

Supersymmetric Dark Matter

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HUH????

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Is “low energy” susy DM still viable?

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yes

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What about high scale susy?

Supersymmetric Dark Matter

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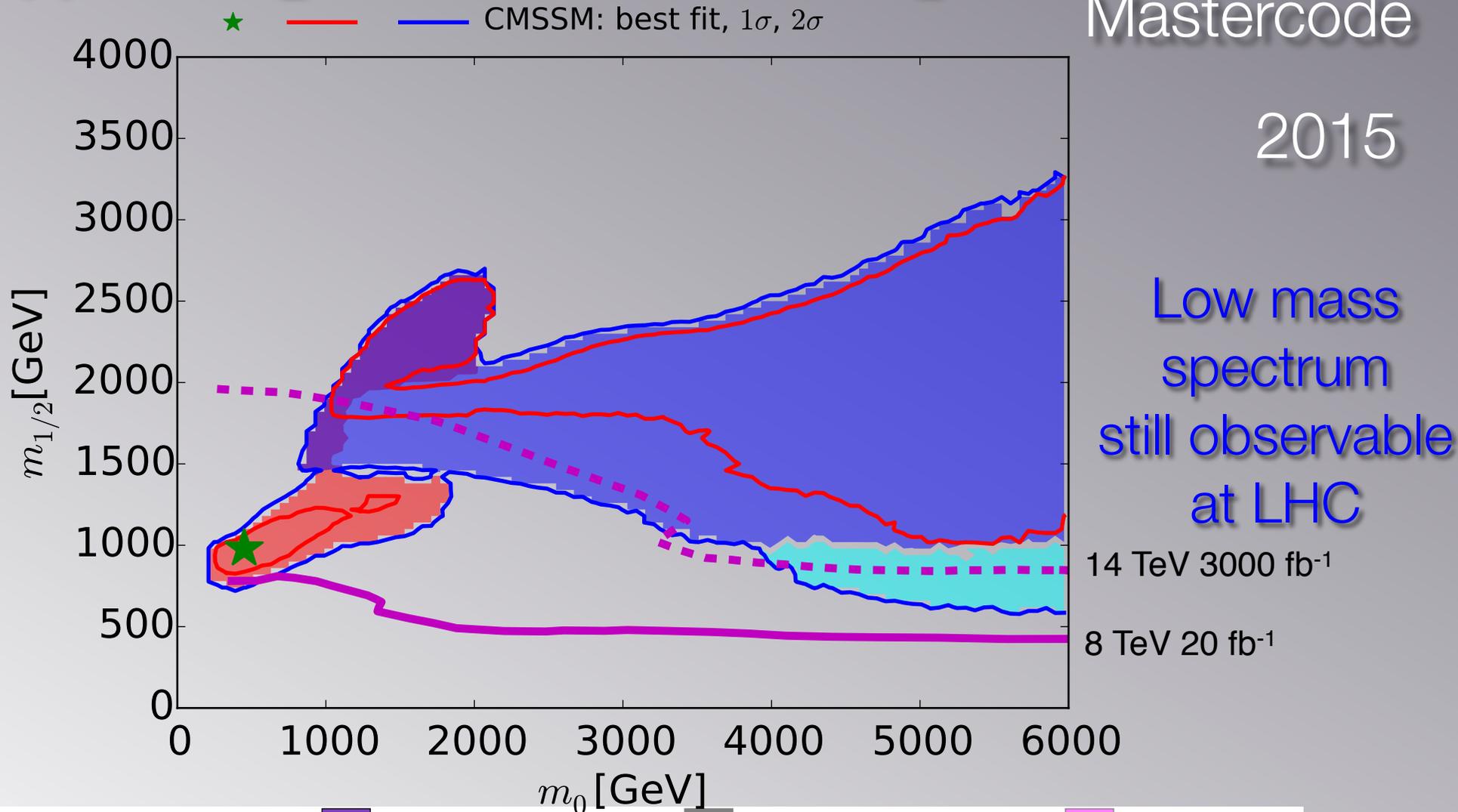
What about high scale susy?

No susy?

$\Delta\chi^2$ map of $m_0 - m_{1/2}$ plane

Mastercode

2015



- | | | | |
|--|--|---|---|
| ■ stau coann. | ■ hybrid | ■ stop coann. | ■ h funnel |
| ■ A/H funnel | ■ $\tilde{\chi}_1^\pm$ coann. | ■ focus point | ■ Z funnel |

CMSSM

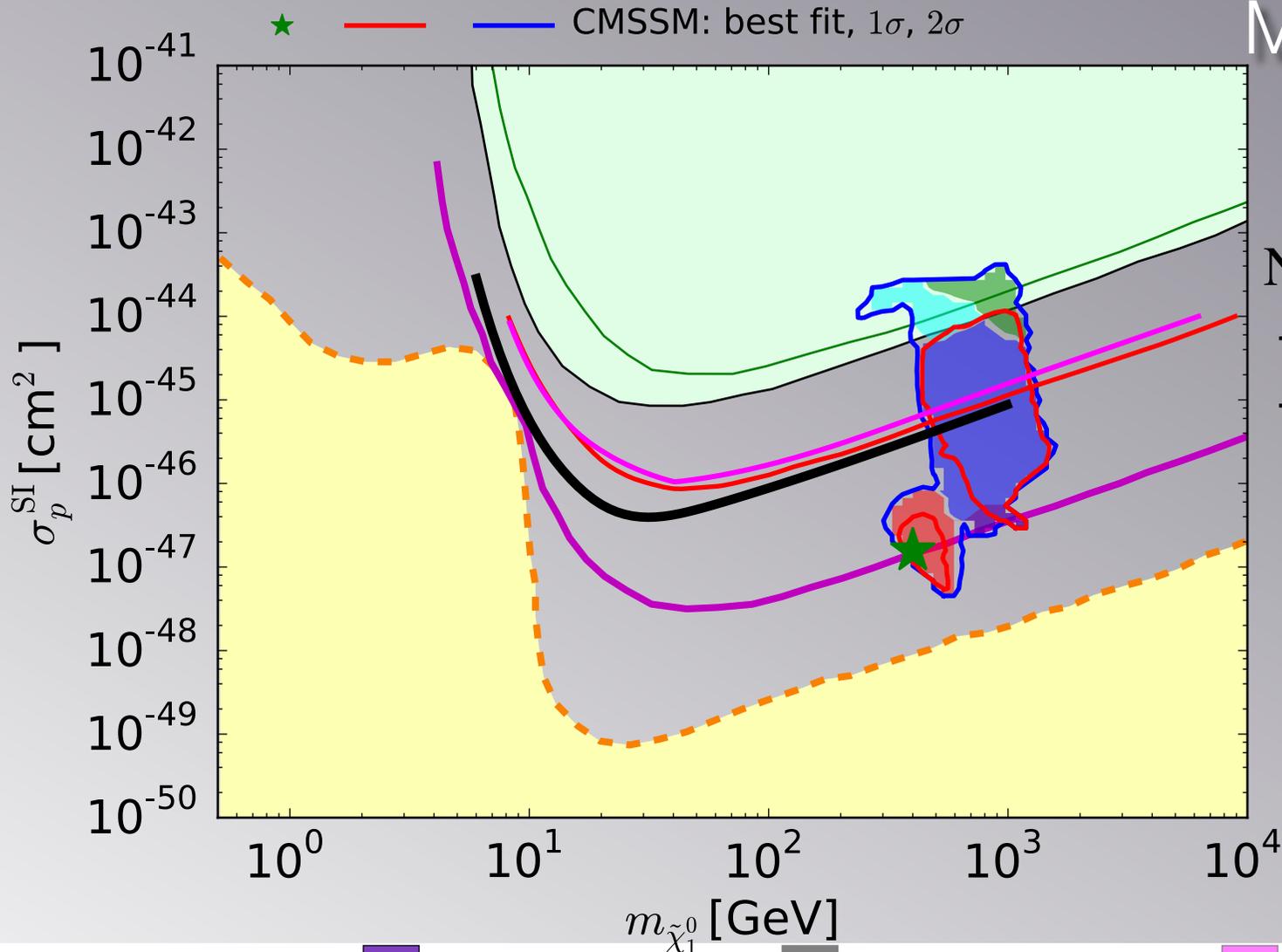
Bagnaschi, Buchmueller, Cavanaugh, Citron, De Roeck, Dolan, Ellis, Flacher, Heinemeyer, Isidori, Malik, Martinez Santos, Olive, Sakurai, de Vries, Weiglein

Elastic scattering cross-section

Mastercode

2015

New LUX bound
+ PandaX
+ XENON1t

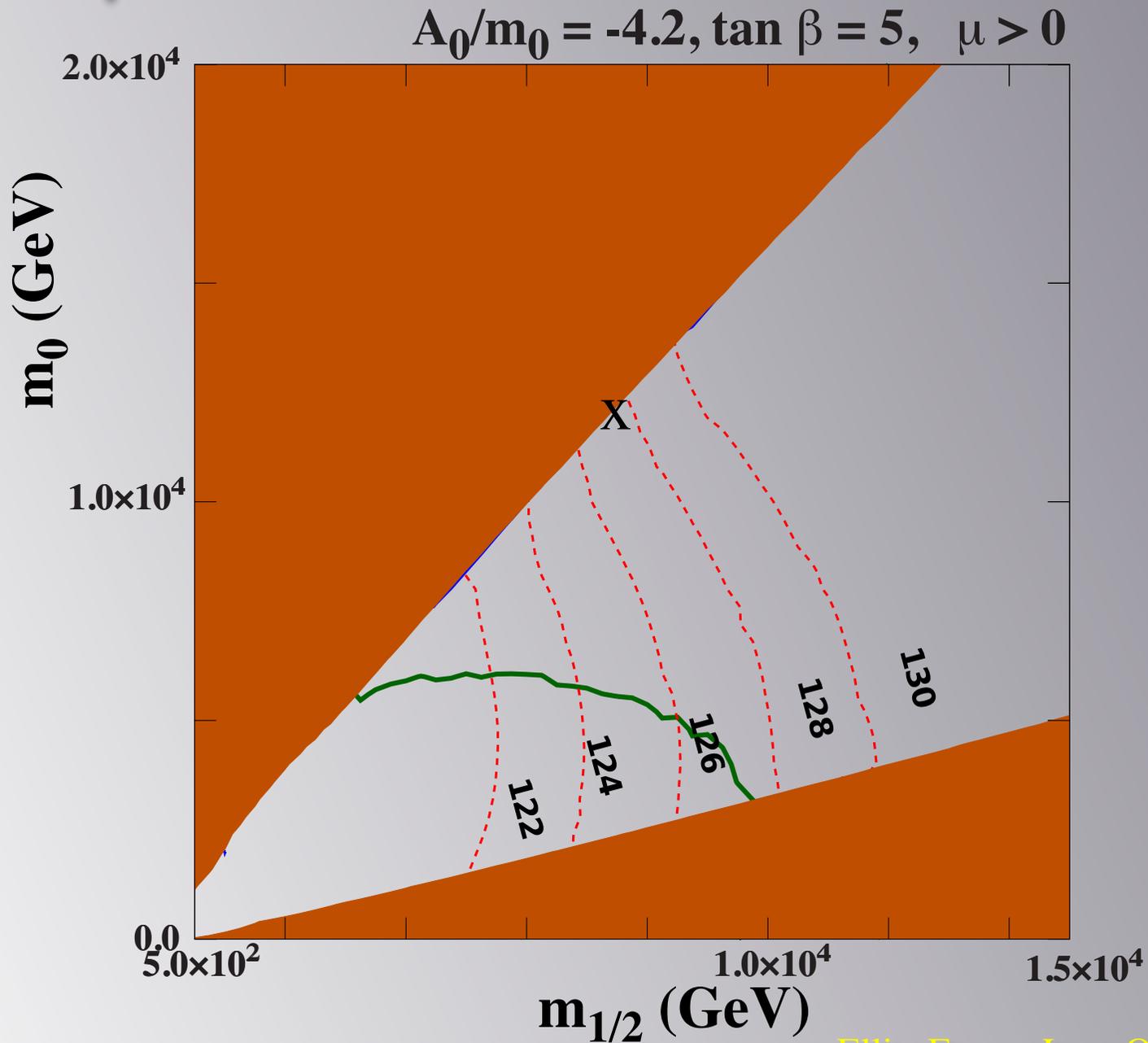


- | | | | |
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CMSSM

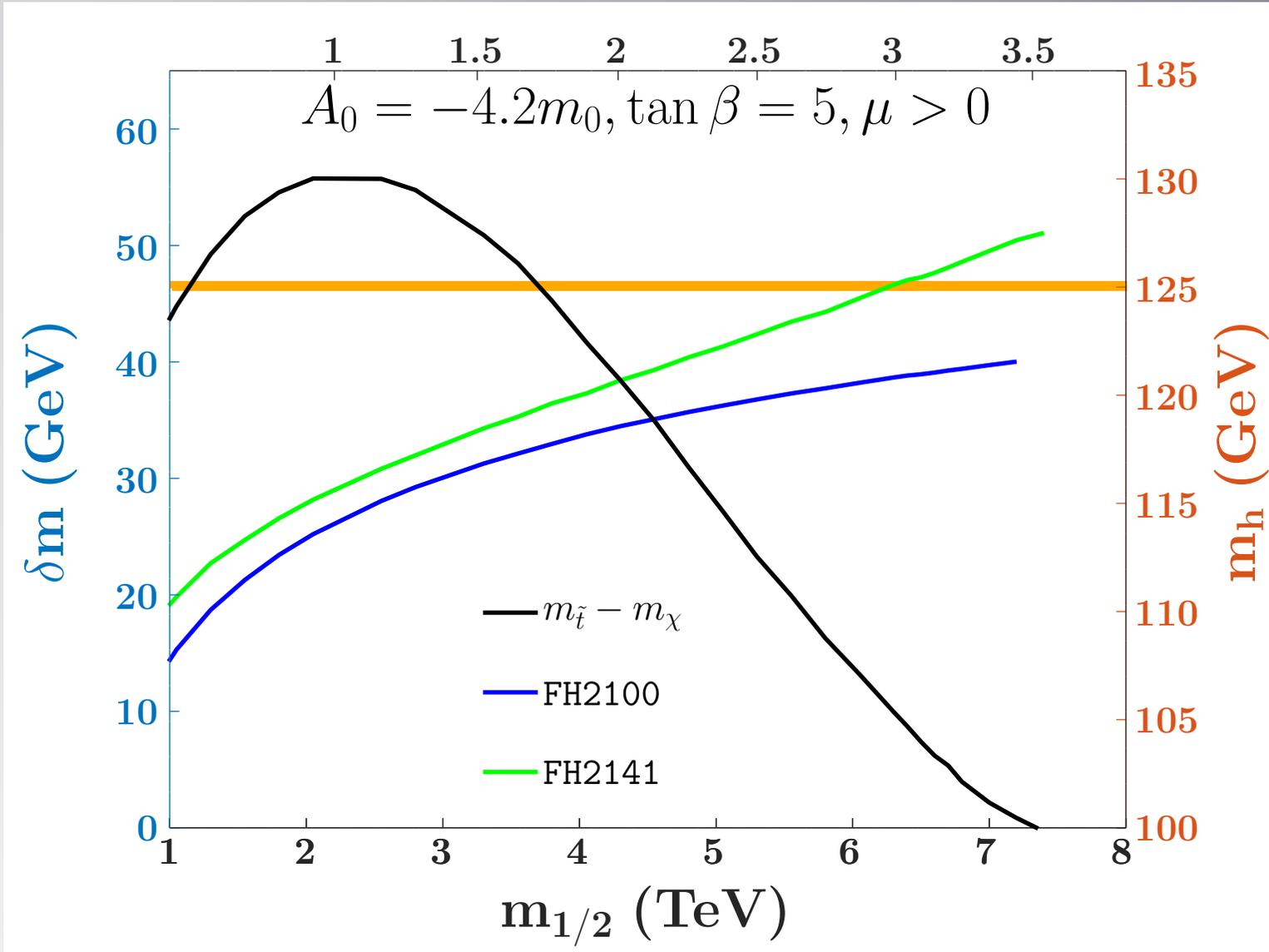
Bagnaschi, Buchmueller, Cavanaugh, Citron, De Roeck, Dolan, Ellis, Flacher, Heinemeyer, Isidori, Malik, Martinez Santos, Olive, Sakurai, de Vries, Weiglein

Stop strip



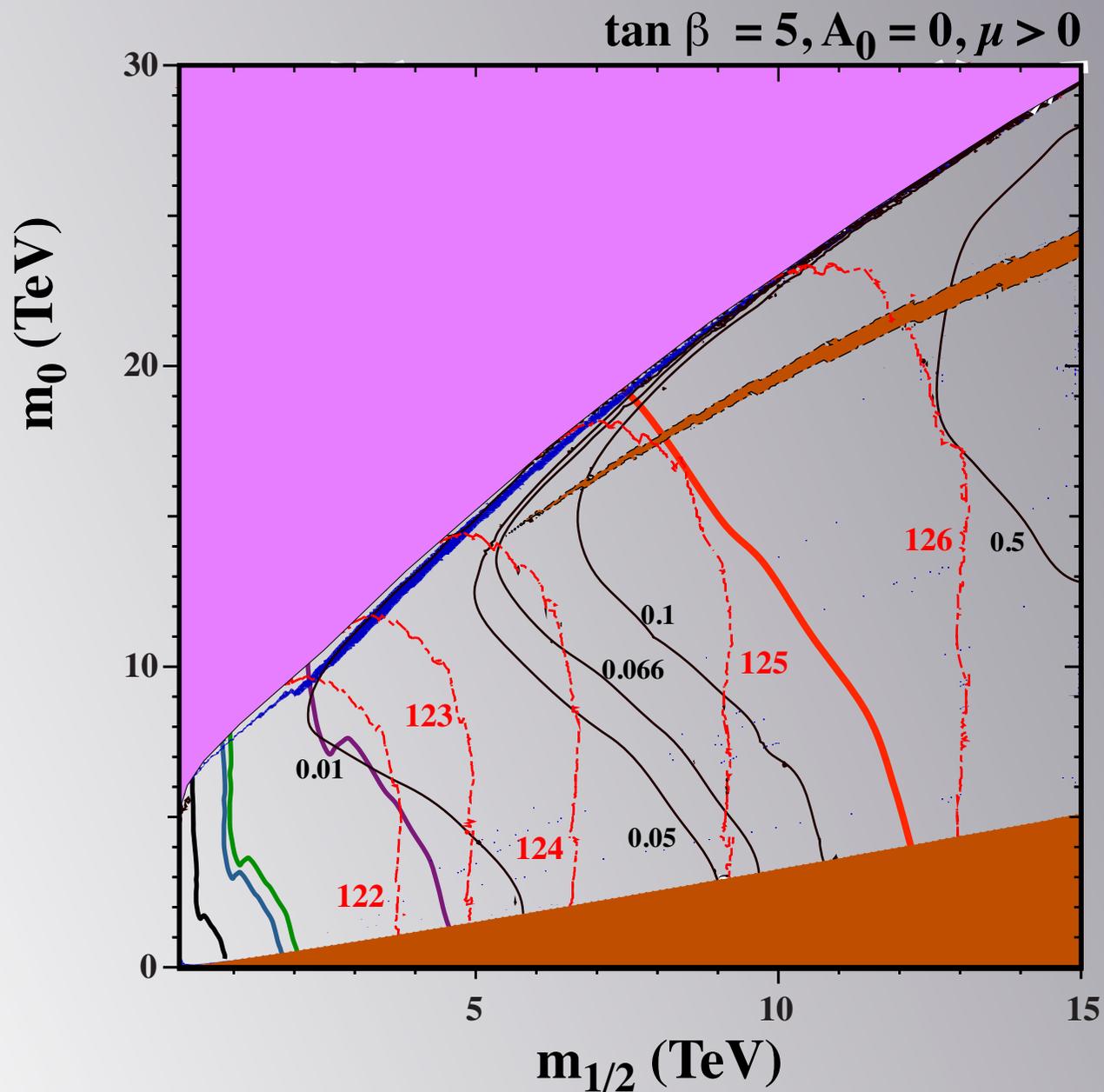
Ellis, Evans, Luo, Olive, Zheng
Bagnaschi et al.

Stop strip



Ellis, Evans, Luo, Olive, Zheng
Bagnaschi et al.

Focus Point



100 TeV 3000 fb⁻¹
33 TeV 3000 fb⁻¹
14 TeV 3000 fb⁻¹
14 TeV 300 fb⁻¹
8 TeV 20 fb⁻¹

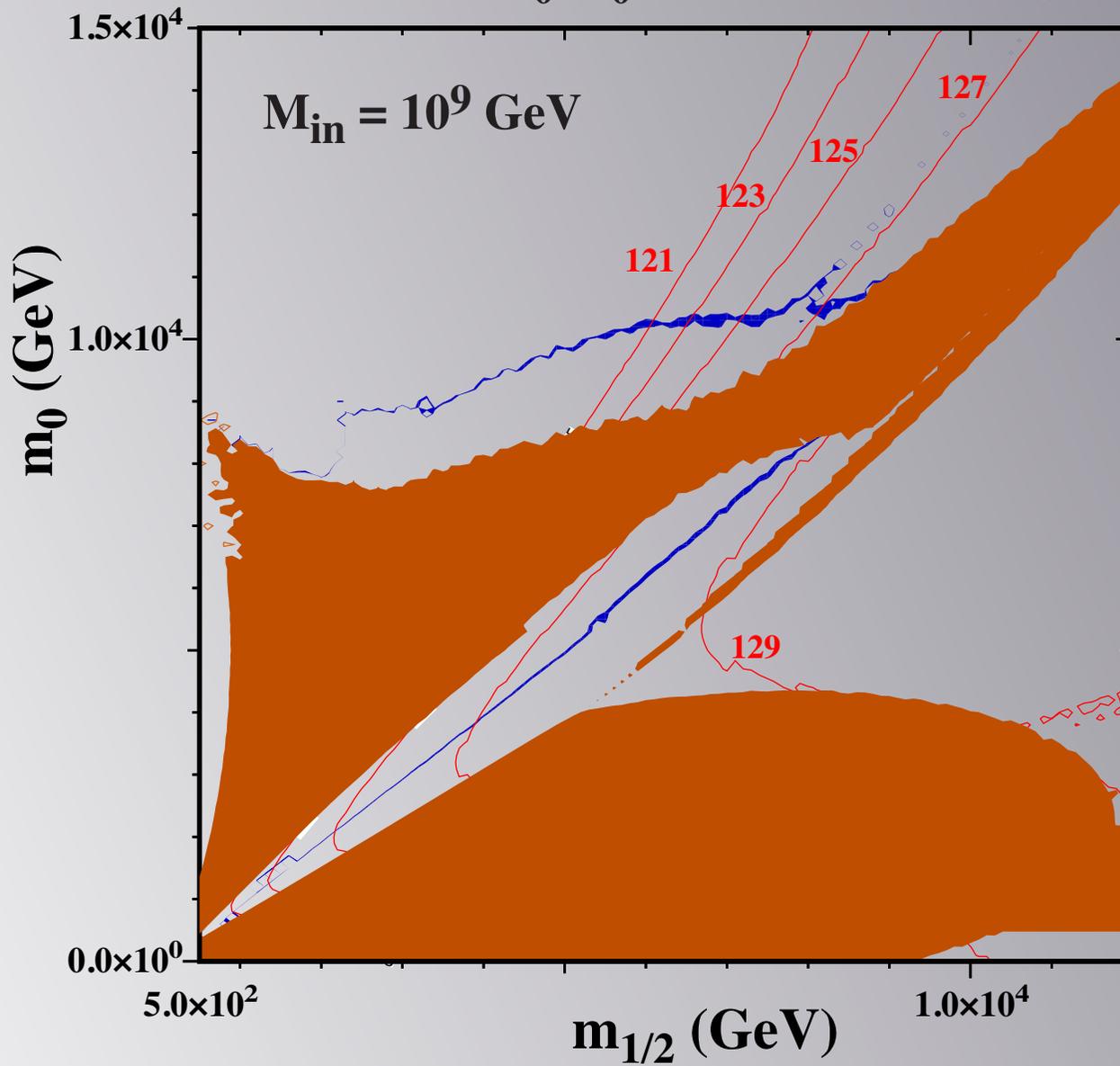
Other Possibilities

Less Constrained (more parameters)

- ✦ NUHM1,2: $m_1^2 = m_2^2 \neq m_0^2$, $m_1^2 \neq m_2^2 \neq m_0^2$
 - ✦ μ and/or m_A free
- ✦ NUGM
 - ✦ gluino coannihilation
- ✦ subGUT models: $M_{in} < M_{GUT}$
 - ✦ new parameter M_{in}
- ✦ SuperGUT models: $M_{in} > M_{GUT}$
 - ✦ requires SU(5) input couplings

SubGUT Stop strip

$$A_0/m_0 = 2.75, \tan \beta = 20, \mu < 0$$



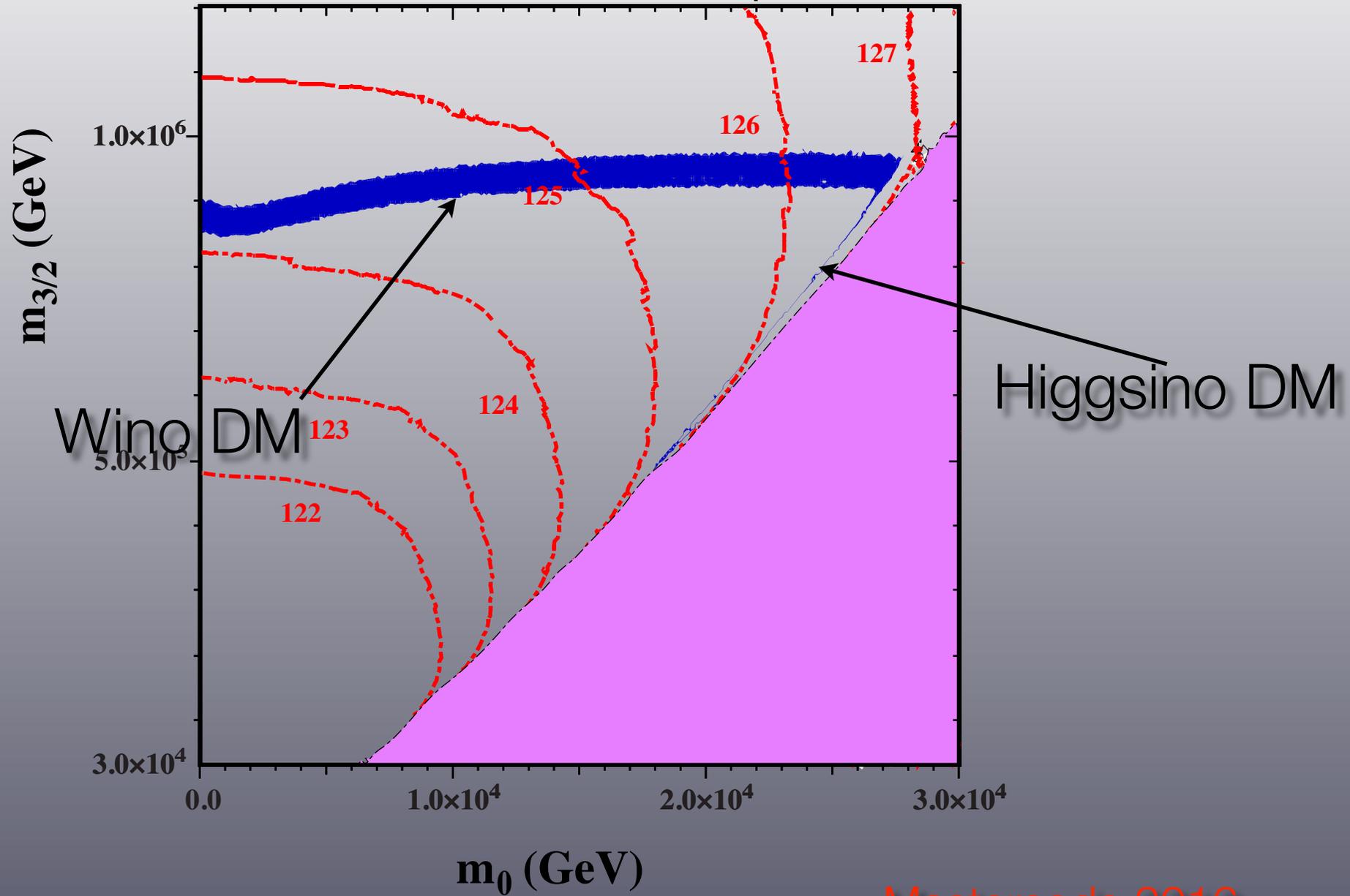
Ellis, Evans, Luo, Olive, Zheng
Bagnaschi et al.

Other Possibilities

More Constrained (fewer parameters)

- ✦ Pure Gravity Mediation
 - ✦ 2 parameter model with very large scalar masses
 - ✦ $m_0 = m_{3/2}, \tan \beta$
- ✦ mAMSB
 - ✦ similar to PGM, but allow $m_0 \neq m_{3/2}$
- ✦ mSUGRA
 - ✦ $B_0 = A_0 - m_0 \Rightarrow \tan \beta$ no longer free

$\tan \beta = 5, \mu > 0$



Even Larger Mass Scales

What if the entire SUSY matter spectrum were very large

with only the gravitino remaining “light”

Benakli, Chen, Dudas, Mambrini
Dudas, Mambrini, Olive

Supersplit Supersymmetry

- 1 parameter model: $m_{3/2}$

Gravitino Mass Limits

For $m_{3/2} \sim 10\text{-}1000$ GeV

Gravitino decays to the LSP/NLSP decays to the gravitino:

Lifetimes $100\text{-}10^8$ s \Rightarrow BBN limits

$$\Gamma_{\text{decay}} \simeq \frac{C^2}{16\pi} \frac{m_\chi^5}{m_{3/2}^2 M_P^2} \quad \text{NLSP} \rightarrow \text{gravitino} + \gamma$$

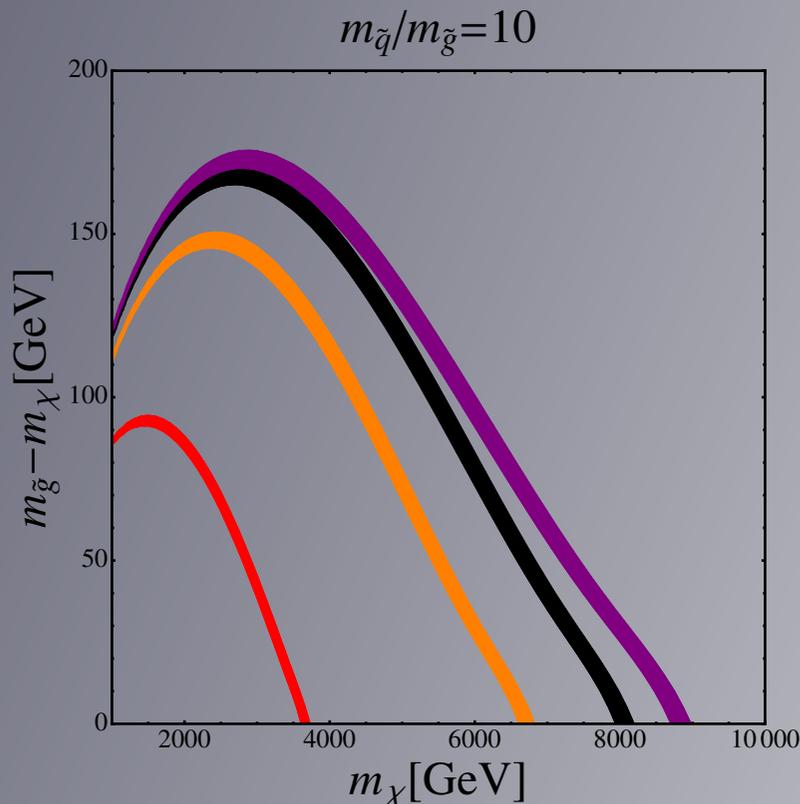
$$\tau_\chi \simeq 100 \text{ s} \Rightarrow m_\chi > 300 \text{ GeV} (m_{3/2}/\text{GeV})^{2/5}$$

Gravitino Mass Limits

$$\tau_\chi \approx 100 \text{ s} \Rightarrow m_\chi > 300 \text{ GeV} (m_{3/2}/\text{GeV})^{2/5}$$

Relic Density: $\Omega_{3/2} h^2 = \frac{m_{3/2}}{m_\chi} \Omega_\chi h^2$ or $\Omega_\chi h^2 \lesssim 0.12 \frac{m_\chi}{m_{3/2}}$

Glino coannihilation



$$m_\chi < 8 \text{ TeV} \Rightarrow m_{3/2} < 4 \text{ TeV}$$

heavier gravitino \rightarrow heavier neutralino
 $\rightarrow \Omega_\chi h^2$ too large $\rightarrow \Omega_{3/2} h^2$ too large

Gravitino Mass Limits

$m_{3/2} < 4 \text{ TeV}$ unless(!) the susy spectrum lies above the inflationary scale.

For $M_{\text{susy}} \sim F^{1/2} > m_{\text{infl}} \sim 3 \times 10^{13} \text{ GeV}$

$$m_{3/2} = \frac{F}{\sqrt{3}M_P} > \frac{m_\phi^2}{\sqrt{3}M_P} \simeq 0.2 \text{ EeV}$$

Toy Model

Dudas, Gherghetta, Mambrini, Olive

No Scale Model:

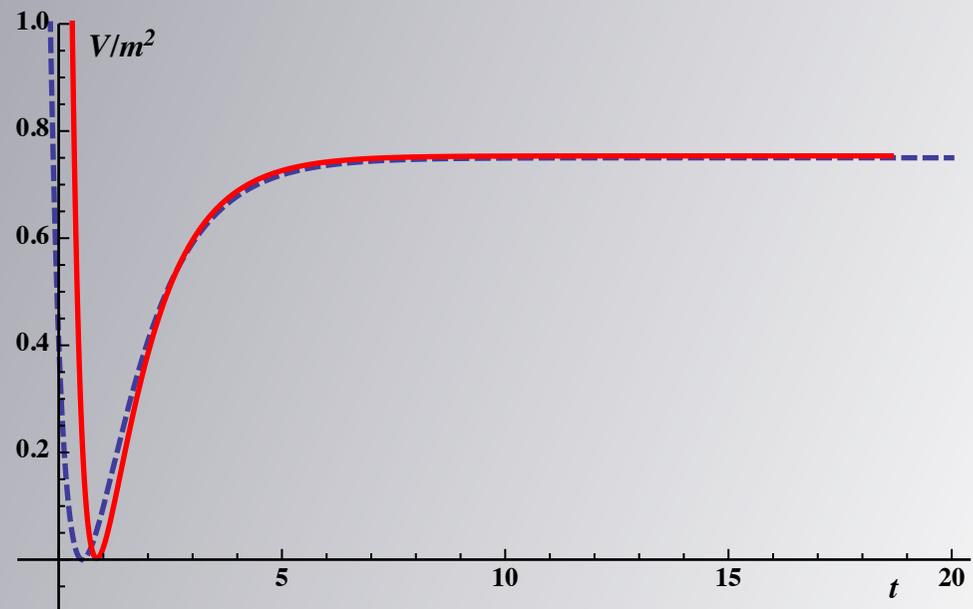
$$K = -3 \ln \left(\underbrace{T + \bar{T}}_{\text{Inflaton}} - \frac{1}{3} \sum_i \underbrace{|\phi_i|^2}_{\text{Matter}} \right) + |z|^2 - \frac{|z|^4}{\Lambda_z^2}$$

\swarrow Polonyi

$$W = \sqrt{3}m\phi(T - 1/2), \\ + \tilde{m}^2(z + b)$$

Starobinsky Inflation

Polonyi Model



Toy Model

for small Λ_z

$$m_{3/2} = m \frac{4\tilde{m}^6 + 2\tilde{m}^2 m^3 M_P}{2\sqrt{3}(m^2 M_P^2 + \tilde{m}^4)^{3/2}} \rightarrow \tilde{m}^2 / \sqrt{3} M_P \quad \text{for small } \tilde{m}^2 / m M_P$$

$$\text{For } \tilde{m} = m \quad m_{3/2} = \frac{m^2}{\sqrt{3} M_P} \approx 0.2 \text{ EeV.}$$

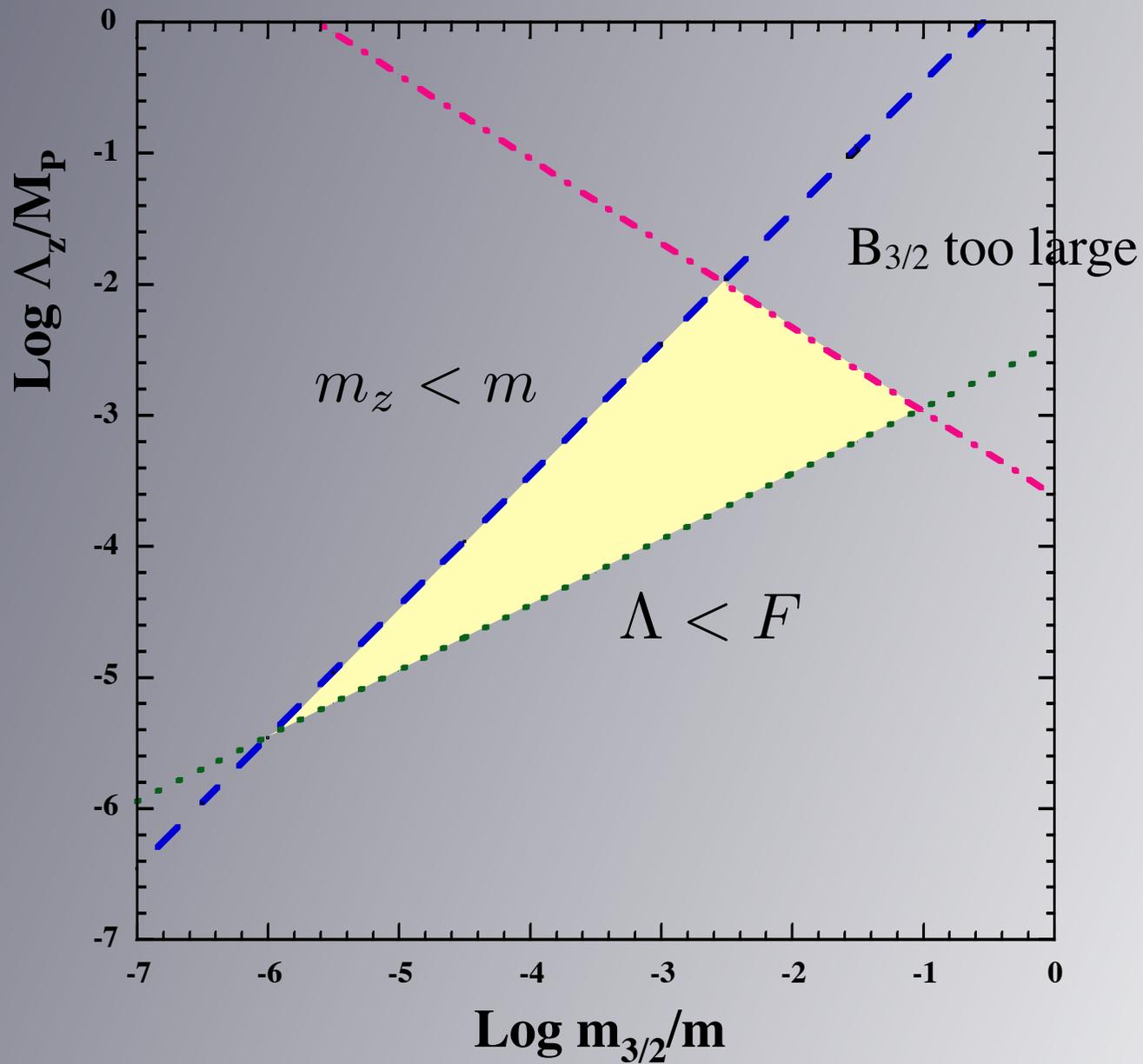
$$m_{1/2} \sim m_{3/2} \frac{M_P^2}{\Lambda_z^2}$$

$$m_z^2 = \frac{12 m_{3/2}^2 M_P^2}{\Lambda_z^2}$$

$$m_0 \sim m_{1/2} \frac{g^2}{16\pi^2}$$

$$\Rightarrow \frac{\Lambda_z}{M_P} < \frac{g}{4\pi} \left(\frac{m}{M_P} \right)^{1/2} \sim \text{few} \times 10^{-3}$$

Toy Model



Gravitino Production

Standard Picture:

gluon + gluon \rightarrow gluino + gravitino

$$\langle\sigma v\rangle \sim \frac{1}{M_P^2} \left(1 + \frac{m_{\tilde{g}}^2}{3m_{3/2}^2} \right)$$

$$\Gamma \sim T^3 \frac{m_{\tilde{g}}^2}{M_P^2 m_{3/2}^2} \quad \frac{n_{3/2}}{n_\gamma} \sim \frac{\Gamma}{H} \sim T \frac{m_{\tilde{g}}^2}{M_P m_{3/2}^2}$$

$m_{\tilde{g}} > m_{3/2}$

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$m_{\tilde{g}} > m_{3/2}$

Not possible if $m_{\tilde{g}} > m_\phi$

Gravitino Production

$$m_{\tilde{g}} > m_{\phi}$$

gluon + gluon \rightarrow gravitino + gravitino

$$\langle \sigma v \rangle \sim \frac{T^6}{M_P^4 m_{3/2}^4}$$

$$\Gamma \sim \frac{T^9}{M_P^4 m_{3/2}^4} \quad \frac{n_{3/2}}{n_{\gamma}} \sim \frac{\Gamma}{H} \sim \frac{T^7}{M_P^3 m_{3/2}^4}$$

$$\Omega_{3/2} h^2 \simeq 0.11 \left(\frac{0.1 \text{ EeV}}{m_{3/2}} \right)^3 \left(\frac{T_{RH}}{2.0 \times 10^{10} \text{ GeV}} \right)^7$$

Reheating

Inflaton decays (dominant channel):

Ellis, Garcia,
Nanopoulos, Olive

$$\mathcal{L}_{\text{eff}} \ni \frac{\text{Re}T}{\sqrt{3}} (n_I + n_L - 3) W^{IL} \bar{W}_{LJ} \Phi_I \bar{\Phi}^J, \\ \sim \mu^2 e^{\sqrt{\frac{2}{3}}t} (|h_u|^2 + |h_d|^2),$$

$$\Gamma_{2h} = \frac{\mu^4}{384\pi m M_P^2} \sin^2 2\beta$$

$$T_{RH} = \left(\frac{10}{g_s}\right)^{1/4} \left(\frac{2\Gamma_{2h} M_P}{\pi c}\right)^{1/2} = 0.5 \frac{y_I}{2\pi} (m M_P)^{1/2}$$

$$y_I = \mu^2 / (4\sqrt{3}mM_P) \quad g_s = 427/4 \quad c \simeq 1.2$$

$$2.7 \times 10^{10} \text{ GeV} \lesssim T_{RH} \lesssim 1.1 \times 10^{12} \text{ GeV}$$

$$m_{3/2} > .2\text{EeV}$$

$$m_{3/2} < T_R$$

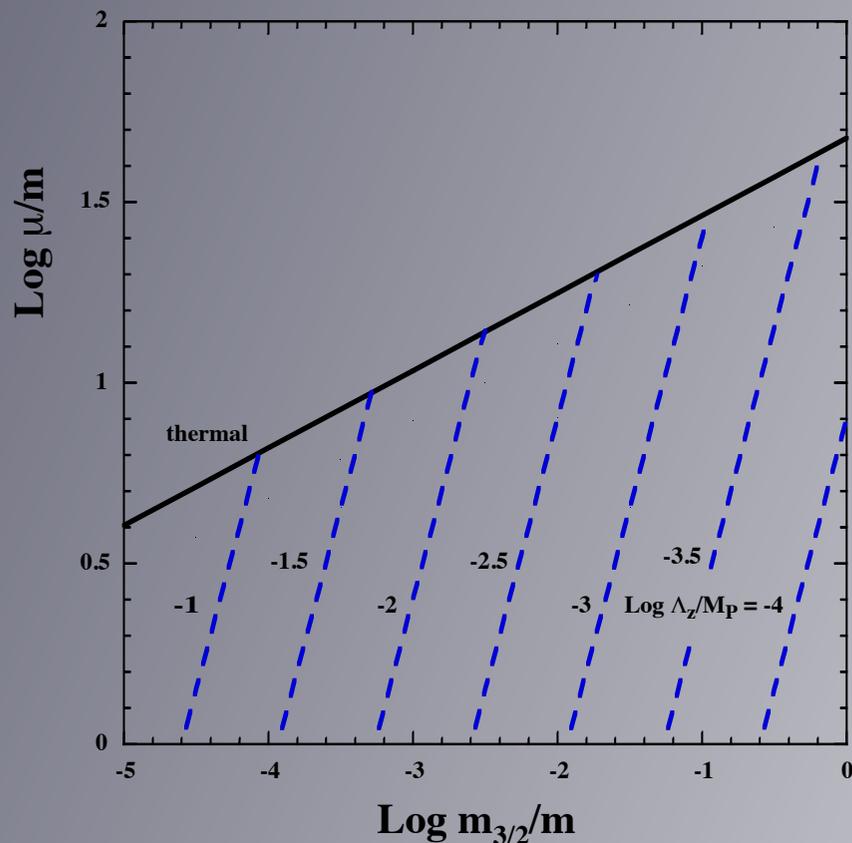
Reheating

Thermal production

$$\Omega_{3/2} h^2 \simeq 0.11 r_{3/2} \left(\frac{0.1 \text{ EeV}}{m_{3/2}} \right)^3 \left(\frac{3 \times 10^{13} \text{ GeV}}{m} \right)^{7/2} \times \left(\frac{\mu}{1.2 \times 10^{14} \text{ GeV}} \right)^{14}$$

gravitinos from inflaton decay

$$\Omega_{3/2}^{\text{decay}} h^2 = 0.11 \left(\frac{B_{3/2}}{1.3 \times 10^{-13}} \right) \left(\frac{y_I}{2.9 \times 10^{-5}} \right)$$



$$B_{3/2} = \frac{9}{2} \left(\frac{\Lambda_z}{M_P} \right)^4 \left(\frac{m_{3/2}}{m} \right)^2 \left(\frac{m}{\mu} \right)^4$$

UV Completion -SO(10)

Ellis, Gherghetta, Kaneta, Olive

$$W \supset \frac{\mu_\Phi}{4!} \Phi^2 + \frac{\mu_\Sigma}{5!} \Sigma \bar{\Sigma} + \frac{\lambda}{4!} \Phi^3 + \frac{\eta}{4!} \Phi \Sigma \bar{\Sigma} + \mu_H H^2 + \frac{1}{4!} \Phi H (\alpha \Sigma + \bar{\alpha} \bar{\Sigma})$$

$$\Phi(\mathbf{210}); \quad \Sigma(\mathbf{126}); \quad \bar{\Sigma}(\overline{\mathbf{126}}); \quad H(\mathbf{10})$$

Vanishing F- and D- terms fixes the vevs

$$v_{1,1,1} = -\frac{\mu_\Phi}{\lambda} \frac{x(1-5x^2)}{(1-x)^2}; \quad v_{1,1,15} = -\frac{\mu_\Phi}{\lambda} \frac{(1-2x-x^2)}{(1-x)}; \quad v_{1,3,15} = -\frac{\mu_\Phi}{\lambda} x;$$
$$\sigma_{1,3,\overline{10}} \sigma_{1,3,10} = \frac{2\mu_\Phi^2}{\eta\lambda} \frac{x(1-3x)(1+x^2)}{(1-x)^2}; \quad -8x^3 + 15x^2 - 14x + 3 = (x-1)^2 \frac{\lambda\mu_\Sigma}{\eta\mu_\Phi}$$

choice of $x \sim 0.63$ leaves one state (in addition to the Higgs) light

$$S = (1, 3, 0) \subset (1, 3, 15) \subset 210$$

gauge coupling unification

Threshold corrections:

$$\left(\frac{1}{g_i^2(\mu_*)} \right) = \left(\frac{1}{g_U^2(\mu_*)} \right) - \left(\frac{\lambda_i}{48\pi^2} \right)$$

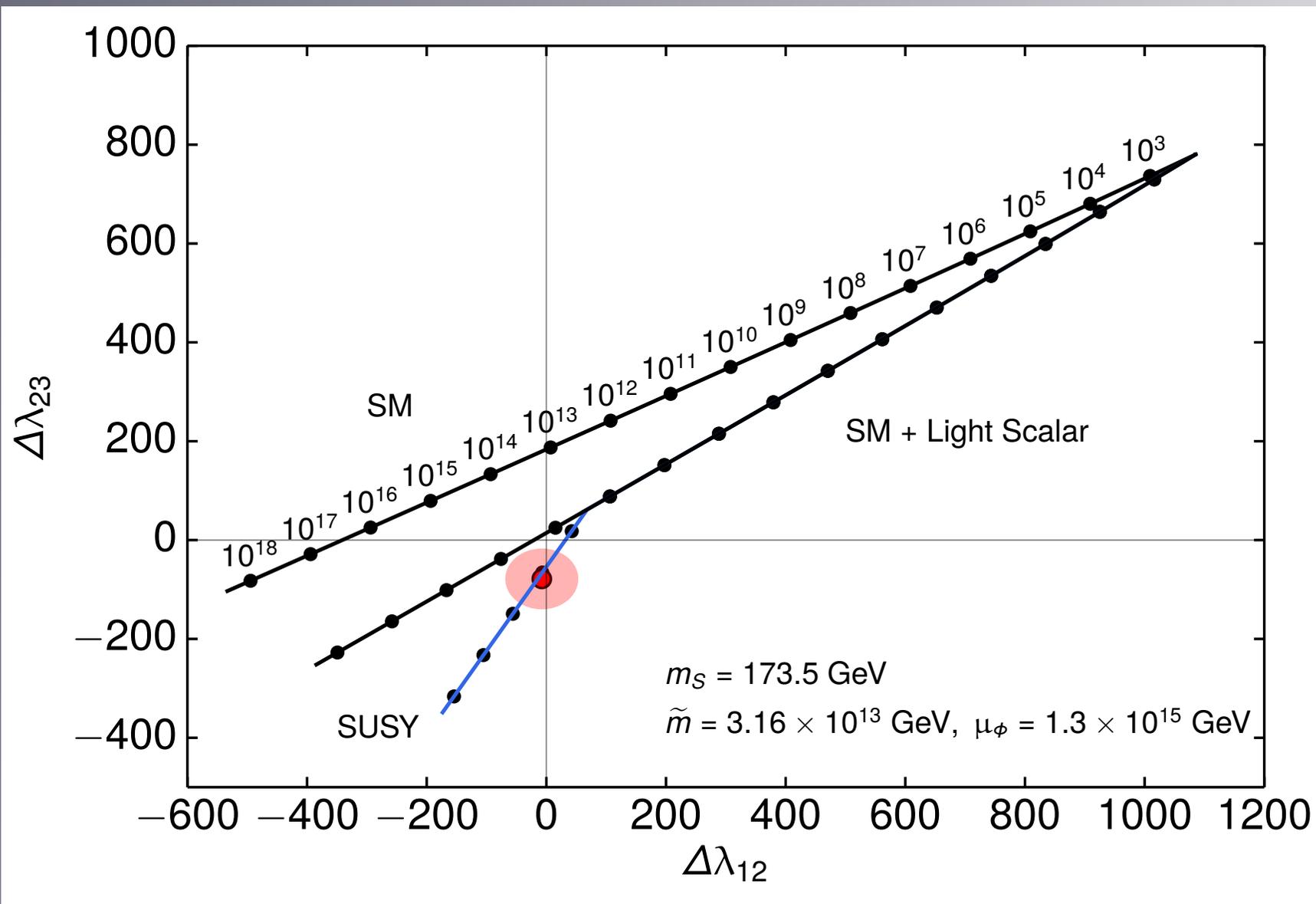
λ_i computable because spectrum is determined

$$\left(\frac{\Delta\lambda_{ij}(\mu)}{48\pi^2} \right) \equiv \left(\frac{1}{g_i^2(\mu)} - \frac{1}{g_j^2(\mu)} \right) = \left(\frac{\lambda_j(\mu) - \lambda_i(\mu)}{48\pi^2} \right)$$

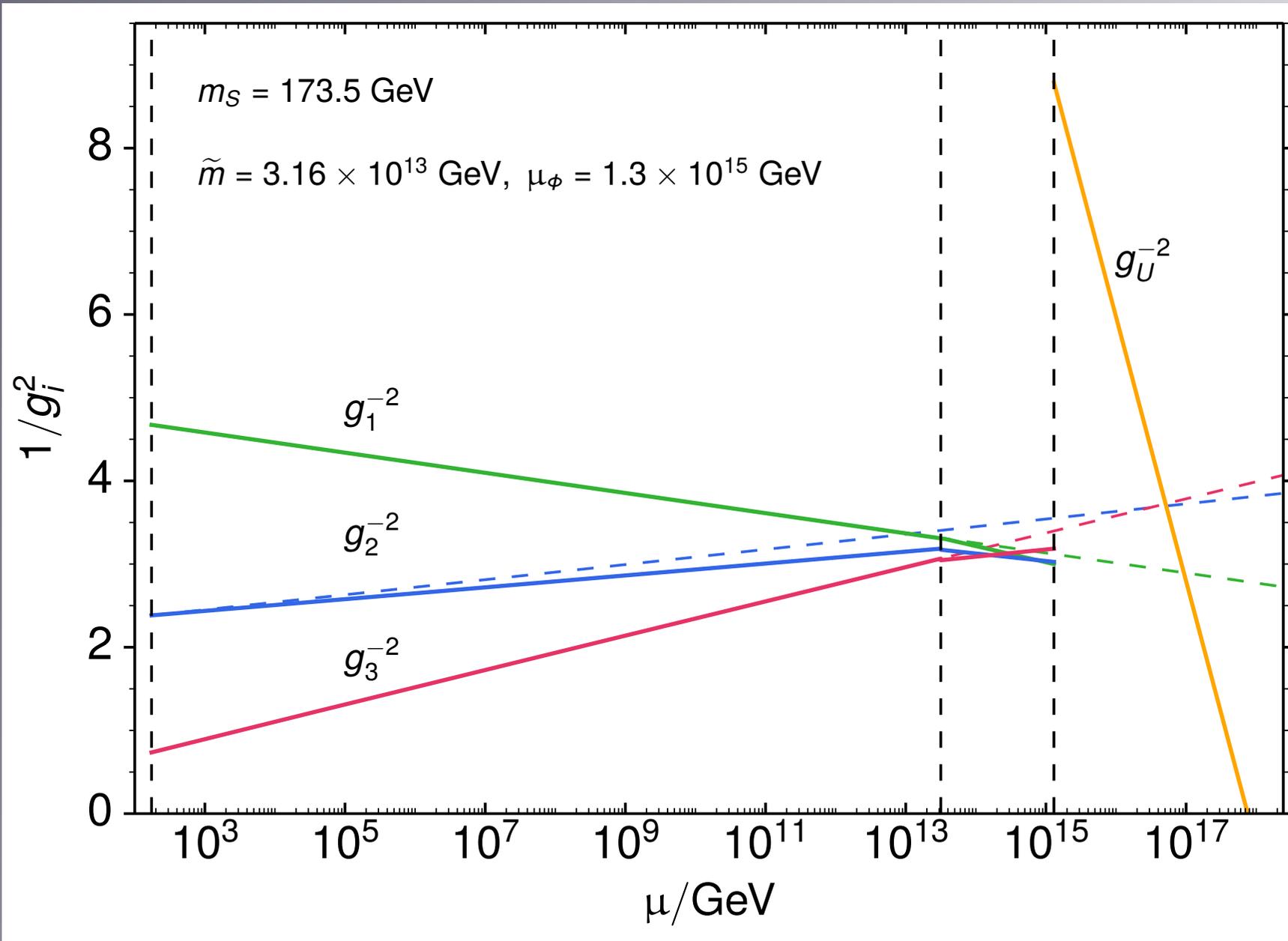
for each λ, η

$$\chi^2(g_U, \mu_\Phi, \tilde{m}, m_\chi) \equiv \sum_{i=1}^3 \left[g_i^{-2}(\mu_\Phi) - \left(g_U^{-2} - \frac{\lambda_i(g_U, \mu_\Phi, \tilde{m}, m_\chi)}{48\pi^2} \right) \right]^2 / \sigma_i^2$$

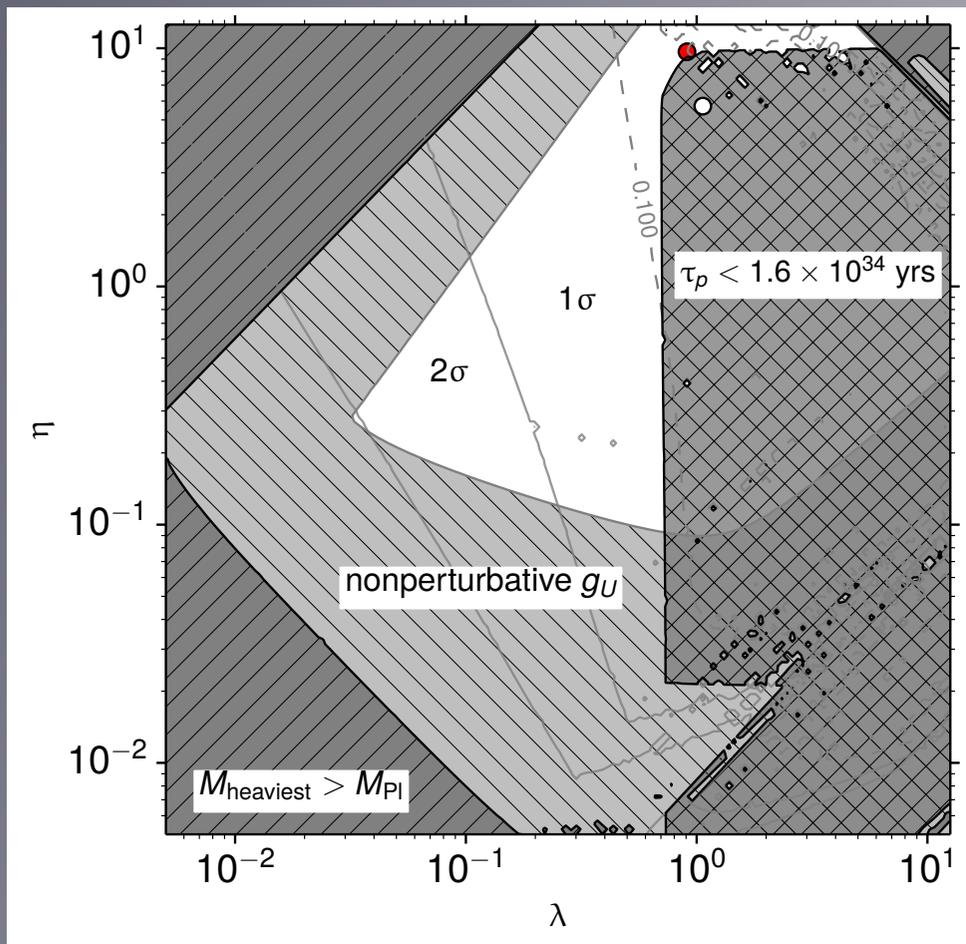
gauge coupling unification



gauge coupling unification



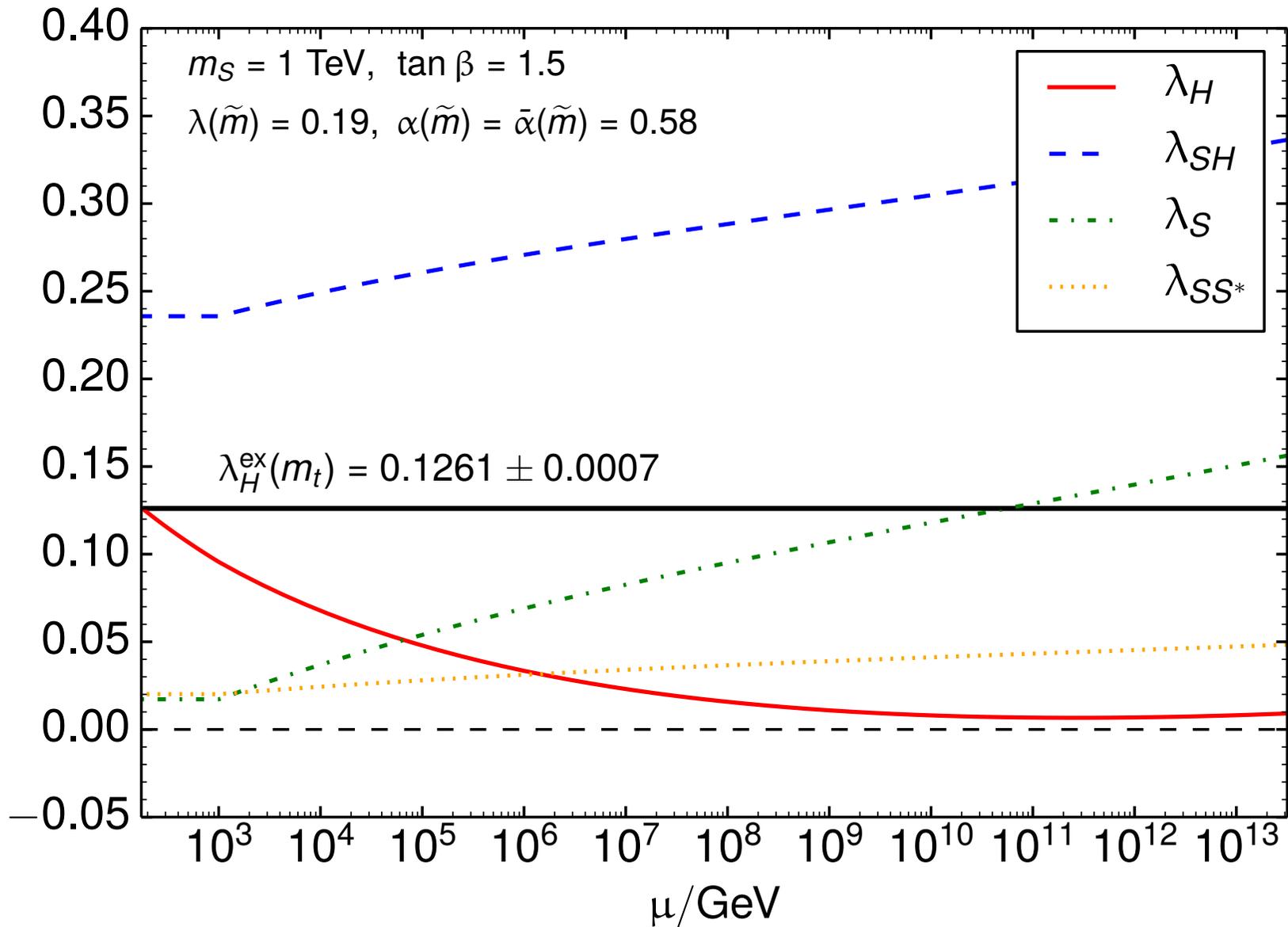
gauge coupling unification



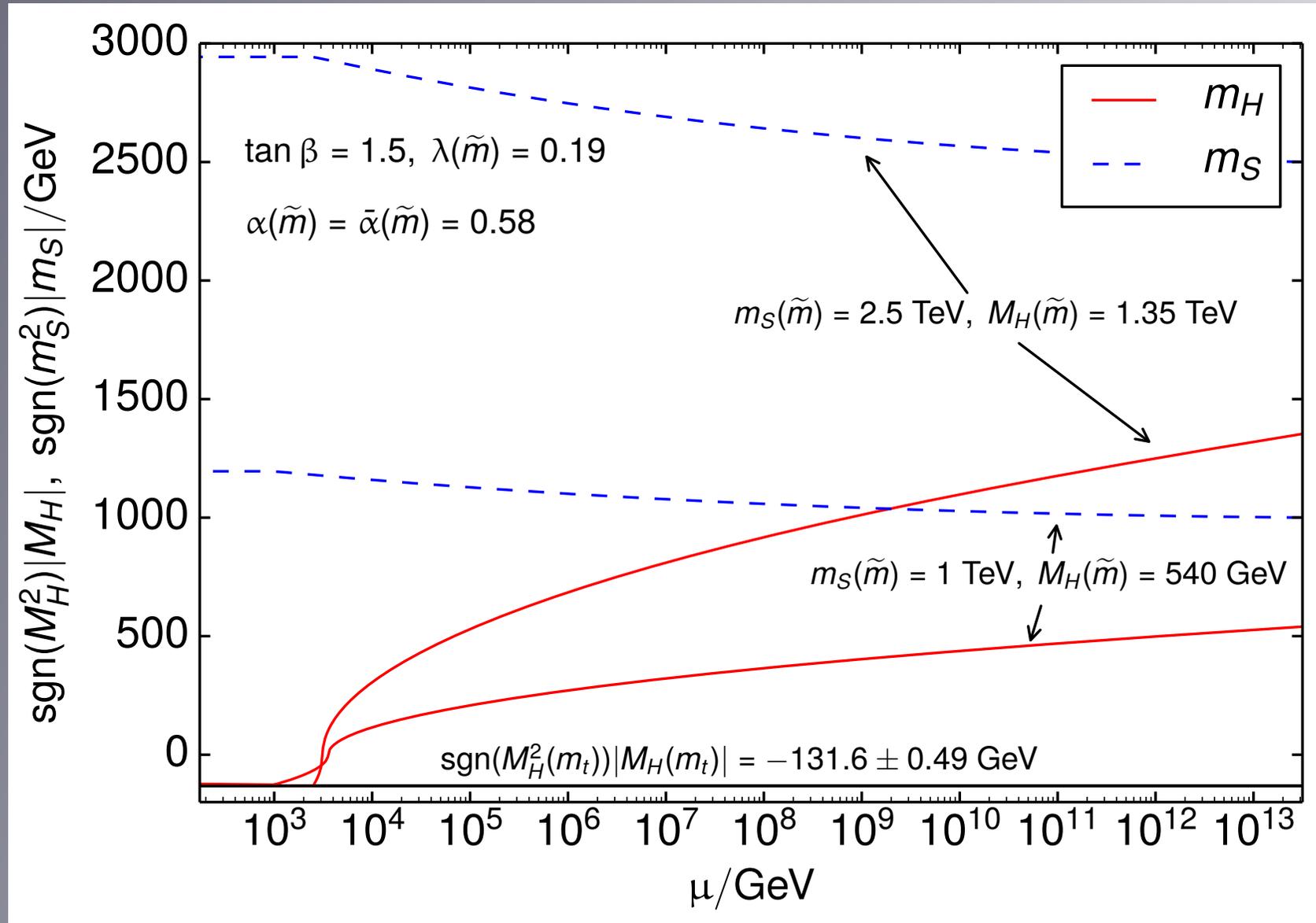
Higgs vacuum stability
achieved through coupling of S
(weak triplet) to H

Radiative EW symmetry breaking

Higgs vacuum stability



Radiative Electroweak Symmetry Breaking



Detection?

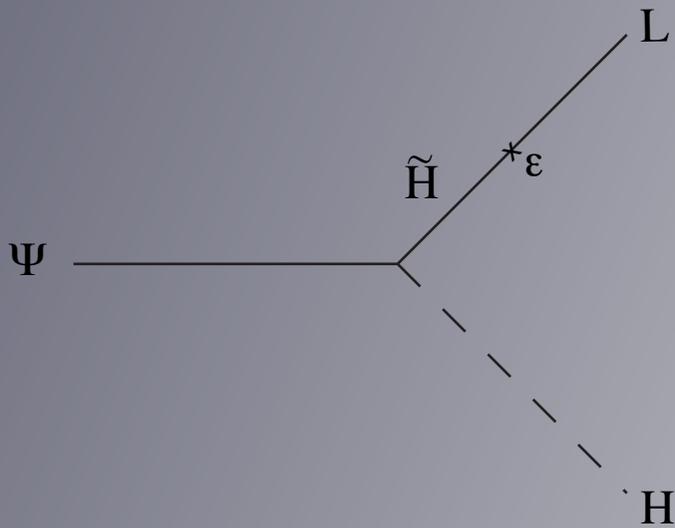
Dudas, Gherghetta, Kaneta,
Mambrini, Olive

Signatures of decay with R-parity violation

$$W_{\text{RPV}} = \mu' L H_u.$$

Normally, $\mu' < 2 \times 10^{-5} \text{ GeV}$ from L-violating interactions

High Scale Susy: $\mu' < 2 \times 10^{-7} \left(\frac{\mu \tilde{m}^{1/2}}{\text{GeV}^{3/2}} \right) \text{ GeV}$



$$\Gamma_{\text{tot}} \simeq \frac{\epsilon^2 c_\beta^2 m_{3/2}^3}{16\pi M_P^2}, \quad \epsilon = \mu' / \mu$$

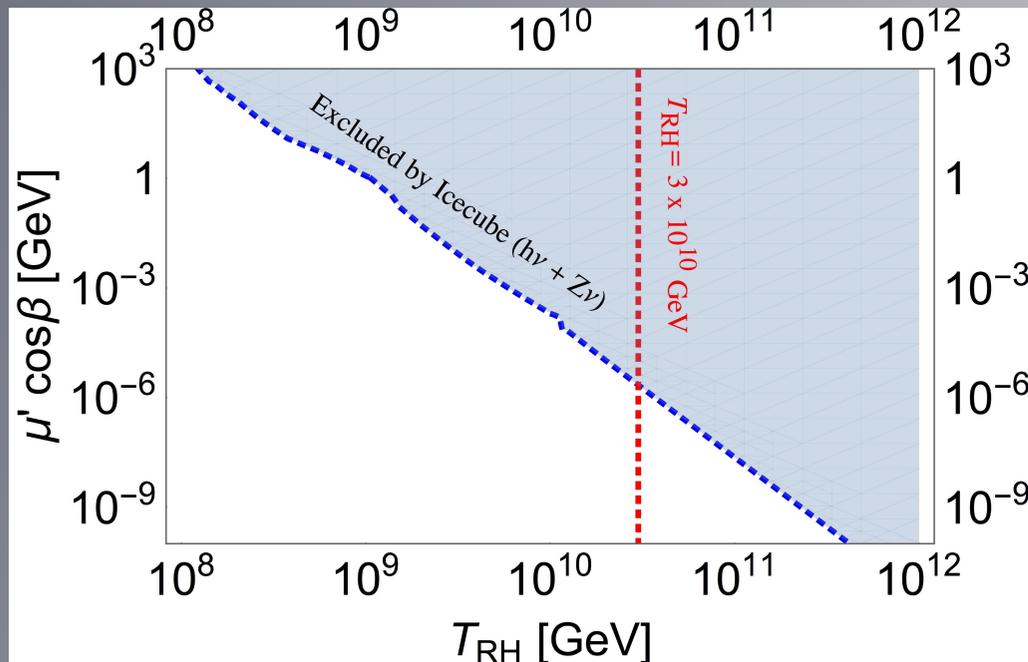
$$\tau_{3/2} \simeq 10^{28} \left(\frac{0.44 \times 10^{-20}}{\epsilon c_\beta} \right)^2 \left(\frac{1 \text{ EeV}}{m_{3/2}} \right)^3 \text{ s.}$$

Detection?

Dudas, Gherghetta, Kaneta,
Mambrini, Olive

$$\tau_{3/2} \simeq 10^{28} \left(\frac{\tilde{m}}{10^{14} \text{ GeV}} \right)^2 \left(\frac{0.44 \text{ keV}}{\mu' c_\beta} \right)^2 \left(\frac{1 \text{ EeV}}{m_{3/2}} \right)^3 \text{ s} \quad \mu \sim \tilde{m} \gg \mu'$$

$$\mu' c_\beta = 14 \text{ keV} \left(\frac{\Omega_{3/2} h^2}{0.11} \right)^{1/2} \left(\frac{10^{28} \text{ s}}{\tau_{3/2}} \right)^{1/2} \left(\frac{\tilde{m}}{10^{14} \text{ GeV}} \right) \left(\frac{2.0 \times 10^{10} \text{ GeV}}{T_{\text{RH}}} \right)^{7/2}$$



Expect about 1 event at
ANITA every 137 years.

ANITA has seen 2 O(EeV)
events in 3 years

Even Larger Mass Scales

Planck Scale SUSY \equiv no susy at low energy

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SO(10) GUT?

Even Larger Mass Scales

Planck Scale SUSY \equiv no susy at low energy

SO(10) GUT?

- ✦ Gauge Coupling Unification
- ✦
- ✦ Stabilization of the Electroweak Vacuum
- ✦ Radiative Electroweak Symmetry Breaking
- ✦ Dark Matter
- ✦ Neutrino masses...

SO(10) DM models

Mambrini, Nagata, Olive, Zheng

1. Pick an Intermediate Scale Gauge Group

$$R_1 \quad SO(10) \longrightarrow G_{\text{int}}$$

2. Use **126** to break G_{int} to SM

$$SO(10) \xrightarrow{R_1} G_{\text{int}} \xrightarrow{R_2} G_{\text{SM}} \otimes \mathbb{Z}_2 \quad R_2 = \mathbf{126} + \dots$$

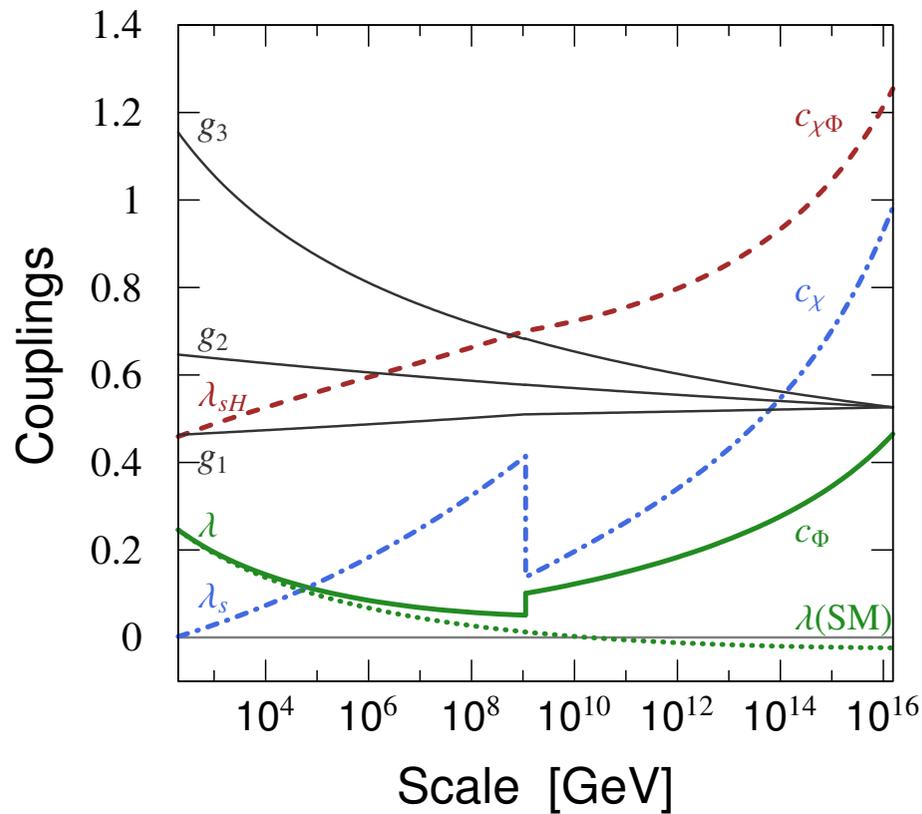
3. Pick DM representation and insure proper splitting within the multiplet, and pick low energy field content

4. Use RGEs to obtain Gauge Coupling Unification

Examples:

Scalars

Higgs portal models
Inert Higgs doublet models



Model	$\log_{10} M_{\text{GUT}}$	$\log_{10} M_{\text{int}}$	α_{GUT}	$\log_{10} \tau_p(p \rightarrow e^+ \pi^0)$
$G_{\text{int}} = \text{SU}(4)_C \otimes \text{SU}(2)_L \otimes \text{SU}(2)_R$				
SA ₄₂₂	16.33	11.08	0.0218	36.8 ± 1.2
SB ₄₂₂	15.62	12.38	0.0228	34.0 ± 1.2
$G_{\text{int}} = \text{SU}(3)_C \otimes \text{SU}(2)_L \otimes \text{SU}(2)_R \otimes \text{U}(1)_{B-L}$				
SA ₃₂₂₁	16.66	8.54	0.0217	38.1 ± 1.2
SB ₃₂₂₁	16.17	9.80	0.0223	36.2 ± 1.2
SC ₃₂₂₁	15.62	9.14	0.0230	34.0 ± 1.2
$G_{\text{int}} = \text{SU}(3)_C \otimes \text{SU}(2)_L \otimes \text{SU}(2)_R \otimes \text{U}(1)_{B-L} \otimes D$				
SA _{3221D}	15.58	10.08	0.0231	33.8 ± 1.2
SB _{3221D}	15.40	10.44	0.0233	33.1 ± 1.2

Example based on scalar singlet DM (SA₃₂₂₁) with

$$G_{\text{int}} = \text{SU}(3)_C \otimes \text{SU}(2)_L \otimes \text{SU}(2)_R \otimes \text{U}(1)_{B-L}$$

Kadastik, Kannike, Raidal;
Mambrini, Nagata, Olive, Zheng

Summary

- LHC susy and Higgs searches have pushed CMSSM-like models to “corners” or strips
- However, still viable and more so beyond the CMSSM
- But maybe the susy spectrum is very heavy, and was never part of the thermal background, yet the gravitino may still be the dark matter!
- Can we learn more from a UV completion?
- Signatures at the EeV scale?