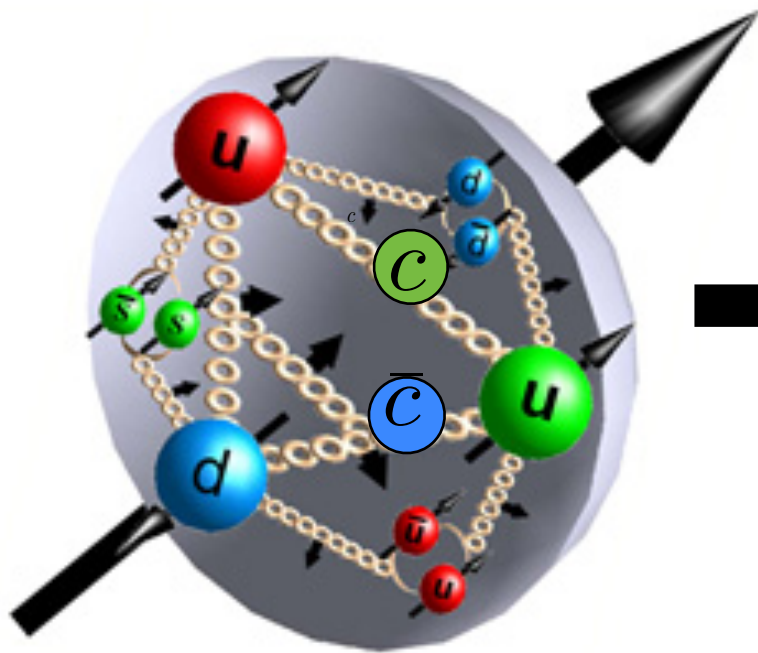
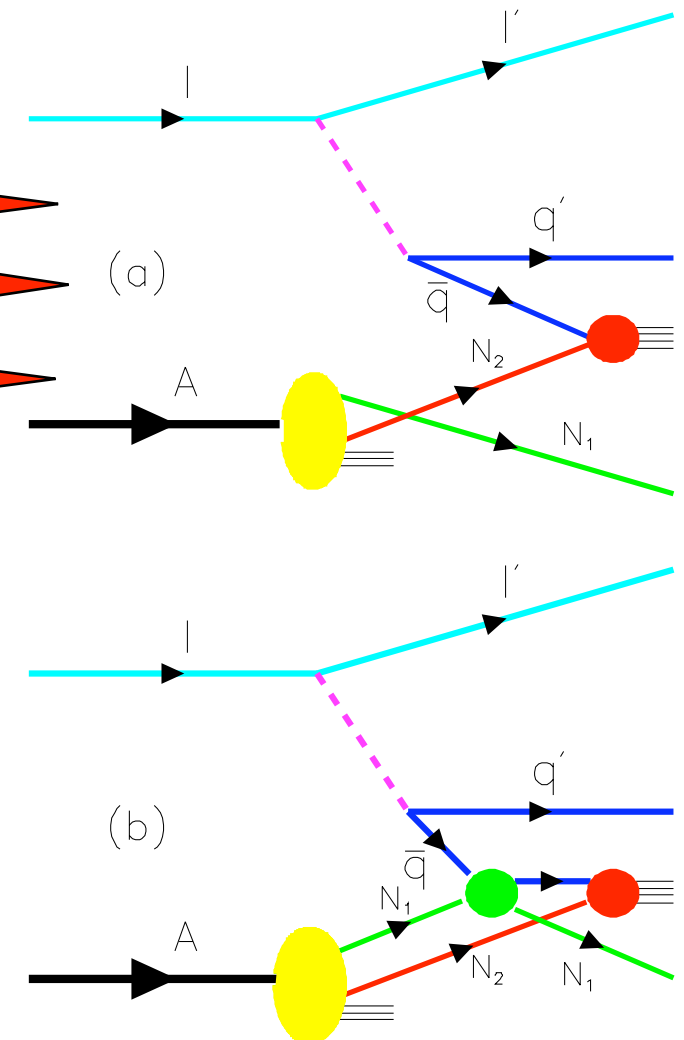
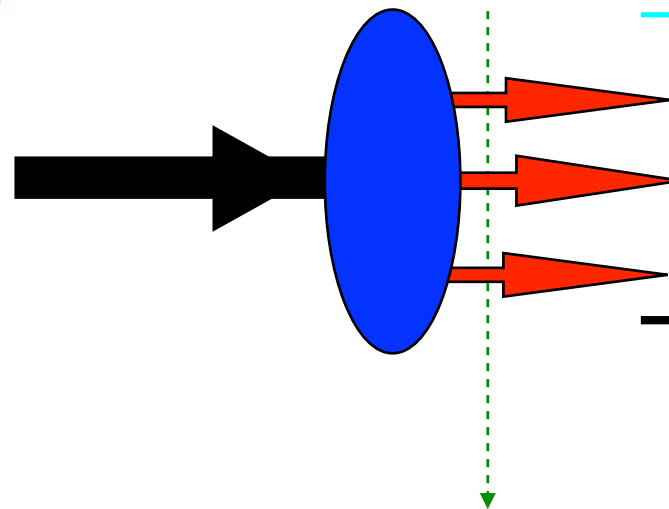


# Novel QCD Features of Hadrons and Nuclei



Fixed  $\tau = t + z/c$



Stan Brodsky



with Guy de Tèramond, Hans Günter Dosch, Cedric Lorce, Kelly Chiu, and Alexandre Deur

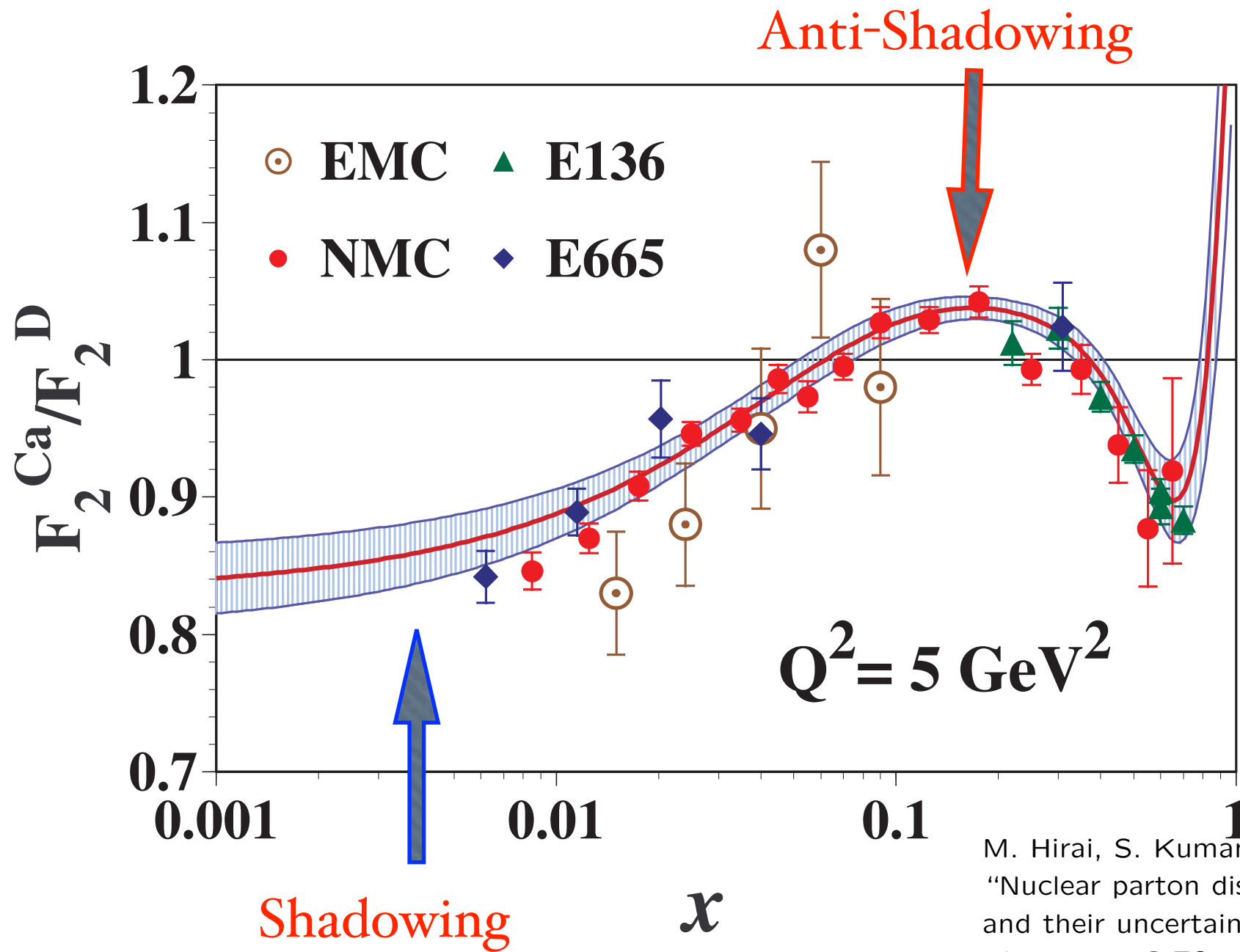
**CDR QCD: Partons and Nuclei**

**Orsay June 1, 2017**

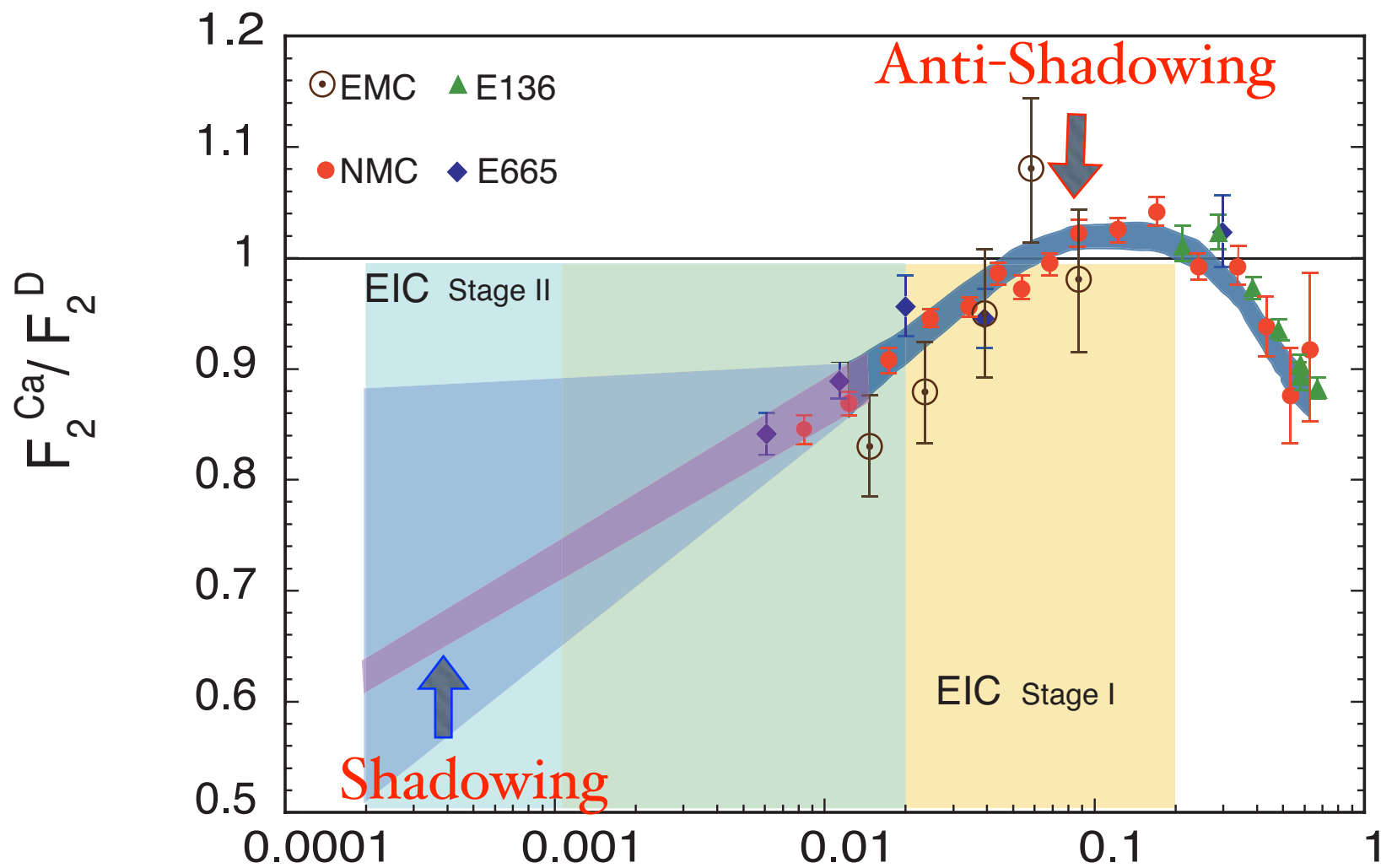
*Is Antishadowing in DIS  
Non-Universal, Flavor-Dependent?*

*Do Nuclear PDFs  
Obey Momentum and other Sum Rules?*



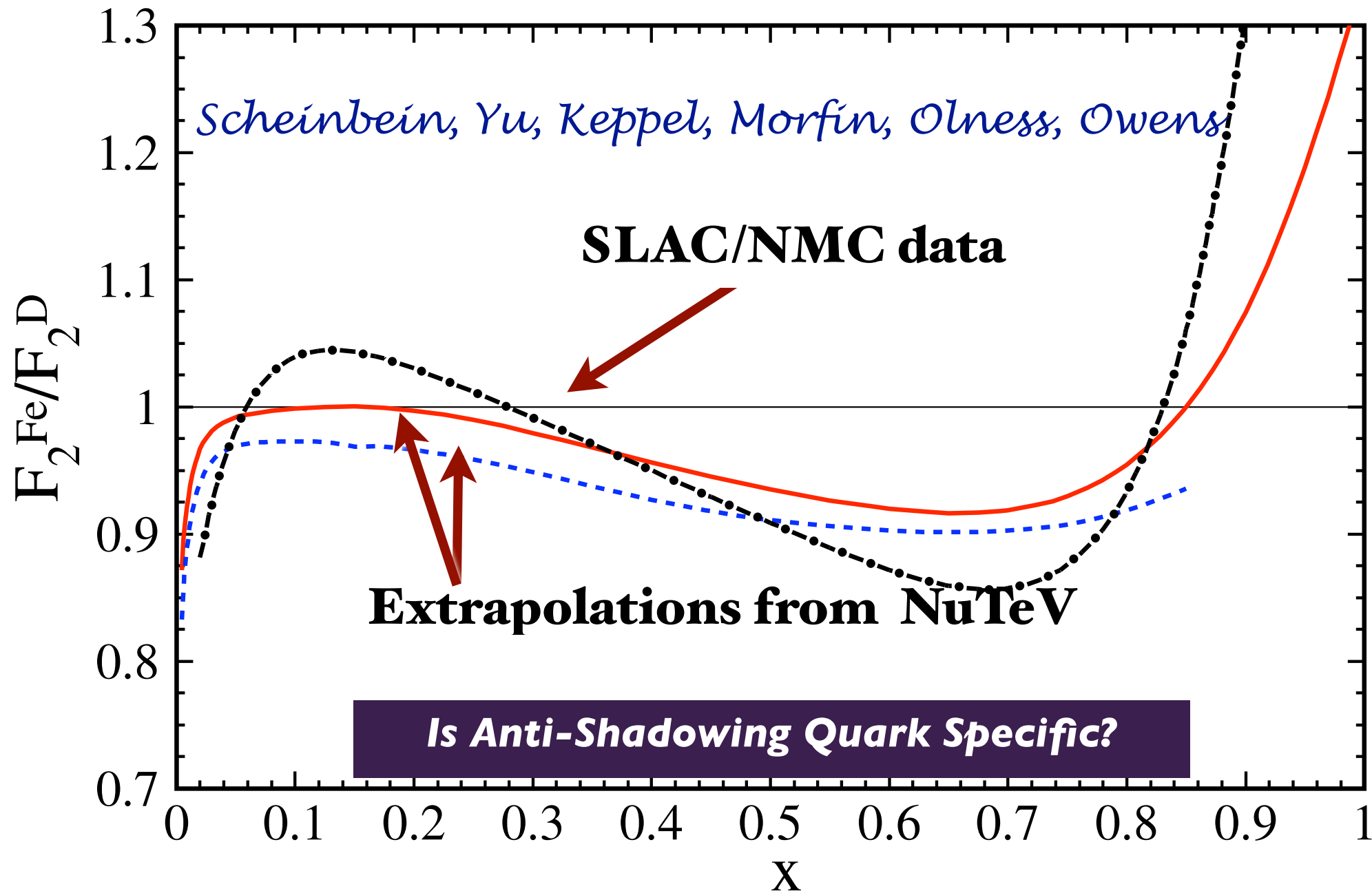


M. Hirai, S. Kumano and T. H. Nagai,  
"Nuclear parton distribution functions  
and their uncertainties,"  
Phys. Rev. C **70**, 044905 (2004)  
[arXiv:hep-ph/0404093].

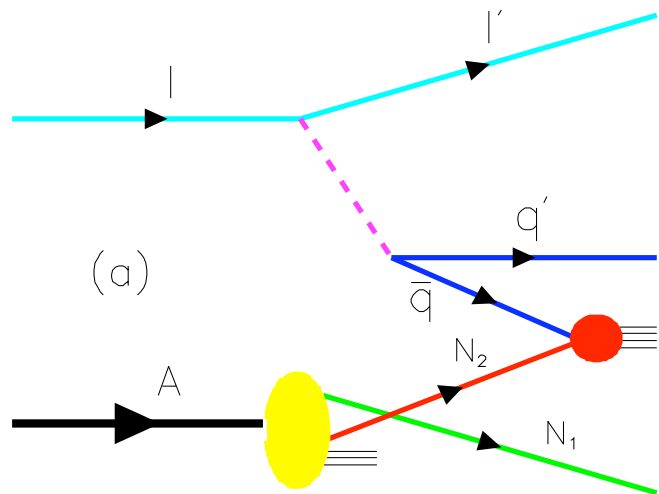


The ratio of nuclear over nucleon  $F_2$  structure function,  $R_2$ , as a function of Bjorken  $x$ , with data from existing fixed target DIS experiments at  $Q^2 > 1 \text{ GeV}^2$ , along with the QCD global fit from EPS09 [153]. Also shown are the respective coverage and resolution of the same measurements at the EIC at Stage-I and Stage-II. The purple error band is the expected systematic uncertainty at the EIC assuming a  $\pm 2\%$  (a total of 4%) systematic error, while the statistical uncertainty is expected to be much smaller.

$$Q^2 = 5 \text{ GeV}^2$$

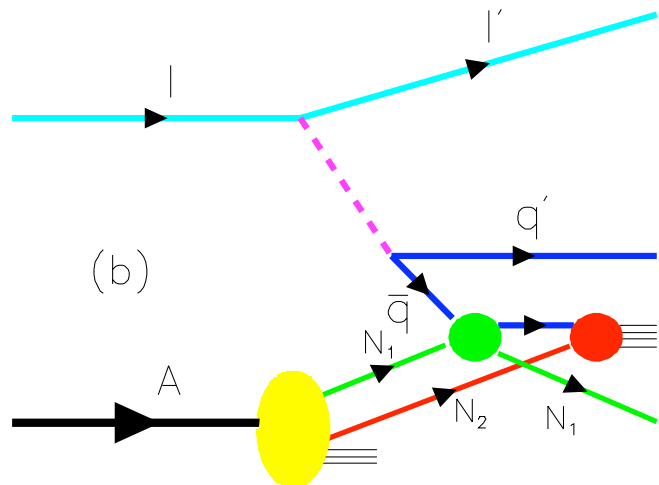


**No anti-shadowing in deep inelastic neutrino scattering !**



The one-step and two-step processes in DIS on a nucleus.

Coherence at small Bjorken  $x_B$  :  
 $1/Mx_B = 2\nu/Q^2 \geq L_A$ .



If the scattering on nucleon  $N_1$  is via pomeron exchange, the one-step and two-step amplitudes are opposite in phase, thus diminishing the  $\bar{q}$  flux reaching  $N_2$ .

→ Shadowing of the DIS nuclear structure functions.

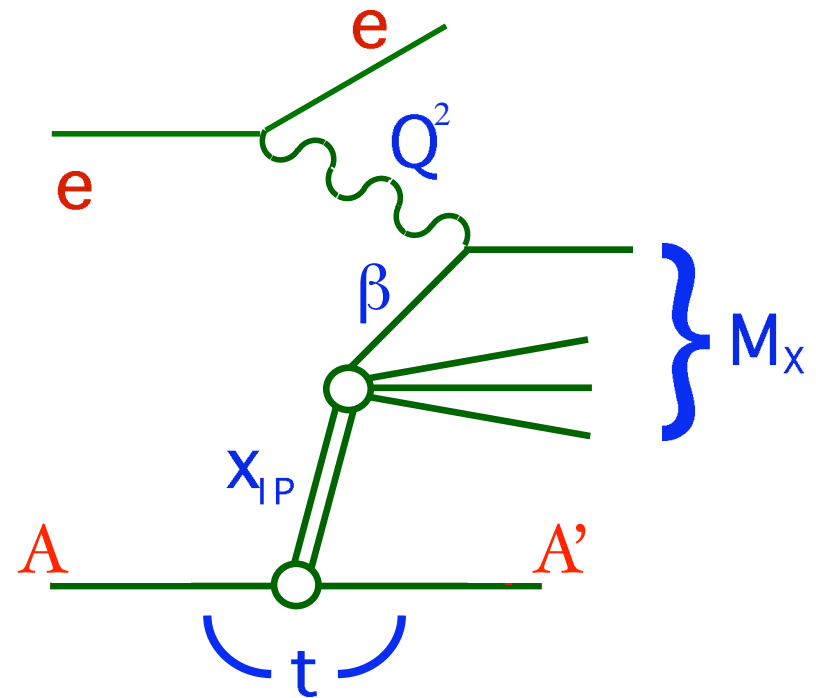
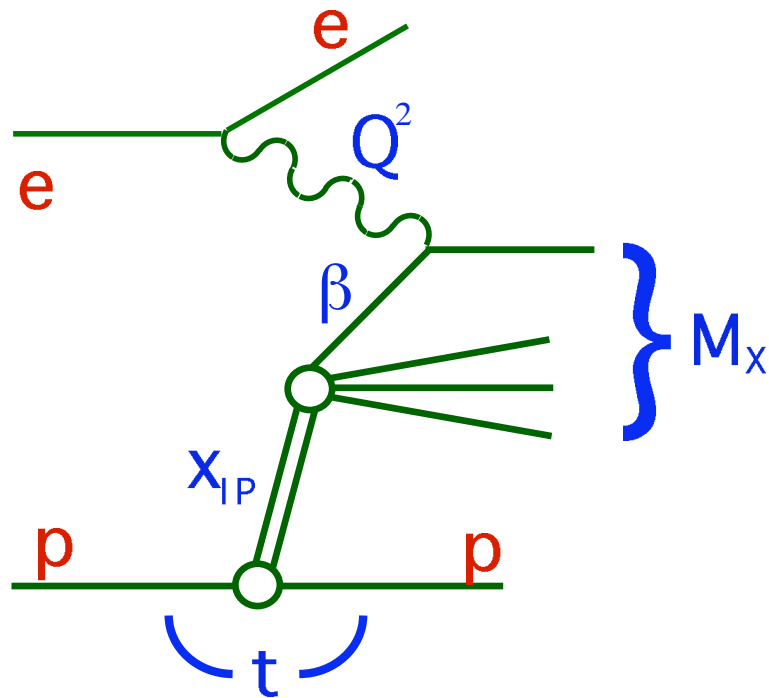
**Diffraction via Pomeron gives destructive interference!**

*Shadowing*

# Diffractive Deep Inelastic Scattering

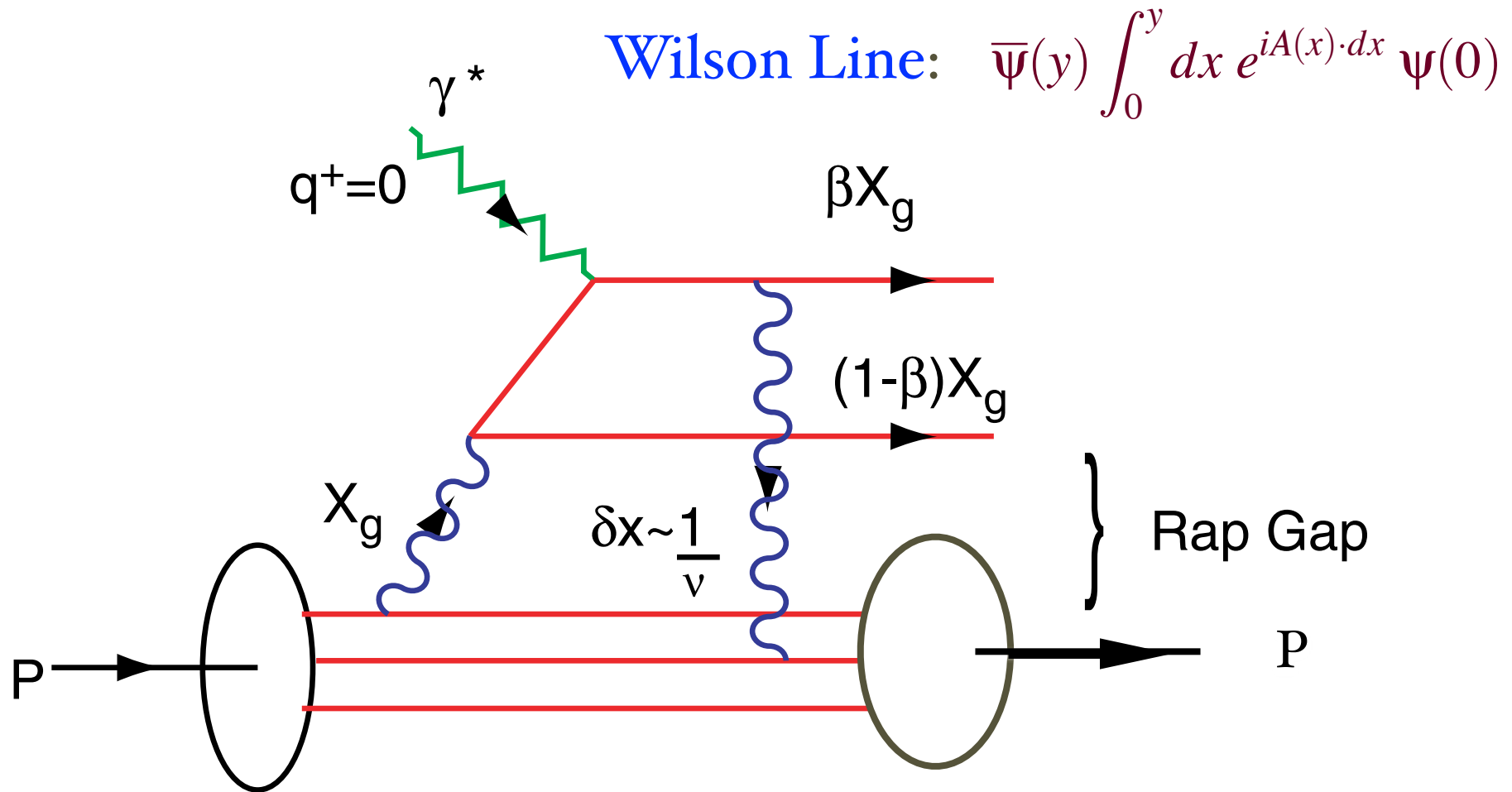
Diffractive DIS  $ep \rightarrow epX$  where there is a large rapidity gap and the target nucleon remains intact probes the final state interaction of the scattered quark with the spectator system via gluon exchange.

Diffractive DIS on nuclei  $eA \rightarrow e'AX$  and hard diffractive reactions such as  $\gamma^* A \rightarrow V A$  can occur coherently leaving the nucleus intact.



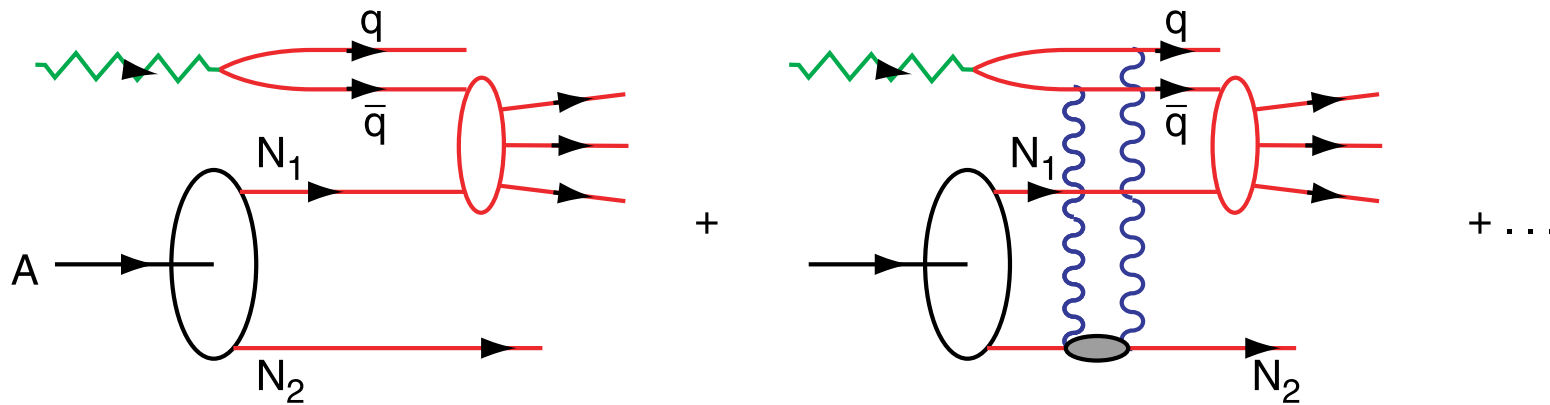


# QCD Mechanism for Rapidity Gaps



**Reproduces lab-frame color dipole approach**

## Nuclear Shadowing in QCD



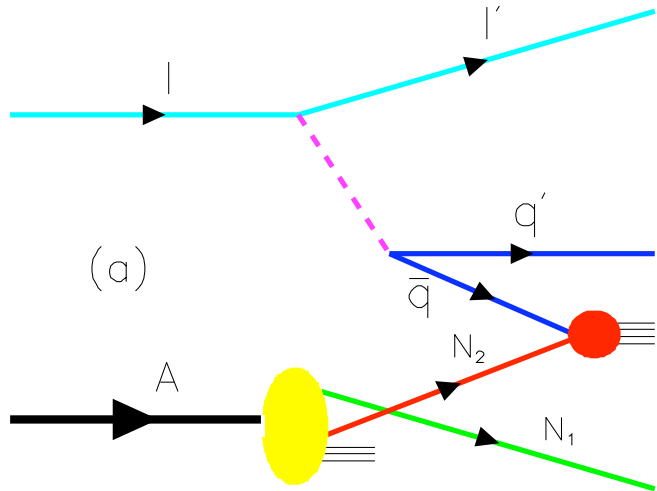
*Shadowing depends on understanding leading twist-diffraction in DIS*

**Nuclear Shadowing not included in nuclear LFWF !**

**Dynamical effect due to virtual photon interacting in nucleus**

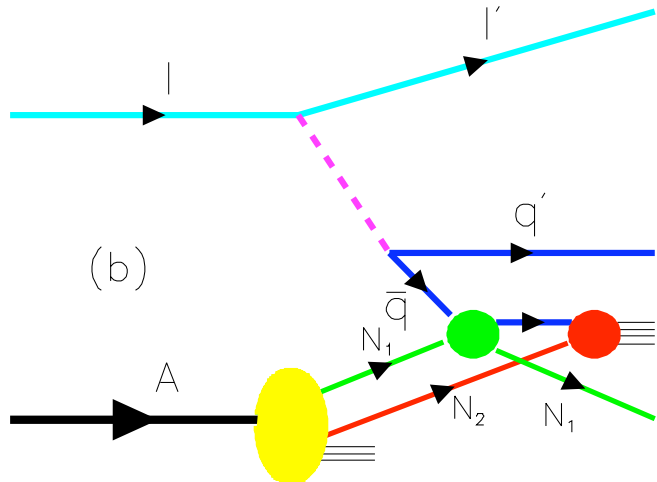
**Diffraction via Reggeon gives constructive interference!**

**Anti-shadowing not universal**



The one-step and two-step processes in DIS on a nucleus.

Coherence at small Bjorken  $x_B$  :  
 $1/Mx_B = 2\nu/Q^2 \geq L_A$ .

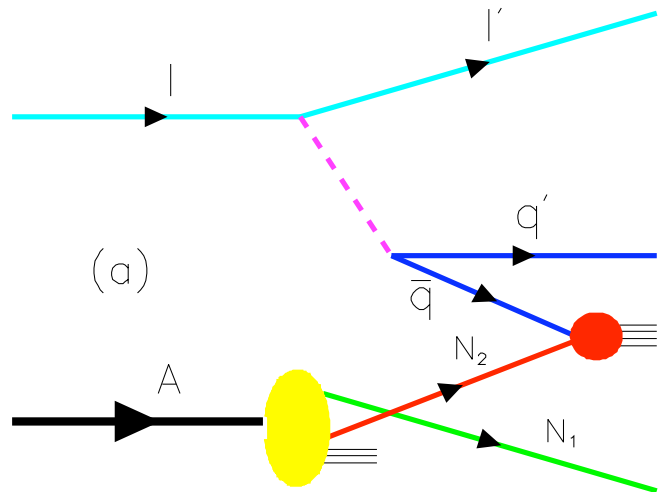


If the scattering on nucleon  $N_1$  is via pomeron exchange, the one-step and two-step amplitudes are opposite in phase, thus diminishing the  $\bar{q}$  flux reaching  $N_2$ .

*Interior nucleons shadowed*

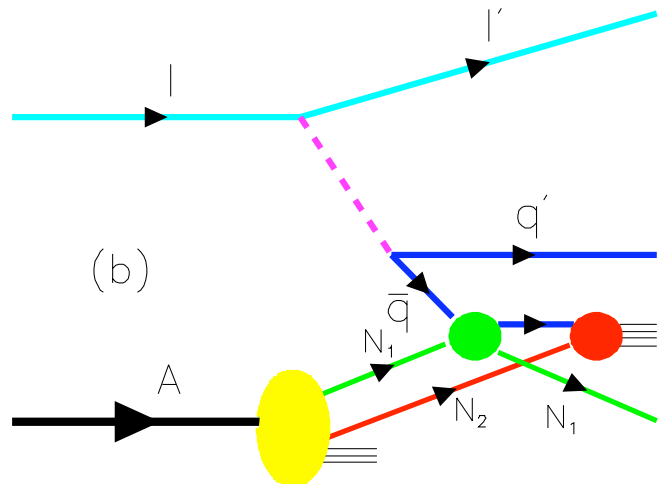
→ Shadowing of the DIS nuclear structure functions.

*Observed HERA DDIS produces nuclear shadowing*



The one-step and two-step processes in DIS on a nucleus.

Coherence at small Bjorken  $x_B$  :  
 $1/Mx_B = 2\nu/Q^2 \geq L_A$ .

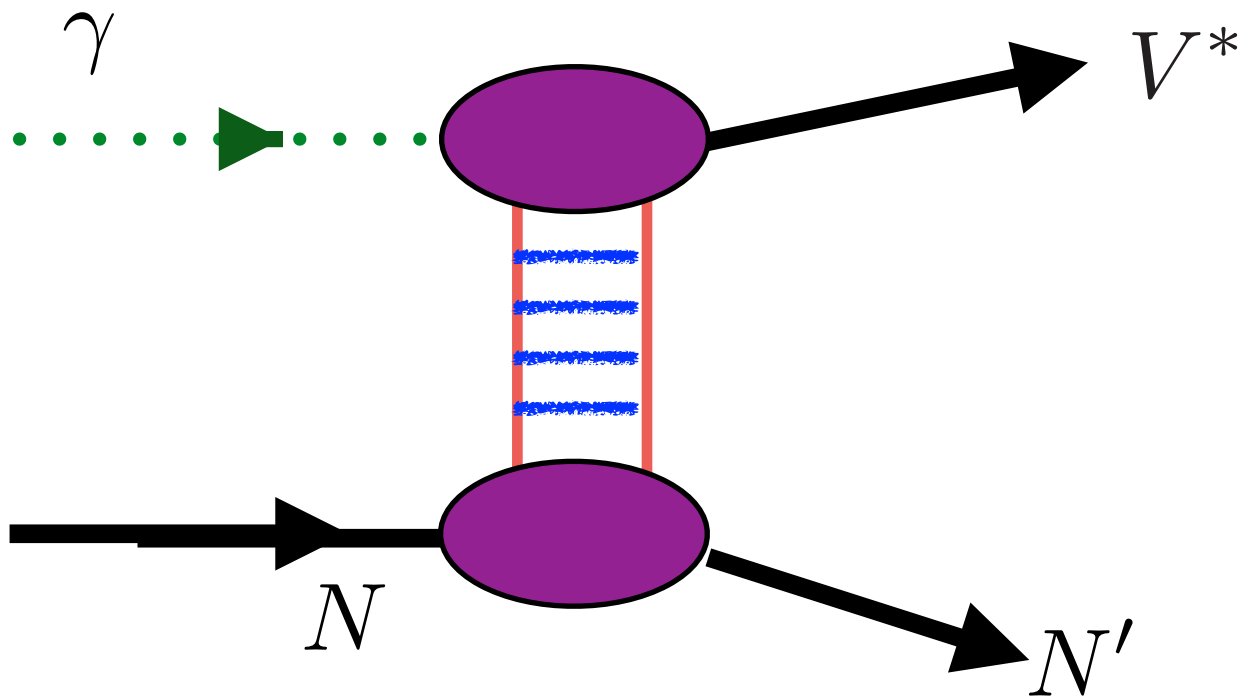


If the scattering on nucleon  $N_1$  is via ~~pomeron~~ exchange, the one-step and two-step amplitudes are ~~opposite in phase, thus diminishing the  $\bar{q}$  flux reaching  $N_2$ .~~

**Regge**  
**constructive in phase**  
 thus **increasing** the flux reaching  $N_2$

*Interior nucleons anti-shadowed*

**Regge Exchange in DDIS produces nuclear anti-shadowing**

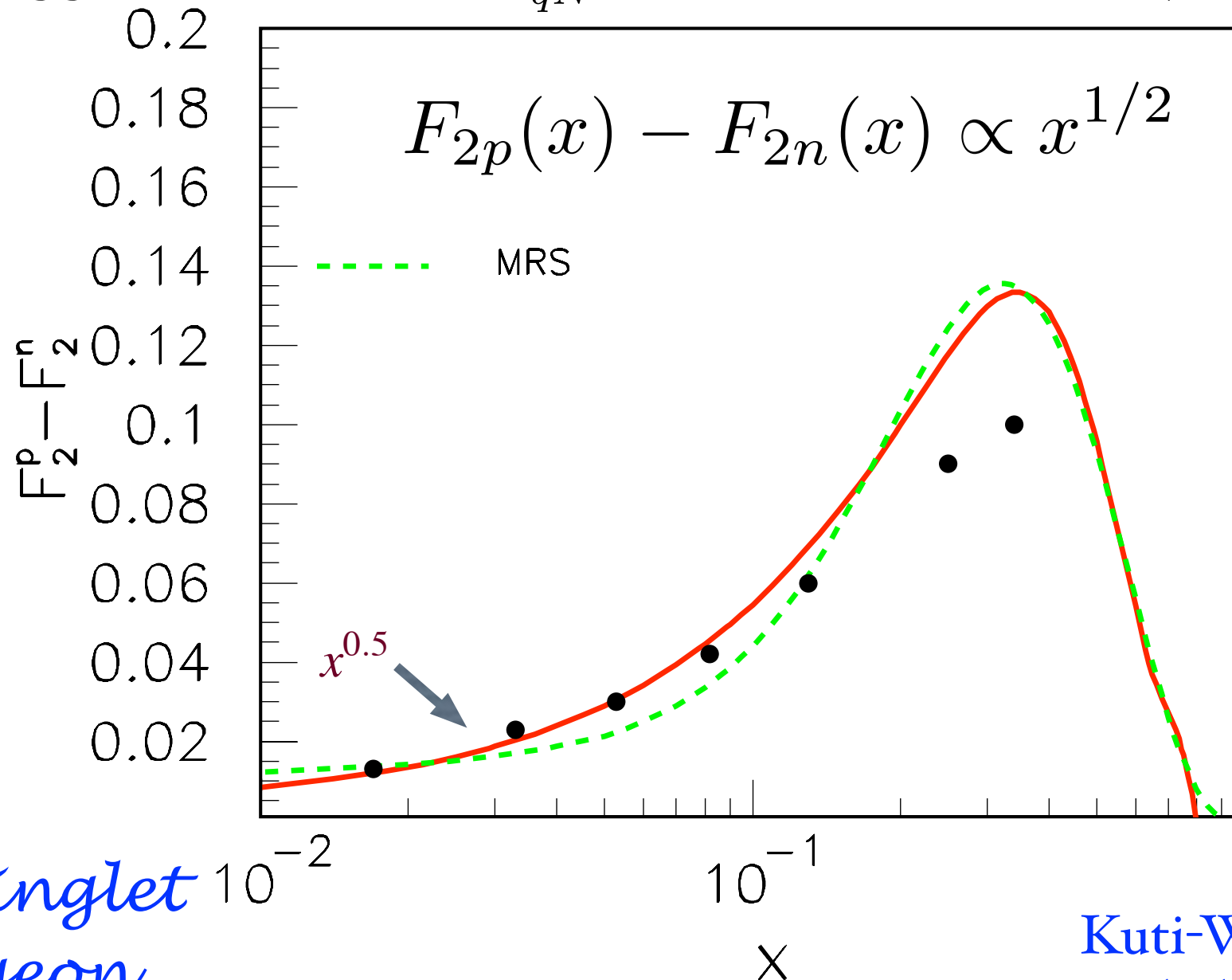


Reggeon Exchange Contribution to DDIS

$$\gamma^* n \rightarrow p V^{*-}$$



Regge contribution:  $\sigma_{\bar{q}N} \sim \hat{s}^{\alpha_R-1}$   $\alpha_R \simeq 1/2$



*Non-singlet  
Reggeon  
Exchange*

*Kuti-Weisskopf  
behavior*

## *Regge Behavior of Scattering Amplitudes*

$$M = \sum_R s^{\alpha_R(t)} F_R(t) e^{i\phi_R} \quad \frac{d\sigma}{dt} \propto \frac{|M|^2}{s^2}$$

$$F_2(x) \sim x^{1-\alpha_R}$$

*R = Pomeron* ( $\alpha_{\mathcal{P}} \simeq 1 + \epsilon$ ),  $C = +$ , *phase = Imaginary*

*Odderon* ( $\alpha_{\mathcal{O}} \simeq 1$ ),  $C = -$ , *phase = Real*

*Reggeon* ( $\alpha_{\mathcal{R}} \simeq 1/2$ ),  $C = \pm$ , *phase = Real + Imaginary*

$\mathcal{FP}$  ( $\alpha_{\mathcal{FP}} \simeq 0$ ),  $C = +$ , *phase = Real*

# Origin of Regge Behavior of Inelastic Structure Functions

Deep

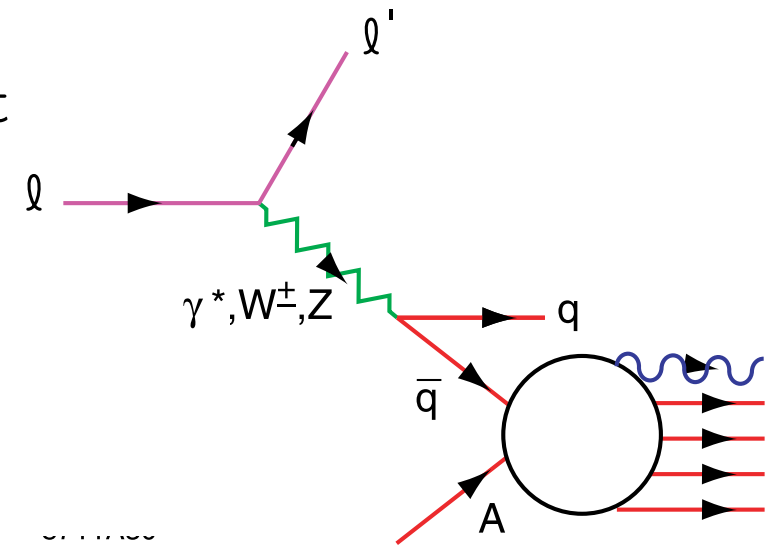
$$F_{2p}(x) - F_{2n}(x) \propto x^{1/2}$$

Antiquark interacts with target nucleus at energy  $\hat{s} \propto \frac{1}{x_{bj}}$

Regge contribution:  $\sigma_{\bar{q}N} \sim \hat{s}^{\alpha_R - 1}$

Nonsinglet Kuti-Weisskoff  $F_{2p} - F_{2n} \propto \sqrt{x_{bj}}$  at small  $x_{bj}$ .

Shadowing of  $\sigma_{\bar{q}M}$  produces shadowing of nuclear structure function.



**Landshoff,  
Polkinghorne, Short  
Close, Gunion, sjb  
Schmidt, Yang, Lu,  
sjb**

# Reggeon Exchange

Regge contribution:  $\sigma_{\bar{q}N} \sim \hat{s}^{\alpha_R-1}$        $\alpha_R \simeq 1/2$

Phase of two-step amplitude relative to one step:

$$\frac{1}{\sqrt{2}}(1-i) \times i = \frac{1}{\sqrt{2}}(i+1)$$

Constructive Interference

Depends on quark flavor!

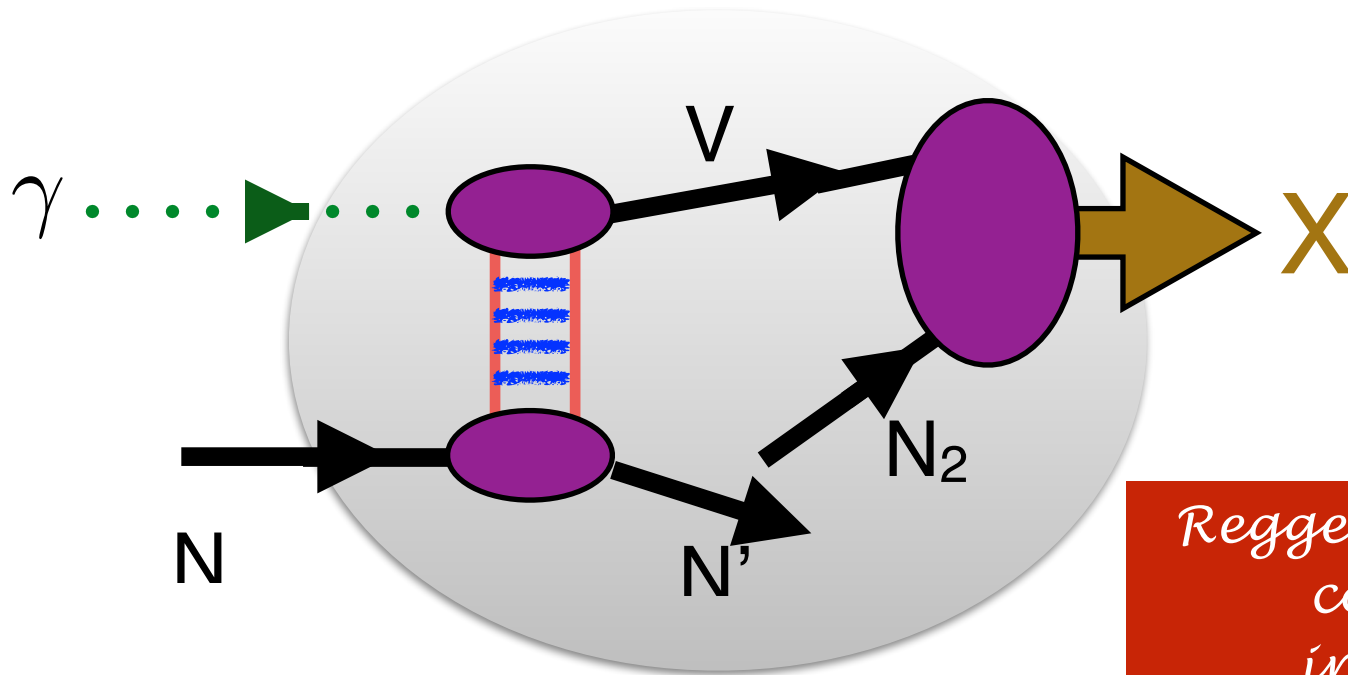
Thus antishadowing is not universal

Different for couplings of  $\gamma^*$ ,  $Z^0$ ,  $W^\pm$

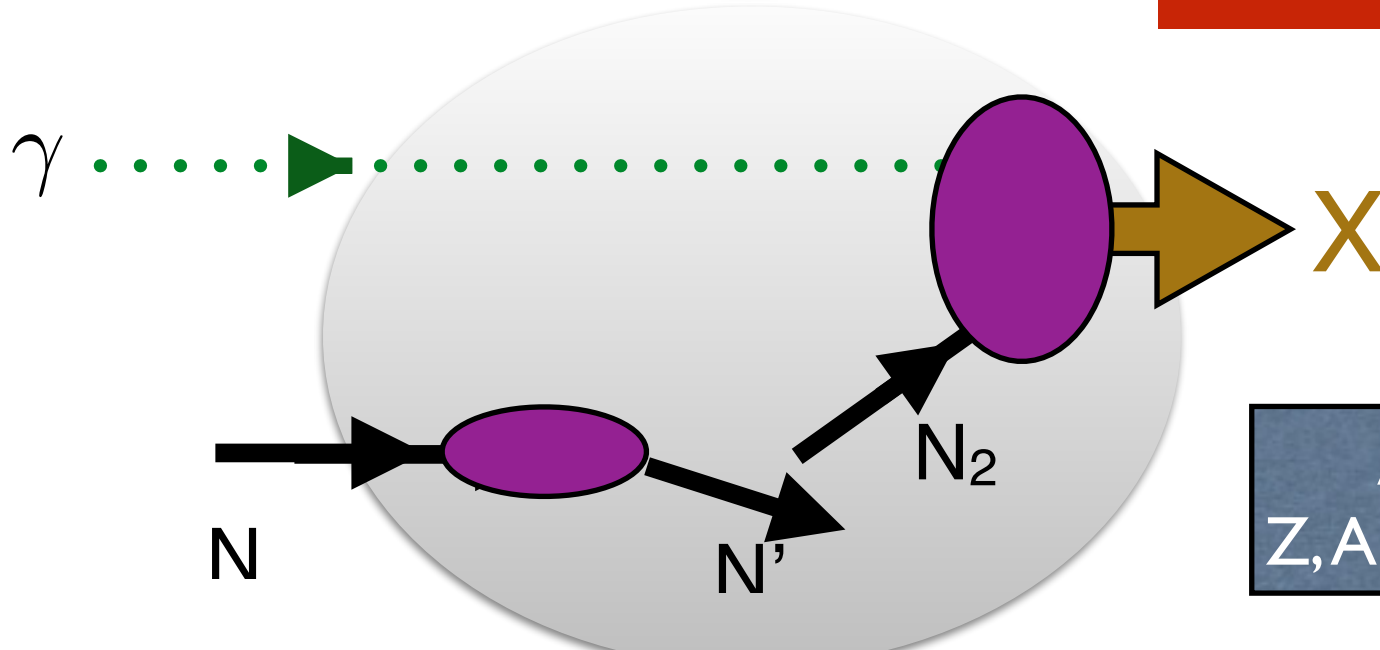
*Test: Tagged Drell-Yan*

# Two-step and One-Step Glauber processes

*$l=1$  Reggeon Exchange on  $N_1$*



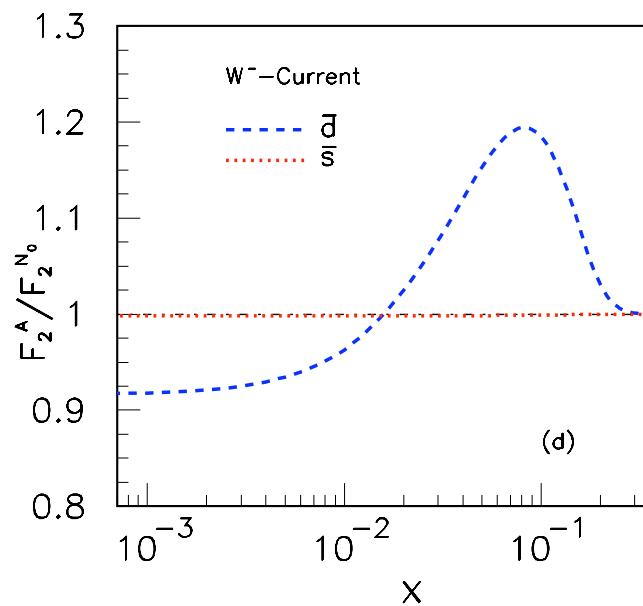
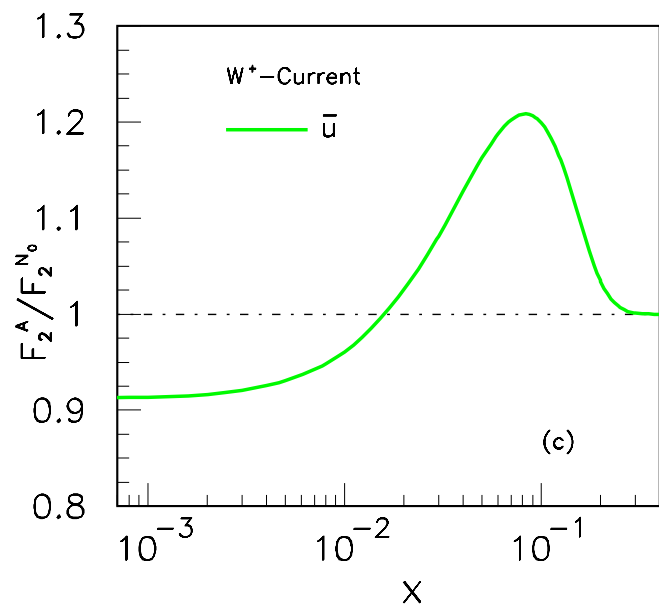
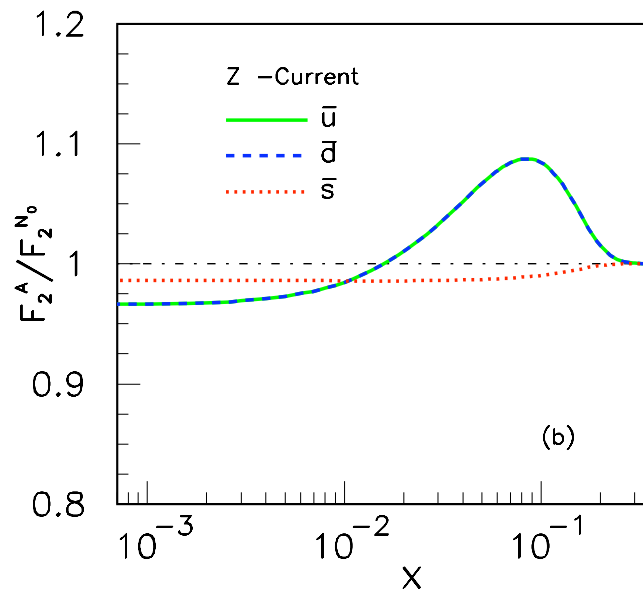
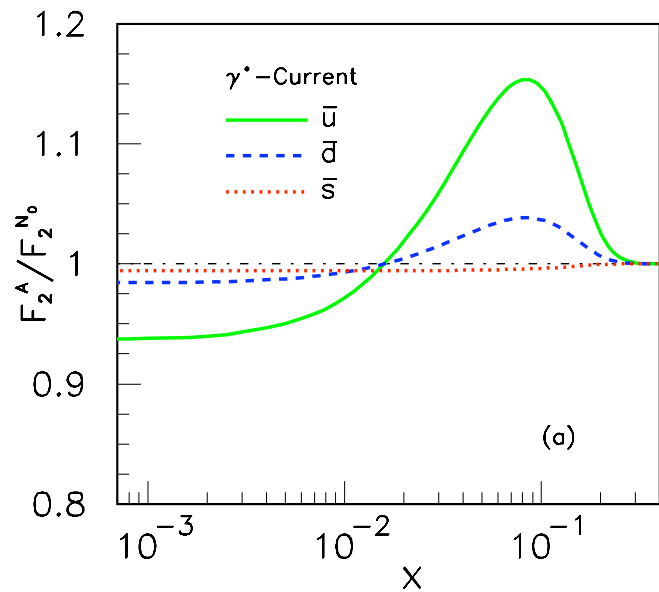
*Regge Phase can give  
constructive  
interference!*



Anomalous  
Z,A-Z dependence



Lu, Schmidt, Yang; sjb

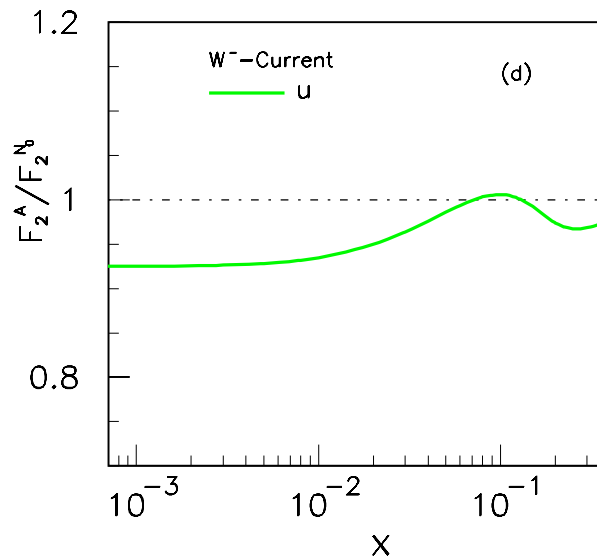
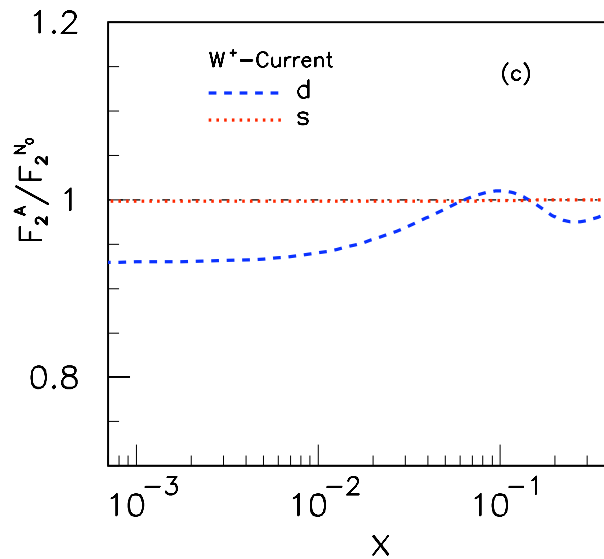
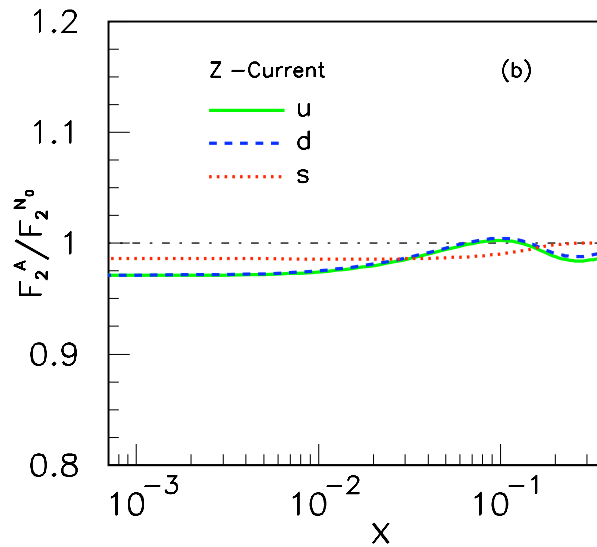
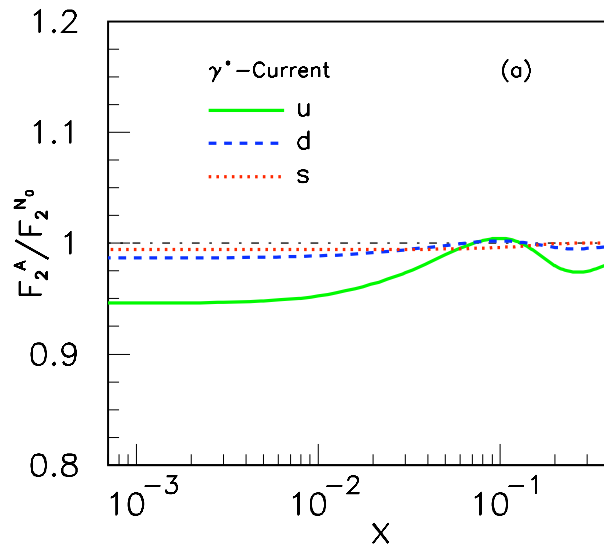


**Modifies  
NuTeV extraction of  
 $\sin^2 \theta_W$**

**Test in flavor-tagged  
DIS at the EIC**

*Nuclear Antishadowing not universal!*

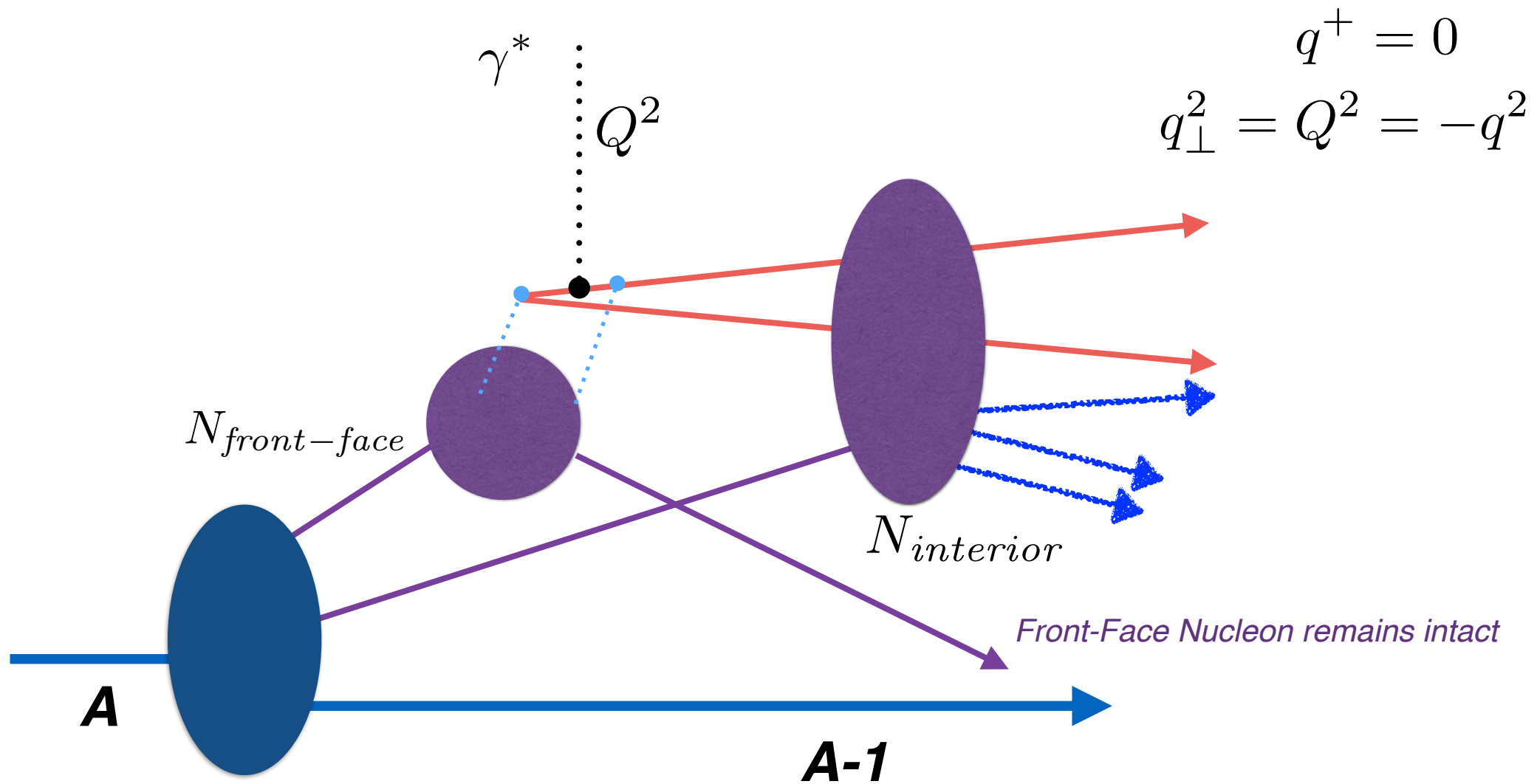
# Shadowing and Antishadowing of DIS Structure Functions



S. J. Brodsky, I. Schmidt and J. J. Yang,  
 “Nuclear Antishadowing in  
 Neutrino Deep Inelastic Scattering,”  
 Phys. Rev. D 70, 116003 (2004)  
 [arXiv:hep-ph/0409279].

**Modifies**  
**NuTeV extraction of**  
 $\sin^2 \theta_W$

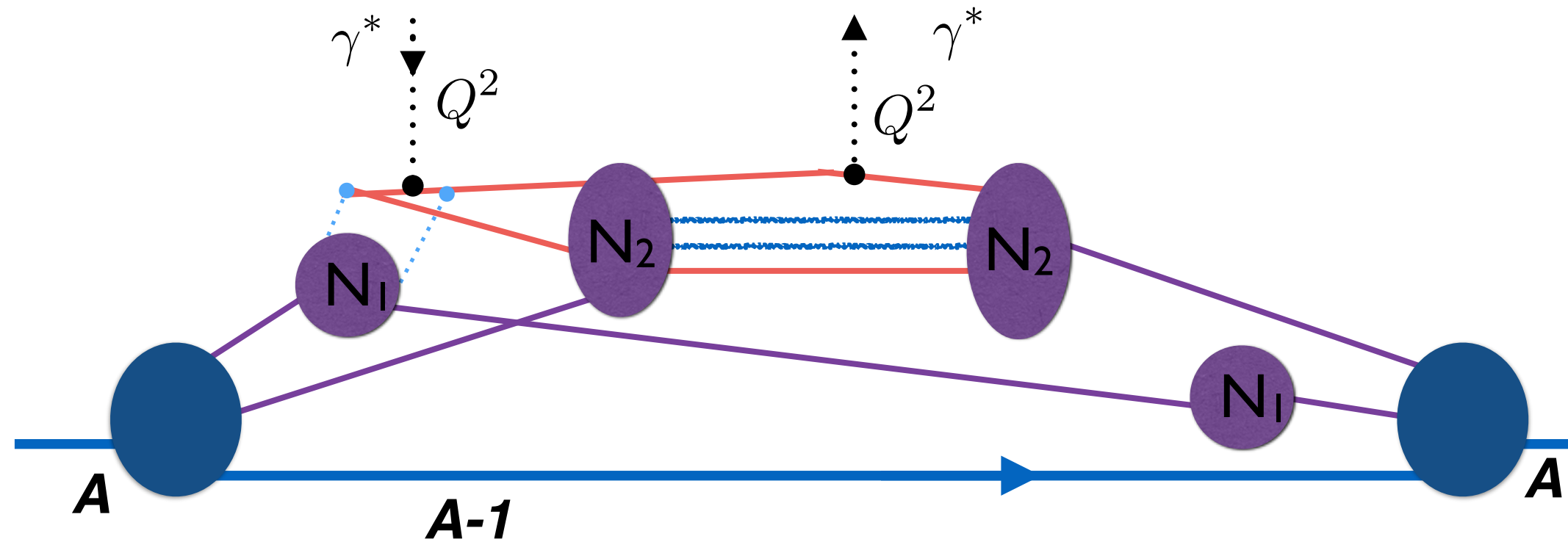
**Test in flavor-tagged**  
**lepton-nucleus collisions**



*Two-Step Process in the  $q^+ = 0$  Parton Model Frame*  
**Illustrates the LF time sequence**

**Illustrates the  
LF time sequence**

$$q^+ = 0 \quad q_{\perp}^2 = Q^2 = -q^2$$



*Front-Face Nucleon  $N_1$  struck*

*Front-Face Nucleon  $N_1$  not struck*

*One-Step / Two-Step Interference*

Study Double Virtual Compton Scattering  $\gamma^* A \rightarrow \gamma^* A$

**Cannot reduce to matrix element of local operator! No Sum Rules!**

LFWFs are real for stable hadrons, nuclei

Liuti, sjb

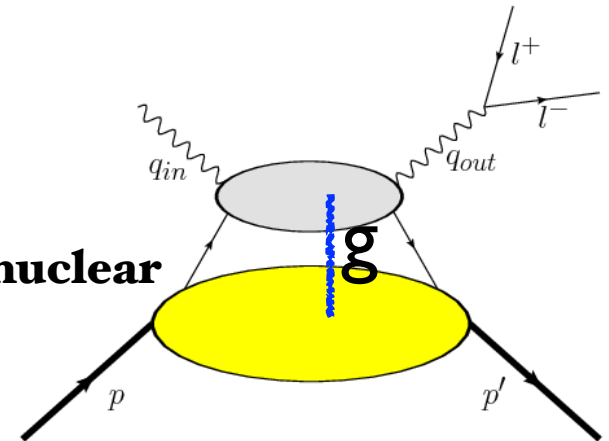
# *Crucial JLab Experiments*

- *Measure Diffractive DIS: Agree with Shadowing of Nuclear Structure Functions?*
- *Isospin Dependence of Diffractive DIS — Reggeon Exchange -*
- *Use deuteron: see  $n$  to  $p$*
- *Flavor Dependence of Antishadowing: Tagged Quark Distributions?*



# ***“Handbag” Approximation***

- **Parton model: assumes current-current correlator carried by single quark propagator at high photon virtuality**
- **Imaginary Part of Virtual Forward Compton Amplitude gives DIS structure Functions**
- **Leading-Twist Dominance — Motivated by the Operator Product Expansion**
- **Produces Momentum and Baryon Number Sum Rules**
- **Real Part:  $J=0$  Fixed Pole from local two-photon operators**
- **Will show: Handbag Approximation invalid for DVCS on a nuclear target because of shadowing, antishadowing!**
- **Recall: Sivers Effect and Diffractive DIS are leading twist!**



The GPD's are non-forward matrix elements of the PDF operator:

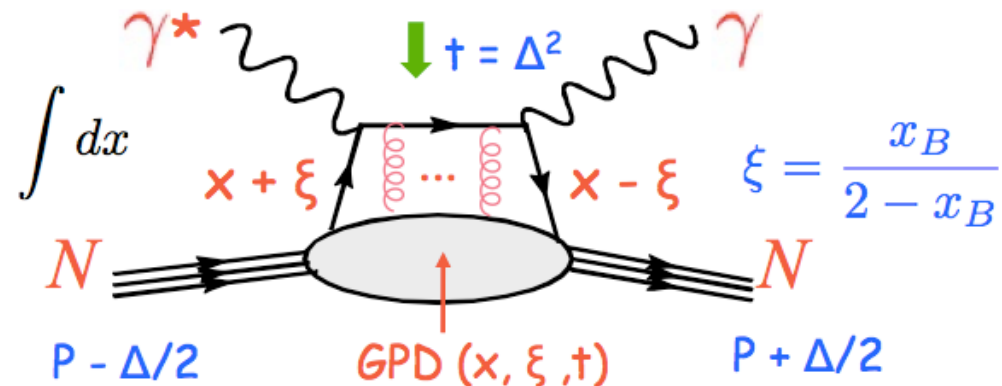
$$\frac{1}{8\pi} \int dr^- e^{imxr^-/2} \langle P + \frac{1}{2}\Delta | \bar{q}(-\frac{1}{2}r) \gamma^+ W[\frac{1}{2}r^-, -\frac{1}{2}r^-] q(\frac{1}{2}r) | P - \frac{1}{2}\Delta \rangle_{r^+=r_\perp=0}$$

$$= \frac{1}{2P^+} \bar{u}(P + \frac{1}{2}\Delta) \left[ H(x, \xi, t) \gamma^+ + E(x, \xi, t) i\sigma^{+\nu} \frac{\Delta_\nu}{2m} \right] u(P - \frac{1}{2}\Delta)$$

The GPD **amplitudes** can be accessed experimentally through the Deeply Virtual Compton Scattering **cross section** at leading twist:  $Q^2 \rightarrow \infty$ .

DVCS:  $e N \rightarrow e' + \gamma + N$

Through  $\Delta_\perp$ , the GPD's contain information about the parton distributions in transverse space.



*Handbag modified by leading-twist lensing!*

# Color Transparency

**Bertsch, Gunion, Goldhaber, sjb**

**Mueller, sjb**

**Frankfurt, Strikman, Miller**

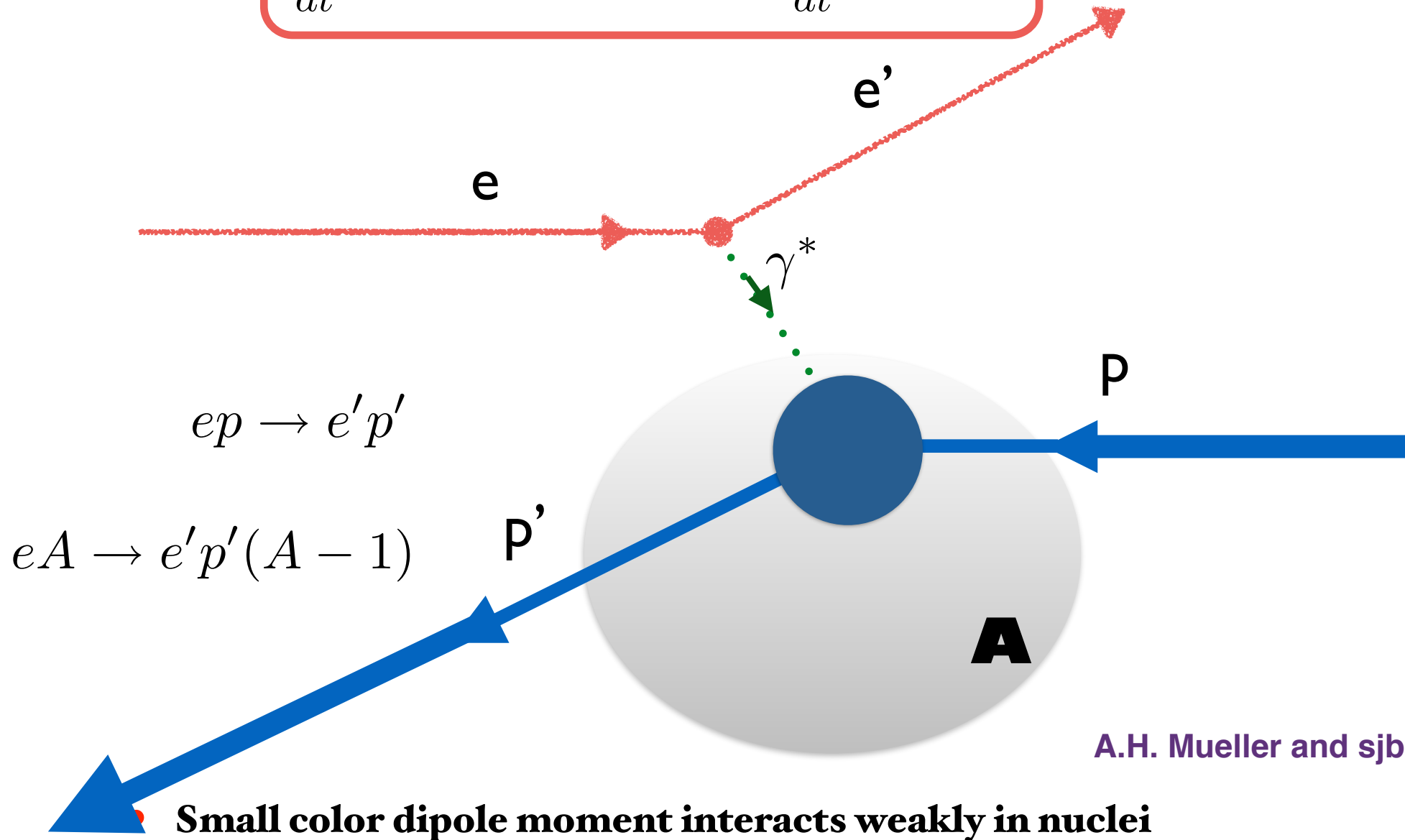
$$\frac{d\sigma}{dt}(eA \rightarrow ep(A-1)) = Z \frac{d\sigma}{dt}(ep \rightarrow ep) \quad \text{at high momentum transfer}$$

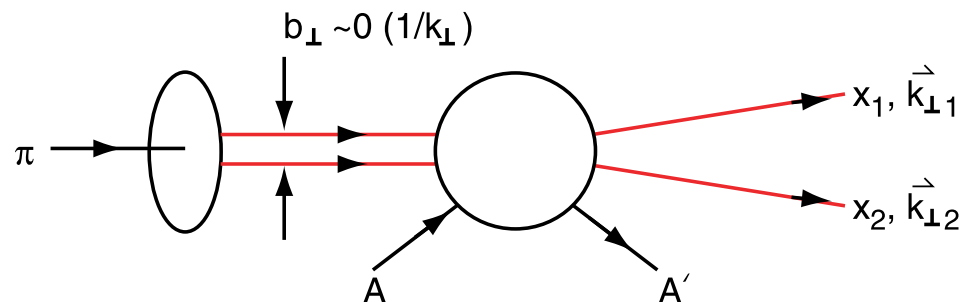
- **Fundamental test of gauge theory in hadron physics**
- **Small color dipole moment interacts weakly in nuclei**
- **Complete coherence at high energies**
- **Many tests in hard exclusive processes**
- **Clear Demonstration of CT from Diffractive Di-Jets**
- **Explains Baryon Anomaly at RHIC**

*See Strikman Talk*

# Color Transparency

$$\frac{d\sigma}{dt}(eA \rightarrow ep(A-1)) = Z \frac{d\sigma}{dt}(ep \rightarrow ep)$$

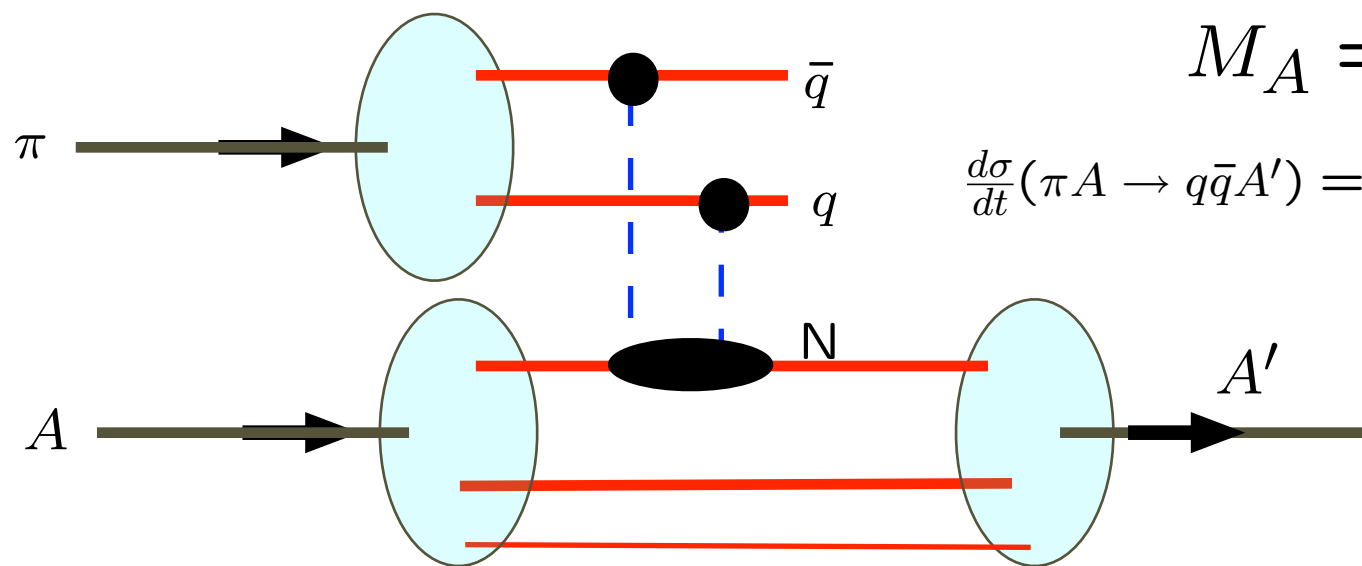




large  $k_{\perp}$ , small  $b_{\perp}$

*Small color-dipole moment pion not absorbed;  
interacts with each nucleon coherently*

QCD COLOR Transparency



$$M_A = A M_N$$

$$\frac{d\sigma}{dt}(\pi A \rightarrow q\bar{q}A') = A^2 \frac{d\sigma}{dt}(\pi N \rightarrow q\bar{q}N') F_A^2(t)$$

**Target left intact**

**Diffraction, Rapidity gap**

# Measure pion LFWF in diffractive dijet production Confirmation of color transparency

A-Dependence results:  $\sigma \propto A^\alpha$

<u><math>k_t</math> range (GeV/c)</u>	<u><math>\alpha</math></u>	<u><math>\alpha</math> (CT)</u>
$1.25 < k_t < 1.5$	$1.64 +0.06 -0.12$	1.25
$1.5 < k_t < 2.0$	$1.52 \pm 0.12$	1.45
$2.0 < k_t < 2.5$	$1.55 \pm 0.16$	1.60

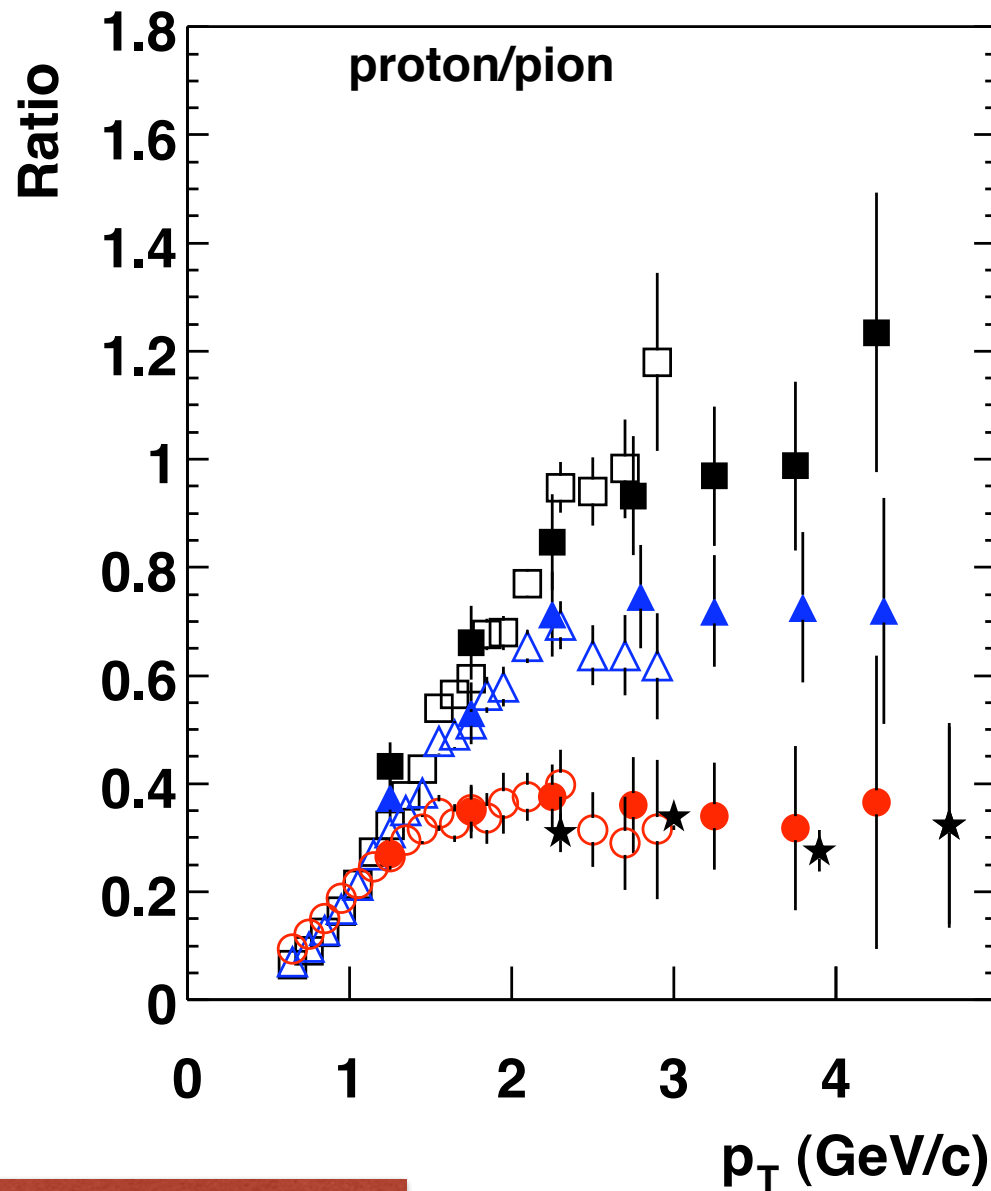
Ashery E791

$$\underline{\alpha \text{ (Incoh.)} = 0.70 \pm 0.1}$$

Conventional Glauber Theory Ruled Out !

Factor of 7

*Particle ratio changes with centrality!*



← **Central**

← **Peripheral**

*Protons less absorbed  
in nuclear collisions than pions  
because of dominant  
color-transparent higher twist process*

*Arleo, Hwang, Sickles, sjb*

**Tannenbaum:  
Baryon Anomaly**

## *Evidence for Direct, Higher-Twist, Color Transparent Subprocesses at RHIC*

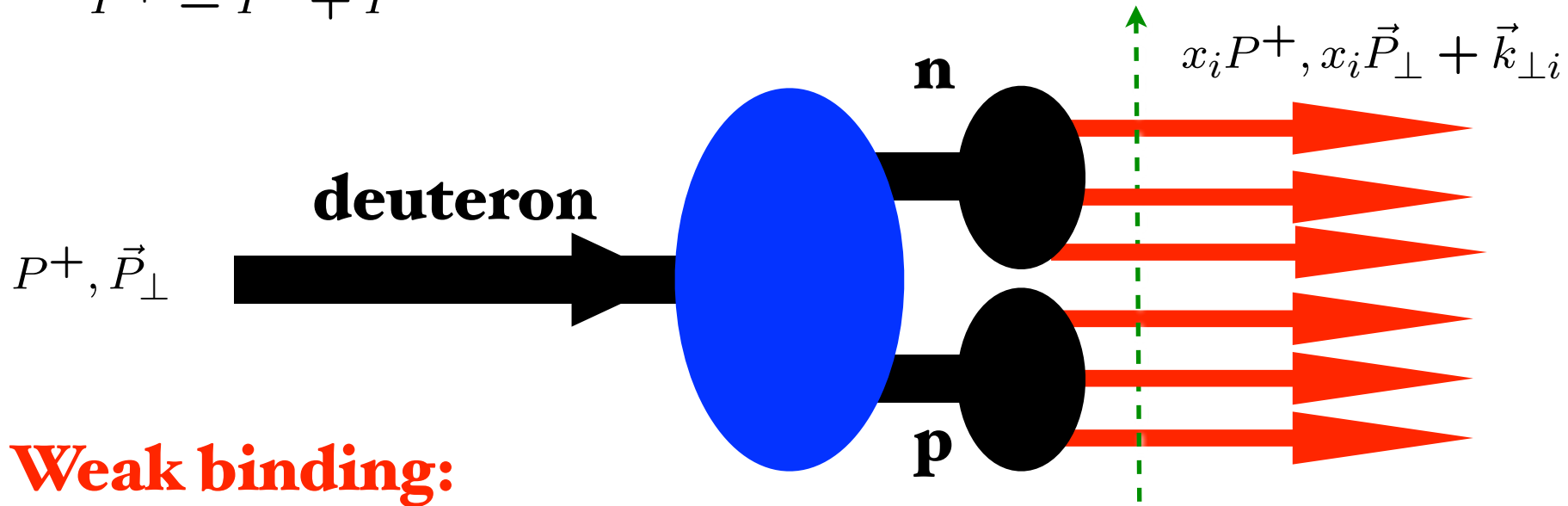
- **Anomalous power behavior at fixed  $x_T$**
- **Protons more likely to come from direct subprocess than pions**
- **protons not from jets! No same-side hadrons**
- **Protons less absorbed than pions in “central” nuclear collisions because of color transparency**
- **Predicts increasing proton to pion ratio in “central” collisions**
- **Exclusive-inclusive connection at  $x_T = 1$**

*EIC: Resolves complex physics signals at hadron and ion colliders*



$$P^+ = P^0 + P^z$$

Fixed  $\tau = t + z/c$



**Weak binding:**

$$\psi_d(x_i, \vec{k}_{\perp i}) = \psi_d^{body} \times \psi_n \times \psi_p$$

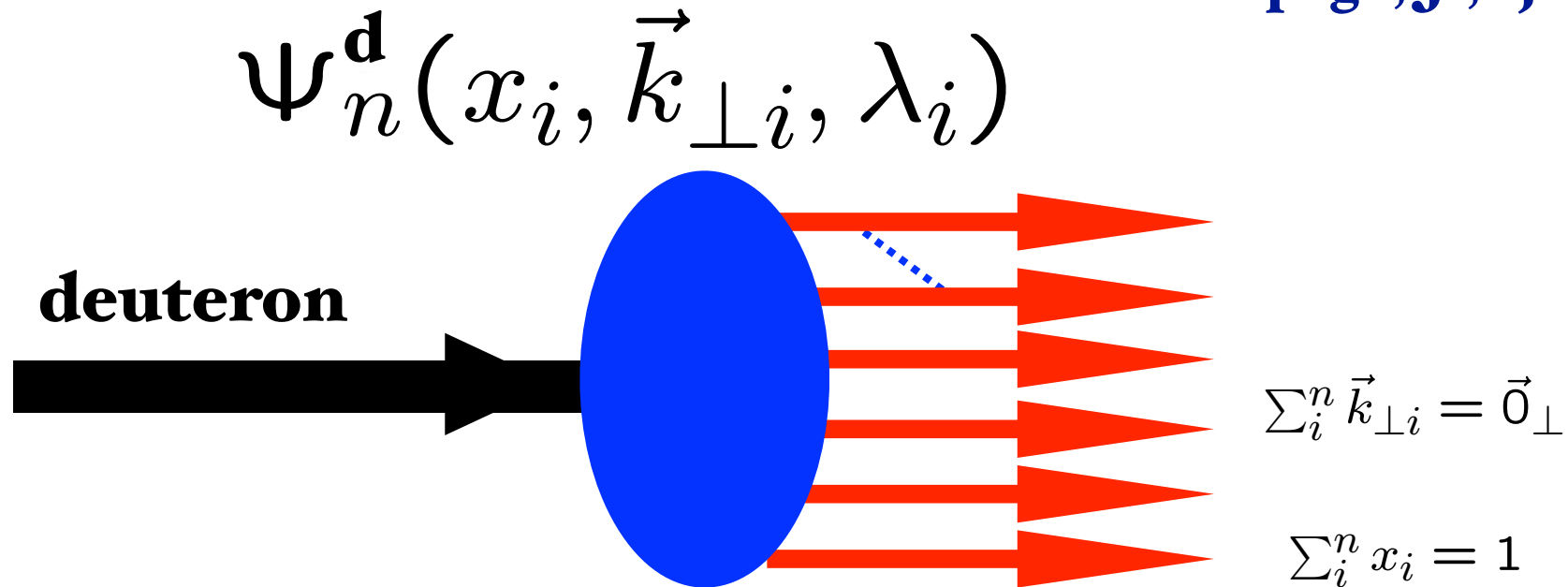
$$\sum_i^n x_i = 1$$

$$\sum_i^n \vec{k}_{\perp i} = \vec{0}_\perp$$

**Nuclear Physics:**  
**Two color-singlet combinations of three  $3_c$**

# pQCD Evolution of 5 color-singlet Fock states

Lepage, Ji, sjb



$$\Phi_n(x_i, Q) = \int^{k_{\perp i}^2 < Q^2} \Pi' d^2 k_{\perp j} \psi_n(x_i, \vec{k}_{\perp j})$$

5 X 5 Matrix Evolution Equation for deuteron  
distribution amplitude

# Hidden Color in QCD

## *Gluon or Quark Exchange within nucleus*

Lepage, Ji, sjb

- Deuteron six-quark wavefunction:
- 5 color-singlet combinations of six color-triplets --
- Only one of the five states is  $|\ln p\rangle$
- Components evolve towards equality at short distances
- Hidden color states dominate deuteron form factor and photodisintegration at high momentum transfer
- Dominates  $x > 1$  domain of deep inelastic scattering on nuclei: quark carries momentum of more than one nucleus!

$$\frac{d\sigma}{dt}(\gamma d \rightarrow \Delta^{++}\Delta^{-}) \simeq \frac{d\sigma}{dt}(\gamma d \rightarrow pn) \text{ at high } Q^2$$

# Hidden Color in QCD

## Study the Deuteron as a QCD Object

- Deuteron six-quark wavefunction
- 5 color-singlet combinations of 6 color-triplets -- only one state is  $|n\ p\rangle$
- Components evolve towards equality at short distances
- Hidden color states dominate deuteron form factor and photodisintegration at high momentum transfer
- Expense Dominance at  $x > 1$
- Predict  $\frac{d\sigma}{dt}(\gamma d \rightarrow \Delta^{++}\Delta^{-}) \simeq \frac{d\sigma}{dt}(\gamma d \rightarrow pn)$  at high  $Q^2$

## Hidden Color of Deuteron

**Deuteron six-quark state has five color-singlet configurations, only one of which is n-p.**

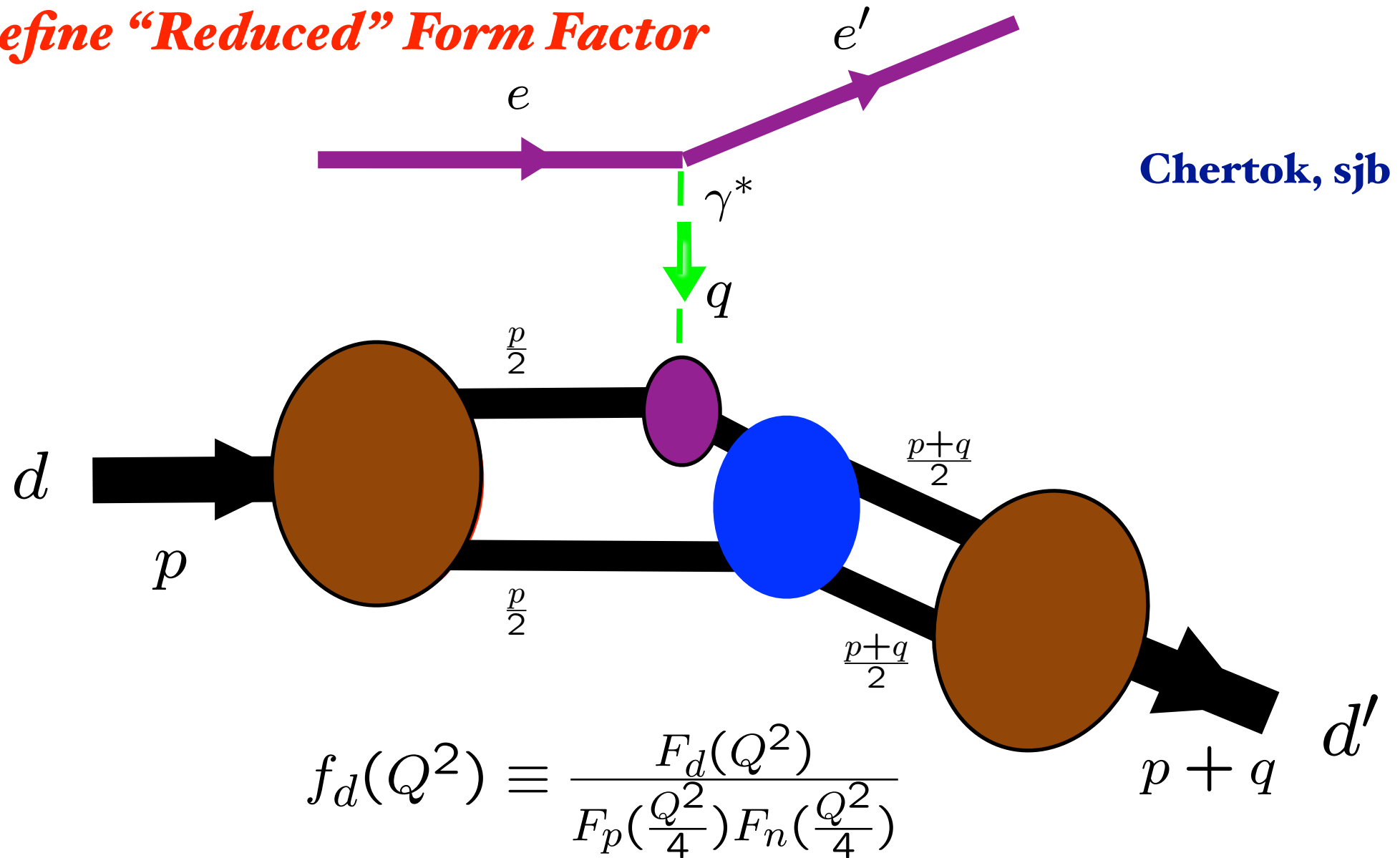
Asymptotic Solution has Expansion

$$\psi_{[6]\{33\}} = \left(\frac{1}{9}\right)^{1/2} \psi_{NN} + \left(\frac{4}{45}\right)^{1/2} \psi_{\Delta\Delta} + \left(\frac{4}{5}\right)^{1/2} \psi_{CC}$$

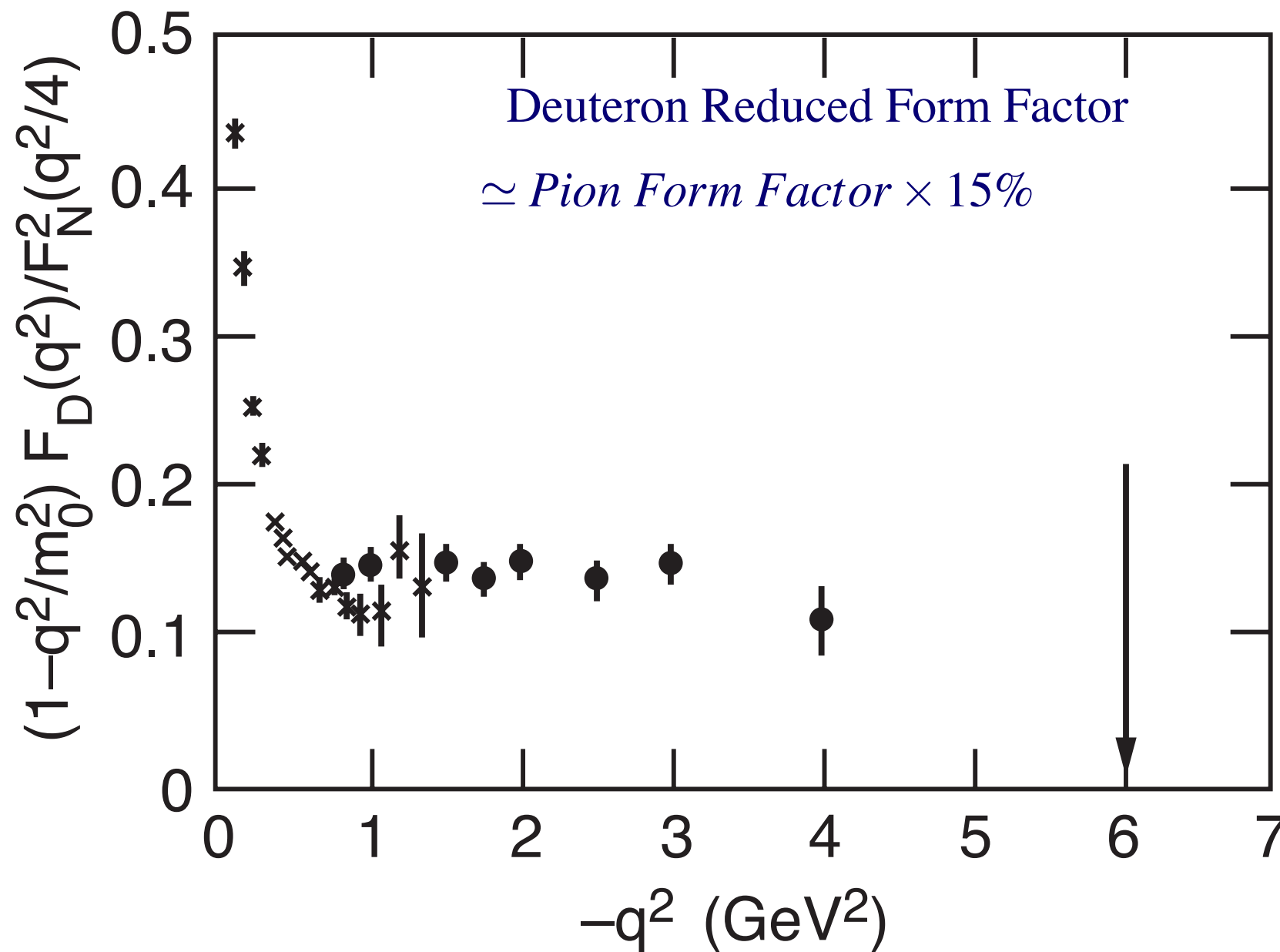
***ERBL Evolution: Transition to Delta-Delta***

**Lepage, Ji, sjb**

*Define “Reduced” Form Factor*



*Elastic electron-deuteron scattering*



# QCD Prediction for Deuteron Form Factor

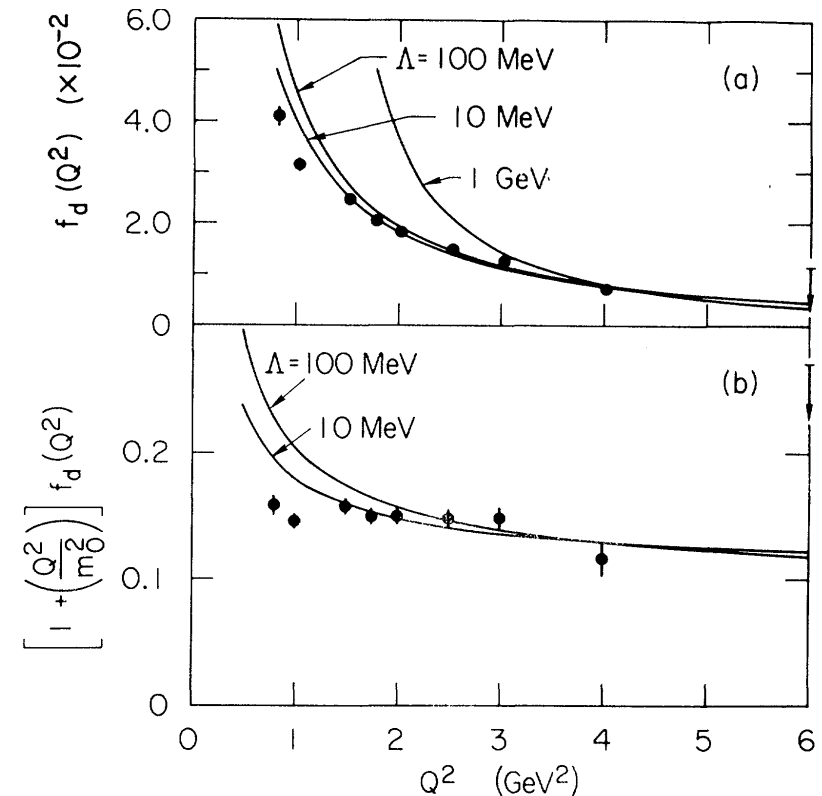
Lepage, Ji, sjb

$$F_d(Q^2) = \left[ \frac{\alpha_s(Q^2)}{Q^2} \right]^5 \sum_{m,n} d_{mn} \left( \ln \frac{Q^2}{\Lambda^2} \right)^{-\gamma_n^d - \gamma_m^d} \left[ 1 + O\left( \alpha_s(Q^2), \frac{m}{Q} \right) \right]$$

Define “Reduced” Form Factor

$$f_d(Q^2) \equiv \frac{F_d(Q^2)}{F_N^2(Q^2/4)}.$$

$$f_d(Q^2) \sim \frac{\alpha_s(Q^2)}{Q^2} \left( \ln \frac{Q^2}{\Lambda^2} \right)^{-(2/5) C_F/\beta}$$



(a) Comparison of the asymptotic QCD prediction  $f_d(Q^2) \propto (1/Q^2) [\ln(Q^2/\Lambda^2)]^{-1-(2/5)C_F/\beta}$  with final data of Ref. 10 for the reduced deuteron form factor, where  $F_N(Q^2) = [1 + Q^2/(0.71 \text{ GeV}^2)]^{-2}$ . The normalization is fixed at the  $Q^2 = 4 \text{ GeV}^2$  data point. (b) Comparison of the prediction  $[1 + (Q^2/m_0^2)] f_d(Q^2) \propto [\ln(Q^2/\Lambda^2)]^{-1-(2/5)C_F/\beta}$  with the above data. The value  $m_0^2 = 0.28 \text{ GeV}^2$  is used

Same large momentum transfer behavior as pion form factor



# Nuclear physics in soft-wall AdS/QCD: deuteron electromagnetic form factors

Thomas Gutsche, Valery E. Lyubovitskij, Ivan Schmidt, and Alfredo Vega

$$F_D(Q^2) \equiv f_D(Q^2) F_p\left(\frac{Q^2}{4}\right) F_n\left(\frac{Q^2}{4}\right)$$

*Chertok, sjb*

*Ji, Lepage, sjb*

$$\left[ -\frac{d^2}{dz^2} + \frac{4(L+4)^2 - 1}{4z^2} + \kappa^4 z^2 + \kappa^2 U_0 \right] \Phi_n(z) = M_{d,n}^2 \Phi_n(z)$$

AdS/QCD, LF Holography

*Katz, et al*

*de Tèramond, sjb*

$$f_d(Q^2) = \frac{30(a+1)(a+2)}{(a+3)(a+4)(a+5)}, \quad F_N(Q^2/4) = \frac{2}{(a+1)(a+2)}$$

$$a = Q^2/4\kappa^2 = Q^2/m_\rho^2$$

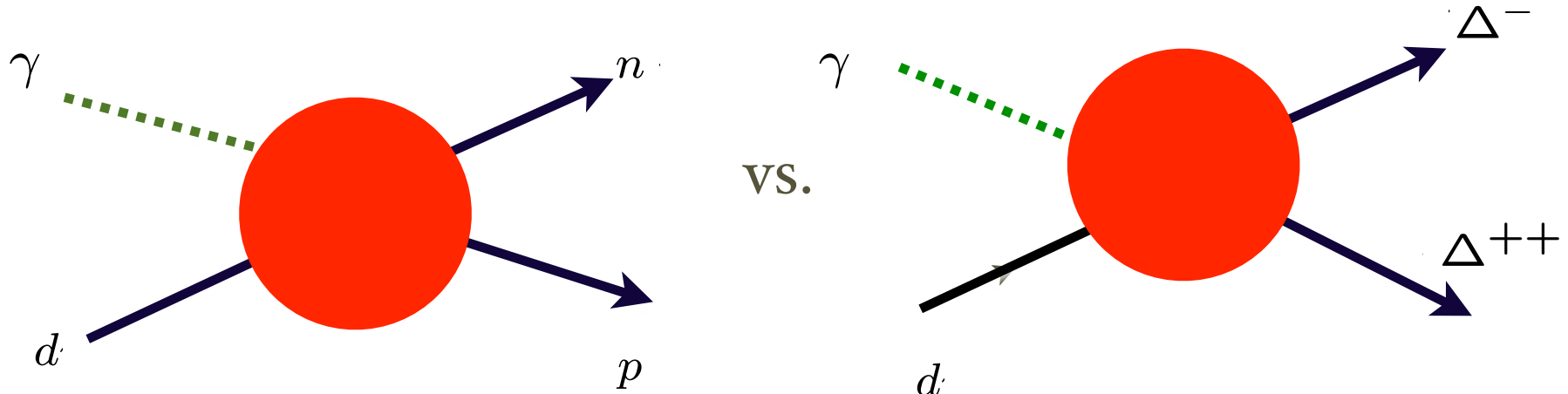
$$Q^2 f_d(Q^2) \rightarrow \text{const}$$

# Test of Hidden Color in Deuteron Photodisintegration

$$R = \frac{\frac{d\sigma}{dt}(\gamma d \rightarrow \Delta^{++} \Delta^{--})}{\frac{d\sigma}{dt}(\gamma d \rightarrow pn)}$$

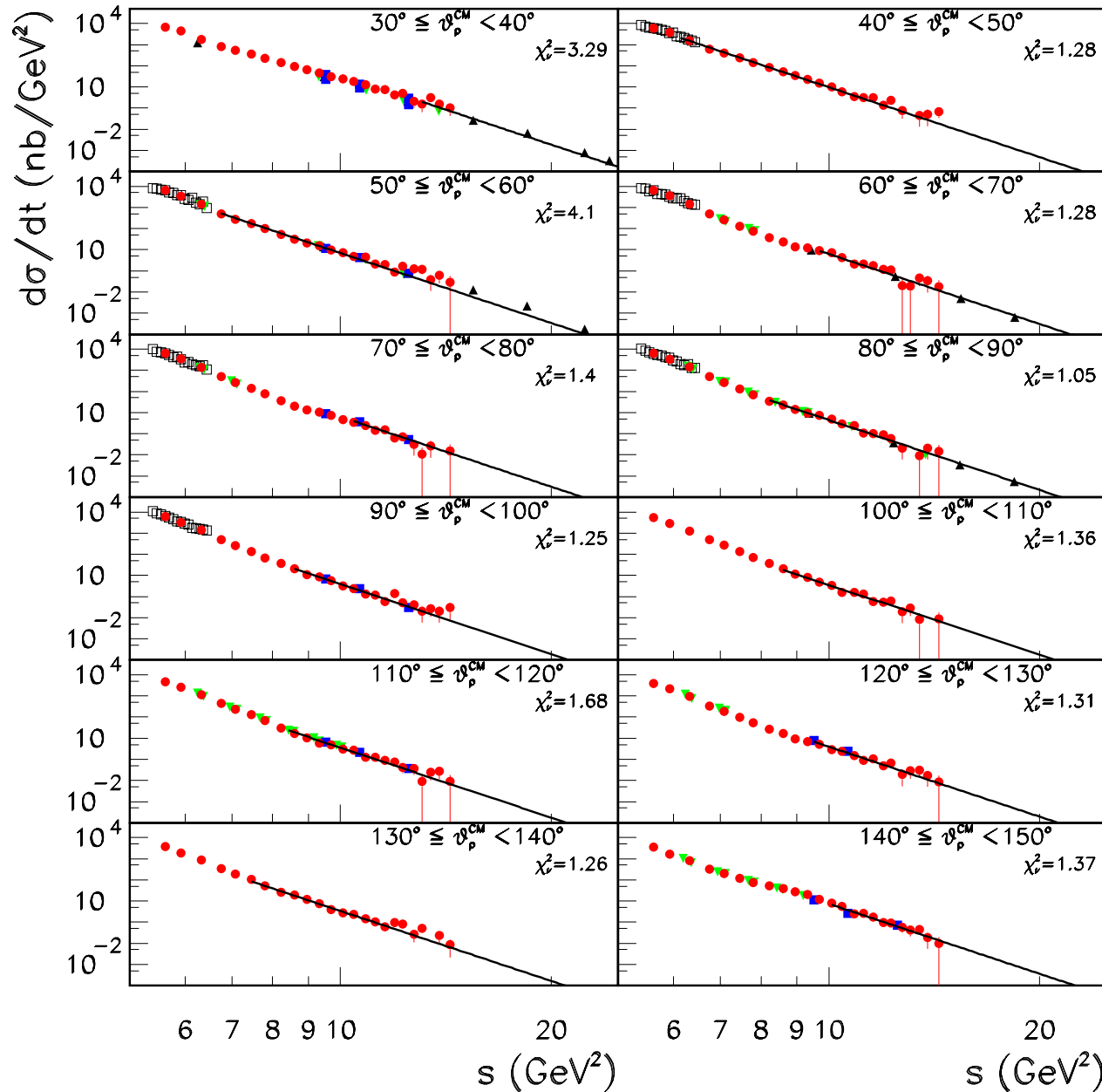
Ratio predicted to approach 2:5

**Ratio should grow with transverse momentum as the hidden color component of the deuteron grows in strength.**



**Possible contribution from pion charge exchange at small  $t$ .**

# Deuteron Photodisintegration



PQCD and AdS/CFT:

$$s^{n_{tot}-2} \frac{d\sigma}{dt} (A+B \rightarrow C+D) = F_{A+B \rightarrow C+D}(\theta_{CM})$$

$$s^{11} \frac{d\sigma}{dt} (\gamma d \rightarrow np) = F(\theta_{CM})$$

$$n_{tot} - 2 = (1 + 6 + 3 + 3) - 2 = 11$$

**Reflects conformal invariance**

# Novel QCD Physics at the EIC

- **Control Collisions of Flux Tubes and Ridge Phenomena**
- **Study Flavor-Dependence of Anti-Shadowing**
- **Heavy Quarks at Large  $x$ ; Exotic States**
- **Direct, color-transparent hard subprocesses and the baryon anomaly**
- **Tri-Jet Production and the proton's LFWF**
- **Odderon-Pomeron Interference**
- **Digluon-initiated subprocesses and anomalous nuclear dependence of quarkonium production**
- **Factorization-Breaking Lensing Corrections**



Each element of  
flash photograph  
illuminated  
along the light front  
*at a fixed*

$$\tau = t + z/c$$

*Evolve in LF time*

$$P^- = i \frac{d}{d\tau}$$

*Eigenvalue*

$$P^- = \frac{\mathcal{M}^2 + \vec{P}_\perp^2}{P^+}$$

$$H_{LF}^{QCD} |\Psi_h\rangle = \mathcal{M}_h^2 |\Psi_h\rangle$$

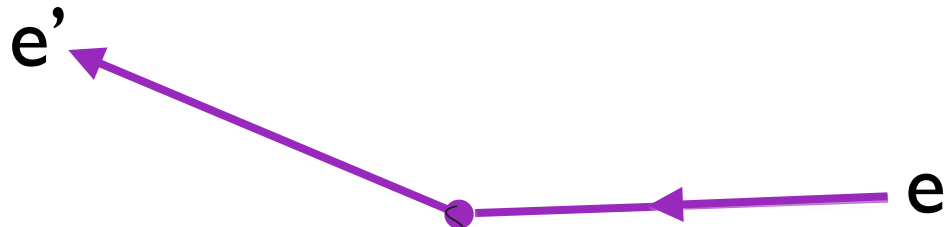


# Advantages of the Dirac's Front Form for Hadron Physics

## *Independent of Observer's Motion*



- **Measurements are made at fixed  $\tau$**
- **Causality is automatic**
- **Structure Functions are squares of LFWFs**
- **Form Factors are overlap of LFWFs**
- **LFWFs are frame-independent: no boosts, no pancakes!**
- **Same structure function measured at an e p collider and the proton rest frame**
- **No dependence on observer's frame**
- **LF Holography: Dual to AdS space**
- **LF Vacuum trivial -- no vacuum condensates!**
- **Profound implications for Cosmological Constant**



$$x = \frac{k^+}{P^+} = \frac{k^0 + k^3}{P^0 + P^3}$$

$P^+, \vec{P}_\perp$



$$\psi_n(x_i, \vec{k}_{\perp i}, \lambda_i)$$

$x_i P^+, x_i \vec{P}_\perp + \vec{k}_{\perp i}$



*Eigenstate of LF Hamiltonian:  
Off-shell in Invariant Mass*

***Measurements of hadron LF  
wavefunction are at fixed LF time***

Fixed  $\tau = t + z/c$



***Like a flash photograph***

$$x_{bj} = x = \frac{k^+}{P^+}$$

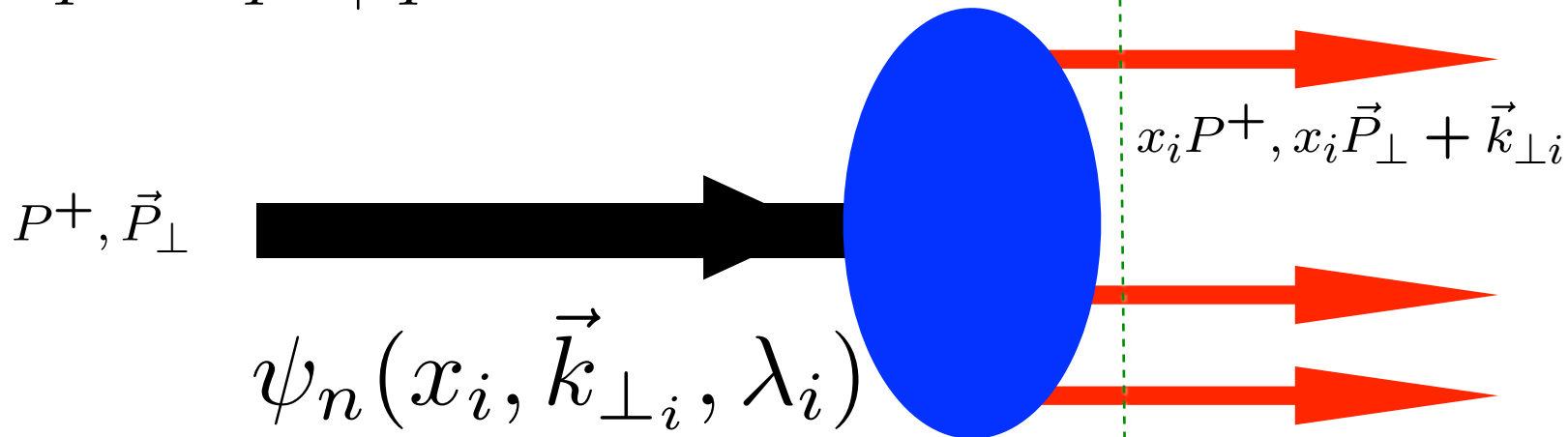
# Light-Front Wavefunctions: **rigorous** representation of composite systems in quantum field theory

*Eigenstate of LF Hamiltonian: Off-shell in Invariant Mass*

$$x = \frac{k^+}{P^+} = \frac{k^0 + k^3}{P^0 + P^3}$$

Fixed  $\tau = t + z/c$

*Fixed LF time*



$$|p, J_z\rangle = \sum_{n=3} \psi_n(x_i, \vec{k}_{\perp i}, \lambda_i) |n; x_i, \vec{k}_{\perp i}, \lambda_i\rangle$$

$$\sum_i^n x_i = 1$$

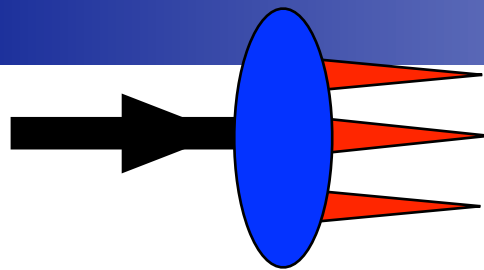
$$\sum_i^n \vec{k}_{\perp i} = \vec{0}_\perp$$

*Invariant under boosts! Independent of  $P^\mu$*

**Sum Rules**

**Causal, Frame-independent. Creation Operators on Simple Vacuum,  
Current Matrix Elements are Overlaps of LFWFS**





• *Light Front Wavefunctions:*

$$\Psi_n(x_i, \vec{k}_{\perp i}, \lambda_i)$$

Transverse density in momentum space

GTMDs

$$x, \vec{k}_{\perp}, \vec{b}_{\perp}$$

Momentum space  $\vec{k}_{\perp} \leftrightarrow \vec{z}_{\perp}$  Position space  
 $\vec{\Delta}_{\perp} \leftrightarrow \vec{b}_{\perp}$

Transverse density in position space

TMDs

$$x, \vec{k}_{\perp}$$

TMFFs

$$\vec{k}_{\perp}, \vec{b}_{\perp}$$

GPDs

$$x, \vec{b}_{\perp}$$

TMSDs

$$\vec{k}_{\perp}$$

PDFs

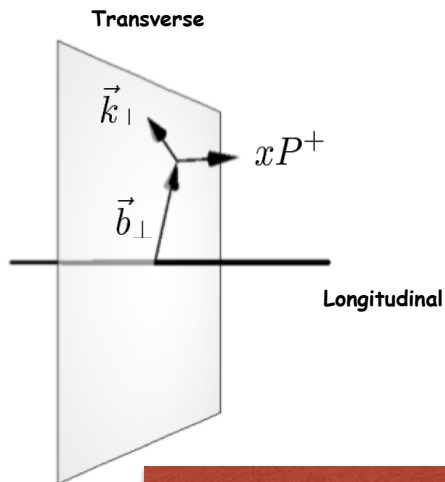
$$x,$$

FFs

$$\vec{b}_{\perp}$$

Charges

*Lorce,  
Pasquini*



**+ Factorization-Breaking Lensing Corrections: Sivers, T-odd**

$\rightarrow$   $\int d^2 b_{\perp}$   
 $\rightarrow$   $\int dx$   
 $\rightarrow$   $\int d^2 k_{\perp}$

$$|p, S_z\rangle = \sum_{n=3} \Psi_n(x_i, \vec{k}_{\perp i}, \lambda_i) |n; \vec{k}_{\perp i}, \lambda_i\rangle$$

*sum over states with  $n=3, 4, \dots$  constituents*

The Light Front Fock State Wavefunctions

$$\Psi_n(x_i, \vec{k}_{\perp i}, \lambda_i)$$

are boost invariant; they are independent of the hadron's energy and momentum  $P^\mu$ .

The light-cone momentum fraction

$$x_i = \frac{k_i^+}{p^+} = \frac{k_i^0 + k_i^z}{P^0 + P^z}$$

are boost invariant.

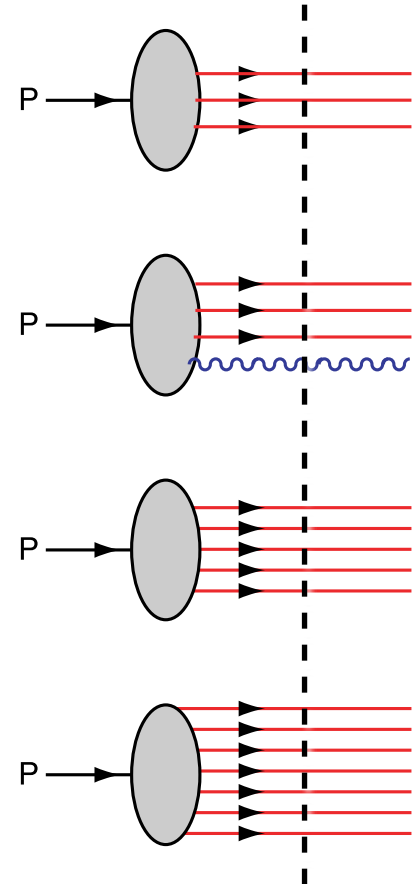
$$\sum_i^n k_i^+ = P^+, \quad \sum_i^n x_i = 1, \quad \sum_i^n \vec{k}_{\perp i} = \vec{0}^\perp.$$

*Intrinsic heavy quarks*  
 **$s(x), c(x), b(x)$  at high  $x$  !**

$$\bar{s}(x) \neq s(x)$$

$$\bar{u}(x) \neq \bar{d}(x)$$

*Deuteron: Hidden Color*



*Fixed LF time*  
 $\tau = t + z/c$

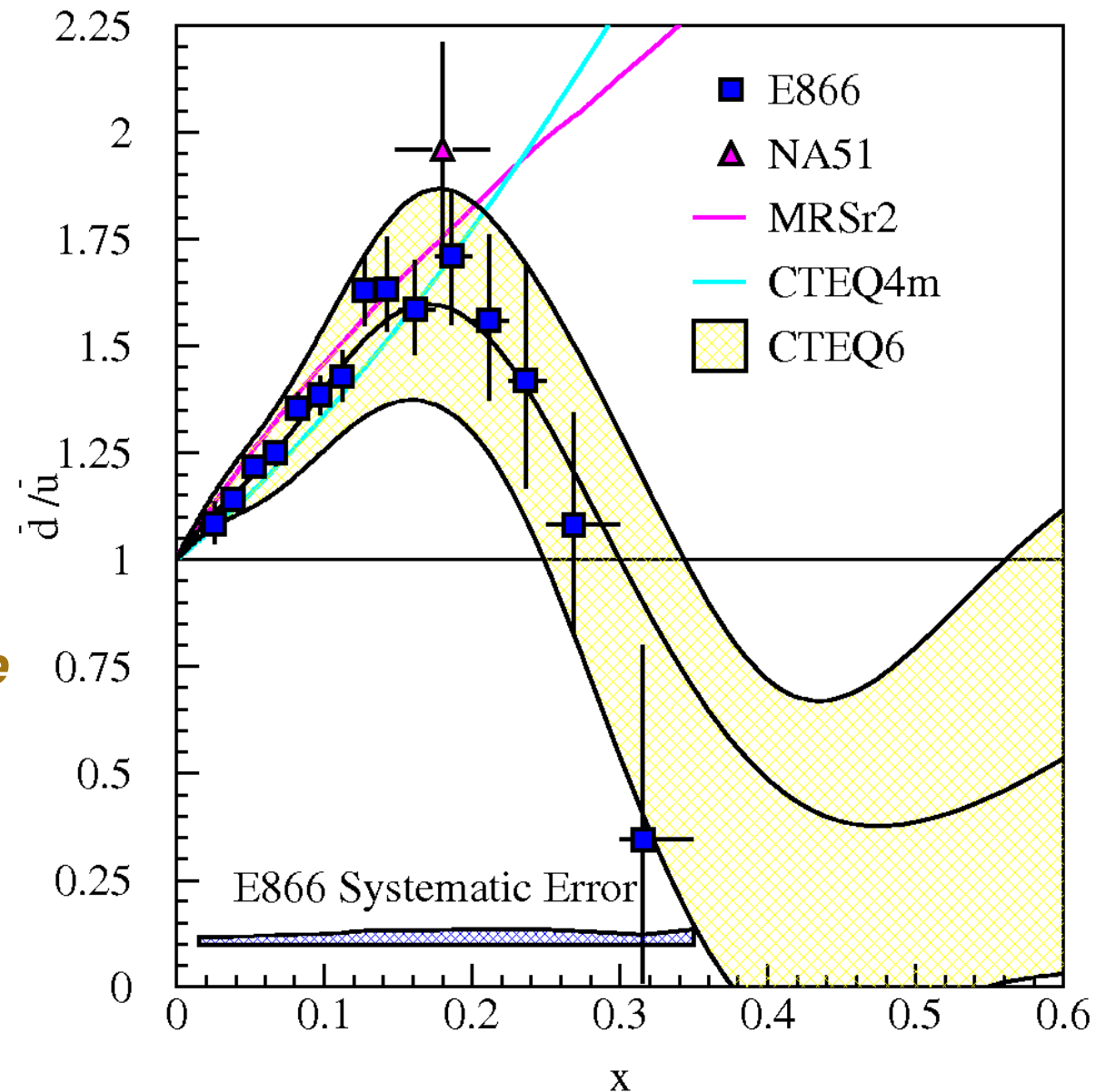
■ E866/NuSea (Drell-Yan)

$$\bar{d}(x) \neq \bar{u}(x)$$

*Interactions of quarks at same  
rapidity in 5-quark Fock state*

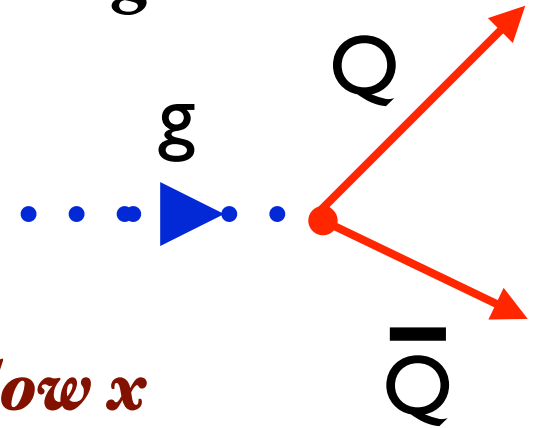
*Intrinsic sea quarks*

$$\bar{d}(x)/\bar{u}(x) \text{ for } 0.015 \leq x \leq 0.35$$



*Do heavy quarks exist in the proton at high  $x$ ?*

*Conventional wisdom:  
gluon splitting*



*Heavy quarks generated only at low  $x$   
via DGLAP evolution  
from gluon splitting*

*Maximally off-shell - requires low  $x$ , high  $W^2$*

$$s(x, \mu_F^2) = c(x, \mu_F^2) = b(x, \mu_F^2) \equiv 0$$

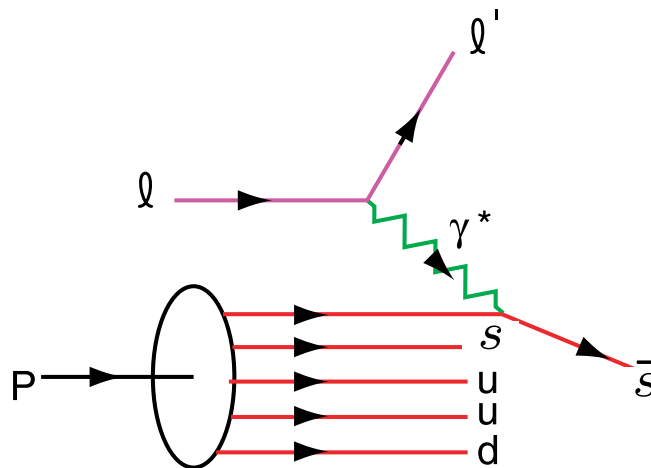
at starting scale  $Q_0^2 = \mu_F^2$

*Conventional wisdom is wrong even in QED!*

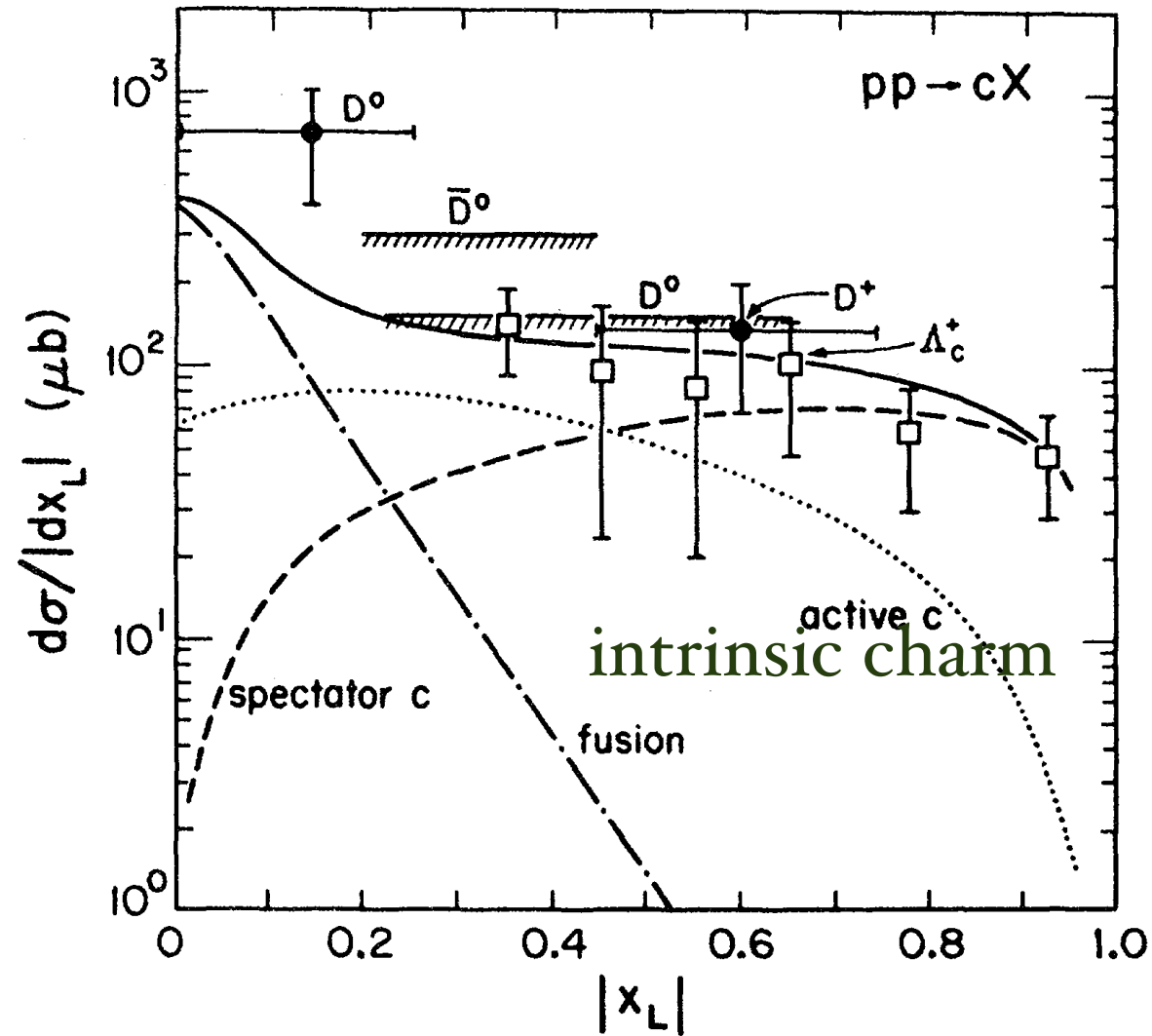
# Measure strangeness distribution in Semi-Inclusive DIS at JLab

$$\text{Is } s(x) = \bar{s}(x)?$$

- **Non-symmetric strange and antistrange sea?**
- **Non-perturbative physics; e.g.**  $|uuds\bar{s}\rangle \simeq |\Lambda(uds)K^+(\bar{s}u)\rangle$
- **Important for interpreting NuTeV anomaly** **B. Q. Ma, sjb**



**Tag struck quark flavor in semi-inclusive DIS**  $ep \rightarrow e' K^+ X$



**Barger, Halzen, Keung**

*Evidence for charm at large  $x$*

- EMC data:  $c(x, Q^2) > 30 \times \text{DGLAP}$   
 $Q^2 = 75 \text{ GeV}^2, x = 0.42$
- High  $x_F$   $pp \rightarrow J/\psi X$
- High  $x_F$   $pp \rightarrow J/\psi J/\psi X$
- High  $x_F$   $pp \rightarrow \Lambda_c X$
- High  $x_F$   $pp \rightarrow \Lambda_b X$
- High  $x_F$   $pp \rightarrow \Xi(ccd)X$  (SELEX)

### **Critical Measurements at threshold for JLab, PANDA**

**Interesting spin, charge asymmetry, threshold, spectator effects**

*Important corrections to B decays; Quarkonium decays*

Gardner, Karliner, sjb

# *Some Key QCD Issues in Electroproduction*

- **Intrinsic Heavy Quarks at high  $x$ ;  $s(x) \neq \bar{s}(x)$**
- **Role of Color Confinement in DIS**
- **Hadronization at the Amplitude Level**
- **Leading-Twist Lensing: Sivvers Effect**
- **Diffraction DIS**
- **Static versus Dynamic Structure Functions**
- **Origin of Shadowing and Anti-Shadowing**
- **Is Anti-Shadowing Non-Universal: Flavor Specific?**
- **Nuclear Correlations and Effects**



***Do heavy quarks exist in the proton at high  $x$ ?***

***Conventional wisdom: impossible!***

***Standard Assumption: Heavy quarks are generated  
via DGLAP evolution  
from gluon splitting***

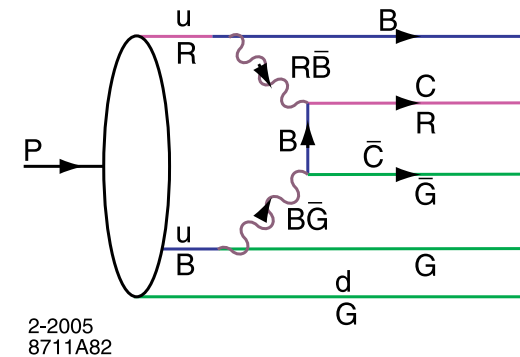
$$s(x, \mu_F^2) = c(x, \mu_F^2) = b(x, \mu_F^2) \equiv 0$$

at starting scale  $\mu_F^2$

***Conventional wisdom is wrong even in QED!***

# Intrinsic Heavy-Quark Fock States

- Rigorous prediction of QCD, OPE
- Color-Octet Color-Octet Fock State!
- Probability  $P_{Q\bar{Q}} \propto \frac{1}{M_Q^2}$   $P_{Q\bar{Q}Q\bar{Q}} \sim \alpha_s^2 P_{Q\bar{Q}}$   $P_{c\bar{c}/p} \simeq 1\%$
- Large Effect at high x
- Greatly increases kinematics of colliders such as Higgs production at high  $x_F$  (Kopeliovich, Schmidt, Soffer, Goldhaber, sjb)
- Severely underestimated in conventional parameterizations of heavy quark distributions (Pumplin, Tung)
- Many empirical tests (Gardener, Karliner, ..)

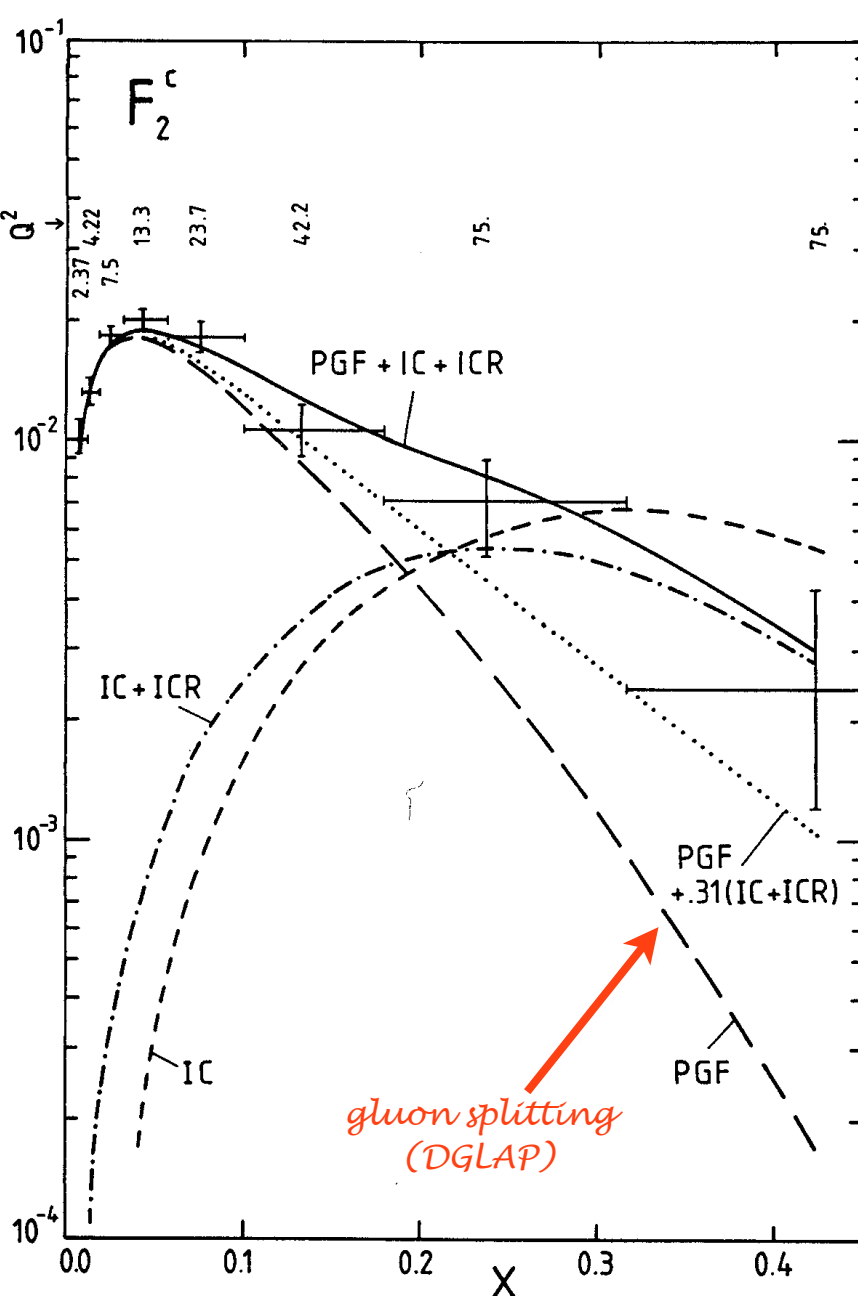


# Measurement of Charm Structure Function!

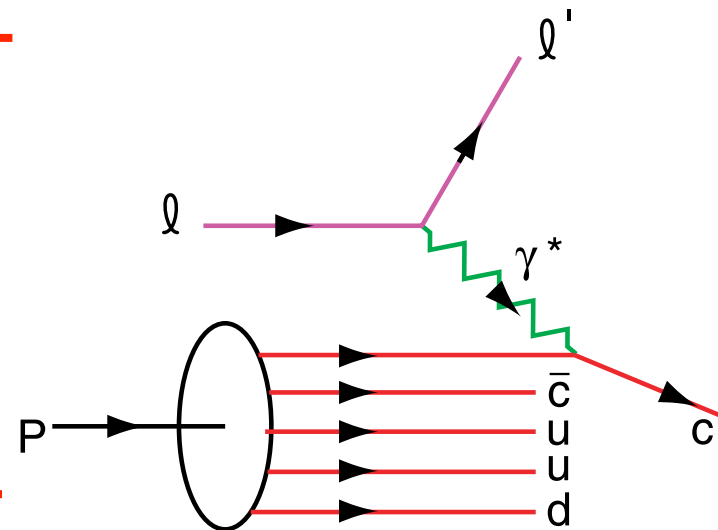
J. J. Aubert et al. [European Muon Collaboration], "Production Of Charmed Particles In 250-GeV Mu+ - Iron Interactions," Nucl. Phys. B 213, 31 (1983).

## First Evidence for Intrinsic Charm

Hoyer, Peterson, Sakai, sjb



factor of 30 !

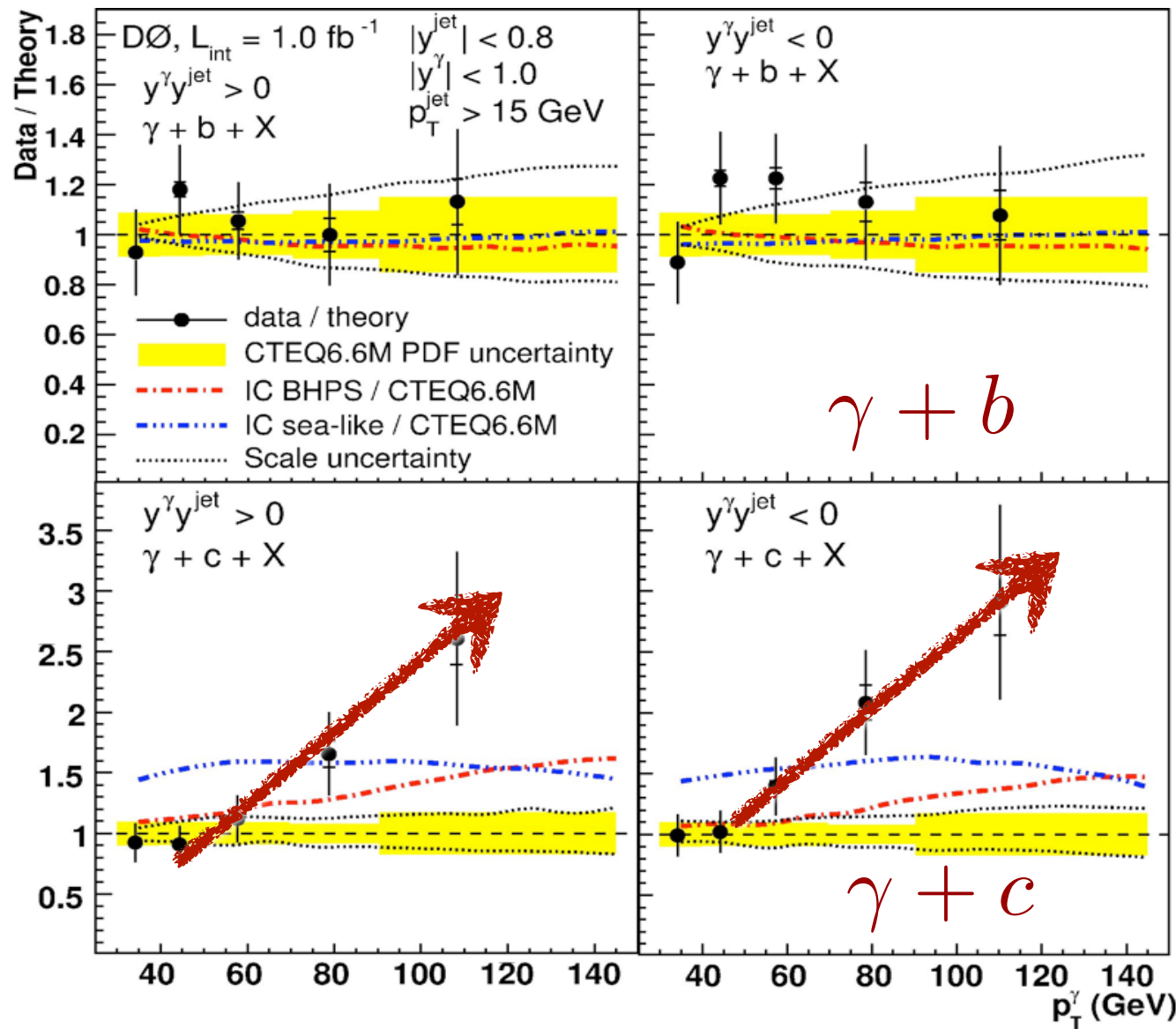


**DGLAP / Photon-Gluon Fusion: factor of 30 too small**

*Two Components (separate evolution):*

$$c(x, Q^2) = c(x, Q^2)_{\text{extrinsic}} + c(x, Q^2)_{\text{intrinsic}}$$

Measurement of  $\gamma + b + X$  and  $\gamma + c + X$  Production Cross Sections  
in  $p\bar{p}$  Collisions at  $\sqrt{s} = 1.96$  TeV



$$\frac{\Delta\sigma(\bar{p}p \rightarrow \gamma c X)}{\Delta\sigma(\bar{p}p \rightarrow \gamma b X)}$$

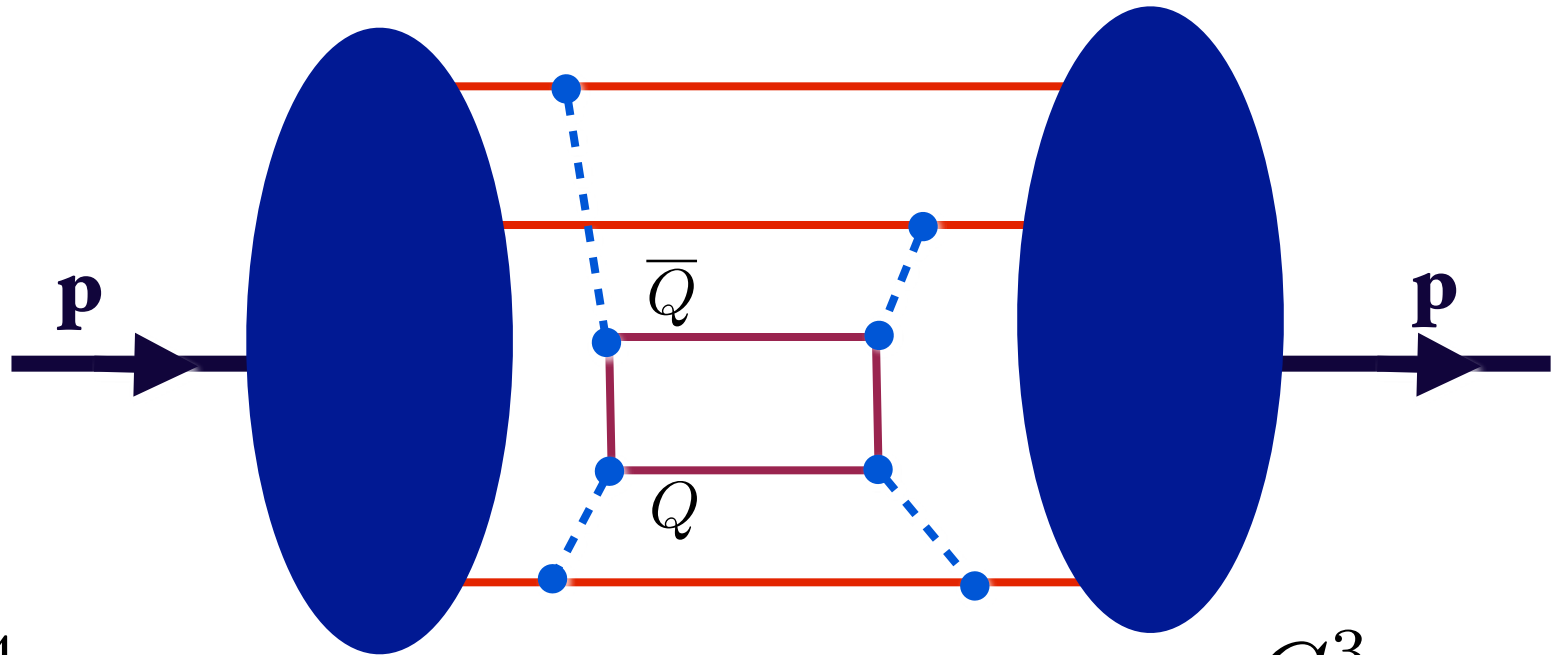
**Ratio**  
**insensitive to**  
**gluon PDF,**  
**scales**

**Signal for**  
**significant IC**  
**at  $x > 0.1$**

**Need COMPASS**  
**Measurement**  
**of  $c(x, Q^2)$ !**

**Proton Self Energy from g g to gg scattering**  
*QCD predicts Intrinsic Heavy Quarks!*

$$x_Q \propto (m_Q^2 + k_\perp^2)^{1/2}$$



$$\frac{F_{\mu\nu}^4}{M_\ell^2}$$

$$\text{Probability (QED)} \propto \frac{1}{M_\ell^4}$$

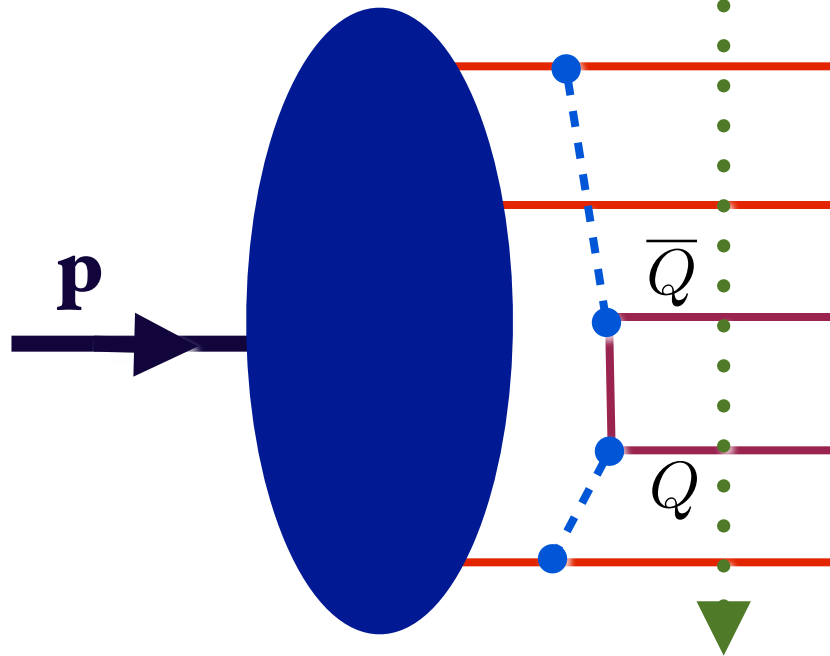
$$\frac{G_{\mu\nu}^3}{M_Q^2}$$

$$\text{Probability (QCD)} \propto \frac{1}{M_Q^2}$$

**Collins, Ellis, Gunion, Mueller, sjb**  
**M. Polyakov, et al.**

*Fixed LF time*

*Proton 5-quark Fock State :  
Intrinsic Heavy Quarks*



*QCD predicts  
Intrinsic Heavy  
Quarks at high  $x$*

**Minimal off-  
shellness**

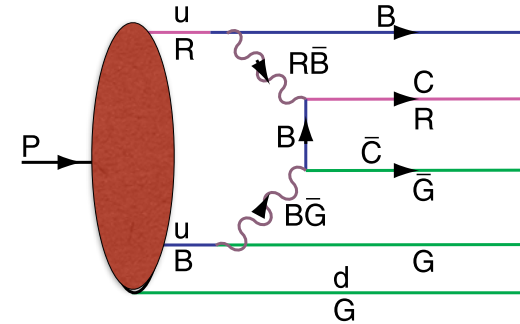
$$x_Q \propto (m_Q^2 + k_\perp^2)^{1/2}$$

$$\text{Probability (QED)} \propto \frac{1}{M_\ell^4}$$

$$\text{Probability (QCD)} \propto \frac{1}{M_Q^2}$$

**Collins, Ellis, Gunion, Mueller, sjb  
M. Polyakov**

# Intrinsic Heavy-Quark Fock



- **Rigorous prediction of QCD, OPE**

- **Color-Octet Color-Octet Fock State**

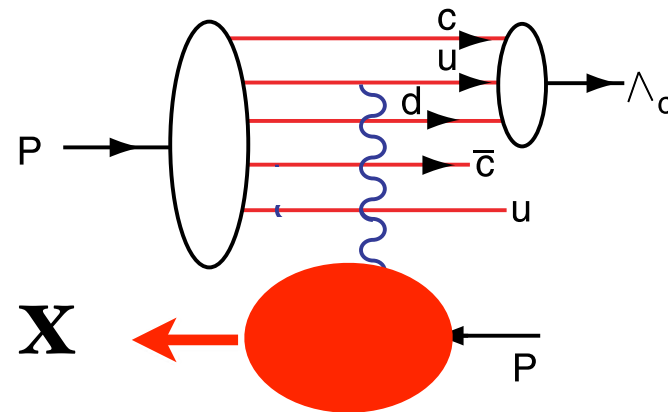
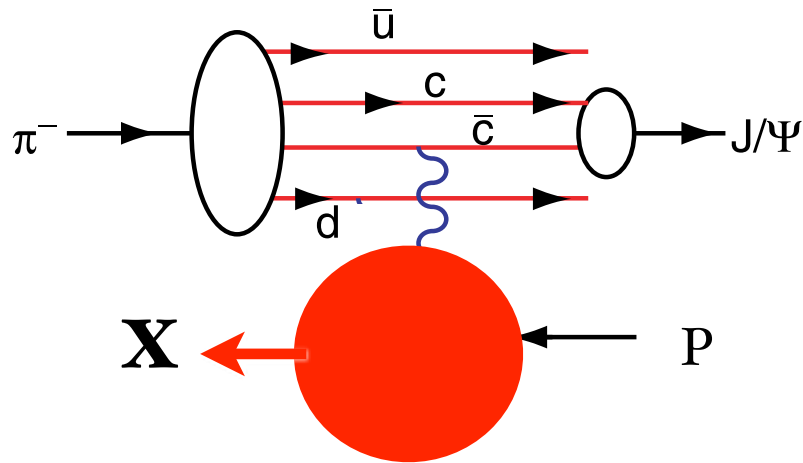
- **Probability**  $P_{Q\bar{Q}} \propto \frac{1}{M_Q^2}$   $P_{Q\bar{Q}Q\bar{Q}} \sim \alpha_s^2 P_{Q\bar{Q}}$   $P_{c\bar{c}/p} \simeq 1\%$

- **Large Effect at high x**

- **Greatly increases kinematics of colliders such as Higgs production (Kopeliovich, Schmidt, Soffer, sjb)**

- **Underestimated in conventional parameterizations of heavy quark distributions (Pumplin, Tung)**

# Leading Hadron Production from Intrinsic Charm



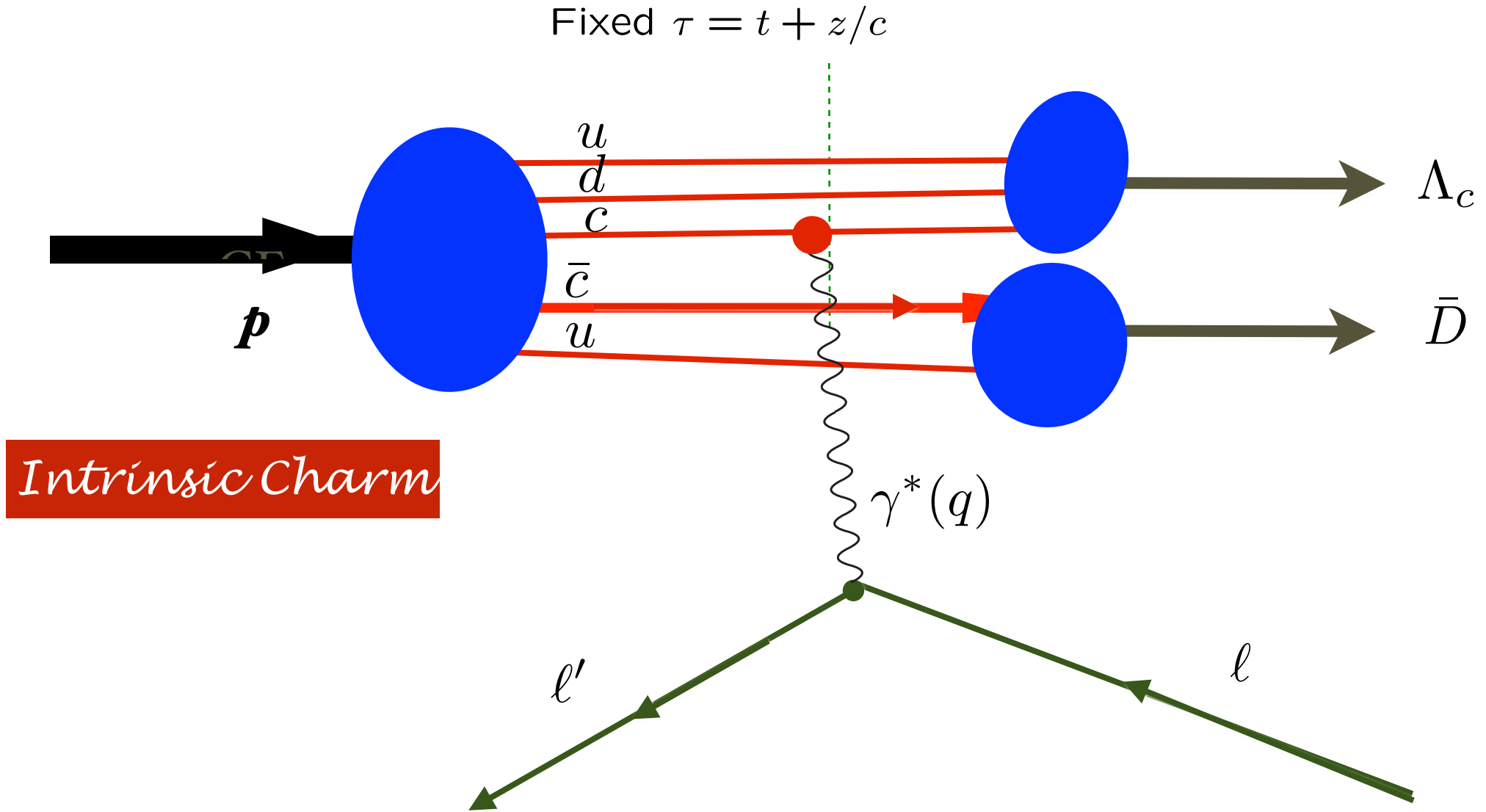
***Spectator counting rules***

$$\frac{dN}{dx_F} \propto (1 - x_F)^{2n_{spect}-1}$$

Coalescence of Comoving Charm and Valence Quarks  
Produce  $J/\psi$ ,  $\Lambda_c$  and other Charm Hadrons at High  $x_F$



# Light-Front Wavefunctions and Heavy-Quark Electroproduction

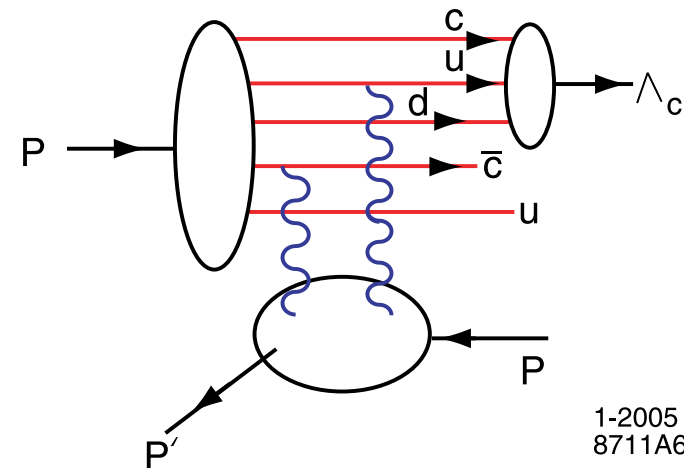
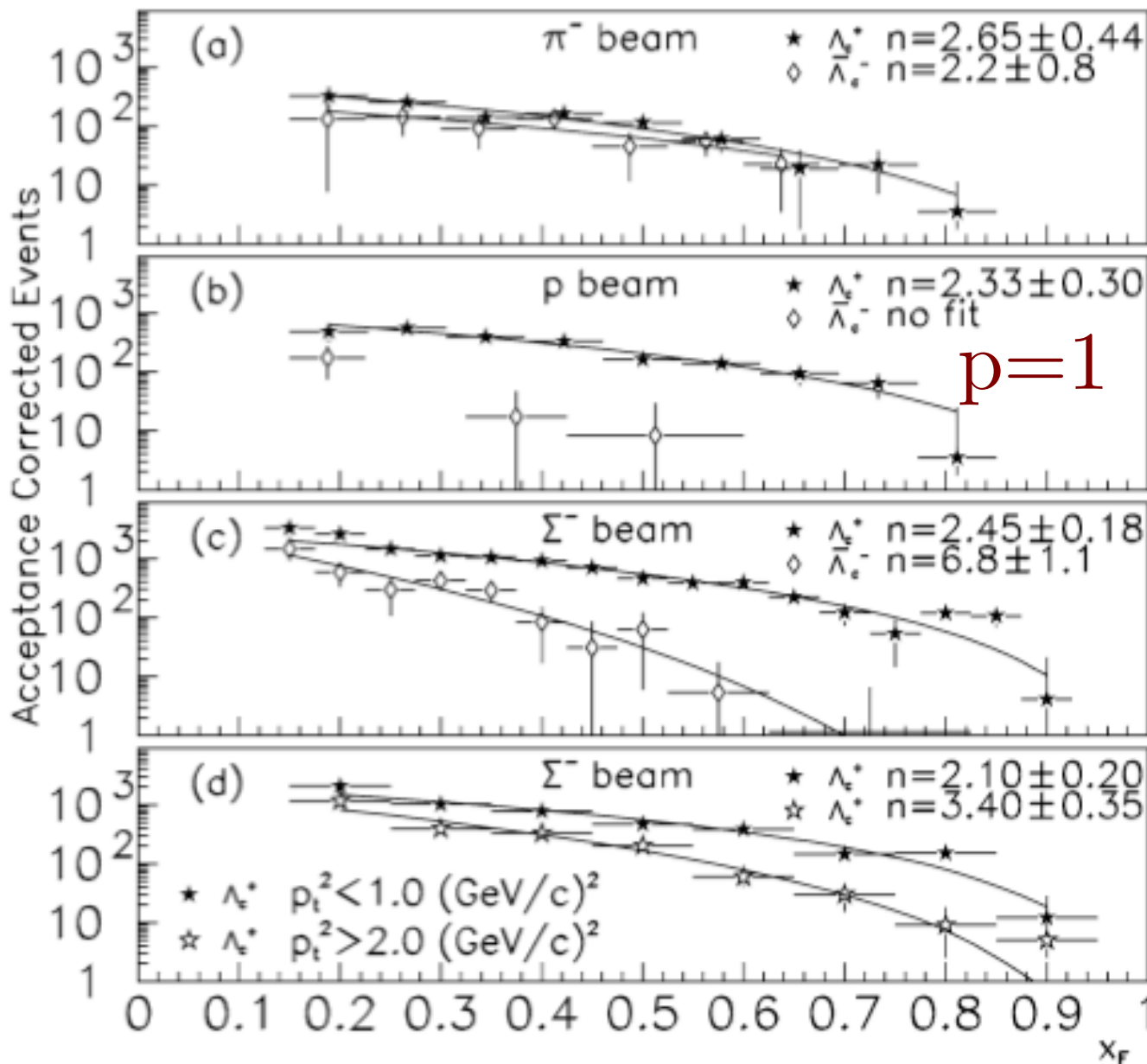


*Threshold Production at JLab!*

Coalescence of comovers produces  $|F\rangle = |\Lambda_c \bar{D}\rangle$  Final State

**Charm Produced in Target-Rapidity Domain**

**SELEX**



$$p(uudc\bar{c}) \rightarrow \Lambda_c(cud)$$

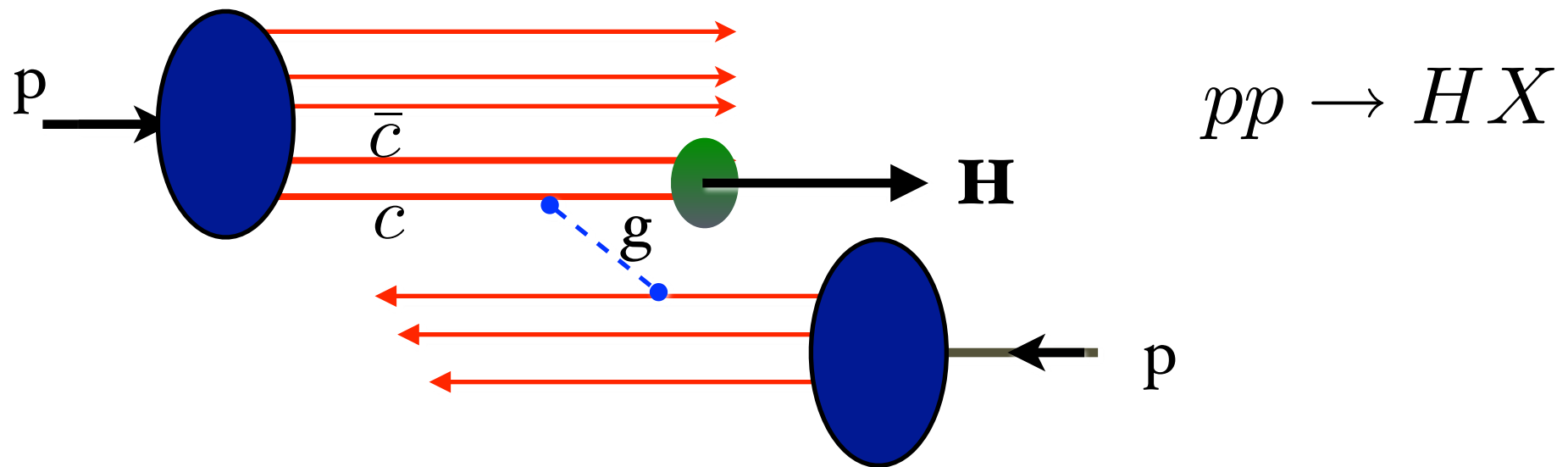
$$n_s = 2$$

**Phase space alone  
gives minimum power**

$$(1 - x_F)^p, p = n_s - 1$$

Maximum fraction  
of projectile momentum  
carried by charm quarks!

# *Intrinsic Charm Mechanism for Inclusive High- $x_F$ Higgs Production*



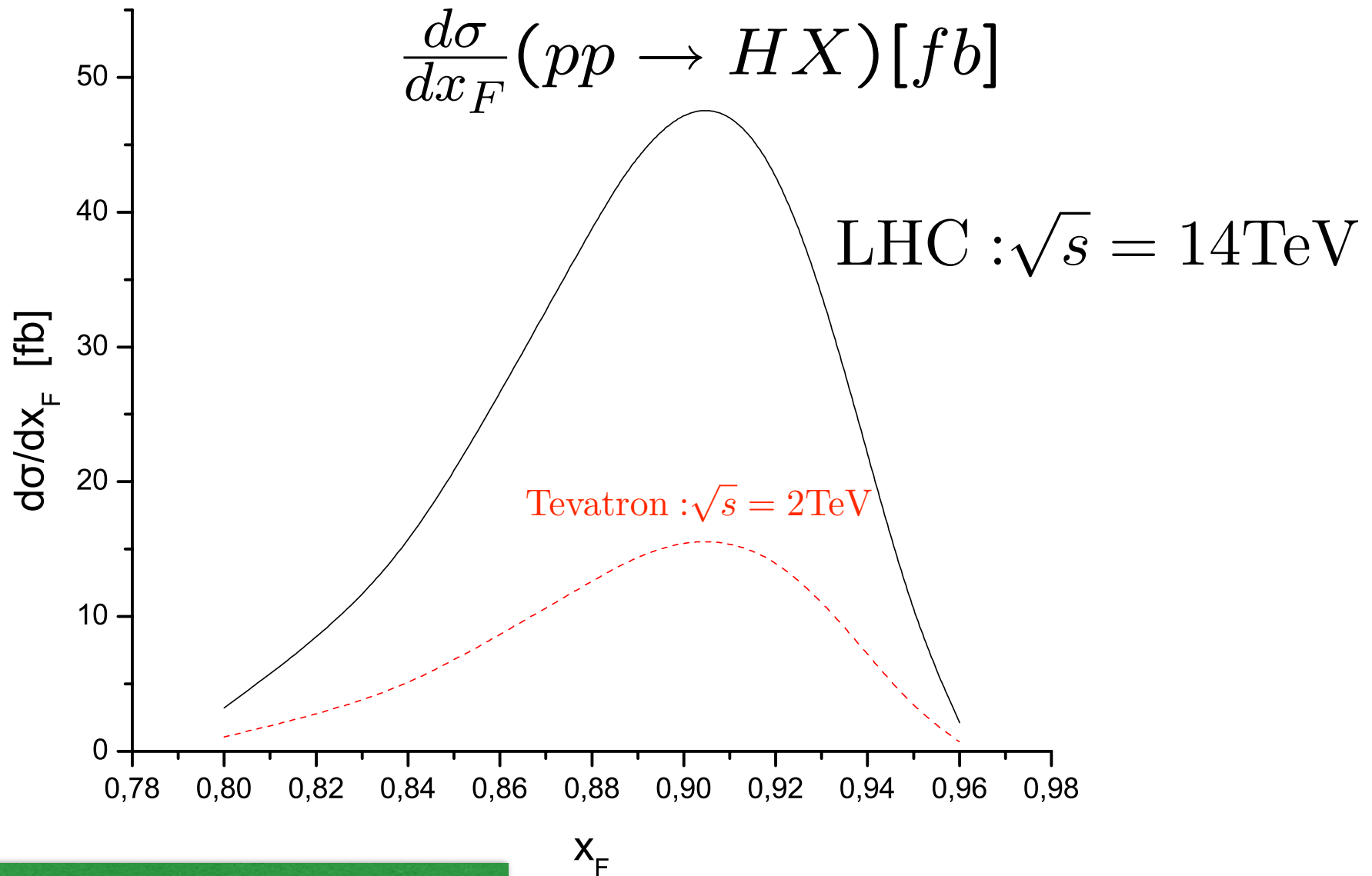
**Also: intrinsic bottom, top**

**Goldhaber, Soffer,  
Kopeliovich, Schmidt, sjb**

**Higgs can have 80% of Proton Momentum!**

*New search strategy for Higgs*

***AFTER: Higgs production at threshold!***



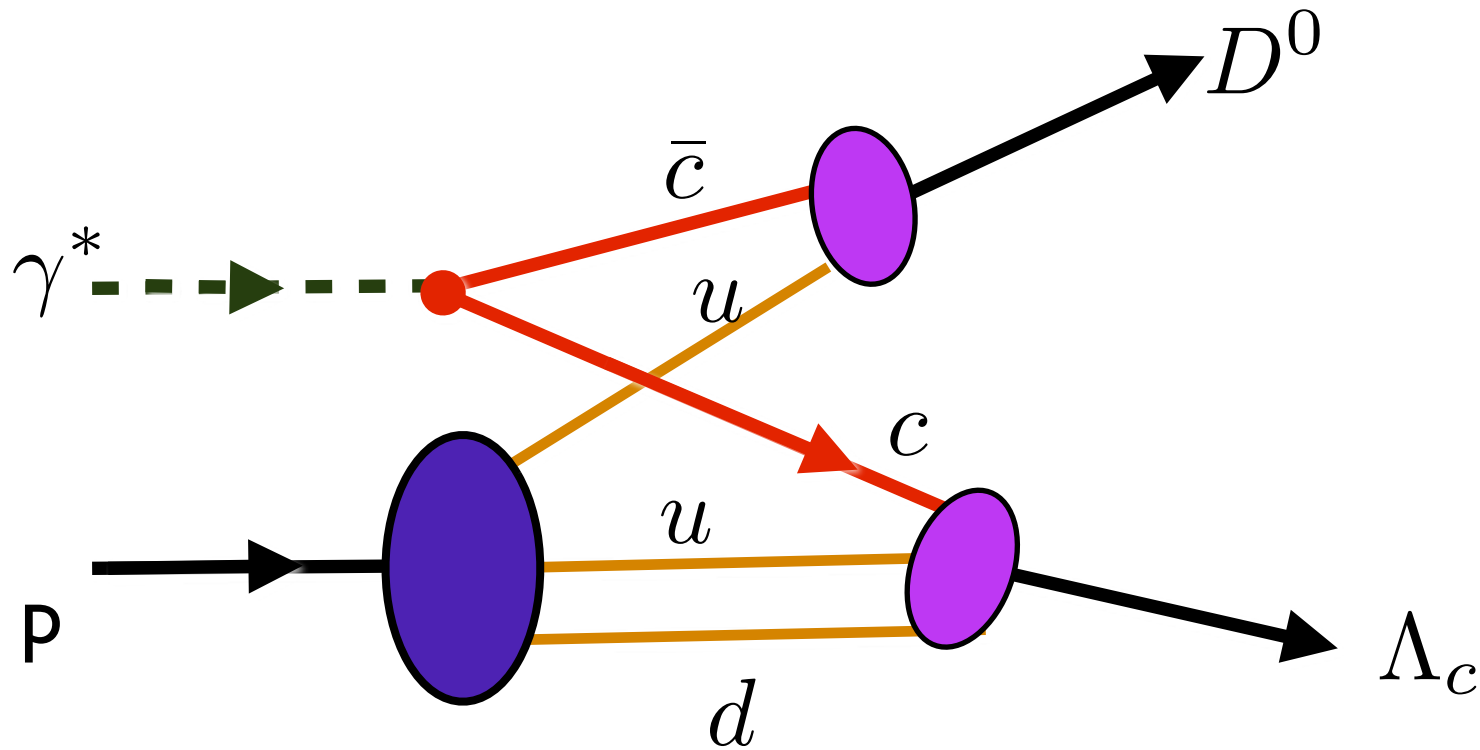
Need High  $x_F$  Acceptance

*Most practical: Higgs to 2 or 4 muons*

**Goldhaber, Kopeliovich,  
Schmidt, Soffer, sjb**

# Open Charm Production at Threshold!

## JLab 12 GeV: A Charm Factory!

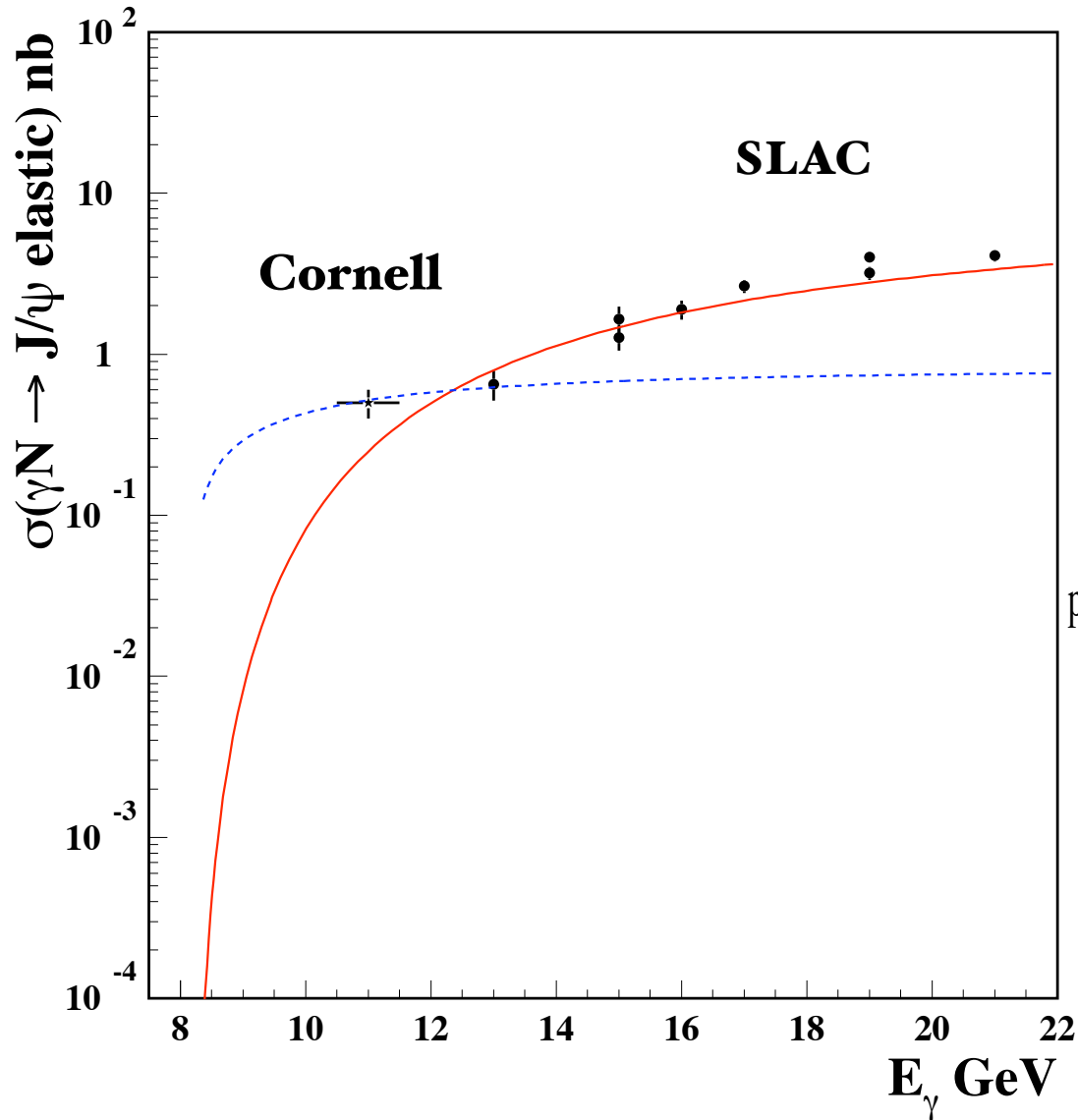


$$\gamma^* p \rightarrow \bar{D}^0 (\bar{c}u) \Lambda_c (cud)$$

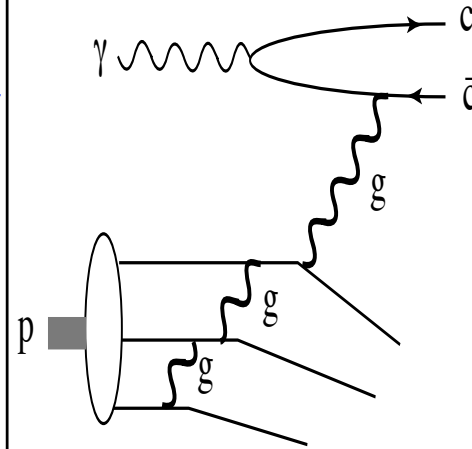
***c and u quark interchange***

$$\gamma p \rightarrow J/\psi p$$

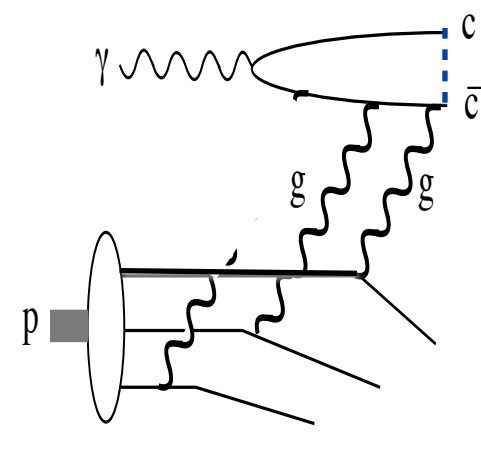
Chudakov, Hoyer, Laget, sjb



cross section: 1 nb



*Leading twist  
contribution*



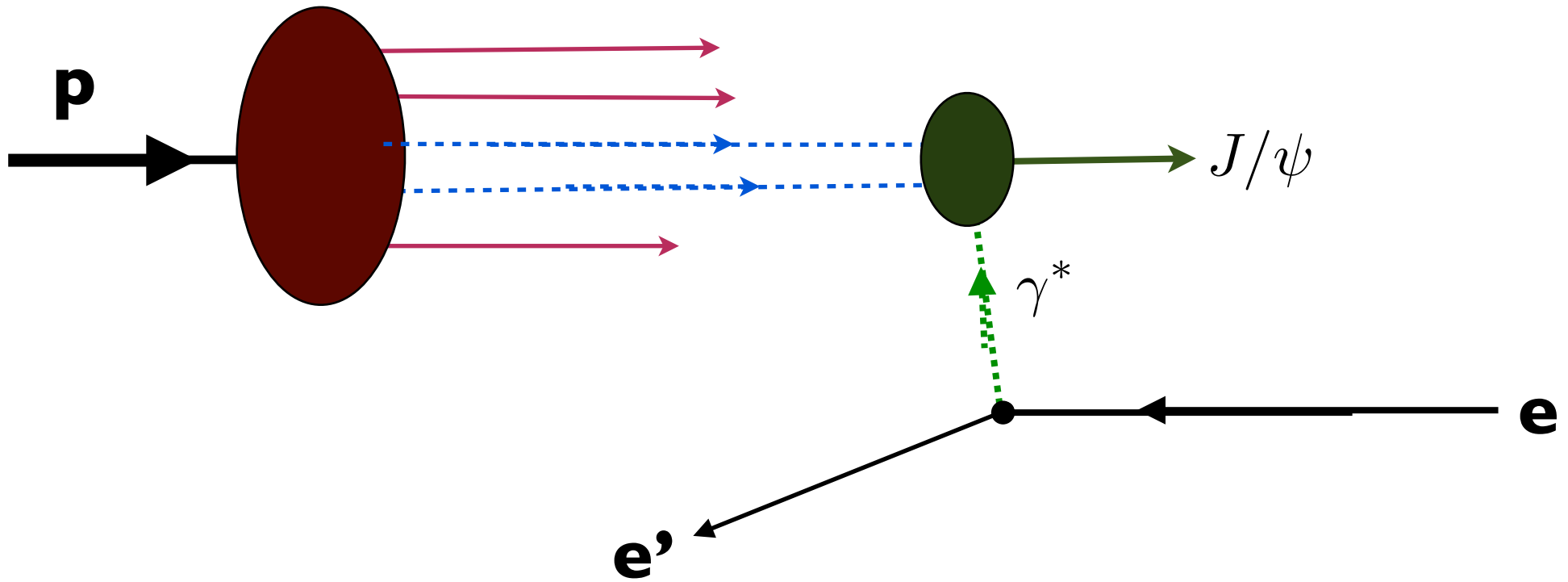
*Dominant near  
threshold*

**Phase space factor  $\beta$  cancelled by gluonic final-state interactions**

**Sommerfeld-Schwinger-Sakharov Effect**

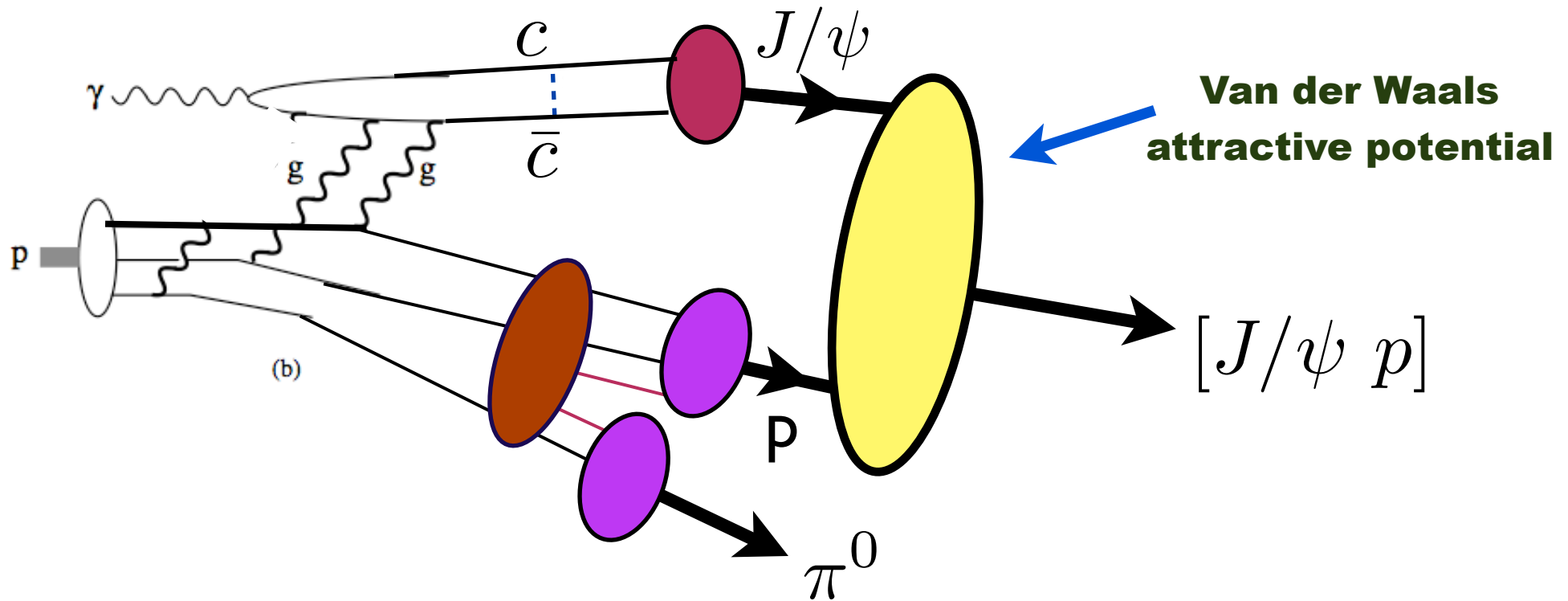
$$\gamma^* p \rightarrow J/\psi X$$

$$(gg)_{1C} + \gamma^* \rightarrow J/\psi$$



***Digluon-initiated subprocess  
in ep and  $\gamma p$  collisions***

# Charmonium Production at Threshold

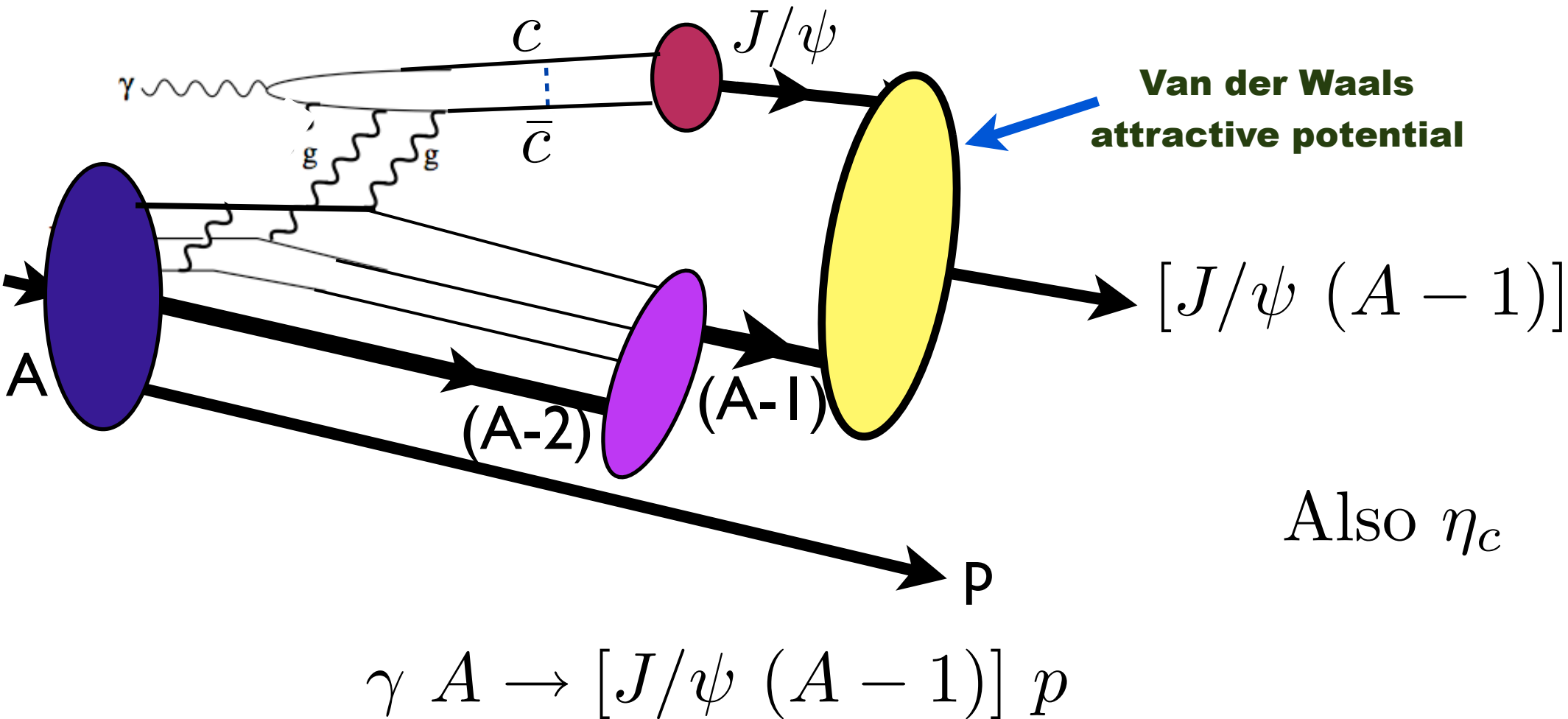


$$\gamma p \rightarrow [J/\psi p] \pi^0 \quad \gamma p \rightarrow [J/\psi n] \pi^+$$

Form proton-charmonium bound state!  $|uudc\bar{c}\rangle$



# Charmonium Production on Nuclei at Threshold



**Form “nuclear-bound” charmonium bound-states!**

# *JLab 12 GeV: An Exotic Charm Factory!*

$\gamma^* p \rightarrow J/\psi + p$  threshold  
at  $\sqrt{s} \simeq 4$  GeV,  $E_{\text{lab}}^{\gamma^*} \simeq 7.5$  GeV.

$\gamma^* p \rightarrow X(3872) + p'$   
 $|c\bar{c}q\bar{q}\rangle$  *tetraquark*

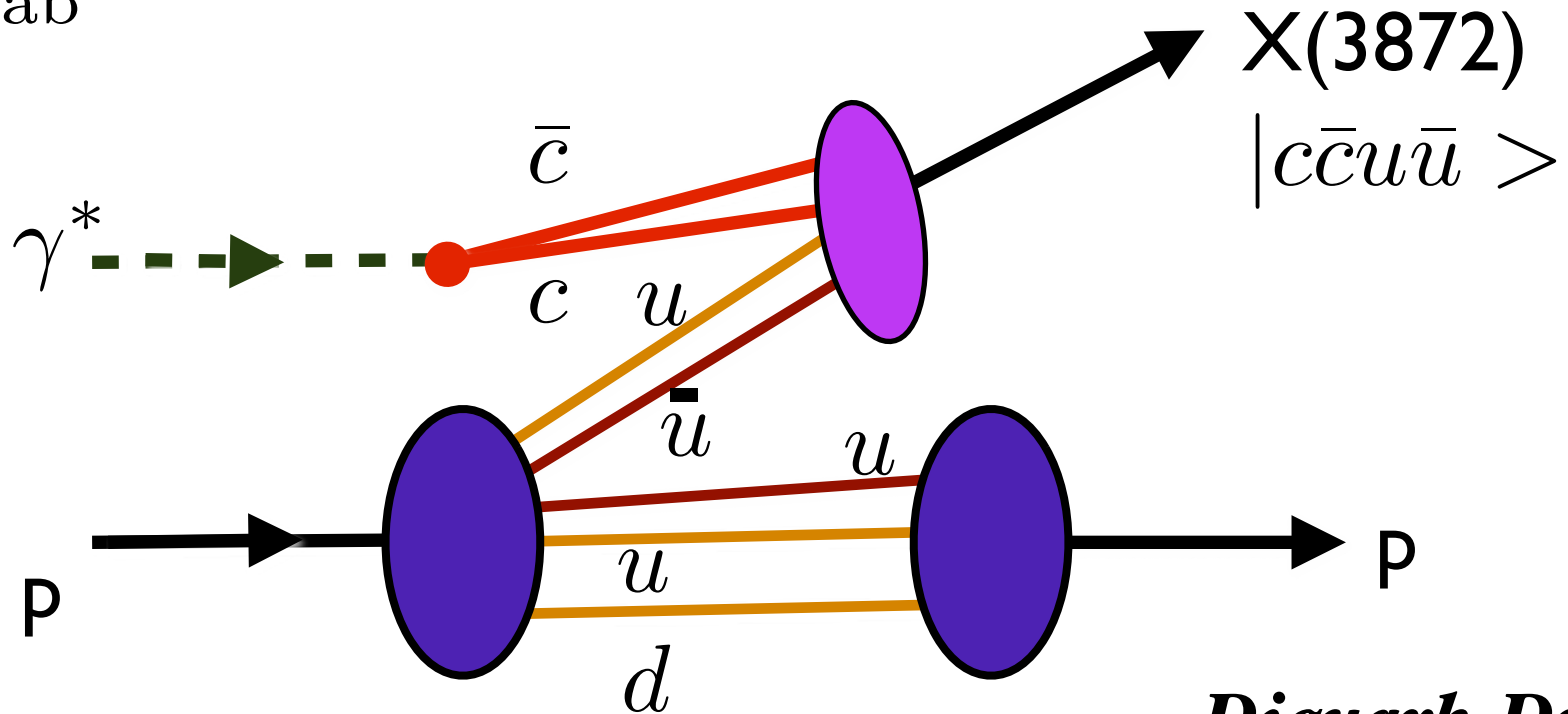
Produce  $[J/\psi + p]$  bound state  
 $|uudc\bar{c}\rangle$  *pentaquark*

$\gamma^* d \rightarrow J/\psi + d$  threshold  
at  $\sqrt{s} \simeq 5$  GeV,  $E_{\text{lab}}^{\gamma^*} \simeq 6$  GeV.

Produce  $[J/\psi + d]$  nuclear-bound quarkonium state  
 $|uudduc\bar{c}\rangle$  *octoquark!*

# Tetraquark Production at Threshold

$$E_{\text{lab}}^{\gamma} > 11.9 \text{ GeV}$$



***Diquark-Diquark  
vs Molecular State?***

$$\gamma^* p \rightarrow X(3872) + p'$$

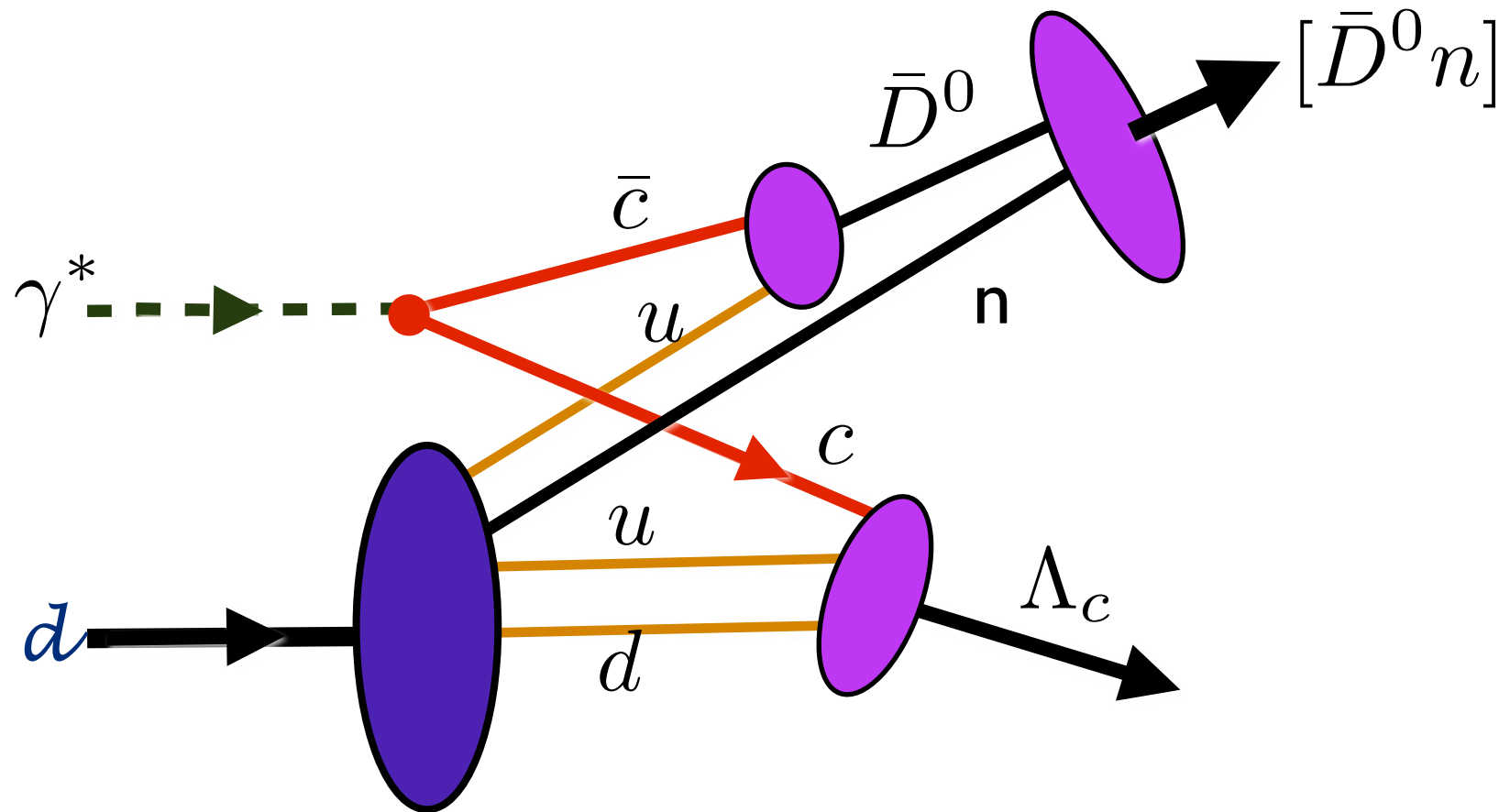
$$|c\bar{c}q\bar{q}\rangle$$

***New approach  
to hadronic decays***

**Dominance of  $\Psi'$  vs  $J/\Psi$  decays**

*Lebed, Hwang, sjb*

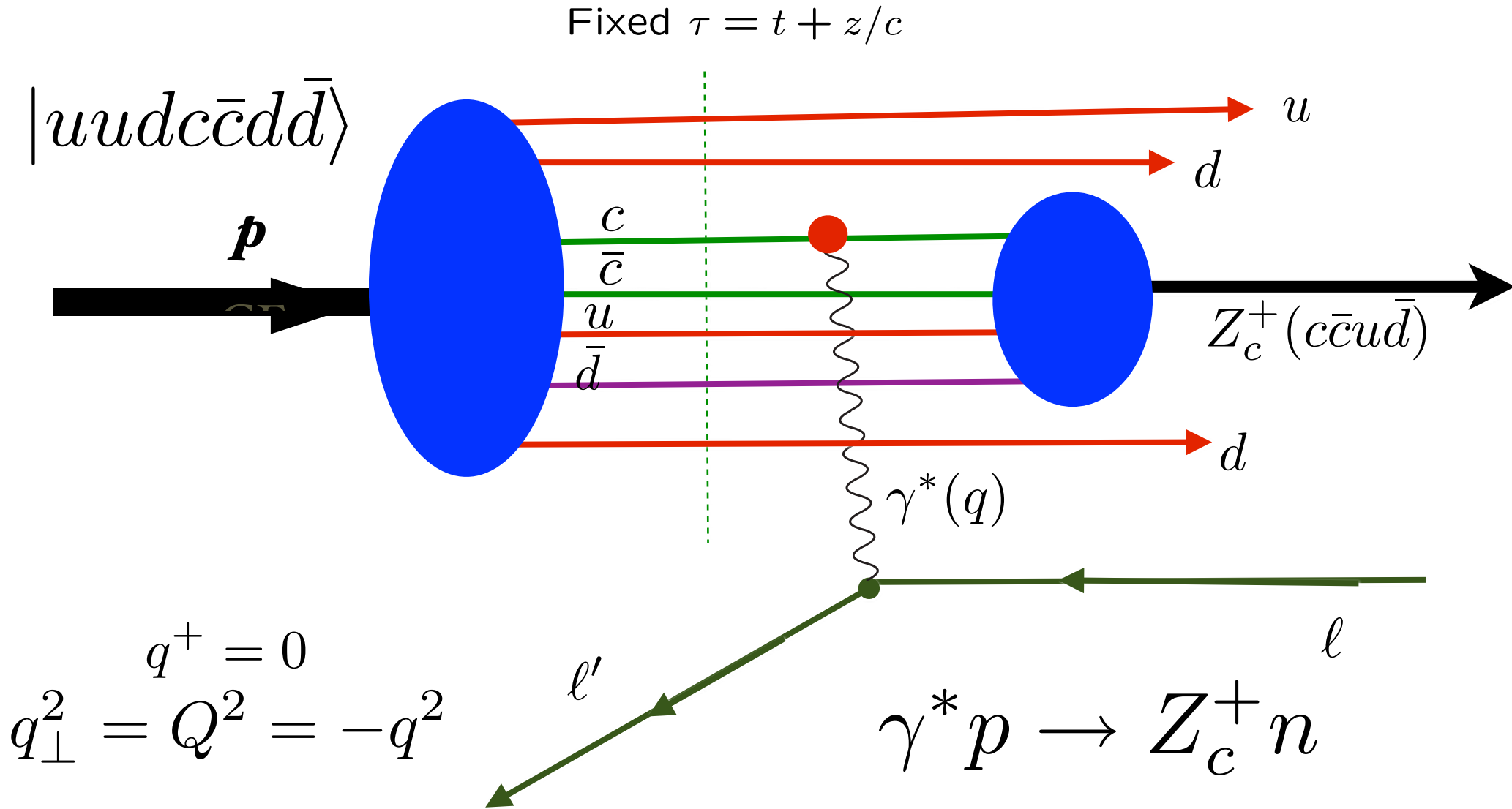
# Open Charm Production at Threshold



$$\gamma^* d \rightarrow \Lambda_c + [\bar{D}^0 (\bar{c}u)n] (\bar{c}uudd)$$

**Create pentaquark on deuteron at low relative velocity**

# Light-Front Wavefunctions and Heavy-Quark Electroproduction

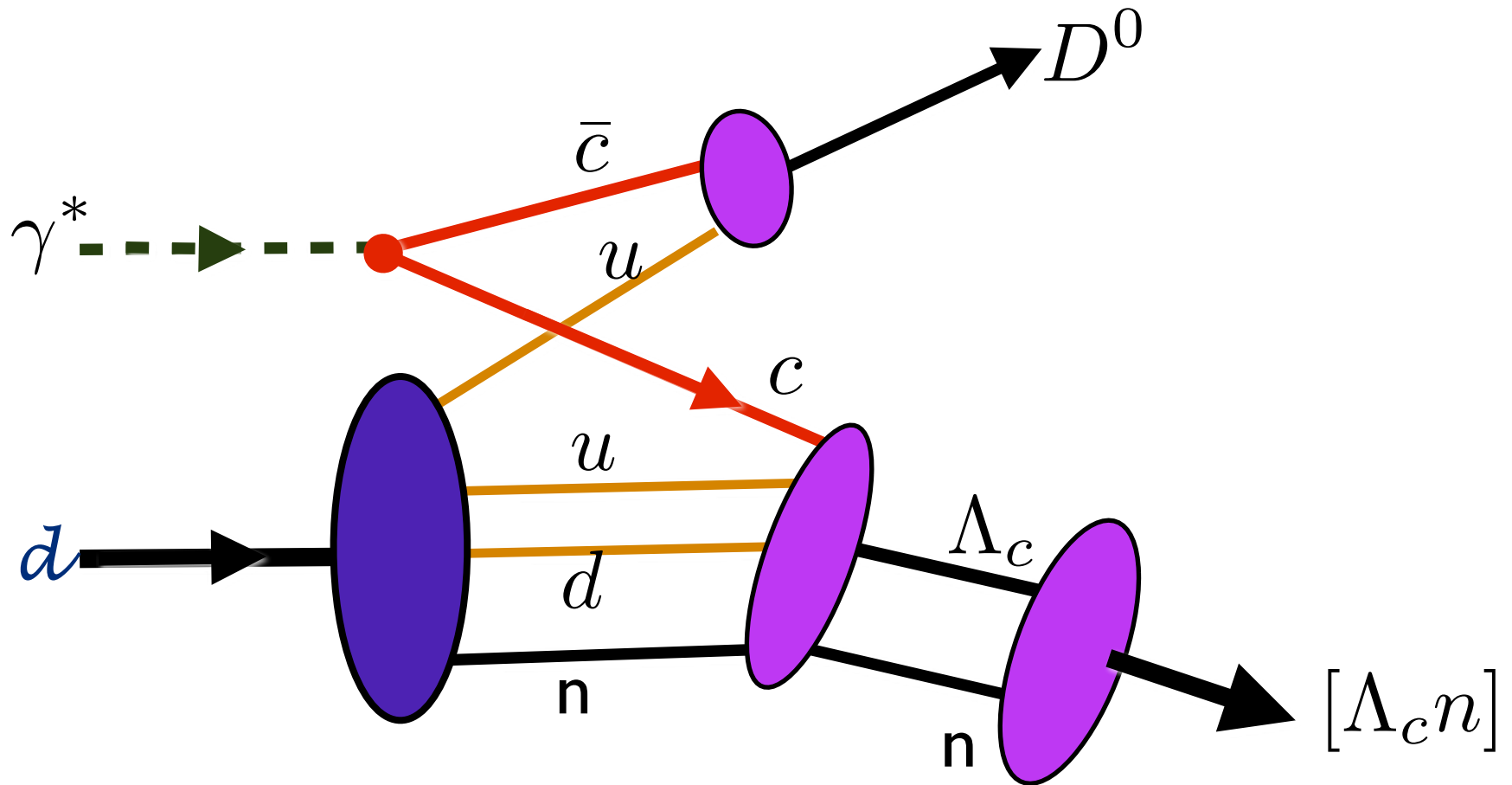


*Produce Charged Tetraquarks at JLab!*

Coalescence of comovers at threshold produces  
 $Z_c^+$  tetraquark resonance

# Open Charm Production at Threshold

***Nuclear binding at low relative velocity***



$$\gamma^* d \rightarrow \bar{D}^0 (\bar{c}u) [\Lambda_c n] (cududd)$$

***Possible charmed B= 2 nucleus***

# Produce Charge $Q=4, I=3, B=2$ Hidden-Color Dibaryon State at JLab

- First suggested by F. Dyson and N-H Xuong (1964)

*“Hexaquark”*

$$[B = 2, Q = +4] \leftrightarrow |u_R^\uparrow u_B^\uparrow u_Y^\uparrow u_R^\downarrow u_B^\downarrow u_Y^\downarrow \rangle$$

- Hidden-Color Six-Quark Configuration
- Decays to  $\Delta^{++}\Delta^{++}$

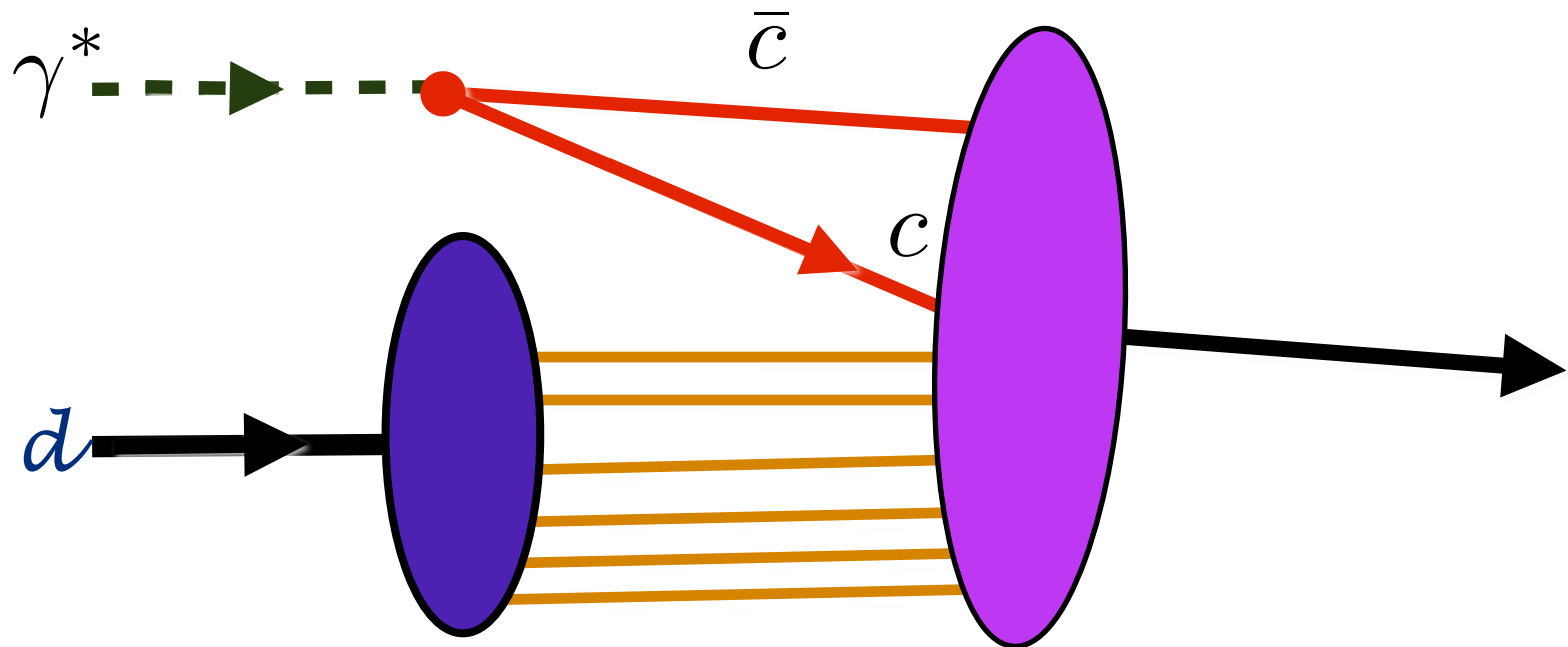
$$\gamma d \rightarrow [B = +2, Q = +4] \pi^- \pi^- \pi^-$$

Discover at JLab!

Bashkanov, Clement, sjb

# Octoquark Production at Threshold

$$M_{\text{octoquark}} \sim 5 \text{ GeV}$$



$$\gamma^* D \rightarrow |uud udc \bar{c} \rangle$$

*Explains Krüsch Effect!*

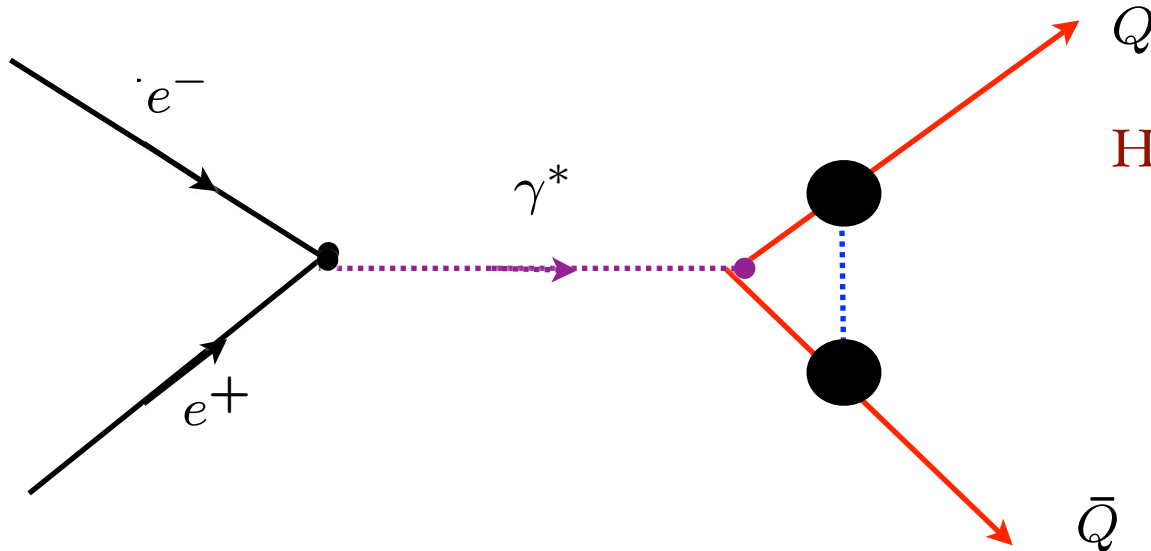


# *JLab 12 GeV: An Exotic Charm Factory!*

- **Charm quarks at high x -- allows charm states to be produced with minimal energy**
- **Charm produced at low velocities in the target -- the target rapidity domain  $x_F \sim -1$**
- **Charm at threshold -- maximal domain for producing exotic states containing charm quarks**
- **Attractive QCD Van der Waals interaction -- “nuclear-bound quarkonium”**  
**Miller, sjb; de Teramond, sjb**
- **Dramatic Spin Correlations in the threshold Domain  $\sigma_L$  vs.  $\sigma_T, A_{NN}$**
- **Strong SSS Threshold Enhancement**

# Charm at Threshold

- *Intrinsic charm Fock state puts 80% of the proton momentum into the electroproduction process*
- *1/velocity enhancement from FSI*
- *CLEO data for quarkonium production at threshold*
- *Krisch effect shows  $B=2$  resonance*
- *all particles produced at small relative rapidity-- resonance production*
- *Many exotic hidden and open charm resonances will be produced at JLab (12 GeV)*



Hoang, Kuhn, Teubner, sjb

$$F_1 + F_2 = \left[ 1 - 2 \frac{\alpha_s(s e^{3/4}/4)}{\pi} \right] \times \left[ 1 + \frac{\pi \alpha_s(s v^2)}{4v} \right]$$

Angular distributions of massive quarks close to threshold.

*Example of Multiple BLM/PMC Scales*

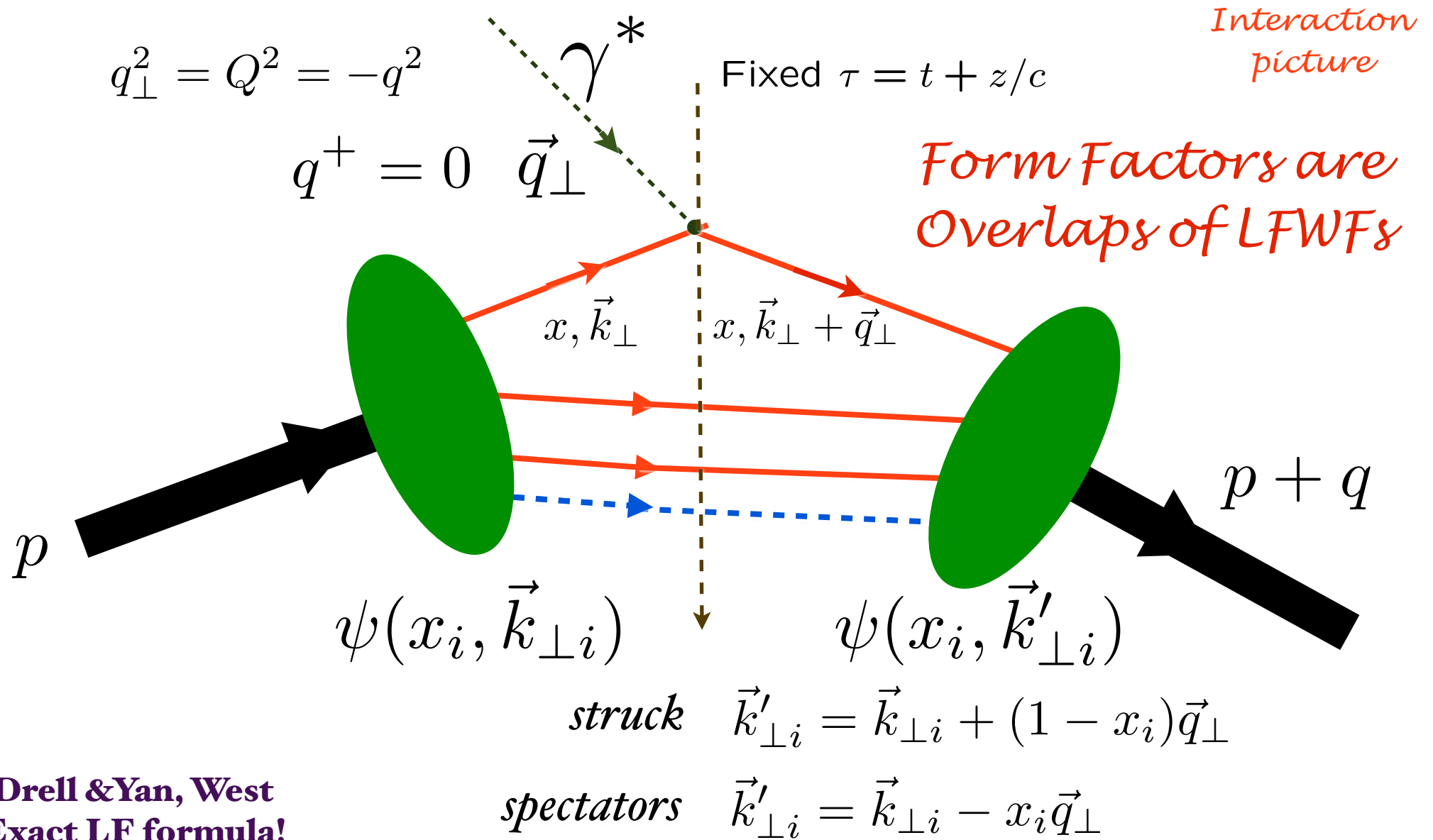
**QCD coupling at small scales at low relative velocity  $v$**

# *Properties of Hard Exclusive Reactions*

- **Dimensional Counting Rules at fixed CM angle**
- **Hadron Helicity Conservation**
- **Color Transparency**
- **Hidden color**
- **$s \gg -t \gg \Lambda_{\text{QCD}}$ : Reggeons have negative-integer intercepts at large  $-t$**
- **$J=0$  Fixed pole in DVCS**
- **Quark interchange — no gluon exchange evident**
- **Renormalization group invariance**
- **No renormalization scale ambiguity**
- **Exclusive inclusive connection with spectator counting rules**
- **Diffraction reactions from pomeron, Reggeon, odderon**

$$\langle p + q | j^+(0) | p \rangle = 2p^+ F(q^2)$$

Front Form



**Drell & Yan, West**  
**Exact LF formula!**

Drell, sjb

*Lepton sees quarks at same LF time  $\tau$*

# Exact LF Formula for Pauli Form Factor

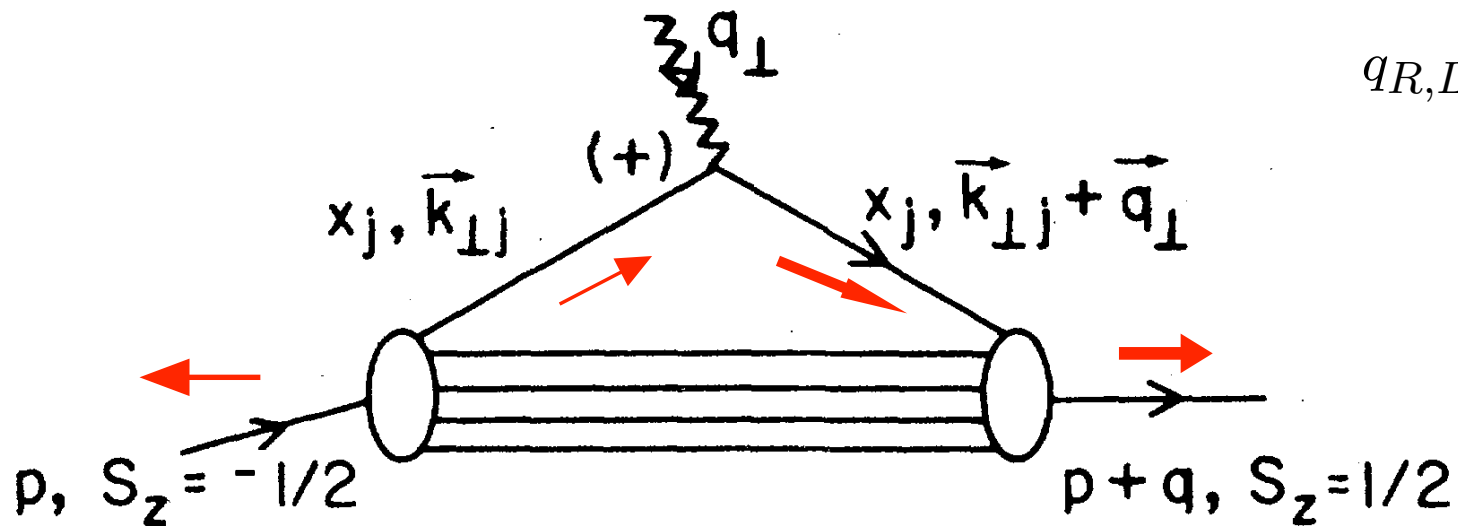
$$\frac{F_2(q^2)}{2M} = \sum_a \int [dx] [d^2 \mathbf{k}_\perp] \sum_j e_j \frac{1}{2} \times$$

Drell, sjb

$$\left[ -\frac{1}{q^L} \psi_a^{\uparrow*}(x_i, \mathbf{k}'_{\perp i}, \lambda_i) \psi_a^{\downarrow}(x_i, \mathbf{k}_{\perp i}, \lambda_i) + \frac{1}{q^R} \psi_a^{\downarrow*}(x_i, \mathbf{k}'_{\perp i}, \lambda_i) \psi_a^{\uparrow}(x_i, \mathbf{k}_{\perp i}, \lambda_i) \right]$$

$$\mathbf{k}'_{\perp i} = \mathbf{k}_{\perp i} - x_i \mathbf{q}_\perp$$

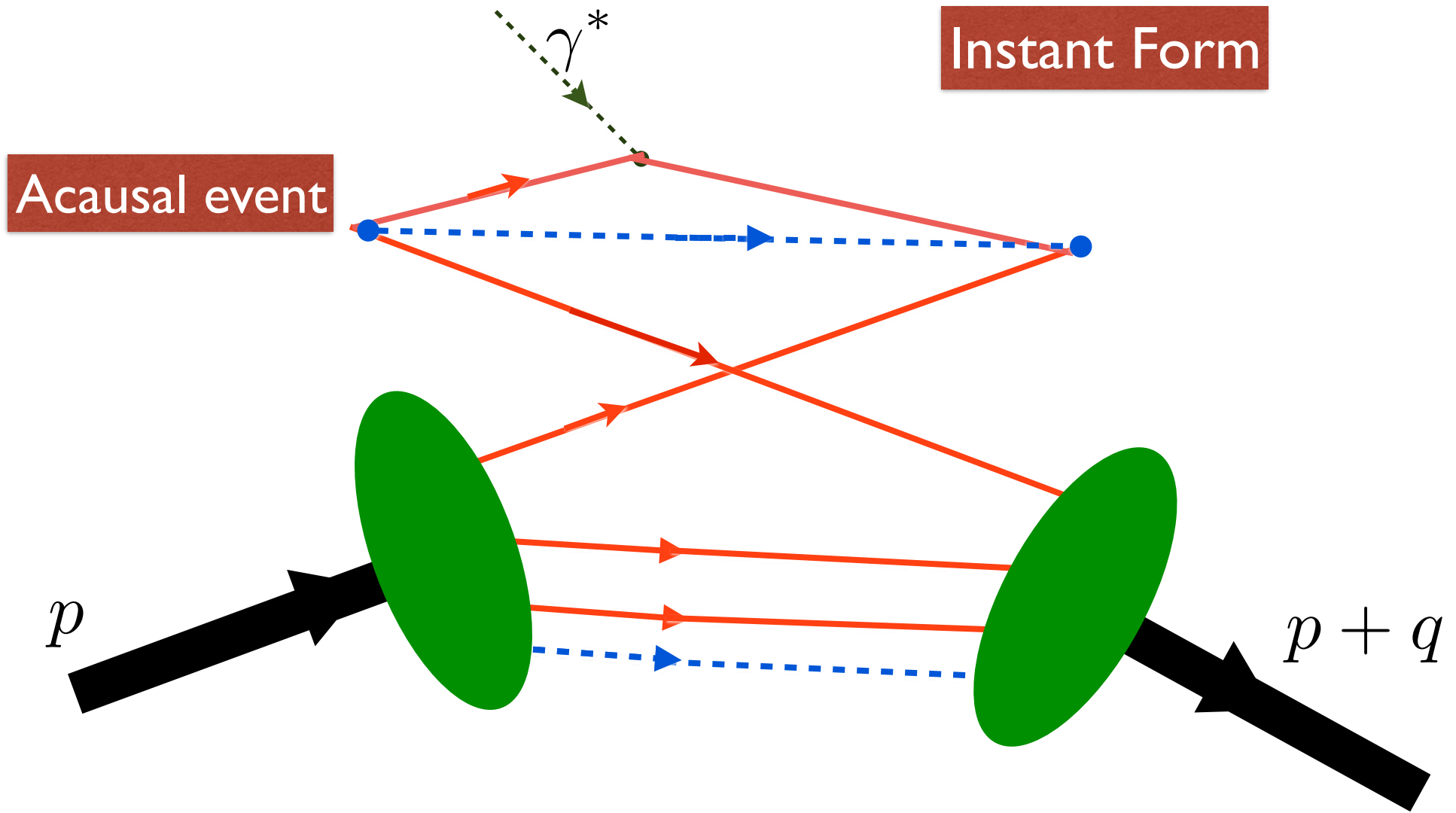
$$\mathbf{k}'_{\perp j} = \mathbf{k}_{\perp j} + (1 - x_j) \mathbf{q}_\perp$$



$$q_{R,L} = q^x \pm i q^y$$

Must have  $\Delta \ell_z = \pm 1$  to have nonzero  $F_2(q^2)$

Nonzero Proton Anomalous Moment -->  
Nonzero orbital quark angular momentum

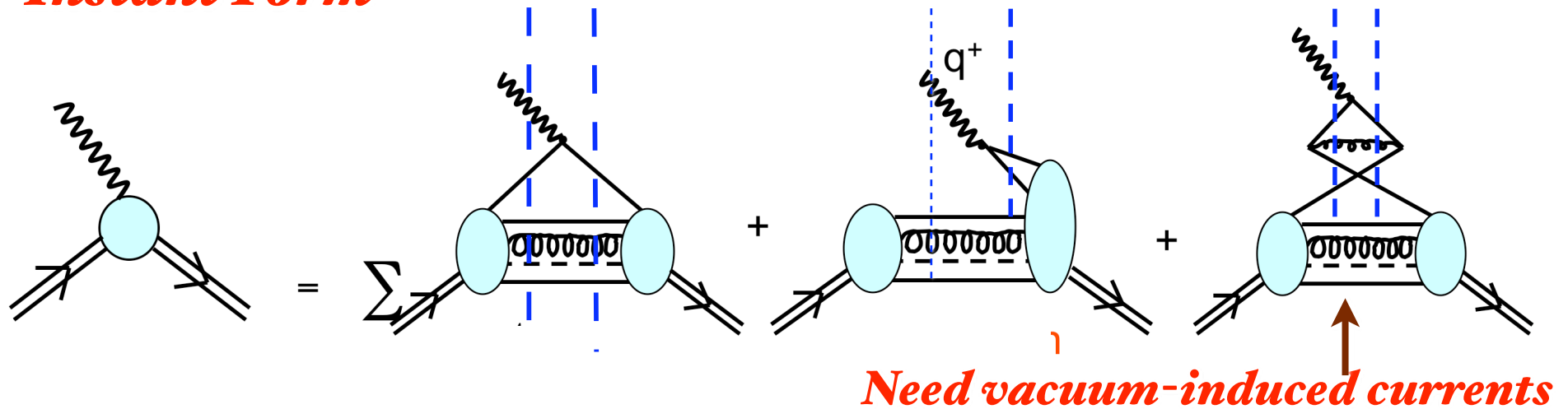


*Must include vacuum-induced currents to compute form factors and other current matrix elements in instant form*

*Boost are dynamical in instant form*

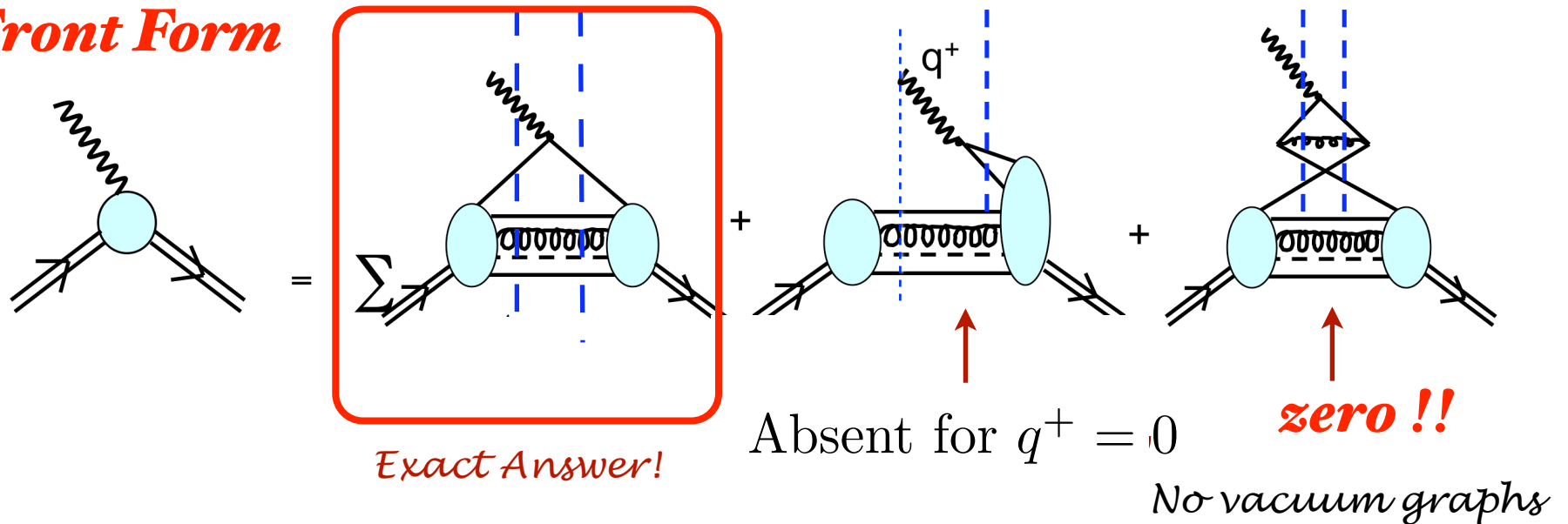
## Calculation of Form Factors in Equal-Time Theory

### Instant Form



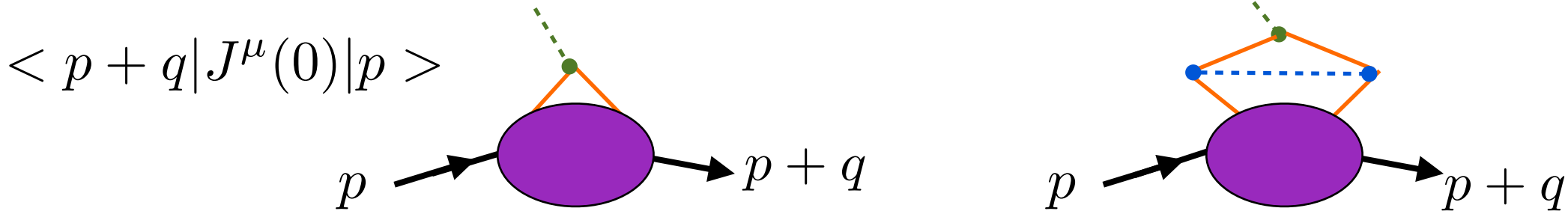
## Calculation of Form Factors in Light-Front Theory

### Front Form

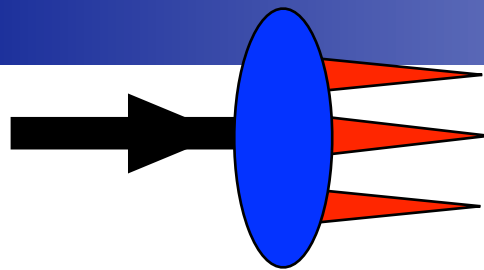




# Calculation of proton form factor in Instant Form



- **Need to boost proton wavefunction from  $p$  to  $p+q$ : Extremely complicated dynamical problem; even the particle number changes**
- **Need to couple to all currents arising from vacuum!! Remains even after normal-ordering**
- **Each time-ordered contribution is frame-dependent**
- **Divide by disconnected vacuum diagrams**
- **Instant form: Violates causality**



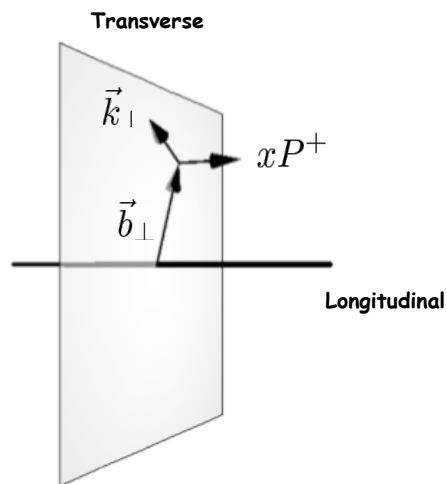
$$\Psi_n(x_i, \vec{k}_{\perp i}, \lambda_i)$$

• *Light Front Wavefunctions:*

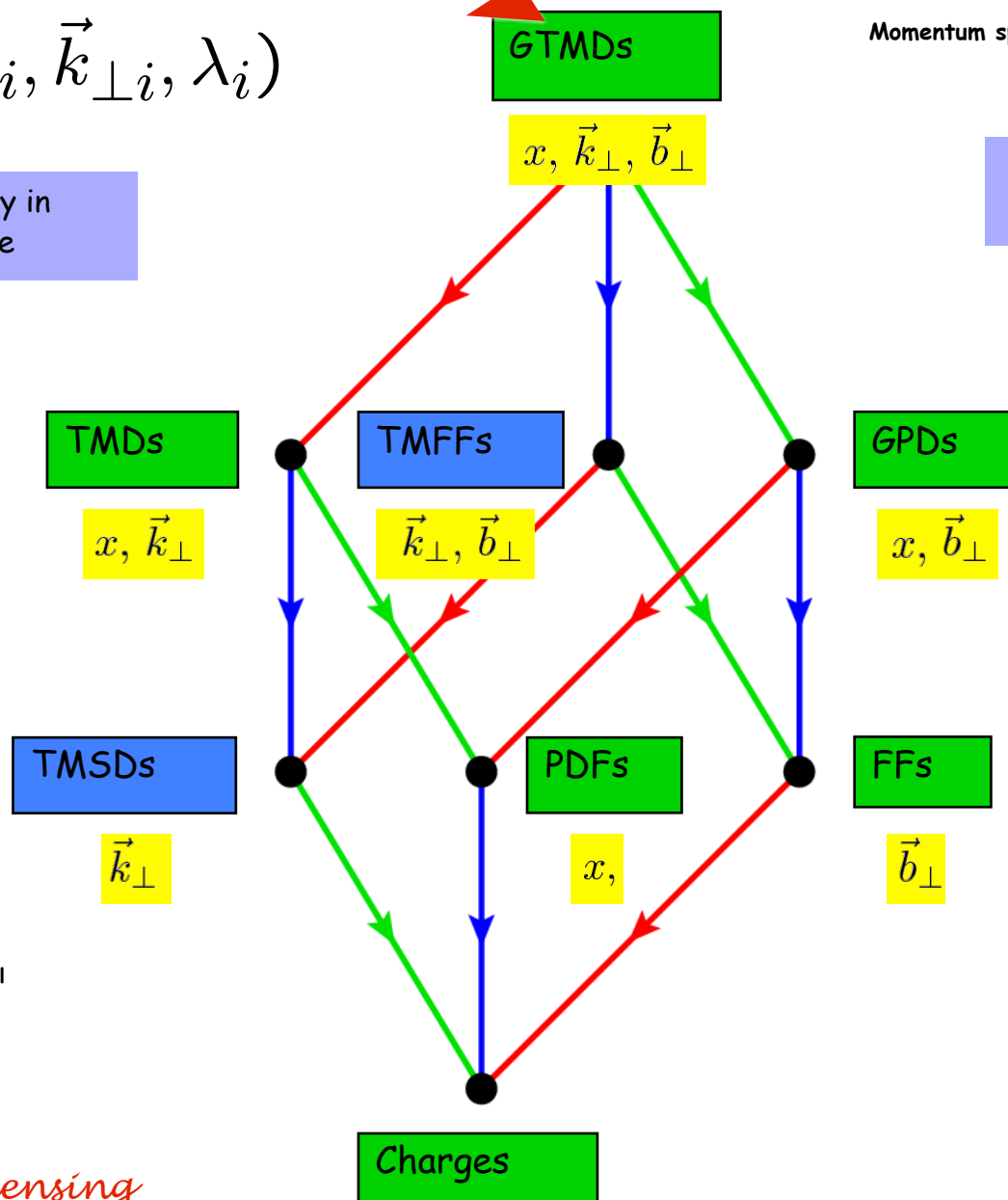
Momentum space  $\vec{k}_{\perp} \leftrightarrow \vec{z}_{\perp}$  Position space  
 $\vec{\Delta}_{\perp} \leftrightarrow \vec{b}_{\perp}$

Transverse density in momentum space

Transverse density in position space



*Sivers, T-odd from lensing*



*Lorce,  
Pasquini*

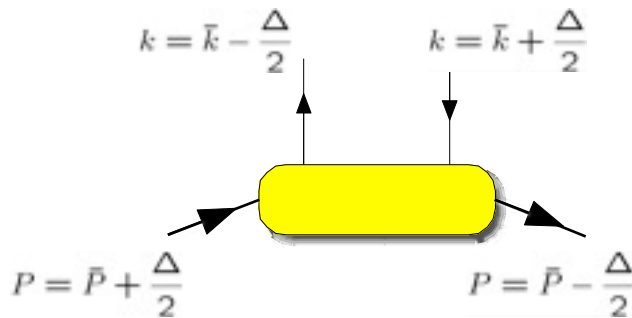
→  $\int d^2 b_{\perp}$   
→  $\int dx$   
→  $\int d^2 k_{\perp}$

# Light-Front Wave Function Overlap Representation

## DVCS/GPD

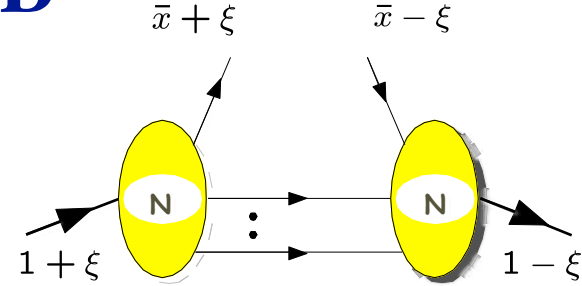
Diehl, Hwang, sjb, NPB596, 2001

See also: Diehl, Feldmann, Jakob, Kroll



$\xi < \bar{x} < 1$

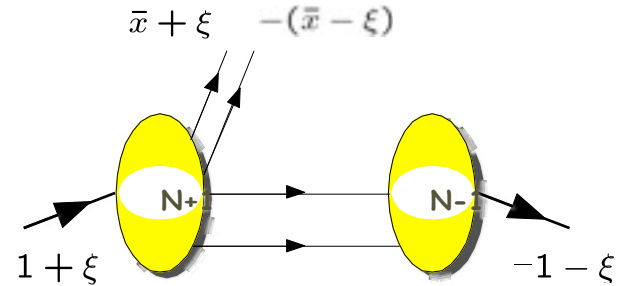
$\sum_N$



**DGLAP**  
*region*

$-\xi < \bar{x} < \xi$

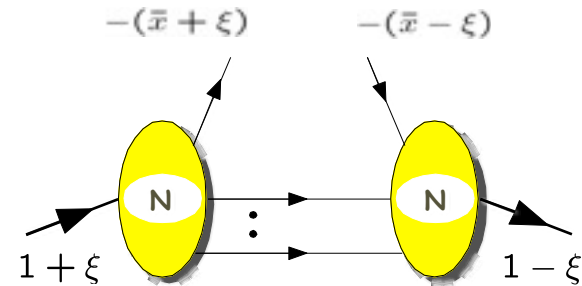
$\sum_N$



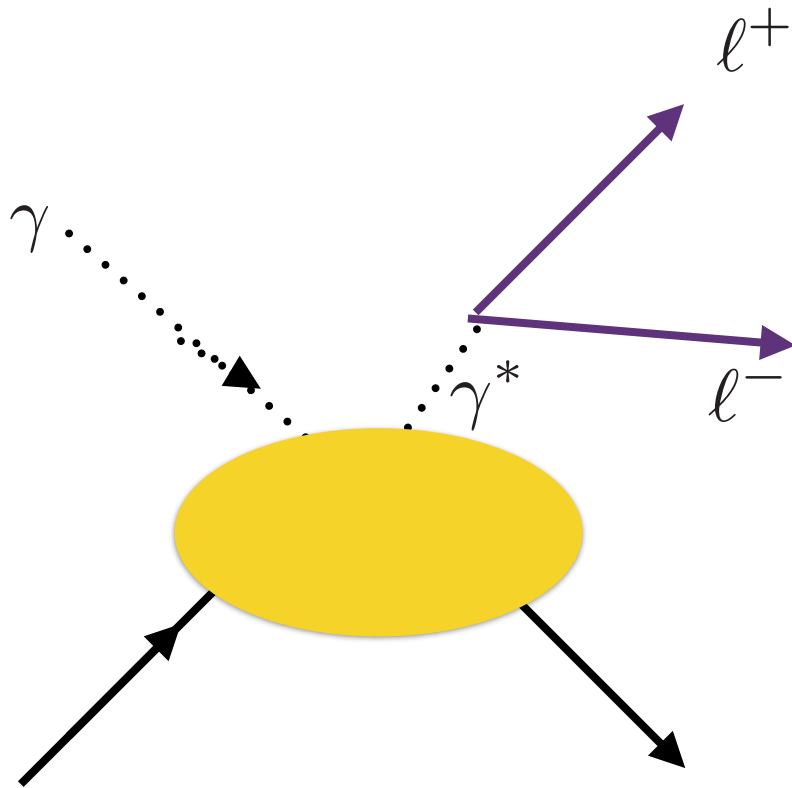
**ERBL**  
*region*

$-1 < \bar{x} < -\xi$

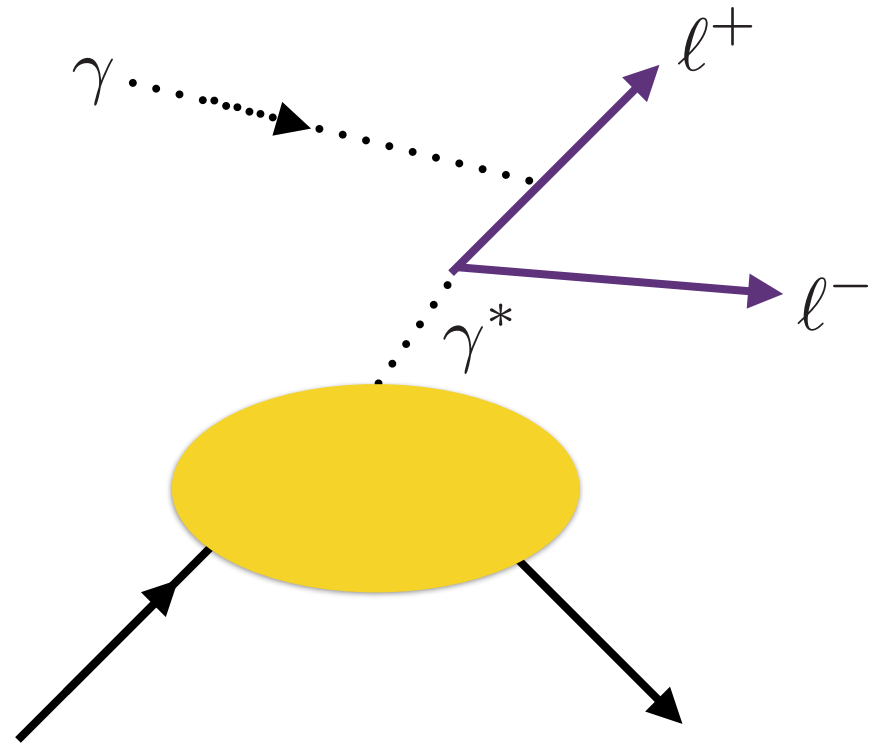
$\sum_N$



**DGLAP**  
*region*



**Virtual Compton**



**Bethe-Heitler**

Interference produces  $\ell^+$  vs.  $\ell^-$  asymmetry

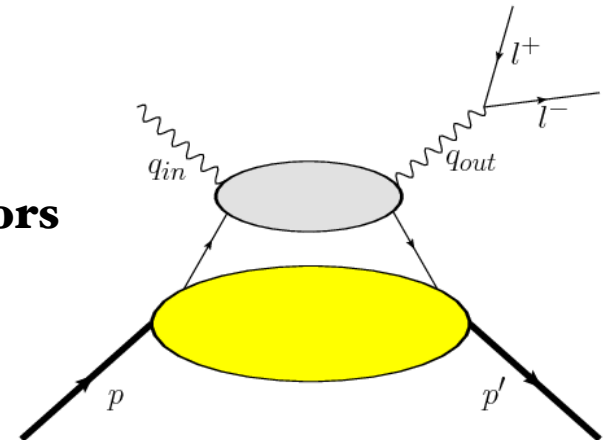
Close, Gunion, sjb

*Measures Real Part of Compton Amplitude*

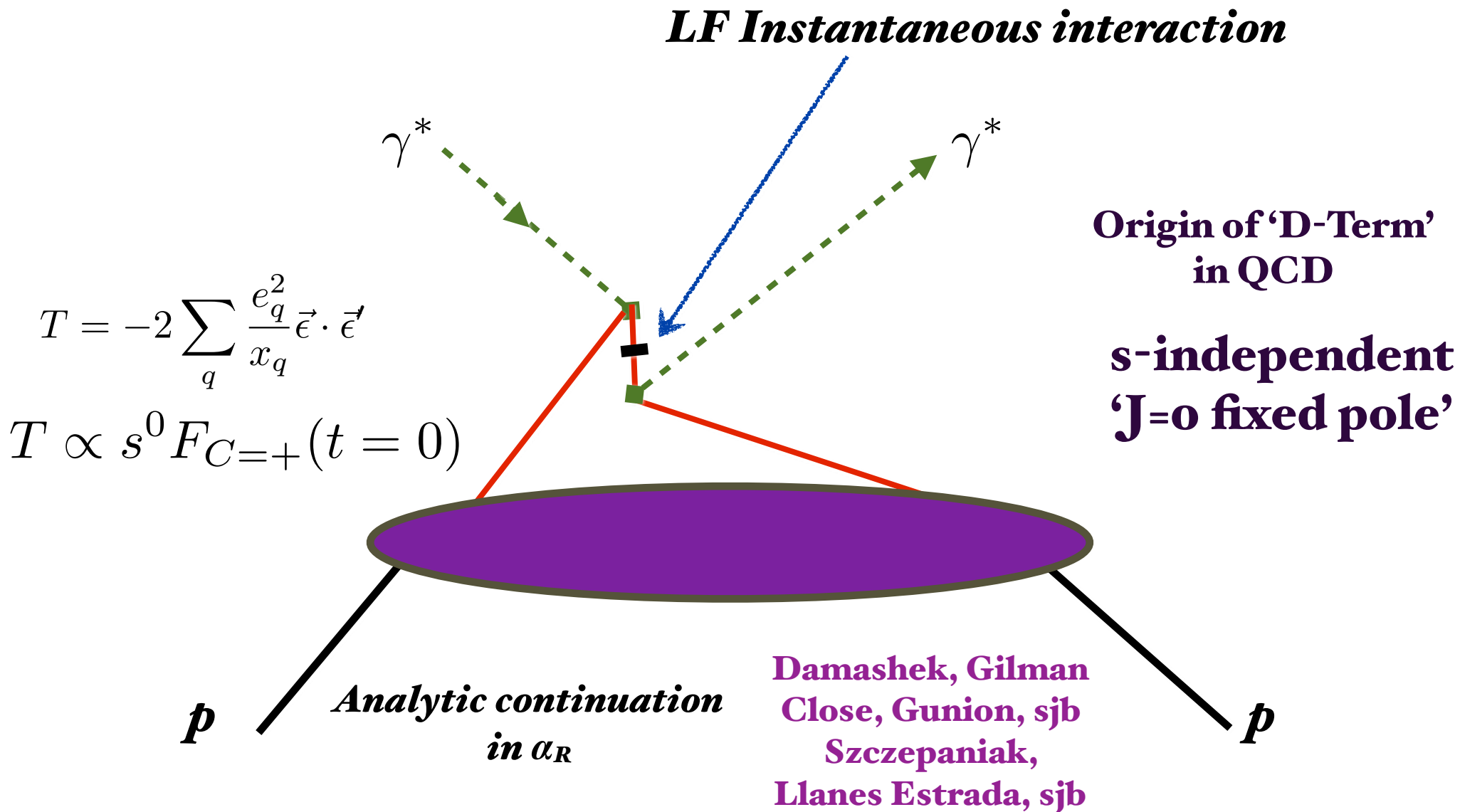
- **Timelike virtual photon couples to product of timelike VM poles**

# ***“Handbag” Approximation***

- **Parton model: assume current-current correlator carried by single quark propagator at high photon virtuality**
- **Imaginary Part of Virtual Forward Compton Amplitude gives DIS structure Functions**
- **Leading-Twist Dominance — Motivated by the Operator Product Expansion**
- **Predicts Momentum and Baryon Number Sum Rules**
- **Real Part:  $J=0$  Fixed Pole from local two-photon operators**
- **Regge Behavior of Compton Amplitude**
- **Timelike virtual photon couples to product of timelike VM poles**
- **High  $t, s$ : Counting rules, hadron helicity conservation, ERBL evolution; quark interchange; distribution amplitudes, color transparency ...**

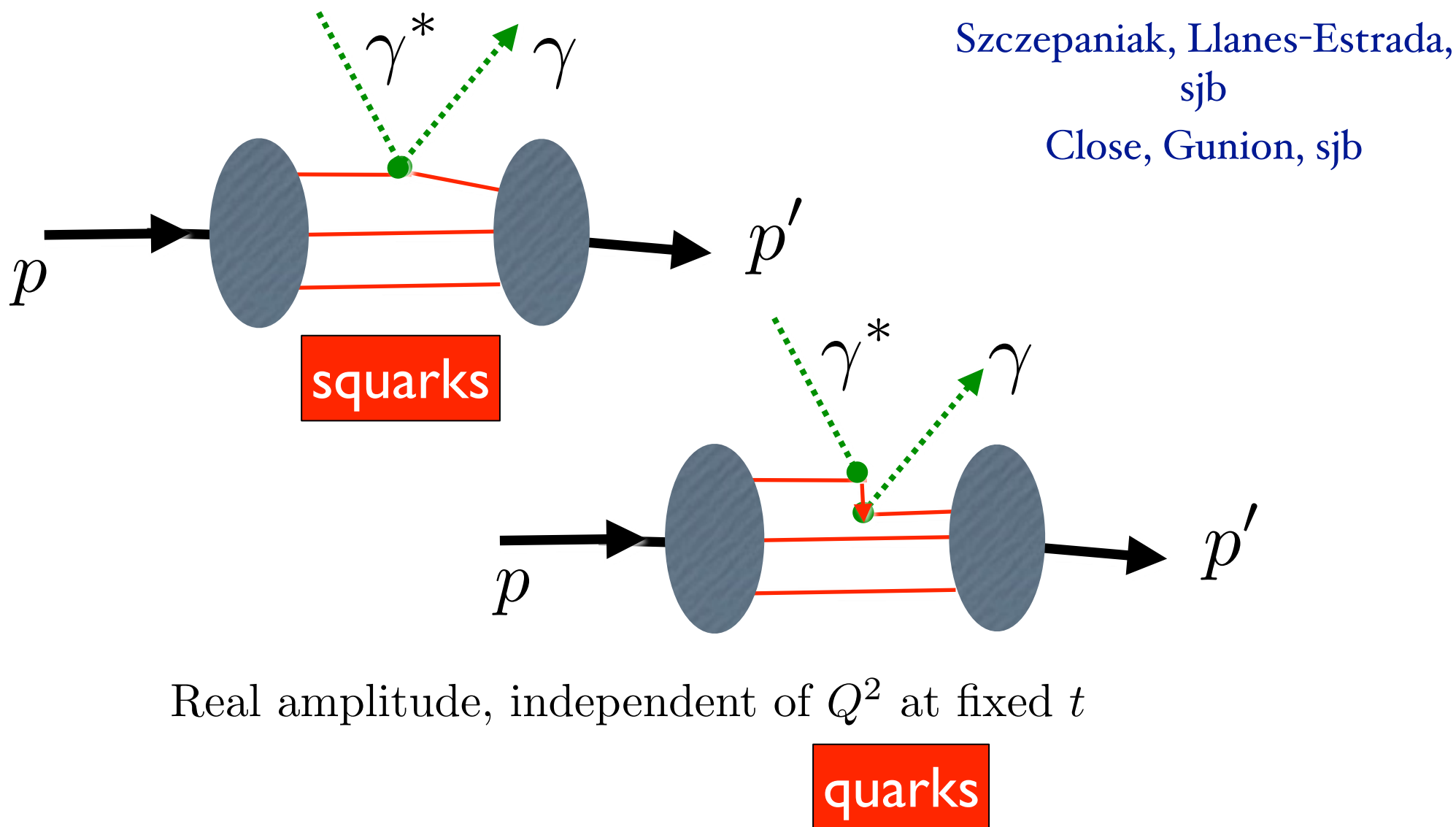


# Leading-Twist Contribution to Real Part of DVCS



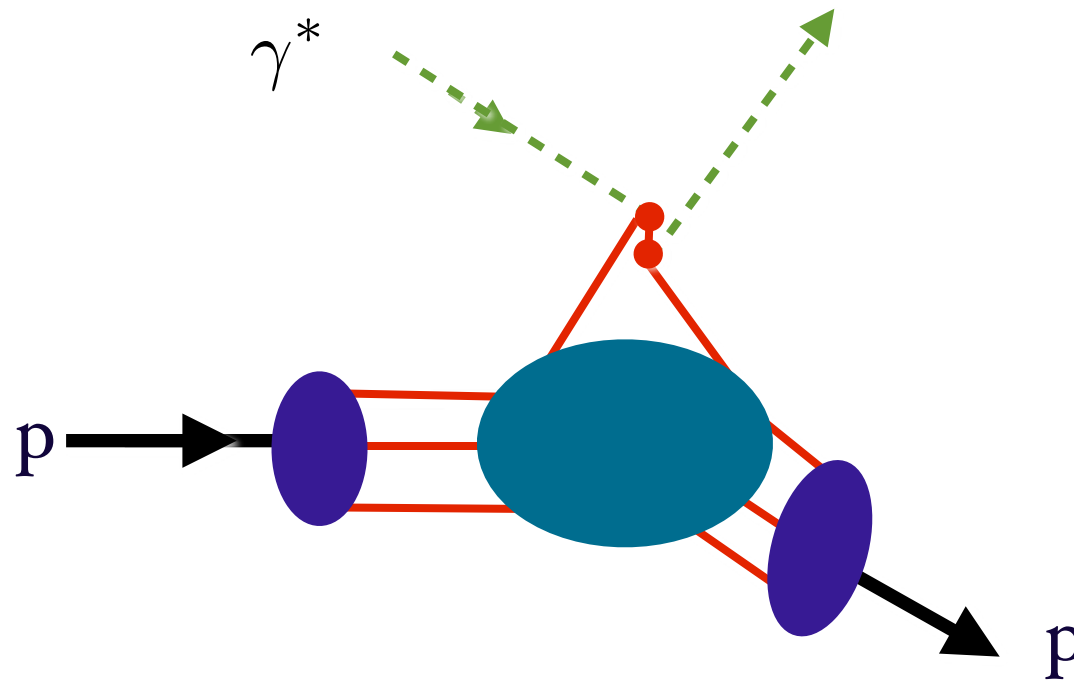
# $J=0$ Fixed Pole Contribution to DVCS

- $J=0$  fixed pole -- direct test of QCD locality -- from seagull or instantaneous contribution to Feynman propagator



# Deeply Virtual Compton Scattering

$$\gamma^* p \rightarrow \gamma p$$



*Seagull interaction  
(instantaneous quark  
exchange or Z-graph)*

$$s \gg -t, Q^2 \gg \Lambda_{QCD}^2$$

*Hard Reggeon  
Domain*

$$T(\gamma^*(q)p \rightarrow \gamma(k) + p) \sim \epsilon \cdot \epsilon' \sum_R s_R^\alpha(t) \beta_R(t)$$

$$\alpha_R(t) \rightarrow 0$$

*Reflects elementary coupling of two photons to quarks*

$$\beta_R(t) \sim \frac{1}{t^2}$$

$$\frac{d\sigma}{dt} \sim \frac{1}{s^2} \frac{1}{t^4} \sim \frac{1}{s^6} \text{ at fixed } \frac{Q^2}{s}, \frac{t}{s}$$



# *J=0 Fixed pole in real and virtual Compton scattering*

Damashek, Gilman;  
Close, Gunion, sjb  
Llanes-Estrada,  
Szczepaniak, sjb

Effective two-photon contact term

Seagull for scalar quarks

Real phase

$$M = s^0 \sum e_q^2 F_q(t)$$

Independent of  $Q^2$  at fixed  $t$

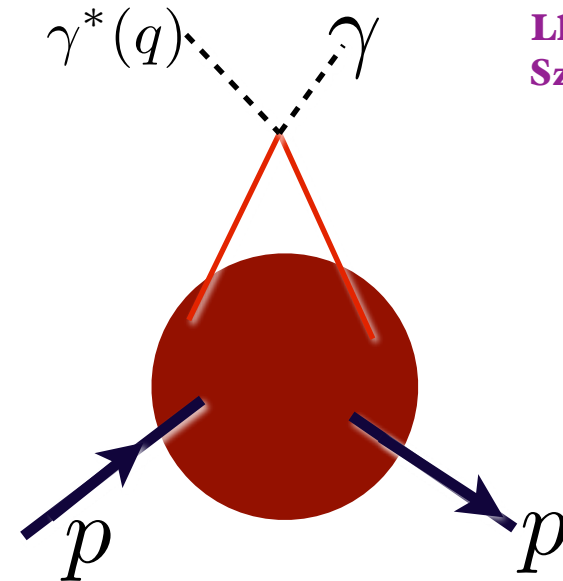
$\langle 1/x \rangle$  Moment: Related to Feynman-Hellman Theorem

Fundamental test of local gauge theory

$Q^2$ -independent contribution to Real DVCS amplitude

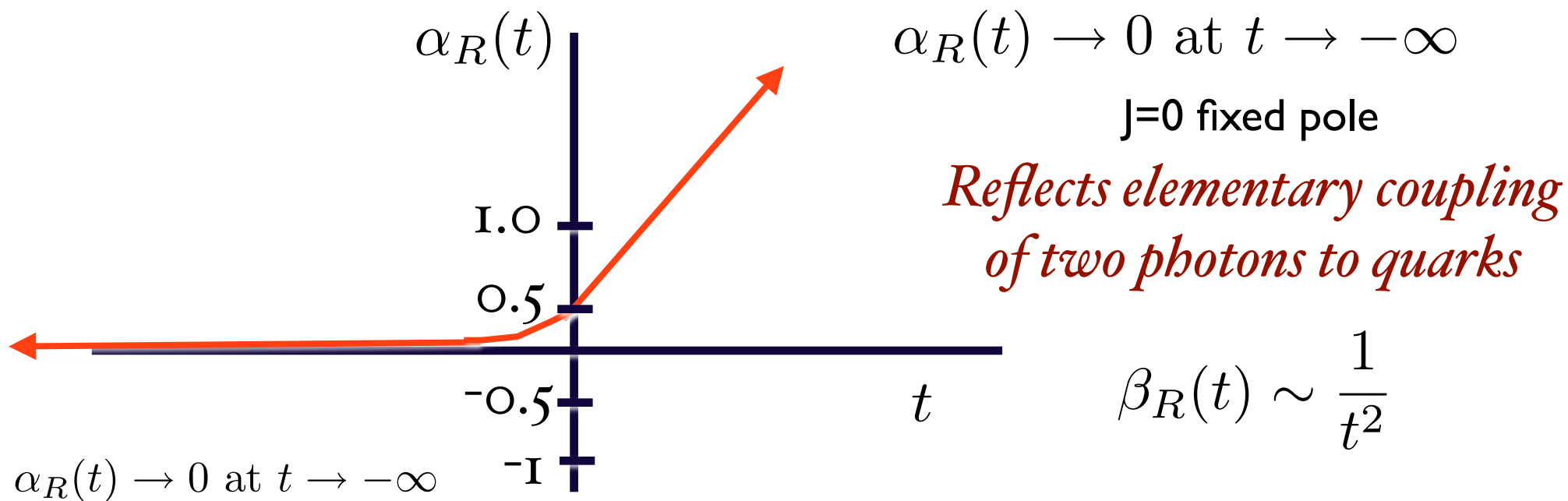
$$s^2 \frac{d\sigma}{dt}(\gamma^* p \rightarrow \gamma p) = F^2(t)$$

*independent of  $s$*



# Regge domain

$$T(\gamma^* p \rightarrow \pi^+ n) \sim \epsilon \cdot p_i \sum_R s_R^\alpha(t) \beta_R(t) \quad s \gg -t, Q^2$$

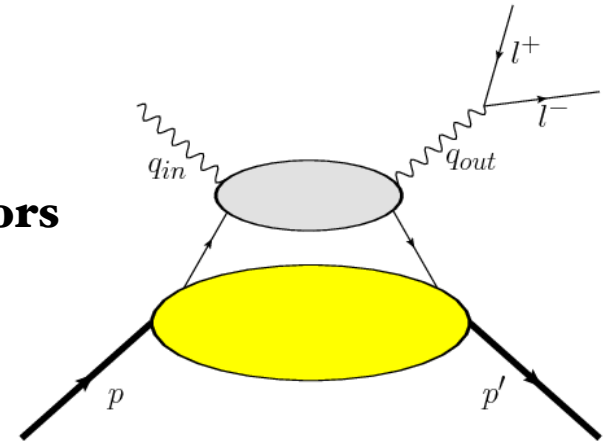


$$\frac{d\sigma}{dt}(\gamma^* p \rightarrow \gamma p) \rightarrow \frac{1}{s^2} \beta_R^2(t) \sim \frac{1}{s^2 t^4} \sim \frac{1}{s^6} \text{ at fixed } \frac{t}{s}, \frac{Q^2}{s}$$

*Fundamental test of QCD*

# ***“Handbag” Approximation***

- **Parton model: assume current-current correlator carried by single quark propagator at high photon virtuality**
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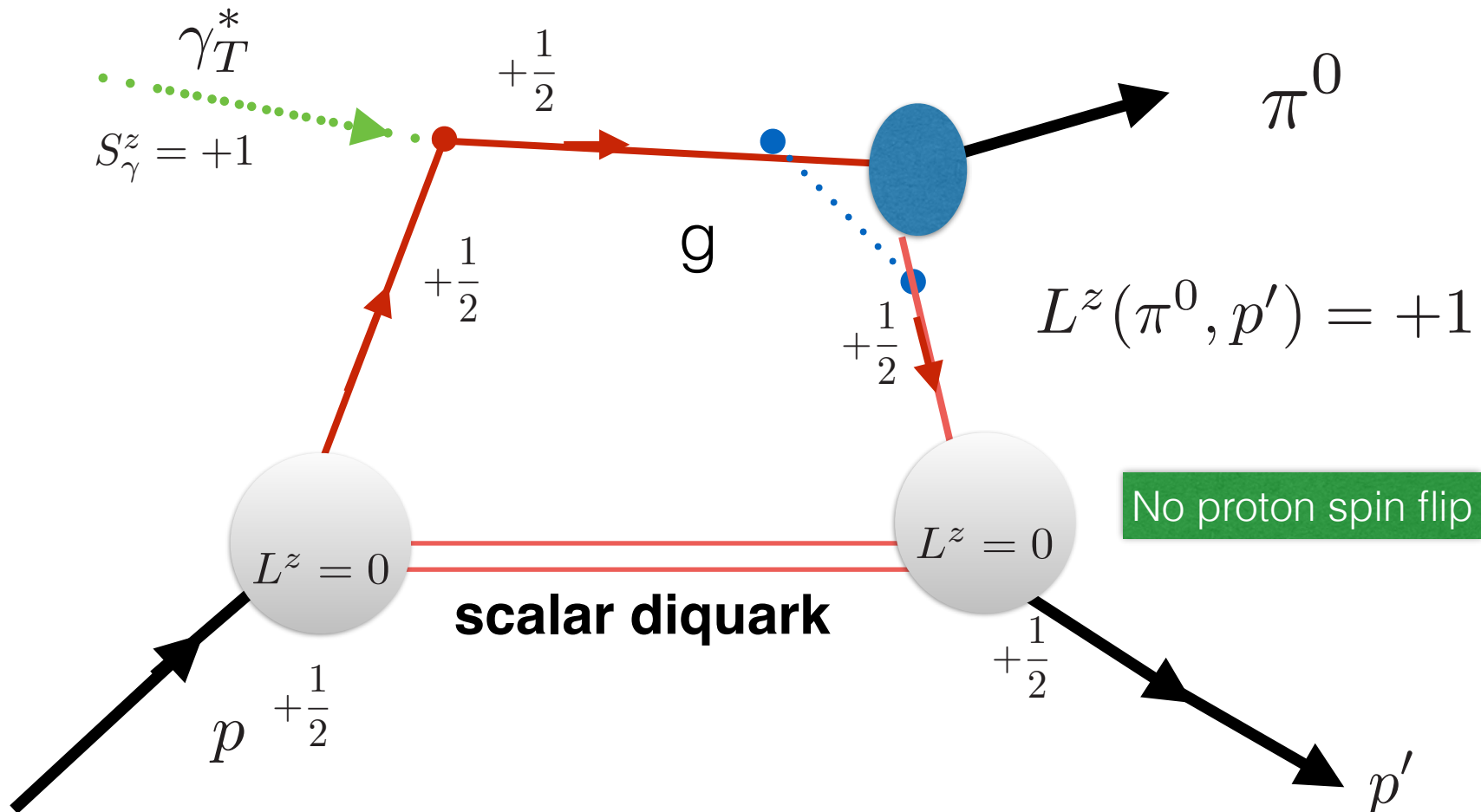


$$\gamma^* p \rightarrow \pi^0 p'$$

No quark chiral flip

*Uses dominant twist-2 pion distribution amplitude*

Vanishes at  $t = 0$  because of  $L^z \neq 0$

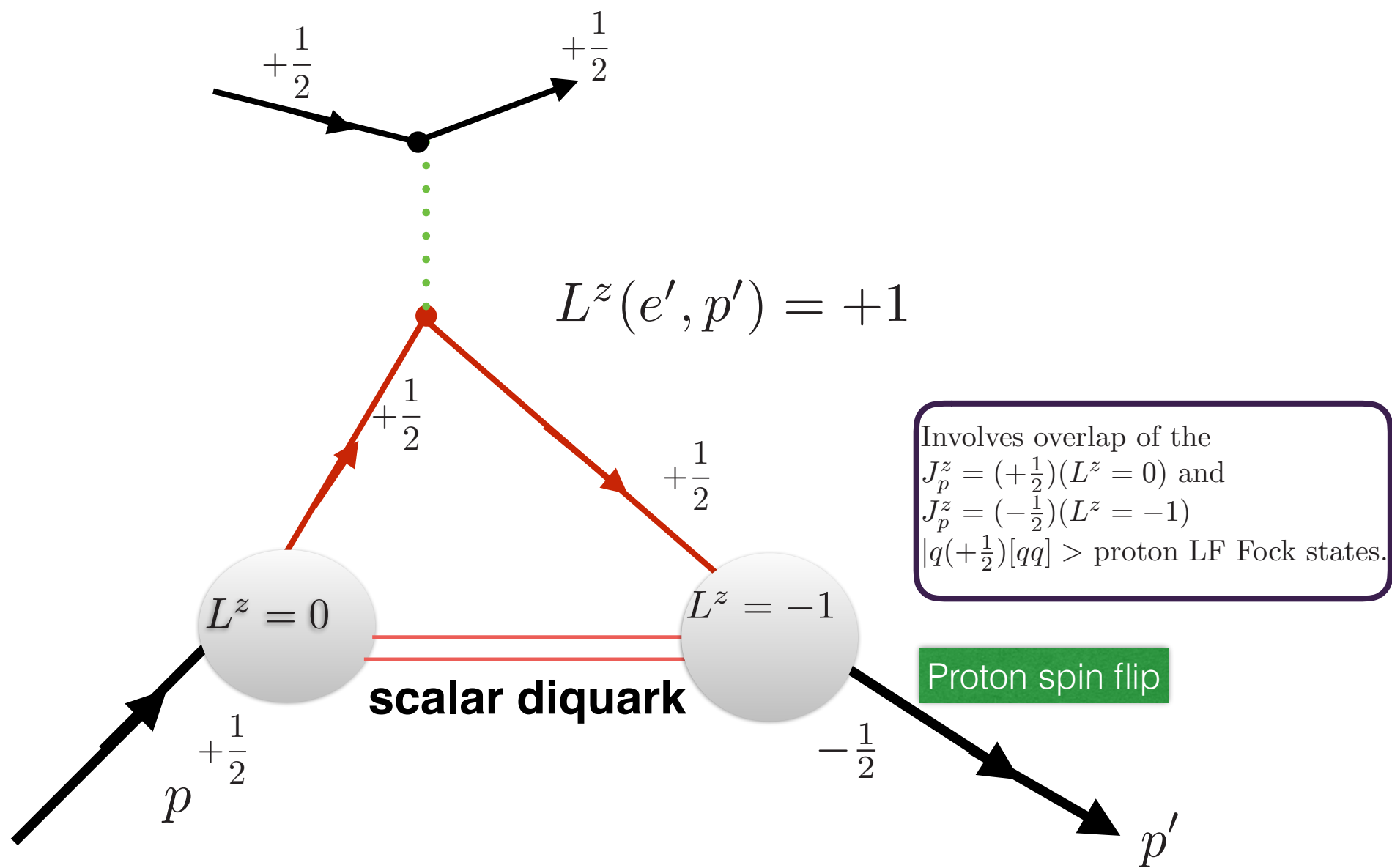


No proton spin flip

No quark chiral flip

$$ep \rightarrow ep'$$

**Pauli Form Factor: Amplitude vanishes at t=0.**



$$\gamma^* p \rightarrow \pi^0 p'$$

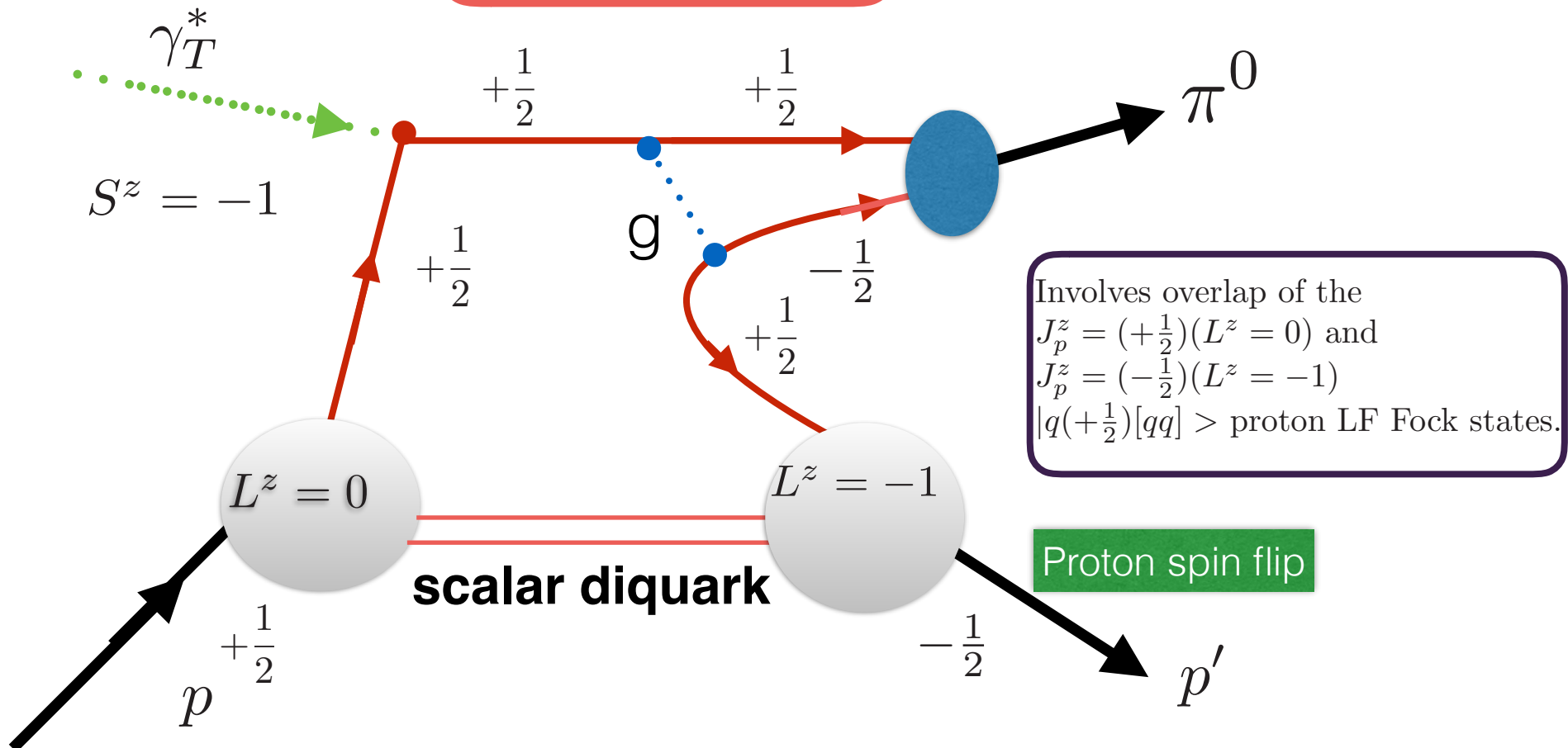
No quark chiral flip

$$J_{init}^z = (-\frac{1}{2}) = -1 + (+\frac{1}{2}) \rightarrow 0 + (-\frac{1}{2}) = (-\frac{1}{2}) = J_{final}^z$$

*Uses dominant twist-2 pion distribution amplitude*

Finite at  $t = 0$

$$L^z(\pi^0, p') = 0$$

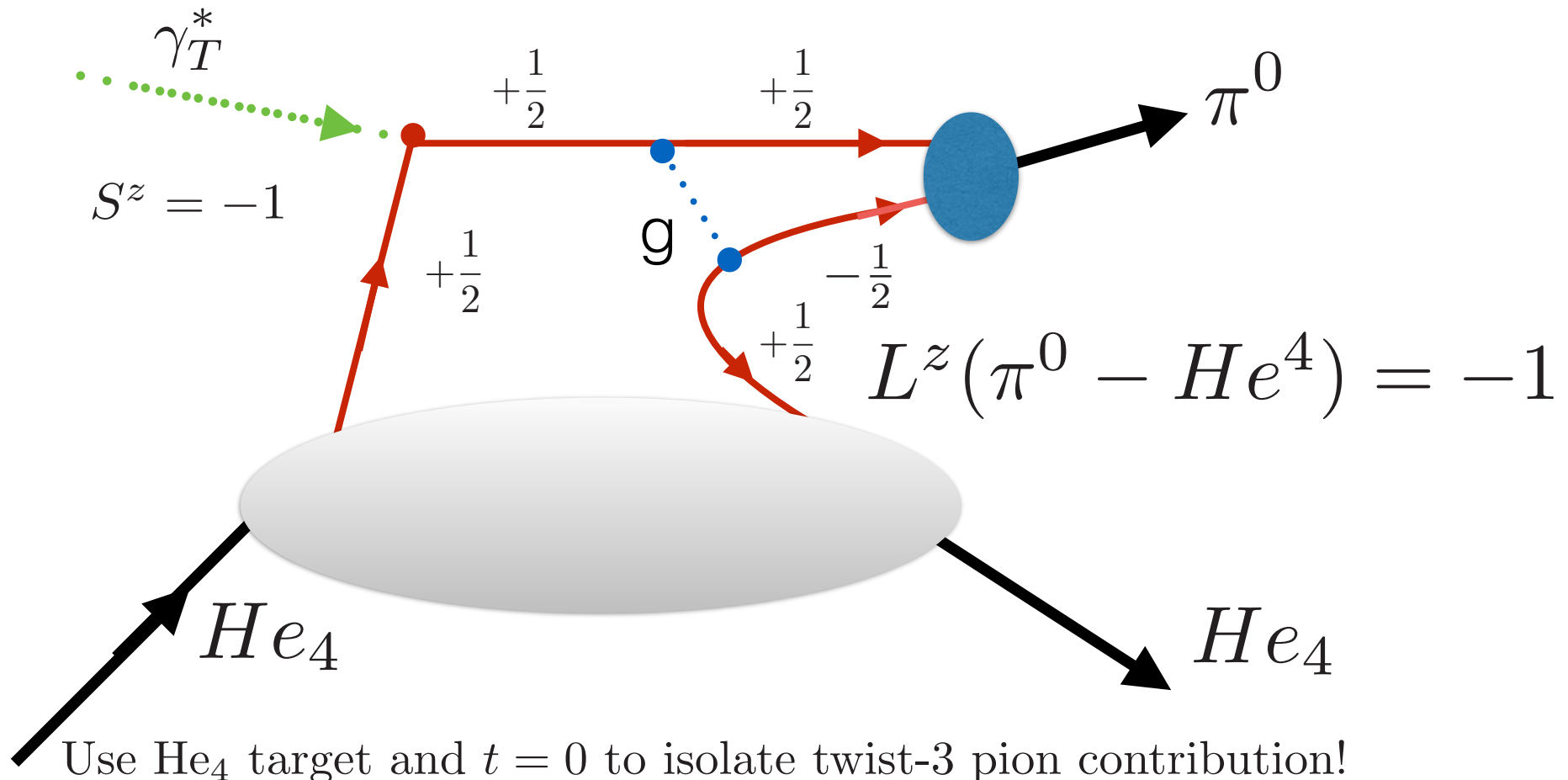


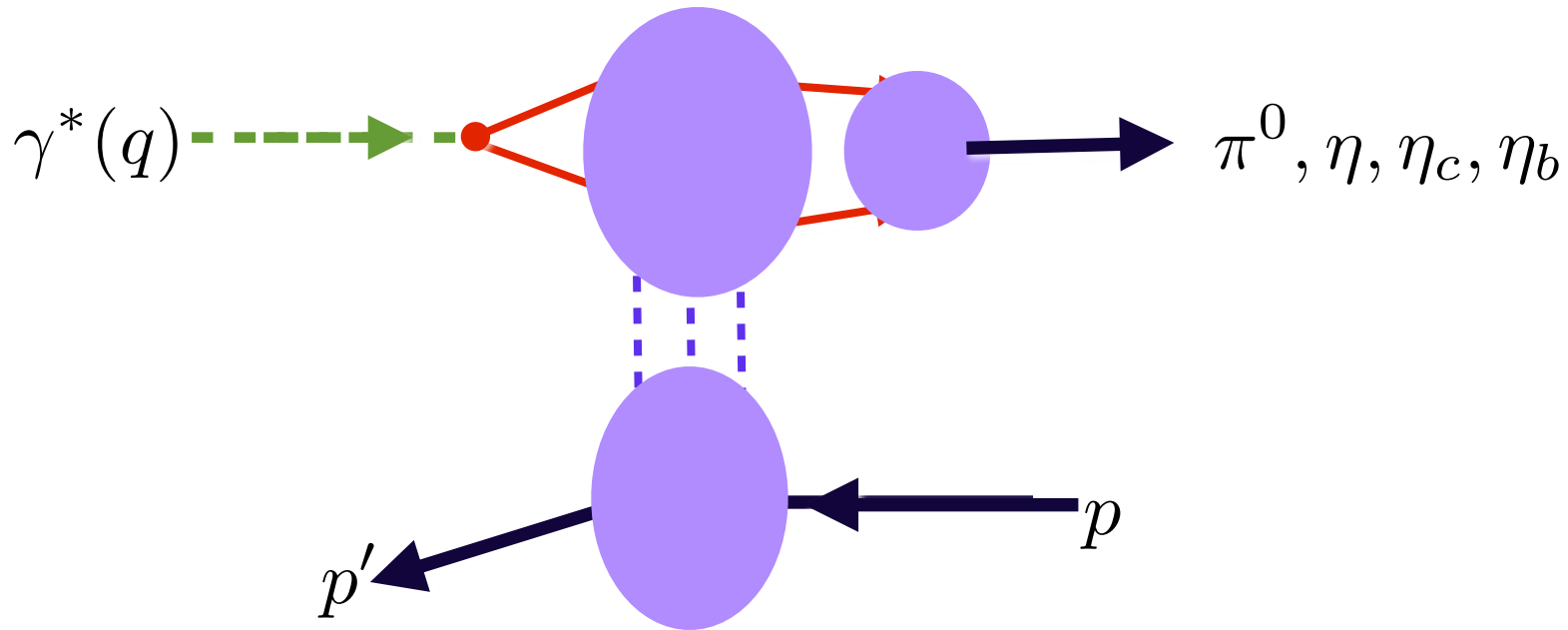
$$\gamma_T^* He_4 \rightarrow \pi_0 He_4$$

No quark chiral flip

*Uses dominant twist-2 pion distribution amplitude*

Vanishes at  $t=0$



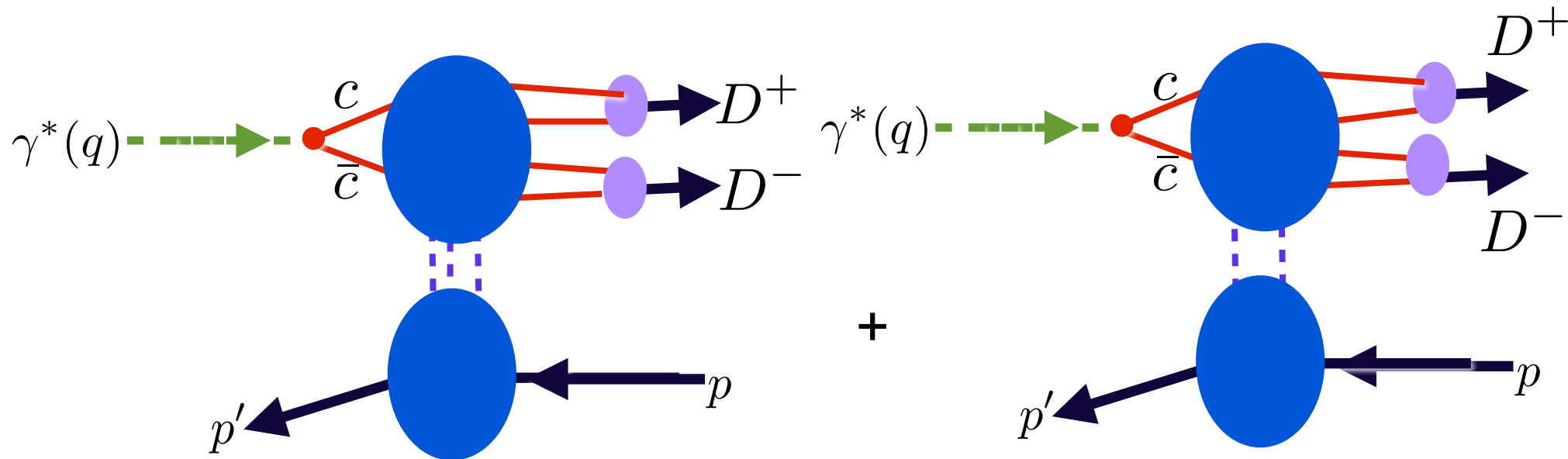


*Odderon has never been observed!*

***Look for Charge Asymmetries from Odderon-Pomeron Interference***

**Merino, Rathsmann,  
sjb**





**Odderon-Pomeron Interference leads to  $K^+ K^-$ ,  $D^+ D^-$  and  $B^+ B^-$  charge and angular asymmetries**

***Odderon at amplitude level***

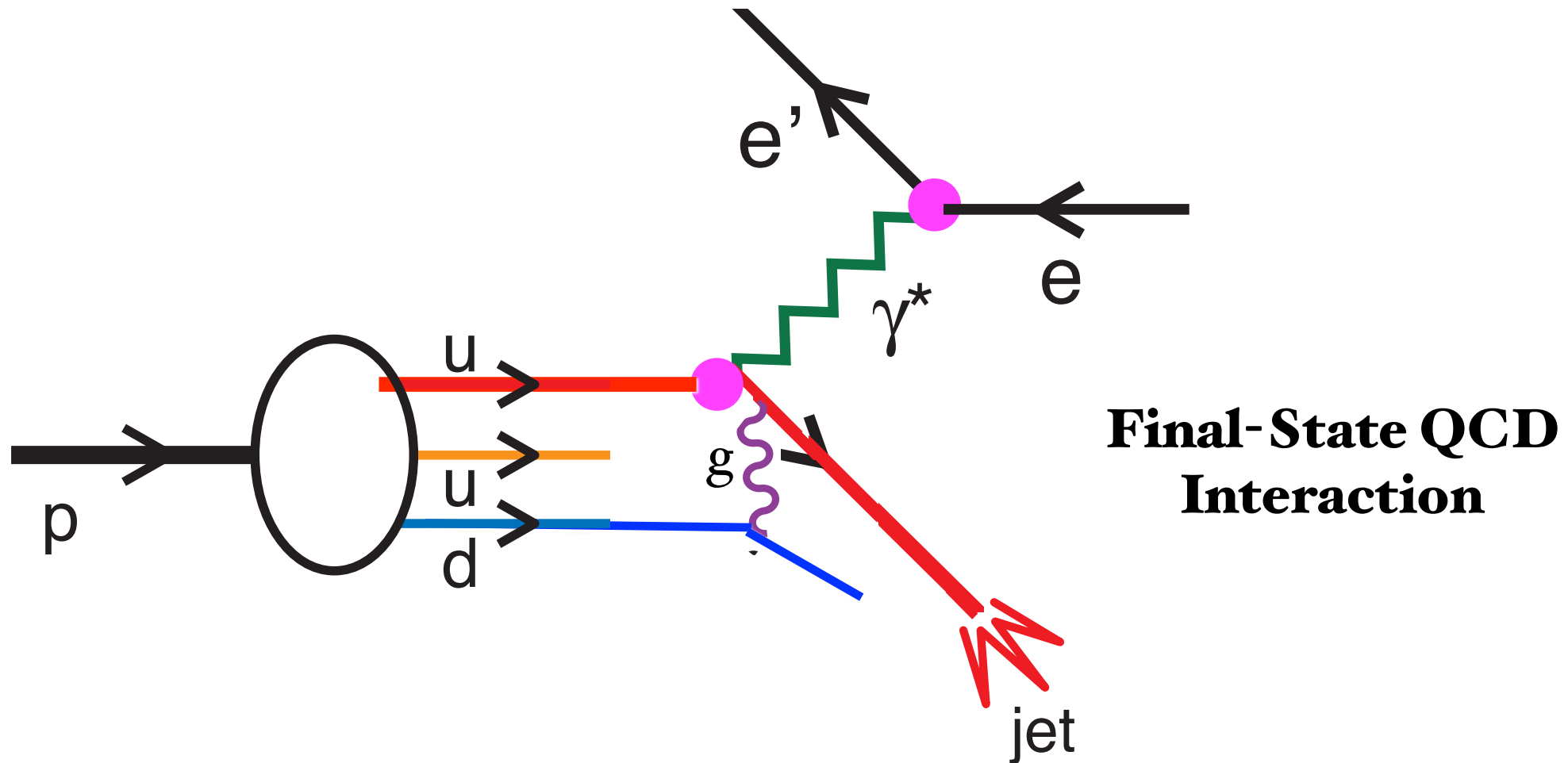
**Strong enhancement at heavy-quark pair threshold from QCD Sakharov-Schwinger-Sommerfeld effect**

**Merino, Rathsmann,  
sjb**

$$\frac{\pi\alpha_s(\beta^2 s)}{\beta}$$

**Hoang, Kuhn,  
sjb**

# Deep Inelastic Electron-Proton Scattering



*Conventional wisdom:  
Final-state interactions of struck quark can be neglected*

# Single-spin asymmetries

## Leading Twist Sivers Effect

Hwang, Schmidt,  
sjb

Collins, Burkardt, Ji, Yuan.  
Pasquini, ...

QCD S- and P-  
Coulomb Phases  
--Wilson Line

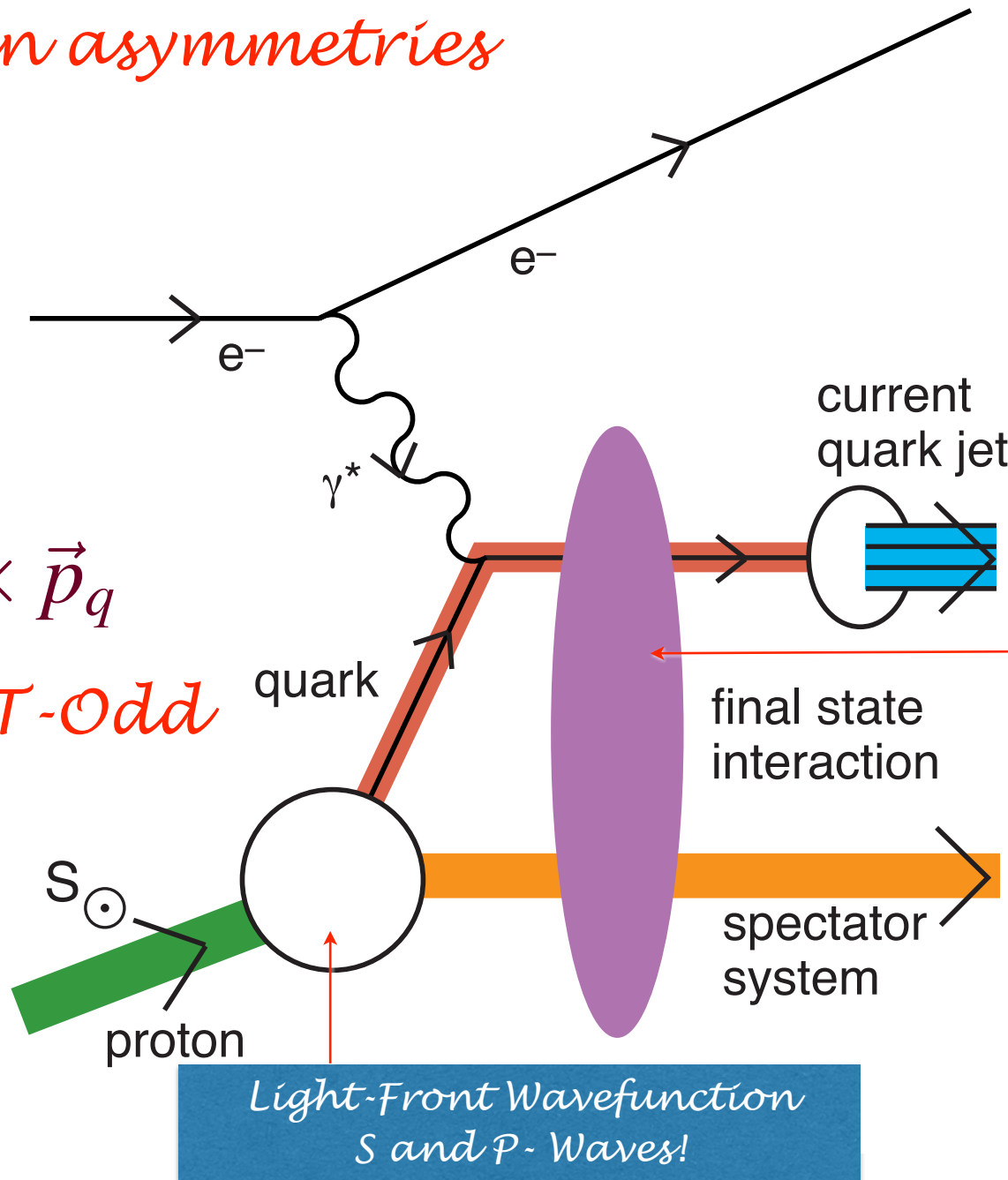
**“Lensing Effect”**

Leading-Twist  
Rescattering  
Violates pQCD  
Factorization!

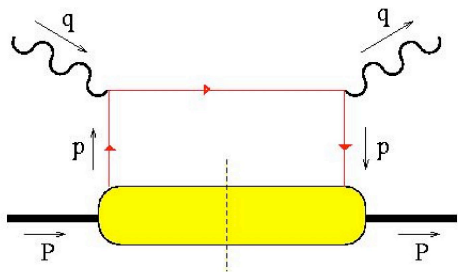
$$i \vec{S}_p \cdot \vec{q} \times \vec{p}_q$$

Pseudo-  $T$ -Odd

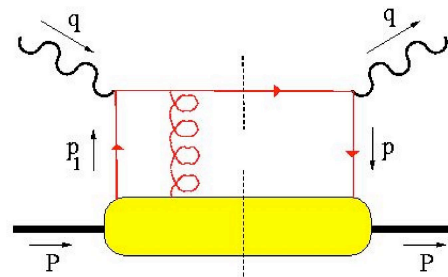
**“Lensing”  
involves soft  
scales**



Sign reversal in DY!



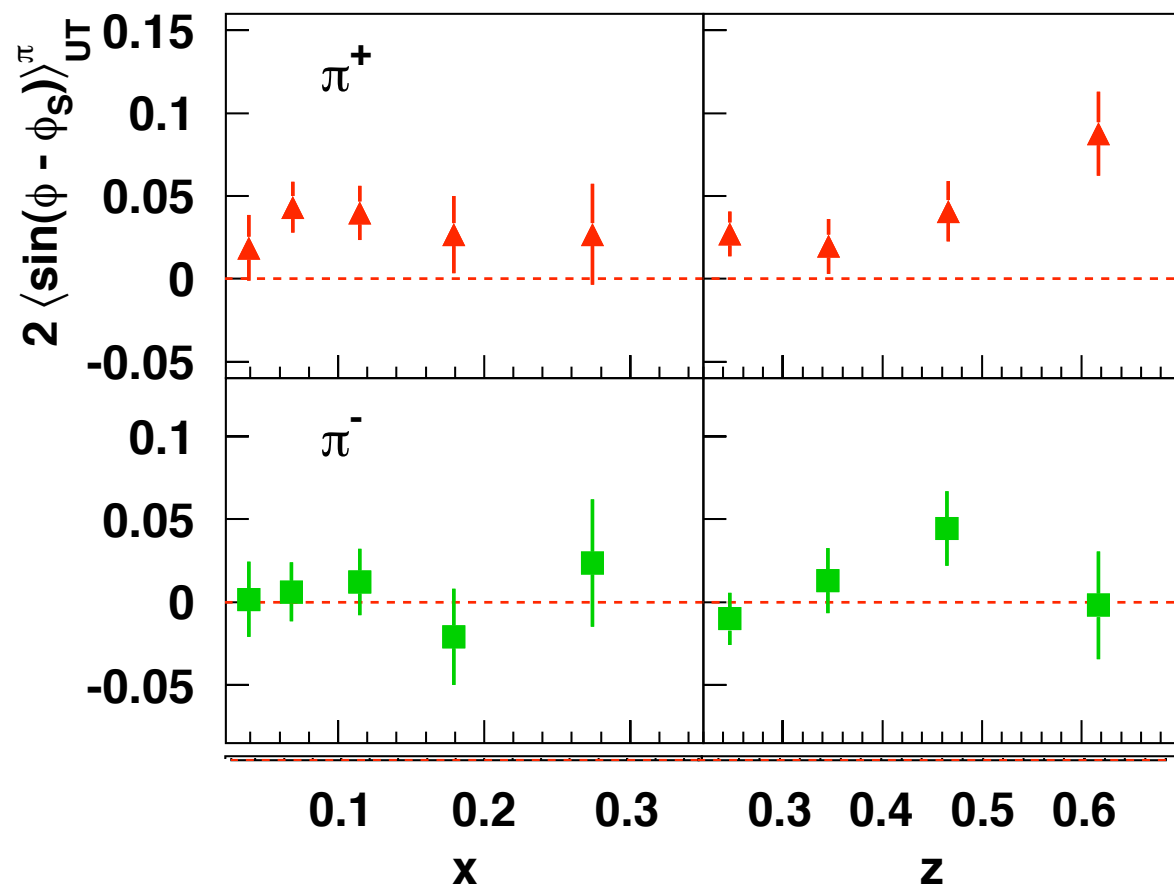
can interfere  
with



and produce  
a T-odd effect!  
(also need  $L_z \neq 0$ )

HERMES coll., A. Airapetian et al., Phys. Rev. Lett. 94 (2005) 012002.

## Sivers asymmetry from HERMES



- First evidence for non-zero Sivers function!
- $\Rightarrow$  presence of non-zero **quark orbital angular momentum!**
- **Positive** for  $\pi^+$ ...  
**Consistent with zero** for  $\pi^-$ ...

**Gamberg: Hermes  
data compatible with BHS model**

**Schmidt, Lu: Hermes  
charge pattern follow quark  
contributions to anomalous moment**

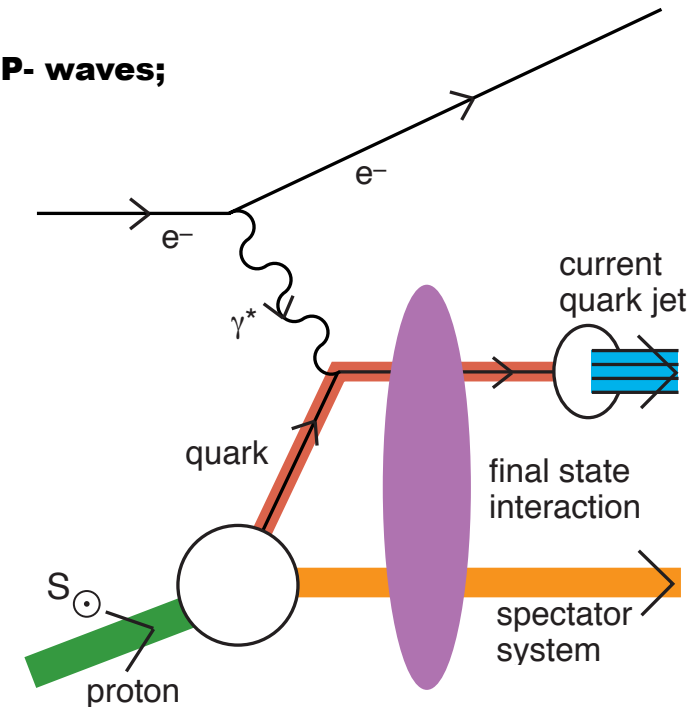
# Final-State Interactions Produce Pseudo T-Odd (Sivers Effect)

Hwang, Schmidt, sjb  
Collins

- **Leading-Twist Bjorken Scaling!**
- **Requires nonzero orbital angular momentum of quark**
- **Arises from the interference of Final-State QCD Coulomb phases in S- and P- waves;**
- **Wilson line effect -- lc gauge prescription**
- **Relate to the quark contribution to the target proton anomalous magnetic moment and final-state QCD phases**
- **QCD phase at soft scale!**
- **New window to QCD coupling and running gluon mass in the IR**
- **QED S and P Coulomb phases infinite -- difference of phases finite!**
- **Alternate: Retarded and Advanced Gauge: Augmented LFWFs**

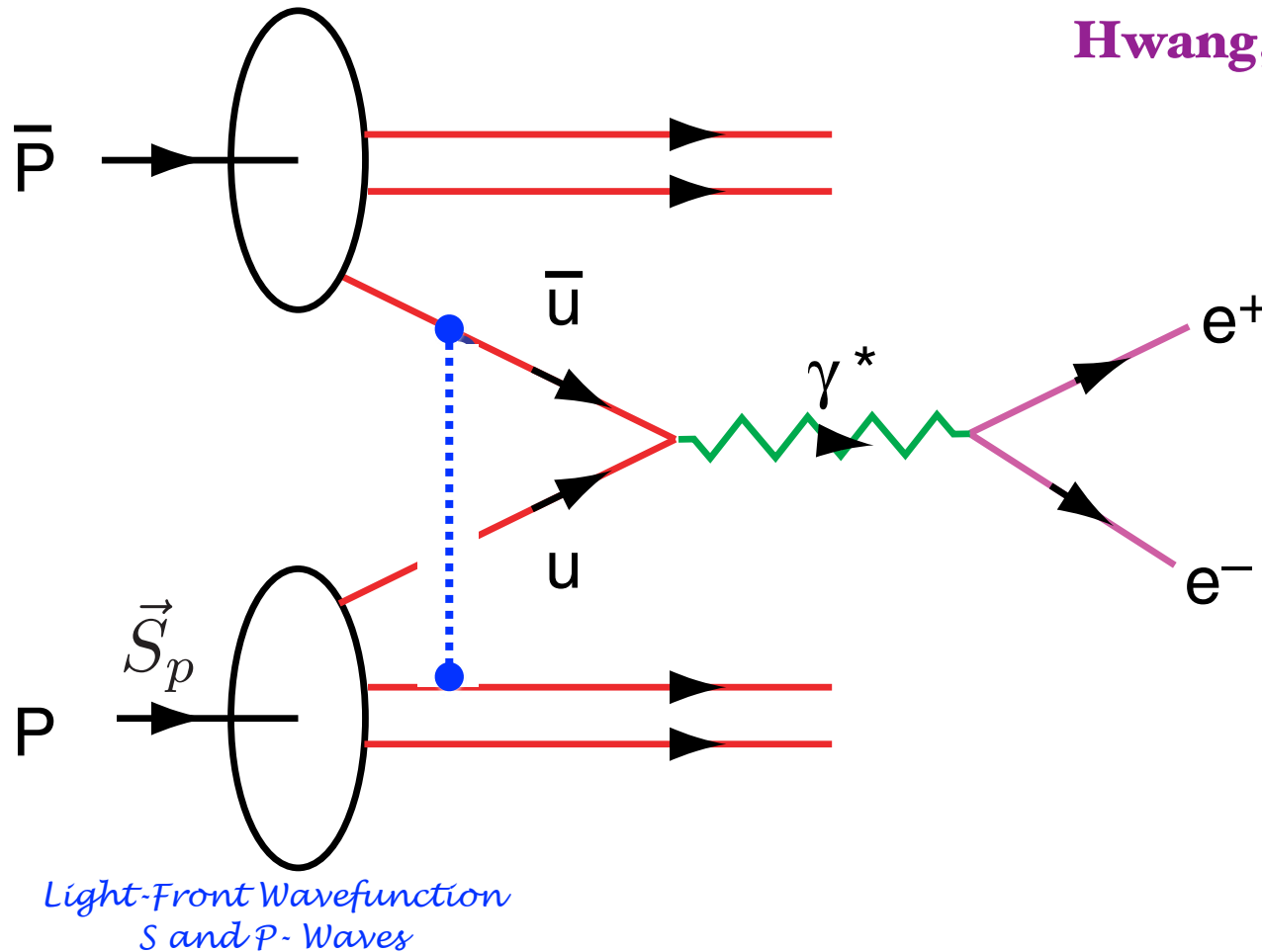
Dae Sung Hwang, Yuri V. Kovchegov,  
Ivan Schmidt, Matthew D. Sievert, sjb

$$i \vec{S} \cdot \vec{p}_{jet} \times \vec{q}$$



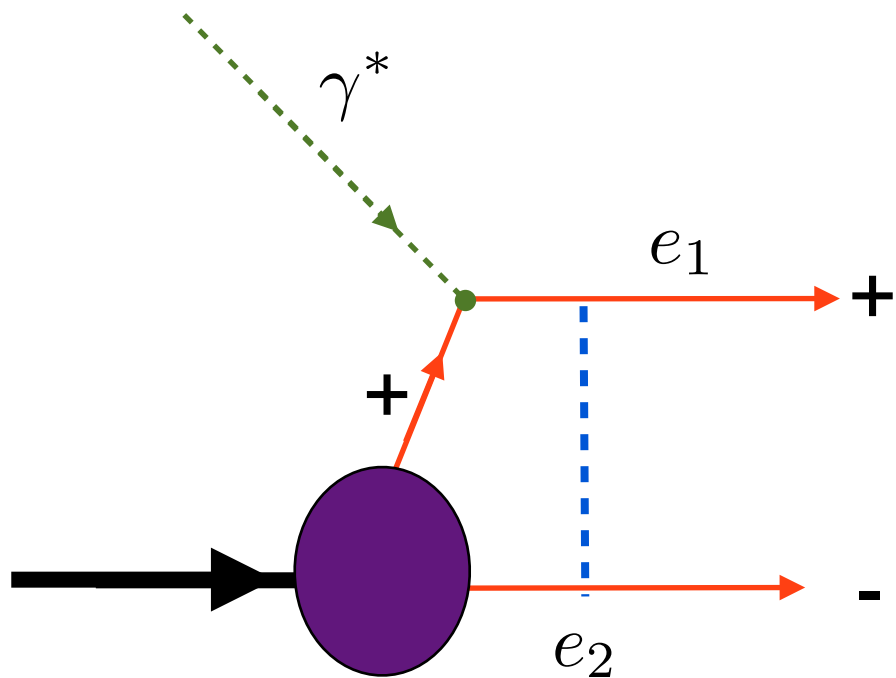
Pasquini, Xiao, Yuan, sjb  
Mulders, Boer      Qiu, Sterman

Collins  
Hwang, Schmidt, sjb



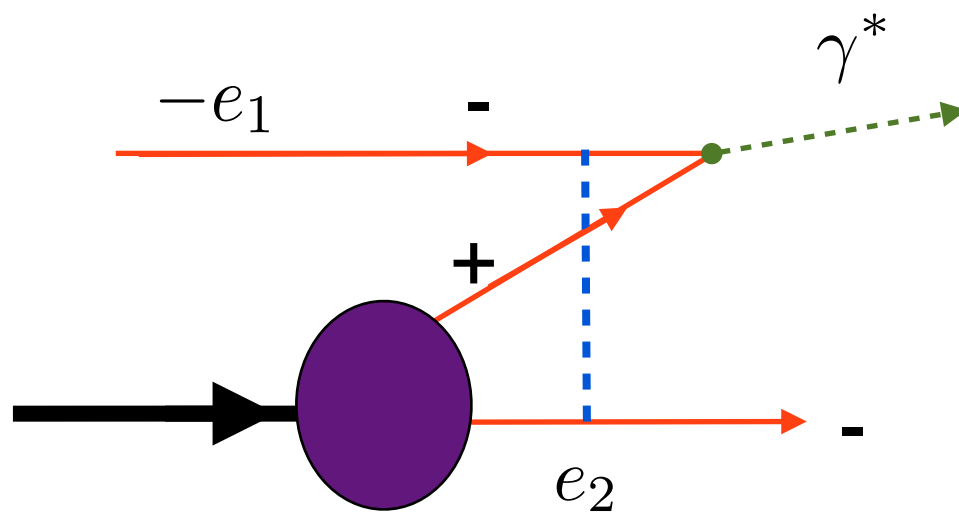
Pseudo-Odd Correlation  $i \vec{S}_p \cdot \vec{q} \times \vec{p}_{\bar{p}}$

**Sivers Effect in Di-Lepton Production is Predicted to have Opposite Sign compared to SIDIS**



DIS

*Attractive, opposite-sign  
rescattering potential*



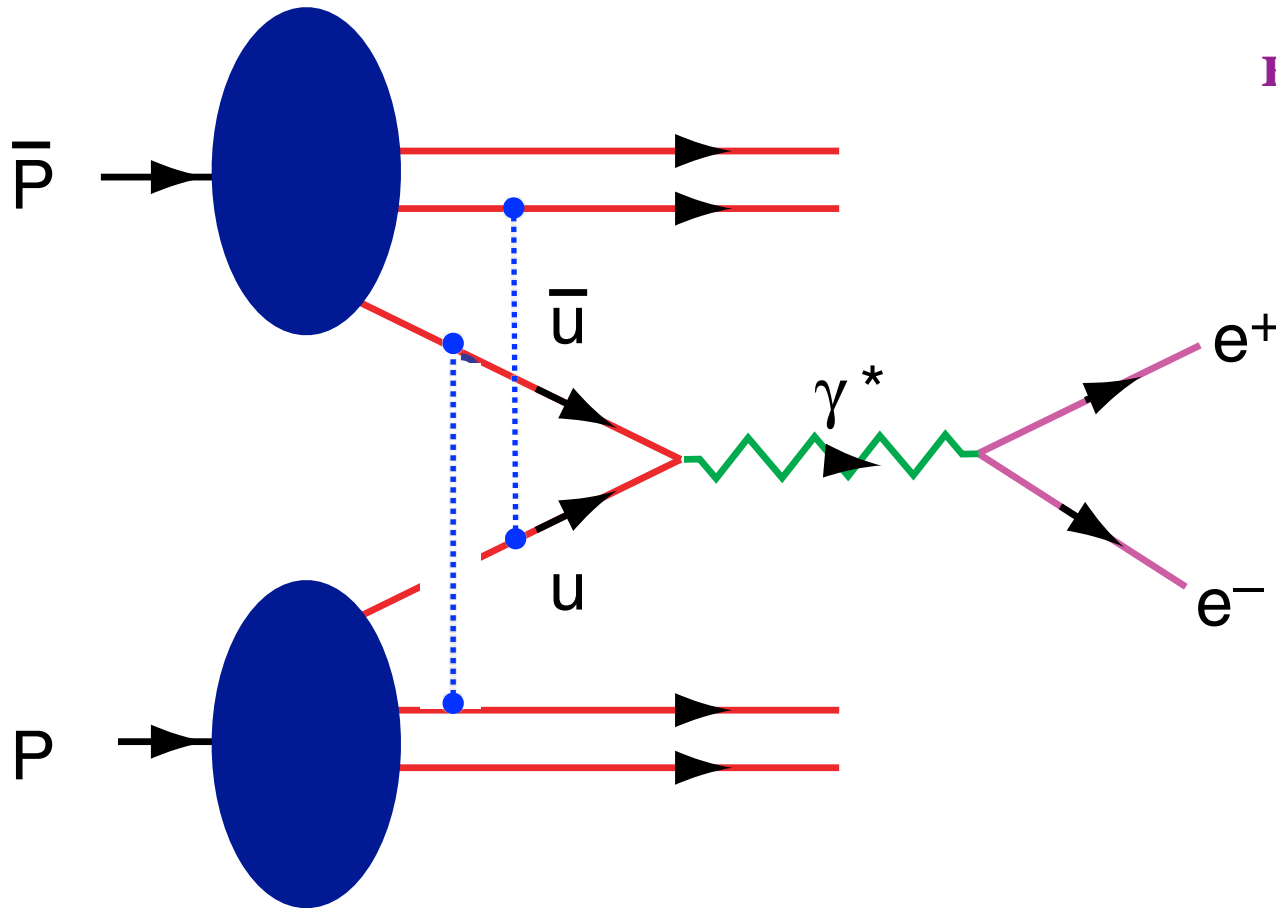
DY

*Repulsive, same-sign  
scattering potential*

**Dae Sung Hwang, Yuri V. Kovchegov,  
Ivan Schmidt, Matthew D. Sievert, sjb**

# Example of Leading-Twist Lensing Correction

Boer, Hwang, sjb



**$DY_{\cos 2\phi}$  correlation at leading twist from double ISI**

*Product of Boer -  
Mulders Functions*

$$h_1^\perp(x_1, \mathbf{p}_\perp^2) \times \bar{h}_1^\perp(x_2, \mathbf{k}_\perp^2)$$

**Violates Lam-Tung relation!**



*Double Initial-State Interactions*

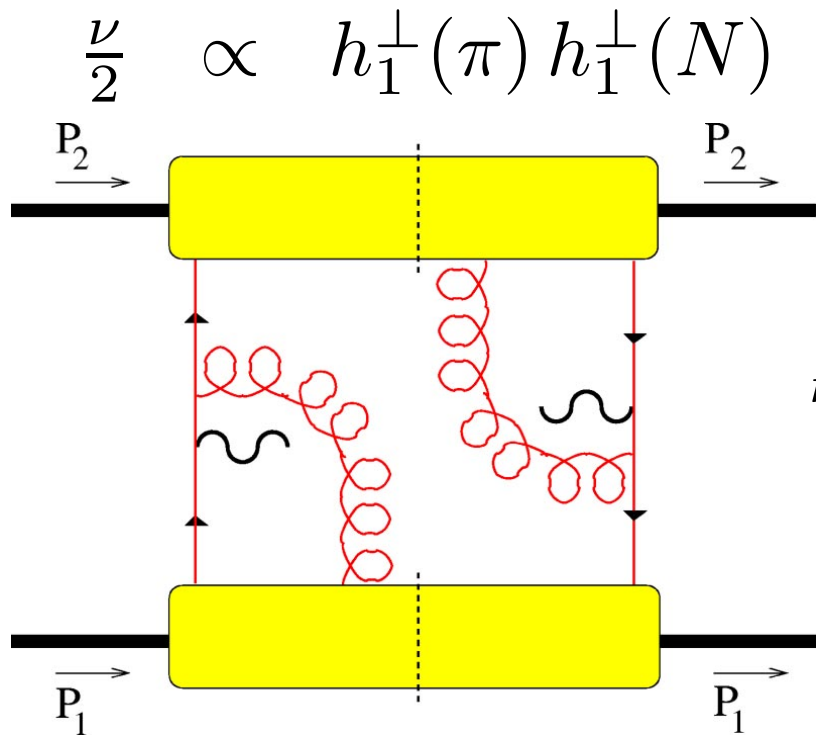
*generate anomalous*  $\cos 2\phi$

Boer, Hwang, sjb

## Drell-Yan planar correlations

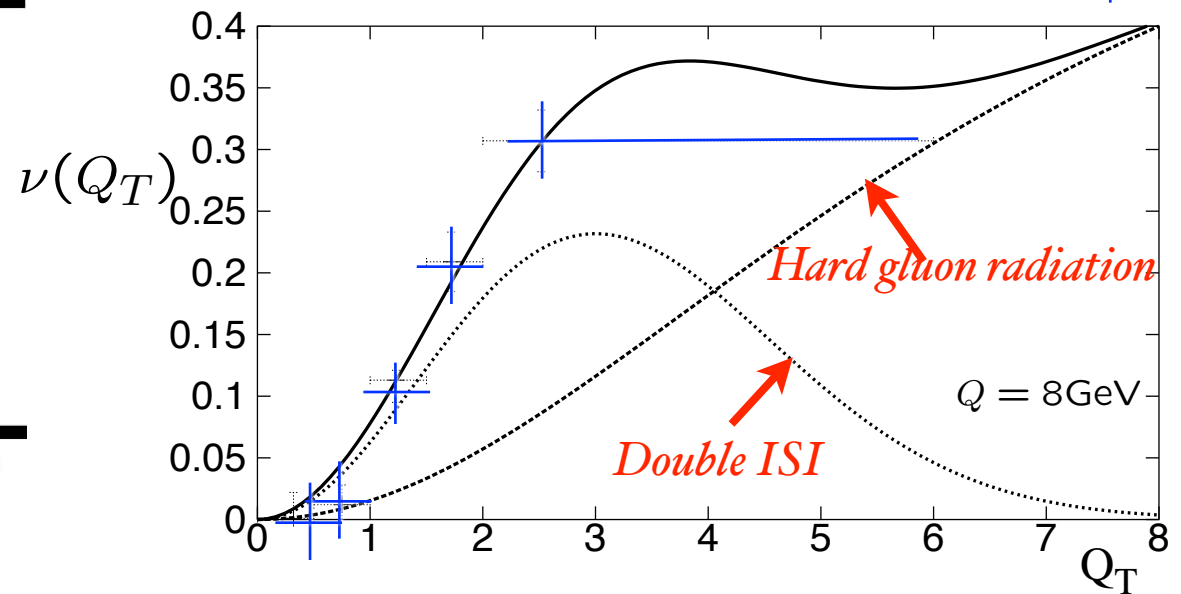
$$\frac{1}{\sigma} \frac{d\sigma}{d\Omega} \propto \left( 1 + \lambda \cos^2 \theta + \mu \sin 2\theta \cos \phi + \frac{\nu}{2} \sin^2 \theta \cos 2\phi \right)$$

PQCD Factorization (Lam Tung):  $1 - \lambda - 2\nu = 0$



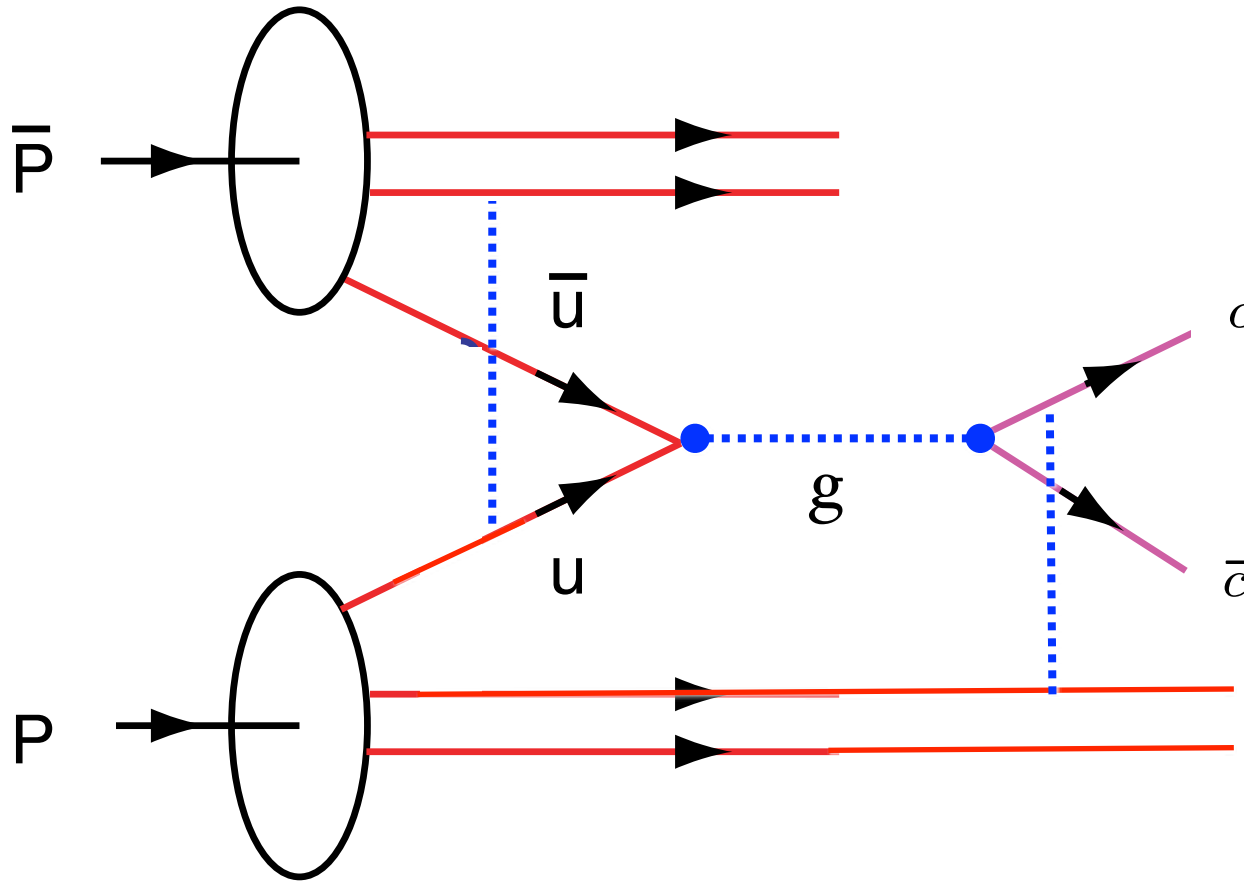
**Violates Lam-Tung relation!**

$$\pi N \rightarrow \mu^+ \mu^- X \quad \text{NA10} \quad +$$



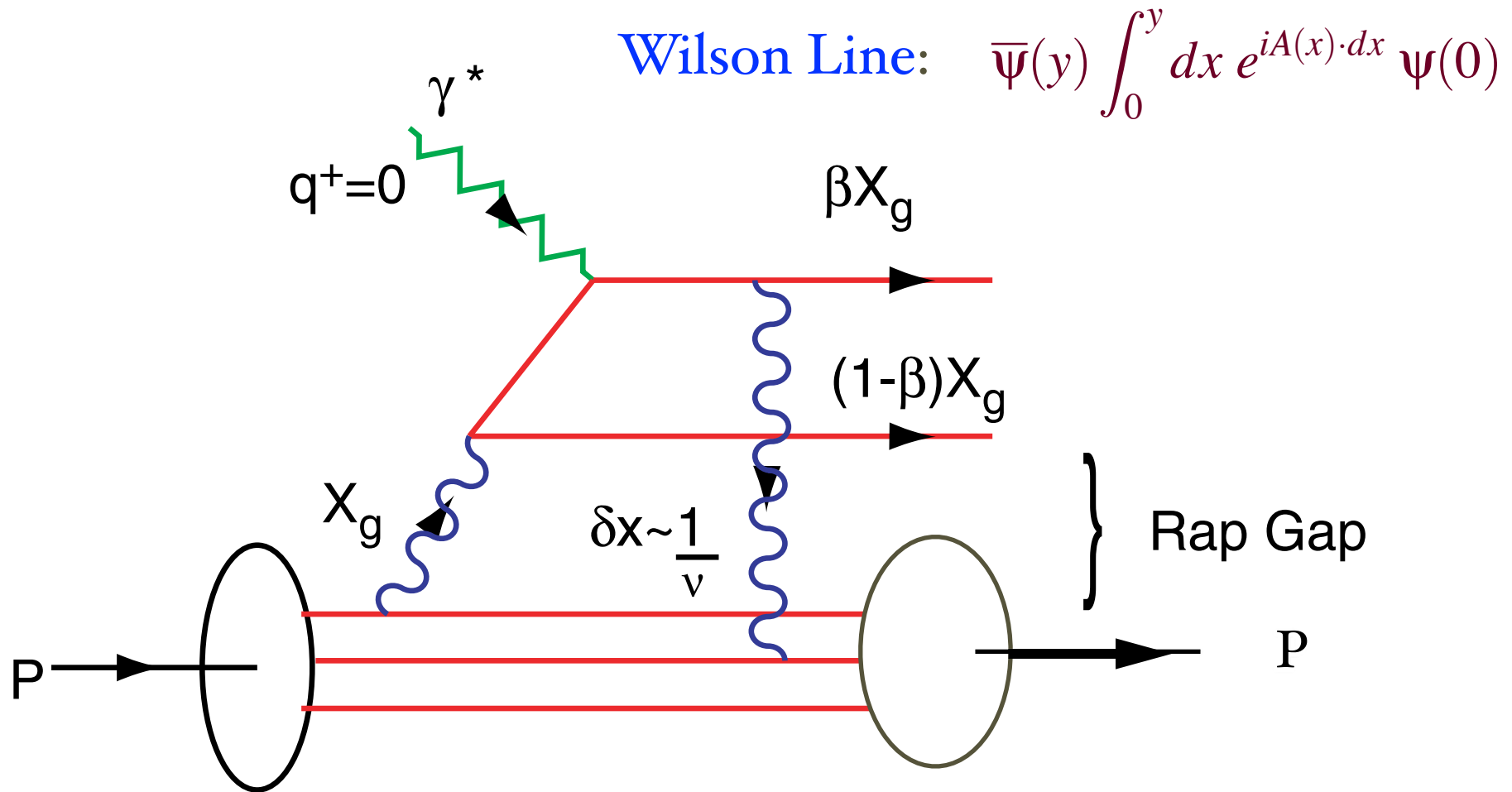
Model: Boer,

See also: Collins and Qiu



*Problem for factorization when both ISI and FSI occur*

# QCD Mechanism for Rapidity Gaps



**Reproduces lab-frame color dipole approach**  
**DDIS: Input for leading twist nuclear shadowing**

*Single-spin  
asymmetries in  
exclusive channels*

**Exclusive  
Sivers Effect  
connects to  
Inclusive Effect**

$$i\vec{S}_\Lambda \cdot \vec{q} \times \vec{p}_K$$

$$i\vec{S}_p \cdot \vec{q} \times \vec{p}_K$$

$$\gamma^* p_\uparrow \rightarrow K^+ \Lambda$$

*Pseudo-T-Odd*

quark

$S_\odot$

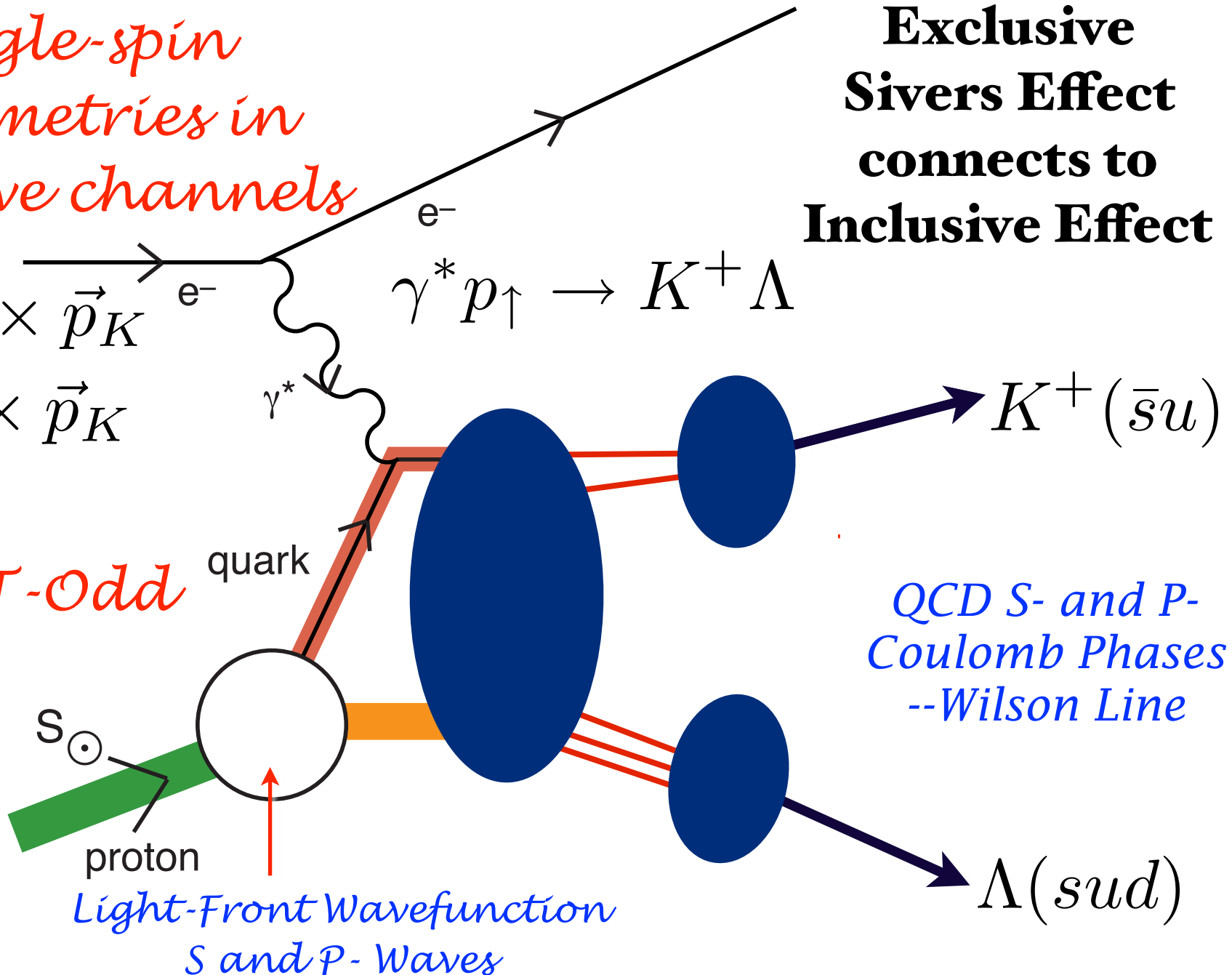
proton

*Light-Front Wavefunction  
S and P-Waves*

*QCD S- and P-  
Coulomb Phases  
--Wilson Line*

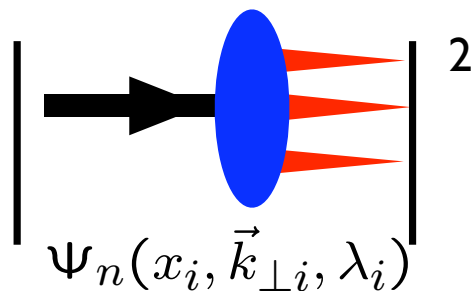
$\Lambda(sud)$

$K^+(\bar{s}u)$




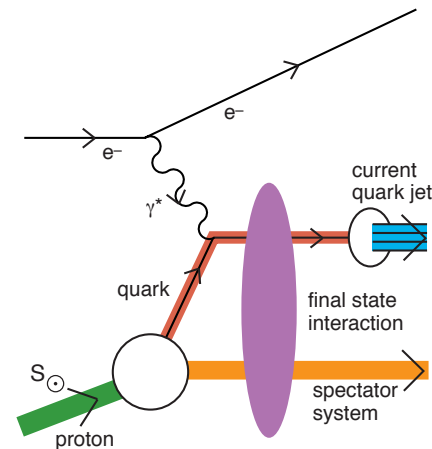
# Static

- Square of Target LFWFs
- No Wilson Line
- Probability Distributions
- Process-Independent
- T-even Observables
- No Shadowing, Anti-Shadowing
- Sum Rules: Momentum and  $J^z$
- DGLAP Evolution; mod. at large  $x$
- No Diffractive DIS



# Dynamic

- Modified by Rescattering: ISI & FSI
- Contains Wilson Line, Phases
- No Probabilistic Interpretation
- Process-Dependent - From Collision
- T-Odd (Sivers, Boer-Mulders, etc.)
- Shadowing, Anti-Shadowing, Saturation
- Sum Rules Not Proven 
- DGLAP Evolution
- Hard Pomeron and Odderon Diffractive DIS



## What is measured!

**Hwang, Schmidt, sjb,**

**Mulders, Boer**

**Qiu, Sterman**

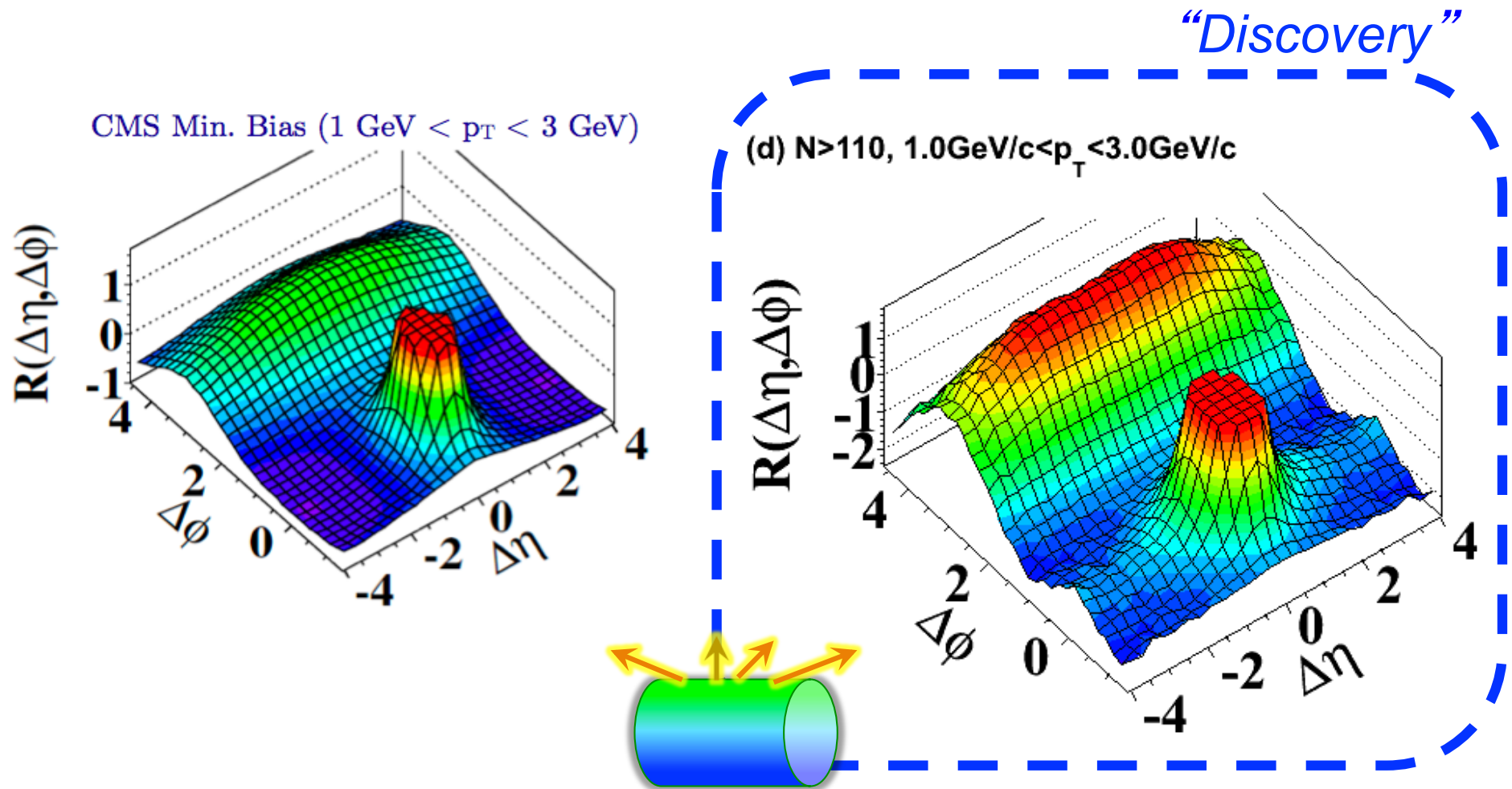
**Collins, Qiu**

**Pasquini, Xiao, Yuan, sjb**

**Liuti, sjb**

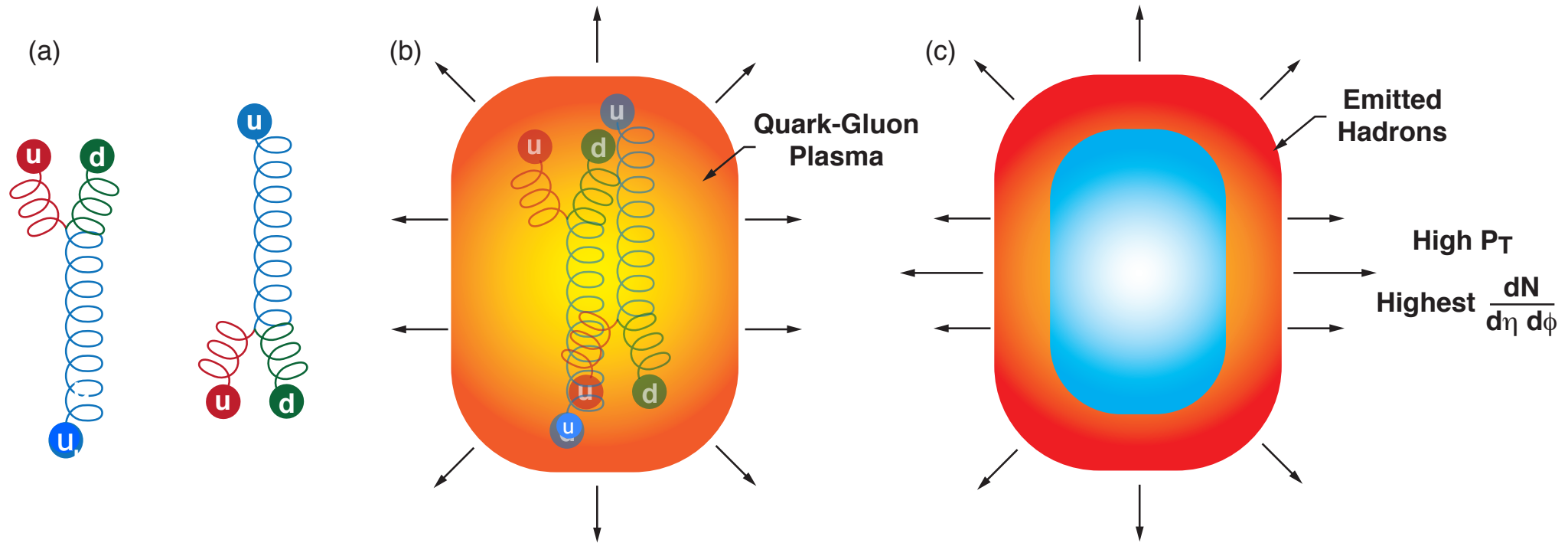
# Ridge in high-multiplicity $p p$ collisions

## Two-particle correlations: CMS results



- ◆ Ridge: Distinct long range correlation in  $\eta$  collimated around  $\Delta\Phi \approx 0$  for two hadrons in the intermediate  $1 < p_T, q_T < 3 \text{ GeV}$

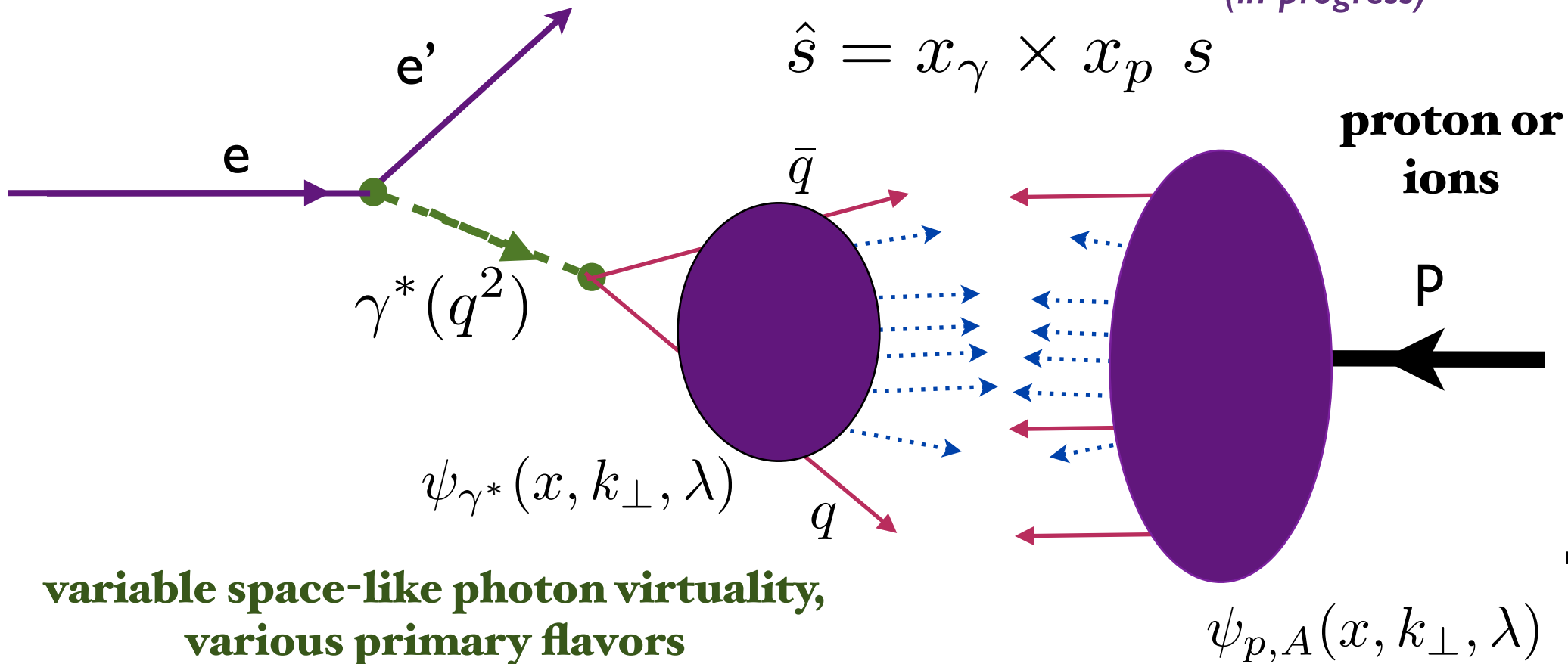
*Ridge may reflect collision of aligned flux tubes*



# Electron-Ion Collider: Virtual Photon-Ion Collider

*Perspective from the e-p collider frame*

S. Glazek, P. Kubiczek, sjb  
(in progress)



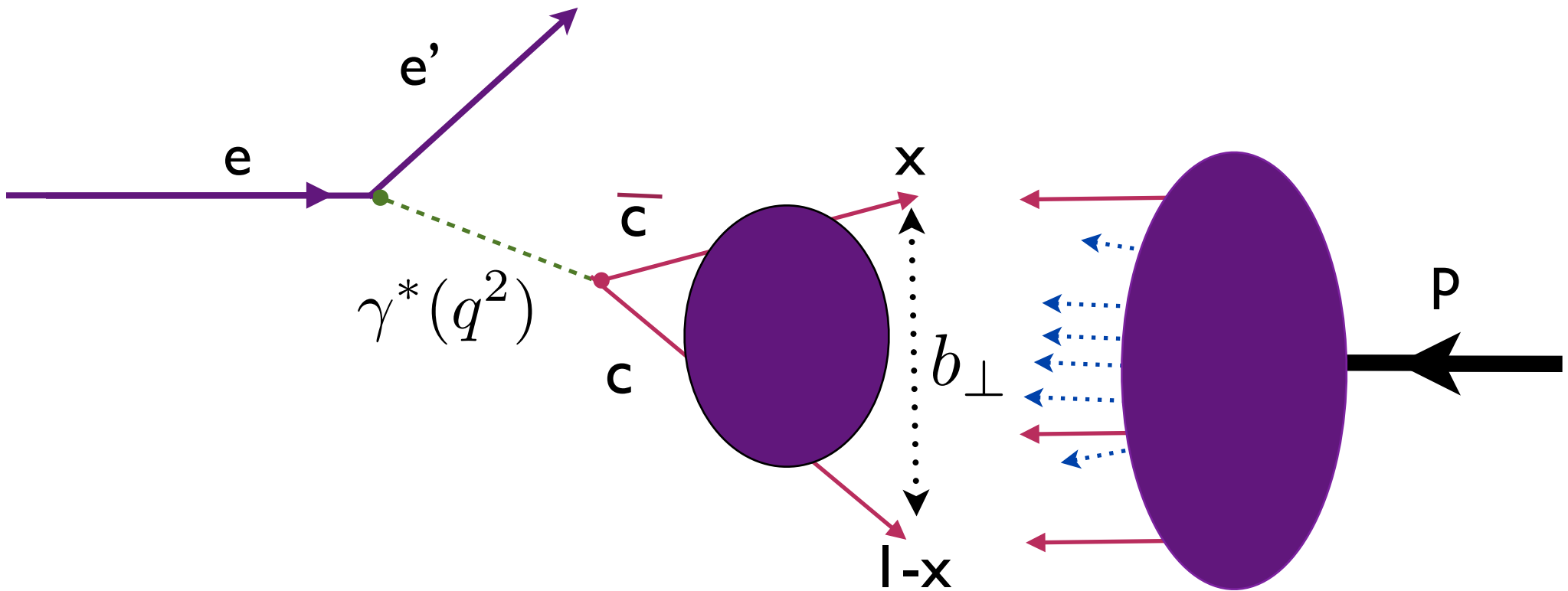
*$\bar{q} q$  plane aligned with lepton scattering plane  $\sim \cos^2 \phi$*

*Front-surface dynamics: shadowing/antishadowing*



*$\bar{c} c$  acts as a 'drill'*

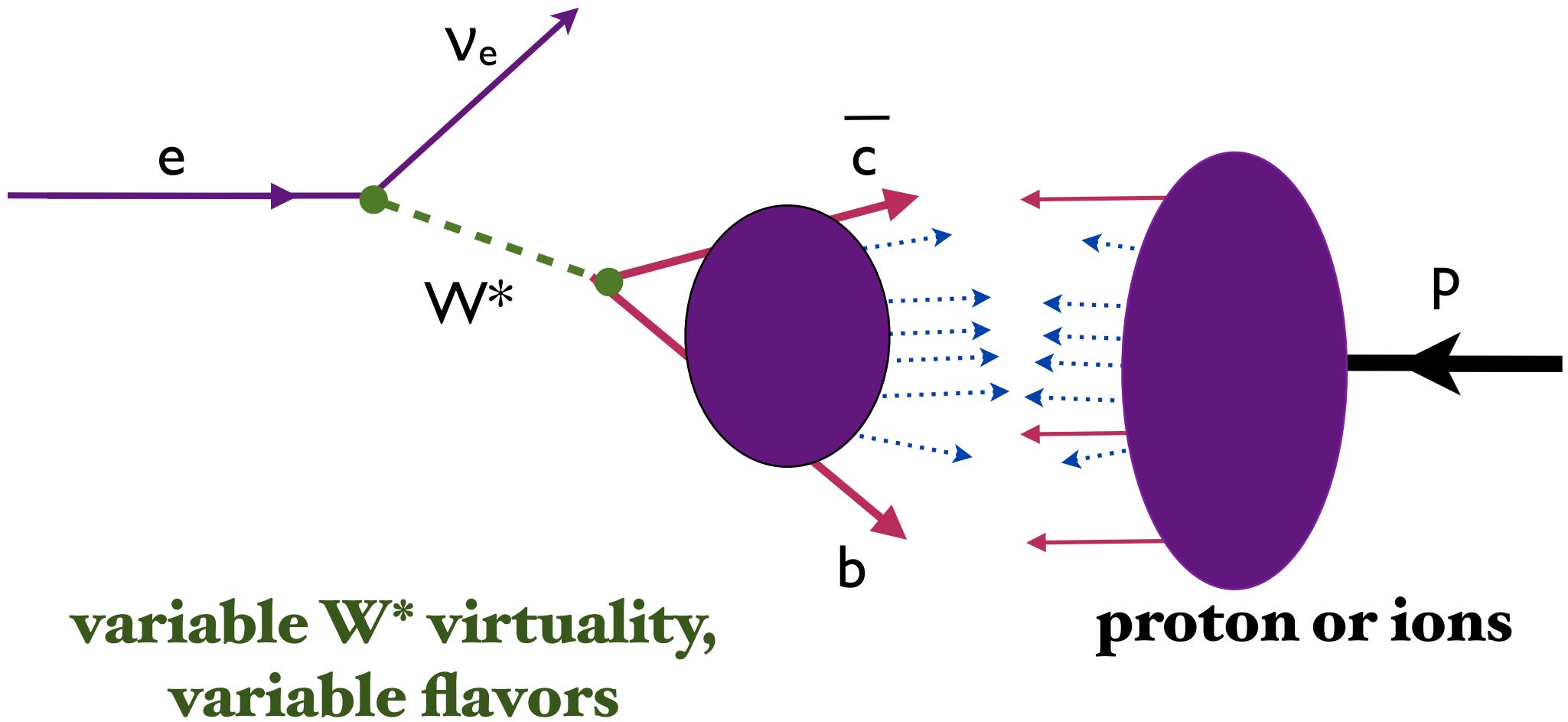
$$\langle b_{\perp}^2 \rangle \sim \frac{1}{Q^2 x(1-x) + m_c^2}$$



**High  $Q^2$  virtual photon at an EIC acts as a precision, small bore, linearly oriented, flavor-dependent probe acting on a proton or nuclear target.**

*Study final-state hadron multiplicity distributions, ridges, nuclear dependence, etc.*

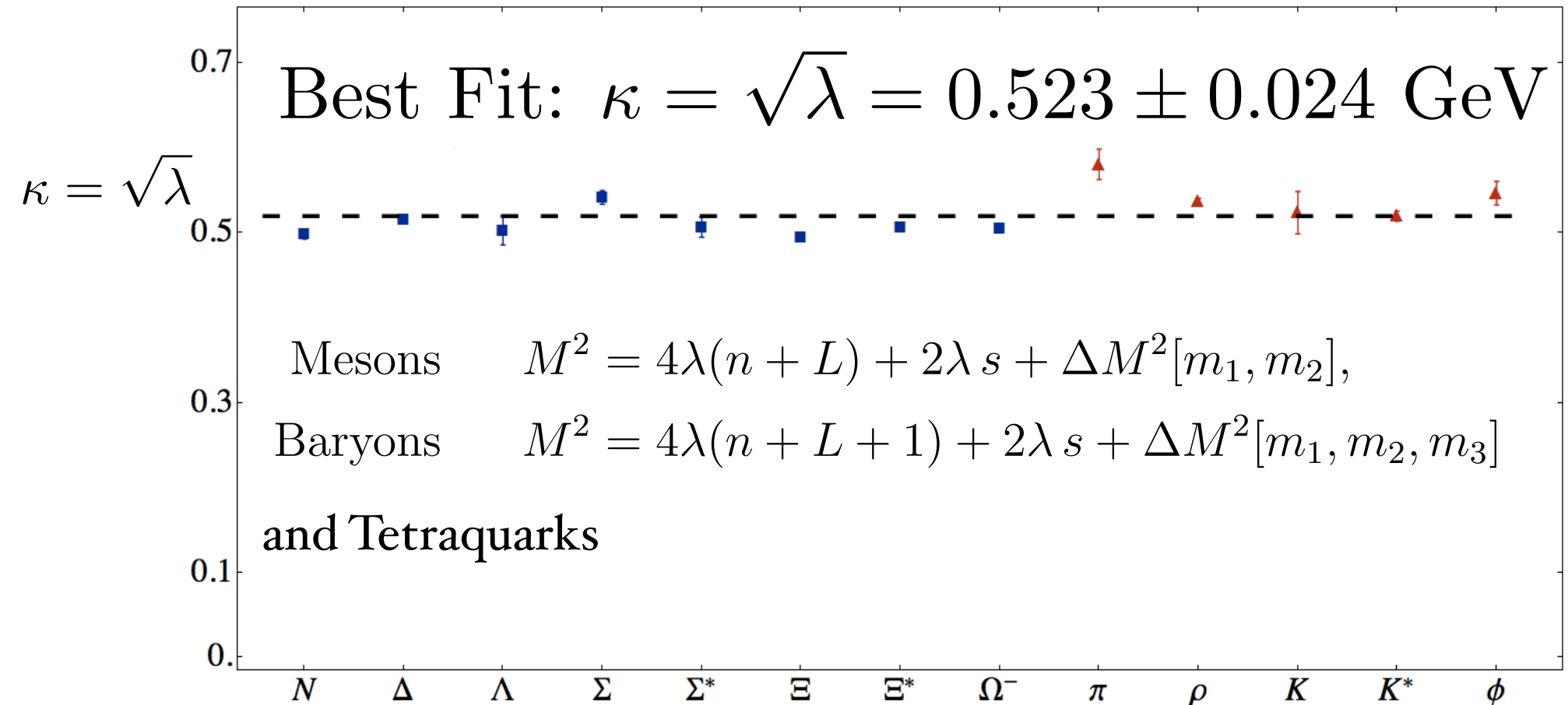
# *EIC: Virtual Weak Boson-Proton Collider*



- Universal Regge slopes

*Dosch, de Teramond,  
Lorce, sjb*

$$M_H^2 = 4\lambda(n + L) + \dots$$

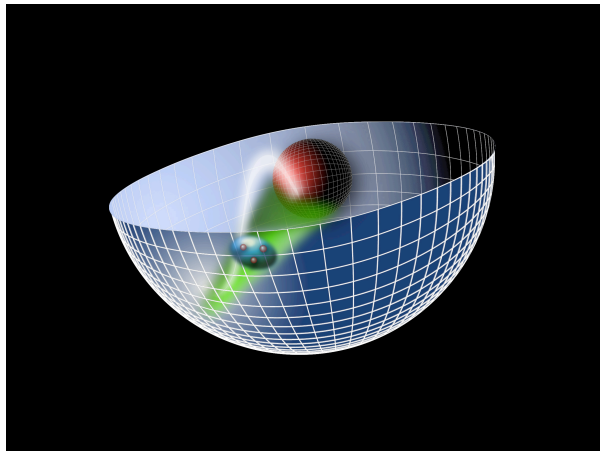


Best fit for the value of the hadronic scale  $\sqrt{\lambda}$  for the different Regge trajectories for baryons and mesons including all radial and orbital excitations using Eqs. (23) and (24). The dotted line is the average value  $\sqrt{\lambda} = 0.523$  GeV; it has the standard deviation  $\sigma = 0.024$  GeV. For the baryon sample alone the values are  $0.509 \pm 0.015$  GeV and for the mesons  $0.524 \pm 0.023$  GeV.

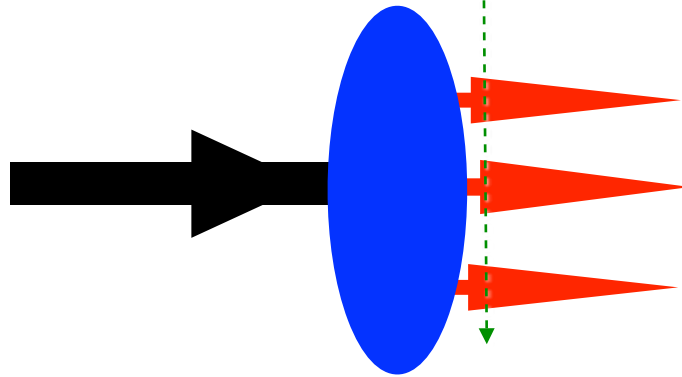
$$\phi(z)$$

# AdS<sub>5</sub>: Conformal Template for QCD

## • *Light-Front Holography*

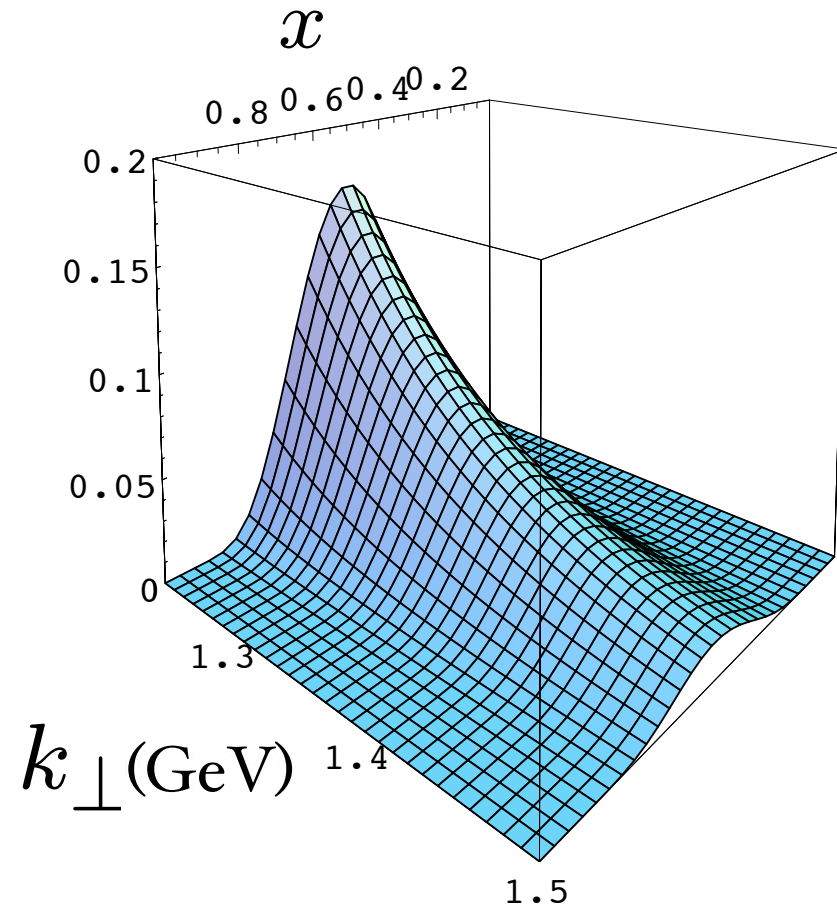


Fixed  $\tau = t + z/c$



$$\Psi_n(x_i, \vec{k}_{\perp i}, \lambda_i)$$

**Duality of AdS<sub>5</sub> with LF  
Hamiltonian Theory**



## • *Light Front Wavefunctions:*

***Light-Front Schrödinger Equation  
Spectroscopy and Dynamics***

with Guy de Teramond, Alexandre Deur,  
Cedric Lorce, Hans Guenter Dosch

# QCD Lagrangian

$$\mathcal{L}_{QCD} = -\frac{1}{4}\text{Tr}(G^{\mu\nu}G_{\mu\nu}) + \sum_{f=1}^{n_f} i\bar{\Psi}_f D_\mu \gamma^\mu \Psi_f + \sum_{f=1}^{n_f} m_f \bar{\Psi}_f \Psi_f$$

$$iD^\mu = i\partial^\mu - gA^\mu \quad G^{\mu\nu} = \partial^\mu A^\nu - \partial^\nu A^\mu - g[A^\mu, A^\nu]$$

**Classical Chiral Lagrangian is Conformally Invariant**

**Where does the QCD Mass Scale  $\Lambda_{QCD}$  come from?**

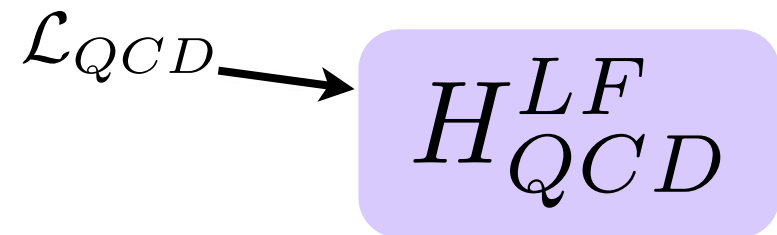
*How does color confinement arise?*

● de Alfaro, Fubini, Furlan:

**Scale can appear in Hamiltonian and EQM  
without affecting conformal invariance of action!**

***Unique confinement potential!***

# Light-Front QCD



$$(H_{LF}^0 + H_{LF}^I) |\Psi\rangle = M^2 |\Psi\rangle$$

$$\left[ \frac{\vec{k}_\perp^2 + m^2}{x(1-x)} + V_{\text{eff}}^{LF} \right] \psi_{LF}(x, \vec{k}_\perp) = M^2 \psi_{LF}(x, \vec{k}_\perp)$$

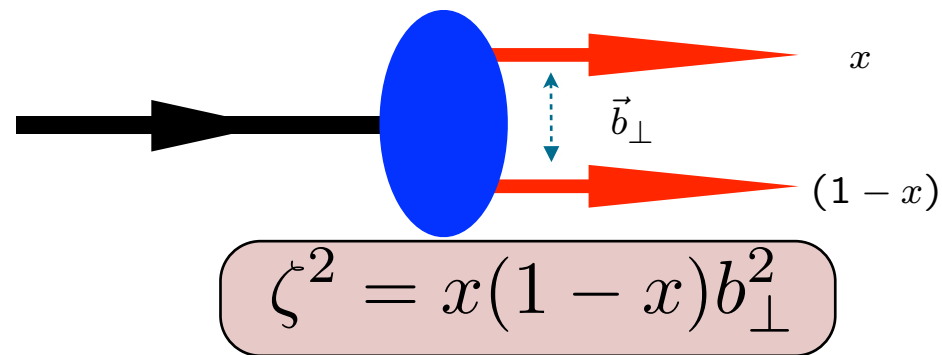
$$\left[ -\frac{d^2}{d\zeta^2} + \frac{1-4L^2}{4\zeta^2} + U(\zeta) \right] \psi(\zeta) = \mathcal{M}^2 \psi(\zeta)$$

**AdS/QCD:**

$$U(\zeta) = \kappa^4 \zeta^2 + 2\kappa^2 (L + S - 1)$$

*Semiclassical first approximation to QCD*

Fixed  $\tau = t + z/c$



*Coupled Fock states*

*Eliminate higher Fock states and retarded interactions*

*Effective two-particle equation*

*Azimuthal Basis*

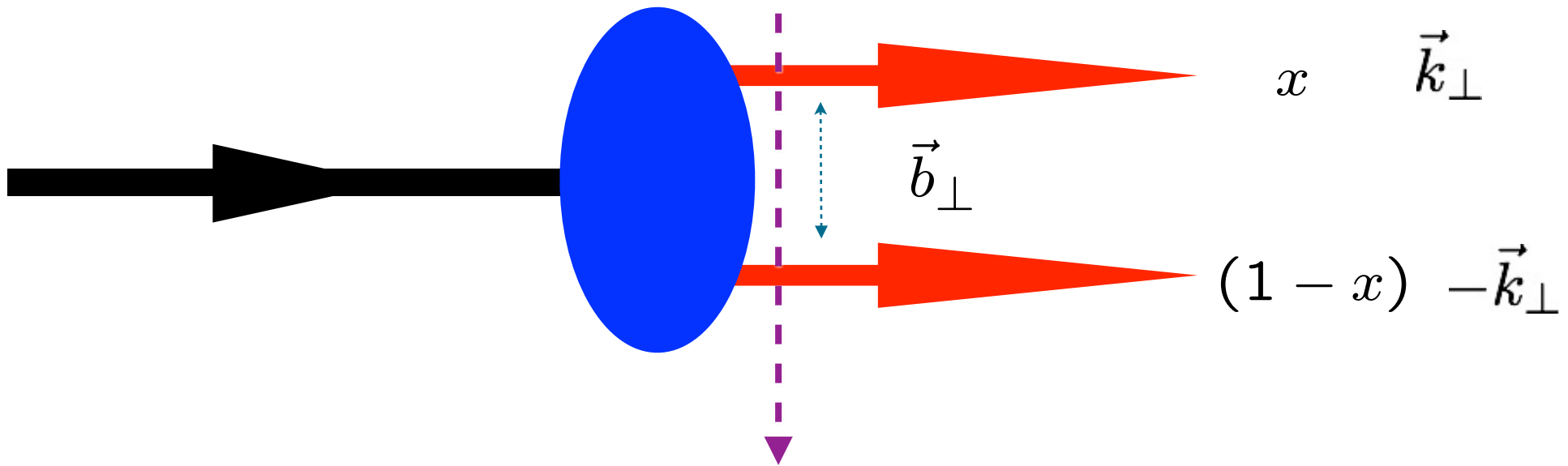
$$\zeta, \phi$$

$$m_q = 0$$

*Confining AdS/QCD potential!*

*Sums an infinite # diagrams*

Fixed  $\tau = t + z/c$



$$\zeta^2 \equiv b_{\perp}^2 x(1-x)$$

*Invariant transverse  
separation*

$$\zeta^2 \text{ conjugate to } \frac{k_{\perp}^2}{x(1-x)} = (p_q + p_{\bar{q}})^2 = \mathcal{M}_{q+\bar{q}}^2$$

$$\int dk^- \Psi_{BS}(P, k) \rightarrow \psi_{LF}(x, \vec{k}_{\perp})$$

# QCD Lagrangian

$$\mathcal{L}_{QCD} = -\frac{1}{4}\text{Tr}(G^{\mu\nu}G_{\mu\nu}) + \sum_{f=1}^{n_f} i\bar{\Psi}_f D_\mu \gamma^\mu \Psi_f + \sum_{f=1}^{n_f} m_f \bar{\Psi}_f \Psi_f$$

$$iD^\mu = i\partial^\mu - gA^\mu \quad G^{\mu\nu} = \partial^\mu A^\nu - \partial^\nu A^\mu - g[A^\mu, A^\nu]$$

**Classical Chiral Lagrangian is Conformally Invariant**

**Where does the QCD Mass Scale come from?**

**QCD does not know what MeV units mean!  
Only Ratios of Masses Determined**

● de Alfaro, Fubini, Furlan:

**Scale can appear in Hamiltonian and EQM  
without affecting conformal invariance of action!**

***Unique confinement potential!***



*Need a First Approximation to QCD*

*Comparable in simplicity to  
Schrödinger Theory in Atomic Physics*

**Relativistic, Frame-Independent, Color-Confining**

**Origin of hadronic mass scale if  $m_q=0$**

Semi-Classical Approximation to QCD

AdS/QCD  
Light-Front Holography  
BLFQ

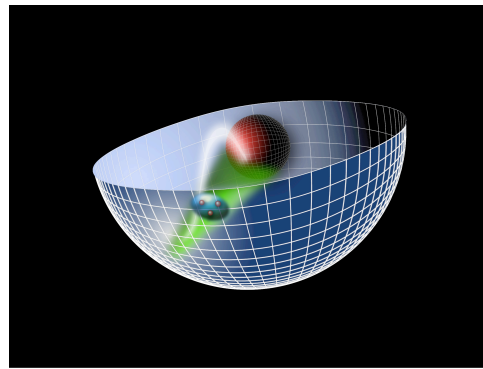
$\hbar \rightarrow 0$   
(Hoyer)

*AdS/QCD*

*Soft-Wall Model*

$$e^{\varphi(z)} = e^{+\kappa^2 z^2}$$

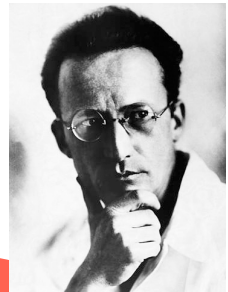
*Single scheme-independent  
fundamental mass scale*



$$\zeta^2 = x(1-x)b_{\perp}^2.$$

*Light-Front Holography*

$$\left[ -\frac{d^2}{d\zeta^2} + \frac{1-4L^2}{4\zeta^2} + U(\zeta) \right] \psi(\zeta) = \mathcal{M}^2 \psi(\zeta)$$



***Light-Front Schrödinger Equation***

$$U(\zeta) = \kappa^4 \zeta^2 + 2\kappa^2 (L + S - 1)$$

***Unique  
Confinement Potential!***

*Preserves Conformal Symmetry  
of the action*

***Confinement scale:***

$$\kappa \simeq 0.6 \text{ GeV}$$

$$1/\kappa \simeq 1/3 \text{ fm}$$

$$m_q = 0$$

● de Alfaro, Fubini, Furlan:

● Fubini, Rabinovici:

***Scale can appear in Hamiltonian and EQM  
without affecting conformal invariance of action!***

# Light-Front Schrödinger Equation

G. de Teramond, sjb

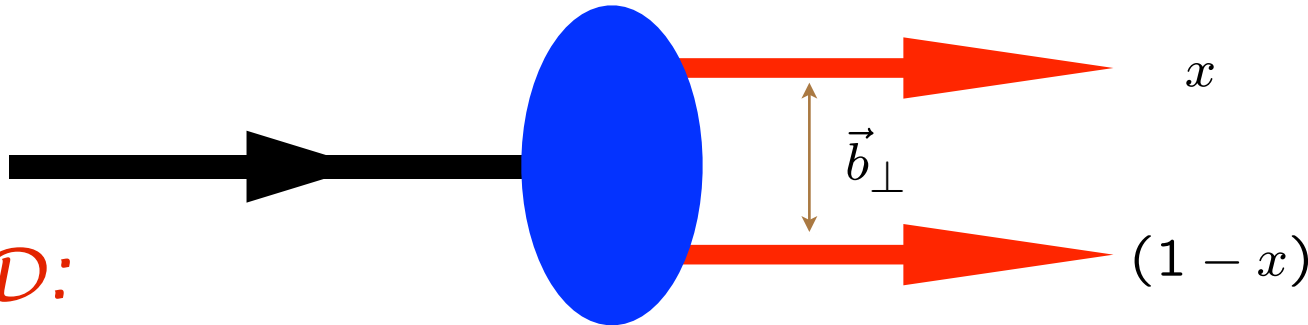
Relativistic LF single-variable radial  
equation for QCD & QED

Frame Independent!

$$\left[ -\frac{d^2}{d\zeta^2} + \frac{m^2}{x(1-x)} + \frac{-1 + 4L^2}{\zeta^2} + U(\zeta, S, L) \right] \psi_{LF}(\zeta) = M^2 \psi_{LF}(\zeta)$$

$$m_q \sim 0$$

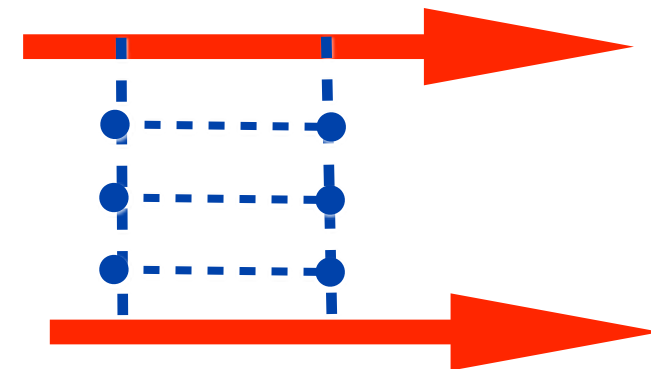
$$\zeta^2 = x(1-x)b_{\perp}^2.$$



*AdS/QCD:*

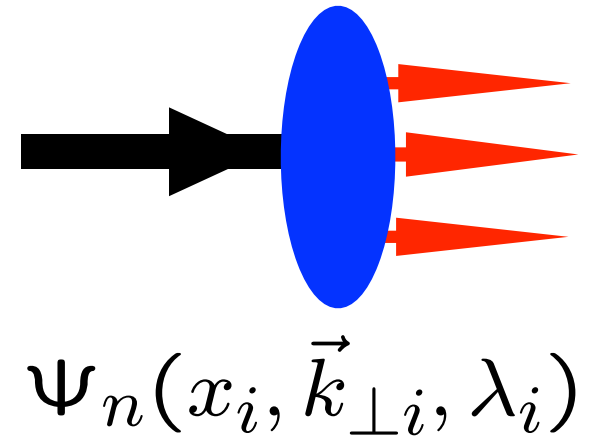
$$U(\zeta, S, L) = \kappa^2 \zeta^2 + \kappa^2 (L + S - 1/2)$$

**U is the exact QCD potential**  
**Conjecture: 'H'-diagrams generate U?**



# AdS/QCD and Light-Front Holography

- A first, semi-classical approximation to nonperturbative QCD
- Hadron Spectroscopy and LF Dynamics
- Color Confinement Potential
- Running QCD Coupling  $\alpha(Q^2)$  at All Scales  $Q^2$
- What sets the QCD Mass Scale?
- Connection of Hadron Masses to  $\Lambda_{\overline{MS}}$



# *Dilaton-Modified AdS/QCD*

$$ds^2 = e^{\varphi(z)} \frac{R^2}{z^2} (\eta_{\mu\nu} x^\mu x^\nu - dz^2)$$

- Soft-wall dilaton profile breaks conformal invariance

$$e^{\varphi(z)} = e^{+\kappa^2 z^2}$$

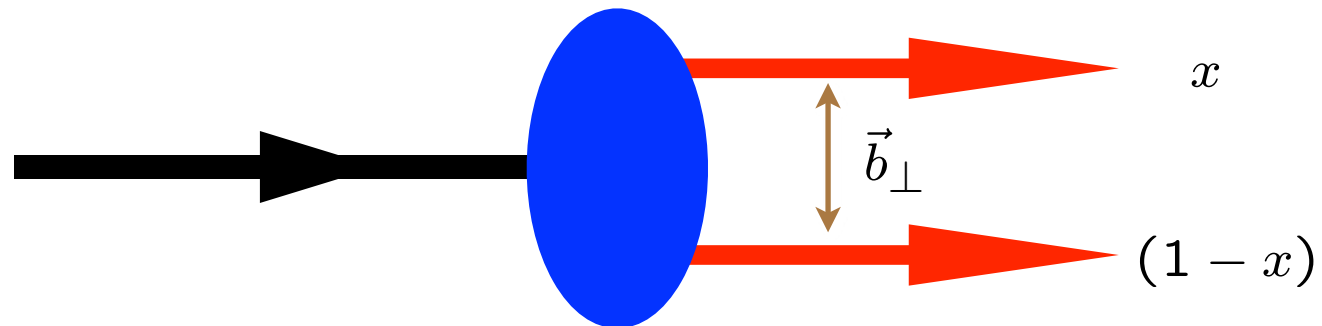
- Color Confinement
- Introduces confinement scale  $\kappa$

$$LF(3+1) \longleftrightarrow AdS_5$$

de Teramond, sjb

$$\psi(x, \vec{b}_\perp) \longleftrightarrow \phi(z)$$

$$\zeta = \sqrt{x(1-x)} \vec{b}_\perp^2 \longleftrightarrow z$$



$$\psi(x, \zeta) = \sqrt{x(1-x)} \zeta^{-1/2} \phi(\zeta)$$

*Light Front Holography: Unique mapping derived from equality of LF and AdS formula for EM and gravitational current matrix elements*

## Meson Spectrum in Soft Wall Model

*Pion: Negative term for  $J=0$  cancels positive terms from LFKÉ and potential*



- Effective potential:  $U(\zeta^2) = \kappa^4 \zeta^2 + 2\kappa^2(J - 1)$

- LF WE

$$\left( -\frac{d^2}{d\zeta^2} - \frac{1 - 4L^2}{4\zeta^2} + \kappa^4 \zeta^2 + 2\kappa^2(J - 1) \right) \phi_J(\zeta) = M^2 \phi_J(\zeta)$$

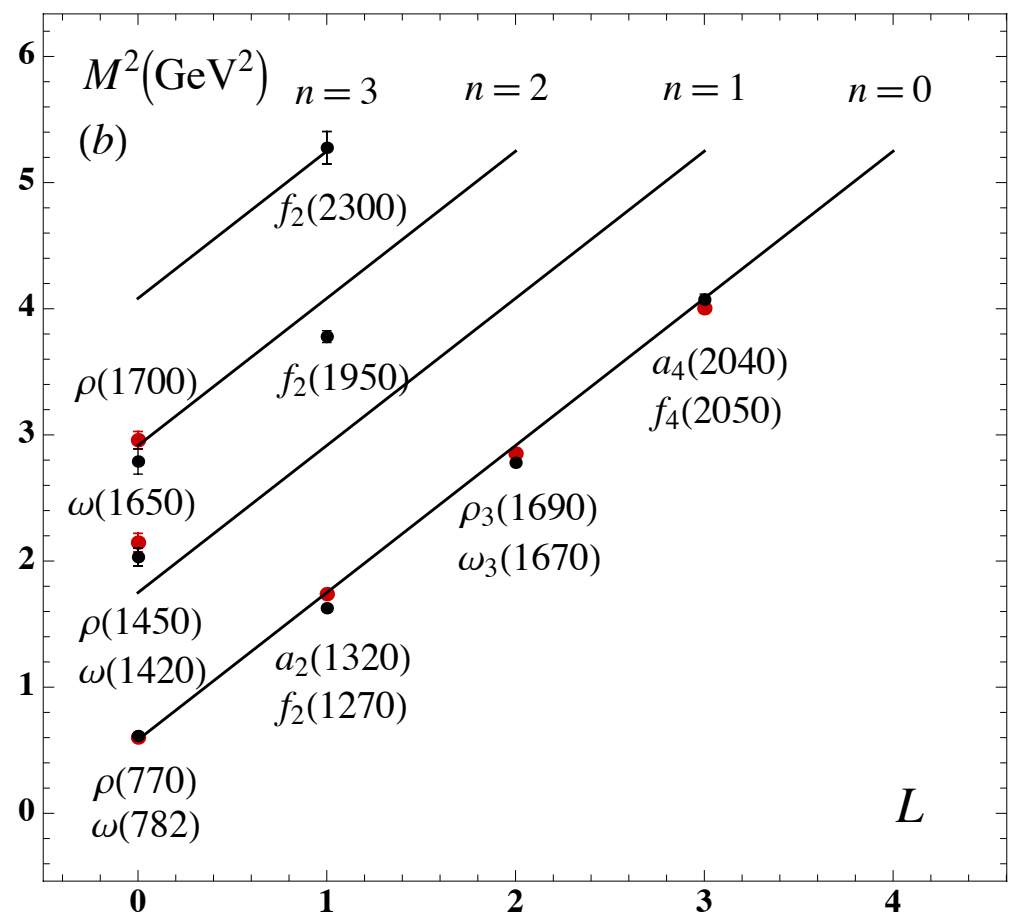
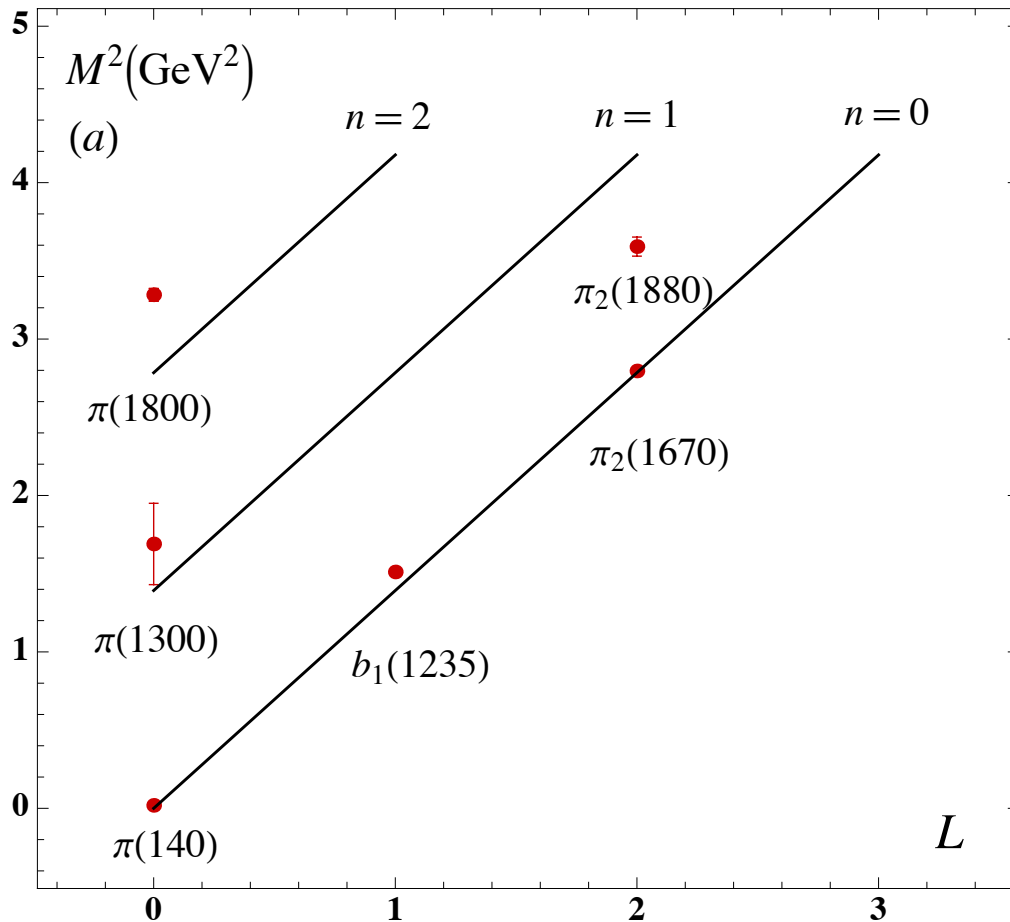
- Normalized eigenfunctions  $\langle \phi | \phi \rangle = \int d\zeta \phi^2(z)^2 = 1$

$$\phi_{n,L}(\zeta) = \kappa^{1+L} \sqrt{\frac{2n!}{(n+L)!}} \zeta^{1/2+L} e^{-\kappa^2 \zeta^2 / 2} L_n^L(\kappa^2 \zeta^2)$$

- Eigenvalues

$$\mathcal{M}_{n,J,L}^2 = 4\kappa^2 \left( n + \frac{J+L}{2} \right)$$

# Prediction from AdS/QCD

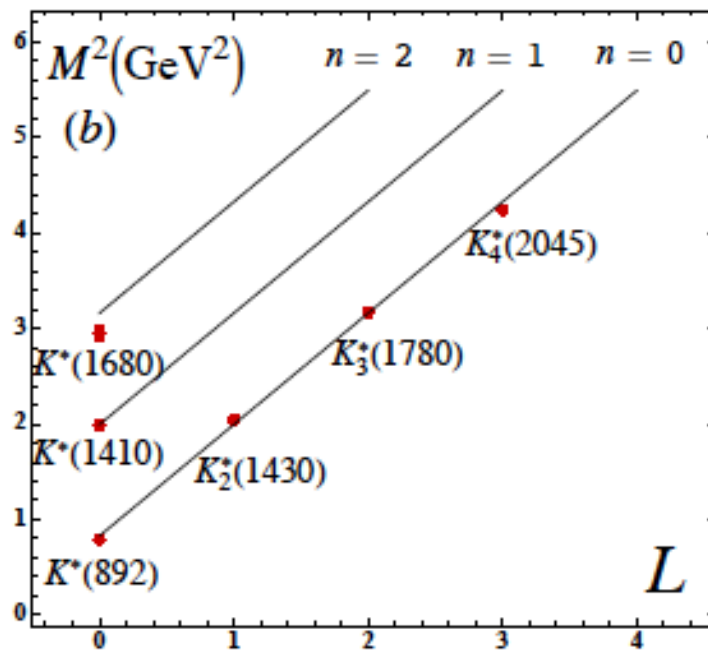
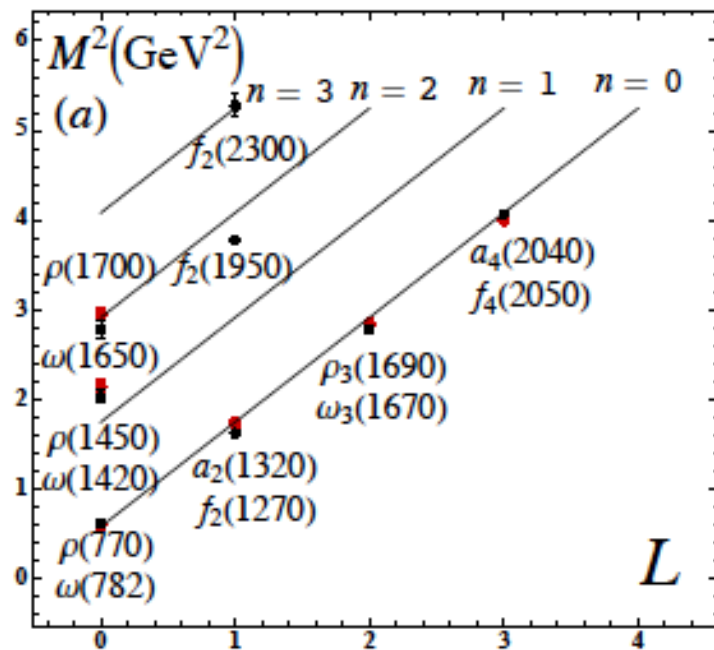
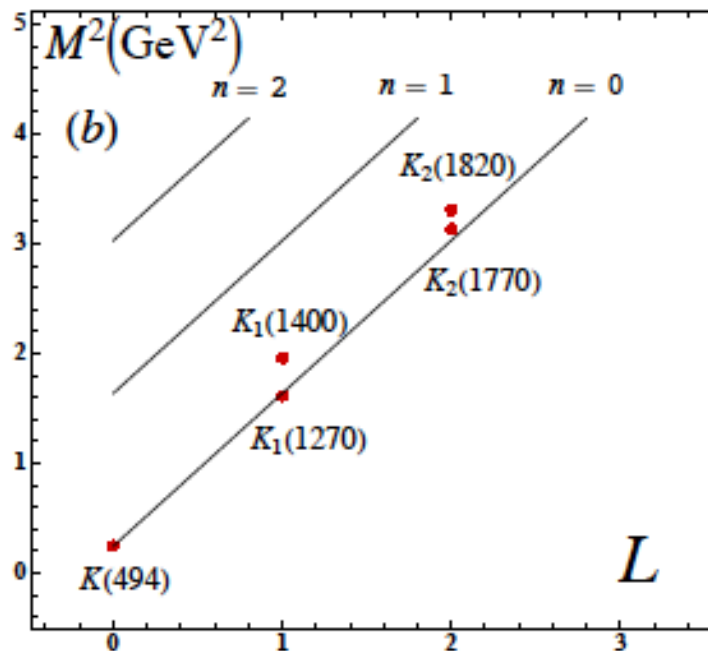
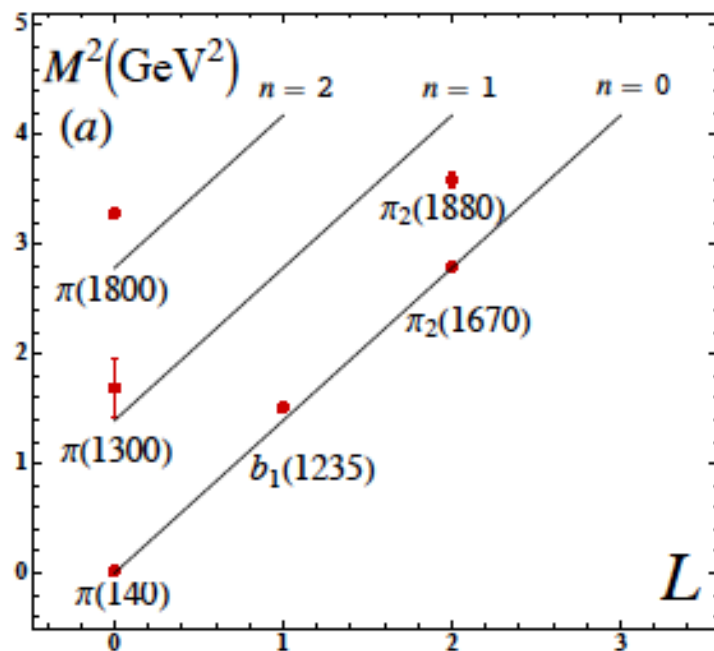


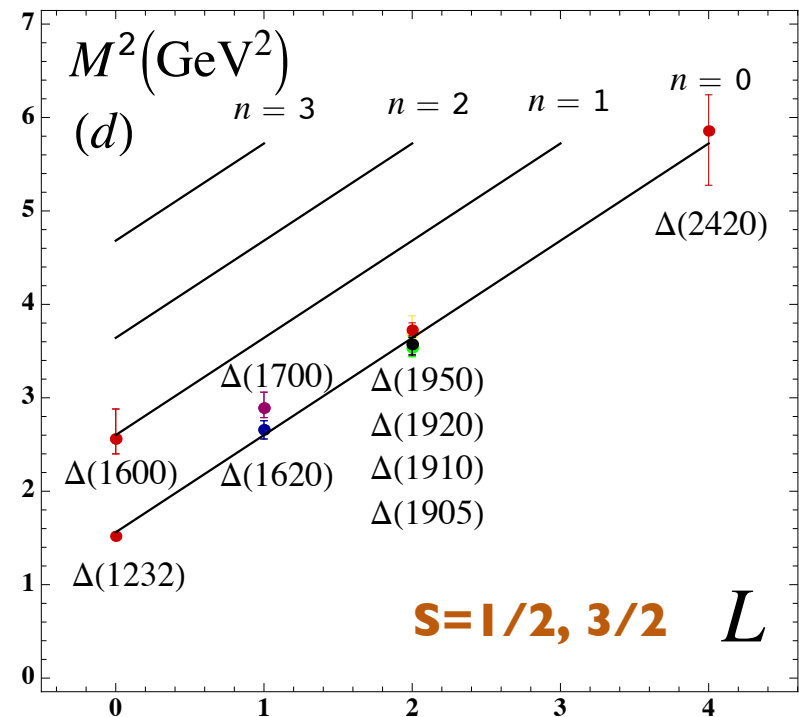
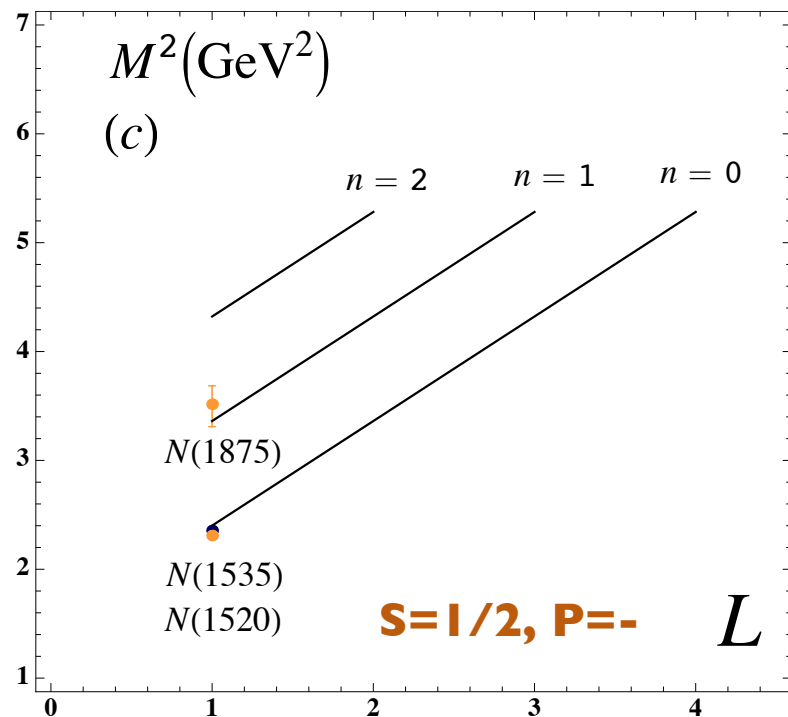
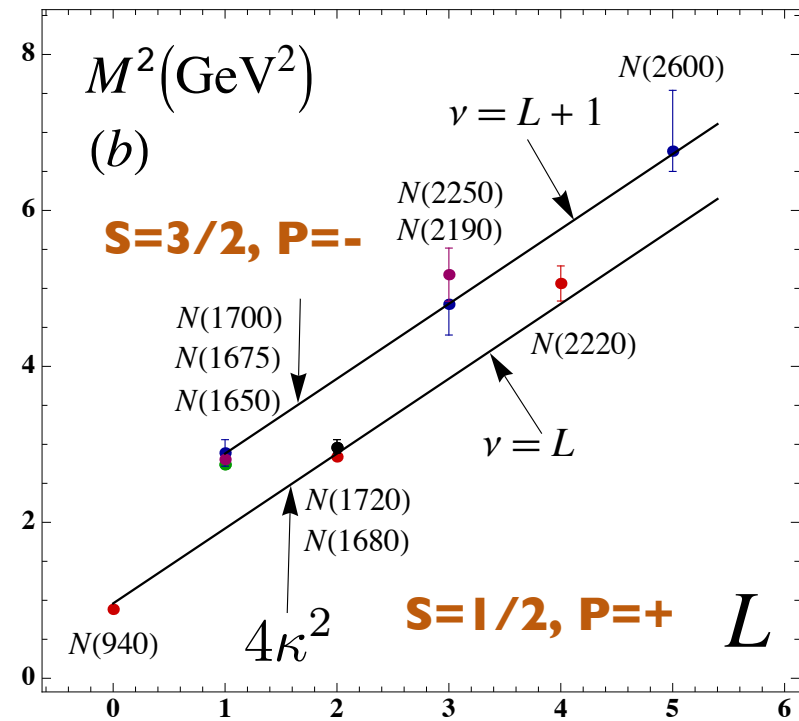
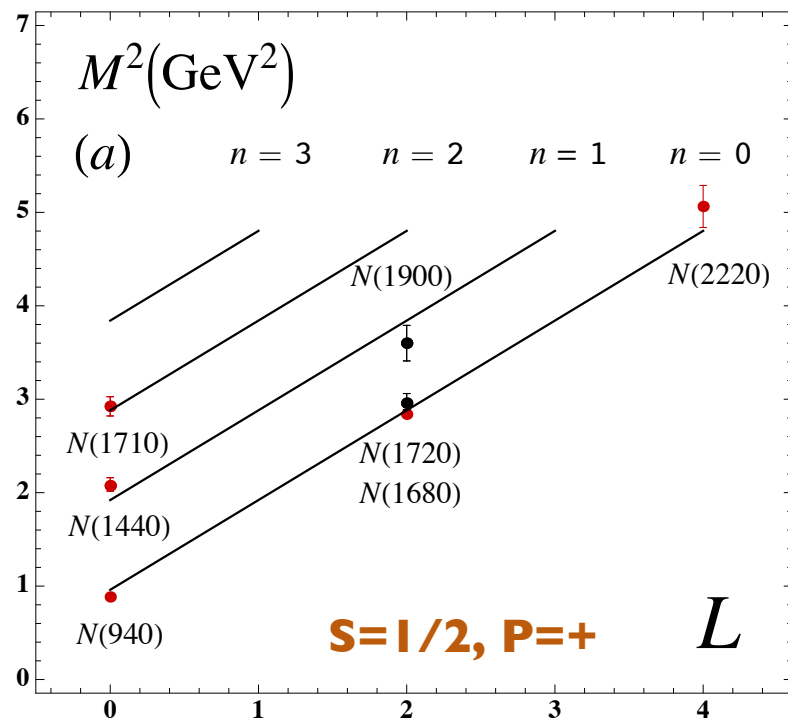
$$m_u = m_d = 0$$

$$M^2(n, L, S) = 4\kappa^2(n + L + S/2)$$



$$M^2 = M_0^2 + \left\langle X \left| \frac{m_q^2}{x} \right| X \right\rangle + \left\langle X \left| \frac{m_{\bar{q}}^2}{1-x} \right| X \right\rangle$$





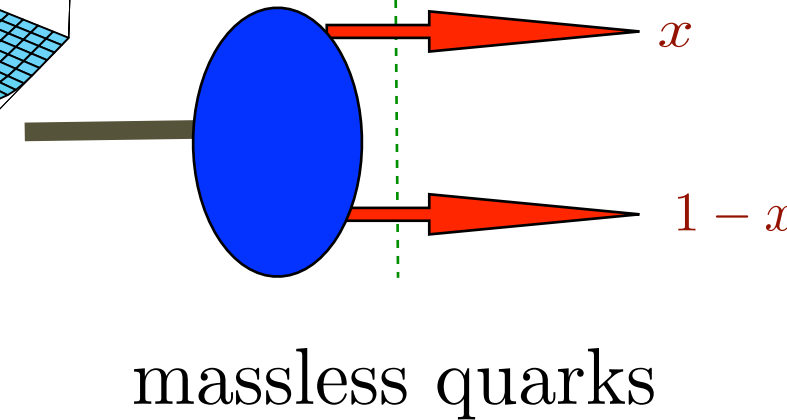
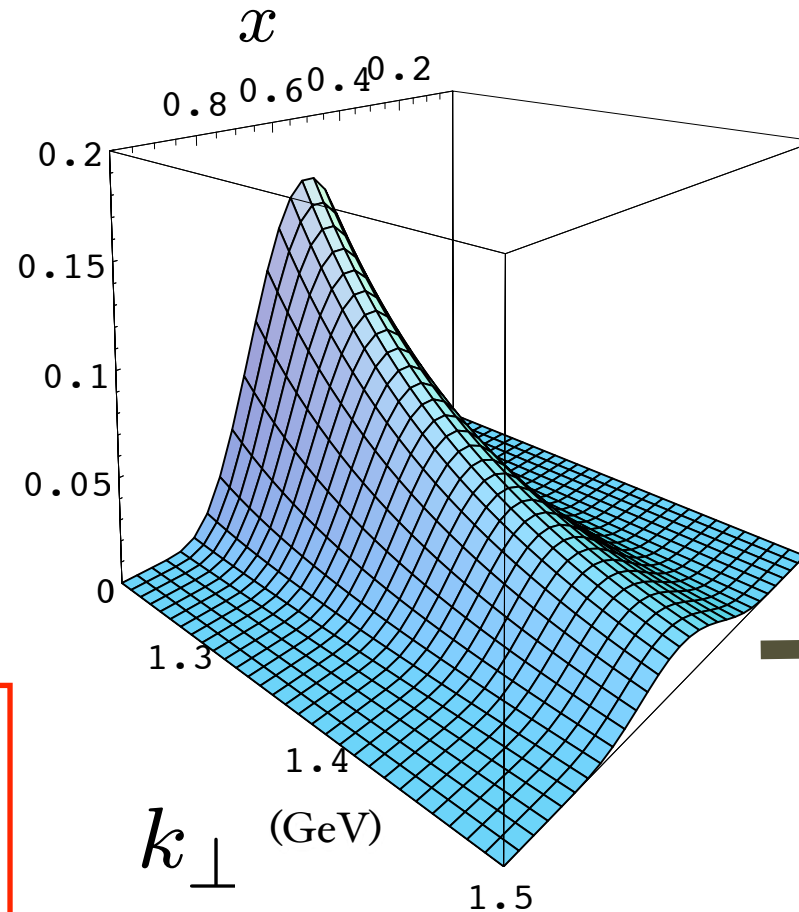
# Prediction from AdS/QCD: Meson LFWF

$$e^{\varphi(z)} = e^{+\kappa^2 z}$$

de Teramond,  
Cao, sjb

“Soft Wall”  
model

$$\psi_M(x, k_\perp^2)$$



**Note coupling**

$$k_\perp^2, x$$

$$\psi_M(x, k_\perp) = \frac{4\pi}{\kappa \sqrt{x(1-x)}} e^{-\frac{k_\perp^2}{2\kappa^2 x(1-x)}}$$

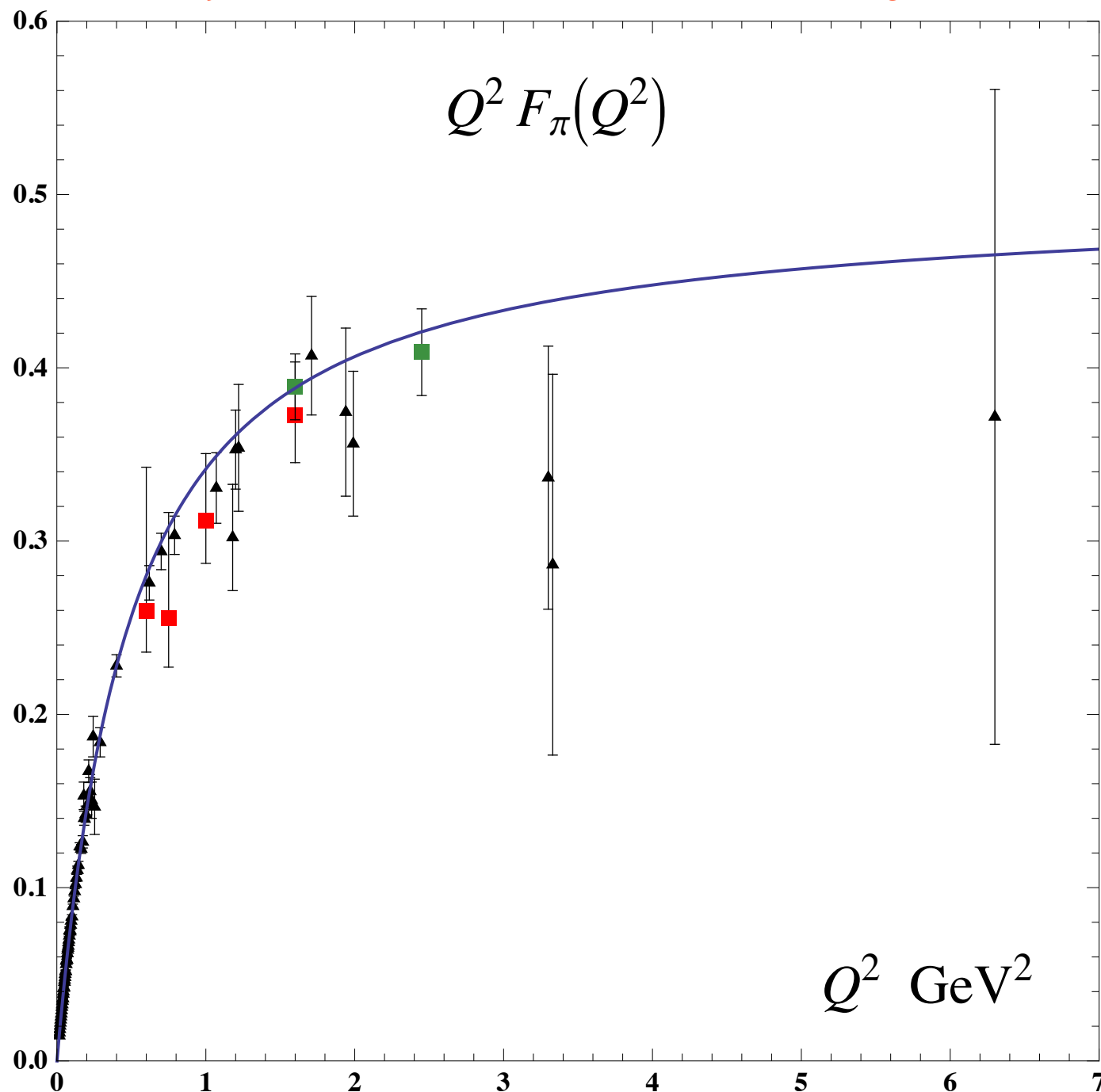
$$f_\pi = \sqrt{P_{q\bar{q}}} \frac{\sqrt{3}}{8} \kappa = 92.4 \text{ MeV}$$

$$\phi_\pi(x) = \frac{4}{\sqrt{3}\pi} f_\pi \sqrt{x(1-x)}$$

**Same as DSE!**

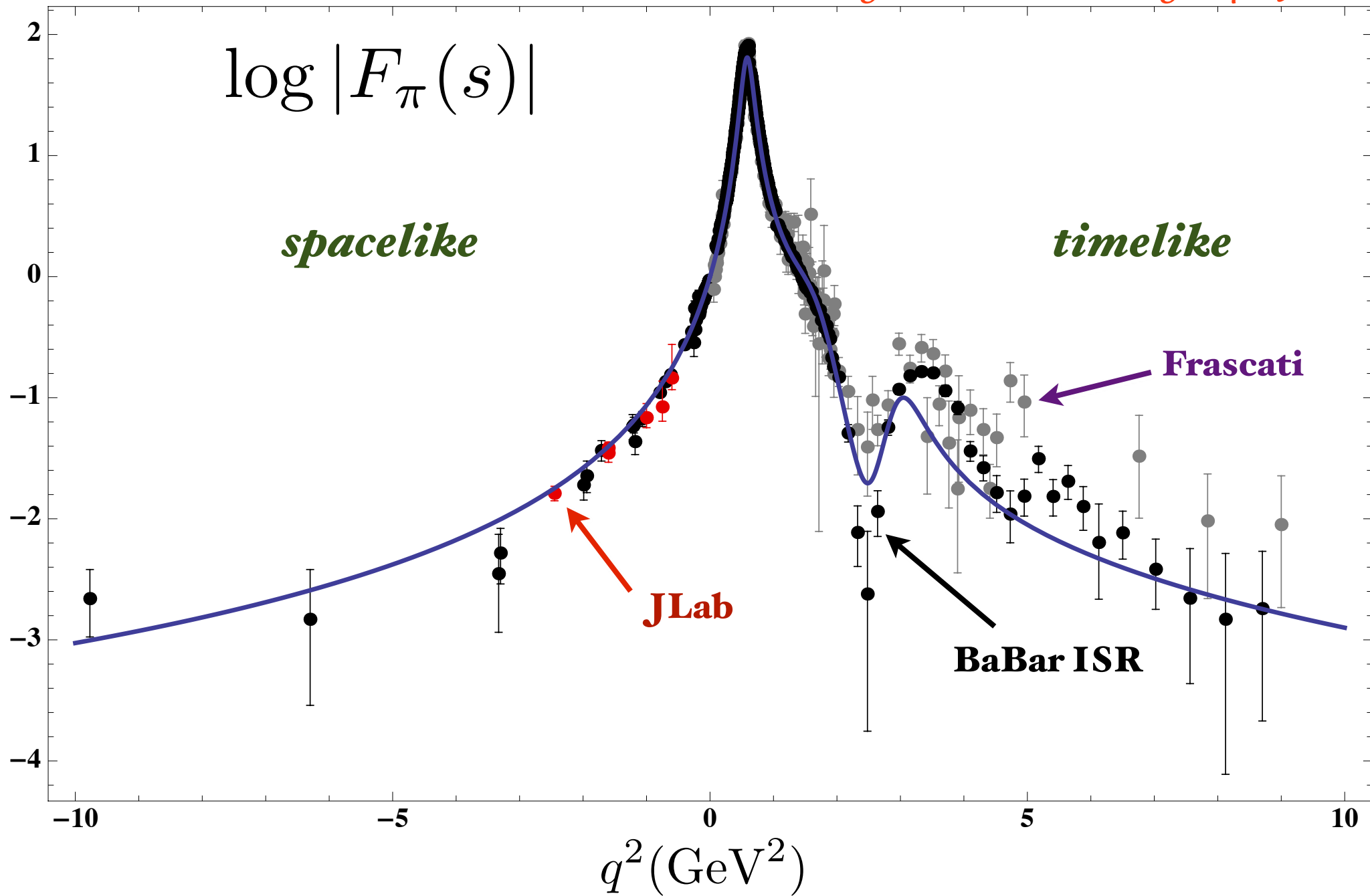
*Provides Connection of Confinement to Hadron Structure*

*Pion Form Factor predicted from AdS/QCD and Light-Front Holography*

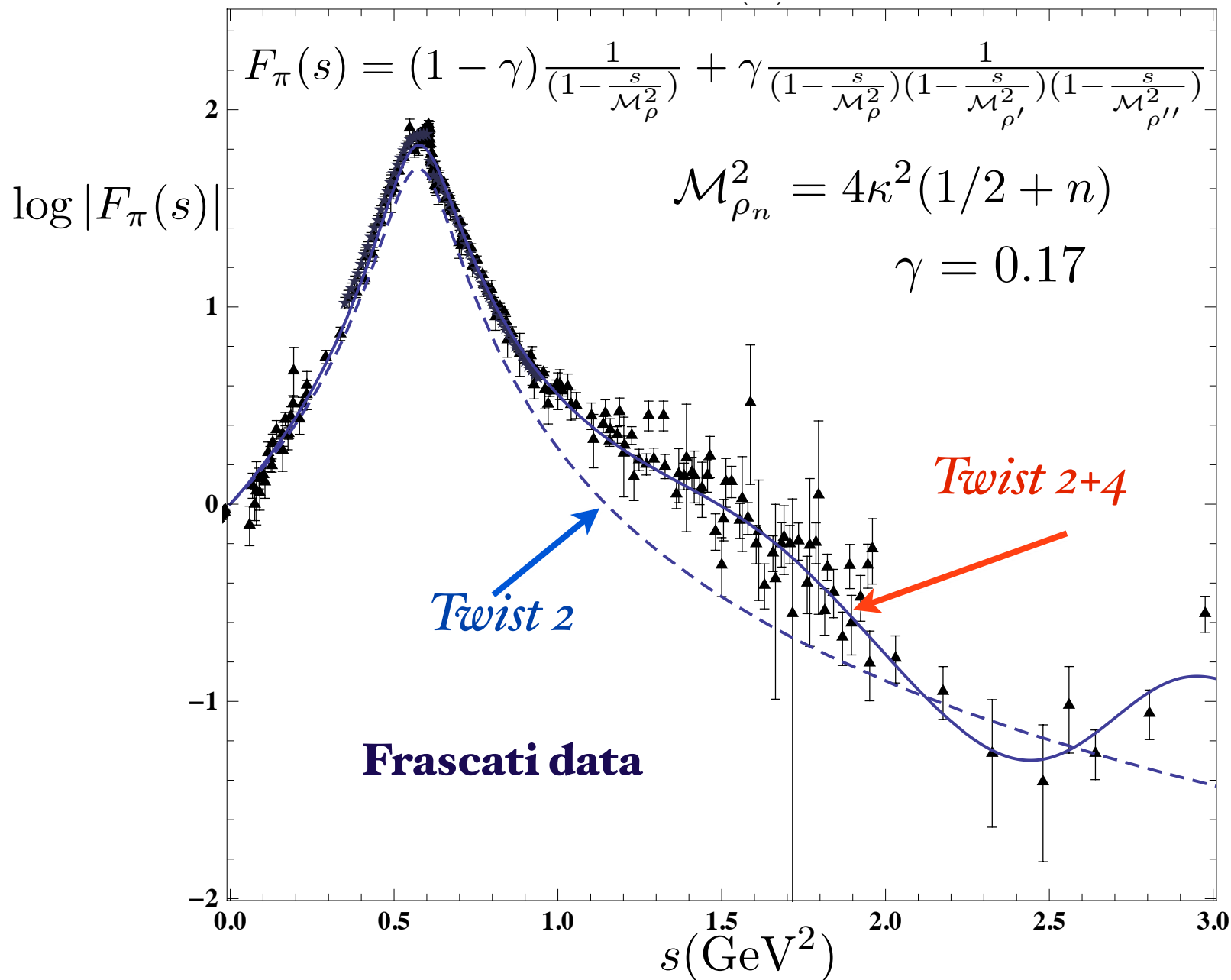


Counting Rules from Leading Twist Obeyed

# Pion Form Factor from AdS/QCD and Light-Front Holography



# Timelike Pion Form Factor from AdS/QCD and Light-Front Holography



*Prescription for  
Timelike poles :*

$$\frac{1}{s - M^2 + i\sqrt{s}\Gamma}$$

**14% four-quark  
probability**

- Compute Dirac proton form factor using SU(6) flavor symmetry

$$F_1^p(Q^2) = R^4 \int \frac{dz}{z^4} V(Q, z) \Psi_+^2(z)$$

- Nucleon AdS wave function

$$\Psi_+(z) = \frac{\kappa^{2+L}}{R^2} \sqrt{\frac{2n!}{(n+L)!}} z^{7/2+L} L_n^{L+1}(\kappa^2 z^2) e^{-\kappa^2 z^2/2}$$

- Normalization ( $F_1^p(0) = 1$ ,  $V(Q=0, z) = 1$ )

$$R^4 \int \frac{dz}{z^4} \Psi_+^2(z) = 1$$

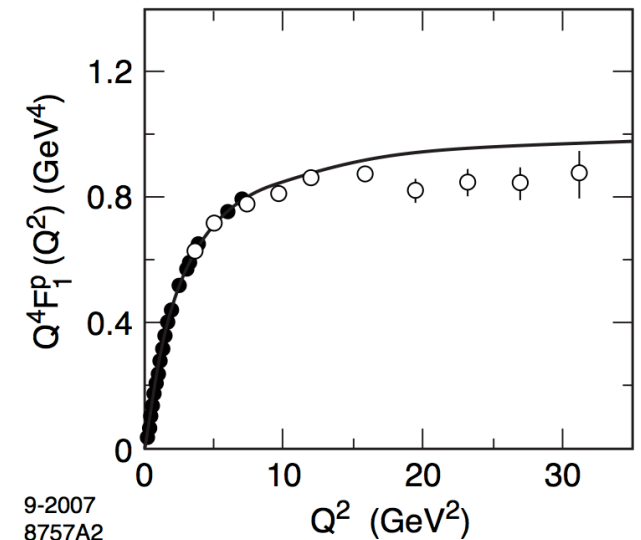
- Bulk-to-boundary propagator [Grigoryan and Radyushkin (2007)]

$$V(Q, z) = \kappa^2 z^2 \int_0^1 \frac{dx}{(1-x)^2} x^{\frac{Q^2}{4\kappa^2}} e^{-\kappa^2 z^2 x/(1-x)}$$

- Find

$$F_1^p(Q^2) = \frac{1}{\left(1 + \frac{Q^2}{\mathcal{M}_{\rho}^2}\right) \left(1 + \frac{Q^2}{\mathcal{M}_{\rho'}^2}\right)}$$

with  $\mathcal{M}_{\rho_n}^2 \rightarrow 4\kappa^2(n + 1/2)$



# AdS/QCD Holographic Wave Function for the $\rho$ Meson and Diffractive $\rho$ Meson Electroproduction

J. R. Forshaw<sup>\*</sup>

*Consortium for Fundamental Physics, School of Physics and Astronomy, University of Manchester,  
Oxford Road, Manchester M13 9PL, United Kingdom*

R. Sandapen<sup>†</sup>

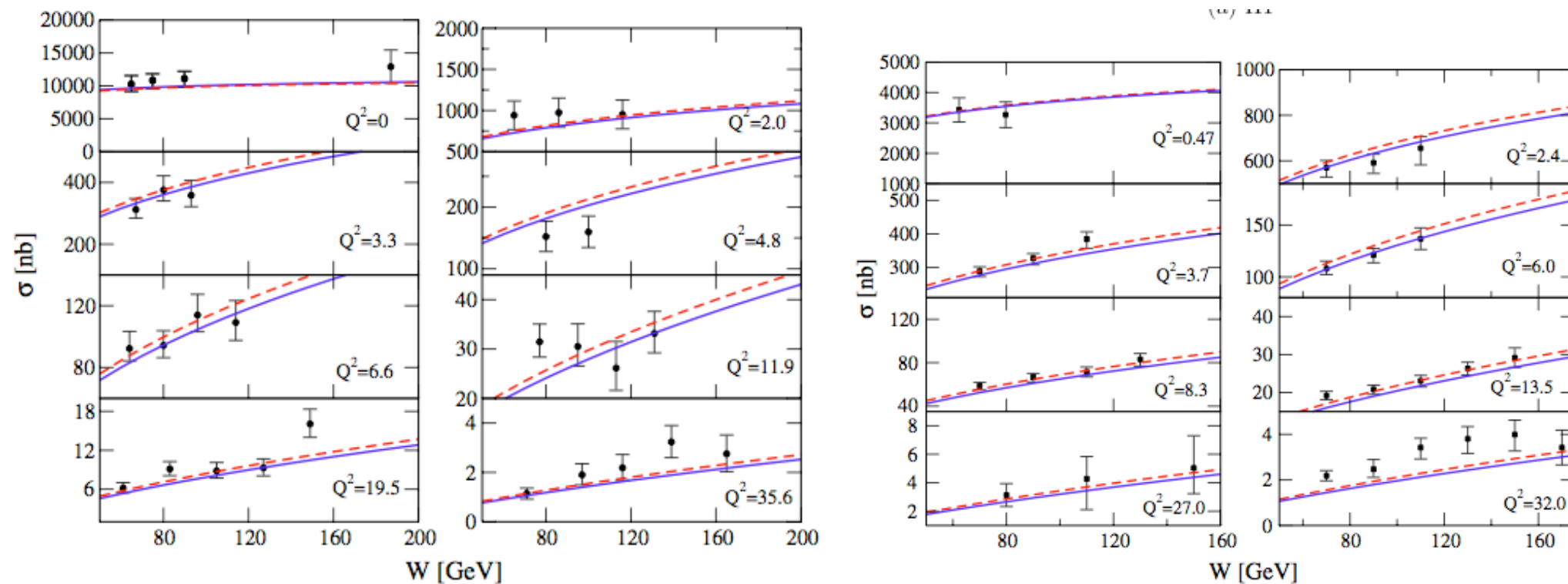
*Département de Physique et d'Astronomie, Université de Moncton, Moncton, New Brunswick E1A3E9, Canada*  
(Received 5 April 2012; published 20 August 2012)

We show that anti-de Sitter/quantum chromodynamics generates predictions for the rate of diffractive  $\rho$ -meson electroproduction that are in agreement with data collected at the Hadron Electron Ring Accelerator electron-proton collider.

$$\psi_M(x, k_\perp) = \frac{4\pi}{\kappa \sqrt{x(1-x)}} e^{-\frac{k_\perp^2}{2\kappa^2 x(1-x)}}$$



# AdS/QCD Holographic Wave Function for the $\rho$ Meson and Diffractive $\rho$ Meson Electroproduction

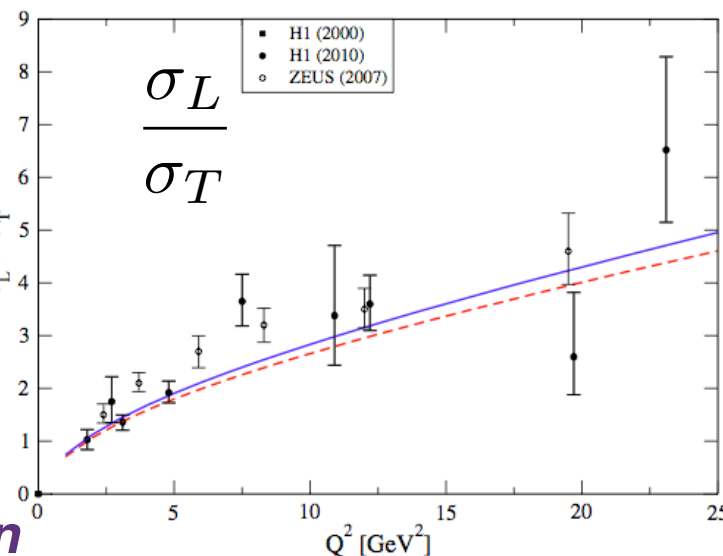


(b) ZEUS

**J. R. Forshaw,  
R. Sandapen**

$$\gamma^* p \rightarrow \rho^0 p'$$

**Nuclear effects:  
Sergey Gevorkyan**



*Prediction from  
Light-Front Holography*

$$\psi_M(x, k_\perp) = \frac{4\pi}{\kappa \sqrt{x(1-x)}} e^{-\frac{k_\perp^2}{2\kappa^2 x(1-x)}}$$

$$\left( -\partial_{\zeta}^2 + \kappa^4 \zeta^2 + 2\kappa^2(L_B + 1) + \frac{4L_B^2 - 1}{4\zeta^2} \right) \psi_J^+ = M^2 \psi_J^+ \quad \text{G}_{22}$$

$$\left( -\partial_{\zeta}^2 + \kappa^4 \zeta^2 + 2\kappa^2 L_B + \frac{4(L_B + 1)^2 - 1}{4\zeta^2} \right) \psi_J^- = M^2 \psi_J^- \quad \text{G}_{11}$$

$$M^2(n, L_B) = 4\kappa^2(n + L_B + 1)$$

**S=1/2, P=+**

*both chiralities*

## Meson Equation

$$\left( -\partial_{\zeta}^2 + \kappa^4 \zeta^2 + 2\kappa^2(J - 1) + \frac{4L_M^2 - 1}{4\zeta^2} \right) \phi_J = M^2 \phi_J \quad \text{G}_{11}$$

$$M^2(n, L_M) = 4\kappa^2(n + L_M)$$

*Same  $\kappa$ !*

**S=0, I=I Meson is superpartner of S=1/2, I=I Baryon**

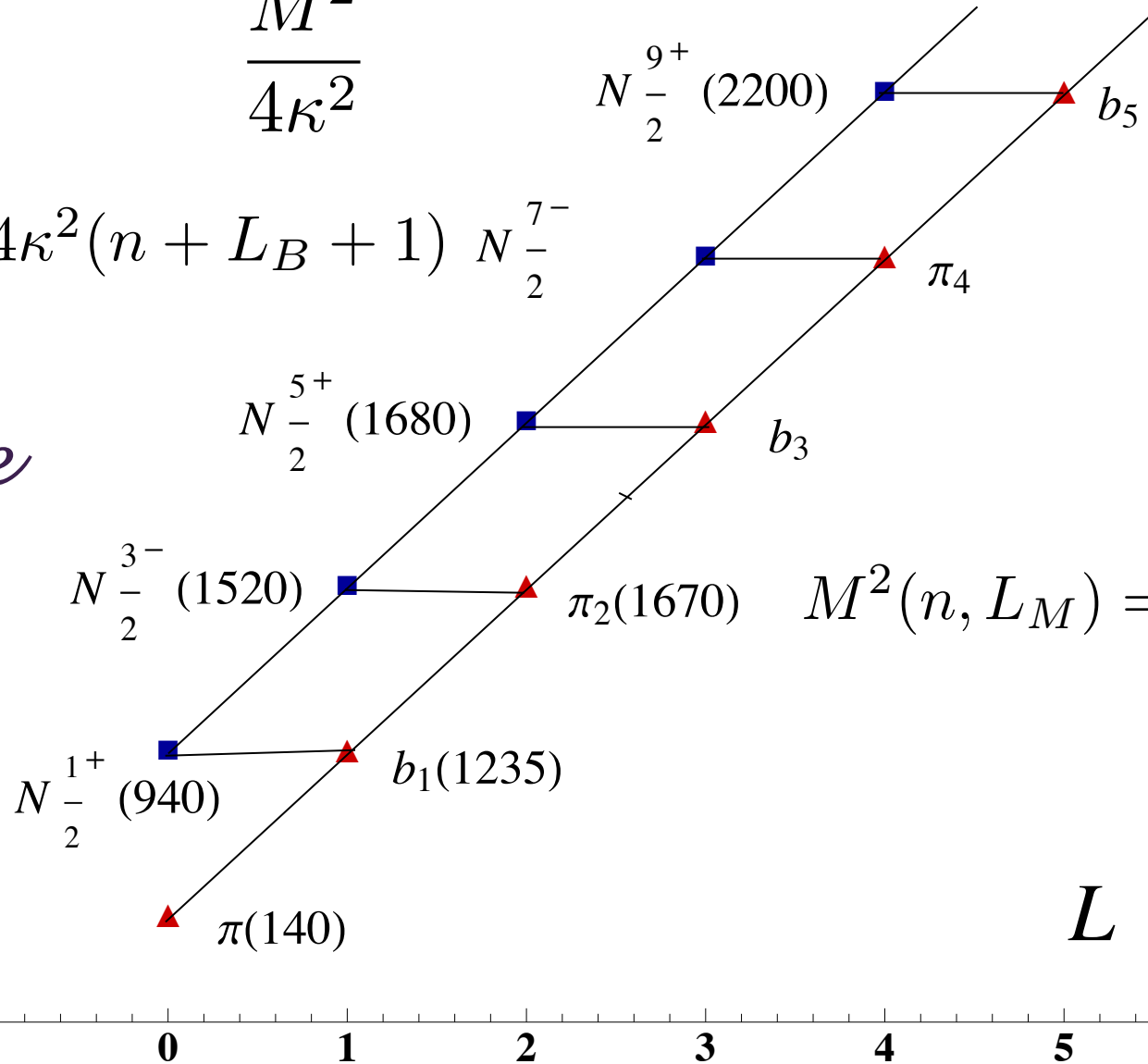
**Meson-Baryon Degeneracy for  $L_M = L_B + 1$**

# Superconformal Algebra

$$\frac{M^2}{4\kappa^2}$$

$$M^2(n, L_B) = 4\kappa^2(n + L_B + 1)$$

*Same slope*



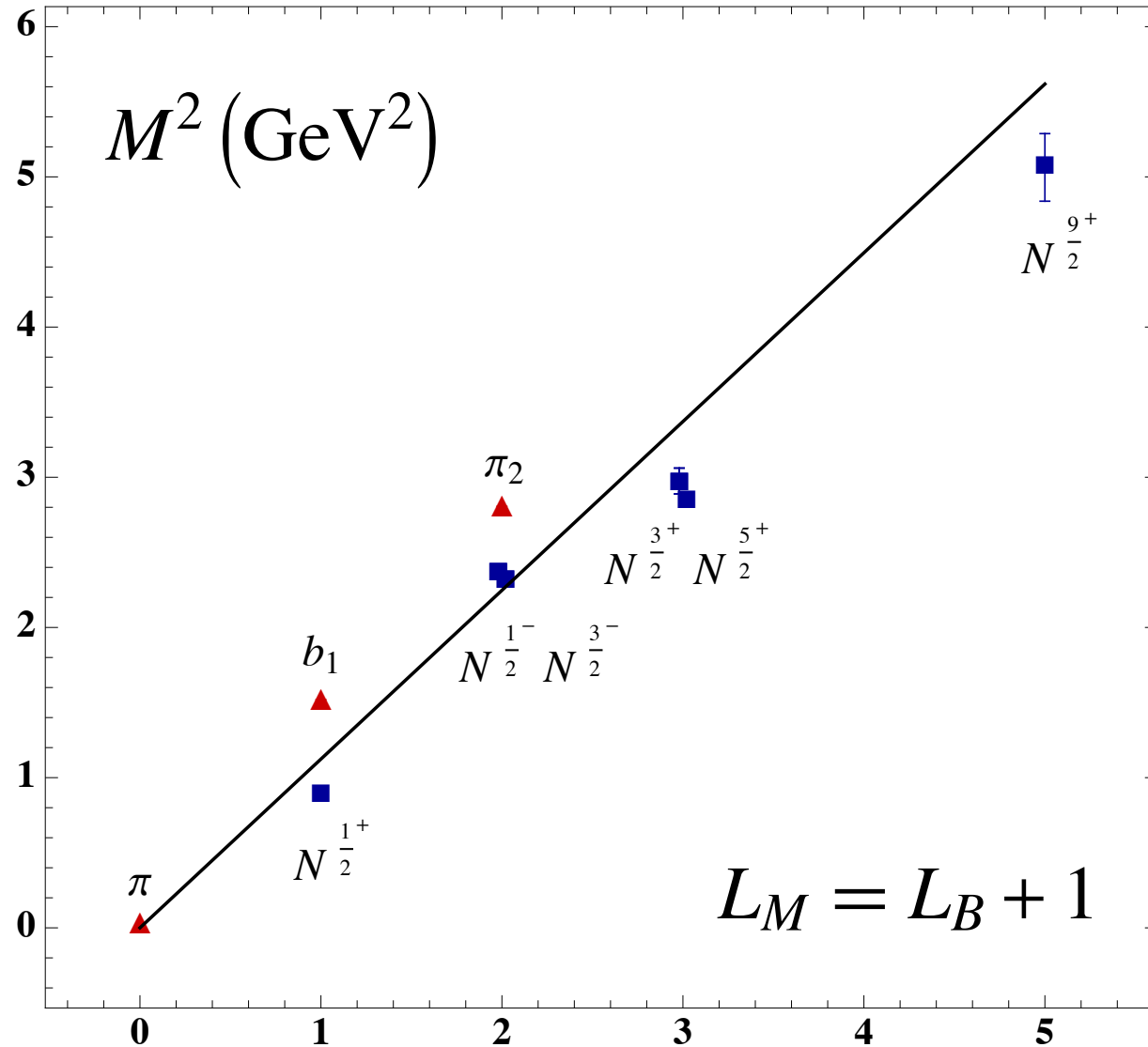
$$M^2(n, L_M) = 4\kappa^2(n + L_M)$$

$L$

**Meson-Baryon  
Mass Degeneracy  
for  $L_M=L_B+1$**

**Dosch, de Teramond, sjb**

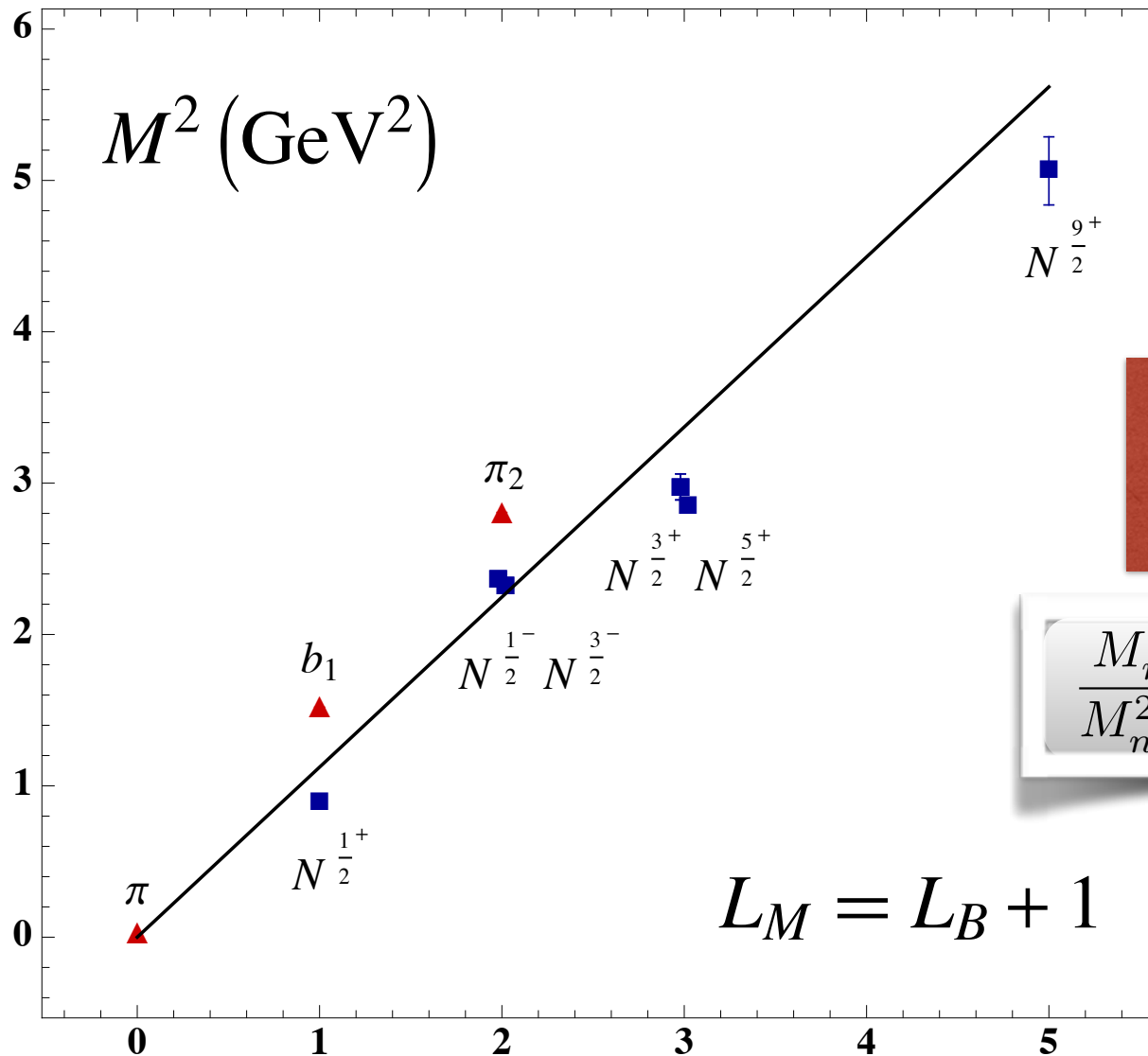
# Superconformal AdS Light-Front Holographic QCD (LFHQCD): Identical meson and baryon spectra!



**Meson-Baryon  
Mass Degeneracy  
for  $L_M = L_B + 1$**

**$S=0, I=I$  Meson is superpartner of  $S=I/2, I=I$  Baryon**

# Superconformal AdS Light-Front Holographic QCD (LFHQCD): Identical meson and baryon spectra!



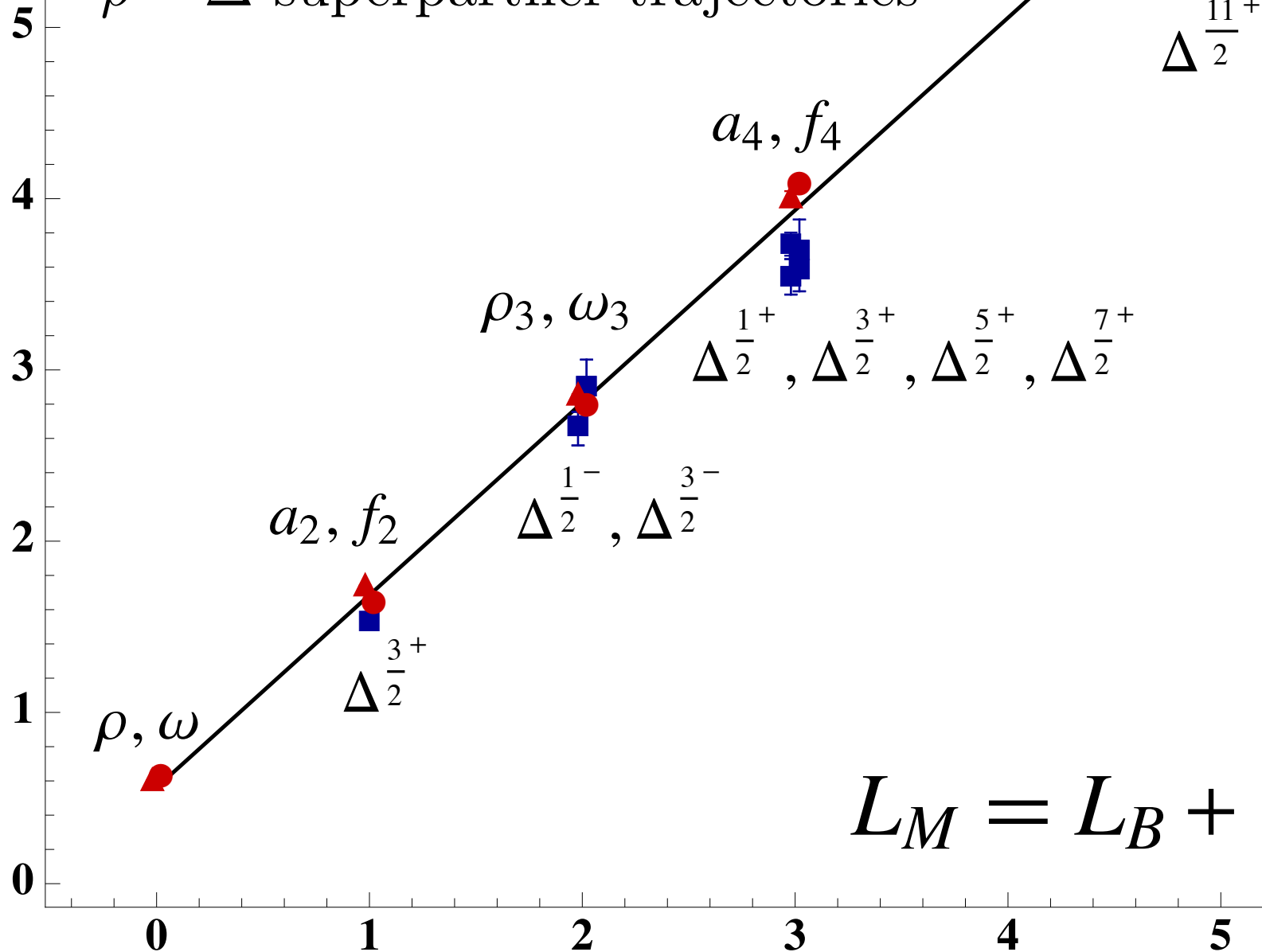
**Meson-Baryon  
Mass Degeneracy  
for  $L_M = L_B + 1$**

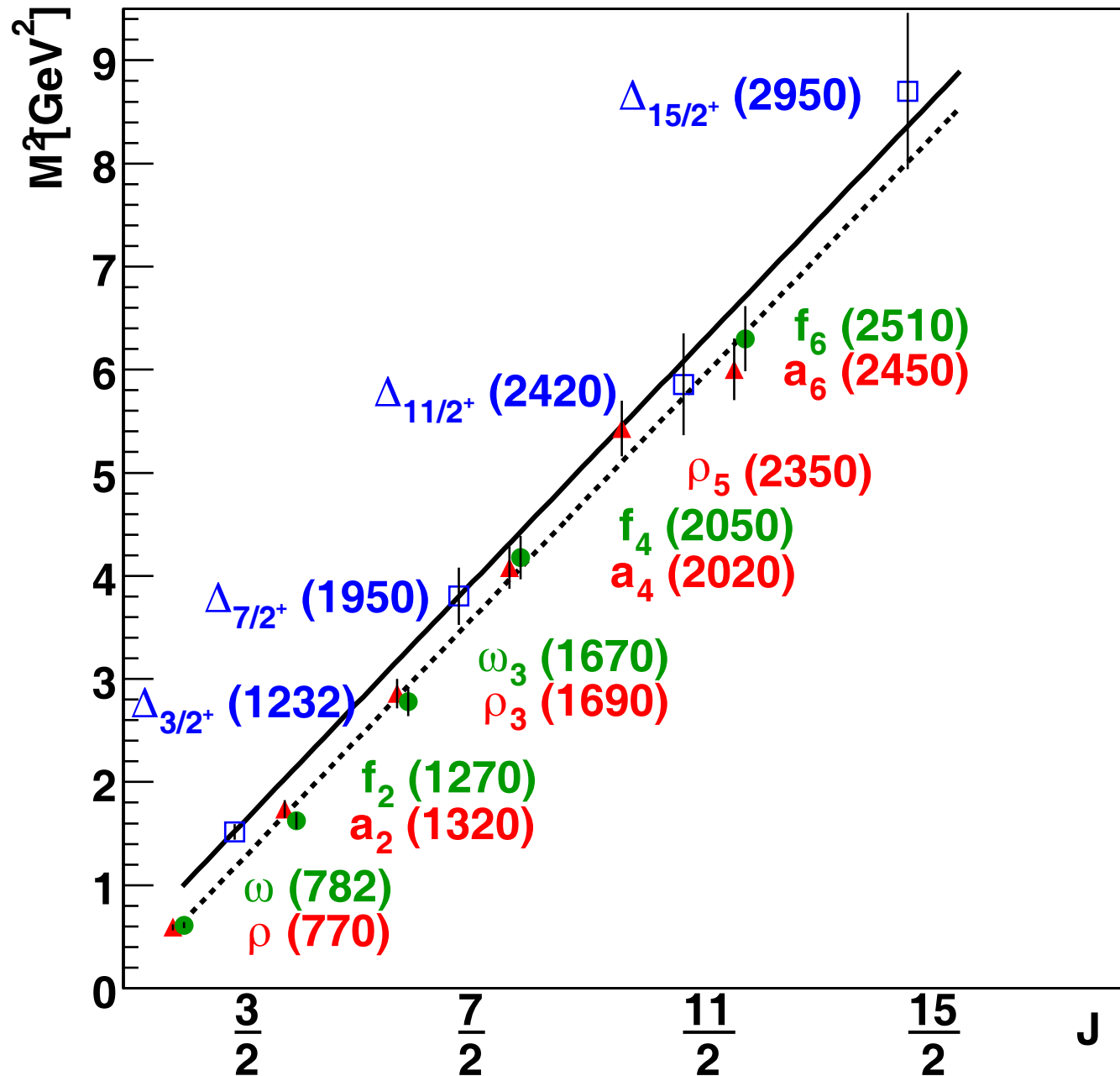
$$\frac{M_{meson}^2}{M_{nucleon}^2} = \frac{n + L_M}{n + L_B + 1}$$

**$S=0, I=I$  Meson is superpartner of  $S=1/2, I=I$  Baryon**

$M^2 \text{ (GeV}^2\text{)}$

$\rho - \Delta$  superpartner trajectories





The leading Regge trajectory:  $\Delta$  resonances with maximal  $J$  in a given mass range.  
Also shown is the Regge trajectory for mesons with  $J = L + S$ .

# Some Features of AdS/QCD

- *Regge spectroscopy—same slope in  $n, L$  for mesons,*
- *Chiral features for  $m_q=0$ :  $m_\pi=0$ , chiral-invariant proton*
- *Hadronic LFWFs : Single dynamical LF radial variable  $\xi$*
- *Counting Rules*
- *Connection between hadron masses and  $\Lambda_{\overline{MS}}$*

**Superconformal AdS Light-Front Holographic QCD (LFHQCD)**  
**Meson-Baryon Mass Degeneracy for  $L_M=L_B+1$**



Bjorken sum rule defines effective charge

$$\alpha_{g1}(Q^2)$$

$$\int_0^1 dx [g_1^{ep}(x, Q^2) - g_1^{en}(x, Q^2)] \equiv \frac{g_a}{6} \left[ 1 - \frac{\alpha_{g1}(Q^2)}{\pi} \right]$$

- **Can be used as standard QCD coupling**
- **Well measured**
- **Asymptotic freedom at large  $Q^2$**
- **Computable at large  $Q^2$  in any pQCD scheme**
- **Universal  $\beta_0, \beta_1$**

$$\alpha_s^{AdS}(Q)/\pi = e^{-Q^2/4\kappa^2}$$

# Running Coupling from Modified AdS/QCD

Deur, de Teramond, sjb

- Consider five-dim gauge fields propagating in  $\text{AdS}_5$  space in dilaton background  $\varphi(z) = \kappa^2 z^2$

$$S = -\frac{1}{4} \int d^4x dz \sqrt{g} e^{\varphi(z)} \frac{1}{g_5^2} G^2$$

- Flow equation

$$\frac{1}{g_5^2(z)} = e^{\varphi(z)} \frac{1}{g_5^2(0)} \quad \text{or} \quad g_5^2(z) = e^{-\kappa^2 z^2} g_5^2(0)$$

where the coupling  $g_5(z)$  incorporates the non-conformal dynamics of confinement

- YM coupling  $\alpha_s(\zeta) = g_{YM}^2(\zeta)/4\pi$  is the five dim coupling up to a factor:  $g_5(z) \rightarrow g_{YM}(\zeta)$
- Coupling measured at momentum scale  $Q$

$$\alpha_s^{AdS}(Q) \sim \int_0^\infty \zeta d\zeta J_0(\zeta Q) \alpha_s^{AdS}(\zeta)$$

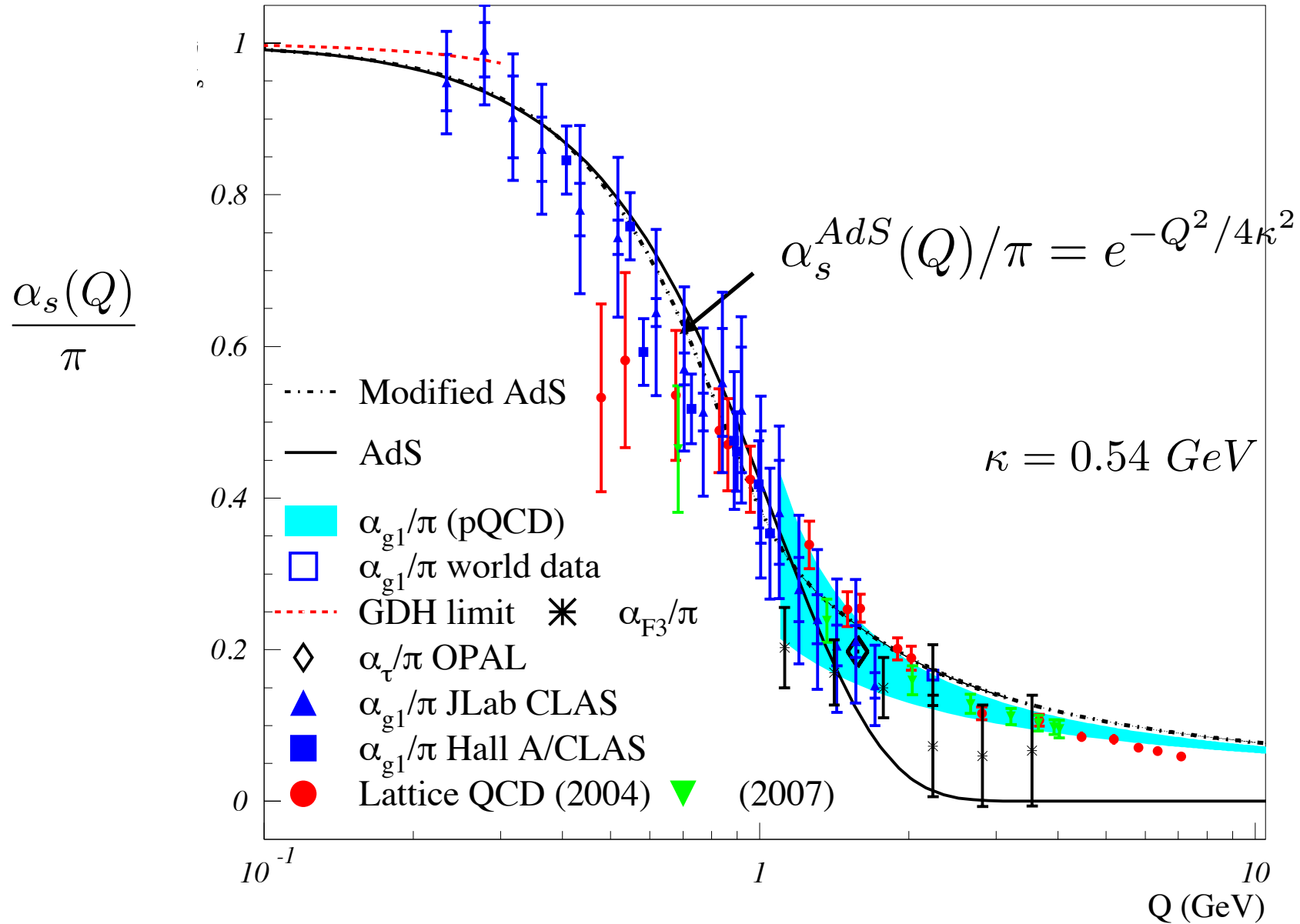
- Solution

$$\alpha_s^{AdS}(Q^2) = \alpha_s^{AdS}(0) e^{-Q^2/4\kappa^2}.$$

where the coupling  $\alpha_s^{AdS}$  incorporates the non-conformal dynamics of confinement

# Running Coupling from Light-Front Holography and AdS/QCD

**Analytic, defined at all scales, IR Fixed Point**



**AdS/QCD dilaton captures the higher twist corrections to effective charges for  $Q < 1 \text{ GeV}$**

$$e^{\varphi} = e^{+\kappa^2 z^2}$$

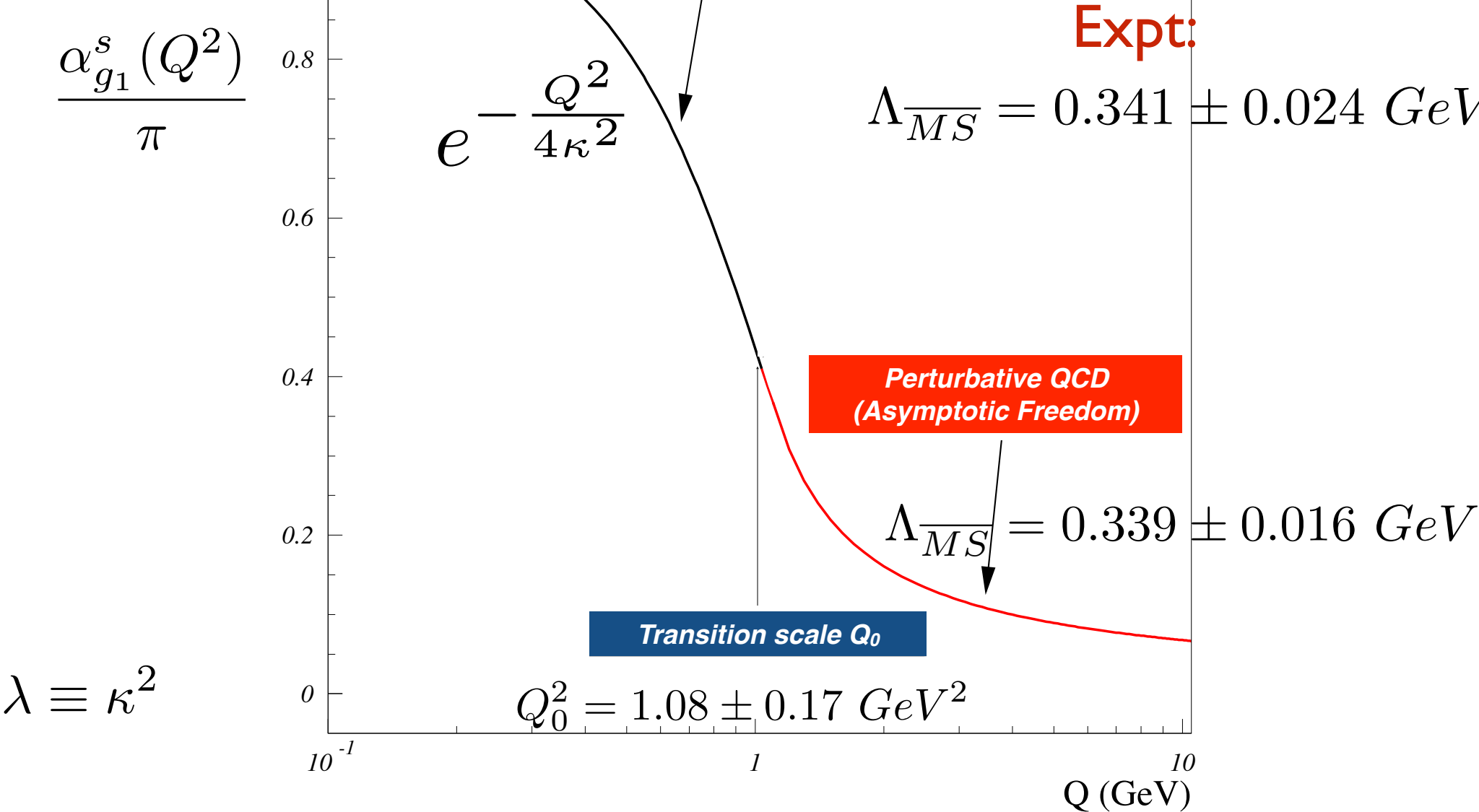
**Deur, de Teramond, sjb**

$$m_\rho = \sqrt{2}\kappa$$

$$m_p = 2\kappa_1$$

Deur, de Tèramond, sjb

**All-Scale QCD Coupling**

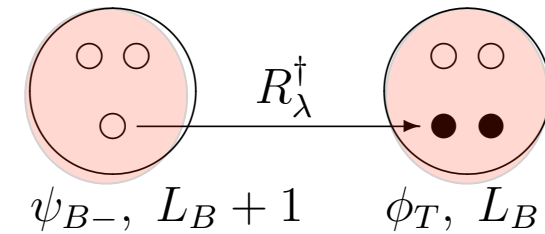
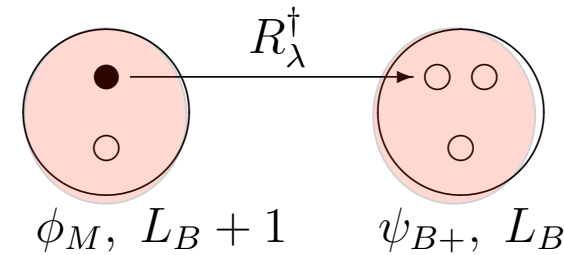


# Superconformal Algebra

## 2X2 Hadronic Multiplets

$$\begin{pmatrix} \phi_M(L_M = L_B + 1) & \psi_{B-}(L_B + 1) \\ \psi_{B+}(L_B) & \phi_T(L_T = L_B) \end{pmatrix}$$

- quark-antiquark meson ( $L_M = L_B + 1$ )
- quark-diquark baryon ( $L_B$ )
- quark-diquark baryon ( $L_B + 1$ )
- diquark-antidiquark tetraquark ( $L_T = L_B$ )
- Universal Regge slopes  $\lambda = \kappa^2$



$$M_H^2/\lambda = \underbrace{(2n + L_H + 1)}_{\text{kinetic}} + \underbrace{(2n + L_H + 1)}_{\text{potential}} + \underbrace{2(L_H + s) + 2\chi}_{\text{contribution from AdS and superconformal algebra}} + \left\langle \sum_i \frac{m_i^2}{x_i} \right\rangle$$

$$\chi(\text{mesons}) = -1$$

$$\chi(\text{baryons, tetraquarks}) = +1$$

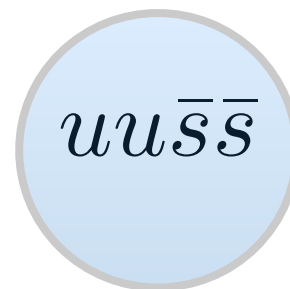
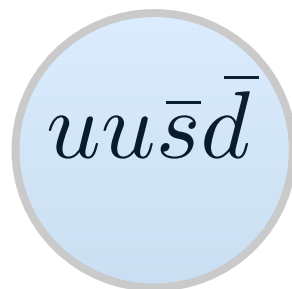
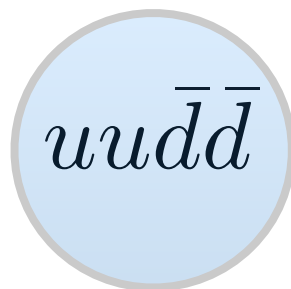
# New World of Tetraquarks

$$3_C \times 3_C = \bar{3}_C + 6_C$$

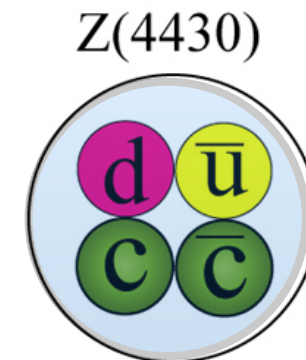
*Bound!*

- Diquark Color-Confined Constituents: Color  $\bar{3}_C$
- Diquark-Antidiquark bound states
- Confinement Force Similar to quark-antiquark  $\bar{3}_C \times 3_C = 1_C$  mesons
- Isospin  $I = 0, \pm 1, \pm 2$  Charge  $Q = 0, \pm 1, \pm 2$

Complete Regge spectrum in n, L



$Q = +2$



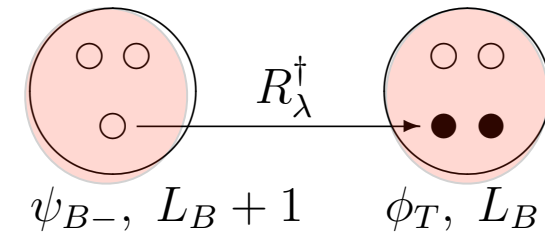
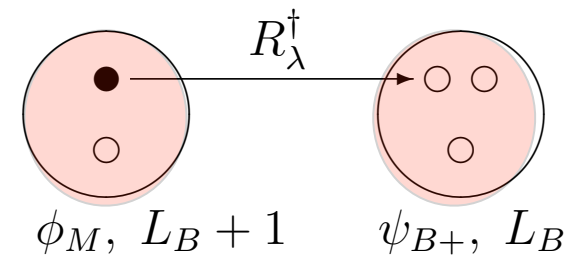
$Q = -1$

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$$\chi(\text{mesons}) = -1$$

$$\chi(\text{baryons, tetraquarks}) = +1$$

# Universal Hadronic Decomposition

$$\frac{\mathcal{M}_H^2}{\lambda} = (1 + 2n + L) + (1 + 2n + L) + (2L + 2S + 4|B| - 2)$$

$$\lambda = \kappa^2$$

- **Universal quark light-front kinetic energy**

$$\Delta\mathcal{M}_{LFKE}^2 = \lambda(1 + 2n + L)$$

- **Universal quark light-front potential energy**

$$\Delta\mathcal{M}_{LFPE}^2 = \lambda(1 + 2n + L)$$

- **Universal Constant Contribution from AdS and Superconformal Quantum Mechanics**

$$\Delta\mathcal{M}_{spin}^2 = \lambda(2L + 2S + 4|B| - 2)$$

hyperfine spin-spin

- plus  $\Delta\mathcal{M}_{quark\ mass}^2 = \sum_q \frac{m_q^2}{x_q}$

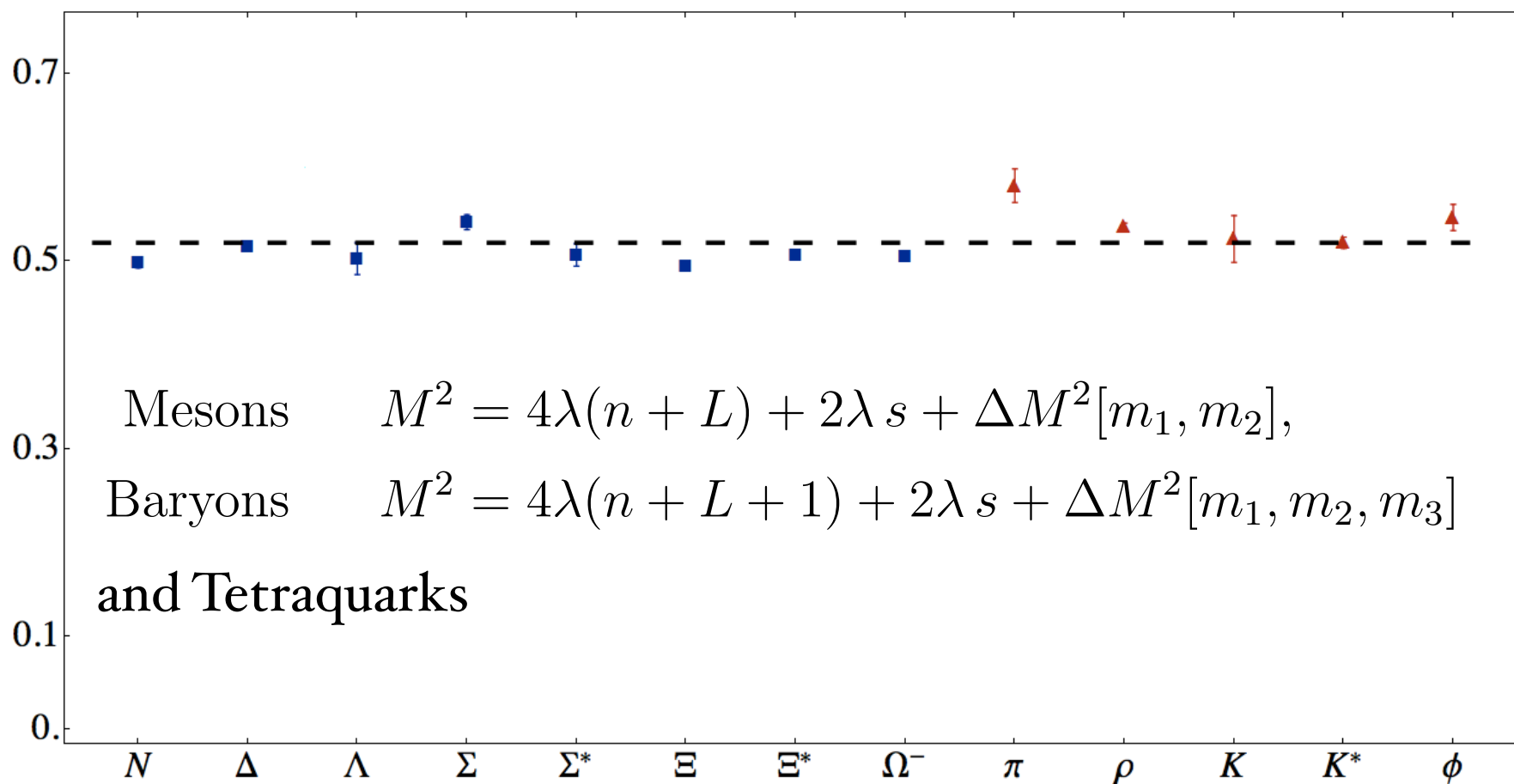
**Equal:  
Virial  
Theorem**



$$\kappa = \sqrt{\lambda}$$

- Universal Regge slopes

$$M_H^2 = 4\lambda(n + L) + \dots$$

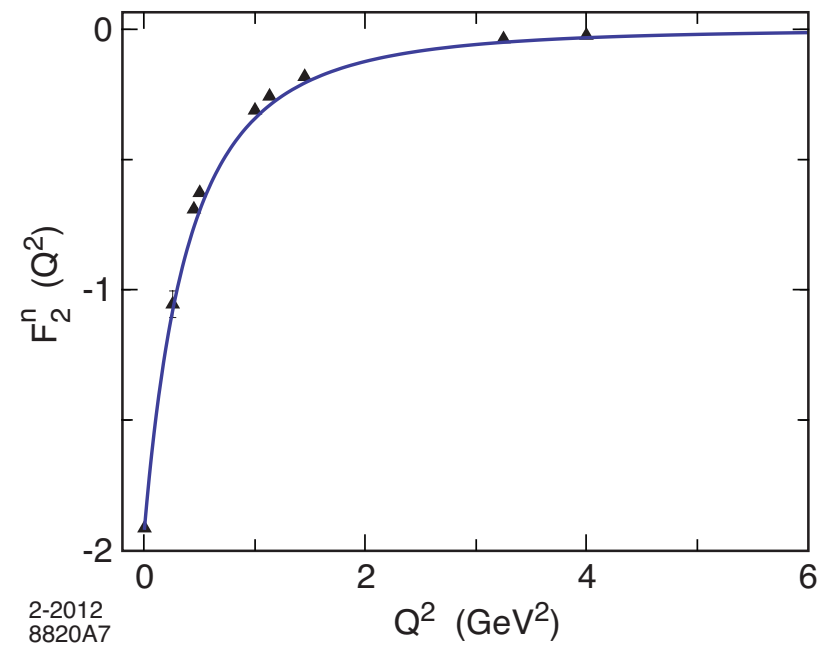
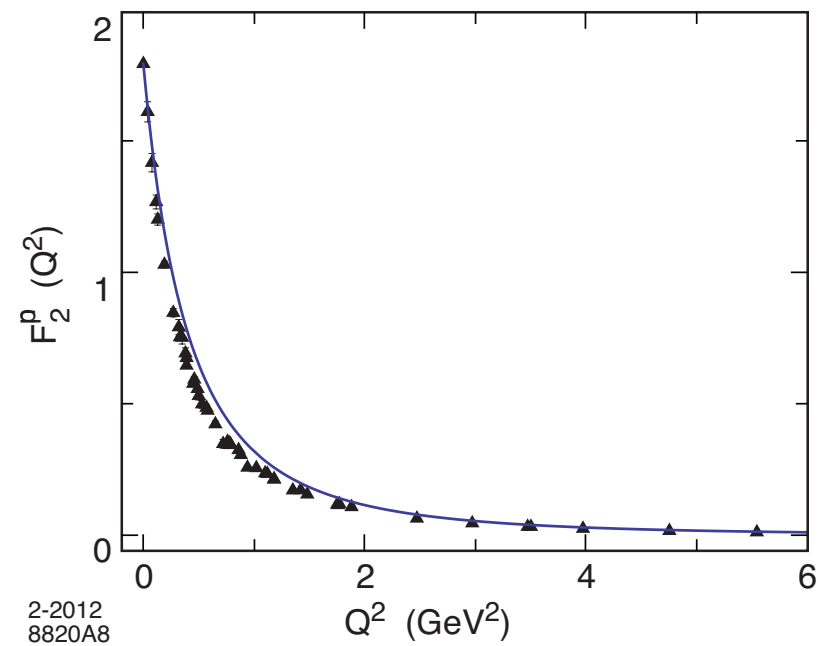
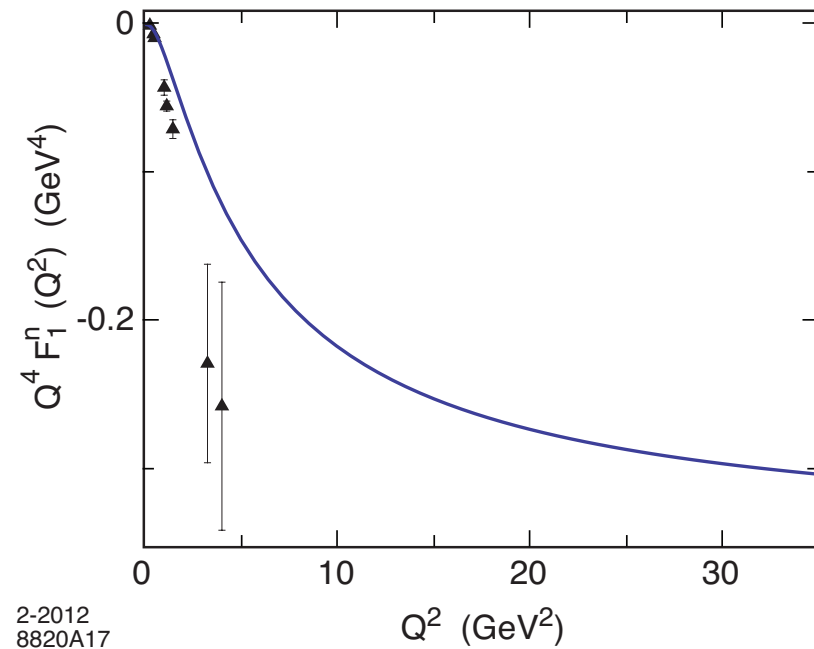
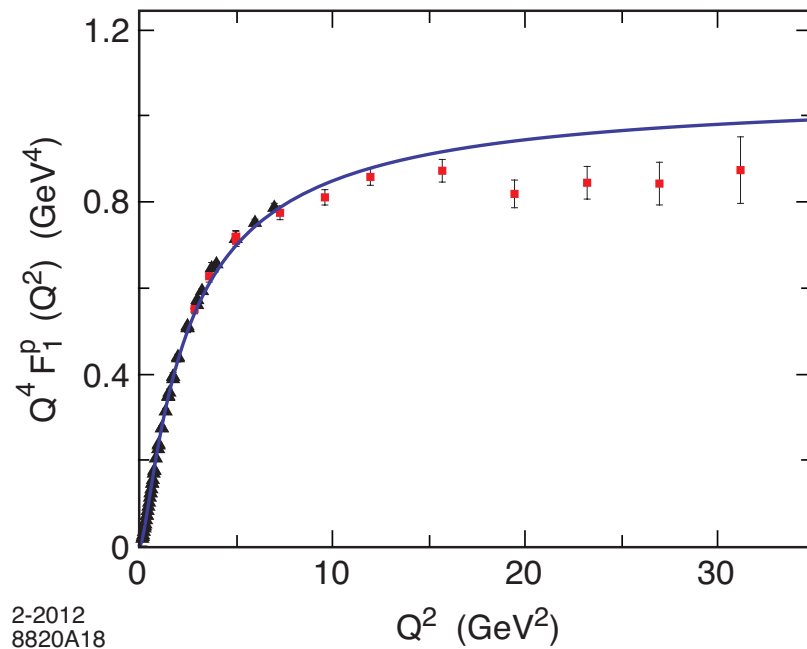


# Interpretation of Mass Scale $\kappa$

- Does not affect conformal symmetry of QCD action
- Self-consistent regularization of IR divergences
- Determines all mass and length scales for zero quark mass
- Compute scheme-dependent  $\Lambda_{\overline{MS}}$  determined in terms of  $\kappa$
- Value of  $\kappa$  itself not determined -- place holder
- Need external constraint such as  $f_\pi$

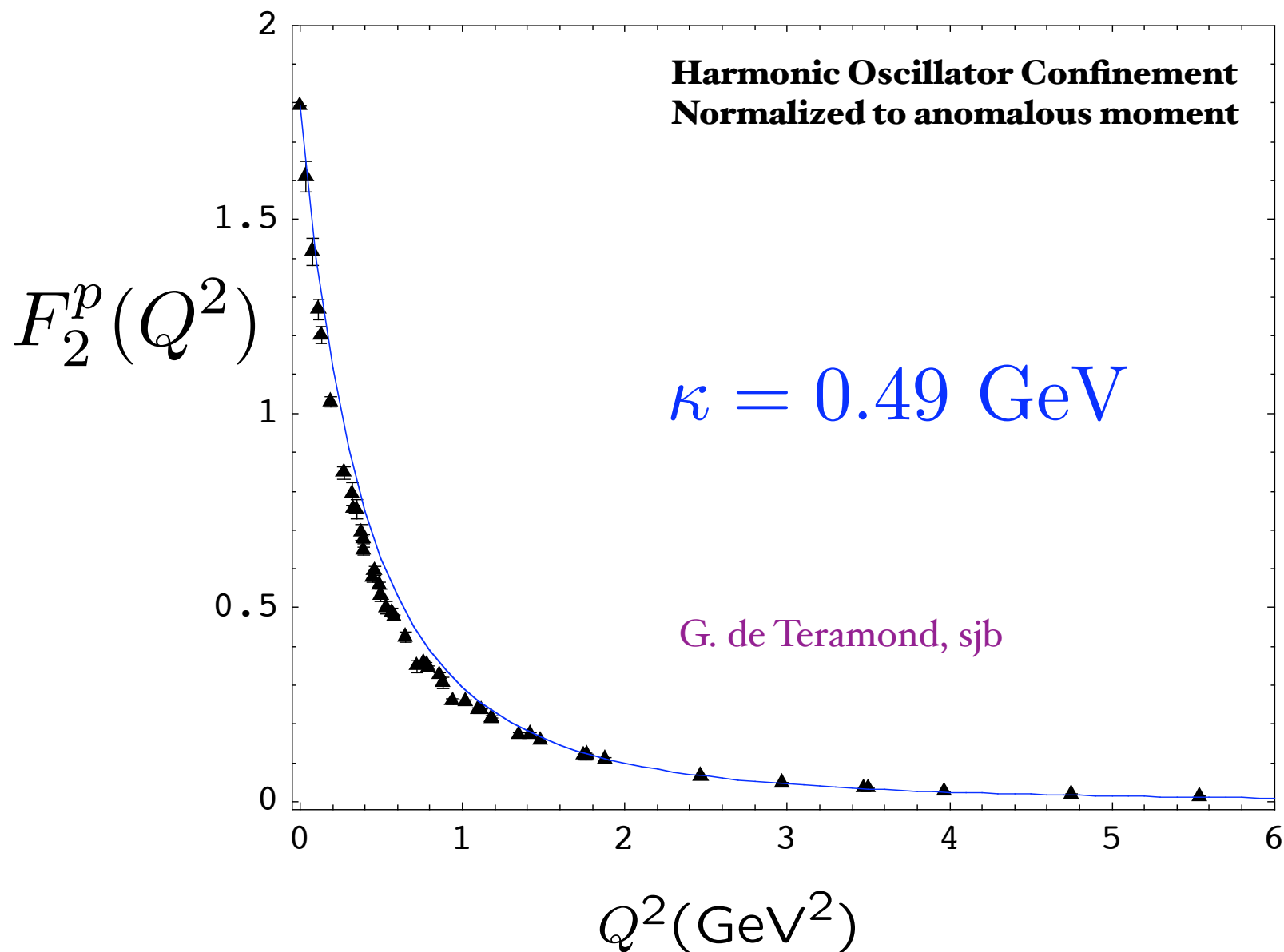
$$\kappa = \sqrt{\lambda}$$

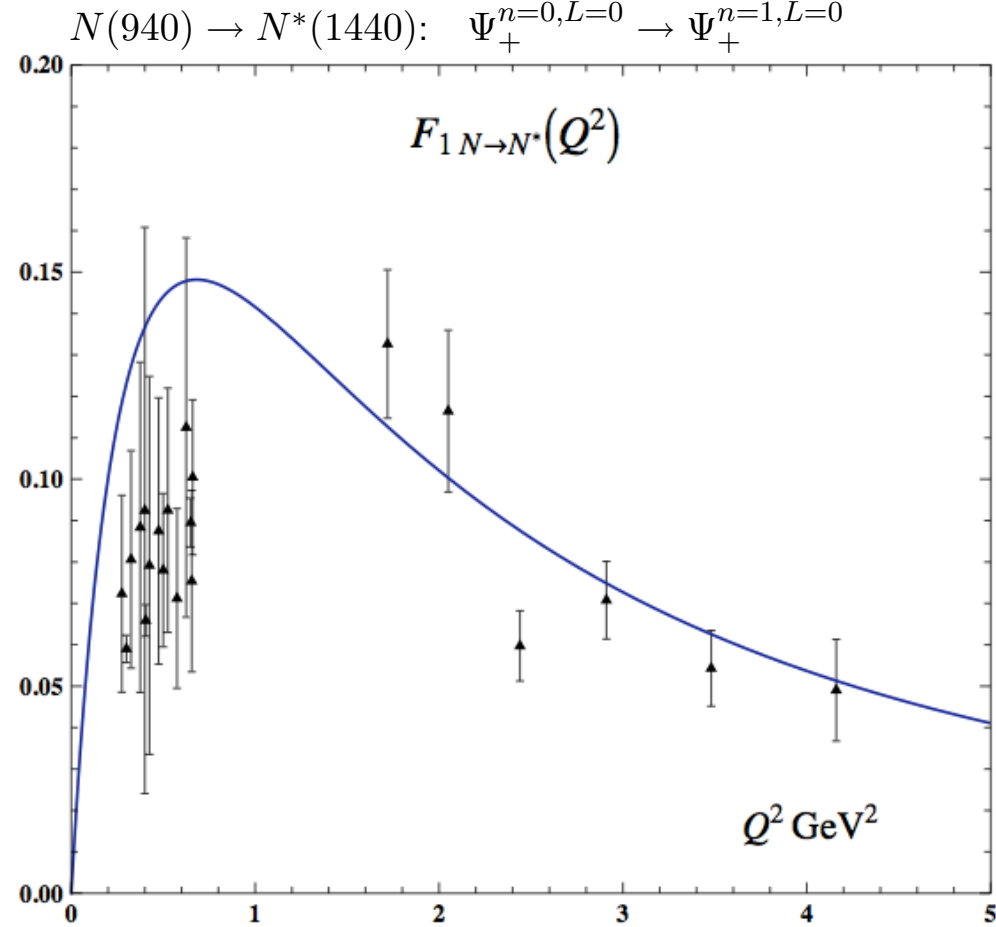
Using  $SU(6)$  flavor symmetry and normalization to static quantities



# Spacelike Pauli Form Factor

From overlap of  $L = 1$  and  $L = 0$  LFWFs





Data from I. Aznauryan, *et al.* CLAS (2009)

$$F_{1N \rightarrow N^*}^p(Q^2) = \frac{2\sqrt{2}}{3} \frac{\frac{Q^2}{M_P^2}}{\left(1 + \frac{Q^2}{\mathcal{M}_{\rho}^2}\right) \left(1 + \frac{Q^2}{\mathcal{M}_{\rho'}^2}\right) \left(1 + \frac{Q^2}{\mathcal{M}_{\rho''}^2}\right)}$$

with  $\mathcal{M}_{\rho_n}^2 \rightarrow 4\kappa^2(n + 1/2)$

# Predictions from AdS Holographic QCD

Dosch, Deur, de Teramond,  
sjb

- Zero-Mass pion for zero quark mass

$$M_{\pi}^2(n, L) = 4\kappa^2(n + L)$$

- Regge Spectroscopy

- Same slope in  $n, L$

- LFWFs, Distribution Amplitudes

$$\phi_{\pi}(x) \propto f_{\pi} \sqrt{x(1-x)}$$

- Form Factors, Structure Functions, GPDs

- Non-perturbative running coupling

$$\alpha_s(Q^2) \propto e^{-\frac{Q^2}{4\kappa^2}}$$

- Meson-Baryon Supersymmetry for  $L_M = L_{B+1}$

$$\lambda = \kappa^2$$

# *Interpretation of Mass Scale $\mathcal{K}$*

- Does not affect conformal symmetry of QCD action
- Self-consistent regularization of IR divergences
- Determines all mass and length scales for zero quark mass
- Compute scheme-dependent  $\Lambda_{\overline{MS}}$  determined in terms of  $\mathcal{K}$
- Value of  $\mathcal{K}$  itself not determined -- place holder
- Need external constraint such as  $f_\pi$

# *Tests of AdS/QCD and LF Holography*

## *JLab 12 GeV*

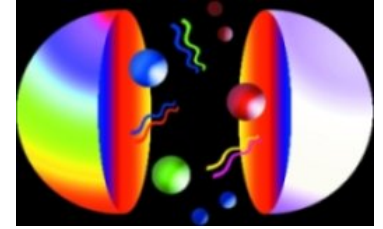
- Spacelike-Transition Form Factors  $F_{\pi \rightarrow b_1}(Q^2)$   $F_{p \rightarrow N^*}(Q^2)$
- Supersymmetric QCD Relations: Spectra, Dynamics
- Baryons: q + diquark  $[q]_{3C} [qq]_{\bar{3}C}$
- Pentaquarks: diquark-antidiquark  $[qq]_{\bar{3}C} [\bar{q}\bar{q}]_{3C}$



# Fermionic Modes and Baryon Spectrum

[Hard wall model: GdT and S. J. Brodsky, PRL **94**, 201601 (2005)]

[Soft wall model: GdT and S. J. Brodsky, (2005), arXiv:1001.5193]



From Nick Evans

- Nucleon LF modes

$$\psi_+(\zeta)_{n,L} = \kappa^{2+L} \sqrt{\frac{2n!}{(n+L)!}} \zeta^{3/2+L} e^{-\kappa^2 \zeta^2 / 2} L_n^{L+1} (\kappa^2 \zeta^2)$$

$$\psi_-(\zeta)_{n,L} = \kappa^{3+L} \frac{1}{\sqrt{n+L+2}} \sqrt{\frac{2n!}{(n+L)!}} \zeta^{5/2+L} e^{-\kappa^2 \zeta^2 / 2} L_n^{L+2} (\kappa^2 \zeta^2)$$

- Normalization

$$\int d\zeta \psi_+^2(\zeta) = \int d\zeta \psi_-^2(\zeta) = 1$$

*Chiral Symmetry  
of Eigenstate!*

- Eigenvalues

$$\mathcal{M}_{n,L,S=1/2}^2 = 4\kappa^2 (n+L+1)$$

- “Chiral partners”

$$\frac{\mathcal{M}_{N(1535)}}{\mathcal{M}_{N(940)}} = \sqrt{2}$$

# Features of Supersymmetric Equations

- $J = L + S$  baryon simultaneously satisfies both equations of G with  $L$ ,  $L+1$  for same mass eigenvalue
  - $J^z = L^z + 1/2 = (L^z + 1) - 1/2$   $S^z = \pm 1/2$
  - Baryon spin carried by quark orbital angular momentum:  $\langle J^z \rangle = L^z + 1/2$
  - Mass-degenerate meson “superpartner” with  $L_M = L_B + 1$ . *“Shifted meson-baryon Duality”*
- Meson and baryon have same  $\kappa$ !

Counting Rules Obeyed

# *AdS/QCD and Light-Front Holography*

$$\mathcal{M}_{n,J,L}^2 = 4\kappa^2 \left( n + \frac{J+L}{2} \right)$$

- **Zero mass pion for  $m_q=0$  ( $n=J=L=0$ )**
- **Regge trajectories: equal slope in  $n$  and  $L$**
- **Form Factors at high  $Q^2$ : Dimensional counting**  
 $[Q^2]^{n-1} F(Q^2) \rightarrow \text{const}$
- **Space-like and Time-like Meson and Baryon Form Factors**
- **Running Coupling for NPQCD**  $\alpha_s(Q^2) \propto e^{-\frac{Q^2}{4\kappa^2}}$
- **Meson Distribution Amplitude**  $\phi_\pi(x) \propto f_\pi \sqrt{x(1-x)}$

# Features of AdS/QCD

*de Tèramond, Dosch, Deur, sjb*

- **Color confining potential  $\kappa^4 \zeta^2$  and universal mass scale from dilaton**

$$e^{\phi(z)} = e^{\kappa^2 z^2} \quad \alpha_s(Q^2) \propto \exp -Q^2/4\kappa^2$$

- **Dimensional transmutation**  $\Lambda_{\overline{MS}} \leftrightarrow \kappa \leftrightarrow m_H$

- **Chiral Action remains conformally invariant despite mass scale** *DAFF*

- **Light-Front Holography: Duality of AdS and independent LF QCD** **frame-**

- **Reproduces observed Regge spectroscopy — slope in n, L, and J for mesons and baryons** **same**

- **Massless pion for massless quark**

- **Supersymmetric meson-baryon dynamics and spectroscopy:**  
 $L_M = L_B + I$

*Superconformal Quantum  
Mechanics  
Fubini and Rabinovici*

# Tests of AdS/QCD and LF Holography at JLab 12 GeV

- **Compare Spacelike-Transition Form Factors, Counting Rules**

$$F_{\pi \rightarrow b_1}(Q^2) \quad \text{vs.} \quad F_{p \rightarrow N^*}(Q^2)$$

- **Supersymmetric QCD Relations: Spectra, Dynamics**

- **Baryons: q + diquark:**  $[q]_{3C} [qq]_{\bar{3}C}$

- **Tetraquarks: diquark-antidiquark?:**  $[qq]_{\bar{3}C} [\bar{q}\bar{q}]_{3C}$

$$M_H^2/\lambda = \underbrace{(2n + L_H + 1)}_{\text{kinetic}} + \underbrace{(2n + L_H + 1)}_{\text{potential}} + \underbrace{2(L_H + s) + 2\chi}_{\text{contribution from AdS and superconformal algebra}}$$

*contribution from 2-dim light-front harmonic oscillator*

# Tony Zee

## "Quantum Field Theory in a Nutshell"

### *Dreams of Exact Solvability*

“In other words, if you manage to calculate  $m_P$  it better come out proportional to  $\Lambda_{QCD}$  since  $\Lambda_{QCD}$  is the only quantity with dimension of mass around.

#### Light-Front Holography:

Similarly for  $m_\rho$ .

$$m_p \simeq 3.21 \Lambda_{\overline{MS}}$$

$$m_\rho \simeq 2.2 \Lambda_{\overline{MS}}$$

Put in precise terms, if you publish a paper with a formula giving  $m_\rho/m_P$  in terms of pure numbers such as 2 and  $\pi$ , the field theory community will hail you as a conquering hero who has solved QCD exactly.”

$$\begin{aligned} (m_q = 0) \\ m_\pi = 0 \end{aligned}$$

$$\frac{m_\rho}{m_P} = \frac{1}{\sqrt{2}}$$

$$\frac{\Lambda_{\overline{MS}}}{m_\rho} = 0.455 \pm 0.031$$

# *Light-Front vacuum can simulate empty universe*

**Shrock, Tandy, Roberts, sjb**

- **Independent of observer frame**
- **Causal**
- **Lowest invariant mass state  $M=0$ .**
- **Trivial up to  $k^+=0$  zero modes-- already normal-ordering**
- **Higgs theory consistent with trivial LF vacuum (Srivastava, sjb)**
- **QCD and AdS/QCD: “In-hadron” condensates (Maris, Tandy Roberts) -- GMOR satisfied.**
- **QED vacuum; no loops**
- **Zero cosmological constant from QED, QCD, EW**

# QCD Myths

- **Anti-Shadowing is Universal**
- **ISI and FSI are higher twist effects and universal**
- **High transverse momentum hadrons arise only from jet fragmentation -- baryon anomaly!**
- **Heavy quarks only from gluon splitting**
- **Renormalization scale cannot be fixed**
- **QCD condensates are vacuum effects**
- **QCD gives  $10^{42}$  to the cosmological constant**
- **QCD Confinement and Mass Scale from  $\Lambda_{\overline{MS}}$**



# *Hot Topics in QCD*

- *Intrinsic Heavy Quarks*
- *Breakdown of pQCD Leading-Twist Factorization*
- *Top/anti-Top asymmetry*
- *Non-universal antishadowing*
- *Demise of QCD Vacuum Condensates*
- *Elimination of the QCD Renormalization Scale Ambiguity*
- *AdS/QCD and Light-Front Holography*

*Crucial to Understand QCD to High Precision to  
Illuminate New Physics*

# Set multiple renormalization scales -- Lensing, DGLAP, ERBL Evolution ...

Choose renormalization scheme; e.g.  $\alpha_s^R(\mu_R^{\text{init}})$

Choose  $\mu_R^{\text{init}}$ ; arbitrary initial renormalization scale

Identify  $\{\beta_i^R\}$  – terms using  $n_f$  – terms  
through the PMC – BLM correspondence principle

Shift scale of  $\alpha_s$  to  $\mu_R^{\text{PMC}}$  to eliminate  $\{\beta_i^R\}$  – terms

Conformal Series

Result is independent of  $\mu_R^{\text{init}}$  and scheme at fixed order

## Principle of Maximum Conformality

## PMC/BLM

**No renormalization scale ambiguity!**

*Result is independent of  
Renormalization scheme  
and initial scale!*

**QED Scale Setting at  $N_C=0$**

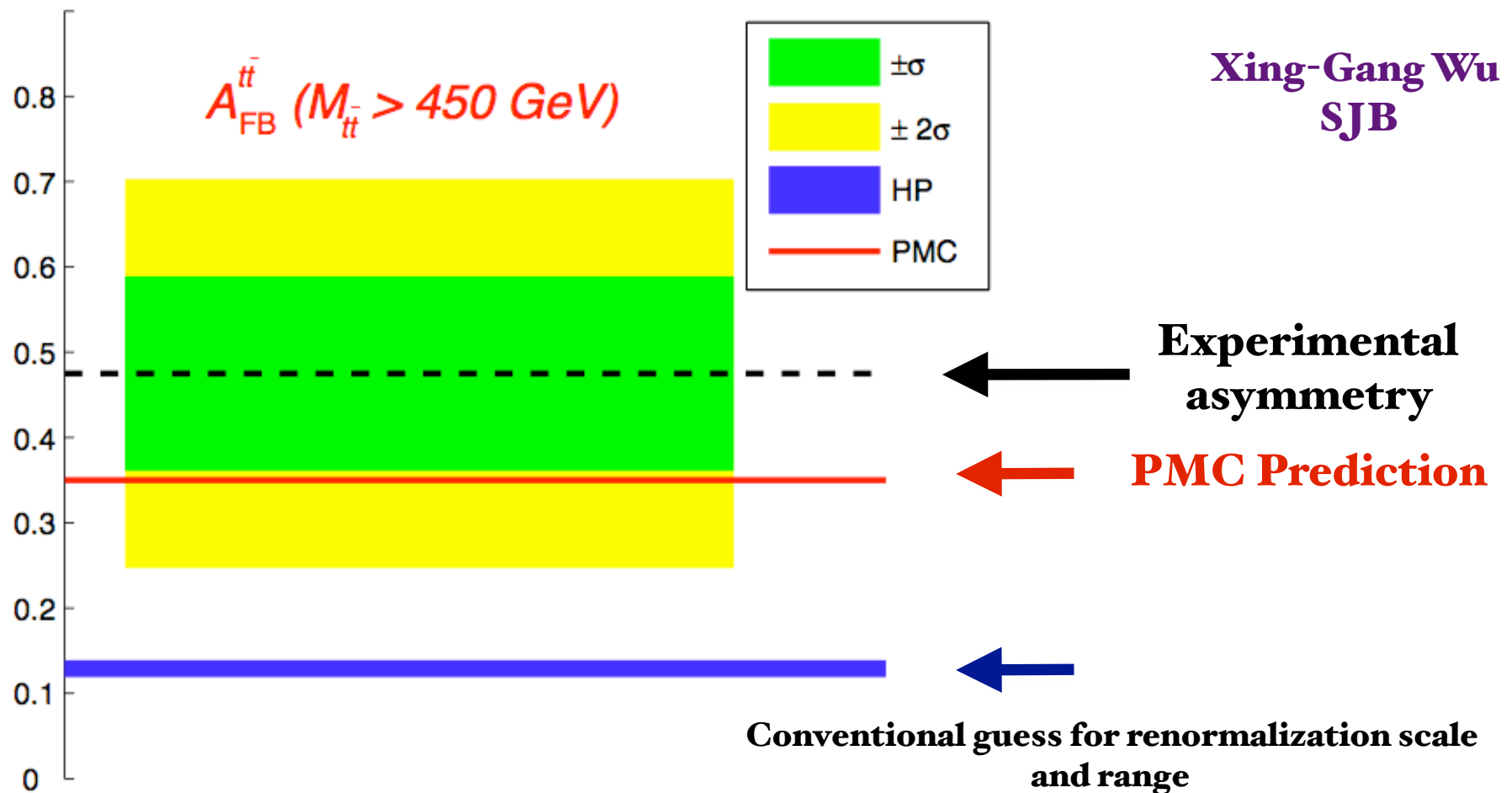
**Eliminates unnecessary  
systematic uncertainty**

Scale fixed at each order

**$\delta$ -Scheme automatically  
identifies  $\beta$ -terms!**

*Xing-Gang Wu, Martin Mojaza  
Leonardo di Giustino, Sfb*

# The Renormalization Scale Ambiguity for Top-Pair Production Eliminated Using the 'Principle of Maximum Conformality' (PMC)

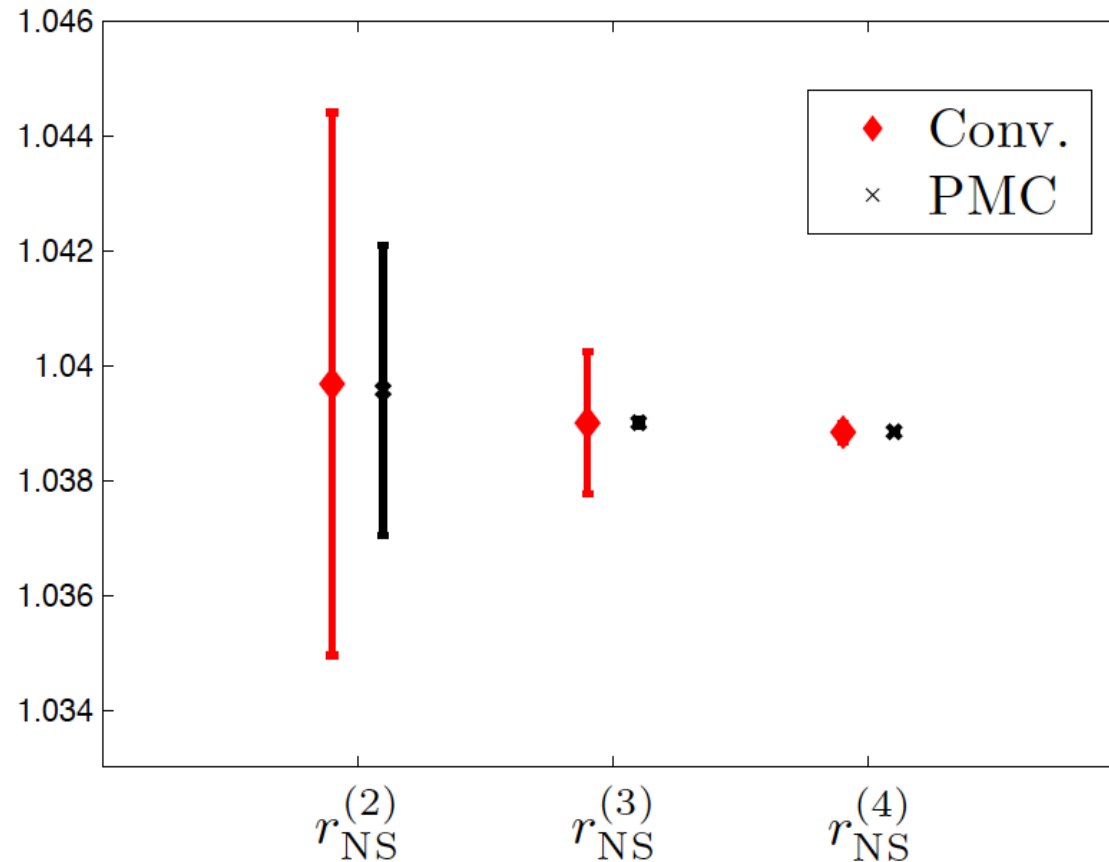


Top quark forward-backward asymmetry predicted by pQCD NNLO within  $1\sigma$  of CDF/D0 measurements using PMC/BLM scale setting

# Reanalysis of the Higher Order Perturbative QCD corrections to Hadronic Z Decays using the Principle of Maximum Conformality

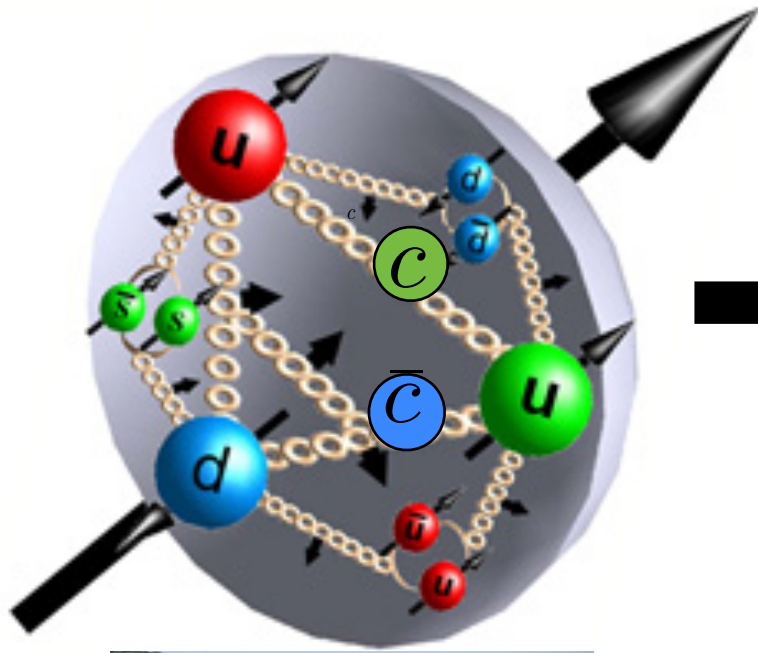
S-Q Wang, X-G Wu, sjb

P.A. Baikov, K.G. Chetyrkin, J.H. Kuhn, and J. Rittinger,  
Phys. Rev. Lett. 108, 222003 (2012).

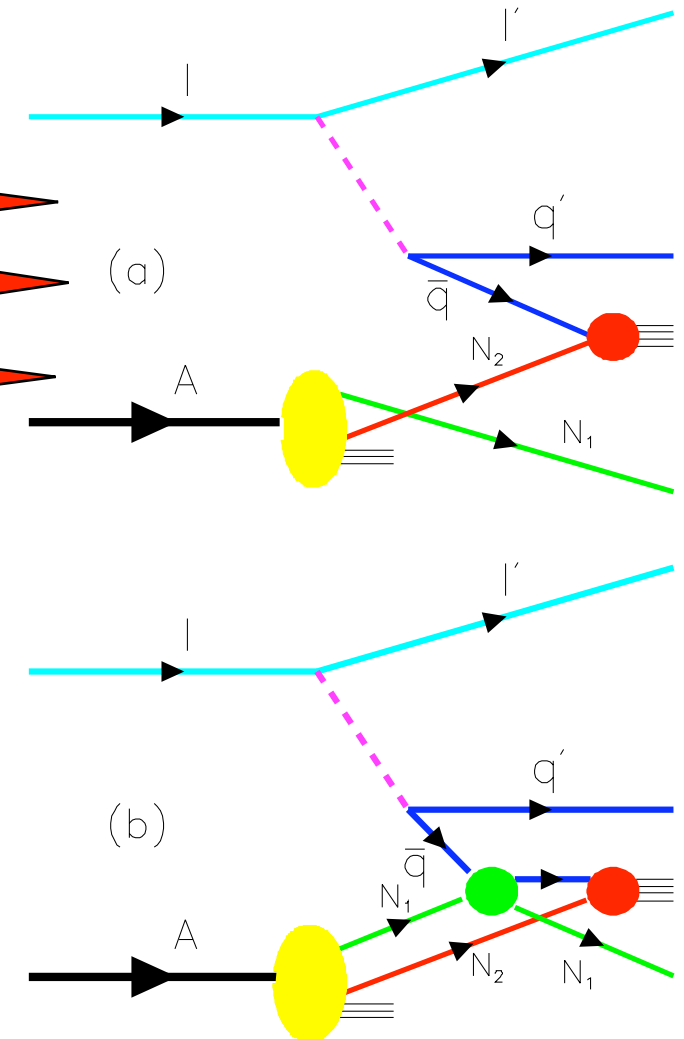
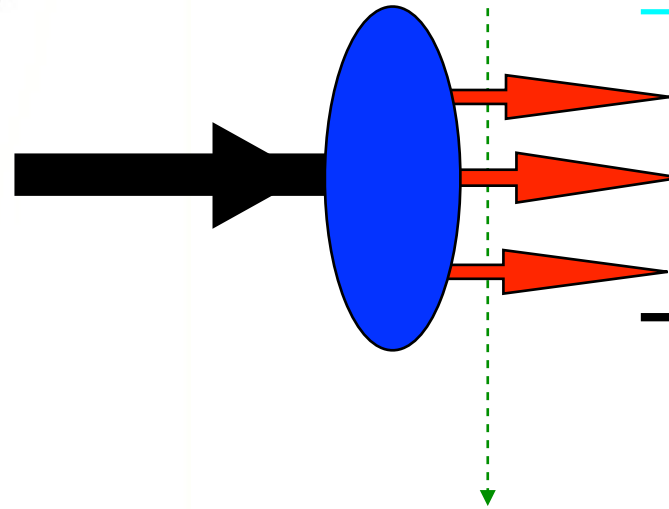


The values of  $r_{\text{NS}}^{(n)} = 1 + \sum_{i=1}^n C_i^{\text{NS}} a_s^i$  and their errors  $\pm |C_n^{\text{NS}} a_s^n|_{\text{MAX}}$ . The diamonds and the crosses are for conventional (Conv.) and PMC scale settings, respectively. The central values assume the initial scale choice  $\mu_r^{\text{init}} = M_Z$ .

# Novel QCD Features of Hadrons and Nuclei



Fixed  $\tau = t + z/c$



Stan Brodsky



with Guy de Tèramond, Hans Günter Dosch, Cedric Lorce, Kelly Chiu, and Alexandre Deur

**CDR QCD: Partons and Nuclei**

**Orsay June 1, 2017**

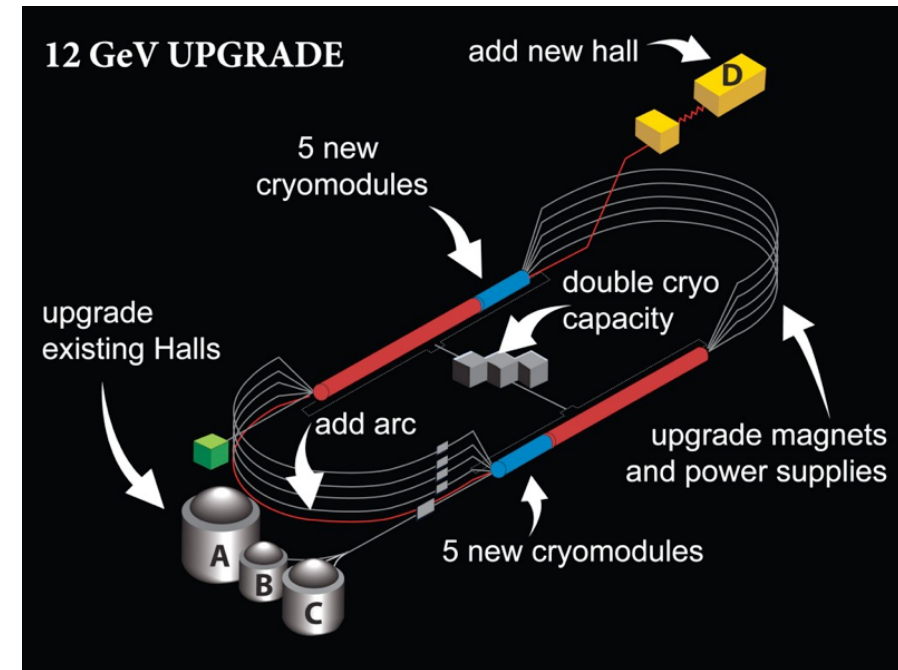
# *JLab 12 GeV: An Exotic Charm Factory!*

- **Charm quarks at high  $x$  -- allows charm states to be produced with minimal energy**
- **Charm produced at low velocities in the target -- the target rapidity domain  $x_F \sim -1$**
- **Charm at threshold -- maximal domain for producing exotic states containing charm quarks**
- **Attractive QCD Van der Waals interaction -- “nuclear-bound quarkonium”**
- **Dramatic Spin Correlations in the threshold Domain**
- **Strong SSS Threshold Enhancement**



# *Novel QCD Phenomena at JLab 12 GeV and the EIC*

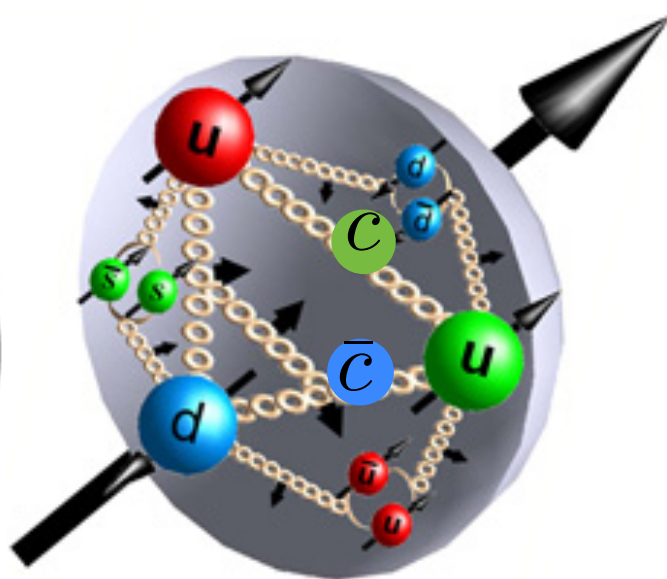
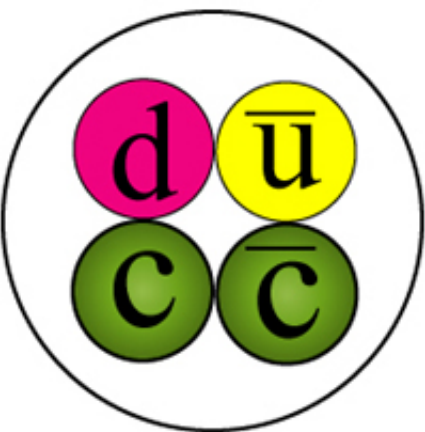
- *Intrinsic Heavy Quarks*
- *Charm at Threshold*
- *Novel Heavy Quark Resonances at Threshold*
- *Nuclear-Bound Quarkonium*
- *Exclusive and Inclusive Sivers Effect.*
- *Breakdown of pQCD Leading-Twist Factorization*
- *Non-universal antishadowing*
- *Hidden Color*
- *$J=0$  Fixed pole in DVCS*



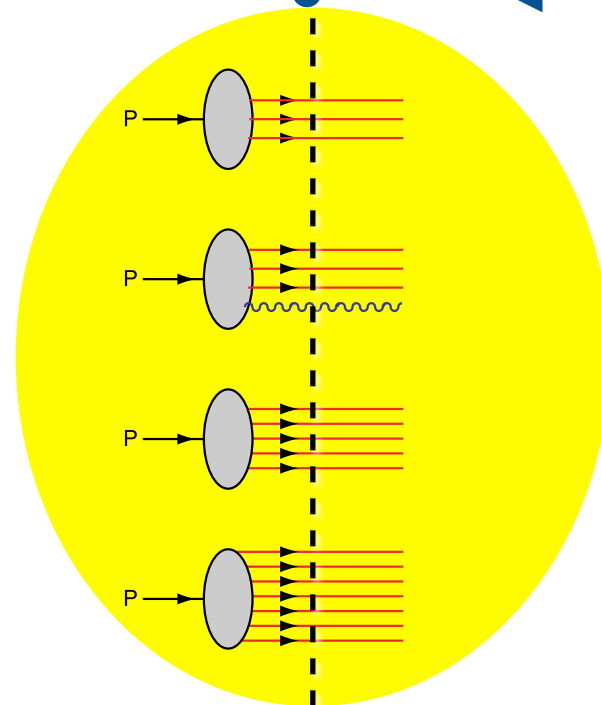
*Illuminate New Hadronic Physics*

# Novel QCD Phenomena in Nuclear Photo - and Electroproduction

**Exotic Hadrons**



$e'$   $e$

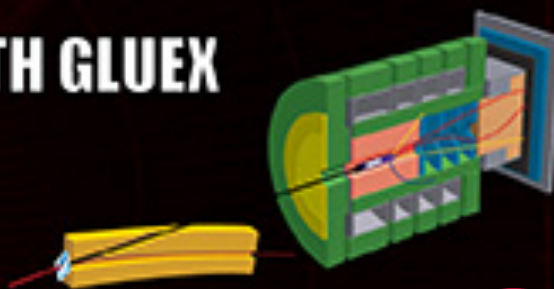


Fixed LF time

$$\tau = t + z/c$$

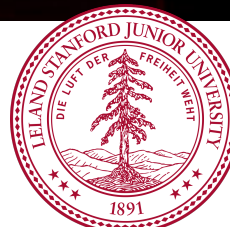
**NUCLEAR PHOTOPRODUCTION WITH GLUEX**

**APRIL 28-29, 2016**



*Stan Brodsky*

**SLAC**  
NATIONAL ACCELERATOR LABORATORY



**Jefferson Lab**  
*April 29, 2016*