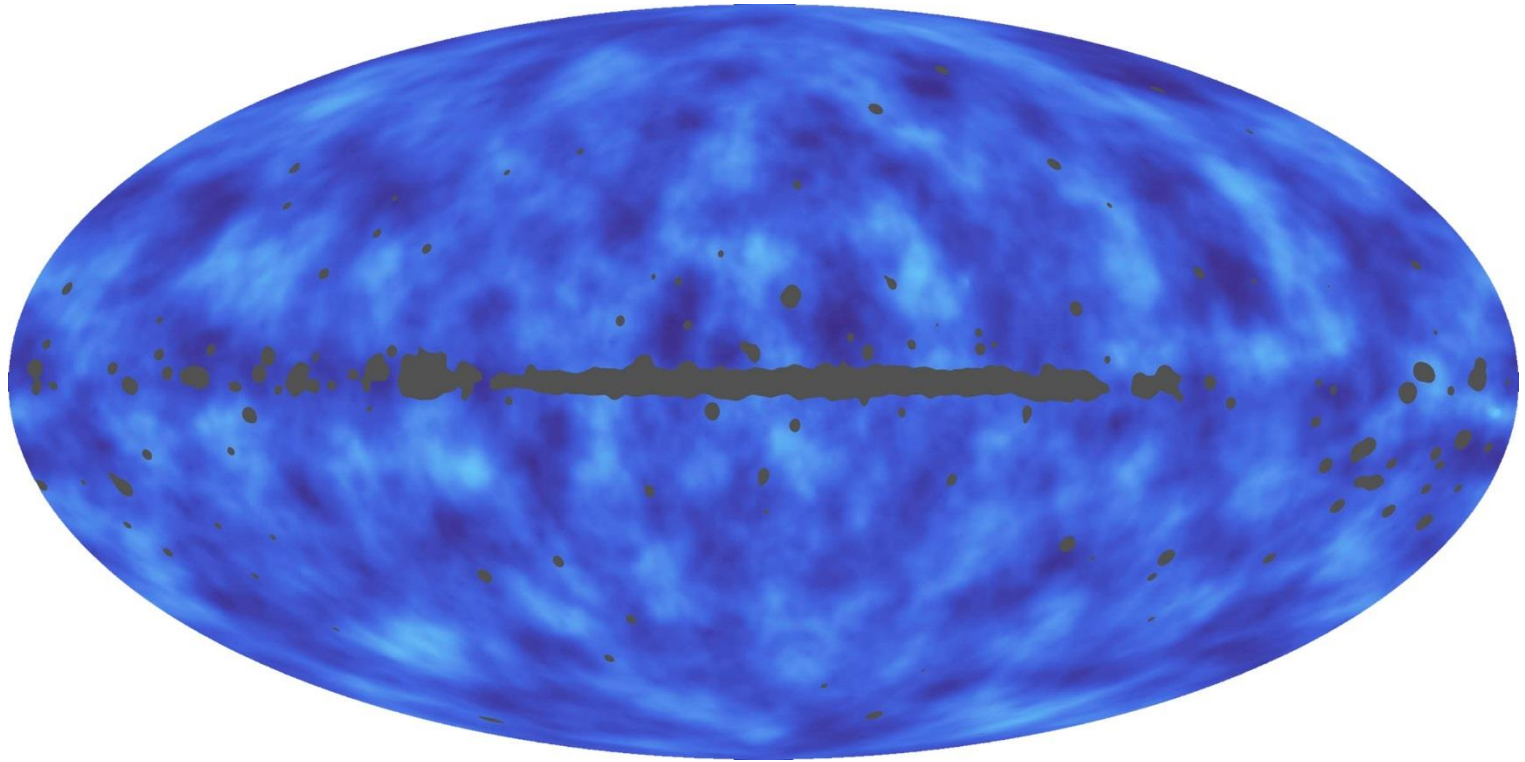


# CMB Lensing and Delensing

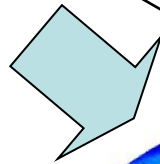
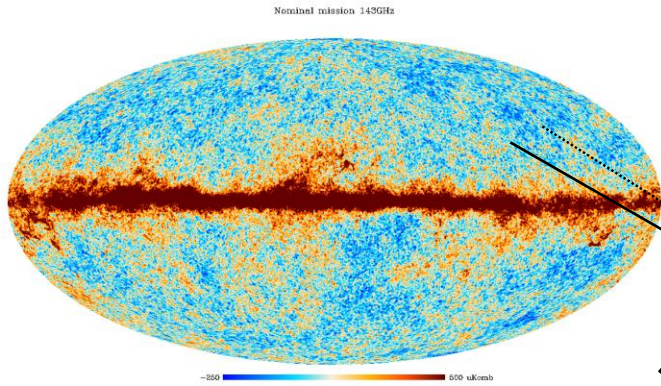
Antony Lewis



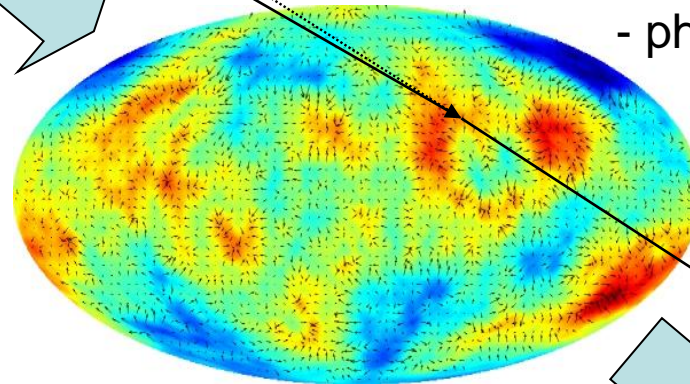
<http://cosmologist.info/>

# CMB Lensing

Last scattering surface



Inhomogeneous universe  
- photons deflected



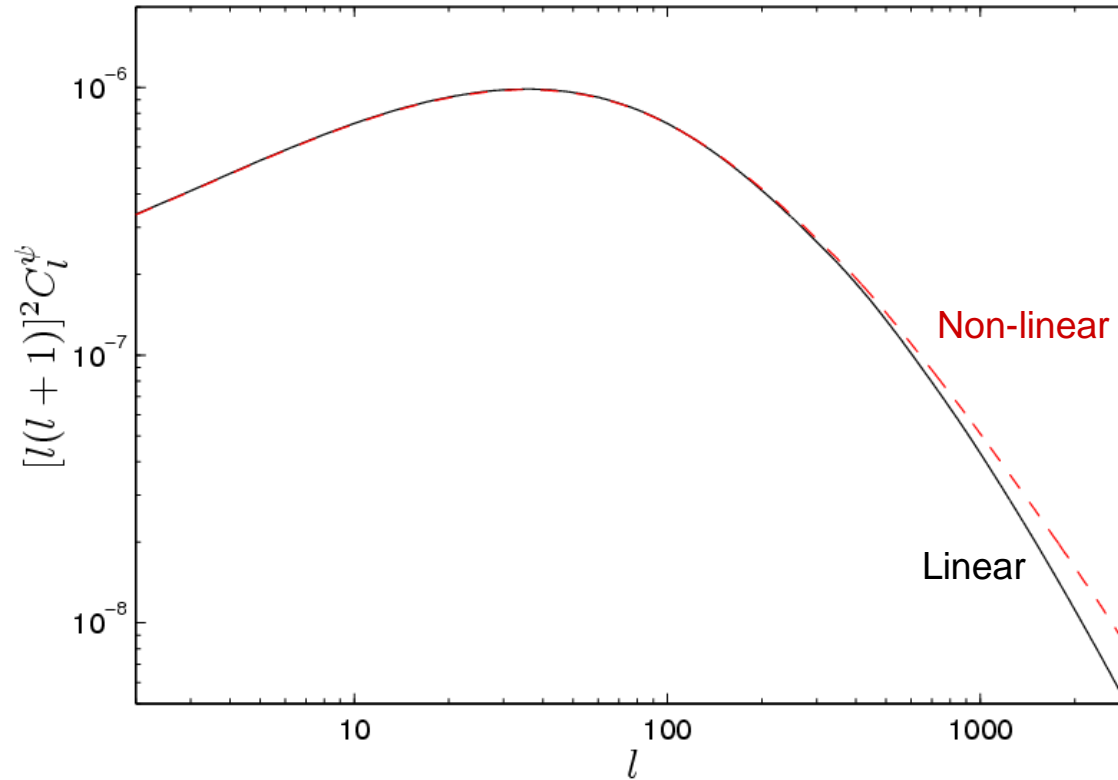
Observer



# Deflection angle power spectrum

Large-scale lenses: potentials nearly linear, clean physics

$$\alpha = \nabla\psi$$



Deflections  $O(10^{-3})$ , but coherent on degree scales

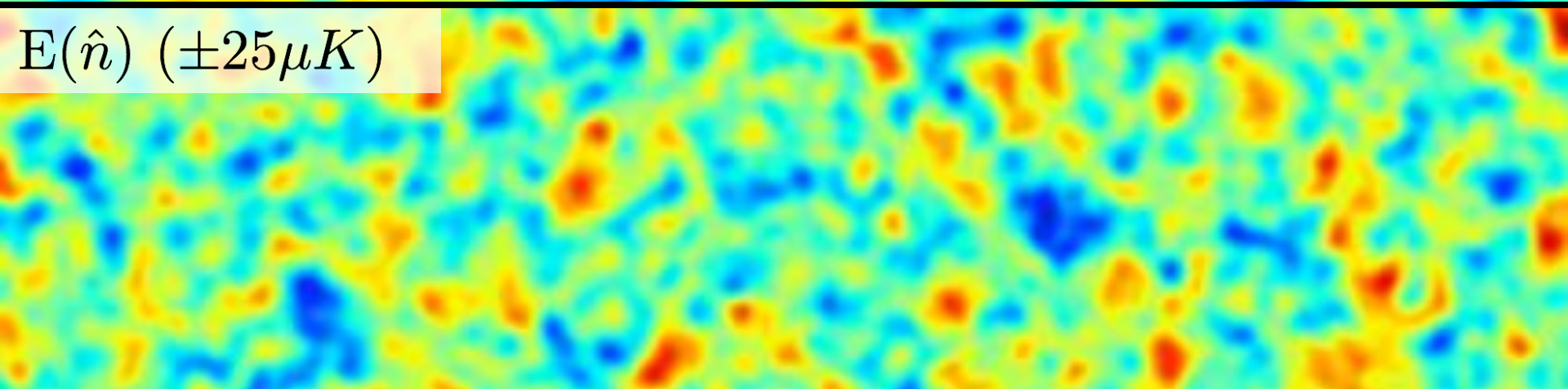
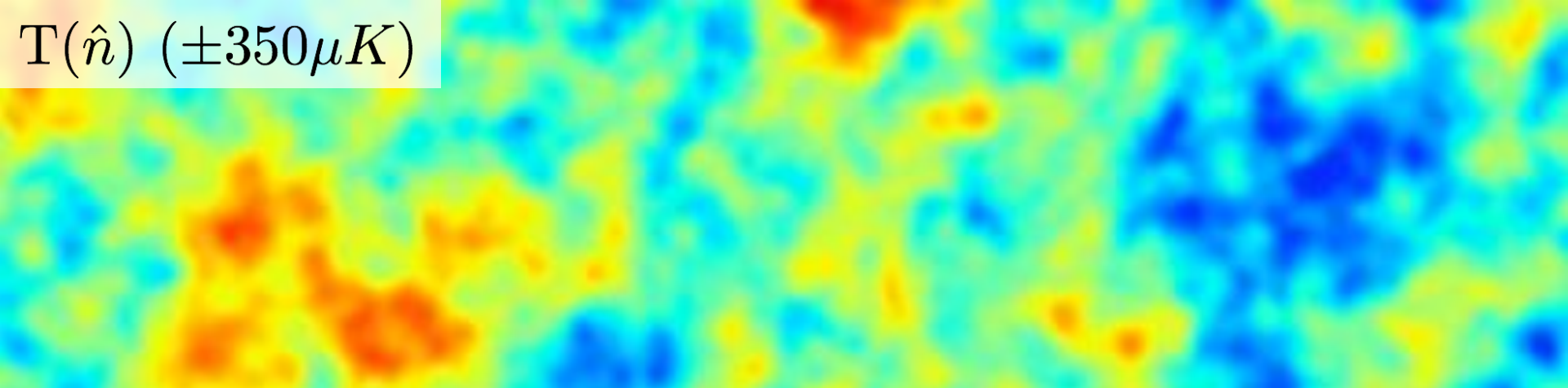
Probes matter distribution at roughly  $0.5 < z < 6$  depending on  $l$

Non-linear structure growth effects not a major headache

$T(\hat{n}) (\pm 350 \mu K)$

$E(\hat{n}) (\pm 25 \mu K)$

$B(\hat{n}) (\pm 2.5 \mu K)$

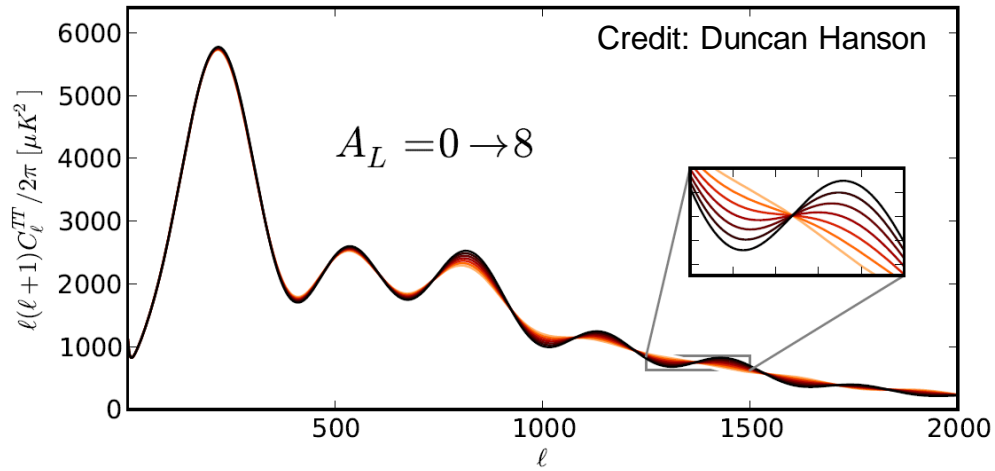


$T(\hat{n}) (\pm 350 \mu K)$

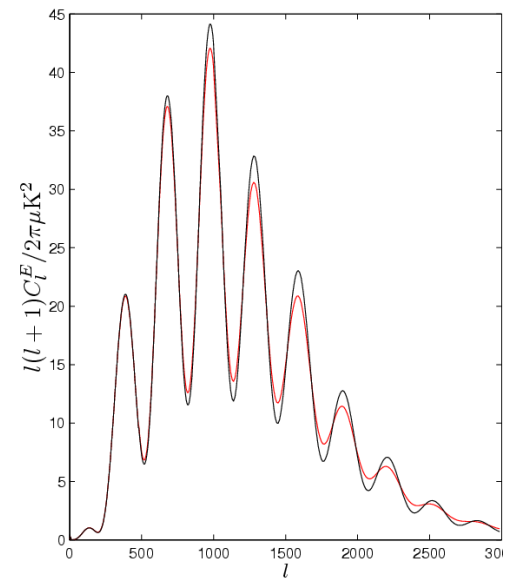
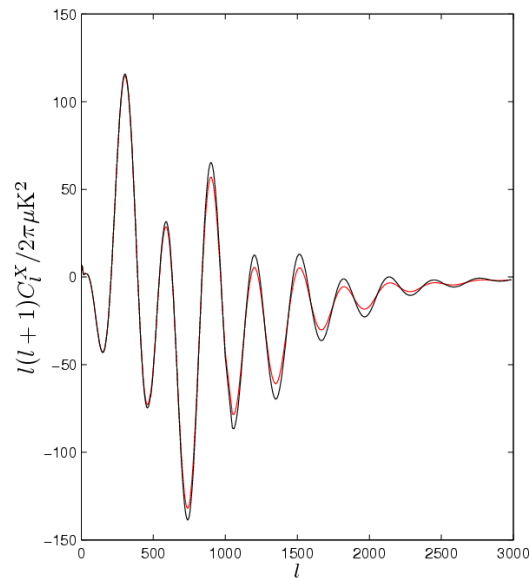
$E(\hat{n}) (\pm 25 \mu K)$

$B(\hat{n}) (\pm 2.5 \mu K)$

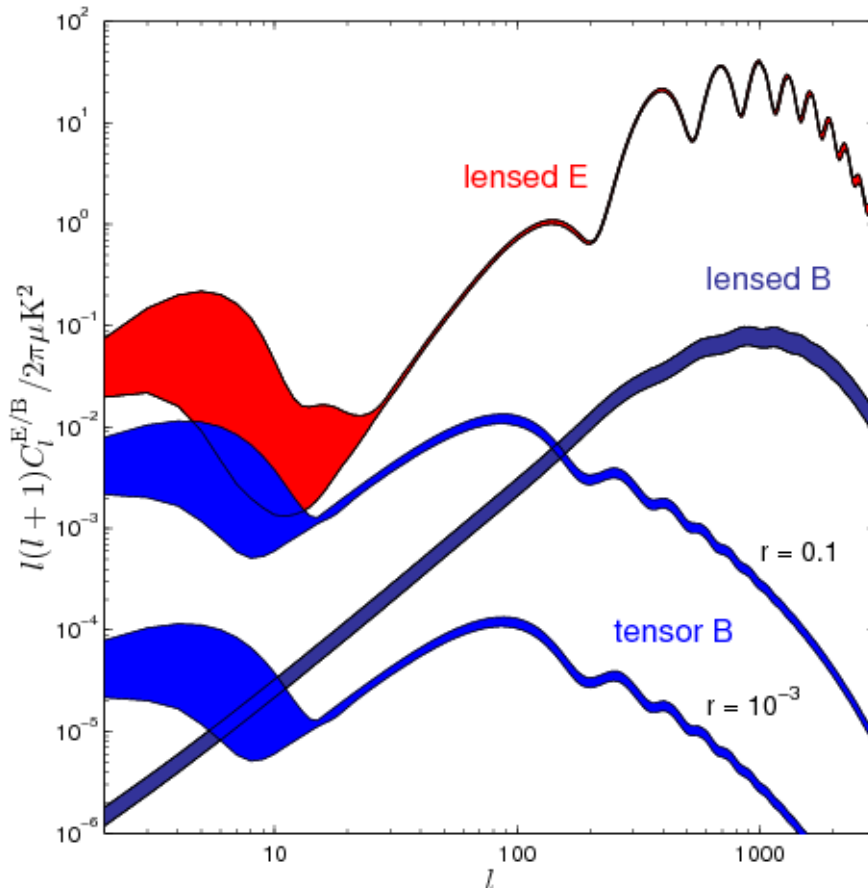
Averaged over the sky, lensing smooths out the power spectrum



TE and EE



# Lensing B-mode

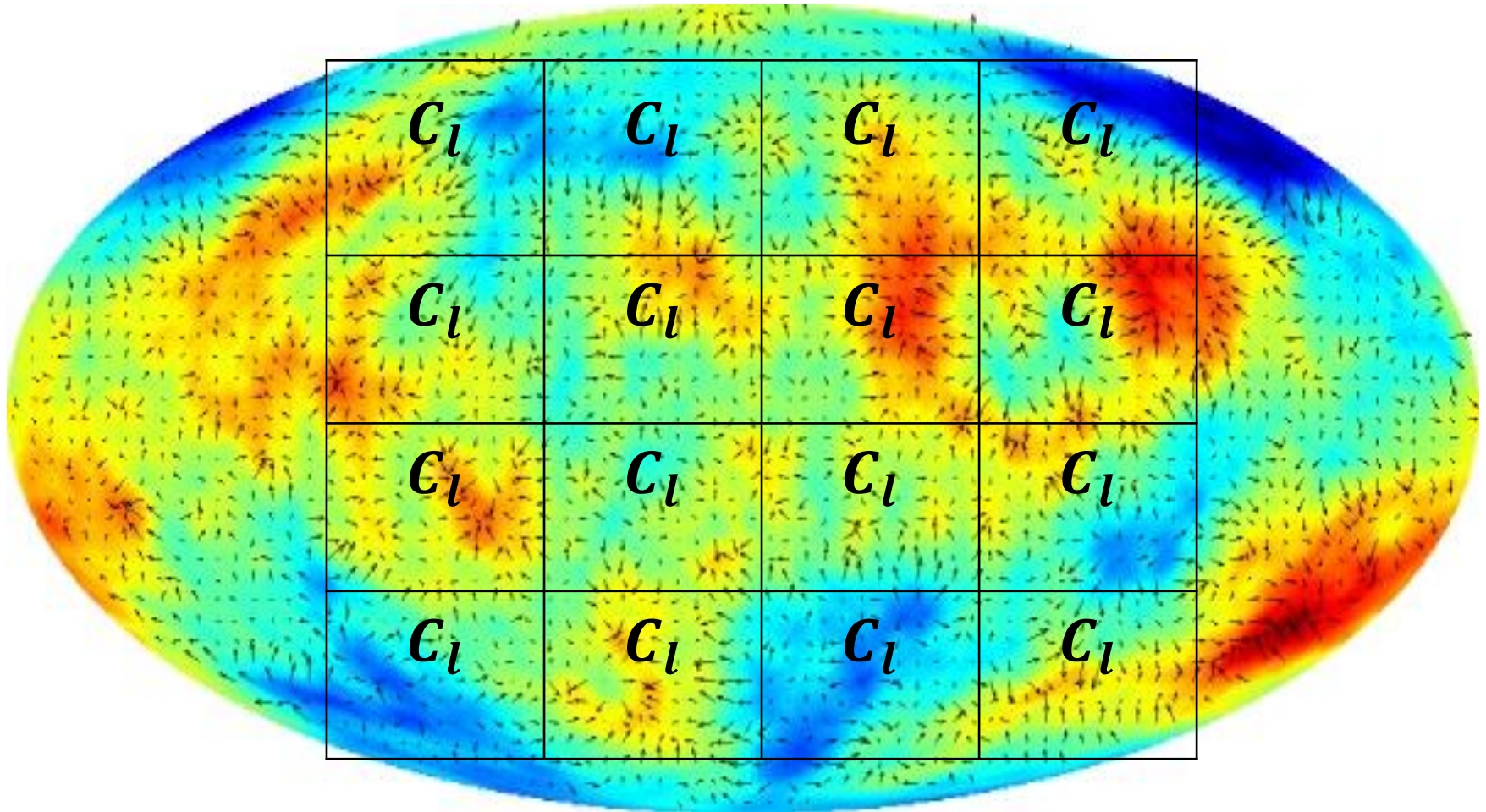


$$\begin{aligned}\tilde{C}_l^B &\sim \int \frac{d^2l'}{(2\pi)^2} l'^4 C_{l'}^\psi C_{l'}^E \sin^2 2(\phi_{l'} - \phi_1) \\ &= \frac{1}{4\pi} \int \frac{dl'}{l'} l'^4 C_{l'}^\psi l'^2 C_{l'}^E,\end{aligned}$$

**For measuring  $r$  lensing B like a white  $\sim 5 \mu K$  arcmin noise**

- Model as noise (power spectrum subtraction – limited by cosmic variance)
- Subtract (map subtraction - *delensing*)

## Lensing reconstruction (concept)



Measure spatial variations in magnification and shear

Use assumed unlensed spectrum, and unlensed statistical isotropy



# Lensing Reconstruction Estimators

## Quadratic estimators

Measure off-diagonal covariance induced by lensing

$$\hat{\psi}(\mathbf{L}) \equiv N(\mathbf{L}) \int \frac{d^2\mathbf{l}}{2\pi} \tilde{\Theta}(\mathbf{l}) \tilde{\Theta}^*(\mathbf{l} - \mathbf{L}) g(\mathbf{l}, \mathbf{L}); \quad (\text{Hu \& Okamoto, etc.})$$

- Fast to implement
- Very nearly optimal for current and S2/S3 observations

## Maximum likelihood

For fixed lenses, sky is Gaussian but anisotropic. Maximize likelihood:

$$-\mathcal{L}(\hat{\Theta}|\alpha) = \frac{1}{2} \hat{\Theta}^T \left( \hat{C}^{\hat{\Theta}\hat{\Theta}} \right)^{-1} \hat{\Theta} + \frac{1}{2} \ln \det(\hat{C}^{\hat{\Theta}\hat{\Theta}}),$$

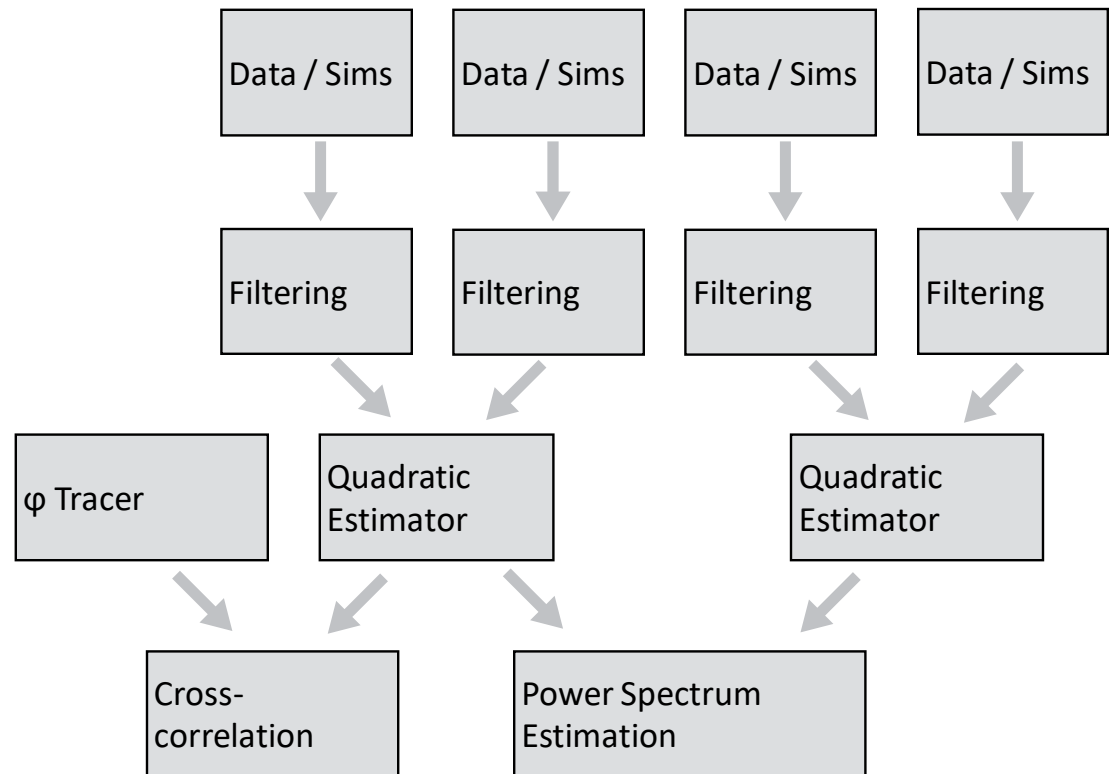
- More expensive, but tractable iteratively (Hirata & Seljak 03, Carron & Lewis 17)
- Better reconstruction at S4 noise levels

# Quadratic Estimator Pipeline

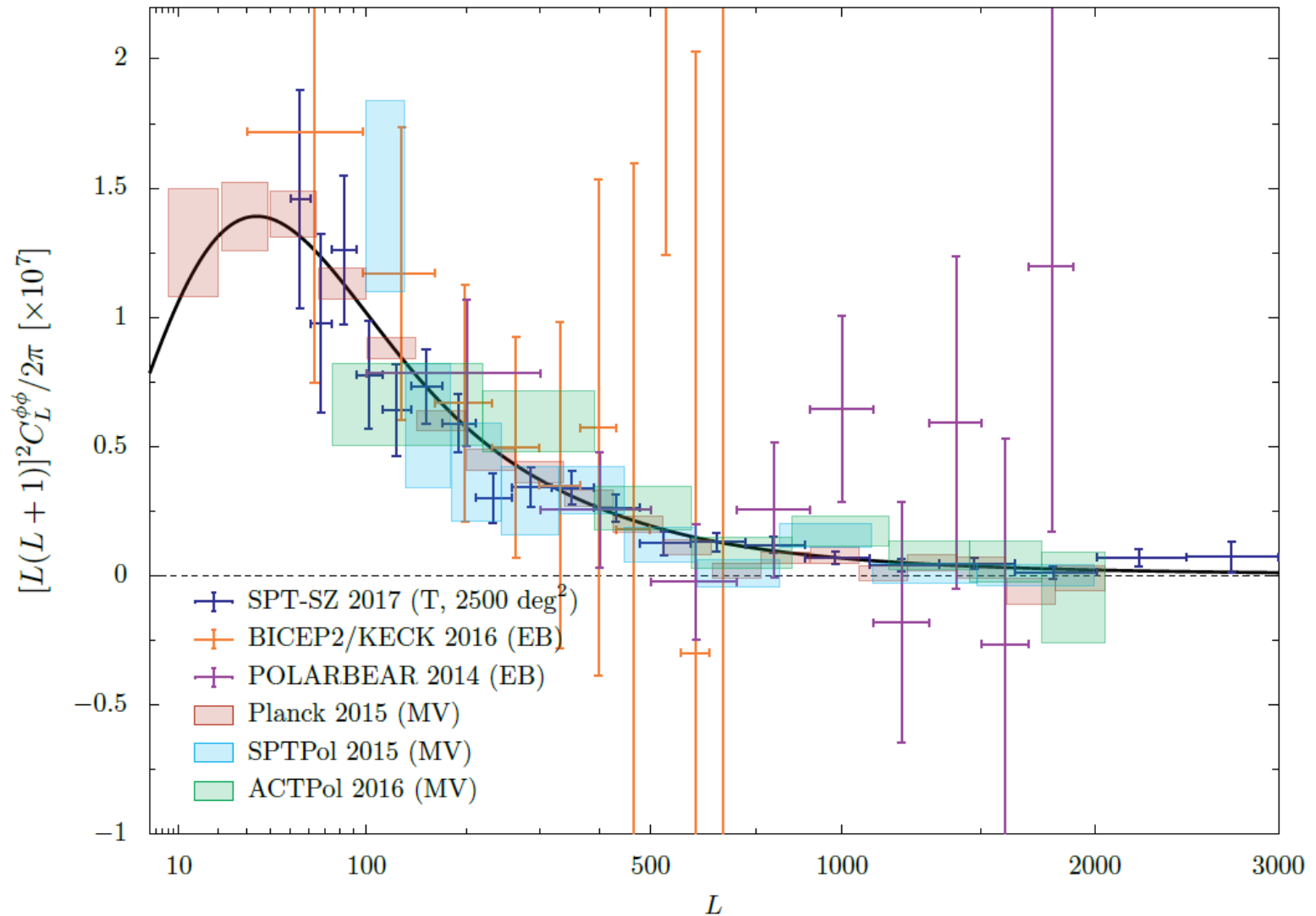
→ process input maps

→ estimate lensing potential from anisotropic 2-point

→ estimate lensing power spectrum.



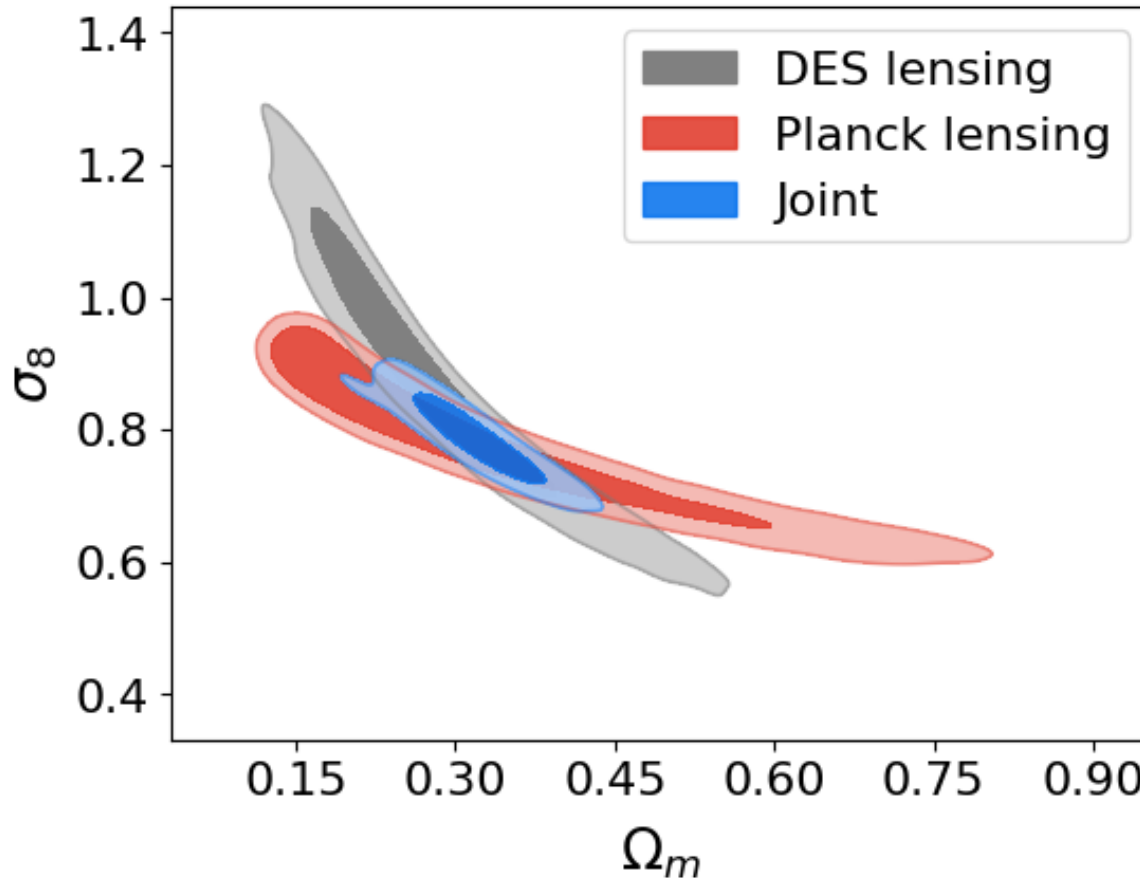
# Current lensing reconstruction power spectra



# CMB lensing currently competitive with galaxy lensing

Probes higher redshift  $\Rightarrow$  constrains  $\Omega_m \sigma_8^{0.25}$  vs. galaxy  $\Omega_m \sigma_8^{0.5}$

DES 1YR +Planck lensing only LCDM forecast



DES 1Yr has 10 nuisance parameters, conservative cuts: limited by modelling not statistics  
CMB lensing currently limited by low S/N (and only one source redshift plane)

# CMB lensing to calibrate shear for galaxy lensing

Galaxy lensing surveys measure (roughly) galaxy ellipticity  $e_g$ .  
Hard to relate directly to lensing shear  $\gamma_{\text{lens}}$ .

$$e_g \sim (1 + m)\gamma_{\text{lens}}$$

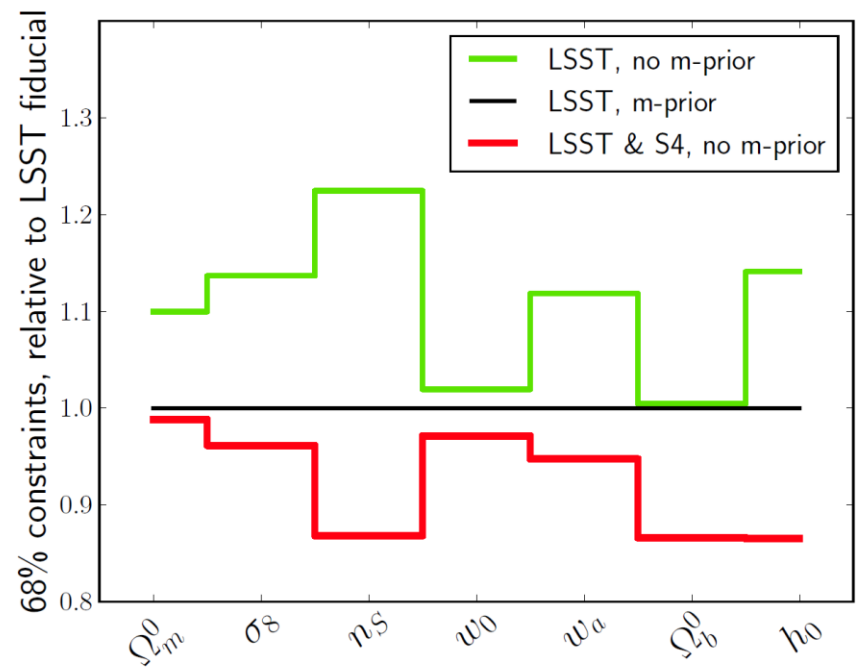
$m$  could mimic different dark energy models.

Cross-correlation with CMB lensing can measure  $m$

**Valuable for EUCLID, WFIRST, LSST, etc.**

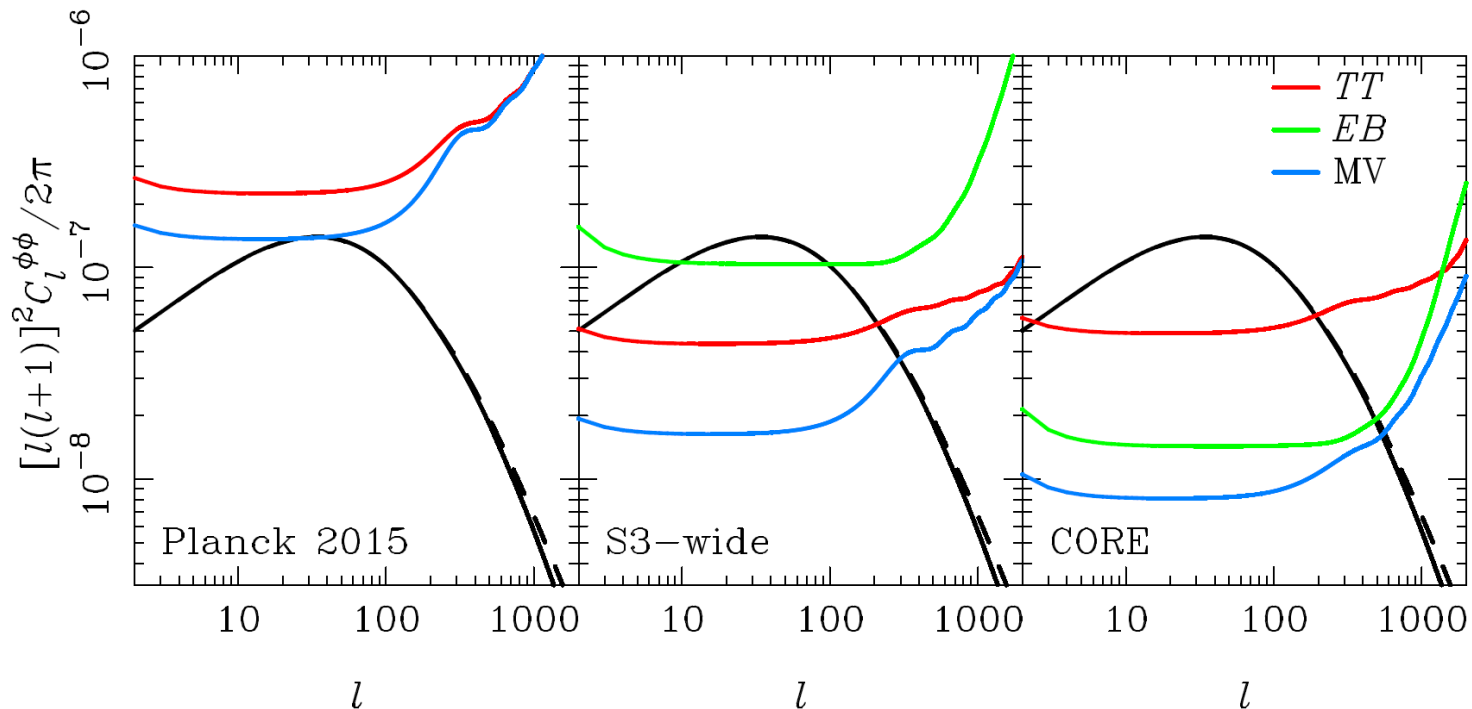
- more robust prior-independent constraints on dark energy

e.g. S4 to calibrate LSST

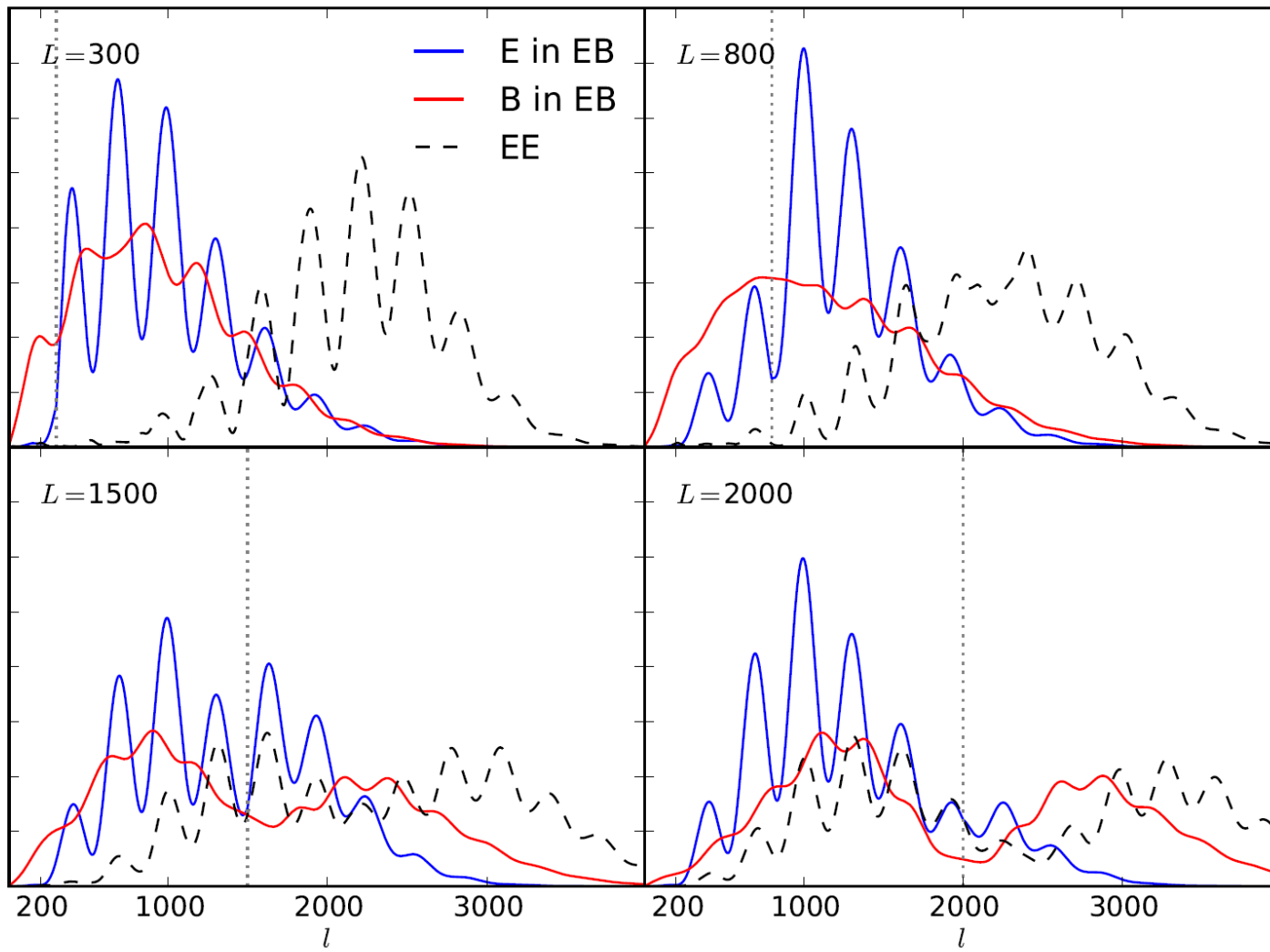


# Lensing reconstruction with polarization

- Expect *no* primordial small-scale B modes (r-modes only large scales  $l < \sim 300$ )
- *All* small-scale B-mode signal is lensing: *no* cosmic variance confusion with primordial signal as for E and T
- Polarization data does *much* better than temperature if sufficiently good S/N (mainly EB estimator).



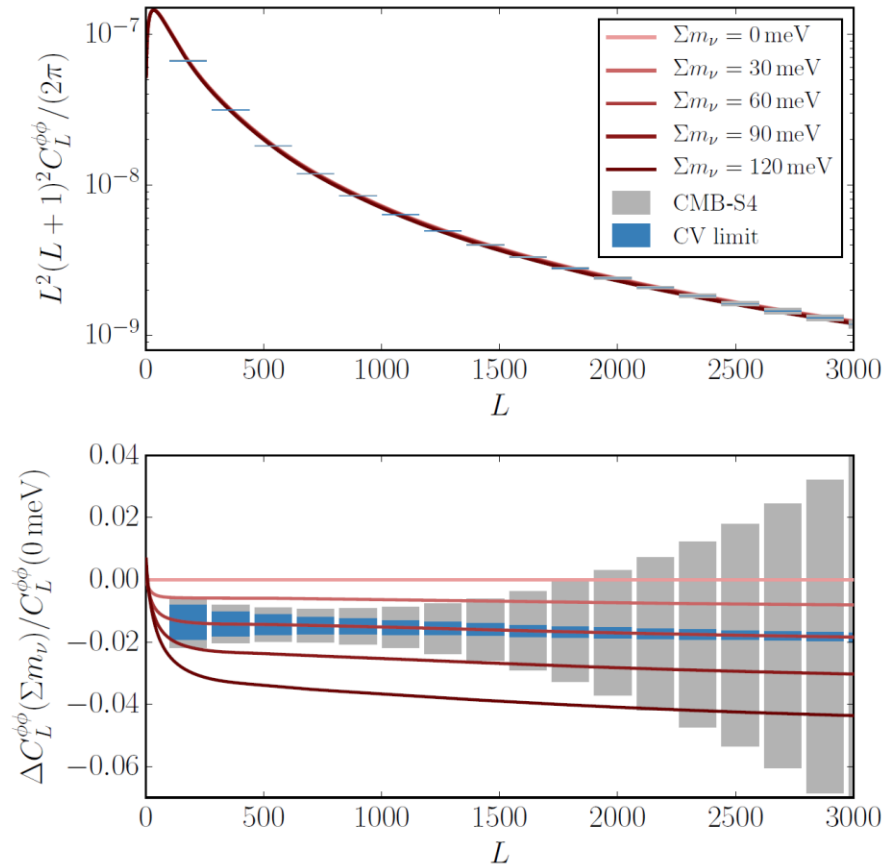
Lensing reconstruction at  $L$  typically needs E,B at  $\ell \gg L$ . **Need small scales.**



(4  $\mu$ K arcmin noise, 1.4 arcmin beam)

# Neutrino mass from high S/N lensing reconstruction

see Erminia's talk



**Figure 49.** Constraining neutrino mass with CMB-S4. Top: lensing power spectra for multiple neutrino masses (curves) together with forecasted errors for S4. Bottom: residual from curve at zero neutrino mass. Error boxes are shown centered at the minimal value of 60 meV. S4 will be targeted to resolve differences in neutrino mass of 20 meV.



# Delensing

$$X^{\text{len}}(\mathbf{n}) = X^{\text{unl}}(\mathbf{n} + \alpha(\mathbf{n}))$$

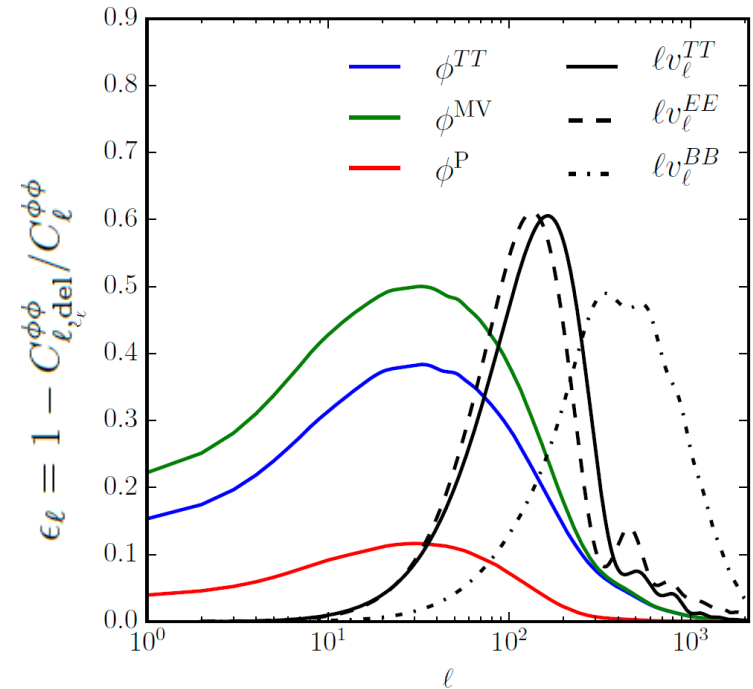
Measure  $\psi$  (hence  $\alpha = \nabla\psi$ )

Re-map back lensed fields  
or subtract perturbative lensing signal

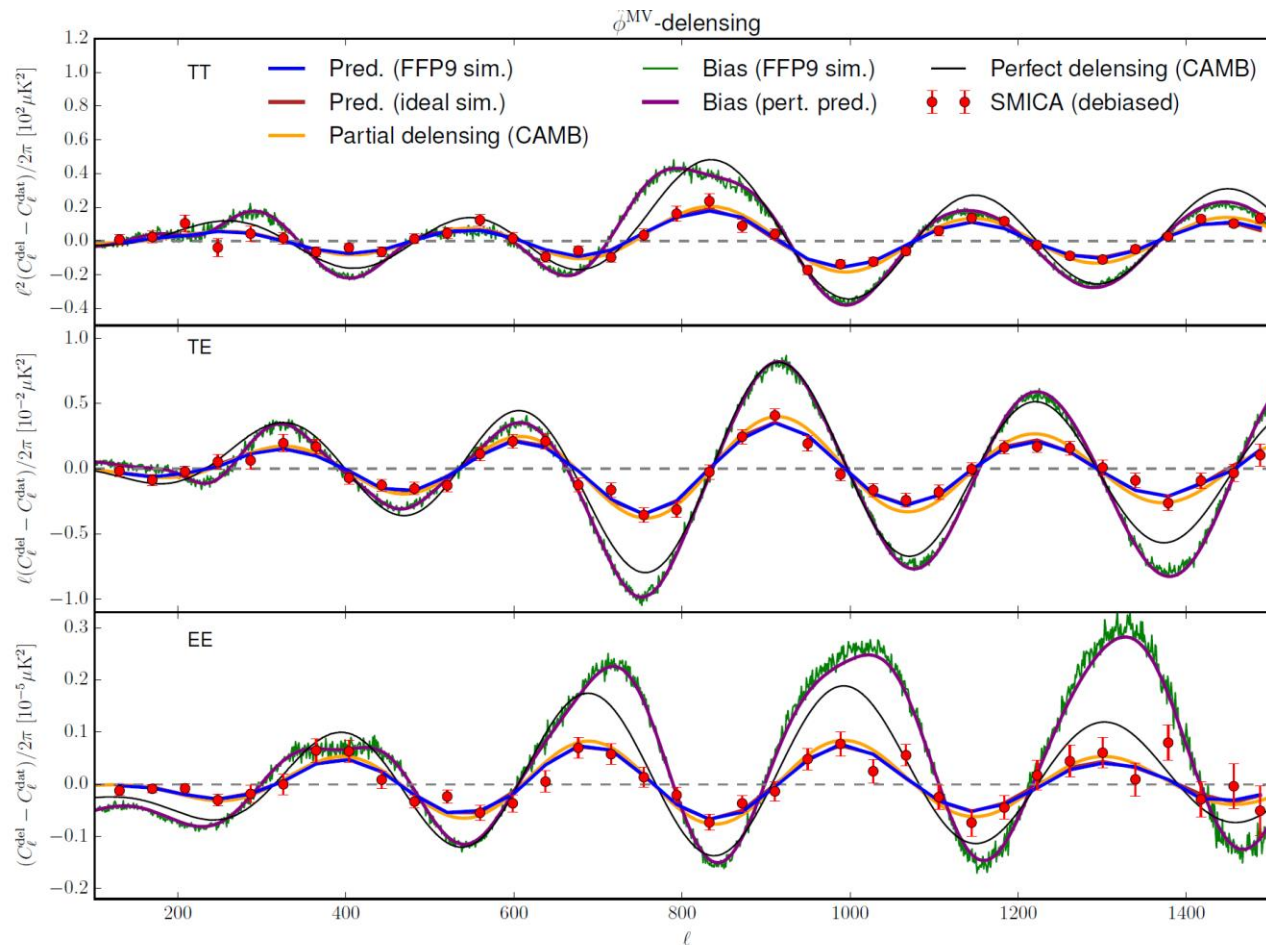
To measure  $\psi$ :

1. Use external tracer of matter,  
e.g. CIB.  
([Sherwin et al 2015](#), [Larsen et al. 2016](#))
2. Use internal lensing reconstruction

Current (Planck) delensing efficiencies



Carron, Lewis, Challinor arXiv:1701.01712



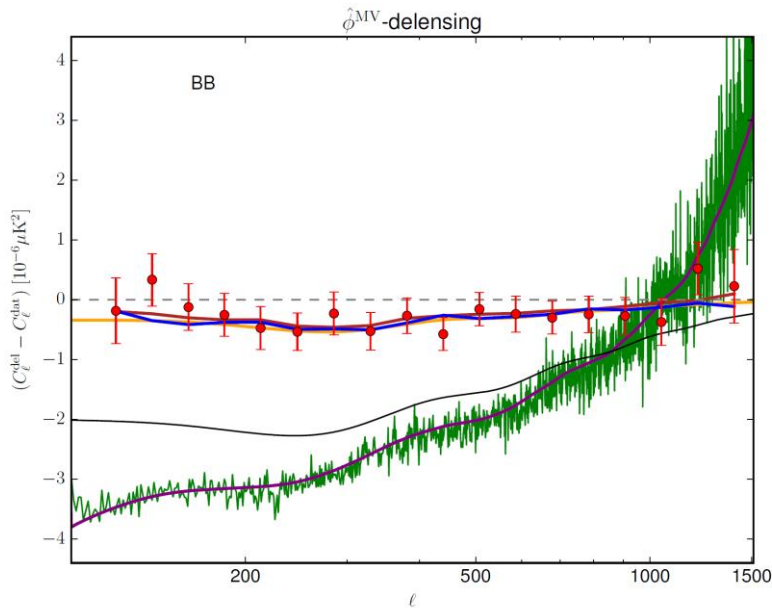
$\sim 25\sigma$  detection of TT delensing,  $20\sigma$  of polarization delensing; consistent with expectations

(S4 EE/TE delensing could sharpen peaks and decrease errors by up to  $\sim 20\%$ , arXiv: **1609.08143**)

# Current status of B-Mode Delensing

## Planck internal

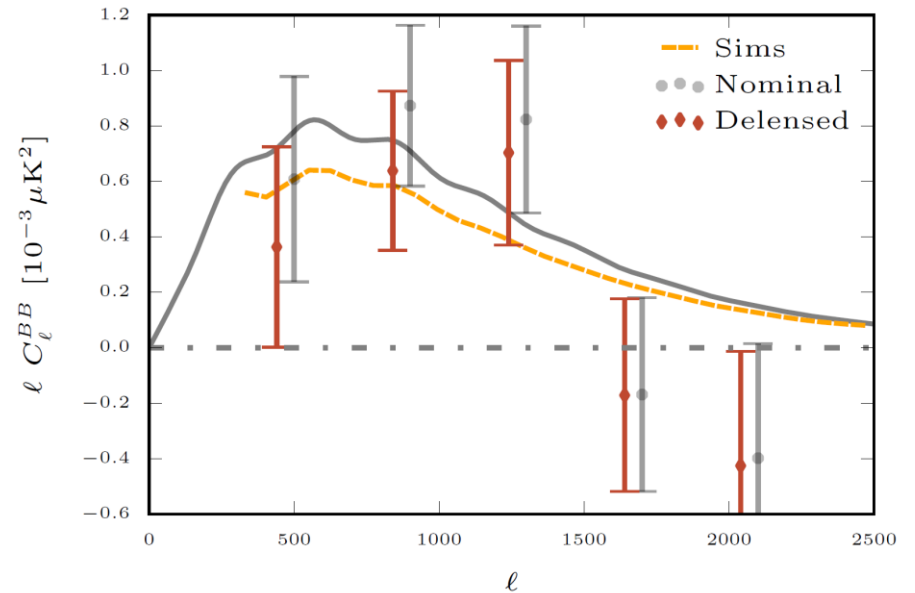
First detection of delensing of B-mode polarization at  $4.5\sigma$



Carron, Lewis, Challinor arXiv:1701.01712

## SPTpol and Herschel

28% delensing detected at  $6.9\sigma$



Manzotti et al. arXiv:1701.04396

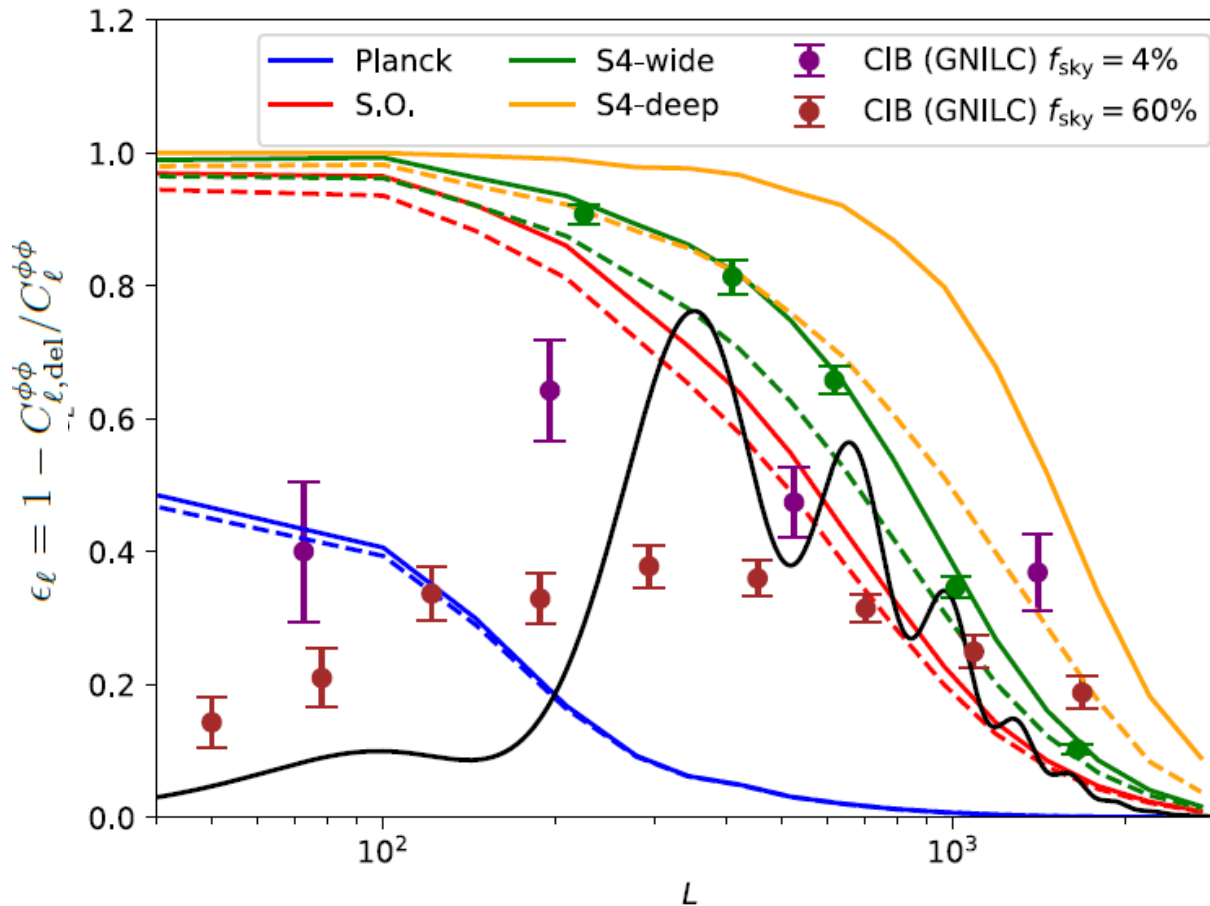
(Proof of principle only: noise high, so does not yet help at all with tensor  $r$  constraint)

# Future lensing reconstruction efficiency

quadratic estimator (dashed)

Iterative estimator (solid)

CIB not competitive for S4, though may help (reddish points)



LensIt: Iterative reconstruction code for realistic data

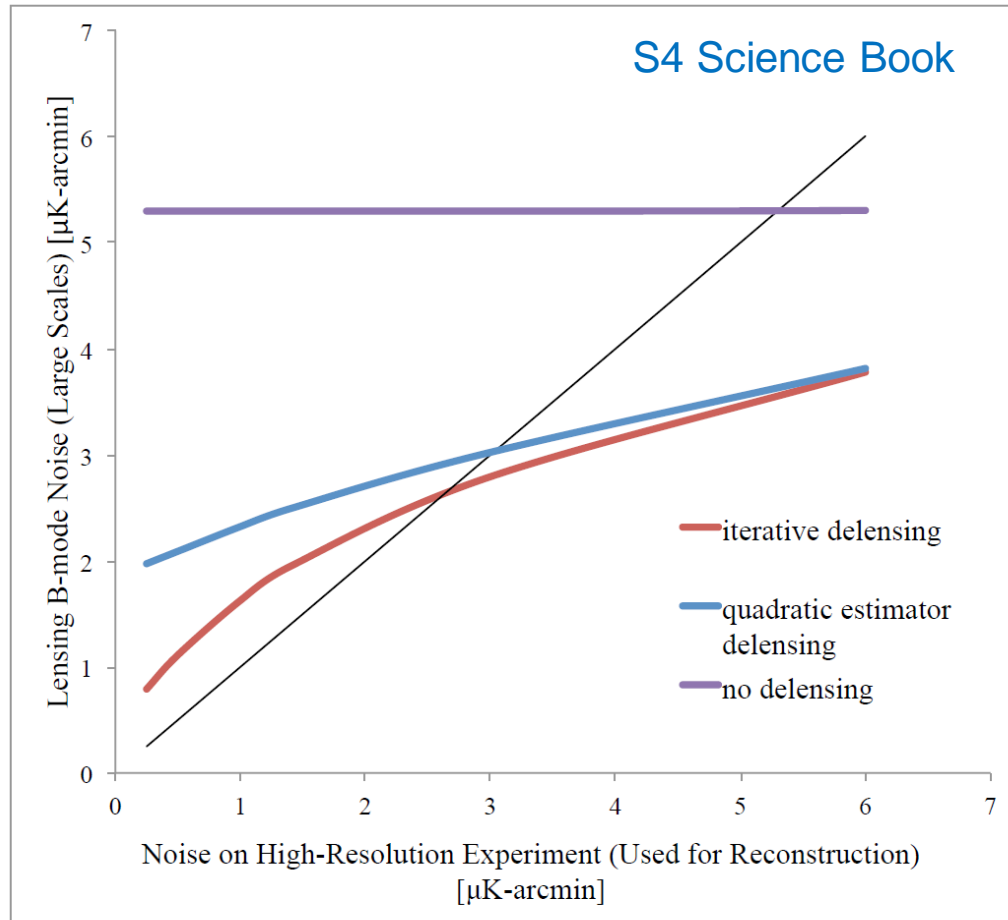
<https://github.com/carronj/LensIt> (Julien Carron)

Carron & Lewis, 1704.08230

(see also Millea et al. arXiv: 1708.06753 for joint reconstruction)

Without delensing,  $r$  limited by lensing not instrumental noise smaller than  $\sim 5 \mu K$  arcmin

Future high-resolution data could remove most of large-scale B-mode “noise” on  $r$



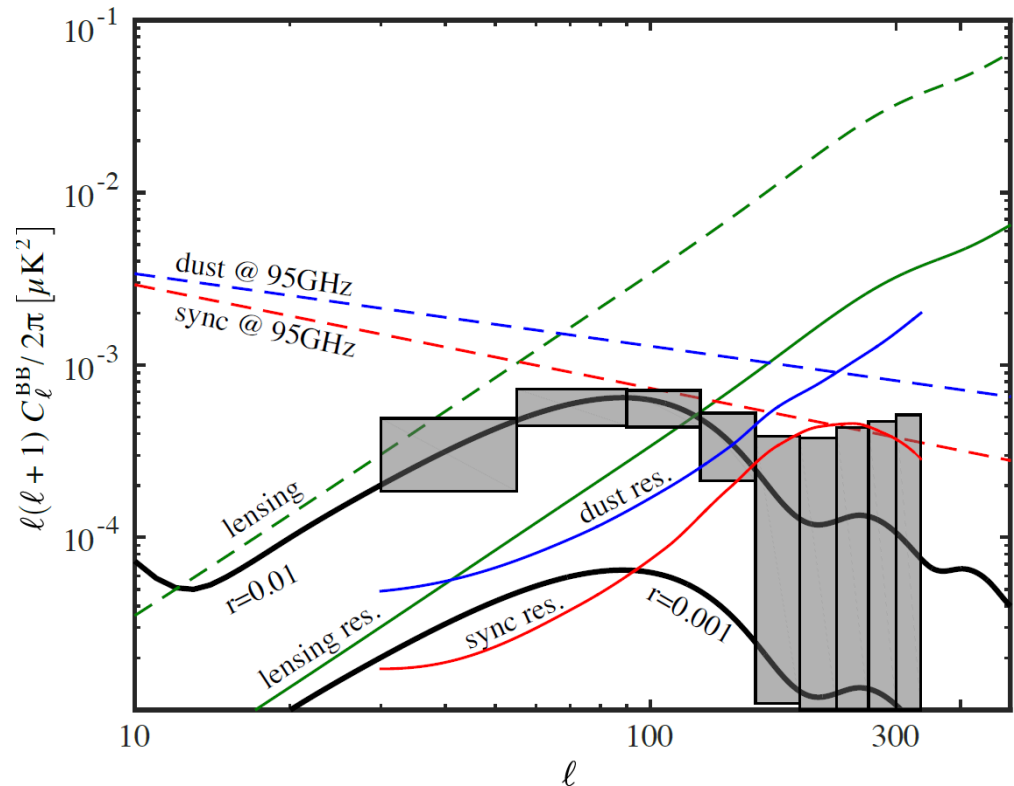
# Limits on delensing

Optimal internal reconstruction in principle only limited by noise down to  $r \sim 10^{-4} - 10^{-6}$

*But:* residual foregrounds in B may limit nearer  $r \sim 10^{-3}$  - see Josquin Errard talk

Lensing B still important source of noise for  $r \sim 10^{-3}$ : delensing still required

e.g. S4 Science Book



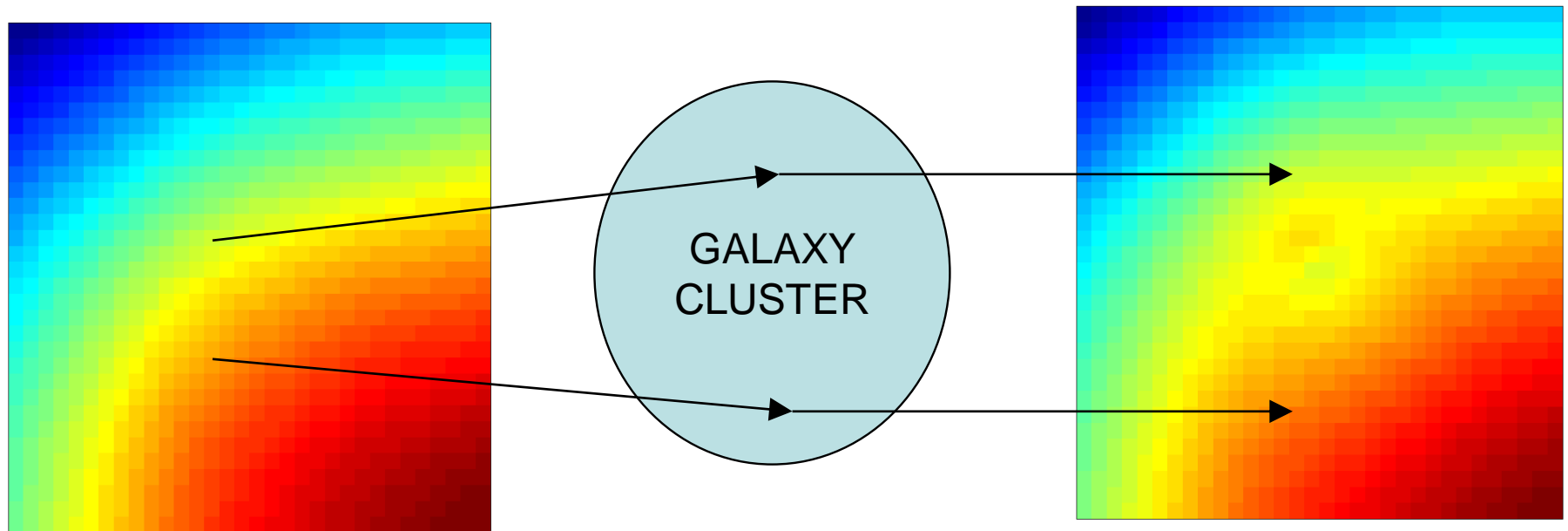
# Cluster CMB lensing

e.g. for mass calibration of high- $z$  clusters

CMB very smooth on small scales: approximately a gradient

Last scattering surface

What we see

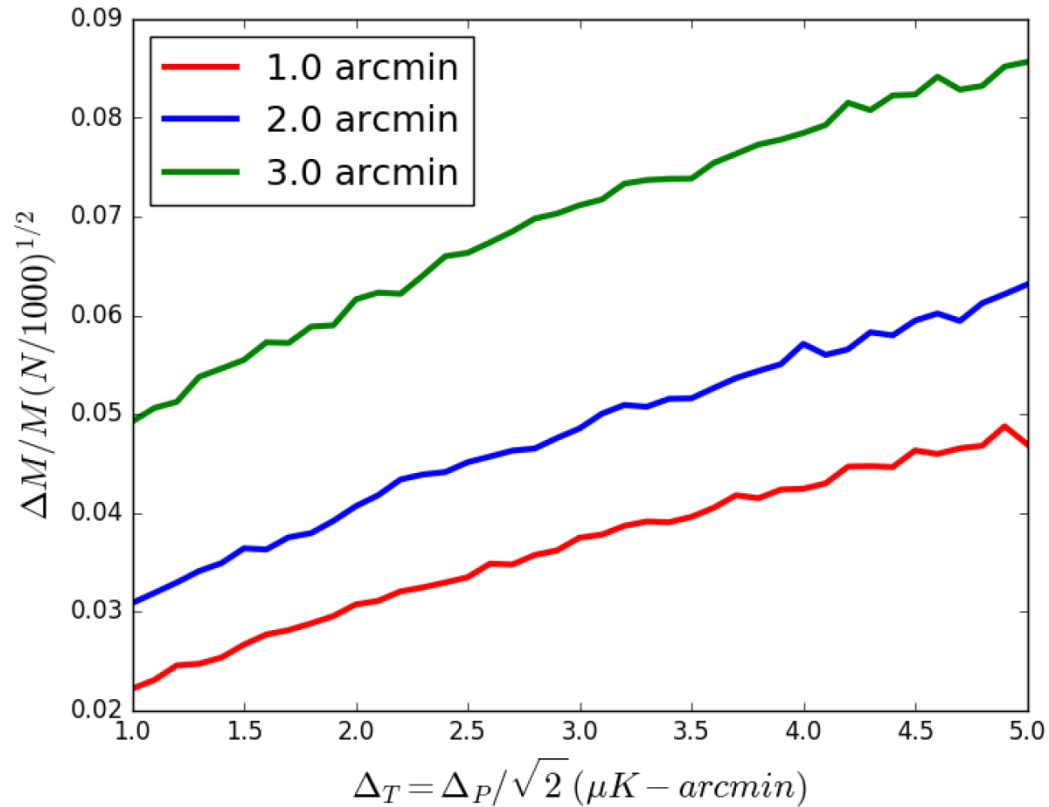


← 0.1 degrees →

Need sensitive ~ arcminute resolution observations

e.g. high-sensitivity, high-resolution CMB can calibrate mass of 1000 stacked clusters to a few percent

S4 Science Book



**Figure 53.** Mass uncertainty from CMB halo lensing measurements stacking  $10^3$  halos of mass  $M_{180\rho_{m0}} \approx 5 \times 10^{14} M_{\odot}$ , as a function of instrumental noise and varying instrumental resolution.



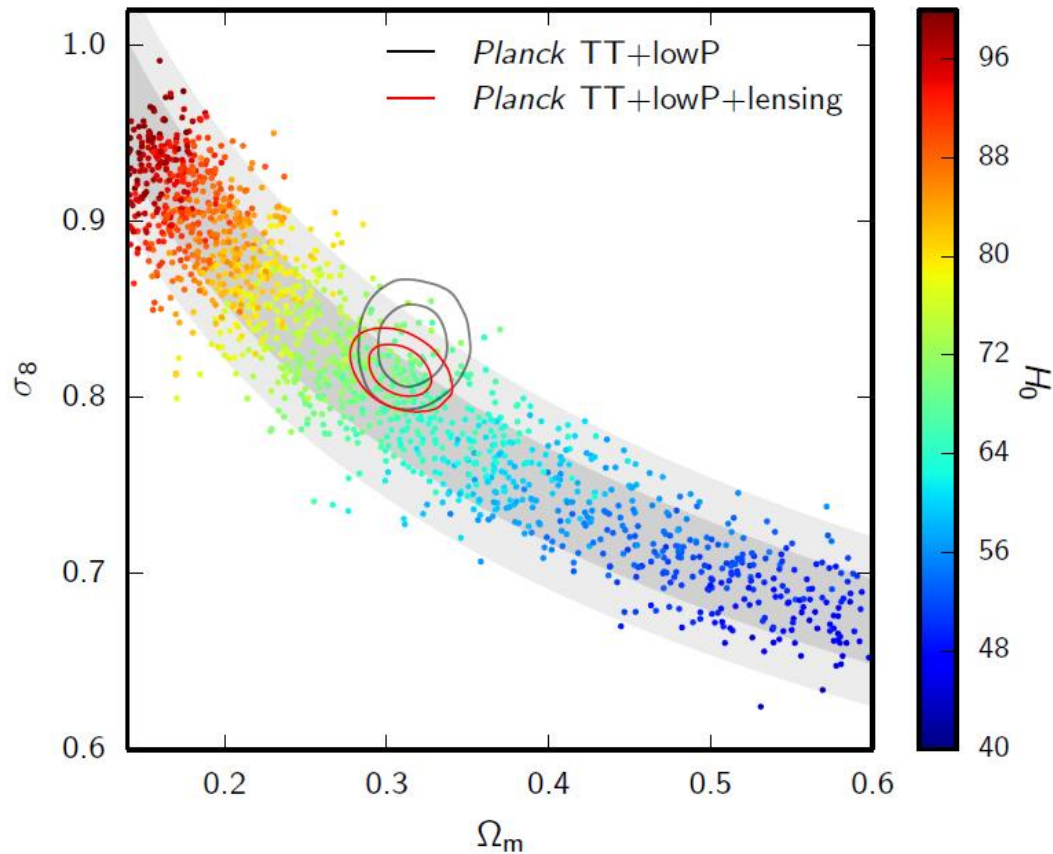
# CMB lensing summary

- Lensing reconstruction probes mass in the universe at  $0.5 \lesssim z \lesssim 7$ .
- Well reconstructed using small-scale CMB polarization
  - needs high resolution even to reconstruct large-scale lensing modes*
- $C_l^\psi$ : integrated probe of total matter fluctuation and geometry
  - measure absolute neutrino mass scale*
- Cross-correlation can calibrate galaxy shear and cluster masses.
  - synergy with galaxy lensing from EUCLID, LSST, etc. for constraining dark energy*
- Generates large-scale B modes with white spectrum ( $5 \mu K$  arcmin lensing ‘noise’)
  - major source of ‘noise’ for primordial gravitational waves if  $r < 10^{-2}$*
- Delensing required to measure  $r \ll 10^{-2}$  optimally
  - CIB currently competitive, but internal reconstruction required for optimal S4
  - use small-scale E and B to reconstruct  $\psi$
  - use  $\psi$  and E to de-lens large-scale B: extract gravity wave signal
  - needs high sensitivity and resolution (few arcminutes)
  - Ultimate  $r$  limit probably determined by large-scale foregrounds not by limitations of delensing
- Delensing detected as proof of principle (TT, TE, EE and BB)

## Cosmological parameters in LCDM

Measures late-time fluctuation amplitude independently of  $\tau$

### Planck 2015 CMB Lensing



Future: measure neutrino mass in combination with CMB/BAO

Total emission+time delay effect dominates on large scales

