

The SIMP paradigm: new territory for thermal relics

Hyun Min Lee

Chung-Ang University, Korea



THE 14TH INTERNATIONAL WORKSHOP
ON THE DARK SIDE OF THE UNIVERSE

DSU |
2018 |

25 - 29 June 2018

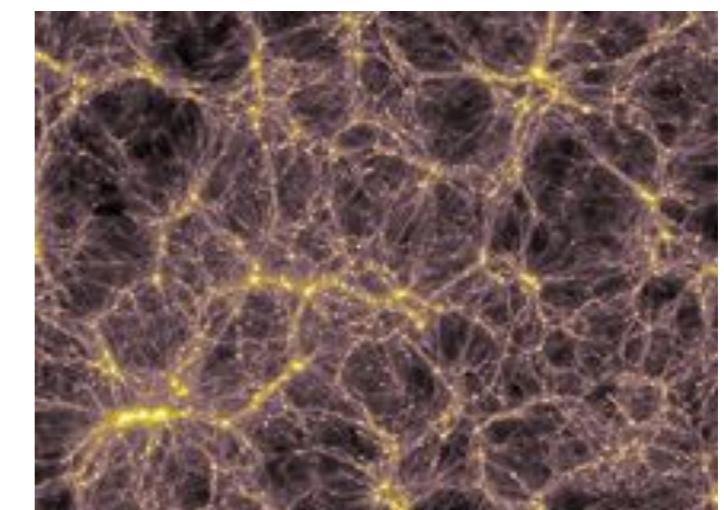
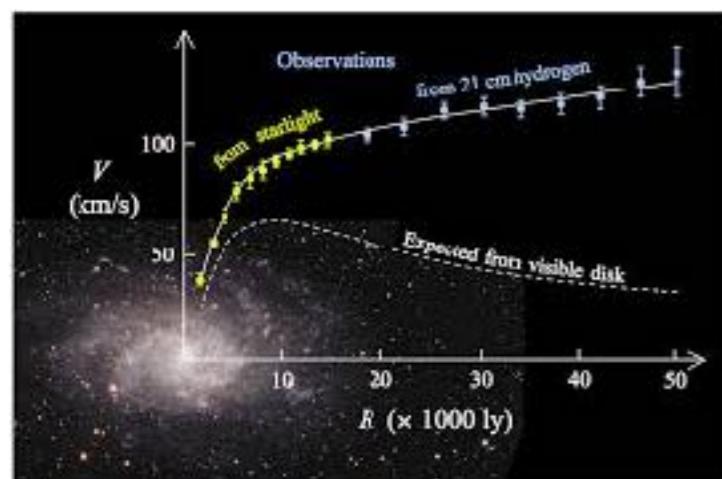
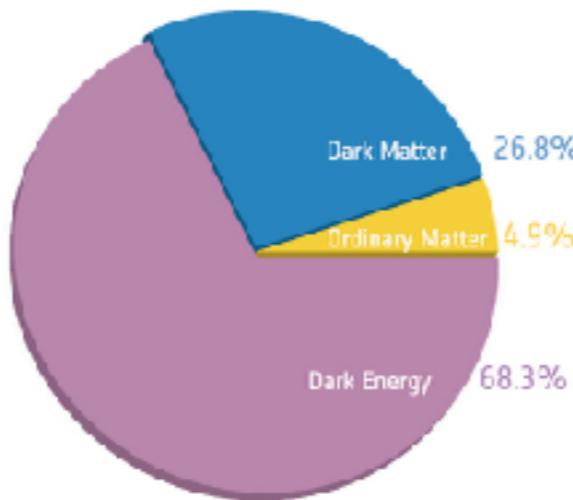
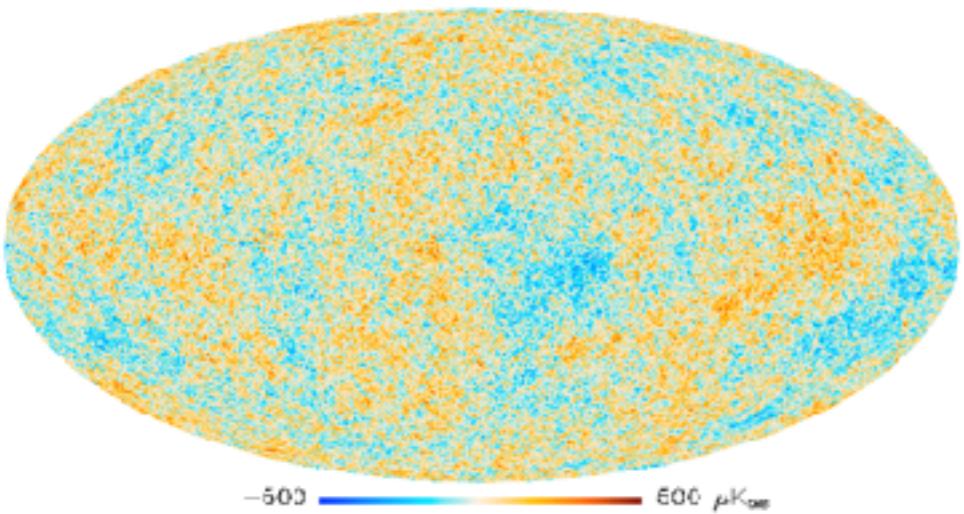
LAPTh, Annecy, France

LAPTh

Outline

- Introduction
- SIMP mesons
- Resonant SIMPs
- Conclusions

Dark matter from sky



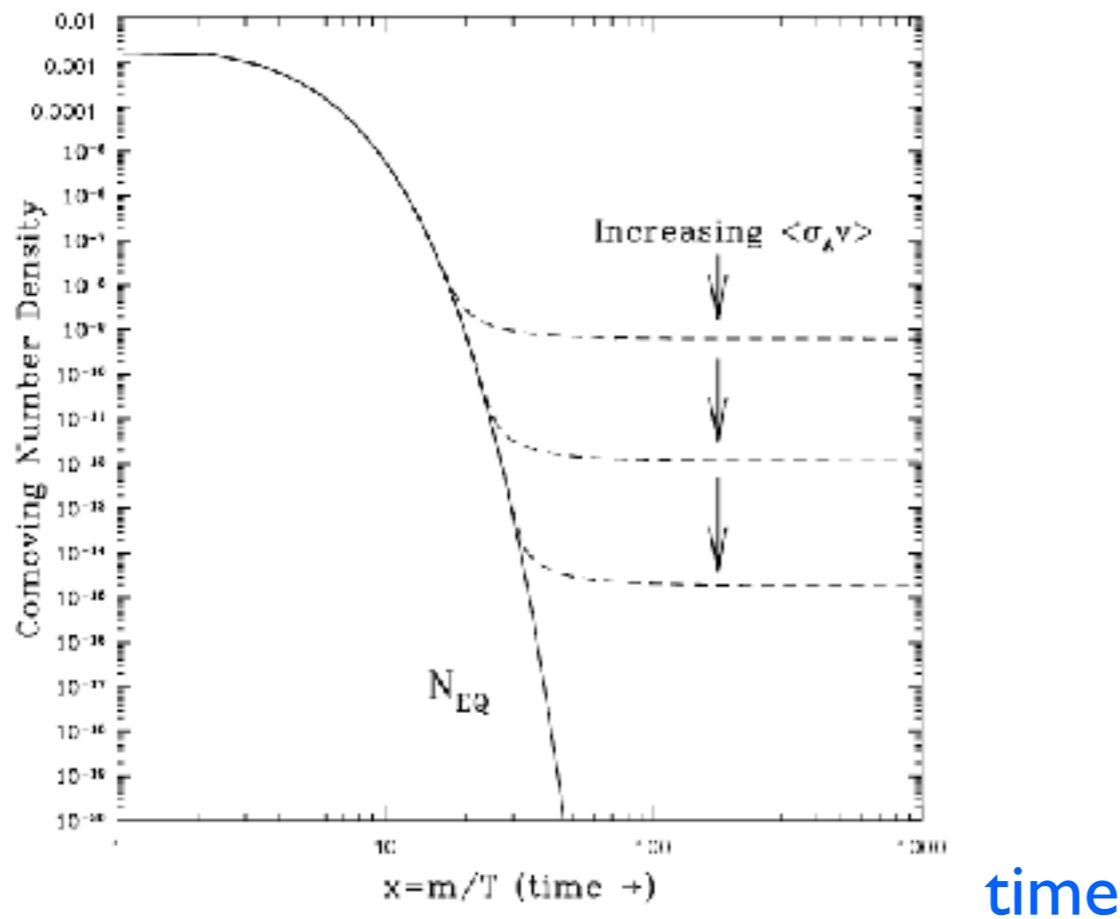
- Various evidences for dark matter from galaxy rotation curves, CMB, gravitational lensing, and large scale structure.

Non-gravitational evidence is missing!
What is particle nature of dark matter?

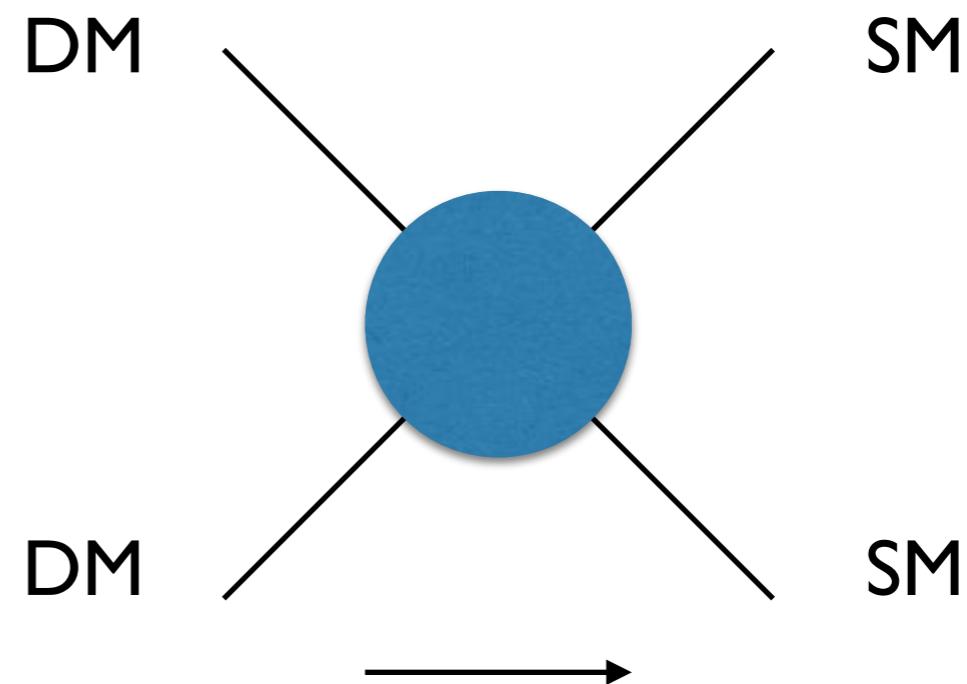
WIMP Paradigm

[Lee, Weinberg(1977)]

DM number



Dark matter once in thermal equilibrium with SM particles

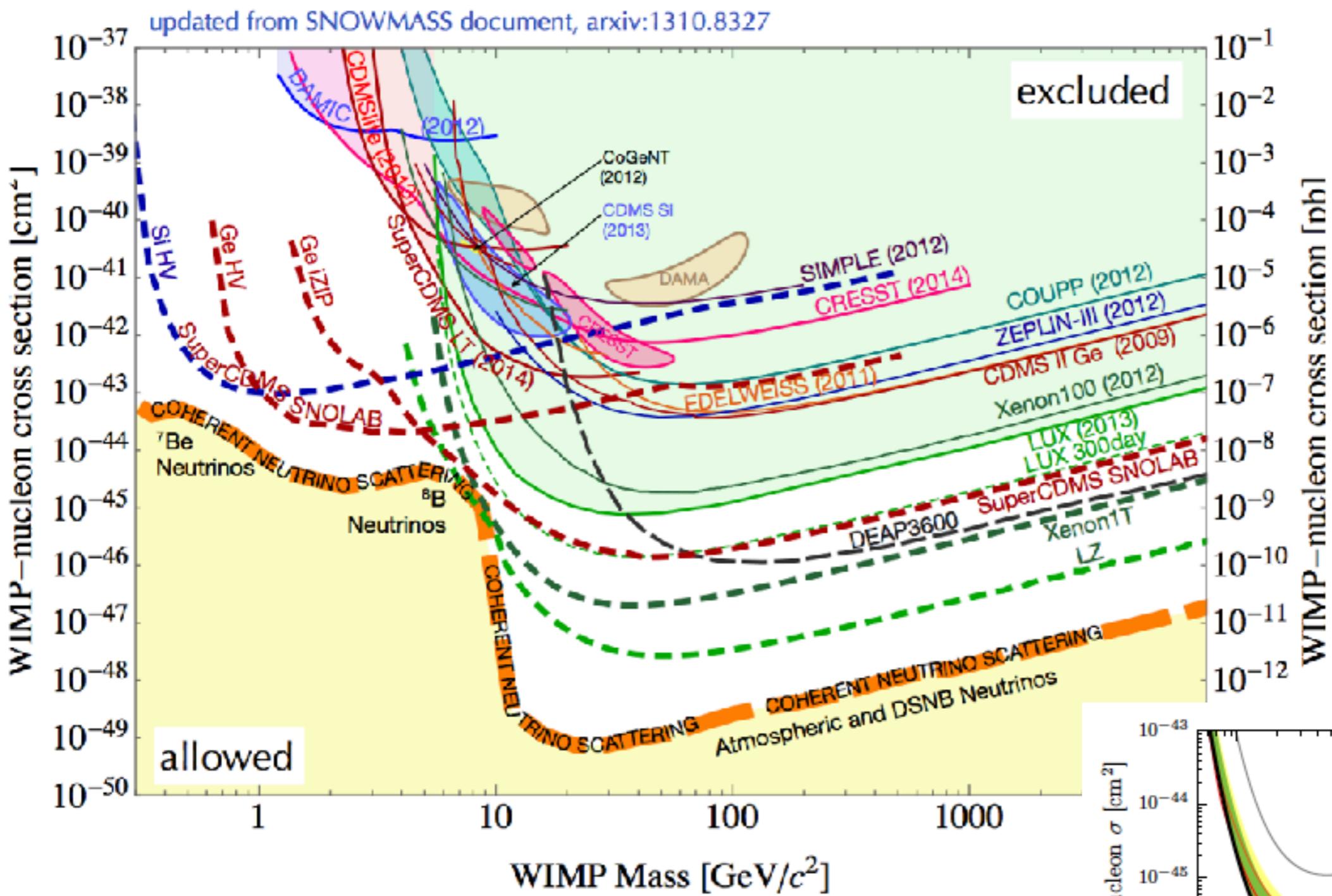


Weak interaction with 100GeV-1TeV mass:

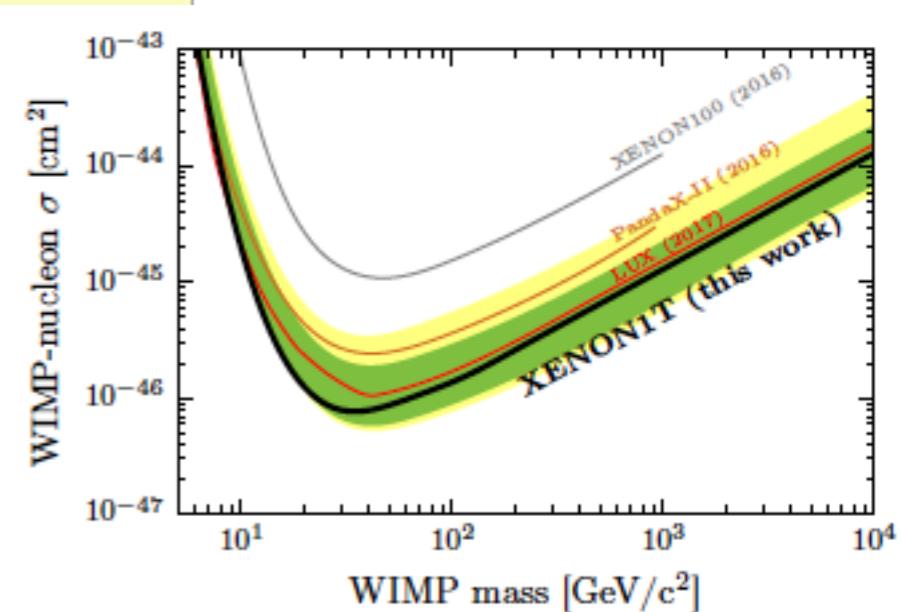
$$\rightarrow \Omega_{DM} h^2 = 0.1 \left(\frac{1 \text{ pb} \cdot c}{\langle \sigma_A v \rangle} \right)$$

Interplay of direct, indirect and collider detections!

WIMP in challenge



No direct evidence for WIMP yet



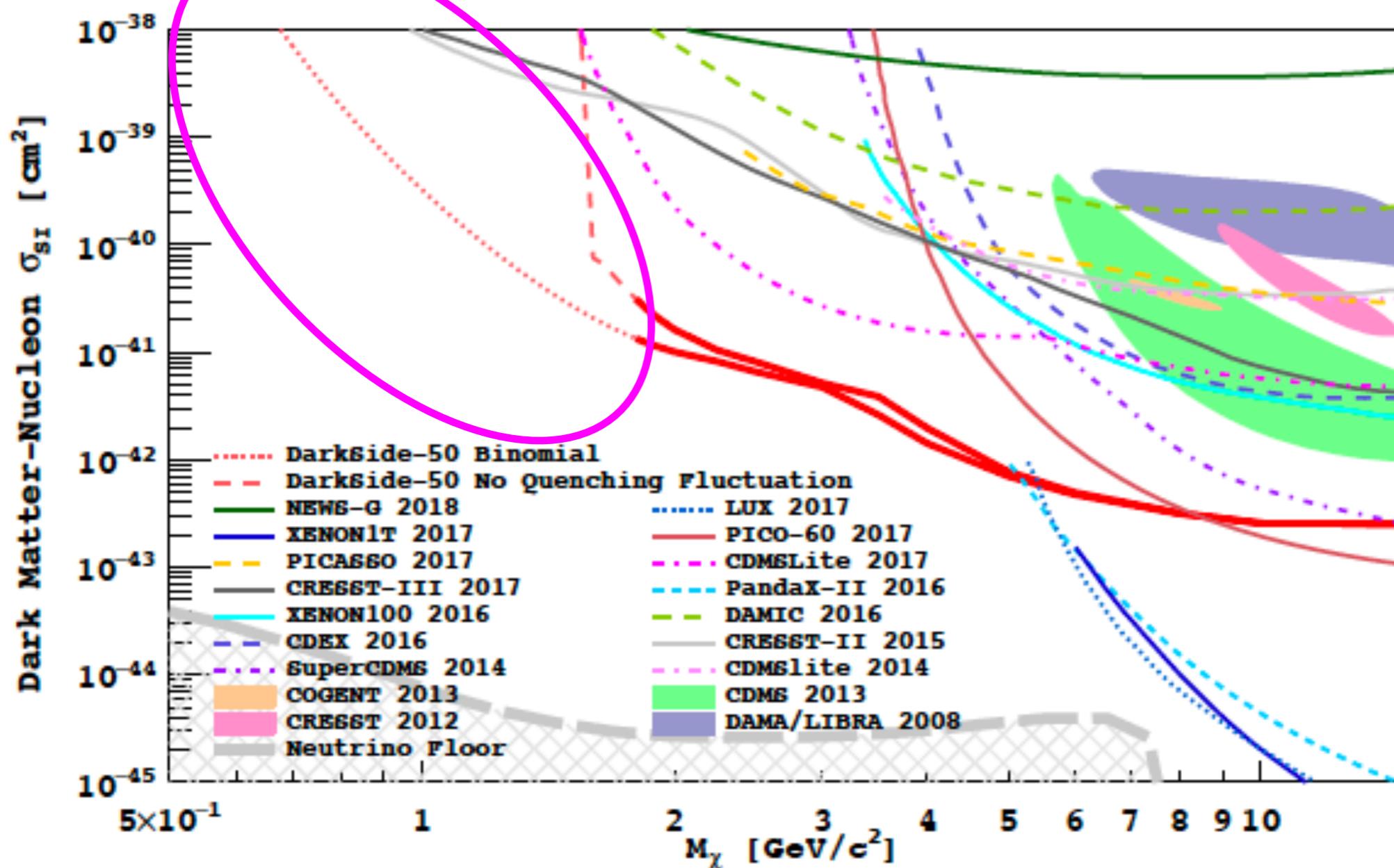
Light dark matter

Below typical WIMP masses: $1 \text{ keV} \lesssim m_{\text{DM}} \lesssim 10 \text{ GeV}$

$$E_R = \frac{\vec{q}^2}{2m_N} = \frac{(m_{\text{DM}}v)^2}{2m_N} \lesssim \text{keV} : \text{Small recoil energy}$$

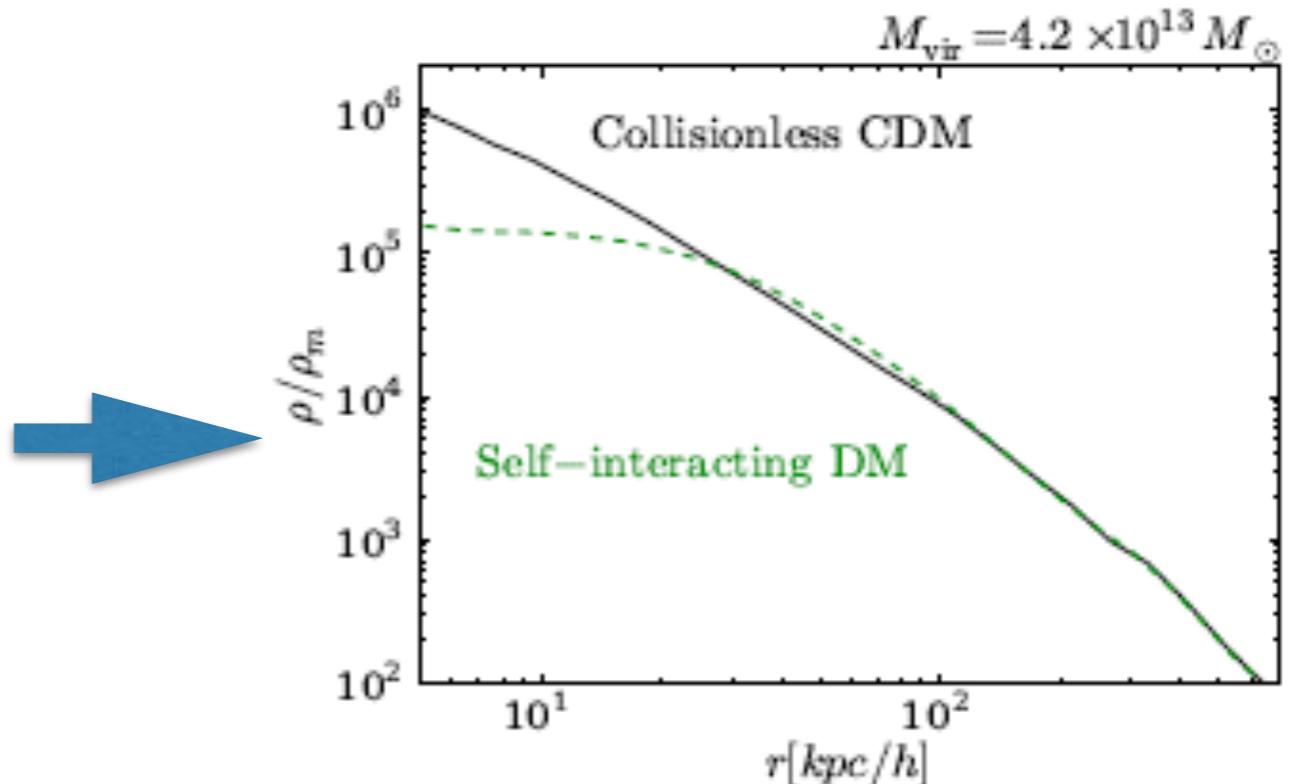
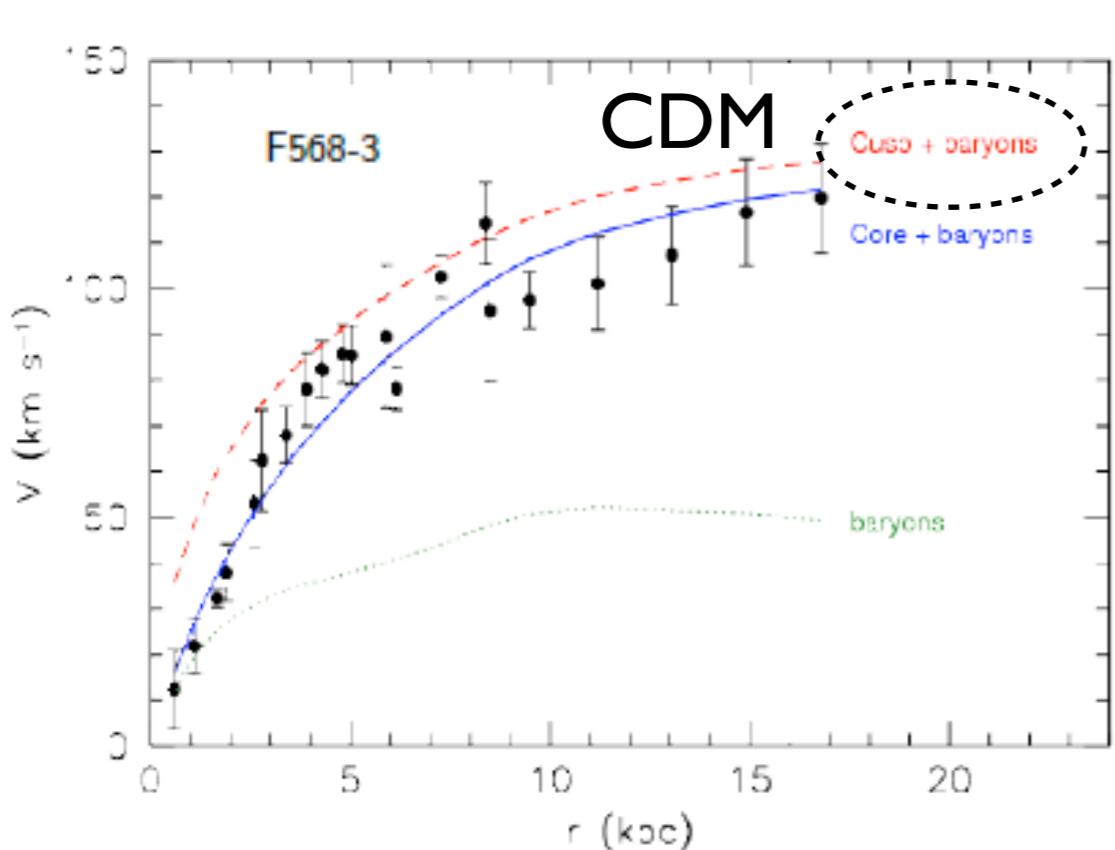
(Fermion DM)

Need to lower the detector threshold.



Self-interacting dark matter

- **Core-cusp problem:** Simulation with CDM (“cusp”) overshoots observed galaxy rotation curves (“core”).



See a review by D.H. Weinberg et al(2013).

Large self-interaction of dark matter solves small-scale problems.

$$\sigma_{\text{self}}/m_{\text{DM}} = 0.1 - 10 \text{ cm}^2/\text{g}$$

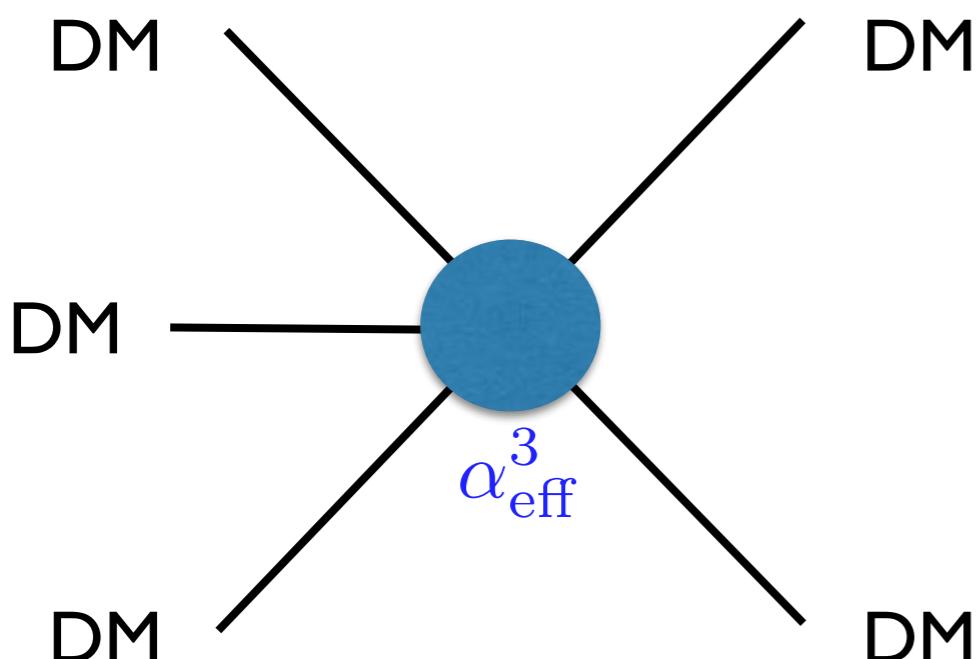
cf. Bullet cluster: $\sigma_{\text{self}}/m_{\text{DM}} < 1 \text{ cm}^2/\text{g}$

- Related problems missing satellites (fewer DM subhalos), too-big-to-fail (masses of dwarf galaxies)

SIDM=SIMP

- Strong Interacting Massive Particles(SIMP) are in chemical equilibrium by self-interactions ($3 \rightarrow 2$ process).

[Carlson,Machacek, Hall (1992);Hochberg et al, 2014; S.-M.Chi, HML, 2015]



$$\frac{dn_{\text{DM}}}{dt} + 3Hn_{\text{DM}} \approx -\langle \sigma v^2 \rangle_{3 \rightarrow 2} (n_{\text{DM}}^3 - n_{\text{DM}}^2 n_{\text{DM}}^{\text{eq}})$$

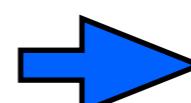
with $\langle \sigma v^2 \rangle_{3 \rightarrow 2} = \frac{\alpha_{\text{eff}}^3}{m_{\text{DM}}^5}$

SIMP freeze-out:

$$\Gamma_{3 \rightarrow 2} = n_{\text{DM}}^2 \langle \sigma v^2 \rangle_{3 \rightarrow 2} \sim H(T_F)$$

Relic density

$$\Omega_{\text{DM}} h^2 \simeq 0.1 \left(\frac{m_{\text{DM}} / 35 \text{ MeV}}{\alpha_{\text{eff}}} \right)^{3/2}$$



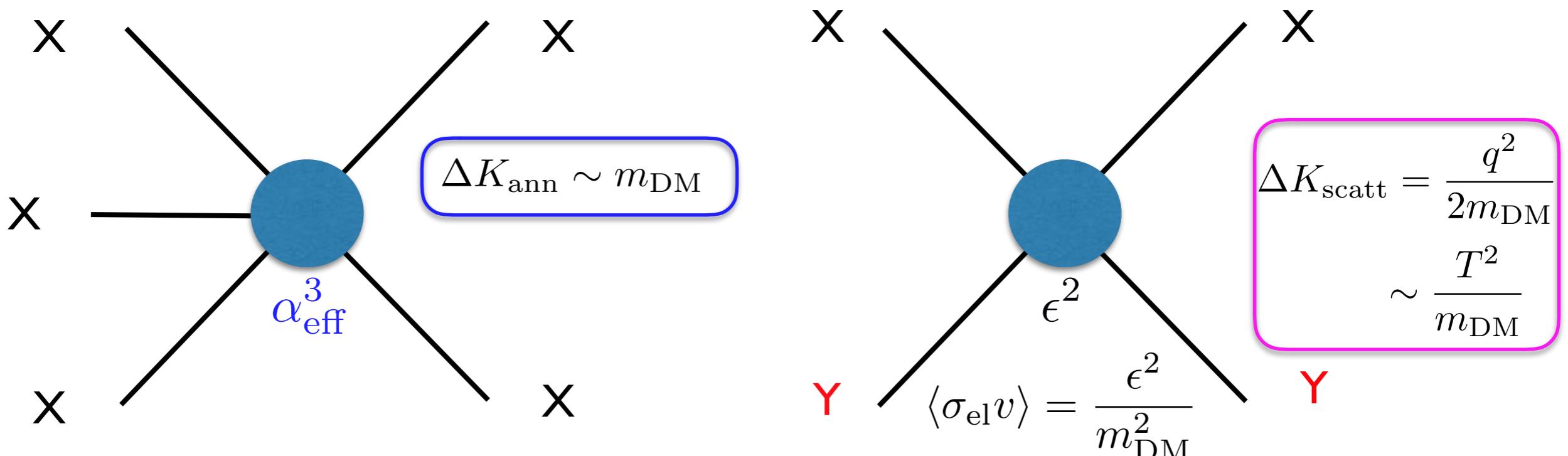
$$\alpha_{\text{eff}} = 1 - 30,$$

$$m_{\text{DM}} = 40 - 1000 \text{ MeV}$$

“Large $2 \rightarrow 2$ self-scattering”

SIMP conditions

- SIMP is heated after annihilation: kinetic equilibrium is necessary for a successful structure formation.



K: DM kinetic energy

$$\dot{K} + 2HK = -m_{\text{DM}}^2 HT^{-1} + T\gamma(T),$$

$3 \rightarrow 2$ elastic scatt.

[de Laix et al, 1995; VSIMPers, 2017]

$$\gamma(T) \sim \left\langle n_Y \sigma_{\text{el}} v_Y \frac{T}{m_{\text{DM}}} \right\rangle.$$

Kinetic equilibrium: $\gamma(T) > H \left(\frac{m_{\text{DM}}}{T} \right)^2$

cf. WIMP: $\gamma(T) > H$

$\epsilon > 10^{-8} \alpha_{\text{eff}}^{1/2}$

- Ineffective $2 \rightarrow 2$ annihilation needs $\epsilon < 2.4 \times 10^{-6} \alpha_{\text{eff}}$

SIMP & Z'-portal

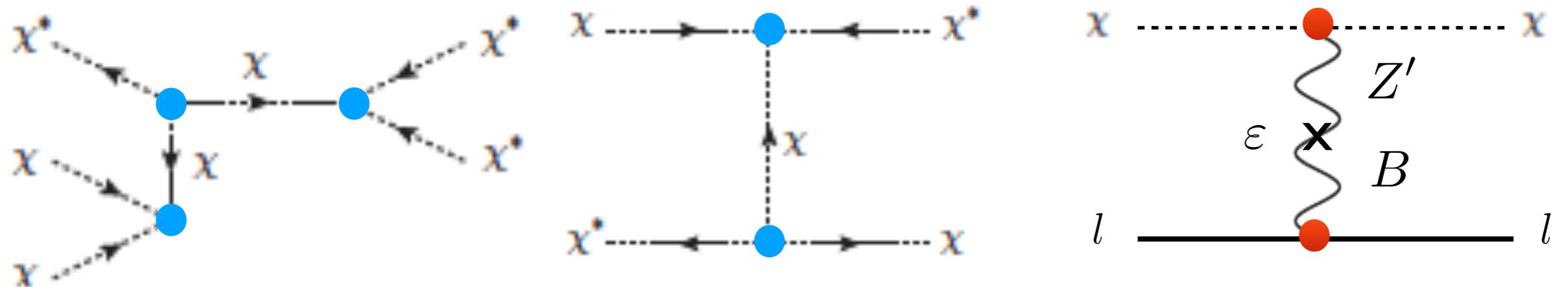
[S.-M.Chi, HML, 2015]

- Z_3 is the minimal discrete symmetry from a dark local $U(1)$ and Z' portal is built-in.

	ϕ	χ
$U(1)_V$	+3	+1

$$\langle \phi \rangle = \frac{1}{\sqrt{2}} v' \rightarrow U(1)_V \rightarrow Z_3.$$

Table 1: $U(1)_V$ charges.

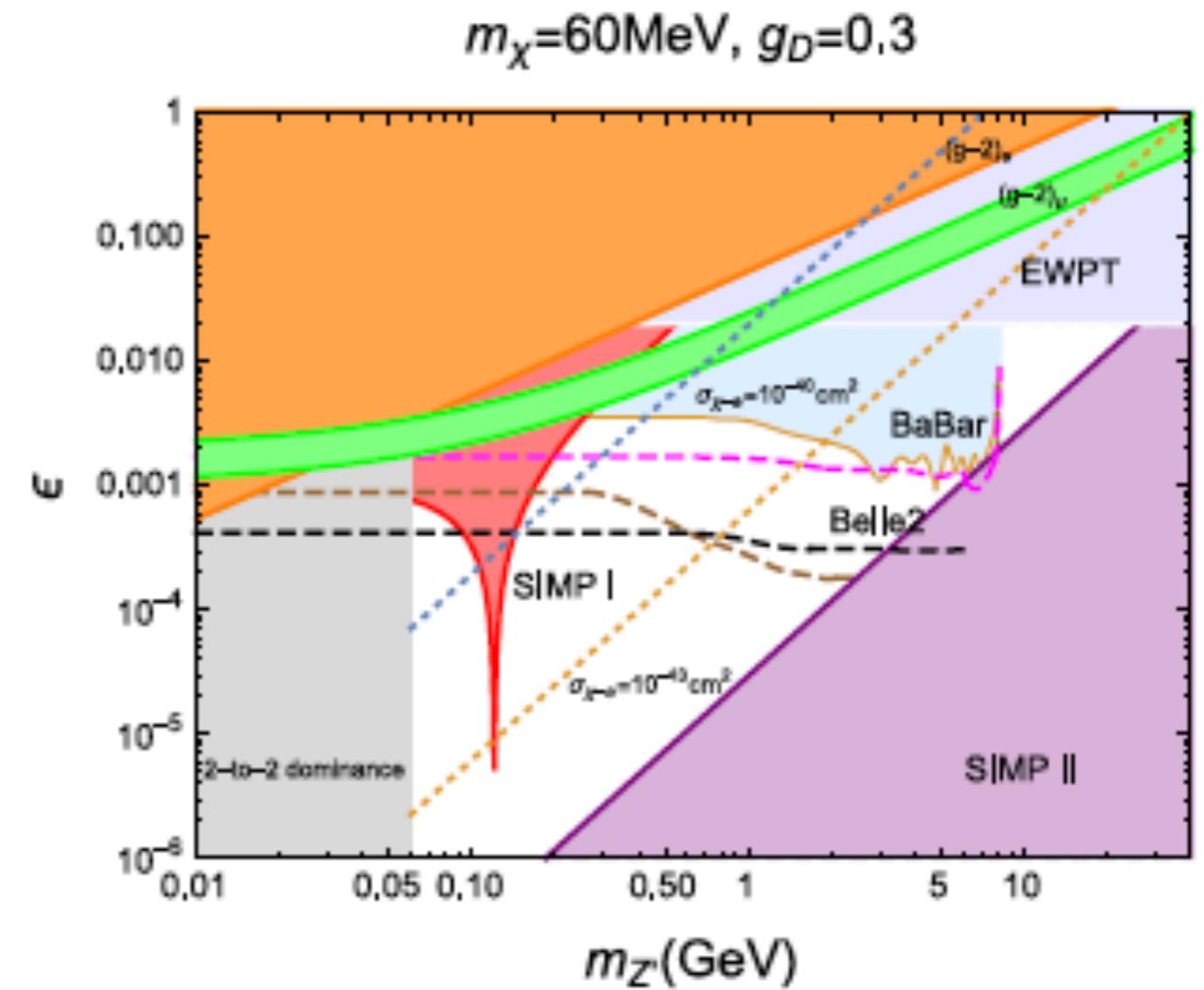
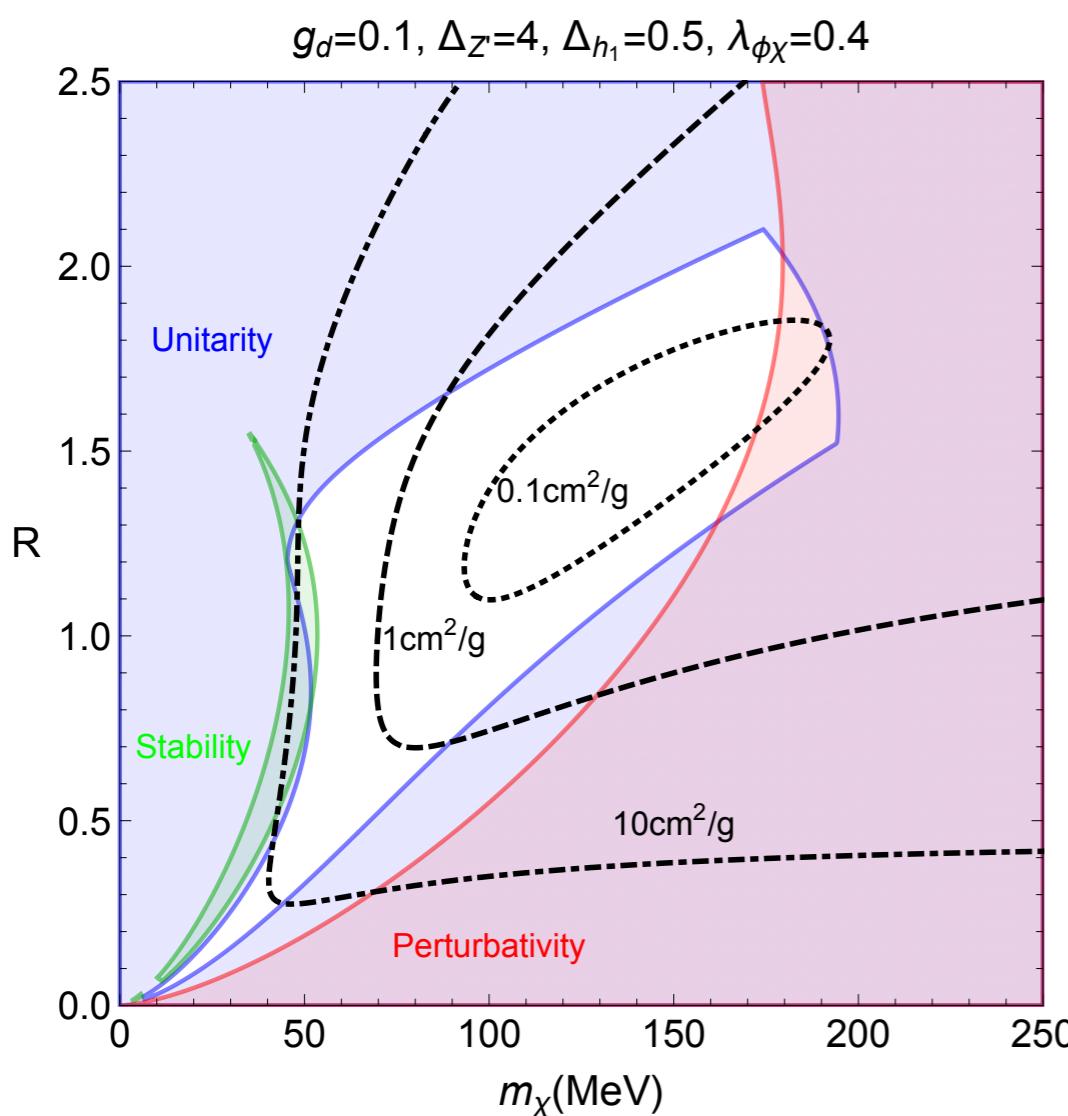


- Correlation btw self-scattering and $3 \rightarrow 2$ annihilation.

$$\sigma_{\text{self}} \sim \frac{\kappa^4}{m_\chi}, \quad \langle \sigma v^2 \rangle \sim \frac{\kappa^6}{m_\chi^5} \rightarrow \alpha_{\text{eff}} \sim \kappa^2$$

Bounds on SIMP

[S.-M. Choi, HML, 2015]

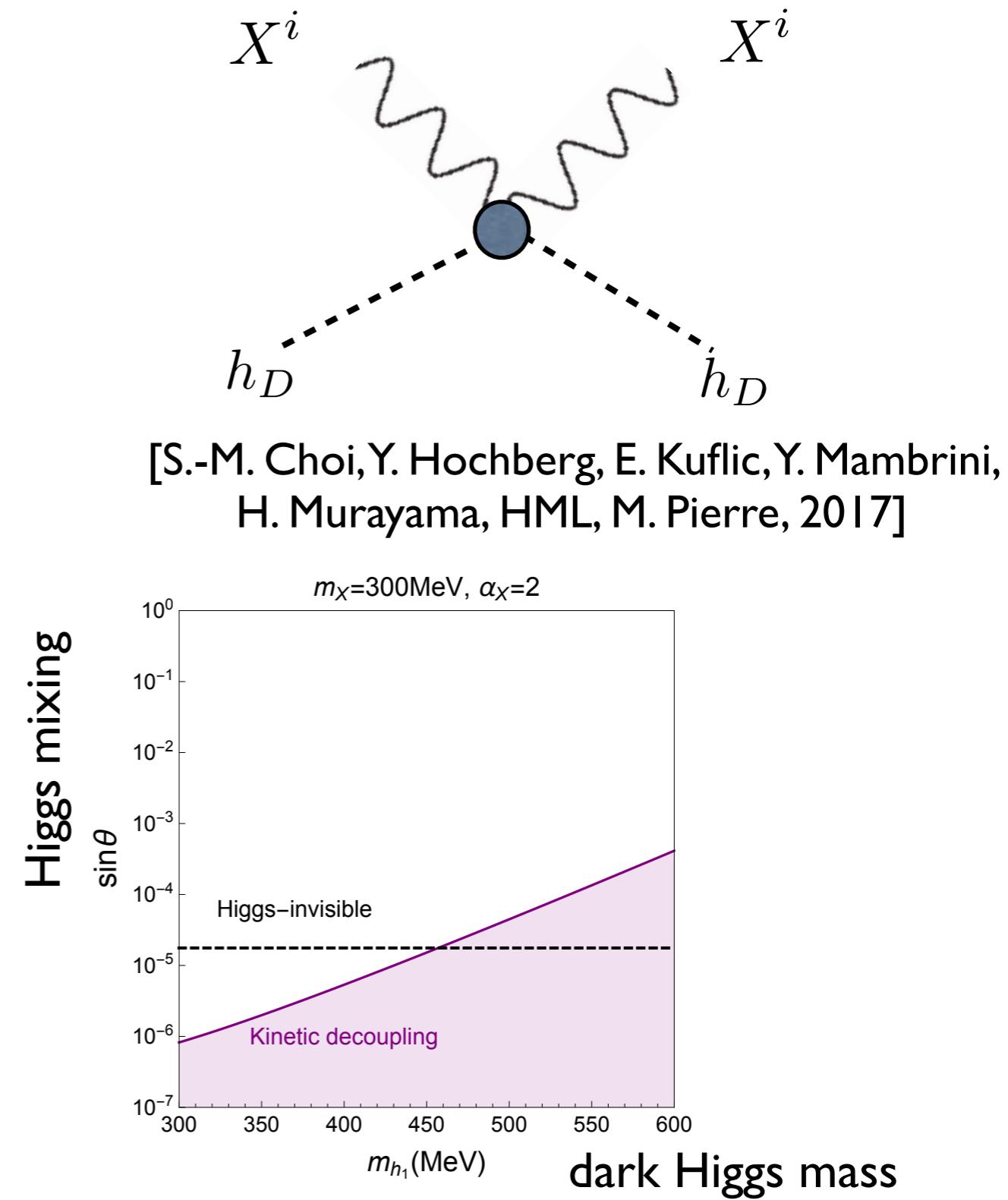
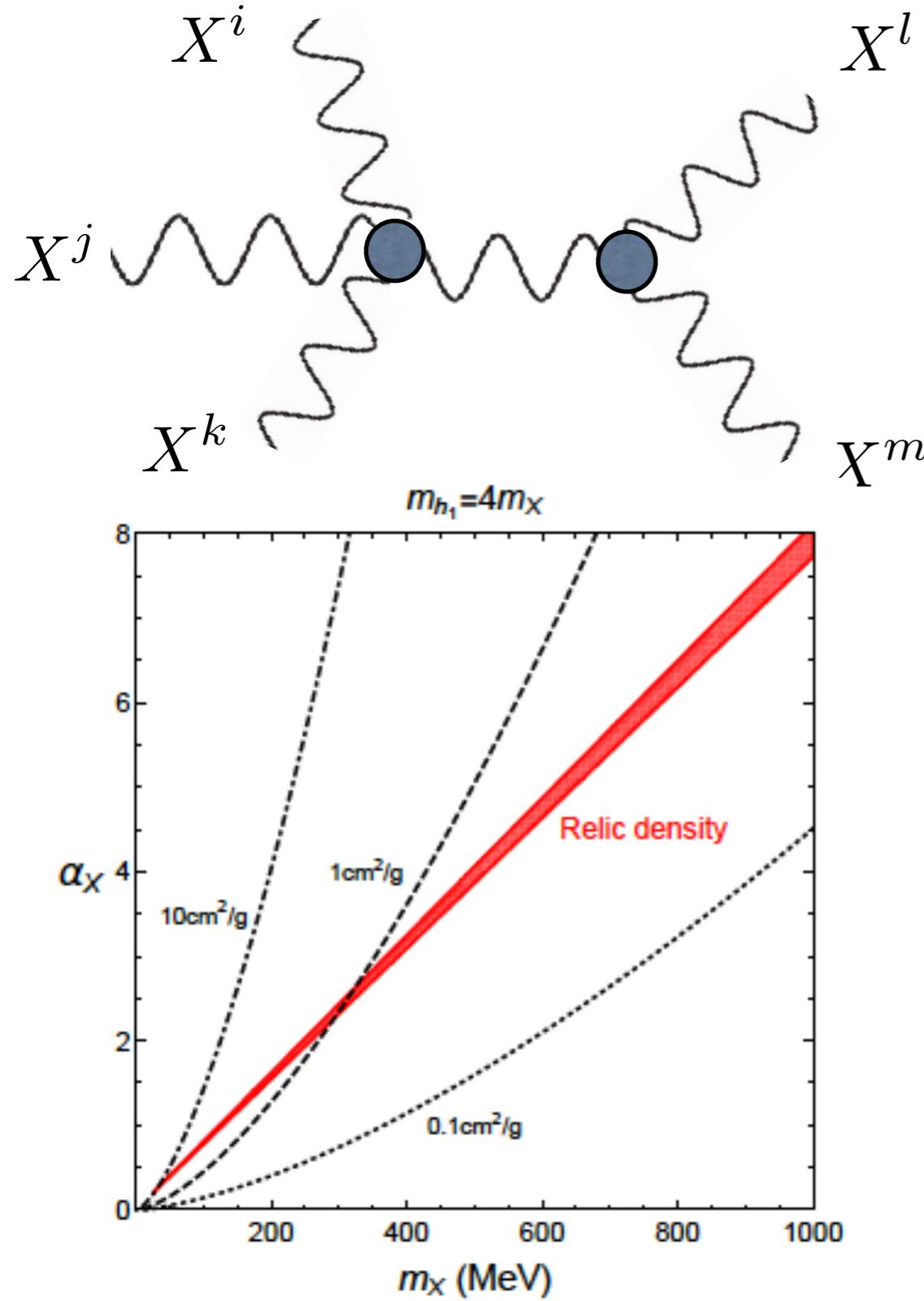


Consistent self-interactions
for relic density & small-
scale problems

Belle2, LHCb (Z' production),
Beam dump exp, Meson decays,
DM-electron scattering, etc.

Vector SIMP & Higgs portal

- Massive $SU(2)_X$ gauge bosons + dark Higgs

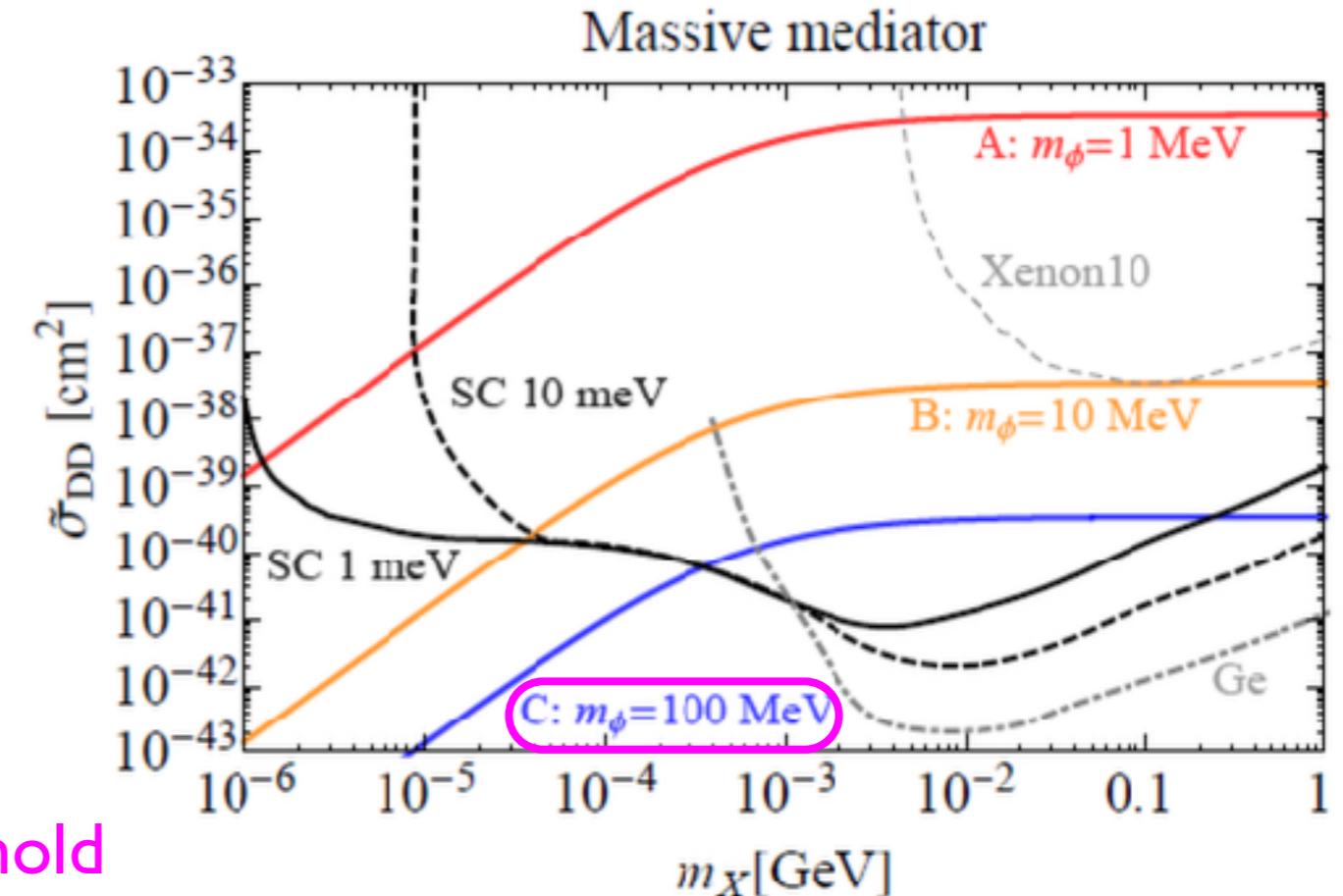
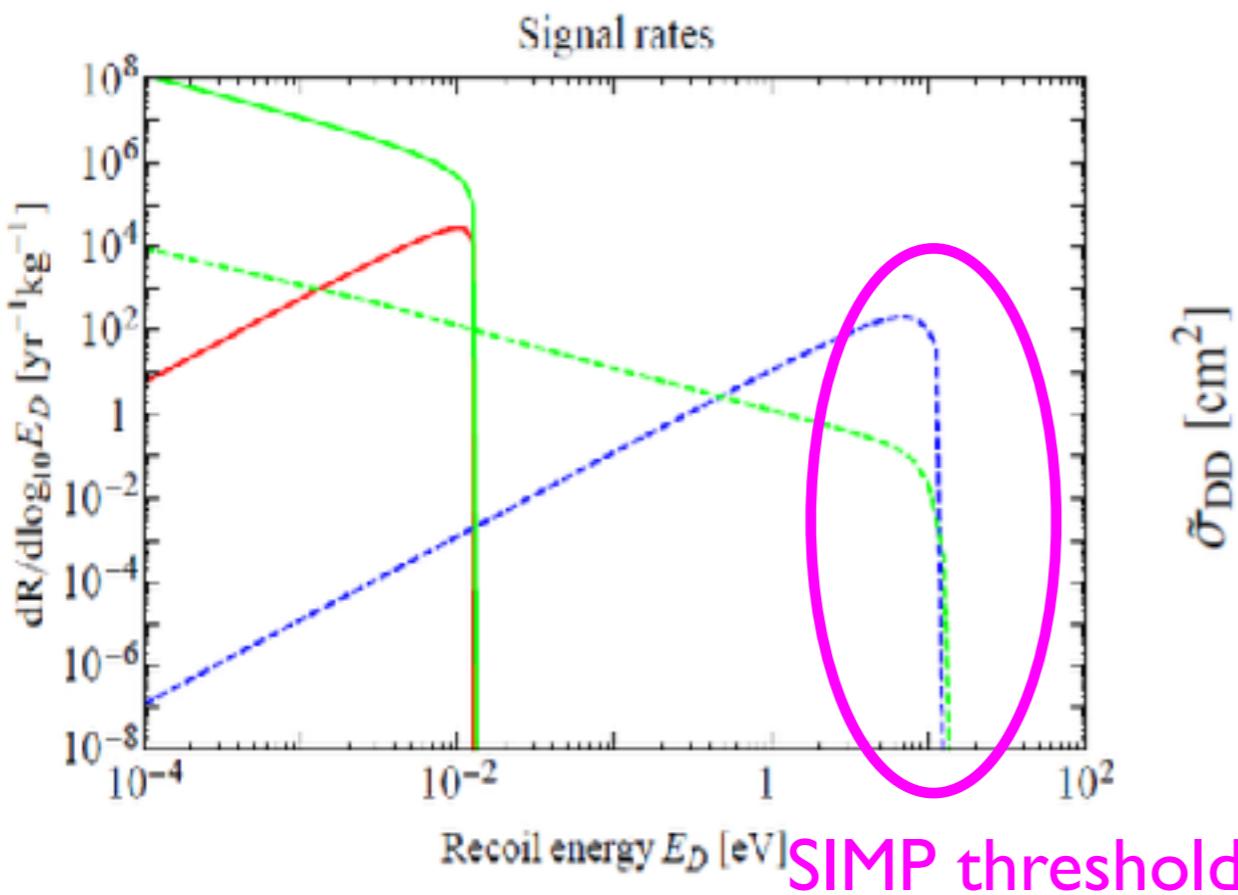
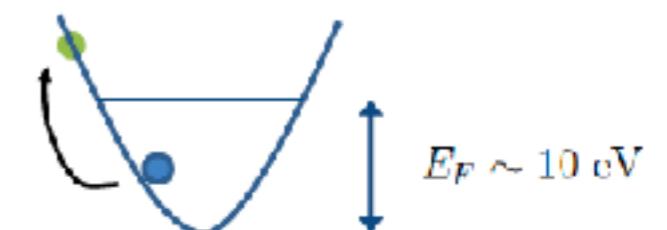


[S.-M. Choi, Y. Hochberg, E. Kuflic, Y. Mambrini,
H. Murayama, HML, M. Pierre, 2017]

SIMP direct detection

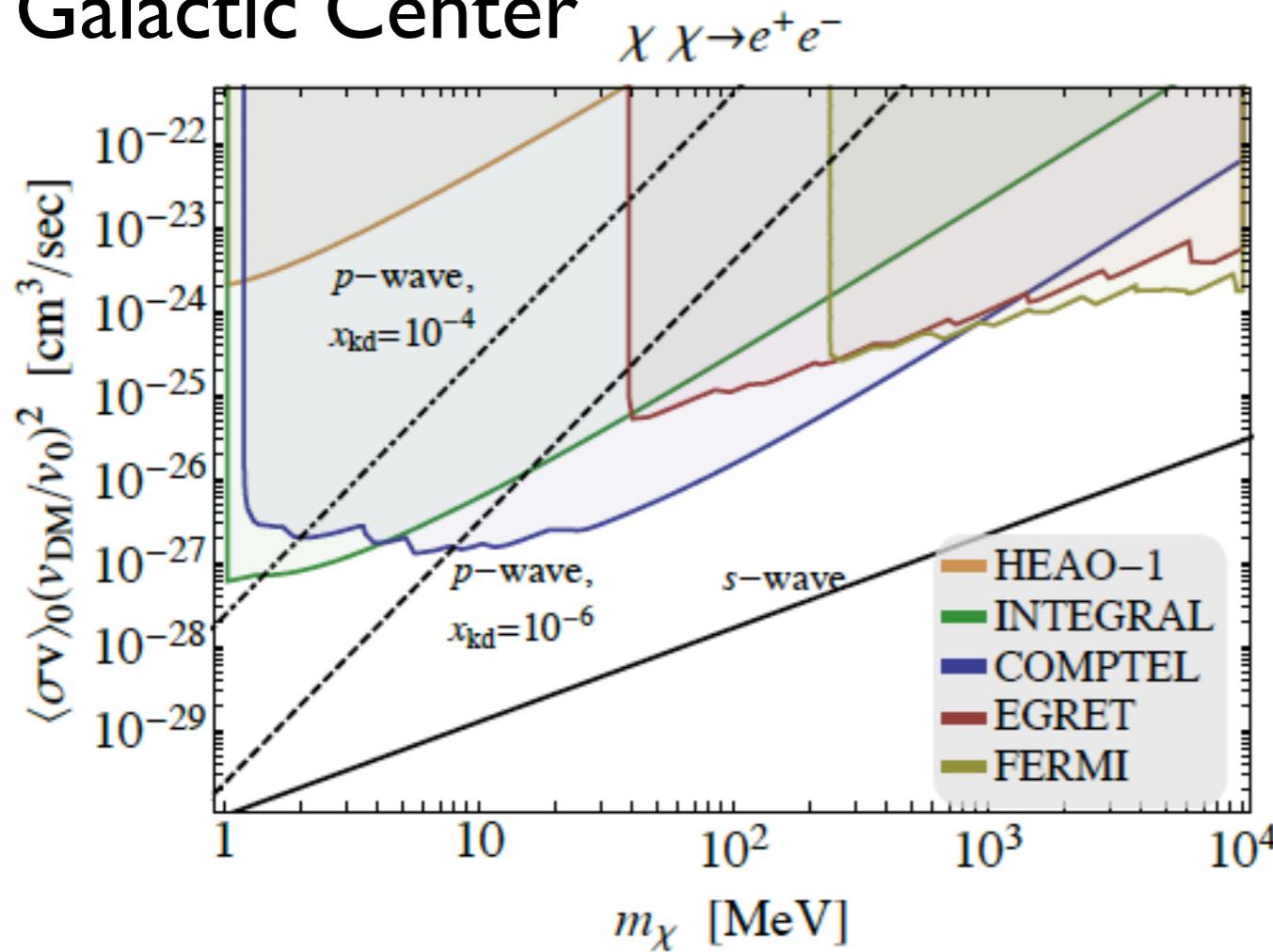
- DM-nucleon scattering: cryogenic semi-conductors
e.g. CDMSlite: Ge, $E_{\text{th}}=56\text{eV}$ $\rightarrow m_{\text{DM}} \gtrsim 1.6\text{ GeV}$
- DM-electron scattering: Cooper-pairs in super-conductors
e.g. Al: $E_F=11.7\text{eV}$, $v_{\text{rel}} \sim v_F = 10^{-2}$
 $\rightarrow m_{\text{DM}} \gtrsim m_e : E_R \lesssim 20\text{ eV}$
 $m_{\text{DM}} v^2 \gtrsim \Delta \sim \text{meV}$

[Hochberg et al (2015)]



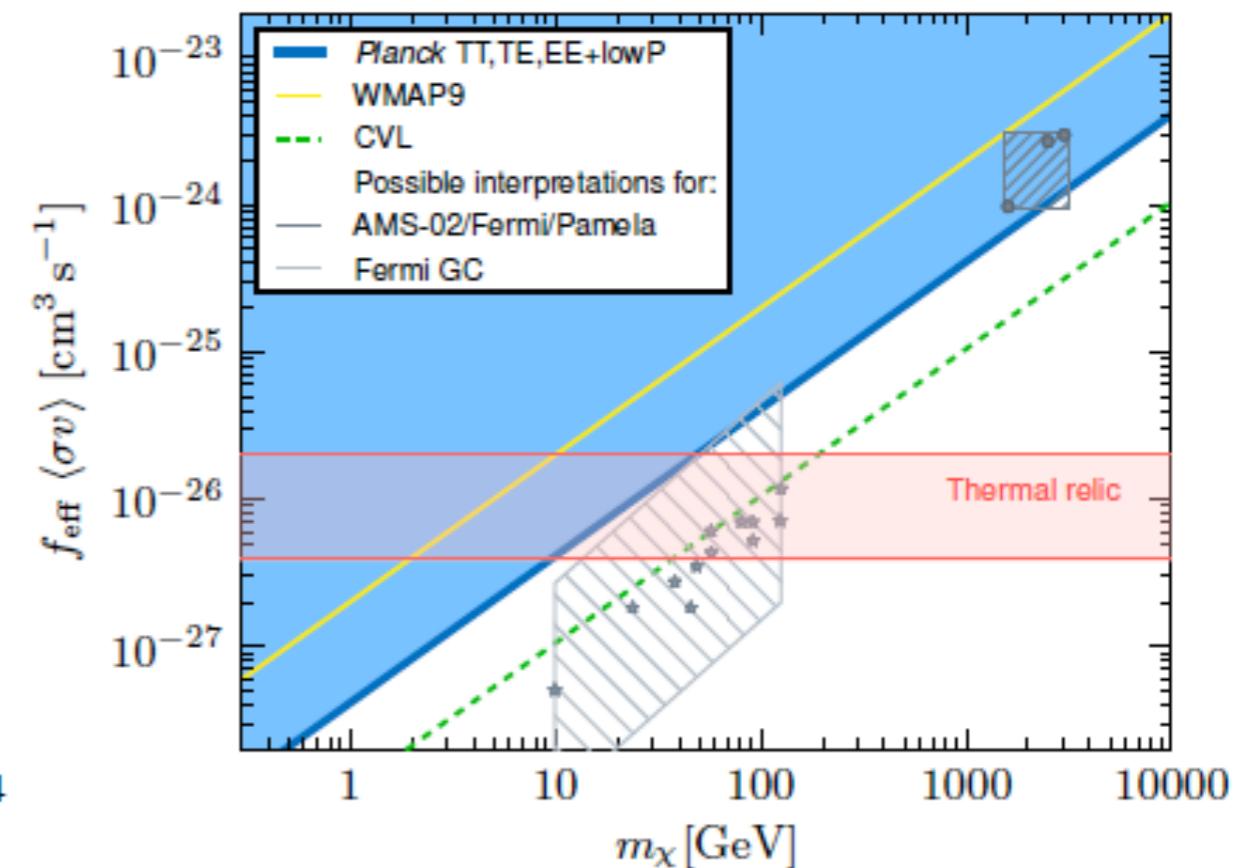
SIMP indirect detection

Galactic Center



[Essig et al, 2013]

CMB

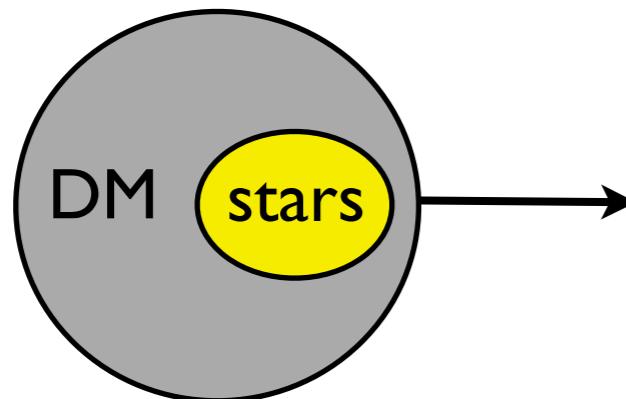


- Gamma-ray & CMB can constrain SIMP DM.
- No bound for scalar SIMP (p-wave suppressed annihilation).

$$\langle \sigma v_{\text{rel}} \rangle_{l+l^-} = \left(1.2 \times 10^{-27} \text{ cm}^3/\text{s} \right) \left(\frac{\varepsilon_2}{10^{-6}} \right)^2 \left(\frac{100 \text{ MeV}}{m_\pi} \right)^2, \quad \varepsilon_2(v) = \varepsilon_2(v_F)(v/v_F)$$

SIMP in merging galaxies

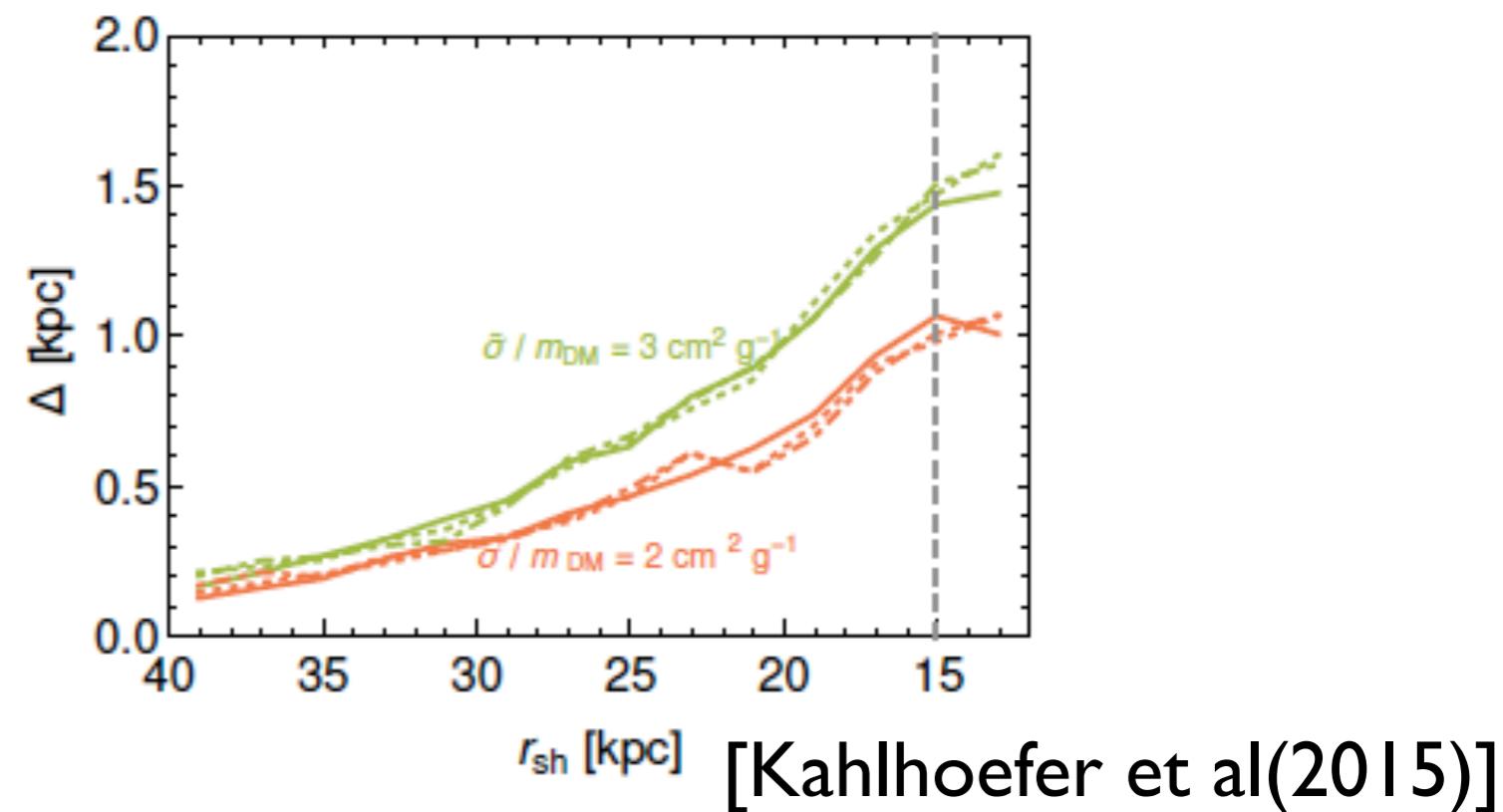
- SIMP self-interactions can make a separation of DM subhalo from bounded stars.



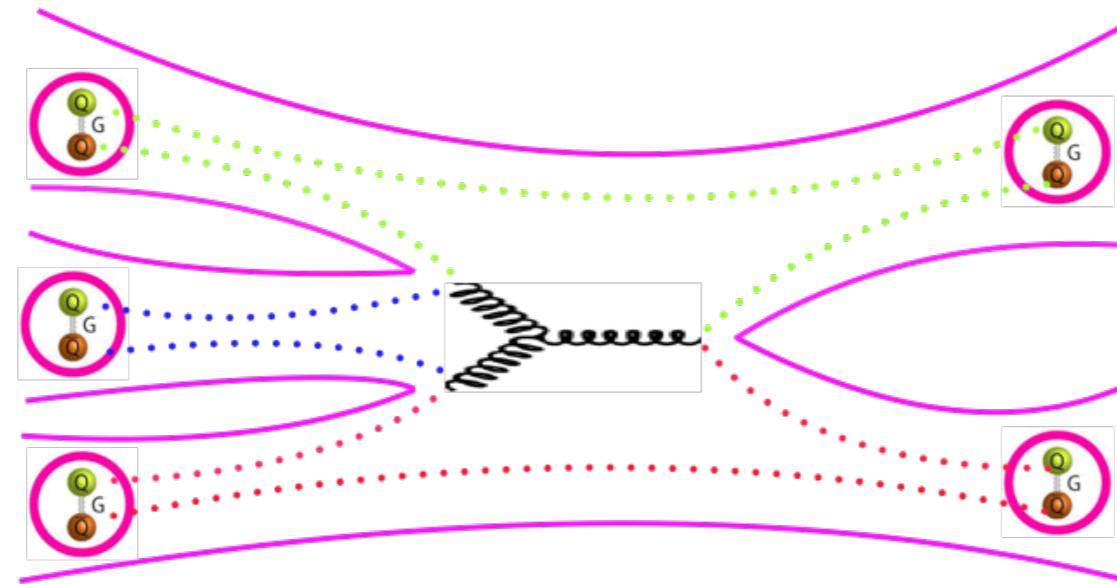
“Drag force” between DM subhalo and larger DM halo is greater than “gravity” between DM subhalo and star.

e.g. Abell 3827 cluster

$\Delta = 1.62^{+0.47}_{-0.49}$ kpc [Massey et al(2015)]



SIMP mesons



Dark QCD for naturalness

[Chacko,Goh,Harnik, 2005]

- Double the SM gauge groups with twin Higgs and matter.

$$[SU(3)_A \times SU(2)_A] \times [SU(3)_B \times SU(2)_B] \times Z_2$$

$$Z_2 : \quad g_A = g_B, \quad H_A \leftrightarrow H_B$$

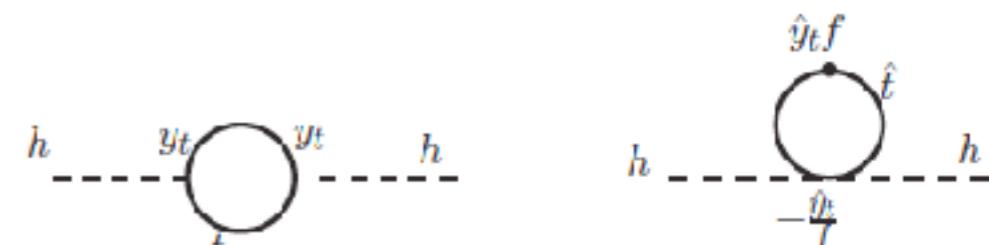
→ Higgs = pseudo-Goldstone bosons on $SU(4)/SU(3)$

- Quadratic divergences of Higgs mass are cancelled by neutral quarks at one-loop.

$$\mathcal{L}_Y = -y_A H_A q_A u_A^c - y_B H_B q_B u_B^c, \quad y_A = y_B.$$

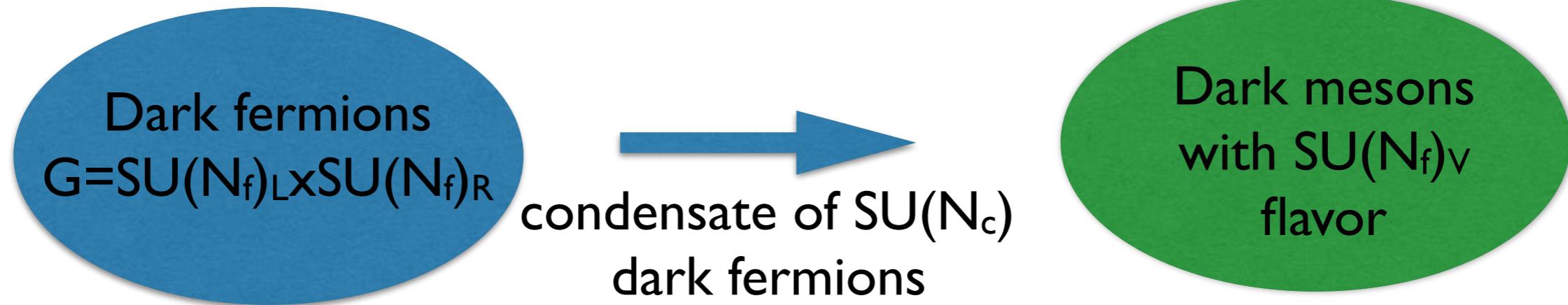
→ $\delta m_h^2 = \frac{3}{4\pi^2} (y_A^2 - y_B^2) \Lambda^2 = 0.$

“Dark QCD”



cf. General orbifold symmetries and QCD: HML, talk
at 2015 CERN TH workshop on neutral naturalness.

SIMPs from Dark QCD



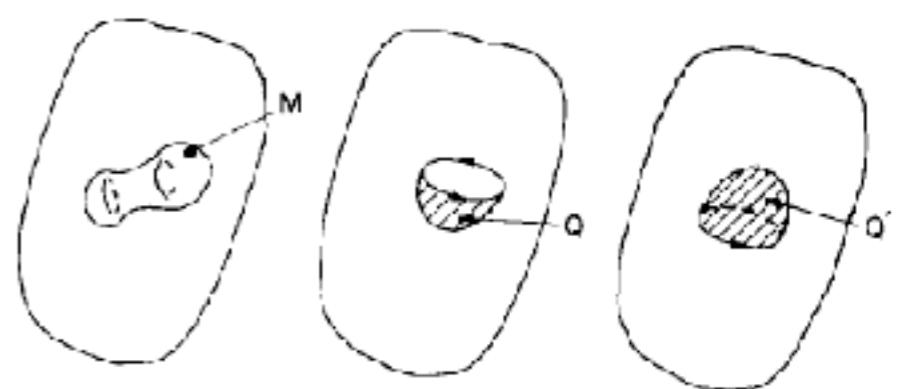
Dark mesons: Strongly Interacting, Light & Stable.

- 5-point self-interactions from **Wess-Zumino-Witten term** for $\pi_5(G/H)=\mathbb{Z}$ (i.e. $N_f \geq 3$). [Wess, Zumino, 1971; Witten, 1983]

$$U = e^{2i\pi/F}, \quad \pi \equiv \pi^a T^a$$

$$\mathcal{L}_{WZW} = \frac{2N_c}{15\pi^2} \epsilon^{\mu\nu\rho\sigma} \text{Tr}[\pi \partial_\mu \pi \partial_\nu \pi \partial_\rho \pi \partial_\sigma \pi]$$

$$N_f = 3 : \frac{\pi}{F} = \frac{\sqrt{2}}{F} \begin{bmatrix} \frac{1}{\sqrt{2}}\tilde{\pi}_0 + \frac{1}{\sqrt{6}}\tilde{\eta}^0 & \tilde{\pi}^+ & \tilde{K}^+ \\ \tilde{\pi}^- & -\frac{1}{\sqrt{2}}\tilde{\pi}_0 + \frac{1}{\sqrt{6}}\tilde{\eta}^0 & \tilde{K}^0 \\ \tilde{K}^- & \tilde{K}^- & -\sqrt{\frac{2}{3}}\tilde{\eta}^0 \end{bmatrix}.$$



N_c : topological invariant
of 5-sphere ($Q+Q'$) in $SU(3)$

WZW & SIMP process

- 5-point scattering vs self-scattering for SIMP mesons

SIMP process:

$$\langle \sigma v^2 \rangle_{3 \rightarrow 2} = \frac{5\sqrt{5}N_c^2 m_\pi^5}{2\pi^5 F^{10}} \frac{t^2}{N_\pi^3} \left(\frac{T_F}{m_\pi} \right)^2 \sim \frac{1}{N_f},$$

$$\Lambda'_{\text{QCD}} \sim \Lambda_{\text{QCD}}$$

Self-scattering:

$$\sigma_{\text{self}} = \frac{m_\pi^2}{32\pi F^4} \frac{a^2}{N_\pi^2} \sim \text{const}$$

$$m_{\tilde{\pi}}^2 \sim m_{\tilde{q}} \frac{(\Lambda'_{\text{QCD}})^3}{F^2} \sim (100 \text{ MeV})^2$$

cf. mirror QCD in twin Higgs models.

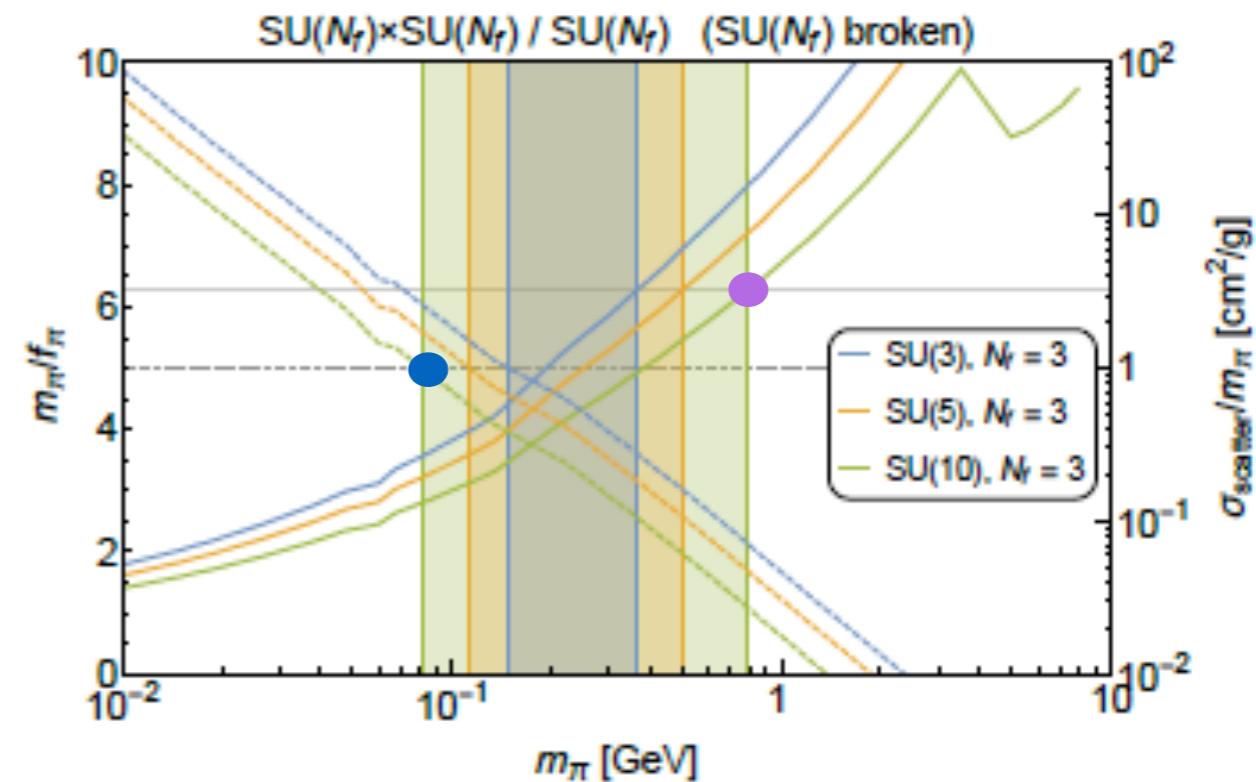
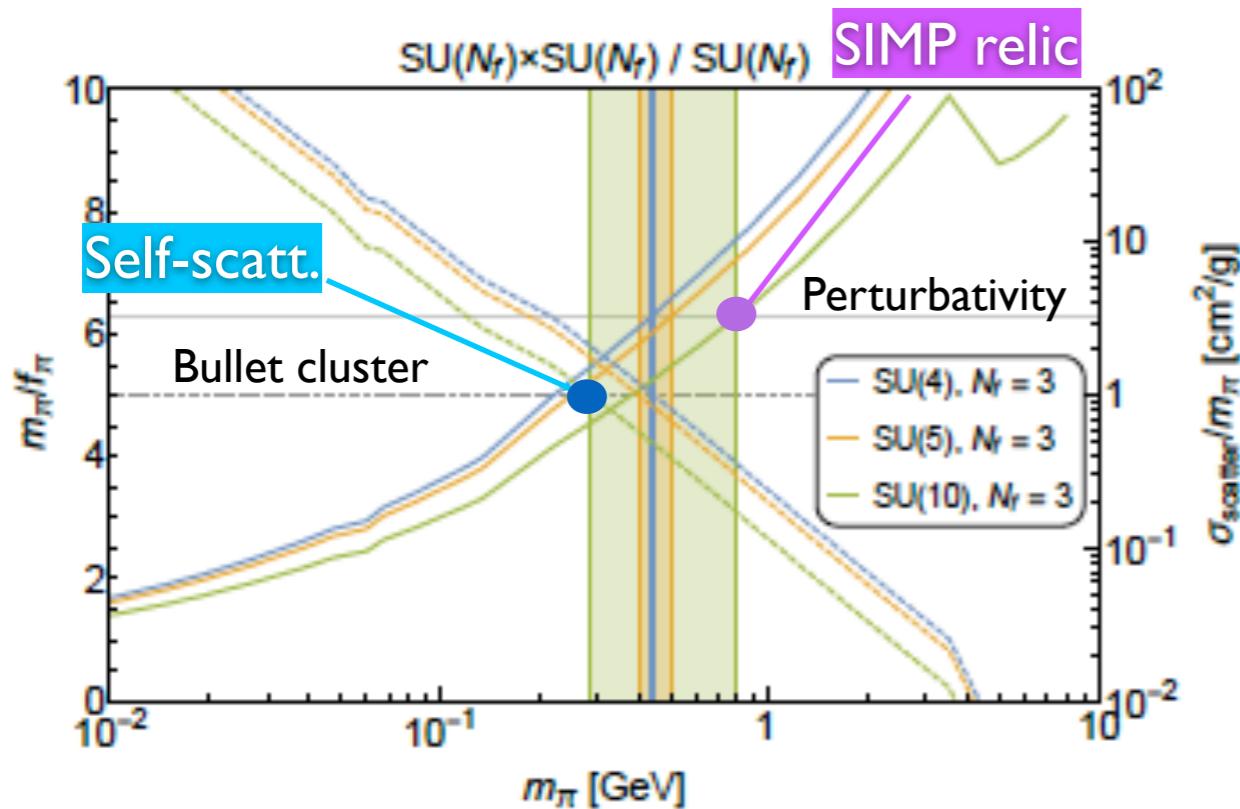
degenerate quark masses



flavor symmetry,
degenerate meson masses

[Hochberg et al, 2014]

Parameters for SIMP mesons



[Hochberg, Kuflik, Murayama, Volansky, Wacker, 2014]

Bullet cluster, Halo shape

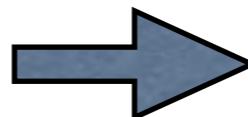
$$\sigma_{\text{self}}/m_{\text{DM}} < 1 \text{ cm}^2/\text{g}$$

Perturbativity

$$m_\pi/f_\pi < 2\pi$$

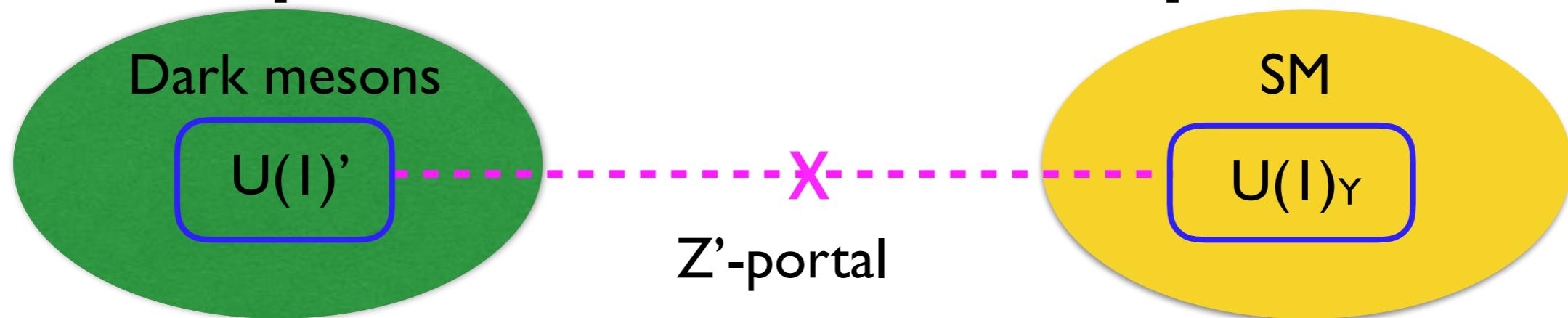
Bullet cluster & perturbativity bounds favor large N_c .

$N_c=3$ case is ruled out!



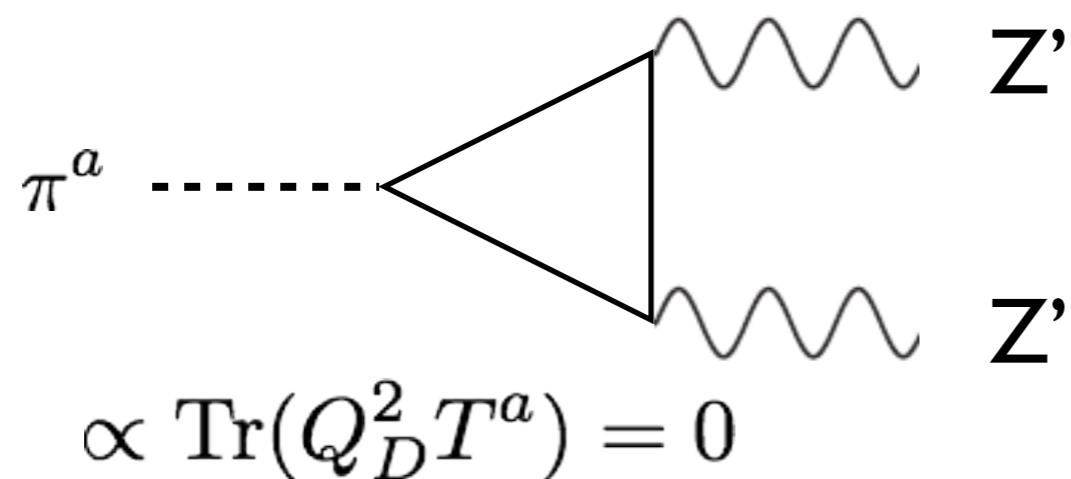
Vector mesons

Equilibrium via Z'-portal

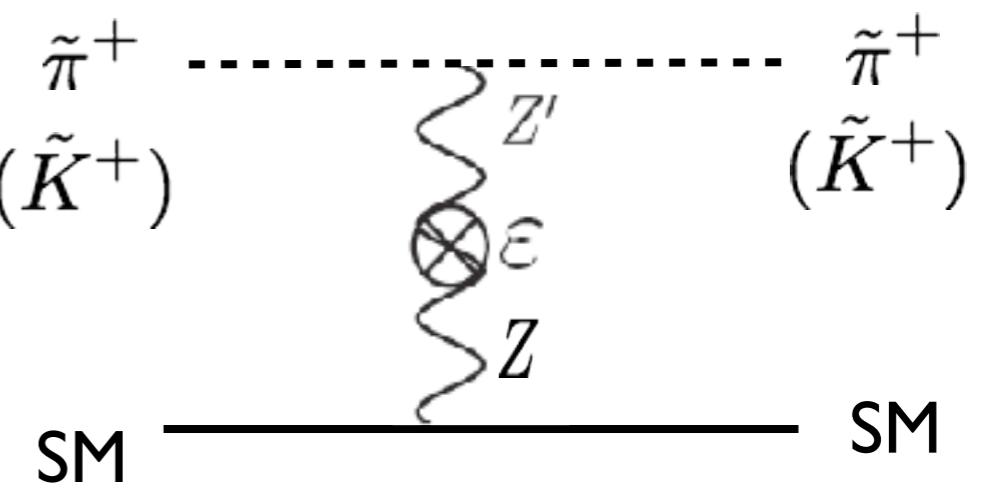


- Vectorial Z' with no chiral anomalies in dark QCD.

[HML, M. Seo, 2015]



$$\rightarrow Q_D = \begin{pmatrix} \frac{1}{3} & 0 & 0 \\ 0 & -\frac{1}{3} & 0 \\ 0 & 0 & -\frac{1}{3} \end{pmatrix}$$



$$\mathcal{L}_{\text{mix}} = -\frac{\varepsilon}{2 \cos \theta_W} F'_{\mu\nu} F^{\mu\nu}$$

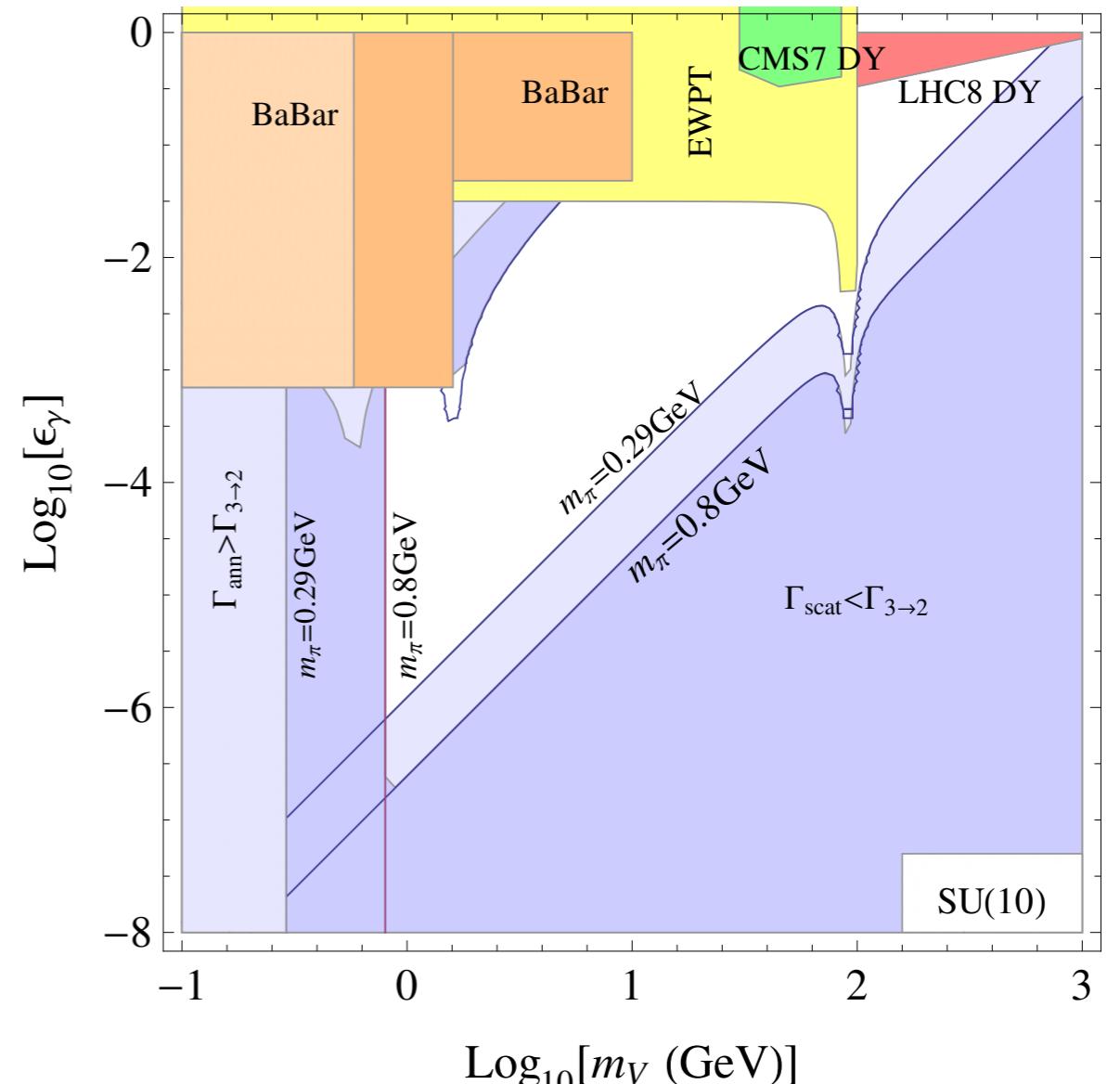
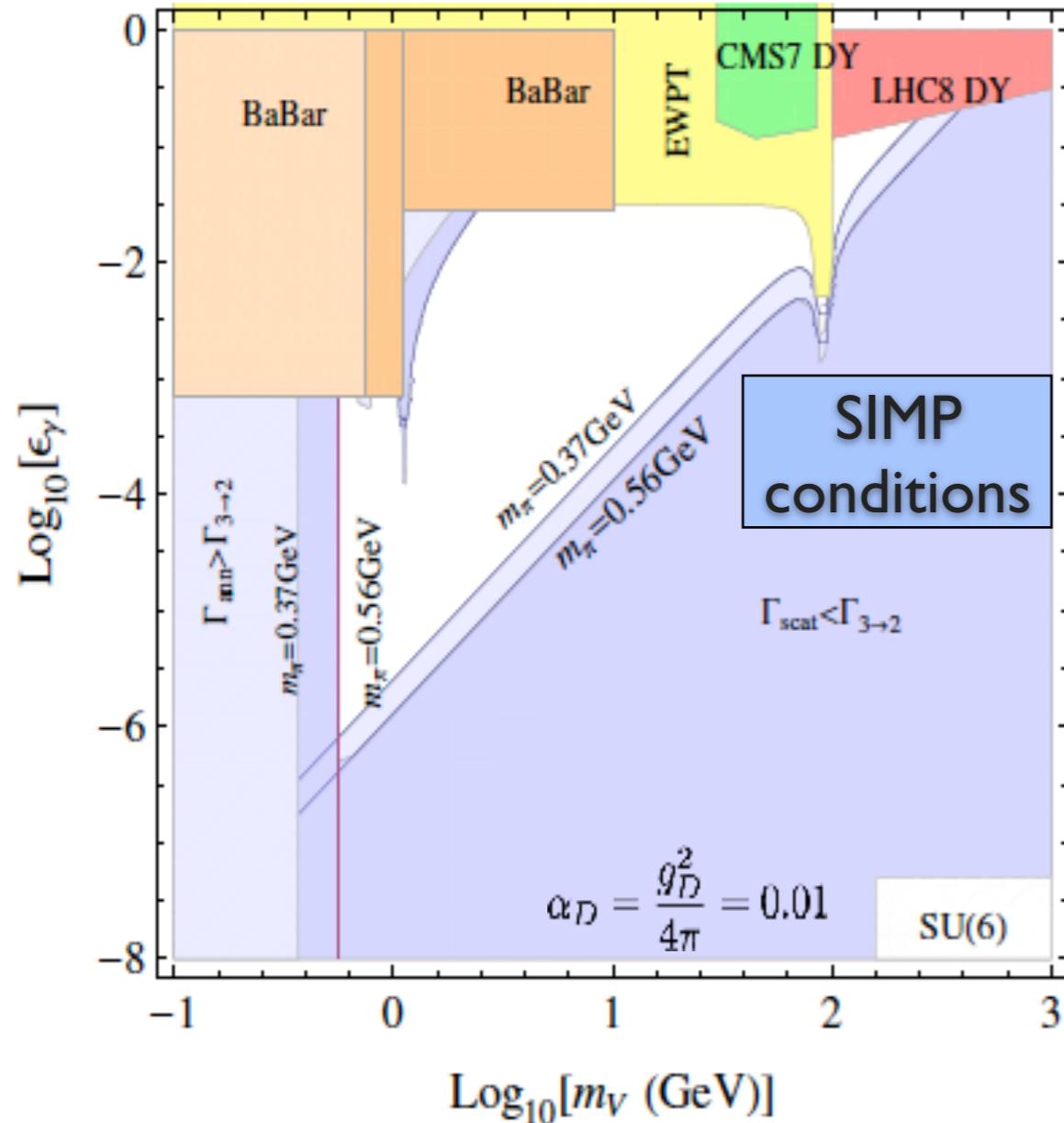
- Small meson mass splitting for SIMP process:

$$\delta \mathcal{L}_{m_\pi} = \alpha_D \Lambda^4 \text{Tr}[Q_D U Q_D U^{-1}]$$

$$\delta m_\pi^2 \sim \alpha_D \Lambda^4 / F^2 \lesssim 0.01 m_\pi^2,$$

Bounds on SIMP mesons

[M.-S. Seo, HML, 2015]



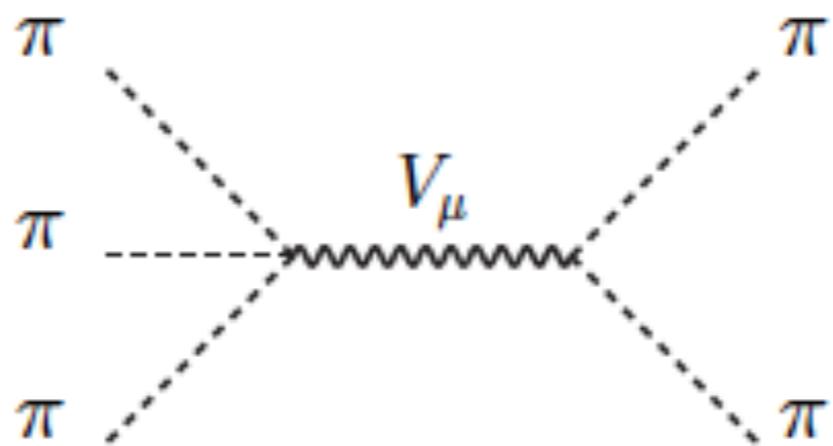
- SIMP parameter space can be probed by Z' searches.

$$e^+ e^- \rightarrow \gamma Z' \rightarrow \gamma(l^+ l^-), \quad e^+ e^- \rightarrow \gamma + \text{MET}$$

$h \rightarrow ZZ'$ (CMS 8TeV), Drell-Yan, dileptons.

cf. Hochberg et al, 2015

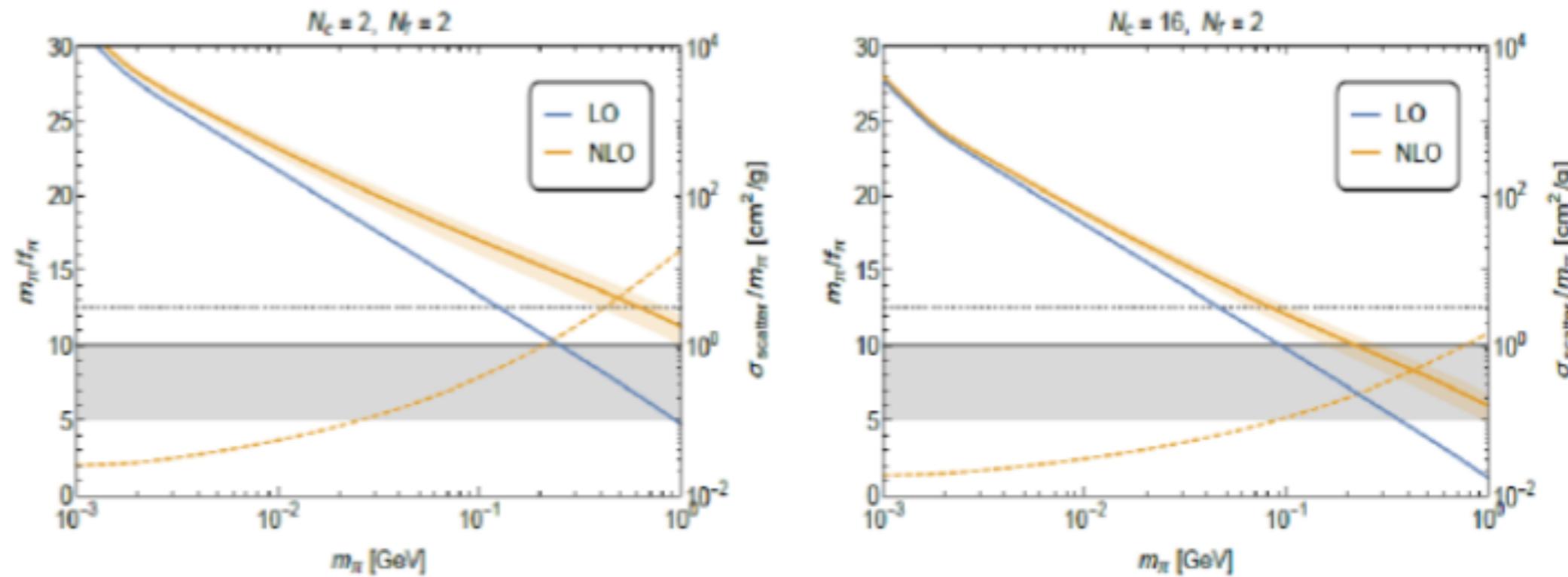
Resonant SIMPs



Perturbativity issue

[Hansen et al, 2015]

- 2→2: LO, 3→2: NLO, in SIMP scenarios.



NLO corrections enlarge 2→2 cross sections, making it harder to satisfy the self-scattering bound.

→ A larger color or a larger meson decay constant?
or additional 3→2 annihilation channels?

Resonant SIMPs

[S.-M.Chi, HML, 2016]

- Z_5 is a minimal (gauged) discrete symmetry for 5-point interacting SIMP.

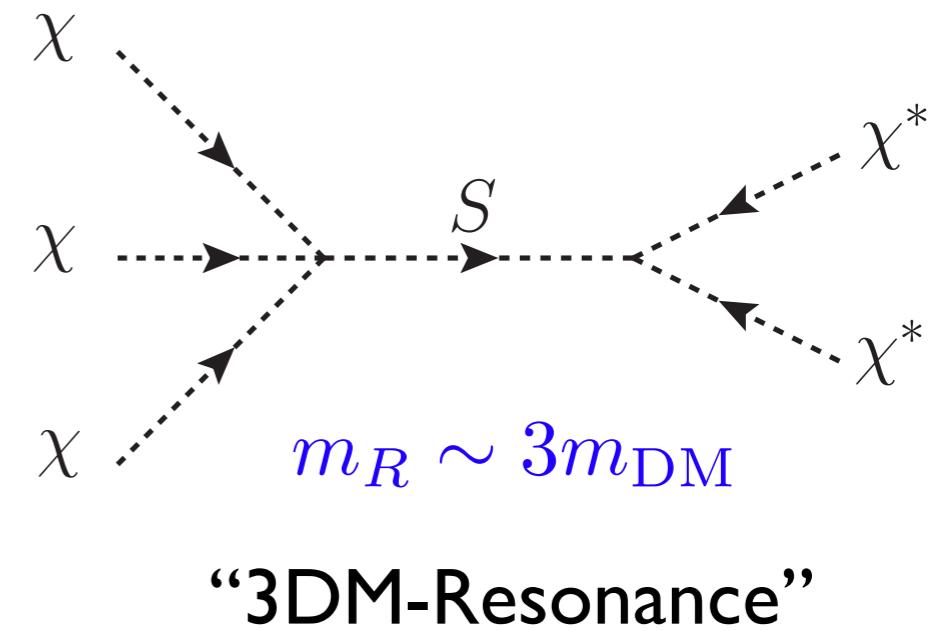
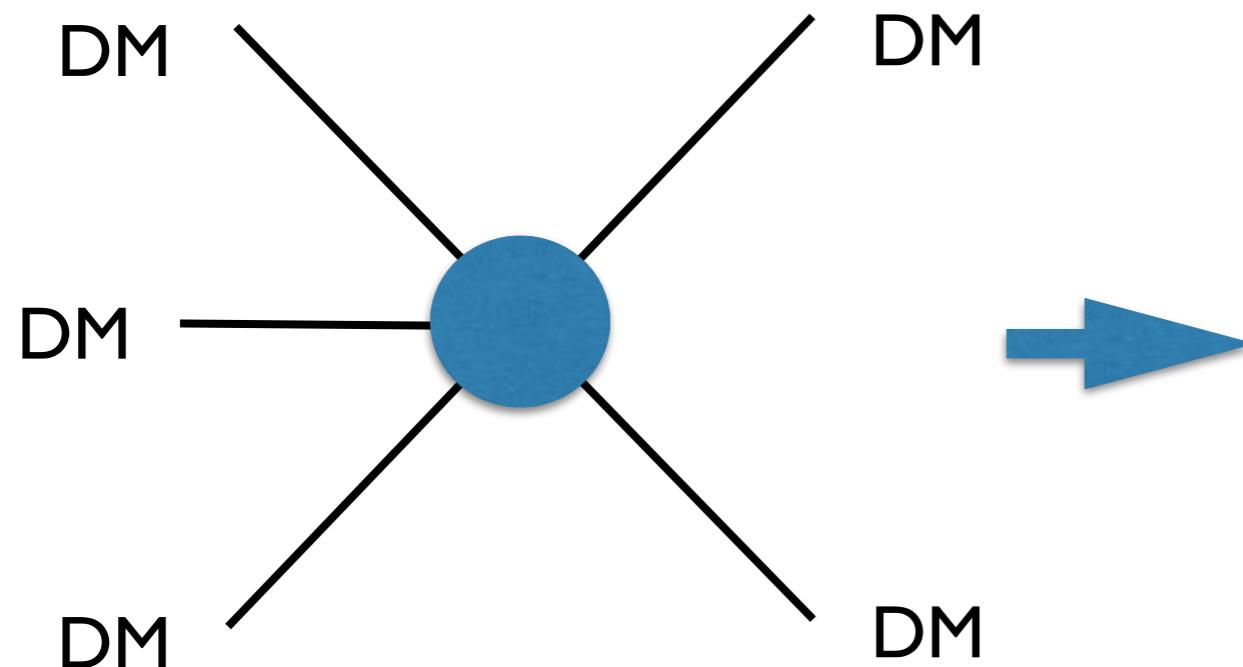
	ϕ	χ	S
$U(1)_V$	+5	+1	+3

$$\langle \phi \rangle = \frac{1}{2} v' \quad \rightarrow \quad U(1)_V \rightarrow Z_5$$

Table 1: $U(1)_V$ charges.

$$\begin{pmatrix} \phi \\ \chi \\ S \end{pmatrix} \rightarrow \begin{pmatrix} 1 & 0 & 0 \\ 0 & \omega & 0 \\ 0 & 0 & \omega^3 \end{pmatrix} \begin{pmatrix} \phi \\ \chi \\ S \end{pmatrix} \quad \omega = e^{i \frac{2}{5}\pi}$$

$$\mathcal{L}_{\text{int}} \supset \frac{1}{\sqrt{2}} \lambda_1 \phi^\dagger S^2 \chi^\dagger + \frac{1}{\sqrt{2}} \lambda_2 \phi^\dagger S \chi^2 + \frac{1}{6} \lambda_3 S^\dagger \chi^3 + \text{h.c.}$$



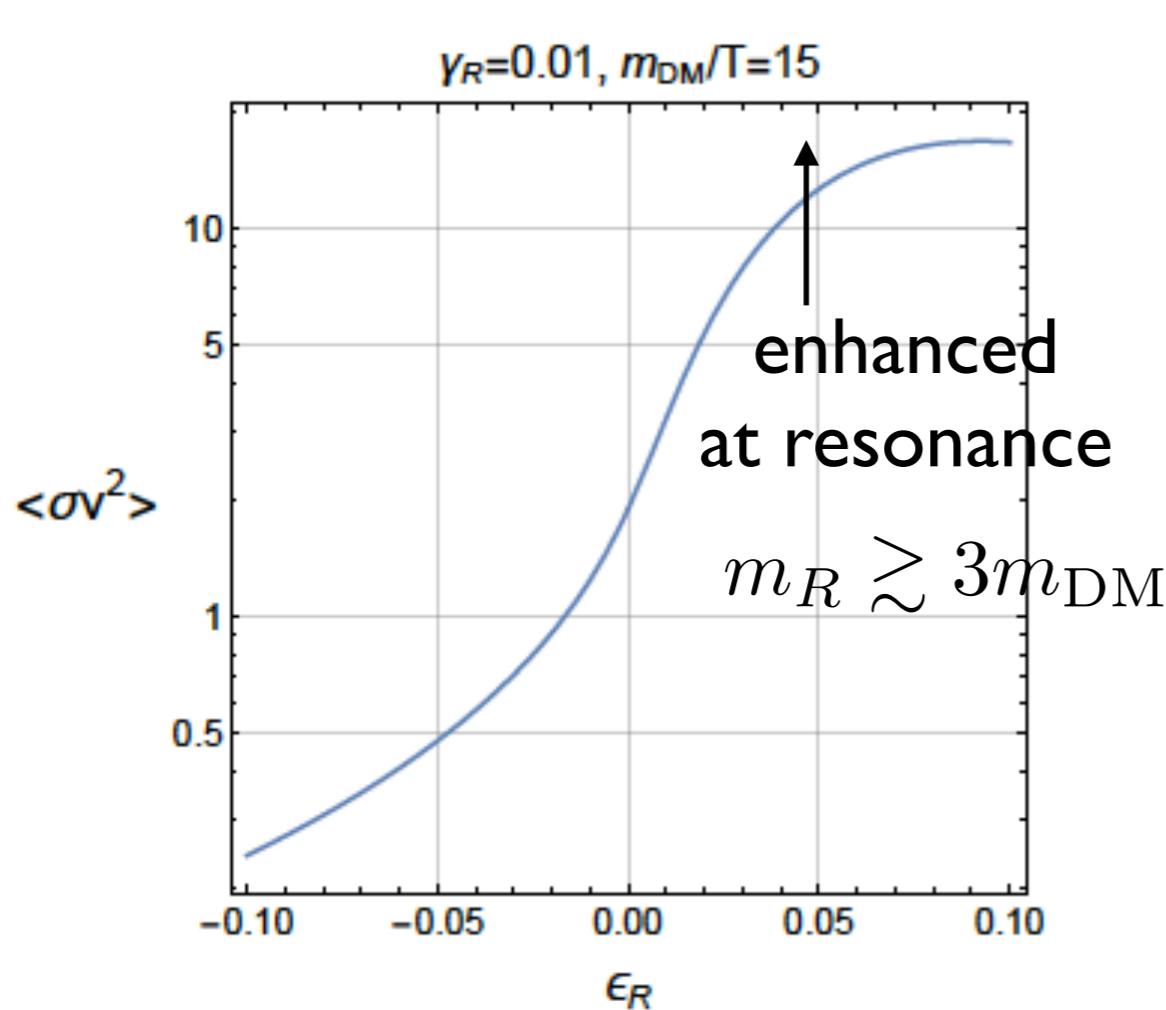
Averaging SIMPs

[S.-M. Choi, HML, M.-S. Seo, 2017]

- Thermal average of $3 \rightarrow 2$ cross section near resonances.

Breit-Wigner form for SIMP:

$$(\sigma v^2)_R = \frac{9\sqrt{5}}{2\beta_\chi \Phi_3 m_R^3} \frac{\gamma_R^2}{(\epsilon_R - \frac{2}{3}\eta)^2 + \gamma_R^2} \text{Br}(R \rightarrow \chi\chi\chi) \text{Br}(R \rightarrow \chi\chi) \equiv b_R \frac{\gamma_R}{(\epsilon_R - \frac{2}{3}\eta)^2 + \gamma_R^2}$$



$$b_R = \sum_{l=0}^{\infty} \frac{b_R^{(l)}}{l!} \eta^l \quad \gamma_R \equiv \frac{m_R \Gamma_R}{9m_{DM}^2} \quad \epsilon_R \equiv \frac{m_R^2 - 9m_{DM}^2}{9m_{DM}^2}$$

Thermal average with narrow width:

$$\gamma_R \ll 1, \quad \langle\sigma v^2\rangle_R \approx \frac{27}{16} \pi \epsilon_R^2 x^3 e^{-\frac{3}{2}x\epsilon_R} \theta(\epsilon_R) \sum_{l=0}^{\infty} \frac{b_R^{(l)}}{l!} \left(\frac{3}{2}\right)^l \epsilon_R^l.$$

3 DM's: higher dimensional phase space

cf. WIMP: $\langle\sigma v\rangle_R \approx 2\sqrt{\pi} \gamma_R \epsilon_R^{1/2} x^{3/2} e^{-x\epsilon_R} \theta(\epsilon_R) \sum_{l=0}^{\infty} \frac{b_l}{l!} \epsilon_R^l.$

Vector Mesons in dark ChPT

SIMP mesons + Vector mesons in dark QCD:

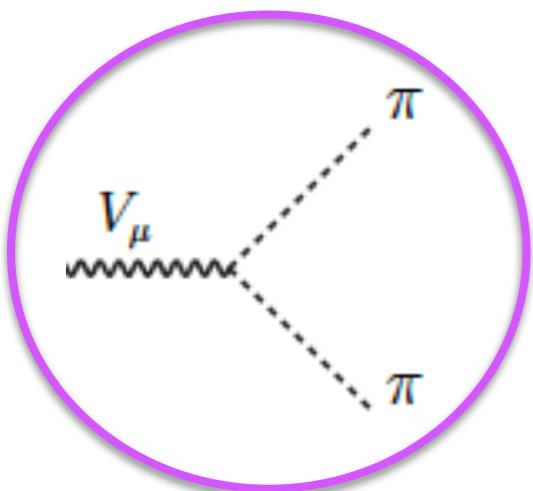
$$\boxed{G = SU(N_f) \vee \times SU(N_f)/SU(N_f) \vee \\ + H_{\text{local}} = SU(N_f) \vee \text{hidden local symmetry}}$$

→ $V_\mu \equiv V_\mu^a t^a = \frac{1}{\sqrt{2}} \begin{pmatrix} \frac{1}{\sqrt{2}}\rho_\mu^0 + \frac{1}{\sqrt{6}}\omega_{8\mu} + \frac{1}{\sqrt{3}}\omega_{0\mu} & \rho_\mu^+ & K_\mu^{*+} \\ \rho_\mu^- & -\frac{1}{\sqrt{2}}\rho_\mu^0 + \frac{1}{\sqrt{6}}\omega_{8\mu} + \frac{1}{\sqrt{3}}\omega_{0\mu} & K_\mu^{*0} \\ K_\mu^{*-} & \overline{K_\mu^{*0}} & -\frac{2}{\sqrt{6}}\omega_{8\mu} + \frac{1}{\sqrt{3}}\omega_{0\mu} \end{pmatrix}$

Extra chiral-invariant term (in unitary gauge):

$$\mathcal{L}_B = -a \frac{f_\pi^2}{4} \text{Tr} \left[(D_\mu \xi_L) \xi_L^\dagger + D_\mu \xi_R) \xi_R^\dagger \right]^2 \quad \xi_L^\dagger(x) = \xi_R(x) = \exp[i\pi(x)/f_\pi]$$

→ $\mathcal{L}_B = m_V^2 \text{Tr} V_\mu V^\mu - 2ig_{V\pi\pi} \text{Tr} (V_\mu [\partial^\mu \pi, \pi]) - \frac{a}{4f_\pi^2} \text{Tr} ([\pi, \partial_\mu \pi]^2)$



VM masses: $m_V^2 = ag^2 f_\pi^2$ degenerate
 VM-pion couplings: $g_{V\pi\pi} = \frac{1}{2}ag$. cf. QCD: $a \simeq 2$

WZW with vector mesons

WZW terms gauged by $H_{\text{local}} = \text{SU}(N_f)v$

$$\Gamma^{anom} = \int d^4x [\mathcal{L}_{WZW} - 15(c_1 \mathcal{L}_1 + c_2 \mathcal{L}_2 + c_3 \mathcal{L}_3)]$$

$$\mathcal{L}_1 = \text{Tr} [\hat{\alpha}_L^3 \hat{\alpha}_R - \hat{\alpha}_R^3 \hat{\alpha}_L] \quad \hat{\alpha}_L = D\xi_L \cdot \xi_L^\dagger = \alpha_L - igV \cdot$$

$$\mathcal{L}_2 = \text{Tr} [\hat{\alpha}_L \hat{\alpha}_R \hat{\alpha}_L \hat{\alpha}_R] \quad \hat{\alpha}_R = D\xi_R \cdot \xi_R^\dagger = \alpha_R - igV$$

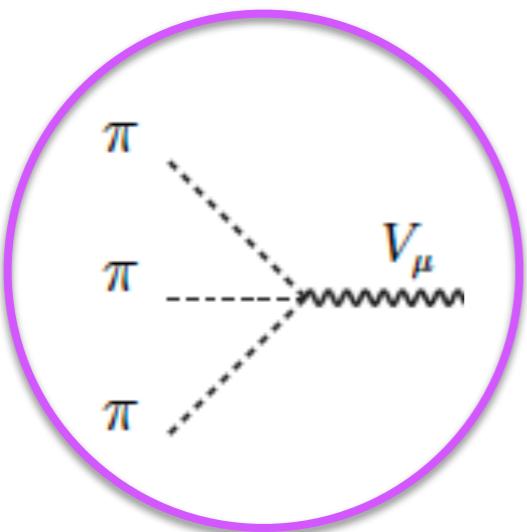
$$\mathcal{L}_3 = i\text{Tr} [F_V (\hat{\alpha}_L \hat{\alpha}_R - \hat{\alpha}_R \hat{\alpha}_L)] \quad F_V = dV - igV^2$$



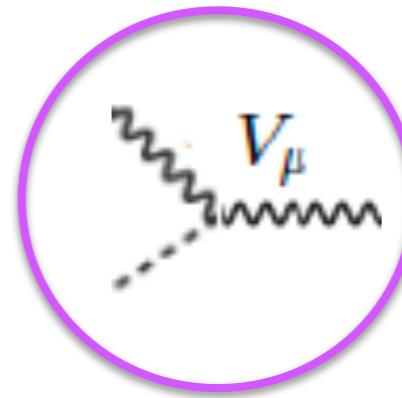
$$\mathcal{L}_1 = -\mathcal{L}_2 = -\frac{4gC}{f_\pi^3} \text{Tr}[V_\mu \partial_\mu \pi \partial_\rho \pi \partial_\sigma \pi],$$

$$\mathcal{L}_3 = -\frac{2igC}{f_\pi} \text{Tr}[\partial_\mu V_\nu (V_\rho \partial_\sigma \pi - \partial_\rho \pi V_\sigma)].$$

$$C = -\frac{iN_c}{240\pi^2}$$



cf. QCD:
 $\omega \rightarrow 3\pi$



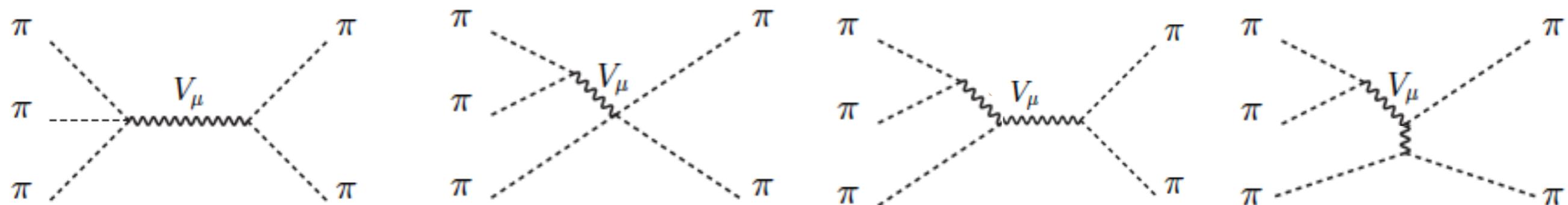
cf. QCD: VM-
 photon mixing
 $\pi^0 \rightarrow 2\gamma$

Dark photon case:
 Berlin et al, 2018

Vector Meson resonances

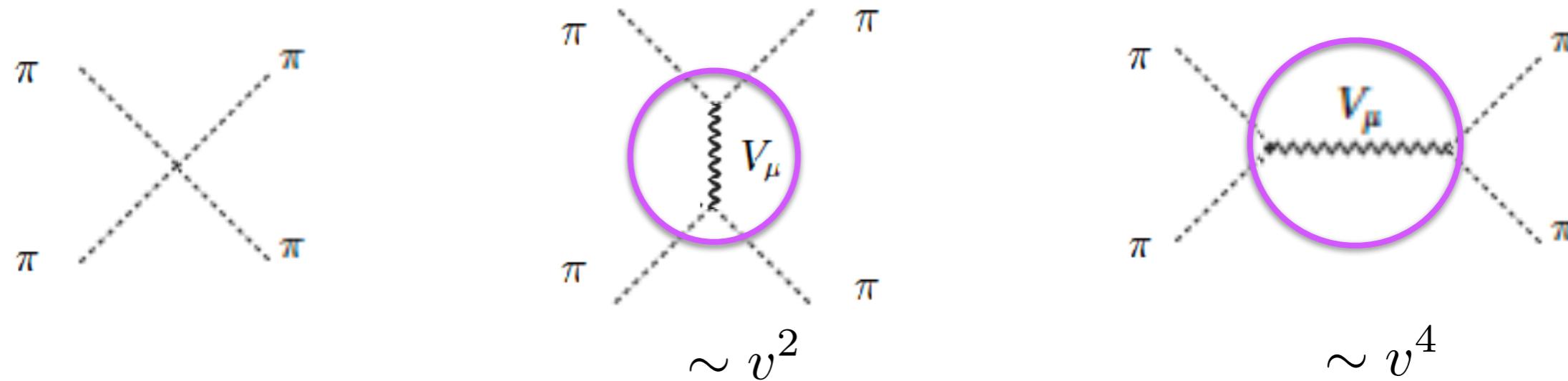
3→2 annihilation:

[S.-Choi,A. Natale, HML, P.Ko, 2018]



→ Enhanced near resonances with 2π or 3π .

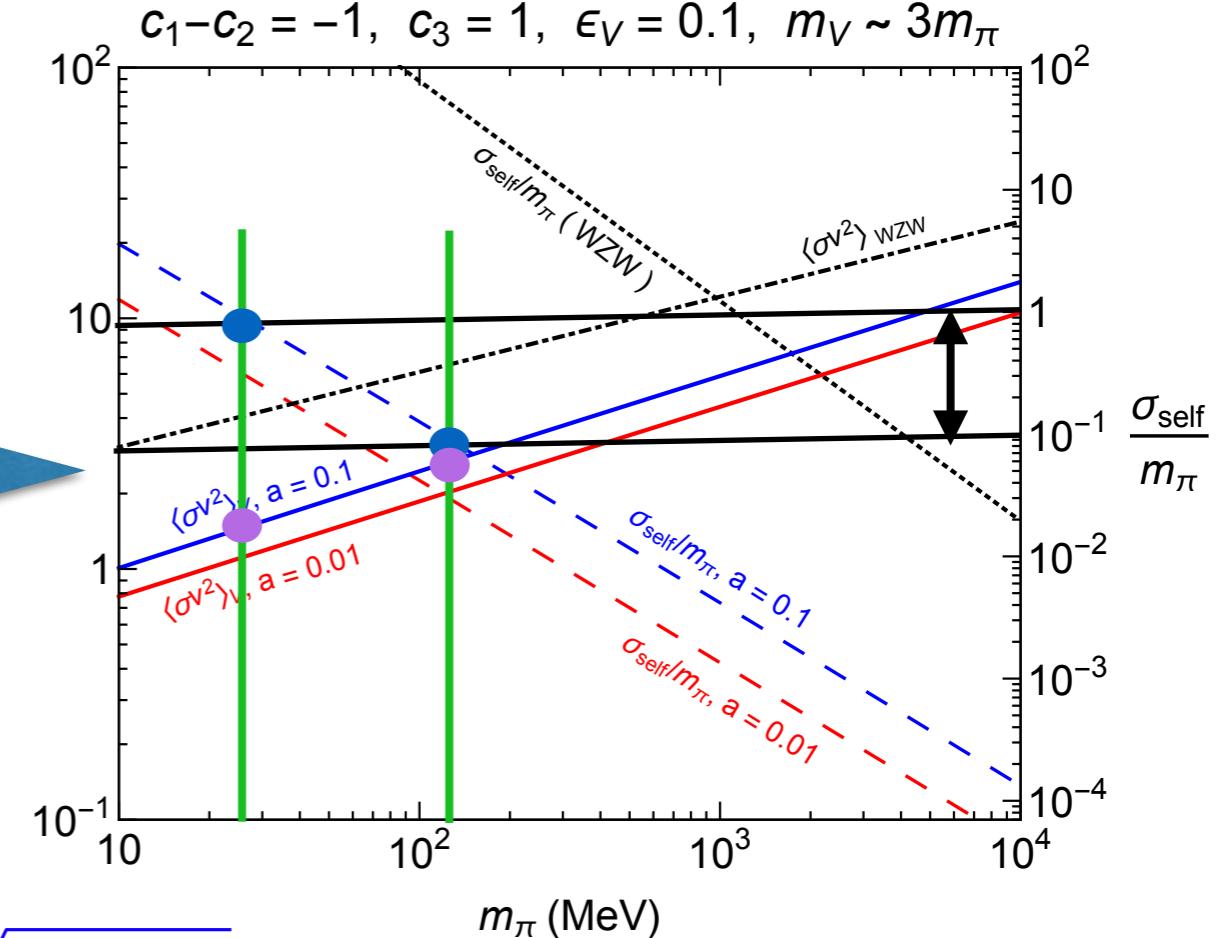
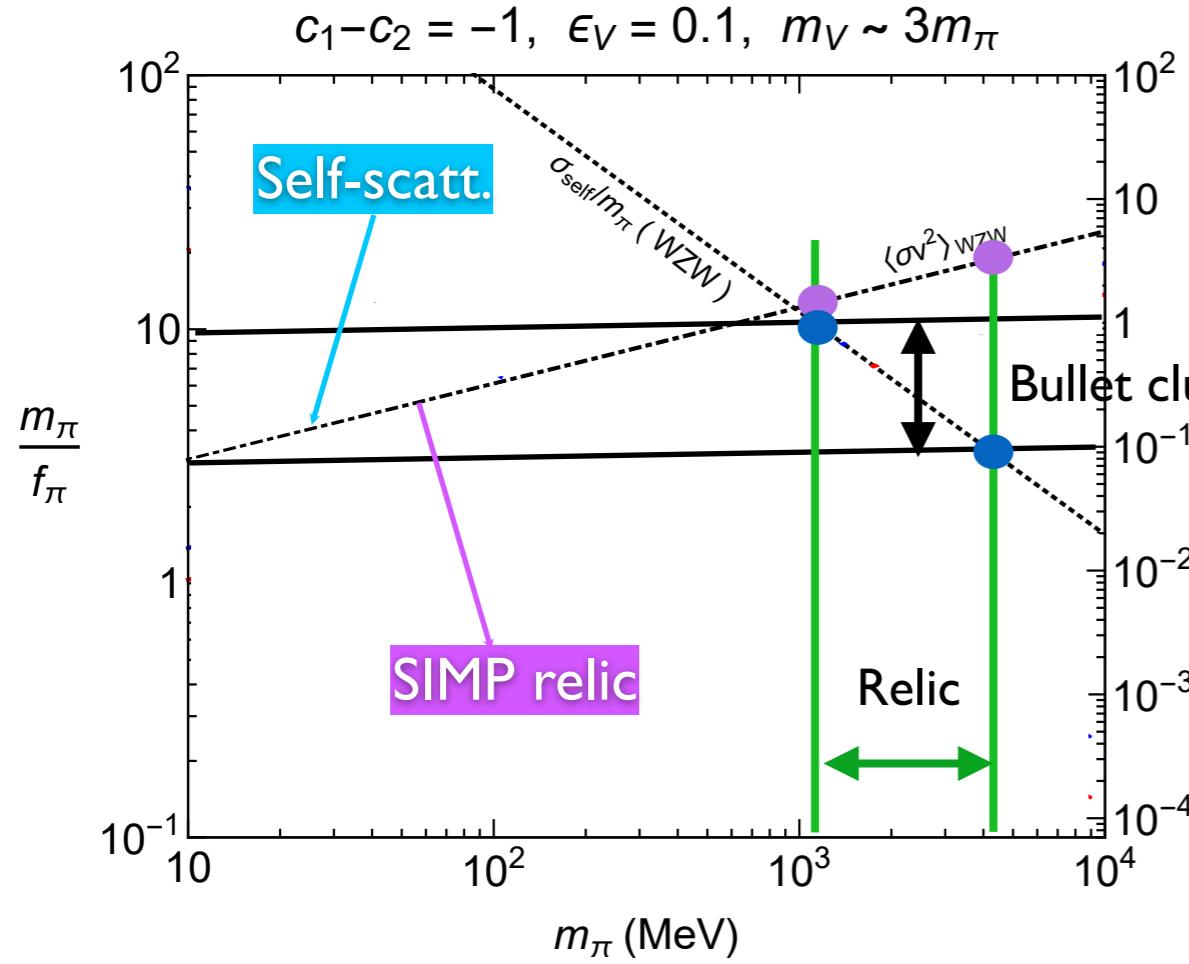
2→2 self-scattering:



→ VM resonance is velocity-suppressed at galaxies and galaxy clusters.

3-meson resonance

[S.-Choi, A. Natale, HML, P. Ko, 2018]



$$m_V = 3m_\pi \sqrt{1 + \epsilon_V}$$

Vector mesons on-resonance improve perturbativity.

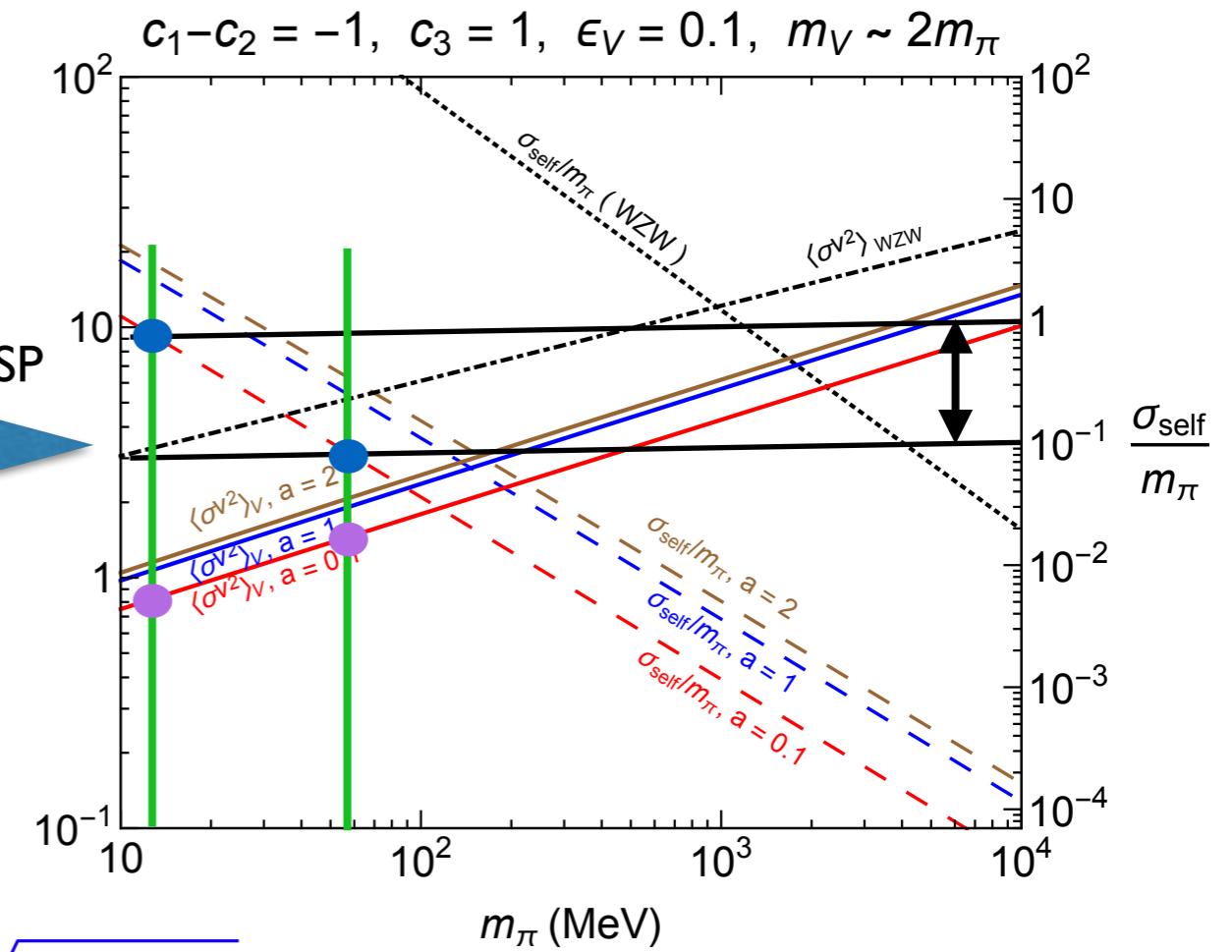
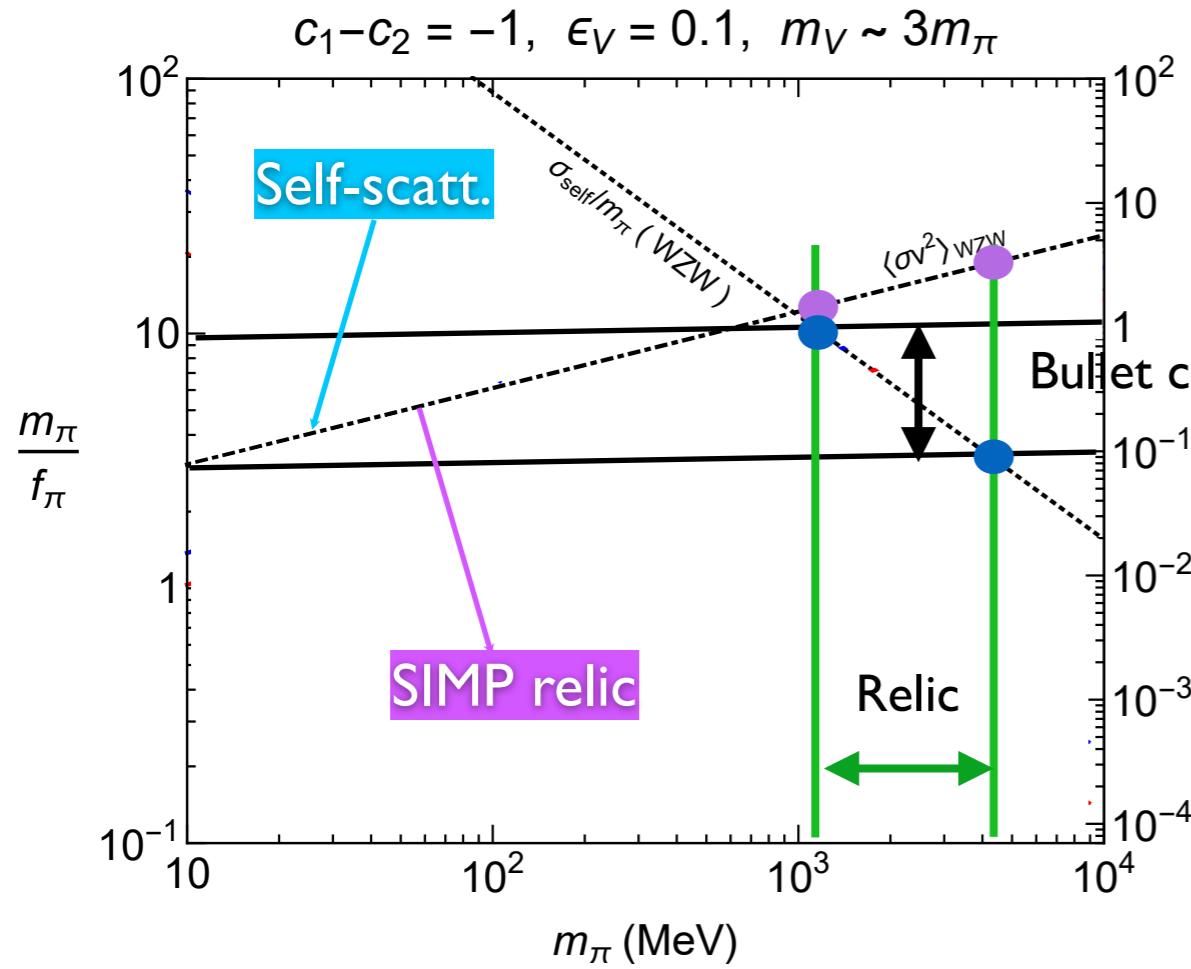
$m_\pi/f_\pi \lesssim 6$ for $g_{V\pi\pi} \lesssim 6$ and $m_\pi \lesssim 1 \text{ GeV}$.

cf. WZW terms only: $m_\pi/f_\pi \lesssim 15$.

Improvement persists for off-resonance too.

2-meson resonance

[S.-Choi, A. Natale, HML, P. Ko, 2018]



$$m_V = 2m_\pi \sqrt{1 + \epsilon_V}$$

Vector mesons on-resonance improve perturbativity.

$m_\pi / f_\pi \lesssim 4$ for $g_{V\pi\pi} \lesssim 1.3$ and $m_\pi \lesssim 1 \text{ GeV}$.

cf. WZW terms only: $m_\pi / f_\pi \lesssim 15$.

Conclusions

- **SIMP dark matter** is a sub-GeV SIDM produced via $3 \rightarrow 2$ freeze-out process and SIMP conditions can be tested by various intensity experiments.
- **Dark mesons** are natural candidates for SIMPs in dark confining gauge groups with flavor symmetries.
- **Vector mesons** unitarize SIMP mesons scenarios and maintain them as valid solutions to small-scale problems.
- **Kinetic equilibrium conditions for SIMPs** via Higgs or Z' portals could reveal the nature of SIMP sector.