

The ANL-Osaka dynamical coupled-channels (DCC) approach for baryon spectroscopy

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Collaborators:

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Satoshi Nakamura (Cruzeiro do Sul U.)

Toru Sato (Osaka U.)

ANL-Osaka DCC approach to N^* & Δ^*

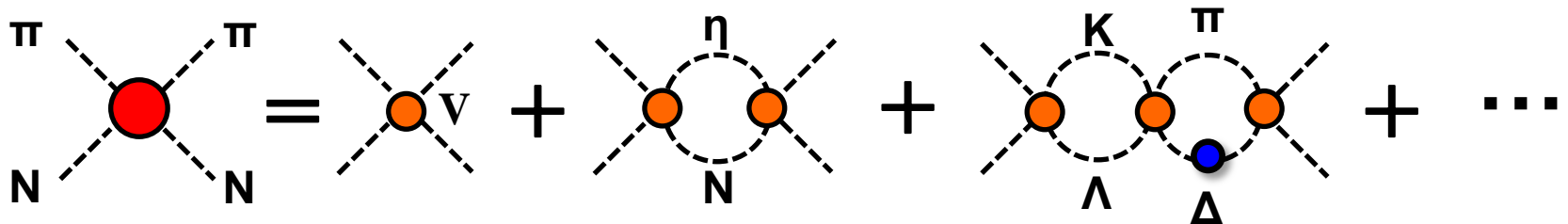
Dynamical coupled-channels model [Matsuyama, Sato, Lee, Phys. Rep. 439(2007)193]

$$T_{a,b}^{(LSJ)}(p_a, p_b; E) = V_{a,b}^{(LSJ)}(p_a, p_b; E) + \underbrace{\sum_c}_{\text{CC effect}} \underbrace{\int_0^\infty q^2 dq}_{\text{off-shell effect}} V_{a,c}^{(LSJ)}(p_a, q; E) G_c(q; E) T_{c,b}^{(LSJ)}(q, p_b; E)$$

$$a, b, c = (\gamma^{(*)}N, \pi N, \eta N, \underbrace{[\pi\Delta, \sigma N, \rho N]}_{\pi\pi N}, K\Lambda, K\Sigma, \dots)$$

- ✓ Summing up all possible transitions between reaction channels !!
 (→ satisfies **multichannel two-** and **three-body unitarity**)

e.g.) πN scattering



- ✓ **Momentum integral** takes into account **off-shell rescattering effects** in the intermediate processes.

ANL-Osaka DCC approach to N^* & Δ^*

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$a, b, c = N, \Delta, \pi, \rho, \sigma, \omega, \dots$

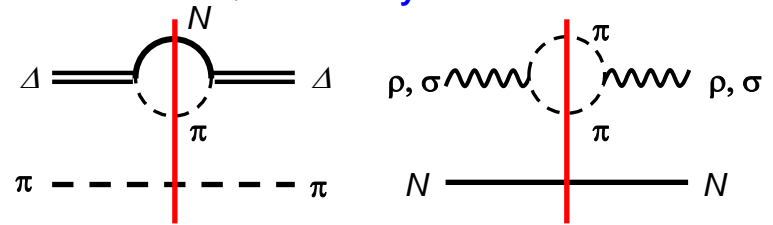
$MB = \pi N, \eta N, K\Lambda, K\Sigma$

Stable channels



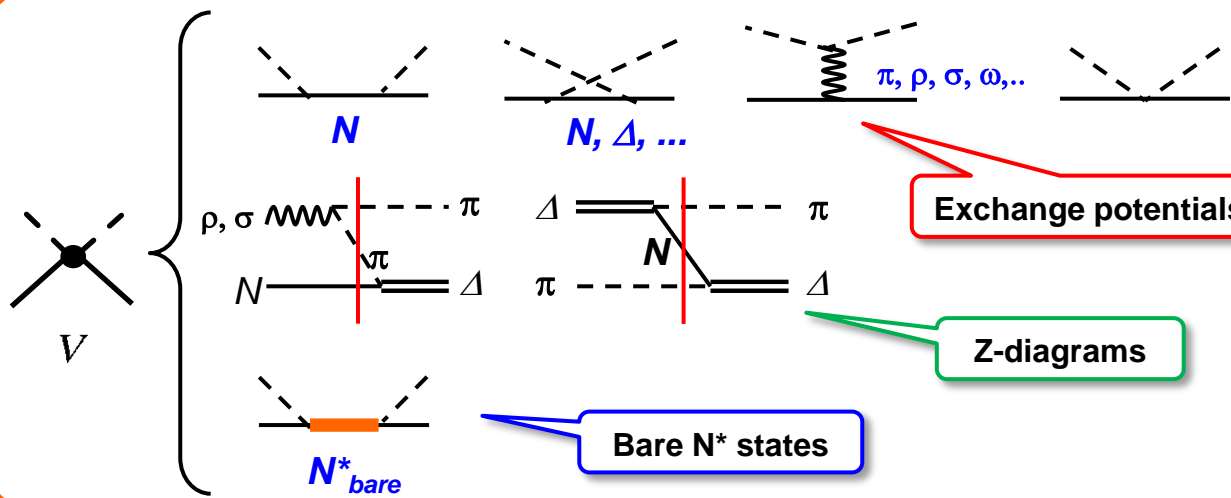
$MB = \pi\Delta, \rho N, \sigma N$

Quasi 2-body channels



✓ Summation
(→)

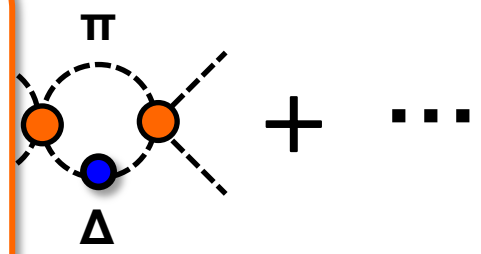
OS
Potentials



Exchange potentials

Z-diagrams

Bare N^* states



Rescattering effects

ANL-Osaka DCC approach to N^* & Δ^*

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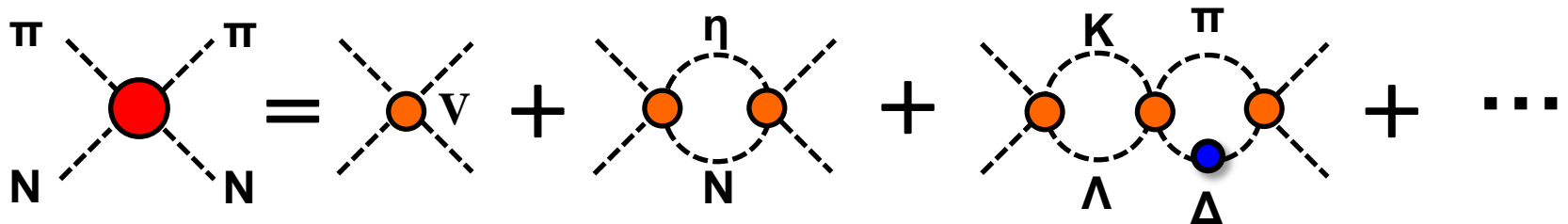
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$\pi\pi N$

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e.g.) πN scattering



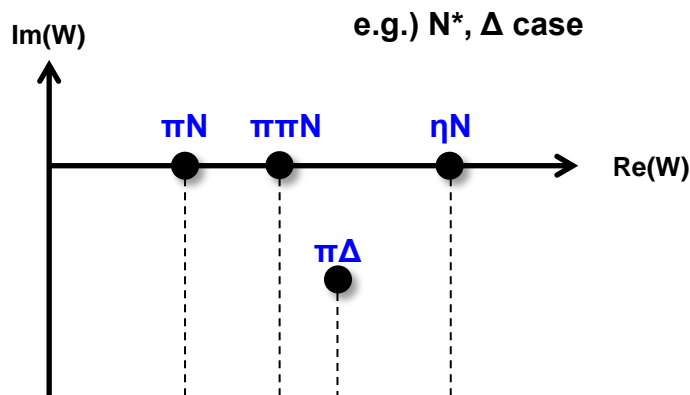
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ANL-Osaka DCC approach to N^* & Δ^*

Dynamical coupled-channels model [Matsuyama, Sato, Lee, Phys. Rep. 439(2007)193]

Why DCC approach ??

- ✓ It defines **proper analytic structure** (branch points, cuts,...) of scattering amplitudes in the **complex energy plane**, as required by scattering theory
- Crucial for extracting resonances “correctly”, and avoiding **WRONG** resonance signals !!
[e.g., Ceci et al, PRC84(2011)015205]



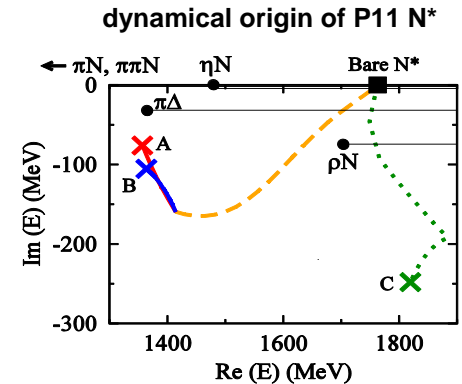
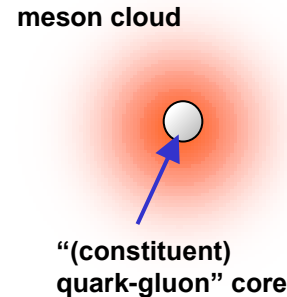
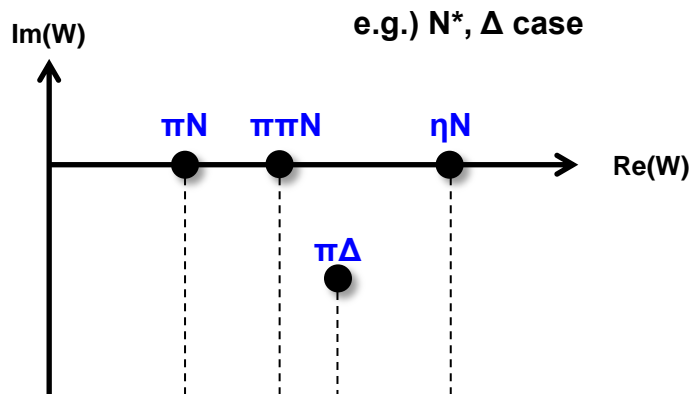
ANL-Osaka DCC approach to N^* & Δ^*

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Why DCC approach ??

- ✓ It defines **proper analytic structure** (branch points, cuts,...) of scattering amplitudes in the **complex energy plane**, as required by scattering theory
- ✓ Interested in clarifying the **physics of reaction dynamics** behind formation, substructure, etc. of baryon resonances.

- Crucial for extracting resonances “correctly”, and avoiding **WRONG** resonance signals !!
[e.g., Ceci et al, PRC84(2011)015205]



Modeling reaction processes appropriately with a model Hamiltonian & solving proper quantum scattering equation (LS eq.) is crucial !!

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Dynamical coupled-channels model [Matsuyama, Sato, Lee, Phys. Rep. 439(2007)193]

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$$a, b, c = (\gamma^{(*)}N, \pi N, \eta N, \boxed{\pi\Delta, \sigma N, \rho N}, K\Lambda, K\Sigma, \dots)$$

$\pi\pi N$

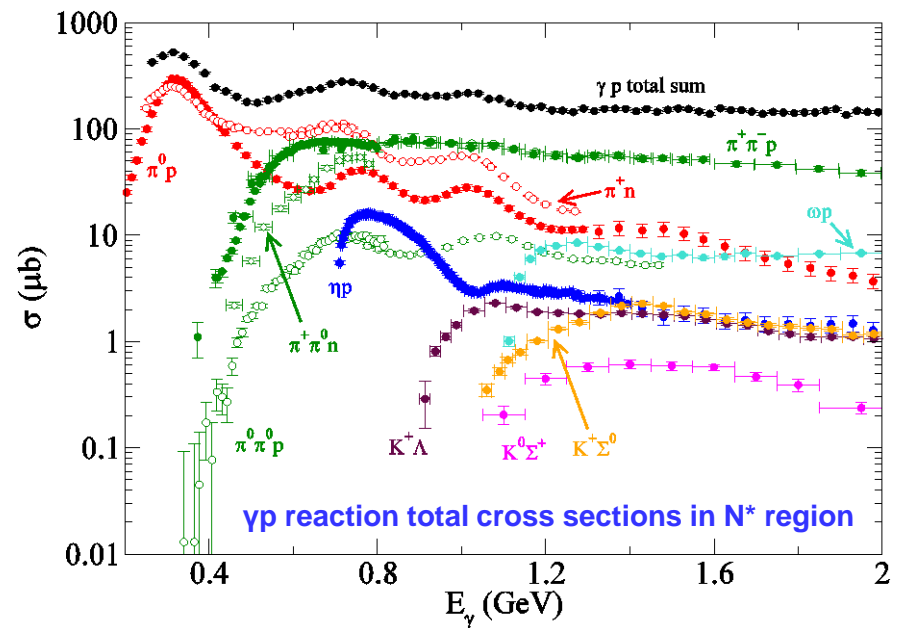
← Region our model can cover →

Latest published model:

HK, Nakamura, Lee, Sato, PRC94(2016)015201
[updated version of PRC88(2013)035209]

Constructed by **simultaneous** analysis of

- πN SAID PW amps. ($W < 2.3$ GeV)
- $\pi\pi \rightarrow \eta N, K\Lambda, K\Sigma$ ($W < 2.1$ GeV)
- $\gamma p \rightarrow \pi N, \eta N, K\Lambda, K\Sigma$ ($W < 2.1$ GeV)
- $\gamma'n' \rightarrow \pi N$ ($W < 2$ GeV)

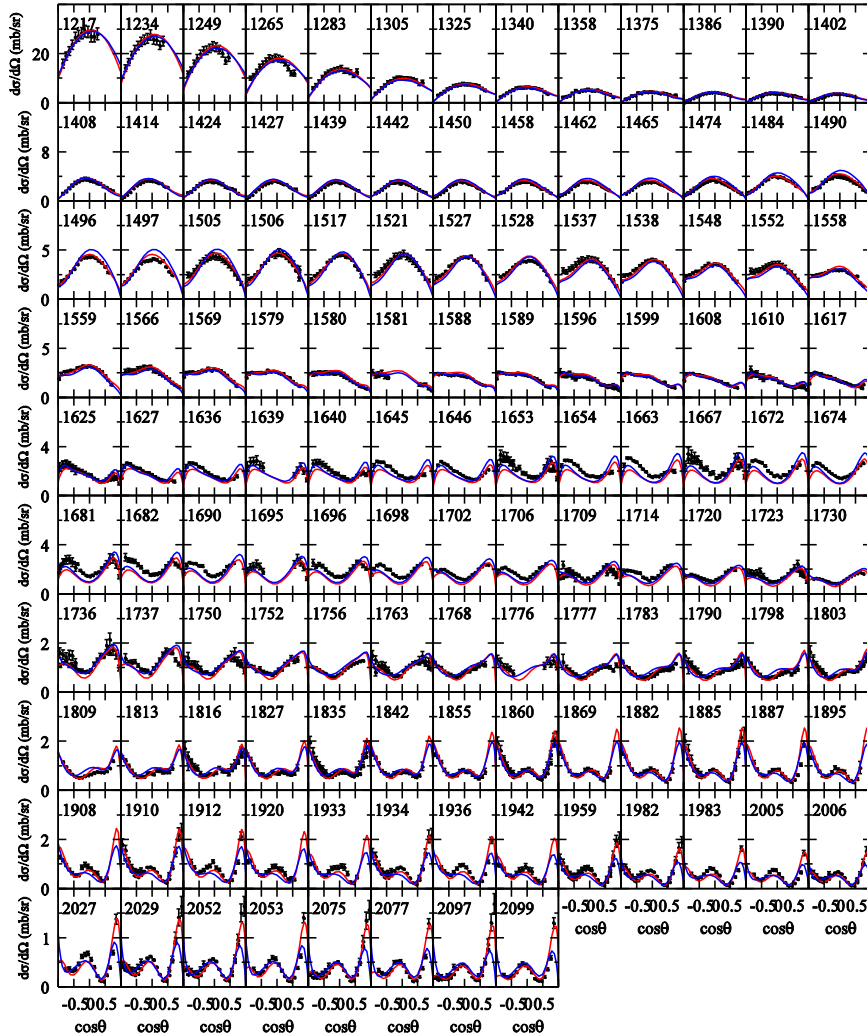


ANL-Osaka DCC approach to N^* & Δ^*

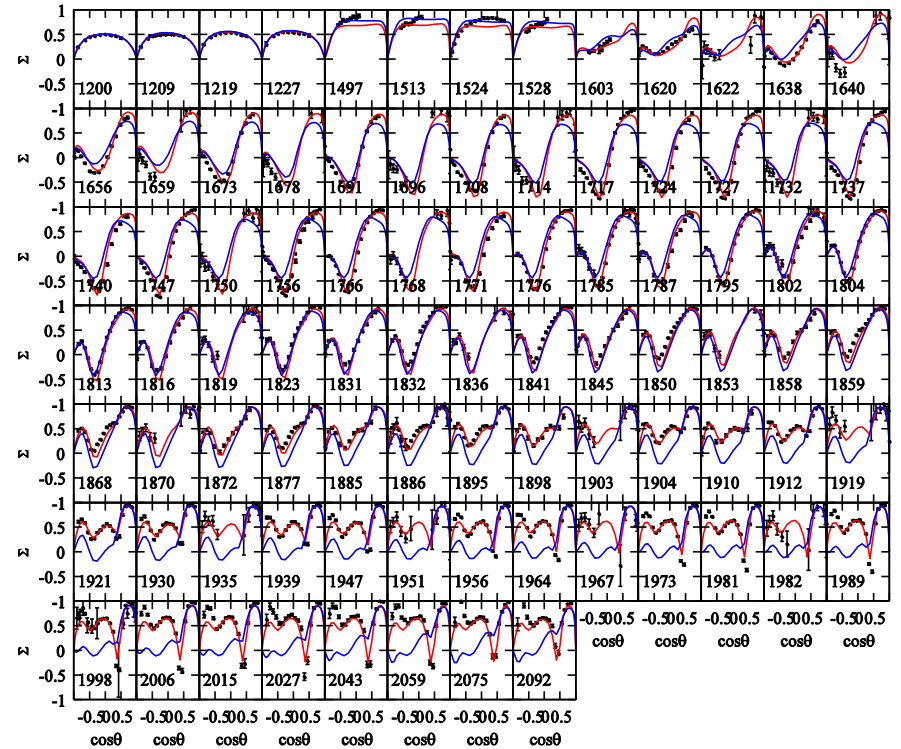
HK, Nakamura, Lee, Sato, PRC88(2013)035209; 94(2016)015201

$\gamma p \rightarrow \pi^0 p$

$d\sigma/d\Omega$ for $W < 2.1$ GeV



Σ for $W < 2.1$ GeV



Red: Updated model [PRC94(2016)015201]

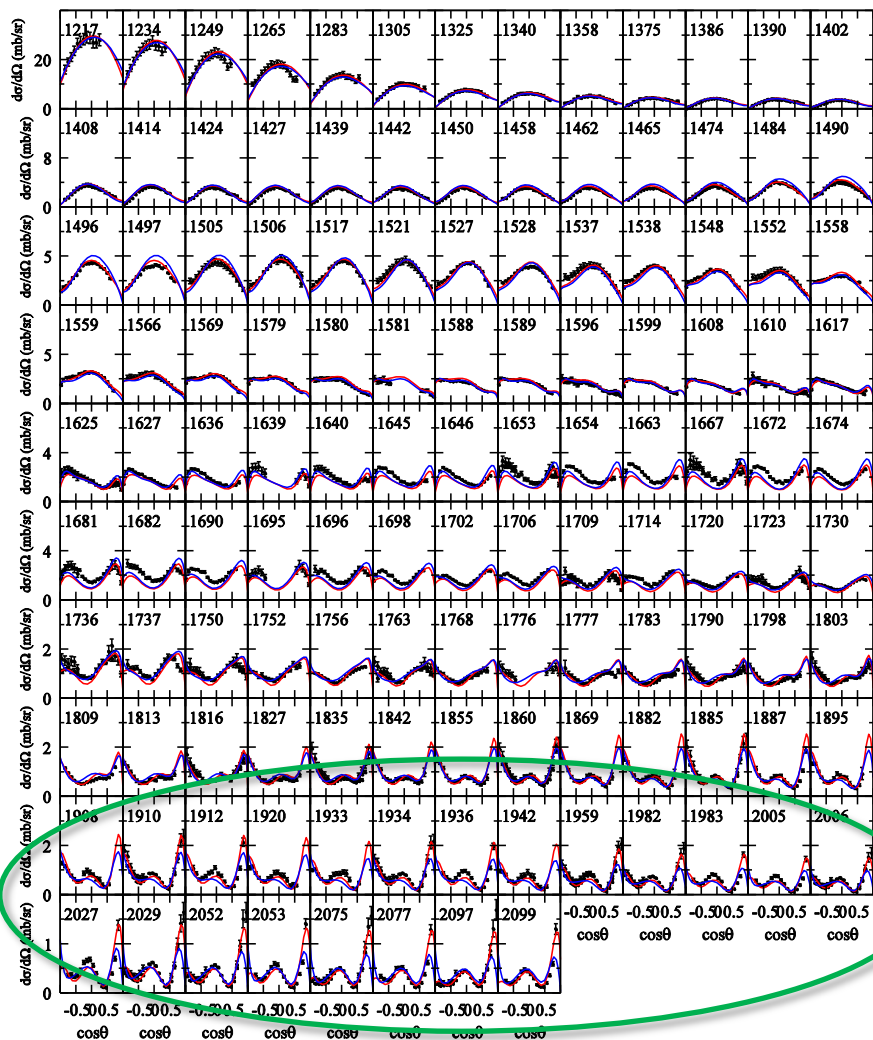
Blue: Original model [PRC88(2013)035209]

ANL-Osaka DCC approach to N^* & Δ^*

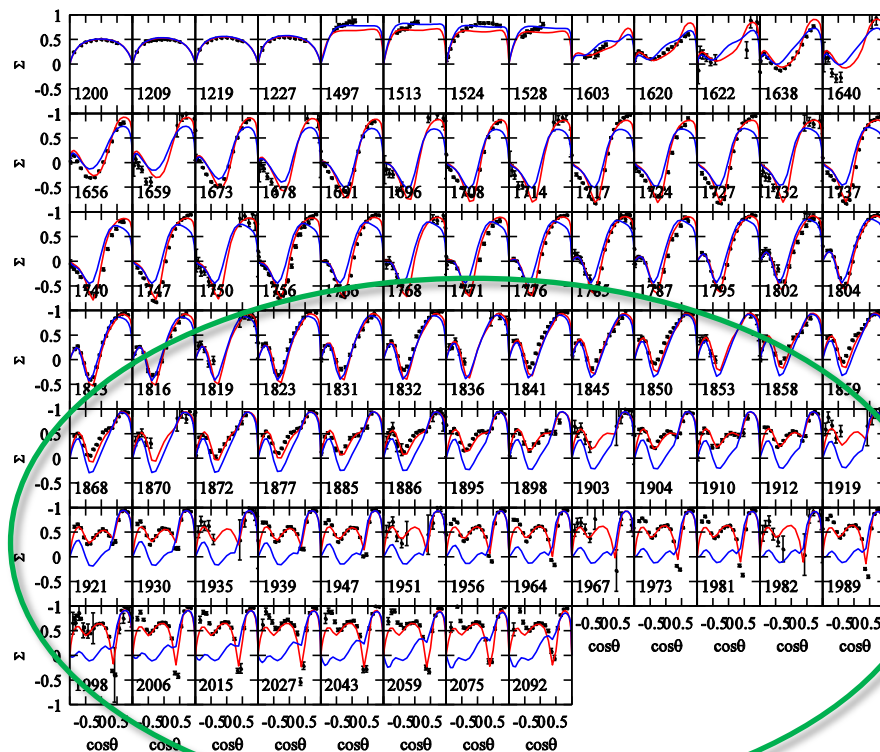
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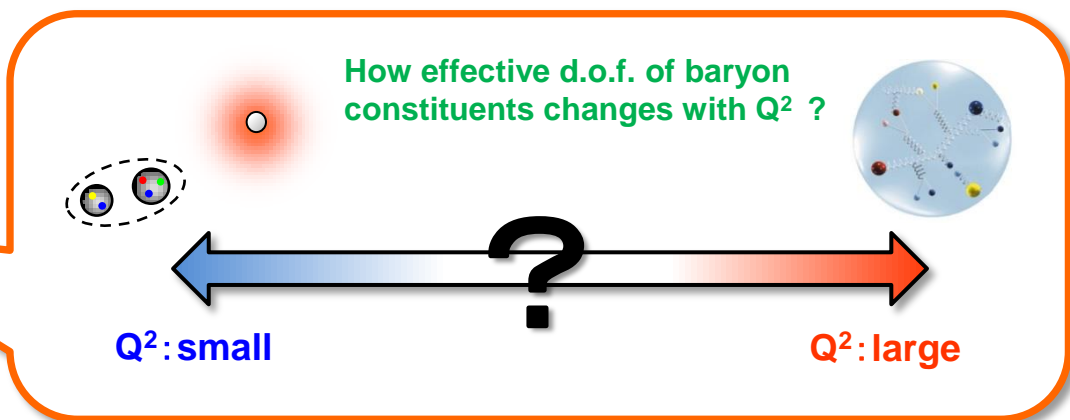
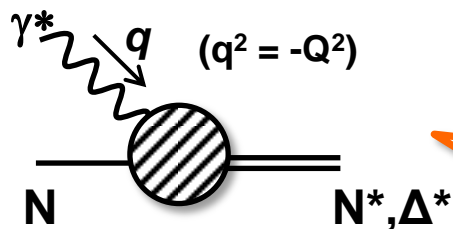


Red: Updated model [PRC94(2016)015201]

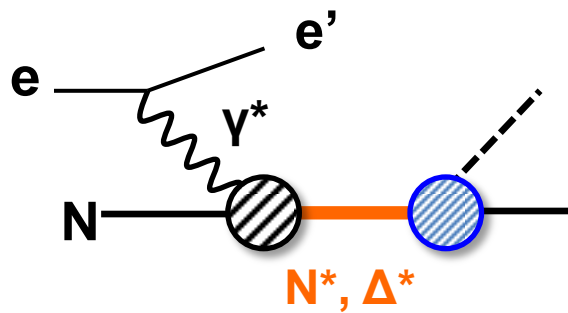
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Analysis of electroproduction reactions: Determining $N-N^*$, $N-\Delta^*$ e.m. transition form factors

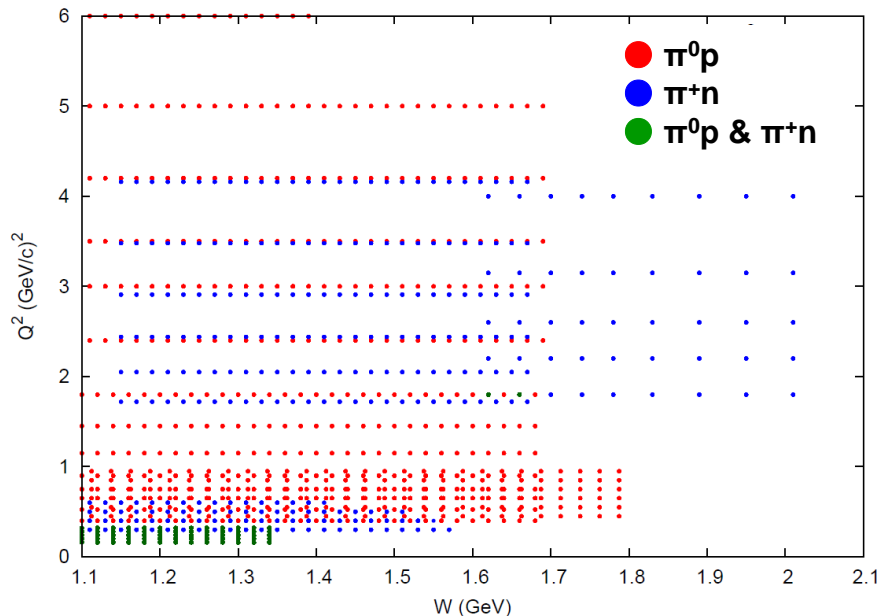
$N-N^*$ e.m. transition form factors



Meson electroproductions:



CLAS database for 1π electroproductions
($Q^2 < 6 \text{ GeV}^2$)



Analysis of electroproduction reactions: Determining $N-N^*$, $N-\Delta^*$ e.m. transition form factors

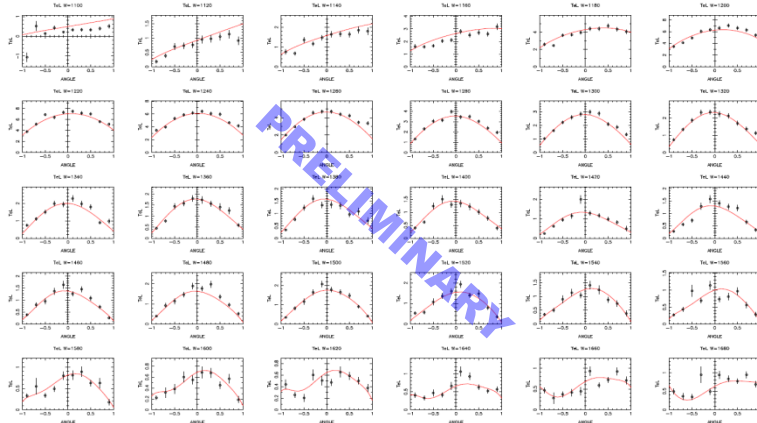
$$\frac{d\sigma^5}{dE_{e'}d\Omega_{e'}d\Omega_{\pi}^*} = \Gamma_{\gamma} \left[\sigma_T + \epsilon\sigma_L + \sqrt{2\epsilon(1+\epsilon)}\sigma_{LT} \cos\phi_{\pi}^* + \epsilon\sigma_{TT} \cos 2\phi_{\pi}^* + h_e \sqrt{2\epsilon(1-\epsilon)}\sigma_{LT'} \sin\phi_{\pi}^* \right].$$

$\sigma_T + \epsilon\sigma_L$ for $ep \rightarrow e\pi^0 p$

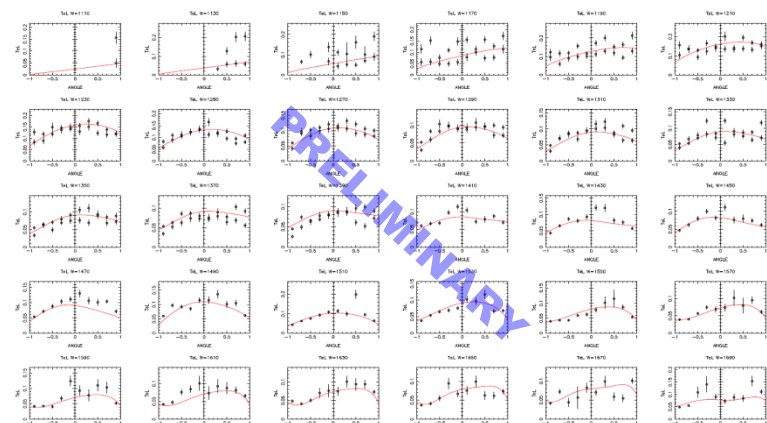
Data for structure functions are obtained with the help of K. Joo and L. C. Smith.

$\sigma_{\alpha} = \sigma_{\alpha}(W, Q^2, \cos\theta_{\pi}^*)$

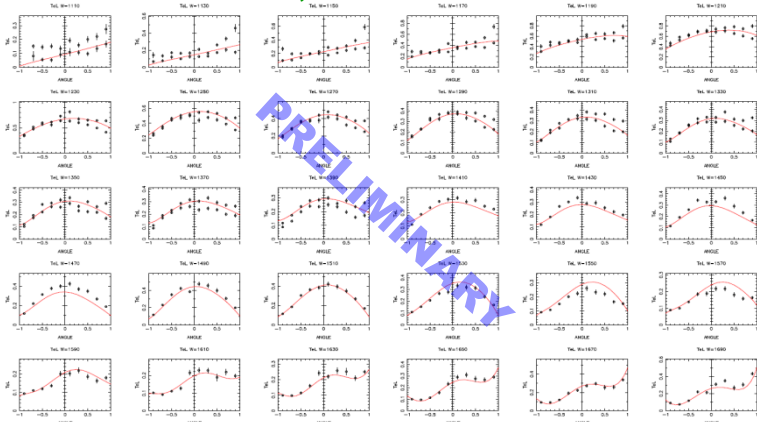
$Q^2 = 1.15 \text{ GeV}^2, 1.10 < W < 1.69 \text{ GeV}$



$Q^2 = 5.0 \text{ GeV}^2, 1.11 < W < 1.69 \text{ GeV}$

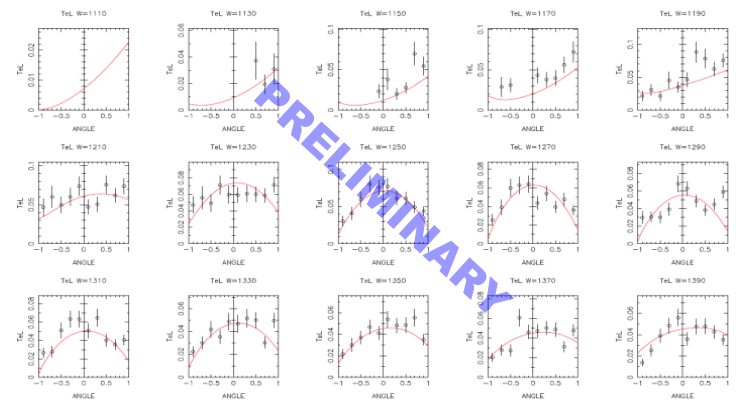


$Q^2 = 3.0 \text{ GeV}^2, 1.11 < W < 1.69 \text{ GeV}$



$\cos\theta$

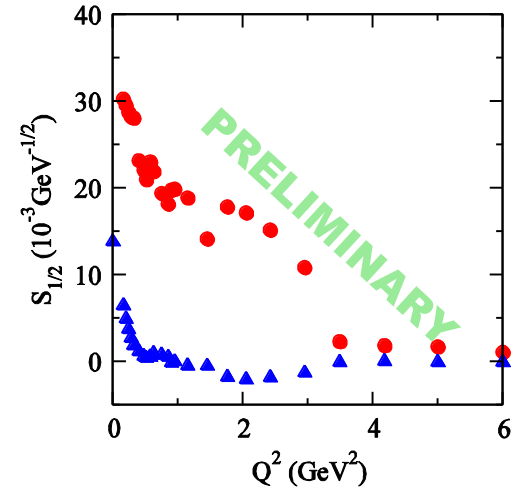
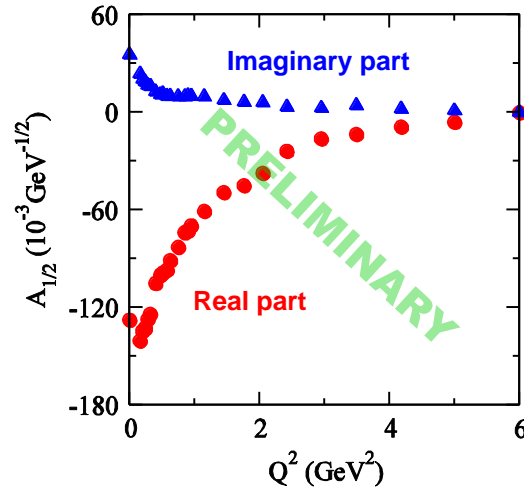
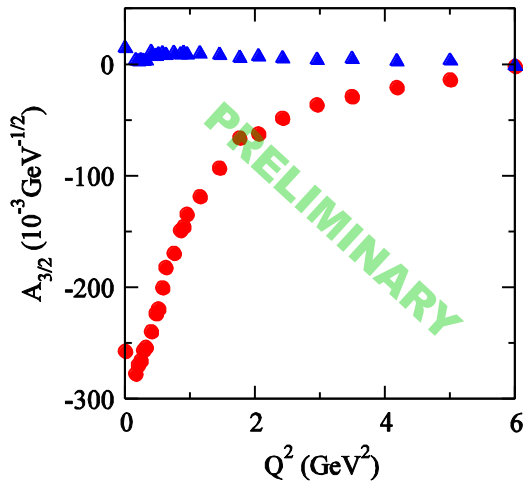
$Q^2 = 6.0 \text{ GeV}^2, 1.11 < W < 1.39 \text{ GeV}$



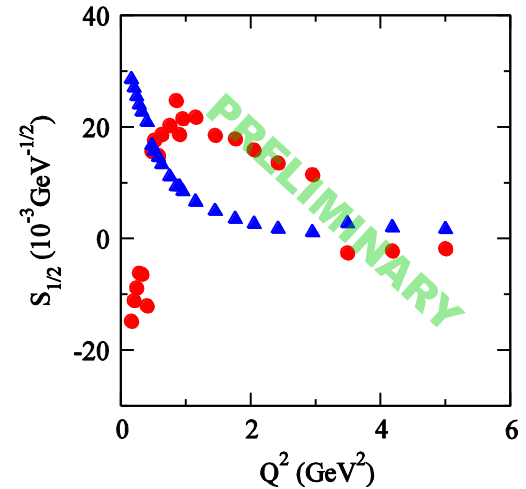
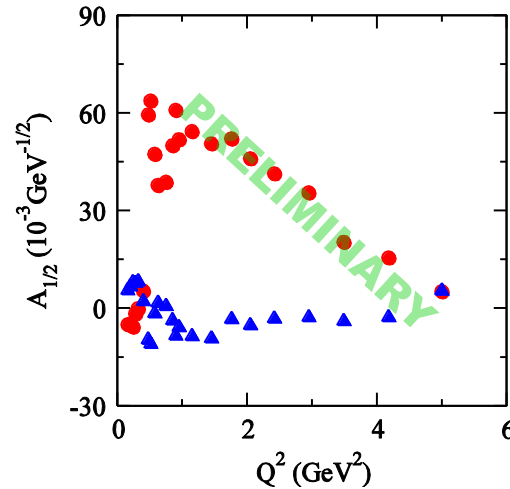
$\cos\theta$

Extracted $\gamma^{(*)}$ $p \rightarrow N^*, \Delta^*$ transition form factors at finite Q^2 (evaluated at resonance poles)

$\gamma^{(*)} p \rightarrow \Delta(1232)3/2^+$



$\gamma^{(*)} p \rightarrow N(1440)1/2^+$



Definition of $A_{1/2}$, $A_{3/2}$, $S_{1/2}$:

$$A_{3/2}(Q^2) \equiv \langle R | J_{e.m.}^\mu(Q^2) \varepsilon_\mu^{(\lambda_\gamma=+1)} | N(\lambda_N = -1/2) \rangle$$

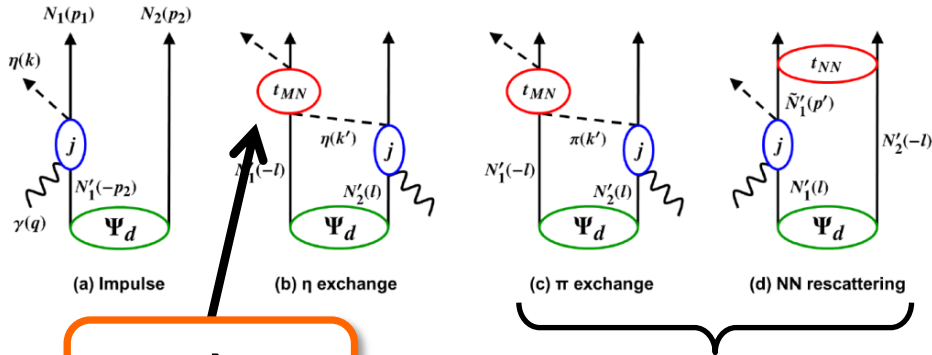
$$A_{1/2}(Q^2) \equiv \langle R | J_{e.m.}^\mu(Q^2) \varepsilon_\mu^{(\lambda_\gamma=+1)} | N(\lambda_N = +1/2) \rangle$$

$$S_{1/2}(Q^2) \equiv \langle R | J_{e.m.}^\mu(Q^2) \varepsilon_\mu^{(\lambda_\gamma=0)} | N(\lambda_N = -1/2) \rangle$$

$\gamma d \rightarrow \eta pn$ reaction: Study of ηN scattering parameters

At $E_\gamma = 940$ MeV & $\theta_p = 0$ deg. :

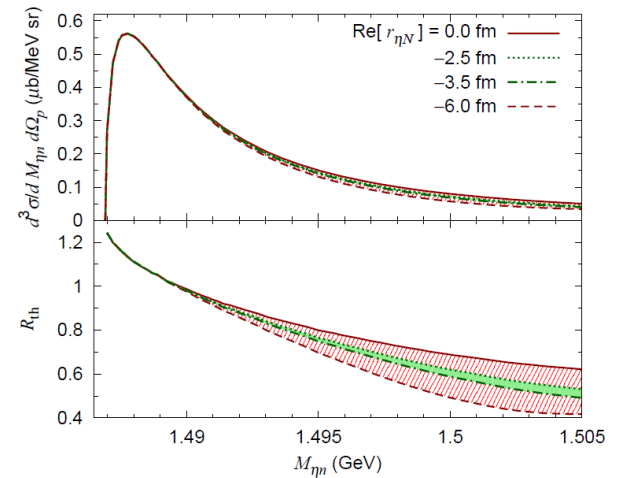
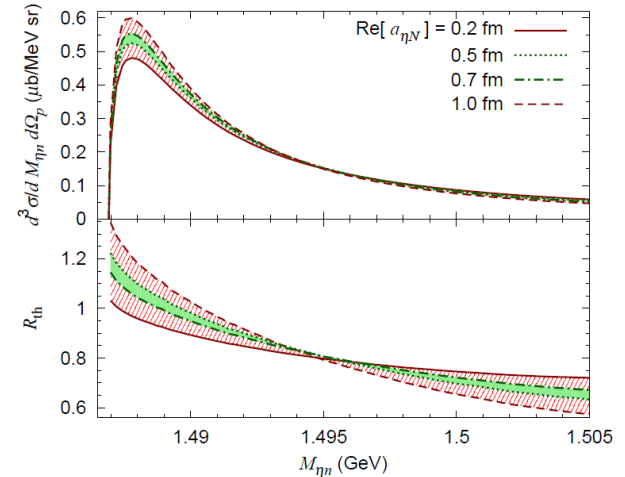
Nakamura, HK, Ishikawa, arXiv:1704.07029



$\eta n \rightarrow \eta n$
rescattering

highly suppressed !!

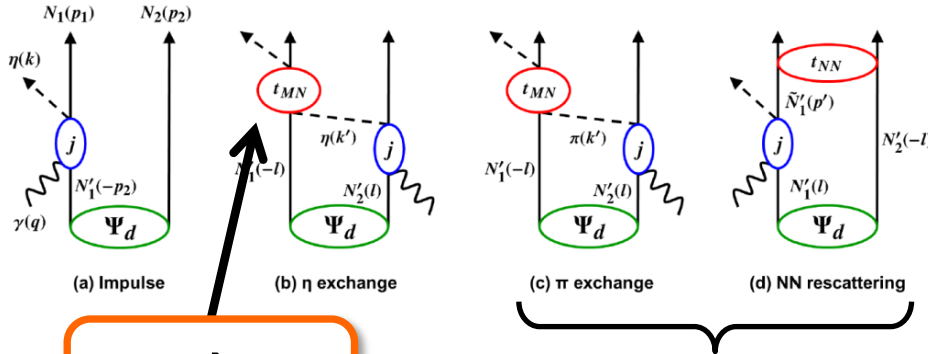
$$R = \frac{d^3 \sigma_{\text{full}} / dM_{\eta n} d\Omega_p |_{\theta_p=0^\circ}}{d^3 \sigma_{\text{imp}} / dM_{\eta n} d\Omega_p |_{\theta_p=0^\circ}}$$



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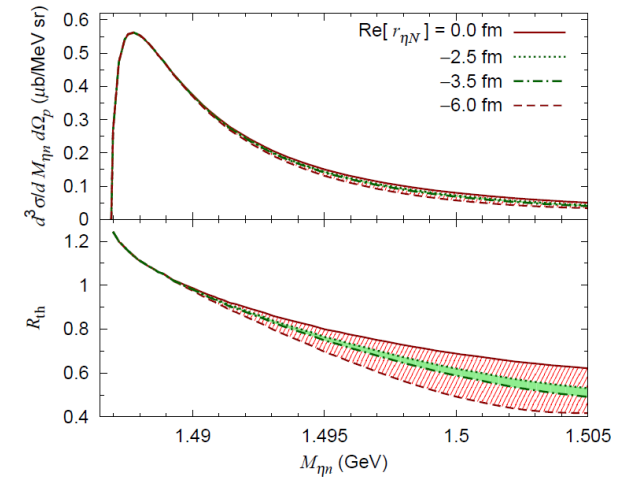
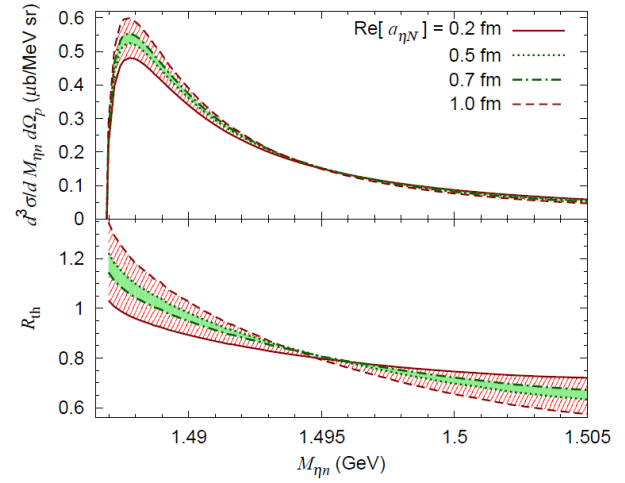
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With 5% accuracy of R (accessible with forthcoming experiment at ELPH@Tohoku U.), uncertainties in real parts of $a_{\eta n}$, $r_{\eta n}$ can be drastically reduced:

$\text{Re}[a_{\eta n}] = 0.45\text{fm} \pm 0.5\text{fm} \rightarrow \dots \pm 0.1\text{fm}$
 $\text{Re}[r_{\eta n}] = -2.5\text{fm} \pm 3.5\text{fm} \rightarrow \dots \pm 0.5\text{fm}$

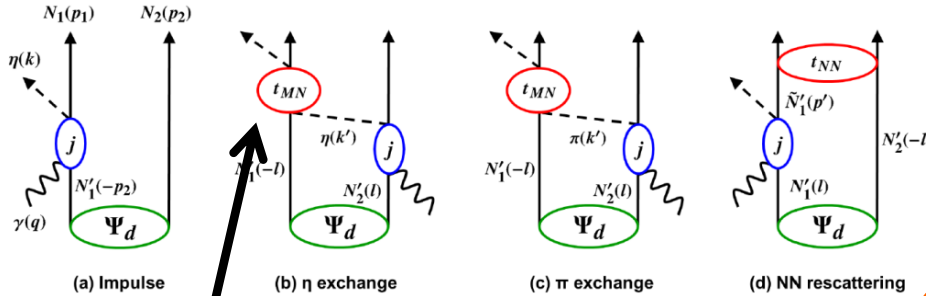
Range from previous estimations



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rescattering

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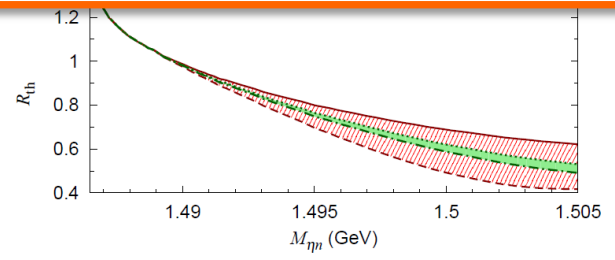
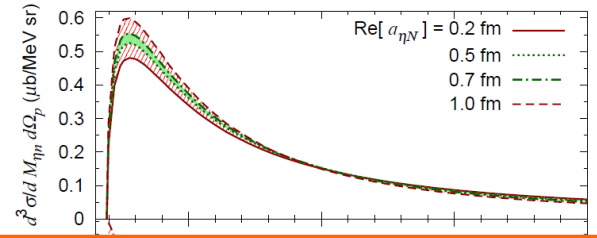
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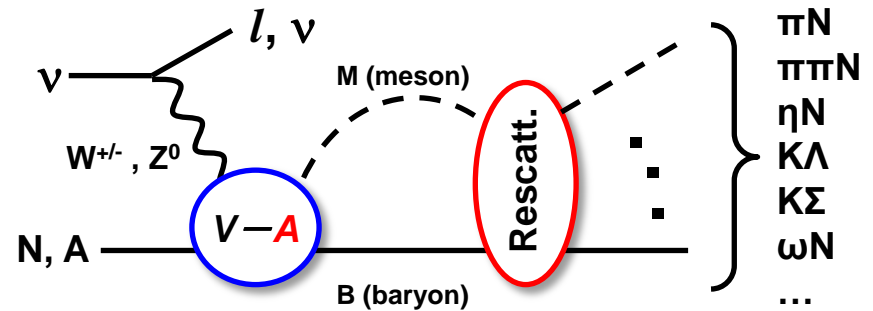
Reliable model that all the relevant subprocesses are under control is very important to have this conclusion !!



Application to neutrino-induced reactions

- ✓ **Reliable neutrino reaction model** is necessary for **precise** determination of neutrino parameters from **future neutrino-oscillation experiments** (leptonic CP phase, neutrino mass hierarchy...)

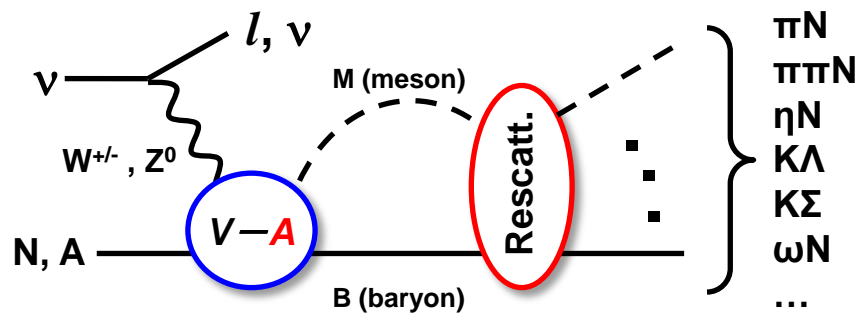
Neutrino-nucleon/nucleus reactions



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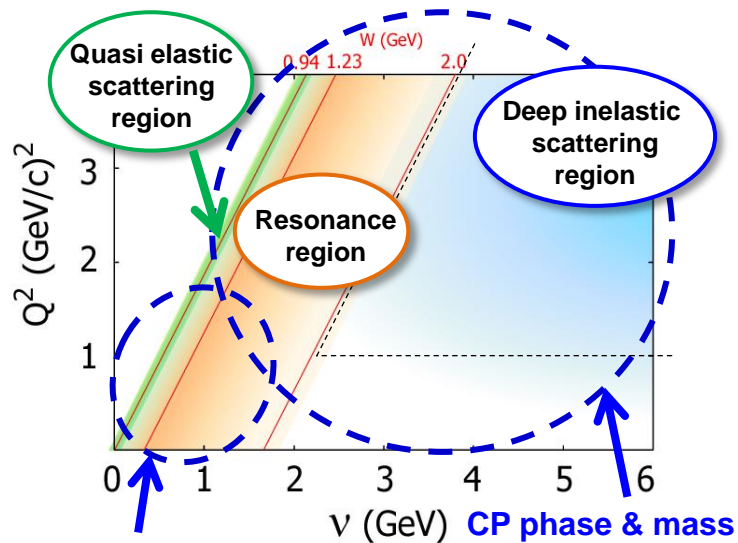
Neutrino-nucleon/nucleus reactions



Collaboration@J-PARC Branch of KEK Theory Center
<http://j-parc-th.kek.jp/html/English/e-index.html>

Y. Hayato (ICRR, U. of Tokyo), M. Hirai (Nippon Inst. Tech.)
 H. Kamano (KEK), S. Kumano (KEK)
 S. Nakamura (Cruzeiro do Sul U.),
 K. Saito (Tokyo U. of Sci.), M. Sakuda (Okayama U.),
 T. Sato (Osaka U.)

[→ **Rept. Prog. Phys. 80(2017)056301**]



T2K (long-baseline exp.)

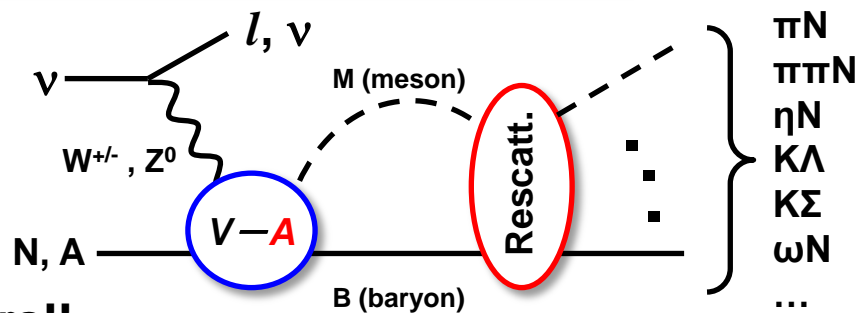
CP phase & mass hierarchy studies with atmospheric exp.

Application to neutrino-induced reactions

- ✓ **Reliable neutrino reaction model** is necessary for **precise** determination of neutrino parameters from **future neutrino-oscillation experiments** (leptonic CP phase, neutrino mass hierarchy...)

- ✓ **Can provide *axial* transition form factors!!**

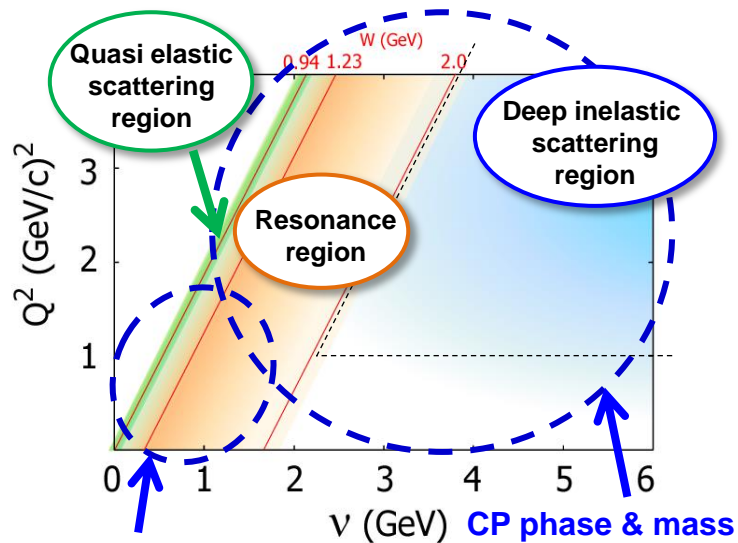
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Collaboration@J-PARC Branch of KEK Theory Center
<http://j-parc-th.kek.jp/html/English/e-index.html>

Y. Hayato (ICRR, U. of Tokyo), M. Hirai (Nippon Inst. Tech.)
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 K. Saito (Tokyo U. of Sci.), M. Sakuda (Okayama U.),
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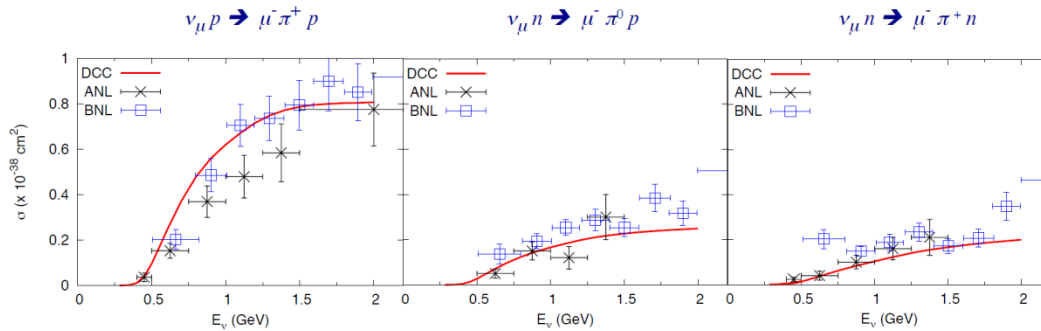
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Application to neutrino-induced reactions

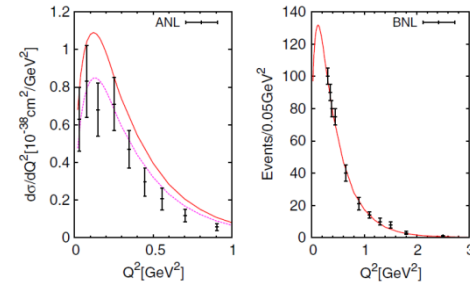
Nakamura, HK, Sato, PRD92(2015)074204

The **first-time** full coupled-channels calculation of ν -nucleon reactions **beyond the $\Delta(1232)$ region !!**

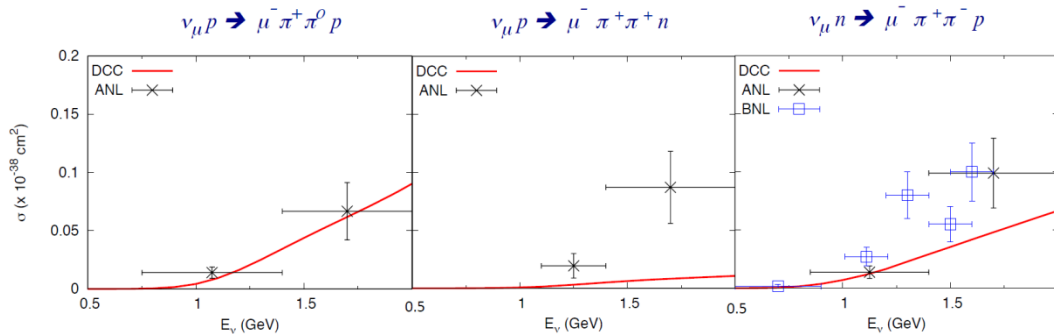
✓ Single pion production:



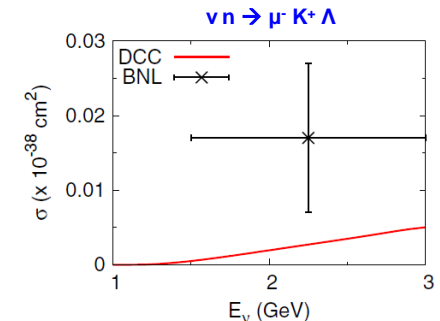
$d\sigma/dQ^2$ for $\nu p \rightarrow \mu^- \pi^+ p$
(flux averaged for E_ν)



✓ Double pion production:



✓ KΛ production:



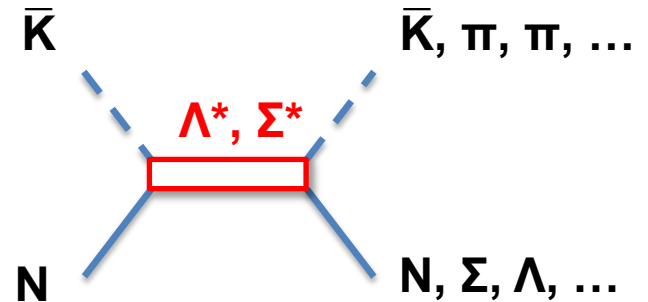
##NOTE: Q^2 dependence of all N-N* axial transition form factors are currently fixed with the nucleon dipole form factor.

ηN & $K\Sigma$ productions can also be calculated.

DCC approach to Λ^* & Σ^* spectroscopy

Recently, our DCC approach has been applied to the analysis of **K-p reactions** to establish the mass spectrum of **Y^* (= Λ^* , Σ^*) baryons with strangeness -1.**

HK, Nakamura, Lee, Sato,
PRC90(2014)065204; PRC92(2015)025205



- ✓ Taking into account $\bar{K}N, \pi\Sigma, \pi\Lambda, \eta\Lambda, K\Xi, \pi\Sigma^*(\pi\pi\Lambda), \bar{K}^*N(\pi\bar{K}N)$ channels.
- ✓ Comprehensive analysis of **ALL** available data (**more than 17,000** data points) of $K^-p \rightarrow \bar{K}N, \pi\Sigma, \pi\Lambda, \eta\Lambda, K\Xi$ up to $W = 2.1$ GeV.

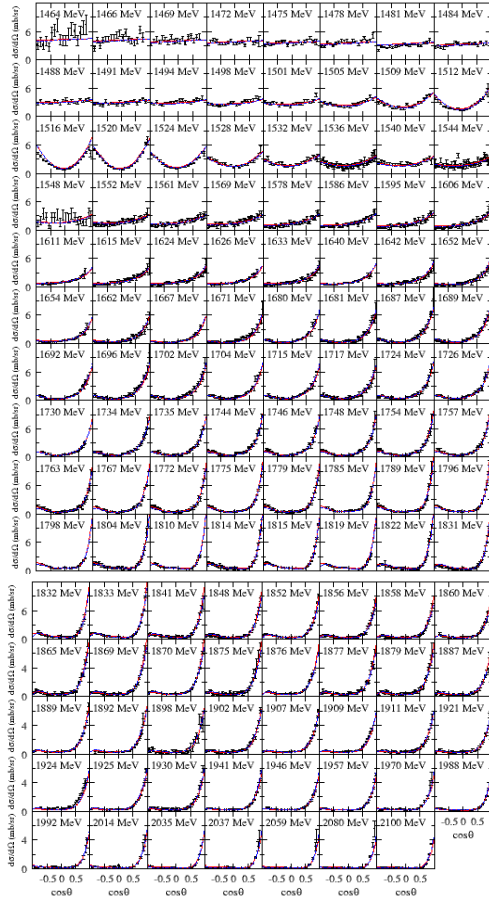


- ✓ Determination of threshold parameters (scattering lengths, effective ranges,...); the **partial-wave amplitudes** of $\bar{K}N \rightarrow \bar{K}N, \pi\Sigma, \pi\Lambda, \eta\Lambda, K\Xi$ for **S, P, D, and F waves.**
- ✓ Extraction of **Y^* resonance parameters** (mass, width, couplings, ...) defined by **poles of scattering amplitudes.**

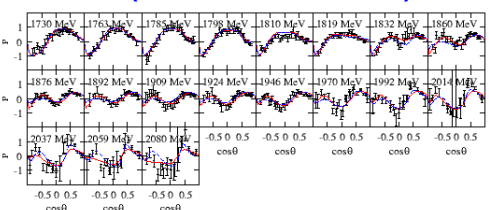
Selected results of the fits

HK, Nakamura, Lee, Sato, PRC90(2014)065204

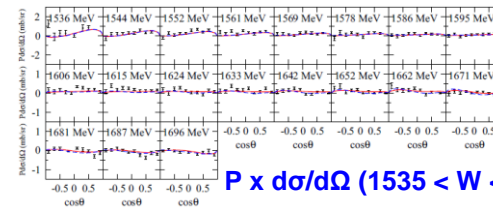
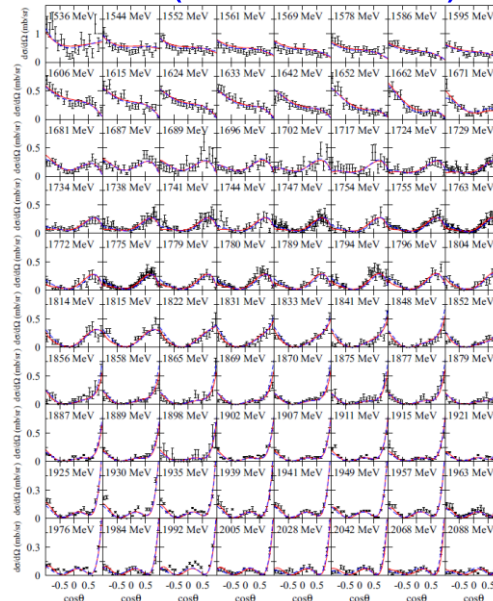
$K^- p \rightarrow K^- p$
 $d\sigma/d\Omega$ ($1464 < W < 2100$ MeV)



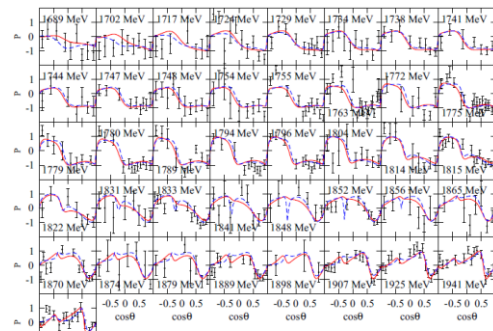
P ($1730 < W < 2080$ MeV)



$K^- p \rightarrow \pi^+ \Sigma^+$
 $d\sigma/d\Omega$ ($1536 < W < 2088$ MeV)

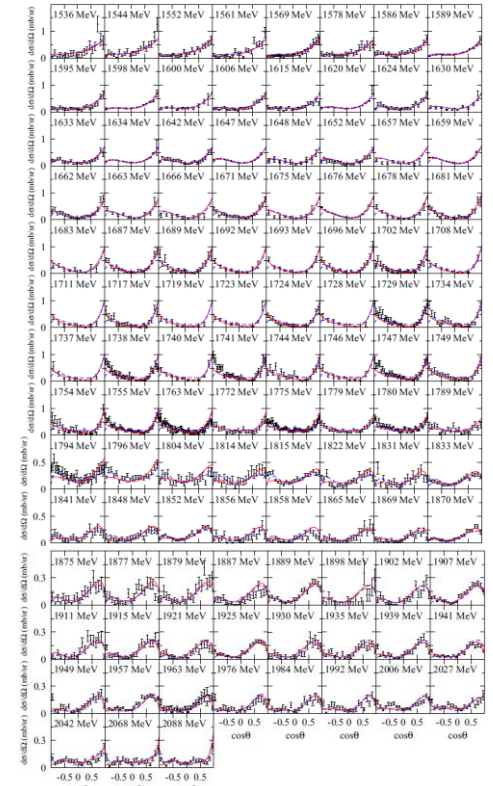


$P \times d\sigma/d\Omega$ ($1535 < W < 1696$ MeV)

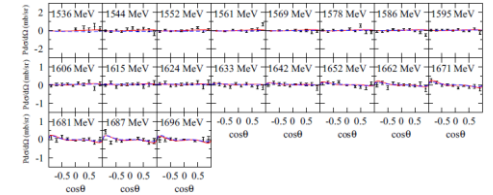


P ($1689 < W < 1957$ MeV)

$K^- p \rightarrow \pi^0 \Lambda$
 $d\sigma/d\Omega$ ($1536 < W < 2088$ MeV)



$P \times d\sigma/d\Omega$ ($1536 < W < 1696$ MeV)



Red curve: Model A
Blue curve: Model B

Λ^* and Σ^* mass spectrum extracted from the K^-p reaction data

HK, Nakamura, Lee, Sato, PRC92(2015)025205

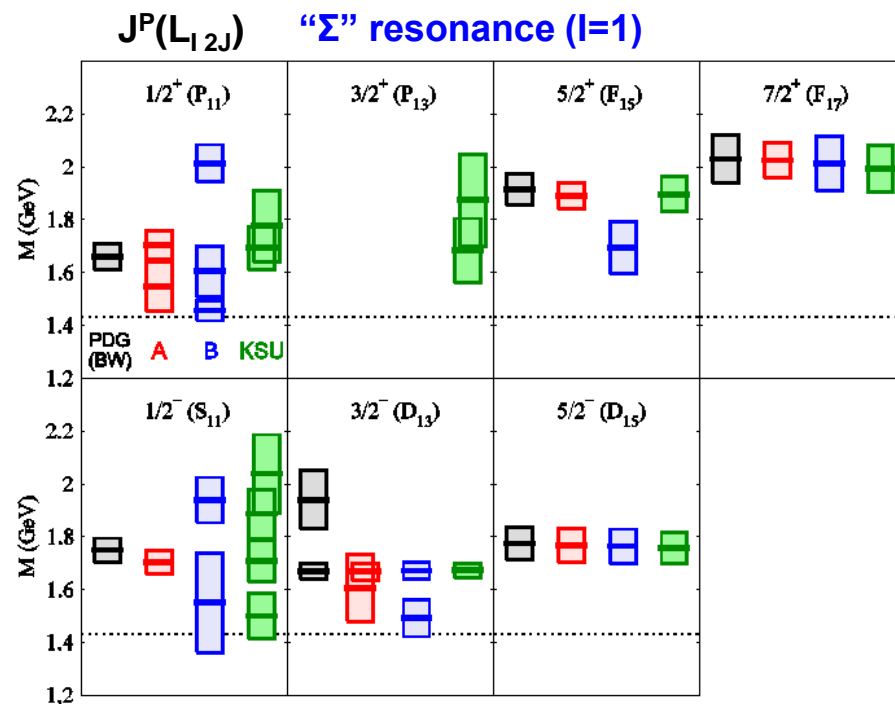
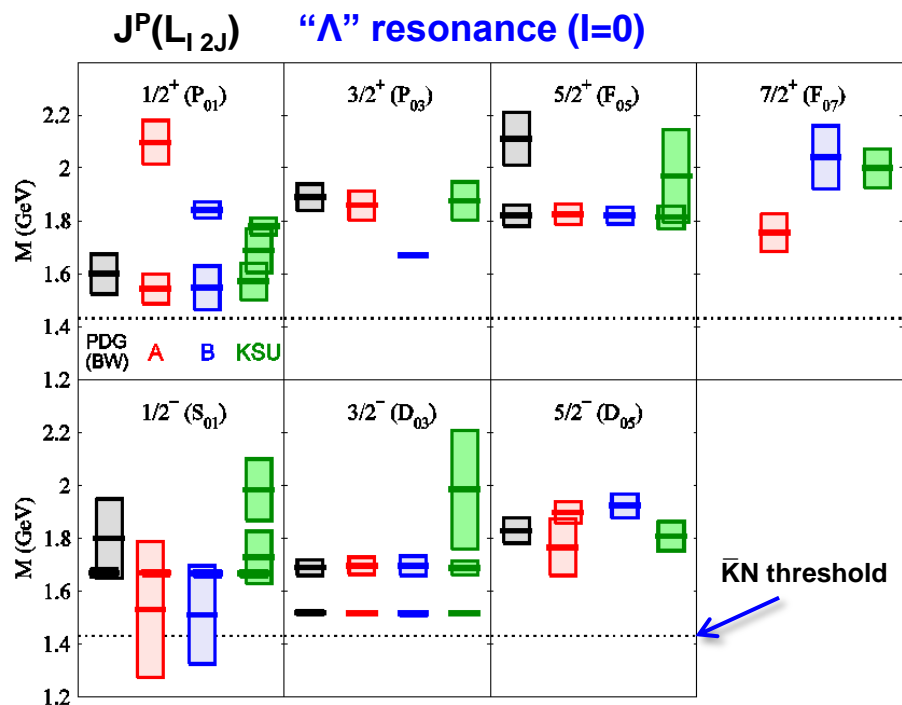
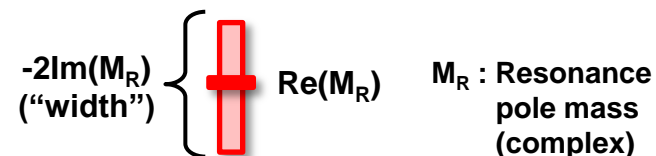
Spectrum for Y^* resonances found above the $\bar{K}N$ threshold

Red: Model A

Blue: Model B

Green: KSU[PRC88(2013)035205]

Black: PDG (only 4- & 3-star Y^* ;
Breit-Wigner)



Λ^* and Σ^* mass spectrum extracted from the K^-p reaction data

HK, Nakamura, Lee, Sato, PRC92(2015)025205

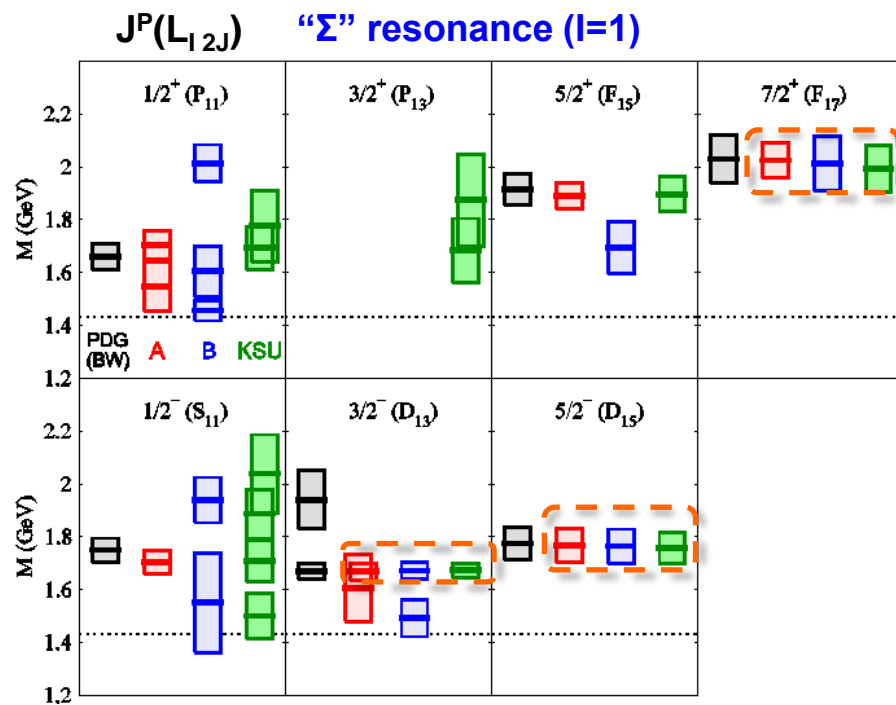
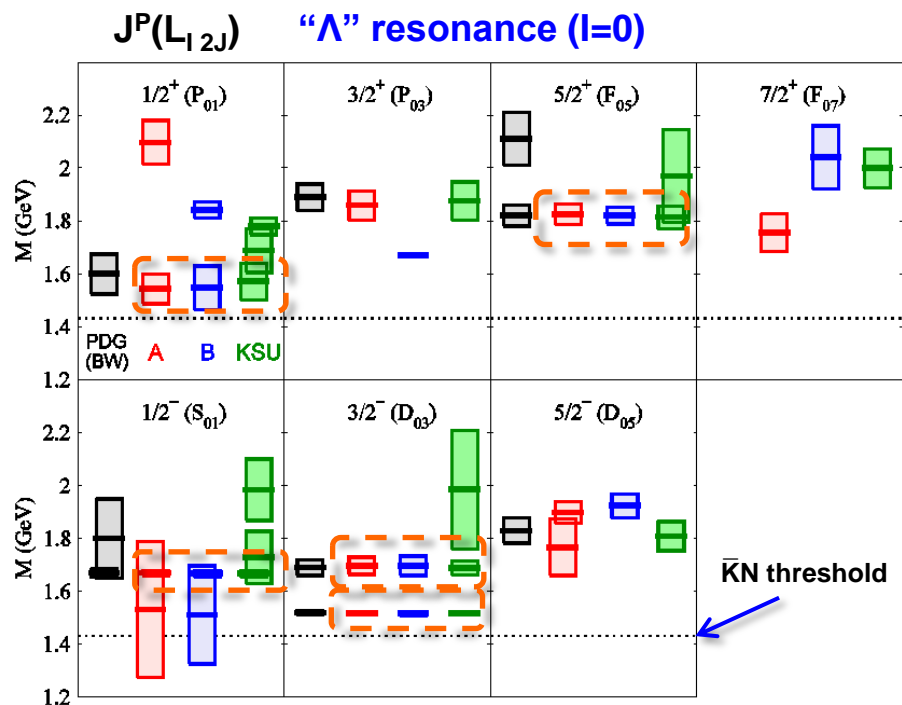
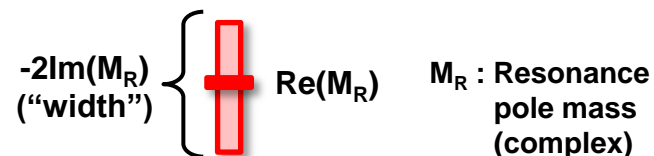
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Λ^* and Σ^* mass spectrum extracted from the K^-p reaction data

HK, Nakamura, Lee, Sato, PRC92(2015)025205

Spectrum for Y^* resonances found above the $\bar{K}N$ threshold

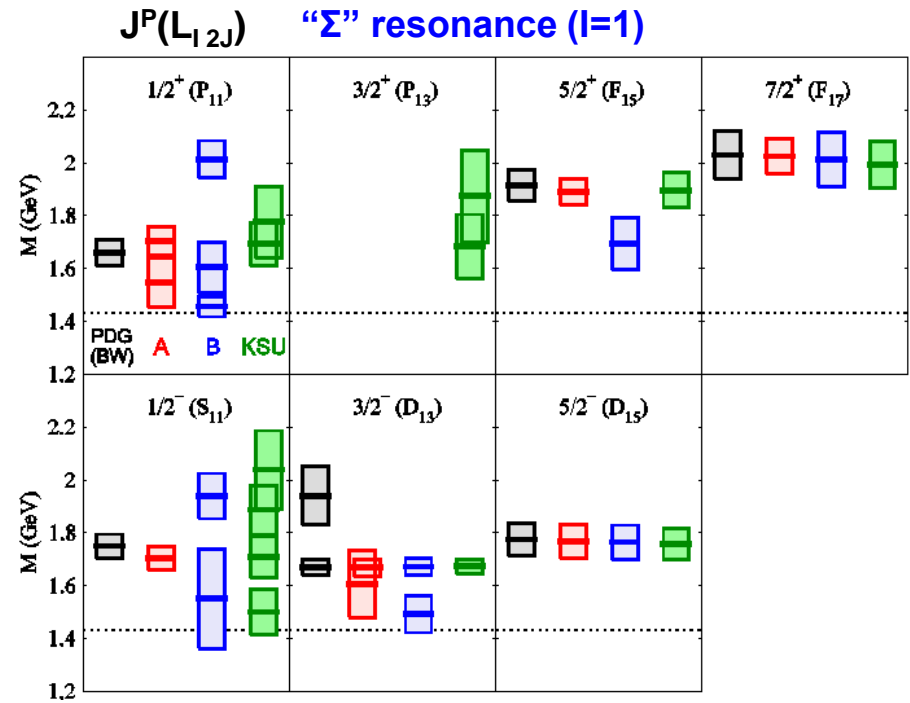
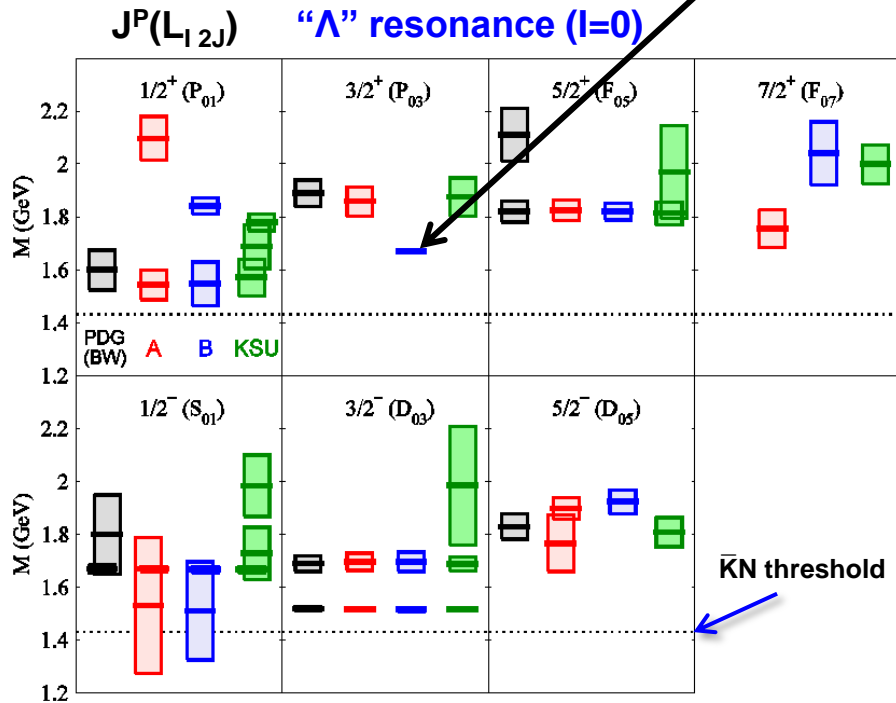
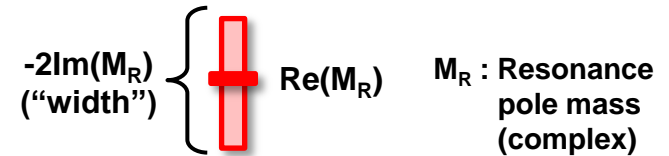
Red: Model A

Blue: Model B

Green: KSU[PRC88(2013)035205]

Black: PDG (only 4- & 3-star Y^* ; Breit-Wigner)

New narrow $3/2^+$ resonance
 $M = 1671 - 5i$ MeV
 near the $\eta\Lambda$ threshold !!



Λ^* and Σ^* mass spectrum extracted from the K^-p reaction data

HK, Nakamura, Lee, Sato, PRC92(2015)025205

Spectrum for Y^* resonances found above the $\bar{K}N$ threshold

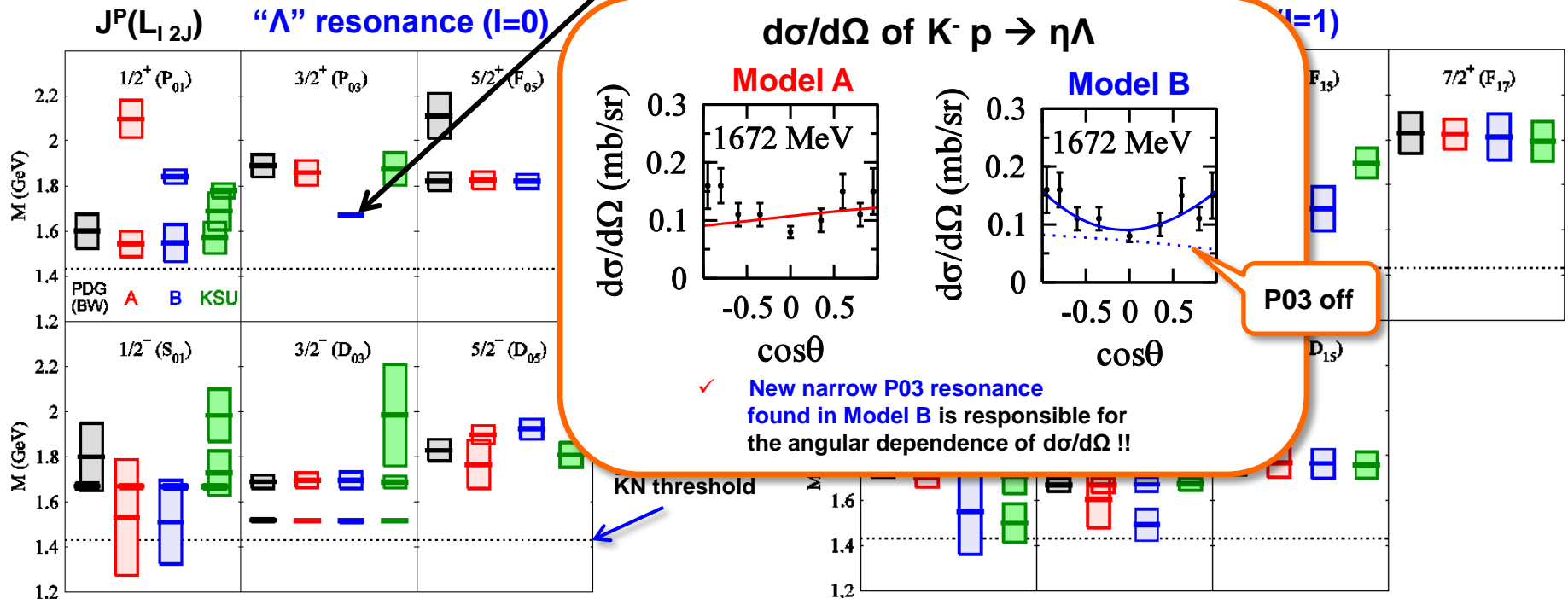
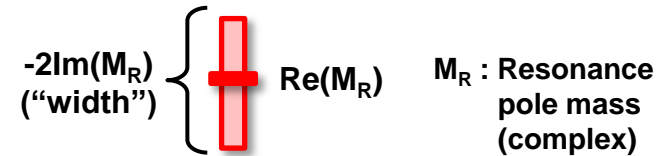
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Spectrum for Y^* resonances found above the $\bar{K}N$ threshold

Red: Model A

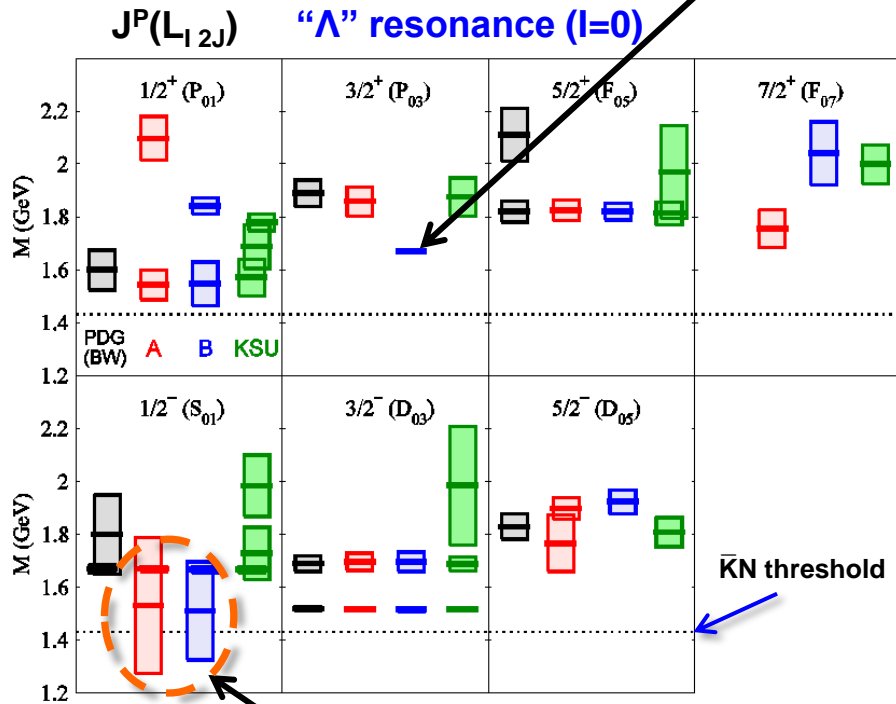
Blue: Model B

Green: KSU[PRC88(2013)035205]

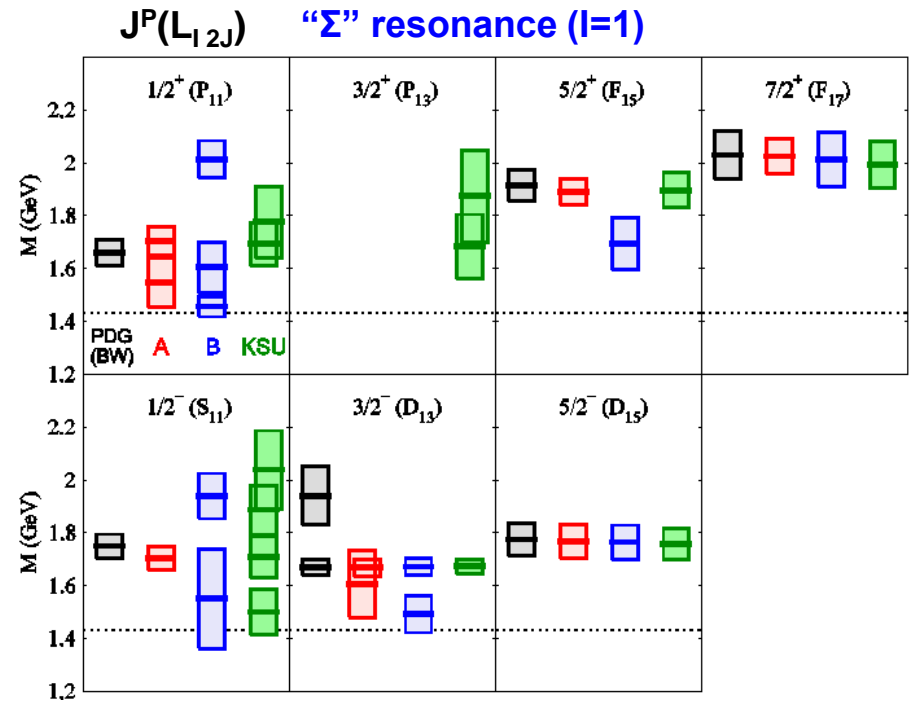
Black: PDG (only 4- & 3-star Y^* ;
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New narrow $3/2^+$ resonance
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near the $\eta\Lambda$ threshold !!

$-2\text{Im}(M_R)$ ("width")
 $\left\{ \begin{array}{l} \text{Red box} \\ \text{Blue box} \end{array} \right.$ $\text{Re}(M_R)$ M_R : Resonance pole mass (complex)



Spin partner of $\Lambda(1520)3/2^-$??



Λ^* and Σ^* mass spectrum extracted from the K^-p reaction data

HK, Nakamura, Lee, Sato, PRC92(2015)025205

Spectrum for Y^* resonances found above the $\bar{K}N$ threshold

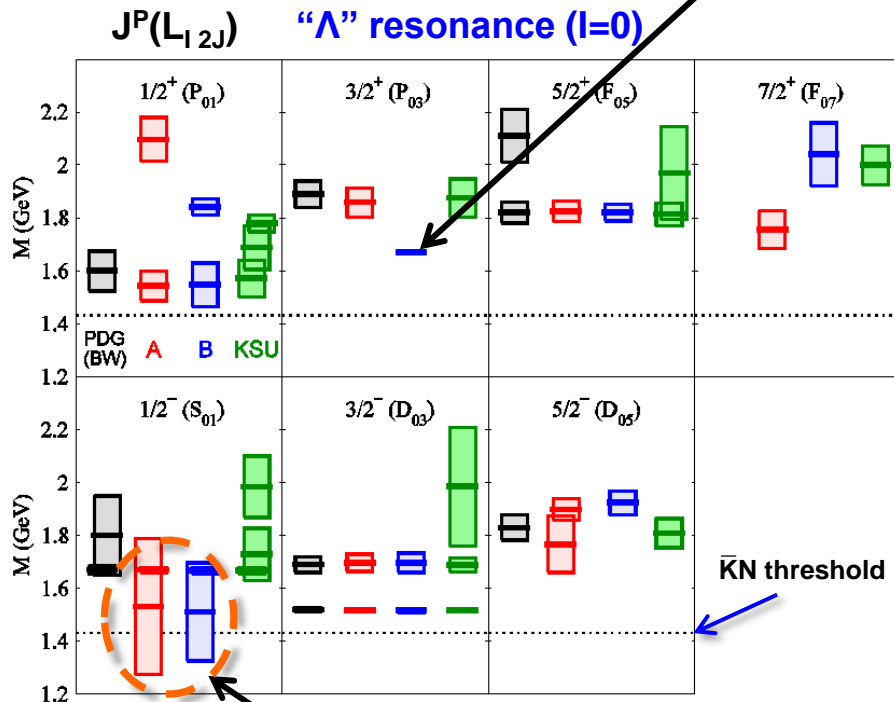
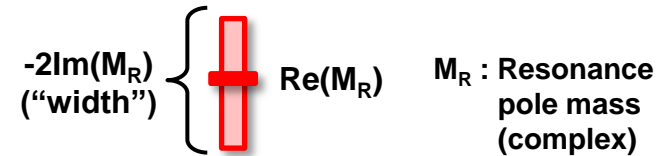
Red: Model A

Blue: Model B

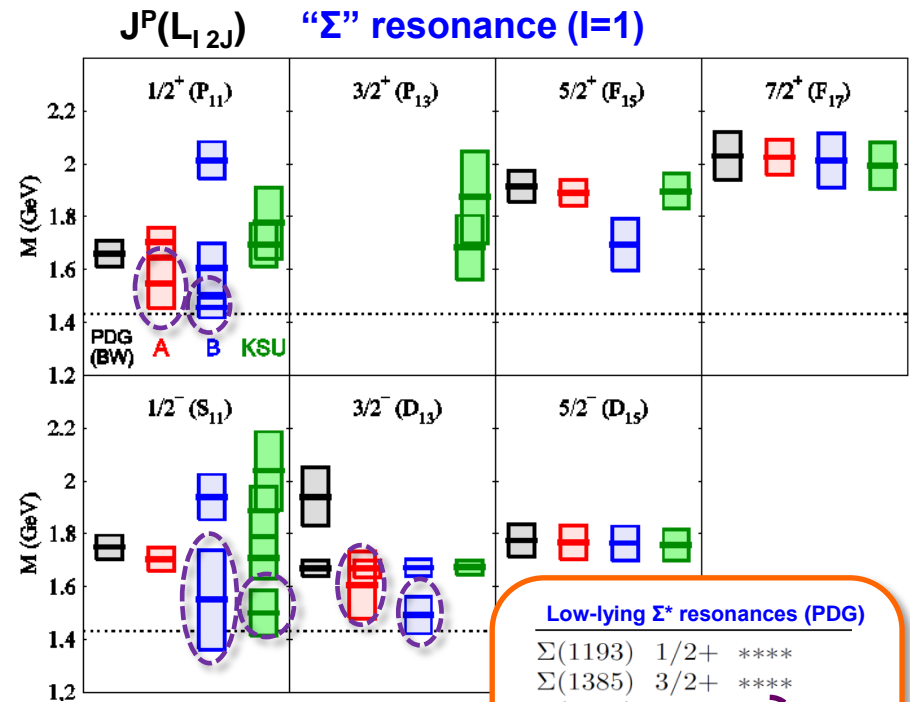
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New narrow $3/2^+$ resonance
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Spin partner of $\Lambda(1520)3/2^-$??



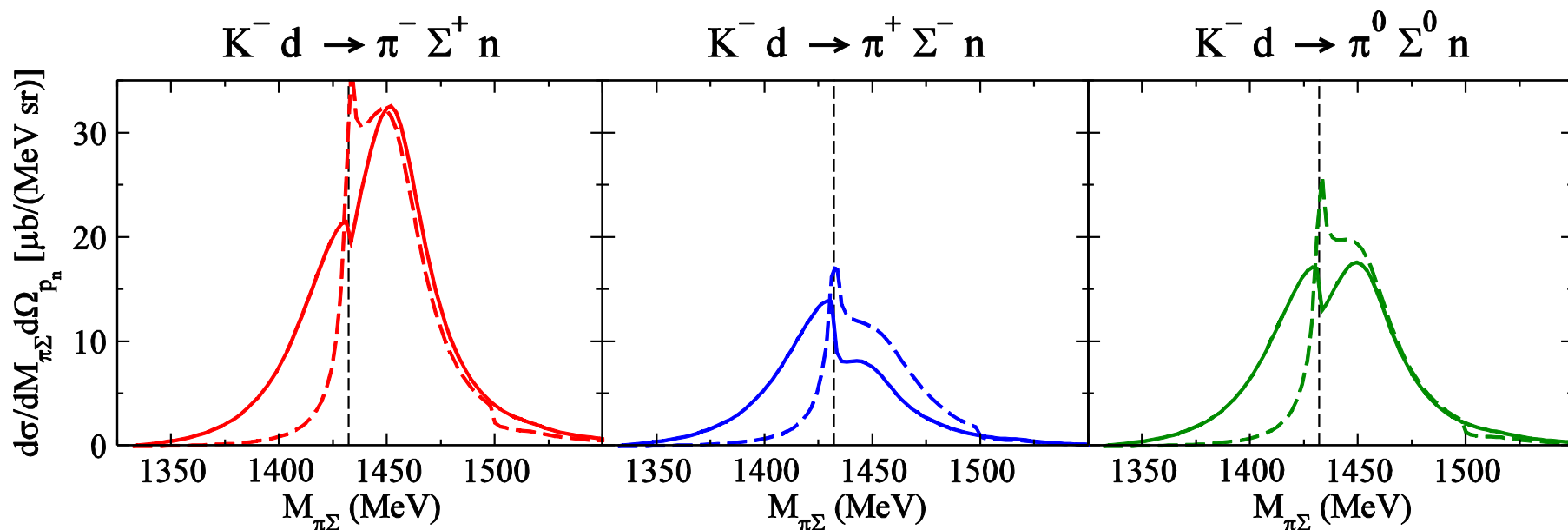
Low-lying Σ^* resonances (PDG)

$\Sigma(1193)$	$1/2^+$	****
$\Sigma(1385)$	$3/2^+$	****
$\Sigma(1480)$		*
$\Sigma(1560)$		**
$\Sigma(1580)$	$3/2^-$	*
$\Sigma(1620)$	$1/2^-$	**
$\Sigma(1660)$	$1/2^+$	***
$\Sigma(1670)$	$3/2^-$	****

$K^- d \rightarrow (\pi\Sigma)_0 n$ reaction: Study of $\Lambda(1405)$ & other low-lying Y^* resonances

HK, Lee, PRC94(2016)015201

$p_{K^-} = 1 \text{ GeV}, \theta_n = 0 \text{ deg.}$



— Full (Model B for $\bar{K}N$ processes)

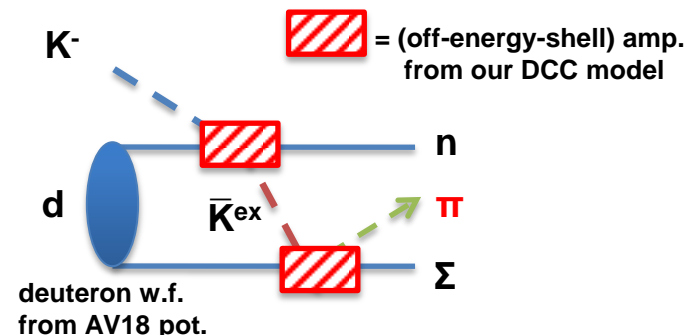
- - - w/o $J^P=1/2^- \Lambda$ resonant amplitude in $\bar{K}^{ex}N \rightarrow \pi\Sigma$

Model B predicts two $J^P=1/2^- \Lambda$ resonances below $\bar{K}N$ threshold:
[PRC92(2015)025205]

$M_R = 1428 - i31 \text{ MeV} \leftarrow$ corresponding to $\Lambda(1405)$

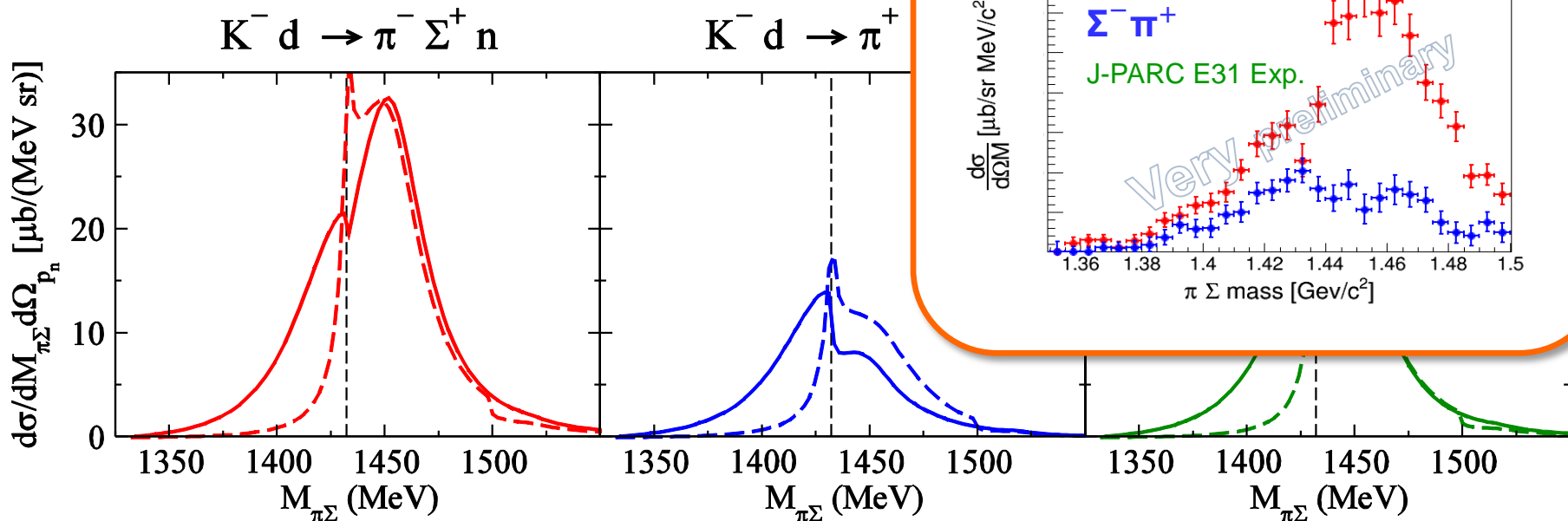
$M_R = 1397 - i98 \text{ MeV}$

“ \bar{K} -exchange” term

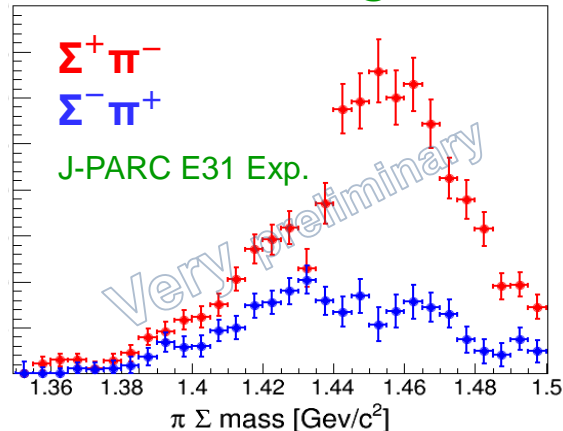


$K^- d \rightarrow (\pi\Sigma)_0 n$ reaction: Study of $\Lambda(1405)$ & other low-lying Y^* resonances

$p_{K^-} = 1 \text{ GeV}, \theta_n = \dots$



Kawasaki-san's talk@MENU2016



— Full (Model B for $\bar{K}N$ processes)

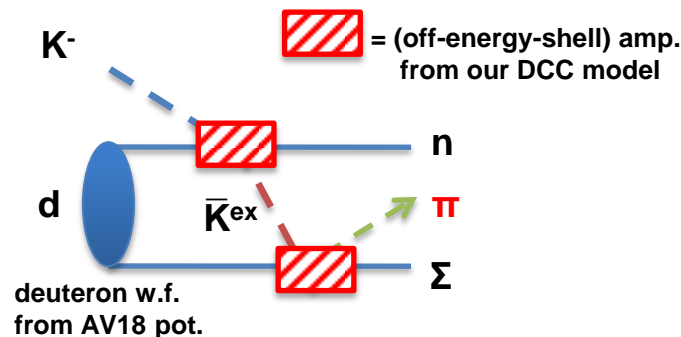
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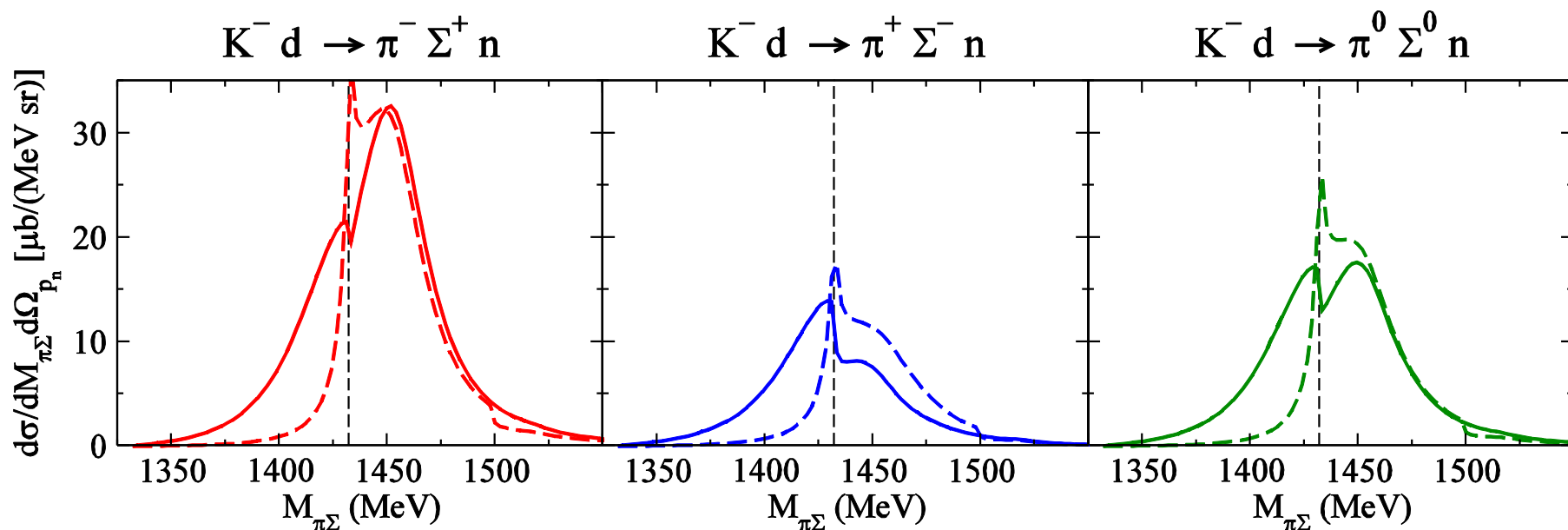
“ \bar{K} -exchange” term



$K^- d \rightarrow (\pi\Sigma)_0 n$ reaction: Study of $\Lambda(1405)$ & other low-lying Y^* resonances

HK, Lee, PRC94(2016)015201

$p_{K^-} = 1 \text{ GeV}, \theta_n = 0 \text{ deg.}$



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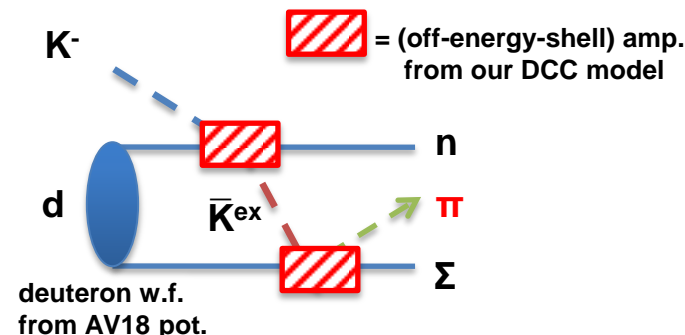
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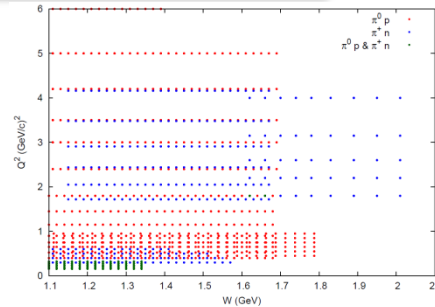
“ \bar{K} -exchange” term



Prospects for studies of baryon transition form factors

N^* & Δ^* e.m. transition form factors ($Q^2 > 0$)

CLAS database for
 1π electroproductions
($Q^2 < 6 \text{ GeV}^2$, $W < 2 \text{ GeV}$)
[ongoing]

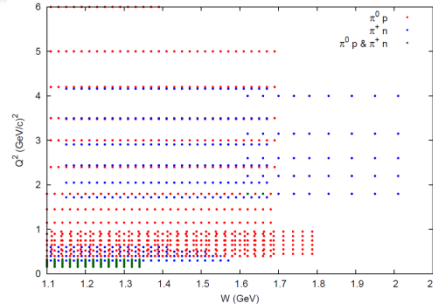


+ $K^+\Lambda$, $K^+\Sigma^0$ electroproduction data
($Q^2=0.65-2.55 \text{ GeV}^2$, $W=1.65-2.25 \text{ GeV}$)

Prospects for studies of baryon transition form factors

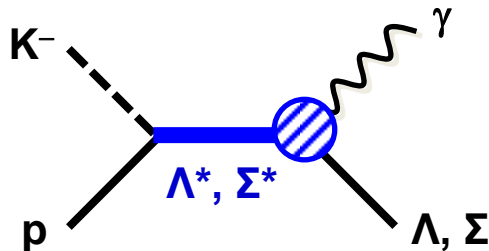
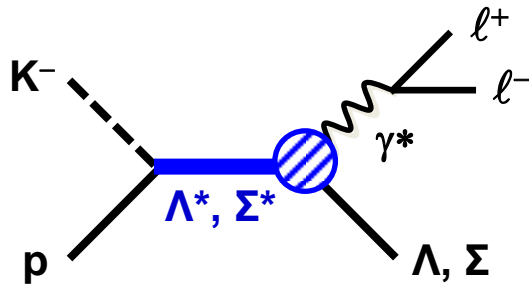
N^* & Δ^* e.m. transition form factors ($Q^2 > 0$)

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[ongoing]



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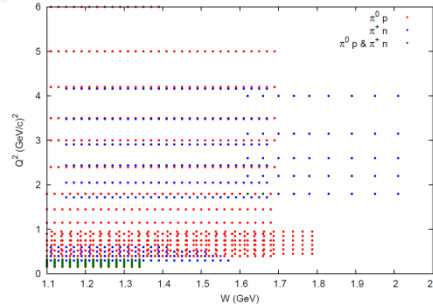
Λ^* & Σ^* e.m. transition form factors ($Q^2 < 0$, $Q^2 = 0$)



Prospects for studies of baryon transition form factors

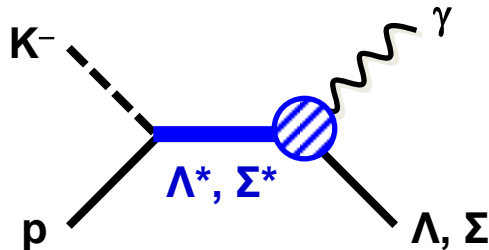
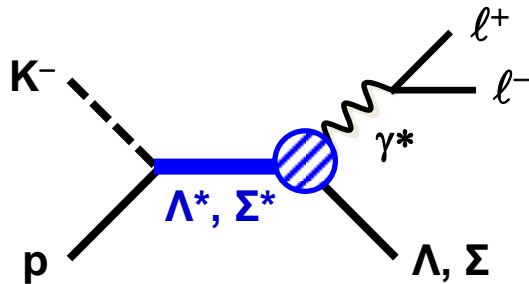
N^* & Δ^* e.m. transition form factors ($Q^2 > 0$)

CLAS database for 1π electroproductions ($Q^2 < 6 \text{ GeV}^2, W < 2 \text{ GeV}$) [ongoing]



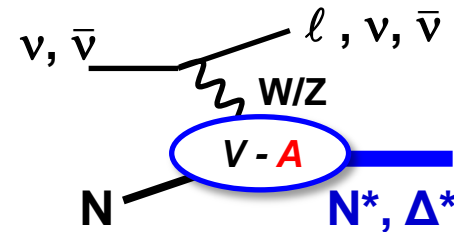
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Λ^* & Σ^* e.m. transition form factors ($Q^2 < 0, Q^2 = 0$)

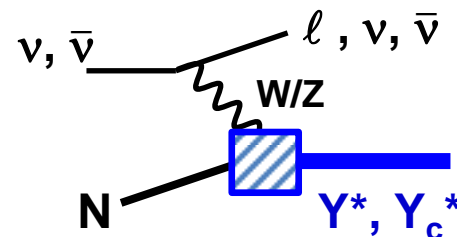


WEAK current transition form factors ($Q^2 < 0$)

✓ Axial transition form factors



✓ $|\Delta S|=1(u \rightarrow s), |\Delta C|=1(d \rightarrow c)$ transition form factors



Thank you for your attention !!

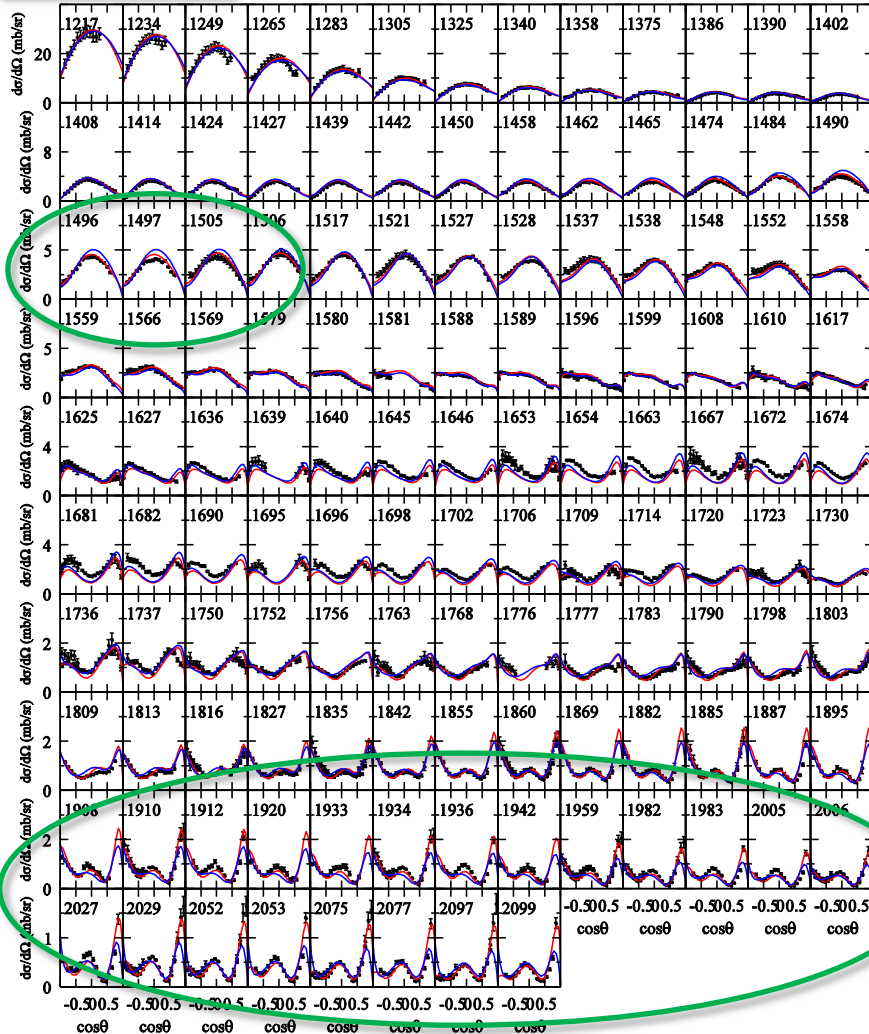
Back up

ANL-Osaka DCC approach to N^* & Δ^*

HK, Nakamura, Lee, Sato, PRC94(2016)015201; PRC88(2013)035209

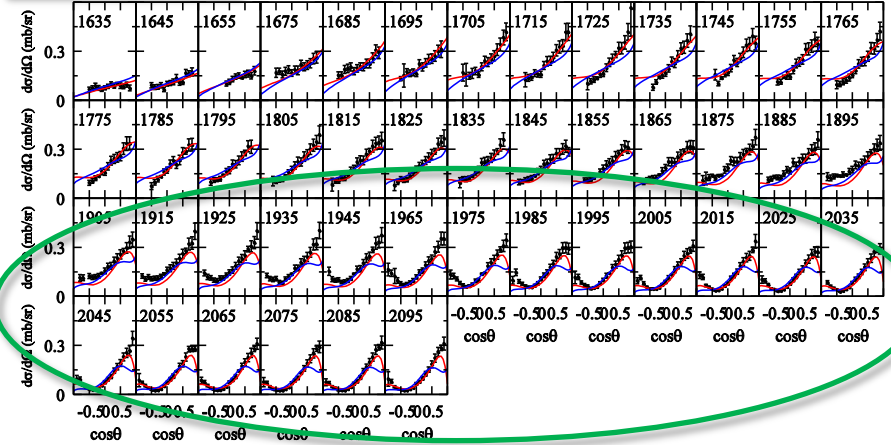
$\gamma p \rightarrow \pi^0 p$

$d\sigma/d\Omega$ for $W < 2.1$ GeV



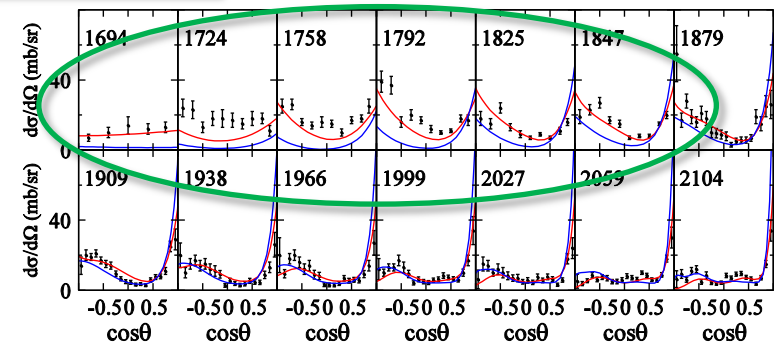
$\gamma p \rightarrow K^+ \Lambda$

$d\sigma/d\Omega$ for $W < 2.1$ GeV



$\pi^+ p \rightarrow K^0 \Sigma^0$

$d\sigma/d\Omega$ for $W < 2.1$ GeV




Red: PRC94(2016)015201(updated ver.)

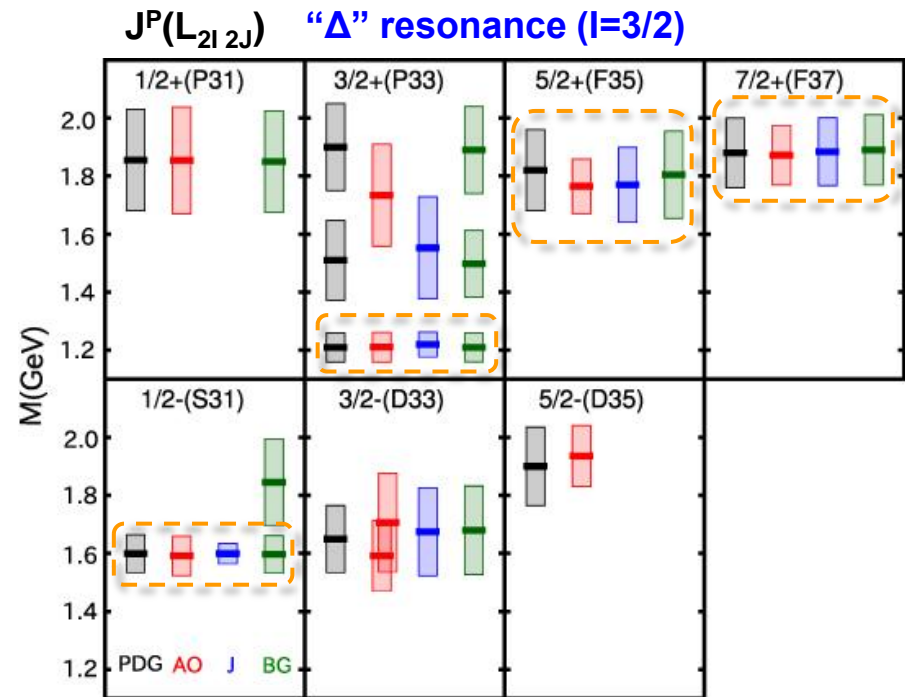
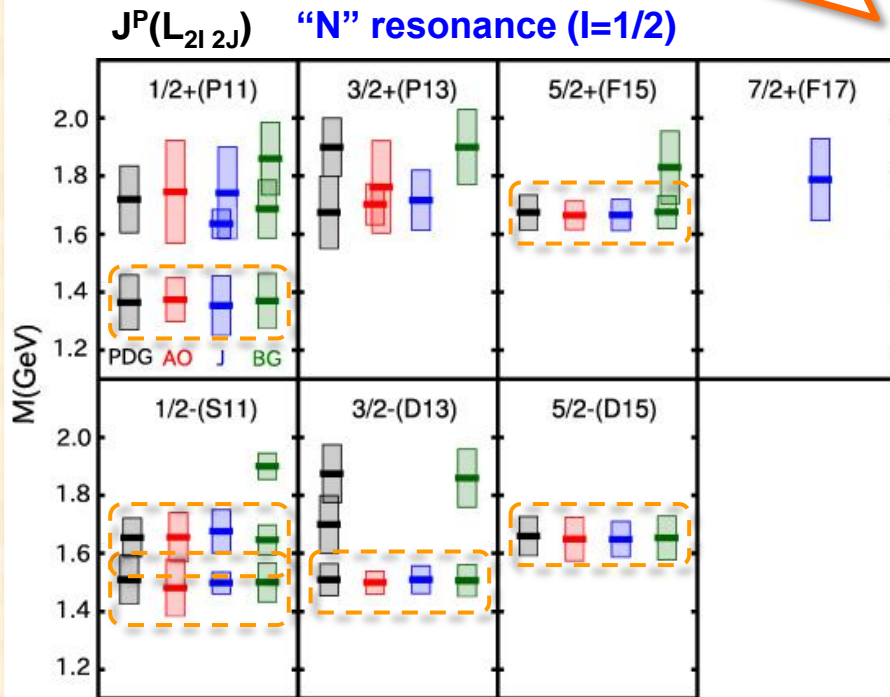
Blue: PRC88(2013)035209

Comparison of N^* & Δ^* spectrum between multichannel analyses

HK, Nakamura, Lee, Sato, PRC88 (2013) 035209

Spectrum for low-lying states with $\text{Re}(M_R) < 1.6$ GeV is now well established !!
(One exception is 2nd P33, Roper-like state of Δ)

$-2\text{Im}(M_R)$ ("width")  $\text{Re}(M_R)$ M_R : Resonance pole mass (complex)



PDG: 4* & 3* states assigned by PDG2012

J : Juelich [DCC, EPJA49(2013)44]

AO : ANL-Osaka (DCC)

BG : Bonn-Gatchina [on-shell K-matrix, EPJA48(2012)5]

Extracted scattering lengths and effective ranges

HK, Nakamura, Lee, Sato, PRC90(2014)065204

Scattering length and effective range

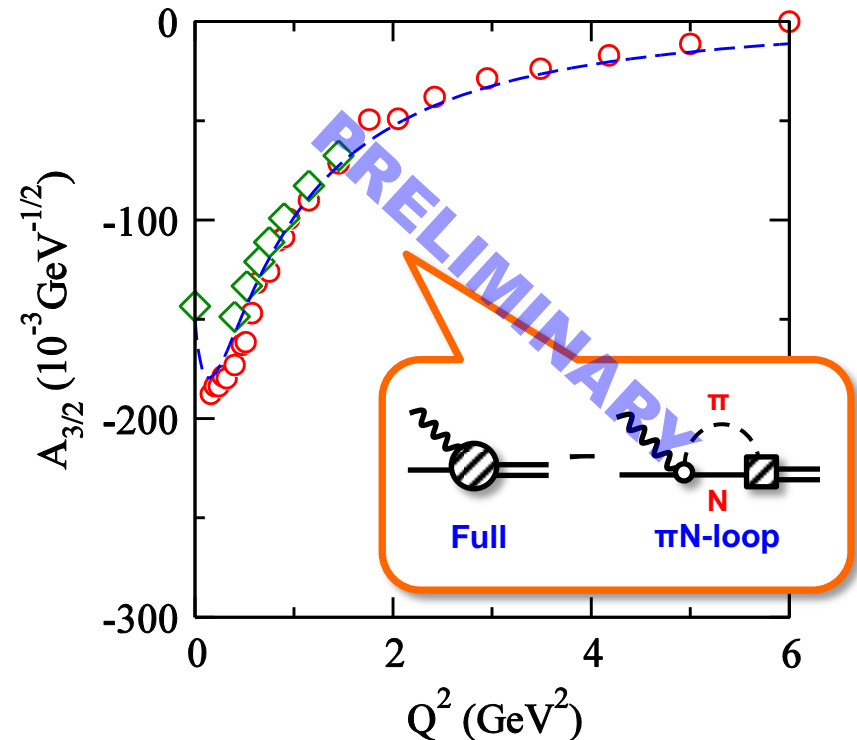
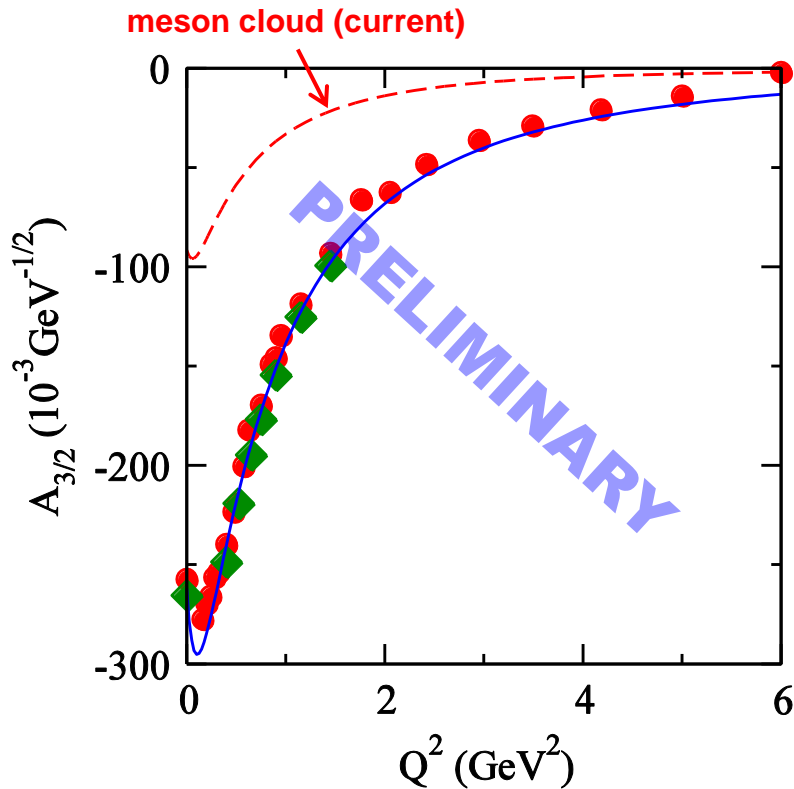
	Model A		Model B	
	$I = 0$	$I = 1$	$I = 0$	$I = 1$
$a_{\bar{K}N}$ (fm)	$-1.37 + i0.67$	$0.07 + i0.81$	$-1.62 + i1.02$	$0.33 + i0.49$
$a_{\eta\Lambda}$ (fm)	$1.35 + i0.36$	-	$0.97 + i0.51$	-
$a_{K\Xi}$ (fm)	$-0.81 + i0.14$	$-0.68 + i0.09$	$-0.89 + i0.13$	$-0.83 + i0.03$
$r_{\bar{K}N}$ (fm)	$0.67 - i0.25$	$1.01 - i0.20$	$0.74 - i0.25$	$-1.03 + i0.19$
$r_{\eta\Lambda}$ (fm)	$-5.67 - i2.24$	-	$-5.82 - i3.32$	-
$r_{K\Xi}$ (fm)	$-0.01 - i0.33$	$-0.42 - i0.49$	$0.13 - i0.20$	$-0.22 - i0.11$

$$a_{K-p} = -0.65 + i0.74 \text{ fm (Model A)}$$

$$a_{K-p} = -0.65 + i0.76 \text{ fm (Model B)}$$

Extracted e.m. transition form factors

- ✓ $N \rightarrow$ "1st P33($J^P=3/2^+$) Δ " transition form factor $A_{3/2}$
[evaluated at Δ pole mass: $M_R = 1210 - i 50$ MeV]



- Current** = $\pi N, \pi\pi N, \eta N, K\Lambda, K\Sigma$; 2 bare states in P33
- JLMS** = $\pi N, \pi\pi N, \eta N$; 2 bare states in P33
[PRC80(2009)025207; 82(2010)045206]
- Sato-Lee** = πN ; 1 bare state in P33
[PRC63(2001)055201; 75(2007)015205]