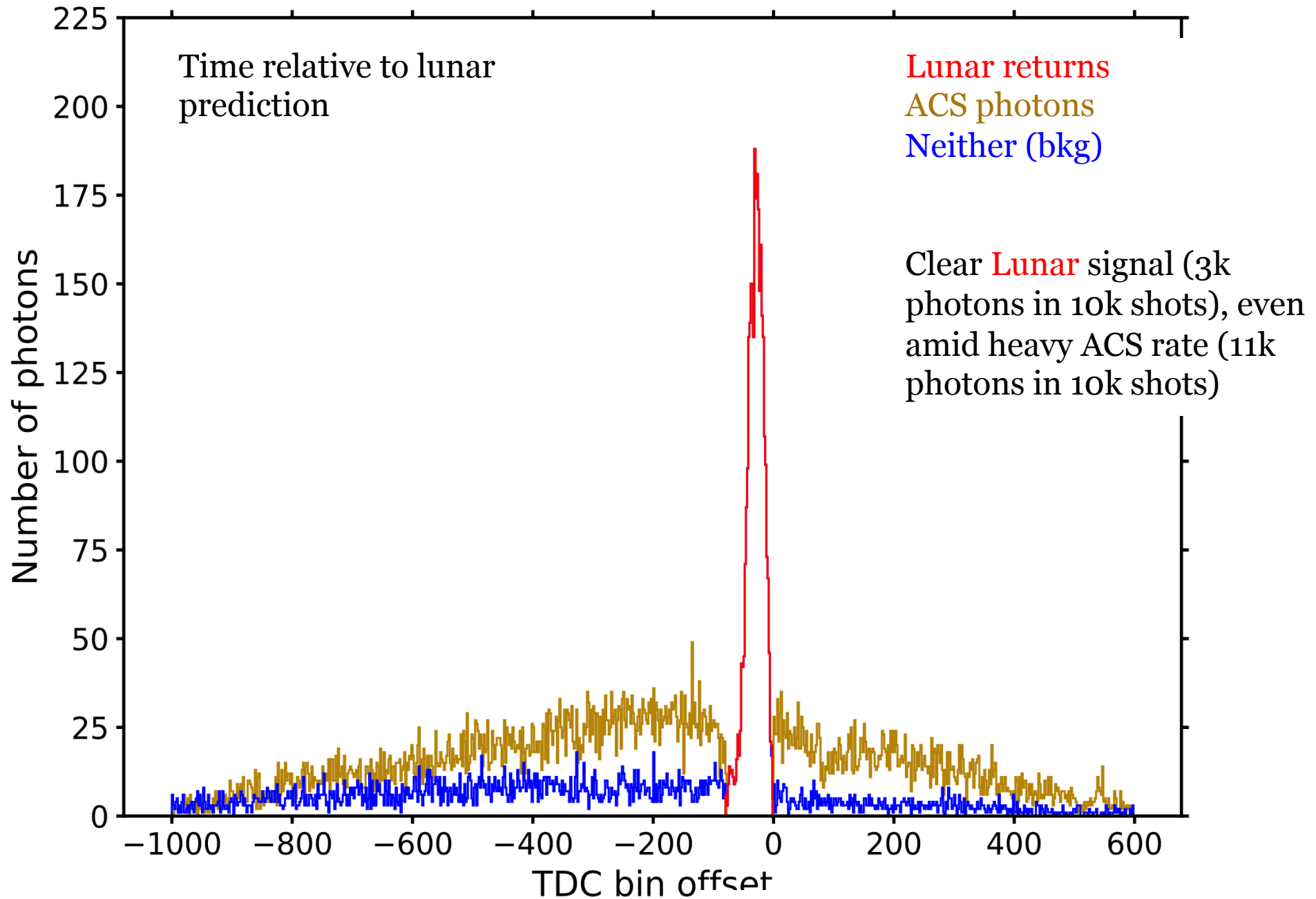
Total shots (10k)  
ACS photons (11k)  
Lunar returns (3k)  
Neither (bkg)  
– clock comparison

Can tag ACS photons very efficiently even when overlaid with Lunar returns.

Use knowledge of ACS clock phase relative to GPS clock



# ACS calibration atop Lunar returns 2016.09.12



Adelberger et al. CQG, 2017 arXiv:1706.09550

# The Absolute Calibration System shows that:

- **APOLLO accuracy is 1–2 mm**, characterized at the sub-mm level  
Confident that **range model deficiencies** cause the  $\sim 10$  mm residuals
- **GPS clock offsets caused  $\sim 2.5$  mm range error (correctable)**  
Back-correction applied to the entire 10-year APOLLO data archive (clock logs)  
**reduces typical archival range error from 2.5 mm to 1.6 mm**
- **Cs clock now in use & on-demand calibration now standard**  
Enables routine monitoring of system stability
- **The ball is squarely in the modeling community's court now.**

Adelberger et al., CQG (2017) arXiv:1706.09550

Liang et al., CQG (2017) arXiv:1706.09421

# Ongoing: Solar System model upgrades

- Very few capable models (rms)

France, Russia, Germany, USA (JPL and **Harvard**)  
Some groups are in communication to share ideas

APOLLO residuals

JPL: ~15 mm

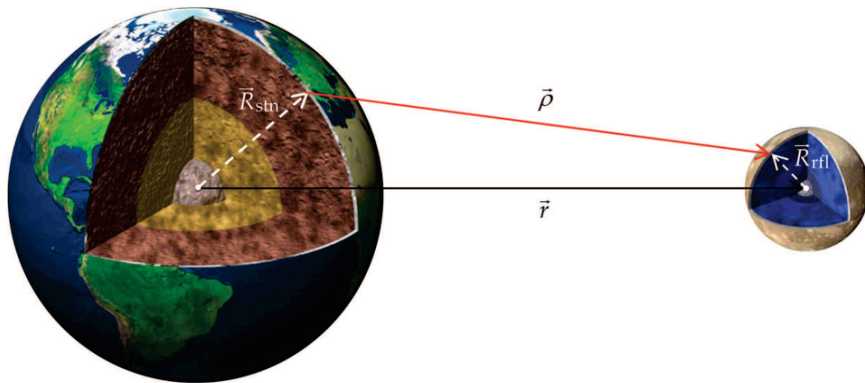
PEP: ~30 mm

**Planetary Ephemeris Program**

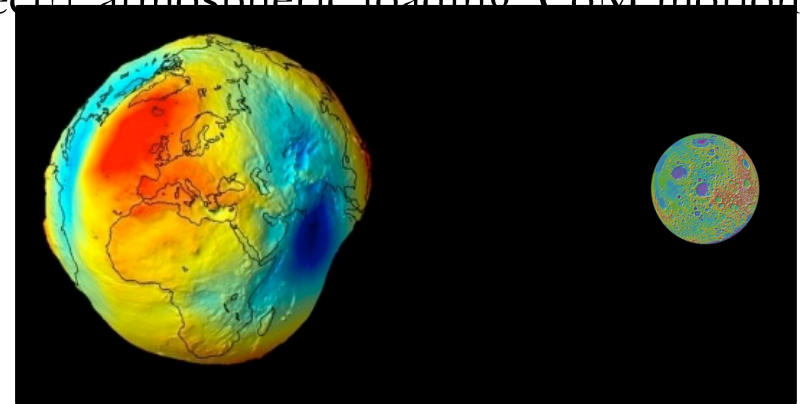
- Current focus of model development

- Find bugs/limitations (e.g. some series truncated for cm accuracy)
- Improve/expand models

Lunar interior, solar radiation pressure (4 mm effect!), atmospheric loading, CoM motion




**US.**





# Ongoing: Solar System model upgrades

- Very few capable models (rms)  
France, Russia, Germany, USA (JPL and **Harvard**)  
Some groups are in communication to share ideas
  - Current focus of model development
    - Find bugs/limitations (e.g. some series truncated for cm accuracy)
    - Improve/expand models  
Lunar interior, solar radiation pressure (4 mm effect!), atmospheric loading, CoM motion
  - **PEP** advantages
    - Full monolithic integration of Solar System + Moon
    - Broad datasets (radar, doppler, planetary fly-bys, pulsar timing)
    - **Tight coupling between APOLLO & PEP: ~real-time testing**
- APOLLO residuals
- JPL: ~15 mm
- PEP: ~30 mm**
- Planetary Ephemeris Program**
- 

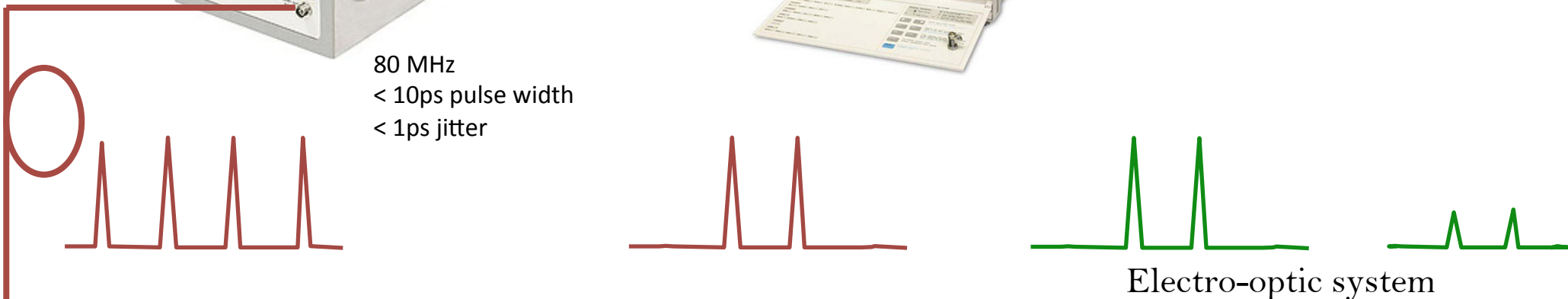
# Conclusion

- LLR provides frontier constraints on gravity
- APOLLO delivers millimeter-accurate LLR data
- Model improvements are required for improved gravitational constraints
- A close and productive APOLLO-PEP collaboration is underway

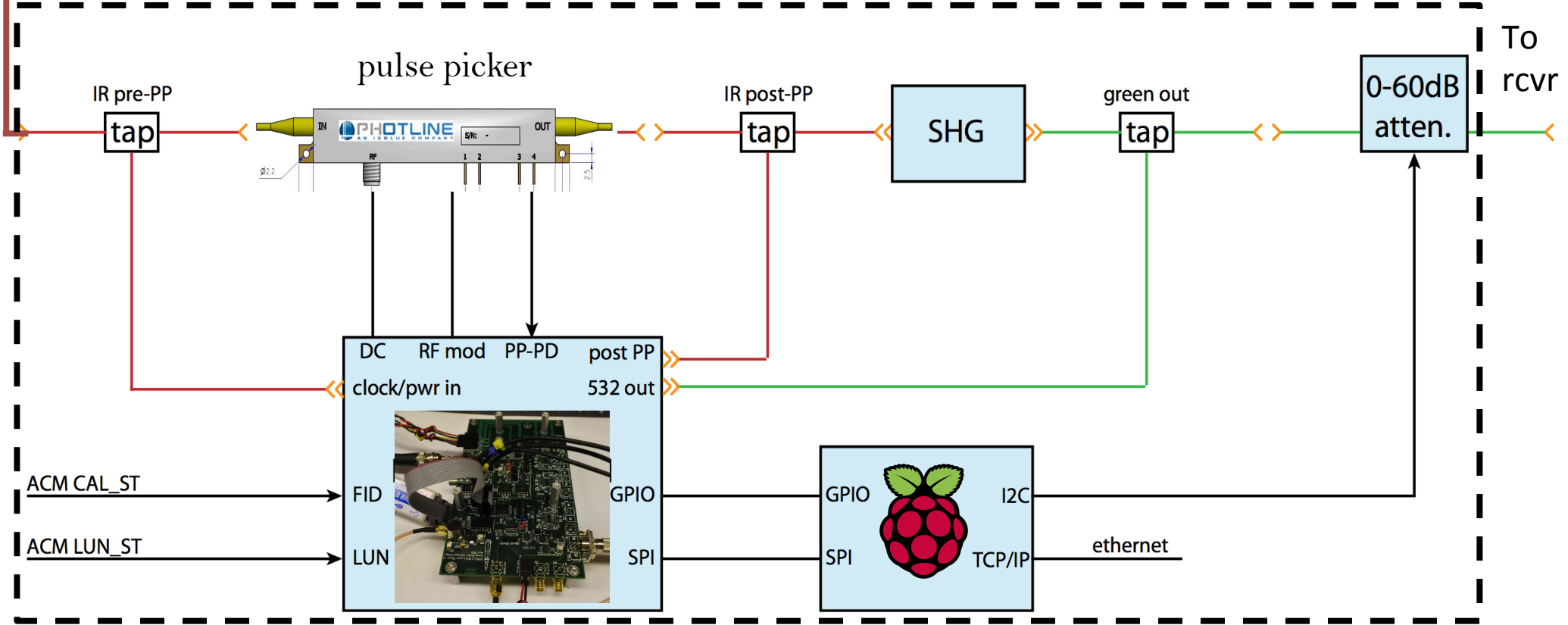
EXTRAS



80 MHz  
< 10ps pulse width  
< 1ps jitter



Electro-optic system



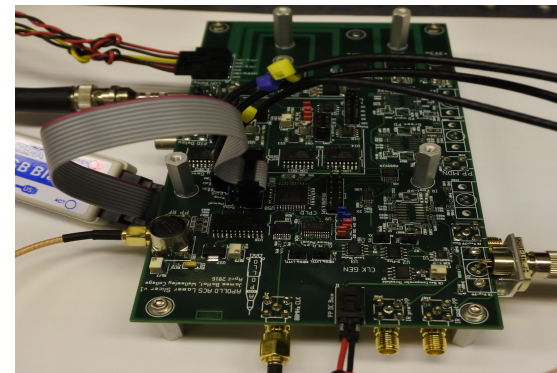


# Absolute Calibration System

- Part 1: Clock: Cs vs. GPS  
Installed February 2016



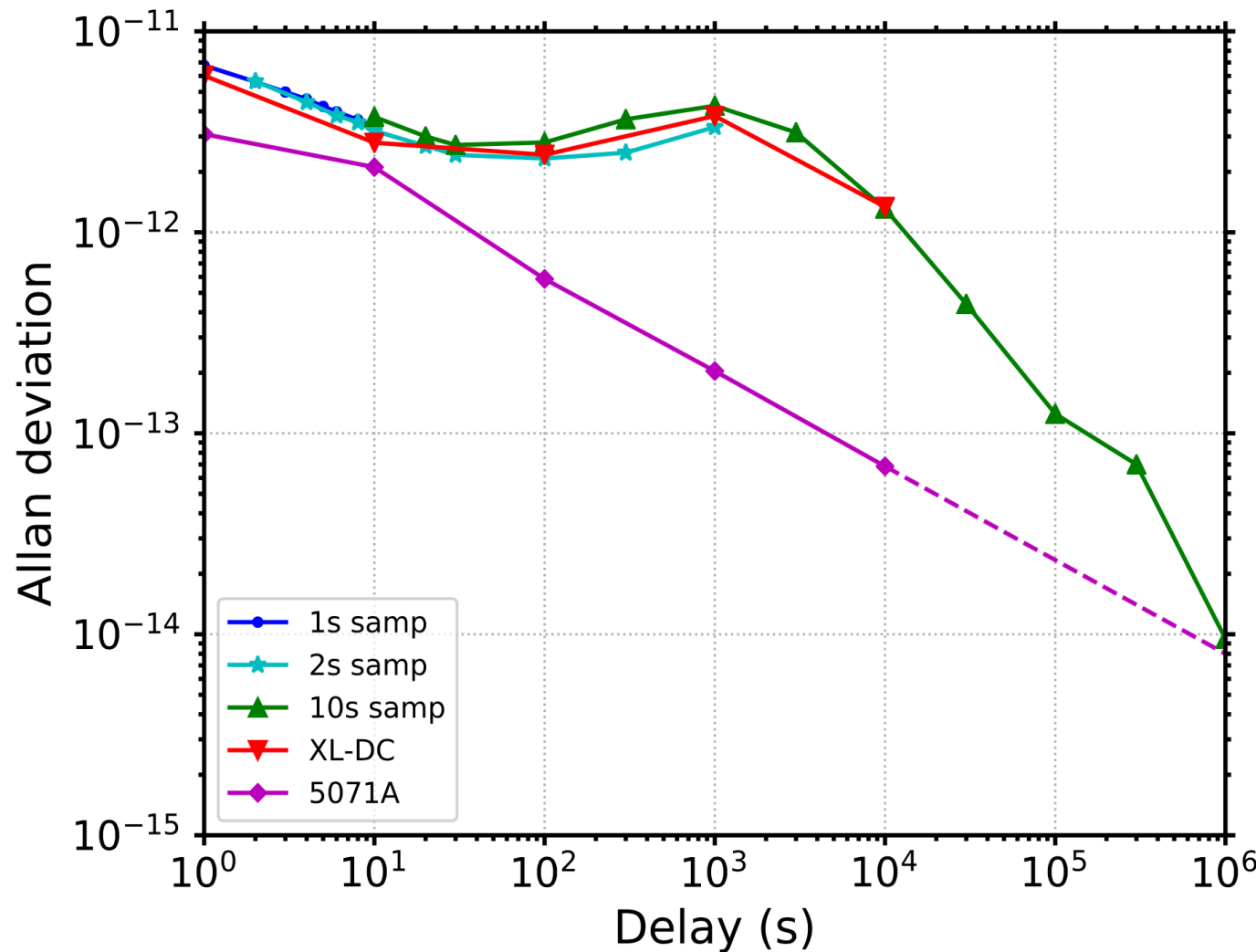
- Part 2: Laser, pulse selection and overlay with  
LLR observations  
Installed August 2016



# Phase 1: Clock installation (Feb. 2016)



# Allan Deviation of Cs and XL-DC clocks



Uses Cs clock as the reference for XL-DC measurements.

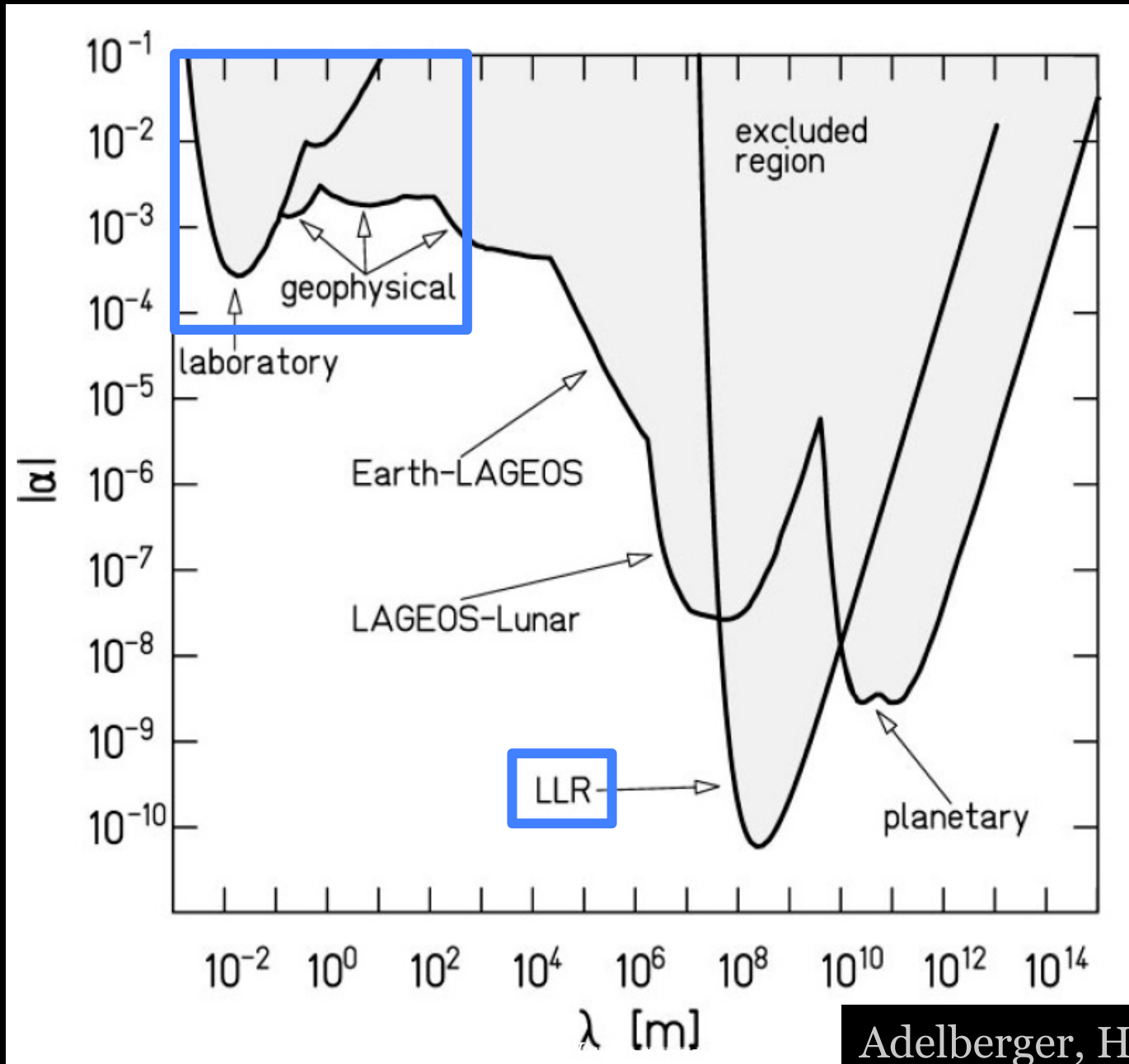
Cs Allen deviation measured by manufacturer relative to a hydrogen maser

Cs has better short-term stability

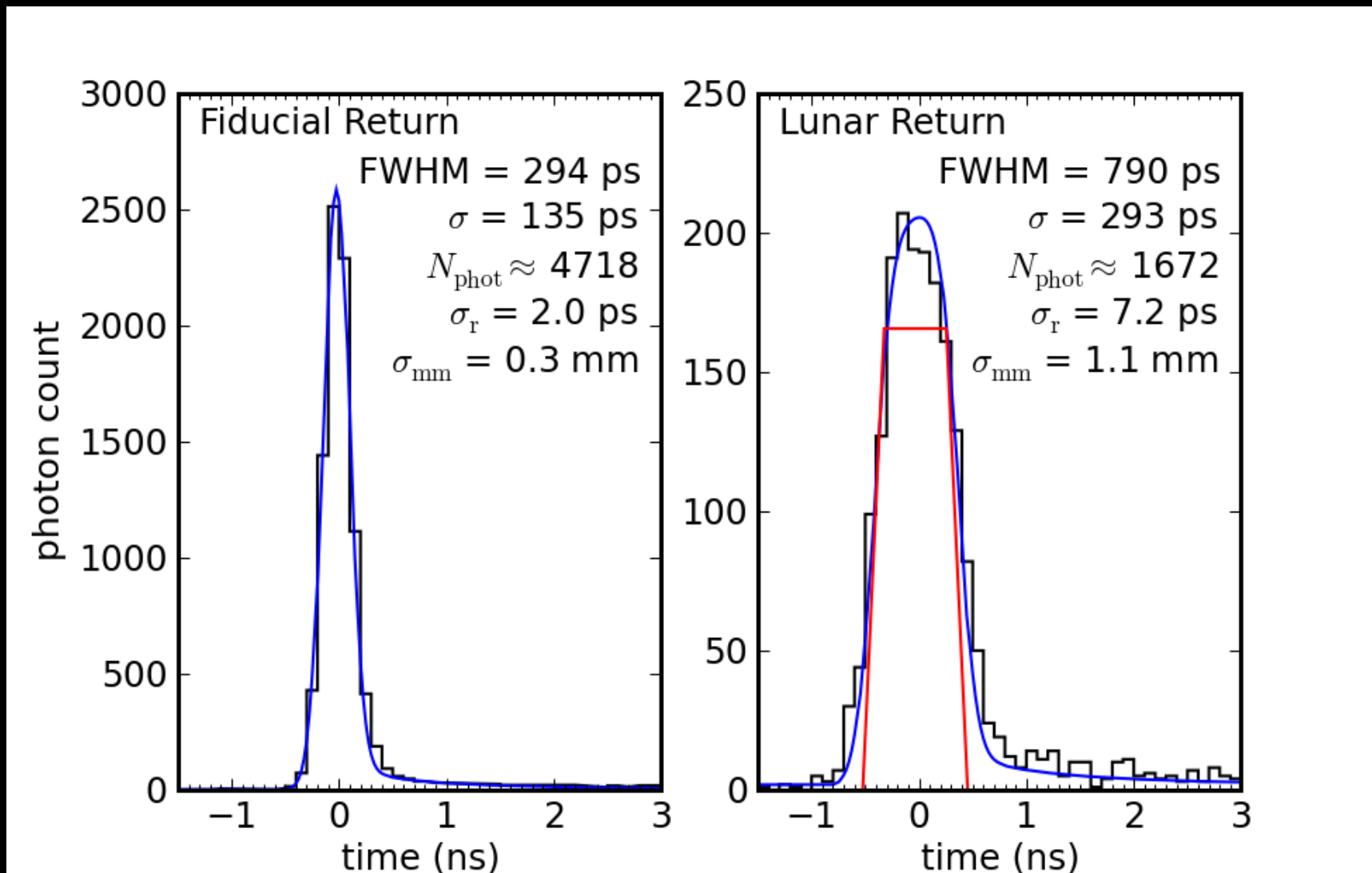
XL-DC does better at  $>10^6$  seconds due to GPS tie-in

Note difficulty of GPS solution at  $10^3$  second timescale (atmospheric effects)

# Yukawa Interaction Constraints



# Fitting the Return & Reflector Trapezoid





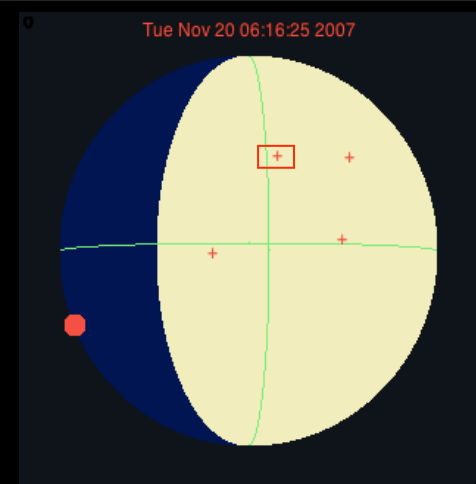
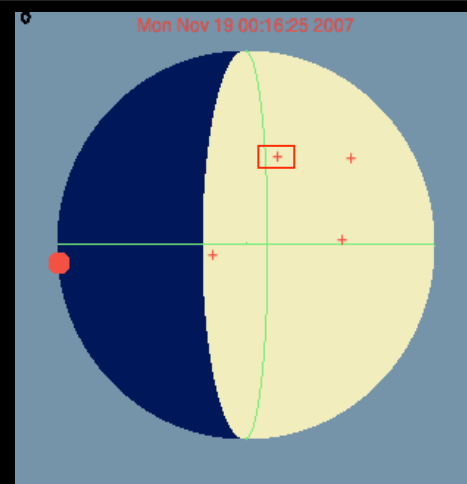
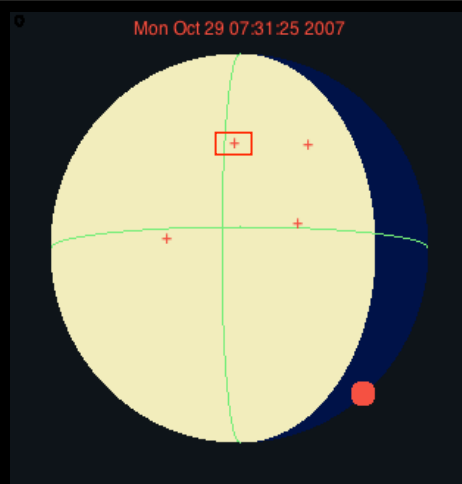
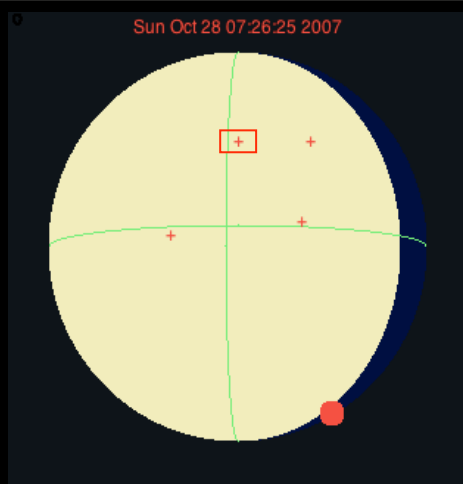
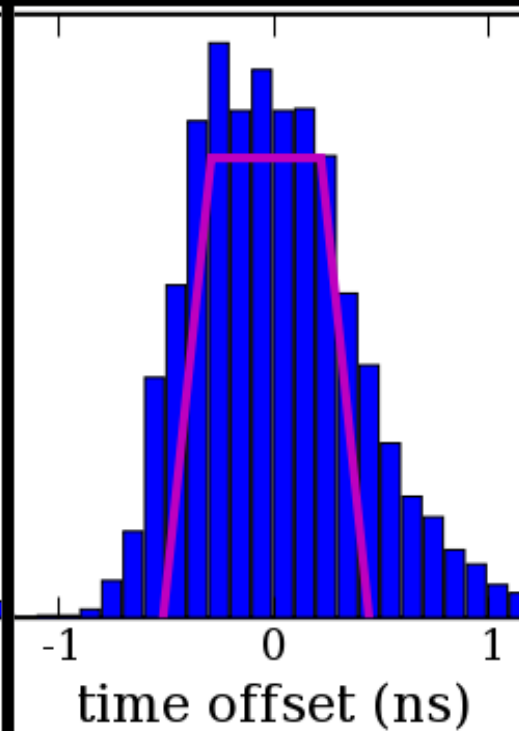
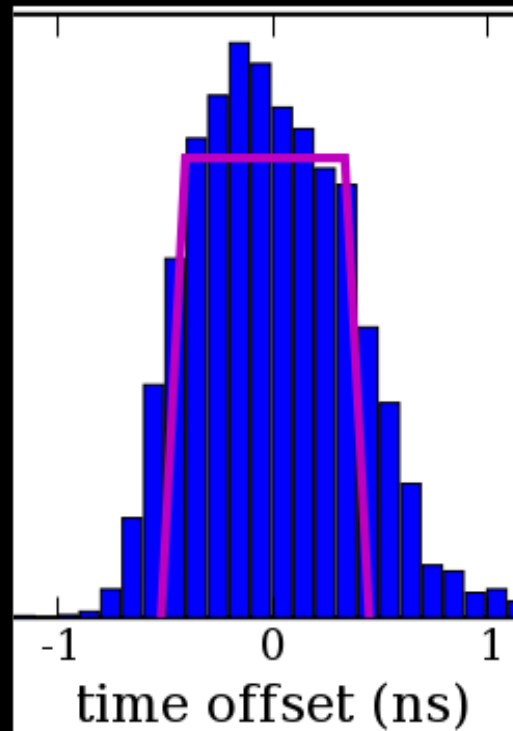
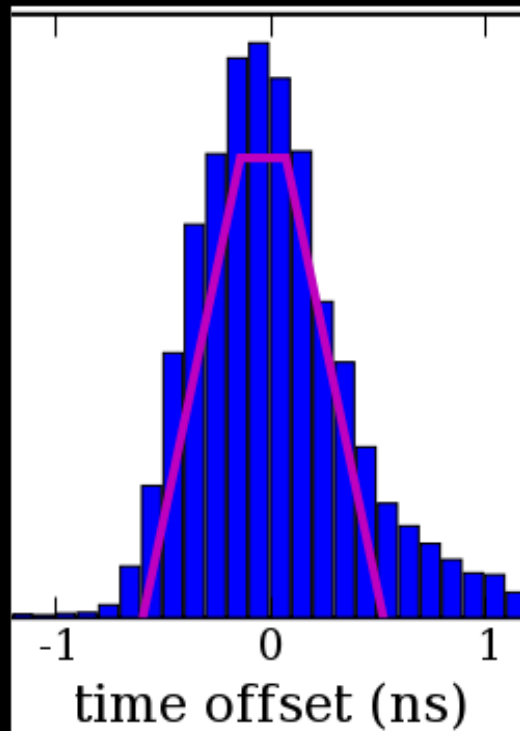
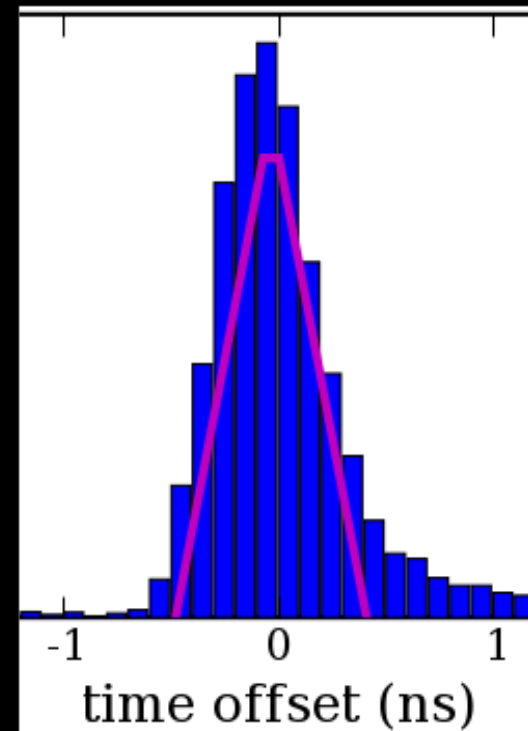
# Sensing the Array Size & Orientation

2007.10.28

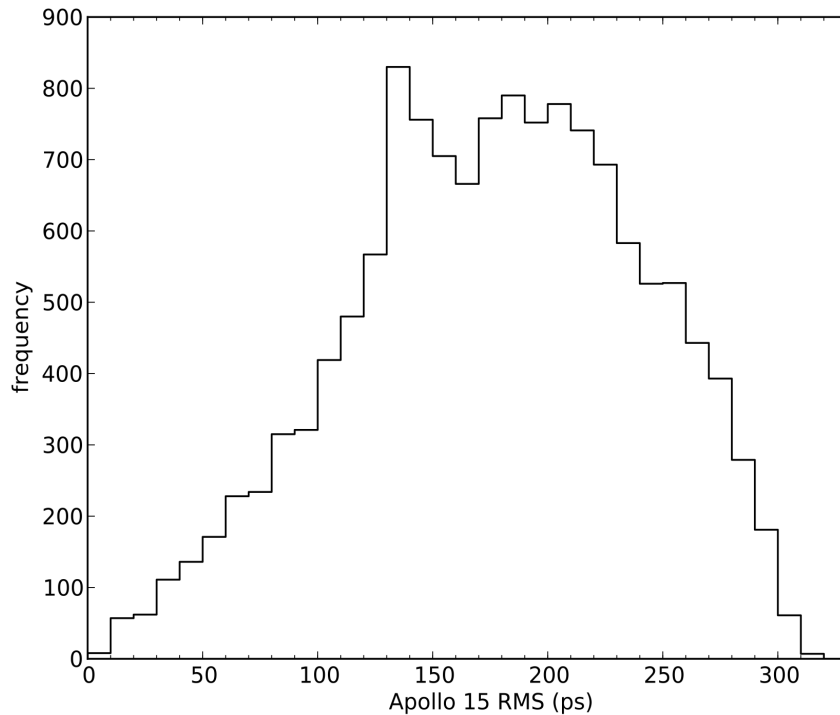
2007.10.29

2007.11.19

2007.11.20



# Libration dominates the error budget



Error Source	RMS Error (ps)	RMS Error (mm)
APD illumination	60	9
APD intrinsic	< 50	< 7.5
Laser pulse	45	7
Timing electronics	20	3
GPS clock	7	1
<b>Total APOLLO</b>	<b>93</b>	<b>14</b>
<b>Retroreflector array</b>	<b>100–300</b>	<b>15–45</b>
<b>Total random uncertainty</b>	<b>136–314</b>	<b>20–47</b>