

Measuring r



Josquin ERRARD
Firenze — Sep 5, 2017





POLARBEAR telescope
5,200m, Atacama desert, Chile

see talk “CMB in Chile” tomorrow

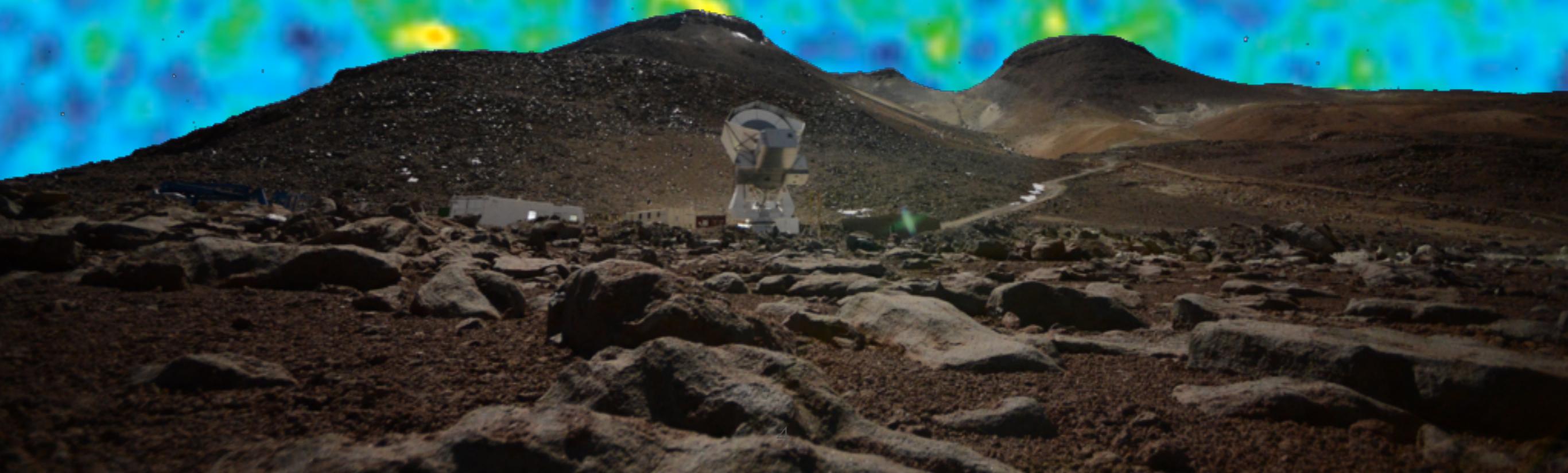
A photograph of a desert landscape under a clear orange sky. In the center, a large yellow sun is visible. In the foreground, there are dark, rocky ground and low hills. In the middle ground, a white building with a large satellite dish on its roof is situated on a hill. A road leads towards the building from the right side of the frame.

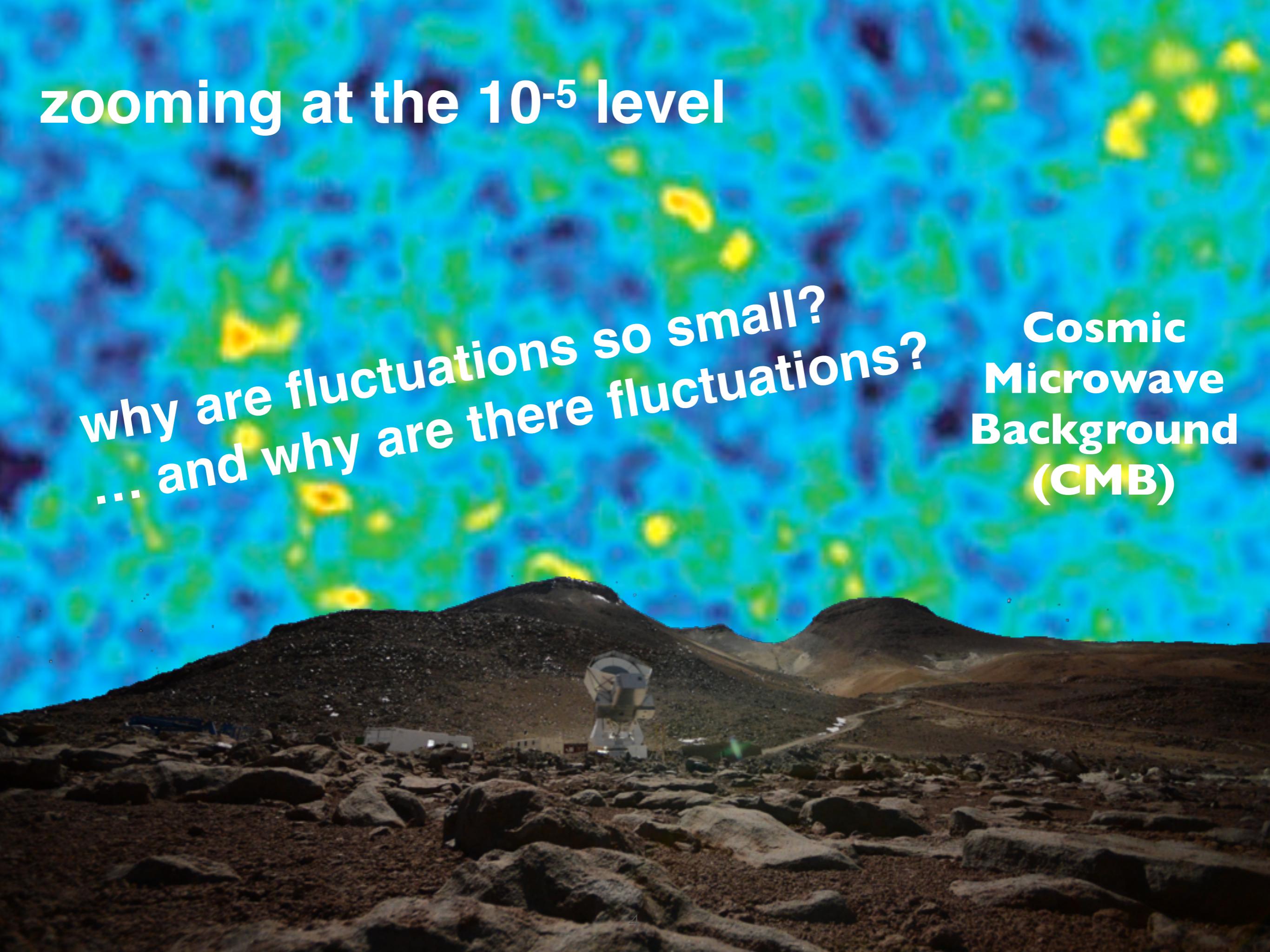
Cosmic Microwave Background (CMB)

POLARBEAR telescope
5,200m, Atacama desert, Chile

zooming at the 10^{-5} level

**Cosmic
Microwave
Background
(CMB)**

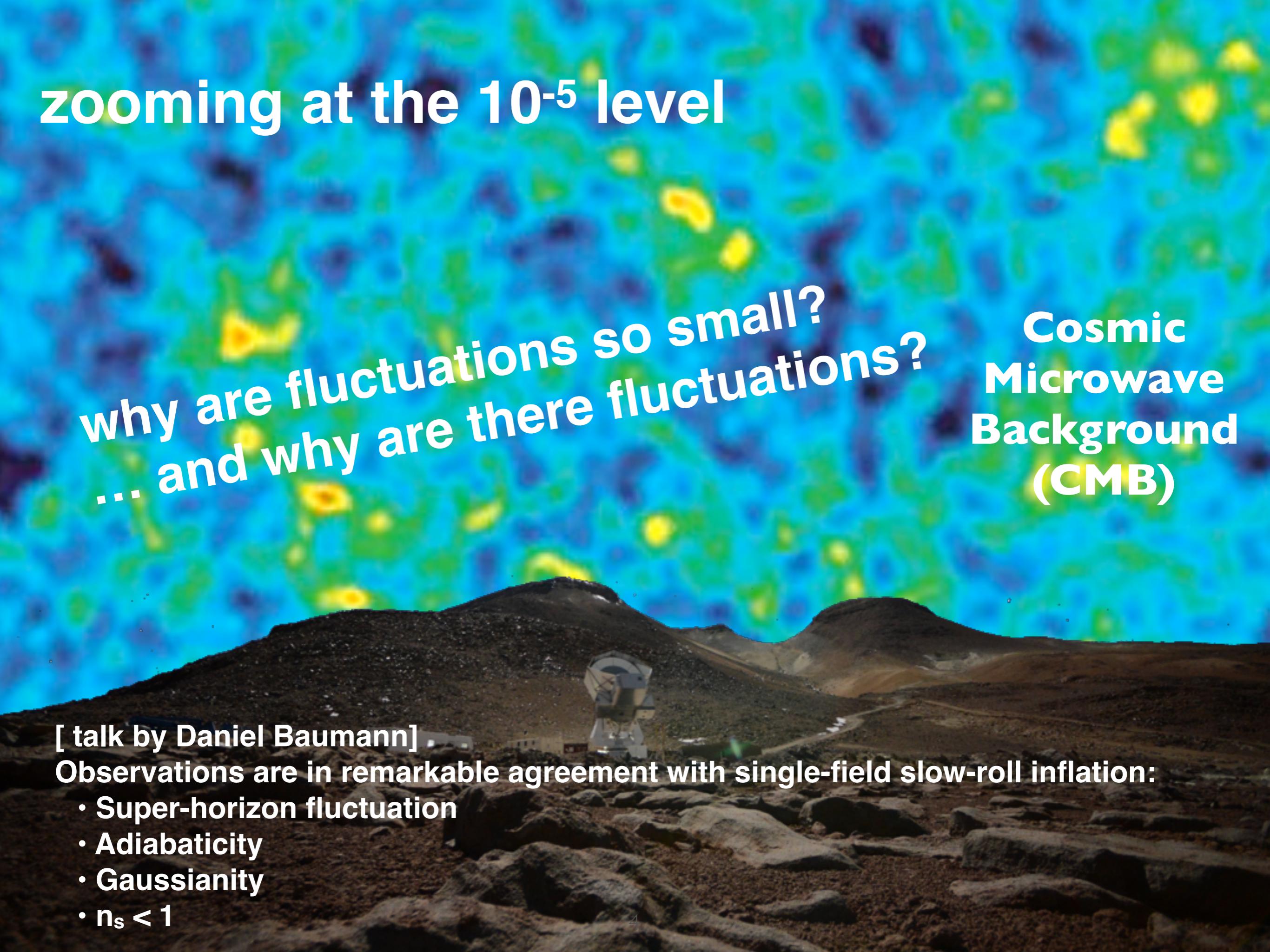




zooming at the 10^{-5} level

why are fluctuations so small?
... and why are there fluctuations?

Cosmic
Microwave
Background
(CMB)



zooming at the 10^{-5} level

why are fluctuations so small?
... and why are there fluctuations?

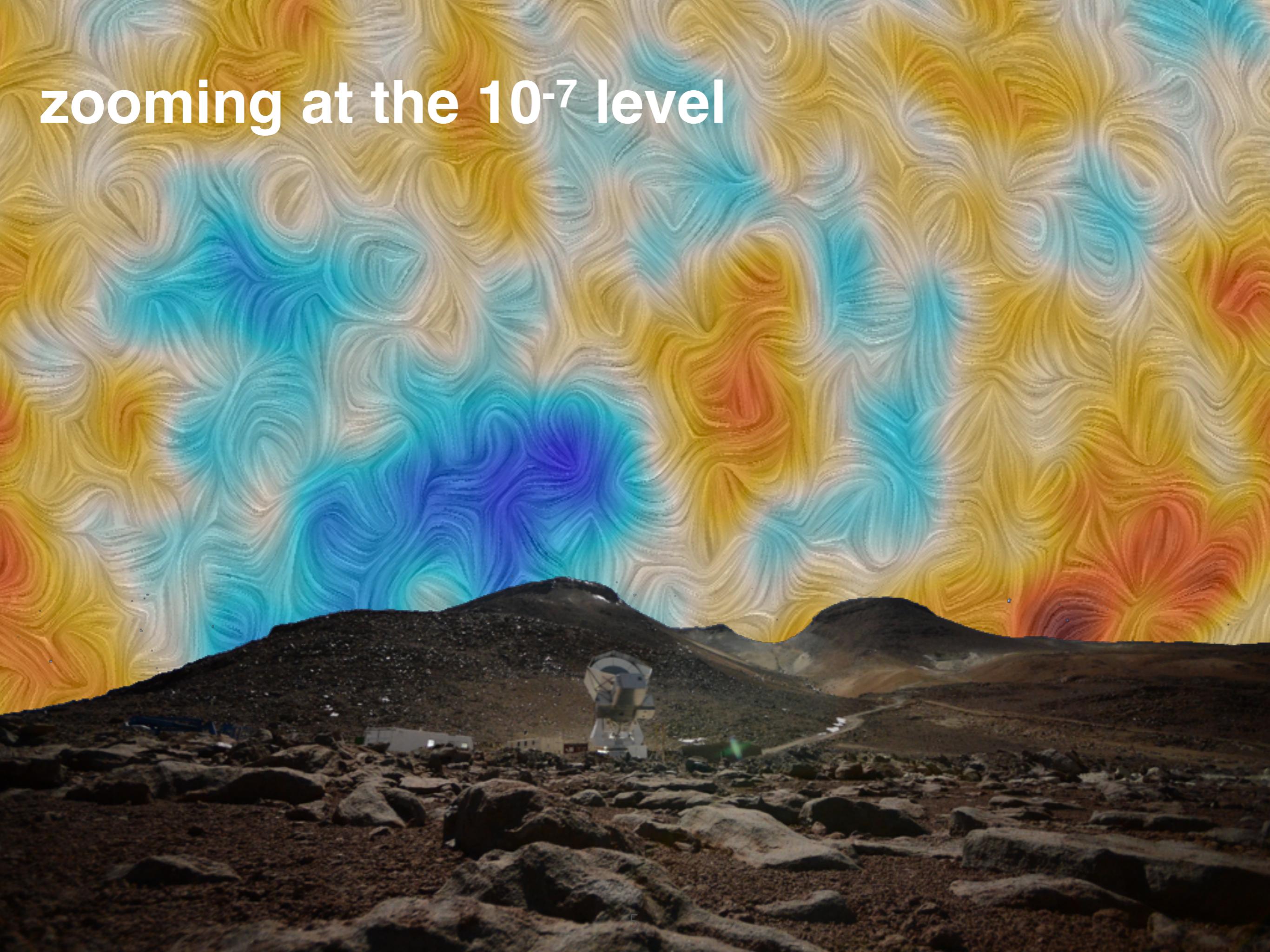
Cosmic
Microwave
Background
(CMB)

[talk by Daniel Baumann]

Observations are in remarkable agreement with single-field slow-roll inflation:

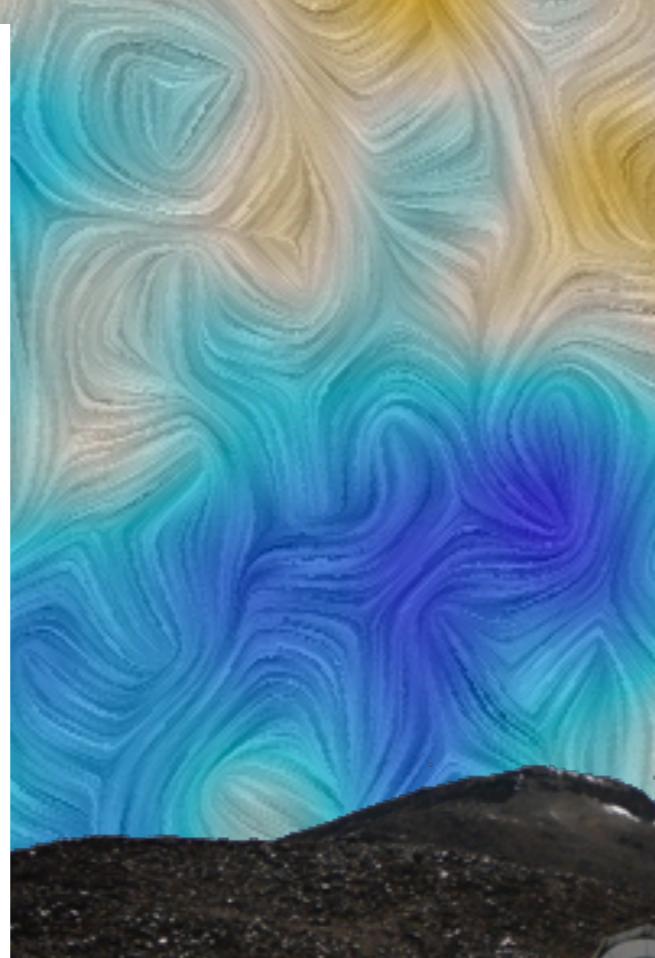
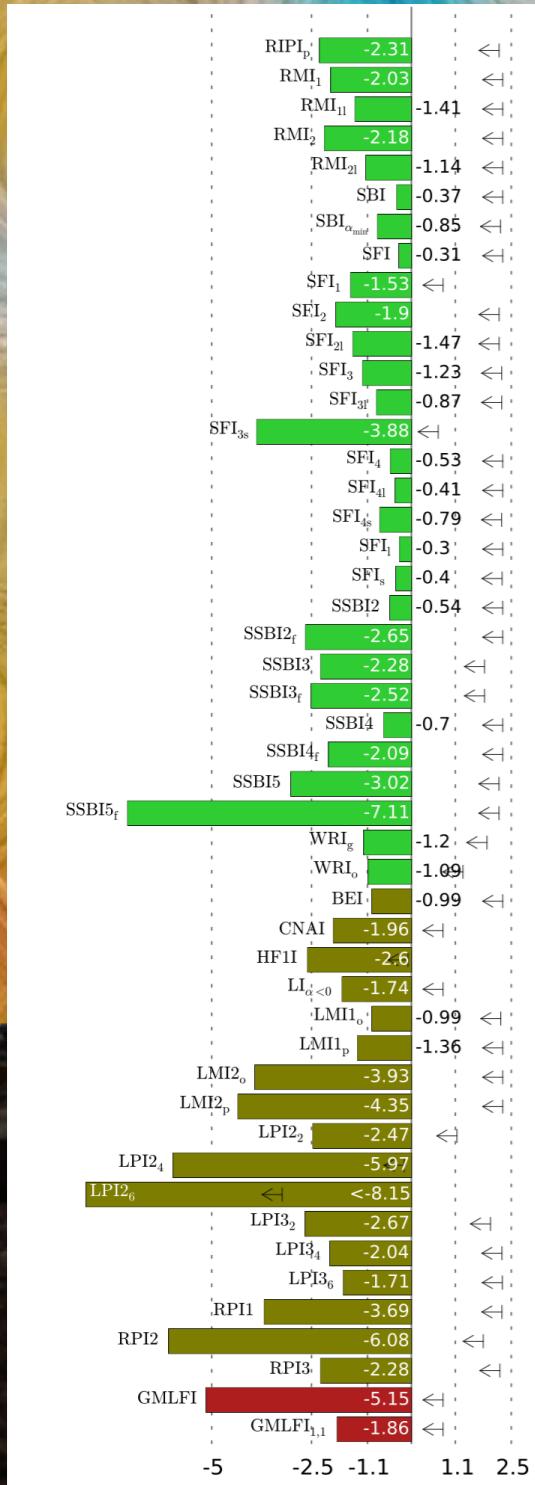
- Super-horizon fluctuation
- Adiabaticity
- Gaussianity
- $n_s < 1$

zooming at the 10^{-7} level



zooming at the 10^{-7} level

► but we want gravitational waves in addition!

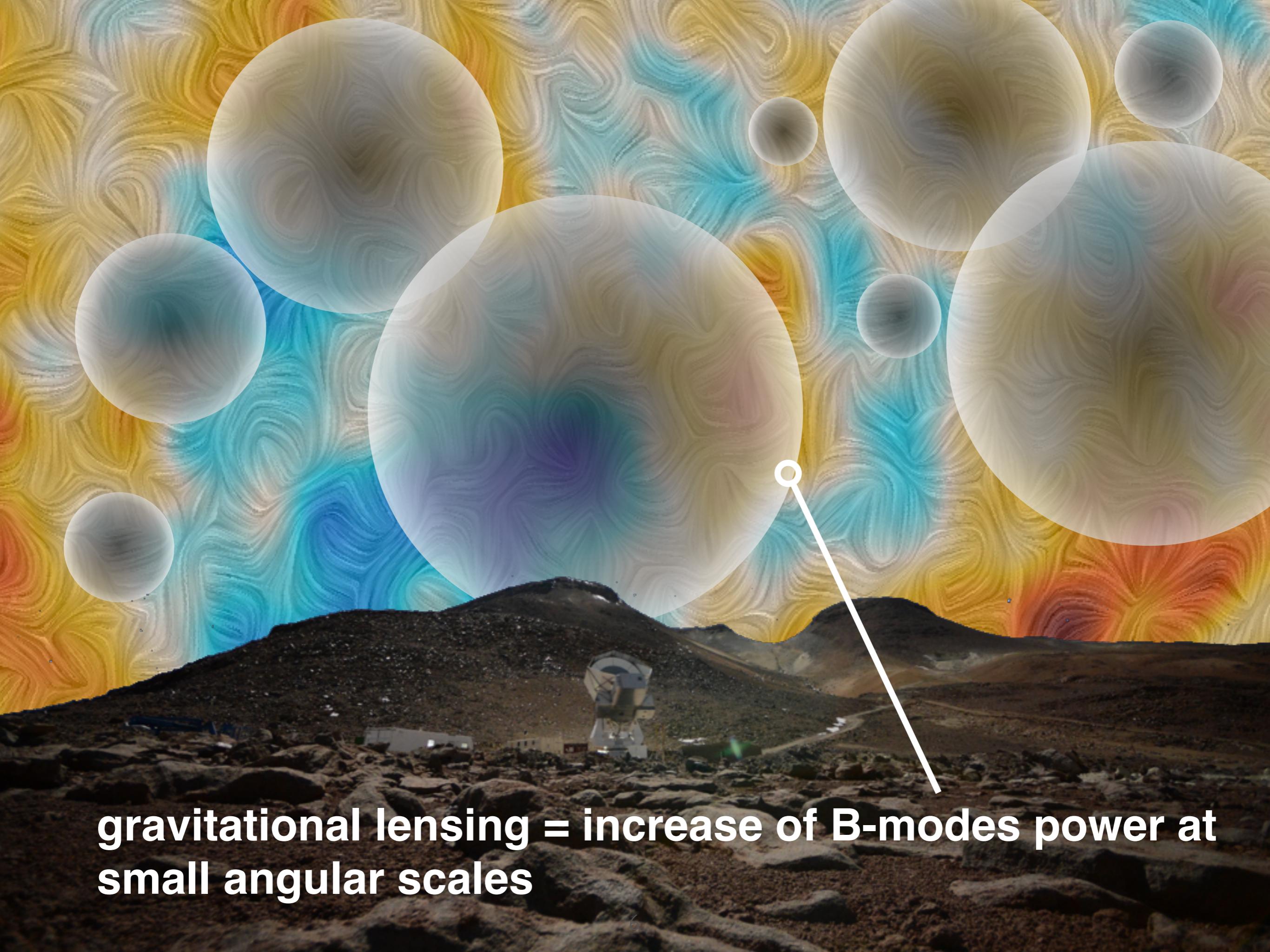


The Best Inflationary Models After Planck
J. Martin, C. Ringeval, R. Trotta, V. Vennin,
JCAP, 2014

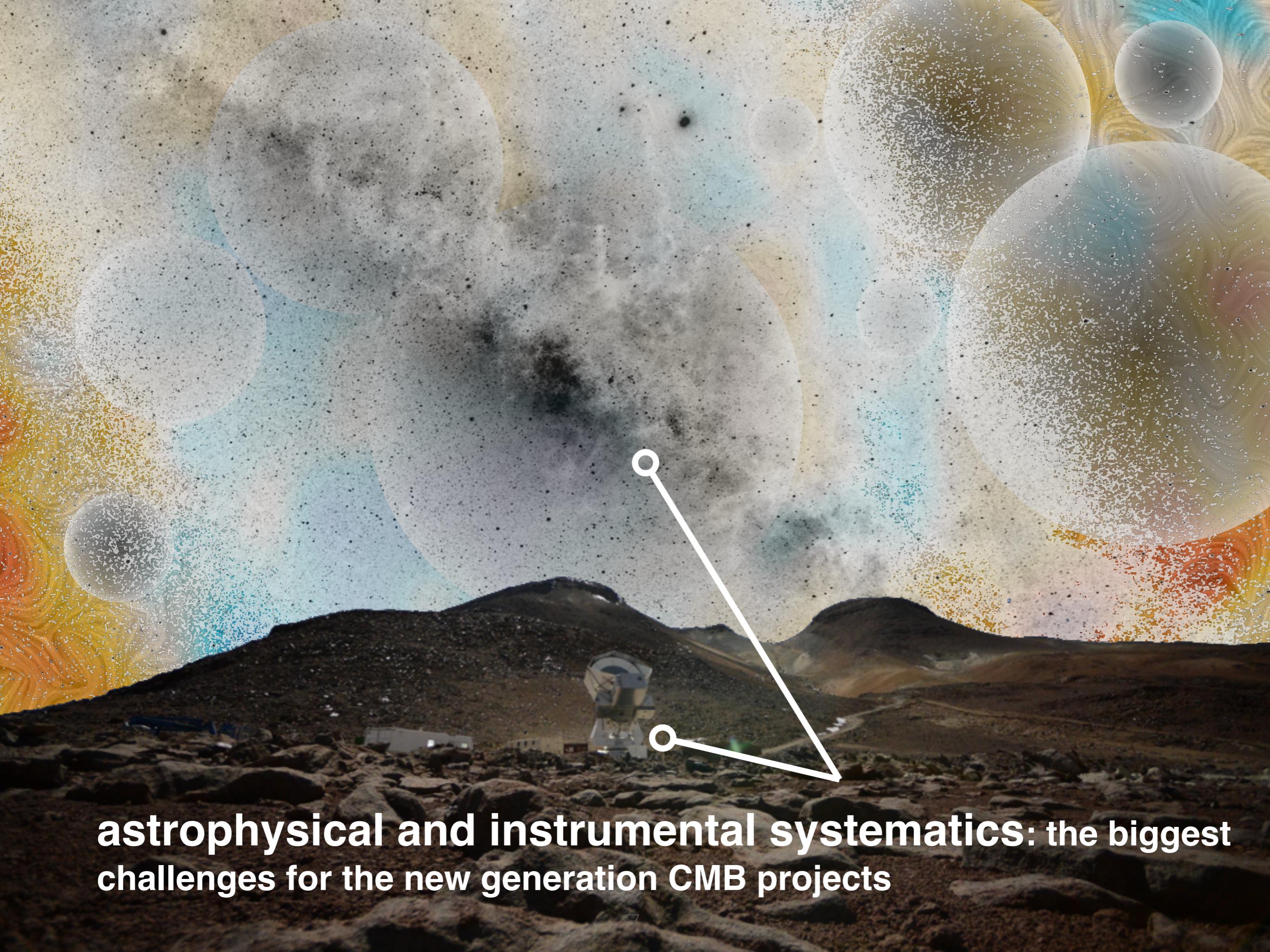
Parameter	Meaning	Physical Origin	Current Status
A_s	Scalar amplitude	H, \dot{H}, c_s	$(2.13 \pm 0.05) \times 10^{-9}$
n_s	Scalar tilt	$\dot{H}, \ddot{H}, \dot{c}_s$	0.965 ± 0.005
$dn_s/d \ln k$	Scalar running	\ddot{H}, \ddot{c}_s	only upper limits
A_t	Tensor amplitude	H	only upper limits
n_t	Tensor tilt	\dot{H}	only upper limits
r	Tensor-to-scalar ratio	\dot{H}, c_s	only upper limits
Ω_k	Curvature	Initial conditions	only upper limits
f_{NL}	Non-Gaussianity	Extra fields, sound speed, ...	only upper limits
S	Isocurvature	Extra fields	only upper limits
$G\mu$	Topological defects	End of inflation	only upper limits

Table 1: Summary of key parameters in inflationary cosmology, together with their likely physical origins and current observational constraints. At present, only upper limits exist for all parameters except A_s and n_s [5].

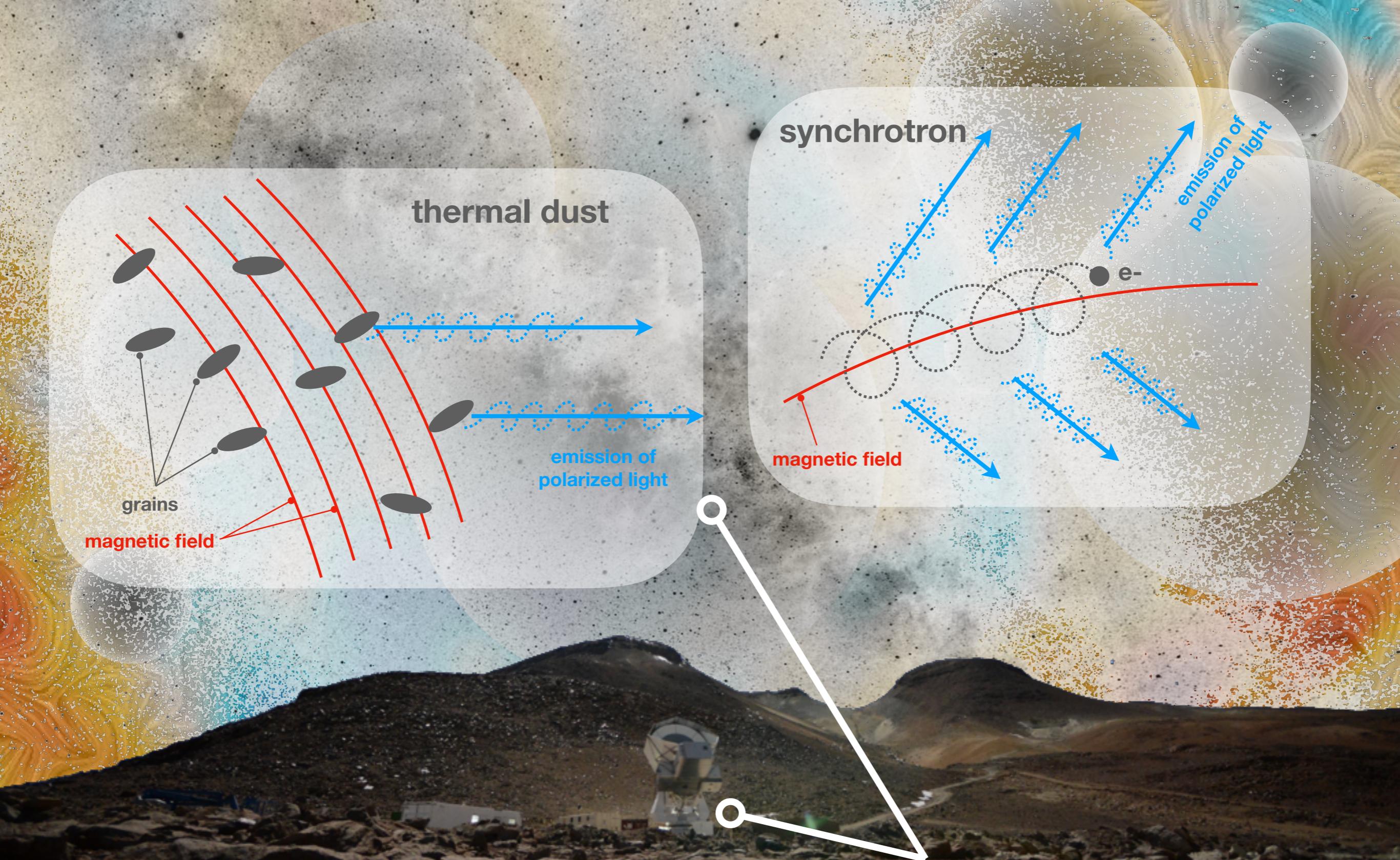
Exploring Cosmic Origins with CORE: Inflation
F. Finelli, M. Bucher et al., JCAP, 2017



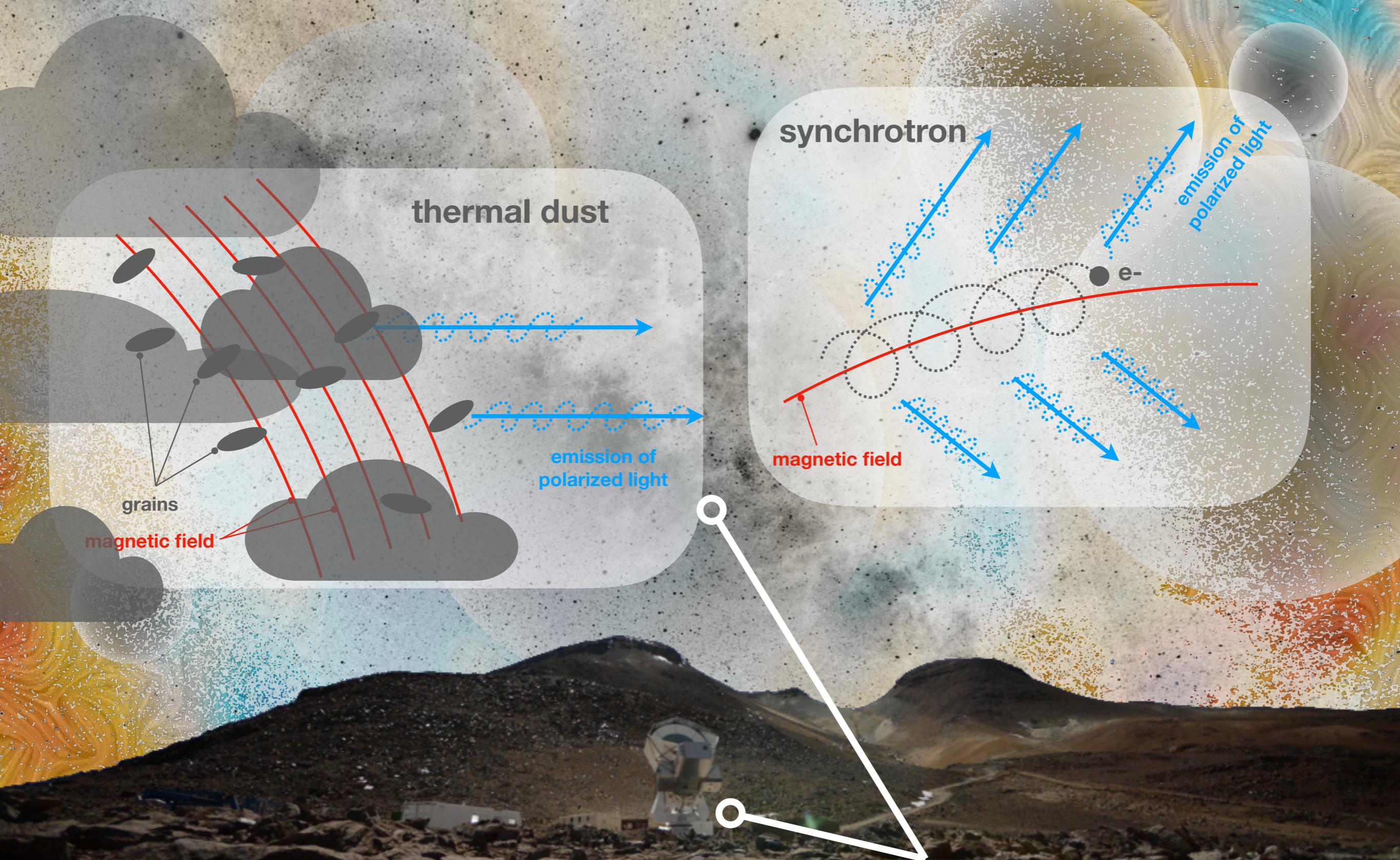
gravitational lensing = increase of B-modes power at small angular scales



astrophysical and instrumental systematics: the biggest challenges for the new generation CMB projects

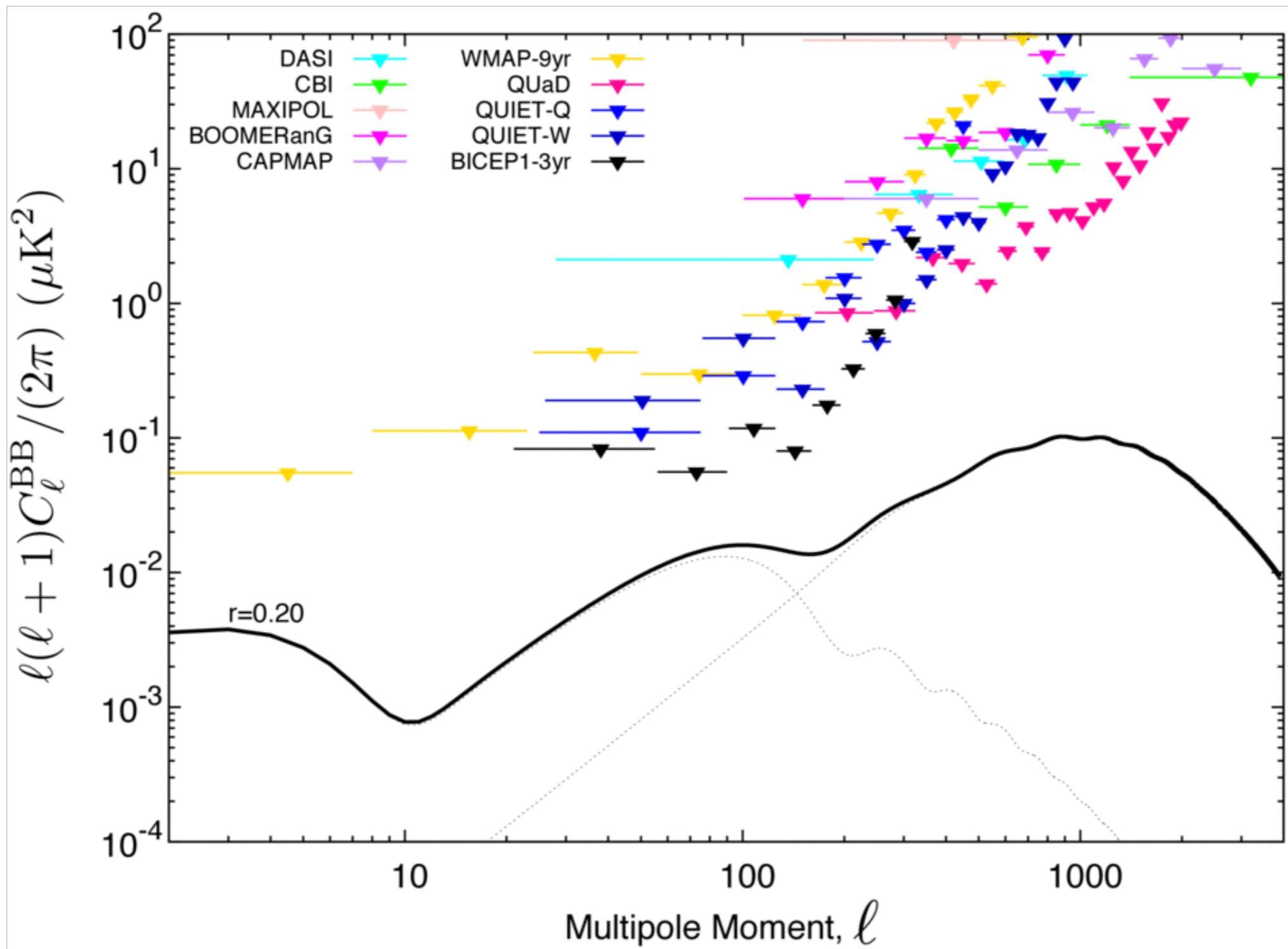


astrophysical and instrumental systematics: the biggest challenges for the new generation CMB projects

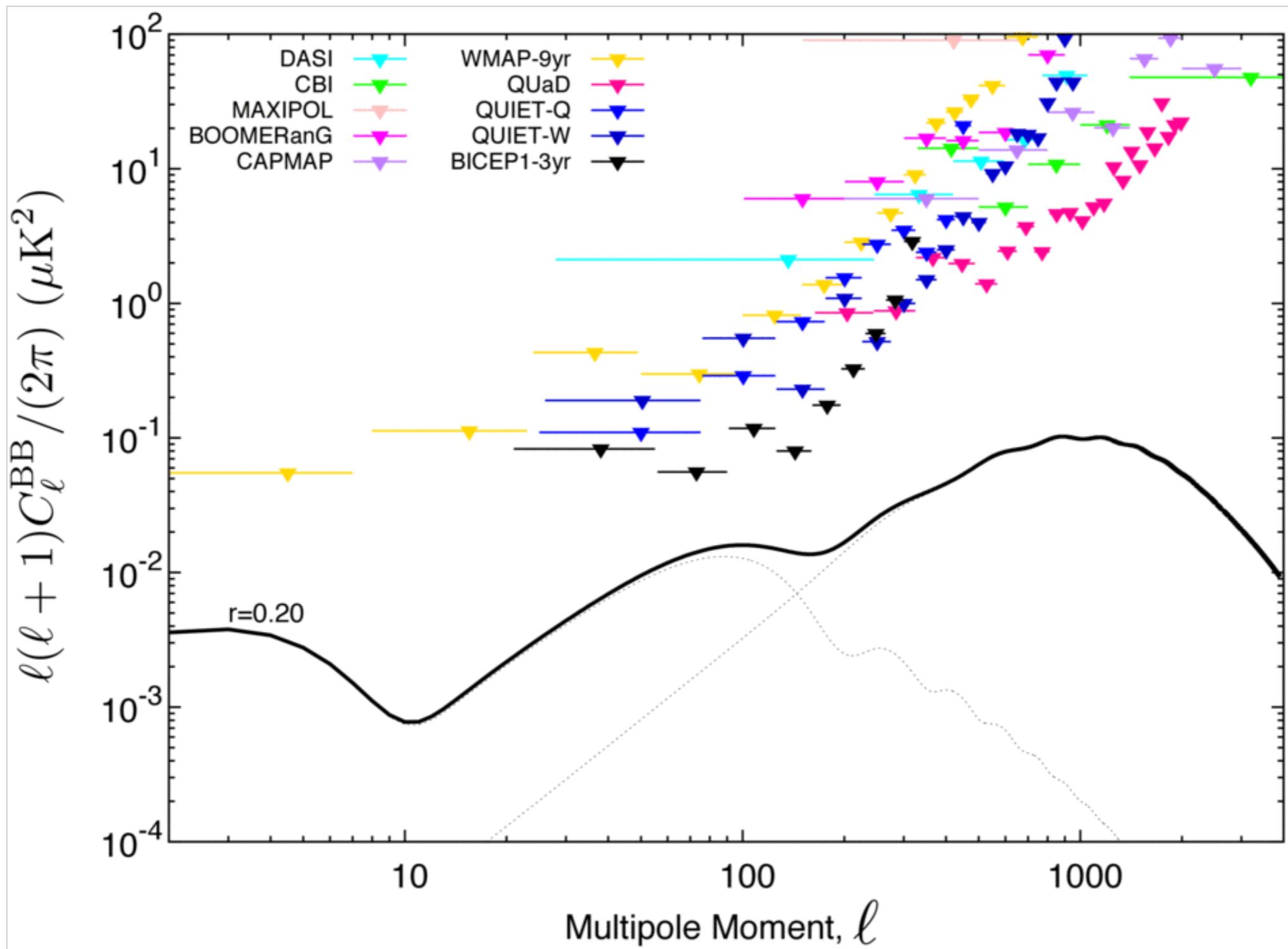


astrophysical and instrumental systematics: the biggest challenges for the new generation CMB projects

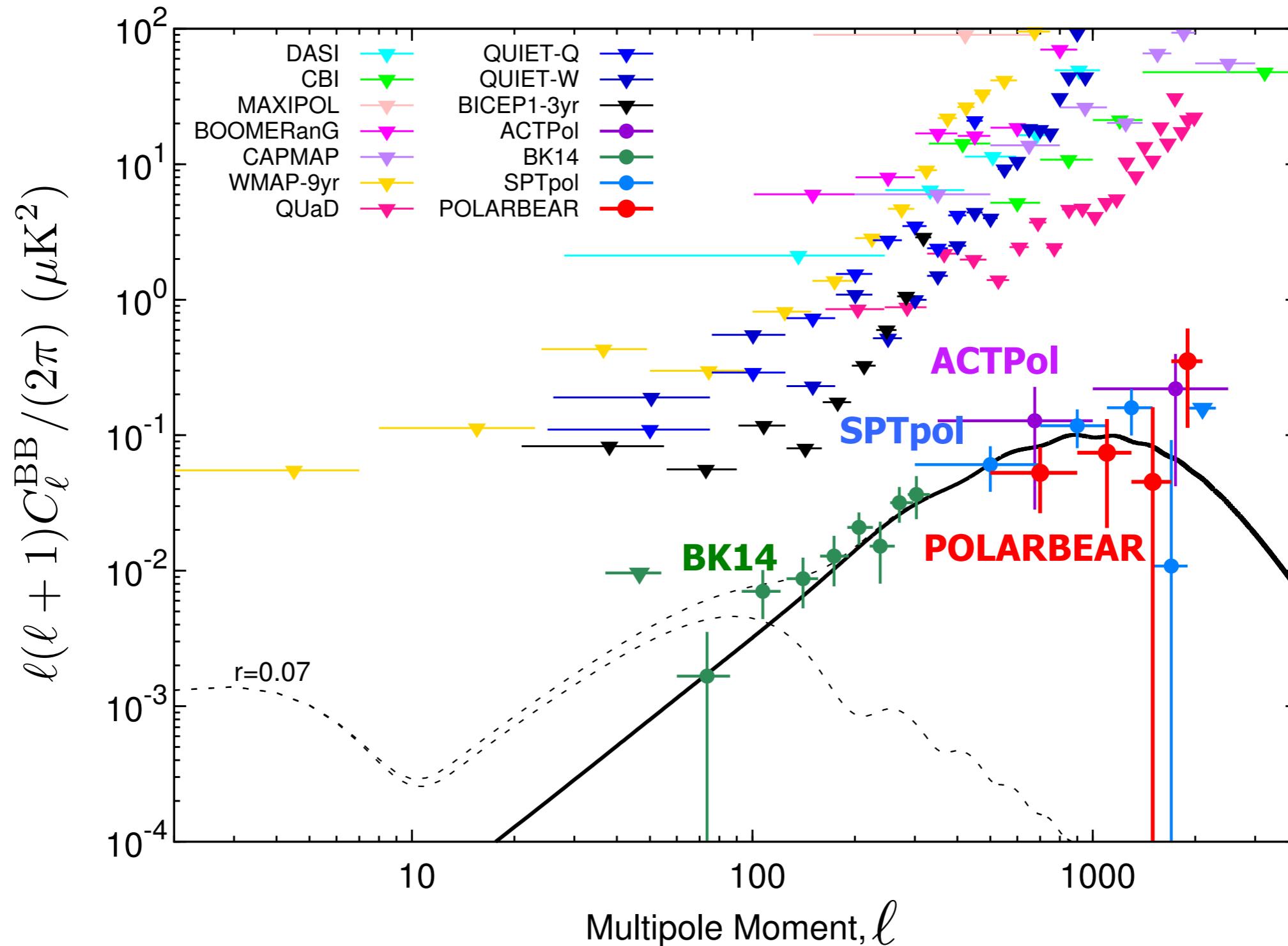
Recent history of direct BB detection



Recent history of direct BB detection

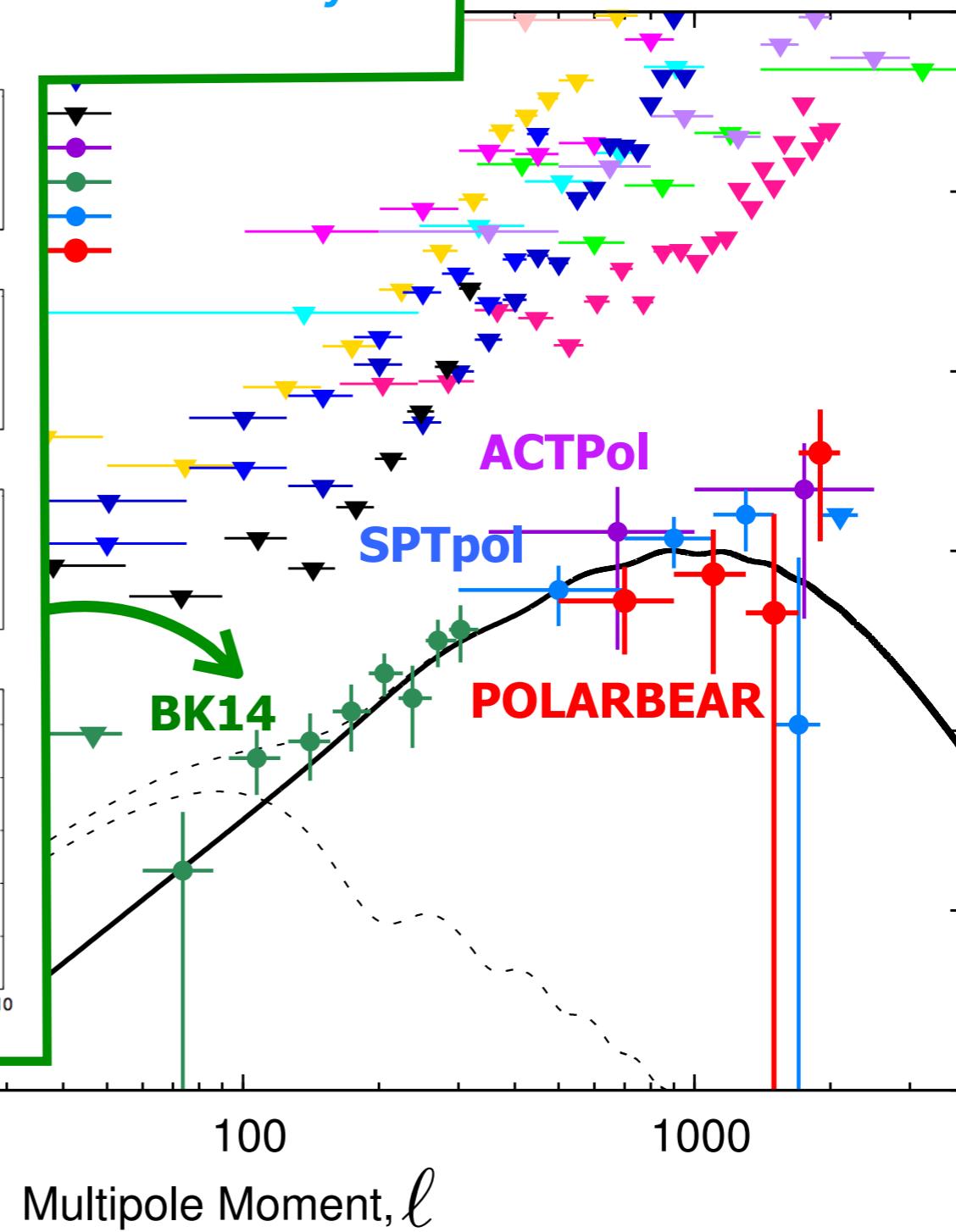
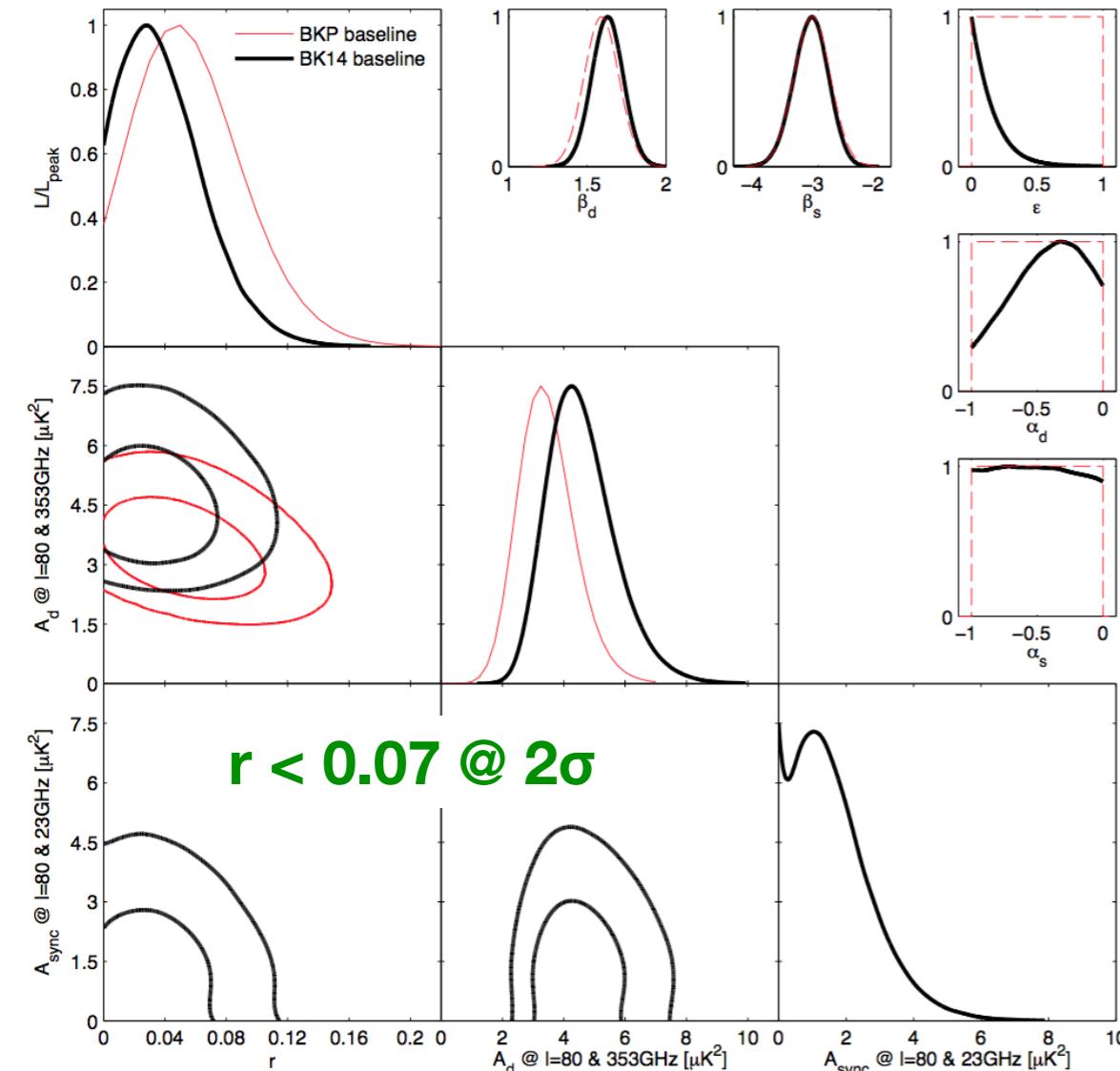


Recent history of direct BB detection

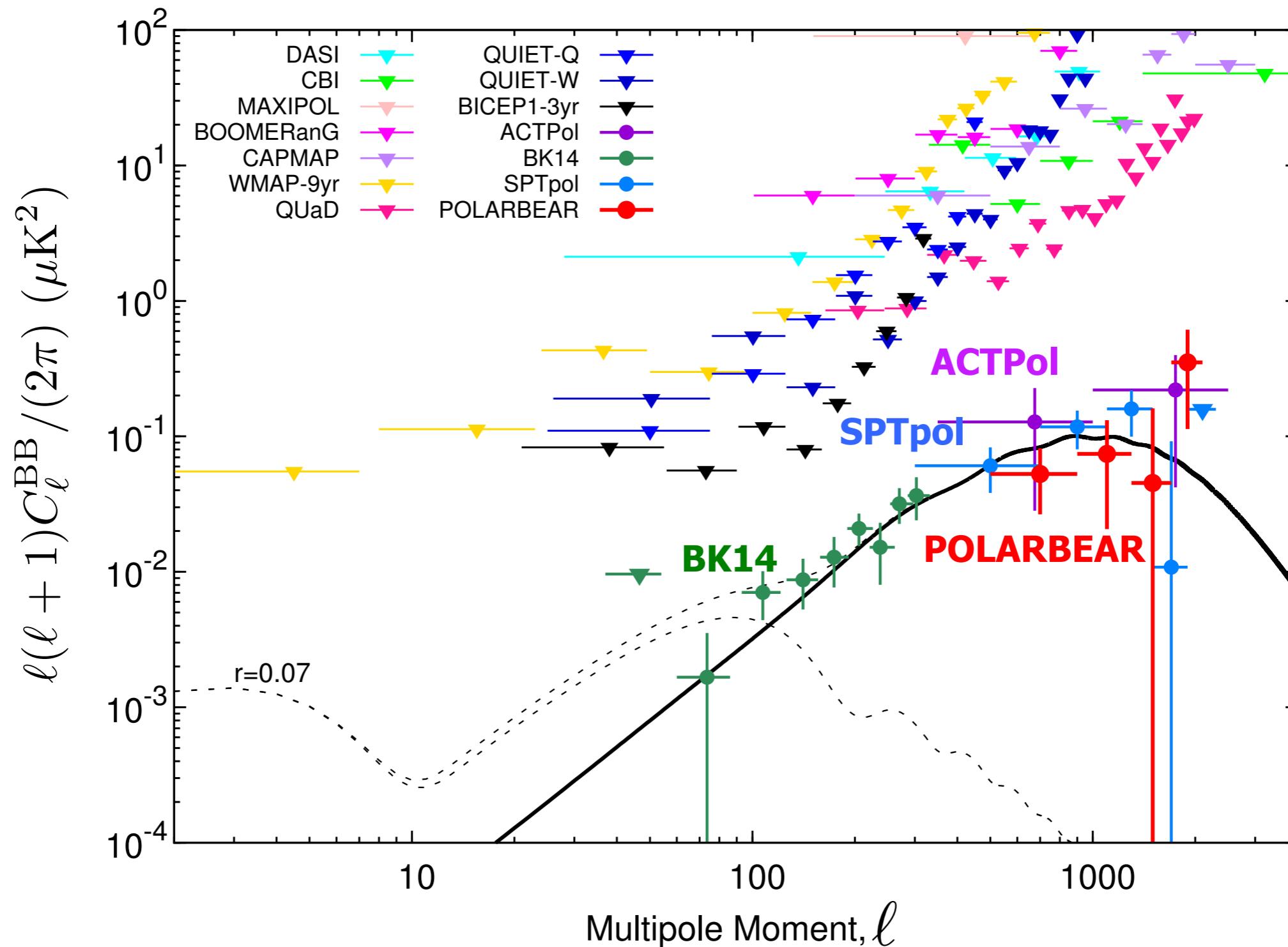


Recent history of direct BB detection

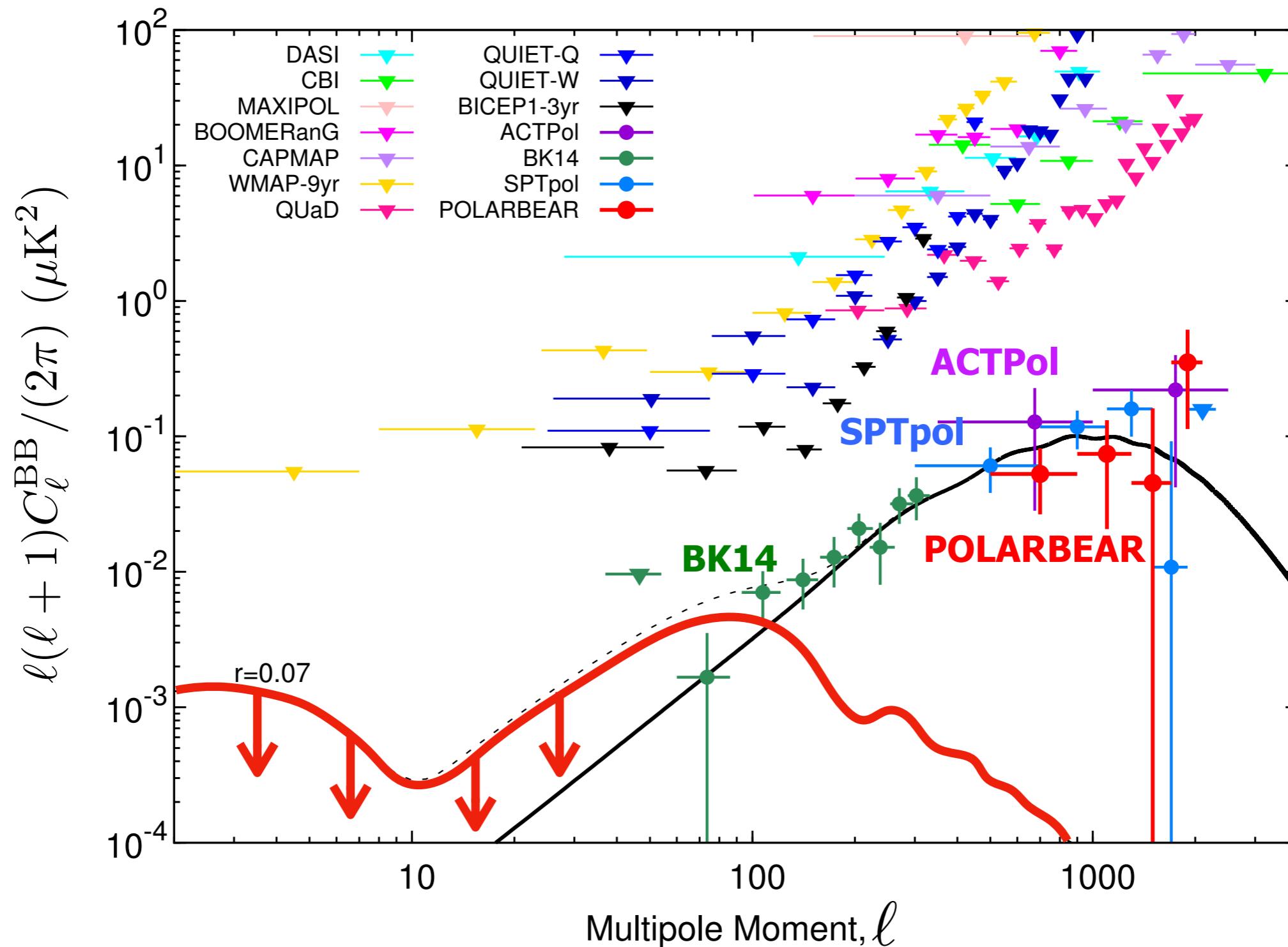
BICEP2 / Keck Array VI: Improved Constraints On Cosmology and Foregrounds When Adding 95 GHz Data From Keck Array
 Keck Array and BICEP2 Collaborations



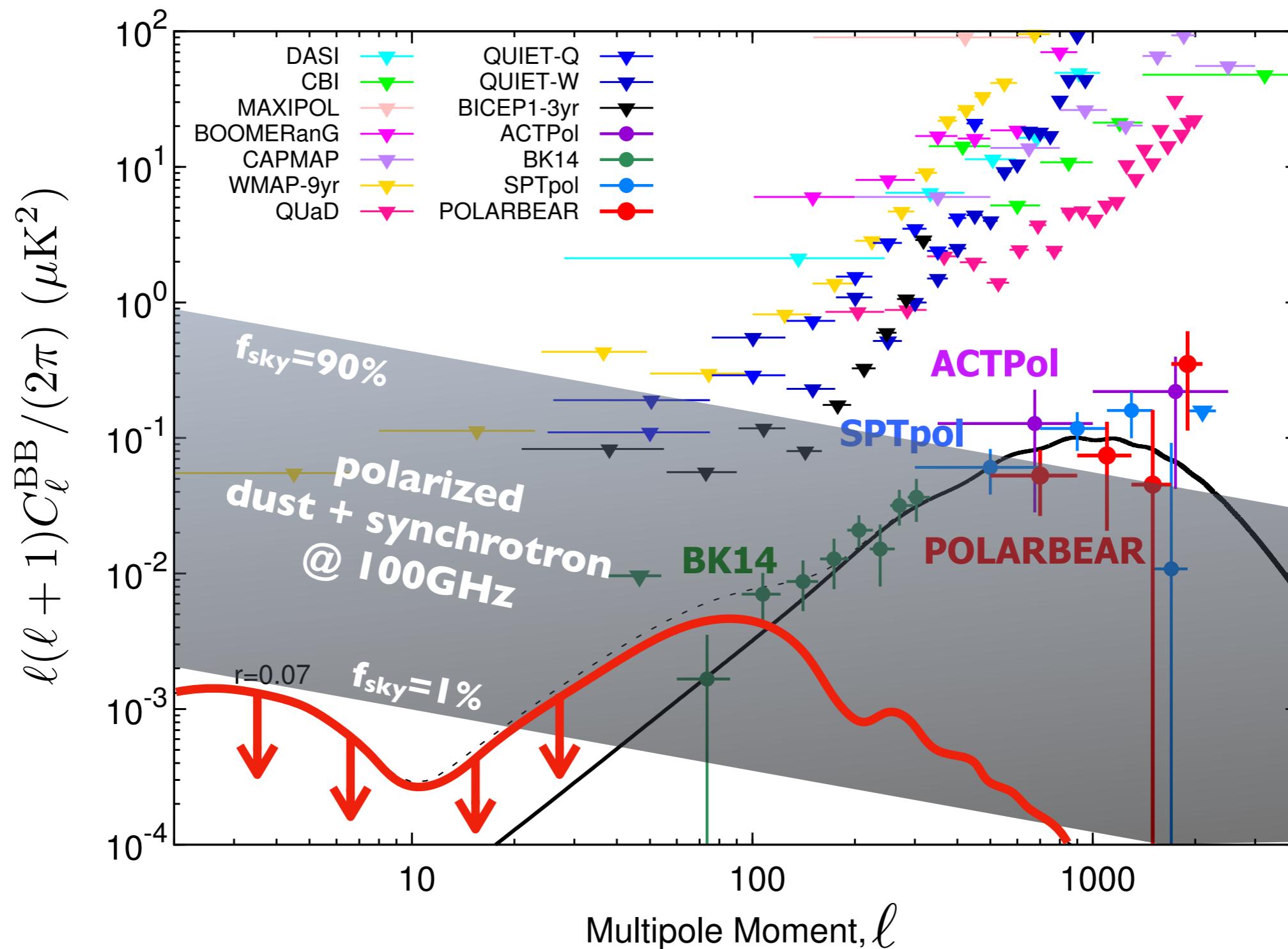
Recent history of direct BB detection



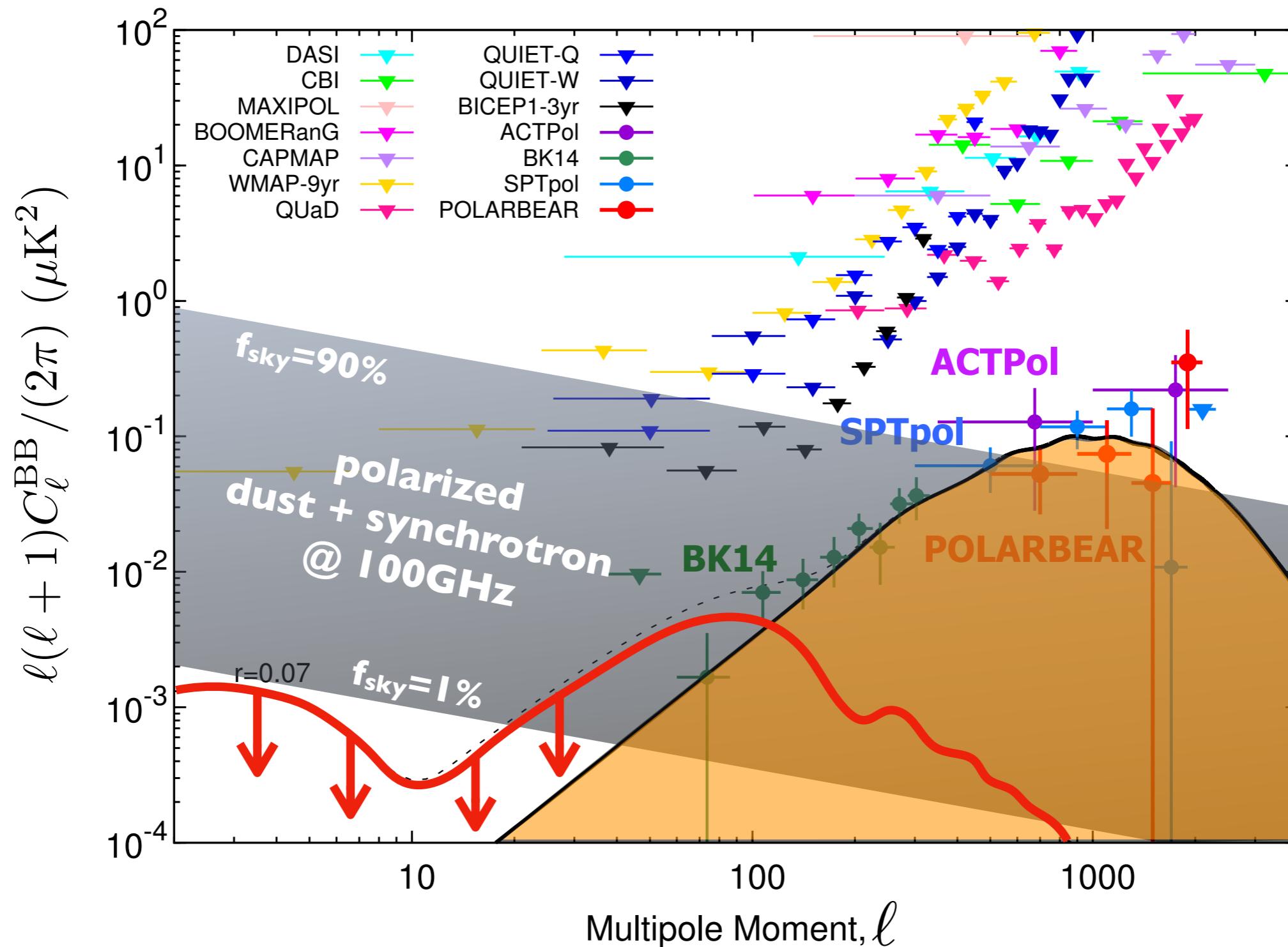
Recent history of direct BB detection



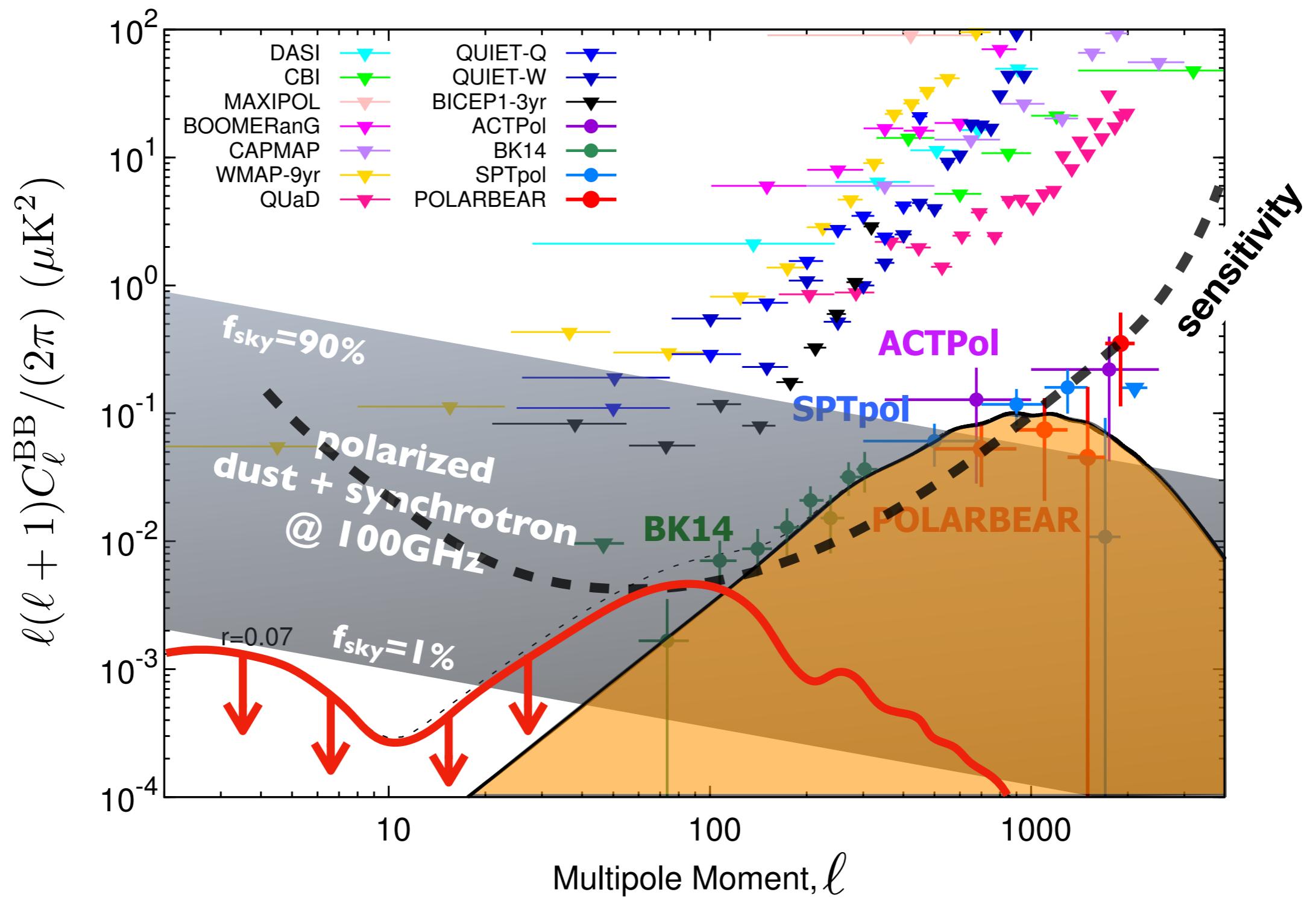
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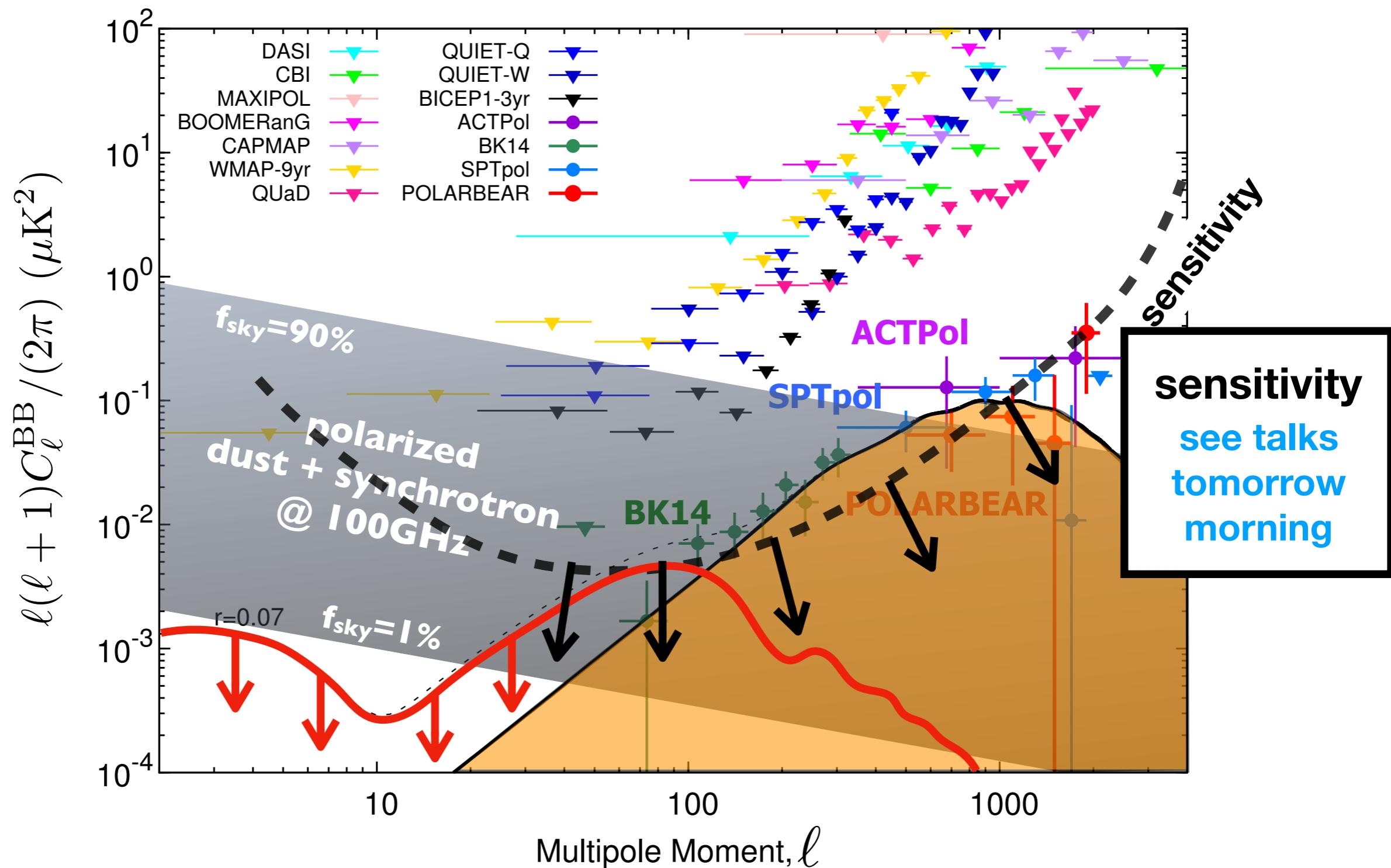
Recent history of direct BB detection



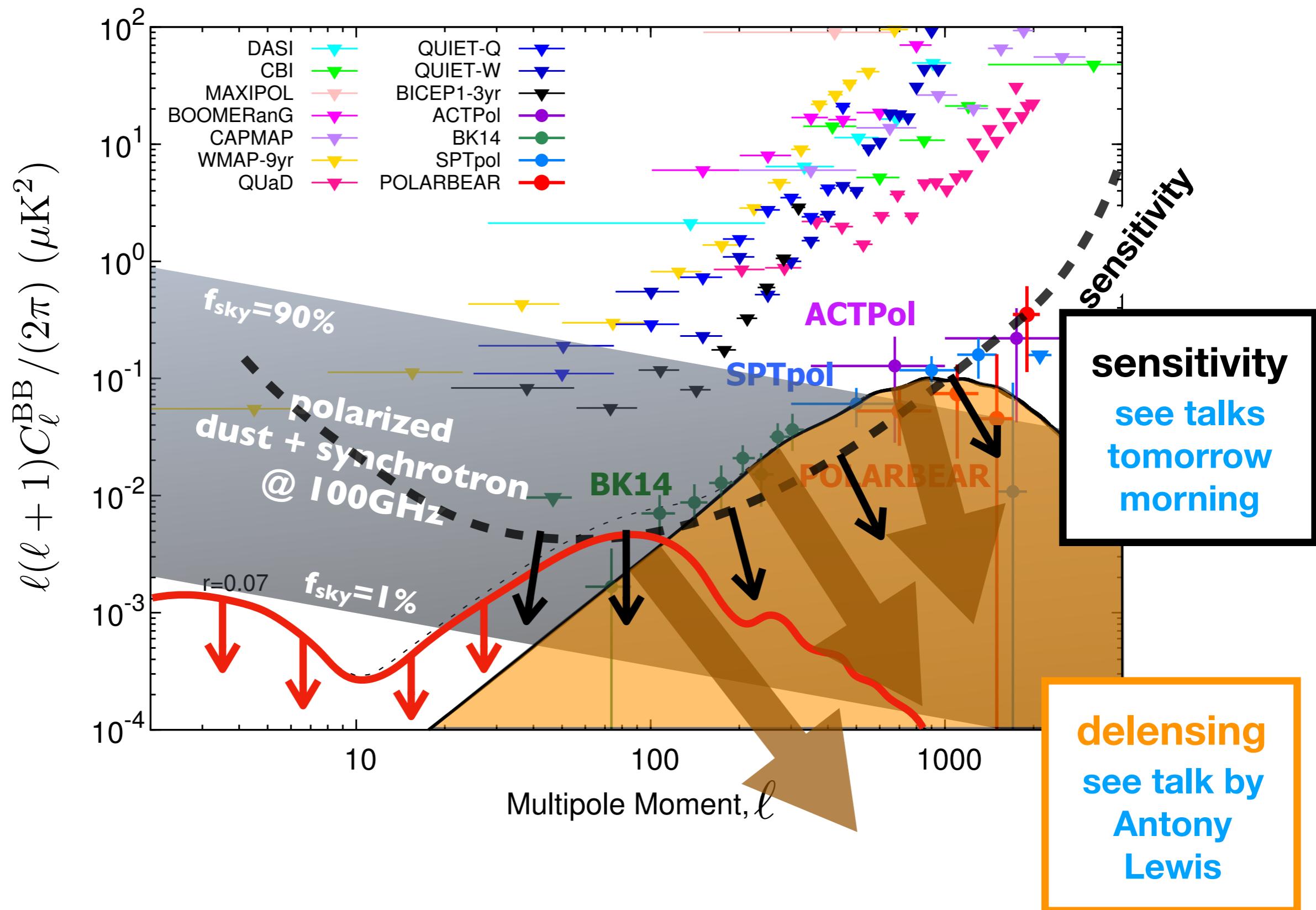
Recent history of direct BB detection



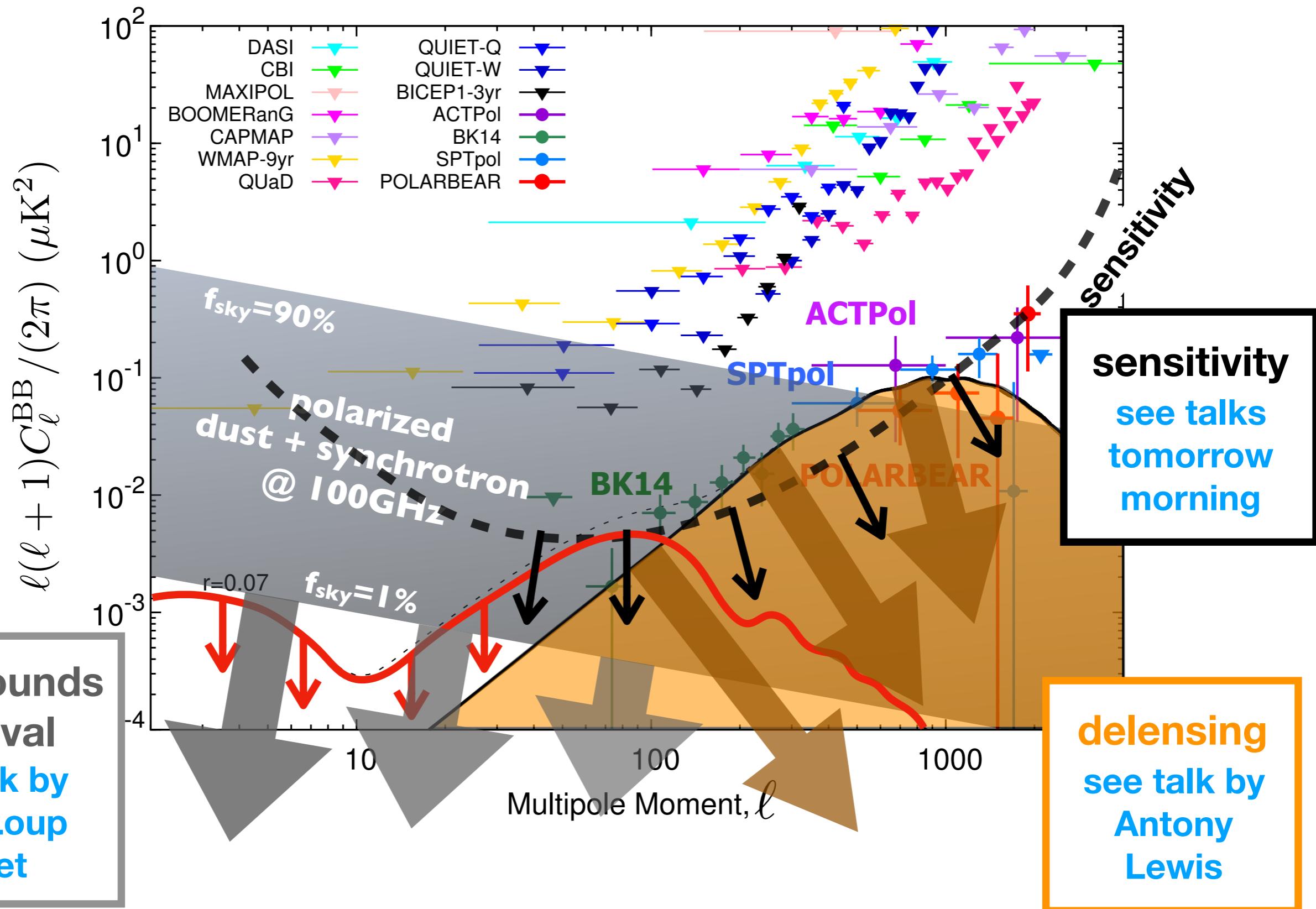
Recent history of direct BB detection

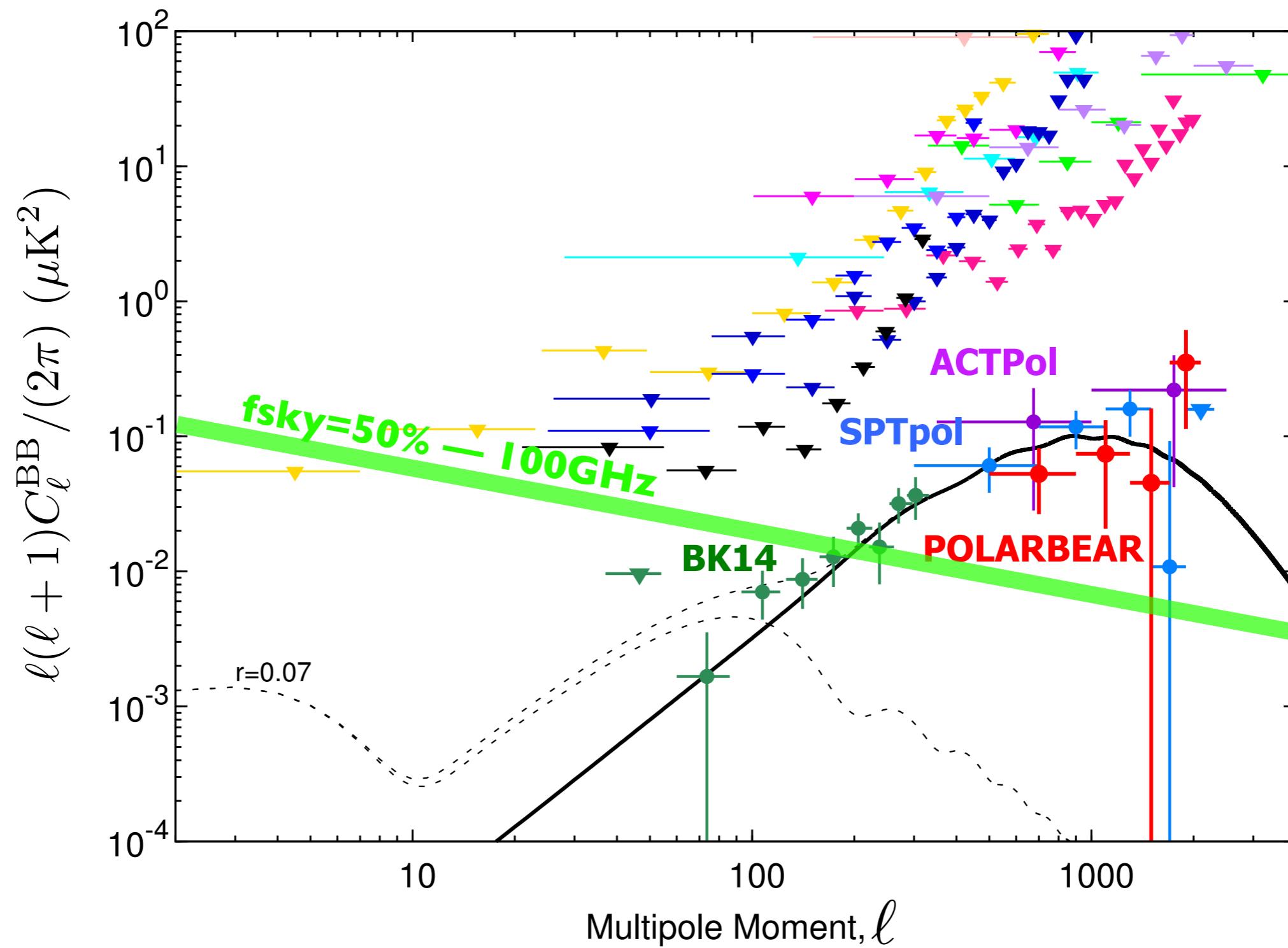


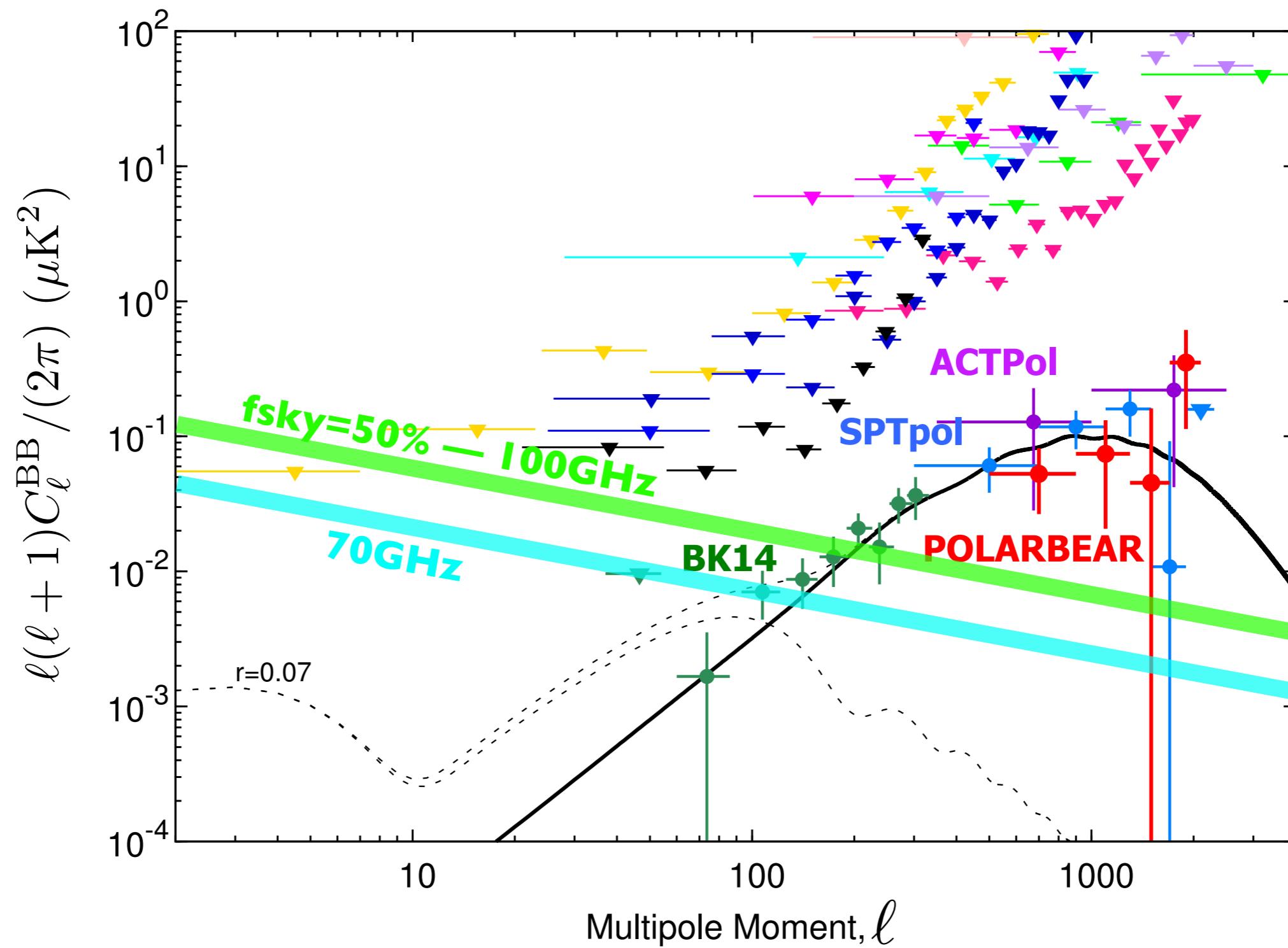
Recent history of direct BB detection

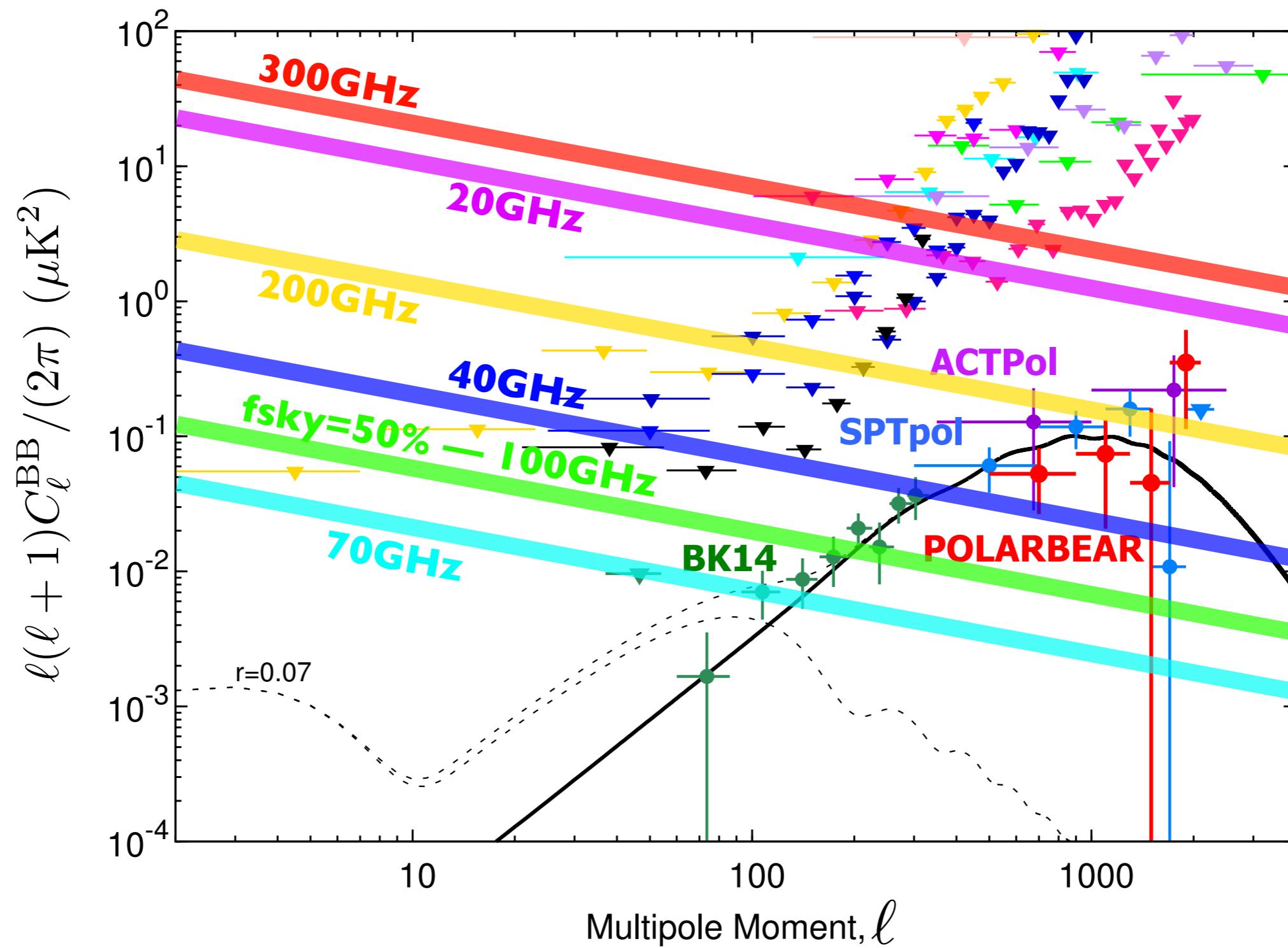


Recent history of direct BB detection





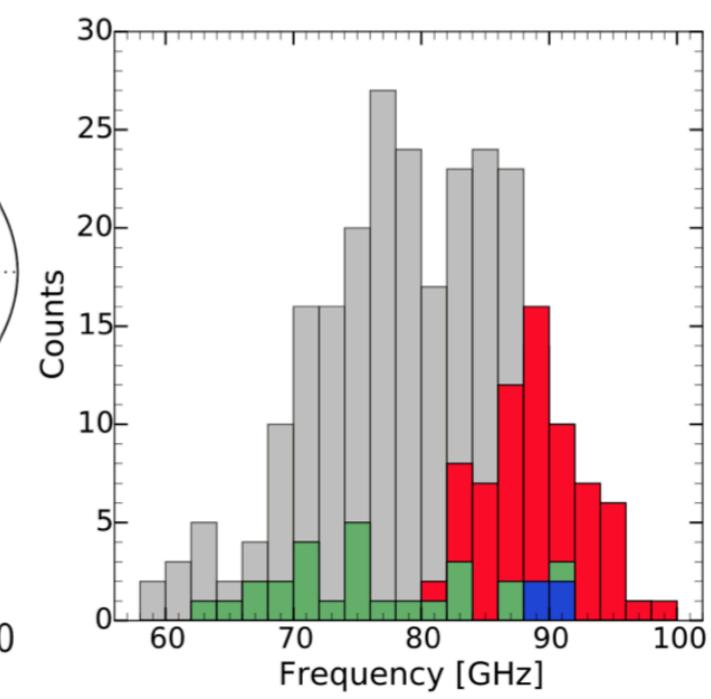
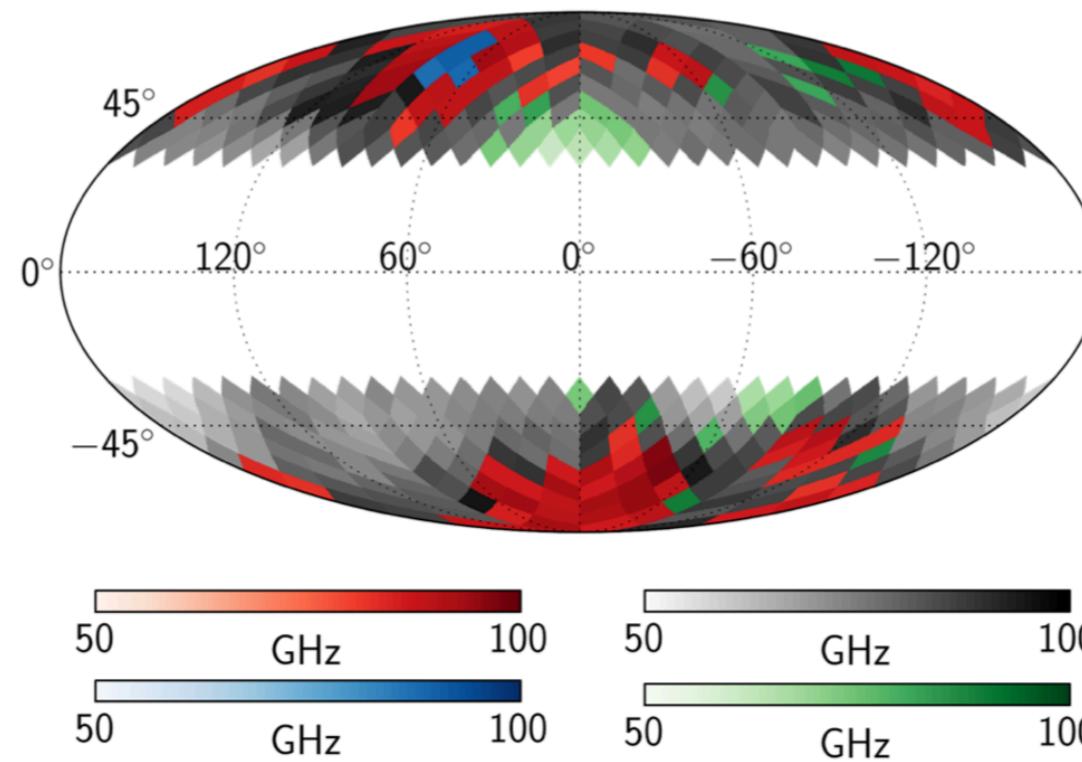
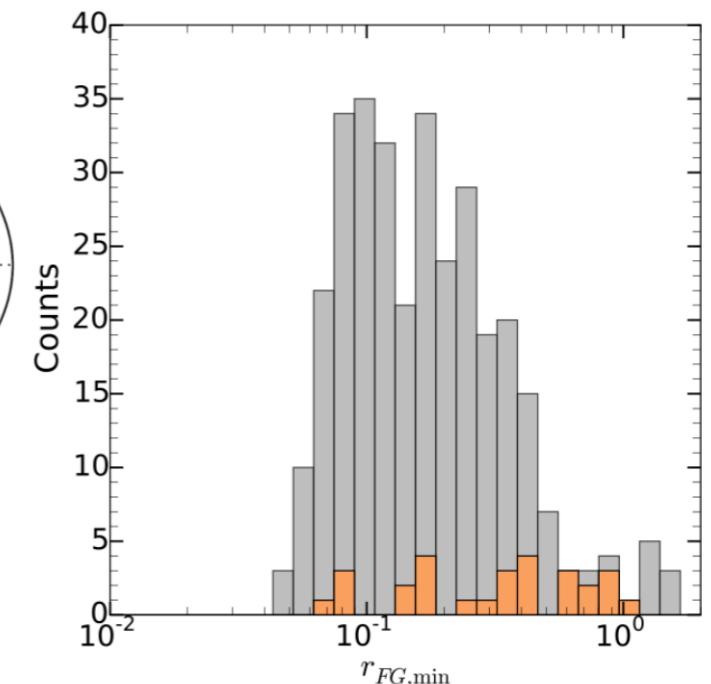
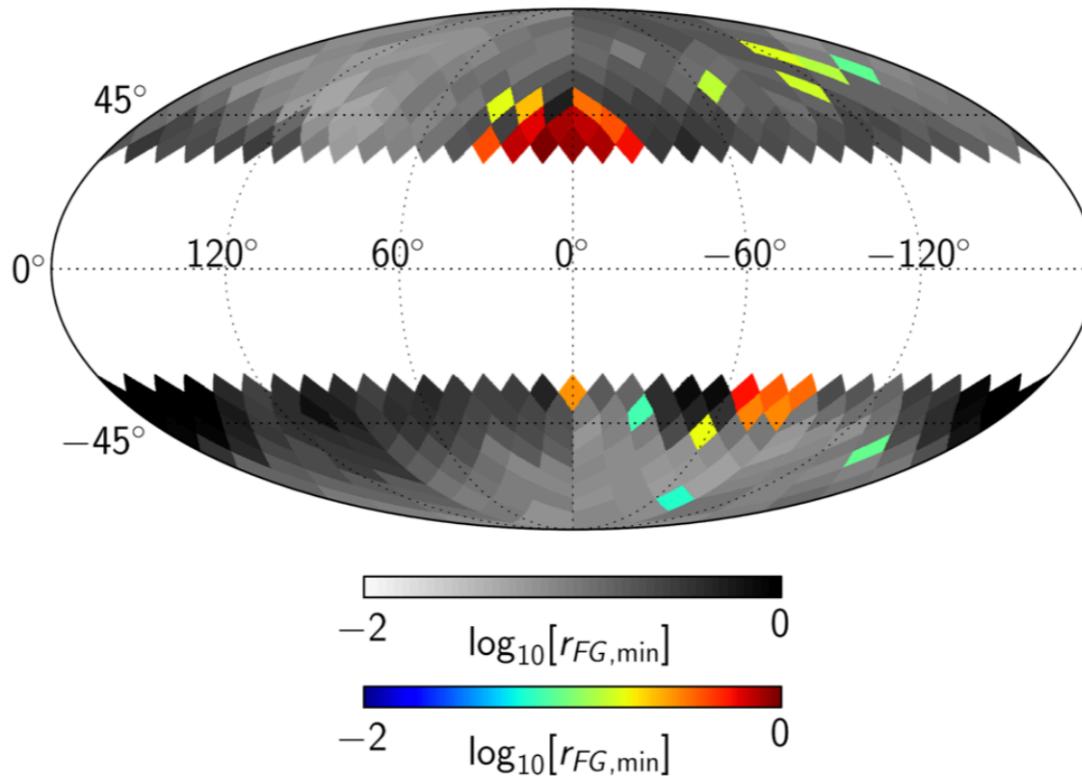




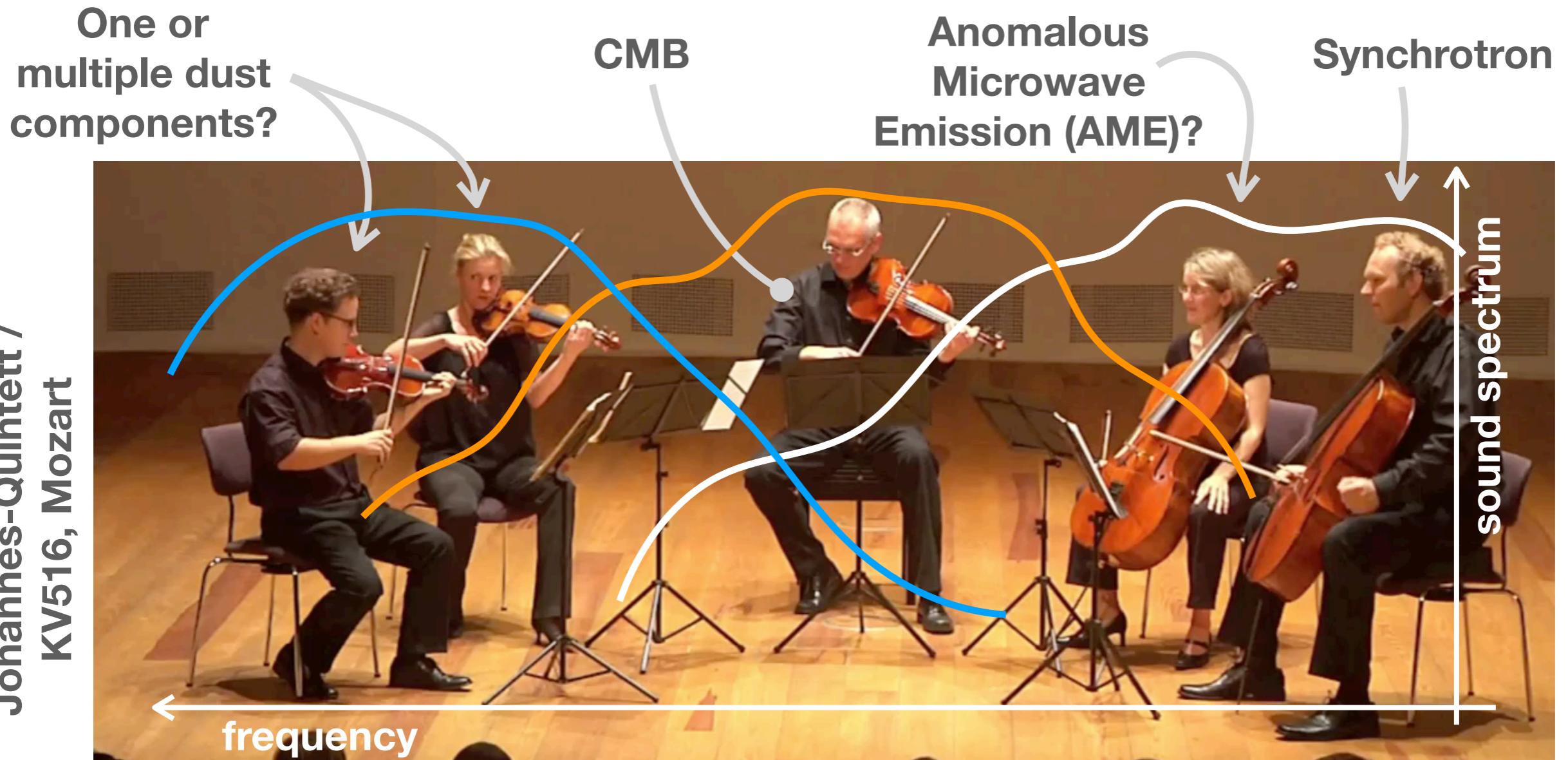
Foregrounds cleaning, option #1 : avoid them?

Characterization of foreground emission at degree angular scale for CMB B-modes observations
N. Krachmalnicoff, C. Baccigalupi et al (2016)

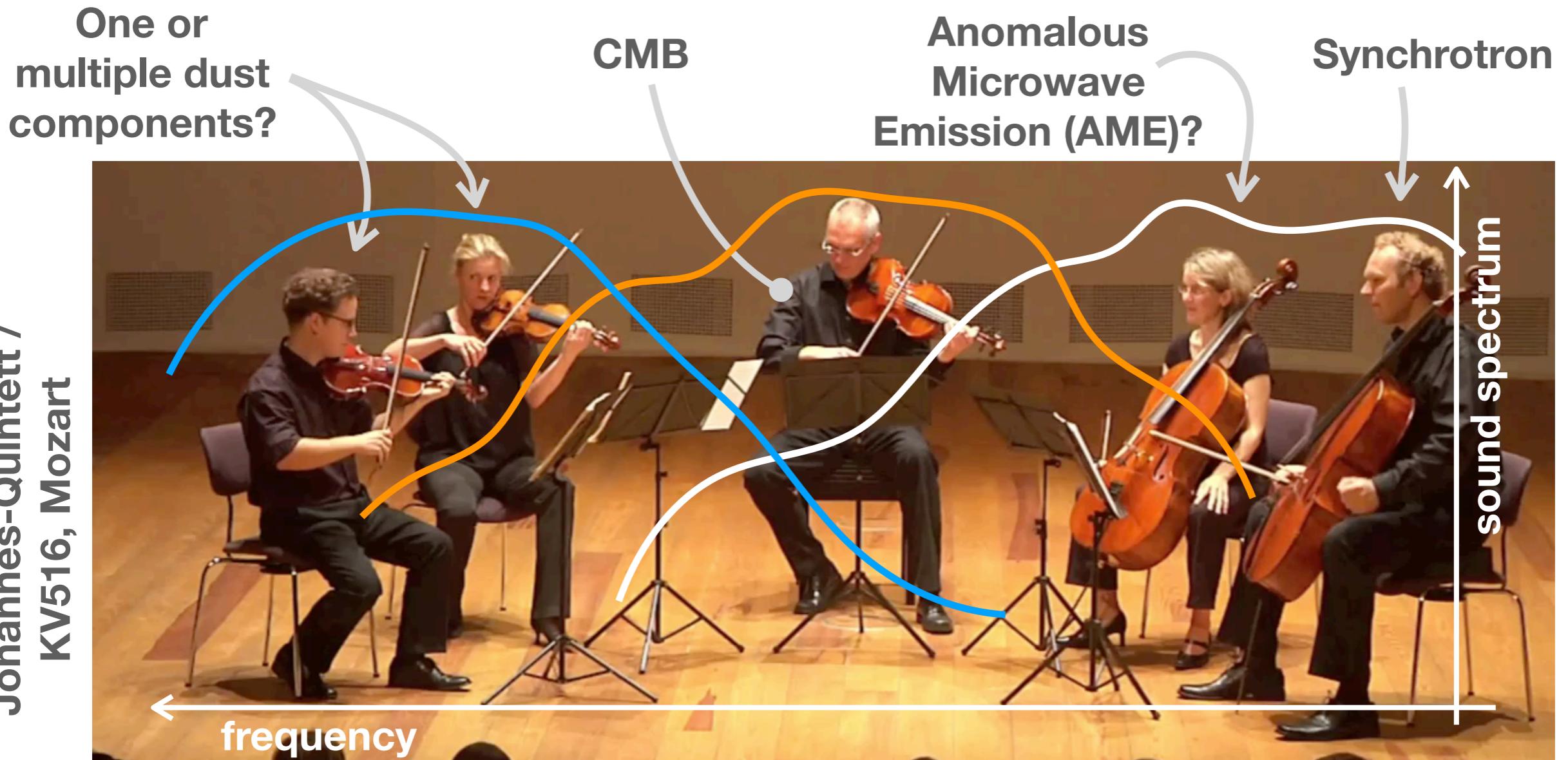
+ **Polarized galactic synchrotron and dust emission and their correlation**
S. K. Choi, L. A. Page (2015)



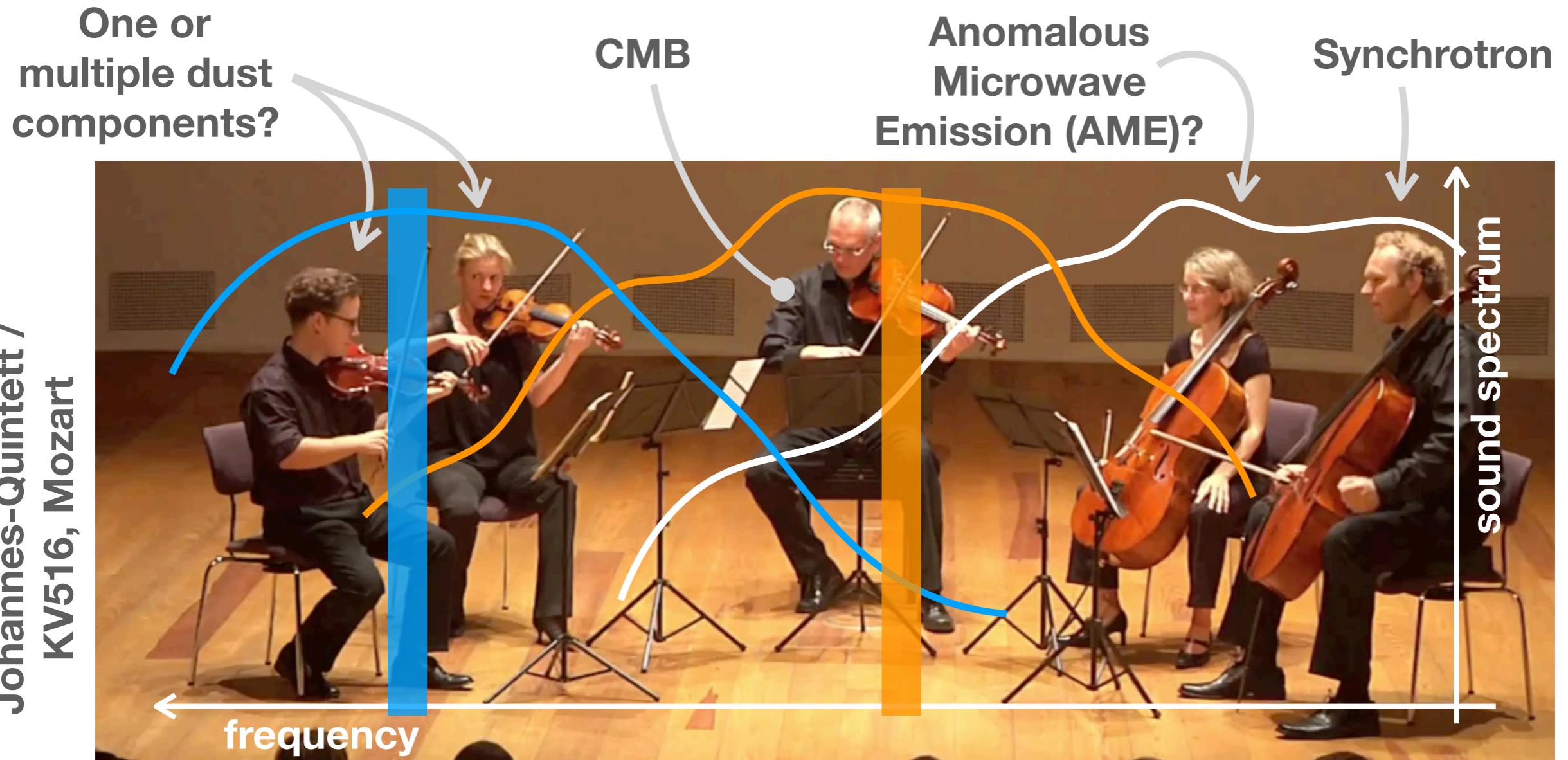
Johannes-Quintett /
KV516, Mozart



Johannes-Quintett /
KV516, Mozart



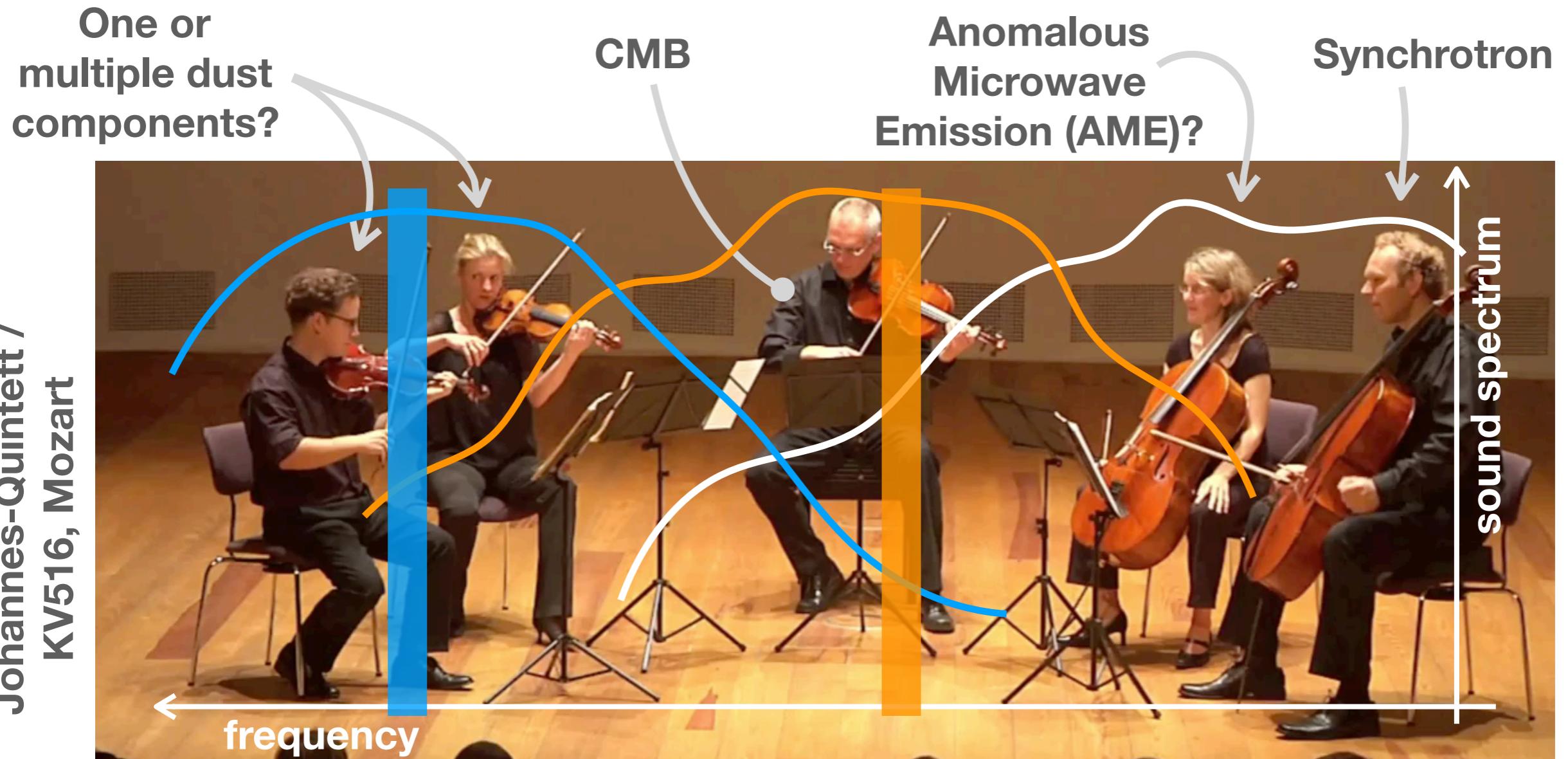
Johannes-Quintett /
KV516, Mozart



$$d_{\nu_0} = a_0 \text{ CMB} + b_0 \text{ dust} + n_{\nu_0}$$

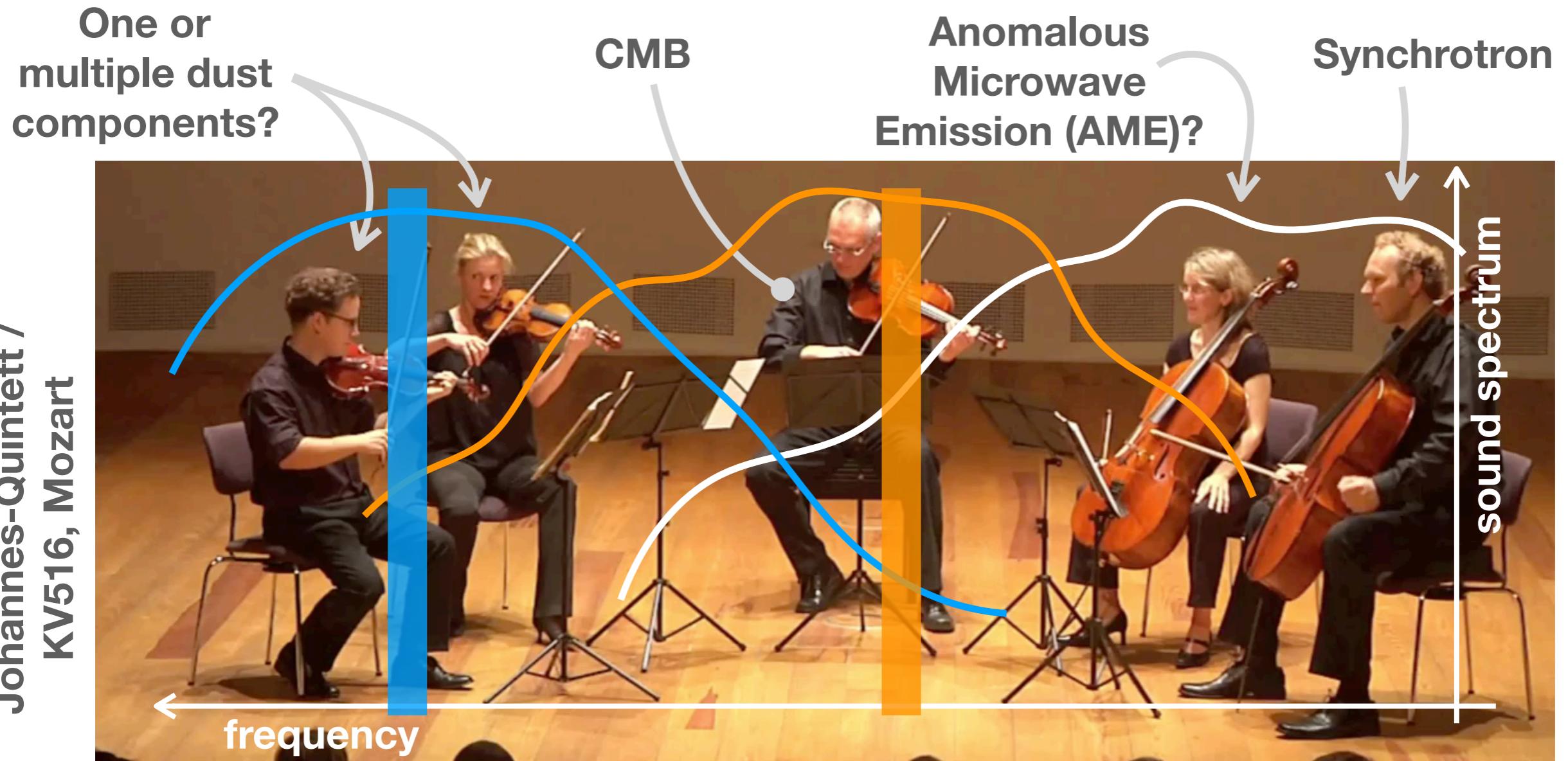
$$d_{\nu_1} = a_1 \text{ CMB} + b_1 \text{ dust} + n_{\nu_1}$$

Johannes-Quintett /
KV516, Mozart



$$\begin{aligned} d_{\nu_0} &= a_0 \text{ CMB} + b_0 \text{ dust} + n_{\nu_0} \\ d_{\nu_1} &= a_1 \text{ CMB} + b_1 \text{ dust} + n_{\nu_1} \end{aligned} \longrightarrow d_{\nu_0} b_1 - d_{\nu_1} b_0 = CMB (b_1 a_0 - b_0 a_1) + n_{\nu_0} b_1 - n_{\nu_1} b_0$$

Johannes-Quintett / KV516, Mozart



$$d_{\nu_0} = a_0 \text{ CMB} + b_0 \text{ dust} + n_{\nu_0}$$

$$d_{\nu_1} = a_1 \text{ CMB} + b_1 \text{ dust} + n_{\nu_1}$$

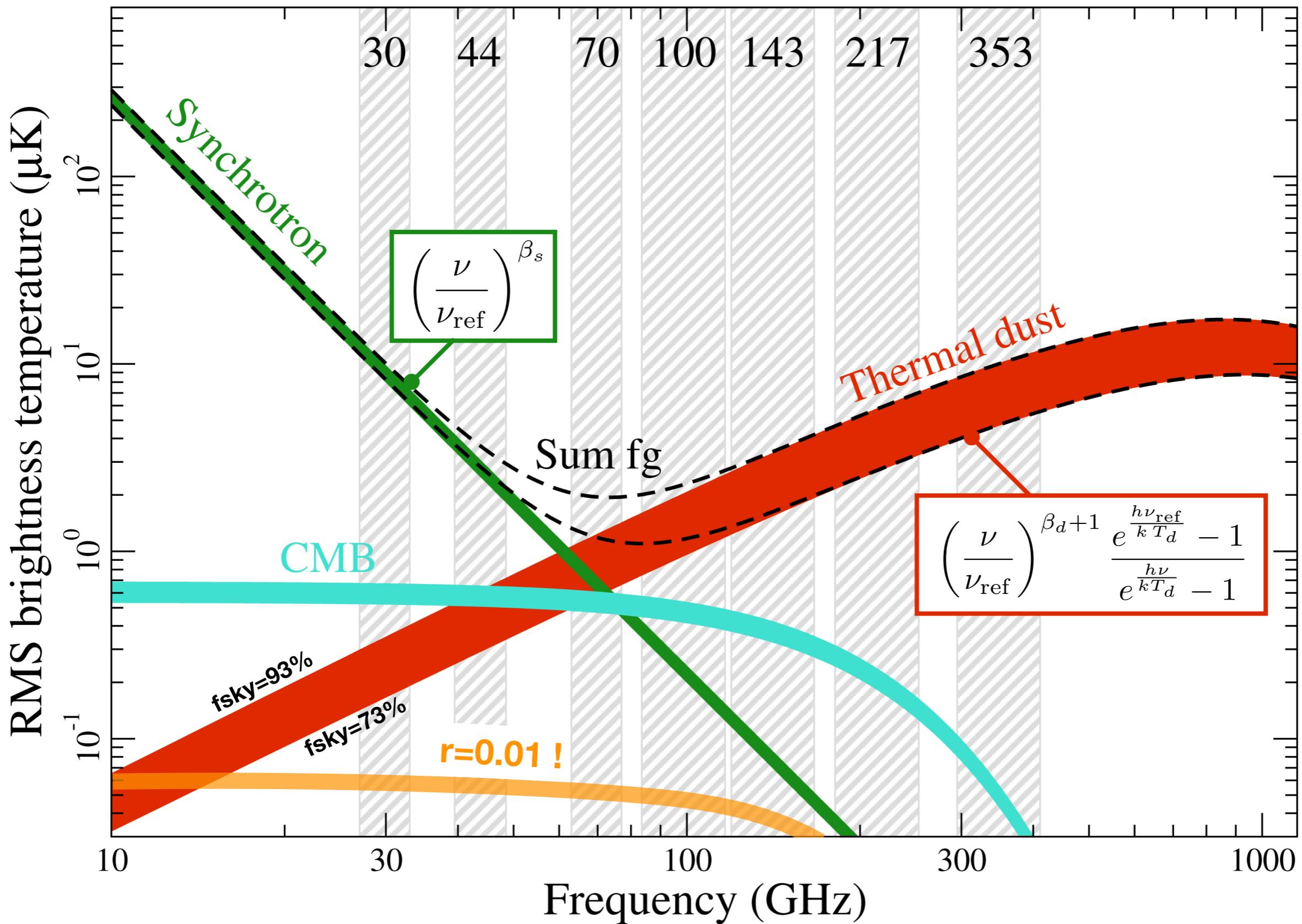
$$\rightarrow d_{\nu_0}b_1 - d_{\nu_1}b_0 = \text{CMB} (b_1a_0 - b_0a_1) + n_{\nu_0}b_1 - n_{\nu_1}b_0$$

boosted variance in recovered CMB

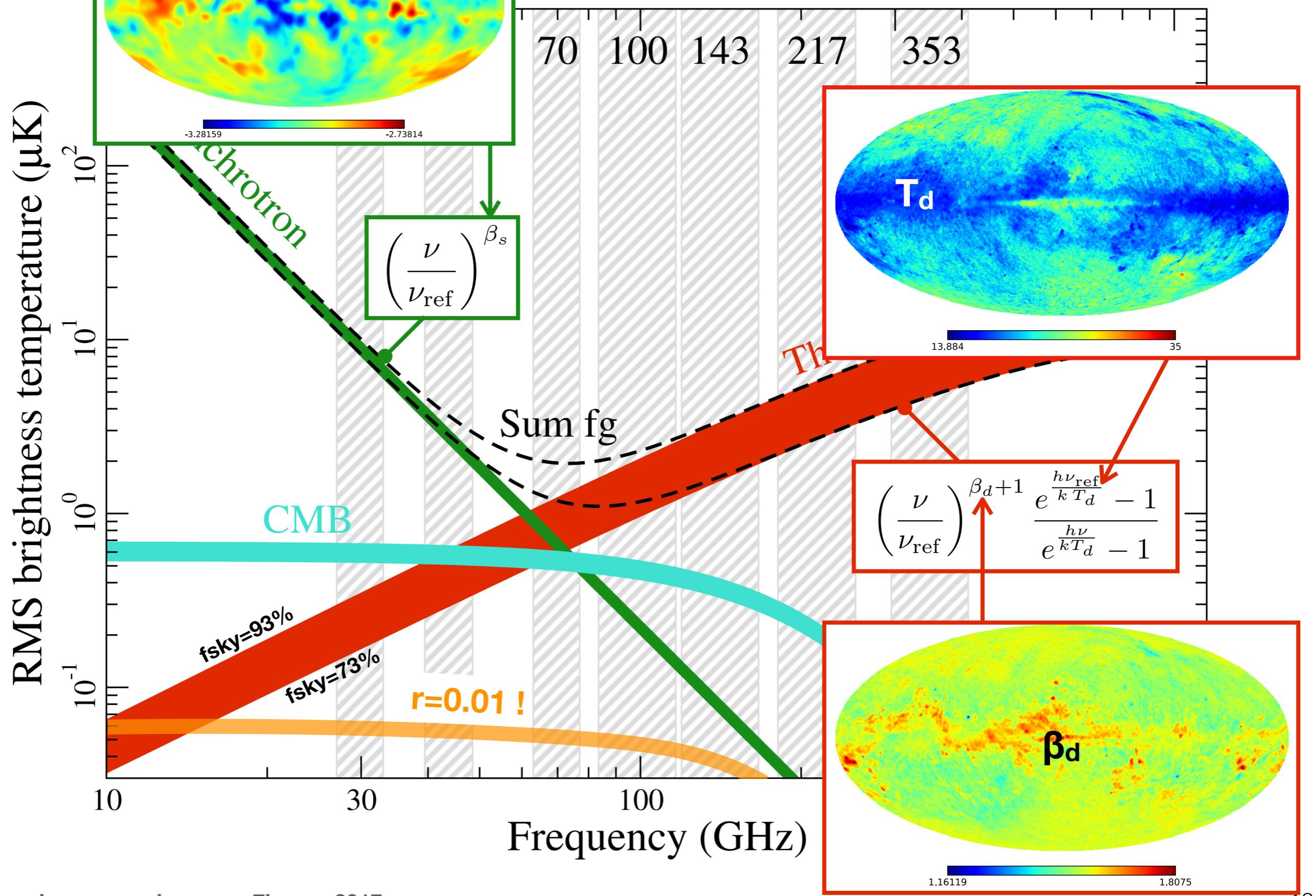
$$\sigma_{\text{CMB}}^2 = \frac{\sigma_{\nu_0}^2 b_1^2 + \sigma_{\nu_1}^2 b_0^2}{(b_1 a_0 - b_0 a_1)^2}$$

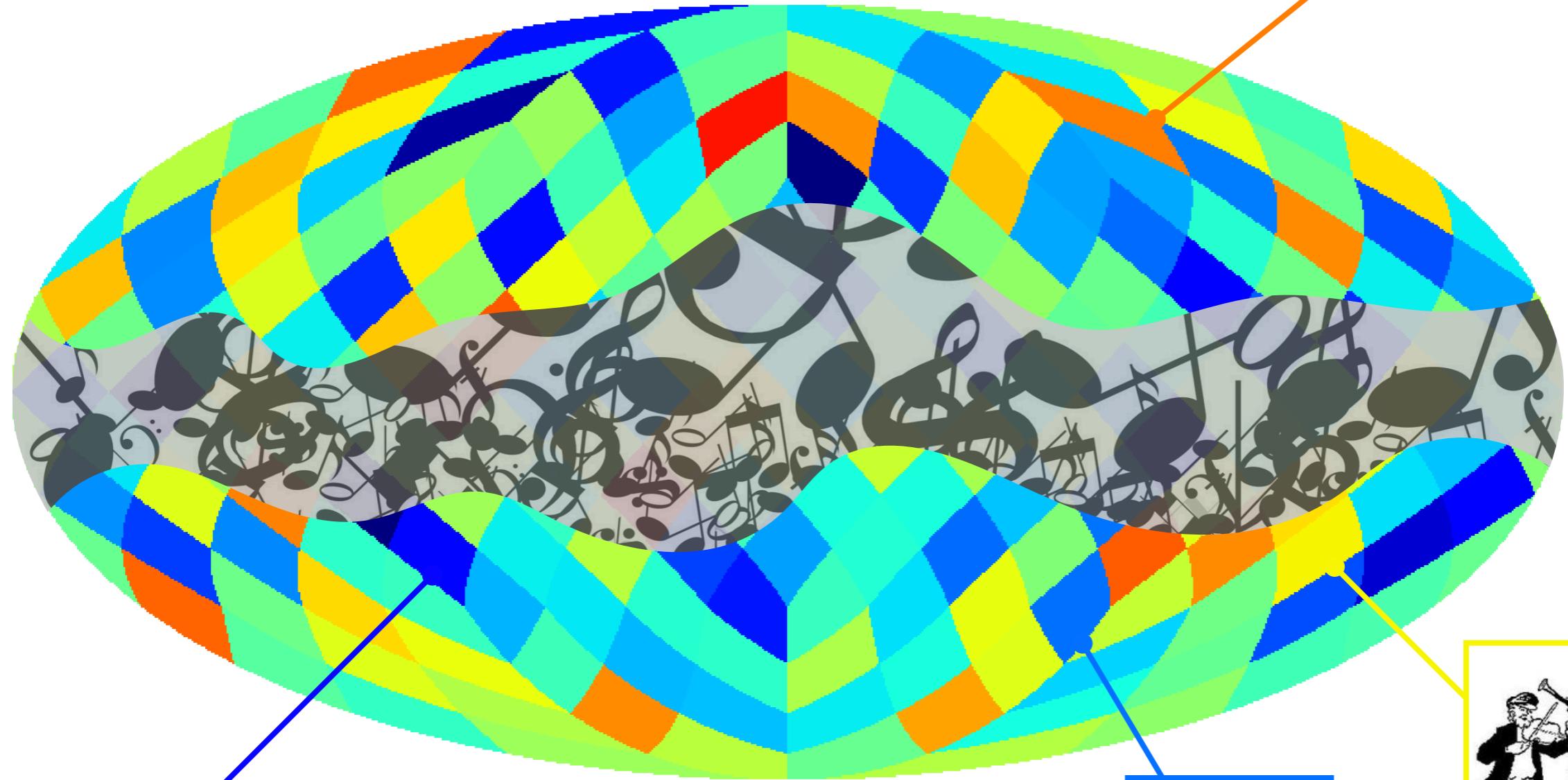
**statistical/systematic residuals
in the cleaned signal**

$$\delta \text{CMB} \propto \delta b_1 (\alpha d_{\nu_0} + \beta d_{\nu_1})$$

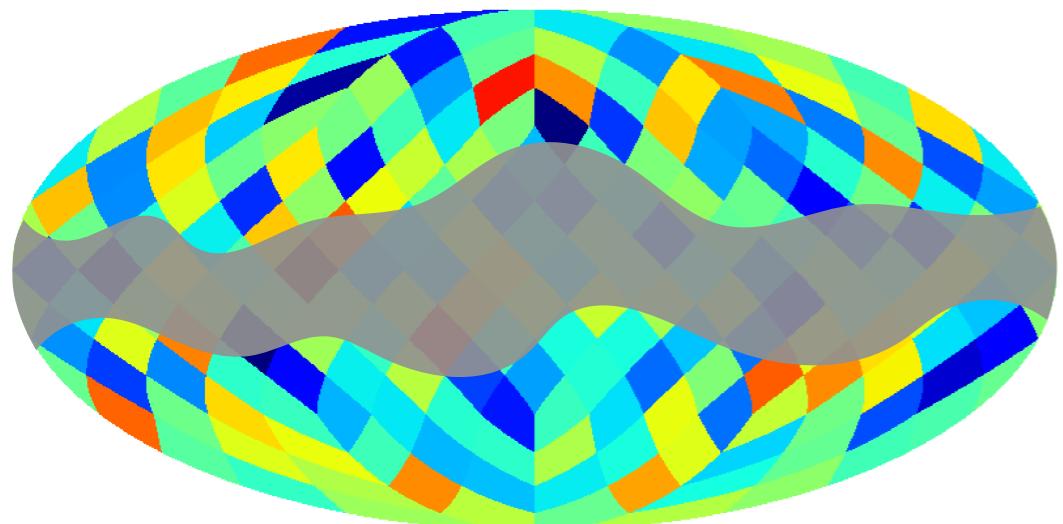


Planck 2015 results. X. Diffuse component separation:
foreground maps, The Planck collaboration, A&A, 2015





Rendition of parametric max-likelihood component separation



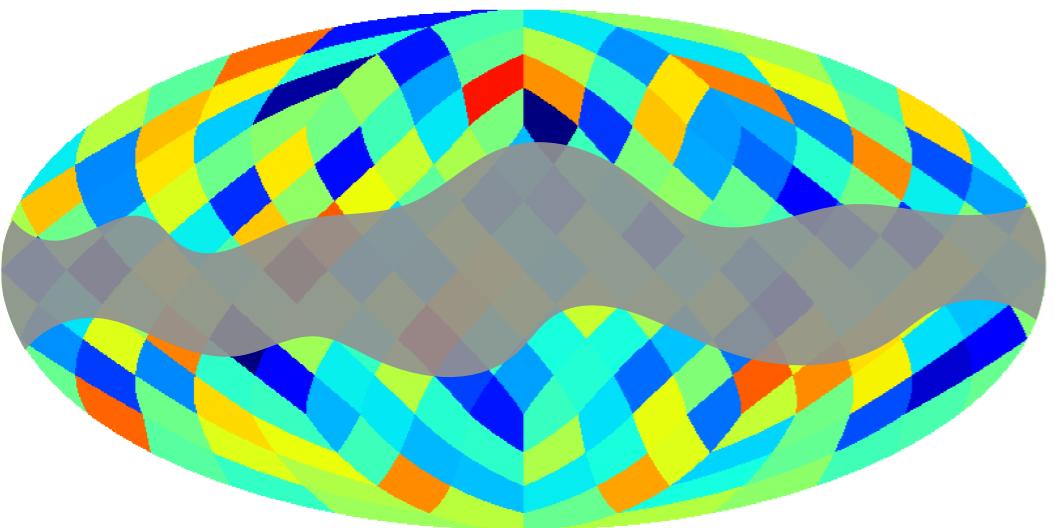
see talk by Jean-Loup Puget this afternoon

data modeling
for each sky pixel:

$$d_i(p) = A_{ij} s_j(p) + n_i(p)$$

$$\mathbf{d} = \mathbf{A} \mathbf{s} + \mathbf{n}$$

Rendition of parametric max-likelihood component separation



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for each sky pixel:

see talk by Jean-Loup Puget this afternoon

$$d_i(p) = A_{ij} s_j(p) + n_i(p)$$

d = **A** **s** + **n**

↑
frequencies
↓

I. estimation of the mixing matrix **A**

$$A_{\text{sync}}^{\text{raw}}(\nu, \nu_{\text{ref}}) \equiv \left(\frac{\nu}{\nu_{\text{ref}}} \right)^{\beta_s}$$

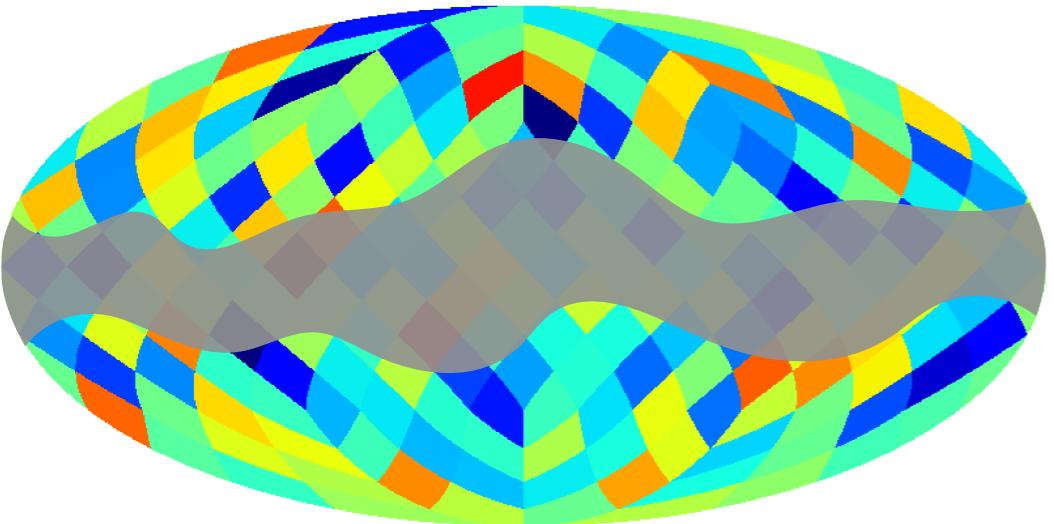
$$A_{\text{dust}}^{\text{raw}}(\nu, \nu_{\text{ref}}) \equiv \left(\frac{\nu}{\nu_{\text{ref}}} \right)^{\beta_d+1} \frac{e^{\frac{h\nu_{\text{ref}}}{kT_d}} - 1}{e^{\frac{h\nu}{kT_d}} - 1}$$

$$\mathbf{A} \equiv \mathbf{A}(\beta = \beta_d, \beta_s, \dots) \longrightarrow \max (\mathcal{L}(\beta))$$

e.g. Stompor et al. (2009)

**not perfect
recovery of input
spectral
parameters ➤
foregrounds
residuals**

Rendition of parametric max-likelihood component separation



data modeling
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$$\mathbf{A} \equiv \mathbf{A}(\beta = \beta_d, \beta_s, \dots) \longrightarrow \max (\mathcal{L}(\beta))$$

e.g. Stompor et al. (2009)

not perfect recovery of input spectral parameters > foregrounds residuals

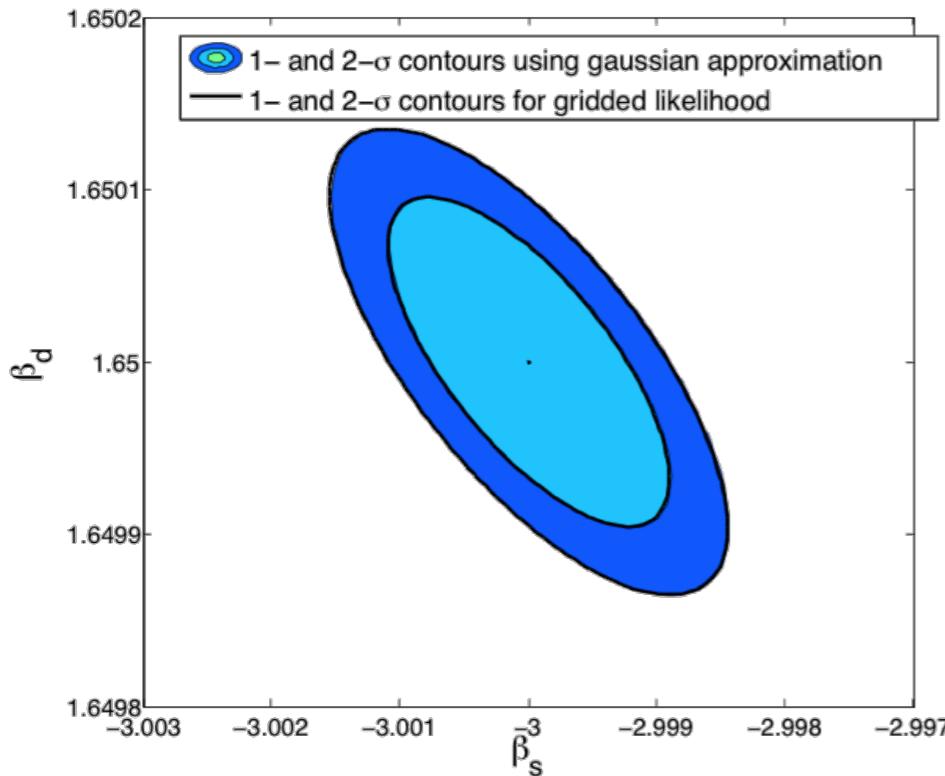
2. solve for **s** [rather general to any comp sep method]

$$\mathbf{s} = (\mathbf{A}^T \mathbf{N}^{-1} \mathbf{A})^{-1} \mathbf{A}^T \mathbf{N}^{-1} \mathbf{d}$$

linear combination of various frequency maps > boosted noise

Rendition of parametric max-likelihood component separation

Statistical error bars on spectral parameters:

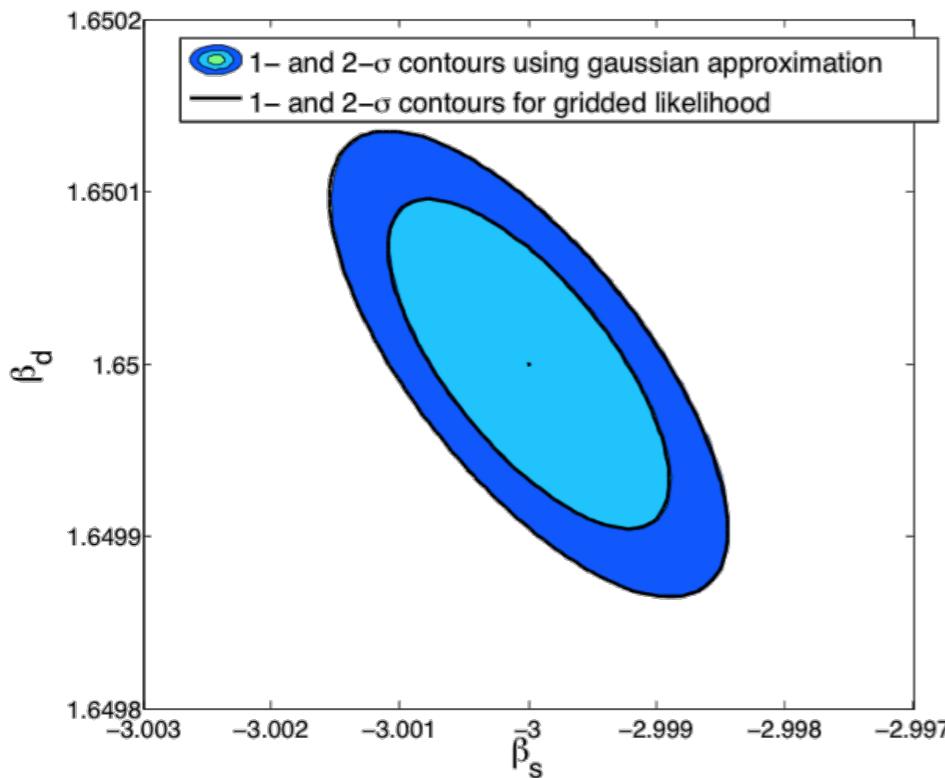


Errard, Stivoli and Stompor (PRD, 2011)

$$\Sigma^{-1} \simeq - \left\langle \frac{\partial^2 \mathcal{L}}{\partial \beta \partial \beta'} \right\rangle_{\text{noise}} \Big|_{\text{true } \beta}$$

Rendition of parametric max-likelihood component separation

Statistical error bars on spectral parameters:



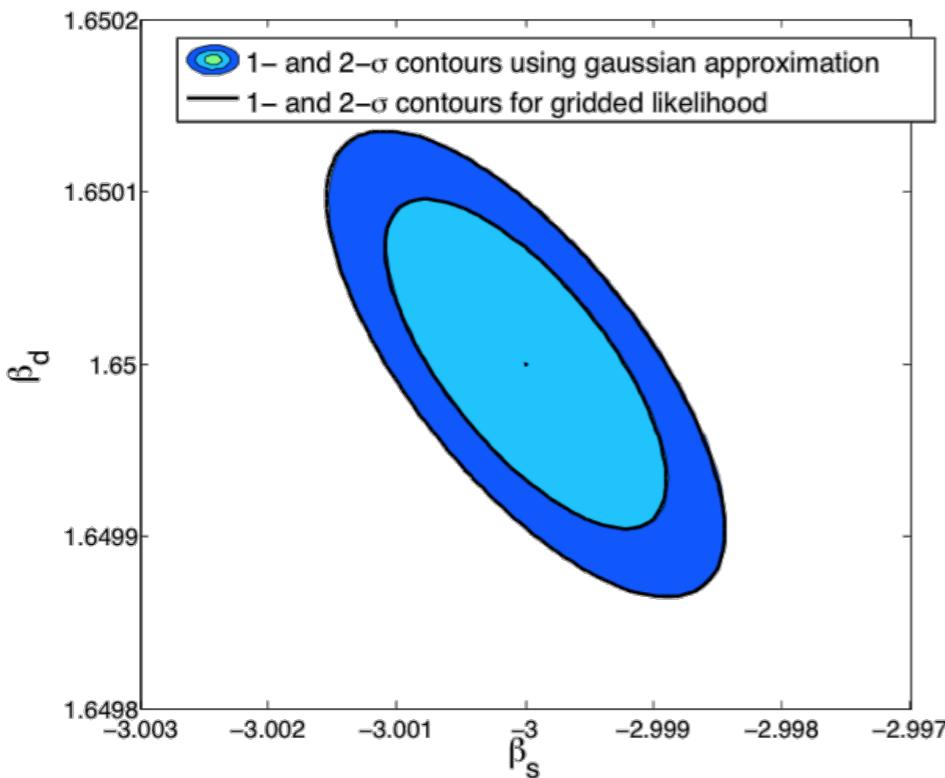
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→ averaged error bars for parametric methods like COMMANDER

Rendition of parametric max-likelihood component separation

Statistical error bars on spectral parameters:



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→ averaged error bars for parametric methods like COMMANDER

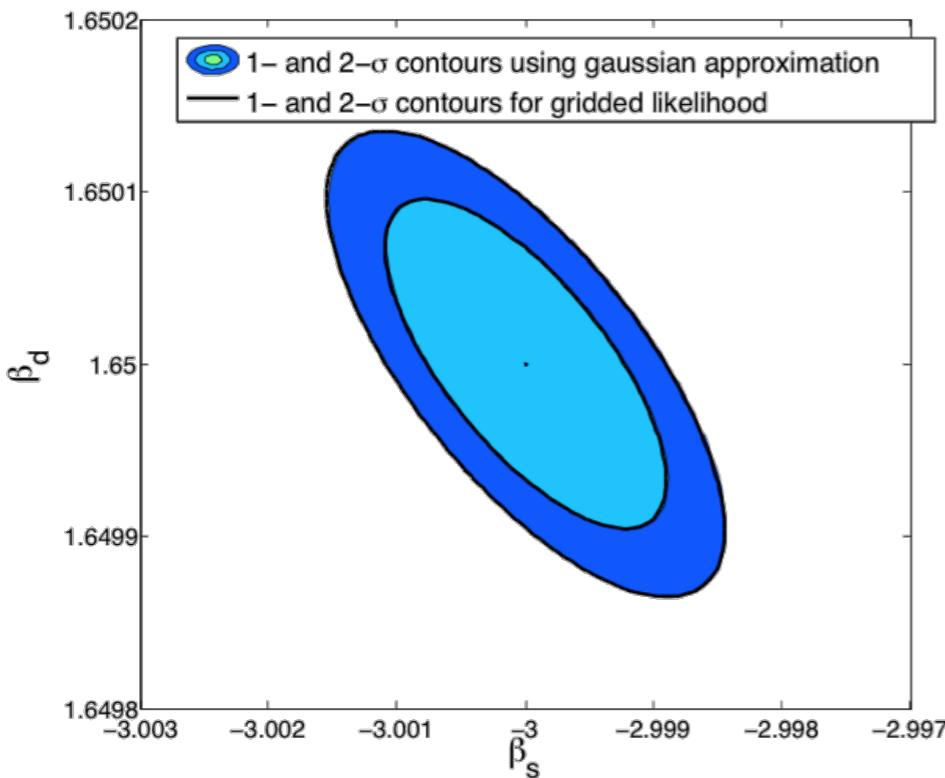
Amplitude of statistical foregrounds residuals:

$$C_\ell^{\text{fg res}} \equiv \sum_{k,k'} \sum_{j,j'} \Sigma_{kk'} \kappa_{kk'}^{jj'} C_\ell^{jj'}$$

Stivoli, Grain, Leach, Tristram, Baccigalupi, Stompor (MNRAS, 2010)

Rendition of parametric max-likelihood component separation

Statistical error bars on spectral parameters:



Errard, Stivoli and Stompor (PRD, 2011)

$$\Sigma^{-1} \simeq - \left\langle \frac{\partial^2 \mathcal{L}}{\partial \beta \partial \beta'} \right\rangle_{\text{noise}} \Big|_{\text{true } \beta}$$

→ averaged error bars for parametric methods like **COMMANDER**

Amplitude of statistical foregrounds residuals:

$$C_\ell^{\text{fg res}} \equiv \sum_{k,k'} \sum_{j,j'} \Sigma_{kk'} \kappa_{kk'}^{jj'} C_\ell^{jj'}$$

Stivoli, Grain, Leach, Tristram, Baccigalupi, Stompor (MNRAS, 2010)

Combination with delensing and cosmological parameters estimation:



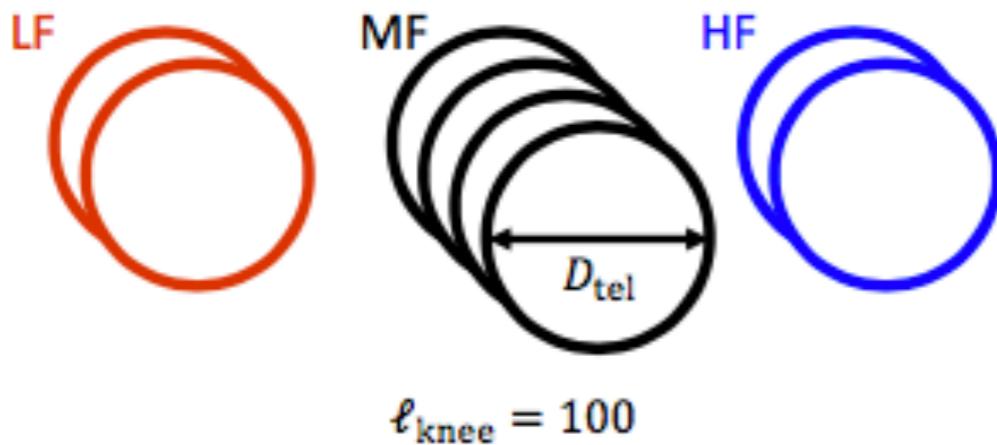
JE, Feeney, Peiris and Jaffe (JCAP, 2016)

Optimization Study for the Experimental Configuration of CMB-S4

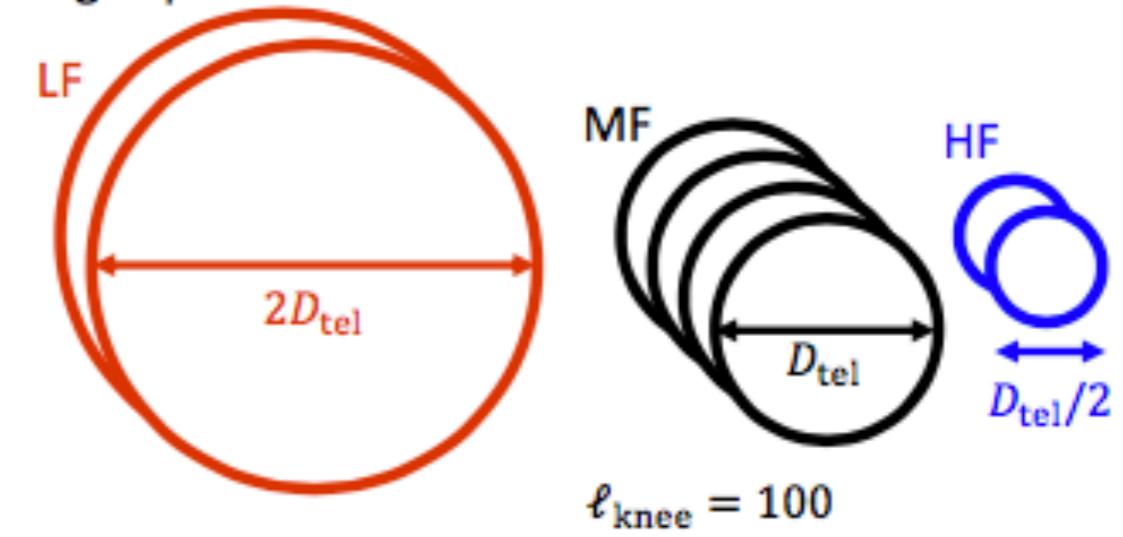
D. Barron et al., arXiv:1702.07467

CMB4CAST
GROUNDS

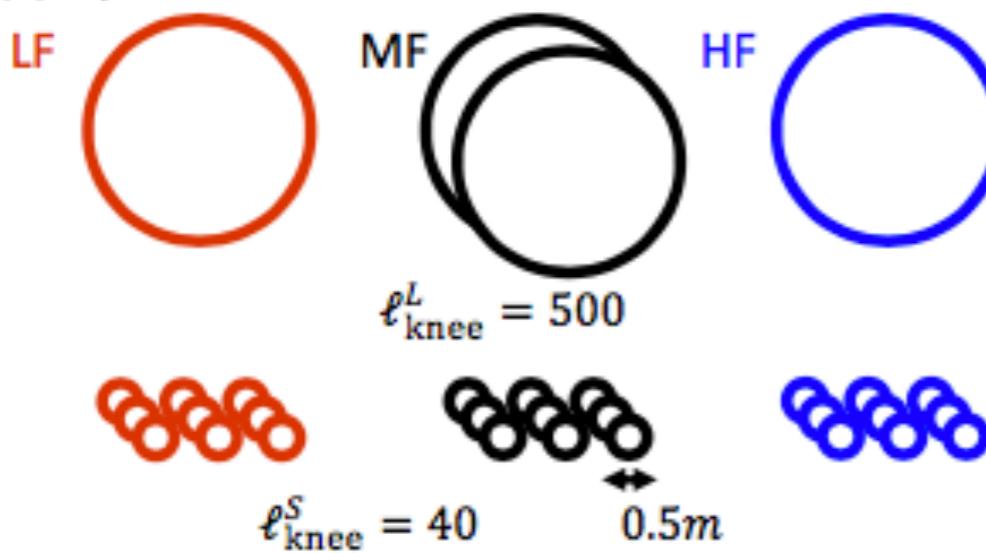
(a) Large aperture-a



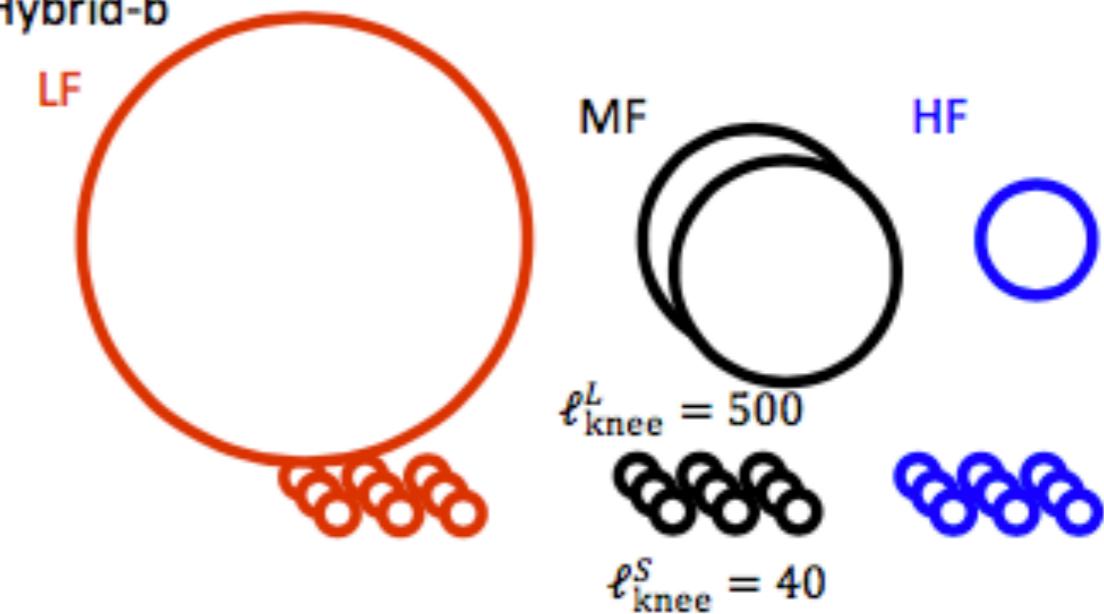
(b) Large aperture-b



(c) Hybrid-a



(d) Hybrid-b



Optimization Study for the Experimental Configuration of CMB-S4

D. Barron et al., arXiv:1702.07467

CMB4CAST
GROUNDS

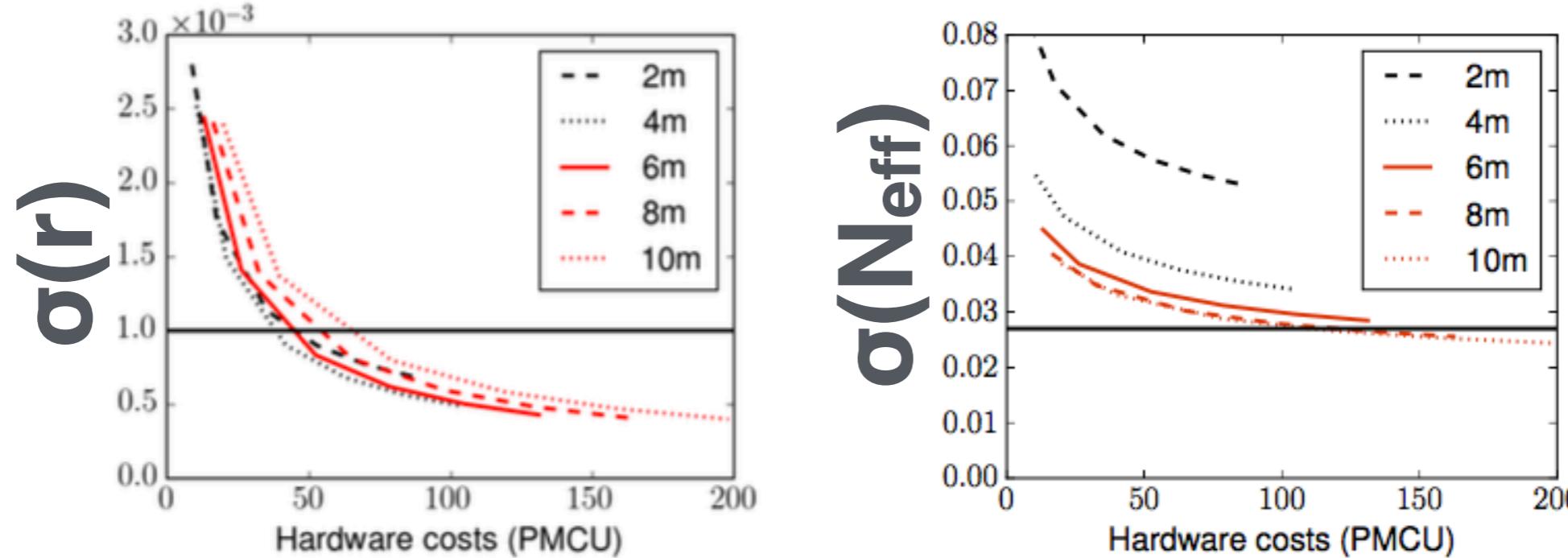
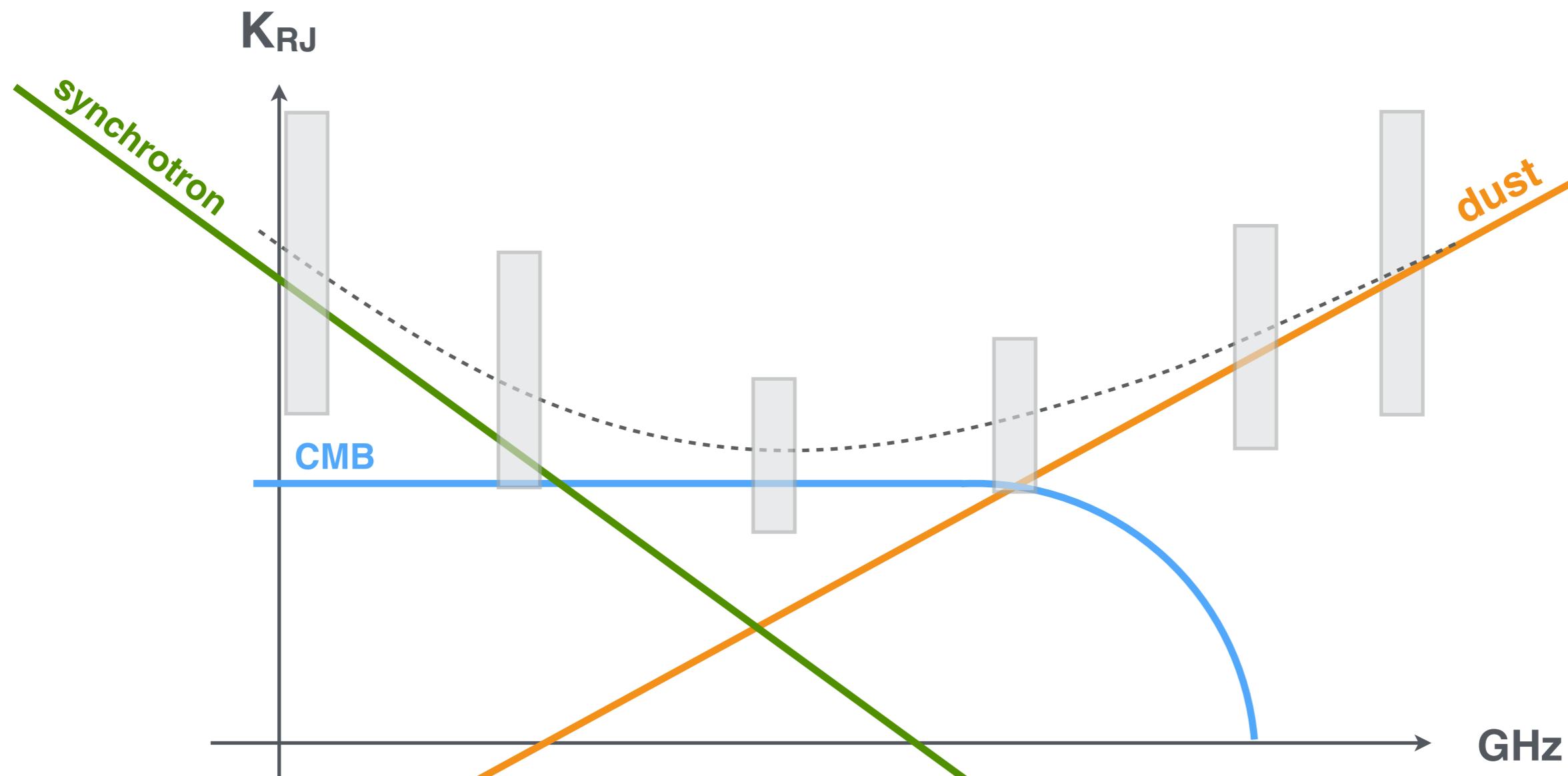
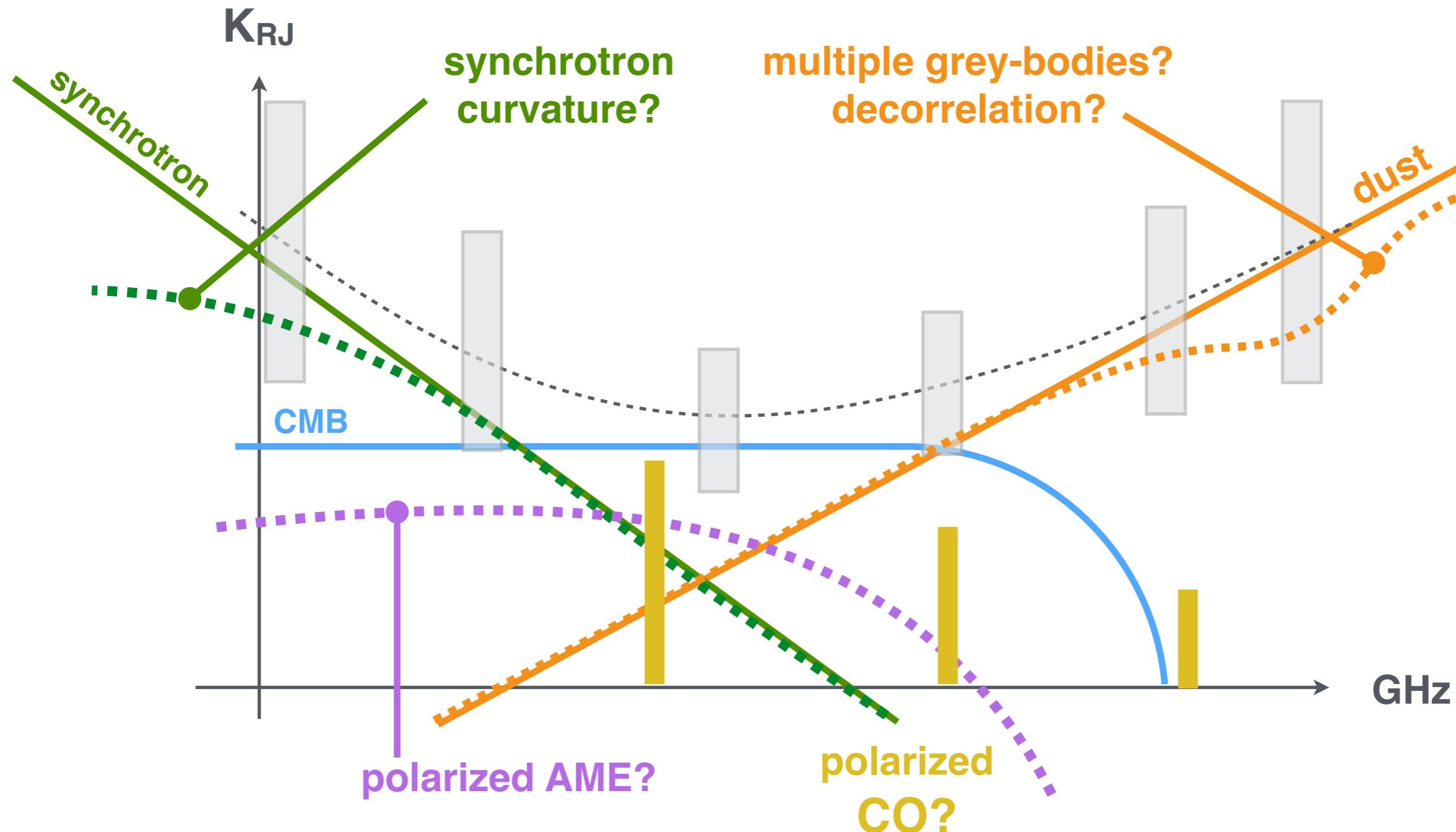


Figure 12 Constraint on r with $f_{\text{sky}} = 0.05$ (left) and N_{eff} with $f_{\text{sky}} = 0.5$ (right) for different apertures, as a function of the total cost of the project. Both are for the large aperture telescope array with fixed aperture sizes (*Large aperture-a*). For both, the improvement saturates approximately at a total hardware cost of 50 PCU. The improvement of r is not linear with the total cost, or with the total number of detectors, because the de-lensing noise levels do not improve as fast as the map depth.

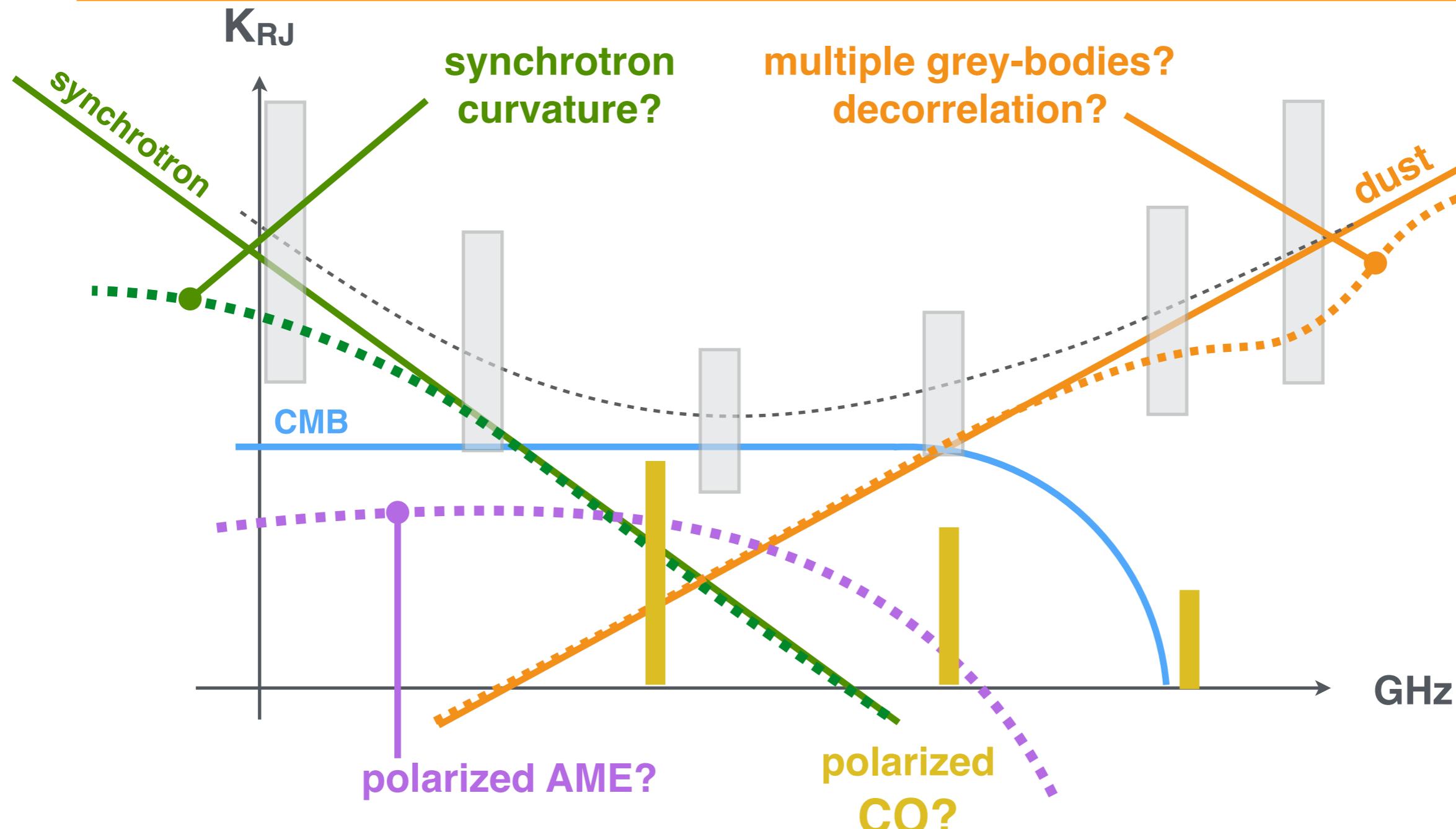
- Framework to optimize overall instrumental configurations
- Connection of science and instrumental configurations
- Optimum is broad, and aperture size of 4-6m is a good number.
- Iteration over the model needed.
 - ★ What's expensive? Which part of the costing has large uncertainty?
 - ★ Which part of the instrumental configuration requires more thoughts? (e.g., LF instruments)
- Foreground complication to be included, e.g. polarized AME, synchrotron curvature, etc.

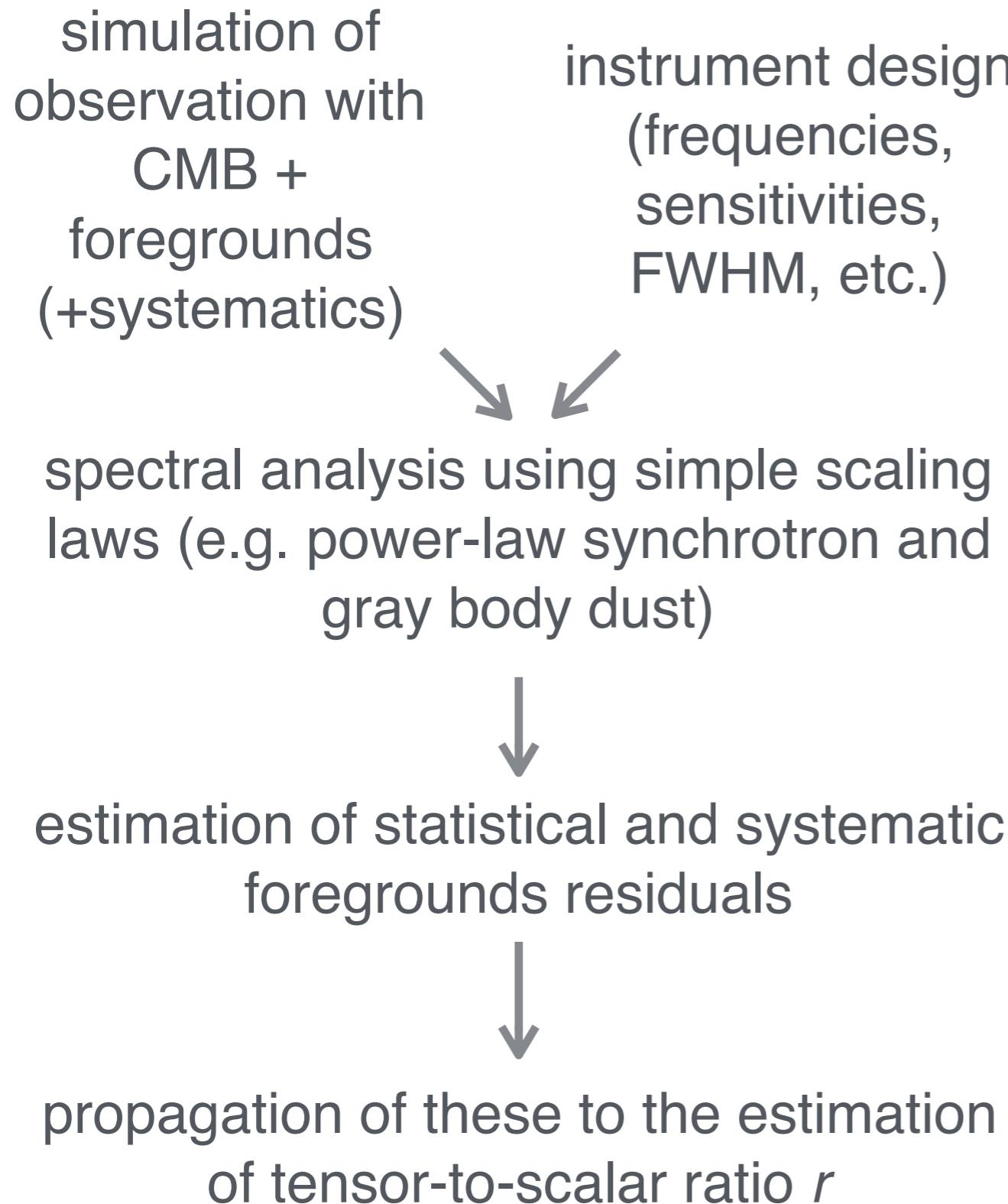




xForecast

Stompor, JE, Poletti (PRL, 2016)





$$\mathbf{d}_p = \hat{\mathbf{A}}_p \hat{\mathbf{s}}_p + \mathbf{n}_p$$

↑
↓
frequencies

$$\mathbf{d} = \mathbf{A} \mathbf{s} + \mathbf{n}$$

$$\langle \mathcal{S}_{spec} \rangle = -\text{tr} \sum_p \left\{ (\mathbf{N}_p^{-1} - \mathbf{P}_p) \left(\hat{\mathbf{d}}_p \hat{\mathbf{d}}_p^t + \mathbf{N}_p \right) \right\}$$

$$C_\ell^{\text{res}} \simeq \otimes_\ell(\tilde{\mathbf{y}}, \tilde{\mathbf{y}}) + \otimes_\ell(\tilde{\mathbf{y}}, \tilde{\mathbf{z}}) + \otimes_\ell(\tilde{\mathbf{z}}, \tilde{\mathbf{y}}) \\ + \text{tr} \left[\Sigma \otimes_\ell(\tilde{\mathbf{Y}}^{(1)}, \tilde{\mathbf{Y}}^{(1)}) \right]$$

$$\langle S^{par} \rangle = \text{tr } \mathbf{C}^{-1} \mathbf{E} + \ln \det \mathbf{C}$$

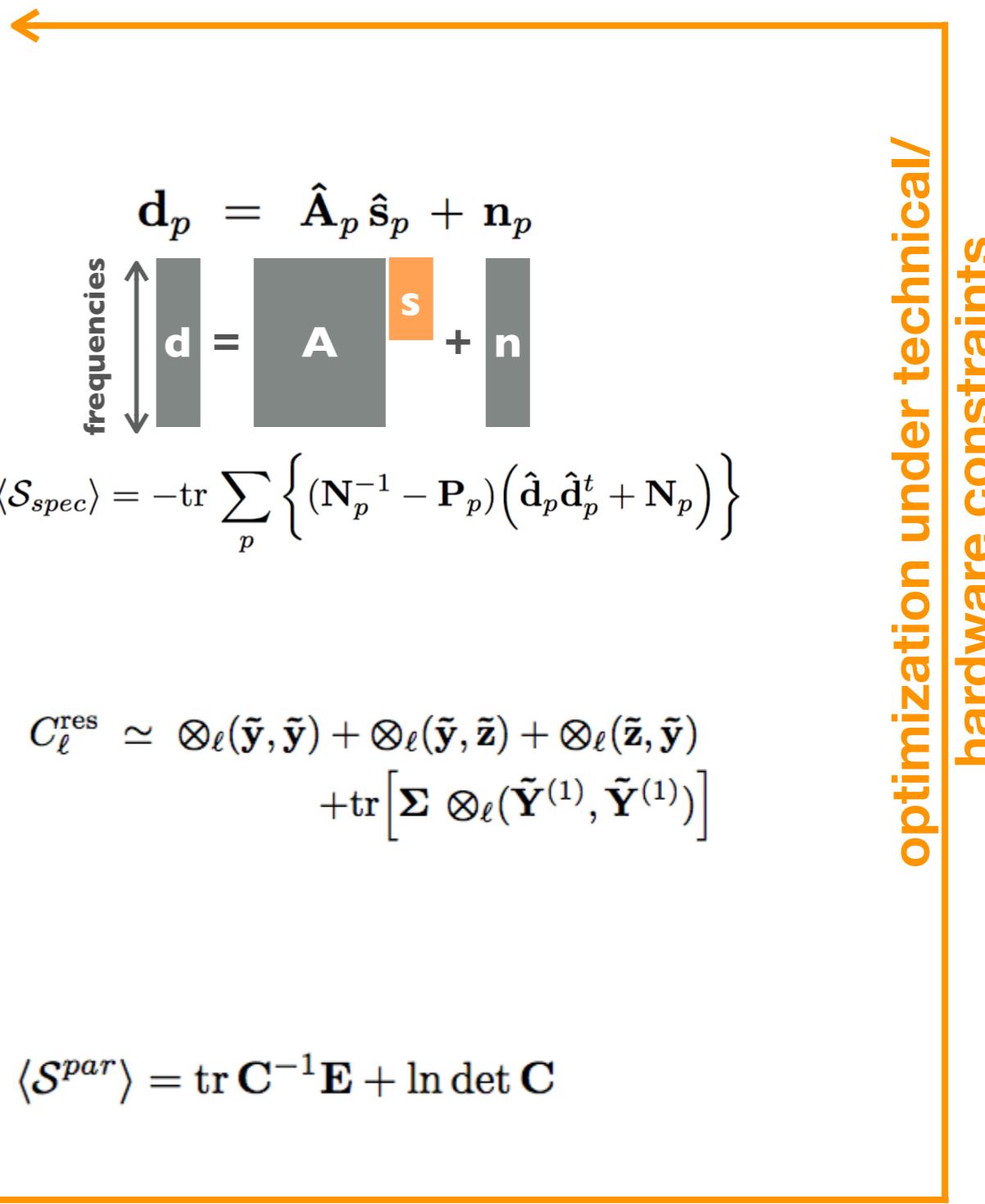
simulation of observation with CMB + foregrounds (+systematics)

spectral analysis using simple scaling laws (e.g. power-law synchrotron and gray body dust)

estimation of statistical and systematic foregrounds residuals

propagation of these to the estimation of tensor-to-scalar ratio r

instrument design (frequencies, sensitivities, FWHM, etc.)



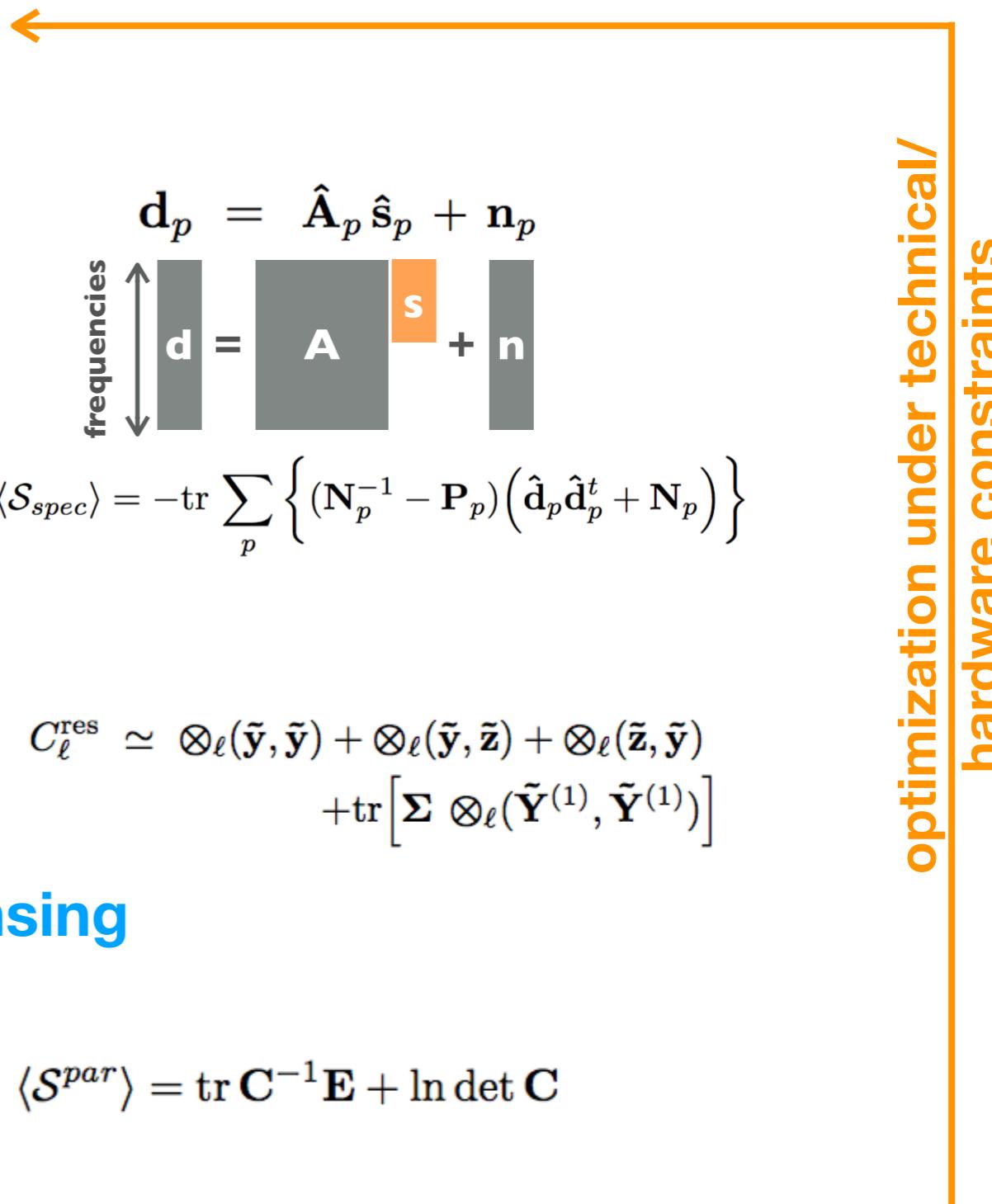
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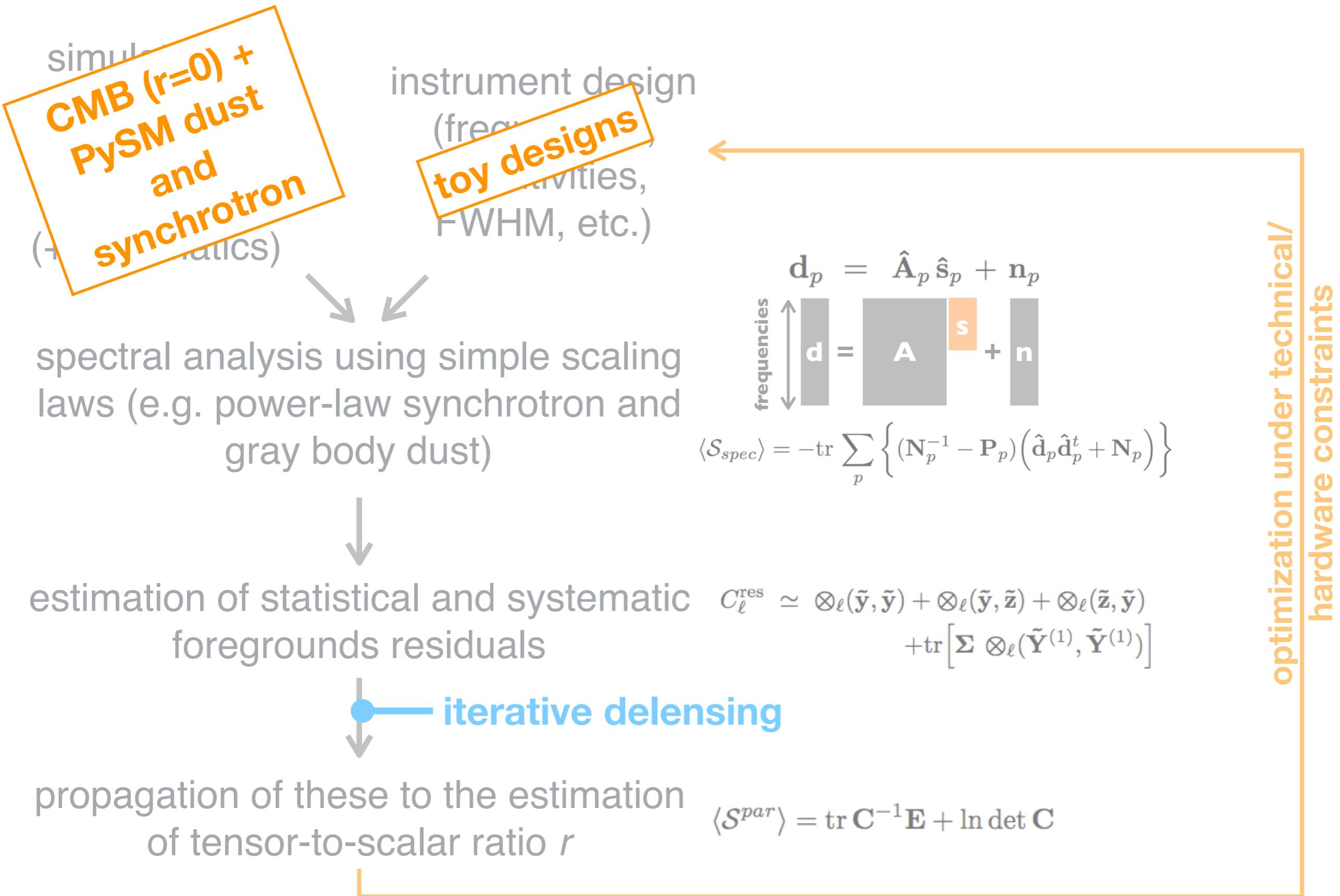
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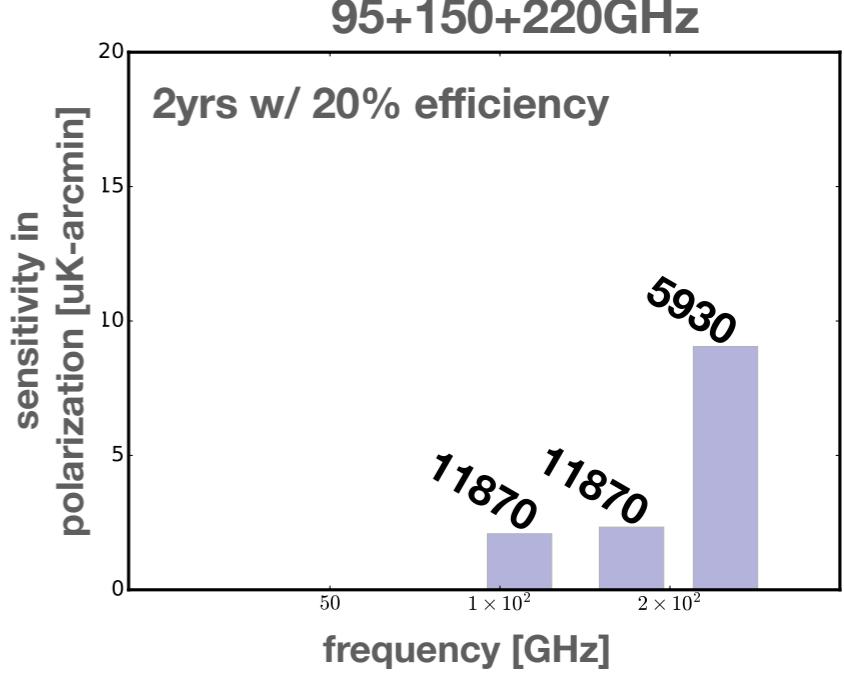
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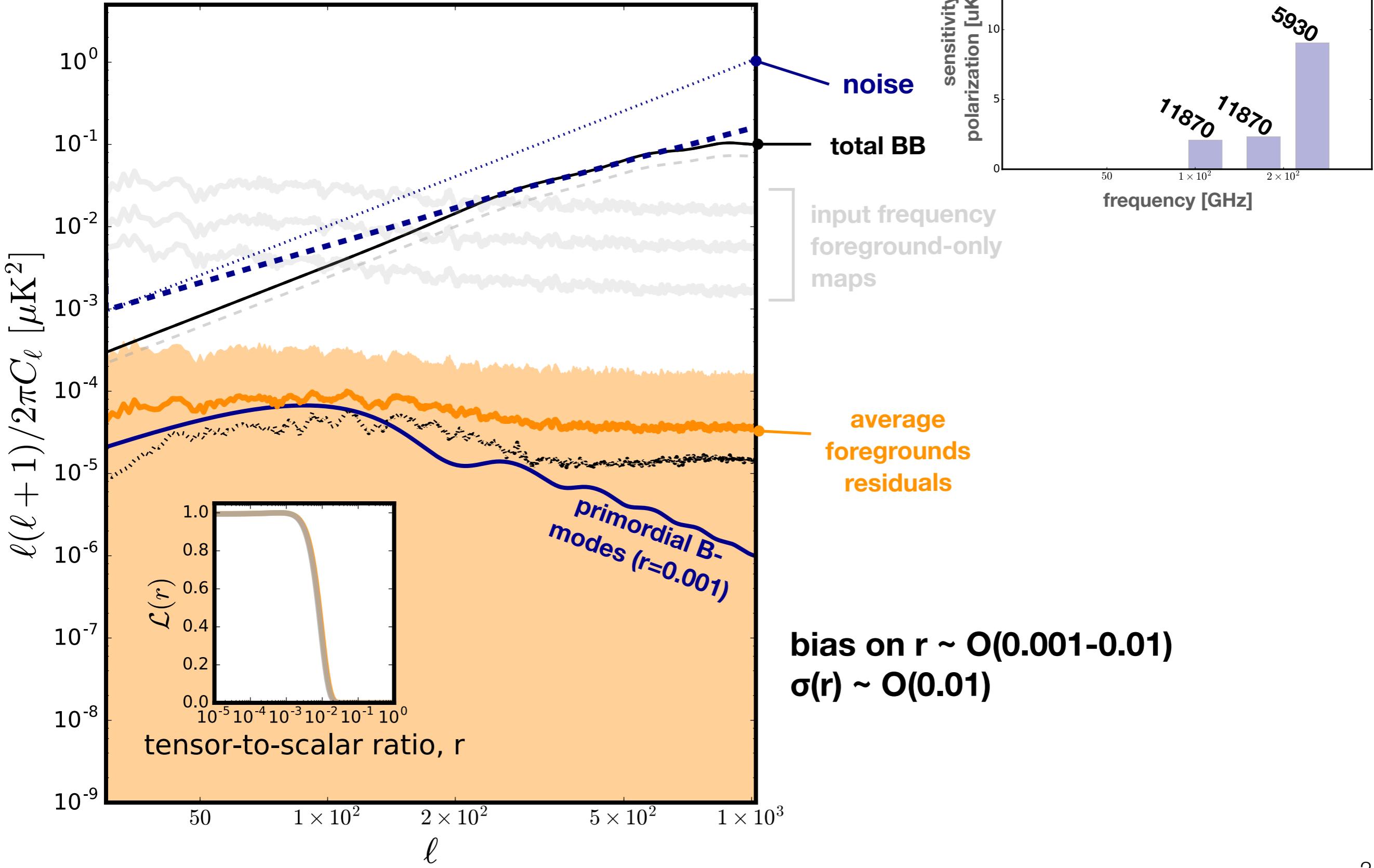
toy example

- with priors from Planck on β , fit for single $\{\beta_d, \beta_s\}$ only
- and few frequency bands from the ground
- on the cleanest fsky=5%



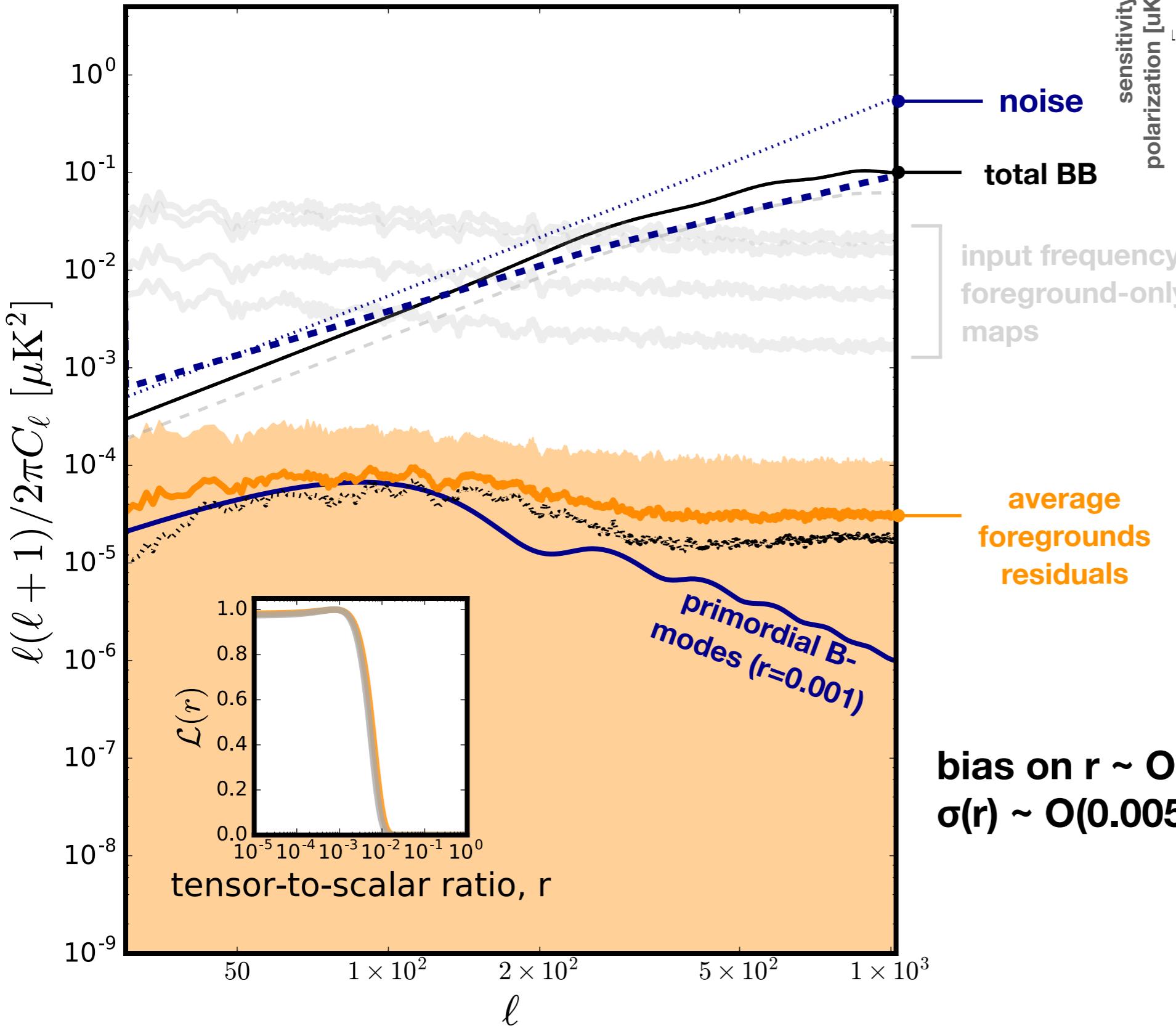
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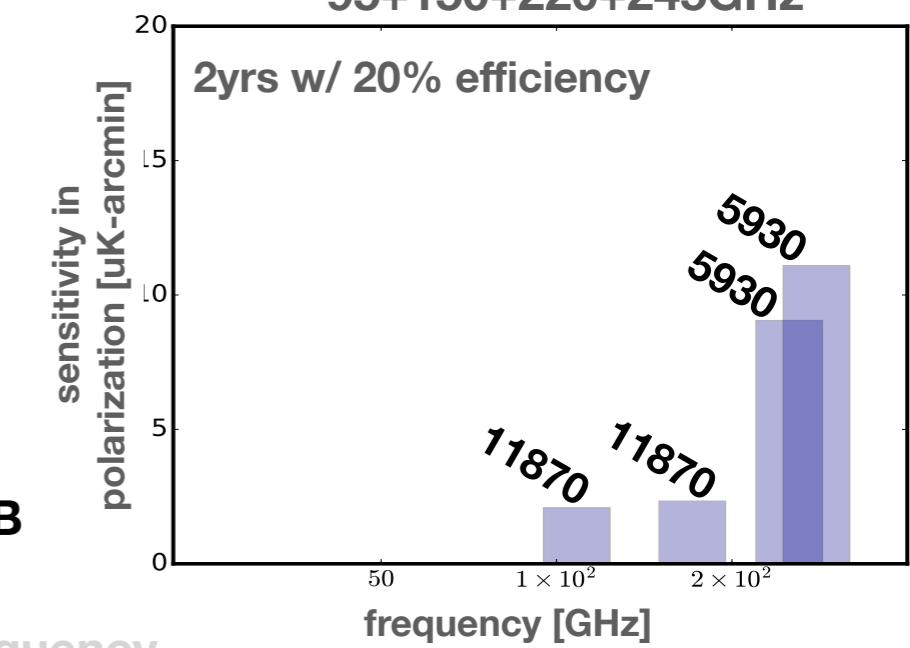
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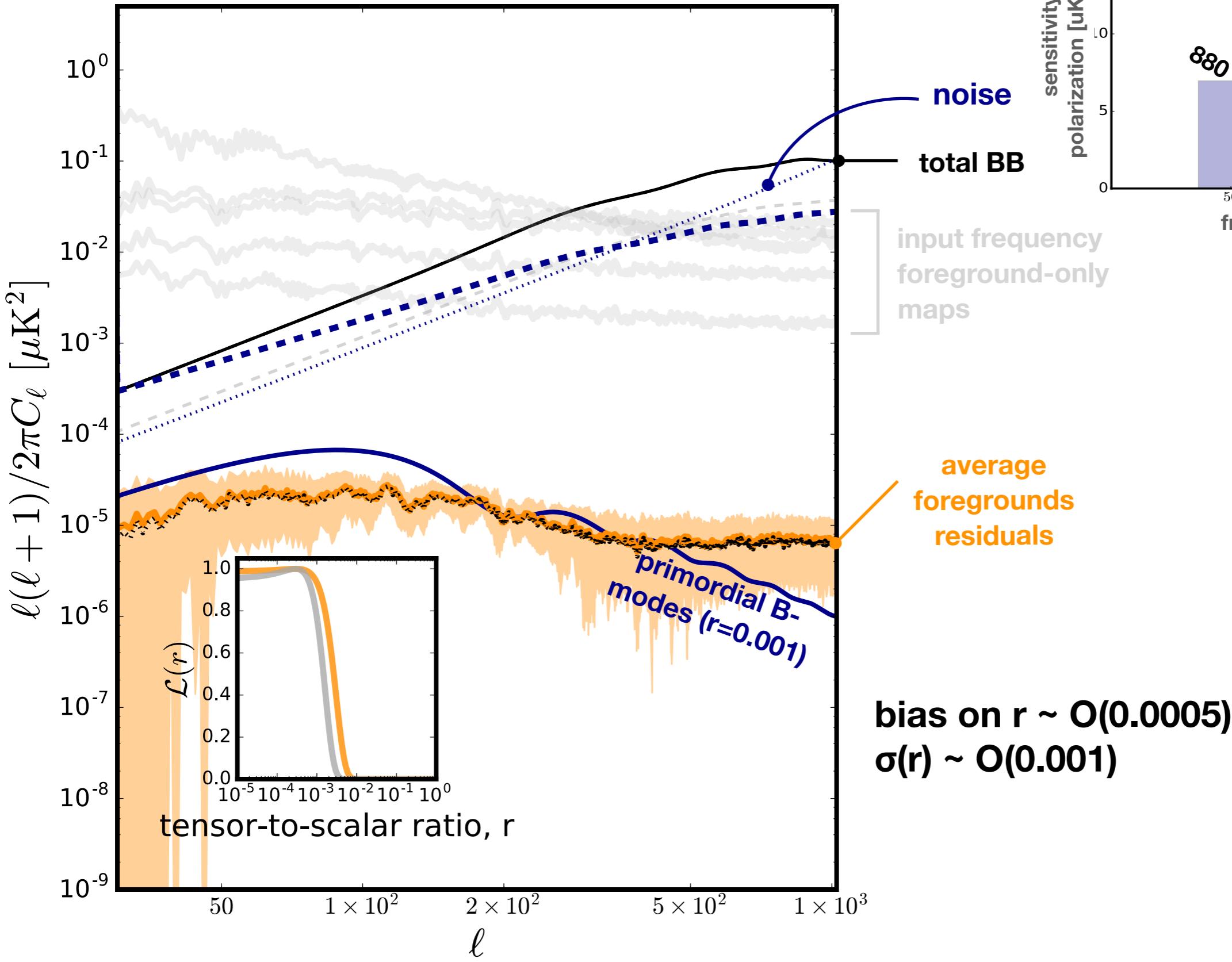
bias on $r \sim \mathcal{O}(0.001-0.005)$
 $\sigma(r) \sim \mathcal{O}(0.005)$

95+150+220+245GHz

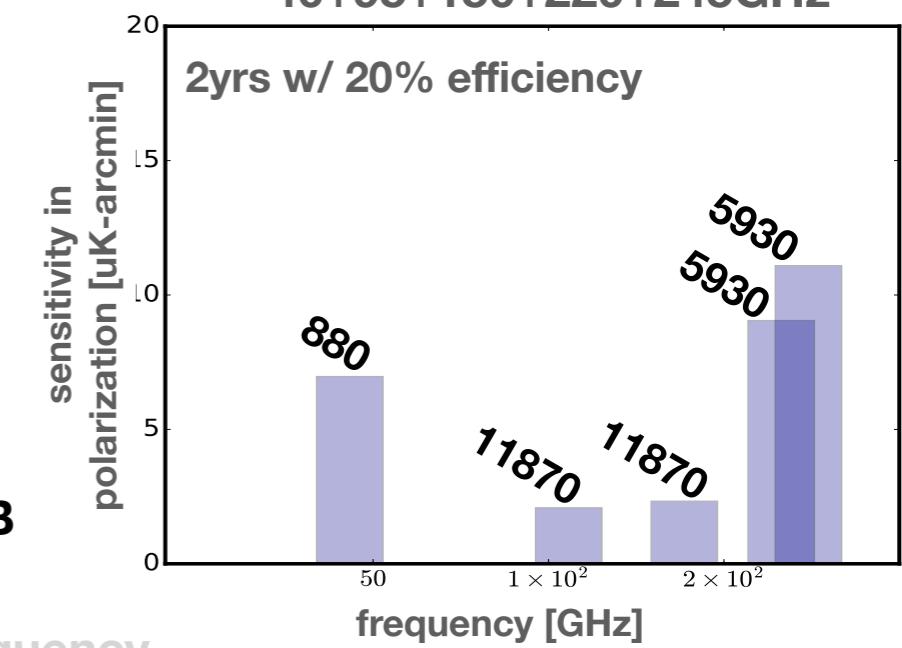


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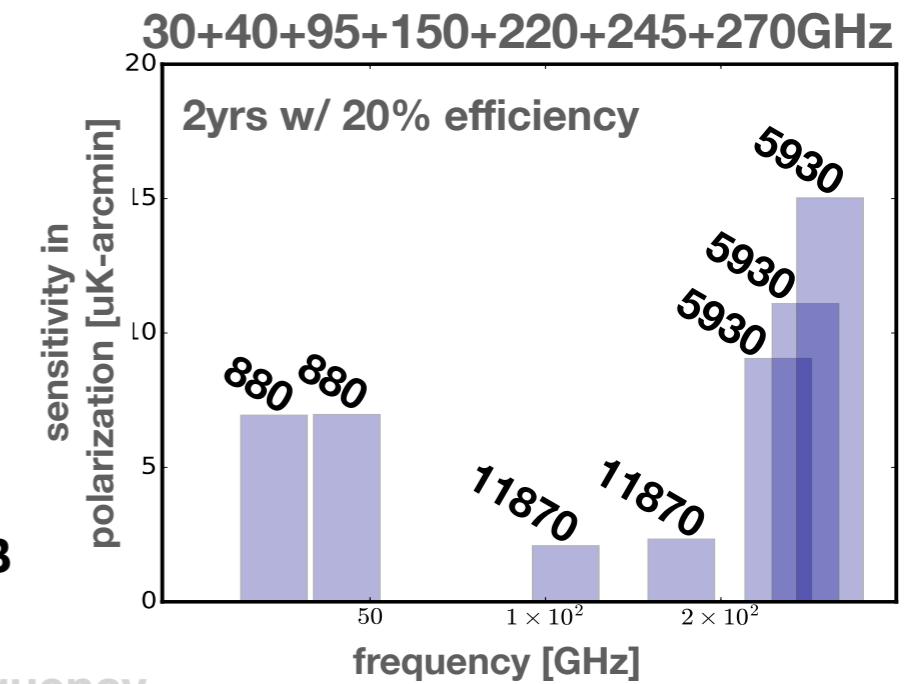
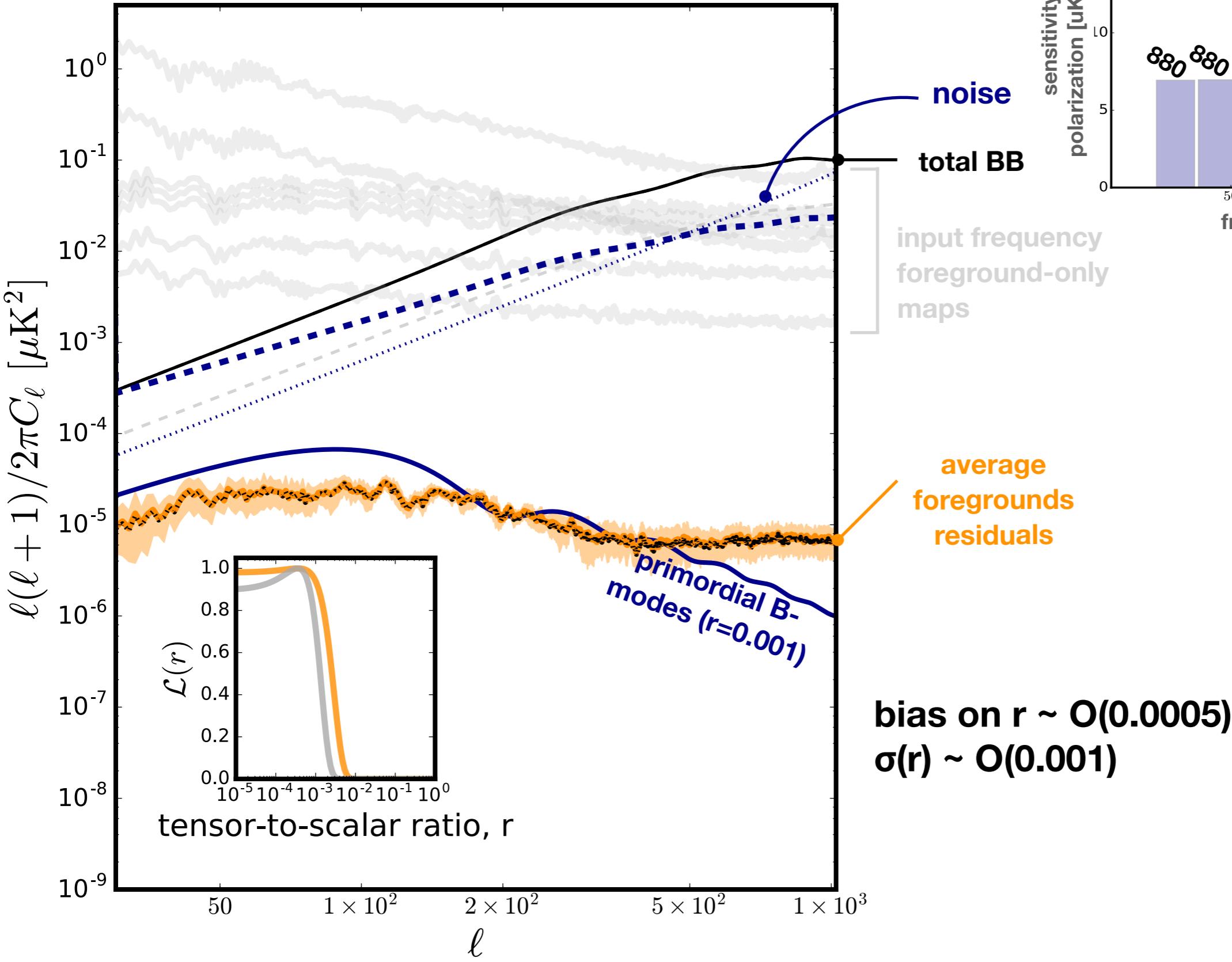


40+95+150+220+245GHz



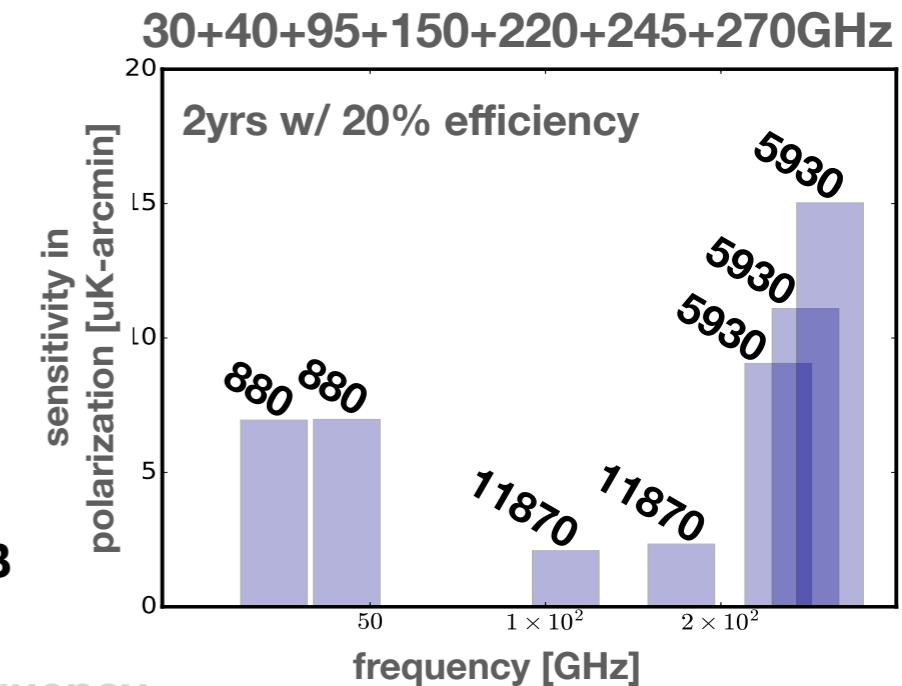
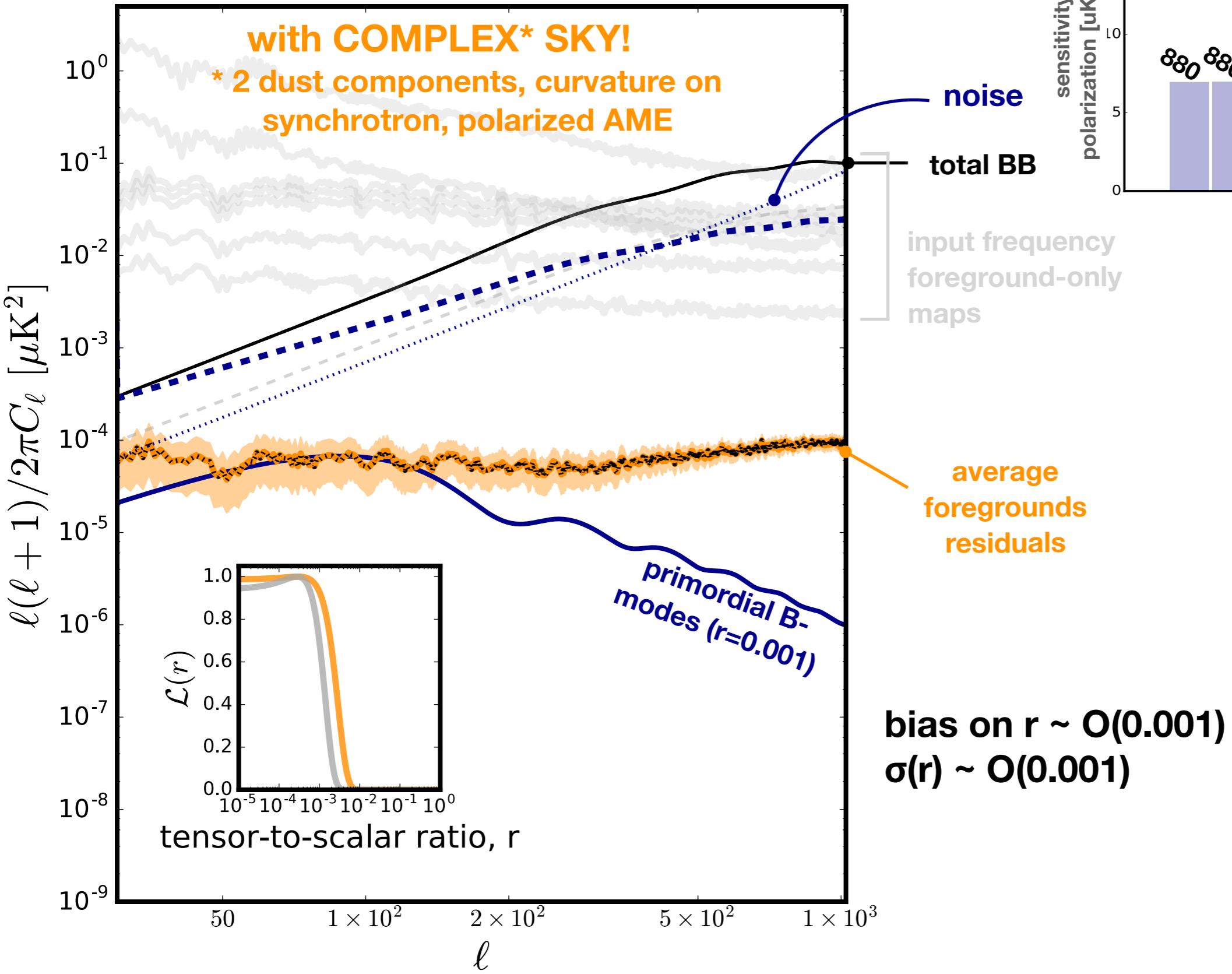
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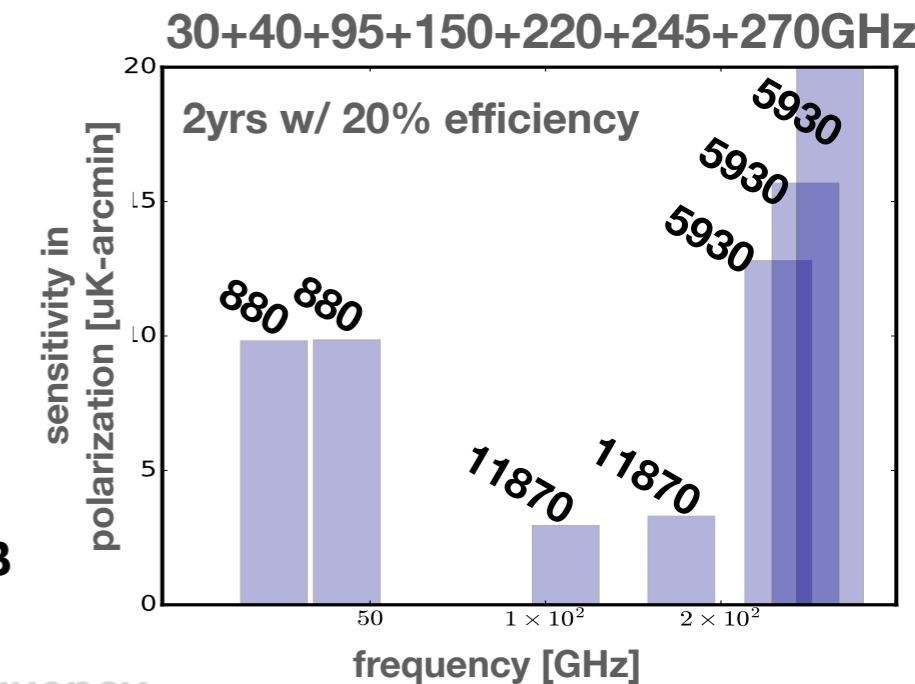
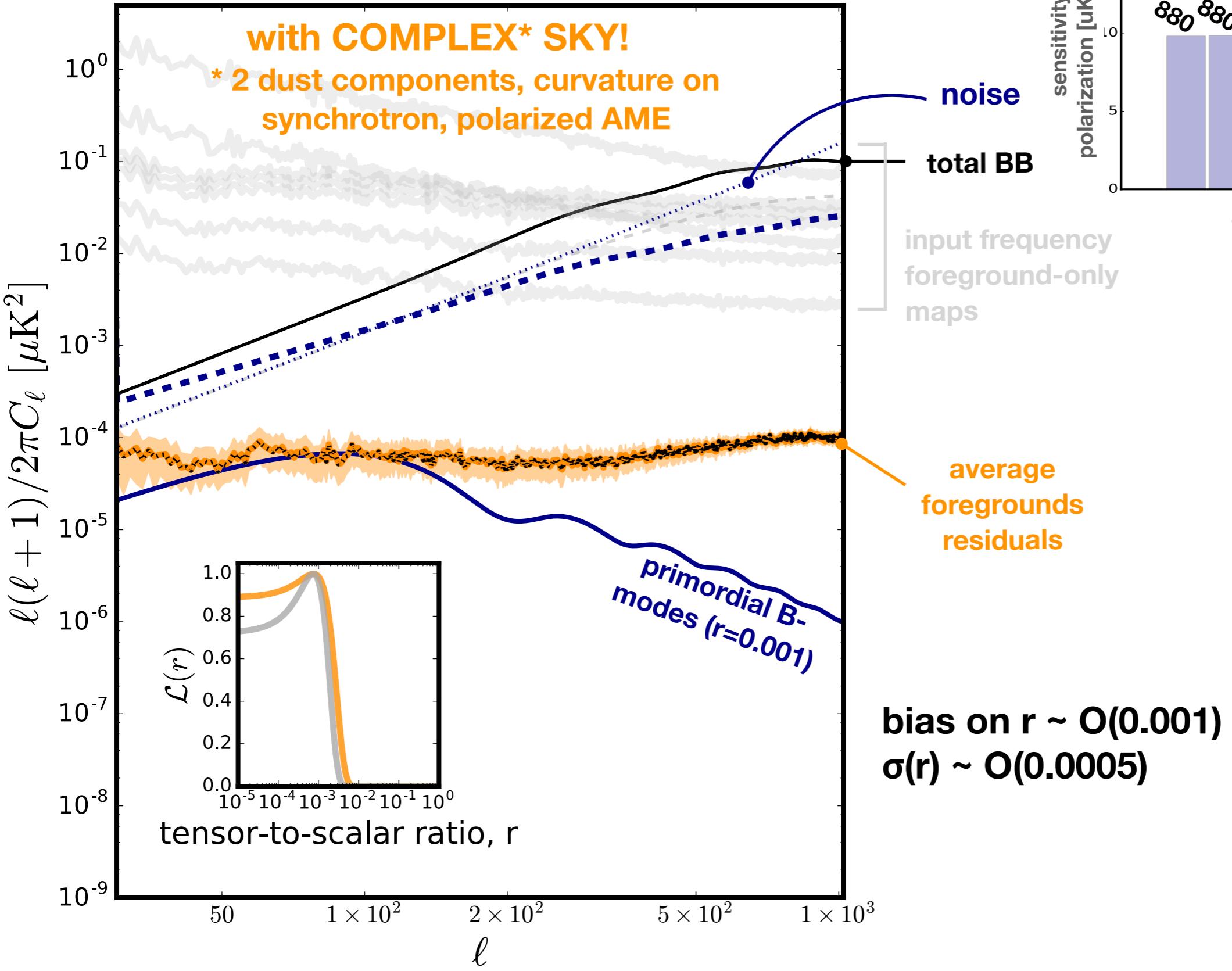
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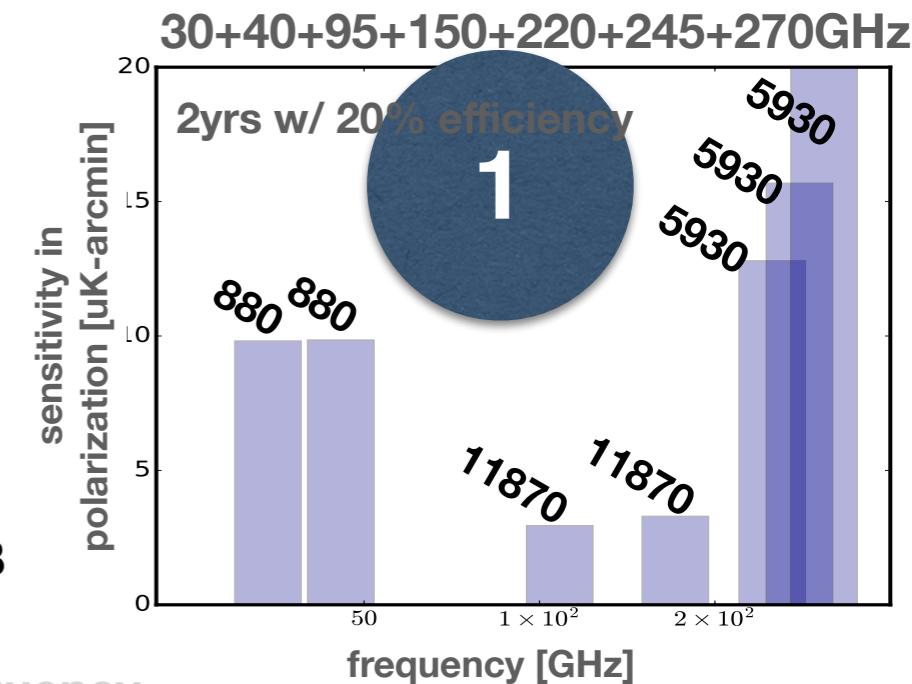
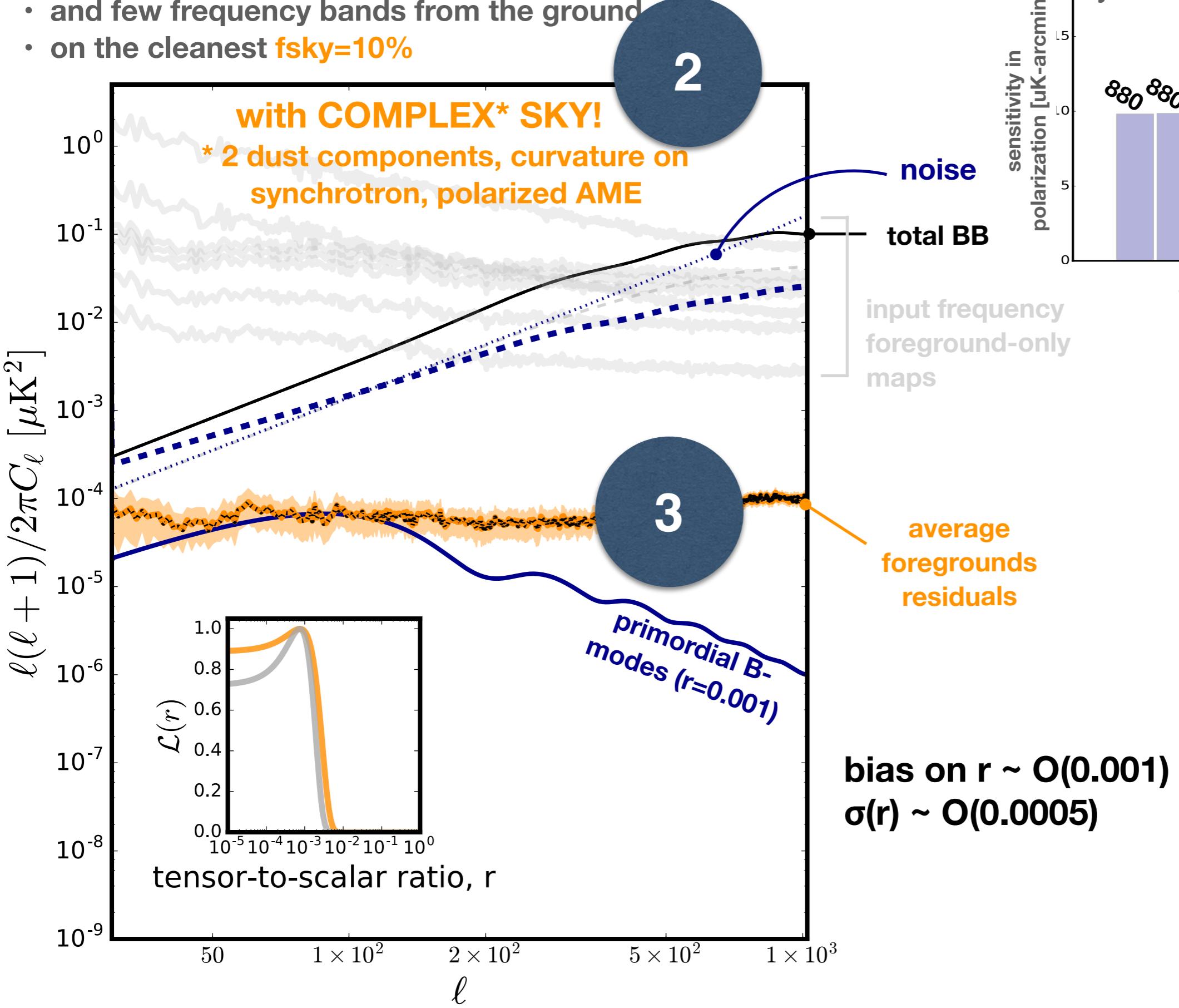
toy example

- with priors from Planck on β , fit for single $\{\beta_d, \beta_s\}$ only
- and few frequency bands from the ground
- on the cleanest $f_{sky}=10\%$



toy example

- with priors from Planck on β , fit for single $\{\beta_d, \beta_s\}$ only
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One should not forget about point sources!

Exploring Cosmic Origins with CORE: B-mode Component Separation M. Remazeilles et al, JCAP, 2017

- In general, the compact source contribution does not impact the large angular scales (near the reionization peak), but can play an important role on intermediate and small angular scales where the lensing-induced B-mode signal is present (Curto et al. 2013).

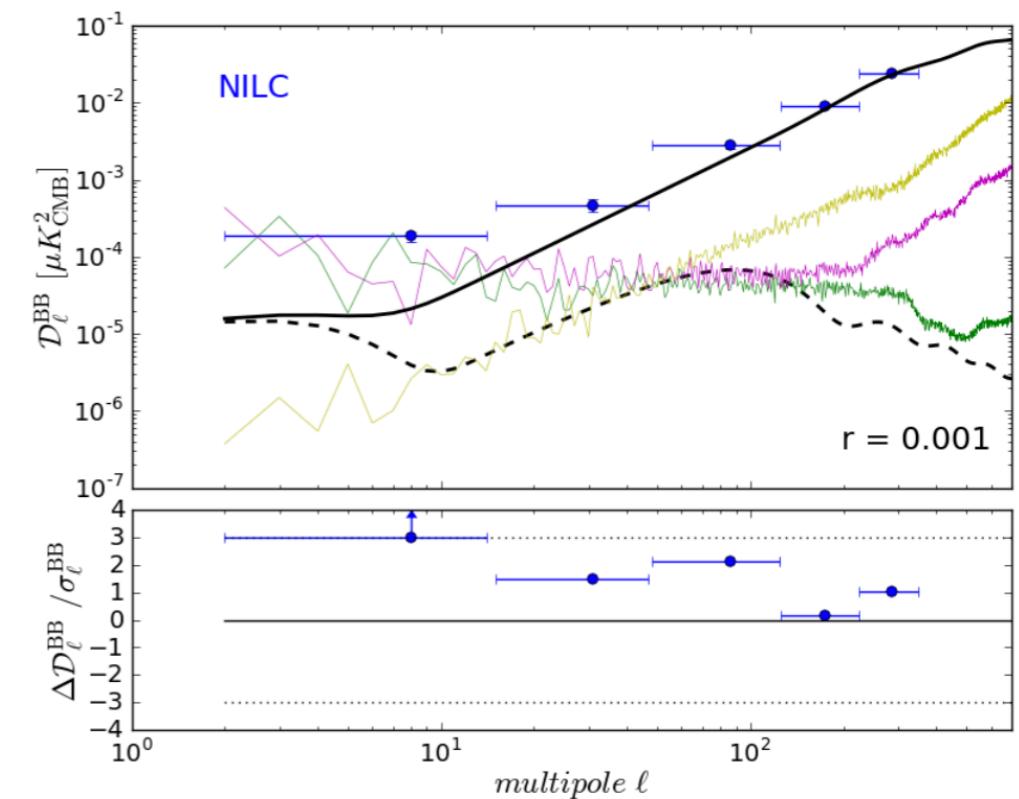
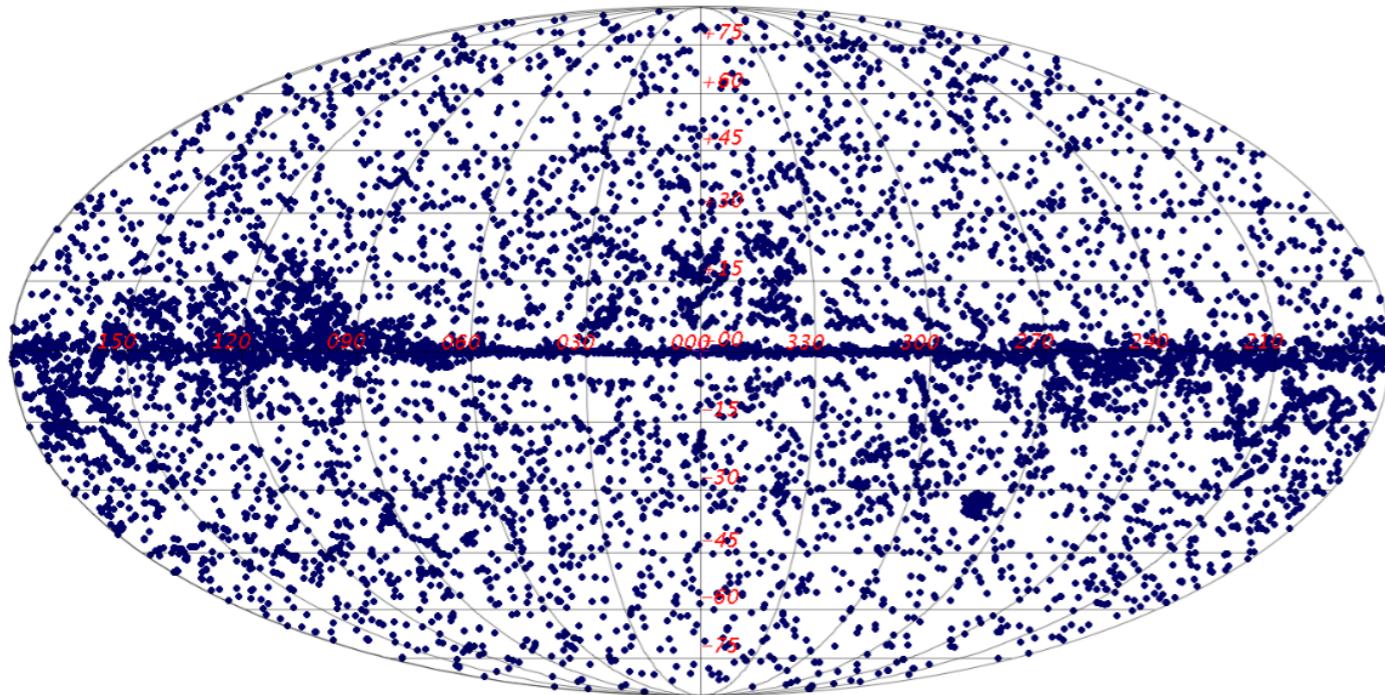


Figure 4. Union of 60 to 600 GHz polarization masks used in the analysis for mitigating the contamination from polarized compact sources. Individual polarized sources are detected in each frequency band of *CORE*.

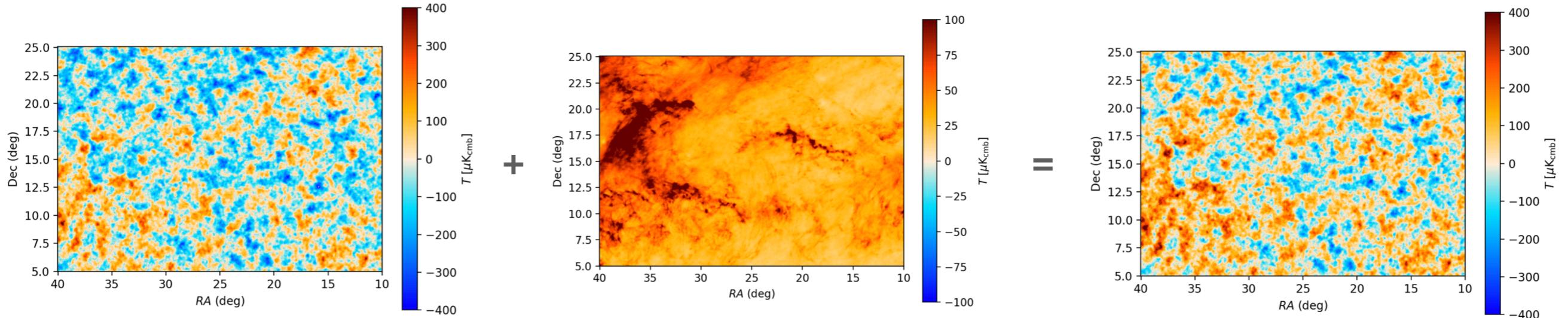
- “careful treatment is required for CMB B-mode polarization observations if the tensor-to-scalar ratio, r , is $\ll 10^{-2}$ ”

Effect of foregrounds on lensing reconstruction and delensing

Exploring cosmic origins with CORE: gravitational lensing of the CMB

A. Challinor et al, JCAP, 2017

+ see also Fantaye, Baccigalupi, Leach, Yadav (2012)

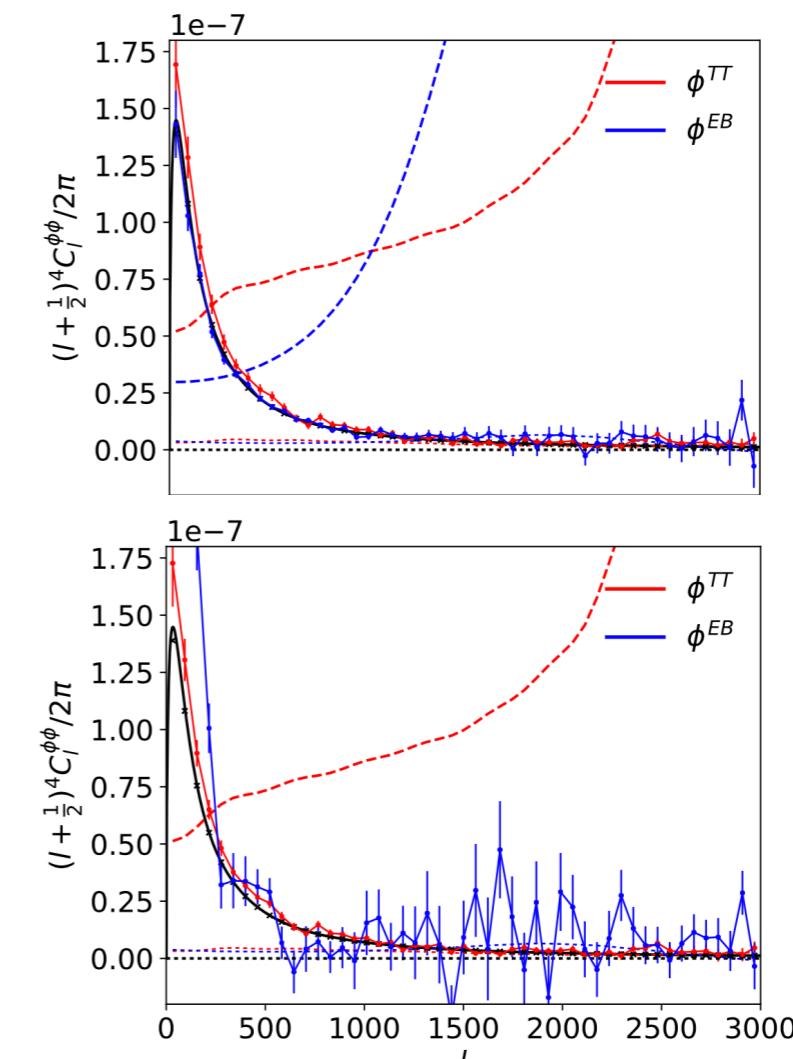
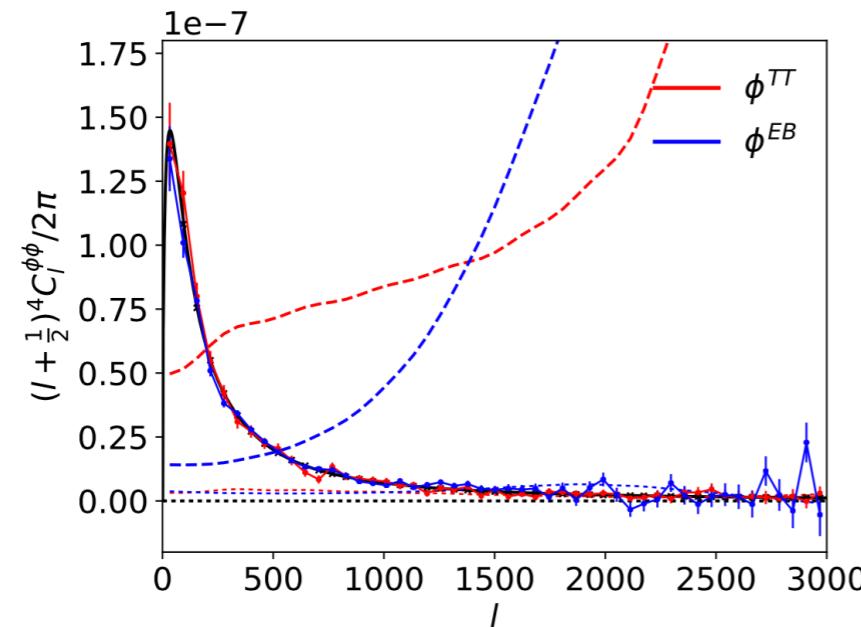
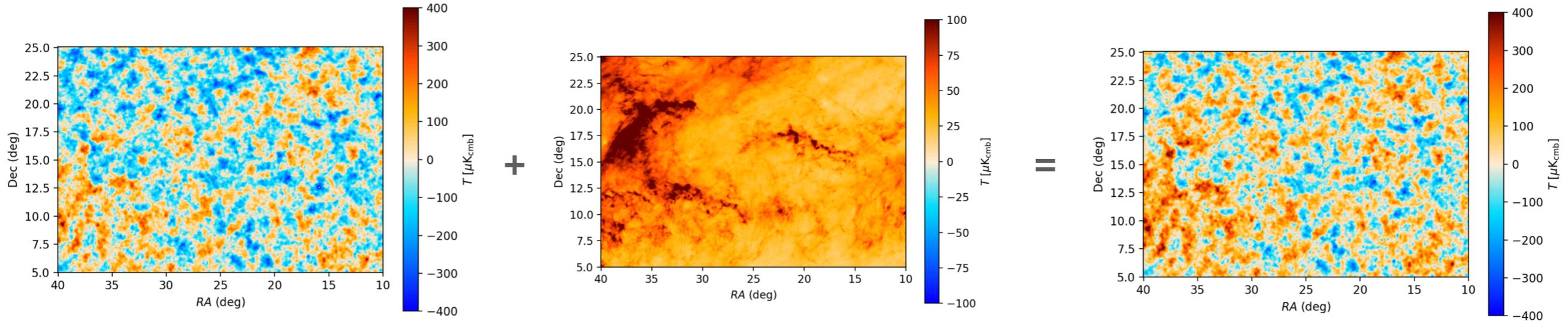


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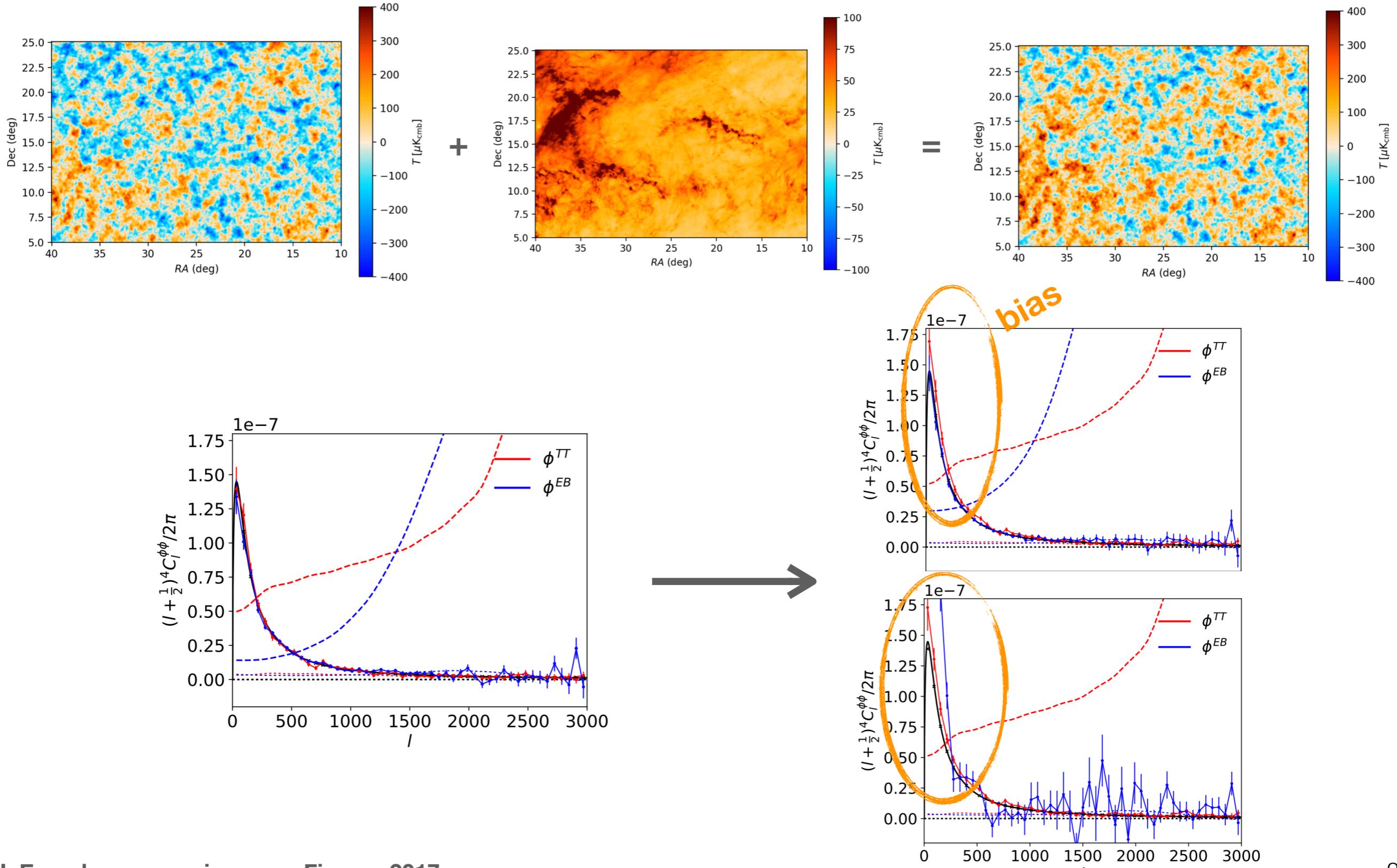


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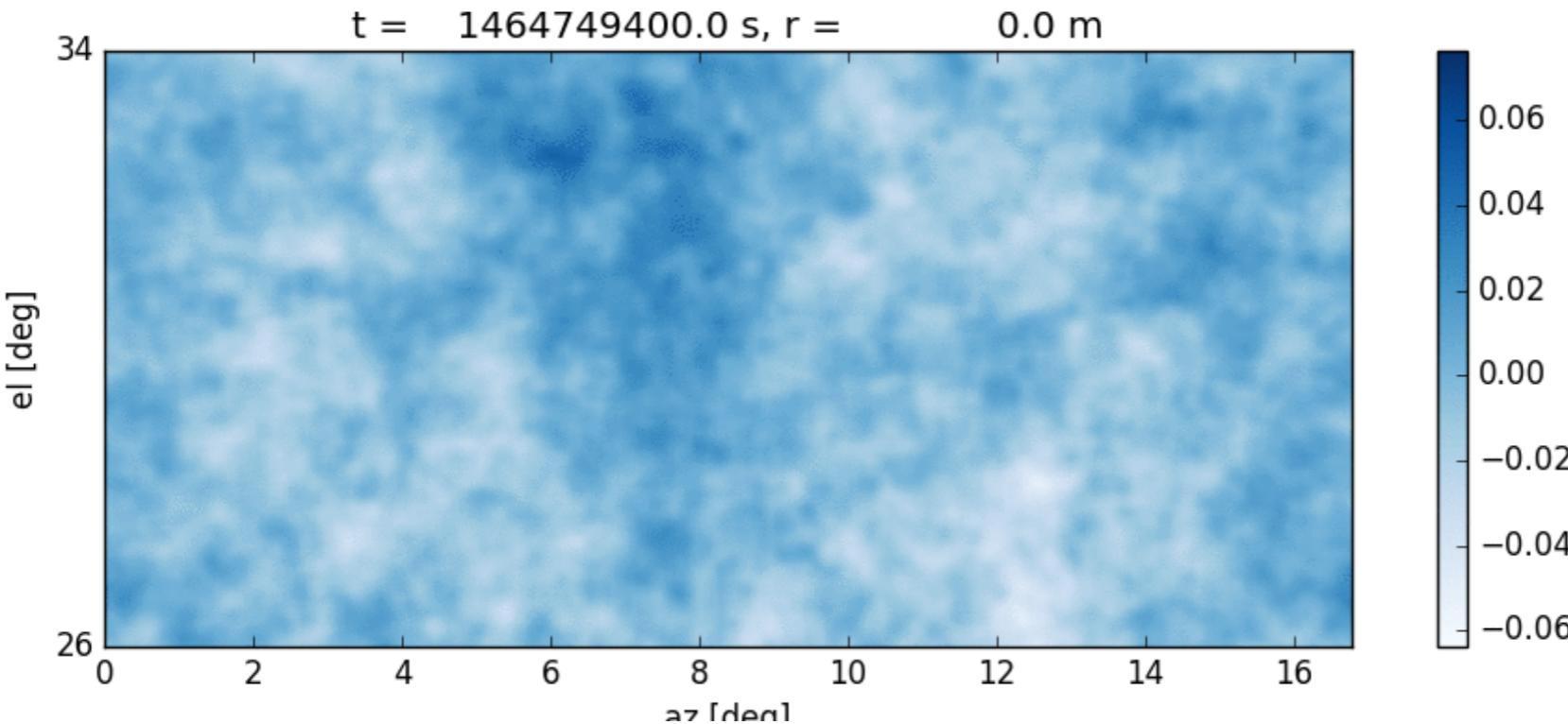


Modeling Atmospheric Emission for CMB Ground-based Observations

JE et al.

The Astrophysical Journal, Volume 809, Issue 1, article id. 63, 19 pp. (2015) arXiv:1501.07911

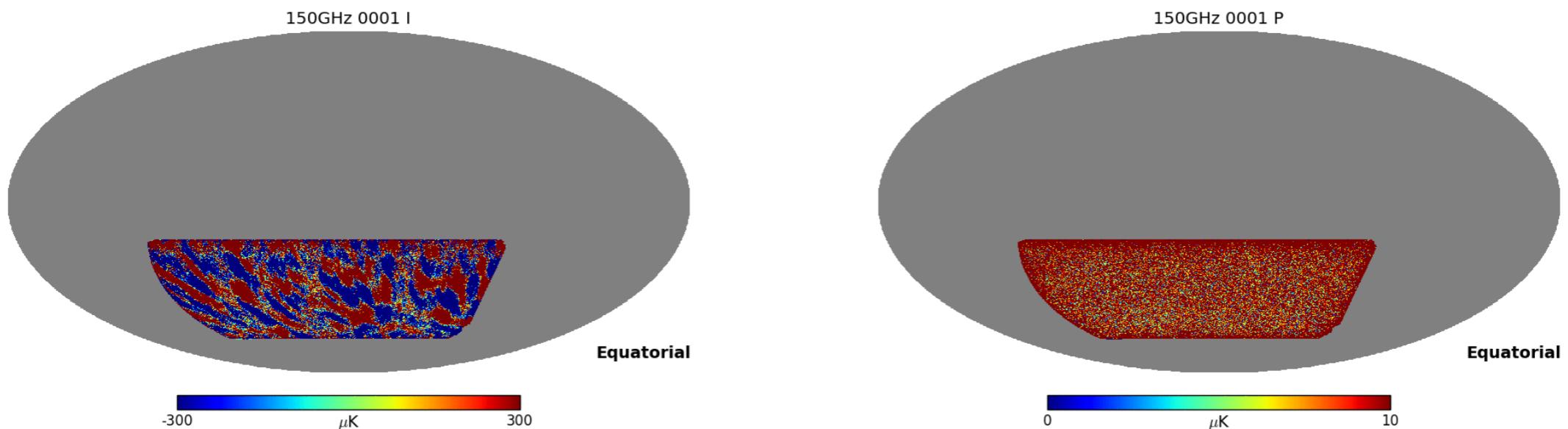
The telescope's view through one realization of turbulent, wind-blown, atmospheric water vapor.



see talk by
Julian Borrill

credit: C³ team @ LBNL

Cumulative daily maps of the sky temperature and polarization at each frequency showing how the atmosphere and noise integrate down over time.

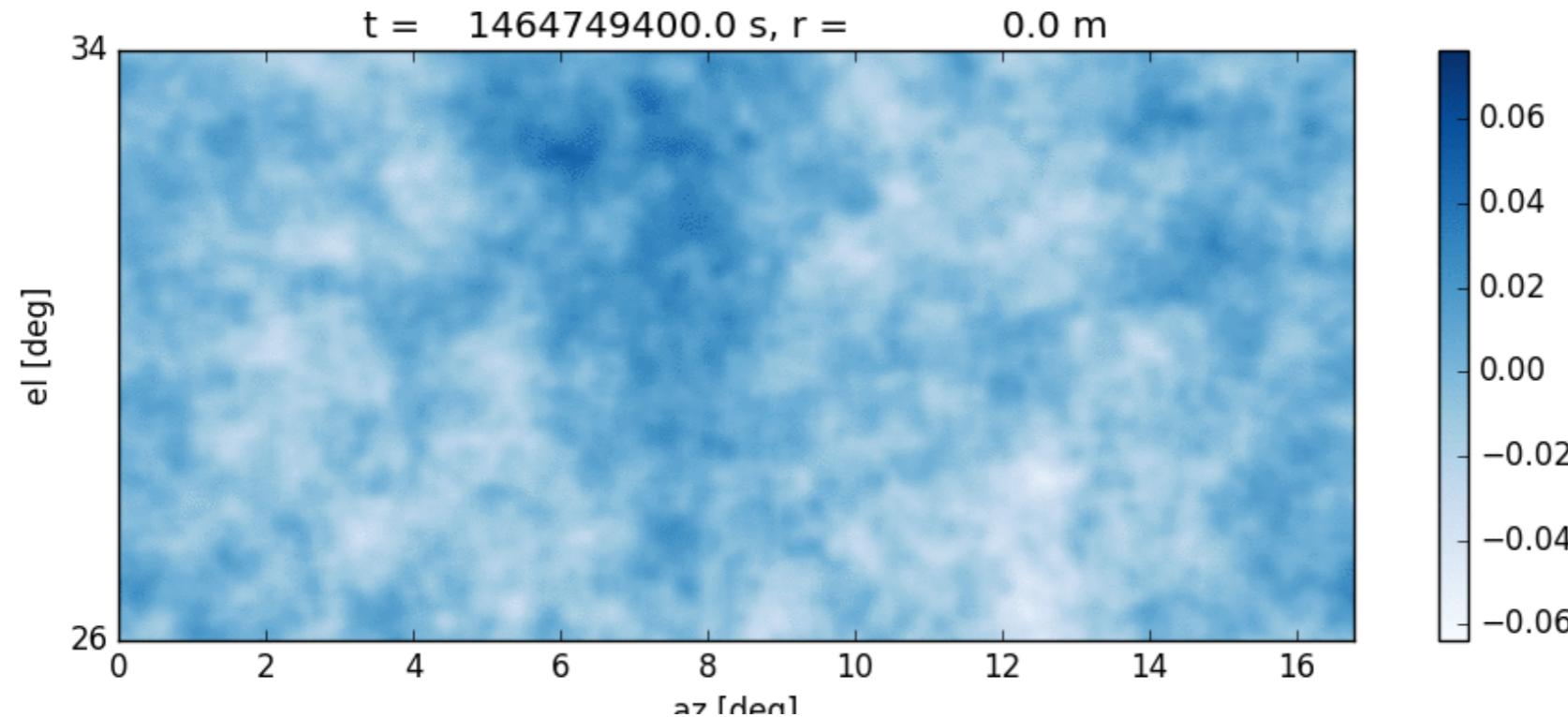


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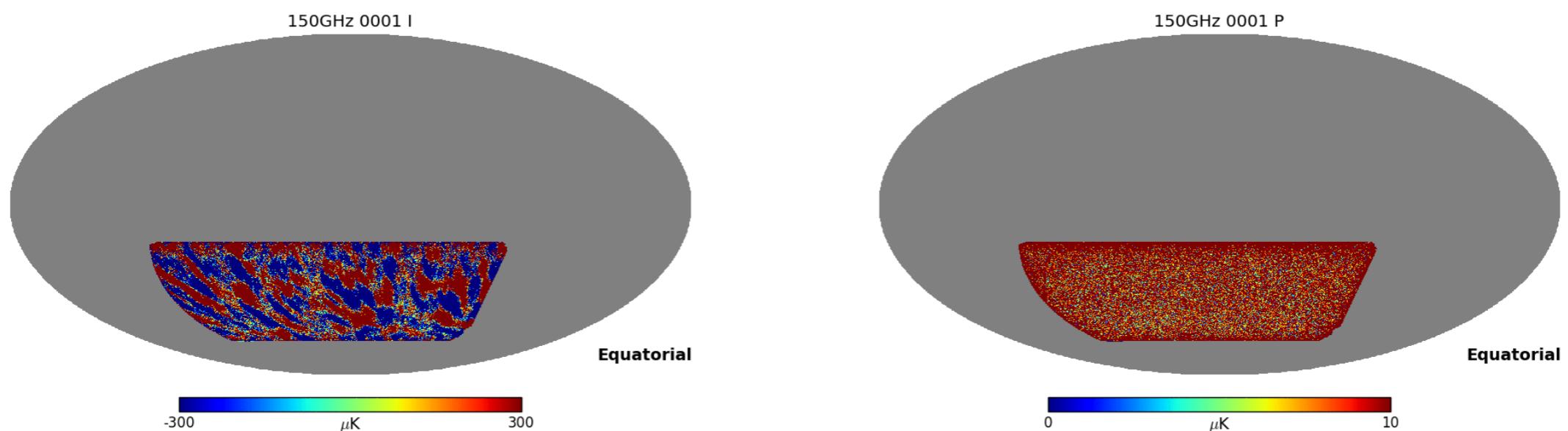
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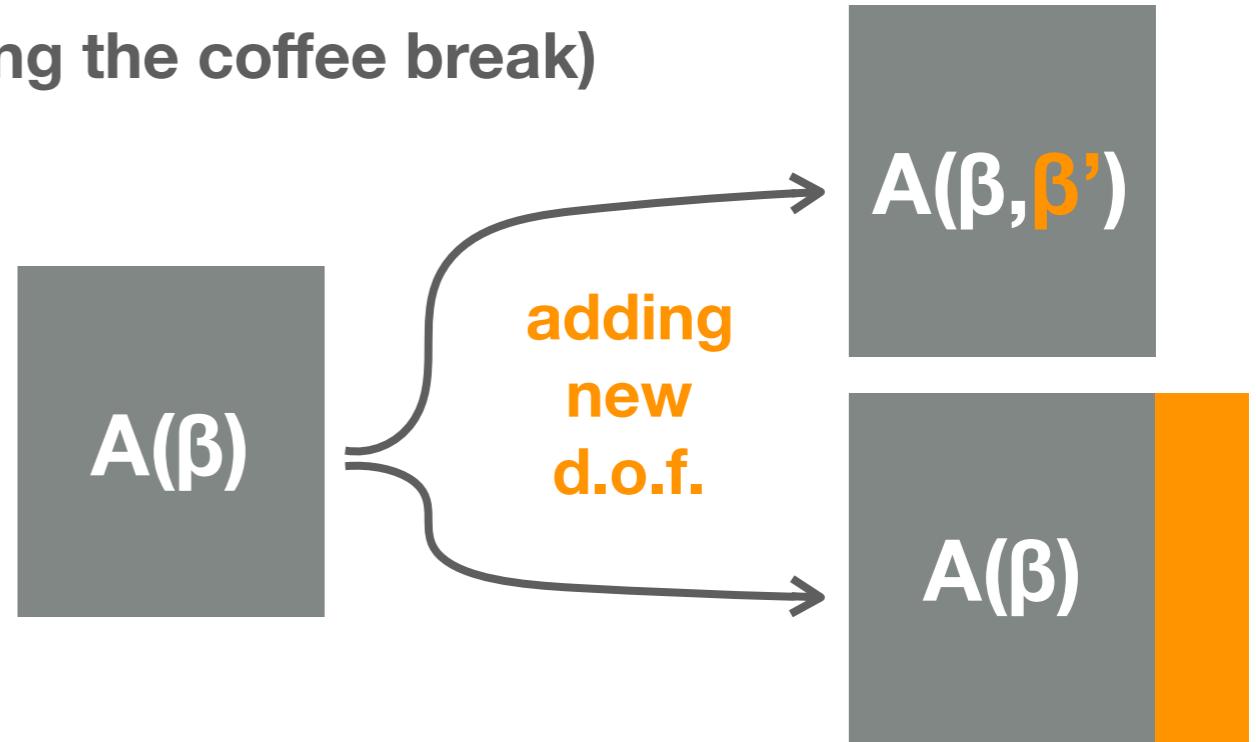
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- component separation is about making a **trade off** between **degrees of freedom in the modeling** and the **statistical error budget**;
- showing that one can **robustly** measure $r=O(0.001)$ is very challenging given the latest foregrounds modeling;
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