

GPD Program at COMPASS



A. Ferrero (CEA-Saclay/IRFU/SPhN)

for the COMPASS Collaboration

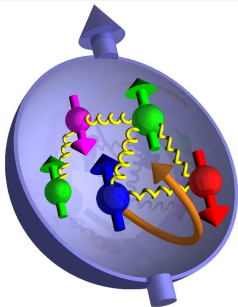
IPN Orsay - 29/5/2017

DE LA RECHERCHE À L'INDUSTRIE

cea

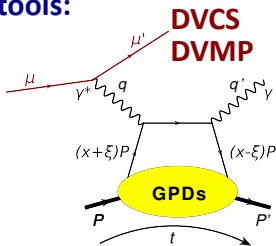
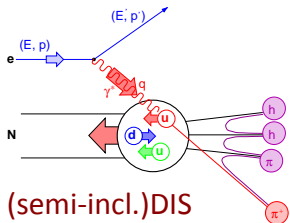


Proton spin sum rule: $\frac{1}{2} = \frac{1}{2}\Delta\Sigma + \Delta G + L_q + L_g$

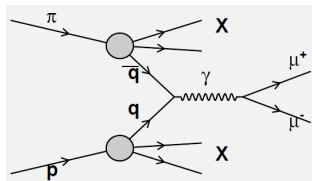


How the proton spin is decomposed in terms of parton's spins ($\Delta\Sigma$, ΔG) and orbital angular momentum (L_q , L_g) is still one of the big open questions in hadronic physics...

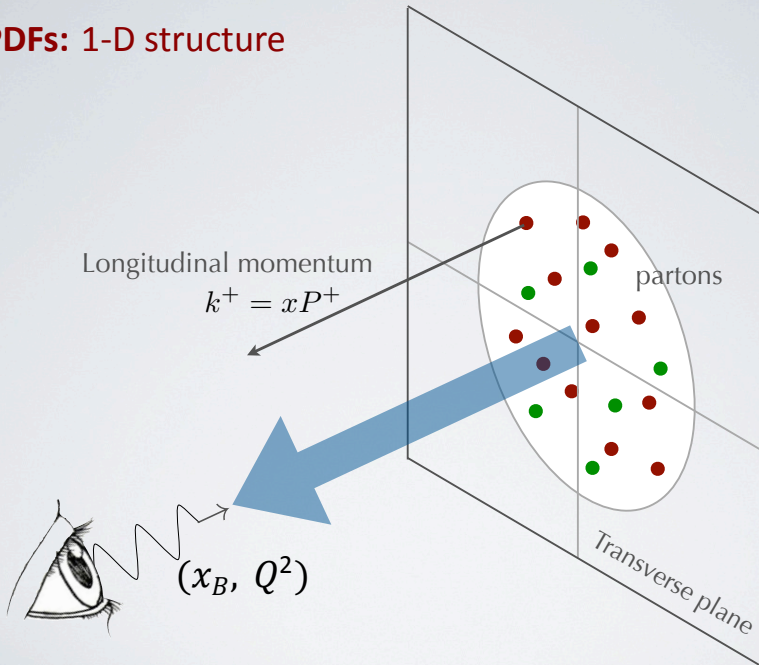
COMPASS experimental tools:



Drell-Yan process



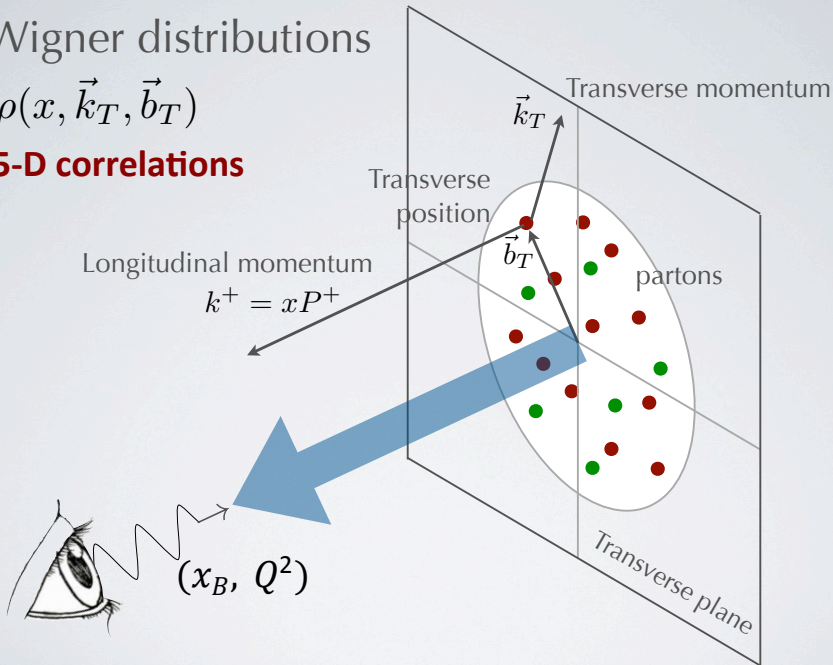
PDFs: 1-D structure



Wigner distributions

$$\rho(x, \vec{k}_T, \vec{b}_T)$$

5-D correlations



Towards a 3D Picture of the Nucleon...

Form Factors (t)

Wigner Distributions

Fourier transform (b_T)

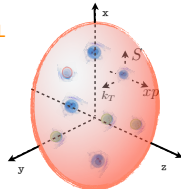
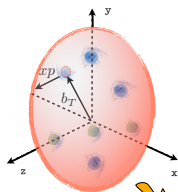
& $\int \text{GPDs}(x, t) \dots dx$

GPDs (x, b_T)

TMDs (x, k_T)

$\int dk_T$

$\int db_{\perp}$



PDFs (x)

$\int \text{GPDs}(x, b_T) \dots db_T$

$\int \text{TMDs}(x, k_T) \dots dk_T$

PDFs $\rightarrow \Delta\Sigma, \Delta G$

TMDs, GPDs \rightarrow $\left\{ \begin{array}{l} \text{“nucleon” tomography} \\ L_{q,g} \end{array} \right.$

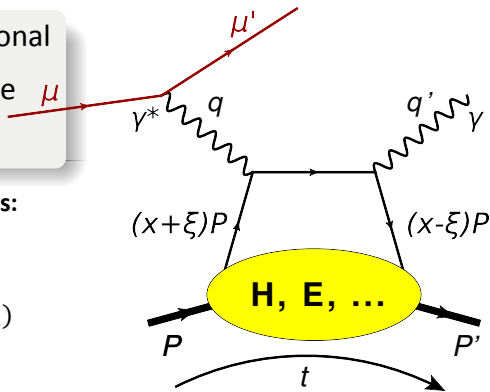
GPDs: correlation between fractional long. momentum x and transverse position b_{\perp} of partons

GPDs depend on the following variables:

x : average long. momentum
(NOT MEASURABLE)

ξ : long. mom. difference $\simeq x_B/(2 - x_B)$

t : four-momentum transfer
related to b_{\perp} via Fourier transform

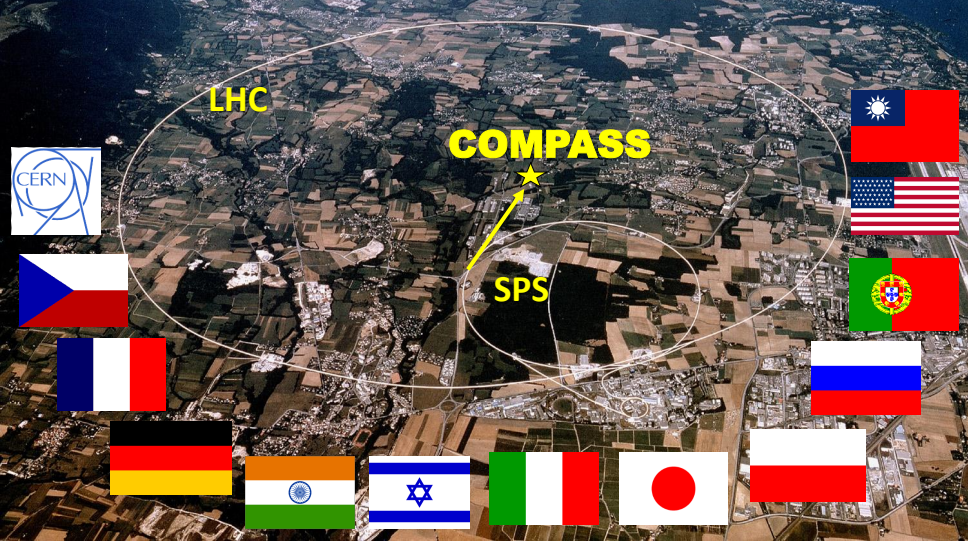


DVCS ($\mathbf{l} \mathbf{p} \rightarrow \mathbf{l}' \mathbf{\gamma} \mathbf{p}'$): “golden” channel for GPD studies

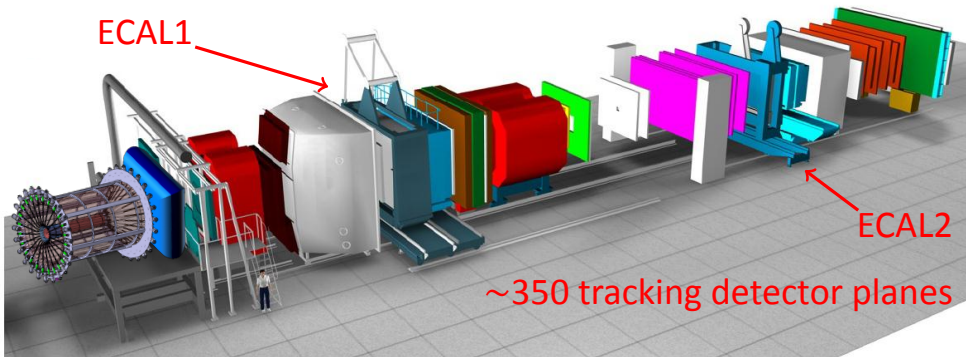
GPDs enter in the DVCS amplitude through Compton Form Factors (CFF):

$$\mathcal{H}(\xi, t) = \int_{-1}^1 dx \frac{H^q(x, \xi, t)}{x - \xi + i\epsilon} = \mathcal{P} \int_{-1}^1 dx \frac{H(x, \xi, t)}{x - \xi} + i\pi H(x = \pm \xi, \xi, t)$$

COMPASS: Versatile facility to study QCD
with hadron (π^\pm , K^\pm , p ...) and lepton (polarized μ^\pm) beams
of ~ 200 GeV for hadron spectroscopy and
hadron structure studies using SIDIS, DY, DVCS, DVMP...



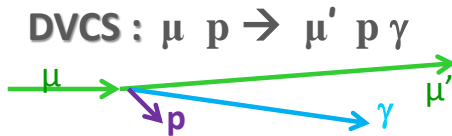
The COMPASS set-up for the GPD programme



Two stage magnetic spectrometer for **large angular & momentum acceptance**

Particle identification with:

- Ring Imaging Cerenkov Detector
- Electromagnetic calorimeters (**ECAL0, ECAL1 & ECAL2**)
- Hadronic calorimeters
- Muon absorbers



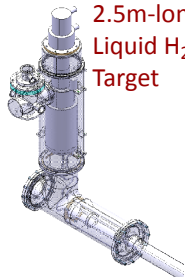
The COMPASS set-up for the GPD programme

ECAL1

ECAL2

~3 Main new equipments

2.5m-long
Liquid H₂
Target



The COMPASS set-up for the GPD programme

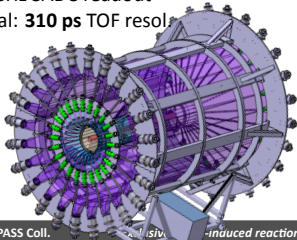
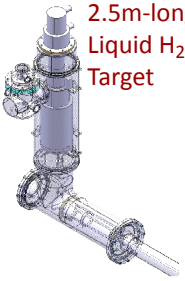
ECAL1

ECAL2

~3 Main new equipments

2.5m-long
Liquid H₂
Target

Target TOF System
24 inner & outer scintillators
1 GHz SADC readout
goal: **310 ps** TOF resolution



The COMPASS set-up for the GPD programme

ECAL1

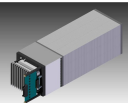
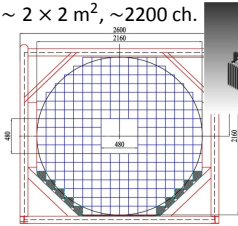
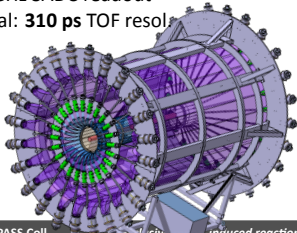
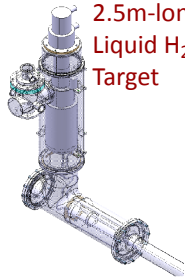
ECAL2

~3 Main new equipments

2.5m-long
Liquid H₂
Target

Target TOF System
24 inner & outer scintillators
1 GHz SADC readout
goal: **310 ps** TOF resol.

ECALO Calorimeter
Shashlyk modules + MAPD readout
~ 2 x 2 m², ~2200 ch.

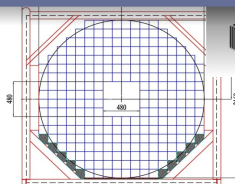
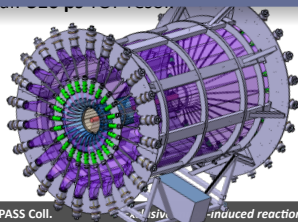
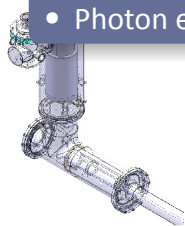


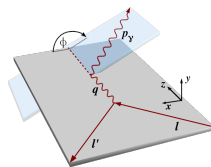
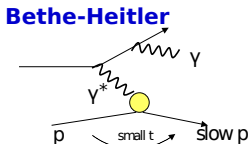
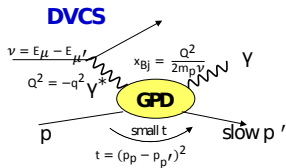
The COMPASS set-up for the GPD programme

ECAL1

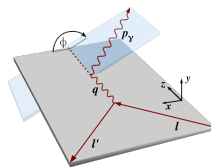
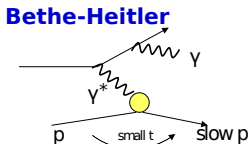
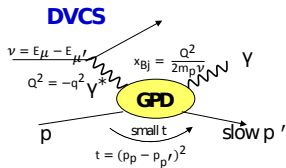
Key features of COMPASS:

- Muon beams with opposite **charge** and **polarization**
 - $E_{\mu} = 160 \text{ GeV}$
 - $\sim 4 \cdot 10^8 \mu/\text{spill}$, 9.6s/40s duty cycle
- Reconstruction of the full event kinematics
- Recoil proton momentum from target TOF detector
- Photon energy and angle from ECALs

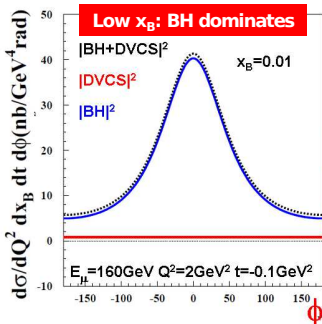




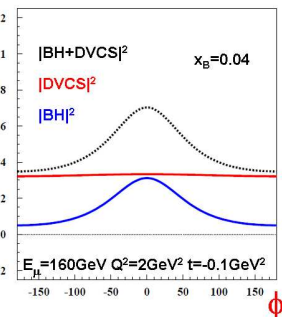
$$d\sigma \propto \underbrace{|T_{DVCS}|^2}_{\text{bilinear combination of GPDs}} + \underbrace{|T_{BH}|^2}_{\text{known to 1 \%}} + \underbrace{\text{interference term}}_{\text{linear combination of GPDs}}$$



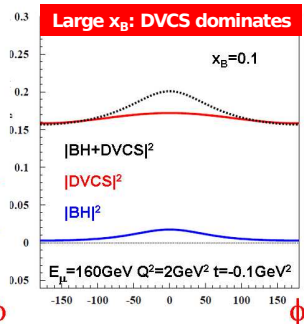
$$d\sigma \propto \underbrace{|T_{DVCS}|^2}_{\text{bilinear combination of GPDs}} + \underbrace{|T_{BH}|^2}_{\text{known to 1 \%}} + \underbrace{\text{interference term}}_{\text{linear combination of GPDs}}$$



reference yield of
almost pure
Bethe-Heitler



Study DVCS with:
 $\text{Re}(T^{\text{DVCS}})$ & $\text{Im}(T^{\text{DVCS}})$
via $(d\sigma^{+\leftarrow} \pm d\sigma^{-\rightarrow})$



Transverse Imaging:
 $d\sigma^{\text{DVCS}}/d|t|$
via $(d\sigma^{+\leftarrow} + d\sigma^{-\rightarrow})$

Transverse Nucleon Imaging at COMPASS

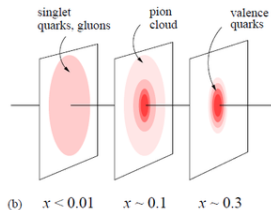
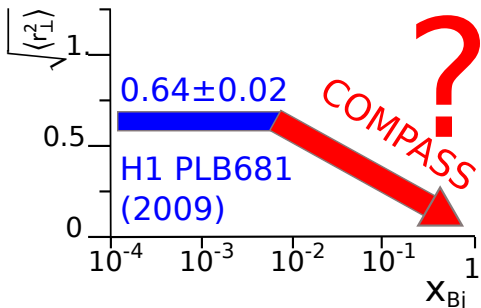
Beam Charge and Spin **SUM**:

$$S_{CS,U} \equiv d\sigma(\mu^{+\leftarrow}) + d\sigma(\mu^{-\rightarrow}) \propto d\sigma^{BH} + d\sigma_{unpol}^{DVCS} + Ks_1^{Int} \sin \phi$$

Integration over ϕ and BH subtraction $\rightarrow d\sigma^{DVCS}/d|t| \sim \exp(-B|t|)$

$$\langle b_{\perp}^2(x_B) \rangle \approx 2B(x_B)$$

$b_{\perp} \rightarrow$ distance between struck parton and baricenter of momentum



Ansatz at small x_B :

$$B(x_B) \approx B_0 + 2\alpha' \ln(x_0/x_B)$$

(inspired by Regge phenomenology)

2012 Pilot Run - 4 weeks

ECAL2

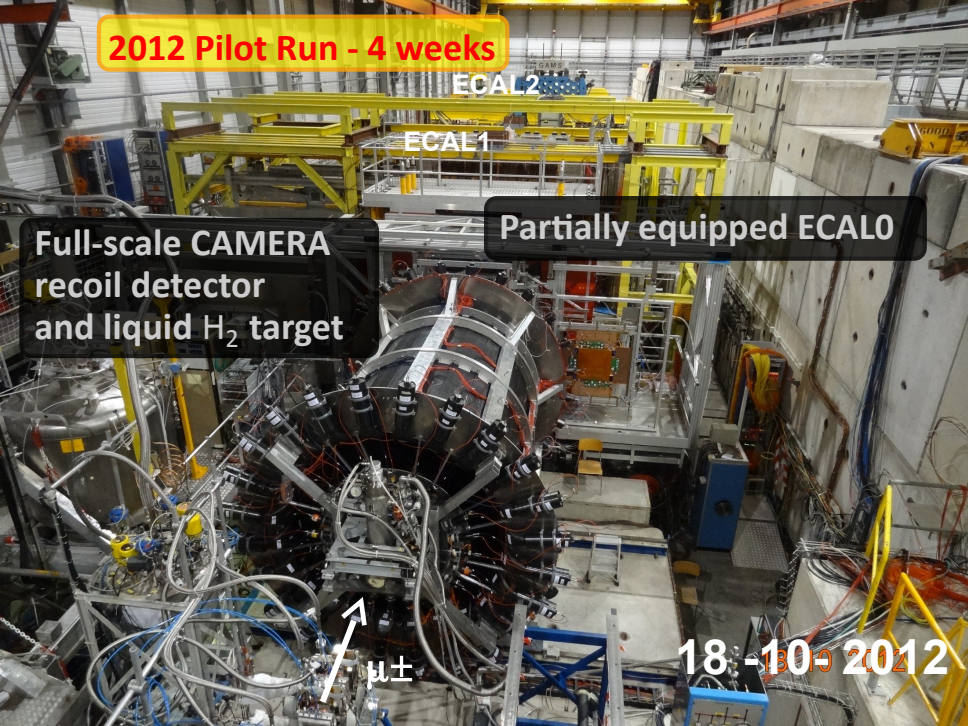
ECAL1

**Full-scale CAMERA
recoil detector
and liquid H₂ target**

Partially equipped ECAL0

$\mu\pm$

18-10-2012



Exclusive Photon Events Selection

Reconstructed interaction vertex in **target volume**

One single photon above DVCS production threshold

$$Q^2 > 1 \text{ (GeV/c)}^2, \quad 0.05 < y < 0.9,$$

$$0.08 \text{ (GeV/c)}^2 < t < 0.64 \text{ (GeV/c)}^2$$

Exclusive Photon Events Selection

Reconstructed interaction vertex in **target volume**

One single photon above DVCS production threshold

$$Q^2 > 1 \text{ (GeV/c)}^2, \quad 0.05 < y < 0.9,$$

$$0.08 \text{ (GeV/c)}^2 < t < 0.64 \text{ (GeV/c)}^2$$

Exclusivity conditions:

- $\Delta\varphi = \varphi_{\text{meas}}^{\text{proton}} - \varphi_{\text{reco}}^{\text{proton}}$

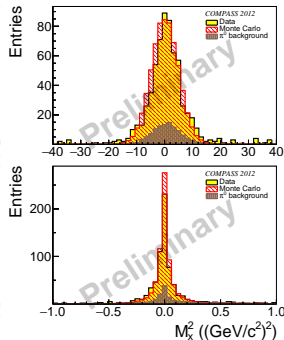
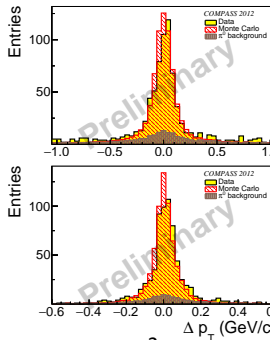
- Vertex pointing (ΔZ_A)

- Transv. mom. balance:

$$\Delta p_T = p_{T,\text{meas}}^{\text{proton}} - p_{T,\text{reco}}^{\text{proton}}$$

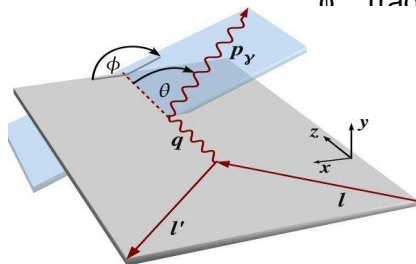
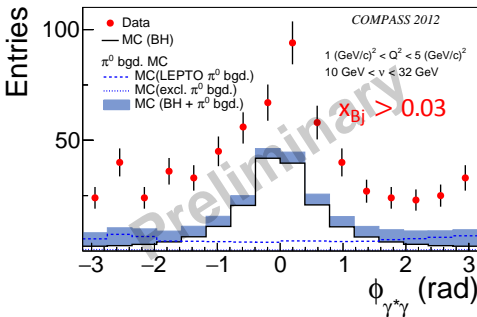
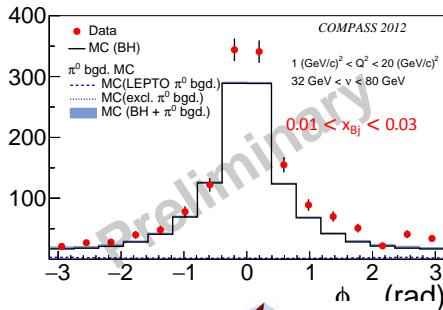
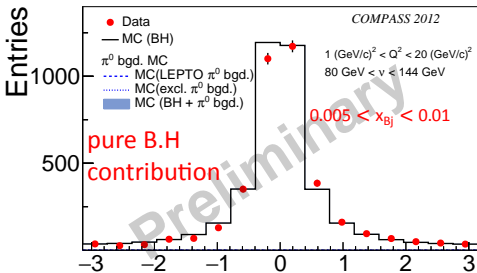
- Four-momentum balance:

$$M_x^2 = (p_{\mu_{\text{in}}} + p_{p_{\text{in}}} - p_{\mu_{\text{out}}} - p_{p_{\text{out}}} - p_{\gamma})^2$$

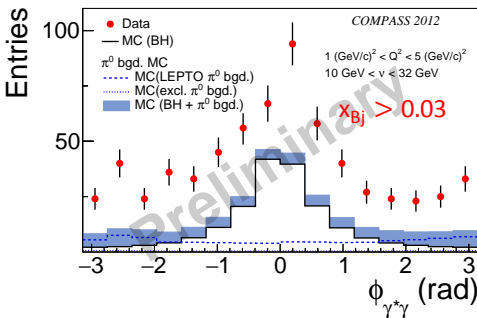
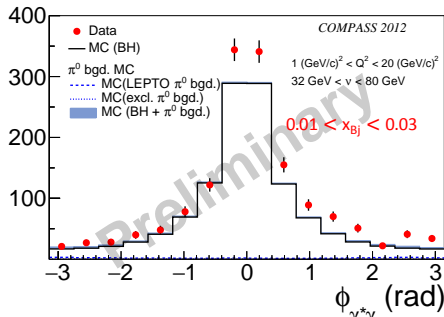
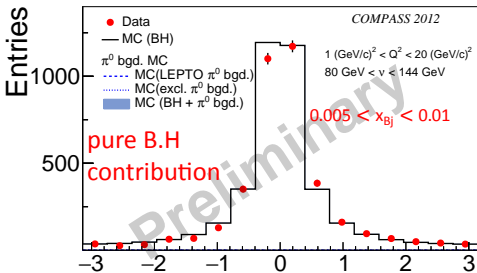


Exclusive γ Azimuthal Distributions for DVCS

Kinematically constrained
vertex fit applied



Exclusive γ Azimuthal Distributions for DVCS



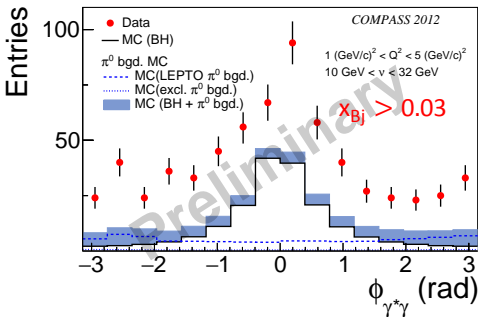
- BH Monte Carlo normalization based on integrated luminosity
- BH process dominant at small x_{Bj}
- π^0 background contributing at large x_{Bj}
- **clear excess of DVCS at large x_{Bj}**

Exclusive γ Azimuthal Distributions for DVCS

t-dependence of DVCS cross-section for $x_{Bj} > 0.03$:

- Subtract BH contribution
- Subtract π^0 background
- Experimental acceptance correction & luminosity normalization

⇒ **DVCS cross-section in 4 bins of $|t|$**



- BH Monte Carlo normalization based on integrated luminosity
- BH process dominant at small x_{Bj}
- π^0 background contributing at large x_{Bj}
- **clear excess of DVCS at large x_{Bj}**

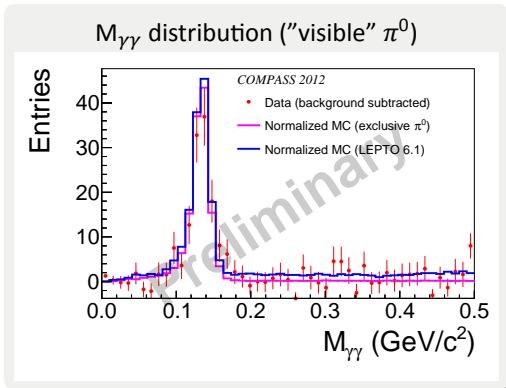
π^0 Background Estimation

π^0 s are one of the main **background sources** for excl. photon events

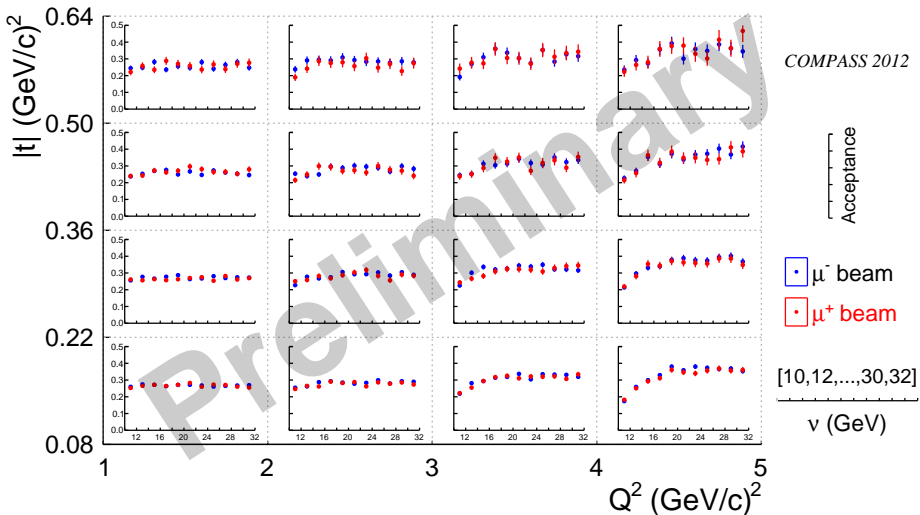
Two possible cases:

- **visible** (both γ detected, **subtracted**)
- **invisible** (one γ “lost”, **estimated with MC**)
 - **Semi-inclusive** \rightarrow LEPTO
 - **Exclusive** \rightarrow HEPGEN/ π^0 (Goloskokov-Kroll model)

MC samples normalized to $M_{\gamma\gamma}$ peak in real data

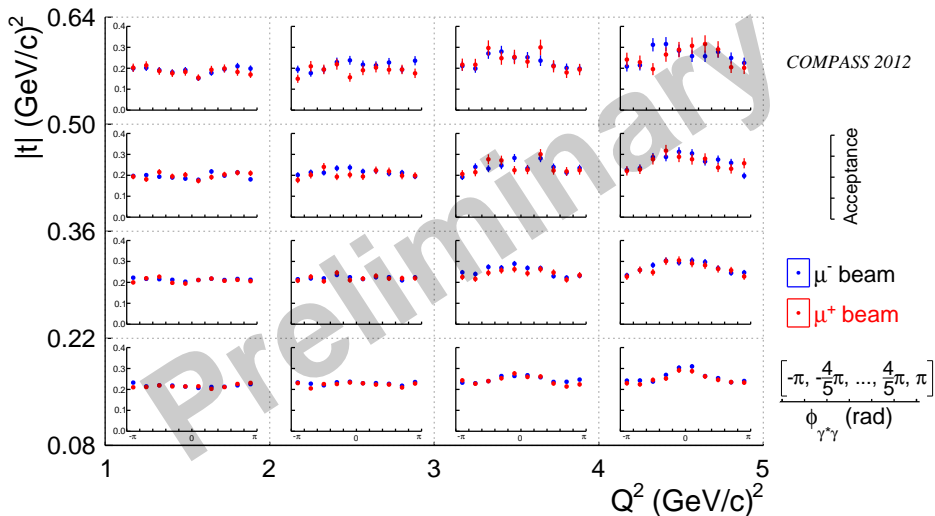


Experimental acceptance for DVCS events



Acceptance binning in Q^2 , ν and $|t|$

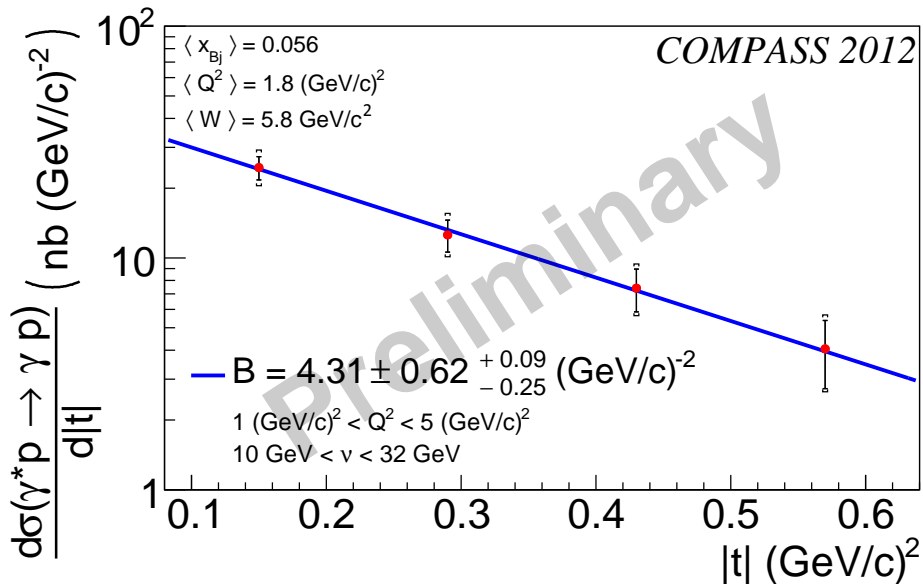
Experimental acceptance for DVCS events



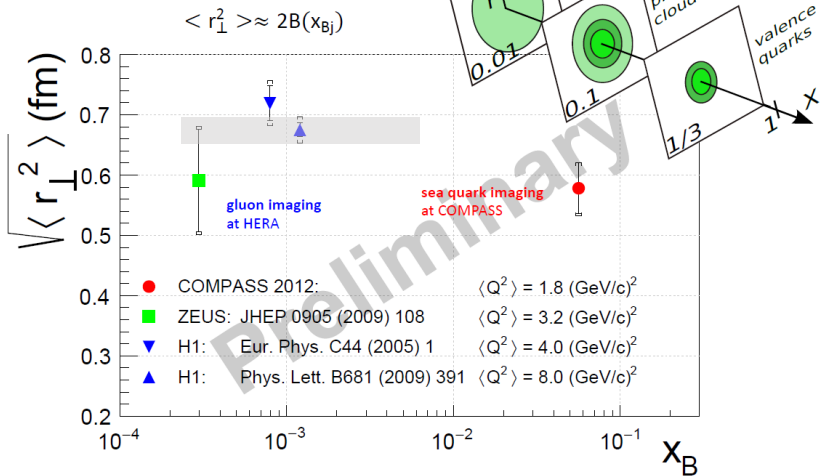
Symmetric acceptance around $\phi = 0$

DVCS x-section and t-slope extraction

Kinematically constrained
vertex fit applied



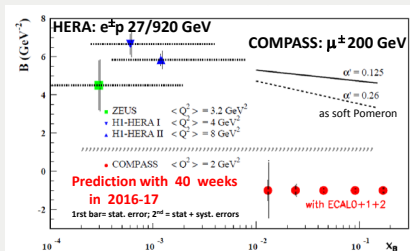
Comparison with HERA results



$$\sqrt{\langle r_{\perp}^2 \rangle} \text{ to be compared to } \sqrt{4 \frac{d}{dt} F_1^P} \Big|_{t=0} = 0.66 \pm 0.01 \text{ fm} \neq \sqrt{4 \frac{d}{dt} G_E^P} \Big|_{t=0} = 0.72 \pm 0.01 \text{ fm} + \sqrt{\kappa/m_p^2} \Big|_{t=0} = 0.88 \text{ fm}$$

COMPASS OUTLOOK:

- Dedicated beam time for GPD studies in 2016-17
- x_{Bj} -dependence of t-slope parameter in sea-quarks domain



- Real and imaginary parts of CFF \mathcal{H} from interference term
- Complementary measurements with exclusive mesons:

$$\pi^0, \rho^0, \phi, \omega \dots$$

What kind of "proton transverse size" are we measuring?

$$d\sigma^{DVCS}/dt \sim \exp(-B|t|)$$

$$B(x_B) = \frac{1}{2} \langle r_{\perp}^2(x_B) \rangle$$

distance between the active quark and the center of momentum of spectators

Transverse size of the nucleon

mainly dominated by $H(x=\xi, \xi, t)$

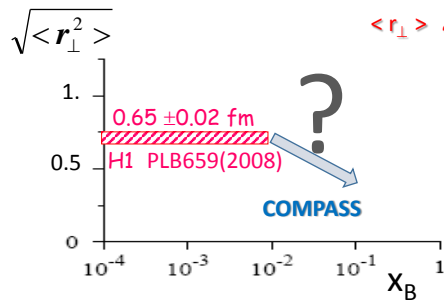
$$A^{DVCS} \text{ linked to } \text{Im}H \sim \exp(-B'|t|)$$

$$B'(x_B) = \frac{1}{4} \langle b_{\perp}^2(x_B) \rangle$$

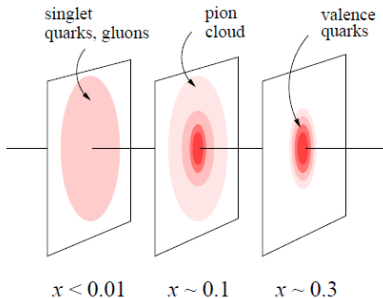
distance between the active quark and the center of momentum of the nucleon

Impact Parameter Representation

$$q(x, b_{\perp}) \leftrightarrow H(x, \xi=0, t)$$



Note $0.65 \text{ fm} = \sqrt{2/3} \times 0.8 \text{ fm}$



Constraining the GPD H @ COMPASS

cross-sections on proton for $\mu^{\downarrow}, \mu^{\uparrow}$ beam with opposite charge & spin (e_{μ} & P_{μ})

$$d\sigma_{(\mu p \rightarrow \mu p \gamma)} = d\sigma^{BH} + d\sigma^{DVCS}_{unpol} + P_{\mu} d\sigma^{DVCS}_{pol} \\ + e_{\mu} a^{BH} \Re A^{DVCS} + e_{\mu} P_{\mu} a^{BH} \Im A^{DVCS}$$

Charge & Spin Difference and Sum:

$$\mathcal{D}_{CS,U} \equiv d\sigma(\mu^{\downarrow}) - d\sigma(\mu^{\uparrow}) \propto c_0^{Int} + c_1^{Int} \cos \phi \quad \text{and} \quad c_{0,1}^{Int} \sim F_1 \Re \mathcal{H} \\ \mathcal{S}_{CS,U} \equiv d\sigma(\mu^{\downarrow}) + d\sigma(\mu^{\uparrow}) \propto d\sigma^{BH} + c_0^{DVCS} + K \cdot s_1^{Int} \sin \phi \quad \text{and} \quad s_1^{Int} \sim F_1 \Im \mathcal{H}$$

$$c_1^{Int} \propto \Re (F_1 \mathcal{H} + \xi (F_1 + F_2) \tilde{\mathcal{H}} - t/4m^2 F_2 \mathcal{E})$$

NOTE: ✓ dominance of \mathcal{H} with a proton target
at COMPASS kinematics
✓ only leading twist and LO

Constraining the GPD \mathcal{H} @ COMPASS

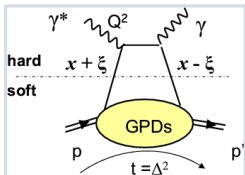
cross-sections on proton for $\mu^{\downarrow}, \mu^{\uparrow}$ beam with opposite charge & spin (\mathbf{e}_μ & \mathbf{P}_μ)

$$d\sigma_{(\mu p \rightarrow \mu p \gamma)} = d\sigma^{\text{BH}} + d\sigma^{\text{DVCS}}_{\text{unpol}} + P_\mu d\sigma^{\text{DVCS}}_{\text{pol}} \\ + \mathbf{e}_\mu a^{\text{BH}} \mathcal{R}e A^{\text{DVCS}} + \mathbf{e}_\mu P_\mu a^{\text{BH}} \text{Im} A^{\text{DVCS}}$$

Charge & Spin Difference and Sum:

$$\mathcal{D}_{CS,U} \equiv d\sigma(\mu^{\downarrow}) - d\sigma(\mu^{\uparrow}) \propto c_0^{\text{Int}} + c_1^{\text{Int}} \cos \phi \quad \text{and} \quad c_{0,1}^{\text{Int}} \sim F_1 \mathcal{R}e \mathcal{H}$$

$$\mathcal{S}_{CS,U} \equiv d\sigma(\mu^{\downarrow}) + d\sigma(\mu^{\uparrow}) \propto d\sigma^{\text{BH}} + c_0^{\text{DVCS}} + K \cdot s_1^{\text{Int}} \sin \phi \quad \text{and} \quad s_1^{\text{Int}} \sim F_1 \text{Im} \mathcal{H}$$



$$\xi \sim x_B / (2 - x_B)$$

$$\text{Im} \mathcal{H}(\xi, t) = \mathcal{H}(x = \xi, \xi, t)$$

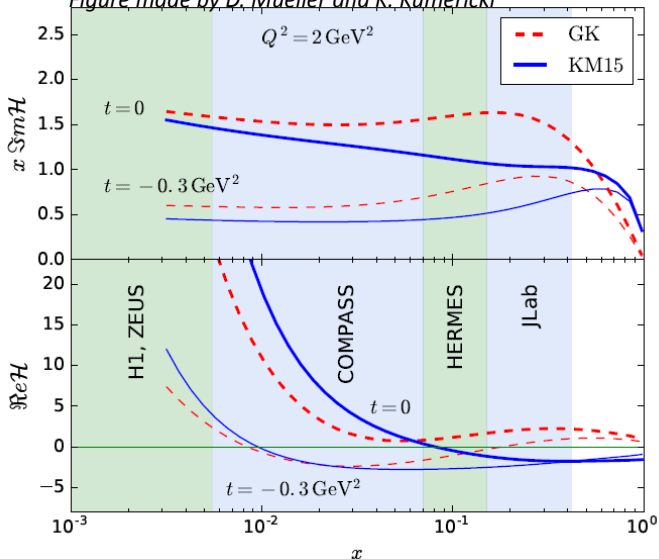
$$\mathcal{R}e \mathcal{H}(\xi, t) = \mathcal{P} \int dx \frac{\mathcal{H}(x, \xi, t)}{x - \xi} = \mathcal{P} \int dx \frac{\mathcal{H}(x, x, t)}{x - \xi} + \mathcal{D}(t)$$

Re part of the Compton Form Factors linked to the \mathcal{D} term

Energy-Momentum Tensor : Polyakov, PLB 555 (2003) 57-62

Re \mathcal{H} and Im \mathcal{H} from Recent Models

Figure made by D. Mueller and K. Kumericki



Im H
Is it rather well known ?

Re H linked to the *D term* is still poorly constrained

KM15 K Kumericki and D Mueller [arXiv:1512.09014v1](https://arxiv.org/abs/1512.09014v1)

GK S.V. Goloskokov, P. Kroll, EPJC53 (2008), EPJA47 (2011)

Beam Charge & Spin Difference

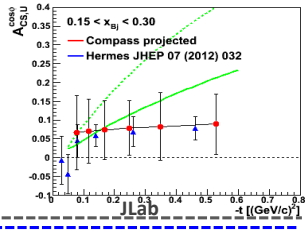
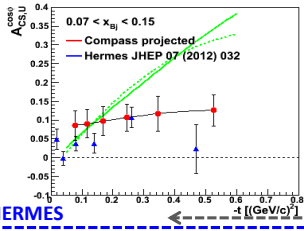
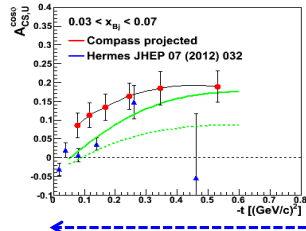
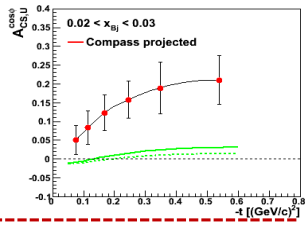
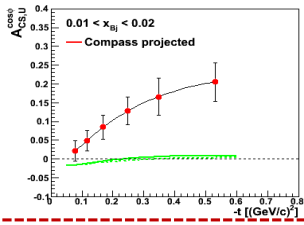
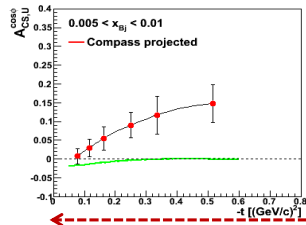
$Re \mathcal{H} > 0$ at H1

< 0 at HERMES

Value of x_B for the node?

$$c_1^I = Re F_1 \mathcal{H}$$

Predictions with
VGG and D.Mueller KM10



HERMES

JLab

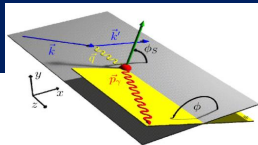
COMPASS 2 years of data $E_\mu = 160 \text{ GeV}$ $1 < Q^2 < 8 \text{ GeV}^2$

Deeply Virtual Meson Production @ COMPASS

This talk: ρ^0 and ω

M. Gorzellik this afternoon: π^0

Exclusive ρ^0 production



$$\left[\frac{\alpha_{em}}{8\pi^3} \frac{y^2}{1-\varepsilon} \frac{1-x_B}{x_B} \frac{1}{Q^2} \right]^{-1} \frac{d\sigma}{dx_{Bj} dQ^2 dt d\phi d\phi_s}$$

$$= \frac{1}{2} \left(\sigma_{++}^{++} + \sigma_{++}^{--} \right) + \varepsilon \sigma_{00}^{++} - \varepsilon \cos(2\phi) \operatorname{Re} \sigma_{+-}^{++} - \sqrt{\varepsilon(1+\varepsilon)} \cos\phi \operatorname{Re} \left(\sigma_{+0}^{++} + \sigma_{+0}^{--} \right)$$

$$- P_\ell \sqrt{\varepsilon(1-\varepsilon)} \sin\phi \operatorname{Im} \left(\sigma_{+0}^{++} + \sigma_{+0}^{--} \right)$$

$$- S_T \left[\sin(\phi - \phi_s) \operatorname{Im} \left(\sigma_{++}^{+-} + \varepsilon \sigma_{00}^{+-} \right) + \frac{\varepsilon}{2} \sin(\phi + \phi_s) \operatorname{Im} \sigma_{+-}^{+-} + \frac{\varepsilon}{2} \sin(3\phi - \phi_s) \operatorname{Im} \sigma_{+-}^{+-} \right]$$

transv. polar.

target

$$+ \left[\sqrt{\varepsilon(1+\varepsilon)} \sin\phi_s \operatorname{Im} \sigma_{+0}^{+-} + \sqrt{\varepsilon(1+\varepsilon)} \sin(2\phi - \phi_s) \operatorname{Im} \sigma_{+0}^{+-} \right]$$

$$+ S_T P_\ell \left[\sqrt{1-\varepsilon^2} \cos(\phi - \phi_s) \operatorname{Re} \sigma_{++}^{+-} \right]$$

transv. polar.

target +

long. polar.

beam

$$- \left[\sqrt{\varepsilon(1-\varepsilon)} \cos\phi_s \operatorname{Re} \sigma_{+0}^{+-} + \sqrt{\varepsilon(1-\varepsilon)} \cos(2\phi - \phi_s) \operatorname{Re} \sigma_{+0}^{+-} \right]$$

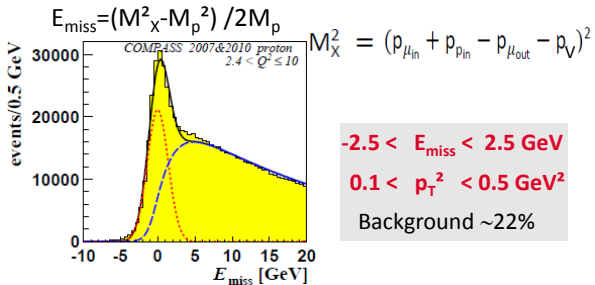
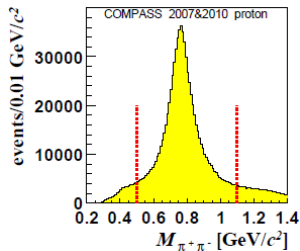
σ_{ij} for nucleon helicity
 σ_{mn} for photon helicity

Dominant interference terms:

then $\gamma_L^* \rightarrow \rho_L^0$
 $\gamma_T^* \rightarrow \rho_L^0$

Selection of $\mu p \rightarrow \mu' V p_{\text{undet.}}$ Events

$V = \rho^0 \rightarrow \pi^+ \pi^-$

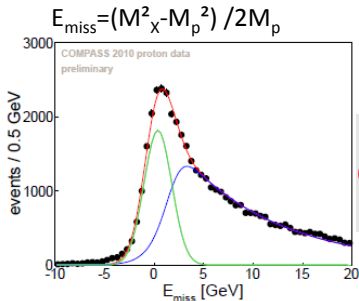
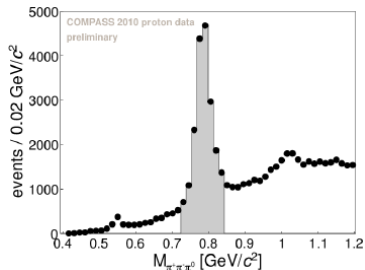


$-2.5 < E_{\text{miss}} < 2.5$ GeV

$0.1 < p_T^2 < 0.5$ GeV²

Background ~22%

$V = \omega \rightarrow \pi^+ \pi^- \pi^0$ BR=89%



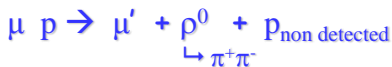
$-3 < E_{\text{miss}} < 3$ GeV

$0.05 < p_T^2 < 0.5$ GeV²

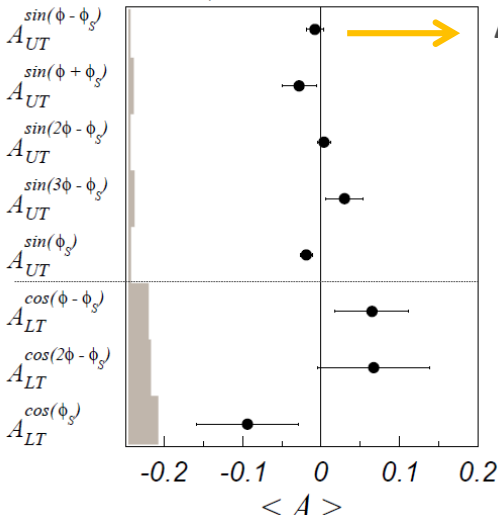
Background ~34%

Excl. ρ^0 Production with Transv. Pol. Target

COMPASS 2007-2010, without recoil detector



$$W = 8.1 \text{ GeV}/c^2, p_T^2 = 0.2 \text{ (GeV}/c)^2, Q^2 = 2.2 \text{ (GeV}/c)^2$$



$$A_{UT} \sin(\phi - \phi_S) \propto \text{Im}(\mathcal{E}^* \mathcal{H})$$

$$E\rho^0 \propto 2/3 E^u + 1/3 E^d + 3/8 E^g$$

✓ Cancellation between
gluon and sea contributions

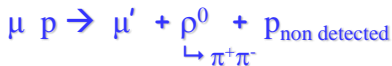
$$\checkmark E^u \text{ val} \sim -E^d \text{ val}$$

COMPASS, NPB 865 (2012) 1-20

⊗ production should be powerful

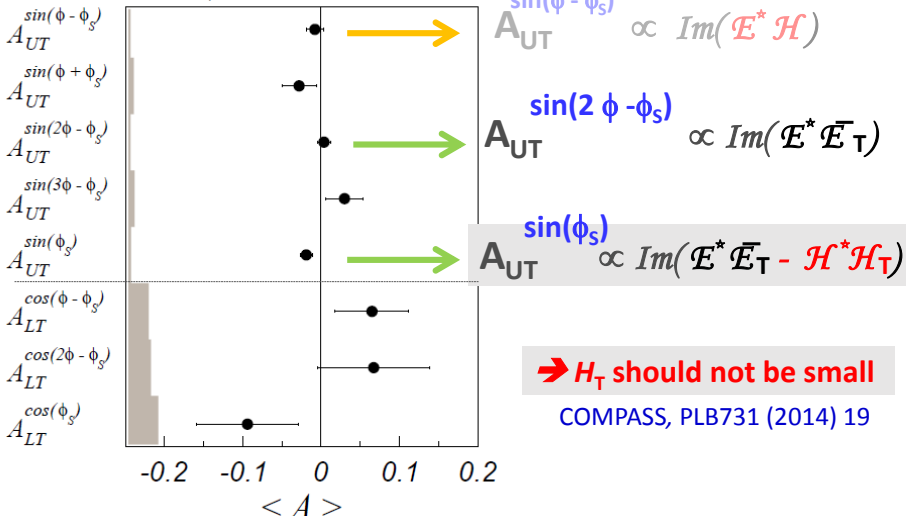
$$E\omega \propto 2/3 E^u - 1/3 E^d + 3/8 E^g$$

Excl. ρ^0 Production with Transv. Pol. Target

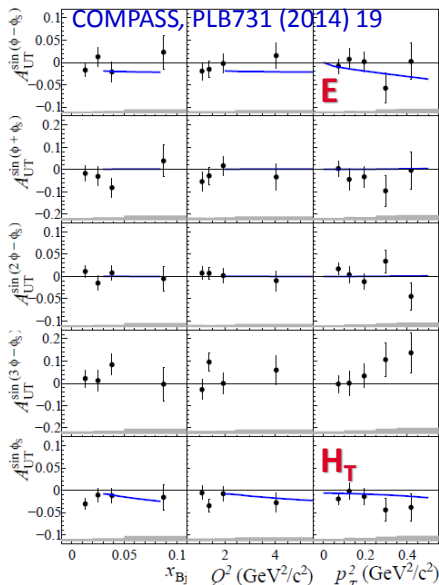


COMPASS 2007-2010, without recoil detector

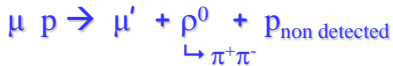
$$W = 8.1 \text{ GeV}/c^2, p_T^2 = 0.2 \text{ (GeV}/c)^2, Q^2 = 2.2 \text{ (GeV}/c)^2$$



Excl. ρ^0 Production with Transv. Pol. Target



$$\langle x_{Bj} \rangle \approx 0.039, \langle Q^2 \rangle \approx 2.0 \text{ GeV}^2, \langle p_T^2 \rangle \approx 0.18 \text{ GeV}^2$$



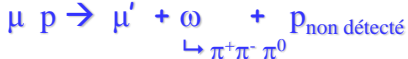
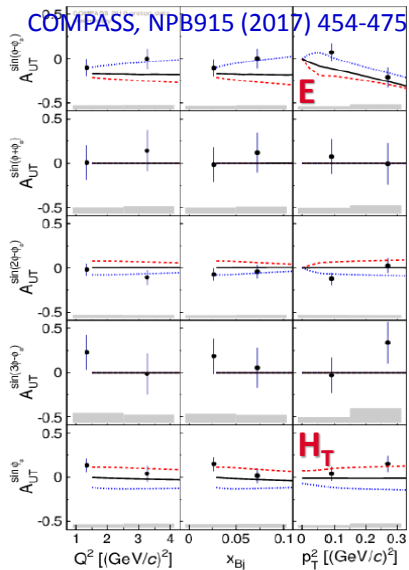
Comparison with a phenomenological GPD-based model

Goloskokov and Kroll (EPJ C74 (2014))

- Phenomenological 'handbag' approach
- Includes twist-3 ρ^0 meson wave functions
- Includes contributions from γ_L^* and γ_T^*

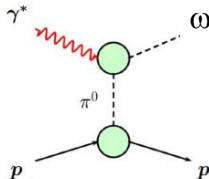
Large contribution of the GPDs E and H_T

Excl. ω Production with Transv. Pol. Target



GK model predictions (EPJ A50 (2014)) including all the GPDs and transverse GPDs

+ the pion pole exchange which is large for ω production



- ▶ positive $\pi\omega$ form factor
- ▶ no pion pole
- ▶ negative $\pi\omega$ form factor

no unambiguous determination of the sign

Backup Slides

Proton « radius » measured at JLab

Fit of 8 CFFs at L.O and L.T.

Dupré, Guidal, Vanderhaeghen, PRD95, 011501(R)(2017)

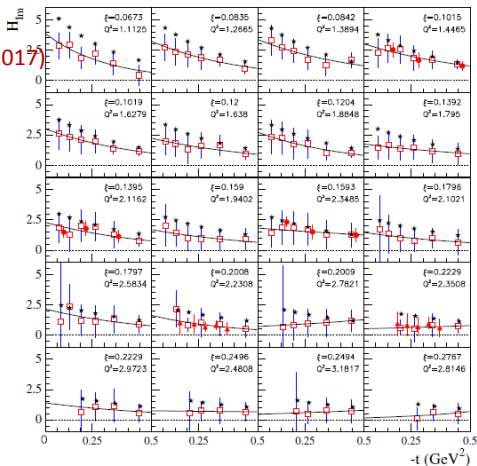
$$s_1^I = \text{Im } F_1^I \mathcal{H}$$

- CLAS σ and $\Delta\sigma$
- ▲ HallA σ and $\Delta\sigma$
- CLAS A_{UL} and A_{LL}

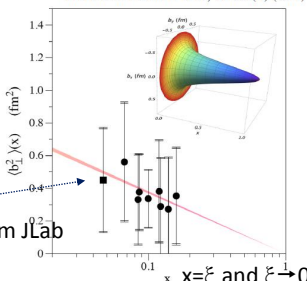
★ VGG model

— Fit $A e^{-B'|t|}$

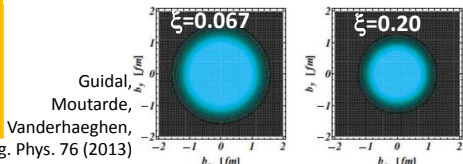
$$\langle b_{\perp}^2 \rangle \approx 4 B'$$



PHYSICAL REVIEW D 95, 011501(R) (2017)



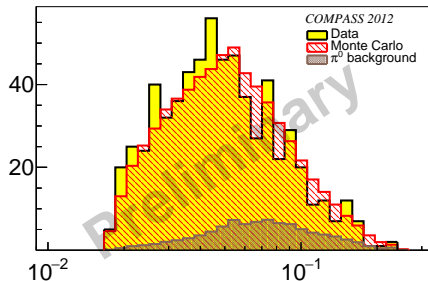
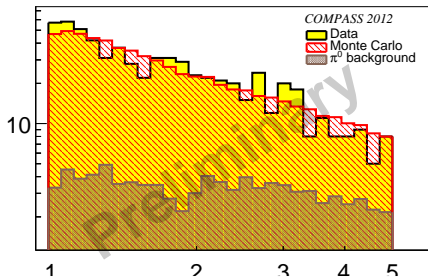
HERMES
+ 8 points from JLab



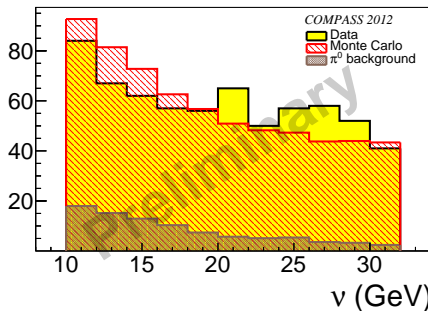
Rept. Prog. Phys. 76 (2013)

Kinematic Distributions for DVCS

Entries



Entries



$$\langle x_{Bj} \rangle = 0.056$$

$$\langle Q_{Bj}^2 \rangle = 1.8 \text{ (GeV/c)}^2$$

$$\langle W \rangle = 5.8 \text{ GeV/c}^2$$

The GPD Physics Programme at COMPASS

2008: Very short test run, short LH₂ target

- Observation of exclusive photon production
- Confirmed the global efficiency $\simeq 10\%$ used for projections

2009: **10 days**, short LH₂ target

- Coarse binning in x_B
- First hint of DVCS at large x_B

2003-10: Exclusive ρ^0 and ω^0 meson production on a **transv. pol. target** and **no recoil detector**

2012: **4 weeks**, full-scale LH₂ target and recoil detector

2016-7: **2 x 6 months** with LH₂ target and recoil det. → **GPD H**

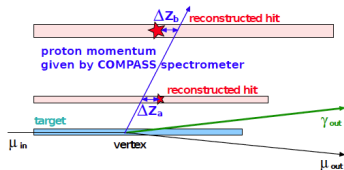
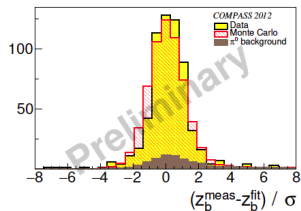
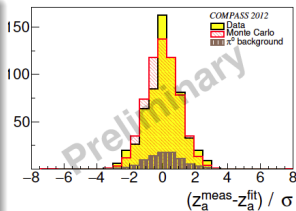
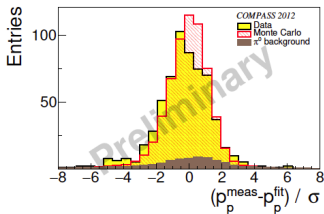
>2018: DVCS with **transv. pol. target** and **recoil detector** → **GPD E**

Future addendum to COMPASS-II proposal

Kinematically constrained fit

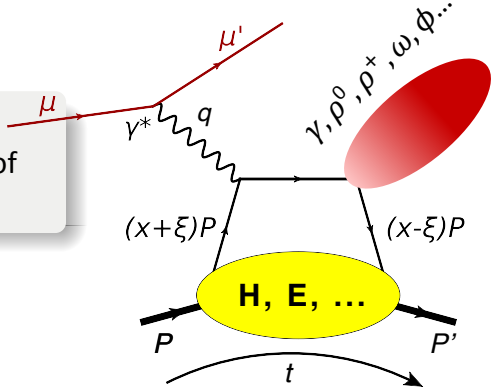
- constrained χ^2 minimisation with NDF=9
- full 4-momentum conservation of the reaction $\mu p \rightarrow \mu p \gamma$
- vertex constraints for μ, μ' and p' included in the fit

⇒ most accurate determination of t



Introduction to GPDs

“GPDs are **non-perturbative** objects entering the description of **hard exclusive** leptonproduction”



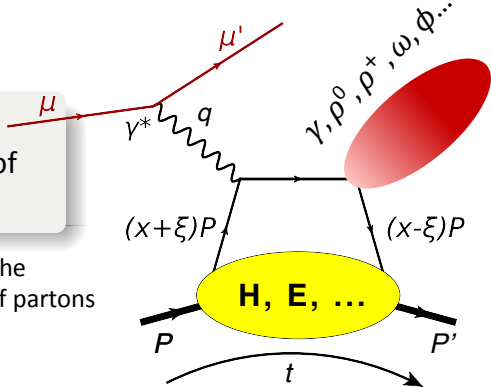
Definition of variables:

- q : exchanged photon four-momentum
- x : average long. momentum - NOT ACCESSIBLE
- ξ : long. mom. difference $\approx x_B/(2 - x_B)$
- t : four-momentum transfer

Introduction to GPDs

“GPDs are **non-perturbative** objects entering the description of **hard exclusive** leptonproduction”

They encode **CORRELATIONS** between the long. mom. x and the transv. position of partons



Definition of variables:

- q : exchanged photon four-momentum
- x : average long. momentum - NOT ACCESSIBLE
- ξ : long. mom. difference $\approx x_B/(2 - x_B)$
- t : four-momentum transfer

Introduction to GPDs

“GPDs are **non-perturbative** objects entering the description of **hard exclusive** leptonproduction”

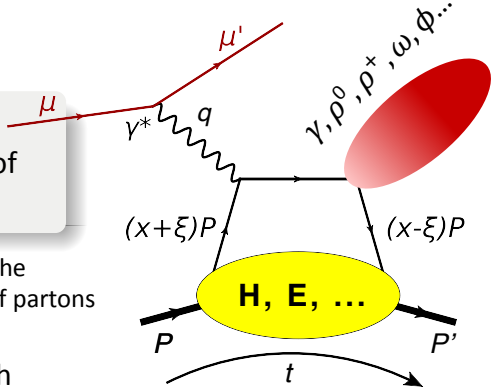
They encode **CORRELATIONS** between the long. mom. \mathbf{x} and the transv. position of partons

Experimentally accessible through Compton Form Factors (CFFs):

$$\text{Im}\mathcal{H}(\xi, \mathbf{t}) = \mathbf{H}(\mathbf{x} = \xi, \xi, \mathbf{t})$$

$$\text{Re}\mathcal{H}(\xi, \mathbf{t}) = \mathcal{P} \int \frac{d\mathbf{x} \mathbf{H}(\mathbf{x}, \mathbf{x} = \xi, \mathbf{t})}{(\mathbf{x} - \xi)} + \mathcal{D}(\mathbf{t})$$

$\mathcal{D}(\mathbf{t})$ connected to **energy-momentum tensor** (Polyakov, PLB 555 (2003) 57-62)



Definition of variables:

- q : exchanged photon four-momentum
- x : average long. momentum - NOT ACCESSIBLE
- ξ : long. mom. difference $\approx x_B/(2 - x_B)$
- \mathbf{t} : four-momentum transfer

Introduction to GPDs

“GPDs are **non-perturbative** objects entering the description of **hard exclusive** leptonproduction”

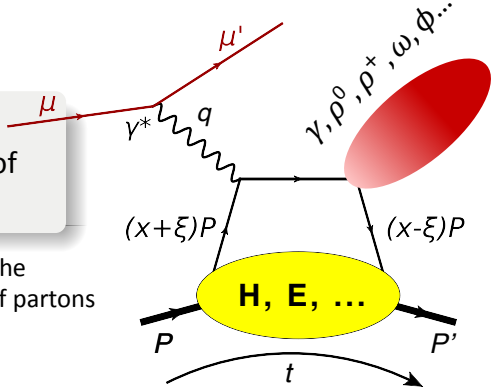
They encode **CORRELATIONS** between the long. mom. \mathbf{x} and the transv. position of partons

They allow to perform so-called “**nucleon tomography**”:

$$d\sigma^{DVCS}/d|t| \sim \exp(-\mathbf{B}|t|)$$

$$\langle b_{\perp}^2(x_B) \rangle \approx 2\mathbf{B}(x_B)$$

b_{\perp} : distance between the struck parton and center of momentum



Definition of variables:

- q : exchanged photon four-momentum
- x : average long. momentum - NOT ACCESSIBLE
- ξ : long. mom. difference $\approx x_B/(2 - x_B)$
- t : four-momentum transfer

Towards a 3D Picture of the Nucleon...

Form Factors (t)

Wigner Distributions

Fourier transform (b_T)

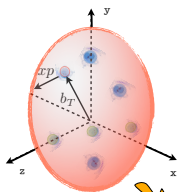
& $\int \text{GPDs}(x, t) \dots dx$

GPDs (x, b_T)

$\int dk_T$

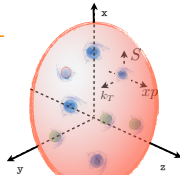
TMDs (x, k_T)

$\int db_{\perp}$



$\int \text{GPDs}(x, b_T) \dots db_T$

PDFs (x)

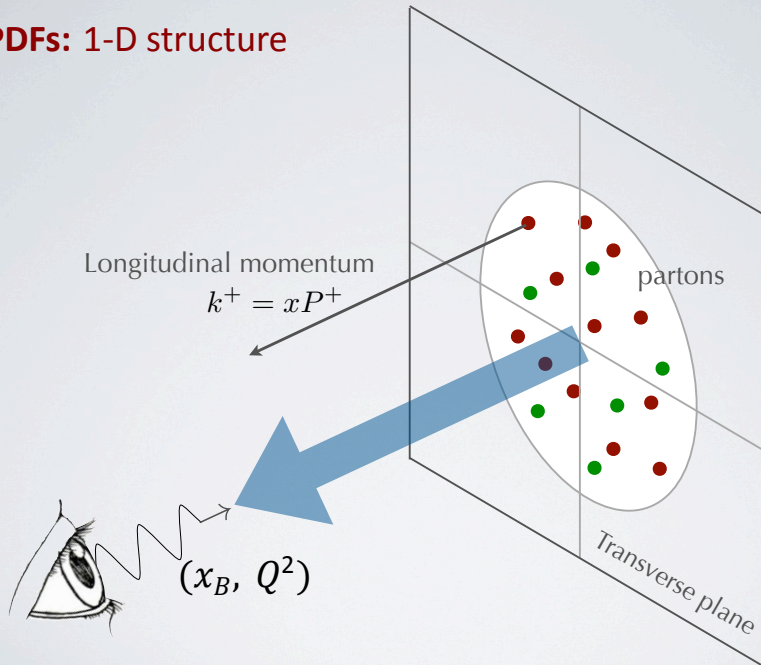


$\int \text{TMDs}(x, k_T) \dots dk_T$

PDFs $\rightarrow \Delta\Sigma, \Delta G$

TMDs, GPDs \rightarrow $\left\{ \begin{array}{l} \text{“nucleon” tomography} \\ L_{q,g} \end{array} \right.$

PDFs: 1-D structure



Wigner distributions

$$\rho(x, \vec{k}_T, \vec{b}_T)$$

5-D correlations

