

**Constraining first moments of GPDs:  
Nucleon Form Factors measurements at high  $Q^2$   
with Super BigBite Spectrometer  
in Hall A at Jefferson Lab 12 GeV**

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**University of Connecticut**

**Nucleon and Resonance Structure with  
Hard Exclusive Processes**  
Orsay, May 29-31, 2017

## Overview

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### **Nucleon structure with (space-like) Form Factors:**

- Theory and experimental status;
- Form factors and spin puzzle: connection with GPDs.

### **Nucleon Form Factors with Super BigBite Spectrometer (SBS):**

- Super BigBite Spectrometer apparatus in Hall A at Jefferson Lab 12 GeV;
- SBS experimental program: Nucleon Form Factors at high  $Q^2$ ;
- Impact of the Form Factor measurements from SBS.

### **Summary**

## Nucleon Structure with (space-like) Form Factors

**Form factors:**

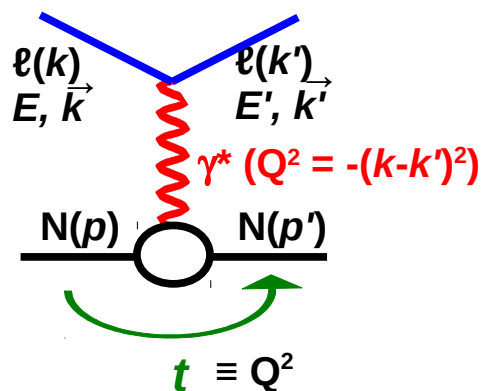
**Parameterization of charge distribution inside the nucleon**

Measured first by Hofstadter and McAllister

[Phys. Rev. **98**, 217 (1955)]

=> **first evidence that nucleon is composite;**

Elastic electron nucleon scattering



Nucleon parameterized

with **2** form factors:

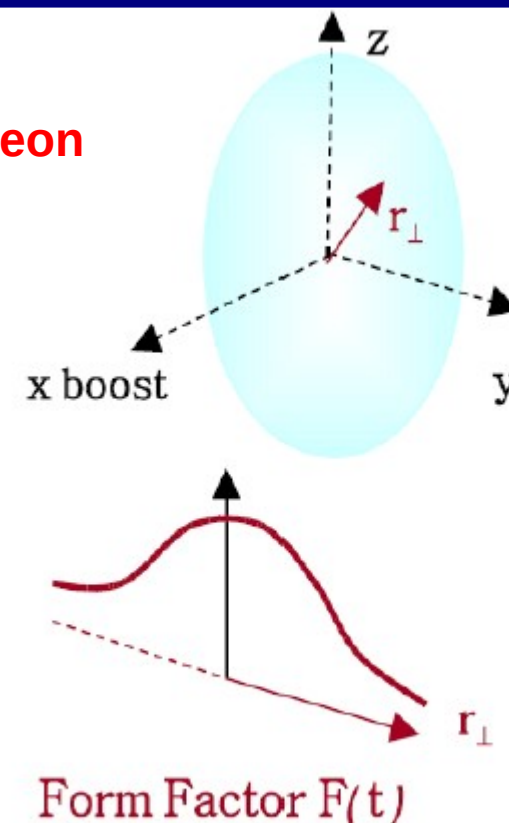
$F_1^q, F_2^q$  (Dirac, Pauli);

or  $G_E, G_M$  (Sachs);

$$G_E = F_1 - \tau F_2$$

$$G_M = F_1 + F_2$$

$$\tau = \frac{Q^2}{4M^2}$$



$$\frac{d\sigma}{d\Omega_e} = \left( \frac{d\sigma}{d\Omega_e} \right)_{Mott} \frac{E'}{E} \left( F_1^2(Q^2) + \left[ F_2^2(Q^2) + 2[F_1^2(Q^2) + F_2^2(Q^2)] \tan^2\left(\frac{\theta_e}{2}\right) \right] \right)$$

$$= \left( \frac{d\sigma}{d\Omega_e} \right)_{Mott} \frac{E'}{E} \frac{1}{1+\tau} \left( G_E^2(Q^2) + \frac{\tau}{\epsilon} G_M^2(Q^2) \right)$$

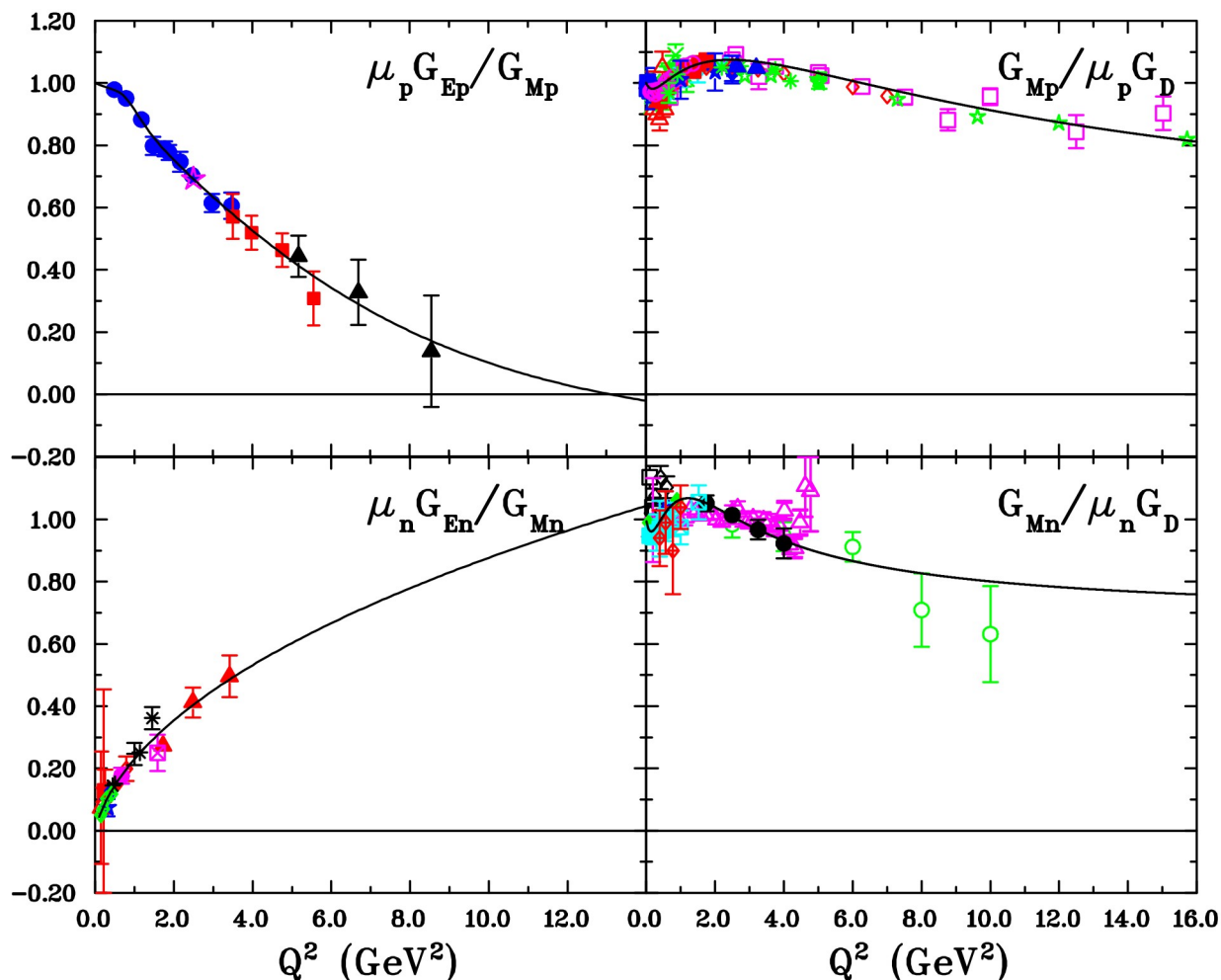
$$\left( \frac{d\sigma}{d\Omega_e} \right)_{Mott} = \frac{\alpha^2 \cos^2(\theta/2)}{4E^2 \sin^4(\theta/2)}$$

Cross section on a point-like proton

$$\epsilon = \frac{1}{1+2(1+\tau) \tan^2(\theta_e/2)}$$

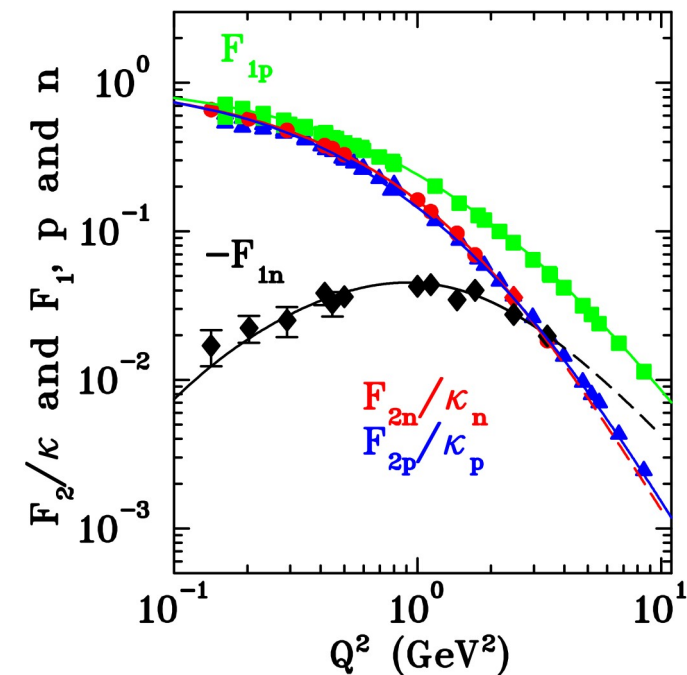
Virtual photon polarization

## Form Factors : Theory and experimental status



\* No data beyond 10 GeV<sup>2</sup> for  $G_E^p$ ,  $G_M^n$ ,  $G_e^n$ ;

Plots taken from [Punjabi *et al.* Eur.Phys.J. **A51** (2015) 79  
Curves: [Kelly, Phys. Rev. **C70**, (2004) 068202]



## Form Factors : Theory and experimental status

### $G_E^p/G_M^p$ : Recoil polarization Vs Rosenbluth cross section separation

#### Rosenbluth separation

$$\Rightarrow \frac{d\sigma}{d\Omega_e}(\epsilon, Q_{cst}^2) \propto \left( G_M^2(Q^2) + \frac{\epsilon}{\tau} G_E^2(Q^2) \right) \rightarrow \text{Strongly affected by } 2\gamma \text{ exch.}$$

#### Recoil polarization experiment: $\vec{e}p \rightarrow e\vec{p}$

Components of polarization transferred:

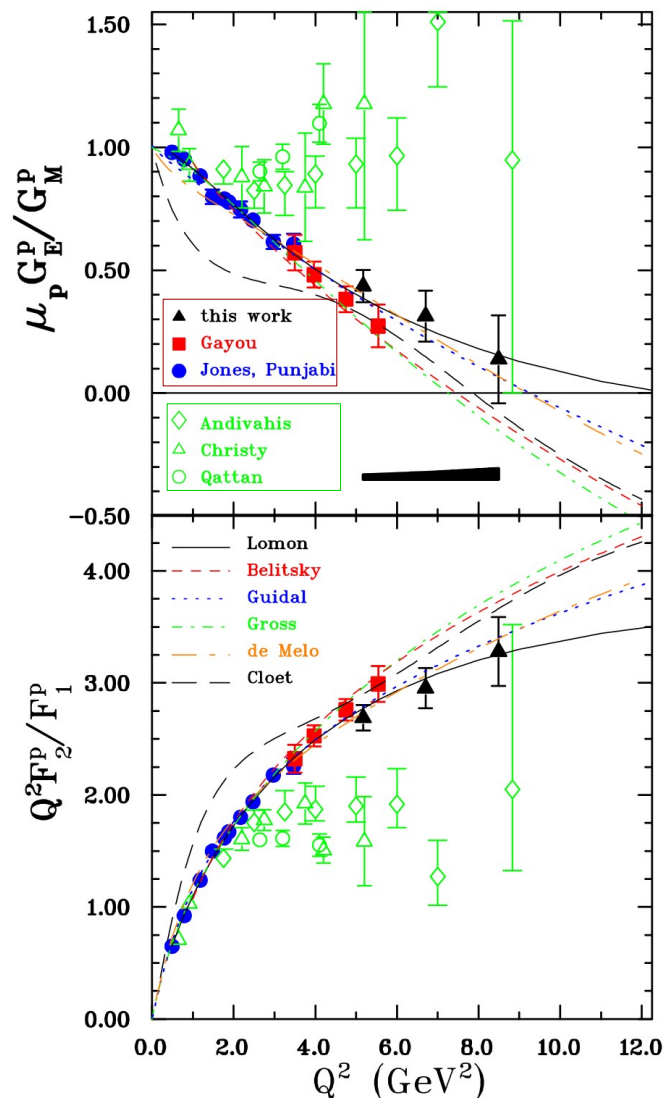
$$\Rightarrow \frac{G_E}{G_M} = -\frac{P_t}{P_l} \frac{E+E'}{2M} \tan\left(\frac{\theta}{2}\right) \rightarrow \text{Slightly affected (few \%)} \text{ by } 2\gamma \text{ exch.}$$

$\Rightarrow$  Much stronger  $Q^2$  dependence of  $G_E/G_M$  for recoil polarization experiments

**$2\gamma$  exchange very likely responsible for this effect**

Elastic  $e^\pm p$  experiments (Olympus @ DESY, CLAS 6 @ JLab) have directly measured  $2\gamma$  exchange at low  $Q^2$ .

[Puckett et. al.: Phys. Rev. Lett. **104** (2010) 242301]



## Form Factors : Theory and experimental status

**Many descriptions of the form factors available:**

**Vector Meson Dominance:** coupling of virtual photon to vector mesons ( $J^{PC} = 1^{-}$ )

**Constituent Quark Models:** Nucleon = 3 quarks in a confining potential;

**Dyson-Schwinger Equation calculations:** Set of equations => non-perturbative approximation of QCD;

**AdS/Light-Front QCD:** QCD calculations on the light cone;

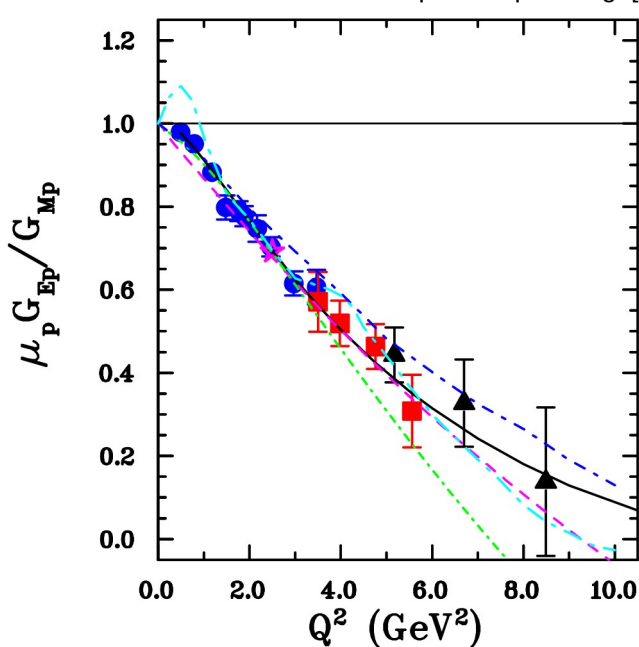
**Lattice QCD:** calculation of QCD within a discrete space time grid (lattice);

=> FF description at  $Q^2 > 10 \text{ GeV}^2$  diverge for most models

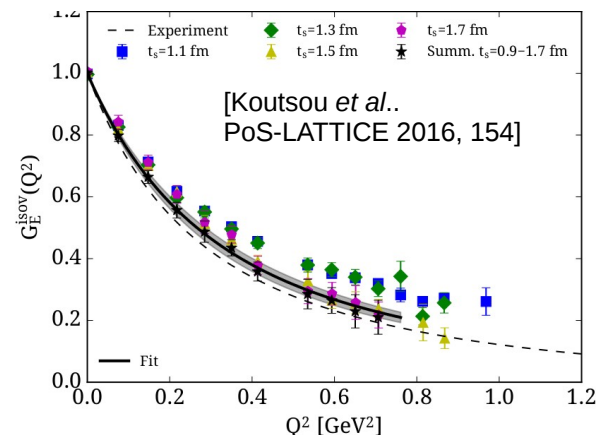
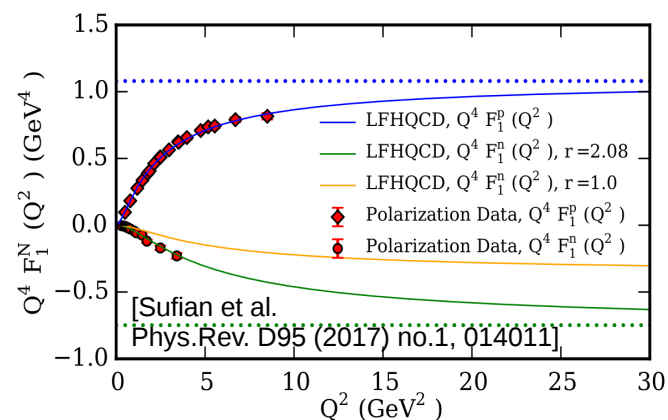
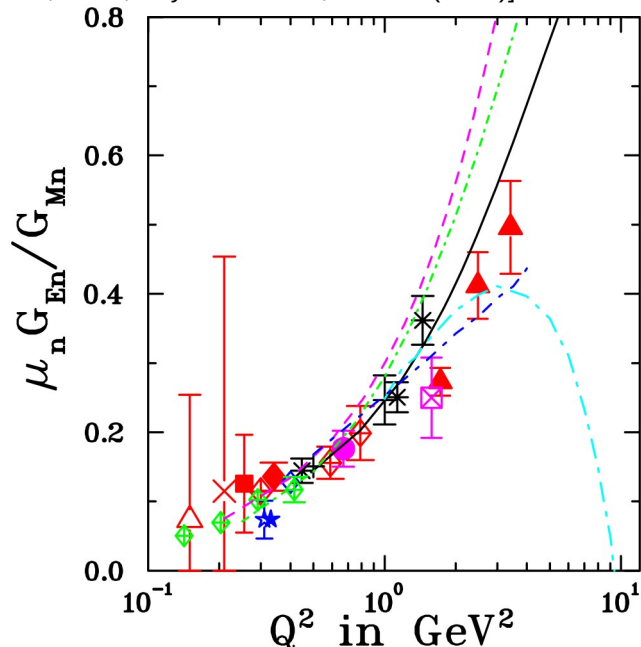
=> additional data will help select which models give the best description

=> great insight on nucleon structure and QCD.

- VMD e.g. [Lomon, arXiv:nucl-th/0609020 (2006)]
- CQM e.g. [Gross, Ramalho, Pena. Phys. Rev. **C77**, 015202 (2008)]
- DSE e.g. [Cloet, Roberts, Thomas, Phys. Rev. Lett. **111**, 101803 (2013)]
- DSE quark-diquark e.g. [Cloet, Miller, Phys. Rev. **C86**, 015208 (2012)]



Plots from [Punjabi et al. Eur.Phys.J. **A51** (2015) 79]



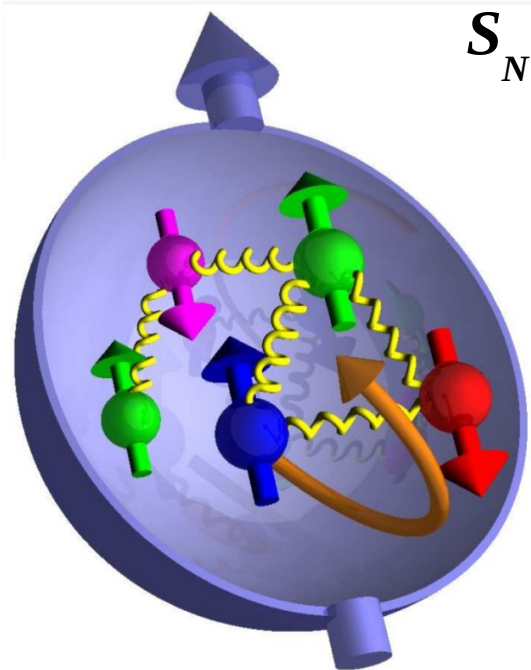
## Form Factors and spin puzzle

Nucleon Spin content:

$$S_N = \frac{1}{2} = \frac{1}{2} \Delta\Sigma + \Delta G + L_q + L_g$$

Static quark model:  
 $\Delta\Sigma = 1 \dots$

**Polarized DIS Experiments:**  
 $\Rightarrow \Delta\Sigma \sim 0.3$



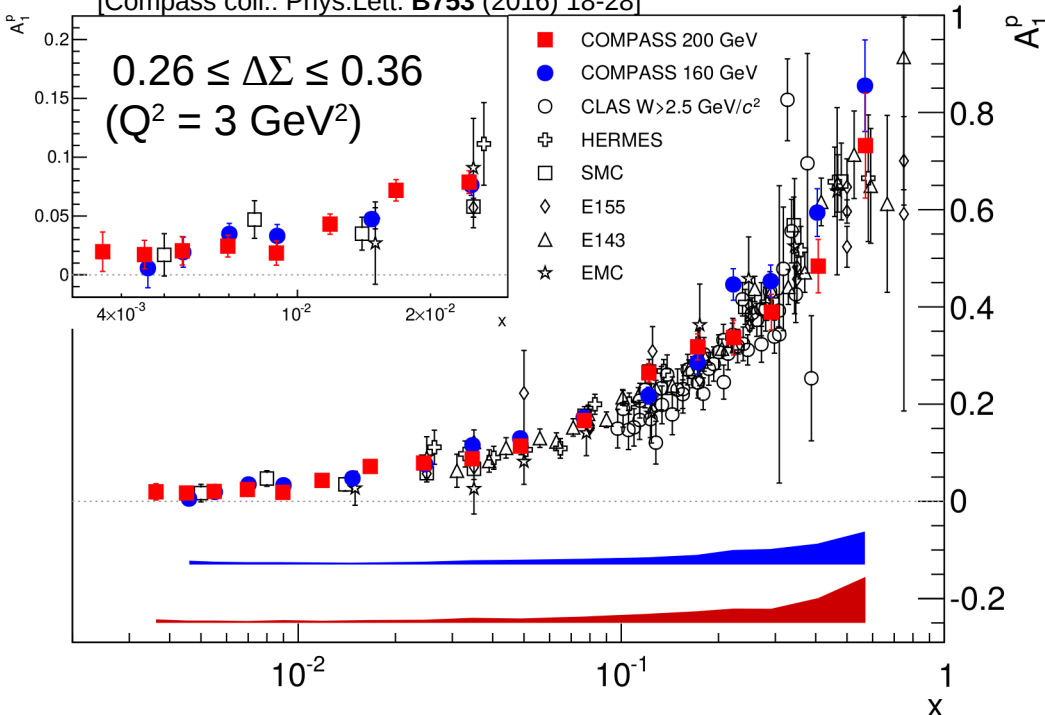
$\Delta G$  ? (Phenix, Compass)

$$\Delta g/g = 0.113 \pm 0.038(\text{stat.}) \pm 0.036(\text{syst.})$$

[Compass coll.: Eur.Phys.J. **C77** (2017) no.4, 209]

Longitudinal double Spin Asymmetry  $A_1^p$

[Compass coll.: Phys.Lett. **B753** (2016) 18-28]



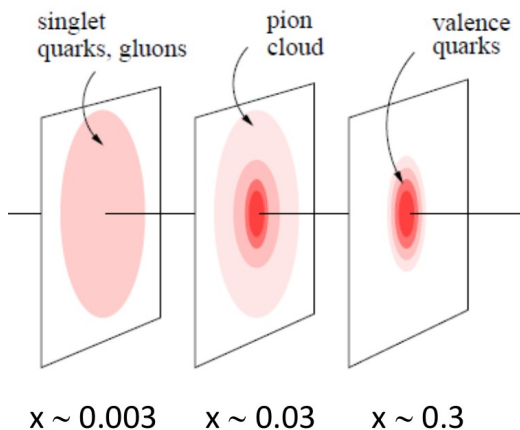
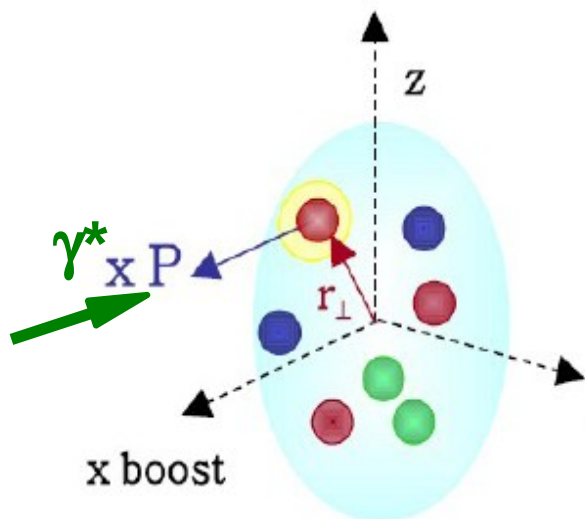
The quarks and gluons contribute to less than  $\frac{1}{2}$  of the total nucleon spin  
 $\Rightarrow$  **Spin puzzle !**

## Form Factors and spin puzzle : Connection with Generalized Parton Distributions (GPDs)

=> Correlation  $r_{\perp} \leftrightarrow xP$

=> **Orbital Angular momentum**

=> Nucleon tomography (“strong size”)

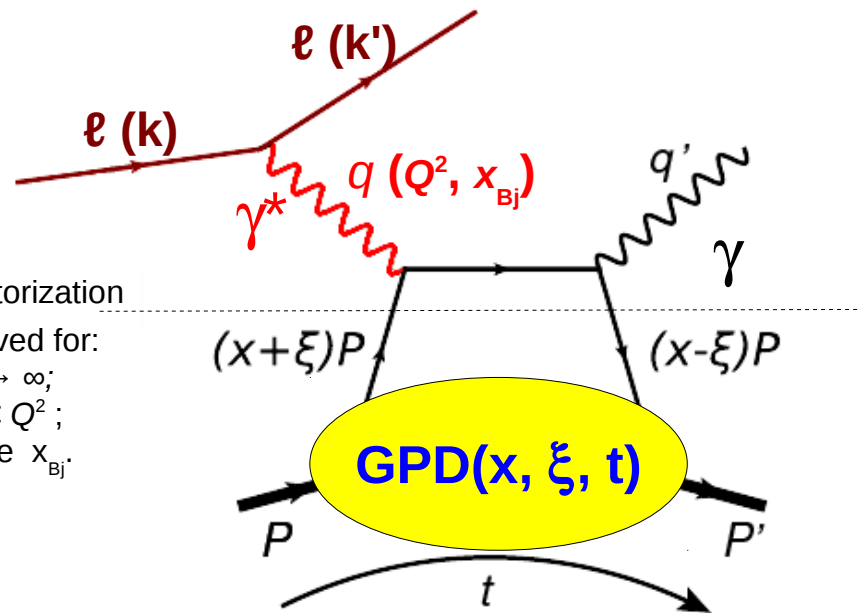


$x \sim 0.003$     $x \sim 0.03$     $x \sim 0.3$

Tomographic parton images of the nucleon

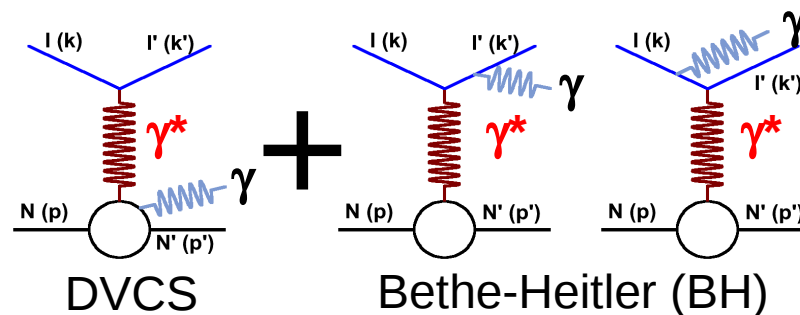
Exclusive reactions

(DVCS:  $ep \rightarrow ep\gamma$ , HEMP:  $ep \rightarrow ep\pi$ )



Factorization

proved for:  
 $Q^2 \rightarrow \infty$ ;  
 $t \ll Q^2$ ;  
finite  $x_{Bj}$ .



$$\sigma^{lp \rightarrow lp\gamma} \propto |BH|^2 + |DVCS|^2 + 2|DVCS||BH|$$

NB: calculation of Bethe-Heitler cross section involves EM Form Factors



## Form Factors and spin puzzle :

### Connection with Generalized Parton Distributions (GPDs)

=> Correlation  $r_{\perp} \leftrightarrow xP$

=> **Orbital Angular momentum**

=> Nucleon tomography (“strong size”)

4 “chiral-even” + 4 “chiral-odd” GPDs:

$$H^q, E^q, \tilde{H}^q, \tilde{E}^q \quad H_T^q, E_T^q, \tilde{H}_T^q, \tilde{E}_T^q$$

In practice: the **observables** are not the GPDs, but the **Compton Form Factors (CFF)**, (moments in  $x$  of the GPDs):

$$\mathcal{F} = \int_{-1}^1 dx \mathcal{C}(x, \xi) F(x, \xi, t)$$

=> First moments in  $x$  of the GPDs:

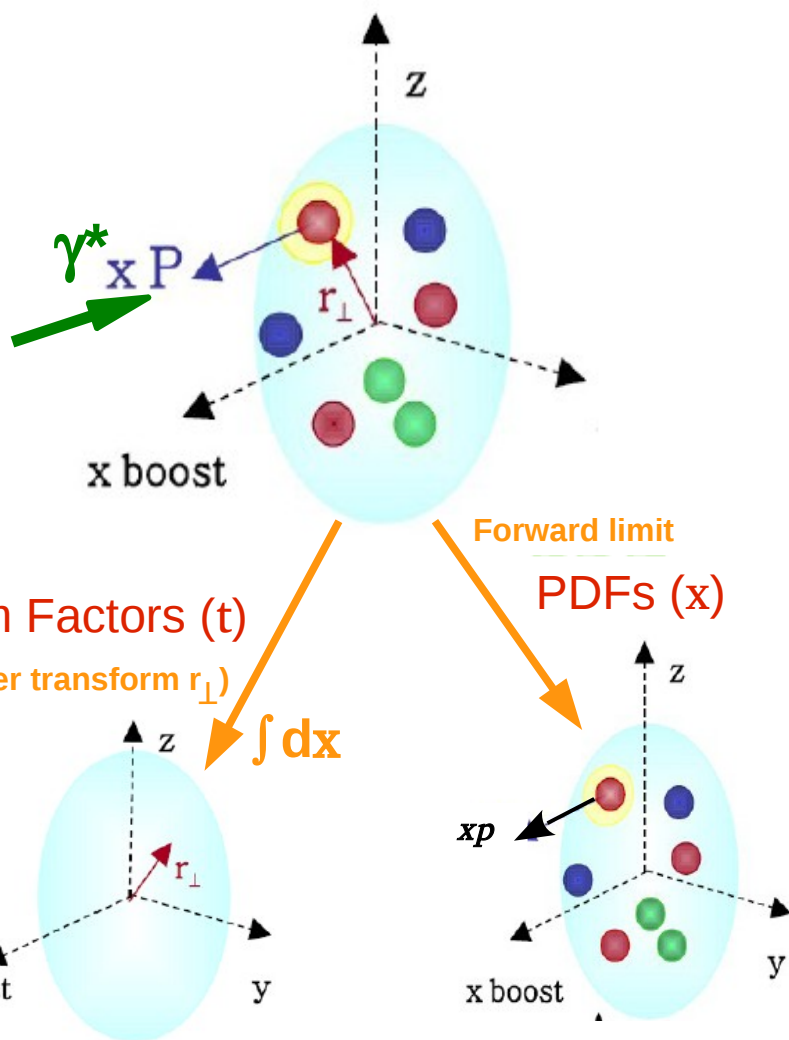
#### Electroweak Form Factors

$\int_{-1}^1 dx H^q(x, \xi, t) = F_1^q(t)$	$\int_{-1}^1 dx \tilde{H}^q(x, \xi, t) = g_A^q(t)$
$\int_{-1}^1 dx E^q(x, \xi, t) = F_2^q(t)$	$\int_{-1}^1 dx \tilde{E}^q(x, \xi, t) = g_P^q(t)$

Higher moments: **Ji sum rule** (direct link with quark total angular momentum  $J$ ):

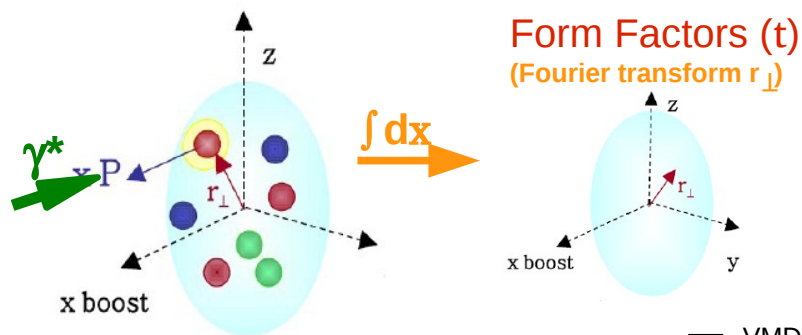
$$\int_{-1}^1 dx x [H^q(x, \xi, t) + E^q(x, \xi, t)] = 2 J_q$$

$$(J_q = L_q + S_q)$$



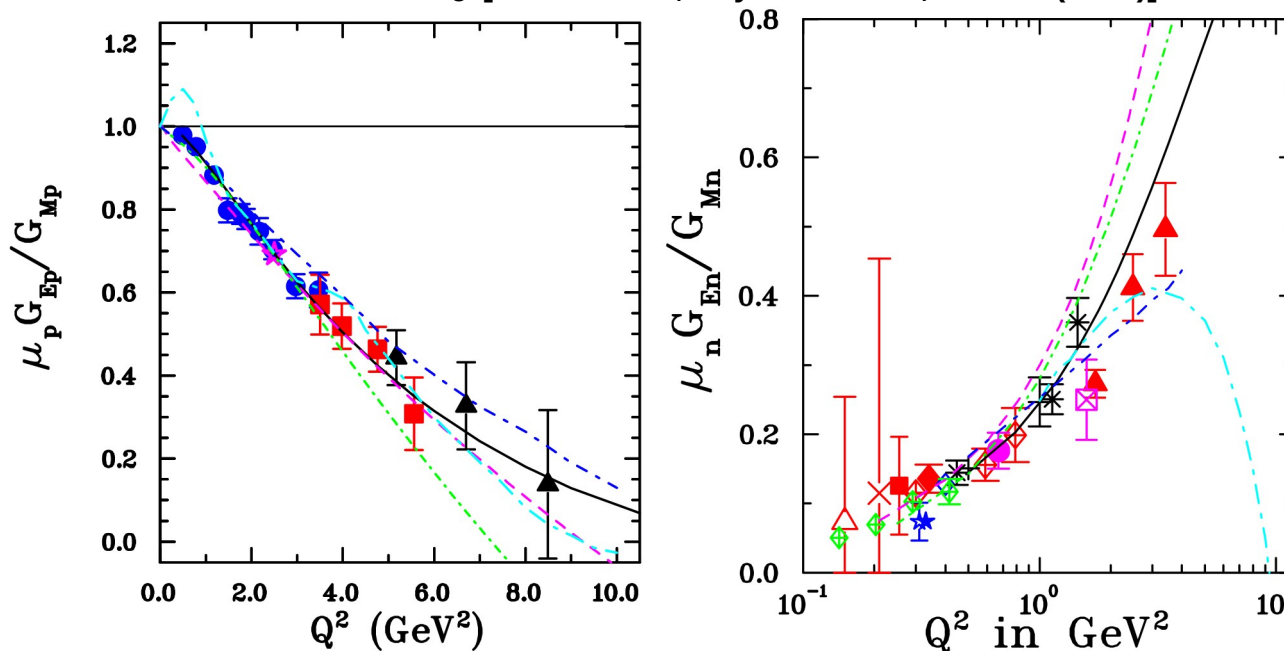
## Form Factors and spin puzzle : Connection with Generalized Parton Distributions (GPDs)

“Feedback”: GPD calculations may also be used to (re)calculate FFs



NB: FF were used in many early GPD models as a simple *ansatz* :  
 $GPD(x, \xi, t) = FF(t) * PDF(x)$

- VMD e.g. [Lomon, arXiv:nucl-th/0609020 (2006)]
- CQM e.g. [Gross, Ramalho, Pena. Phys. Rev. **C77**, 015202 (2008)]
- DSE e.g. [Cloet, Roberts, Thomas, Phys. Rev. Lett. **111**, 101803 (2013)]
- DSE quark-diquark e.g. [Cloet, Miller, Phys. Rev. **C86**, 015208 (2012)]
- **GPD e.g. [Guidal et al., Phys. Rev. **D72**, 054013 (2005)]**



## Overview

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### **Nucleon Form Factors with Super BigBite Spectrometer (SBS):**

- Super BigBite Spectrometer apparatus in Hall A at Jefferson Lab 12 GeV;
- SBS experimental program: Nucleon Form Factors at high  $Q^2$ ;
- Impact of the Form Factor measurements from SBS.

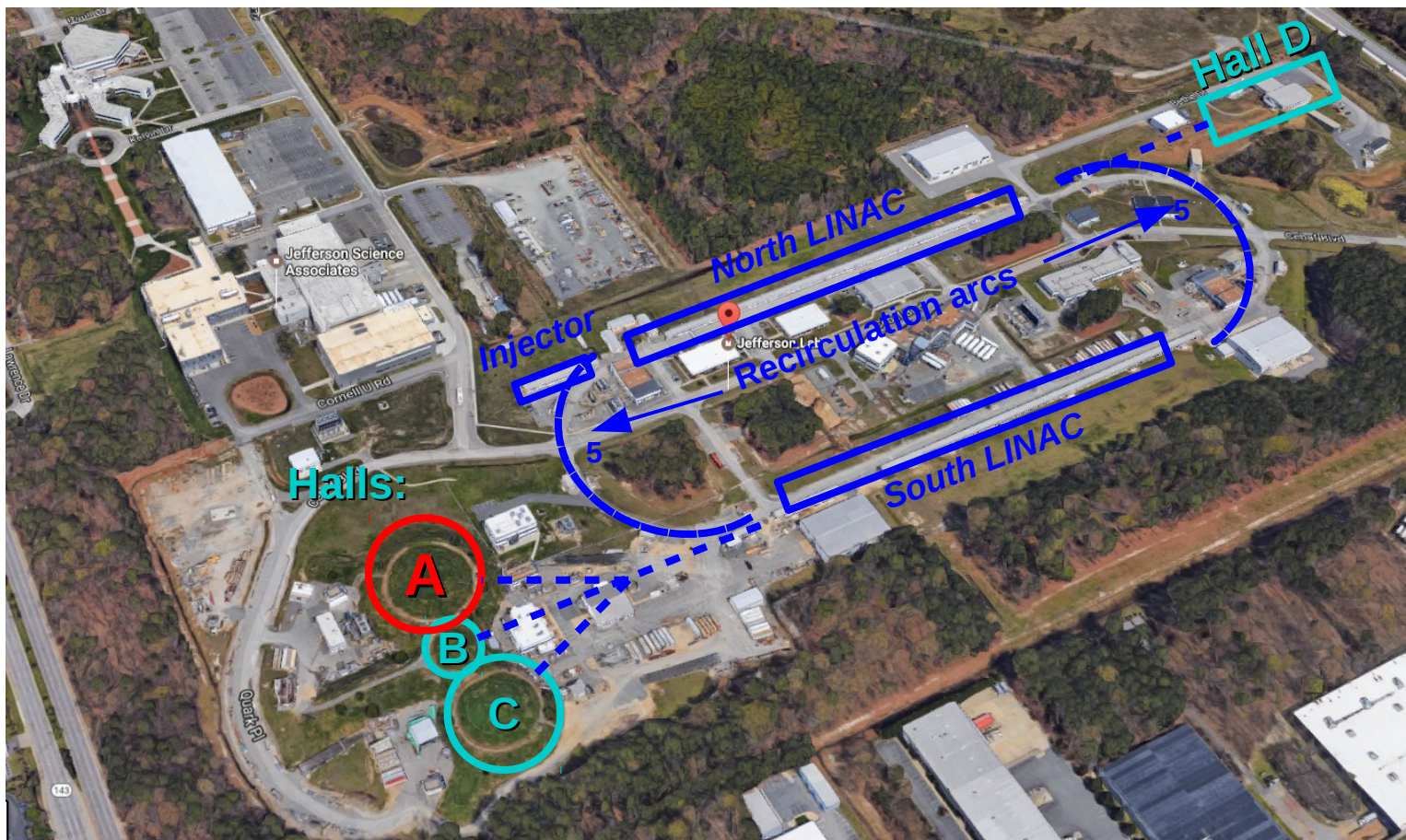
### **Summary**

## Super BigBite Spectrometer apparatus in Hall A at Jefferson Lab 12 GeV.

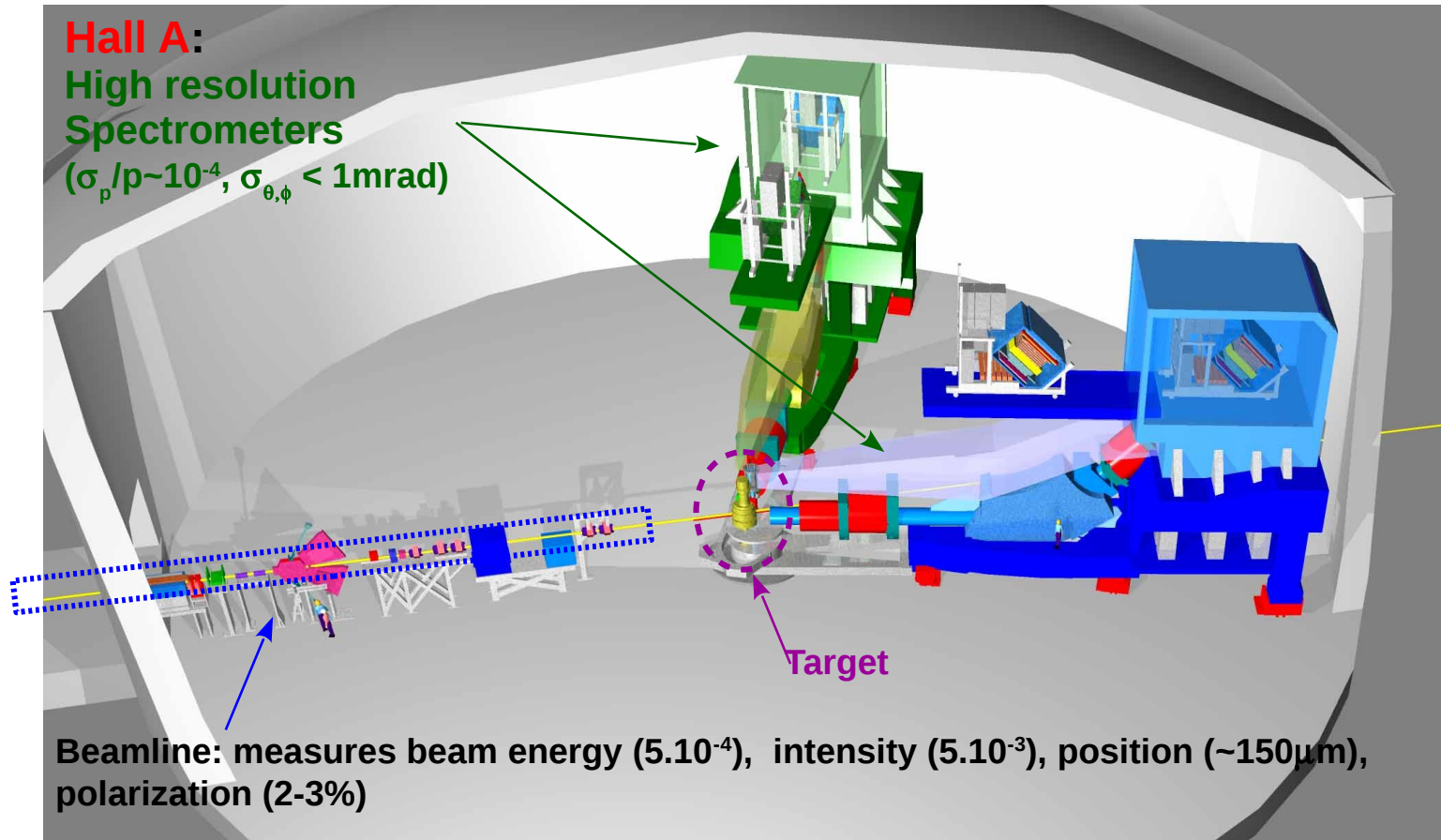
Jefferson Lab @ 12 GeV:

Continuous wave beam,  $I_{\text{max}} \sim 80 \mu\text{A}$ ,  $\text{Pol}_{\text{beam max}} \geq 85 \%$ ,

$E_{\text{max}} = 11 \text{ GeV}$  in Halls A, B, C (12 GeV for Hall D only).



# Super BigBite Spectrometer apparatus in Hall A at Jefferson Lab 12 GeV.



# Super BigBite Spectrometer apparatus in Hall A at Jefferson Lab 12 GeV.

## Super BigBite spectrometer:

Medium solid angle spectrometer with *modular detector package* behind a dipole magnet.

**one of the major new projects for Hall A @ Jefferson Lab 12 GeV.**

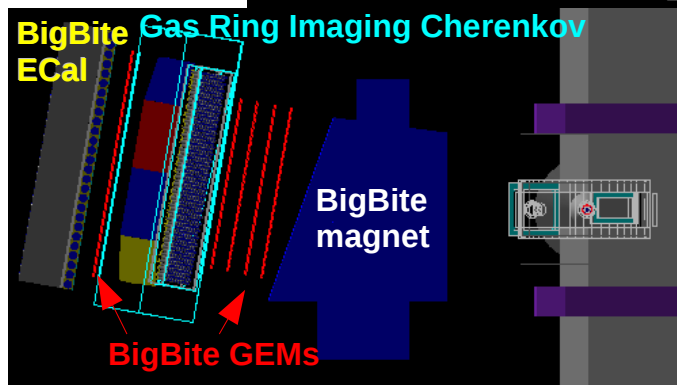
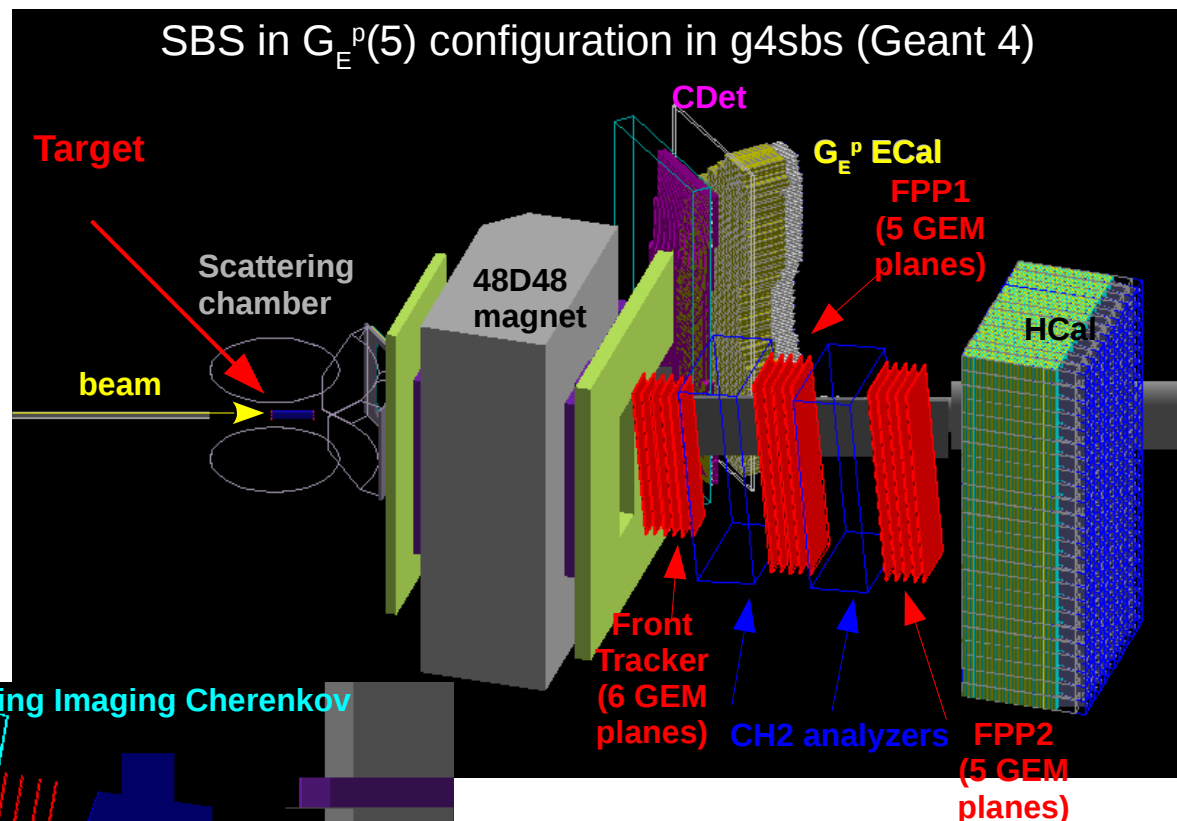
*Earliest run start: 2019, ~200 running days approved;*

## Physics programs:

- **Form factors at high  $Q^2$ :**
  - \*  $G_M^n$  ( $LD_2$ ),  $G_E^n$  (pol.  $^3He$ );
  - \*  $G_E^p$  ( $LH_2$ , recoil pol);
- **Semi-Inclusive DIS ( $^3He$ );**
- **Tagged DIS**

## Other new SBS subsystems:

- \* Ring Imaging Cherenkov (SIDIS);
- \* GEM trackers (SIDIS);
- \* radial TPC (TDIS);
- \* Large Angle Calorimeter (TDIS);
- + **new detector package for BigBite:**
- \* GEM trackers;
- \* New hodoscope;
- \* Gas Ring Imaging Cherenkov



# Super BigBite Spectrometer apparatus in Hall A at Jefferson Lab 12 GeV.

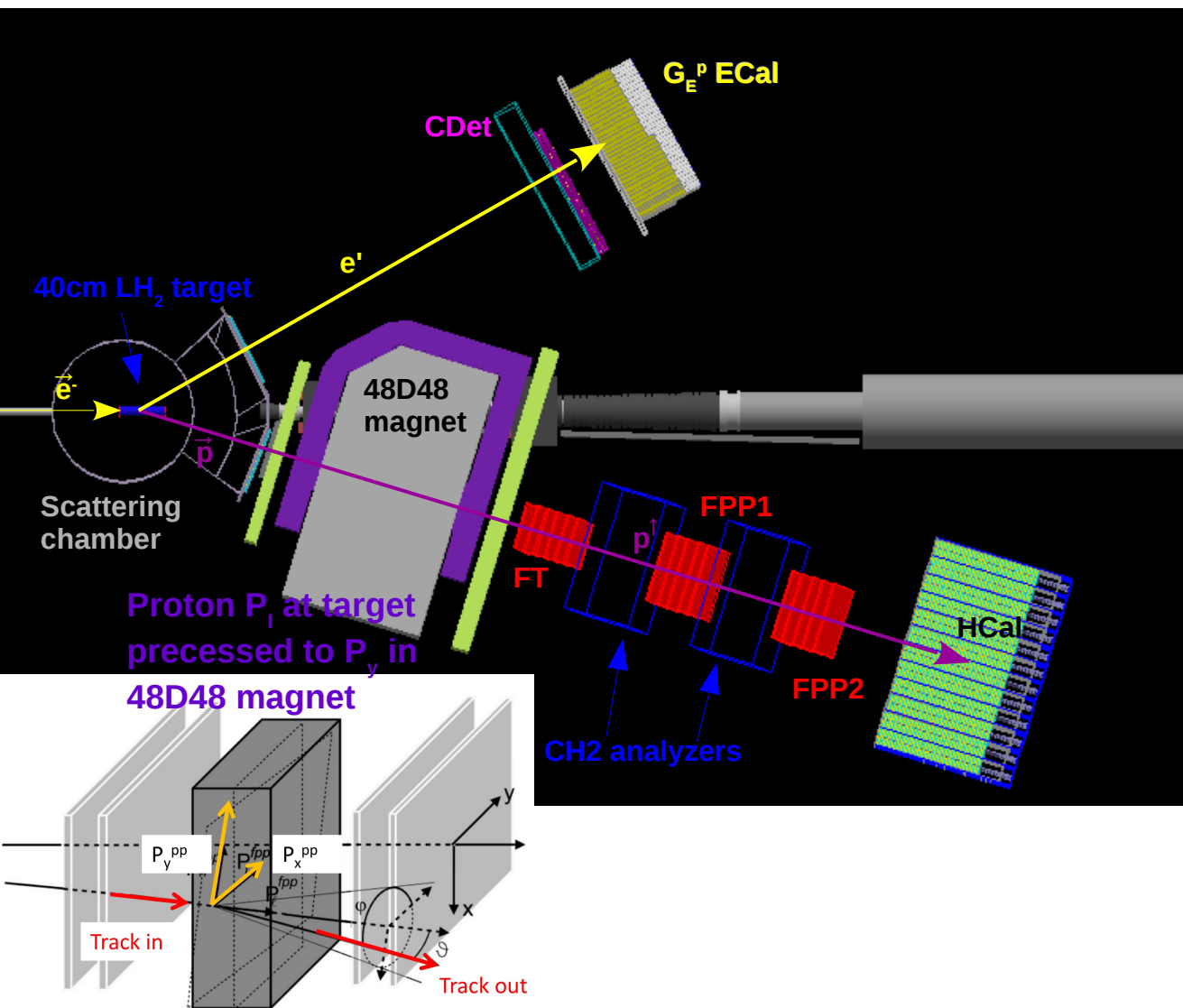
## Super BigBite Spectrometer Collaboration: *Institutions involved*

- \* Argonne National Lab. (USA)
- \* Carnegie Mellon U. (USA);
- \* Christopher Newport U. (USA);
- \* Hampton U. (USA);
- \* Idaho State U. (USA);
- \* INFN Bari (Italy);
- \* INFN Genova (Italy)
- \* INFN Roma, (Italy);
- \* James Madison U. (USA);
- \* Jefferson Lab. (USA);
- \* Mississippi State U. (USA);
- \* Norfolk State U. (USA);
- \* Norfolk State U. (Norfolk, USA);
- \* North Carolina A&T U. (Greensboro, USA);
- \* North Carolina Central U. (Durham, USA);
- \* Ohio U. (USA);
- \* St Mary's U. (Canada);
- \* Stony Brook U. (USA);
- \* U. of Connecticut (USA);
- \* U. of Glasgow (Glasgow, Scotland);
- \* U. of Virginia (USA);
- \* U. of William and Mary (USA);
- \* Yerevan State U. (Armenia);

=> international collaboration !

## SBS experimental program: Proton electric Form Factor ( $G_E^p$ ) E12-07-109

Purpose: measure ratio  $G_E^p/G_M^p$  up to  $12 \text{ GeV}^2$  with recoil proton polarization ( $\propto P_t/P_l$ )



$$\frac{G_E}{G_M} = -\frac{P_t}{P_l} \frac{E+E'}{2M} \tan\left(\frac{\theta}{2}\right) [1 + o_{2\gamma}]$$

Experimental conditions:

$$I_{\text{beam}} = 75 \mu\text{A}; \text{Pol}_{\text{beam}} \geq 85\%;$$

Proton polarization eff = 50%;

Acceptances:

$$\Delta\Omega_e = 130 \text{ msr}$$

$$\Delta\Omega_p \geq 30 \text{ msr}$$

Resolutions:

$$\text{ECal: } \sigma_E/E \sim 8\%;$$

Proton arm:

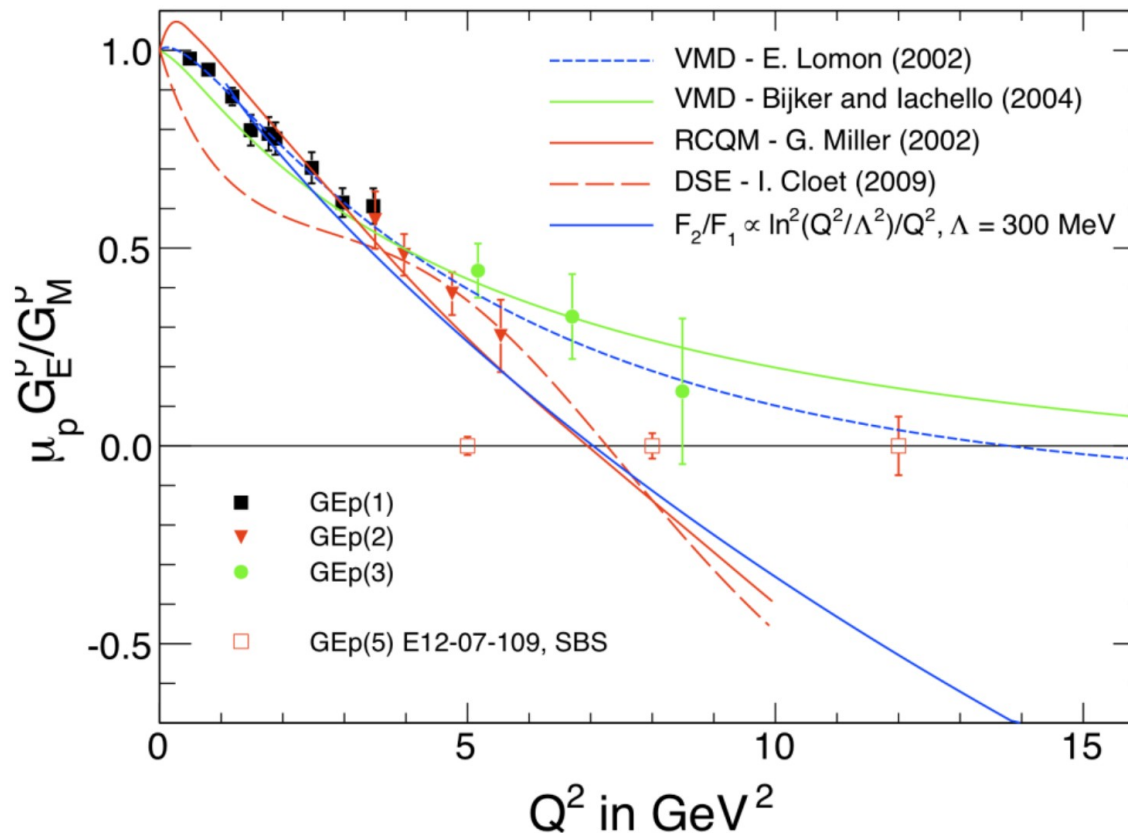
$$* \text{ momentum: } \sigma_p/p = 1\%;$$

$$* \text{ angle: } 1\text{mrad}$$

$$* \text{ vertex reconstruction: } 5\text{mm}$$



## SBS experimental program: Proton electric Form Factor ( $G_E^p$ )



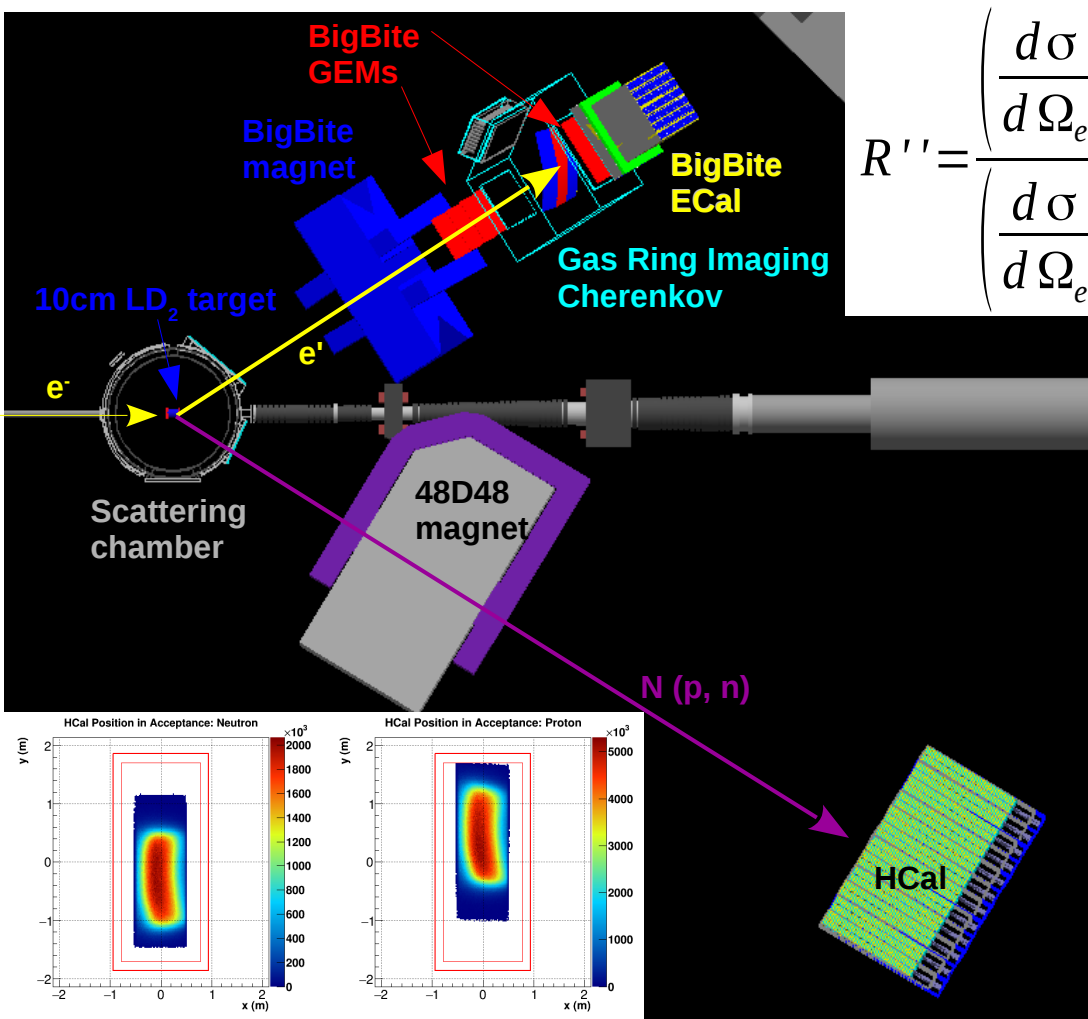
- \* Measurement of  $G_E^p$  at  $Q^2 = 12 \text{ GeV}^2$  (**unprecedented**), with excellent statistical accuracy; lower  $Q^2$  points will *greatly surpass statistical accuracy* of previous measurements
- \* additional constraints on FF models: **selection of best descriptions of  $G_E^p/G_M^p$**  (and/or improvement of others)

## SBS experimental program: Neutron magnetic Form Factor ( $G_M^n$ )

E12-09-019

Neutron form factors => flavor separation of Dirac-Pauli Form Factors

Purpose: measure  $G_M^n$  up to  $13.5 \text{ GeV}^2$  with quasi-elastic electron scattering on deuterium;  
measure  $R = \sigma(en \rightarrow en)/\sigma(ep \rightarrow ep) \Rightarrow$  many systematic uncertainties cancel in R;



$$R'' = \frac{\left( \frac{d\sigma}{d\Omega_e} \right)_{d(e, e' n)}}{\left( \frac{d\sigma}{d\Omega_e} \right)_{d(e, e' p)}}$$

Nuclear corrections;  
(syst cancel in ratio)  
1 $\gamma$  exchange appx;  
 $G_E^n \leq 1\%(G_M^n) \Rightarrow$

$$R = \eta \frac{\sigma_{Mott} \frac{\tau/\epsilon}{1+\tau} (G_M^n)^2}{\left( \frac{d\sigma}{d\Omega_e} \right)_{p(e, e')}} = \frac{1}{1 + 2(E/M_N) \sin^2(\theta_e/2)}$$

$$\eta = \frac{1}{1 + 2(E/M_N) \sin^2(\theta_e/2)}$$

Experimental conditions:

$$I_{\text{beam}} = 44 \mu\text{A};$$

Acceptances:

$$\Delta\Omega_e = 40 \text{ msr}$$

$$\Delta\Omega_p \geq 30 \text{ msr}$$

Resolutions:

Electron arm (Big Bite):

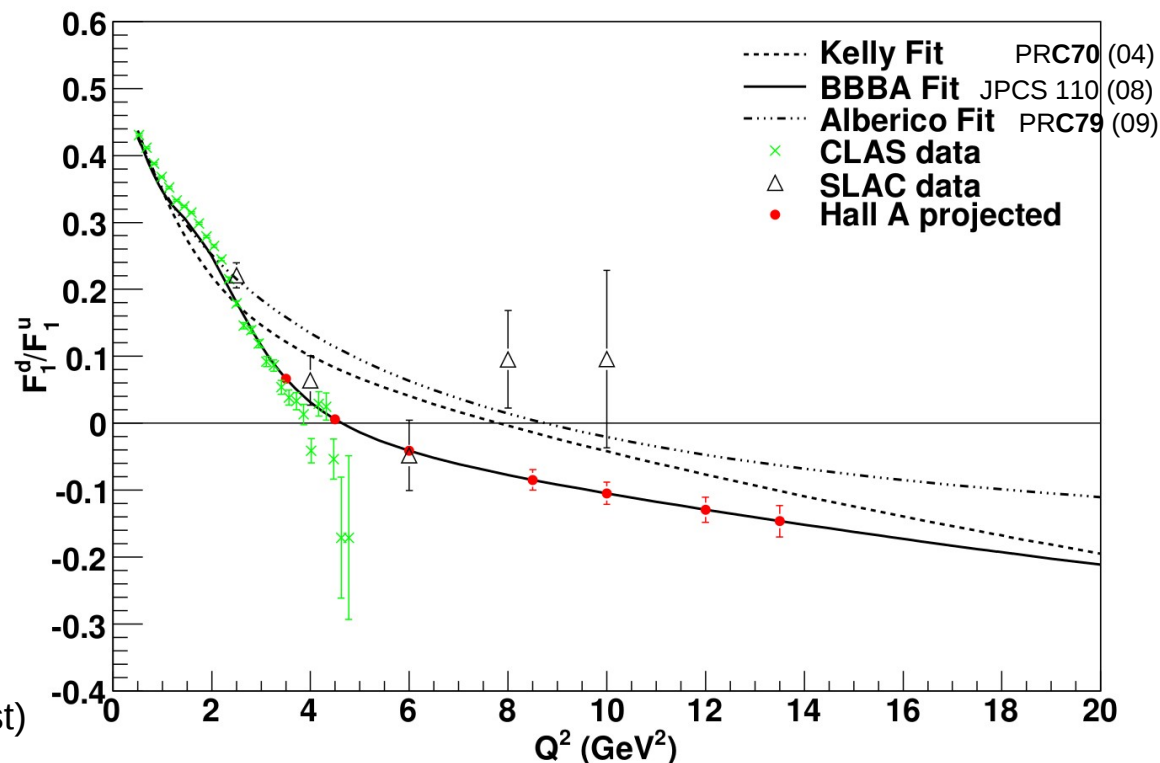
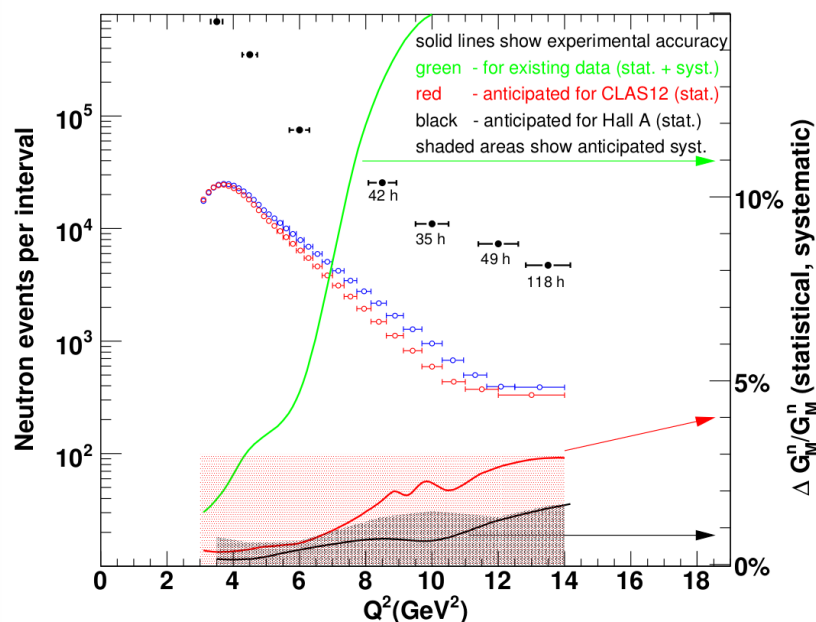
\* momentum:  $\sigma_p/p = 1\%$ ;

\* angle: 1mrad

\* vtx reconstruction: 5mm

HCal:  $\sigma_{\text{position}} \sim 1.5\text{cm}$

## SBS experimental program: Neutron magnetic Form Factor ( $G_M^n$ )



Complementarity with CLAS12 (E12-07-104):  
better coverage from CLAS12, better accuracy (stat-syst)  
from Hall A SBS

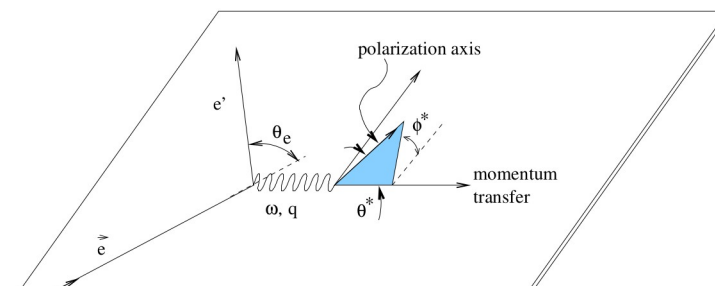
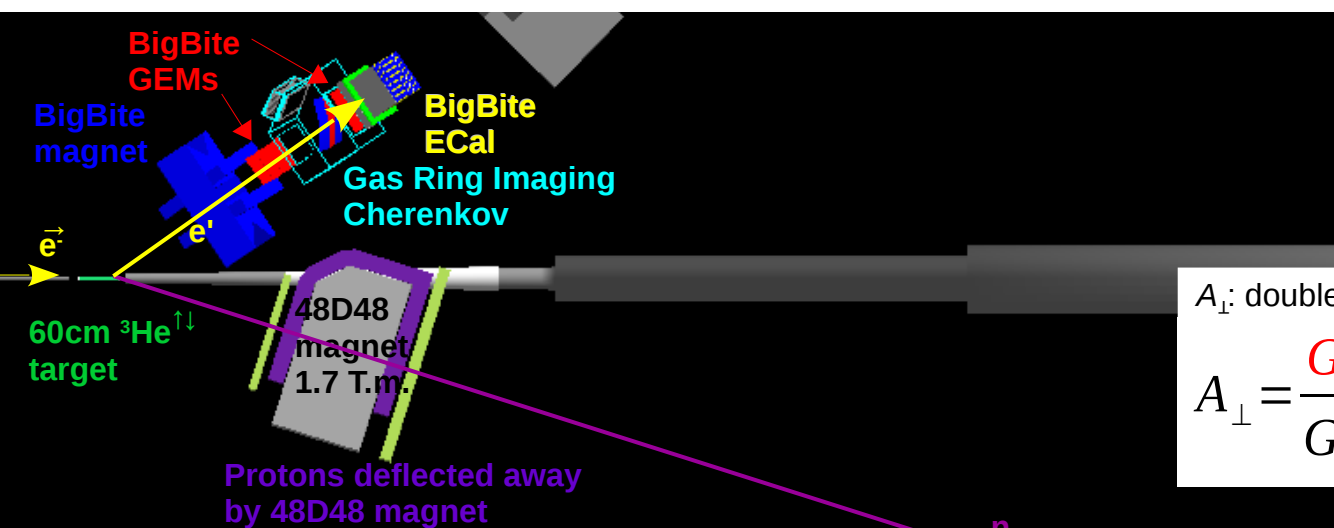
- \* Very accurate measurement of  $G_M^n$  up to  $Q^2 = 13.5 \text{ GeV}^2$  (unprecedented) and possible quark flavor separation of  $F_1/F_2$  (combined with  $G_M^p$  in Hall A).
- \* Complementary measurement from CLAS12
- \* Precision of those measurements will be a great improvement w.r.t. existing data.

## SBS experimental program: Neutron electric Form Factor ( $G_E^n$ )

E12-09-016

Neutron form factors => flavor separation of Dirac-Pauli Form Factors

Purpose: measure ratio  $G_E^n/G_M^n$  with double polarization ( $L_{\text{beam}}, T_{\text{target}}$ )

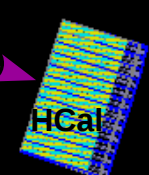


$A_{\perp}$ : double spin asymmetry, target spin  $\perp$  momentum transfer:

$$A_{\perp} = \frac{G_E^n}{G_M^n} \frac{2\sqrt{\tau(\tau-1)} \tan(\theta_e/2)}{(G_E^n/G_M^n)^2 + (\tau + 2\tau(1+\tau) \tan^2(\theta_e/2))}$$

Protons deflected away by 48D48 magnet

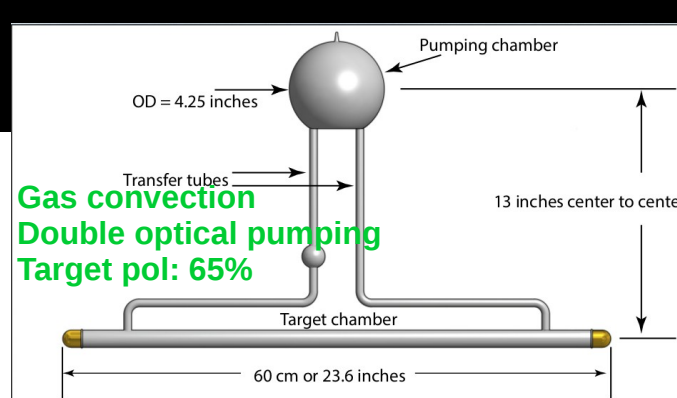
$n$



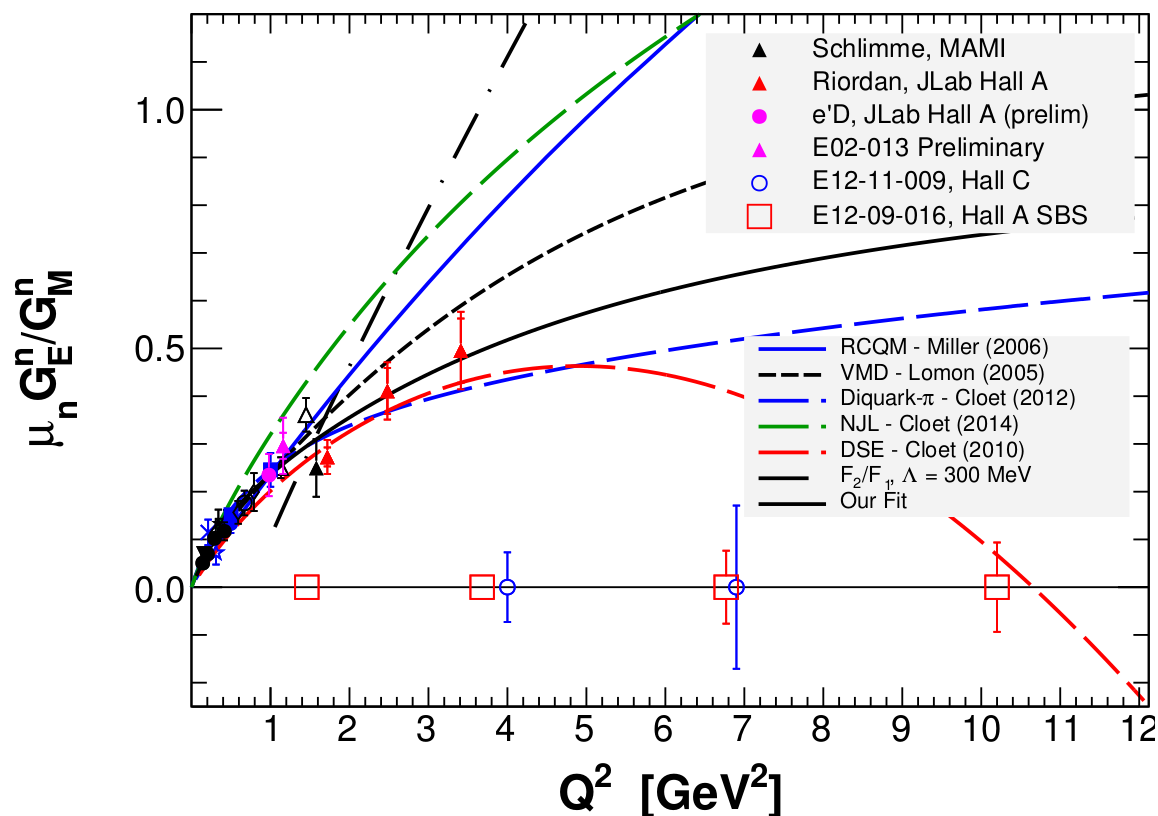
Experimental conditions:  
 $I_{\text{beam}} = 60 \mu\text{A}$ ;  
 $Pol_{\text{beam}} \geq 85\%$ ;  
 $Pol_{\text{tgt}} \geq 65\%$

Resolutions:  
 See two slides ago...  
 Required HCal ToF resolution:  
 $< 1 \text{ ns}$

Acceptances:  
 $\Delta\Omega_e = 40 \text{ msr}$   
 $\Delta\Omega_p \geq 30 \text{ msr}$



## SBS experimental program: Neutron electric Form Factor ( $G_E^n$ )



\* Measurement of  $G_E^n$  up to  $Q^2 = 10$  GeV<sup>2</sup> (unprecedented: *currently no data beyond 4 GeV<sup>2</sup>*), with good statistical precision

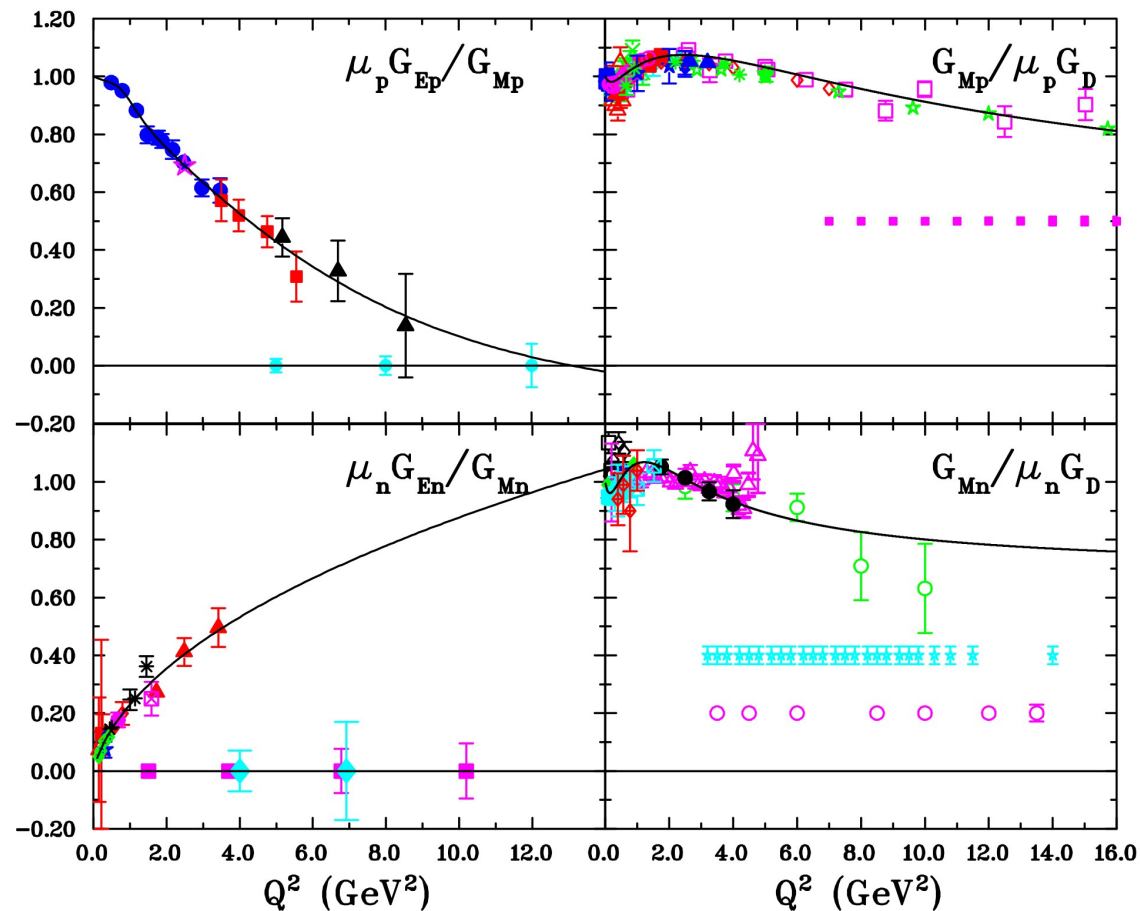
\* Additional constraint on FF models: **selection of best descriptions of  $G_E^n/G_M^n$**  (and/or improvement of others)

## Impact of Form Factor measurements from SBS (I)

\* Many measurements at unprecedented  $Q^2$  values (up to  $10 \text{ GeV}^2$  or more), with good to excellent statistical and systematic accuracy.

=> Great extension of the Form Factors world data set at higher  $Q^2$  !

=> Drastic new constraints on FF models available => improve understanding of nucleon structure.



## Impact of Form Factor measurements from SBS (II)

### Benefits for future GPD experiments (e.g. EIC)

#### Electron Ion Collider

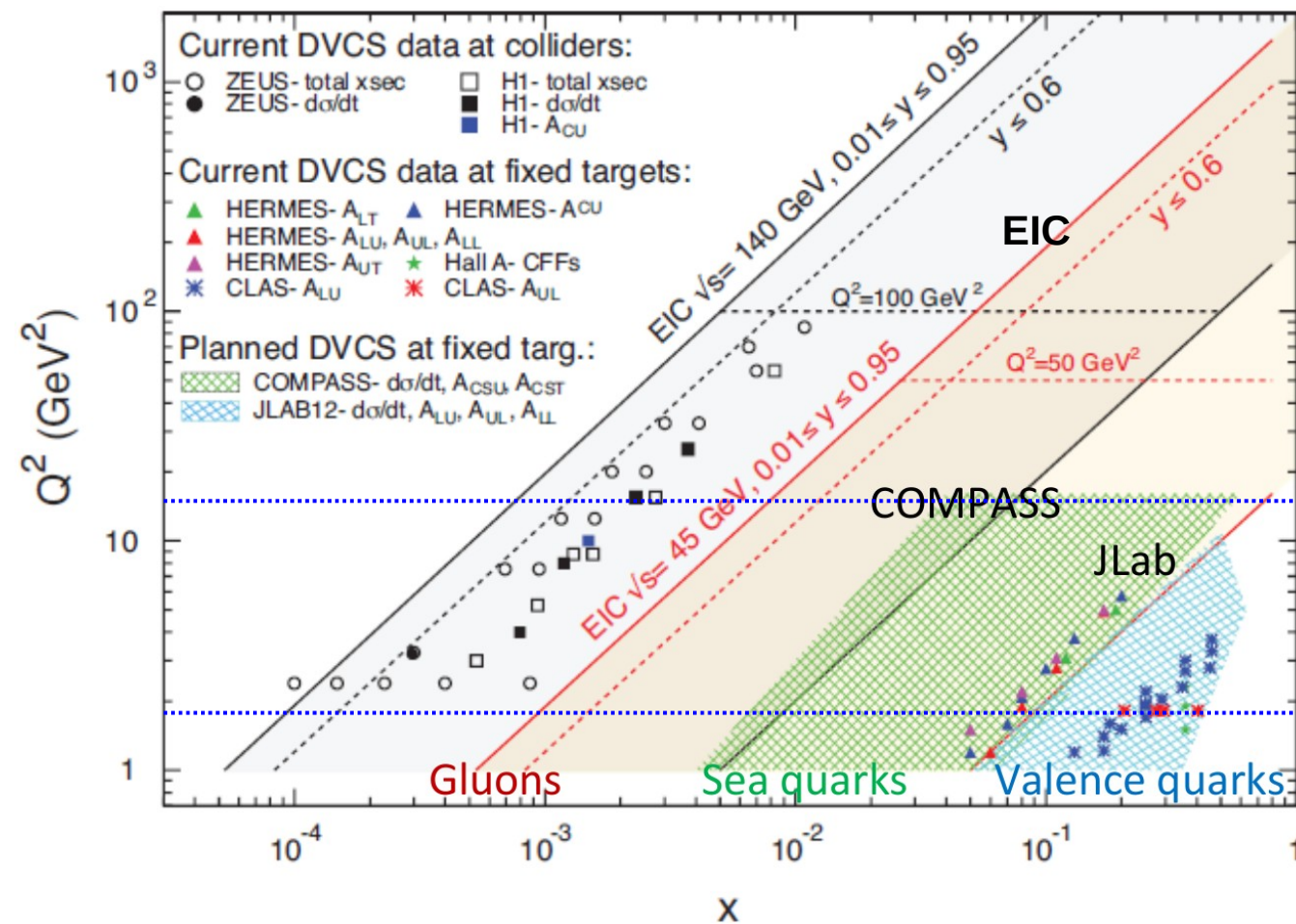
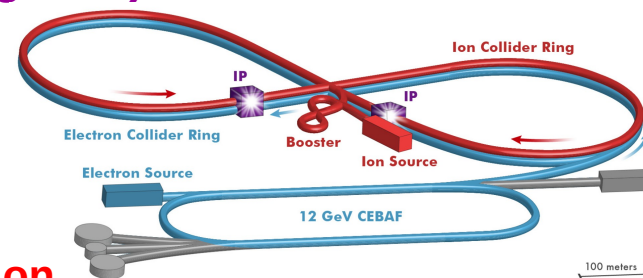
Energies: ~10 GeV electron, ~100 GeV proton

Luminosity:  $10^{33}$  to  $10^{34}$  cm<sup>-2</sup> s<sup>-1</sup> per IP (>100x better than HERA)

Polarization: >70% for both beams

At IP: longitudinal for both beams, transverse for ions only

=> **Great tool for measurement of exclusive channels for GPD extraction.**



***Q<sup>2</sup> Coverage of SBS high precision measurements:***

Their impact *may* go beyond this  $Q^2$  range because of the constraint these measurements will put on current FF models.

## Overview

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### Nucleon structure with (space-like) Form Factors:

- Theory and experimental status;
- Form factors and spin puzzle: connection with GPDs.

### Nucleon Form Factors with Super BigBite Spectrometer (SBS):

- Super BigBite Spectrometer apparatus in Hall A at Jefferson Lab 12 GeV;
- SBS experimental program: Nucleon Form Factors at high  $Q^2$ ;
- Impact of the Form Factor measurements from SBS.

### Summary



## Summary

**Form Factor measurements have known a *huge* regain of interest:**

- at low  $Q^2$  (proton radius puzzle – not mentioned here);
- **at high  $Q^2$**  (proton spin puzzle and GPDs).

**Super BigBite Spectrometer bears a *complete* program to measure Form Factors** ( $G_E^p$ ,  $G_M^n$ ,  $G_E^n$ ), which will greatly extend  $Q^2$  range as well as statistical accuracy of existing measurements;

**The impact of these data will be two-fold:**

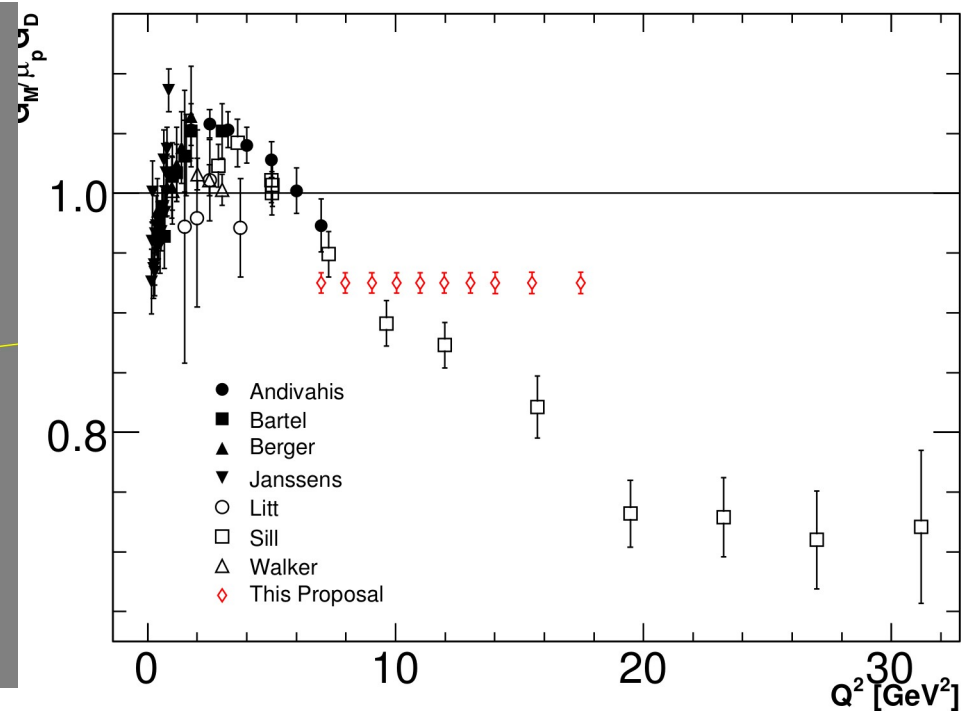
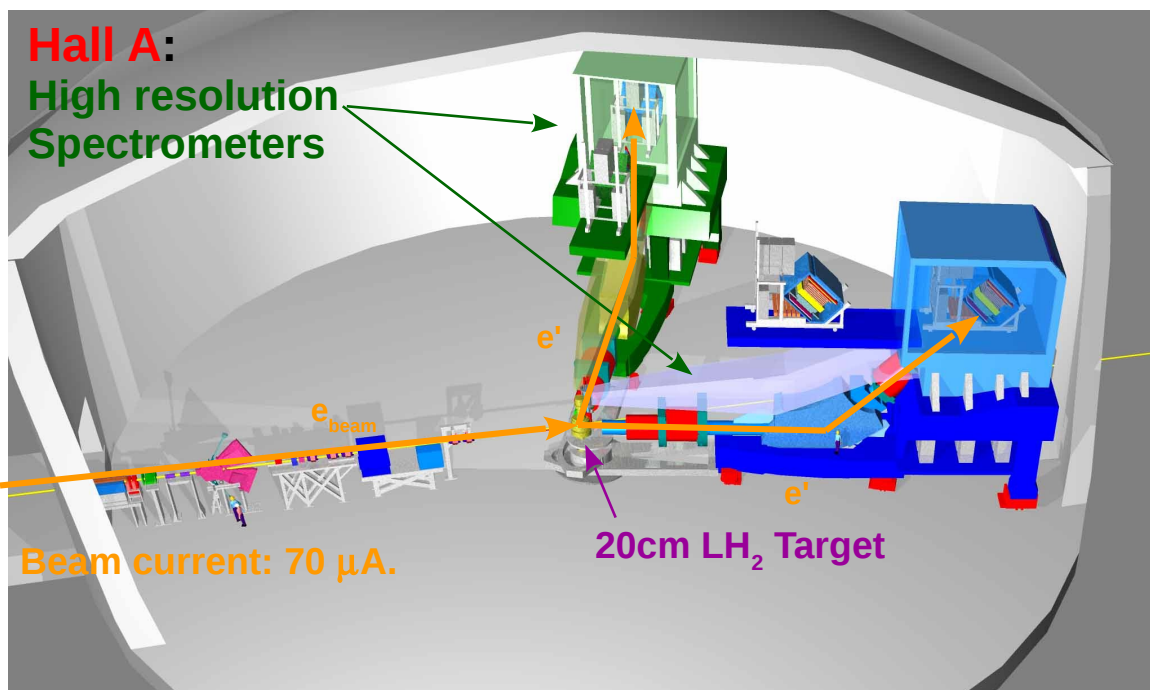
- \* **improve understanding of QCD and nucleon structure** by selecting the most accurate FF description(s) among the many available;
- \* provide **first moments of GPDs for measurements at a future EIC:**

---

**Thank you for your attention !**

## FF experimental program in Hall A: Proton magnetic Form Factor ( $G_M^p$ )

High precision  $G_M^p$  data taken in Hall A 12 GeV with High Resolution Spectrometers (under analysis)

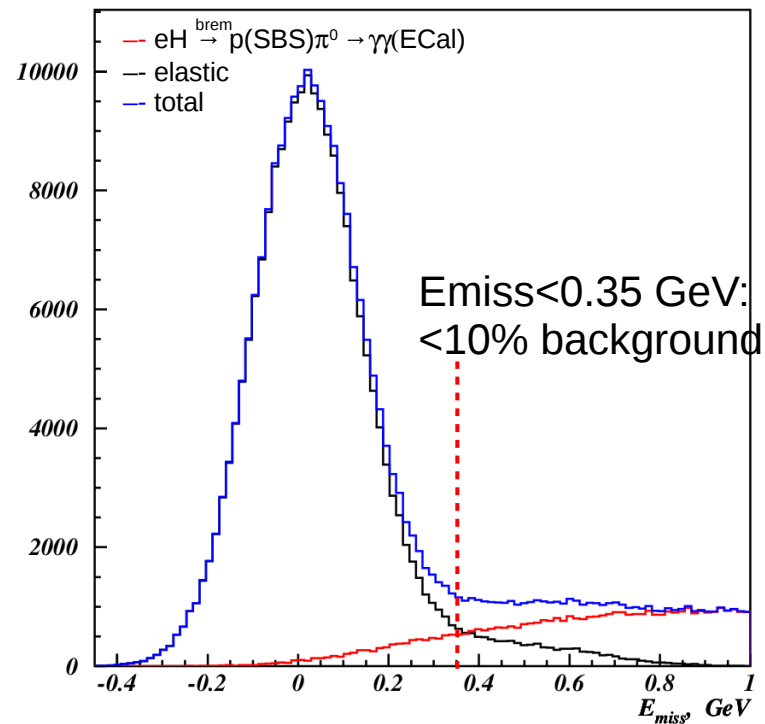
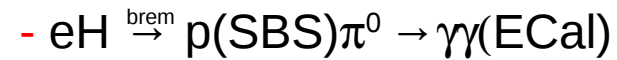


Measured with  $H(e, e')p$

HRS ( $\sigma_p/p \sim 10^{-4}$ ,  $\sigma_{\theta, \phi} < 1\text{mrad}$ ) provides great accuracy for proton selection

## SBS experimental program: Proton electric Form Factor ( $G_E^p$ )

Dominant Background:

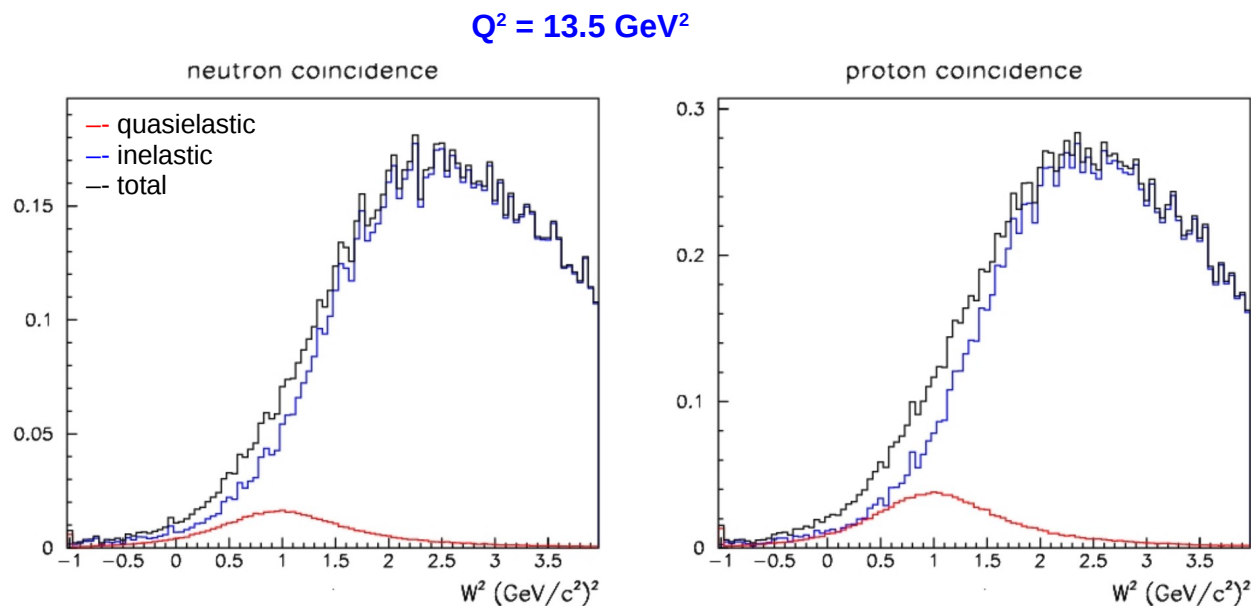


*Presumably low systematics.*

## SBS experimental program: Neutron magnetic Form Factor ( $G_M^n$ ) at high $Q^2$

**Main source of systematics: inelastic contamination**

$Q^2$ (GeV <sup>2</sup> )	$\Delta R/R$ stat. (%)	$\Delta R/R$ syst. (%)	$\Delta G_M^n / G_M^n$ frac. (%)
3.5	0.3	1.5	1.48
4.5	0.3	1.2	1.25
6.0	0.8	1.3	1.24
8.5	1.4	2.6	2.04
10.0	1.3	2.9	2.12
12.0	2.4	2.6	2.26
13.5	3.2	3.2	2.65

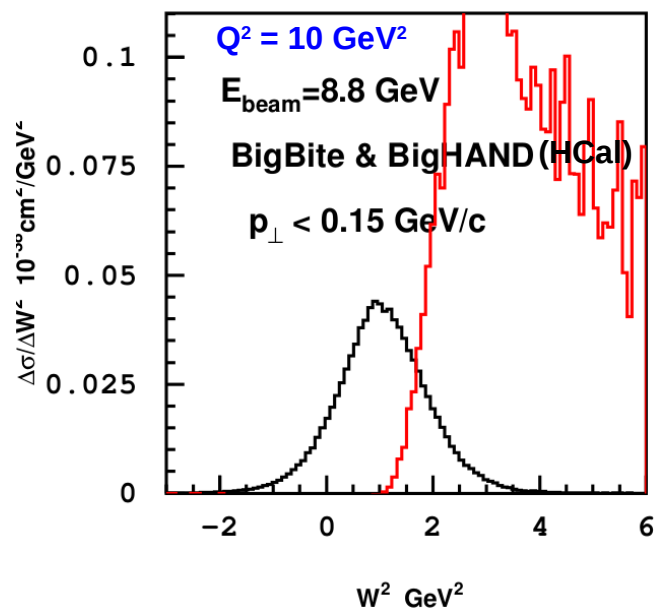


Fractional error on  $G_M^n$  :  $\frac{1}{2} \Delta R/R(\text{tot})$  ( $G_M^n \propto R^{1/2}$ )

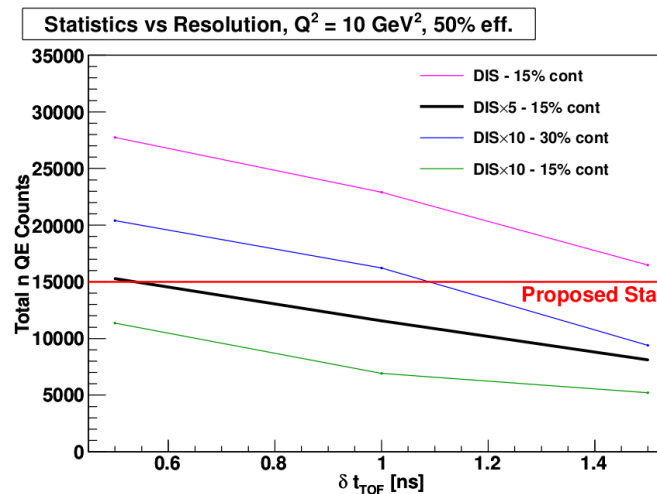
## SBS experimental program: Neutron magnetic Form Factor ( $G_E^n$ ) at high $Q^2$

$Q^2$ (GeV <sup>2</sup> )	$\Delta(G_E^n/G_m^n)/$ ( $G_E^n/G_m^n$ ) stat. (%)	$\Delta(G_E^n/G_m^n)/$ ( $G_E^n/G_m^n$ ) syst. (%)
1.5	1.3	2.4
4.0	6.0	4.4
7.0	19.8	7.3
10.0	22.5	6.6

Main source of systematics: inelastic contamination

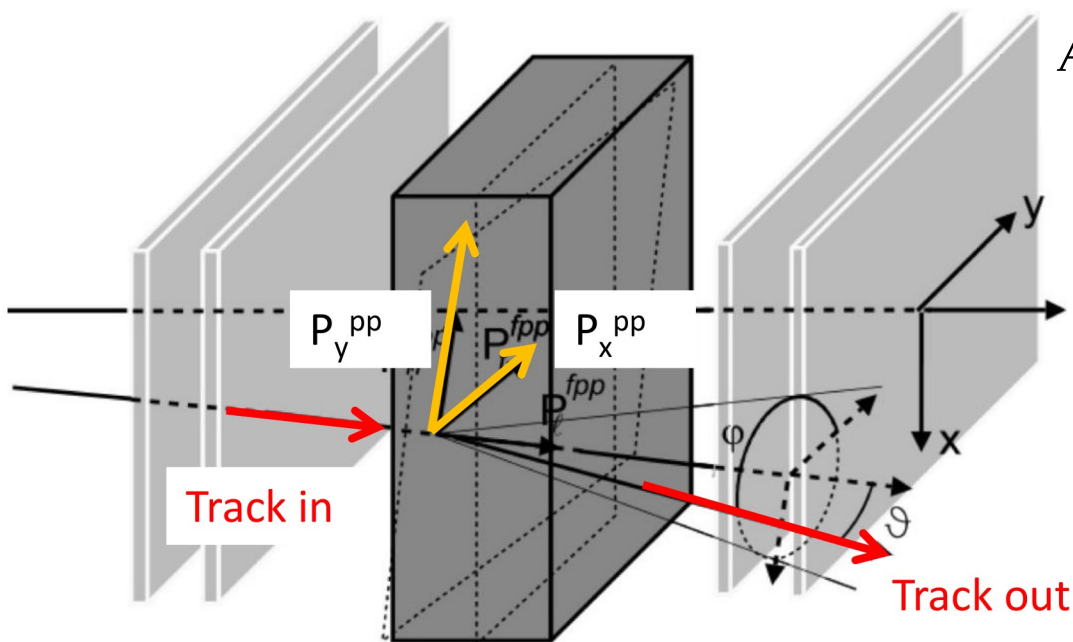


Inelastic contamination reduced with a cut on TOF



## SBS experimental program: Proton electric Form Factor ( $G_E^p$ )

**Focal Plane Polarimeter:** Uses azimuthal asymmetry of the proton scattering off-matter induced by spin-orbit coupling.

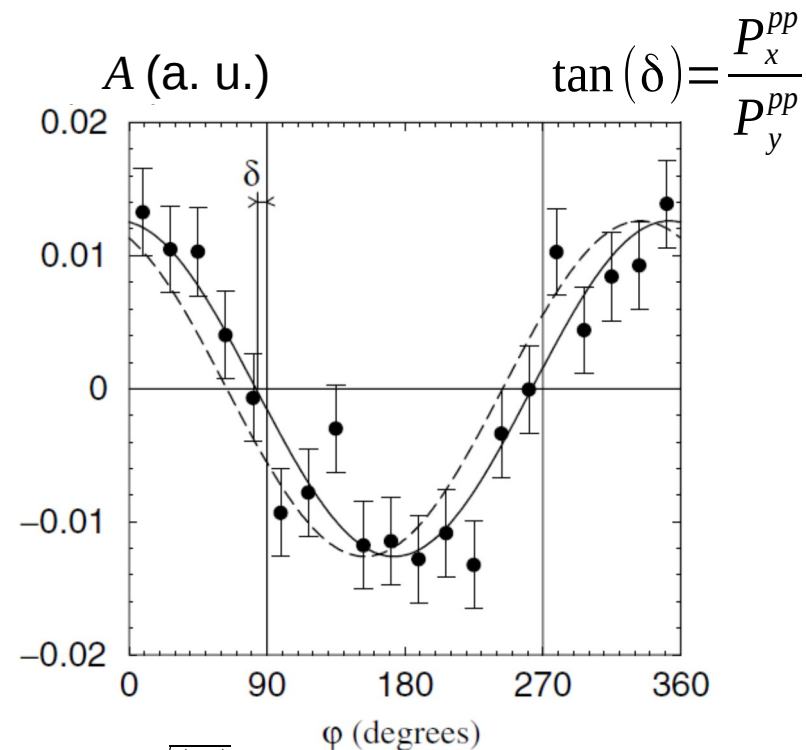


**Scattered proton yield  $f(\text{beam helicity } \pm)$**

$$f^\pm(\vartheta, \phi) = \frac{\epsilon^{pp}(\vartheta, \phi)}{2\pi} = \left[ 1 \pm A_y (P_x^{pp} \sin \phi + P_y^{pp} \cos \phi) \right]$$

$$A = \frac{f^+ - f^-}{f^+ + f^-} = A_y (P_x^{pp} \sin \phi + P_y^{pp} \cos \phi) = A_y \cos(\phi - \delta)$$

**Polarimeter only measures transverse components of polarization wrt proton momentum direction**

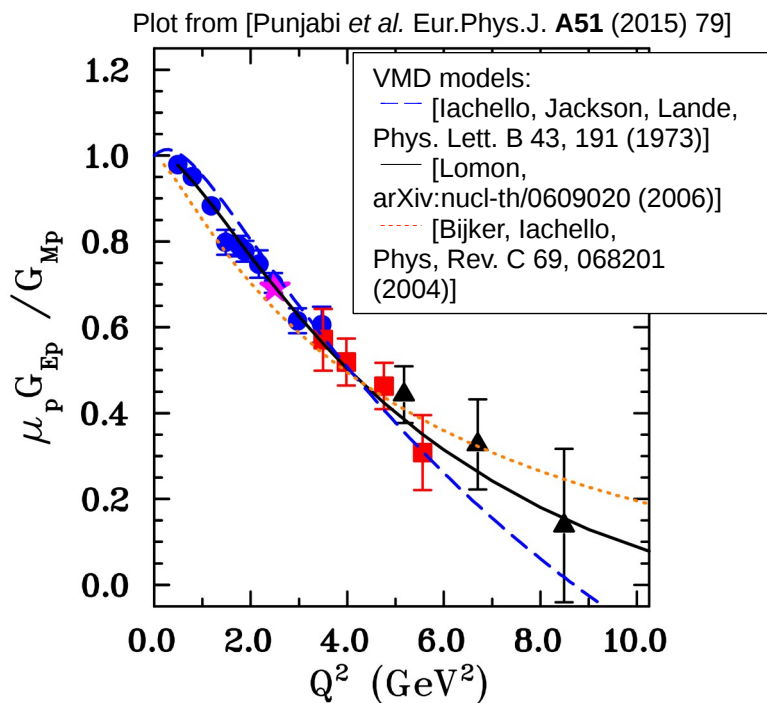
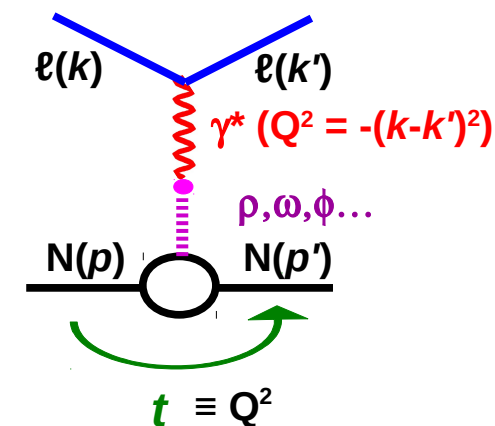


$$\sigma_{P_{x,y}^{pp}} \sim \frac{\sqrt{2}}{A P_e \sqrt{N}} \Rightarrow \text{need max } P_e$$

## Form Factors : Theory and experimental status

### Vector Meson Dominance models:

- \* coupling of photon to vector mesons ( $J^{PC} = 1^{--}$ )
- \* can be analytically continued to timelike region (dispersion analysis)
- => proton radius...



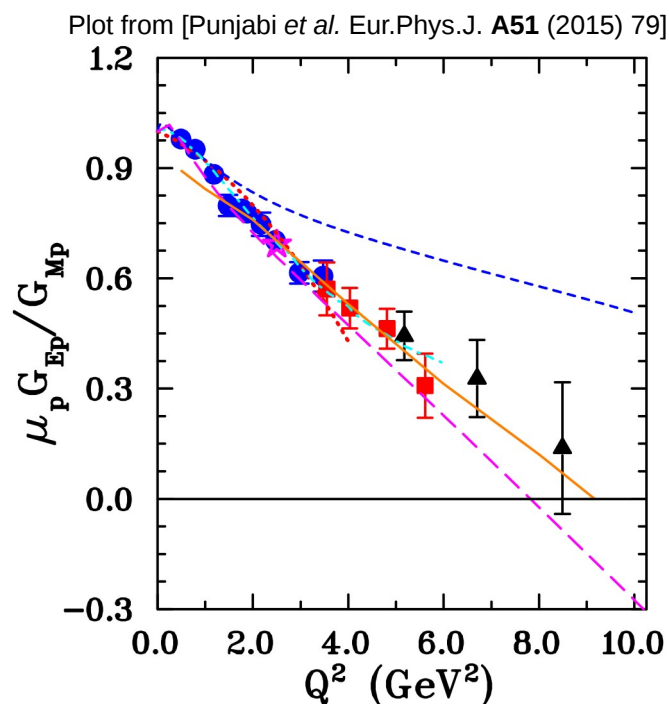
- Data:
- [Jones *et al.* Phys. Rev. Lett **84**, (2000) 1398; Punjabi *et al.* Phys. Rev. Lett **C71**, (2005) 055202]
  - [Gayou *et al.* Phys. Rev. Lett **88**, (2002) 092301]
  - ▲ [Puckett *et al.* Phys. Rev. Lett **104**, (2010) 242301]
  - ☆ [Meziane *et al.* Phys. Rev. Lett **106**, (2011) 132501]



## Form Factors : Theory and experimental status

### Constituant Quark Models:

- \* Nucleon modeled as 3 quarks in a confining potential
  - \* Requires Poincare transformation of constituents/proton before and after interactions;
  - \* exists with many dynamics:
    - Point form (dynamical space and time translations);
    - Instant form (dynamical time translation and boost);
    - Light-front form (dynamical LF transverse rotations and 1 translation component);
- may include additional features (quark FFs, covariant spectator model, pion cloud model,...)



CQM models:

- [Gross *et al.*, Phys. Rev. **C77**, 015202 (2008)]
- [Boffi *et al.*, Eur. Phys. J **A14**, 17 (2002)]
- [de Melo *et al.*, Phys. Lett. **B671**, 153 (2009)]
- [Chung, Coester, Phys. Rev. D**44**, 229 (1991)]
- [Cordarelli *et al.*, Phys. Lett. **B357**, 267 (1995)]

Data:

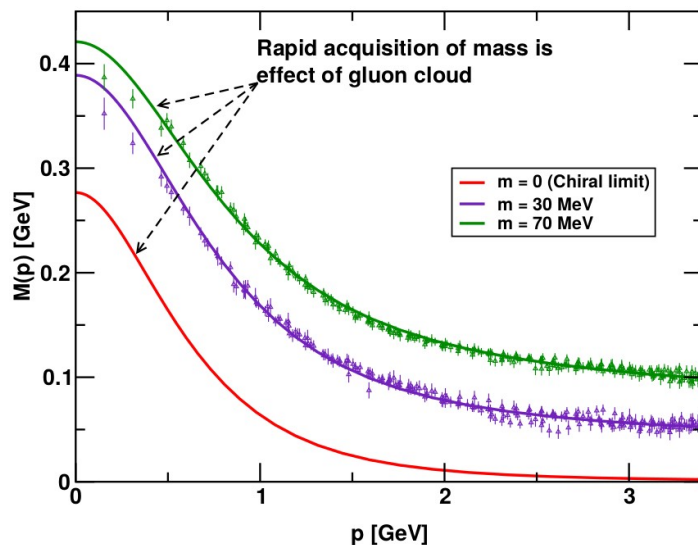
- [Jones *et al.* Phys. Rev. Lett **84**, (2000) 1398; Punjabi *et al.* Phys. Rev. Lett **C71**, (2005) 055202]
- [Gayou *et al.* Phys. Rev. Lett **88**, (2002) 092301]
- ▲ [Puckett *et al.* Phys. Rev. Lett **104**, (2010) 242301]
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## Form Factors : Theory and experimental status

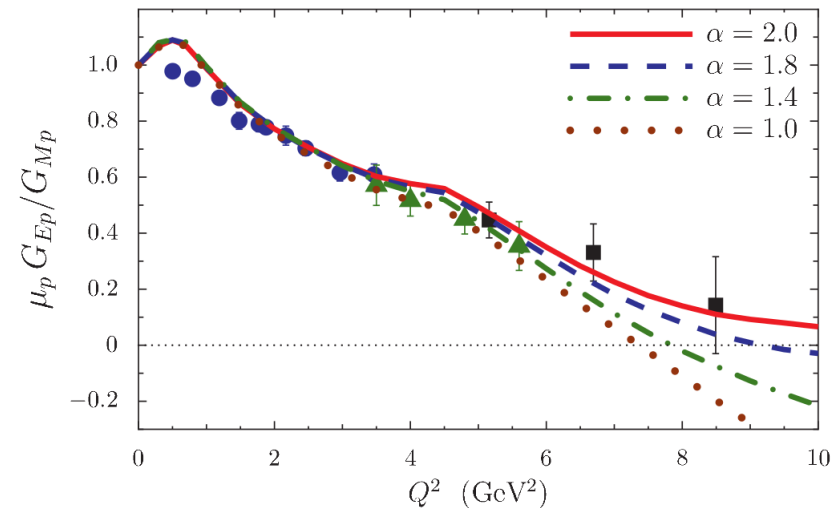
### Dyson Schwinger Equation calculations:

- \* Non Perturbative approximation of QCD
  - \* Infinite set of equations, truncated in such a way that it does not alter QCD symmetries
  - \* May also be used for the calculation of other quantities (e.g. PDFs, GPDs)
- => e.g. describes the *full* quark propagator with “dressing” as function of momentum (agrees with L-QCD)

[Bashir *et al.*, Commun. Theor. Phys. **58**, 79 (2012)]



[Cloet, Roberts, Thomas, Phys. Rev. Lett. **111**, 101803 (2013)]

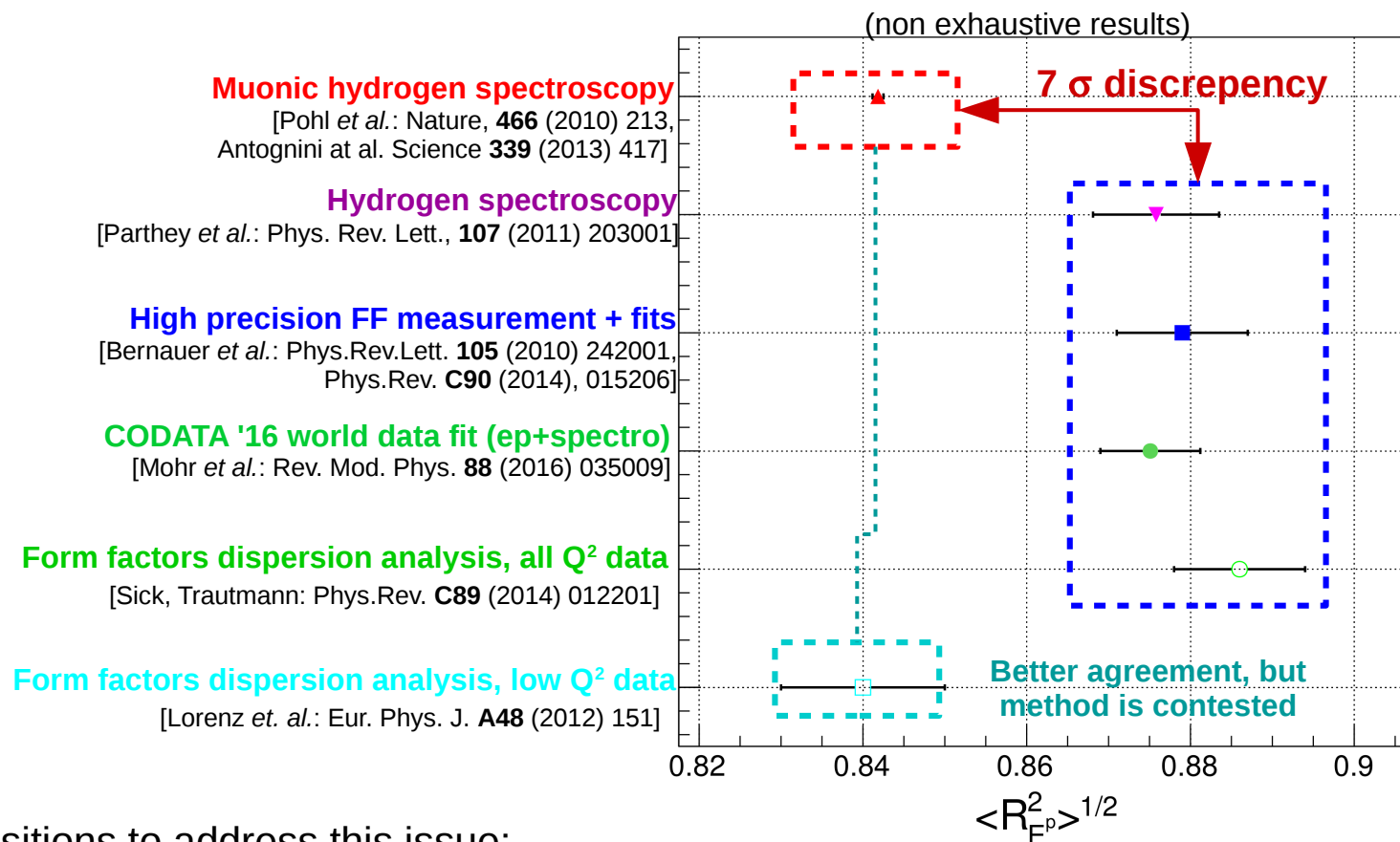


## Form Factors: Open questions and issues

### Proton Radius puzzle:

Form Factors at  $Q^2 = 0 \Rightarrow$  proton charge radius:

$$\langle r_{E_p}^2 \rangle = -6 \left. \frac{dG_E^p}{dQ^2} \right|_{Q^2=0}$$

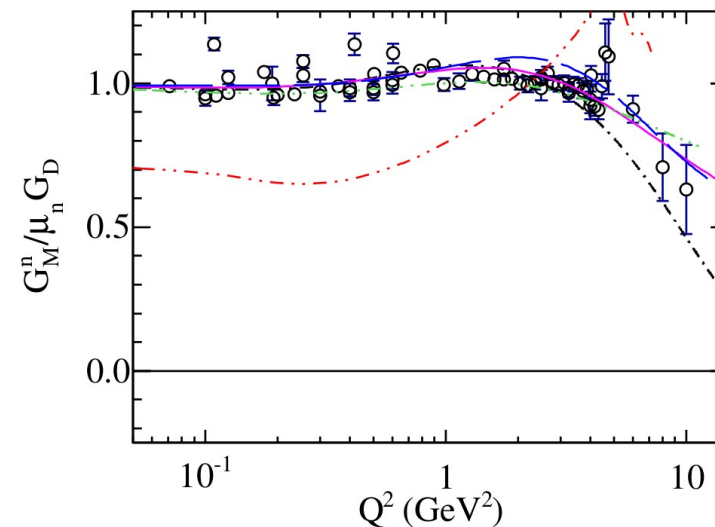
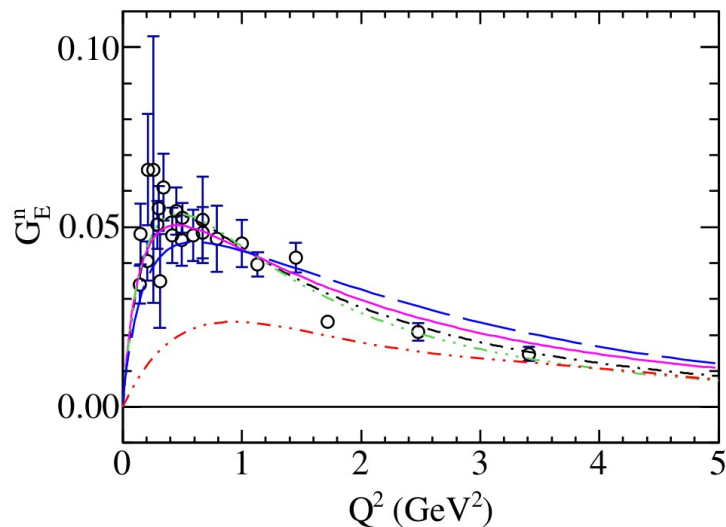
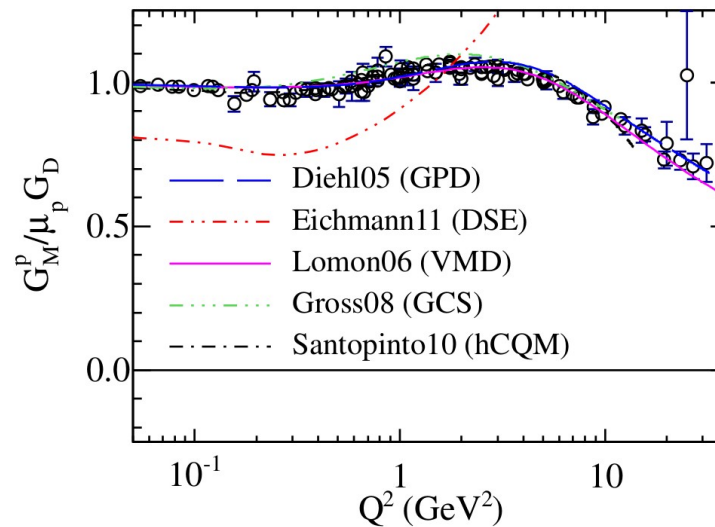
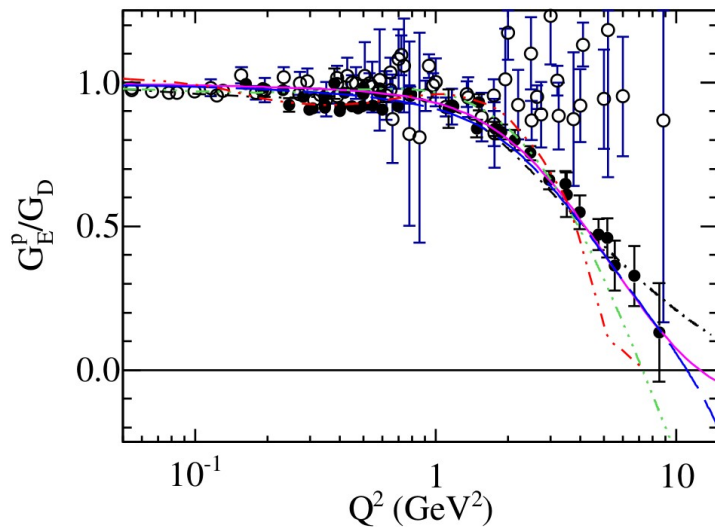


Many propositions to address this issue:

- \* very low  $Q^2$  measurements, down to  $\sim 10^{-3}$  GeV<sup>2</sup> (e.g. initial state radiation at Mainz);
- \* low  $Q^2$  elastic  $ep$  and  $\mu p$  measurement (MUSE @ PSI);

$\Rightarrow$  by providing new constraints on current form factor models and global FF fits, high  $Q^2$  form factor measurements might also give a new insight towards the solution of this issue...

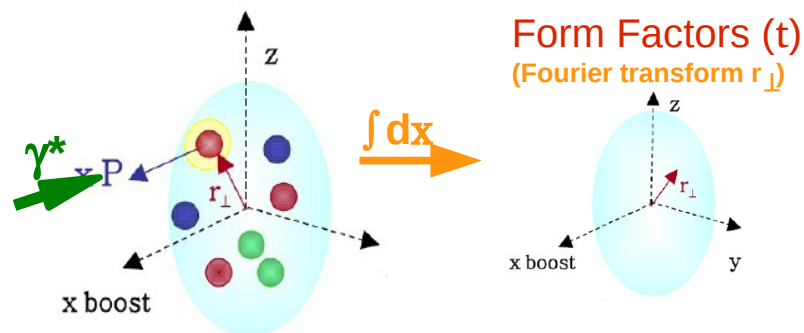
## Form Factors : Theory and experimental status



- \* No data beyond 10 GeV<sup>2</sup> for  $G_E^p$ ,  $G_M^n$ ,  $G_e^n$ ;
- \* FF predictions diverge at higher  $Q^2$  from one model to the other.

## Form Factors and spin puzzle : Connection with Generalized Parton Distributions (GPDs)

“Feedback”: GPD calculations may also be used to (re)calculate FFs



NB: FF were used in many early GPD models as a simple *ansatz* :  
 $GPD(x, \xi, t) = FF(t) * PDF(x)$

