

# Baryon-to-meson transition distribution amplitudes: formalism and experimental perspectives

K. Semenov-Tian-Shansky\*

\* Petersburg Nuclear Physics Institute, Gatchina, Russia

ECT\* Trento, May 10 2017

In collaboration with: J.P. Lansberg (IPN, Orsay), B. Pire (Ecole Polytechnique, Palaiseau), L. Szymanowski (NCNR, Warsaw, Poland).



Petersburg  
Nuclear  
Physics  
Institute



## Outline

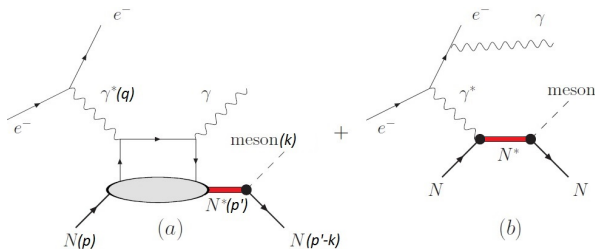
- 1 Introduction: DAs, GPDs, TDAs
- 2 Forward and backward kinematical regimes
- 3  $\pi N$  TDAs: definition, properties, support, spectral representation, crossing and chiral constraints.
- 4 Current status of experimental analysis at Jlab and feasibility studies for  $\bar{P}$ ANDA.
- 5 Summary and Outlook

For references see [B. Pire, K. S., L. Szymanowski, Few Body Syst. 58 \(2017\)](#)

## Motivation: new tools for baryon spectroscopy

- Hadronic probes ( $\pi N$  scattering).
- Electromagnetic (and weak) probes:  $\langle N^*(p') | \sum_f e_f \bar{\Psi}_f \gamma_\mu \Psi_f | N(p) \rangle$ .
- Baryon spectroscopy program with non-diagonal DVCS for Jlab@12GeV:  
**M. Amarian, M. Polyakov, I. Strakovsky and K.S.'08**. Excitation of  $N^*$  by non-local quark-gluon operators:

$$\langle N^* | \bar{\Psi}(0)[0; z] \Psi(z) | N \rangle; \quad \langle N^* | F_{\alpha\beta}(0)[0; z] F_{\mu\nu}(z) | N \rangle; \quad (z^2 = 0).$$



**N.b.**  $-q^2, (p+q)^2$  - large;  
 $|(p'-p)^2|, p'^2$  - moderate.

- Excitation of resonances by arbitrary spin probe.
- Explicit access to gluons.

## Hard Exclusive Processes: GPDs, DAs

- Factorization theorems for hard reactions: amplitude as convolution of perturbative and non-perturbative parts.
- Main objects: matrix elements of QCD light-cone ( $z^2 = 0$ ) operators.

- Quark bilinear light-cone operator:

$$\langle A | \bar{\Psi}(0)[0; z] \Psi(z) | B \rangle$$

⇒ PDFs, meson DAs, GPDs, transition GPDs, etc.

- Three quark bilinear light-cone operator

$$\langle A | \Psi(z_1)[z_1; z_2] \Psi(z_2)[z_2; z_3] \Psi(z_3)[z_3; z_1] | B \rangle$$

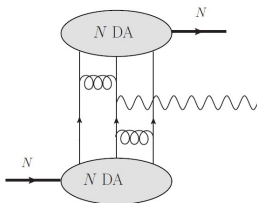
- $\langle A | = \langle 0 |$ ;  $B$  - baryon ⇒ baryon DA. QCD description of nucleon e.m. FF.



# Nucleon DA: well known examples

## Nucleon e.m. FF

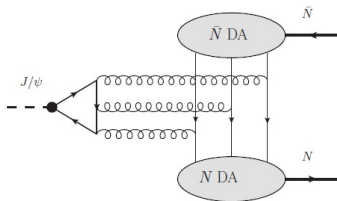
Brodsky & Lepage'81 Efremov & Radyushkin'80



## Charmonium decay

$$J/\psi \rightarrow \bar{N} + N$$

Brodsky & Lepage'81 Chernyak, Ogloblin, and Zhitnitsky'89



## Baryon-to-meson TDAs

$$\langle A | \Psi(z_1)[z_1; z_2] \Psi(z_2)[z_2; z_3] \Psi(z_3)[z_3; z_1] | B \rangle$$

- Let  $\langle A |$  be a light meson state ( $\pi, \eta, \rho, \omega, \dots$ )  $B$  - baryon  $\Rightarrow$  baryon-to-meson TDAs.

### Common features with

- baryon DAs: same operator;
- GPDs:  $\langle B |$  and  $|A\rangle$  are not of the same momentum  $\Rightarrow$  skewness:

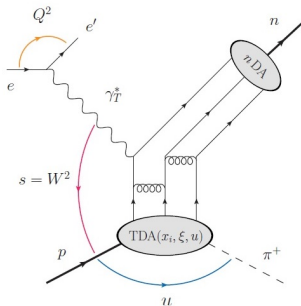
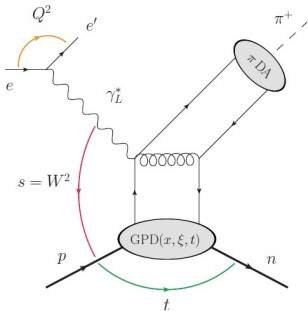
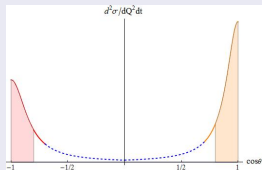
$$\xi = -\frac{(p_A - p_B) \cdot n}{(p_A + p_B) \cdot n}.$$

# Factorization regimes for hard meson production

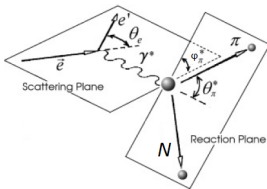
Two complementary regimes in generalized Bjorken limit ( $-q^2 = Q^2$ ,  $W^2$  – large;

$$x_B = \frac{Q^2}{2p \cdot q} - \text{fixed):}$$

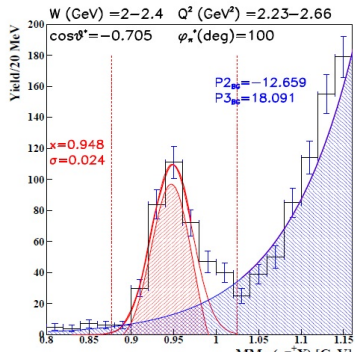
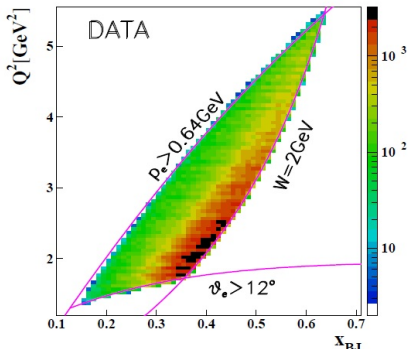
- $t \sim 0$  (forward peak) factorized description in terms of GPDs [J. Collins, L. Frankfurt, M. Strikman'97](#);
- $u \sim 0$  (backward peak) factorized description in terms of TDAs [L. Frankfurt, M. V. Polyakov, M. Strikman et al.'02](#);



# Backward meson electroproduction @ Jlab



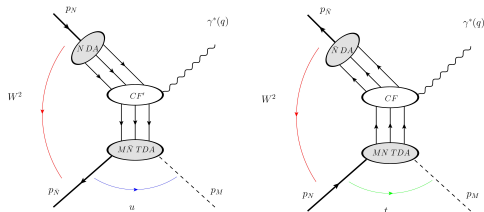
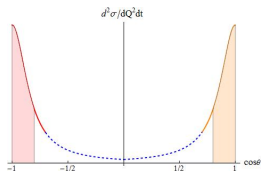
- Data from JLab @ 6 GeV exists for the backward  $\gamma^* p \rightarrow \pi^+ n$ ;
- Analysis (Oct.2001-Jan.2002 run)  
K. Park, M. Guidal, B. Pire and K.S., in preparation



# Baryon to meson TDAs at $\bar{P}$ ANDA I



- **Lansberg et al.'12**:  $\pi N$  TDAs occur in factorized description of  $\bar{N} + N \rightarrow \gamma^*(q) + \pi \rightarrow \ell^+ + \ell^- + \pi$ .
- Two regimes (forward and backward).  $C$  invariance  $\Rightarrow$  perfect symmetry.



## $\bar{P}$ ANDA @ GSI-FAIR

- $E_{\bar{p}} \leq 15 \text{ GeV}; W^2 \leq 30 \text{ GeV}^2$

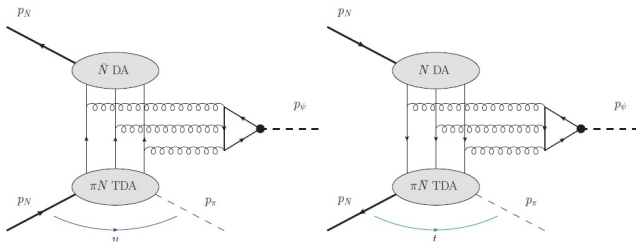
- Planned to be done with the proton FF studies in the timelike region.
- **M. C. Mora Espi, M. Zambrana, F. Maas, K.S.'15**: feasibility of  $\bar{p}p \rightarrow e^+e^-\pi^0$  @ $\bar{P}$ ANDA.

# Baryon to meson TDAs at $\bar{P}ANDA$ II

- Charmonium production in association with a pion [Pire et al.'13](#)

$$\bar{N} + N \rightarrow J/\psi + \pi.$$

- Same TDAs  $\Rightarrow$  test of universality.
- Forward and backward regimes.

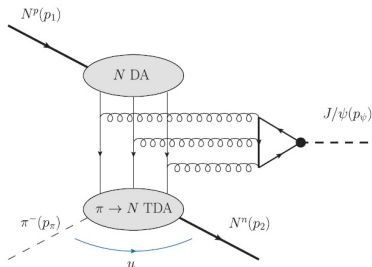


## Baryon to meson TDAs at J-Parc

- J-Parc intense pion beam option:  $P_\pi = 10 - 20$  GeV.
- Charmonium production in association with a nucleon [B. Pire, L. Szymanowski and K.S. , PRD 95, 2017.](#)

$$\pi^- + p \rightarrow n + J/\psi$$

- Near-forward regime:  $|(p_\pi - p_2)^2| \ll W^2, M_\psi^2$ .



## Twist-3 $\pi N$ TDA

J.P.Lansberg, B.Pire & L.Szymanowski'07:

$$\begin{aligned} & 4(P \cdot n)^3 \int \left[ \prod_{i=1}^3 \frac{dz_i}{2\pi} e^{ix_i z_i (P \cdot n)} \right] \langle \pi(p_\pi) | \varepsilon_{c_1 c_2 c_3} \Psi_\rho^{c_1}(z_1 n) \Psi_\tau^{c_2}(z_2 n) \Psi_\chi^{c_3}(z_3 n) | N(p_1, s_1) \rangle \\ &= \delta(2\xi - x_1 - x_2 - x_3) i \frac{f_N}{f_\pi M} \\ & \times \left[ V_1^{\pi N} (\hat{P}C)_{\rho\tau} (\hat{P}U)_\chi + A_1^{\pi N} (\hat{P}\gamma^5 C)_{\rho\tau} (\gamma^5 \hat{P}U)_\chi + T_1^{\pi N} (\sigma_{P\mu} C)_{\rho\tau} (\gamma^\mu \hat{P}U)_\chi \right. \\ & + V_2^{\pi N} (\hat{P}C)_{\rho\tau} (\hat{\Delta}U)_\chi + A_2^{\pi N} (\hat{P}\gamma^5 C)_{\rho\tau} (\gamma^5 \hat{\Delta}U)_\chi + T_2^{\pi N} (\sigma_{P\mu} C)_{\rho\tau} (\gamma^\mu \hat{\Delta}U)_\chi \\ & \left. + \frac{1}{M} T_3^{\pi N} (\sigma_{P\Delta} C)_{\rho\tau} (\hat{P}U)_\chi + \frac{1}{M} T_4^{\pi N} (\sigma_{P\Delta} C)_{\rho\tau} (\hat{\Delta}U)_\chi \right] \end{aligned}$$

- $P = \frac{1}{2}(p_1 + p_\pi)$ ;  $\Delta = (p_\pi - p_1)$ ;  $n^2 = p^2 = 0$ ;  $2p \cdot n = 1$ ;  $\sigma_{P\mu} \equiv P^\nu \sigma_{\nu\mu}$ ;
- $C$ : charge conjugation matrix;
- $f_N = 5.2 \cdot 10^{-3} \text{ GeV}^2$  (V. Chernyak and A. Zhitnitsky'84);
- $\xi = -\frac{\Delta \cdot n}{2P \cdot n}$
- 8 TDAs:  $H(x_1, x_2, x_3, \xi, \Delta^2, \mu^2) \equiv \{V_i, A_i, T_i\}(x_1, x_2, x_3, \xi, \Delta^2, \mu^2)$
- c.f. 3 leading twist nucleon DAs:  $V^P, A^P, T^P$



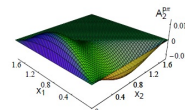
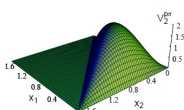
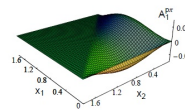
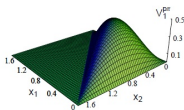
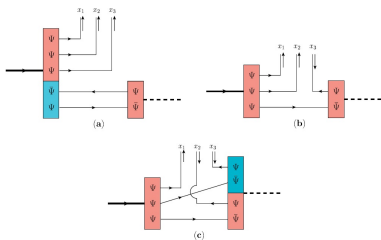
# Interpretation and modeling of $\pi N$ TDAs I

- Mellin moments in  $x_i \Rightarrow \pi N$  matrix elements of local operators

$$\left[ i\vec{D}^{\mu_1} \dots i\vec{D}^{\mu_{n_1}} \Psi_\rho(0) \right] \left[ i\vec{D}^{\nu_1} \dots i\vec{D}^{\nu_{n_2}} \Psi_\tau(0) \right] \left[ i\vec{D}^{\lambda_1} \dots i\vec{D}^{\lambda_{n_3}} \Psi_\chi(0) \right].$$

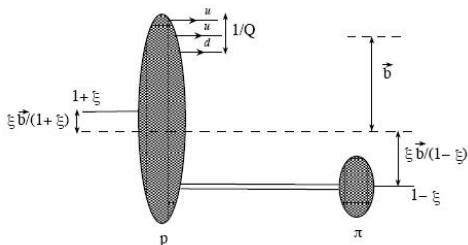
Can be studied on the lattice [Y. Aoki et al.](#)

- $\pi N$  TDAs provides information on the next to minimal Fock state. Light-cone quark model interpretation [B. Pasquini et al. 2009](#):



## Interpretation and modelling of $\pi N$ TDAs II

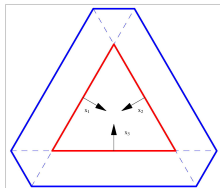
- Impact parameter space interpretation: the Fourier transform  $\Delta_T \rightarrow b_T$  of TDAs  $\Rightarrow$  transverse imaging of the nucleon



## Fundamental theoretical requirements for $\pi N$ TDAs:

### B. Pire, L.Szymanowski, KS'10,11:

- 1 restricted support in  $x_1, x_2, x_3$ : intersection of three stripes  $-1 + \xi \leq x_i \leq 1 + \xi$  ( $\sum_i x_i = 2\xi$ )
  - 2 polynomiality in  $\xi$  of the Mellin moments in  $x_i$
  - 3 isospin + permutation symmetry
  - 4 crossing:  $\pi N$  TDA  $\leftrightarrow$   $\pi N$  GDA
  - 5 chiral properties: soft pion theorem
  - 6 QCD evolution
- Spectral representation **A. Radyushkin'97** generalized for  $\pi N$  TDAs ensures polynomiality and support:

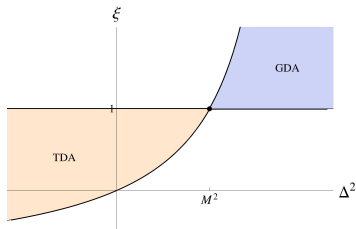


$$\begin{aligned} H(x_1, x_2, x_3 = 2\xi - x_1 - x_2, \xi) \\ = \left[ \prod_{i=1}^3 \int_{\Omega_i} d\beta_i d\alpha_i \right] \delta(x_1 - \xi - \beta_1 - \alpha_1 \xi) \delta(x_2 - \xi - \beta_2 - \alpha_2 \xi) \\ \times \delta(\beta_1 + \beta_2 + \beta_3) \delta(\alpha_1 + \alpha_2 + \alpha_3 + 1) F(\beta_1, \beta_2, \beta_3, \alpha_1, \alpha_2, \alpha_3); \end{aligned}$$

- $\Omega_i$ :  $\{|\beta_i| \leq 1, |\alpha_i| \leq 1 - |\beta_i|\}$  are copies of the usual DD square ;
- $F(\dots)$ : six variables that are subject to two constraints  $\Rightarrow$  **quadruple distributions**

## Crossing and soft pion theorem for $\pi N$ GDA/TDA

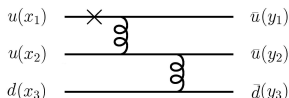
- Crossing relates  $\pi N$  TDAs in  $\gamma^* N \rightarrow \pi N'$  and  $\pi N$  GDAs (light-cone wave function)
- Physical domain in  $(\Delta^2, \xi)$ -plane (defined by  $\Delta_T^2 \leq 0$ ) in the chiral limit ( $m_\pi = 0$ ):



- Soft pion theorem [P. Pobylitsa, M. Polyakov and M. Strikman'01](#) ( $Q^2 \gg \Lambda_{\text{QCD}}^3/m_\pi$ ) constrains  $\pi N$  GDA at the threshold  $\xi = 1$ ,  $\Delta^2 = M^2$  in terms of nucleon DAs  $V^P$ ,  $A^P$ ,  $T^P$  (see [V. Braun, D. Ivanov, A. Lenz, A. Peters'08](#)).

## Calculation of the amplitude

- LO amplitude for  $\bar{p}p \rightarrow \gamma^* \pi^0$  can be computed as in J.P. Lansberg, B. Pire and L. Szymanowski'07
- 21 diagrams contribute



$$\mathcal{I} \sim \int_{-1+\xi}^{1+\xi} d^3x \delta(x_1 + x_2 + x_3 - 2\xi) \int_{-1}^1 d^3y \delta(1 - y_1 - y_2 - y_3) \left( \sum_{\alpha=1}^{21} R_{\alpha} \right)$$

Each  $R_{\alpha}$ , has the structure:

$$R_{\alpha} \sim K_{\alpha}(x_1, x_2, x_3) \times Q_{\alpha}(y_1, y_2, y_3) \times$$

[combination of  $\pi N$  TDAs]  $\times$  [combination of nucleon DAs]

$$R_1 = \frac{q^{\mu} (2\xi)^2 [(V_1^{p\pi^0} - A_1^{p\pi^0})(V^p - A^p) + 4T_1^{p\pi^0} T^p + 2\frac{\Delta^2}{M^2} T_4^{p\pi^0} T^p]}{(2\xi - x_1 + i\epsilon)^2 (x_3 + i\epsilon) (1 - y_1)^2 y_3}$$

c.f.  $\int_{-1}^1 dx \frac{H(x, \xi)}{x \pm \xi \mp i\epsilon} \int_0^1 dy \frac{\phi_M(y)}{y}$  for HMP

## $\rho\bar{p} \rightarrow \pi\gamma^*$ amplitude and $\bar{p}p \rightarrow \gamma^*\pi \rightarrow \ell^+\ell^-\pi$ cross section

$$\mathcal{M}_{s_p s_{\bar{p}}}^\lambda = -i \frac{(4\pi\alpha_s)^2 \sqrt{4\pi\alpha_{em}} f_N^2}{54f_\pi} \frac{1}{Q^4} \left[ S_{s_p s_{\bar{p}}}^\lambda \mathcal{I}(\xi, \Delta^2) - S'_{s_p s_{\bar{p}}}{}^\lambda \mathcal{I}'(\xi, \Delta^2) \right],$$

where

$$S_{s_p s_{\bar{p}}}^\lambda \equiv \bar{V}(p_{\bar{p}}, s_{\bar{p}}) \hat{\epsilon}^*(\lambda) \gamma_5 U(p_p, s_p);$$

$$S'_{s_p s_{\bar{p}}}{}^\lambda \equiv \frac{1}{M} \bar{V}(p_{\bar{p}}, s_{\bar{p}}) \hat{\epsilon}^*(\lambda) \hat{\Delta}_T \gamma_5 U(p_p, s_p),$$

### $\bar{p}p \rightarrow \gamma^*\pi \rightarrow \ell^+\ell^-\pi$ cross section

$$\frac{d\sigma}{dtdQ^2 d\cos\theta_\ell} = \int d\varphi_\ell \frac{2\pi e^2 (1 + \cos^2\theta_\ell)}{Q^2} \frac{|\overline{\mathcal{M}_T}|^2}{64W^2(W^2 - 4M^2)(2\pi)^4}.$$

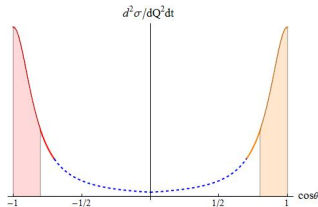
## Essential points of the approach

- Off-shell photon is transversally polarized at leading twist  $\Rightarrow$  characteristic behavior in lepton polar angle:  $1 + \cos^2 \theta_l$
- $1/Q^8$  scaling behavior of the  $p\bar{p} \rightarrow \gamma^* \pi$  cross section
- Non-zero imaginary part of the amplitude.

## Cross section estimates

$$\frac{d\sigma}{dt dQ^2 d \cos \theta_\ell} = \int d\varphi_\ell \frac{2\pi e^2 (1 + \cos^2 \theta_\ell)}{Q^2} \frac{|\overline{\mathcal{M}}_T|^2}{64 W^2 (W^2 - 4M^2) (2\pi)^4}.$$

- Useful cut:  $|\Delta_T^2|$ -cut  $\Leftrightarrow$  cut in  $\theta_{\text{CMS}}$ .
- This helps to focus on forward (backward) regime.



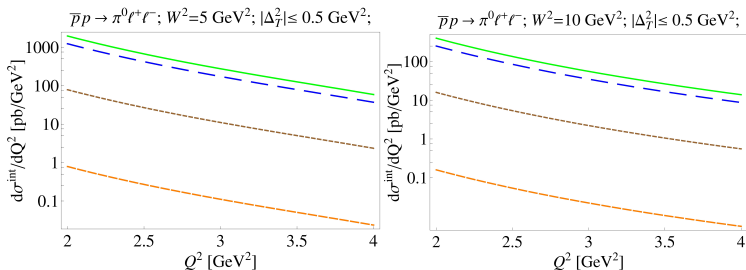
### Integrated cross section

$$\frac{d\sigma^{\text{int}}}{dQ^2} (|\Delta_T^2|_{\text{max}}) \equiv \int_{t_{\text{min}}}^{t_{\text{max}}} dt \int d\theta_\ell \frac{d\sigma}{dt dQ^2 d \cos \theta_\ell}$$



## $\bar{p}p \rightarrow \pi^0 \gamma^* \rightarrow \pi^0 \ell^+ \ell^-$ cross section

- Nucleon pole dominates over quadruple distribution part for PANDA conditions
- Numerical input: COZ, KS, BLW NLO, BLW NNLO phenomenological solutions for nucleon DAs



- Cross section of  $\bar{p}n \rightarrow \pi^- \gamma^* \rightarrow \pi^- \ell^+ \ell^-$  is larger by factor 2. But requires neutron target.

## First feasibility studies for $\bar{P}ANDA$

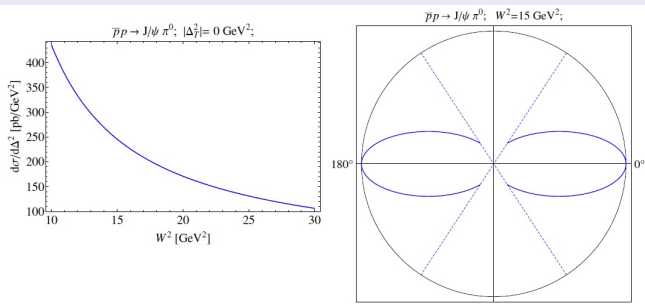
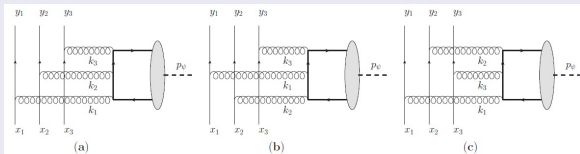
M. C. Mora Espi, M. Zambrana, F. Maas, K.S' 15

- Study of  $p\bar{p} \rightarrow e^+e^-\pi^0$  (signal) with  $p\bar{p} \rightarrow \pi^+\pi^-\pi^0$  (main hadronic background).
- Simulations performed for  $s = 5 \text{ GeV}^2$  and  $s = 10 \text{ GeV}^2$
- $|\cos\theta_\pi^*| > 0.5$  cut imposed
- Modified version of [Lansberg, Pire, Szymanowski.'07](#) model used for  $\pi N$  TDAs used as input for MC.
- $2 \text{ fb}^{-1}$  of integrated luminosity assumed ( $\sim 5$  months High Lumi.)
- Expected number of signal events then is 3350 and 465 for  $s = 5 \text{ GeV}^2$  and  $s = 10 \text{ GeV}^2$

# $N \bar{N} \rightarrow J/\psi \pi$ at $\bar{P}ANDA$

Amplitude calculation and cross section estimates B. Pire, L. Szymanowski, KS,'13

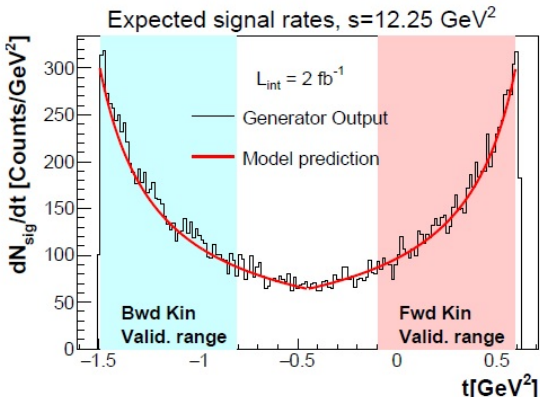
## Unpolarized cross section and angular distribution



# Feasibility study of $p\bar{p} \rightarrow J/\psi\pi^0$ at $\bar{P}$ ANDA

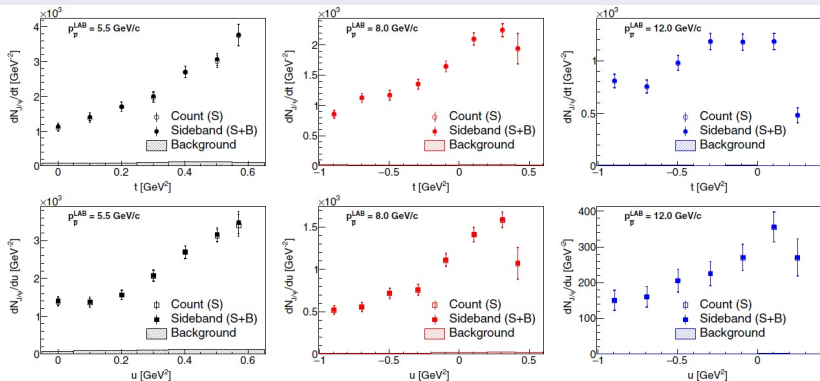
B. Ramstein, E. Atomssa and  $\bar{P}$ ANDA collaboration and K.S. PRD 95'17

- Event generator based on TDA model prediction Pire et al.'13.
- Simulations performed for  $s = 12.2 \text{ GeV}^2$ ,  $s = 16.9 \text{ GeV}^2$  and  $s = 24.3 \text{ GeV}^2$ .
- Study of  $p\bar{p} \rightarrow J/\psi\pi^0$  (signal) with background from  $p\bar{p} \rightarrow \pi^+\pi^-\pi^0$  and  $p\bar{p} \rightarrow J/\psi\pi^0\pi^0$  and other sources.



# Feasibility study of $\bar{p}p \rightarrow J/\psi\pi^0$ at $\bar{P}ANDA$

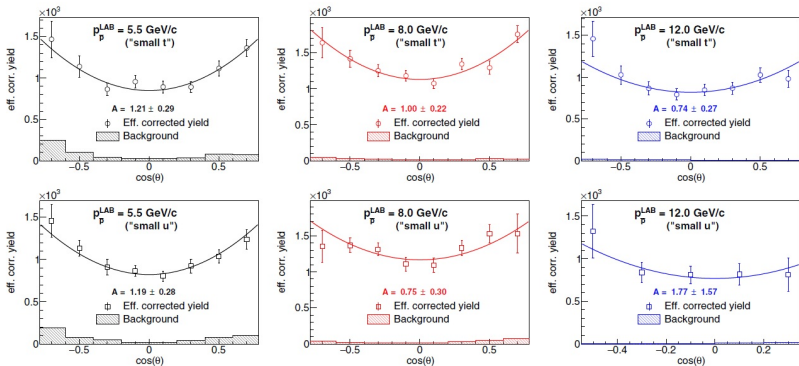
## Signal and Background Count Rates vs. $t$ and $u$



- Signal and background count rates for  $2 \text{ fb}^{-1}$  ( $\sim 5$  months in High Luminosity mode)
- Worst case scenario at  $p_{\bar{p}} = 5.5 \text{ GeV}/c$ : S/B at least factor 10.

# Feasibility study of $\bar{p}p \rightarrow J/\psi\pi^0$ at $\bar{P}ANDA$

## Angular distribution of $J/\psi$ decay electrons



- Signal count extracted from fits corrected for efficiency
- Free fit with  $B(1 + A \cos^2 \theta_\ell^*)$ .

# Pion electroproduction at backward angles with CLAS

K. Park et al. *in preparation*

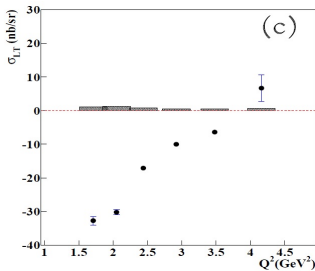
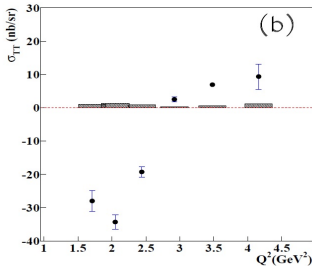
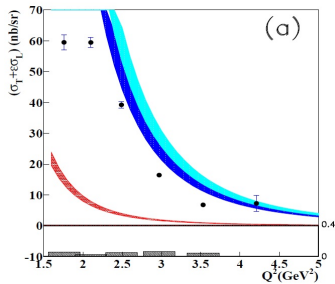
$$\frac{d\sigma}{d\Omega_{\pi}^*} = A + B \cos \varphi_{\pi}^* + C \cos 2\varphi_{\pi}^*, \quad \text{where}$$

$$A = \sigma_T + \epsilon\sigma_L; \quad B = \sqrt{2\epsilon(1+\epsilon)}\sigma_{LT};$$

$$C = \epsilon\sigma_{TT}$$

Table: Determination of kinematic bin.

Variable	Number of bins	Range	Bin size
$W$	1	2.0 – 2.4 GeV	400 MeV
$Q^2$	5	1.6 – 4.5 GeV <sup>2</sup>	various
$\Delta_T^2$	1	0 – 0.5 GeV <sup>2</sup>	0.5 GeV <sup>2</sup>
$\varphi_{\pi}^*$	9	0° – 360°	40°



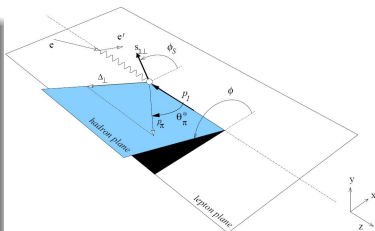
## Conclusions & Outlook

- 1 Nucleon to meson TDAs provide new information about correlation of partons inside hadrons
- 2 We strongly encourage to try to detect near forward and backward signals for various mesons ( $\pi$ ,  $\eta$ ,  $\omega$ ,  $\rho$ ): there could be interesting physics around!
- 3 Theoretical understanding is growing up: spectral representation for  $\pi N$  TDA based on quadruple distributions; factorized Ansatz for quadruple distributions with input at  $\xi = 1$ .
- 4 Some experimental success achieved for backward  $\gamma^* N \rightarrow N' \pi$  already at 6 GeV (and more is expected at 12 GeV)
- 5  $\bar{p} N \rightarrow \pi \ell^+ \ell^-$  ( $q^2$  - timelike) and  $\bar{p} N \rightarrow \pi J/\psi$  @ PANDA would allow to check universality of TDAs
- 6 Open questions: proof of factorization theorems, interpretation in the impact parameter space, analytic properties of the amplitude



# Transverse Target Single Spin Asymmetry $\gamma^* N \rightarrow \pi N$

- TSA =  $\sigma^\uparrow - \sigma^\downarrow \sim \text{Im part of the amplitude}$
- it probes the contribution of the DGLAP-like regions
- One expects a TSA vanishing with  $Q^2$  and  $W^2$  for (simple) baryon-exchange approaches
- Non vanishing and  $Q^2$ -independent TSA within TDA approach



$$\mathcal{A} = \frac{1}{|\vec{s}_1|} \left( \int_0^\pi d\tilde{\phi} |\mathcal{M}_T^{s_1}|^2 - \int_\pi^{2\pi} d\tilde{\phi} |\mathcal{M}_T^{s_1}|^2 \right) \left( \int_0^{2\pi} d\tilde{\phi} |\mathcal{M}_T^{s_1}|^2 \right)^{-1}$$

