Dynamical Clockwork Axions

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IRN Terascale Meeting, Montpellier, 5th July 2017

 $\label{eq:Based on arXiv: 1706.04529} In \mbox{ collaboration with Masahiro Ibe (ICRR/IPMU) and Michele Frigerio$







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Dynamical Clockwork Axions



2 The Strong CP problem and Axions

- 3 Clockwork Composite Axions
- 4 Clockwork Axion phenomenology

 A mechanism for generating exponentially suppressed couplings from a theory with only O(1) parameters

 Equivalently, generate an interaction scale much larger than the dynamical scale of the theory



- N + 1 complex scalars, ϕ_j , global U(1)^{N+1} symmetry
- Spontaneous symmetry breaking at high scale, f
- Asymmetric explicit breaking to U(1)₀ by nearest neighbour coupling at much lower scale,

$$V = \sum_{j=0}^{N} \left(-m^2 |\phi_j|^2 + \frac{\lambda}{4} |\phi_j|^4 \right) + \sum_{j=0}^{N-1} \frac{\epsilon}{f^{q-3}} \phi_j^{\dagger} \phi_{j+1}^q + h.c.$$
(1)

¹Choi & Im 1511.00132; Kaplan & Rattazzi 1511.01827; Giudice & McCullough (<u>16</u>10.0796<u>2</u>) < < ≥ >

Scalar Clockwork

• High-energy Lagrangian,

$$V = \sum_{j=0}^{N} \left(-m^2 |\phi_j|^2 + \frac{\lambda}{4} |\phi_j|^4 \right) + \sum_{j=0}^{N-1} \frac{\epsilon}{f^{q-3}} \phi_j^{\dagger} \phi_{j+1}^q + h.c.$$
(2)

• Parametrise in terms of NGBs, $\phi_j \rightarrow U_j \equiv f e^{i \pi_j / \sqrt{2} f}$, then

$$V = -2\epsilon f^4 \sum_{j=0}^{N-1} \cos\left(\frac{\pi_j - q\pi_{j+1}}{\sqrt{2}f}\right)^2$$
(3)

• Orthogonal rotation to mass basis $\pi_j = O_{jk}a_k$, with $m_{a_0} = 0$,

$$O_{j0} - qO_{j+1,0} = 0$$

 $\Rightarrow O_{j0} = rac{\mathcal{N}}{q^j}, \ \mathcal{N} \approx 1$ (4)

• a_0 component of π_j decreases **exponentially** with j

• Final step: couple Clockwork to the SM at the final site,

$$\mathcal{L} = \mathcal{L}_{SM} + \mathcal{L}_{Clock} + \frac{\pi_N \mathcal{O}_{SM}^{(d)}}{f^{d-3}} + h.c.$$

$$\approx \mathcal{L}_{SM} + \mathcal{L}_{Clock} + \frac{a_0 \mathcal{O}_{SM}^{(d)}}{q^N f^{d-3}} + \sum_{j=1}^N \frac{a_j \mathcal{O}_{SM}^{(d)}}{A_j f^{d-3}} + h.c., \quad (5)$$

where $A_j \sim \mathcal{O}(1)$.

- Coupling of NGB to SM suppressed by q^N
- E.g. if d = 4, the new effective scale is $f_{eff} = q^N f \gg f$



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• The SM Lagrangian includes the CP-violating term,

$$\mathcal{L}_{\theta} = \frac{\theta_{QCD}}{32\pi^2} G \tilde{G} \tag{6}$$

• Measured coefficient of this term is

$$\overline{\theta} = \theta_{QCD} - \arg(\det[Y_d Y_u]), \tag{7}$$

and experimentally (neutron EDM) we know $|\overline{ heta}| < 10^{-10}$

- QCD term and EW term should be unrelated!
- Severe fine-tuning required: this is the Strong CP problem

Axion solution

- Make $\overline{\theta}$ a dynamical field
- Impose a $U(1)_{PQ}$ symmetry, which must be
 - a. Axial
 - b. Spontaneously broken at scale $f_a \gg \Lambda_{QCD}$
 - c. Explicitly broken by the QCD anomaly, i.e. $aG\,\tilde{G}$ term
- The $U(1)_{PQ}$ pNGB is the axion, defined by $\overline{\theta} = \frac{a}{f_a}$
- Axion potential from the QCD anomaly is

$$V(a) \sim -\Lambda_{QCD}^4 \cos\left(\frac{a}{f_a}\right),$$
 (8)

and this take $\overline{\theta} \rightarrow \mathbf{0}$ dynamically

 Lower bound on f_a from supernova energy loss, upper bound from overproduction of axions via misalignment mechanism,

$$4 \times 10^8 \text{ GeV} \lesssim f_a \lesssim 10^{12} \text{ GeV}$$
 (9)

KSVZ axion²

- Simple construction of axion model: $U(1)_{PQ}$ must be
 - a. axial \Rightarrow introduce vector-like fermion, ψ
 - b. anomalous w.r.t. to QCD \Rightarrow give ψ QCD charge
 - c. spontaneously broken \Rightarrow add a complex scalar, σ , with a VEV
- Giving ψ_L, ψ_R, σ appropriate charges, we can write

$$\mathcal{L} \supset y\overline{\psi}_{L}\sigma\psi_{R} + h.c., \tag{10}$$

and the VEV of $\sigma \sim \frac{f_a}{\sqrt{2}} e^{ia/f_a}$ breaks $U(1)_{PQ}$ spontaneously • Below the scale f_a , axion couples to QCD,

$$\mathcal{L} \supset \frac{aG\tilde{G}}{32\pi^2 f_a},\tag{11}$$

which generates the cosine potential that takes $\overline{ heta}
ightarrow 0$

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²Kim, J.E., Phys. Rev. Lett. 43 (1979) 103; Shifman, M.A., Vainstein, V.I., and Zakharov, V.I., Nucl. Phys. B 166 (1980) 4933

The Clockwork axion

- Recall Scalar Clockwork model
- If only π_N is coupled to QCD anomaly, we have

$$\mathcal{L} = \frac{\pi_N}{32\pi^2 f} G\tilde{G}$$
$$\approx \frac{a_0}{32\pi^2 q^N f} G\tilde{G} + \dots, \qquad (12)$$

i.e. an effective axion decay constant $f_a = q^N f \gg f$.

- So it's possible to set f at O(TeV) and connect EW/LHC-scale physics to axion physics
- Shift in θ
 from U(1)_{PQ}-breaking gravity terms depends on the size of f
 <u>f</u>
 M_{Pl}, so lower dynamical scale better protects θ

- This is a nice example of the Clockwork in action, but we may wonder:
 - Where do all these scalars come from?
 - What is the origin of the scale *f*? Is it stable against quantum corrections?
 - What is the effect of gravity on the $U(1)^{N+1}$ symmetry?
 - What is the size of q? (it's not predicted)
 - How can we distinguish this axion model?
- In short, many open theory and phenomenology questions





2 The Strong CP problem and Axions





- Motivation: avoid elementary scalars, generate f_a dynamically
- Introduce strongly-coupled gauge $SU(N_c)_a$, condenses at Λ_a
- Vector-like fermions $Q_{L,R} \sim (N_c, 3)$ and $\psi_{L,R} \sim (N_c, 1)$ under $SU(N_c)_a \times SU(3)_{QCD}$
- There is a $U(1)^{(Q)}_A imes U(1)^{(\psi)}_A$ symmetry, which is broken:
 - spontaneously by fermion bilinears, $\left<\overline{Q}_{Li}Q_{Ri}\right> = \left<\overline{\psi}_L\psi_R\right> \sim \Lambda_a^3$
 - explicitly by $SU(N_c)_a$ and $SU(3)_{QCD}$ anomalies

³Kim, J.E., Phys. Rev. D31 (1985) 1733.

- $U(1)_{PQ}$ is linear combination broken **only** by QCD anomaly
- Q, ψ have PQ charges +1, -3 respectively • recall $Q_{L,R} \sim (N_c, 3), \psi_{L,R} \sim (N_c, 1)$
- Light pNGB is the composite axion, a $\sim \frac{\overline{Q}\gamma^5 Q 3\overline{\psi}\gamma^5 \psi}{\sqrt{10}}$
- Same coupling to QCD as before, with $f_a \sim \Lambda_a$, and $\overline{\theta} \to 0$

Extending the composite axion model with Clockwork

- For the composite axion, we introduced an additional, asymptotically-free SU(N_c) and 2 vector-like fermions
- Let's **Clockwork** this, and introduce
 - *N* copies of asymptotically-free *SU*(*N_c*)
 - N + 1 vector-like fermions





Clockwork realisation in strongly-coupled gauge theories

• In Composite axion model, $\psi \sim (\mathsf{N_c},\mathbf{1})$, $Q \sim (\mathsf{N_c},\mathbf{3})$

Our Clockwork extension is:

	$SU(N_c)_1$	$SU(N_c)_2$	$SU(N_c)_3$		$SU(N_c)_N$	SU(3) _{QCD}
ψ_{0}	N _c	1	1		1	1
ψ_1	R	N _c	1		1	1
ψ_2	1	R	N _c		1	1
-	:	:	:	·	÷	:
ψ_{N-1}	1	1	1		N _c	1
ψ_{N}	1	1	1		R	3

 Notably, this arrangement mimics the Clockwork's asymmetric nearest-neighbour couplings

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The Clockwork realisation

- For each ψ_j there is a $U(1)_A^{(\psi_j)}$ symmetry, overall there is a $U(1)_A^{N+1}$ symmetry
- Since the $SU(N_c)_j$ confine, the fermion bilinear condensates,

$$\left\langle \overline{\psi}_{i}\psi_{i}\right\rangle pprox\Lambda^{3},$$
 (13)

spontaneously break the $U(1)_A^{N+1}$

• The NGBs, π_j , associated with SSB of $U(1)^{(\psi_j)}_{\mathcal{A}}$ are given by

$$\overline{\psi}_j \psi_j \sim \Lambda^3 e^{i\pi_j} \tag{14}$$

- $U(1)_A^{(\psi_j)}$ explicitly broken by $SU(N_c)_j$ and $SU(N_c)_{j+1}$ anomalies
- However, there is a preserved, anomaly-free U(1)_A, with current

$$j_A^{\mu} = \sum_{j=0}^{N} q_j \times j_j^{\mu}; \qquad j_j^{\mu} = \frac{1}{2} \overline{\psi}_j \gamma_5 \gamma^{\mu} \psi_j.$$
(15)

• As in scalar example, there is one NGB and N massive pNGBs

• Identify exact NGB as the axion and exact $U(1)_A$ as $U(1)_{PQ}$

• The $U(1)_{PQ}$ charges are $q_j \approx q^{-j}$, with the Clockwork factor

$$q = -\frac{2T(\mathbf{R})N_c}{d(\mathbf{R})},\tag{16}$$

where $T(\mathbf{R})$, $d(\mathbf{R})$ are the Dynkin index and dimension of \mathbf{R} , e.g. $\mathbf{R} \equiv \mathbf{A}_2$, $N_c = 5$ gives q = -3/2

• The axion component in the pNGBs is

$$\pi_j = q_j \frac{a}{f},\tag{17}$$

where $f \sim \Lambda/4\pi$

Realising the QCD axion

	$SU(N_c)_1$	$SU(N_c)_2$	$SU(N_c)_3$		$SU(N_c)_N$	$SU(3)_{QCD}$
ψ_0	N _c	1	1		1	1
ψ_1	R	Nc	1		1	1
ψ_2	1	R	N _c		1	1
:	:		:	•••	:	:
ψ_{N}	1	1	1		R	3

• $U(1)_{PQ}$ is broken by the QCD anomaly, and the Clockwork axion arises as desired:

$$\mathcal{L} \supset \frac{d(\mathbf{R})\pi_N}{32\pi^2} G\tilde{G} \approx \frac{d(\mathbf{R})a}{32\pi^2 q^N f} G\tilde{G} + \dots,$$
(18)

i.e. effective axion decay constant is $f_{\rm a}\approx \frac{q^N}{d({\rm R})}f\gg f$

Alternative model: contact connection



• Contact interactions (enforced by a \mathbb{Z}_m^{N-1} symmetry)

$$\mathcal{L}_{contact} = \frac{1}{M_*^2} \sum_{j=1}^{N-1} \left(\overline{\psi}_{Lj} \psi_{Rj} \right)^{\dagger} \left(\overline{Q}_{Lj+1} Q_{Rj+1} \right) + h.c.$$
(19)

Achieve larger Clockwork factor,

$$q = -\frac{T(\mathbf{R}_{\psi})}{T(\mathbf{R}_{\mathbf{Q}})} \sim \mathcal{O}(N_c) \gg 1 \tag{20}$$

- We can connect EW/LHC-scale physics to axion physics
- Better protection of $\overline{\theta}$ against cut-off (depends on $\frac{f}{M_{Pl}}$)
- Specific to this realisation:
 - Provides a symmetry explanation for the convenient nearest neighour couplings
 - $\bullet\,$ Initial scale, $\Lambda,$ is stable against quantum corrections
 - *U*(1)_{*PQ*} arises as accidental symmetry from the gauge symmetries and fermion content
 - Predicts Clockwork factor
 - Consequently, interesting phenomenology ...

What is Clockwork?

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Several interesting avenues:

- Collider signatures
- Cosmology
- Coupling to photons





- Spectrum of new coloured particles depends on model
- Dynamical model and one realisation of contact-connection model predicts colour octet scalar meson with mass $m_8 \sim \frac{g_s \Lambda}{4\pi}$, which can be pair produced or singly produced via

$$\mathcal{L} \supset \frac{g_s^2}{4\pi\Lambda} S_8 G \tilde{G} \tag{21}$$

- Dijet search in Run II can constrain production cross section to $\sigma \lesssim {\cal O}(0.1)$ pb, testing $m_8 \sim$ TeV 4
- *SU*(*N_c*) baryons and other hadrons generally too heavy to be found at LHC

⁴See e.g. Belyaev, A. et al., JHEP 1701 (2017) 094□ → ∢ ♂ →

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• Contact-connection model may include vector-like quarks, Q_{N+1} , with mass $m_{Q_{N+1}} \sim \mathcal{O}(\Lambda^3/M_*^2)$, that interact with the SM, e.g. via

$$\mathcal{L} \supset \epsilon \overline{q}_{Li} \tilde{H} Q_{N+1R} \tag{22}$$

 \bullet ATLAS and CMS set $m_{T,B}\gtrsim 800$ GeV at 95% CL

• CMS expects to set $m_{T,B}\gtrsim 1.85$ TeV at 95% CL with 3000 fb $^{-1}$ of $\sqrt{s}=14$ TeV data

• Coherent oscillation of axion field provides a relic abundance,

$$\Omega_a h^2 \approx 0.07 \alpha_i^2 \left(\frac{f_a}{10^{12} \text{ GeV}}\right)^{7/6}, \qquad (23)$$

for initial misalignment angle, $\alpha_i \in [-\pi, \pi]$

- If f = 1 TeV (recall $f_a \approx q^N f$), correct relic density
 - For $N \sim \mathcal{O}(50)$ in $N_c = 5$ dynamical model
 - For $N \sim \mathcal{O}(15)$ in $N_c = 4$ contact-connection model
- Large domain wall number due to fractional clockwork factor, $N_{DW} \sim s^N$, where q = r/s
- To avoid domain wall problem, require U(1)_{PQ} be broken during inflation and not restored afterwards

Baryonic DM

- Each fermion, ψ_j, Q_j has associated U(1)_V symmetry in contact-connection model
- Lightest baryon under each U(1)_V is a stable bound state with mass m_B ~ O(N_cΛ)
- Large relic density if reheating temperature lies in the window

$$T_F \lesssim T_R \lesssim \Lambda,$$
 (24)

where the baryonic freeze-out temperature is given by

$$x_F \sim \frac{1}{2}\log(x_F) + 35 - \log\left(\frac{m_B}{\text{TeV}}\right); \quad x_F \equiv \frac{m_B}{T_F}$$
 (25)

• Then relic density of baryonic dark matter is

$$\Omega_{\mathcal{B}}h^2 \sim 0.1 \frac{N}{15} \left(\frac{m_{\mathcal{B}}}{20 \text{ TeV}}\right)^2 \tag{26}$$

- Suppose ψ_j or Q_j has $\mathcal{O}(1)$ charge under $U(1)_Y$
- Then axion-photon coupling goes as

$$\mathcal{L} \sim \frac{a}{32\pi^2 q^j f} F \tilde{F} \approx \frac{q^{N-j} a}{32\pi^2 f_a} F \tilde{F} + \dots$$
(27)

- Axion can have much larger coupling to photons than conventional models!⁵
- Makes axion more 'visible' in haloscopes, e.g. ADMX

⁵See also Farina, M. et al., JHEP 1701 (2017) 095 □ → <∂ → < ≥

- Clockwork is an interesting mechanism to generate exponentially small couplings
- We have constructed models where Clockwork emerges in a sequence of strongly-coupled gauge theories, and applied them to the composite axion
- Can link LHC-scale physics to axion physics with stable f_a , protection of $\overline{\theta}$, prediction of Clockwork factor
- Range of phenomenology, from the collider to the cosmos, and the possibility that the axion has a large coupling to photons
- Still early days for Clockwork: many unexplored realisations/applications!

Questions or comments?









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Dynamical Clockwork Axions

Back-up Slides

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Group Theory and Clockwork factor

- Choices of N_c, R are restricted by: a) SU(N_c) must be asymptotically-free; b) need |q| > 1
- To ensure asymptotic freedom, require

$$11N_c - 4N_c T(\mathbf{R}) - 2d(\mathbf{R}) > 0$$
⁽²⁸⁾

• Should choose $\mathbf{R} \equiv \mathbf{A_2}$ and $N_c = 4, 5$, giving

$$q = -\frac{4}{3} (N_c = 4); \qquad q = -\frac{3}{2} (N_c = 5)$$
 (29)

Alternative model: contact connection



• Contact interactions (enforced by a \mathbb{Z}_m^{N-1} symmetry)

$$\mathcal{L}_{contact} = \frac{1}{M_*^2} \sum_{j=1}^{N-1} \left(\overline{\psi}_{Lj} \psi_{Rj} \right)^{\dagger} \left(\overline{Q}_{Lj+1} Q_{Rj+1} \right) + h.c.$$
(30)

Contact-connection model

• $U(1)_A^{2N}$ broken spontaneously by fermion condensates,

$$\overline{Q}_{j}Q_{j} \sim \Lambda^{3}e^{i\pi_{j}}; \qquad \overline{\psi}_{j}\psi_{j} \sim \Lambda^{3}e^{i\xi_{j}}$$
(31)

- Contact interactions and anomalies explicitly breaks $U(1)_A^{2N} \rightarrow U(1)_A \equiv U(1)_{PQ}$, so there is one exact NGB
- Preserved $U(1)_A$ current given by

$$j_{A}^{\mu} = \sum_{j=1}^{N} \left(q_{Qj} j_{Qj}^{\mu} + q_{\psi j} j_{Q\psi}^{\mu} \right), \qquad j_{fj}^{\mu} = \frac{1}{2} \overline{f} \gamma_{5} \gamma^{\mu} f$$
(32)

• Axion component in pNGB modes is in geometric progression

$$\pi_{j} \approx q_{Qj} \frac{a}{f} + \dots, \qquad \xi_{j} \approx q_{\psi j} \frac{a}{f} + \dots, \text{ with}$$
$$q_{Qj} = q^{1-j}, \qquad \qquad q_{\psi j} = q^{-j}. \tag{33}$$

• This model admits a larger Clockwork factor,

$$q = -\frac{T(\mathbf{R}_{\psi})}{T(\mathbf{R}_{\mathbf{Q}})} \sim \mathcal{O}(N_c) \gg 1.$$
(34)

Realising the QCD axion

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$$\begin{array}{c|c} & SU(N_c)_N \\ \hline Q_N & \mathbf{R}_Q \\ \hline \psi_N & \mathbf{R}_\psi \end{array} \end{array} \xrightarrow{} \begin{array}{c} & SU(3)_{\rm QCD} \\ \hline Q_{N+1} & \mathbf{3} \end{array}$$

- Can introduce N_f flavours of Q_{N+1} with $q_{Q_{N+1}} = q_{\psi_N}$
- $U(1)_A$ is broken by the QCD anomaly, and

$$\mathcal{L} \supset \frac{N_f q_{Q_{N+1}} \pi_{N+1}}{32\pi^2} G \tilde{G} \approx \frac{N_f a}{32\pi^2 q^N f} G \tilde{G} + \dots, \qquad (35)$$

i.e. effective axion decay constant is $f_{\rm a}\approx \frac{q^N}{N_{\rm f}}f\gg f$